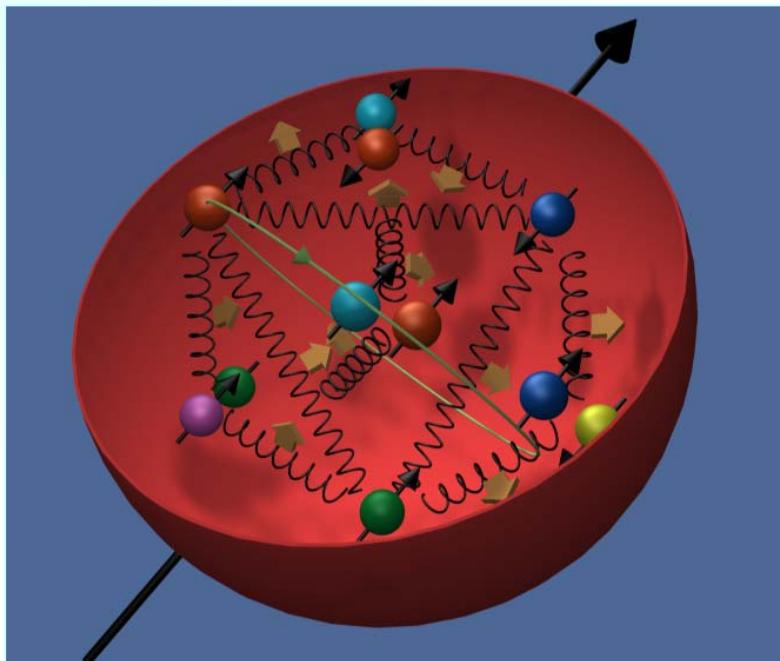




# Selected Recent **hermes** Results on Parton Distribution and Fragmentation Functions

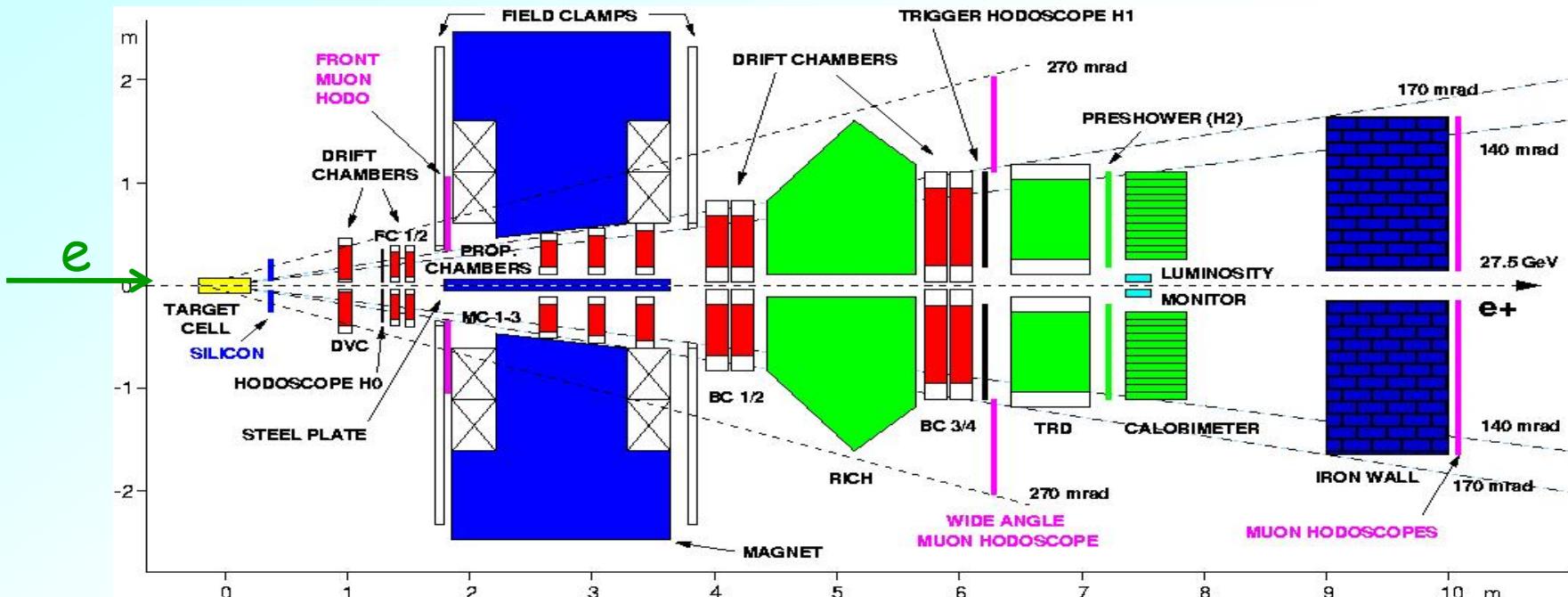
Klaus Rith

University of Erlangen-Nürnberg & DESY



Main **HERMES** research topics:

- Origin of nucleon **spin**
- Details of nucleon **structure**

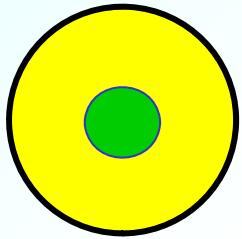


- HERA longitudinally polarized 27.6 GeV  $e^+e^-$  beam
- Polarized and unpolarized internal gas target (spin flip every 90 s)
- Kinematics:  $0.02 < x < 0.7$ ,  $1.0 \text{ GeV}^2 < Q^2 < 15 \text{ GeV}^2$
- Data taking: summer 1995 - June 30, 2007
- 1995-2000: longitudinal target polarization, 2002-2005: transverse target pol.  
2006-2007: unpolarized H, D targets + Recoil Detector

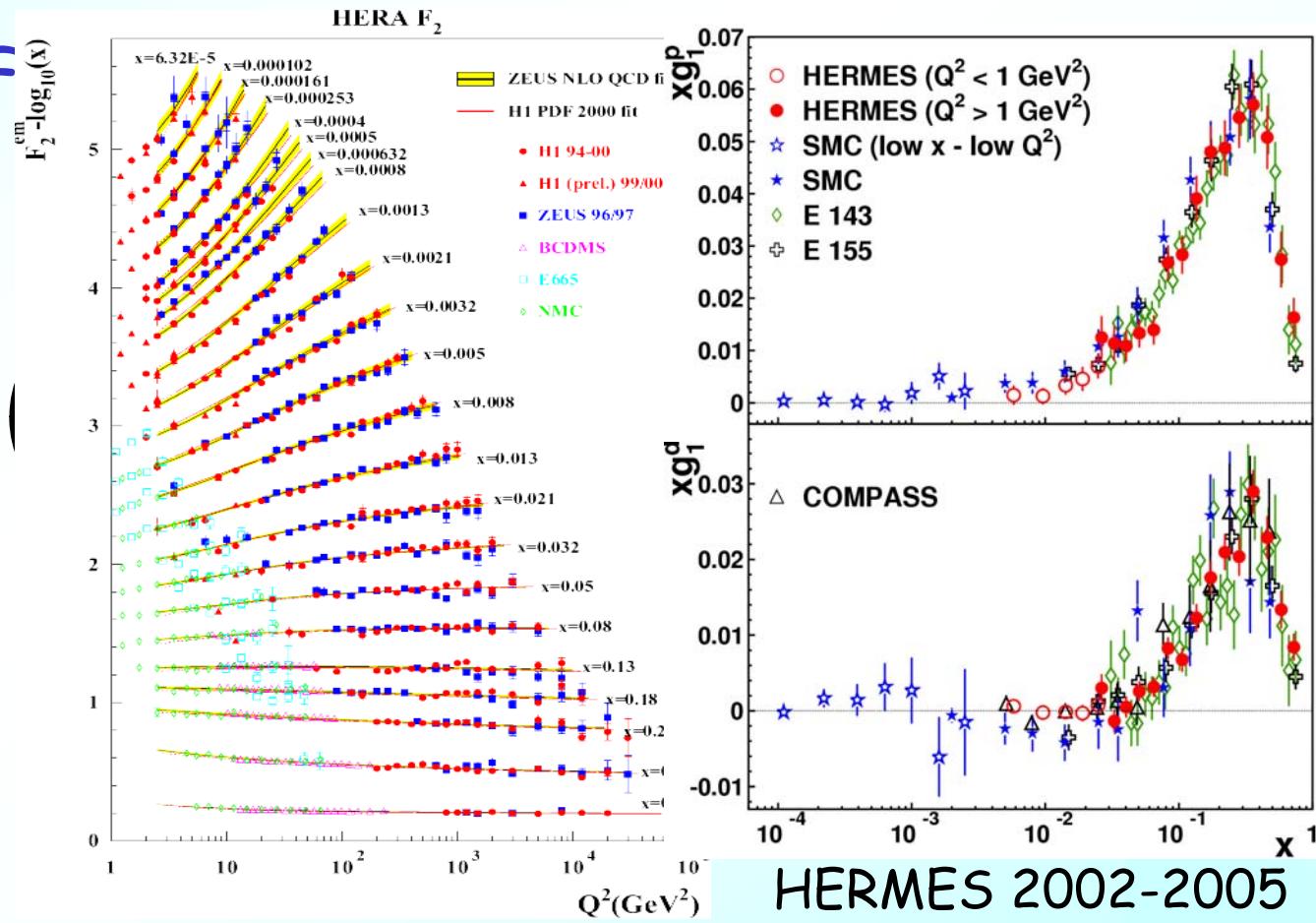
# Leading-twist Parton Distributions

Complete description of nucleon by quark momentum and spin distributions at leading-twist: **3  $k_T$ -integrated distribution functions (DF)**

Unpolarised DF  
 $q(x) \equiv f_1^q(x)$

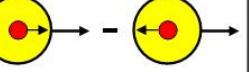
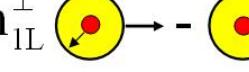
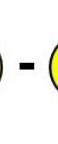
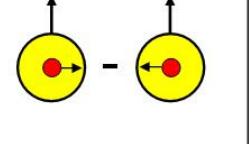
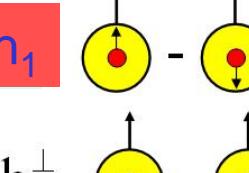


well known



# Transverse Momentum Dependent DFs

## Quark distribution functions

|         |   | quark  |  |  |
|---------|---|--|--|--|
|         |   | U  | L  | T  |
| nucleon | U | $f_1$           |  | $h_1^\perp$   |
|         | L |  | $g_1$           | $h_{1L}^\perp$   |
|         | T | $f_{1T}^\perp$  | $g_{1T}^\perp$  | $h_1$ <br>$h_{1T}^\perp$  |

Boer-Mulders DF  
(chiral-odd)

Transversity DF  
(chiral-odd)

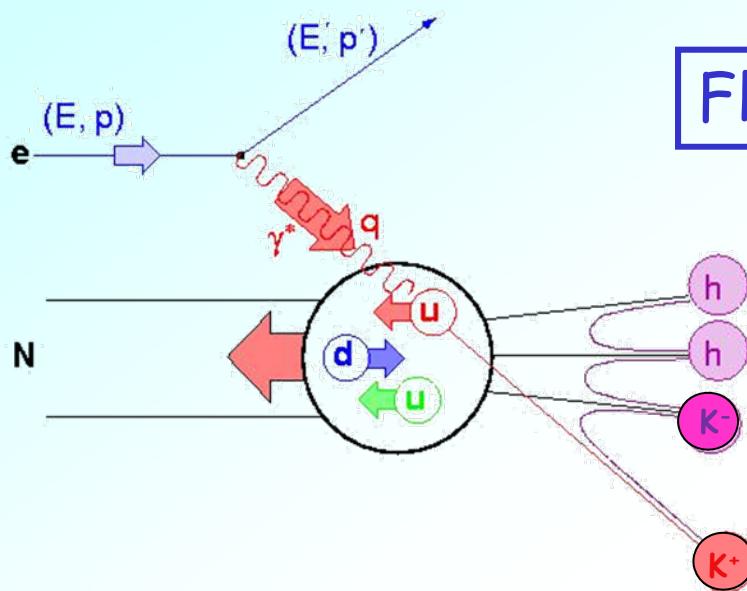
Sivers DF (T-odd)

## Fragmentation functions (FF)

$D_1 \equiv D_q^h = \text{,normal' FF},$

$H_1^\perp = \text{spin-dependent Collins FF (chiral-odd)}$

# Quark Distributions from SIDIS



## Flavor tagging

$$v = E - E', Q^2 = -q^2 = -(l - l')^2$$

$x = Q^2/(2Mv)$  = fraction of nucleon's longitudinal momentum carried by struck quark

$$q(x) = \text{quark number density}$$

Leading hadron originates with large probability from struck quark

$D_q^h(z)$  := Fragmentation function (FF)  $z = E_h/v$

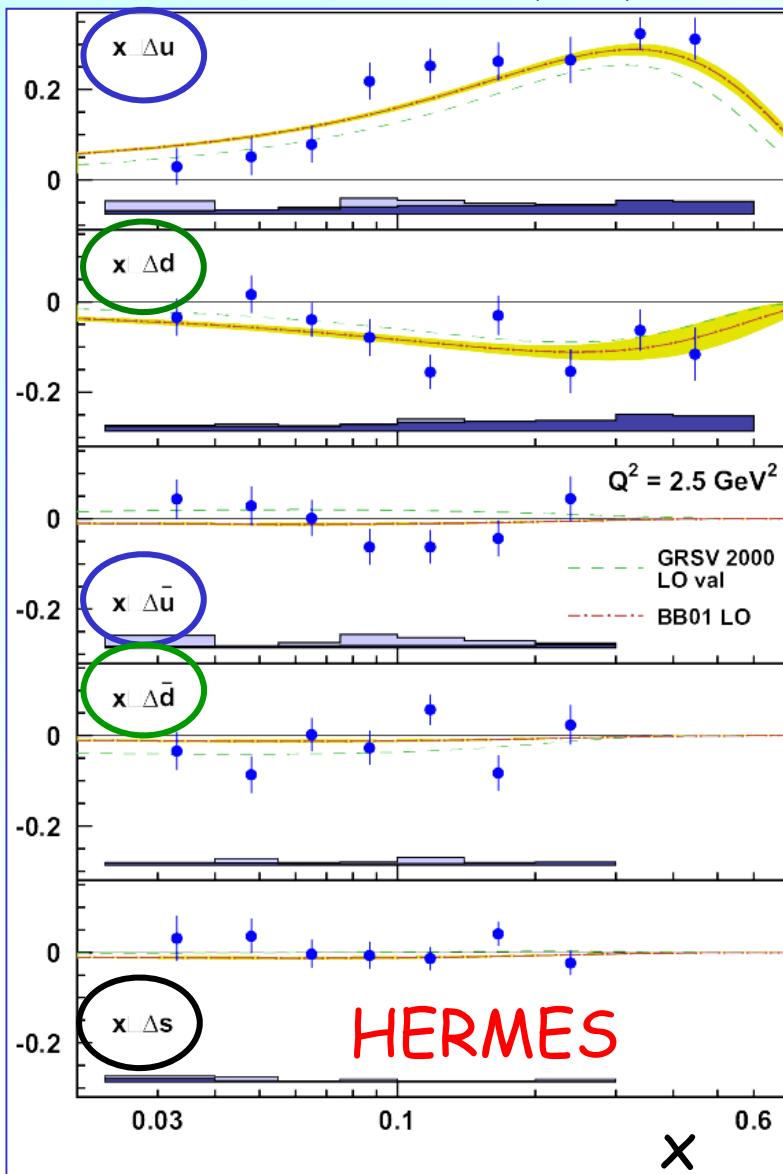
Measure hadron asymmetries

$$A_{LL}(x, z) \equiv \frac{\sum_q z_q^2 \Delta q(x) D_q^h(z)}{\sum_q z_q^2 q(x) D_q^h(z)}$$

Targets:  $\vec{H}, \vec{D}$ ;  $h = \pi^\pm, K^\pm, p$  (identified with RICH)

# Quark Helicity Distributions $\Delta q(x)$

PRD 71 (2005) 012003



- u quarks: large positive polarisation
- d quarks: negative polarisation  

$$\Delta d(x) \approx -0.4 \Delta u(x)$$
- Sea quarks ( $\bar{u}, \bar{d}, s$ ): polarisation compatible with 0.



# The Strange Sea: $S(x)$ , $\Delta S(x)$

## Inputs:

- Multiplicities for  $K^+$  and  $K^-$  from unpolarized deuteron

$$d^2N_D^{DIS}/dx dQ^2 = K_U(x, Q^2)[5Q(x) + 2S(x)]$$

where  $Q(x) = u(x) + \bar{u}(x) + d(x) + \bar{d}(x)$  and  $S(x) = s(x) + \bar{s}(x)$

$$d^2N_D^{K\pm}/dx dQ^2 = K_U(x, Q^2)[Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz]$$

where  $D_Q^K(z) = 4D_u^K(z) + D_d^K(z)$  and  $D_S^K(z) = 2D_s^K(z)$

- Inclusive and  $K^+$ ,  $K^-$  asymmetries from polarized deuteron

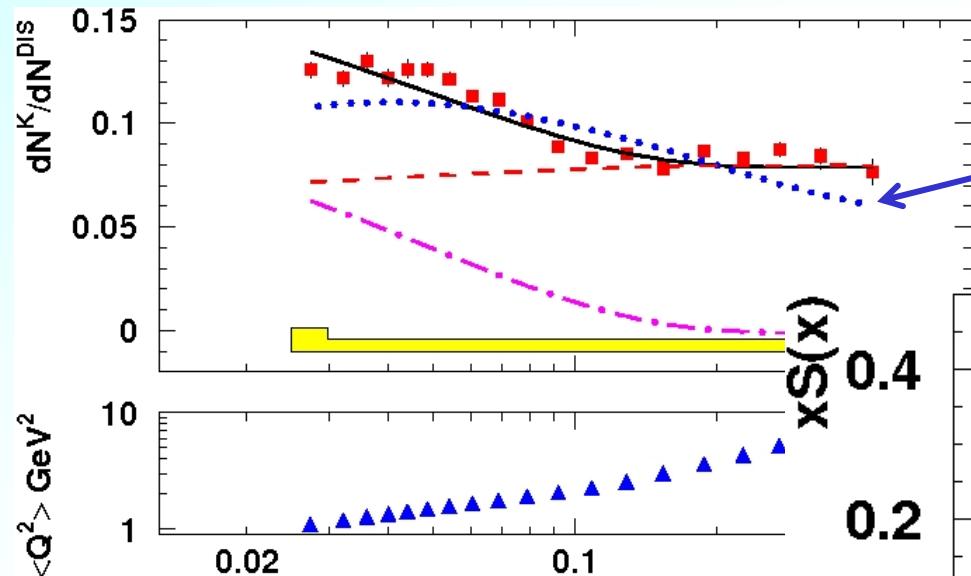
$$A_{1,D} d^2N^{DIS}/dx dQ^2 = K_{LL}(x, Q^2)[5\Delta Q(x) + 2\Delta S(x)]$$

$$A_{1,D}^{K\pm} d^2N^{K\pm}/dx dQ^2 = K_{LL}(x, Q^2)[\Delta Q(x) \int D_Q^K(z) dz + \Delta S(x) \int D_S^K(z) dz]$$

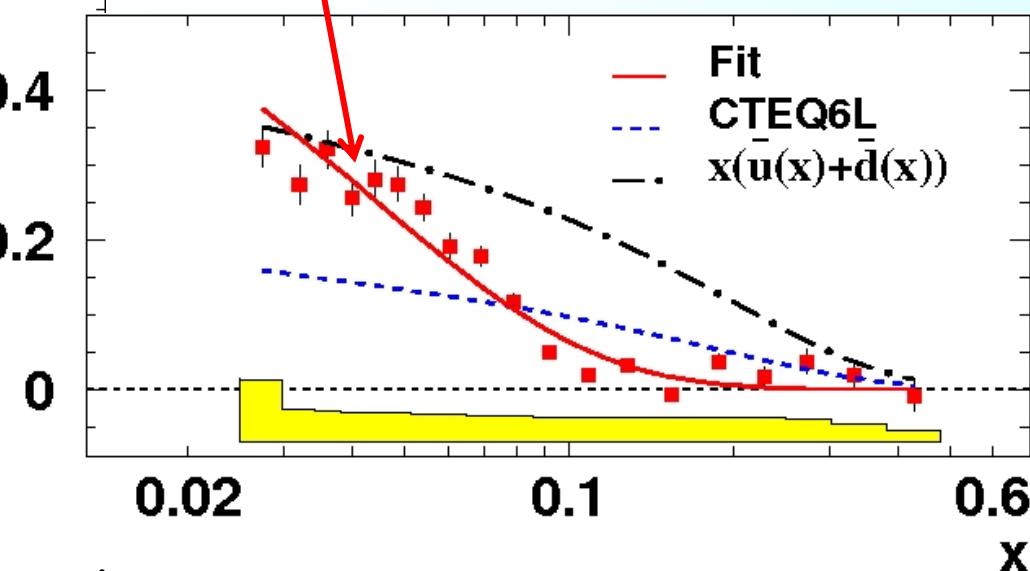
# $S(x)$ from Kaon Multiplicities

$$\frac{dN^{K^\pm}}{dN^{\text{DIS}}} = \frac{Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz}{5 Q(x) + 2 S(x)} \xrightarrow{x > 0.3} \frac{\int D_Q^K(z) dz}{5}$$

P.L. B666 (2008) 466



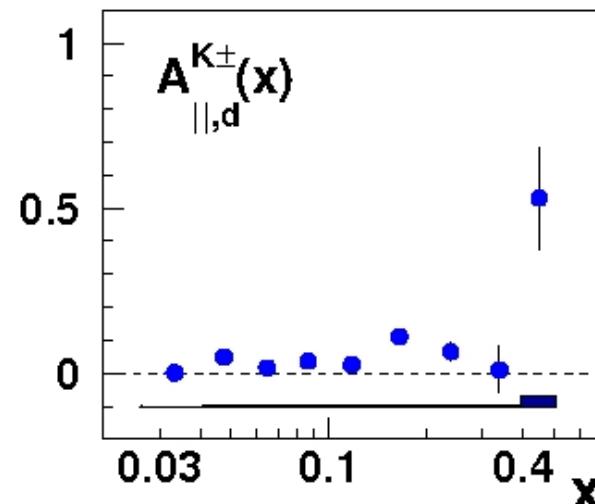
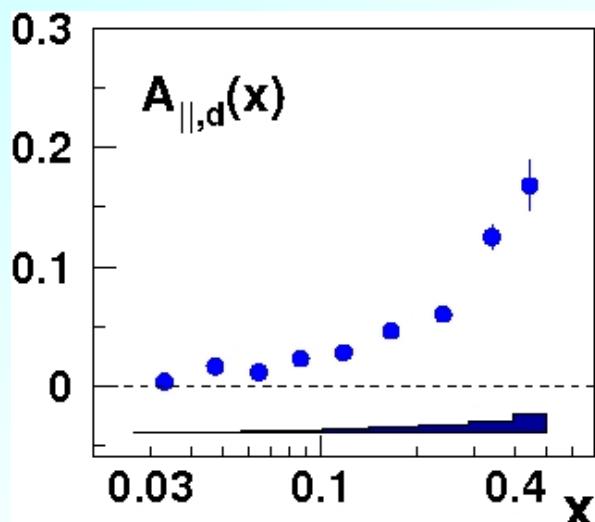
●  $S(x)$  from CTEQ6L with  
 $\int D_Q^K(z) dz$  &  $\int D_S^K(z) dz$  as free  
parameters (dotted) does not  
fit the data



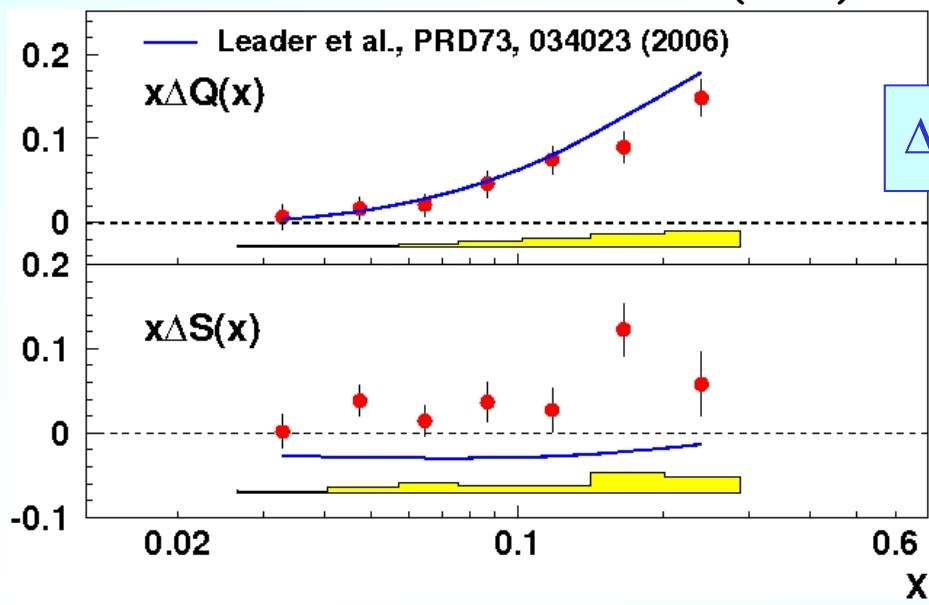
●  $S(x)$  much softer than  
assumed by current PDFs  
(mainly based on  $\nu N \rightarrow \mu^+ \mu^- X$ )

Take  $\int D_S^K(z) dz = 1.27 \pm 0.13$  from de Florian et al.

# $\Delta S(x)$ from Kaon Asymmetries



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$$\Delta S = 0.037 \pm 0.019(\text{stat.}) \pm 0.027(\text{syst.})$$

compared to

$$\Delta S = -0.085 \pm 0.013(\text{stat.}) \pm 0.012(\text{syst.})$$

from inclusive data and SU(3)

Large negative contribution  
from low  $x$ ?

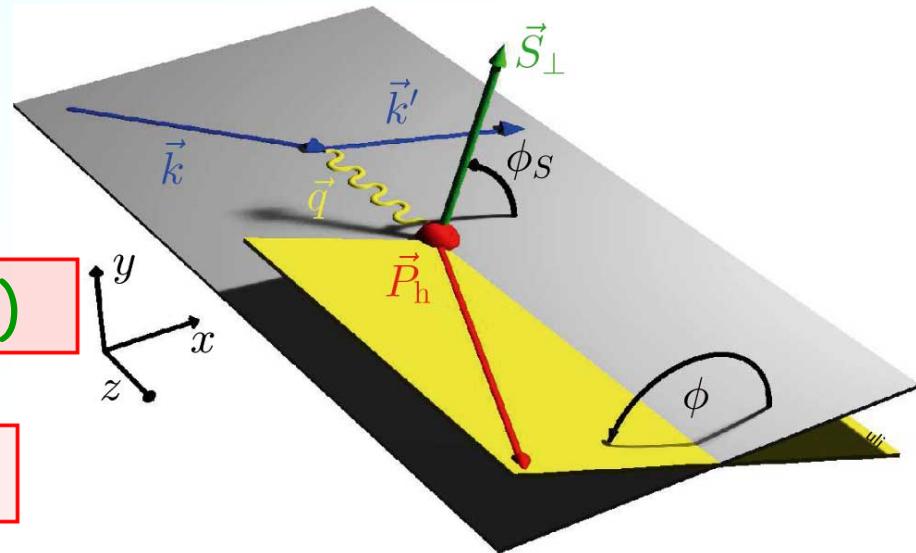
# Transverse Azimuthal Angular Asymmetries

Amplitude has 2 components:

**Transversity DF**

$$2\langle \sin(\phi + \phi_S) \rangle_{UT}^h \sim h_1^q(x) \otimes H_1^{\perp q}(z)$$

**Collins FF**



**Unpolarised FF**

$$2\langle \sin(\phi - \phi_S) \rangle_{UT}^h \sim f_{1T}^{\perp q}(x) \otimes D_1^q(z)$$

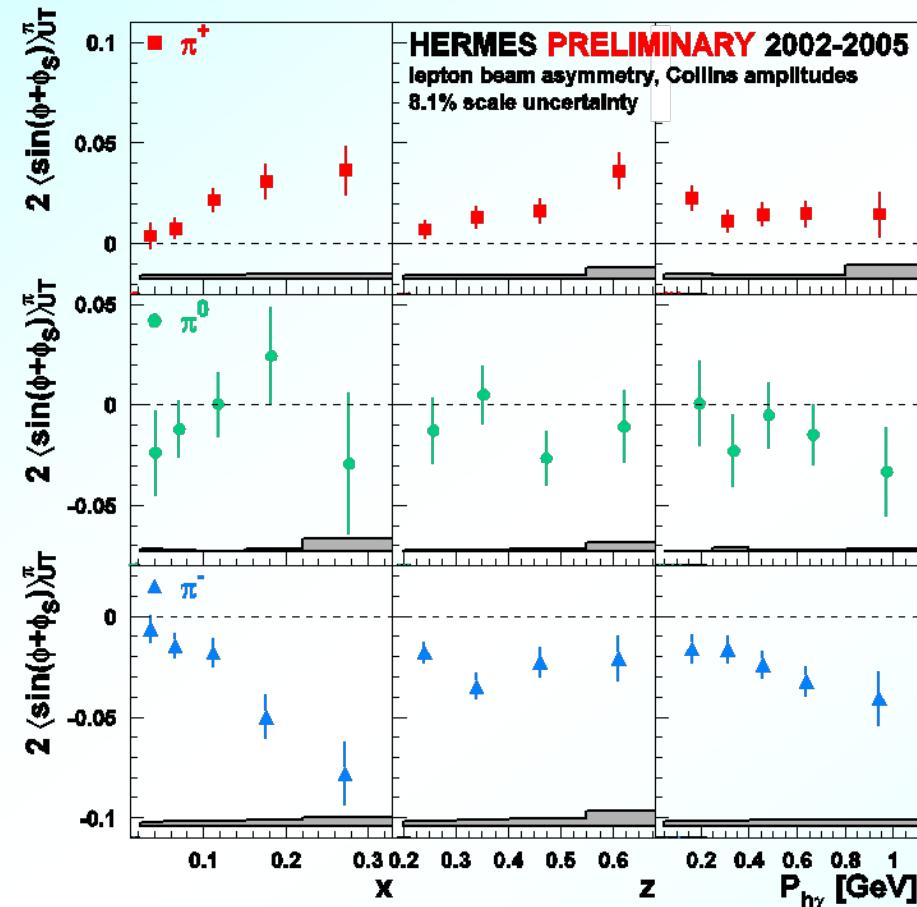
**Sivers DF**

(Requires non-vanishing orbital angular momenta  $L_q$  of quarks)

## Transversity DF

$$2\langle \sin(\phi + \phi_s) \rangle^h_{UT} \sim h_1^q(x) \otimes H_1^{\perp q}(z)$$

## Collins FF



| N/q | U              | L        | T              |
|-----|----------------|----------|----------------|
| U   | $f_1$          |          | $h_1^\perp$    |
| L   |                | $g_1$    | $h_{1L}^\perp$ |
| T   | $f_{1T}^\perp$ | $g_{1T}$ | $h_1^\perp$    |

- First measurement of non-zero Collins effect

- Both Collins fragmentation function and transversity distribution function are sizeable

- Surprisingly large  $\pi^-$  asymmetry

- Possible source: large contribution (with opposite sign) from unfavored fragmentation, i.e.  $u \rightarrow \pi^-$

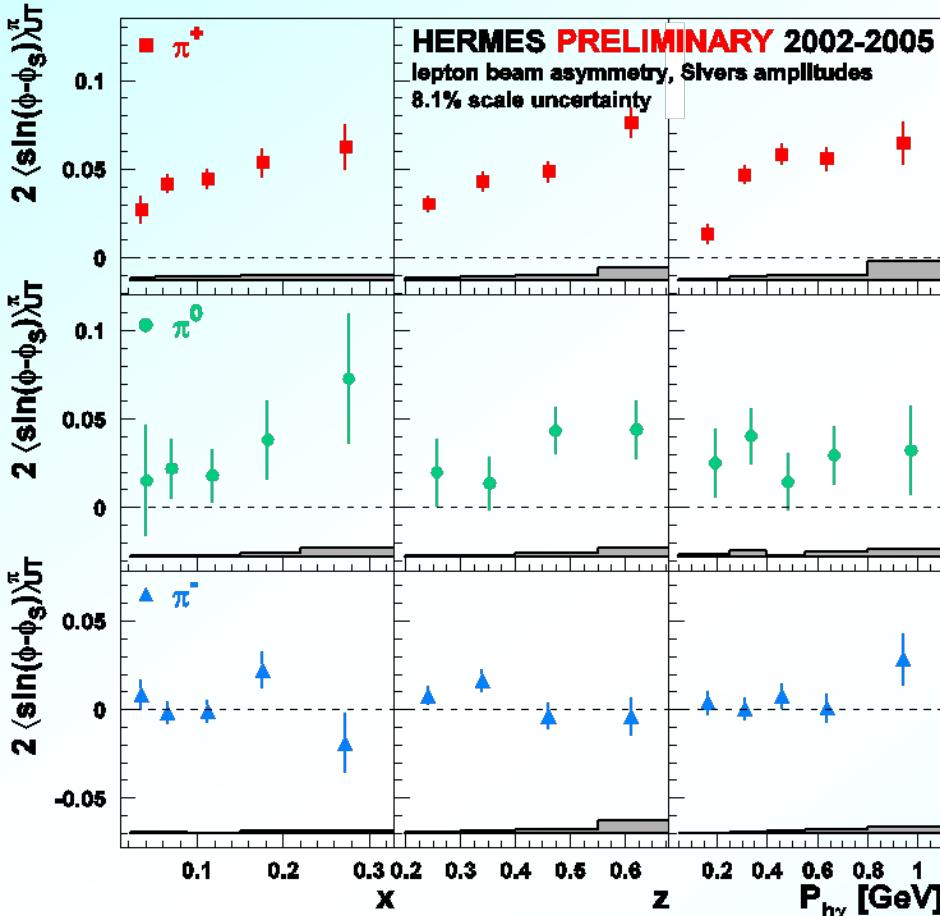
$$H_1^{\perp, \text{disf}} \approx - H_1^{\perp, \text{fav}}$$

# Sivers Amplitudes

Sivers DF

$$2\langle \sin(\phi - \phi_s) \rangle_{UT}^h \sim f_{1T}^{\perp q}(x) \otimes D_1^q(z)$$

| N/q | U              | L        | T                    |
|-----|----------------|----------|----------------------|
| U   | $f_1$          |          | $h_1^\perp$          |
| L   |                | $g_1$    | $h_{1L}^\perp$       |
| T   | $f_{1T}^\perp$ | $g_{1T}$ | $h_1$ $h_{1T}^\perp$ |

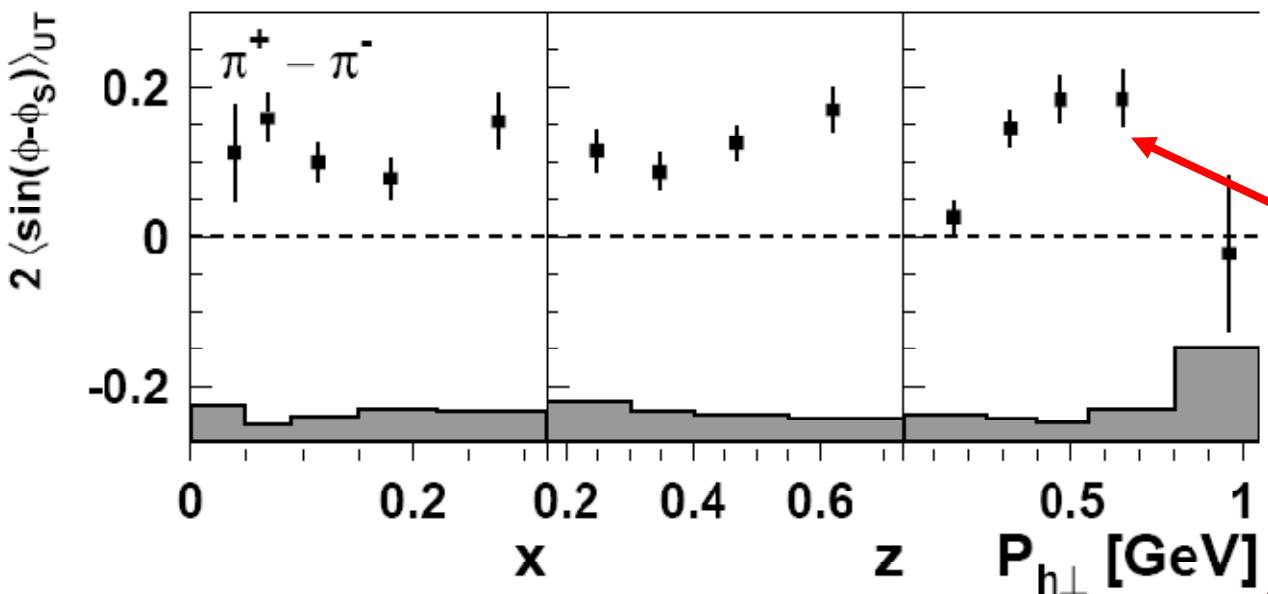


First observation of non-zero Sivers distribution function in DIS

Experimental evidence for orbital angular momentum  $L_q$  of quarks

But: Quantitative contribution of  $L_q$  to nucleon spin still unclear

**HERMES PRELIMINARY 2002-2005**  
lepton beam amplitudes, 8.1% scale uncertainty

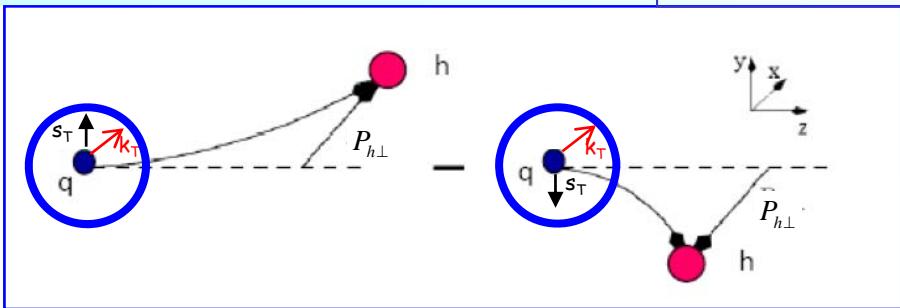


access to  
Sivers valence  
distribution

$$2\langle \sin(\phi - \phi_s) \rangle_{UT}^{\pi^+ - \pi^-} = -2 \frac{4f_{1T}^{\perp, u_v} - f_{1T}^{\perp, d_v}}{4f_1^{\perp, u_v} - f_1^{\perp, d_v}}$$

# Azimuthal Asymmetries in Unpolarised SIDIS

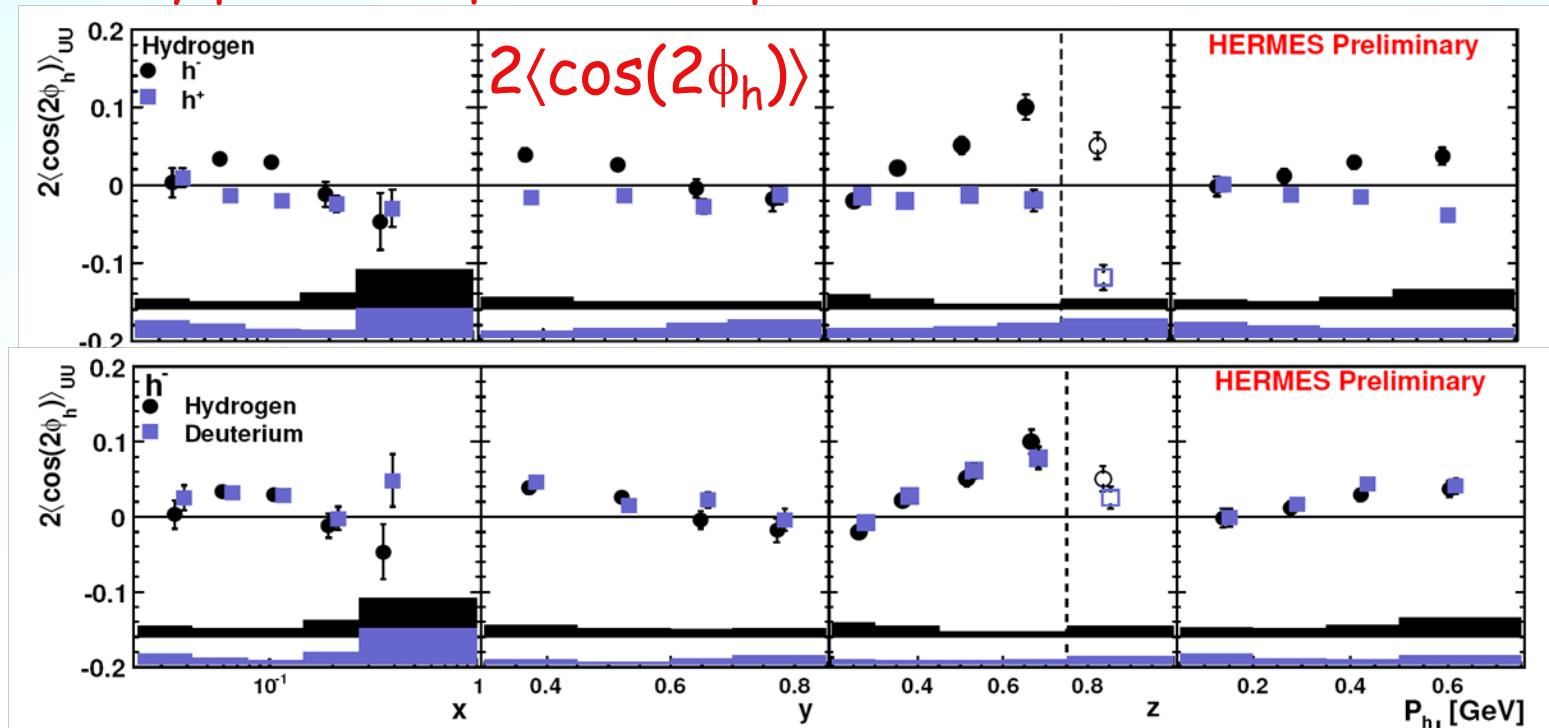
## Boer-Mulders DF



| N/q | U              | L        | T                    |
|-----|----------------|----------|----------------------|
| U   | $f_1$          |          | $h_1^\perp$          |
| L   |                | $g_1$    | $h_{1L}^\perp$       |
| T   | $f_{1T}^\perp$ | $g_{1T}$ | $h_1$ $h_{1T}^\perp$ |

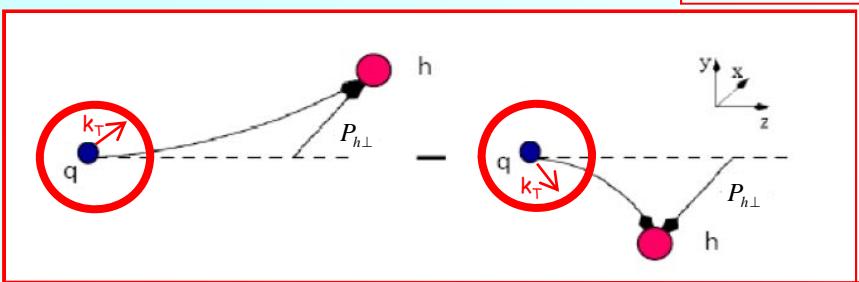
$$F_{UU}^{\cos 2\phi} = C \left[ -\frac{2(\hat{h} \cdot \vec{k}_T)(\hat{h} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} h_1^\perp H_1^\perp \right]$$

transversely polarised quarks in unpolarised nucleon



# Azimuthal Asymmetries in Unpolarised SIDIS

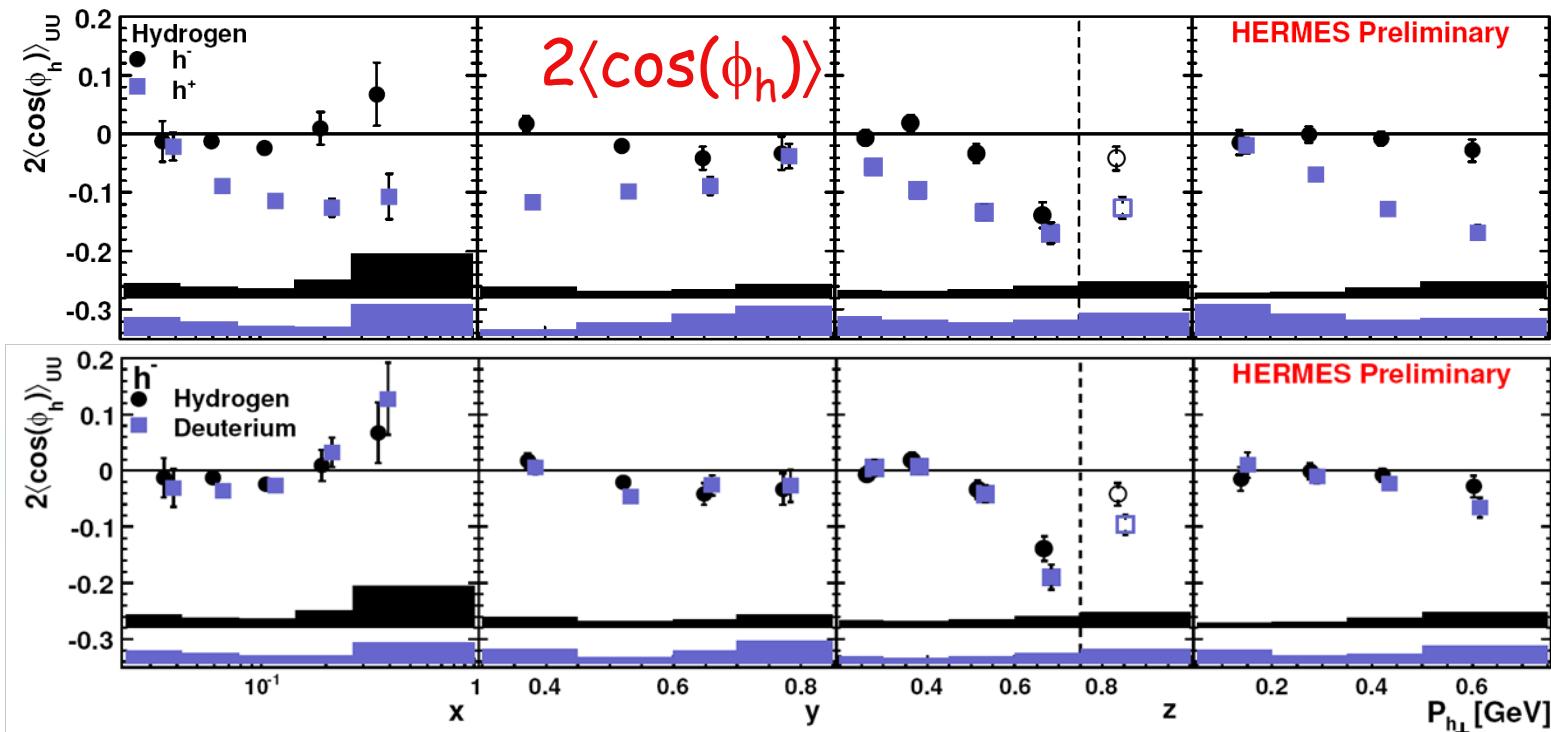
Cahn effect



| N/q | U              | L        | T                    |
|-----|----------------|----------|----------------------|
| U   | $f_1$          |          | $h_1^\perp$          |
| L   |                | $g_1$    | $h_{1L}^\perp$       |
| T   | $f_{1T}^\perp$ | $g_{1T}$ | $h_1$ $h_{1T}^\perp$ |

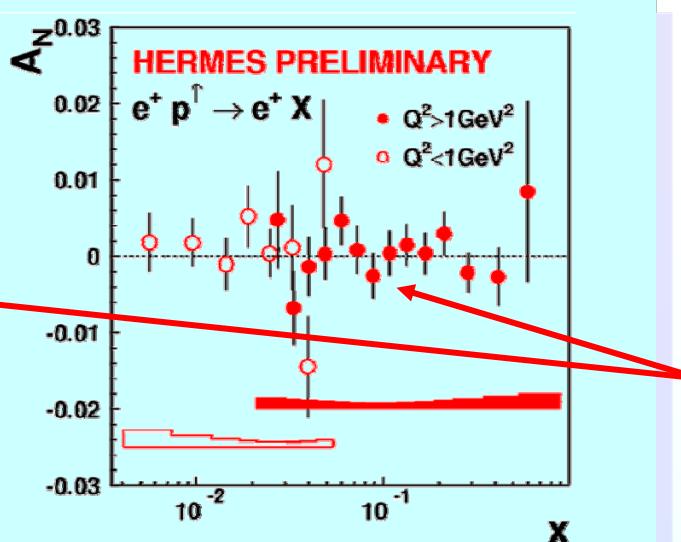
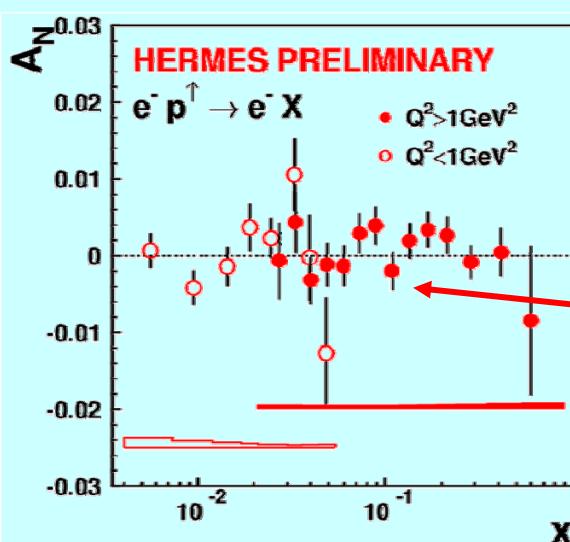
$$F_{UU}^{\cos\phi} = \frac{2M}{Q} C \left[ -\frac{\hat{h} \cdot \vec{p}_T}{M_h} x \langle h_1^\perp H_1^\perp \rangle - \frac{\hat{h} \cdot \vec{k}_T}{M} x \langle f_1 D_1 \rangle \right]$$

Intrinsic transverse quark momentum



# Transverse Azimuthal Asymmetry in DIS

1-photon exchange approximation: TAA forbidden



(Spin-flip every 90 s)

$A_N \neq 0$ : Signature of  
2-photon exchange

$$A_N = O(10^{-3})$$

Compatible  
with zero !

- HERMES provides new constraints for  $S(x)$  at low  $Q^2$
  
- HERMES made a first glimpse at various Transverse Momentum dependent parton Distribution functions
  
- TMDs offer a large amount of new information on the nucleon structure They need to be explored in detail by the next generation of experiments at future high-luminosity e-N facilities