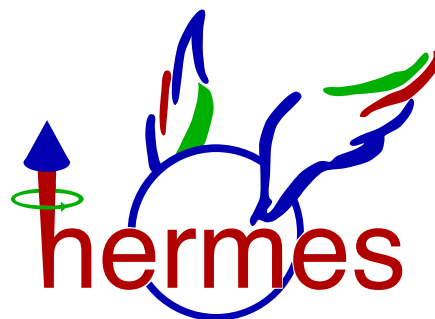


GPD's @ HERMES

Aram Movsisyan

Yerevan Physics Institute

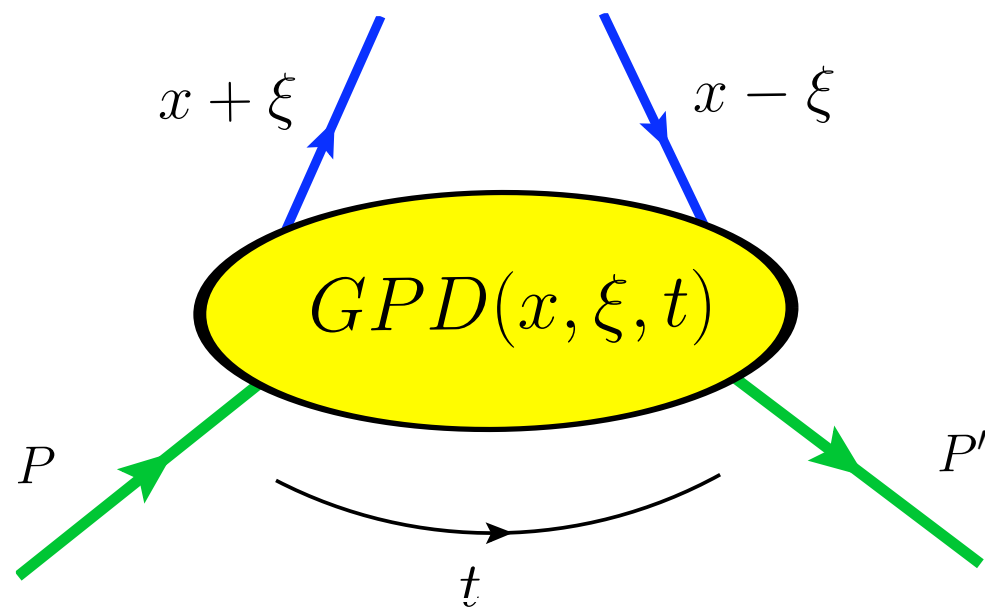


for the HERMES collaboration

QNP Palaiseau, France, 19.04.2012

GPDs describe the nucleon structure in terms of quark and gluon degrees of freedom

Correlation between transverse position and longitudinal momentum fraction of quark in the nucleon



Relation to total angular momentum (Ji relation):

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x (H_q(x, \xi, t) + E_q(x, \xi, t))$$

Form Factors:

Transverse distribution of quarks in space coordinate.

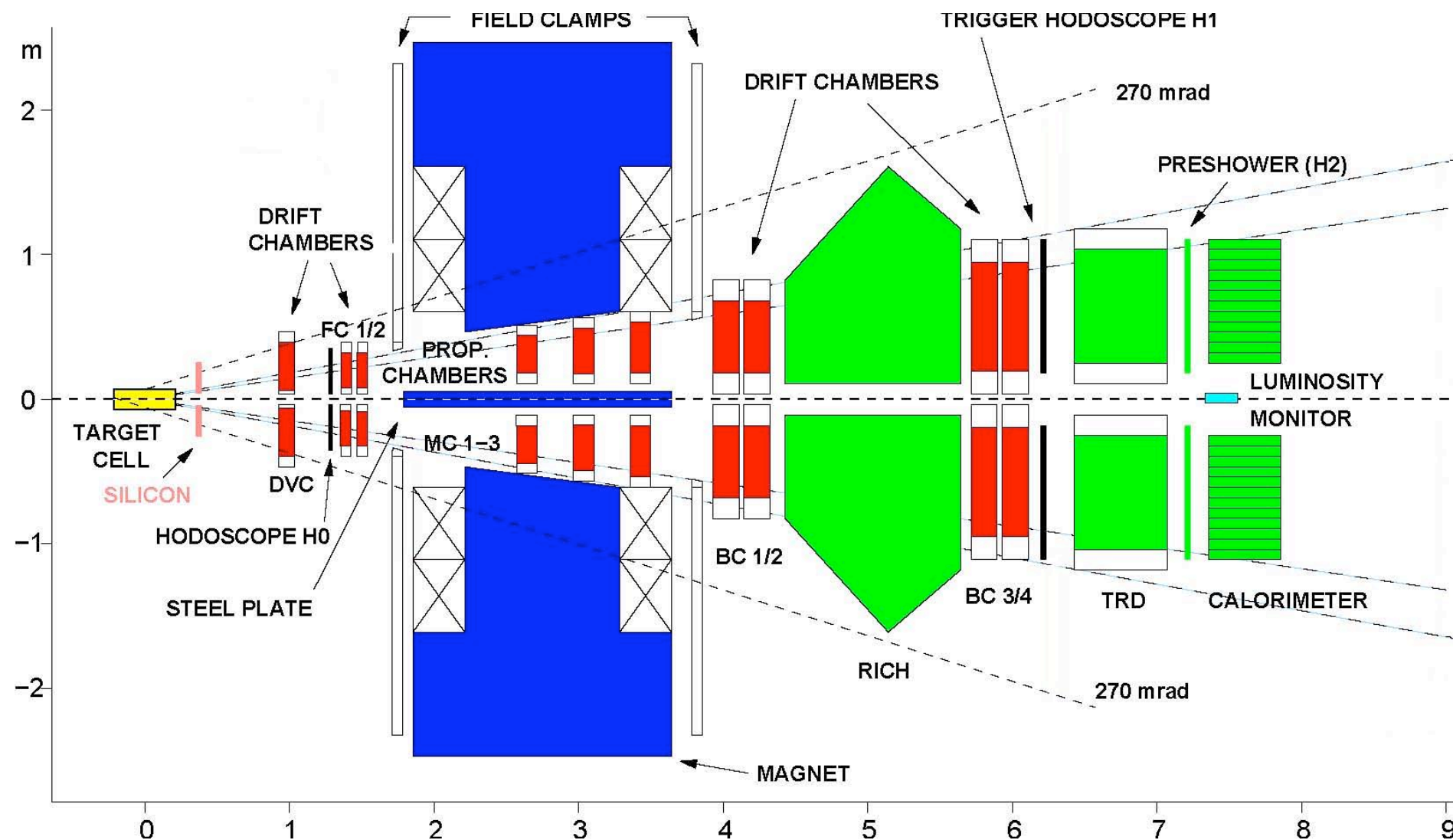
$$F(t) = \int dx^* GPD(x, \xi, t)$$

PDFs:

Quark longitudinal momentum fraction in the nucleon.

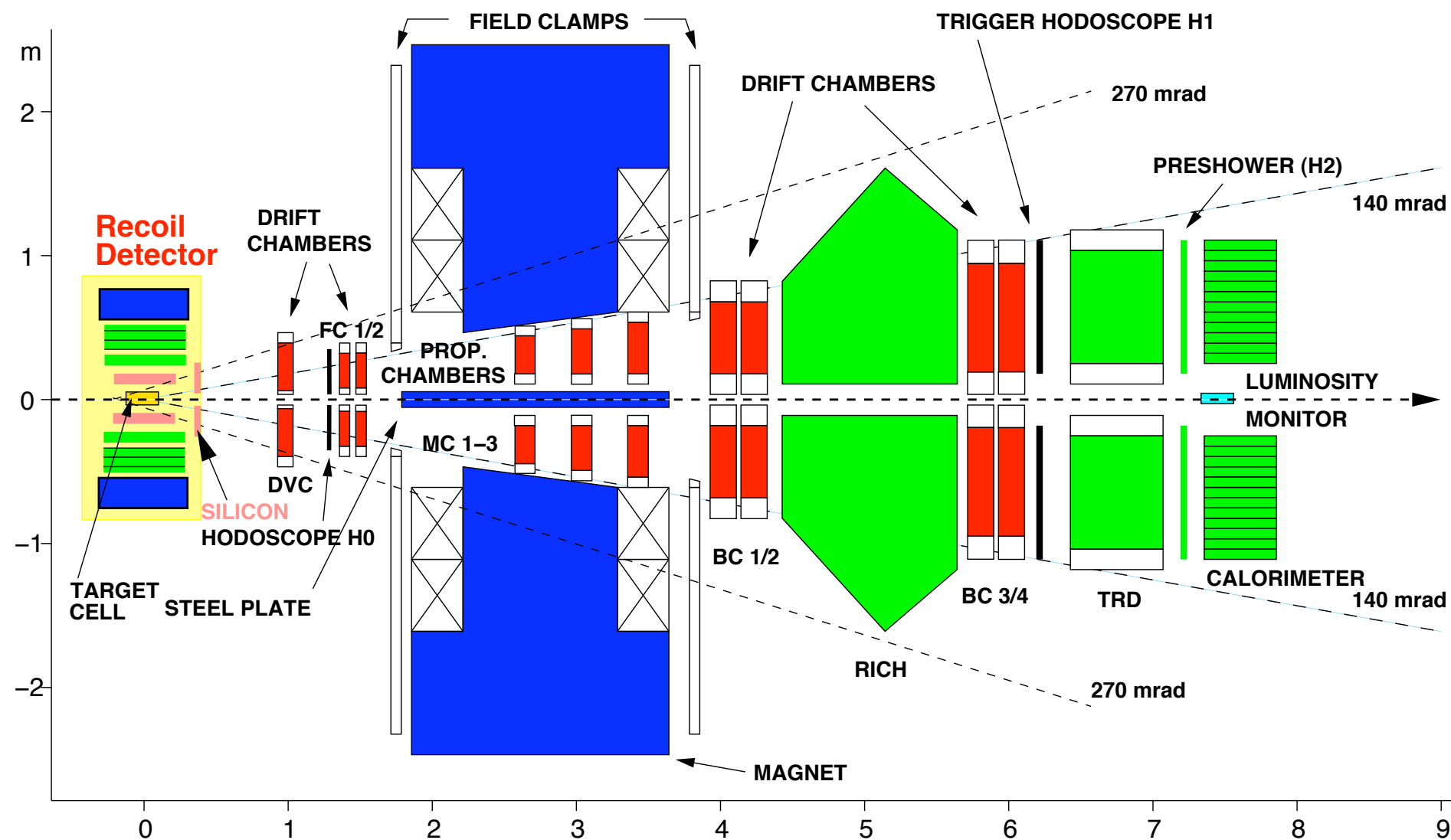
$$q(x) = GPD(x, \xi=0, t=0)$$

leading-twist, quark chirality conserving		
spin-1/2	unpolarized	polarized
no nucleon hel. flip	H	$\tilde{H}$
nucleon hel. flip	E	$\tilde{E}$



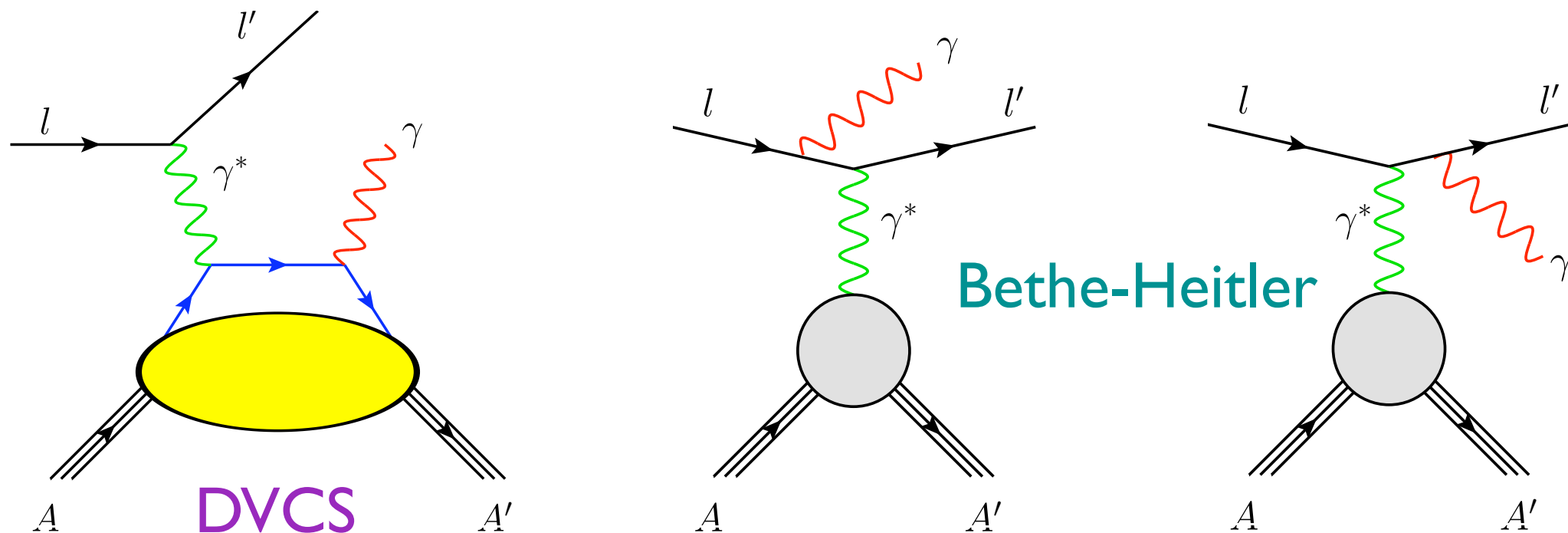
Longitudinally polarized
 e^+e^- Beam
27.6 GeV

- Data Taking: 1995-2007
 - Reconstruction: $\delta p/p < 2\%$, $\delta\Theta < 1$ mrad
 - Internal gas targets: unpol H, D, He, N, Ne, Kr, Xe, Lpol He, H, D, Tpol H
 - Particle ID: TRD, Preshower, Calorimeter, RICH
- lepton-hadron separation > 99 % efficiency



Longitudinally polarized
e⁺/e⁻ Beam
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- Data Taking: 1995-2007
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- lepton-hadron separation > 99 % efficiency
- In 2006-2007 : Data Taking with Recoil Detector



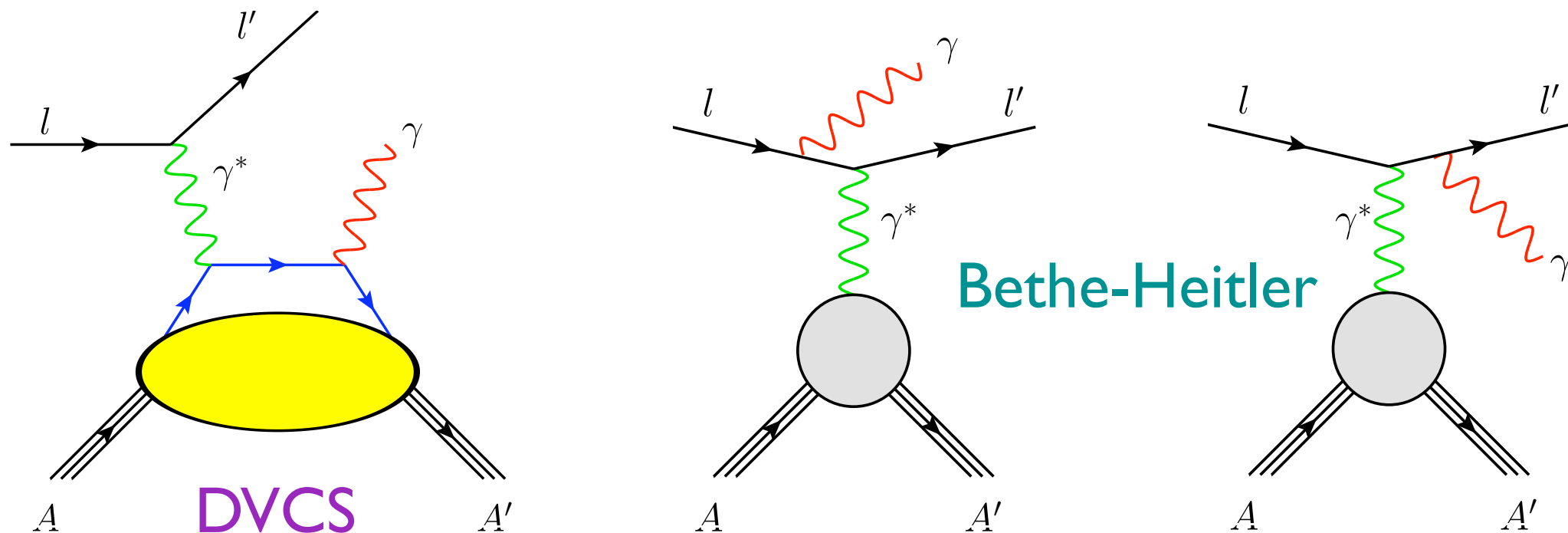
DVCS and Bethe-Heitler $\Rightarrow$ Same final state $\Rightarrow$ Interference

$$\frac{d\sigma}{dx_B dQ^2 d|t| d\phi} \propto |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \underbrace{\mathcal{T}_{DVCS}\mathcal{T}_{BH}^* + \mathcal{T}_{BH}\mathcal{T}_{DVCS}^*}_I$$

At HERMES kinematics $|\mathcal{T}_{DVCS}|^2 \ll |\mathcal{T}_{BH}|^2$

DVCS amplitudes can be accessed through Interference

Interference $\Rightarrow$ non-zero azimuthal asymmetries



$$\frac{d\sigma}{dx_B dQ^2 d|t| d\phi} \propto |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \underbrace{\mathcal{T}_{DVCS} \mathcal{T}_{BH}^* + \mathcal{T}_{BH} \mathcal{T}_{DVCS}^*}_I$$

Bethe-Heitler is parametrized in terms of electromagnetic **Form-Factors** F_1, F_2

DVCS is parametrized in terms of **Compton Form-Factors** $\mathcal{H}, \mathcal{E}, \tilde{\mathcal{H}}, \tilde{\mathcal{E}}$

CFFs = convolutions of hard scattering amplitudes and GPD's

$$\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q(\xi, x) F^q(x, \xi, t)$$

$$|\mathcal{T}_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi) + s_1^{\text{BH}} \sin(\phi) \right\}$$

$$|\mathcal{T}_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left\{ \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + \sum_{n=1}^2 s_n^{\text{DVCS}} \sin(n\phi) \right\}$$

$$\mathcal{I} = -\frac{K_{\text{I}e\ell}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^3 c_n^{\text{I}} \cos(n\phi) + \sum_{n=1}^3 s_n^{\text{I}} \sin(n\phi) \right\}$$

- **Beam-Charge asymmetry**

$$\sigma(e^+, \phi) - \sigma(e^-, \phi) \propto \text{Re}[F_1 \mathcal{H}]$$

- **Beam-Spin Asymmetry**

$$\sigma(\vec{e}, \phi) - \sigma(\overleftarrow{e}, \phi) \propto \text{Im}[F_1 \mathcal{H}]$$

- **Longitudinal Target-Spin Asymmetry**

$$\sigma(\vec{P}, \phi) - \sigma(\overleftarrow{P}, \phi) \propto \text{Im}[F_1 \tilde{\mathcal{H}}]$$

- **Longitudinal Double-Spin Asymmetry**

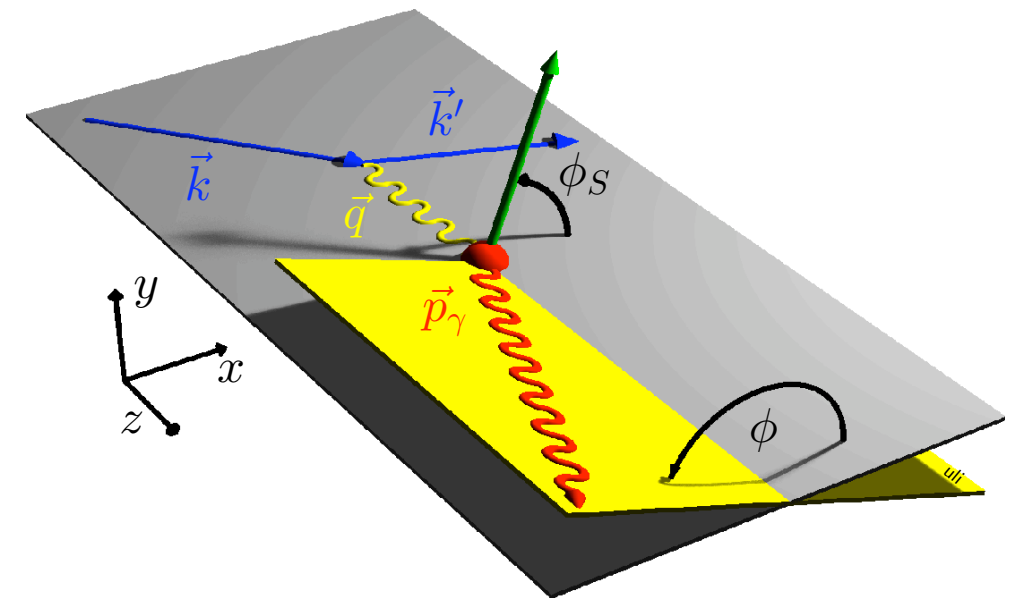
$$\sigma(\vec{P}, \vec{e}, \phi) - \sigma(\vec{P}, \overleftarrow{e}, \phi) \propto \text{Re}[F_1 \tilde{\mathcal{H}}]$$

- **Transverse Target-Spin Asymmetry**

$$\sigma(\phi, \phi_S) - \sigma(\phi, \phi_S + \pi) \propto \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}]$$

- **Transverse Double-Spin Asymmetry**

$$\sigma(\vec{e}, \phi, \phi_S) - \sigma(\overleftarrow{e}, \phi, \phi_S + \pi) \propto \text{Re}[F_2 \mathcal{H} - F_1 \mathcal{E}]$$



Event Selection w/o Recoil Detector

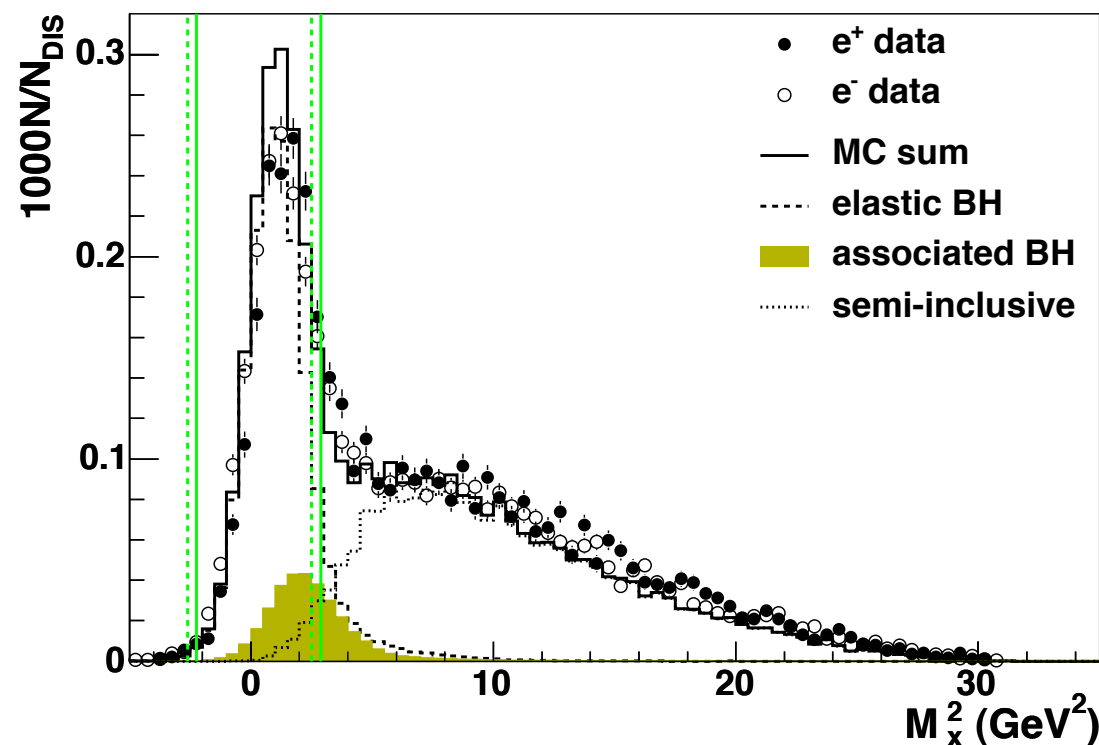
- Events with one DIS lepton and one trackless cluster in the calorimeter.
- Recoiling nucleon was not detected

⇒ Exclusivity via missing mass technique: $M_x^2 = (P + q - q')^2$

$$W^2 > 9 \text{ GeV}^2, \quad \nu < 22 \text{ GeV}$$

$$0.03 < x_B < 0.35, \quad 1 < Q^2 < 10 \text{ GeV}^2$$

$$-t < 0.7 \text{ GeV}^2, \quad E_\gamma > 5 \text{ GeV}$$



Proton:

- Elastic; $ep \rightarrow ep\gamma$
- Associated; mainly $ep \rightarrow e\Delta^+\gamma$
- SIDIS; mainly $ep \rightarrow e\pi^0 X \approx 4\%$

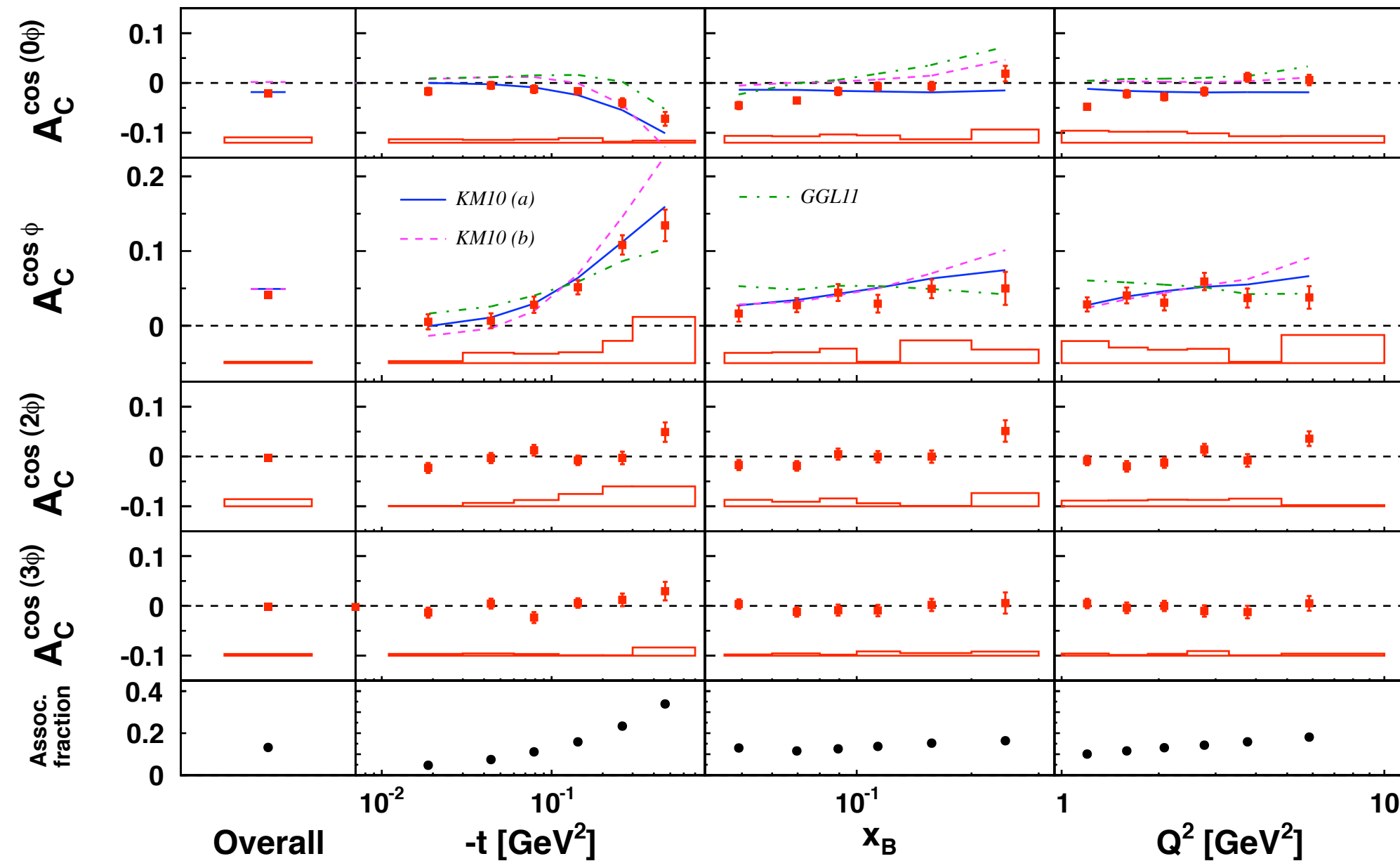
SIDIS background correction:

$$A_{excl.} = \frac{1}{1 - f_{BG}} [A_{meas.} - f_{BG} A_{BG}]$$

$$-2.25 \text{ GeV}^2 < M_x^2 < 2.89 \text{ GeV}^2$$

Associated cannot be resolved → defined as a part of signal.

$$\mathcal{A}_C(\phi) = \frac{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})}$$



$$\propto -A_C^{\cos(\phi)}$$

$$\propto \text{Re}[F_1 \mathcal{H}]$$

Beam charge asymmetry

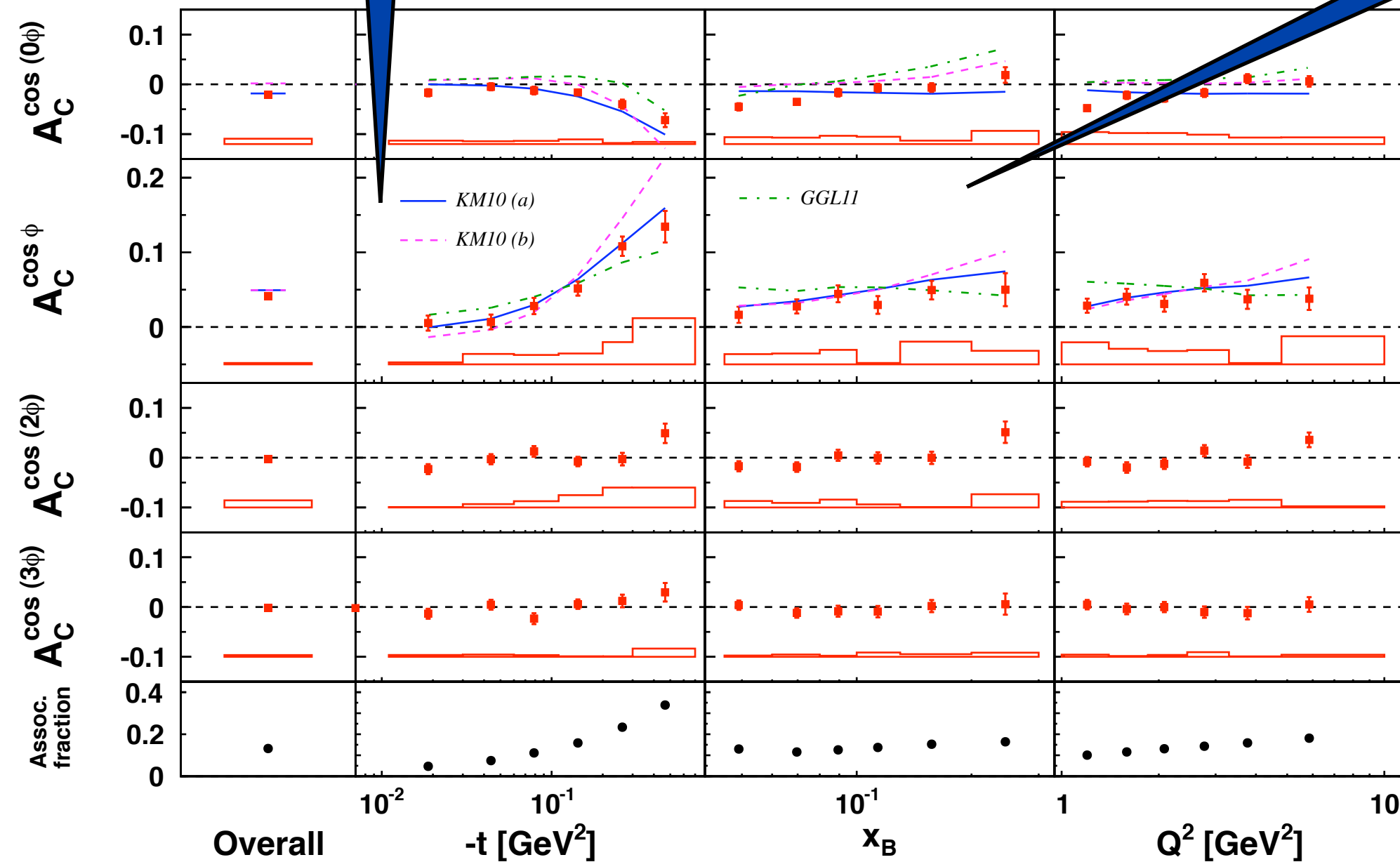
- non-zero leading amplitude
- strong $-t$ dependence
- no x_B and Q^2 dependencies
- good agreement with model predictions

Fractions of associated process from MC

KM10: Global fit
including data from JLab,
HERMES and HERA
K. Kumericki, D. Muller
Nucl.Phys.B 841 (2010) 1

$$\mathcal{A}_C(\phi) = \frac{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})}$$

GGL11: Model calculation
G. Goldstein, S. Liuti,
J. Hernandez
Phys.Rev.D 84 034007 (2011)



$$\propto -A_C^{\cos(\phi)}$$

$$\propto \text{Re}[F_1 \mathcal{H}]$$

Beam charge asymmetry

- non-zero leading amplitude
- strong $-t$ dependence
- no x_B and Q^2 dependencies
- good agreement with model predictions

Fractions of associated
process from MC

$$A_{LU}^{I,DVCS}(\phi) = \frac{(\sigma^{+\rightarrow} - \sigma^{+\leftarrow})_+ (\sigma^{-\rightarrow} - \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})}$$

Charge-difference beam-helicity asymmetry

- significant negative value of the leading amplitude
- no kinematic dependencies
- non leading amplitudes are consistent with zero

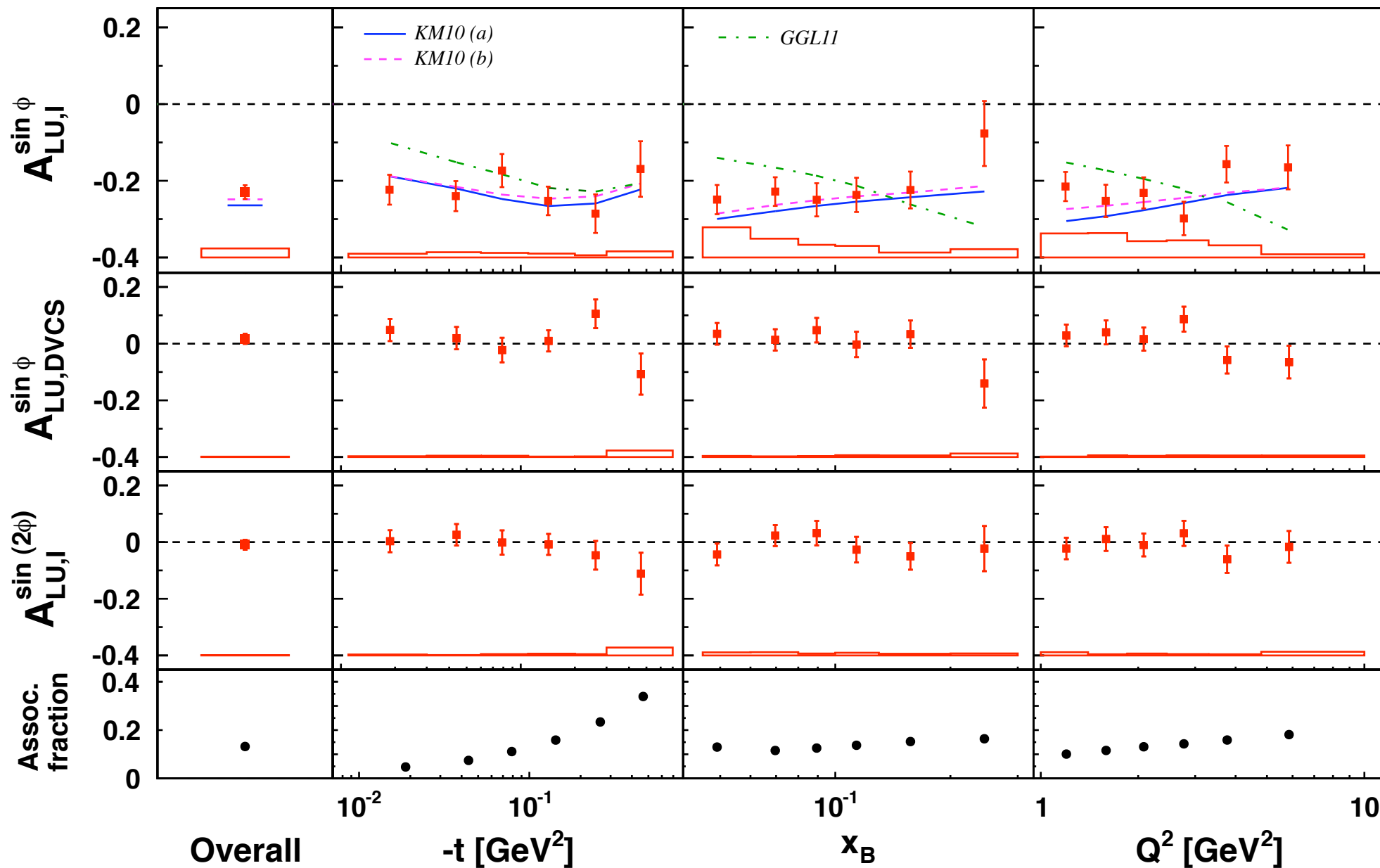
$$\propto \text{Im} [F_1 \mathcal{H}]$$

$$\propto \text{Im} [\mathcal{H} \mathcal{H}^* + \tilde{\mathcal{H}} \tilde{\mathcal{H}}^*]$$

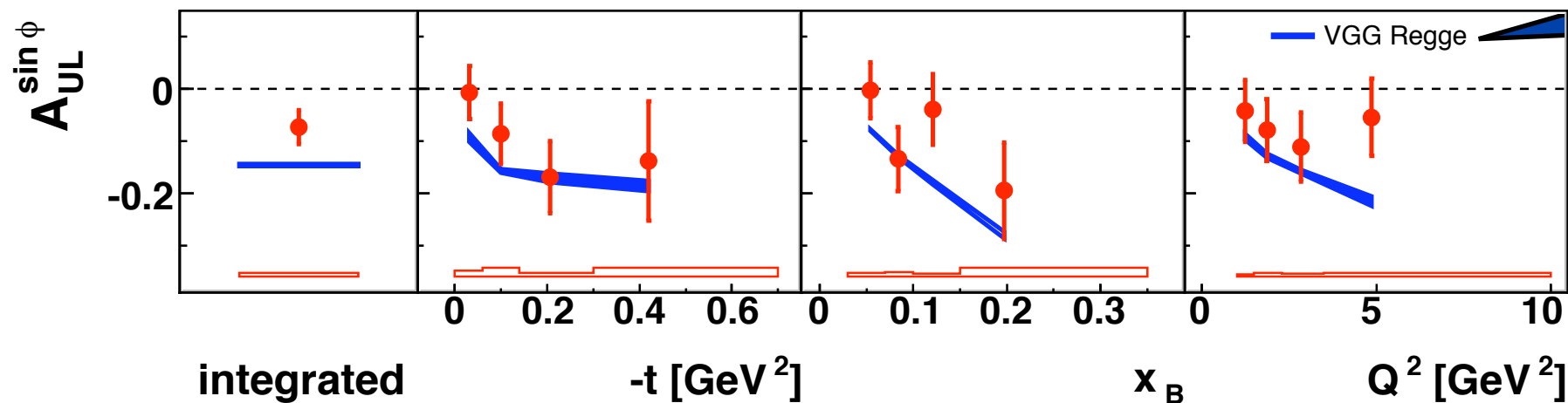
Charge-averaged beam-helicity asymmetry

- consistent with zero

Fractions of associated process from MC



$$\mathcal{A}_{UL}(\phi) = \frac{(\sigma^{\rightarrow\Rightarrow} + \sigma^{\leftarrow\Rightarrow}) - (\sigma^{\rightarrow\Leftarrow} + \sigma^{\leftarrow\Leftarrow})}{(\sigma^{\rightarrow\Rightarrow} + \sigma^{\leftarrow\Rightarrow}) + (\sigma^{\rightarrow\Leftarrow} + \sigma^{\leftarrow\Leftarrow})}$$



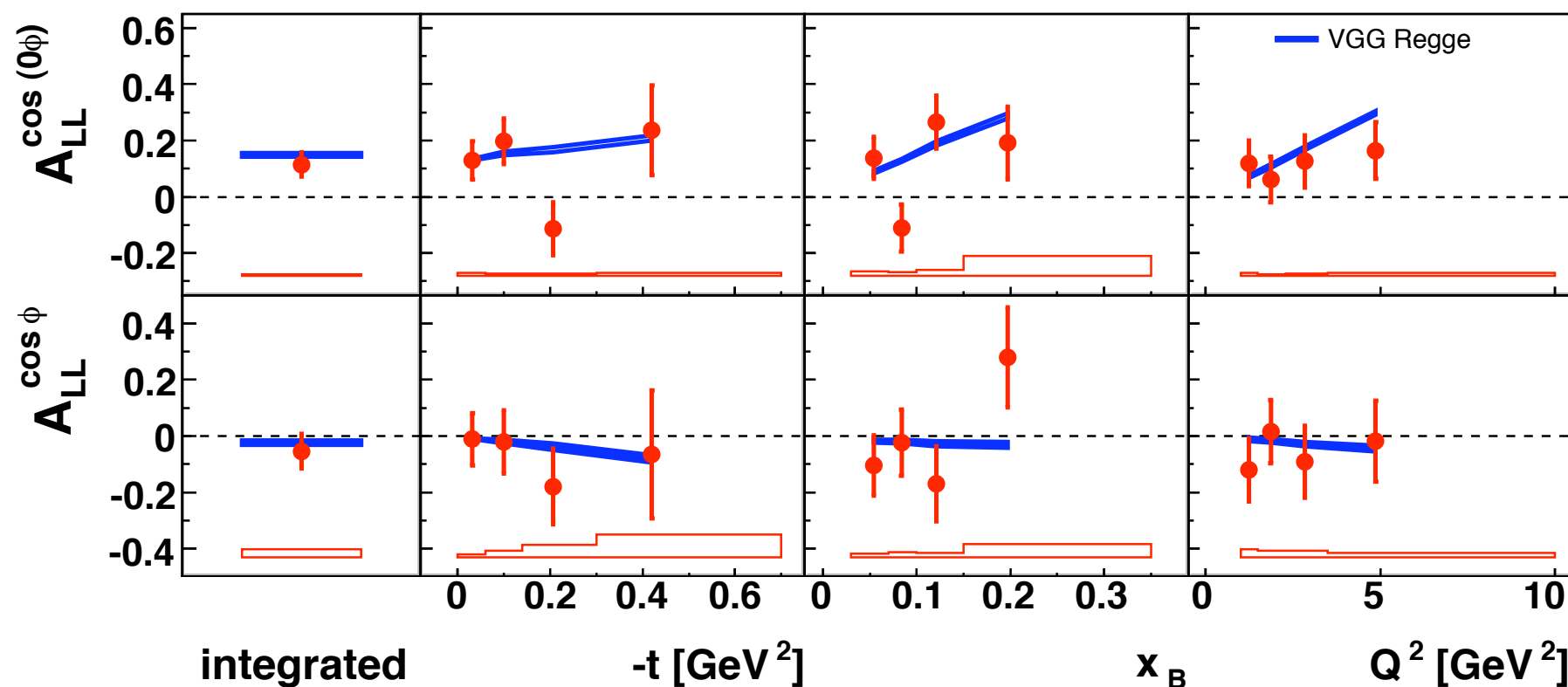
VGG: Model calculation
M. Vanderhaeghen, P. Guichon, M. Guidal
Phys..Rev.D (1999) 094017
Prog. Nucl. Phys, 47 (2001) 401

$$\propto \text{Im} [F_1 \tilde{\mathcal{H}}]$$

Longitudinal Target Spin
Asymmetry

- non-zero negative value of the leading $\sin(\phi)$ amplitude
- mild kinematic dependence

$$\mathcal{A}_{LL}(\phi) = \frac{(\sigma^{\rightarrow\Rightarrow} + \sigma^{\leftarrow\Leftarrow}) - (\sigma^{\rightarrow\Leftarrow} + \sigma^{\leftarrow\Rightarrow})}{(\sigma^{\rightarrow\Rightarrow} + \sigma^{\leftarrow\Leftarrow}) + (\sigma^{\rightarrow\Leftarrow} + \sigma^{\leftarrow\Rightarrow})}$$



Longitudinal Double-Spin
Asymmetry

- constant term is positive
- leading $\cos(\phi)$ amplitude is consistent with zero

$$\propto \text{Re} [F_1 \tilde{\mathcal{H}}]$$

Asymmetry amplitudes are attributed not only to squared DVCS and Interference terms but also to squared BH term

Transverse Single Target-Spin and Double-Spin asymmetries

$$A_{UT}^{I,DVCS}(\phi, \phi_S) = \frac{(\sigma^{+\uparrow} - \sigma^{+\downarrow})_+ (\sigma^{-\uparrow} - \sigma^{-\downarrow})}{(\sigma^{+\uparrow} + \sigma^{+\downarrow}) + (\sigma^{-\uparrow} + \sigma^{-\downarrow})}$$

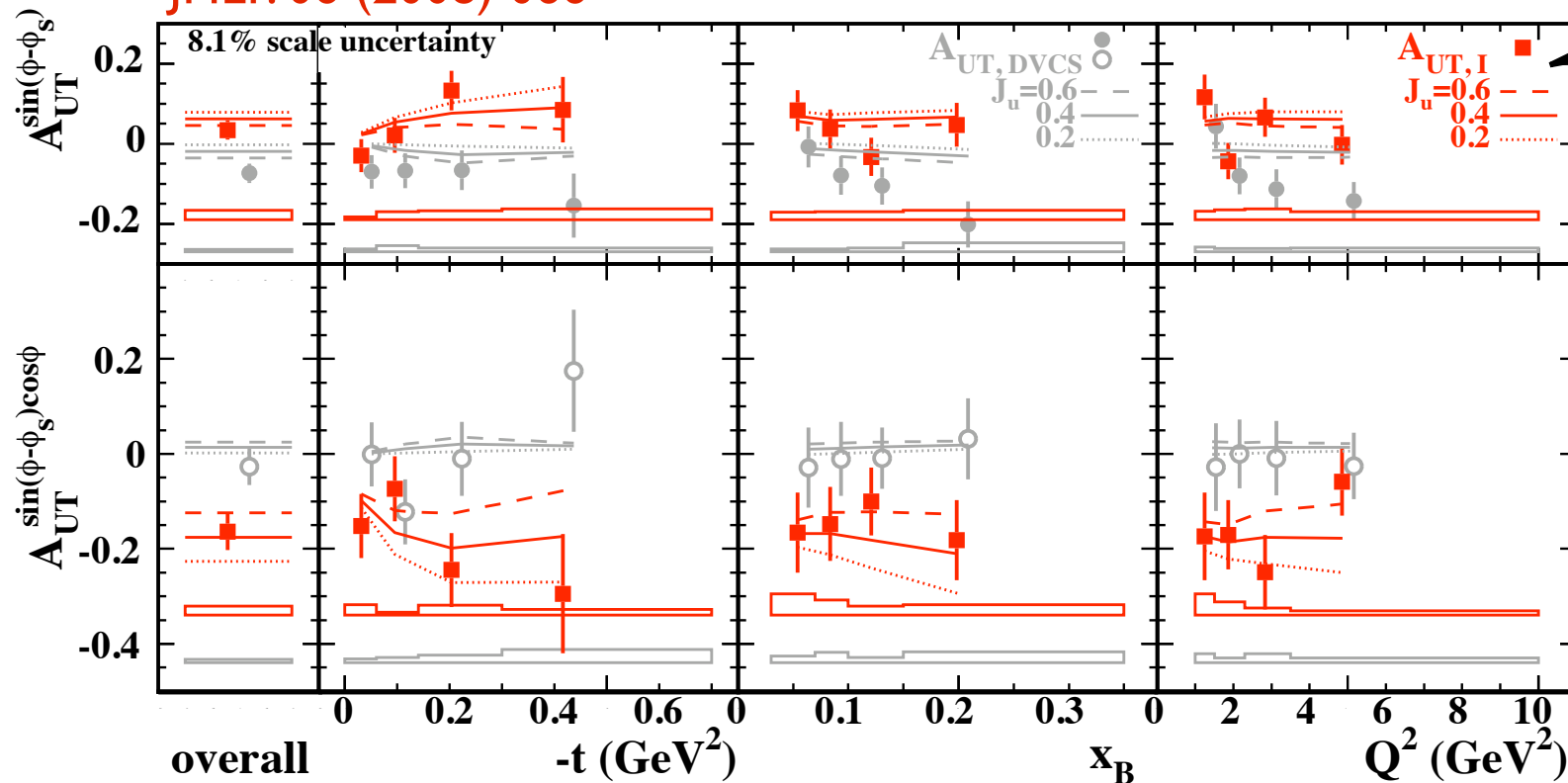
VGG: Model calculation

M. Vanderhaeghen, P. Guichon, M. Guidal

Phys. Rev. D (1999) 094017

Prog. Nucl. Phys, 47 (2001) 401

JHEP. 06 (2008) 066



Charge-difference Transverse Target-Spin asymmetry

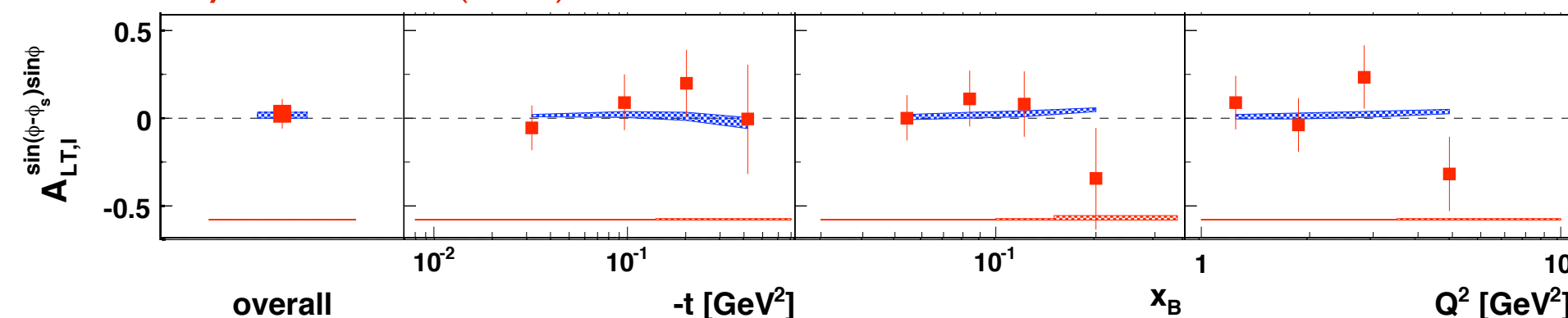
- Non-zero leading $\cos(n\phi)$ amplitudes.

$$\propto \frac{\text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}]}{\text{Im}[\mathcal{H} \mathcal{E}^* - \mathcal{E} \mathcal{H}^* - \xi(\tilde{\mathcal{H}} \tilde{\mathcal{E}}^* - \tilde{\mathcal{E}} \tilde{\mathcal{H}}^*)]}$$

Leading $\cos(\phi)$ amplitude of charge difference target-spin asymmetry A_{UT}^I is sensitive to CFF $\mathcal{E}$, therefore J_u .

$$A_{LT}^I(\phi, \phi_S) = \frac{(\vec{\sigma}^{+\uparrow} + \vec{\sigma}^{+\downarrow} - \vec{\sigma}^{+\downarrow} - \vec{\sigma}^{+\uparrow}) - (\vec{\sigma}^{-\uparrow} + \vec{\sigma}^{-\downarrow} - \vec{\sigma}^{-\downarrow} - \vec{\sigma}^{-\uparrow})}{(\vec{\sigma}^{+\uparrow} + \vec{\sigma}^{+\downarrow} + \vec{\sigma}^{+\downarrow} + \vec{\sigma}^{+\uparrow}) + (\vec{\sigma}^{-\uparrow} + \vec{\sigma}^{-\downarrow} + \vec{\sigma}^{-\downarrow} + \vec{\sigma}^{-\uparrow})}$$

Phys. Lett. B704 (2011) 15-23



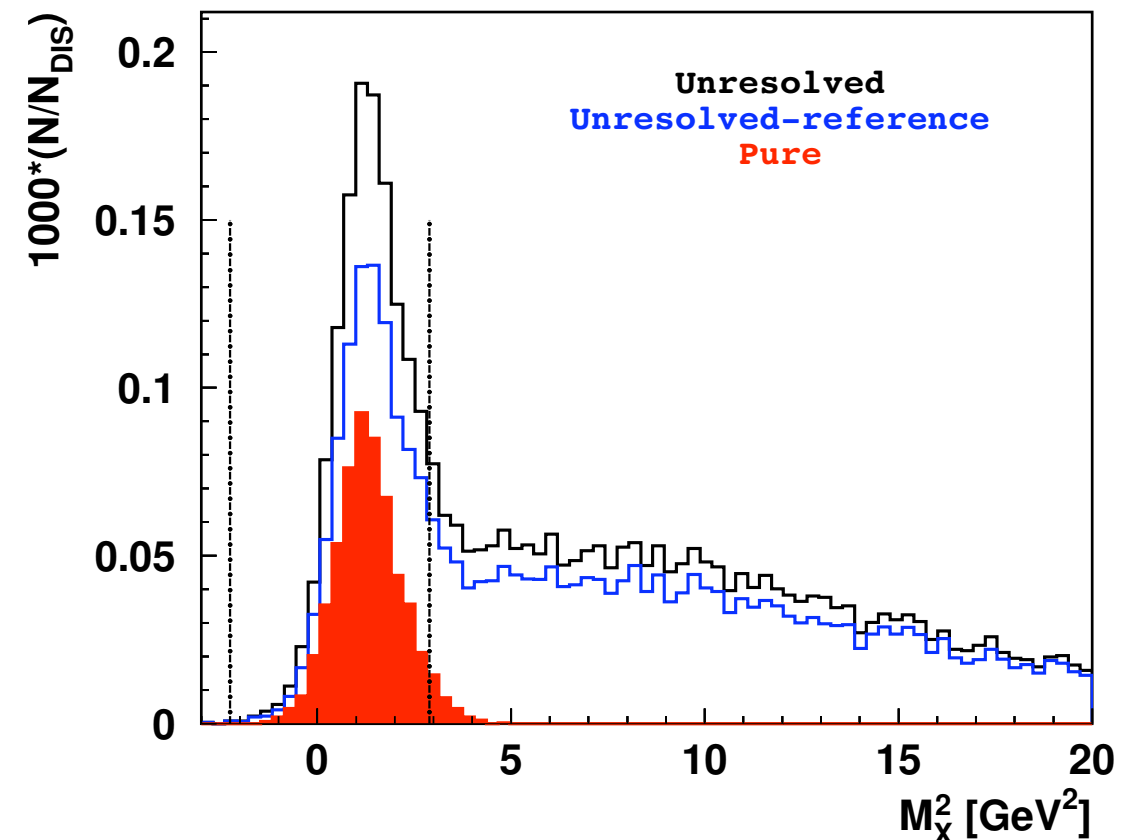
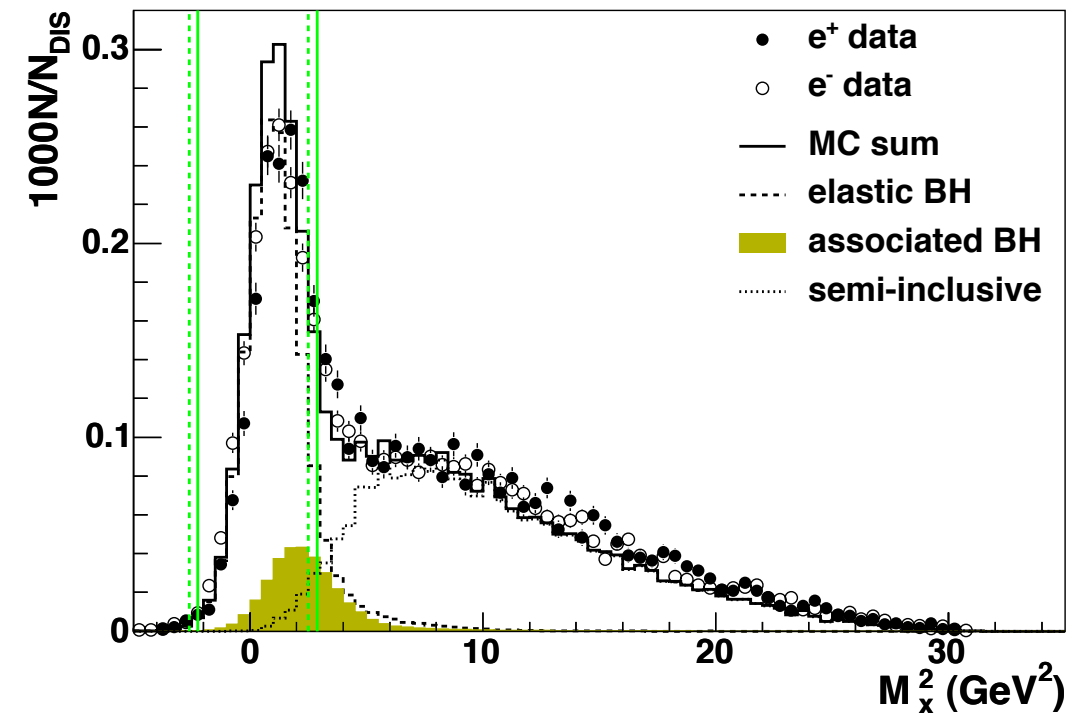
Charge-difference Transverse Double-Spin asymmetry

- leading amplitudes are consistent with zero
- sensitivity to is suppressed J_u is suppressed by kinematic pre-factor

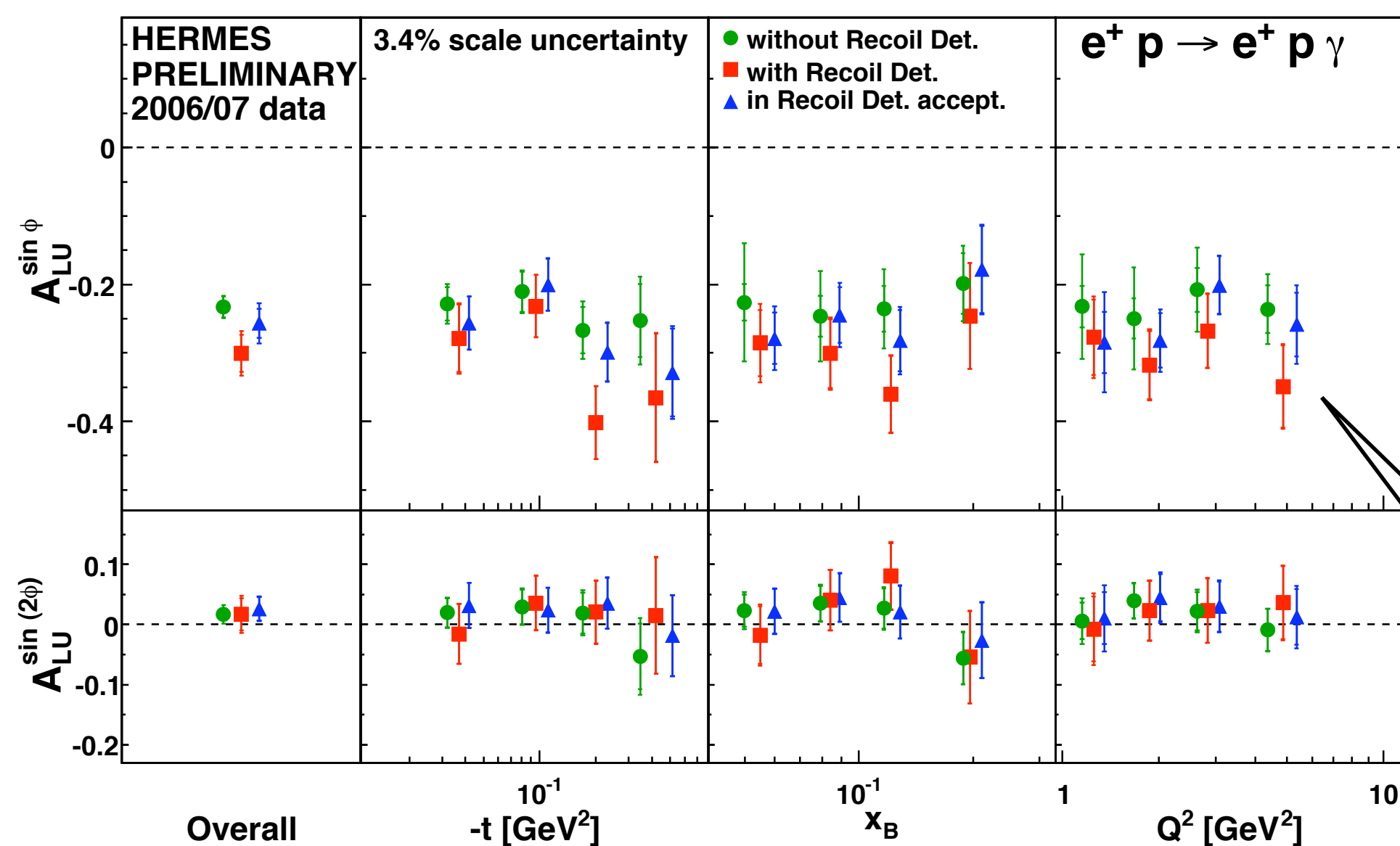
$$\propto \text{Re}[F_2 \mathcal{H} - F_1 \mathcal{E}]$$

Event Selection with Recoil Detector

- Events with one DIS lepton and one trackless cluster in the calorimeter.
- “**Unresolved**” for associated process $ep \rightarrow e\Delta^+\gamma \approx 12\%$
- “**Unresolved reference**” sample.
- “Hypothetical” proton required in the Recoil Detector acceptance.
- “**Pure Elastic**” sample.
- Kinematic event fitting technique.
Allows to achieve purity $> 99.9\%$



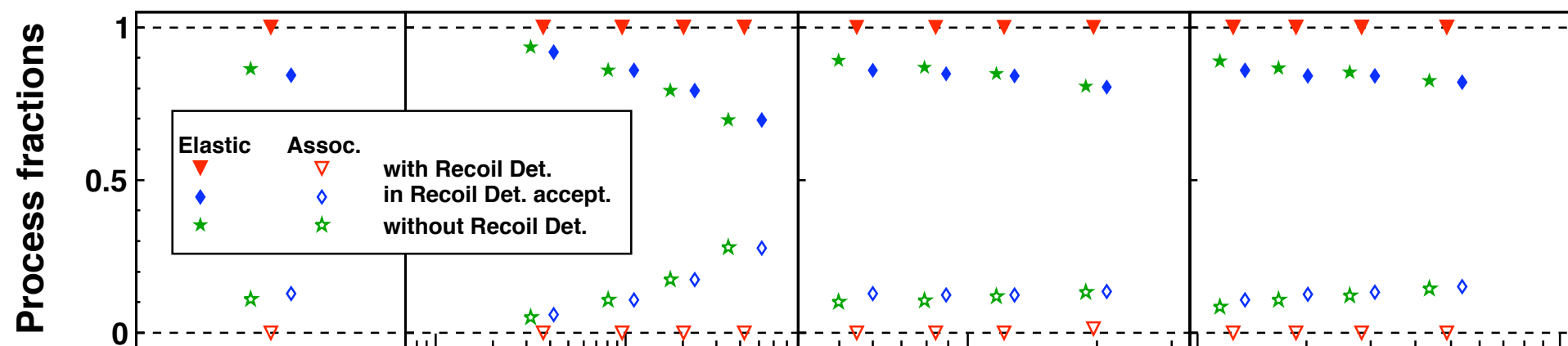
Beam-Spin asymmetry with Recoil



$$A_{LU}(\phi) = \frac{\sigma^{+\rightarrow} - \sigma^{+\leftarrow}}{\sigma^{+\rightarrow} + \sigma^{+\leftarrow}}$$

Indication of slightly larger magnitude of leading amplitude for pure elastic sample compared with reference sample

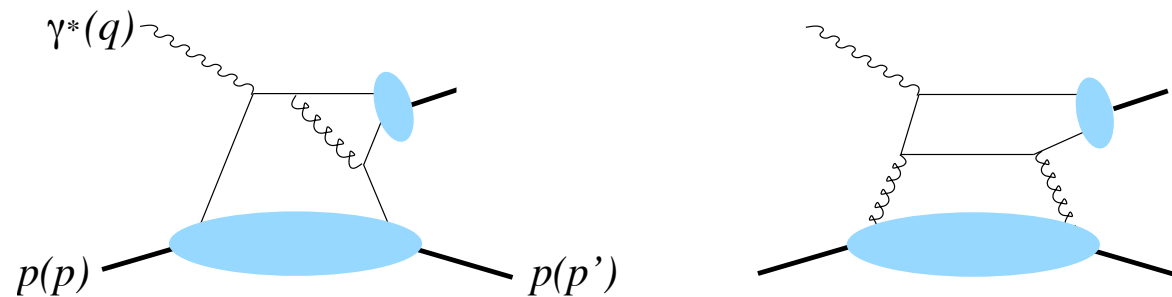
Unresolved
Unresolved Reference
Pure Elastic



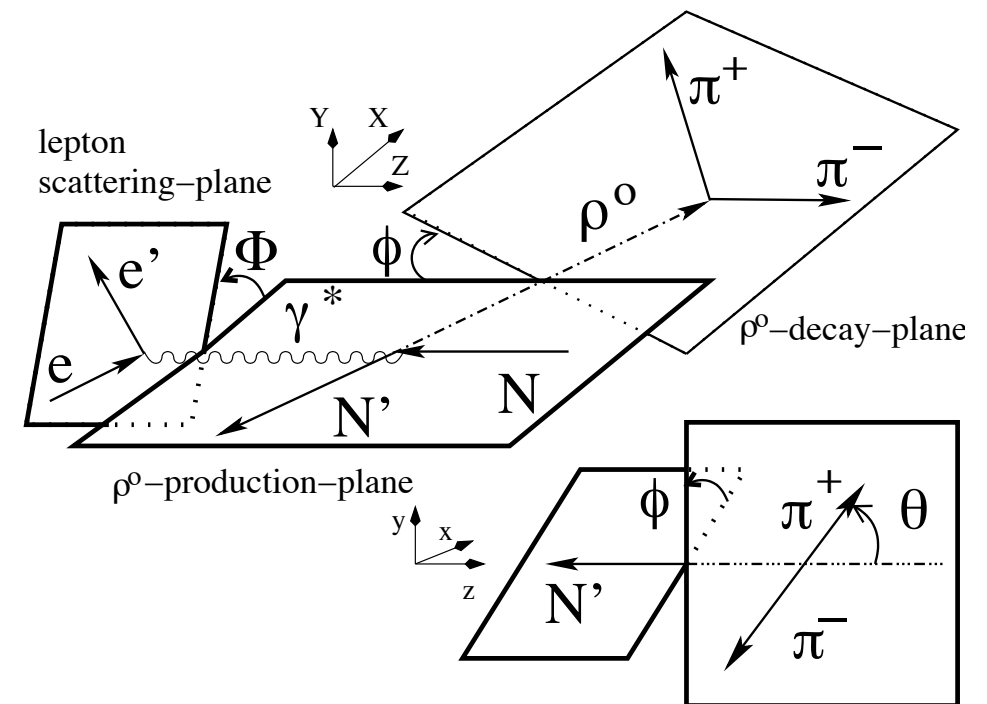
Fractional contributions of elastic and associated processes for different samples

pQCD description of the process.

- I) dissociation of the virtual photon into quark-antiquark pair
- II) scattering of a pair on a nucleon
- III) formation of the observed vector meson



UPE GPDs $\tilde{H}, \tilde{E}$
NPE GPDs H, E



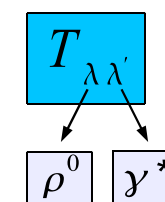
Cross Section

$$\frac{d\sigma}{dx_B dQ^2 dt d\Phi d\cos\theta d\phi} \propto \frac{d\sigma}{dx_B dQ^2 dt} W(x_B, Q^2, t, \Phi, \cos\theta, \phi)$$

production and decay angular distribution: W decomposition

$$W = W_{UU} + P_\ell W_{LU} + S_L W_{UL} + P_\ell S_L W_{LL} + S_T W_{UT} + P_\ell S_T W_{LT}$$

parameterization in terms of helicity amplitudes



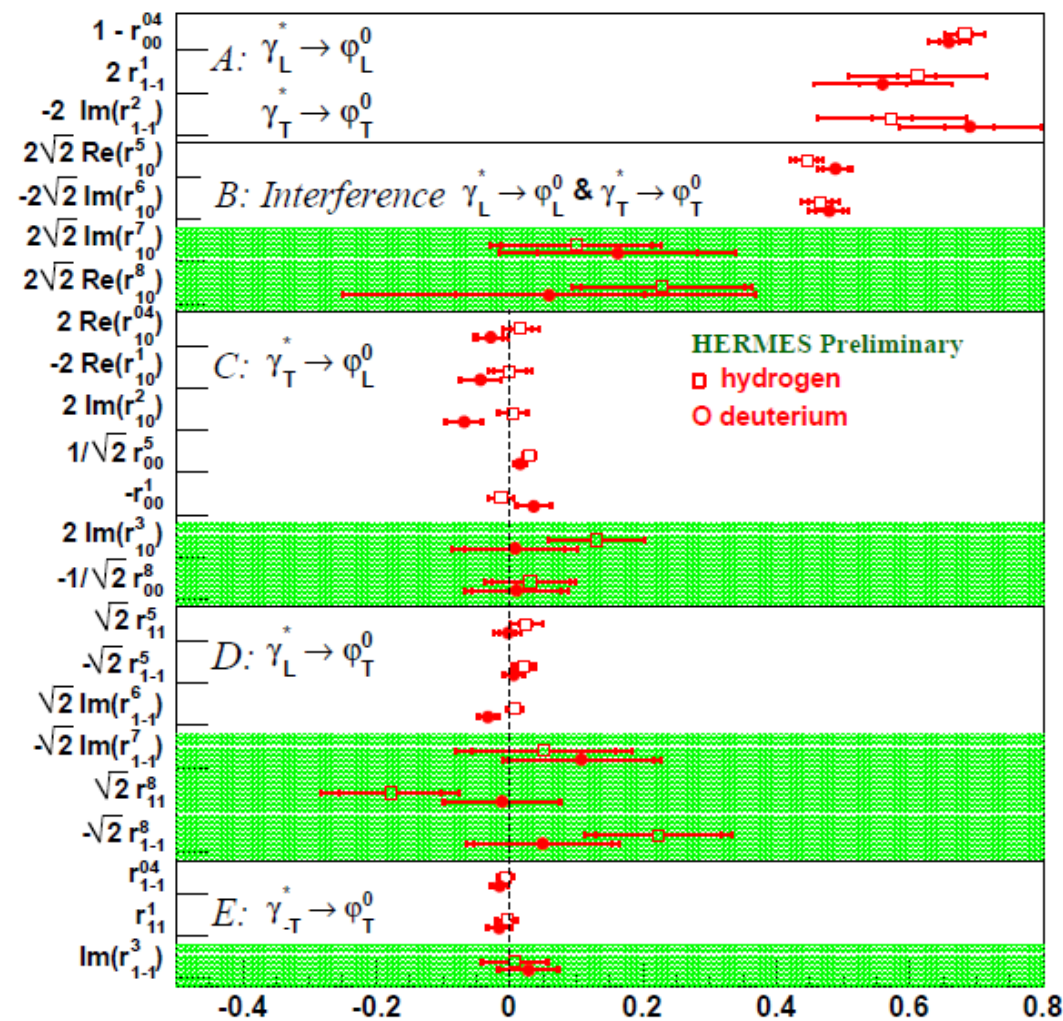
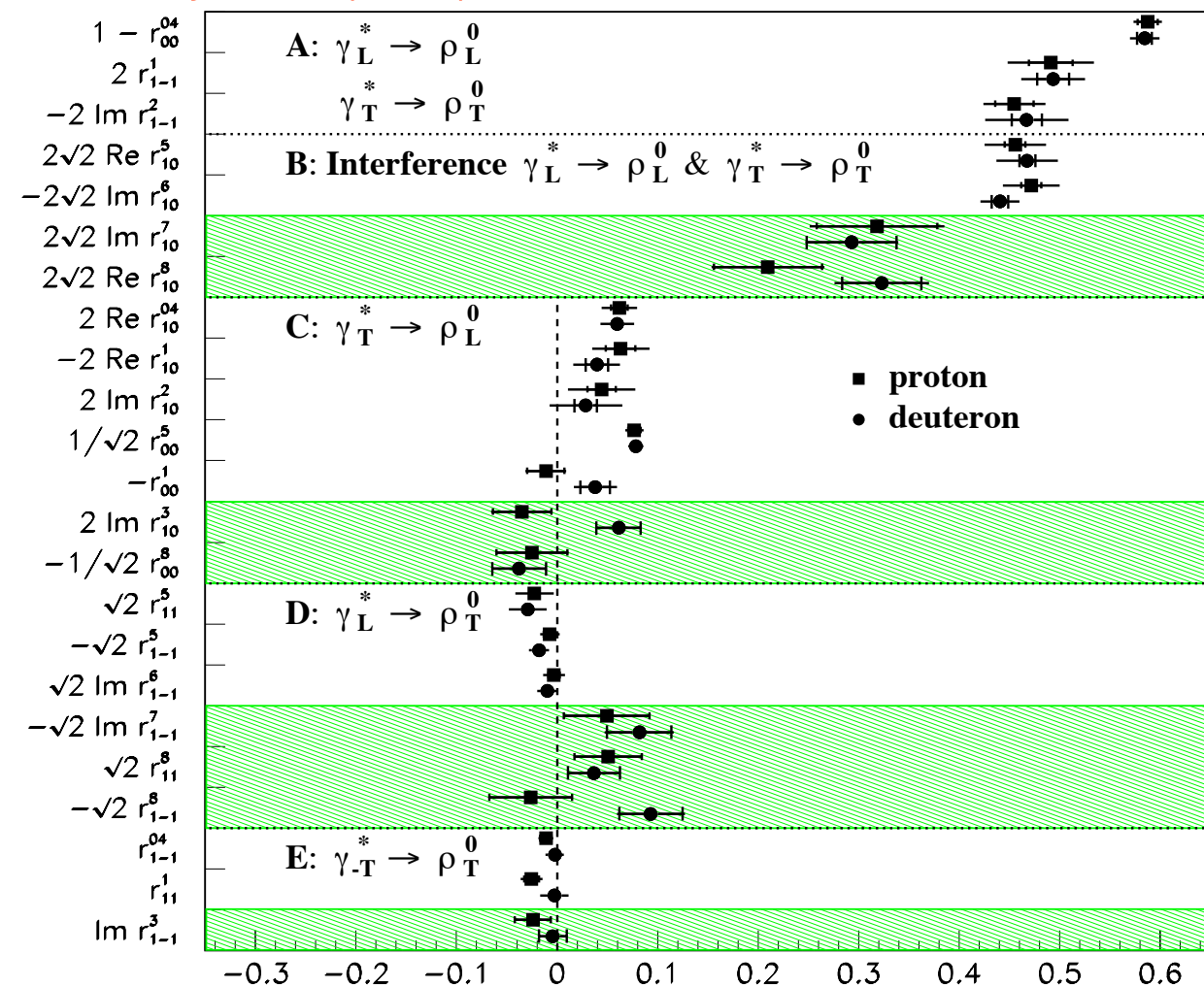
or SDMEs



ρ^0 and ϕ SDMEs on an unpolarized target

$$|T_{00}|^2 \sim |T_{11}|^2 \gg |T_{01}|^2 > |T_{10}|^2 \sim |T_{-11}|^2$$

EPJ C 62 (2009) 659-694



$\gamma_L^* \rightarrow V_L$ & $\gamma_T^* \rightarrow V_T$

- SDMEs are significantly different from zero
- 10-20% difference between ρ and ϕ SDMEs

$\gamma_T^* \rightarrow V_L$

- pronounced difference between ρ and ϕ SDMEs
- 2-10 σ level violation from SCHC for ρ

$\gamma_L^* \rightarrow V_T$ & $\gamma_{-T}^* \rightarrow V_T$

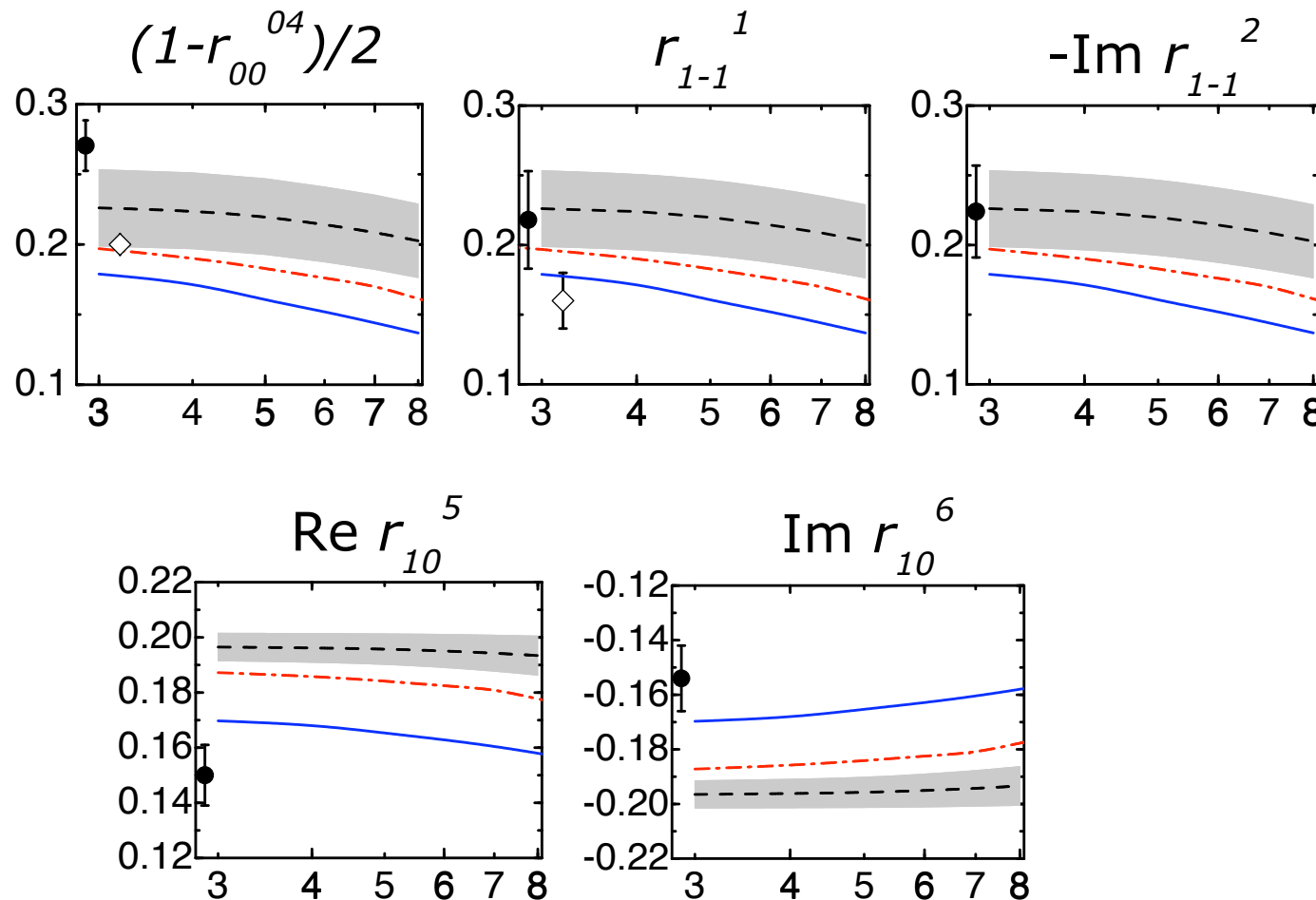
- SDMEs are consistent with zero

- Selected hierarchy is confirmed

- No differences between proton and deuteron

Comparison of ρ^0 SDMEs to GPD model

GPD model: [S. Goloskokov, P. Kroll \(2007\)](#)



$$\tan \delta_{11} = \frac{\text{Im}(T_{11}/T_{00})}{\text{Re}(T_{11}/T_{00})}$$

HERMES result $\delta_{11}=31.5 \pm 1.4$ deg.

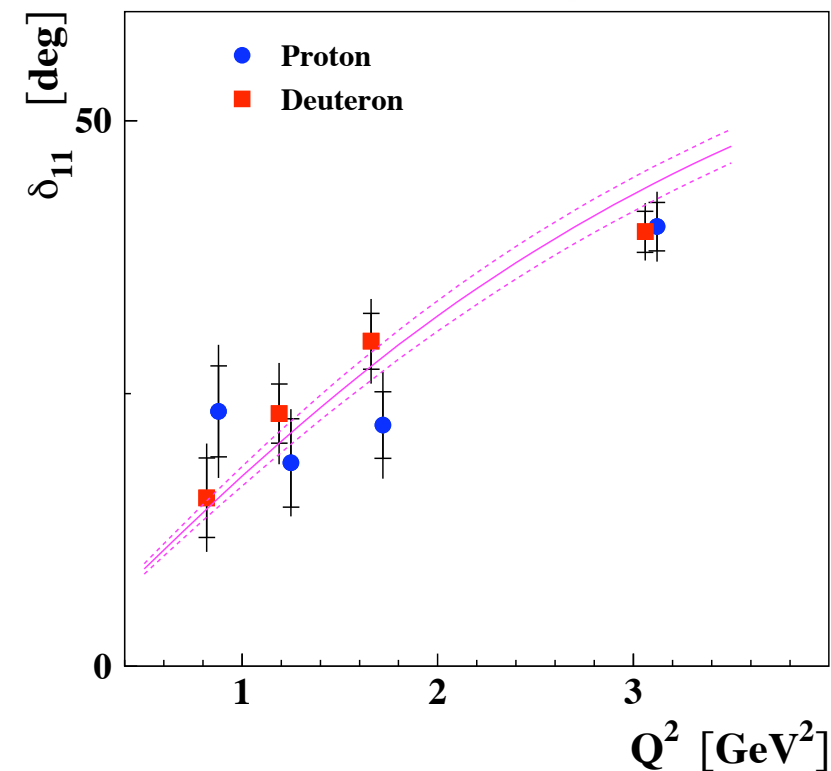
Large phase difference was observed also by H1 ($\delta_{11}=20$)

W=5 GeV (HERMES)
W=10 GeV (COMPASS)
W=75 GeV (H1, ZEUS)

$\gamma^*_L \rightarrow \rho^0_L$ & $\gamma^*_T \rightarrow \rho^0_T$

$$1 - r_{00}^{04}, r_{1-1}^1, -\text{Im} r_{1-1}^2 \propto T_{11}$$

model is in an agreement with data
interference $\gamma^*_L \rightarrow \rho^0_L$ & $\gamma^*_T \rightarrow \rho^0_T$
model dose not describe the data
model predicts phase difference
between T_{00} and T_{11} , $\delta_{11}=3.1$ deg.



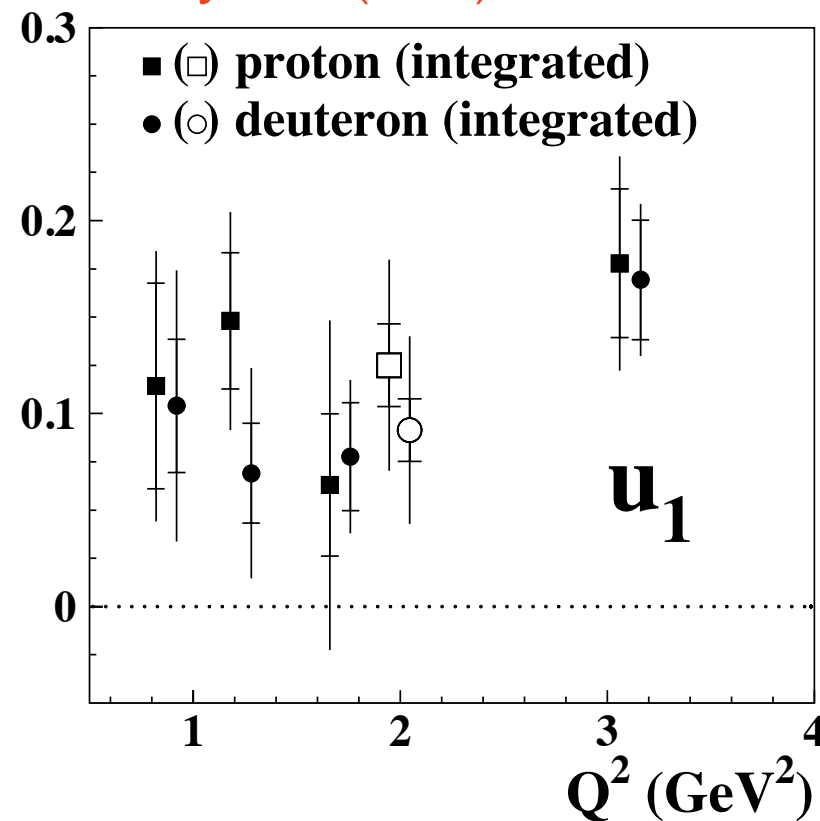
Observation of Unnatural-parity exchange

At large W^2 and Q^2 the transition should be suppressed by M/Q

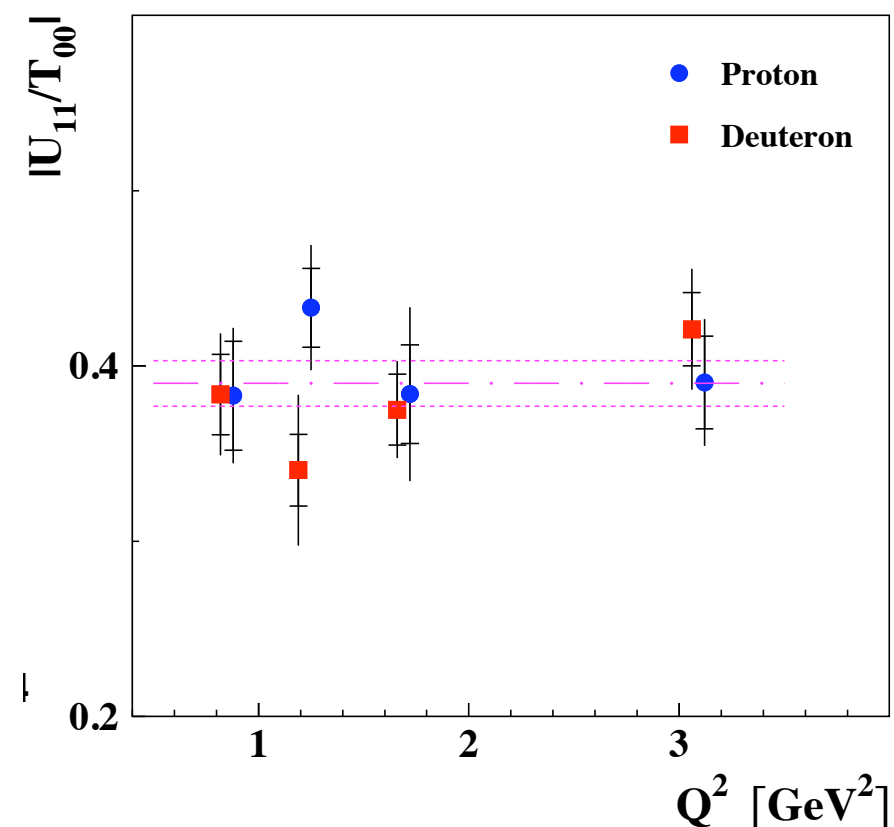
- direct helicity amplitude ratio analysis: U_{11}/T_{00}
- the combination of SDMEs is expected to be zero in case of NPE

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1 \quad u_2 = r_{11}^5 + r_{1-1}^5 \quad u_3 = r_{11}^8 + r_{1-1}^8$$

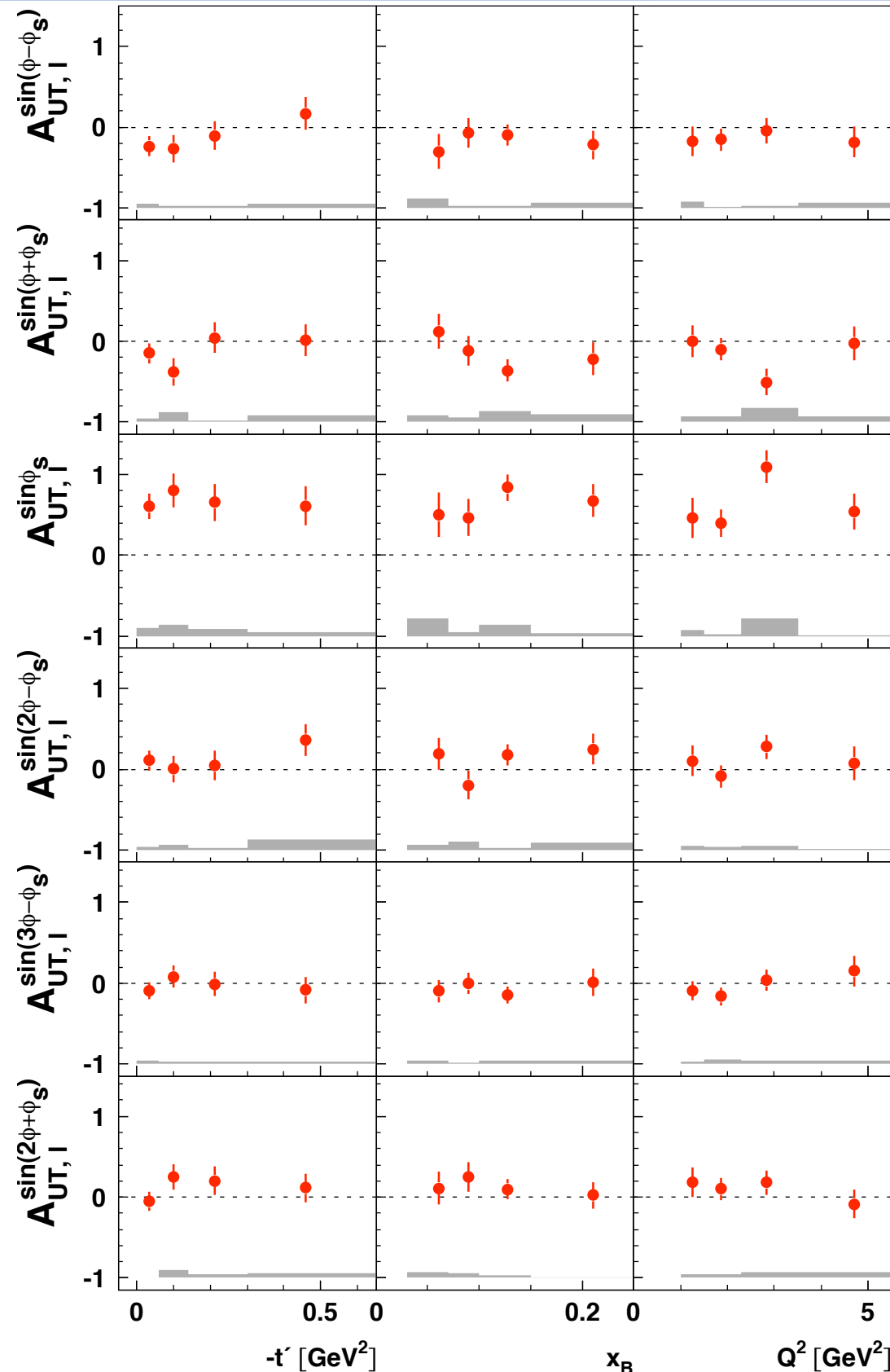
EPJ C 62 (2009) 659-694



EPJ C 71 (2011) 1609

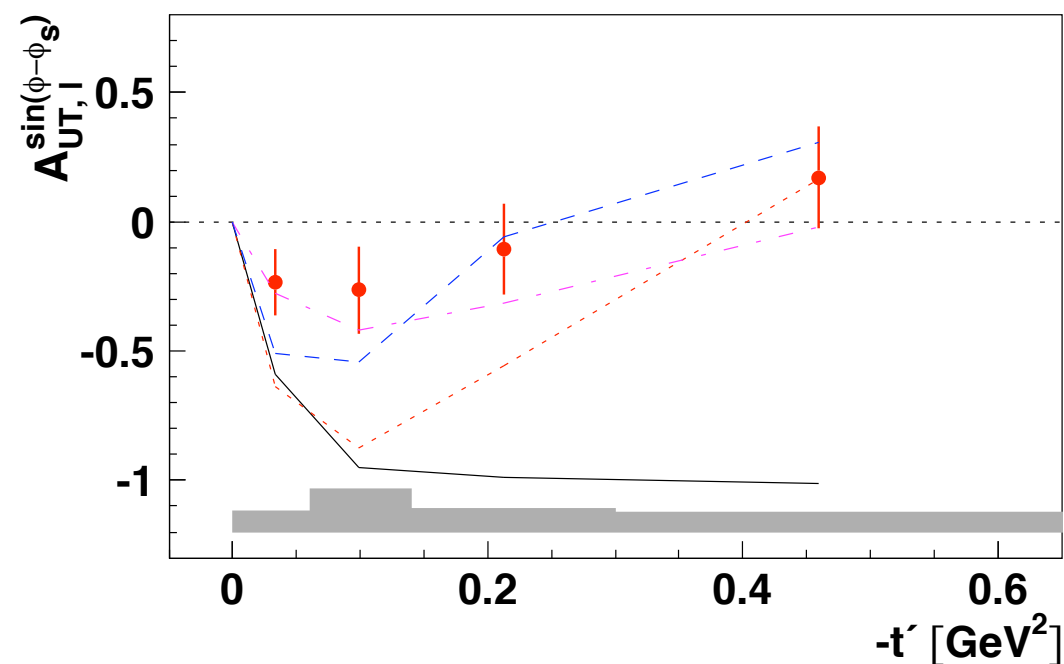


- Significant UPE contribution for ρ^0
Sensitivity to GPD $\tilde{H}$
- No signal of UPE contribution for ϕ

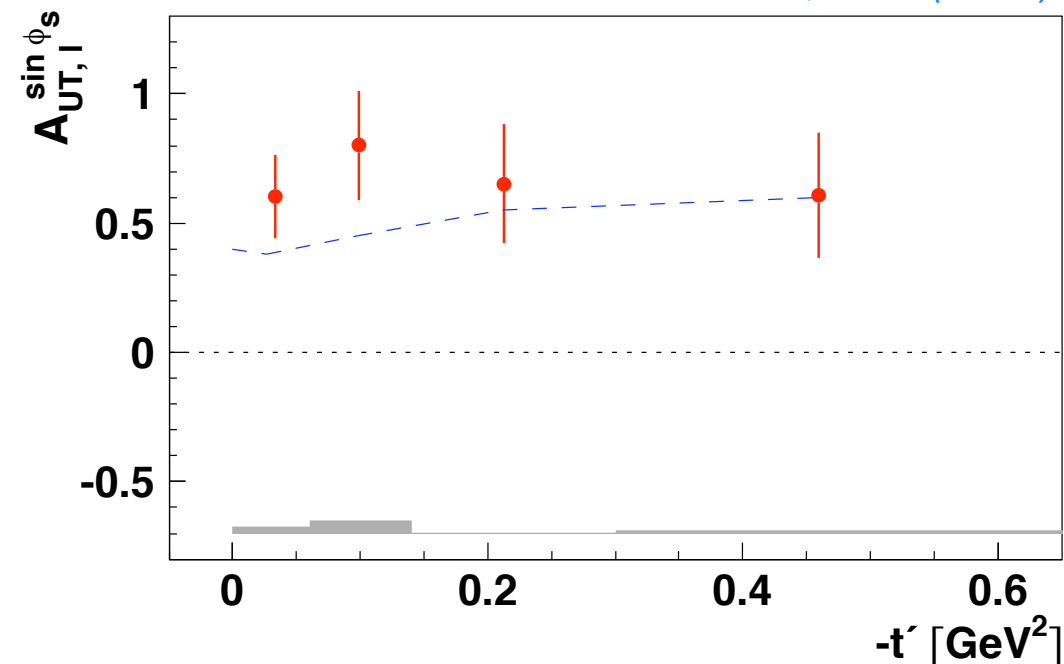


$$\mathcal{A}_{UT}(\phi, \phi_S) = \frac{\sigma^{\uparrow\uparrow} - \sigma^{\downarrow\downarrow}}{\sigma^{\uparrow\uparrow} + \sigma^{\downarrow\downarrow}}$$

- 6 azimuthal asymmetry amplitudes are measured
- no L/T separation
- small overall value for the leading asymmetry amplitude $A_{UT}^{\sin(\phi - \phi_S)}$
- unexpectedly large value for the asymmetry amplitude $A_{UT}^{\sin(\phi_S)}$
- other amplitudes are consistent with zero
- evidence for contribution from transversally polarized photons



-Goloskokov, Kroll (2009)-



Leading amplitude $A_{UT}^{\sin(\phi-\phi_S)}$

- small asymmetry with possible sign change
- $A_{UT}^{\sin(\phi-\phi_S)} \propto \text{Im}(\tilde{\mathcal{E}} * \tilde{\mathcal{H}})$
- theoretical expectation:
large negative value *Frankfurt et.al. (2001)*
Belitsky, Muller (2001)
- difference could be due the γ^*_T .
Goloskokov, Kroll (2009)
Bechler, Muller (2009)

amplitude $A_{UT}^{\sin(\phi_S)}$

- large positive value
- mild t' dependence
- does not vanish at $-t'=0$
- can be explained by a sizable interference between contributions from γ^*_L and γ^*_T .

Summary

