

Overview of recent HERMES results on transverse-momentum-dependent spin asymmetries in semi-inclusive DIS

Gunar.Schnell @ DESY.de

Spin-momentum structure of the nucleon

$$\frac{1}{2}\text{Tr}\left[(\gamma^+ + \lambda\gamma^+\gamma_5)\Phi\right] = \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + \lambda\Lambda g_1 + \lambda S^i k^i\frac{1}{m}g_{1T}\right]$$

$$\frac{1}{2}\text{Tr}\left[(\gamma^+ - s^j i\sigma^{+j}\gamma_5)\Phi\right] = \frac{1}{2}\left[f_1 + S^i\epsilon^{ij}k^j\frac{1}{m}f_{1T}^\perp + s^i\epsilon^{ij}k^j\frac{1}{m}h_1^\perp + s^i S^i h_1\right. \\ \left.+ s^i(2k^i k^j - \mathbf{k}^2\delta^{ij})S^j\frac{1}{2m^2}h_{1T}^\perp + \Lambda s^i k^i\frac{1}{m}h_{1L}^\perp\right]$$

quark pol.

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

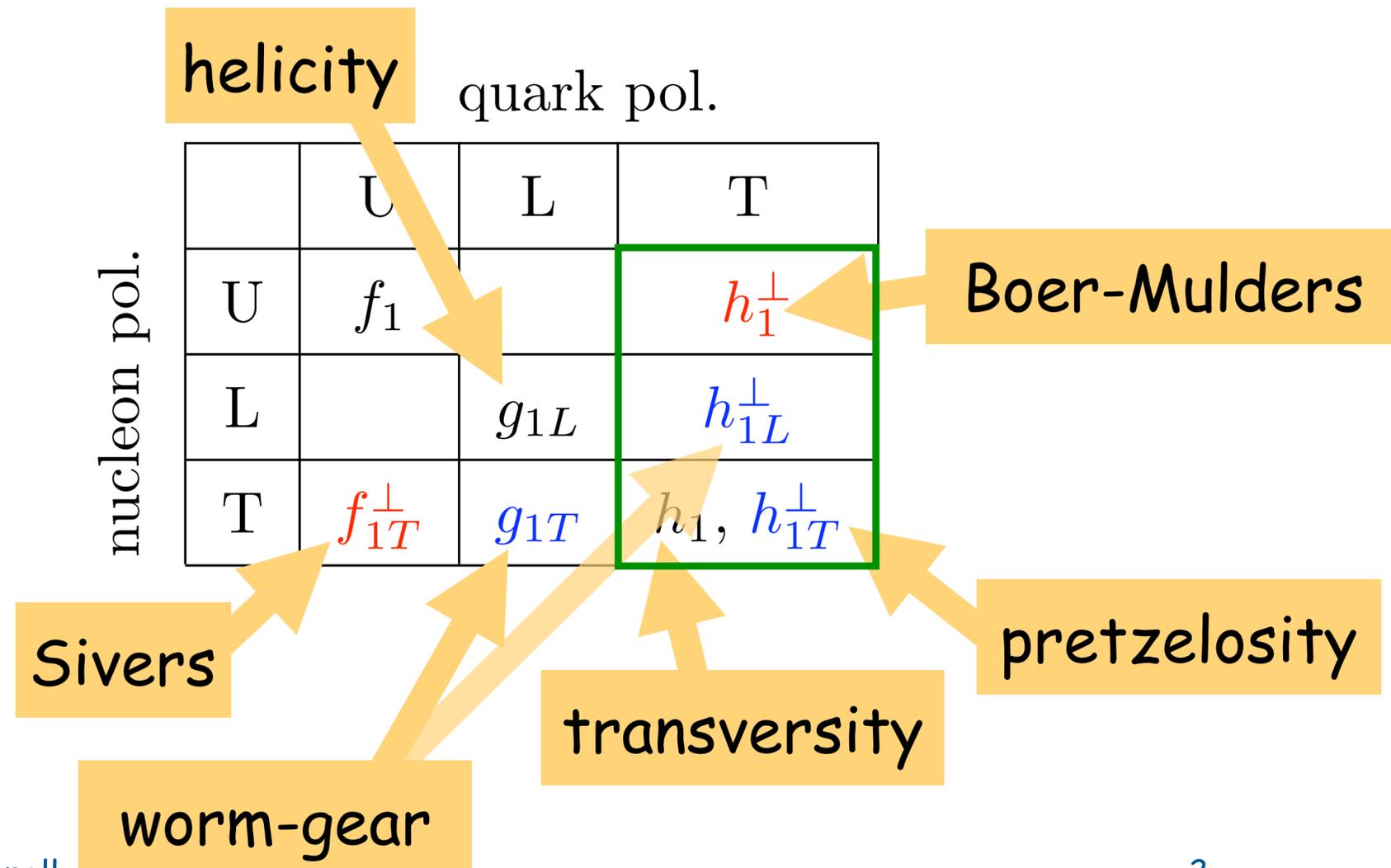
nucleon pol.

- each TMD describes a particular spin-momentum correlation
- functions in black survive integration over transverse momentum
- functions in green box are chirally odd
- functions in red are naive T-odd

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TMDs in hadronization

quark pol.

	U	L	T
hadron pol.	U	D_1	H_1^\perp
	L		G_1
	T	D_{1T}^\perp	G_{1T}^\perp
			H_1 H_{1T}^\perp

TMDs in hadronization

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T	D_{1T}^\perp	G_{1T}^\perp	$H_1 \quad H_{1T}^\perp$

→ relevant for unpolarized final state

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→ relevant for unpolarized final state

Collins FF: $H_1^\perp, q \rightarrow h$

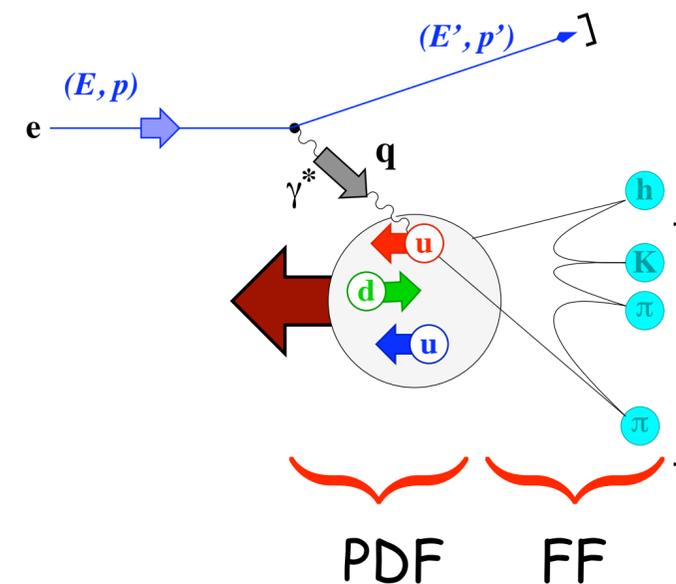
ordinary FF: $D_1^{q \rightarrow h}$

TMDs in hadronization

quark pol.

	U	L	T		
hadron pol.	U	D_1		H_1^\perp	<p>→ relevant for unpolarized final state</p> <p>} polarized final-state hadrons</p>
	L		G_1	H_{1L}^\perp	
	T	D_{1T}^\perp	G_{1T}^\perp	H_1 H_{1T}^\perp	

Probing TMDs in semi-inclusive DIS



		quark pol.		
		U	L	T
nucleon pol.	U	f_1		h_1^\perp
	L		g_{1L}	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

in SIDIS*) couple PDFs to:

Collins FF: $H_1^{\perp, q \rightarrow h}$

ordinary FF: $D_1^{q \rightarrow h}$

⇒ give rise to characteristic azimuthal dependences

*) semi-inclusive DIS with unpolarized final state

semi-inclusive DIS

- excluding transverse polarization:

$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \right.$$

$$+ \sqrt{2\epsilon} \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi$$

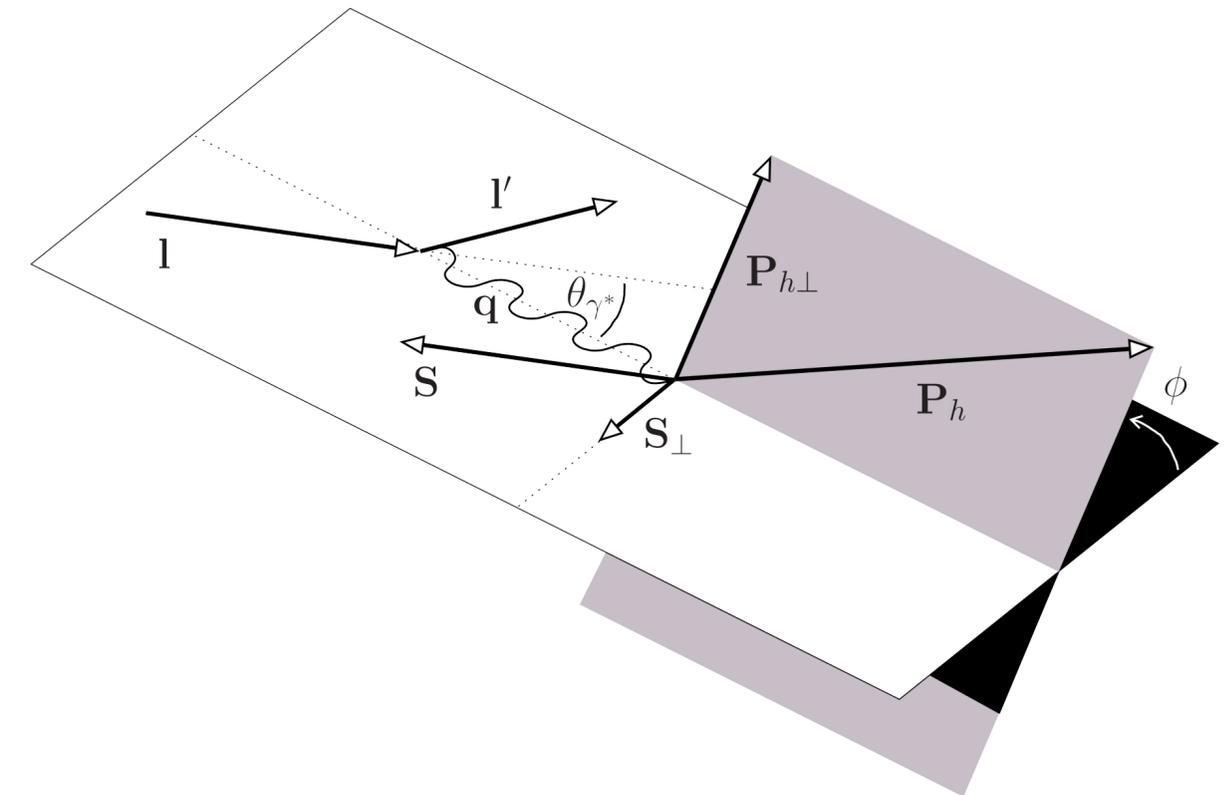
$$+ \sqrt{2\epsilon} \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi$$

$$\left. + \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \right\}$$

$$F_{XY}^{h,\text{mod}} = F_{XY}^{h,\text{mod}}(x, Q^2, z, P_{h\perp})$$



 Beam (λ) / Target (Λ)
 helicities



semi-inclusive DIS

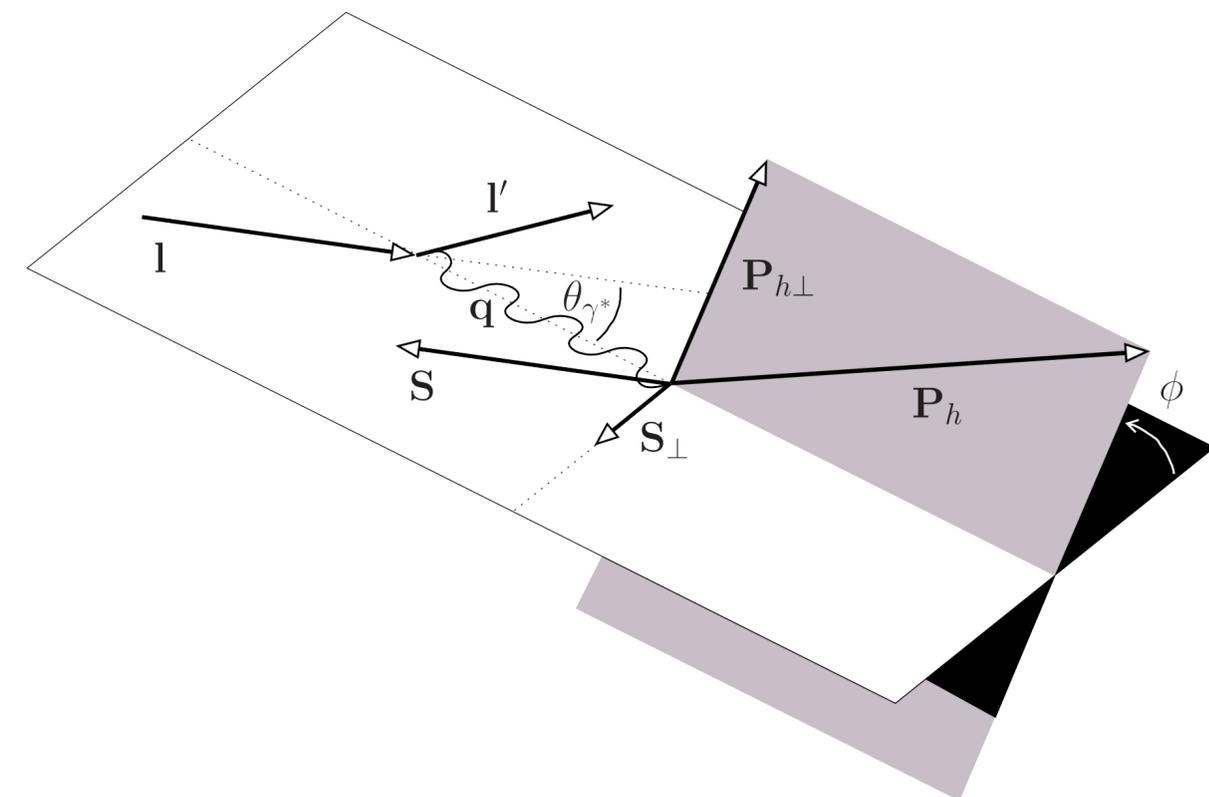
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$$\left\{ \begin{aligned} &F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \\ &+ \sqrt{2\epsilon} \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi \\ &+ \sqrt{2\epsilon} \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi \\ &+ \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \end{aligned} \right\}$$

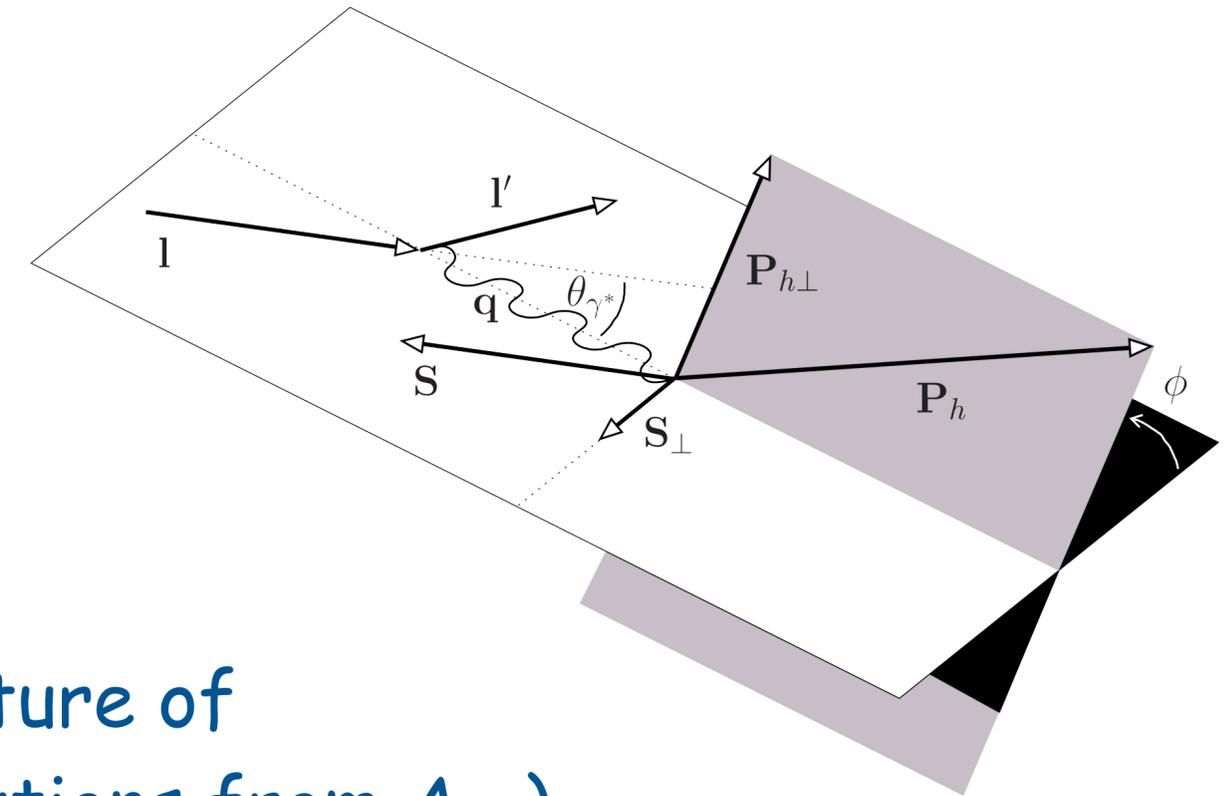
- double-spin asymmetry:

$$A_{LL}^h \equiv \frac{\sigma_{++}^h - \sigma_{+-}^h + \sigma_{--}^h - \sigma_{-+}^h}{\sigma_{++}^h + \sigma_{+-}^h + \sigma_{--}^h + \sigma_{-+}^h}$$



semi-inclusive DIS

- in experiment extract instead $A_{||}$ which differs from A_{LL} in the way the polarization is measured:
- A_{LL} : along virtual-photon direction
- $A_{||}$: along beam direction (results in small admixture of transverse target polarization and thus contributions from A_{LT})
- $A_{||}$ related to virtual-photon-nucleon asymmetry A_1



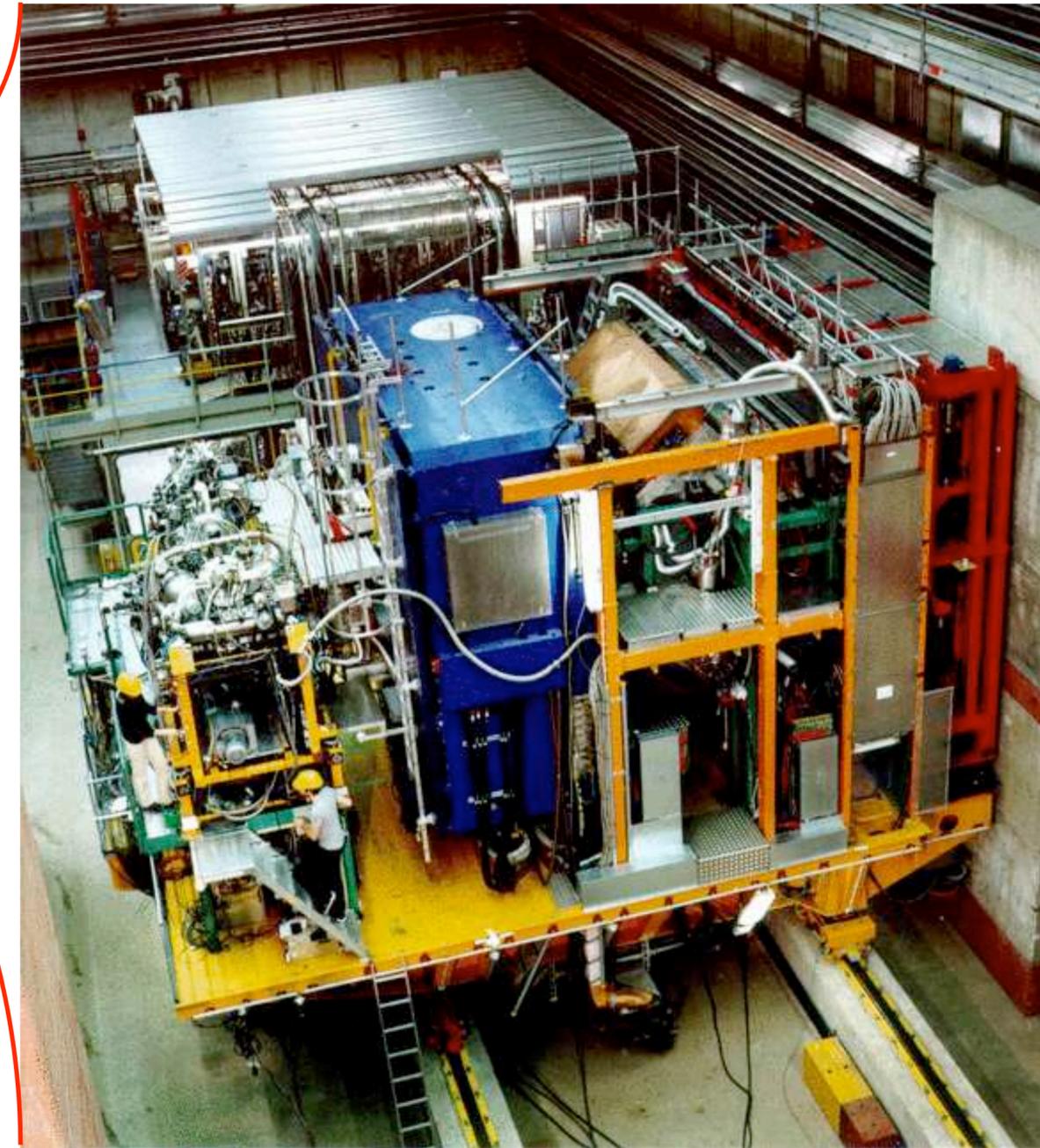
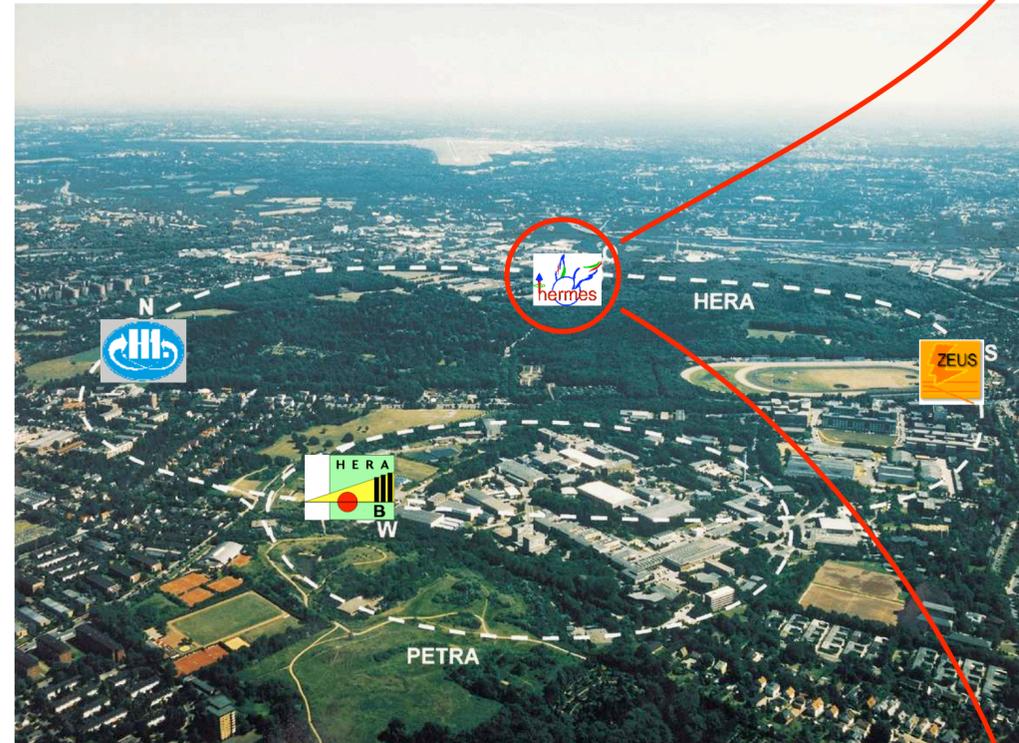
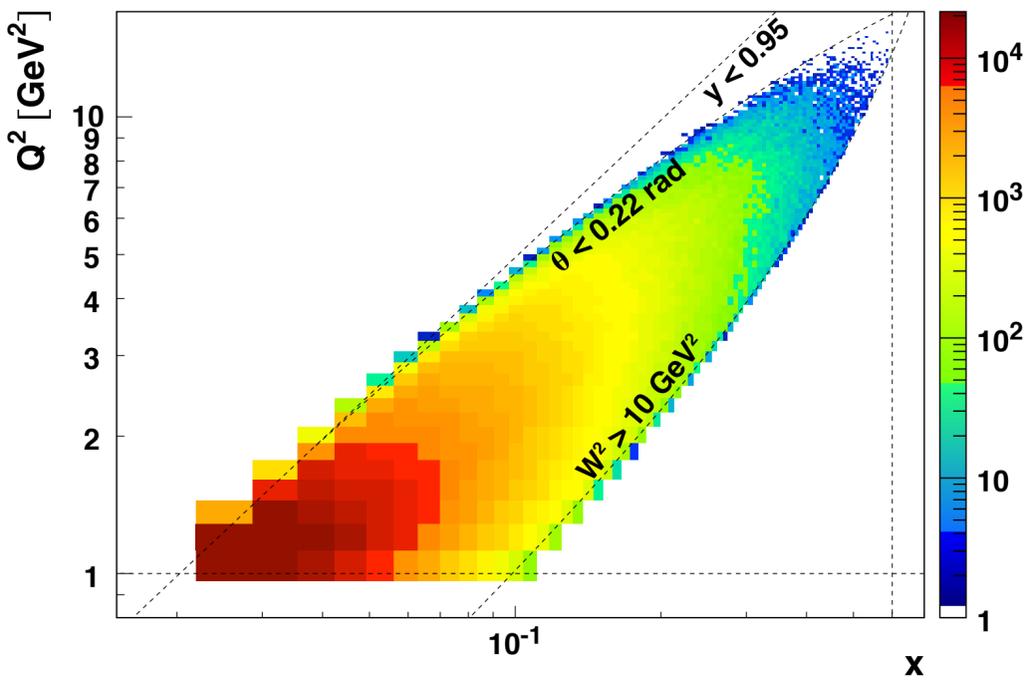
$$A_1^h = \frac{1}{D(1 + \eta\gamma)} A_{||}^h$$

$$D = \frac{1 - (1 - y)\epsilon}{1 + \epsilon R}$$

$$\eta = \frac{\epsilon\gamma y}{1 - (1 - y)\epsilon}$$

HERMES (†2007) @ DESY

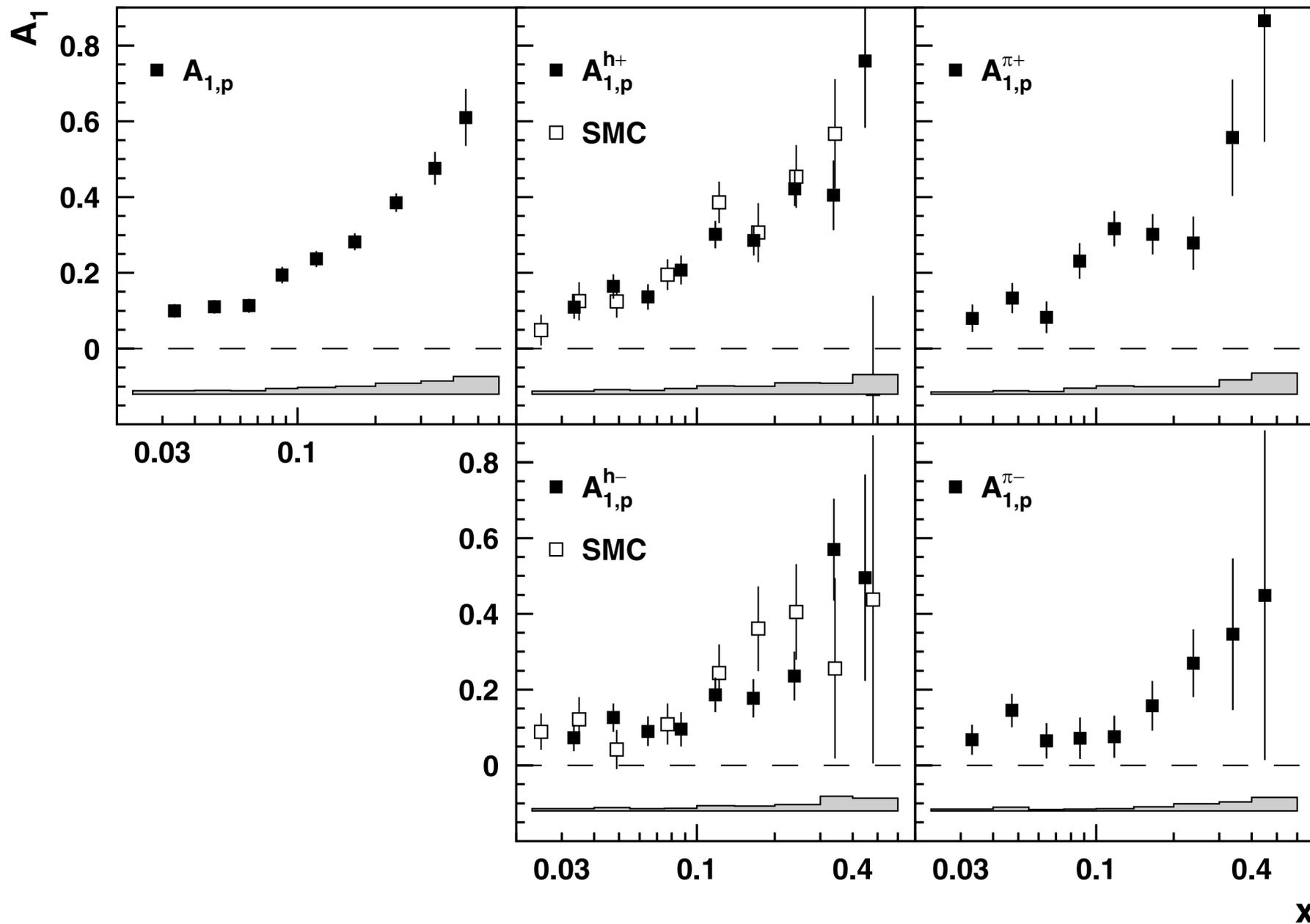
27.6 GeV polarized e^+/e^- beam scattered off ...



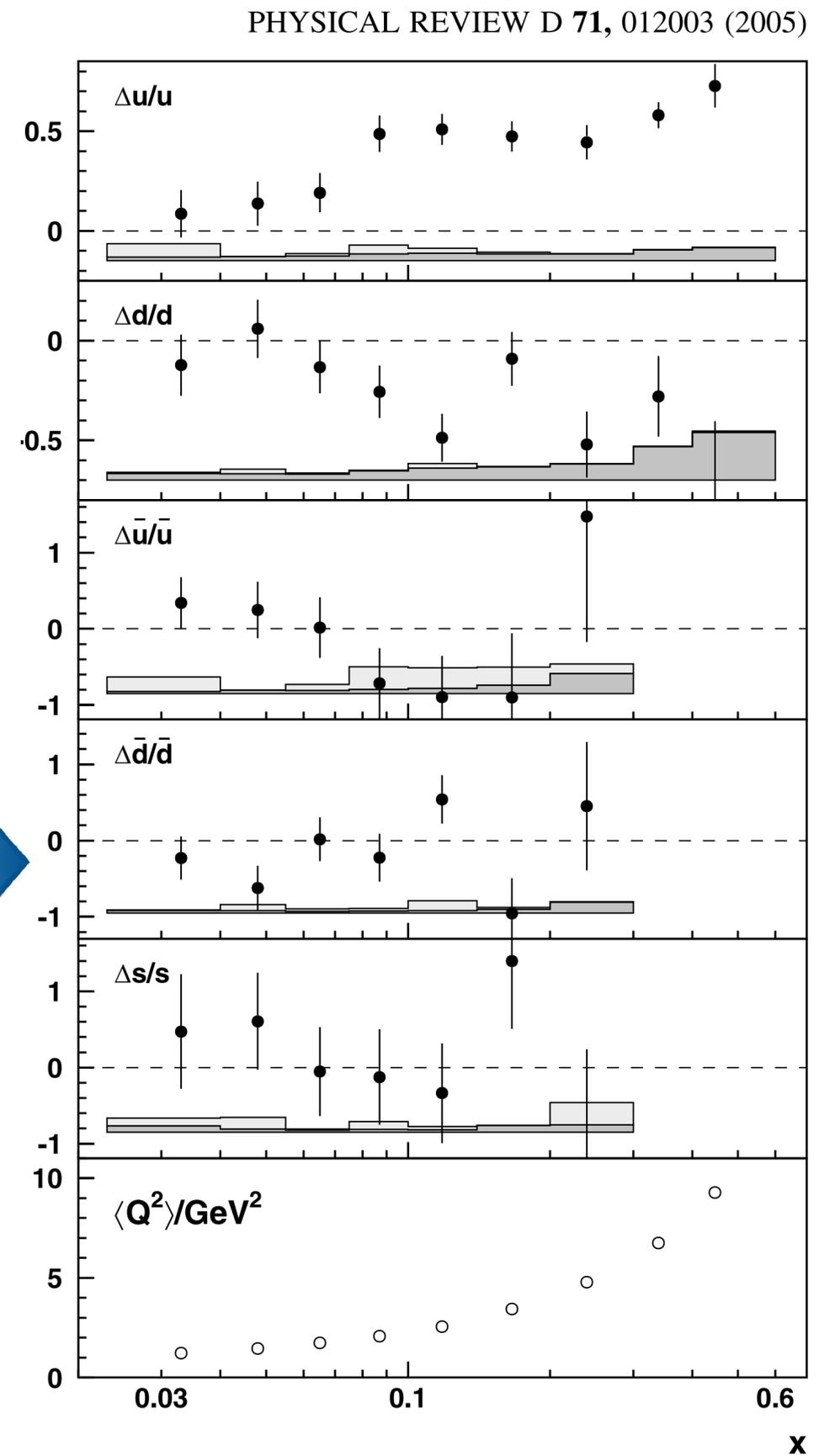
- ✓ unpolarized (H, D, He, ..., Xe) as well as
- ✓ transversely (H) or longitudinally (H, D, He) polarized pure gas targets
- ✓ particle ID (incl. dual-radiator RICH) for efficient $e/\pi/K/p$ separation

previous HERMES analysis

- (semi-) inclusive asymmetries used for LO extraction of helicity PDFs



Monte Carlo



re-analysis of double-spin asymmetries

- revisited [PRD 71 (2005) 012003] A_1 analysis at HERMES in order to
 - exploit slightly larger data set (less restrictive momentum range)
 - provide $A_{||}$ in addition to A_1

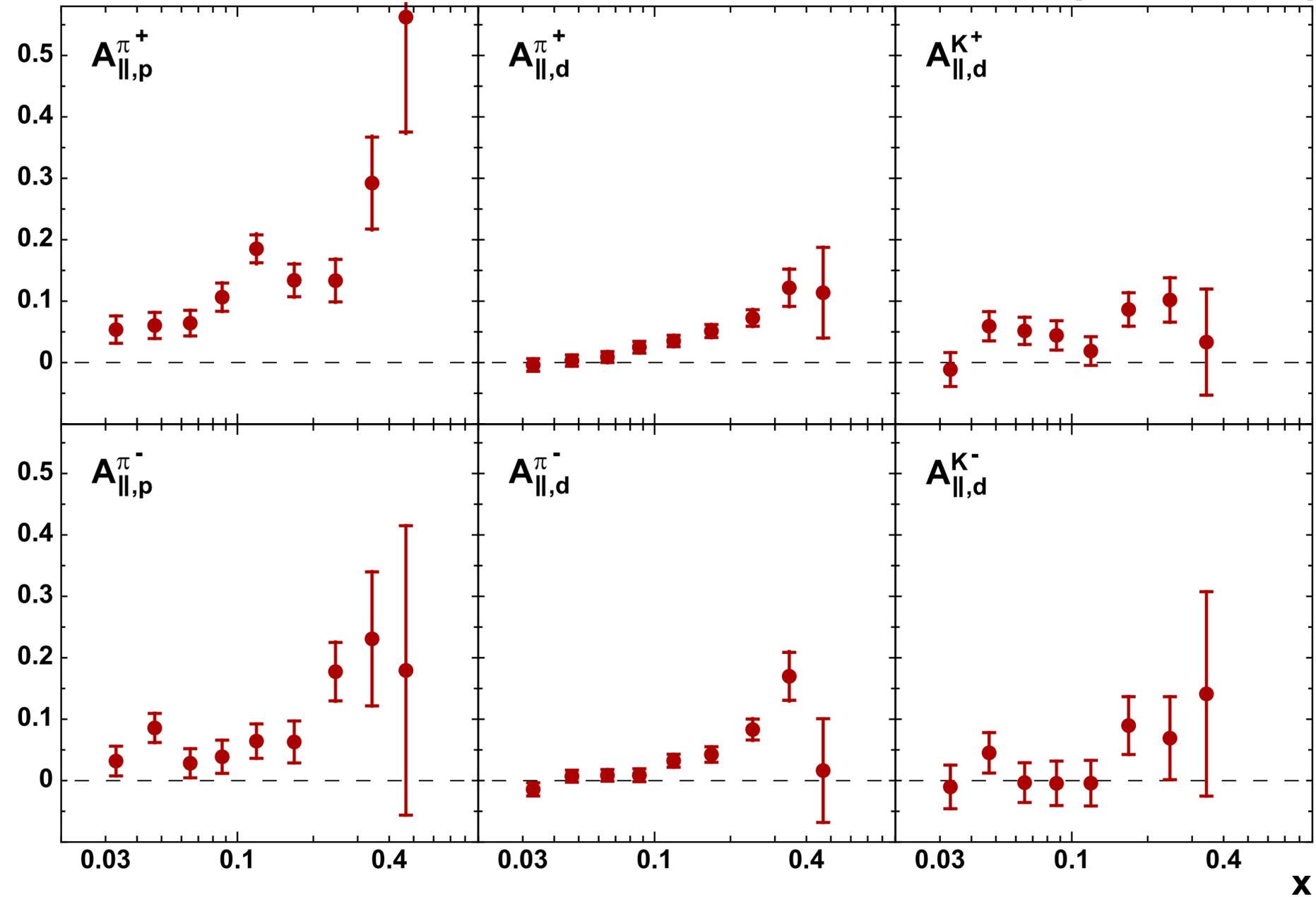
$$A_1^h = \frac{1}{D(1 + \eta\gamma)} A_{||}^h \quad D = \frac{1 - (1 - y)\epsilon}{1 + \epsilon R}$$

R (ratio of longitudinal-to-transverse cross-sec'n) still to be measured!
[only available for inclusive DIS data, e.g., used in g_1 SF measurements]

- correct for D-state admixture (deuteron case) on asymmetry level
- correct better for azimuthal asymmetries coupling to acceptance
- look at multi-dimensional ($x, z, P_{h\perp}$) dependences
- extract twist-3 cosine modulations

x dependence of $A_{||}$

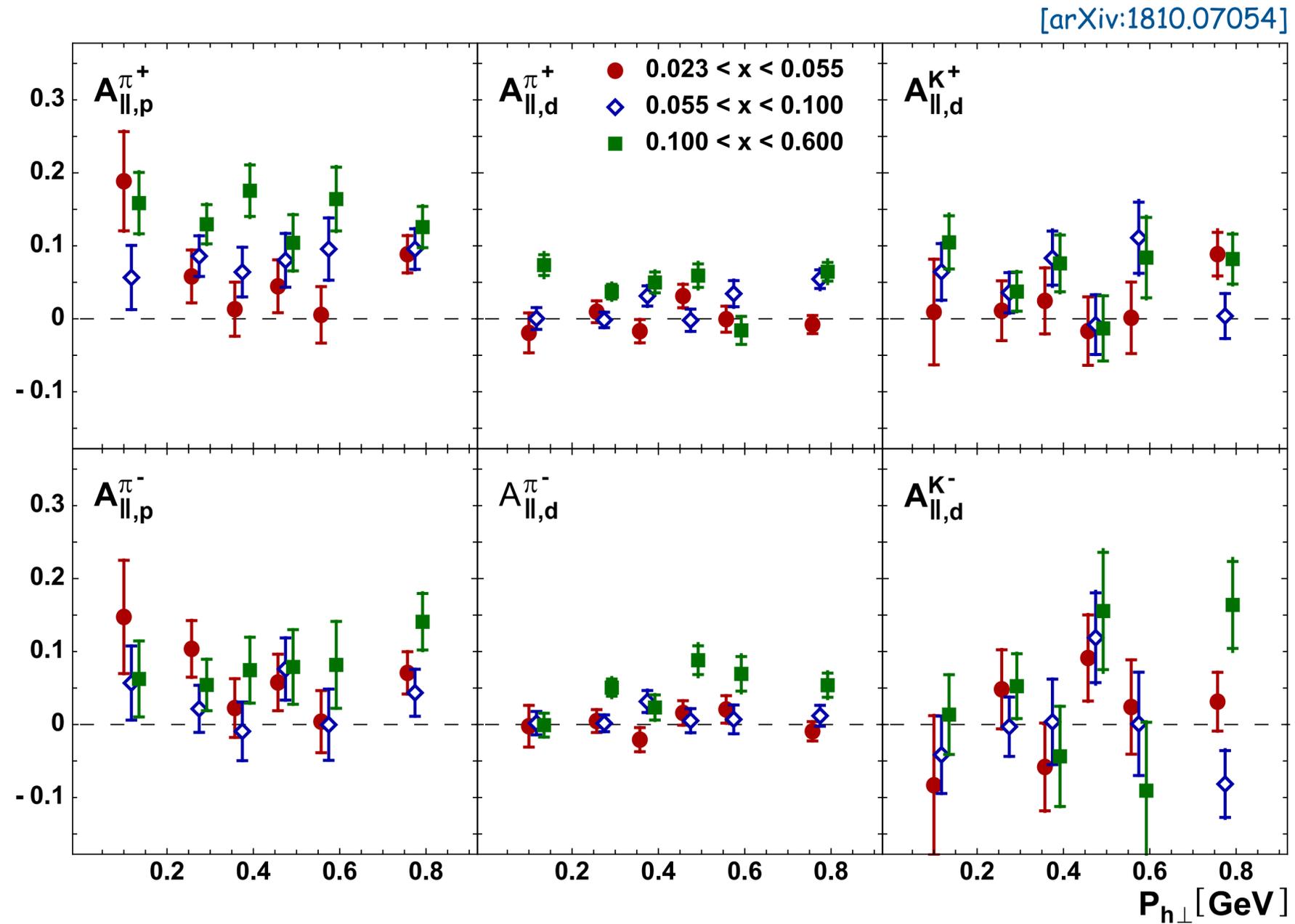
[arXiv:1810.07054]



☑ fully consistent with previous HERMES publication [PRD 71 (2005) 012003]

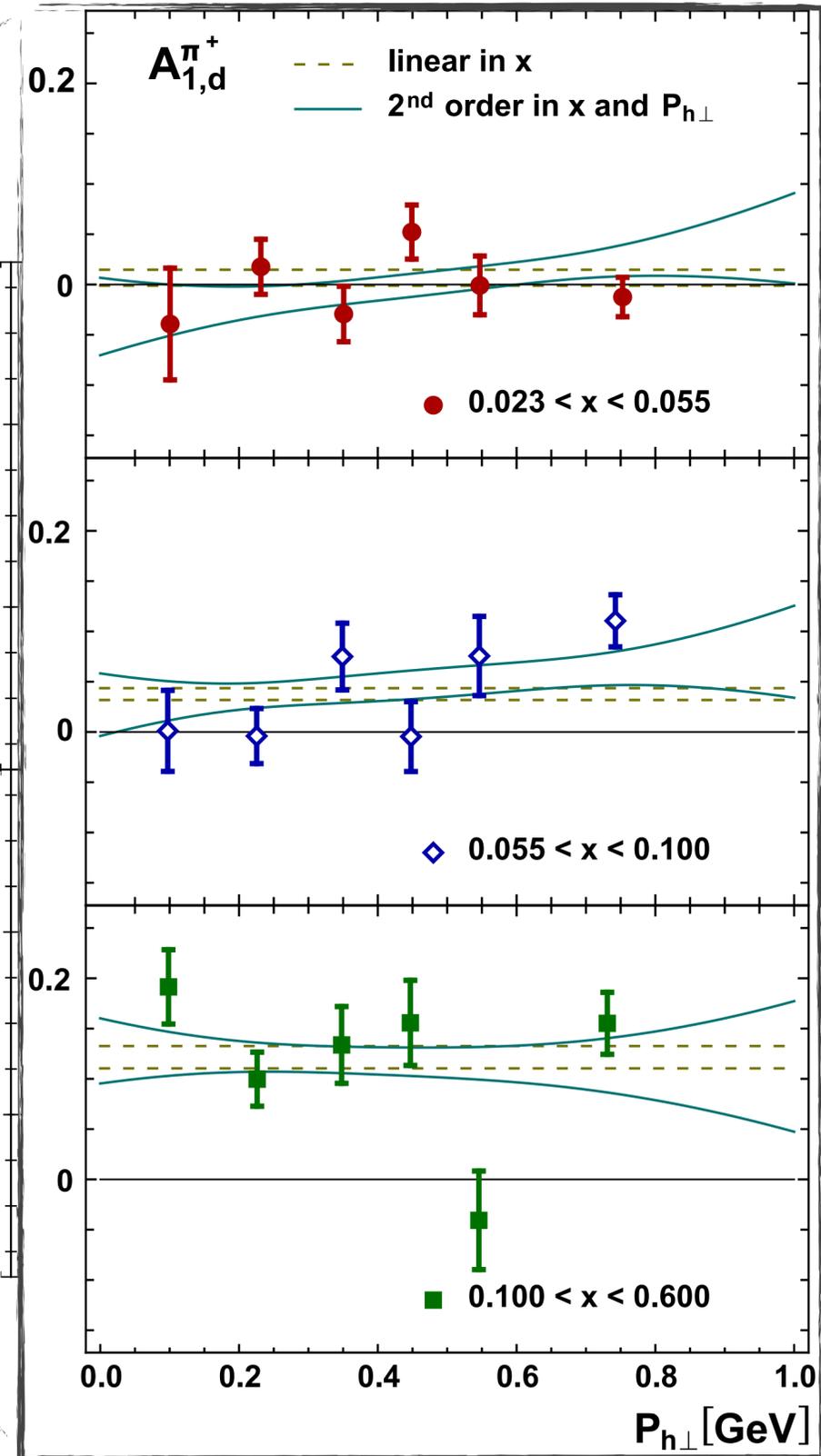
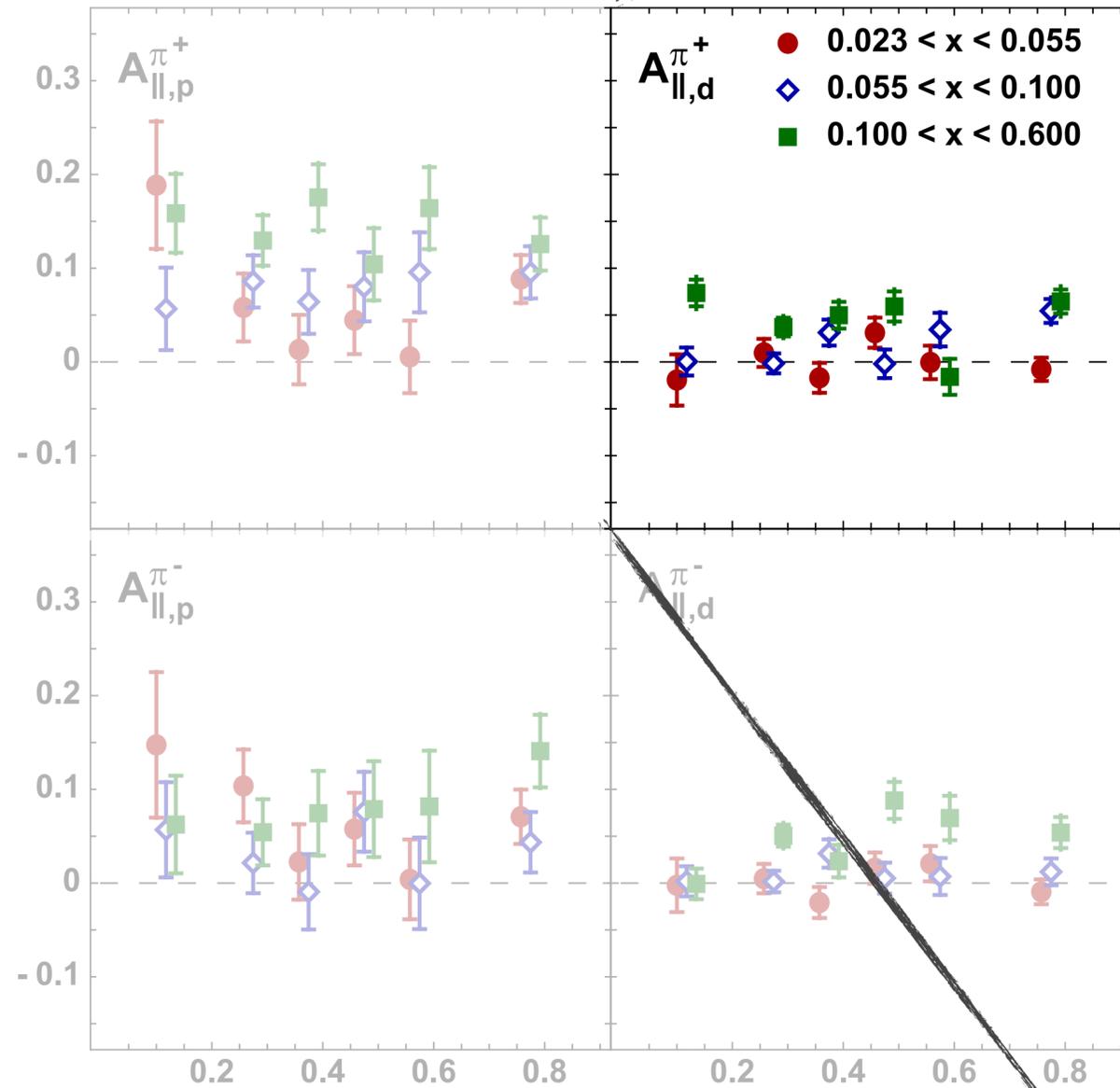
$P_{h\perp}$ dependence of $A_{||}$ (three x ranges)

- no strong dependence (beyond on x)



$P_{h\perp}$ dependence of $A_{||}$ (three x ranges)

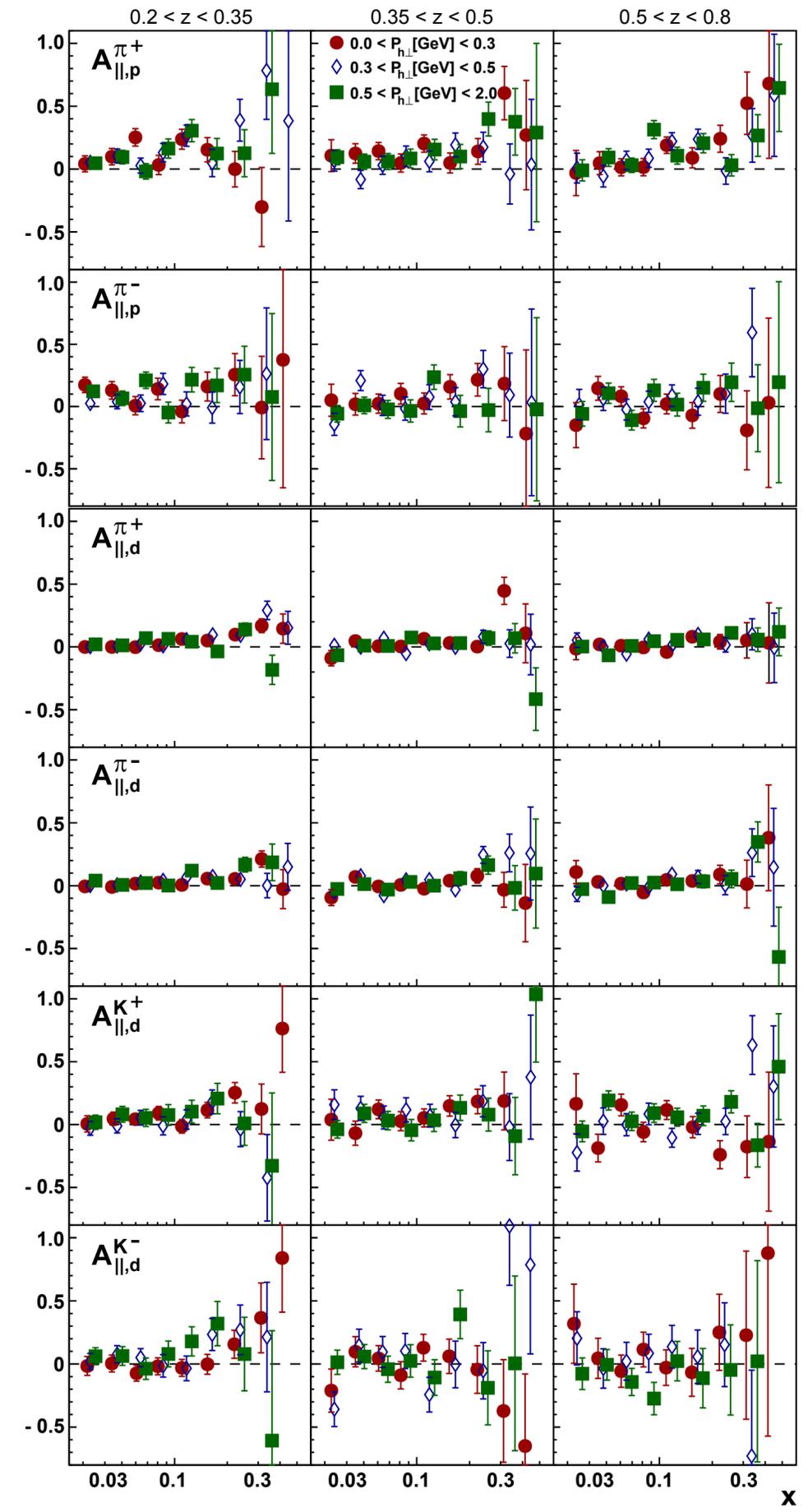
- no strong dependence (beyond on x)



- also fit to A_1 fit does not favor an additional dependence on $P_{h\perp}$

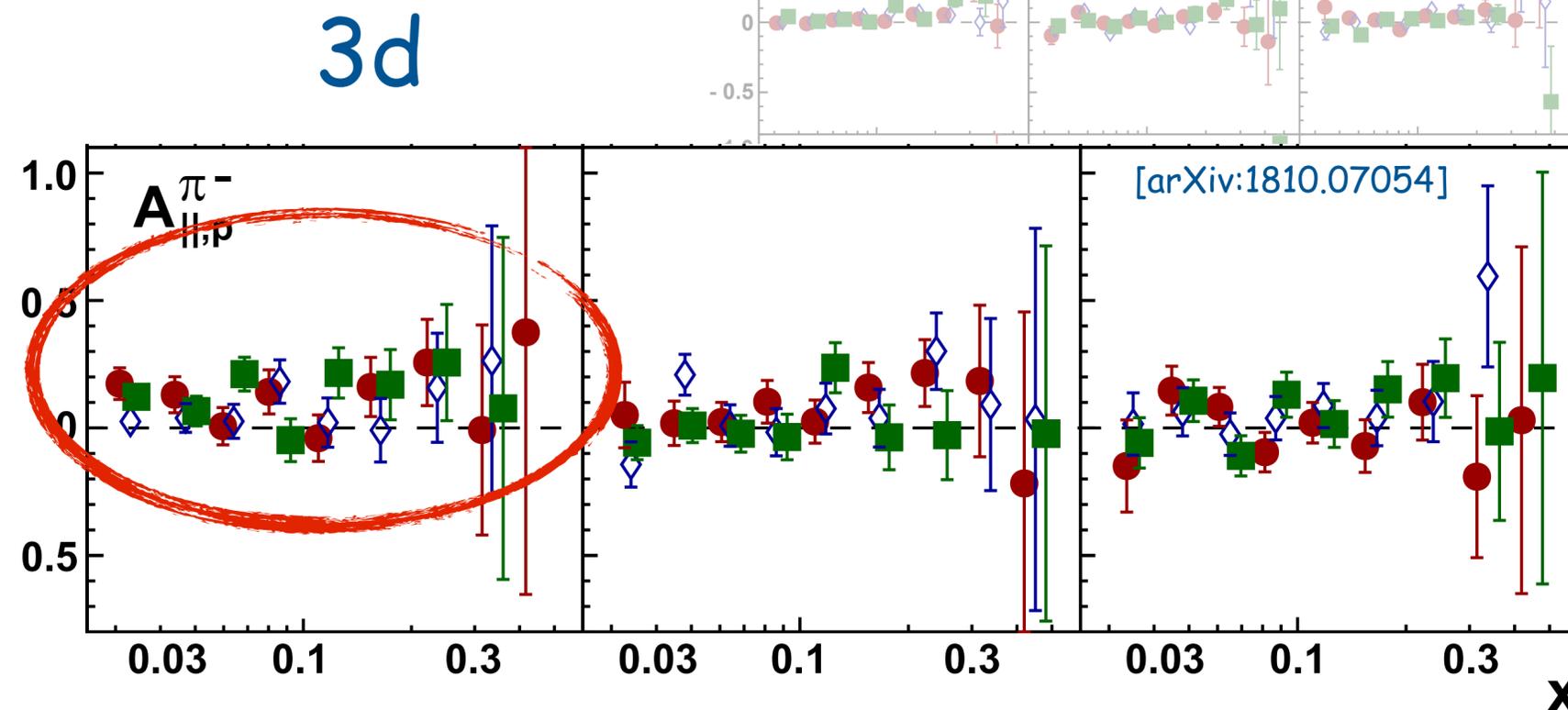
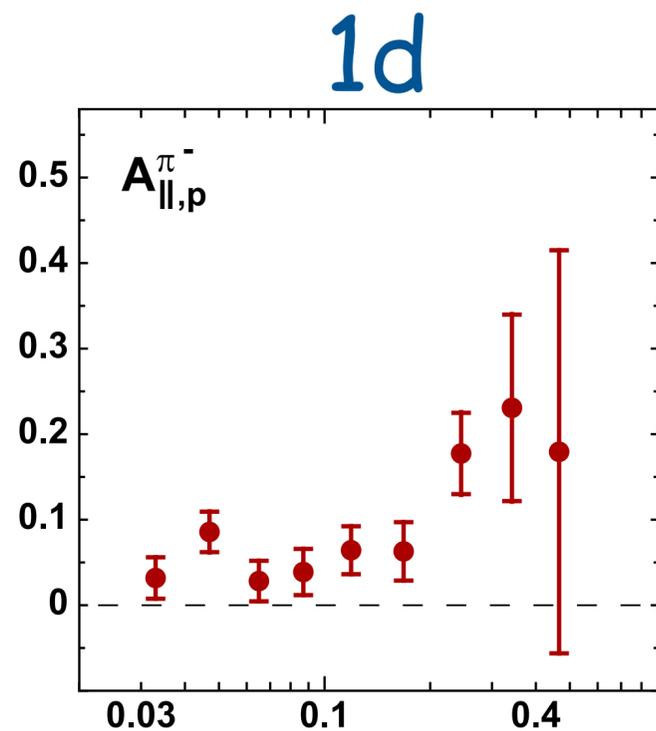
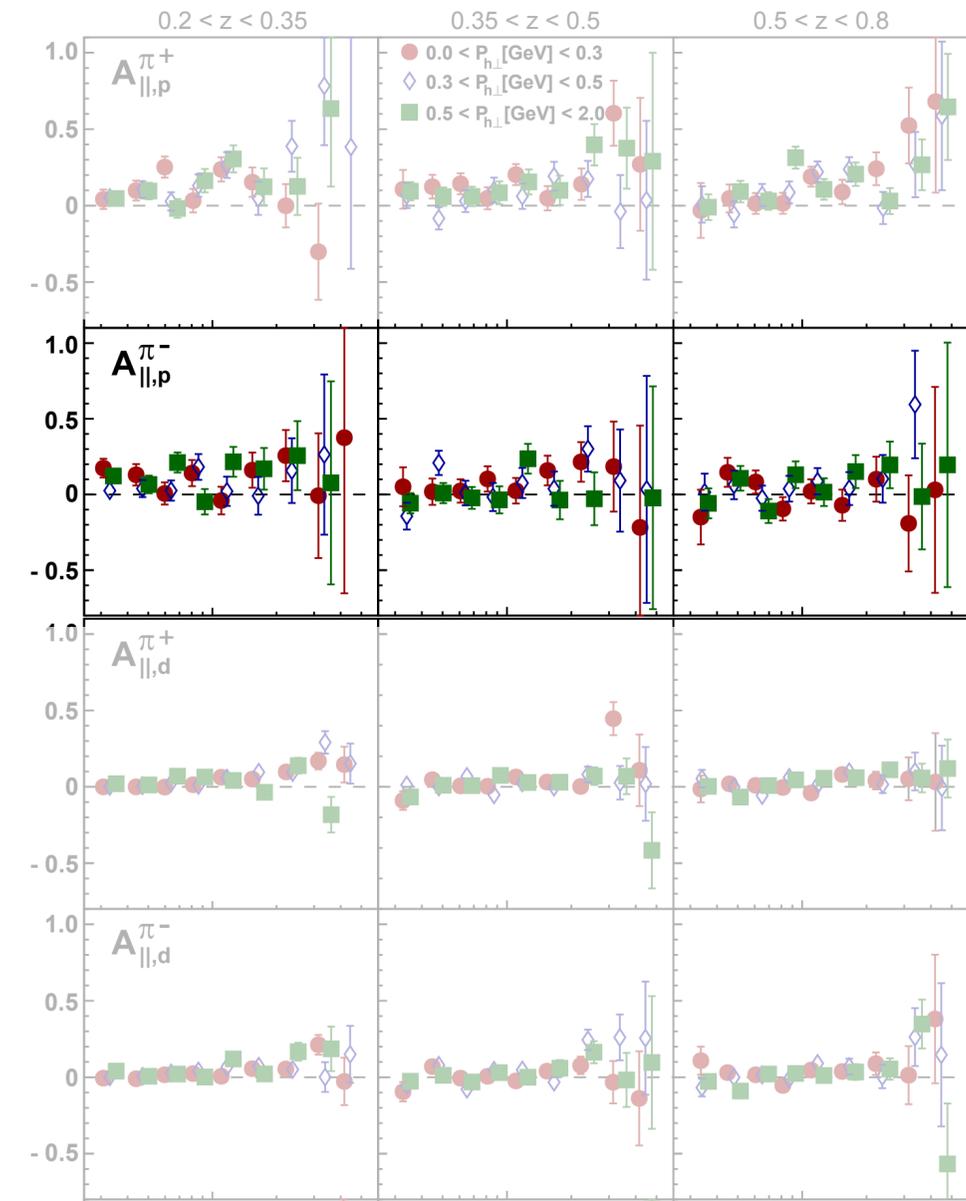
3-dimensional binning

- first-ever 3d binning provides transverse-momentum dependence



3-dimensional binning

- first-ever 3d binning provides transverse-momentum dependence
- but also extra flavor sensitivity, e.g.,
 - π^- asymmetries mainly coming from **low- z** region where **disfavored fragmentation** large and thus **sensitivity to the large positive up-quark polarization**



hadron-charge difference asymmetries

$$A_1^{h^+ - h^-}(x) \equiv \frac{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) - \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}{\left(\sigma_{1/2}^{h^+} - \sigma_{1/2}^{h^-}\right) + \left(\sigma_{3/2}^{h^+} - \sigma_{3/2}^{h^-}\right)}$$

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- at leading-order and leading-twist, assuming charge conjugation symmetry for fragmentation functions:

$$A_{1,d}^{h^+ - h^-} \stackrel{\text{LO LT}}{=} \frac{g_1^{u_v} + g_1^{d_v}}{f_1^{u_v} + f_1^{d_v}}$$

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- assuming also isospin symmetry in fragmentation:

$$A_{1,p}^{h^+ - h^-} \stackrel{\text{LO}_{\text{LT}}}{=} \frac{4g_1^{u_v} - g_1^{d_v}}{4f_1^{u_v} - f_1^{d_v}}$$

hadron-charge difference asymmetries

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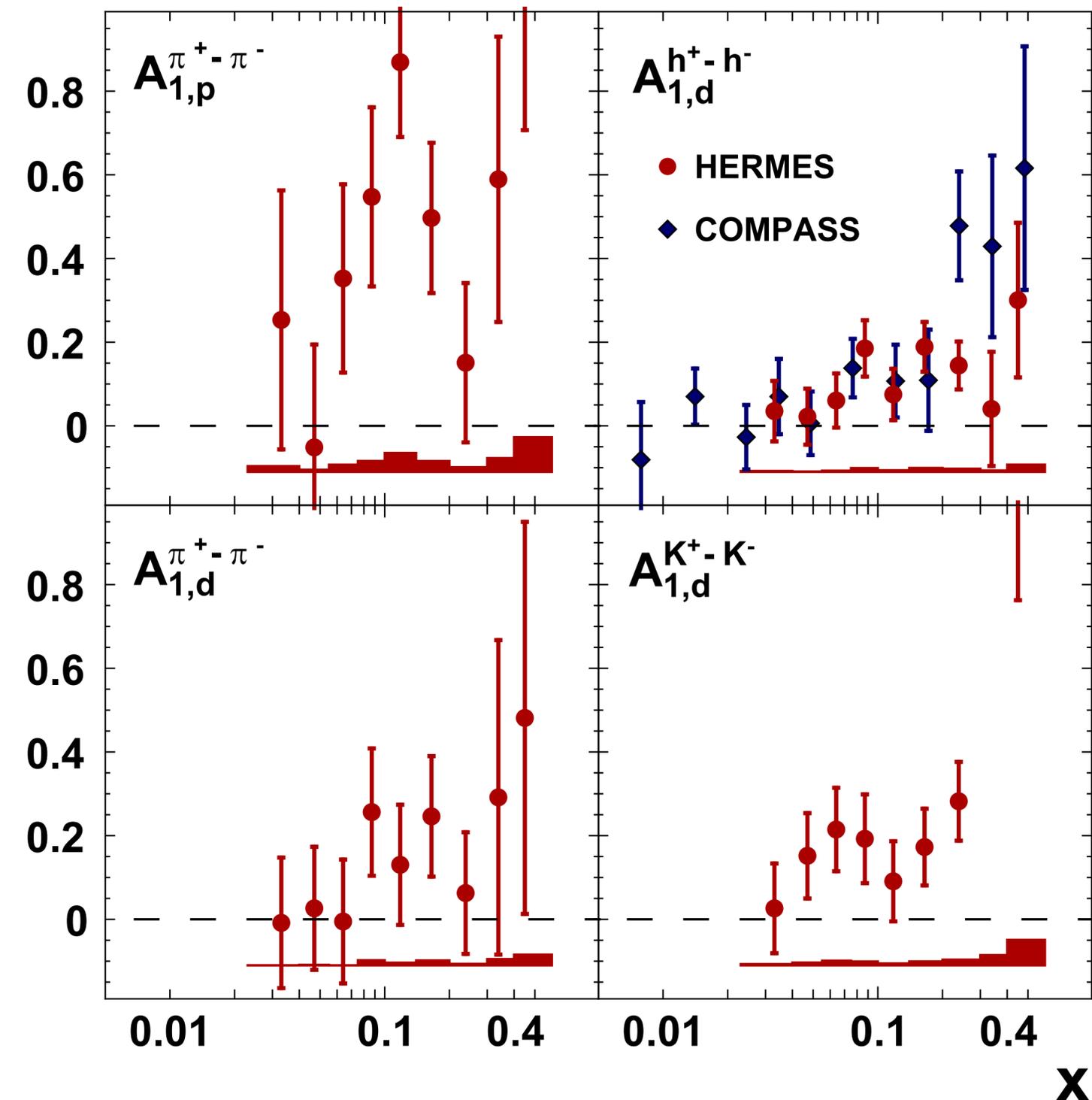
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- can be used to extract valence helicity distributions

hadron-charge difference asymmetries

[arXiv:1810.07054]

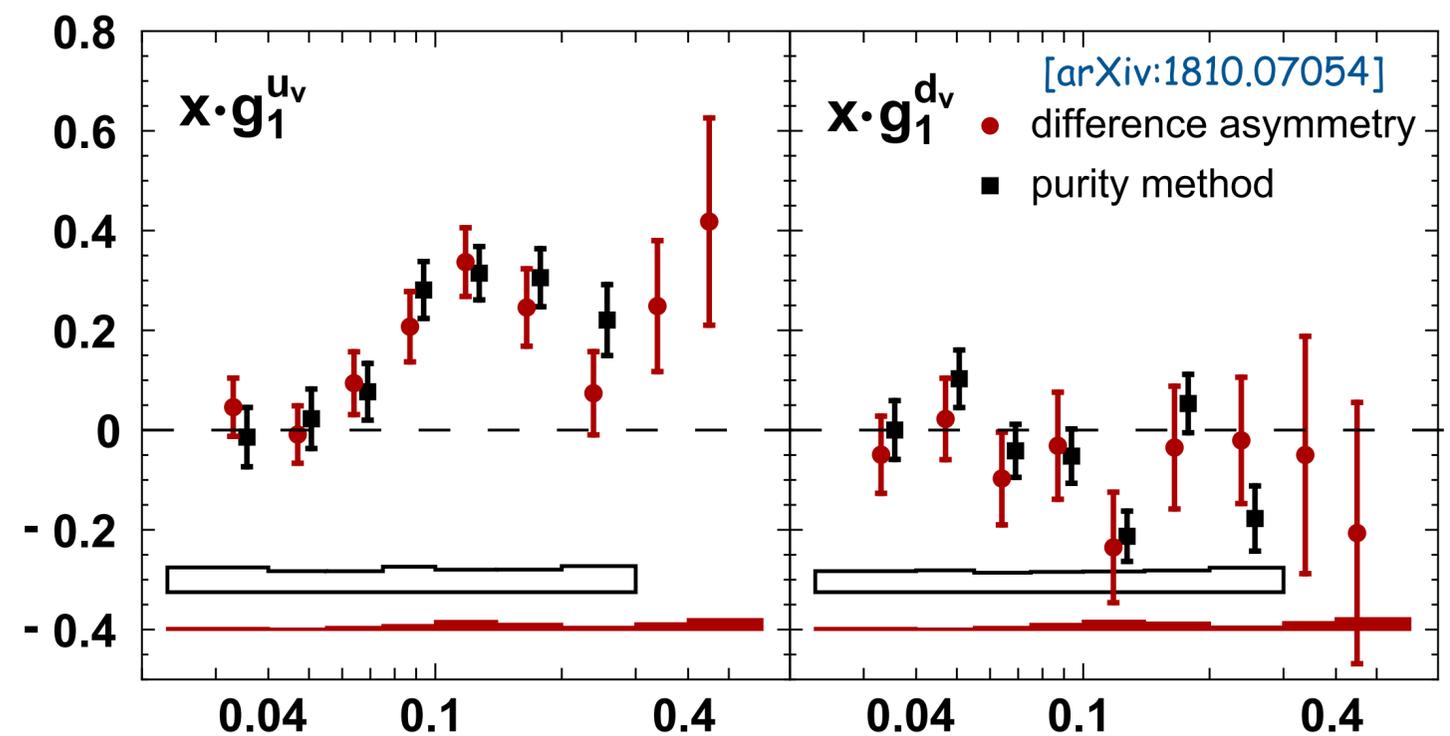
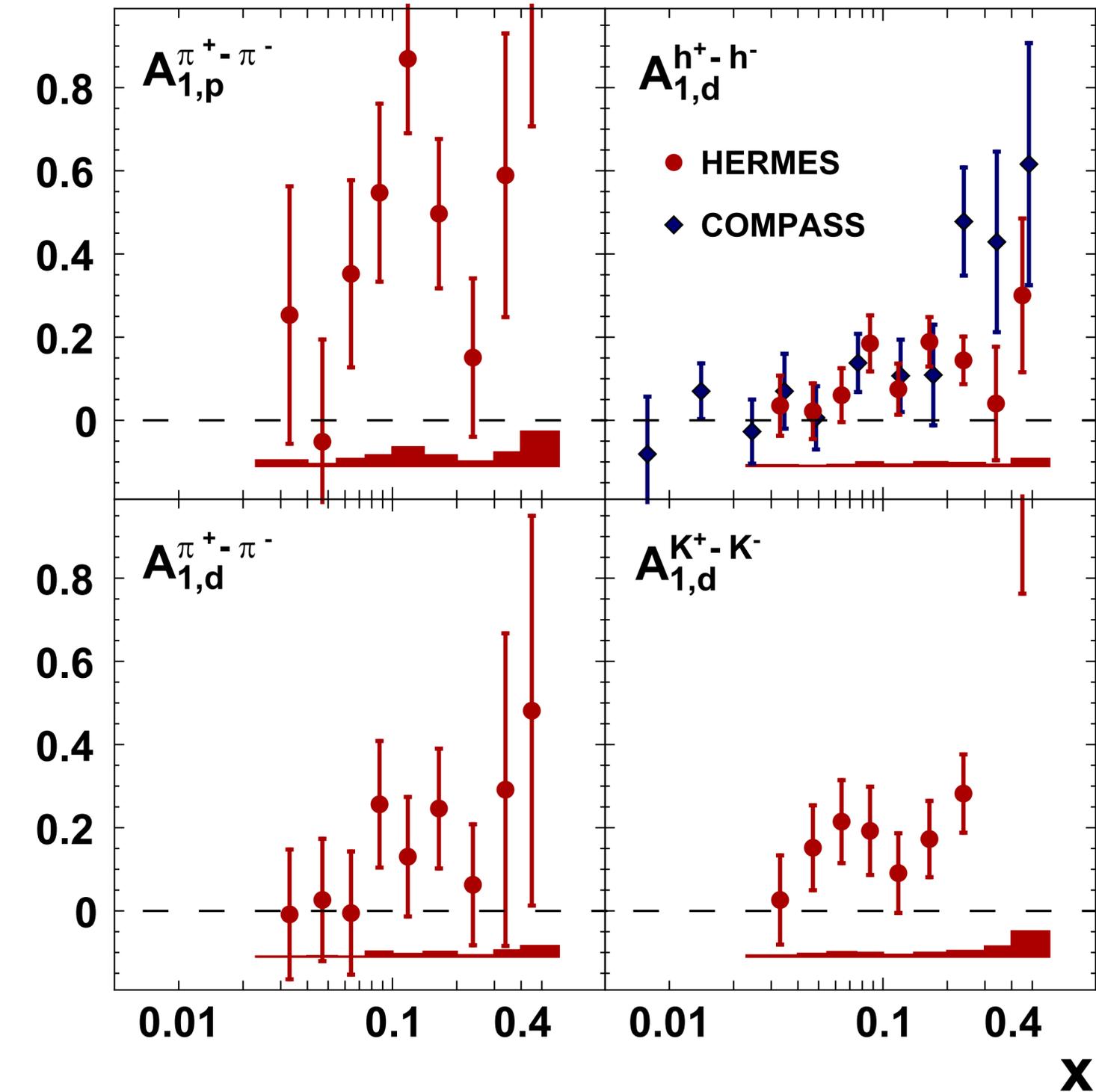


- no significant hadron-type dependence for deuterons
- deuteron results (unidentified hadrons) consistent with COMPASS

hadron-charge difference asymmetries

[arXiv:1810.07054]

- no significant hadron-type dependence for deuterons
- deuteron results (unidentified hadrons) consistent with *COMPASS*
- valence distributions consistent with JETSET-based extraction:



- with transverse target polarization:

$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi d\phi_s} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right)$$

$$\left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \text{terms not involving transv. polarization} \right.$$

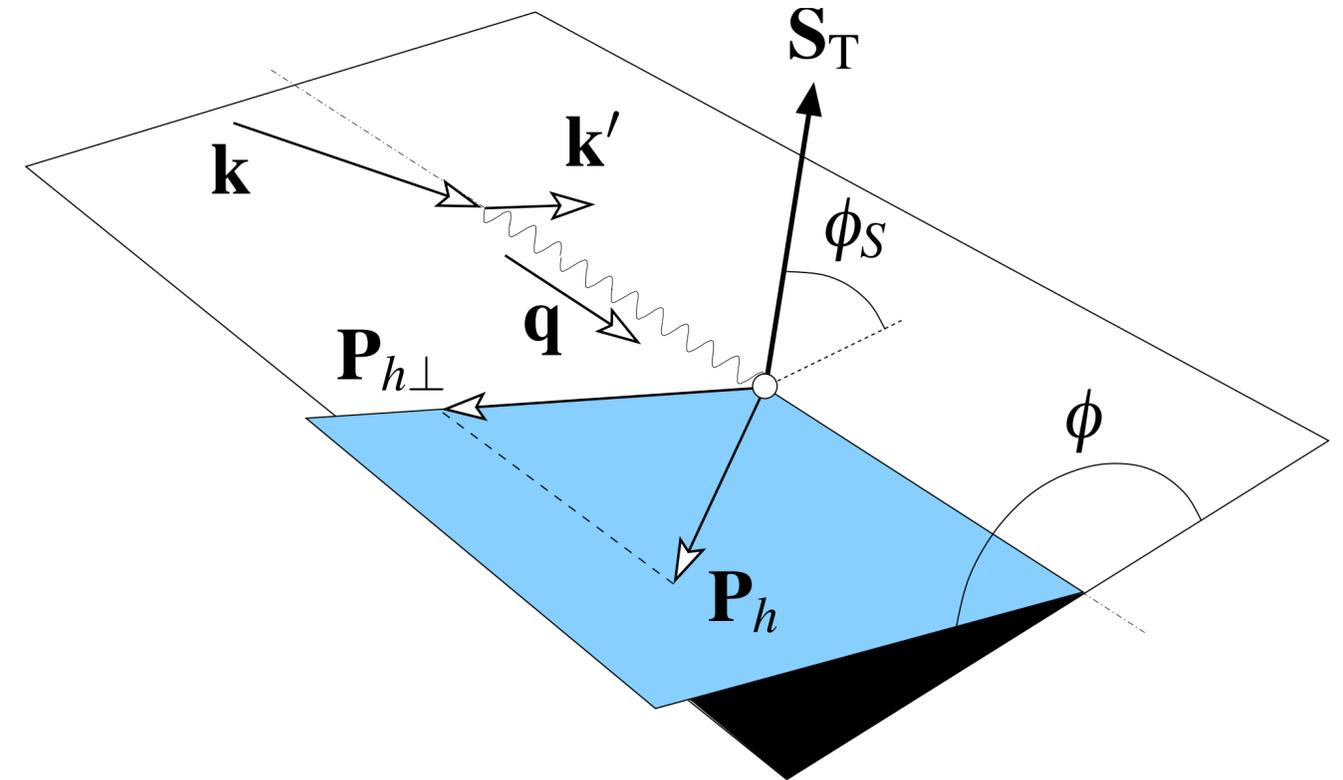
$$+ S_T \left[\left(F_{UT,T}^{h,\sin(\phi-\phi_s)} + \epsilon F_{UT,L}^{h,\sin(\phi-\phi_s)} \right) \sin(\phi - \phi_s) \right.$$

$$+ \epsilon F_{UT}^{h,\sin(\phi+\phi_s)} \sin(\phi + \phi_s) + \epsilon F_{UT}^{h,\sin(3\phi-\phi_s)} \sin(3\phi - \phi_s) \left. \right]$$

$$+ \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin\phi_s} \sin\phi_s + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin(2\phi-\phi_s)} \sin(2\phi - \phi_s) \left. \right]$$

$$+ S_T \lambda \left[\sqrt{1-\epsilon^2} F_{LT}^{h,\cos(\phi-\phi_s)} \cos(\phi - \phi_s) \right.$$

$$\left. \left. + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos\phi_s} \cos\phi_s + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos(2\phi-\phi_s)} \cos(2\phi - \phi_s) \right] \right\}$$



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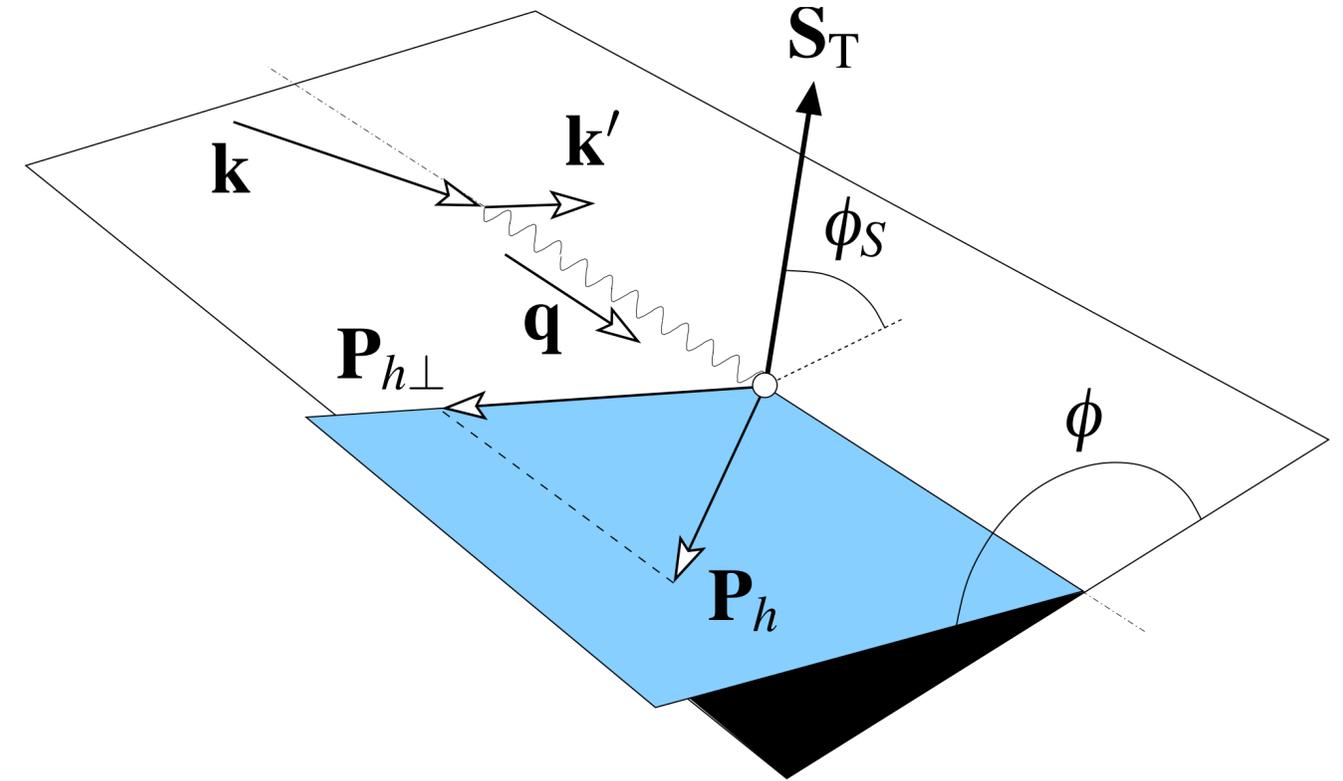
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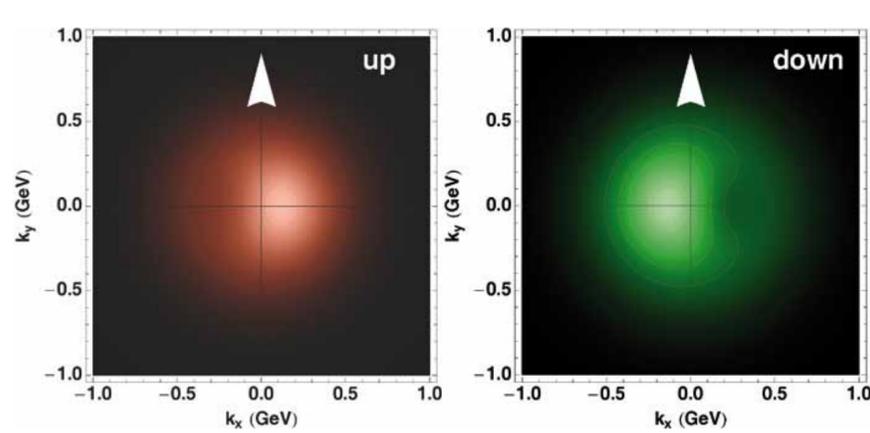
$$\left. + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin\phi_s} \sin\phi_s + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{h,\sin(2\phi-\phi_s)} \sin(2\phi - \phi_s) \right]$$

$$+ S_T \lambda \left[\sqrt{1-\epsilon^2} F_{LT}^{h,\cos(\phi-\phi_s)} \cos(\phi - \phi_s) \right.$$

$$\left. + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos\phi_s} \cos\phi_s + \sqrt{2\epsilon(1-\epsilon)} F_{LT}^{h,\cos(2\phi-\phi_s)} \cos(2\phi - \phi_s) \right] \left. \right\}$$



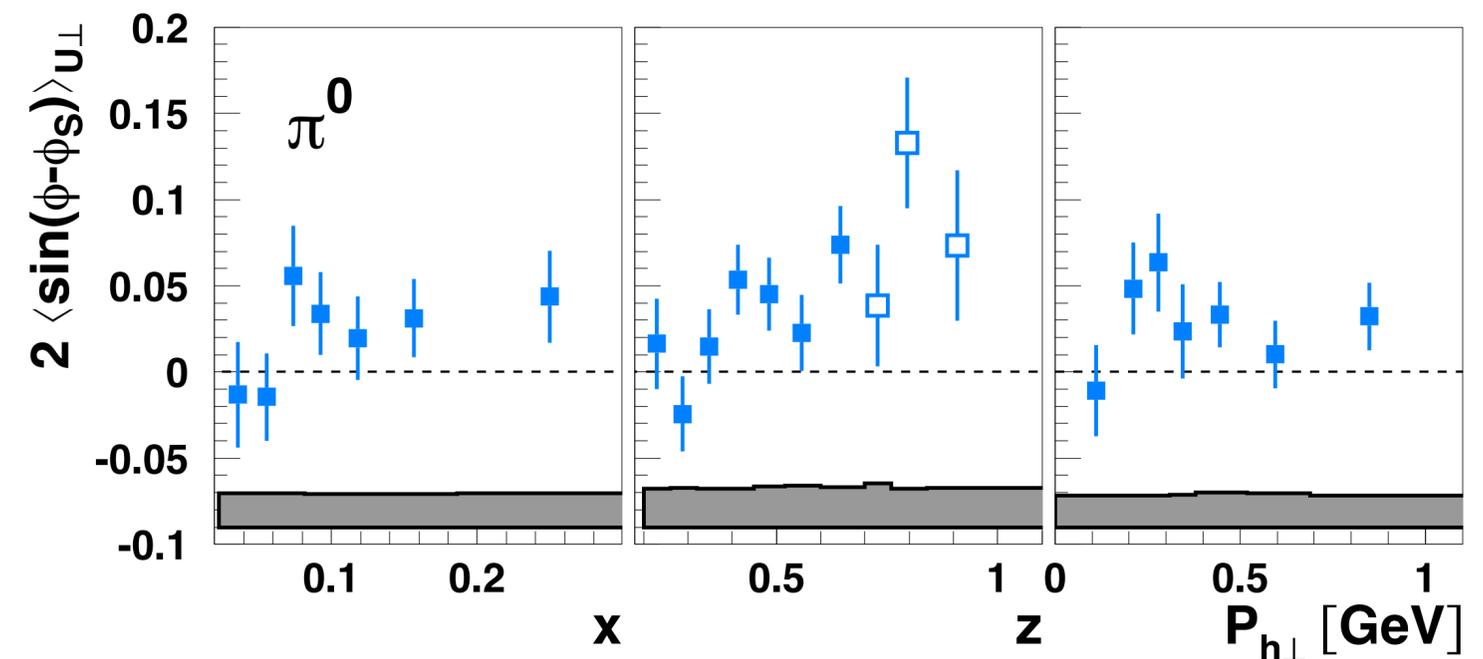
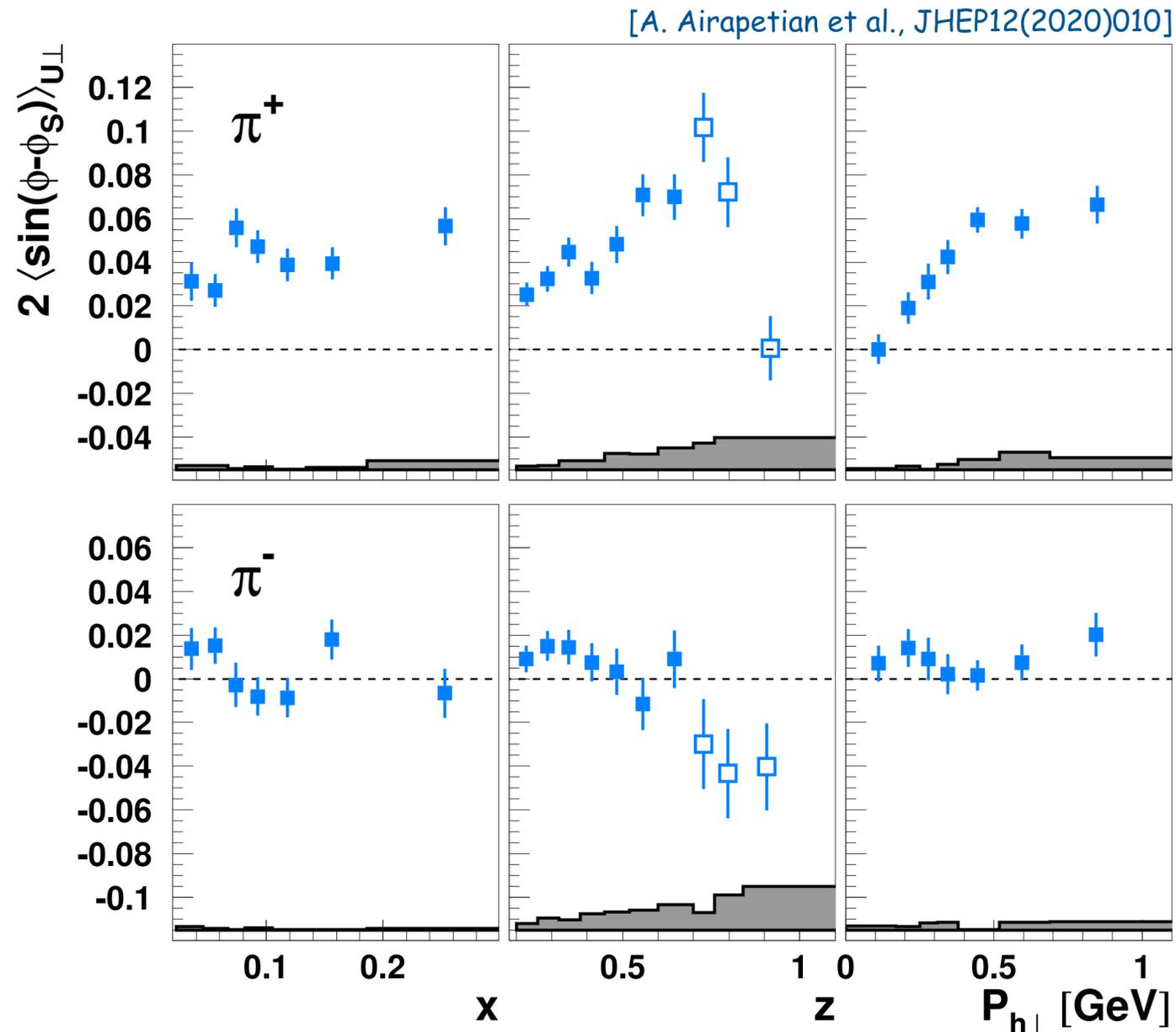
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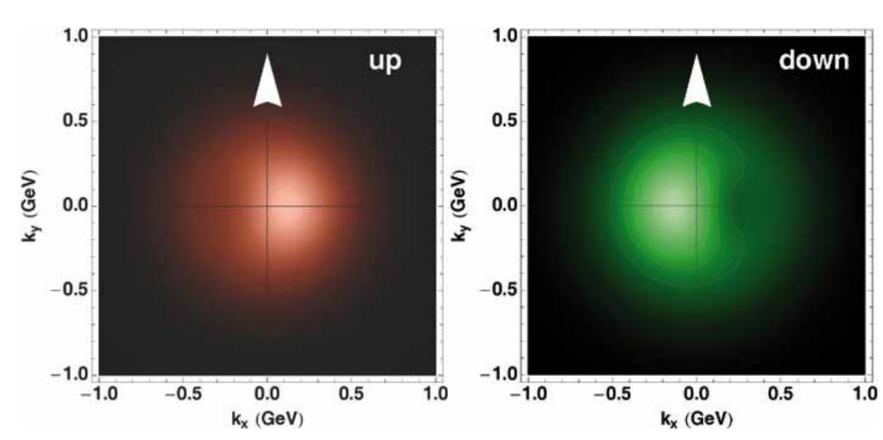
[A. Bacchetta et al.]

Sivers amplitudes for pions

- Sivers TMD probes correlation between nucleon spin and parton transverse momentum
- previous HERMES results focused on $z < 0.7$



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T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

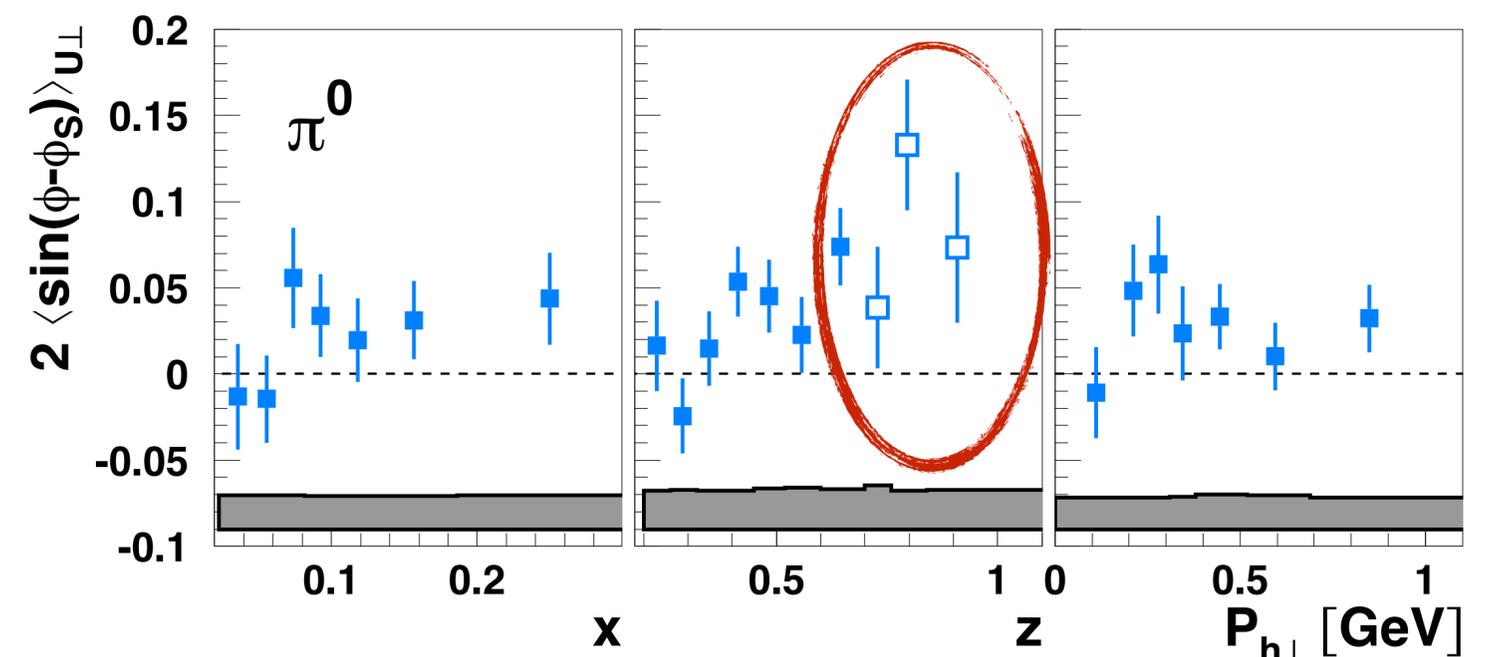
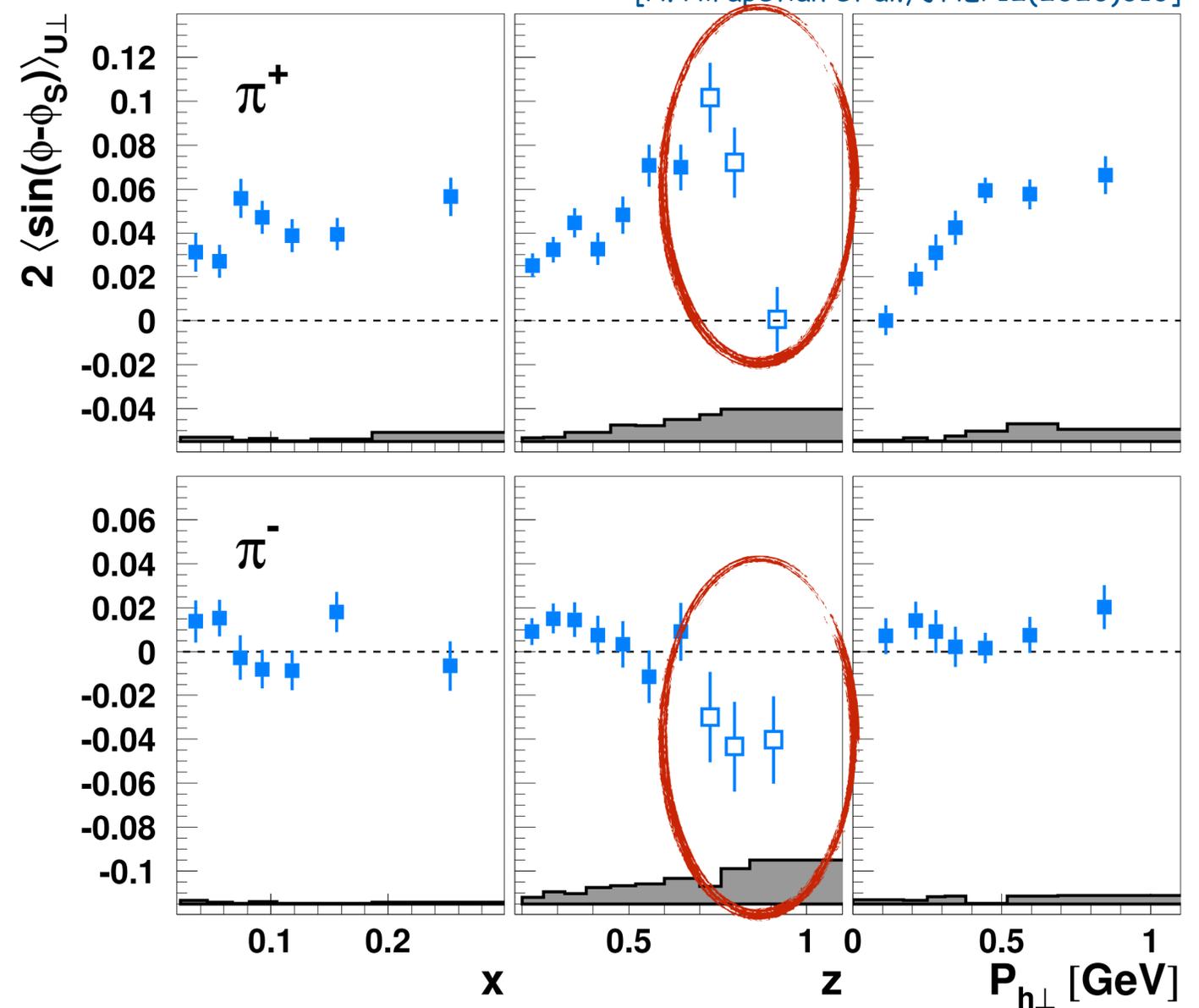


[A. Bacchetta et al.]

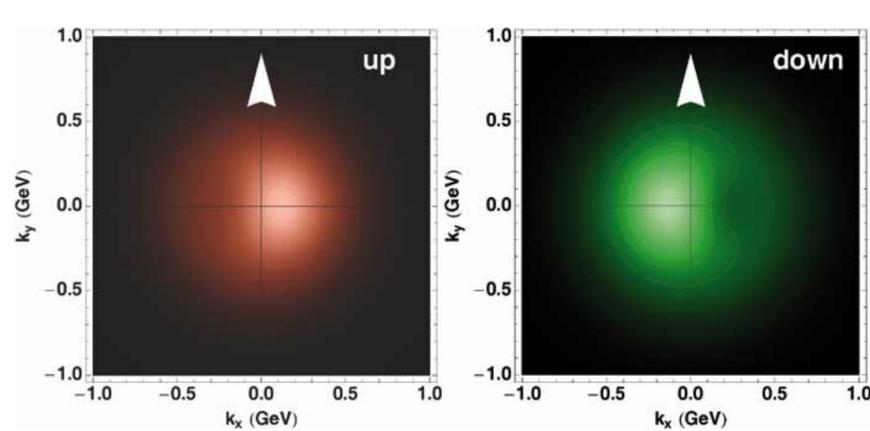
Sivers amplitudes for pions

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- previous HERMES results focused on $z < 0.7$
- high- z data probes transition region towards exclusive meson production but also increased sensitivity to struck quark's flavor

[A. Airapetian et al., JHEP12(2020)010]



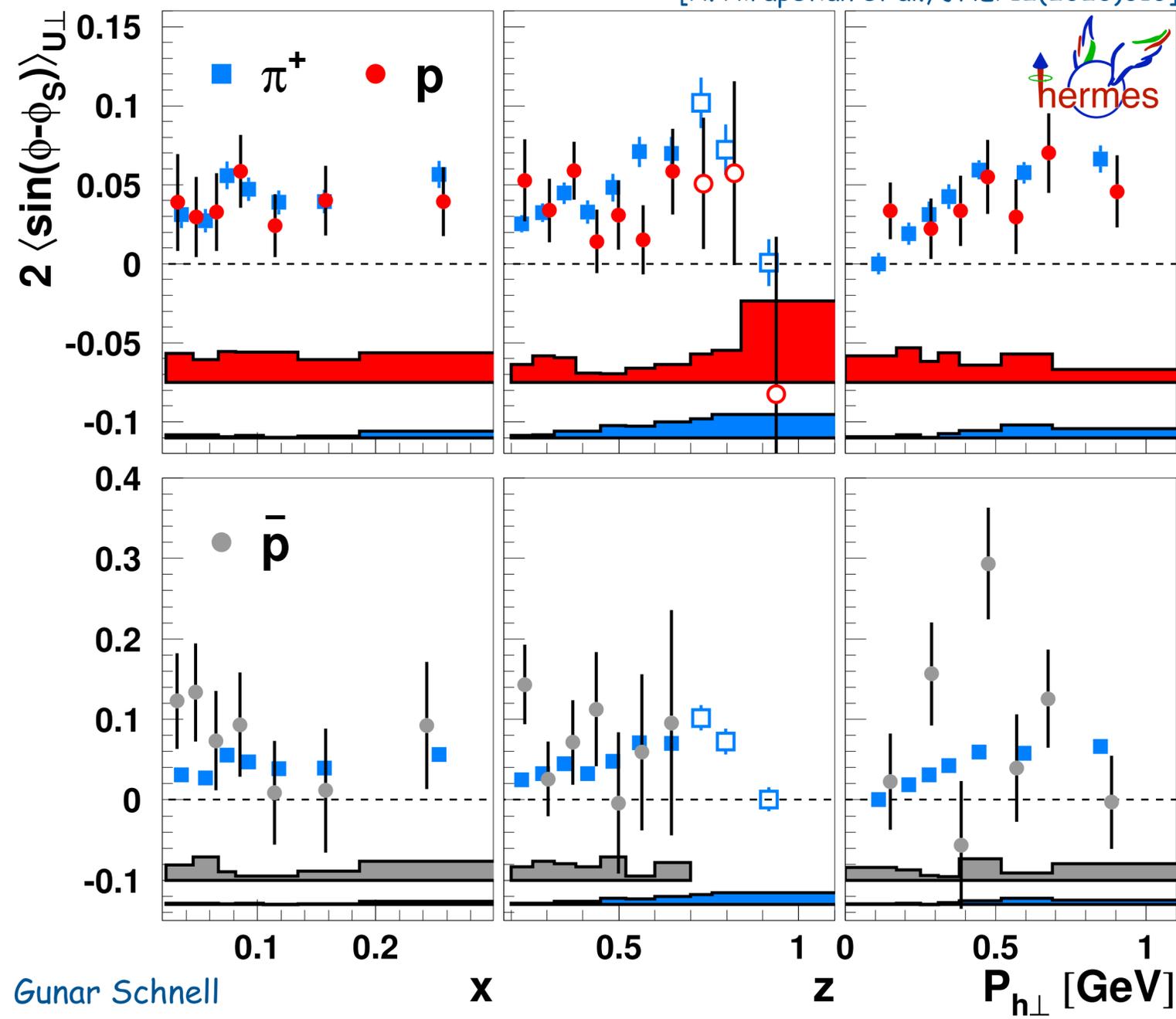
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Sivers amplitudes pions vs. (anti)protons

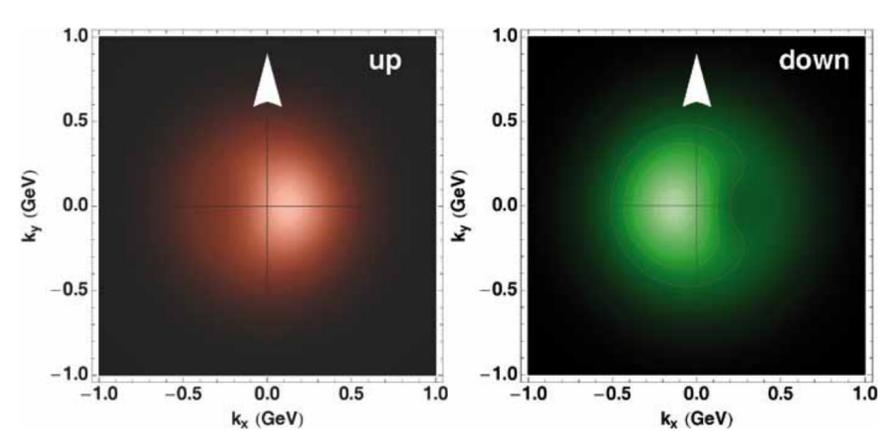
[A. Airapetian et al., JHEP12(2020)010]



● first-ever results for protons and anti-protons

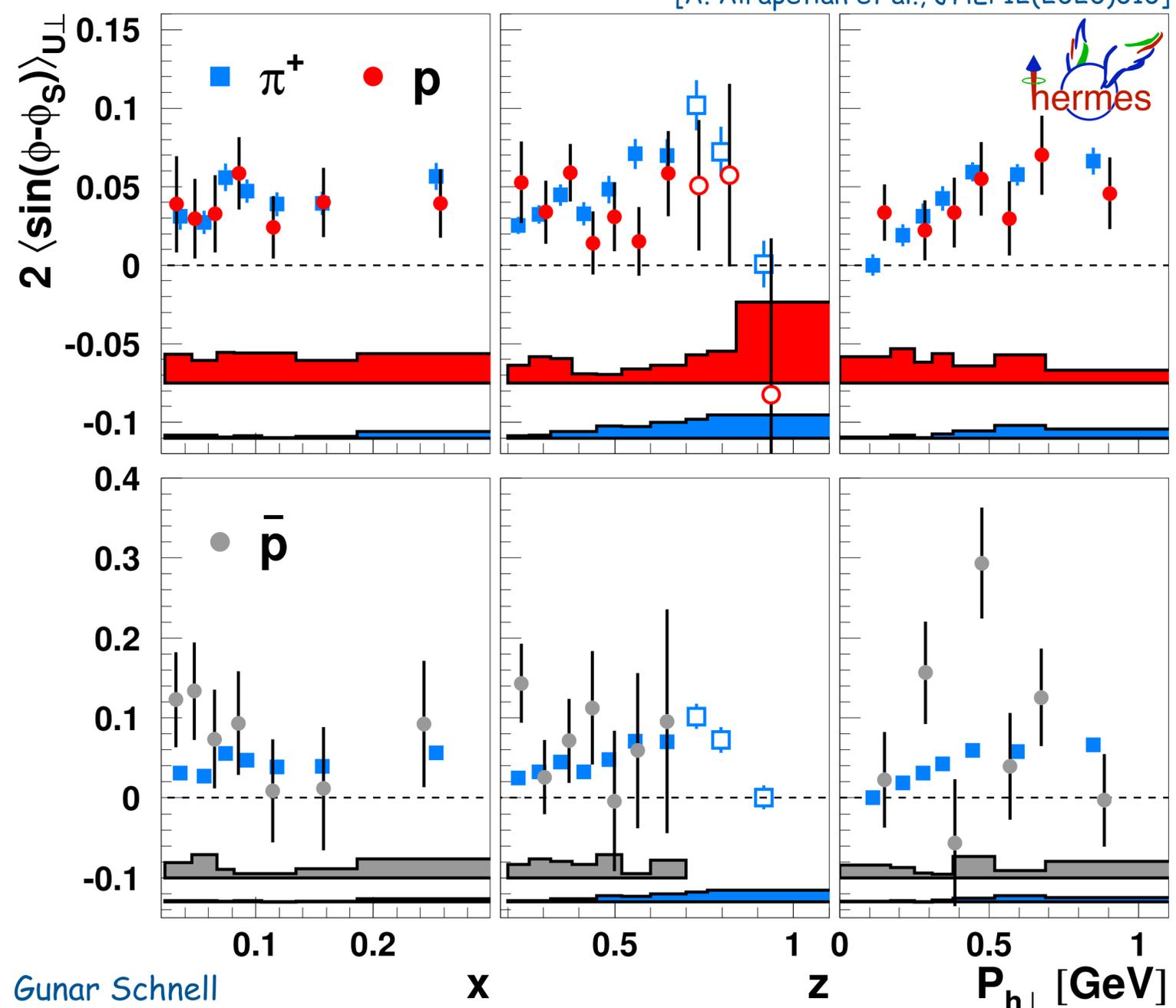
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[A. Airapetian et al., JHEP12(2020)010]



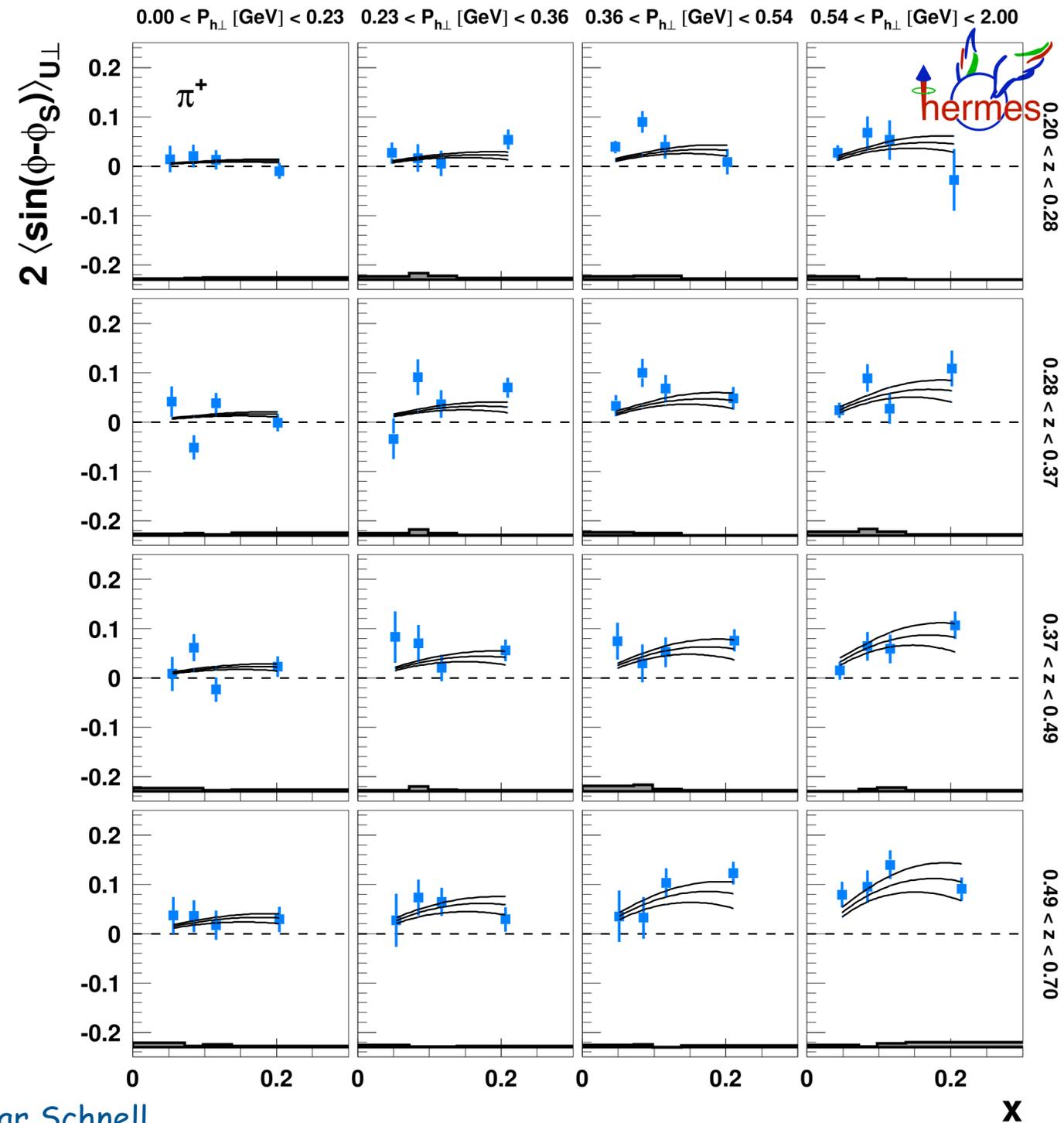
- first-ever results for protons and anti-protons
- similar-magnitude asymmetries for (anti)protons and pions
- ➡ consequence of u-quark dominance in both cases?

Sivers amplitudes

multi-dimensional analysis

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

[A. Airapetian et al., JHEP12(2020)010]



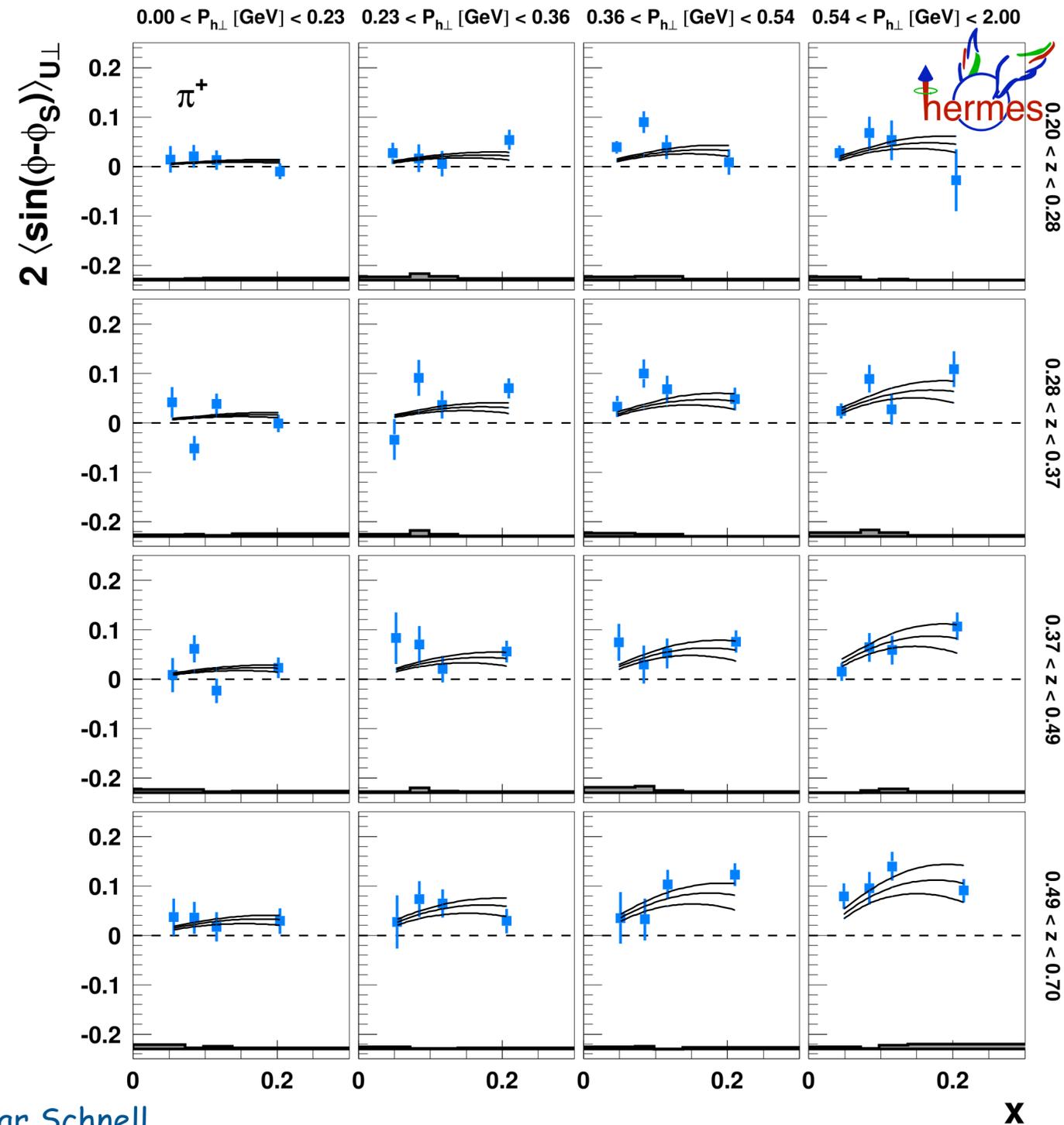
- 3d analysis: 4x4x4 bins in $(x, z, P_{h\perp})$
- reduced systematics
- disentangle correlations
- isolate phase-space region with large signal strength

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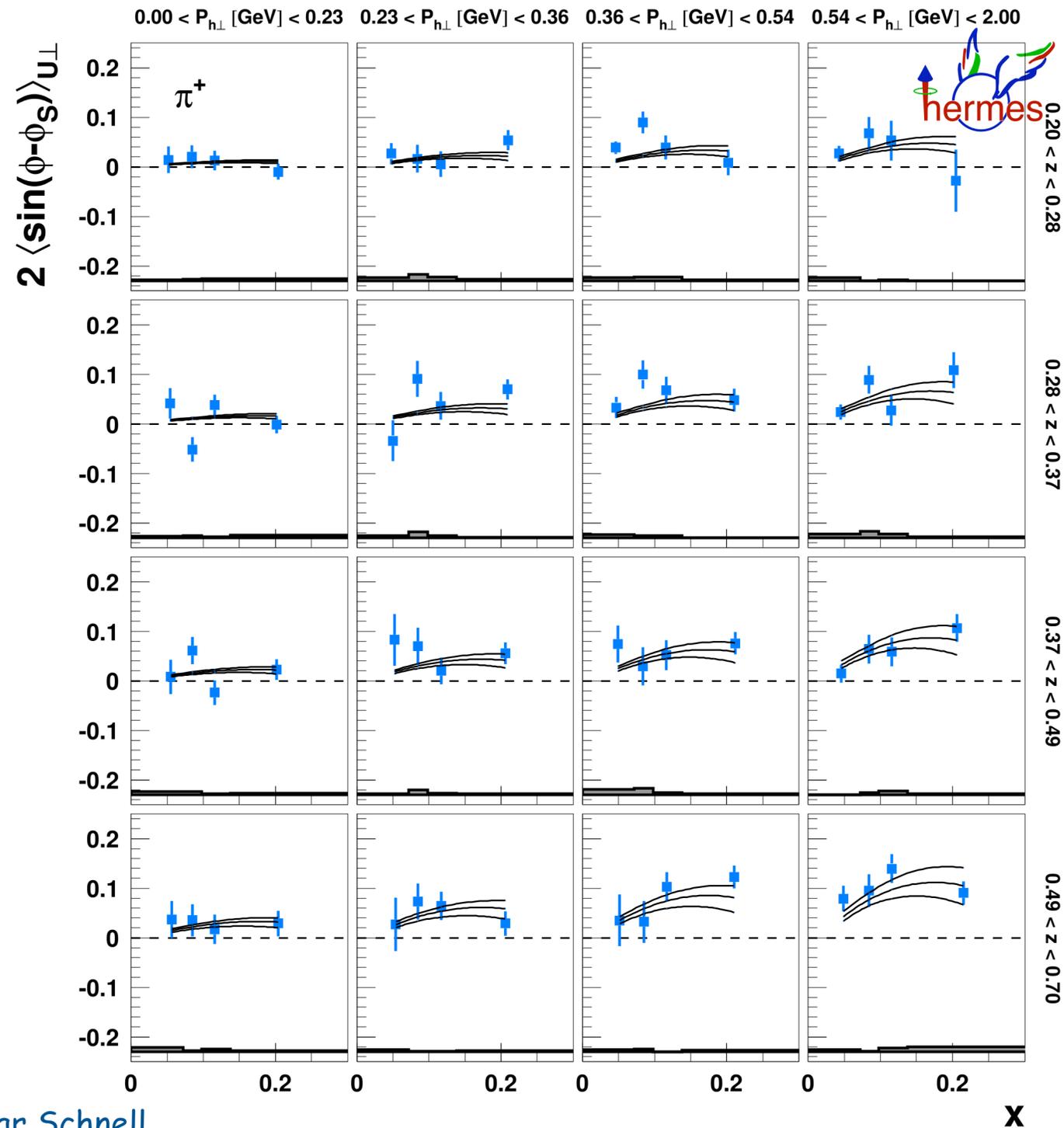
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[A. Airapetian et al., JHEP12(2020)010]



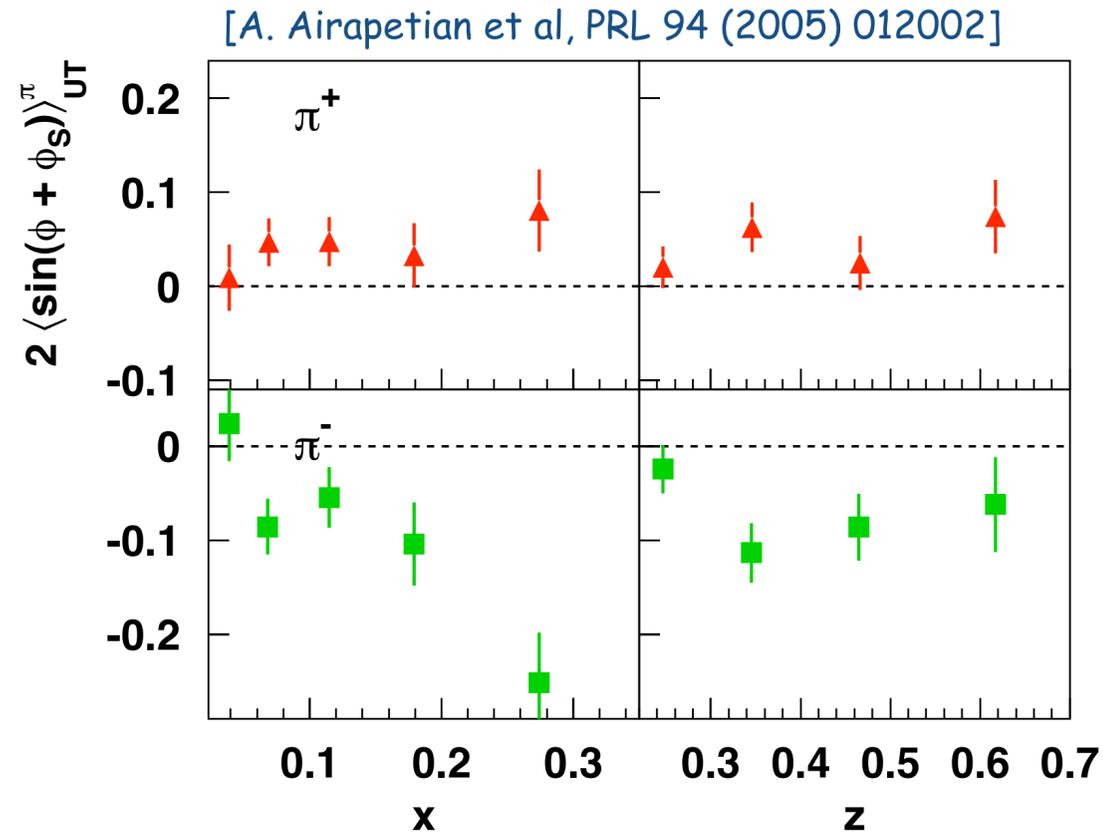
- 3d analysis: 4x4x4 bins in $(x, z, P_{h\perp})$
- reduced systematics
- disentangle correlations
- isolate phase-space region with large signal strength
- allows more detailed comparison with calculations
- accompanied by kinematic distribution to guide phenomenology*)

*) see, e.g., backup slides or supplemental material of JHEP12(2020)0210

Transversity

(Collins fragmentation)

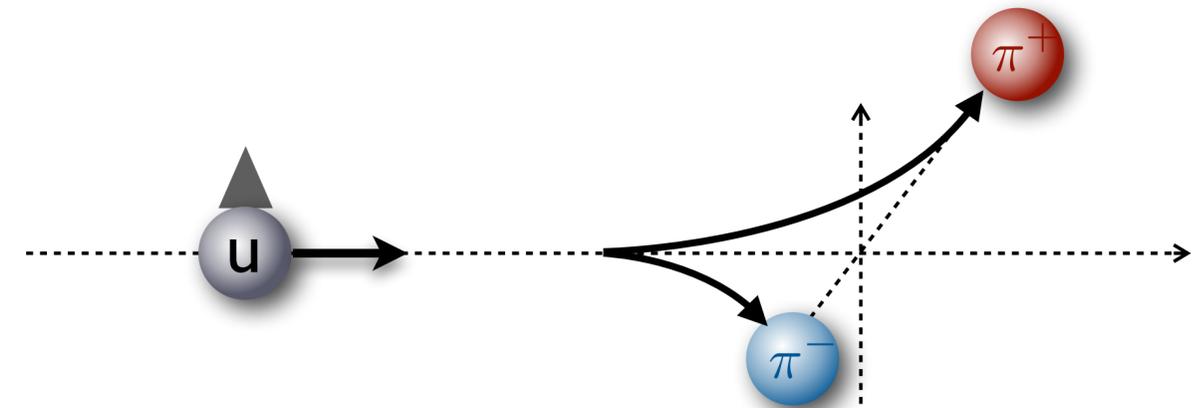
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2005: First evidence from HERMES
SIDIS on proton

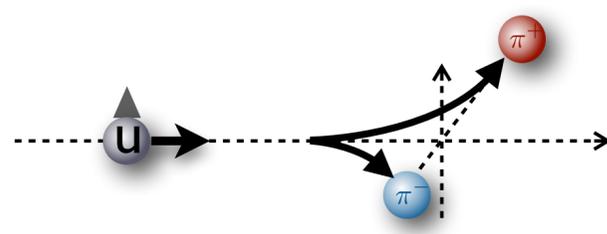
Non-zero transversity
Non-zero Collins function

- significant in size and opposite in sign for charged pions
- disfavored Collins FF large and opposite in sign to favored one

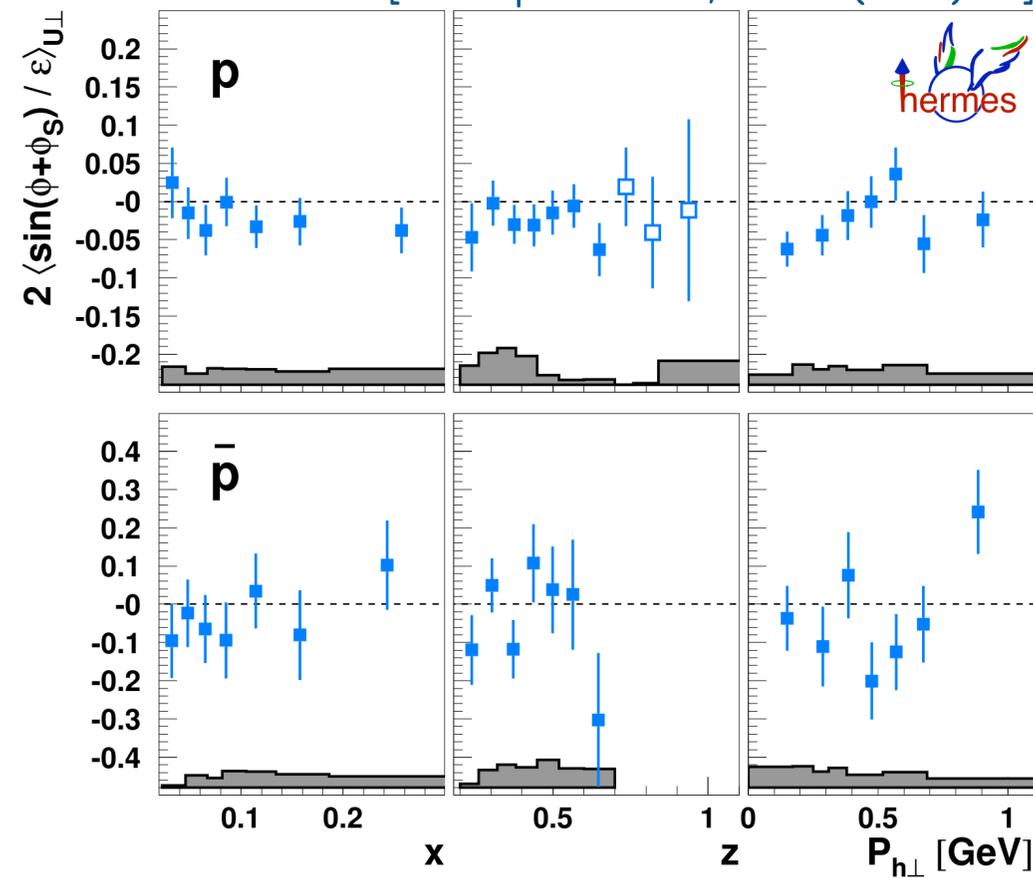


Collins amplitudes

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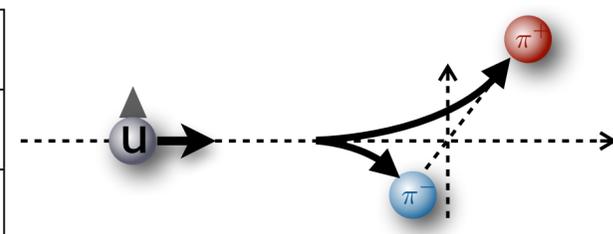
[A. Airapetian et al., JHEP12(2020)010]



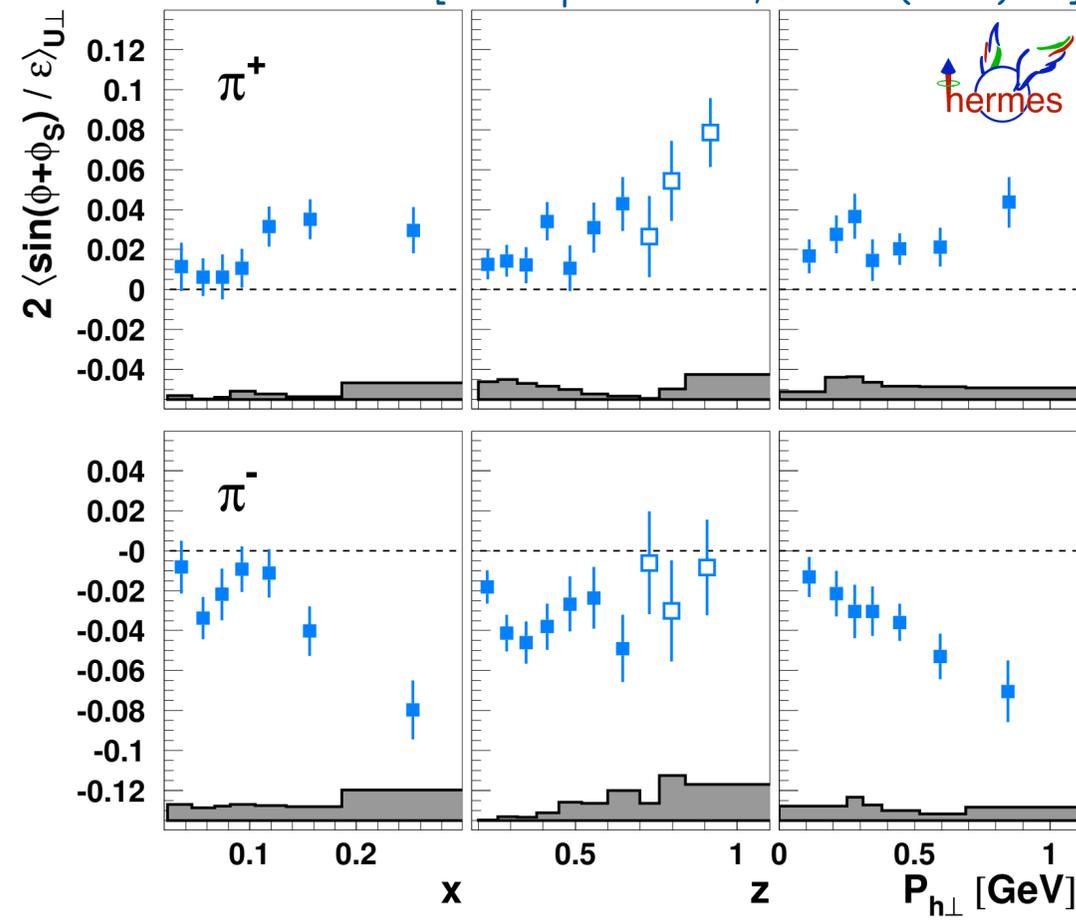
- first-ever results for (anti-)protons consistent with zero
 ➔ vanishing Collins effect for (spin-1/2) baryons?

Collins amplitudes

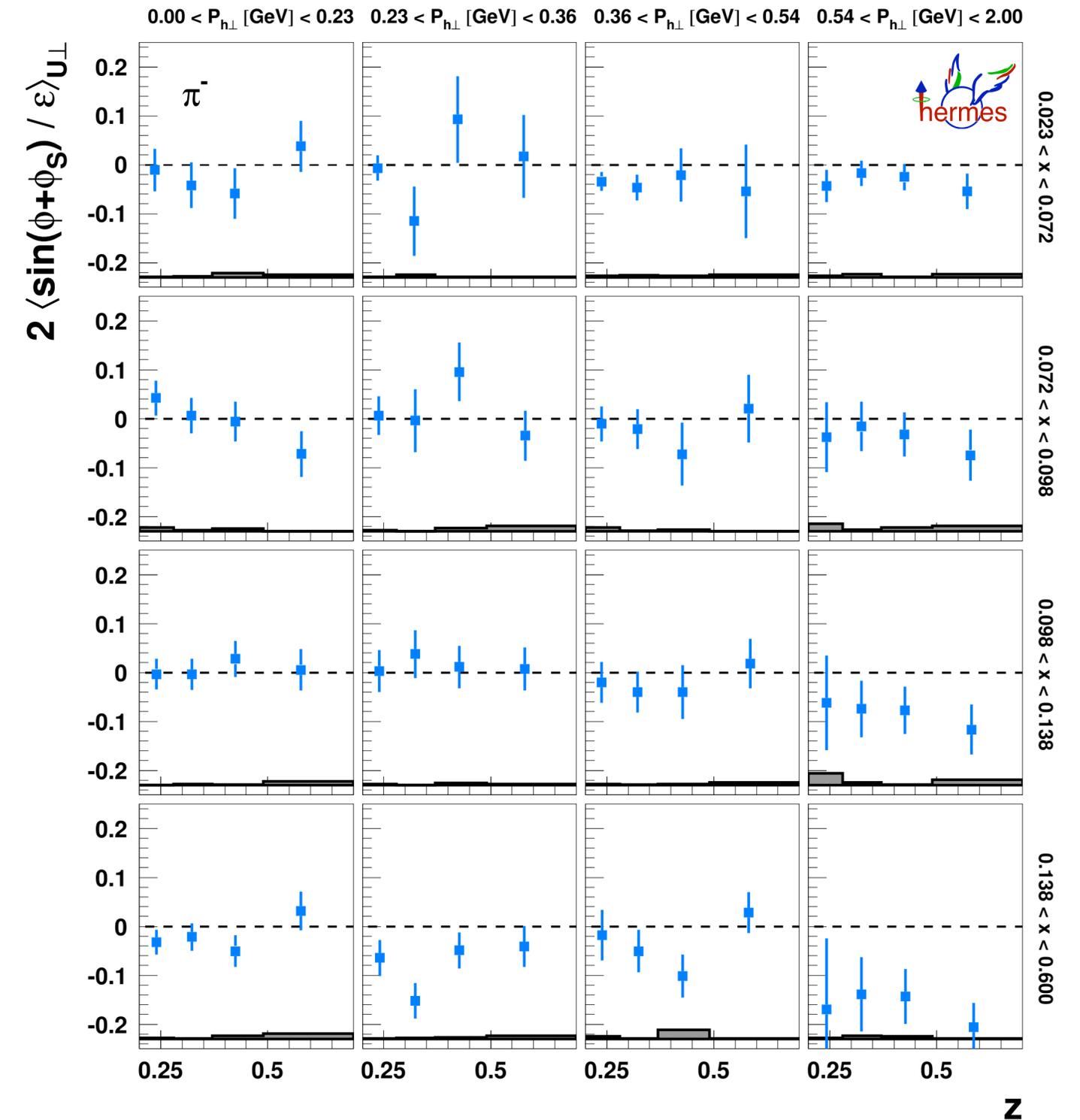
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[A. Airapetian et al., JHEP12(2020)010]

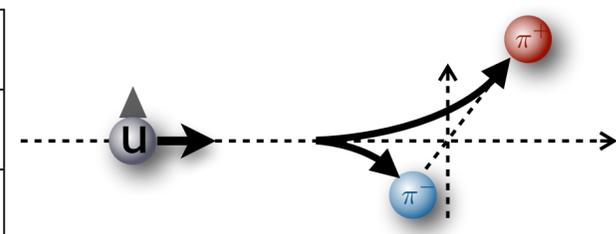


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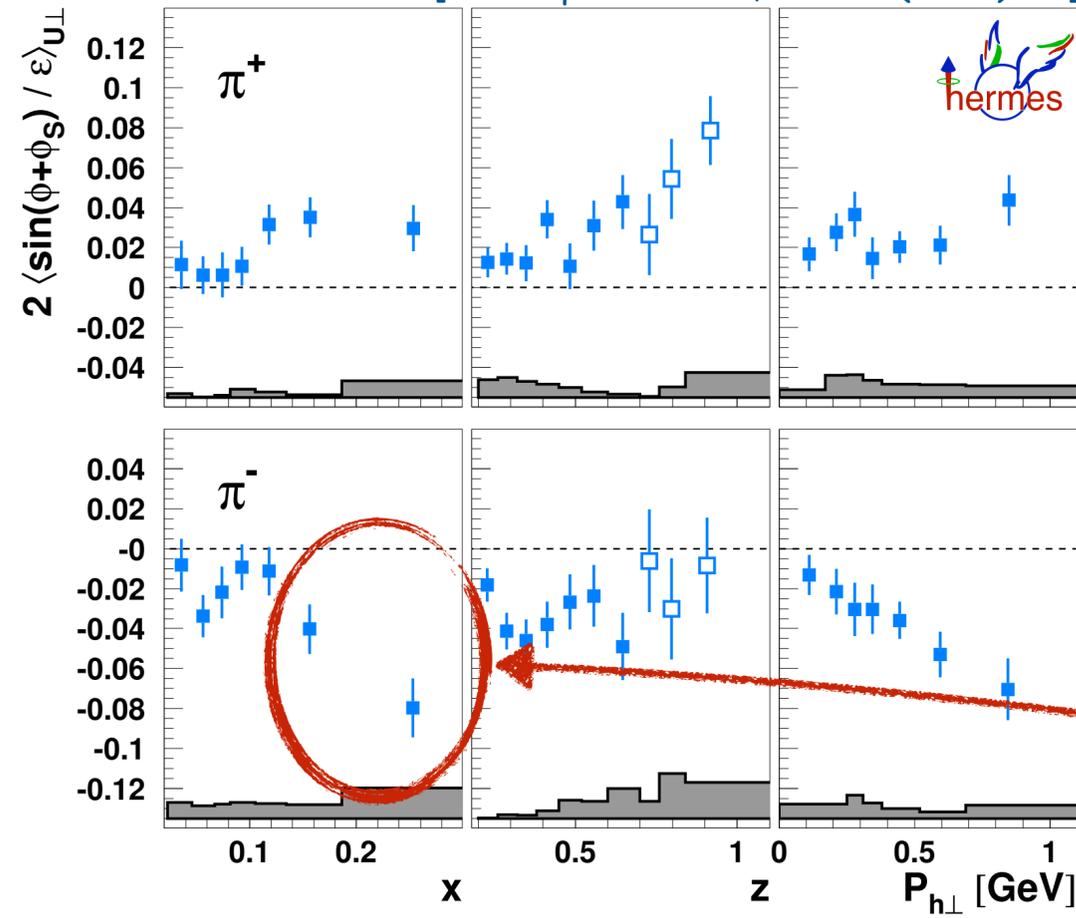


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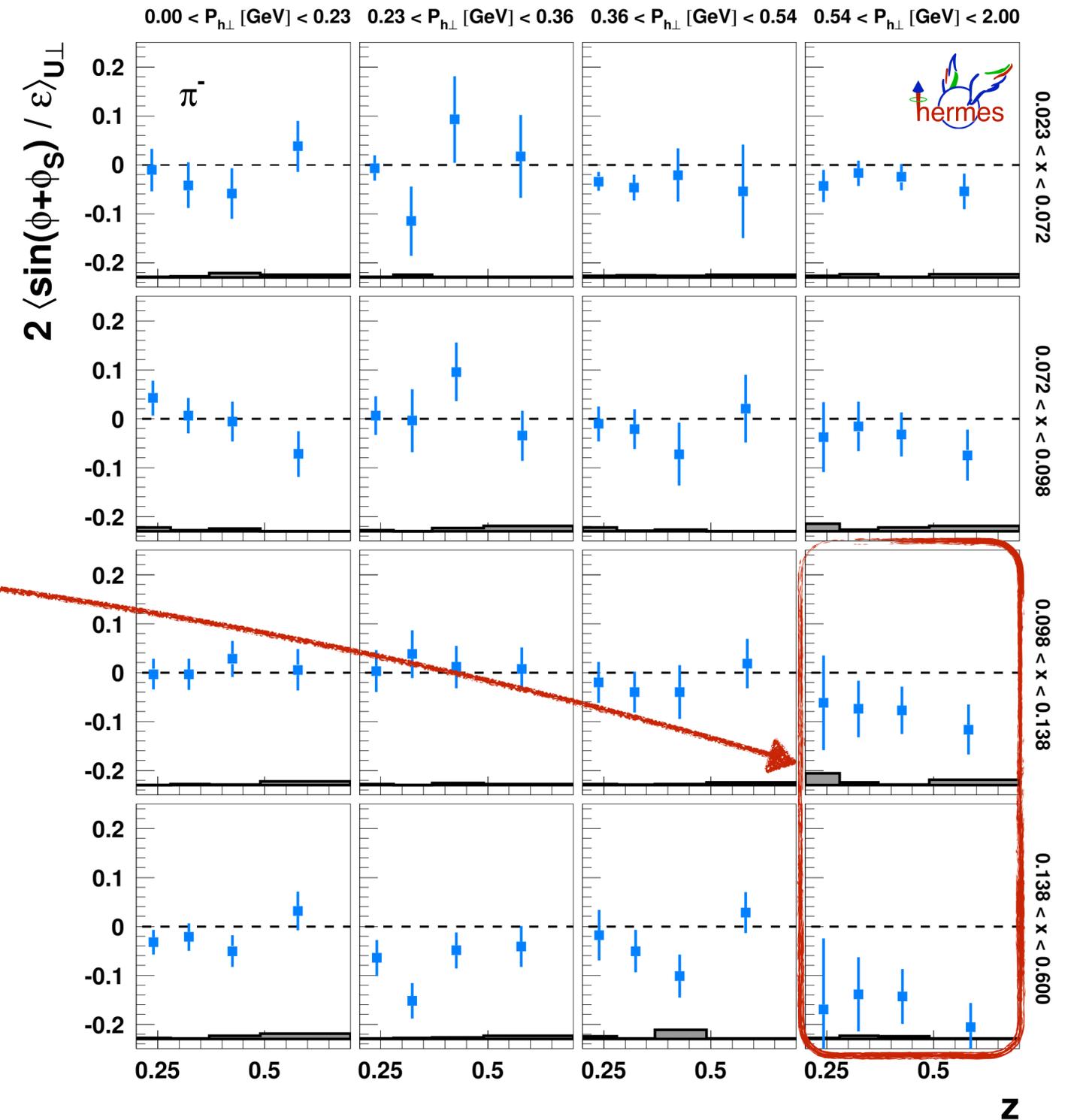
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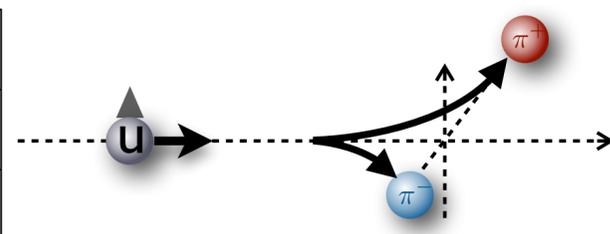


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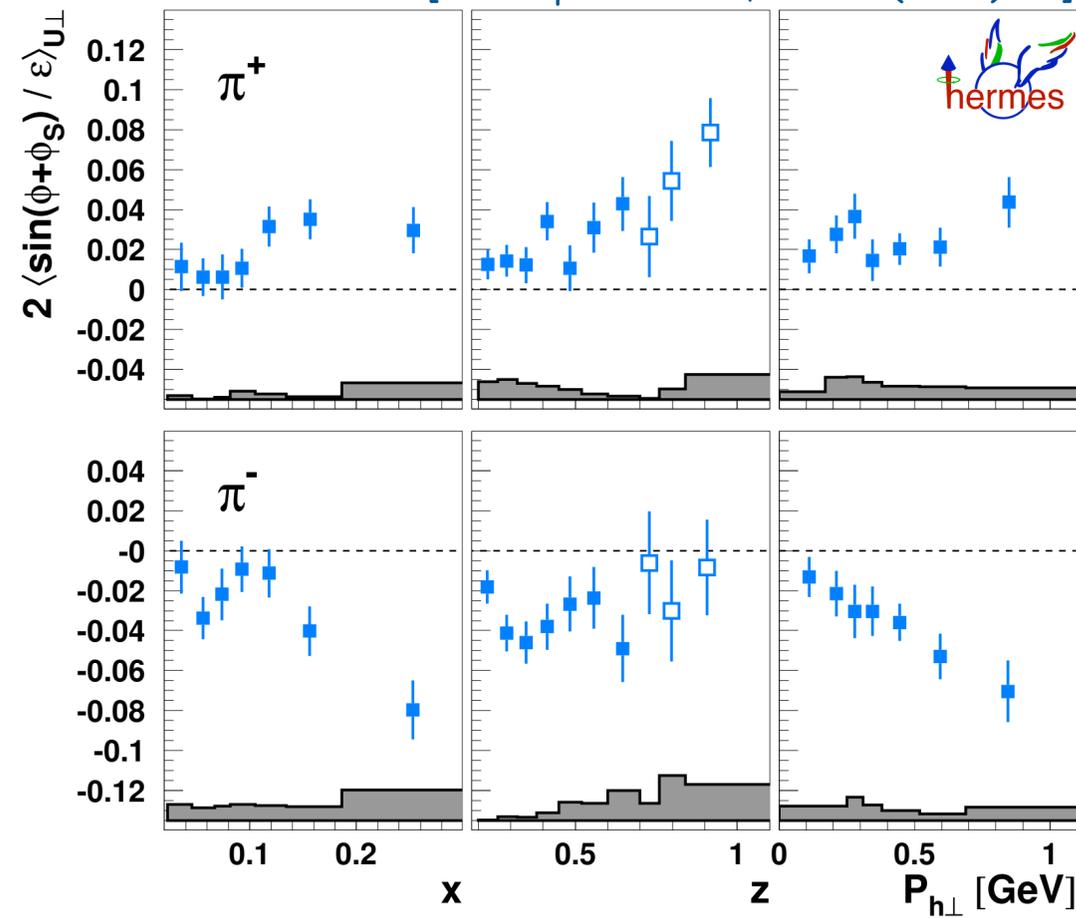


Collins amplitudes

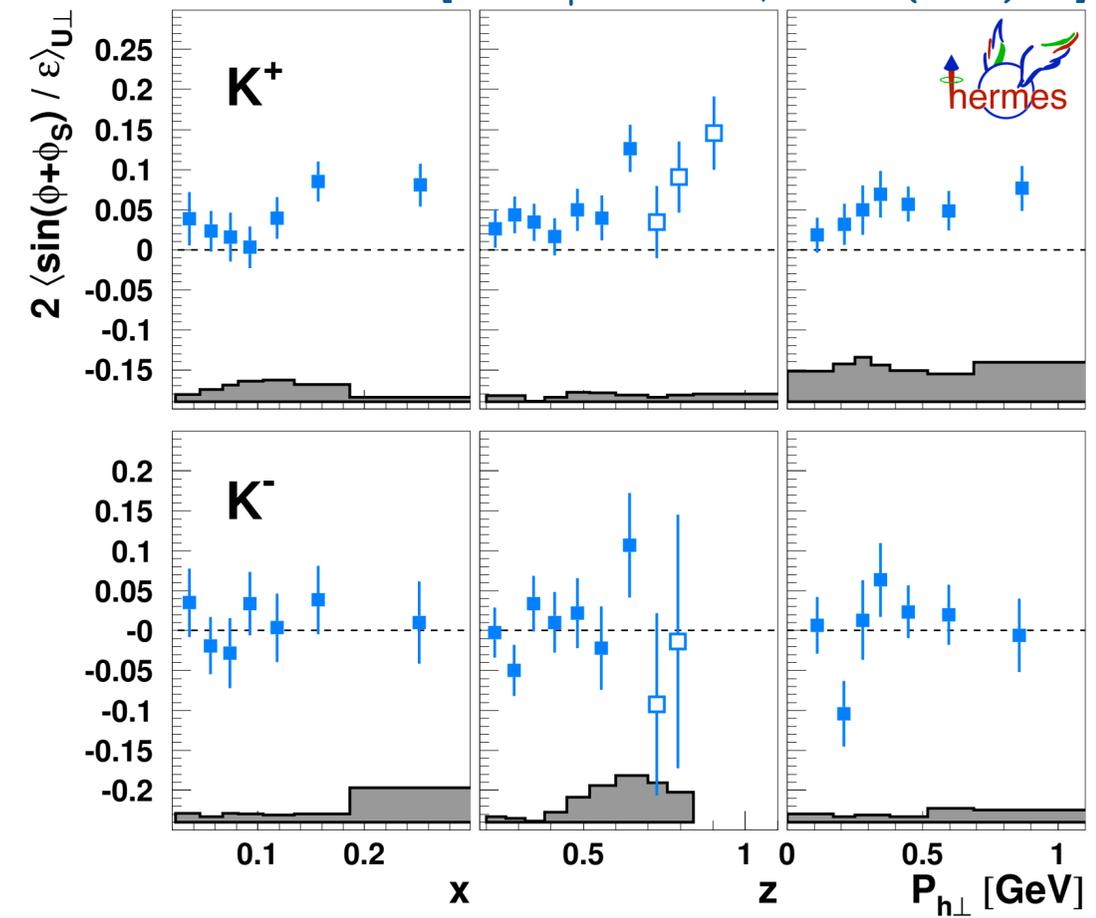
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[A. Airapetian et al., JHEP12(2020)010]

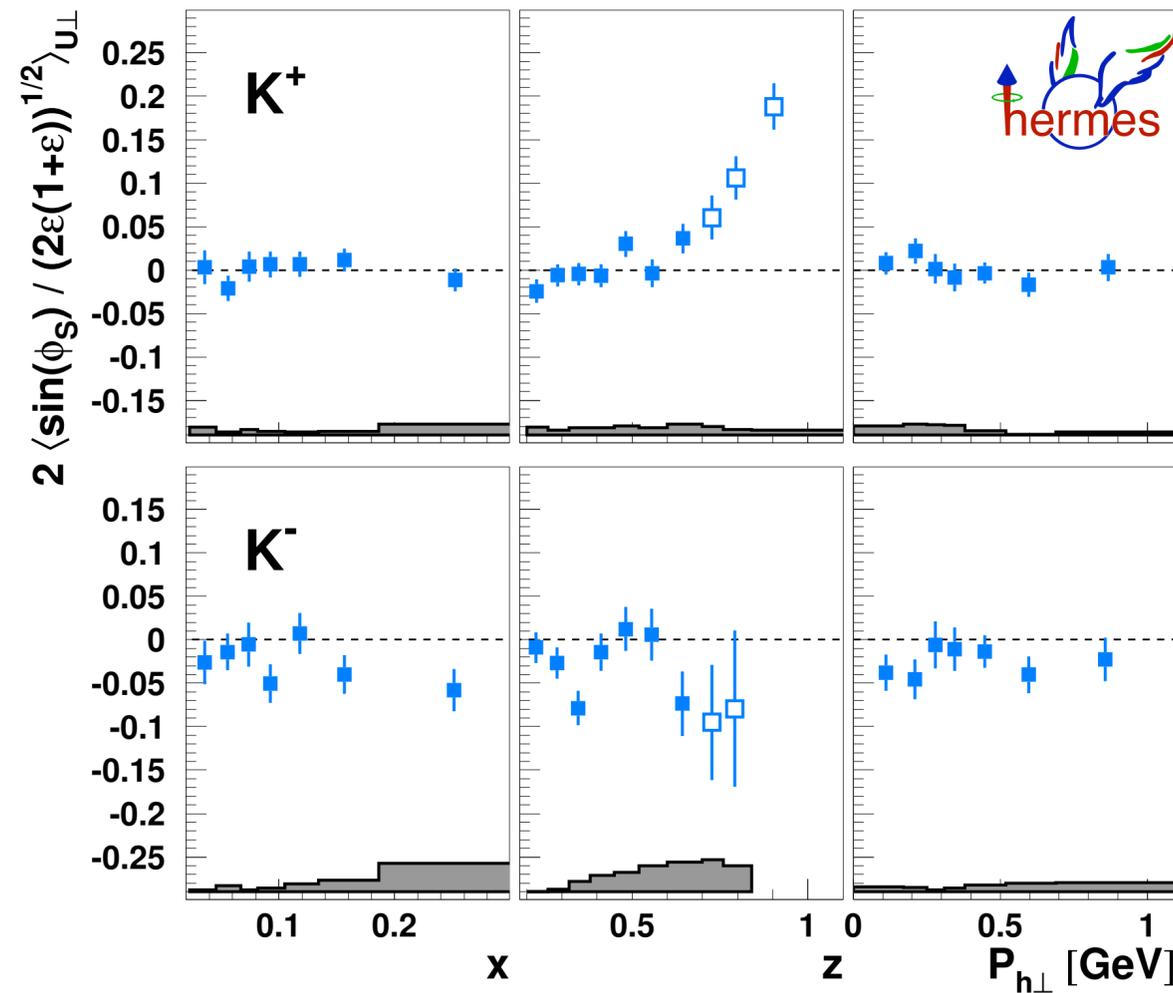
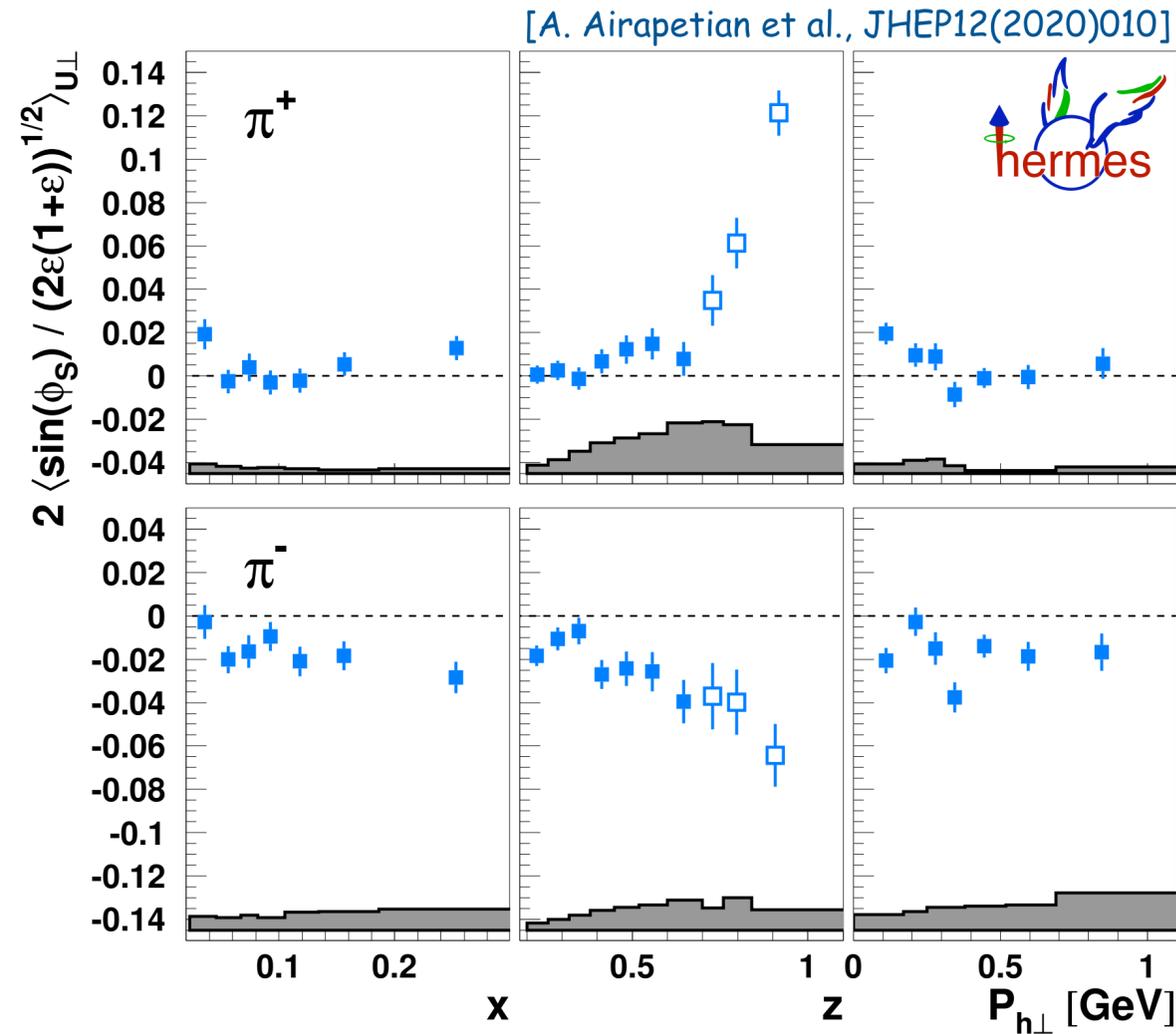


[A. Airapetian et al., JHEP12(2020)010]



- results for (anti-)protons consistent with zero
 ➔ vanishing Collins effect for (spin-1/2) baryons?
- analysis now performed in 3d
- high- z region probes transition region to exclusive domain (with increasing amplitudes for positive pions and kaons)

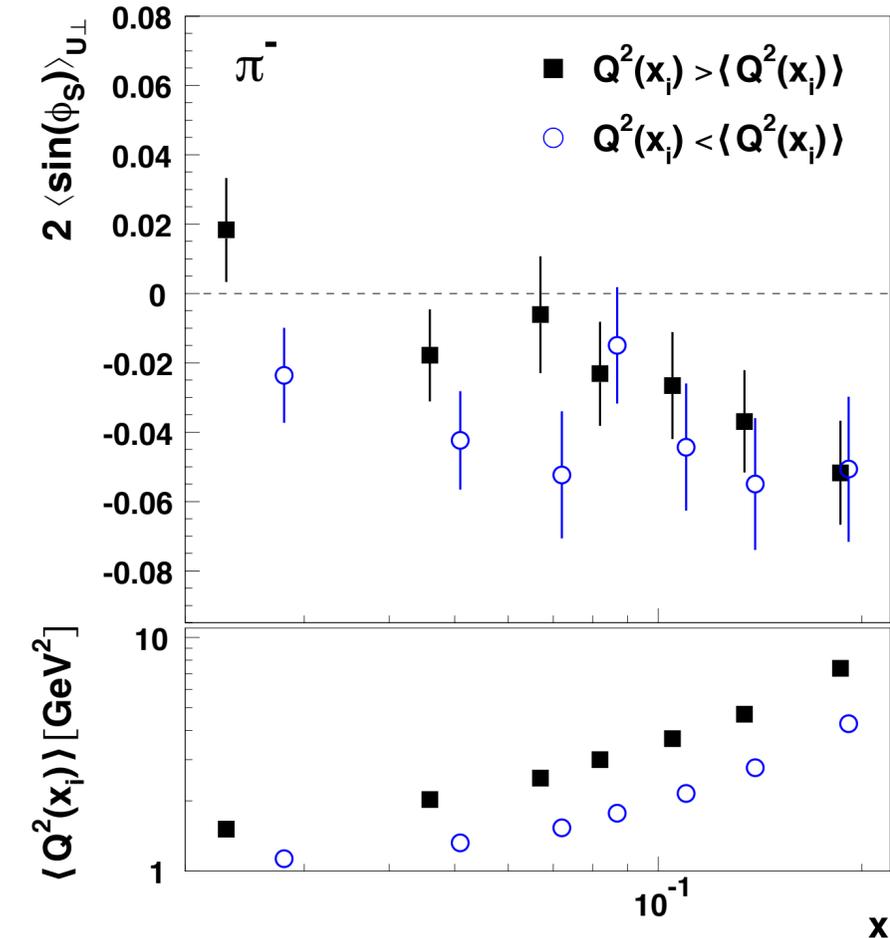
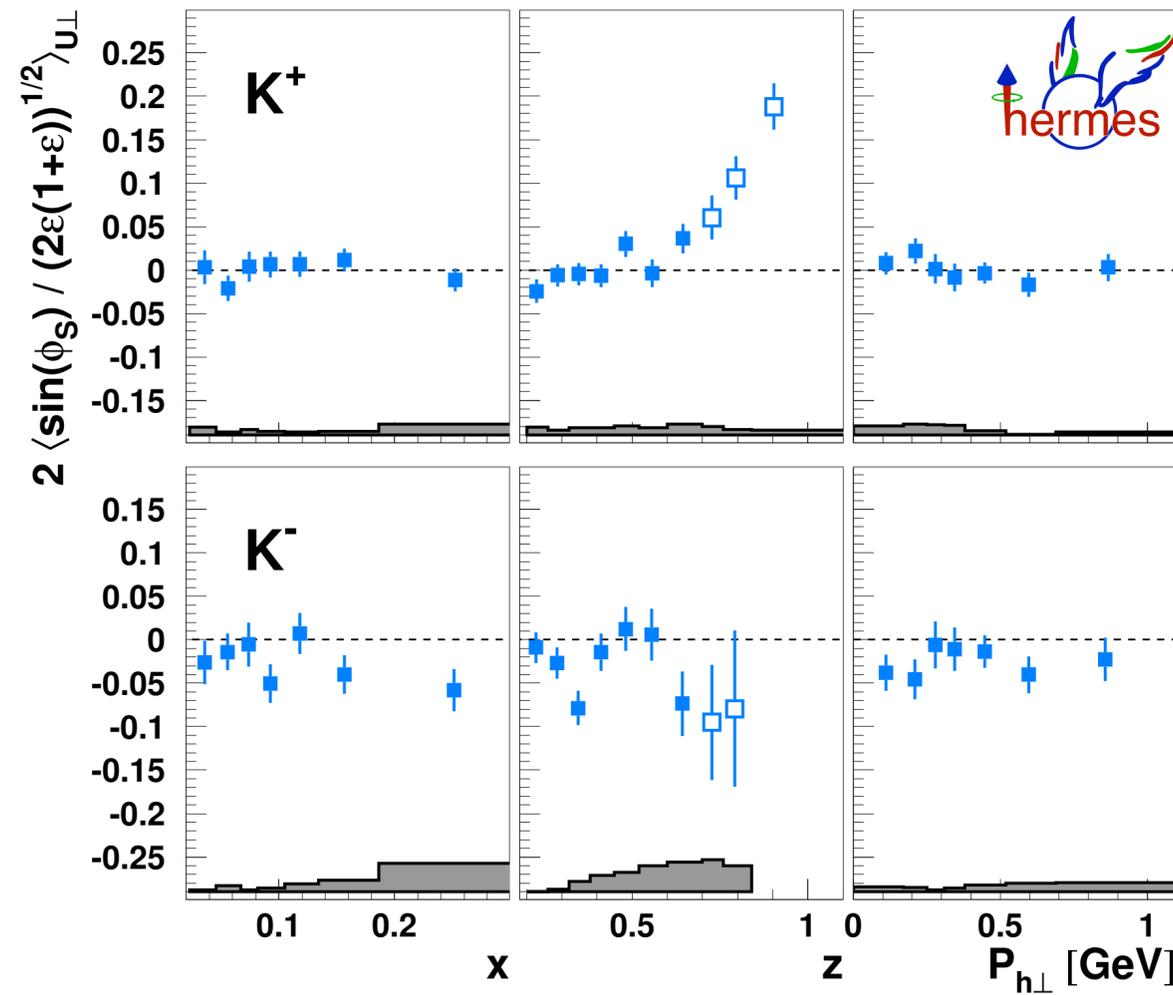
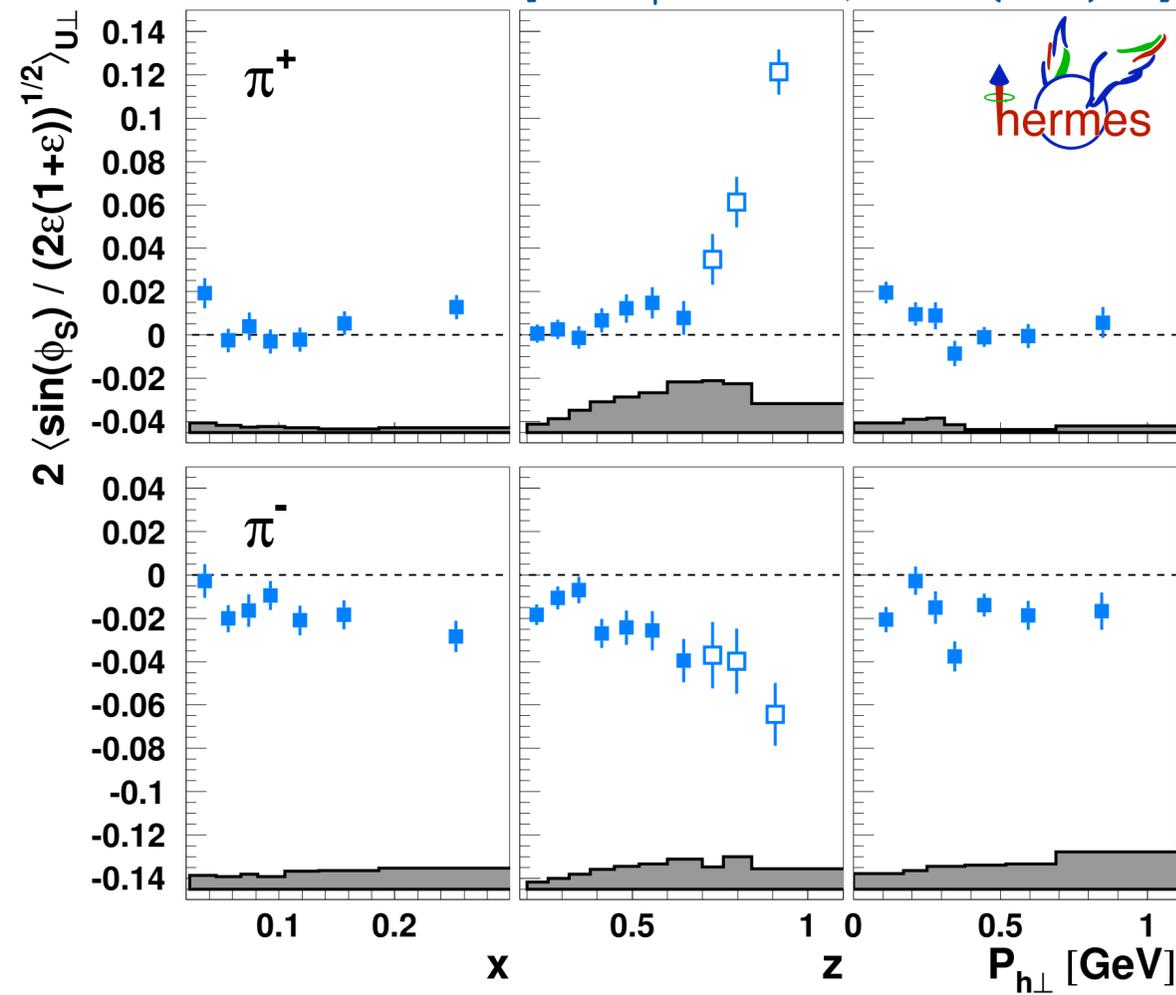
subleading twist — $\langle \sin(\phi_s) \rangle_{UT}$



- clearly non-zero asymmetries with opposite sign for charged pions (Collins-like behavior)
- striking z dependence and in particular magnitude

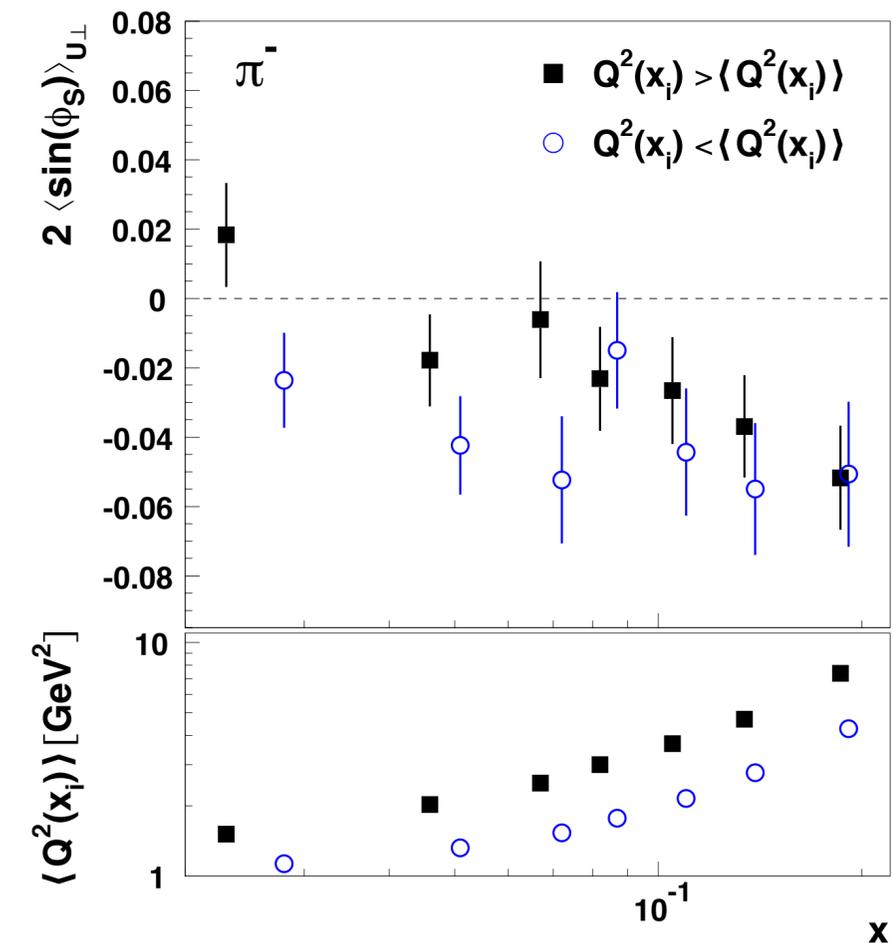
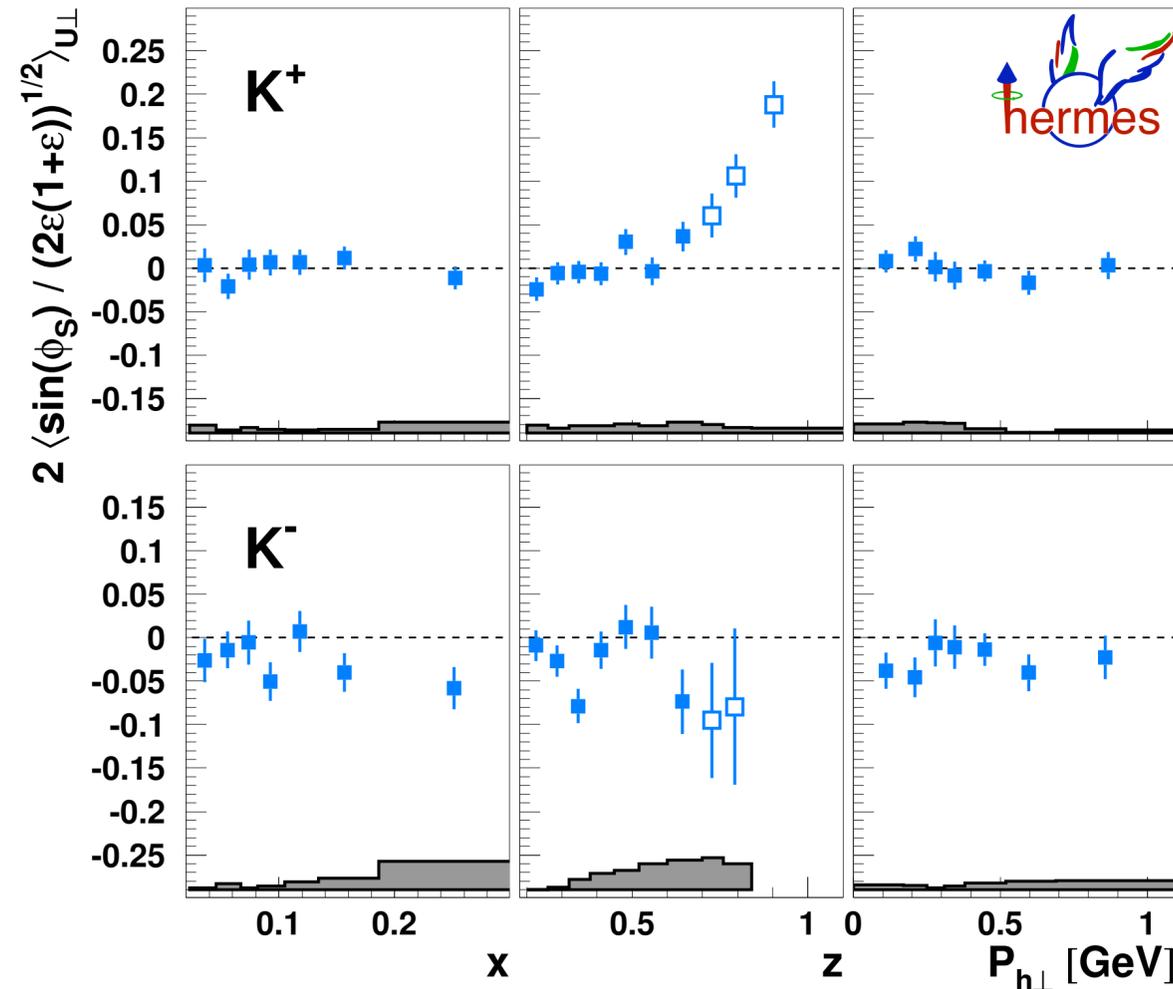
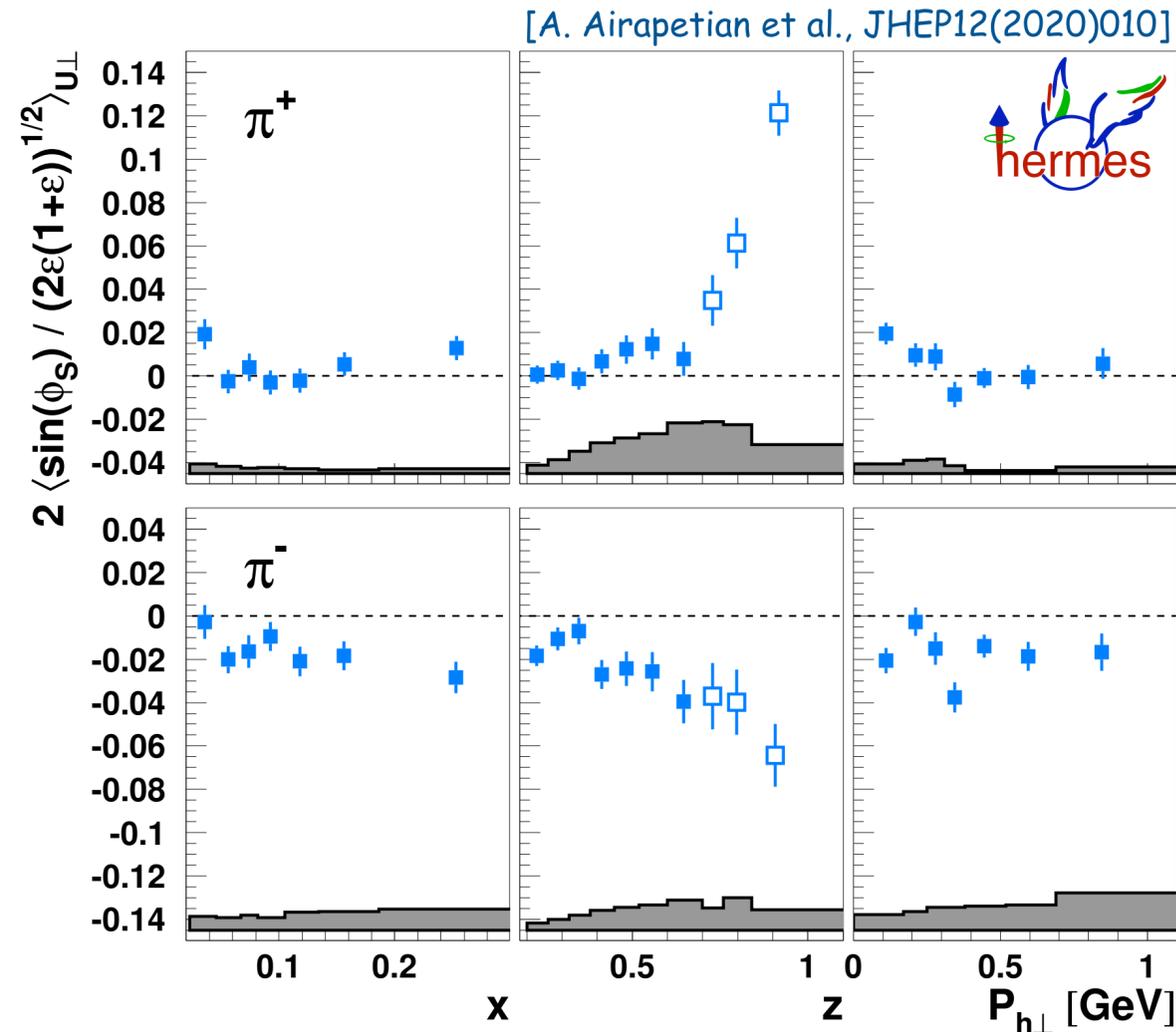
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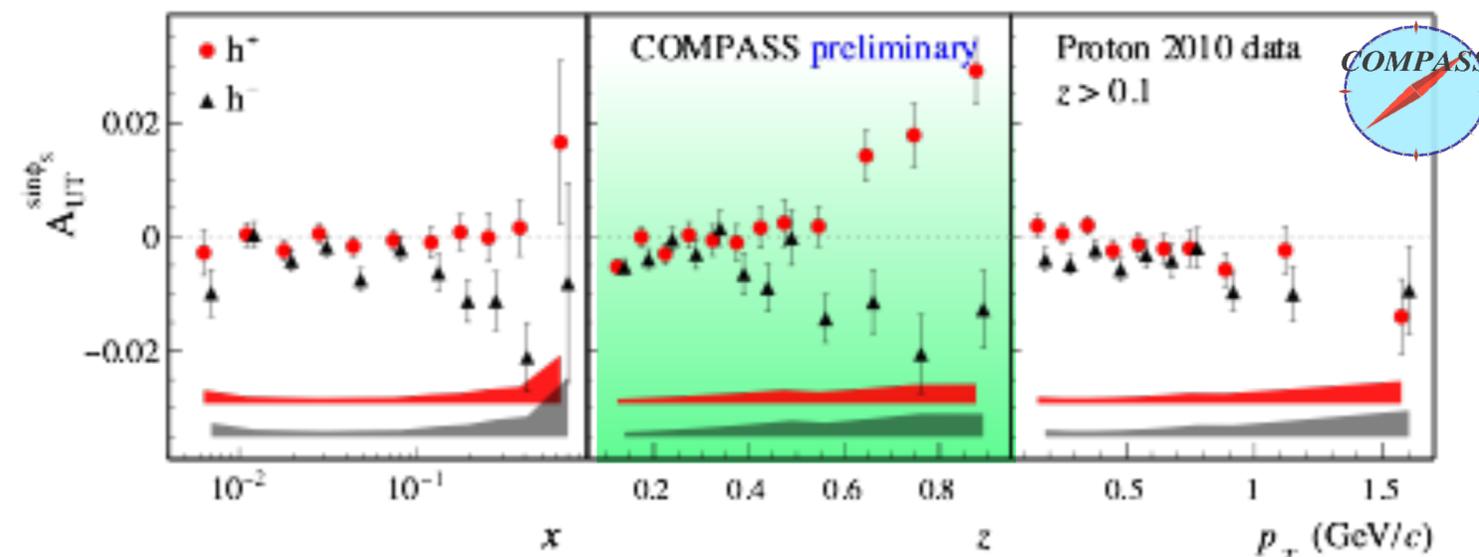


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- hint of Q suppression

subleading twist — $\langle \sin(\phi_s) \rangle_{UT}$



- clearly non-zero asymmetries with opposite sign for charged pions (Collins-like behavior)
- striking z dependence and in particular magnitude
- hint of Q suppression
- similar z behaviour seen at COMPASS



- HERMES continues producing results long after its shut down
- latest publications provide 3-dimensional presentations of longitudinal and transverse SSA and DSA
- completes the TMD analyses of single-hadron production
- multi-d analyses not only important to reduce experimental systematics but also to permit the isolation of the phase space of interest
- several significant leading-twist spin-momentum correlations (Sivers, Collins, worm-gear) and surprising twist-3 effects
- by now, **basically all but one (A_{UL}) asymmetries** extracted simultaneously in **three or even four dimensions** — a rich data set on transverse-momentum distributions
- complementary to data from other facilities

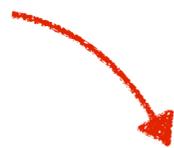
backup slides

double-spin asymmetry $A_{||}$

$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[\frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

double-spin asymmetry $A_{||}$

azimuthal
correction


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nucleon-in-nucleus
depolarization factor
(0.926 for deuteron due
to D-state admixture)

double-spin asymmetry $A_{||}$

azimuthal correction

luminosities

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polarization-weighted luminosities

double-spin asymmetry $A_{||}$

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nucleon-in-nucleus depolarization factor (0.926 for deuteron due to D-state admixture)

polarization-weighted luminosities

unfolded for QED radiation to Born level

double-spin asymmetry $A_{||}$

$$A_{||}^h \equiv \frac{C_{\phi}^h}{f_D} \left[\frac{L_{\Rightarrow} N_{\Leftarrow}^h - L_{\Leftarrow} N_{\Rightarrow}^h}{L_{P,\Rightarrow} N_{\Leftarrow}^h + L_{P,\Leftarrow} N_{\Rightarrow}^h} \right]_B$$

- dominated by statistical uncertainties
- main systematics arise from
 - polarization measurements [6.6% for hydrogen, 5.7% for deuterium]
 - azimuthal correction [$O(\text{few } \%)$]

azimuthal-asymmetry corrections

measured

"polarized Cahn" effect etc.

$$\tilde{A}_{\parallel}^h(x, Q^2, z, P_{h\perp}) = \frac{\int d\phi \sigma_{\parallel}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}{\int d\phi \sigma_{UU}^h(x, Q^2, z, P_{h\perp}, \phi) \xi(\phi)}$$

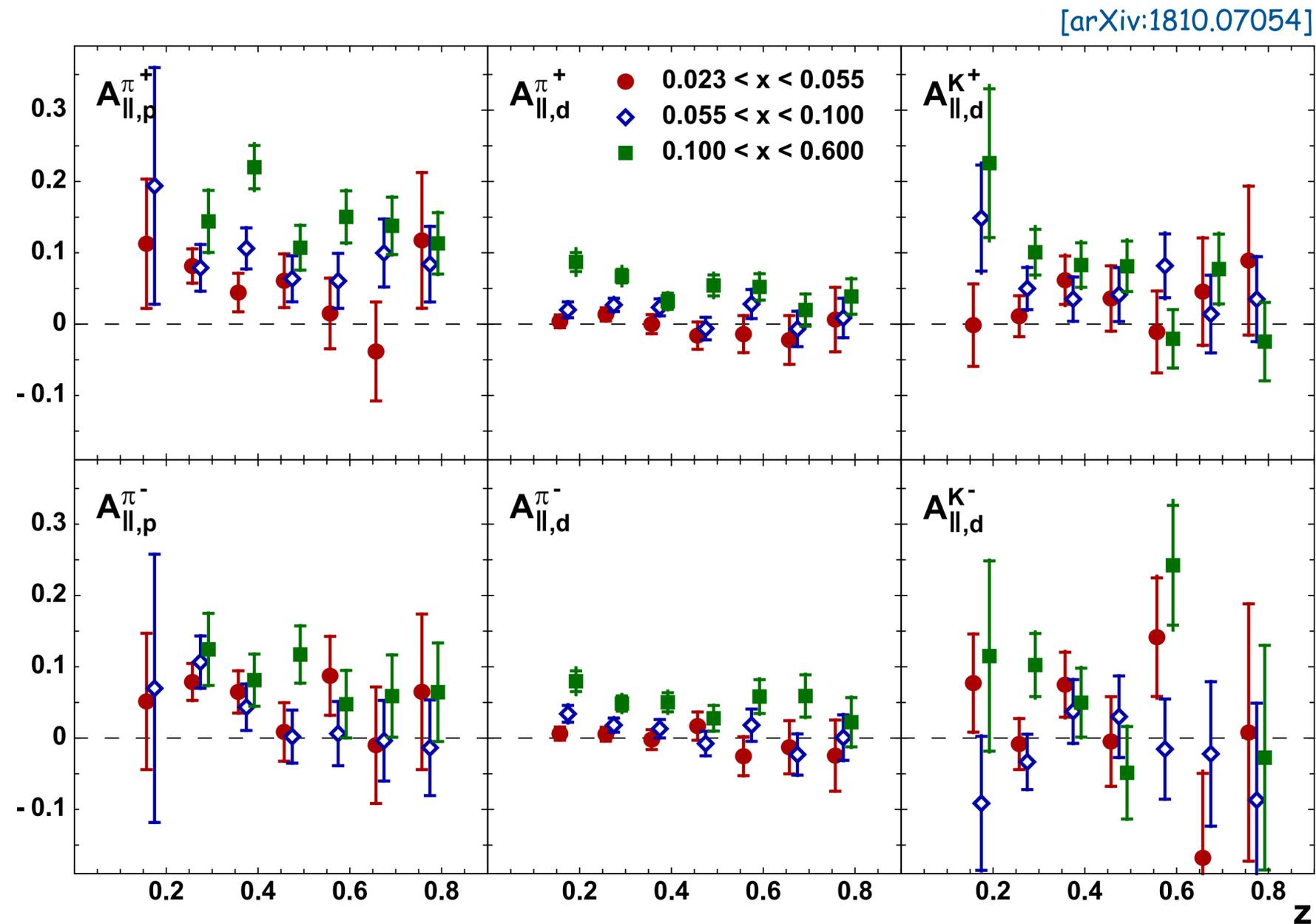
Boer-Mulders and Cahn effects etc.

azimuthal acceptance

- both numerator and in particular denominator ϕ dependent
 - in theory integrated out
 - in praxis, detector acceptance also ϕ dependent
 - convolution of physics & acceptance leads to bias in normalization of asymmetries
- implement data-driven model for azimuthal modulations [PRD 87 (2013) 012010] into MC 
extract correction factor & apply to data

z dependence of $A_{||}$ (three x ranges)

- in general, no strong z -dependence visible



semi-inclusive DIS

- excluding transverse polarization:

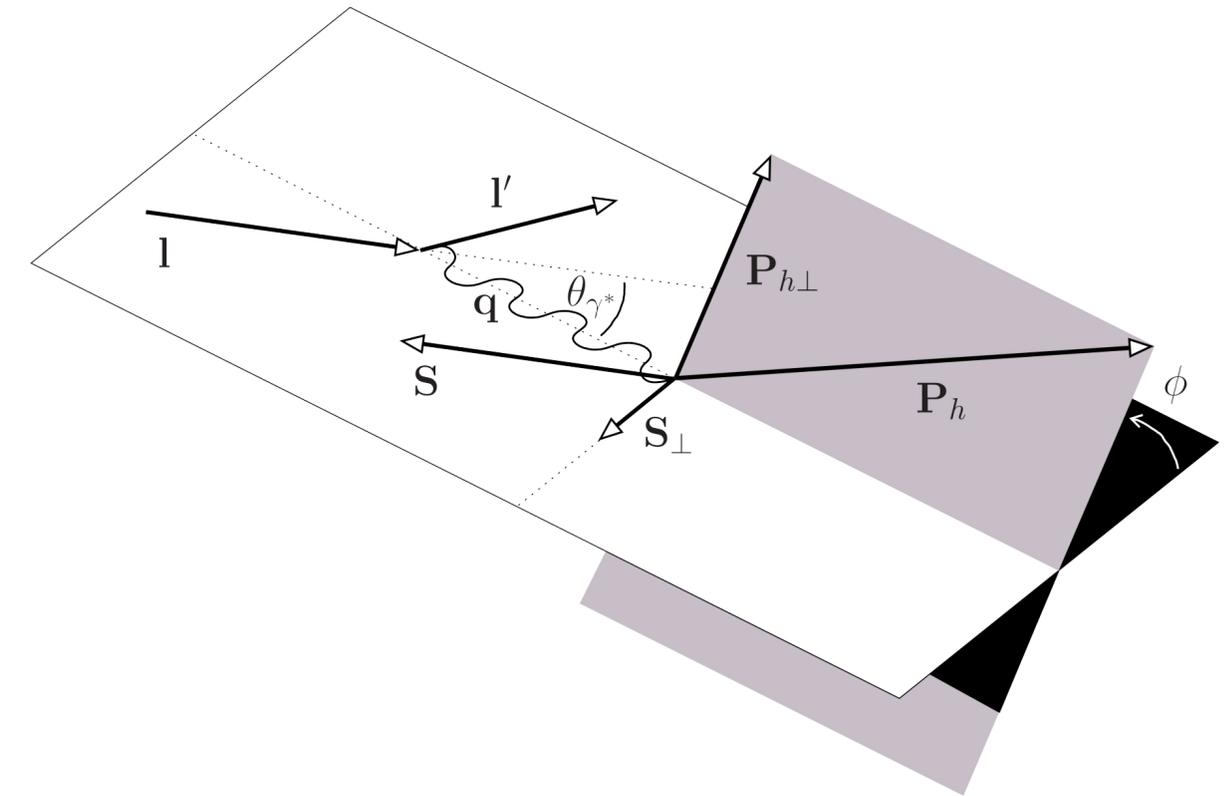
$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ \begin{aligned} &F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \\ &+ \sqrt{2\epsilon} \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi \\ &+ \sqrt{2\epsilon} \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi \\ &+ \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \end{aligned} \right\}$$

$$F_{XY}^{h,\text{mod}} = F_{XY}^{h,\text{mod}}(x, Q^2, z, P_{h\perp})$$



 Beam (λ) / Target (Λ)
 helicities



semi-inclusive DIS

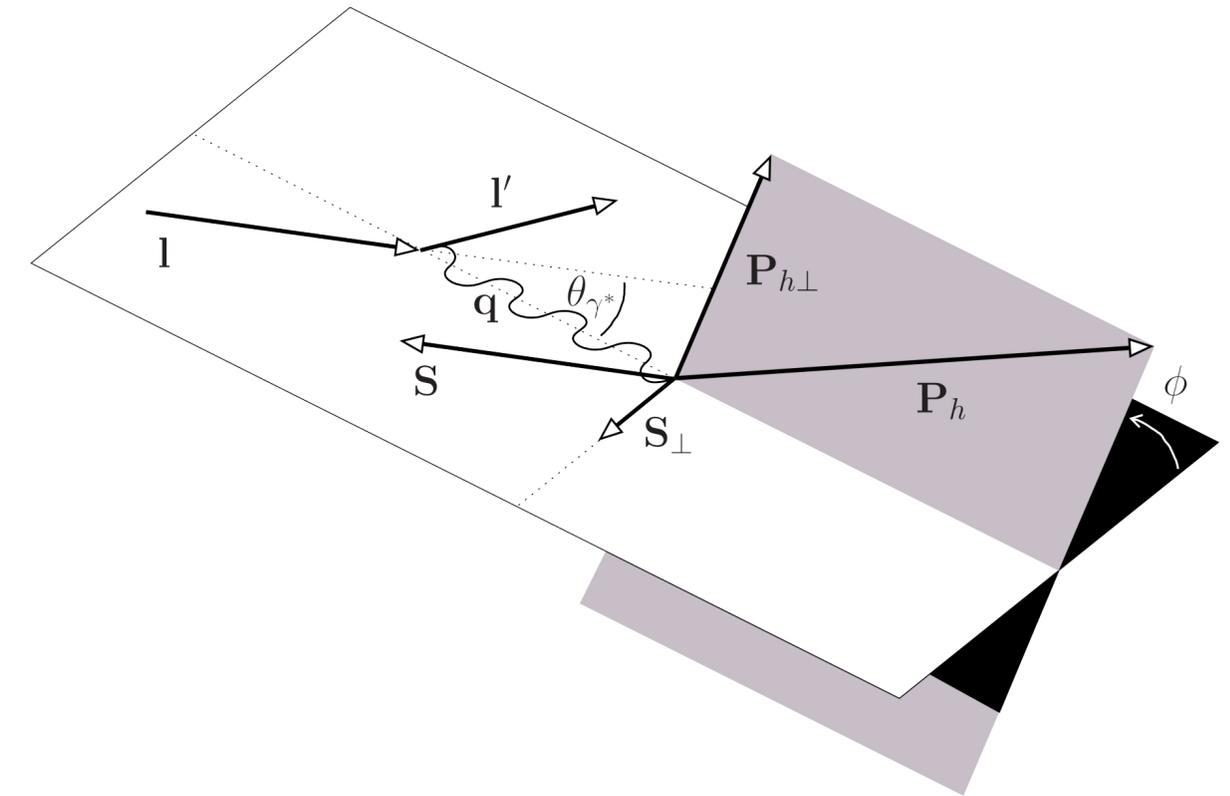
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- single-spin asymmetry:

$$A_{LU}^h \equiv \frac{\sigma_{+-}^h + \sigma_{++}^h - \sigma_{-+}^h - \sigma_{--}^h}{\sigma_{+-}^h + \sigma_{++}^h + \sigma_{-+}^h + \sigma_{--}^h}$$



beam-helicity asymmetry

$$\frac{M_h}{Mz} h_1^\perp \tilde{E} \oplus xg^\perp D_1 \oplus \frac{M_h}{Mz} f_1 \tilde{G}^\perp \oplus xeH_1^\perp$$

- naive-T-odd Boer-Mulders (BM) function coupled to a twist-3 FF
 - signs of BM from unpolarized SIDIS
 - little known about interaction-dependent FF

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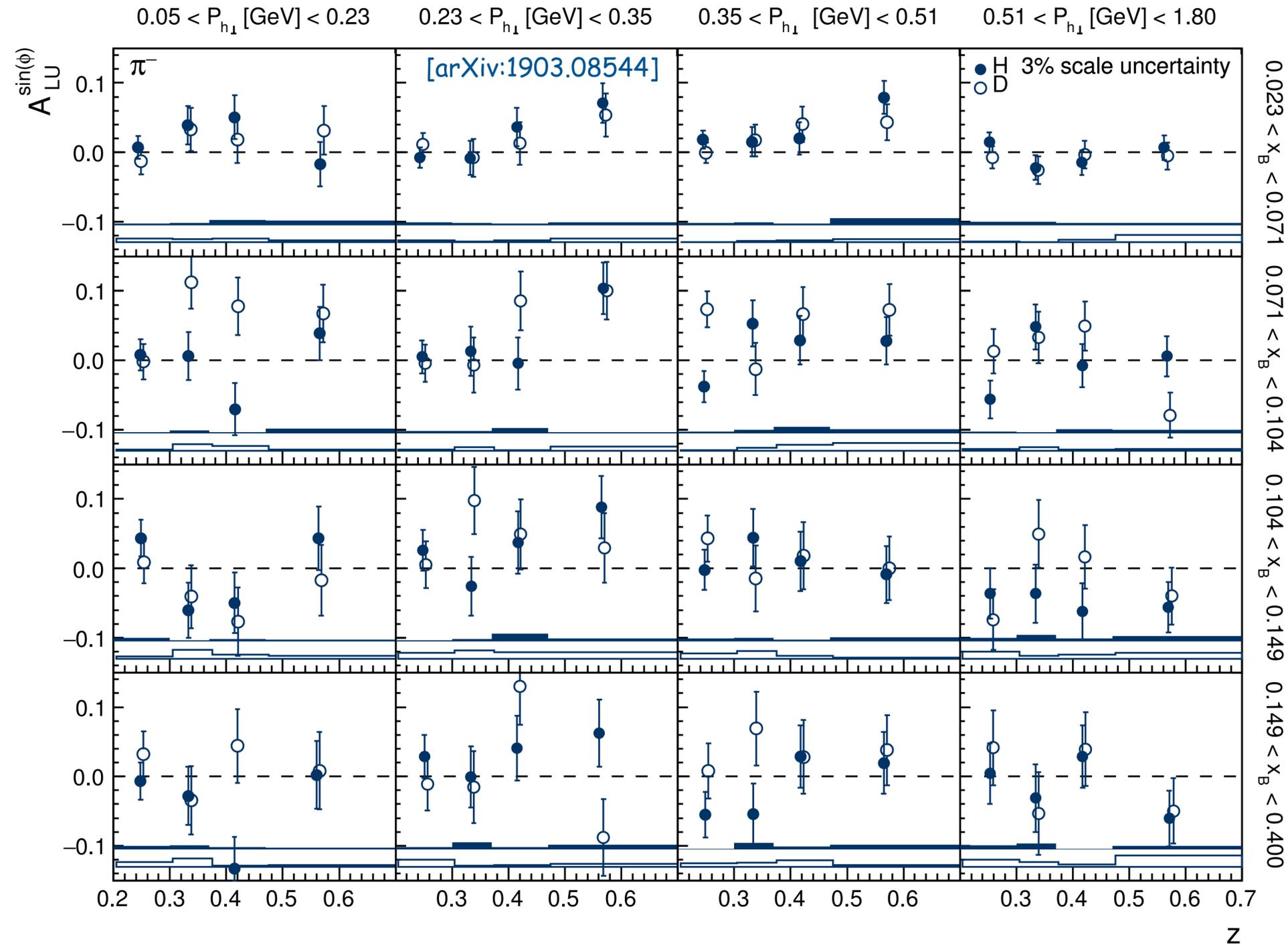
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- little known about naive-T-odd g^\perp ; singled out in A_{LU} in jet production
- large unpolarized f_1 , coupled to interaction-dependent FF
- twist-3 e survives integration over $P_{h\perp}$; here coupled to Collins FF
 - e linked to the pion-nucleon σ -term
 - interpreted as color force (from remnant) on transversely polarized quarks at the moment of being struck by virtual photon

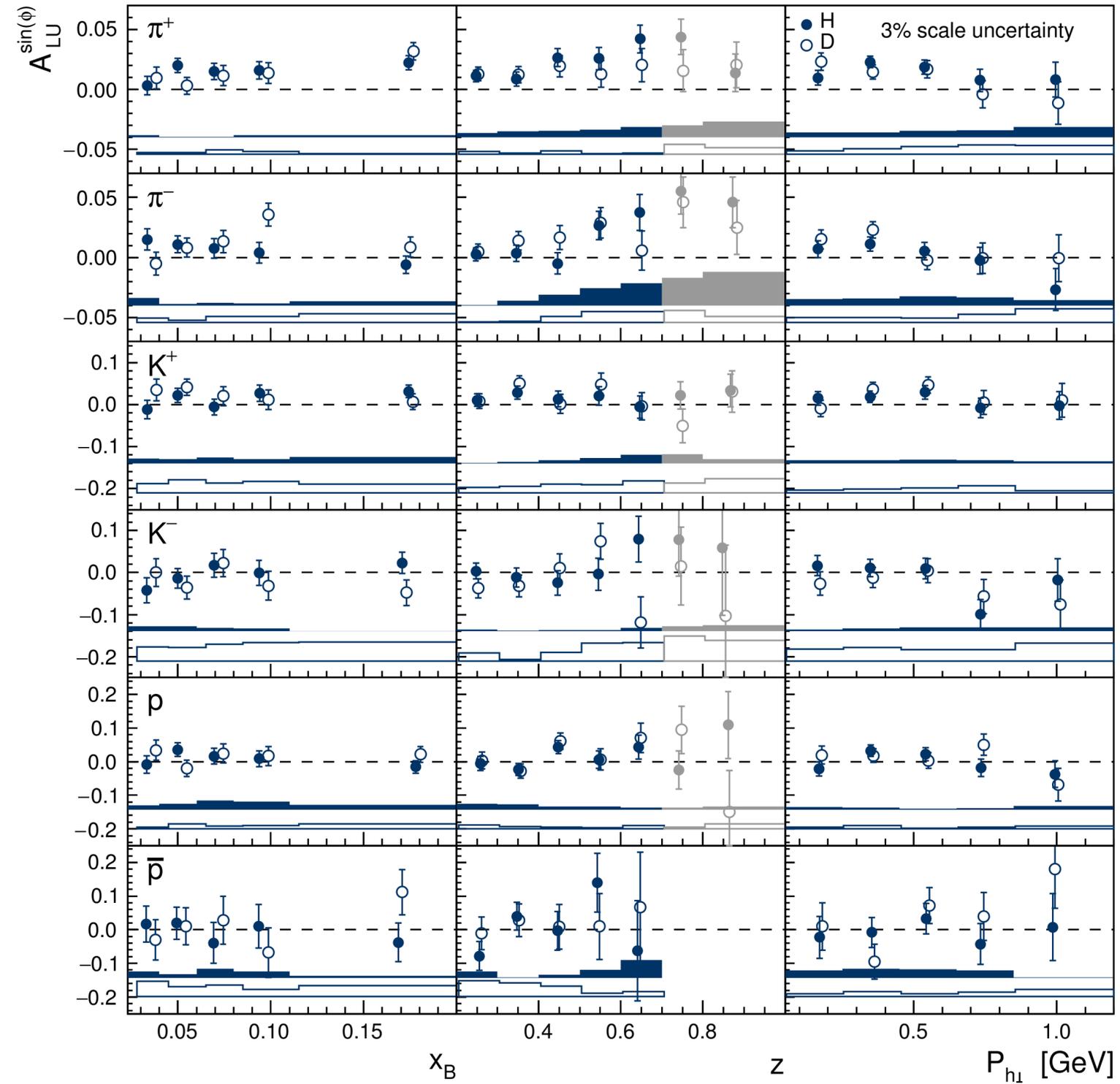
3d beam-helicity asymmetry for π^-



most comprehensive presentation, for discussion use 1d binning

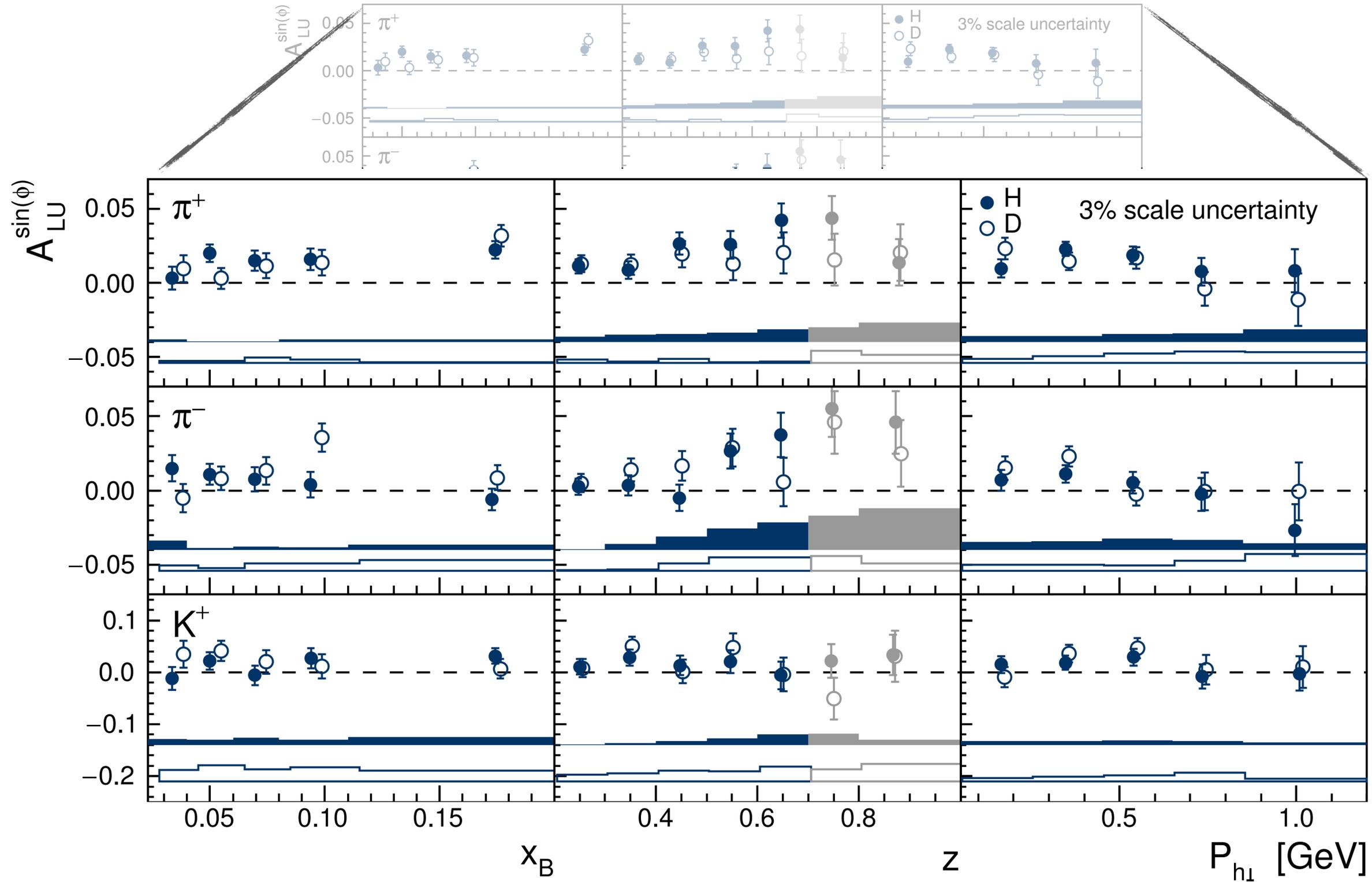
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[arXiv:1903.08544]

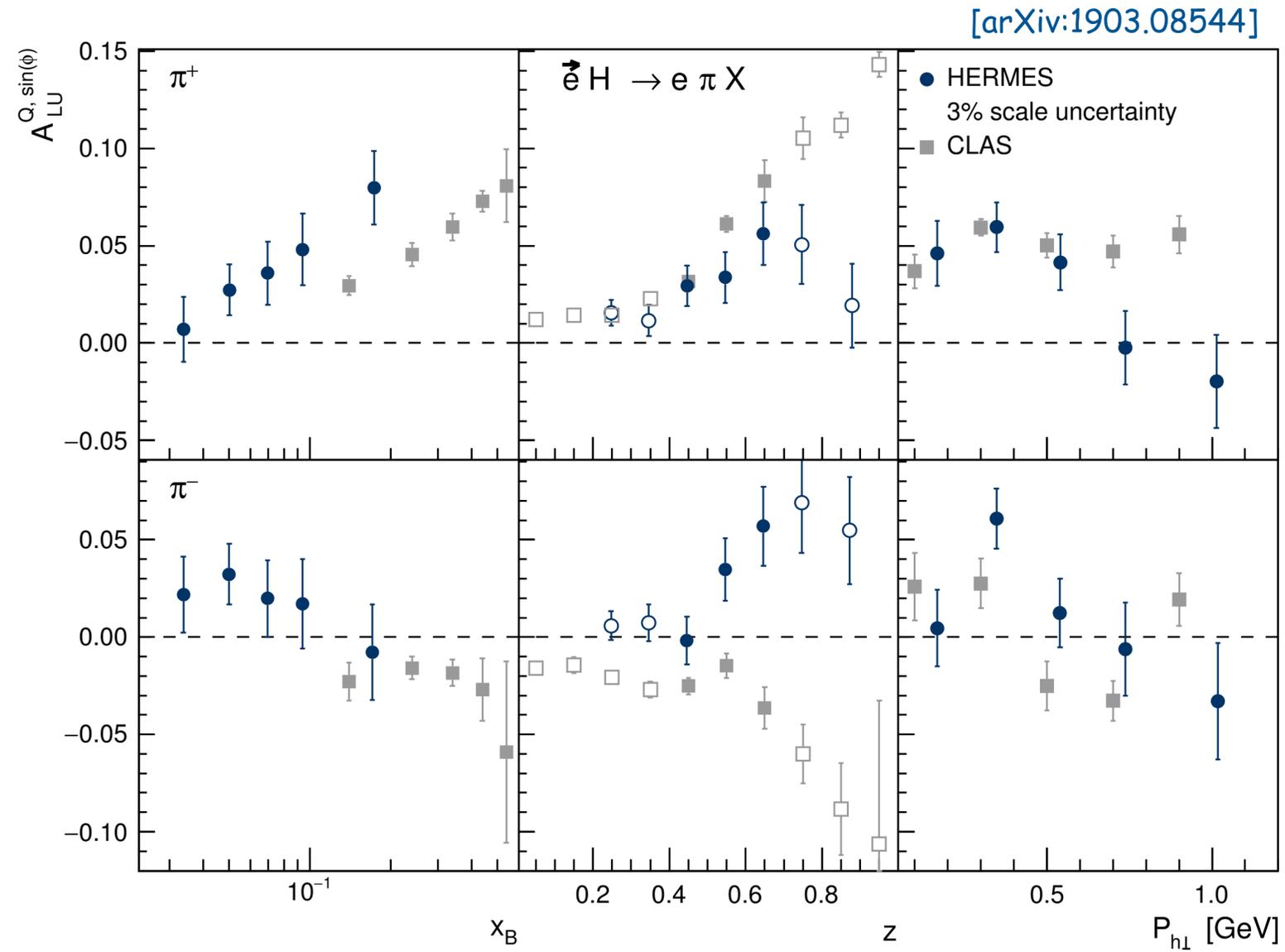


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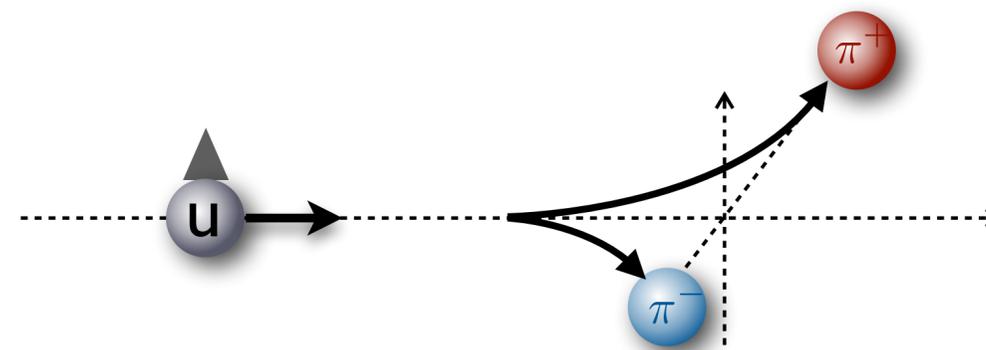
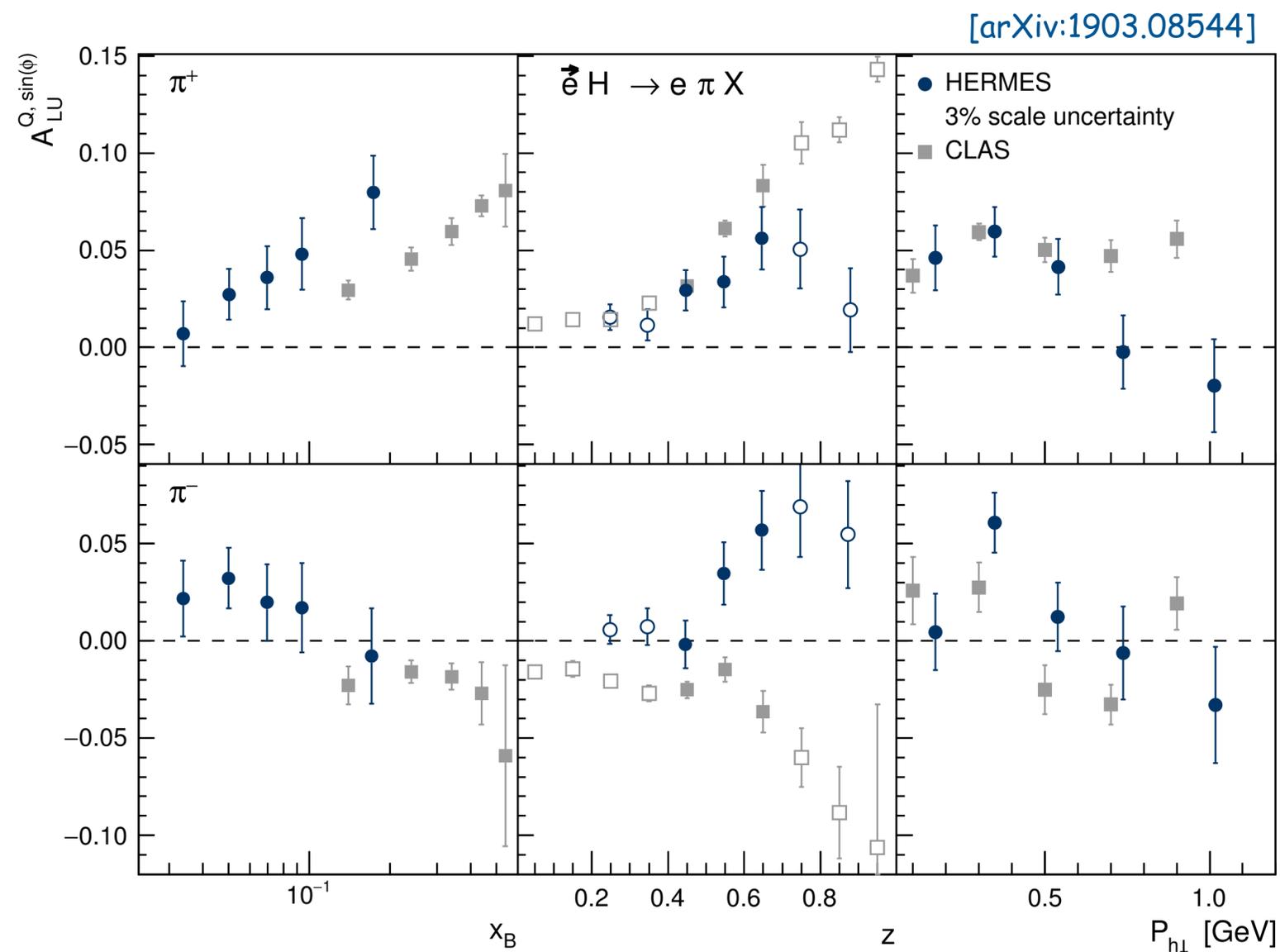


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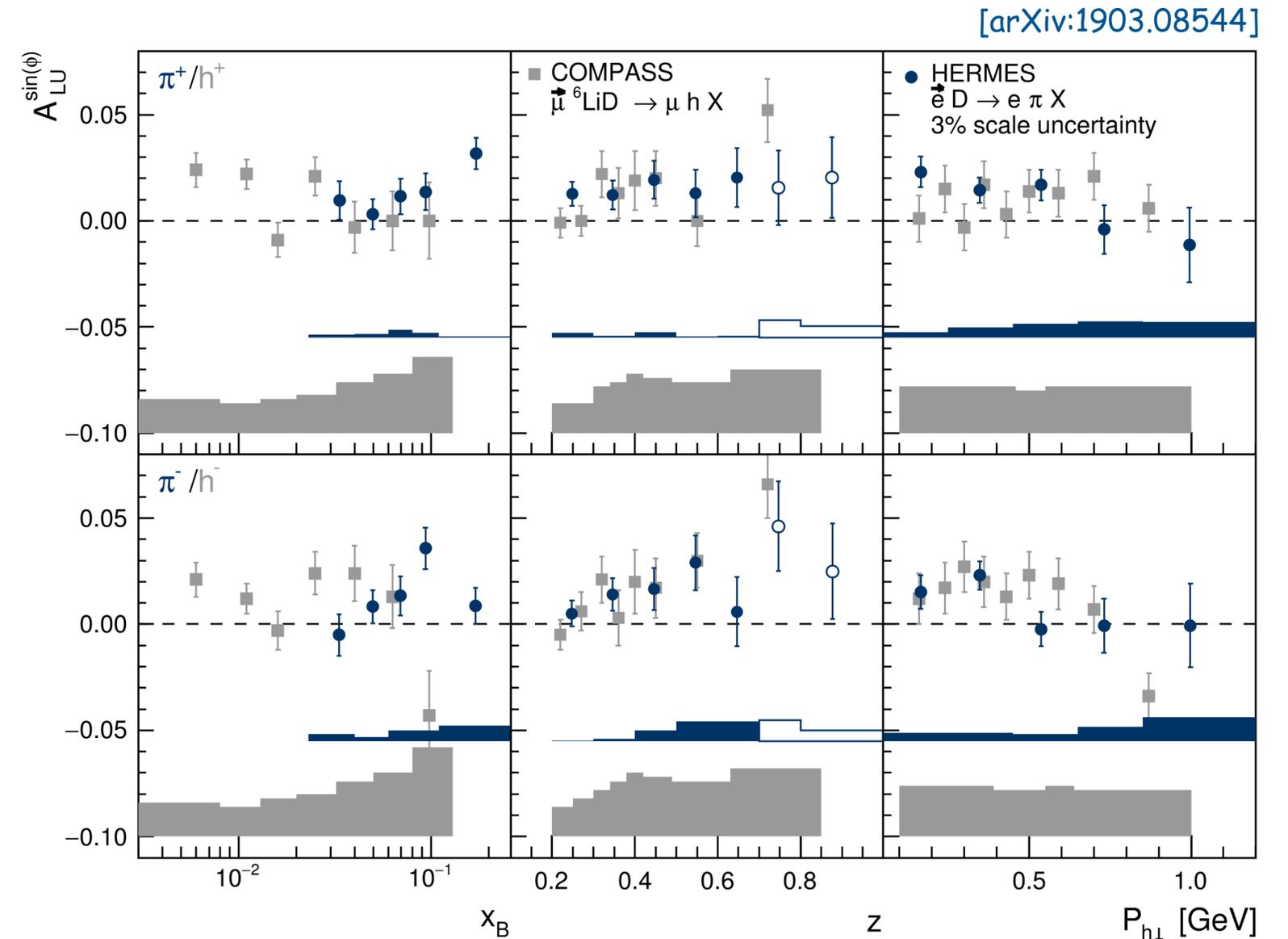
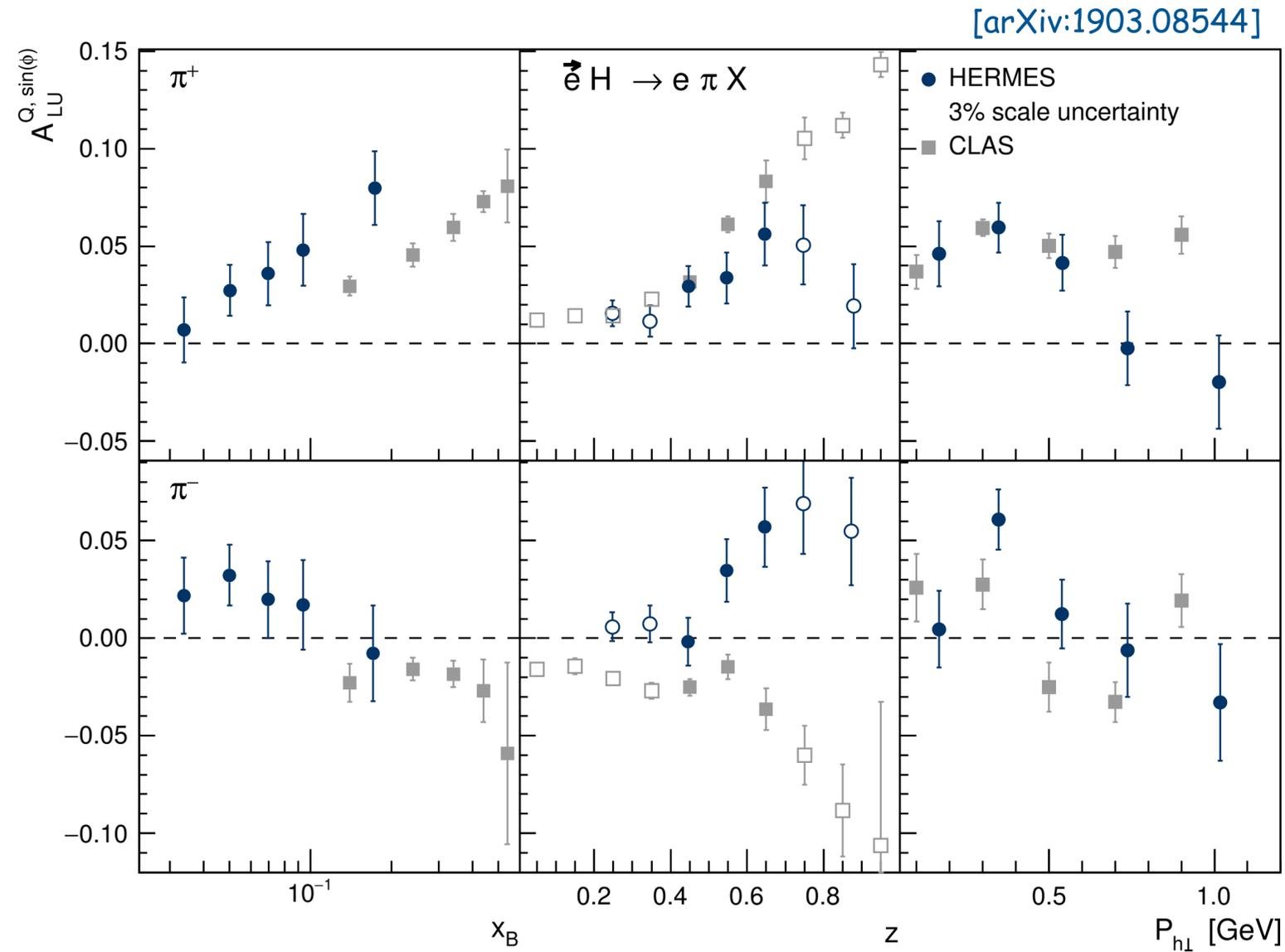
● opposite behavior at HERMES/CLAS of negative pions in z projection due to different x -range probed

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- opposite behavior at HERMES/CLAS of negative pions in z projection due to different x -range probed
- CLAS more sensitive to $e(x) \otimes$ Collins term due to higher x probed?

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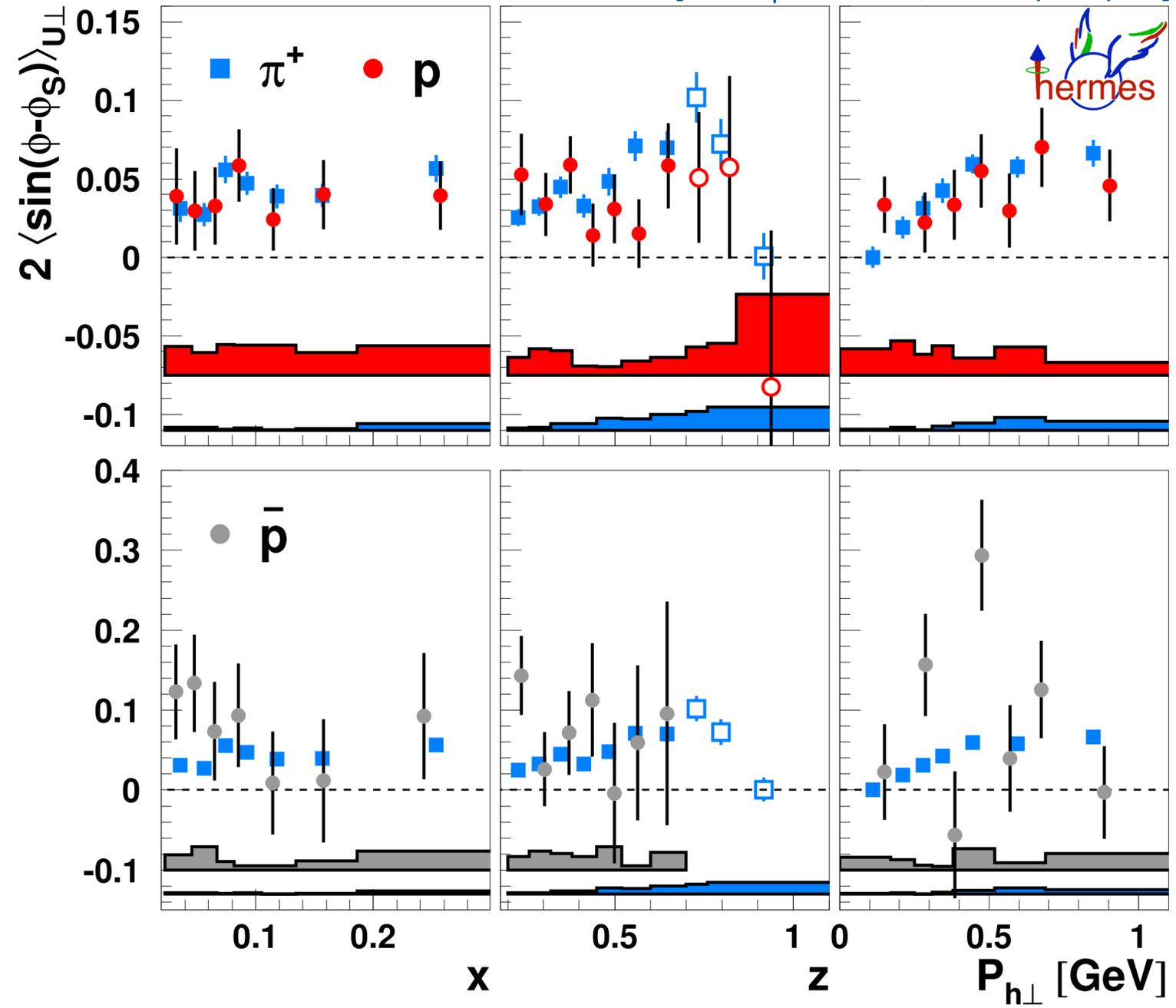


- opposite behavior at HERMES/CLAS of negative pions in z projection due to different x-range probed
- CLAS more sensitive to $e(x) \otimes$ Collins term due to higher x probed?
- consistent behavior for charged pions / hadrons at HERMES / COMPASS for isoscalar targets

Sivers amplitudes pions vs. (anti)protons

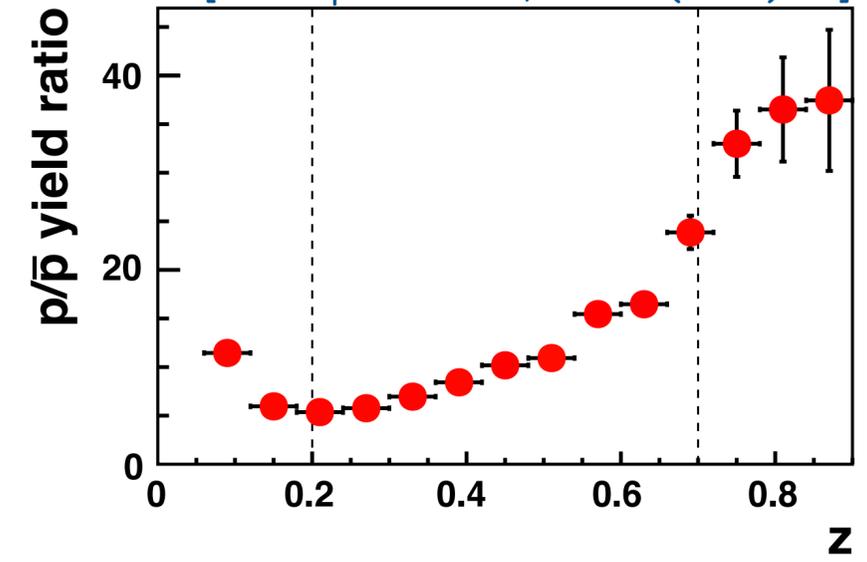
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[A. Airapetian et al., JHEP12(2020)010]



similar-magnitude asymmetries for (anti)protons and pions
 → consequence of u-quark dominance in both cases?

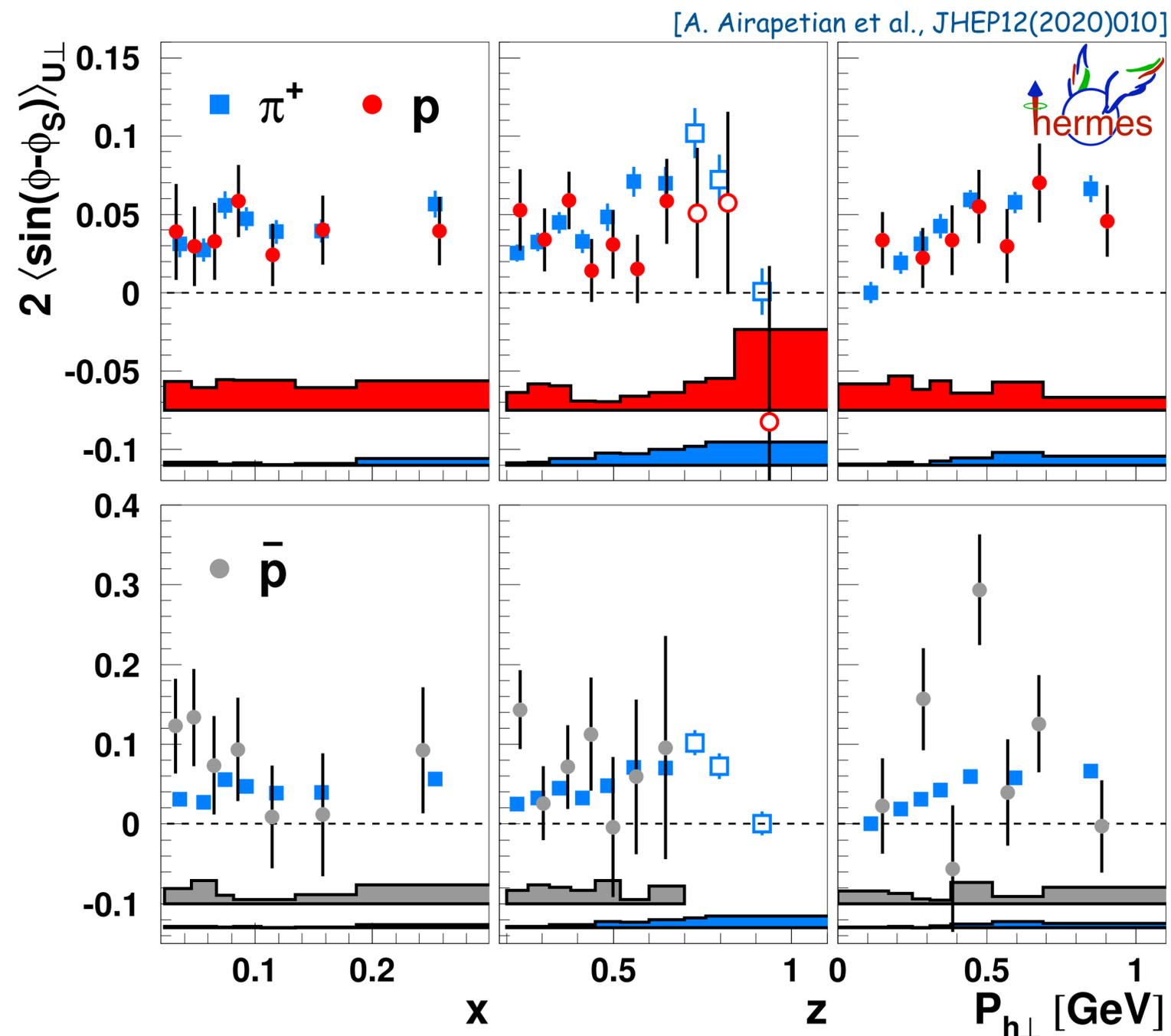
[A. Airapetian et al., JHEP12(2020)010]



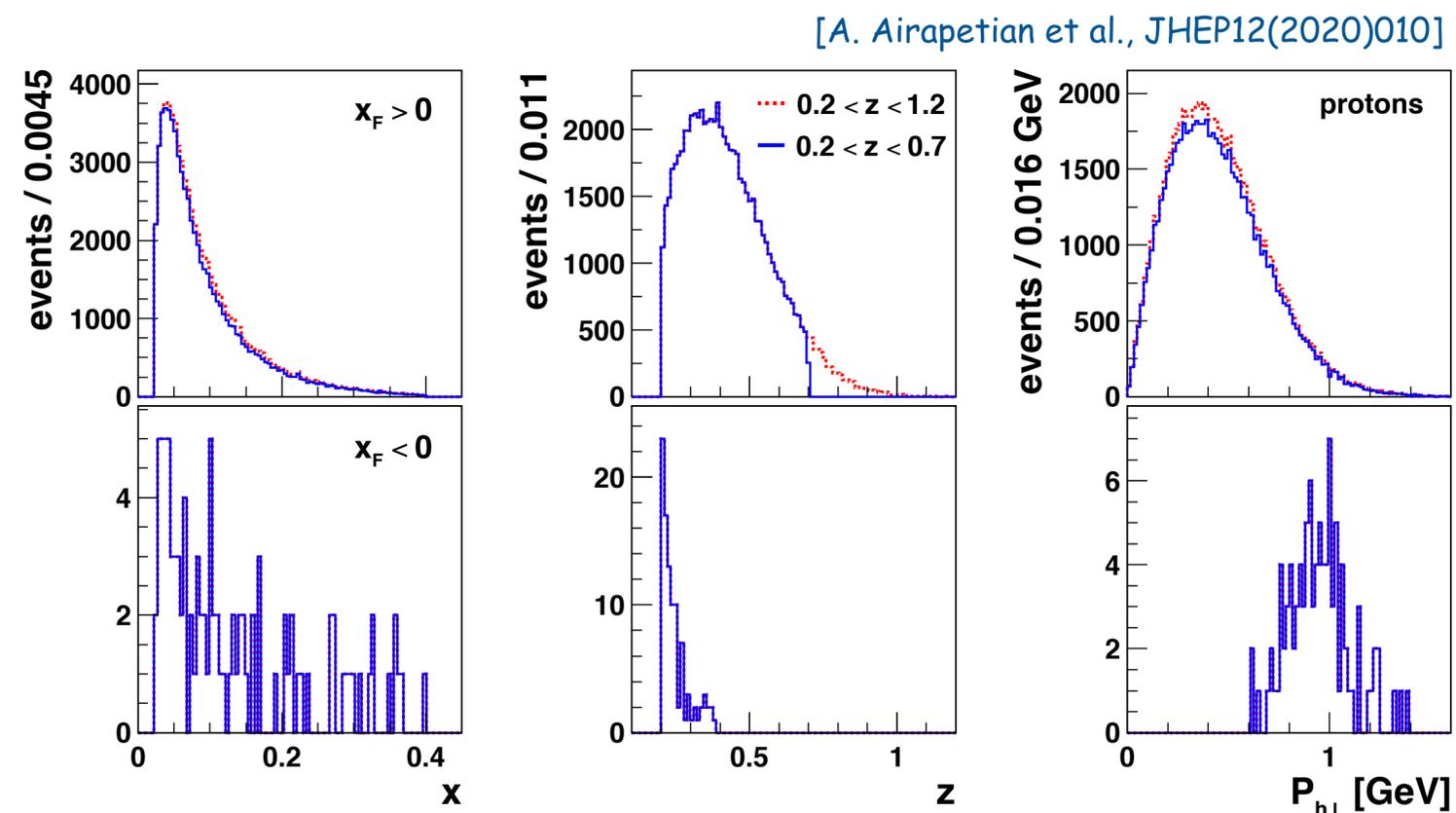
possibly, onset of target fragmentation only at lower z

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Sivers amplitudes pions vs. (anti)protons



similar-magnitude asymmetries for (anti)protons and pions
 → consequence of u-quark dominance in both cases?

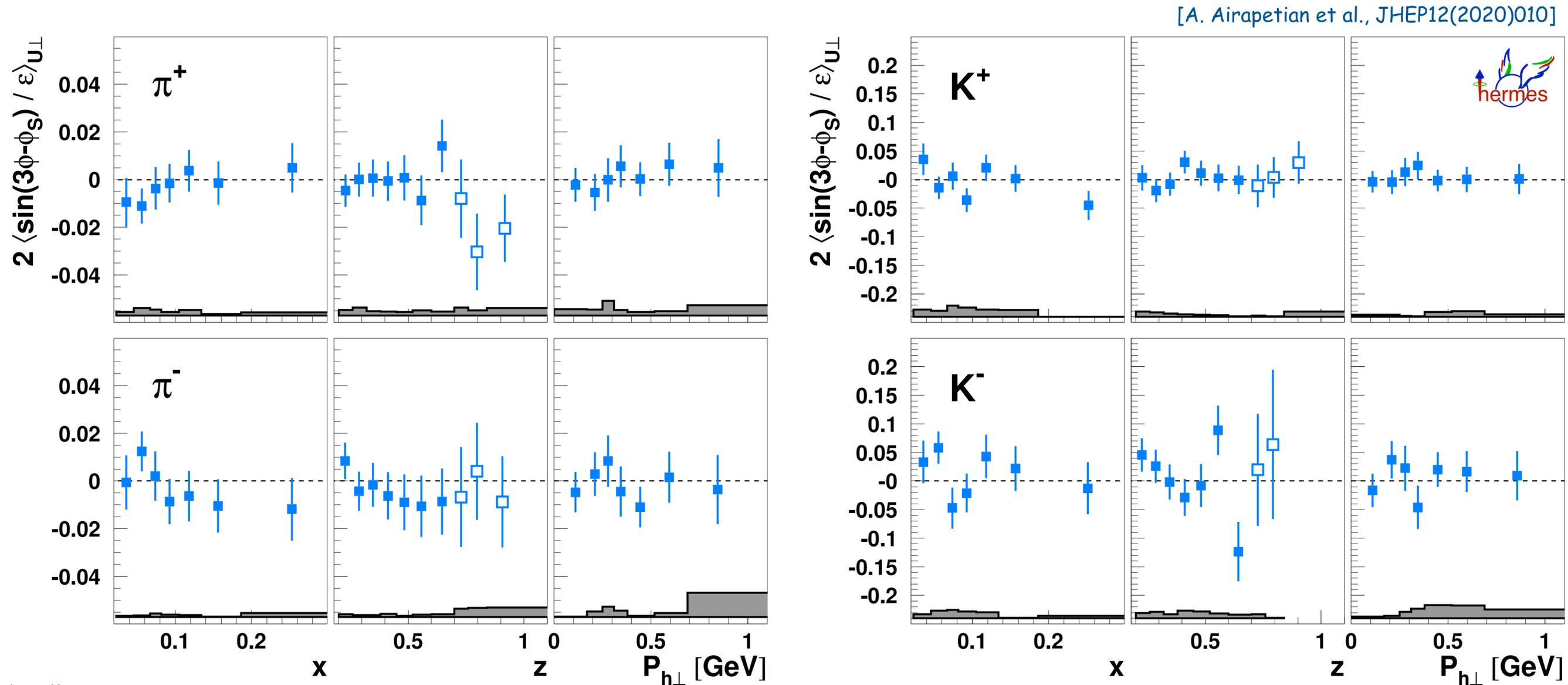


possibly, onset of target fragmentation only at lower z

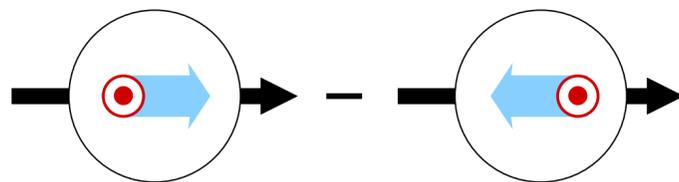
Pretzelosity

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

- chiral-odd \rightarrow needs Collins FF (or similar)
- $^1\text{H}, ^2\text{H}$ & ^3He data consistently small
- cancelations? pretzelosity=zero? or just the additional suppression by two powers of $P_{h\perp}$

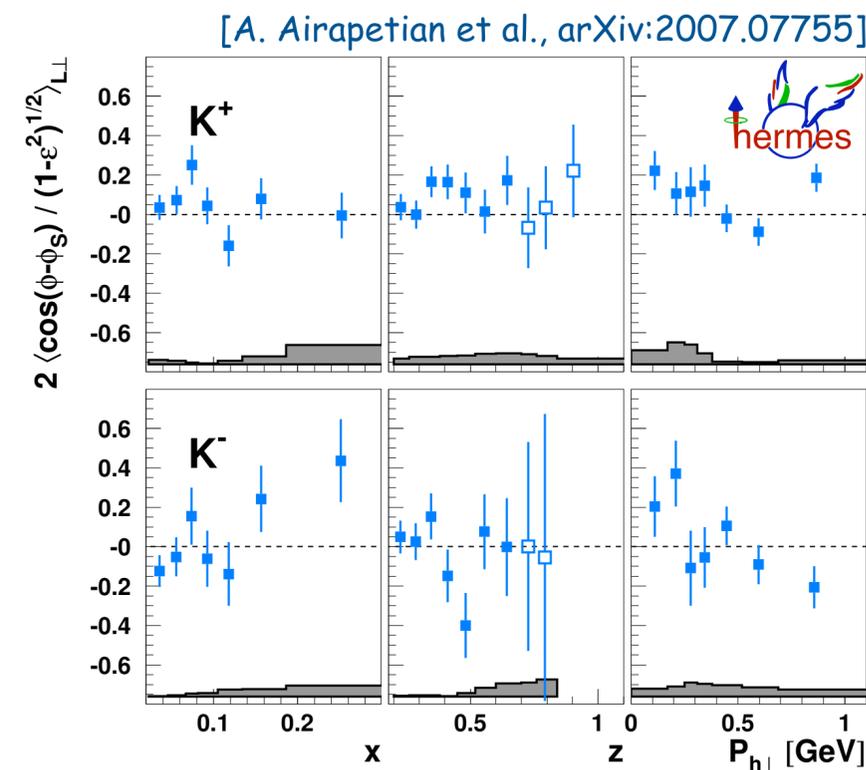
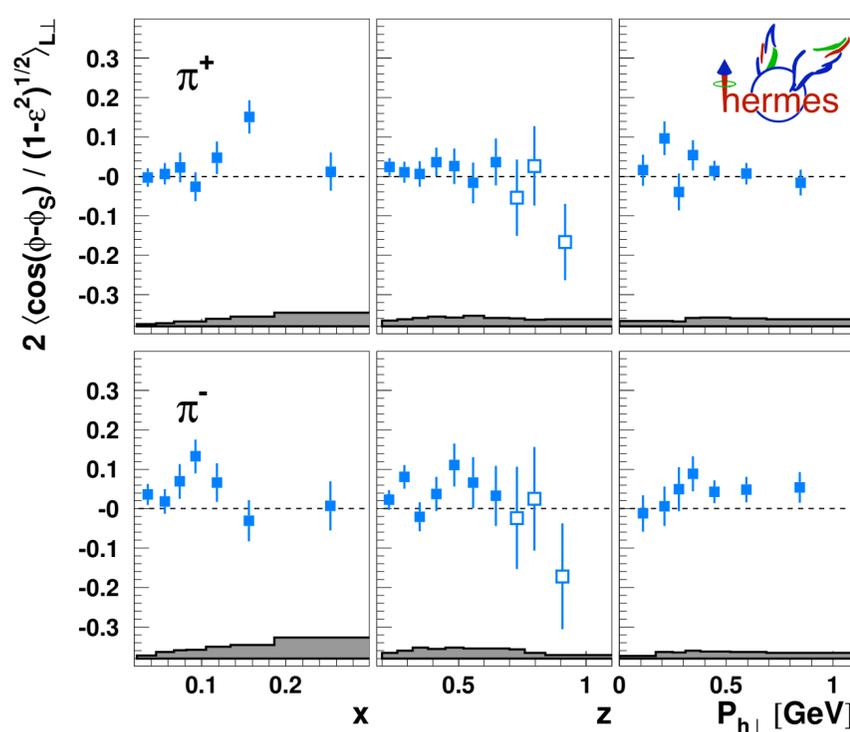
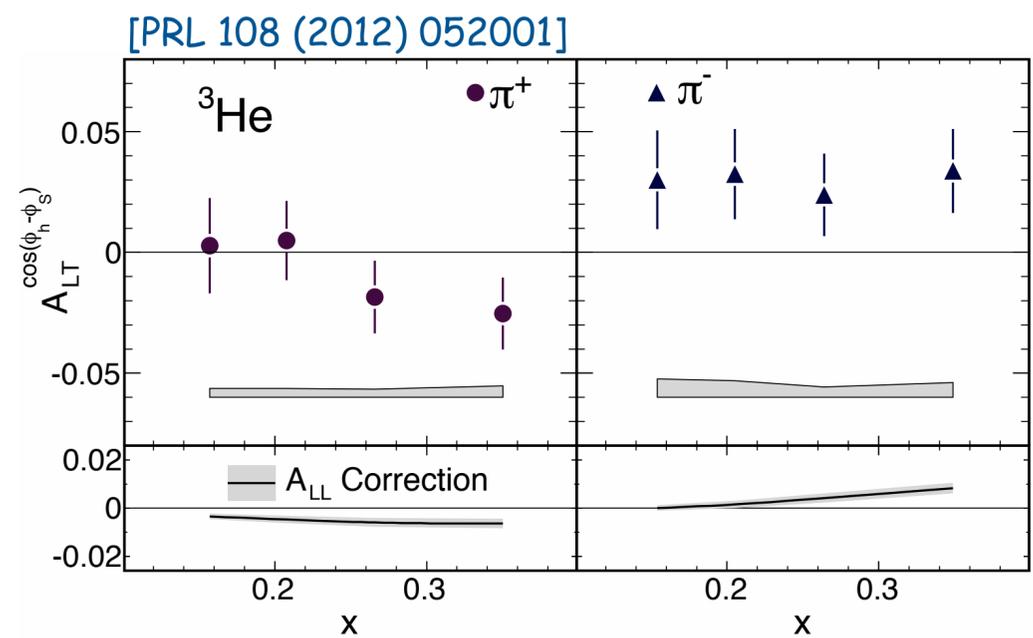
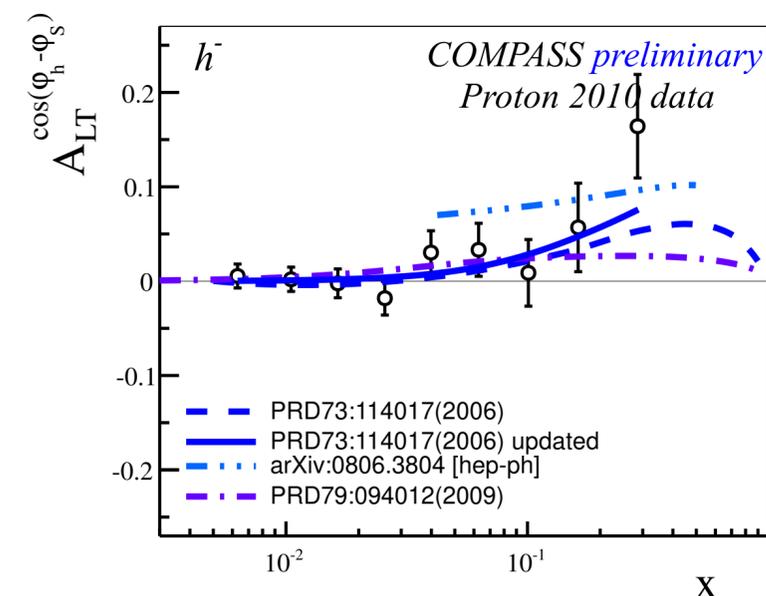
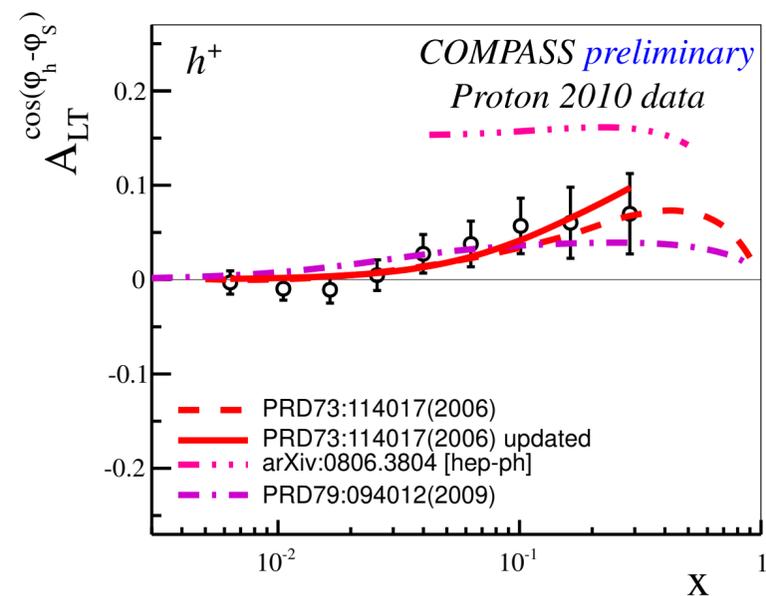


	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

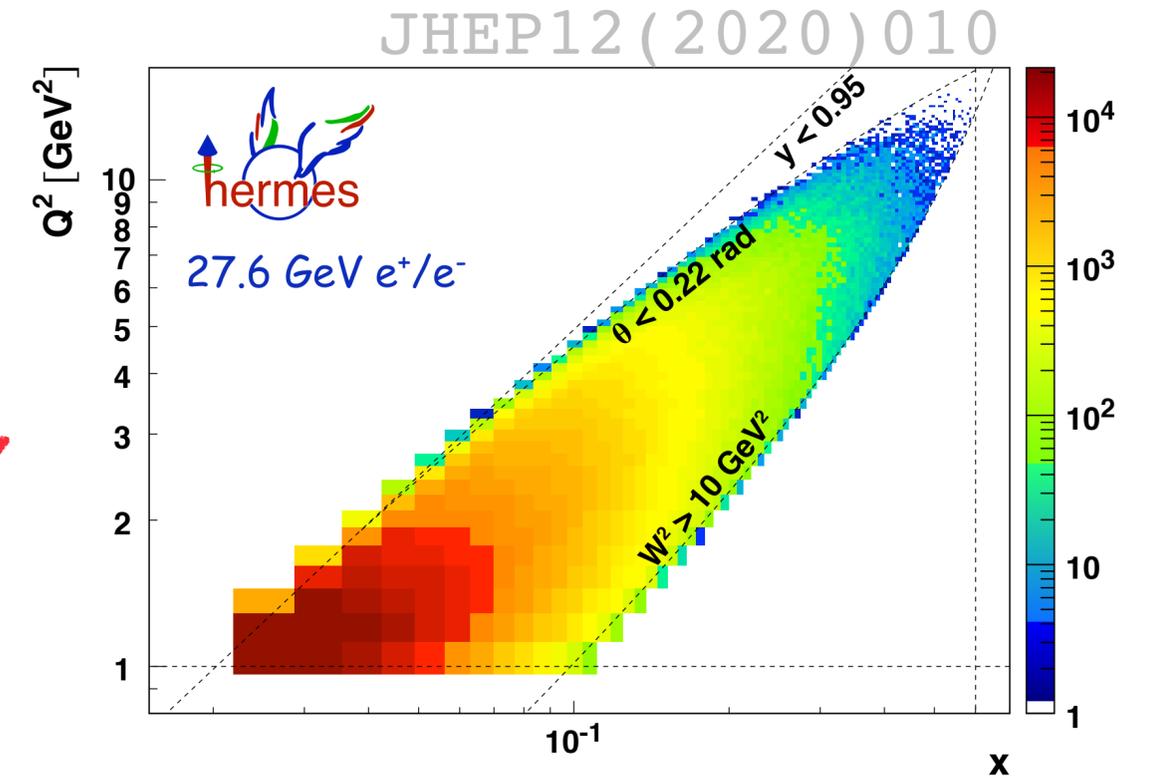
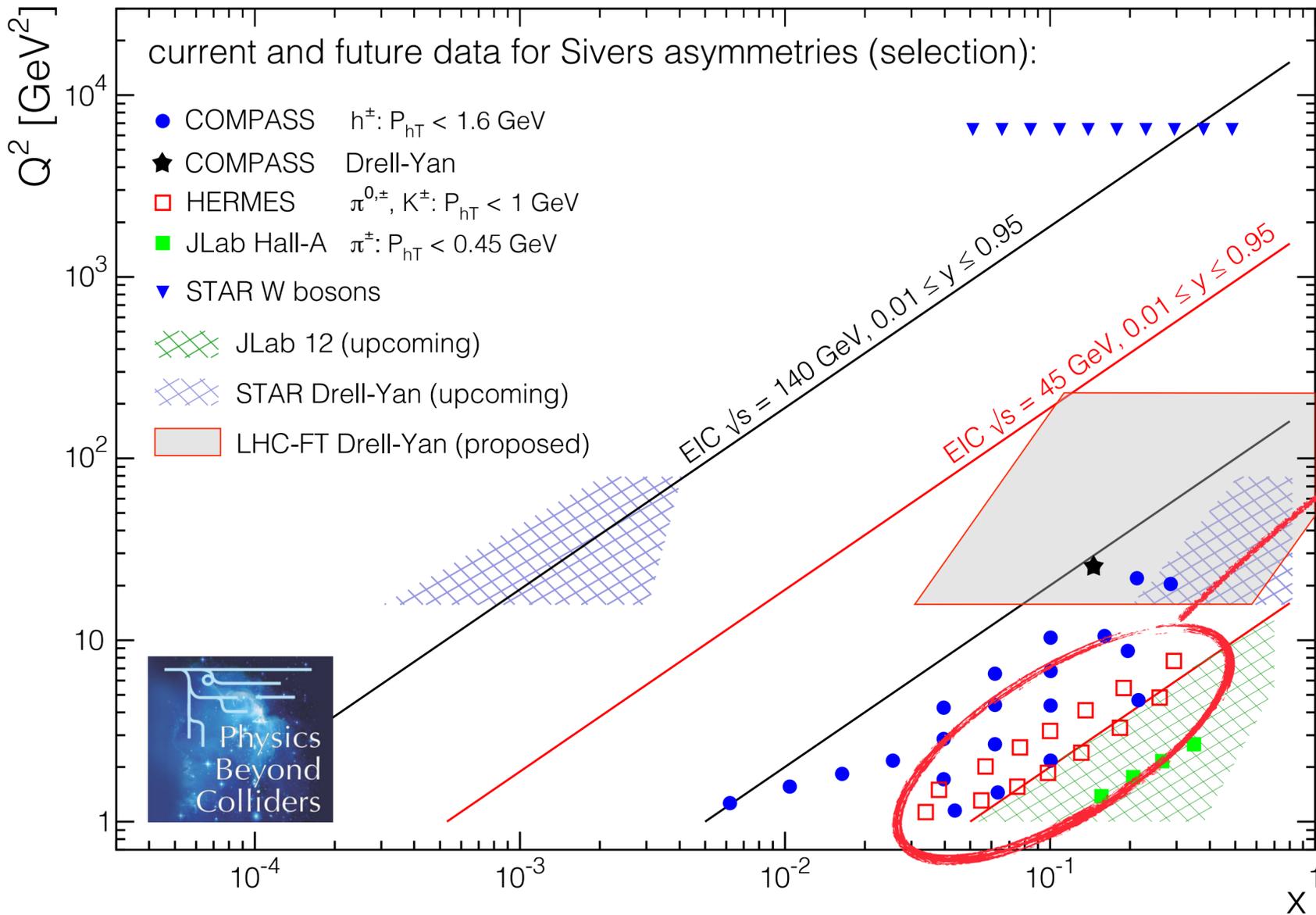


Worm-Gear II

- chiral even, couples to D_1
- evidences from
 - ^3He target at JLab
 - H target at COMPASS & HERMES



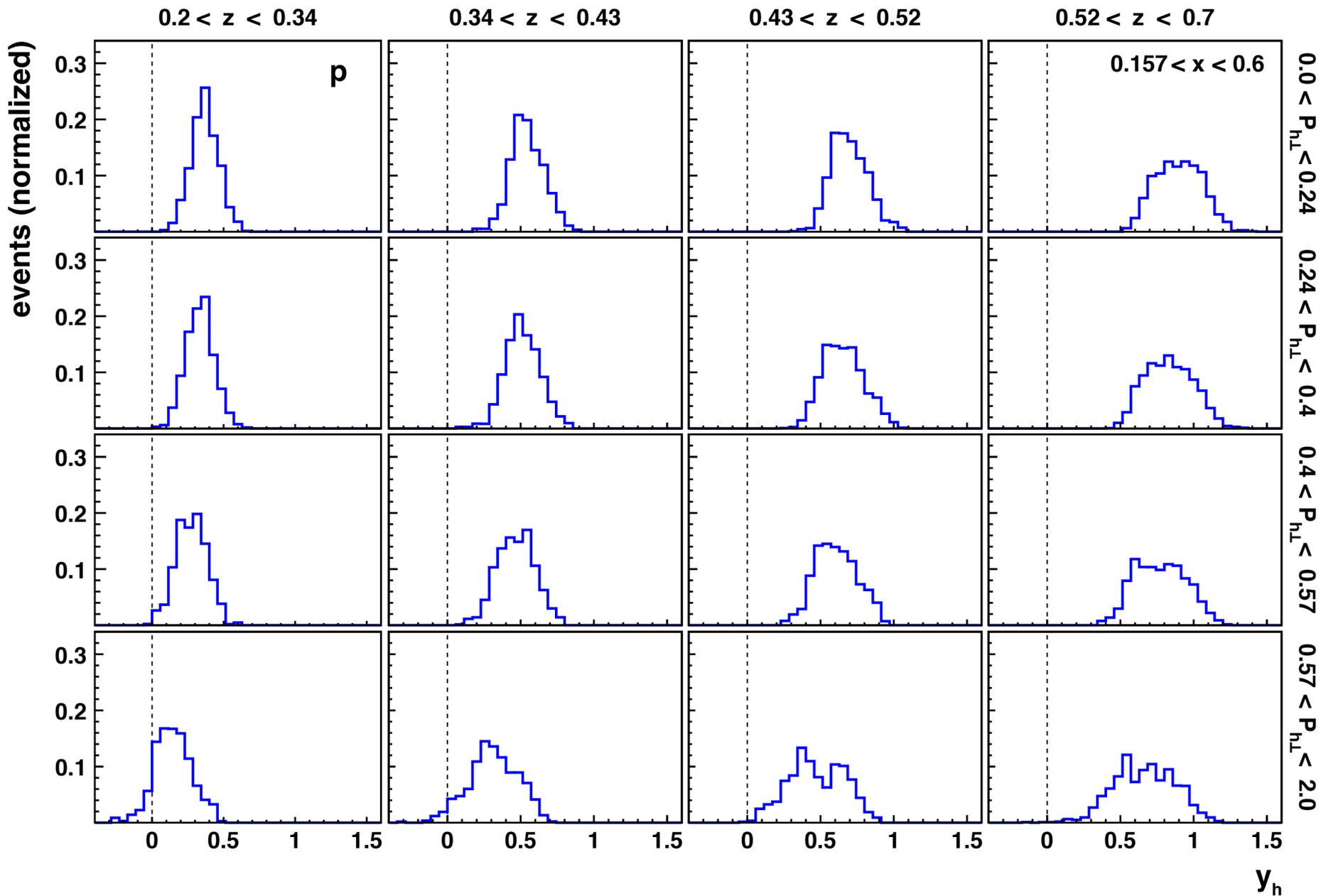
2d kinematic phase space



Scattered lepton:	$Q^2 > 1 \text{ GeV}^2$	
	$W^2 > 10 \text{ GeV}^2$	
Detected hadrons:	$0.023 < x < 0.6$	
	$0.1 < y < 0.95$	
	$2 \text{ GeV} < \mathbf{P}_h < 15 \text{ GeV}$	charged mesons
	$4 \text{ GeV} < \mathbf{P}_h < 15 \text{ GeV}$	(anti)protons
	$ \mathbf{P}_h > 2 \text{ GeV}$	neutral pions
	$P_{h\perp} < 2 \text{ GeV}$	
	$0.2 < z < 0.7$	(1.2 for the "semi-exclusive" region)

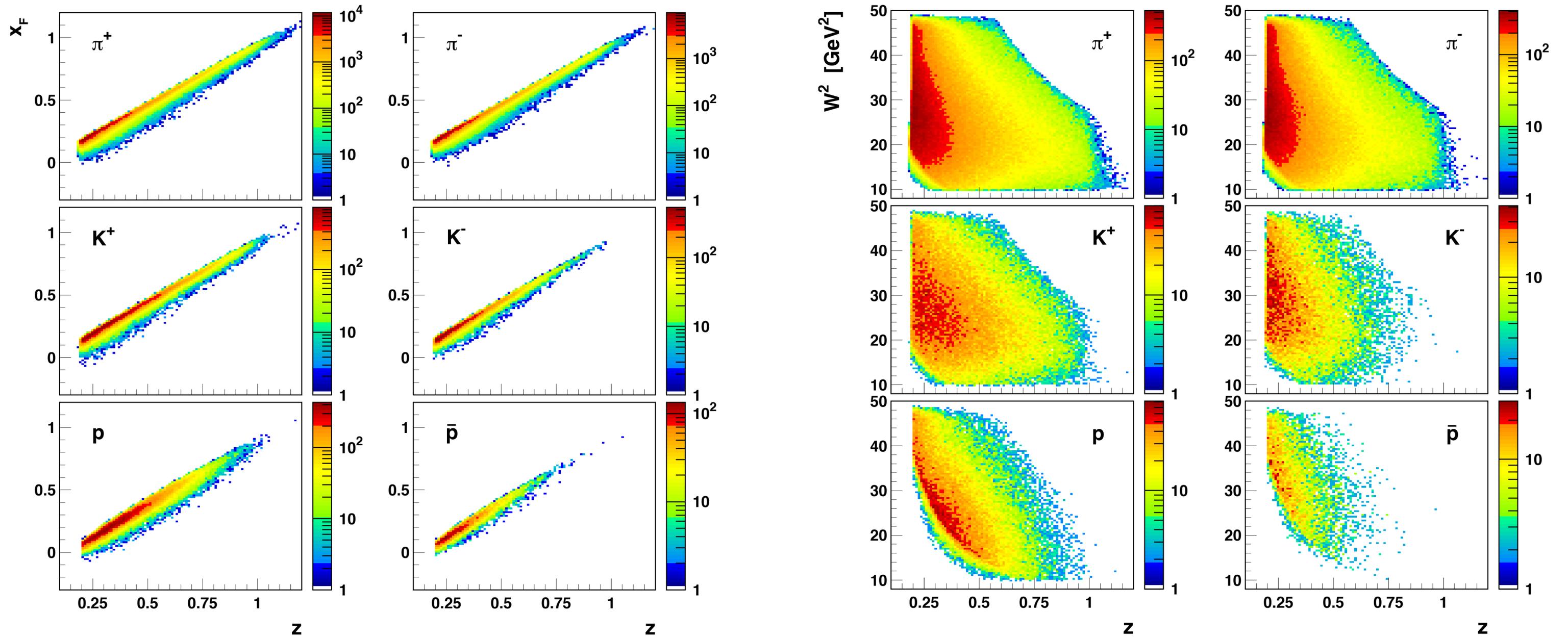
Table 3. Restrictions on selected kinematics variables. The upper limit on z of 1.2 applies only to the analysis of the z dependence.

hadron production at HERMES



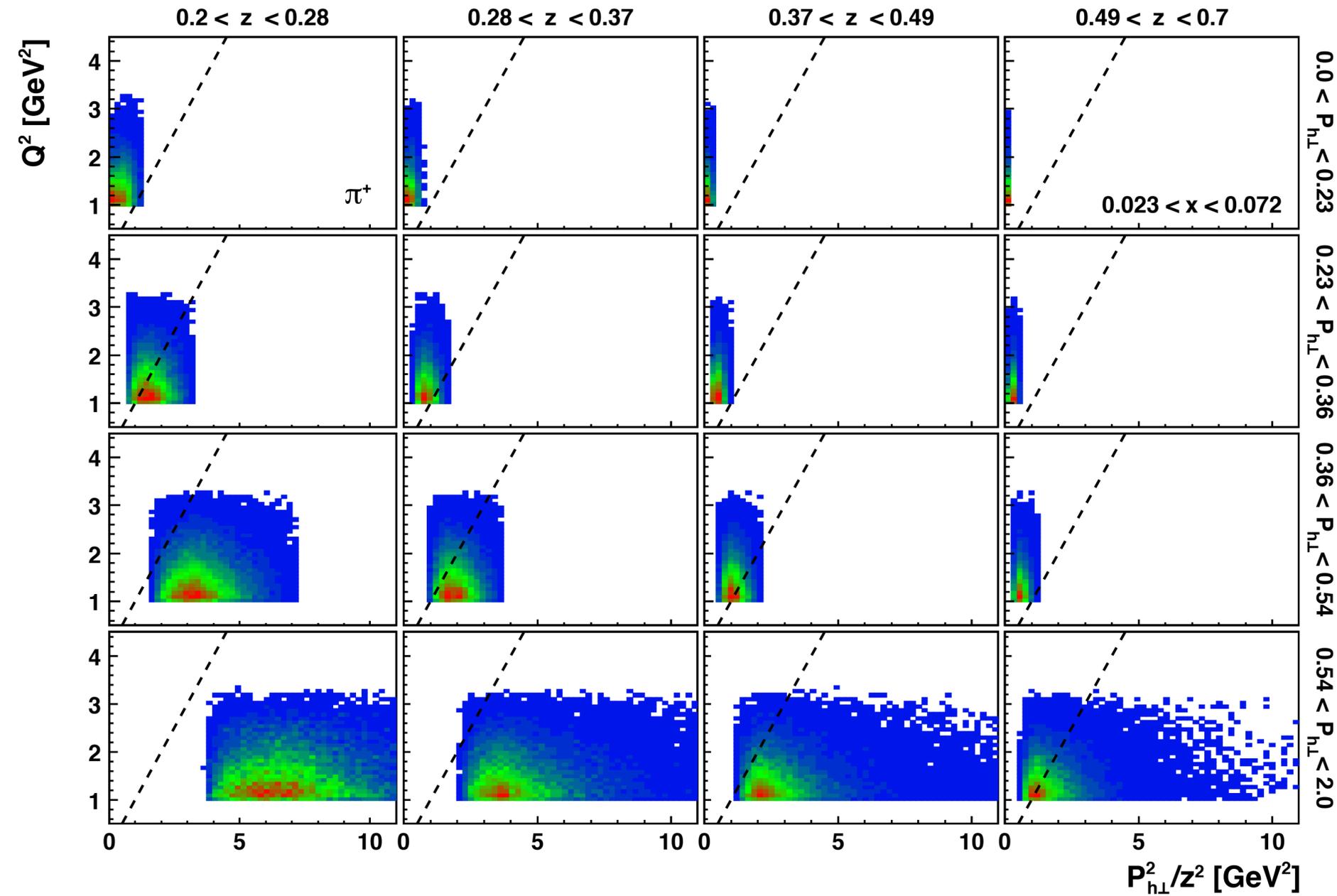
- forward-acceptance favors current fragmentation
- backward rapidity populates large- $P_{h\perp}$ region [as expected]
- rapidity distributions available for all kinematic bins (e.g., highest-x bin protons)

current vs. target fragmentation



TMD factorization: a 2-scale problem

lowest x bin

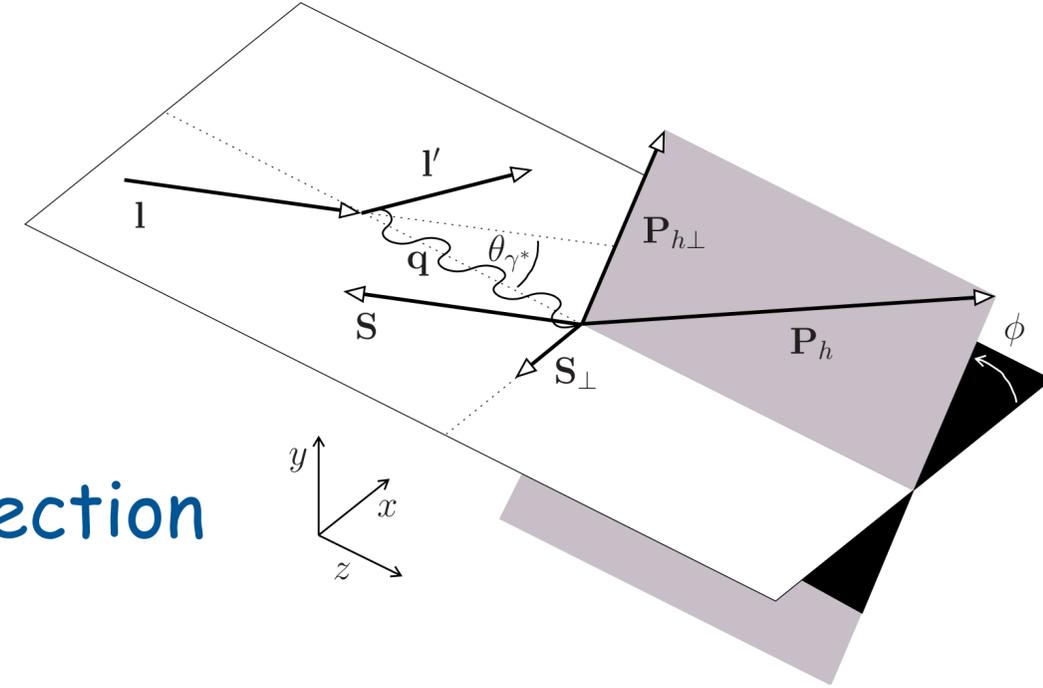


--- $Q^2 = P_{h\perp}^2/z^2$

all other x-bins included in the
Supplemental Material of
[JHEP12\(2020\)010](#)

Mixing of target polarizations

- theory done w.r.t. virtual-photon direction
- experiments use targets polarized w.r.t. lepton-beam direction



➔ mixing of longitudinal and transverse polarization effects
 [Diehl & Sapeta, EPJ C 41 (2005) 515], e.g.,

$$\begin{pmatrix} \langle \sin \phi \rangle_{UL}^l \\ \langle \sin(\phi - \phi_S) \rangle_{UT}^l \\ \langle \sin(\phi + \phi_S) \rangle_{UT}^l \end{pmatrix} = \begin{pmatrix} \cos \theta_{\gamma^*} & -\sin \theta_{\gamma^*} & -\sin \theta_{\gamma^*} \\ \frac{1}{2} \sin \theta_{\gamma^*} & \cos \theta_{\gamma^*} & 0 \\ \frac{1}{2} \sin \theta_{\gamma^*} & 0 & \cos \theta_{\gamma^*} \end{pmatrix} \begin{pmatrix} \langle \sin \phi \rangle_{UL}^q \\ \langle \sin(\phi - \phi_S) \rangle_{UT} \\ \langle \sin(\phi + \phi_S) \rangle_{UT} \end{pmatrix}$$

➔ need data on same target for both polarization orientations!

Mixing of target polarizations

- theory done w.r.t. virtual-photon direction
- experiments use targets polarized w.r.t. lepton-beam direction

➔ mixing of longitudinal and transverse polarization effects

