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# *Hard exclusive electroproduction of vector mesons at HERMES*

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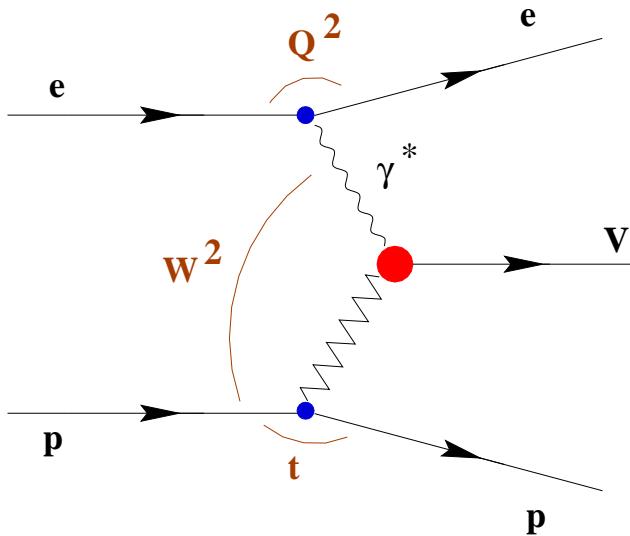
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on behalf of HERMES Collaboration

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- Basics
  - Spin Density Matrix Elements (SDMEs) : definitions and their determination
  - The observables derived :
    - SDME's for  $\phi$  and  $\rho^0$  vector mesons
    - Dependences of SDME's on  $Q^2$  and  $t'$
    - $R = \frac{\sigma_L}{\sigma_T}$
    - the signatures of the Natural or Unnatural Parity Exchange amplitudes
  - Ratio of Helicity Amplitudes for Exclusive  $\rho^0$
  - The Transverse Target Spin Asymmetry -  $A_{UT}$
  - Conclusions

# $e + p \rightarrow e' + p' + V$ : **Basics**



## Kinematics:

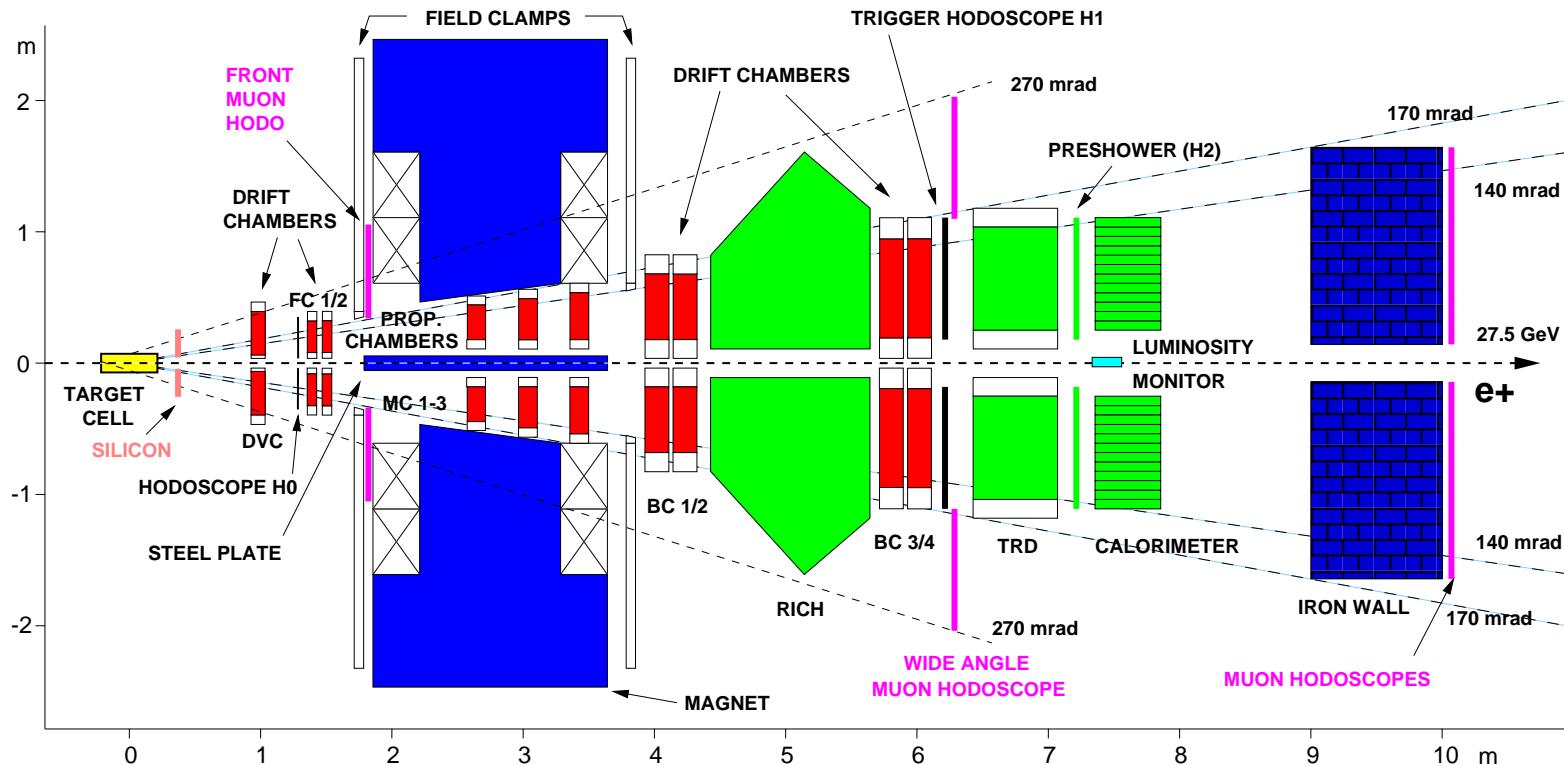
- $\nu = 3.5 \div 24 \text{ GeV}$ ,
- $Q^2 = 1.0 \div 7.0 \text{ GeV}^2$ ,
- $W = 3.0 \div 6.5 \text{ GeV}$ ,
- $x_{Bj} = 0.01 \div 0.35$ ,
- $-t' = (t - t_{min})$
- $-t' = 0 \div 0.4 \text{ GeV}^2$ ,

- In the one photon approximation  
 $\equiv \gamma^* + p \rightarrow p' + V$
- The amplitude of this process can be factorized:  
 $A = \Phi_{\gamma^* \rightarrow q\bar{q}}^* \otimes A_{q\bar{q} + p \rightarrow q\bar{q} + p} \otimes \Phi_{q\bar{q} \rightarrow V}$ .  
 In these three steps the interaction time of ( $q\bar{q}$ ) with target is shorter than the time of  $\gamma^*$  fluctuation and formation of VM.  
 (Collins, Frankfurt and Strikman Phys.Rev D56(1997)2982)
- $\gamma^* + N \rightarrow V + N'$  is a good tool to study the helicity conservation:
  - helicity state of  $\gamma^*$  is easy to determine (QED)
  - helicity of VM from angular distributions of decay products:  
 $\phi \rightarrow K^+ K^-$  and  $\rho^0 \rightarrow \pi^+ \pi^-$

# *Spin Density Matrix Elements (SDMEs)*

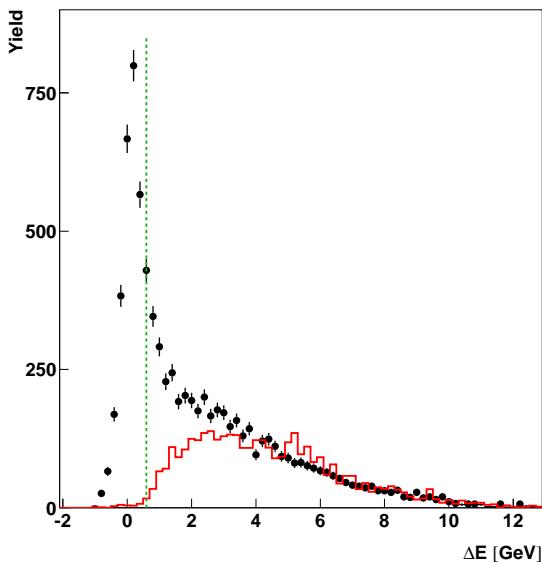
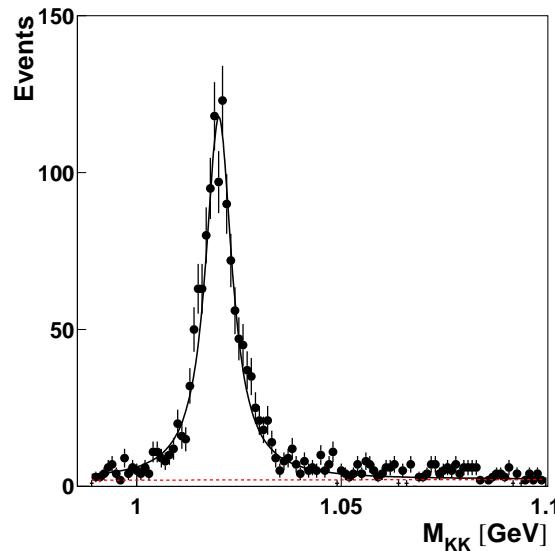
- SDMEs:  $r_{\lambda_V \lambda'_V}^{\alpha} \sim \rho(V) = \frac{1}{N} \sum_{\lambda'_\gamma, \lambda_\gamma} (T_{\lambda_V \lambda_\gamma} \rho(\gamma) T_{\lambda'_V \lambda'_\gamma}^+)$   
 spin-density matrix of the vector meson  $\rho(V)$  expressed in terms of the photon matrix  $\rho(\gamma)$   
 and helicity amplitude  $T_{\lambda_V \lambda_\gamma}$
- presented according to K.Schilling and G.Wolf (Nucl. Phys. B61 (1973) 381)  
 $\alpha = 0,4$  - longtd. or transv. photon with  $\lambda_V = 0$ ;     $\alpha = 1-2$  - transv. with lin. pol. ;  
 $\alpha = 3$  - transv. with cir. pol.;     $\alpha = 5-8$  - interf. transv./longtd. terms.
- measured at  $5 < W < 75$  GeV (HERMES, COMPASS, H1, ZEUS)
- provide access to helicity amplitudes  $T_{\lambda_V \lambda_\gamma}$  and phases, which are:
  - extracted from SDMEs
  - calculated from GPDs:S.V.Goloskokov,P.Kroll arXiv:0708.3569 [hep-ph]27.08.07; Eur.Phys.J. C 50,829 (2007) hep-ph/0601290; Eur.Phys.J. C 42,281 (2005) hep-ph/0501242

# HERMES SPECTROMETER

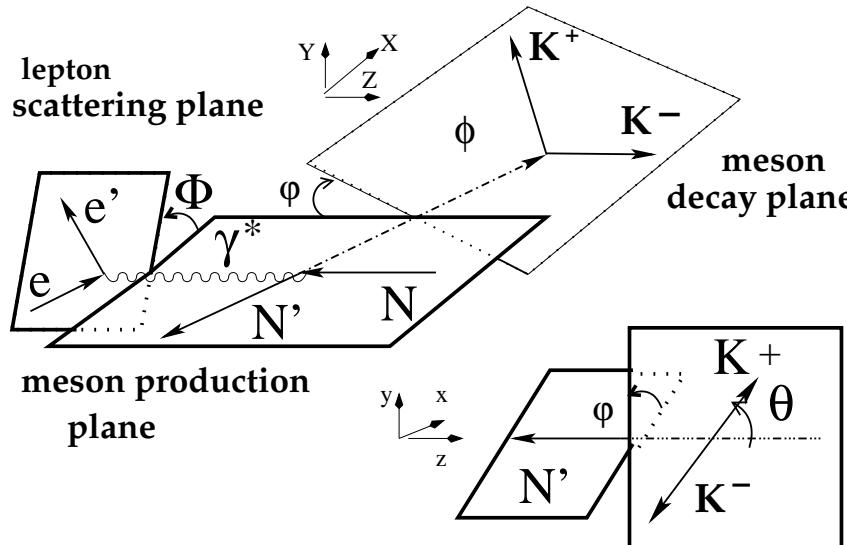


- Acceptance:  $|\Theta_x| < 170 \text{ mrad}$ ,  $40 < |\Theta_y| < 140 \text{ mrad}$ ,
- Resolution  $\delta p/p < 1 \%$ ,  $\delta \Theta < 0.6 \text{ mrad}$ ,
- Identification efficiency: positron/electron above 99% , hadron average is 99%,
- Contamination of hadrons (positrons) in the positron (hadron) sample - below 0.01% (0.6%)
- Good separation of pions, kaons, protons and other hadrons for momenta between 2- 15 GeV,
- Average target polarization (years 2002-2005) is 72 %.

# Excl. Events. Method of determination SDMEs



$$\Delta E = \frac{M_x^2 - M_p}{2M_p}.$$



**Definition of angles.**

- Simulated events: matrix of fully reconstructed MC events **from initial uniform angular distribution**
- **Binned Maximum Likelihood Method:**  $8 \times 8 \times 8$  bins of  $\cos(\Theta), \phi, \Phi$ . **Simultaneous fit of 23 SDMEs**  $r_{ij}^\alpha = W(\Phi, \phi, \cos \Theta)$  **for data with negative and positive beam helicity** ( $<|P_b|> = 53.5\%$ )

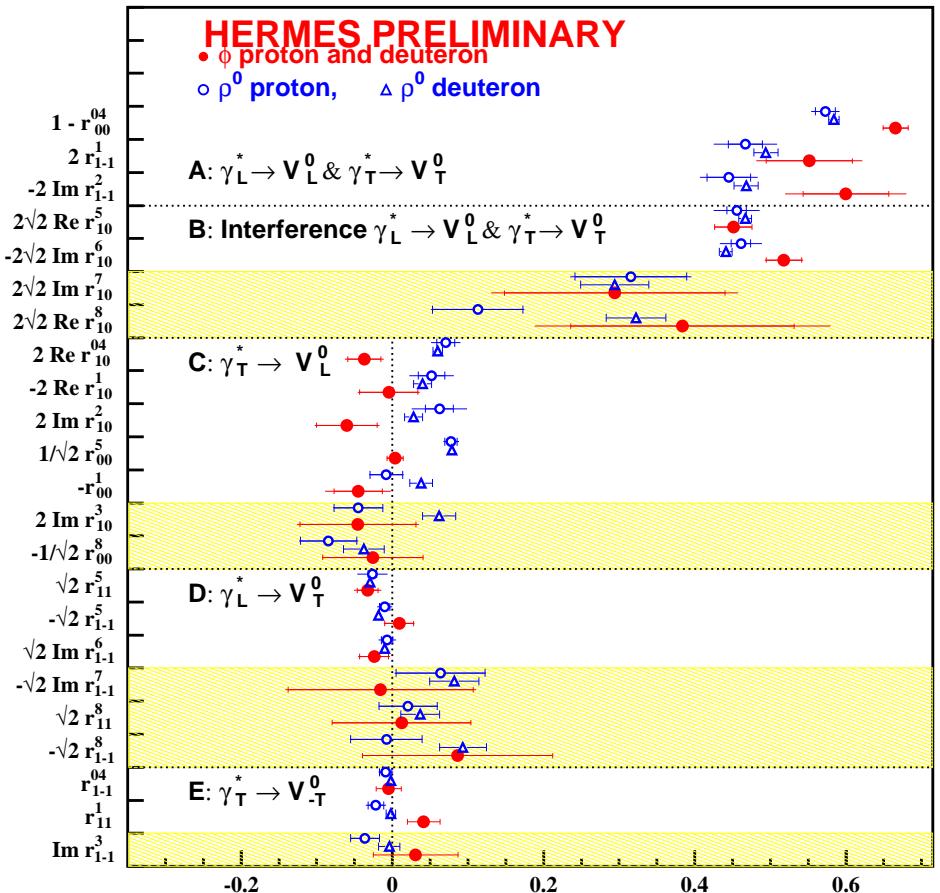
**A- SCHC**  $\gamma_L^* \rightarrow \phi_L$  and  $\gamma_T^* \rightarrow \phi_T$   
 $|T_{11}|^2 \propto 1 - r_{00}^{04} \propto r_{1-1}^1 \propto -\text{Im}\{r_{1-1}^2\}$

**B- Interference:**  $\gamma_L^* \rightarrow \phi_L$  and  $\gamma_T^* \rightarrow \phi_T$   
 $\text{Re}\{T_{00}T_{11}^*\} \propto \text{Re}\{r_{10}^5\} \propto -\text{Im}\{r_{10}^6\}$   
 $\text{Im}\{T_{11}T_{00}^*\} \propto \text{Im}\{r_{10}^7\} \propto \text{Re}\{r_{10}^8\}$

**C- Spin Flip:**  $\gamma_T^* \rightarrow \phi_L$   
 $\text{Re}\{T_{11}T_{01}^*\} \propto \text{Re}\{r_{10}^{04}\}$   
 $\propto \text{Re}\{r_{10}^1\} \propto \text{Im}\{r_{10}^2\}$   
 $\text{Re}\{T_{01}T_{00}^*\} \propto r_{00}^5$   
 $|T_{01}|^2 \propto r_{00}^1$   
 $\text{Im}\{T_{01}T_{11}^*\} \propto \text{Im}\{r_{10}^3\}$   
 $\text{Im}\{T_{01}T_{00}^*\} \propto r_{00}^8$

**D-Spin Flip:**  $\gamma_L^* \rightarrow \phi_T$   
 $\text{Re}\{T_{10}T_{11}^*\} \propto r_{11}^5 \propto r_{1-1}^5 \propto \text{Im}\{r_{1-1}^6\}$   
 $\text{Im}\{T_{10}T_{11}^*\} \propto \text{Im}\{r_{1-1}^7\} \propto r_{11}^8 \propto r_{1-1}^8$

**E- Double Spin Flip:**  $\gamma_T^* \rightarrow \phi_{-T}$   
 $\text{Re}\{T_{1-1}T_{11}^*\} \propto r_{1-1}^{04} \propto r_{11}^1$   
 $\text{Im}\{T_{1-1}T_{11}^*\} \propto \text{Im}\{r_{1-1}^3\}$



**Diff. for class A :**  $|T_{11}^\phi|^2 > |T_{11}^\rho|^2 (\sim 20\%)$  scaled SDME

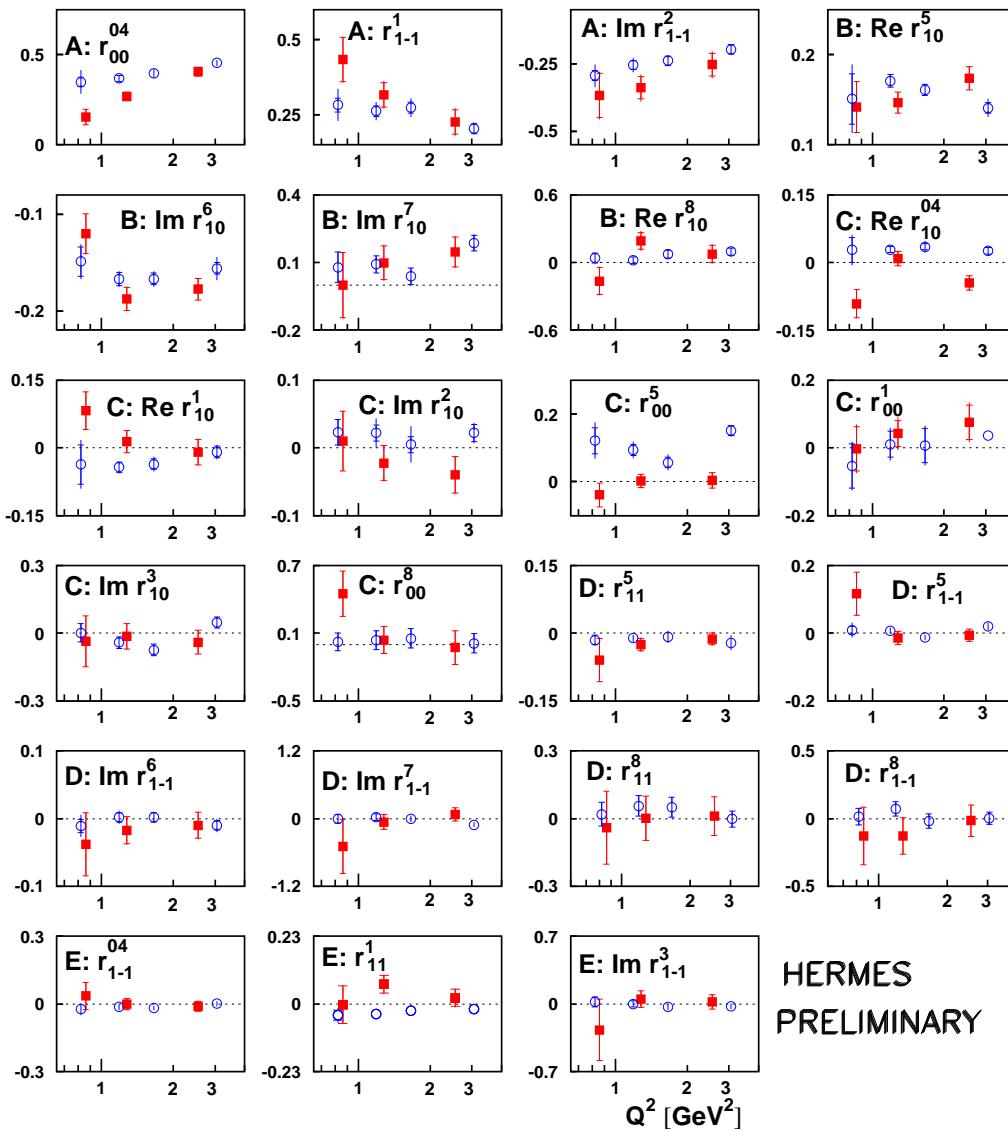
**B:**  $(T_{11}T_{00}^*)$ ,  $\rho^0 \sim \phi$  diff. phases  $T_{11}$  and  $T_{00}$

$$\text{tg}(\delta\phi) = (\text{Im } r_{10}^7 + \text{Re } r_{10}^8) / (\text{Re } r_{10}^5 - \text{Im } r_{10}^6),$$

$$\delta_{p+d}^\phi = 33.0^\circ \pm 7.4^\circ, \delta_p^\rho = 30.0^\circ \pm 5.0^\circ \pm 2.4^\circ$$

**and C:** for  $\rho^0 > 0$ ,

# Dependences of SDME's on $Q^2$



HERMES  
PRELIMINARY

The dependences of SDME's on  $Q^2$  for proton and deuteron data. The outer bars represent the total, the inner ones the statistical errors.

$\phi$  - red closed squares,  $\rho^0$  - open blue circles.

See classes A, B; C -  $r_{00}^5$ .

## NOTATION:

**A- SCHC**  $\gamma_L^* \rightarrow \phi_L$  and  $\gamma_T^* \rightarrow \phi_T$

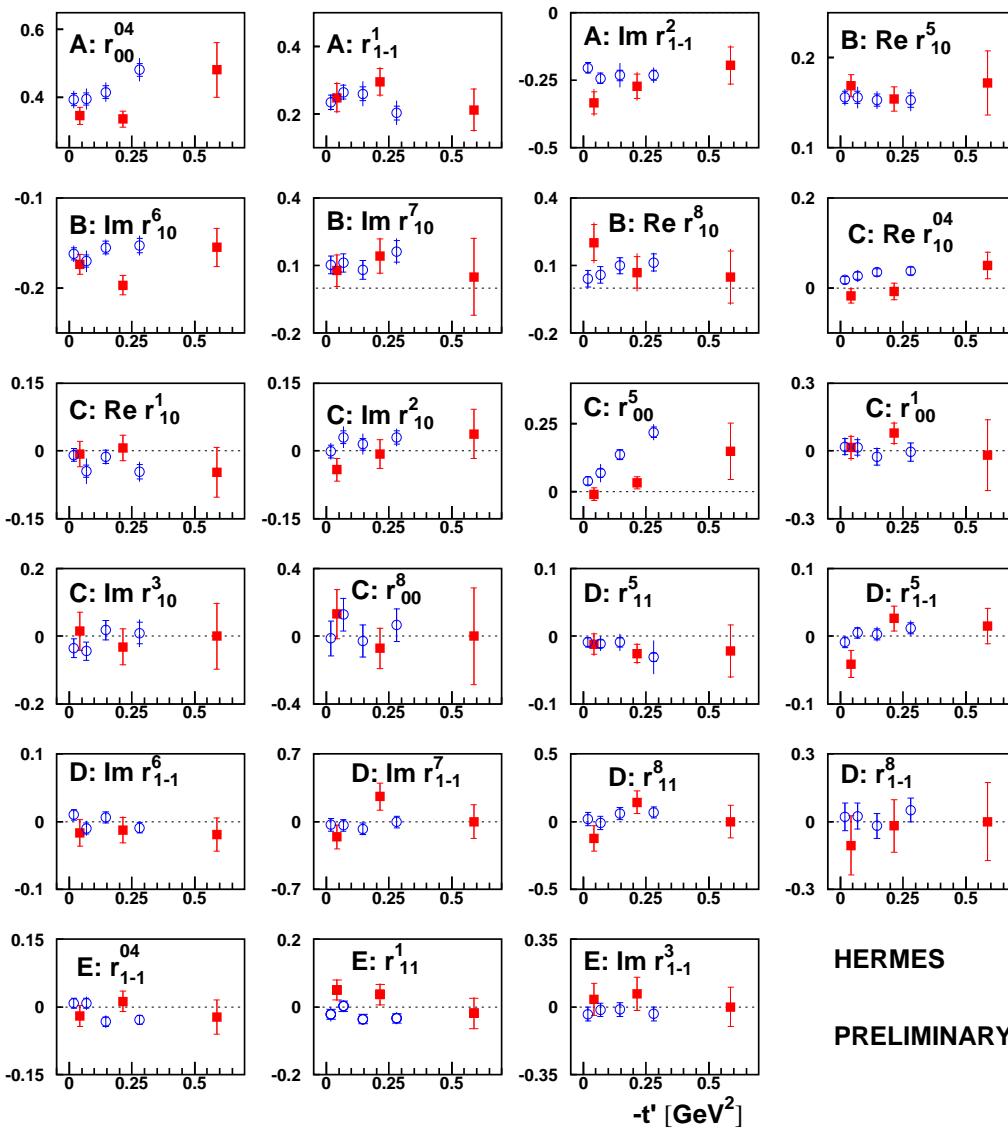
**B- Interference:**  $\gamma_L^* \rightarrow \phi_L$  and  $\gamma_T^* \rightarrow \phi_T$

**C- Spin Flip:**  $\gamma_T^* \rightarrow \phi_L$

**D-Spin Flip:**  $\gamma_L^* \rightarrow \phi_T$

**E- Double Spin Flip:**  $\gamma_T^* \rightarrow \phi_{-T}$

# Dependences of SDME's on $t'$



The dependences of SDME's on  $t'$  for proton and deuteron data. The outer bars represent the total, the inner ones the statistical errors.

$\phi$  - red closed squares,  $\rho^0$  - open blue circles.

See class C .

## NOTATION:

**A- SCHC**  $\gamma_L^* \rightarrow \phi_L$  and  $\gamma_T^* \rightarrow \phi_T$

**B- Interference:**  $\gamma_L^* \rightarrow \phi_L$  and  $\gamma_T^* \rightarrow \phi_T$

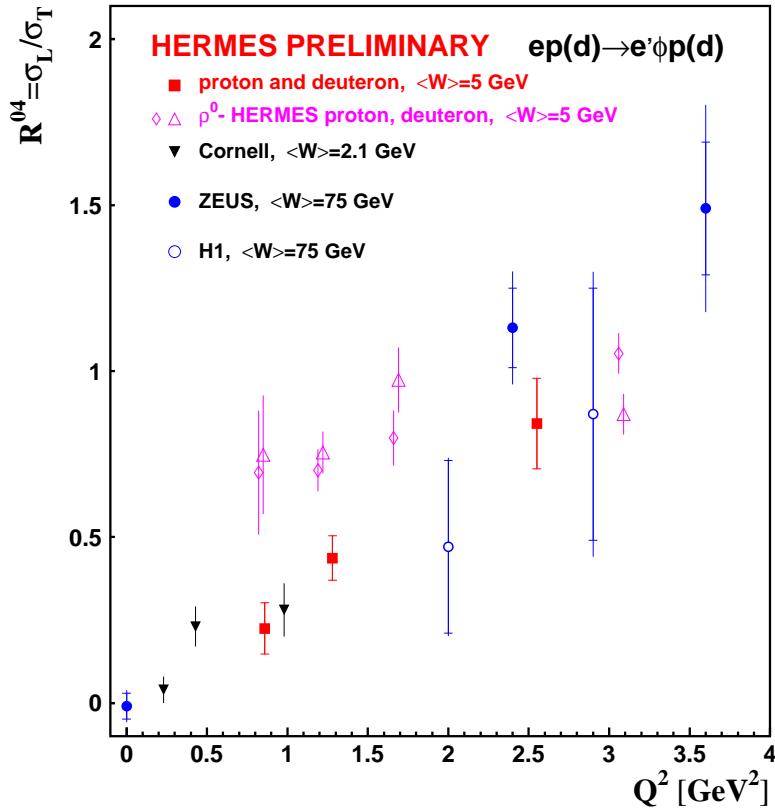
**C- Spin Flip:**  $\gamma_T^* \rightarrow \phi_L$

**D-Spin Flip:**  $\gamma_L^* \rightarrow \phi_T$

**E- Double Spin Flip:**  $\gamma_T^* \rightarrow \phi_{-T}$

HERMES  
PRELIMINARY

# Longitudinal-to-Transverse Cross-Section Ratio



Comparison of commonly measured:

$$R^{04} = \frac{\sigma_L}{\sigma_T} = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1 - r_{00}^{04}},$$

where:

$$r_{00}^{04} = \sum \{ \epsilon |T_{00}|^2 + |T_{11}|^2 \} / \sigma_{tot}$$

$$\sigma_{tot} = \epsilon \sigma_L + \sigma_T$$

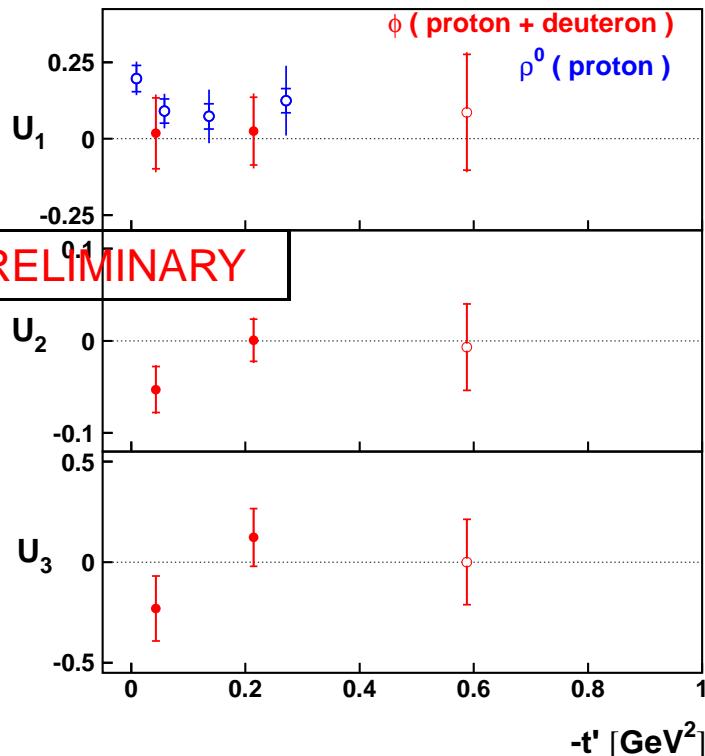
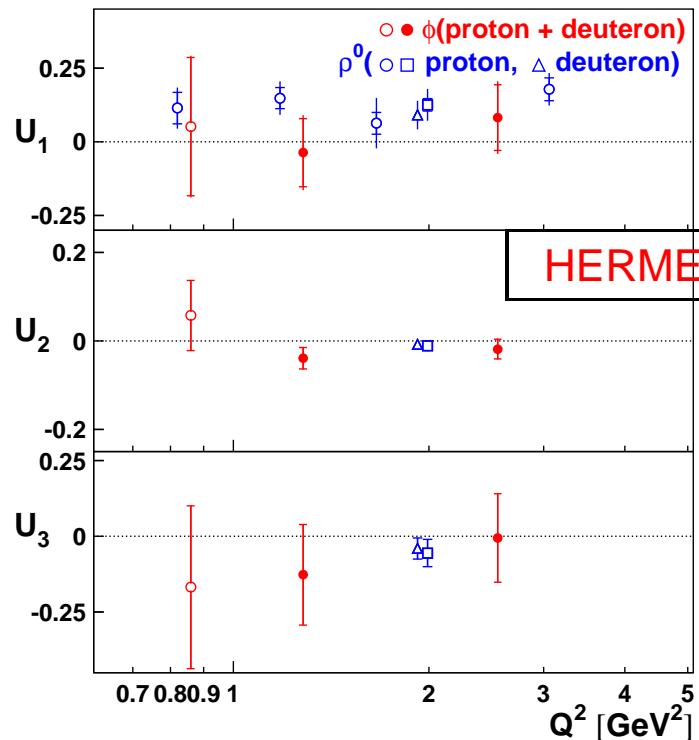
$$\text{Theory: } R = \frac{Q^2}{M_V^2},$$

S. Brodsky et al., Phys. Rev. D50(1994) 3134

Modifications to those dependences are expected due to the  $Q^2$  dependence of gluon density, the quark transverse movement(Fermi motion) and quark virtuality as well as the  $Q^2$  dependence of the strong coupling constant  $\alpha_s$ . L. Frankfurt et al., Phys. Rev.D54 (1996) 3194, (Fermi motion)  
I. Royen et al., Nucl. Phys. B 545 (1999) 505 and Phys. Lett. B 513 (2001) 337

⇒  $R^{04}$  for  $\phi$  meson at HERMES is in good agreement with world data.

# Unnatural Parity Exchange in $\phi$ Meson Leptoproduction



$$U_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{1-1}^1 - 2r_{11}^1;$$

$$U_2 = r_{1-1}^5 + r_{11}^5; \quad \underline{U_3 = r_{1-1}^8 + r_{11}^8.}$$

$$U_1 = \tilde{\Sigma}(4\epsilon|U_{10}|^2 + 2|U_{11} + 2U_{-11}|^2)/\mathcal{N};$$

$$U_2 + iU_3 = \sqrt{(2)}\tilde{\Sigma}\{(U_{11} + U_{-11})^*U_{10}\}/\mathcal{N}.$$

$$\tilde{\Sigma}U_{\lambda_V\lambda_\gamma}U_{\lambda'_V\lambda'_\gamma}^* = \frac{1}{2} \sum_{\lambda_N, \lambda_{N'}} U_{\lambda_V\lambda'_N; \lambda_\gamma\lambda_N} U_{\lambda'_V\lambda'_N; \lambda_\gamma^*\lambda_N}^*$$

hierarchy:  $\tilde{\Sigma}|U_{11}|^2 \gg \tilde{\Sigma}|U_{10}|^2, \tilde{\Sigma}|U_{01}|^2, \tilde{\Sigma}|U_{-11}|^2,$

no interference NPE and UPE:  $\tilde{\Sigma}T_{\lambda_V, \lambda_\gamma} U_{\lambda'_V, \lambda'_\gamma}^* = 0$

# Ratios of Helicity Amplitudes

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## EXPERIMENT

The real and imaginary parts of ratios of natural-parity-exchange helicity amplitudes:

$T_{11} (\gamma_T^* \rightarrow \rho_T)$ ,  $T_{01} (\gamma_T^* \rightarrow \rho_L)$ ,  $T_{10} (\gamma_L^* \rightarrow \rho_T)$ ,  $T_{1-1} (\gamma_{-T}^* \rightarrow \rho_T)$  to  $T_{00} (\gamma_L^* \rightarrow \rho_L)$

and for the unnatural-parity-exchange amplitude  $U_{11}$  the ratio  $|U_{11}|/|T_{00}|$  were obtained.

Beam: longitudinally polarized electron/positron 27.6 GeV

Targets: hydrogen and deuterium unpolarized

Kinematical region:  $0.5 \text{ GeV}^2 < Q^2 < 7.0 \text{ GeV}^2$ ,  $3.0 \text{ GeV} < W < 6.3 \text{ GeV}$ ,  $-t' < 0.4 \text{ GeV}^2$

The  $Q^2$  and  $-t'$  dependences are also extracted.

Divided in 16 bins for  $Q^2$ :  $0.5 \div 1.0 \div 2.0 \div 7.0 \text{ GeV}^2$ ;

for  $-t'$   $0.0 \div 0.04 \div 0.10 \div 0.2 \div 0.4 \text{ GeV}^2$ .

Extractions: use angular distributions:  $\cos(\theta)$ ,  $\Phi$  and  $\phi$  as well as isotropic simulation sample (RHOMC).

# Ratios of Helicity Amplitudes

## Theoretical studies:

D. Yu. Ivanov and R. Kirshner Phys. Rev. D58(1998) 114026 [hep-ph/9807324],

E.V. Kuraev, N.N. Nikolaev, and B.G. Zakharov, Pis'ma ZHETF,68,(1998) 667

## pQCD:

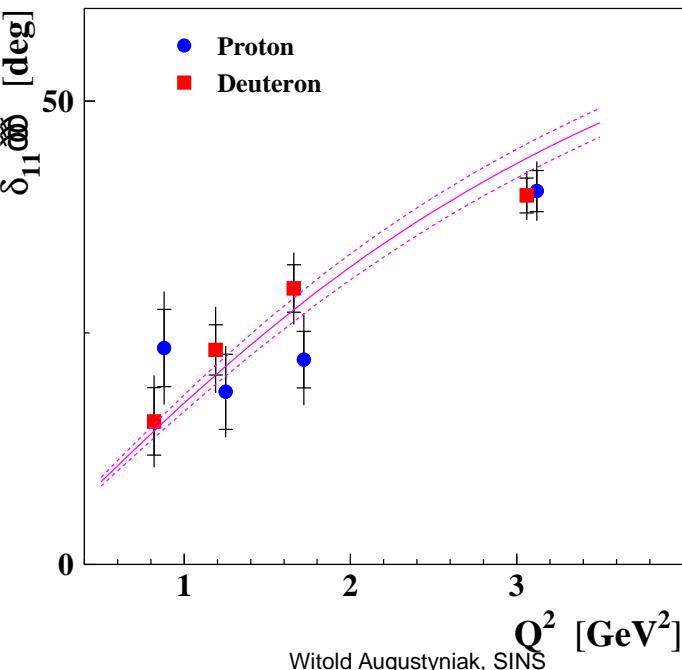
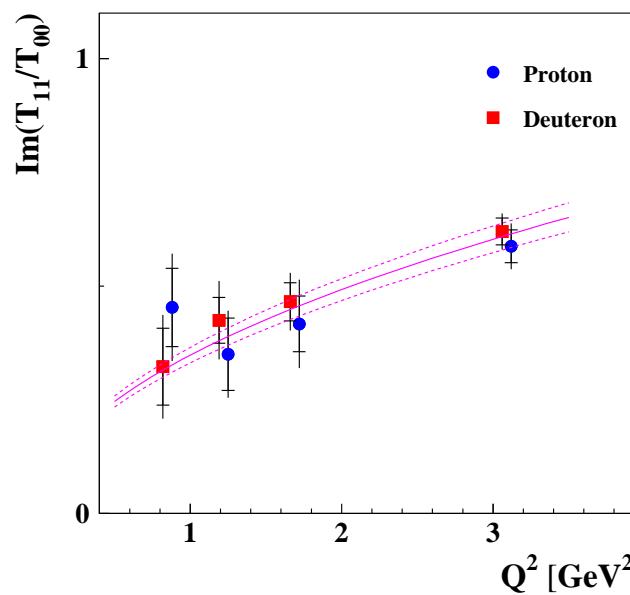
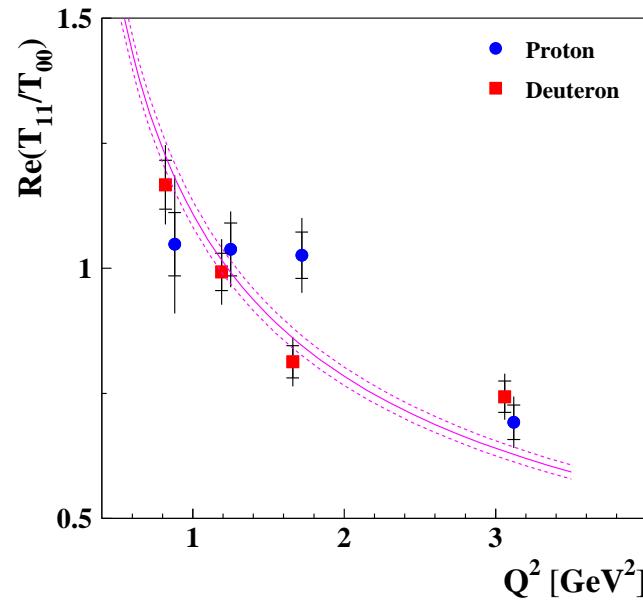
$$t_{11} = \frac{T_{11}}{T_{00}} \propto \frac{M_V}{Q},$$

$$t_{01} = \frac{T_{01}}{T_{00}} \propto \frac{\sqrt{(-t')}}{Q},$$

$$t_{10} = \frac{T_{10}}{T_{00}} \propto \frac{M_V \sqrt{(-t')}}{Q^2 + M_V^2},$$

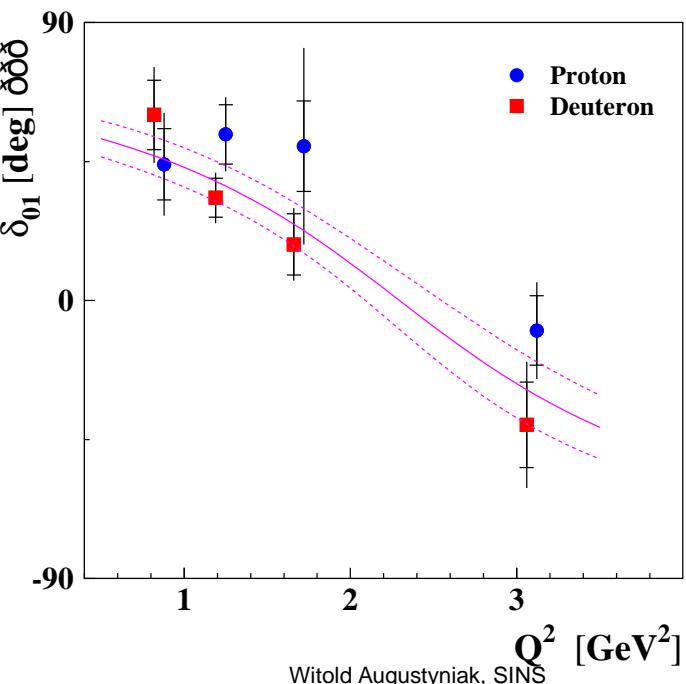
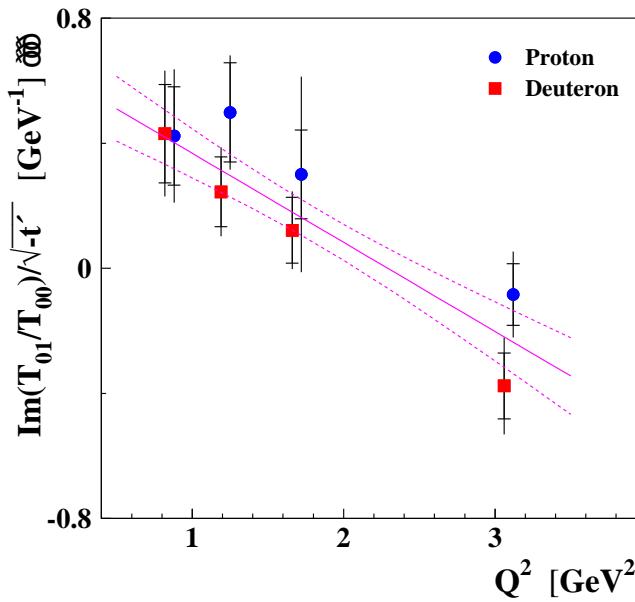
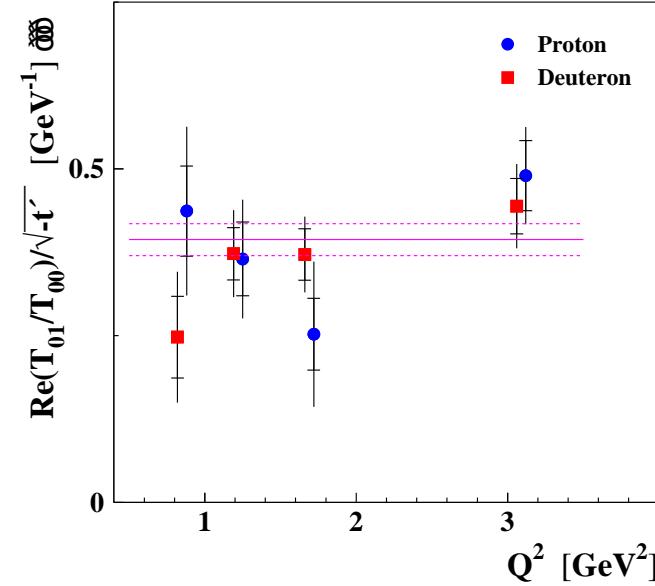
$$t_{1-1} = \frac{T_{1-1}}{T_{00}} \propto \frac{-t' M_V}{Q} \left( \frac{C_1}{Q^2 + M_V^2} + \frac{C_2}{\mu^2} \right),$$

# Ratios of Helicity Amplitudes $t_{11}$



$Q^2$  dependence of  $\text{Re}(T_{11}/T_{00})$ ,  $\text{Im}(T_{11}/T_{00})$  and their phase difference  $\delta_{11}$ , for hydrogen and deuterium targets. Parameterization is given by the function:  $\text{Re}(t_{11})=a/Q$  and  $\text{Im}(t_{11})=bQ$ . (The function for  $\text{Im}(T_{11}/T_{00})$  different from theoretical predictions.) High value of  $\delta_{11}$  is observed.

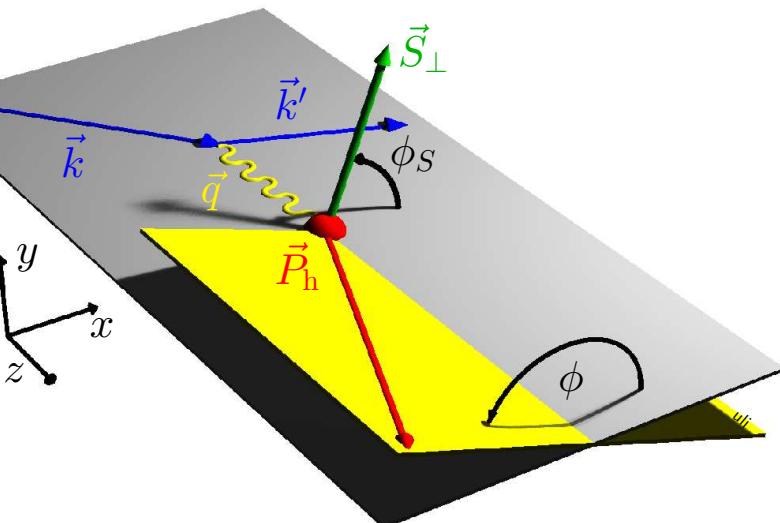
# Ratios of Helicity Amplitudes $t_{01}$



$Q^2$  dependence of  $Re(T_{01}/T_{00})$ ,  $Im(T_{01}/T_{00})$  and their phase difference  $\delta_{01}$  for hydrogen and deuterium targets.  
The  $Q^2$  dependence was observed only for  $Im(t_{01})$ .

# $A_{UT}$ : Definition of the azimuthal angles

## TRENTO CONVENTION



$\phi$  and  $\phi_S$  are angles defined by the lepton-scattering plane and the VM production plane or target spin vector in the center-of-mass system ( $\gamma^*, p$ ).

$$\cos \phi = \frac{(\vec{q} \times \vec{v}) \cdot (\vec{k} \times \vec{k}')}{|\vec{q} \times \vec{v}| \cdot |\vec{k} \times \vec{k}'|}, \quad \sin \phi = \frac{[(\vec{k} \times \vec{v}) \cdot \vec{q}]}{|\vec{k} \times \vec{q}| \cdot |\vec{q} \times \vec{v}|},$$

$$\cos \phi_S = \frac{(\vec{q} \times \vec{S}) \cdot (\vec{k} \times \vec{k}')}{|\vec{q} \times \vec{S}| \cdot |\vec{k} \times \vec{k}'|}, \quad \sin \phi_S = \frac{[(\vec{k} \times \vec{S}) \cdot \vec{q}]}{|\vec{k} \times \vec{q}| \cdot |\vec{q} \times \vec{S}|},$$

Relation between the azimuthal angles in the selected frames:

$$F^{q \perp S}(S_T, S_L, \phi, \phi_S) = \mathcal{R}(\theta, \gamma) F^{k \perp S}(P_T, P_L, \psi, \psi_S),$$

where:  $\sin \theta = \gamma(1-y - \frac{1}{4}y^2\gamma^2)/(1+\gamma^2)$ ,  $\gamma = 2x_B M_p/Q$ .

$$S_T = \frac{P_T \cos \theta}{\sqrt{1 - \sin^2 \theta \sin^2 \phi_S}}.$$

# $A_{UT}$ : Main definitions and relations

M.Diehl, S. Sapeta  
 hep-ph/0503023

$$\left[ \frac{\cos \theta}{1 - \sin^2 \theta \sin^2 \phi_S} \right]^{-1} \left[ \frac{\alpha_{\text{em}}}{8\pi^3} \frac{y^2}{1-\varepsilon} \frac{1-x_B}{x_B} \frac{1}{Q^2} \right]^{-1} \frac{d\sigma}{dx_B dQ^2 d\phi d\phi_S} \Big|_{P_L=0}$$

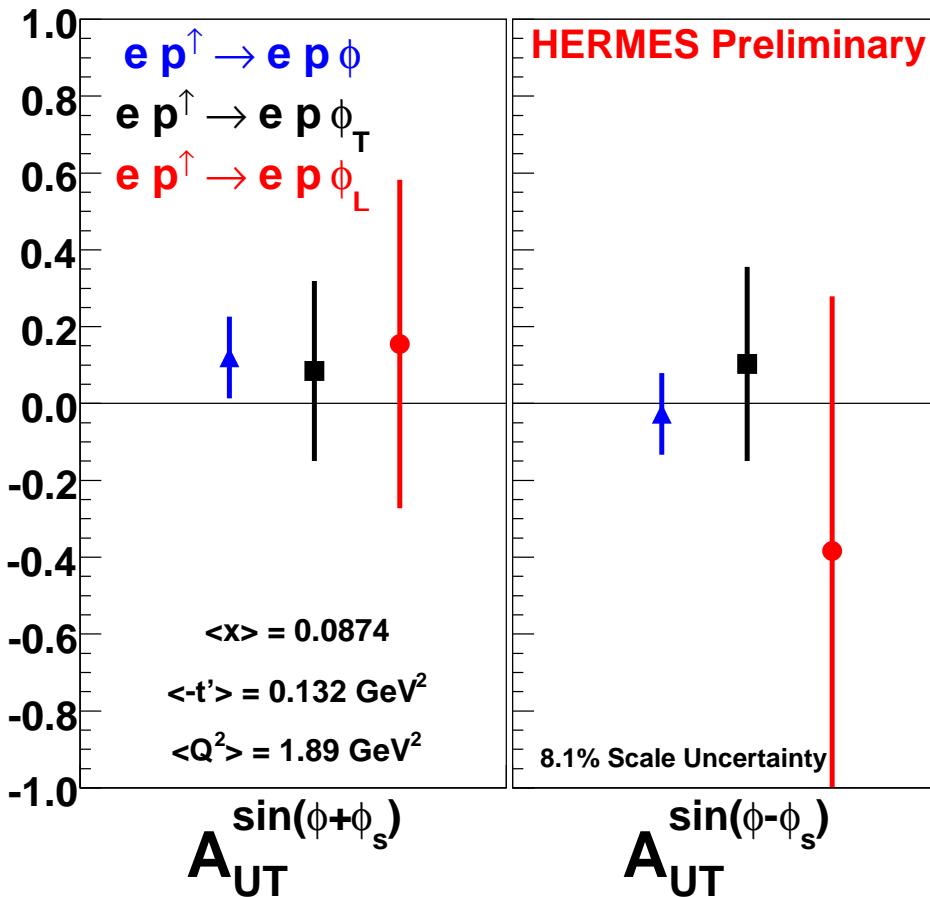
= terms independent of  $P_T$

$$- \frac{P_T}{\sqrt{1 - \sin^2 \theta \sin^2 \phi_S}} \left[ \begin{aligned} & \sin \phi_S \cos \theta \sqrt{\varepsilon(1+\varepsilon)} \text{Im } \sigma_{+0}^{+-} \\ & + \sin(\phi - \phi_S) \left( \cos \theta \text{Im } (\sigma_{++}^{+-} + \varepsilon \sigma_{00}^{+-}) + \frac{1}{2} \sin \theta \sqrt{\varepsilon(1+\varepsilon)} \text{Im } (\sigma_{+0}^{++} - \sigma_{+0}^{--}) \right) \\ & + \sin(\phi + \phi_S) \left( \cos \theta \frac{\varepsilon}{2} \text{Im } \sigma_{+-}^{+-} + \frac{1}{2} \sin \theta \sqrt{\varepsilon(1+\varepsilon)} \text{Im } (\sigma_{+0}^{++} - \sigma_{+0}^{--}) \right) \\ & + \sin(2\phi - \phi_S) \left( \cos \theta \sqrt{\varepsilon(1+\varepsilon)} \text{Im } \sigma_{+0}^{-+} + \frac{1}{2} \sin \theta \varepsilon \text{Im } \sigma_{+-}^{++} \right) \\ & + \sin(2\phi + \phi_S) \frac{1}{2} \sin \theta \varepsilon \text{Im } \sigma_{+-}^{++} \\ & + \sin(3\phi - \phi_S) \cos \theta \frac{\varepsilon}{2} \text{Im } \sigma_{+-}^{-+} \end{aligned} \right]$$

$$A_{UT} \sim \cos \theta \text{Im} (\sigma_{++}^{+-} + \varepsilon \sigma_{00}^{+-})$$

where:  $\sigma_{mn}^{ij}(Q^2, x_B)$  are cross sections or interference terms with indices: (i, j) describing polarization of the protons ( $p$  and  $p'$ ) as well as (m,n) - polarization of ( $\gamma^*$  and VM),  
 $\varepsilon$  - ratio of longitudinal to transverse photon flux

# $A_{UT}$ for $\phi$ vector mesons



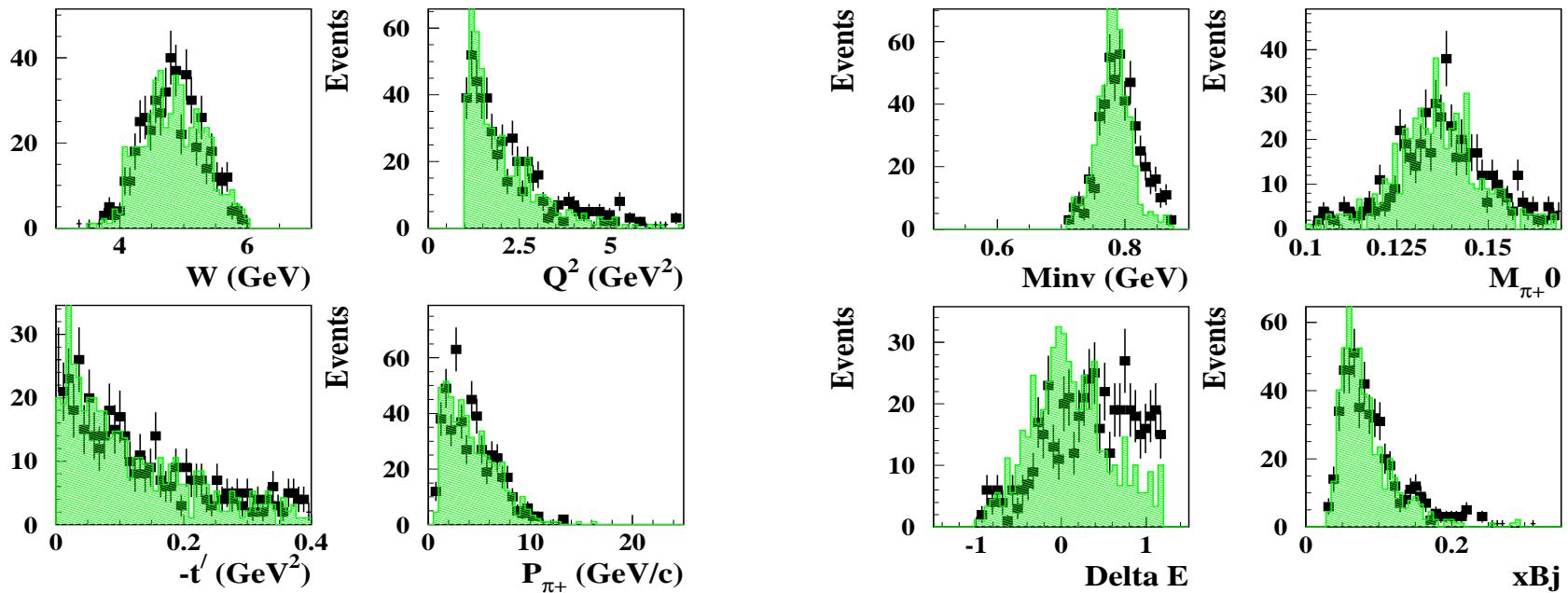
Used cuts:

- Fiducial cuts
- Determine:  $e^\pm, K^+, K^-$
- Cut for the opening angle of decaying  $\phi$  meson
- Cut for  $P_\phi > 7.5 \text{ GeV}/c$
- Kinematical cuts  $Q^2 > 1 \text{ GeV}$ ,  $-t' < 0.5 \text{ GeV}^2$ ,  $W > 5 \text{ GeV}$

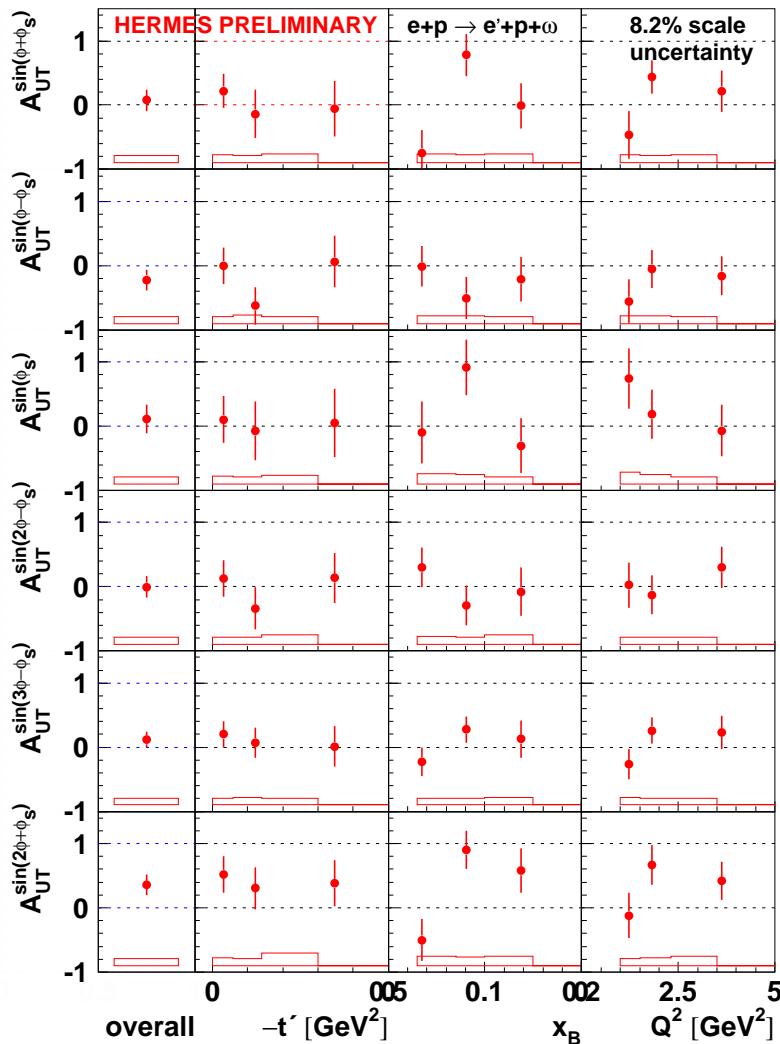
Amplitudes  $A_{UT}$  determined for  $\phi$  vector mesons (blue) and separated for longitudinal (red) as well as transverse (black)  $\phi$  mesons components.

Transverse Target Spin Asymmetry (TTSA) method provide information about E GPDs function that are sensitive to helicity-flip. E GPDs functions contain information about the orbital angular momentum of the quarks.

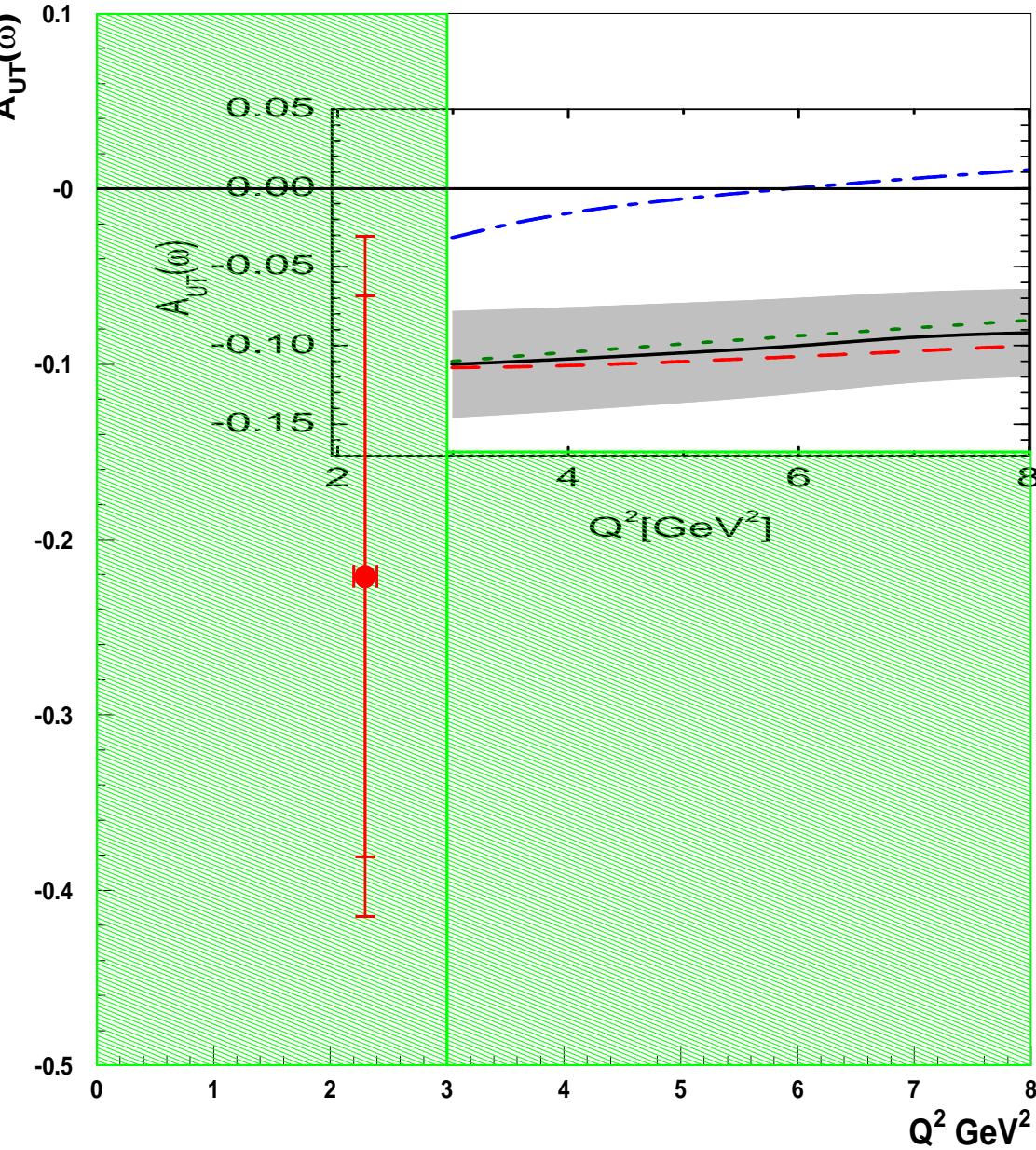
# Main observables for $\omega$



Distributions of several kinematic variables from data on exclusive  $\omega$  meson leptoproduction (black squares) in comparison with simulated events from PYTHIA (dashed areas). Simulated events are normalized to the data.



The moments of  $A_{UT}$  for  $\omega$  in the common kinematic interval and their  $-t'$ ,  $x_B$  and  $Q^2$ -dependences after background subtraction. Statistical uncertainties are shown as error bars. Red boxes at the bottom of each plot represent the systematic uncertainties.



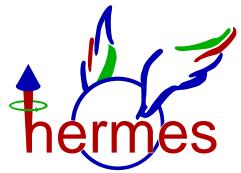
$A_{UT}$ : experimental value and theoretical predictions. The theoretical predictions from GK model. The solid, dashed, dotted and dash-dotted lines represent the results for different variants. The shaded band indicates the theoretical uncertainty for one variant. The other variants have similar uncertainties.

- Comparison of SDMEs for  $\phi$  and  $\rho^0$ 
  - SDMEs  $\sim |T_{11}|^2$  (class A) are higher ( $\sim 20\%$ ) for  $\phi$  compared to those for  $\rho^0$
  - Values of SDMEs belonging to class B are similar. Sign and value of the difference phases  $T_{11}$  and  $T_{00}$  is found
  - Class C: in the case of  $\phi$ , SDMEs fluctuate near zero opposite to  $\rho^0$  where non-zero elements indicate a single-spin-flip.
- Dependences of SDMEs and other observables on  $Q^2$  and  $t'$ 
  - Regular dependence of SDMEs on  $Q^2$  and different behaviour for  $\phi$  and  $\rho^0$  is observed
  - Dependence  $R^{04} = \frac{\sigma_L}{\sigma_T}$  on  $Q^2$  agrees with other measurements
  - Different dependences of  $R^{04}$  on  $Q^2$  for  $\phi$  and  $\rho^0$  vector mesons are observed
  - Observed dependence of  $r_{00}^5$  on  $t'$  for  $\rho^0$  is not seen for  $\phi$
  - Observed signals of unnatural parity exchange for  $\rho^0$  are not seen for  $\phi$
- Ratios of Helicity Amplitudes
  - Different dependences on  $Q^2$  of real and imaginary ratios:  $t_{11}$  and  $t_{01}$  are observed.



$A_{UT}$

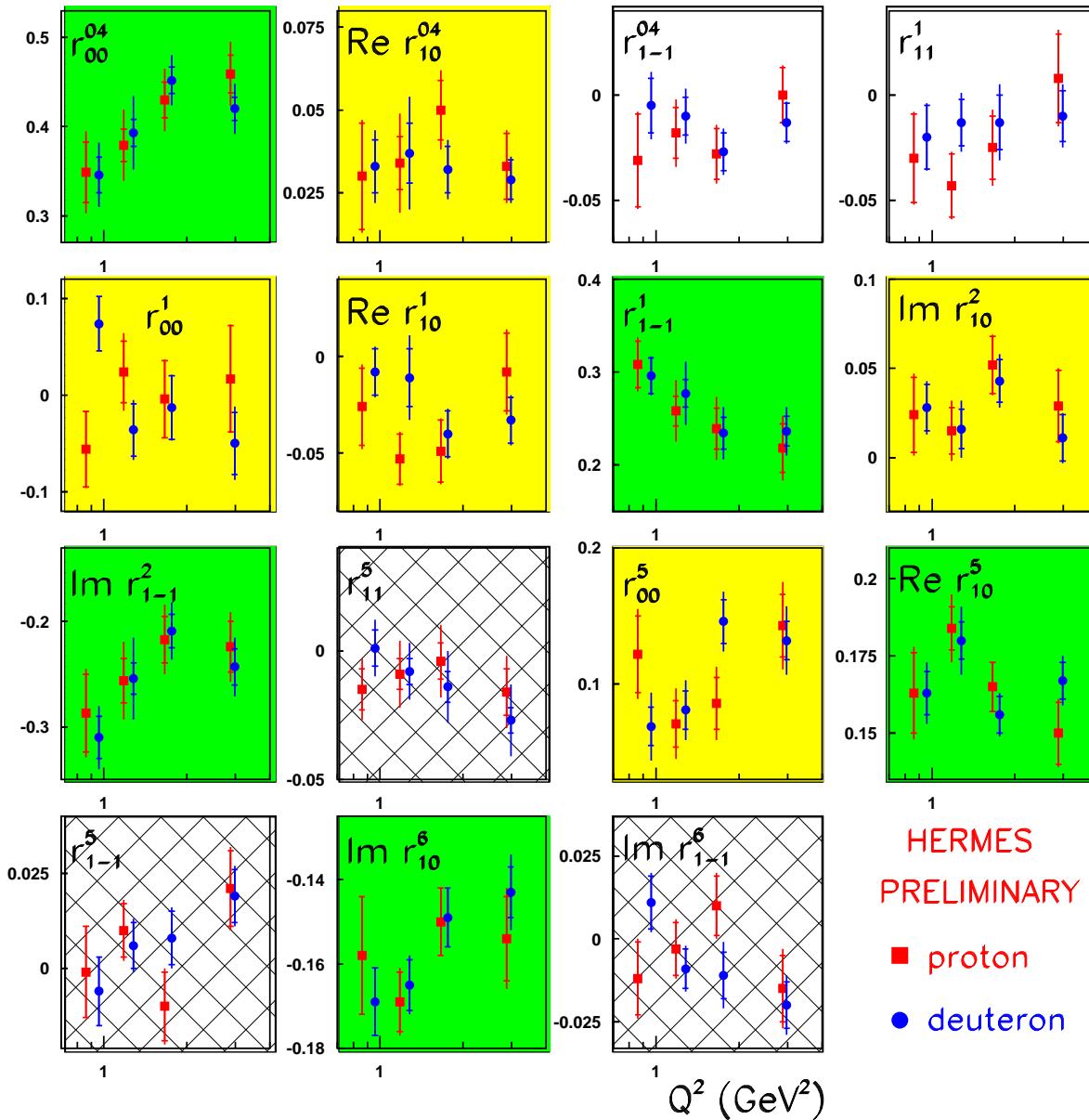
- Near zero value of  $A_{UT}$  for  $\phi$  is found
- Negative value of  $A_{UT}$  for  $\omega$  is found
- Both values are predicted by theoretical models:S.V. Goloskolov, P. Kroll hep-ph/0809412 and F.Ellinghaus et al, Eur. Phys. J C46 729 (2006)



## *Additional slides*

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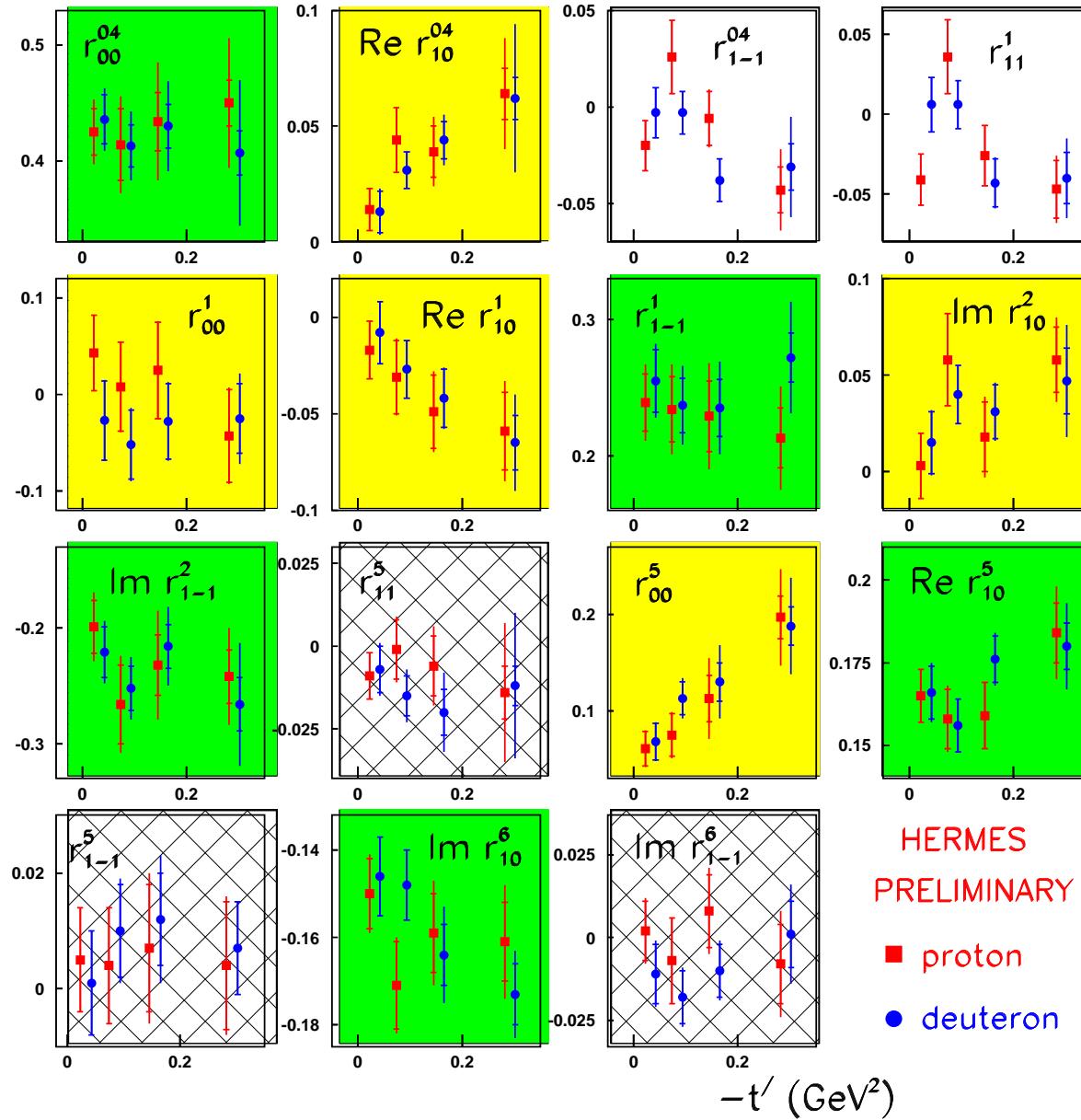
# Dependencies of $\rho^0$ meson SDME's on $Q^2$



HERMES  
PRELIMINARY

- proton
- deuteron

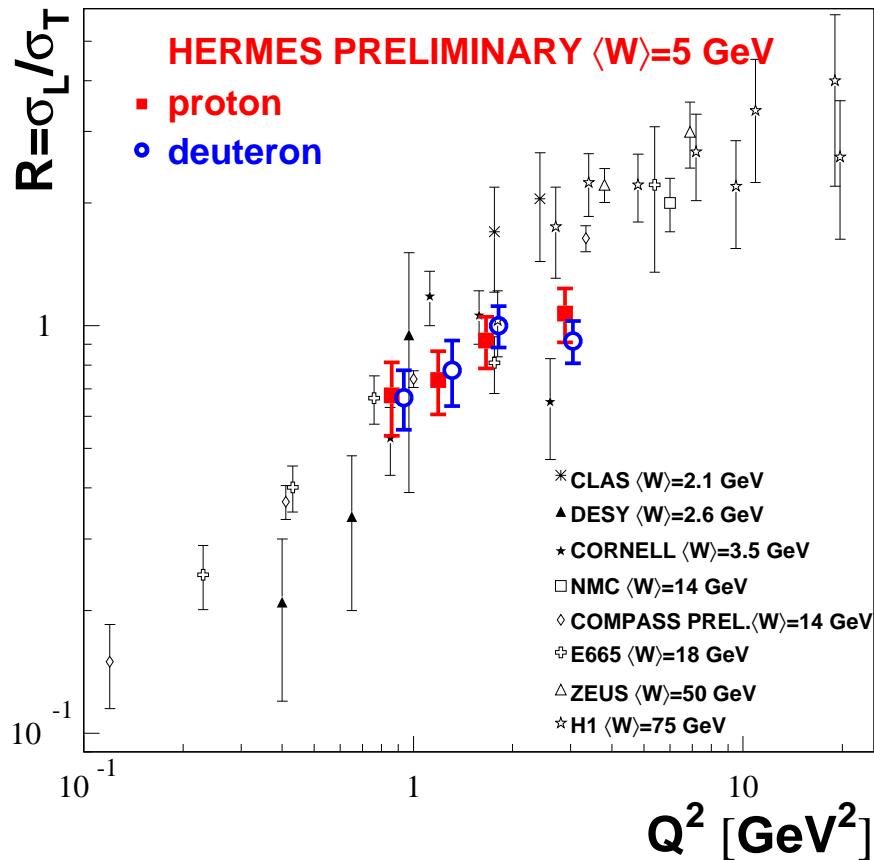
# Dependencies of $\rho^0$ meson SDME's on $t'$



HERMES  
PRELIMINARY

- proton
- deuteron

# $\rho^0$ Longitudinal-to-Transverse Cross-Section Ratio



Comparison of commonly measured:

$$R^{04} = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1 - r_{00}^{04}},$$

$$r_{00}^{04} = \sum \{ \epsilon |T_{00}|^2 + |T_{01}|^2 + |U_{01}|^2 \} / \sigma_{tot},$$

$$\sigma_{tot} = \epsilon \sigma_L + \sigma_T,$$

$$\sigma_T = \sum \{ |T_{11}|^2 + |T_{01}|^2 + |T_{1-1}|^2 + |U_{11}|^2 \},$$

$$\sigma_L = \sum \{ |T_{00}|^2 + 2|T_{10}|^2 \}.$$

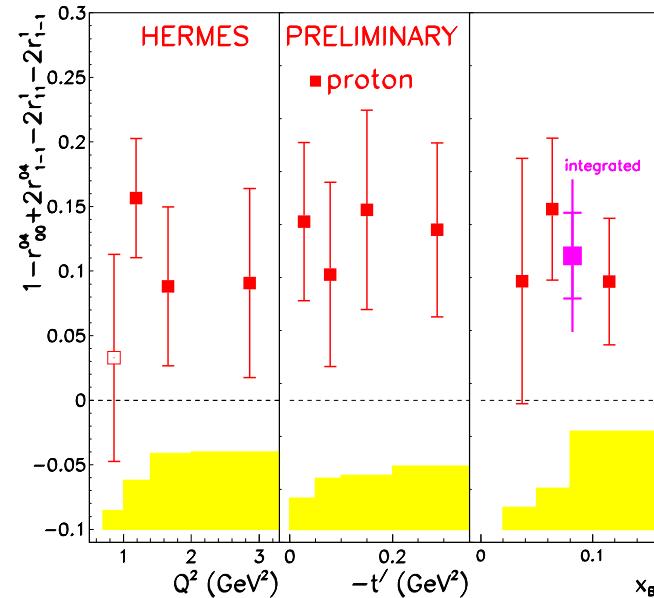
Due to the helicity-flip and unnatural parity amplitudes  $R^{04}$  depends on kinematic conditions, and is not identical to  $R \equiv |T_{00}|^2 / |T_{11}|^2$  at SCHC and NPE dominance.

⇒ Second order contribution of spin-flip amplitudes to  $R^{04}$

⇒ HERMES  $\rho^0$  data on  $R^{04}$  are suggestive to  $R(W)$ -dependence

# Unnatural Parity Exchange (UPE) in $\rho^0$ Leptoproduction

- Natural-parity exchange: interaction is mediated by a particle of ‘natural’ parity: vector or scalar meson:  
 $J^P = 0^+, 1^-$  e.g.  $\rho^0, \omega, a_2$
- Unnatural parity exchange is mediated by pseudoscalar or axial meson:  
 $J^P = 0^-, 1^+$ , e.g.  $\pi, a_1, b_1 \rightarrow$  only quark-exchange contribution
- No interference between NPE and UPE contributions on unpolarized target
- Extracted from SDMEs:  
 $U2 + iU3 \propto (U_{11} + U_{1-1}) * U_{10}$   
 $U2 = r_{11}^5 + r_{1-1}^5$   
p:  $U2 = -0.012 \pm 0.006_{stat} \pm 0.012_{syst}$   
d:  $U2 = -0.008 \pm 0.0046_{stat} \pm 0.010_{syst}$   
 $U3 = r_{11}^5 + r_{1-1}^5$   
p:  $U3 = -0.020 \pm 0.050_{stat} \pm 0.007_{syst}$   
d:  $U3 = -0.021 \pm 0.038_{stat} \pm 0.011_{syst}$



- $U1 \propto \epsilon |U_{10}|^2 + 2|U_{11} + U_{1-1}|^2$   
 $U1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$   
p:  $U1 = 2|U_{11}|^2 = 0.132 \pm 0.026_{st} \pm 0.053_{syst}$   
d:  $U1 = 0.094 \pm 0.020_{st} \pm 0.044_{syst}$   
p+d:  $U1 = 0.109 \pm 0.037_{tot}$
- ⇒ **Indication on hierarchy of  $\rho^0$  UPE amplitudes:**  
 $|U_{11}| \gg |U_{10}| \sim |U_{01}|$

$$A_{UT} = -2 \frac{\text{Im}[\mathcal{M}_{+-,++}^* \mathcal{M}_{++,++} + \epsilon \text{Im}[\mathcal{M}_{0-,0+}^* \mathcal{M}_{0+,0+}]]}{\Sigma_{\nu'} [|\mathcal{M}_{+\nu',++}|^2 + \epsilon |\mathcal{M}_{0\nu',0+}|^2]},$$

$$\mathcal{M}_{\mu,+,+\mu}(V) = \frac{e}{2} \left\{ \sum_a e_a \mathcal{C}_V^{aa} \langle H \rangle_{V\mu}^g + \sum_{ab} \mathcal{C}_V^{ab} \langle H \rangle_{V\mu}^{ab} \right\},$$

$$,-,\mu+(V) = -\frac{e}{2} \frac{\sqrt{(-t)}}{M+m} \left\{ \sum_a e_a \mathcal{C}_V^{aa} \langle E \rangle_{V\mu}^g + \sum_{ab} \mathcal{C}_V^{ab} \langle E \rangle_{V\mu}^{ab} \right\},$$

$$\langle F \rangle_{V\mu}^g = \sum_{\lambda} \int_0^1 d\bar{x} \mathcal{H}_{\mu\lambda,\mu\lambda}^{Vg}(\bar{x}, \xi, Q^2, t=0) F^g(\bar{x}, \xi, t),$$

$$\langle F \rangle_{V\mu}^{ab} = \sum_{\lambda} \int_{-1}^1 d\bar{x} \mathcal{H}_{\mu\lambda,\mu\lambda}^{Vab}(\bar{x}, \xi, Q^2, t=0) F^{ab}(\bar{x}, \xi, t),$$

$$\mathcal{H}_{\mu\lambda,\mu\lambda}^{Vab} = \int d\tau d^2 b \hat{\Psi}_{V\mu}(\tau, -\mathbf{b}) \hat{\mathcal{F}}(\bar{x}, \xi, \tau, Q^2, \mathbf{b})$$

$$\mathbf{x} \alpha_s(\mu_R) \exp[-S(\tau, \mathbf{b}, Q^2)],$$

$$(\tau, \mathbf{k}_\perp) = 8\pi^2 \sqrt{2N_C} f_{Vj}(\mu_F) a_{Vj}^2 [1 + B_1^{Vj}(\mu_F) C_1^{3/2} (2\tau - 1) \\ + B_2^{Vj}(\mu_F) C_2^{3/2} (2\tau - 1)] \exp[-a_{Vj}^2 \mathbf{k}_\perp^2 / (\tau \bar{\tau})].$$

S.V.Goloskokov and P.Kroll

[hep-ph/0809412](#)

Important characteristics of G.K. theory:

Introduce the quark transverse momenta with model regulation :  $\frac{1}{dQ^2} = \frac{1}{dQ^2 + k_\perp^2}$ .

The weight factors comprise the flavor structure of VM:

$$C_\omega^{uu} = C_\omega^{dd} = \frac{1}{\sqrt{2}}, C_\phi^{ss} = 1,$$

F(=H,E),

$\hat{F}$  - hard scattering kernel

Sudakov effect in b space.

Parameters of wave function.