

# Exclusive meson production at HERMES

S. I. Manaenkov,

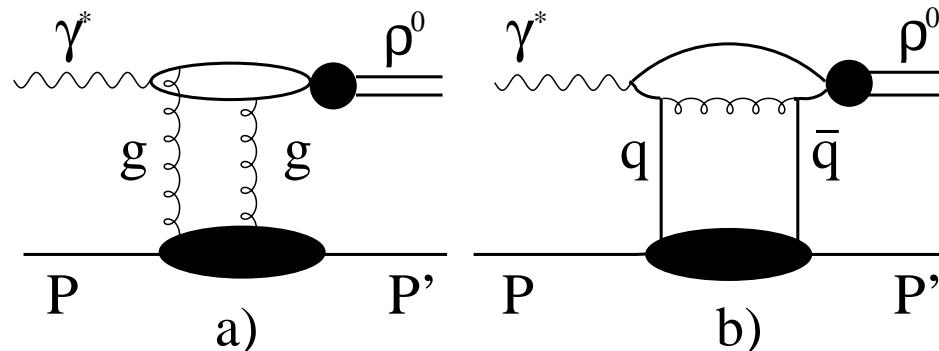
NRC "Kurchatov Institute", Petersburg Nuclear Physics Institute,  
on behalf of the HERMES Collaboration

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- Physics Motivation
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- Summary

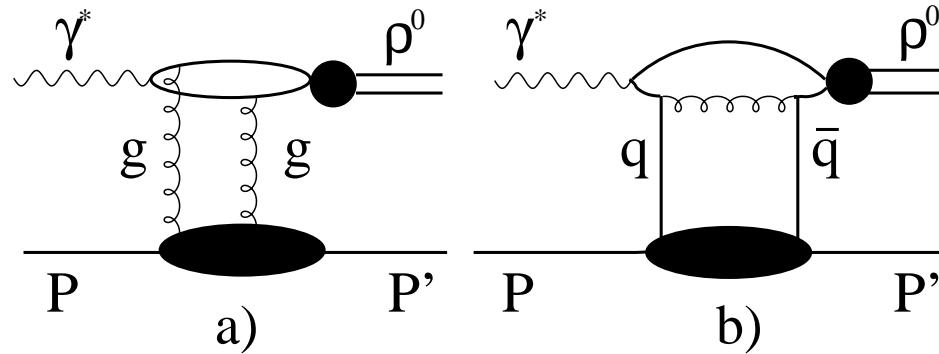
# Physics Motivation



- $\gamma^* + N \rightarrow V + N$  is a perfect reaction to study both vector-meson ( $V = \rho^0, \phi, \omega, \dots$ ) production mechanism and hadron (nucleon) structure.
- Properties of Spin-Density Matrix Elements (SDMEs).  
SDMEs are coefficients in the angular distribution of final particles and therefore can be extracted from data.  
SDMEs are expressible in terms of ratios of helicity amplitudes of  $\gamma^* + N \rightarrow V + N$  reaction, hence ratios can be obtained from angular distribution of final particles.
- Generalized Parton Distributions (GPDs) of the nucleon can be obtained from the amplitude  $F_{00} \equiv F_{0\frac{1}{2}0\frac{1}{2}} (\gamma_L \rightarrow V_L)$  for which factorization theorem is proved.  
GPDs permit to calculate the contribution of the total angular momentum of a quark of some flavour or gluon to the nucleon spin (Ji's sum rule).

# Physics Motivation

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- Generalized Parton Distributions (GPDs)

Quark GPDs:  $H_q(x, \xi, t)$ ,  $\tilde{H}_q(x, \xi, t)$ ,  $E_q(x, \xi, t)$ ,  $\tilde{E}_q(x, \xi, t)$ .

Gluon GPDs:  $H_g(x, \xi, t)$ ,  $\tilde{H}_g(x, \xi, t)$ ,  $E_g(x, \xi, t)$ ,  $\tilde{E}_g(x, \xi, t)$ .

$H_{q,g}$  and  $\tilde{H}_{q,g}$  can be obtained from nucleon helicity non-flip amplitudes ( $\lambda_N = \lambda'_N$ ).

$E_{q,g}$  and  $\tilde{E}_{q,g}$  can be extracted from nucleon helicity-flip amplitudes ( $\lambda_N \neq \lambda'_N$ ).

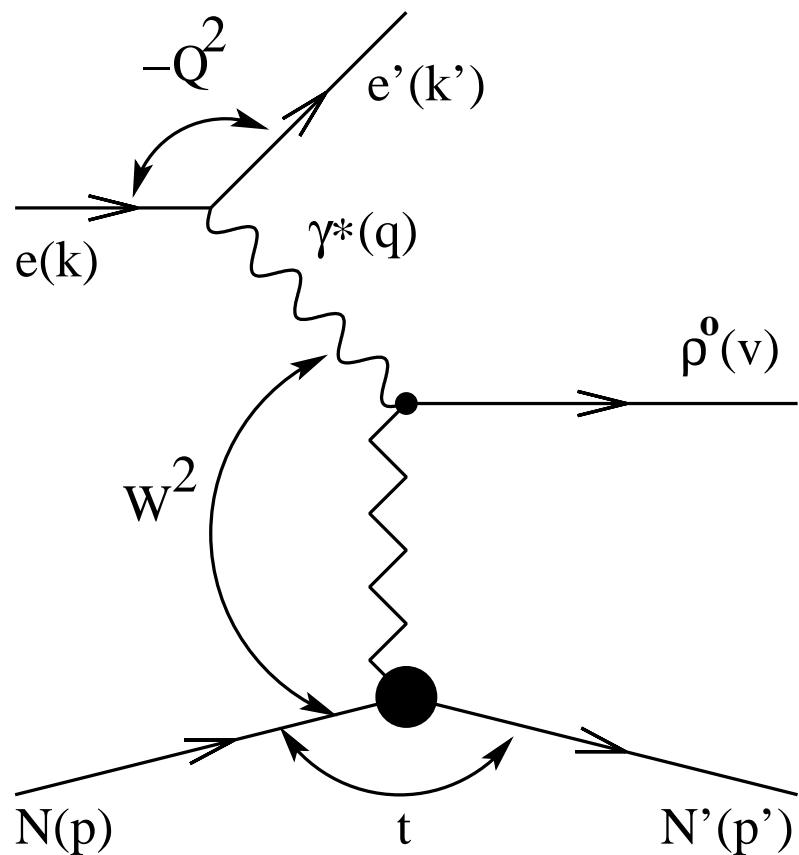
- Ji's Sum Rules

$$\frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t \rightarrow 0) + E^q(x, \xi, t \rightarrow 0)] = \langle J_q \rangle,$$

$$\int_{-1}^1 dx x [H^g(x, \xi, t \rightarrow 0) + E^g(x, \xi, t \rightarrow 0)] = \langle J_g \rangle.$$

To use the Ji's sum rules  $E^q(x, \xi, t \rightarrow 0)$  is to be extracted from data on polarized targets at  $t \neq 0$ .

## Phenomenological description of reaction $e + N \rightarrow e' + V + N'$



$$e(\lambda) \rightarrow e'(\lambda') + \gamma^*(\lambda_\gamma), \\ \gamma^*(\lambda_\gamma) + N(\lambda_N) \rightarrow V(\lambda_V) + N'(\lambda'_N);$$

$$S_{fi} = \sum_{\lambda_\gamma} \langle k' \lambda' | j_{(l)}^\mu | k \lambda \rangle e_\mu^{*(\lambda_\gamma)}$$

$$e_\sigma^{(\lambda_\gamma)} (-1)^{\lambda_\gamma} \langle v \lambda_V p' \lambda'_N | J_{(h)}^\sigma | p \lambda_N \rangle / q^2;$$

$$\langle k' \lambda' | j_{(l)}^\mu | k \lambda \rangle = \bar{u}(k', \lambda') \gamma^\mu u(k, \lambda);$$

$$F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N}$$

$$= (-1)^{\lambda_\gamma} \langle v \lambda_V p' \lambda'_N | J_{(h)}^\sigma | p \lambda_N \rangle e_\sigma^{(\lambda_\gamma)}.$$

# Phenomenological description of reaction $e + N \rightarrow e' + V + N'$

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- First process  $e \rightarrow e + \gamma^*$  (QED). Spin-density matrix of virtual photon  $\rho_{\lambda\gamma\lambda'\gamma}$ .
- Second process  $\gamma^* + N \rightarrow V + N$  (QCD). Helicity amplitudes  $F_{\lambda_V\lambda'_N\lambda_\gamma\lambda_N}$ .  
Spin-Density Matrix of  $V$ :  $r = \frac{F\rho F^+}{\mathcal{N}}$ .  $\rho = \sum (c_\alpha \Sigma^\alpha)$ ,  $r^\alpha = \frac{F\Sigma^\alpha F^+}{\mathcal{N}}$ ,  $r = \sum c_\alpha r^\alpha$ .
- Third process. Examples: i)  $V = \omega$ ;  $\omega \rightarrow \pi^+ + \pi^- + \pi^0$  ( $\rightarrow \gamma + \gamma$ ).  
 $\omega$ :  $J^P = 1^-$ ,  $P(3\pi) = -1$ , orbital motion  $1^+$ :  $Y_{1\lambda_\omega}(\vec{n})$ ,  $\vec{n}$  is a unit normal to  $\omega$ -decay plane;  
ii)  $V = \rho$ ;  $J^P = 1^-$ ,  $P(2\pi) = +1$ ,  $Y_{1\lambda_\rho}(\vec{n})$ ,  $\vec{n} = \vec{p}_{\pi^+}/|\vec{p}_{\pi^+}|$ .
- Spin-Density Matrix Elements (SDMEs)  $r_{\lambda_V\lambda'_V}$  of the vector meson are extracted from the angular distribution of final particles

$$\mathcal{W}(\Phi, \Theta, \phi) = \sum_{\lambda_V, \lambda'_V} Y_{1\lambda_V}(\vec{n}) r_{\lambda_V\lambda'_V} Y_{1\lambda'_V}^*(\vec{n}) = \sum_{\lambda_V, \lambda'_V} Y_{1\lambda_V}(\Theta, \phi) r_{\lambda_V\lambda'_V}(\Phi) Y_{1\lambda'_V}^*(\Theta, \phi).$$

- Quantities (SDMEs)  $r_{\lambda_V\lambda'_V}^\alpha$  can be calculated from the relation

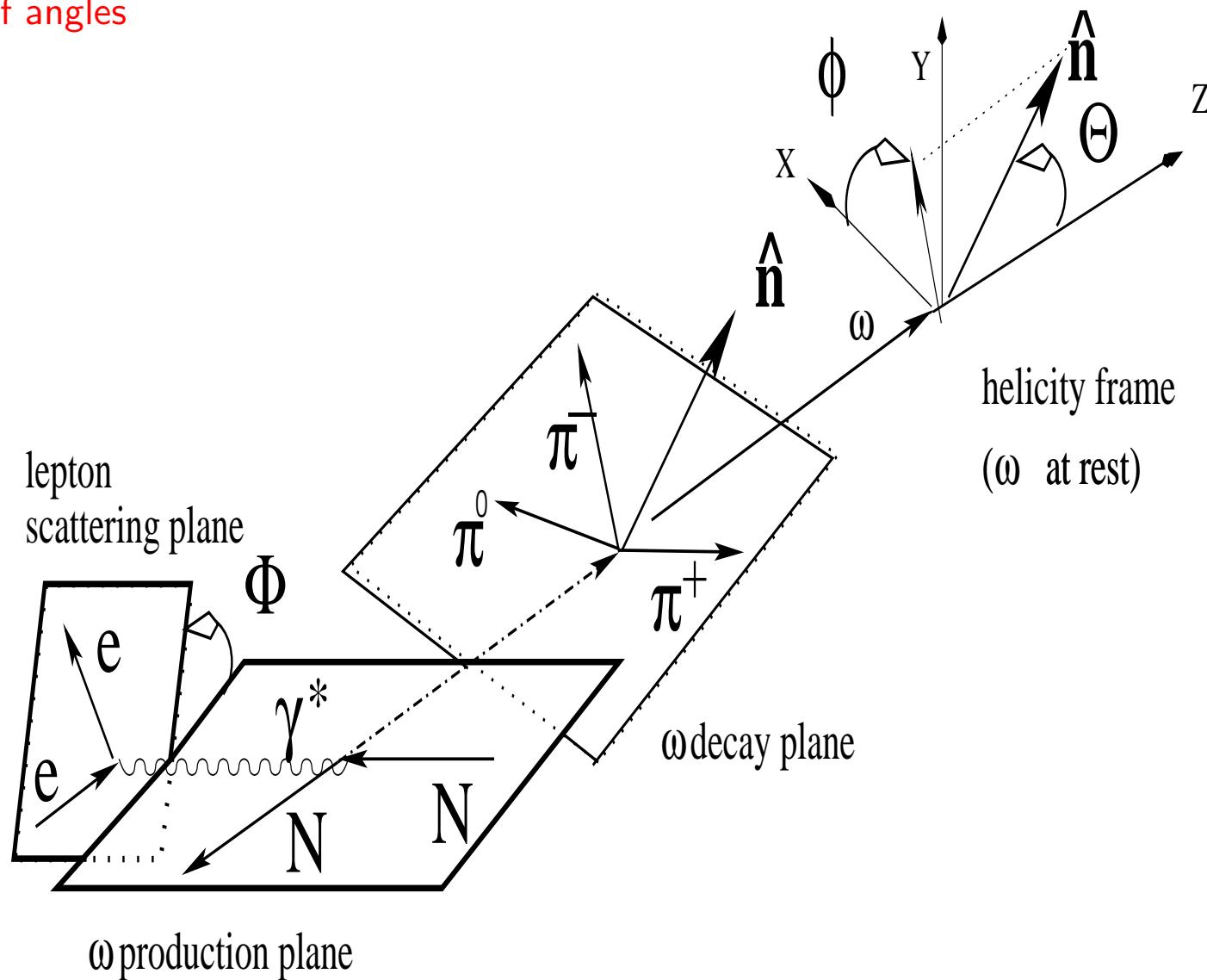
$$r_{\lambda_V\lambda'_V}^\alpha = \frac{1}{2\mathcal{N}\alpha} \sum F_{\lambda_V\lambda'_N\lambda_\gamma\lambda_N} \Sigma_{\lambda_\gamma\lambda'_\gamma}^\alpha F_{\lambda'_V\lambda'_N\lambda'_\gamma\lambda_N}^*,$$

where  $\Sigma^\alpha$  is a set of nine hermitian matrixes:

$$\Sigma^0 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \Sigma^1 = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}, \quad \Sigma^5 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix}, \dots$$

# Phenomenological description of reaction $e + N \rightarrow e' + V + N'$

- Definition of angles



# The HERMES Experiment

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## $\omega$ -meson production

- Longitudinally polarized electron/positron beam with energy of 27.6 GeV.
- Momentum resolution  $\Delta P/P < 1.5\%$ . Efficiency of electron identification 98%.
- Only three tracks of charged particles in any event, two calorimeter clusters ( $\gamma, \gamma$ ).
- Energy of scattered electron (positron)  $E'_e > 3.5$  GeV.
- $6.3 \text{ GeV} > W > 3.0 \text{ GeV}$ ,  $Q^2 > 1 \text{ GeV}^2$ ,  $-t' = -(t - t_{max}) < 0.2 \text{ GeV}^2$ .
- Recoil nucleon was not detected. Missing mass criterion was used.

$$\Delta E = \frac{M_X^2 - M_p^2}{2M_p}; \quad -1.0 \text{ GeV} < \Delta E < 0.8 \text{ GeV};$$

$M_X$  ( $M_p$ ) mass of recoil system (proton).

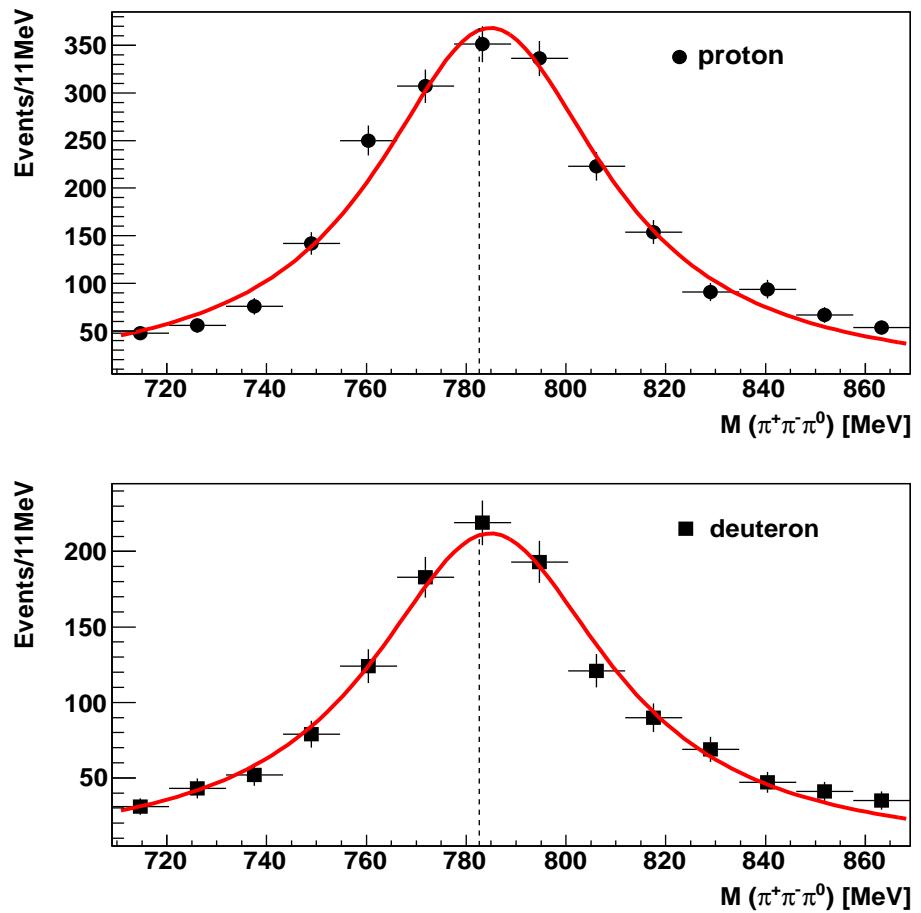
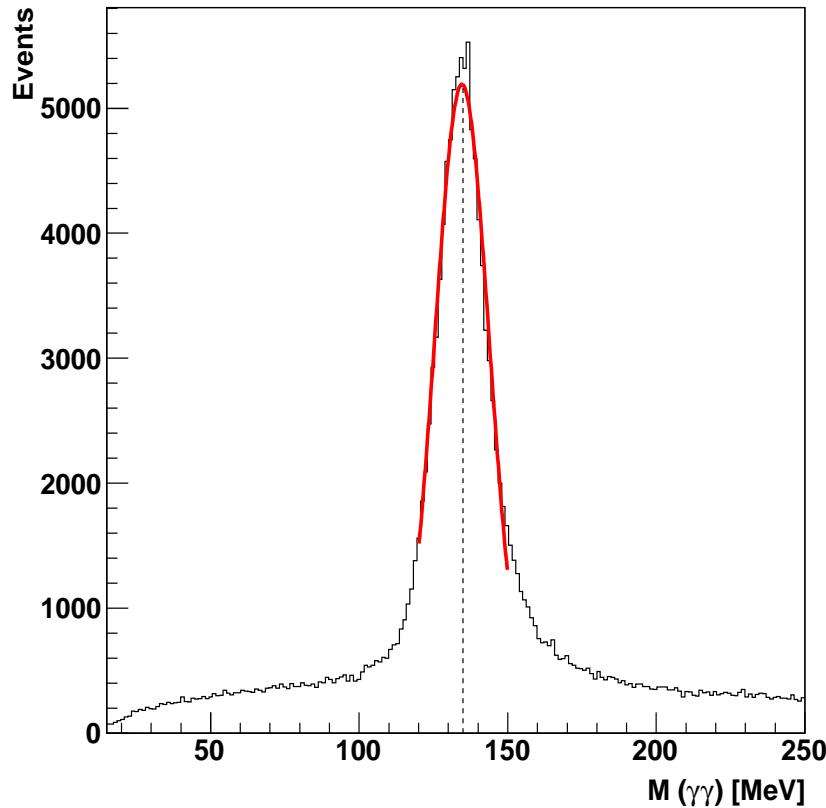
- $0.11 \text{ GeV} < M(\gamma\gamma) < 0.16 \text{ GeV}$ ;  $0.71 \text{ GeV} < M(\pi^+\pi^-\pi^0) < 0.87 \text{ GeV}$ .
- $16\% < \text{fraction of background} < 26\%$  for increasing  $-t'$ .
- 2260 events with exclusive  $\omega$  meson produced on unpolarized proton and 1332 on deuteron were accumulated in 1996 - 2007 years.
- A. Airapetian et al. (the HERMES Collaboration), Eur. Phys. J. C74, (2014) 3110.
- 279 exclusively produced  $\omega$  mesons with unpolarized beam on transversely polarized proton ( $|\vec{S}_\perp| \approx 0.72$ ) in 2002 - 2007 years.
- A. Airapetian et al. (the HERMES Collaboration), Eur. Phys. J. C75 (2015) 600.

## $\rho$ -meson production

- 8741 events with exclusive  $\rho$ -mesons produced with unpolarized and longitudinally polarized beam on transversely polarized proton ( $|\vec{S}_\perp| \approx 0.72$ ) for  $-t' \leq 0.4 \text{ GeV}^2$  in 2002 - 2005 years.  
 $0.6 \text{ GeV} < M(\pi^+\pi^-) < 1.0 \text{ GeV}$ .

# The HERMES Experiment

- Mass distributions for  $\pi^0$  and  $\omega$  decays



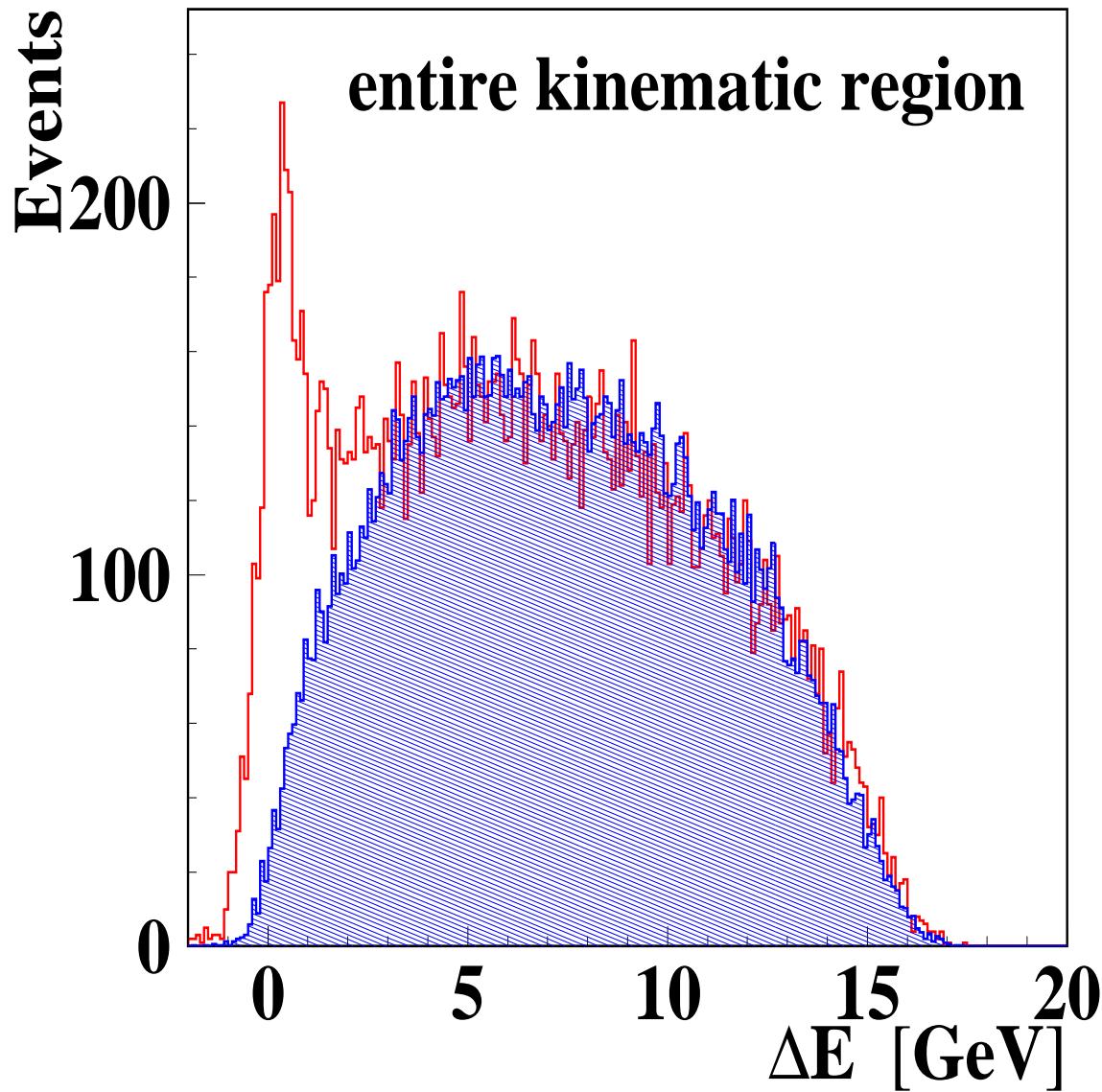
Left panel:  $\gamma\gamma$  mass distribution for  $\pi^0$  decay ( $m_{\pi^0} = 134.7 \pm 19.9$  MeV).

Right panel:  $\pi^+, \pi^-, \pi^0$  mass distribution for  $\omega$  decay.

$M_\omega = 784.8 \pm 55.8$  MeV (proton target),

$M_\omega = 784.6 \pm 58.2$  MeV (deuteron target).

$\Delta E$  distribution for  $\omega$  meson production



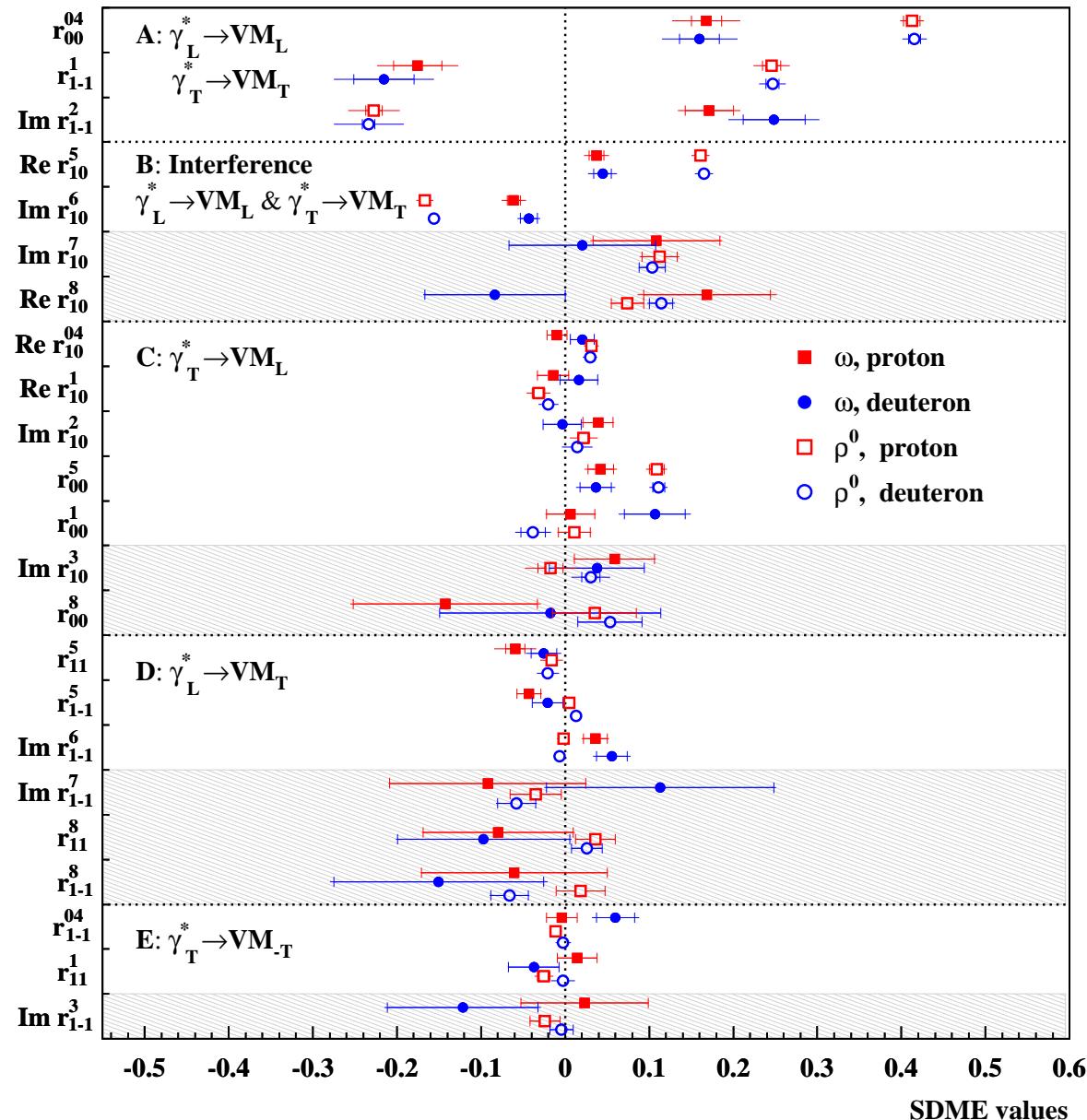
$$\Delta E = \frac{M_X^2 - M_p^2}{2M_p}. \quad M_X \text{ and } M_p \text{ are masses of recoil system and proton, respectively.}$$

# Results on Spin-Density Matrix Elements

- S-Channel Helicity Conservation (SCHC):  
helicity amplitudes with  $\lambda_V = \lambda_\gamma$  are dominant ( $T_{00}$ ,  $T_{11}$ ,  $U_{11}$ ).  
 $T_{\lambda_V \mu_N \lambda_\gamma \lambda_N}$  is Natural Parity Exchange (NPE) amplitude.  
 $U_{\lambda_V \mu_N \lambda_\gamma \lambda_N}$  is Unnatural Parity Exchange (UPE) amplitude.  
$$T_{\lambda_V \mu_N \lambda_\gamma \lambda_N} = \left[ F_{\lambda_V \mu_N \lambda_\gamma \lambda_N} + (-1)^{\mu_N - \lambda_N} F_{\lambda_V - \mu_N \lambda_\gamma - \lambda_N} \right] / 2,$$
$$U_{\lambda_V \mu_N \lambda_\gamma \lambda_N} = \left[ F_{\lambda_V \mu_N \lambda_\gamma \lambda_N} - (-1)^{\mu_N - \lambda_N} F_{\lambda_V - \mu_N \lambda_\gamma - \lambda_N} \right] / 2,$$
- Class A of SDMEs: Main terms proportional to  $|T_{00}|^2$  or  $|T_{11}|^2$ .  
Class B: Main terms proportional to  $\text{Re}[T_{00} T_{11}^*]$  or  $\text{Im}[T_{00} T_{11}^*]$ .  
Class C: Main terms proportional to  $T_{01}$  ( $\sim \sqrt{-t'}/M_p$  at small  $-t'$ ).  
Class D: Main terms proportional to  $T_{10}$  ( $\sim \sqrt{-t'}/M_p$  at small  $-t'$ ).  
Class E: Main terms proportional to  $T_{1-1}$  ( $-t'/M_p^2$  at small  $-t'$ ).  
If SCHC is valid all elements of classes C, D, E are zero.
- Check of SCHC relations for Class-A and B SDMEs for the proton  
 $r_{1-1}^1 + \text{Im}[r_{1-1}^2] = -0.004 \pm 0.038 \pm 0.015$ ,  
 $\text{Re}[r_{10}^5] + \text{Im}[r_{10}^6] = -0.024 \pm 0.013 \pm 0.004$ ,  
 $\text{Im}[r_{10}^7] - \text{Re}[r_{10}^8] = -0.060 \pm 0.100 \pm 0.018$ ,  
and deuteron  
 $r_{1-1}^1 + \text{Im}[r_{1-1}^2] = 0.033 \pm 0.049 \pm 0.016$ ,  
 $\text{Re}[r_{10}^5] + \text{Im}[r_{10}^6] = 0.001 \pm 0.016 \pm 0.005$ ,  
 $\text{Im}[r_{10}^7] - \text{Re}[r_{10}^8] = 0.104 \pm 0.110 \pm 0.023$ .

# Results on Spin-Density Matrix Elements

- Comparison of results for  $\omega$  and  $\rho^0$  mesons for entire kinematic region



"Polarized" SDMEs (shaded areas) are measured by HERMES for the first time.

# Results on Spin-Density Matrix Elements

- Enigma of the  $\rho - \omega$  difference for class A SDMEs

$$\text{Im}\{r_{1-1}^2\} - r_{1-1}^1 = \frac{1}{N}(-|T_{1\frac{1}{2}1\frac{1}{2}}|^2 - |T_{1-\frac{1}{2}1\frac{1}{2}}|^2 + |U_{1\frac{1}{2}1\frac{1}{2}}|^2 + |U_{1-\frac{1}{2}1\frac{1}{2}}|^2) > 0.???$$

$T_{\lambda V^\mu N^\lambda \gamma^\lambda N}$  is Natural Parity Exchange (NPE) amplitude.

$U_{\lambda V^\mu N^\lambda \gamma^\lambda N}$  is Unnatural Parity Exchange (UPE) amplitude.

In Regge Phenomenology, NPE amplitudes are due to exchanges of Pomeron,  $\rho$ ,  $\omega$ ,  $f_2$ ,  $a_2$ , ... reggeons with natural parity ( $J^P = 0^+, 1^-, 2^+$ , ...).

UPE amplitudes are due to exchanges of  $\pi$ ,  $a_1$ , ... reggeons with unnatural parity ( $J^P = 0^-, 1^+, 2^-$ , ...).

Pion exchange at intermediate  $W$  and  $Q^2$ .

Vertices  $\gamma\omega\pi$  and  $\pi NN$  are big  $\Rightarrow |U_{11}| > |T_{11}|$  Dominant UPE contribution.

- How to make the  $U_{11}$  amplitude large (dominant) at large  $Q^2$ ?

First step: hard  $\rho^0$  production (big  $Q^2$ ).

Modulus of amplitude  $|T_{11}(\gamma + N \rightarrow \rho^0 + N)| > |T_{11}(\gamma + N \rightarrow \omega + N)|$ .

Second step: pion exchange in final state  $\rho^0 + N \rightarrow \omega + N$ .

$\rho^0 \rightarrow \omega + \pi^0$ ,  $\pi^0 + N \rightarrow N$ . Vertices  $\rho^0\omega\pi$  and  $\pi NN$  are big.

Peripherical pion exchange (soft) is combined with hard  $\rho^0$  production at high  $Q^2$ .

- Factorization theorem

FT is proved for  $T_{00}$  ( $\gamma_L \rightarrow V_L$ ) only.  $U_{00} \equiv 0$ .

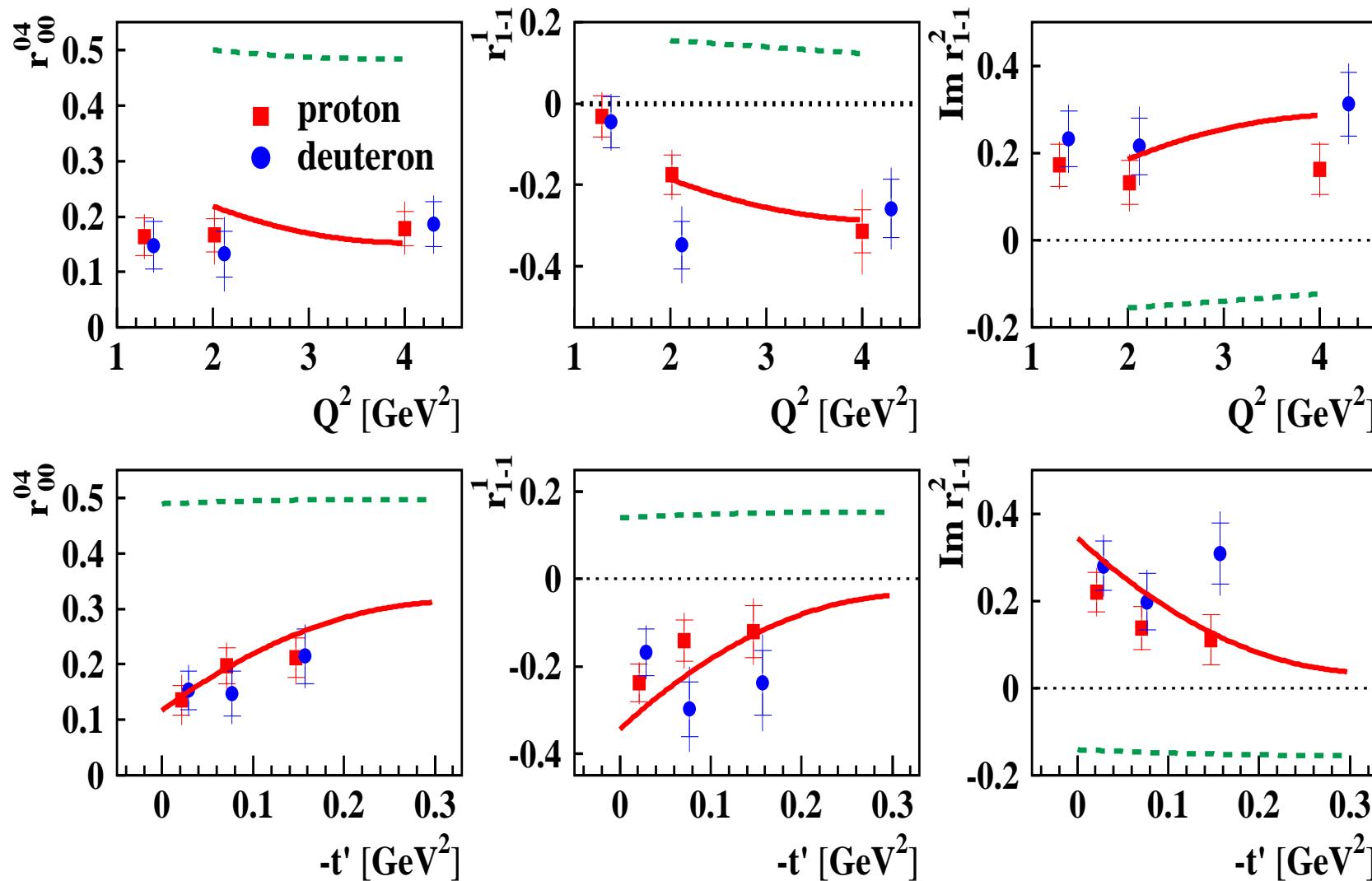
Ivanov-Kirshner:  $|F_{00}/F_{11}| \propto Q$  at  $Q \rightarrow \infty$ .  $F_{00} = T_{00}$ ,  $F_{11} = T_{11} + U_{11}$ .

It is true for the "direct" amplitudes without final state interaction.

Fractional contribution of pion exchange goes to zero at  $W \rightarrow \infty$ .

# Kinematic Dependences of SDMEs

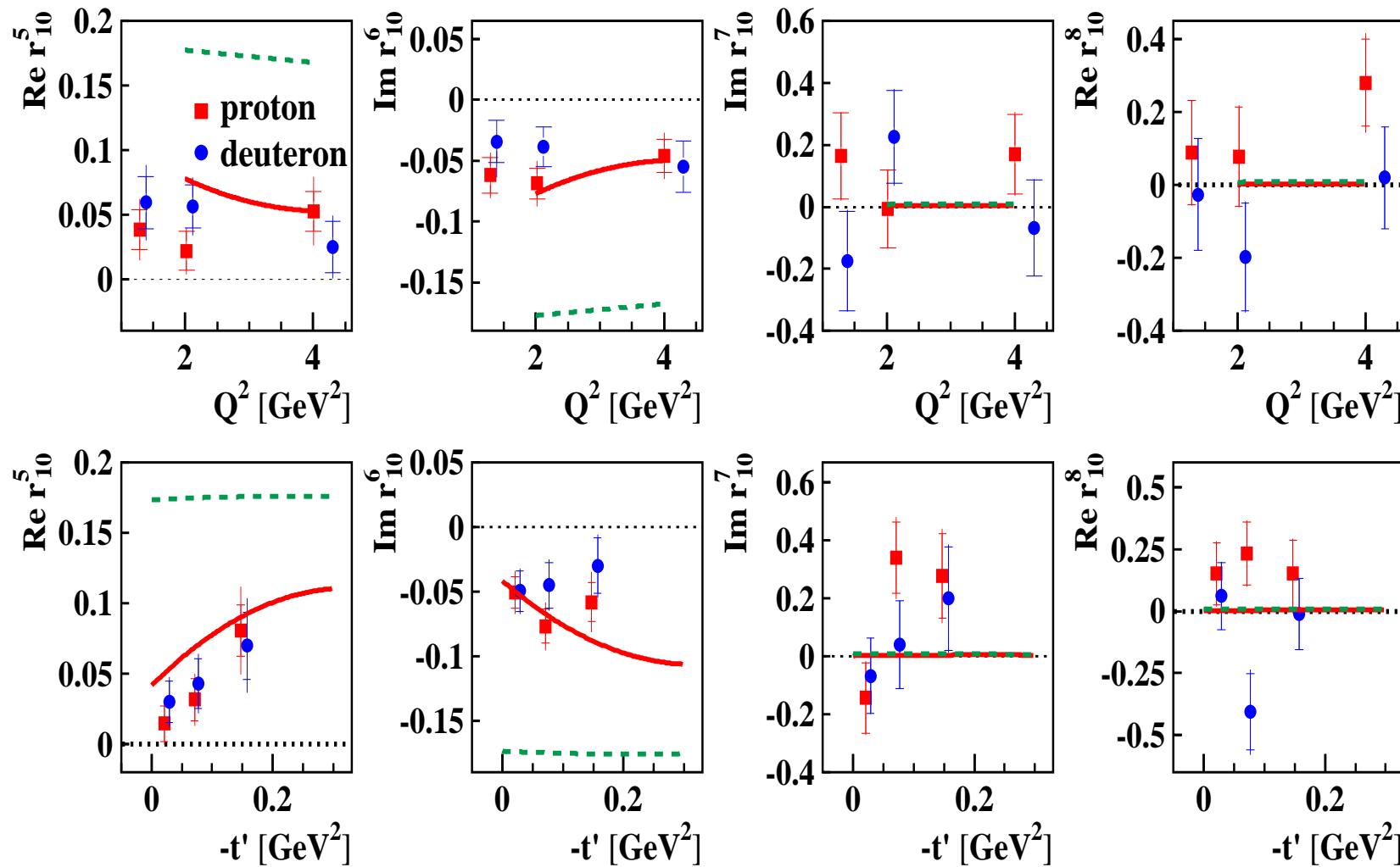
- Kinematic dependences of class-A SDMEs



Red solid (green dashed) curves are obtained with (without) pion pole contribution in the Goloskokov-Kroll model.

# Kinematic Dependences of SDMEs

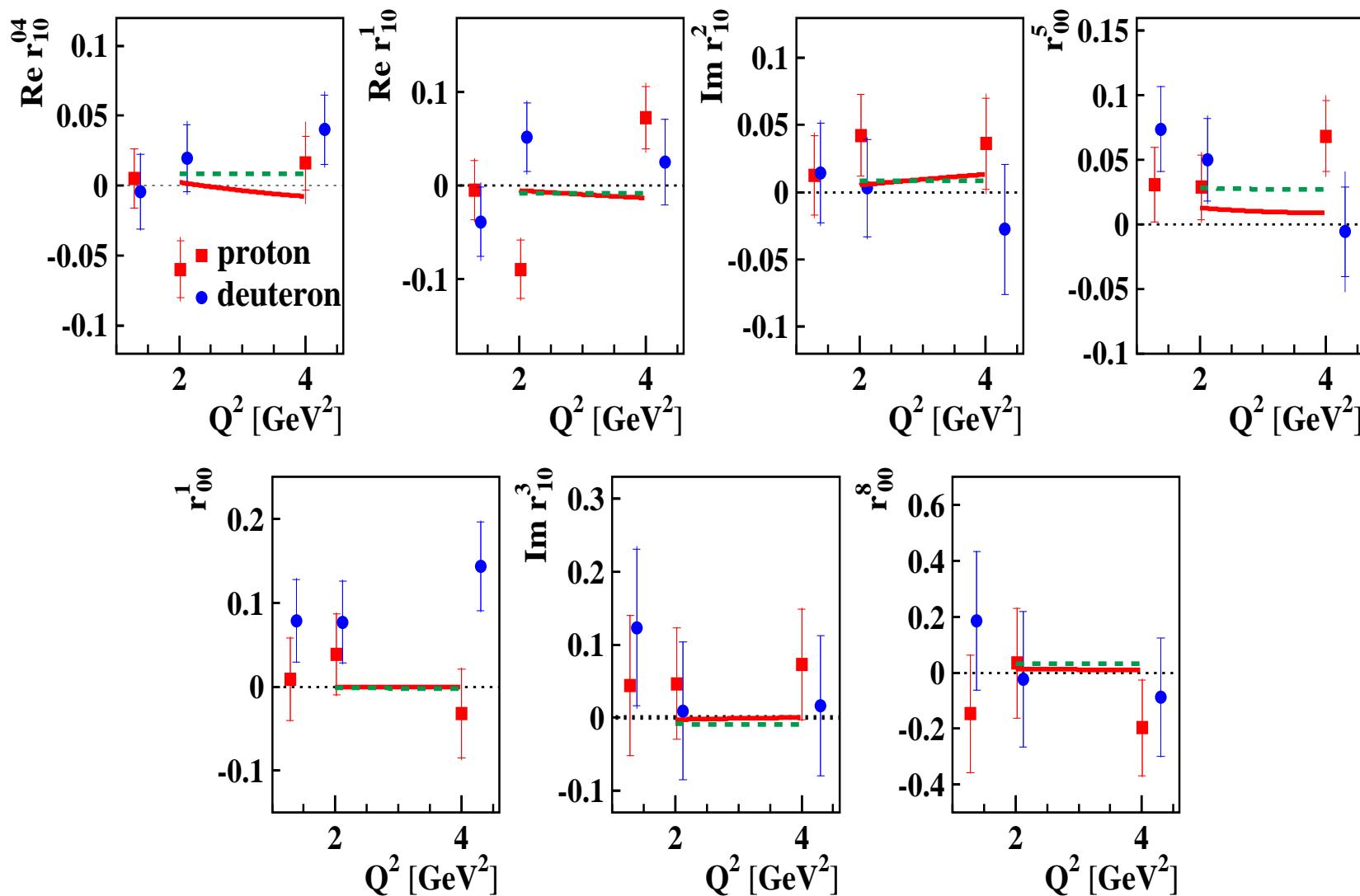
- Kinematic dependences of class-B SDMEs



Red solid (green dashed) curves are obtained with (without) pion pole contribution  
in the Goloskokov-Kroll model.

# Kinematic Dependences of SDMEs

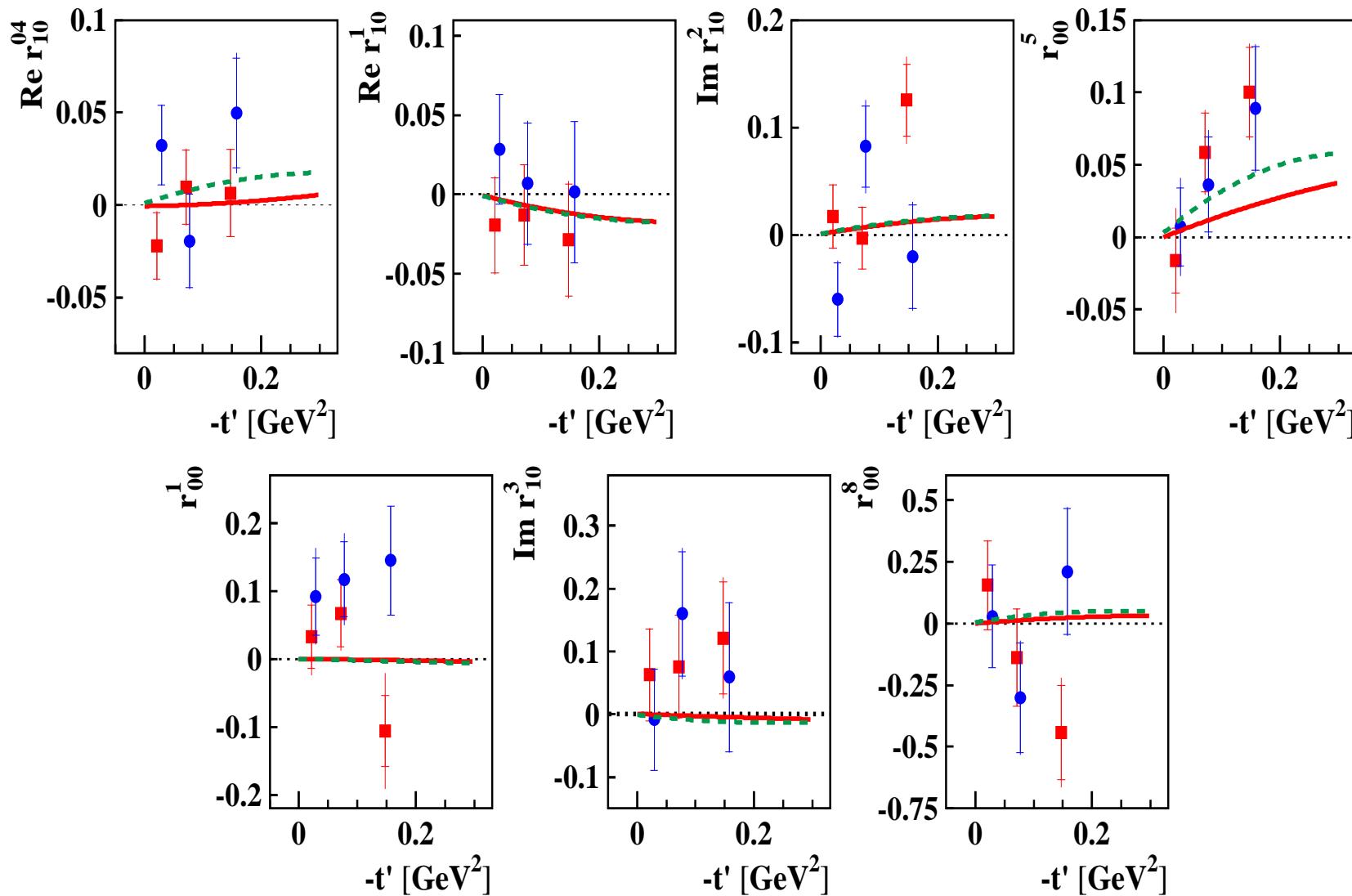
- Kinematic dependences of class-C SDMEs



Red solid (green dashed) curves are obtained with (without) pion pole contribution in the Goloskokov-Kroll model.

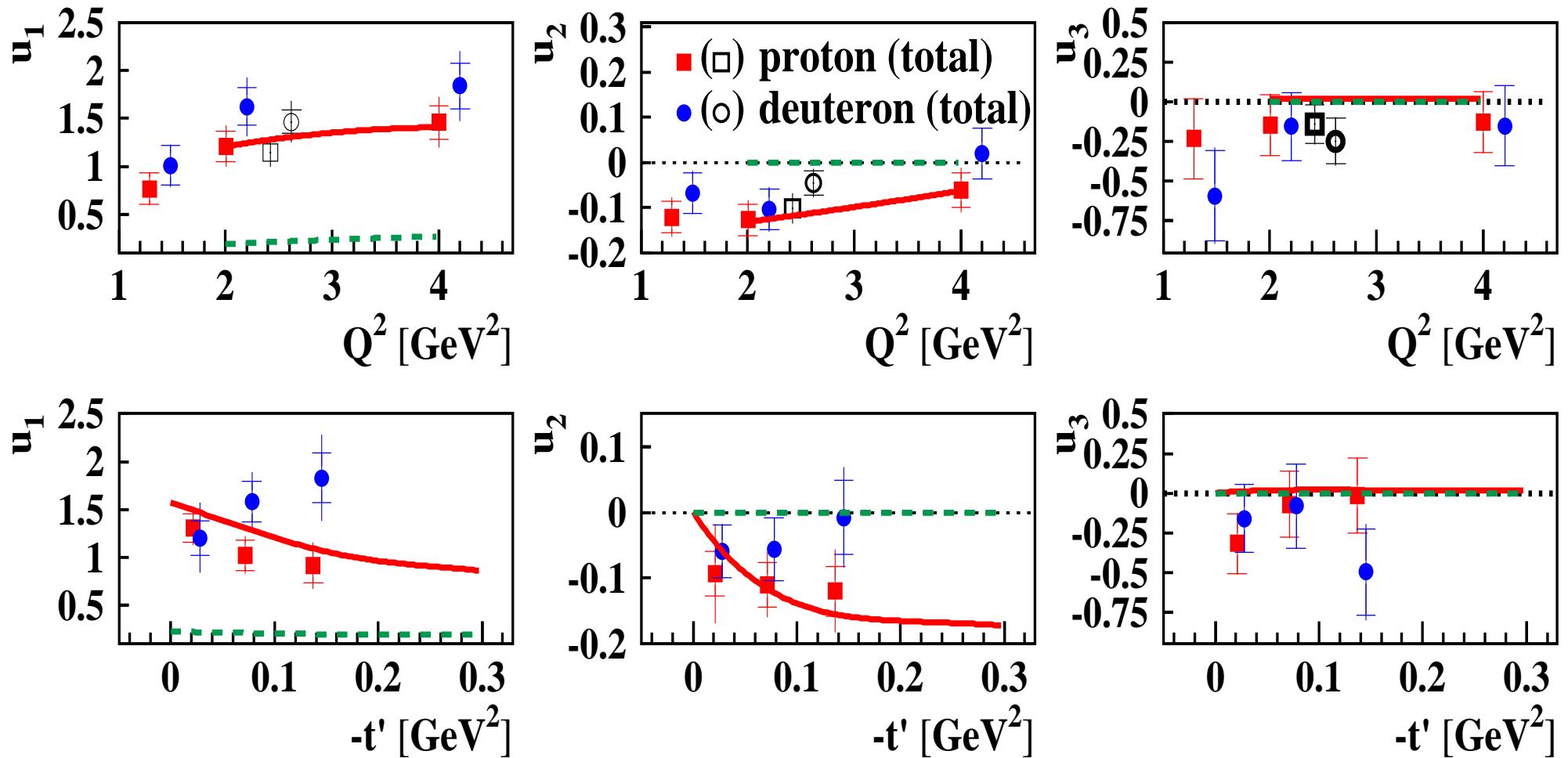
# Kinematic Dependences of SDMEs

- Kinematic dependences of class-C SDMEs



Red solid (green dashed) curves are obtained with (without) pion pole contribution in the Goloskokov-Kroll model.

# Test of Unnatural-Parity Exchange



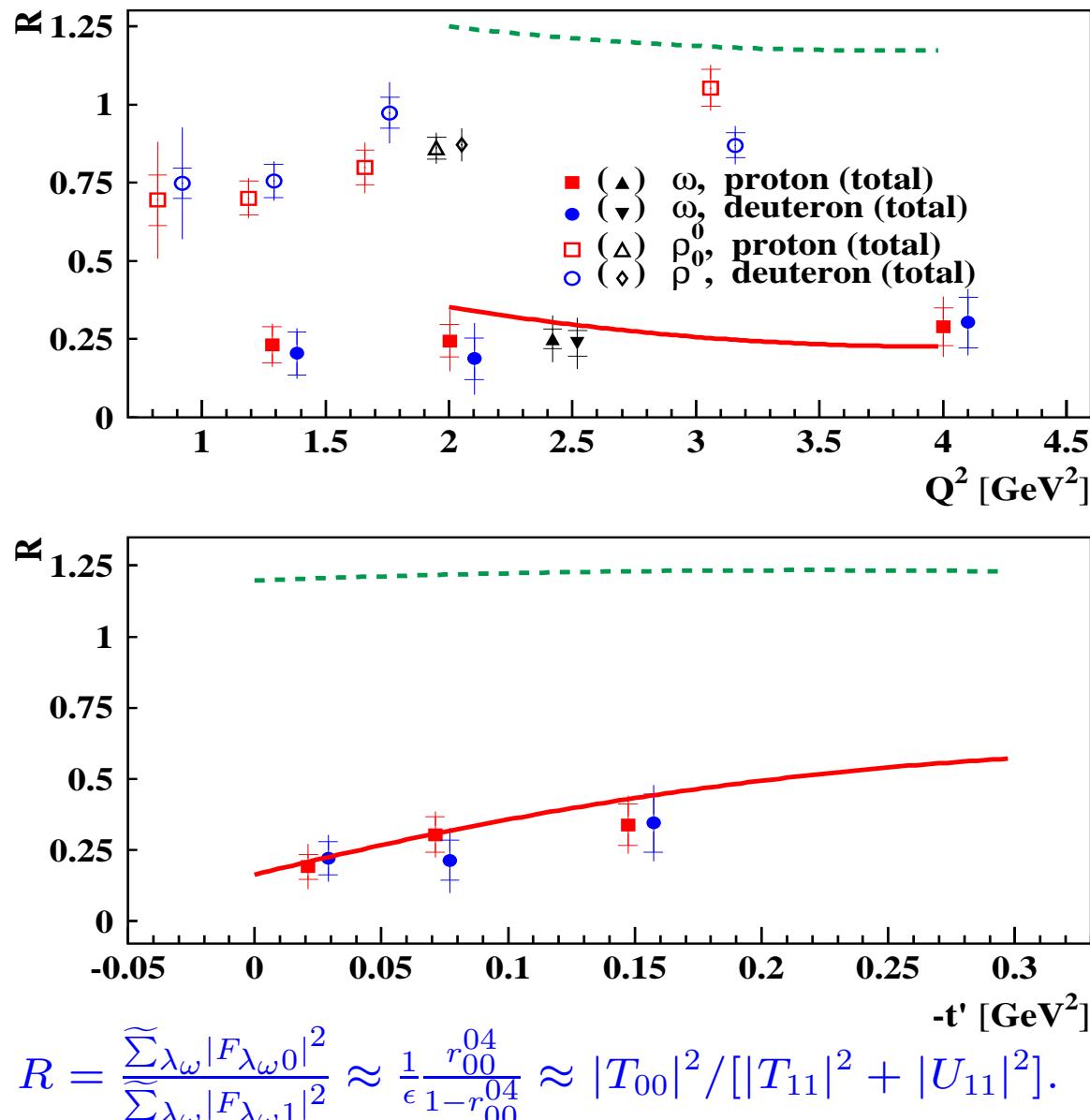
$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1, \quad u_1 = \sum \frac{4\epsilon|U_{10}|^2 + 2|U_{11} + U_{-11}|^2}{N}, \quad \epsilon = \frac{n_L^\gamma}{n_T^\gamma} \approx 0.8,$$

$$u_2 = r_{11}^5 + r_{1-1}^5, \quad u_3 = r_{11}^8 + r_{1-1}^8, \quad u_2 + iu_3 = \sqrt{2} \sum \frac{(U_{11} + U_{-11})U_{10}^*}{N}.$$

Red solid (green dashed) curves are obtained with (without) pion pole contribution in the Goloskokov-Kroll model.

# Longitudinal-to-Transverse Cross-Section Ratio

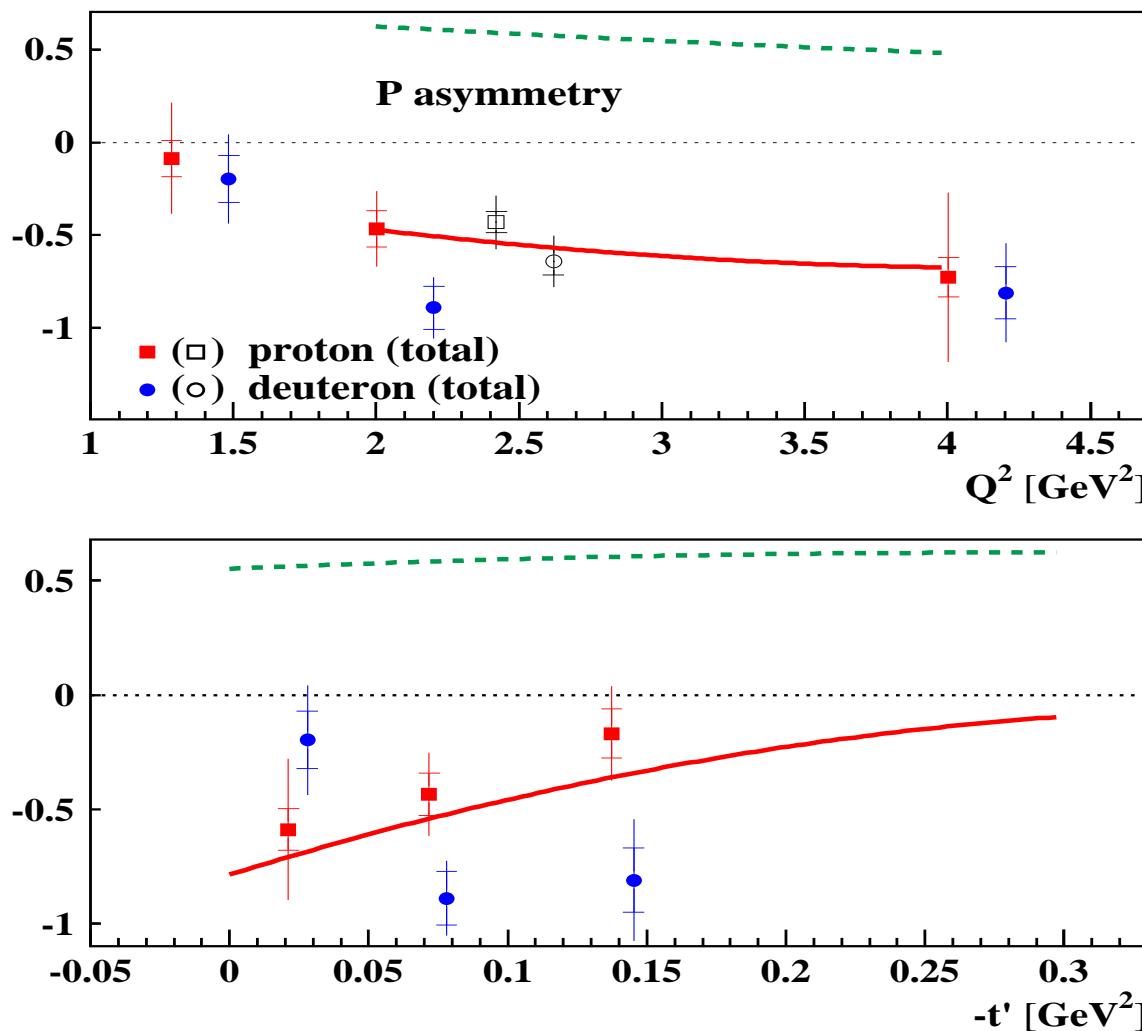
Kinematic dependence of  $R = d\sigma_L/d\sigma_T$



$$R = \frac{\sum_{\lambda\omega} |F_{\lambda\omega 0}|^2}{\sum_{\lambda\omega} |F_{\lambda\omega 1}|^2} \approx \frac{r_{00}^{04}}{\epsilon_1 r_{00}^{04}} \approx |T_{00}|^2 / [|T_{11}|^2 + |U_{11}|^2].$$

Curves show result of Goloskokov-Kroll calculations.

# UPE-to-NPE Asymmetry

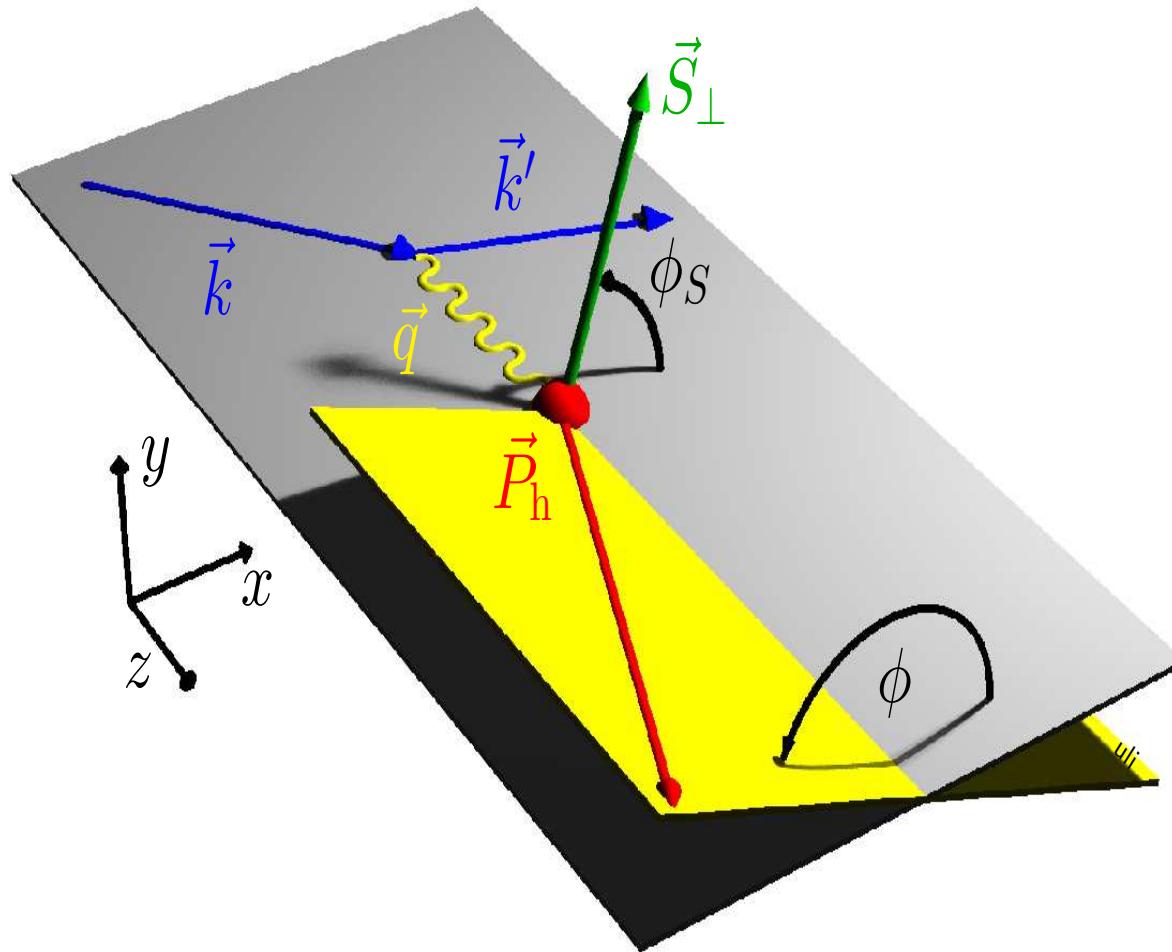


$$P = \frac{d\sigma_T^N - d\sigma_T^U}{d\sigma_T^N + d\sigma_T^U} \approx \frac{2r_{1-1}^1 - r_{00}^1}{1 - r_{00}^{04}}$$

Curves show result of Goloskokov-Kroll calculations.

# Transverse-Target-Spin Asymmetry

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Definition of Angles  $\phi$  and  $\phi_S$

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# Transverse-Target-Spin Asymmetry

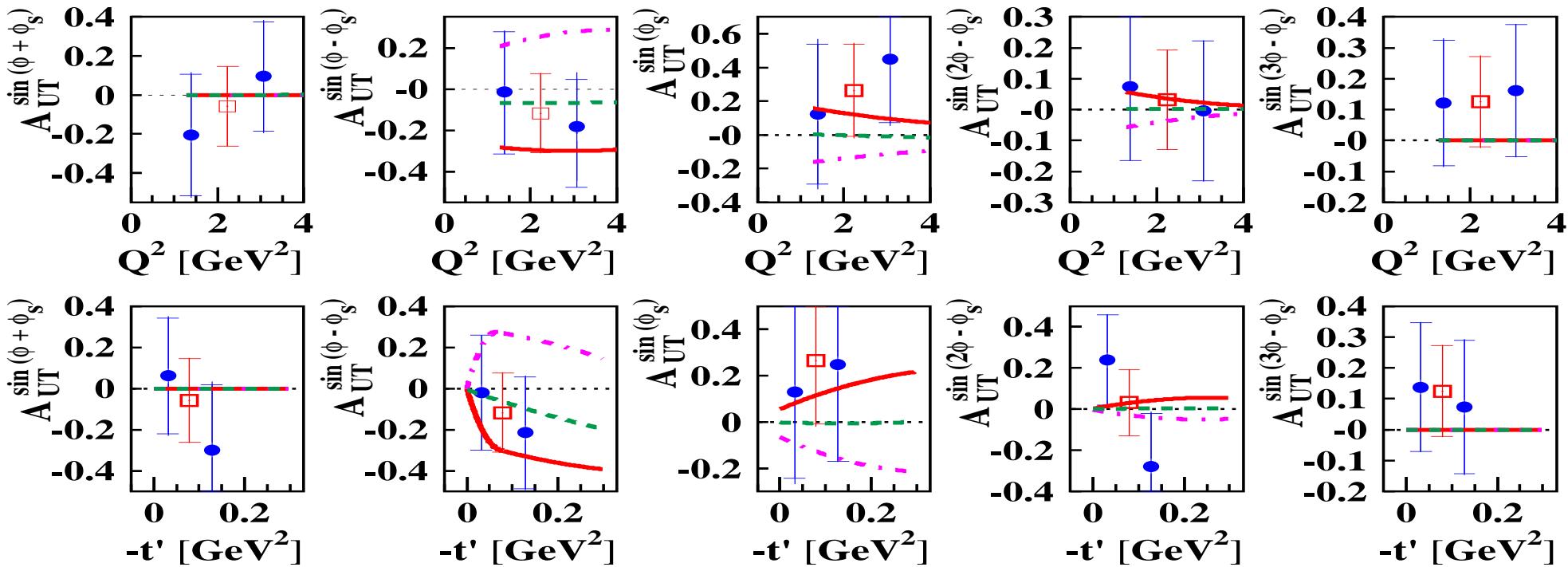
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Definition of asymmetry amplitudes

$$\begin{aligned}\mathcal{W}(\phi, \phi_S) = & 1 + A_{UU}^{\cos(\phi)} \cos(\phi) + A_{UU}^{\cos(2\phi)} \cos(2\phi) \\ & + S_\perp [A_{UT}^{\sin(\phi+\phi_S)} \sin(\phi + \phi_S) \\ & + A_{UT}^{\sin(\phi-\phi_S)} \sin(\phi - \phi_S) \\ & + A_{UT}^{\sin(\phi_S)} \sin(\phi_S) \\ & + A_{UT}^{\sin(2\phi-\phi_S)} \sin(2\phi - \phi_S) \\ & + A_{UT}^{\sin(3\phi-\phi_S)} \sin(3\phi - \phi_S)].\end{aligned}$$

# Transverse-Target-Spin Asymmetry

Asymmetry for total sctatistics

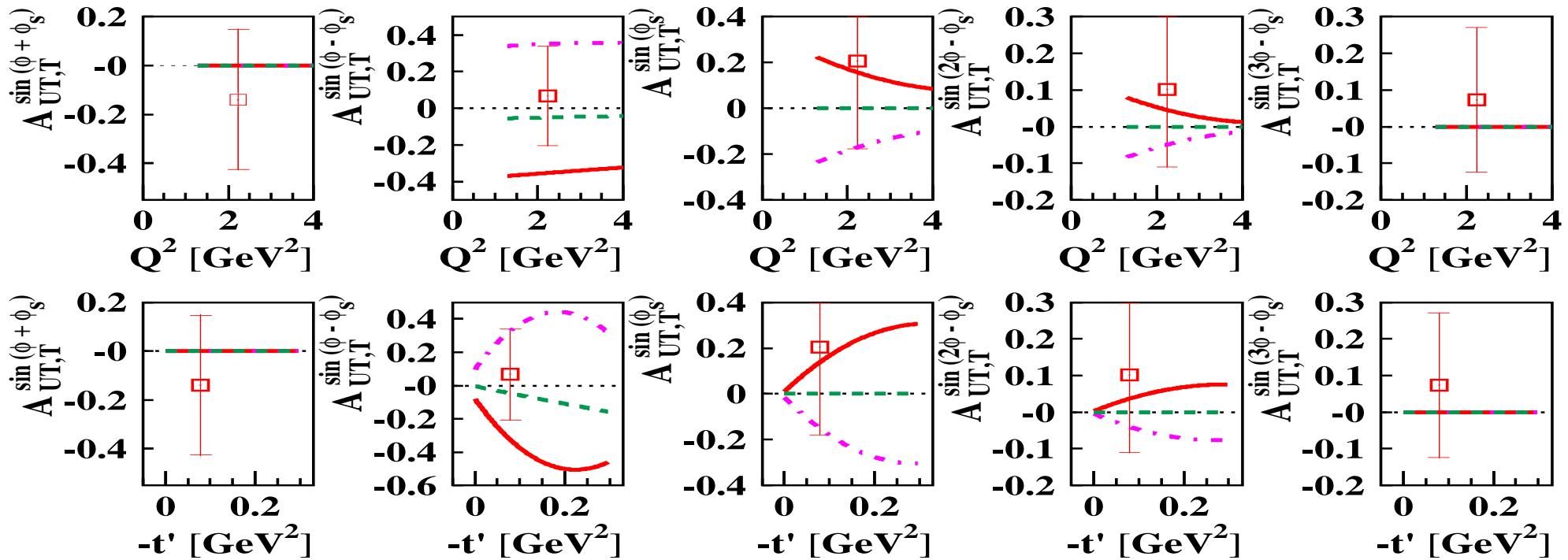


Curves show results of Goloskokov-Kroll calculations: solid (dash-dotted) lines for positive (negative)  $\pi\omega$  transition form factor, dashed lines are obtained without pion exchange contribution.

Open squares show mean values of asymmetry amplitudes.

# Transverse-Target-Spin Asymmetry

Asymmetry for transversely polarized  $\omega$  mesons



Curves show results of Goloskokov-Kroll calculations: solid (dash-dotted) lines for positive (negative)  $\pi\omega$  transition form factor, dashed lines are obtained without pion exchange contribution.

Open squares show mean values of asymmetry amplitudes.

# Extraction of Helicity Amplitude Ratios

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More detailed definition of helicity amplitudes

Amplitudes without nucleon helicity flip:

$$T_{\lambda_V \lambda_\gamma}^{(1)} \equiv T_{\lambda_V \frac{1}{2} \lambda_\gamma \frac{1}{2}} = T_{\lambda_V -\frac{1}{2} \lambda_\gamma -\frac{1}{2}}, \quad U_{\lambda_V \lambda_\gamma}^{(1)} \equiv U_{\lambda_V \frac{1}{2} \lambda_\gamma \frac{1}{2}} = -U_{\lambda_V -\frac{1}{2} \lambda_\gamma -\frac{1}{2}},$$

Amplitudes with nucleon helicity flip:

$$T_{\lambda_V \lambda_\gamma}^{(2)} \equiv T_{\lambda_V \frac{1}{2} \lambda_\gamma -\frac{1}{2}} = -T_{\lambda_V -\frac{1}{2} \lambda_\gamma \frac{1}{2}}, \quad U_{\lambda_V \lambda_\gamma}^{(2)} \equiv U_{\lambda_V \frac{1}{2} \lambda_\gamma -\frac{1}{2}} = U_{\lambda_V -\frac{1}{2} \lambda_\gamma \frac{1}{2}},$$

Angular distribution is dimensionless quantity, hence it may depend on the helicity amplitude ratios only.

Amplitude ratios:

$$t_{\lambda_V \lambda_\gamma}^{(1)} = T_{\lambda_V \lambda_\gamma}^{(1)} / T_{00}^{(1)}, \quad t_{\lambda_V \lambda_\gamma}^{(2)} = T_{\lambda_V \lambda_\gamma}^{(2)} / T_{00}^{(1)}, \quad u_{\lambda_V \lambda_\gamma}^{(1)} = U_{\lambda_V \lambda_\gamma}^{(1)} / T_{00}^{(1)}, \quad u_{\lambda_V \lambda_\gamma}^{(2)} = U_{\lambda_V \lambda_\gamma}^{(2)} / T_{00}^{(1)}.$$

Total number of independent amplitude ratios is 17 (34 real functions).

Small amplitudes can be reliably extracted if there is product of those by the amplitude  $T_{00}^{(1)}$  or  $T_{11}^{(1)}$  being dominant at large  $Q^2$  and small  $t$ .

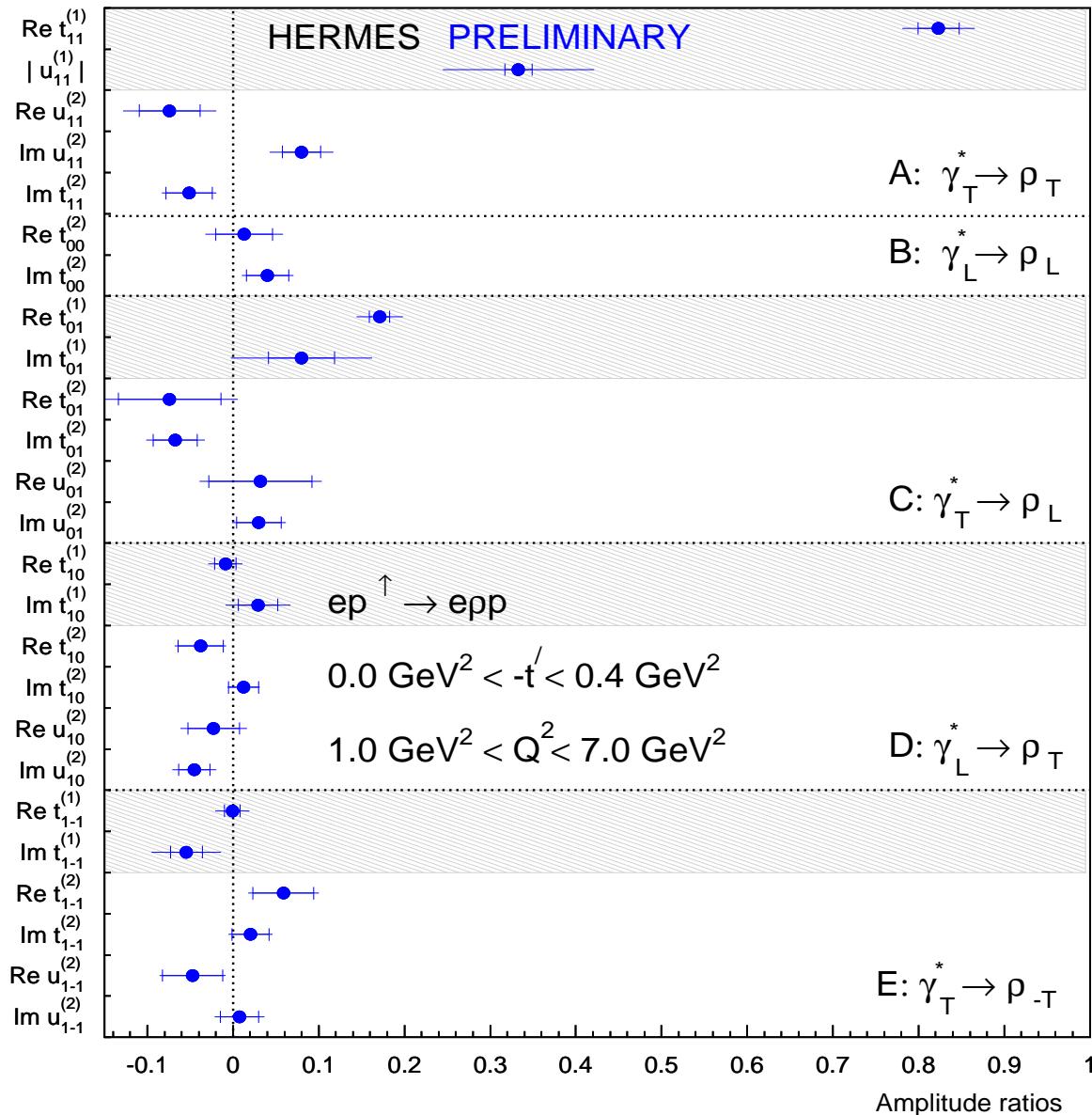
For longitudinally polarized beam and transversely polarized target only 25 parameters can be reliably extracted.

For the present data, the phase shifts of  $T_{11}^{(1)}$  and  $U_{11}^{(1)}$  are fixed from previous HERMES data.

Ratios  $u_{10}^{(1)}$ ,  $u_{10}^{(1)}$ ,  $u_{1-1}^{(1)}$  are not obtained from present data since they are multiplied by small factor  $\sqrt{1-\epsilon} S_L$  with the longitudinal (with respect of virtual photon) target polarization  $S_L < 0.04$

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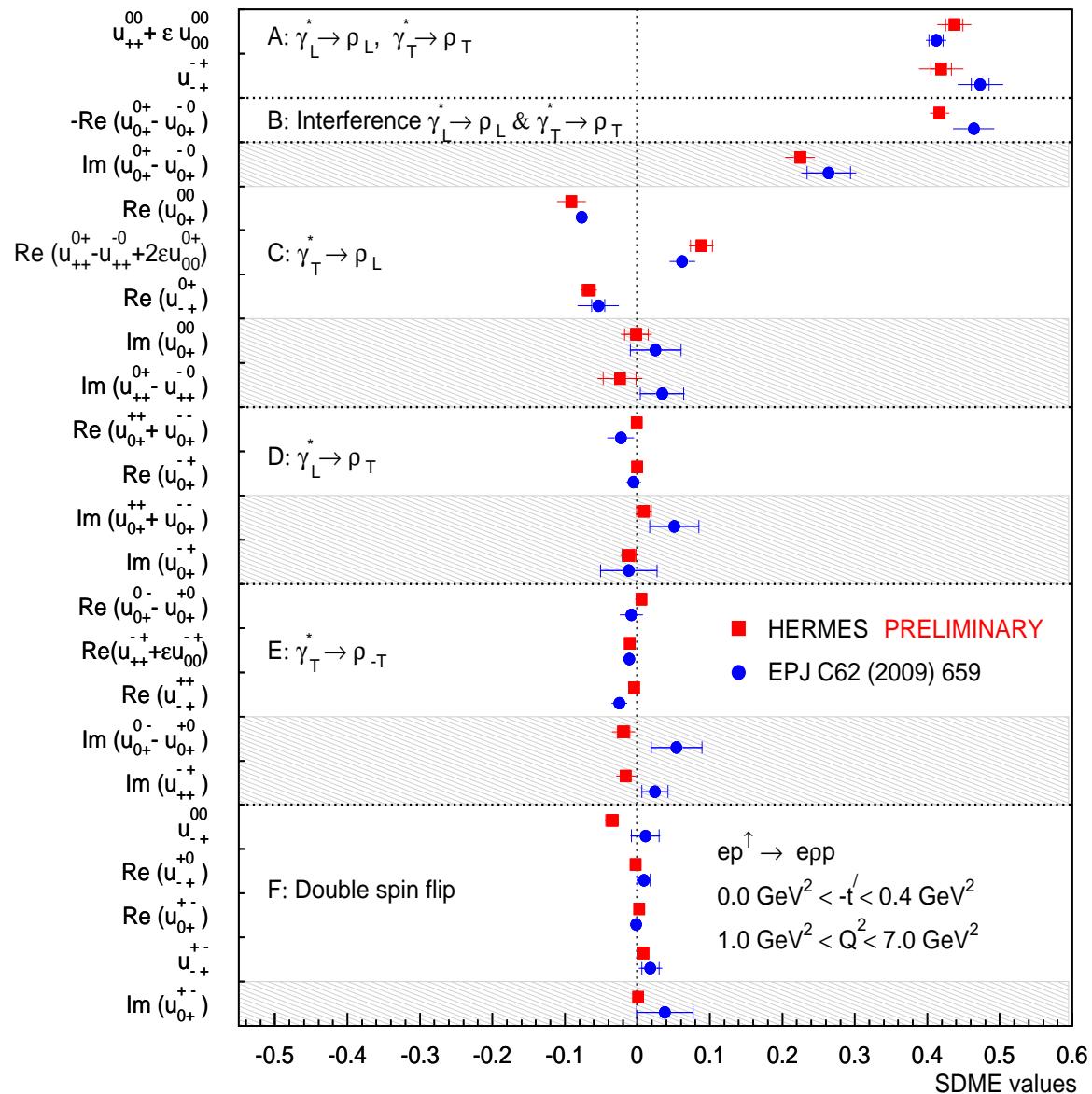
# Extraction of Helicity Amplitude Ratios



Ratios of amplitudes without nucleon spin flip are shown in shaded areas.

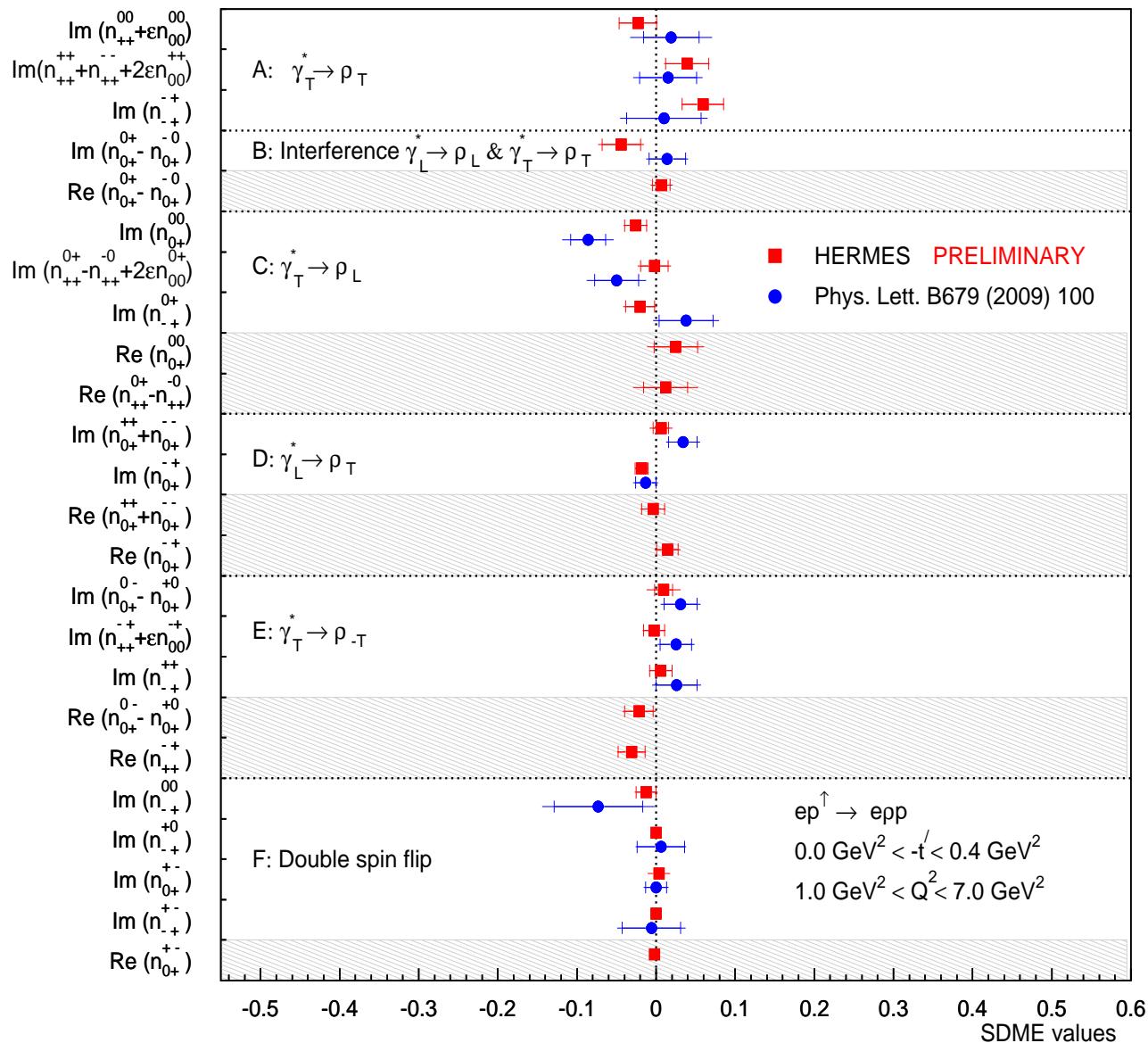
They were also obtained in previous HERMES analysis (Eur. Phys. J. C71 (2011) 1609).

# Extraction of Helicity Amplitude Ratios



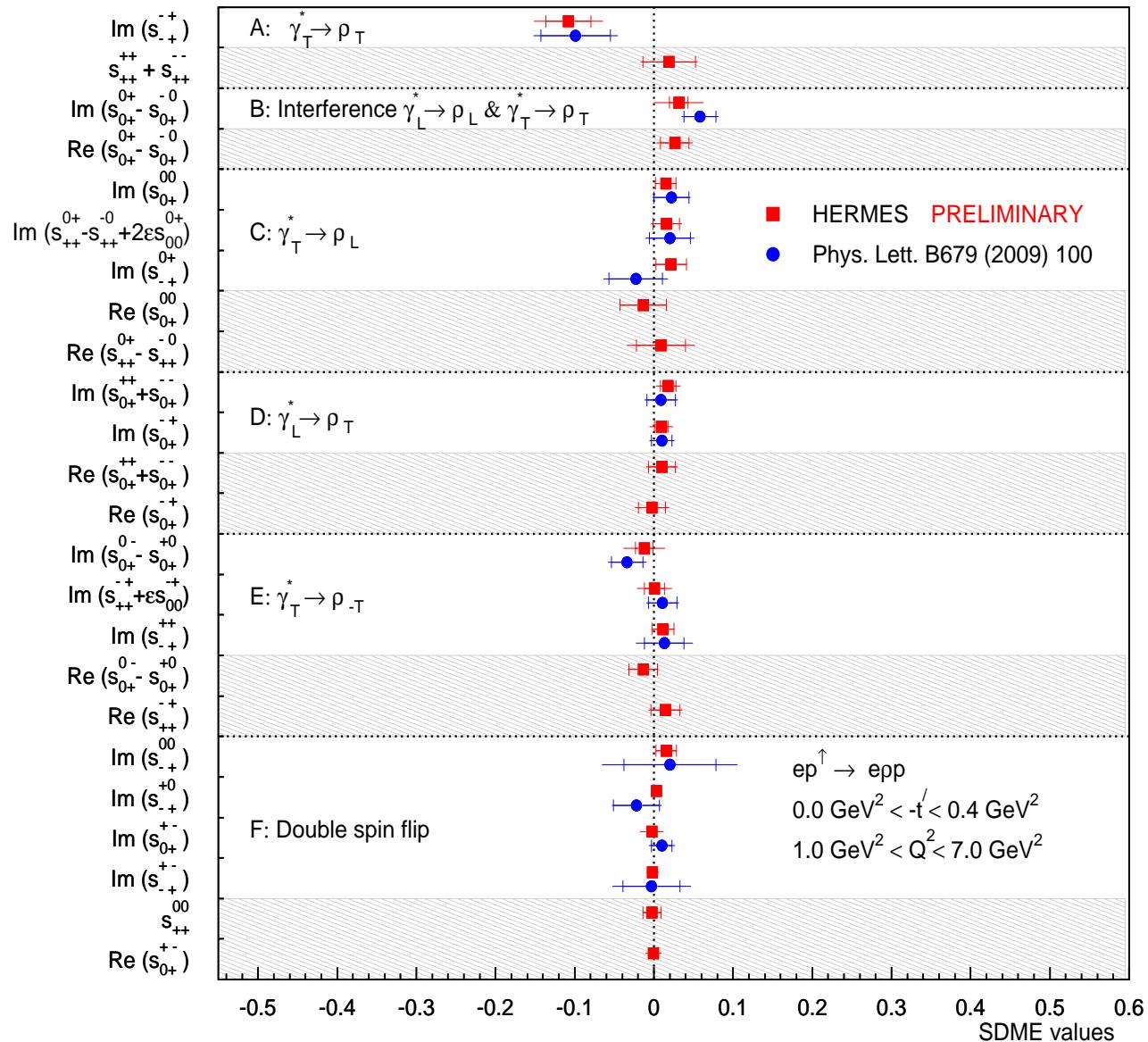
"Polarized" SDMEs (which can be obtained only with longitudinally polarized beam) are shown in shaded areas.

# Extraction of Helicity Amplitude Ratios



"Polarized" SDMEs (which can be obtained only with longitudinally polarized beam) are shown in shaded areas.

# Extraction of Helicity Amplitude Ratios



"Polarized" SDMEs (which can be obtained only with longitudinally polarized beam) are shown in shaded areas.

## Summary

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- Exclusive vector-meson electroproduction in DIS is studied at HERMES using a longitudinally polarized electron/positron beam and unpolarized or transversely polarized hydrogen and deuterium targets in the kinematic region  $Q^2 > 1.0 \text{ GeV}^2$ ,  $3.0 \text{ GeV} < W < 6.3 \text{ GeV}$ , and  $-t' < 0.2 \text{ GeV}^2$ .
- Using an unbinned maximum likelihood method, 15 unpolarized, and, for the first time, 8 polarized spin-density matrix elements are extracted from data on exclusive  $\omega$ -meson production.
- No significant differences between proton and deuteron results are seen.
- While the values of class-A and B SDMEs agree with the hypothesis of  $s$ -channel helicity conservation, the class-C SDME  $r_{00}^5$  indicates a violation of SCHC.
- Using the SDMEs  $r_{1-1}^1$  and  $\text{Im}\{r_{1-1}^2\}$  it is shown that  $|U_{11}|^2 > |T_{11}|^2$ .
- The importance of UPE transitions is also shown by considering  $u_1$ ,  $u_2$ ,  $u_3$  and the UPE-to-NPE asymmetry. This suggests that at HERMES energies  $\pi^0$ ,  $a_1\dots$  exchanges play a significant role.
- The longitudinal-to-transverse cross-section ratio  $R = d\sigma_L/d\sigma_T$  for the  $\omega$  meson is  $R = 0.25 \pm 0.03 \pm 0.07$  at  $\langle Q^2 \rangle = 2.4 \text{ GeV}^2$ ,  $\langle -t' \rangle = 0.08 \text{ GeV}^2$ ,  $\langle W \rangle = 4.8 \text{ GeV}$ .
- HERMES accumulated 279  $\omega$  mesons produced in exclusive DIS on transversely polarized proton. Two cosine and five sine azimuthal modulations of the cross section are obtained for the entire kinematic bin. Extracted asymmetry amplitudes favors probably a positive sign of  $\pi\omega$  form factor.
- In order to estimate the angular momentum contribution of a quark or gluon to the nucleon spin with the help of the Ji sum rule, the  $E(x, \xi, t)$  distribution is to be extracted from the data on the vector-meson production from the transversely polarized nucleon. For the first time, the amplitude analysis of the  $\rho^0$ -meson electroproduction on the transversely polarized proton is performed by HERMES and information on 25 real functions is obtained.

## Backup Slides

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- Dependence of angular distribution on SDMEs

$$\mathcal{W}^{U+L}(\Phi, \phi, \cos \Theta) = \mathcal{W}^U(\Phi, \phi, \cos \Theta) + P_b \mathcal{W}^L(\Phi, \phi, \cos \Theta)$$

$$\begin{aligned}\mathcal{W}^U(\Phi, \phi, \cos \Theta) = & \frac{3}{8\pi^2} \left[ \frac{1}{2}(1 - r_{00}^{04}) + \frac{1}{2}(3r_{00}^{04} - 1) \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^{04}\} \sin 2\Theta \cos \phi - r_{1-1}^{04} \sin^2 \Theta \cos 2\phi \right. \\ & - \epsilon \cos 2\Phi \left( r_{11}^1 \sin^2 \Theta + r_{00}^1 \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^1\} \sin 2\Theta \cos \phi - r_{1-1}^1 \sin^2 \Theta \cos 2\phi \right) \\ & - \epsilon \sin 2\Phi \left( \sqrt{2}\text{Im}\{r_{10}^2\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^2\} \sin^2 \Theta \sin 2\phi \right) \\ & + \sqrt{2\epsilon(1 + \epsilon)} \cos \Phi \left( r_{11}^5 \sin^2 \Theta + r_{00}^5 \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^5\} \sin 2\Theta \cos \phi - r_{1-1}^5 \sin^2 \Theta \cos 2\phi \right) \\ & \left. + \sqrt{2\epsilon(1 + \epsilon)} \sin \Phi \left( \sqrt{2}\text{Im}\{r_{10}^6\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^6\} \sin^2 \Theta \sin 2\phi \right) \right],\end{aligned}$$

$$\begin{aligned}\mathcal{W}^L(\Phi, \phi, \cos \Theta) = & \frac{3}{8\pi^2} \left[ \sqrt{1 - \epsilon^2} \left( \sqrt{2}\text{Im}\{r_{10}^3\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^3\} \sin^2 \Theta \sin 2\phi \right) \right. \\ & + \sqrt{2\epsilon(1 - \epsilon)} \cos \Phi \left( \sqrt{2}\text{Im}\{r_{10}^7\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^7\} \sin^2 \Theta \sin 2\phi \right) \\ & \left. + \sqrt{2\epsilon(1 - \epsilon)} \sin \Phi \left( r_{11}^8 \sin^2 \Theta + r_{00}^8 \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^8\} \sin 2\Theta \cos \phi - r_{1-1}^8 \sin^2 \Theta \cos 2\phi \right) \right].\end{aligned}$$

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## Unbinned Maximum Likelihood Method

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- Calculation of "background" SDMEs

Two Monte Carlo (MC) sets.

First (normalization) MC set: uniform angular distribution ( $\cos \Theta, \Phi, \phi$ ). Number of events is  $N_{MC}$ .

Second (background pseudo-data) MC set for calculation of a set  $S_{bg}$  of 15 background SDMEs. Number of events  $N_{PD}$ .

Log-likelihood function for background pseudo-data events for unpolarized (U) beam

$$-\ln L(S_{bg}) = -\sum_{i=1}^{N_{PD}} \ln \frac{\mathcal{W}^U(S_{bg}, \Phi_i, \phi_i, \cos \Theta_i)}{\tilde{\mathcal{N}}_{bg}(S_{bg})},$$

$$\tilde{\mathcal{N}}_{bg}(S_{bg}) = \sum_{j=1}^{N_{MC}} \mathcal{W}^U(S_{bg}, \Phi_j, \phi_j, \cos \Theta_j).$$

- Calculation of physical SDMEs

$N$  total number of experimental events in exclusive region.

$S$  set of 23 SDMEs for unpolarized target and longitudinally (L) polarized beam.

$$-\ln L(S) = -\sum_{i=1}^N \ln \left[ \frac{(1-f_{bg}) * \mathcal{W}^{U+L}(S, \Phi_i, \phi_i, \cos \Theta_i)}{\tilde{\mathcal{N}}(S, S_{bg})} + \frac{f_{bg} * \mathcal{W}^U(S_{bg}, \Phi_i, \phi_i, \cos \Theta_i)}{\tilde{\mathcal{N}}(S, S_{bg})} \right]$$

$f_{bg}$  fraction of background events in experimental events in exclusive region.

The total normalization factor

$$\begin{aligned} \tilde{\mathcal{N}}(S, S_{bg}) &= \\ \sum_{j=1}^{N_{MC}} [(1 - f_{bg}) * \mathcal{W}^{U+L}(S, \Phi_j, \phi_j, \cos \Theta_j) &+ f_{bg} * \mathcal{W}^U(S_{bg}, \Phi_j, \phi_j, \cos \Theta_j)] \end{aligned}$$

# Unbinned Maximum Likelihood Method

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- No background corrections

$$\ln \mathcal{L} = \sum_i^I \ln [\mathcal{W}(\mathcal{R}, (P_b)_i, (P_T)_i, \Phi_i, \Psi_i, \theta_i, \varphi_i)) / N_i],$$

$$N_i = K_1 + K_2(P_b)_i + K_3(P_T)_i + K_4(P_b)_i(P_T)_i$$

$(P_b)_i$  beam polarization,  $(P_T)_i$  target polarization for  $i$ -th event,  
 $\mathcal{R}$  set of amplitude ratios.

$$N_{++} = \frac{1}{L} \sum_{m=1}^L \mathcal{W}(\mathcal{R}, (P_b = 1), (P_T = 1), \Phi_m, \Psi_m, \theta_m, \varphi_m)$$

$N_{+-}$  corresponds to  $P_b = 1, P_T = -1$ ,  $N_{-+}$  to  $P_b = -1, P_T = 1$  etc.

$K_1, K_2, K_3$ , and  $K_4$  are linear combinations of  $N_{++}, N_{+-}, N_{-+}$ , and  $N_{--}$ .

- Likelihood function with background corrections

$$\ln \mathcal{L}_{tot} = \sum_i^I \ln \left[ (1 - f_{bg}) \frac{\mathcal{W}(\mathcal{R}, (P_b)_i, (P_T)_i, \Phi_i, \Psi_i, \theta_i, \varphi_i)}{N_i} + f_{bg} \frac{\mathcal{W}_{bg}((P_b)_i, (P_T)_i, \Phi_i, \Psi_i, \theta_i, \varphi_i)}{N_i^{bg}} \right]$$

Angular distribution,  $\mathcal{W}_{bg}$  of background events is assumed to be independent of polarizations  $P_b$  and  $P_T$ ,  $f_{bg}$  fraction of reconstructed background events.

$$N_i^{bg} = \frac{1}{L} \sum_{m=1}^L \mathcal{W}_{bg}((P_b = 0), (P_T = 0), \Phi_m, \Psi_m, \theta_m, \varphi_m)$$

$$\ln \mathcal{L}_{tot} = \sum_i^I \ln \left[ \frac{(1 - g_{bg}) \mathcal{W}(\mathcal{R}, (P_b)_i, (P_T)_i, \Phi_i, \Psi_i, \theta_i, \varphi_i) N_i + g_{bg} \mathcal{W}_{bg}((P_b)_i, (P_T)_i, \Phi_i, \Psi_i, \theta_i, \varphi_i)}{(1 - g_{bg}) N_i + g_{bg} N_i^{bg}} \right]$$

$g_{bg}$  is the fraction of background in  $4\pi$  (before interaction of particles with detector)