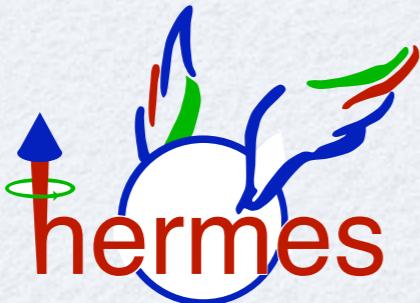


LATEST NEWS ON DVCS FROM HERMES



Caroline Riedl
EIC Meeting at BNL
August 25, 2009

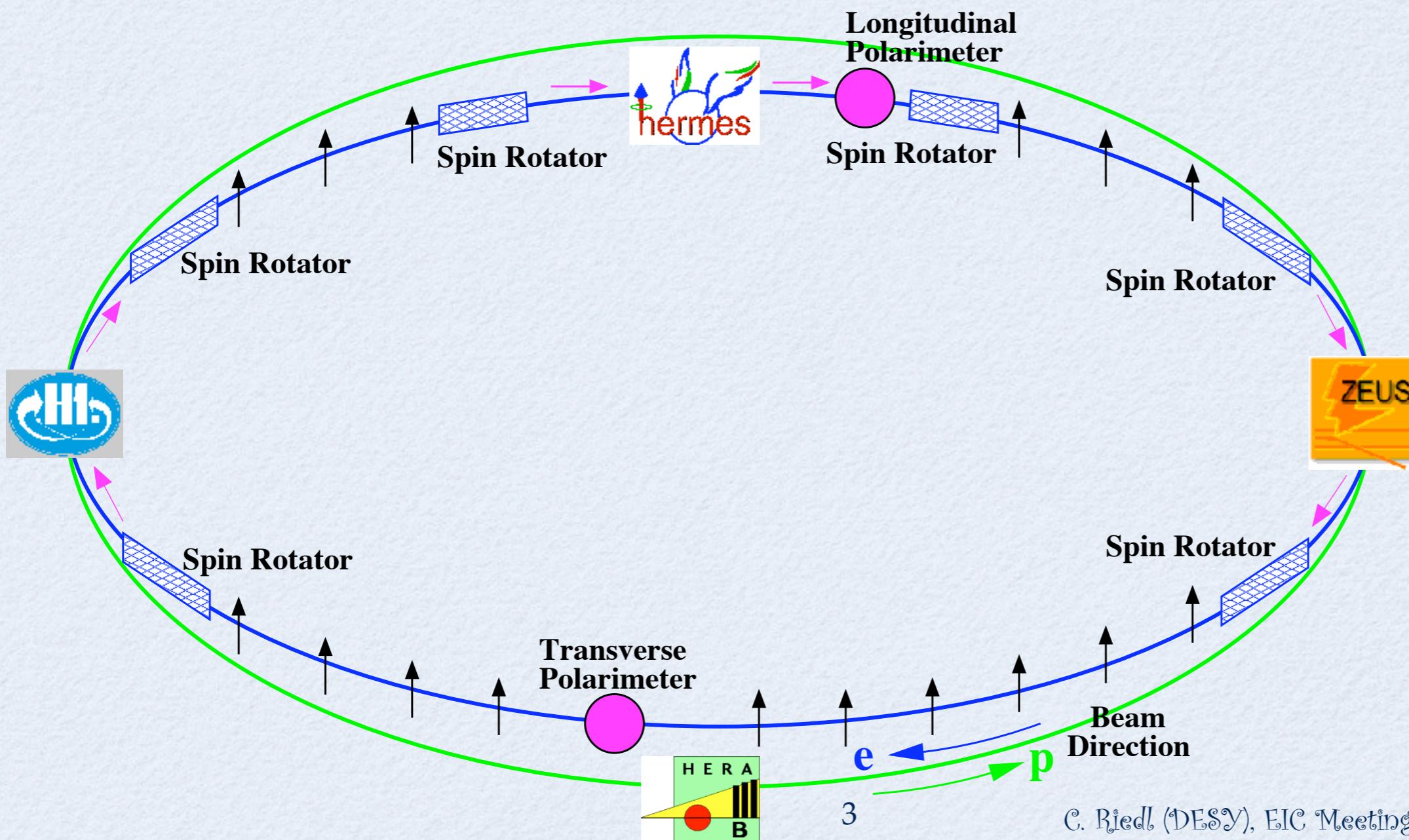


Latest News on DVCS from HERMES

- * Appetizer: HERA and HERMES
- * Motivation: Generalized Parton Distributions, orbital angular momentum and 3-dimensional nucleon structure
- * Measurements of azimuthal asymmetries in DVCS
 - * Beam helicity and charge asymmetries on hydrogen and nuclear targets
 - * Transverse target spin asymmetry on hydrogen
- * A Recoil Detector for HERMES

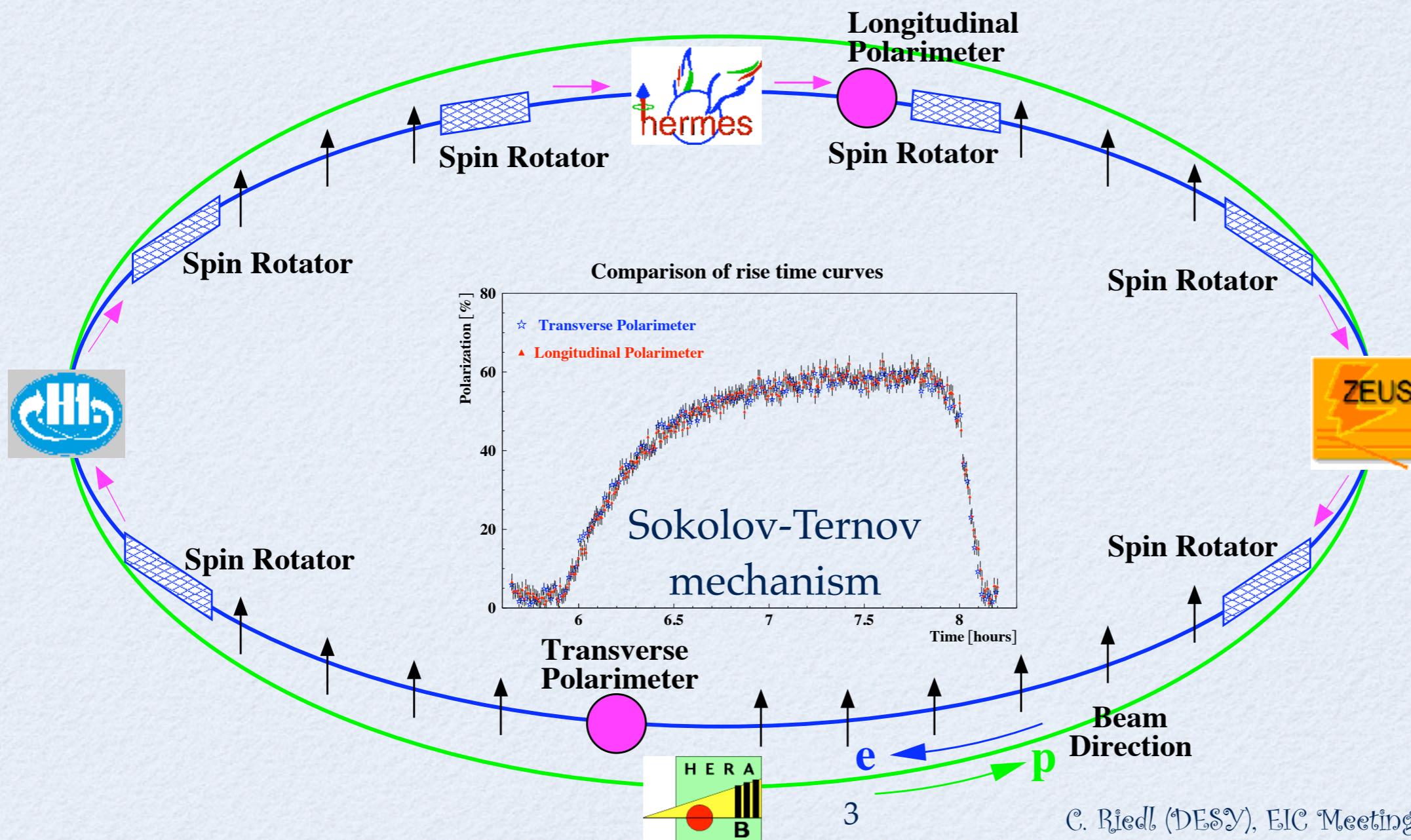
HERA @ DESY in Hamburg, Germany

- * Polarized electron/positron beam of 27.6 GeV and 40mA
- * Beam polarization 30...65%, 2 beam helicities
- * Proton beam of 920 GeV / 90 mA

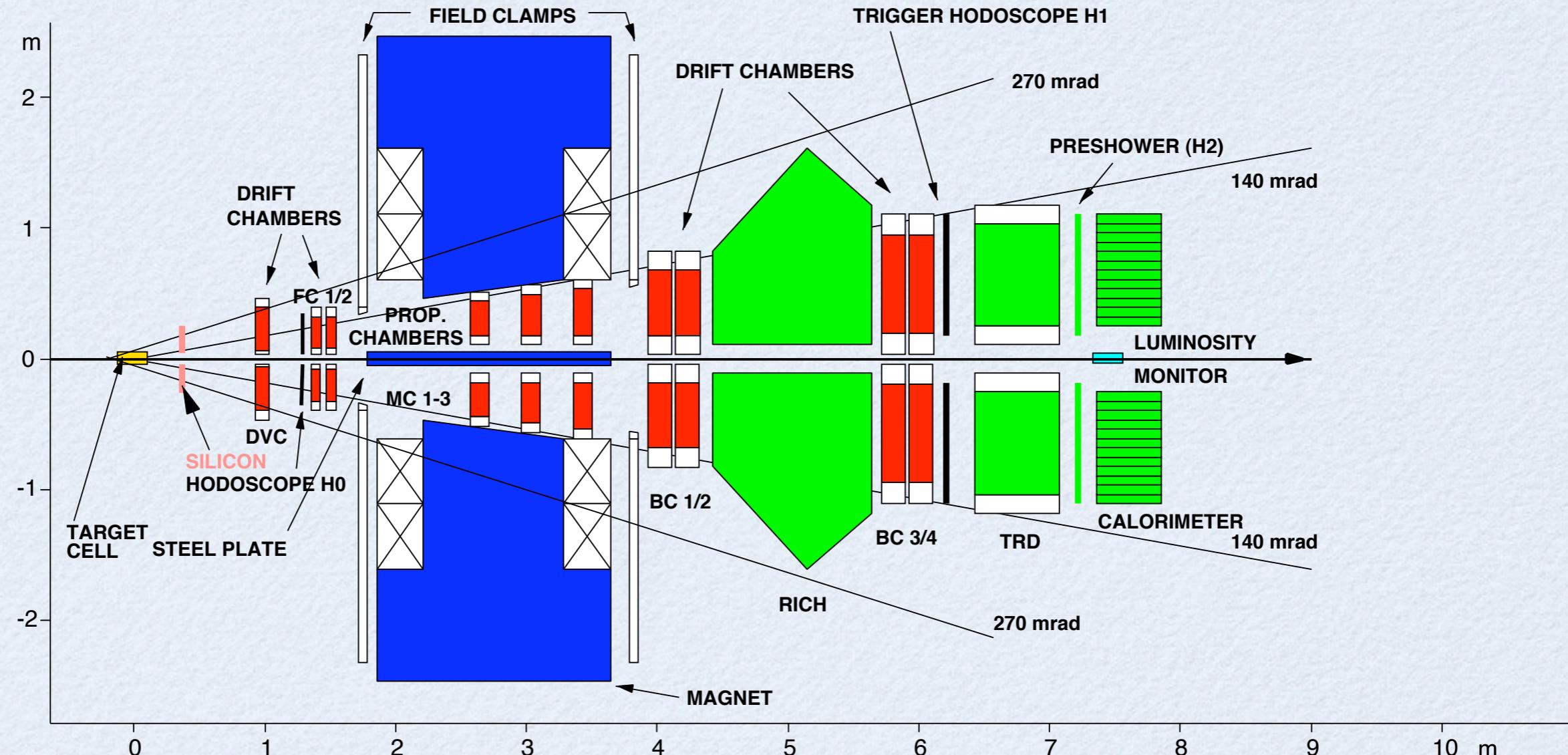


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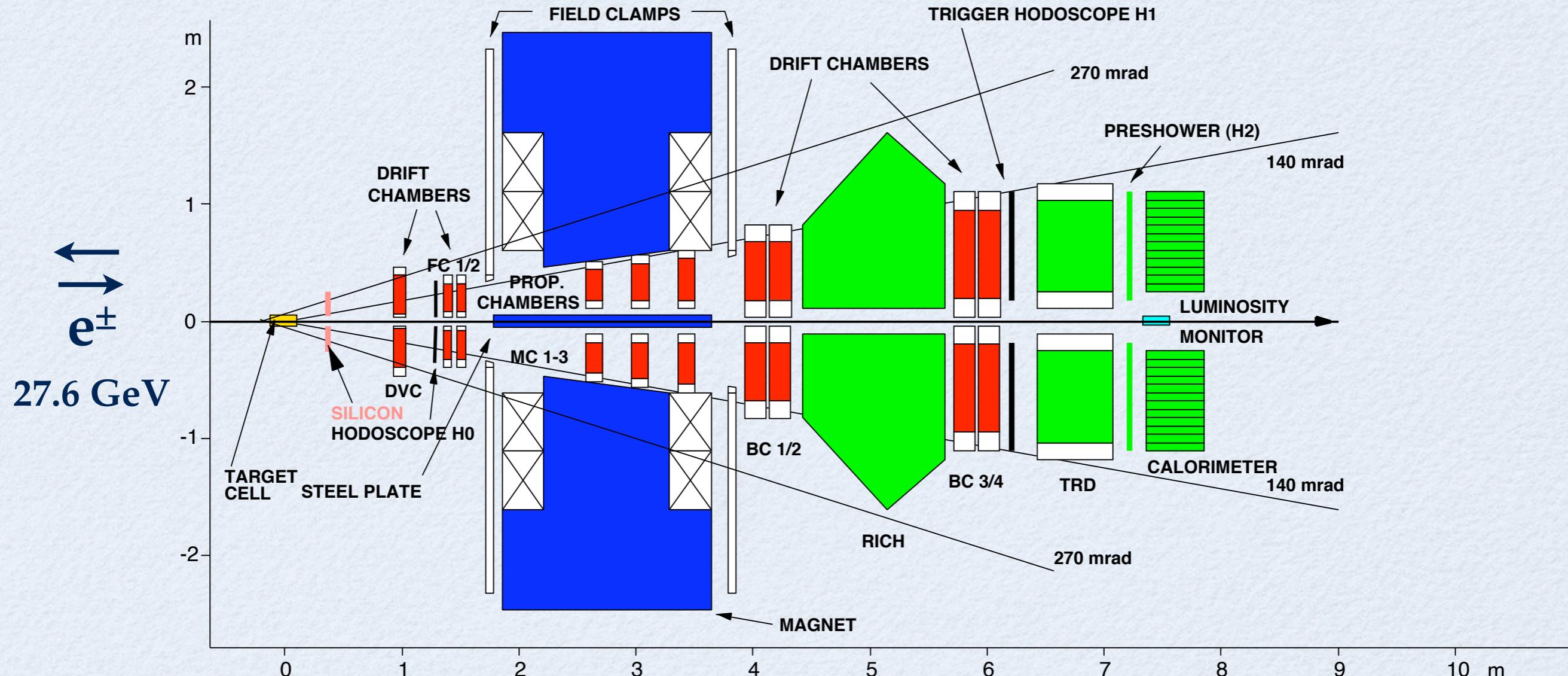
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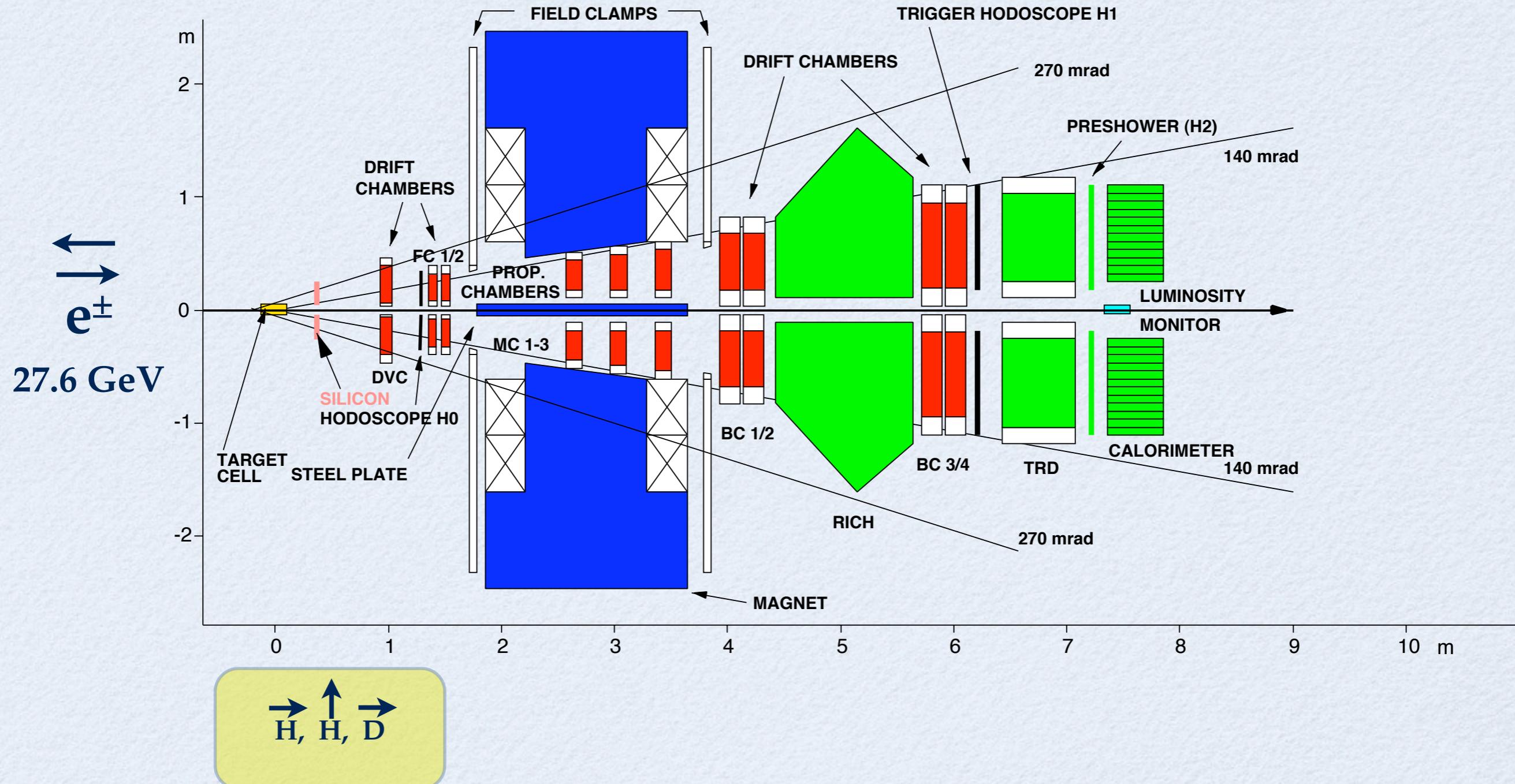
HERMES: HERa MEasurement of Spin



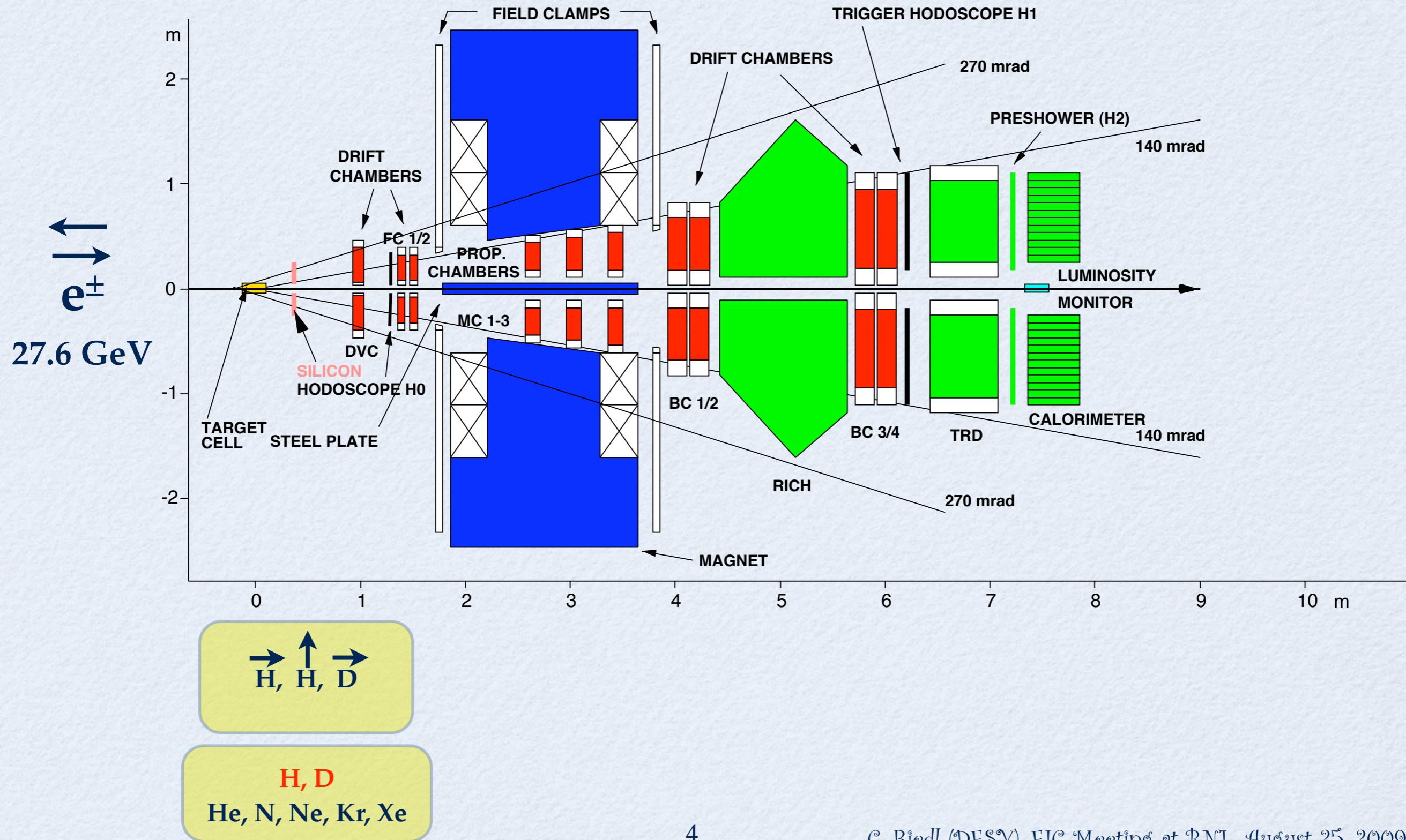
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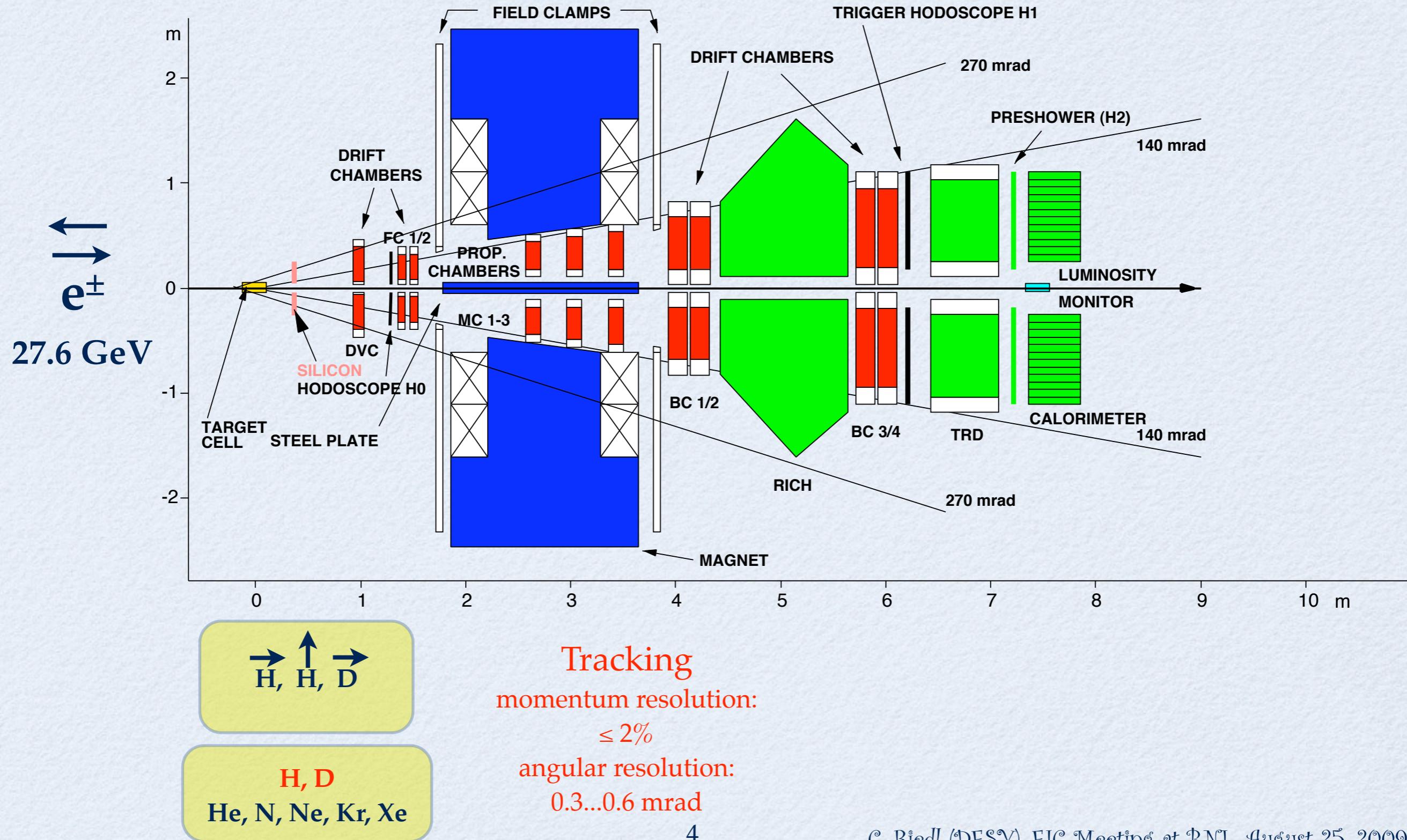
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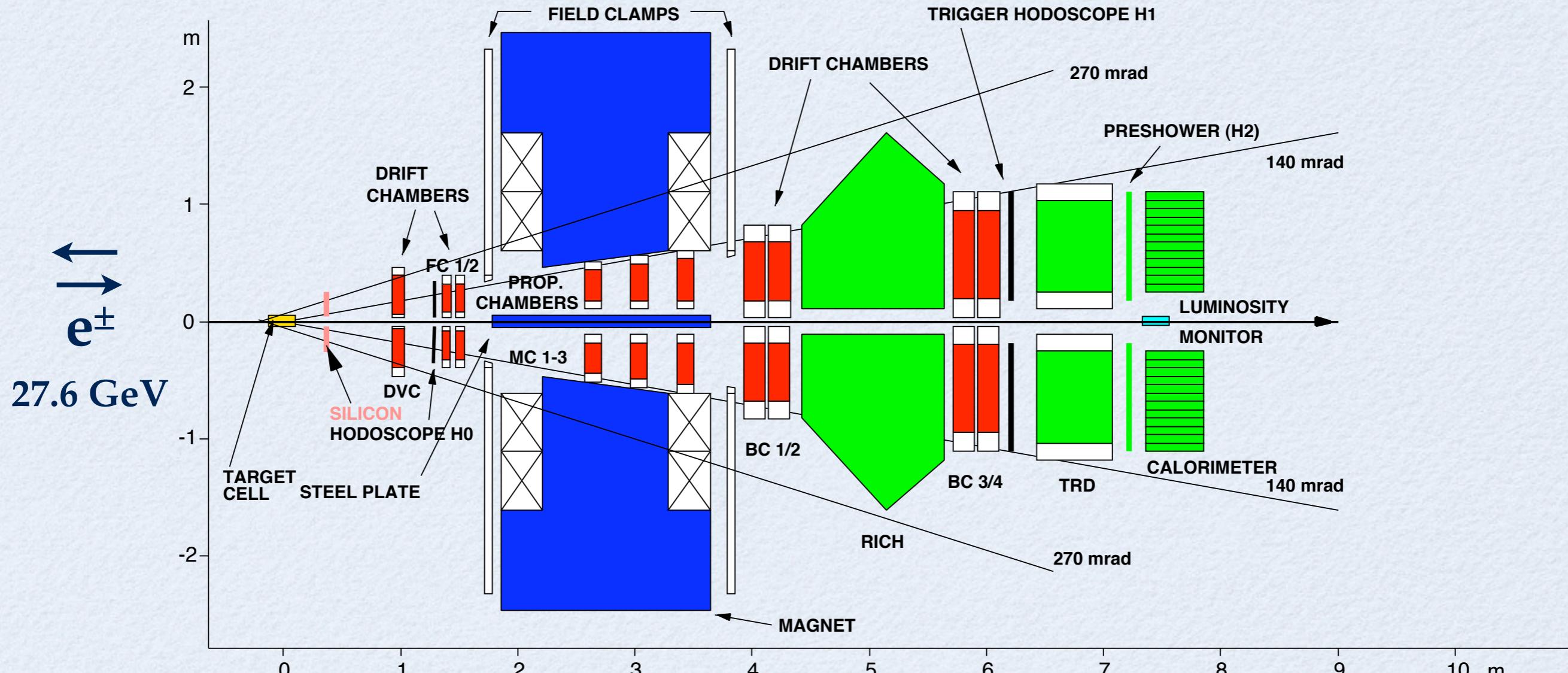
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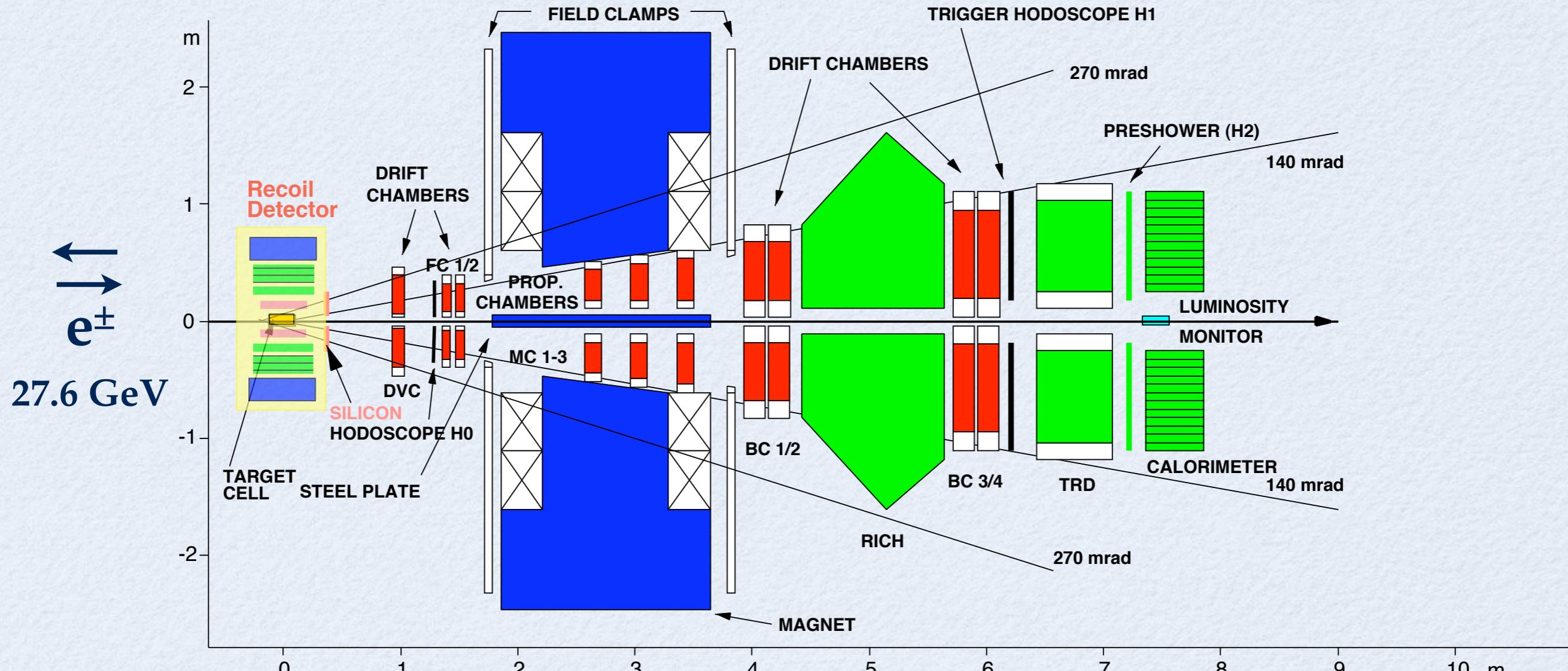
$\vec{H}, \vec{H}, \vec{D}$

H, D
He, N, Ne, Kr, Xe

Tracking
momentum resolution:
 $\leq 2\%$
angular resolution:
0.3...0.6 mrad

Particle IDentification
electron ID: 98-99%
hadron contamination <1%
RICH: 2...15 GeV

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Deep Inelastic Scattering in ep collisions

Inclusive kinematics

Virtual photon virtuality:

$$Q^2 \equiv -q^2 := (k - k')^2$$

$$\stackrel{\text{lab}}{\approx} 4EE' \sin^2(\theta/2)$$

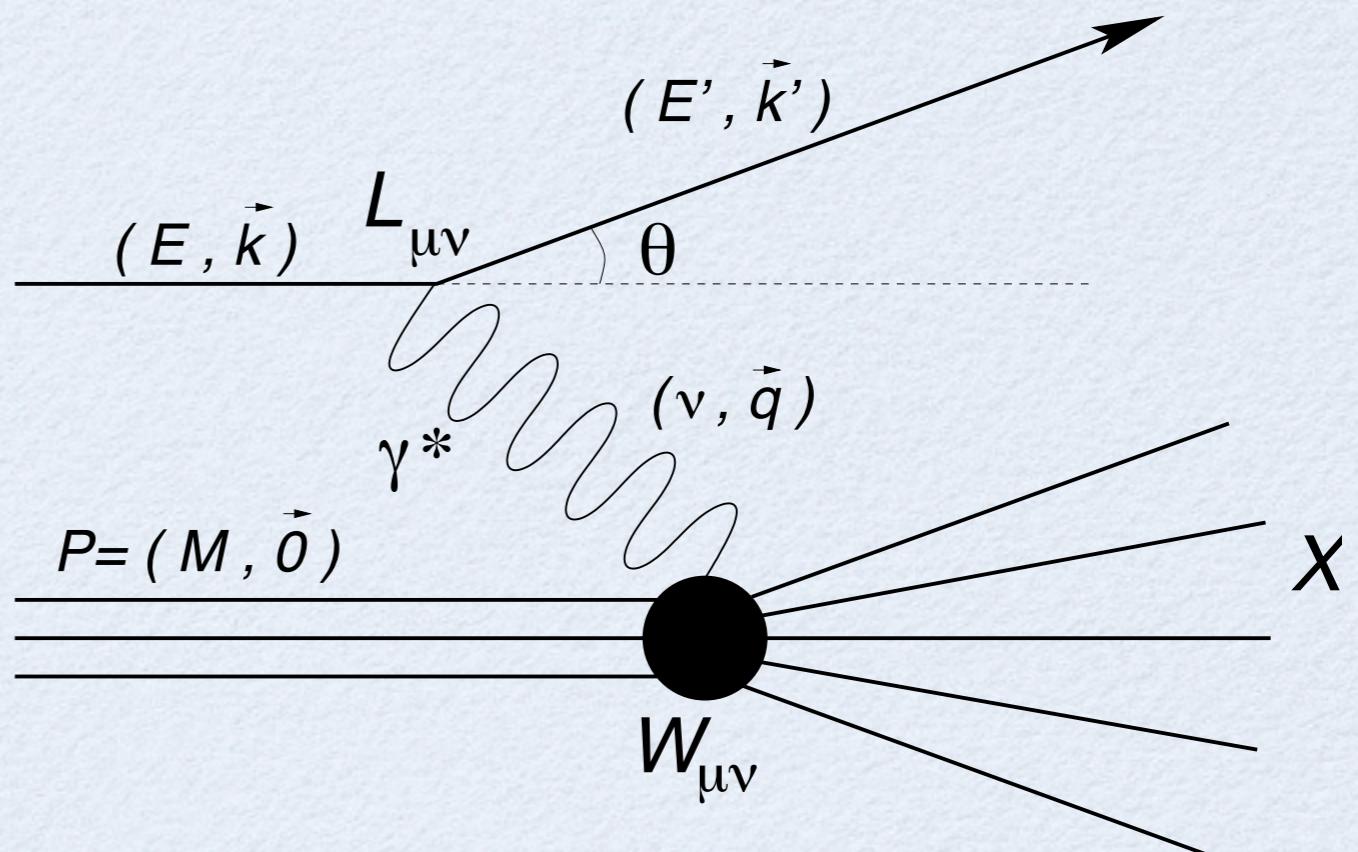
Bjørken scaling variable:

$$x_B := \frac{Q^2}{2Pq} \stackrel{\text{lab}}{=} \frac{Q^2}{2M(E - E')}$$

Invariant mass squared of X:

$$W^2 := (P + q)^2$$

$$\stackrel{\text{lab}}{=} M^2 + 2M(E - E') - Q^2$$



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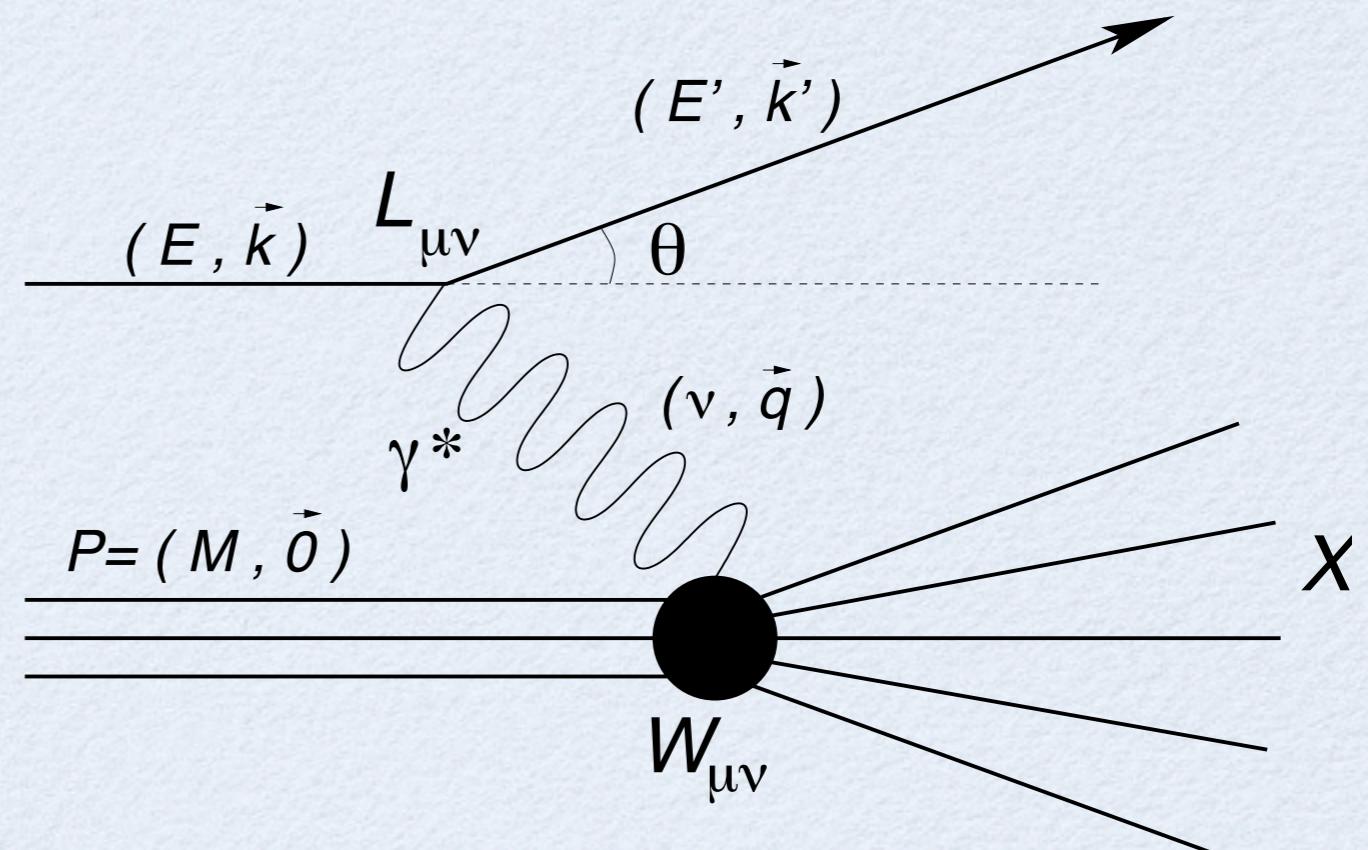
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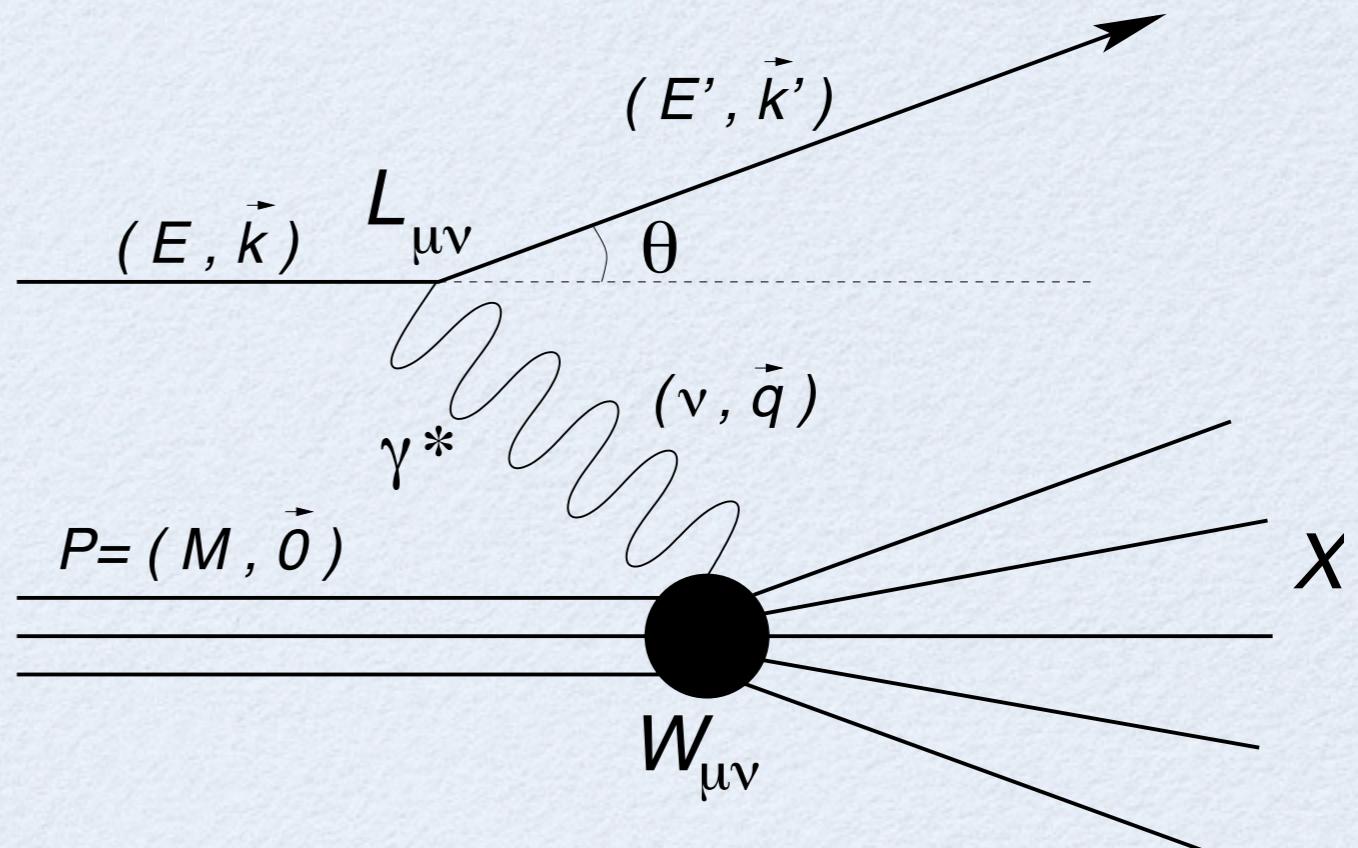
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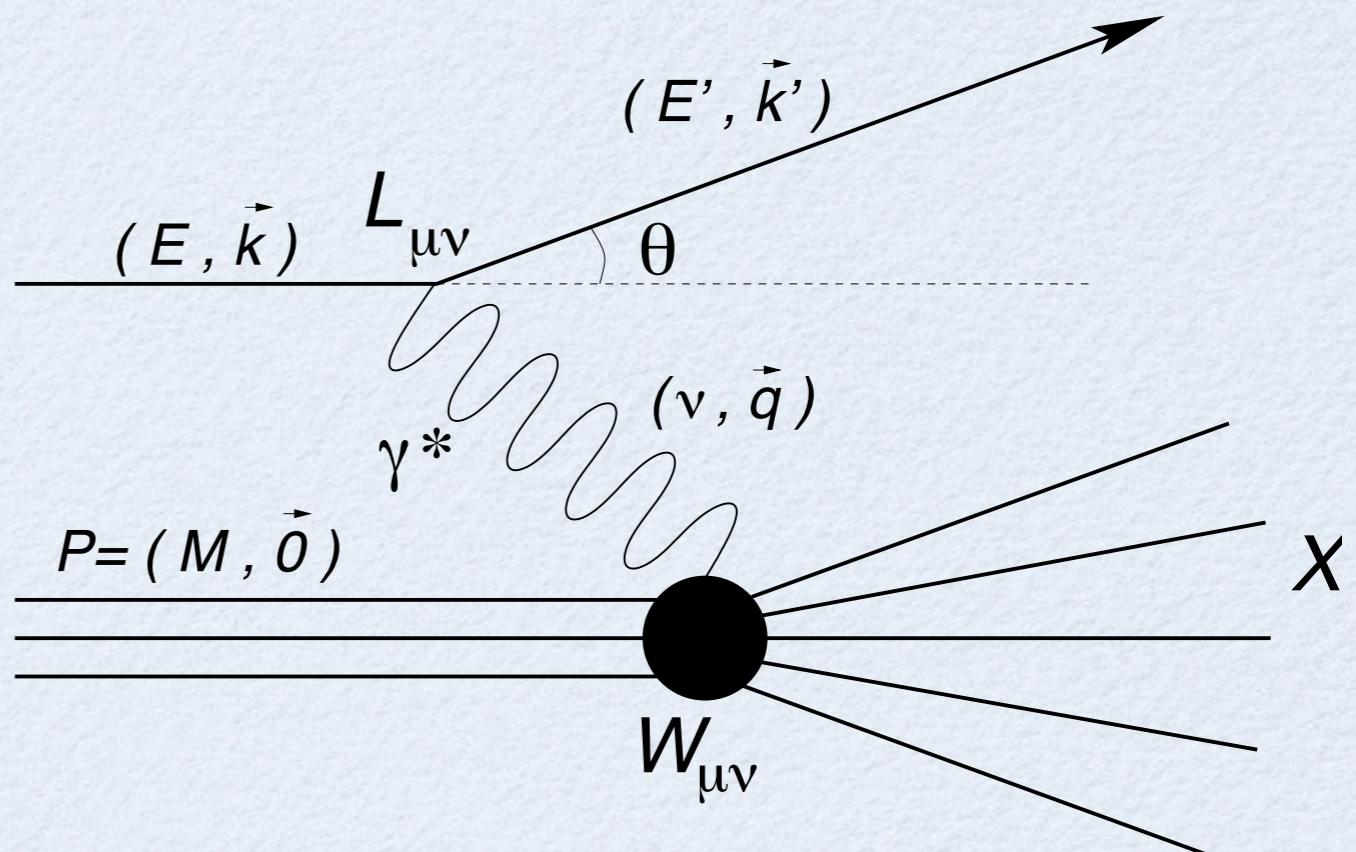
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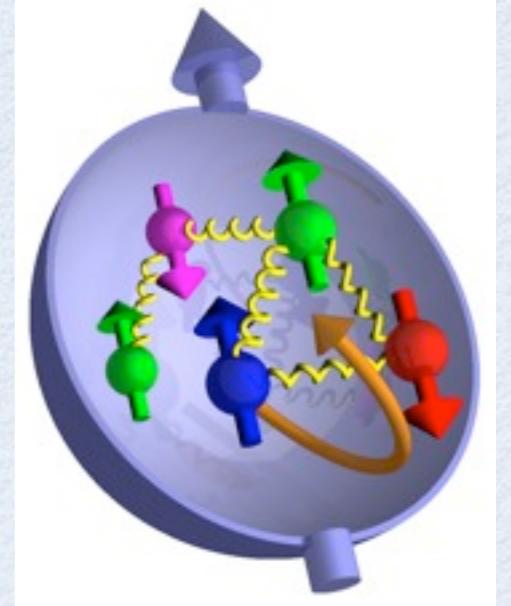


Semi-inclusive kinematics
involve kinematics of produced hadrons

Exclusive kinematics
complete spectrum of X known

The Composition of the Nucleon's Spin

$$\frac{1}{2}\hbar = J_{\text{quarks}} + J_{\text{gluons}}$$



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Hermes Phys. Rev. **D75** (2007) 012007: $\Delta\Sigma = 0.330 \pm 0.011(\text{theo}) \pm 0.025(\text{exp}) \pm 0.028(\text{evol})$

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Ji relation

Ji, PRL **78** (1997) 610

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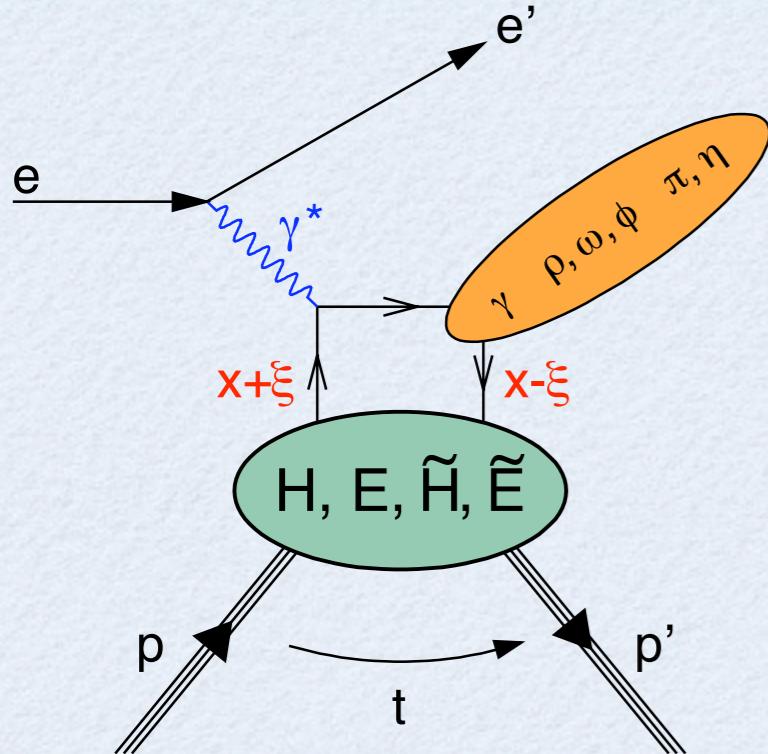
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Generalized Parton Distributions (GPDs)

Generalized Parton Distributions



- * Access through hard exclusive reactions
 - * t : squared momentum transfer to target
 - * x : average longitudinal momentum fraction of quark before/after
 - * ξ : $1/2$ difference
- * GPDs $F^q(x, \xi, t)$ parameterize the non-perturbative nucleon structure
 - contain info on parton-parton correlations

- * 4 GPDs that conserve quark chirality (Spin-1/2 target, leading-twist)

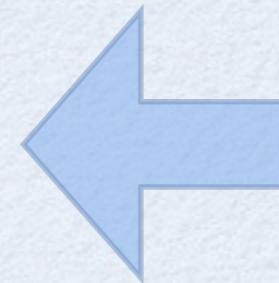
nucleon helicity ↓	quark helicity independent	quark helicity dependent
	photon: $J^P=1^-$ (DVCS)	
conserved	H	H̃
flipped	E	Ẽ
	$J^P=1^-$ mesons	$J^P=0^-$ mesons

GPDs: A unifying picture of nucleon structure

Parton Distribution
Functions:
longitudinal momentum



GPDs
 $F^q(x, \xi, t)$



Form Factors:
transverse position

$$H^q(x, 0, 0) = q(x)$$

forward limit $\xi=0, t=0$

$$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t)$$

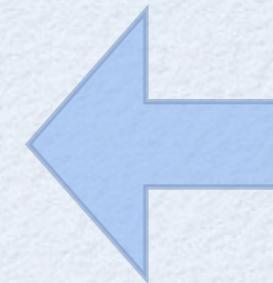
moments of GPDs

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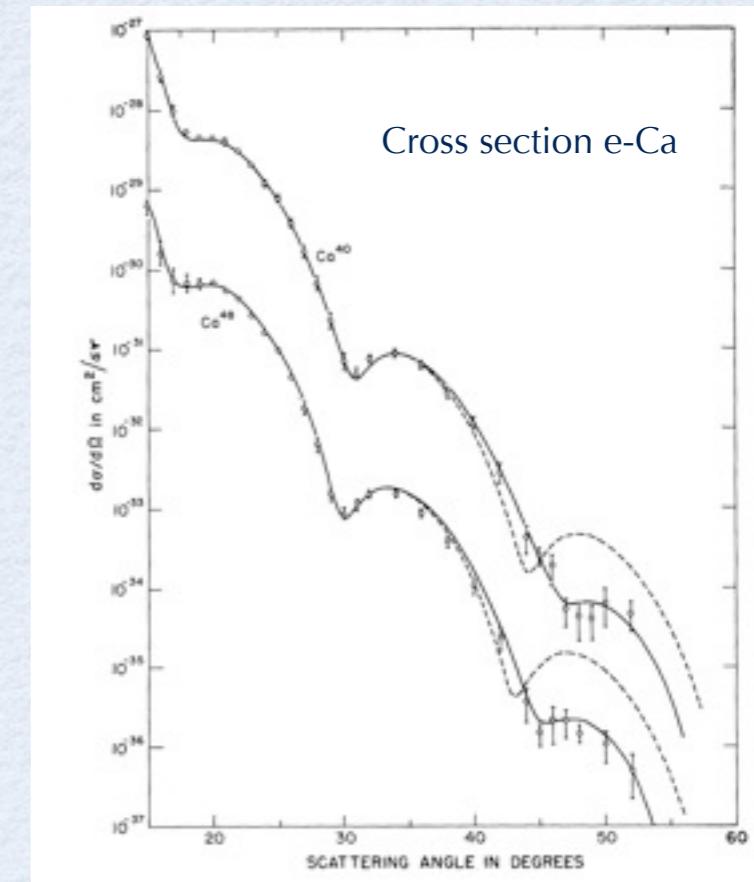
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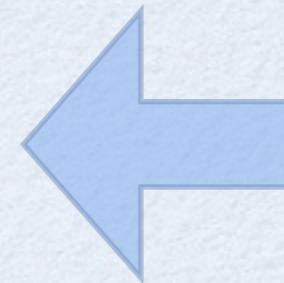
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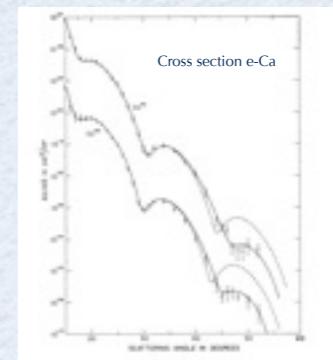
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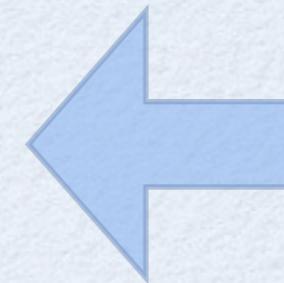
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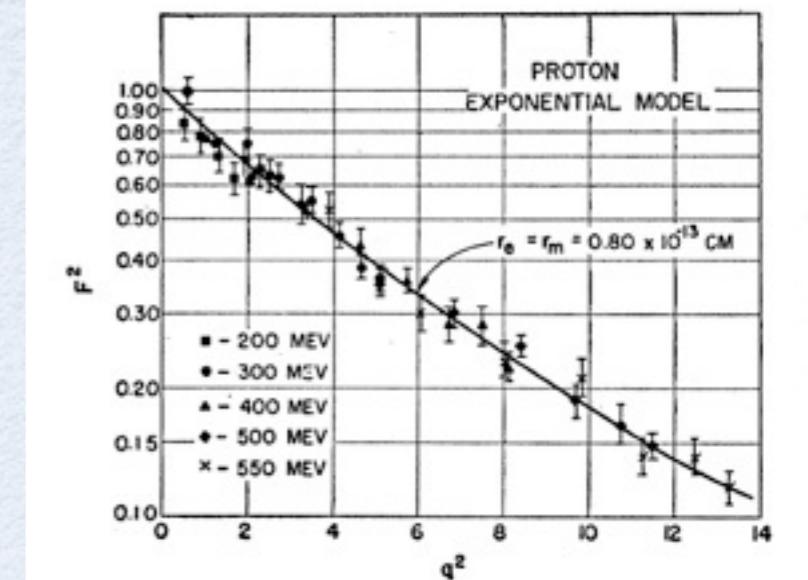
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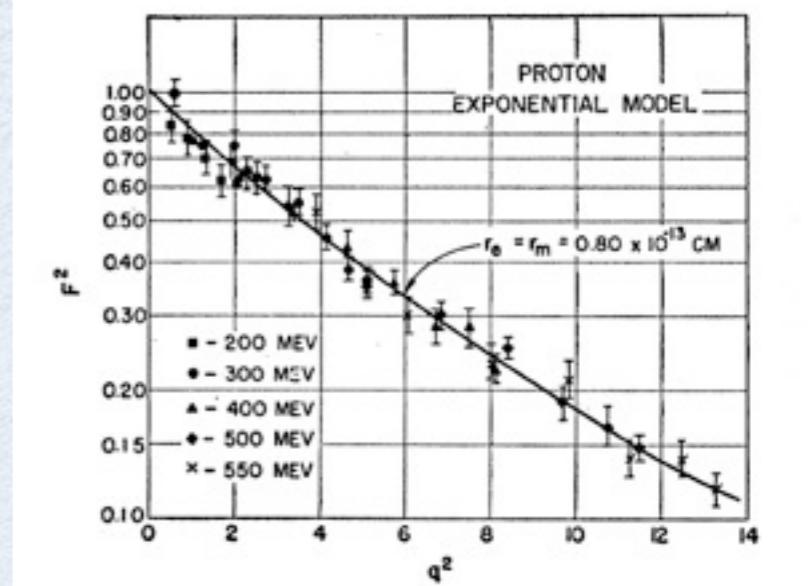
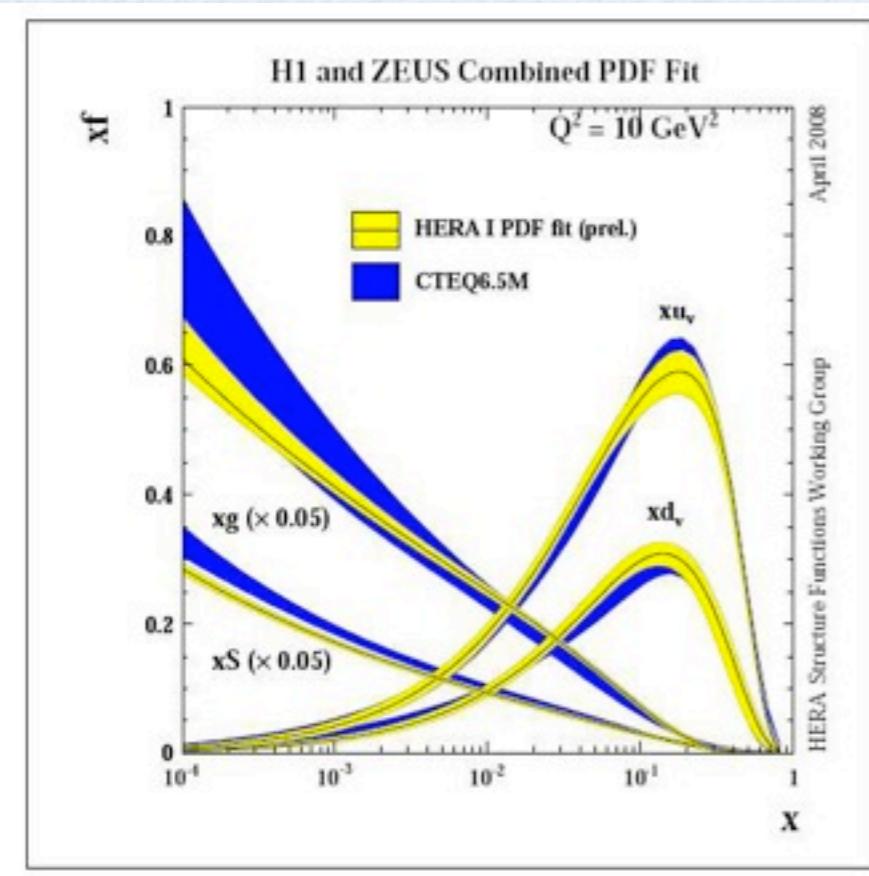
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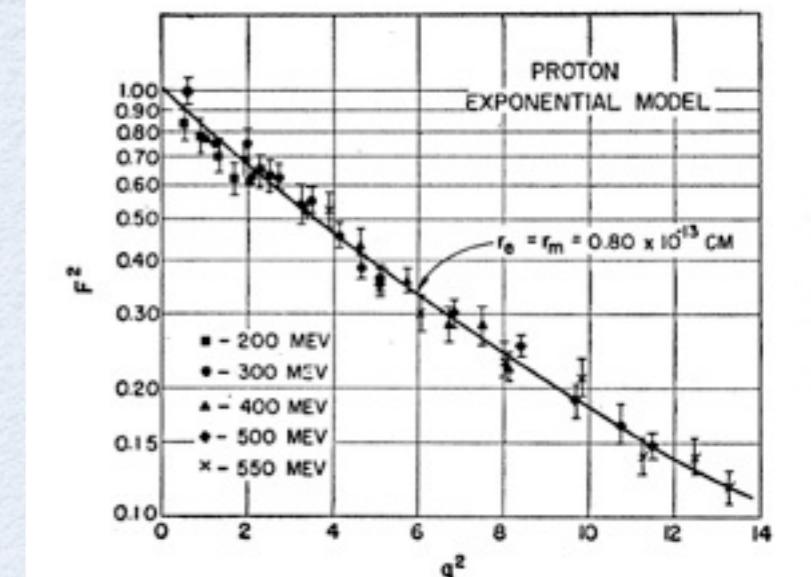
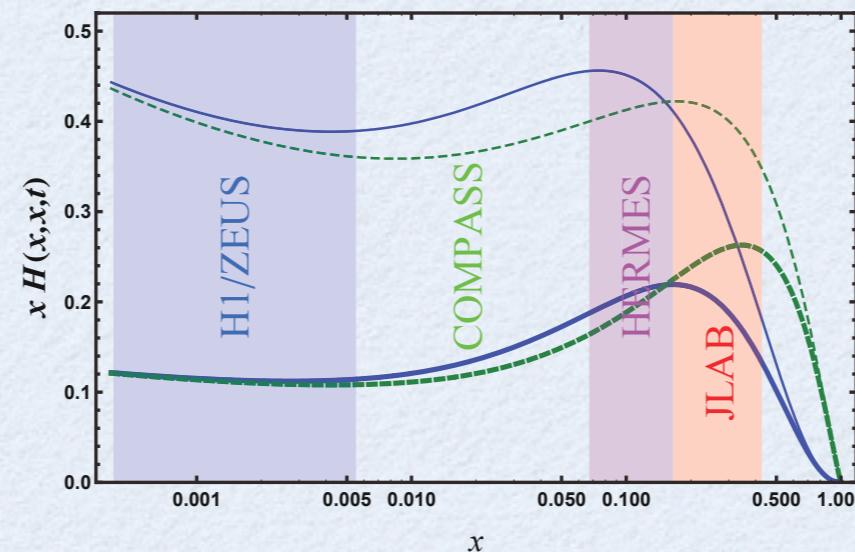
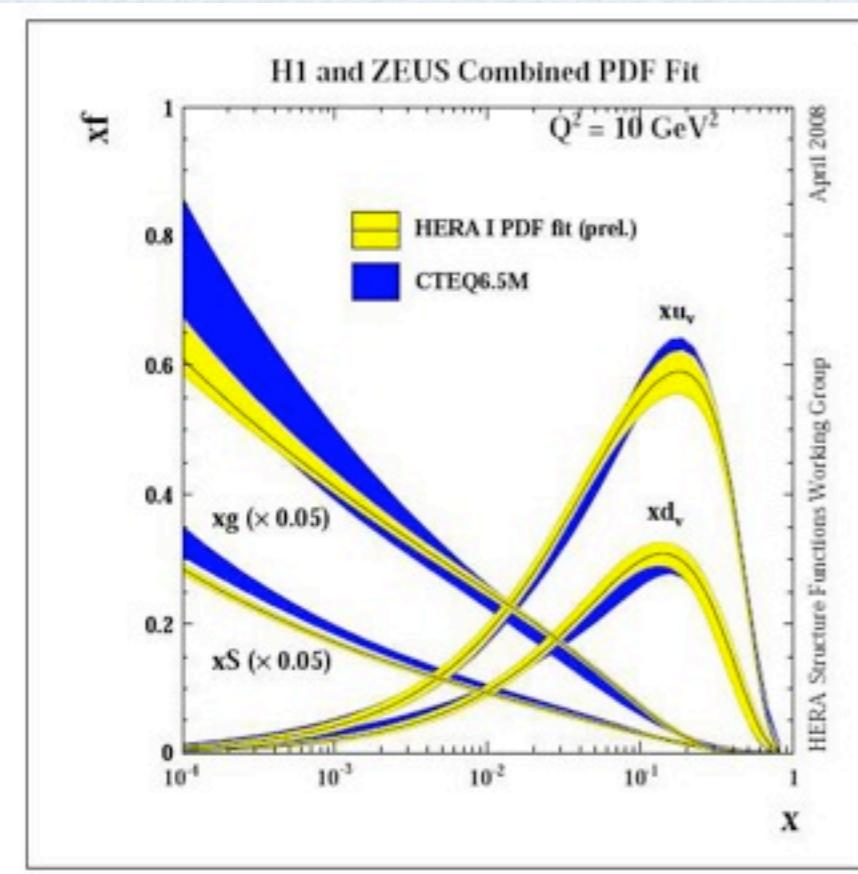
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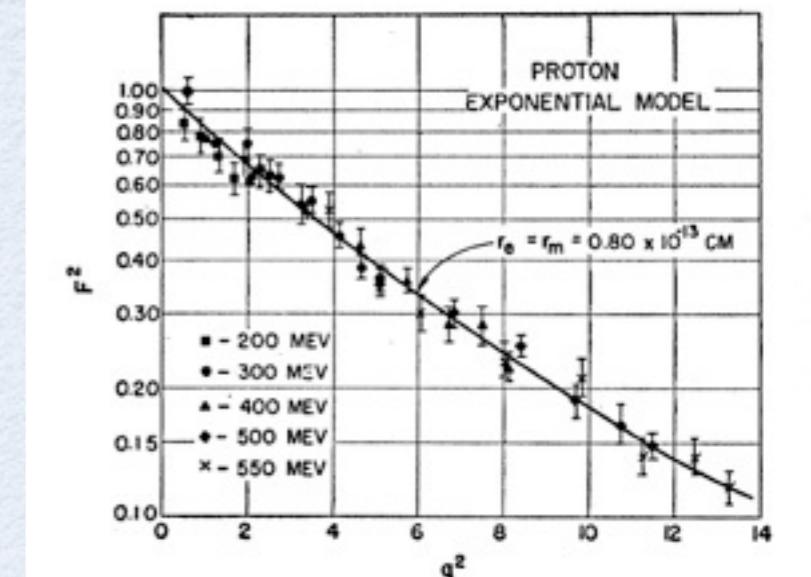
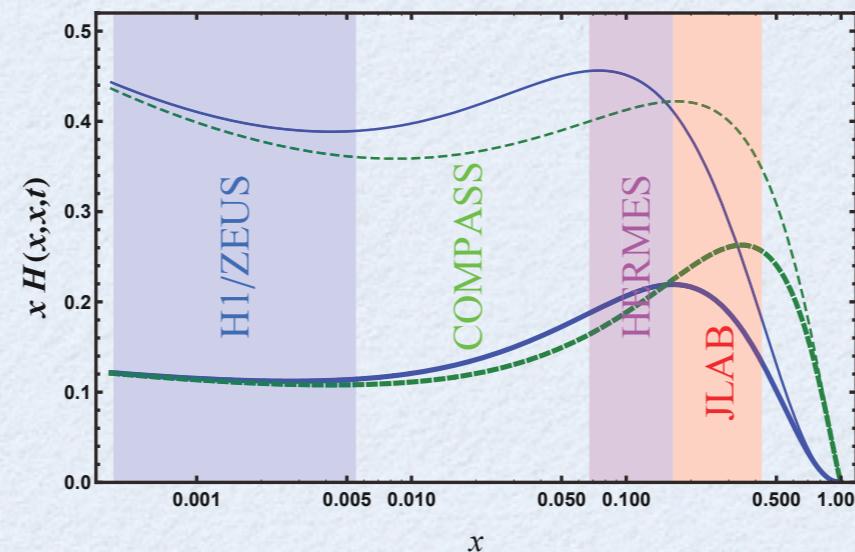
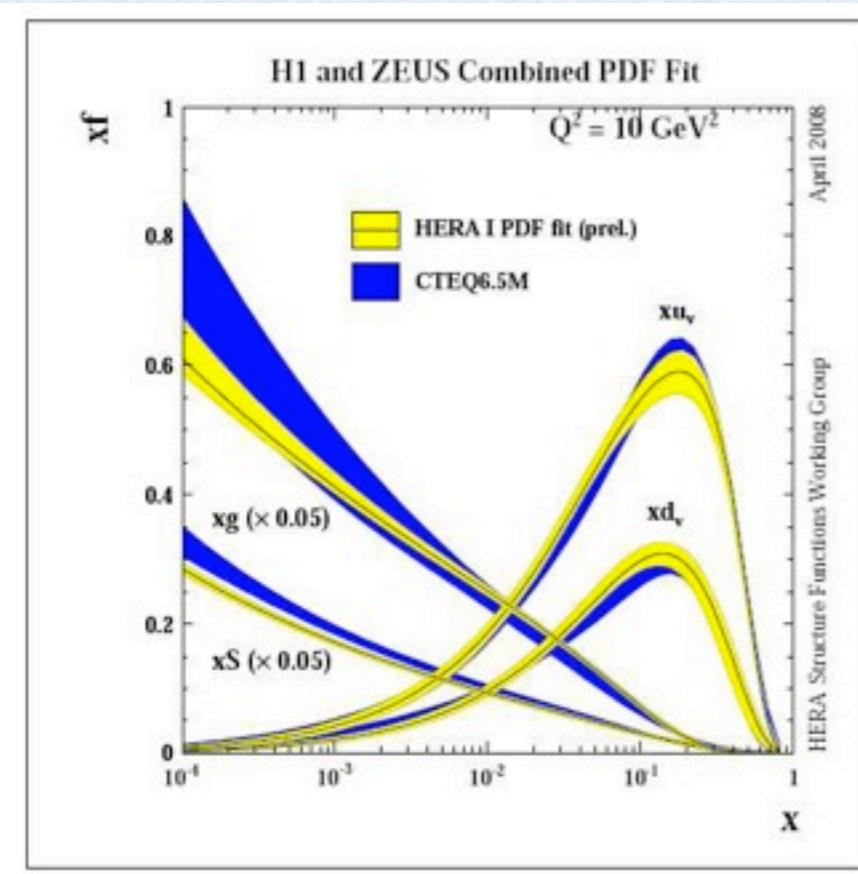
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“Nucleon Tomography”

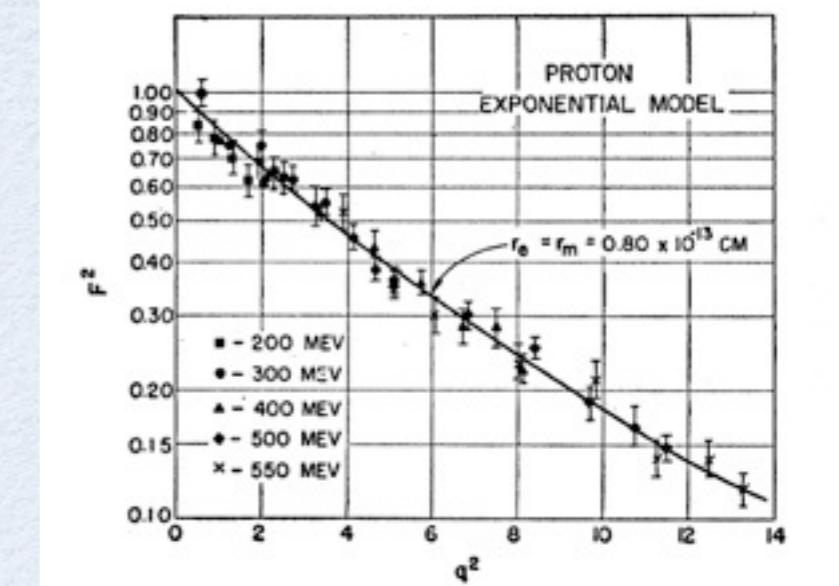
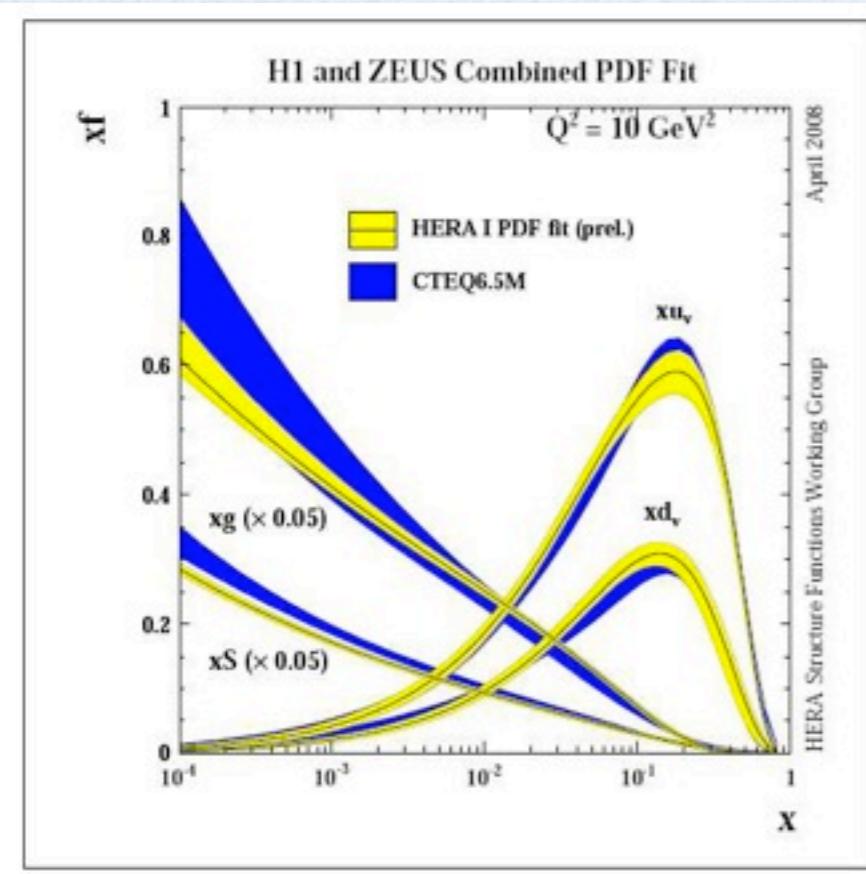
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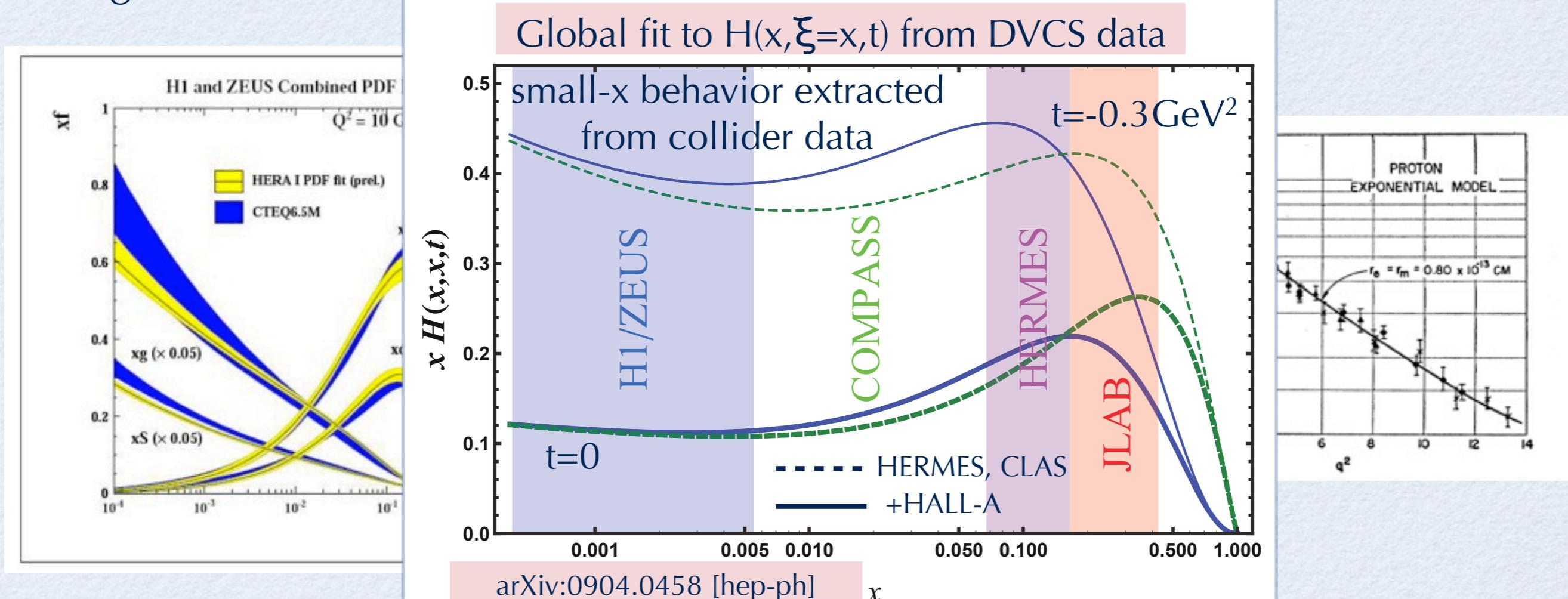
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Deeply Virtual Compton Scattering (DVCS)

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Reminder: inclusive DIS

$$\sigma_{\text{DIS}} \sim \sum_x \left| \text{Diagram} \right|^2$$

$\sim \text{Im} \left(\text{Diagram} \right)$

optical theorem

forward Compton scattering amplitude

The diagram illustrates the connection between Deeply Virtual Compton Scattering (DVCS) and Deep Inelastic Scattering (DIS). It shows that the cross-section for DIS is proportional to the sum of the squares of the forward Compton scattering amplitudes for different nucleon constituents (x). The forward Compton scattering amplitude is related to the imaginary part of the scattering amplitude, as indicated by the arrow and the label 'optical theorem'.

Deeply Virtual Compton Scattering (DVCS)

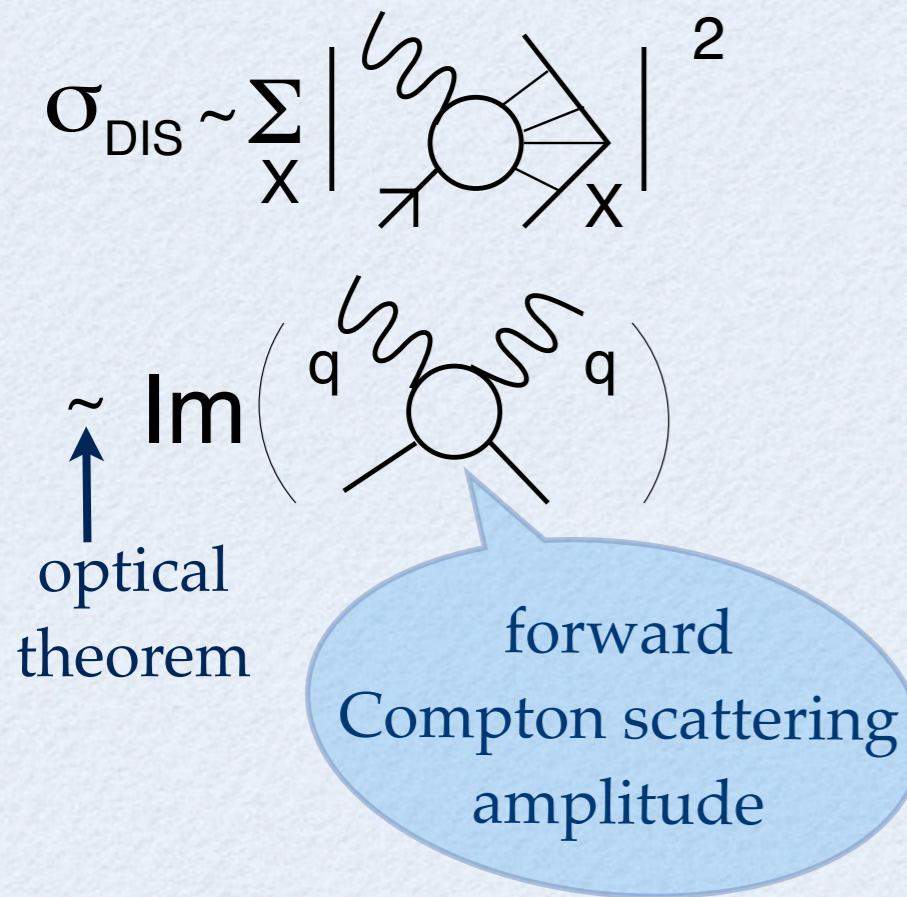
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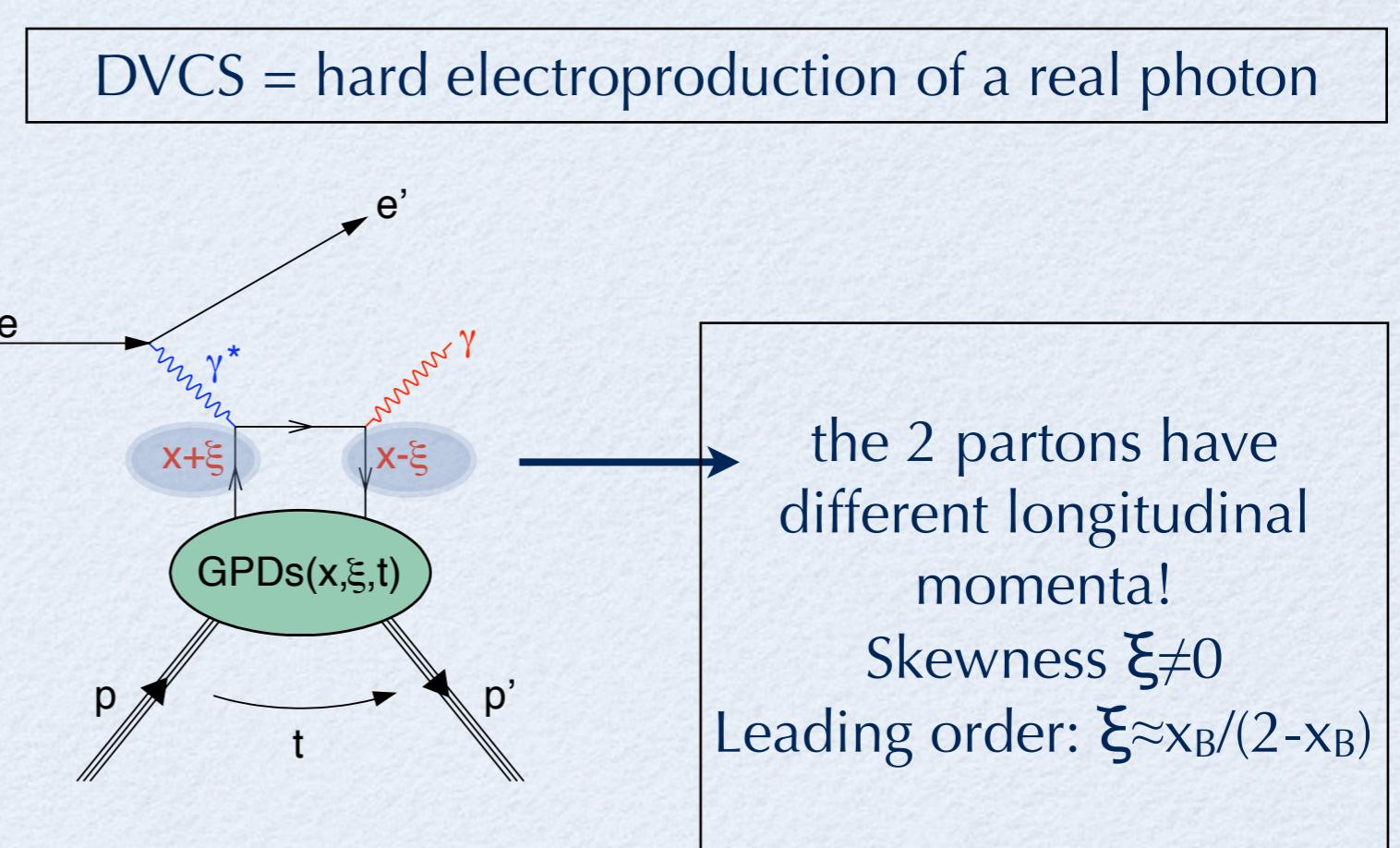
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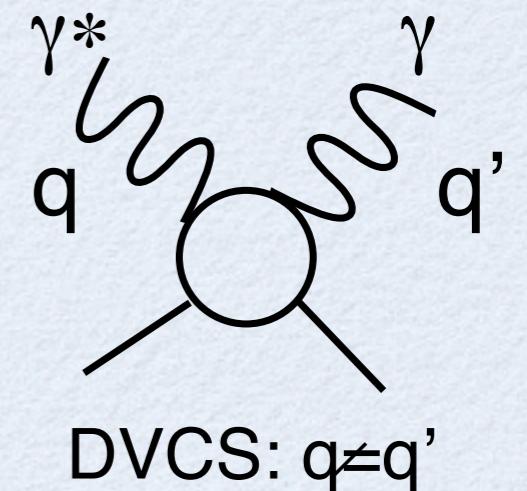
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DVCS: $q \neq q'$

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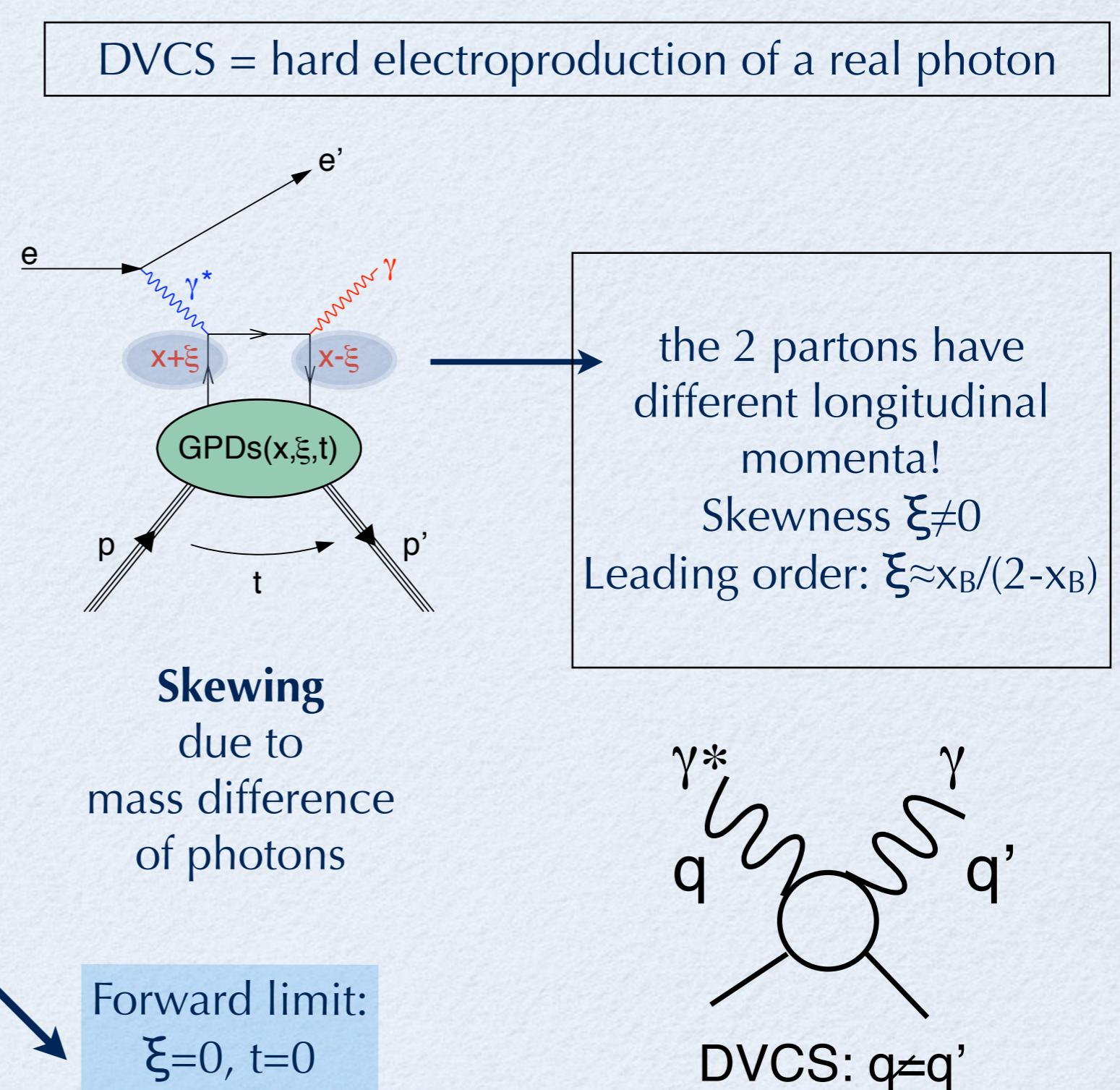
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The $\gamma^* N \rightarrow \gamma N$ Cross Section

$$\sigma_{\gamma^*\gamma N} = \left| \text{DVCS} + \text{Bethe-Heitler (BH)} \right|^2$$

Bjørken limit:
large Q^2 (small distances)
large energy of γ^* (small times)
small t , fixed x_B

$$= |\tau_{\text{DVCS}}|^2 + |\tau_{\text{BH}}|^2 + \tau_{\text{DVCS}} \tau_{\text{BH}}^* + \tau_{\text{DVCS}}^* \tau_{\text{BH}}$$

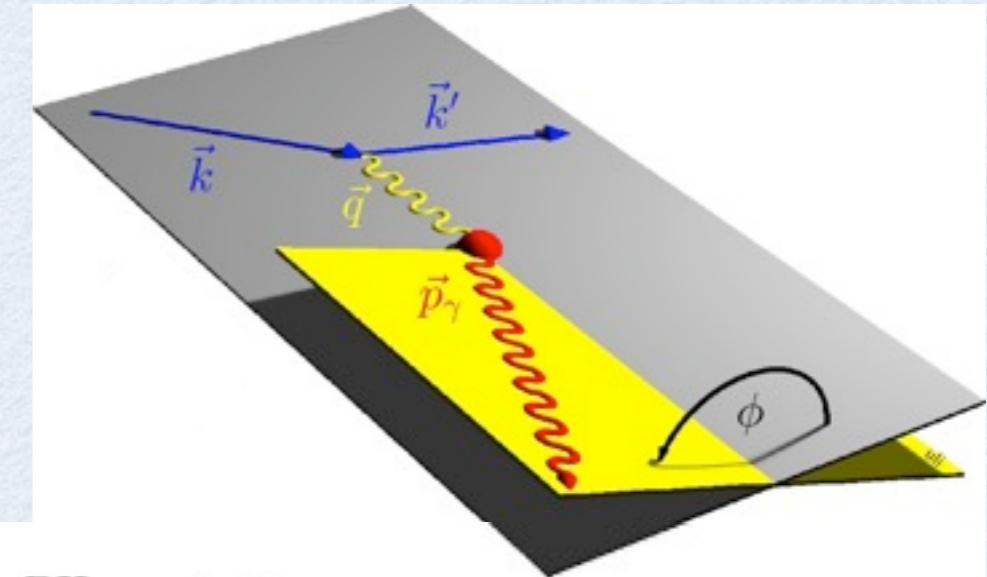
DVCS-BH interference term \mathcal{I}

Contribution at colliders.
Fixed target:
 $|\tau_{\text{DVCS}}|^2 \ll |\tau_{\text{BH}}|^2$

exactly calculable in QED
given the nucleon elastic form factors F_1 and F_2

Azimuthal Dependences in $\gamma^* N \rightarrow \gamma N$

- Unpolarized target
- Lepton beam with charge C_B and polarization P_B



Fourier expansion in azimuthal angle ϕ

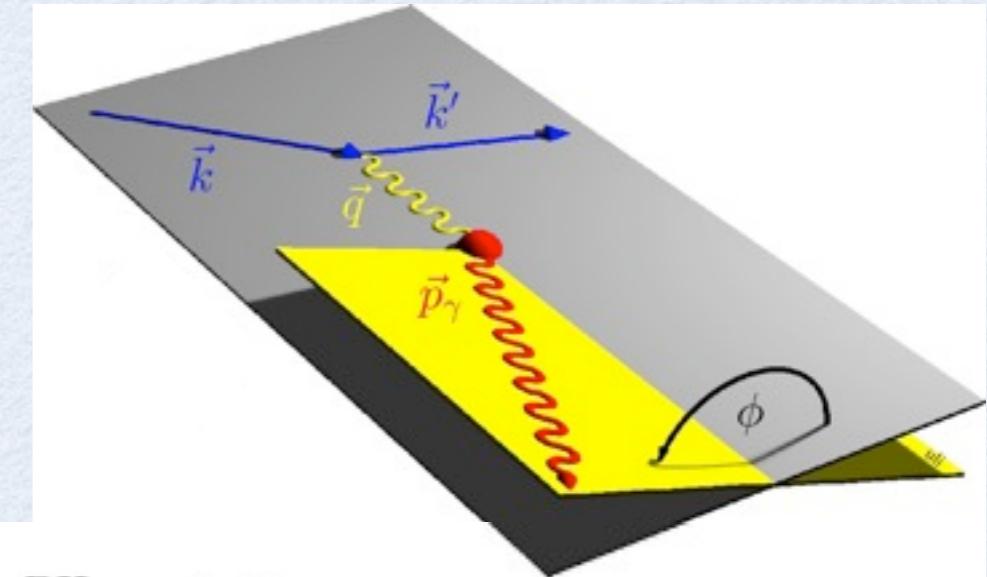
$$|T_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi)$$

$$|T_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left[\sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + P_B \sum_{n=1}^1 s_n^{\text{DVCS}} \sin(n\phi) \right]$$

$$\mathcal{I} = \frac{C_B K_I}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + P_B \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right]$$

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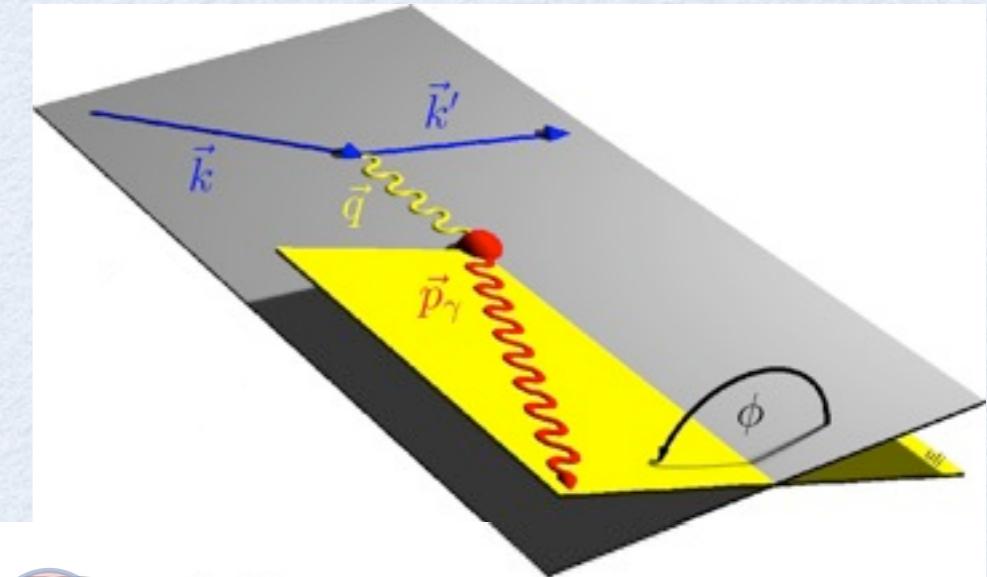
$$|T_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left[\sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + P_B \sum_{n=1}^1 s_n^{\text{DVCS}} \sin(n\phi) \right]$$

$$\mathcal{I} = \frac{C_B K_T}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + P_B \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right]$$

Bethe-Heitler propagators $\mathcal{P}(\phi)$

Azimuthal Dependences in $\gamma^* N \rightarrow \gamma N$

- Unpolarized target
- Lepton beam with charge C_B and polarization P_B



Fourier expansion in azimuthal angle ϕ

$$|T_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi)$$

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$$\mathcal{I} = \frac{C_B K_I}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=0}^3 c_n^I \cos(n\phi) + P_B \sum_{n=1}^2 s_n^I \sin(n\phi) \right]$$

Bethe-Heitler propagators $\mathcal{P}(\phi)$

Wanted:
Fourier coefficients
 s_n and c_n
of BH, DVCS, and I terms

Measured Azimuthal Asymmetries in DVCS

Born cross-section:

$$\sigma(\phi; P_B, C_B) = \sigma_{UU}(\phi) \cdot [1 + P_B \mathcal{A}_{LU}^{\text{DVCS}}(\phi) + C_B P_B \mathcal{A}_{LU}^T(\phi) + C_B \mathcal{A}_C(\phi)]$$

Beam helicity asymmetries

Old approach at HERMES
and CLAS: single charge BSA

$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^\rightarrow - d\sigma^\leftarrow}{d\sigma^\rightarrow + d\sigma^\leftarrow}$$

no separate access

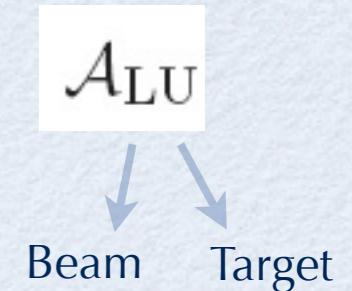
to s_1^T and s_1^{DVCS}

BSA:

projects out imaginary
part of τ_{DVCS}

Beam charge asymmetry

BCA:
projects out real part
of τ_{DVCS}



$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$

Measured Azimuthal Asymmetries in DVCS

Born cross-section:

$$\sigma(\phi; P_B, C_B) = \sigma_{UU}(\phi) \cdot [1 + P_B \mathcal{A}_{LU}^{\text{DVCS}}(\phi) + C_B P_B \mathcal{A}_{LU}^T(\phi) + C_B \mathcal{A}_C(\phi)]$$

Beam helicity asymmetries

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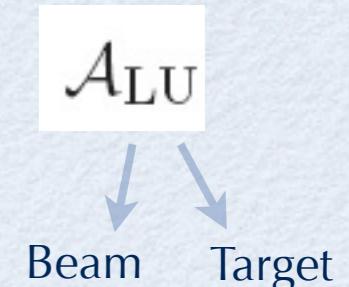
$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

no separate access
to s_1^I and s_1^{DVCS}

BSA:
projects out imaginary
part of τ_{DVCS}

Beam charge asymmetry

BCA:
projects out real part
of τ_{DVCS}



$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$

New approach at HERMES:
 s_1^I and s_1^{DVCS} can be disentangled

Charge difference BSA:

$$\mathcal{A}_{LU}^I(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

$$\mathcal{A}_{LU}^{\text{DVCS}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

Charge average BSA:

Relation: asymmetries \leftrightarrow Fourier coefficients

Beam helicity asymmetries:

$$\mathcal{A}_{\text{LU}}^{\mathcal{T}}(\phi) = \frac{1}{\mathcal{D}(\phi)} \cdot \frac{x_B}{Q^2} [s_1^{\mathcal{T}} \sin(\phi) + s_2^{\mathcal{T}} \sin(2\phi)]$$

$$\mathcal{A}_{\text{LU}}^{\text{DVCS}}(\phi) = \frac{1}{\mathcal{D}(\phi)} \cdot \frac{x_B^2 t \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)}{Q^2} s_1^{\text{DVCS}} \sin(\phi)$$

Beam charge asymmetry:

$$\mathcal{A}_C(\phi) = -\frac{1}{\mathcal{D}(\phi)} \cdot \frac{x_B}{y} [c_0^{\mathcal{T}} + c_1^{\mathcal{T}} \cos(\phi) + c_2^{\mathcal{T}} \cos(2\phi) + c_3^{\mathcal{T}} \cos(3\phi)]$$

Relation: asymmetries \leftrightarrow Fourier coefficients

Beam helicity asymmetries:

$$\mathcal{A}_{\text{LU}}^{\mathcal{T}}(\phi) = \frac{1}{\mathcal{D}(\phi)} \cdot \frac{x_B}{Q^2} [s_1^{\mathcal{T}} \sin(\phi) + s_2^{\mathcal{T}} \sin(2\phi)]$$

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Additional ϕ dependence
in denominator through
BH propagators

$$\mathcal{D}(\phi) = \frac{\sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi)}{(1+\epsilon^2)^2} + \frac{x_B^2 t \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)}{Q^2} \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi)$$

From Azimuthal Asymmetries to GPDs

- * To obtain Fourier coefficients = asymmetry amplitudes:
 - Combine data with different beam charges and helicities and **fit all amplitudes simultaneously**

- * Compton Form Factors (CFFs) $\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q^\mp(\xi, x) F^q(x, \xi, t)$
 - * Define linear combination of CFFs: $\mathcal{C}_{\text{unp}}^{\mathcal{I}} = F_1 \mathcal{H} + \xi(F_1 + F_2) \tilde{H} - \frac{t}{4M^2} F_2 \mathcal{E}$
 - * $F_1(t), F_2(t)$: Dirac, Pauli nucleonic form factors

- * Leading twist level (twist-2):

$$c_1^{\mathcal{I}} \propto \frac{\sqrt{-t}}{Q} \Re [\mathcal{C}_{\text{unp}}^{\mathcal{I}}] \propto -\frac{Q}{\sqrt{-t}} c_0^{\mathcal{I}}$$

constant term

BCA

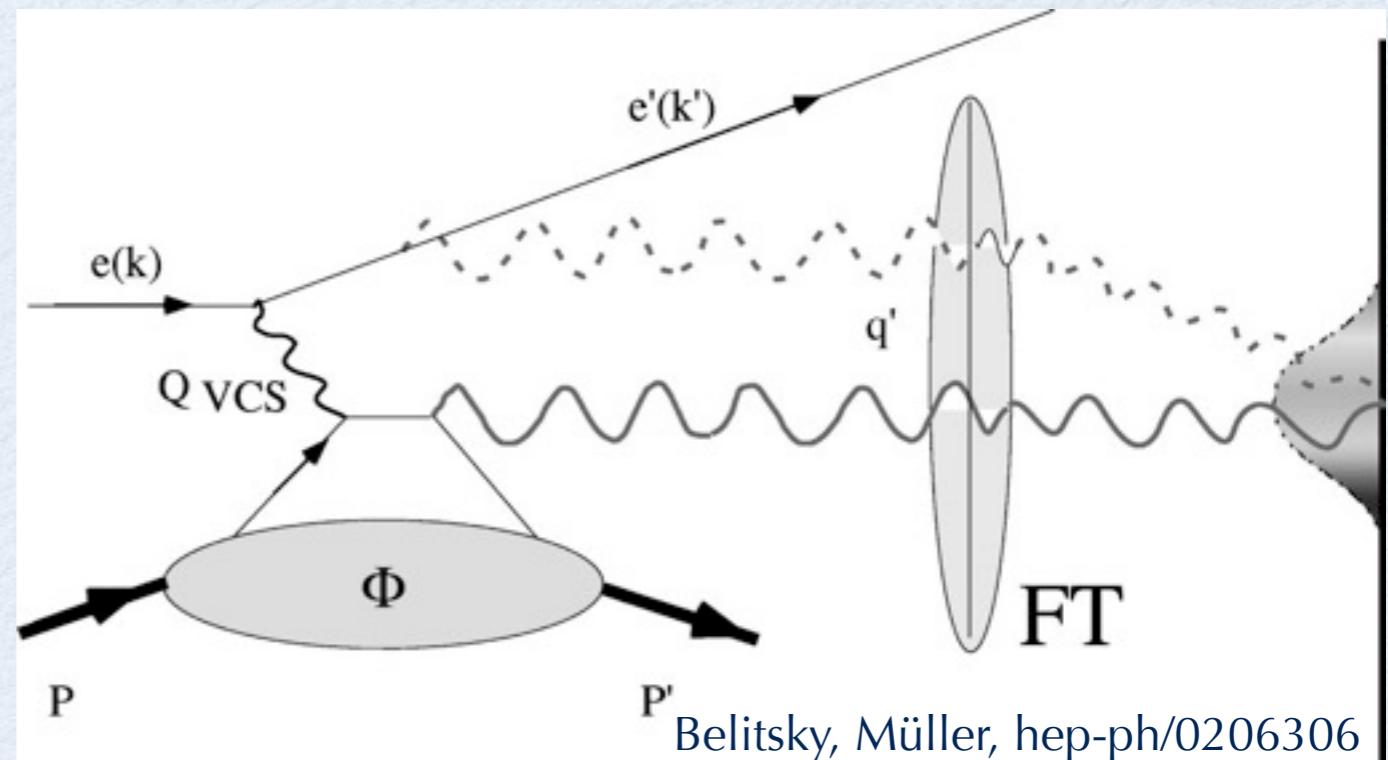
twist-2 GPD

$$s_1^{\mathcal{I}} \propto \frac{\sqrt{-t}}{Q} \Im [\mathcal{C}_{\text{unp}}^{\mathcal{I}}]$$

BSA

Holographic Principle / Femtophotography

- Wanted: 3-dim spatial picture
 - $(FT)^{-1}$ of diffraction pattern, given amplitude $\tau = Ae^{i\varphi}$
 - Need both magnitude A & phase φ
 - Usually $|\tau|^2$ is measured, phase is lost (e.g. PDFs)
-
- Holography technique:
 - Known BH process as reference amplitude that magnifies DVCS effect
 - Measure phase of DVCS through its interference with BH

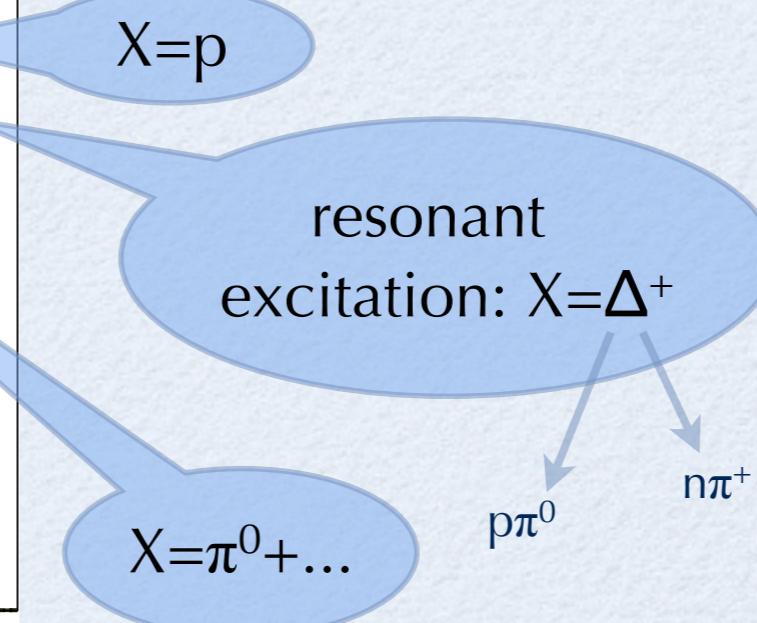
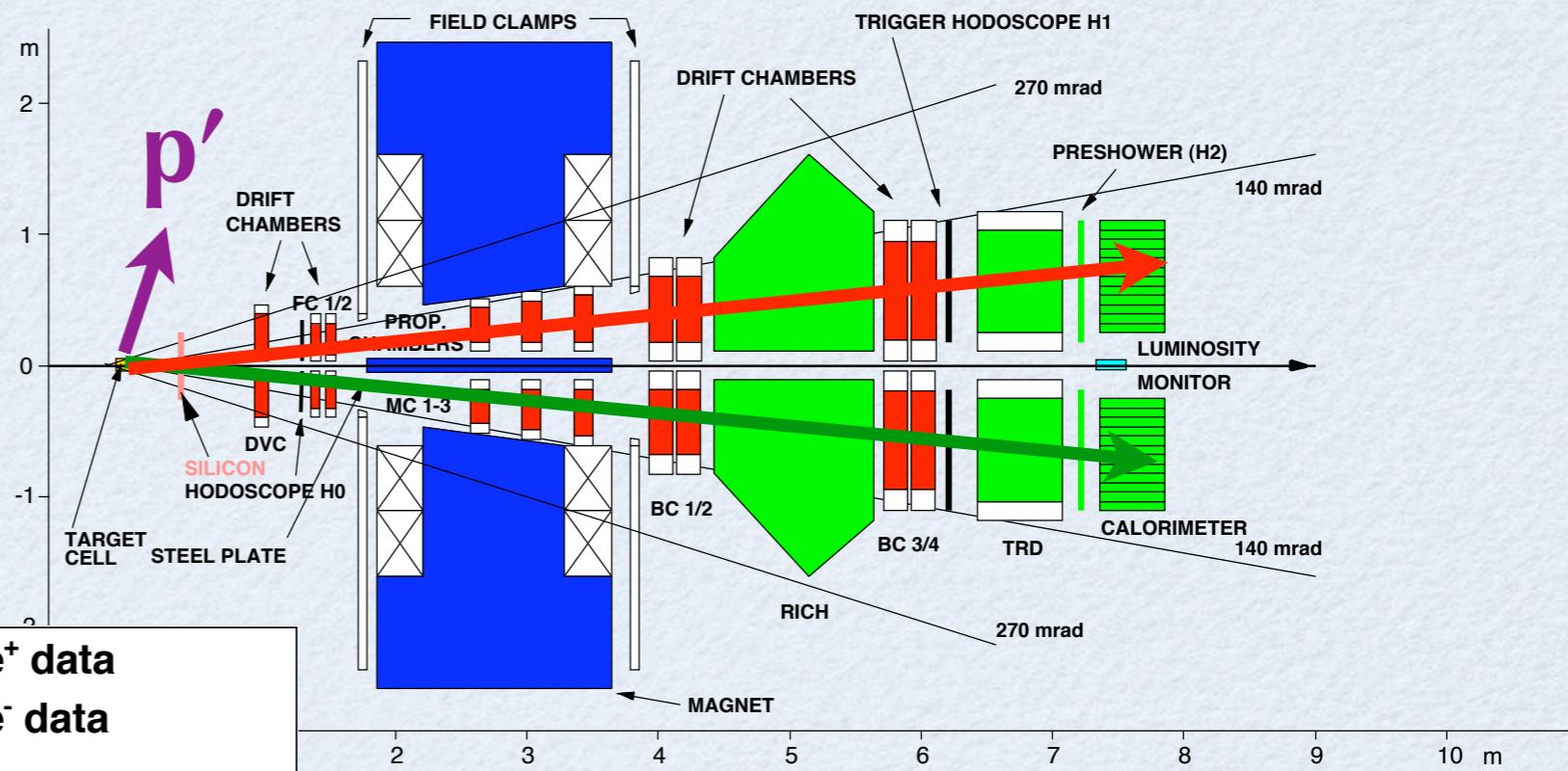
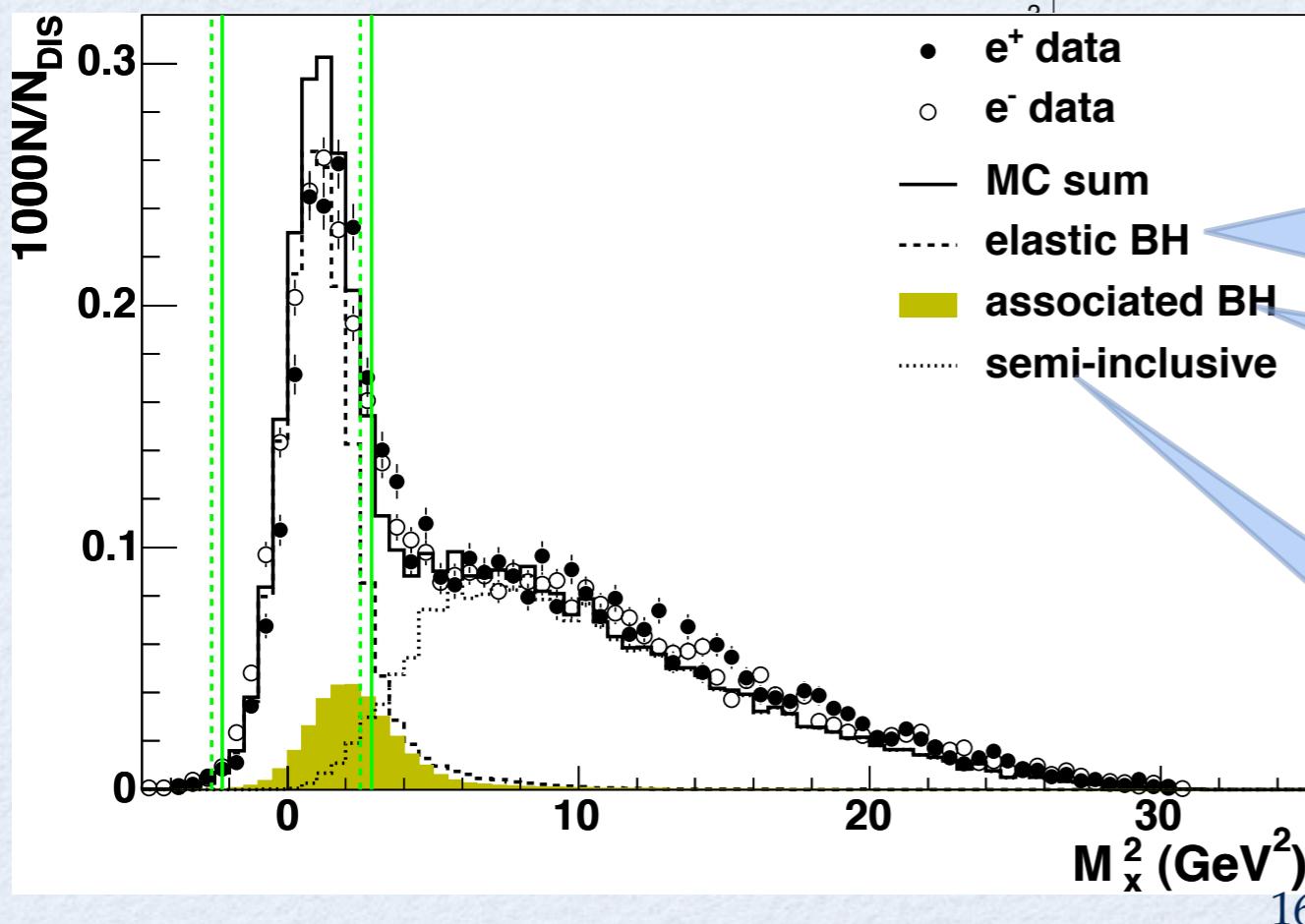


Belitsky, Müller, hep-ph/0206306

DVCS at HERMES 1996-2005 (w/o Recoil)

Detected particles:
electron and photon

Missing mass technique for
 $ep \rightarrow eX\gamma$
 $M_x^2 = (p + q - p_\gamma)^2$



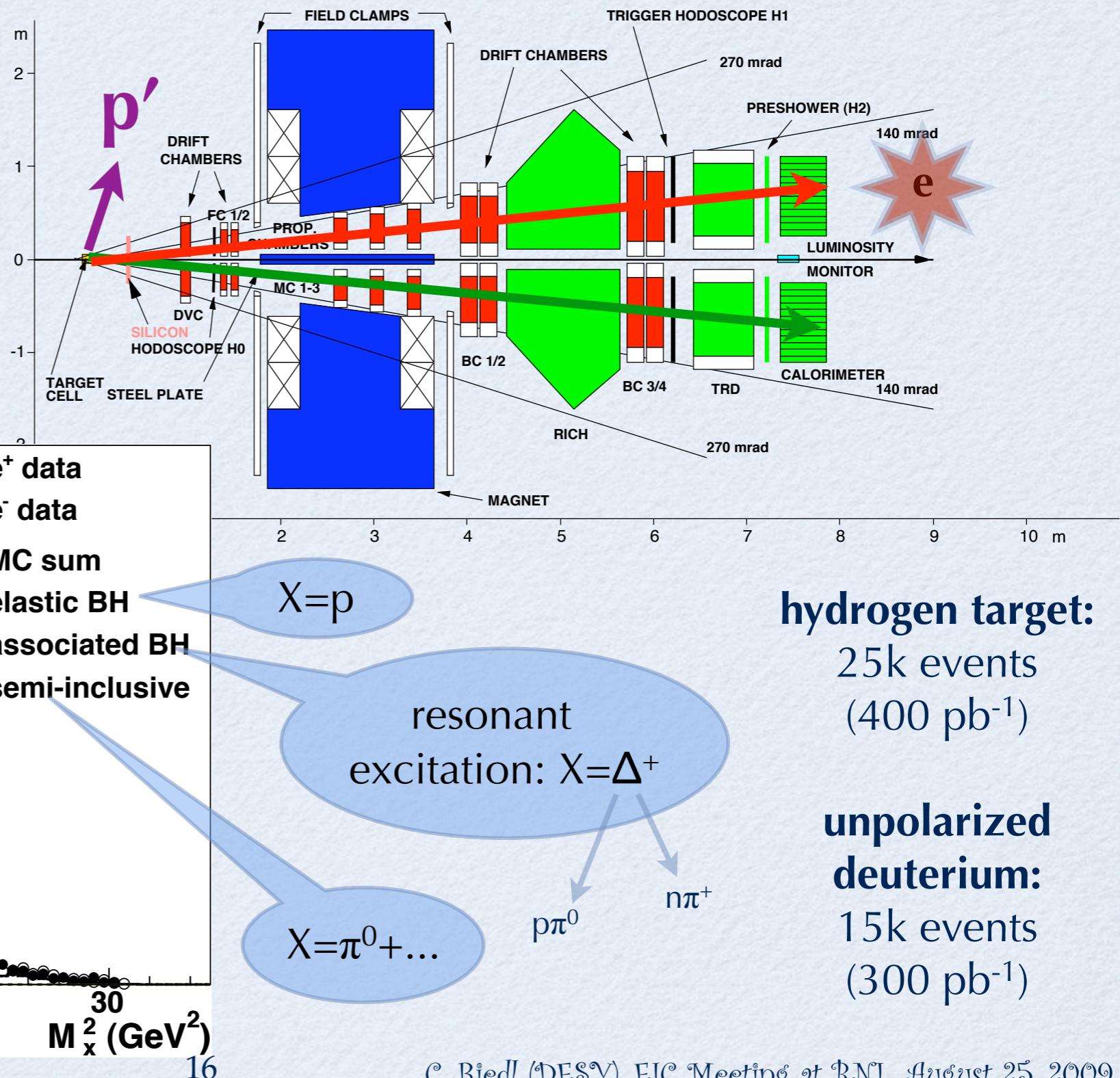
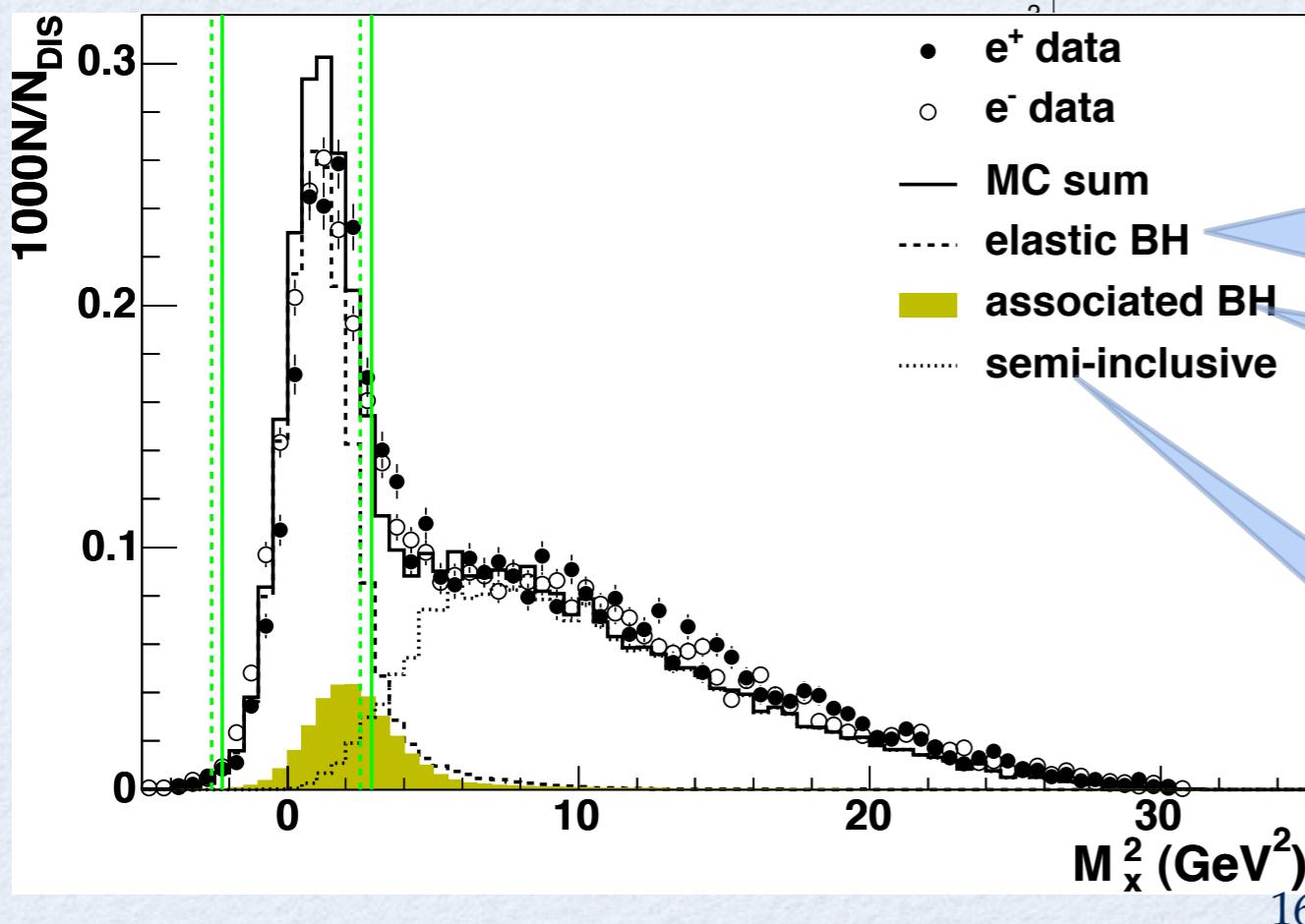
hydrogen target:
25k events
(400 pb^{-1})

unpolarized deuterium:
15k events
(300 pb^{-1})

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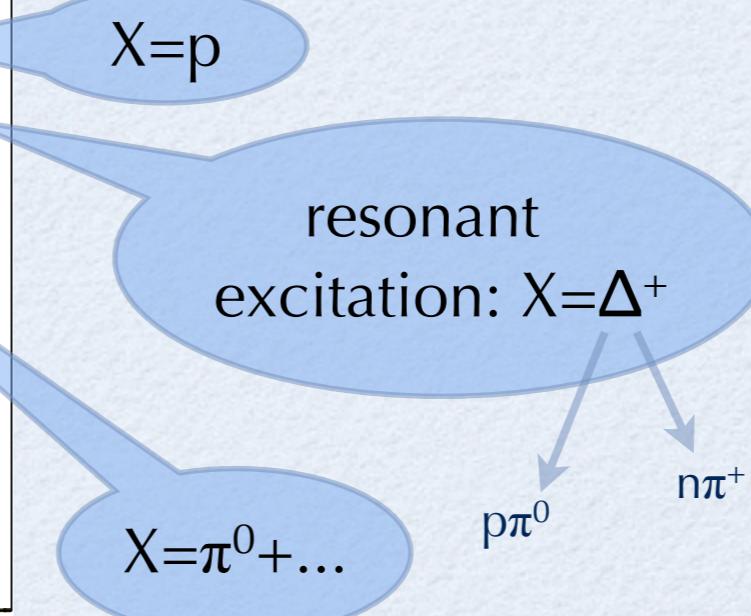
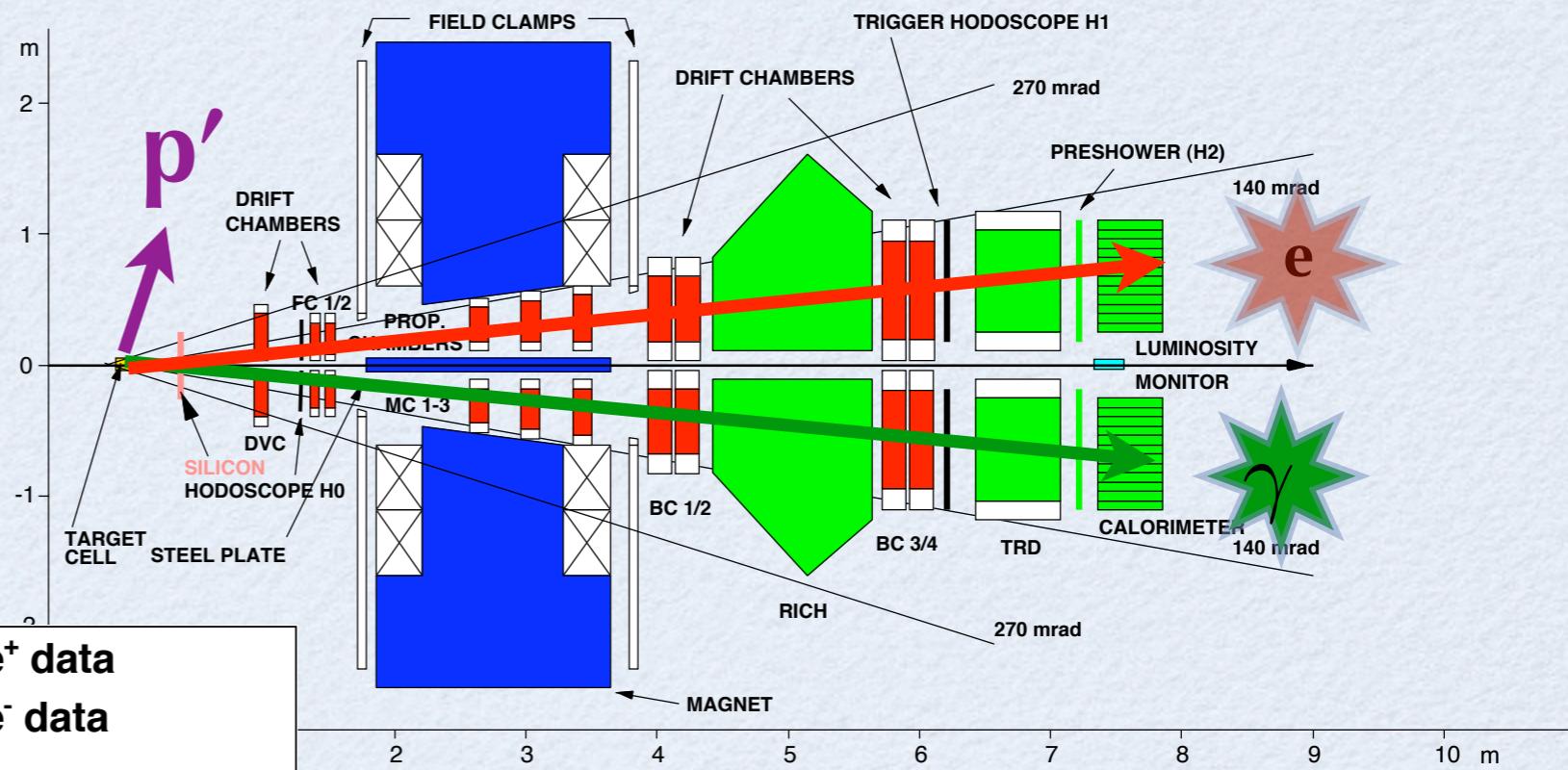
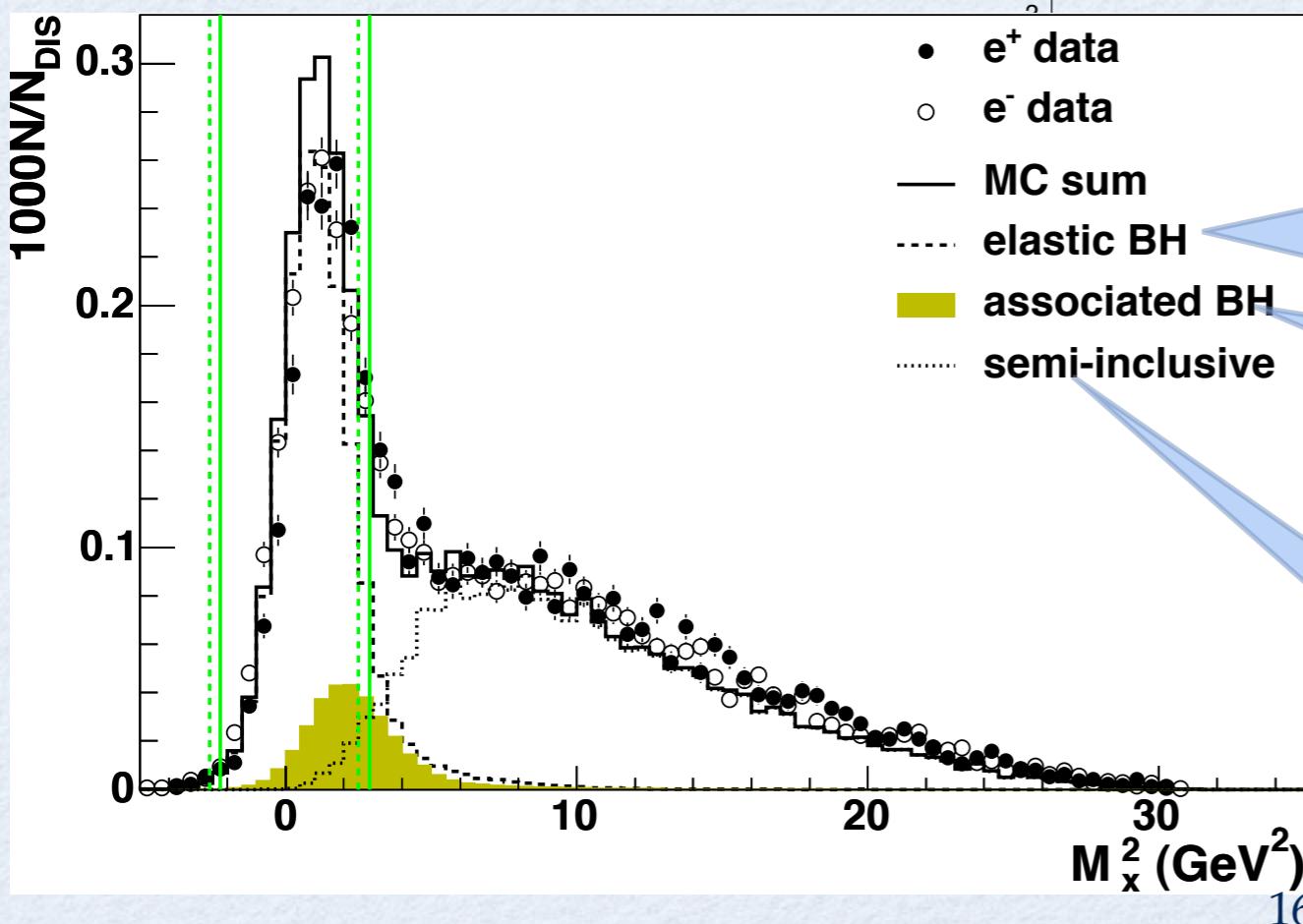
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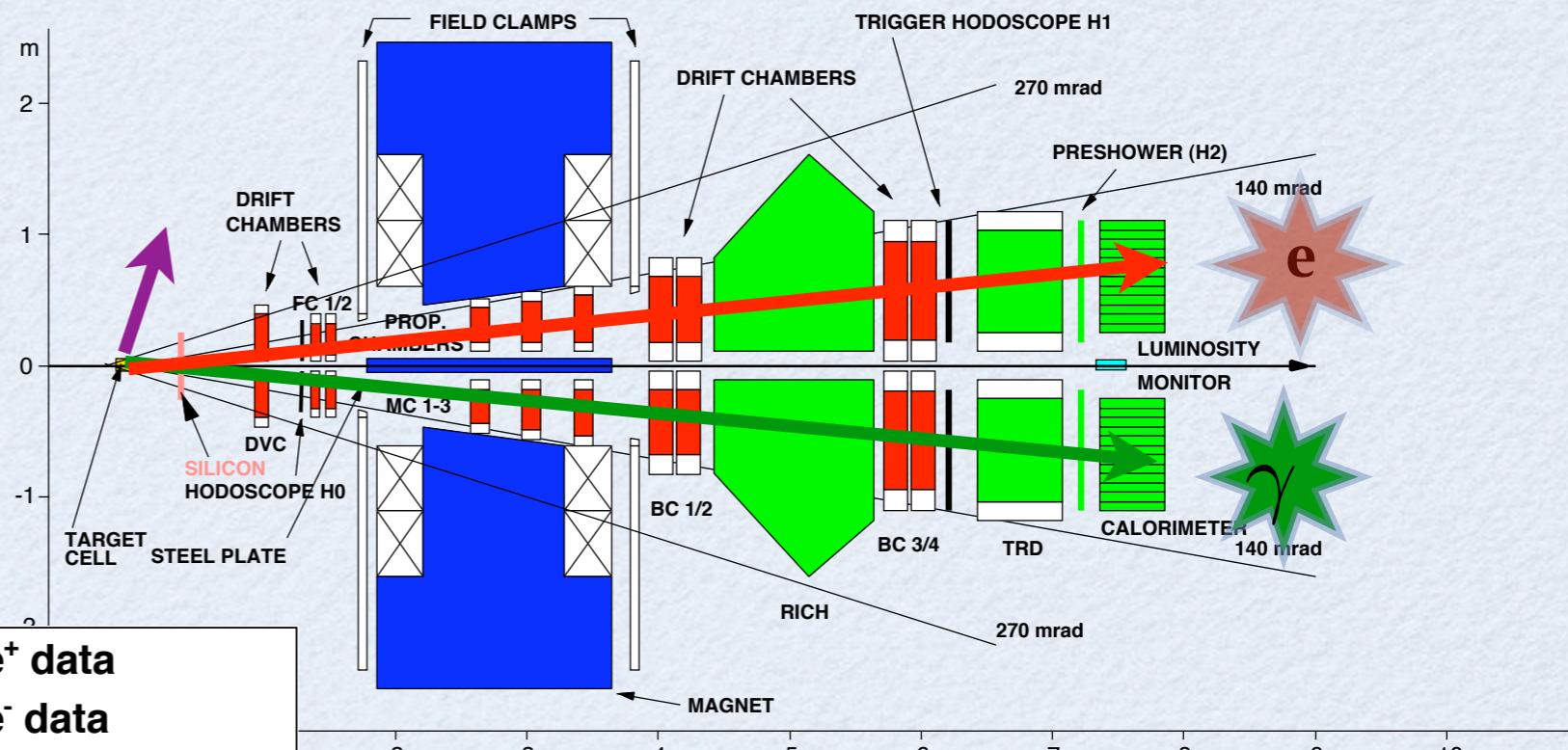
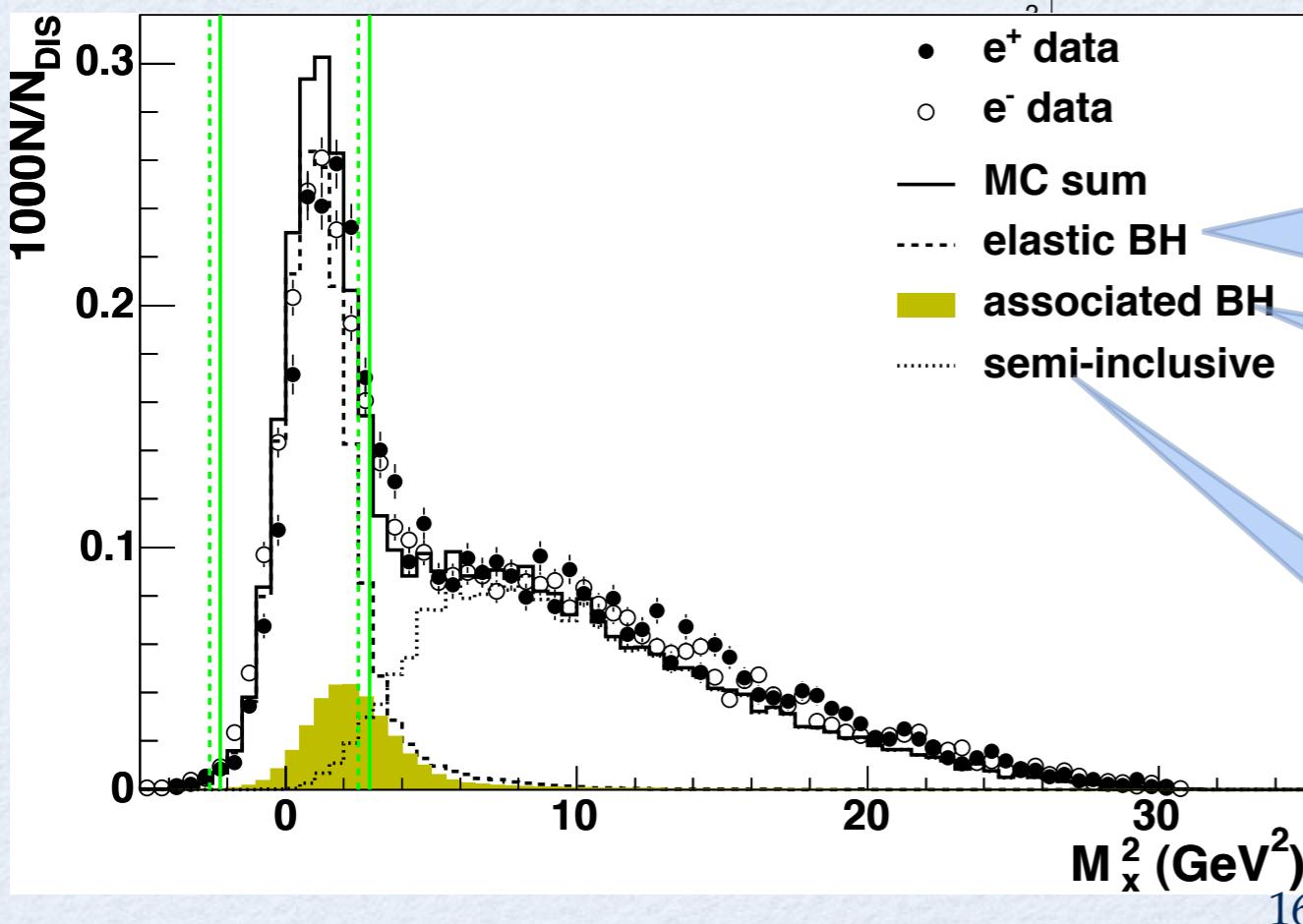
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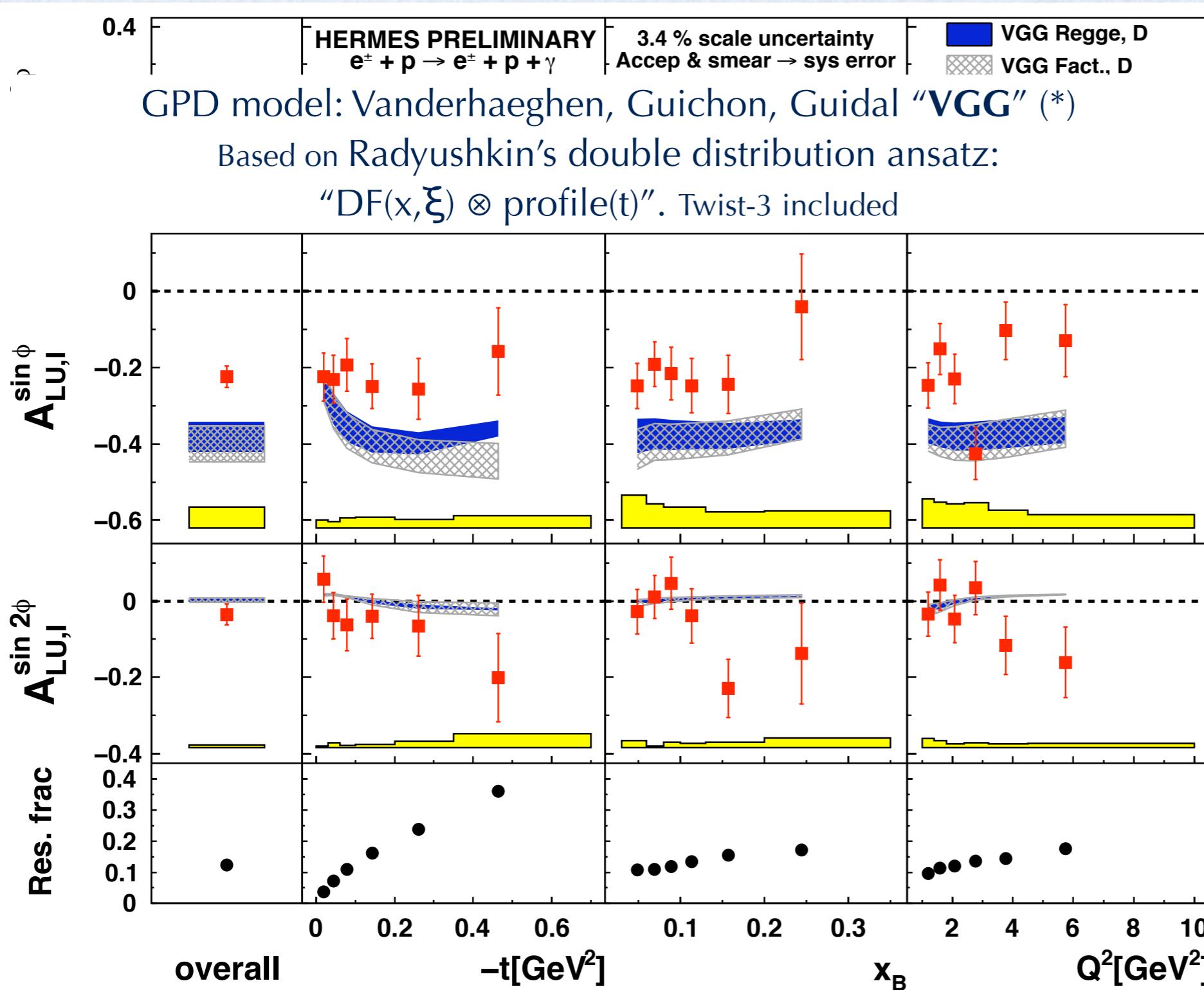
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HERMES: BSA from I on hydrogen

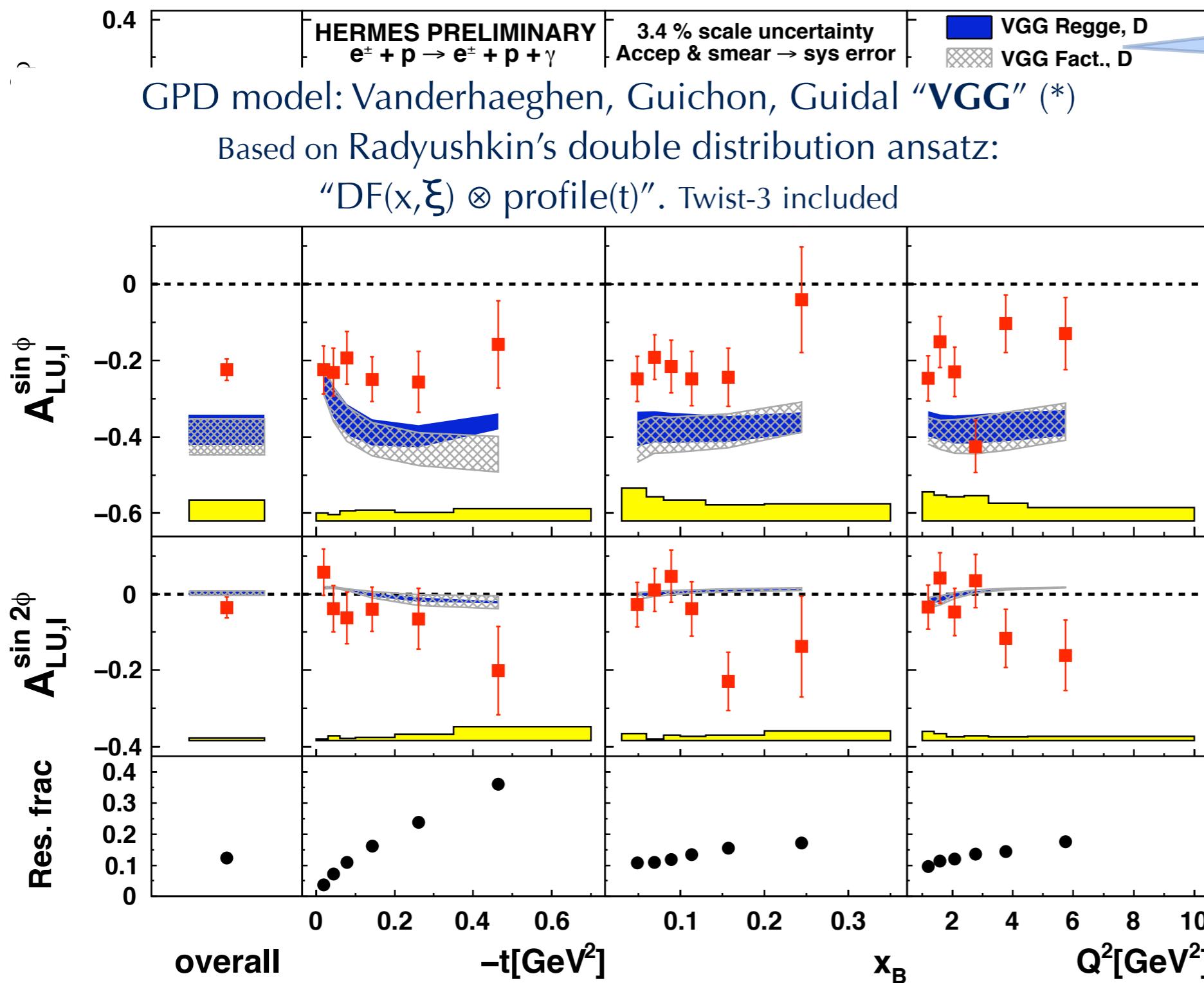


$$\propto \Im [F_1 \mathcal{H}]$$

← Higher twist (twist-3)

← Fraction of resonant excitation

HERMES: BSA from I on hydrogen



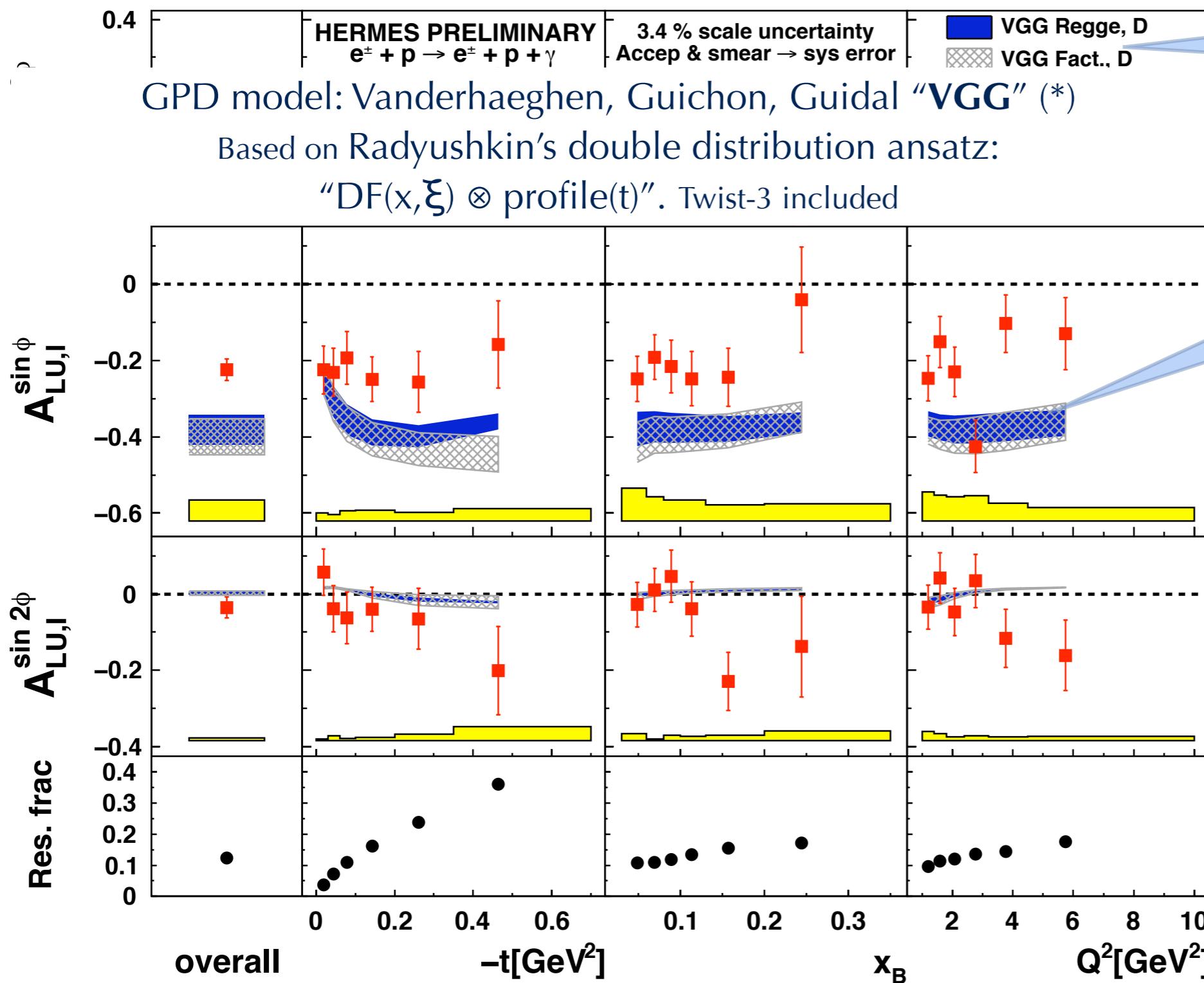
D-term to restore polynomiality

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HERMES: BSA from I on hydrogen



D-term to restore polynomiality

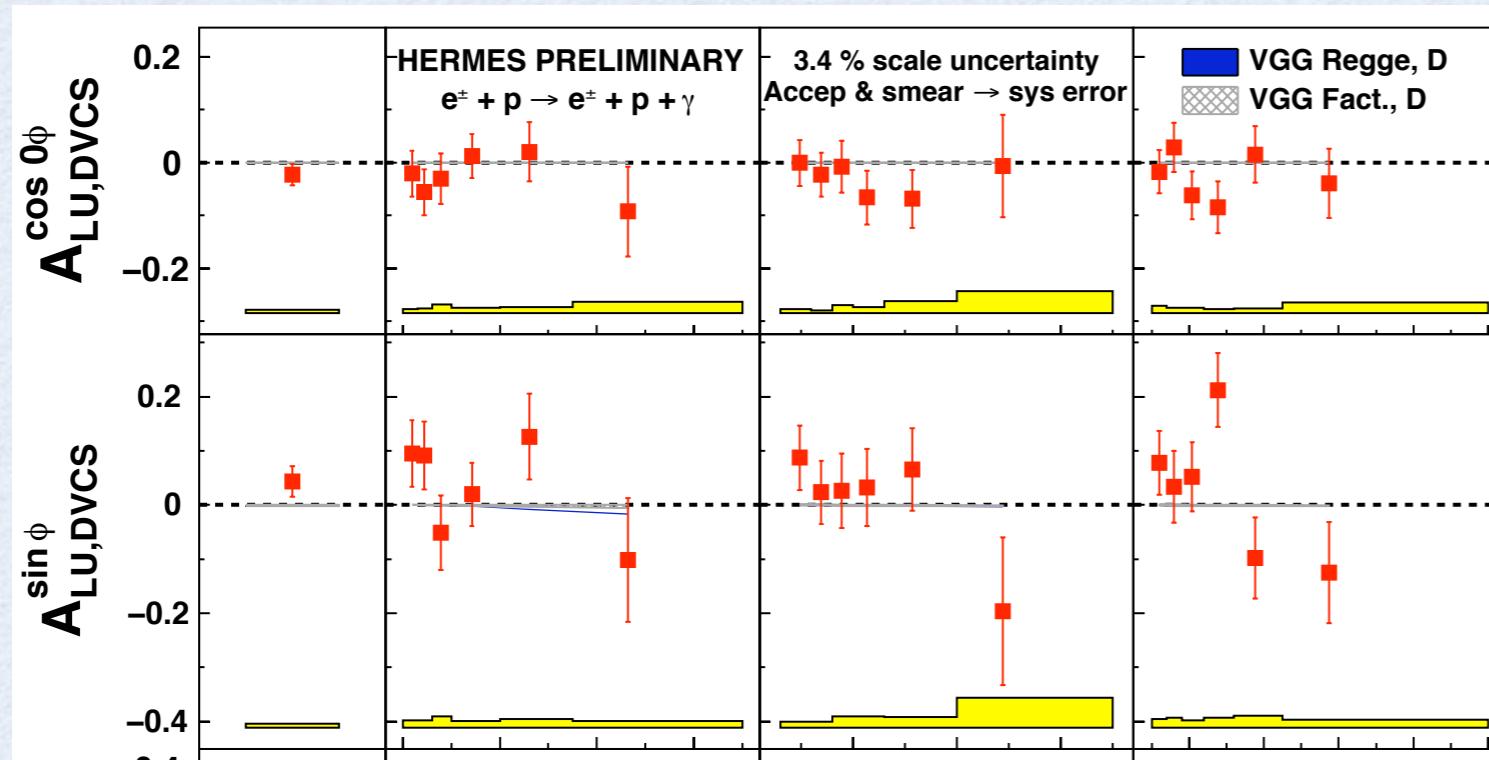
Bands by variation of skewness parameters

$$\propto \Im [F_1 \mathcal{H}]$$

← Higher twist (twist-3)

← Fraction of resonant excitation

HERMES: BSA from $|\tau_{DVCS}|^2$ on hydrogen



$$\propto [\mathcal{H}\mathcal{H}^* + \tilde{\mathcal{H}}\tilde{\mathcal{H}}^*]$$

bilinear combination of CFFs

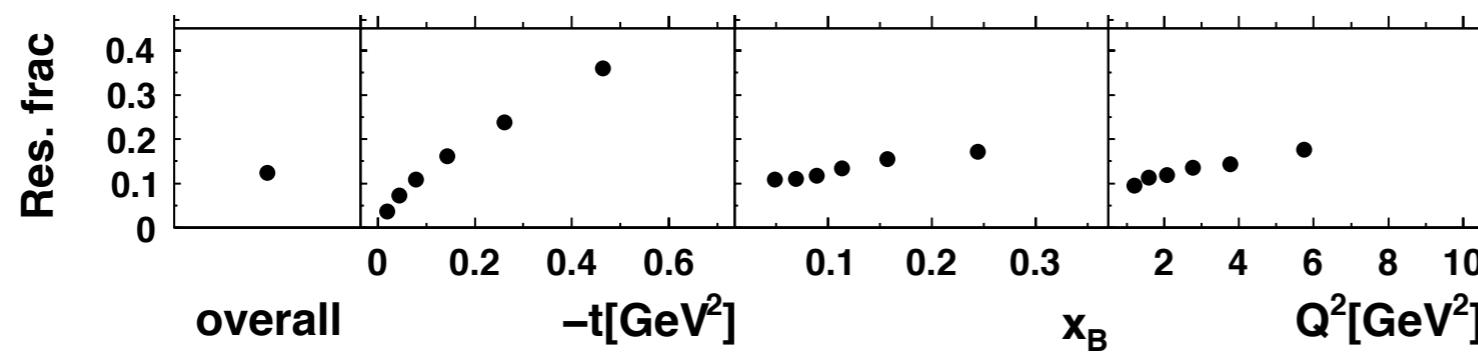
← Higher twist (twist-3)

GPD model: Vanderhaeghen, Guichon, Guidal ("VGG")

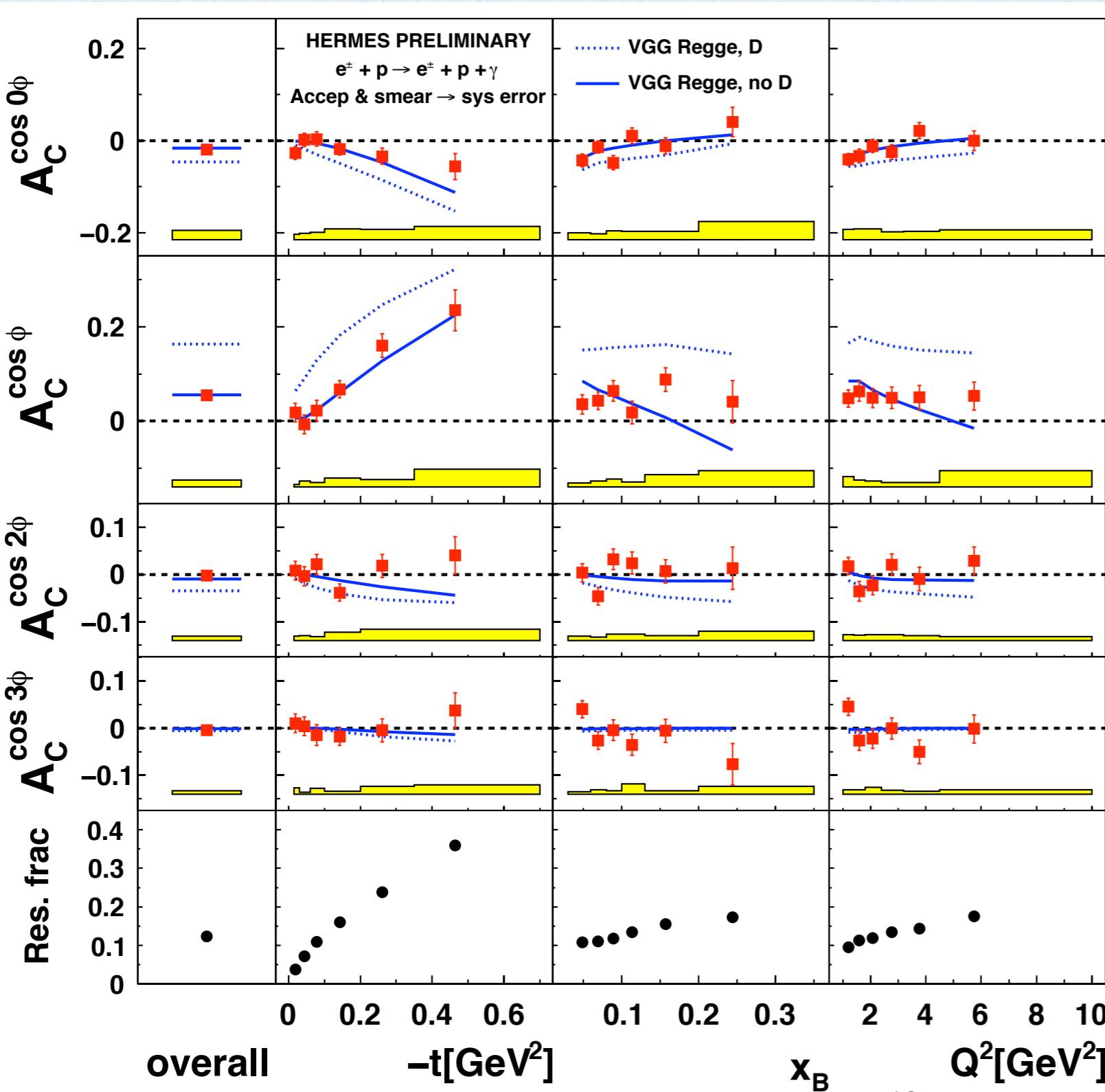
Phys. Rev. **D60** (1999) and Prog. Nucl. Phys. **47** (2001) 401

Based on double distribution ansatz: "DF(x, ξ) \otimes profile(t)".

Twist-3 included



HERMES: BCA on hydrogen



constant term:

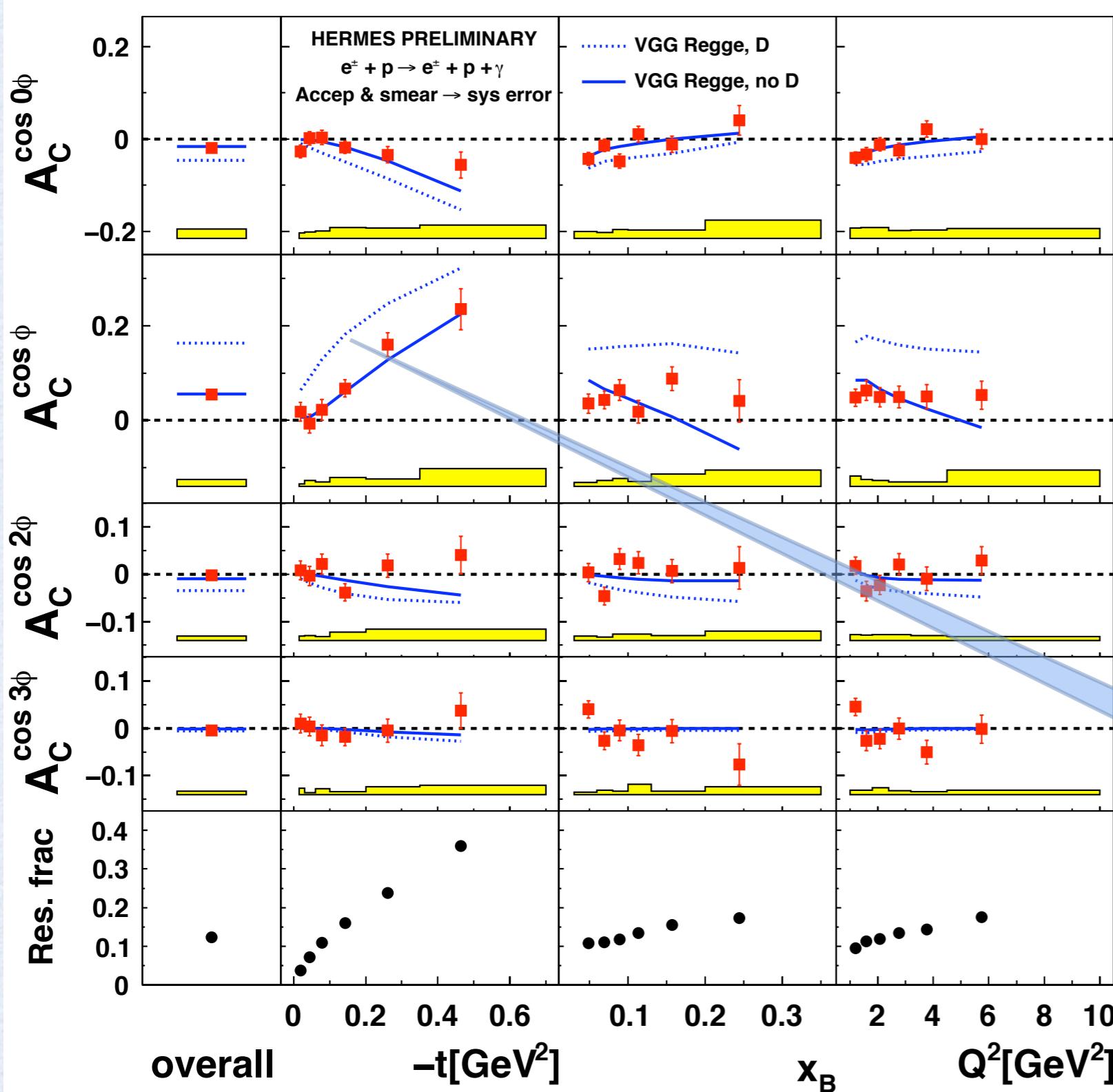
$$\propto -A_C^{\cos \phi}$$

$$\propto \Re [F_1 \mathcal{H}]$$

← Higher twist (twist-3)

← Gluon leading twist

HERMES: BCA on hydrogen



constant term:

$$\propto -A_C^{\cos \phi}$$

$$\propto \Re [F_1 \mathcal{H}]$$

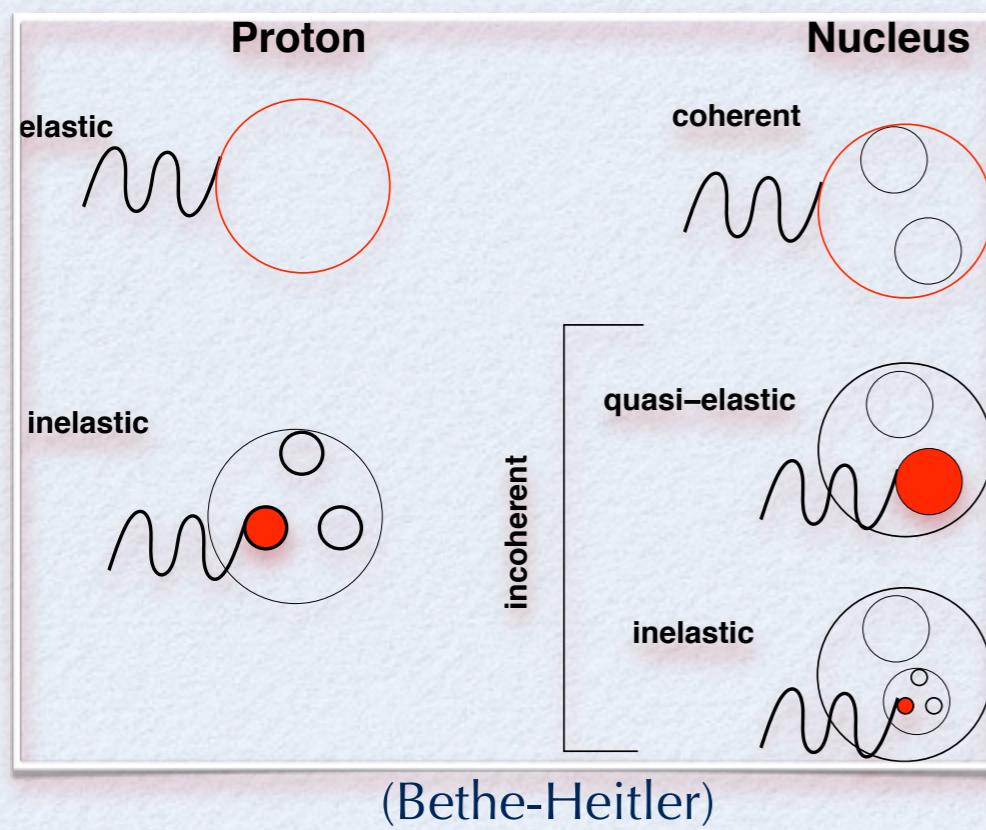
← Higher twist (twist-3)

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VGG with
D-term
disfavored

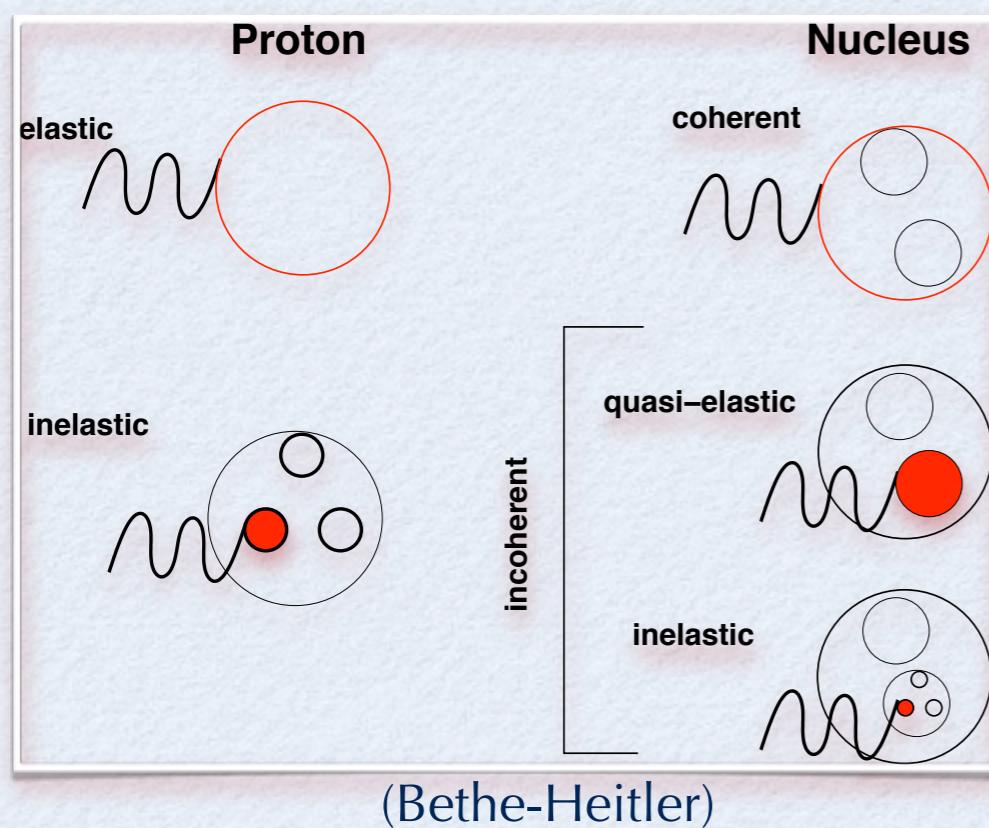
DVCS on Nuclear Targets

- * How does the nuclear environment modify parton-parton correlations?
- * How do nucleon properties change in the nuclear medium?

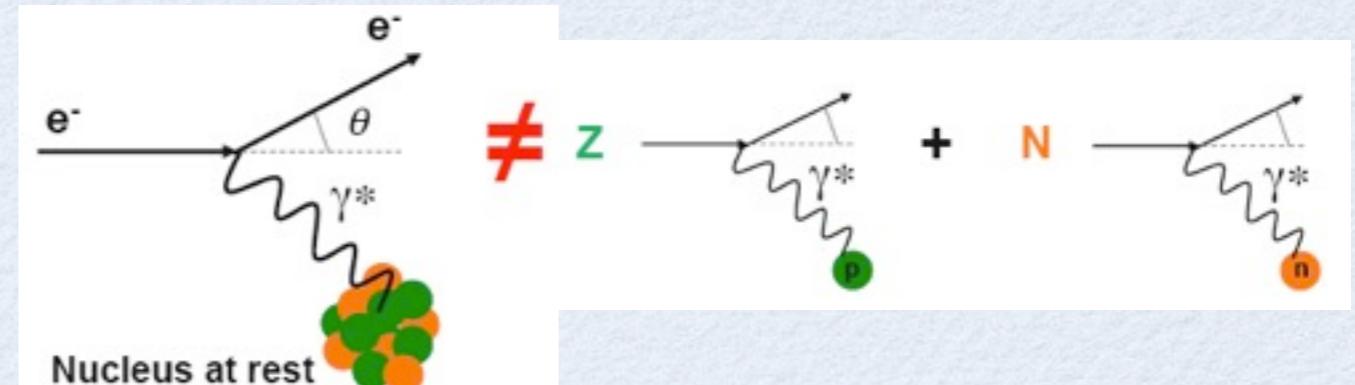


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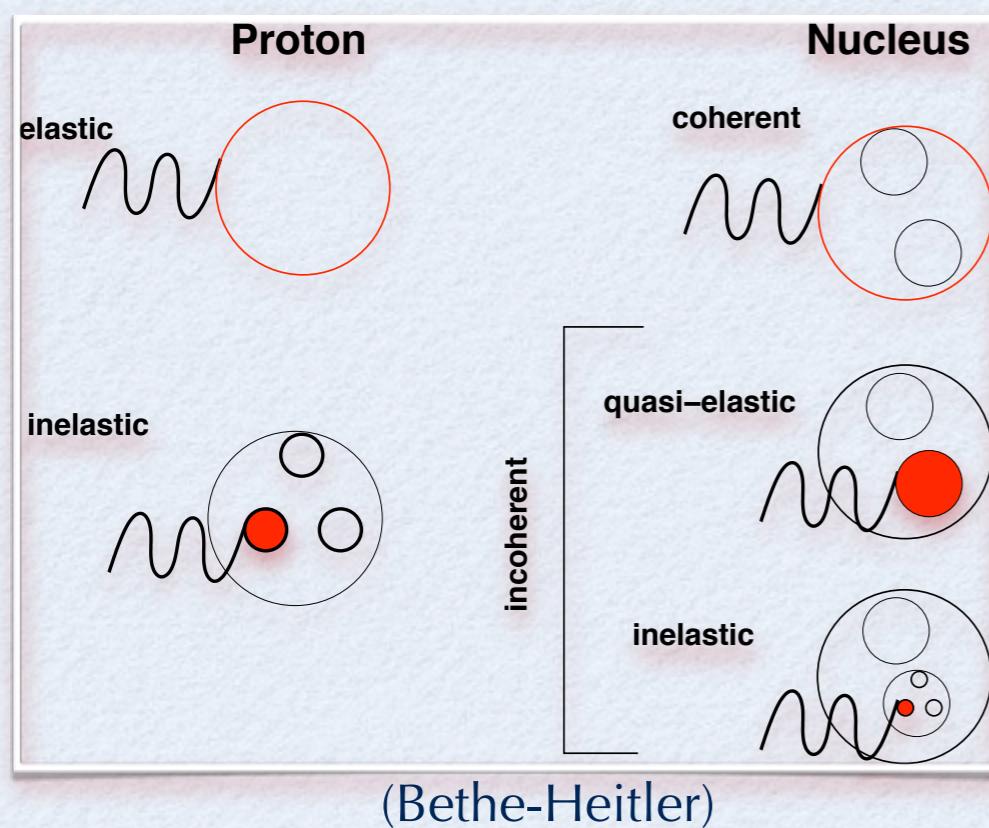
- * DVCS in coherent region:
new insights into 'generalized EMC effect'?



- Nuclear GPDs \neq GPDs of free nucleon
- Enhancement of effect when leaving forward limit?
- caused by transverse motion of partons in nuclei?
- important role of mesonic degrees of freedom?
- manifest in strong increase of real part of τ_{DVCS} with atomic mass number A ?

DVCS on Nuclear Targets

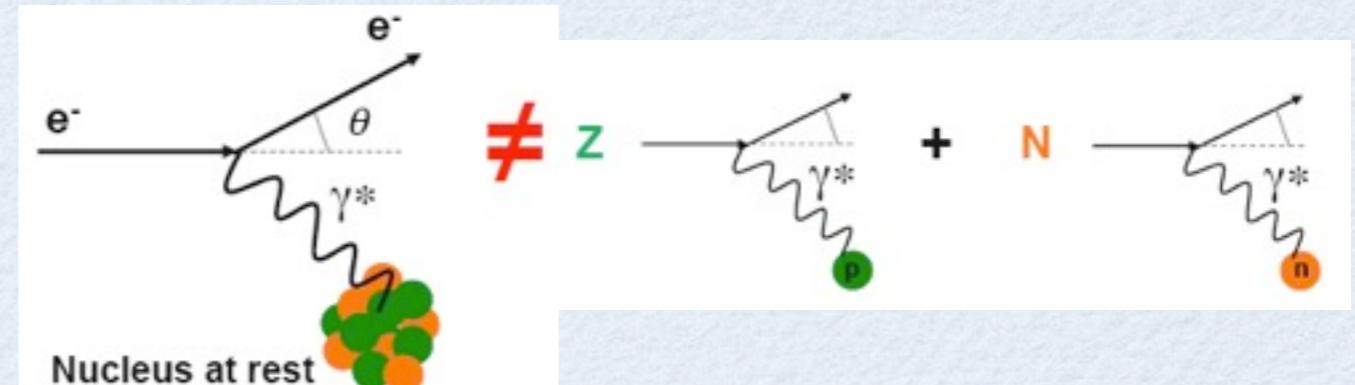
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HERMES
measurements
on nuclear
targets

Target	spin	L (pb^{-1})
H	1/2	227
He	0	32
N	1	51
Ne	0	86
Kr	0	77
Xe	0, 1/2, 3/2	47

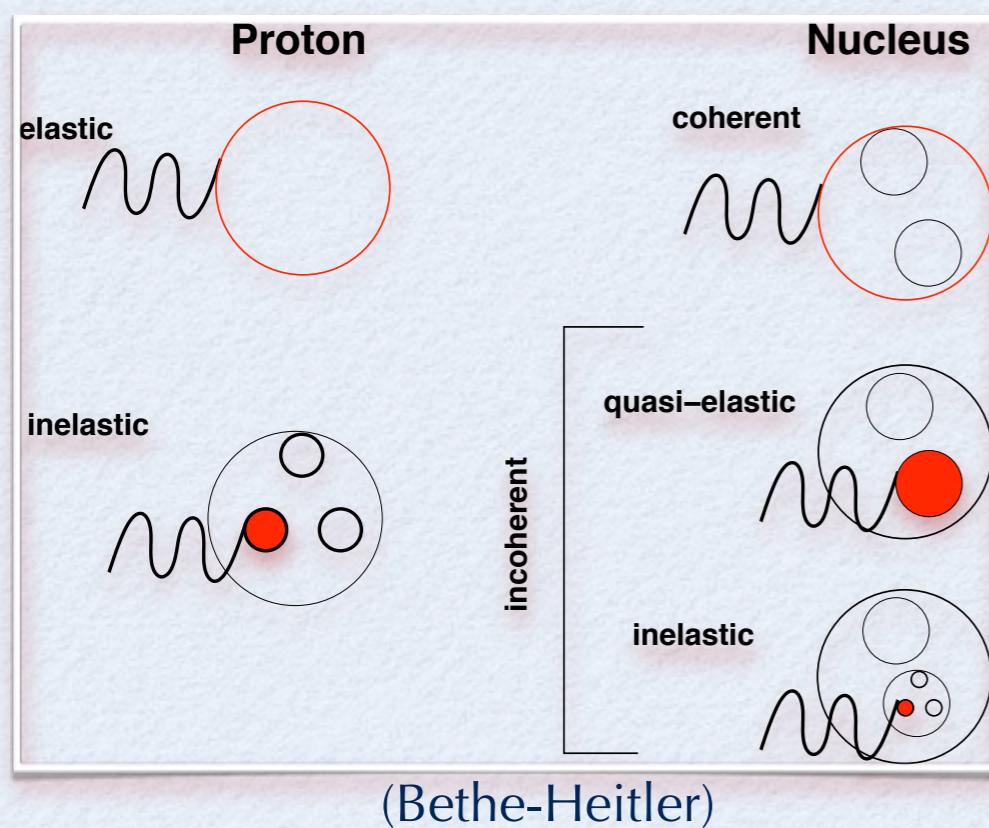
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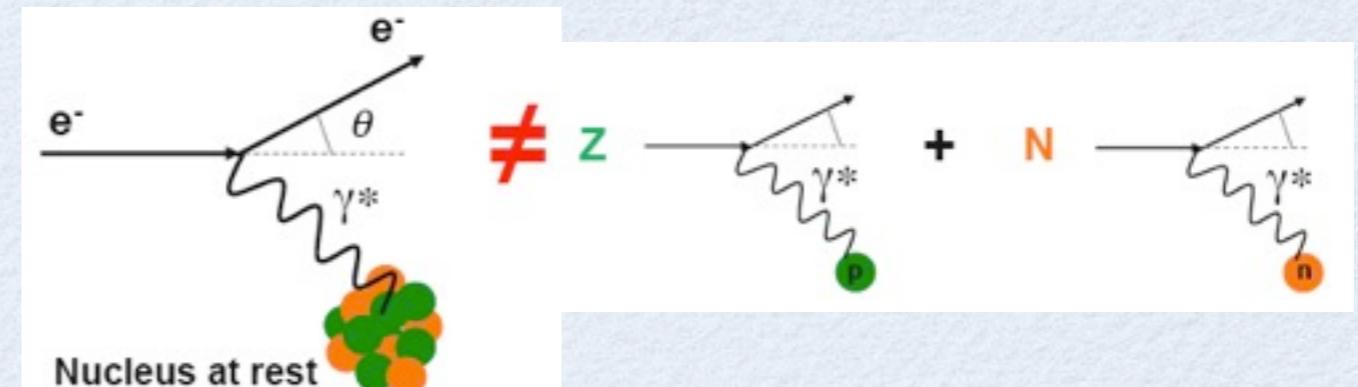
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DVCS on Nuclear Targets

- * How does the nuclear environment modify parton-parton correlations?
- * How do nucleon properties change in the nuclear medium?



- * DVCS in coherent region: new insights into 'generalized EMC effect'?



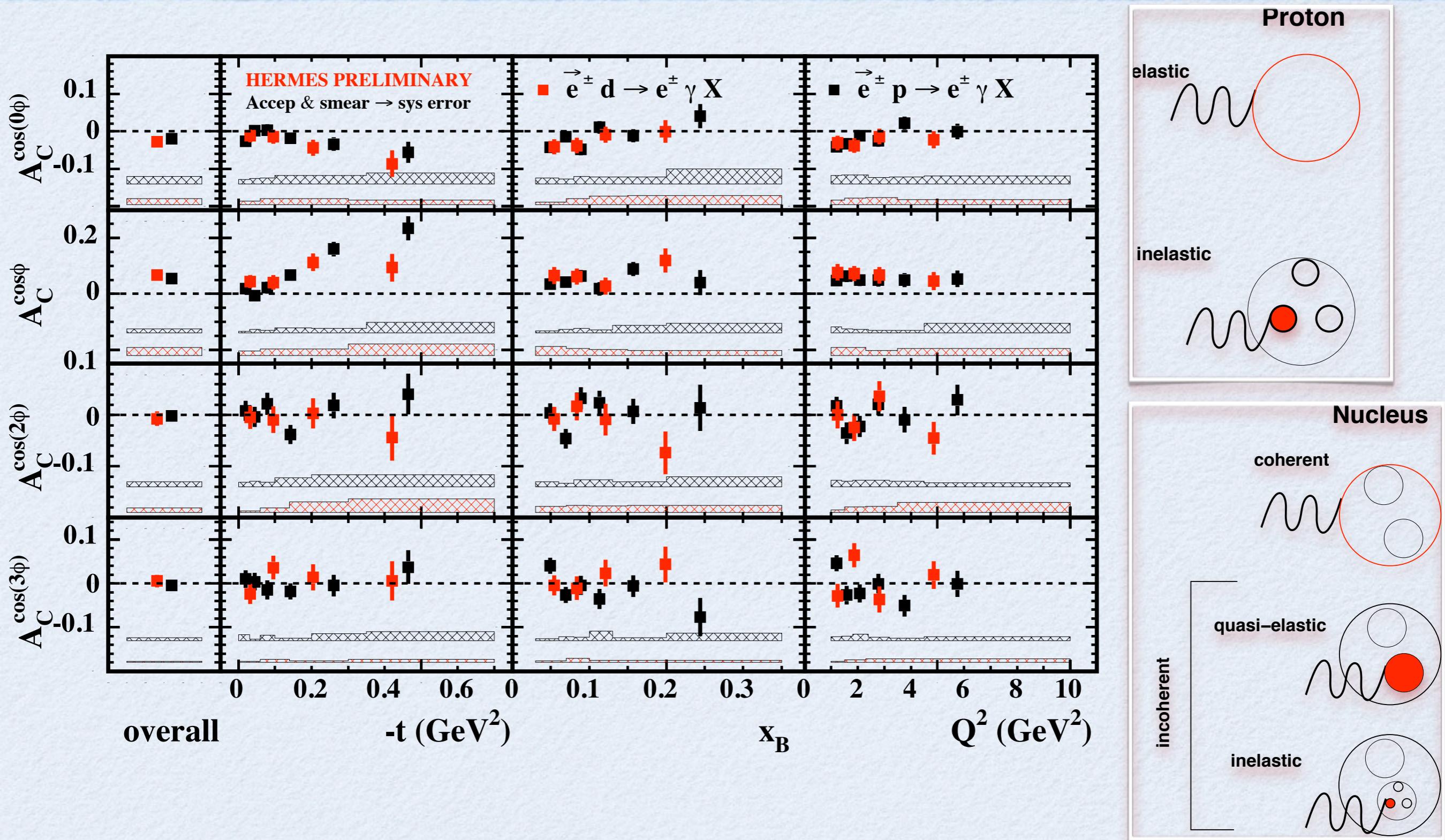
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**HERMES
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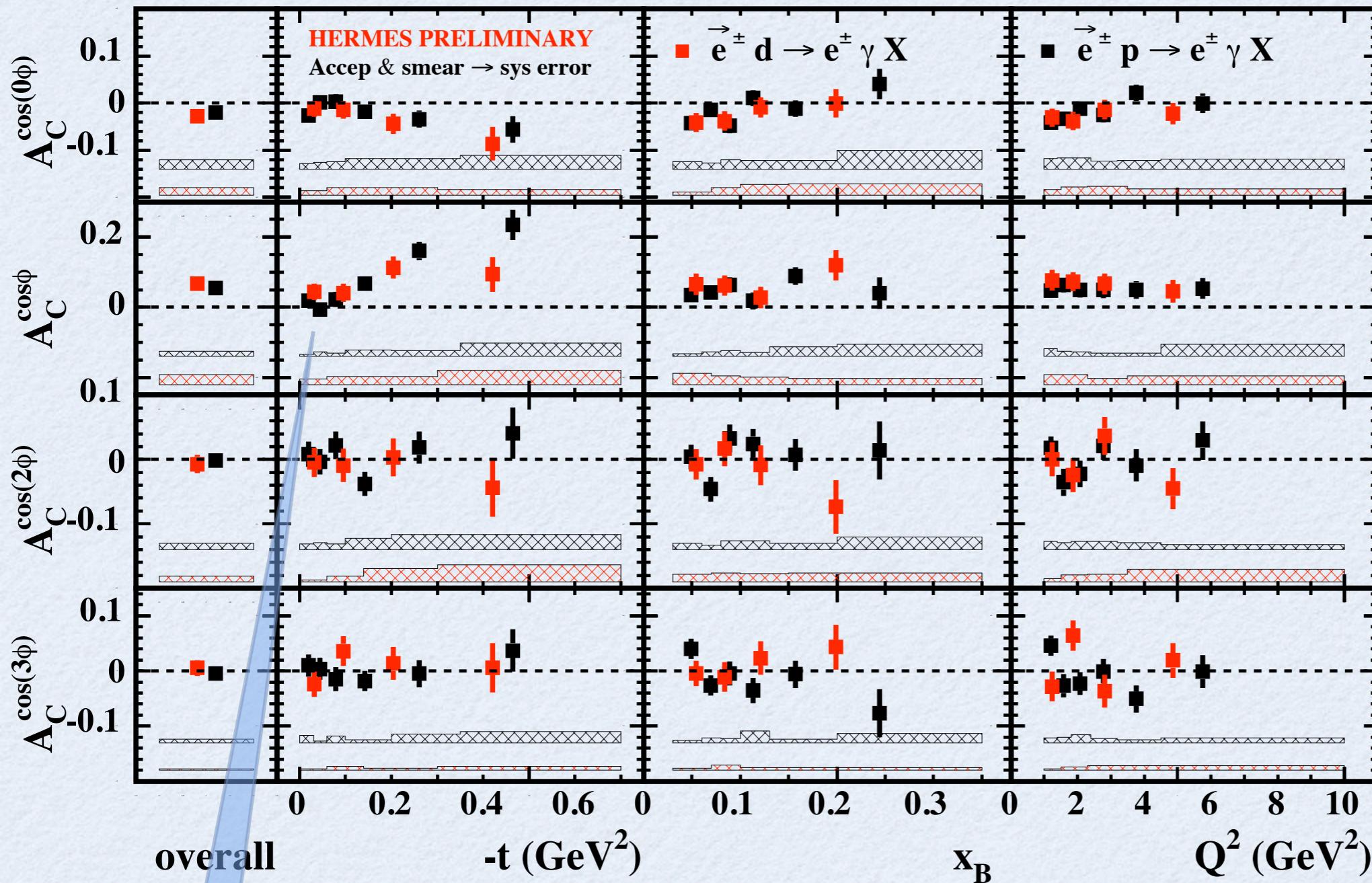
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N	1	51
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Xe	0, 1/2, 3/2	47

+ deuterium,
spin-1, 300 pb^{-1}

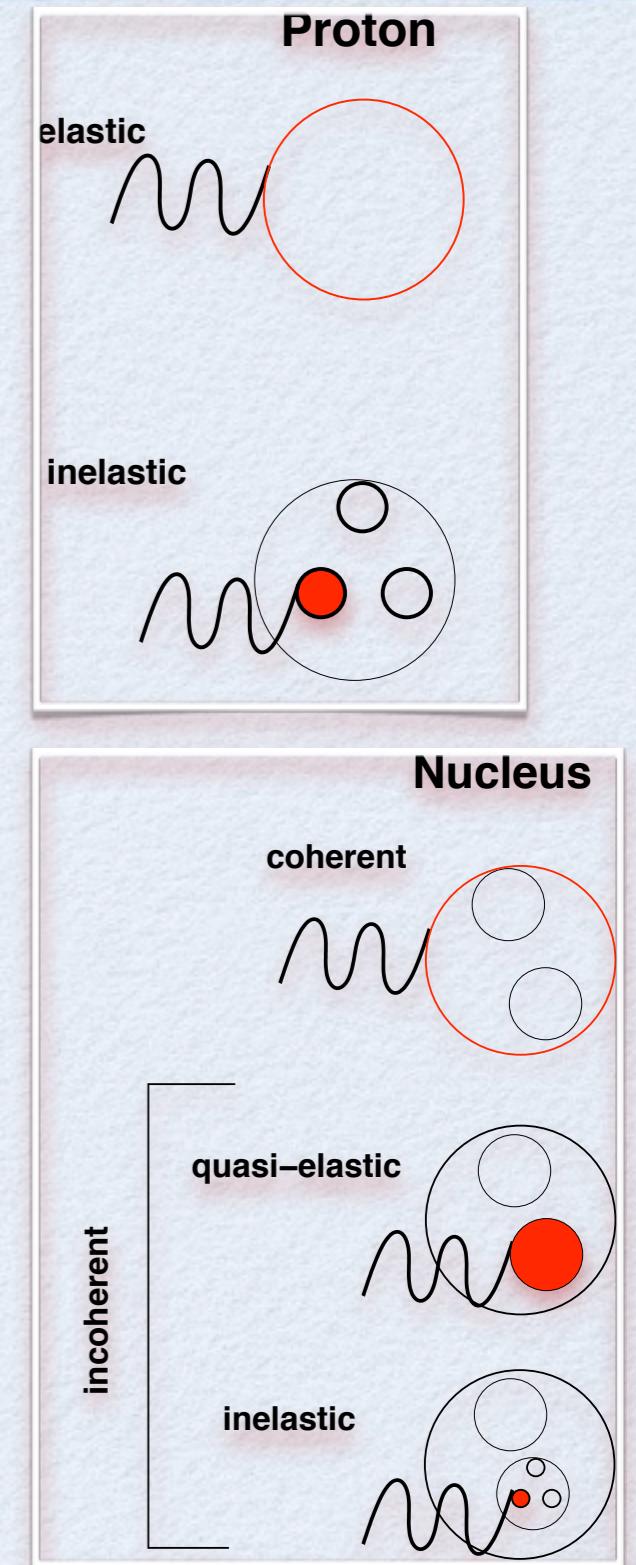
HERMES: BCAs on hydrogen and deuterium



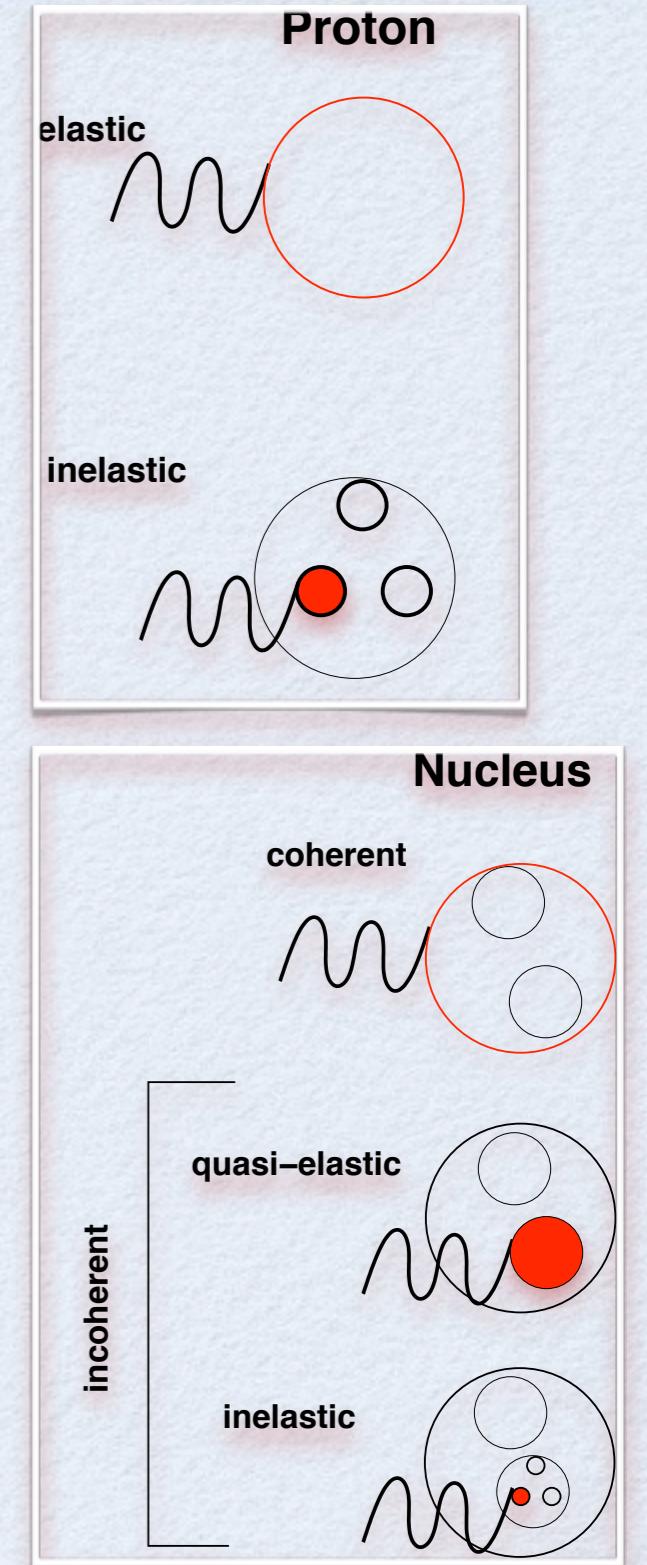
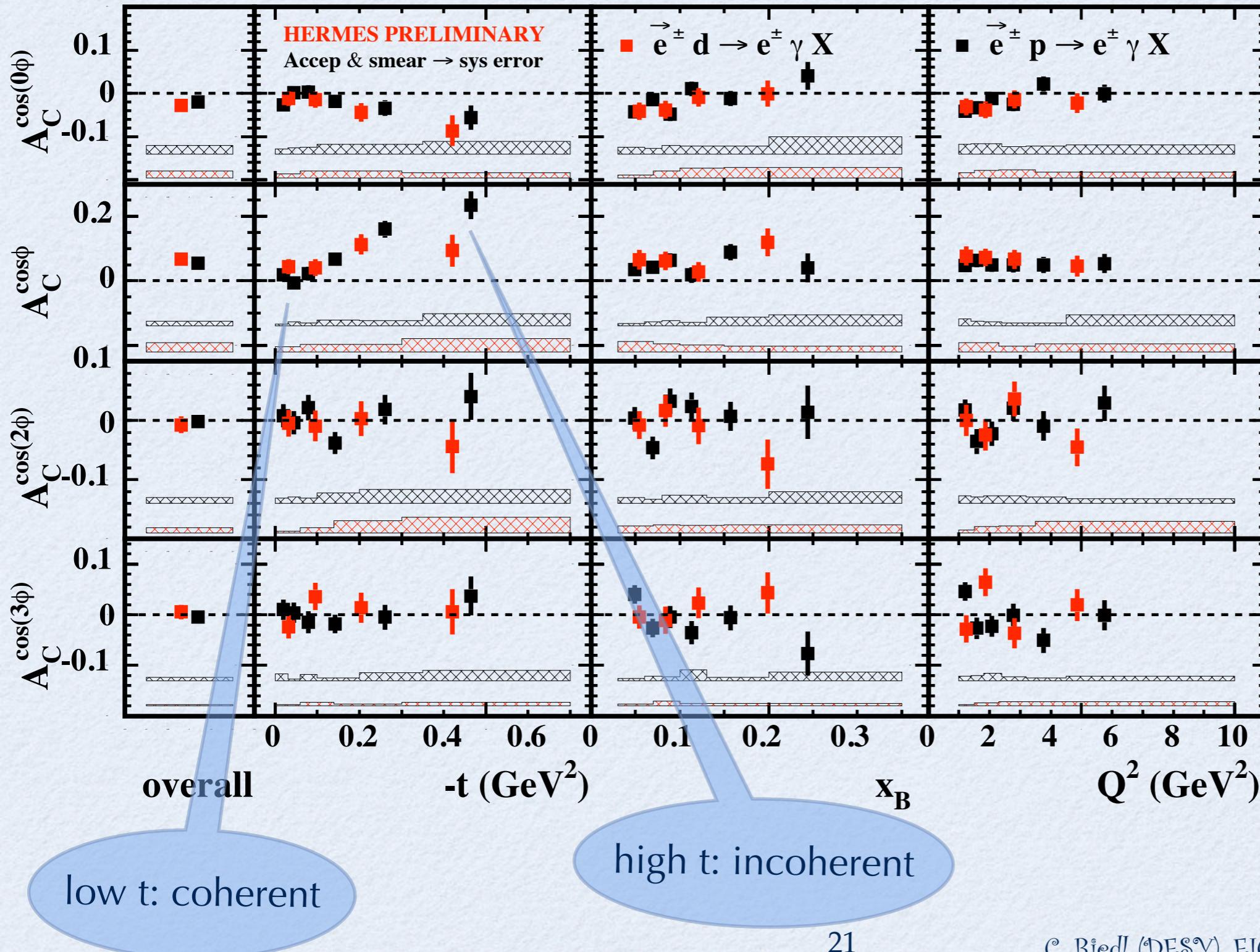
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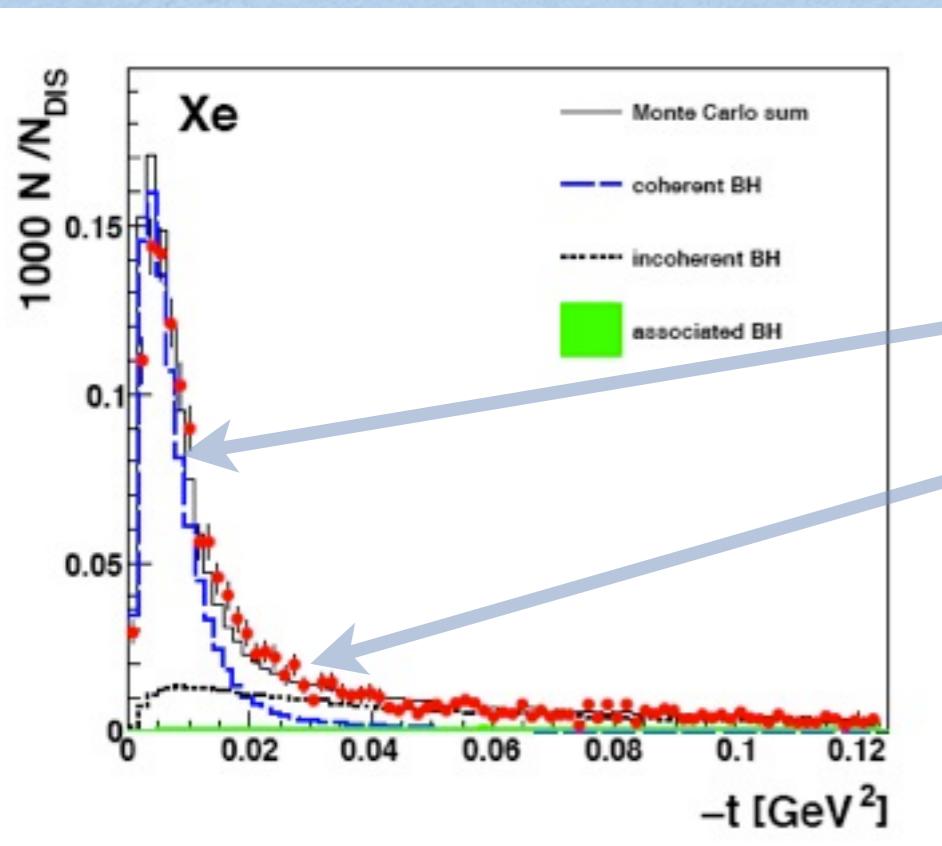
overall
low t : coherent



HERMES: BCAs on hydrogen and deuterium



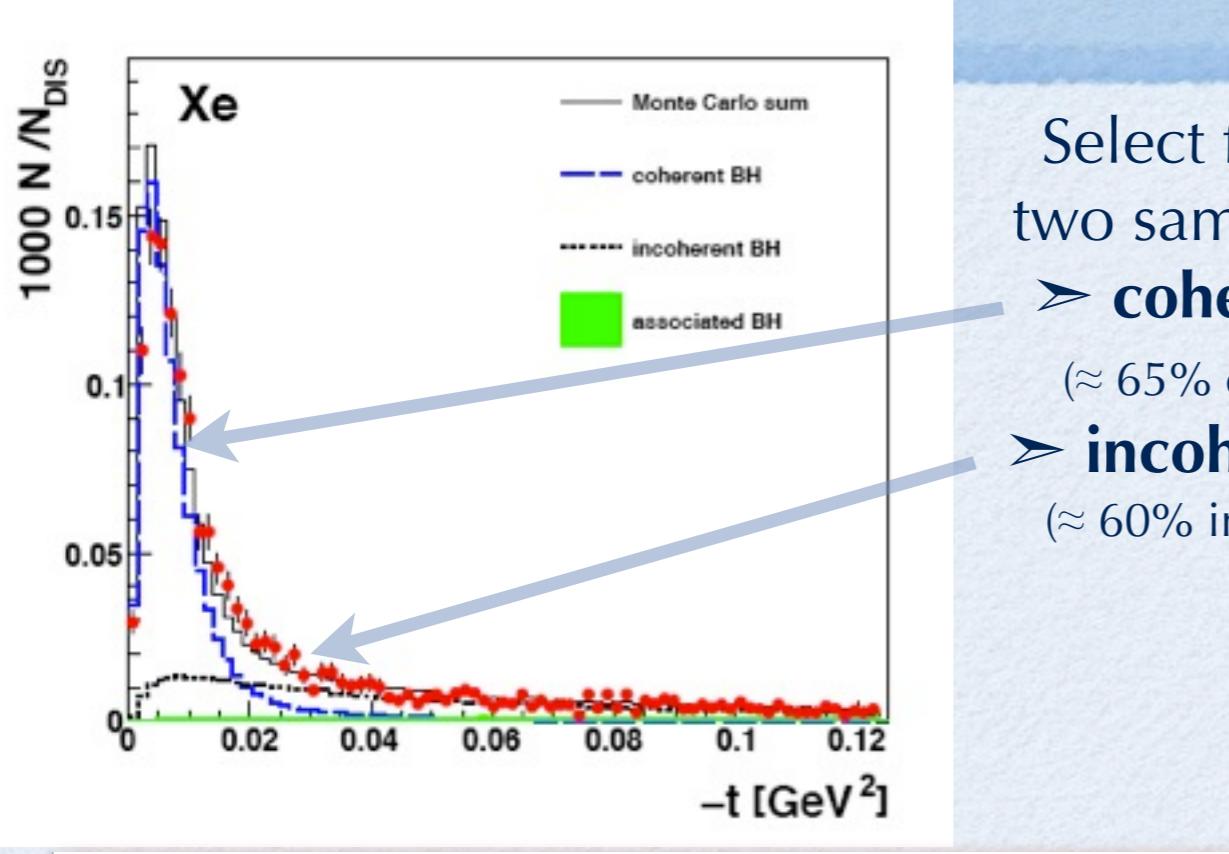
DVCS at HERMES: Nuclear mass dependence



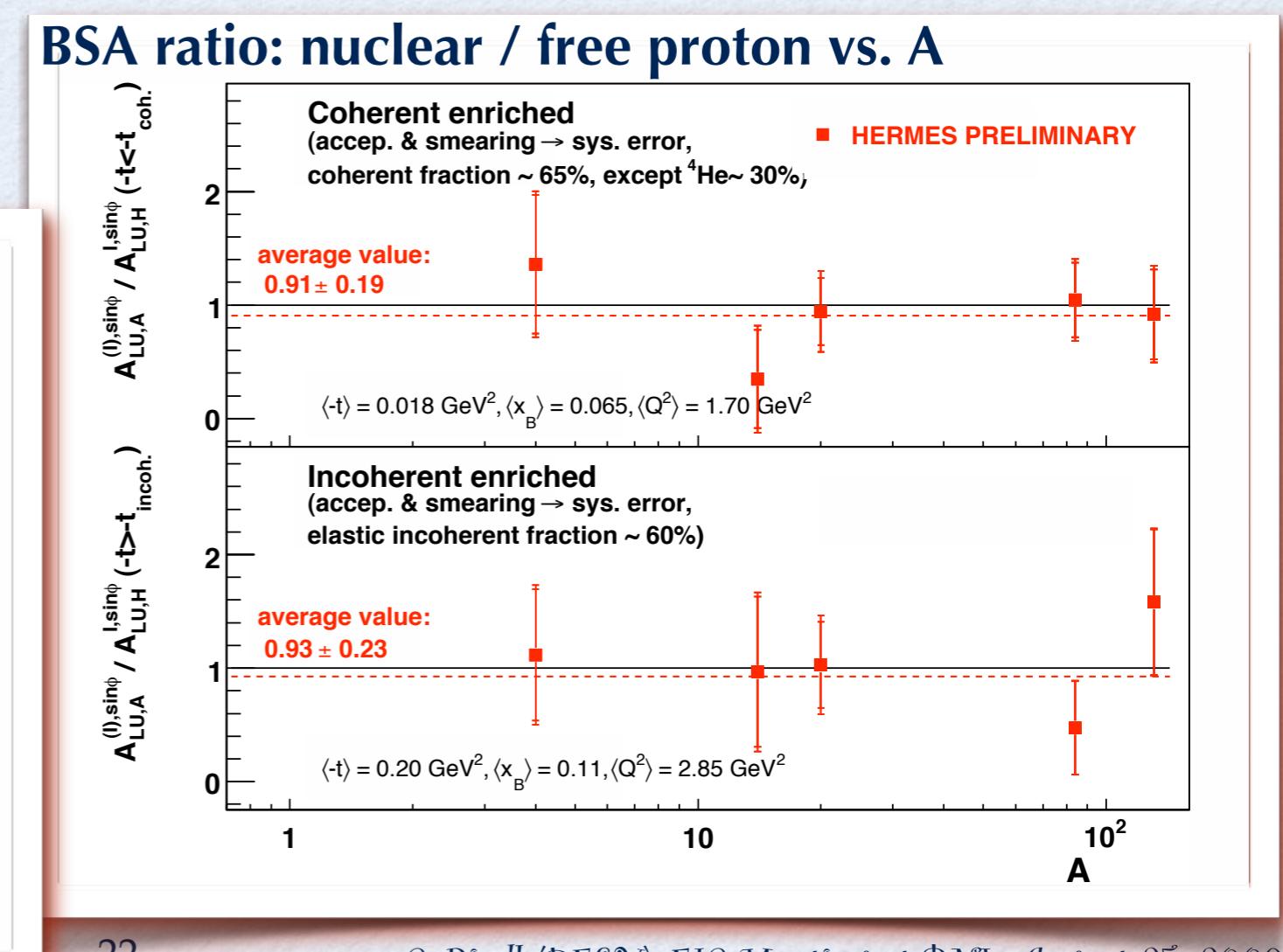
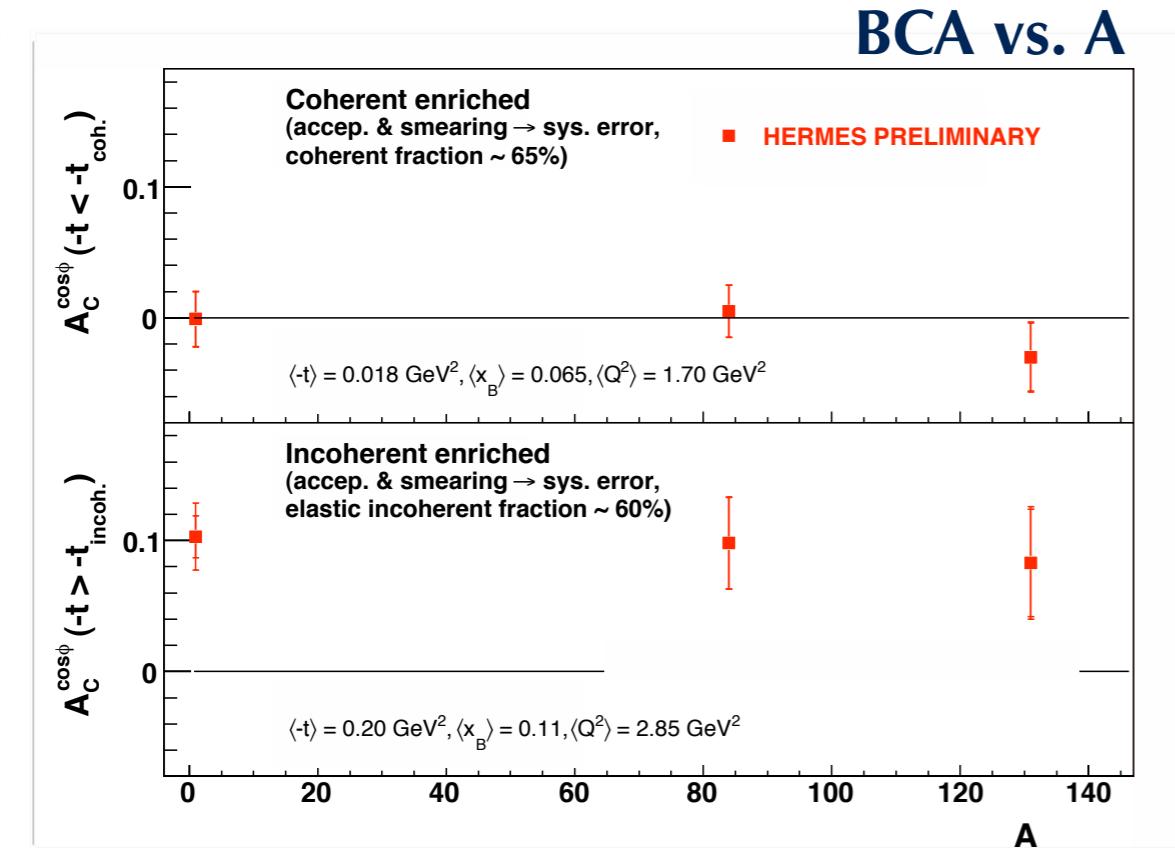
Select for each target
two samples (t -cutoffs):

- **coherent enriched**
($\approx 65\%$ coherent fraction)
- **incoherent enriched**
($\approx 60\%$ incoherent fraction)

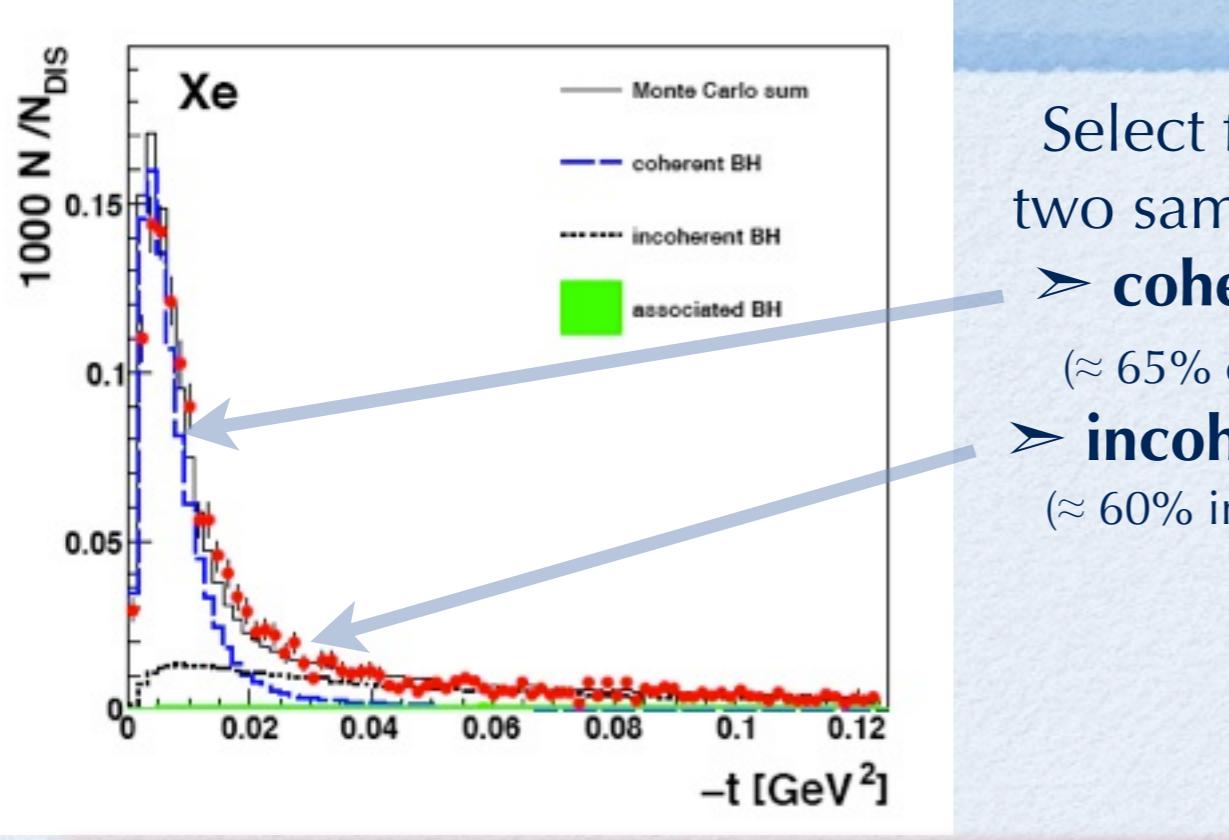
DVCS at HERMES: Nuclear mass dependence



Select for each target two samples (t -cutoffs):
 ➤ **coherent enriched**
 (≈ 65% coherent fraction)
 ➤ **incoherent enriched**
 (≈ 60% incoherent fraction)



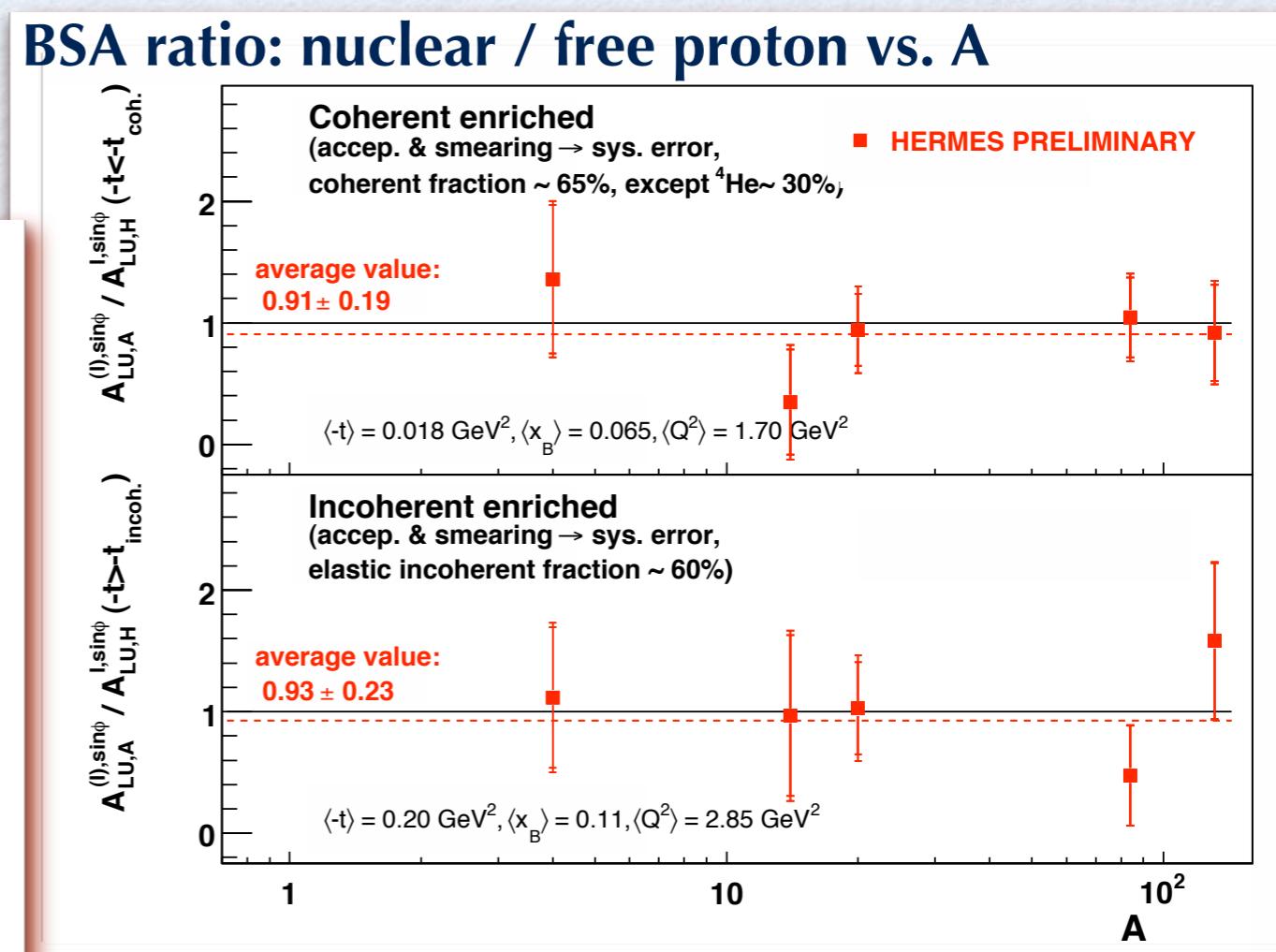
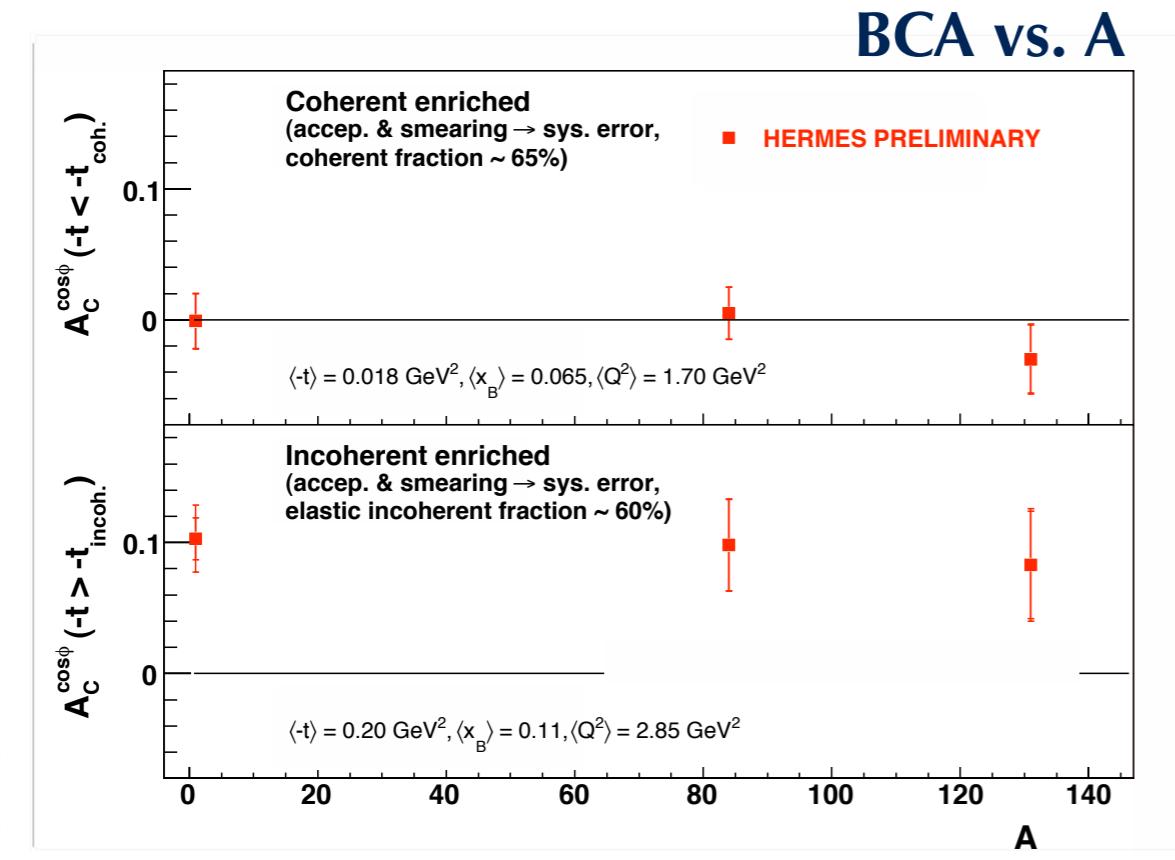
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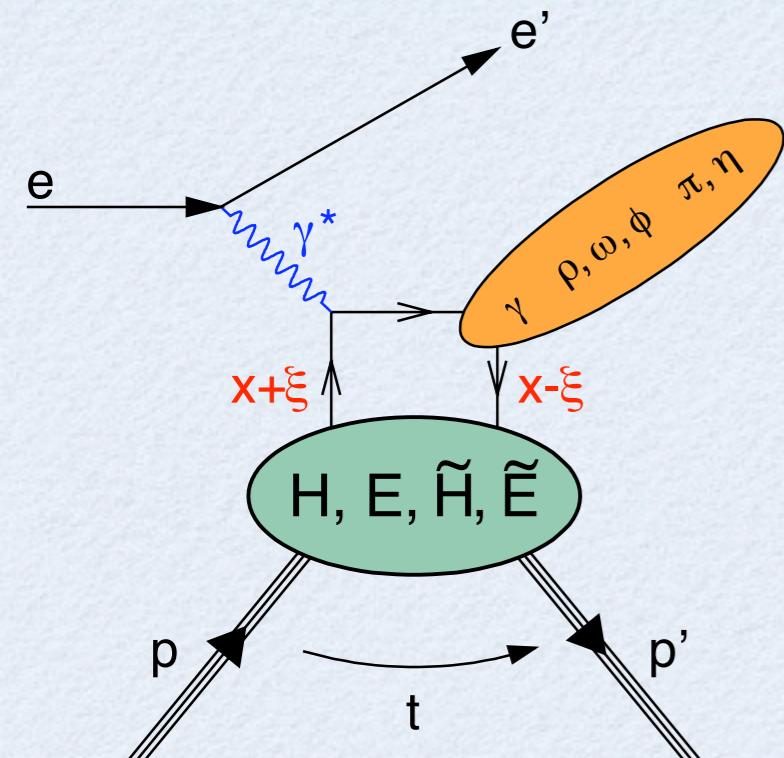
Select for each target two samples (t -cutoffs):

- > **coherent enriched**
($\approx 65\%$ coherent fraction)
- > **incoherent enriched**
($\approx 60\%$ incoherent fraction)

No nuclear mass dependence of BCA and BSA observed within uncertainties
⇒ no enhancement of τ_{DVCS}



Exclusivity at HERMES in a Nutshell

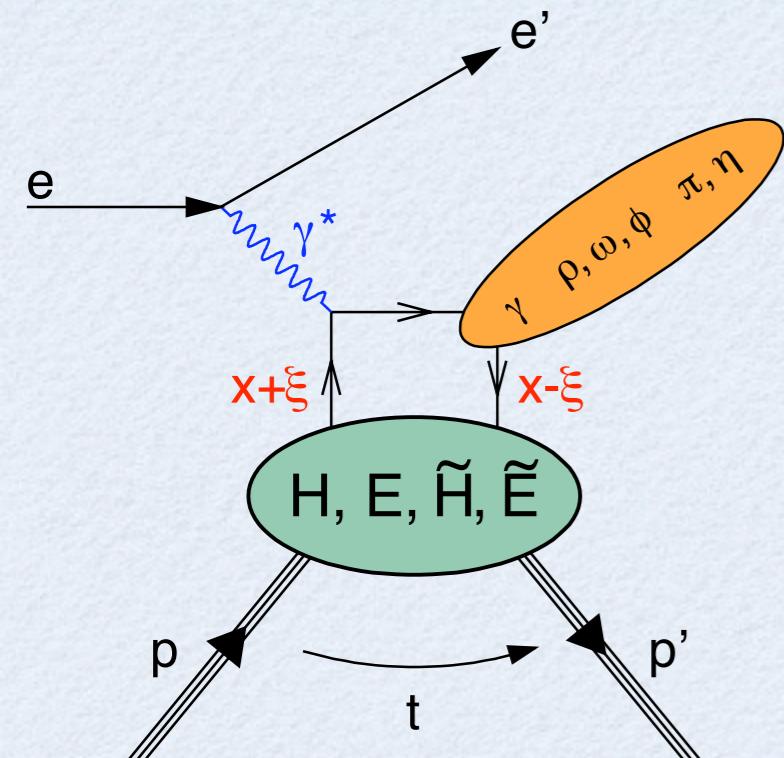


GPD access at HERMES:

nucleon helicity	quark helicity independent	quark helicity dependent
	photon: $J^P=1^-$ (DVCS)	
conserved	$H: A_C, A_{LU}, A_{UT}$	$\tilde{H}: A_{UL}, [A_{UT}]$
flipped	$E: A_{UT}$	$\tilde{E}: [A_{UT}]$
	$J^P=1^-$ mesons	$J^P=0^-$ mesons

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx \ x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

Exclusivity at HERMES in a Nutshell

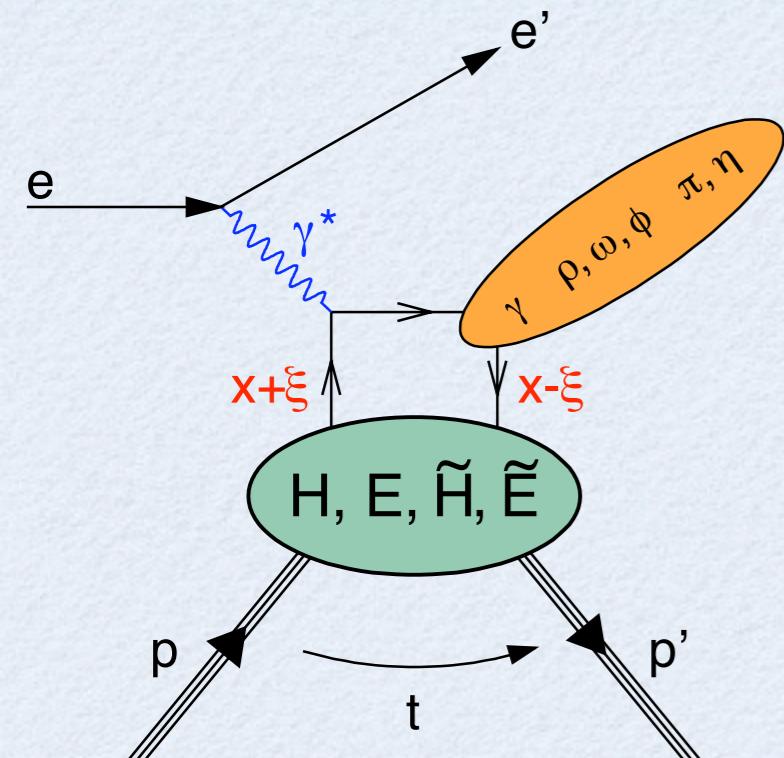


GPD access at HERMES:

nucleon helicity	quark helicity independent	quark helicity dependent
conserved	photon: $J^P=1^-$ (DVCS)	\tilde{H} : $A_{UL}, [A_{UT}]$
flipped	H : A_C, A_{LU} , A_{UT}	\tilde{E} : $[A_{UT}]$
	$J^P=1^-$ mesons	$J^P=0^-$ mesons

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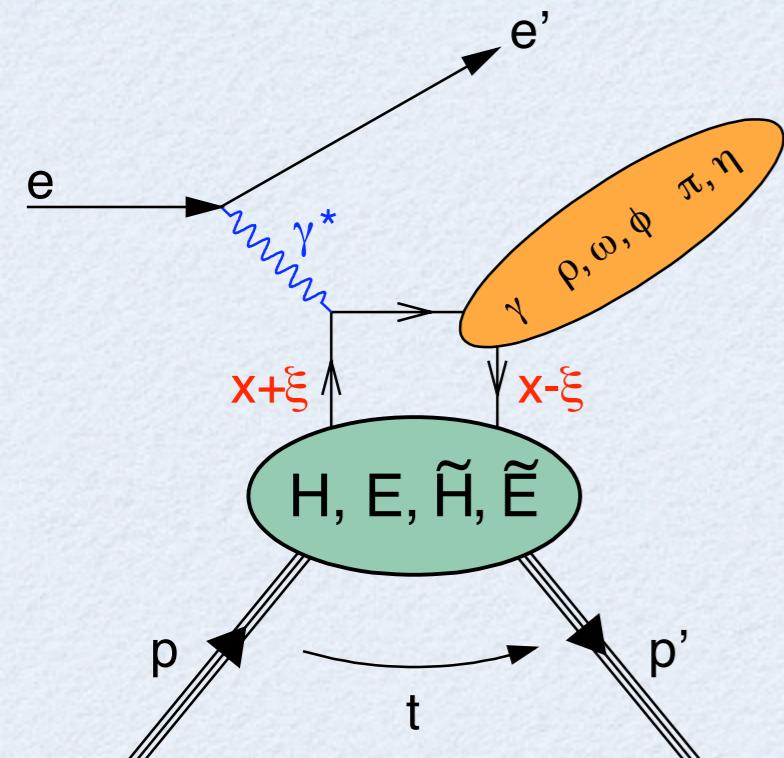


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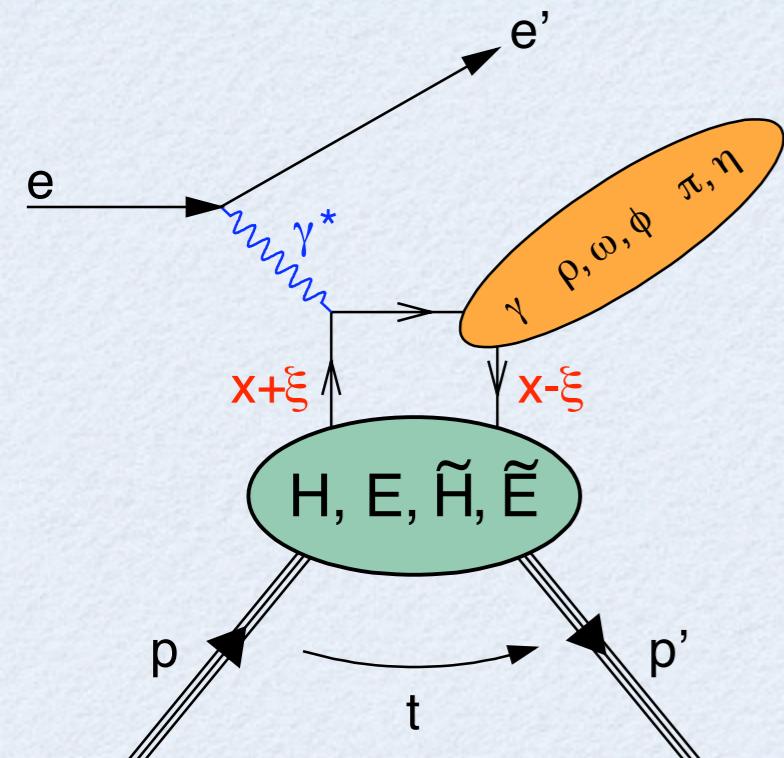
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	$J^P=1^-$ mesons	$J^P=0^-$ mesons

Annotations from the diagram:

- vector mesons** (ρ^0, ω, ϕ) are associated with the $J^P=1^-$ mesons row.
- pseudoscalar mesons** (π^+, η) are associated with the $J^P=0^-$ mesons row.

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx \ x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

Exclusivity at HERMES in a Nutshell



GPD access at HERMES:

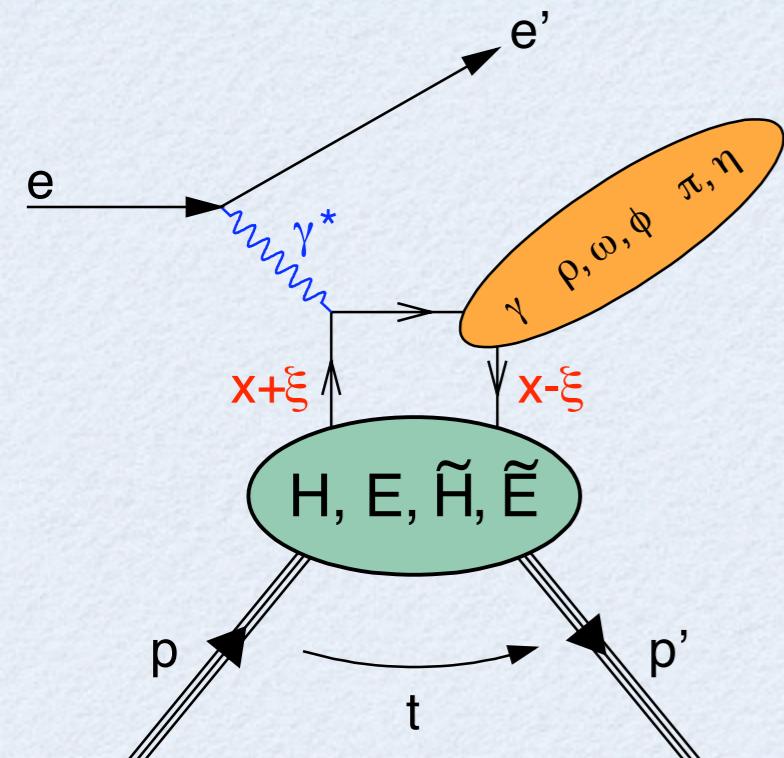
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vector mesons ρ^0, ω, ϕ

pseudoscalar mesons π^+, η

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

Exclusivity at HERMES in a Nutshell



GPD access at HERMES:

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	$J^P=1^-$ mesons	$J^P=0^-$ mesons

Annotations below the table:

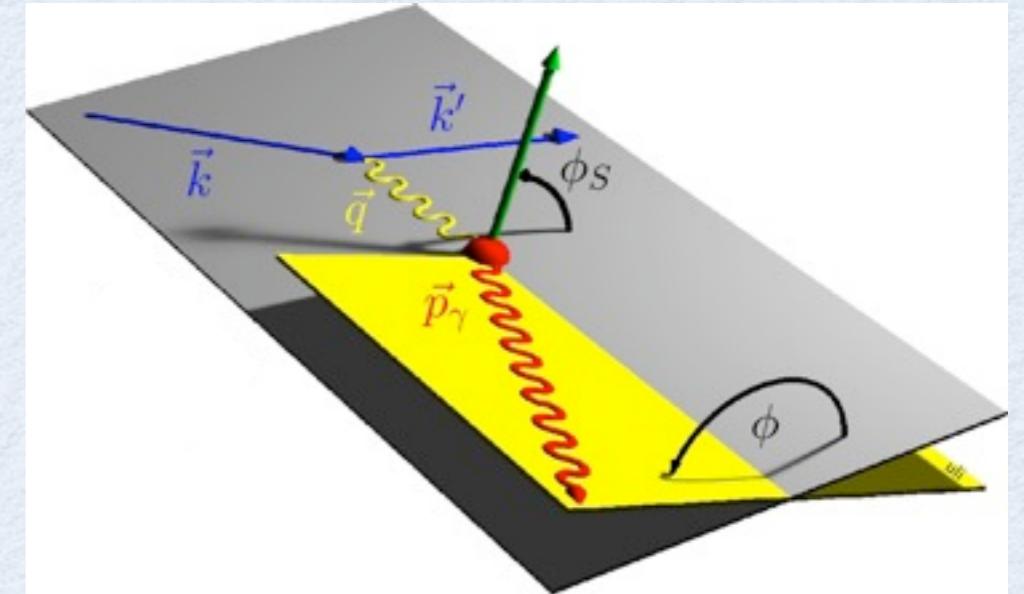
- vector mesons**: ρ^0, ω, ϕ (circled in red)
- pseudoscalar mesons**: π^+, η (circled in purple)

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

DVCS Transverse Target Spin Asymmetry $\mathcal{A}_{\text{UT}}(\phi, \phi_s)$

- * \mathcal{A}_{UT} : the only DVCS asymmetry on the proton for which **GPD E is not suppressed**

(Hall-A: BSA on neutron)



- * **HERMES**: transversely polarized hydrogen, 170 pb^{-1} , 2 beam charges
 - Separation of DVCS and interference terms possible

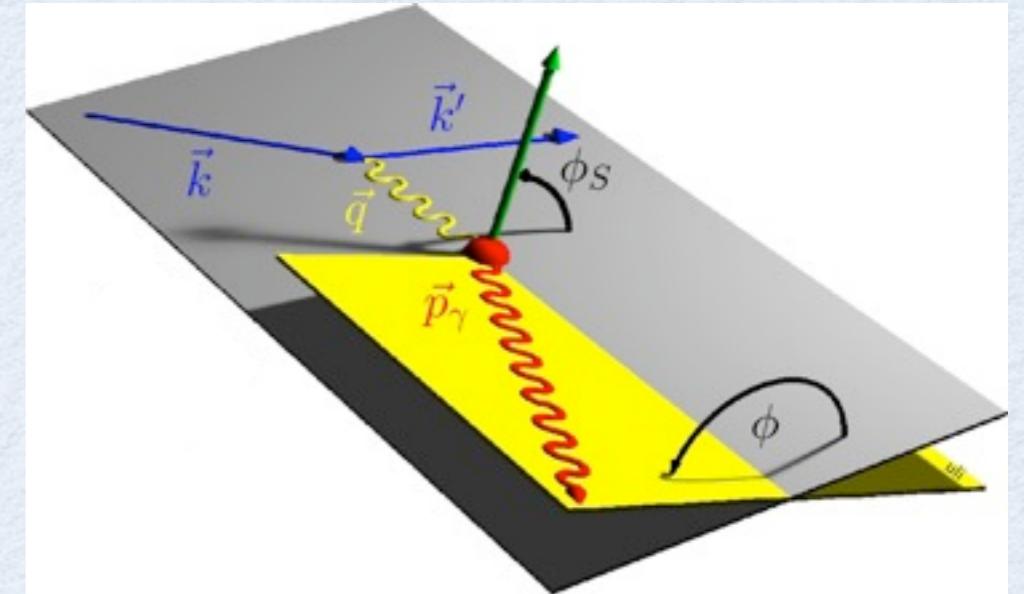
$$A_{\text{UT}}^T(\phi, \phi_s) \propto [d\sigma^+(\phi, \phi_s) - d\sigma^-(\phi, \phi_s)] - [d\sigma^+(\phi, \phi_s + \pi) - d\sigma^-(\phi, \phi_s + \pi)]$$

$$\begin{aligned} A_{\text{UT}}^T(\phi, \phi_s) &\propto \text{Im} (F_2 \mathcal{H} - F_1 \mathcal{E}) \sin(\phi - \phi_s) \cos \phi \\ &+ \text{Im} (F_2 \tilde{\mathcal{H}} - (F_1 + \xi F_2) \tilde{\mathcal{E}}) \cos(\phi - \phi_s) \sin \phi \end{aligned}$$

DVCS Transverse Target Spin Asymmetry $\mathcal{A}_{\text{UT}}(\phi, \phi_s)$

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➤ Separation of DVCS and interference terms possible

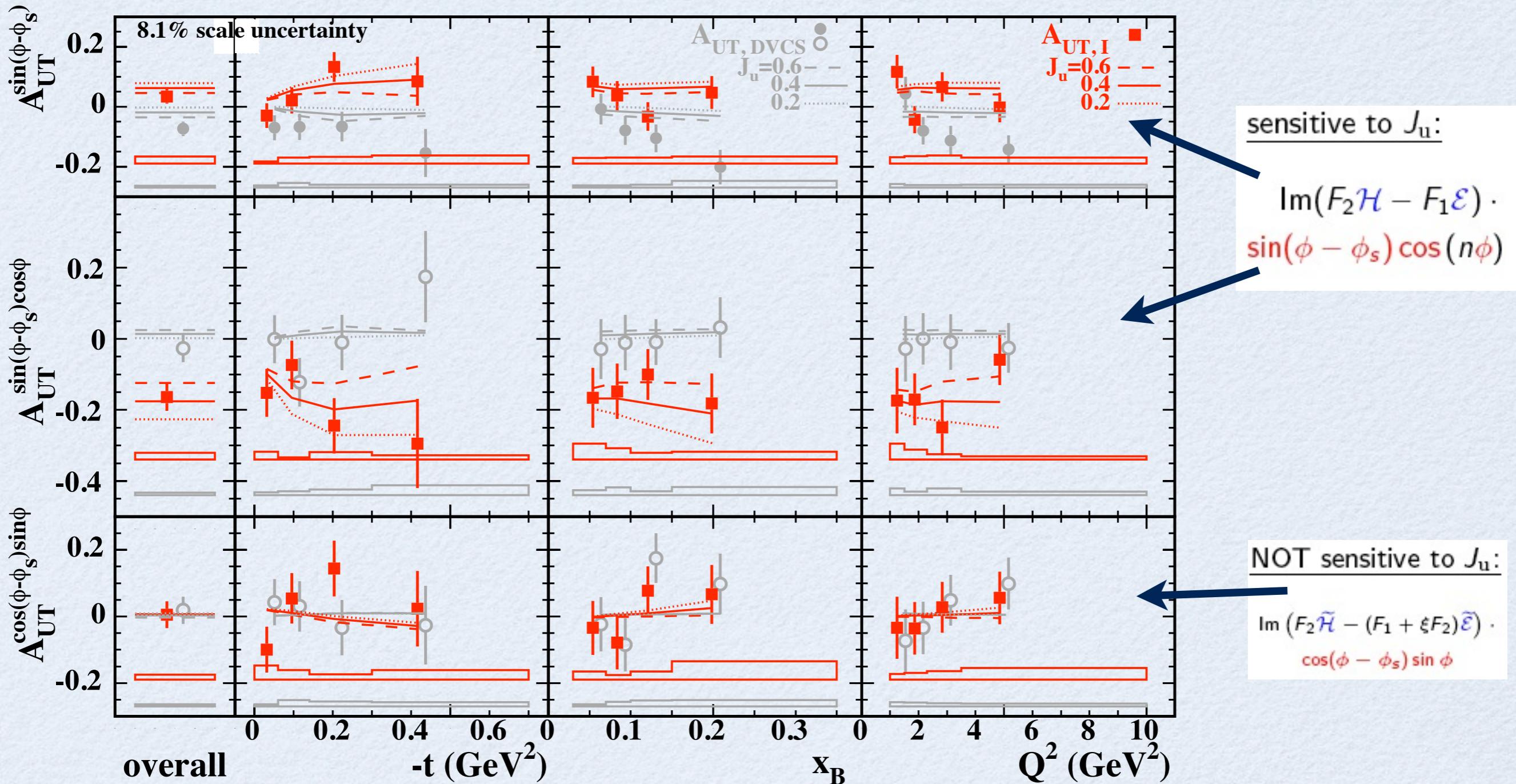
$$\mathcal{A}_{\text{UT}}^{\text{DVCS}}(\phi, \phi_s)$$

also sensitive to GPD E
(bilinear combination)

$$\mathcal{A}_{\text{UT}}^{\mathcal{T}}(\phi, \phi_s) \propto [d\sigma^+(\phi, \phi_s) - d\sigma^-(\phi, \phi_s)]^+ + [d\sigma^+(\phi, \phi_s + \pi) - d\sigma^-(\phi, \phi_s + \pi)]^-$$

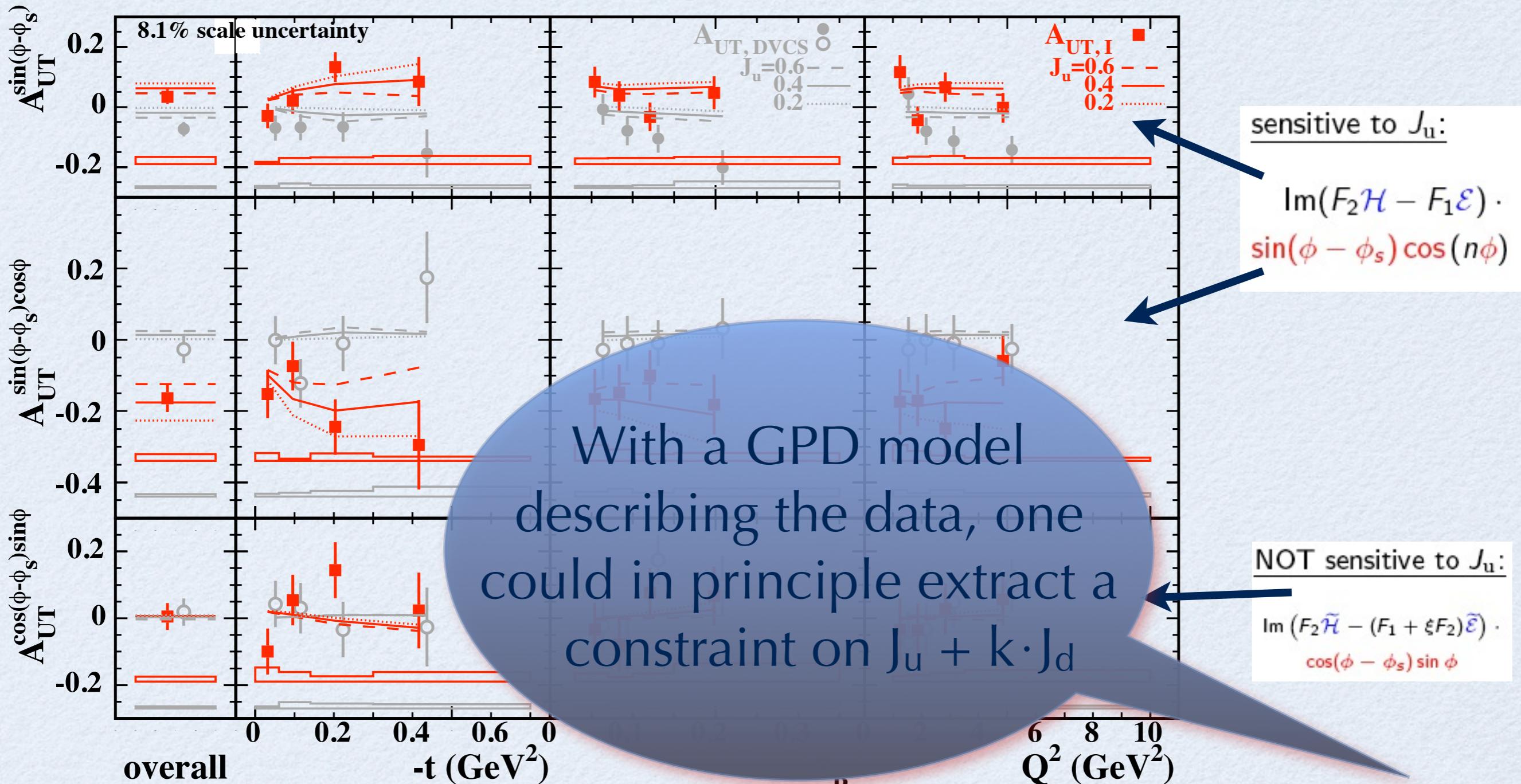
$$\begin{aligned} \mathcal{A}_{\text{UT}}^{\mathcal{T}}(\phi, \phi_s) &\propto \text{Im} (F_2 \mathcal{H} - F_1 \mathcal{E}) \sin(\phi - \phi_s) \cos \phi \\ &+ \text{Im} (F_2 \tilde{\mathcal{H}} - (F_1 + \xi F_2) \tilde{\mathcal{E}}) \cos(\phi - \phi_s) \sin \phi \end{aligned}$$

HERMES DVCS \mathcal{A}_{UT} Amplitudes



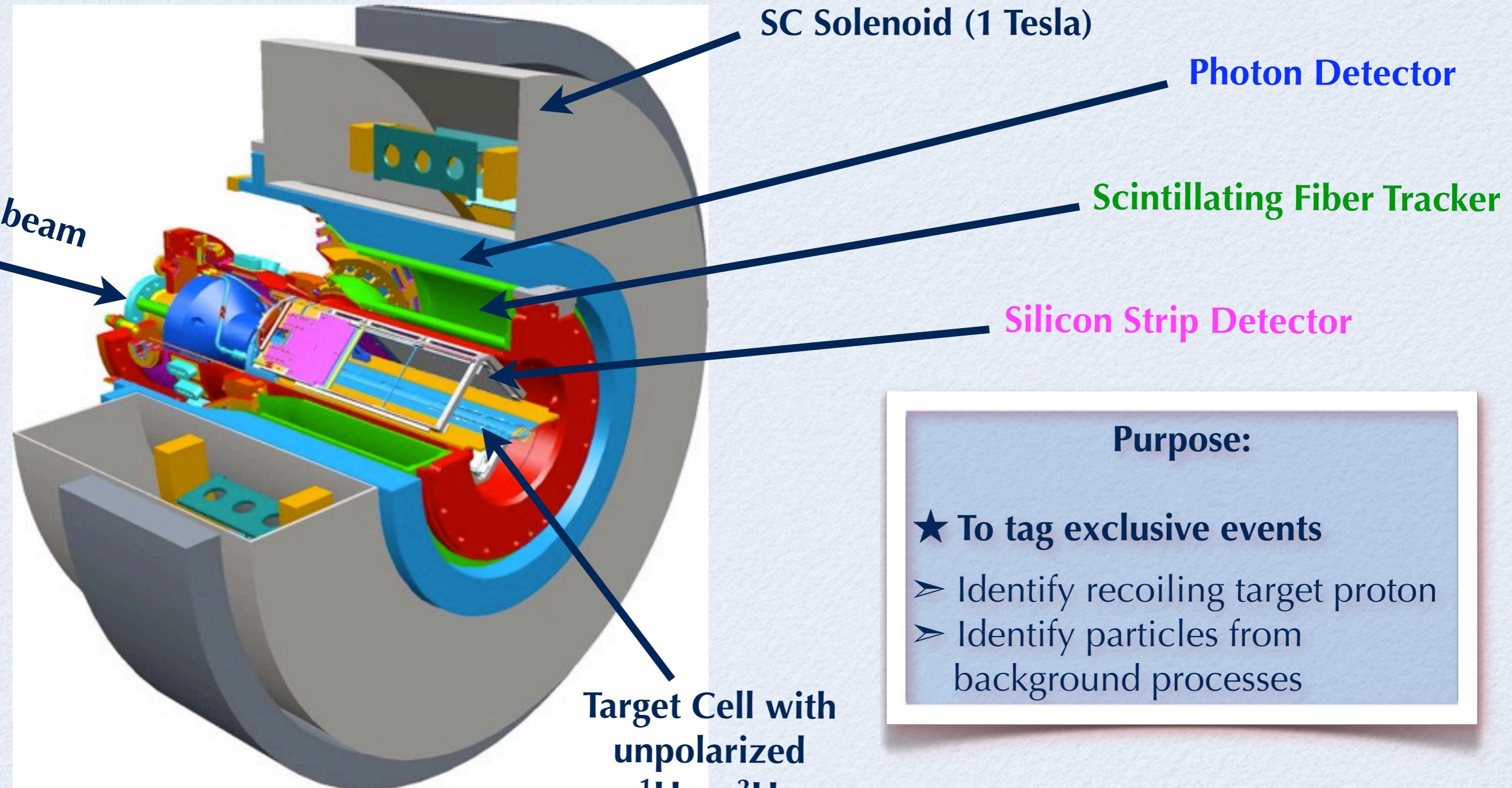
Model: VGG with variation of J_u , while $J_d=0$

HERMES DVCS \mathcal{A}_{UT} Amplitudes



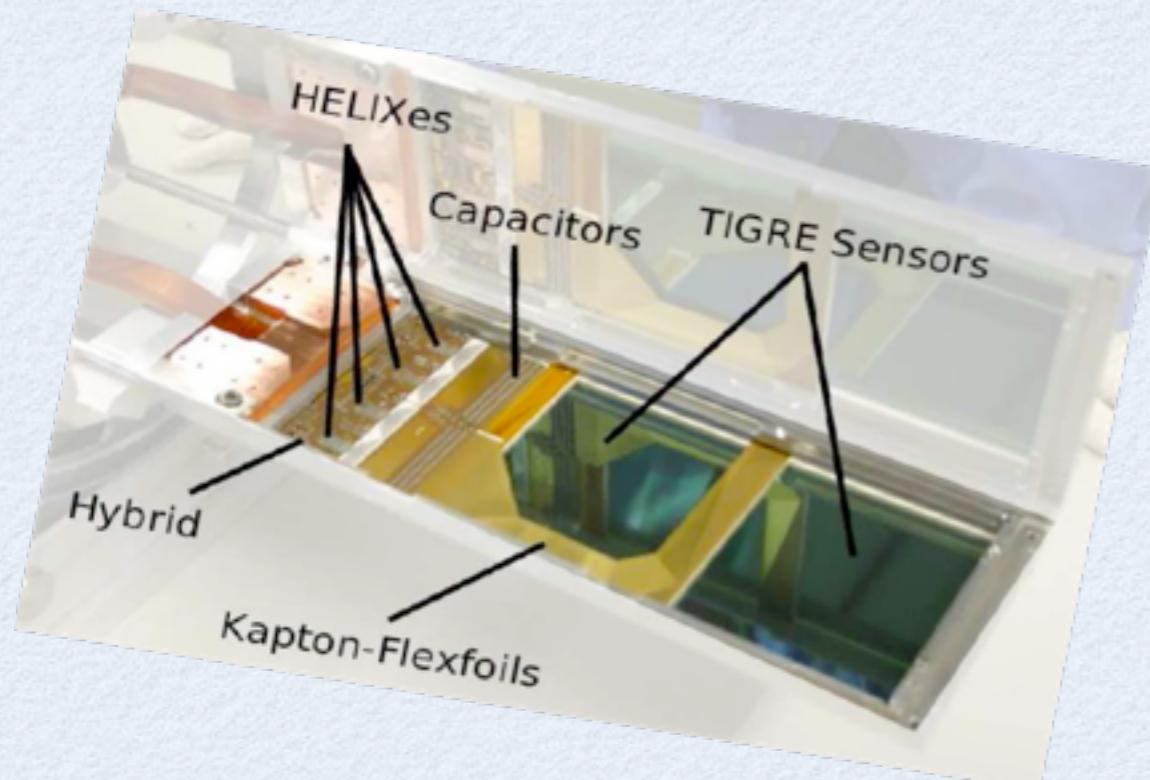
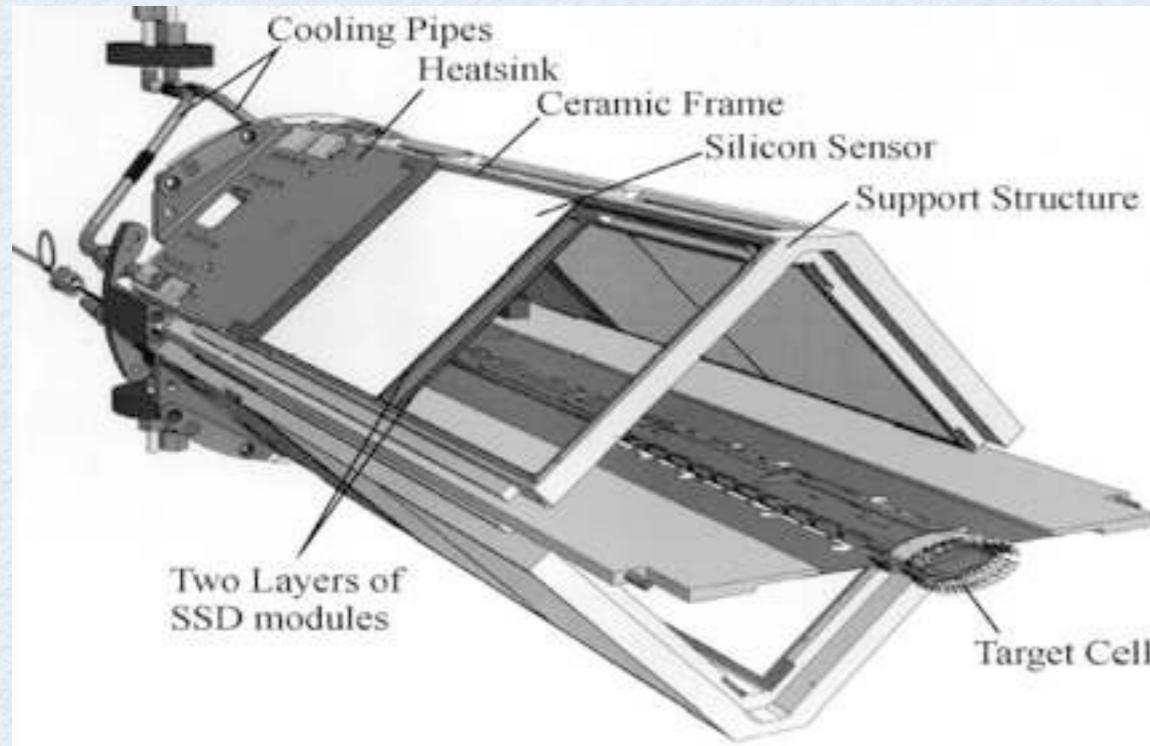
Model: VGG with variation of J_u , while $J_d=0$

HERMES 2006-2007: Recoil Detector



^1H (^2H): factor of 1.6 (0.5)
more than 1996-2005

The Silicon Strip Detector (SSD)

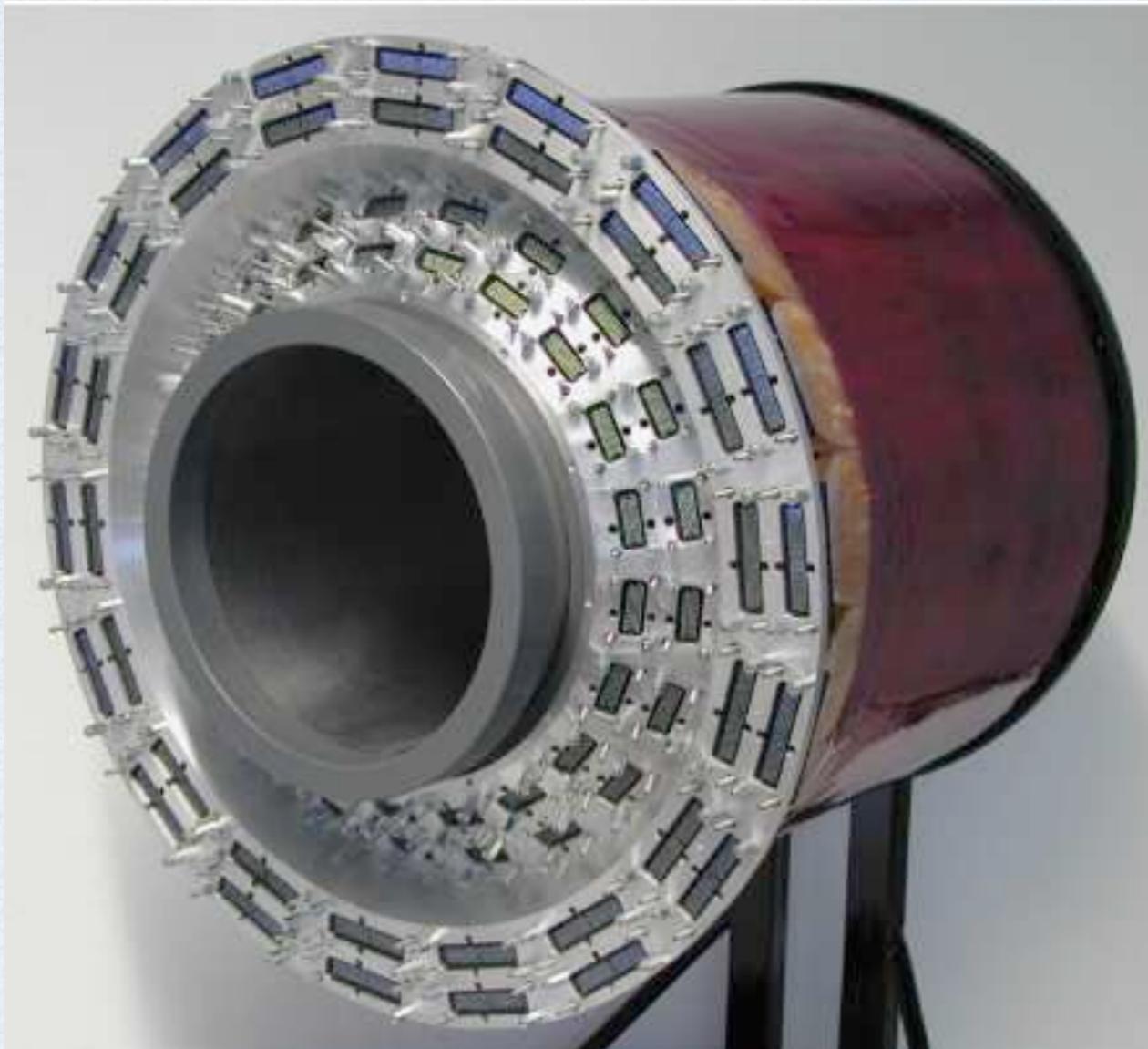


- Purpose:
 - ▶ Track reconstruction
 - ▶ Momenta: $> 125 \text{ MeV}/c$
 - ▶ PID for low and medium momenta
- 2 layers of 16 double-sided sensors
 - ▶ $(10 \text{ cm} \times 10 \text{ cm})$ active area
 - ▶ $300 \mu\text{m}$ thickness
- Inside accelerator vacuum,
5 cm close to electron beam

$E_{\text{kin}} \approx 8 \text{ MeV}$
for protons

to reach as low t as possible

The Scintillating Fiber Tracker (SFT)



- Purpose:
 - ▶ Track reconstruction
 - ▶ Momenta: 250-1400 MeV/c (protons)
 - ▶ PID for medium and high momenta
- 2 Barrels with each 4 layers of scintillating fibers
- Per Barrel:
 - ▶ 2 parallel layers
 - ▶ 2 stereo-layers
 - ▶ Stereo angle: 10°



The Photon Detector (PD)

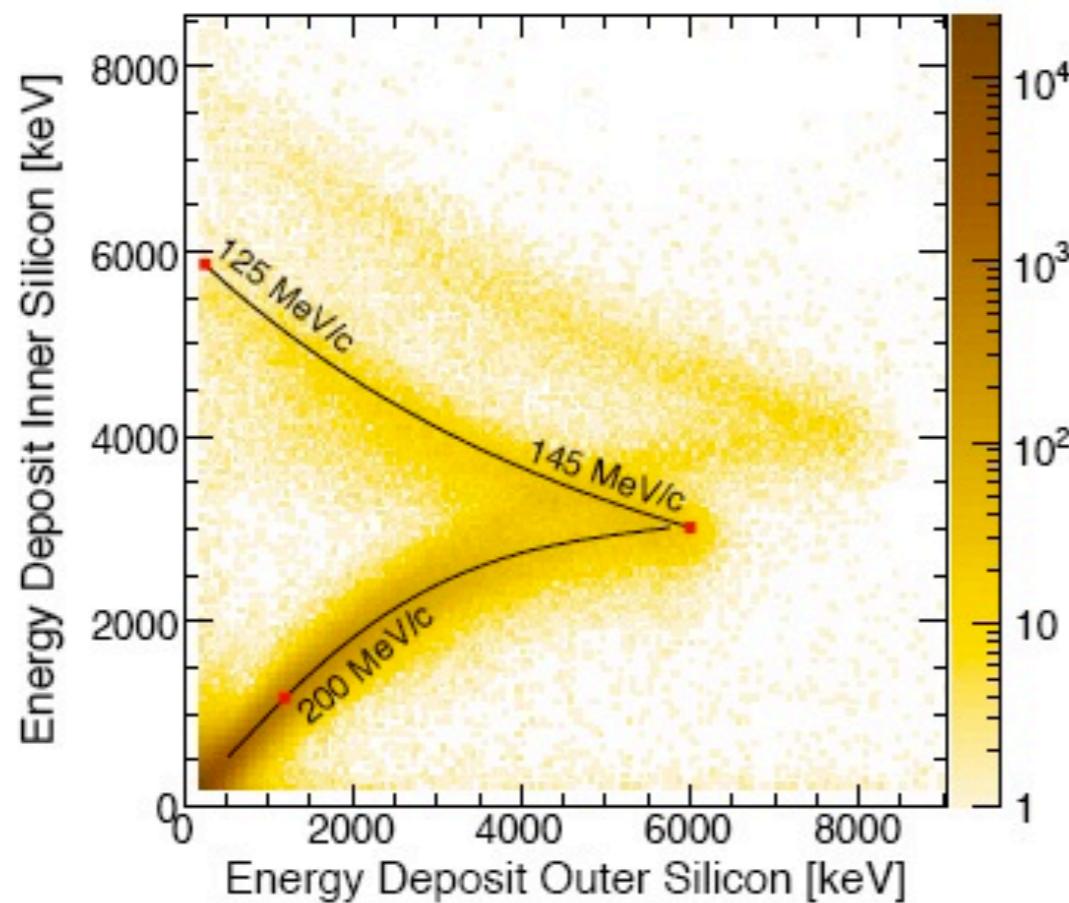


- Purpose:
 - ▶ Detection of photons from resonance decay $\Delta^+ \rightarrow p\pi^0$
 - ▶ PID for $p > 600$ MeV/c
- 3 layers of tungsten/scintillator sandwich
 - ▶ 1 layer parallel to beam axis
 - ▶ 2 layers under $+45^\circ/-45^\circ$ angles

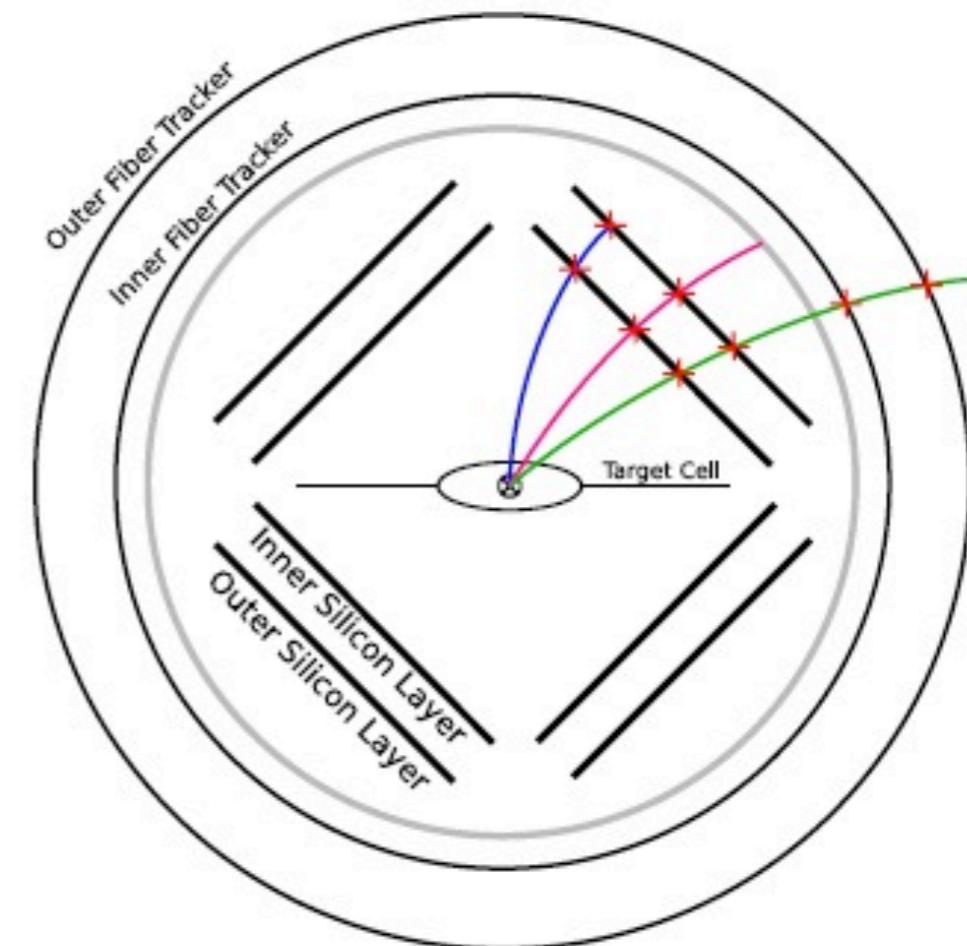


Tracking with the Recoil Detector

Energy Deposit in the SSD



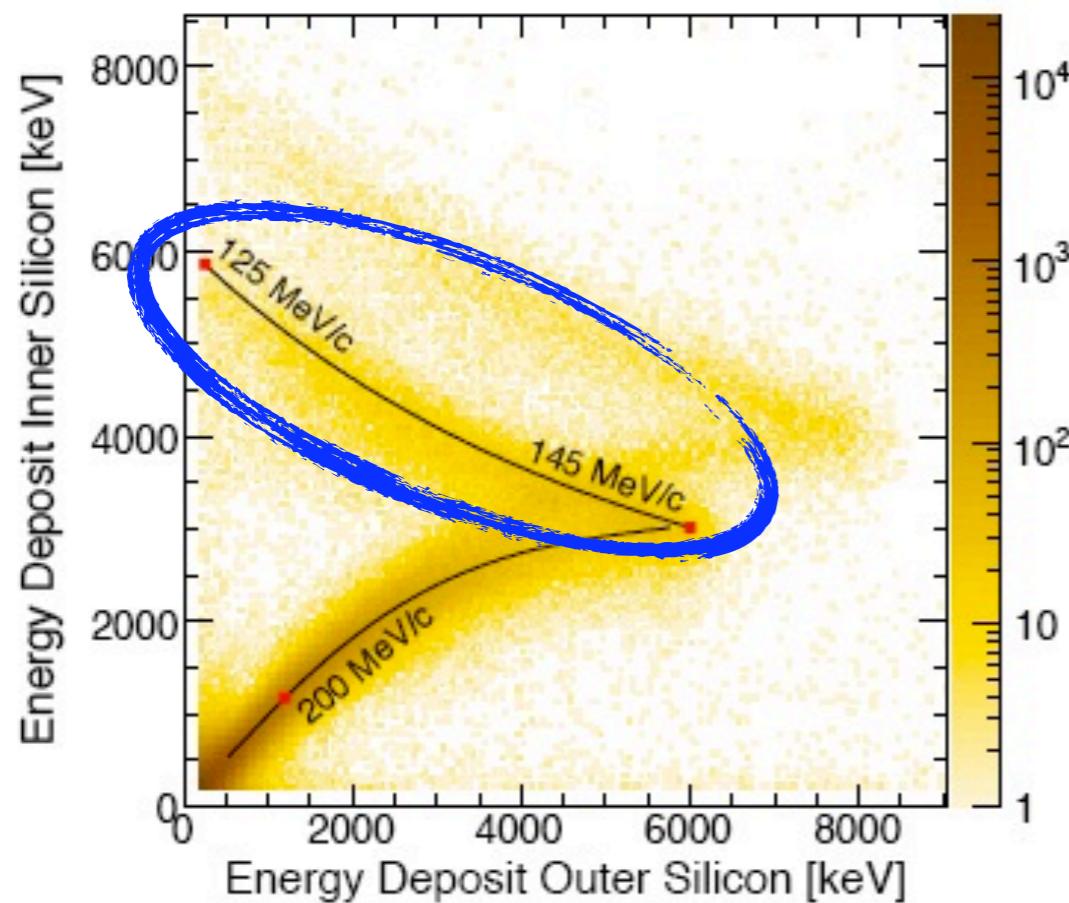
Transverse View of Detector



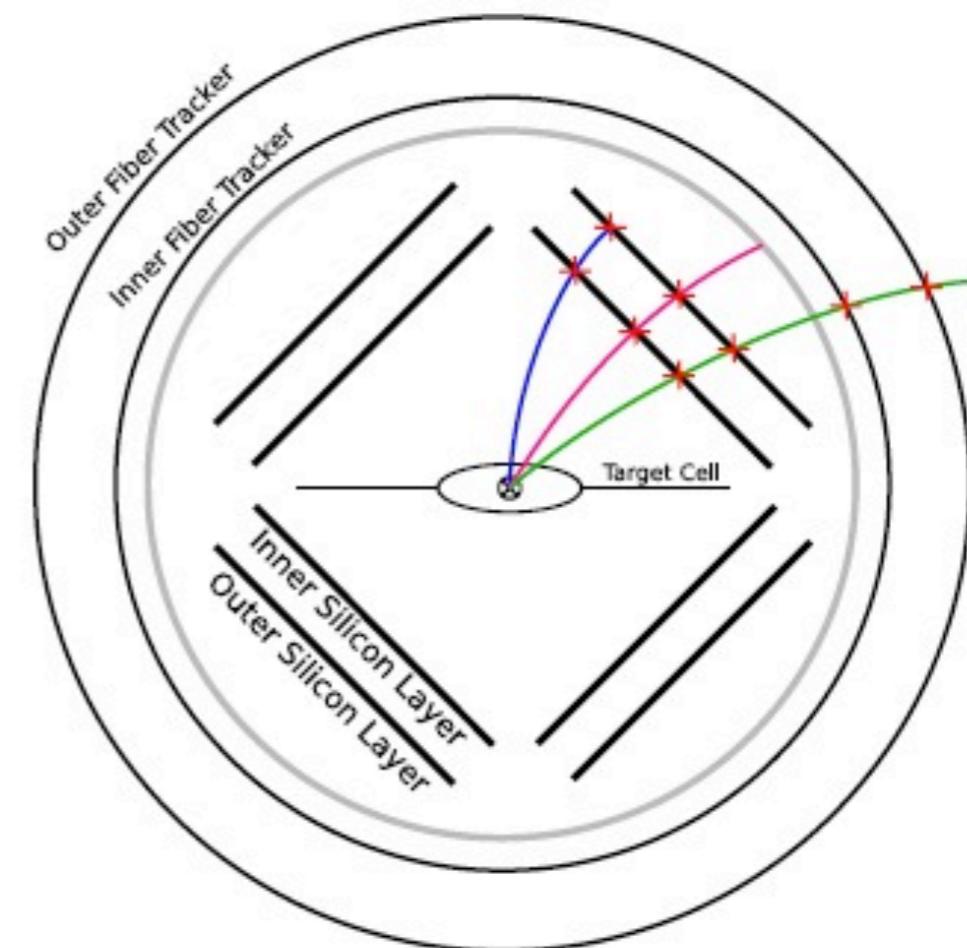
- **Low-energy protons:** momentum $\propto (\sum_i \Delta E_i)^{-1}$
- **Medium-energy protons:** momentum $\propto (\frac{dE}{dx})^{-1}$ (Bethe-Bloch)
- **Higher-energy particles (protons/pions):** momentum $\propto eB\rho$

Tracking with the Recoil Detector

Energy Deposit in the SSD



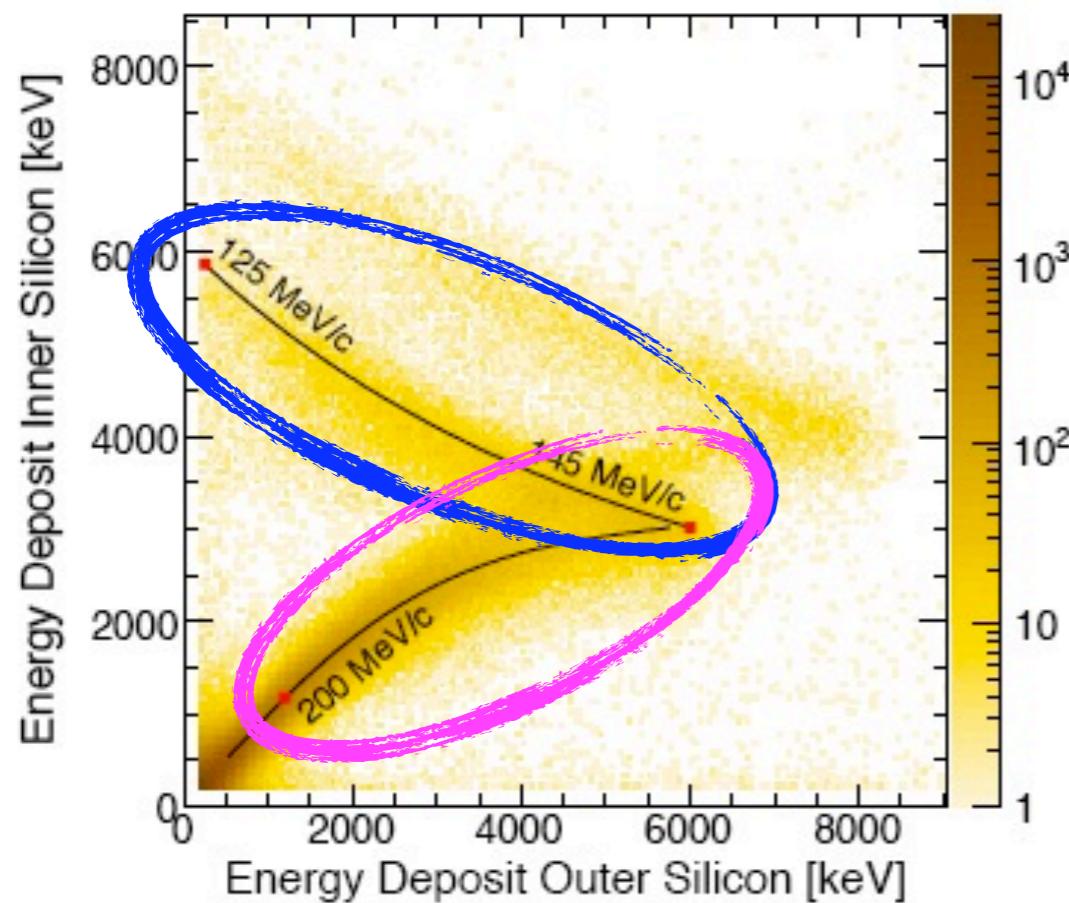
Transverse View of Detector



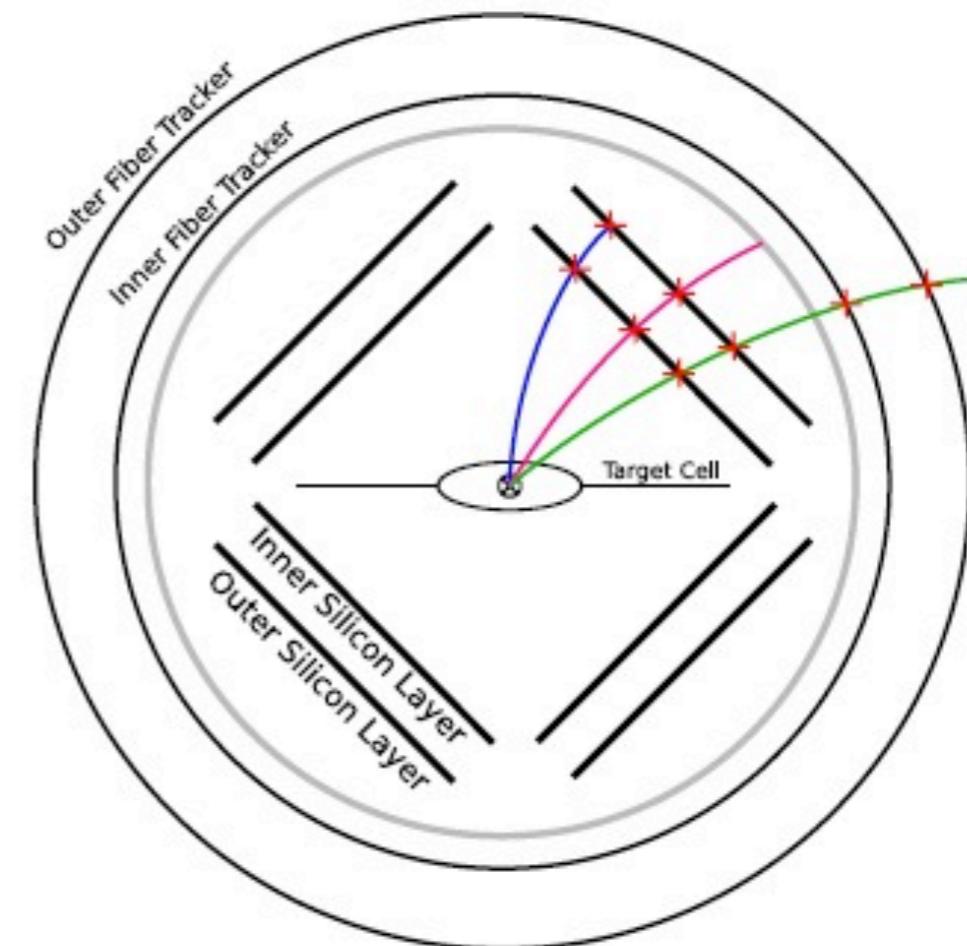
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Tracking with the Recoil Detector

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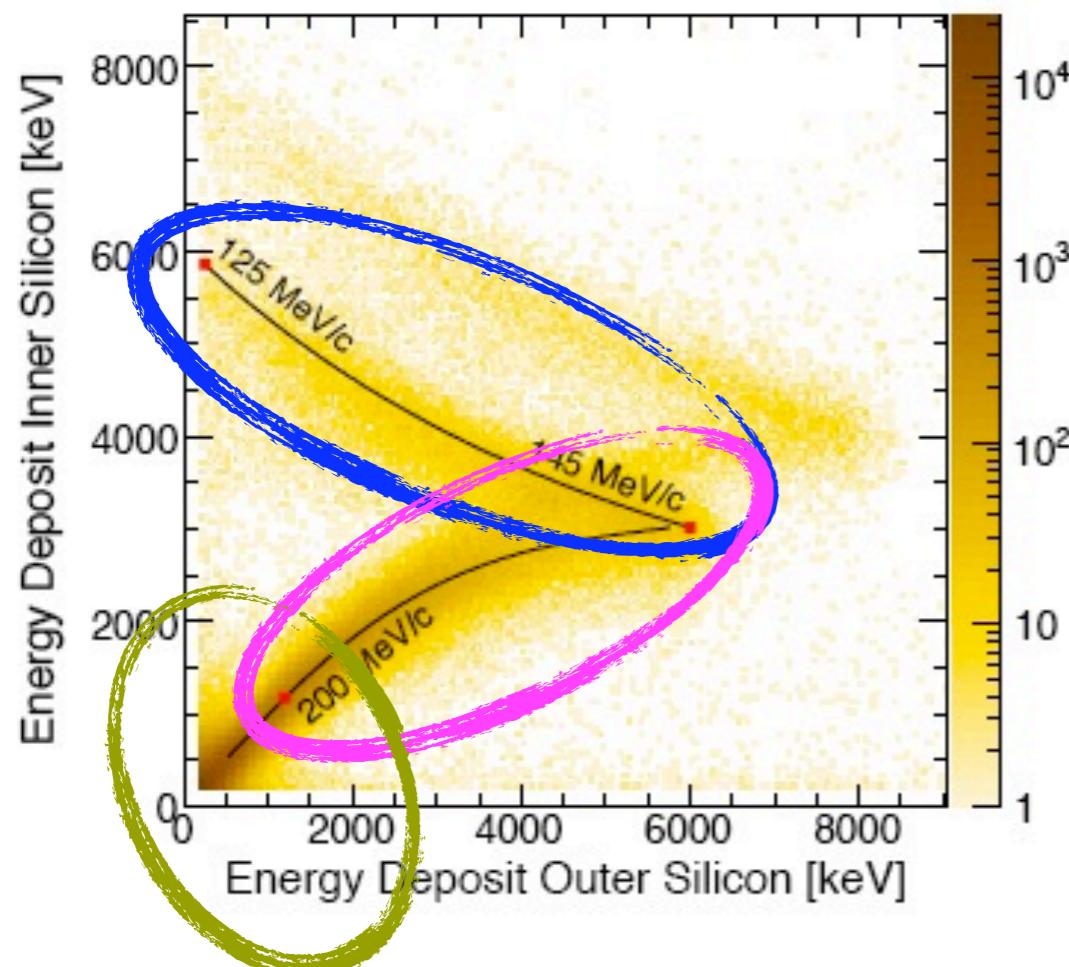
Transverse View of Detector



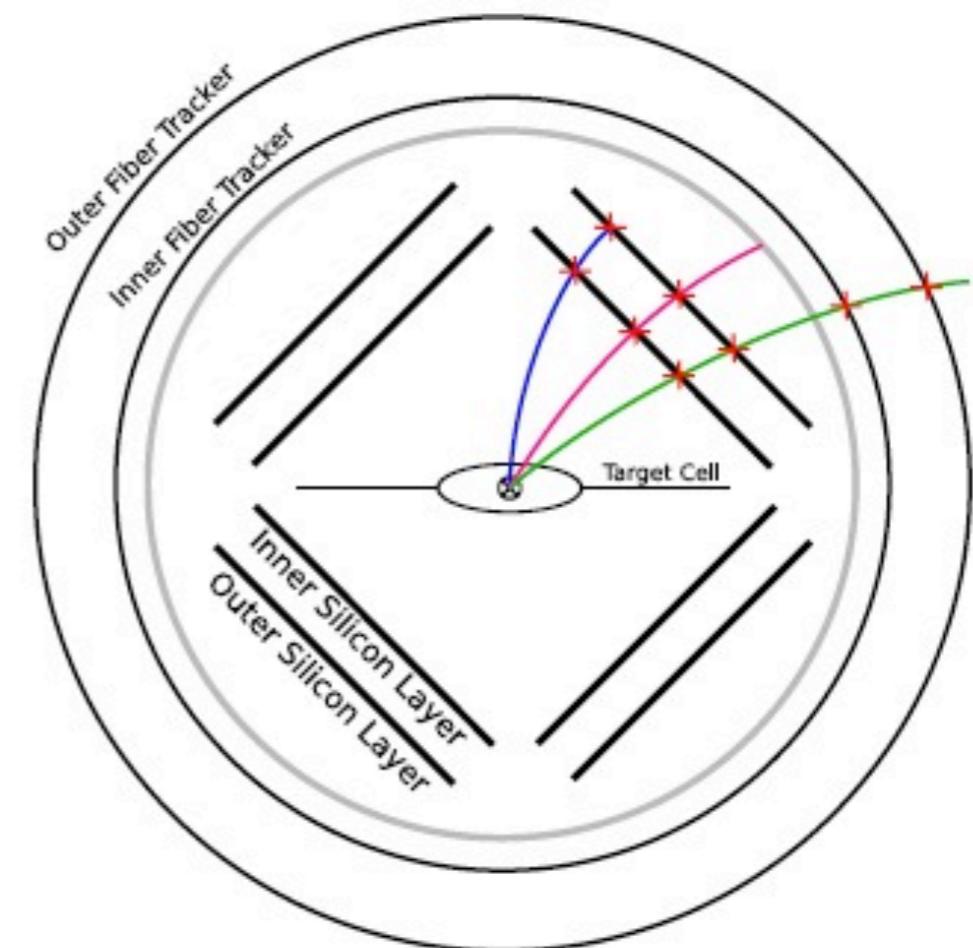
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Tracking with the Recoil Detector

Energy Deposit in the SSD

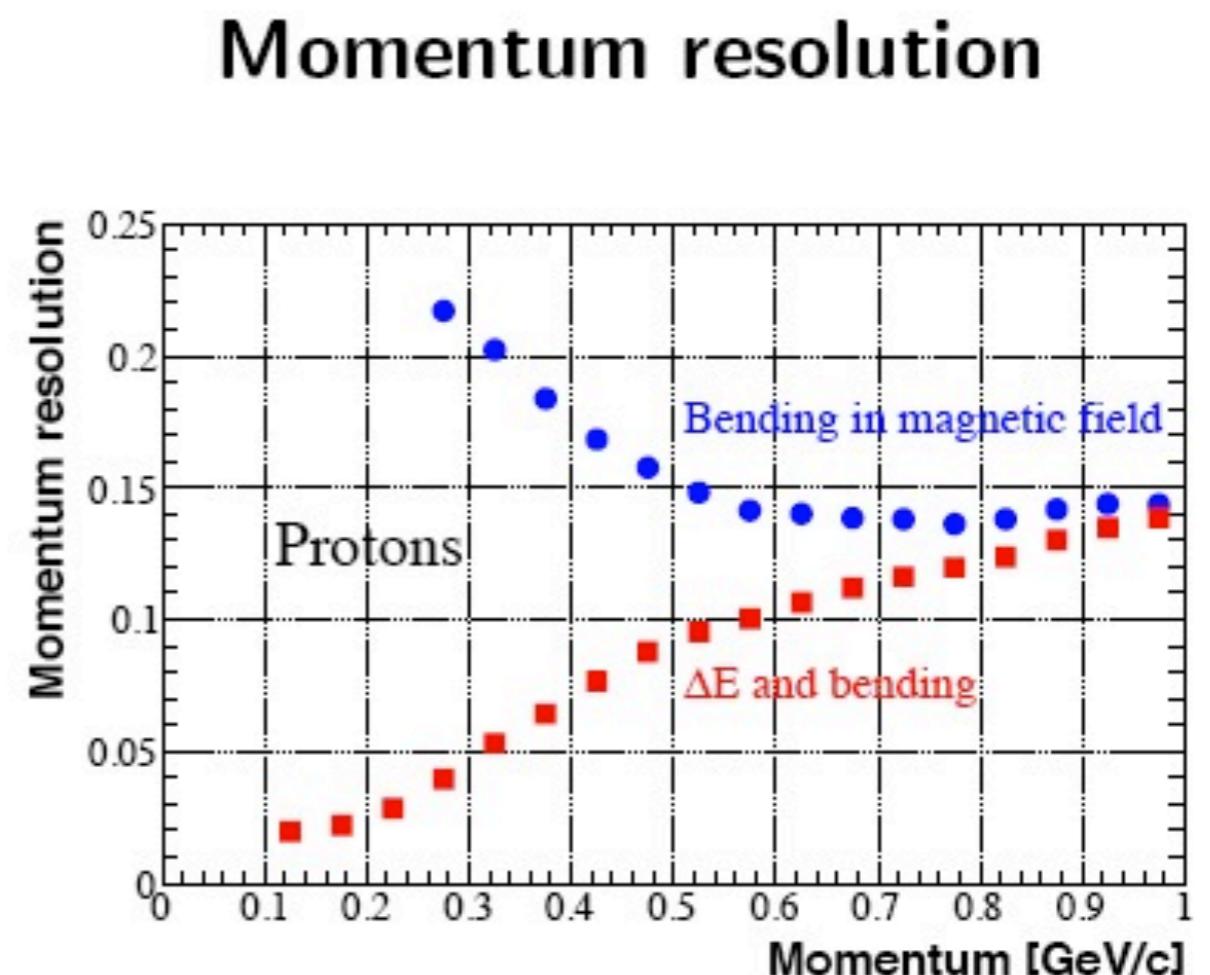
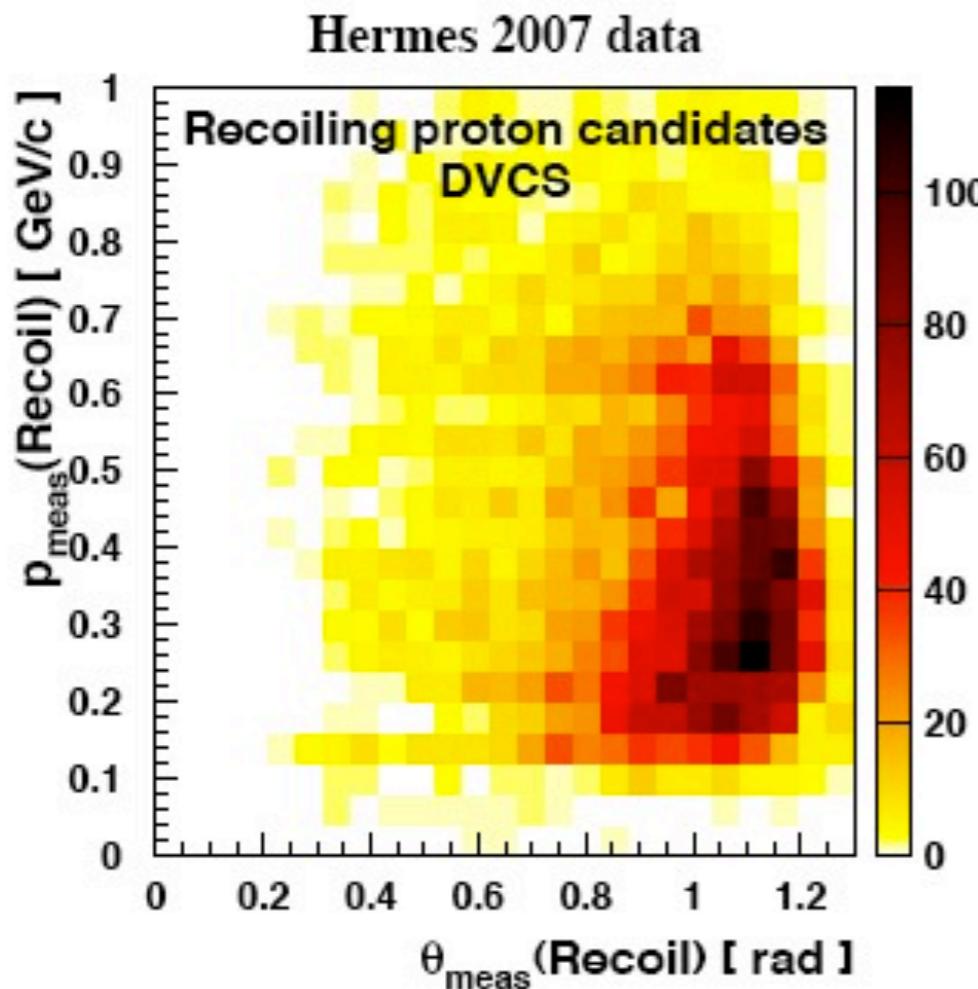


Transverse View of Detector



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Reconstructed Momenta and Angles

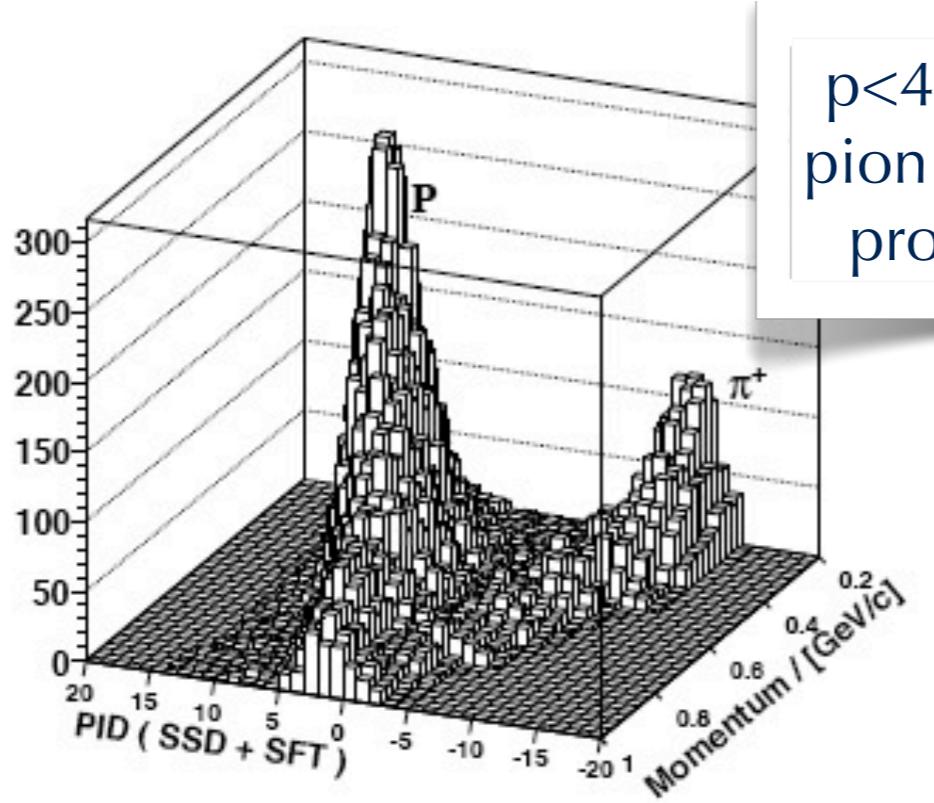


- Recoiling target protons
 - ▶ Large θ -angles $\lesssim 90^\circ$
 - ▶ Small momenta $< 1 \text{ GeV}/c$
- Azimuthal ϕ coverage: 76%
- ΔE accounted for in track fitting
 $\Rightarrow \Delta p/p$ improvement

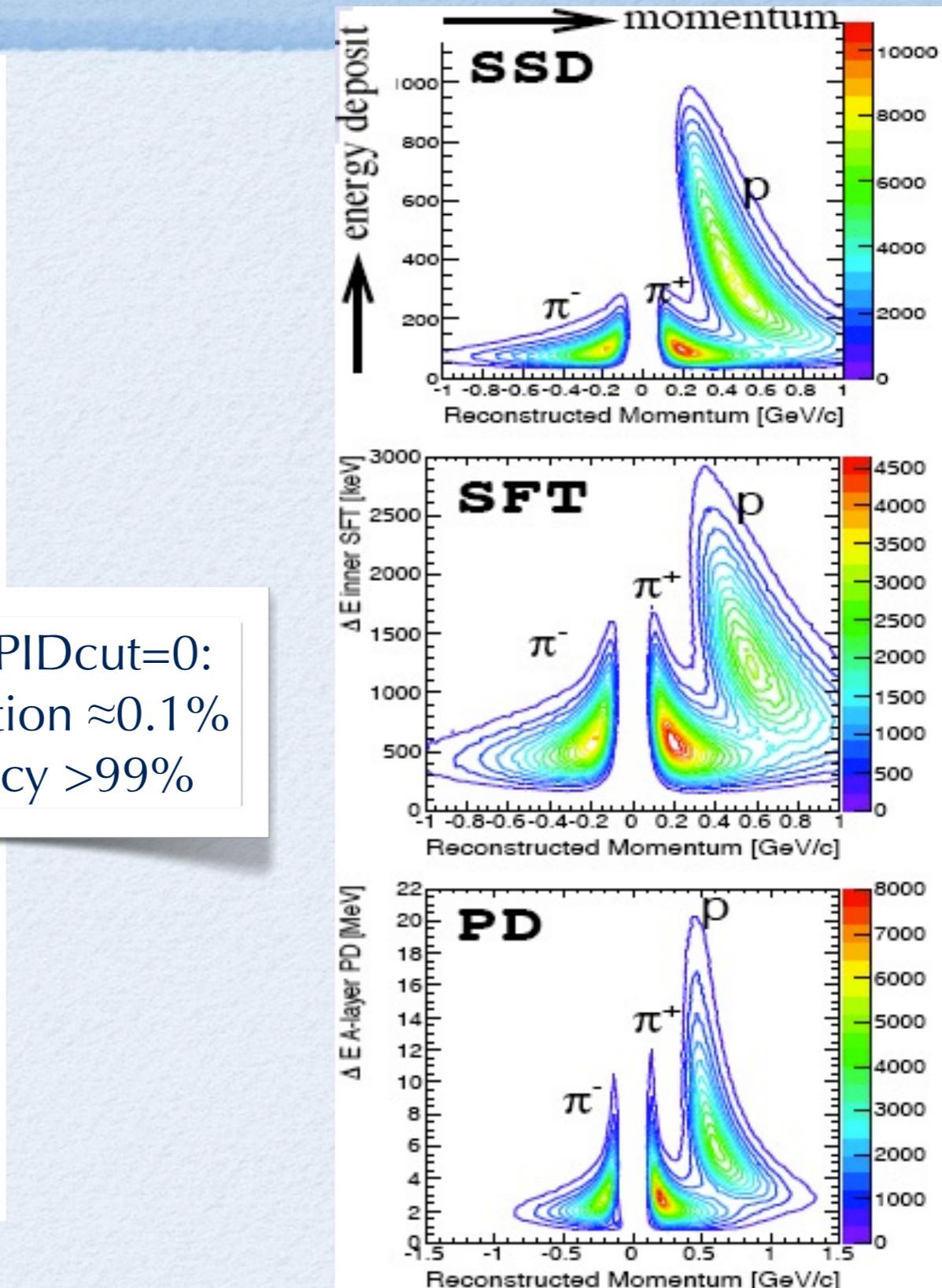
Proton / Pion Separation with the Recoil

- $p < 600 \text{ MeV}/c$: SSD + SFT (6 layers)
- $p > 600 \text{ MeV}/c$: include PD
- Log-likelihood formalism:

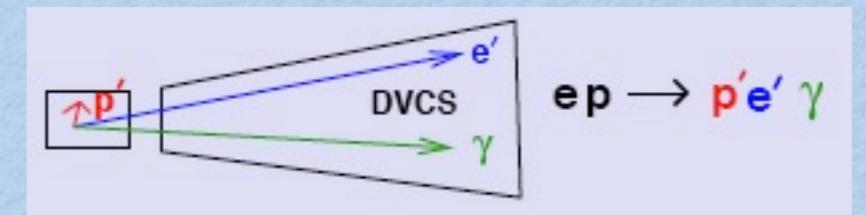
$$\text{PID} \equiv \log \frac{\mathcal{P}(\Delta E|\text{proton}, p)}{\mathcal{P}(\Delta E|\text{pion}, p)}$$



$p < 450 \text{ MeV}/c$, $\text{PIDcut}=0$:
pion contamination $\approx 0.1\%$
proton efficiency $> 99\%$

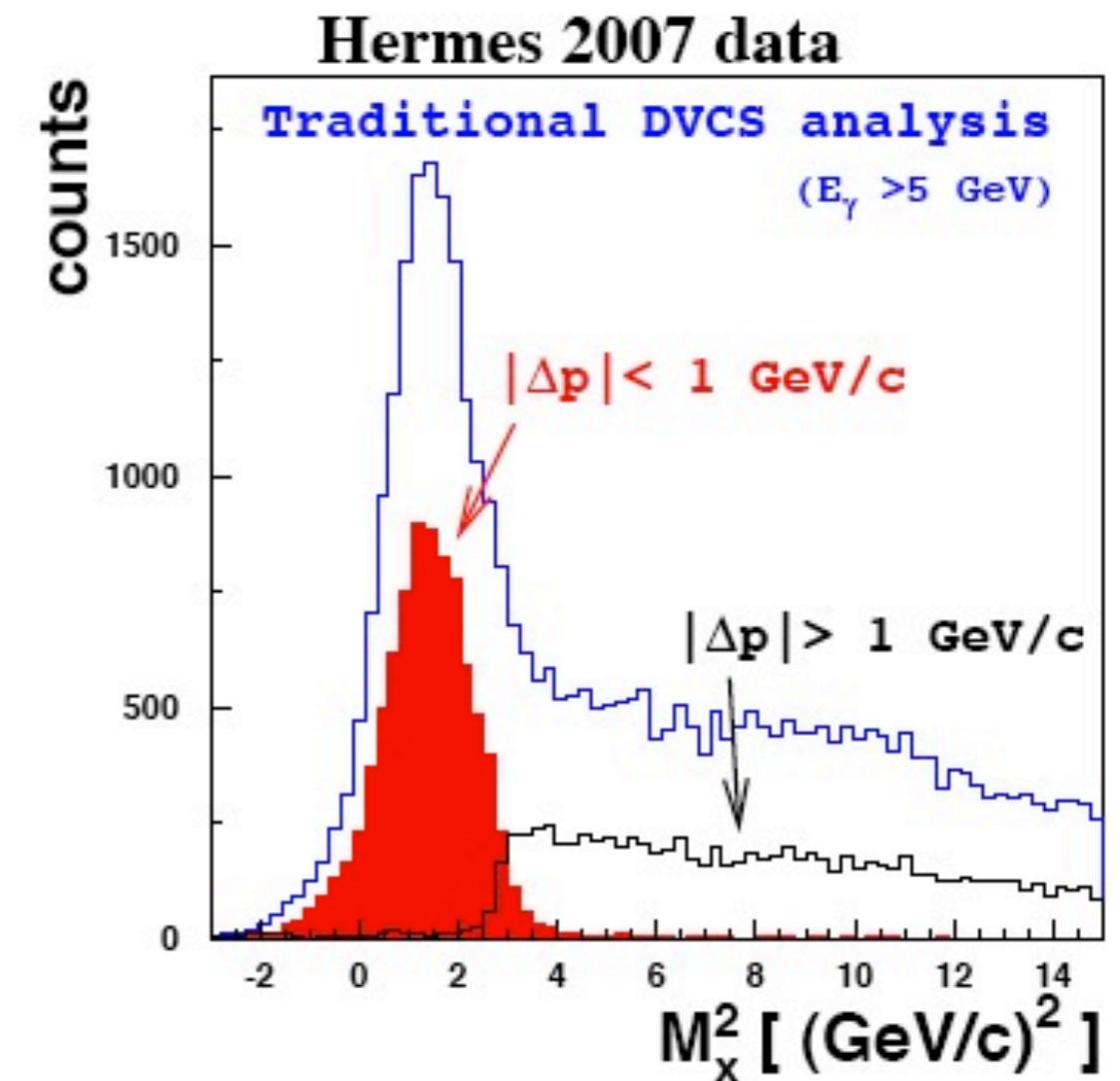
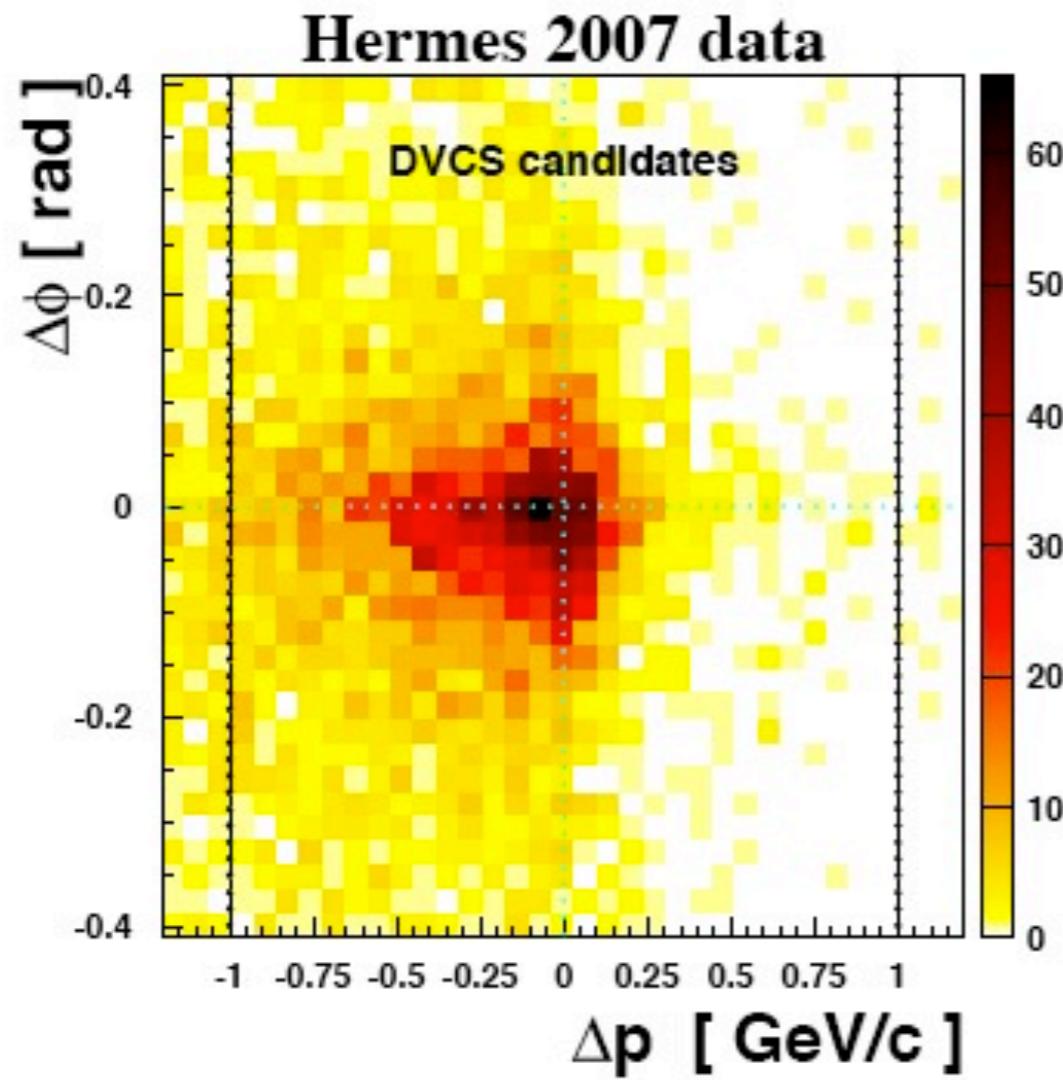


DVCS and the Recoil



- Missing ϕ : $\Delta\phi = \phi_{\text{meas}} - \phi_{\text{calc}}$
- Missing p : $\Delta p = p_{\text{meas}} - p_{\text{calc}}$

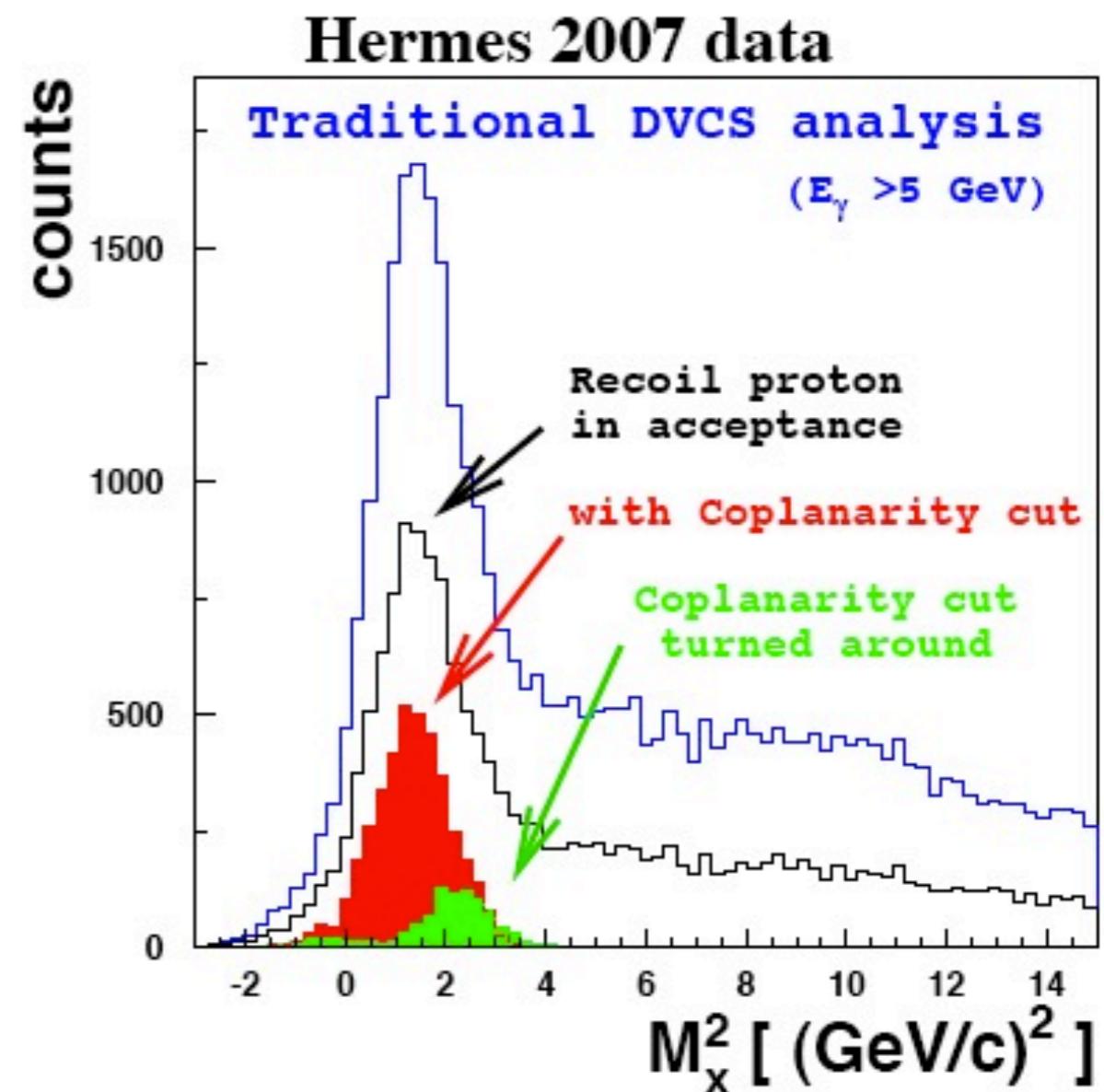
Missing Mass ($\approx M_P^2$):
 $M_X^2 = (p + p_{\gamma^*} - p_\gamma)^2$



Separation of Resonant States in DVCS

DVCS / Bethe Heitler

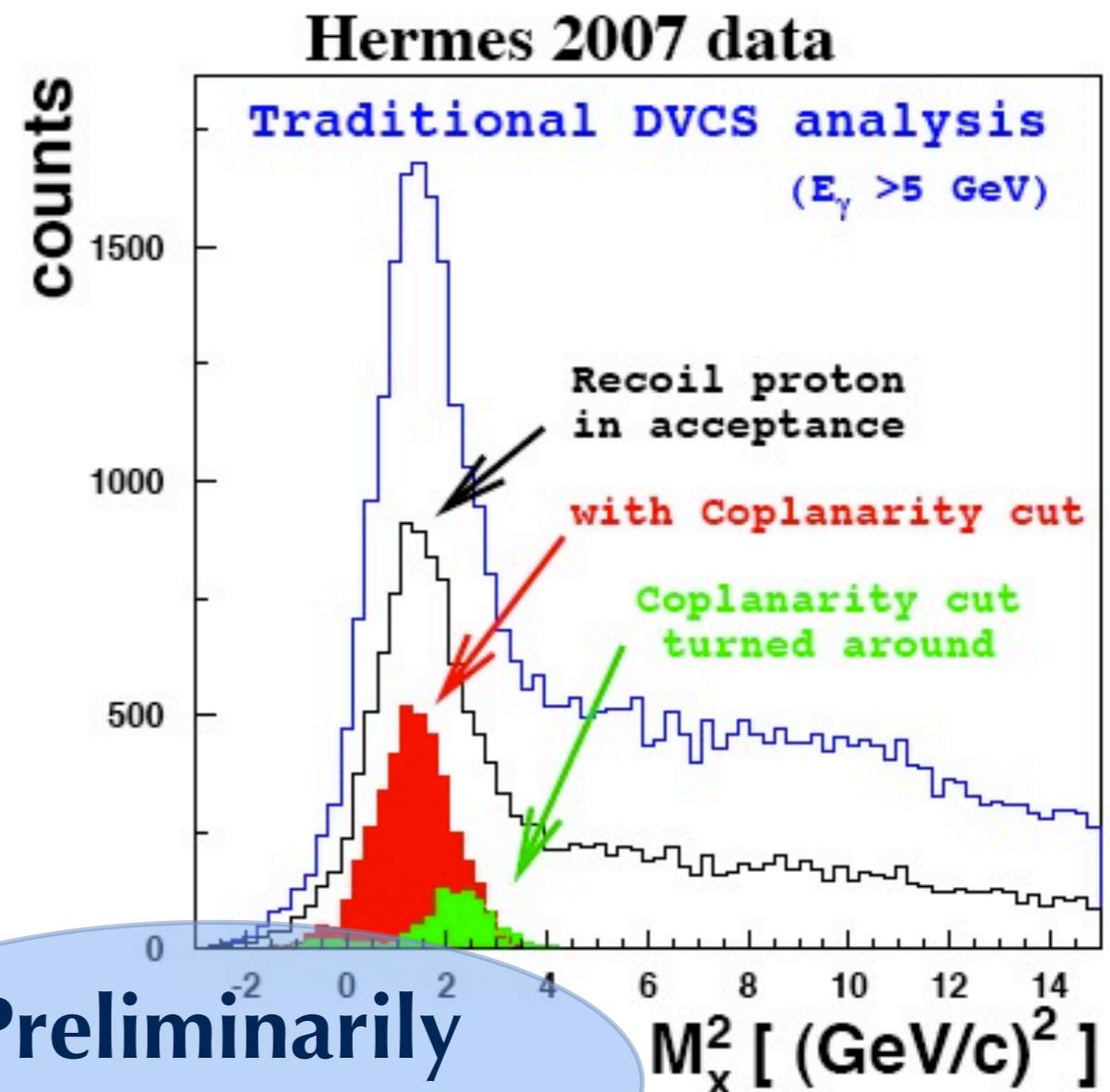
- Elastic:
 - ▶ $ep \rightarrow ep\gamma$
- Resonant ('associated'):
 - ▶ $ep \rightarrow e\Delta^+\gamma$
 $\Delta^+ \rightarrow \begin{cases} n\pi^+, 1/3 \\ p\pi^0, 2/3 \end{cases}$
 - ▶ 12% of signal
- Presence of $\pi^0 \Rightarrow$ proton fails coplanarity cut
 - ▶ Select elastic:
 - ★ $|\Delta\phi| < 0.1 \text{ rad}$
 - ★ $|p_T^{\text{calc}}| / |p_T^{\text{meas}}| = 0.5 \div 1.5$
 - ▶ Select resonant:
 - ★ $|\Delta\phi| > 0.35 \text{ rad}$



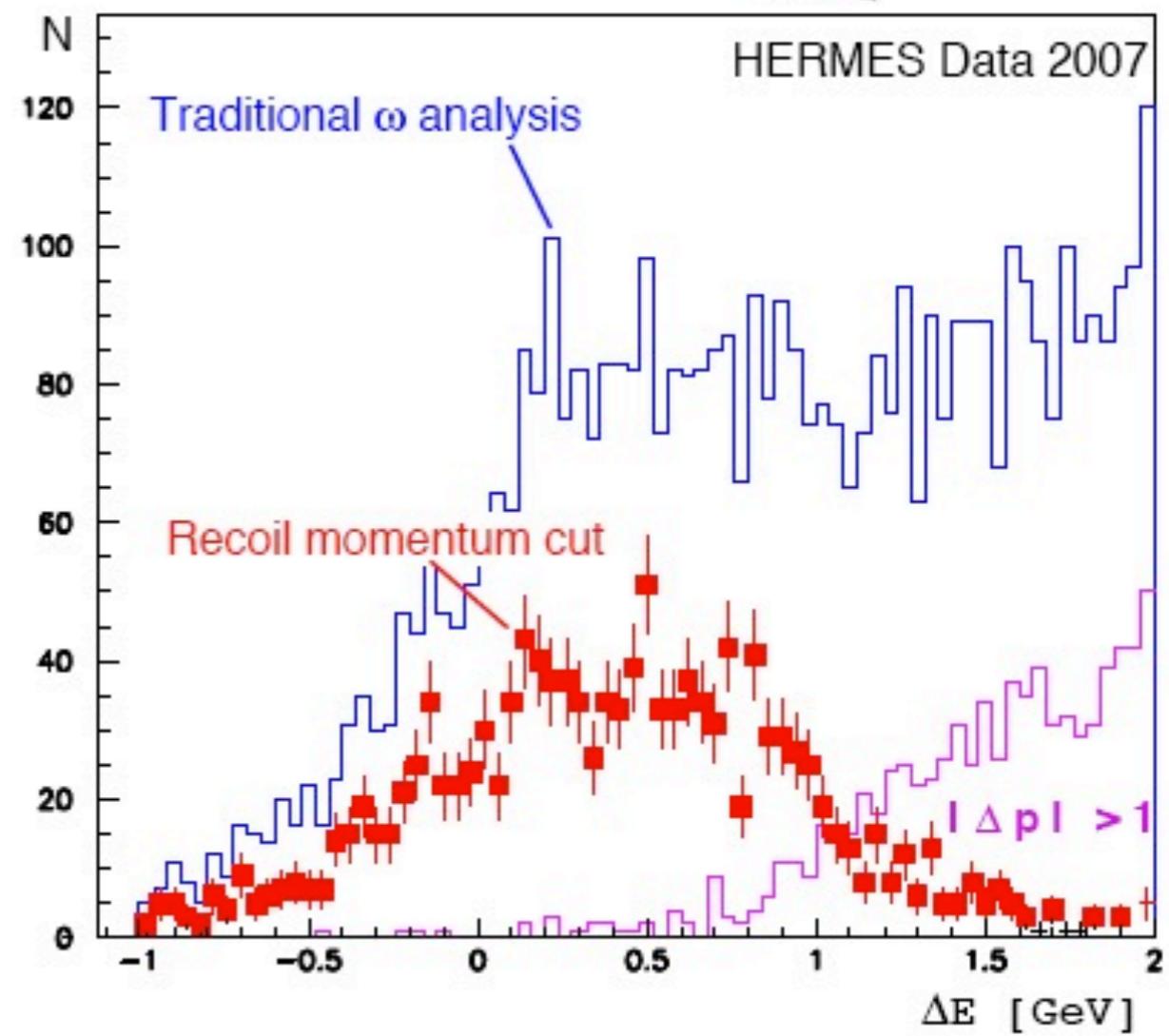
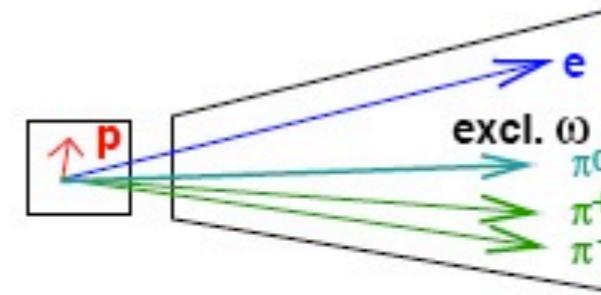
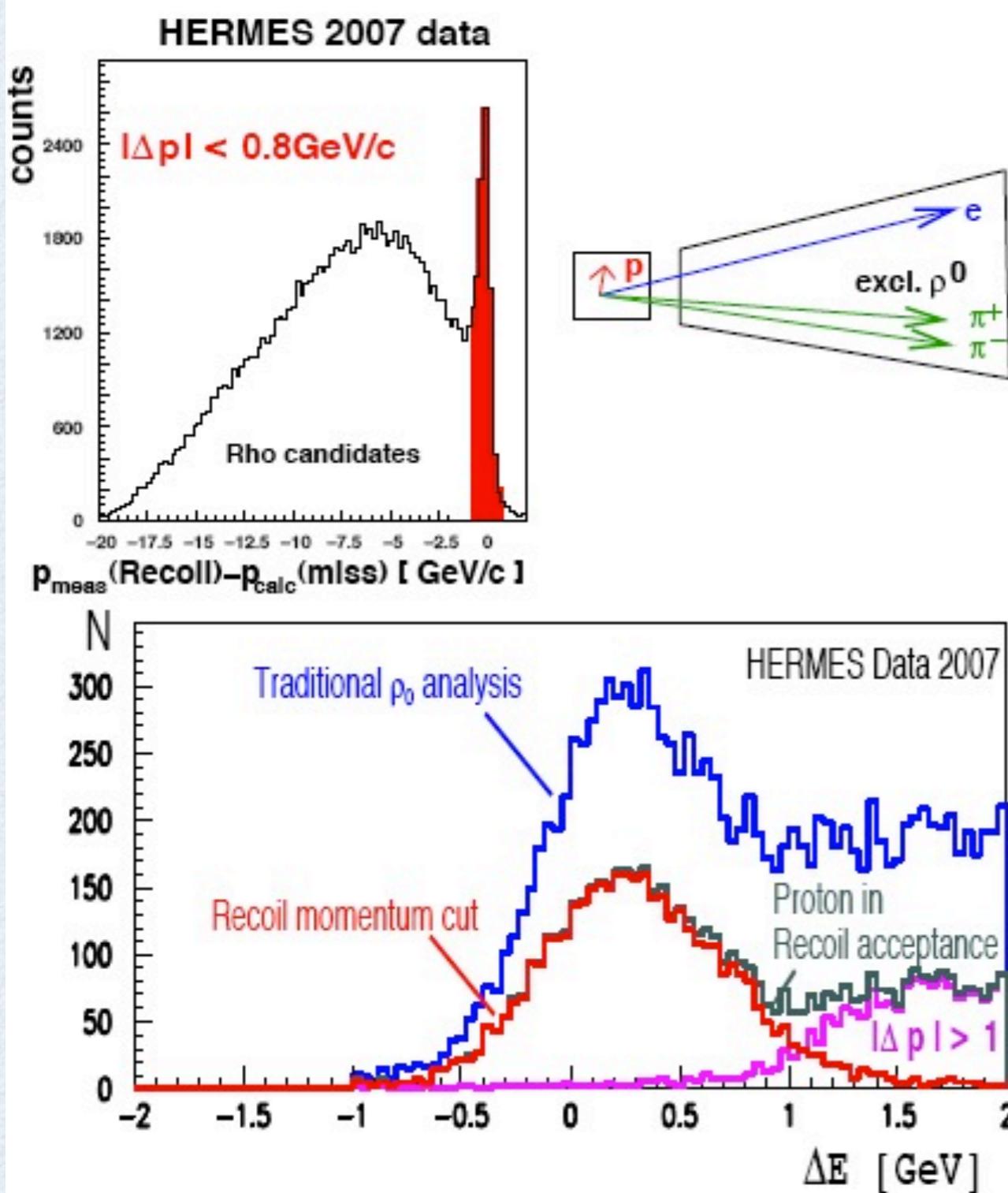
Separation of Resonant States in DVCS

DVCS / Bethe Heitler

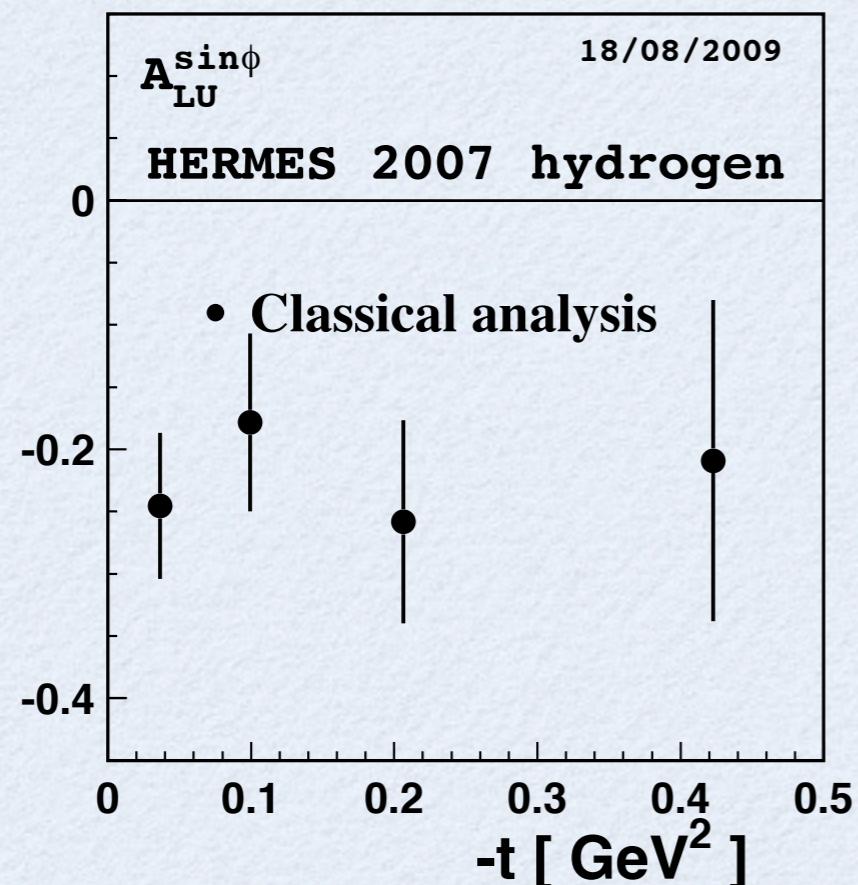
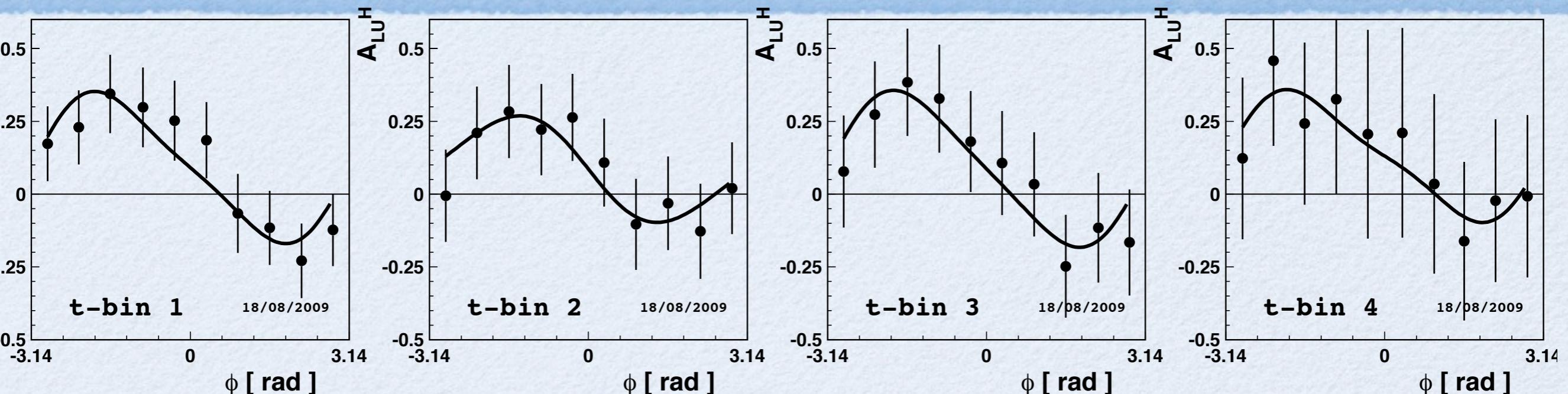
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Exclusive Mesons and the Recoil



DVCS Beam Helicity Asymmetry with Recoil

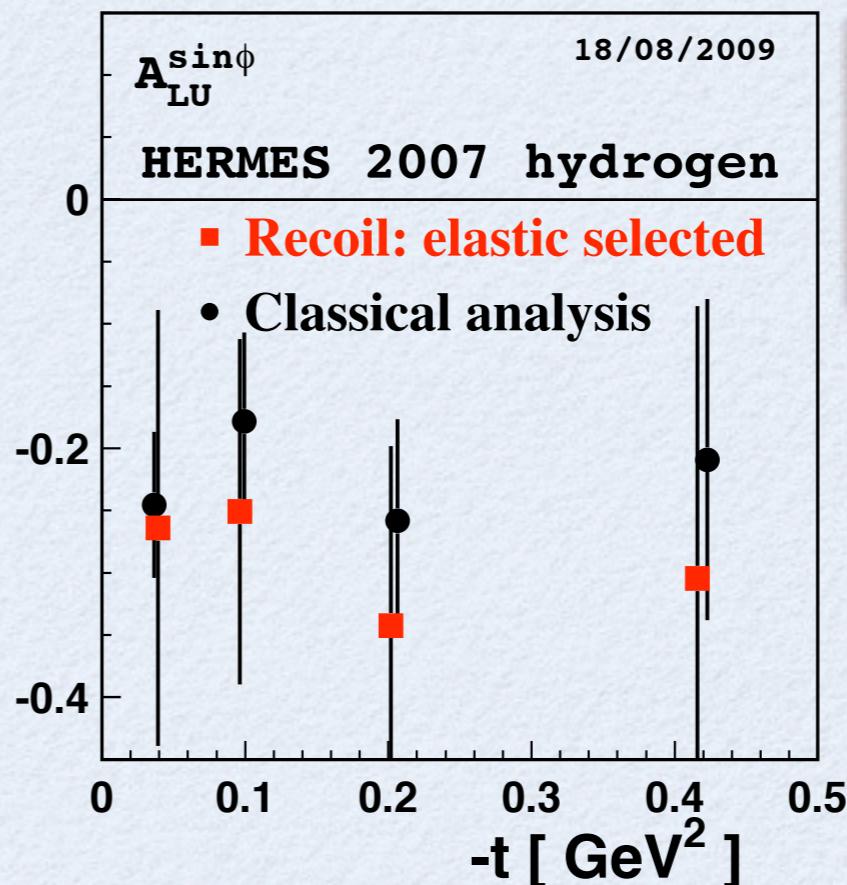
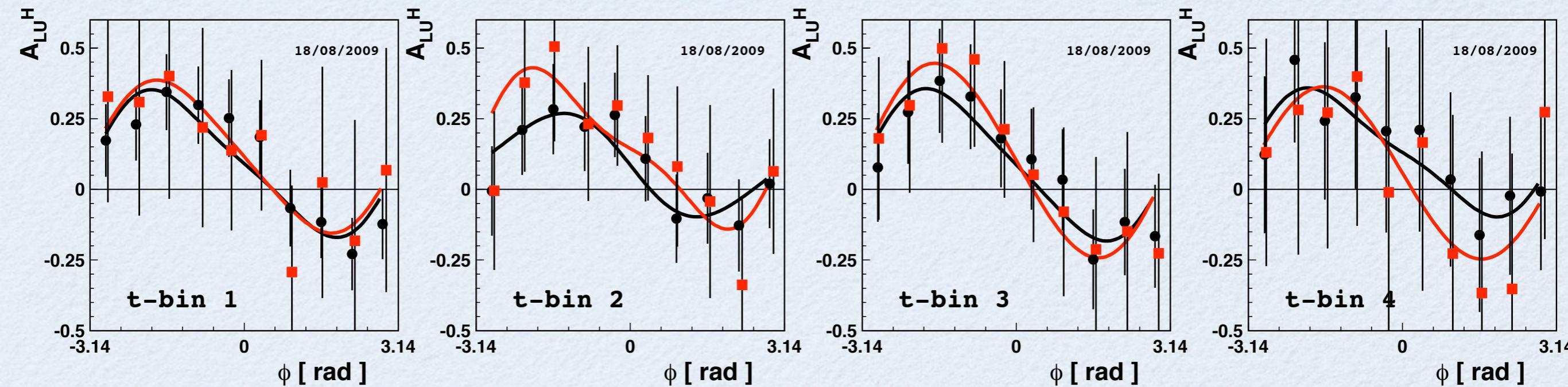


Pre-preliminary,
private analysis

DVCS Beam Helicity Asymmetry with Recoil

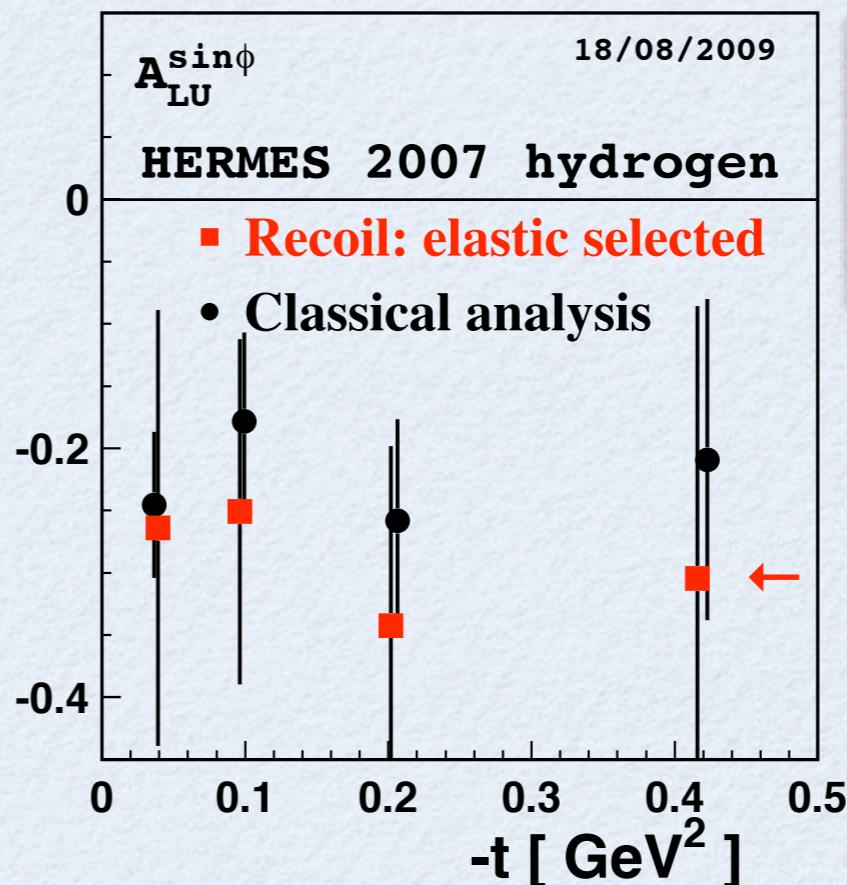
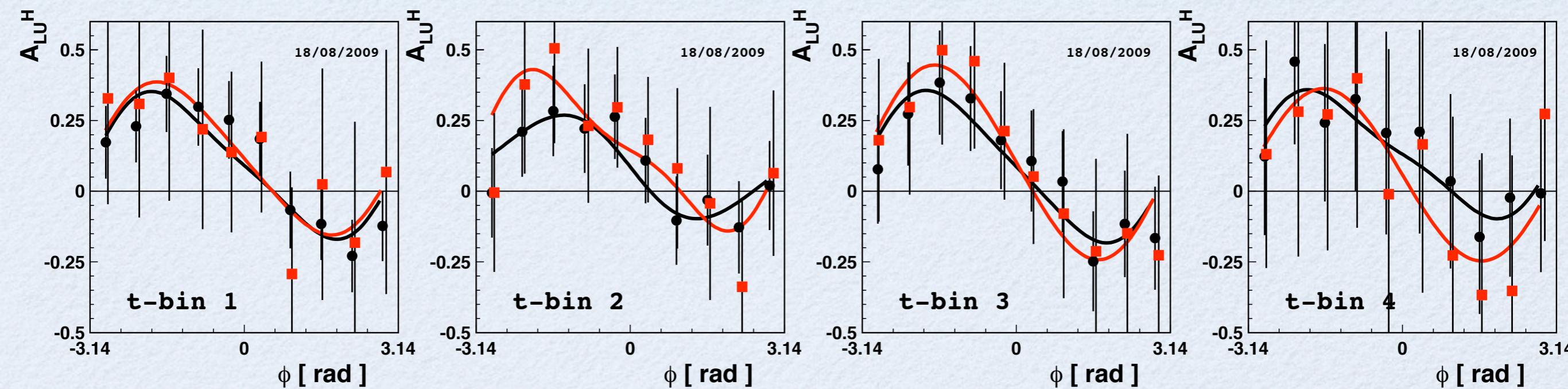
Pre-preliminary,
private analysis

DVCS Beam Helicity Asymmetry with Recoil



Pre-preliminary,
private analysis

DVCS Beam Helicity Asymmetry with Recoil



Pre-preliminary,
private analysis

Elastic fraction: >95 %

Summary

- * Generalized Parton Distributions
 - * Give glimpse of three-dimensional structure of nucleons
 - * Allow to access total angular momentum carried by quarks
- * Deeply Virtual Compton Scattering:
the golden channel to study GPDs
 - * Measurements of cross sections and asymmetries as input to GPD constraints and fits
 - * Measurement of various azimuthal asymmetries at HERMES and other fixed target experiments
- * HERMES high lumi run 2006/2007 with Recoil detector
 - * Exclusive event tagging
 - * First time: separation of elastic and resonant BSA in DVCS