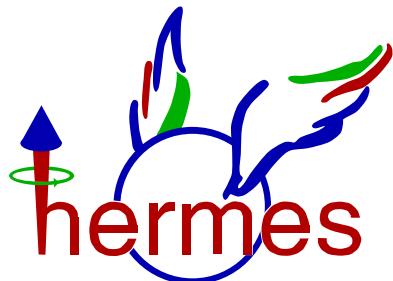


# First Transverse Target Data from HERMES

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University of Illinois at Urbana-Champaign  
Transversity Workshop,  
Athens, Greece  
October 6 - 7, 2003



- *The Collins and Sivers Effects*
- *A<sub>UT</sub> Data Analysis and First Results*
- *Some Interpretation ...*

**Thanks to superb analysis crew!**

**Gunar Schnell** (Tokyo)

**Ralf Seidl \*** (Erlangen)

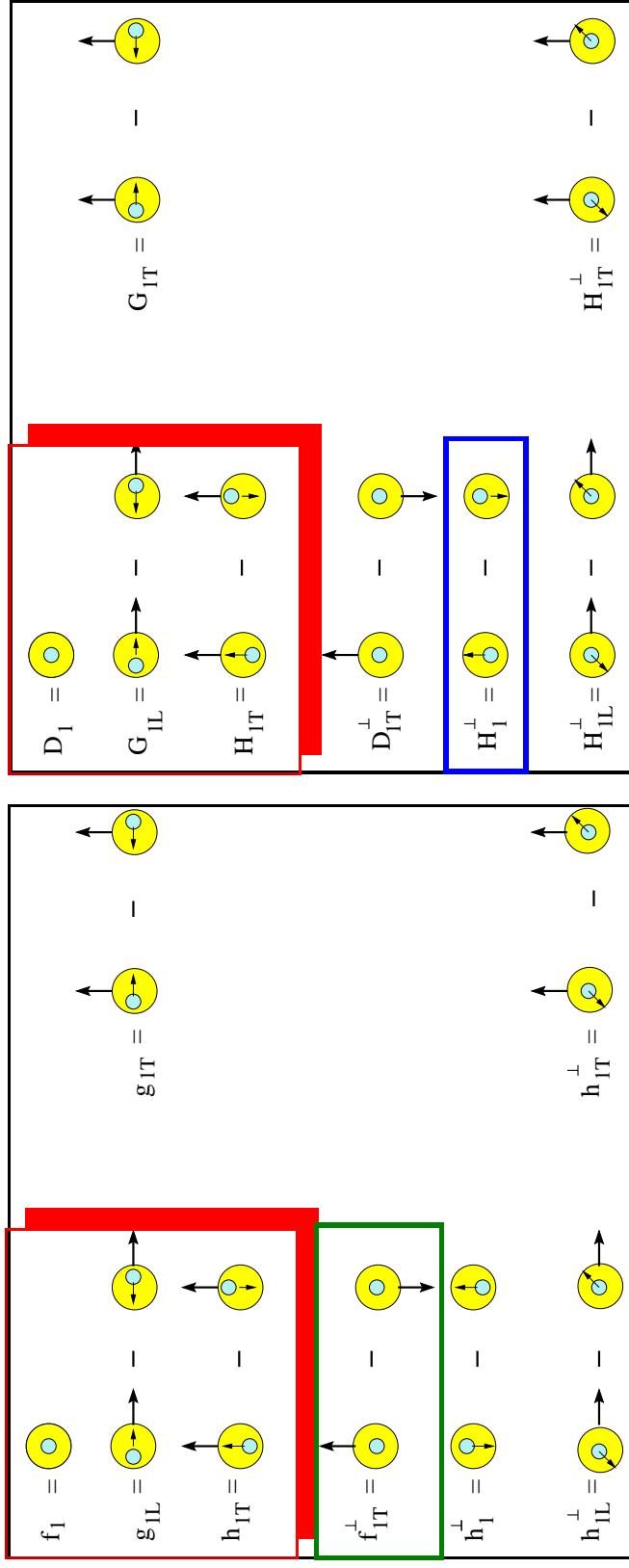
**Ulrike Elschenbroich** (Gent)

\* *Thank you for use of slides from CIPANP!*



# $k_\perp$ dependent DFs or FFs

$$\sigma^{eH \rightarrow ehX} = \sum_q f^{H \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes D^{q \rightarrow h}$$

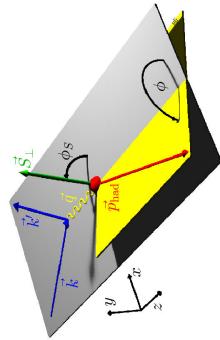


- survive  $k_\perp$  integration

- T-even and T-odd functions
- chiral-even and chiral-odd functions

- Sivers function

- Collins function



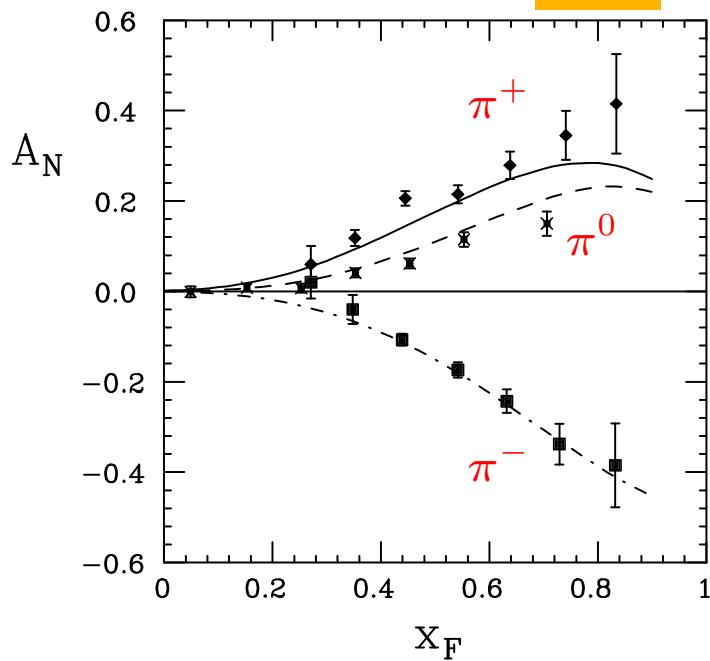
# E704: Sivers or Collins?

The E704 single-spin asymmetry could be due to ...

## Sivers Effect

T-odd **dist<sup>n</sup>** function

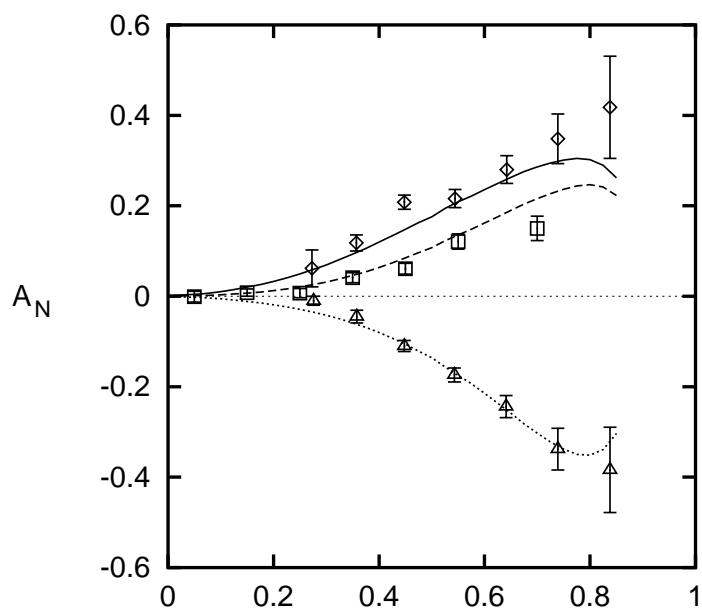
$$f_{1T}^{\perp}$$



## Collins Effect

T-odd **frag<sup>n</sup>** function

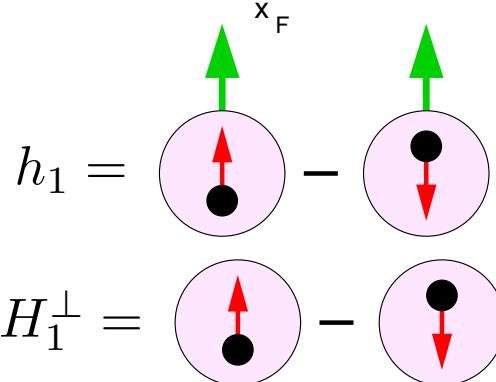
$$H_1^{\perp}$$



## Collins Effect

$$A_N \sim h_1(x) H_1^{\perp}(z)$$

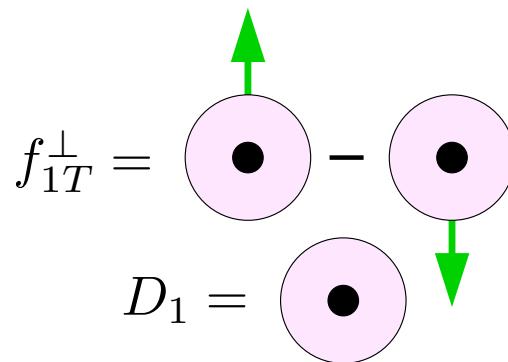
⇒ access to **transversity!**



## Sivers Effect

$$A_N \sim f_{1T}^{\perp}(x) D_1^{\perp}(z)$$

⇒ access to **T-odd dist<sup>n</sup> func**



**QCD T-invariant : T-odd DF or FF → interference**

# E704: T-odd Frag<sup>n</sup> or Dist<sup>n</sup> Function?

Transversity \* Collins  
Fragmentation Func

**Helicity distributions**

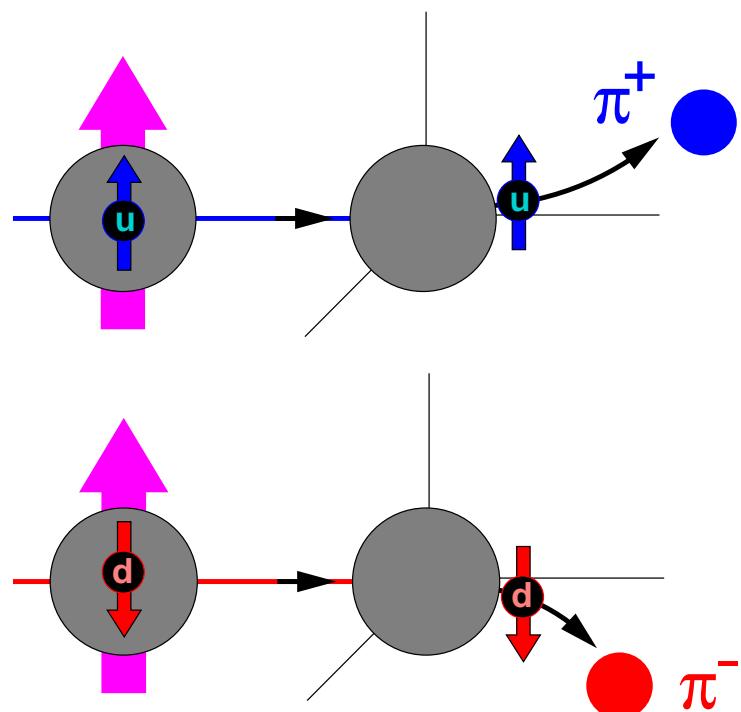
$$\Delta u > 0, \quad \Delta d < 0$$

:

**Transverse dist<sup>n</sup>s**

$$\delta u > 0, \quad \delta d < 0 ?$$

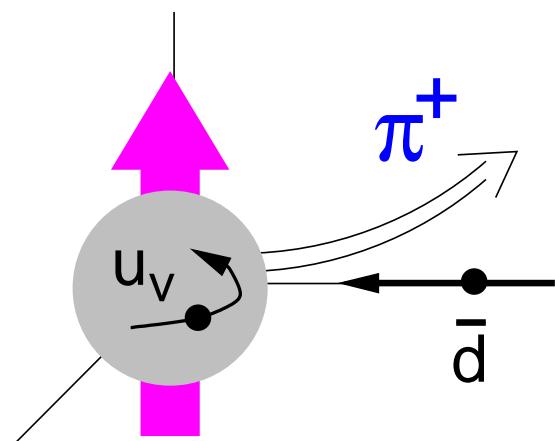
*probably ...*



**Model of Meng, Chou, & Yang**

Valence quarks = relativistic Dirac p'cles in central potential

- relativistic quarks in eigenstates of  $J$   
... shared between  $L$  and  $S$
- symmetrized wavefunction  
 $\rightarrow \Delta u = +4/3, \Delta d = -1/3$
- forward  $\pi^+$  produced from orbiting  $u_v$   
quark at front surface of beam



**Sivers Idea**

Consider dependence  
of parton densities on  
intrinsic  $k_T$  == quark orbital motion

$$f_{1T}^\perp(x_a, \mathbf{k}_{Ta}) = \text{pink circle with up arrow} - \text{pink circle with down arrow}$$

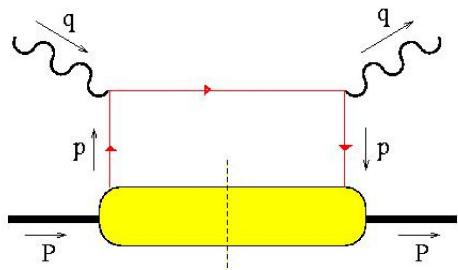
# The Leading-Twist Sivers Function

*Can it exist in DIS?*

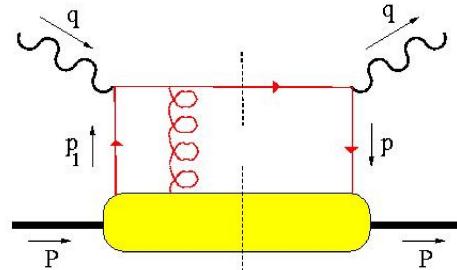
A T-odd function like  $f_{1T}^\perp$  must arise from interference ...  
but a distribution function is just a forward scattering amplitude,  
how can it contain an interference?

$$\left| \begin{array}{c} \text{wavy line } q \\ \parallel \quad \parallel \\ \text{horizontal line } P \end{array} \right\| \rightarrow \left| \begin{array}{c} \text{wavy line } q \\ \parallel \quad \parallel \\ \text{horizontal line } P \end{array} \right\|^2 \sim \text{Im} \left\{ \begin{array}{c} \text{wavy line } q \\ \parallel \quad \parallel \\ \text{horizontal line } P \end{array} \right\}$$

**Brodsky, Hwang, & Schmidt 2002**



can interfere with



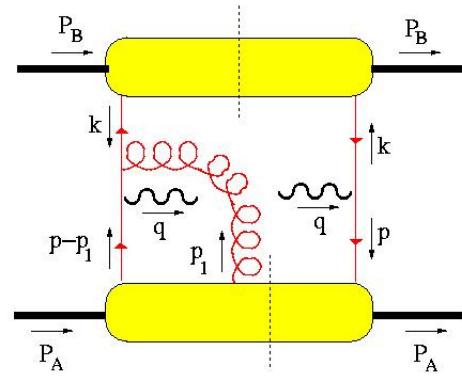
and produce a T-odd effect!

( **also requires**  $L_z \neq 0$  ... so does  $F_2(q)$  form factor )

**It looks higher-twist, but it's not ...**  
**→ these are soft gluons**

Such soft-gluon reinteractions  
with the soft wavefunction are  
**final (or initial) state interactions** ...  
and may be **process dependent!**

→ new **universality issues** ...



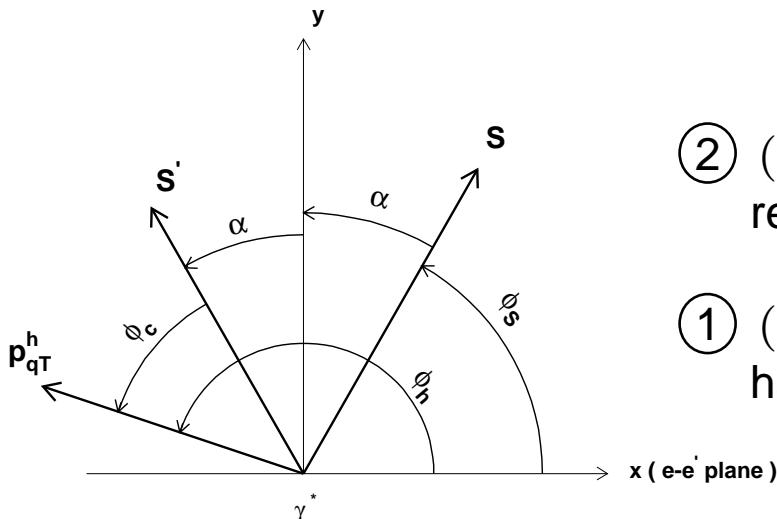
e.g. Drell-Yan

# T-odd Distribution vs Fragmentation Function

SIDIS xsec  $d\sigma_{UT}$  with *transverse target* polarization has **two** similar terms:

$$\begin{aligned} \textcircled{1} \quad \sin(\phi_h^l + \phi_S^l) \otimes h_1 &= \text{Diagram } 1 - \text{Diagram } 2 \otimes H_1^\perp = \text{Diagram } 3 - \text{Diagram } 4 \\ \textcircled{2} \quad \sin(\phi_h^l - \phi_S^l) \otimes f_{1T}^\perp &= \text{Diagram } 5 - \text{Diagram } 6 \otimes D_1 = \text{Diagram } 7 \end{aligned}$$

**separate Sivers and Collins mechanisms**



- ②  $(\phi_h^l - \phi_S^l)$  = angle of hadron relative to **initial** quark spin
- ①  $(\phi_h^l + \phi_S^l) = \pi + (\phi_h^l - \phi_S^{l'})$  = hadron relative to **final** quark spin

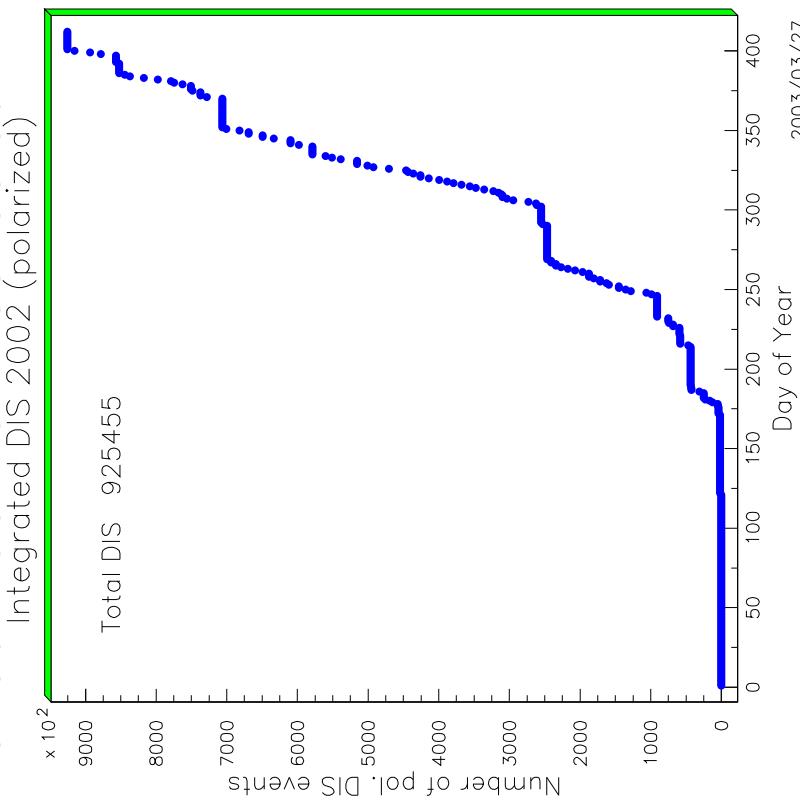
Cannot distinguish in:

- **longitudinal-target case** ...
  - transverse component has  $\phi_S^l = 0$ .
- **inclusive  $\pi$  production**, e.g.  $p^\uparrow p \rightarrow \pi X$ 
  - jet axis not known

## Data Collection 2002-2003 and Cuts

### Transverse Hydrogen target installed in 2001

**not so much lumi collected ...**

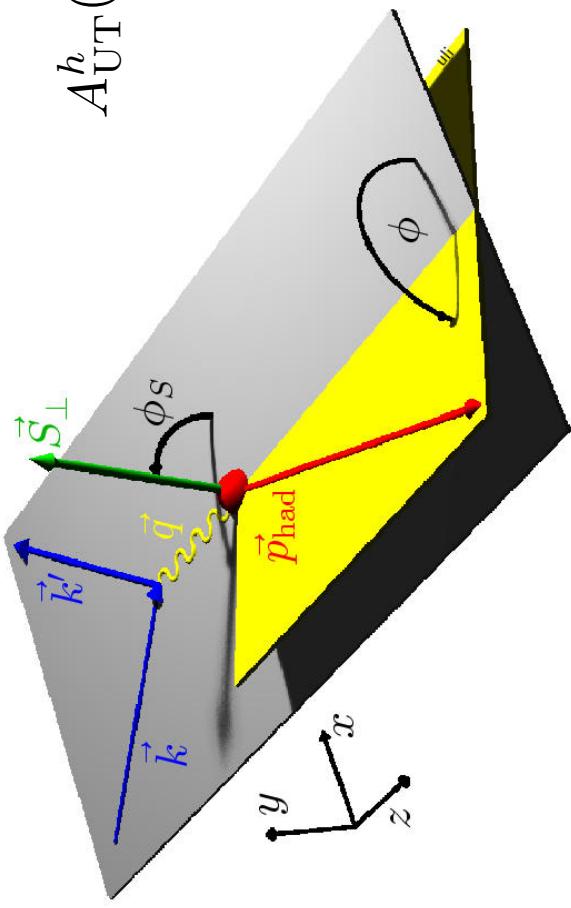


### SIDIS cuts

- $0.1 \leq y < 0.85$
- $0.023 < x < 0.4$
- $Q^2 > 1 \text{ GeV}^2$
- $W^2 > 10 \text{ GeV}^2$
- $0.2 < z < 0.7$   
(avoid exclusive region)
- $0.02 \text{ rad} < \theta_{\gamma,\pi}$

year	target gas	spin orientation	# pol. DIS
96-97	hydrogen	L	2.4 M
98-00	deuterium	L	9.1 M ☺
02-03	hydrogen	T	0.7 M ☺

# Definition of Angles and Asymmetries



$$\begin{aligned}
 A_{\text{UT}}^h(\phi, \phi_S) &= \frac{1}{|P_T|} \frac{N_h^\uparrow(\phi, \phi_S) - N_h^\downarrow(\phi, \phi_S)}{N_h^\uparrow(\phi, \phi_S) + N_h^\downarrow(\phi, \phi_S)} \\
 &= A_{\text{UT}}^{\text{Collins}} \sin(\phi + \phi_S) \\
 &\quad + A_{\text{UT}}^{\text{Sivers}} \sin(\phi - \phi_S)
 \end{aligned}$$

**fit amplitudes simultaneously**

(prevents mixing of effects by acceptance)

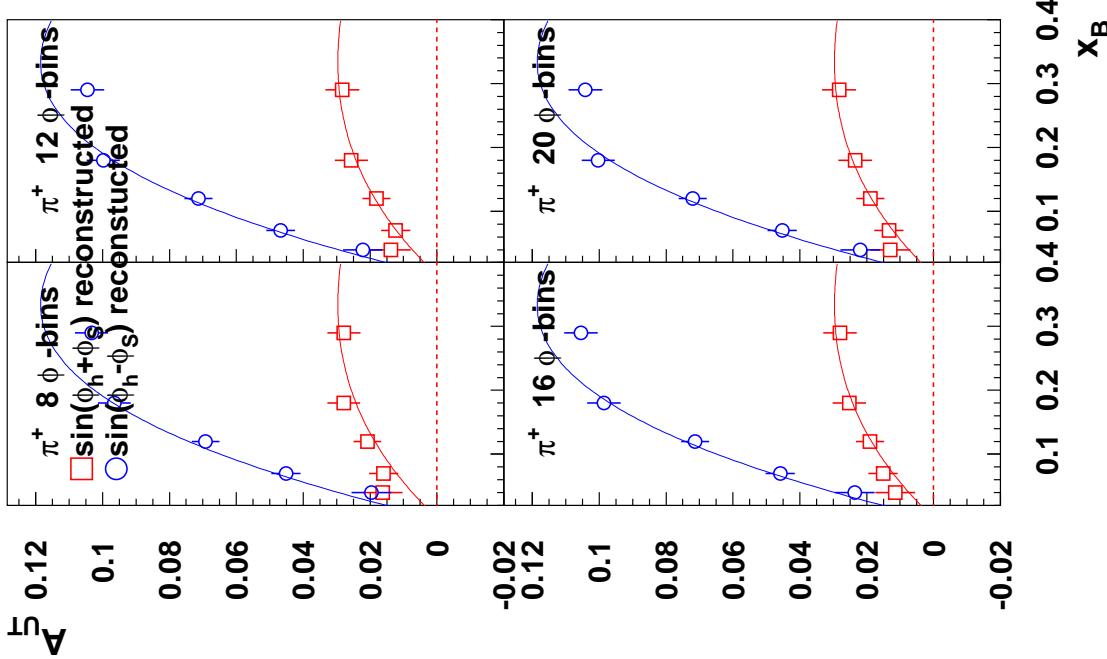
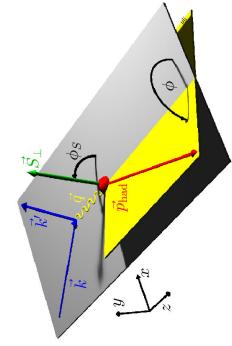
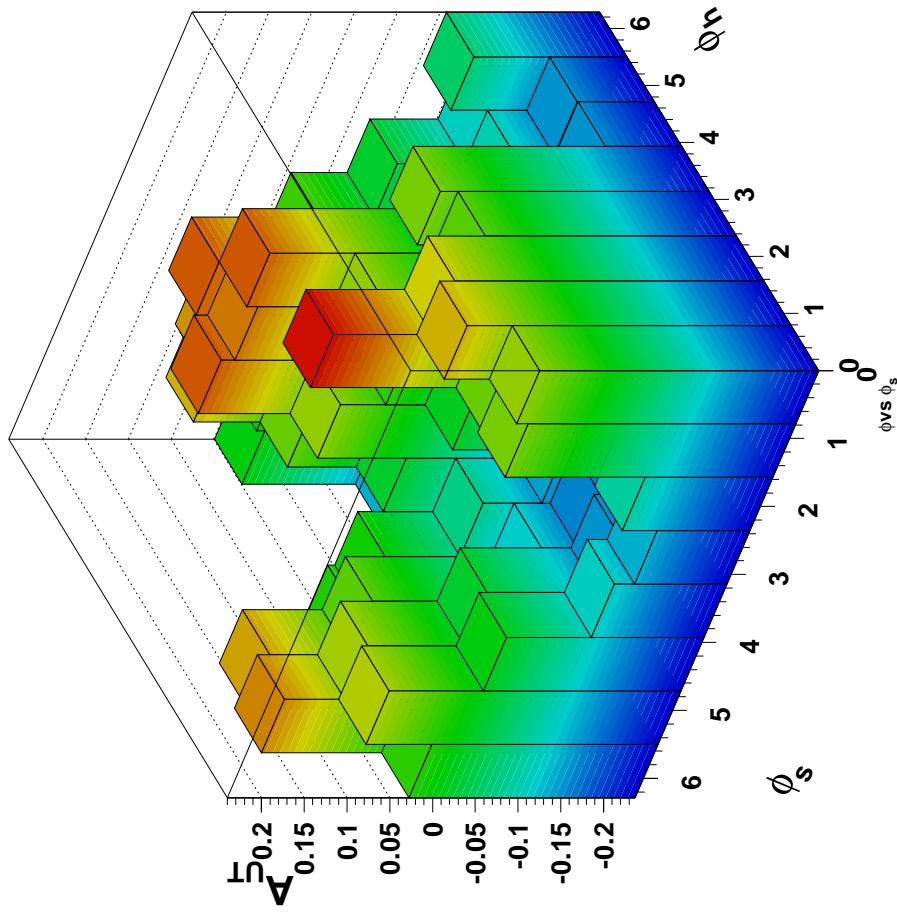
$A_{\text{UT}}^{\text{Collins}, \text{wt}}$	$= \frac{2 \langle \frac{Q_T}{M_\pi} \sin(\phi + \phi_S) \rangle_{\text{UT}}}{\langle 1 \rangle_{\text{UU}}} =  S_T  \frac{\sum_q e_q^2 \mathbf{h}_1^q \mathbf{H}_1^{\perp(1), q \rightarrow h}}{\sum_q e_q^2 f_1^q D_1^{q \rightarrow h}} \frac{1 - y}{1 - y + y^2/2}$
$A_{\text{UT}}^{\text{Sivers}, \text{wt}}$	$= \frac{2 \langle \frac{Q_T}{M_\pi} \sin(\phi - \phi_S) \rangle_{\text{UT}}}{\langle 1 \rangle_{\text{UU}}} =  S_T  \frac{\sum_q e_q^2 \mathbf{f}_{1\text{T}}^{\perp, q} \mathbf{D}_1^{q \rightarrow h}}{\sum_q e_q^2 f_1^q D_1^{q \rightarrow h}}$
$A_{\text{UT}}^{\text{Collins}}$	$= \frac{2 \langle \sin(\phi + \phi_S) \rangle_{\text{UT}}}{\langle 1 \rangle_{\text{UU}}} \sim A_{\text{UT}}^{\text{Collins}, \text{wt}} \cdot \frac{M_\pi z}{2 \langle P_{\pi^\perp} \rangle}$
$A_{\text{UT}}^{\text{Sivers}}$	$= \frac{2 \langle \sin(\phi - \phi_S) \rangle_{\text{UT}}}{\langle 1 \rangle_{\text{UU}}} \sim A_{\text{UT}}^{\text{Sivers}, \text{wt}} \cdot \frac{M z}{2 \langle P_{\pi^\perp} \rangle}$

Weighted moments

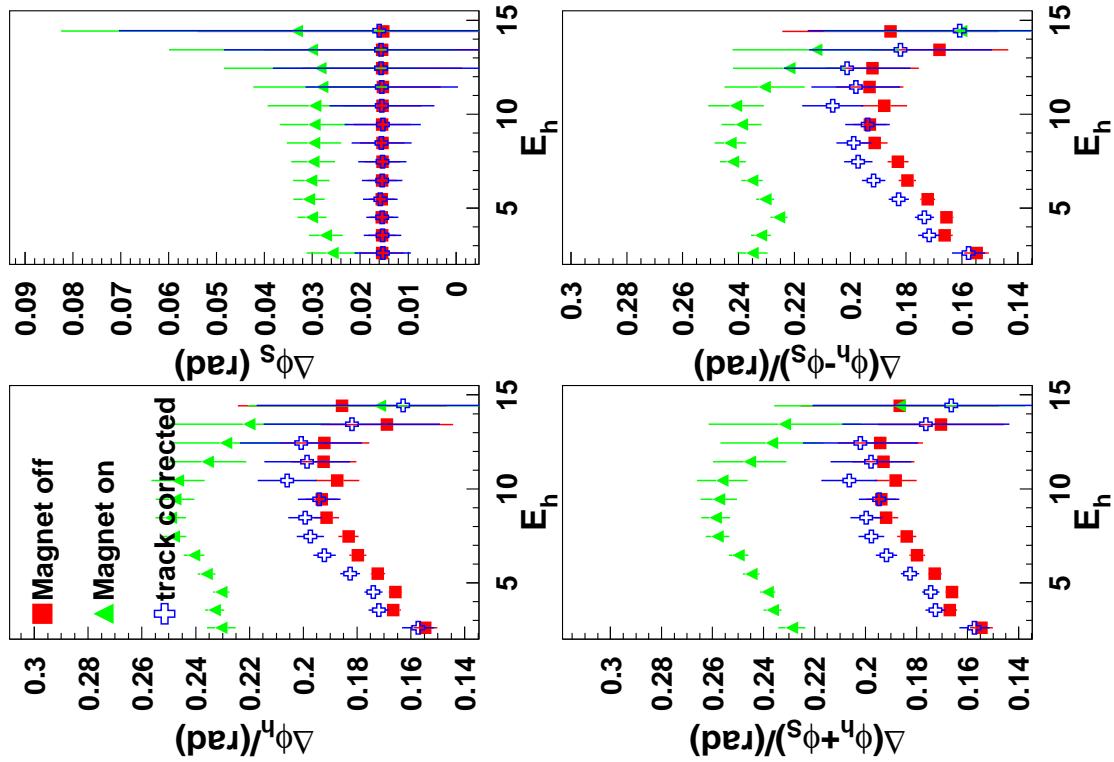
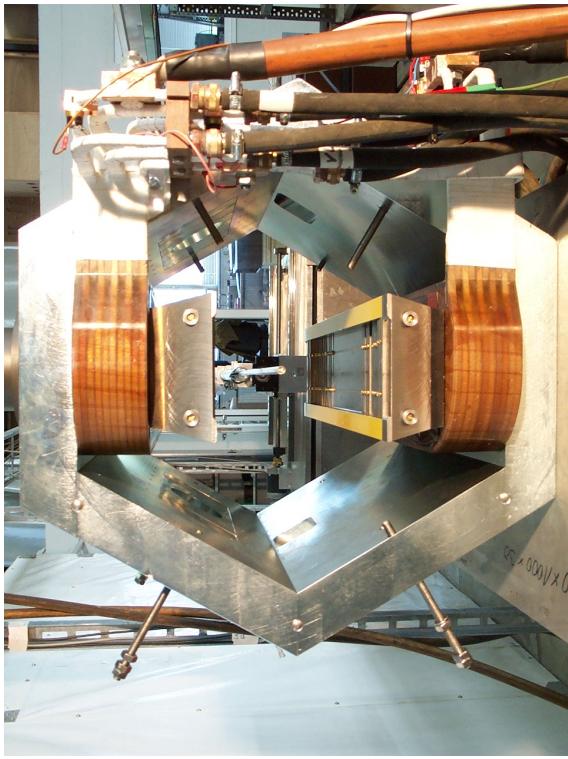
Unweighted moments

**(in Gaussian ansatz)**

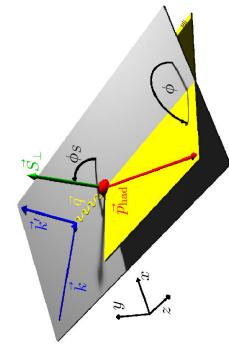
# MC: reconstruction of moments



# MC-studies: resolutions

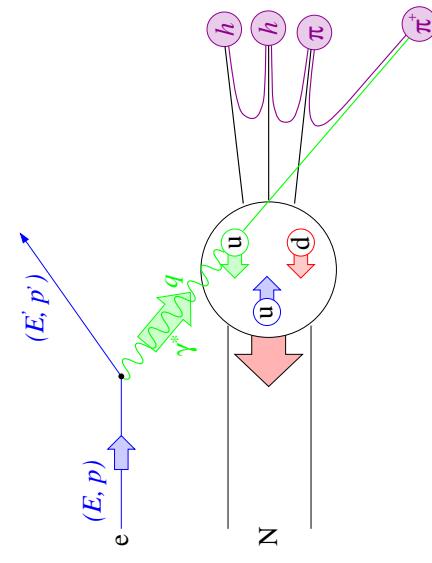


and many more systematic  
checks by Ralf, Uli, & Gunnar!

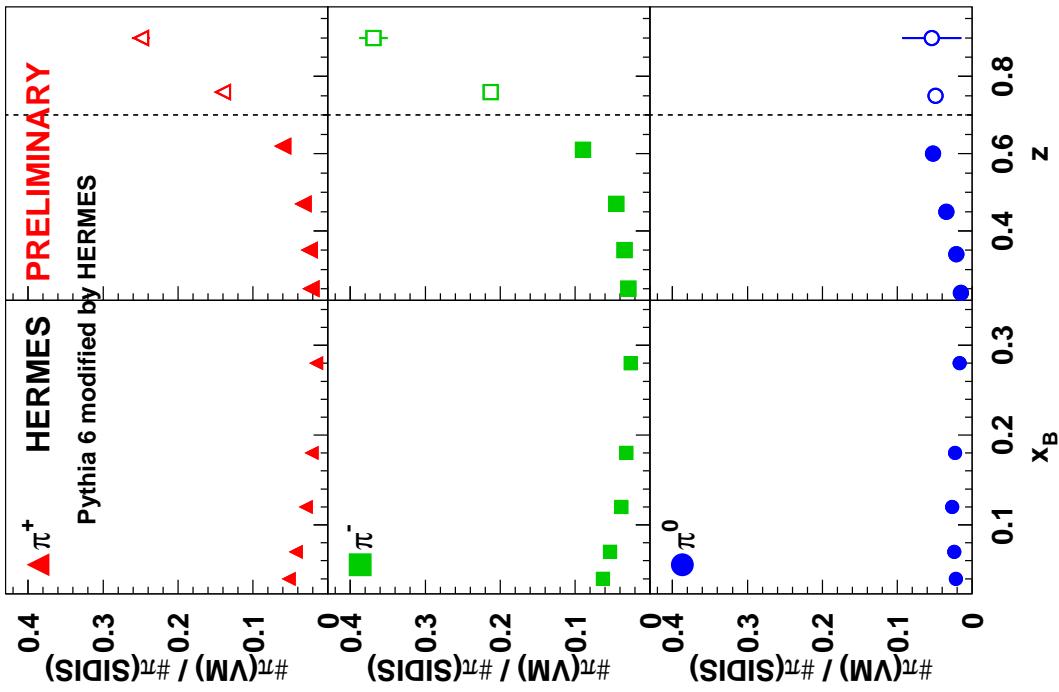
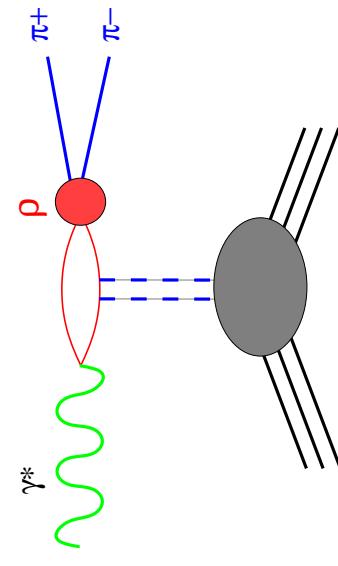


# Uncertainty from Diffractive VM Contribution

**Desired process:** SIDIS  $e p \rightarrow \pi^+ X$

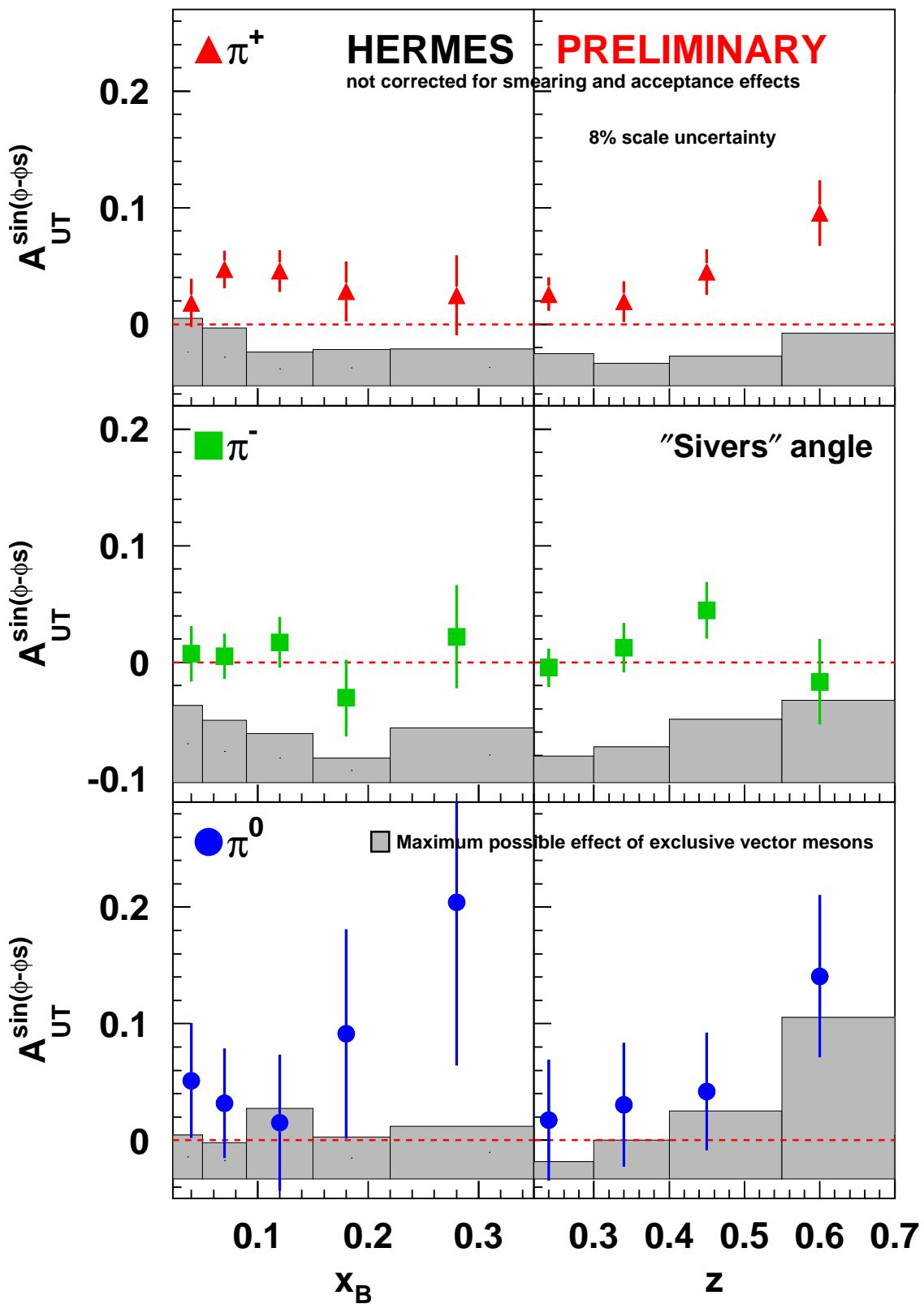


**Diffractive  $\rho^0$  production:  
different physics**



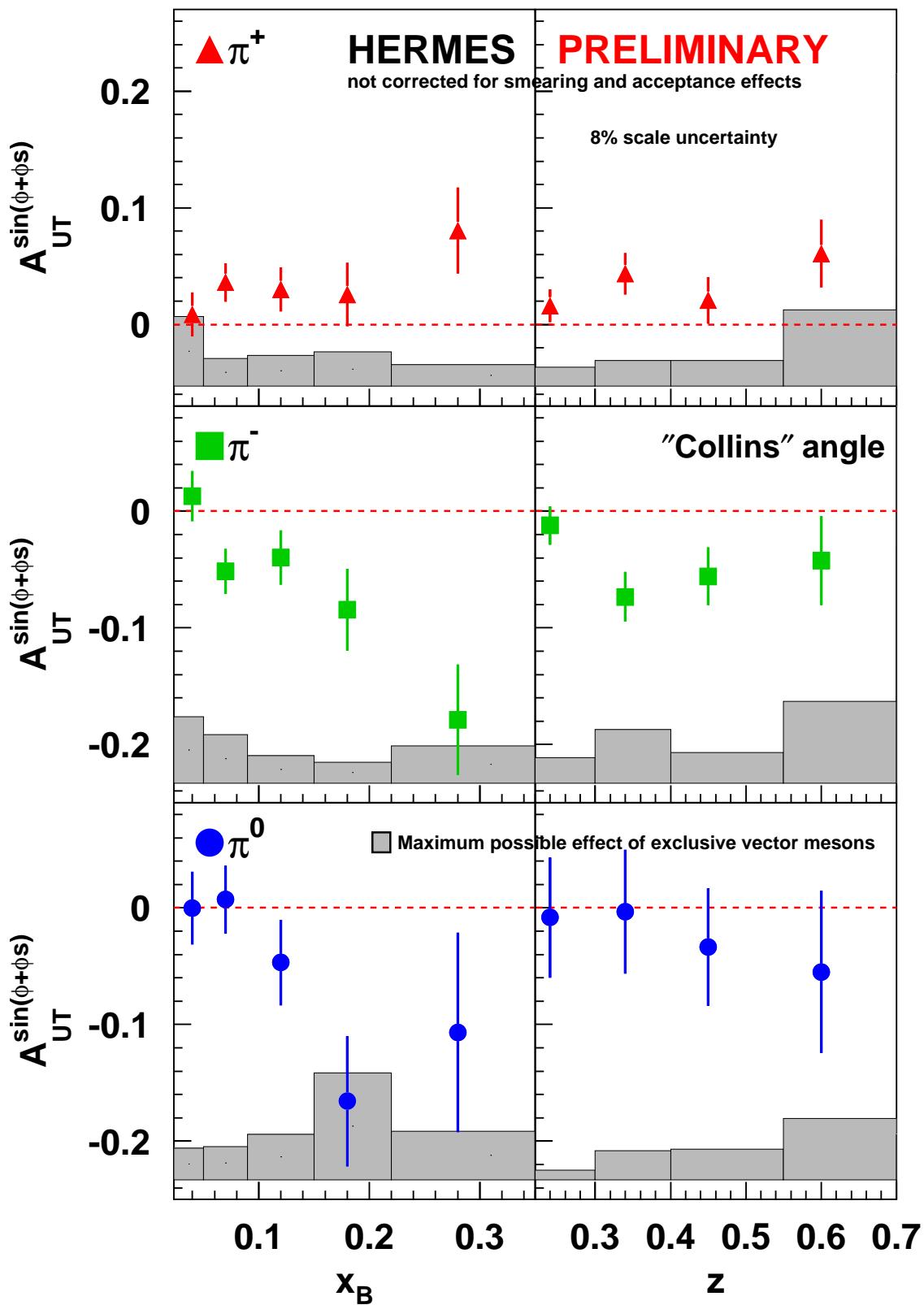
**Conservative approach:** calculate systematic error for full range of possible diffractive  $\rho$  asymmetries:  $A_{\text{UT}}^{\text{Collins}, \rho}$  and  $A_{\text{UT}}^{\text{Sivers}, \rho} = \pm 1$

# Unweighted Sivers Moments $A_{\text{UT}}^{\sin(\phi - \phi_S)}$



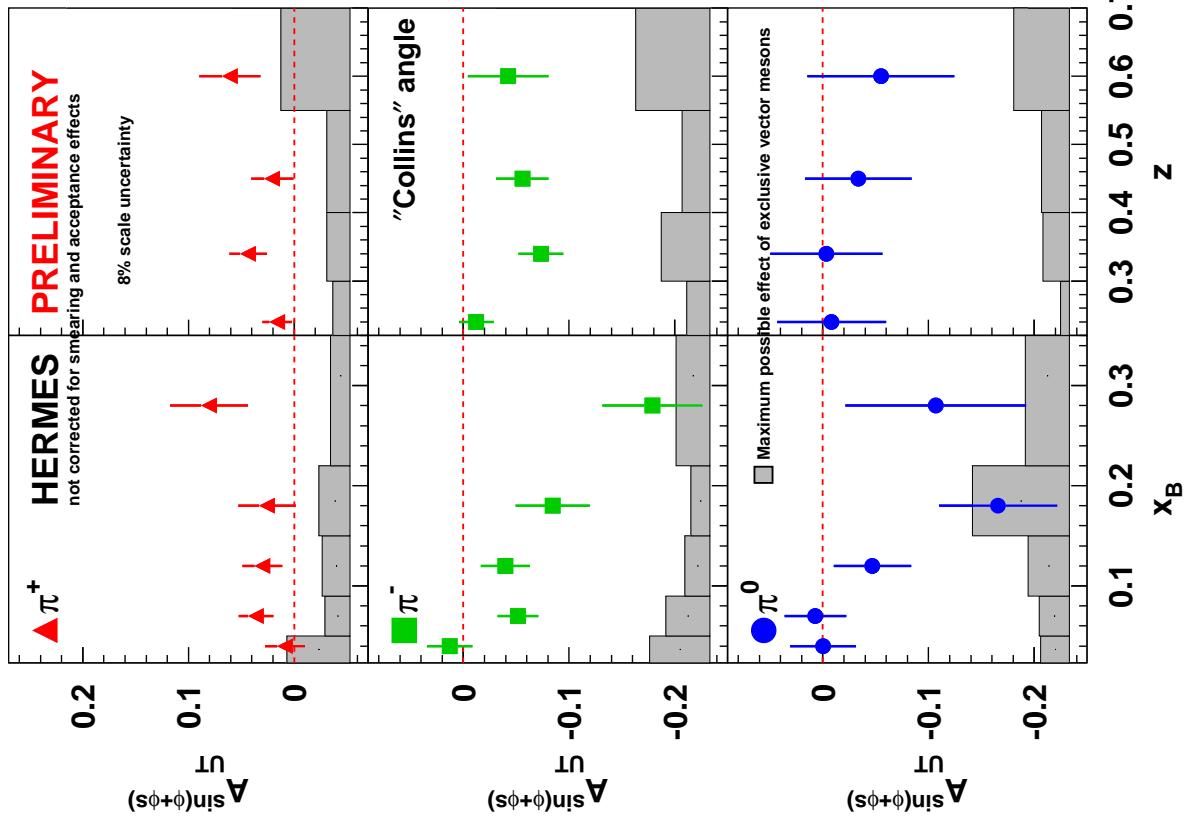
→ asym's small, but Sivers  $\langle A_{\text{UT}}^{\pi^+} \rangle$  is  $3\sigma$  away from zero

# Unweighted Collins Moments $A_{\text{UT}}^{\sin(\phi+\phi_s)}$



→  $A^{\pi^+}$  small, but large negative  $\pi^0$  and  $\pi^-$  asym's

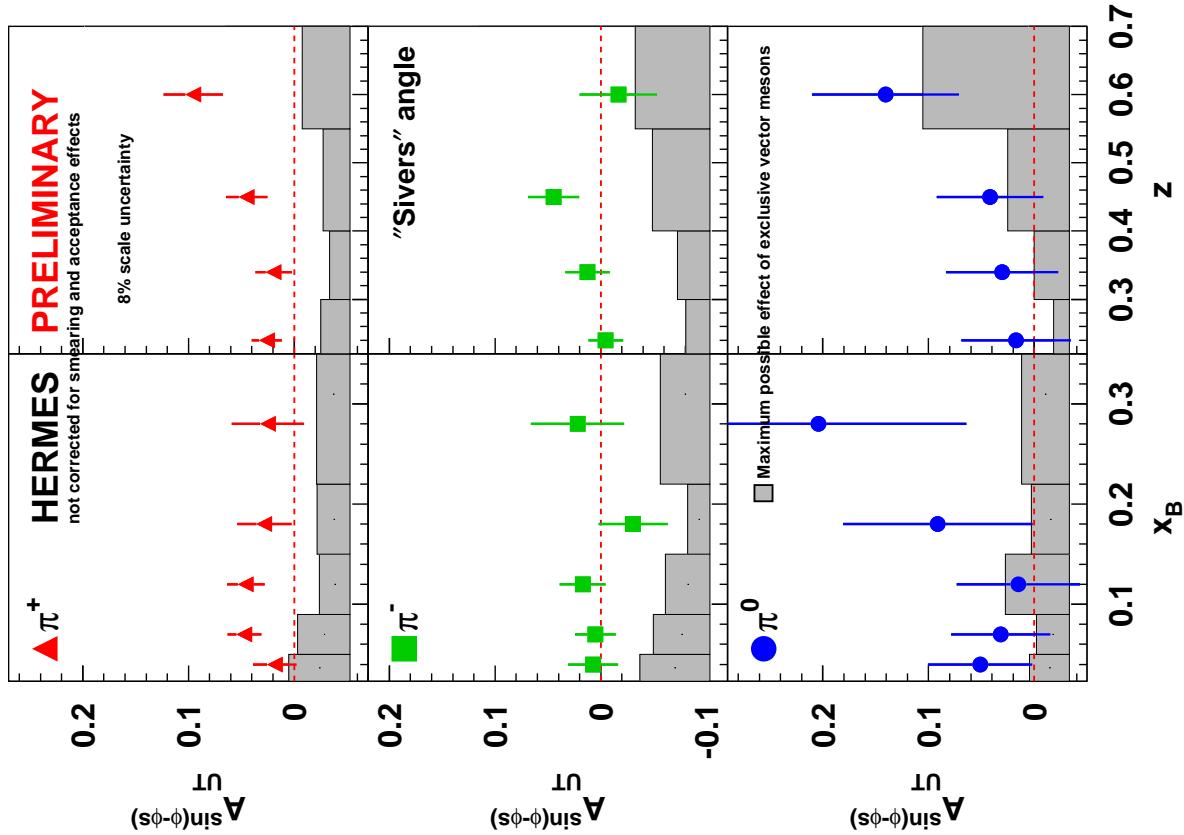
## “Collins” Moments



Collins asym large for  $\pi^0$  and  $\pi^-$

3 $\sigma$  away from zero ...

## “Sivers” Moments

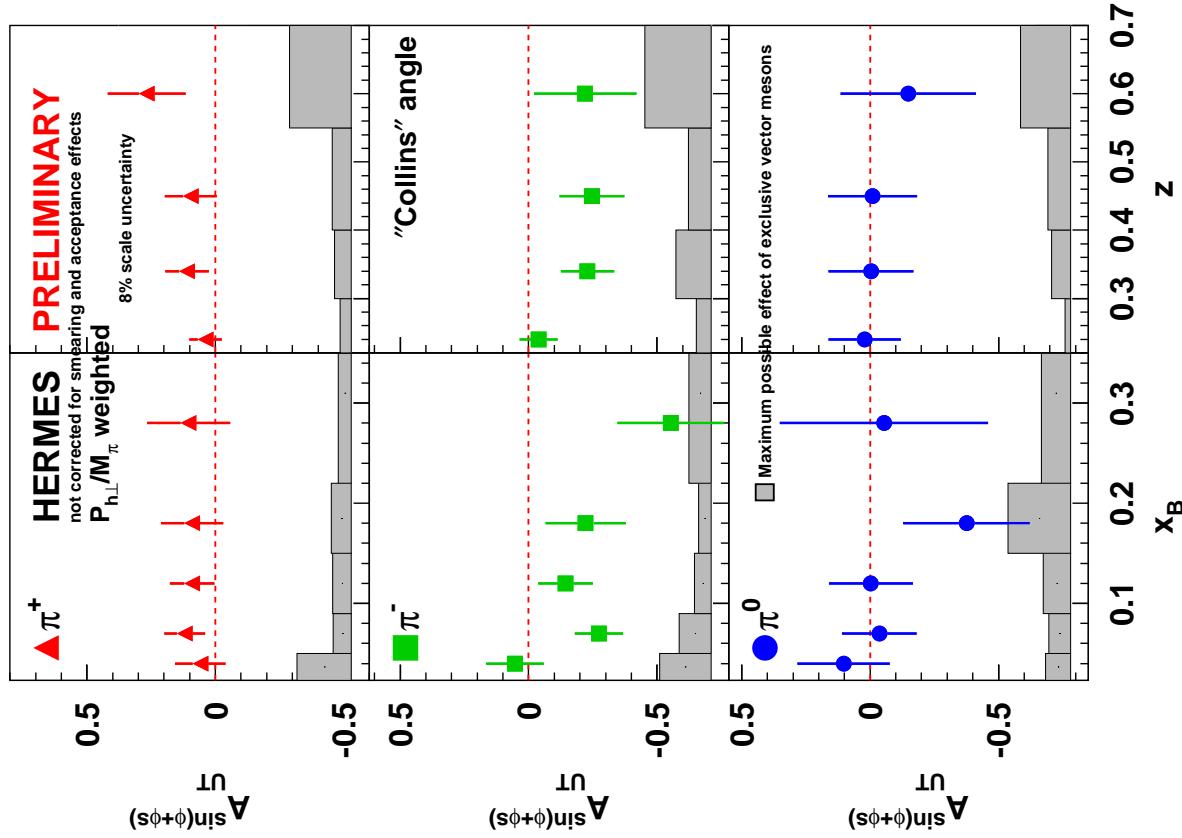


Sivers  $\langle A \pi^+ \rangle$

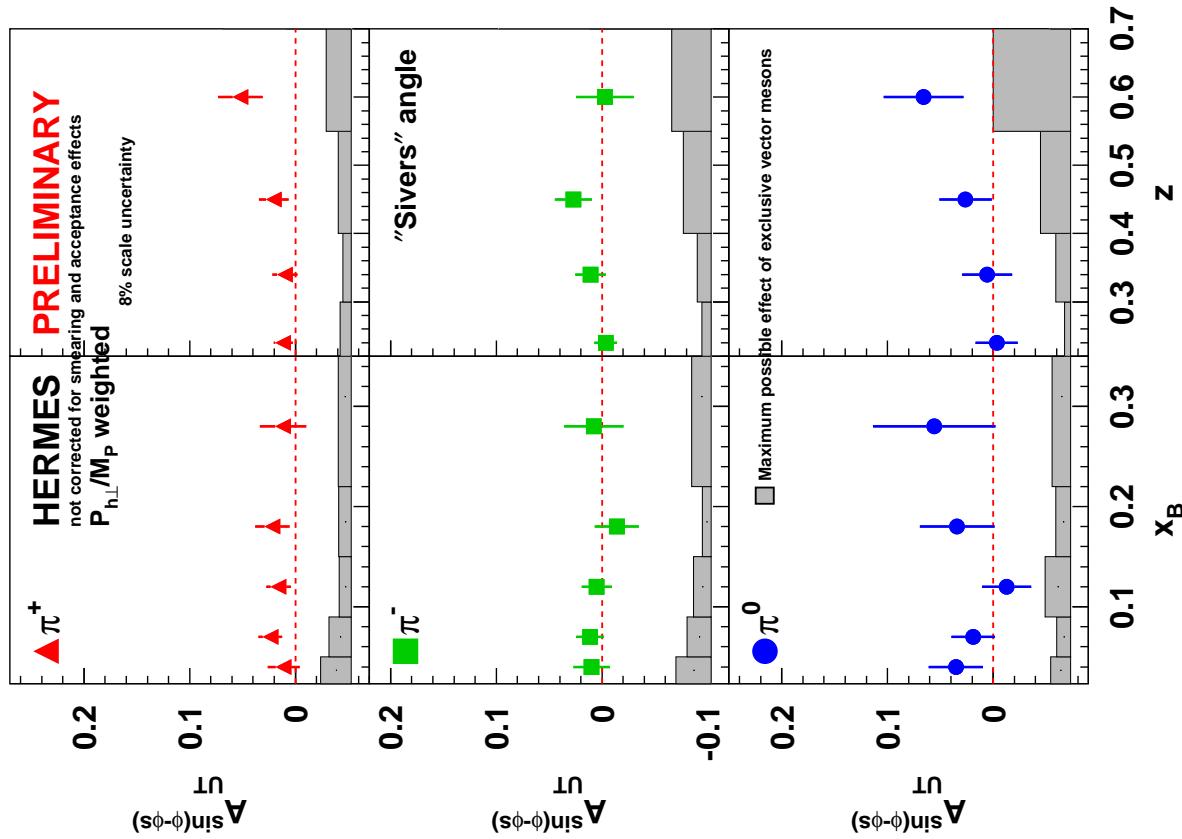
Results I: Unweighted Moments



## “Collins” Moments



## “Sivers” Moments



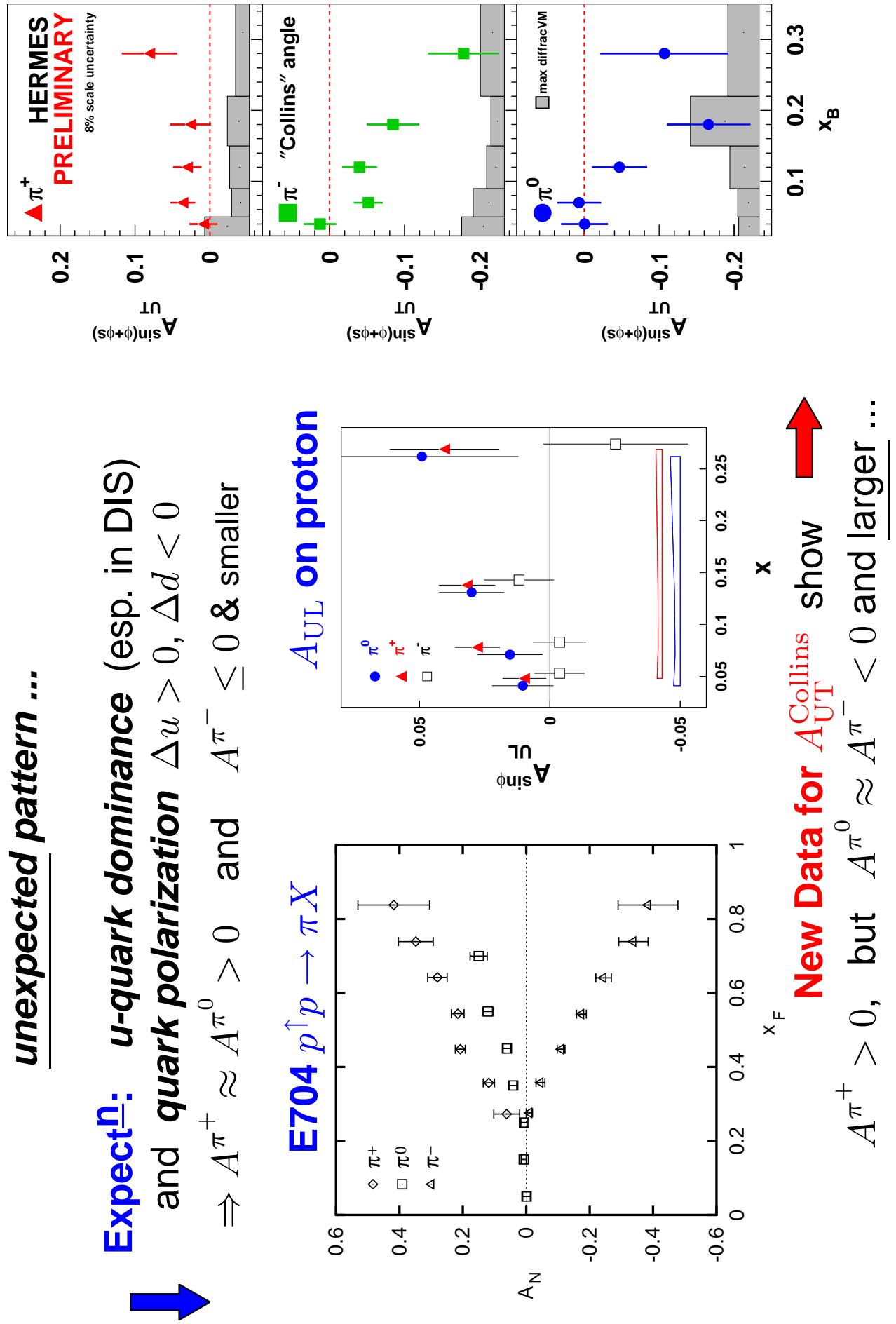
(No correction yet for experimental acceptance in  $p_T$ )

**Results II:  $p_T/M_\pi$ -weighted Moments**

# Interpretation of Collins Results

The Collins results for  $\pi^+$ ,  $\pi^-$ ,  $\pi^0$  show an unexpected pattern ...

**Expect<sub>n</sub>:** u-quark dominance (esp. in DIS)  
and quark polarization  $\Delta_u > 0$ ,  $\Delta_d < 0$   
 $\Rightarrow A_{\pi^+} \approx A_{\pi^0} > 0$  and  $A_{\pi^-} \leq 0$  & smaller



# Interpretation of Collins Results

## Minimalist Assumptions

- $A_{\text{UT}}^{\text{Collins}}$  is ***leading twist***

- Collins FF obeys ***favoured / disfavoured*** symmetry:

$$H_{\text{fav}} \equiv H_{1\perp}^{u \rightarrow \pi^+} = H_{1\perp}^{d \rightarrow \pi^-} = H_{1\perp}^{\bar{u} \rightarrow \pi^-} = H_{1\perp}^{\bar{d} \rightarrow \pi^+}$$

$$H_{\text{dis}} \equiv H_{1\perp}^{u \rightarrow \pi^-} = H_{1\perp}^{d \rightarrow \pi^+} = H_{1\perp}^{\bar{u} \rightarrow \pi^+} = H_{1\perp}^{\bar{d} \rightarrow \pi^-}$$

$$\Rightarrow A^{\pi^+} = k \frac{(4\delta u + \delta \bar{d})H_{\text{fav}} + (\delta d + 4\delta \bar{u})H_{\text{dis}}}{(4u + \bar{d})D_{\text{fav}} + (d + 4\bar{u})D_{\text{dis}}}, \quad A^{\pi^-} = k \dots, \quad \text{etc}$$

**Consider Asym Ratios**  $\alpha^- \equiv A^{\pi^-}/A^{\pi^+}$ ,  $\alpha^0 \equiv A^{\pi^0}/A^{\pi^+}$

$$r \equiv \frac{d + 4\bar{u}}{u + \bar{d}/4} \quad \eta \equiv \frac{D_{\text{dis}}}{D_{\text{fav}}} \Rightarrow \alpha^- = \left( \frac{4\eta_H + \delta r}{4\eta + r} \right) \left( \frac{4 + r\eta}{4 + \delta r\eta_H} \right)$$

$$\delta r \equiv \frac{\delta d + 4\delta \bar{u}}{\delta u + \delta \bar{d}/4} \quad \eta_H \equiv \frac{H_{\text{dis}}}{H_{\text{fav}}} \quad \alpha^0 = \frac{(4 + \delta r)(1 + \eta_H)}{(4 + r)(1 + \eta)} \left( \frac{4 + r\eta}{4 + \delta r\eta_H} \right)$$

$\Rightarrow$  **Constraint Equ<sup>n</sup>** involving ***only unpolarized*** q'ties

$$\alpha^- C = \alpha^0(1 + C) - 1 \quad \text{where} \quad C \equiv \frac{4\eta + r}{4 + \eta r}$$

$\Rightarrow$  **Solution Space** in  $\eta_H$  vs  $\delta r$  can be determined:

$$\eta_H = \frac{\delta r - 4(\alpha^- C)}{(\alpha^- C)\delta r - 4} \quad \text{and} \quad \eta_H = \frac{\delta r - 4(\alpha^0(1 + C) - 1)}{(\alpha^0(1 + C) - 1)\delta r - 4}$$

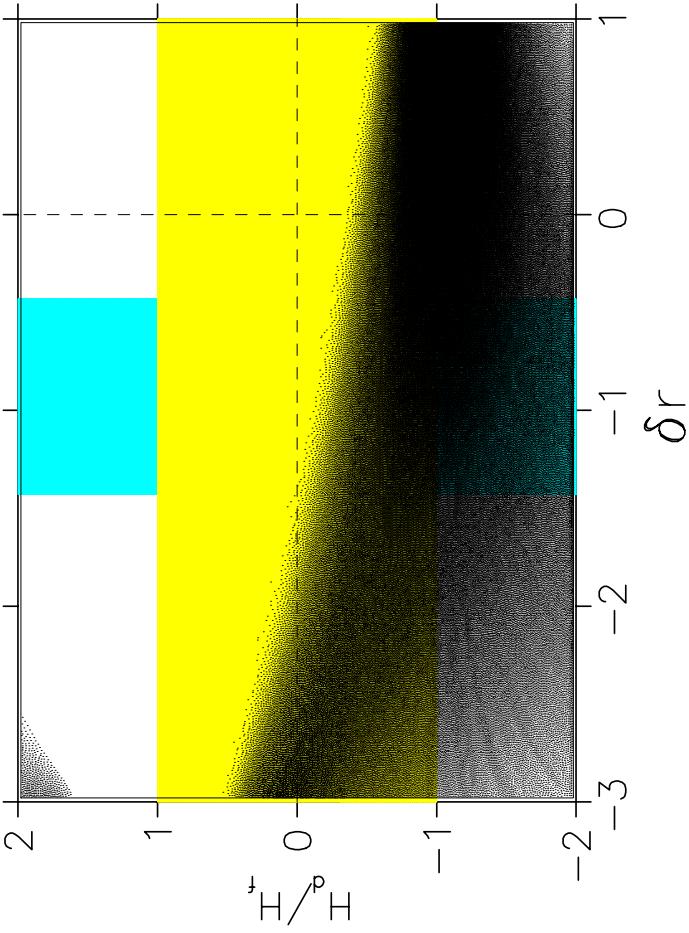
# Interpretation of Collins Results

- ① **Constraint equation:** well satisfied by both weighted and unweighted asymmetries (within  $1\sigma$  statistical)  $\rightarrow$  no problem with internal consistency

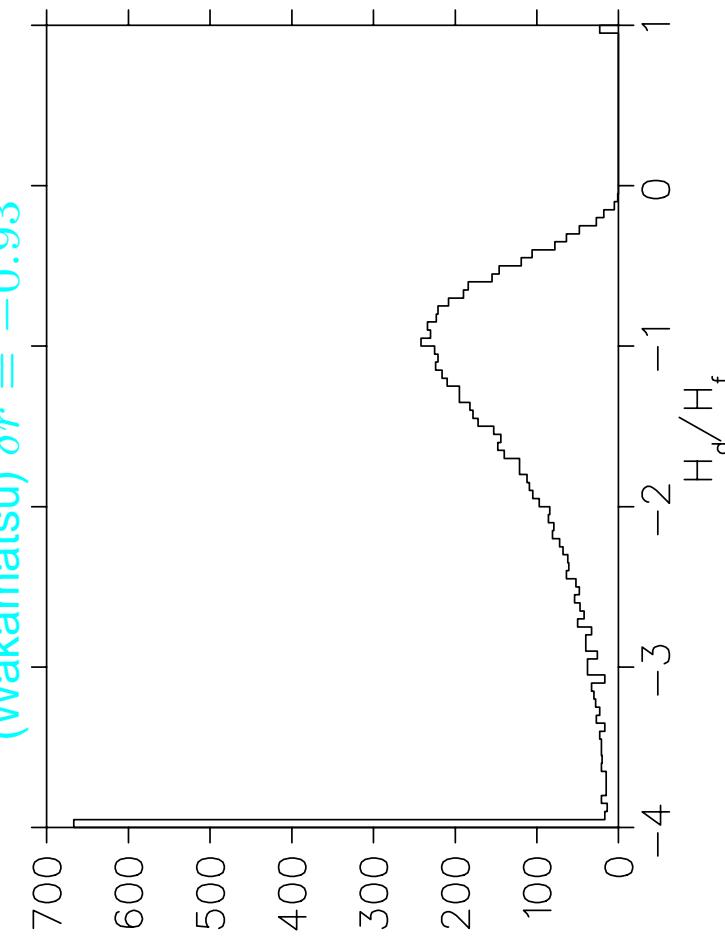
② **Solution space** for  $\delta r \approx \delta d/\delta u$  vs  $\eta_H = H_{\text{dis}}/H_{\text{fav}}$

solution space populated

according to statistical errors



$\eta_H$  solutions at  $\chi_{\text{QSM}}$  value  
(Wakamatsu)  $\delta r = -0.93$

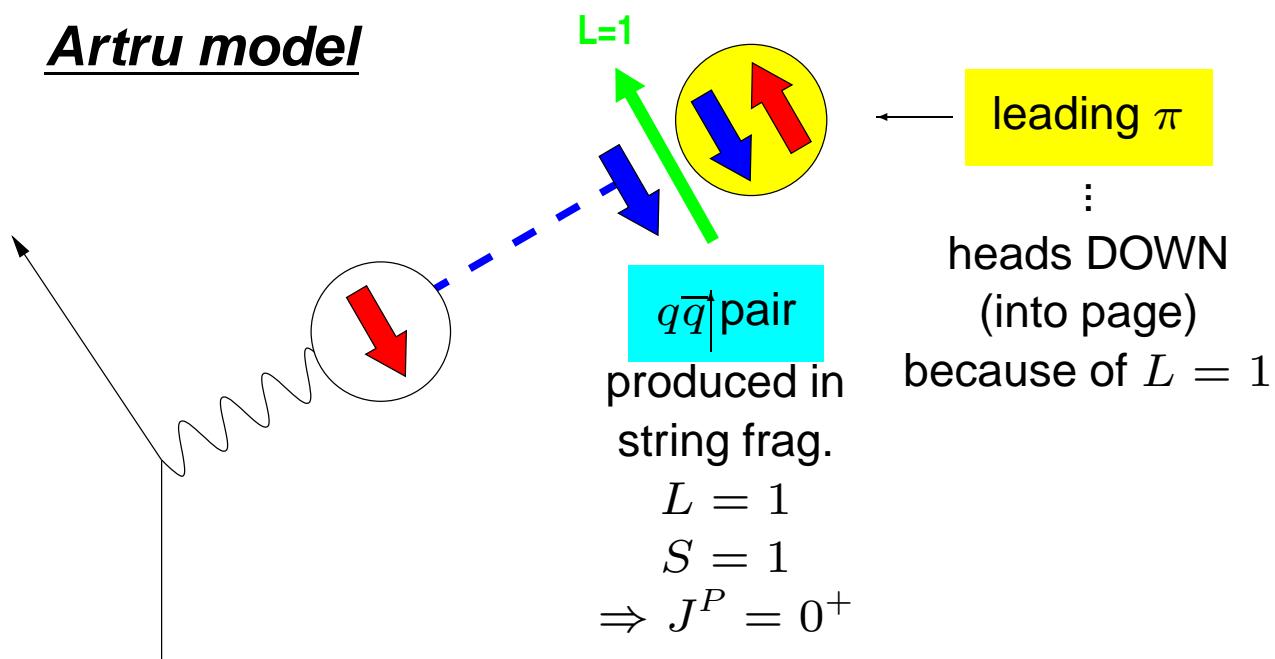


**Neglecting possible diffractive contamination**, there seems to be a

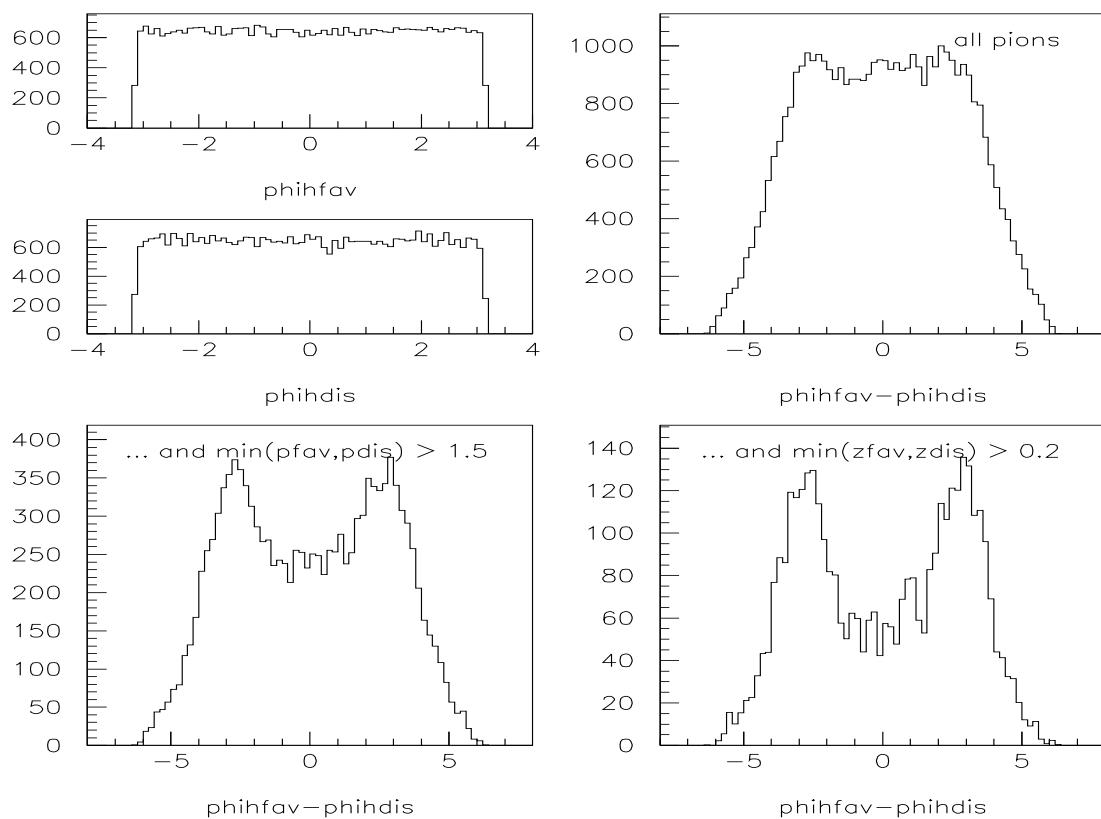
pronounced indication that  $H_{\text{fav}} \approx -H_{\text{dis}}$

# Interpretation of Collins Results

## Artru model



→ **unpolarized Lund Monte Carlo** result on  $\phi$  correlation between favoured and disfavoured pions ...



**Perhaps  $H_{\text{dis}} \approx -H_{\text{fav}}$  is not only reasonable, but likely ?**

## Extracting Distribution Functions

Further analysis using all measured asymmetries (not just ratios):

$$A_{\text{UT}}^{\text{Collins,wt}}(x, z) = \frac{\sum_q e_q^2 \mathbf{h}_1^q(\mathbf{x}) \mathbf{H}_1^{\perp(1), q \rightarrow h}(\mathbf{z})}{\sum_q e_q^2 f_1^q(x) D_1^{q \rightarrow h}(z)} \frac{1-y}{1-y+y^2/2}$$
$$A_{\text{UT}}^{\text{Sivers,wt}}(x, z) = \frac{\sum_q e_q^2 \mathbf{f}_{1\text{T}}^{\perp, q}(\mathbf{x}) \mathbf{D}_1^{q \rightarrow h}(\mathbf{z})}{\sum_q e_q^2 f_1^q(x) D_1^{q \rightarrow h}(z)}$$

- for transversity extraction, Collins FF must be determined
  - need normalization point from **another process**
  - analysis of BELLE  $e^+e^-$  data eagerly awaited!  
(universality seems to be under control for SIDIS and  $e^+e^-$ )
- for Sivers extraction, everything is known to generate purities
- look forward to COMPASS data on **deuterium** target to help disentangle contributions by flavour

# Other Ways to Measure $h_1(x)$

## ① Interference Fragmentation Function to two pions

Analysis is in progress ...

## ② Higher Twist Fragmentation Function $\tilde{E}$

$$d\sigma_{LT} \sim \cos(\phi_S^l) \left[ \frac{Mx}{Q} \cdot g_T(x) D_1(z) + \frac{M_h}{zQ} \cdot \mathbf{h}_1(x) \tilde{E}(z) \right]$$

... calculation of Ji & Zhu suggests  $\tilde{E}(z) = \frac{m_q}{M} z D_1(z) \approx \frac{1}{3} z D_1(z)$

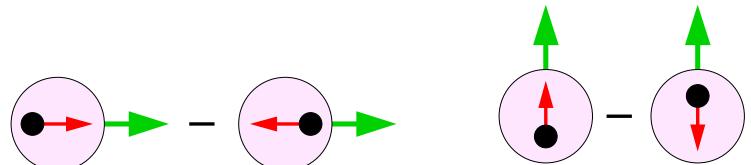
## ③ Final State Polariz<sup>n</sup> (spin transfer to $\Lambda$ )

Method requires significant  
spin transfer from quark to  $\Lambda$   
in fragmentation process ...

$$d\sigma_{UTT} \sim \cos(\phi_S^l + \phi_{S_h}^l) \cdot \mathbf{h}_1(x) H_1(z)$$

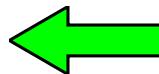
*longitudinal spin transfer:*  $G_1(z)$

*transverse spin transfer:*  $H_1(z)$

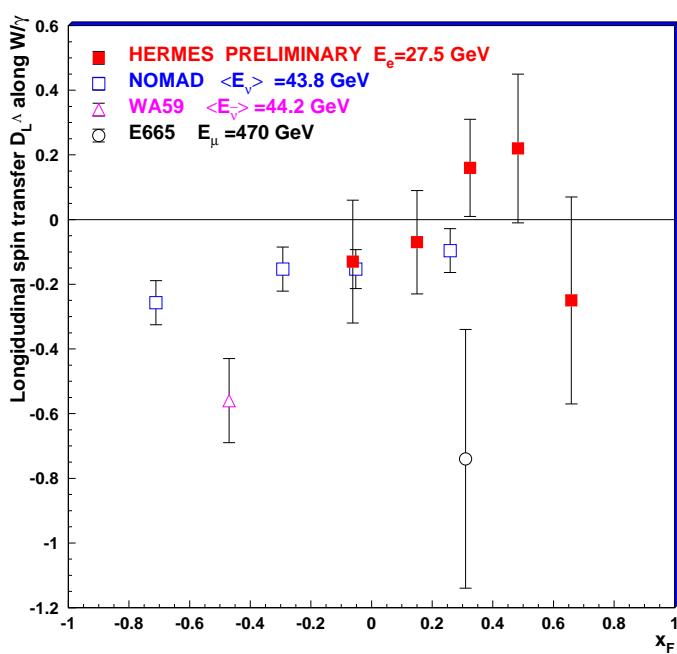


⋮

But longitudinal spin-transfer results from HERMES 2000 data indicate **small**  $G_1(z)$  ...



***not too promising*** ☹





## Conclusions

*A<sub>UT</sub> asymmetries are small and statistics are still limited but ...*

- First observation of ***non-zero Sivers*** effect !
- ***Large Collins*** asymmetries measured for  $\pi^0$  and  $\pi^-$
- Tentative conclusion: **disfavoured** Collins fragmentation function of ***opposite sign*** and similar magnitude to **favoured** function
- Contamination of asymmetries from ***diffractive vector meson*** production must be better constrained and understood
- **More data** eagerly anticipated ... !