

# Study of the spin structure at HERMES

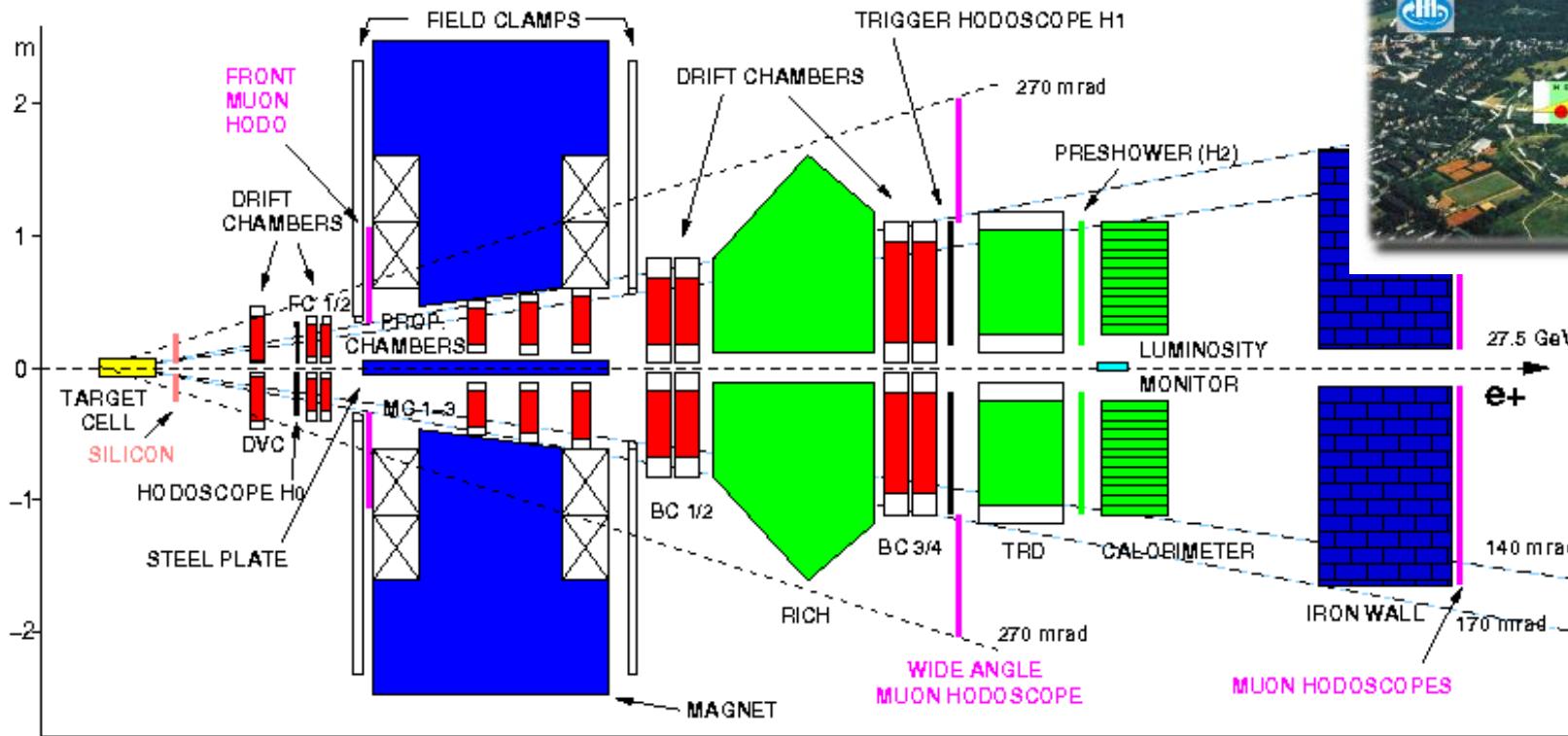
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University of the Basque Country

Frontiers and Careers in Photonuclear Physics  
August 7-9, 2014  
Cambridge MA

# Outline

- The HERMES experiment
- The proton in 3D: generalized parton distributions
- Charge separated single-spin asymmetries
- The proton in 3D: transverse-momentum-dependent parton distributions
- Single-spin asymmetries in semi-inclusive DIS on a transversely polarised target
- Spin-independent non-collinear cross section

# The HERMES experiment



data taking from  
1995 until 2007

## Beam

longitudinally polarised  $e^+$  &  $e^-$

$E=27.6 \text{ GeV}$

## Gaseous internal target

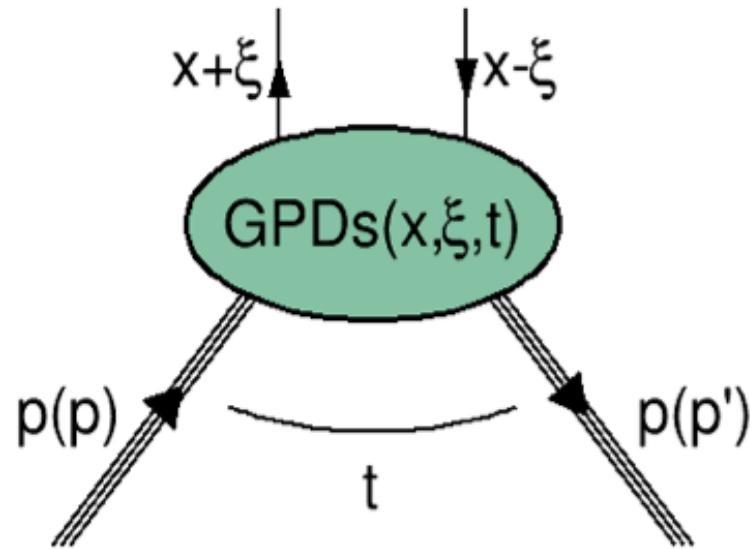
transversely polarised H

longitudinally polarised H, De, He  
unpolarised H, De, He, Ne, Kr, Xe

## Particle identification

- lepton-hadron PID:  
high-efficiency (>98%) &  
low contamination (<1%)
- hadron PID via RICH 2-15 GeV

# Generalized Parton Distributions (GPDs)



$x$ =average longitudinal momentum fraction  
 $2\xi$ =average longitudinal momentum transfer  
 $t$ =squared momentum transfer to nucleon

four quark helicity-conserving GPDs at twist-2

$$H^q(x, \xi, t)$$

$$E^q(x, \xi, t)$$

spin independent

$$\tilde{H}^q(x, \xi, t)$$

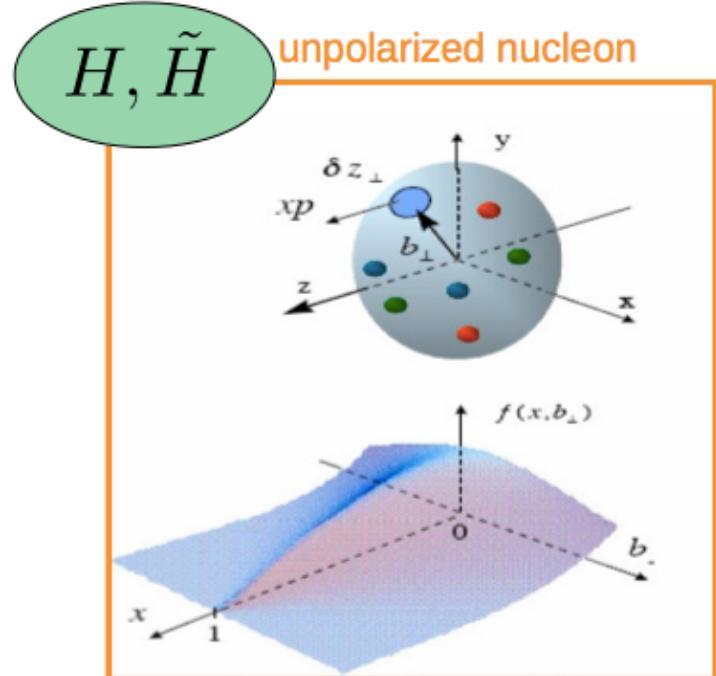
$$\tilde{E}^q(x, \xi, t)$$

spin dependent

proton-helicity non-flip

proton-helicity flip

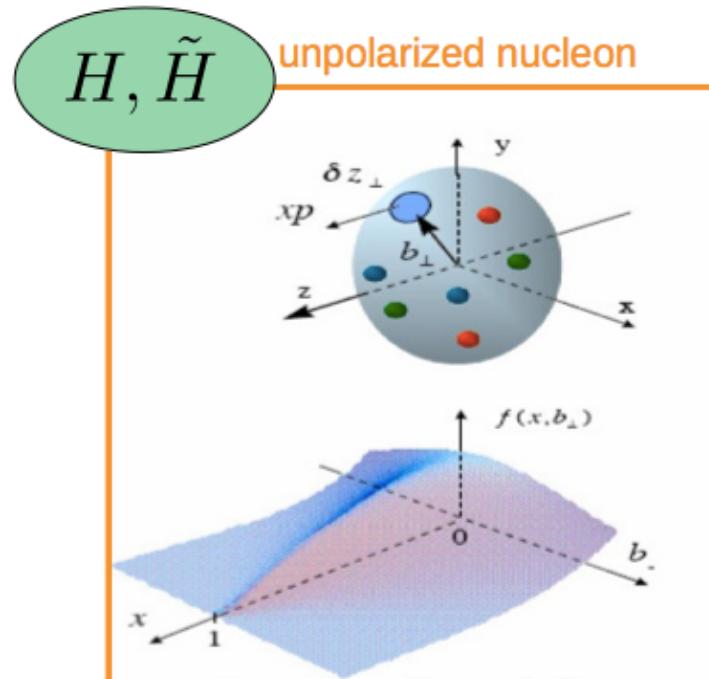
# Generalized Parton Distributions (GPDs)



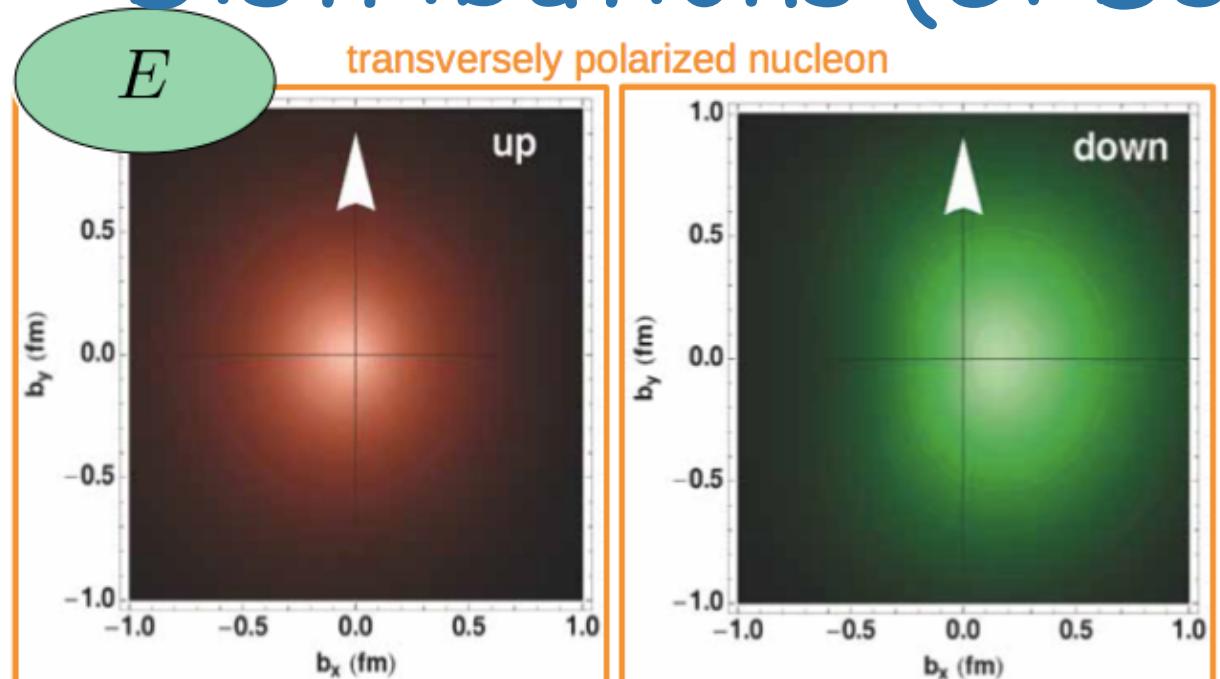
helicity-(in)dependent probability distribution  
of quarks as a function of their longitudinal  
fractional momentum and transverse position

M. Burkardt, Phys. Rev. D 62 (2000) 071503

# Generalized Parton Distributions (GPDs)



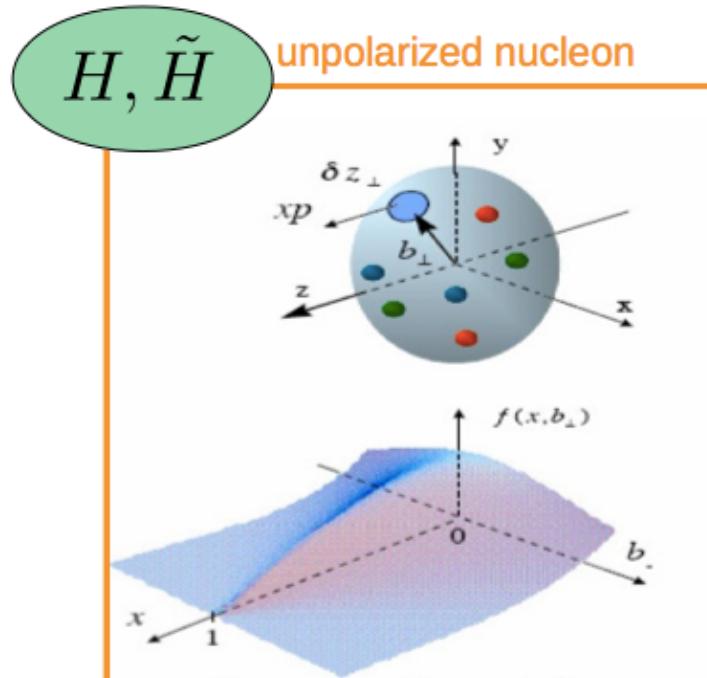
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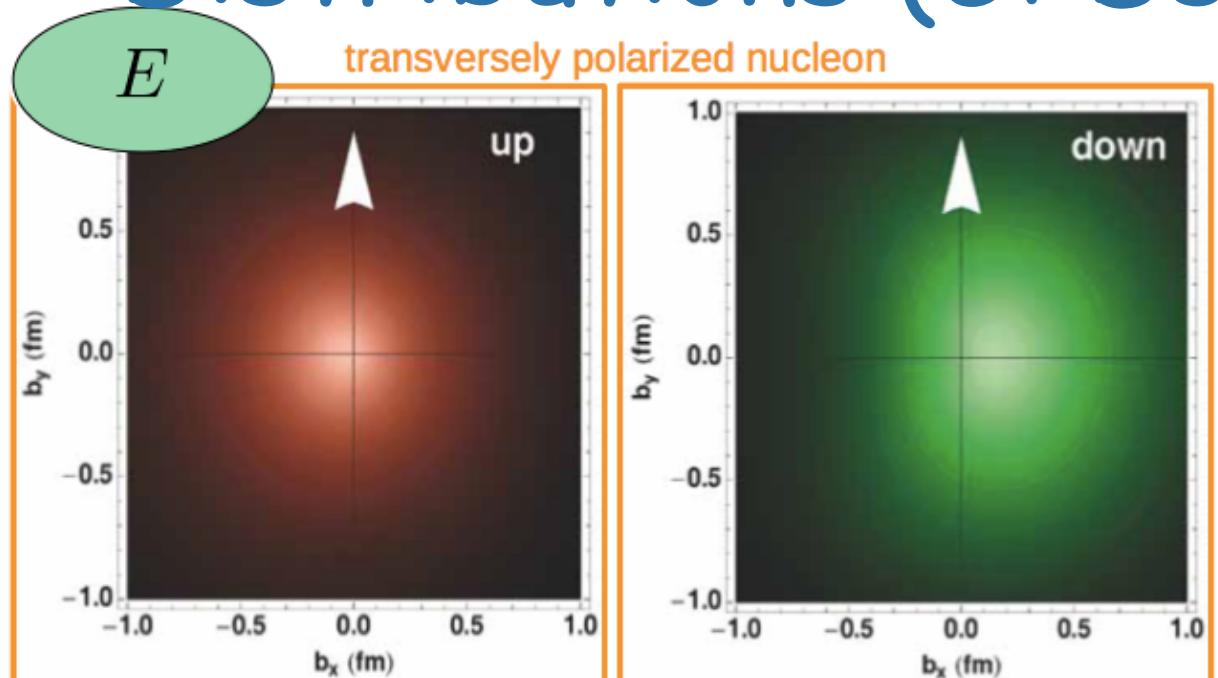
pictures taken from A. Bacchetta and M. Contalbrigo, Il Nuovo Saggiatore **28** (2012) 1-2

distortion of quark probability distribution  
compared to unpolarized nucleon  
M. Burkardt, Phys. Rev. D **66** (2002) 114005

# Generalized Parton Distributions (GPDs)



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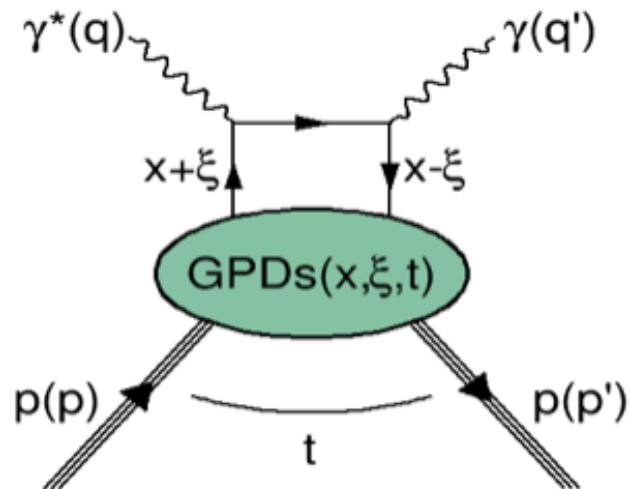
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$$J^q = \lim_{t \rightarrow 0} \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)] \rightarrow \text{quark orbital angular momentum}$$

X. Ji, Phys. Rev. Lett. **78** (1997) 610

# Deeply virtual Compton scattering (DVCS)

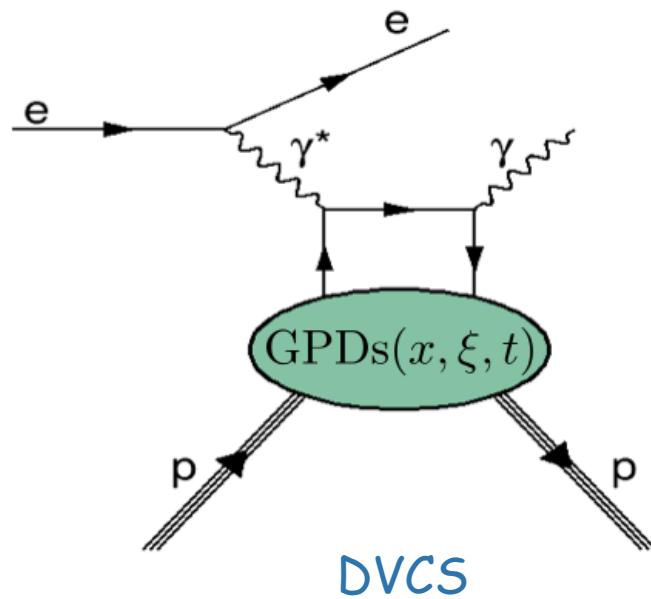


$$Q^2 \equiv -q^2$$

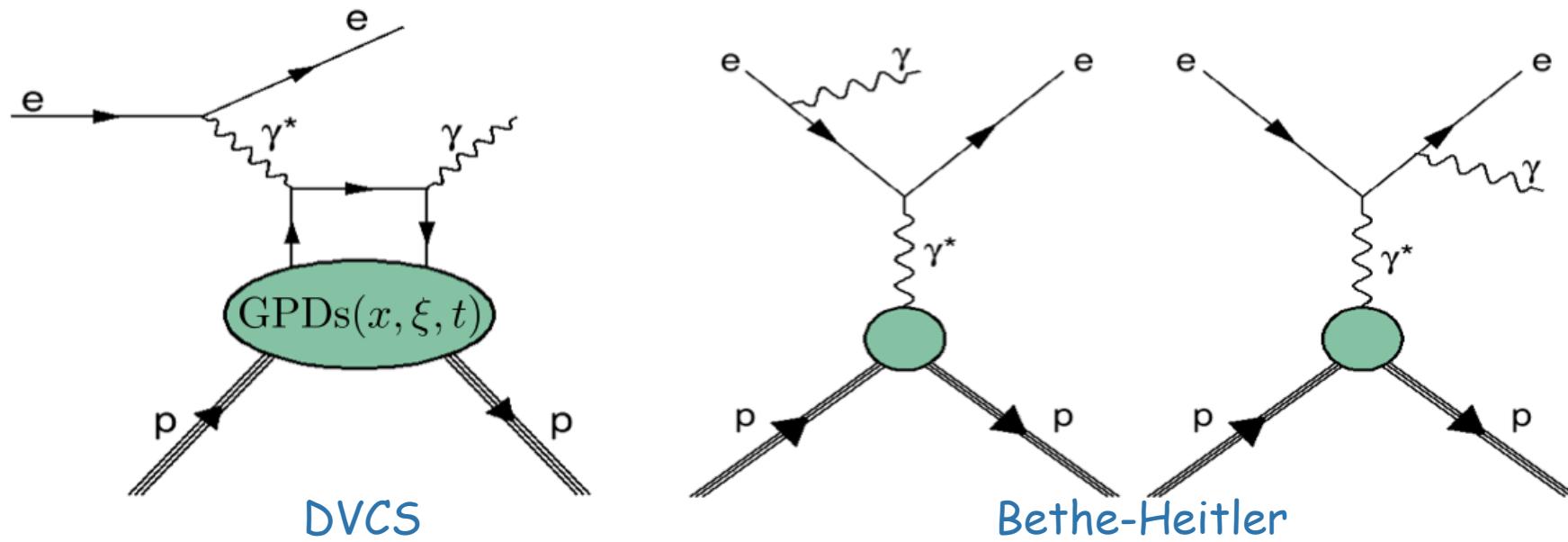
$$x_B \equiv \frac{Q^2}{2pq}$$

$$\xi \approx \frac{x_B}{2 - x_B}$$

# Exclusive lepto-production of real photons



# Exclusive lepto-production of real photons

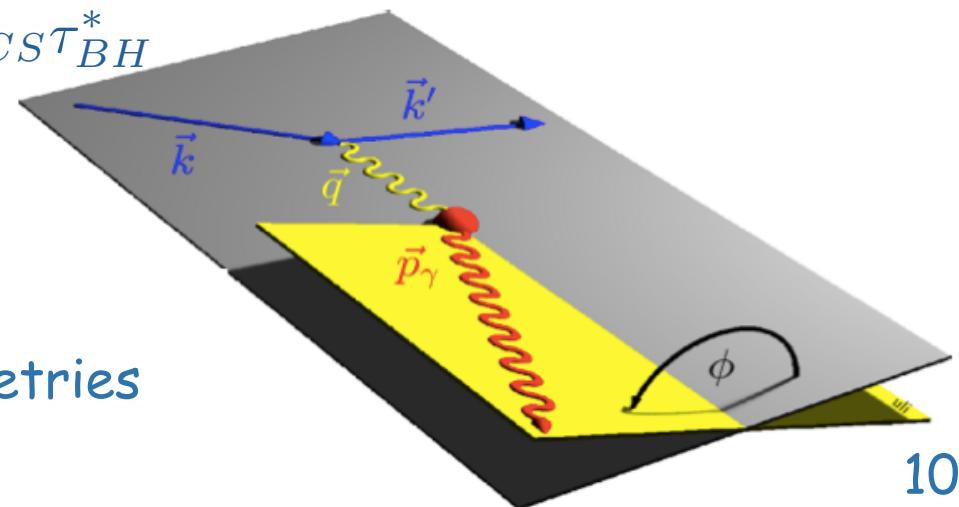


$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{BH} \tau_{DVCS}^* + \tau_{DVCS} \tau_{BH}^*$$

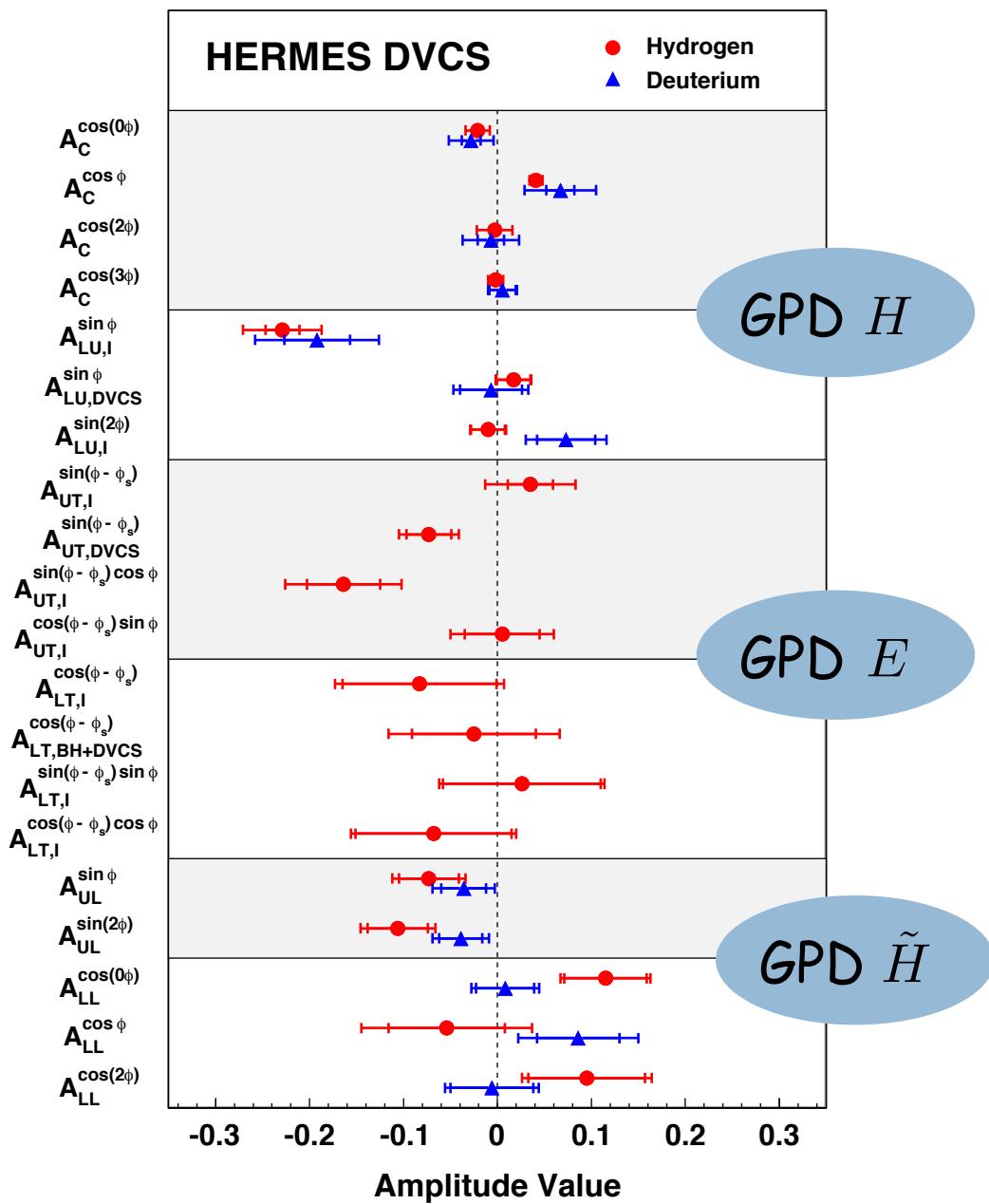
$|\tau_{BH}|$  calculable with knowledge form factors

$|\tau_{BH}| \gg |\tau_{DVCS}|$  at HERMES

interference term through azimuthal asymmetries



# DVCS at HERMES



beam-charge asymmetry

JHEP 07 (2012) 32

Nucl. Phys. B 829 (2010) 1

beam-helicity asymmetry

JHEP 07 (2012) 32

Nucl. Phys. B 829 (2010) 1

transverse target-spin asymmetry

JHEP 06 (2008) 066

double spin (LT) asymmetry

Phys. Lett. B 704 (2011) 15

longitudinal target-spin asymmetry

JHEP 06 (2010) 019

Nucl. Phys. B 842 (2011) 265

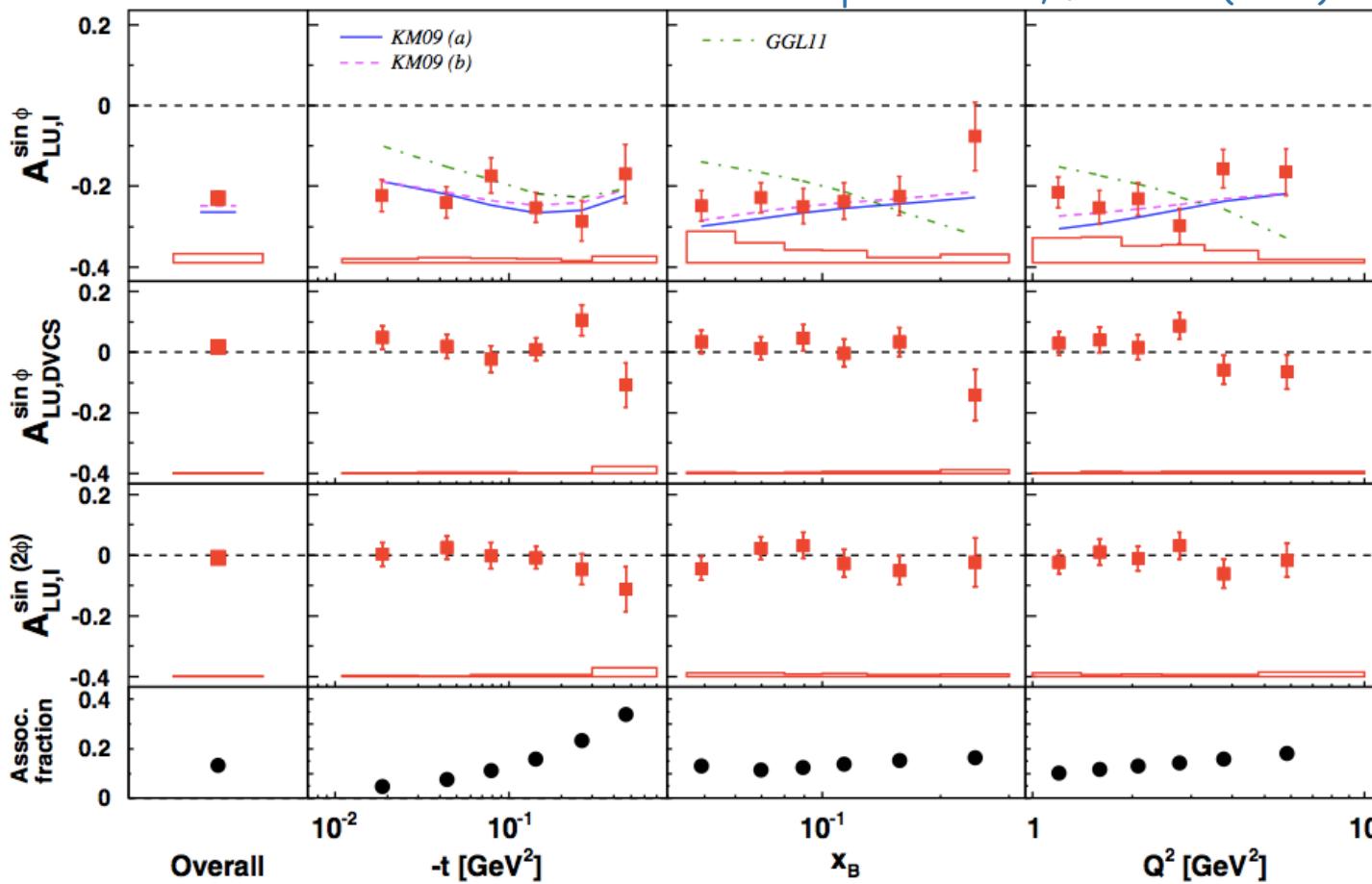
double spin (LL) asymmetry

JHEP 06 (2010) 019

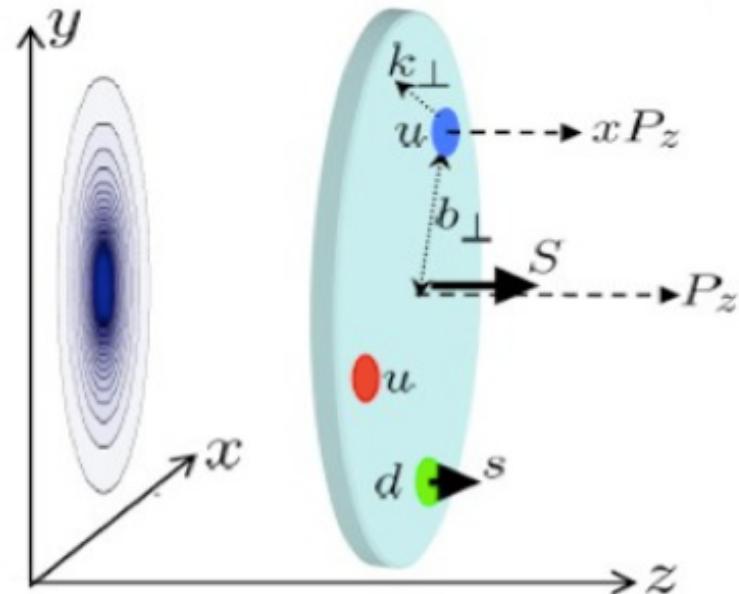
Nucl. Phys. B 842 (2011) 265

# Charge-separated beam-helicity asymmetry

A. Airapetian et al., JHEP 07 (2012) 32



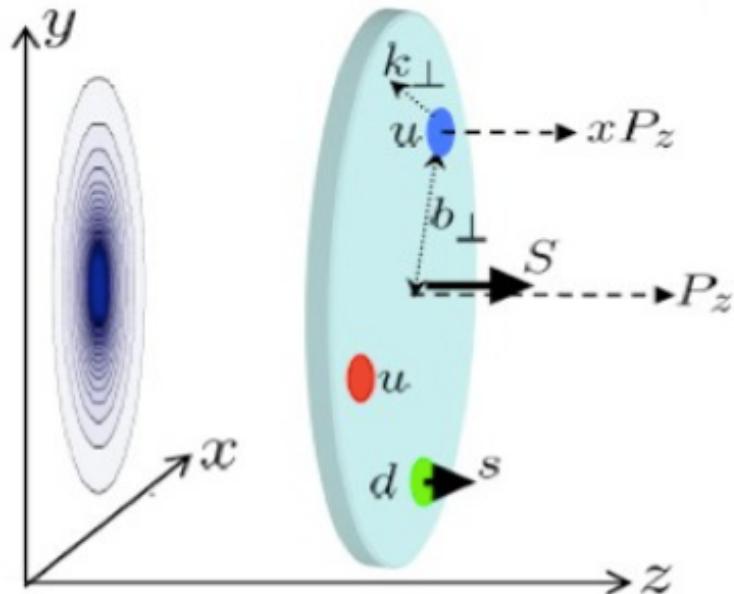
KM09: Nucl. Phys. B **841** (2010) 1:  
fit to HERMES, ZEUS, H1 data  
Fit to HERMES, ZEUS, H1,  
Jefferson Lab data  
  
GGL11:  
Phys. Rev. D **84** (2011) 034007



$$W(x, \vec{k}_T, \vec{b}_\perp)$$

Generalized parton distributions

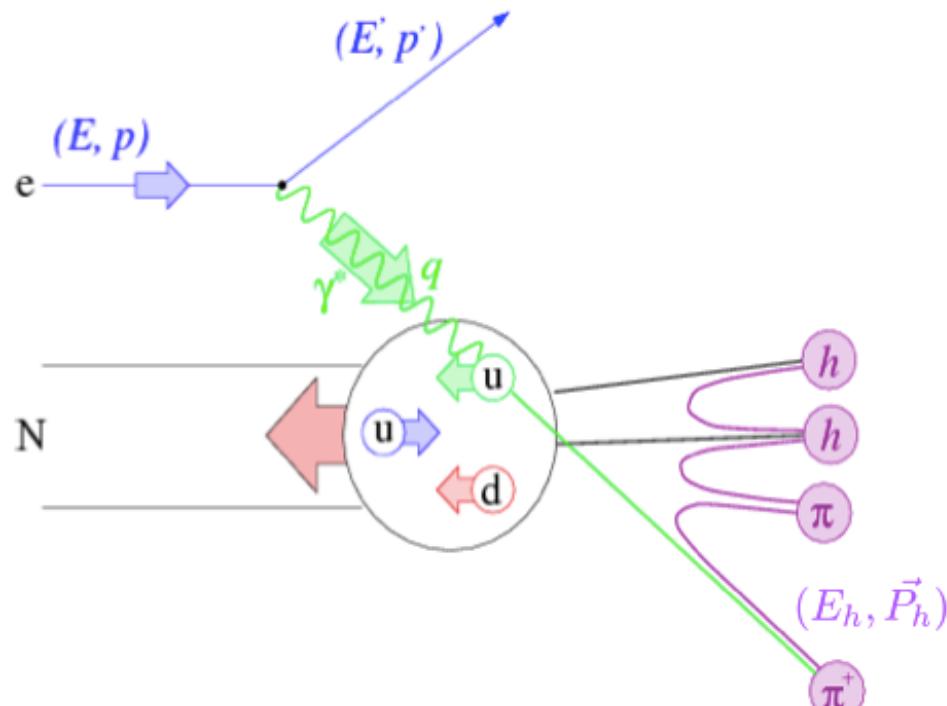
$$\int d^2 \vec{k}_T W(x, \vec{k}_T, \vec{b}_\perp) = \text{GPDs } (x, \xi, t)$$



Generalized parton distributions  
 $\int d^2 \vec{k}_T W(x, \vec{k}_T, \vec{b}_\perp) = \text{GPDs } (x, \xi, t)$

Transverse-momentum-dependent  
 parton distribution functions  
 $\int d^2 \vec{b}_\perp W(x, \vec{k}_T, \vec{b}_\perp) = \text{TMD PDFs } (x, \vec{k}_T)$

# Semi-inclusive deep-inelastic scattering



$$Q^2 = -q^2$$

$$\nu \stackrel{lab}{=} E - E'$$

$$W^2 = M_N^2 + 2M_N\nu - Q^2$$

$$y \stackrel{lab}{=} \frac{\nu}{E}$$

$$x_B \stackrel{lab}{=} \frac{Q^2}{2M_N\nu}$$

$$z \stackrel{lab}{=} \frac{E_h}{\nu} \quad P_{h\perp} = \frac{|\vec{q} \times \vec{P}_h|}{|\vec{q}|}$$

$$\sigma^{ep \rightarrow eh} = \sum_q DF^{p \rightarrow q}(x_B, p_T^2, Q^2) \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}(z, k_T^2, Q^2)$$

Distribution functions (DFs): distribution of quarks in nucleon

Fragmentation functions (FFs): fragmentation of struck quark into final-state hadron

$p_T$ : intrinsic transverse momentum of struck quark

$k_T$ : transverse momentum of struck quark acquired during fragmentation

# Transverse-momentum-dependent distributions (TMDs)

TMD PDFs

$$f_1 = \text{yellow circle with blue dot}$$

$$g_{1L} = \text{yellow circle with blue dot and horizontal arrow pointing right}$$

$$h_{1T} = \text{yellow circle with blue dot and vertical arrow pointing up}$$

$$f_{1T}^\perp = \text{yellow circle with blue dot and vertical arrow pointing up}$$

$$h_1^\perp = \text{yellow circle with blue dot and vertical arrow pointing down}$$

$$h_{1L}^\perp = \text{yellow circle with blue dot and horizontal arrow pointing right}$$

leading twist

TMD FFs

$$D_1 = \text{yellow circle with blue dot}$$

$$G_{1L} = \text{yellow circle with blue dot and horizontal arrow pointing right}$$

$$H_{1T} = \text{yellow circle with blue dot and vertical arrow pointing up}$$

$$D_{1T}^\perp = \text{yellow circle with blue dot and vertical arrow pointing up}$$

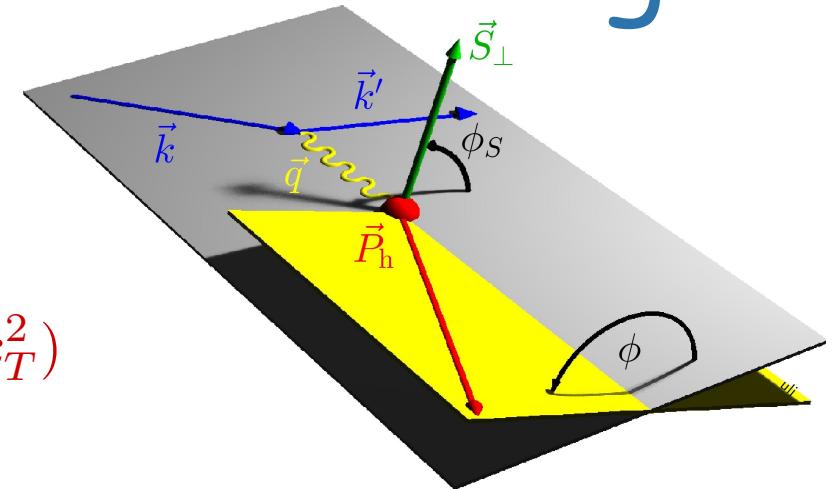
$$H_1^\perp = \text{yellow circle with blue dot and vertical arrow pointing down}$$

$$H_{1L}^\perp = \text{yellow circle with blue dot and horizontal arrow pointing right}$$

# Single-spin asymmetries on a transversely polarised target

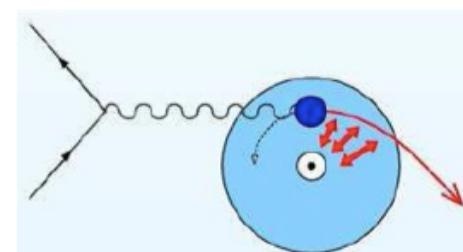
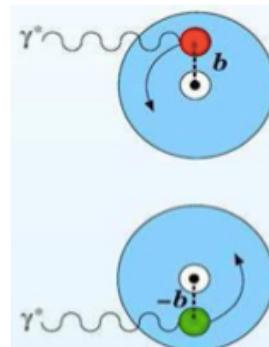
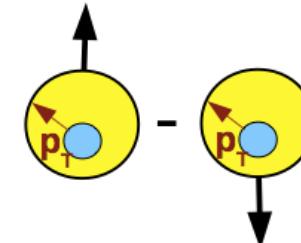
$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

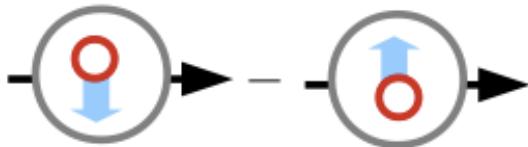
$$\propto \sin(\phi - \phi_S) \sum_q e_q \frac{\vec{p}_T \cdot \hat{P}_{h\perp}}{M_h} f_{1T}^{\perp, q}(x_B, p_T^2) \otimes D_1^q(z, k_T^2)$$



Sivers distribution function  $f_{1T}^{\perp, q}(x_B, p_T^2, Q^2)$

- requires non-zero quark orbital angular momentum
- naive-T-odd
- FSI left-right (azimuthal) asymmetry in direction of outgoing hadron

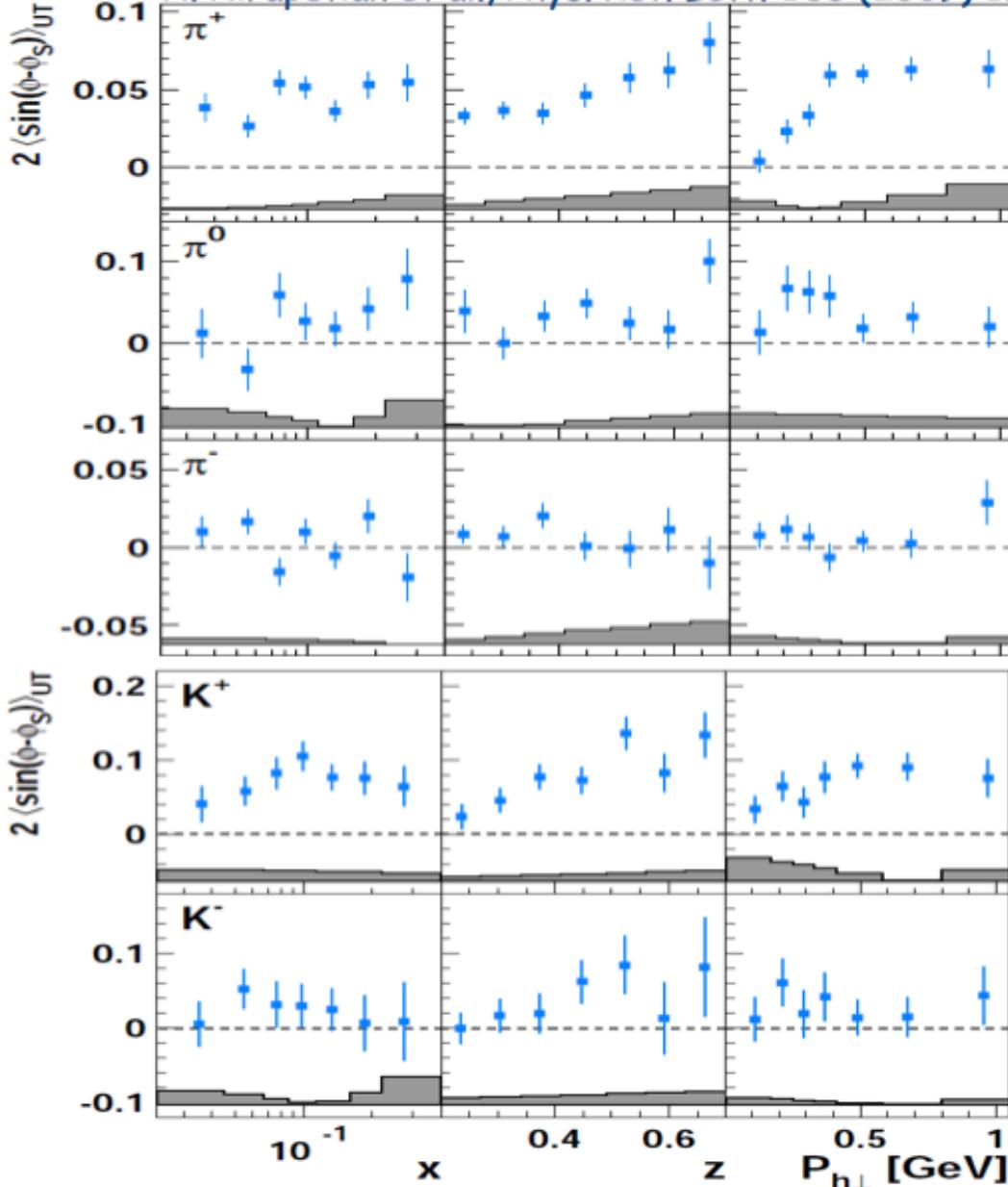




# Sivers amplitude

$$F_{UT}^{\sin(\phi_h - \phi_S)} \propto f_{1T}^\perp \otimes D_1$$

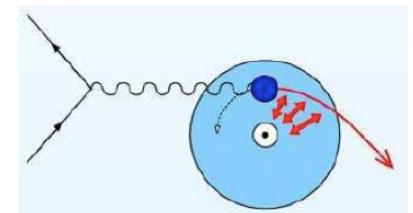
A. Airapetian et al., Phys. Rev. Lett. 103 (2009) 152002



- $\pi^+$  significantly positive  
→ orbital angular momentum
- u-quark dominance for  $\pi^+$  amplitude

$$\approx -\frac{f_{1T}^{\perp,u}(x, k_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, p_T^2)}{f_1^u(x, k_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, p_T^2)}$$

→  $f_{1T}^{\perp,u}(x, k_T^2) < 0$



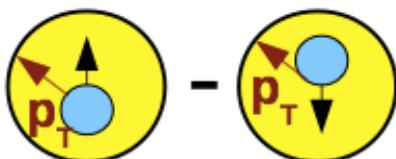
- $\pi^-$ : u- and d-quark cancelation  
→  $f_{1T}^{\perp,d}(x, k_T^2) > 0$

# Non-collinear spin-independent semi-inclusive DIS cross section

$$\frac{d\sigma}{dx_B dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{x_B y Q^2} \left( 1 + \frac{\gamma^2}{2x_B} \right) (A(y) F_{UU,T} + B(y) F_{UU,L} + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h})$$

$$F_{UU}^{\cos 2\phi_h} = -\frac{2(\hat{P}_{h\perp} \cdot \vec{p}_T)(\hat{P}_{h\perp} \cdot \vec{k}_T) - \vec{p}_T \cdot \vec{k}_T}{M_h M} h_1^\perp \otimes H_1^\perp$$

Boer-Mulders DF  $h_1^\perp$



- chiral odd
- naïve-T-odd

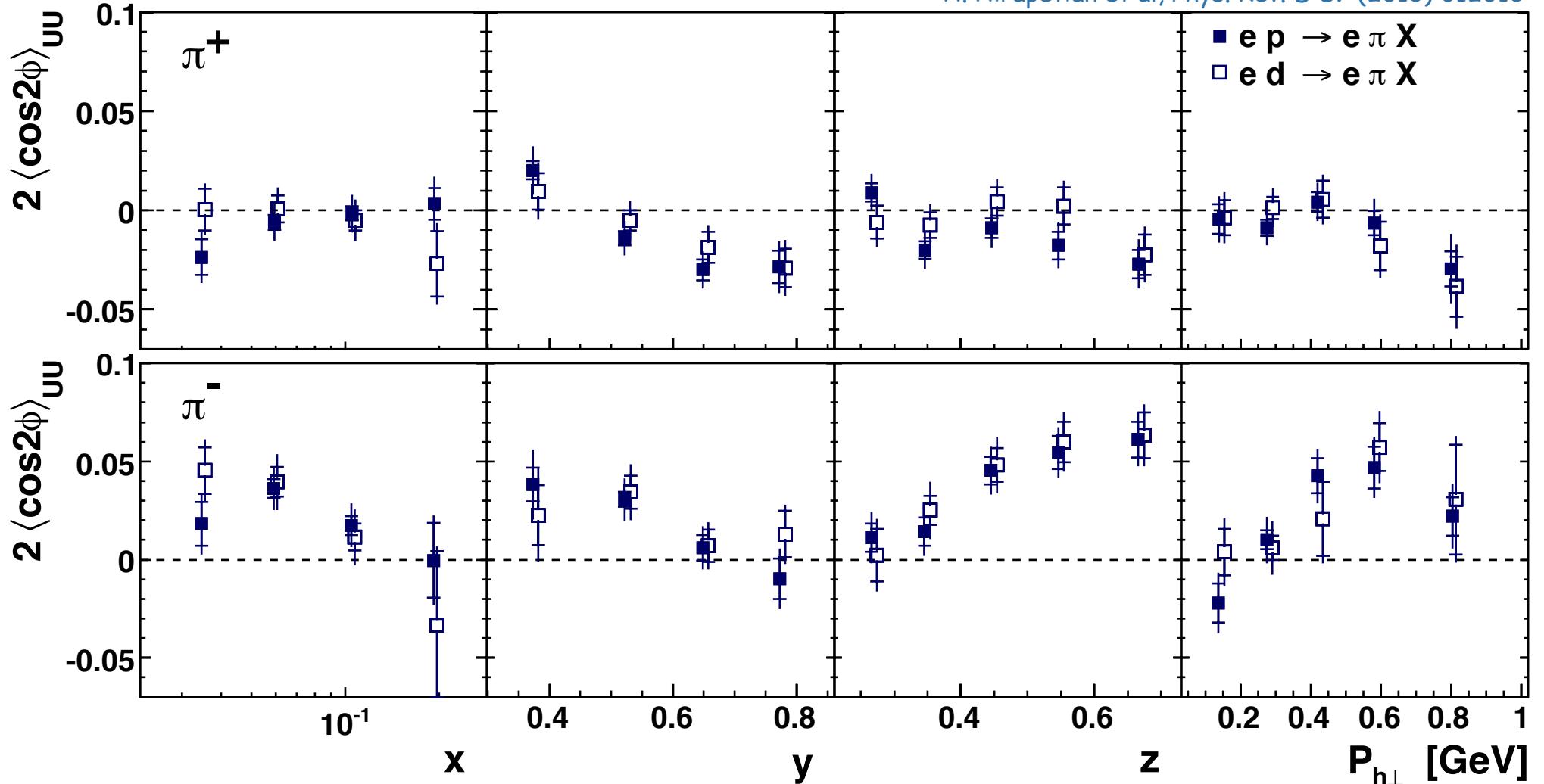


Collins FF  $H_1^\perp$

- chiral odd
- naïve-T-odd

# Results for pions

A. Airapetian et al, Phys. Rev. D 87 (2013) 012010

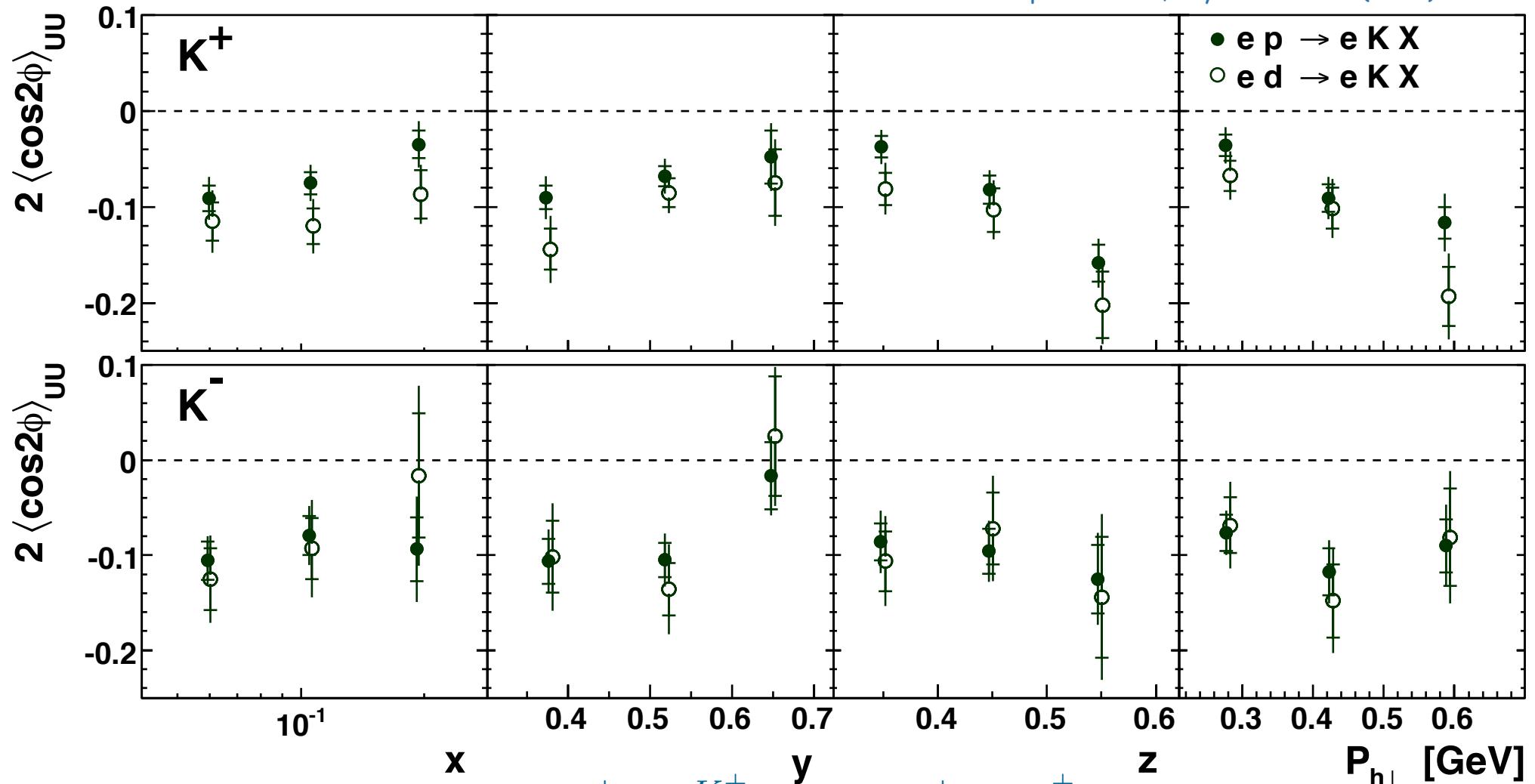


- H-D comparison:  $h_1^{\perp,u} \approx h_1^{\perp,d}$

- $\pi^- > 0 \leftrightarrow \pi^+ \leq 0 : H_1^{\perp,fav} \approx H_1^{\perp,unfav}$

# Results for kaons

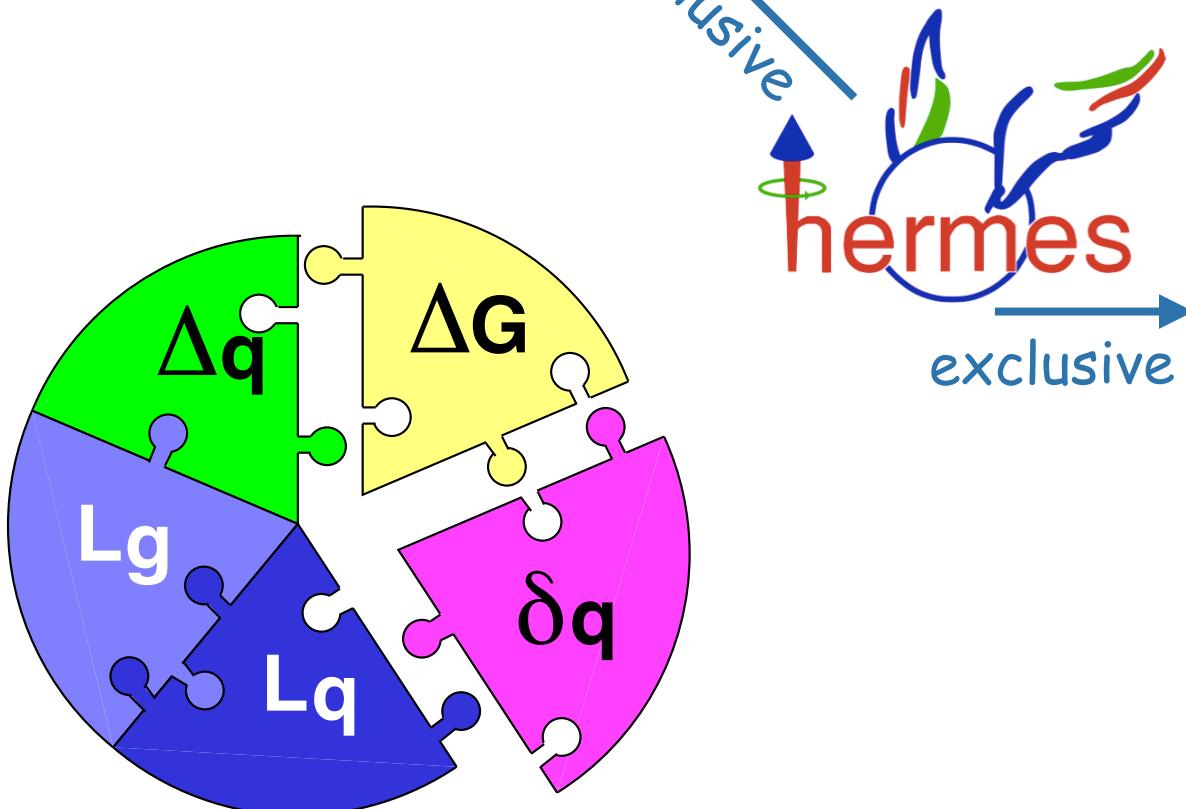
A. Airapetian et al, Phys. Rev. D 87 (2013) 012010



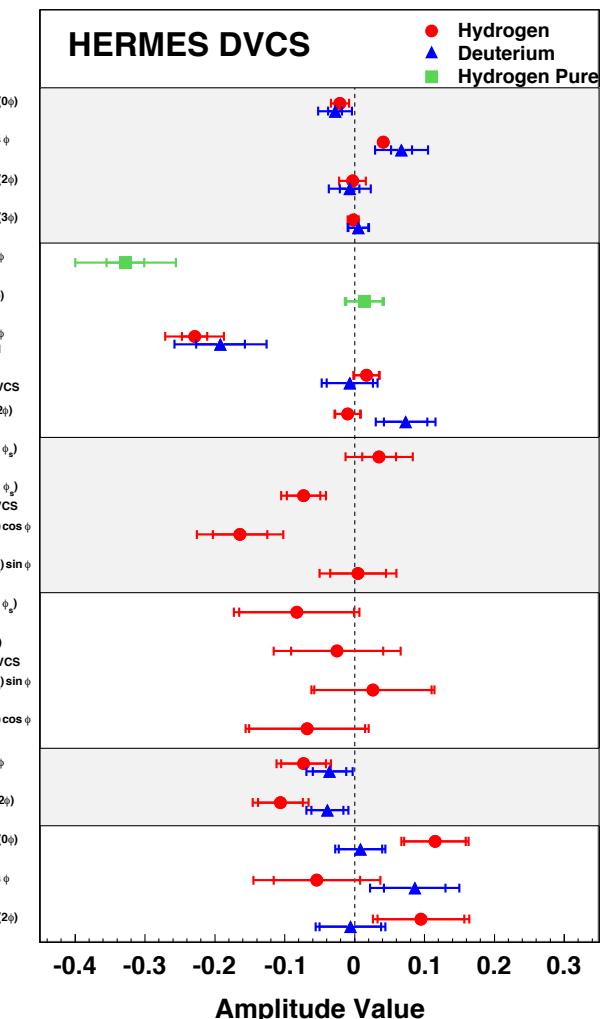
- $K^+ < 0$ : Artru model:  $\text{sign } H_1^{\perp, u \rightarrow K^+} = \text{sign } H_1^{\perp, u \rightarrow \pi^+}$
- $K^+ \approx K^-$ :  $u$  dominance  $\xrightarrow{?} H_1^{\perp, u \rightarrow K^+} = H_1^{\perp, u \rightarrow K^-}$ ; role of sea quarks? 21

## transverse momentum distributions (TMDs)

		quark		
		U	L	T
nucleon	U	$f_1$		
	L		$g_1$	
	T	$f_{1T}^\perp$		$g_{1T}^\perp$

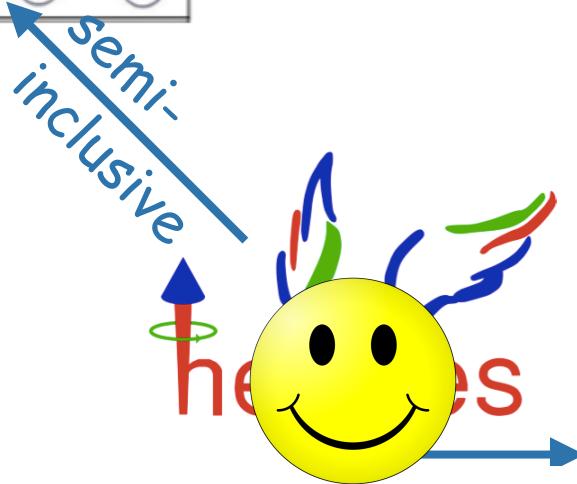
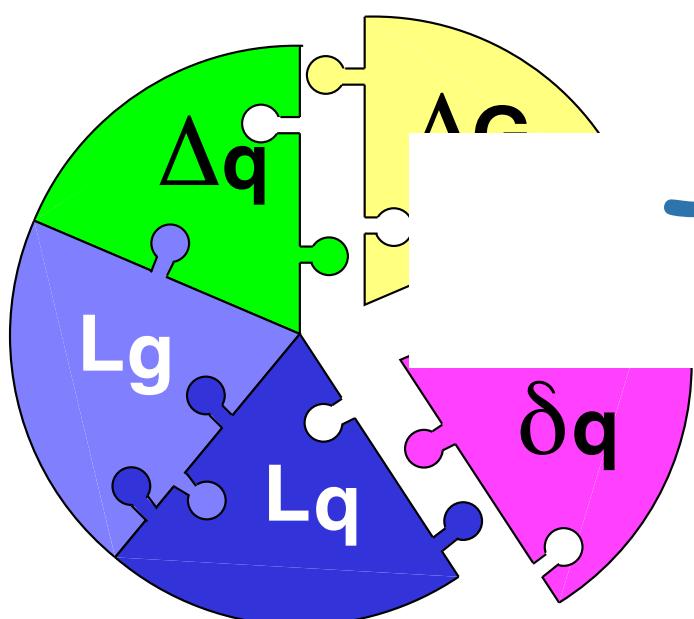


# Summary



## transverse momentum distributions (TMDs)

		quark		
		U	L	T
nucleon	U	$f_1$		$h_1^\perp$
	L		$g_1$	$h_{1L}^\perp$
	T	$f_{1T}^\perp$	$g_{1T}^\perp$	$h_{1T}^\perp$



# Thank you

# Summary

