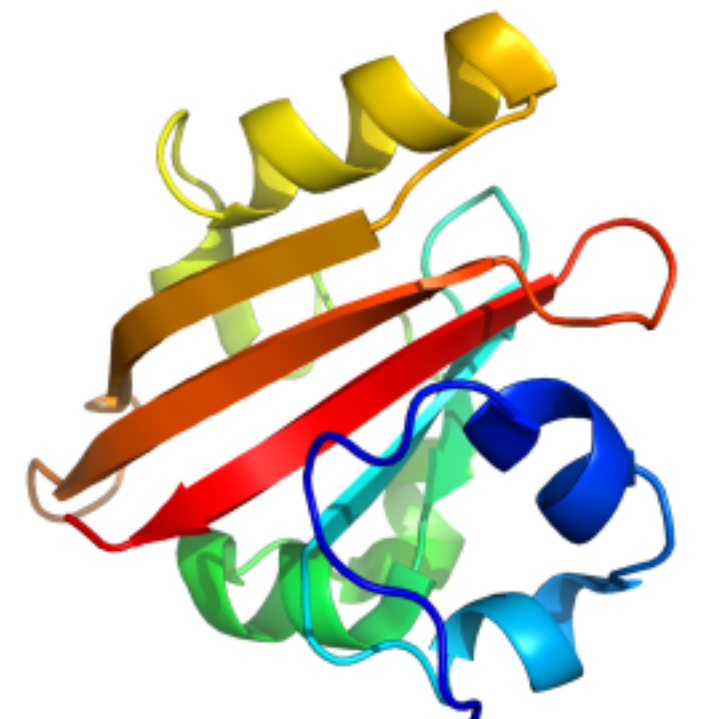
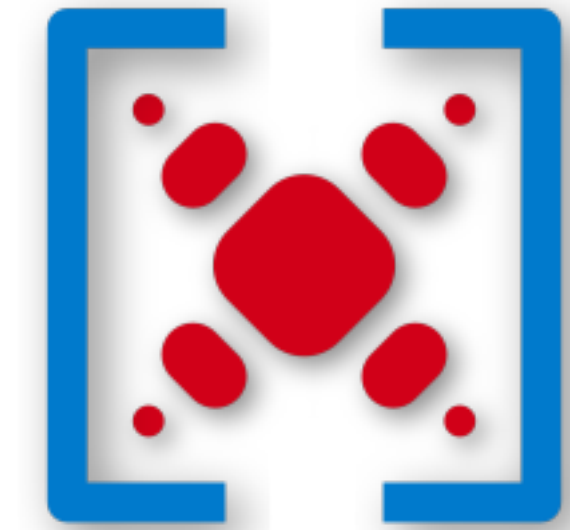
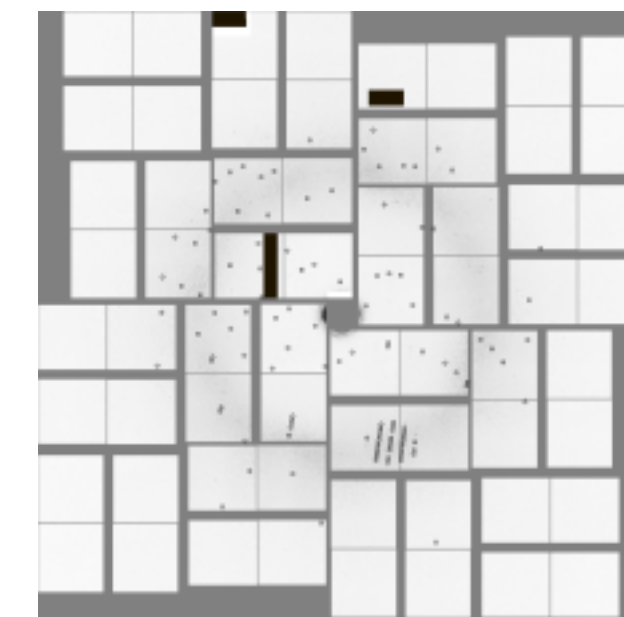


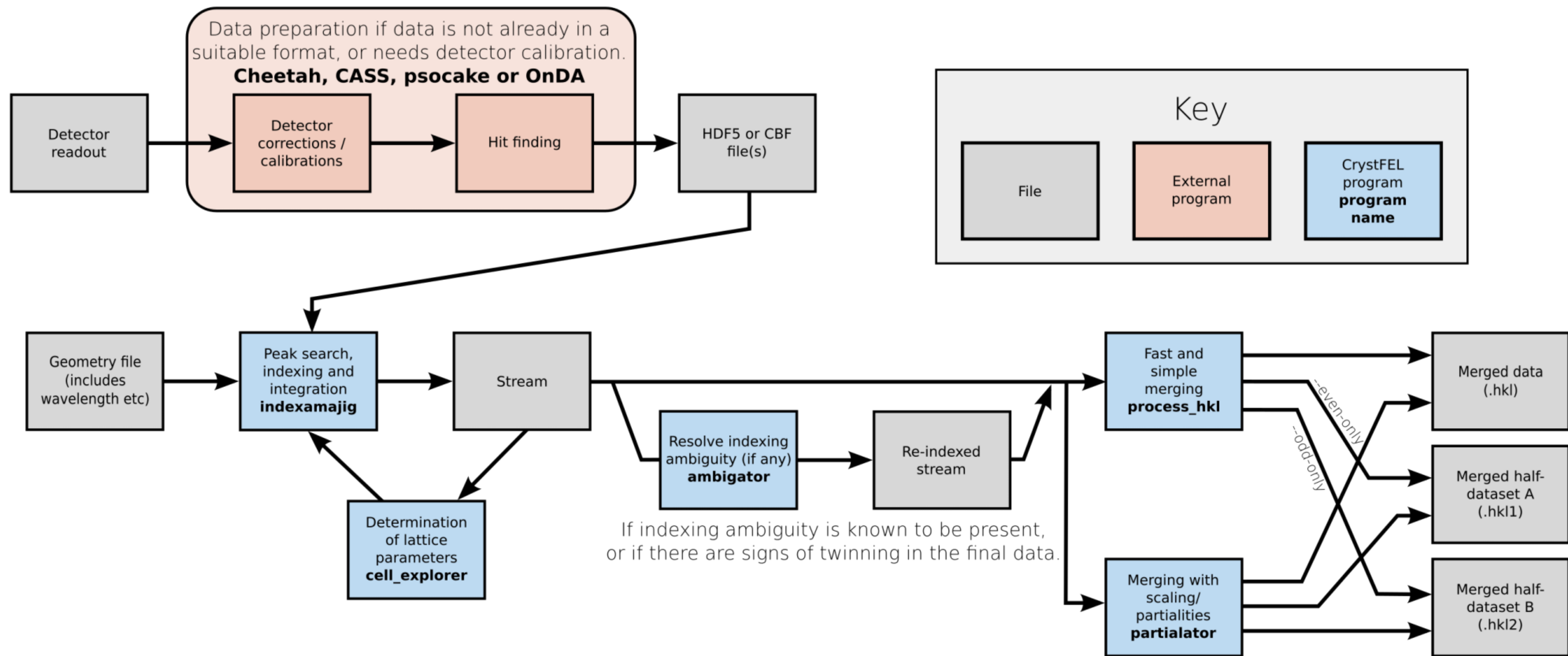
Data processing

Theory of data processing for serial crystallography

Thomas White
Gothenburg CrystFEL workshop
27. January 2020



Data processing pipeline

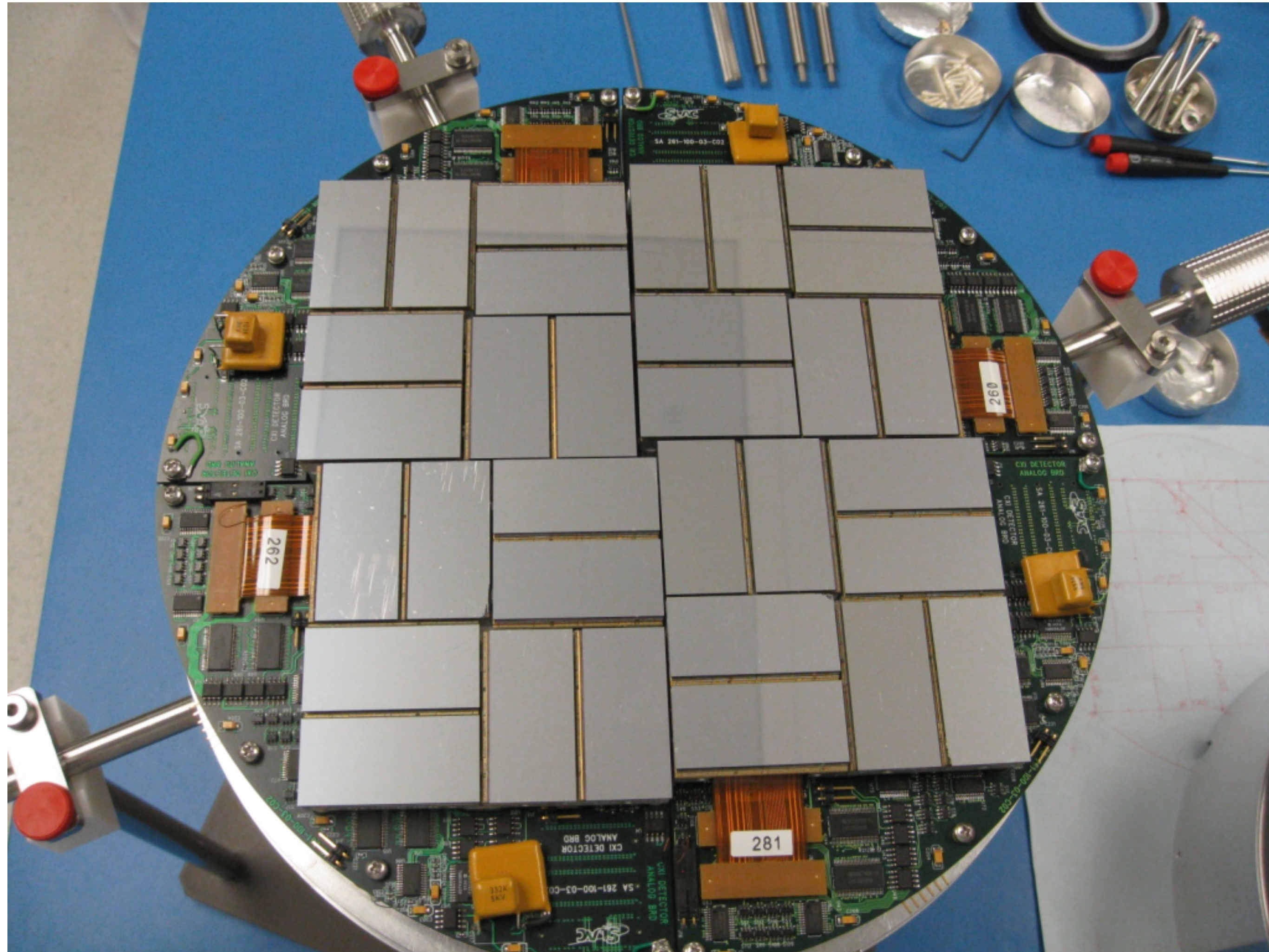


The past and future

The oscillation method (Arndt & Wonacott, 1977) is now generally accepted as the most efficient means for photographic data collection from crystals with unit-cell dimensions greater than about 100 Å. For very large unit cells (average dimensions greater than about 250 Å), the usual method must be modified to realize its full efficiency – in particular, to cope with situations where only one good photograph, instead of a series of contiguous ones, can be taken within the lifetime of a crystal. Essentially, the resulting 'one crystal–one photograph' condition requires a different treatment of partially recorded reflections. This paper describes general aspects of the new procedure and gives a detailed account of its application to data collection from crystalline tomato bushy stunt virus (TBSV: space group $I23$, $a = 383.2$ Å) to 2.9 Å resolution.

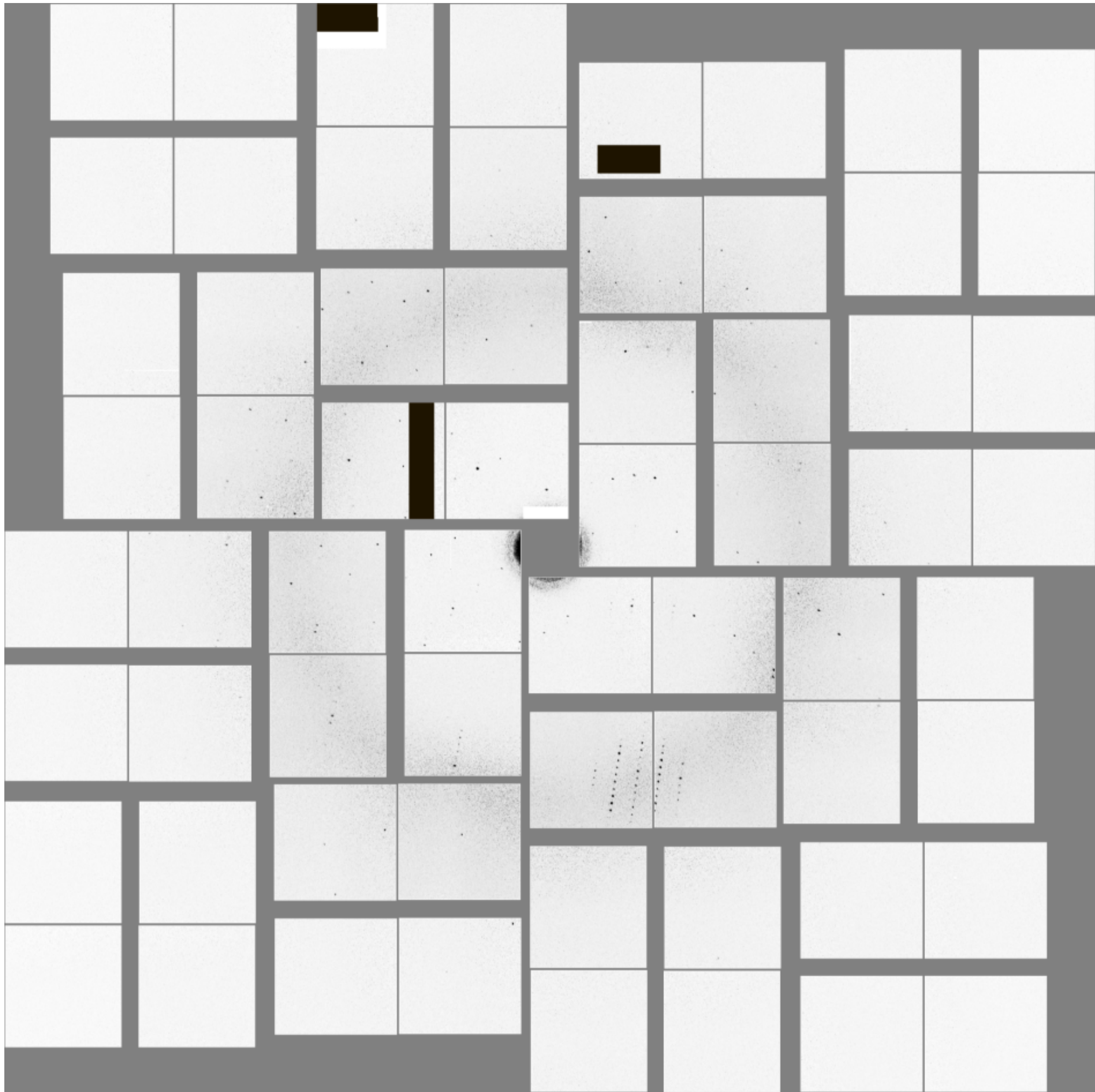
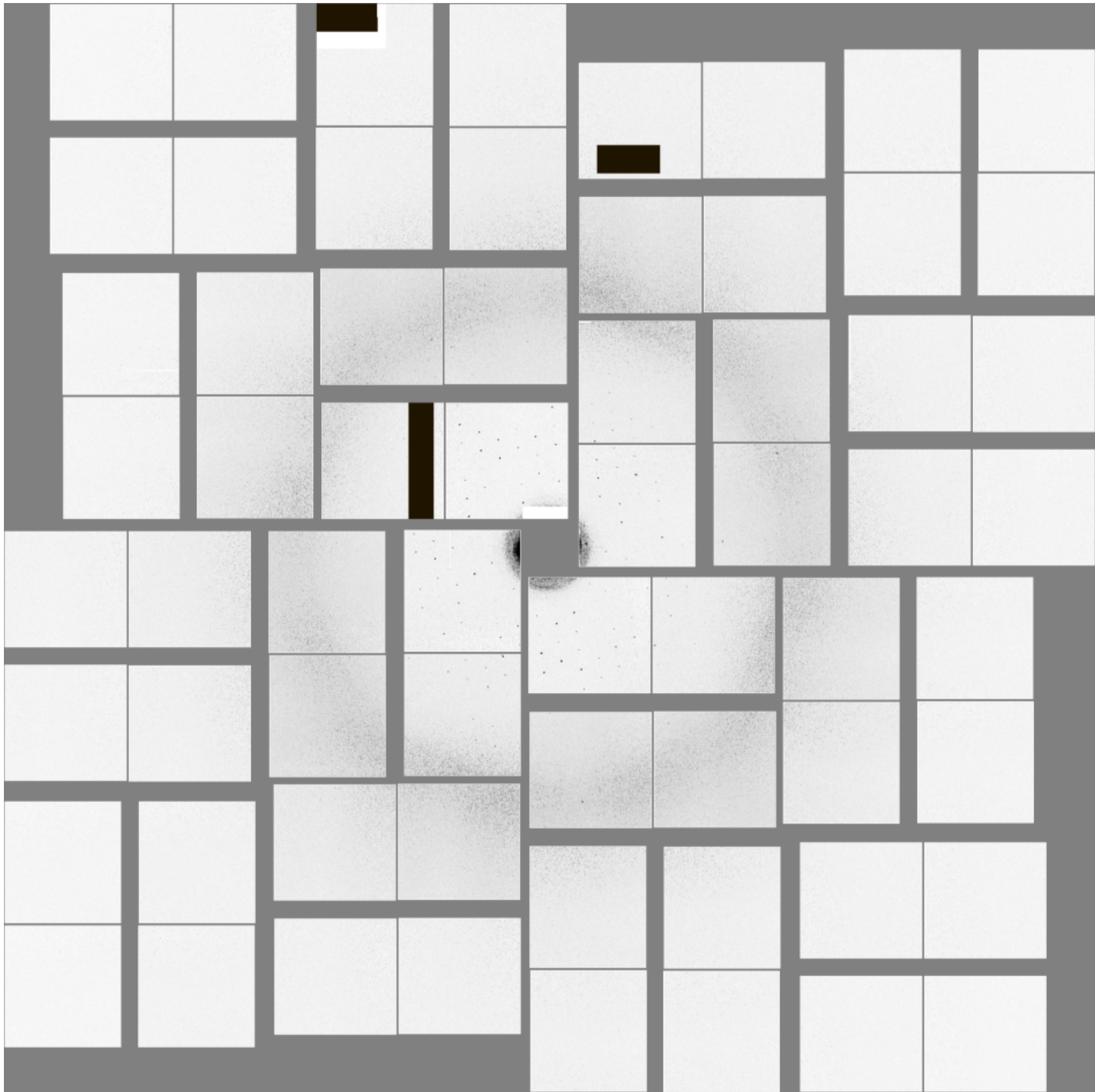
Winkler, Schutt and Harrison, Acta Cryst. A35 (1979), p901-911

Multi-panel detector geometry

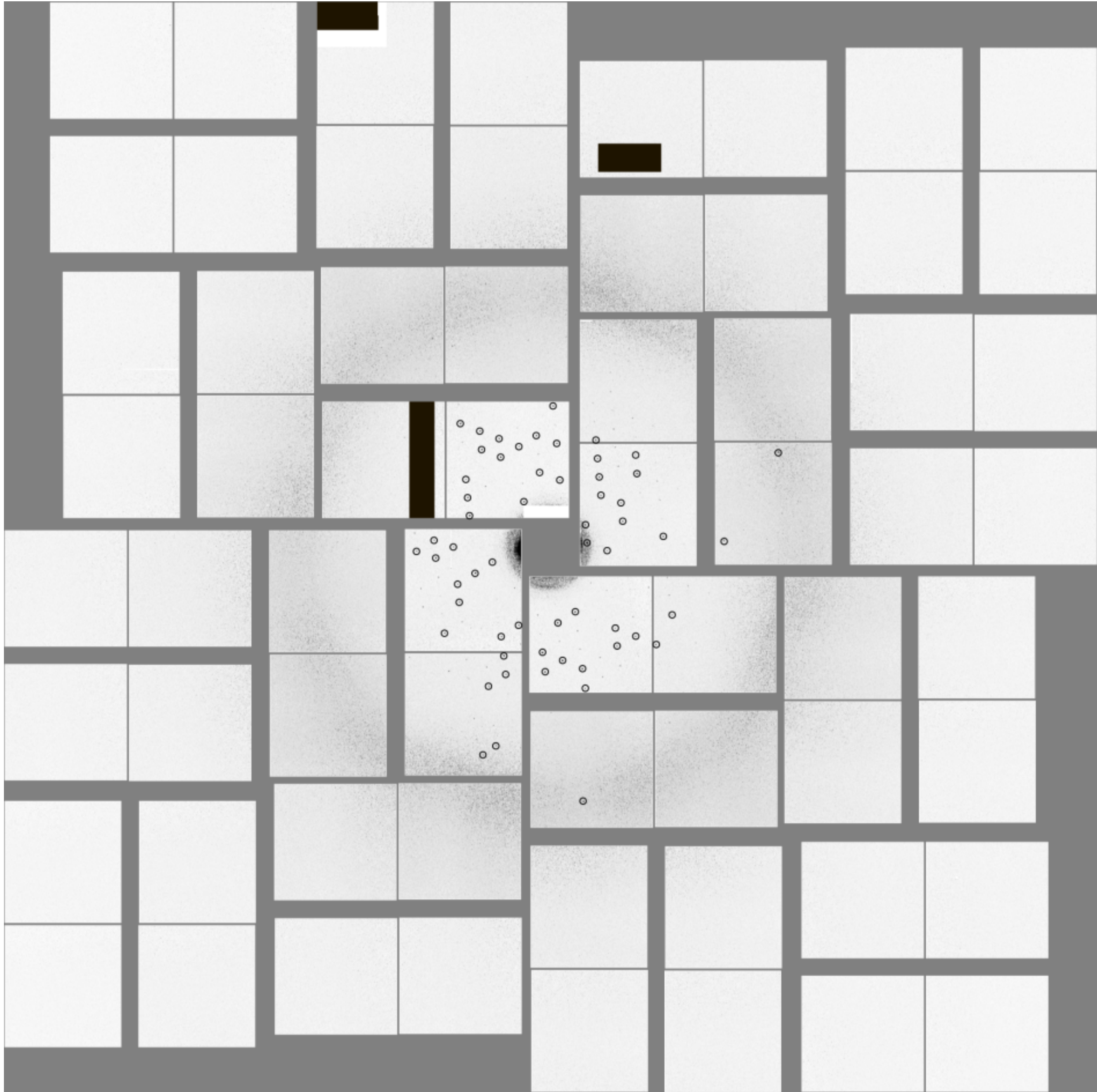


Cornell-SLAC Pixel Array Detector ("CSPAD")
Image: SLAC National Accelerator Laboratory

Diffraction patterns

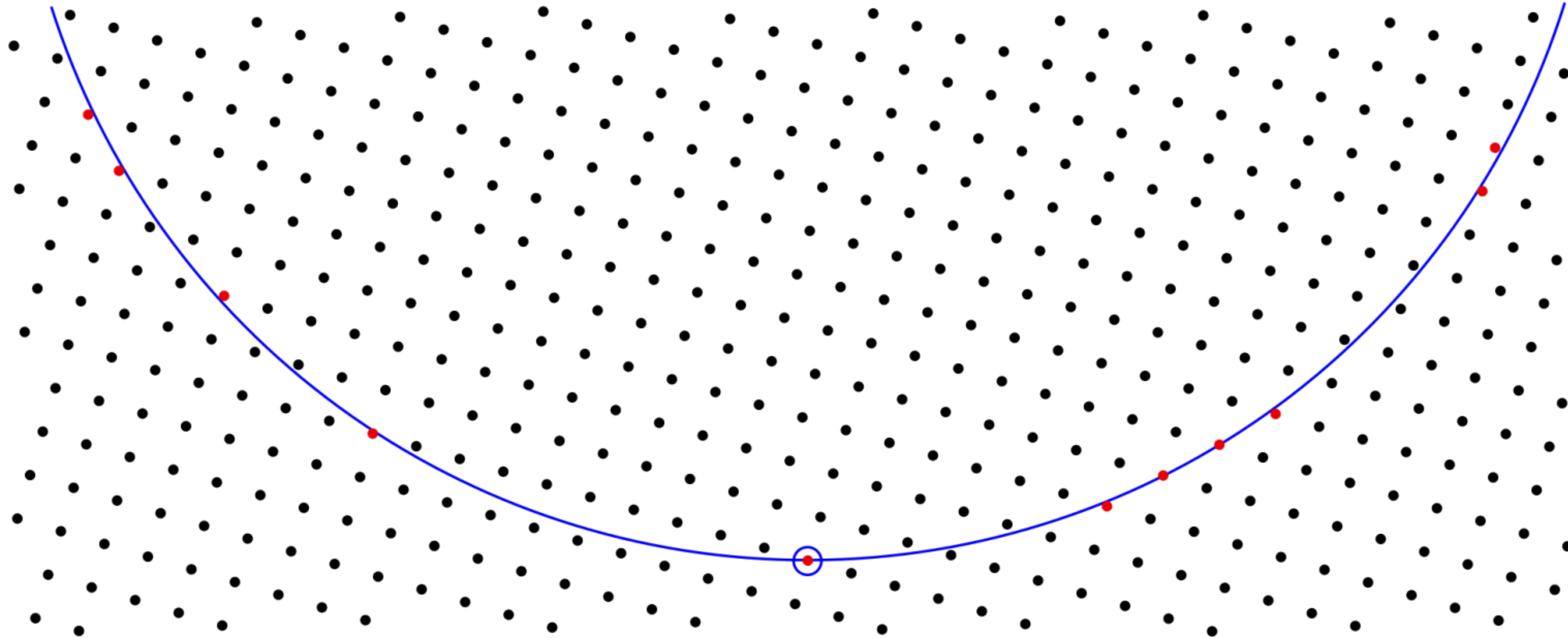


Diffraction patterns

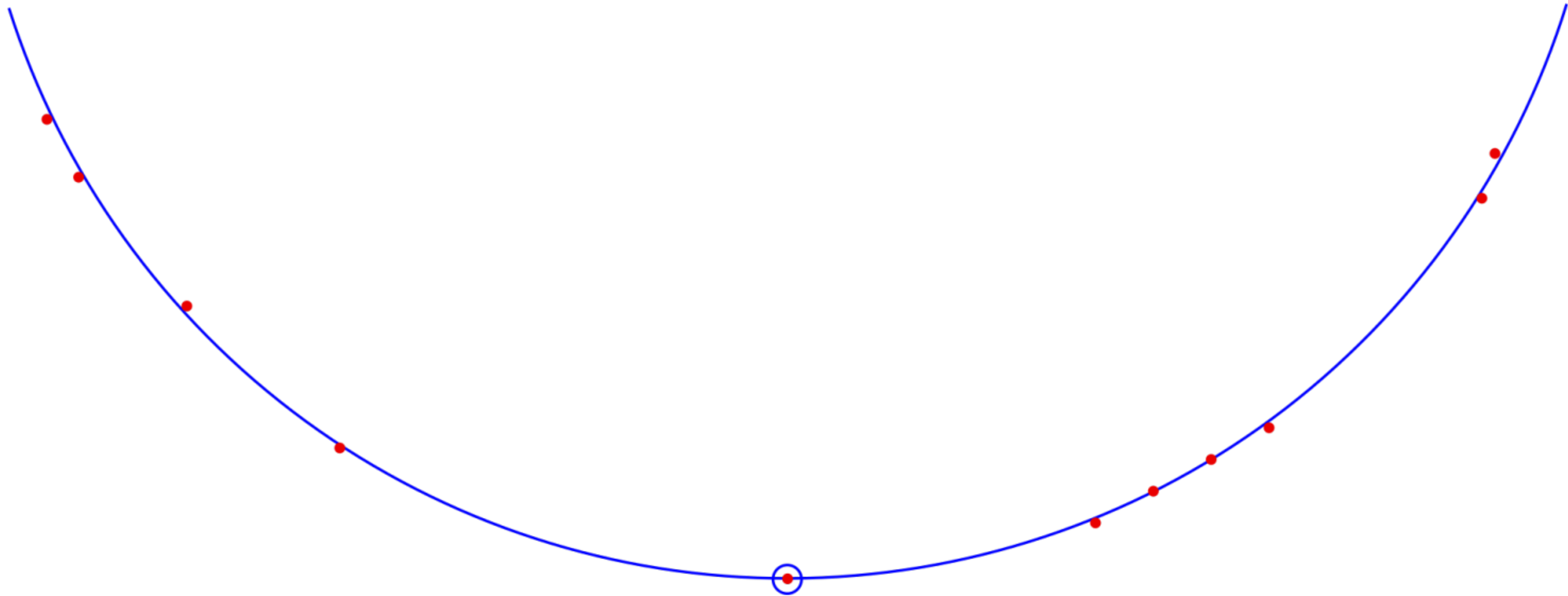


Indexing the diffraction pattern

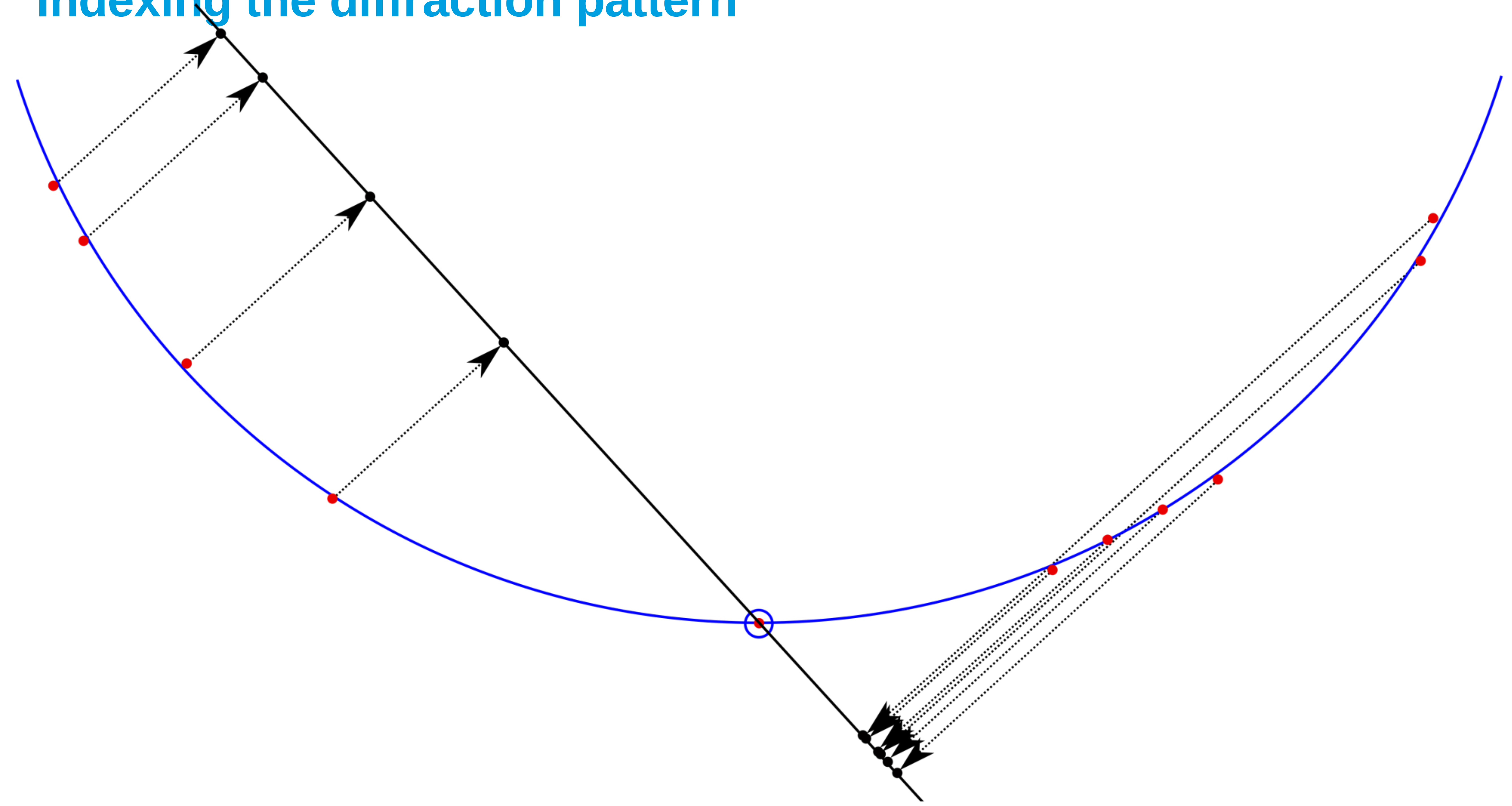
$$2d \sin \theta = \lambda$$



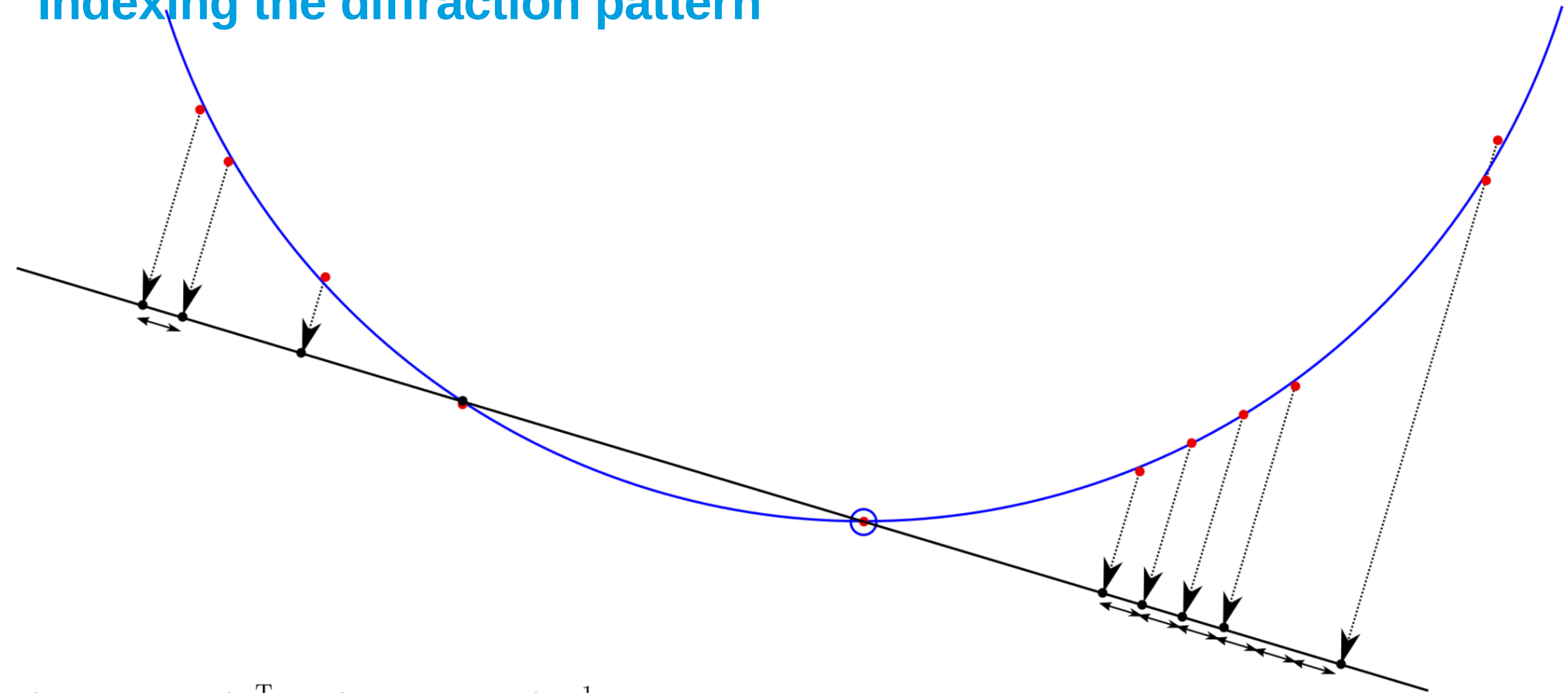
Indexing the diffraction pattern



Indexing the diffraction pattern

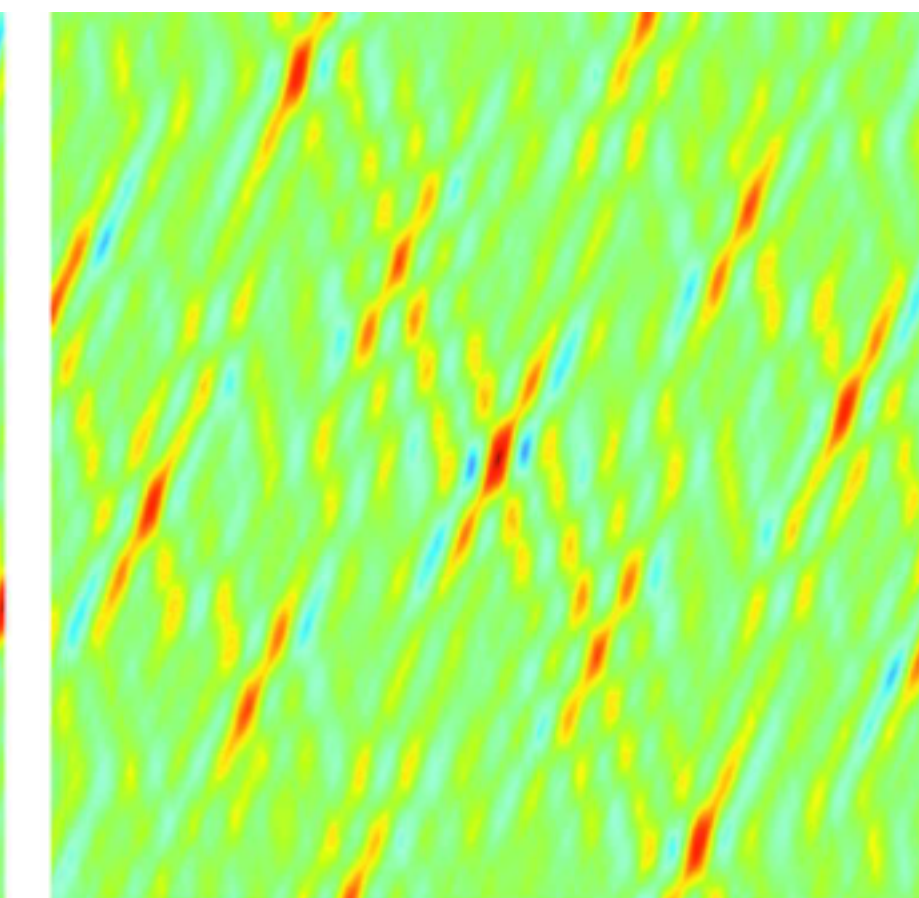
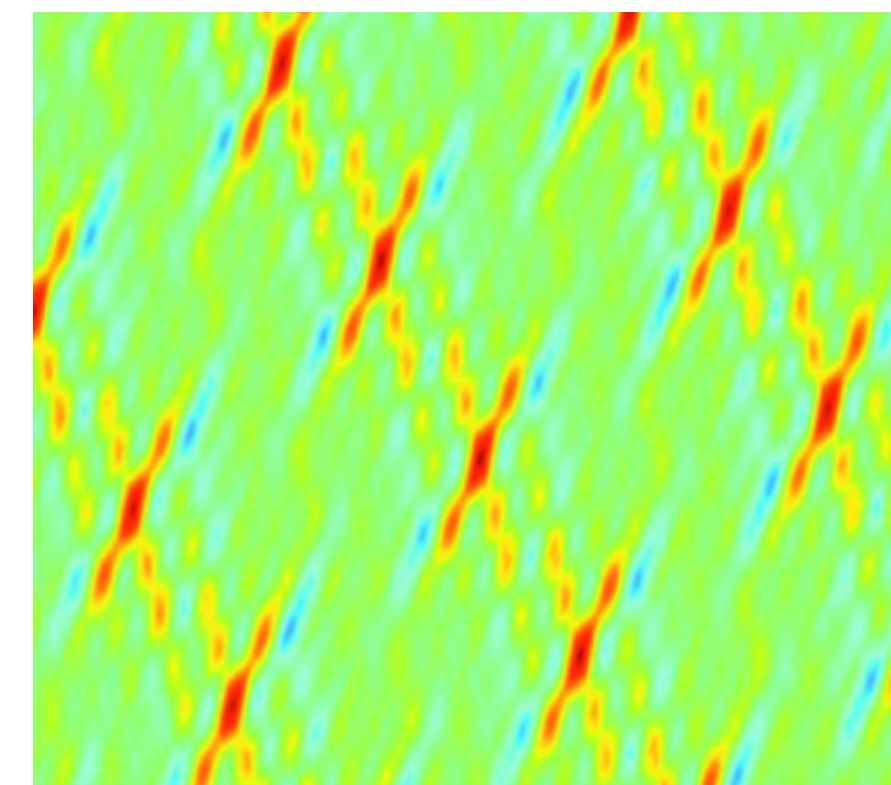
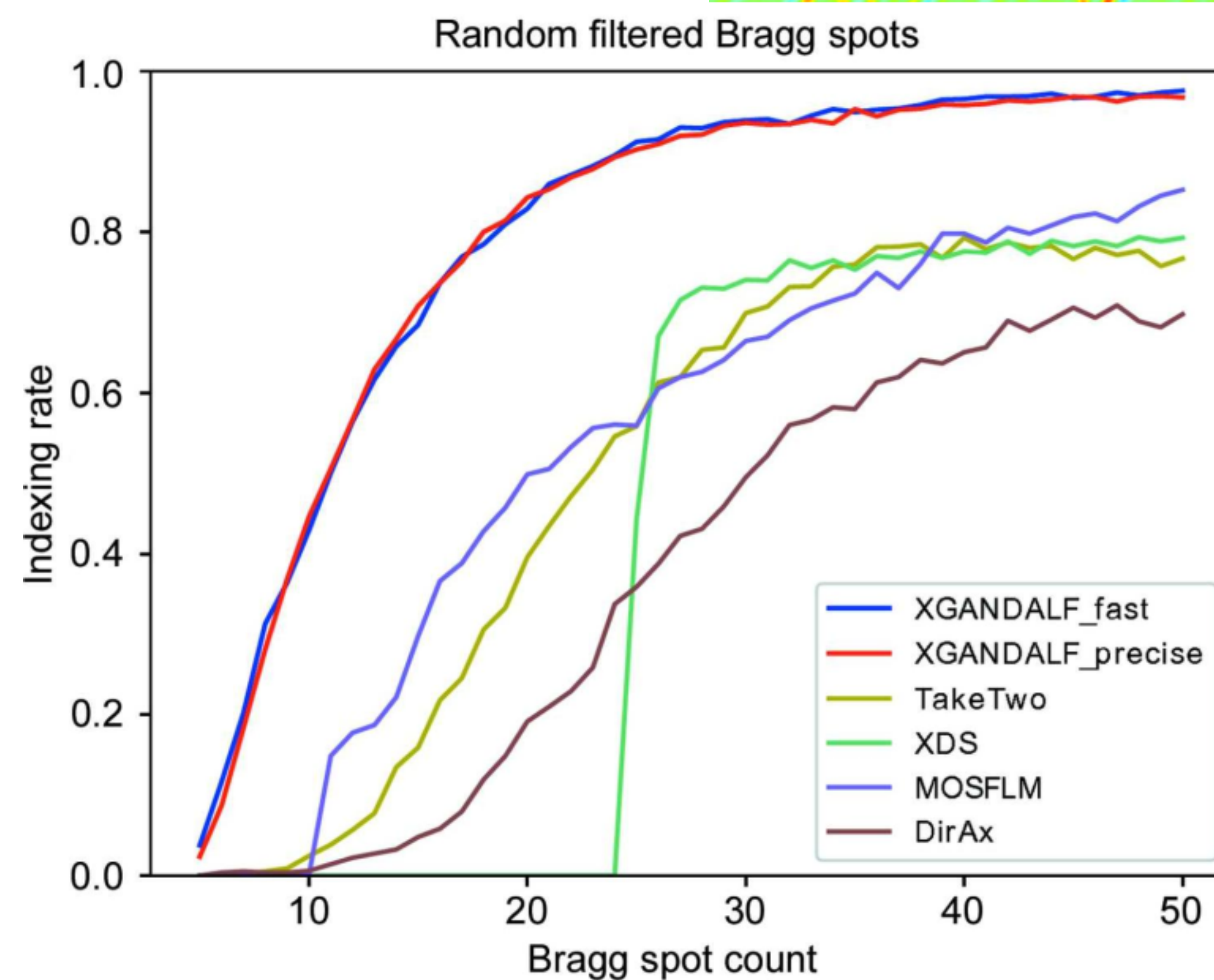
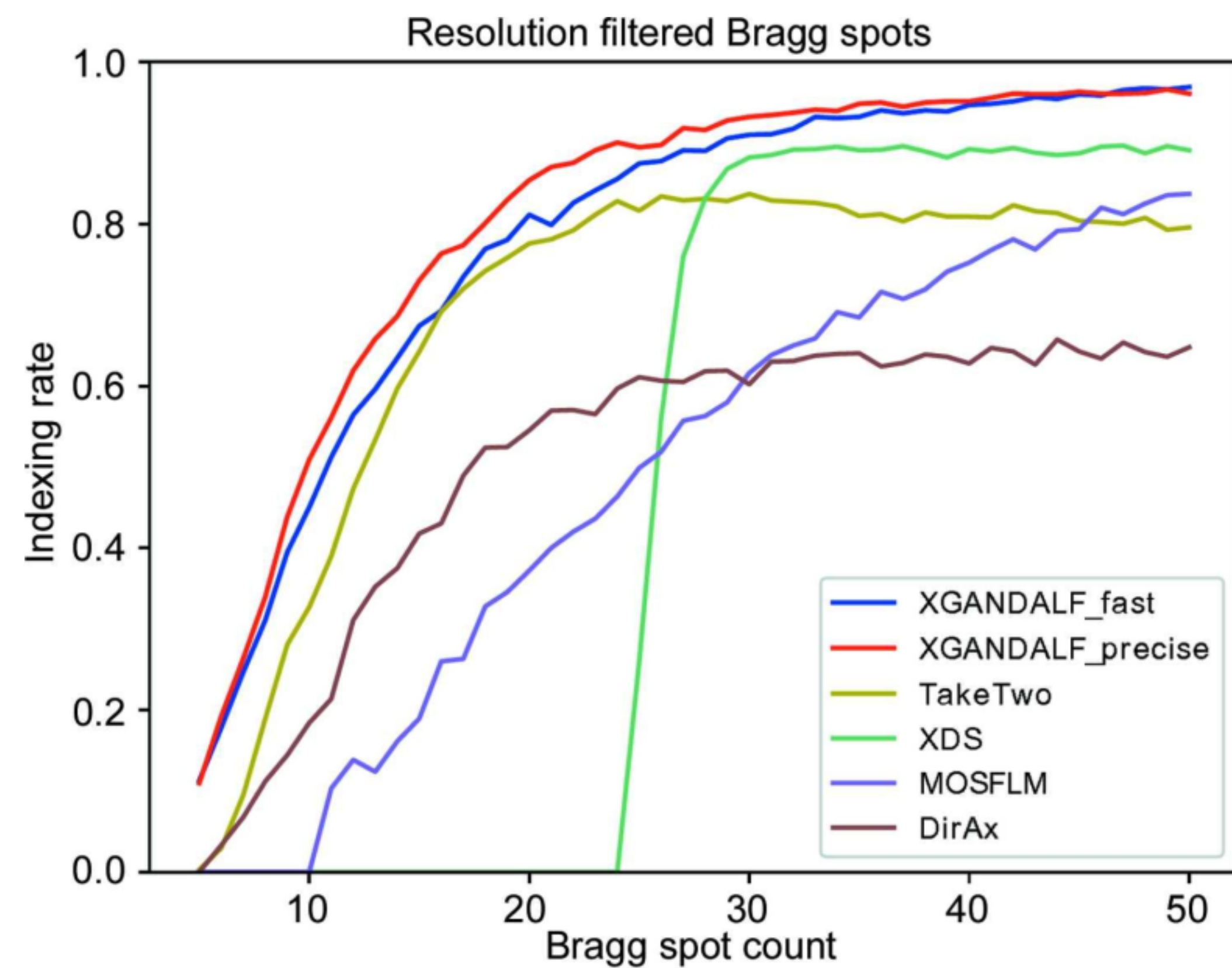


Indexing the diffraction pattern

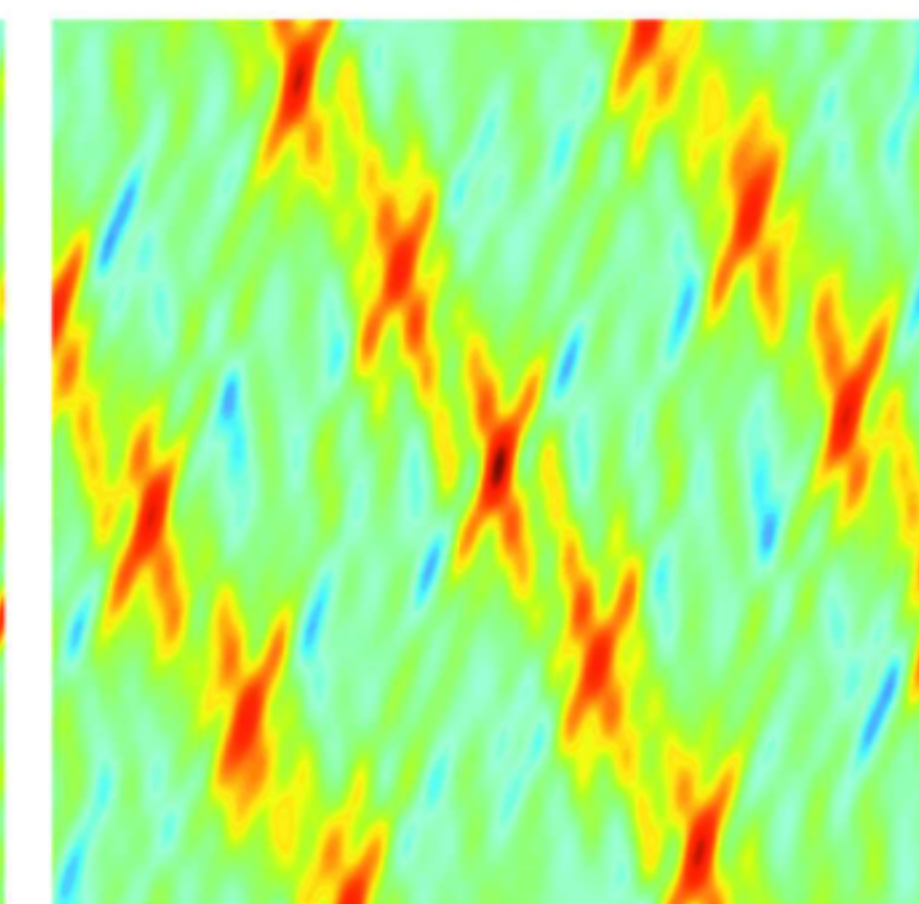


$$\begin{pmatrix} a_x^* & a_y^* & a_z^* \\ b_x^* & b_y^* & b_z^* \\ c_x^* & c_y^* & c_z^* \end{pmatrix}^T = \begin{pmatrix} a_x & a_y & a_z \\ b_x & b_y & b_z \\ c_x & c_y & c_z \end{pmatrix}^{-1}$$

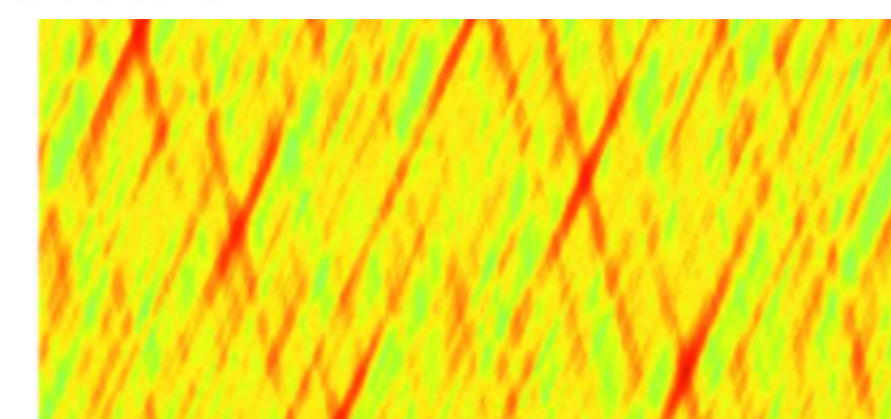
XGANDALF indexer for snapshots



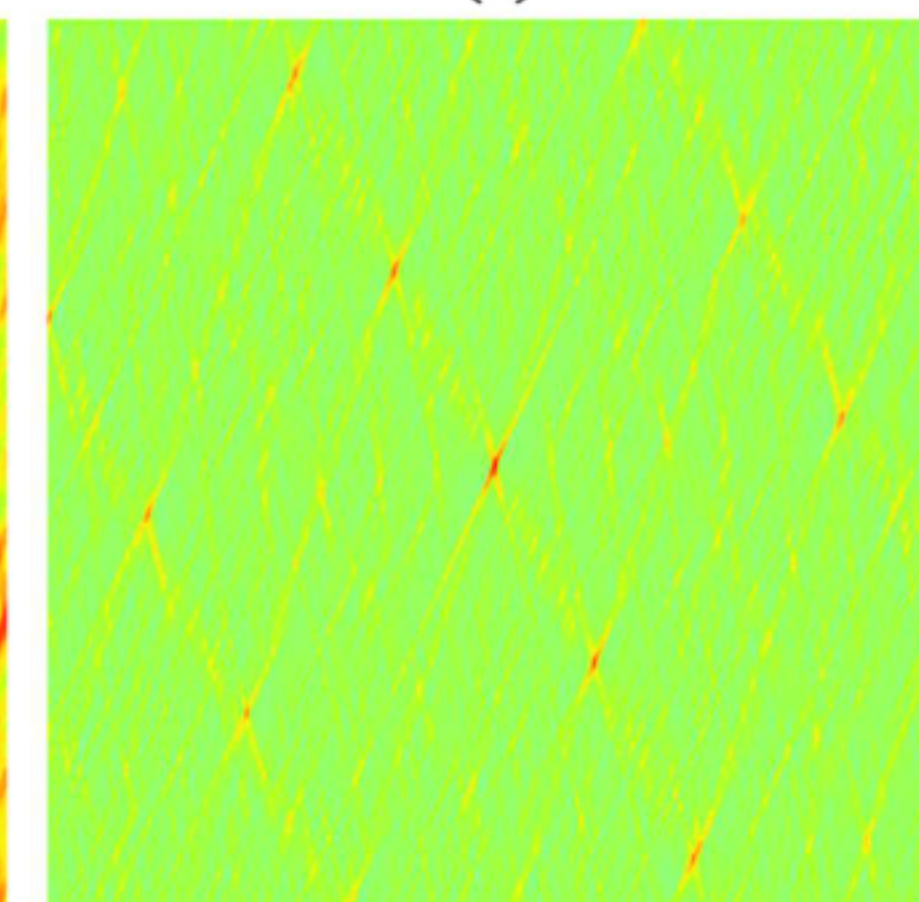
(b)



(d)



(e)

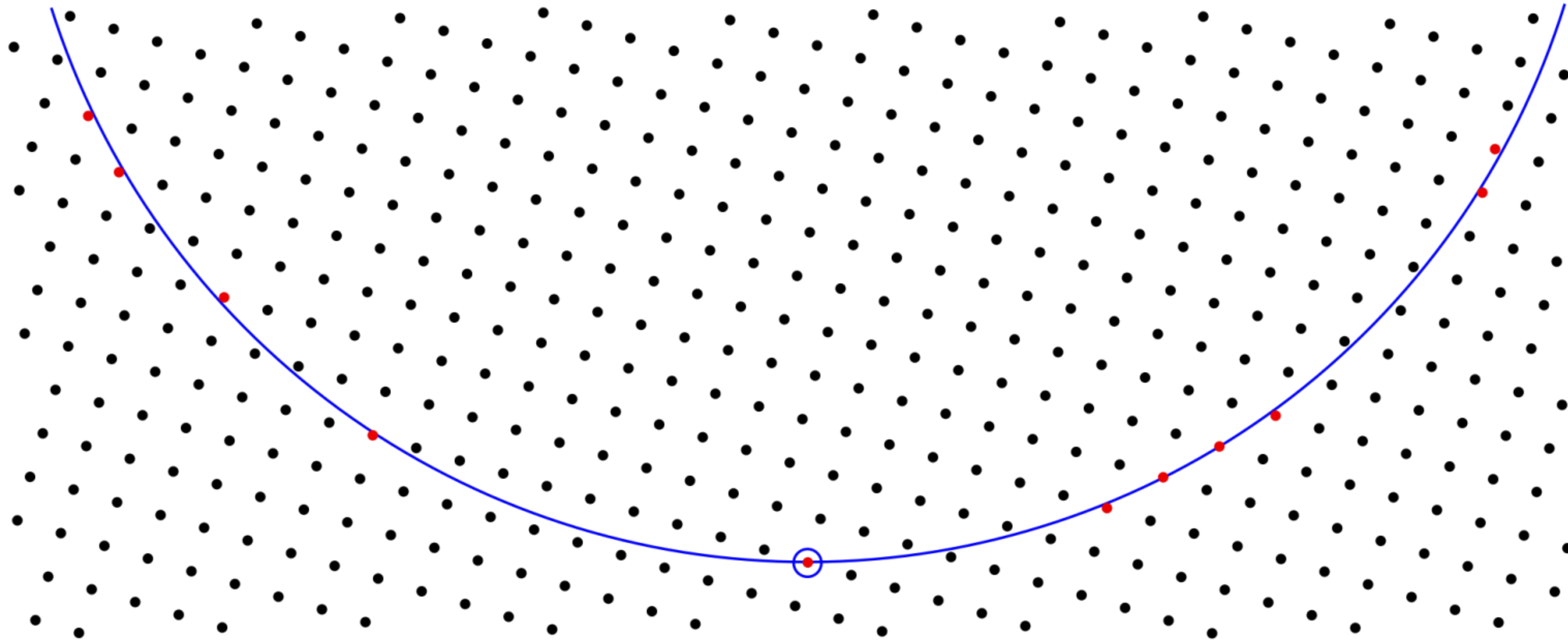


(f)

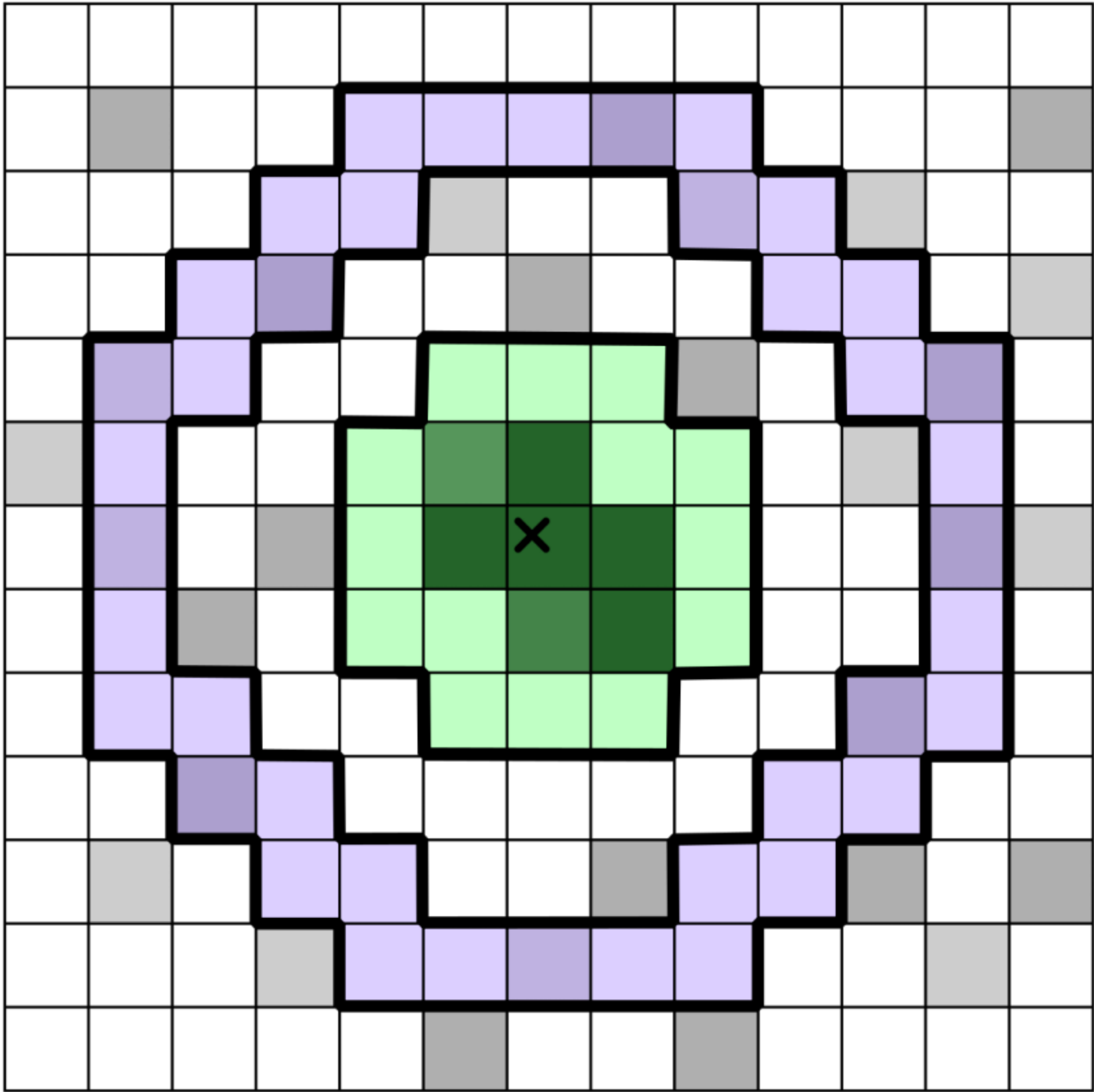
Y. Gevorkov et al, Acta Crystallographica A75 (2019) p694-704

Reflection "prediction"

Important difference from before: all lattice points get projected, not just the ones with peaks

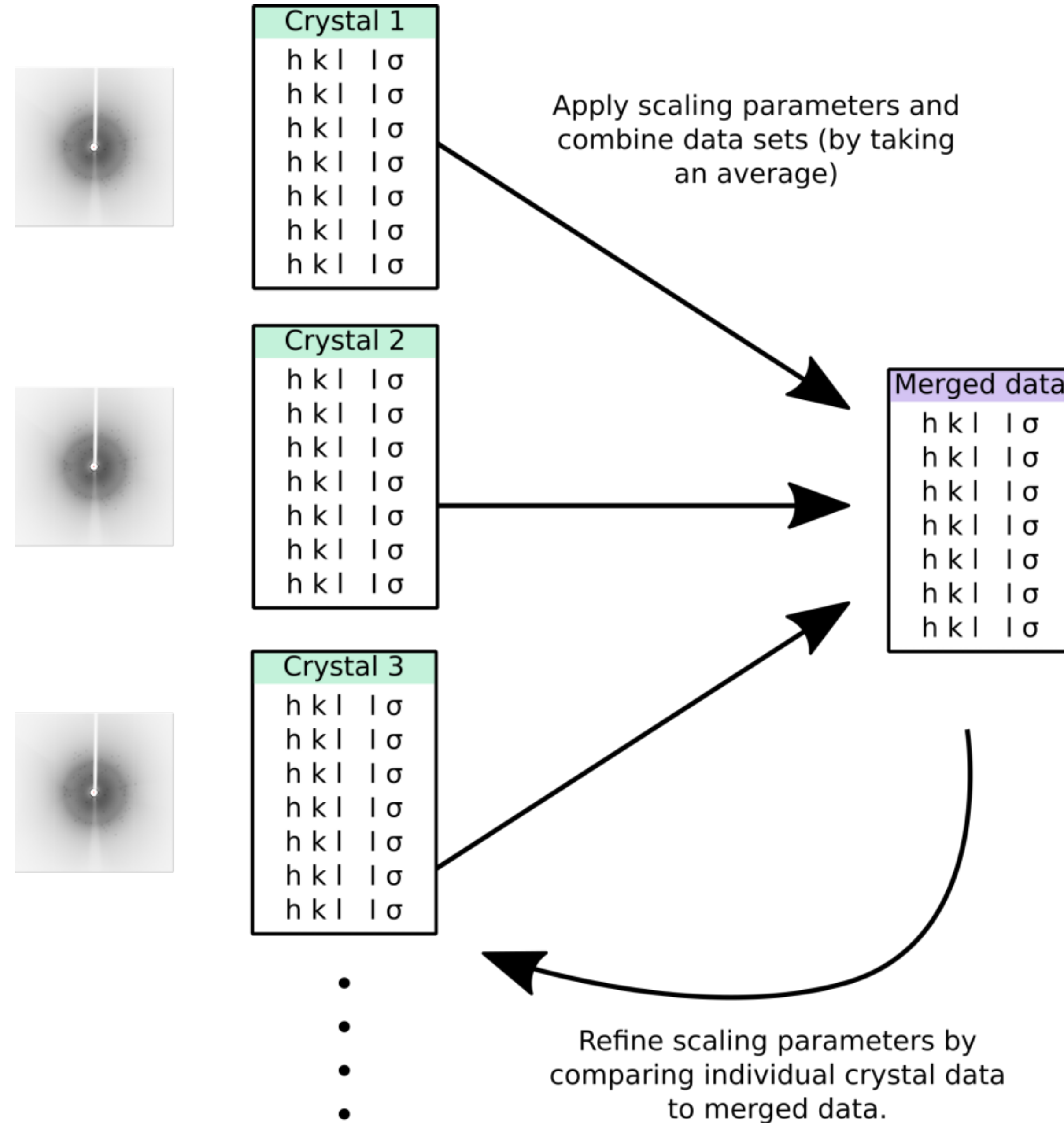


Reflection integration



- ✕ Integration fiducial
- Peak region
- Background region

Merging the measurements



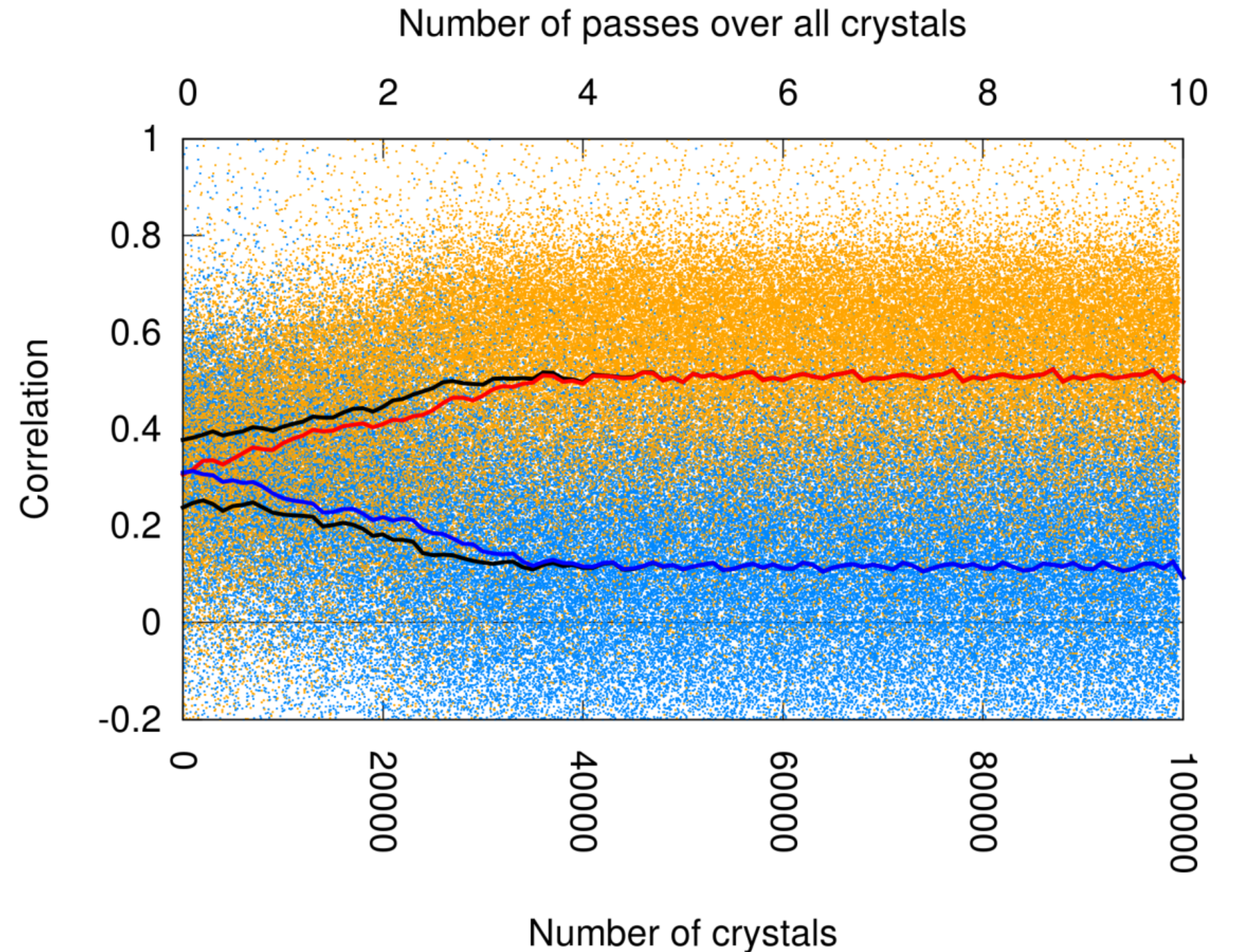
Indexing ambiguities

Clustering algorithm:

Brehm and Diederichs
Acta Cryst. D70 (2014) p101-109

Simplified (1D) version:

White, ... Brehm, ... Diederichs, ...
J. Appl. Cryst. 49 (2016) p680
(see section 4)



Figures of merit

From merged data:

Average $I/\sigma(I)$

Number of measurements per merged reflection

Split pattern into two halves, merge each half separately:

R_{split}

$CC^{1/2}$

CC^*

..... all measure pretty much the same thing

Go back and look at individual patterns again:

$\Delta CC^{1/2}$ ("delta CC half") - see Assmann et al. J. Appl. Cryst. 49 (2016) p1021

What is CrystFEL?

SFX data processing pipeline

- **indexamajig** - Indexing and integration
- **process_hkl** - Monte Carlo merging, simple scaling
- **partialator** - Scaling, partialities, post-refinement
- **ambigator** - Resolve indexing ambiguities

Figures of merit

- **check_hkl** - Completeness, multiplicity, SNR
- **compare_hkl** - Compare reflection data

Simulation tools

- **partial_sim** - Calculate partial reflections
- **pattern_sim** - Fourier simulation

Visualisation tools

- **hdfsee** - Display diffraction patterns
- **render_hkl** - Visualise reflection data
- **cell_explorer** - Examine unit cell distributions

Utilities / other

- **get_hkl** - Twin, example, add noise
- **list_events** - Create event lists
- **geoptimiser** - Refine detector geometry
- **whirligig** - Find rotation series
- **cell_tool** - Unit cell manipulations

Lots of supporting scripts (mostly in Python)

Documentation (manual pages, --help, example files)

Lots more on website (tutorial, demonstration data, citation lists, best practice guidelines, ...)



CrystFEL 0.9.0

- New cell_tool
- Interface to PinkIndexer
- Reflection prediction for electrons and wide bandwidth X-rays
- Arbitrary spectrum API
- ZMQ/MsgPack interface
- New cell comparison algorithm
- Faster deltaCChalf calculation
- Arbitrary polarisation/degree of polarisation (needed for LCLS-II)
- Improvements to multi-lattice indexing
- Handle CBF files natively

Advanced topics

Indexing ambiguities

... how to know there's an ambiguity, and how to fix it

Partiality modelling and post-refinement

Special considerations for TR-SX, MAD and MIR

Recognise when there's an ambiguity

Warning signs:

Point group 3, 4, 6, 312, 321 or 23

(432, 622, 32, 422, 222, 2 and 1 are OK)

.... but you'd have to know the structure already

Twin warnings from Phenix, CCP4 etc, or `check_hkl --ltest` :

```
$ check_hkl test.hkl -p 4ET8.pdb --ltest --ignore-negs
```

```
Using symmetry from reflection file: 4/mmm
```

```
Discarded 0 reflections (out of 3033) with I/sigma(I) < -inf
```

```
Discarded 672 reflections because they had negative intensities.
```

```
2631 pairs
```

```
<|L|> = 0.512 (ideal untwinned 0.500, twinned 0.375)
```

```
<L^2> = 0.344 (ideal untwinned 0.333, twinned 0.200)
```

```
$
```


Twin warnings mean...

1. There's an indexing ambiguity which you need to resolve
 2. The crystals are really (physically) twinned
 3. There's some weird data artifact (e.g. bad detector calibration)
- any combination of the above.

Symmetry classification for serial crystallography

Triclinic lattice

$\bar{1}$	1	$P\bar{1}$	P1
-----------	----------	------------	-----------

Monoclinic lattice

	m		Pm, Pc, Cm, Cc
2	$\underline{2/m}$	P2, P2₁, C2	$\underline{P2/m}, \underline{P2_1/m}, \underline{C2/m}, \underline{P2/c}, \underline{P2_1/c}, \underline{C2/c}$

Orthorhombic lattice

	mm2		Pmm2, Pmc2 ₁ , Pcc2, Pma2, Pca2 ₁ , Pnc2, Pmn2 ₁ , Pba2, Pna2 ₁ , Pnn2, Cmm2, Cmc2 ₁ , Ccc2, Amm2, Aem2, Ama2, Aea2, Fmm2, Fdd2, Imm2, Iba2, Ima2
222	$\underline{mmm}$	P222, P222₁, P2₁2₁2, P2₁2₁2₁, C222₁, C222, F222, I222, I2₁2₁2₁	$\underline{Pmmm}, \underline{Pnnn}, \underline{Pccm}, \underline{Pban}, \underline{Pmma}, \underline{Pnna}, \underline{Pmna}, \underline{Pcca}, \underline{Pbam}, \underline{Pccn}, \underline{Pbcm}, \underline{Pnnm}, \underline{Pmmn}, \underline{Pbcn}, \underline{Pbca}, \underline{Pnma}, \underline{Cmcm}, \underline{Cmce}, \underline{Cmmm}, \underline{Cccm}, \underline{Cmme}, \underline{Ccce}, \underline{Fmmm}, \underline{Fddd}, \underline{Immm}, \underline{Ibam}, \underline{Ibca}, \underline{Imma}$

Tetragonal lattice									
4	$\bar{4}$			4mm	P4, P4 ₁ , P4 ₂ , P4 ₃ , I4, I4 ₁	P $\bar{4}$, I $\bar{4}$			P4mm, P4bm, P4 ₂ cm, P4 ₂ nm, P4cc, P4nc, P4 ₂ mc, P4 ₂ bc, I4mm, I4cm, I4 ₁ md, I4 ₁ cd
	$\bar{4}2m$	$\bar{4}m2$	<u>4/m</u>			P $\bar{4}2m$, P $\bar{4}2c$, P $\bar{4}2_1m$, P $\bar{4}2_1c$, I $\bar{4}2m$, I $\bar{4}2d$	P $\bar{4}m2$, P $\bar{4}c2$, P $\bar{4}b2$, P $\bar{4}n2$, I $\bar{4}m2$, I $\bar{4}c2$	<u>P4/m</u> , <u>P4₂/m</u> , <u>P4/n</u> , <u>P4₂/n</u> , <u>I4/m</u> , <u>I4₁/a</u>	
422	<u>4/mmm</u>				P422, P42 ₁ 2, P4 ₁ 22, P4 ₁ 2 ₁ 2, P4 ₂ 22, P4 ₂ 2 ₁ 2, P4 ₃ 22, P4 ₃ 2 ₁ 2, I422, I4 ₁ 22	P4/mmm, P4/mcc, P4/nbm, P4/nnc, P4/mbm, P4/mnc, P4/nmm, P4/ncc, P4 ₂ /mmc, P4 ₂ /mcm, P4 ₂ /nbc, P4 ₂ /nnm, P4 ₂ /mbc, P4 ₂ /mnm, P4 ₂ /nmc, P4 ₂ /ncm, I4/mmm, I4/mcm, I4 ₁ /amd, I4 ₁ /acd			

Rhombohedral lattice

3	$\bar{3}$	3m	R3 (H3)	$\underline{R\bar{3}} (H\bar{3})$
32	$\bar{3}m$		R32 (H32)	$\underline{R\bar{3}m} (H\bar{3}m)$

Hexagonal lattice																	
3			$\bar{3}$						P3, P3 ₁ , P3 ₂			$P\bar{3}$					
6	312	321							P6, P6 ₁ , P6 ₅ , P6 ₂ , P6 ₄ , P6 ₃	P312, P3 ₁ 12, P3 ₂ 12	P321, P3 ₁ 21, P3 ₂ 21						
			$\underline{3m1}$ $\bar{6}m2$ $\bar{6}2m$ $\underline{31m}$									$\underline{P3m1}, \underline{P3c1}$ $P\bar{6}$ $P31m, P31c$					
			$\underline{6/m}$ 6mm									$\underline{P6/m}, \underline{P6_3/m}$ P6mm, P6cc, P6 ₃ cm, P6 ₃ mc					
622			$\underline{6/mmm}$						P622, P6 ₁ 22, P6 ₅ 22, P6 ₂ 22, P6 ₄ 22, P6 ₃ 22			$\underline{P6/mmm}, \underline{P6/mcc}, \underline{P6_3/mcm}, \underline{P6_3/mmc}$					

Cubic lattice

23	$\bar{4}3m$	$\underline{m\bar{3}}$	P23, F23, I23, P2₁3, I2₁3	$P\bar{4}3m, F\bar{4}3m, I\bar{4}3m, P\bar{4}3n, F43c, I\bar{4}3d$	$\underline{Pm\bar{3}}, \underline{Pn\bar{3}}, \underline{Fm\bar{3}}, \underline{Fd\bar{3}}, \underline{Im\bar{3}}, \underline{Pa\bar{3}}, \underline{Ia\bar{3}}$
432	$\underline{m\bar{3}m}$		P432, P4₂32, F432, F4₁32, I432, P4₃32, P4₁32, I4₁32	$\underline{Pm\bar{3}m}, \underline{Pn\bar{3}n}, \underline{Pm\bar{3}n}, \underline{Pn\bar{3}m}, \underline{Fm\bar{3}m}, \underline{Fm\bar{3}c}, \underline{Fd\bar{3}m}, \underline{Fd\bar{3}c}, \underline{Im\bar{3}m}, \underline{Ia\bar{3}d}$	

Spotting "accidental" ambiguities

```
$ cell_tool 4ET8.pdb --find-ambi -y 422
```

```
Input unit cell: 4ET8.pdb
```

```
-----> The input unit cell:
```

```
tetragonal P, unique axis c, right handed.
```

```
a    b    c        alpha  beta  gamma
```

```
79.00 79.00 38.00 A   90.00 90.00 90.00 deg
```

```
Looking for ambiguities up to 3x each lattice length.
```

```
This will take about 30 seconds. Please wait...
```

```
[....]
```

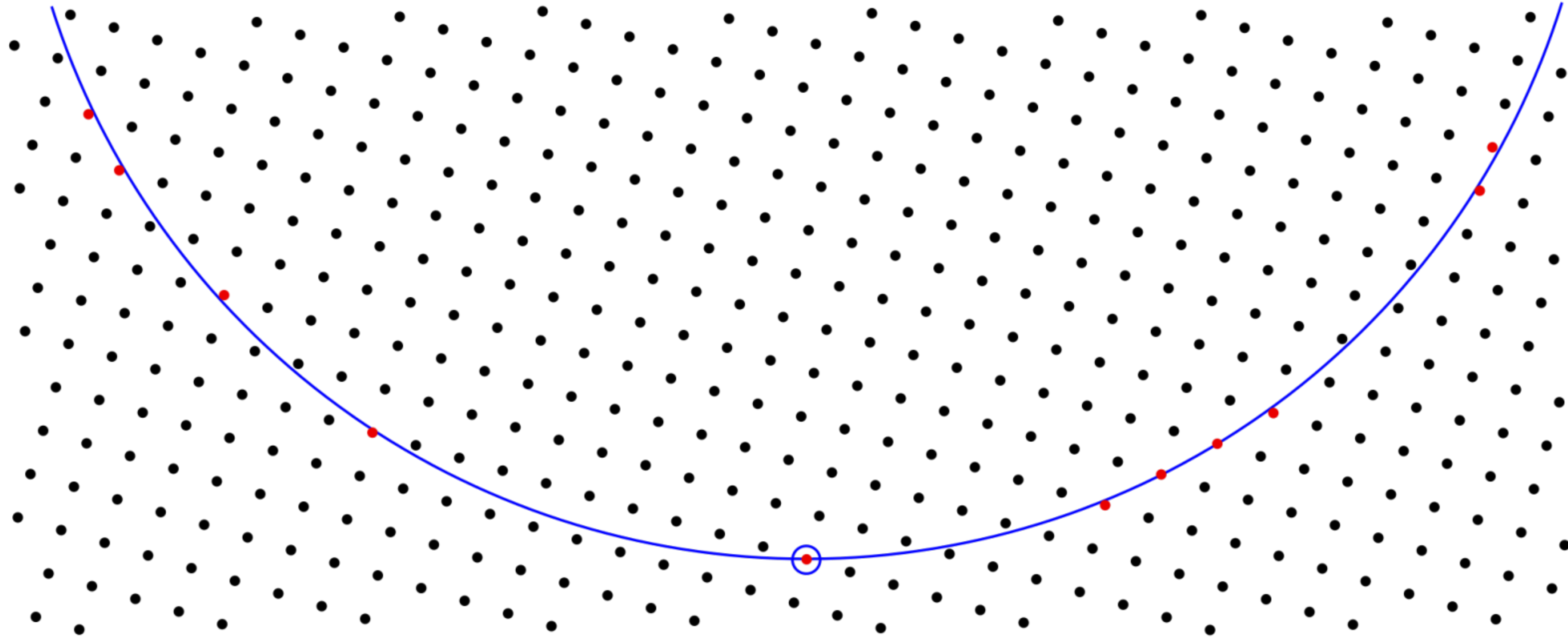
```
Observed symmetry operations:
```

```
Observed : hkl    -h,-k,l  -h,k,-l  -k,-h,-l  k,-h,l   -k,h,l   k,h,-l   h,-k,-l
```

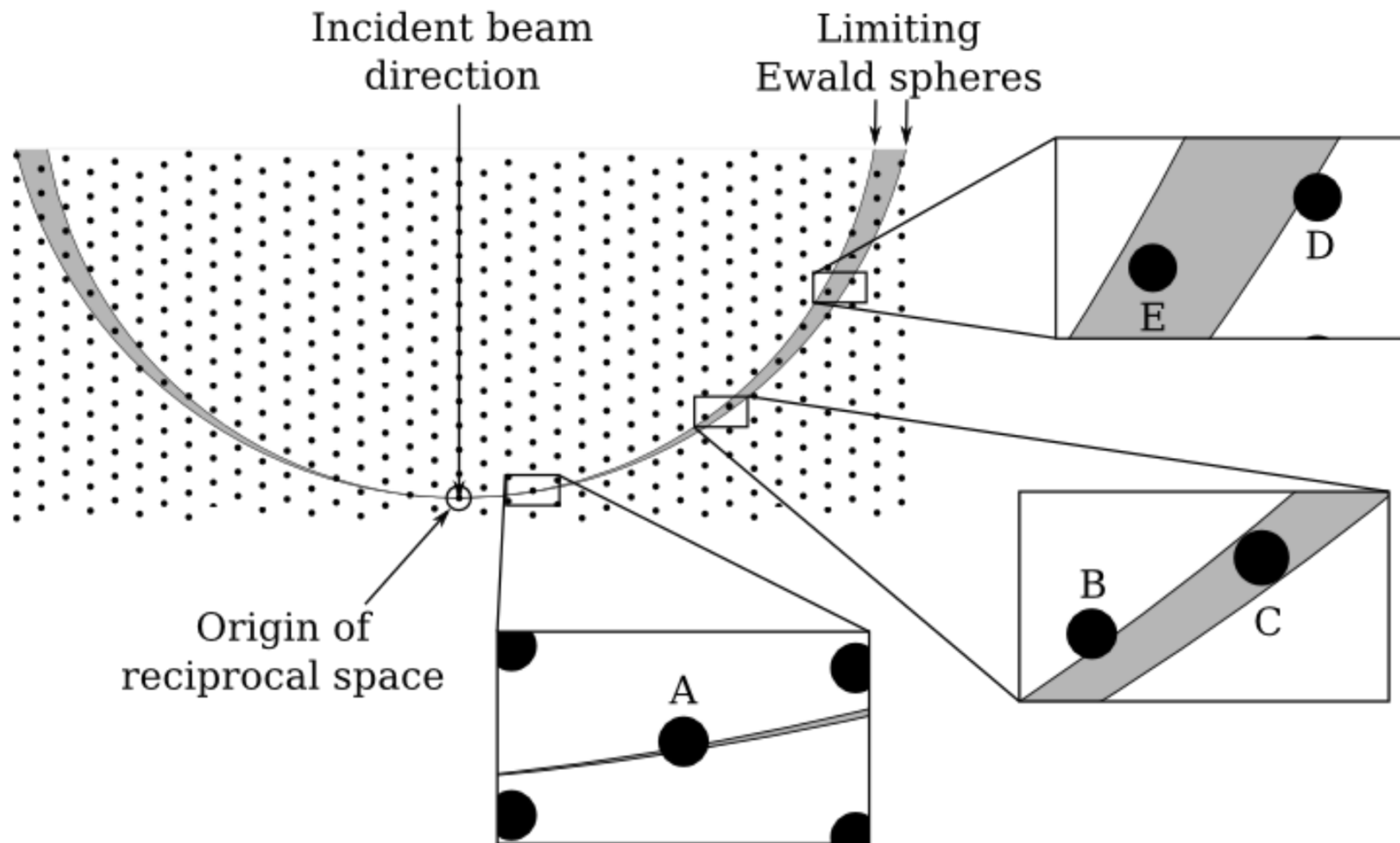
```
Ambiguity operations:
```

```
Observed -> 422 :
```

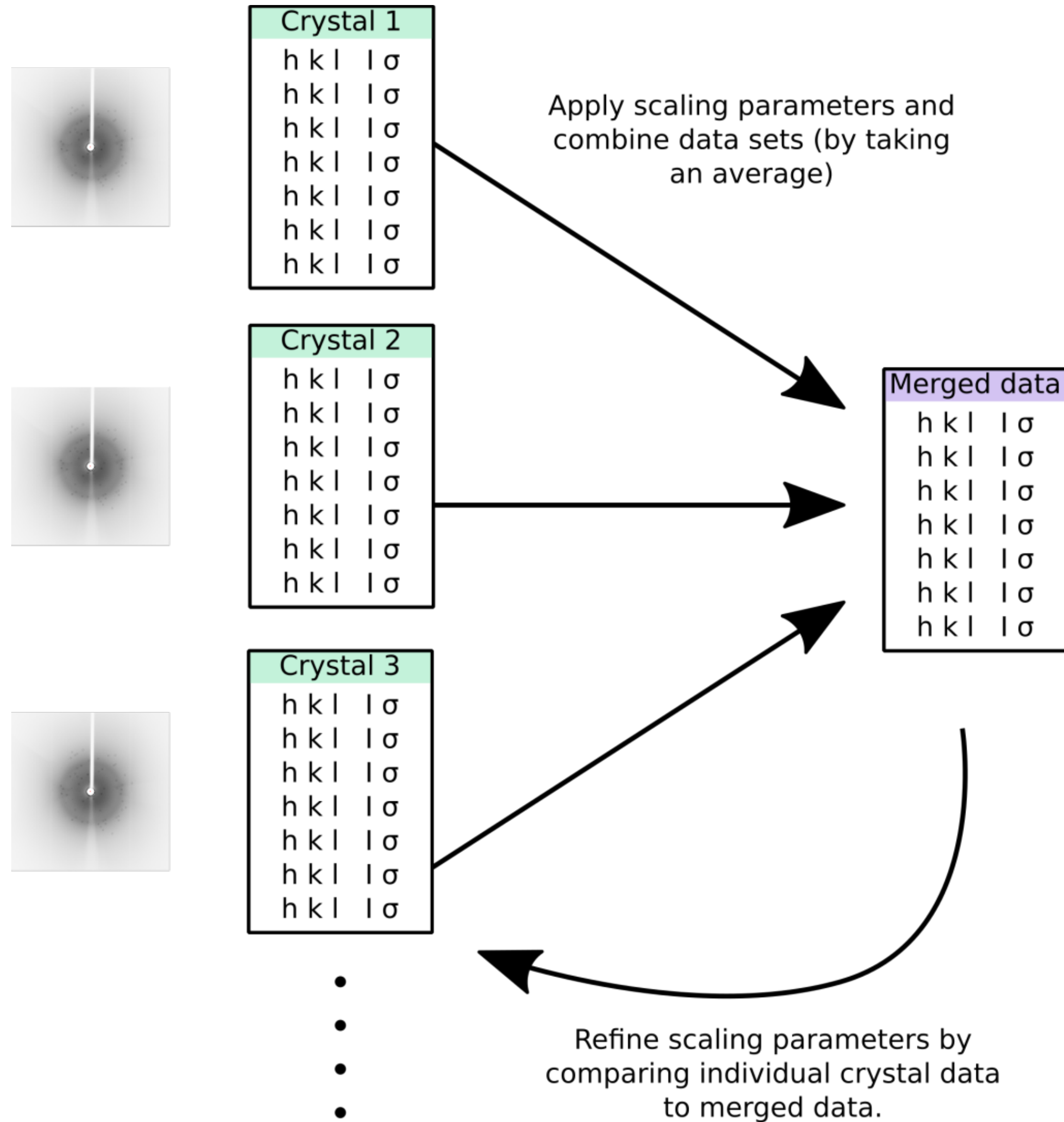
Reflection partiality



Reflection partiality



Post-refinement



Partiality models available in CrystFEL (v0.9.0)

`partialator --model=unity`

Set all partialities to 1 (no modelling)

`partialator --model=xsphere`

Numerical integration across arbitrary spectrum

See Ginn et al, Acta Cryst. D71, p1400 (2015)

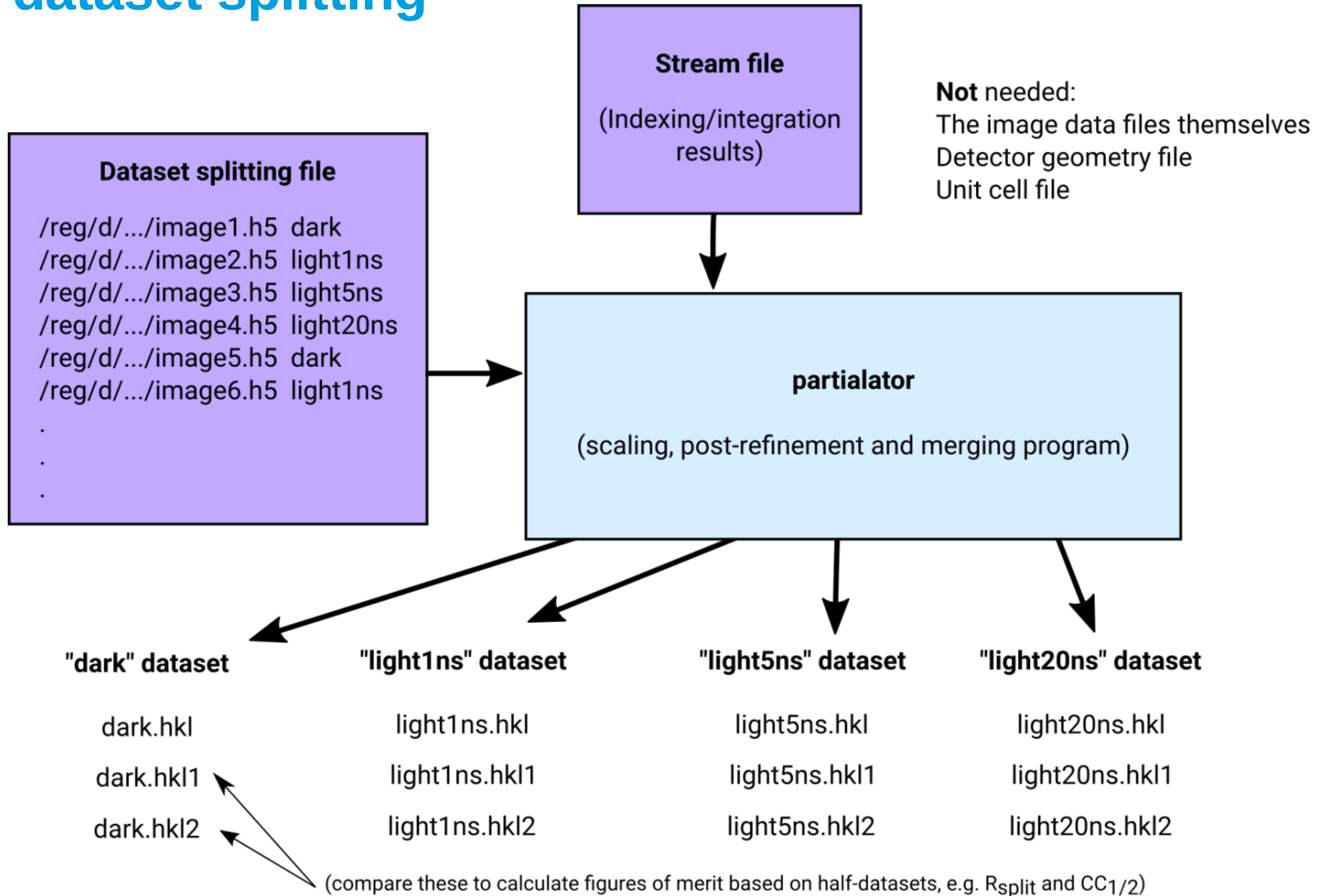
`partialator --model=offset`

Thin Ewald sphere, like Kabsch, Acta Cryst. D70, p2204 (2014)

`partialator --model=ggpm`

Analytically-defined model based on Gaussian overlap integrals
(Needs X-ray spectrum to be an analytical function)

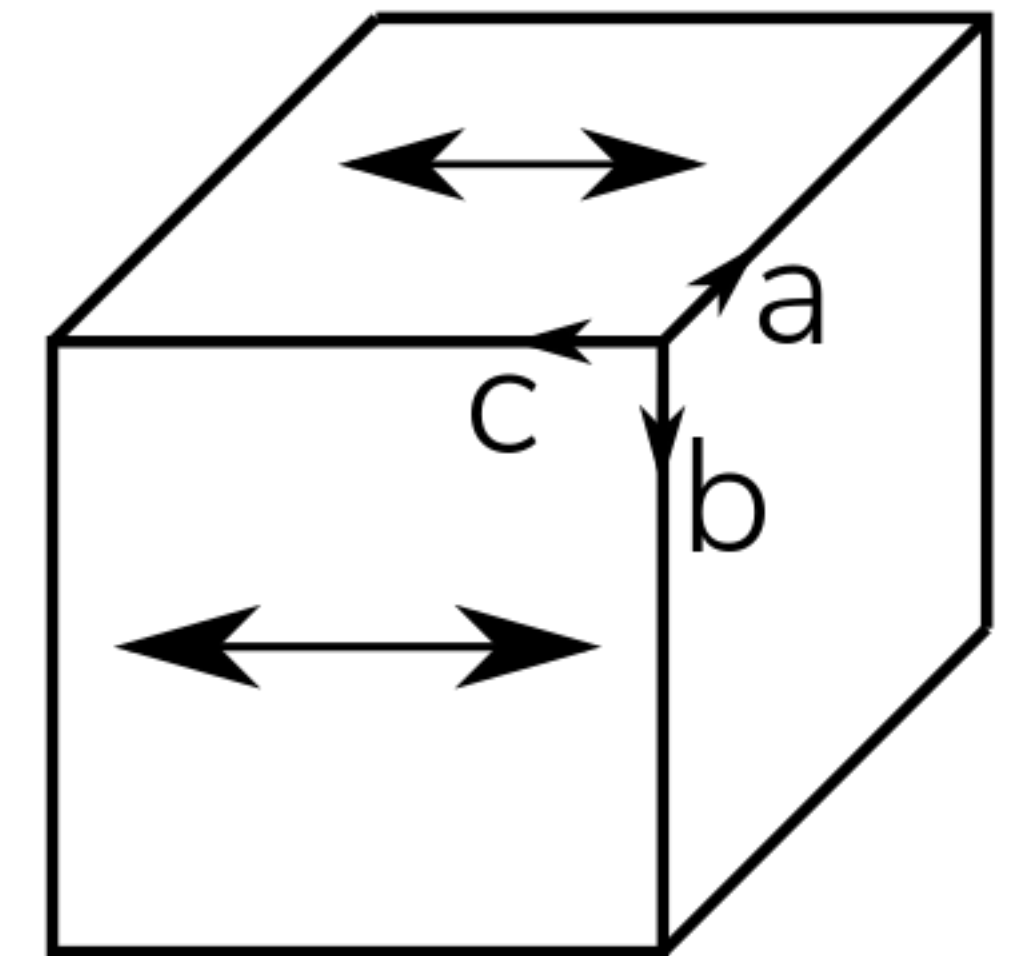
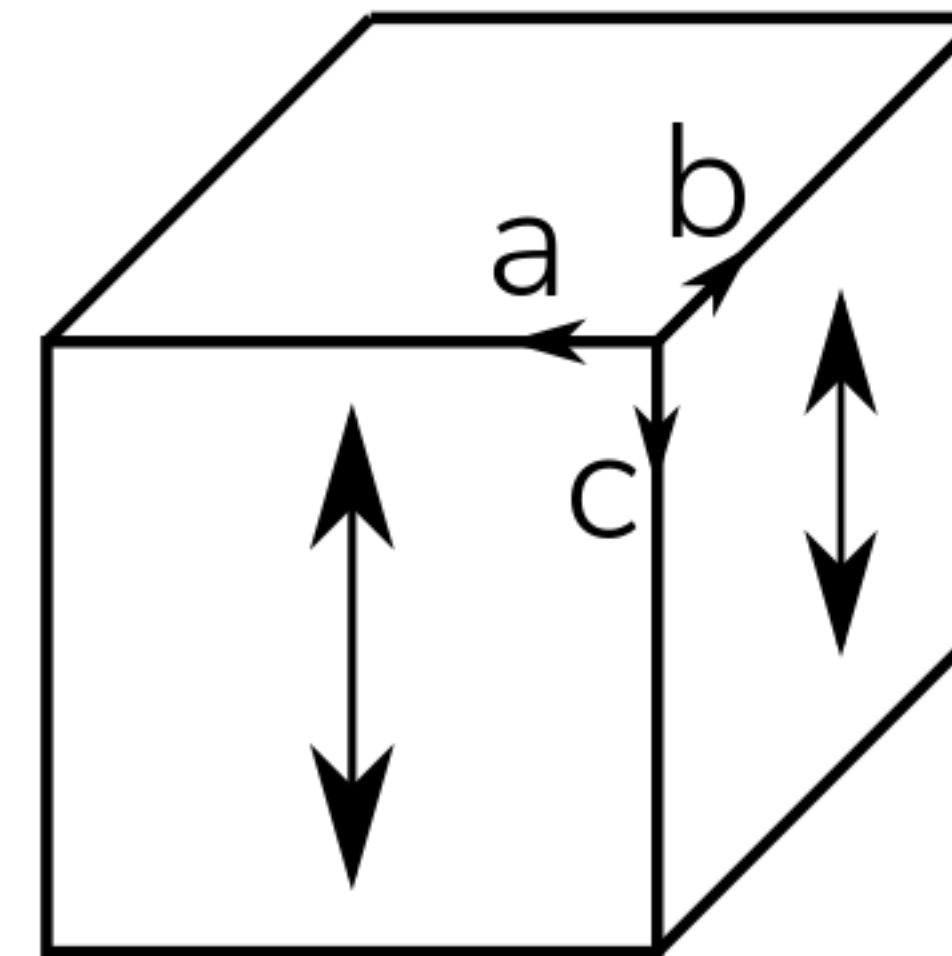
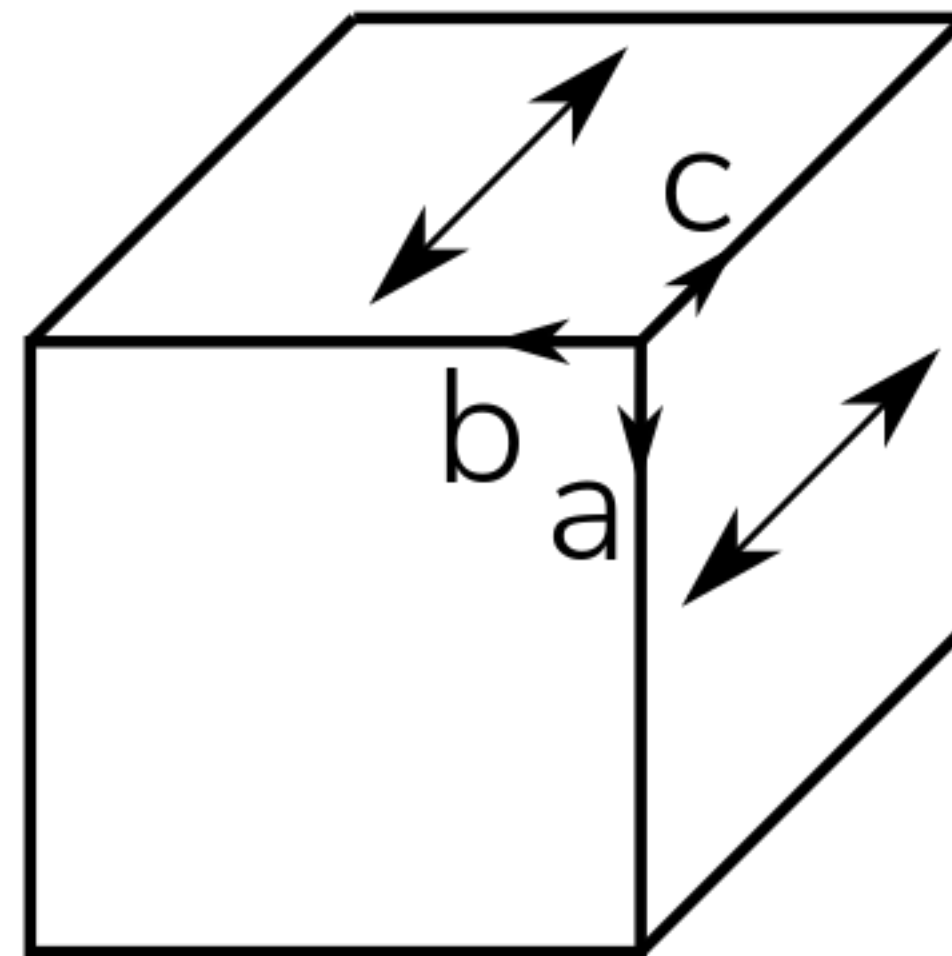
Custom dataset splitting



Three-way ambiguity in human melatonin receptor

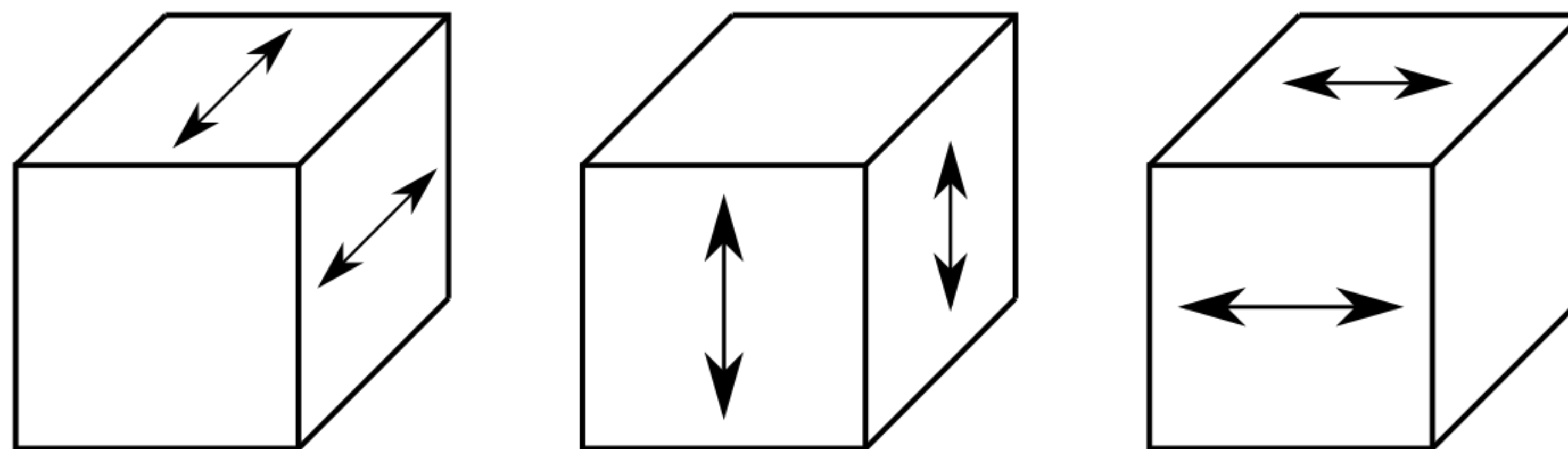
Tetragonal P
 $a = 122.3 \text{ \AA}$
 $b = 122.3 \text{ \AA}$
 $c = 122.8 \text{ \AA}$
 $\alpha = 90^\circ$
 $\beta = 90^\circ$
 $\gamma = 90^\circ$

Indexing ambiguity: $hkl \rightarrow klh \rightarrow lkh \rightarrow hkl \rightarrow \dots$
One indexing ambiguity, three possibilities



B. Stauch, L. C. Johansson, J. D. McCorvy, N. Patel, G. Won Han, X.-P. Huang, C. Gati, A. Batyuk, S. T. Slocum, A. Ishchenko, W. Brehm, T. A. White, N. Michaelian, C. Madsen, L. Zhu, T. D. Grant, J. M. Grandner, A. Shiriaeva, R. H. J. Olsen, A. R. Tribo, S. Yous, R. C. Stevens, U. Weierstall, V. Katritch, B. L. Roth, W. Liu, V. Cherezov.
Nature 569 (2019) p284

Resolving a three-way cyclic ambiguity



$\frac{1}{3}$

$\frac{1}{3}$

$\frac{1}{3}$

First run of ambigator:

$\frac{2}{3}$

$\frac{1}{6}$

$\frac{1}{6}$

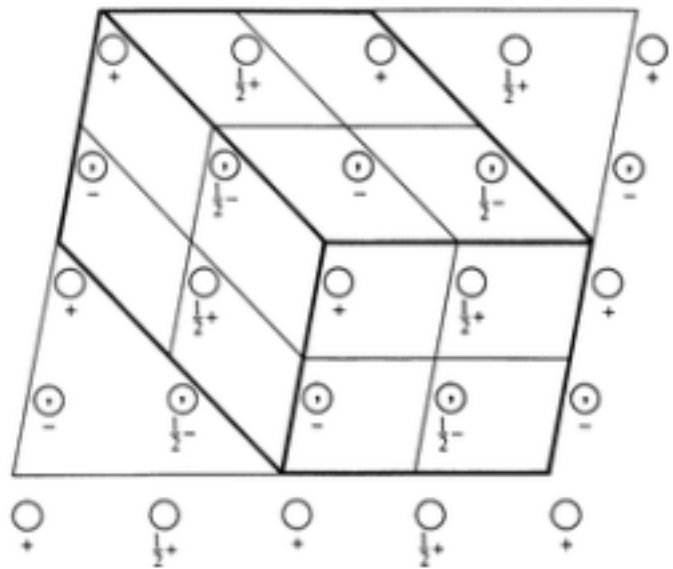
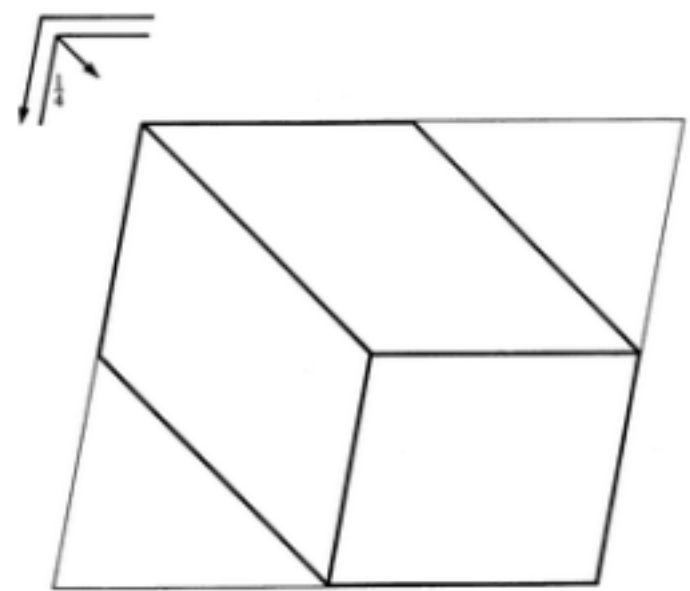
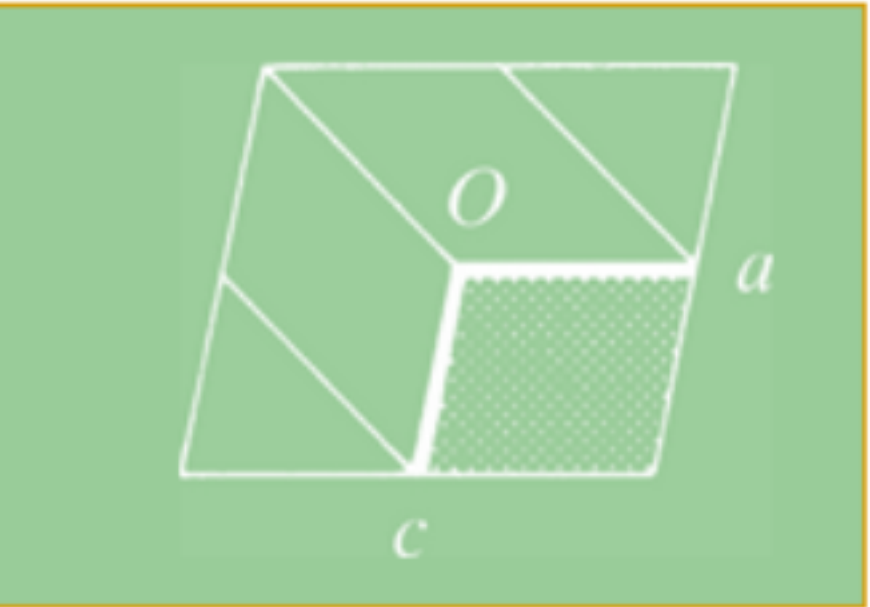
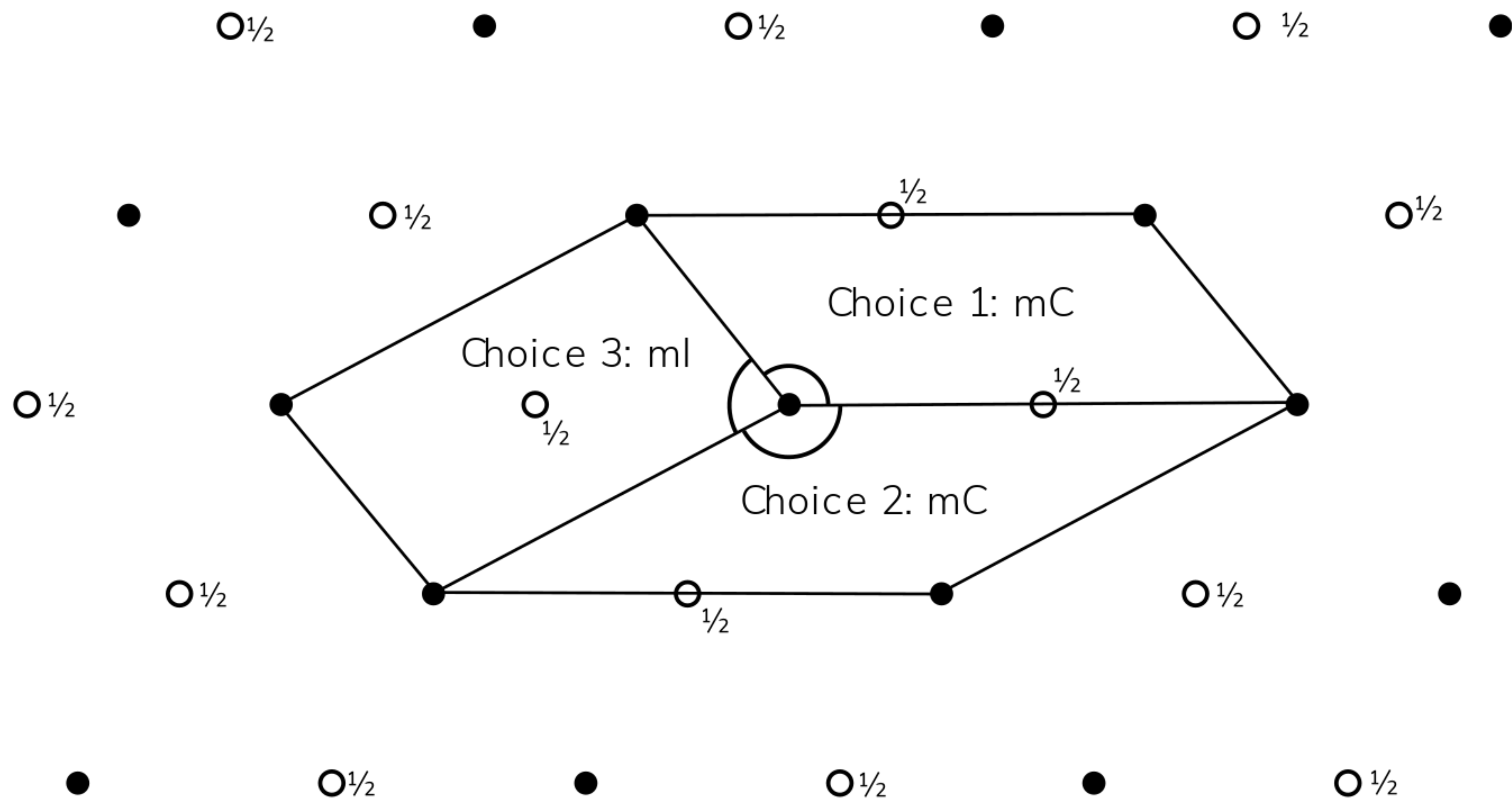
Second run of ambigator:

$\frac{5}{6}$

$\frac{1}{12}$

$\frac{1}{12}$

Cell choices for monoclinic C-centered structures



CrystFEL unit cell tool

Find possible indexing ambiguities:

```
$ cell_tool -p mystructure.cell --find-ambi
```

Calculate radii of all powder rings (useful for calibration):

```
$ cell_tool -p mystructure.cell --rings
```

Calculate all unit cell choices for monoclinic C cell:

```
$ cell_tool -p mystructure.cell --cell-choices
```

Transform a unit cell:

```
$ cell_tool -p mystructure.cell --transform=b,a-2b,c
```

Calculate primitive unit cell from centered cell:

```
$ cell_tool -p mystructure.cell --uncenter
```

Find transformation relating two cells:

```
$ cell_tool -p mystructure.cell --compare other.cell
```


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Wolfgang Brehm (U. Konstanz, now CFEL)

Valerio Mariani

Parker de Waal (Van Andel Inst.)

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Keitaro Yamashita (SPring-8)

Oleksandr Yefanov

Helen Ginn (U. Oxford)

Steve Aplin

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Yaroslav Gevorkov

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