

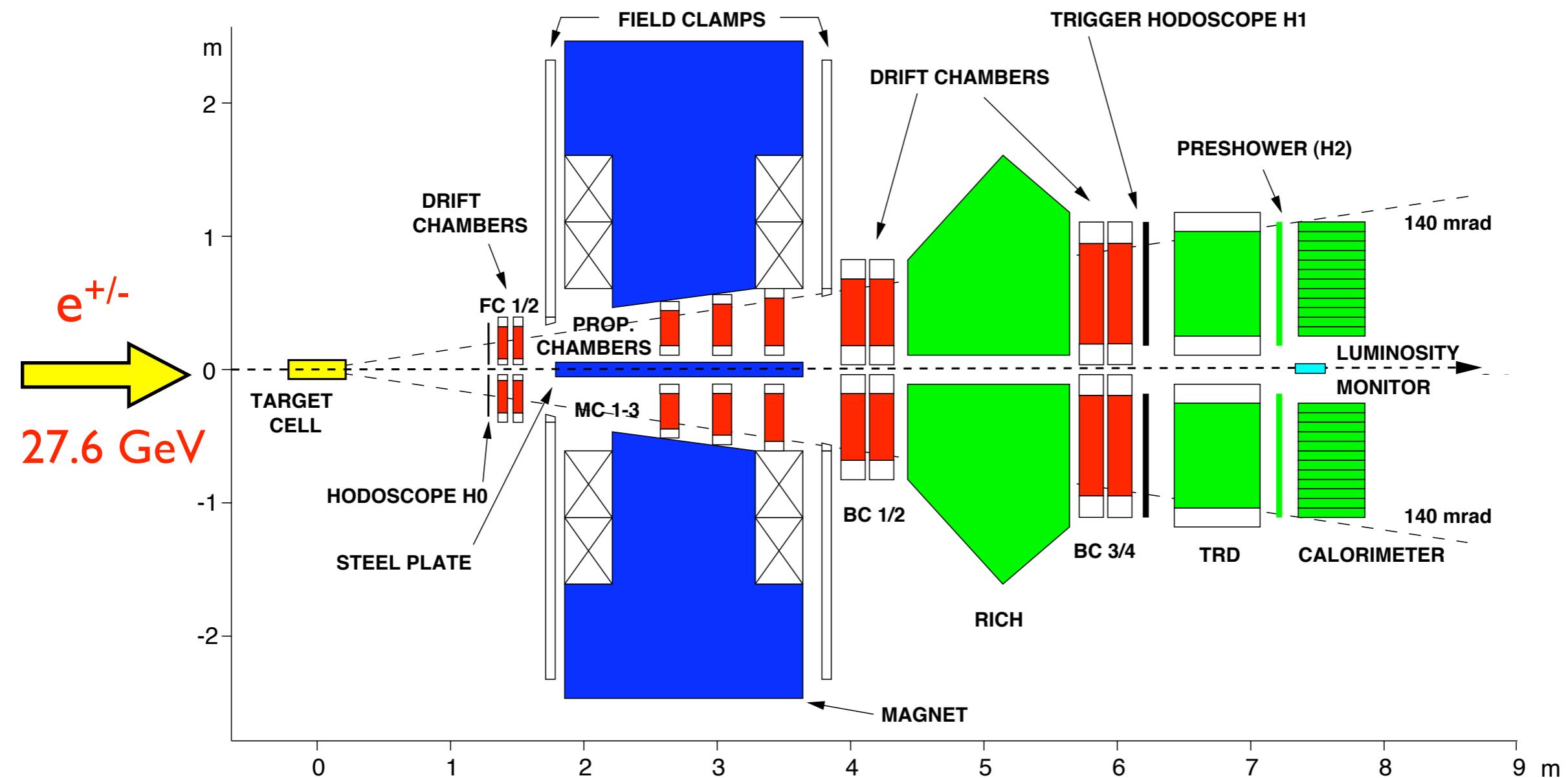
# Latest results on transverse momentum dependent distribution functions

Achim Hillenbrand  
(DESY Zeuthen)

for the  collaboration

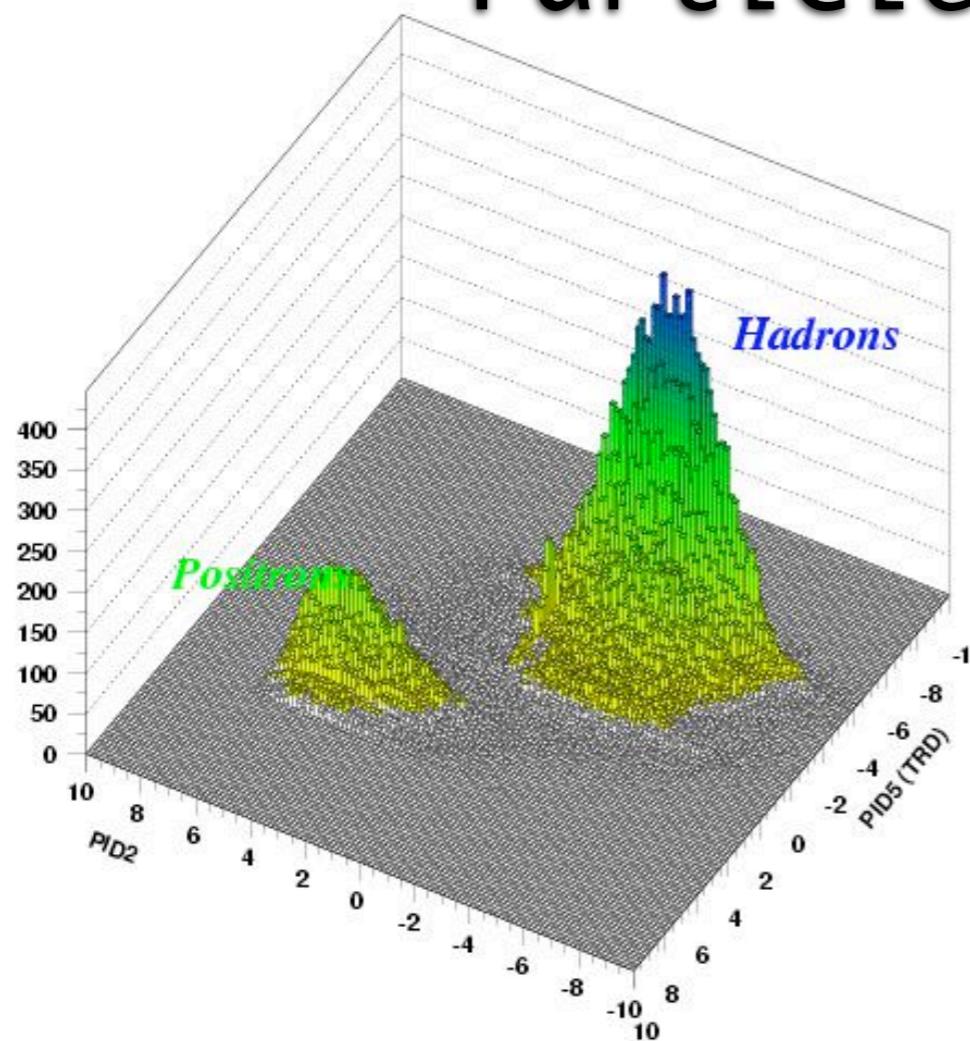
- HERMES overview
- Transverse single-spin asymmetries in semi-inclusive DIS
  - ▶ Collins effect (final results: Phys. Lett. B 693 (2010) 10-16)
  - ▶ Sivers effect (final results: PRL 103 (2009) 152002)
- Transverse target single-spin asymmetries in inclusive hadron production in DIS (new preliminary results)

# HERMES Spectrometer



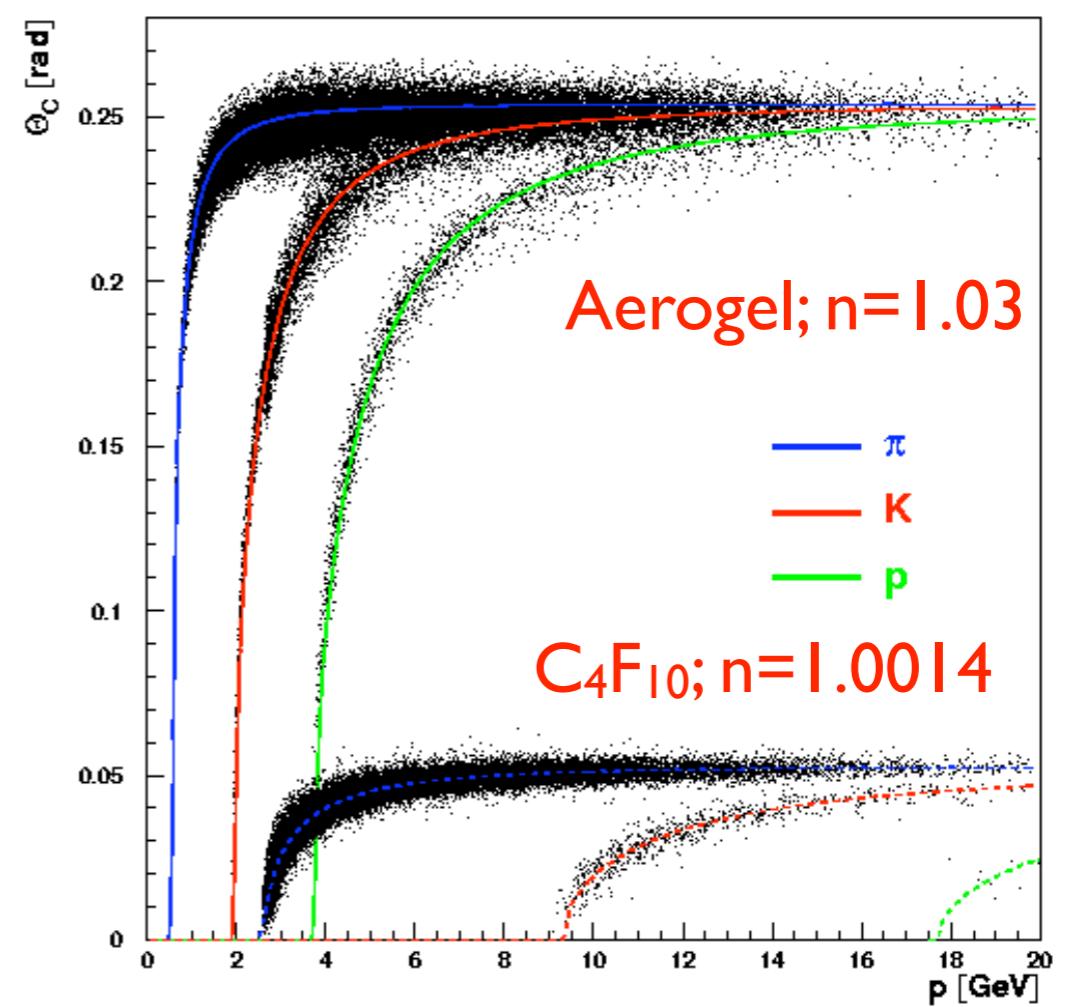
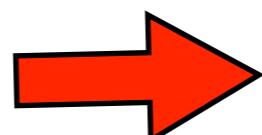
- forward acceptance spectrometer:  $40 \text{ mrad} \leq \Theta \leq 220 \text{ mrad}$
- kinematic coverage:  $0.02 \leq x_{Bj} \leq 0.8$  for  $Q^2 > 1 \text{ GeV}^2$  and  $W > 2 \text{ GeV}$
- tracking:  $\delta P/P = 0.7\% - 2.5\%$ ,  $\delta \Theta \leq 1 \text{ mrad}$
- **PID: TRD, Preshower, Calorimeter, RICH**

# Particle Identification



excellent lepton/hadron separation

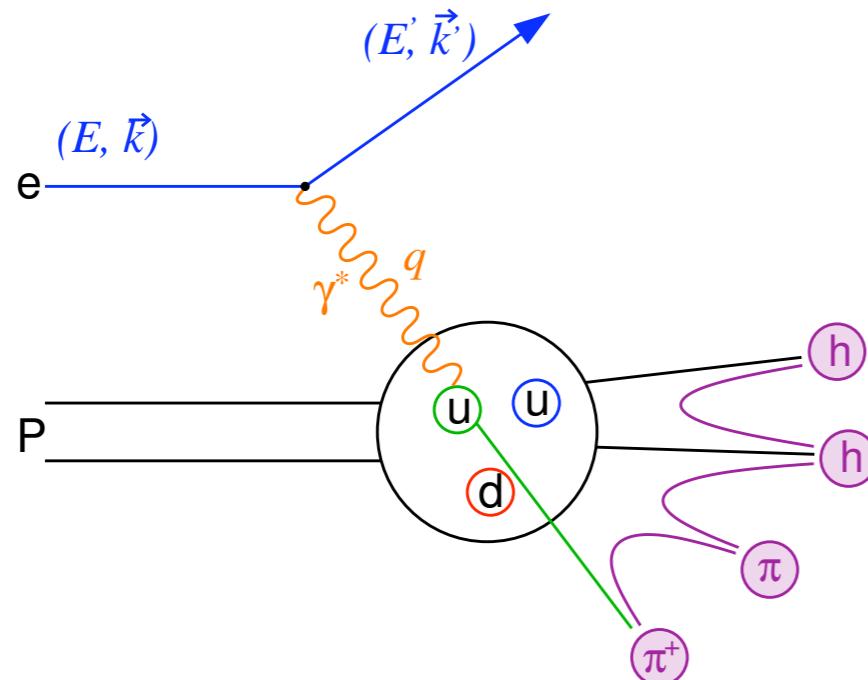
RICH: two radiators allow  
hadron separation  
between 2-15 GeV



# Transverse target single-spin asymmetries in semi-inclusive DIS

# DIS: probing the nucleon structure

e<sup>+, -</sup> @ 27.6 GeV (HERA)



$$\begin{aligned} Q^2 &= -q^2 = -(k - k')^2 \\ \nu &\stackrel{lab}{=} E - E' \\ x &= \frac{Q^2}{2M\nu} \\ z &\stackrel{lab}{=} \frac{E_{\text{had}}}{\nu} \end{aligned}$$

Target:  
H:  $\langle P_{\text{trans}} \rangle \sim 72.5 \pm 5.3\%$

Cross section contains Distribution Functions and Fragmentation Functions:

$$\sigma^{ep \rightarrow ehX} \sim \sum_q DF^{p \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}$$

DF: distribution of quarks in the nucleon

FF: fragmentation of (struck) quark into hadronic final state

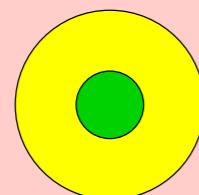
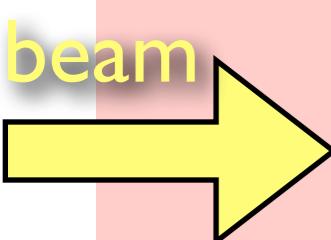
# Distribution functions

Leading twist:

**3 DFs survive integration over transverse quark momenta**

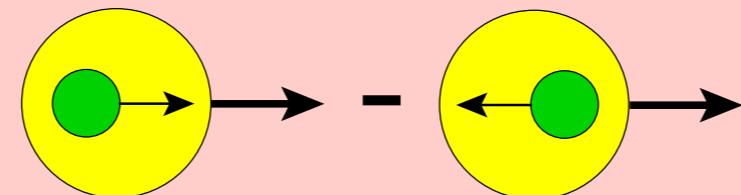
**momentum distribution**

$$q(x)$$



**helicity distribution**

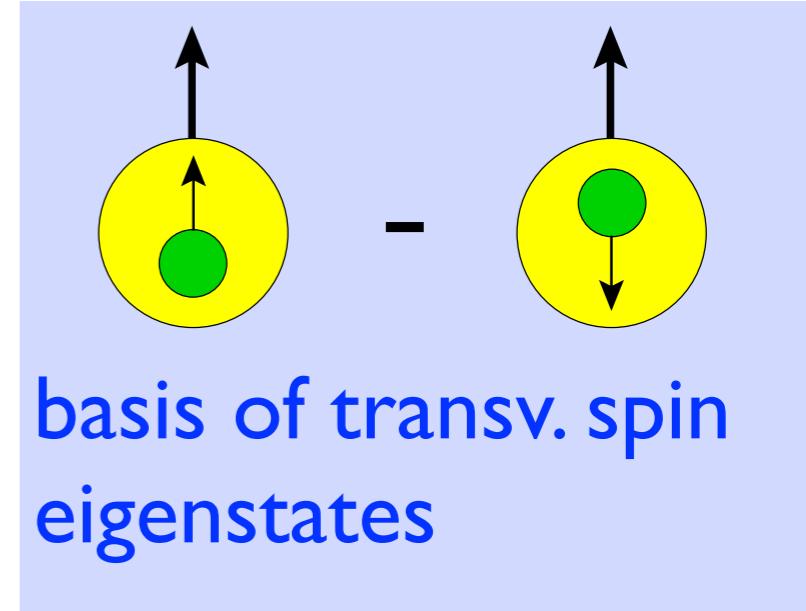
$$\Delta q(x)$$



**helicity basis**

**transversity distribution**

$$\delta q(x)$$

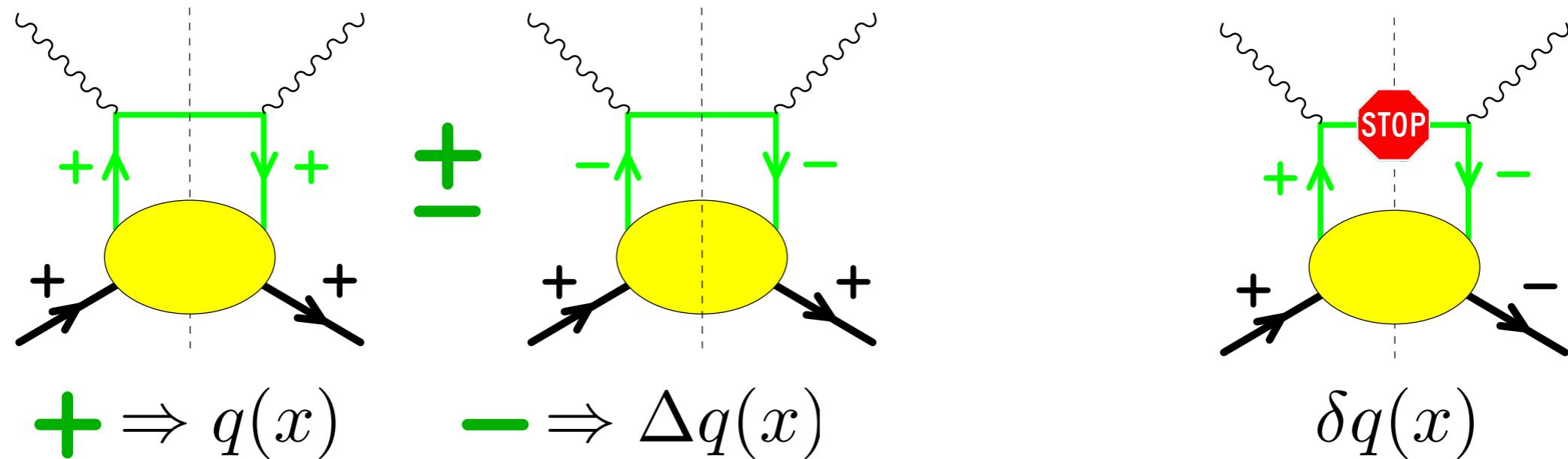


**basis of transv. spin eigenstates**

**all three DFs needed for complete description of the nucleon!**

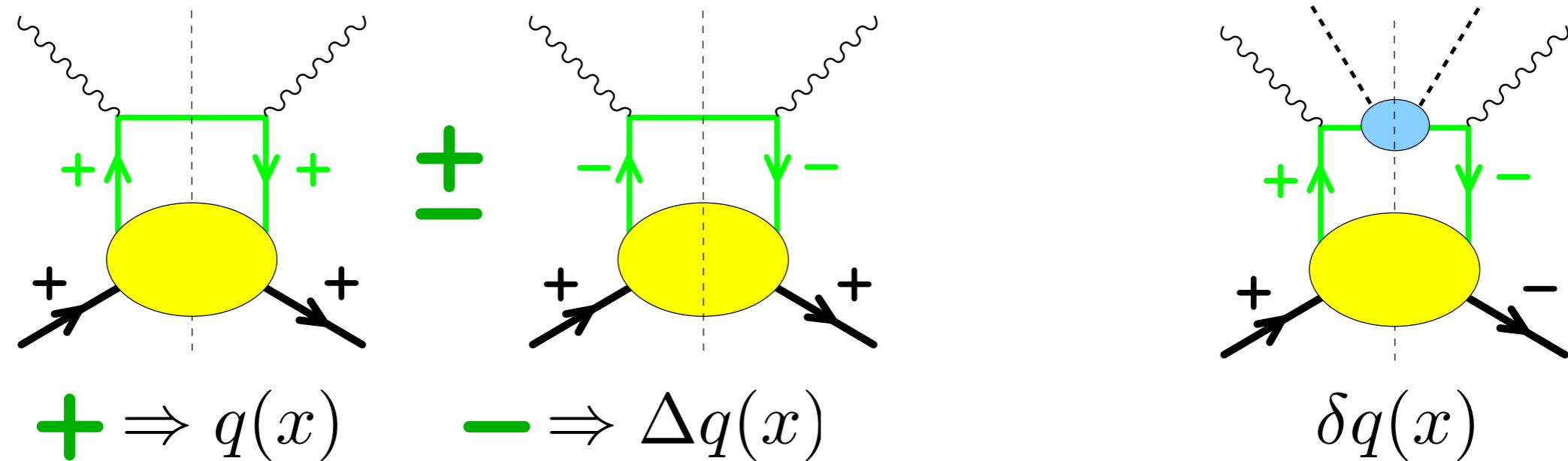
# Transversity $\delta q$

- $\delta q$ : helicity-flip of the quark  $\Rightarrow$  chiral-odd

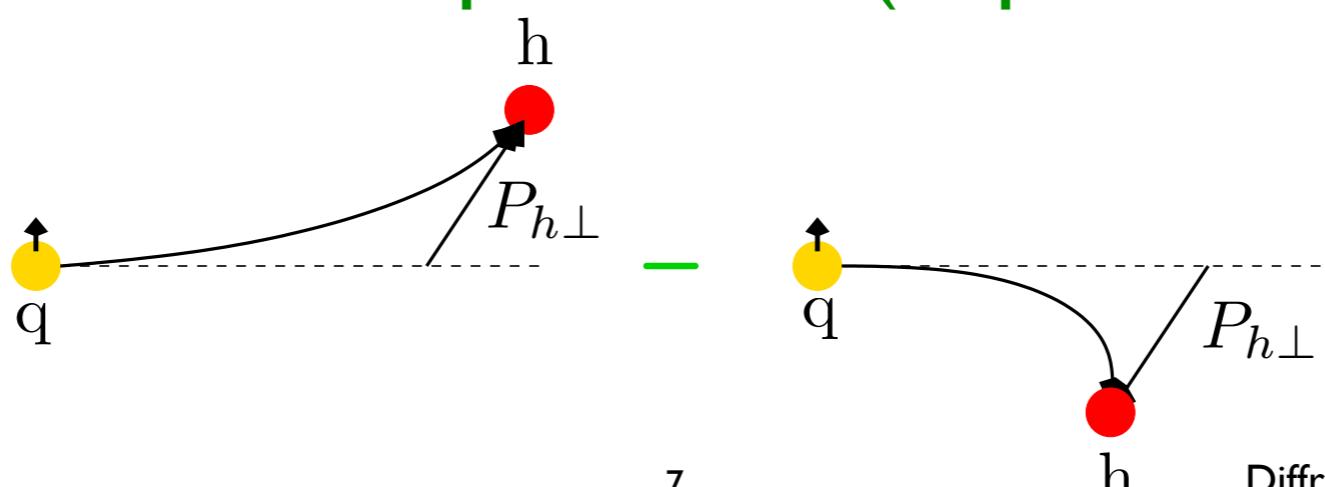


# Transversity $\delta q$

- $\delta q$ : helicity-flip of the quark  $\Rightarrow$  chiral-odd



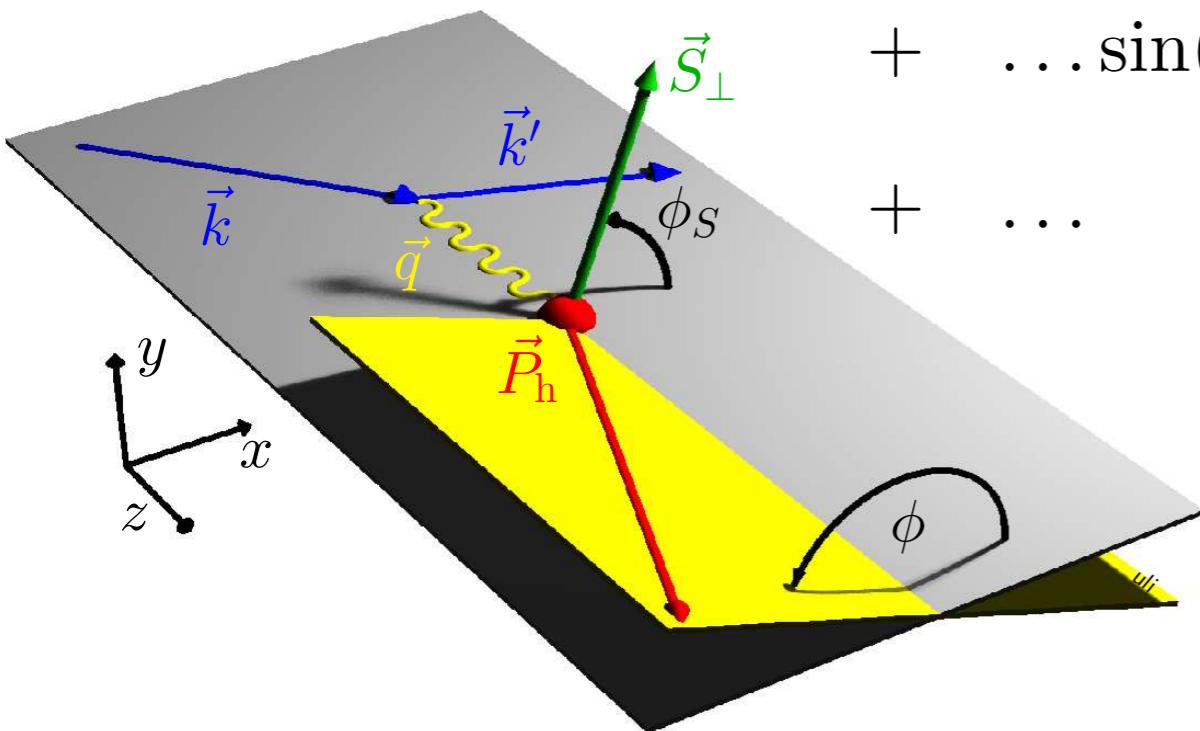
- Collins-FF  $H_{I^\perp}$  describes **correlation** between **transverse polarisation of fragmenting quark** and the **transverse momentum  $P_{h\perp}$  of the produced (unpolarised) hadron**



# Azimuthal Asymmetries

Measurement of cross-section asymmetries depending on the azimuthal angles  $\Phi$  and  $\Phi_S$

$$\begin{aligned}
 A_{UT}(\phi, \phi_S, \dots) &= \frac{1}{S_\perp} \frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow} \\
 &\sim \dots \sin(\phi + \phi_S) \frac{\sum_q e_q^2 \mathcal{I} [\dots \delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2)]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)} \\
 &+ \dots \sin(\phi - \phi_S) \frac{\sum_q e_q^2 \mathcal{I} [\dots f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2)]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}
 \end{aligned}$$



$\mathcal{I} [\dots]$  convolution integral over  
initial ( $\text{p}_T$ ) and final ( $\text{k}_T$ )  
quark transverse momenta

# Azimuthal Asymmetries

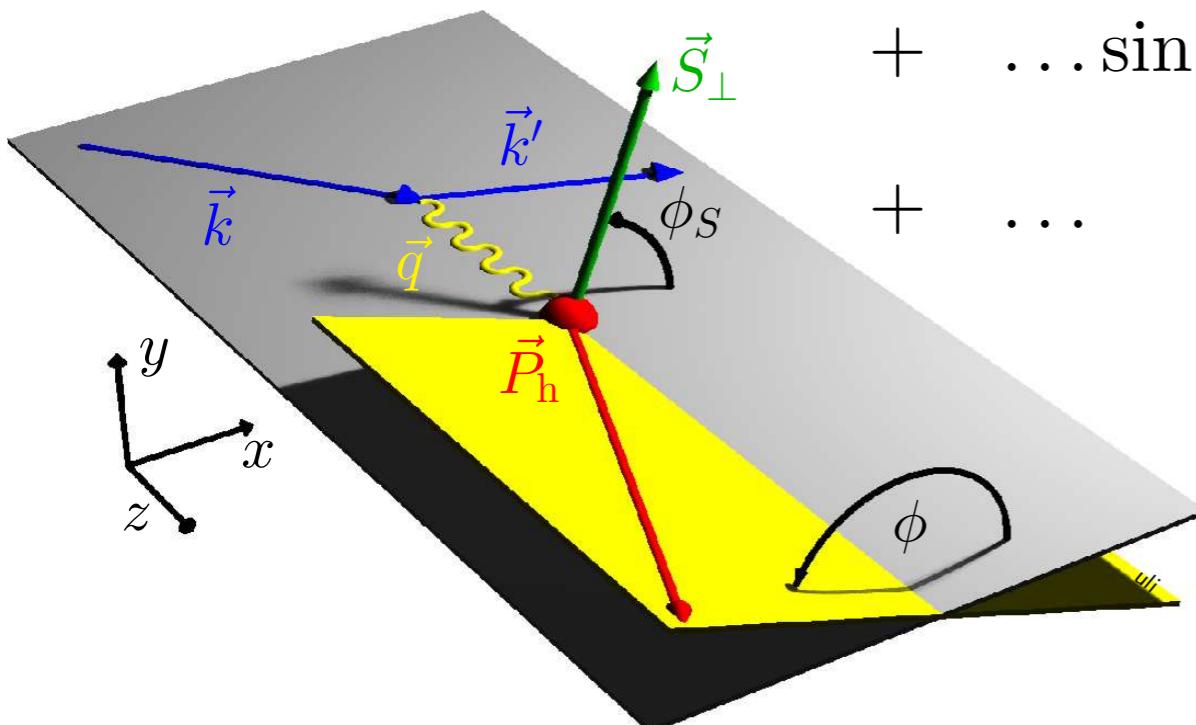
Measurement of cross-section asymmetries depending on the azimuthal angles  $\Phi$  and  $\Phi_S$

$$A_{UT}(\phi, \phi_S, \dots) = \frac{1}{S_\perp} \frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow}$$

**Collins Amplitude**

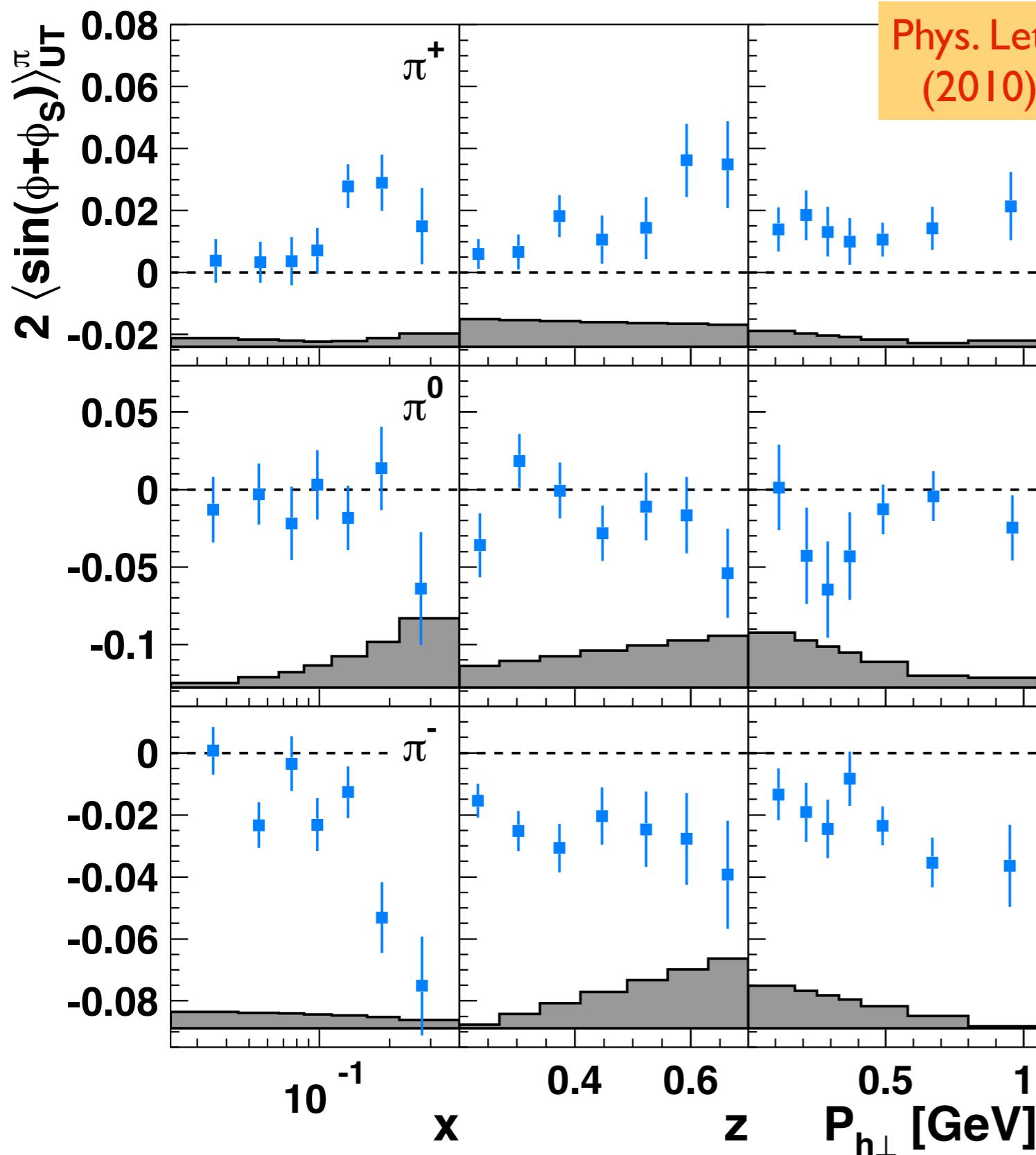
$$\sim \dots \sin(\phi + \phi_S) \frac{\sum_q e_q^2 \mathcal{I} [\dots \delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2)]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

$$+ \dots \sin(\phi - \phi_S) \frac{\sum_q e_q^2 \mathcal{I} [\dots f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2)]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$



$\mathcal{I} [\dots]$  convolution integral over initial ( $p_T$ ) and final ( $k_T$ ) quark transverse momenta

# Collins Amplitudes for Pions



Phys. Lett. B 693  
(2010) 10-16

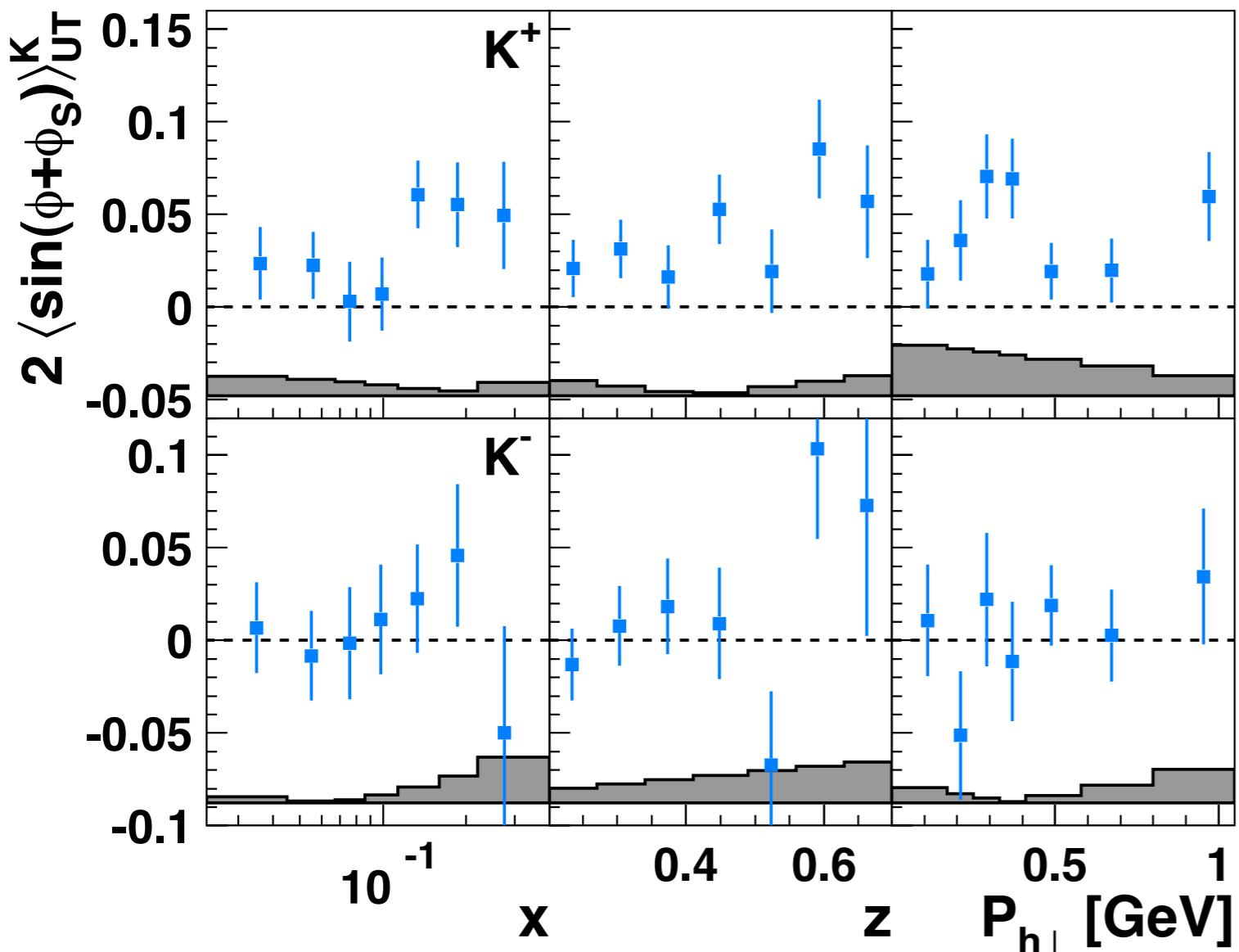
$$A_C \propto \delta q \otimes H_1^\perp$$

- positive amplitudes for  $\pi^+$
  - large negative  $\pi^-$  amplitude
  - $\pi^0$  consistent with zero (isospin symmetry)
  - information from another process on Collins FF (BELLE) allows extraction of  $\delta q$  (eg. Anselmino et. al. Phys. Rev. D75:054032, 2007)
- $u \rightarrow \pi^+ \Rightarrow H_1^{\perp, \text{fav}}$   
 $u \rightarrow \pi^- \Rightarrow H_1^{\perp, \text{unfav}}$   
 $\Rightarrow H_1^{\perp, \text{fav}} \approx -H_1^{\perp, \text{unfav}}$

# Collins Amplitudes for Kaons

Phys. Lett. B 693  
(2010) 10-16

$$A_C \propto \delta q \otimes H_1^\perp$$



- Collins amplitudes for  $K^+$  **larger than for  $\pi^+$**
- Collins fragmentation function for kaons **unknown**
- Collins amplitudes for  $K^-$  **consistent with zero**
- Sea quark transversity **expected to be small**

# Azimuthal Asymmetries

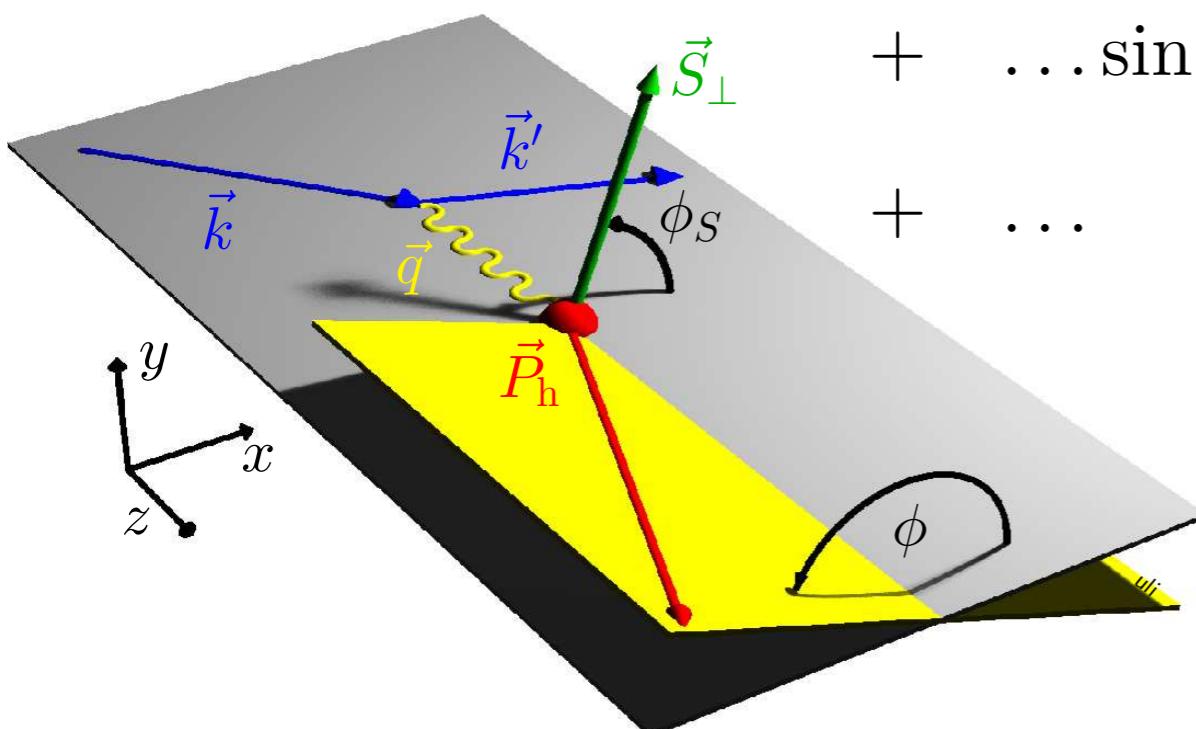
Measurement of cross-section asymmetries depending on the azimuthal angles  $\Phi$  and  $\Phi_S$

$$A_{UT}(\phi, \phi_S, \dots) = \frac{1}{S_\perp} \frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow}$$

**Collins Amplitude**

$$\sim \dots \sin(\phi + \phi_S) \frac{\sum_q e_q^2 \mathcal{I} [\dots \delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2)]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

$$+ \dots \sin(\phi - \phi_S) \frac{\sum_q e_q^2 \mathcal{I} [\dots f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2)]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$



$\mathcal{I} [\dots]$  convolution integral over  
initial ( $p_T$ ) and final ( $k_T$ )  
quark transverse momenta

# Azimuthal Asymmetries

Measurement of cross-section asymmetries depending on the azimuthal angles  $\Phi$  and  $\Phi_S$

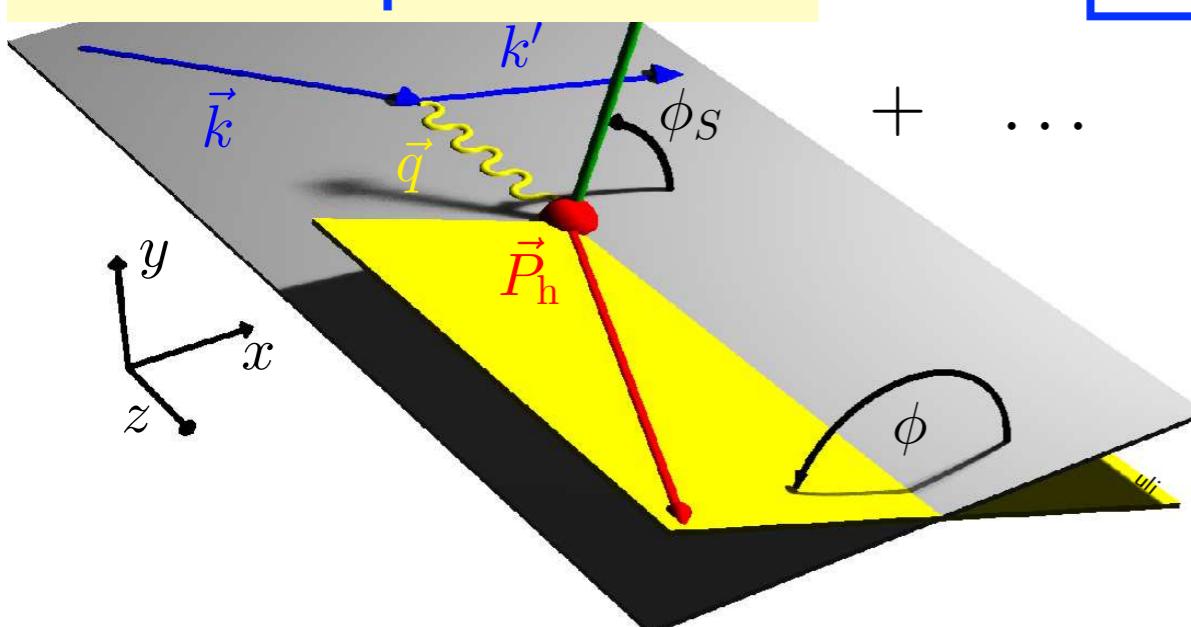
$$A_{UT}(\phi, \phi_S, \dots) = \frac{1}{S_\perp} \frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow}$$

**Collins Amplitude**

$$\sim \dots \boxed{\sin(\phi + \phi_S)} \frac{\sum_q e_q^2 \mathcal{I} \left[ \dots \boxed{\delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2)} \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

**Sivers Amplitude**

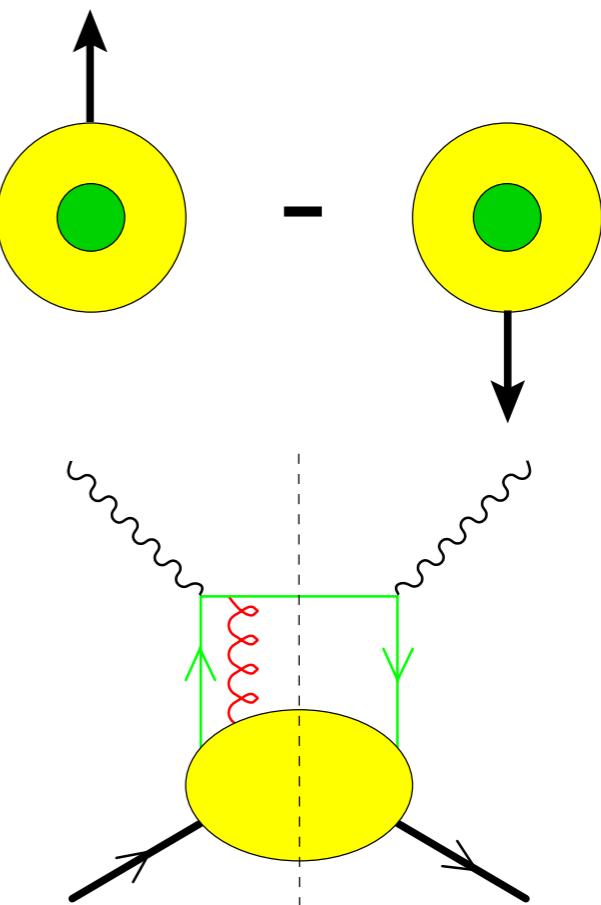
$$+ \dots \boxed{\sin(\phi - \phi_S)} \frac{\sum_q e_q^2 \mathcal{I} \left[ \dots \boxed{f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2)} \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$



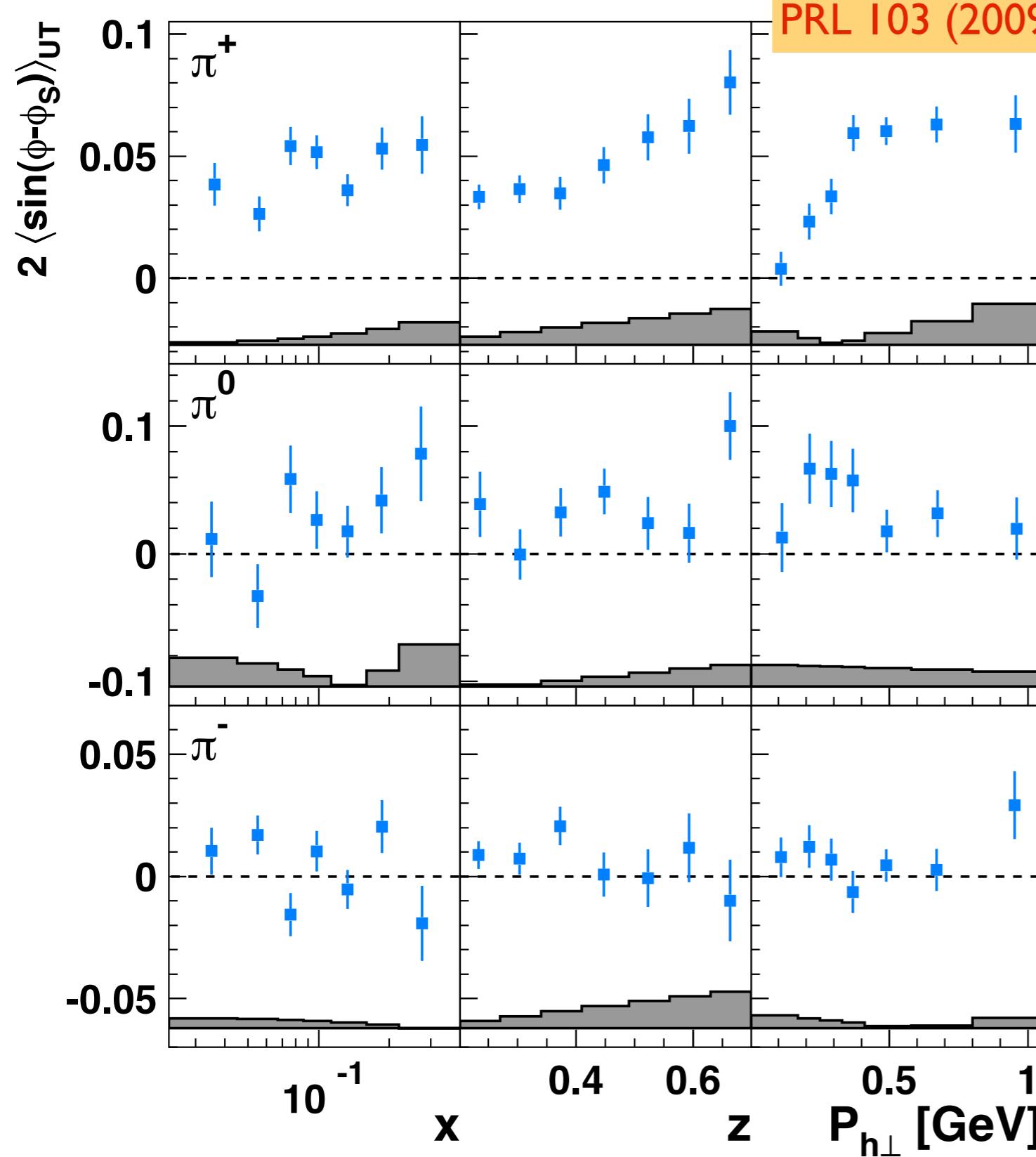
$\mathcal{I}[\dots]$  convolution integral over  
initial ( $\text{pt}$ ) and final ( $\text{k}_T$ )  
quark transverse momenta

# Sivers function

- describes **correlation** between **intrinsic transverse quark momentum ( $p_T$ )** and **transverse nucleon spin**
- chiral-even function
- T-odd functions allowed due to **final state interactions (FSI)**:  
quark rescattering via a soft gluon
- non-zero Sivers function requires  
**non-vanishing orbital angular momentum**  
in the nucleon wave function  
**(can contribute to nucleon spin!)**



# Sivers Amplitudes for Pions



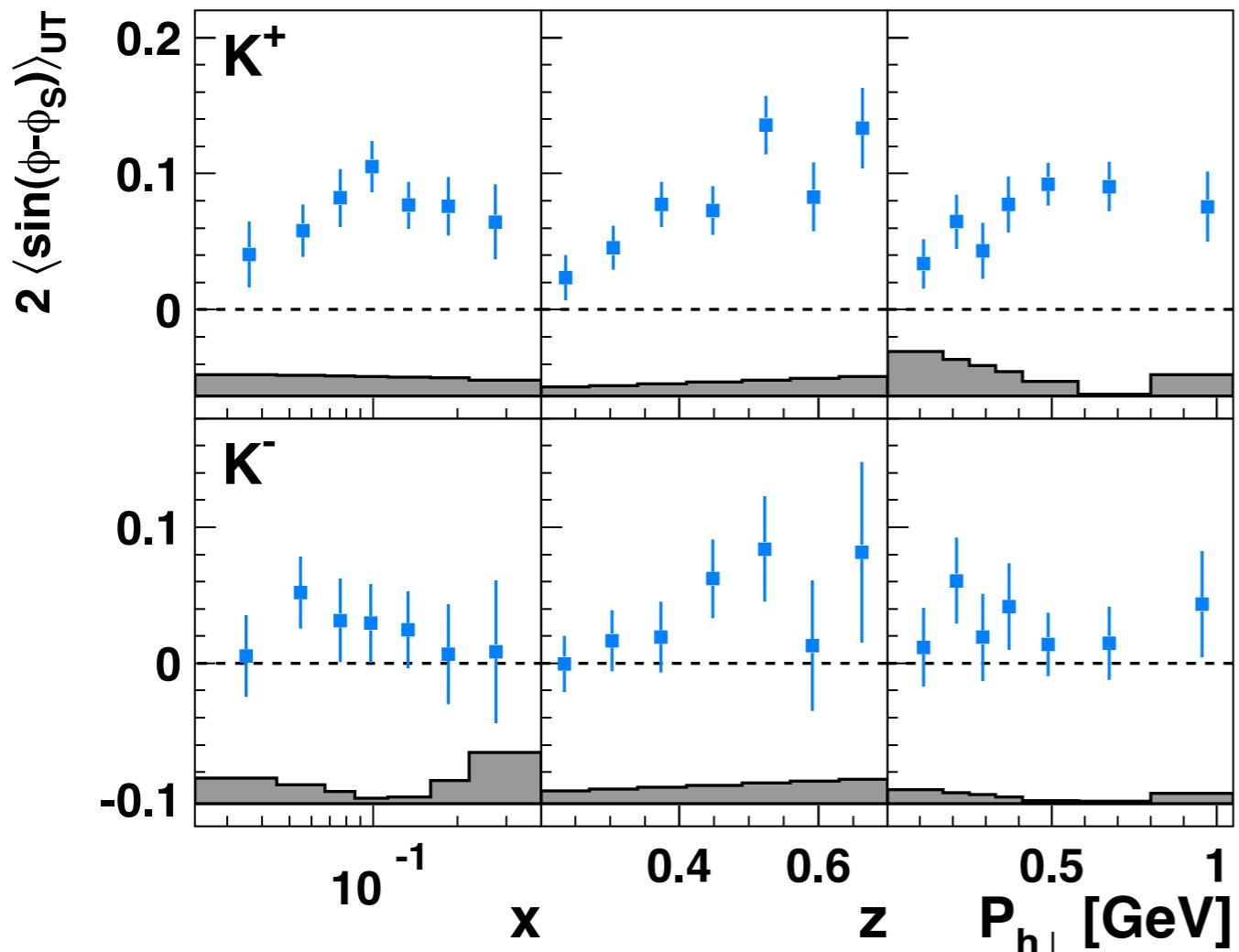
PRL 103 (2009) 152002

$$A_S \propto f_{1T}^\perp \otimes D_1^q$$

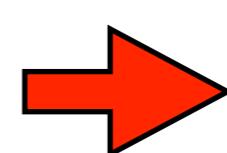
- significantly positive for  $\pi^+$
- rise with low  $P_{h\perp}$ , plateau at high  $P_{h\perp}$
- implies non-zero orbital angular momentum of quarks
- slightly positive for  $\pi^-$
- isospin symmetry of  $\pi$  mesons fulfilled

# Sivers Amplitudes for Kaons

PRL 103 (2009) 152002



- significantly positive for  $K^+$
- implies non-zero orbital angular momentum of quarks
- slightly positive for  $K^-$
- $K^+$  amplitude larger than  $\pi^+$  amplitude

 sea quark contribution to Sivers mechanism may be important

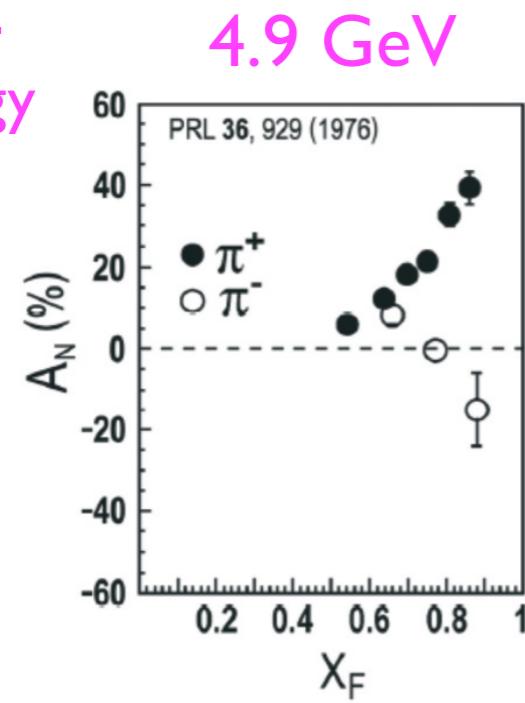
$$\pi^+ = |u\bar{d}\rangle \quad K^+ = |u\bar{s}\rangle$$

# Transverse target single-spin asymmetries in inclusive hadron production in DIS

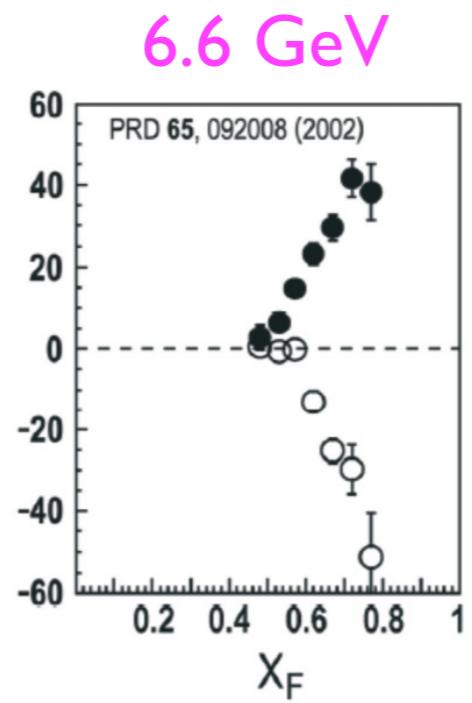
# Transverse single-spin asymmetry of inclusive hadrons (I)

- reminder: clear **non-zero left-right asymmetry  $A_N$**  measured in **inclusive pion production in  $p^\uparrow p$  collisions:**

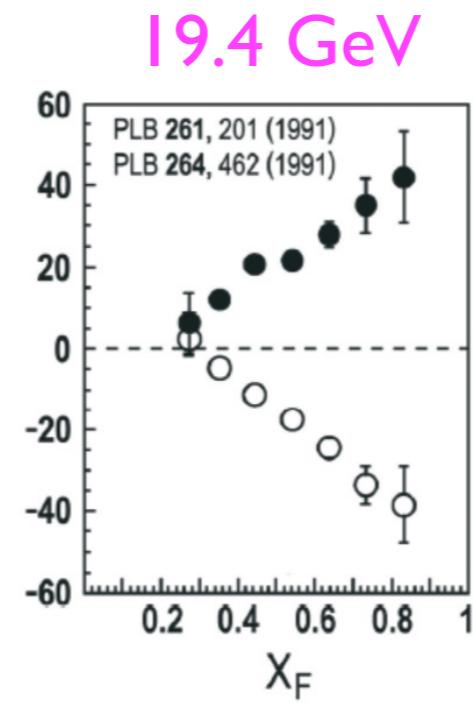
center-of-  
mass energy



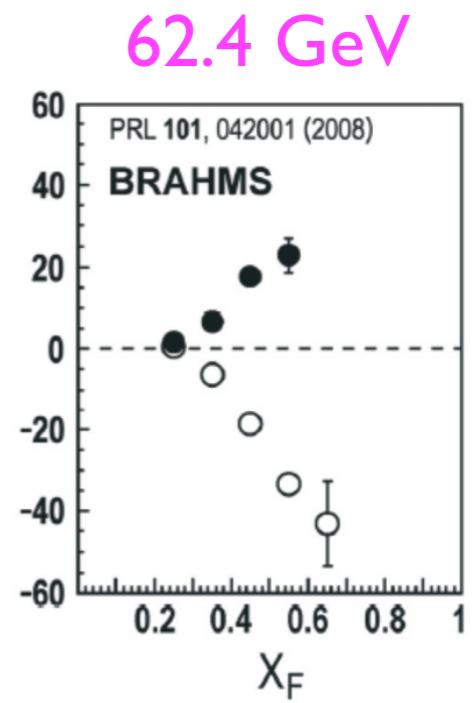
1976



2002



1991

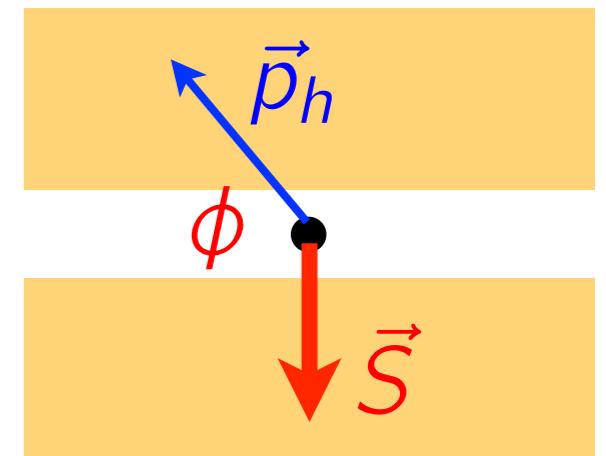


2008

- two models for two approaches:
  - TMD approach: both Sivers and Collins can contribute
  - collinear (high- $p_T$ ) approach: Sivers-like and Collins-like

# Transverse single-spin asymmetry of inclusive hadrons (II)

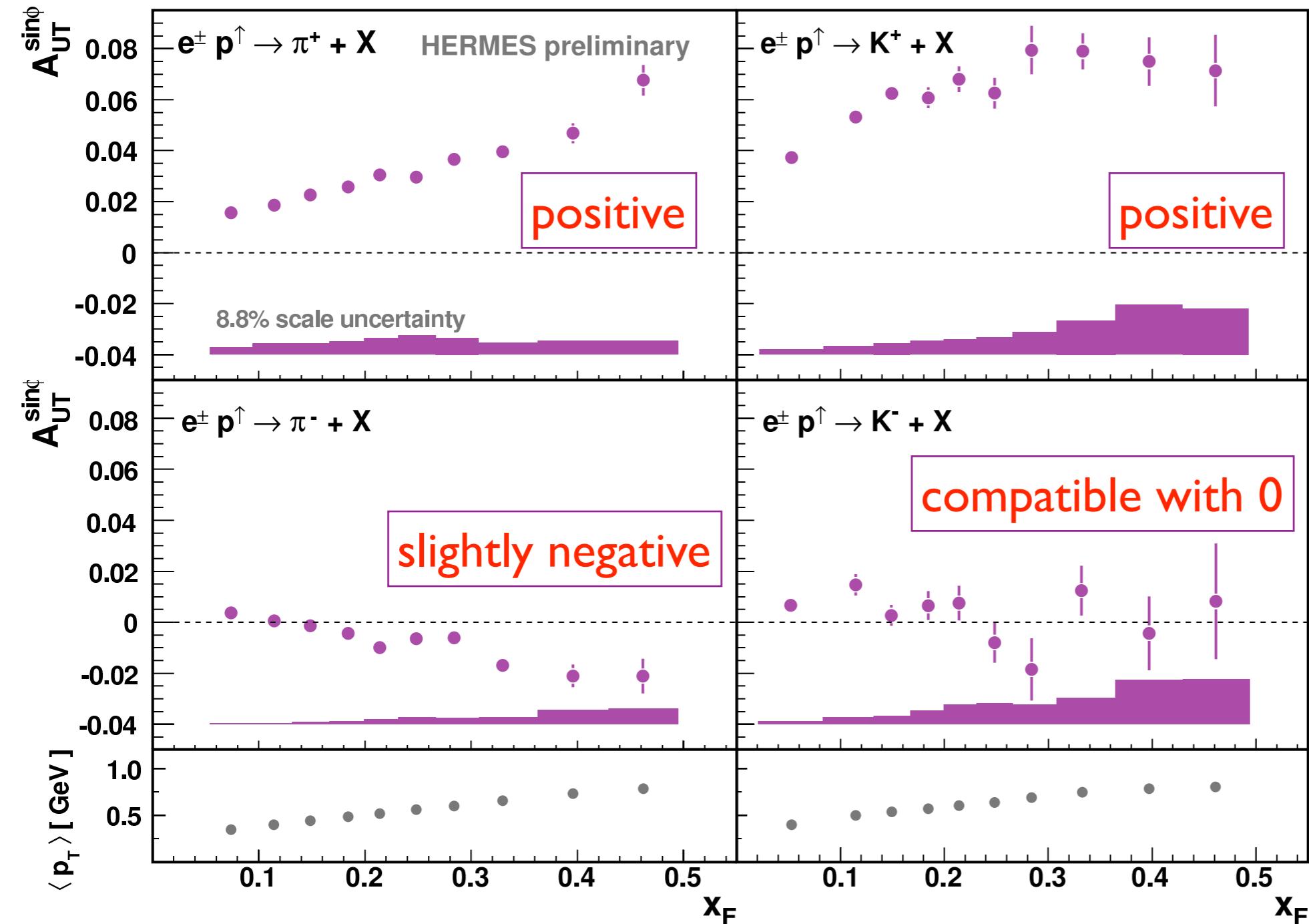
- so far: all available data from  $p^\uparrow p$  collisions
- HERMES data:
  - ▶ first data on leptoproduction  $l p^\uparrow$   
(scattered lepton not detected  $\Rightarrow$  quasi-real photoproduction)
  - ▶ high statistics ( $\sim 100$  Million hadrons)
  - ▶ complimentary to  $p^\uparrow p$ , cleaner channel (one  $p$  quark field)
  - ▶ target spin  $S$  reversed every 90s (cancelation of systematic effects)



$$A_{UT}(x, Q^2, \phi) \cong A_{UT}^{\sin \phi}(x, Q^2) \sin(\phi)$$

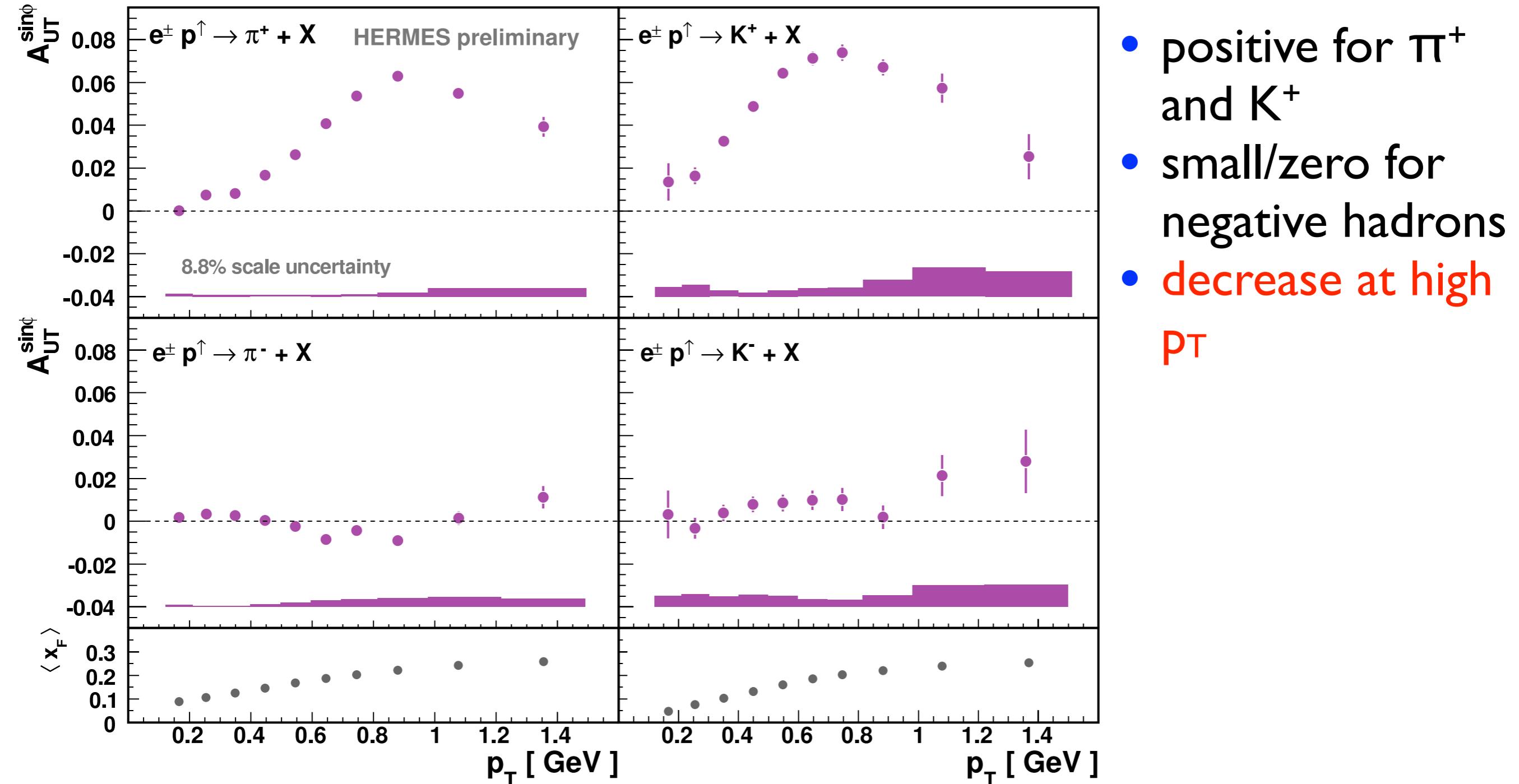
- prediction:  $A_{UT} \rightarrow 0$  for high  $p_T$  and for  $p_T \rightarrow 0$

# A<sub>UT</sub> of incl hadrons vs x<sub>F</sub>

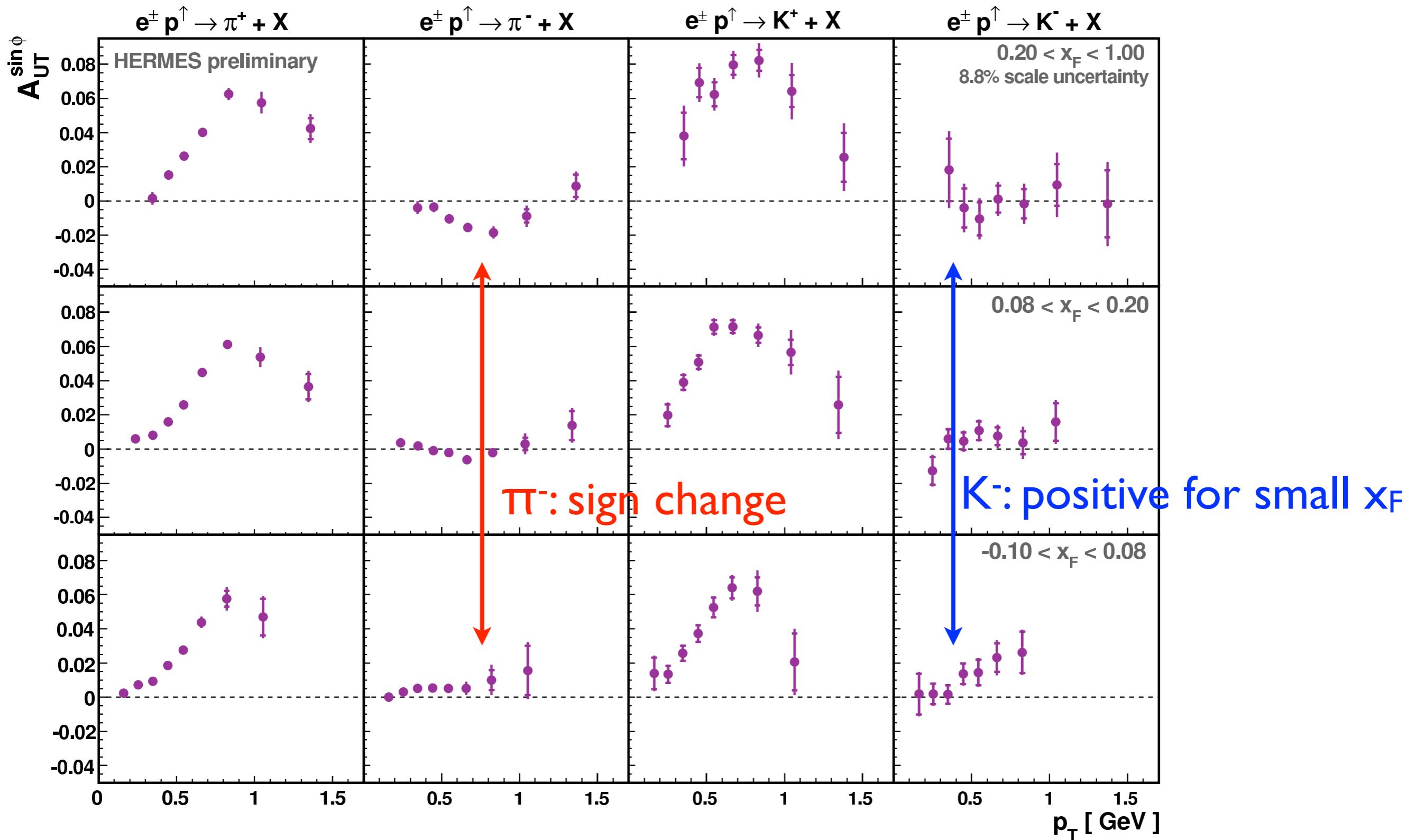


- $\pi\pi$ : similar to  $p^\uparrow p$
- $K$ :
- $p^\uparrow p$  (Brahms):  
 $K^+$  and  $K^-$  same size and same sign

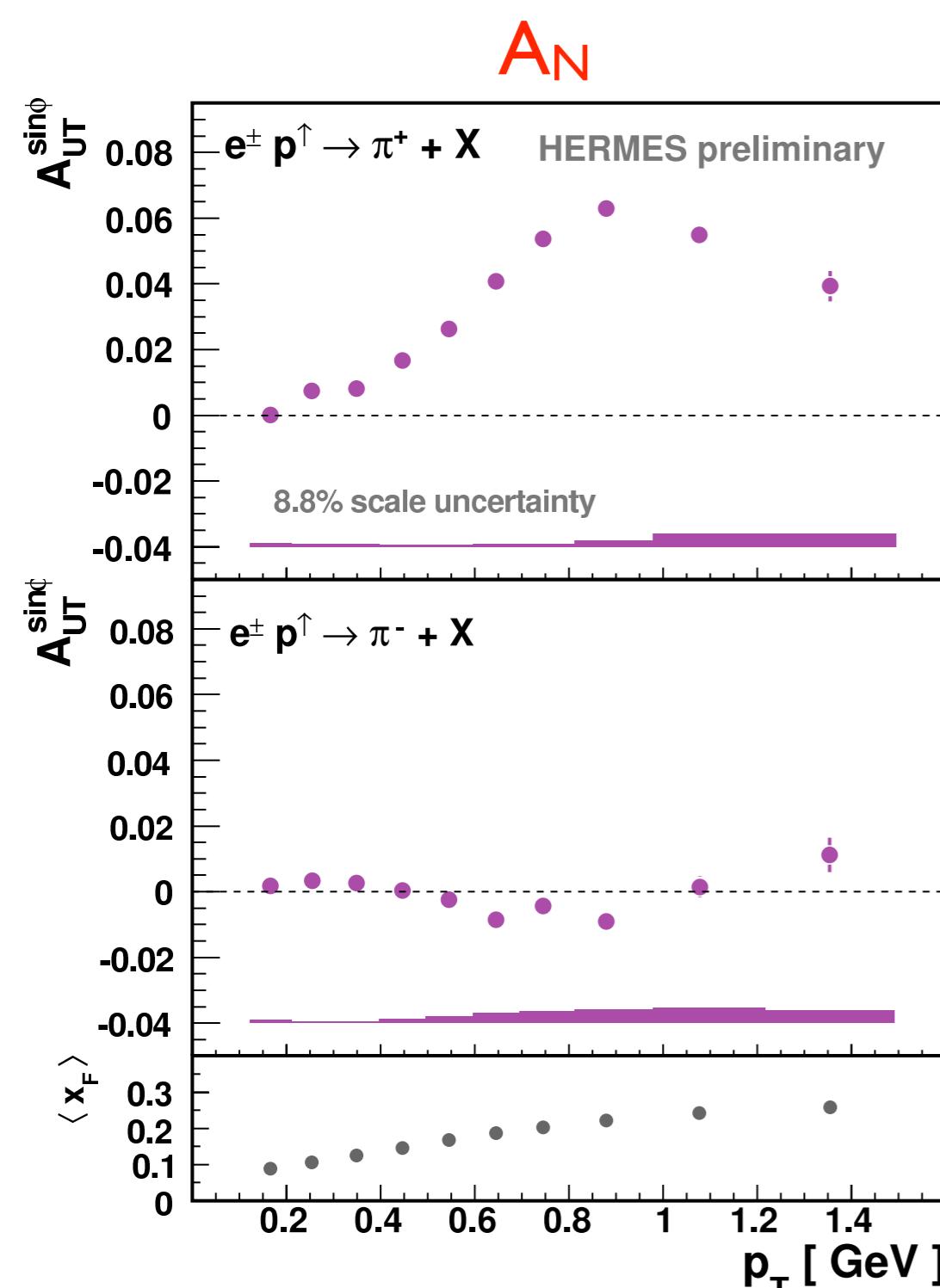
# A<sub>UT</sub> of incl hadrons vs p<sub>T</sub>



# A<sub>UT</sub> of incl hadrons: 2D

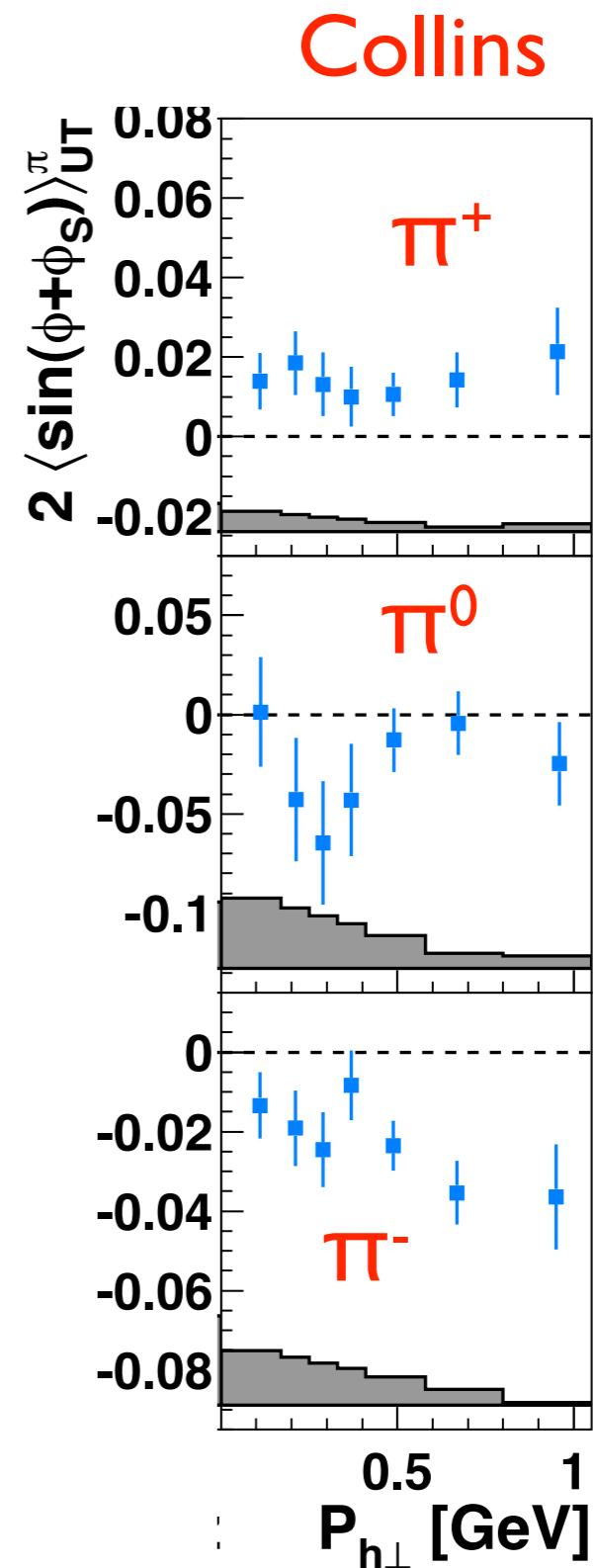
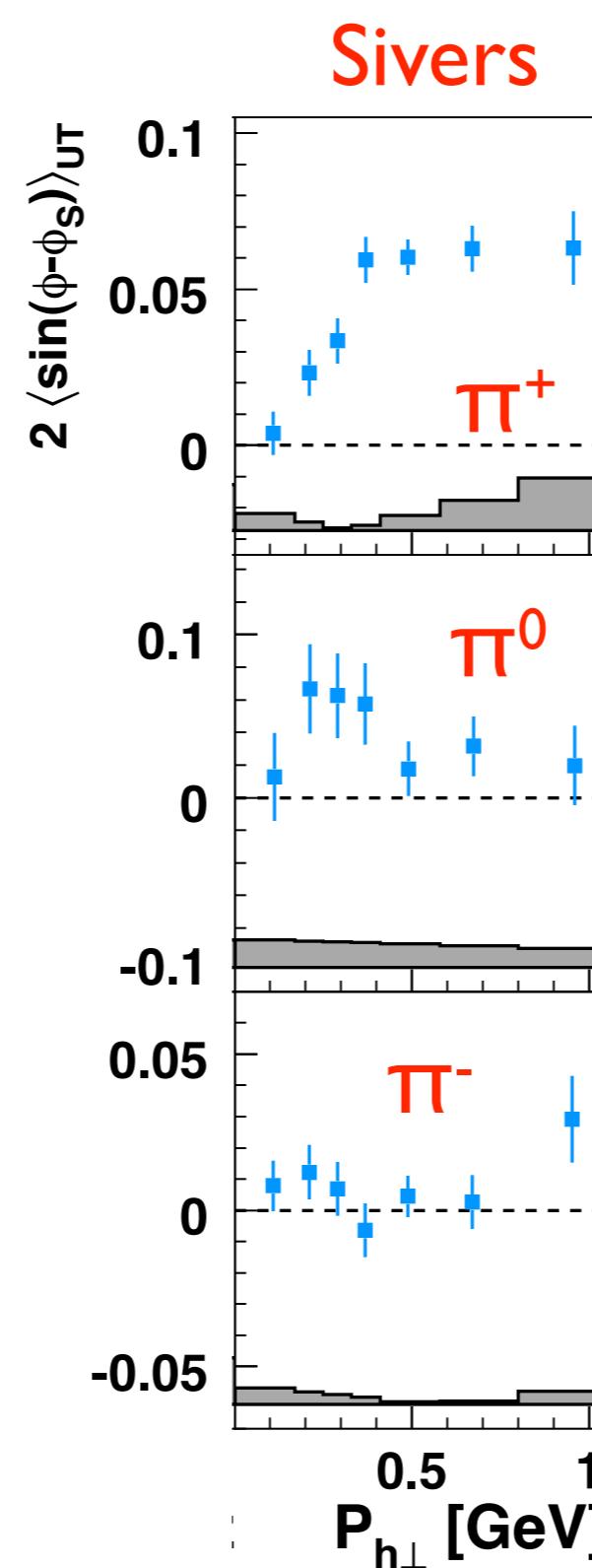


# $A_{UT}$ of incl pions vs $p_t$



$A_N$  resembles Sivers effect

as predicted in M.Anselmino et al., PRD 81(2010) 034007

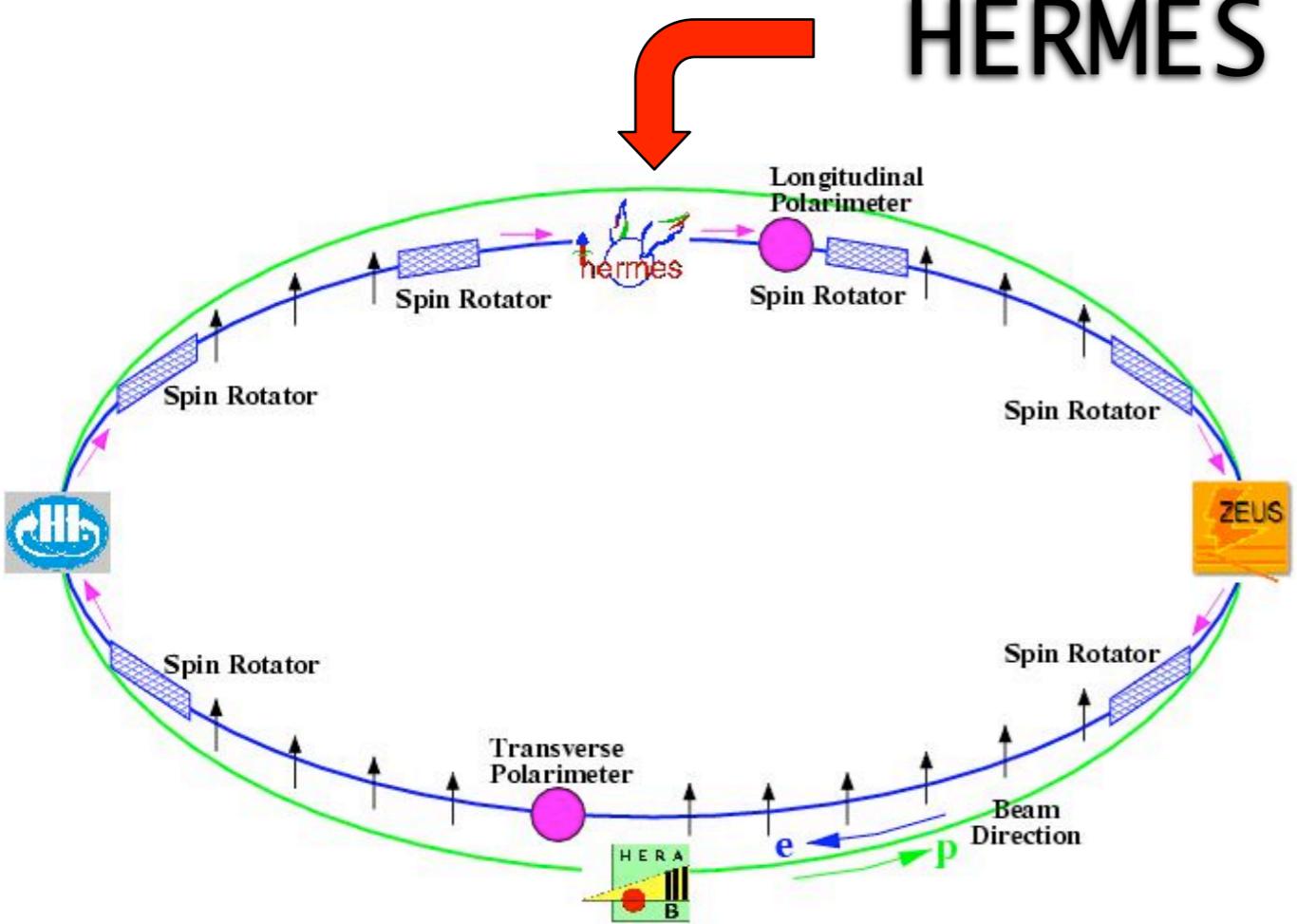


# Conclusions

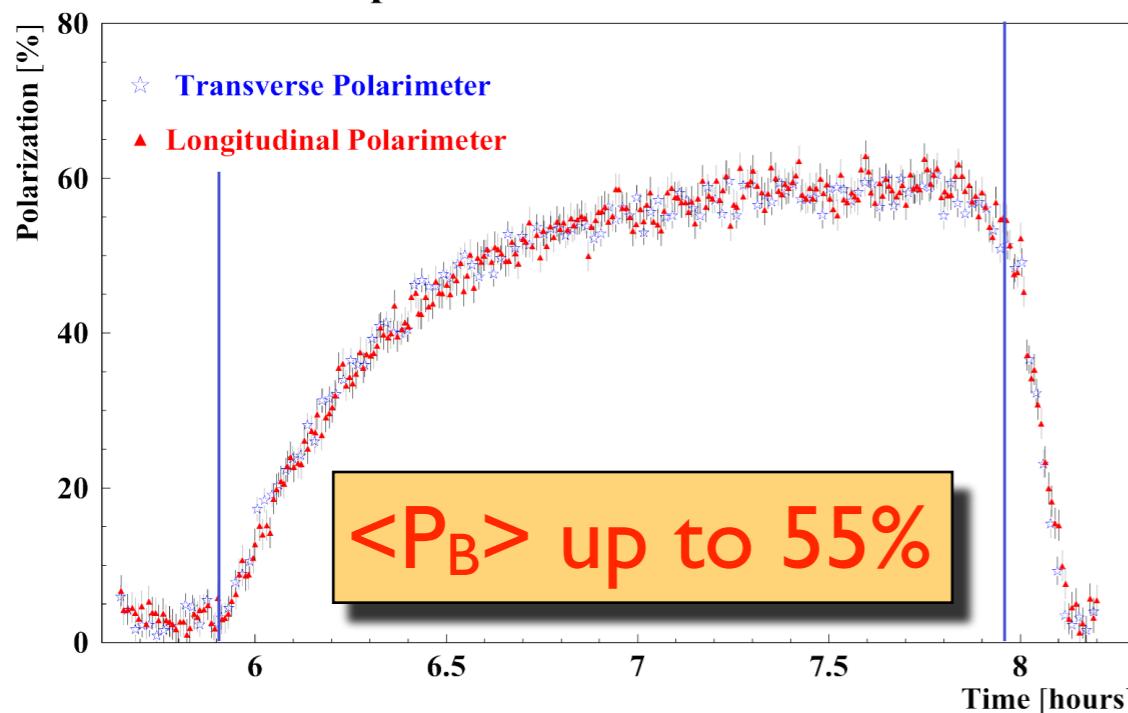
- final results on Collins amplitudes published
  - ▶ significant Collins amplitudes for charged pions and  $K^+$   
⇒ enables quantitative extraction of transversity distribution
- significant Sivers amplitudes for  $\pi^+$  and  $K^+$  mesons
  - ⇒ clear (and first) evidence of naive T-odd parton distribution
  - ⇒ enables quantitative extraction of the Sivers function
- new preliminary results on transverse target single-spin asymmetries in inclusive hadron production
  - ▶ large asymmetry for  $\pi^+$  and  $K^+$
  - ▶ no good theoretical understanding yet of inclusive TTSA

# Backup

# HERMES @ HERA



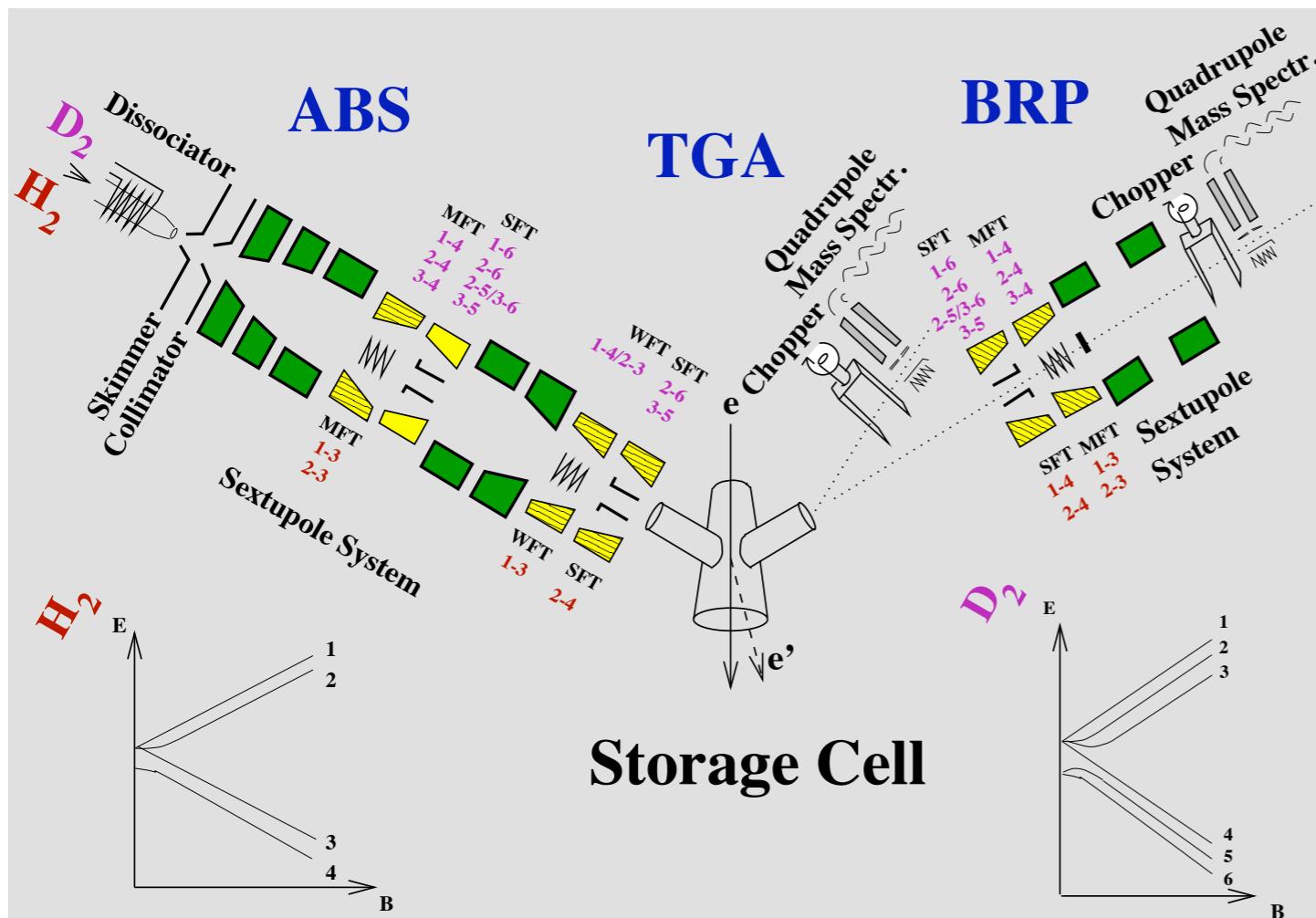
Comparison of rise time curves



- Fixed target experiment  
→ only using HERA lepton ( $e^+/e^-$ ) beam
- HERA lepton beam self-polarizing  
→ cross section asymmetry in synchrotron radiation emission leads to build-up of transverse polarization (Sokolov-Ternov effect)
- Spin-rotators → longitudinal polarization at HERMES interaction region
- Beam polarization measured by two independent polarimeters

# The HERMES Target

Gaseous target in storage cell aligned with lepton beam



**Polarization:**  
 longitudinal: ~85%  
 transversal: ~75%

## Features:

- Pure target (**no dilution**)
- **Unpolarized targets:**  
**variety of nuclear targets**
  - ▶ H, D, He, Ne, Kr, ...
- **Polarized targets:**
  - ▶ Longitudinal pol. ( $\leq 2000$ )  
 H, D, He
  - ▶ Transverse pol. (2002-2005)  
 H
  - ▶ **Rapid reversal of polarization direction**  
**within 0.5s (every 90s)**