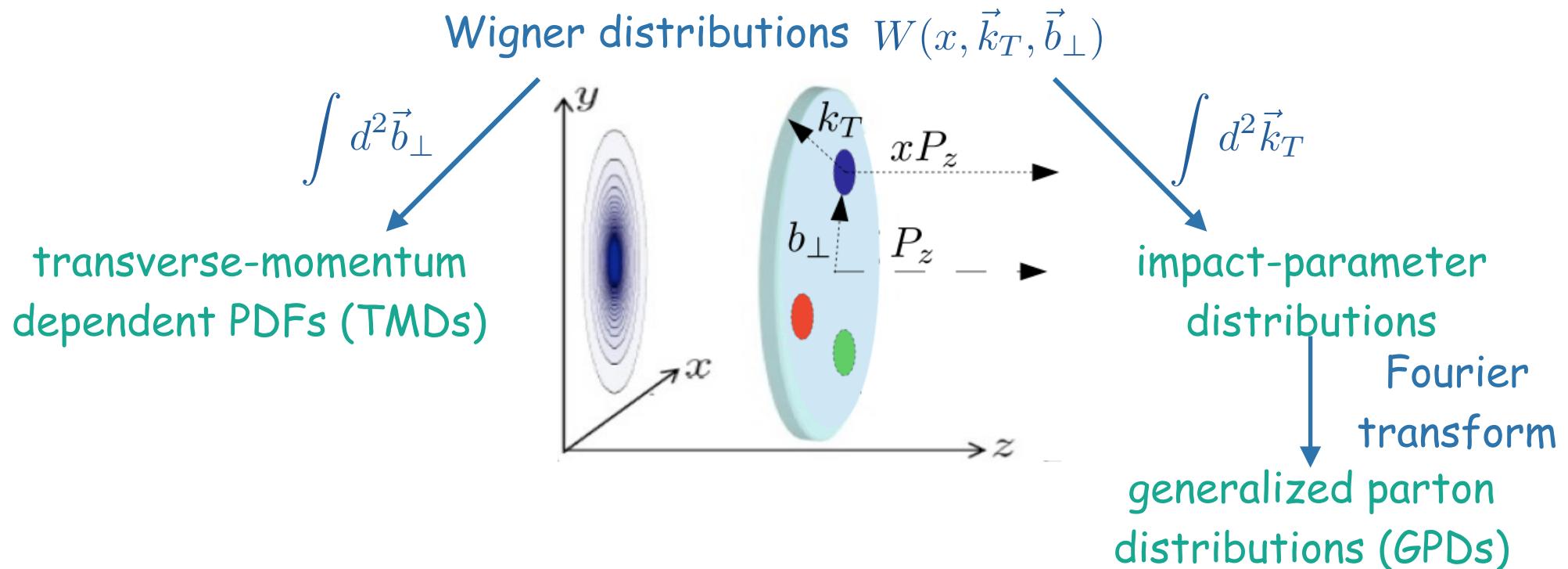


# The structure of the proton from the hermes point of view

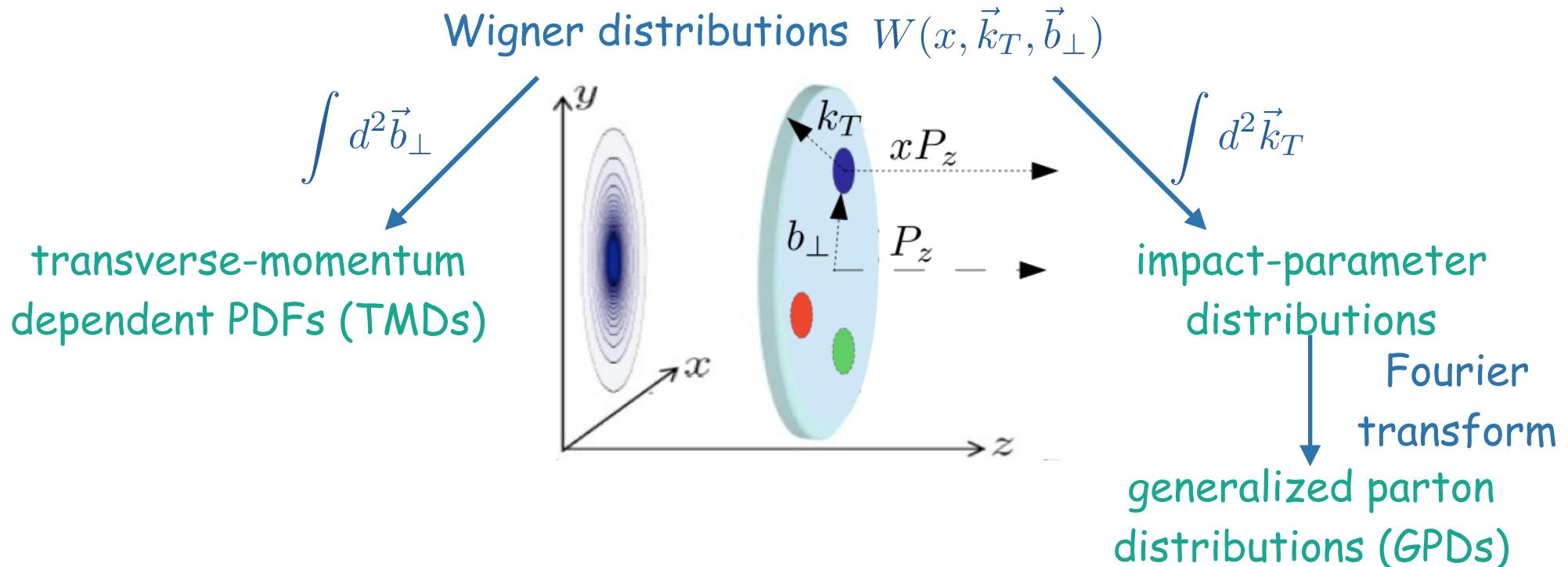
Charlotte Van Hulse, on behalf of the HERMES collaboration  
University of the Basque Country UPV/EHU - Spain

GRC - Photonuclear reactions  
Holderness NH - Aug 10-15, 2014

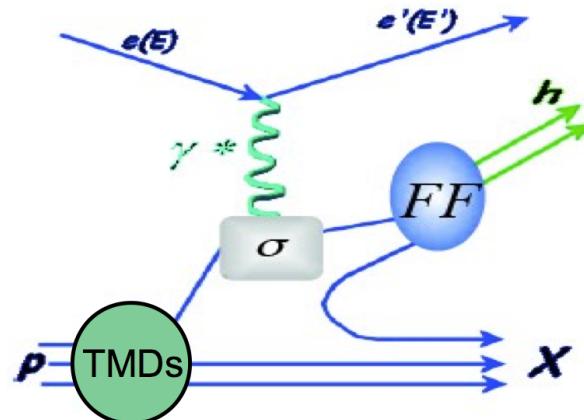
# The nucleon in multiple dimensions



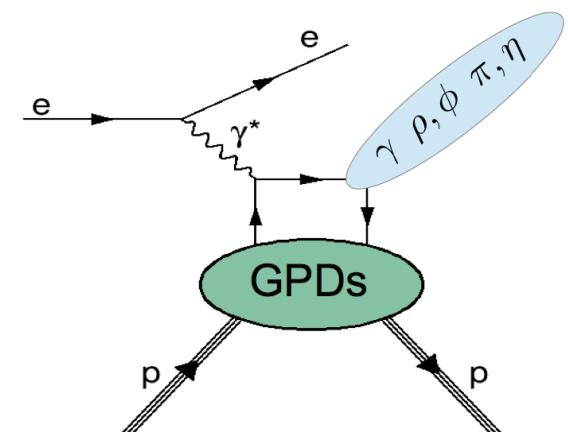
# The nucleon in multiple dimensions



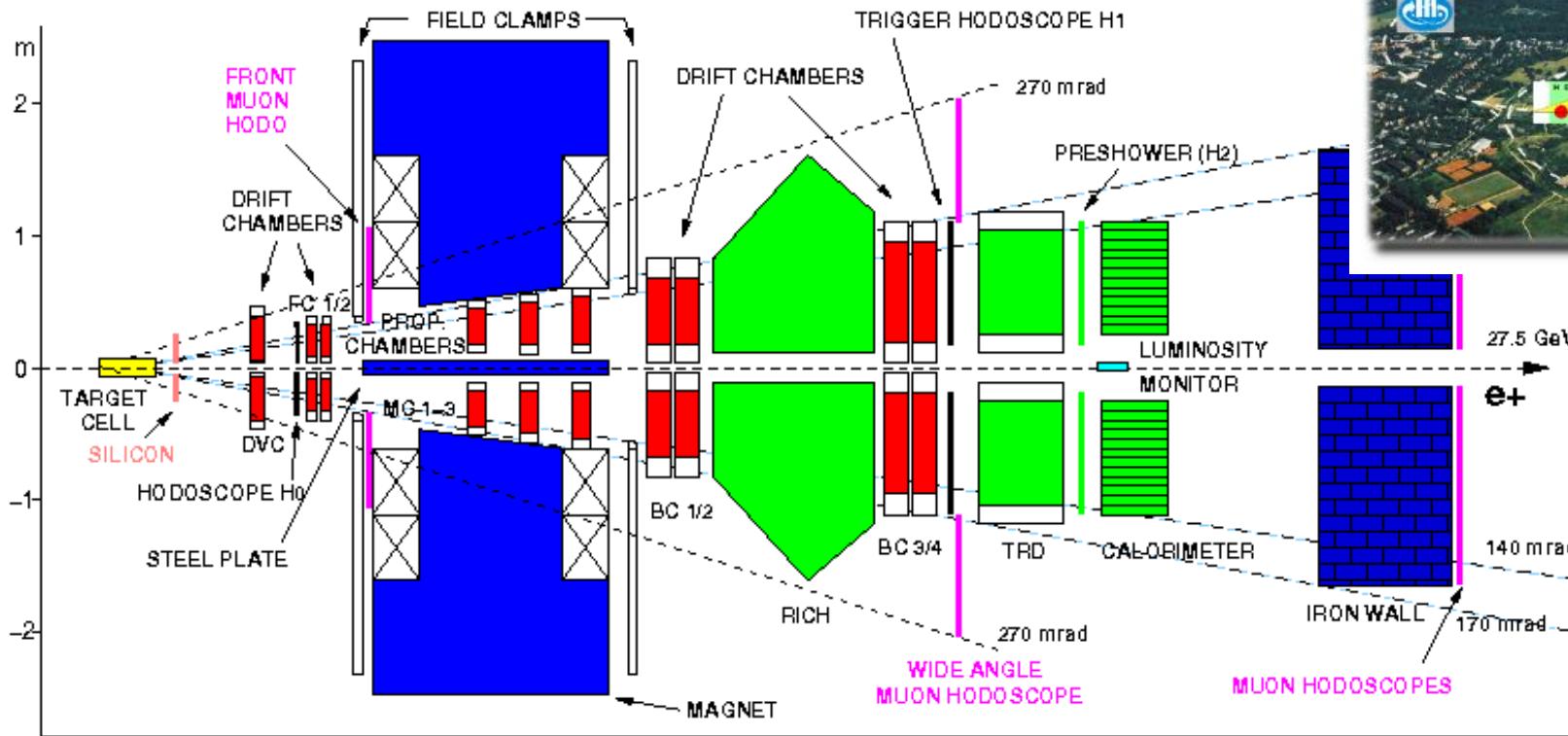
semi-inclusive deep-inelastic scattering (DIS)



hard exclusive reactions



# The HERMES experiment



data taking from  
1995 until 2007

## Beam

longitudinally polarised

$e^+$  &  $e^-$

$E=27.6$  GeV

## Gaseous internal target

transversely polarised H

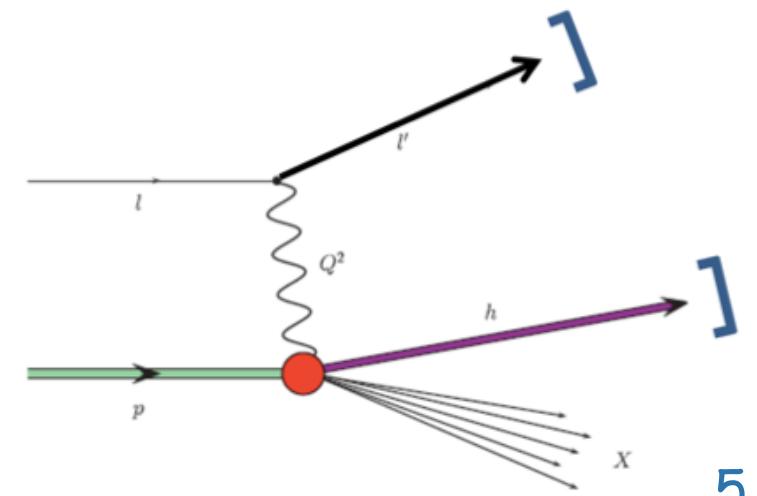
longitudinally polarised H, De, He

unpolarised H, De, He, Ne, Kr, Xe

## Particle identification

- lepton-hadron PID:  
high-efficiency (>98%) &  
low contamination (<1%)
- hadron PID via RICH 2-15 GeV

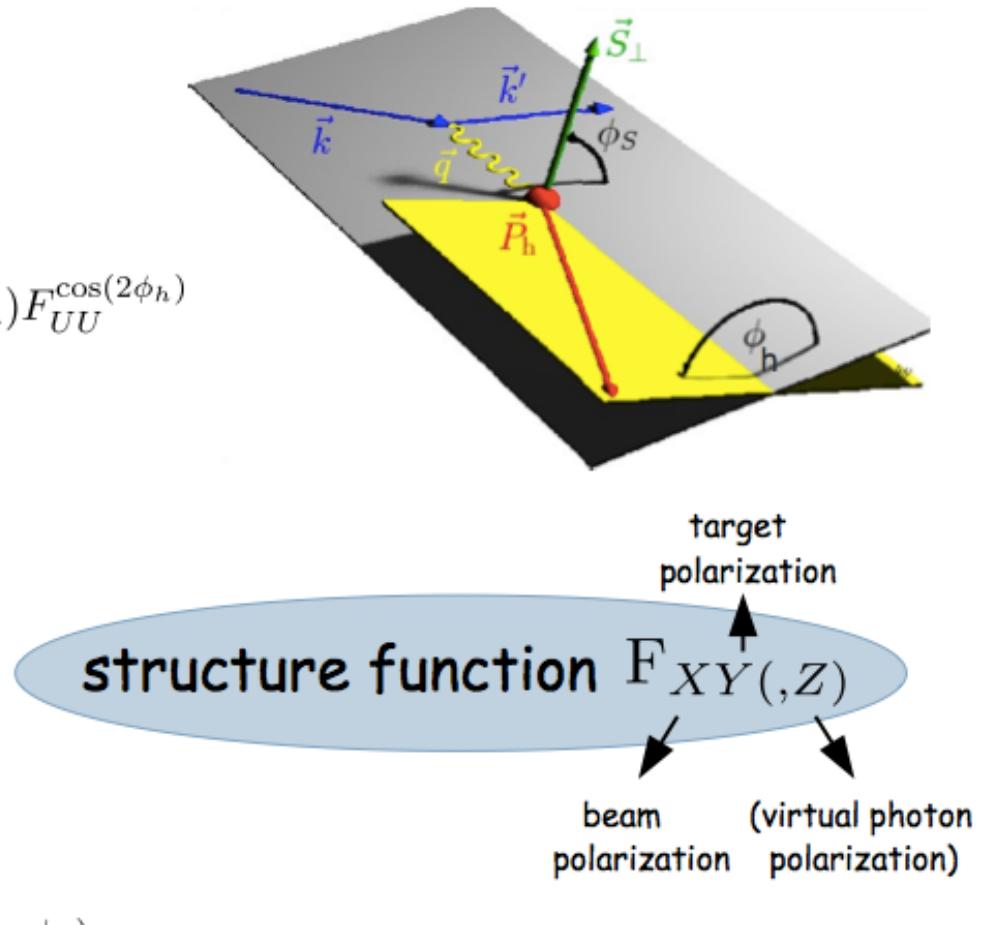
# Semi-inclusive DIS



# Semi-inclusive DIS cross section

$$\frac{d\sigma}{dxdydzd\phi_h dP_{h\perp}^2 d\phi_S} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right)$$

$$\left\{ \begin{array}{l} F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi_h) F_{UU}^{\cos(\phi_h)} + \epsilon \cos(2\phi_h) F_{UU}^{\cos(2\phi_h)} \\ \quad \xrightarrow{\text{beam polarization}} \\ + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin(\phi_h) F_{LU}^{\sin(\phi_h)} \\ \quad \xrightarrow{\text{longitudinal target polarization}} \\ + S_L \left[ \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_h) F_{UL}^{\sin(\phi_h)} + \epsilon \sin(2\phi_h) F_{UL}^{\sin(2\phi_h)} \right] \\ + S_L \lambda_e \left[ \sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_h) F_{LL}^{\cos(\phi_h)} \right] \\ \quad \xrightarrow{\text{transverse target polarization}} \\ + S_T \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \epsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\ + \epsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \epsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \\ + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \Big] \\ + S_T \lambda_e \left[ \sqrt{1-\epsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \right. \\ \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \end{array} \right\}$$



**structure function**  $F_{XY}(,Z)$

target polarization

beam polarization (virtual photon polarization)

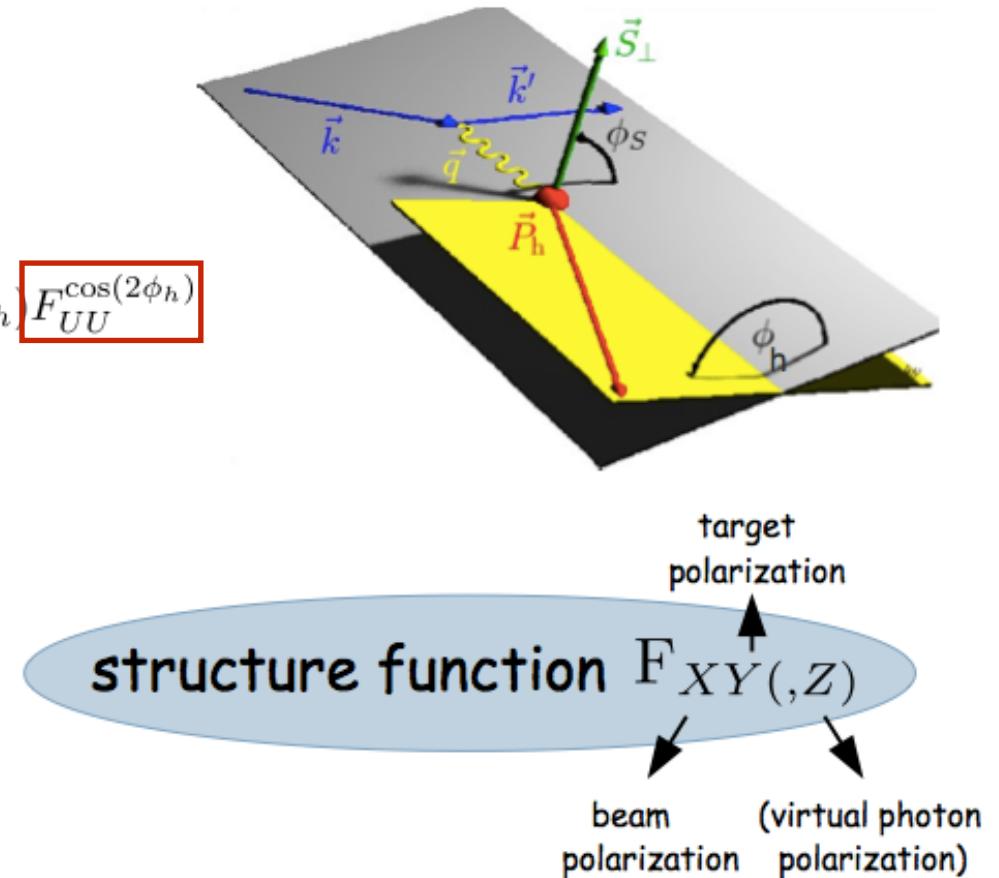
# Semi-inclusive DIS cross section

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$$\begin{aligned} & + S_L \lambda_e \left[ \sqrt{1-\epsilon^2} \boxed{F_{LL}} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_h) F_{LL}^{\cos(\phi_h)} \right] \\ & \quad \xrightarrow{\text{transverse target polarization}} \\ & + S_T \left[ \sin(\phi_h - \phi_S) \left( \boxed{F_{UT,T}^{\sin(\phi_h - \phi_S)}} + \epsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \\ & + \epsilon \sin(\phi_h + \phi_S) \boxed{F_{UT}^{\sin(\phi_h + \phi_S)}} + \epsilon \sin(3\phi_h - \phi_S) \boxed{F_{UT}^{\sin(3\phi_h - \phi_S)}} \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] \end{aligned}$$

$$\begin{aligned} & + S_T \lambda_e \left[ \sqrt{1-\epsilon^2} \cos(\phi_h - \phi_S) \boxed{F_{LT}^{\cos(\phi_h - \phi_S)}} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \end{aligned} \Bigg\}$$



structure function  $F_{XY}(,Z)$

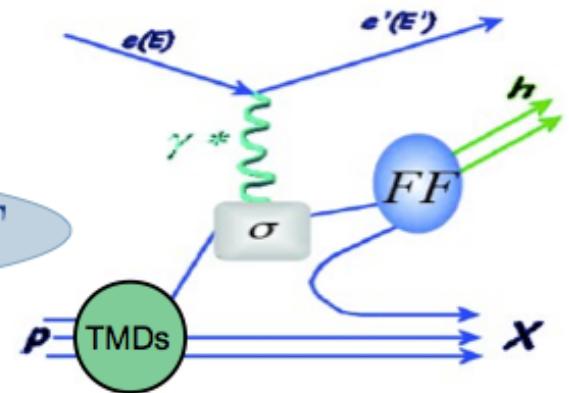
target polarization

beam polarization (virtual photon polarization)

leading twist

# Semi-inclusive DIS cross section

structure function  $F_{XY} \propto TMD \otimes FF$



transverse momentum distributions (TMDs)

		quark		
		U	L	T
nucleon	U	$f_1$		$h_1^\perp$ -
	L		$g_1$ -	$h_{1L}^\perp$ -
	T	$f_{1T}^\perp$ -	$g_{1T}^\perp$ -	$h_1$ $h_{1T}^\perp$



nucleon with transverse/longitudinal spin



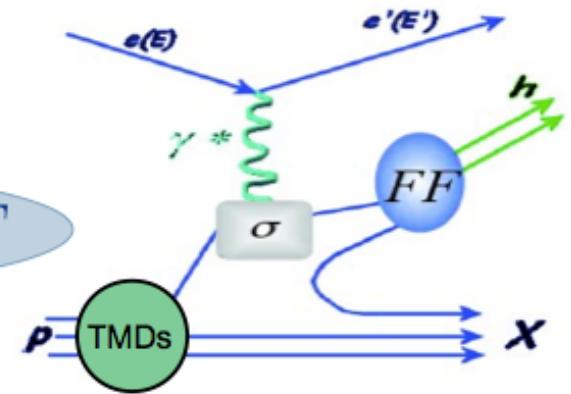
quark with transverse/longitudinal spin



quark transverse momentum

# Semi-inclusive DIS cross section

structure function  $F_{XY} \propto TMD \otimes FF$



transverse momentum distributions (TMDs)

		quark		
		U	L	T
nucleon	U	$f_1$		
	L		$g_1$	
	T	$f_{1T}^\perp$	$g_{1T}^\perp$	

fragmentation functions (FFs)

		quark		
		U	L	T
hadron	h		$D_1$	
	U			



nucleon with transverse/longitudinal spin



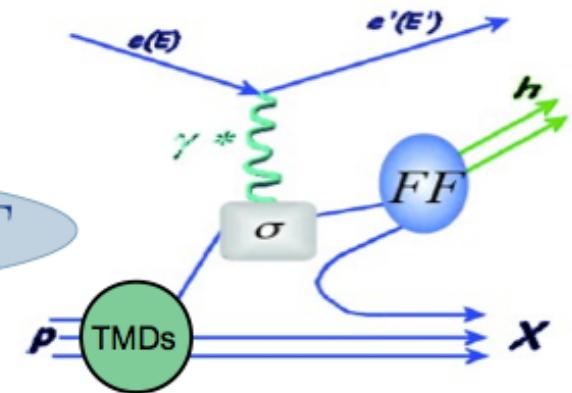
quark with transverse/longitudinal spin



quark transverse momentum

# Semi-inclusive DIS cross section

structure function  $F_{XY} \propto TMD \otimes FF$



transverse momentum distributions (TMDs)

		quark	
		L	T
nucleon	U	$f_1$	-
L		$g_1$ -	-
T		$f_{1T}^\perp$ -	$g_{1T}^\perp$ -

spin-independent DF

Sivers DF

fragmentation functions (FFs)

		quark	
		L	T
h	U	$D_1$	-

spin-independent FF



nucleon with transverse/longitudinal spin



quark with transverse/longitudinal spin



quark transverse momentum

# Hadron multiplicities

$$\frac{d\sigma}{dxdydzd\phi_h dP_{h\perp}^2} \xrightarrow{\text{unpolarized target}} \int d\phi_h M^h(x_B, Q^2, z, P_{h\perp}) = \frac{1}{d^2 N^{DIS}(x_B, Q^2)} \frac{d^4 N^h(x_B, Q^2, z, P_{h\perp})}{dz dP_{h\perp}}$$

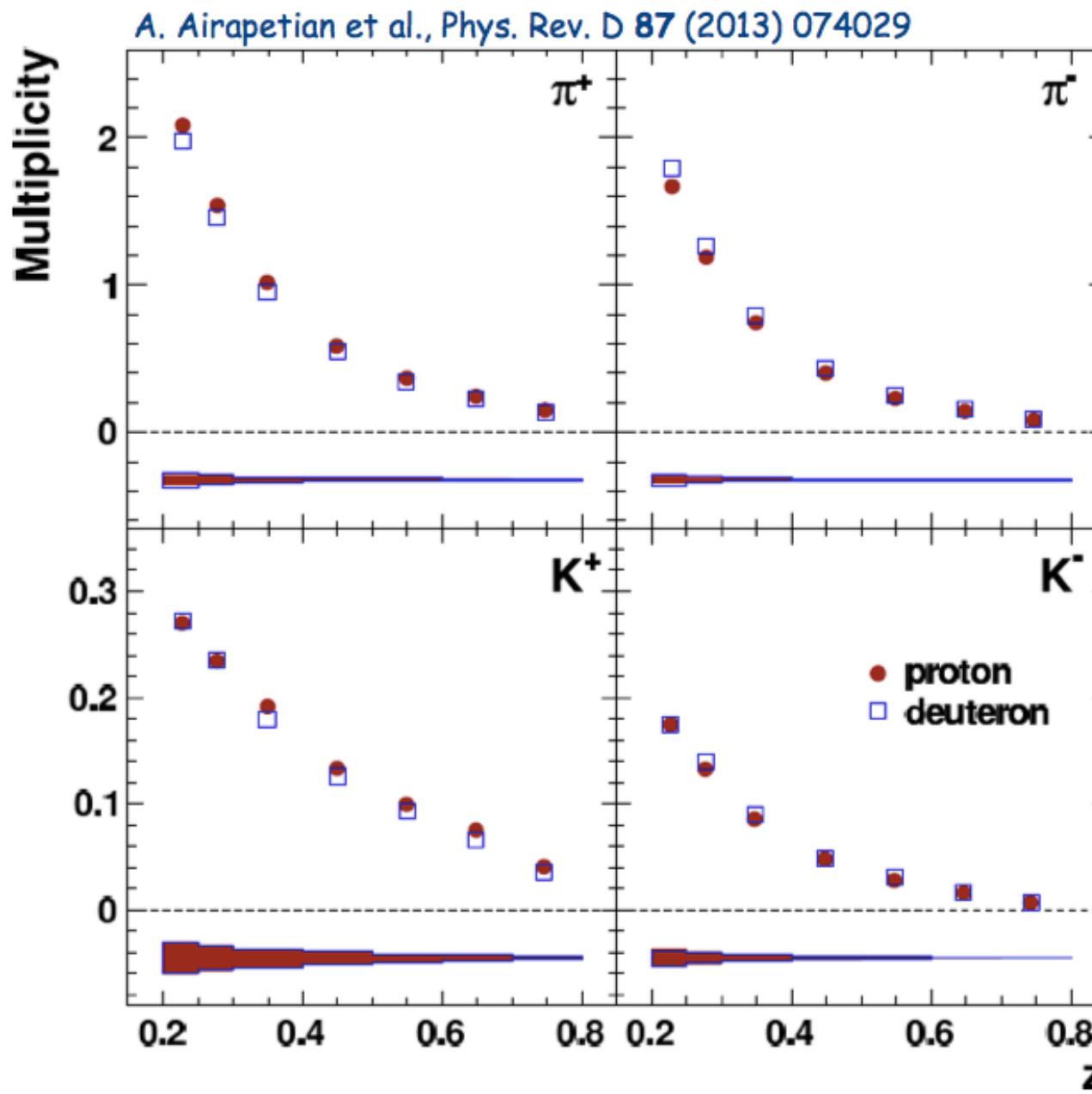
$$\propto \frac{F_{UU,T} + \epsilon F_{UU,L}}{F_T + \epsilon F_L}$$

$$\propto \frac{\sum_q e_q^2 f_1^q(x_B, k_T^2, Q^2) \otimes D_1^q(z, p_T^2, Q^2)}{\sum_q e_q^2 f_1^q(x_B, Q^2)}$$

$k_T$  : transverse momentum of struck quark

$p_T$  : transverse momentum of fragmenting quark

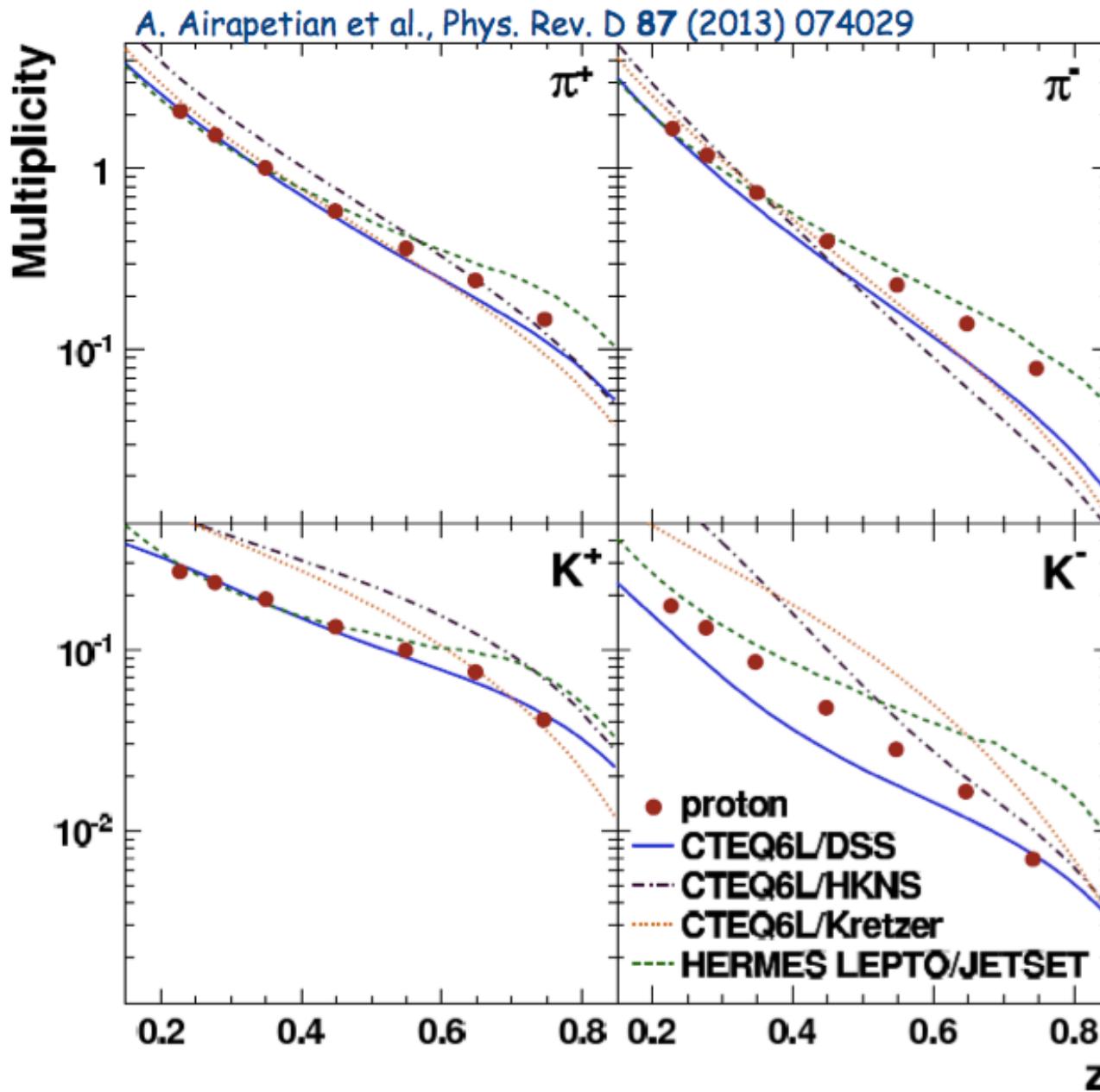
# Results projected in z



multiplicities reflect

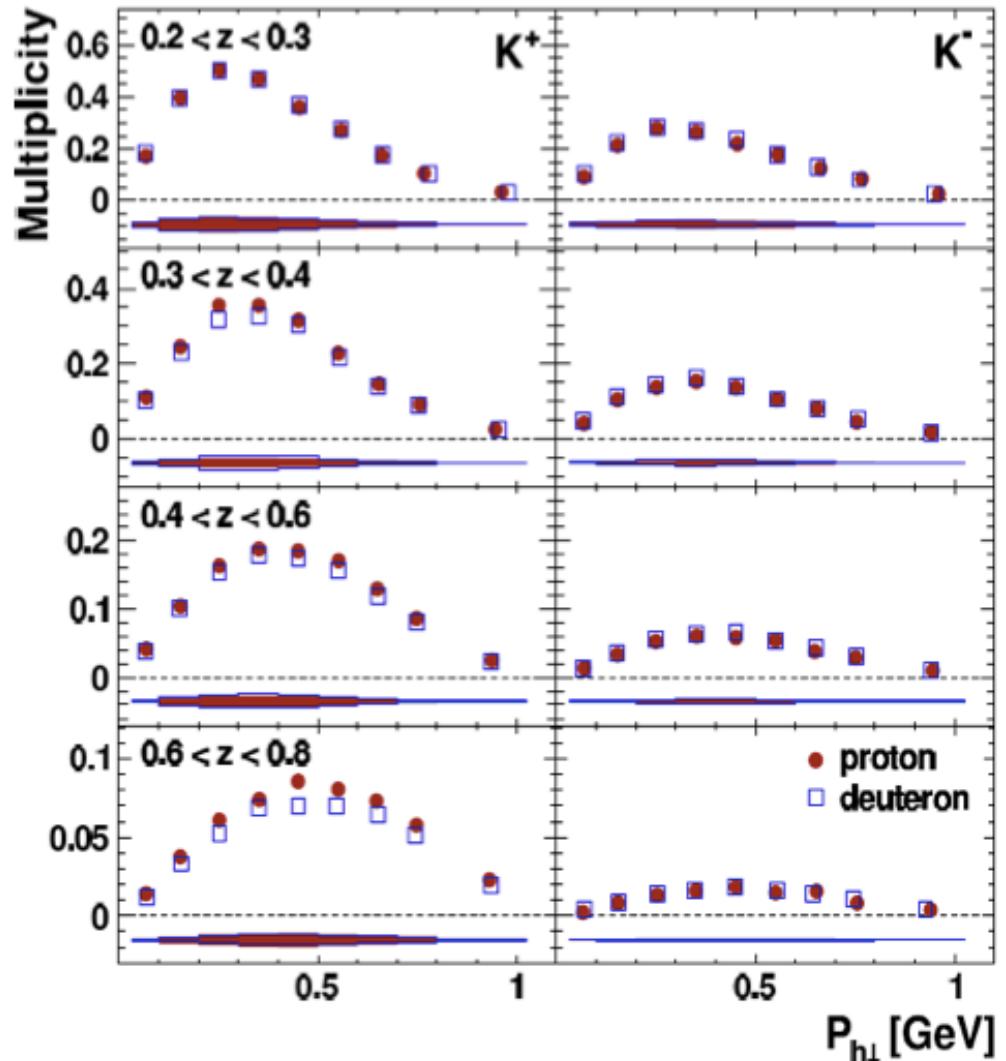
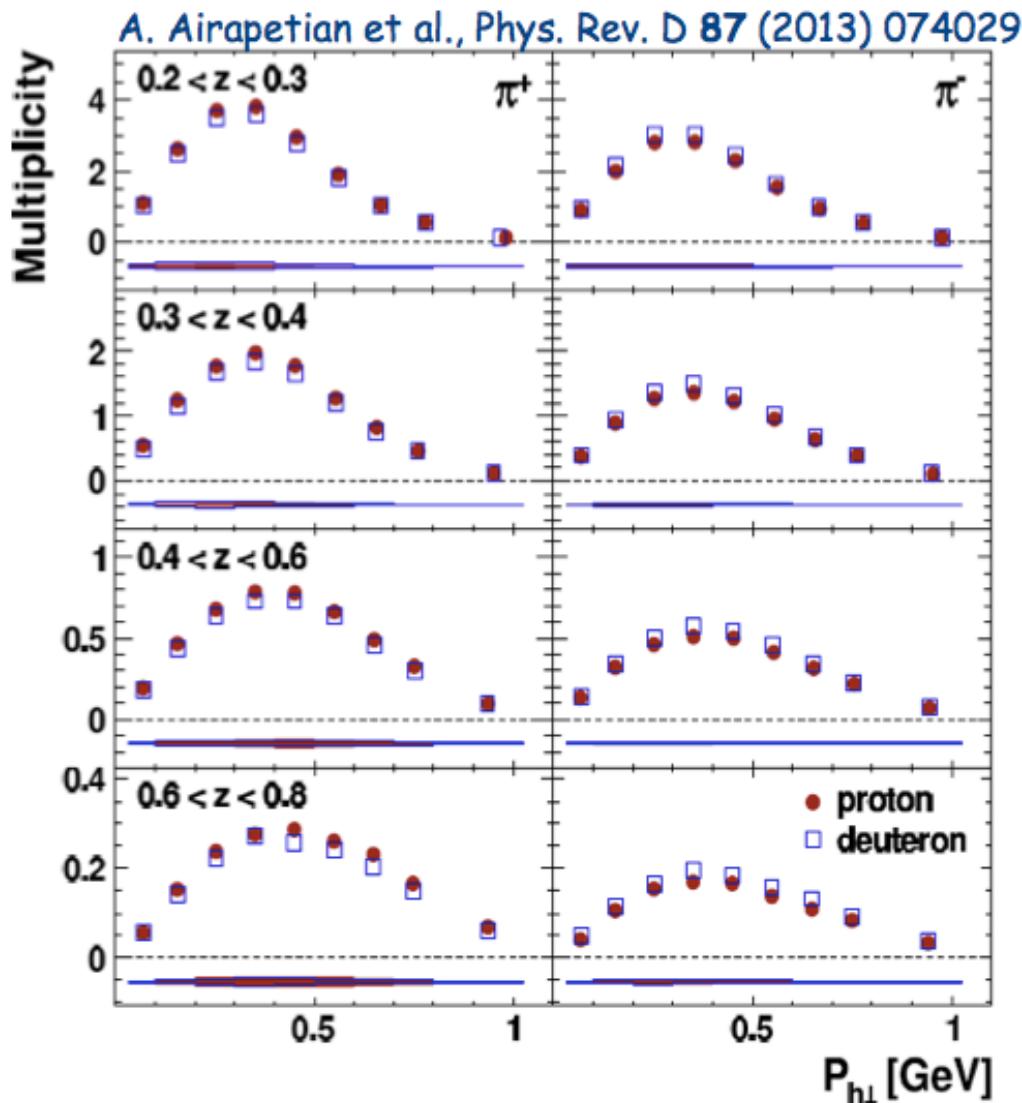
- nucleon valence-quark content
- favored  $\longleftrightarrow$  unfavored fragmentation

# Comparison to models



- leading order in  $\alpha_S$
- CTEQ6L PDFs  
JHEP 0207 (2002) 012
- DSS FFs  
Phys. Rev. D **75** (2007) 114010
- Kretzer FFs  
Phys. Rev. D **62** (2000) 054001
- reasonable agreement between DSS and positive mesons
- poor agreement for negative mesons

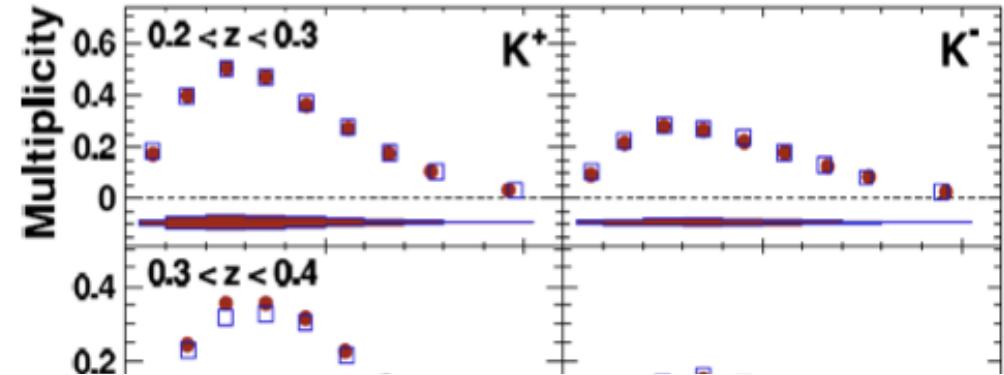
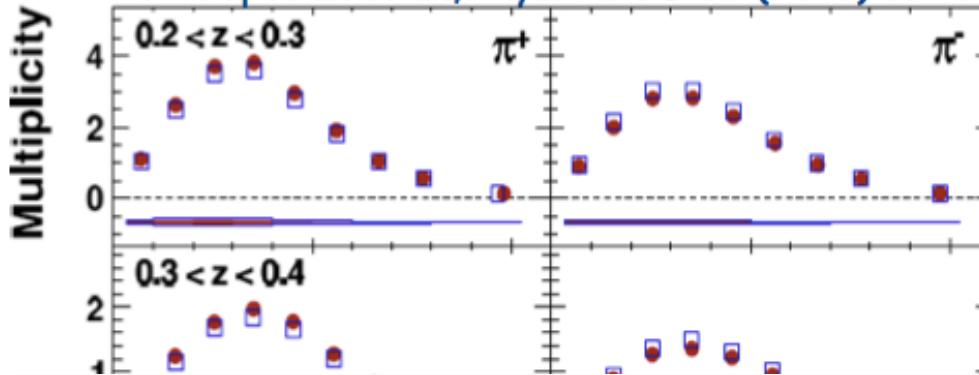
# Results projected in z and $P_{h\perp}$



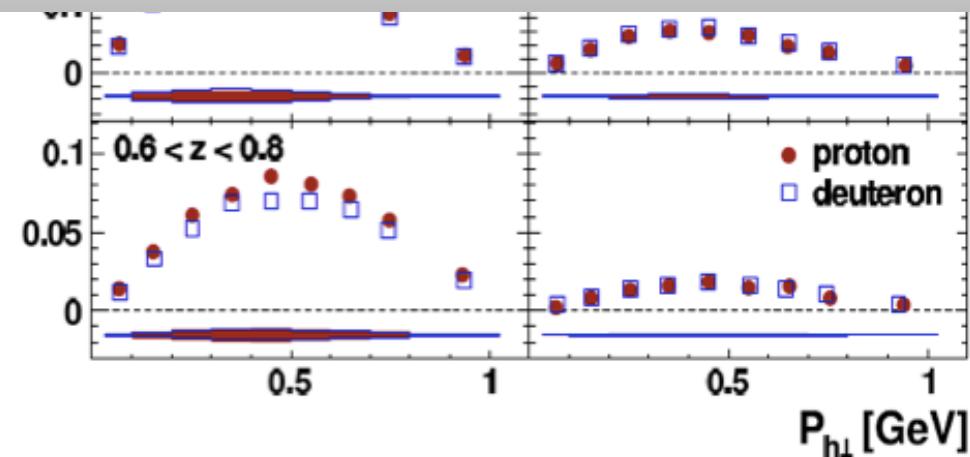
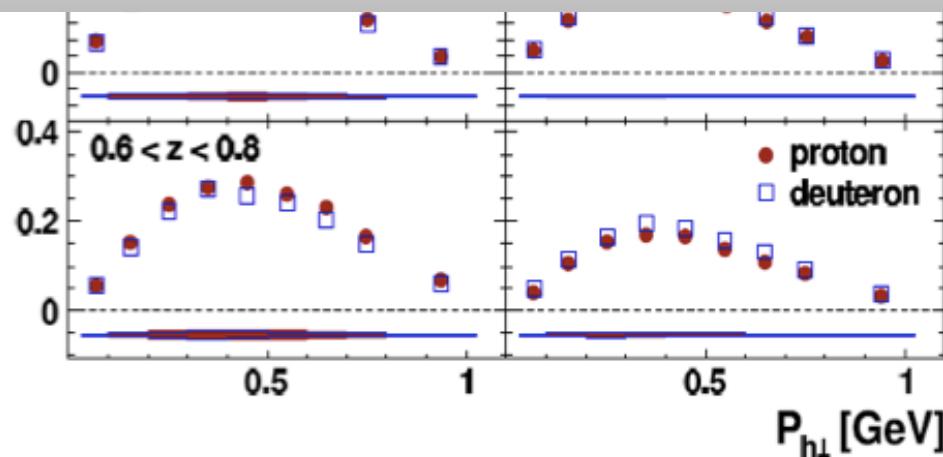
- $P_{h\perp}$  distribution reflects transverse intrinsic struck-quark momentum & transverse momentum acquired in fragmentation process
- $K^-$  displays broader distribution

# Results projected in z and $P_{h\perp}$

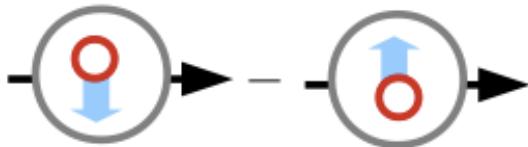
A. Airapetian et al., Phys. Rev. D 87 (2013) 074029



multi-dimensional analysis: more projections via  
<http://www-hermes.desy.de/multiplicities>



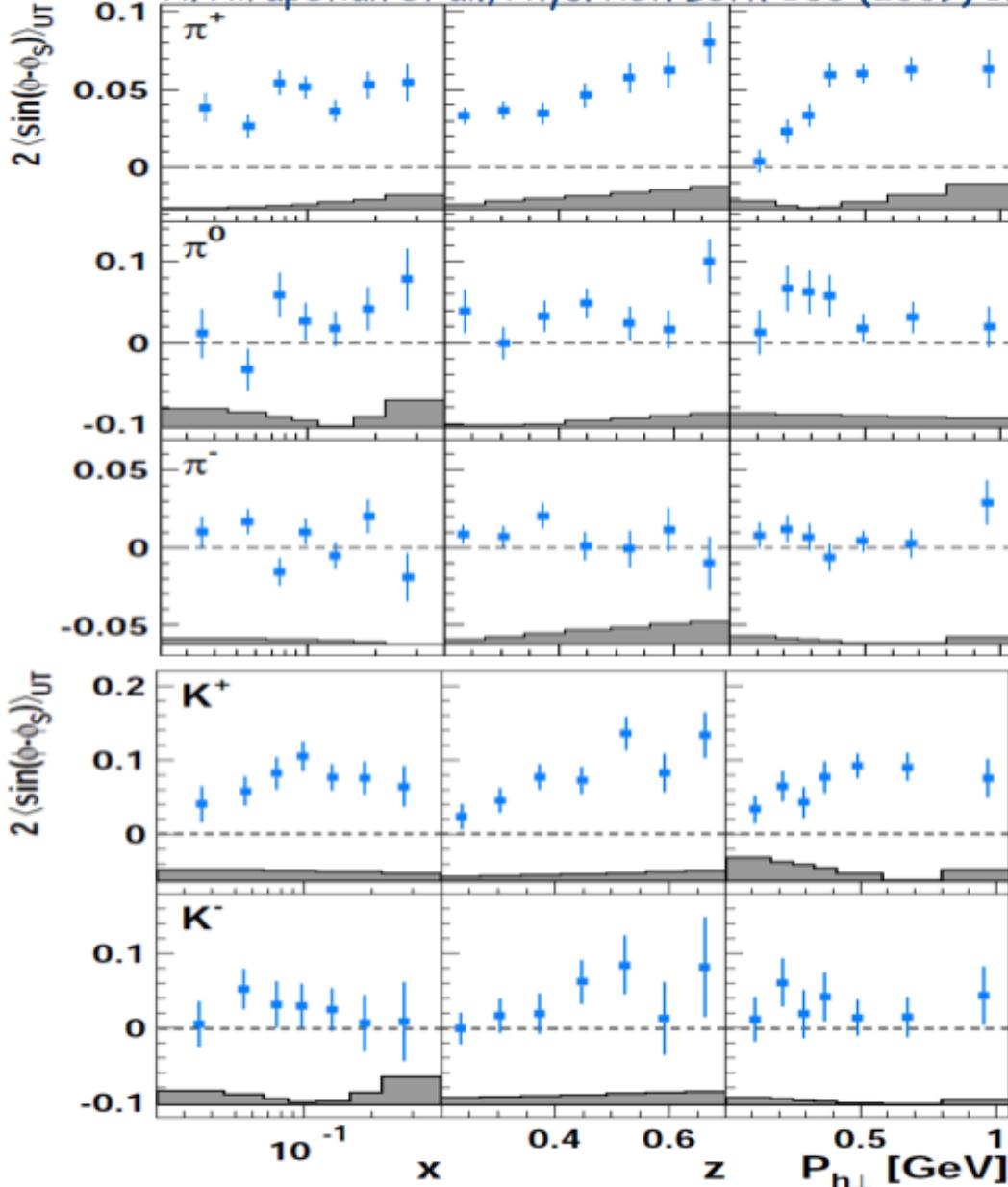
- $P_{h\perp}$  distribution reflects transverse intrinsic struck-quark momentum & transverse momentum acquired in fragmentation process
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# Sivers amplitude

$$F_{UT}^{\sin(\phi_h - \phi_S)} \propto f_{1T}^\perp \otimes D_1$$

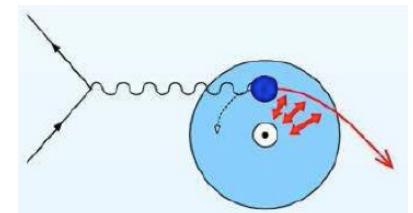
A. Airapetian et al., Phys. Rev. Lett. 103 (2009) 152002



- $\pi^+$  significantly positive  
→ orbital angular momentum
- u-quark dominance for  $\pi^+$  amplitude

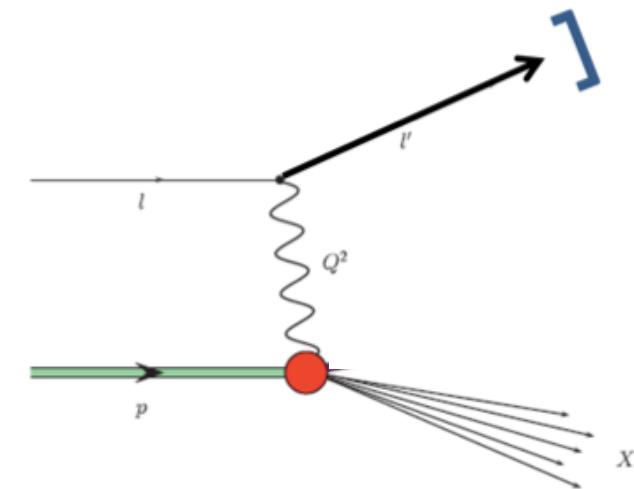
$$\approx -\frac{f_{1T}^{\perp,u}(x, k_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, p_T^2)}{f_1^u(x, k_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, p_T^2)}$$

→  $f_{1T}^{\perp,u}(x, k_T^2) < 0$



- $\pi^-$ : u- and d-quark cancelation  
→  $f_{1T}^{\perp,d}(x, k_T^2) > 0$

# $A_{LT}$ inclusive DIS



# Structure function $g_2$

transversely polarized target

- $\frac{d^3\sigma_{LT}}{dx dy d\phi'} \propto -h_k \left( \frac{y}{2} g_1(x, Q^2) + g_2(x, Q^2) \right) \cos(\phi')$   
access via 
$$A_{LT}(x, Q^2, \phi') = h_l \frac{\sigma_{LT}(x, Q^2, \phi')}{\sigma_{UU}(x, Q^2, \phi')} = -A_T \cos(\phi')$$
- $g_2(x) = g_2^{WW} + \bar{g}_2(x)$        $d_2 = 3 \int_0^1 dx x^2 \bar{g}_2(x)$

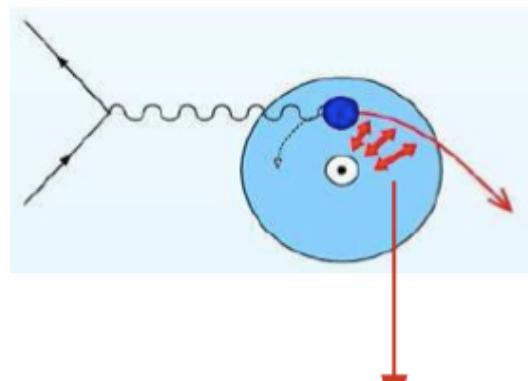
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access via  $A_{LT}(x, Q^2, \phi') = h_l \frac{\sigma_{LT}(x, Q^2, \phi')}{\sigma_{UU}(x, Q^2, \phi')} = -A_T \cos(\phi')$

- $g_2(x) = g_2^{WW} + \bar{g}_2(x) \quad d_2 = 3 \int_0^1 dx x^2 \bar{g}_2(x)$

- Sivers effect



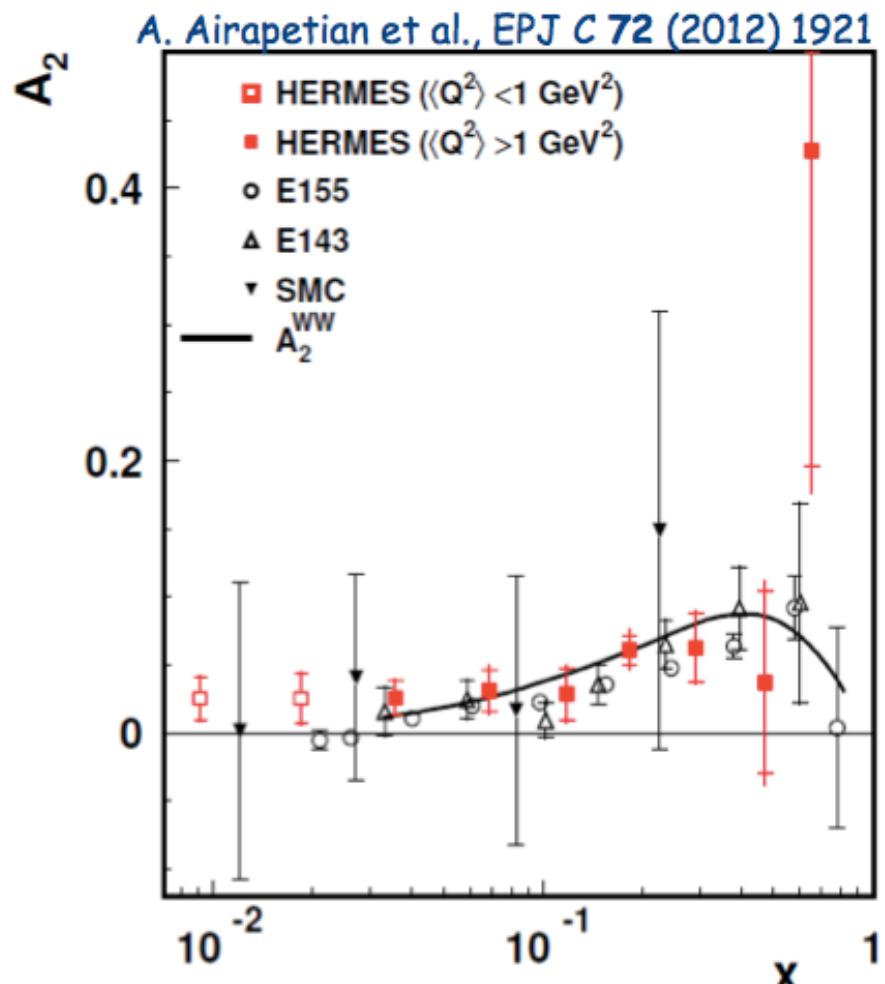
FSI from  $t=0 \rightarrow \infty$

force on struck quark at  $t=0$

$$\propto -d_2$$

M. Burkardt arXiv:0810.3589

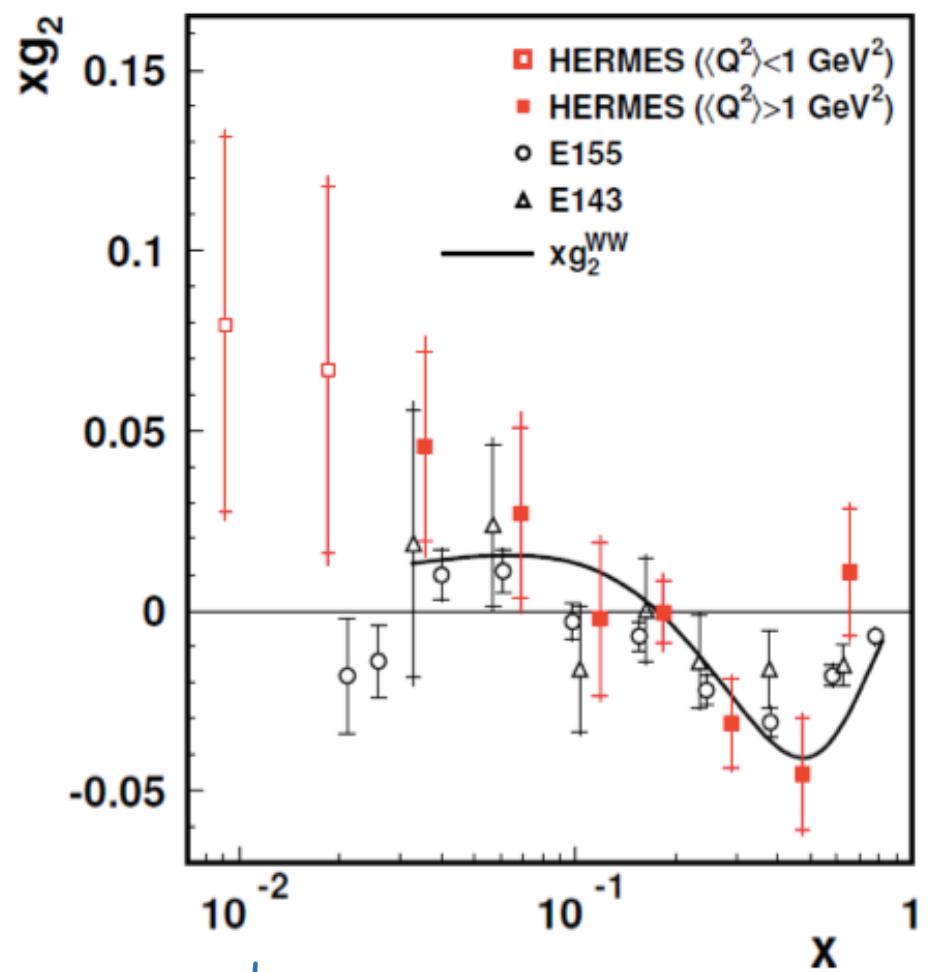
# $A_2$ and $g_2$



- evaluation of Burkhardt-Cottingham sum rule

$$\int_{0.023}^{0.9} dx g_2(x) = 0.006 \pm 0.024 \pm 0.017$$

$$\text{E143+E155: } \int_{0.02}^{0.8} dx g_2(x) = -0.042 \pm 0.008$$

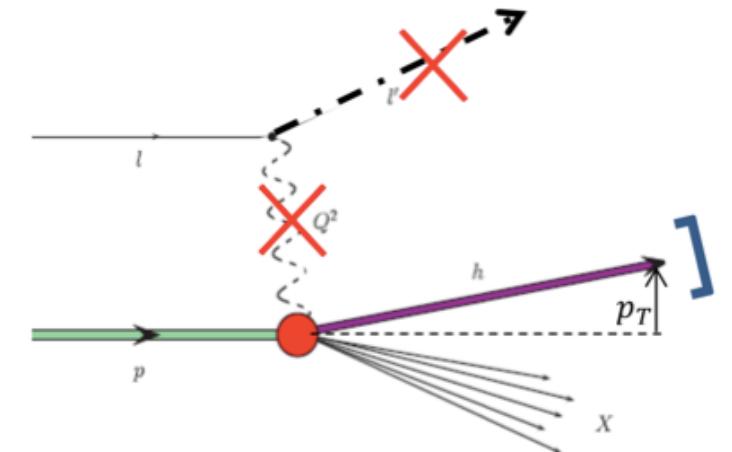


- $d_2$

$$d_2 = 0.0148 \pm 0.0096 \pm 0.0048$$

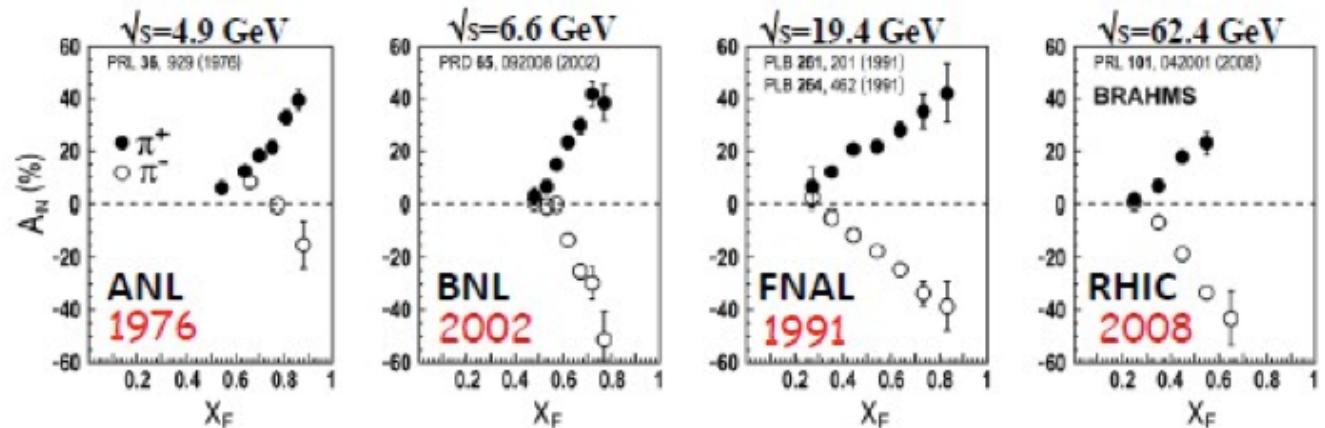
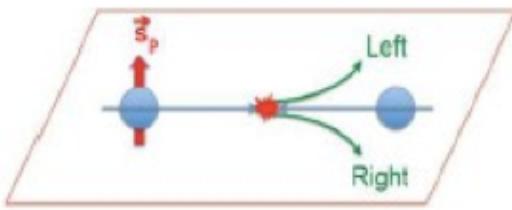
$$\text{E143+E155: } d_2 = 0.0032 \pm 0.0017$$

# AUT inclusive



# Transverse target single-spin asymmetry in inclusive electroproduction of pions and kaons

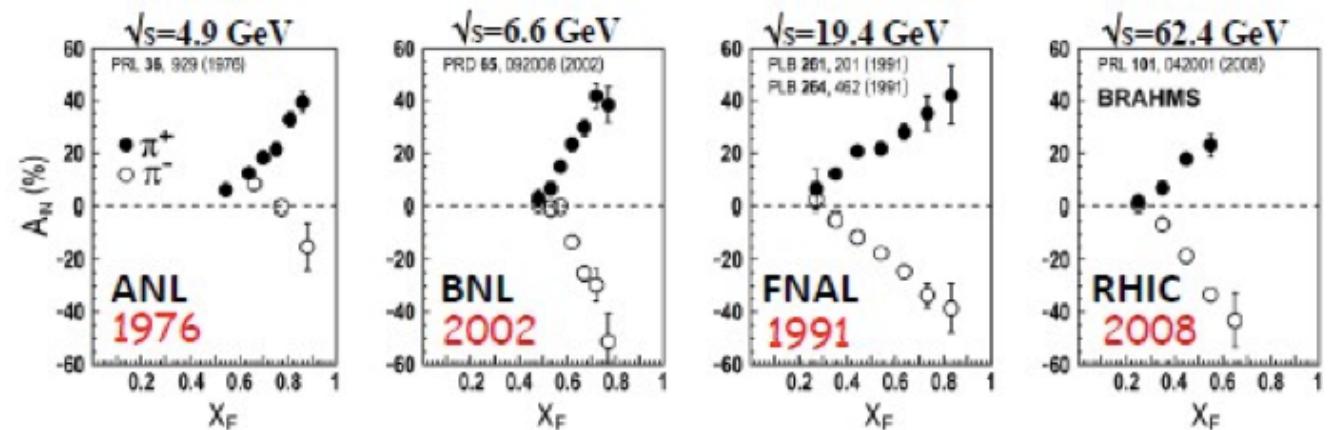
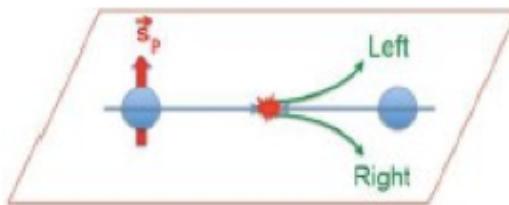
- various polarized pp scattering experiments consistently observe since 35 years large  $A_N$  asymmetries, with  $\sqrt{s}$  from 5 to 200 GeV



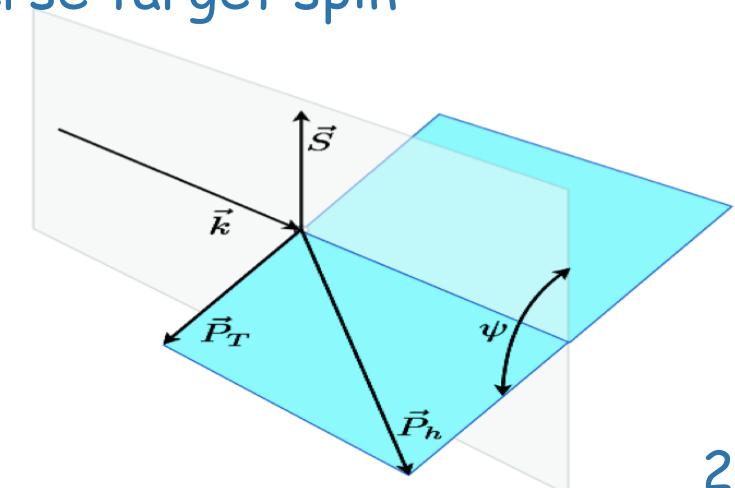
- not interpretable in leading-twist based on collinear factorisation

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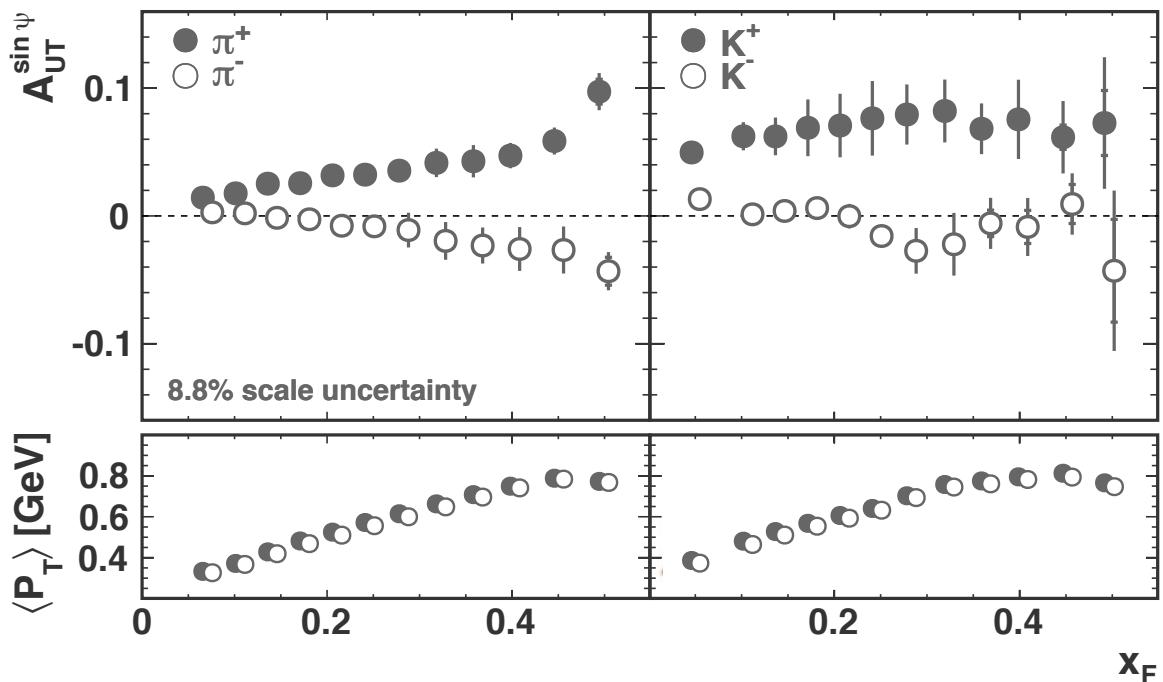
- not interpretable in leading-twist based on collinear factorisation
  - HERMES measurement of inclusive transverse target spin asymmetry  $A_{UT}^{\sin(\psi)}$ :
- $$d\sigma = d\sigma_{UU} [1 + s_\perp A_{UT}^{\sin(\psi)} \sin(\psi)]$$
- $A_{UT}^{\sin(\psi)} = \frac{\pi}{2} A_N$
  - at HERMES:  $\sin(\psi) \sim \sin(\phi - \phi_S)$



# Results: $x_F$ dependence

$$x_F = 2P_L/\sqrt{s}$$

A. Airapetian et al, Phys. Lett. B 728 (2014) 183-190



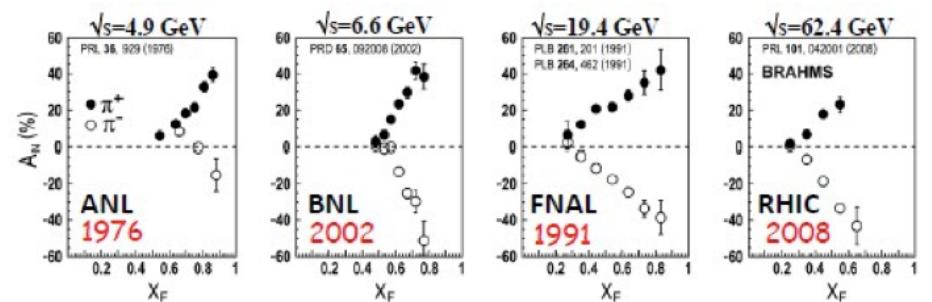
$\pi^+$

- positive, increase linearly with  $x_F$

$\pi^-$

- negative, decrease linearly with  $x_F$

$x_F$  behavior of pions similar to what observed in hadron-hadron collisions



$K^+$

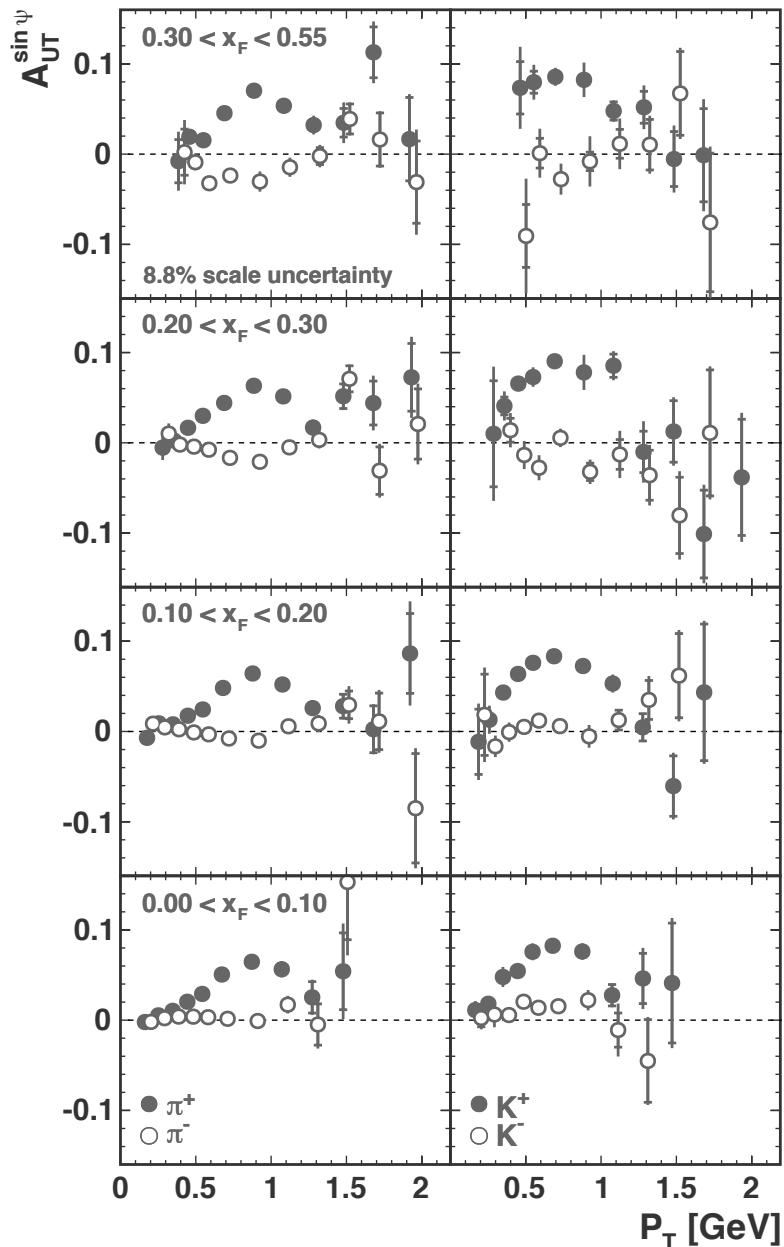
- positive, ~constant with  $x_F$

$K^-$

- compatible with zero, with small variations over  $x_F$

# Results: disentangle $x_F$ and $P_T$ dependence

A. Airapetian et al, Phys. Lett. B 728 (2014) 183-190



$\pi^+$

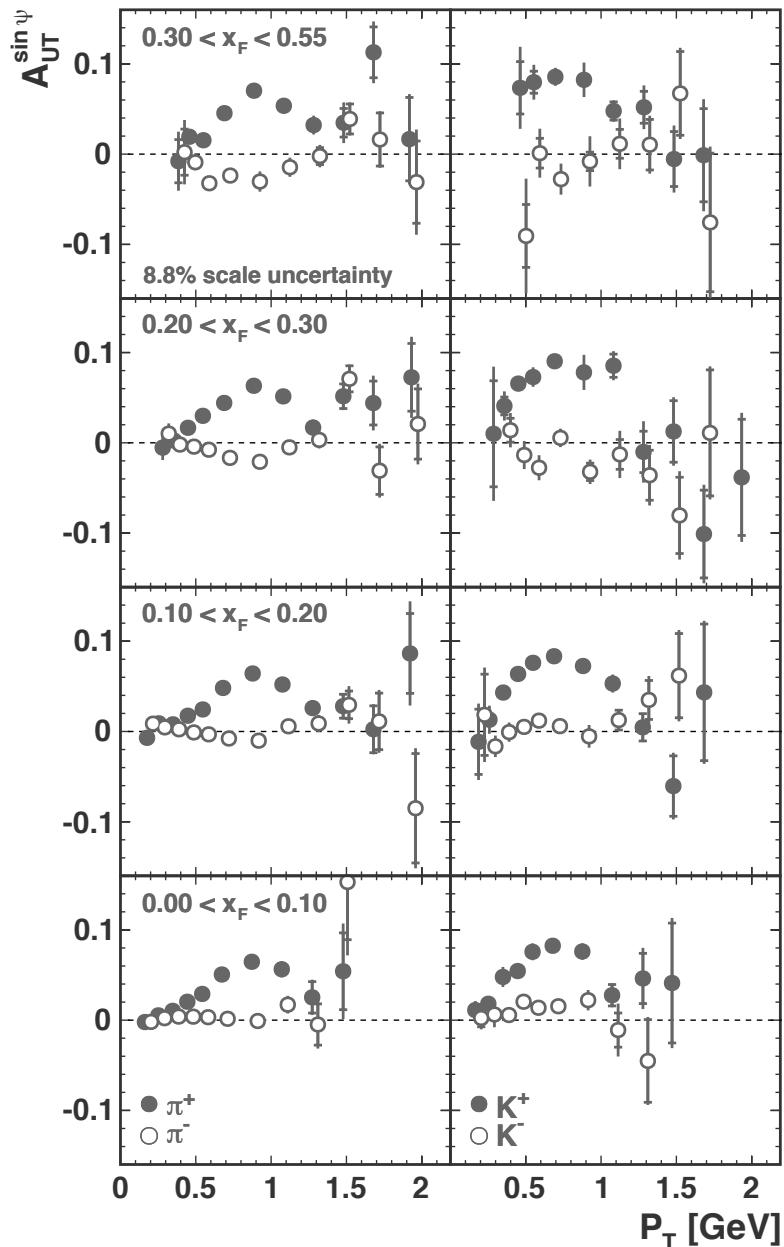
- increase with  $P_T$  up to  $P_T \approx 0.8$  GeV
- $P_T$  dependence independent of  $x_F$
- $x_F$  increase from  $P_T$  dependence

$\pi^-$

- small amplitudes,
- varyingly positive and negative with  $P_T$
- decrease with increasing  $x_F$

# Results: disentangle $x_F$ and $P_T$ dependence

A. Airapetian et al, Phys. Lett. B 728 (2014) 183-190



$K^+$

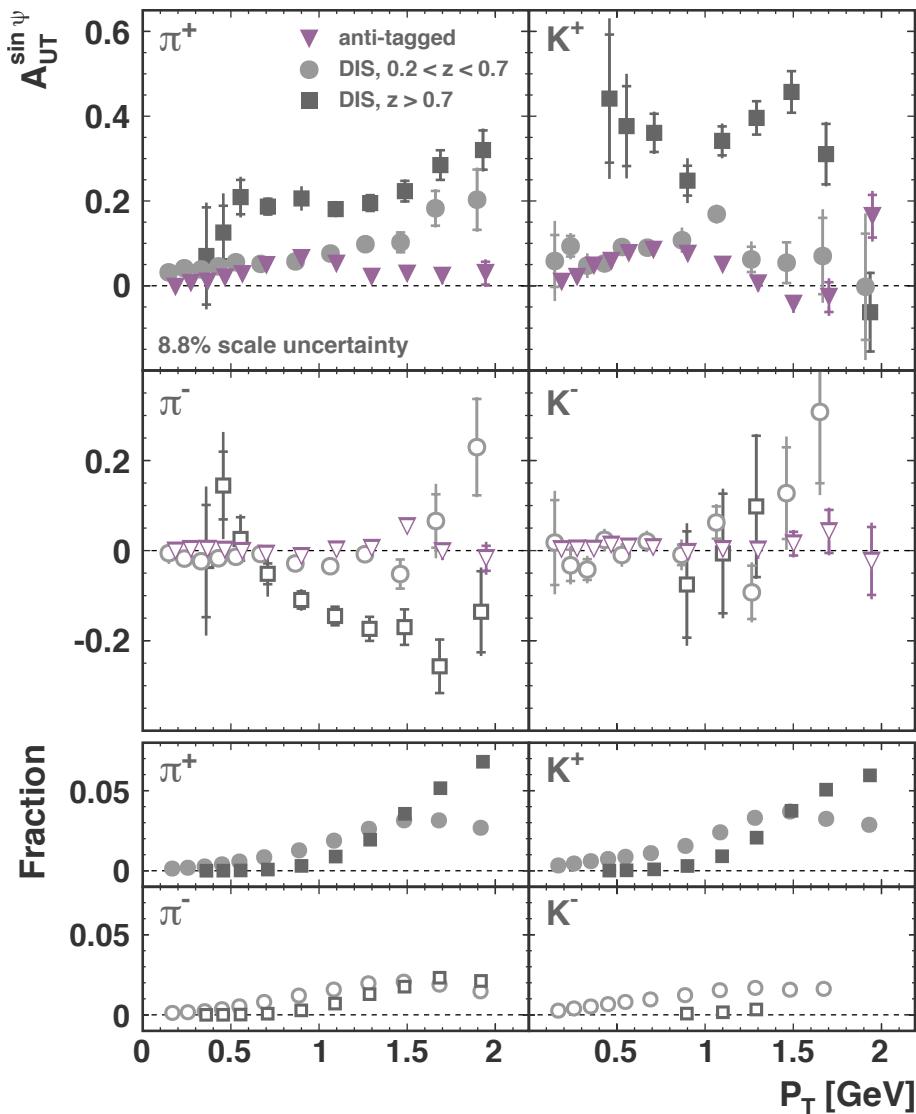
- increase with  $P_T$  up to  $P_T \approx 0.8$  GeV
- increase with increasing  $x_F$

$K^-$

- small amplitudes
- decrease with increasing  $x_F$

# Contribution of various subsamples

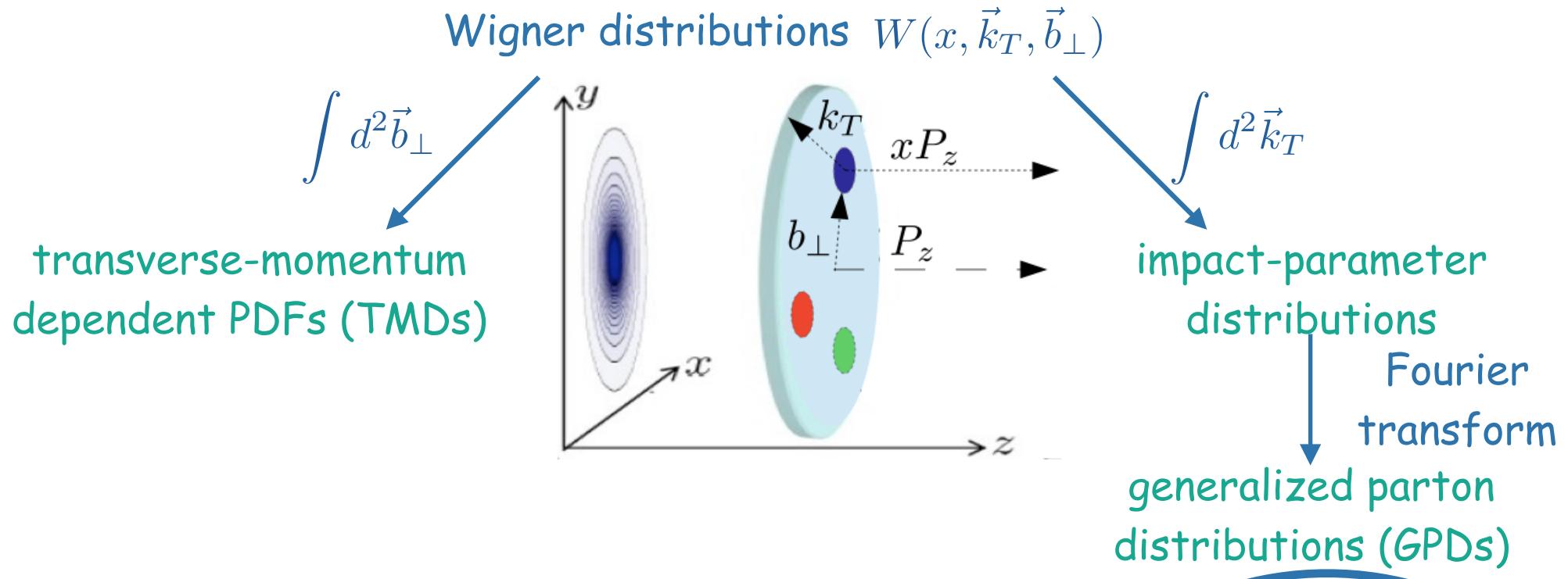
A. Airapetian et al, Phys. Lett. B 728 (2014) 183-190



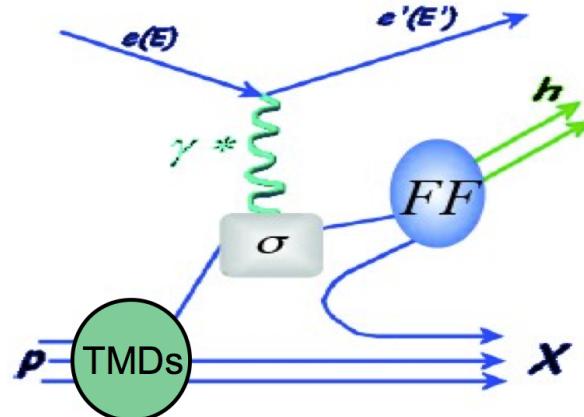
3 subsamples:

- anti-tagged: no  $e^\pm$  detected (mostly  $Q^2 \approx 0$ )
- DIS with  $0.2 < z < 0.7$
- DIS with  $z > 0.7$
- anti-tagged results  $\sim$  overall results, majority of statistics
- $0.2 < z < 0.7$  results: similar to Sivers amplitudes
- $z > 0.7$  results: large asymmetries

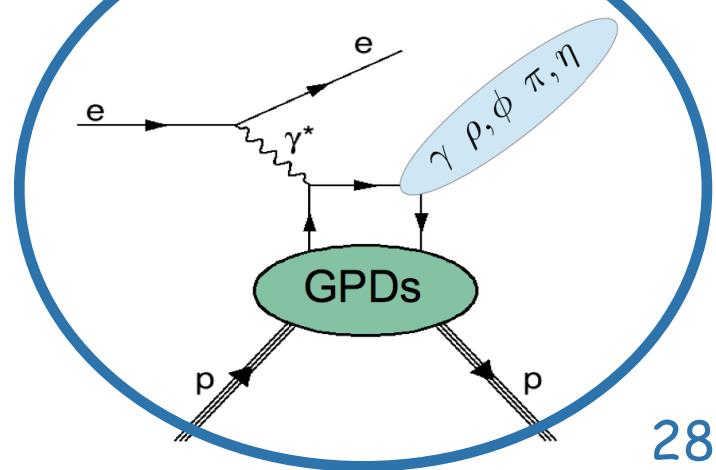
# The nucleon in multiple dimensions



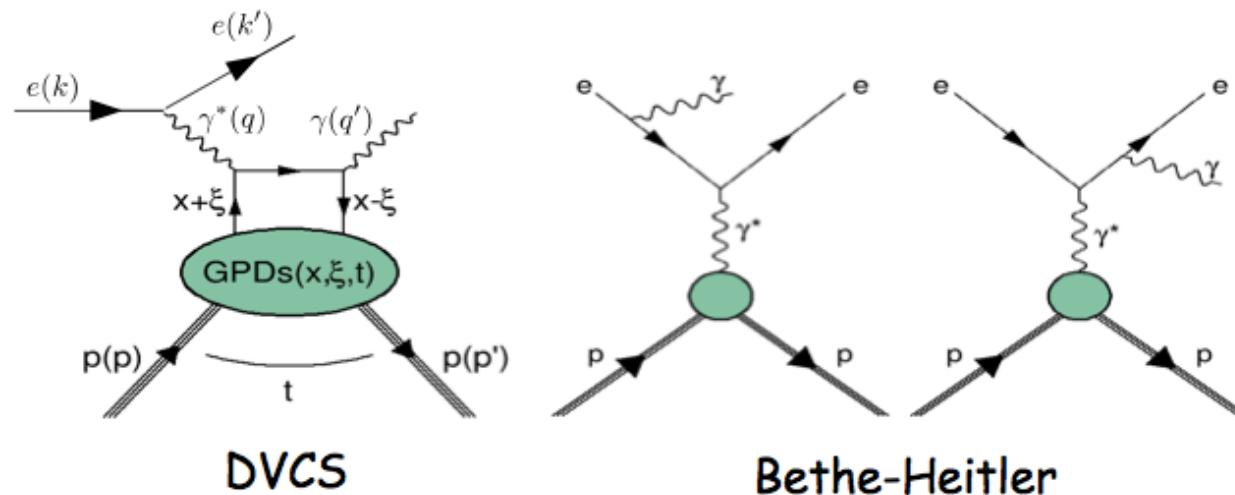
semi-inclusive deep-inelastic scattering (DIS)



hard exclusive reactions

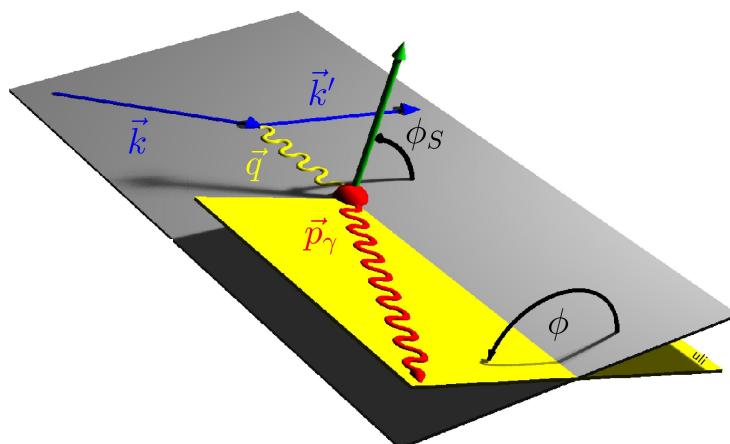


# Exclusive production of real photons

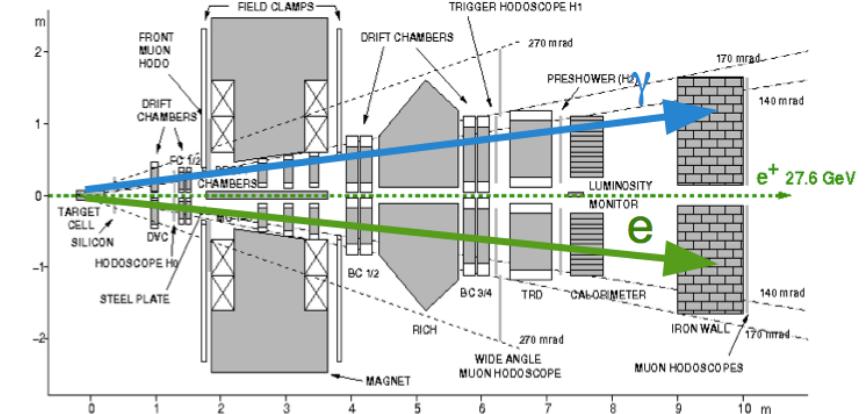
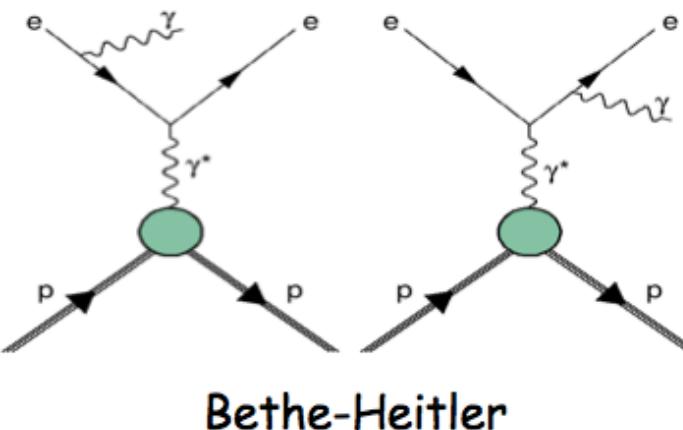
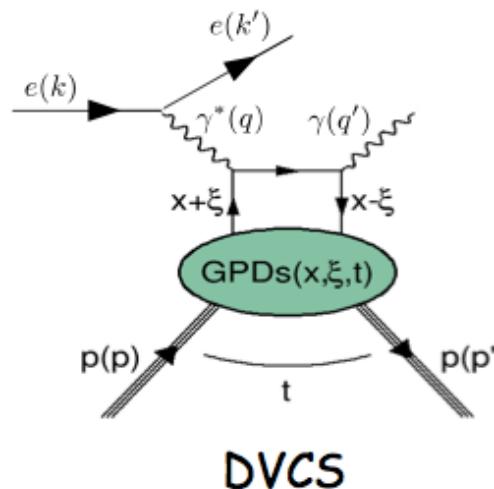


$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{BH}\tau_{DVCS}^* + \tau_{DVCS}\tau_{BH}^*$$

→ access through azimuthal asymmetries

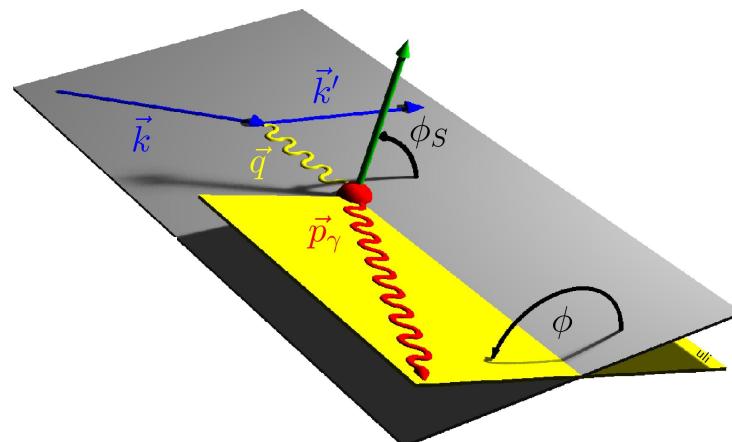


# Exclusive production of real photons



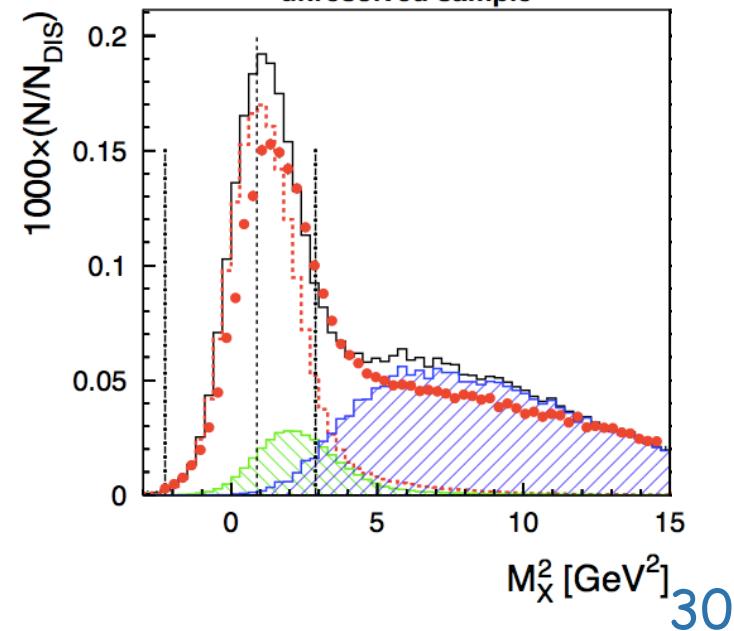
$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{BH}\tau_{DVCS}^* + \tau_{DVCS}\tau_{BH}^*$$

→ access through azimuthal asymmetries

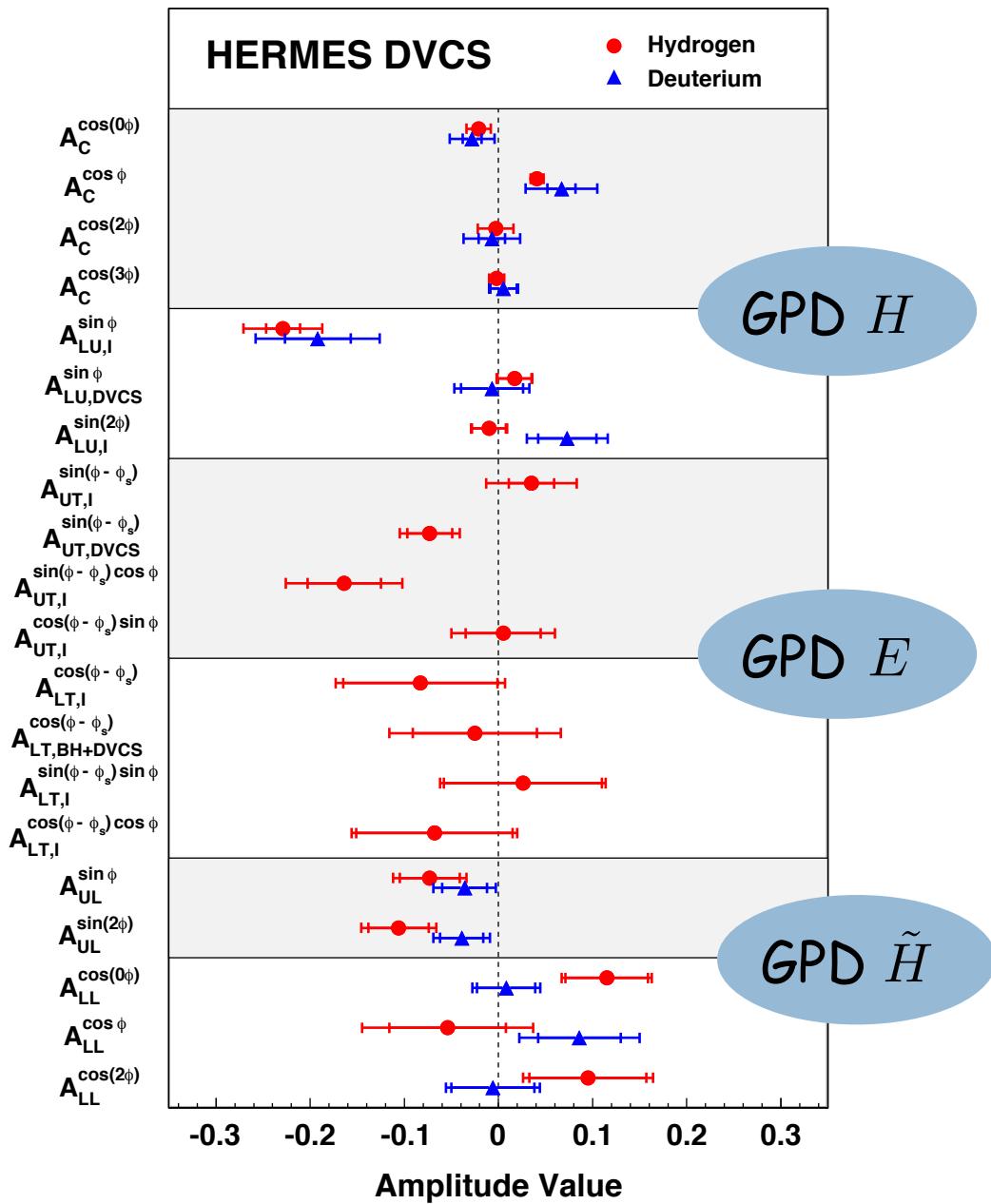


exclusivity: reconstruct proton via missing mass:

unresolved sample



# DVCS at HERMES



beam-charge asymmetry

JHEP 07 (2012) 32

Nucl. Phys. B 829 (2010) 1

beam-helicity asymmetry

JHEP 07 (2012) 32

Nucl. Phys. B 829 (2010) 1

transverse target-spin asymmetry

JHEP 06 (2008) 066

double spin (LT) asymmetry

Phys. Lett. B 704 (2011) 15

longitudinal target-spin asymmetry

JHEP 06 (2010) 019

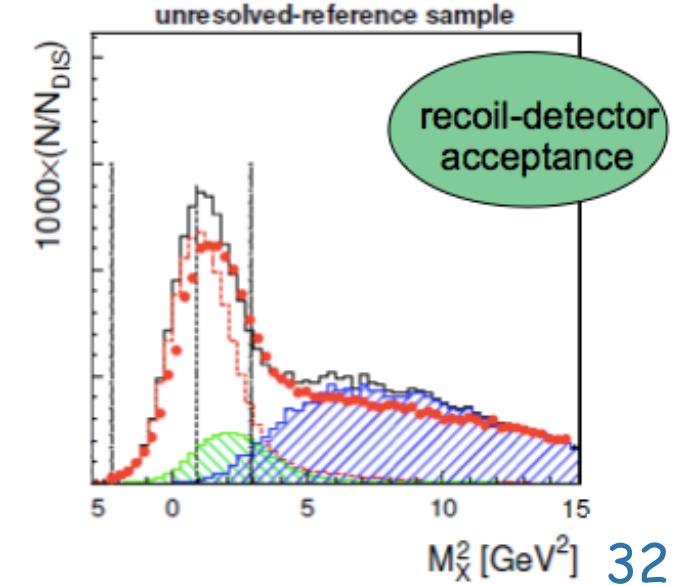
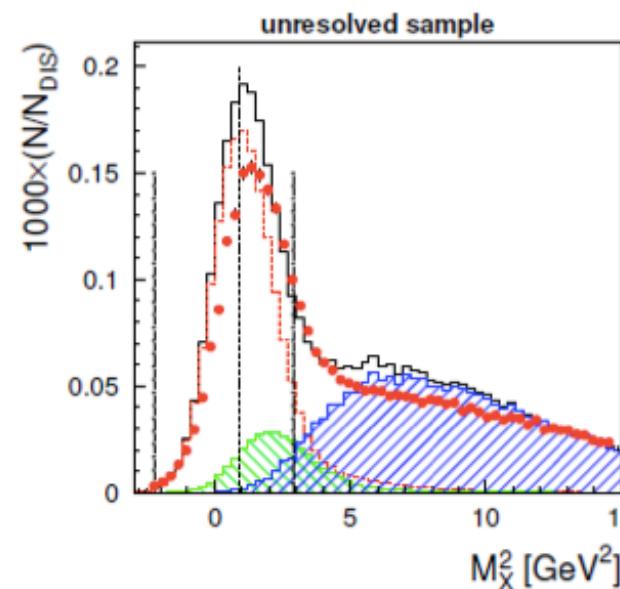
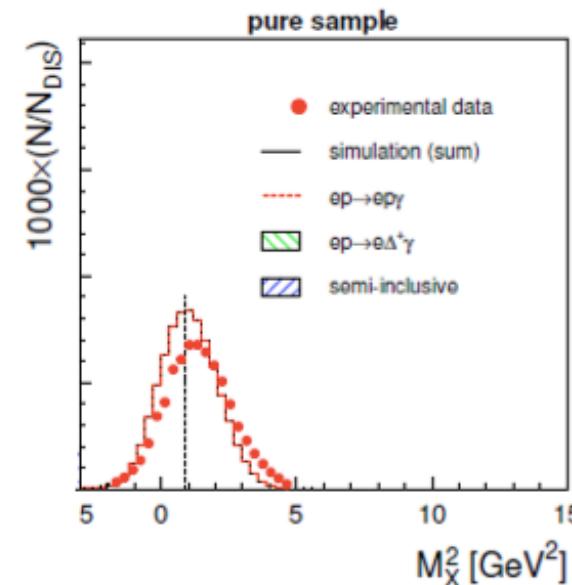
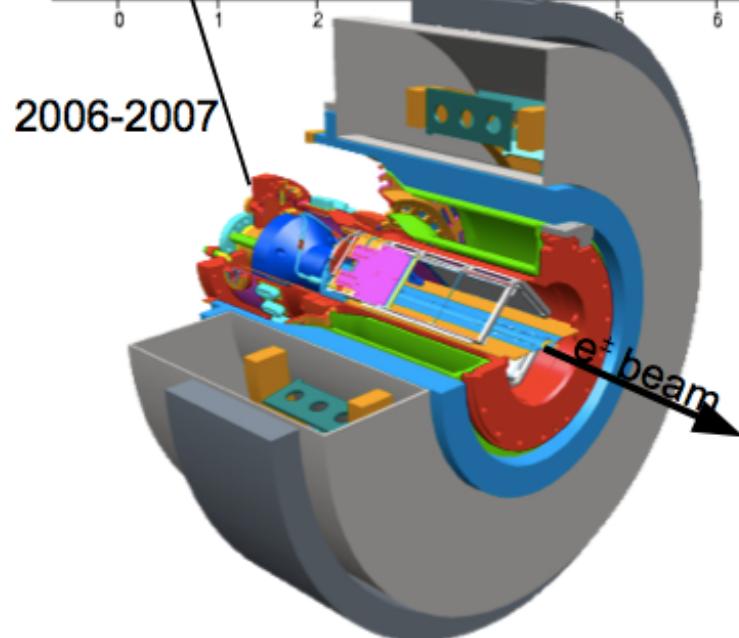
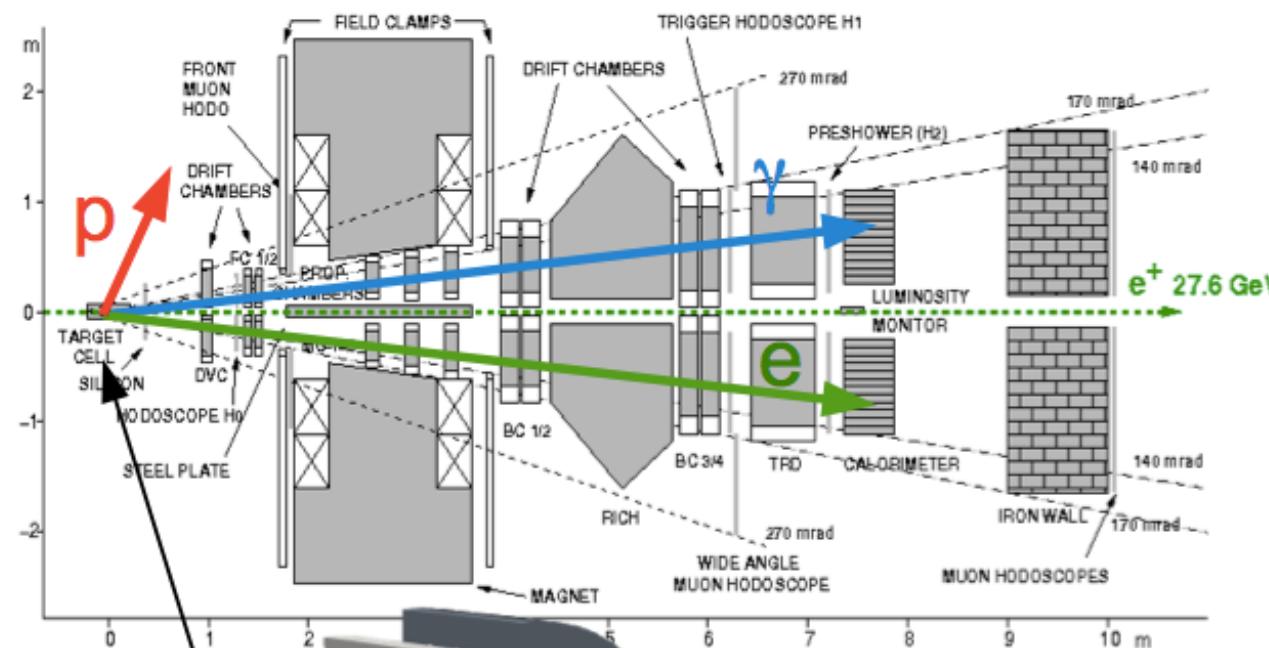
Nucl. Phys. B 842 (2011) 265

double spin (LL) asymmetry

JHEP 06 (2010) 019

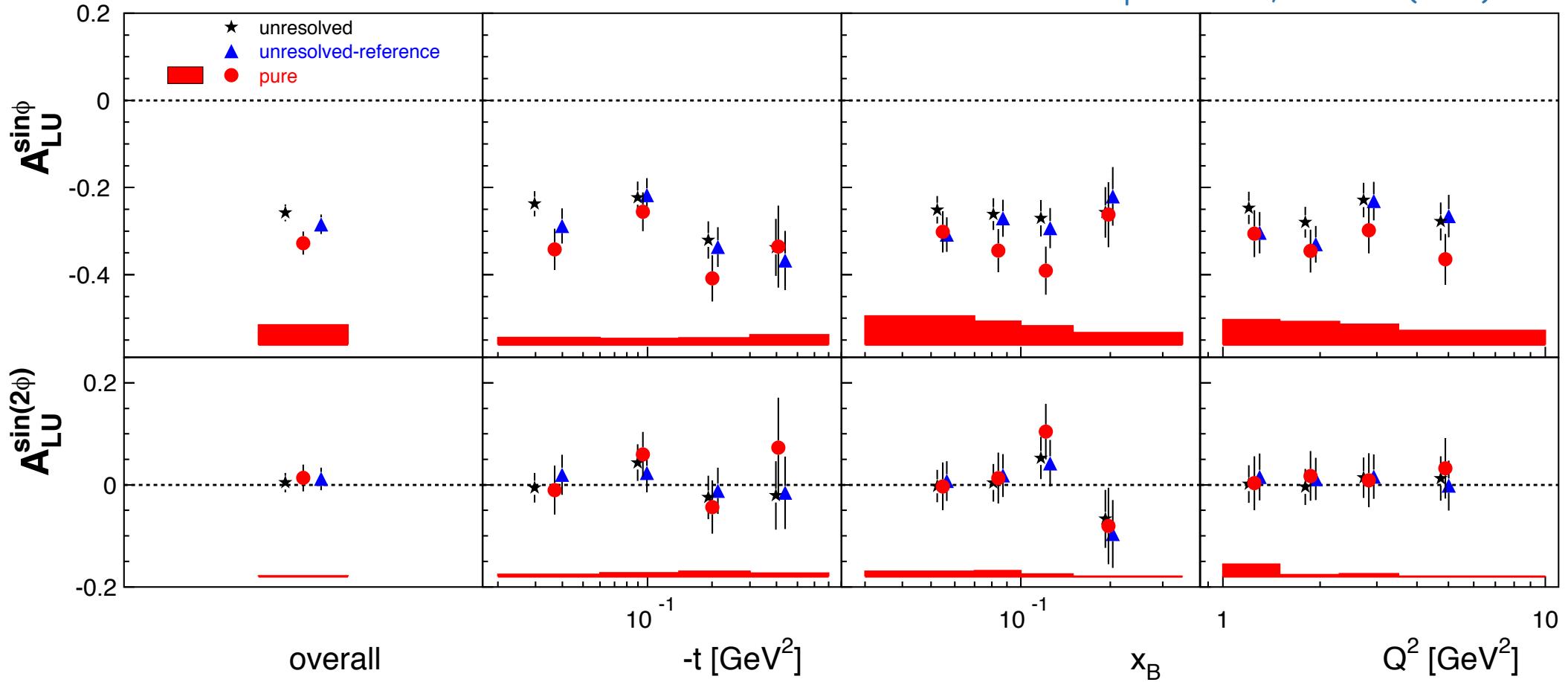
Nucl. Phys. B 842 (2011) 265

# DVCS/BH complete event reconstruction



# Beam-helicity asymmetry

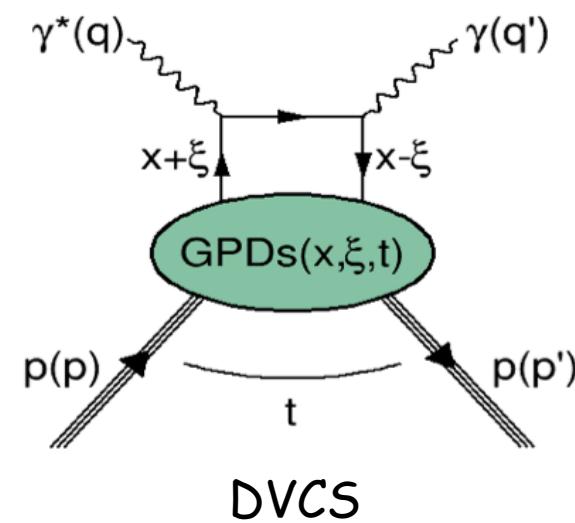
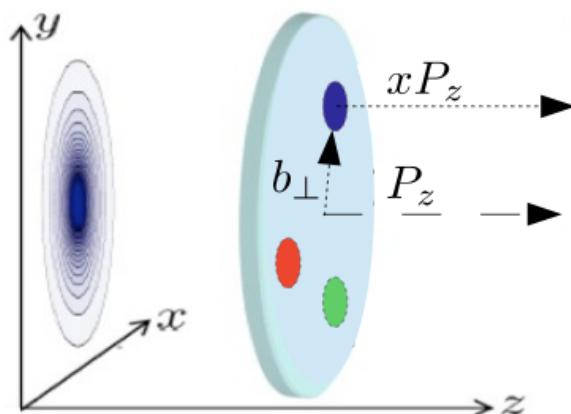
A. Airapetian et al, JHEP 10 (2012) 042



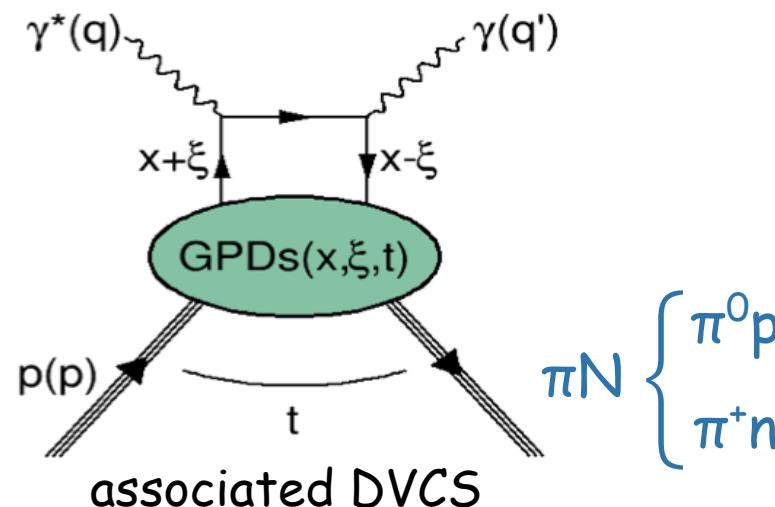
- additional 1.96% scale uncertainty from beam polarization
- leading asymmetry from pure sample is larger

# Beam-helicity asymmetry in $e p \rightarrow e \gamma \pi N$ in $\Delta$ -resonance region

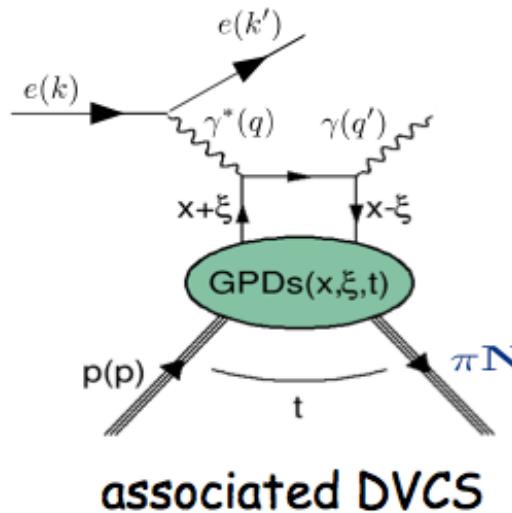
GPDs: quark distribution in longitudinal-momentum and transverse-position space



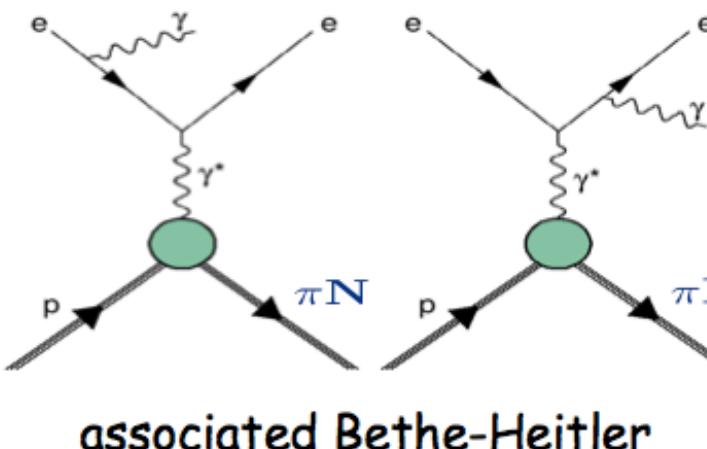
transition GPDs  $p \rightarrow \pi N$



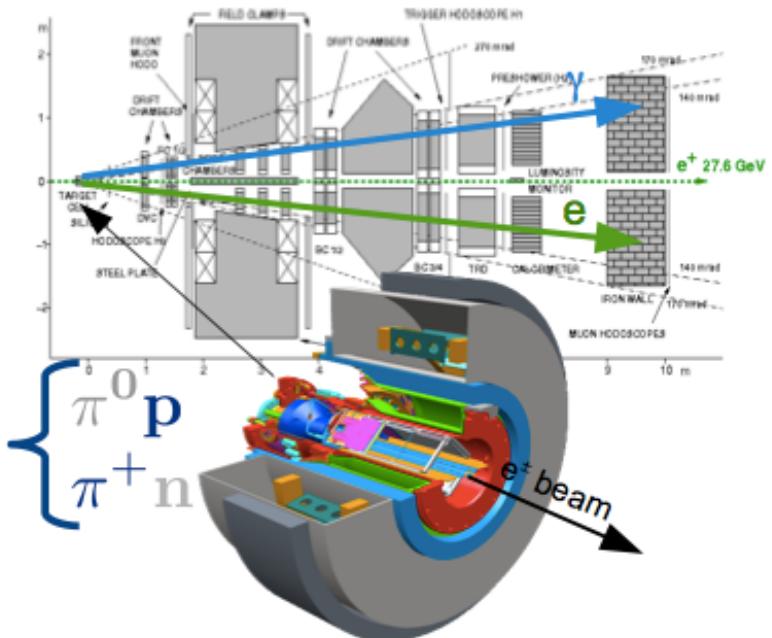
# Beam-helicity asymmetry in $e p \rightarrow e \gamma \pi N$ in $\Delta$ -resonance region



associated DVCS

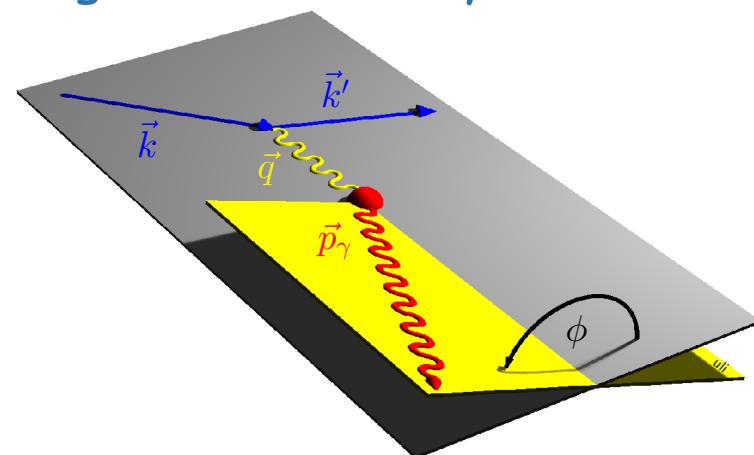


associated Bethe-Heitler



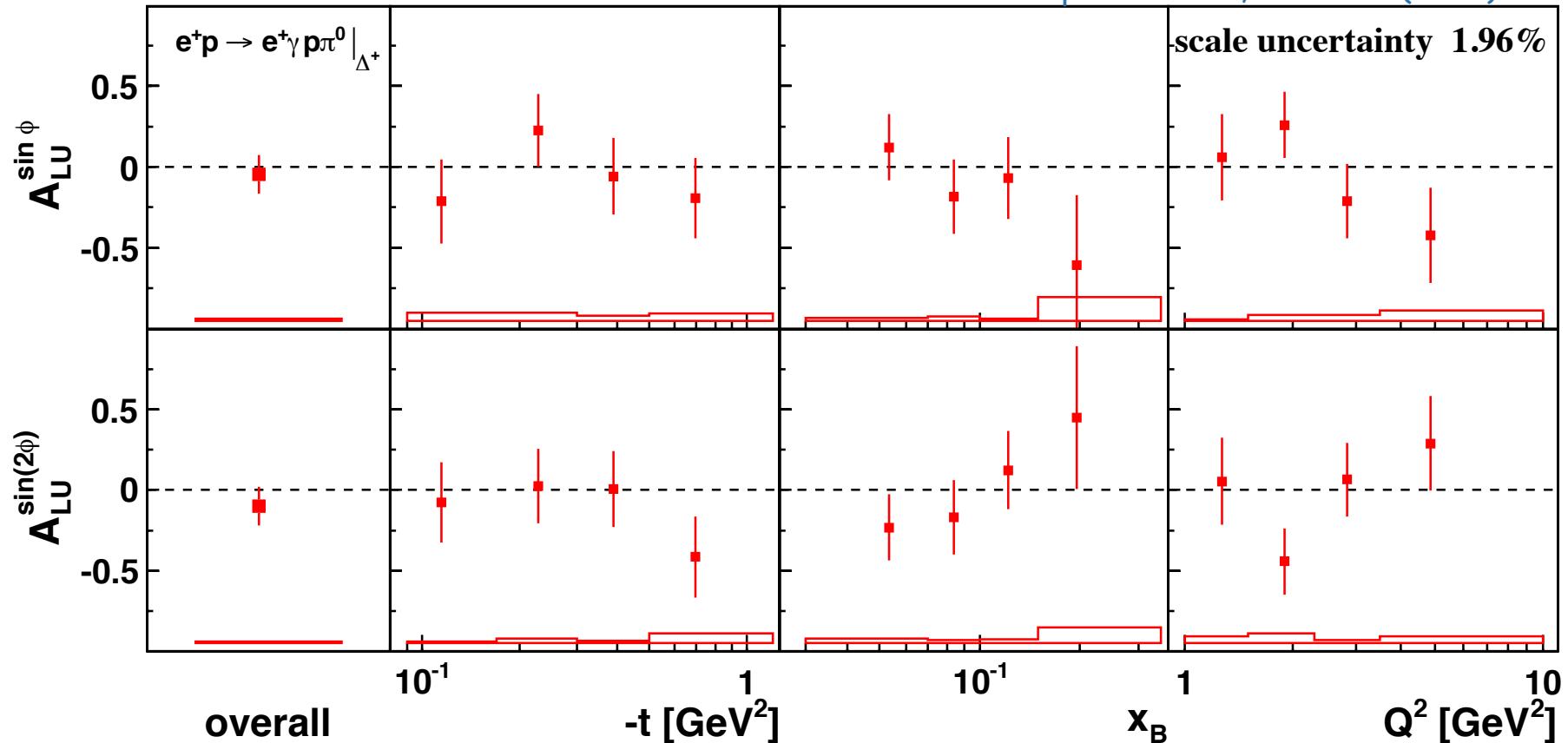
recoil detector

- $p$  and  $\pi^+$  via PID
- $\pi^0$  and  $n$  undetected
- kinematic fitting
- select region around  $\Delta$ -resonance



# Beam-helicity asymmetry in $e p \rightarrow e \gamma \pi^0 p$ in $\Delta$ -resonance region

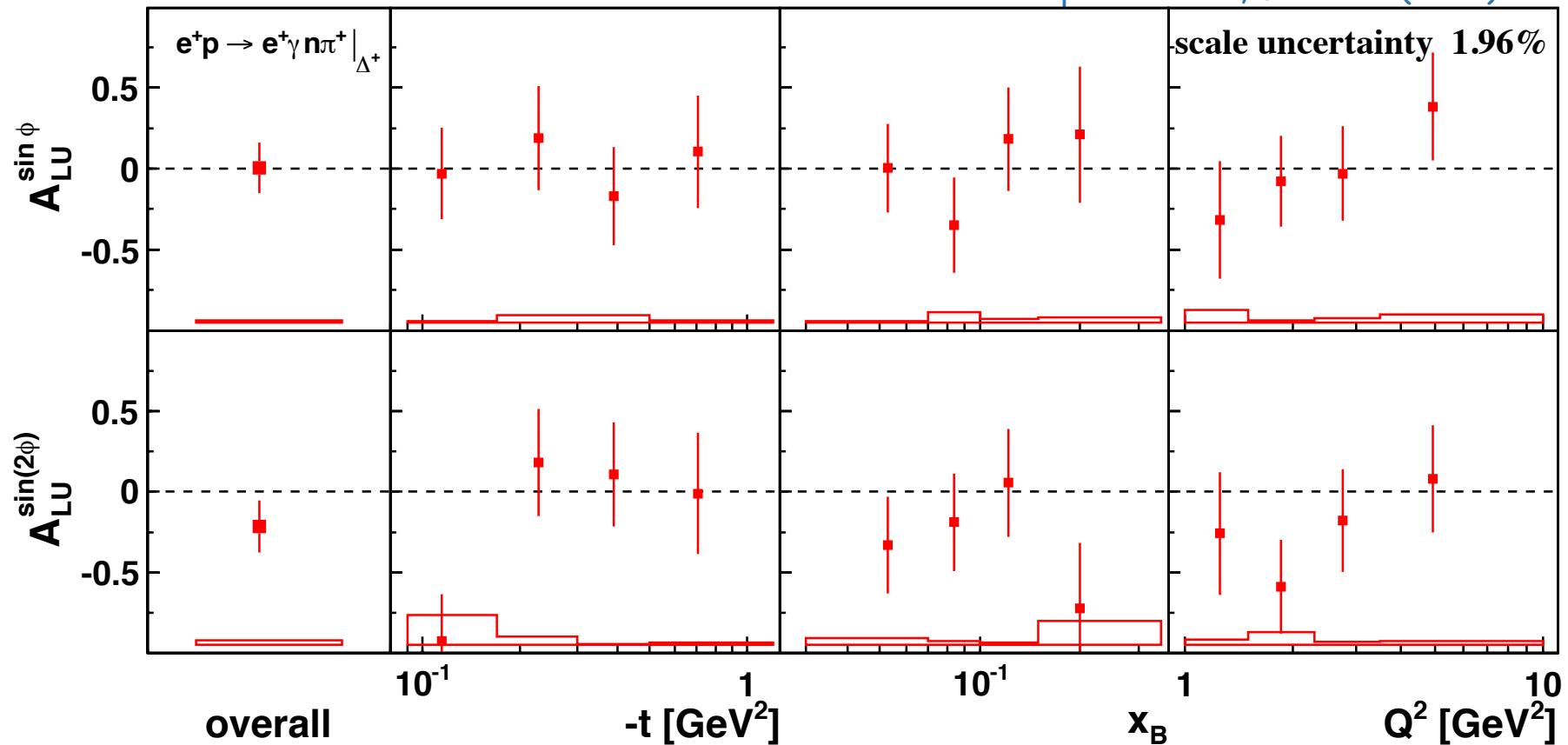
A. Airapetian et al., JHEP 01 (2014) 077



- asymmetry background correction from SIDIS (11%) and  $e p \rightarrow e \gamma p$  (4.6%)
- leading asymmetry consistent with zero

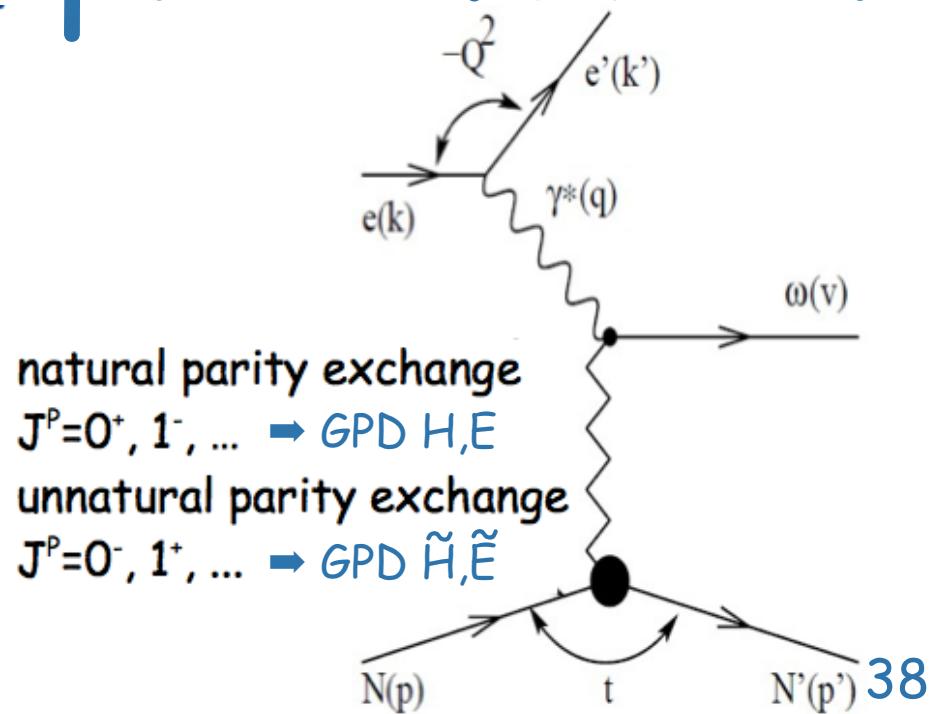
# Beam-helicity asymmetry in $e^+p \rightarrow e^+\gamma\pi^+n$ in $\Delta$ -resonance region

A. Airapetian et al., JHEP 01 (2014) 077



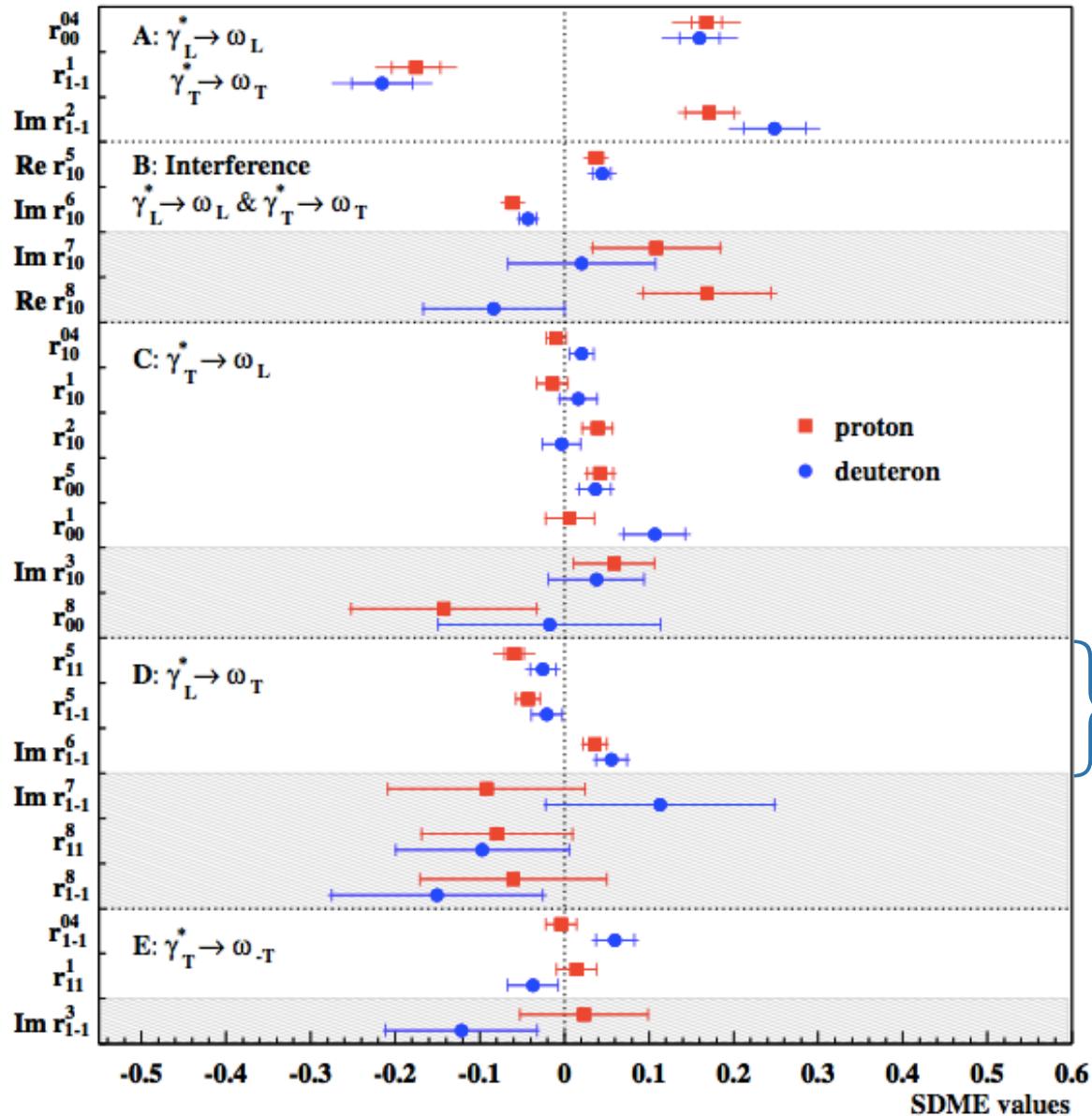
- asymmetry background correction from SIDIS (23%) and  $e^+p \rightarrow e^+p$  (0.2%)
- leading asymmetry consistent with zero

# Exclusive $\omega$ production



# Exclusive $\omega$ production

A. Airapetian et al., arXiv:1407.2119

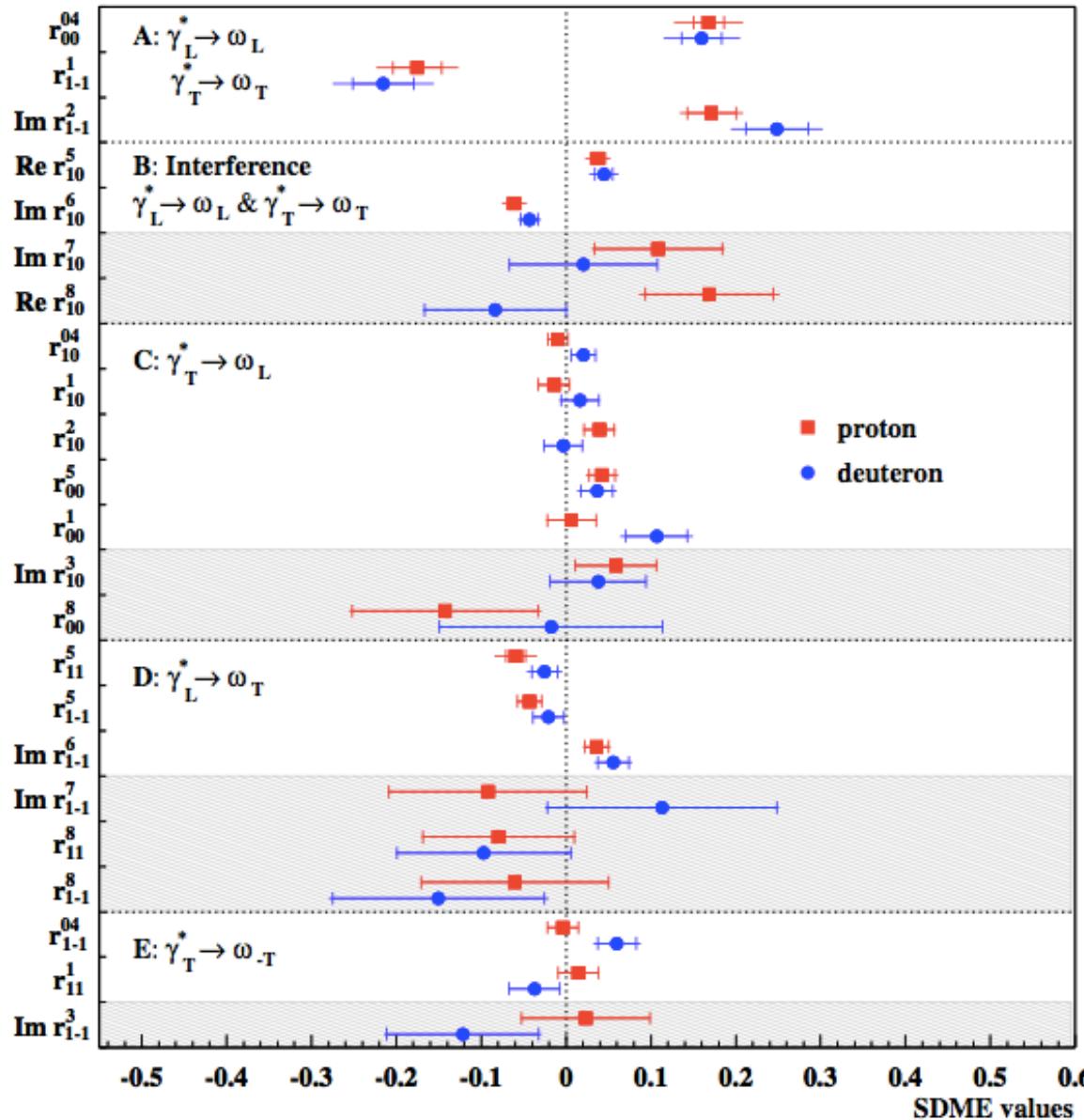


- SDMEs compatible for proton and deuteron
- slight violation of s-channel helicity conservation

$$\begin{aligned}
 r_{11}^5 + r_{1-1}^5 - \Im r_{1-1}^6 \\
 = -0.14 \pm 0.02 \pm 0.04 \\
 = -0.10 \pm 0.03 \pm 0.03
 \end{aligned}$$

# Exclusive $\omega$ production

A. Airapetian et al., arXiv:1407.2119



•  $\omega$ - $\rho^0$  comparison:

- $\omega$ :  $r_{1-1}^1 < 0$
- $\rho^0$ :  $r_{1-1}^1 > 0$

•  $\omega$ :  $\Im r_{1-1}^2 > 0$

•  $\rho^0$ :  $\Im r_{1-1}^2 < 0$

large unnatural parity  
exchange for  $\omega$  production

exclusive  $\rho^0$ :

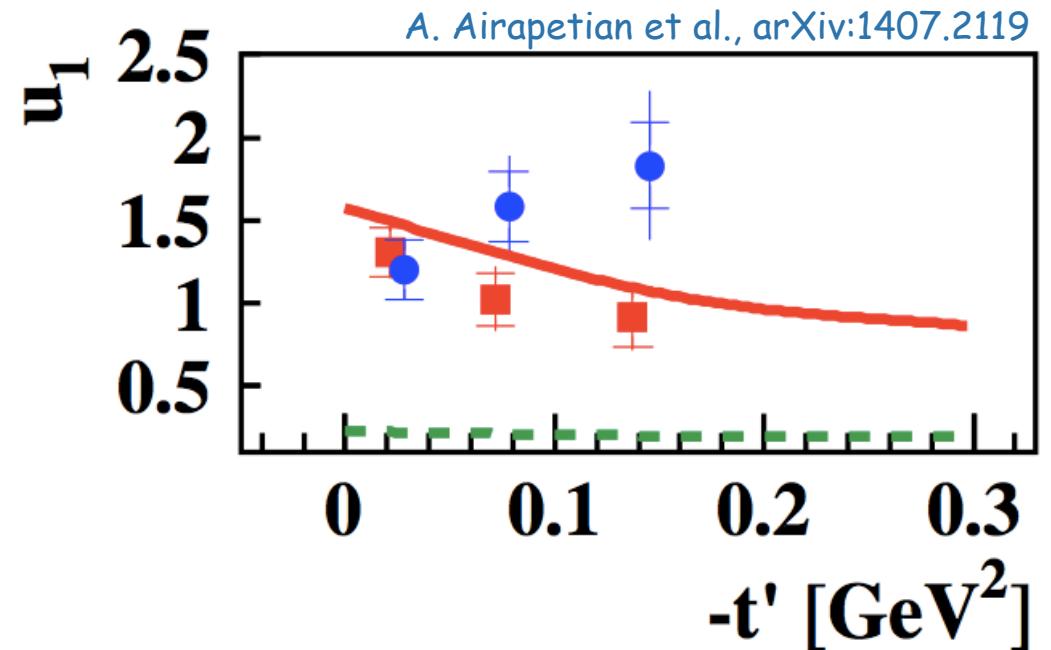
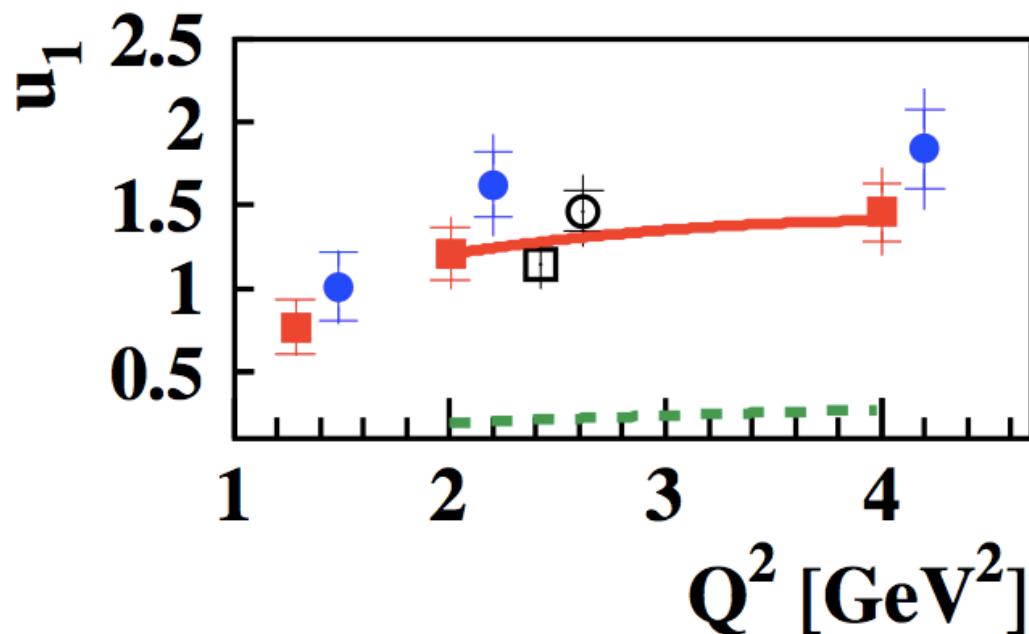
A. Airapetian et al., Eur. Phys. J. C 62 (2009) 659

# Exclusive $\omega$ production

- test of unnatural parity exchange:

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$$

$$\propto 2\epsilon|U_{10}|^2 + |U_{11} + U_{-11}|^2$$



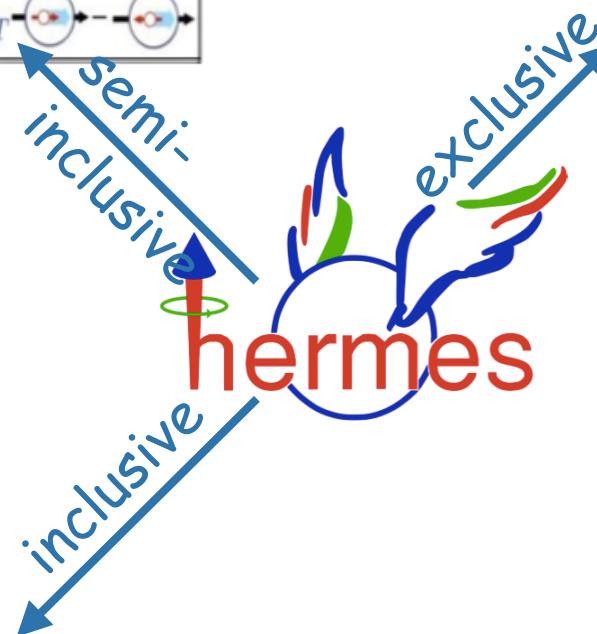
- large unnatural parity exchange
- model for protons - S. Goloskokov and P. Kroll, arXiv. 1407.1141:
  - without pion-pole contribution
  - with pion-pole contribution

# transverse momentum distributions (TMDs)

$P_{h\perp}$  dependence:  
PRD 87 (2013) 074029

		quark	
		L	T
nucleon	U	$f_1$	
L		$g_1$	
T		$g_{1T}^\perp$	
		$h_1$	
		$h_{1L}^\perp$	
		$h_{1T}^\perp$	

PRL 94 (2005) 012002  
PRL 103 (2009) 152002

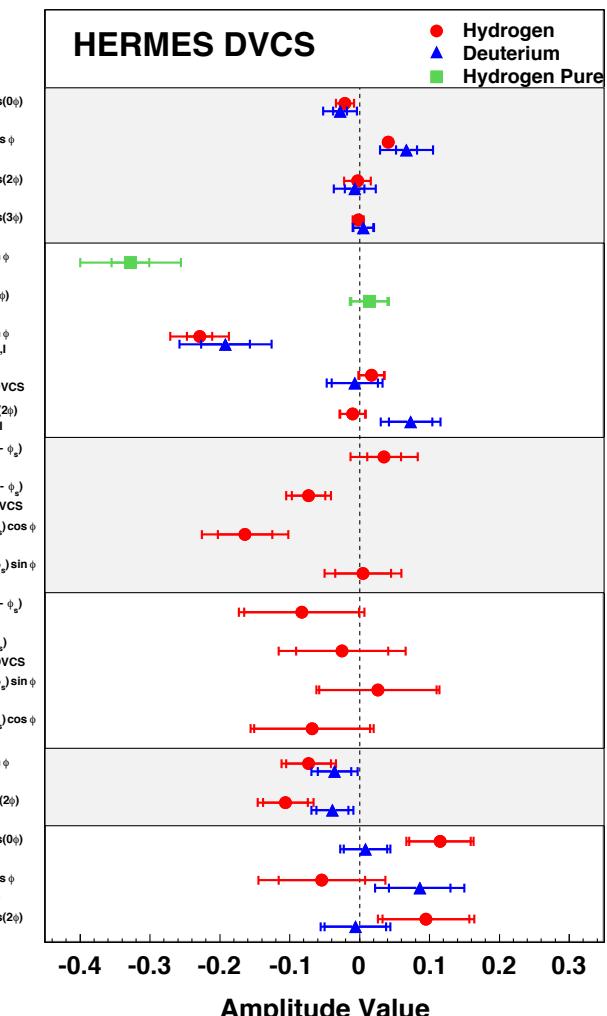


→  $g_2$  - EPJ C 72 (2012) 1921

→  $A_{UT}$  - Phys. Lett. B 728 (2014) 183-190

# Summary

exclusive w production  
arXiv:1407.2119



Back up

# Hadron multiplicities: VM fractions

