

# QUARK ORBITAL ANGULAR MOMENTUM AND EXCLUSIVE PROCESSES AT HERMES

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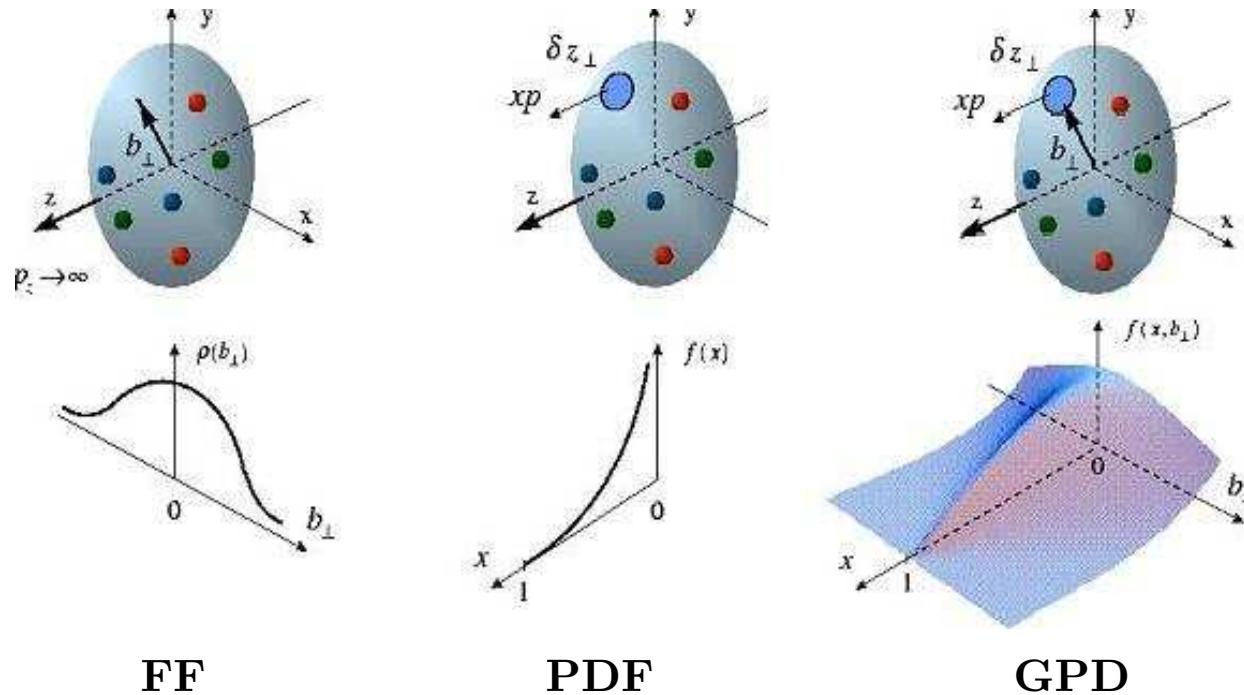
FOR THE HERMES-COLLABORATION

CIPANP, PUERTO RICO, MAY 2006

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- GENERALIZED PARTON DISTRIBUTIONS (GPDS)
- EXCLUSIVE PRODUCTION OF PHOTONS (DVCS) AND MESONS
- HERMES RESULTS
- FIRST MODEL DEPENDENT CONSTRAINT ON QUARK ORBITAL ANGULAR MOMENTUM

# GPDs: PARAMETERIZATION OF THE NUCLEON STRUCTURE



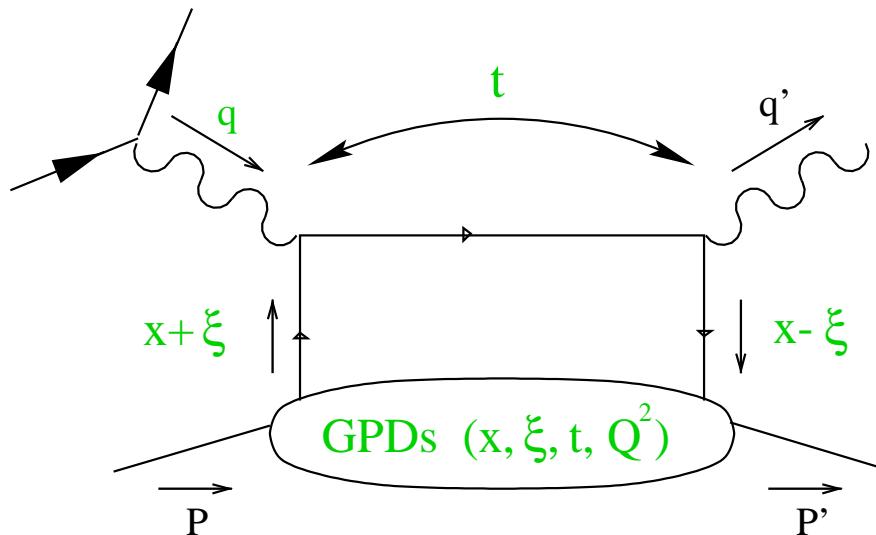
- FORM FACTORS → TRANSVERSE POSITION ← ELASTIC SCATTERING
- PDFs → LONGITUDINAL MOMENTUM DISTRIBUTION ← DIS
- GPDs → ACCESS TO TRANSVERSE POSITION AND LONGITUDINAL MOMENTUM DISTR. AT THE SAME TIME, 3-D PICTURE ← EXCLUSIVE REACTIONS

# GENERALIZED PARTON DISTRIBUTIONS (GPDs)

SIMPLEST/CLEANEST HARD EXCLUSIVE PROCESS:

DEEPLY-VIRTUAL ELECTROPRODUCTION OF REAL PHOTONS:  $e p \rightarrow e' p' \gamma$

DEEPLY-VIRTUAL COMPTON SCATTERING (DVCS):

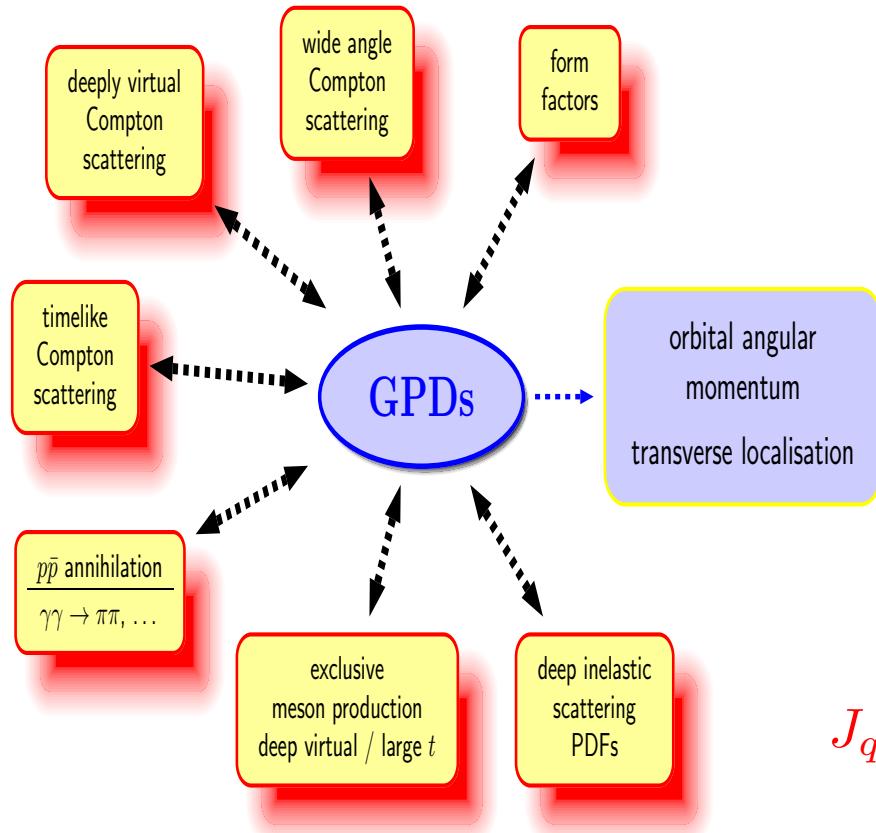


- LONGITUDINAL MOMENTUM FRACTIONS:  
 $x \in [-1, 1]$  (NOT ACCESSIBLE)  
 $\xi \approx x_B / (2 - x_B)$
- $t = (q - q')^2$   
( $\gamma^* \rightarrow \gamma$  MOMENTUM TRANSFER)
- $Q^2 = -q^2$

⇒ MEASUREMENTS AS FUNCTION OF  $x_B$ ,  $t$ ,  $Q^2$

DVCS: ACCESS TO ALL FOUR GPDs  $H$ ,  $\tilde{H}$ ,  $E$ ,  $\tilde{E}$   
MESONS: ACCESS TO  $H$ ,  $E$  (VM) AND  $\tilde{H}$ ,  $\tilde{E}$  (PS)

# OVERVIEW GPDs



PDFs: GPDs IN THE LIMIT  $t \rightarrow 0$   
e.g.  $H(x, 0, 0) = q(x)$

FFs: FIRST MOMENTS OF GPDs  
e.g.  $\int_{-1}^1 dx H(x, \xi, t) = F_1(t)$

ONLY KNOWN (QUANTITATIVE)  
ACCESS TO (TOTAL)  
ORBITAL ANGULAR MOMENTUM:

$$J_q = \lim_{t \rightarrow 0} \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

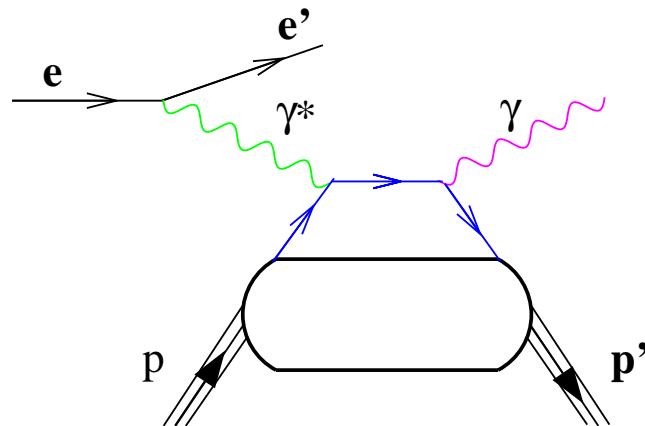
(ORIGINAL) HERMES MOTIVATION:

NUCLEON (LONG.) SPIN STRUCTURE:  $1/2 = \underbrace{1/2(\Delta u + \Delta d + \Delta s)}_{J_q=?} + \overbrace{L_q}^{\text{?}} + \overbrace{J_g}^{\text{?}}$

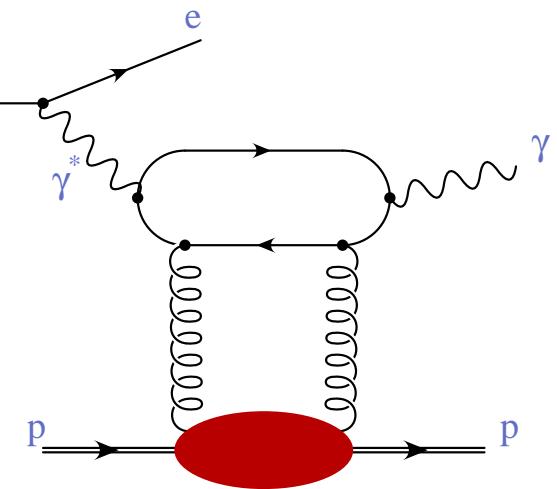
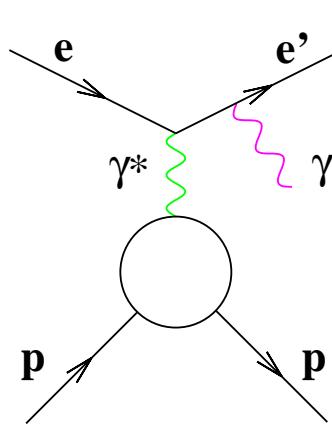


# HowTo ACCESS GPDS VIA DVCS?

DVCS FINAL STATE  $e + p \rightarrow e' + p' + \gamma$  IS INDISTINGUISHABLE FROM THE BETHE-HEITLER PROCESS (BH) → AMPLITUDES ADD COHERENTLY



FIXED-TARGET, COLLIDER



COLLIDER

PHOTON-PRODUCTION CROSS SECTION:

$$d\sigma \propto |\tau_{\text{DVCS}} + \tau_{\text{BH}}|^2 = |\tau_{\text{DVCS}}|^2 + |\tau_{\text{BH}}|^2 + \underbrace{(\tau_{\text{DVCS}}^* \tau_{\text{BH}} + \tau_{\text{BH}}^* \tau_{\text{DVCS}})}_I$$

# DVCS MEASUREMENTS

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$$d\sigma \propto |\tau_{\text{BH}}|^2 + \underbrace{(\tau_{\text{DVCS}}^* \tau_{\text{BH}} + \tau_{\text{BH}}^* \tau_{\text{DVCS}})}_I + |\tau_{\text{DVCS}}|^2$$

$|\tau_{\text{BH}}|^2$  CALCULABLE IN QED WITH THE KNOWLEDGE OF THE FORM FACTORS

$$I \propto \pm \left( c_0^I + \sum_{n=1}^3 c_n^I \cos(n\phi) + \lambda \sum_{n=1}^3 s_n^I \sin(n\phi) \right)$$

DVCS CROSS SECTION (H1, ZEUS):

MEASUREMENT INTEGRATED OVER  $\phi$

$\rightarrow I = 0$  (AT TWIST-2), SUBTRACT  $|\tau_{\text{BH}}|^2$

(GPDs ENTER IN QUADRATIC COMBINATIONS)

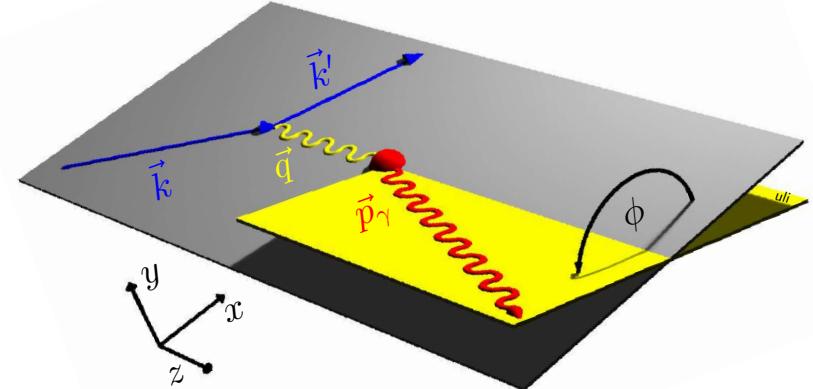
AZIMUTHAL ASYMMETRIES

(HERMES, JLAB):

DVCS AMPLITUDES DIRECTLY ACCESSIBLE

VIA  $I \Rightarrow$  MAGNITUDE + PHASE!!!

(GPDs ENTER IN LINEAR COMBINATIONS)



# AZIMUTHAL ASYMMETRIES

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$$I \propto \pm(c_0^I + \sum_n [c_n^I \cos(n\phi) + \lambda s_n^I \sin(n\phi)])$$

BEAM-SPIN ASYMMETRY (BSA) AND BEAM-CHARGE ASYMMETRY (BCA)  
ON UNPOLARIZED TARGET:

$$\text{BSA} : d\sigma(\vec{e^+}p) - d\sigma(\overleftarrow{e^+}p) \sim s_{1,unp}^I \sin(\phi) \sim \sin(\phi) \times \text{Im } M_{unp}^{1,1}$$

$$\text{BCA} : d\sigma(e^+p) - d\sigma(e^-p) \sim c_{1,unp}^I \cos(\phi) \sim \cos(\phi) \times \text{Re } M_{unp}^{1,1}$$

(HIGHER TWIST/ORDER  $\rightarrow \cos 2\phi, \cos 3\phi, \sin 2\phi$ )

$$M_{unp}^{1,1} = F_1(t) H_1(\xi, t) + \frac{x_B}{2-x_B} (F_1(t) + F_2(t)) \tilde{H}_1(\xi, t) - \frac{t}{4M^2} F_2(t) E_1(\xi, t)$$

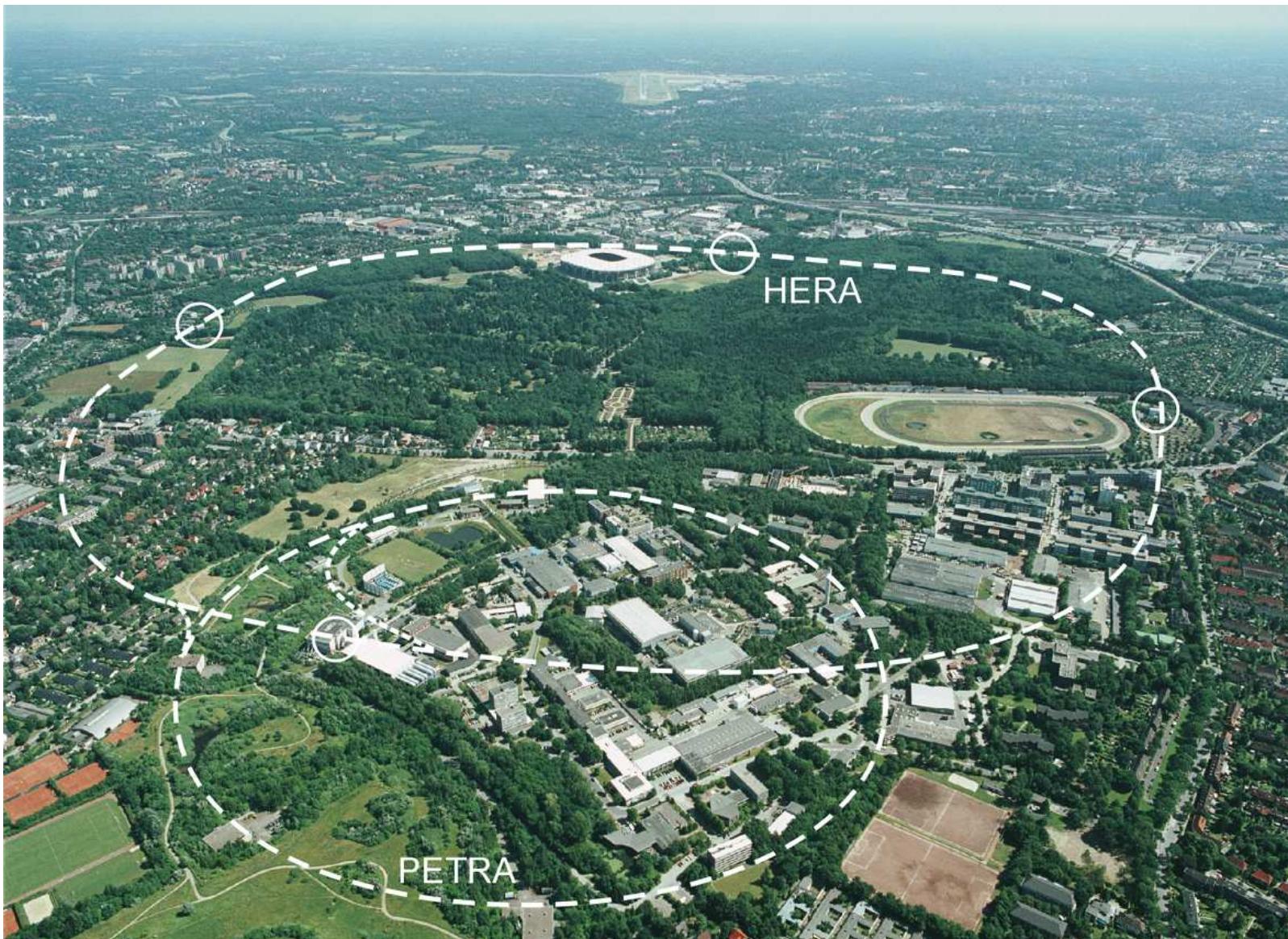
$\langle x_B \rangle, \langle -t \rangle \approx 0.1 \Rightarrow$  COMPTON FORM-FACTOR  $H_1 \Rightarrow$  GPD  $H$

NEED BOTH CHARGES AND POLARIZED BEAM  
 $\Rightarrow$  HERA!!!



# THE HERA ACCELERATOR AT DESY (HAMBURG)

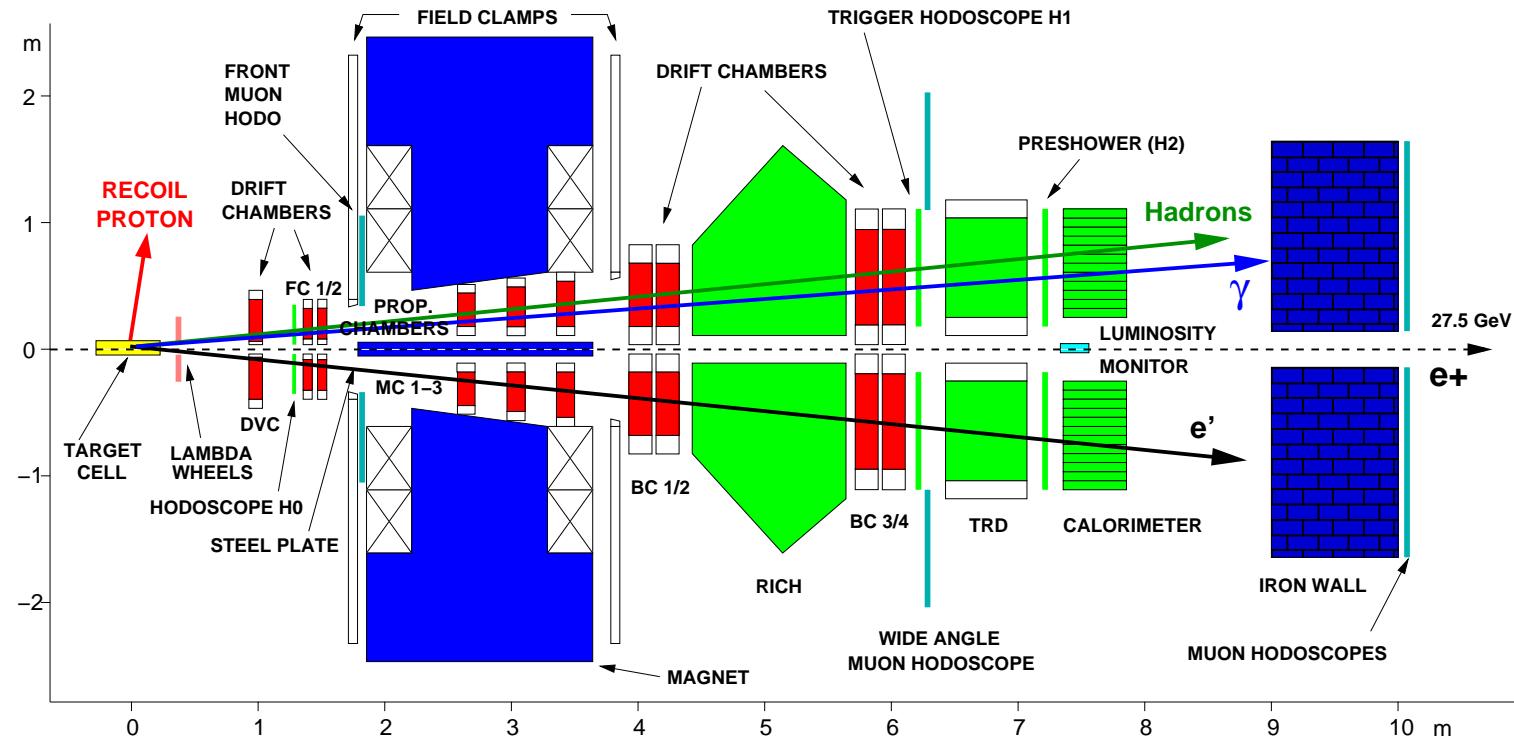
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Frank Ellinghaus, Puerto Rico, May 2006

# HERMES EVENT SELECTION

HERA BEAM: 27.6 GeV,  $e^+$  AND  $e^-$ ,  $\langle P \rangle \approx 35 - 55\%$

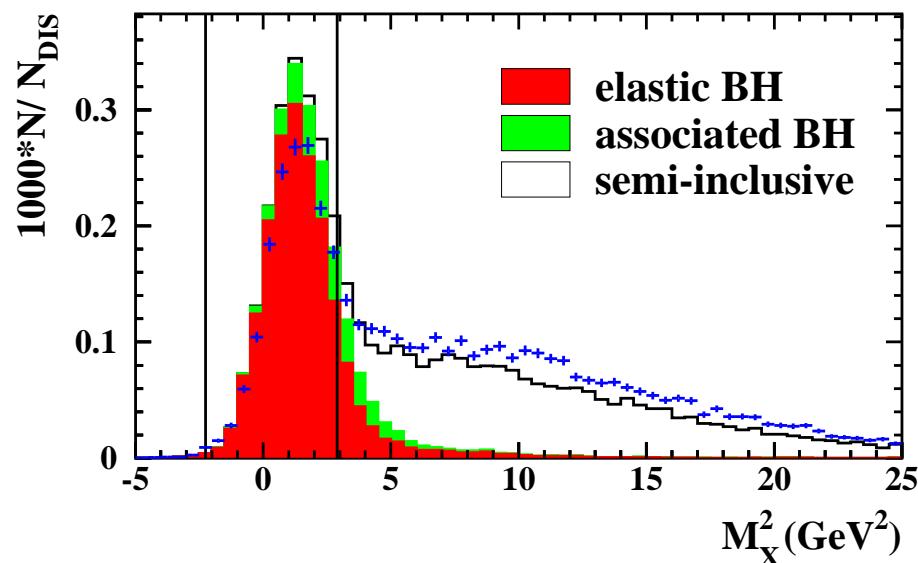


EVENTS WITH EXACTLY ONE DIS-POSITRON/DIS-ELECTRON AND EXACTLY ONE PHOTON IN THE CALORIMETER (OR ONE ( $\rho^0 \rightarrow \pi^+\pi^-$  PAIR))

NO RECOIL DETECTION (YET)  $\Rightarrow$  EXCLUSIVITY VIA ...

# EXCLUSIVITY FOR DVCS VIA MISSING MASS

$M_x^2 \equiv (q + p - p_\gamma)^2 \Rightarrow$  MC FOR BACKGROUND AND CUTS ( $\rightarrow$  RESOLUTION)!



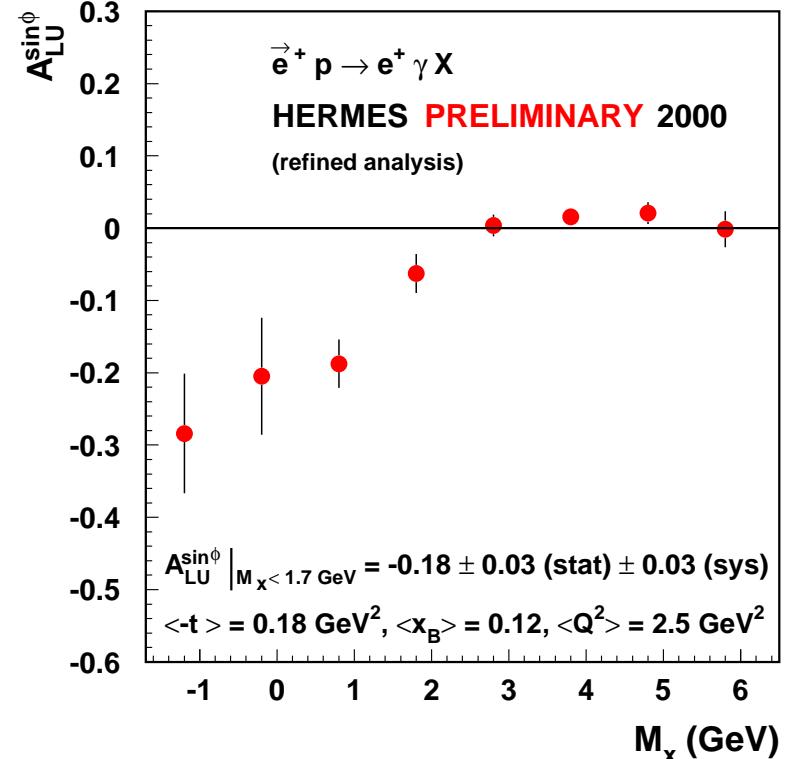
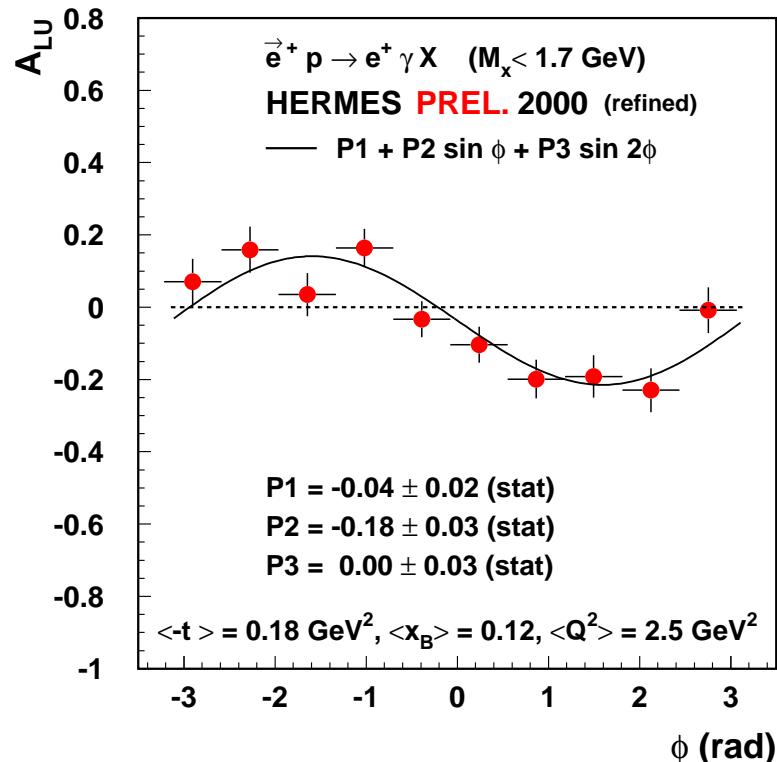
- ELASTIC BH ( $e p \rightarrow e' p' \gamma$ )
- ASSOCIATED BH  
(MAINLY  $e p \rightarrow e' \Delta^+ \gamma$ )
- SEMI-INCLUSIVE  
(MAINLY  $e p \rightarrow e' \pi^0 X$ )
- EXCLUSIVE  $\pi^0$  ( $e p \rightarrow e' \pi^0$ )  
NOT SHOWN (SMALL)

NOT SIMULATED: DVCS PROCESS (DVCS c.s. “UNKNOWN”, DVCS  $\ll$  BH)  
+ RADIATIVE CORRECTIONS TO BH ( $\rightarrow$  EXCL. PEAK OVERESTIMATED, BG UNDERESTIMATED)

$\Rightarrow$  “EXCLUSIVE” BIN ( $-1.5 < M_x < 1.7$  GeV)  
 $\Rightarrow$  OVERALL BACKGROUND CONTRIBUTION  $\approx 15\%$

# BEAM-SPIN ASYMMETRY (BSA)

$$A_{LU}(\phi) = \frac{1}{<|P_b|>} \frac{\vec{N}(\phi) - \overleftarrow{N}(\phi)}{\vec{N}(\phi) + \overleftarrow{N}(\phi)}$$



$A_{LU}$  IN EXCLUSIVE BIN: EXPECTED  
 $\sin(\phi)$  DEPENDENCE  $\Rightarrow \text{Im } M_{unp}^{1,1}$

$\sin(\phi)$ -MOMENT IN NON-EXCLUSIVE  
REGION: SMALL AND SLIGHTLY  
POSITIVE ( $\rightarrow \pi^0$ )

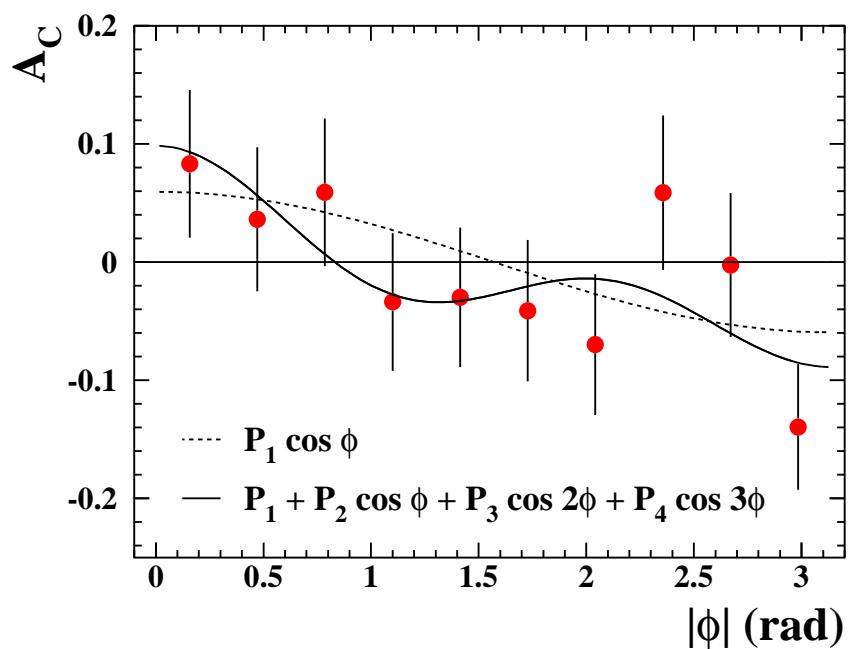
(RESULTS FROM 1996/97 → PRL **87**, 182001 (2001))



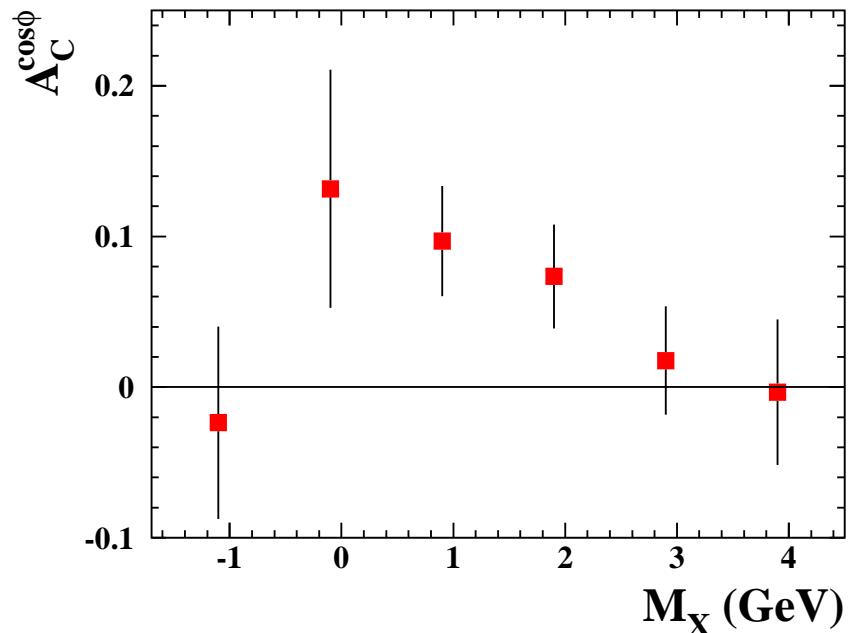
# BCA: BEAM-CHARGE ASYMMETRY (*hep-ex/0605108, subm. to PRL*)

$$A_C(\phi) = \frac{N^+(\phi) - N^-(\phi)}{N^+(\phi) + N^-(\phi)} \propto I \propto \pm(c_0^I + \sum_{n=1}^3 c_n^I \cos(n\phi) + \lambda \sum_{n=1}^2 s_n^I \sin(n\phi))$$

$\Rightarrow$  CALCULATE “SYMMETRIZED” BCA ( $\phi \rightarrow |\phi|$ ) TO GET RID OF ALL  $\sin(\phi)$ -DEPENDENCES DUE TO POLARIZED BEAM.



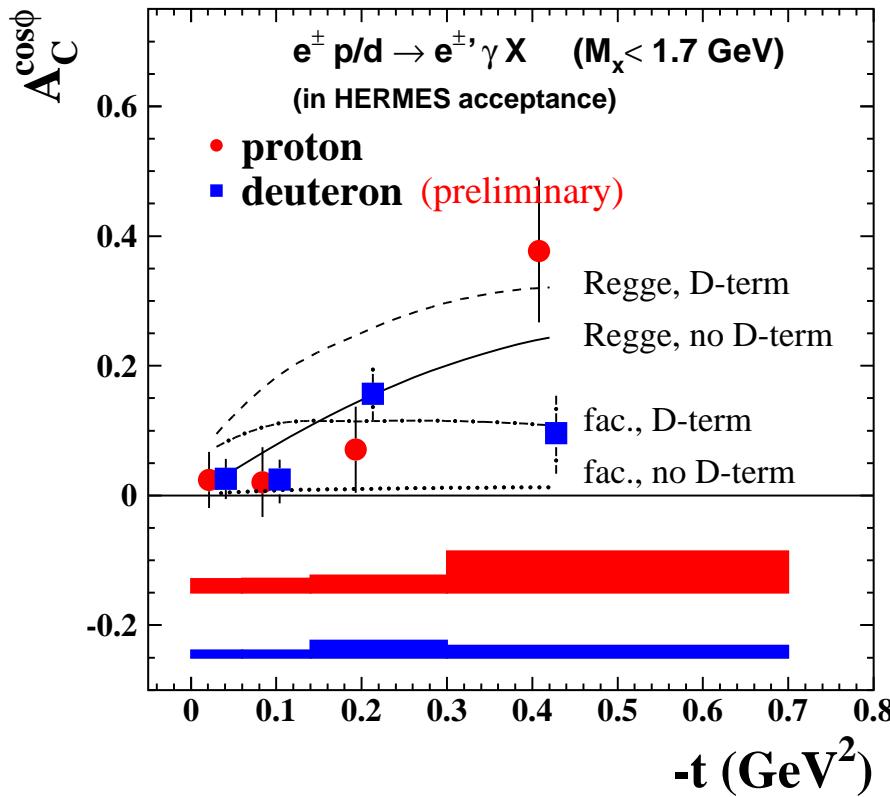
$A_C$  IN EXCLUSIVE BIN: EXPECTED  
 $\cos(\phi)$  DEPENDENCE  $\Rightarrow \text{Re } M_{unp}^{1,1}$



$\cos(\phi)$ -MOMENTS ZERO AT HIGHER  
MISSING MASS

# BEAM-CHARGE ASYMMETRY (BCA) VERSUS $-t$

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ALSO: DVCS ON DEUTERIUM:  
COHERENT PRODUCTION ON D ONLY  
IN FIRST  $t$ -BIN ( $\approx 40\%$ )  
⇒ NO EFFECT SEEN  
→  $\approx$  P-TARGET  
POSSIBLE DIFFERENCE IN LAST BIN  
(→ NEUTRON)

GPD MODEL CALC. AT AVERAGE KINEMATIC VALUES PER BIN  
(CODE BY VANDERHAEGHEN, GUICHON, GUIDAL)

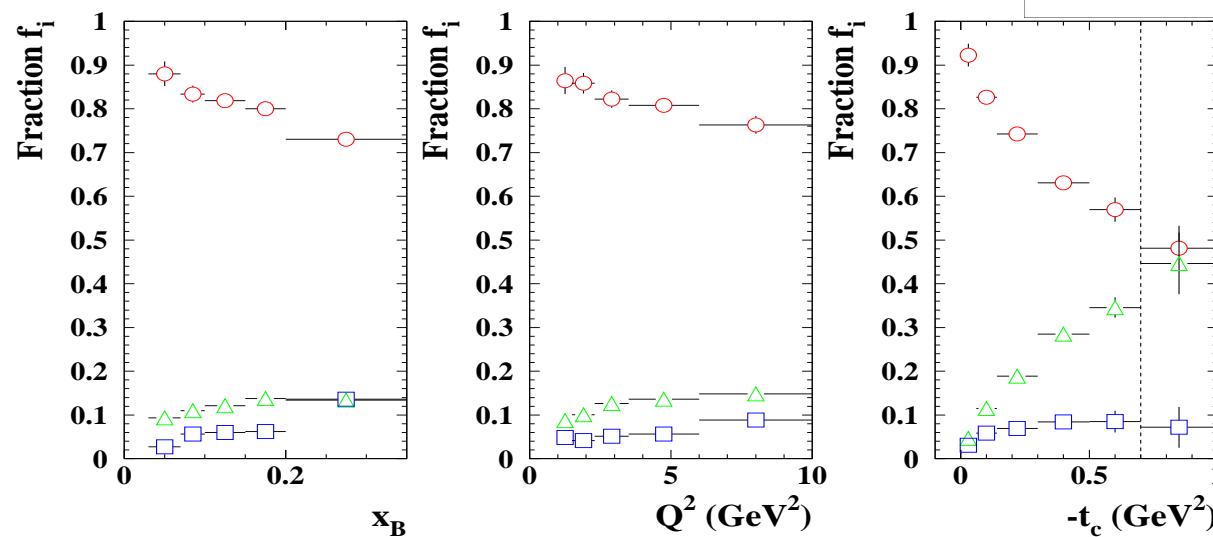
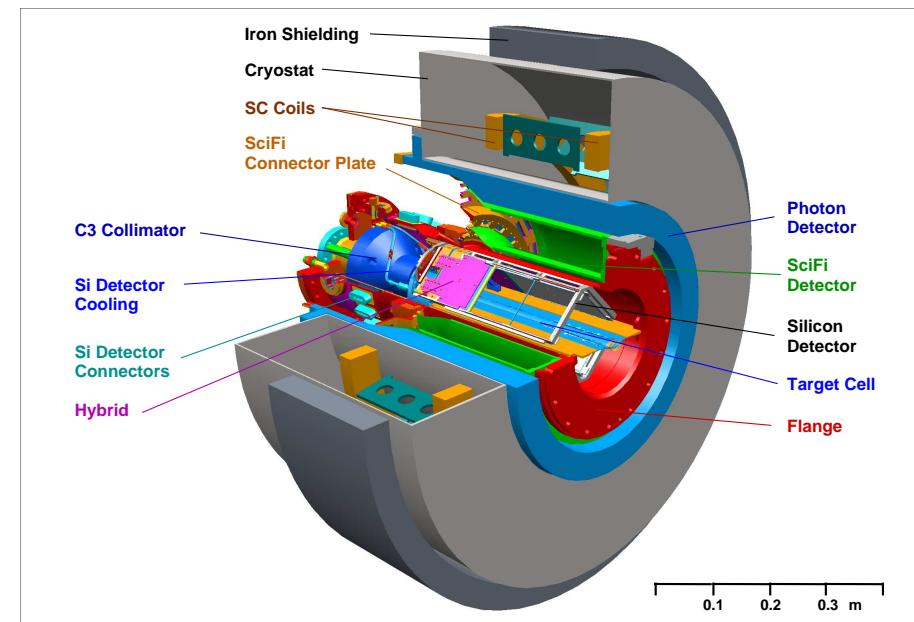
TINY  $e^-p$  SAMPLE ( $L \approx 10 \text{ PB}^{-1}$ ) ⇒ REGGE+D-TERM DISFAVORED  
⇒  $t$ -DEPENDENCE OF BCA HAS HIGH SENSITIVITY TO GPD MODELS!

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# MORE ON H TO COME

## RECOIL DETECTOR AND UNPOL. TARGETS (2006/2007)

- ENSURES EXCLUSIVITY OF EVENTS
  - SEMI-INCLUSIVE BACKGROUND  
 $5\% \Rightarrow \ll 1\%$
  - ASSOCIATED BACKGROUND 10%  
 $\Rightarrow \approx 1\%$

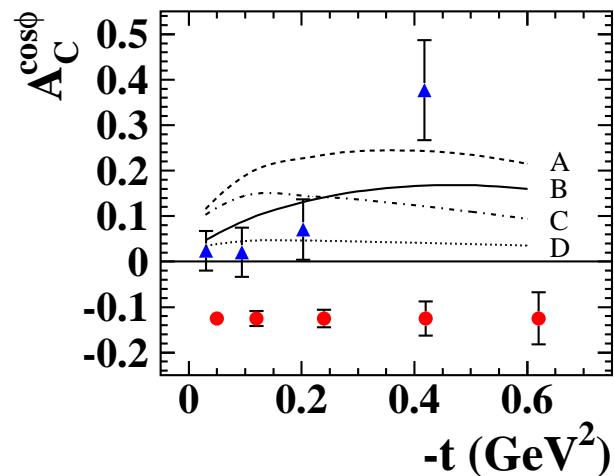


$\Rightarrow$  ESSENTIAL AT  
LARGER  $-t$  VALUES

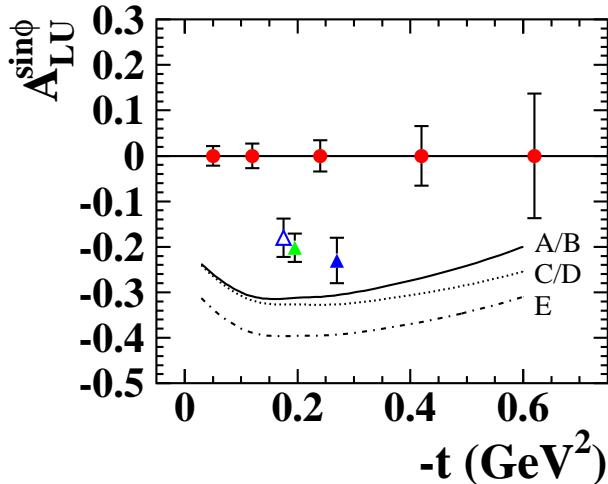
# THE GPD H, SUMMARY AND OUTLOOK

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BCA



BSA



$\triangle$ : HERMES PRELIM./PUBLISHED

$\triangle$ : CLAS, PRL, 2001 ( $\times -1$ )

$\bullet$ :  $1fb^{-1} e^+$  AND  $0.25fb^{-1} e^-$ , POL. = 35% (EXP. 2002-2007 DATA)

**BCA**: HIGH SENSITIVITY TO  $t$ -DEPENDENCE (FACT./REGGE) AND D-TERM

**BSA**: HIGHEST SENSITIVITY TO  $b_s$  PARAMETER IN PROFILE FUNCTION

POSSIBILITY TO “MAP OUT” GPD  $H^u$  IN THE FINAL TWO HERA YEARS.



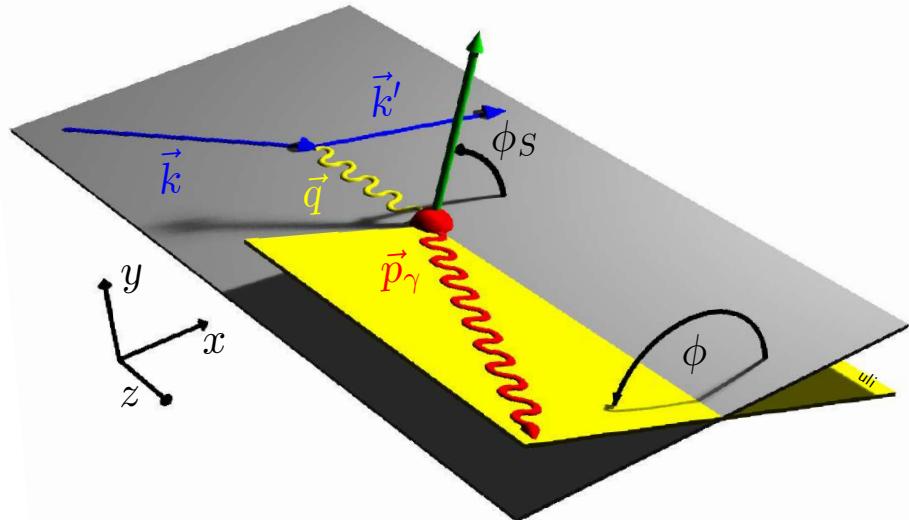
# WHAT ABOUT THE GPD $E$ ?

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REMEMBER:

$$J_q = \lim_{t \rightarrow 0} \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

GPD  $E$  IS ALWAYS KINEMATICALLY SUPPRESSED, EXCEPT IN:  
 $A_{UT}$ : UNPOLARIZED BEAM,  
 TRANSVERSELY POL. TARGET

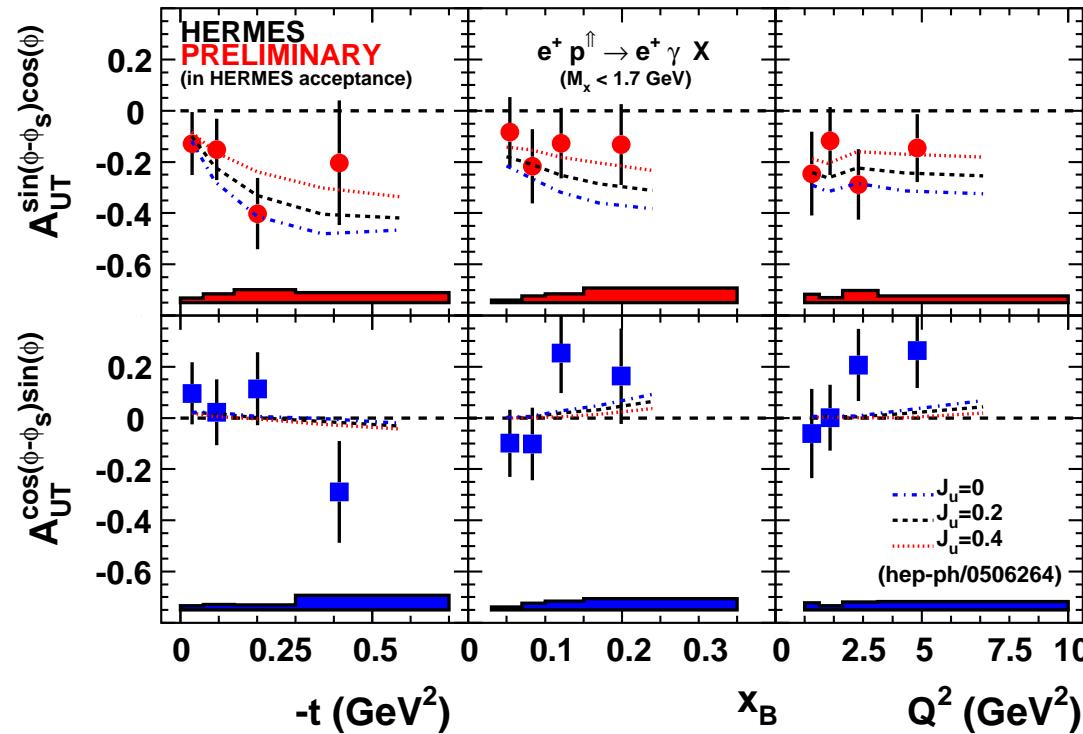


$$A_{UT}(\phi, \phi_s) = \frac{1}{|P_T|} \cdot \frac{d\sigma^{\uparrow}(\phi, \phi_s) - d\sigma^{\downarrow}(\phi, \phi'_s)}{d\sigma^{\uparrow}(\phi, \phi_s) + d\sigma^{\downarrow}(\phi, \phi'_s)}$$

$$\propto \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}] \cdot \sin(\phi - \phi_s) \cos \phi + \text{Im}[F_2 \tilde{\mathcal{H}} - F_1 \xi \tilde{\mathcal{E}}] \cdot \cos(\phi - \phi_s) \sin \phi$$

# DVCS TTSA COMPARED TO THE MODEL CALCULATIONS!

DATA TAKING WITH TRANSVERSE HYDROGEN TARGET FINISHED  
 ≈ 10 MILLION ON TAPE, HALF THE DATA (2002-2004) ANALYZED

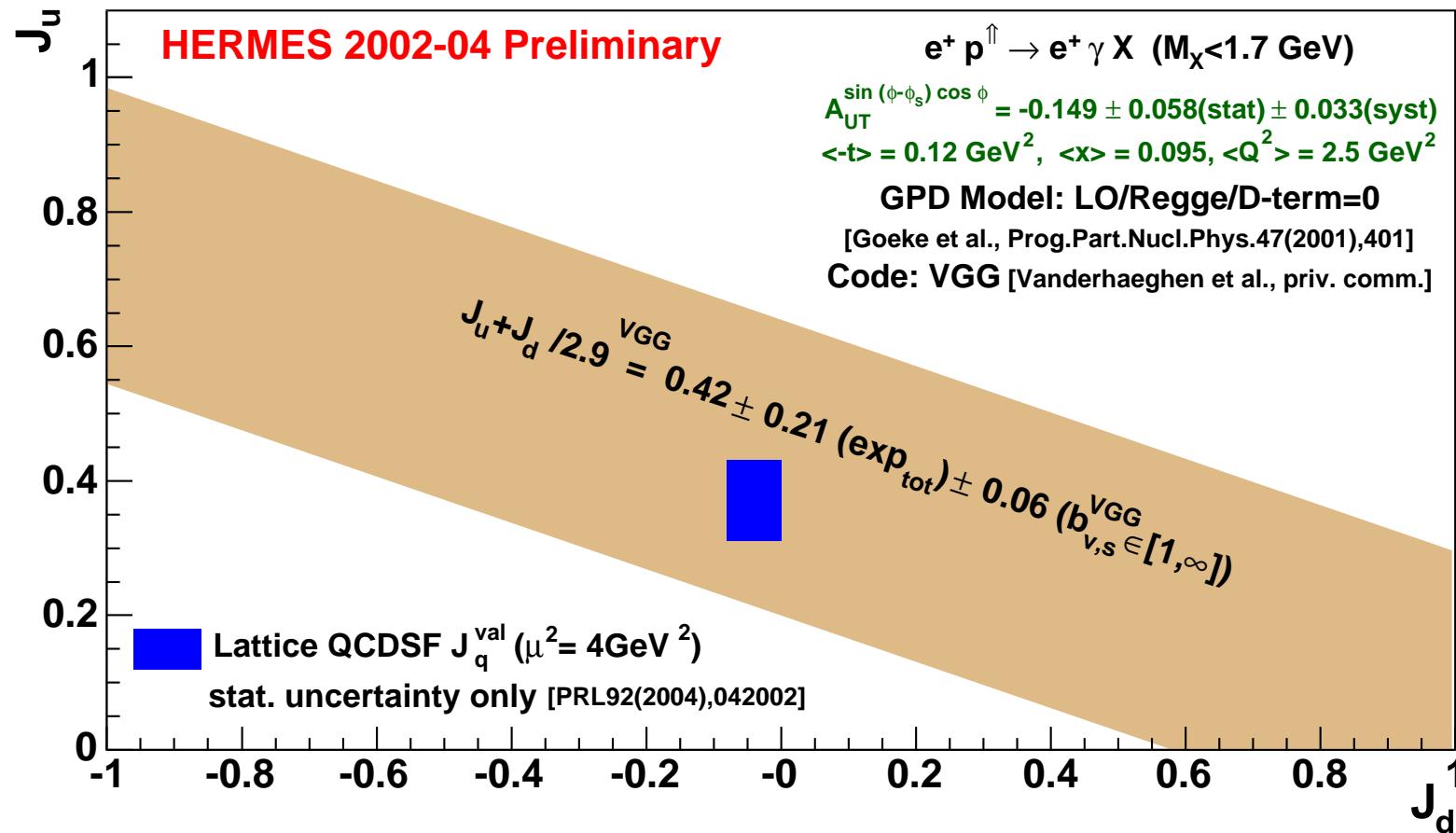


$A_{UT}^{\sin(\phi-\phi_s)\cos\phi}$  LARGELY INDEPENDENT ON ALL MODEL PARAMETERS BUT  $J_u$   
 (F.E., NOWAK, VINNIKOV, YE, HEP-PH/0506264)

⇒ FIRST MODEL DEPENDENT EXTRACTION OF  $J_u$  POSSIBLE!



# FIRST CONSTRAINT ON ANGULAR MOMENTUM !

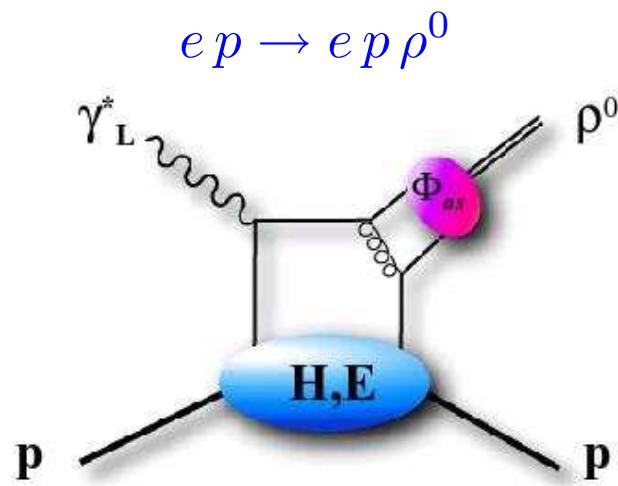


⇒ FIRST MODEL DEPENDENT CONSTRAINT ON TOTAL QUARK ANGULAR MOMENTUM  $J_u, J_d$ .



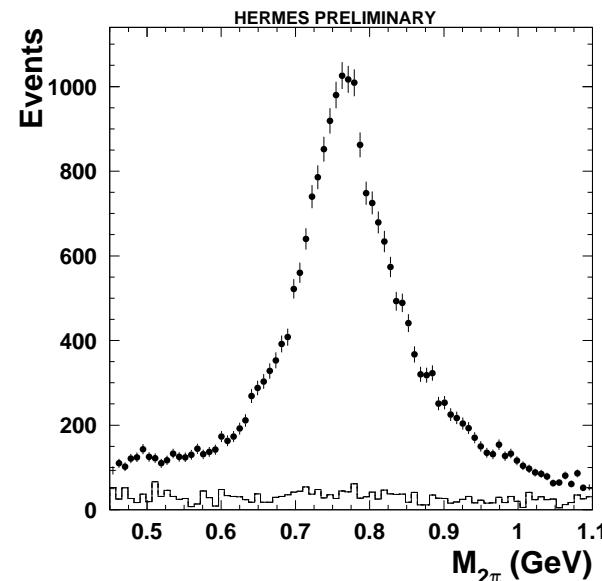
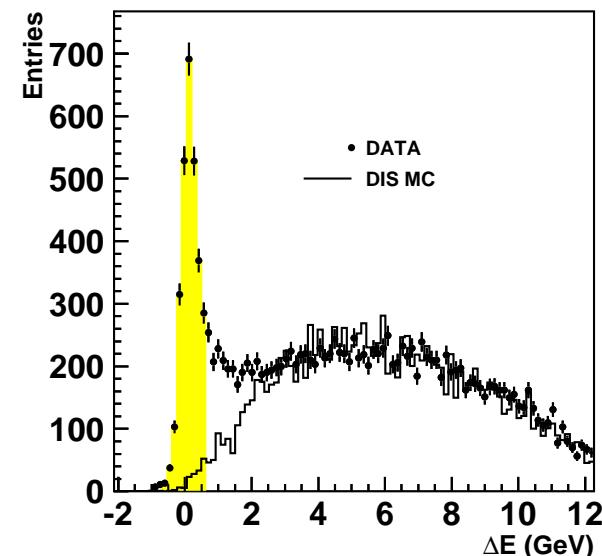
# EXCLUSIVE VECTOR MESON PRODUCTION

THE (ONLY) OTHER (PROMISING)  
ACCESS TO E (J) (ON A P TARGET):  
 $A_{UT}$  IN EXCLUSIVE  $\rho^0$  PRODUCTION:



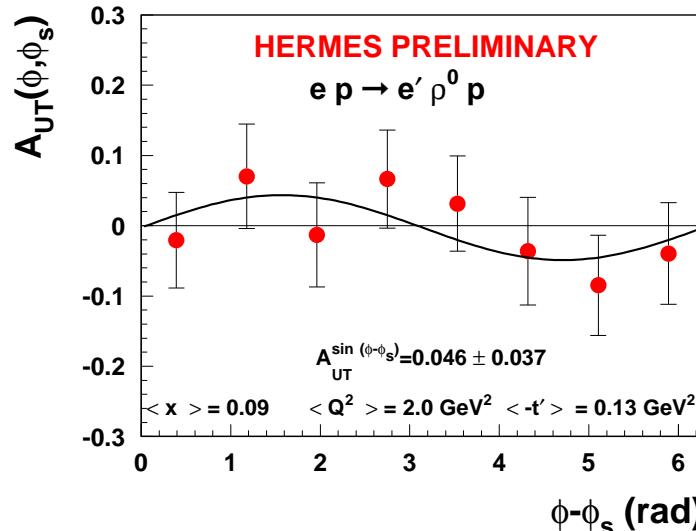
EVENT SELECTION:

- $\rho^0 \rightarrow \pi^+ \pi^-$ ,
- NO RECOIL DETECTION
- → MISSING ENERGY

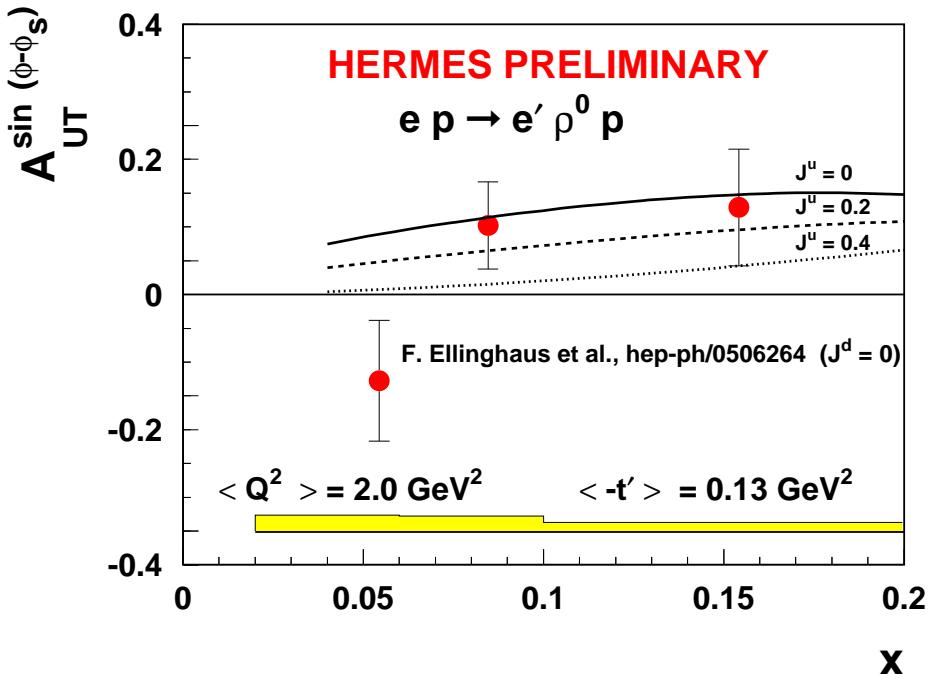


# THE GDP $E$ IN THE TRANSV. TARGET-SPIN ASYMMETRY

$$A_{UT}(\phi, \phi_s) = \frac{1}{|P_T|} \cdot \frac{d\sigma^{\uparrow}(\phi, \phi_s) - d\sigma^{\downarrow}(\phi, \phi_s)}{d\sigma^{\uparrow}(\phi, \phi_s) + d\sigma^{\downarrow}(\phi, \phi_s)} \propto H E \cdot \sin(\phi - \phi_s)$$



EXPECTED  $\sin \phi$  BEHAVIOR  
 (NO L/T SEPARATION YET)



AGREEMENT WITH THEORETICAL CALCULATION.  
 (CALCULATION/FACTORIZATION PROOF FOR LONGITUDINAL PHOTONS ONLY)

AGAIN: SAME SIZE DATA SET TO COME,  $A_{UT}^\rho$  LESS SENSITIVE TO  $J_u$  WHEN COMPARED TO  $A_{UT}^{DVCS} \rightarrow$  PROVIDE ADDITIONAL CONSTRAINTS



# SUMMARY

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- HARD EXCLUSIVE PROCESSES PROBE GPDs
- RESULTS SO FAR IN GENERAL AGREEMENT WITH BASIC MODELS AND ASSUMPTIONS.
- 2006/2007 DATA TAKING (+RECOIL DETECTOR) DEVOTED TO EXCLUSIVE REACTIONS:  
→ “MAP OUT” GPD  $H^u$  VIA DVCS BEAM-SPIN AND BEAM-CHARGE ASYMMETRY
- DVCS ON TRANSVERSE POLARIZED TARGET:  
FIRST MODEL DEPENDENT CONSTRAINT ON THE TOTAL ANGULAR MOMENTUM OF U-QUARKS ( $J_u$ ) AND D-QUARKS ( $J_d$ ) IN THE NUCLEON.

