



# Charged-hadron lepto-production off unpolarized protons and deuterons at hermes







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  - both are ingredients of basically every (spin) asymmetry
  - may probe quark flavors less accessible in inclusive DIS
- complimentary info on FFs to  $e^+e^-$  (e.g., charge separation)

#### Polarization-averaged cross section



$$\frac{d^5\sigma}{dxdydzd\phi_h dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$$

 $\vec{P}_h$ 

 $+\sqrt{2\epsilon(1-\epsilon)}F_{UU}^{\cos\phi_h}\cos\phi_h + \epsilon F_{UU}^{\cos2\phi_h}\cos2\phi_h\}$ 



[see, e.g., Bacchetta et al., JHEP 0702 (2007) 093]

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## Some experimental challenges ...

- pureness of targets
- Iarge kinematic acceptance
- excellent particle identification
- no spin asymmetry -> worry more about systematics, e.g.,
  - efficiencies
  - absolute luminosity
  - acceptance
  - smearing

## The HERMES Experiment

27.5 GeV  $e^+/e^-$  beam of HERA





## The HERMES Experiment

- pure gas targets
- internal to lepton ring
- unpolarized (<sup>1</sup>H ... Xe)
- Iong. polarized: <sup>1</sup>H, <sup>2</sup>H, <sup>3</sup>He
- transversely polarized: <sup>1</sup>H





## ... schematically



Particle ID detectors allow for

- lepton/hadron separation
- RICH: pion/kaon/proton discrimination 2GeV<p<15GeV

#### accessing the various terms

$$\frac{d^5\sigma}{dxdydzd\phi_h dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \{F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1-\epsilon)} F_{UU}^{\cos\phi_h} \cos\phi_h + \epsilon F_{UU}^{\cos2\phi_h} \cos2\phi_h\}$$

## accessing the various terms

hadron multiplicity: normalize to inclusive DIS cross section

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# accessing the various terms

hadron multiplicity: normalize to inclusive DIS cross section

 $\frac{1}{dxdy} \propto F_T + \epsilon F_L$ 

 $d^2 \sigma^{\text{incl.DIS}}$ 

$$\frac{d^4 \mathcal{M}^h(x, y, z, P_{h\perp}^2)}{dx dy dz dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \frac{F_{UU,T} + \epsilon F_{UU,L}}{F_T + \epsilon F_L}$$

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## accessing the various terms hadron multiplicity: normalize to inclusive DIS $\frac{d^4 \mathcal{M}^h(x, y, z, P_{h\perp}^2)}{dx dy dz dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \frac{F_{UU,T} + \epsilon F_{V,L}}{F_T + \epsilon F_{L}}$ cross section $d^2 \sigma^{\text{incl.DIS}}$ $\frac{\sigma}{dxdy} \propto F_T + \epsilon F_L$ $\approx \frac{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^{q \to h}(z, K_T^2)}{\sum_q e_q^2 f_1^q(x)}$ $\frac{d^5\sigma}{dxdydzd\phi_h dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$ $+\sqrt{2\epsilon(1-\epsilon)}F_{UU}^{\cos\phi_h}\cos\phi_h + \epsilon F_{UU}^{\cos2\phi_h}\cos2\phi_h\}$

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 $+\sqrt{2\epsilon(1-\epsilon)}F_{UU}^{\cos\phi_h}\cos\phi_h+\epsilon F_{UU}^{\cos2\phi_h}\cos2\phi_h\}$ 

moments: normalize to azimuthindependent cross-section









#### ... event migration ...



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## inversion of relation gives Born cross section from measured yields G. Schnell SPIN2016

## Multi-D vs. 1D unfolding at work



Neglecting to unfold in z changes x dependence dramatically 1D unfolding clearly insufficient

### kinematic range used at HERMES



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#### Influence from exclusive VM

for instance:  $ep \rightarrow ep \rho^0 \rightarrow ep \pi^+ \pi^-$ 



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## Multiplicities: z projection

most exhaustive data set on ( $P_{h\perp}$ -integrated) electro-production of charged identified mesons on nucleons



 slight differences between proton and deuteron targets: reflection of valence structure of target and produced meson, e.g. u/d -> π<sup>+</sup> / π<sup>-</sup> p = |uud> and n = |udd>

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 K<sup>-</sup> pure "sea object" hence suppressed and hardly any difference for proton and deuteron

## Multiplicities: z projection



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proton target:
(deuteron similar)

- positive hadrons in general better described than negative ones
  - better understanding of favored fragmentation?
- best described by HERMES Jetset tune and DSS FF set

kaons best described by DSS FF set, though all with problems in describing K<sup>-</sup>

## Multiplicity ratio: z projection



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## Multiplicity ratio: z projection



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## Multiplicities: x-z projection



#### Multiplicities: x-z projection



## Multiplicities: x-z projection



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weaker dependence on x

remaining dependence from f<sub>1</sub> - D<sub>1</sub> convolution over quark flavors

$$\sum_{q} \frac{e_q^2 f_1^q(x)}{\sum_{q'} e_{q'}^2 f_1^{q'}(x)} D_1^{q \to \pi}(z)$$

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#### Strange-quark distribution

- use isoscalar probe and target to extract (here at LO!) strange-quark distribution
- only need K<sup>+</sup>+K<sup>-</sup> multiplicities on deuteron

$$S(x)\int \mathcal{D}_{S}^{K}(z) \, \mathrm{d}z \simeq Q(x) \left[ 5 \frac{\mathrm{d}^{2} N^{K}(x)}{\mathrm{d}^{2} N^{\mathrm{DIS}}(x)} - \int \mathcal{D}_{Q}^{K}(z) \, \mathrm{d}z \right]$$



$$\begin{split} \mathbf{S}(\mathbf{x}) &= \mathbf{s}(\mathbf{x}) + \mathbf{\bar{s}}(\mathbf{x}) \\ \mathbf{Q}(\mathbf{x}) &= \mathbf{u}(\mathbf{x}) + \mathbf{\bar{u}}(\mathbf{x}) + \mathbf{d}(\mathbf{x}) + \mathbf{\bar{d}}(\mathbf{x}) \\ \mathcal{D}_{\mathbf{S}}^{\mathbf{K}} &= \mathbf{D}_{1}^{\mathbf{s} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\mathbf{\bar{s}} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\mathbf{s} \rightarrow \mathbf{K}^{-}} + \mathbf{D}_{1}^{\mathbf{\bar{s}} \rightarrow \mathbf{K}^{-}} \\ \mathcal{D}_{\mathbf{Q}}^{\mathbf{K}} &= 4\mathbf{D}_{1}^{\mathbf{u} \rightarrow \mathbf{K}^{+}} + 4\mathbf{D}_{1}^{\mathbf{\bar{u}} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\mathbf{d} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\mathbf{\bar{d}} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_$$

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assume vanishing strangeness at high x to extract non-strange fragmentation



$$\begin{split} \mathbf{S}(\mathbf{x}) &= \mathbf{s}(\mathbf{x}) + \overline{\mathbf{s}}(\mathbf{x}) \\ \mathbf{Q}(\mathbf{x}) &= \mathbf{u}(\mathbf{x}) + \overline{\mathbf{u}}(\mathbf{x}) + \mathbf{d}(\mathbf{x}) + \overline{\mathbf{d}}(\mathbf{x}) \\ \mathcal{D}_{\mathbf{S}}^{\mathbf{K}} &= \mathbf{D}_{1}^{\mathbf{s} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\overline{\mathbf{s}} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\mathbf{s} \rightarrow \mathbf{K}^{-}} + \mathbf{D}_{1}^{\overline{\mathbf{s}} \rightarrow \mathbf{K}^{-}} \\ \mathcal{D}_{\mathbf{Q}}^{\mathbf{K}} &= 4\mathbf{D}_{1}^{\mathbf{u} \rightarrow \mathbf{K}^{+}} + 4\mathbf{D}_{1}^{\overline{\mathbf{u}} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\mathbf{d} \rightarrow \mathbf{K}^{+}} + \mathbf{D}_{1}^{\overline{\mathbf{d}} \rightarrow \mathbf{K}^{+}} + \dots \end{split}$$

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• assume vanishing strangeness at high x to extract non-strange fragmentation



#### Transverse momentum dependence

- multi-dimensional analysis allows going beyond collinear factorization
- flavor information on transverse momenta via target variation and hadron ID



#### Transverse momentum dependence

- multi-dimensional analysis allows going beyond collinear factorization
- flavor information on transverse momenta via target variation and hadron ID
   TMD VII session



#### caveats

all the data available at <u>http://hermes.desy.de/multiplicities</u>

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- important consequences
  - comparison to calculations best done performing the same integration over phase space

• average multiplicity is not multiplicity at average kinematics

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 even though having similar average kinematics, multiplicities in the two projections are different

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- the average along the valley will be smaller than the average along the gradient
- still the average kinematics can be the same

# integrating vs. using average kinematics

(by now old)
 DSS07 FF fit to
 z-Q<sup>2</sup> projection

z-x "prediction" reasonable well when using integration over phase-space limits (red lines) 10



# integrating vs. using average kinematics

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 DSS07 FF fit to
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z-x "prediction" reasonable well when using integration over phase-space limits (red lines) 10

significant changes when using average kinematics



... anticip





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## not all can (yet) be extracted from data

- e.g., observables that rely on perfect cancelations of large quantities in order to access inherently small quantities
  - it was suggested to look at a different combination of multiplicities than in the isoscalar extraction of s(x) to test the latter
  - involves difference of multiplicities, which emphasizes small corrections that might be needed to perfectly describe multiplicities:

$$\frac{\mathrm{d}N^{K'}}{\mathrm{d}N^{\mathrm{DIS}}} \equiv \frac{5Q+2S}{Q} \frac{\mathrm{d}N^{K}}{\mathrm{d}N^{\mathrm{DIS}}} - \frac{5Q+2S}{u_{v}+d_{v}} \frac{\mathrm{d}N^{\mathrm{Kdiff}}}{\mathrm{d}N^{\mathrm{DIS}}}$$
$$\stackrel{\mathrm{LO},s=\bar{s}}{\equiv} 8D_{\bar{u}}^{K^{+}} + 2D_{\bar{d}}^{K^{+}} + \frac{S}{Q}D_{S}^{K}$$

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Iarge spread both from (limited) knowledge of PDFs (left) and FFs (right)

no high-x limit to be used to constrain disfavored kaon FFs

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similar problem when look at just the ("scaled") difference multiplicity

$$\frac{dN^{K^{\text{diff}}}}{dN^{\text{DIS}}} \equiv \frac{d(N^{K^+} - N^{K^-})}{dN^{\text{DIS}}}$$
$$\underbrace{LO_{,s} = \bar{s}}_{LO_{,s} = \bar{s}} \frac{(u_v + d_v)(4D_u^{K^+} - 4D_{\bar{u}}^{K^+} + D_d^{K^+} - D_{\bar{d}}^{K^+})}{5Q + 2S}$$

#### Conclusions

- HERMES managed step from spin-asymmetry experiment to unpolarized-target experiment
- most comprehensive data set on charged-separated identified meson lepto-production on both proton and deuterons
- multi-dimensional analysis and various targets allow study of correlations and flavor dependences
- analysis of averages requires careful consideration of kinematic ranges averaged over
- transverse-momentum dependence -> TMD Session VII

## backup slides



#### **COMPASS** multi-D binning

