# Probing Nucleons and Nuclei in High Energy Collisions INT - October 8<sup>th</sup>, 2018

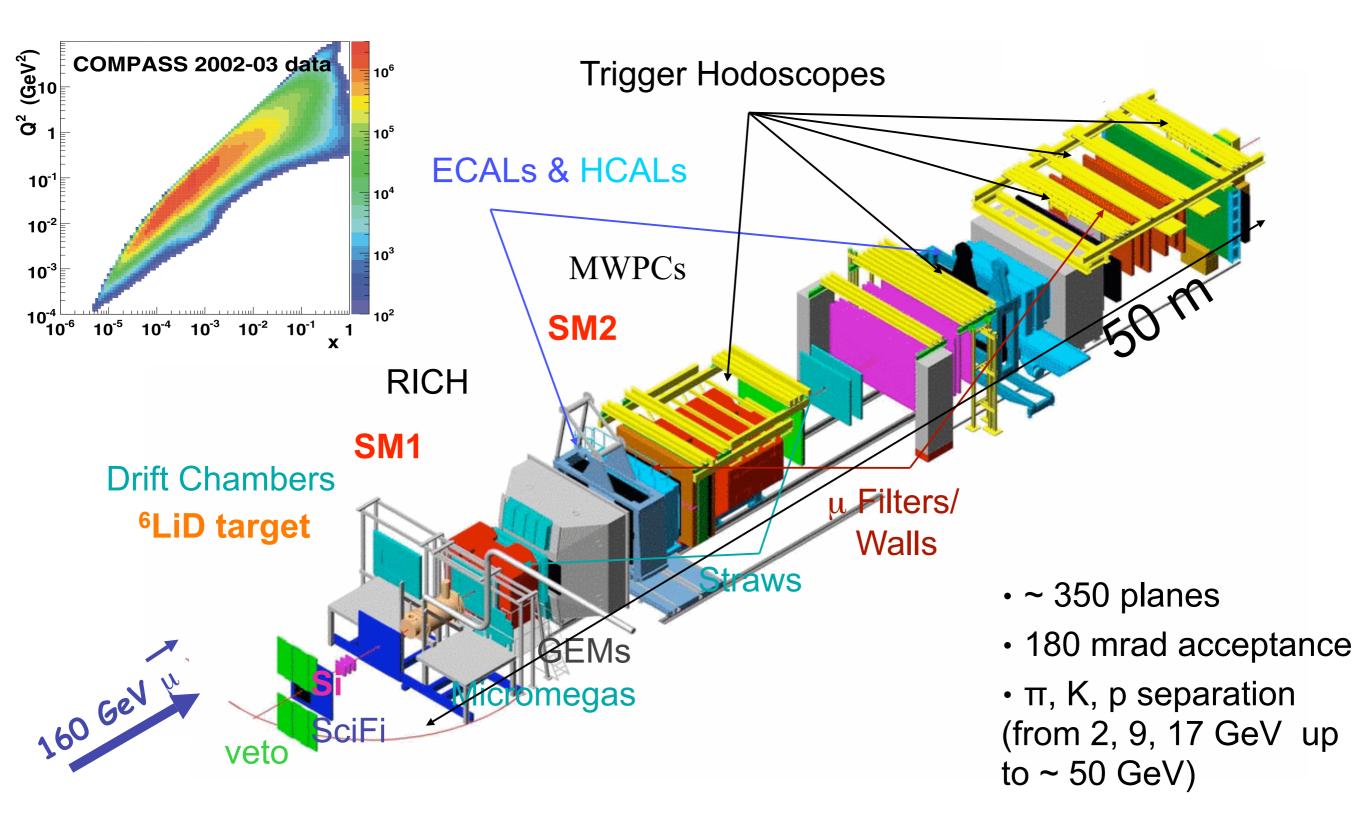
# Measurements of transverse momentum distributions in semi-inclusive DIS

- from a mainly European perspective -



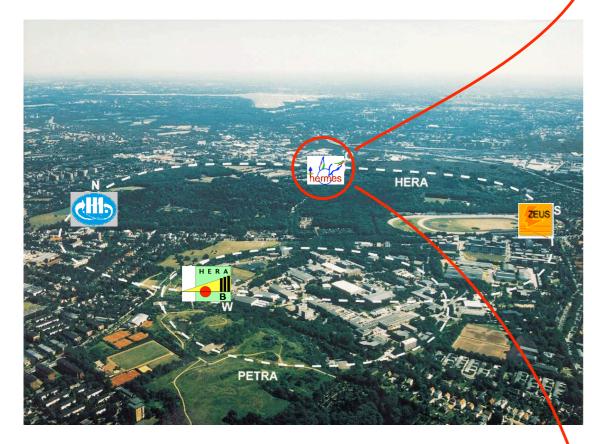


# The COMPASS experiment @ CERN



# HERMES Experiment (†2007) @ DESY

27.6 GeV polarized e<sup>+</sup>/e<sup>-</sup> beam scattered off ...



- unpolarized (H, D, He,..., Xe)
- as well as transversely (H) and longitudinally (H, D, He) polarized (pure) gas targets



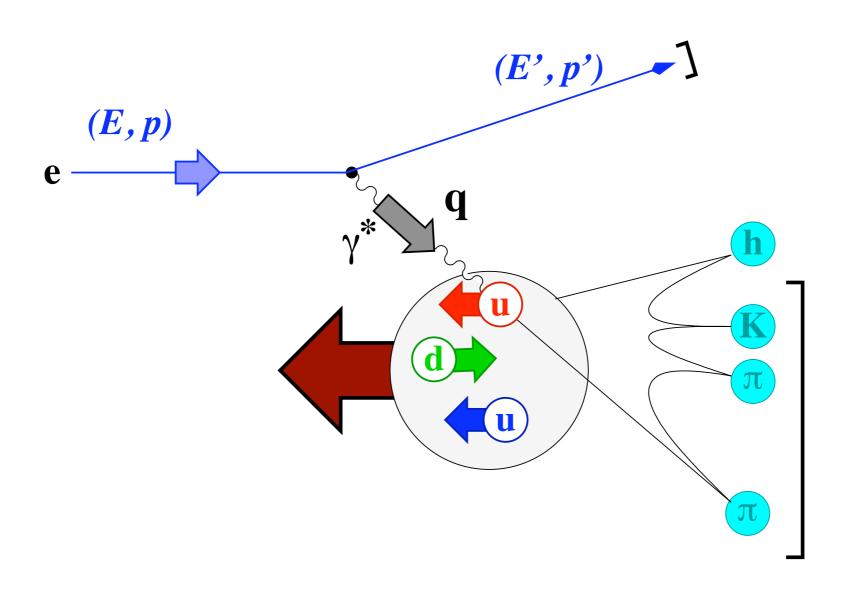
# getting polarized nucleons

- common polarized targets
  - gas targets -> pure, but lower density
  - solid (e.g. NH<sub>3</sub>) targets -> high density, but large dilution

# getting polarized nucleons

- common polarized targets
  - gas targets -> pure, but lower density
  - solid (e.g. NH3) targets -> high density, but large dilution
- statistical precision: ~  $\frac{1}{fP_BP_T}\frac{1}{\sqrt{N}}$  (f... dilution factor)
  - solid targets  $f \approx 0.2 \rightarrow$  directly scales uncertainties (as do  $P_B \& P_T$ )
  - dilution also kinematics dependent (partially unknown systematics)

# Semi-inclusive DIS



## Spin-momentum structure of the nucleon

$$\frac{1}{2}\operatorname{Tr}\left[\left(\gamma^{+} + \lambda\gamma^{+}\gamma_{5}\right)\Phi\right] = \frac{1}{2}\left[f_{1} + S^{i}\epsilon^{ij}k^{j}\frac{1}{m}f_{1T}^{\perp} + \lambda\Lambda g_{1} + \lambda S^{i}k^{i}\frac{1}{m}g_{1T}\right]$$

$$\frac{1}{2} \text{Tr} \left[ (\gamma^{+} - s^{j} i \sigma^{+j} \gamma_{5}) \Phi \right] = \frac{1}{2} \left| f_{1} + S^{i} \epsilon^{ij} k^{j} \frac{1}{m} f_{1T}^{\perp} + s^{i} \epsilon^{ij} k^{j} \frac{1}{m} h_{1}^{\perp} + s^{i} S^{i} h_{1} \right|$$

$$+ s^{i} (2k^{i}k^{j} - \mathbf{k}^{2}\delta^{ij})S^{j} \frac{1}{2m^{2}} h_{1T}^{\perp} + \Lambda s^{i}k^{i} \frac{1}{m} h_{1L}^{\perp}$$

quark pol.

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	U	$oxed{L}$	${ m T}$
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
$\Box$	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

- each TMD describes a particular spinmomentum correlation
- functions in black survive integration over transverse momentum
- functions in green box are chirally odd
- functions in red are naive T-odd

# Spin-momentum structure of the nucleon

$$\frac{1}{2}\operatorname{Tr}\left[\left(\gamma^{+} + \lambda\gamma^{+}\gamma_{5}\right)\Phi\right] = \frac{1}{2}\left[f_{1} + S^{i}\epsilon^{ij}k^{j}\frac{1}{m}f_{1T}^{\perp} + \lambda\Lambda g_{1} + \lambda S^{i}k^{i}\frac{1}{m}g_{1T}\right]$$

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## helicity

quark pol.

	$\Gamma$	${ m L}$	${ m T}$
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
T	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

# $+ s^{i} (2k^{i}k^{j} - \mathbf{k}^{2}\delta^{ij})S^{j} \frac{1}{2m^{2}} h_{1T}^{\perp} + \Lambda s^{i}k^{i} \frac{1}{m} h_{1L}^{\perp}$

# Boer-Mulders scribes a particular spin-relation

 functions in black survive integration over transverse momentum

#### Sivers

nucleon pol

transversity

pretzelosity green box are chirally odd

functions in red are naive T-odd

worm-gear

quark pol.

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	U	${ m L}$	${ m T}$
U	$D_1$		$H_1^\perp$
${ m L}$		$G_1$	$H_{1L}^{\perp}$
${ m T}$	$D_{1T}^{\perp}$	$G_{1T}^{\perp}$	$H_1 H_{1T}^{\perp}$

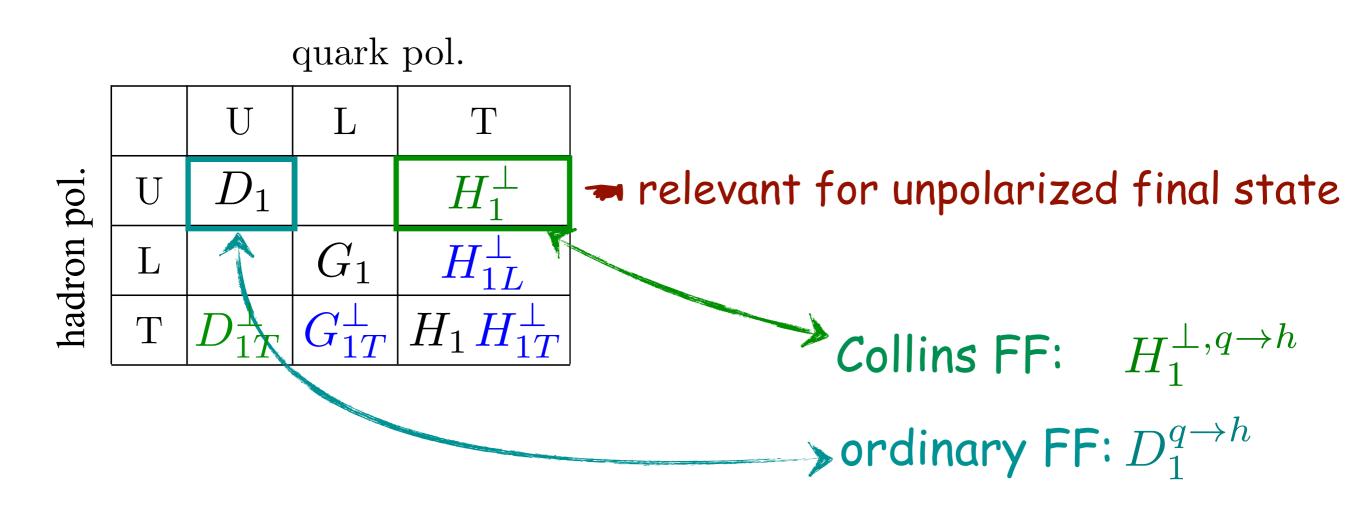
quark pol.

hadron pol.

	U	${ m L}$	${ m T}$
U	$D_1$		$H_1^{\perp}$
L		$G_1$	$H_{1L}^{\perp}$
T	$D_{1T}^{\perp}$	$G_{1T}^{\perp}$	$H_1 H_{1T}^{\perp}$

- relevant for unpolarized final state

R. Seidl, A. Vossen



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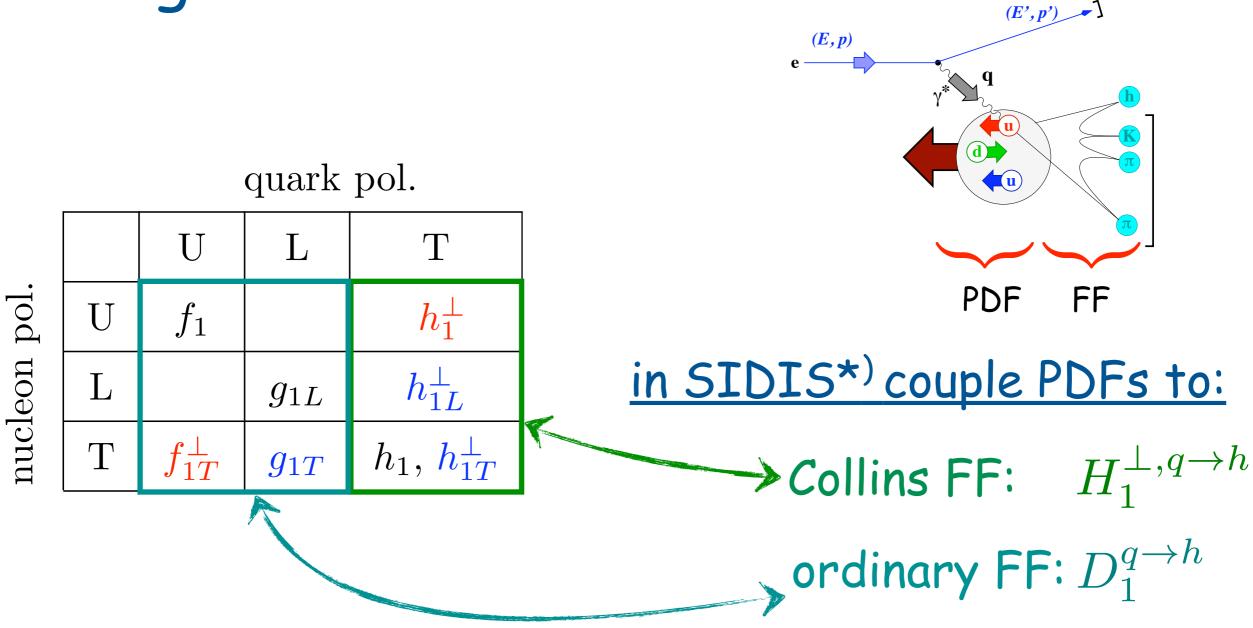
quark pol.

relevant for unpolarized final state

polarized final-state hadrons

R. Seidl, A. Vossen





## → give rise to characteristic azimuthal dependences

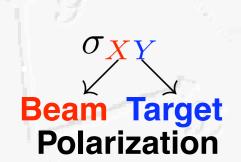
\*) semi-inclusive DIS with unpolarized final state

# one-hadron production (ep-ehX)

$$d\sigma = d\sigma_{UU}^0 + \cos 2\phi \, d\sigma_{UU}^1 + \frac{1}{Q}\cos\phi \, d\sigma_{UU}^2 + \lambda_e \frac{1}{Q}\sin\phi \, d\sigma_{LU}^3$$

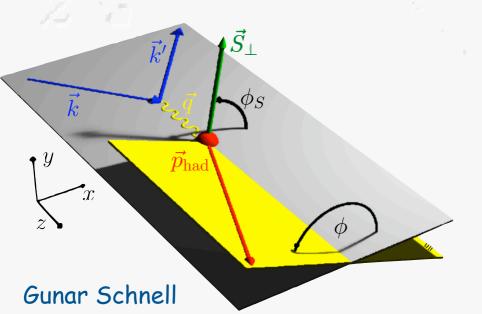
$$+S_L \left\{ \sin 2\phi \, d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi \, d\sigma_{UL}^5 + \lambda_e \left[ d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi \, d\sigma_{LL}^7 \right] \right\}$$

$$+S_T \left\{ \sin(\phi - \phi_S) d\sigma_{UT}^8 + \sin(\phi + \phi_S) d\sigma_{UT}^9 + \sin(3\phi - \phi_S) d\sigma_{UT}^{10} \right\}$$



$$+\frac{1}{Q}\left(\sin(2\phi-\phi_S)\ d\sigma_{UT}^{11} + \sin\phi_S\ d\sigma_{UT}^{12}\right)$$

$$+\lambda_{e} \left[ \cos(\phi - \phi_{S}) \, d\sigma_{LT}^{13} + \frac{1}{Q} \left( \cos\phi_{S} \, d\sigma_{LT}^{14} + \cos(2\phi - \phi_{S}) \, d\sigma_{LT}^{15} \right) \right] \right\}$$



Mulders and Tangermann, Nucl. Phys. B 461 (1996) 197

Boer and Mulders, Phys. Rev. D 57 (1998) 5780

Bacchetta et al., Phys. Lett. B 595 (2004) 309

Bacchetta et al., JHEP 0702 (2007) 093

"Trento Conventions", Phys. Rev. D 70 (2004) 117504

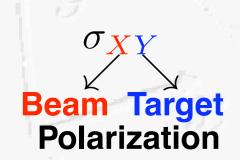
INT-18-3, Seattle

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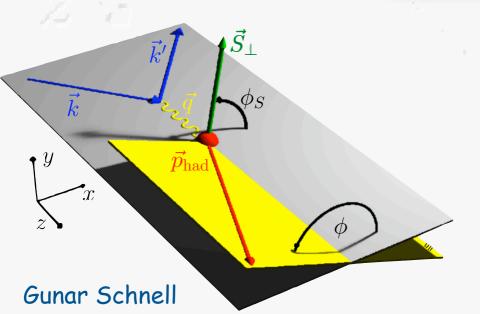
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$$+\frac{1}{Q}\left(\sin(2\phi-\phi_S)\ d\sigma_{UT}^{11} + \sin\phi_S\ d\sigma_{UT}^{12}\right)$$

$$+\lambda_{e} \left[ \cos(\phi - \phi_{S}) \, d\sigma_{LT}^{13} + \frac{1}{Q} \left( \cos\phi_{S} \, d\sigma_{LT}^{14} + \cos(2\phi - \phi_{S}) \, d\sigma_{LT}^{15} \right) \right] \right\}$$



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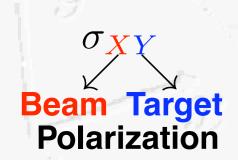
INT-18-3, Seattle

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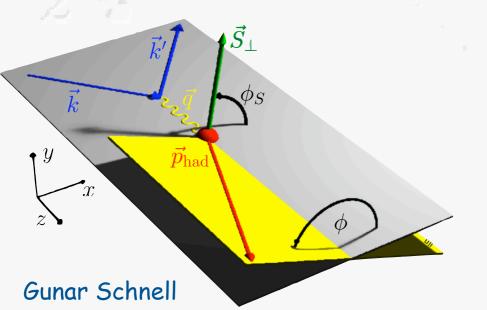
$$+S_L \left\{ \frac{\sin 2\phi \, d\sigma_{UL}^4}{Q} + \frac{1}{Q} \sin \phi \, d\sigma_{UL}^5 + \lambda_e \left[ \frac{d\sigma_{LL}^6}{Q} + \frac{1}{Q} \cos \phi \, d\sigma_{LL}^7 \right] \right\}$$

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# ... possible measurements

$$\frac{d^{5}\sigma}{dxdydzd\phi_{h}dP_{h\perp}^{2}} \propto \left(1 + \frac{\gamma^{2}}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\} 
+ \sqrt{2\epsilon(1 - \epsilon)} F_{UU}^{\cos\phi_{h}} \cos\phi_{h} + \epsilon F_{UU}^{\cos2\phi_{h}} \cos2\phi_{h} \right\}$$

... possible measurements

normalize to inclusive DIS cross section

$$\frac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$$

$$+\sqrt{2\epsilon(1-\epsilon)}F_{UU}^{\cos\phi_h}\cos\phi_h+\epsilon F_{UU}^{\cos2\phi_h}\cos2\phi_h$$

possible measurements

normalize to inclusive DIS cross section

 $\frac{d^2\sigma^{\rm incl.DIS}}{dxdy} \propto F_T + \epsilon F_L$ 

$$\rightarrow$$
  $\frac{d^4}{d^4}$ 

$$\frac{d^4 \mathcal{M}^h(x, y, z, P_{h\perp}^2)}{dx dy dz dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \frac{F_{UU,T} + \epsilon F_{UU,L}}{F_T + \epsilon F_L}$$

$$\frac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$$

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$$\frac{d^2\sigma^{
m incl.DIS}}{dxdy}$$
  $\propto$   $F_T + \epsilon F_L$ 

$$\approx \frac{\sum_{q} e_{q}^{2} f_{1}^{q}(x, p_{T}^{2}) \otimes D_{1}^{q \to h}(z, K_{T}^{2})}{\sum_{q} e_{q}^{2} f_{1}^{q}(x)}$$

$$\frac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto$$

$$\frac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$$

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possible measurements

normalize to inclusive DIS cross section

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$$\frac{d^2\sigma^{\rm incl.DIS}}{dxdy} \propto F_T + \epsilon F_L$$

$$\approx \frac{\sum_{q} e_{q}^{2} f_{1}^{q}(x, p_{T}^{2}) \otimes D_{1}^{q \to h}(z, K_{T}^{2})}{\sum_{q} e_{q}^{2} f_{1}^{q}(x)}$$

$$rac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto$$

$$\frac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$$

$$+\sqrt{2\epsilon(1-\epsilon)}F_{UU}^{\cos\phi_h}\cos\phi_h+\epsilon F_{UU}^{\cos2\phi_h}\cos2\phi_h$$

#### moments:

normalize to azimuthindependent cross-section

# ... possible measurements

normalize to inclusive DIS cross section

$$rac{d^2 \sigma^{
m incl.DIS}}{dxdy} \propto F_T + \epsilon F_L$$

$$\rightarrow \frac{d^4 \mathcal{M}^h(x, y, z, P_{h\perp}^2)}{dx dy dz dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \frac{F_{UU,T} + \epsilon F_{U,L}}{F_T + \epsilon F_L}$$

$$\approx \frac{\sum_{q} e_{q}^{2} f_{1}^{q}(x, p_{T}^{2}) \otimes D_{1}^{q \to h}(z, K_{T}^{2})}{\sum_{q} e_{q}^{2} f_{1}^{q}(x)}$$

$$\frac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$$

$$+\sqrt{2\epsilon(1-\epsilon)}F_{UU}^{\cos\phi_h}\cos\phi_h + \epsilon F_{UU}^{\cos2\phi_h}\cos2\phi_h\}$$

$$+2\langle\cos2\phi\rangle_{UU} \equiv 2\frac{\int d\phi_h\cos2\phi\,d\sigma}{\int d\phi_hd\sigma} = \frac{\epsilon F_{UU}^{\cos2\phi}}{F_{UUT} + \epsilon F_{UUL}}$$

#### moments:

normalize to azimuthindependent cross-section

# ... possible measurements

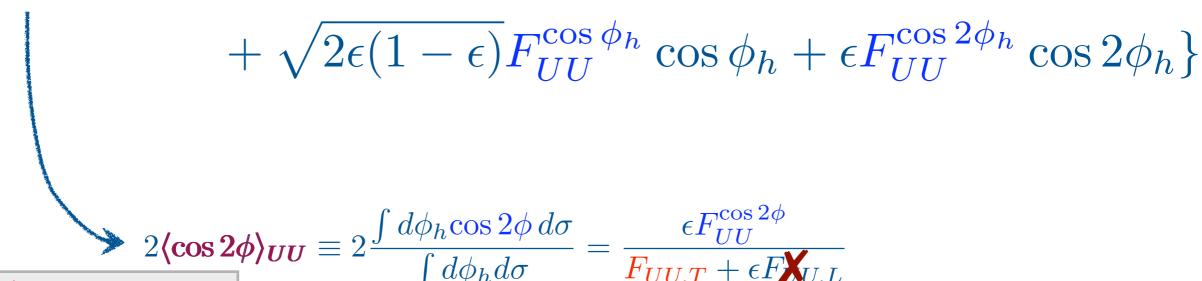
normalize to inclusive DIS cross section

$$rac{d^2 \sigma^{
m incl.DIS}}{dxdy} \propto F_T + \epsilon F_L$$

$$\rightarrow \frac{d^4 \mathcal{M}^h(x, y, z, P_{h\perp}^2)}{dx dy dz dP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \frac{F_{UU,T} + \epsilon F_{U,L}}{F_T + \epsilon F_L}$$

$$\approx \frac{\sum_{q} e_q^2 f_1^q(x, p_T^2) \otimes D_1^{q \to h}(z, K_T^2)}{\sum_{q} e_q^2 f_1^q(x)}$$

$$\frac{d^5\sigma}{dxdydzd\phi_hdP_{h\perp}^2} \propto \left(1 + \frac{\gamma^2}{2x}\right) \left\{F_{UU,T} + \epsilon F_{UU,L}\right\}$$



#### moments:

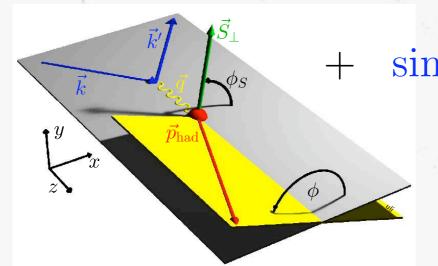
normalize to azimuthindependent cross-section

$$\approx \epsilon \frac{\sum_{q} e_{q}^{2} h_{1}^{\perp,q}(x, p_{T}^{2}) \otimes_{BM} H_{1}^{\perp,q \to h}(z, K_{T}^{2})}{\sum_{q} e_{q}^{2} f_{1}^{q}(x, p_{T}^{2}) \otimes D_{1}^{q \to h}(z, K_{T}^{2})}$$

# ... azimuthal spin asymmetries

$$A_{UT}(\phi, \phi_S) = \frac{1}{\langle |S_{\perp}| \rangle} \frac{N_h^{\uparrow}(\phi, \phi_S) - N_h^{\downarrow}(\phi, \phi_S)}{N_h^{\uparrow}(\phi, \phi_S) + N_h^{\downarrow}(\phi, \phi_S)}$$

$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 \mathcal{I} \left[ \frac{k_T \hat{P}_{h\perp}}{M_h} h_1^q(x, p_T^2) H_1^{\perp, q}(z, k_T^2) \right]$$



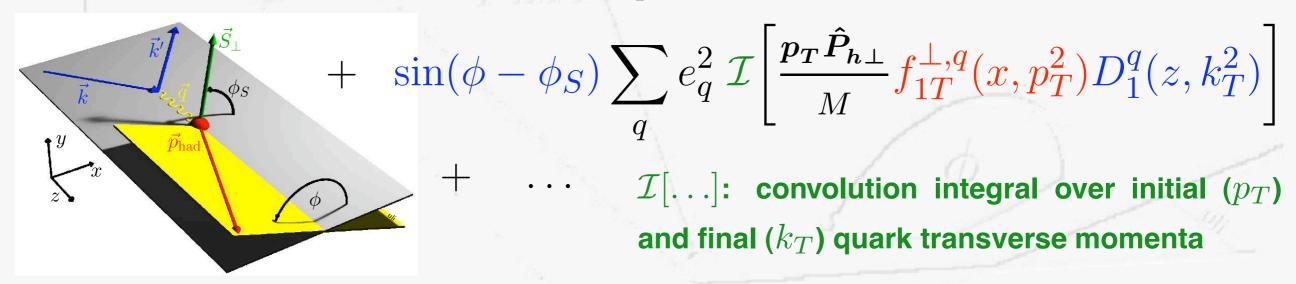
+ 
$$\sin(\phi - \phi_S) \sum_{q} e_q^2 \mathcal{I} \left[ \frac{p_T \hat{P}_{h\perp}}{M} f_{1T}^{\perp,q}(x, p_T^2) D_1^q(z, k_T^2) \right]$$

 $\mathcal{I}[\ldots]$ : convolution integral over initial  $(p_T)$  and final  $(k_T)$  quark transverse momenta

# ... azimuthal spin asymmetries

$$A_{UT}(\phi, \phi_S) = \frac{1}{\langle |S_{\perp}| \rangle} \frac{N_h^{\uparrow}(\phi, \phi_S) - N_h^{\downarrow}(\phi, \phi_S)}{N_h^{\uparrow}(\phi, \phi_S) + N_h^{\downarrow}(\phi, \phi_S)}$$

$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 \mathcal{I} \left[ \frac{k_T \hat{P}_{h\perp}}{M_h} h_1^q(x, p_T^2) H_1^{\perp, q}(z, k_T^2) \right]$$



fit azimuthal modulations, e.g., using maximum-likelihood method

$$PDF(2\langle\sin(\phi\pm\phi_S)\rangle_{UT},\ldots,\phi,\phi_S) = \frac{1}{2}\{1 + P_T(2\langle\sin(\phi\pm\phi_S)\rangle_{UT}\sin(\phi\pm\phi_S) + \ldots)\}$$

# "Qual der Wahl"

- SIDIS structure functions come with various kinematic prefactors
  - include in definition of asymmetries ("cross-section asym.") M.L.  $pdf \propto [1 + \mathcal{A}^{\sin(\phi + \phi_s)}(x, y, z, P_{h\perp}) + \dots]$
  - factor out from asymmetries ("structure-fct. asym.")

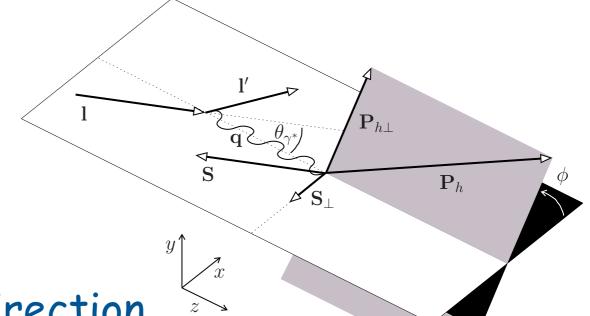
M.L. pdf 
$$\propto [1 + D(y)A^{\sin(\phi + \phi_s)}(x, y, z, P_{h\perp}) + \dots]$$

# "Qual der Wahl"

- SIDIS structure functions come with various kinematic prefactors
  - include in definition of asymmetries ("cross-section asym.") M.L.  $pdf \propto [1 + \mathcal{A}^{\sin(\phi + \phi_s)}(x, y, z, P_{h\perp}) + \dots]$
  - factor out from asymmetries ("structure-fct. asym.")

    M.L. pdf  $\propto [1 + D(y)A^{\sin(\phi+\phi_s)}(x,y,z,P_{h\perp}) + \dots]$
- latter facilitates comparisons between experiments and simplifies kinematic dependences by removing known dependences
  - but what about twist suppression, also factor out?
  - and what about other kinematically suppressed contributions?

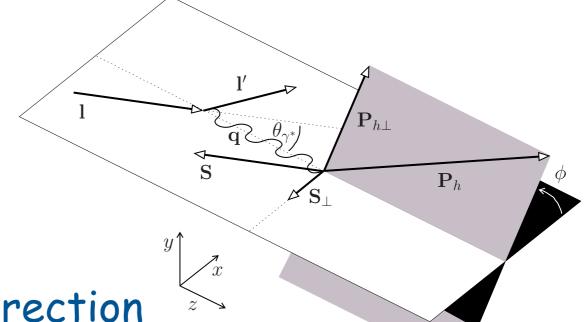
# ... other complications



- theory done w.r.t. virtual-photon direction
- experiments use targets polarized w.r.t. lepton-beam direction

Gunar Schnell 13 INT-18-3, Seattle

# ... other complications

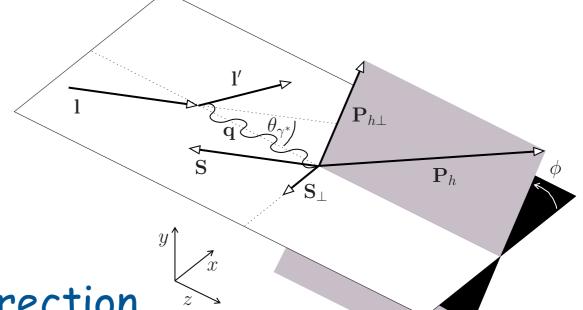


- theory done w.r.t. virtual-photon direction
- experiments use targets polarized w.r.t. lepton-beam direction
- → mixing of longitudinal and transverse polarization effects
  [Diehl & Sapeta, EPJ C 41 (2005) 515], e.g.,

$$\begin{pmatrix}
\left\langle \sin \phi \right\rangle_{UL}^{\mathsf{I}} \\
\left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^{\mathsf{I}} \\
\left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^{\mathsf{I}}
\end{pmatrix} = \begin{pmatrix}
\cos \theta_{\gamma^*} & -\sin \theta_{\gamma^*} & -\sin \theta_{\gamma^*} \\
\frac{1}{2} \sin \theta_{\gamma^*} & \cos \theta_{\gamma^*} & 0 \\
\frac{1}{2} \sin \theta_{\gamma^*} & 0 & \cos \theta_{\gamma^*}
\end{pmatrix} \begin{pmatrix}
\left\langle \sin \phi \right\rangle_{UL}^{\mathsf{q}} \\
\left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^{\mathsf{U}} \\
\left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^{\mathsf{U}}
\end{pmatrix}$$

( $\cos heta_{\gamma^*} \simeq 1$  ,  $\sin heta_{\gamma^*}$  up to 15% at HERMES energies)

# ... other complications



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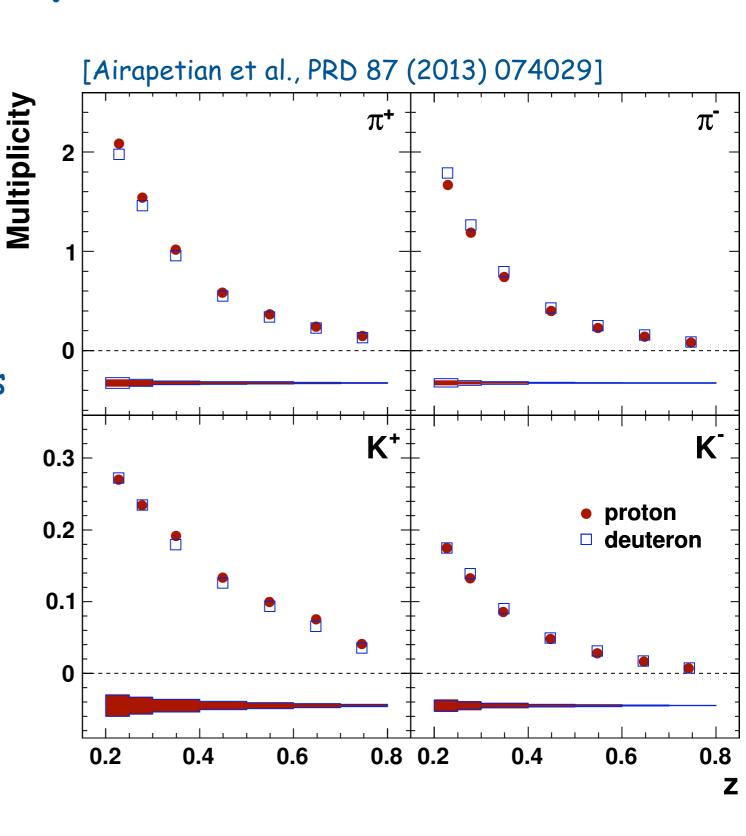
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\end{pmatrix} \begin{pmatrix}
\left\langle \sin \phi \right\rangle_{UL}^{\mathsf{q}} \\
\left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^{\mathsf{U}} \\
\left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^{\mathsf{U}}
\end{pmatrix}$$

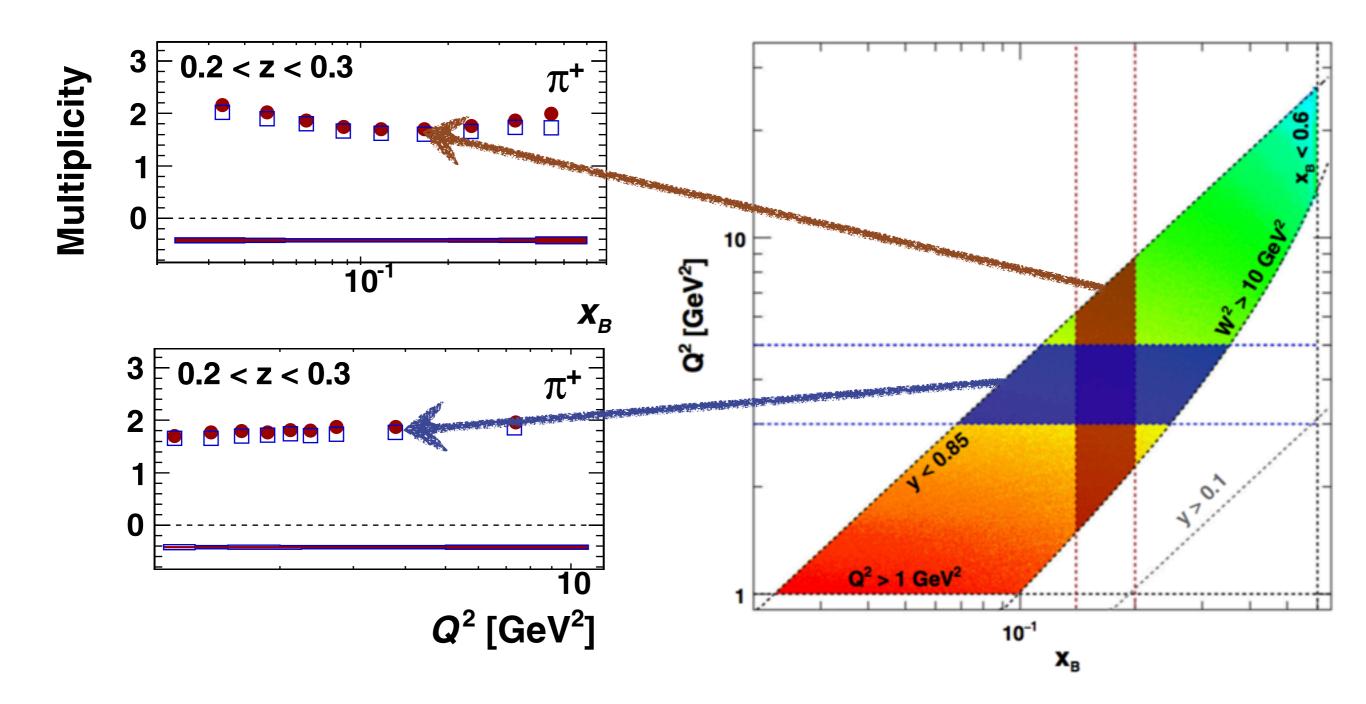
need data on same target for both polarization orientations!

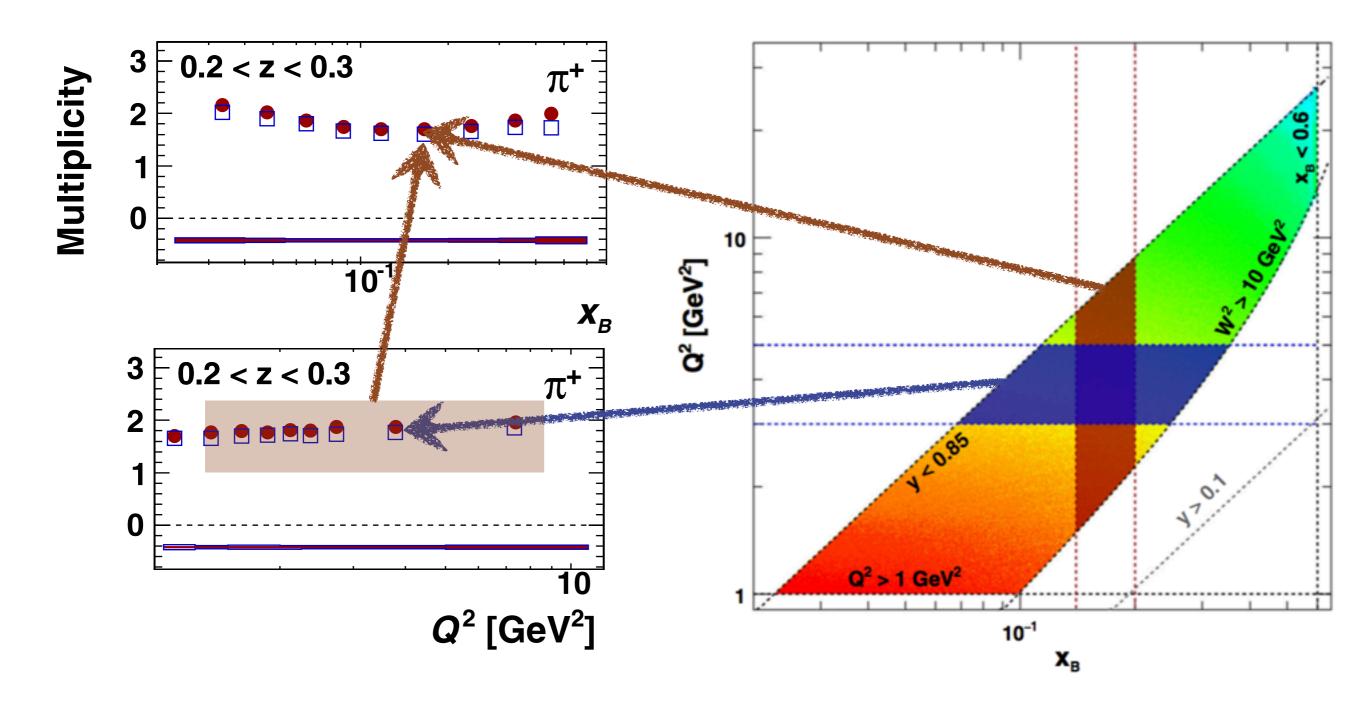
# ... results ...

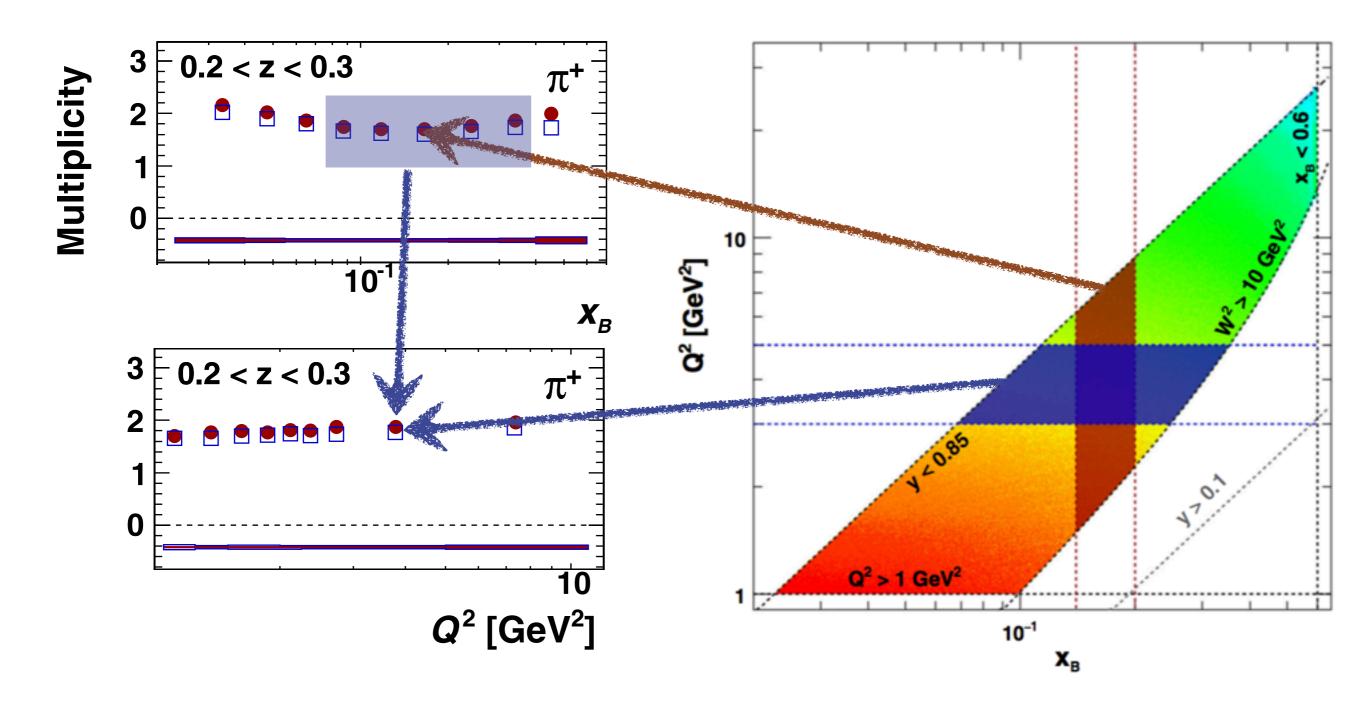
# multiplicities @ HERMES

- extensive data set on pure proton and deuteron targets for identified charged mesons
  - access to flavor dependence of fragmentation through different mesons and targets
- input to fragmentation function analyses
- extracted in a multi-dimensional unfolding procedure:
  - $\bullet$  (x, z,  $P_{h\perp}$ )
  - $\bullet$  (Q<sup>2</sup>, z, P<sub>h</sub>)

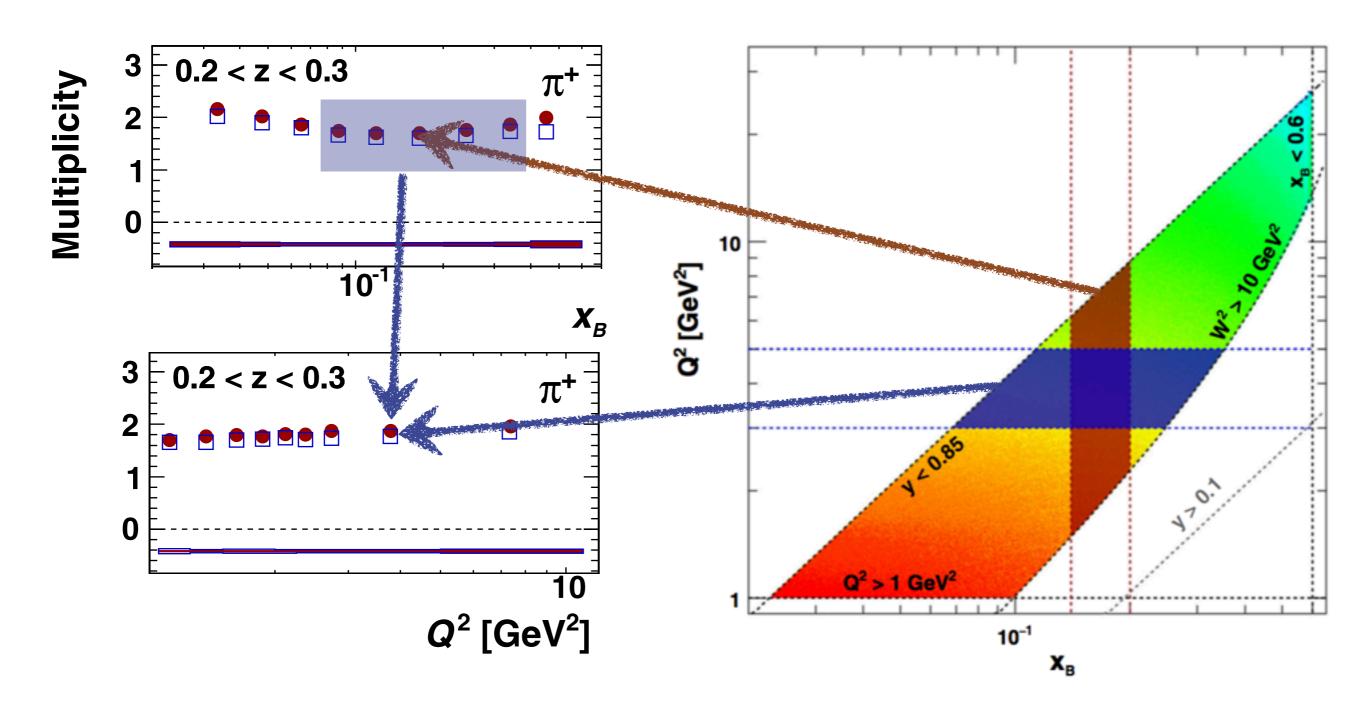




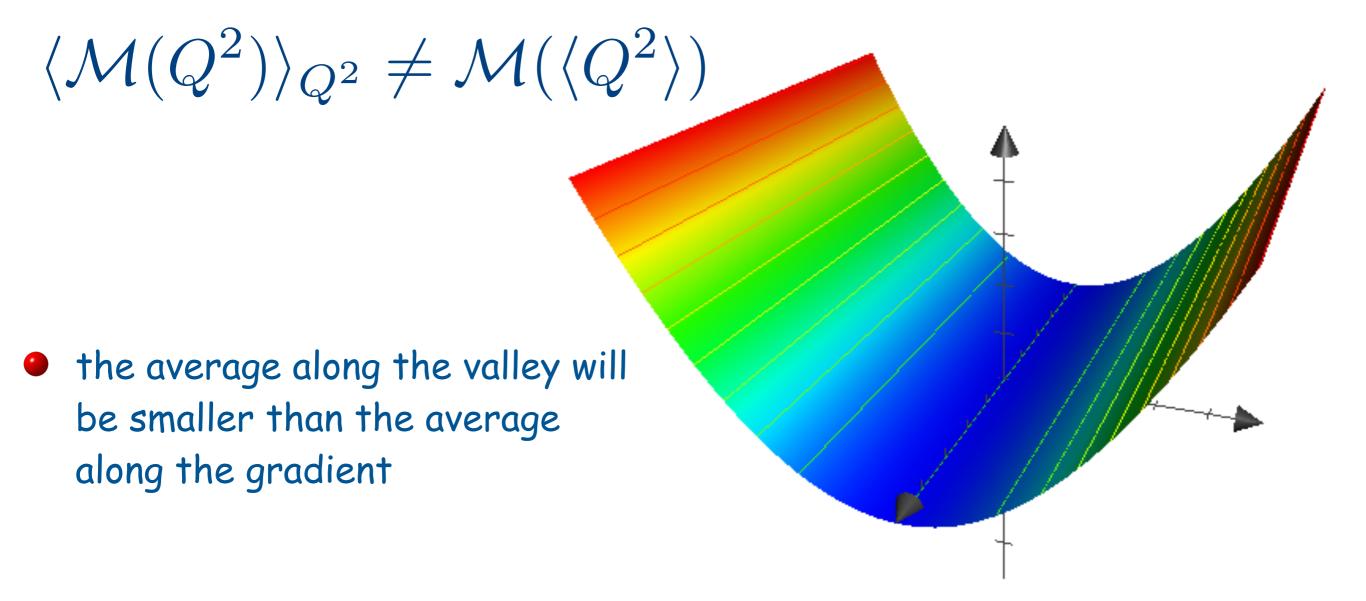


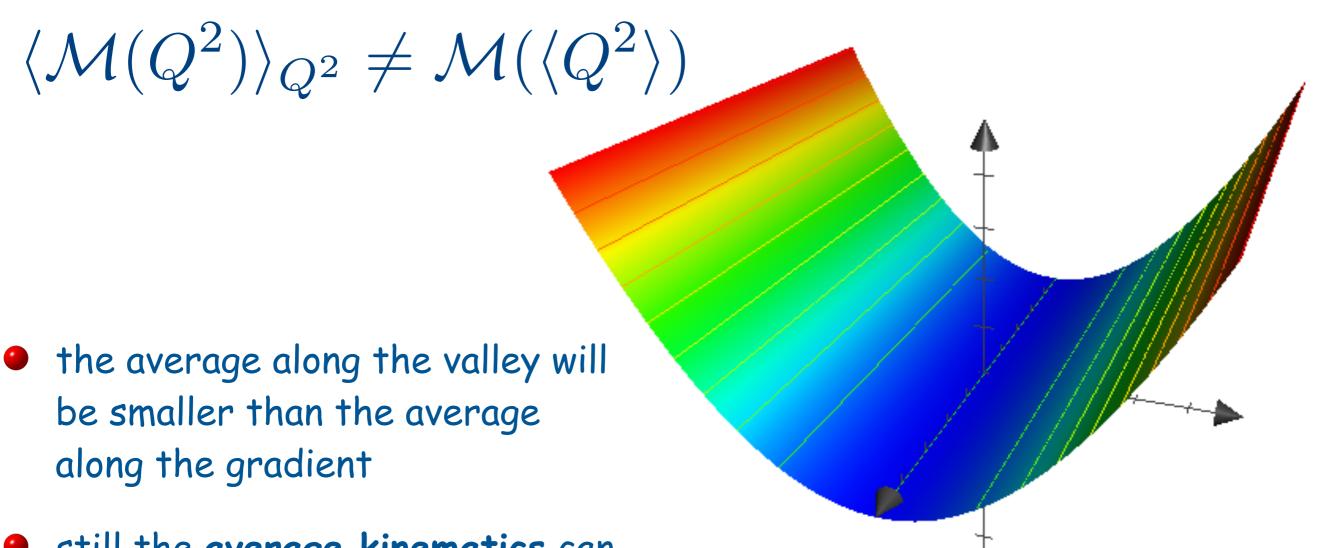




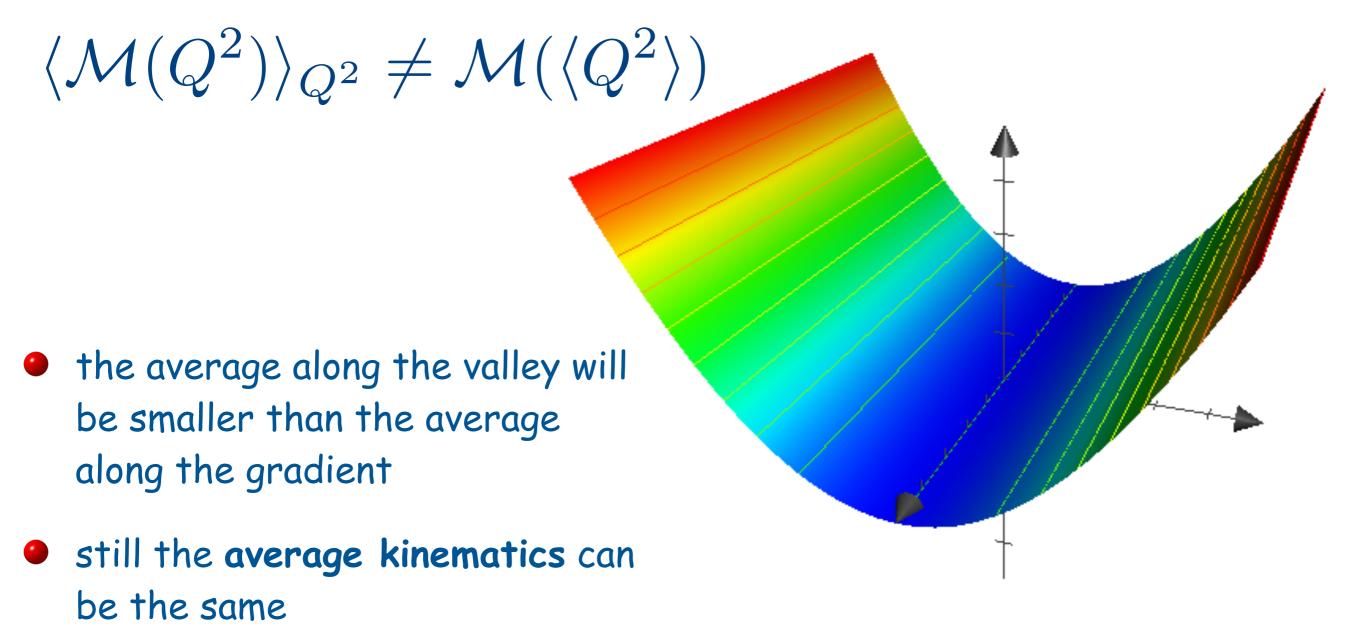


 even though having similar average kinematics, multiplicities in the two projections are different





 still the average kinematics can be the same

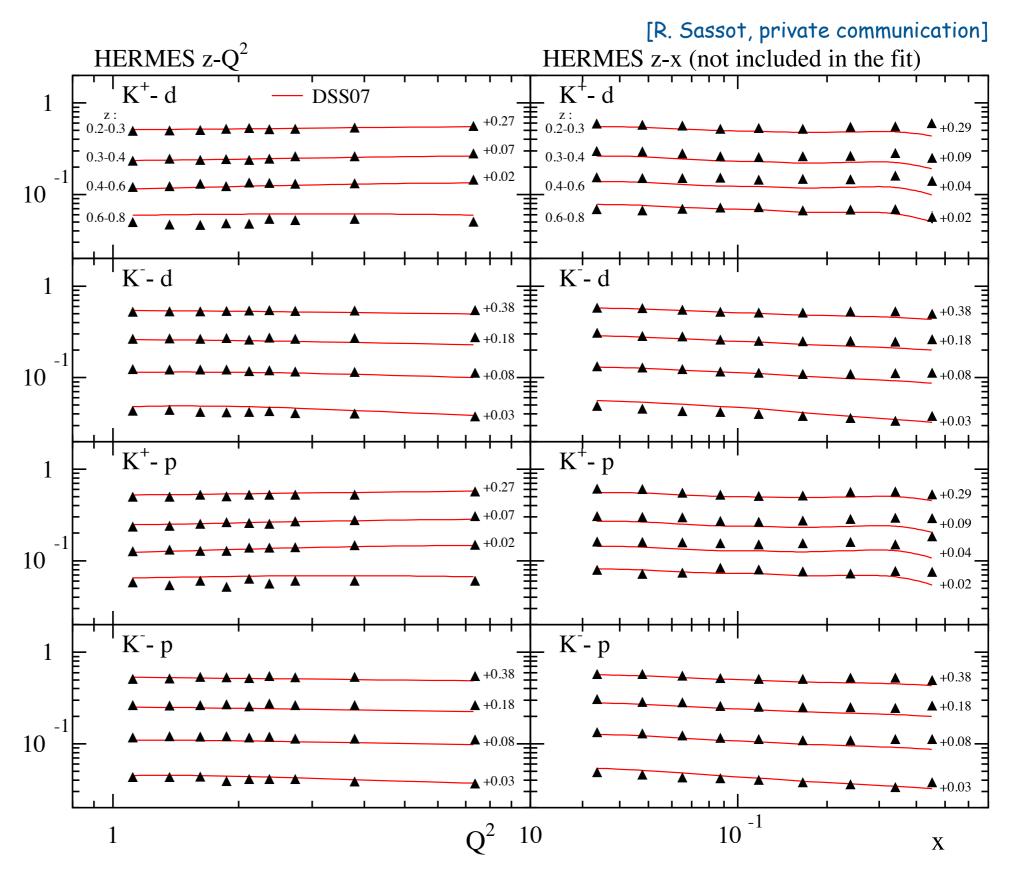


take-away messages: (when told so) integrate your cross section over the kinematic ranges dictated by the experiment (e.g., do not simply evaluate it at the average kinematics)

To experiments: fully differential analyses!

#### integrating vs. using average kinematics

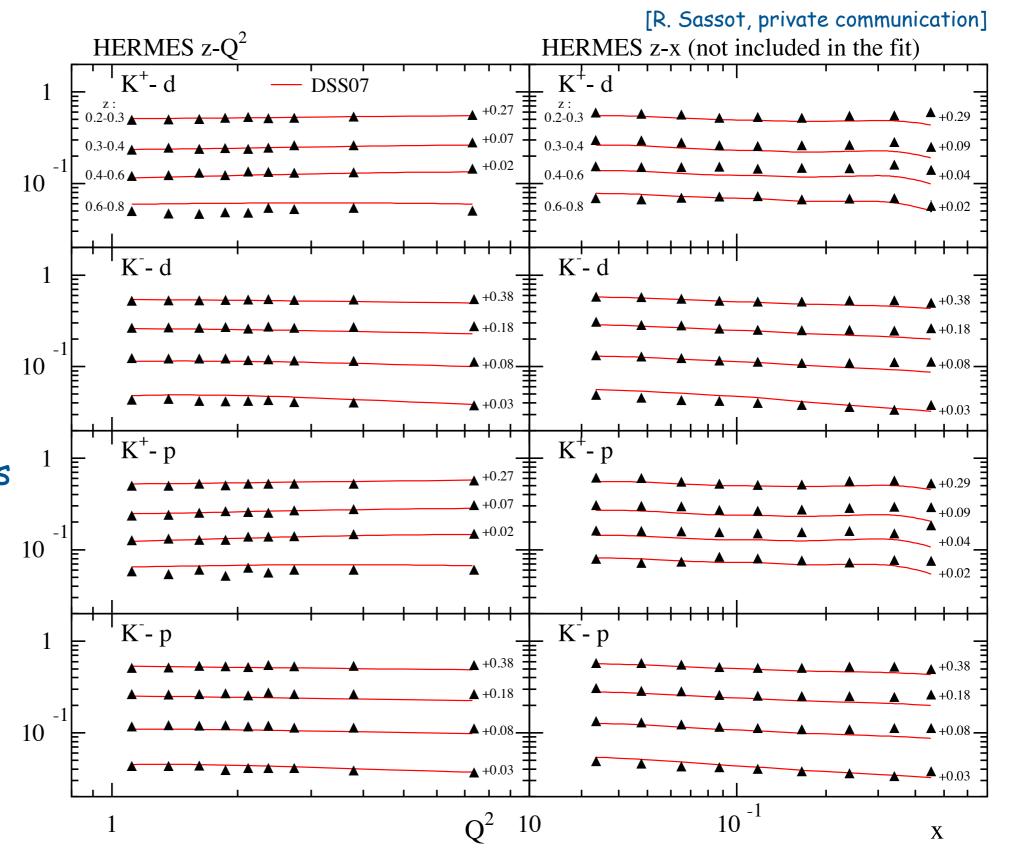
(by now old)
 DSS07 FF fit to
 z-Q² projection



#### integrating vs. using average kinematics

(by now old)
 DSS07 FF fit to
 z-Q² projection

z-x "prediction"
reasonable well
when using
integration over
phase-space limits
(red lines)

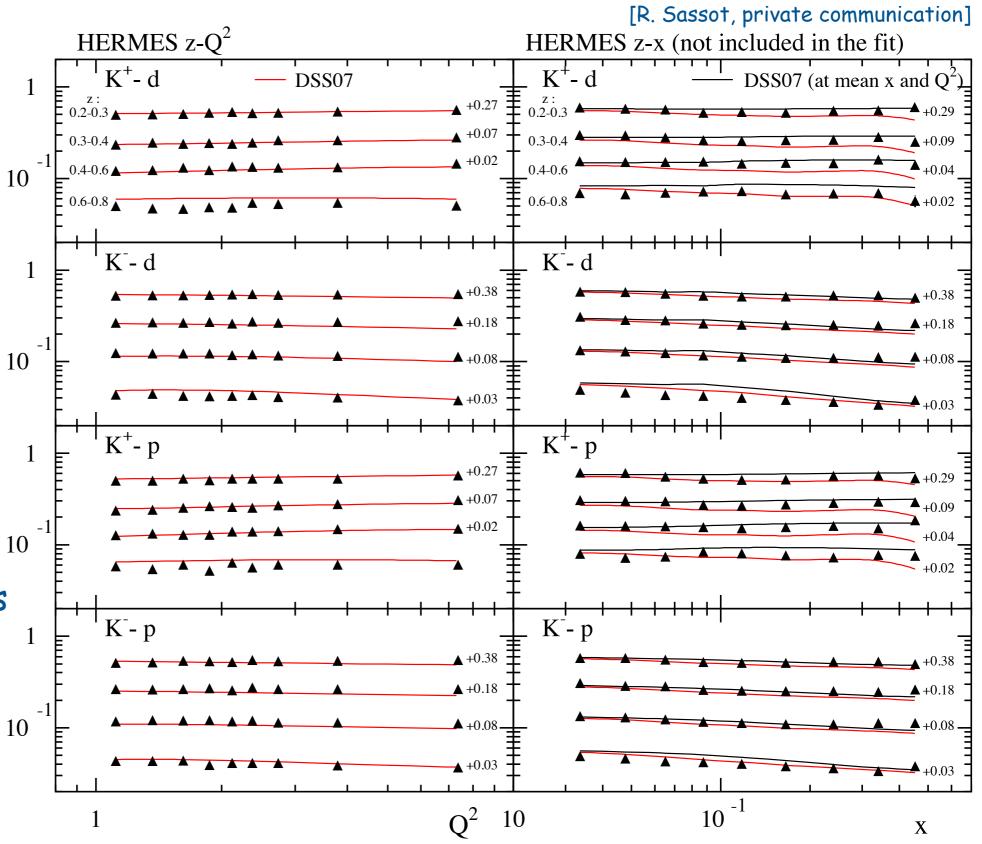


#### integrating vs. using average kinematics

(by now old)
 DSS07 FF fit to
 z-Q² projection

z-x "prediction"
reasonable well
when using
integration over
phase-space limits
(red lines)

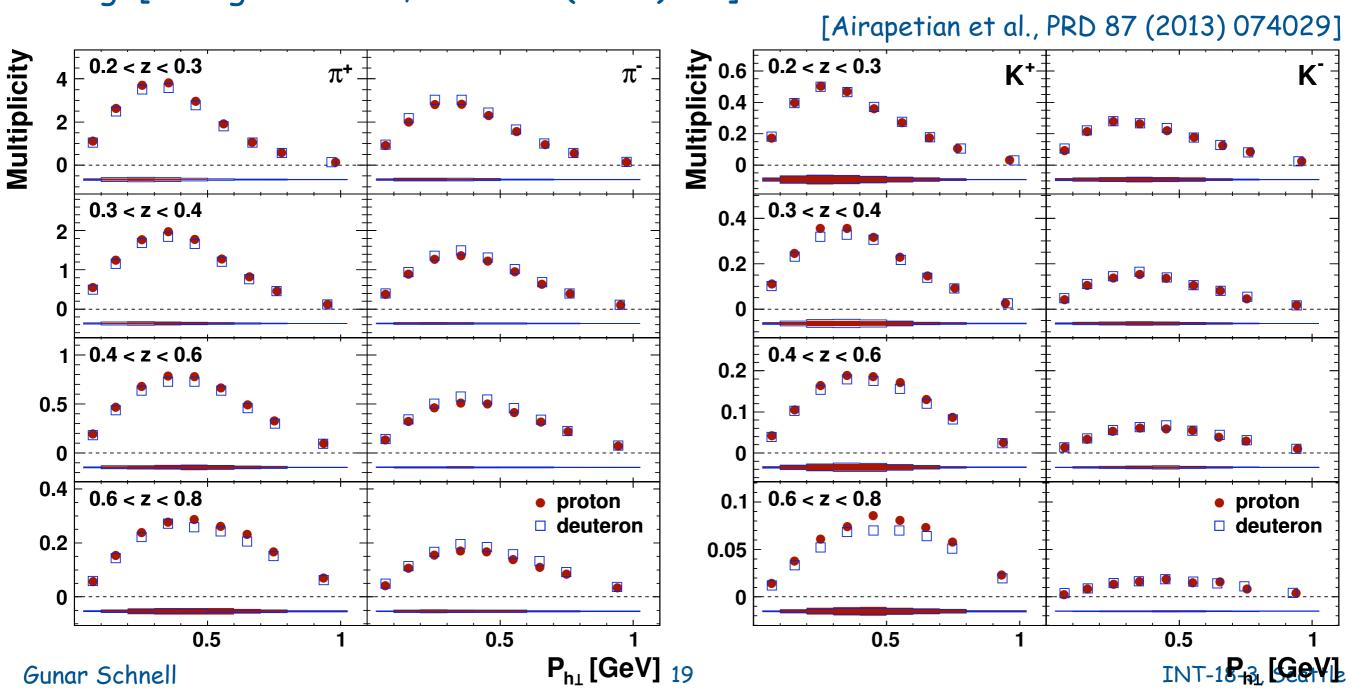
significant changes
 when using
 average
 kinematics



	U	$oxed{L}$	m T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
$\Gamma$	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

#### Ph1 dependence

- multi-dimensional analysis allows going beyond collinear factorization
- flavor information on transverse momenta via target variation and hadron ID
   e.g. [A. Signori et al., JHEP 11(2013)194]



	U	L	T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

## $P_{h\perp}$ -multiplicity landscape

	EMC [11]	HERMES [15]	JLAB [31]	COMPASS [16]	COMPASS (This paper)
Target	p/d	p/d	d	d	d
Beam energy (GeV)	100–280	27.6	5.479	160	160
Hadron type	$h^\pm$	$\pi^\pm,~\mathrm{K}^\pm$	$\pi^\pm$	$h^\pm$	$h^\pm$
Observable	$M^{h^++h^-}$	$M^h$	$\sigma^h$	$M^h$	$M^h$
$Q_{\min}^2 (\text{GeV}/c)^2$	2/3/4/5	1	2	1	1
$W_{\min}^2 \ (\text{GeV}/c^2)^2$	-	10	4	25	25
y range	[0.2, 0.8]	[0.1, 0.85]	[0.1, 0.9]	[0.1, 0.9]	[0.1, 0.9]
x range	[0.01,1]	[0.023, 0.6]	[0.2,0.6]	[0.004, 0.12]	[0.003, 0.4]
$P_{\rm hT}^2$ range $({\rm GeV}/c)^2$	[0.081, 15.8]	[0.0047, 0.9]	[0.004, 0.196]	[0.02, 0.72]	[0.02,3]

- [11] J. Ashman et al. (EMC), Z. Phys. C 52, 361 (1991).
- [15] A. Airapetian et al. (HERMES), Phys. Rev. D87, 074029 (2013).
- [16] C. Adolph et al. (COMPASS), Eur. Phys. J. C73, 2531 (2013); 75, 94(E) (2015).
- [31] R. Asaturyan et al., Phys. Rev. C 85, 015202 (2012).
- ["This paper"] M. Aghasyan et al. (COMPASS), Phys. Rev. D 97, 032006 (2018).

... as well as more limited measurements by H1 and Zeus

	U	L	T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

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Observable	$M^{h^++h^-}$	$M^h$	$\sigma^h$	$M^h$	$M^h$
$Q_{\rm min}^2~({\rm GeV}/c)^2$	2/3/4/5	1	2	1	1
$Q_{ m min}^2 \; ({ m GeV}/c)^2 \ W_{ m min}^2 \; ({ m GeV}/c^2)^2$	-	10	4	25	25
y range	[0.2, 0.8]	[0.1, 0.85]	[0.1, 0.9]	[0.1, 0.9]	[0.1, 0.9]
x range	[0.01,1]	[0.023, 0.6]	[0.2,0.6]	[0.004, 0.12]	[0.003, 0.4]
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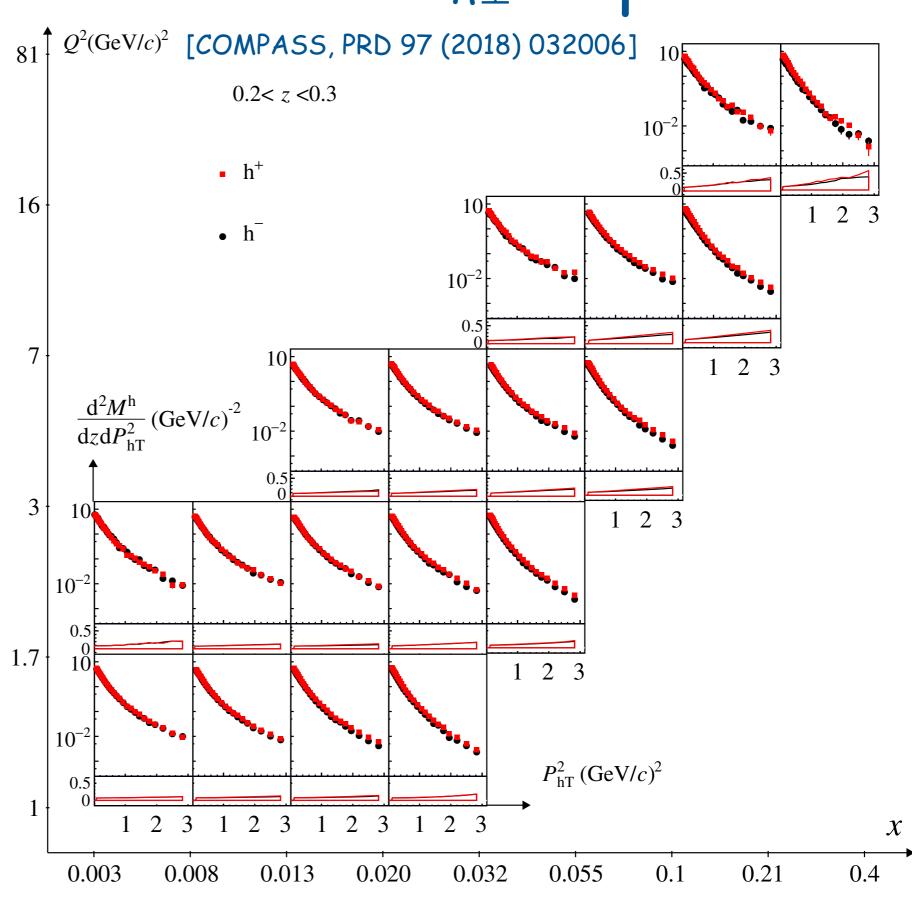
- [11] J. Ashman et al. (EMC), Z. Phys. C 52, 361 (1991).
- [15] A. Airapetian et al. (HERMES), Phys. Rev. D87, 074029 (2013).
- [16] C. Adolph et al. (COMPASS), Eur. Phys. J. C73, 2531 (2013); 75, 94(E) (2015).
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... as well as more limited measurements by H1 and Zeus

	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

- data on LiD target
- differential in x, z,  $Q^2$ ,  $P_{h\perp}^2$
- one example (lowest z bin)
- high statistical precision allows detailed studies

#### Ph1 dependence

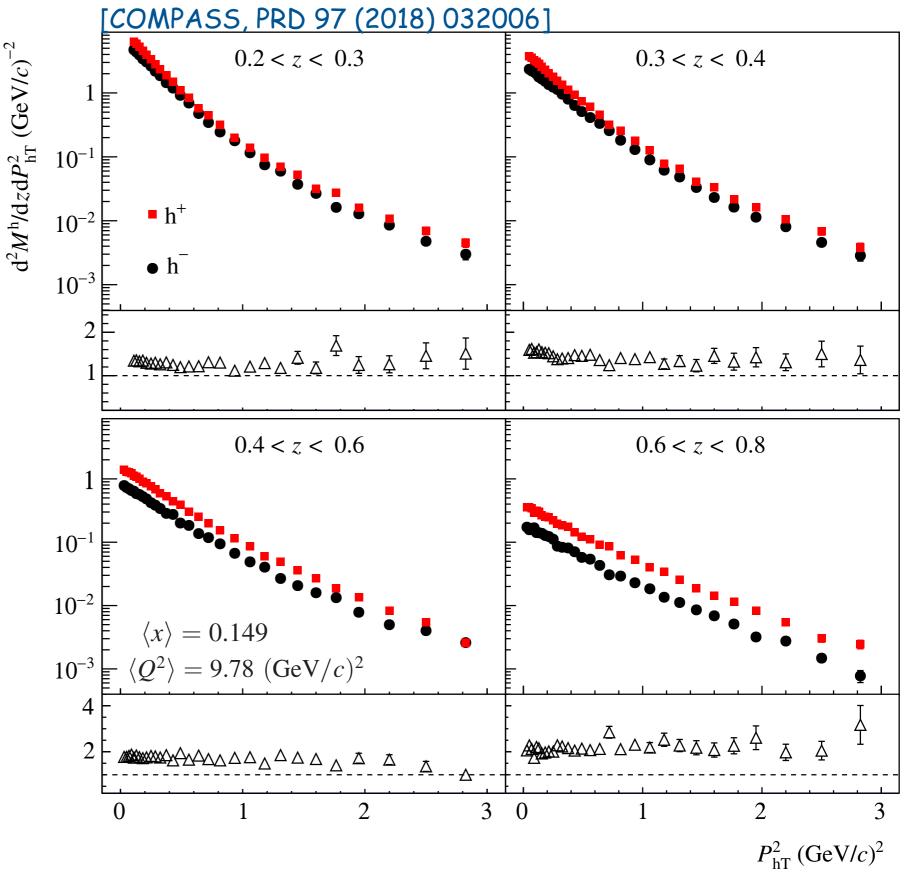


	U	${ m L}$	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

# differences between h<sup>+</sup> and h<sup>-</sup> increase with z

#### $P_{h\perp}$ dependence

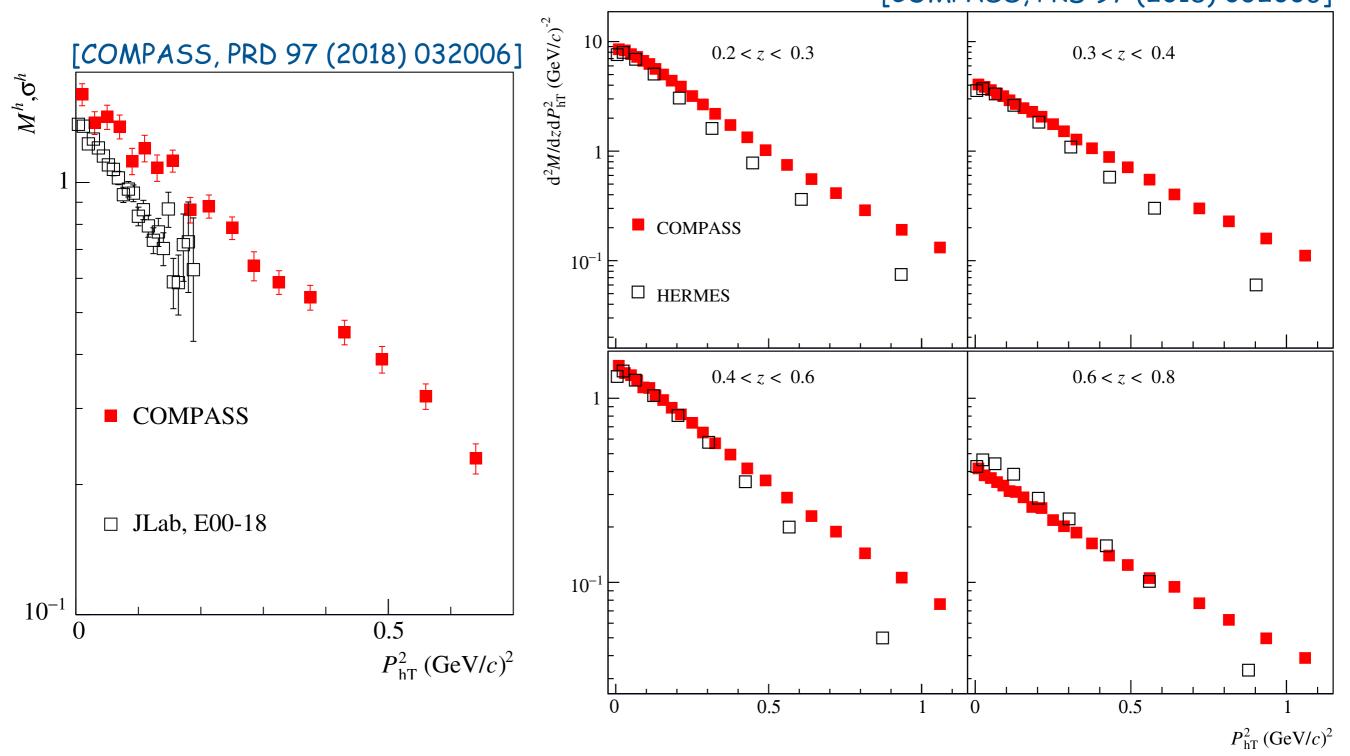
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	U	L	$\Gamma$
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
T	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

#### COMPASS vs. JLab & HERMES

#### [COMPASS, PRD 97 (2018) 032006]

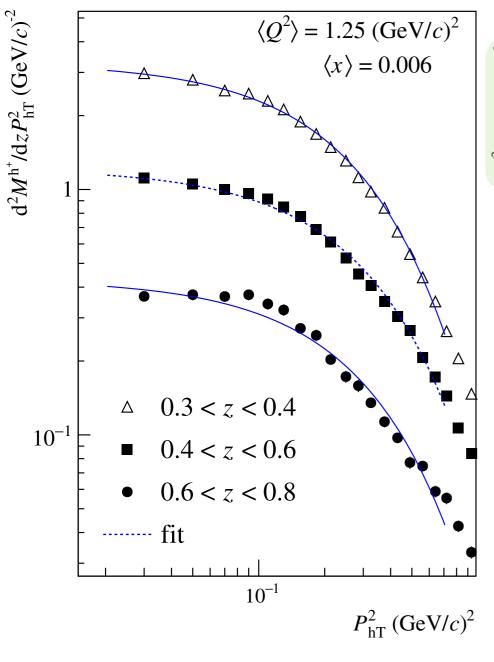


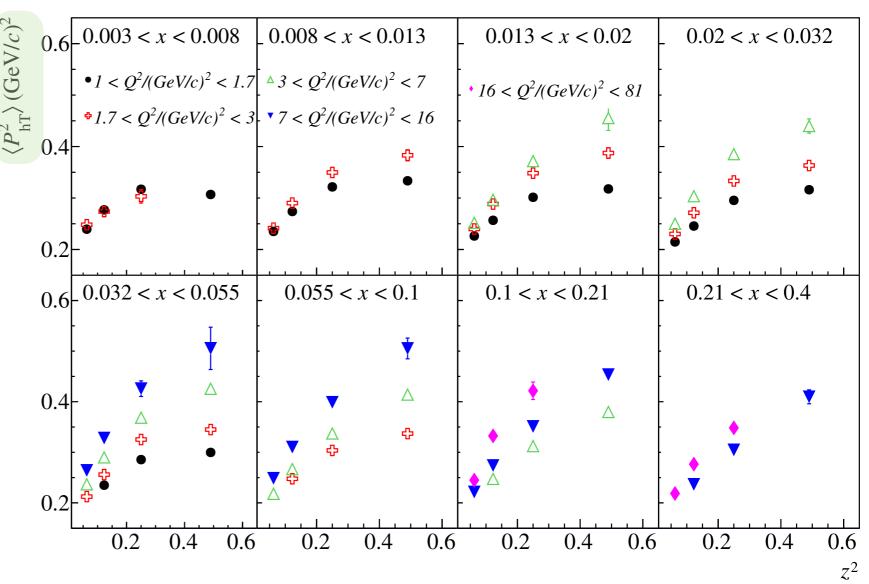
	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

## fitting the $P_{h\perp}$ dependence

$$\frac{\mathrm{d}^{2}M^{\mathrm{h}}(x,Q^{2};z)}{\mathrm{d}z\mathrm{d}P_{\mathrm{hT}}^{2}} = \frac{N}{\langle P_{\mathrm{hT}}^{2} \rangle} \exp\left(-\frac{P_{\mathrm{hT}}^{2}}{\langle P_{\mathrm{hT}}^{2} \rangle}\right)$$

#### [COMPASS, PRD 97 (2018) 032006]

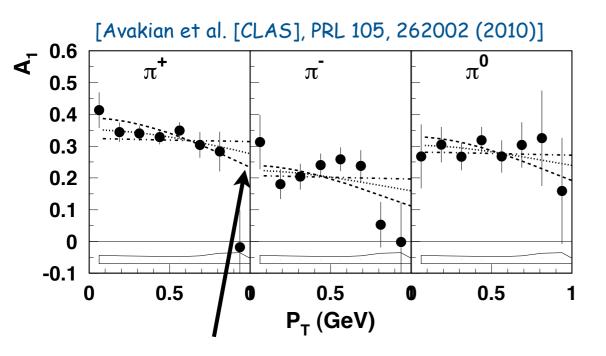




$$\langle P_{h\perp}^2(z) \rangle = z^2 \langle p_T^2 \rangle + \langle K_T^2 \rangle$$
 does not work!

	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
$\Gamma$	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

#### Helicity density



CLAS data hints at width  $\mu_2$  of  $g_1$  that is less than the width  $\mu_0$  of  $f_1$ 

$$f_1^q(x, k_T) = f_1(x) \frac{1}{\pi \mu_0^2} \exp\left(-\frac{k_T^2}{\mu_0^2}\right)$$
$$g_1^q(x, k_T) = g_1(x) \frac{1}{\pi \mu_2^2} \exp\left(-\frac{k_T^2}{\mu_2^2}\right)$$

... also suggested by lattice QCD

	U	L	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

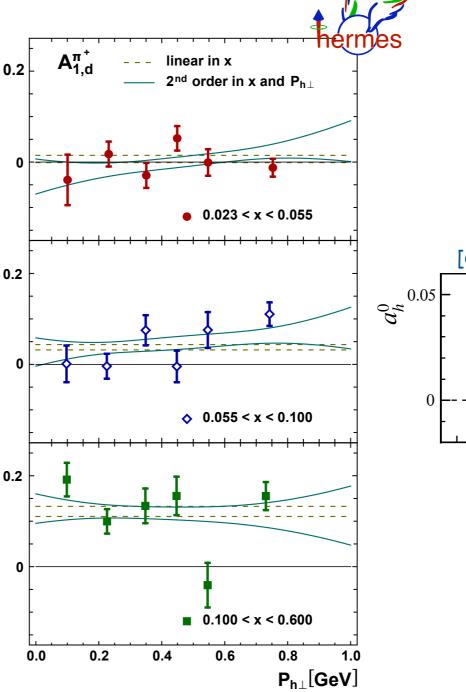
#### 

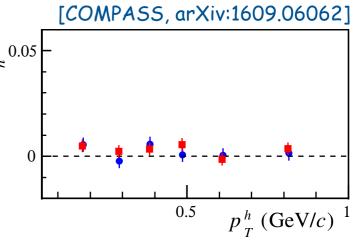
## CLAS data hints at width $\mu_2$ of $g_1$ that is less than the width $\mu_0$ of $f_1$

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$$g_1^q(x, k_T) = g_1(x) \frac{1}{\pi \mu_2^2} \exp\left(-\frac{k_T^2}{\mu_2^2}\right)$$

#### ... also suggested by lattice QCD

## Helicity density

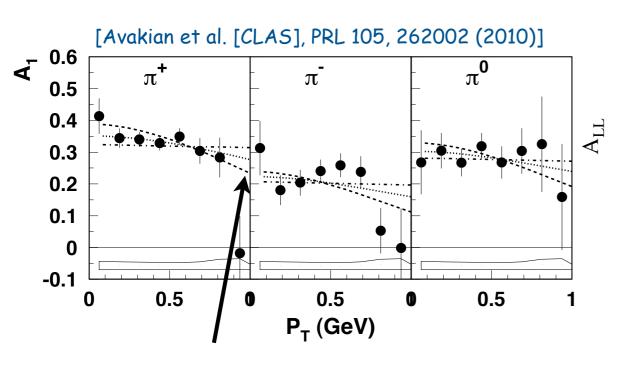


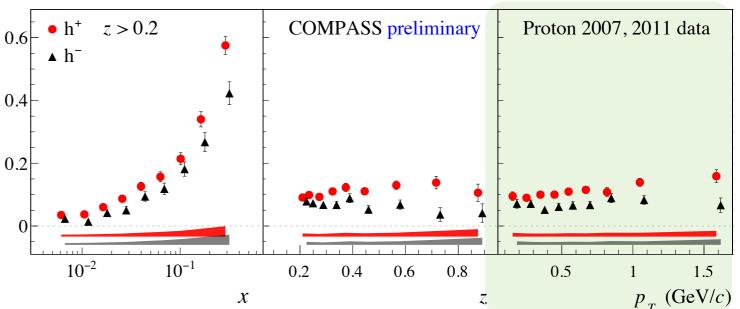


no significant  $P_{h\perp}$  dependences seen on D at HERMES and COMPASS

	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

## Helicity density





CLAS data hints at width  $\mu_2$  of  $g_1$  that is less than the width  $\mu_0$  of  $f_1$ 

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$$g_1^q(x, k_T) = g_1(x) \frac{1}{\pi \mu_2^2} \exp\left(-\frac{k_T^2}{\mu_2^2}\right)$$

perhaps a hint on protons at COMPASS? (but opposite trend than at CLAS)

... also suggested by lattice QCD

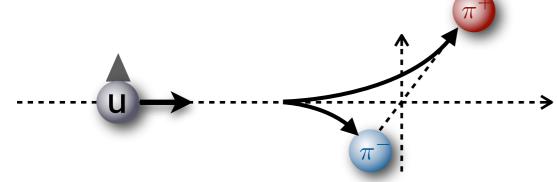
no significant  $P_{h\perp}$  dependences seen on D at HERMES and COMPASS

## The quest for transversity

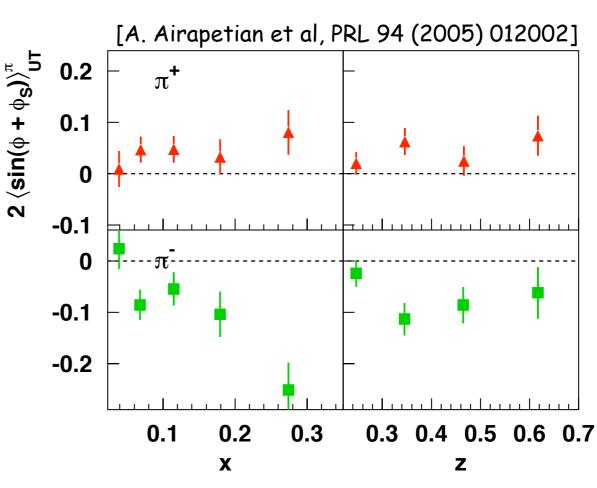
	U	L	${ m T}$
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

# Transversity (Collins fragmentation)

- significant in size and opposite in sign for charged pions
- disfavored Collins FF large and opposite in sign to favored one



leads to various cancellations in SSA observables

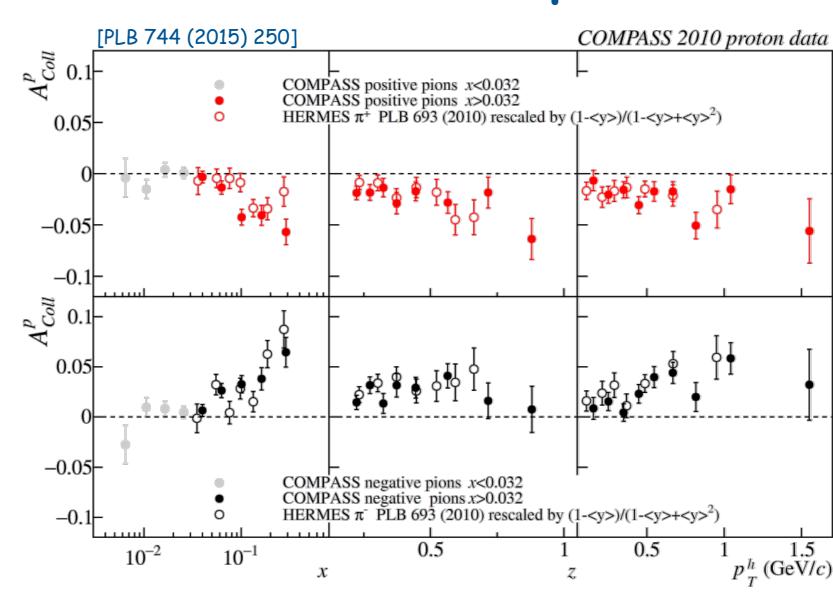


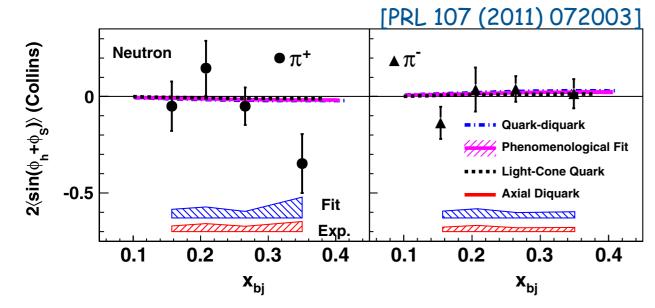
2005: First evidence from HERMES SIDIS on proton

Non-zero transversity
Non-zero Collins function

	U	${ m L}$	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

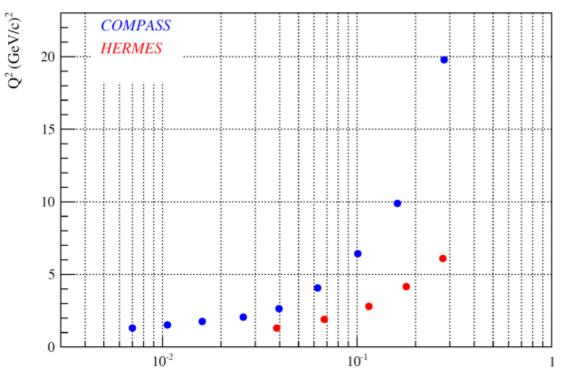
- since those early days, a wealth of new results:
  - COMPASS
     [PLB 692 (2010) 240,
     PLB 717 (2012) 376, PLB 744 (2015) 250]
  - HERMES
    [PLB 693 (2010) 11]
  - Jefferson Lab [PRL 107 (2011) 072003]

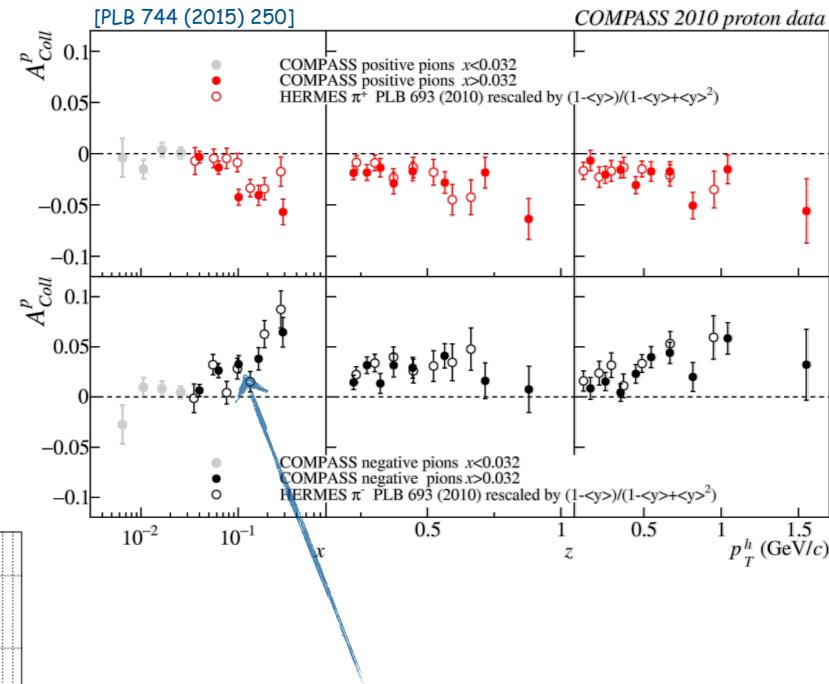




	U	L	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^\perp$

- since those early days, a wealth of new results:
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  - Jefferson Lab [PRL 107 (2011) 072003]

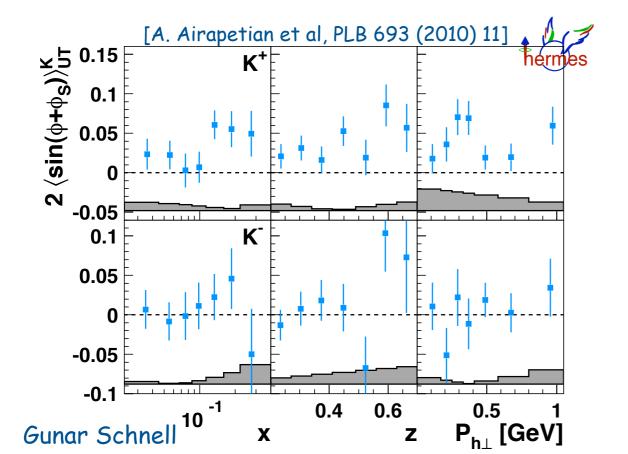


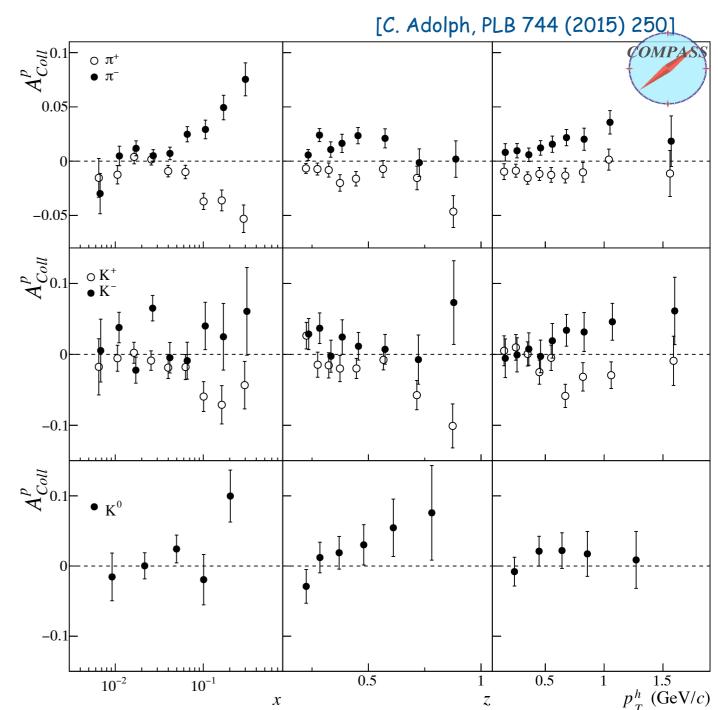


- excellent agreement of various proton data, also with neutron results
- no indication of strong evolution effects

	U	L	T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^\perp$

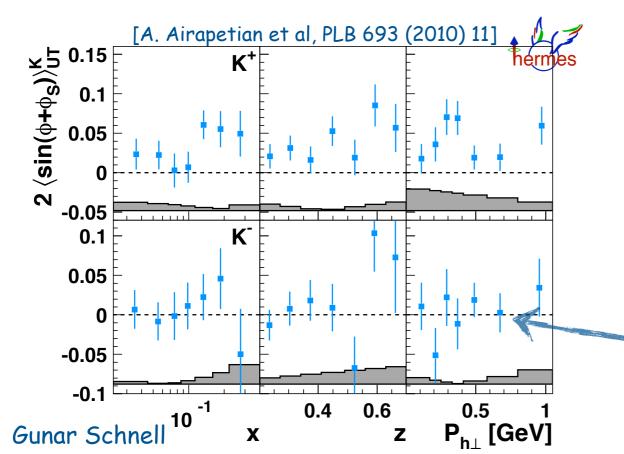
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    [PRL 107 (2011) 072003]

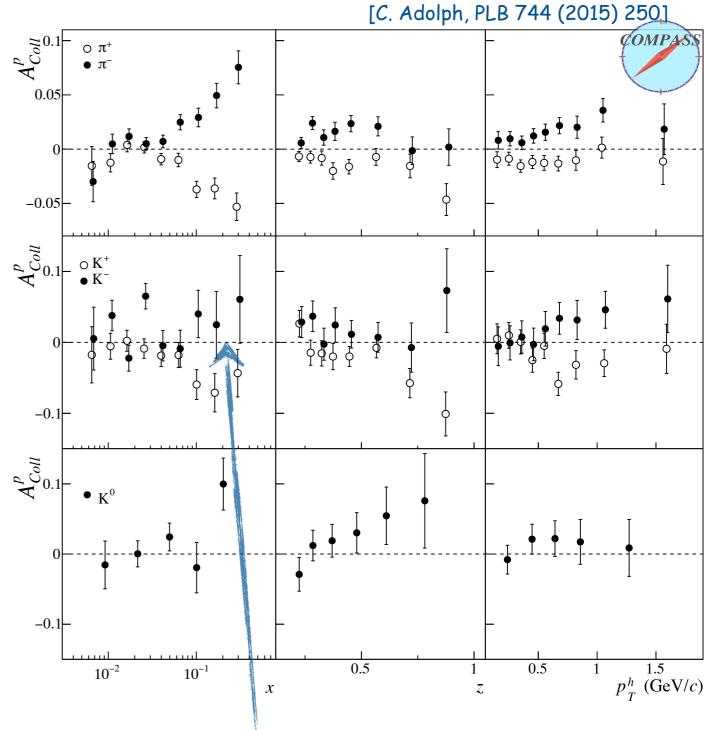




	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^\perp$

- since those early days, a wealth of new results:
  - COMPASS
     [PLB 692 (2010) 240,
     PLB 717 (2012) 376, PLB 744 (2015) 250]
  - HERMES
    [PLB 693 (2010) 11]
  - Jefferson Lab
    [PRL 107 (2011) 072003]





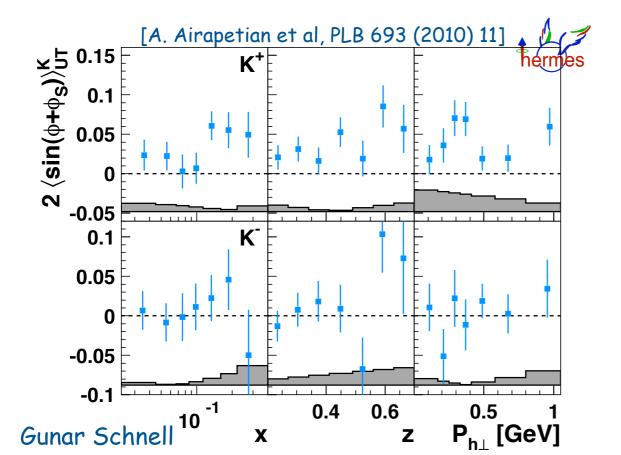
cancelation of (unfavored) u and d fragmentation (opposite signs of up and down transversity)?

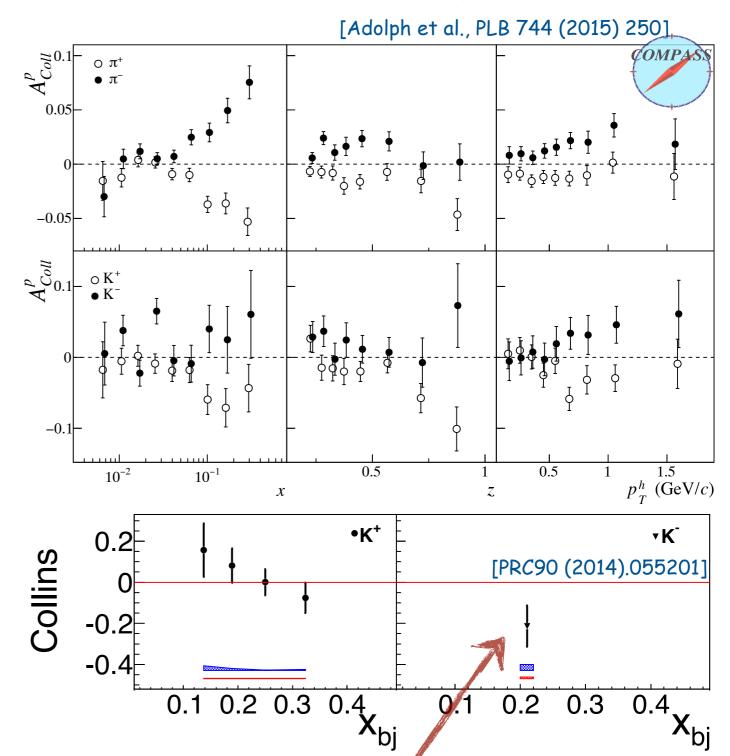
29

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	U	${ m L}$	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

- since those early days, a wealth of new results:
  - COMPASS
     [PLB 692 (2010) 240,
     PLB 717 (2012) 376, PLB 744 (2015) 250]
  - HERMES
    [PLB 693 (2010) 11]
  - Jefferson Lab
    [PRL 107 (2011) 072003, PRC90 (2014).055201]





but relatively large K<sup>-</sup> asymmetry on <sup>3</sup>He?

#### the "Collins trap"

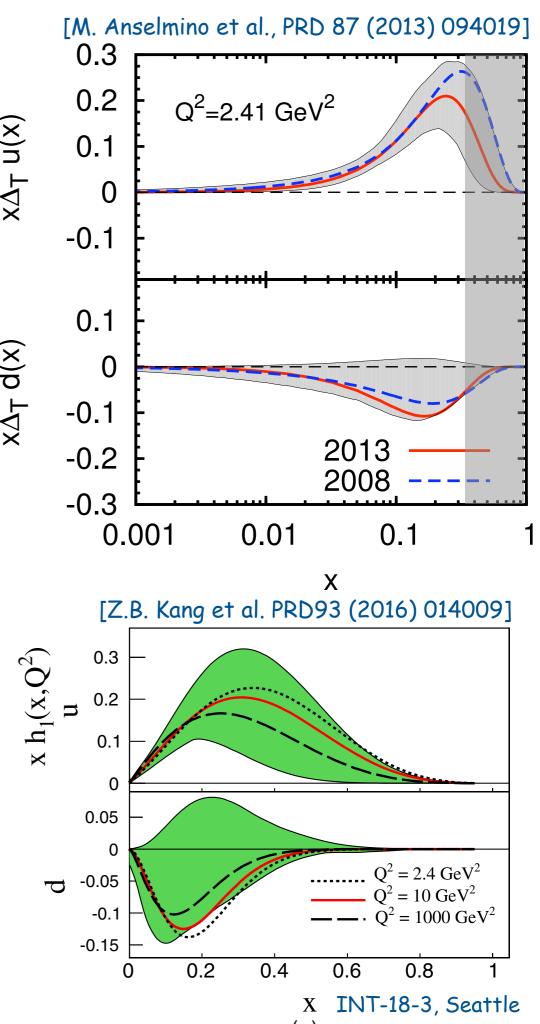
$$H_{1,\mathrm{fav}}^{\perp} \simeq -H_{1,\mathrm{dis}}^{\perp}$$

#### thus

$$\langle \sin(\phi + \phi_S) \rangle_{UT}^{\pi^+} \sim (4h_1^u - h_1^d) H_{1,\text{fav}}^{\perp}$$

$$\langle \sin(\phi + \phi_S) \rangle_{UT}^{\pi^-} \sim - \left(4h_1^u - h_1^d\right) H_{1,\text{fav}}^{\perp}$$

"impossible" to disentangle u/d transversity -> current limits driven mainly by Soffer bound?



#### the "Collins trap"

$$H_{1,\text{fav}}^{\perp} \simeq -H_{1,\text{dis}}^{\perp}$$

#### thus

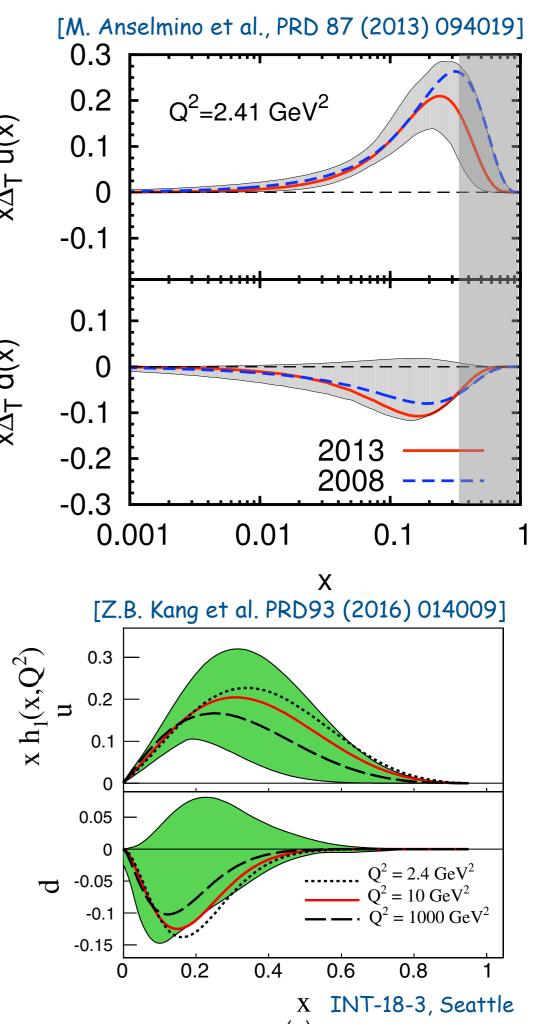
$$\langle \sin(\phi + \phi_S) \rangle_{UT}^{\pi^+} \sim (4h_1^u - h_1^d) H_{1,\text{fav}}^{\perp}$$

$$\langle \sin(\phi + \phi_S) \rangle_{UT}^{\pi^-} \sim - \left(4h_1^u - h_1^d\right) H_{1,\text{fav}}^{\perp}$$

"impossible" to disentangle u/d transversity -> current limits driven mainly by Soffer bound?

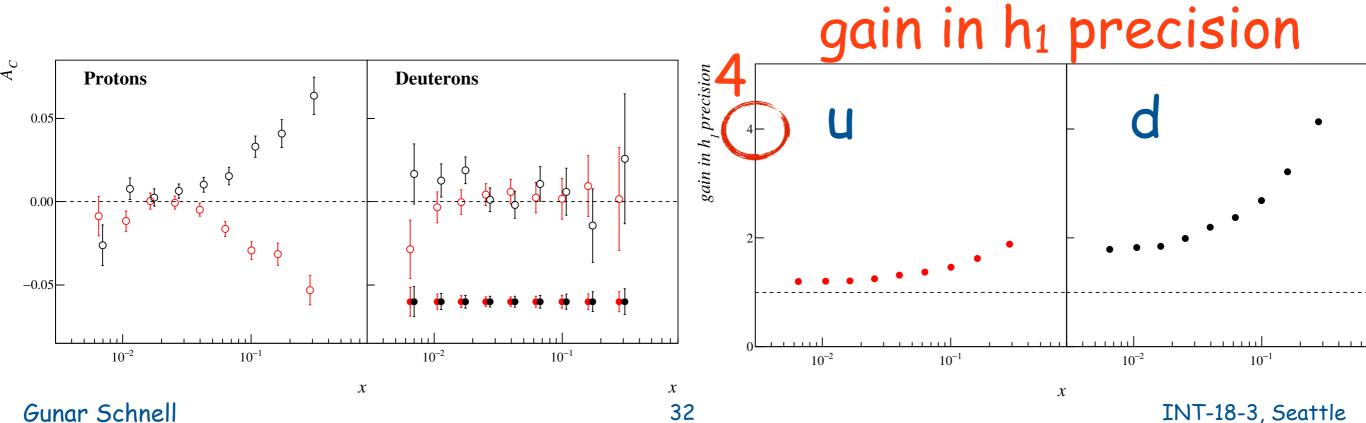
clearly need precise data from "neutron" target(s), e.g., COMPASS d, and later JLab12 & EIC

(valid for all chiral-odd TMDs)



#### d-transversity running at COMPASS

- currently much more p than d data available
- add another year of d running after CERN LS2 (2021)
  - large impact on d-transversity
  - reduced correlations between u and d transversity
     (note, correlations important in tensor-charge calculation)

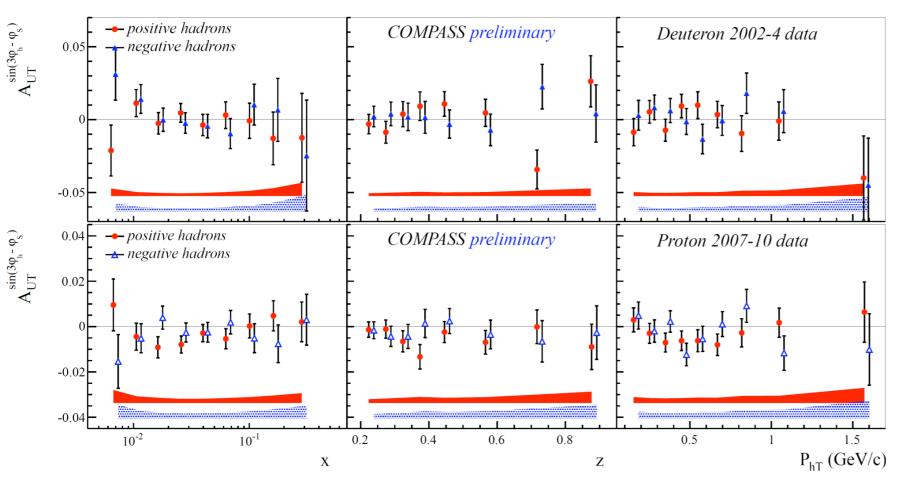


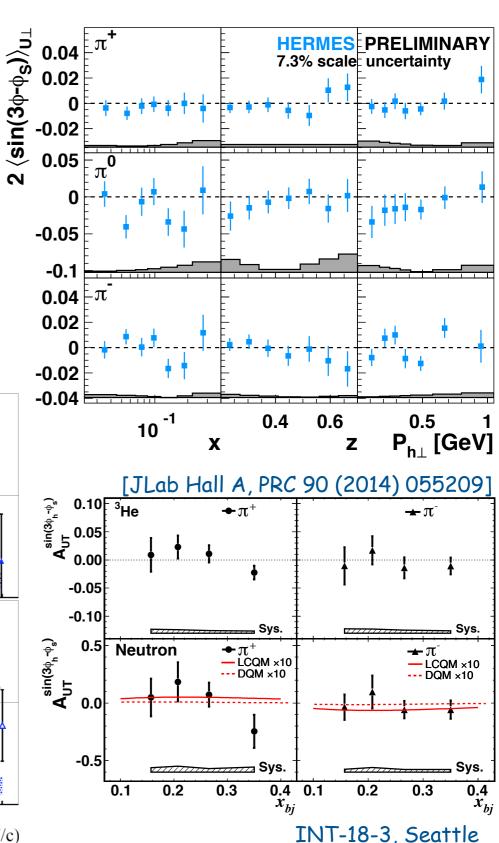
## Transversity's friends

	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
T	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

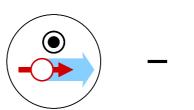
#### Pretzelosity

- chiral-odd > needs Collins FF (or similar)
- <sup>1</sup>H, <sup>2</sup>H & <sup>3</sup>He data consistently small
- cancelations? pretzelosity=zero? or just the additional suppression by two powers of  $P_{h\perp}$





	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

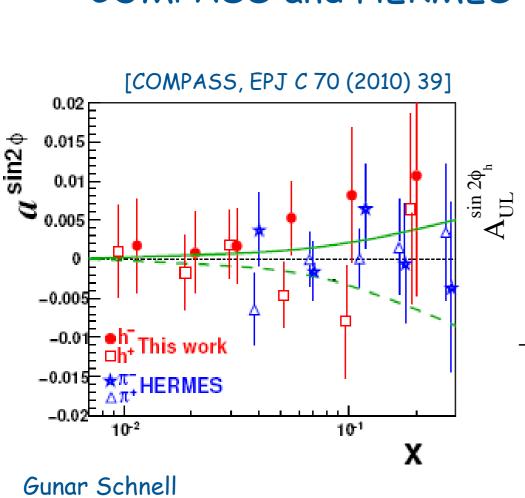


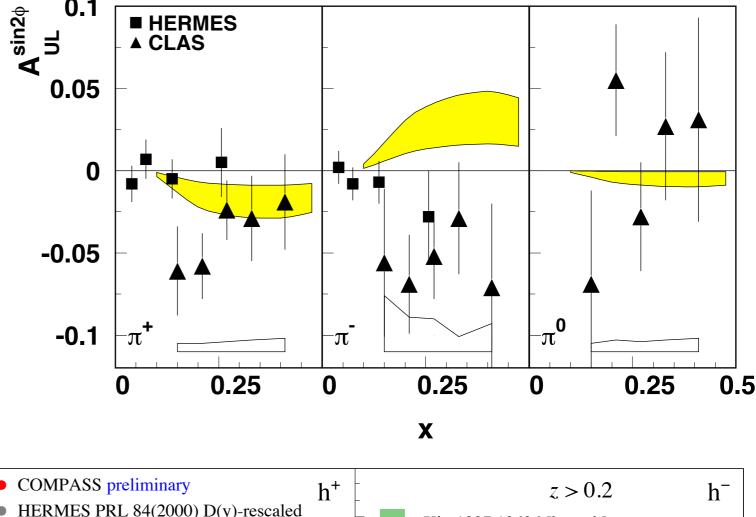


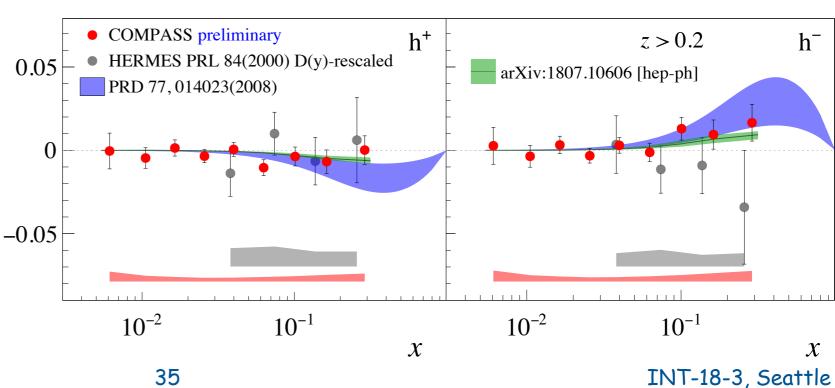
#### Worm-Gear I

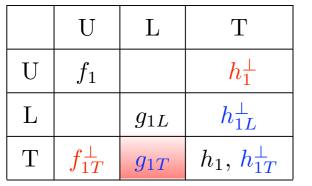
[CLAS, PRL 105 (2010) 262002]

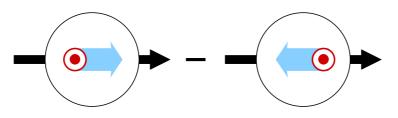
- again: chiral-odd
- evidence from CLAS?
- consistent with zero at COMPASS and HERMES



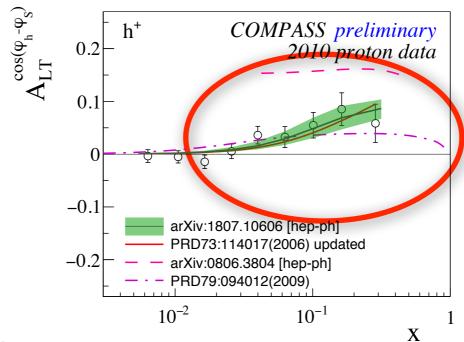




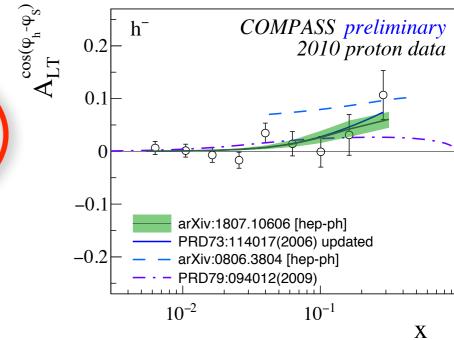




#### Worm-Gear II



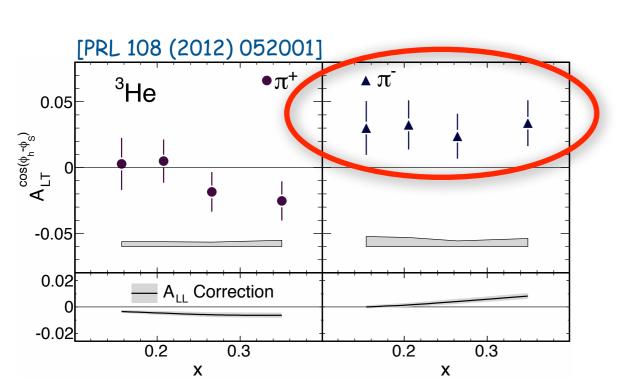
36

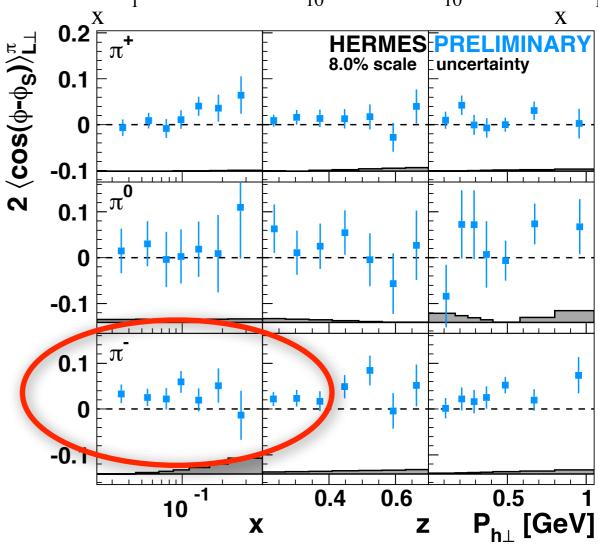


<sup>3</sup>He target at JLab

first evidences:

H target at COMPASS & HERMES



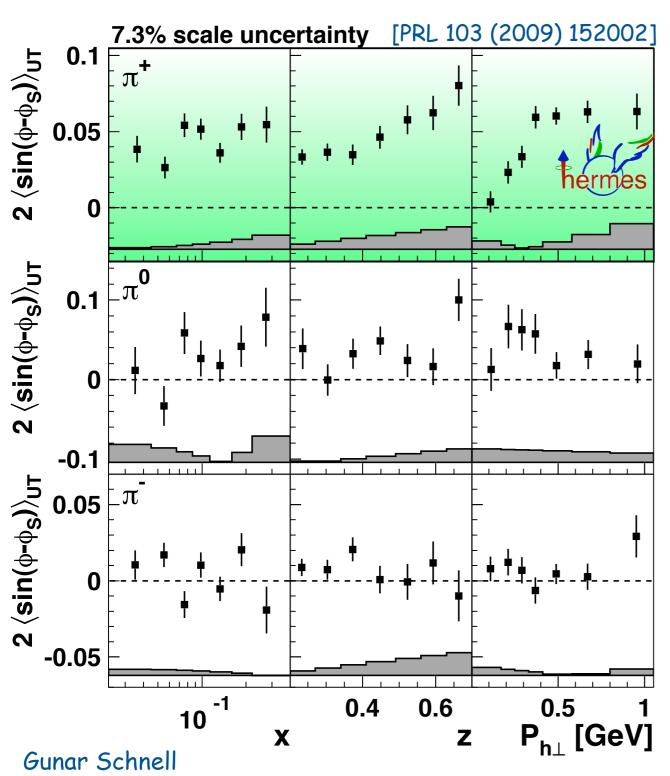


INT-18-3, Seattle

	U	${ m L}$	T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

#### Sivers amplitudes for pions

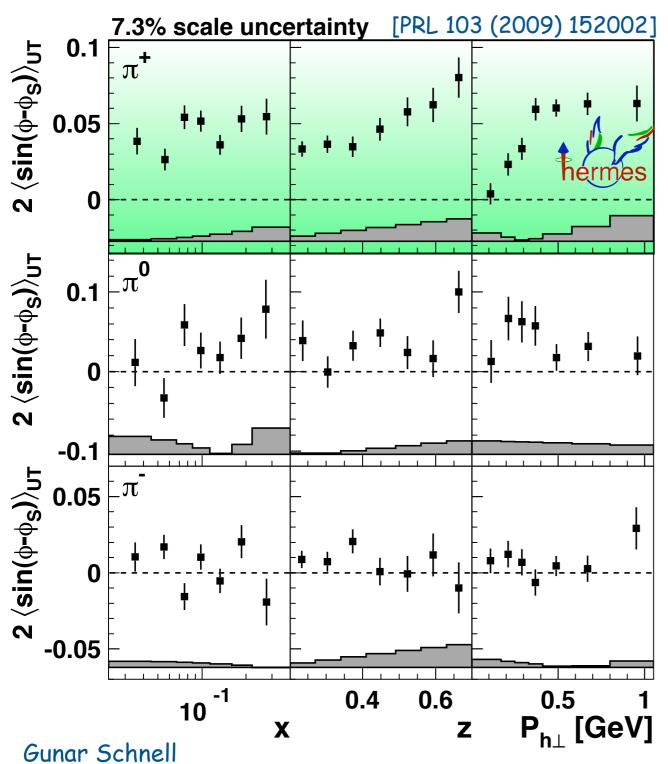
$$2\langle \sin(\phi - \phi_S) \rangle_{\text{UT}} = -\frac{\sum_q e_q^2 f_{1T}^{\perp, q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$



	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

#### Sivers amplitudes for pions

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# $\pi^{+}$ dominated by u-quark scattering:

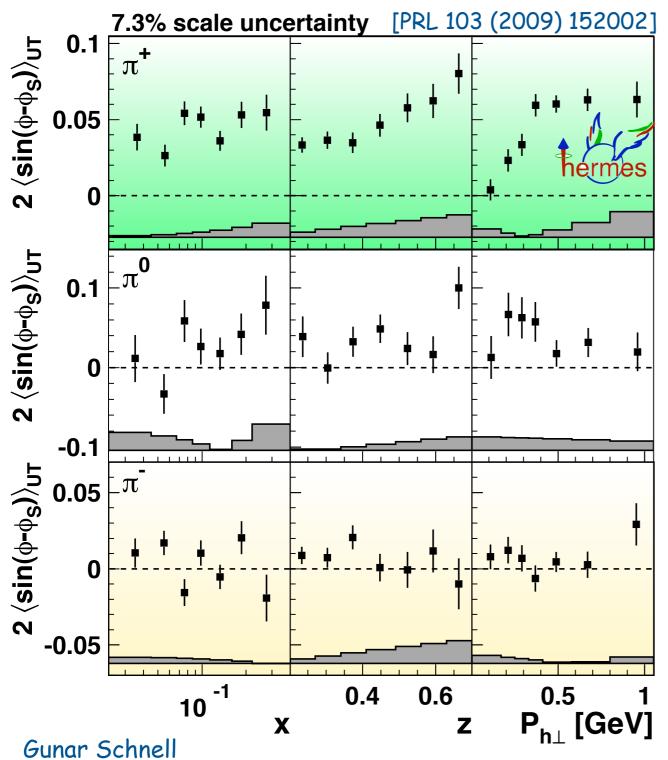
$$\simeq - \frac{f_{1T}^{\perp,u}(x,p_T^2) \otimes_{\mathcal{W}} D_1^{u \to \pi^+}(z,k_T^2)}{f_1^u(x,p_T^2) \otimes D_1^{u \to \pi^+}(z,k_T^2)}$$

#### u-quark Sivers DF < 0

	U	L	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

#### Sivers amplitudes for pions

$$2\langle \sin(\phi - \phi_S) \rangle_{\text{UT}} = -\frac{\sum_q e_q^2 f_{1T}^{\perp, q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, k_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, k_T^2)}$$



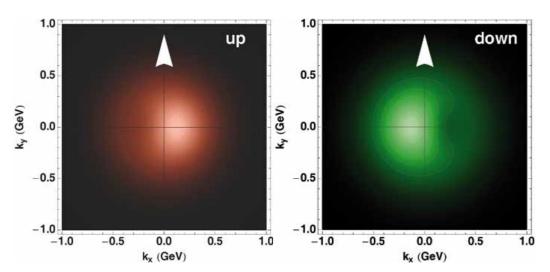
 $\pi^{\dagger}$  dominated by u-quark scattering:

$$\simeq - \frac{f_{1T}^{\perp,u}(x,p_T^2) \otimes_{\mathcal{W}} D_1^{u \to \pi^+}(z,k_T^2)}{f_1^u(x,p_T^2) \otimes D_1^{u \to \pi^+}(z,k_T^2)}$$

u-quark Sivers DF < 0

d-quark Sivers DF > 0 (cancelation for  $\pi^-$ )

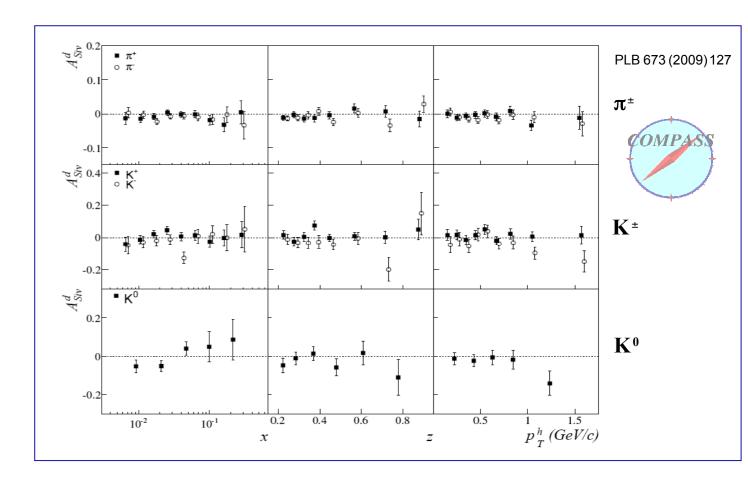
	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$



[A. Bacchetta et al.]

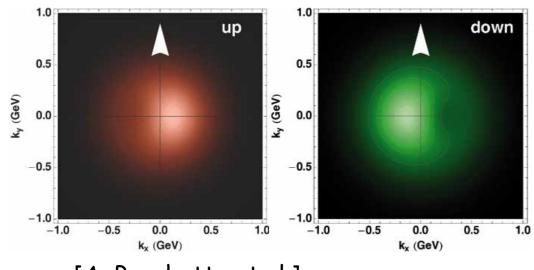
 cancelation for D target supports opposite signs of up and down Sivers

#### Sivers amplitudes

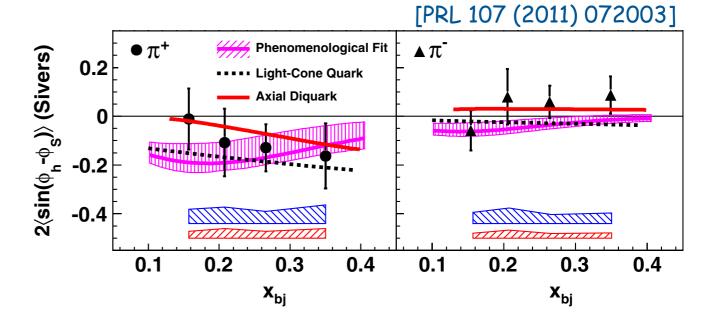


	U	${ m L}$	${ m T}$
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

#### Sivers amplitudes

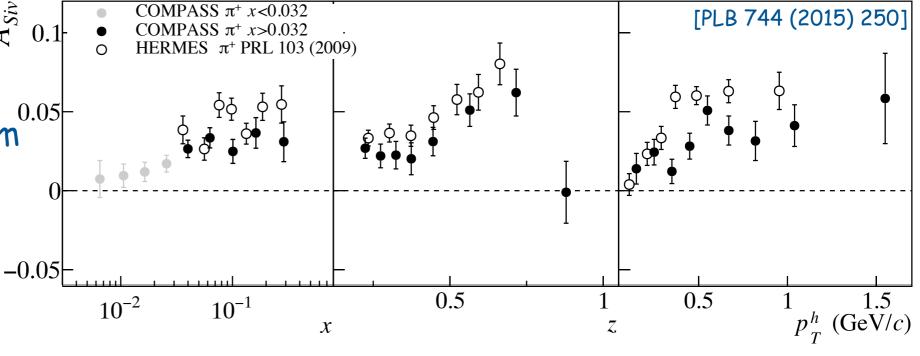


[A. Bacchetta et al.]



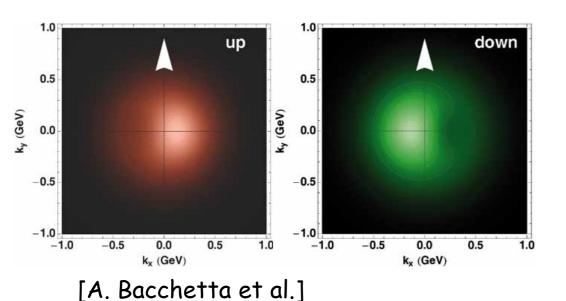
cancelation for D target
 supports opposite signs of
 up and down Sivers

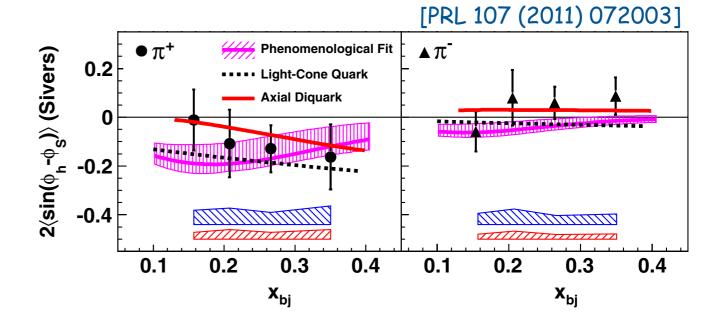
newer results from JLab on using 3He target and from COMPASS for proton target (also multi-d)



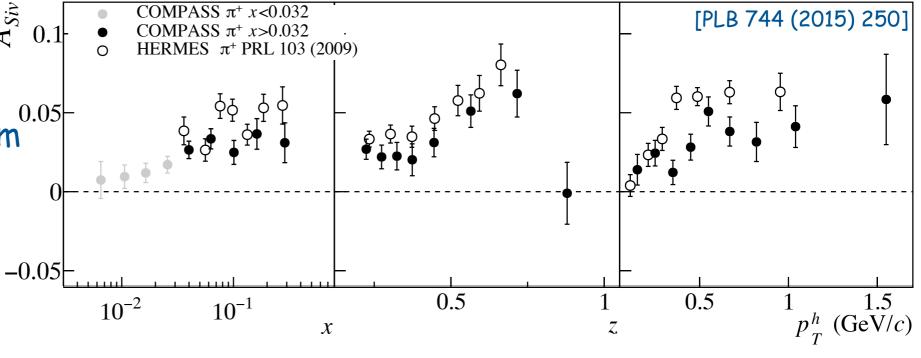
	U	${ m L}$	m T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

#### Sivers amplitudes



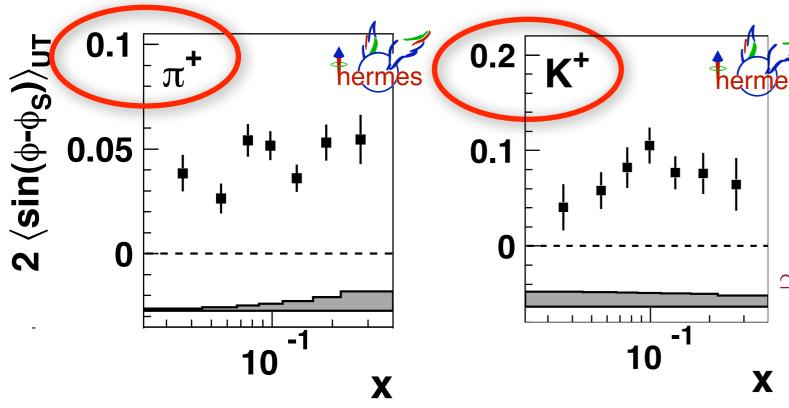


- cancelation for D target
   supports opposite signs of
   up and down Sivers
- newer results from JLab using <sup>3</sup>He target and from COMPASS for proton target (also multi-d)
- hint of Q<sup>2</sup> dependence from COMPASS vs. HERMES



	U	L	${ m T}$
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
T	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

# Sivers amplitudes pions vs. kaons

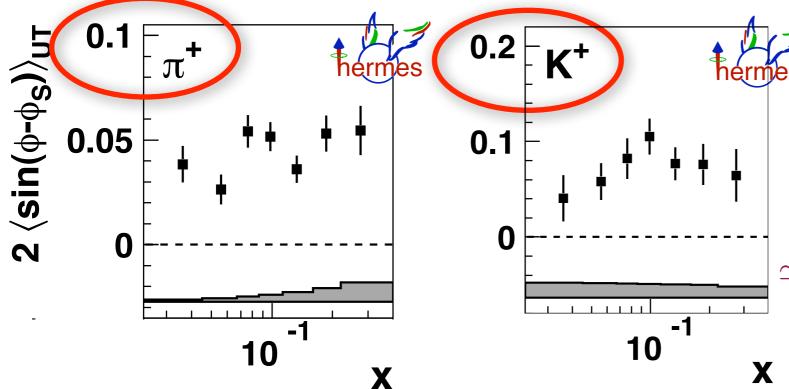


somewhat unexpected if dominated by scattering off u-quarks:

$$\simeq - \ \frac{\mathbf{f_{1T}^{\perp,u}(\mathbf{x}, \mathbf{p_T^2}) \otimes_{\mathcal{W}} \mathbf{D_1^{u \rightarrow \pi^+/K^+}(\mathbf{z}, \mathbf{k_T^2})}}{\mathbf{f_1^u(\mathbf{x}, \mathbf{p_T^2}) \otimes \mathbf{D_1^{u \rightarrow \pi^+/K^+}(\mathbf{z}, \mathbf{k_T^2})}}$$

	U	L	${ m T}$
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, \frac{h_{1T}^{\perp}}{}$

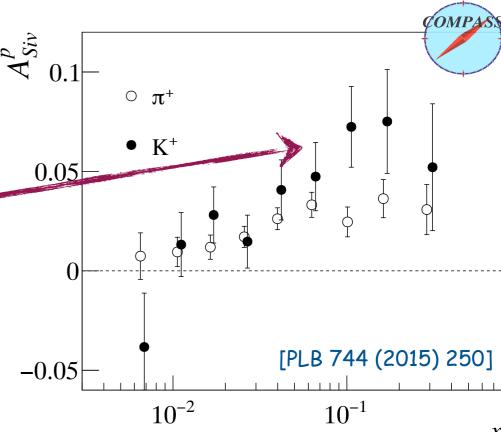
# Sivers amplitudes pions vs. kaons



somewhat unexpected if dominated by scattering off u-quarks:

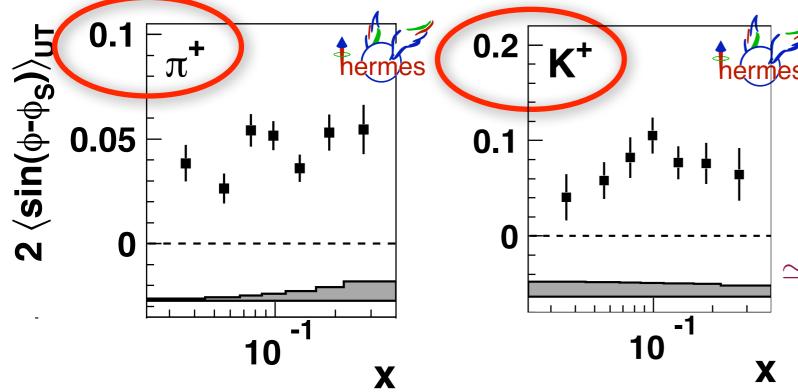
$$\simeq - \ \frac{\mathbf{f_{1T}^{\perp,u}(\mathbf{x}, \mathbf{p_T^2}) \otimes_{\mathcal{W}} \mathbf{D_1^{u \rightarrow \pi^+/K^+}(\mathbf{z}, \mathbf{k_T^2})}}{\mathbf{f_1^u(\mathbf{x}, \mathbf{p_T^2}) \otimes \mathbf{D_1^{u \rightarrow \pi^+/K^+}(\mathbf{z}, \mathbf{k_T^2})}}$$

larger amplitudes seen also by COMPASS



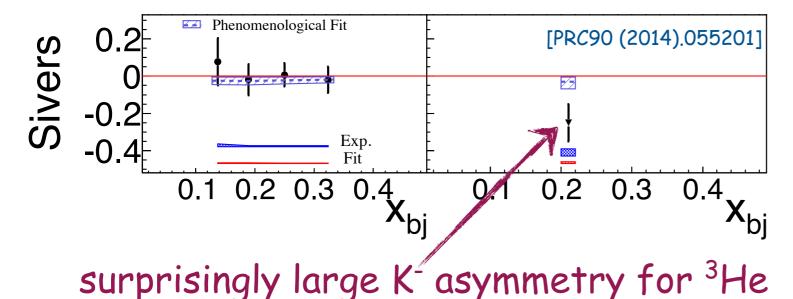
	U	L	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

# Sivers amplitudes pions vs. kaons

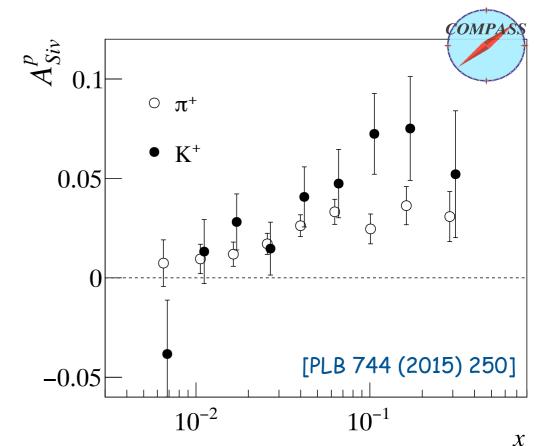


somewhat unexpected if dominated by scattering off u-quarks:

$$\simeq - \ \frac{\mathbf{f_{1T}^{\perp,u}}(\mathbf{x},\mathbf{p_T^2}) \otimes_{\mathcal{W}} \mathbf{D_1^{u \to \pi^+/K^+}}(\mathbf{z},\mathbf{k_T^2})}{\mathbf{f_1^u}(\mathbf{x},\mathbf{p_T^2}) \otimes \mathbf{D_1^{u \to \pi^+/K^+}}(\mathbf{z},\mathbf{k_T^2}))}$$



target (but zero for K<sup>+</sup>?!)



# interlude: dealing with multi-d dependences

- TMD cross sections differential in at least 5 variables
  - some easily parametrized (e.g., azimuthal dependences)
  - others mostly unknown

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  - even different kinematic bins can't disentangle underlying physics dependences
  - e.g., binning in x involves [incomplete] integration(s) over  $P_{h\perp}$

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  - some easily parametrized (e.g., azimuthal dependences)
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- one-dimensional binning provide only glimpse of true physics
  - even different kinematic bins can't disentangle underlying physics dependences
  - e.g., binning in x involves [incomplete] integration(s) over  $P_{h\perp}$
- further complication: physics (cross sections) folded with acceptance
  - NO experiment has flat acceptance in full multi-d kinematic space

$$\frac{N^{+}(x) - N^{-}(x)}{N^{+}(x) - N^{-}(x)} = \frac{\int d\omega \, \epsilon(x, \omega) \, \Delta\sigma(x, \omega)}{\int d\omega \, \epsilon(x, \omega) \, \sigma(x, \omega)}$$

ullet measured cross sections / asymmetries often contain "remnants" of experimental acceptance  $\epsilon$ 

$$\frac{N^{+}(x) - N^{-}(x)}{N^{+}(x) - N^{-}(x)} = \frac{\int d\omega \, \epsilon(x, \omega) \, \Delta\sigma(x, \omega)}{\int d\omega \, \epsilon(x, \omega) \, \sigma(x, \omega)} \neq \frac{\int d\omega \, \Delta\sigma(x, \omega)}{\int d\omega \, \sigma(x, \omega)}$$

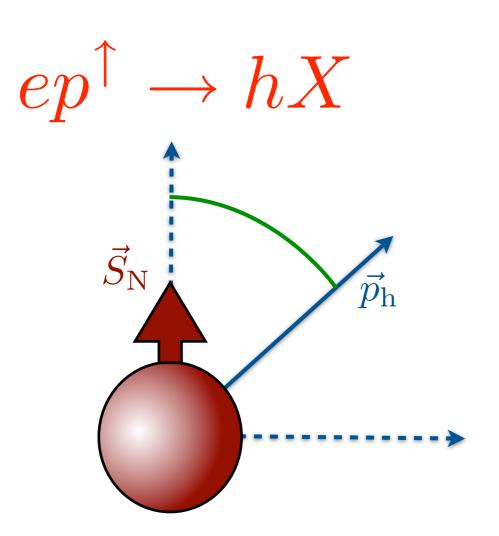
ullet measured cross sections / asymmetries often contain "remnants" of experimental acceptance  $\epsilon$ 

$$\frac{N^{+}(x) - N^{-}(x)}{N^{+}(x) - N^{-}(x)} = \frac{\int d\omega \, \epsilon(x, \omega) \, \Delta\sigma(x, \omega)}{\int d\omega \, \epsilon(x, \omega) \, \sigma(x, \omega)} \neq A(x, \langle \omega \rangle)$$

- $\bullet$  measured cross sections / asymmetries often contain "remnants" of experimental acceptance  $\varepsilon$
- difficult to evaluate precisely in absence of good physics model
  - general challenge to statistically precise data sets
  - avoid 1d binning/presentation of data
  - theorist: watch out for precise definition (if given!) of experimental results reported ... and try not to treat data points of different projections as independent

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 clear left-right asymmetries for pions and positive kaons



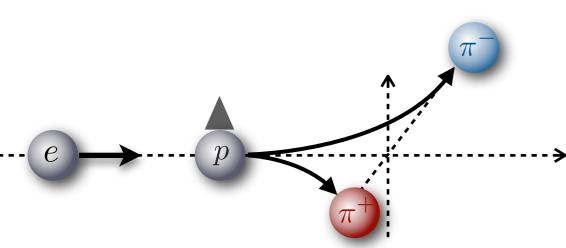
lepton going into the plane

[Airapetian et al., Phys. Lett. B 728, 183-190 (2014)] -0.1 8.8% scale uncertainty 00000000000  $\langle P_T \rangle$  [GeV] 8.0 0.6 0.2 0.2 0.4 0.4 -0.1 8.8% scale uncertainty **№** 0.3 0.2 0.1 1.5 0.5 2 0.5 P<sub>+</sub> [GeV]

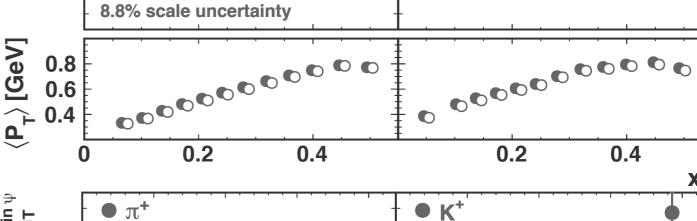
INT-18-3, Seattle

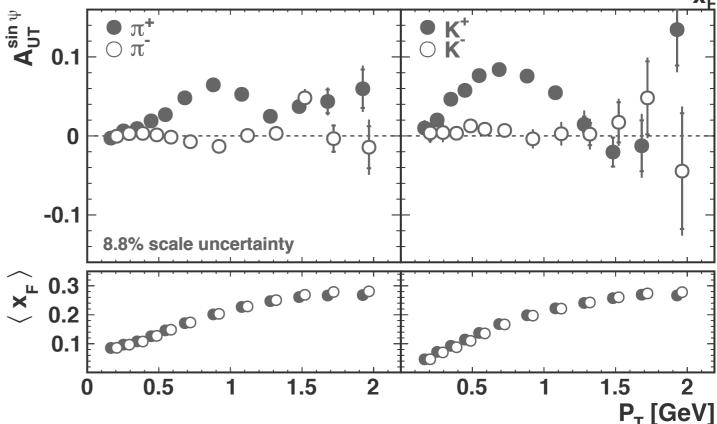
• clear left-right asymmetries for pions and positive kaons

increasing with x<sub>F</sub> (as in pp)



[Airapetian et al., Phys. Lett. B 728, 183-190 (2014)]  $0 \quad K^{+} \quad K^{-} \quad K$ 



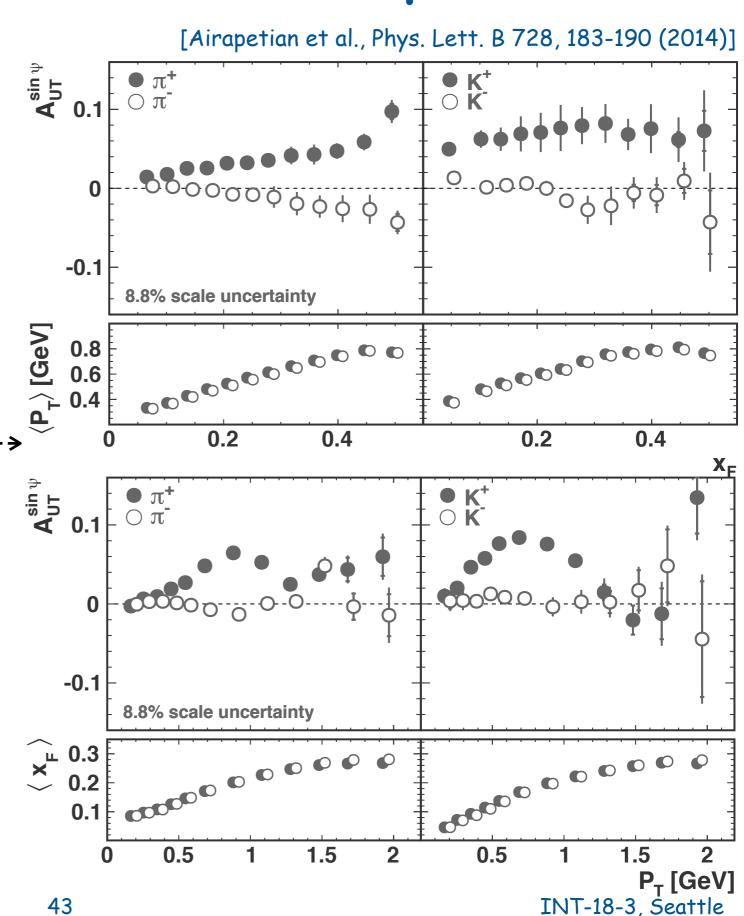


 clear left-right asymmetries for pions and positive kaons

increasing with x<sub>F</sub> (as in pp)

 $e \longrightarrow p$   $\pi^{+}$ 

• initially increasing with  $P_T$  with a fall-off at larger  $P_T$ 

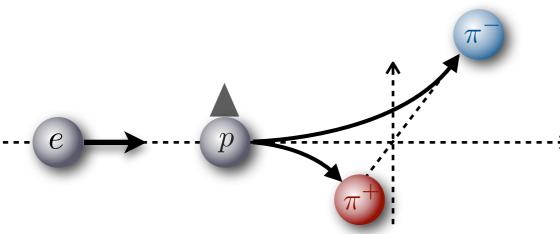


Gunar Schnell

43

 clear left-right asymmetries for pions and positive kaons

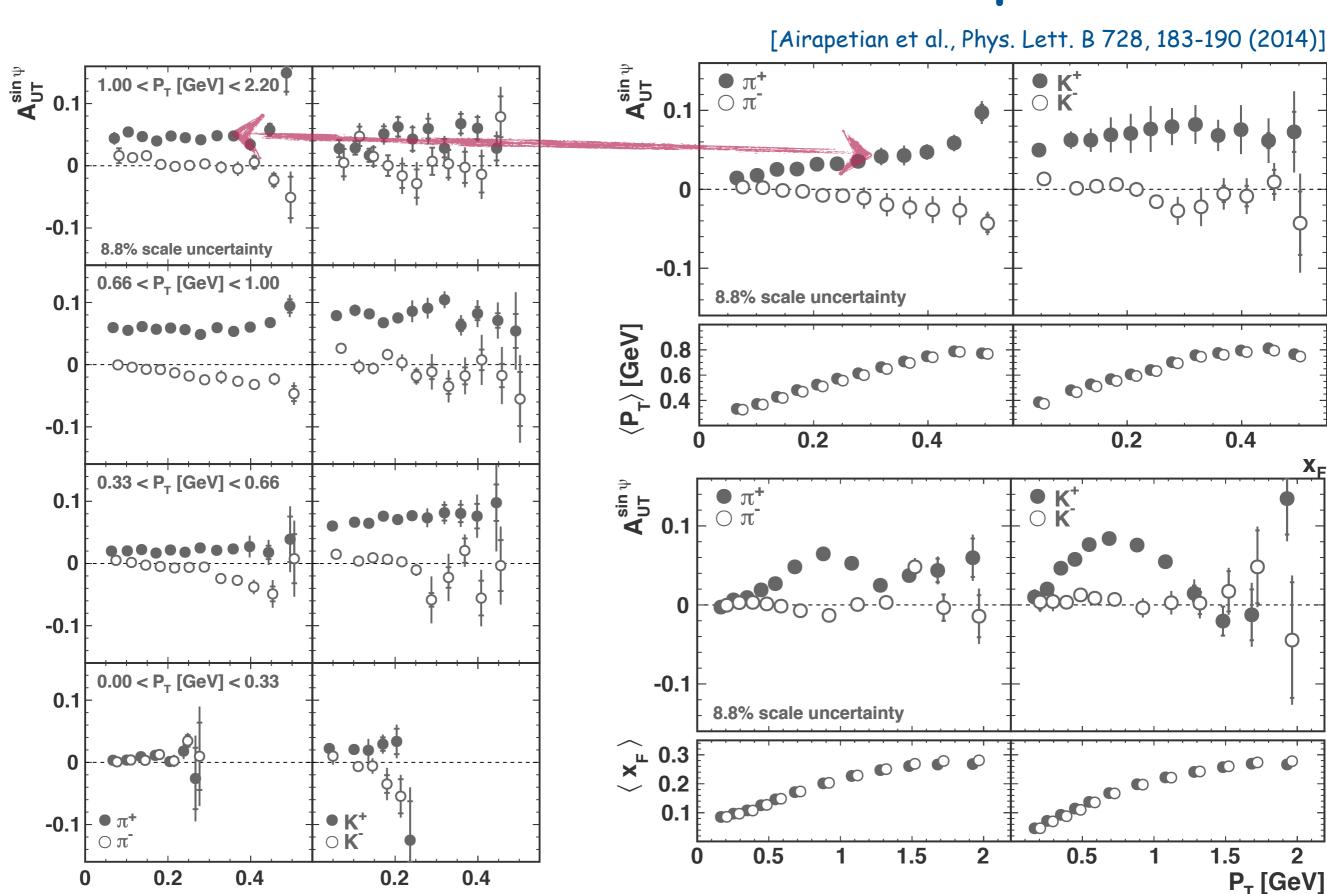
• increasing with  $x_F$  (as in pp)



- initially increasing with  $P_T$  with a fall-off at larger  $P_T$
- x<sub>F</sub> and P<sub>T</sub> correlated
  - → look at 2D dependences

[Airapetian et al., Phys. Lett. B 728, 183-190 (2014)] -0.1 8.8% scale uncertainty 0000000000 8.0 0.6 0.2 0.4 0.2 0.4 -0.1 8.8% scale uncertainty × 0.3 0.1 0.5 1.5 0.5 2 P<sub>+</sub> [GeV]

INT-18-3, Seattle



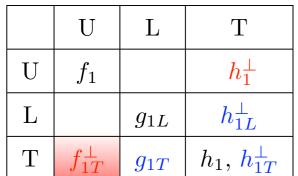
44

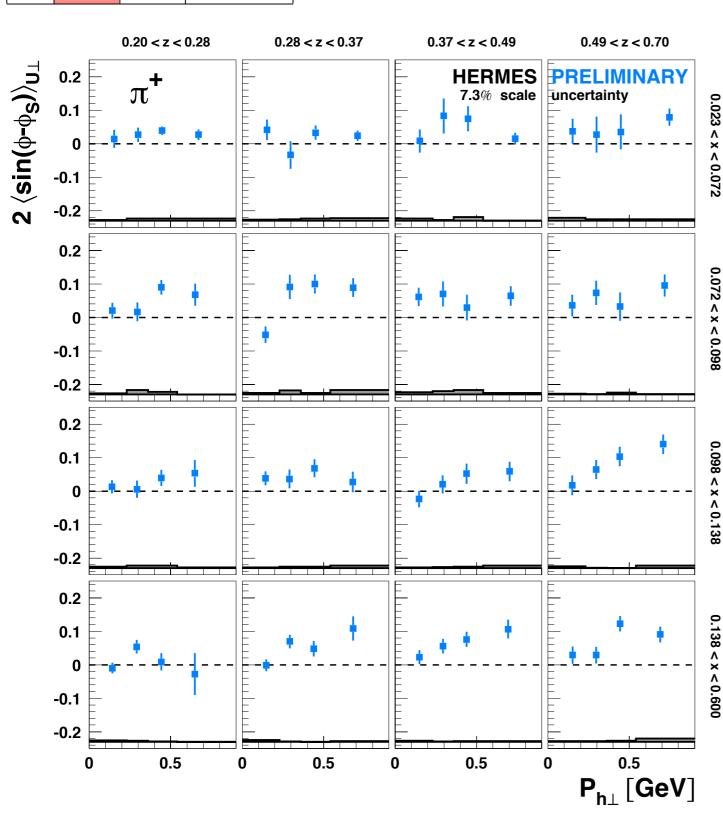
INT-18-3, Seattle

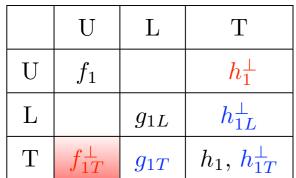
 $X_{\mathsf{F}}$ 

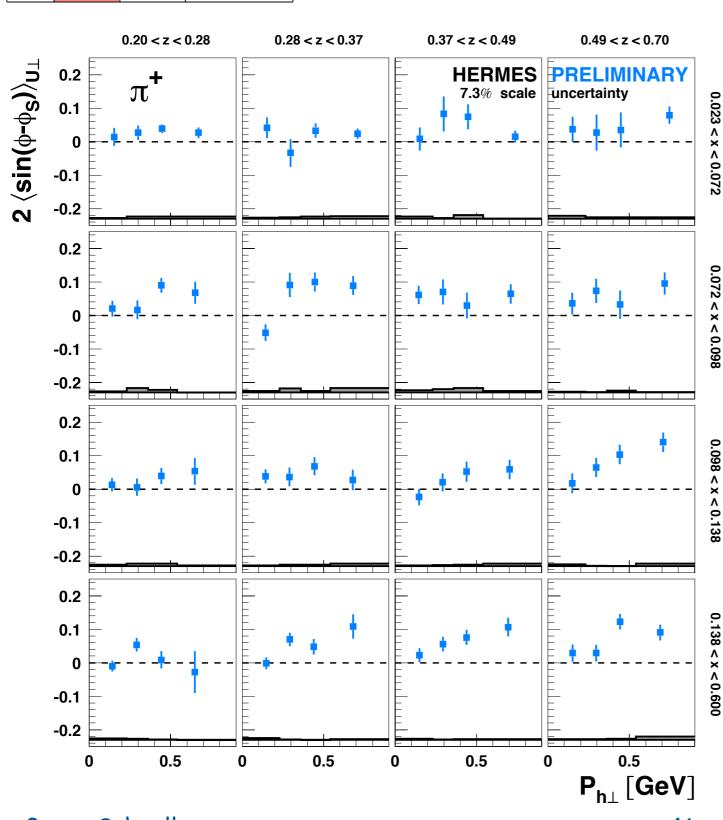
Gunar Schnell

# back to SIDIS

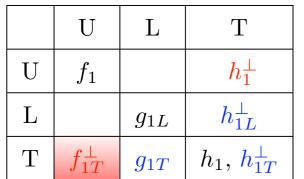


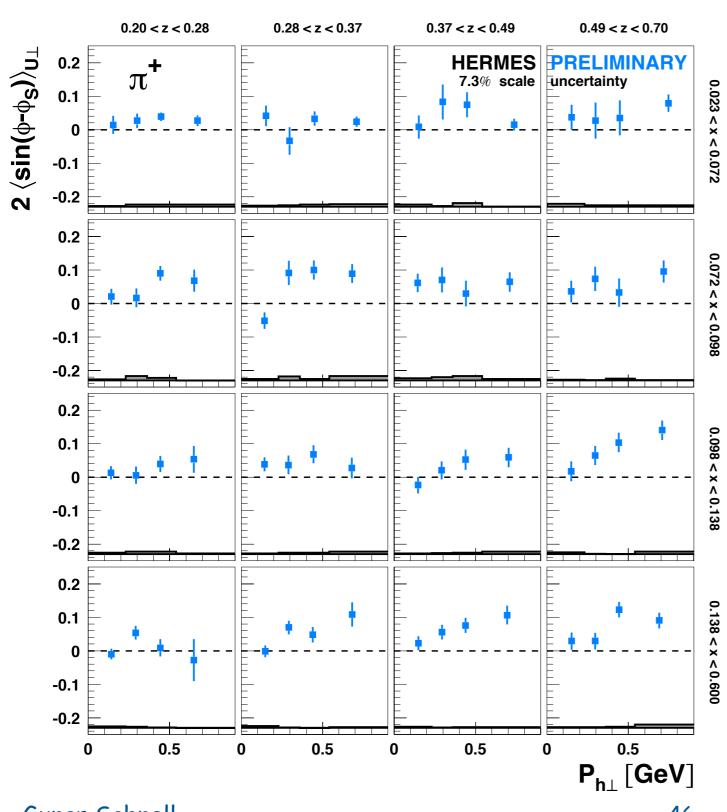




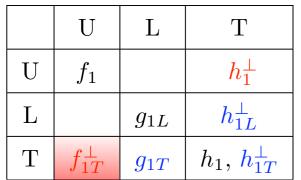


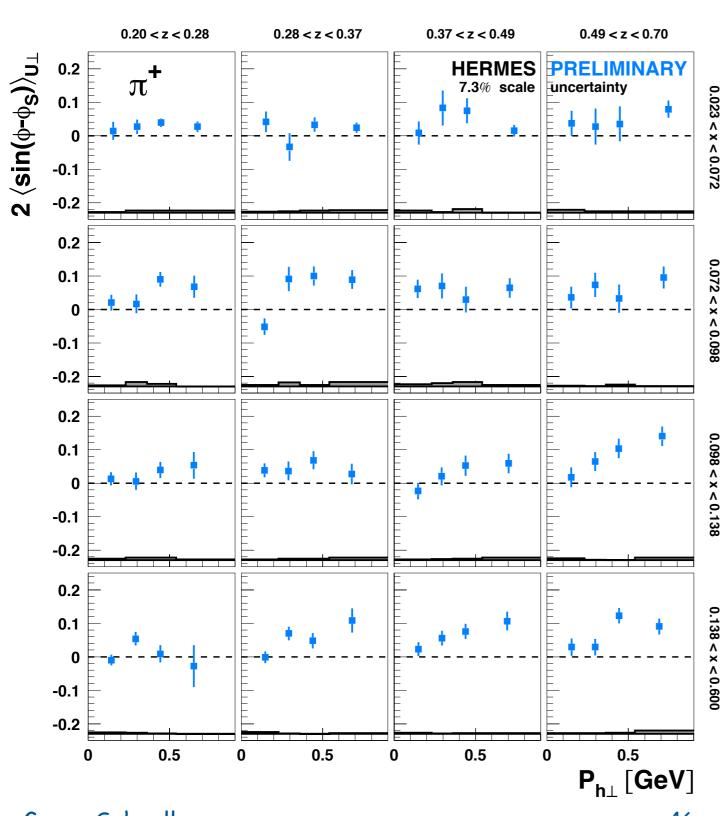
• 3d analysis: 4x4x4 bins in  $(x,z, P_{h\perp})$ 





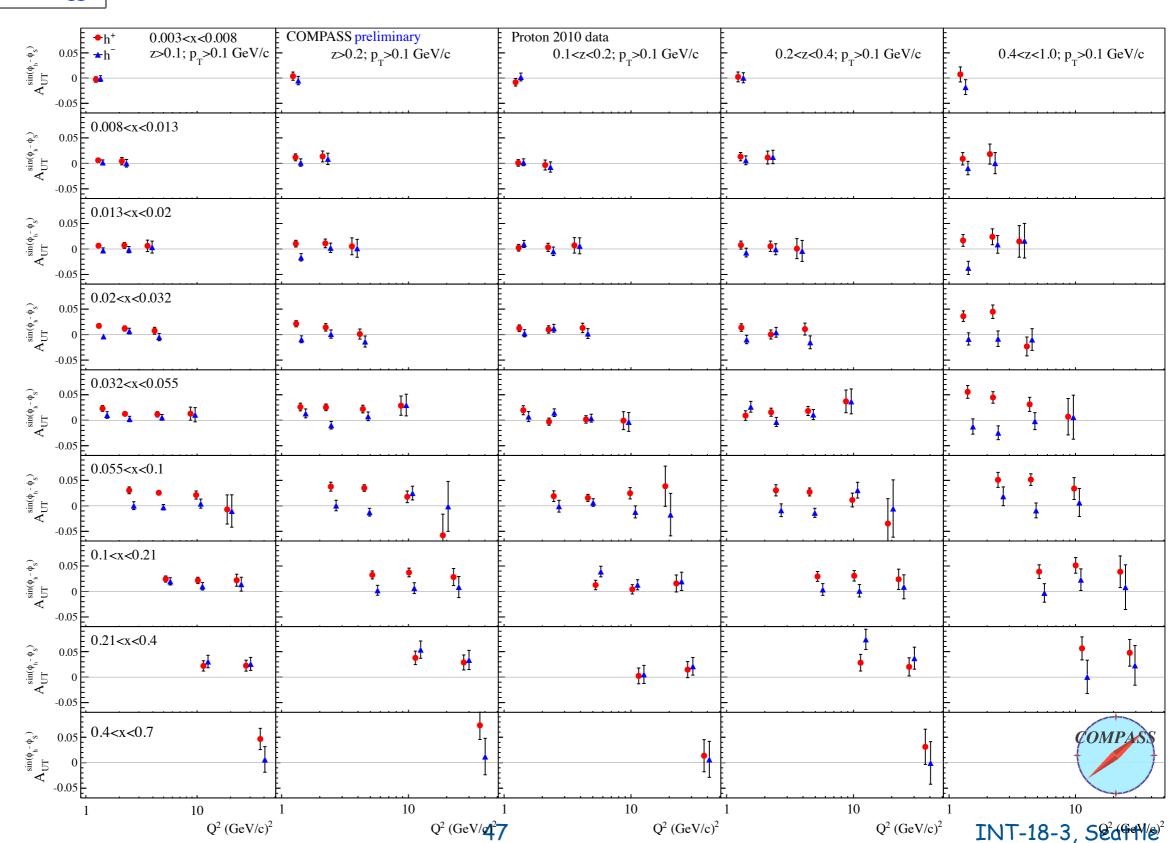
- 3d analysis: 4x4x4 bins in  $(x,z, P_{h\perp})$
- reduced systematics
- disentangle correlations
- isolate phase-space region with large signal strength





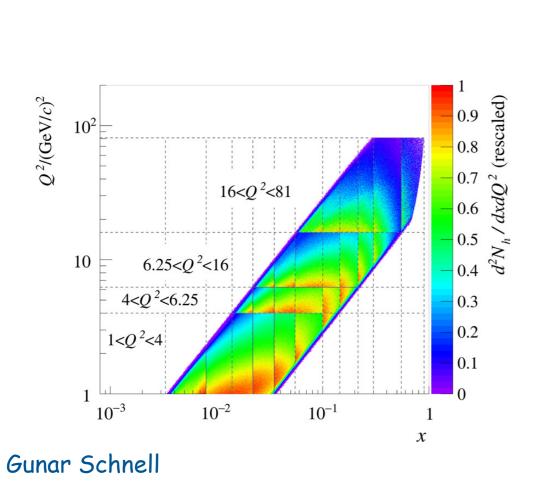
- 3d analysis: 4x4x4 bins in  $(x,z, P_{h\perp})$
- reduced systematics
- disentangle correlations
- isolate phase-space region with large signal strength
- allows more detailed comparison with calculations

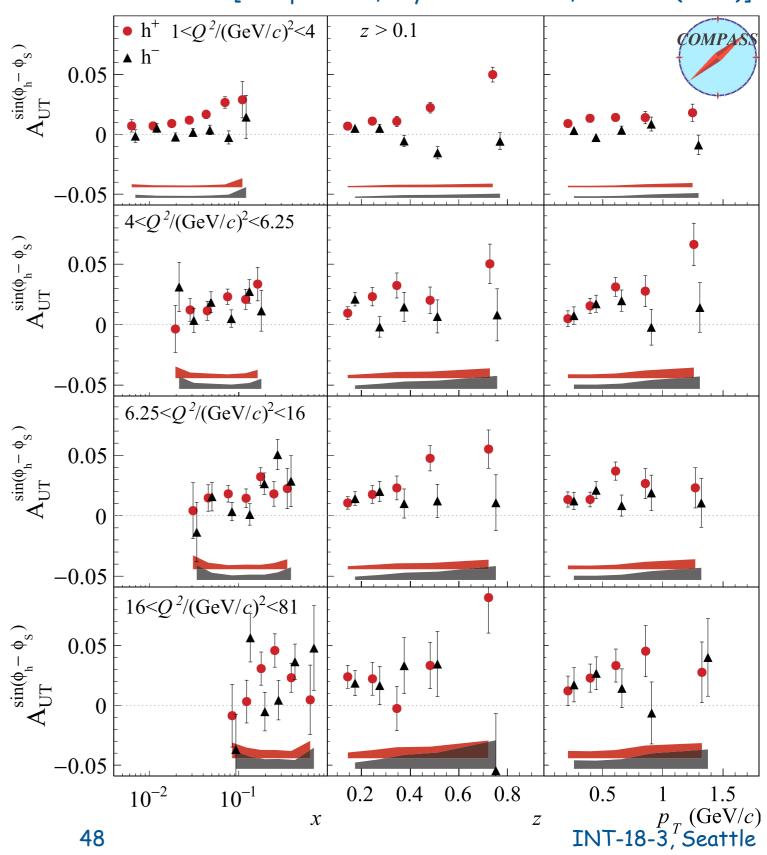
	U	L	Т
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$



	U	${ m L}$	m T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

[Adolph et al., Phys. Lett. B 770, 138-145 (2017)]

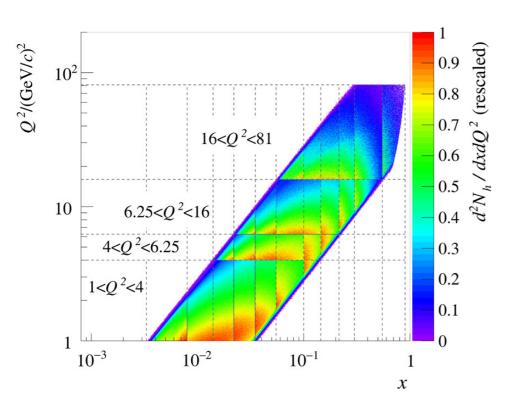


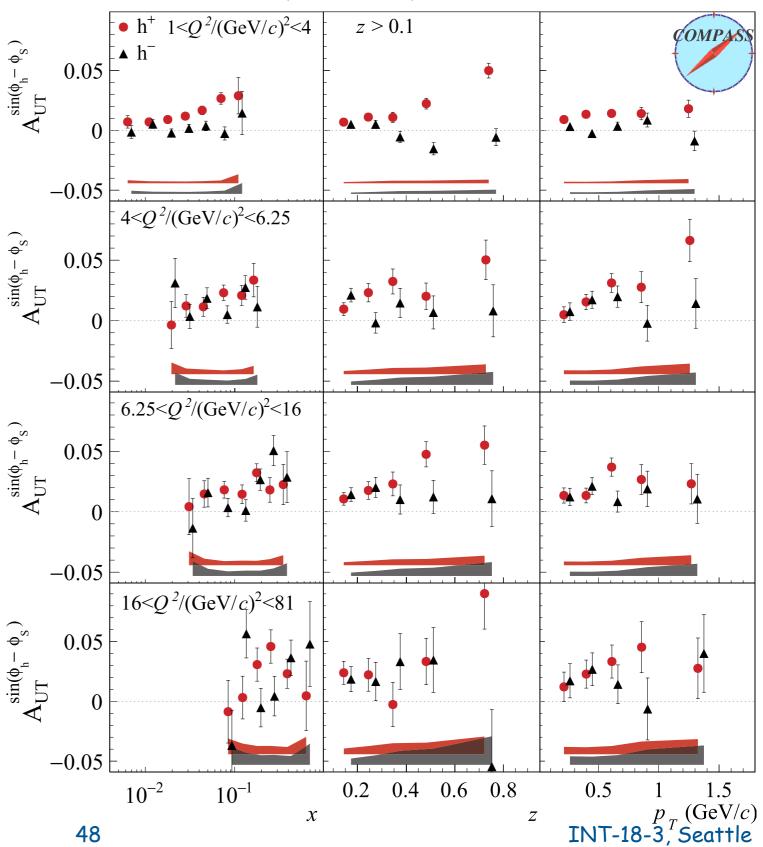


	U	${ m L}$	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

[Adolph et al., Phys. Lett. B 770, 138-145 (2017)]

2d analysis to match Q<sup>2</sup>
 range probed in Drell-Yan



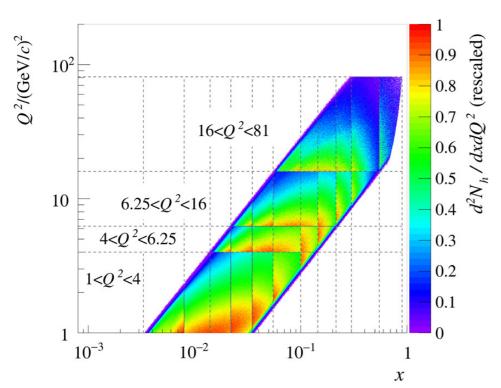


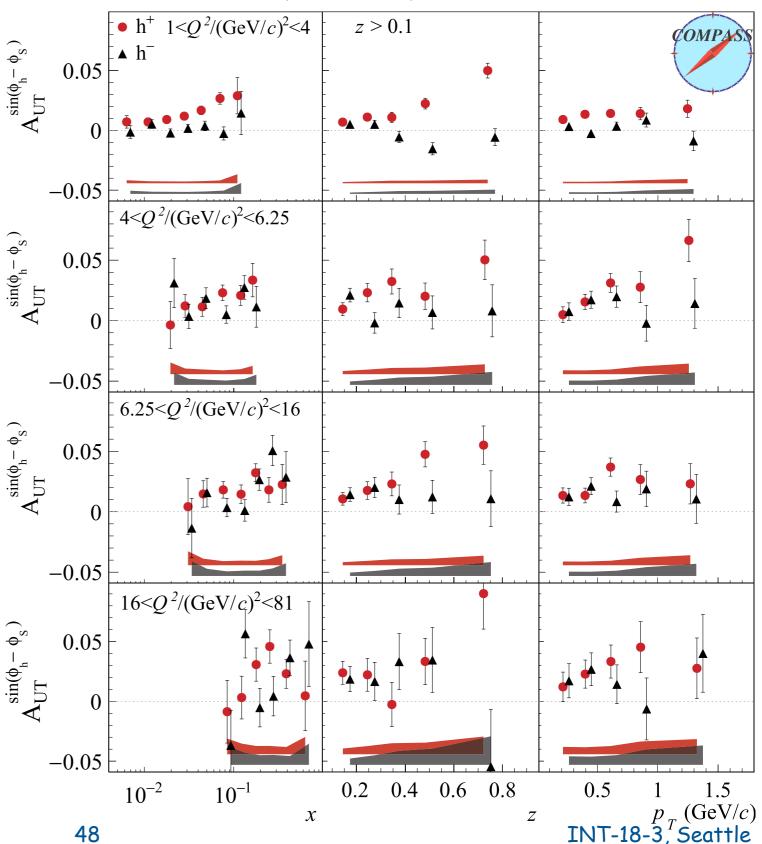
Gunar Schnell

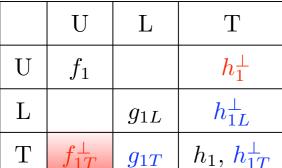
	U	${ m L}$	$\Gamma$
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
T	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

[Adolph et al., Phys. Lett. B 770, 138-145 (2017)]

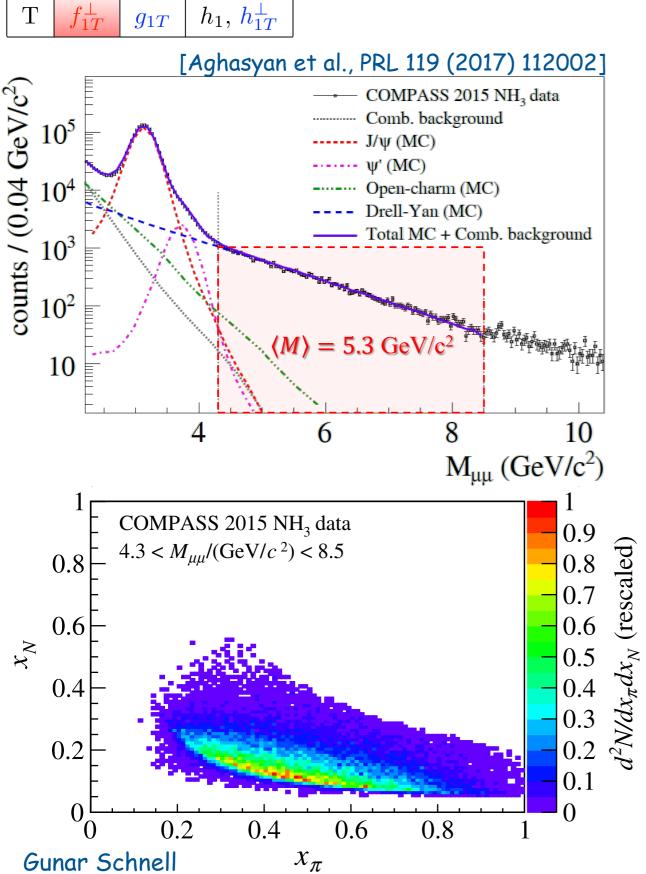
- 2d analysis to match Q<sup>2</sup>
   range probed in Drell-Yan
- allows also more detailed evolution studies



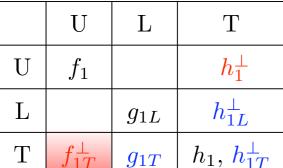




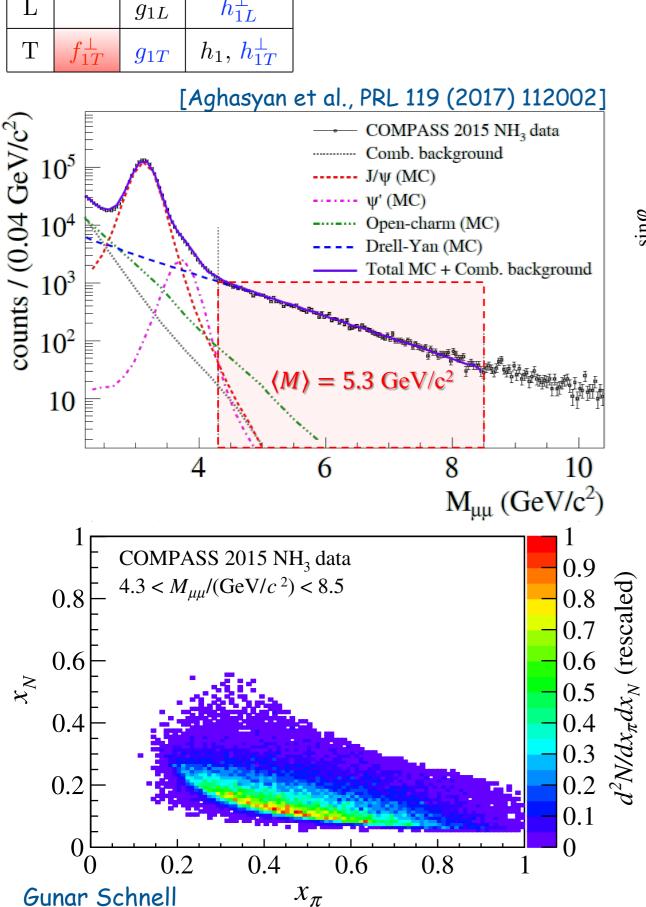
#### Sivers amplitudes - Drell-Yan

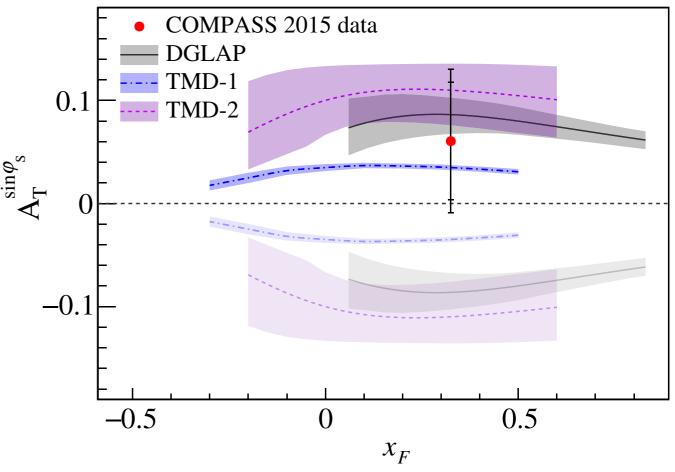


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#### Sivers amplitudes - Drell-Yan



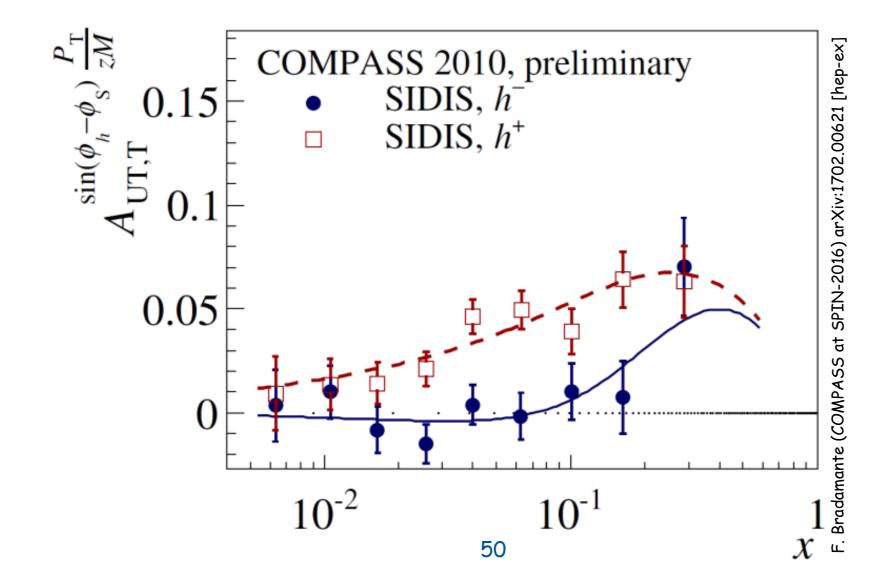


- (slight) preference for sign change
- some model curves move around when properly adjusted to exp.'s kinematics
- more data currently taken

	U	${ m L}$	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

# Sivers amplitudes - weighted

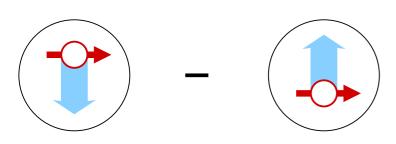
- $\bullet$   $P_{h\perp}$  weighting, in principle, resolves convolutions [A. Kotzinian and P. Mulders, PLB 406 (1997) 373)]
- requires excellent control of detector efficiencies
- often no full integral (low- and high- $P_{h\perp}$  missing)



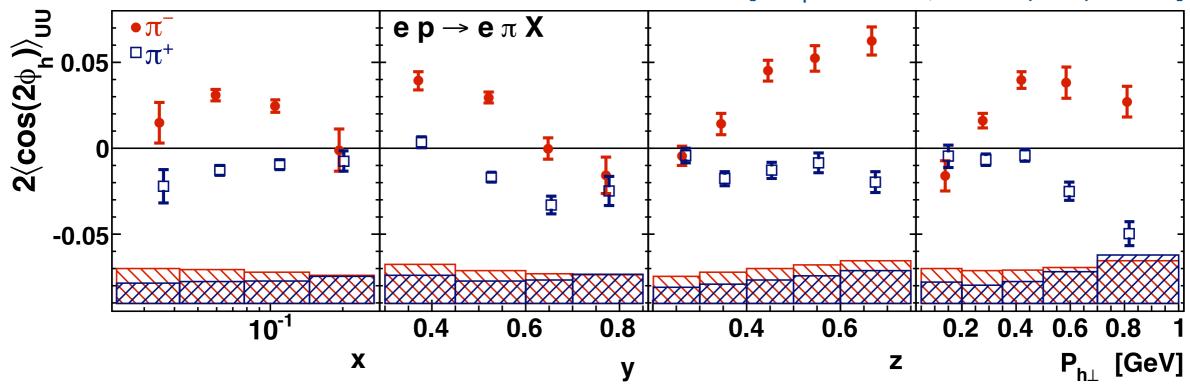
modulations in spin-independent SIDIS cross section

$$\frac{\mathrm{d}^5 \sigma}{\mathrm{d}x \, \mathrm{d}y \, \mathrm{d}z \, \mathrm{d}\phi_h \, \mathrm{d}P_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \left( 1 + \frac{\gamma^2}{2x} \right) \left\{ A(y) F_{\mathrm{UU},\mathrm{T}} + B(y) F_{\mathrm{UU},\mathrm{L}} + C(y) \cos \phi_h F_{\mathrm{UU}}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{\mathrm{UU}}^{\cos 2\phi_h} \right\}$$

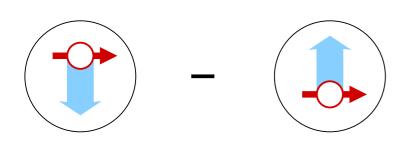
$$\begin{array}{c} \text{leading twist} \\ F_{UU}^{\cos 2\phi_h} \propto C \\ \hline - \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} \\ \hline \text{next to leading twist} \\ \hline F_{UU}^{\cos \phi_h} \propto \frac{2M}{C} \\ \hline - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} x \ h_1^\perp H_1^\perp \\ \hline \end{array} \\ \text{Interaction dependent} \\ \hline \text{terms neglected} \\ \text{(Implicit sum over quark flavours)} \\ \end{array}$$



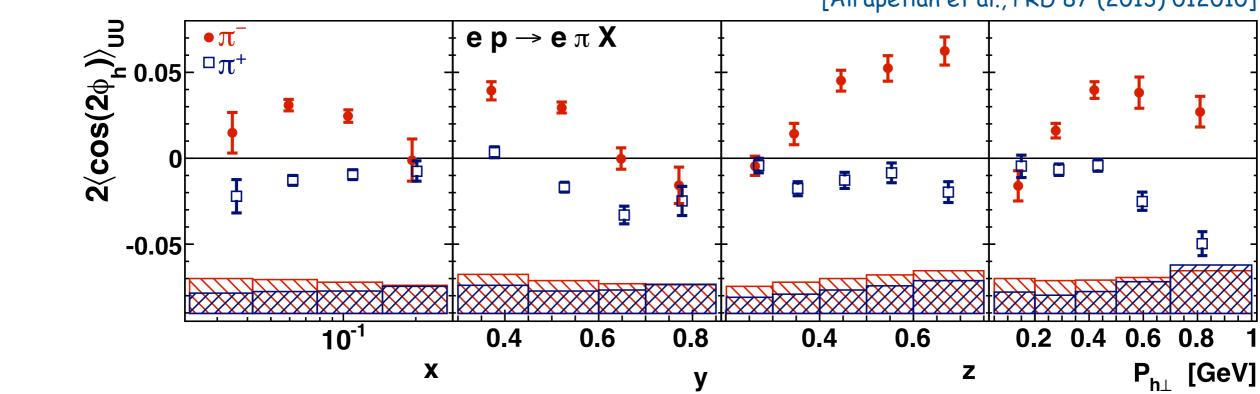
[Airapetian et al., PRD 87 (2013) 012010]



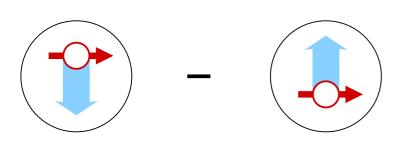
not zero!

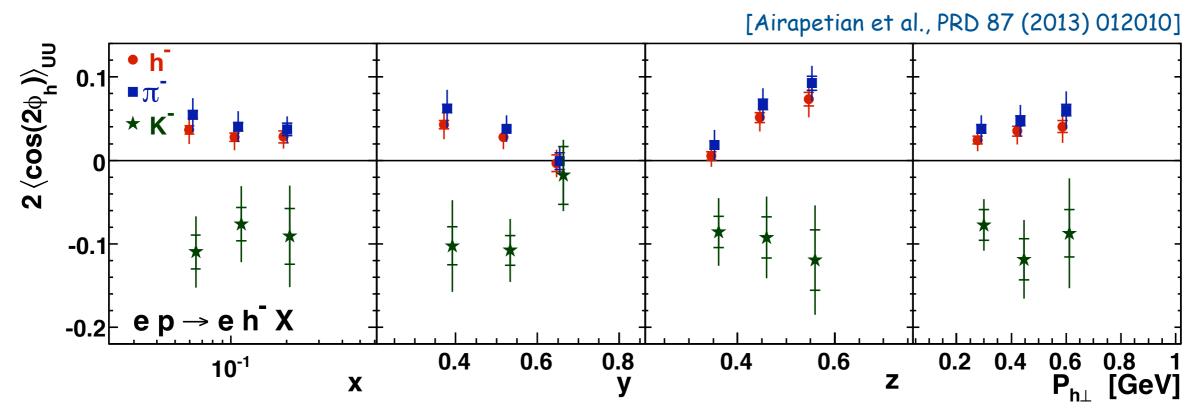


[Airapetian et al., PRD 87 (2013) 012010]

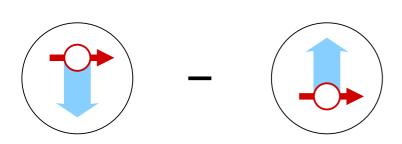


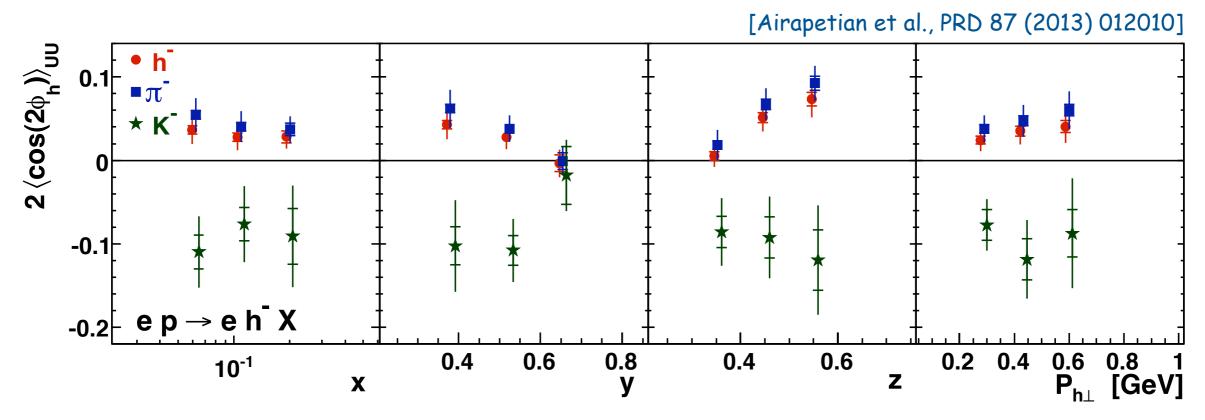
- not zero!
- opposite sign for charged pions with larger magnitude for  $\pi^-$  -> same-sign BM-function for valence quarks?





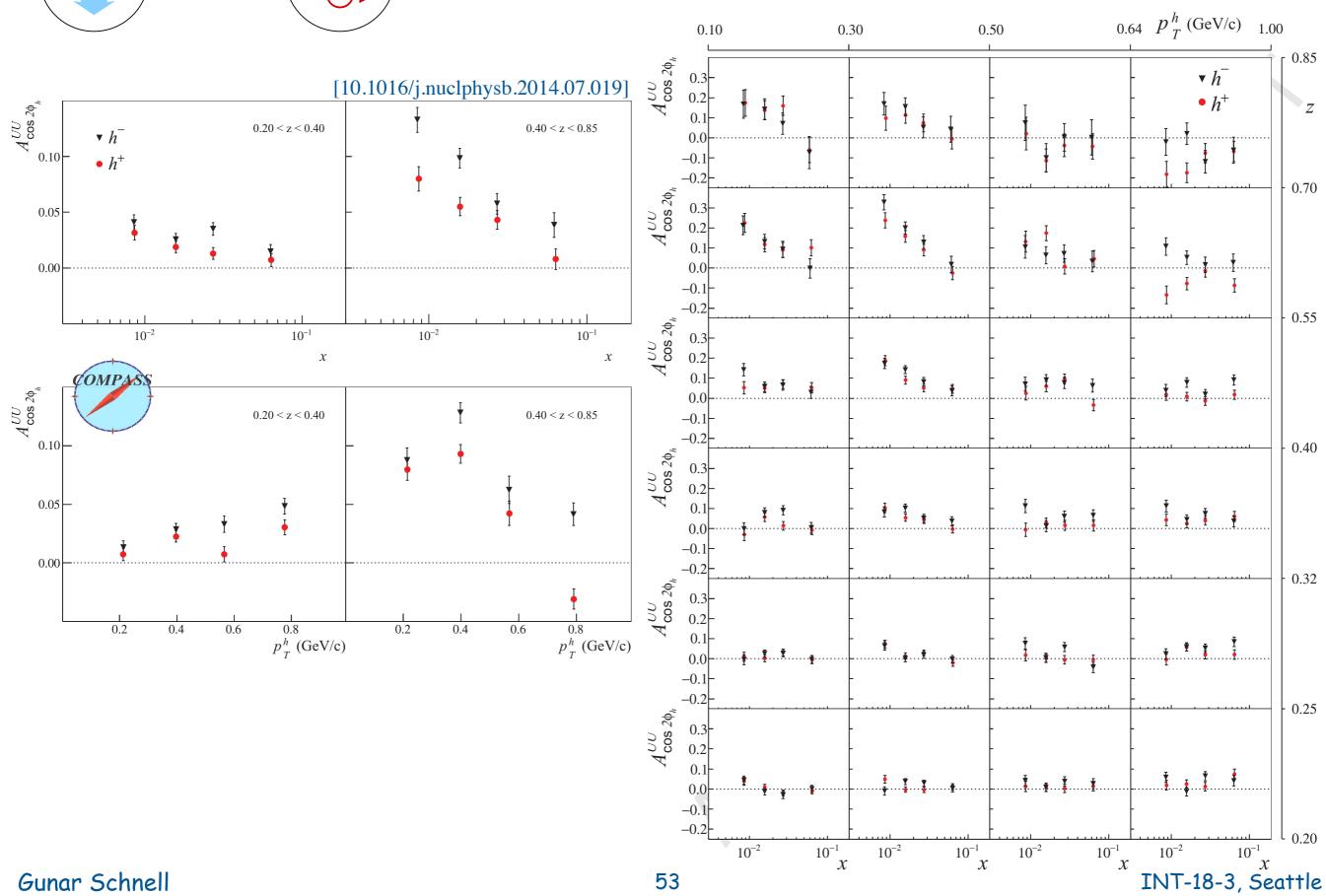
- not zero!
- opposite sign for charged pions with larger magnitude for  $\pi^-$  -> same-sign BM-function for valence quarks?
- intriguing behavior for kaons



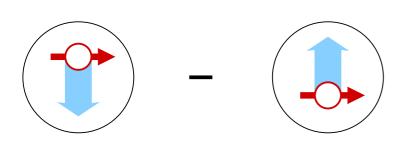


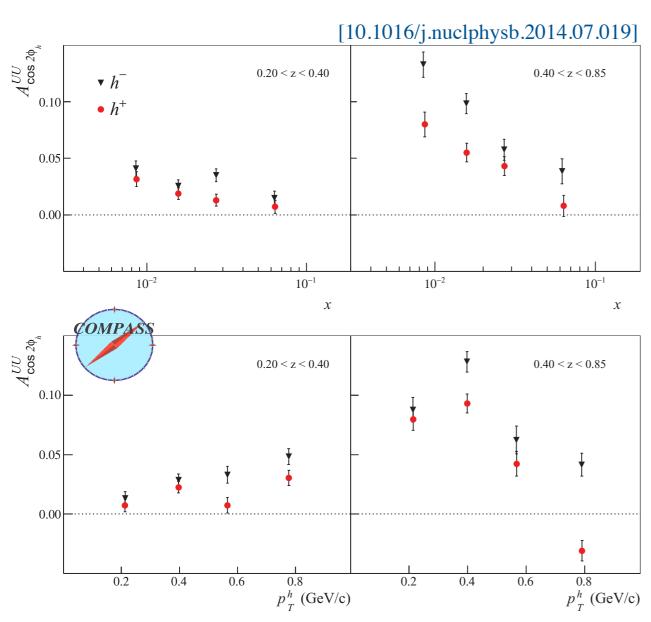
- not zero!
- opposite sign for charged pions with larger magnitude for  $\pi^-$  -> same-sign BM-function for valence quarks?
- intriguing behavior for kaons
- available in multidimensional binning both from HERMES and from COMPASS





53





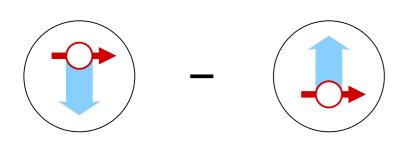
 $_{0.64}$   $p_T^h$  (GeV/c)  $_{1.00}$ 0.50 0.30 0.85  $A_{\cos2\phi_n}^{UU}$ 0.3  $A_{\cos 2\phi_h}^{UU}$ 0.55  $A_{\cos 2\phi_{\scriptscriptstyle h}}^{\scriptscriptstyle UU}$ 0.2  $A_{\cos2\phi_{_{h}}}^{UU}$  $A_{\cos2\phi_{\scriptscriptstyle h}}^{\scriptscriptstyle UU}$  $A_{\cos2\phi_n}^{UU}$ 0.25 -0.1 $10^{-2}$  $10^{-2}$  $10^{-1}$  $10^{-1}$  $10^{-2}$  $10^{-1}$  $10^{-2}$  $10^{-1}$  $\chi$ 

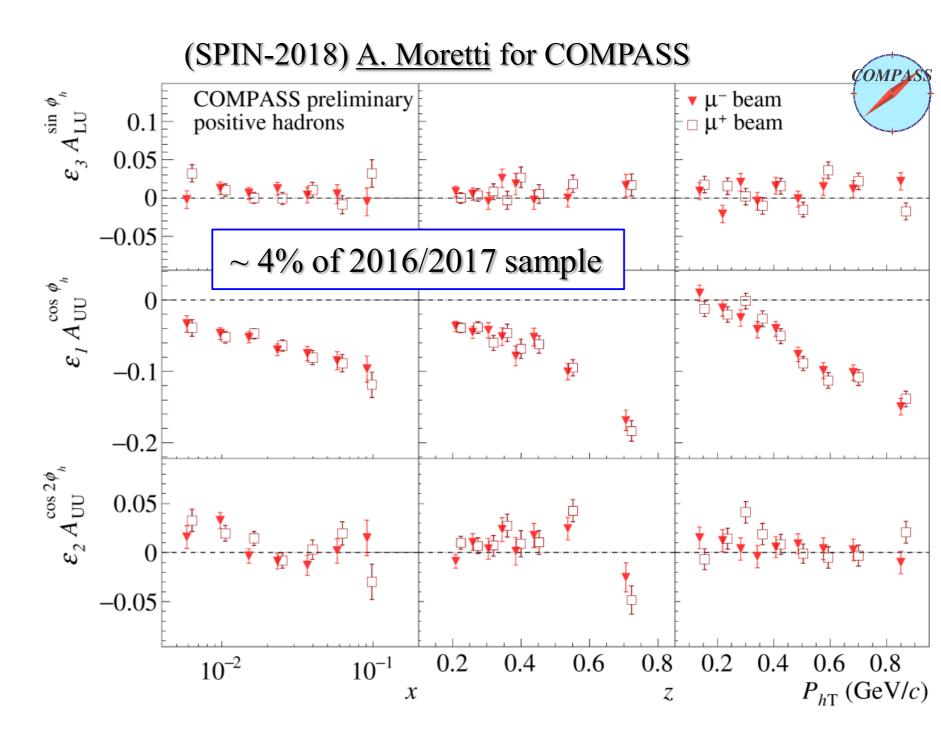
INT-18-3, Seattle

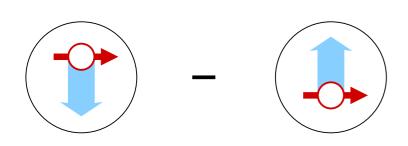
 $\chi$ 

53

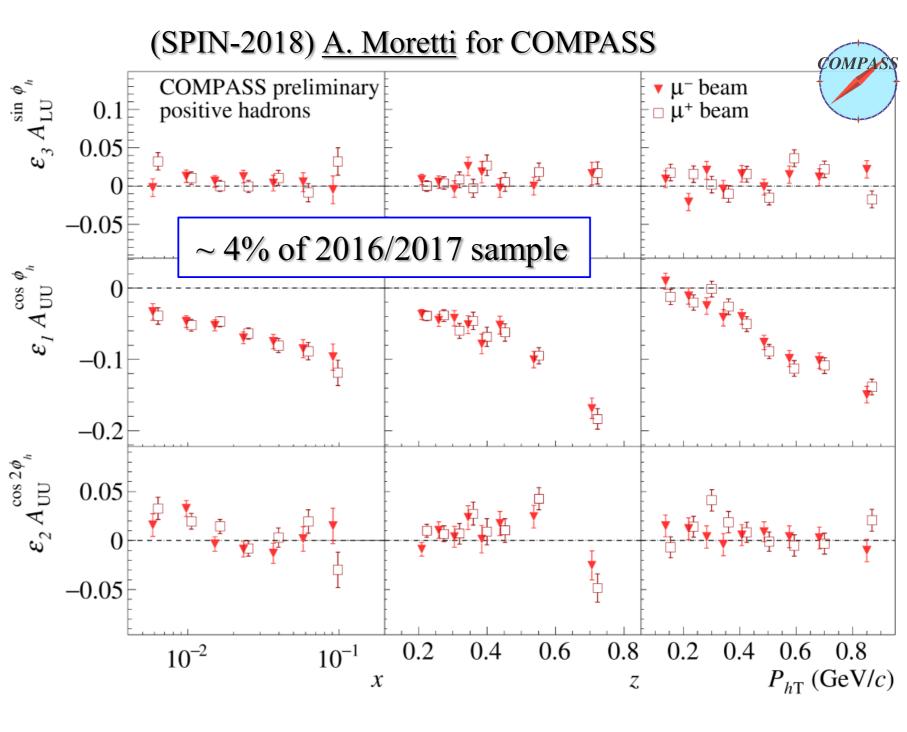
unlike HERMES same sign for h<sup>+</sup> and h<sup>-</sup>, though still different from each other

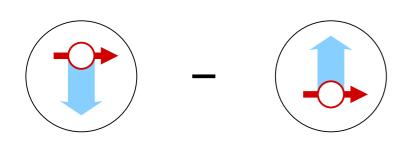






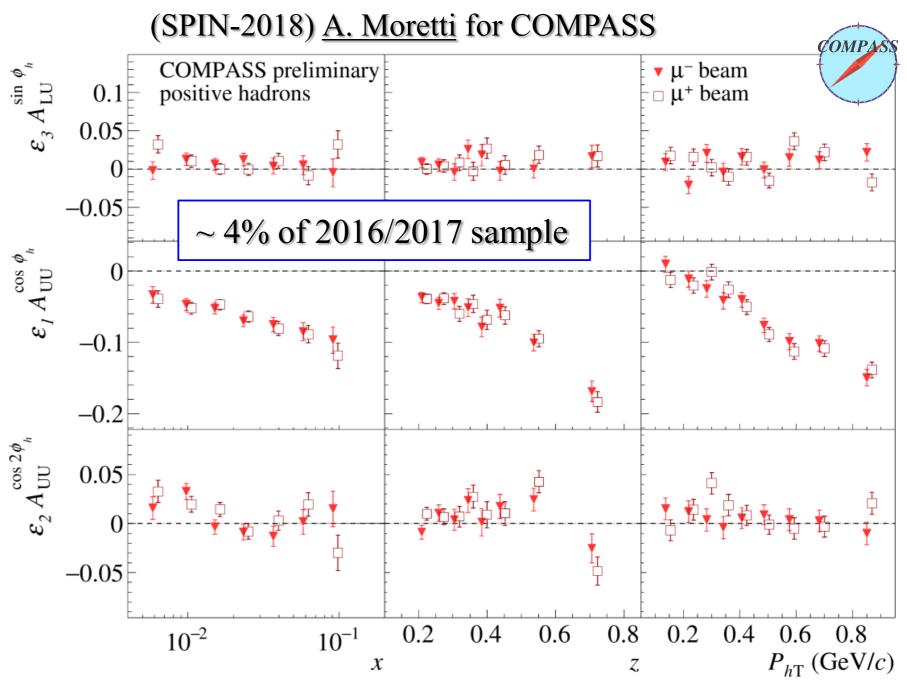
in 2016/17 extensive strain data set collected on strain liquid-H target (DVCS program)





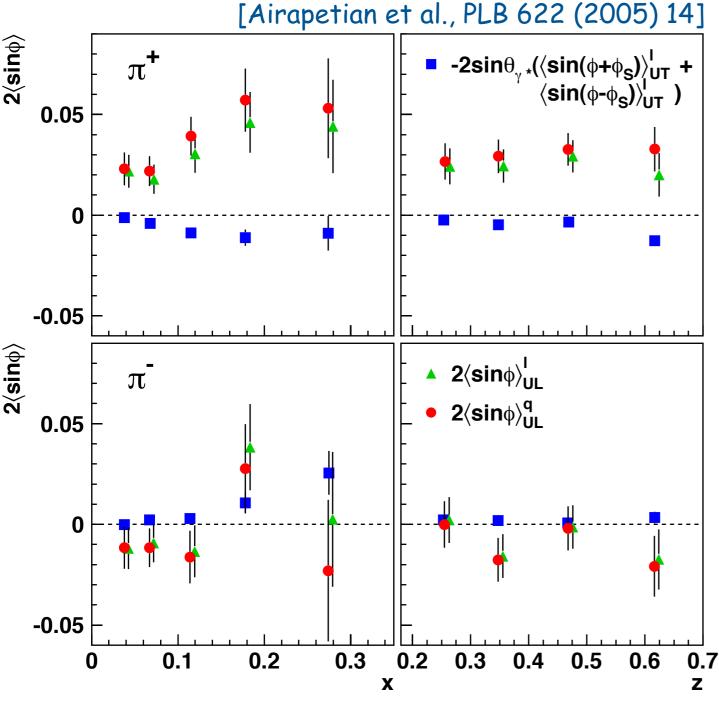
### signs of Boer-Mulders

- in 2016/17 extensive strain data set collected on strain liquid-H target (DVCS program)
- will allow precision studies of multiplicities and Auu & Alu modulations



# non-vanishing twist-3

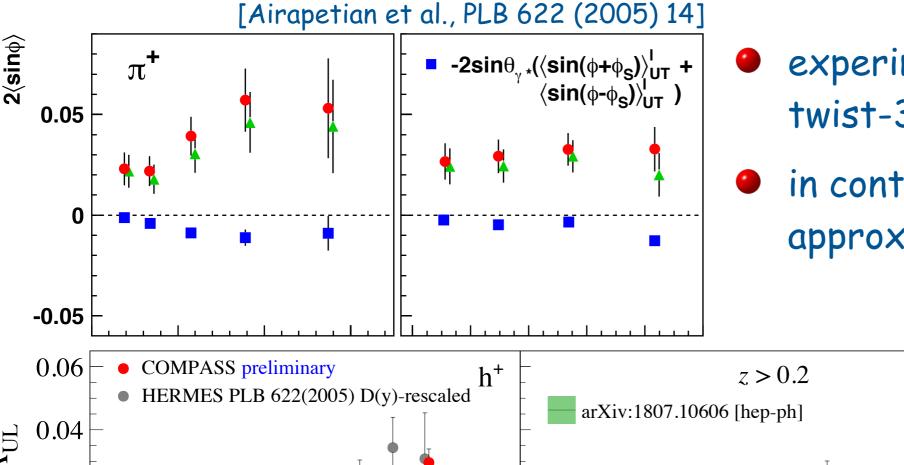
$$\left\langle \sin \phi \right\rangle_{UL}^{\mathsf{q}} = \left\langle \sin \phi \right\rangle_{UL}^{\mathsf{I}} + \sin \theta_{\gamma^*} \left( \left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^{\mathsf{I}} + \left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^{\mathsf{I}} \right)$$



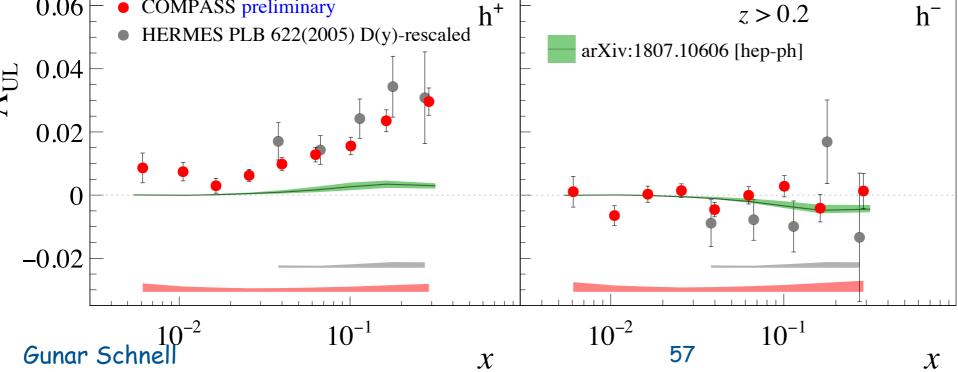
- $\bullet$  experimental  $A_{UL}$  dominated by twist-3 contribution
  - correction for A<sub>UT</sub>
     contribution increases purely longitudinal asymmetry for positive pions
  - consistent with zero for  $\pi^-$

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$$\left\langle \sin \phi \right\rangle_{UL}^{\mathsf{q}} = \left\langle \sin \phi \right\rangle_{UL}^{\mathsf{I}} + \sin \theta_{\gamma^*} \left( \left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^{\mathsf{I}} + \left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^{\mathsf{I}} \right)$$

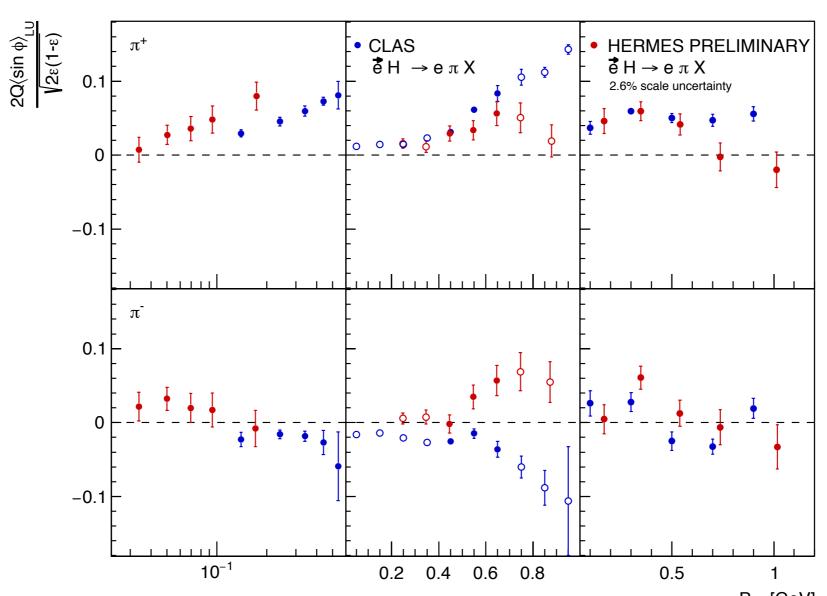


- $\bullet$  experimental  $A_{UL}$  dominated by twist-3 contribution
- in contrast to WW-type approximation [1807.10606]



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$$\frac{M_h}{Mz}h_1^{\perp}E \oplus xg^{\perp}D_1 \oplus \frac{M_h}{Mz}f_1G^{\perp} \oplus xeH_1^{\perp}$$



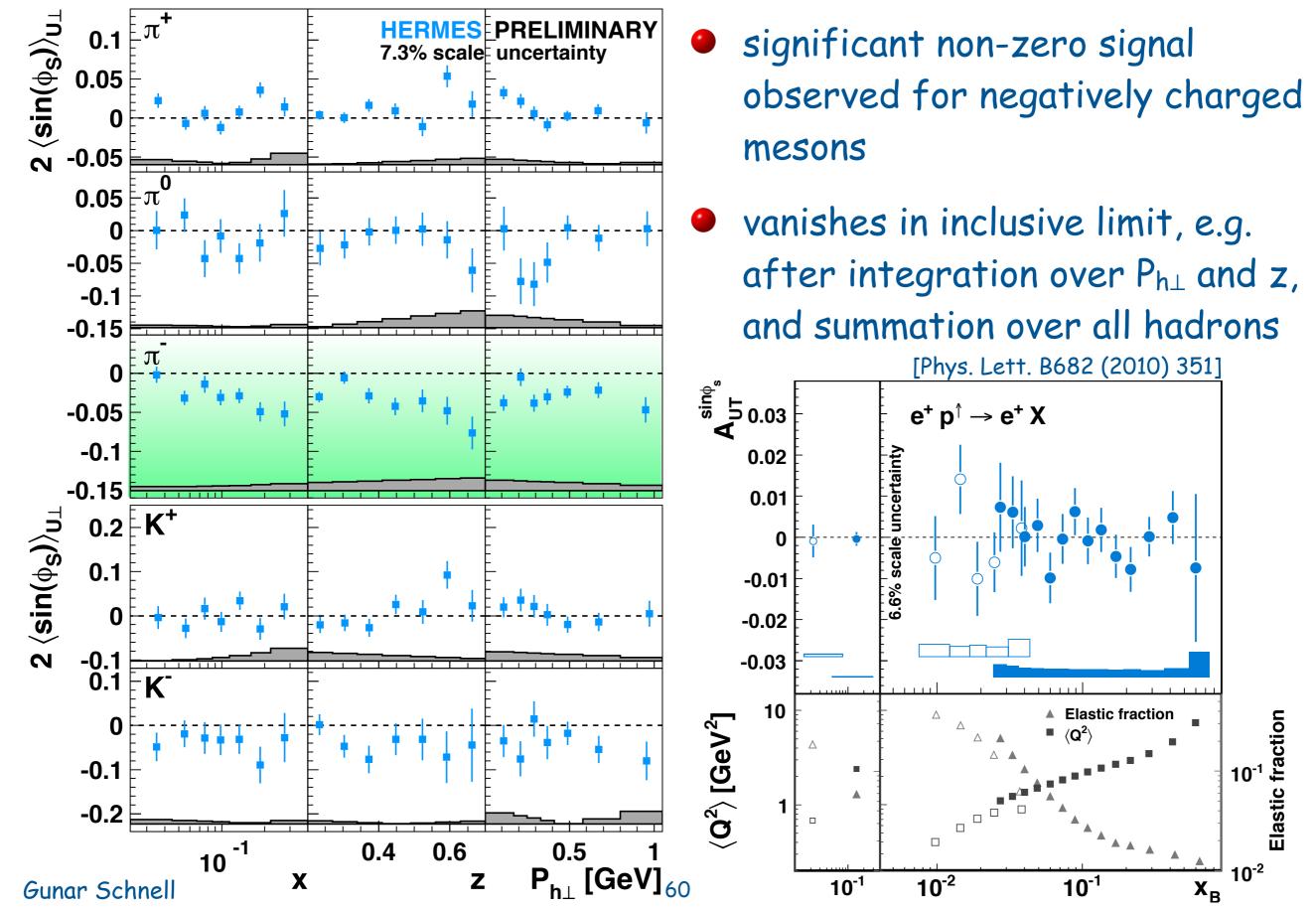
- opposite behavior at HERMES/CLAS of negative pions in z projection due to different x-range probed
- CLAS more sensitive to e(x)Collins term due to higher x probed?

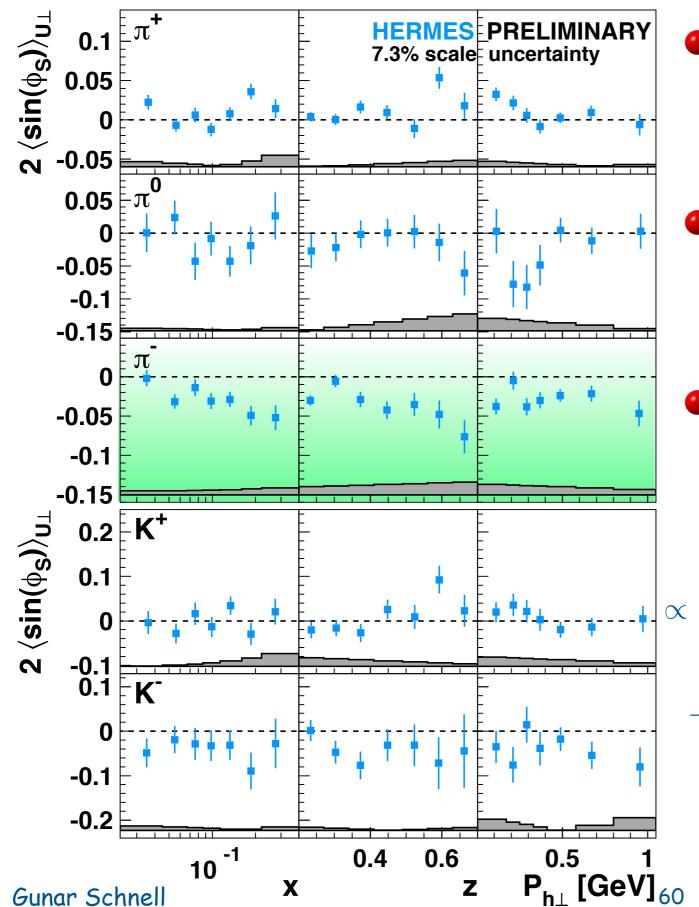
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#### subleading twist II - <sin(\$)>LU

$$\frac{M_h}{Mz}h_1^\perp E \oplus xg^\perp D_1 \oplus \frac{M_h}{Mz}f_1G^\perp \oplus xeH_1^\perp$$

 consistent behavior for charged pions / hadrons at HERMES / COMPASS for isoscalar targets

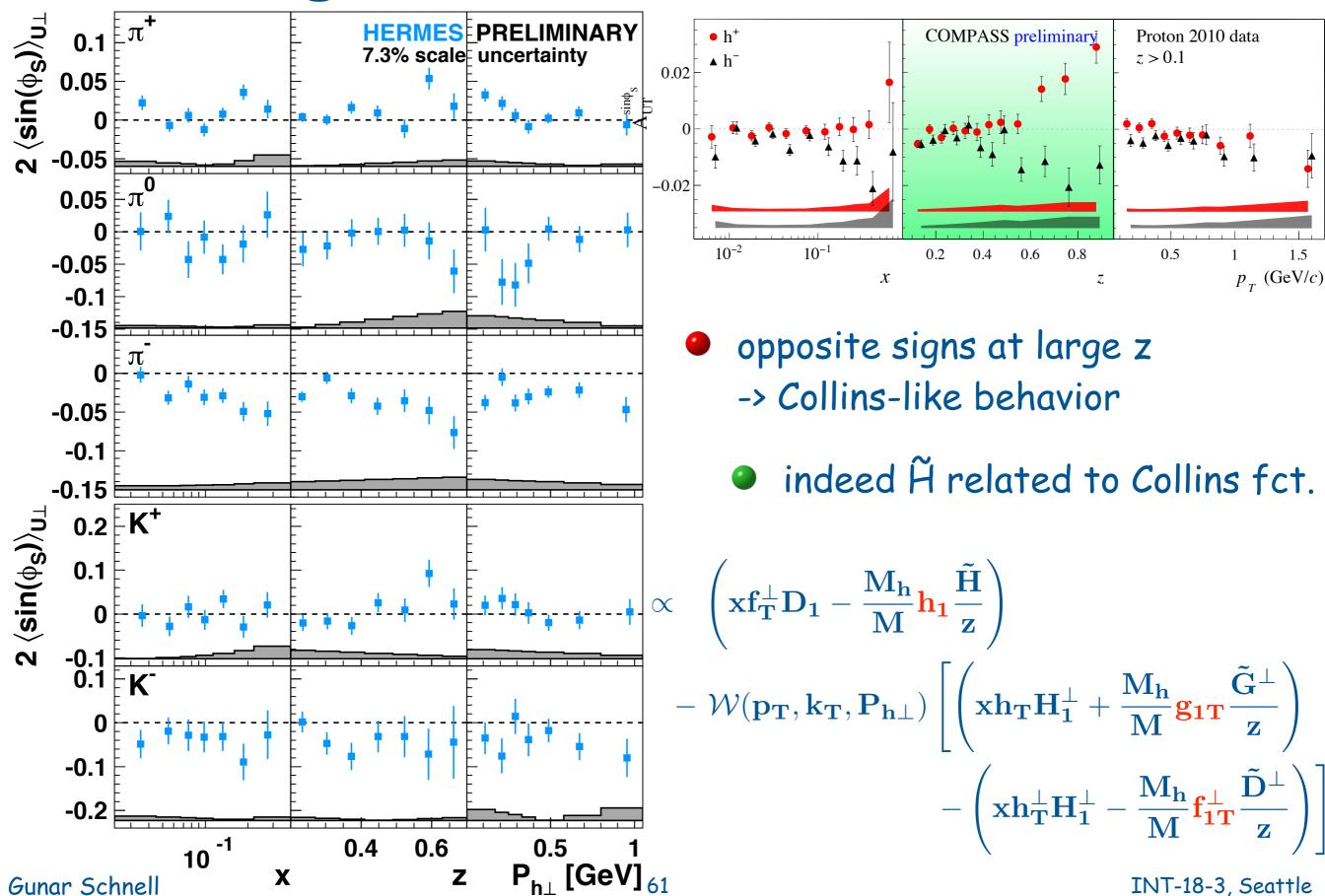




- significant non-zero signal observed for negatively charged mesons
- vanishes in inclusive limit, e.g. after integration over  $P_{h\perp}$  and z, and summation over all hadrons
- various terms related to transversity, worm-gear, Sivers etc.:

$$\left(\mathbf{x}\mathbf{f}_{\mathbf{T}}^{\perp}\mathbf{D_{1}}-rac{\mathbf{M_{h}}}{\mathbf{M}}\mathbf{h_{1}}rac{ ilde{\mathbf{H}}}{\mathbf{z}}
ight)$$

$$-~\mathcal{W}(\mathbf{p_T}, \mathbf{k_T}, \mathbf{P_{h\perp}}) \left[ \left( \mathbf{xh_T} \mathbf{H_1^{\perp}} + \frac{\mathbf{M_h}}{\mathbf{M}} \mathbf{g_{1T}} \frac{\mathbf{\tilde{G}^{\perp}}}{\mathbf{z}} \right) \right. \\ \left. - \left( \mathbf{xh_T^{\perp}} \mathbf{H_1^{\perp}} - \frac{\mathbf{M_h}}{\mathbf{M}} \mathbf{f_{1T}^{\perp}} \frac{\mathbf{\tilde{D}^{\perp}}}{\mathbf{z}} \right) \right.$$



0.4

X

10

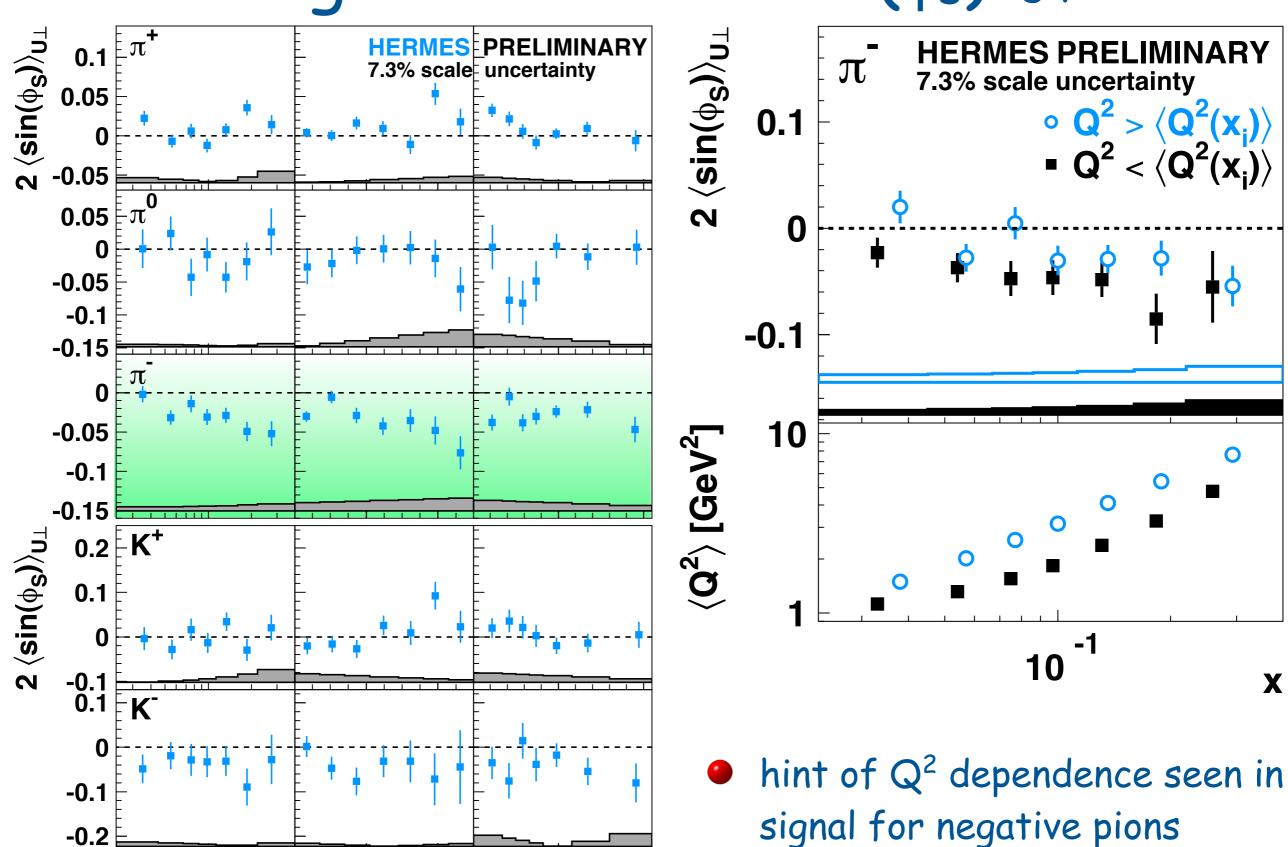
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0.6

Z

0.5

 $P_{h\perp}$  [GeV]<sub>62</sub>



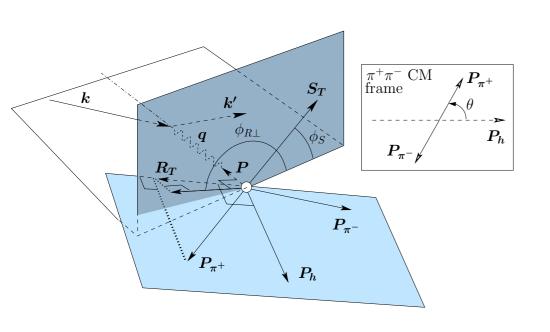
#### conclusions

- 1st round of SIDIS measurements coming to an end
- various indications of flavor-& spin-dependent transverse momentum
- transversity is non-zero and quite sizable
  - d-quark transversity difficult to access with only proton targets
- Sivers and chiral-even worm-gear function also clearly non-zero
- various sizable twist-3 effects
- highlights still to come
  - HERMES transverse-target, A<sub>LU</sub> & A<sub>LL</sub> asymmetries
  - COMPASS transverse d; high-statistics data set on unpol. pure H; multi-d asymmetries
- precision measurements needed to fully map TMD landscape (fully differential!)
- need also program with polarized D and <sup>3</sup>He

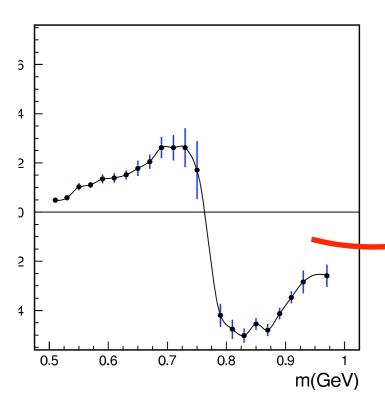
# backup

	U	$oxed{L}$	T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^\perp$

# Transversity (2-hadron fragmentation)



 $A_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sin\theta h_1 H_1^{\triangleleft}$ 



#### Jaffe et al. [hep-ph/9709322]:

$$H_1^{\triangleleft,sp}(z,M_{\pi\pi}^2) = \frac{\sin\delta_0\sin\delta_1\sin(\delta_0-\delta_1)H_1^{\triangleleft,sp'}(z)}{\delta_0\left(\delta_1\right) \to \mathsf{S}(\mathsf{P})\text{-wave phase shifts}}$$

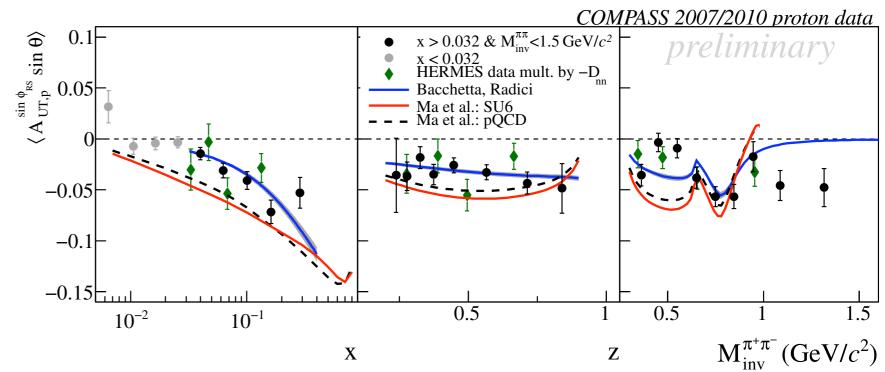
$$= \mathcal{P}(M_{\pi\pi}^2)H_1^{\triangleleft,sp'}(z)$$

 $\Rightarrow A_{UT}$  might depend strongly on  $M_{\pi\pi}$ 

	U	L	T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

# Transversity (2-hadron fragmentation)

[A. Airapetian et al., JHEP 06 (2008) 017] COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10] COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02]

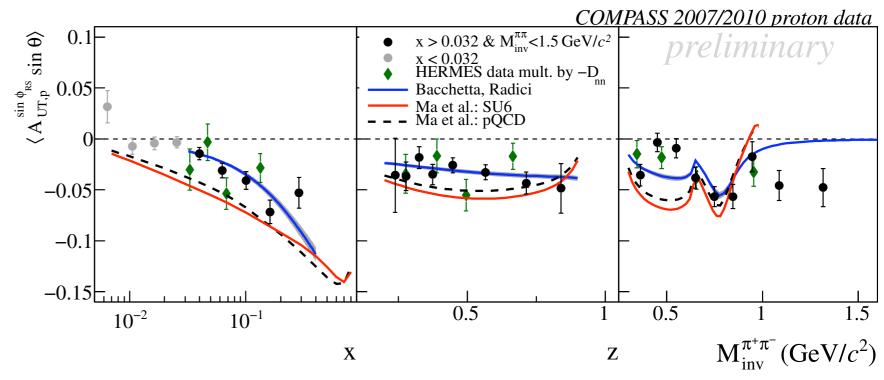


	U	L	T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^\perp$

# Transversity (2-hadron fragmentation)

HERMES, COMPASS:
 for comparison scaled
 HERMES data by
 depolarization factor and
 changed sign

[A. Airapetian et al., JHEP 06 (2008) 017] COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10] COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02]

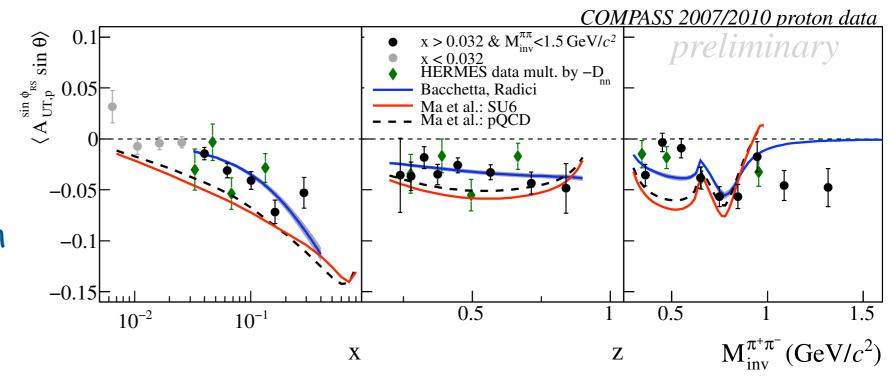


	U	L	${ m T}$
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
$\Gamma$	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^{\perp}$

# Transversity (2-hadron fragmentation)

- HERMES, COMPASS:
   for comparison scaled
   HERMES data by
   depolarization factor and
   changed sign
- <sup>2</sup>H results consistent with zero

[A. Airapetian et al., JHEP 06 (2008) 017] COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10] COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02]



	U	L	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

0.20 < z. < 0.27

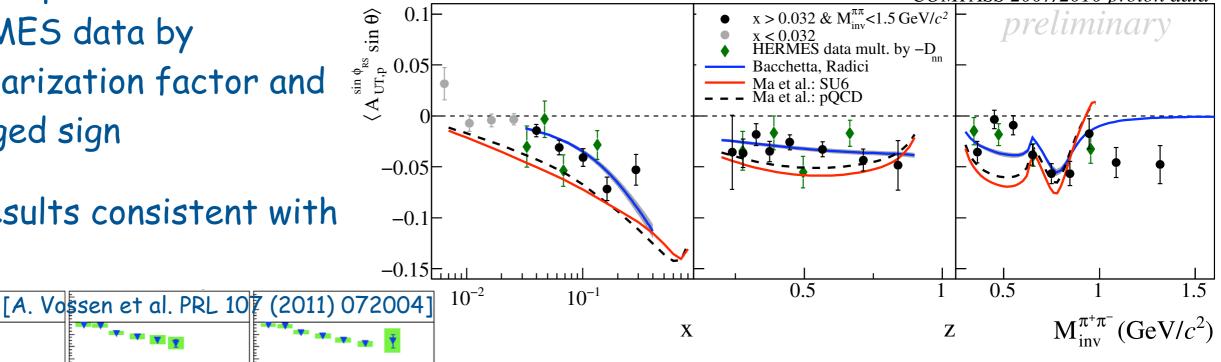
Gunar Schnell

# Transversity (2-hadron fragmentation)

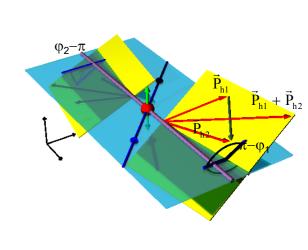
HERMES, COMPASS: for comparison scaled HERMES data by depolarization factor and changed sign

<sup>2</sup>H results consistent with zero

[A. Airapetian et al., JHEP 06 (2008) 017] COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10] COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02] COMPASS 2007/2010 proton data



data from e<sup>+</sup>e<sup>-</sup> by BELLE



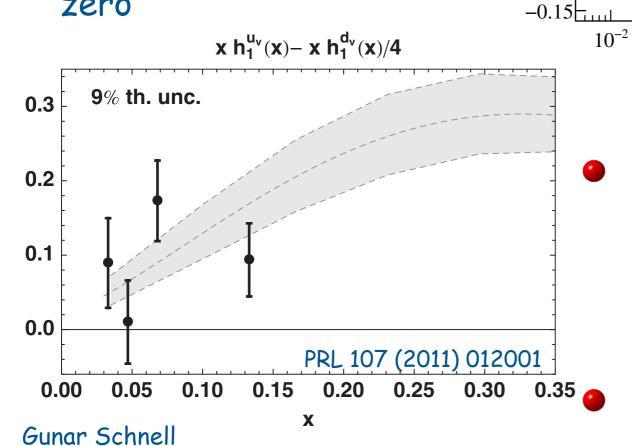
	U	${ m L}$	$oxed{T}$
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Τ	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

# (2-hadron fragmentation)

Transversity

- HERMES, COMPASS:
  for comparison scaled
  HERMES data by
  depolarization factor and
  changed sign
- <sup>2</sup>H results consistent with zero

[A. Airapetian et al., JHEP 06 (2008) 017] COMPASS 2007: [C. Adolph et al., Phys. Lett. B713 (2012) 10] COMPASS 2010: [C. Braun et al., Nuovo Cimento C 035 (2012) 02] COMPASS 2007/2010 proton data 0.1 0.1  $0.032 & M_{inv}^{\pi\pi} < 1.5 \text{ GeV/}c^2$   $0.032 & M_{inv}^{$ 



-0.05

-0.1

data from e<sup>+</sup>e<sup>-</sup> by BELLE allow first (collinear) extraction of transversity (compared to Anselmino et al.)

X

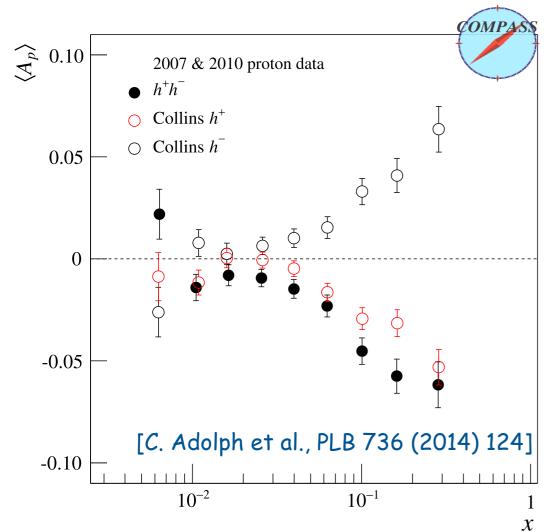
 $10^{-1}$ 

updated analysis available (incl. COMPASS)

INT-18-3, Seattle

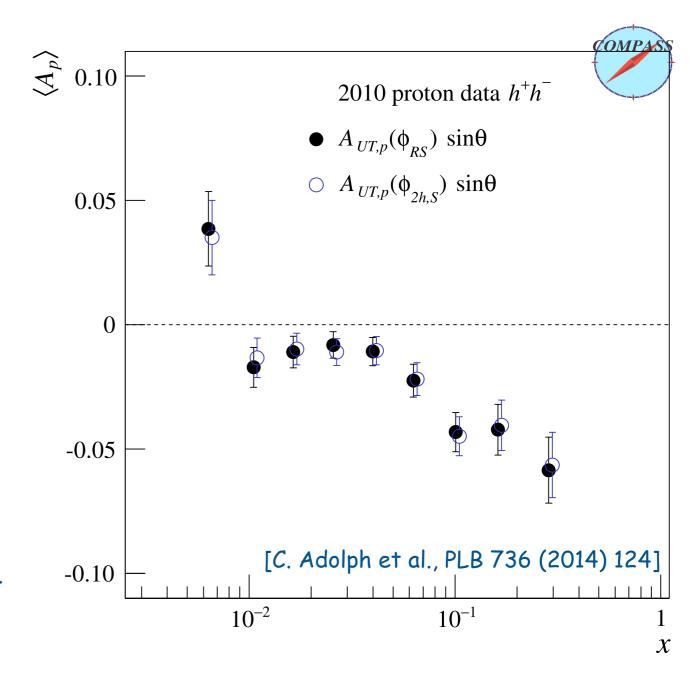
 $M_{inv}^{\pi^+\pi^-}$  (GeV/ $c^2$ )

	U	${ m L}$	m T
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$

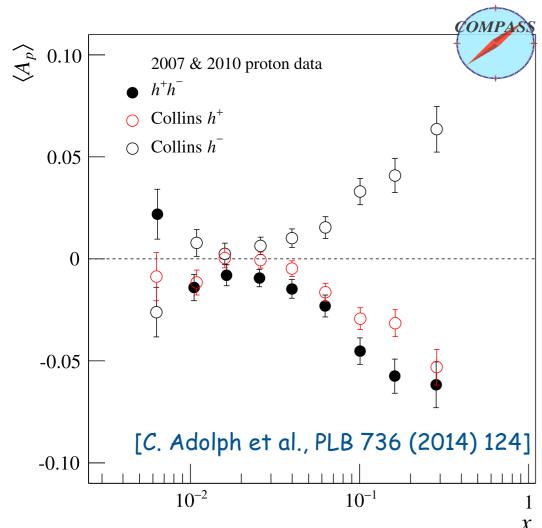




 suggested common origin of Collins and di-hadron FF in PLB 736 (2014) 124

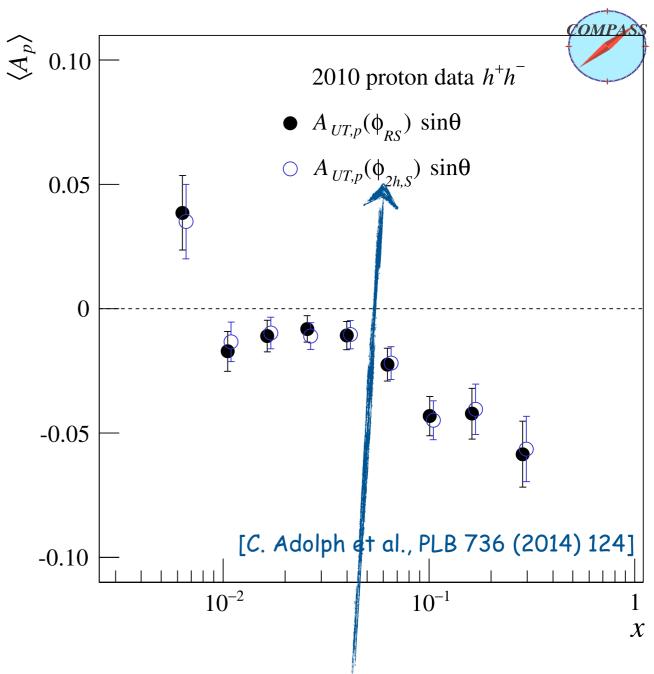


	U	${ m L}$	${ m T}$
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
T	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$



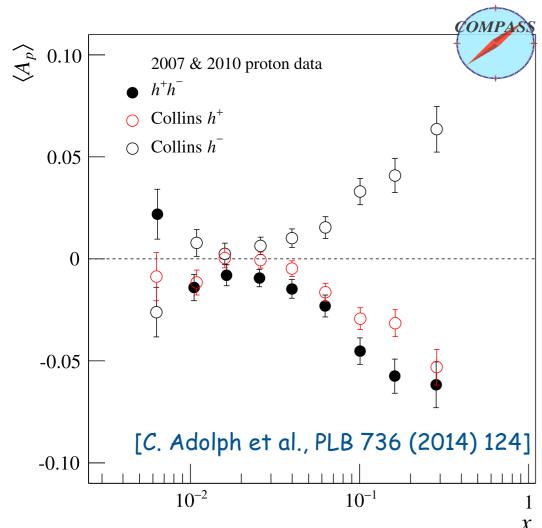


 suggested common origin of Collins and di-hadron FF in PLB 736 (2014) 124



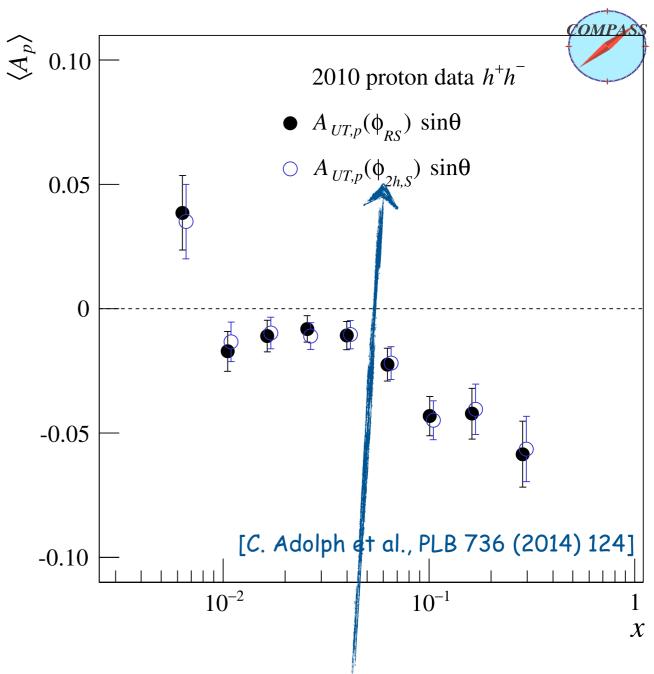
"Collins angle" of  $oldsymbol{R}_N = \hat{oldsymbol{p}}_{T,h^+} - \hat{oldsymbol{p}}_{T,h^-}$ 

	U	${ m L}$	${ m T}$
U	$f_1$		$h_1^{\perp}$
L		$g_{1L}$	$h_{1L}^{\perp}$
T	$f_{1T}^{\perp}$	$g_{1T}$	$h_1,h_{1T}^\perp$



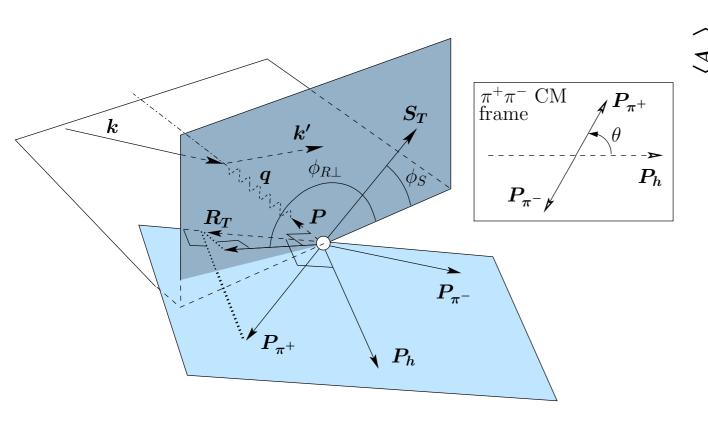


 suggested common origin of Collins and di-hadron FF in PLB 736 (2014) 124



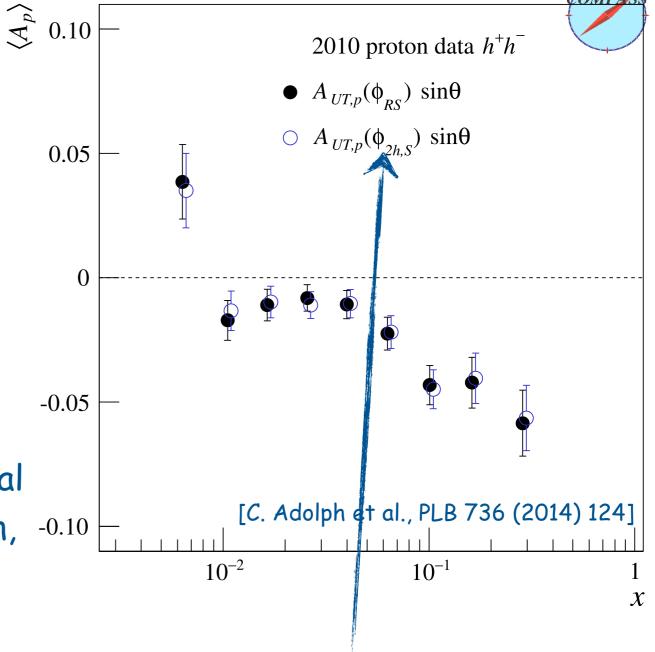
"Collins angle" of  $oldsymbol{R}_N = \hat{oldsymbol{p}}_{T,h^+} - \hat{oldsymbol{p}}_{T,h^-}$ 

	U	L	Т
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^{\perp}$
Т	$f_{1T}^{\perp}$	$g_{1T}$	$h_1, h_{1T}^\perp$



in the limit of collinear  $P_h$  (w.r.t. virtual photon), e.g., in collinear factorization, -0.10  $\phi_{2h,S}$  reduces just to  $\phi_{RS}$ 

no big surprise that those two asymmetries are very similar?

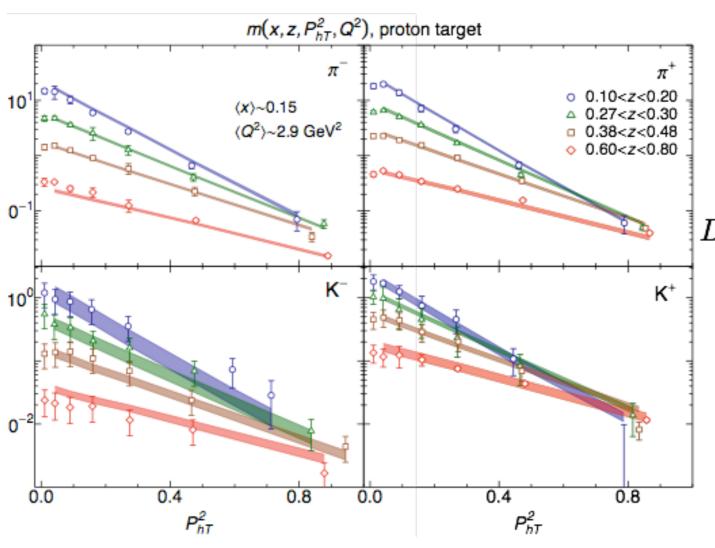


"Collins angle" of  $oldsymbol{R}_N = \hat{oldsymbol{p}}_{T,h^+} - \hat{oldsymbol{p}}_{T,h^-}$ 

# FF TMD flavor dependence

#### • fit to HERMES multiplicity data:

$$m_N^h(x,z,\boldsymbol{P}_{hT}^2;Q^2) = \frac{\pi}{\sum_q e_q^2 \, f_1^q(x;Q^2)} \, \sum_q e_q^2 \, f_1^q(x;Q^2) \, D_1^{q \to h}(z;Q^2) \, \frac{e^{-\boldsymbol{P}_{hT}^2/\langle \boldsymbol{P}_{hT,q}^2 \rangle}}{\pi \, \langle \boldsymbol{P}_{hT,q}^2 \rangle}$$



$$f_1^q(x,\boldsymbol{k}_\perp^2;Q^2) = f_1^q(x;Q^2) \; \frac{e^{-\boldsymbol{k}_\perp^2/\langle \boldsymbol{k}_{\perp,q}^2\rangle}}{\pi \langle \boldsymbol{k}_{\perp,q}^2\rangle}$$

$$D_1^{q o h}(z, oldsymbol{P}_{\perp}^2; Q^2) = D_1^{q o h}(z; Q^2) \; rac{e^{-oldsymbol{P}_{\perp}^2/\langle oldsymbol{P}_{\perp,q o h}^2
angle}}{\pi \langle oldsymbol{P}_{\perp,q o h}^2
angle}$$

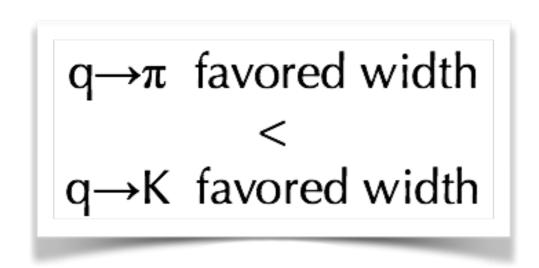
$$\langle m{P}_{hT,q}^2 
angle = z^2 \langle m{k}_{\perp,q}^2 
angle + \langle m{P}_{\perp,q o h}^2 
angle$$

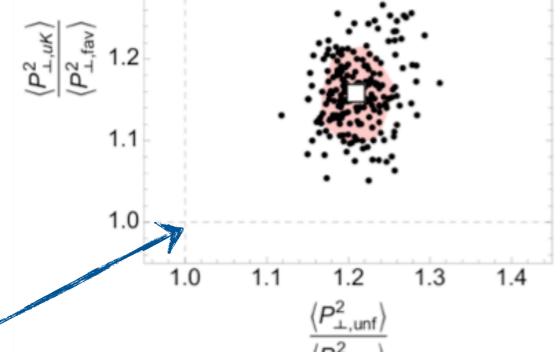
[A. Signori, A. Bacchetta, M. Radici and GS, JHEP 11(2013)194]

## FF TMD flavor dependence

• fit to HERMES multiplicity data:

[A. Signori, A. Bacchetta, M. Radici and GS, JHEP 11(2013)194]





point of no flavor dep.

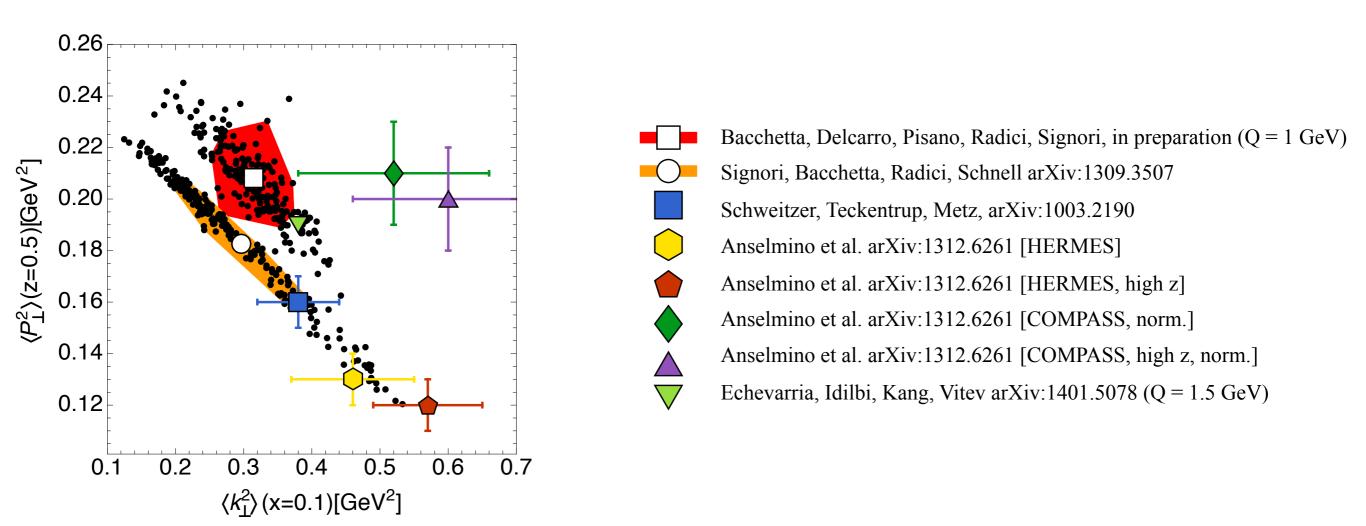
 $q\rightarrow\pi$  favored width < unfavored

1.4

1.3

## FF TMD flavor dependence

• fit to SIDIS, DY & Z boson production: JHEP 06 (2017) 081



- fit to e<sup>+</sup>e<sup>-</sup> data: PLB 772 (2017) 78-86
- new data: COMPASS arXiv:1709.07374