

The World Machine LHC: Jets, Higgs, and Beyond

(or: “*a strong machine for weak interactions*”)



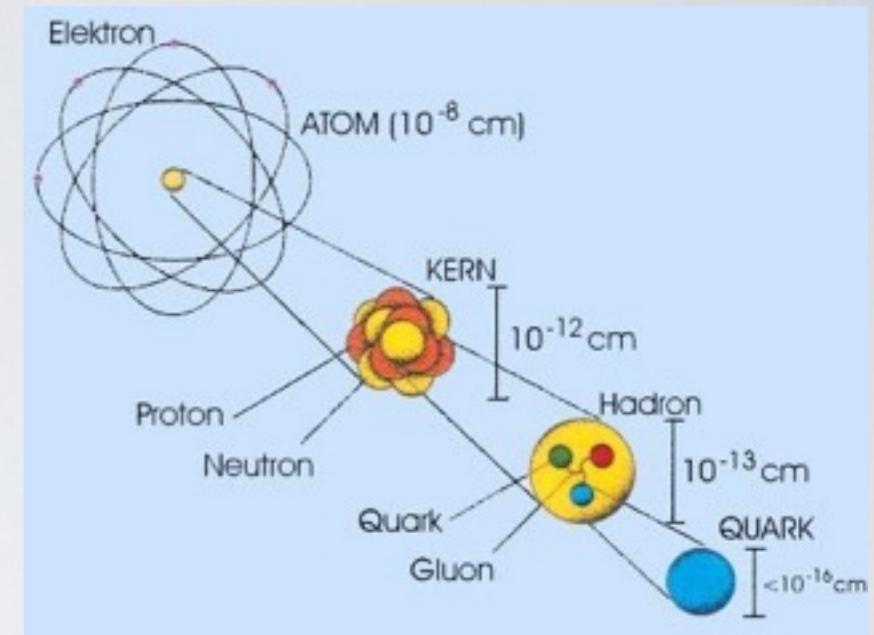
Jürgen R. Reuter, DESY



Why colliders?

Resolving power: $\Delta x \sim \Delta E^{-1} \Rightarrow$
High energy accelerators

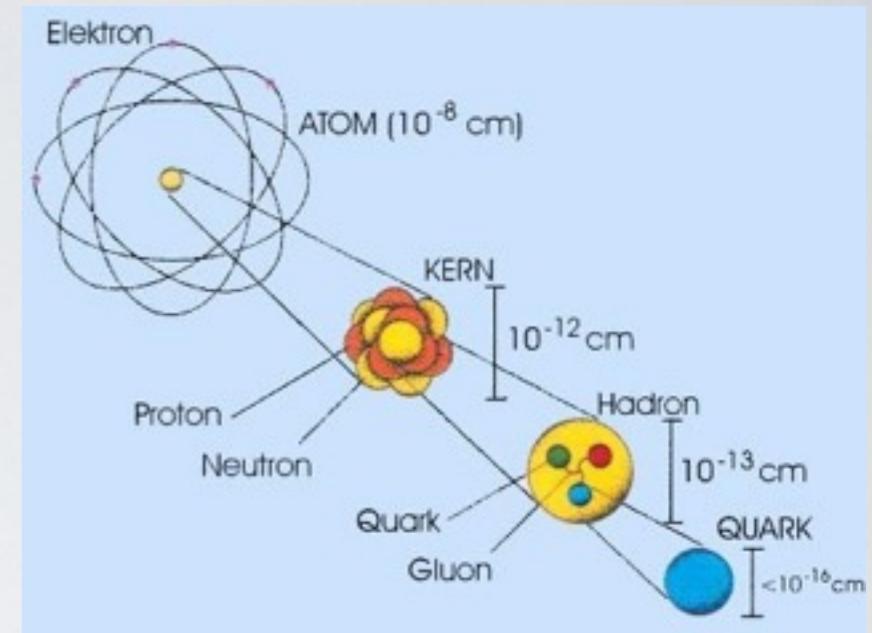
System	Size	Energy
Molecules	10^{-8} m	\sim meV
Atoms	10^{-10} m	\sim eV ... keV
Nuclei	10^{-14} m	\sim MeV ... 10 MeV
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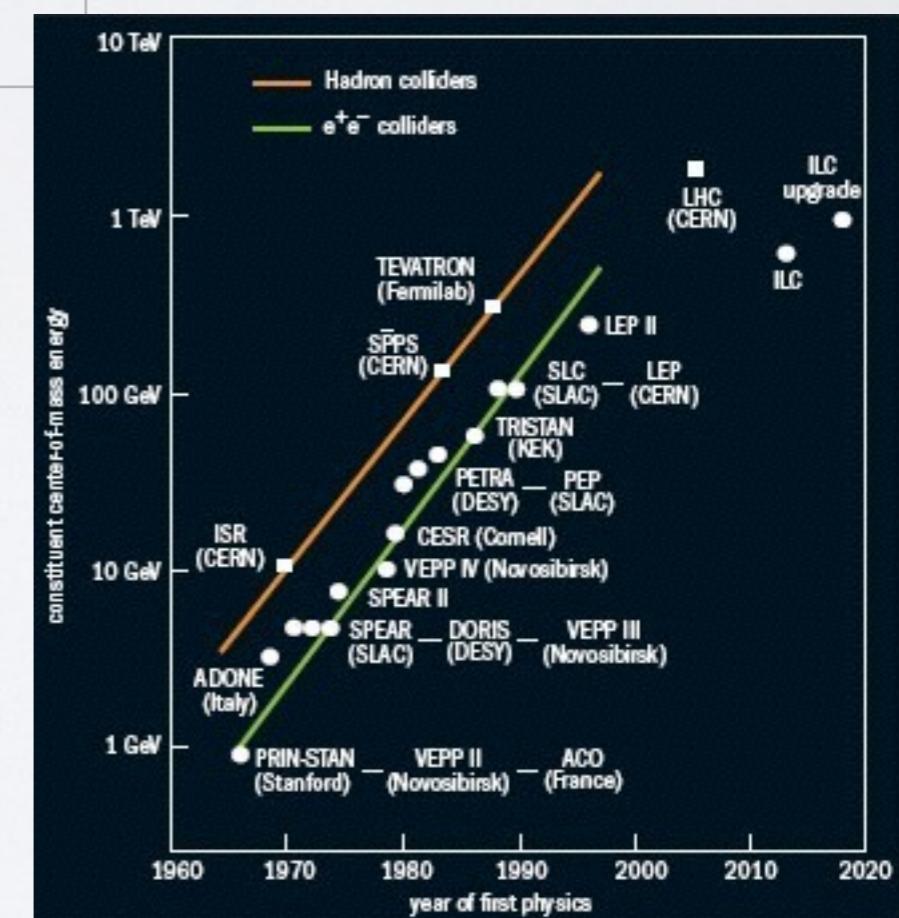
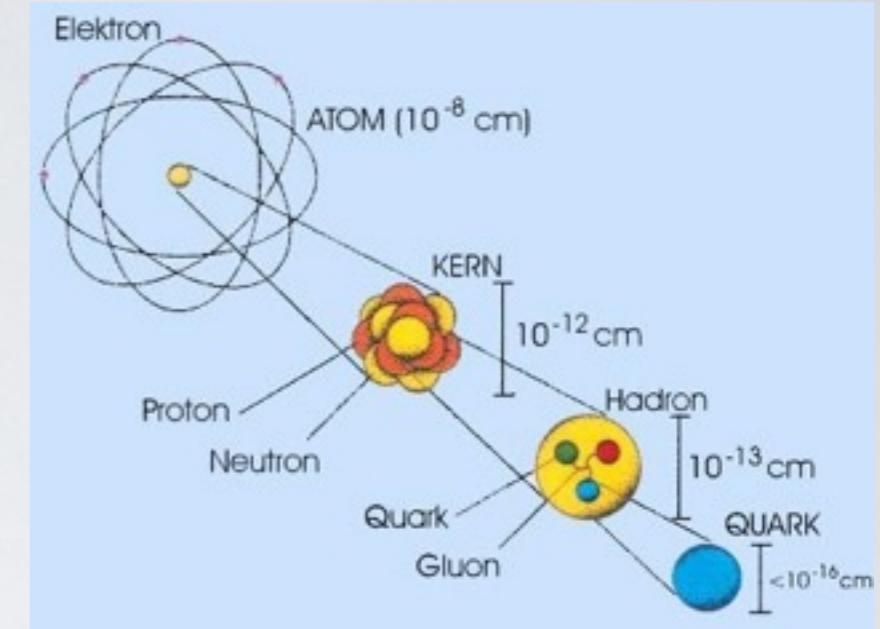


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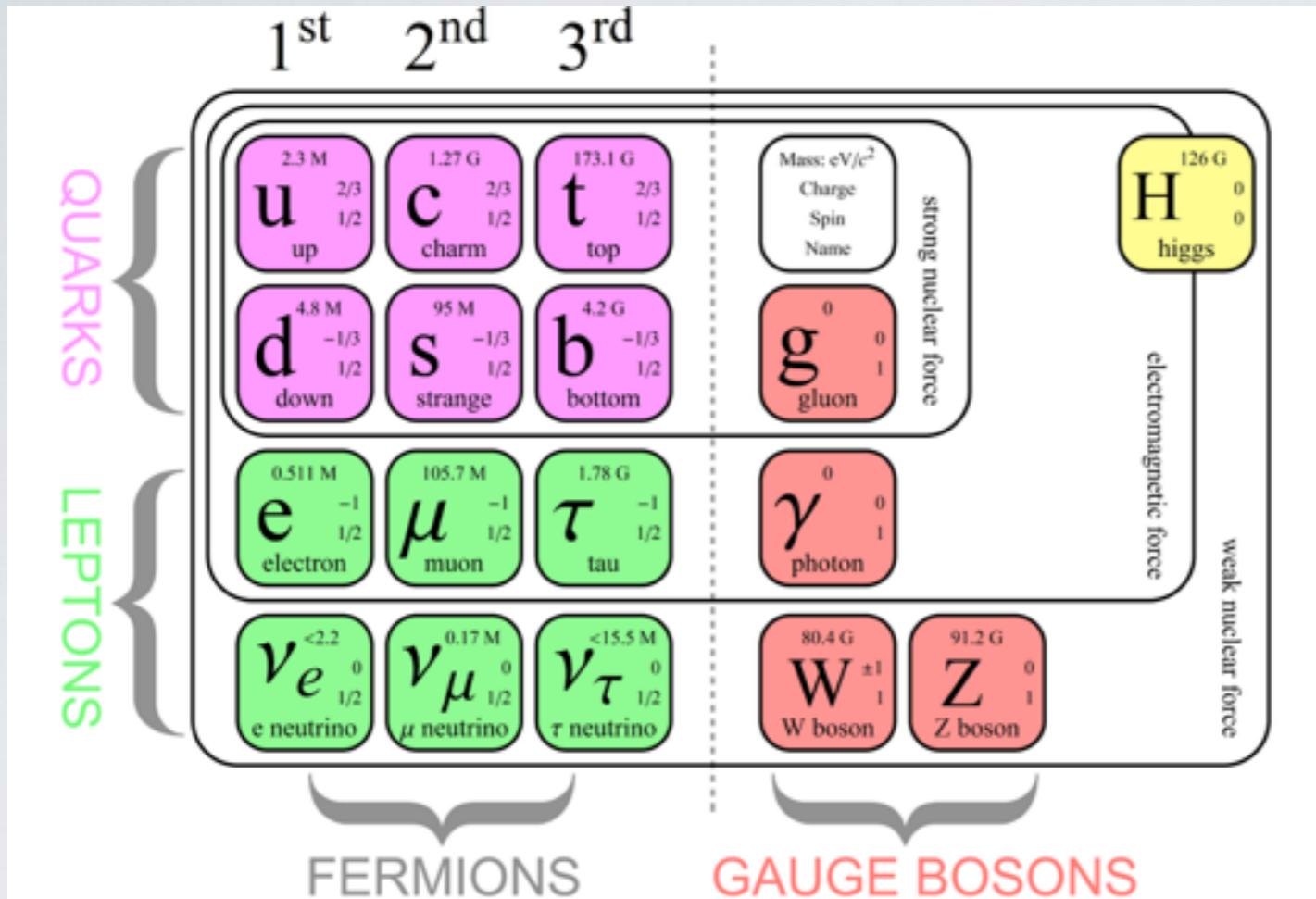
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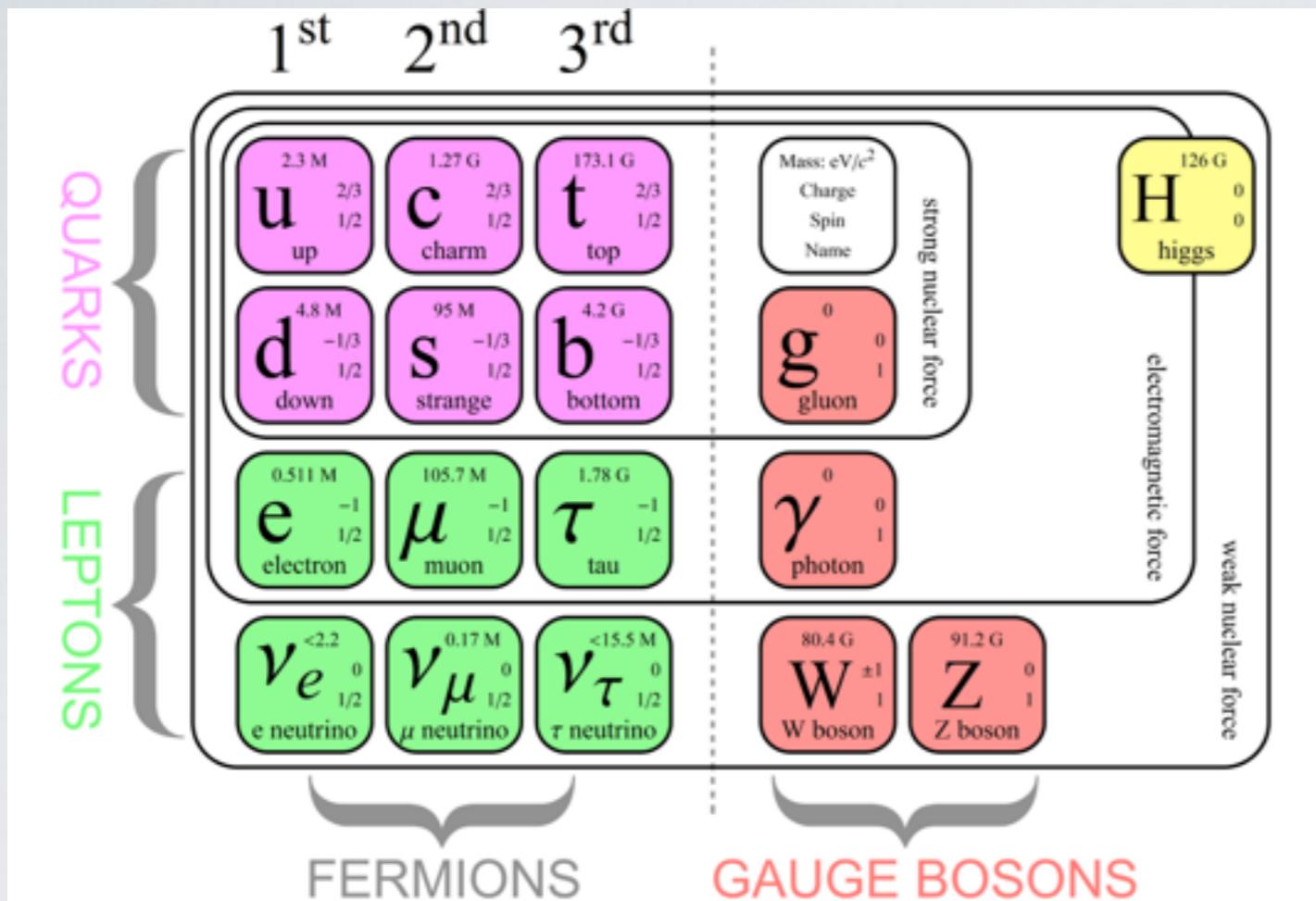


Again, why? The ‘Standard Model’ in a Nutshell

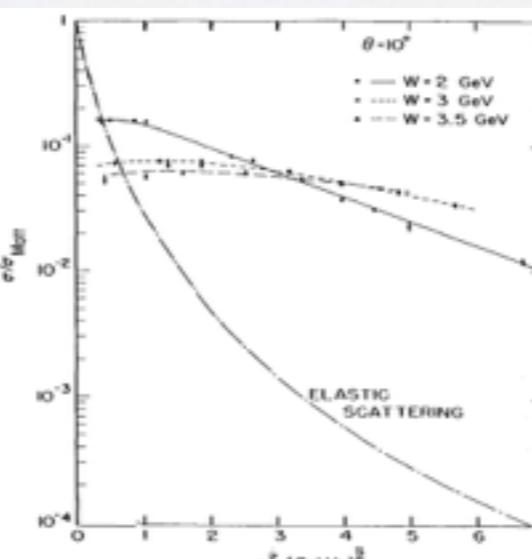


- Standard Model (SM) is $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ gauge theory
- Nuclear forces known since 1930s

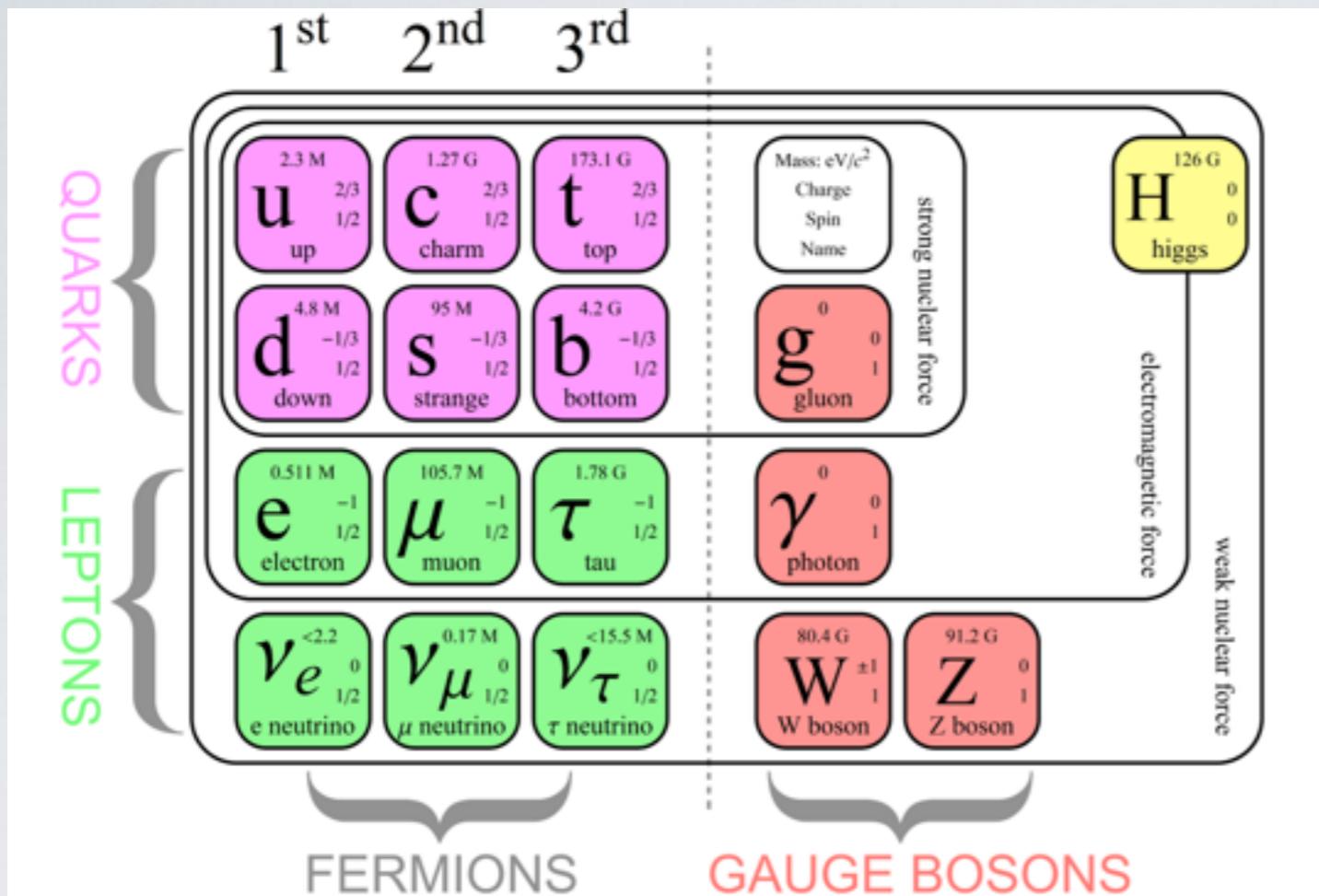
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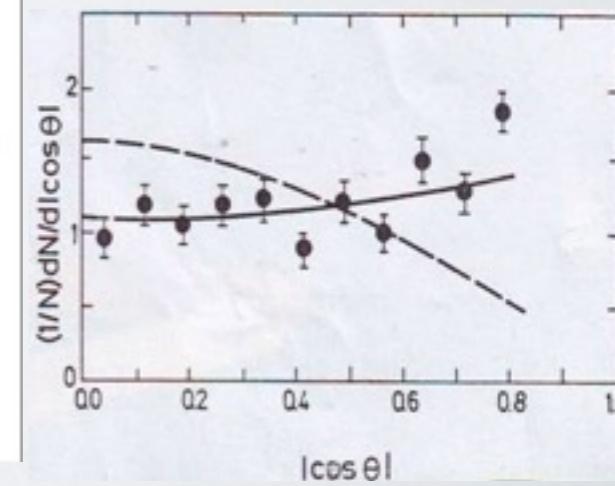
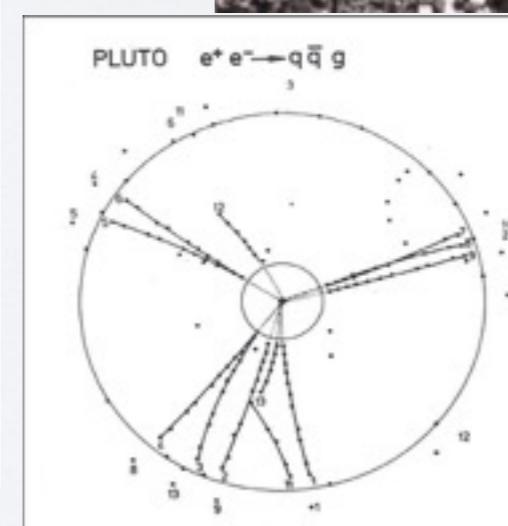
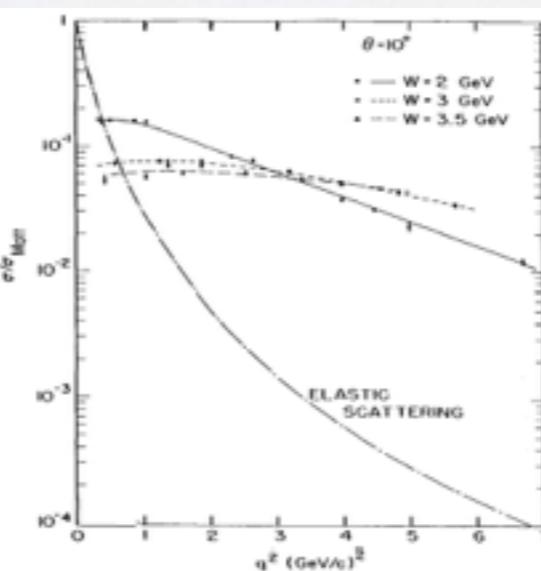
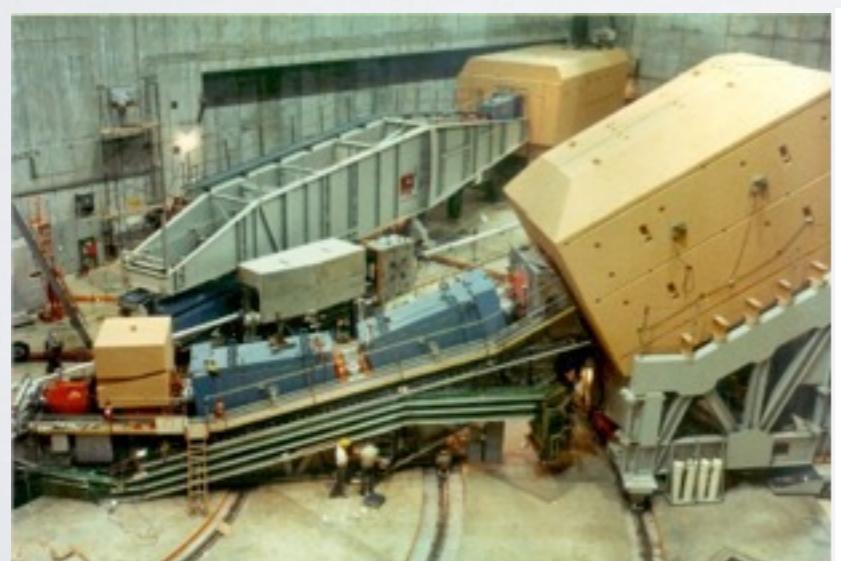
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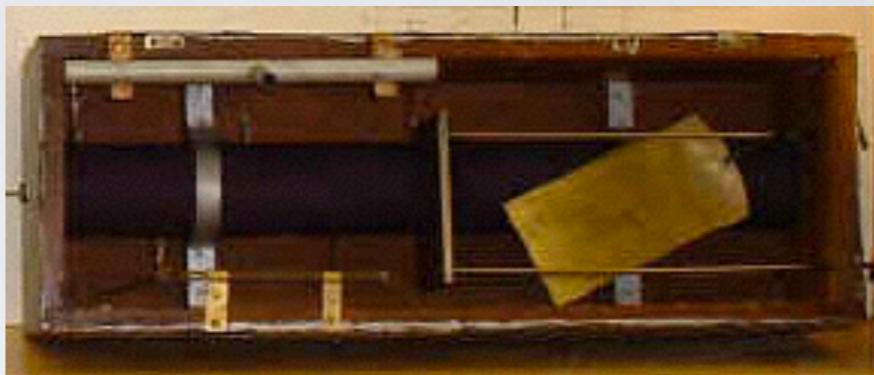


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- Fermi Effective Field Theory charged current weak processes (points to high scale **U**)



VIII. *Uranium Radiation and the Electrical Conduction produced by it.* By E. RUTHERFORD, M.A., B.Sc., formerly 1851 Science Scholar, Coutts Trotter Student, Trinity College, Cambridge; McDonald Professor of Physics, McGill University, Montreal*.

THE remarkable radiation emitted by uranium and its compounds has been studied by its discoverer, Becquerel, and the results of his investigations on the nature and properties of the radiation have been given in a series of papers in the *Couptes Rendus*†. He showed that the radiation, continuously emitted from uranium compounds, has the power of passing through considerable thicknesses of metals and other opaque substances; it has the power of acting on a photographic plate and of discharging positive and negative electrification to an equal degree. The gas through which the radiation passes is made a temporary conductor of electricity and preserves its power of discharging electrification for a short time after the source of radiation has been removed.

The results of Becquerel showed that H^ontgen and uranium radiations were very similar in their power of penetrating solid bodies and producing conduction in a gas exposed to them; but there was an essential difference between the two types of radiation. He found that uranium radiation could be refracted and polarized, while no definite results showing

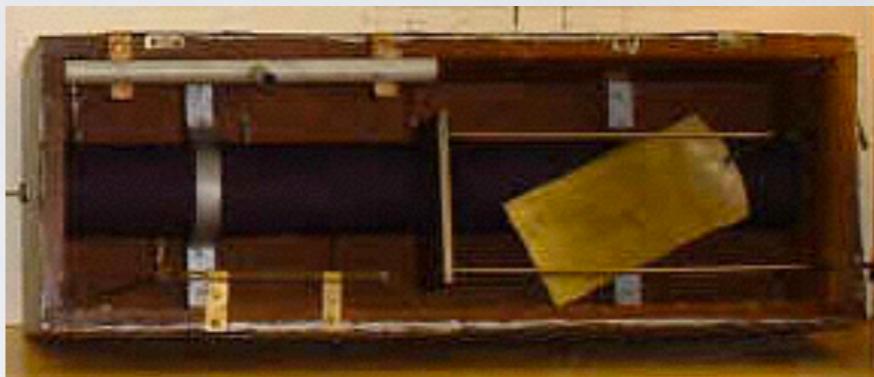
* Communicated by Prof. J. J. Thomson, F.R.S.

† C. R. 1896, pp. 420, 501, 559, 689, 767; 1897, pp. 438, 800,

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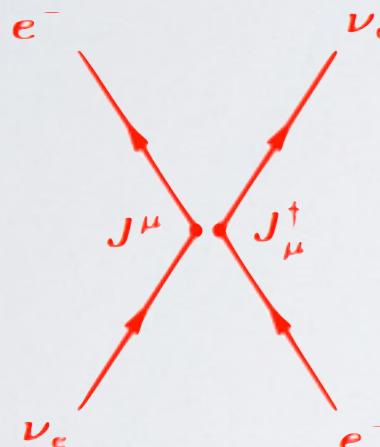
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Effective theory leads to invalidity / unitarity violation at higher energies

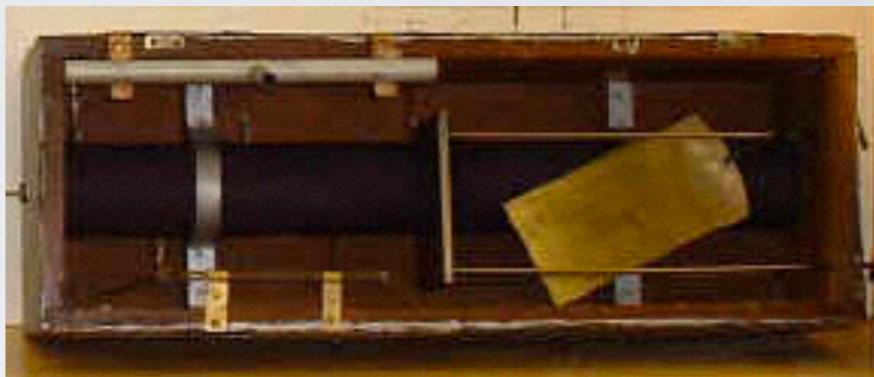


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S-wave unitarity demands: $\sqrt{s} \lesssim 500 \text{ GeV}$

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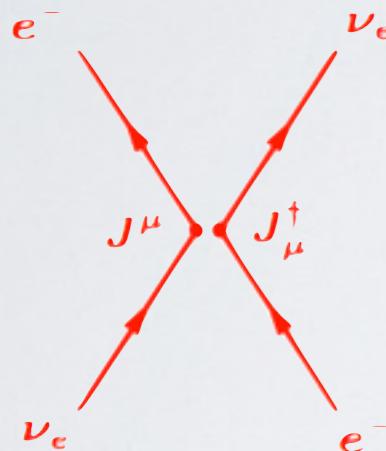
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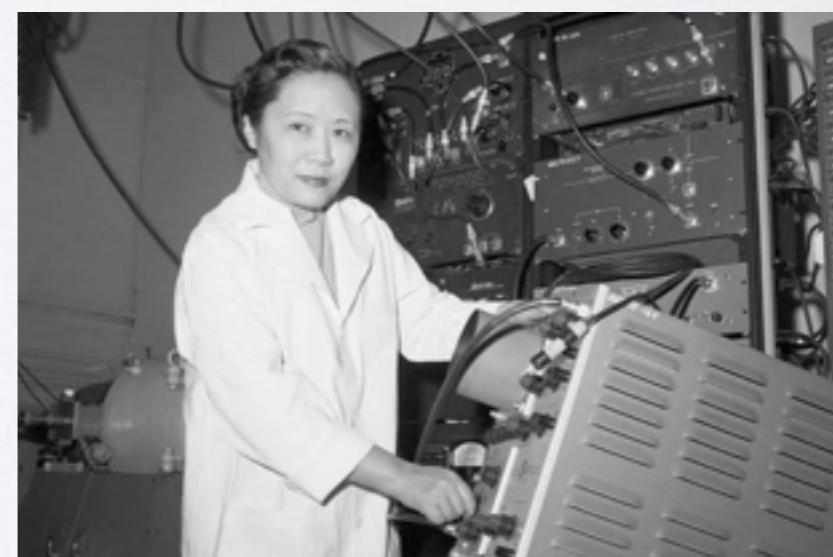
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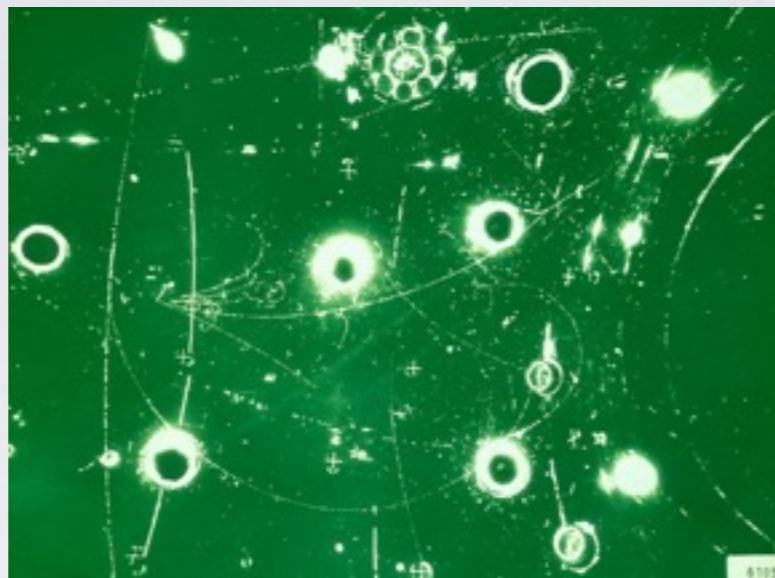
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- P violation, 1955
- Neutrino is left-handed, 1956
- CP violation, 1964
- Brout-Englert-Higgs mechanism, 1960/61/64

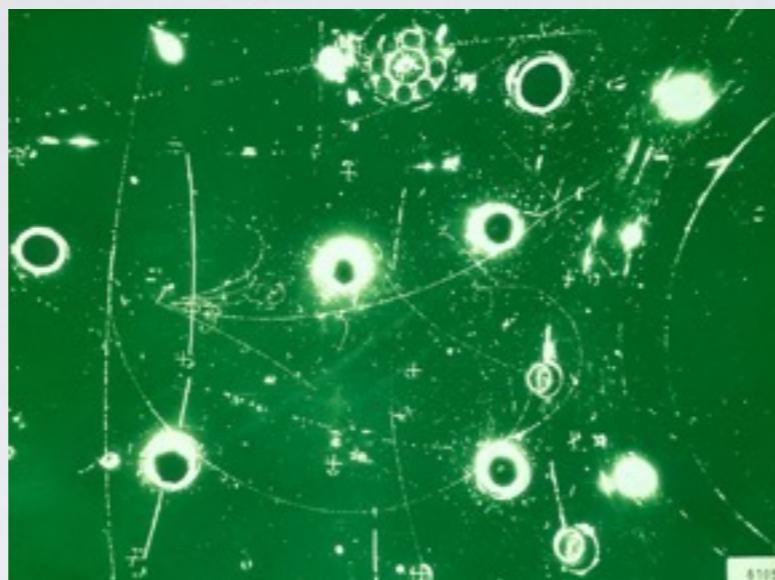


The mystery of Electroweak Symmetry Breaking

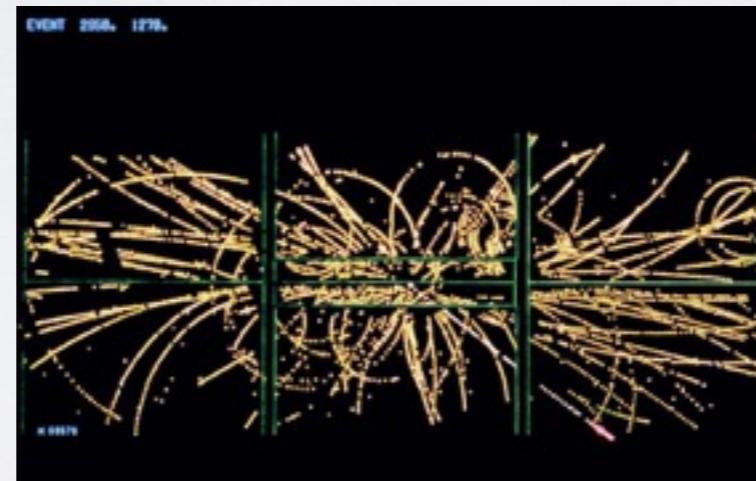


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- Discovery of neutral currents (CERN, Gargamelle, 1973)

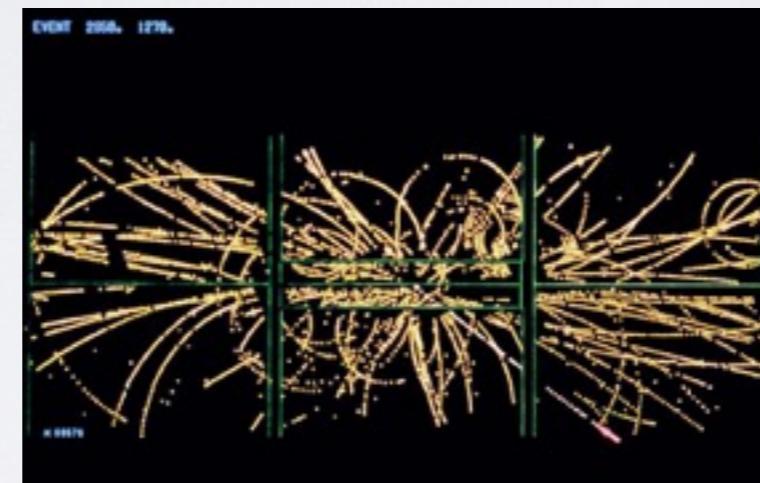
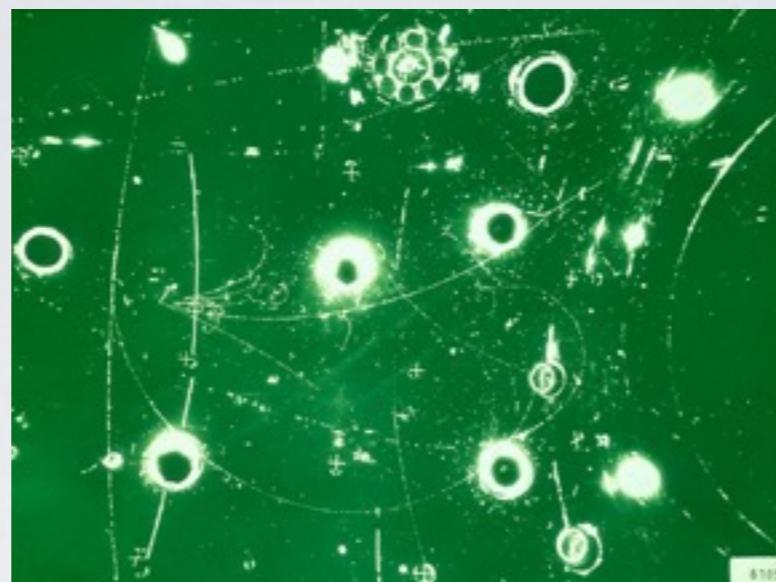
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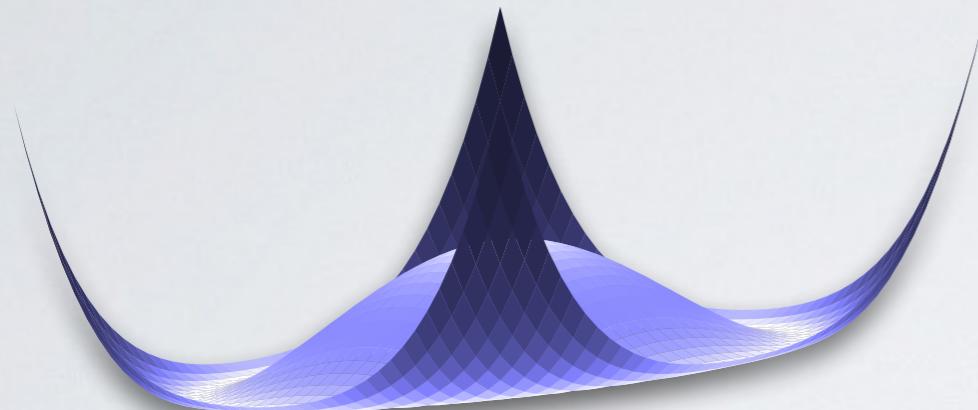
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- All mass terms are forbidden by symmetry (except for the Higgs)

Q_L	u_R	d_R	L_L	e_R	H	ν_R
$(\mathbf{2}, \mathbf{3})_{\frac{1}{3}}$	$(\mathbf{1}, \mathbf{3})_{\frac{4}{3}}$	$(\mathbf{1}, \mathbf{3})_{-\frac{2}{3}}$	$(\mathbf{2}, \mathbf{1})_1$	$(\mathbf{1}, \mathbf{1})_{-2}$	$(\mathbf{2}, \mathbf{1})_1$	$(\mathbf{1}, \mathbf{1})_0$

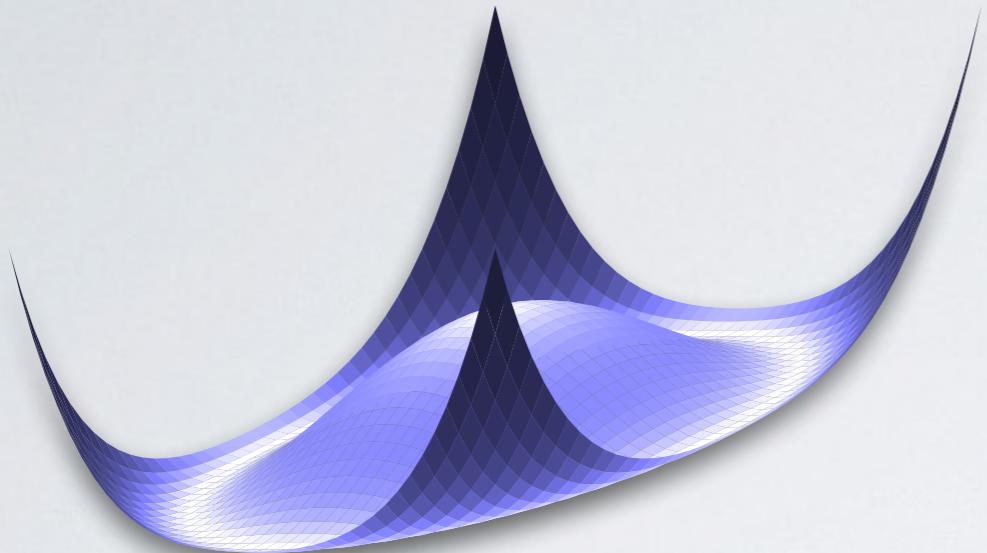
The Higgs breaking parameterization

$$V(\phi) = -\mu^2|\phi|^2 + \frac{\lambda}{2}(|\phi|^2)^2$$



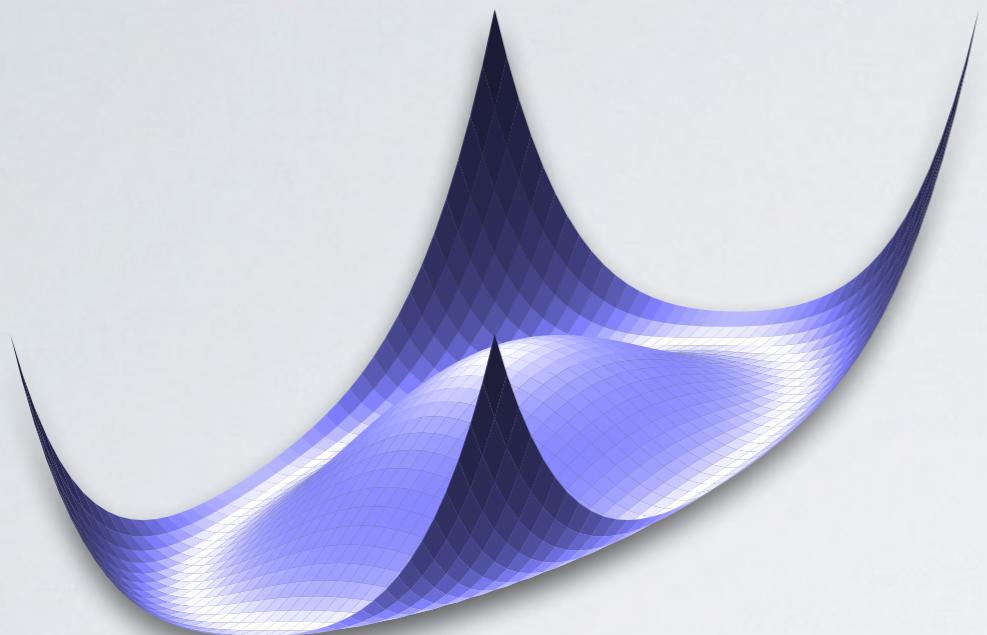
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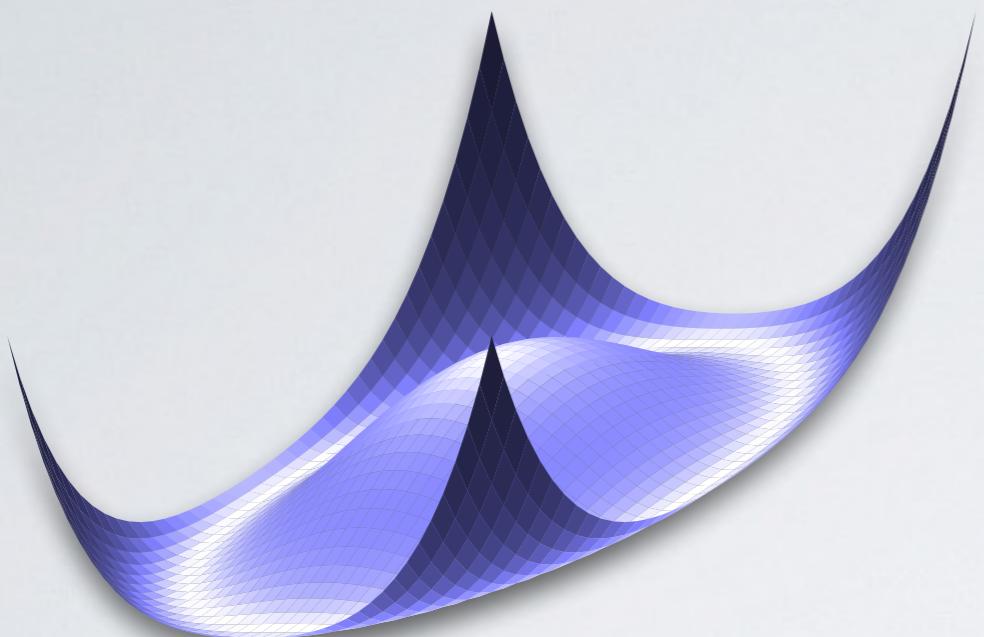


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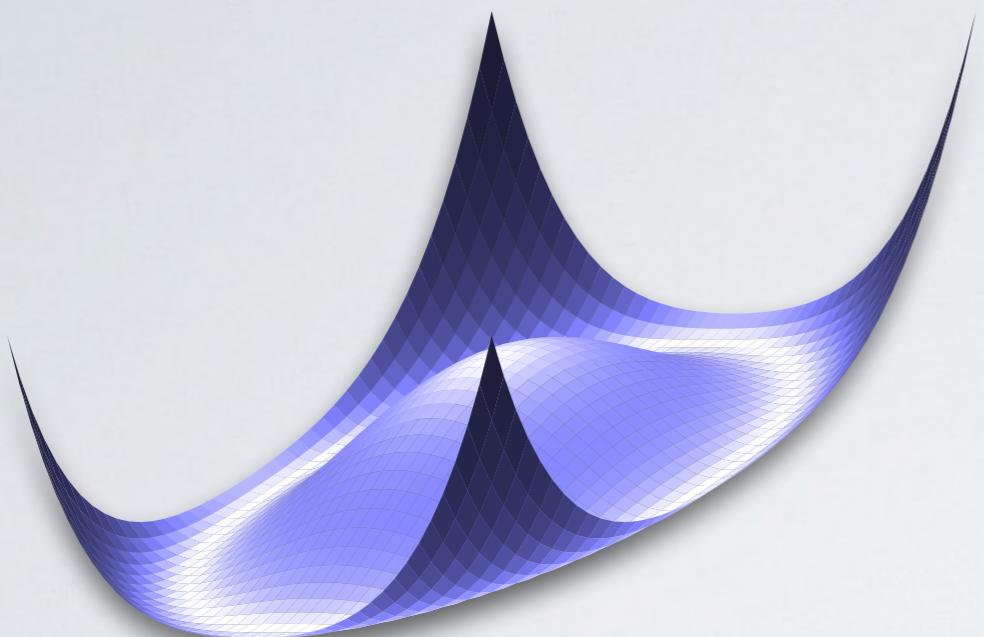


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- Higgs potential has non-trivial minimum
- Radial excitation (massive): **Higgs field**
- Phase: **Goldstone boson**

$$\phi(x) = \frac{1}{\sqrt{2}}(v + h(x))e^{\frac{i}{v}\pi(x)}$$

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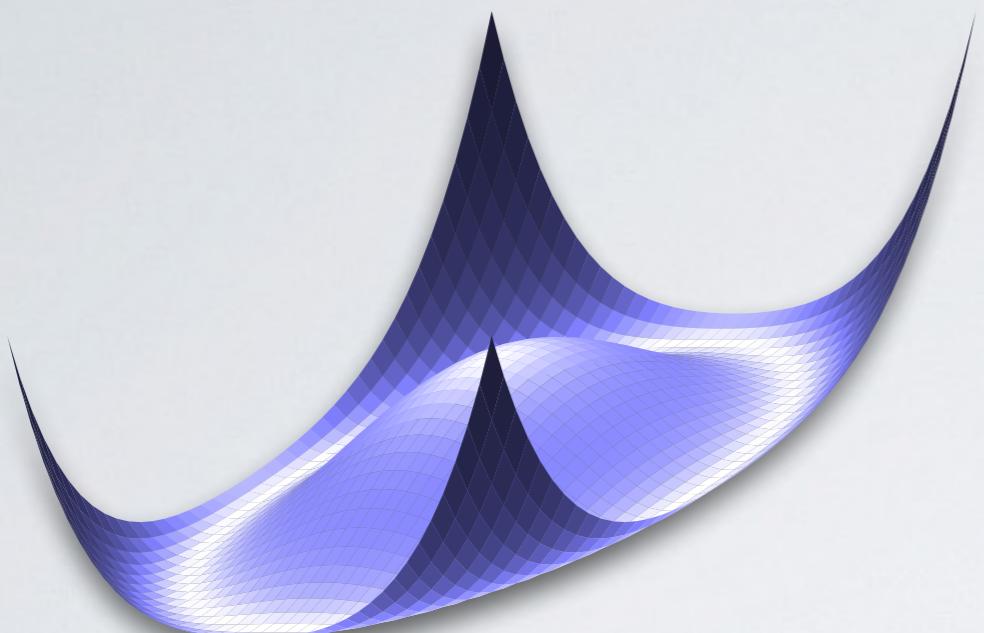
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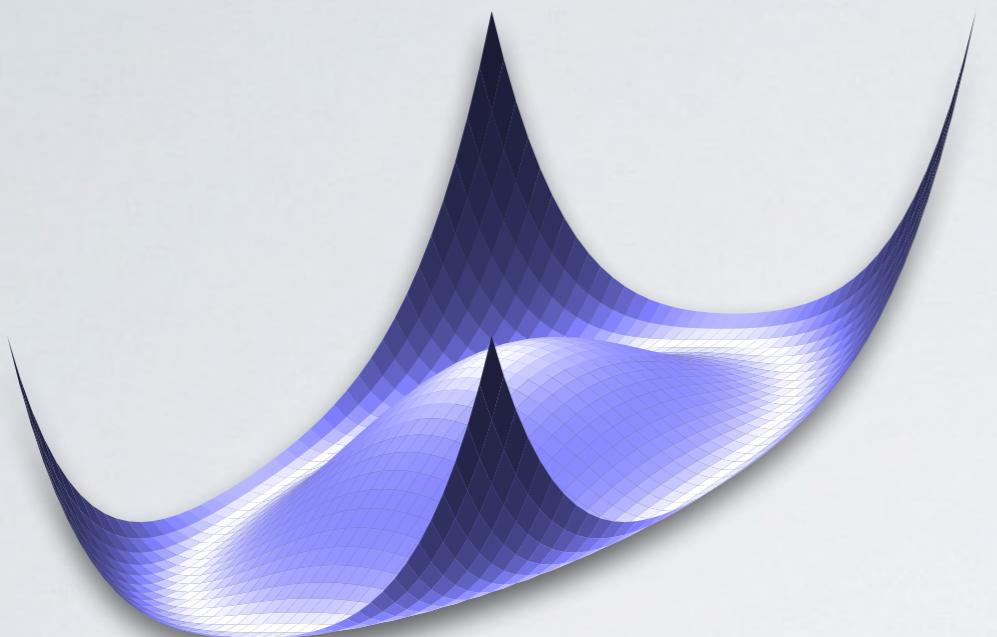
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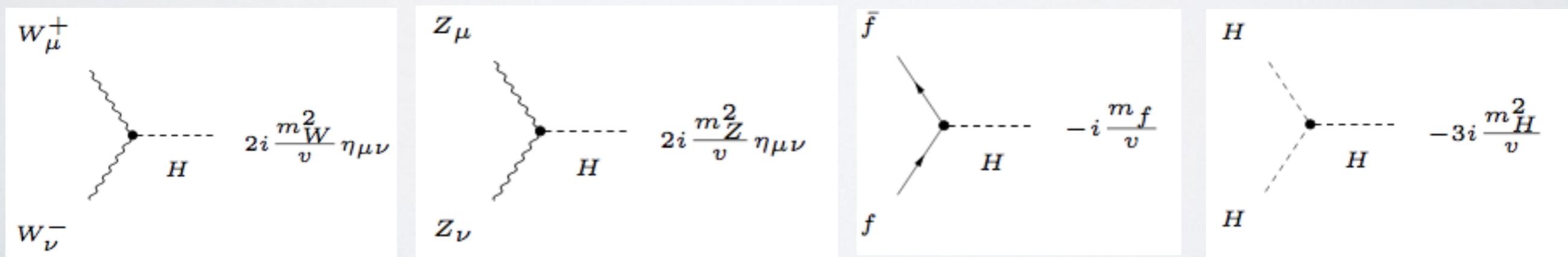
Particle masses \propto Higgs coupling strength \iff Higgs couples \propto particle masses

$$m_W = gv/2$$

$$m_Z = gv/(2 \cos \theta_W)$$

$$m_f = vY_f/\sqrt{2}$$

$$m_H = v\sqrt{\lambda}$$



A potential potential problem

Even discovery of SM Higgs boson has not solved puzzle of Electroweak Symmetry Breaking



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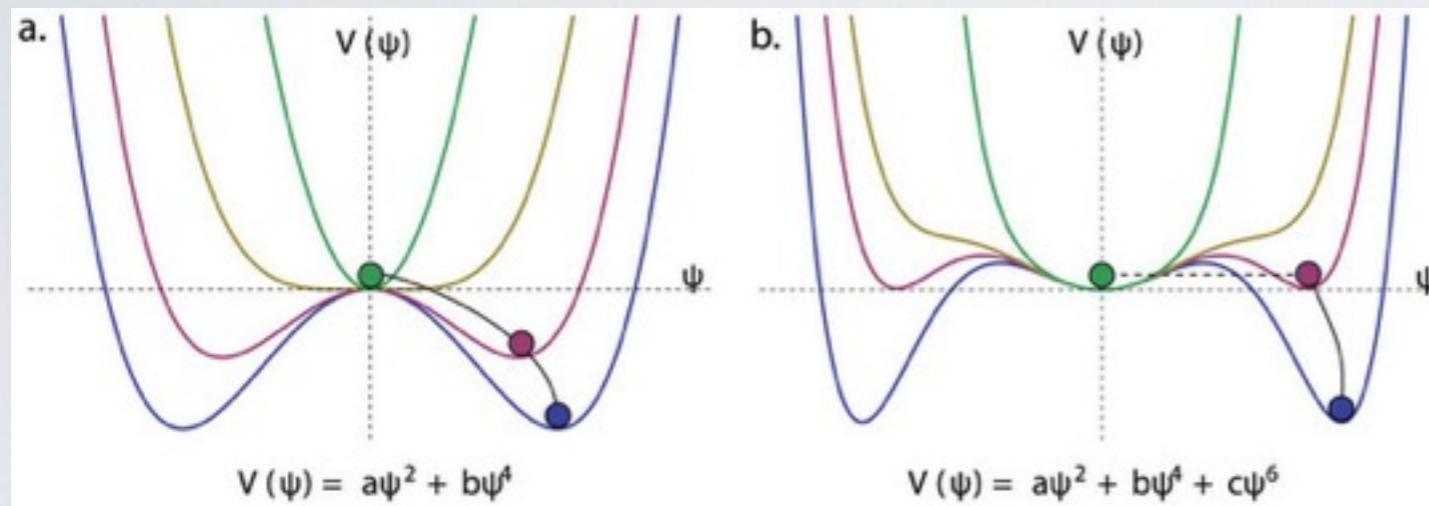
Higgs system similar to a Quantum Phase Transition with Landau-Ginzburg potential



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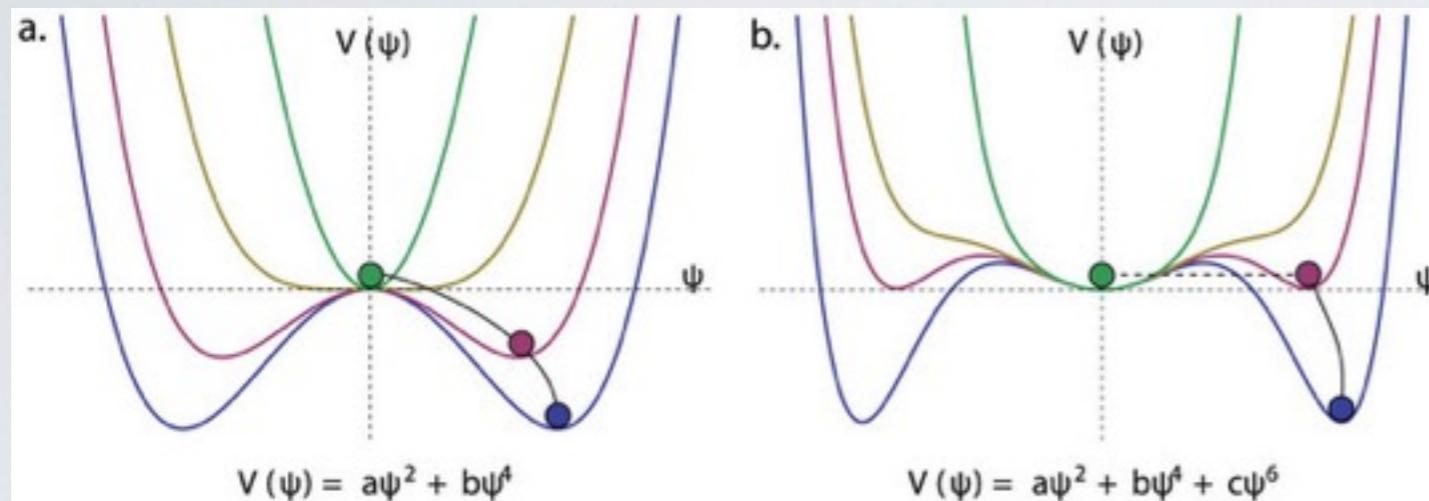
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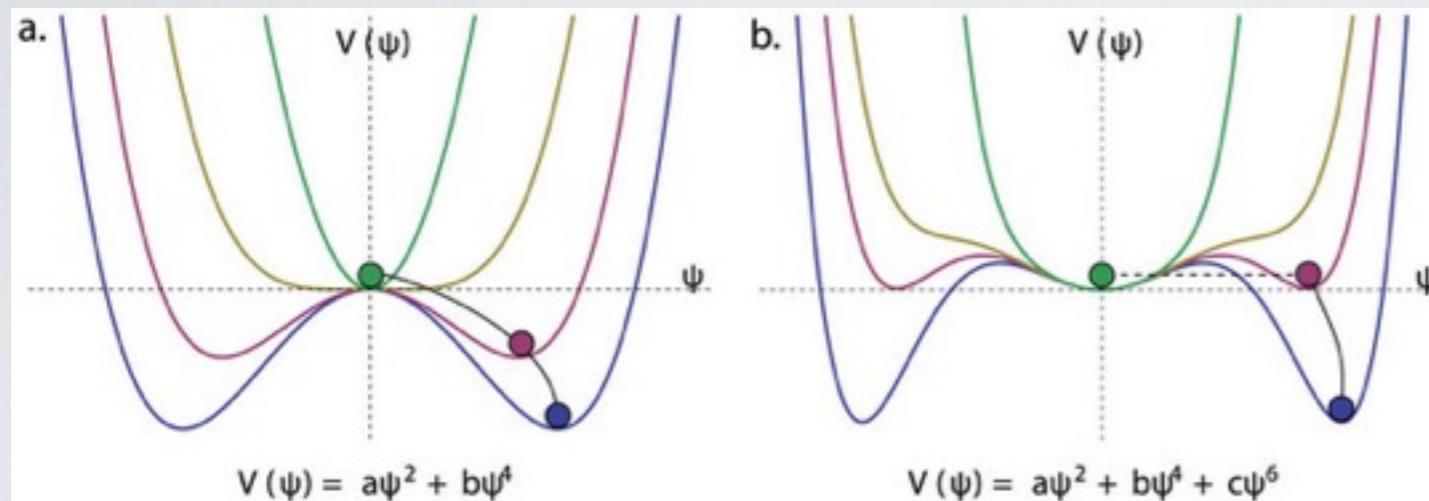
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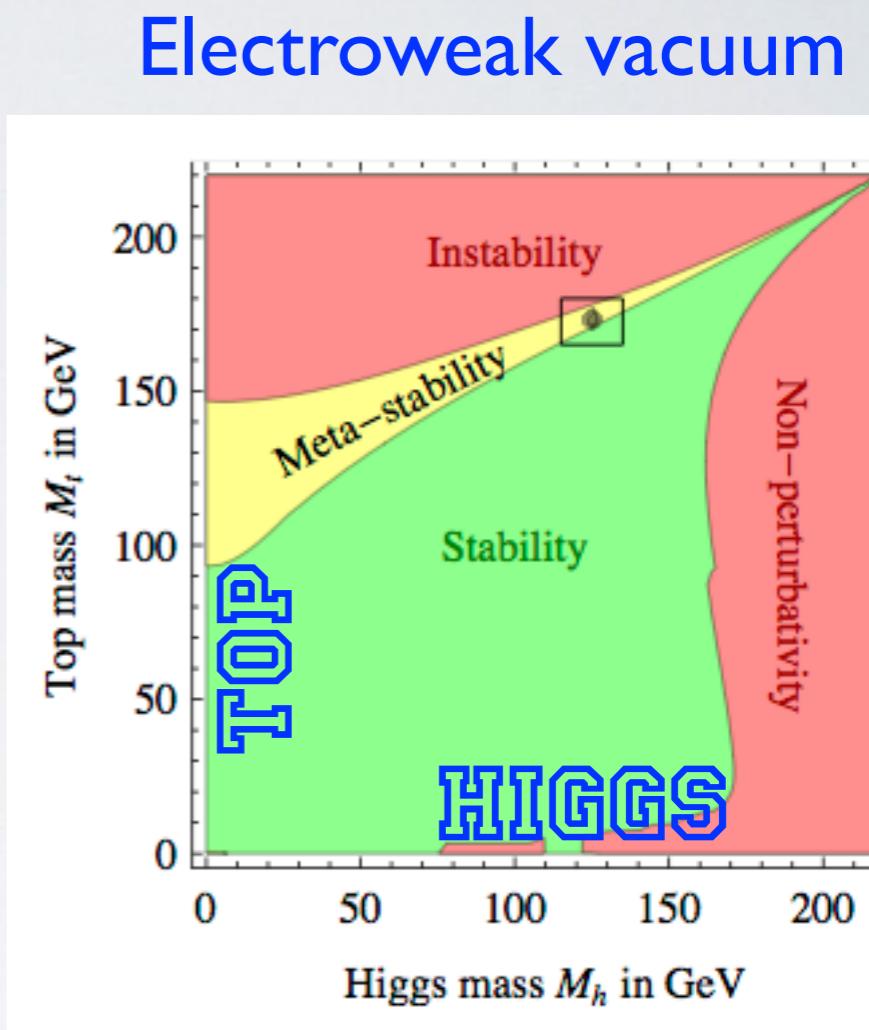
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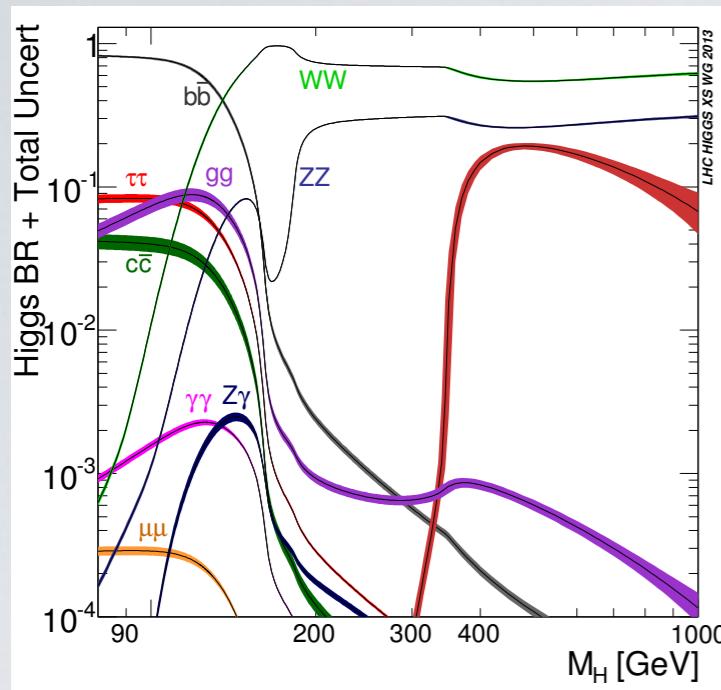
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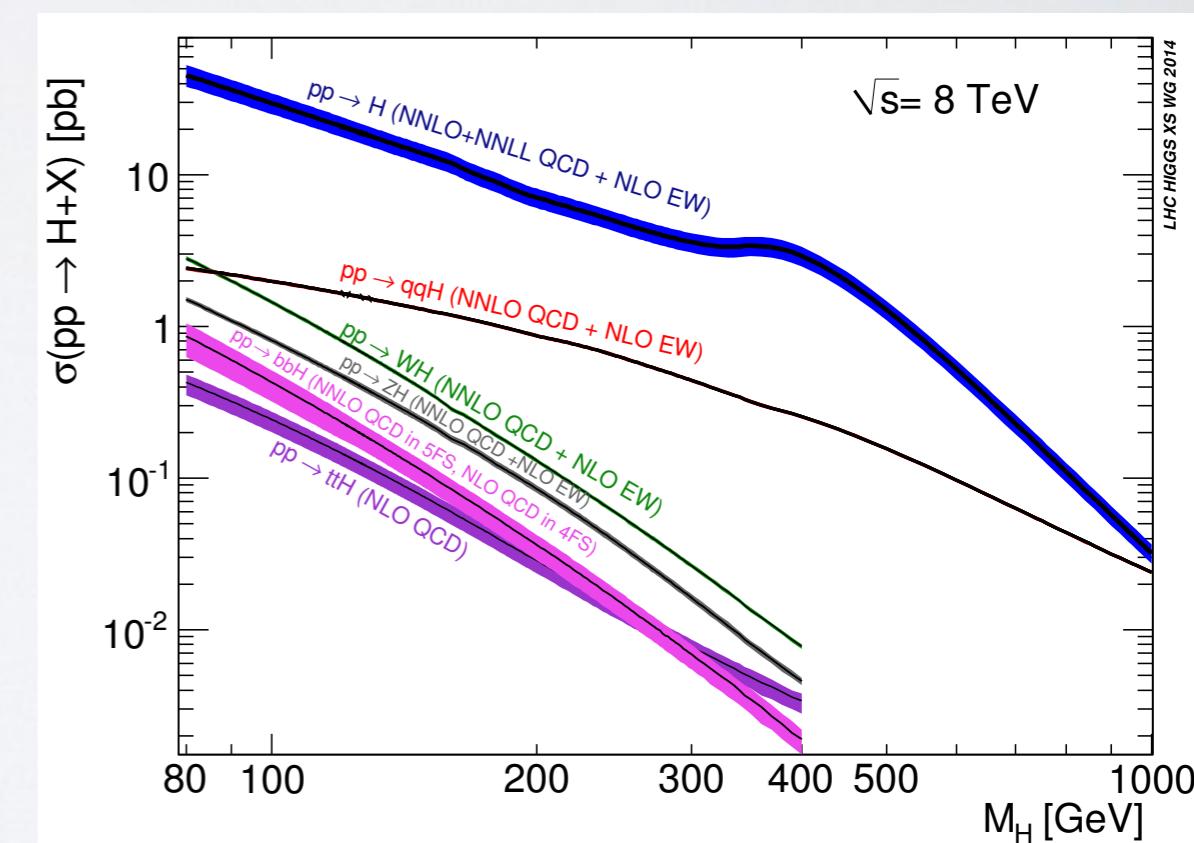
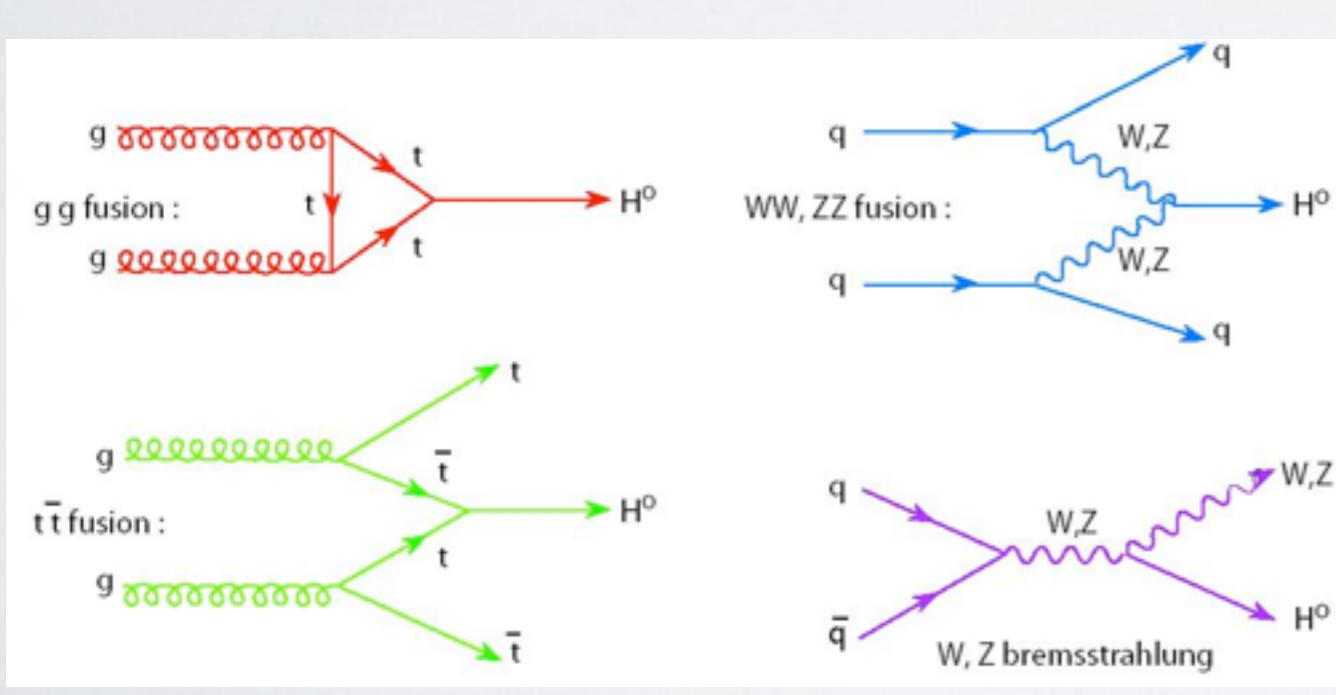
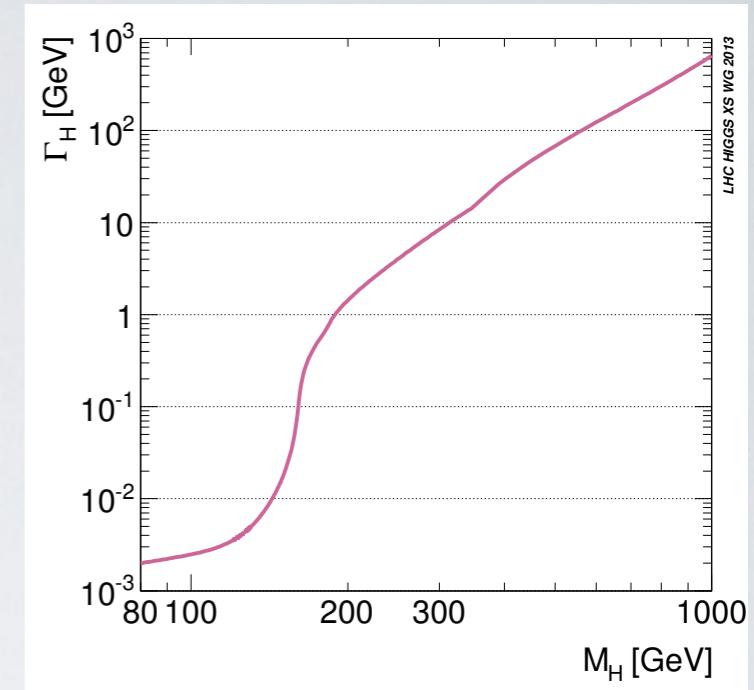
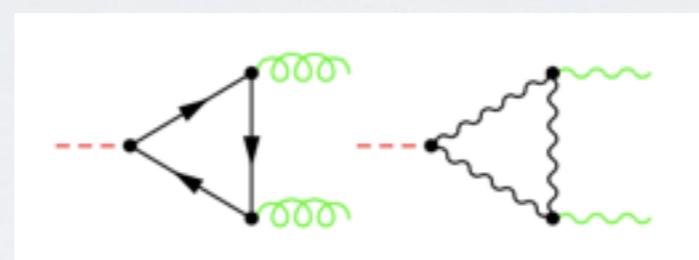
(note: plot under assumptions of NO additional BSM)



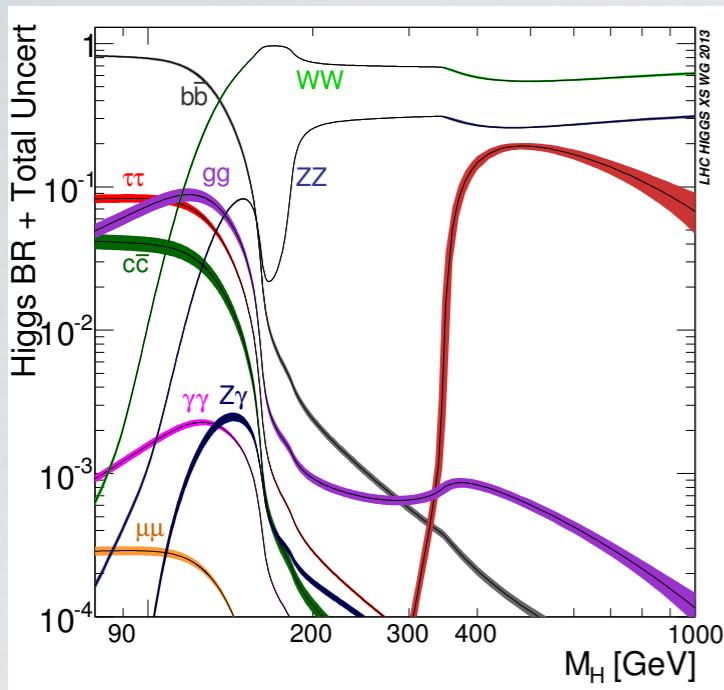
The Higgs boson at a hadron collider



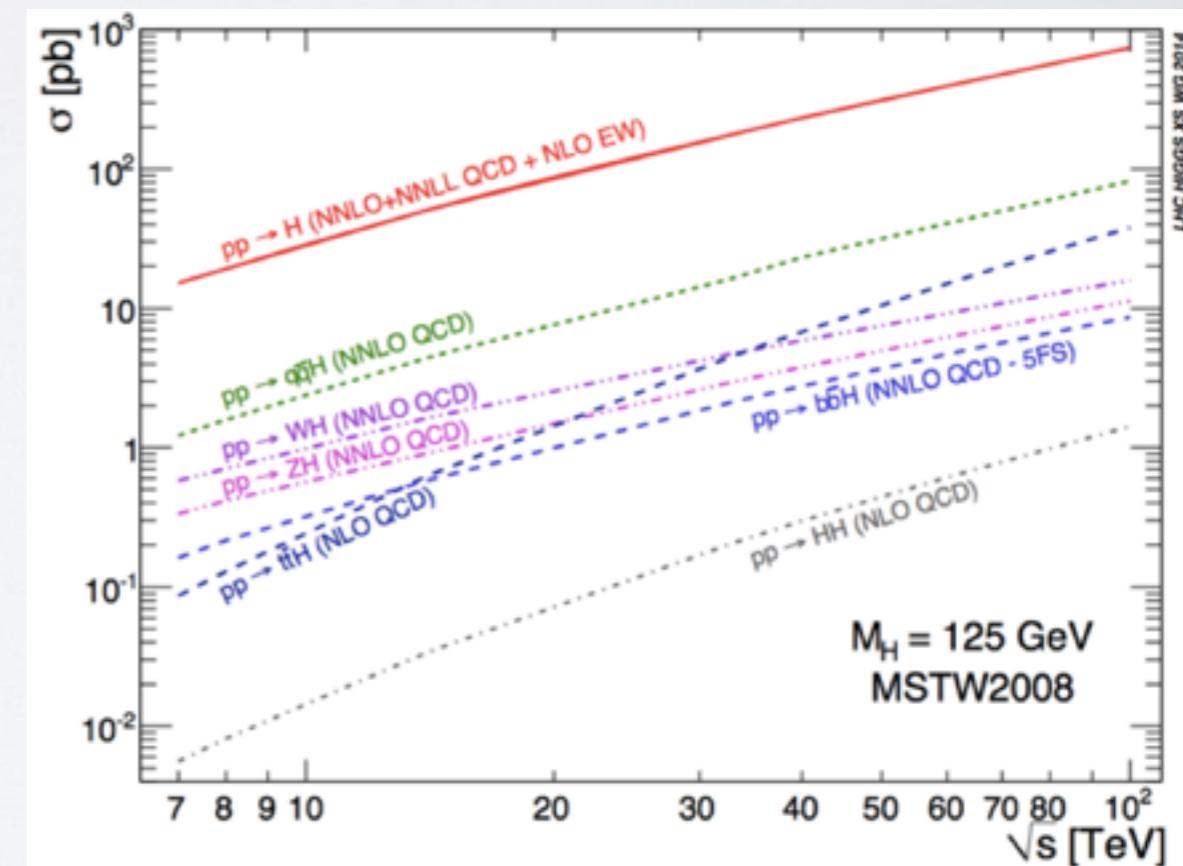
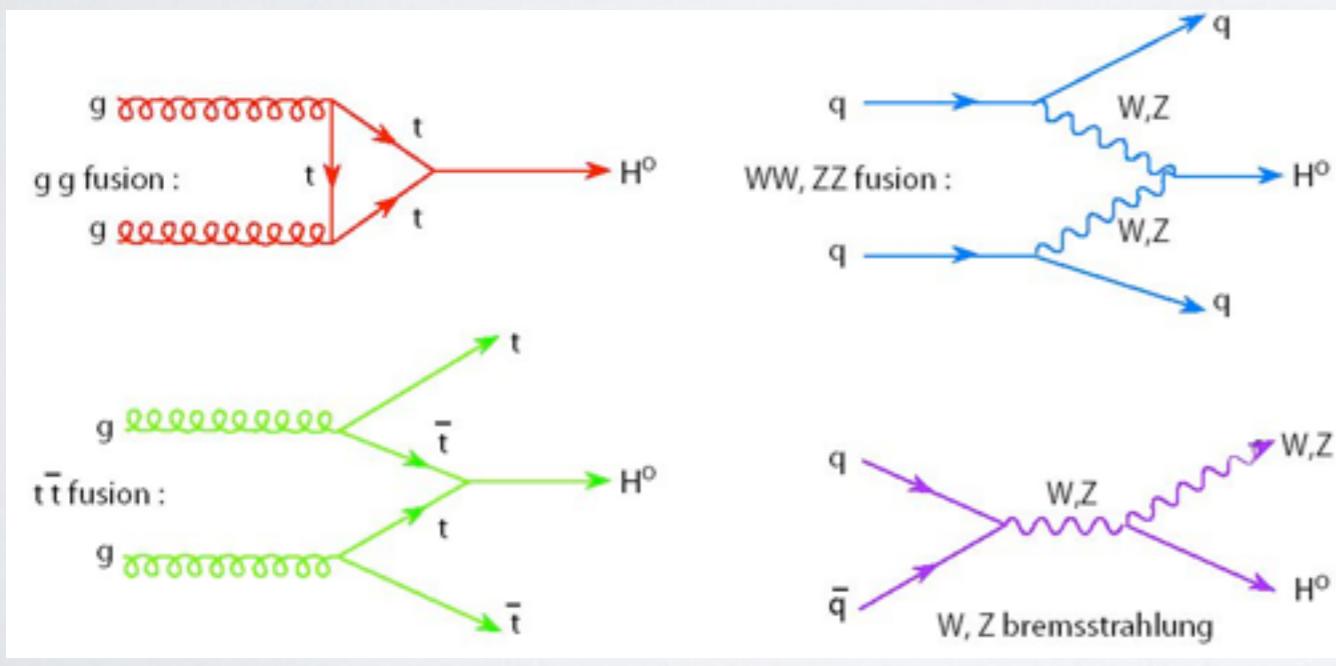
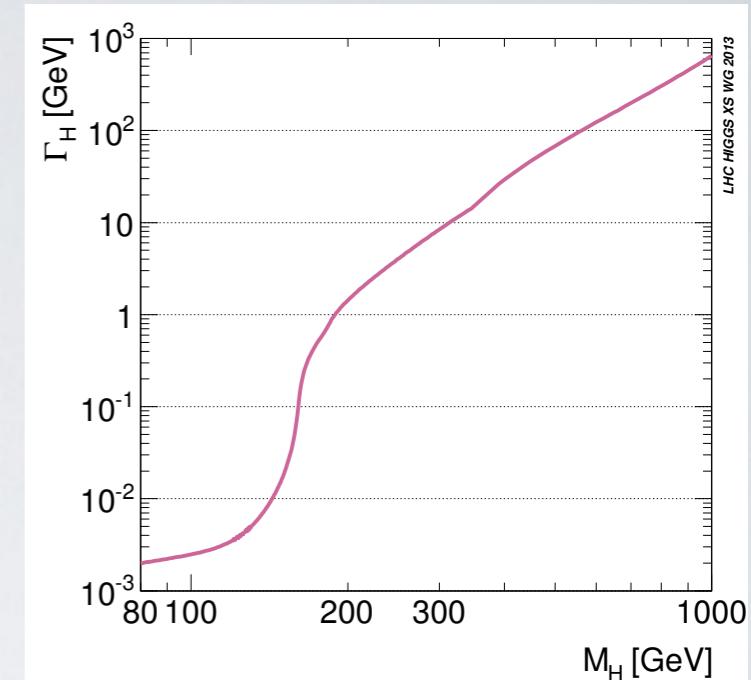
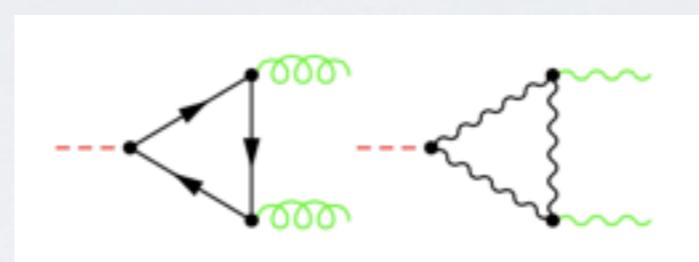
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The “guaranteed” SSC discovery

Superconducting Super Collider (SSC): 87.1 km tunnel, design: 40 TeV $p\bar{p}$ collisions

1999
1999



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The World Machine LHC

Christmas WS, Univ. Autonoma Madrid, 10.12.2015

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[1st SSC Workshop: 1976
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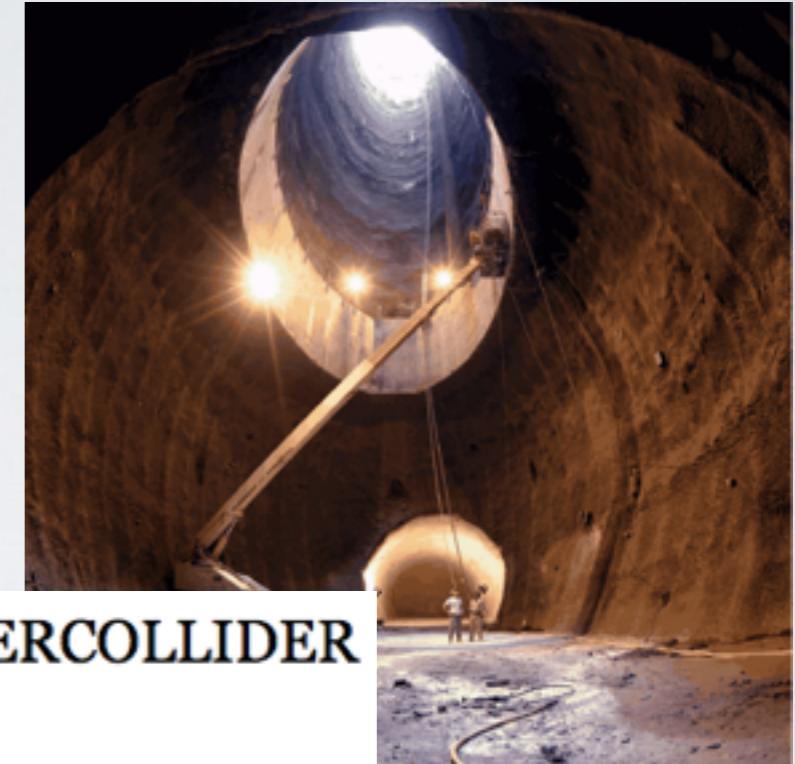
The New York Times

HOUSE DEALS BLOW TO SUPERCOLLIDER

By CLIFFORD KRAUSS,
Published: June 25, 1993

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1999
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The “guaranteed” SSC discovery

Superconducting Super Collider (SSC): 87.1 km tunnel, design: 40 TeV $p\bar{p}$ collisions



23.5 km tunnel bored, 17 shafts, 2 caverns, 1 LINAC tunnel finished

[1st SSC Workshop: 1976
1st LHC Workshop: 1982]

The New York Times

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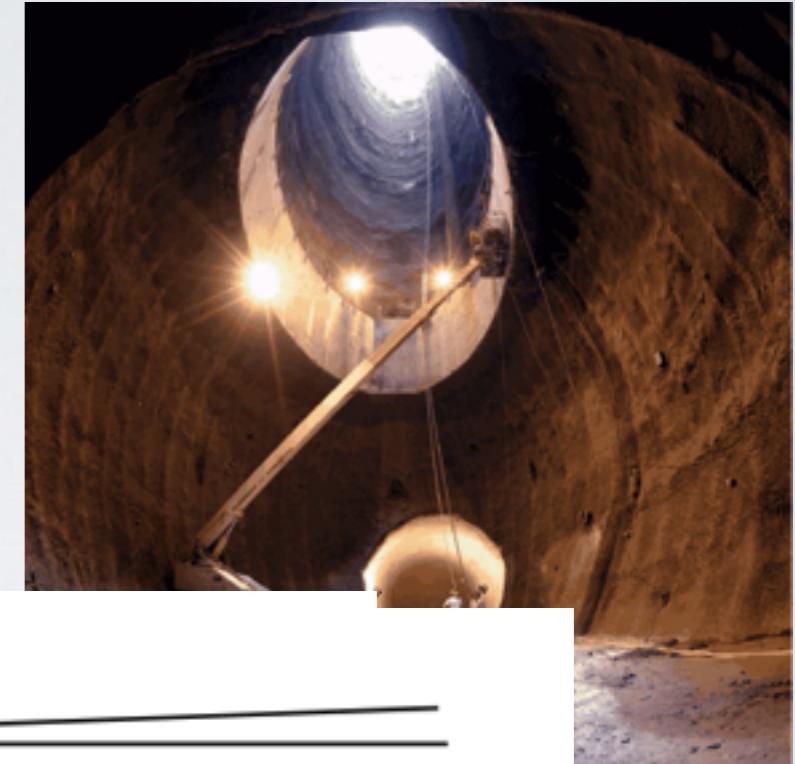
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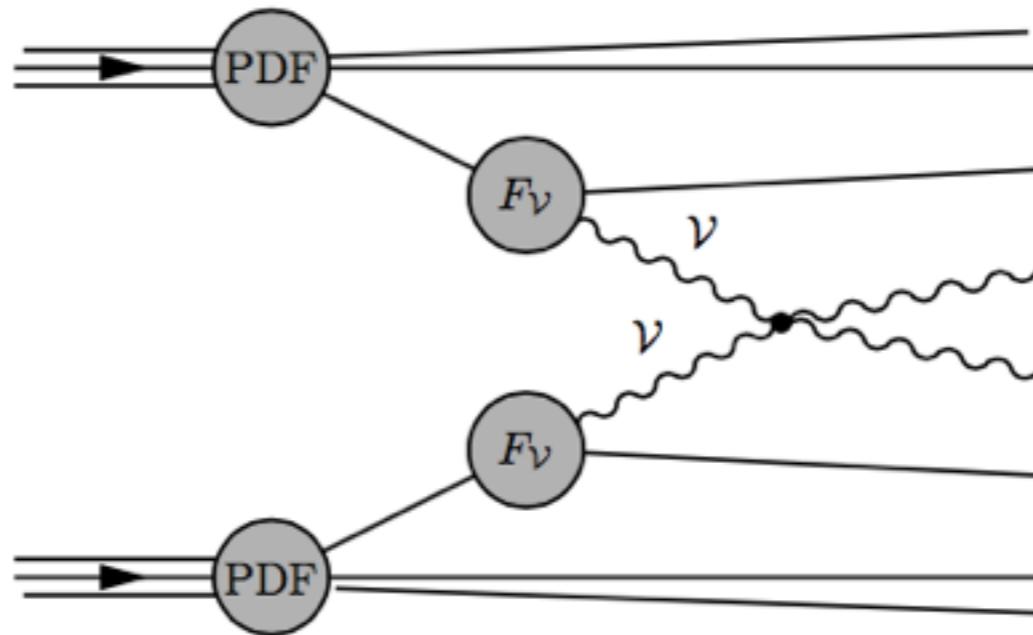


The New York Times

HOUSI

By CLIFFORD KELLEY
Published: June 1
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Either Higgs discovery or something in WW scattering at 1-1.5 TeV



The “guaranteed” LHC discovery

Optical Theorem (Unitarity of the S(cattering) Matrix):

$$\sigma_{\text{tot}} = \text{Im} [\mathcal{M}_{ii}(t = 0)] / s \quad t = -s(1 - \cos \theta)/2$$

Partial wave amplitudes:

$$\mathcal{M}(s, t, u) = 32\pi \sum_{\ell} (2\ell + 1) \mathcal{A}_{\ell}(s) P_{\ell}(\cos \theta) \quad (\text{“Power spectrum”})$$



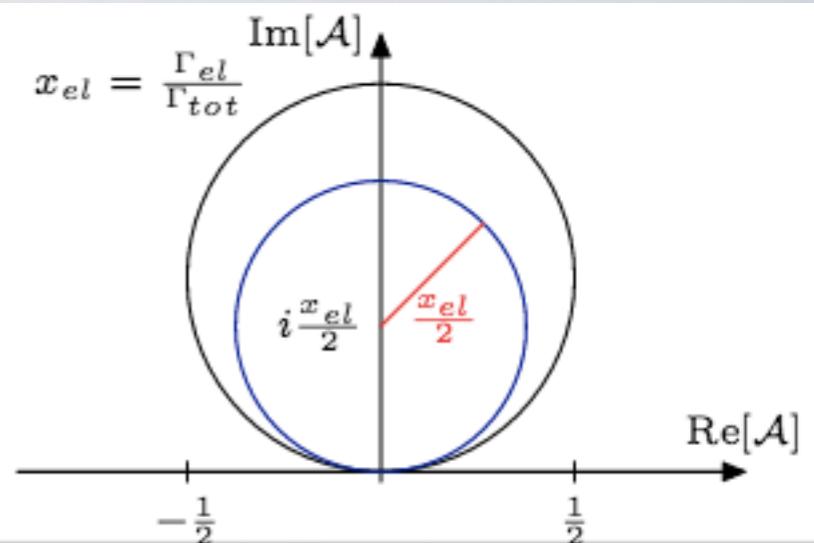
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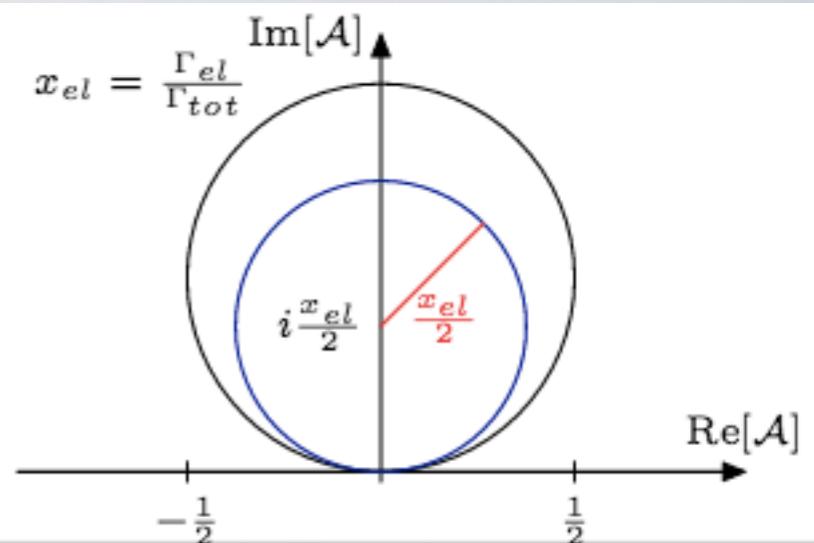
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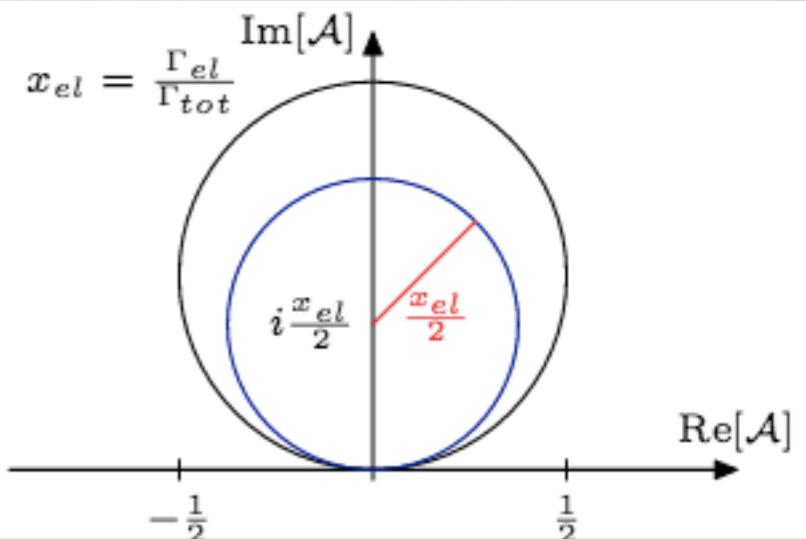
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SM longitudinal isospin eigenamplitudes ($\mathcal{A}_{I,\text{spin}=J}$):

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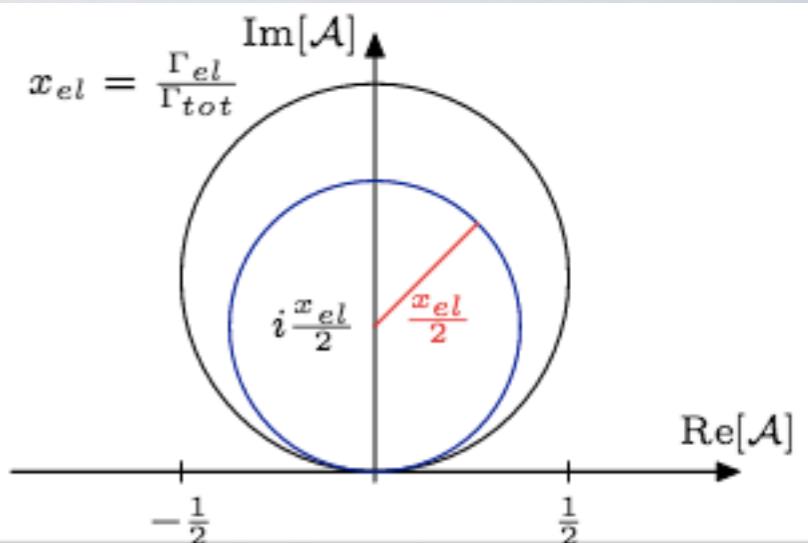
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Lee/Quigg/Thacker, 1973

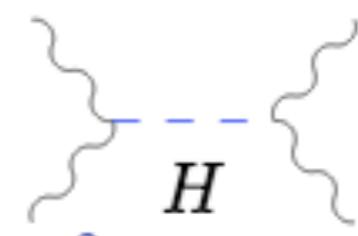
exceeds unitarity bound $|\mathcal{A}_{IJ}| \lesssim \frac{1}{2}$ at:

$$I = 0 : \quad E \sim \sqrt{8\pi}v = 1.2 \text{ TeV}$$

$$I = 1 : \quad E \sim \sqrt{48\pi}v = 3.5 \text{ TeV}$$

$$I = 2 : \quad E \sim \sqrt{16\pi}v = 1.7 \text{ TeV}$$

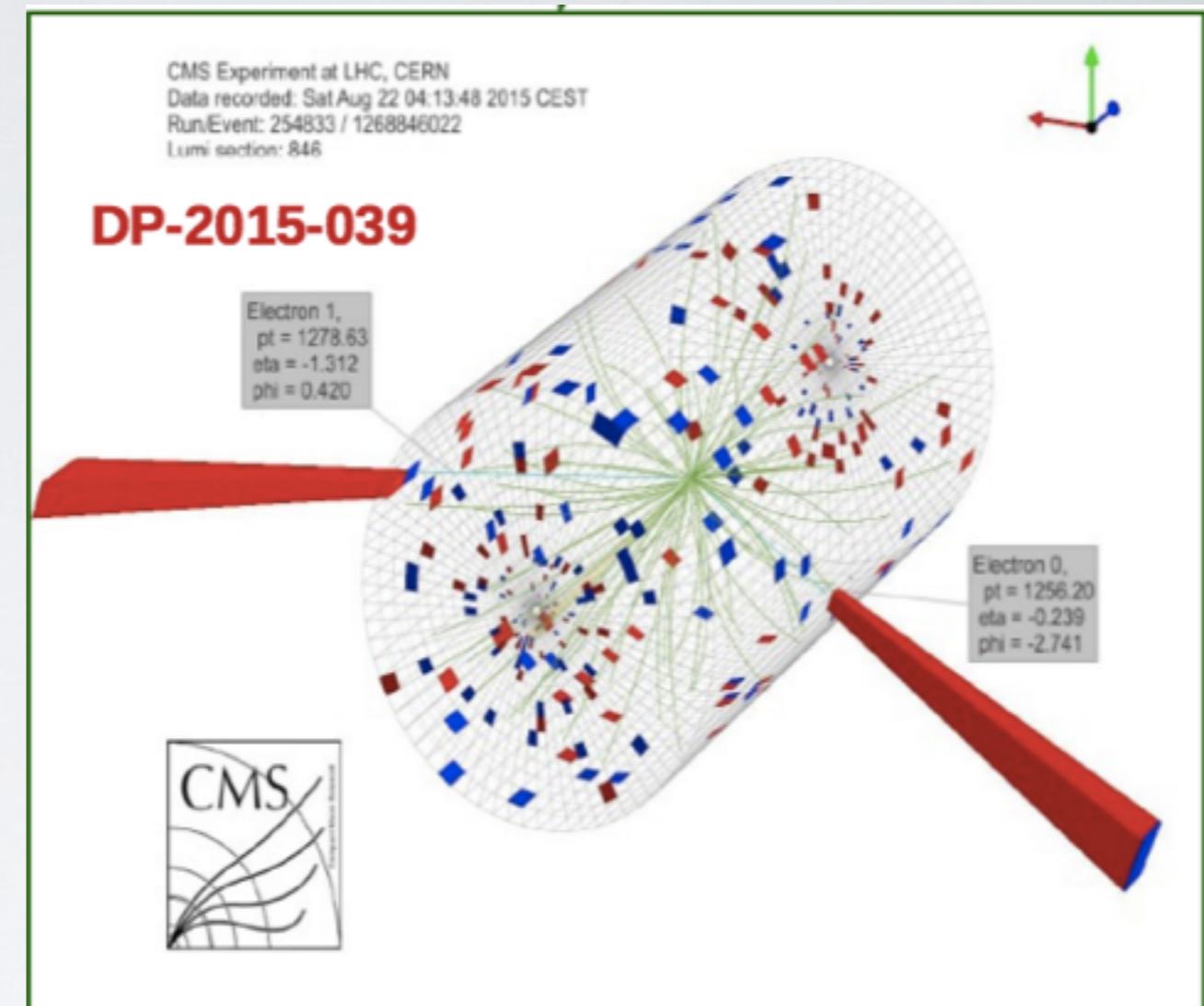
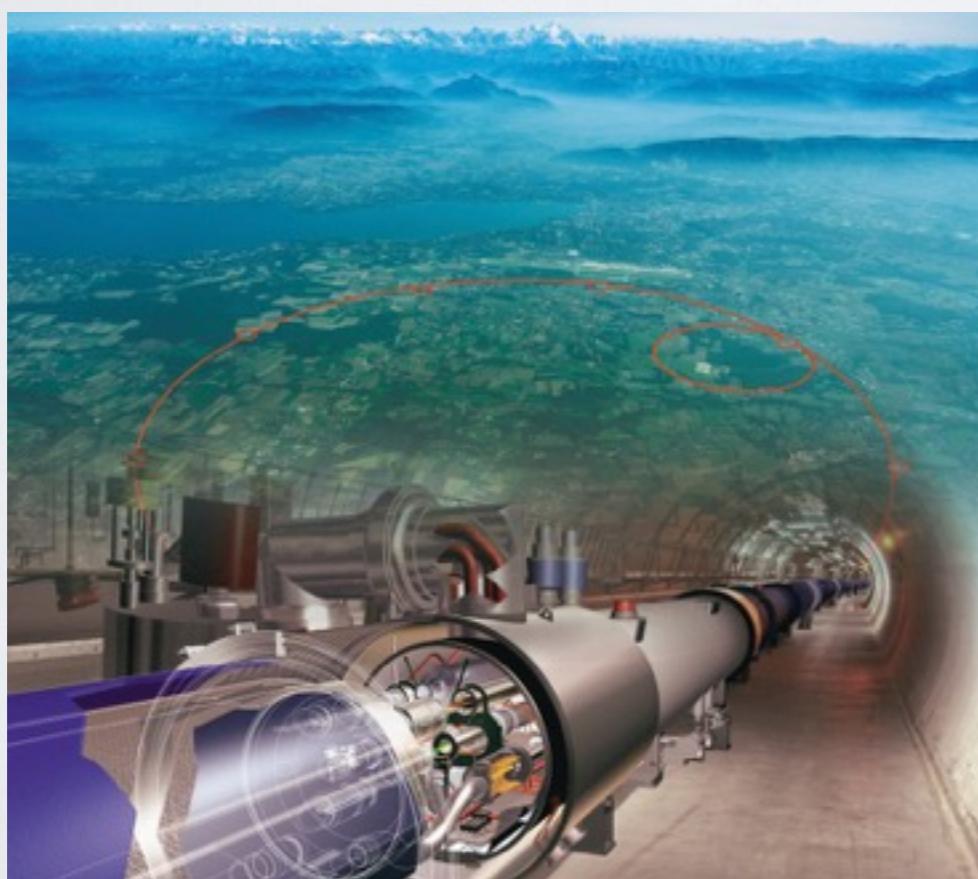
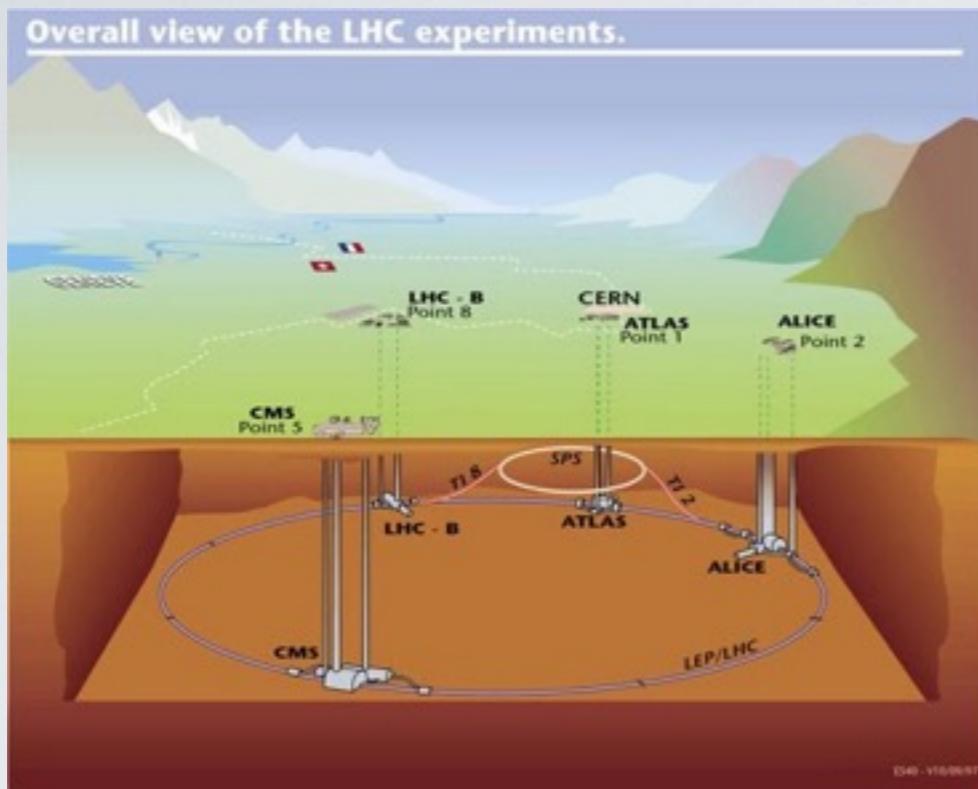
Higgs exchange:



$$\mathcal{A}(s, t, u) = -\frac{M_H^2}{v^2} \frac{s}{s - M_H^2}$$

Unitarity: $M_H \lesssim \sqrt{8\pi}v \sim 1.2 \text{ TeV}$

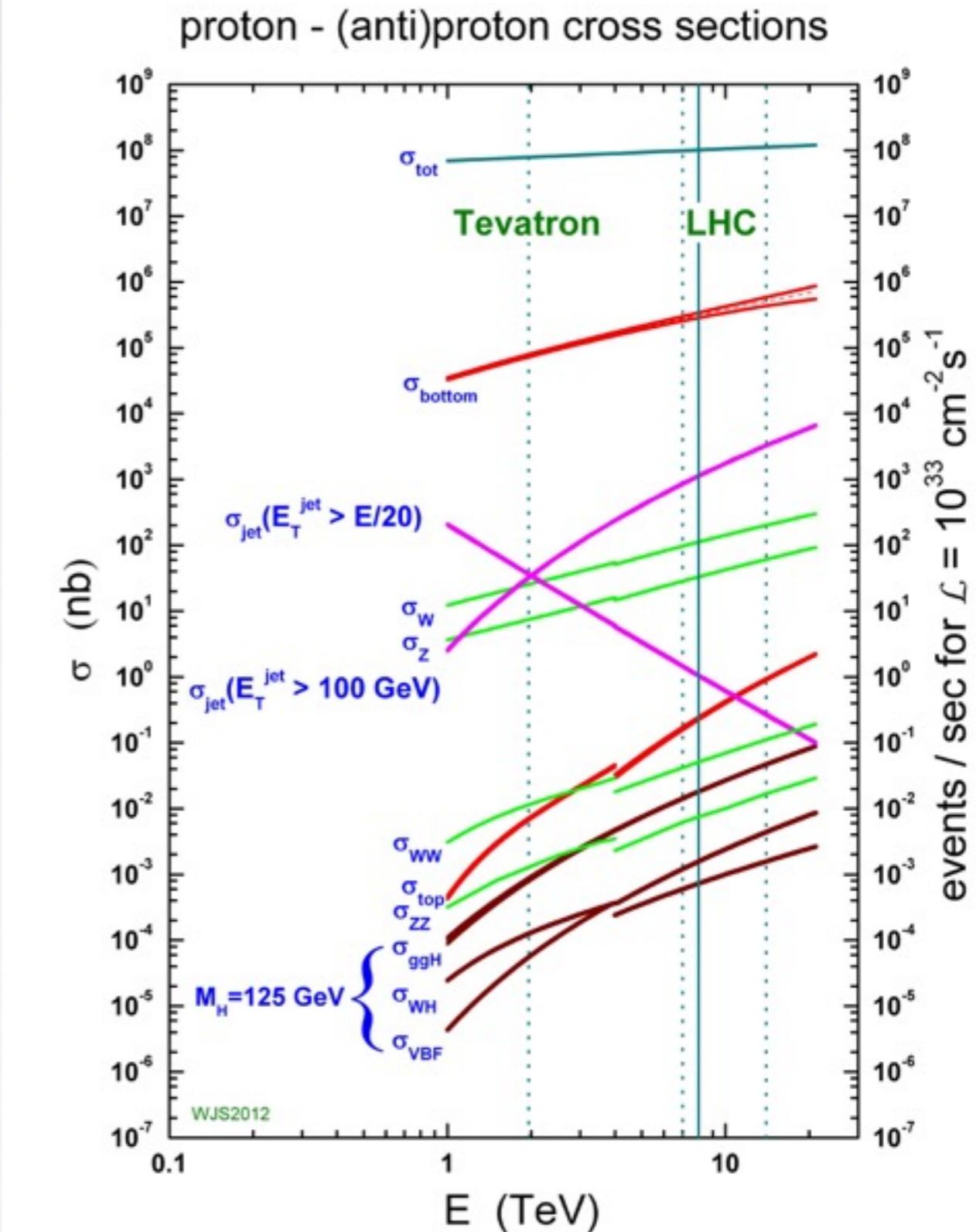
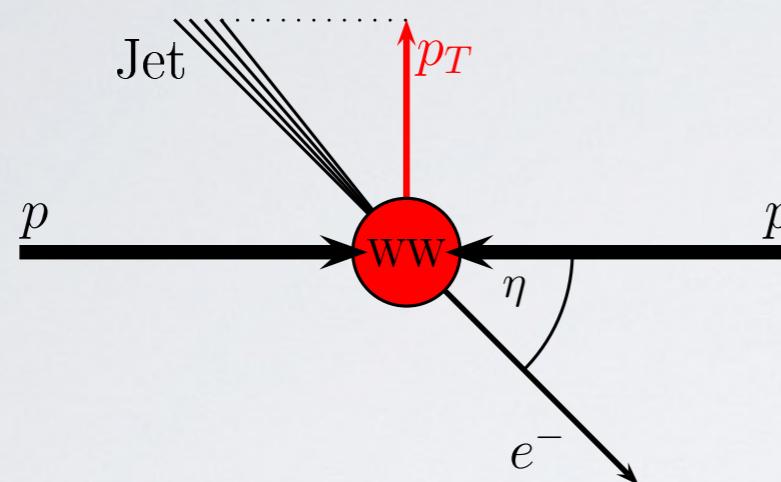
The Challenge of the Large Hadron Collider



CMS Run II event: $M(ee) = 2.9 \text{ TeV}$

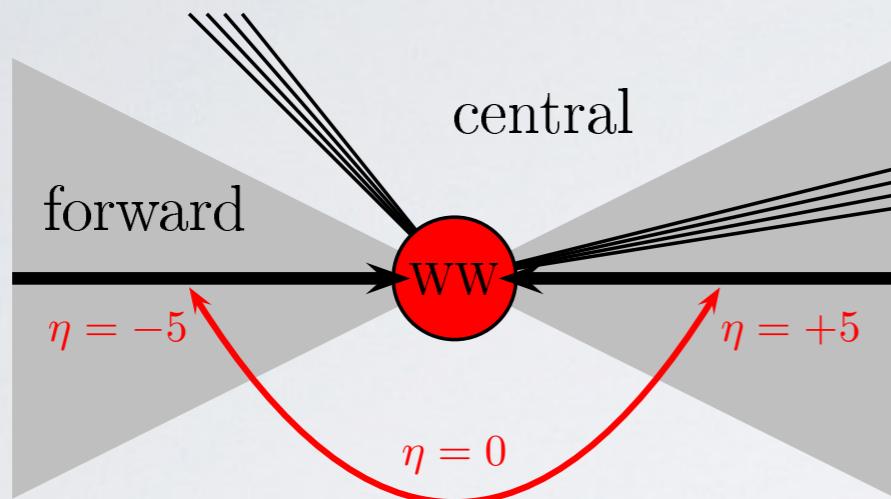
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- Different partonic subprocesses: qq , qg , gg
- No fixed partonic energy

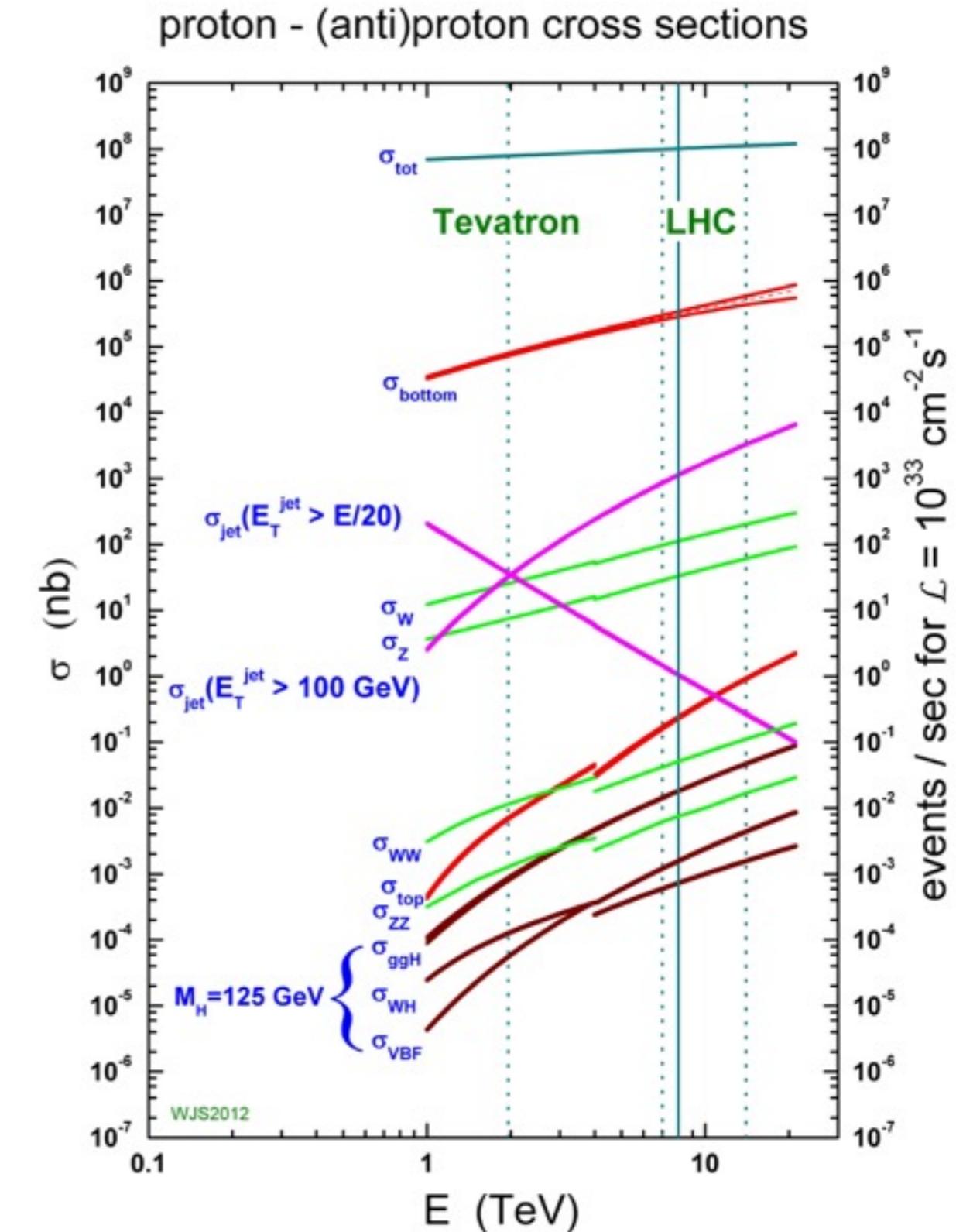


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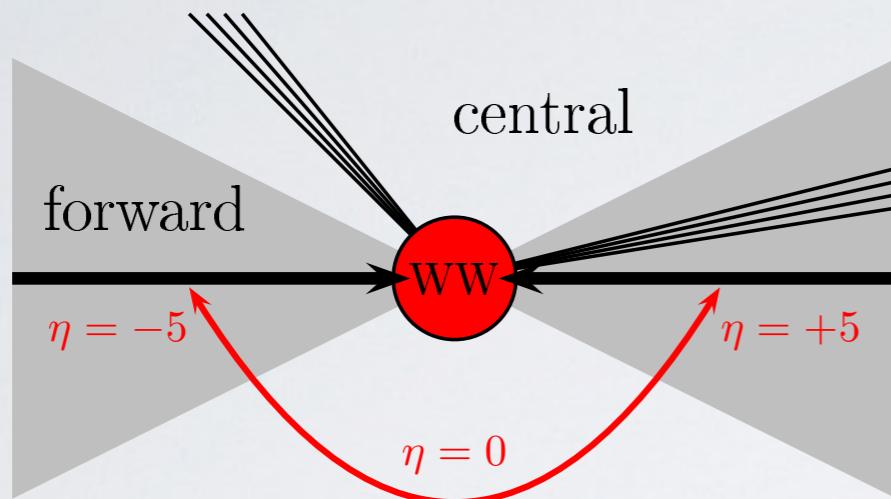


- Luminosity: $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- Huge rates for jets, bottom, tops
- 6,000,000 bottoms / sec
- Need for hard- and software trigger



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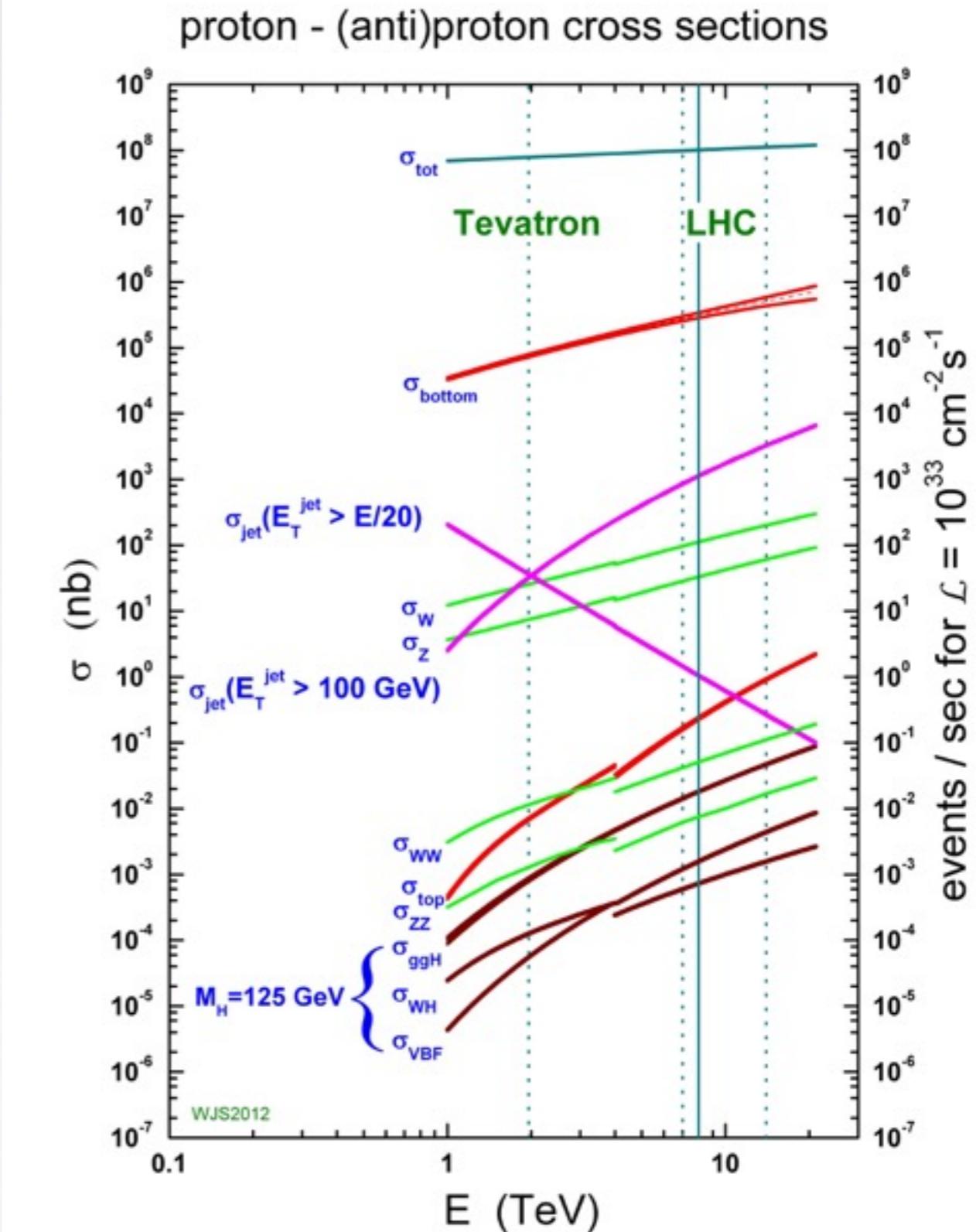


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S. Weinberg:

“To find something interesting at the LHC is like you would like to find out for what a single dollar in the U.S. federal budget has been spent for.”



The Higgs boson discovery

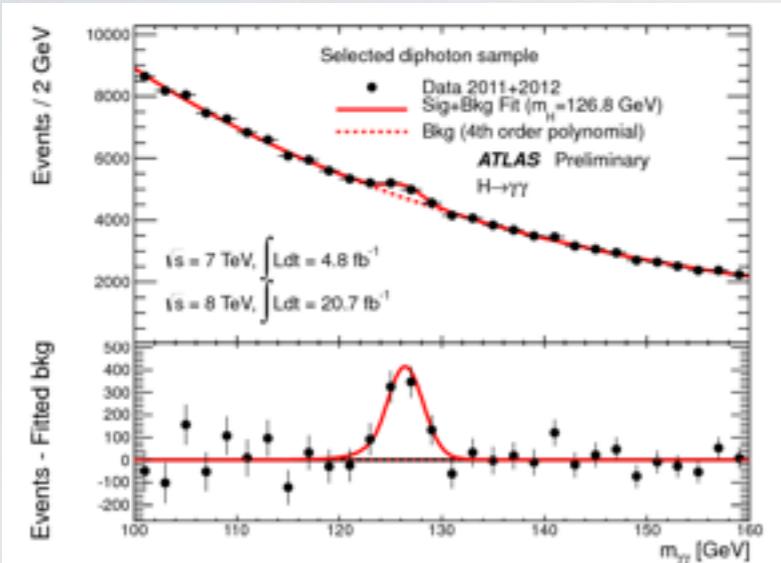
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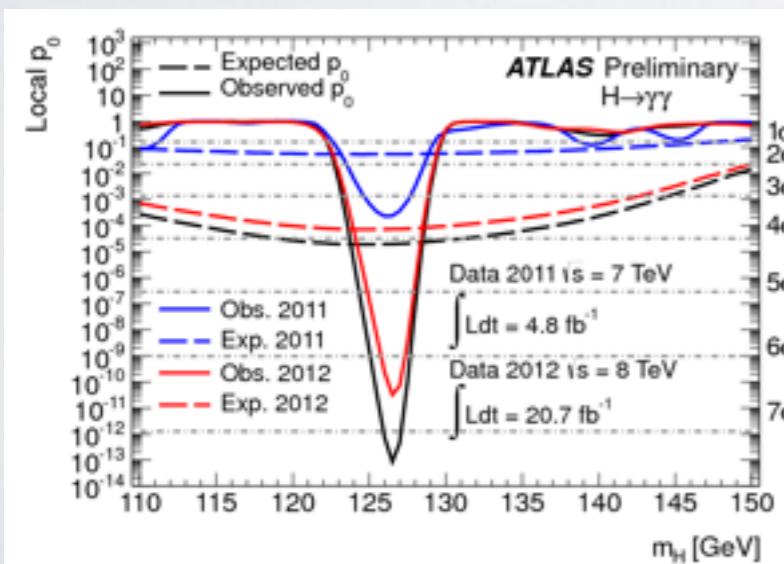
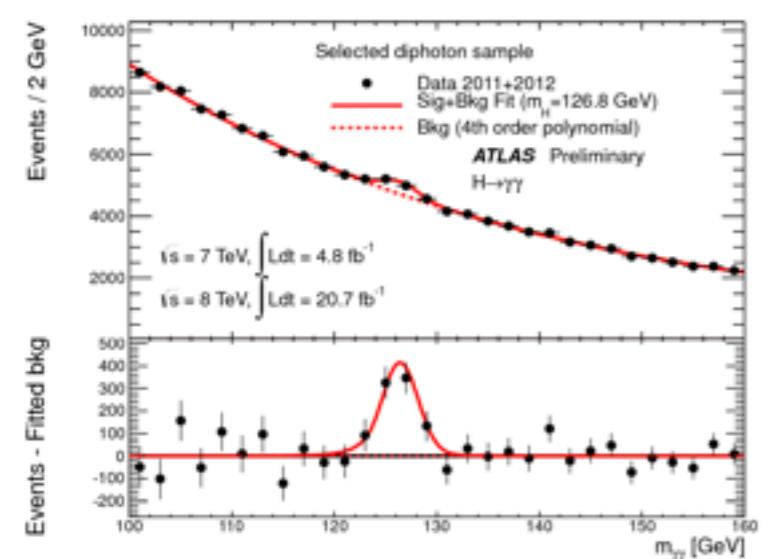
$$pp \rightarrow H \rightarrow \gamma\gamma$$



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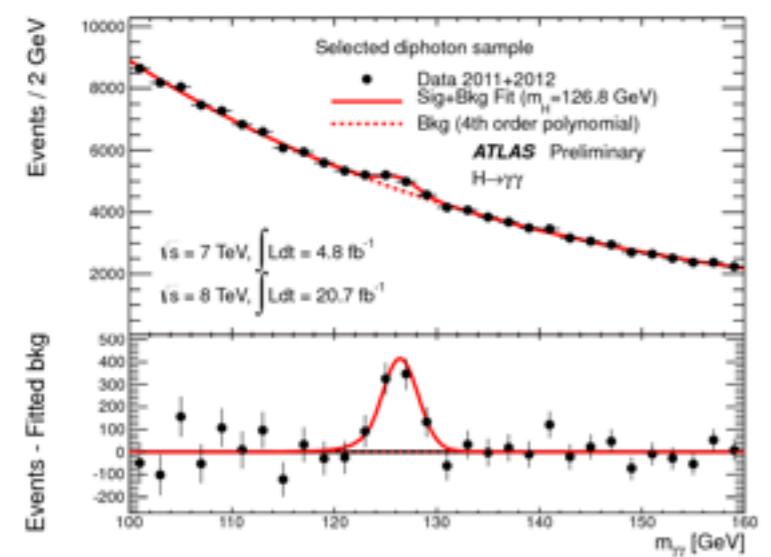
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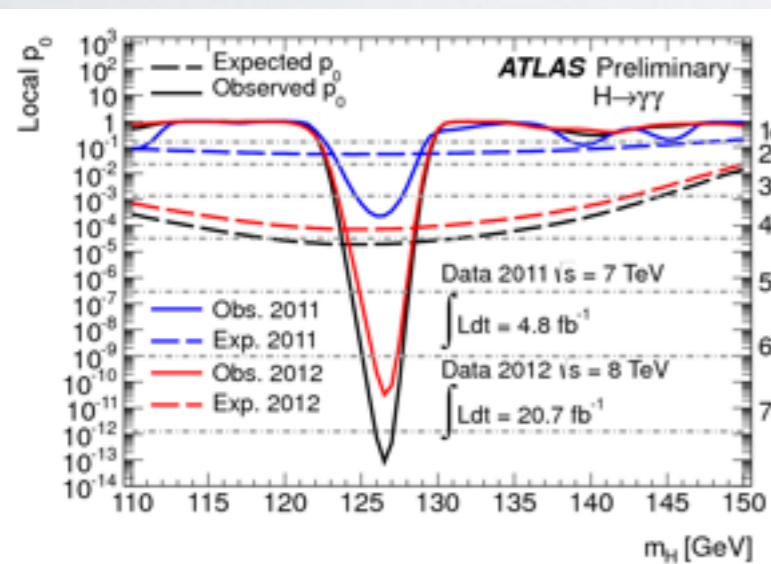
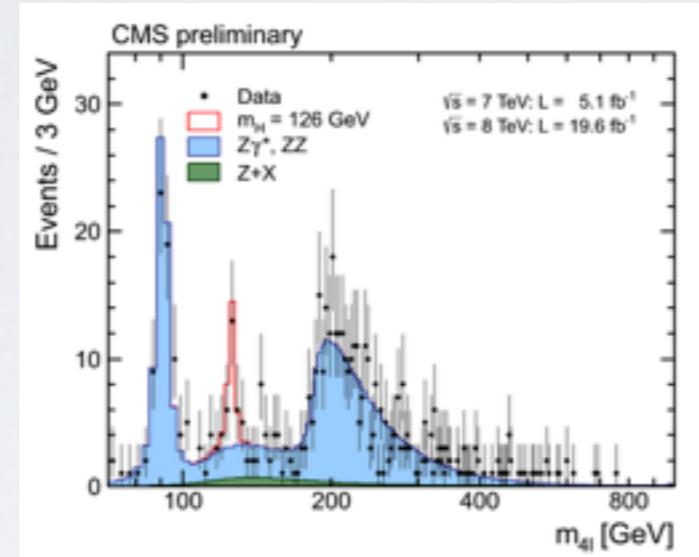
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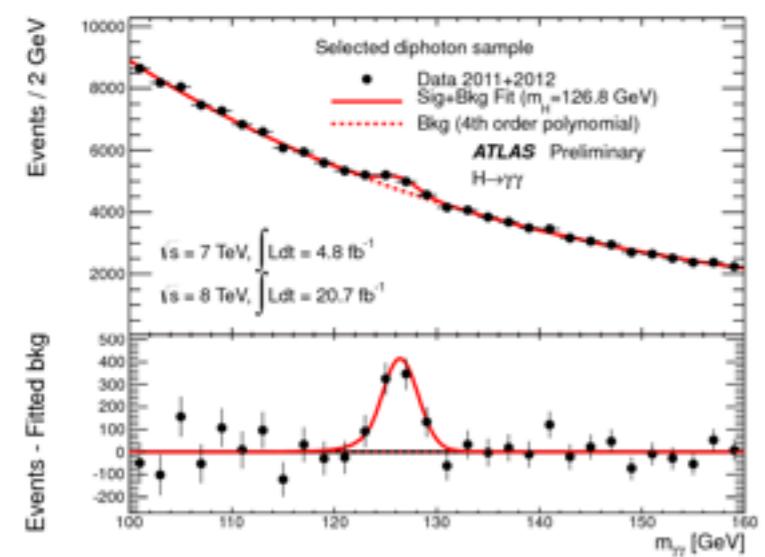
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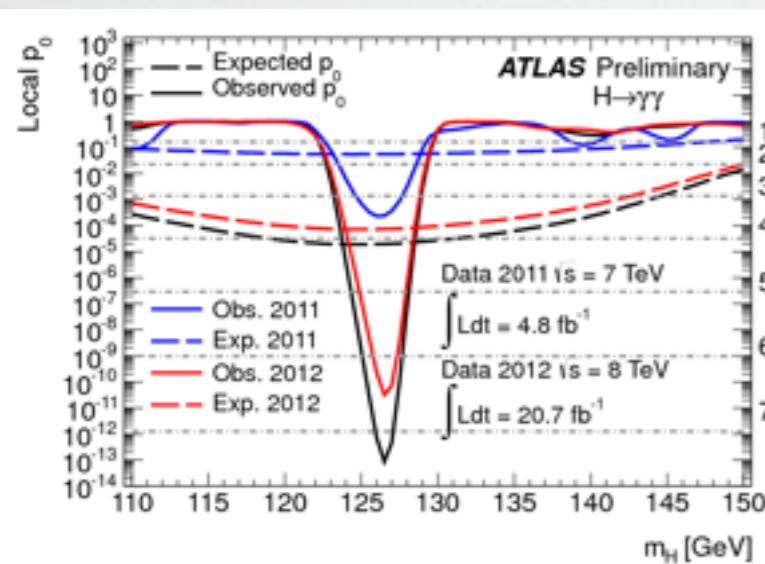
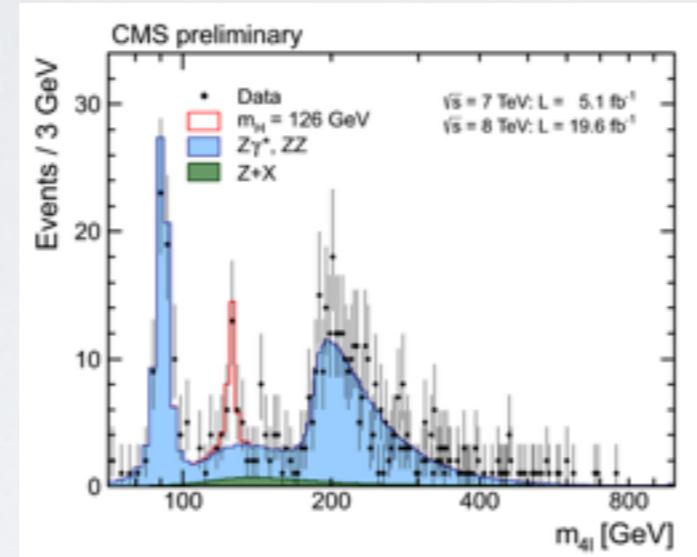
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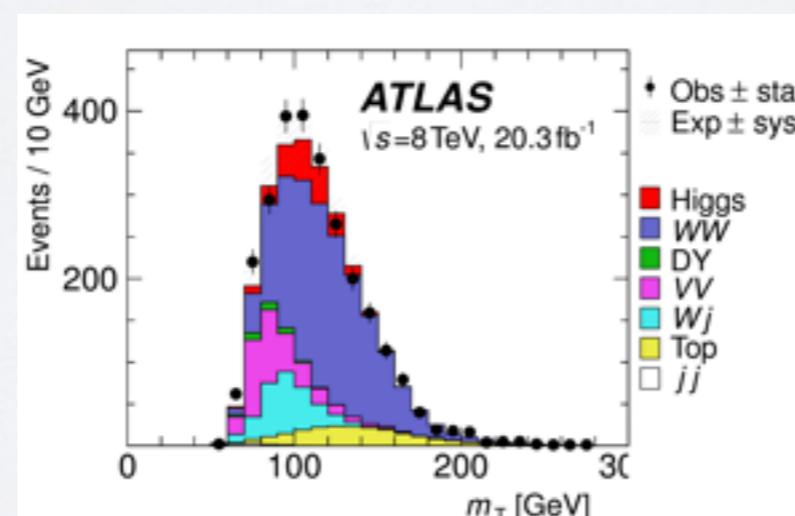
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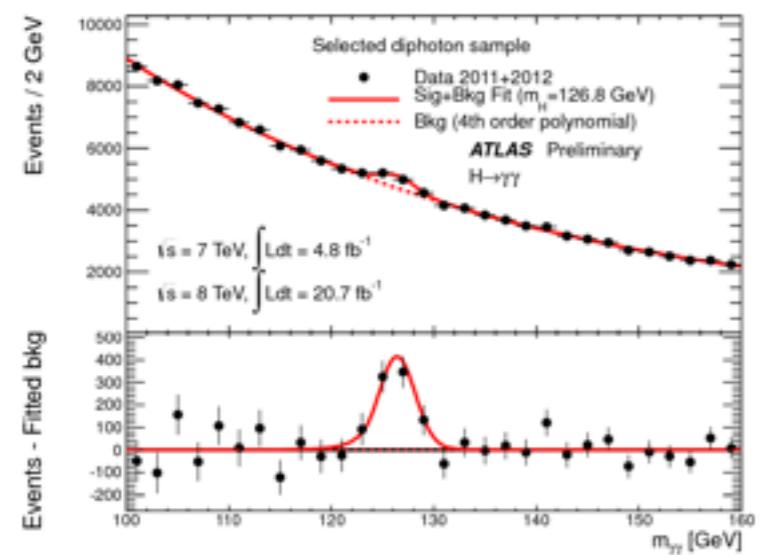
$pp \rightarrow H \rightarrow WW^* \rightarrow \ell\nu\ell\nu$



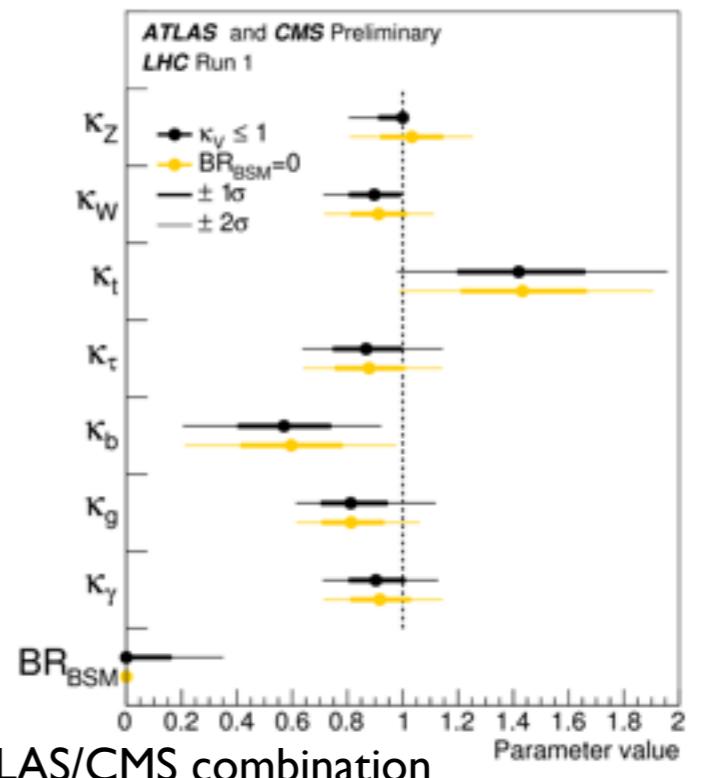
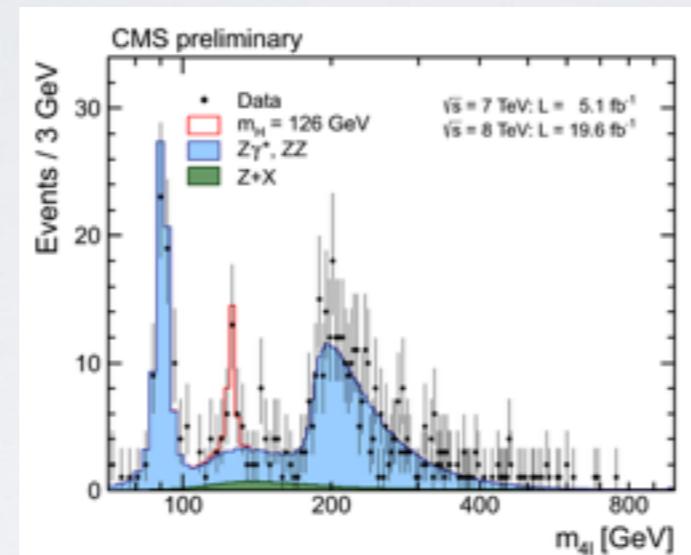
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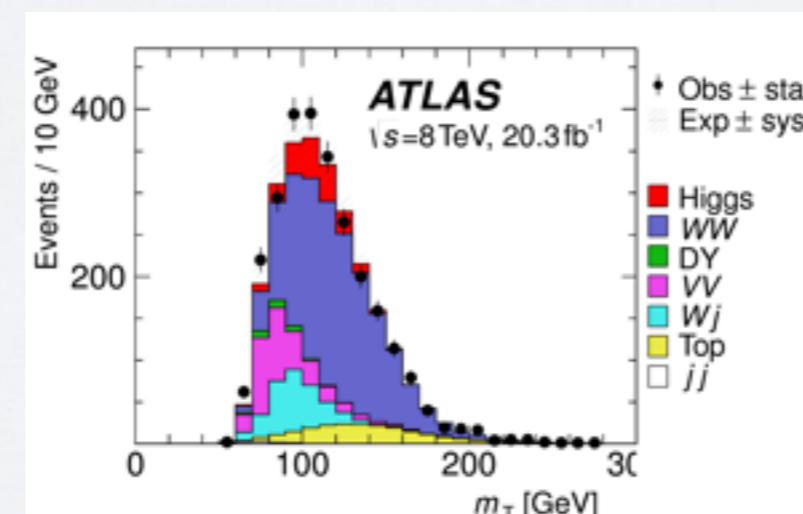
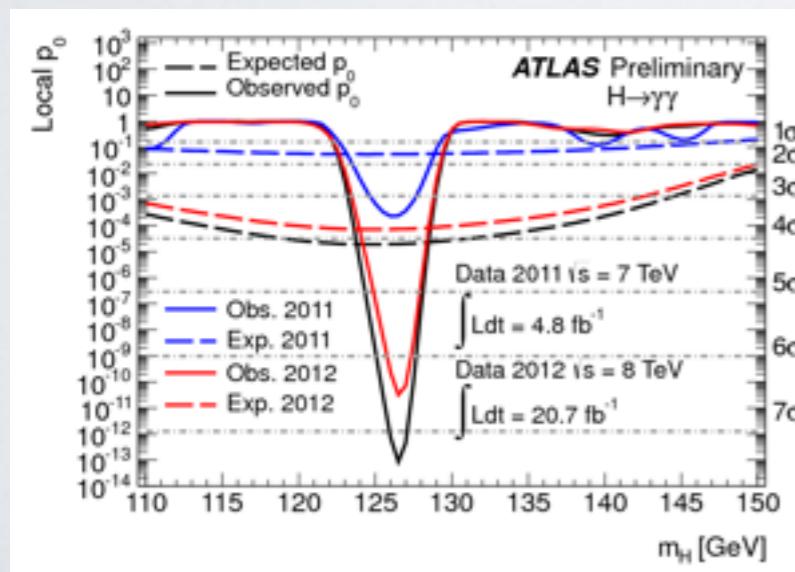
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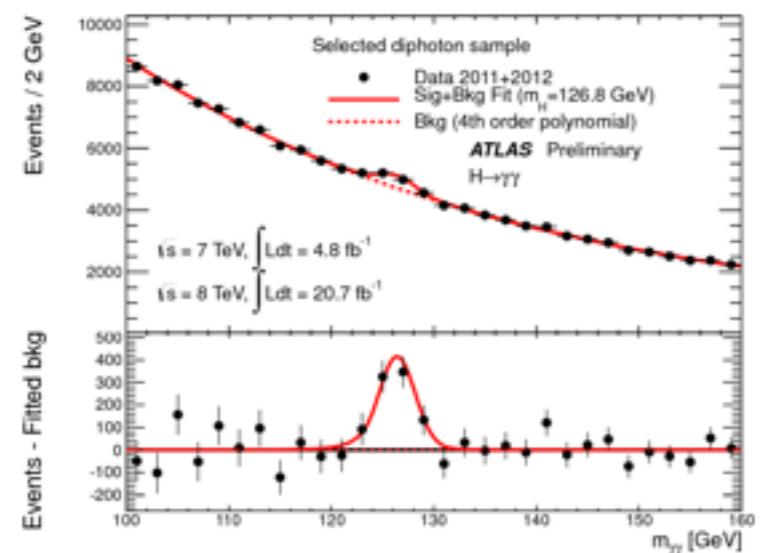
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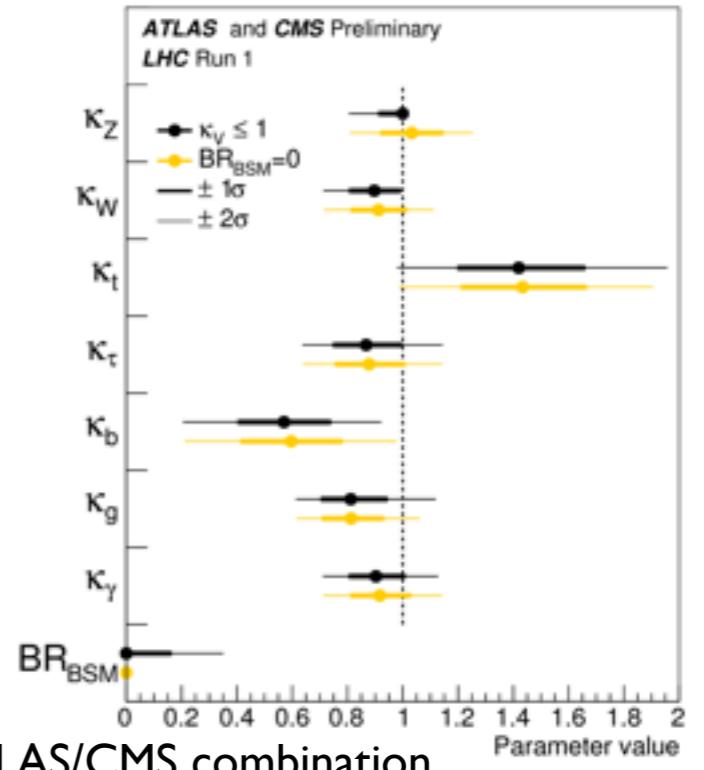
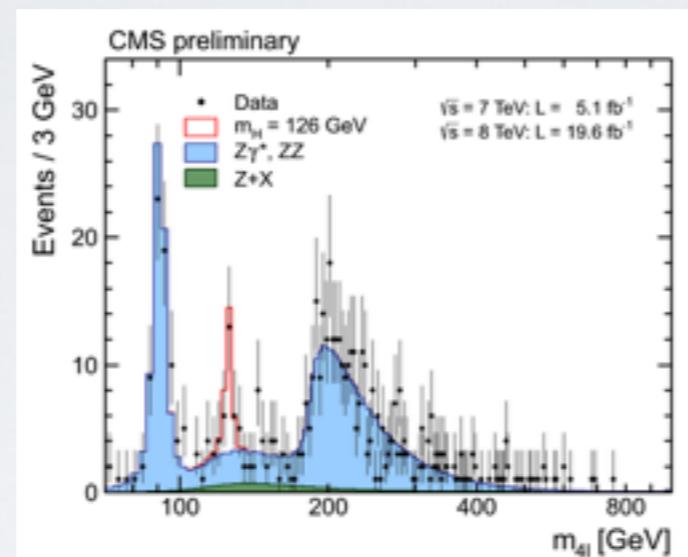
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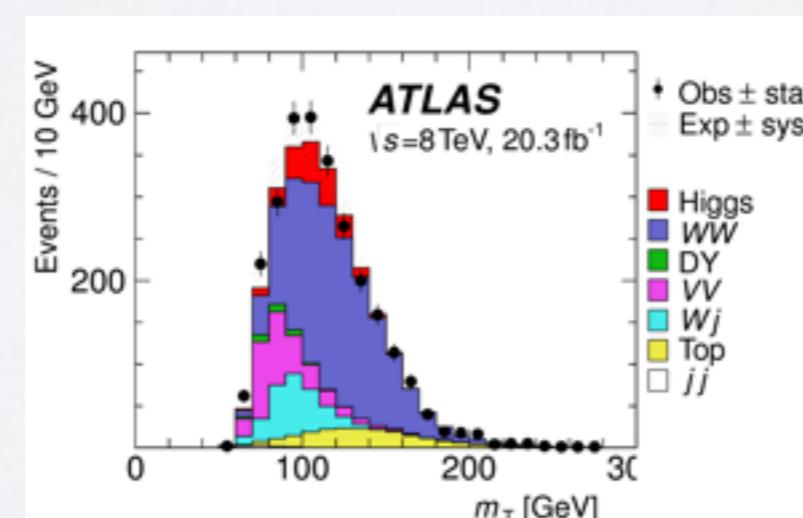
$pp \rightarrow H \rightarrow \gamma\gamma$



$pp \rightarrow H \rightarrow ZZ^* \rightarrow \ell\ell\ell\ell$



$pp \rightarrow H \rightarrow WW^* \rightarrow \ell\nu\ell\nu$

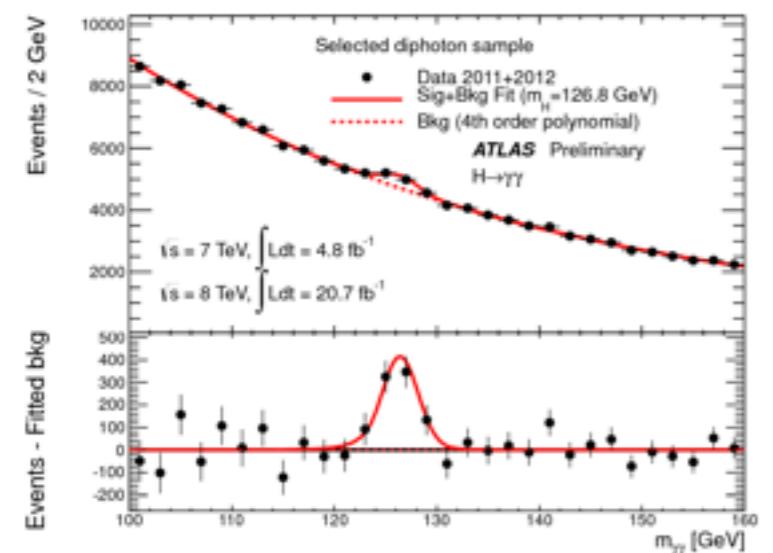


What's the most important radiative correction for LHC physics?

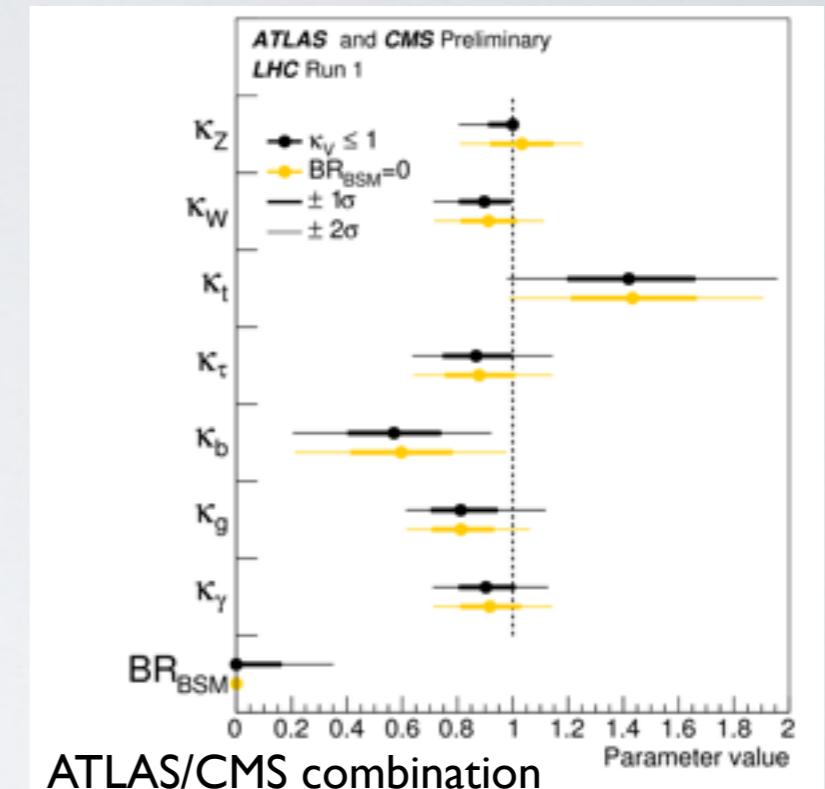
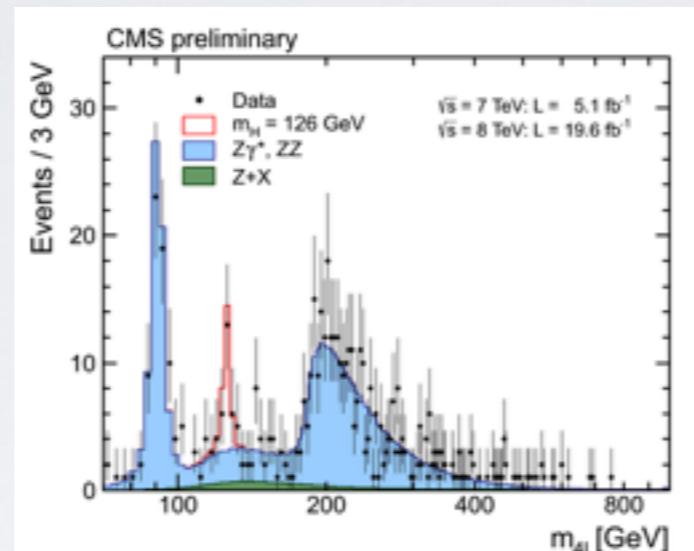
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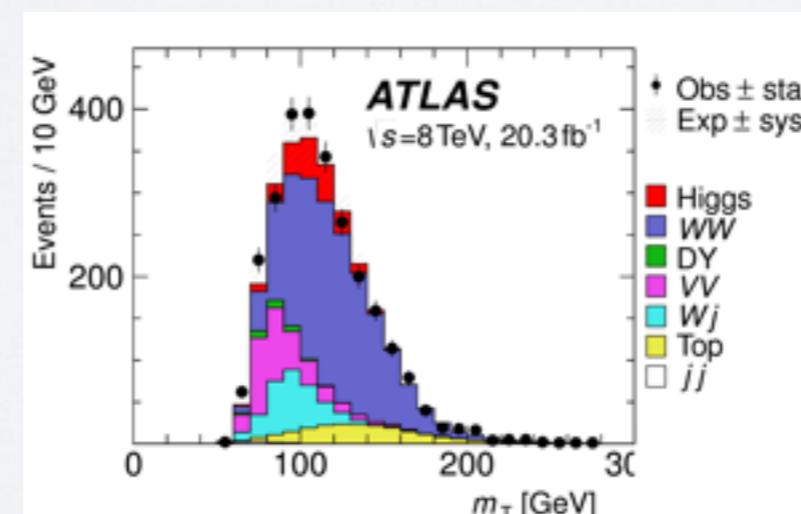
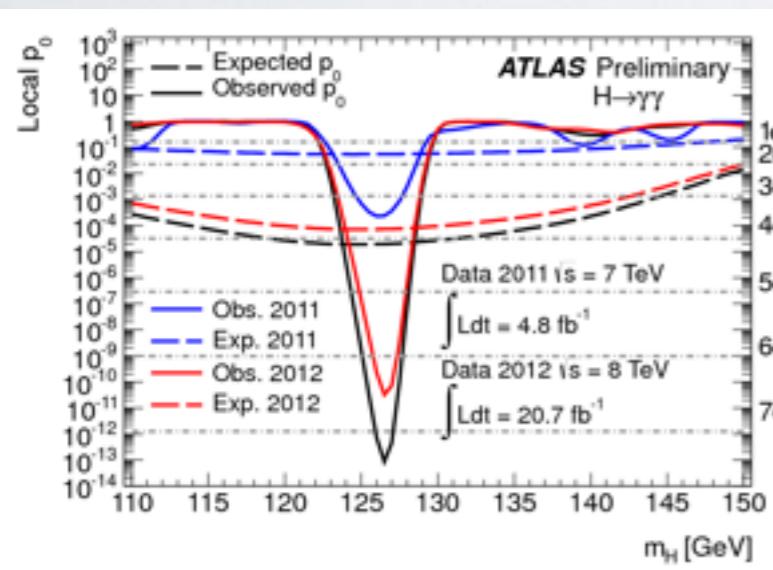
$pp \rightarrow H \rightarrow \gamma\gamma$



$pp \rightarrow H \rightarrow ZZ^* \rightarrow llll$



$pp \rightarrow H \rightarrow WW^* \rightarrow l\nu l\nu$



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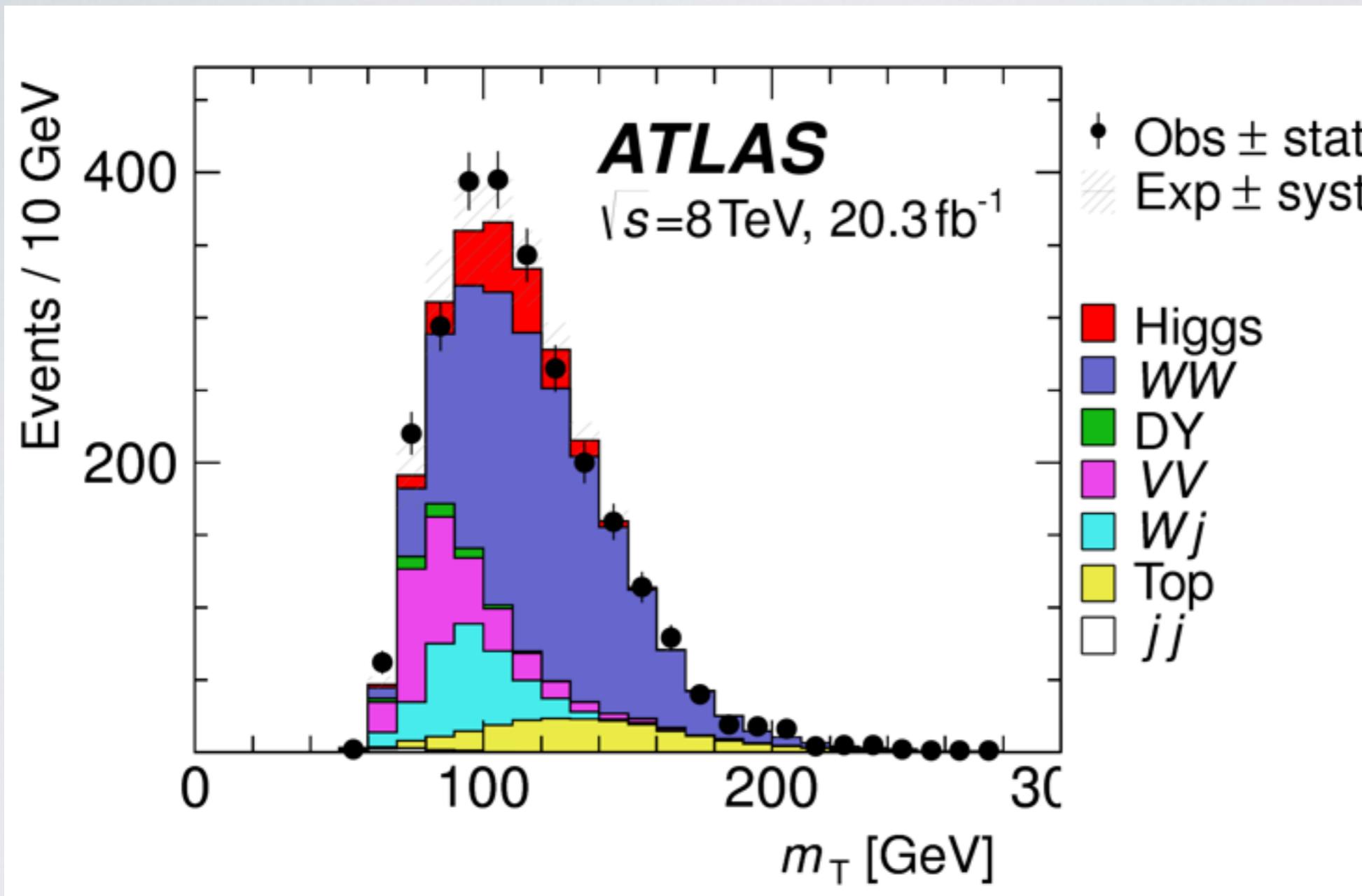
$$\boxed{\Gamma_{bb}} \implies \text{BR}(H \rightarrow bb) : 95\% \rightarrow 57\%$$

for the $\phi^\circ \rightarrow b\bar{b}$ width. QCD corrections have been computed with the result that in the $m_{\phi^\circ} > 40$ GeV mass range, $\Gamma(\phi^\circ \rightarrow b\bar{b}) \sim \frac{1}{2}\Gamma_0(\phi^\circ \rightarrow b\bar{b})$. Thus, in our studies we may be erring on the conservative side.

J. Gunion, SSC status, 1989

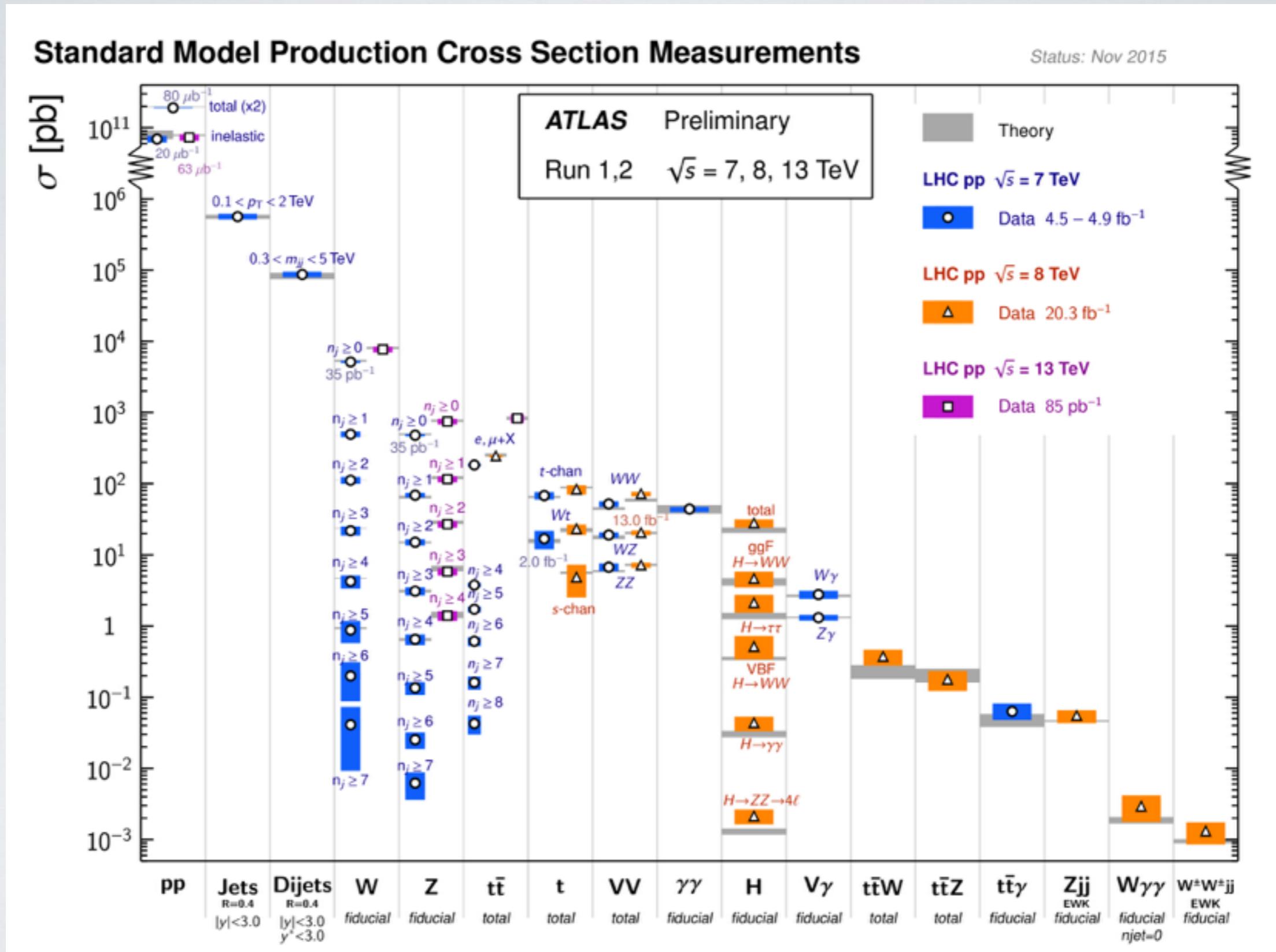


The shiny result revisited: ...

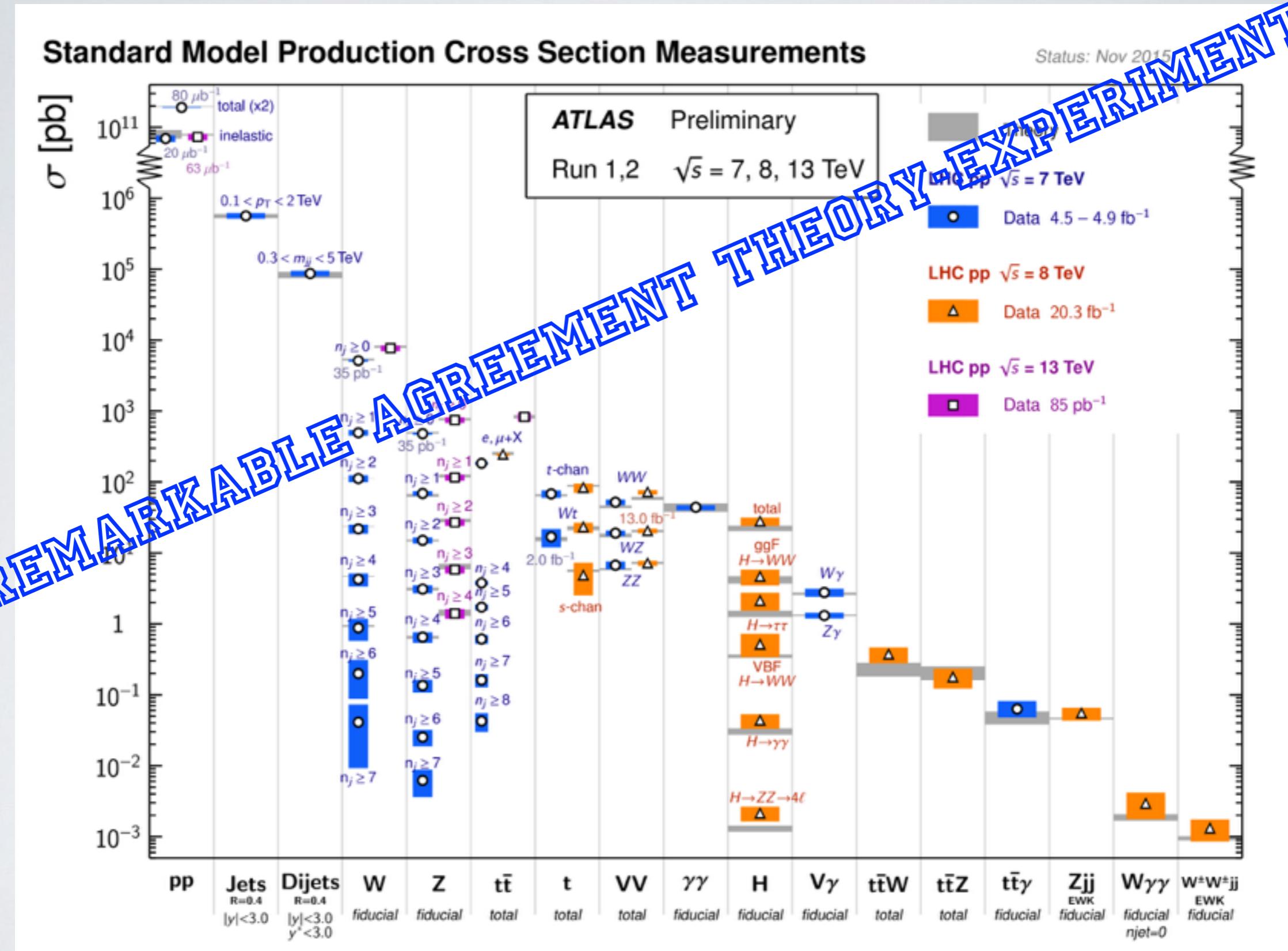


Many different channels must be known to very high precision in order to detect the signal !!!

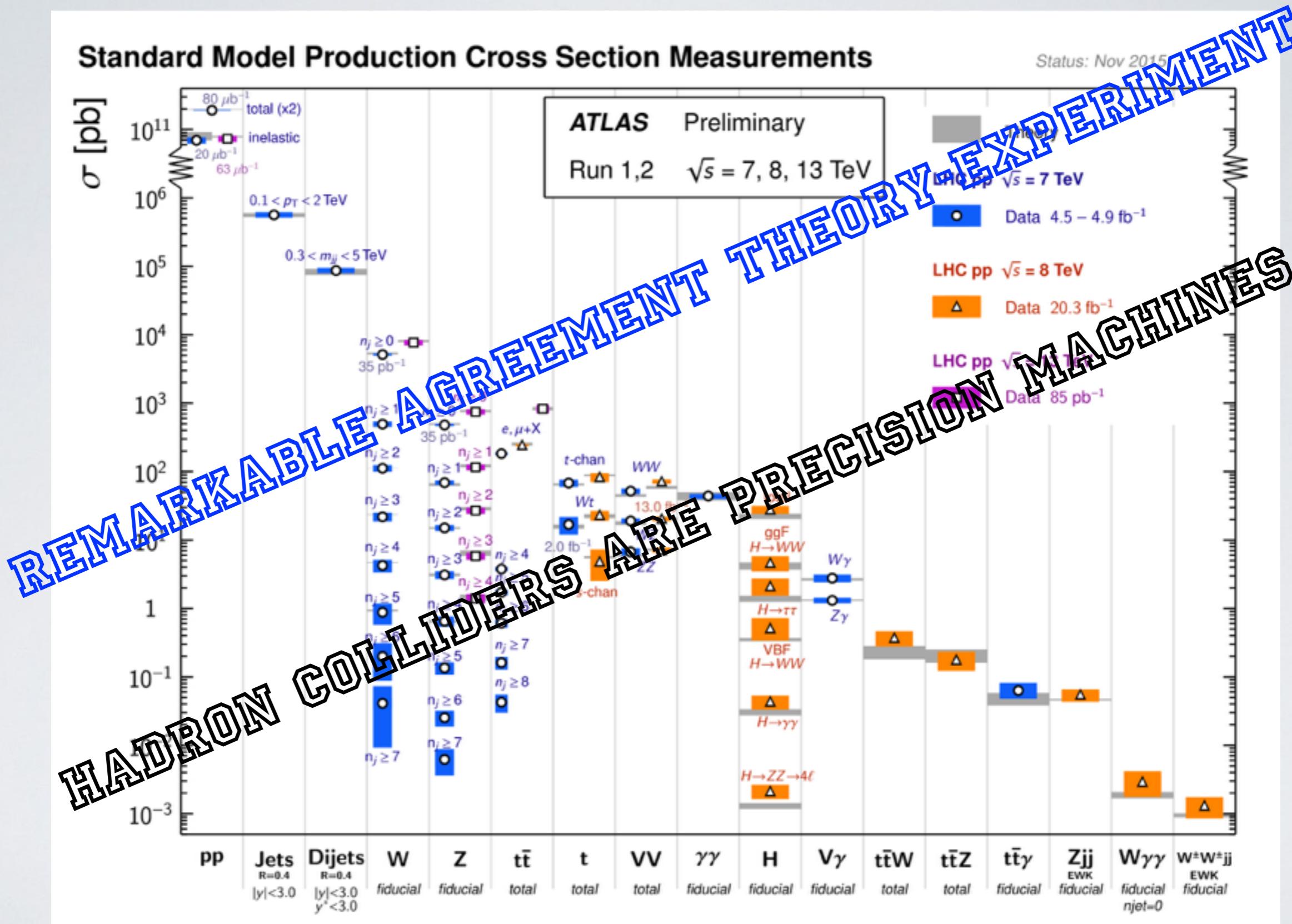
What goes into theory prediction?



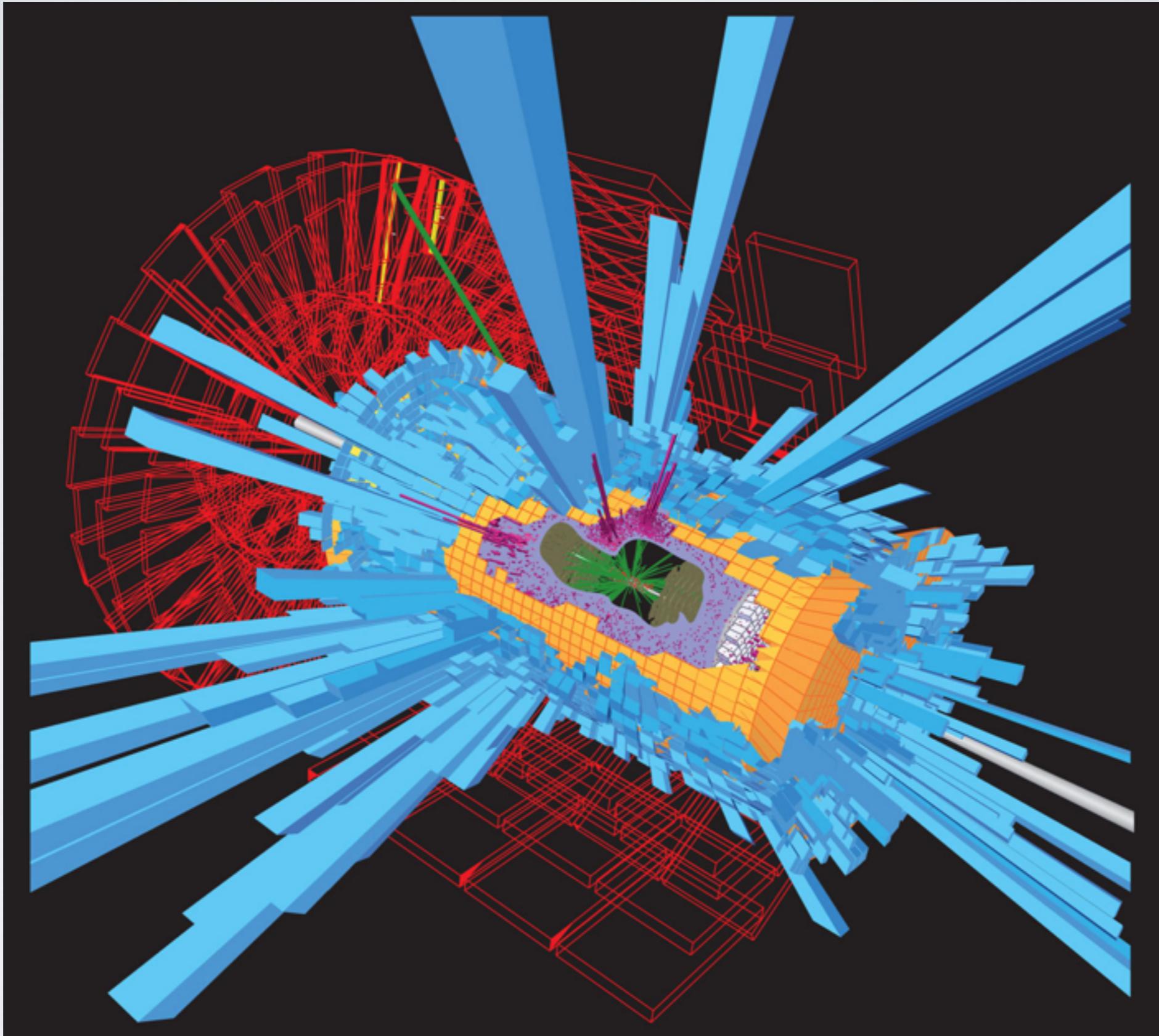
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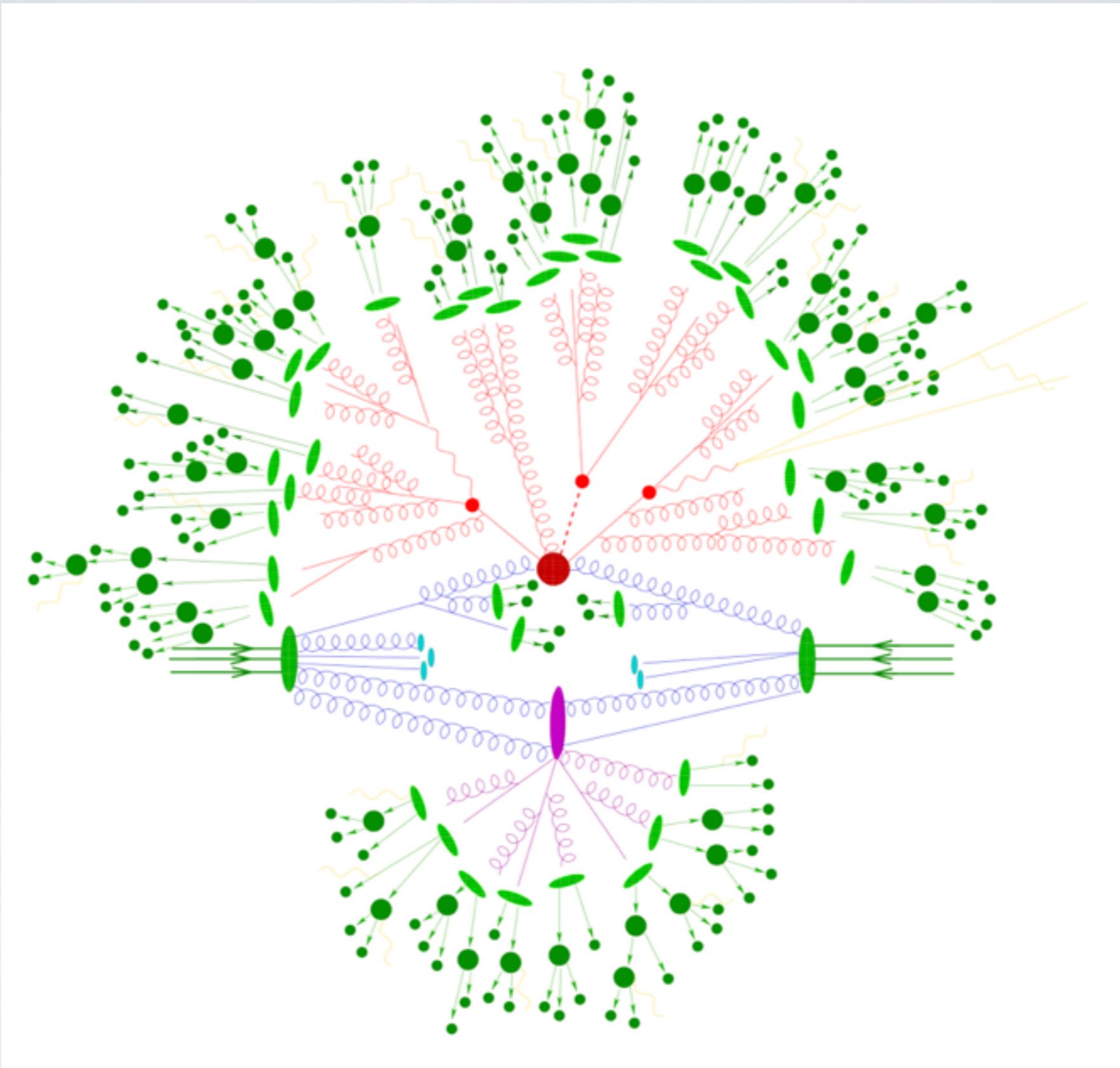
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Events at hadron colliders ... Experiment

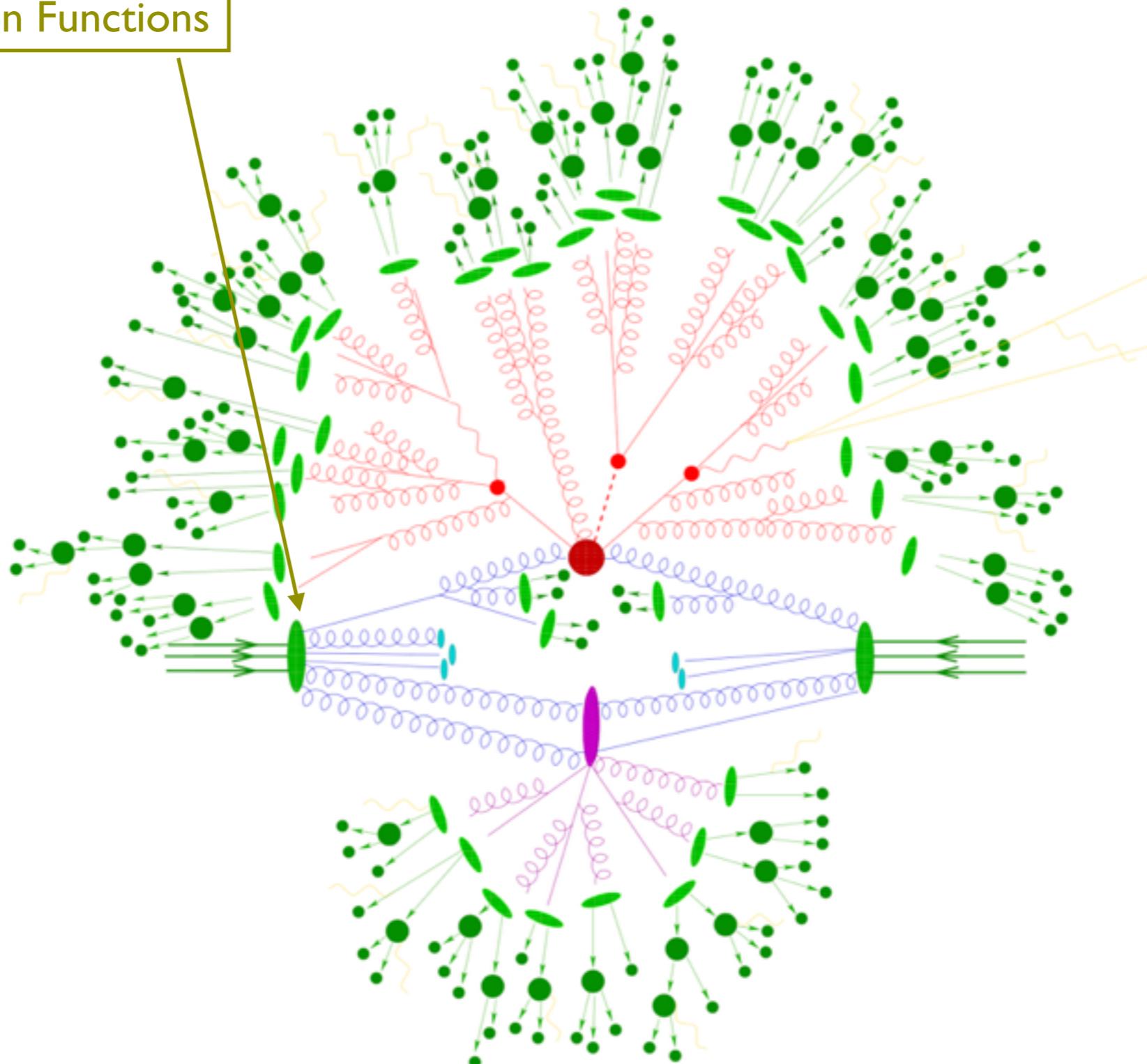


Events at hadron colliders ... Theory



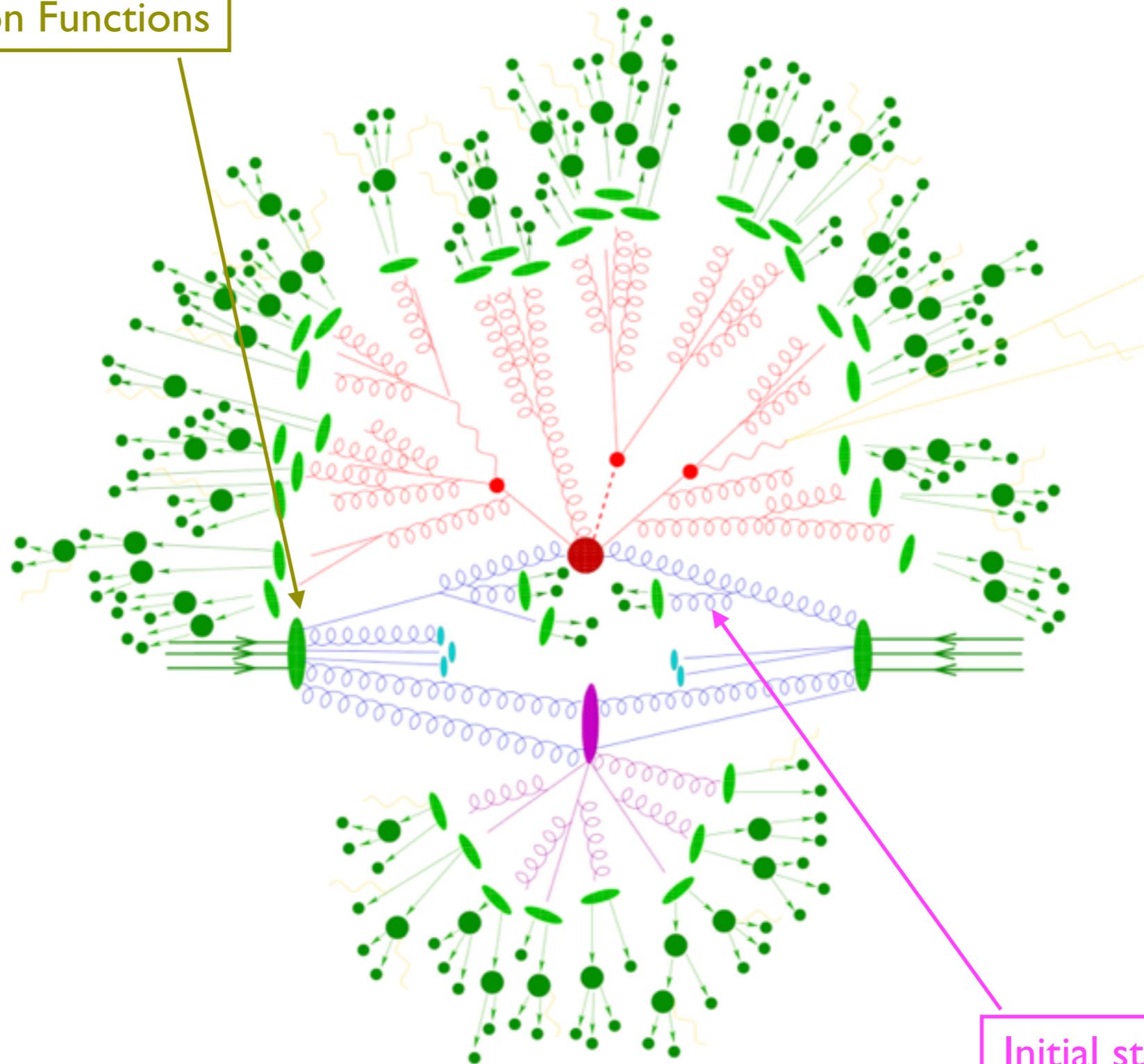
Events at hadron colliders ... Theory

Parton Distribution Functions



Events at hadron colliders ... Theory

Parton Distribution Functions



Initial state QCD radiation

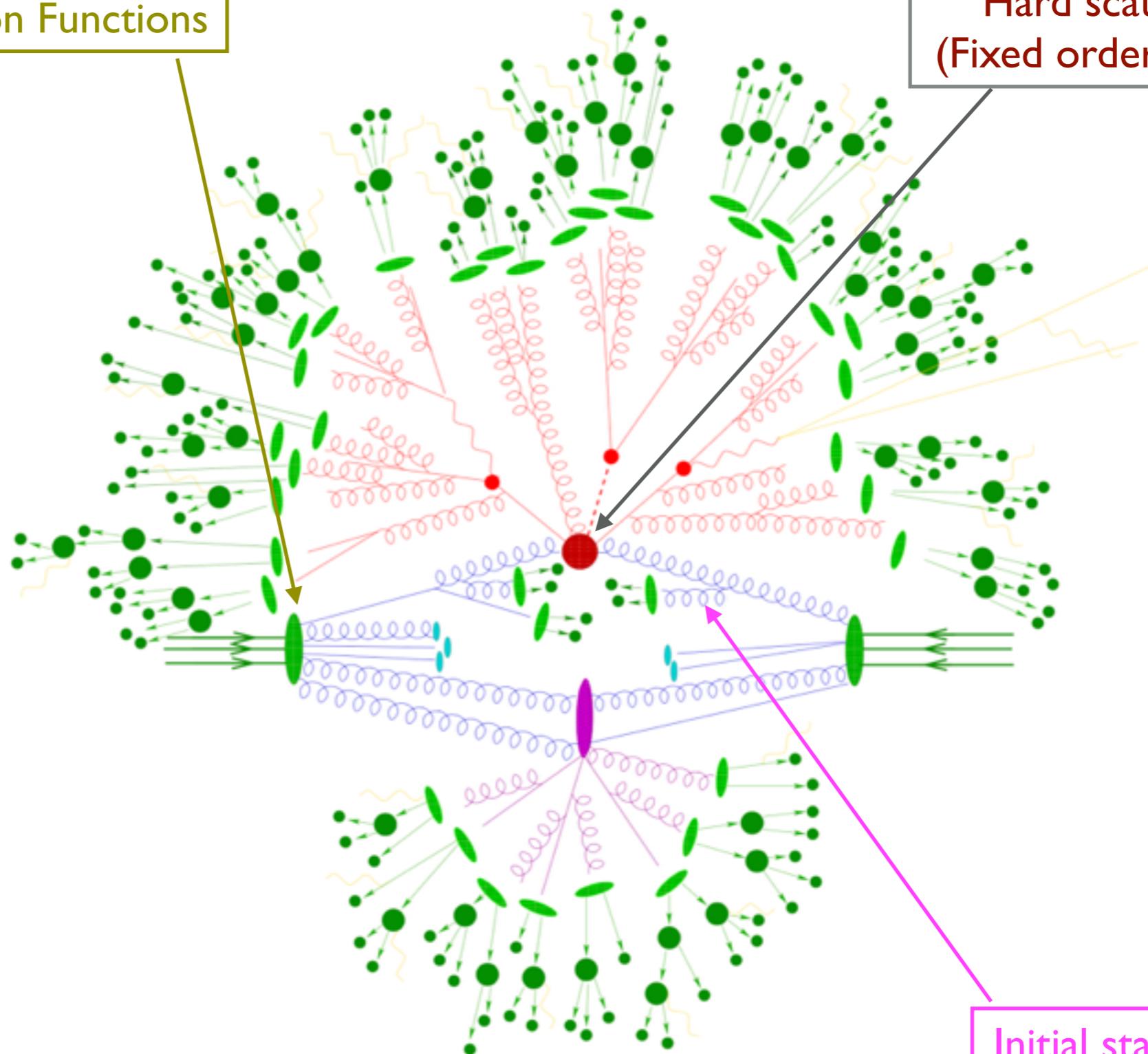


Events at hadron colliders ... Theory

Parton Distribution Functions

Hard scattering process
(Fixed order + resummation)

Initial state QCD radiation



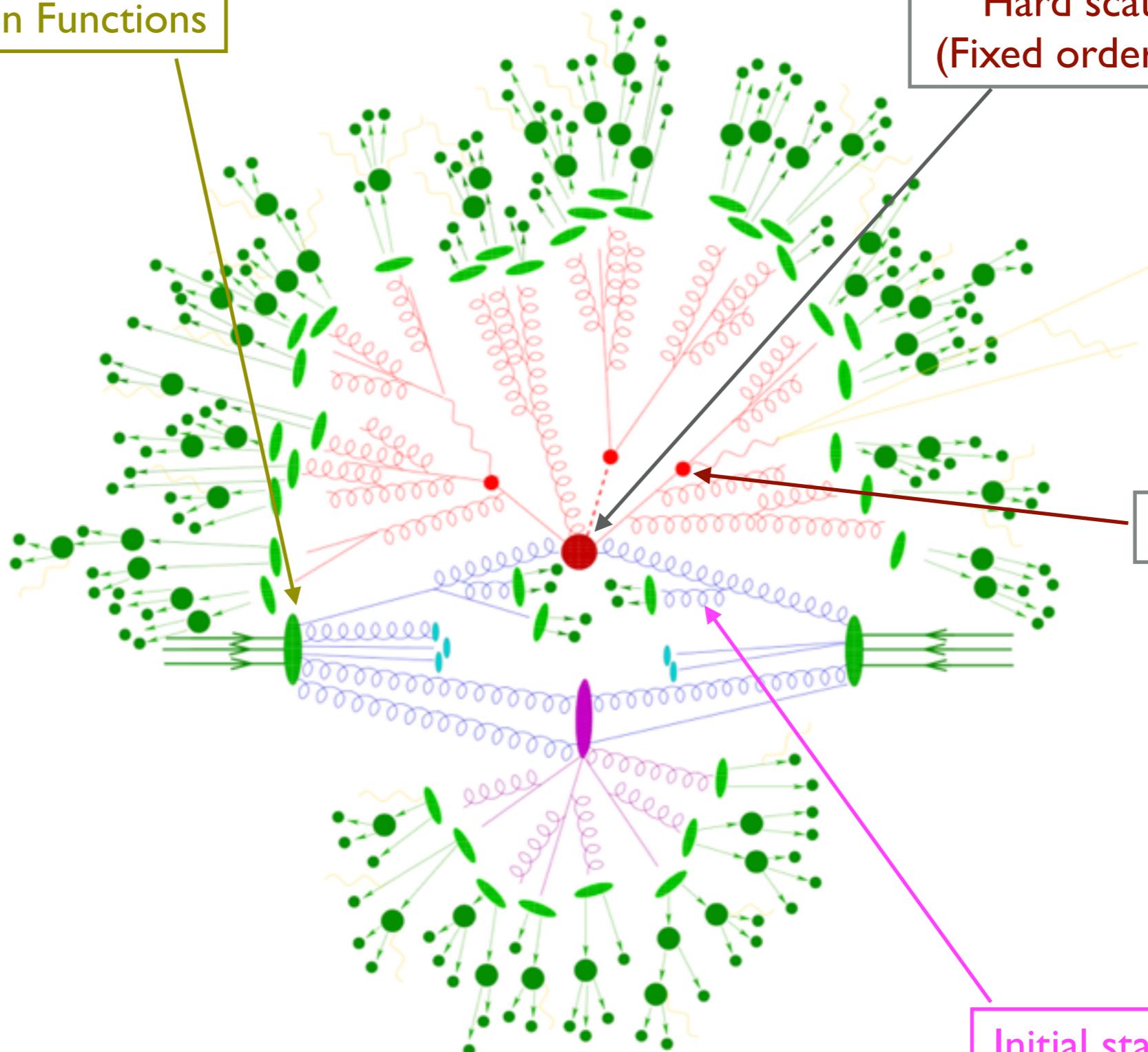
Events at hadron colliders ... Theory

Parton Distribution Functions

Hard scattering process
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Final state decays

Initial state QCD radiation



Events at hadron colliders ... Theory

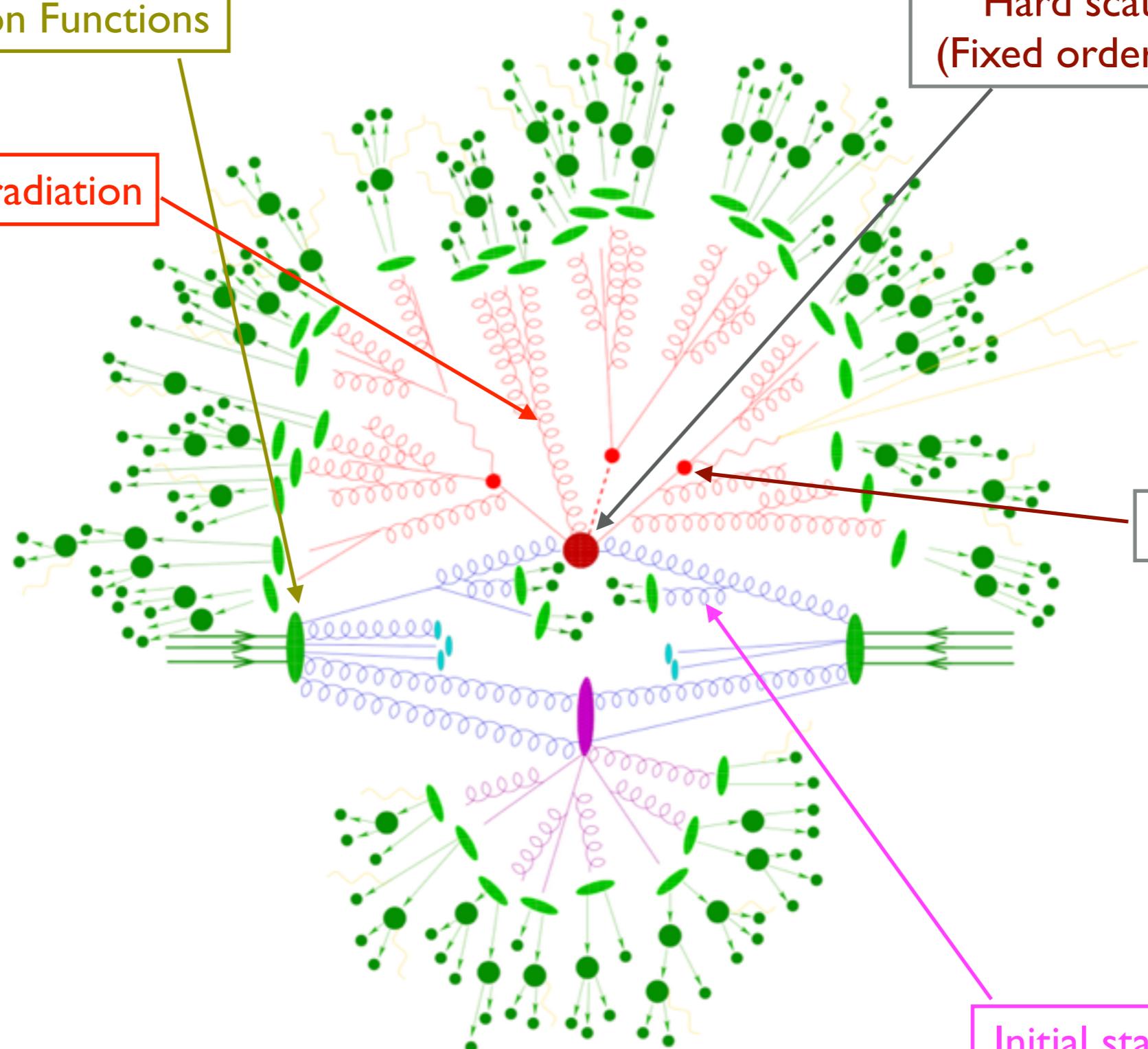
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Final state QCD radiation

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Initial state QCD radiation



Events at hadron colliders ... Theory

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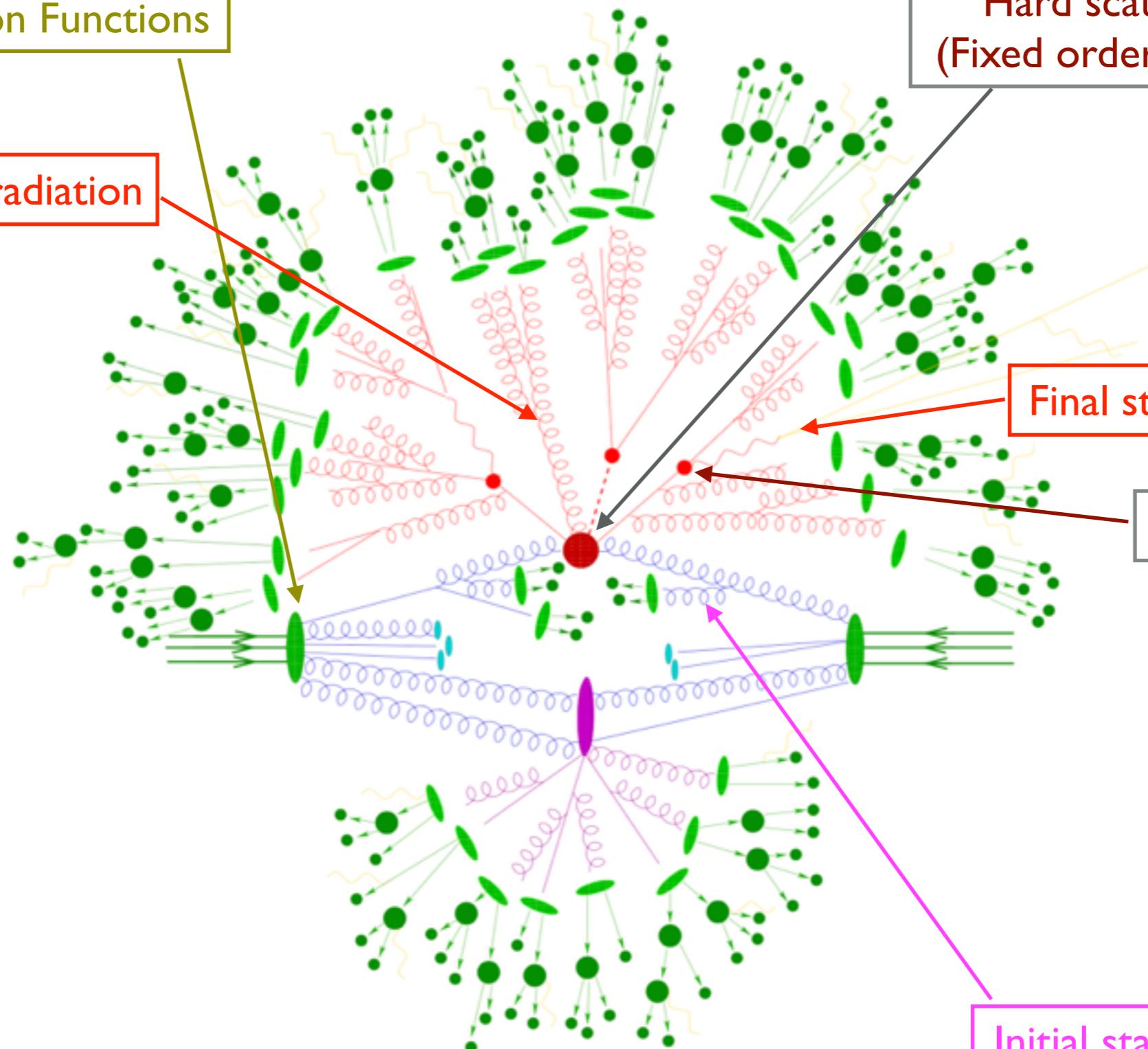
Hard scattering process
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Final state QCD radiation

Final state QED radiation

Final state decays

Initial state QCD radiation



Events at hadron colliders ... Theory

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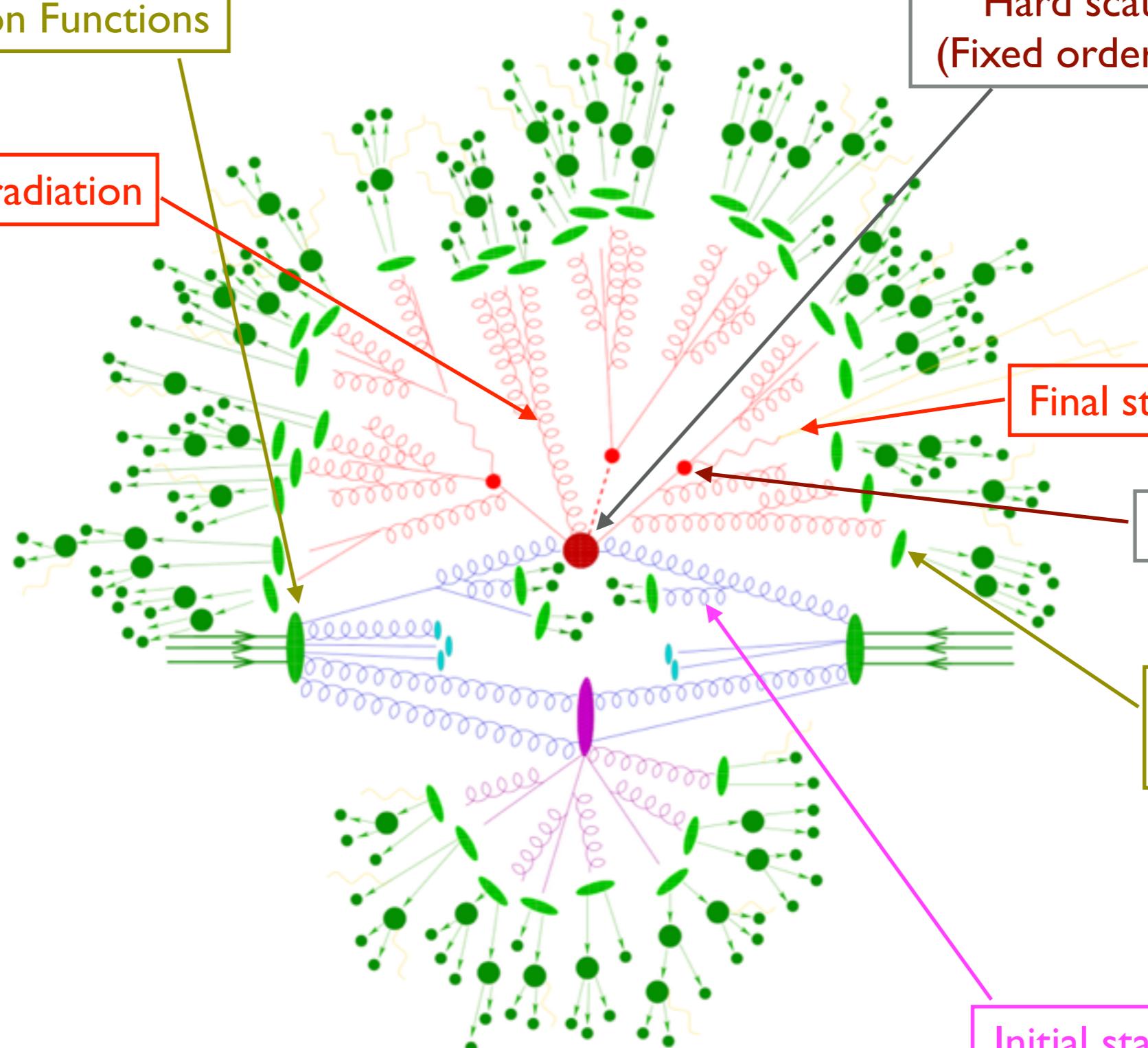
Final state QCD radiation

Final state QED radiation

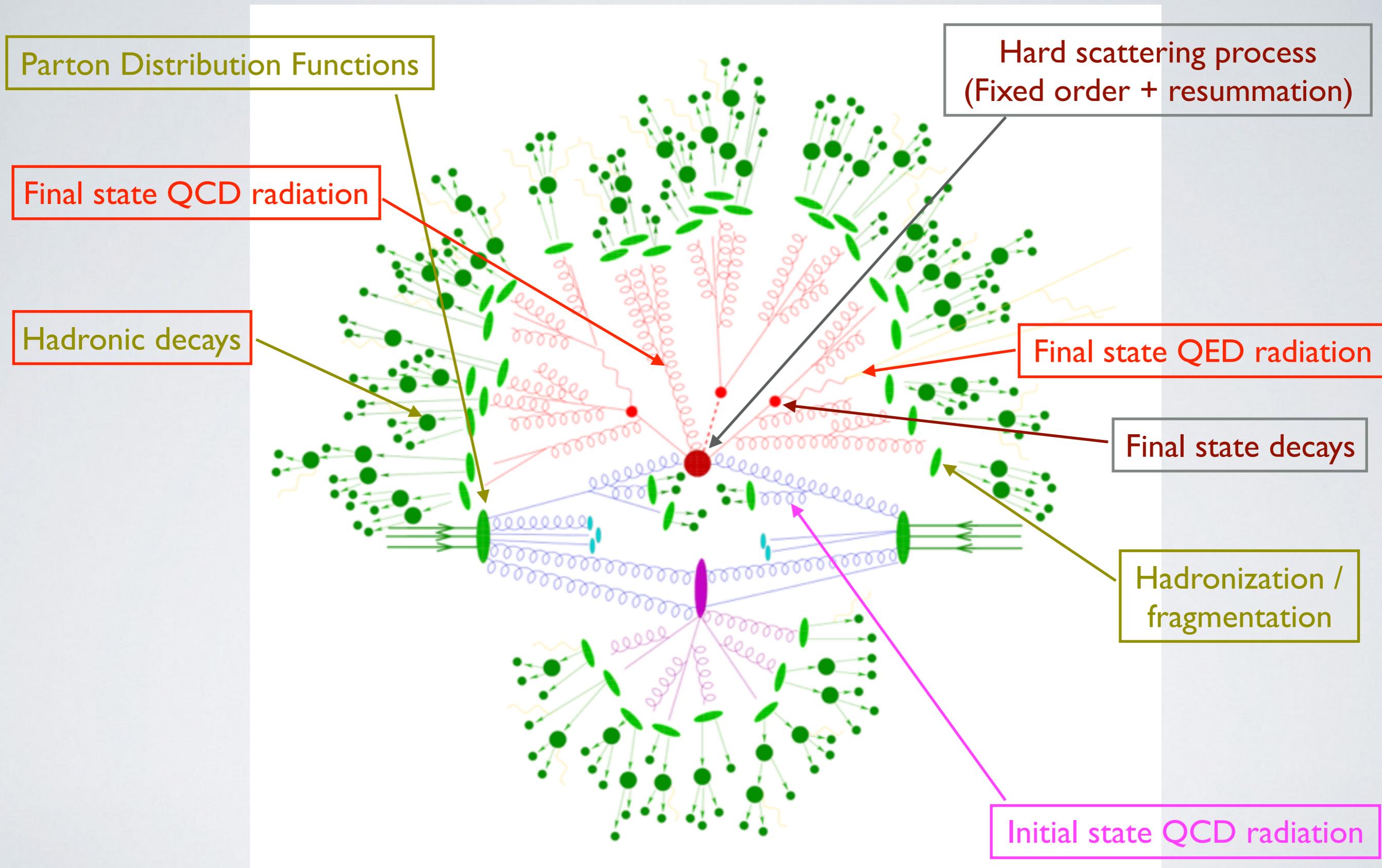
Final state decays

Hadronization /
fragmentation

Initial state QCD radiation



Events at hadron colliders ... Theory



Events at hadron colliders ... Theory

Parton Distribution Functions

Hard scattering process
(Fixed order + resummation)

Final state QCD radiation

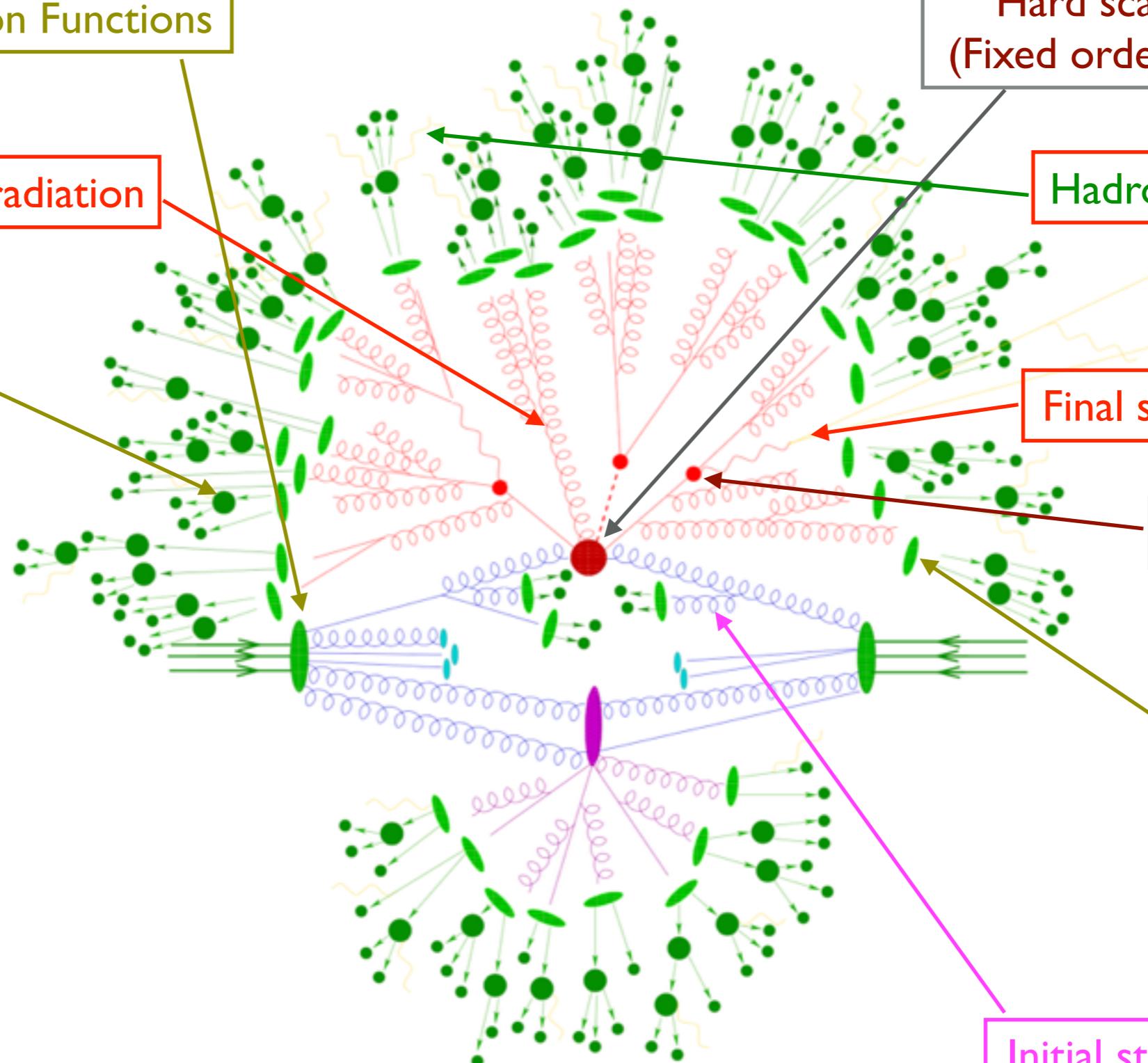
Hadronic QED radiation

Hadronic decays

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Events at hadron colliders ... Theory

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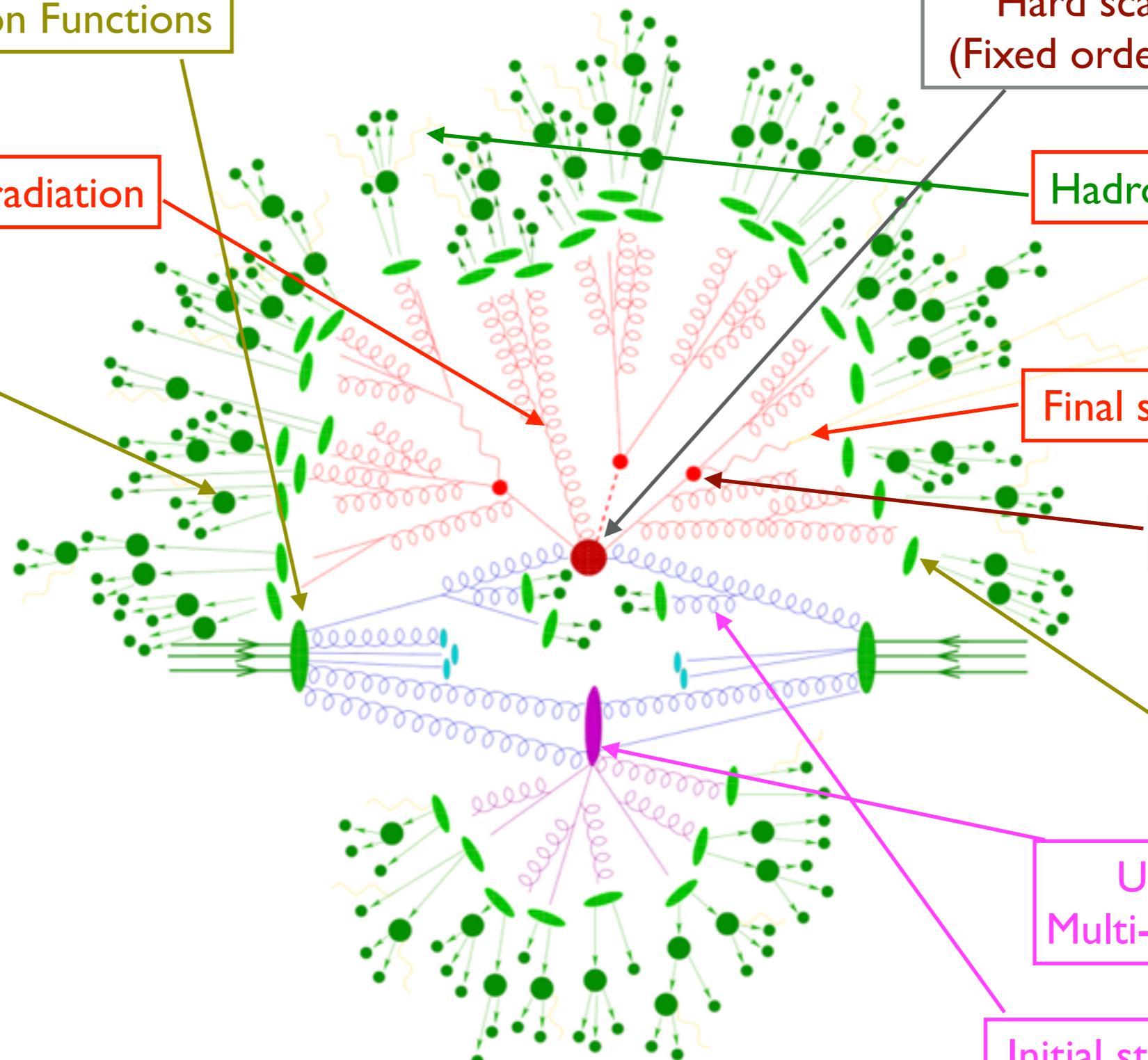
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Underlying Event:
Multi-Parton Interactions

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Events at hadron colliders ... Theory

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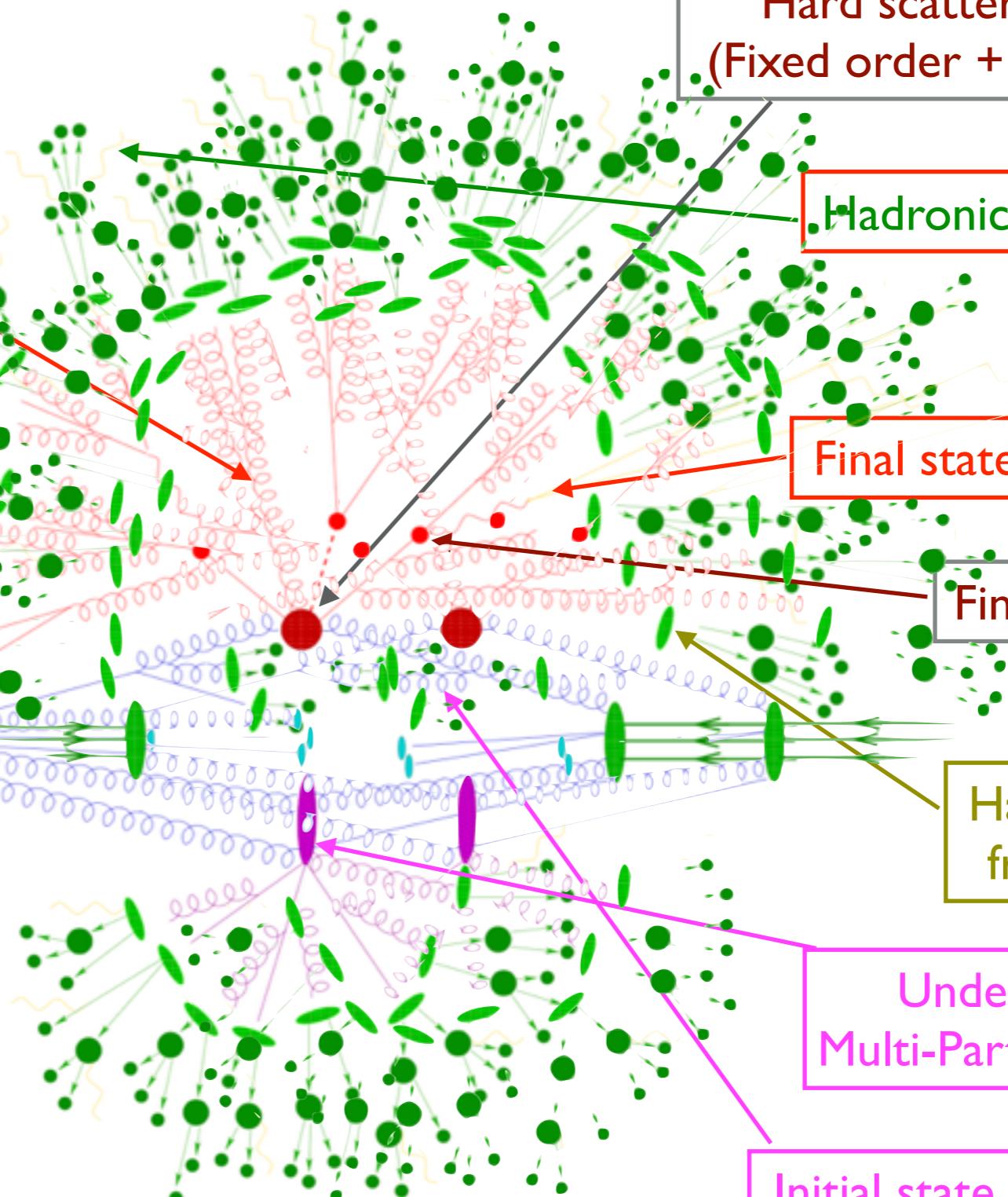
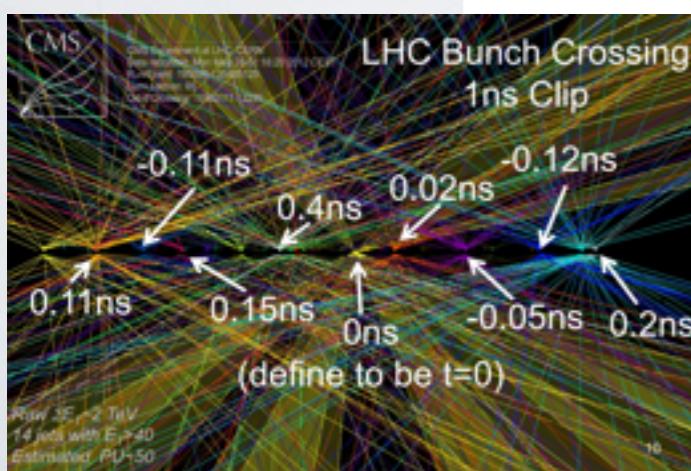
Hadronic QED radiation

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Final state QED radiation

Pile up

Hadronization /
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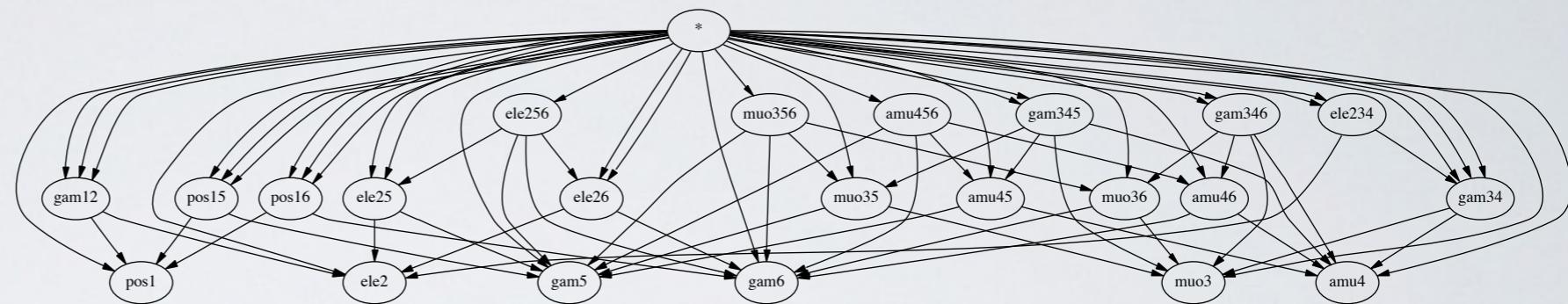
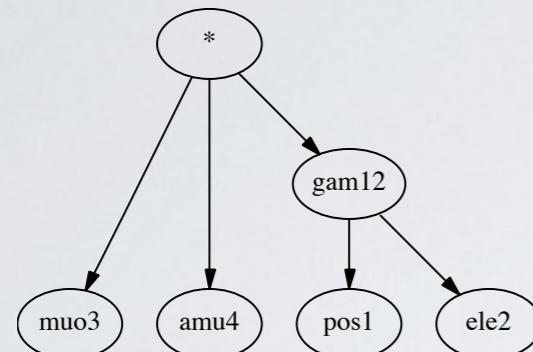
Hard process: Fixed order perturbation theory

- Perturbative amplitudes for $2 \rightarrow n$ scattering grows factorially with n
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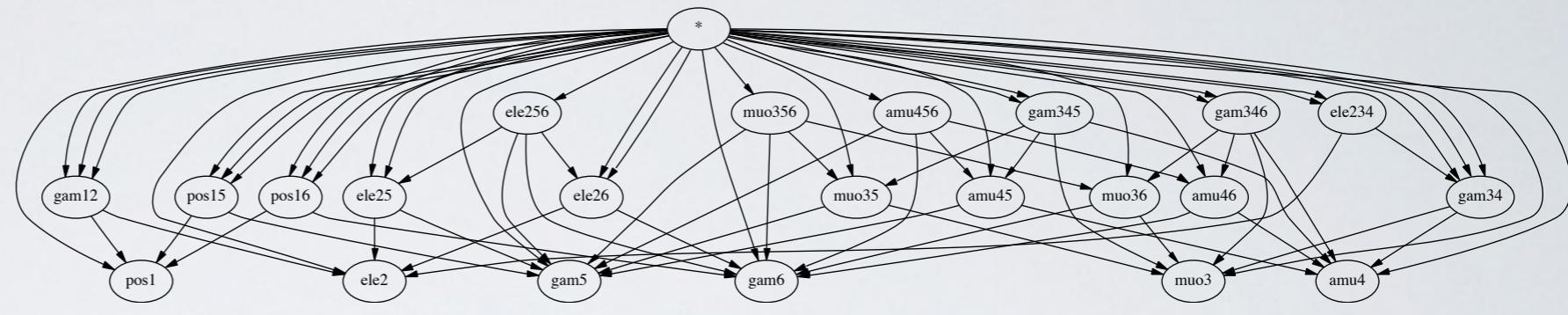
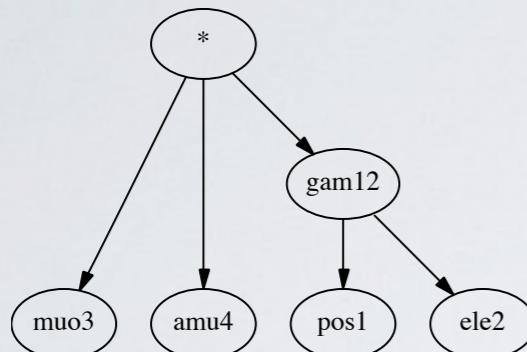
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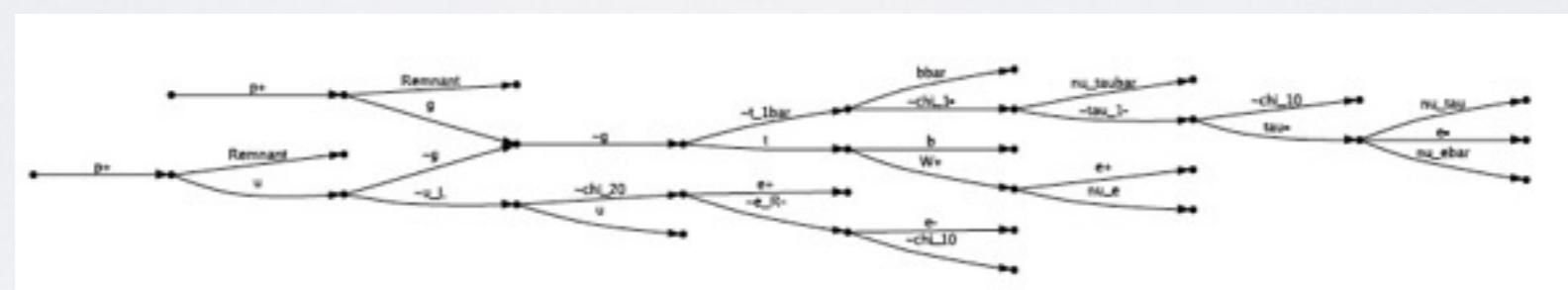


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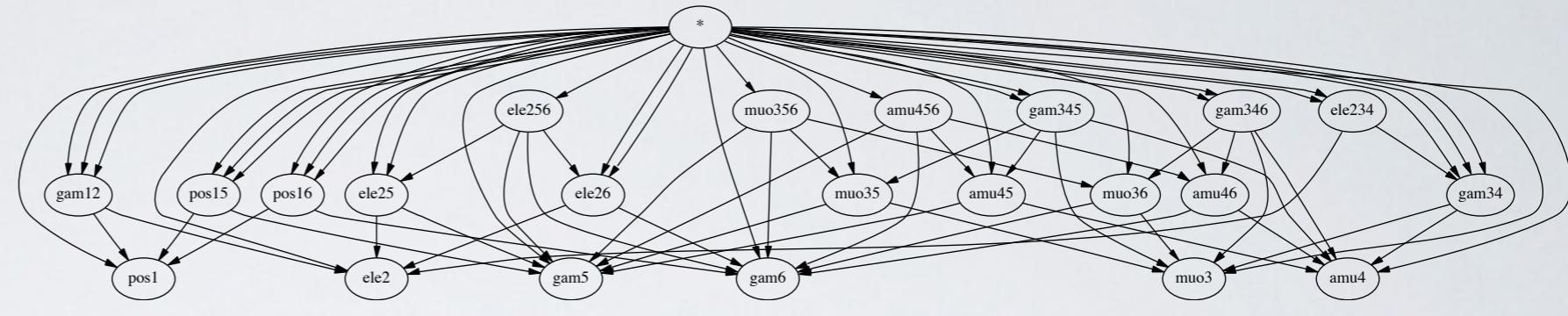
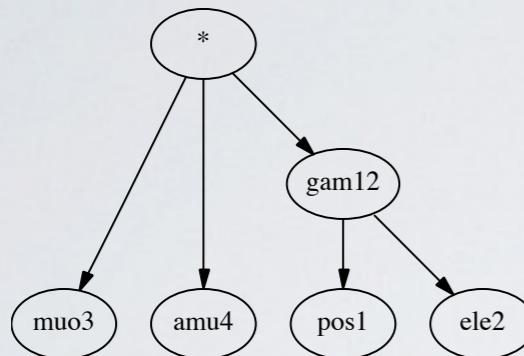


- Tree-level problem solved (for the matrix elements)
- Several smaller or bigger issues remaining:
- Large number of external legs, processes treated factorized as cascades

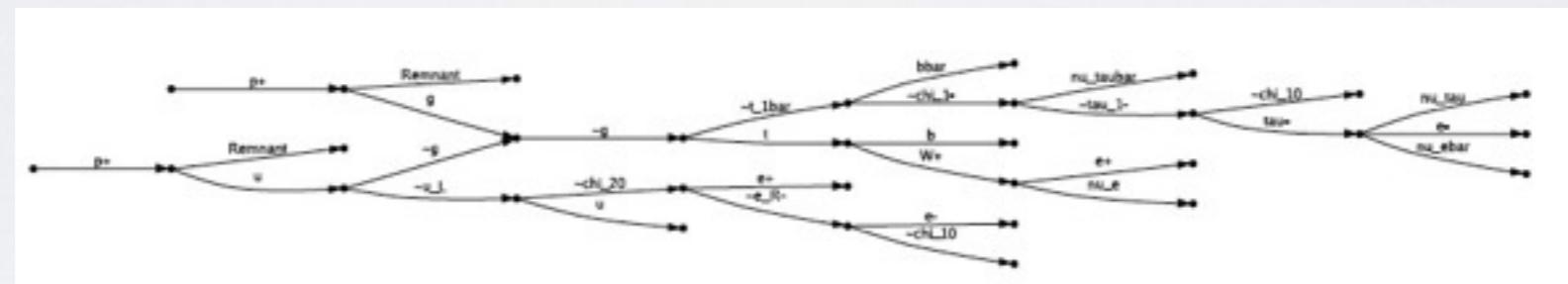


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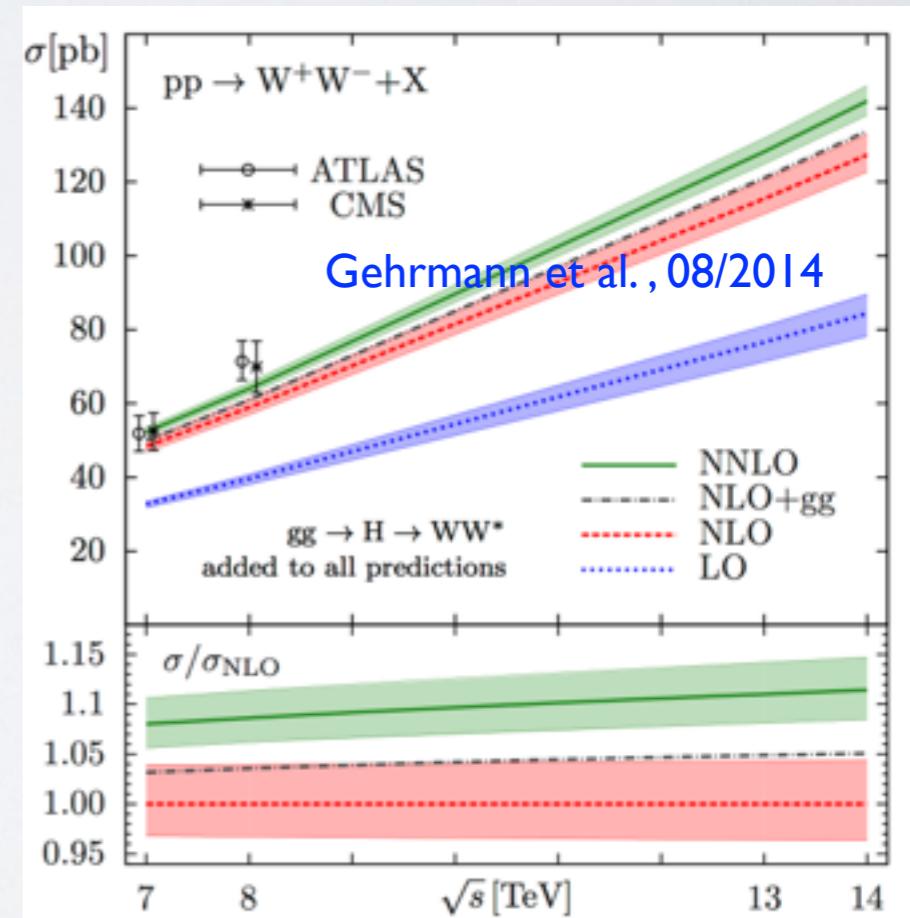
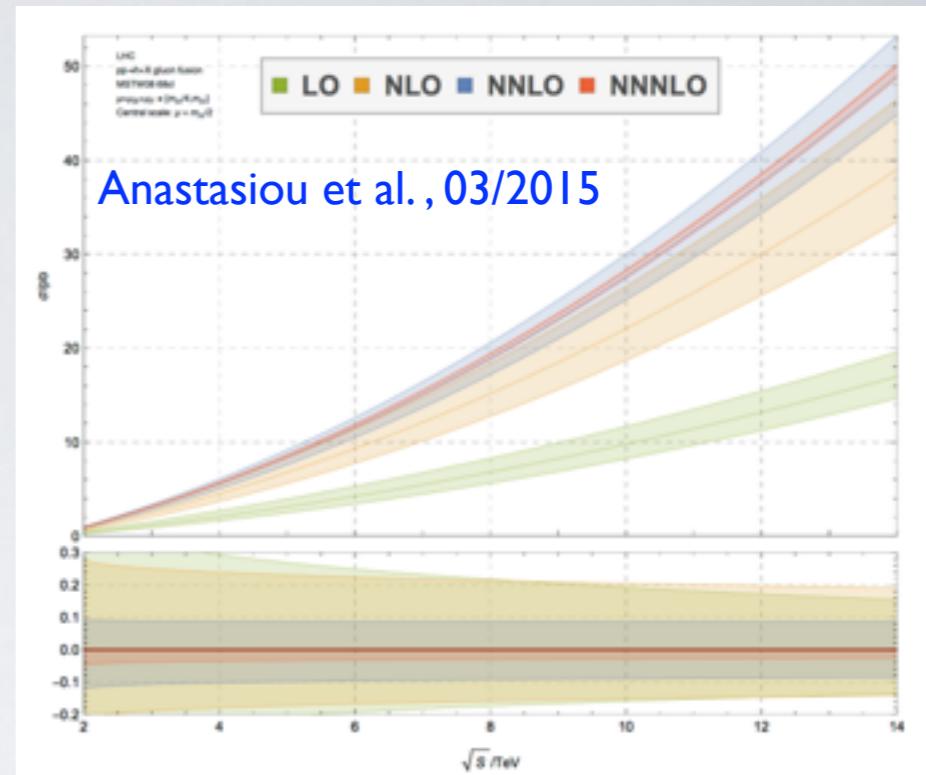


- Multi-dimensional phase-space integration
- Major bottleneck!
- Several algorithms: flat [RAMBO], simplistic heuristics [ALPGEN], diagram-based [MadEvent], [QCD]-radiation driven [SAGE], resonance/singularity importance-ordered [WHIZARD]
- Complicated QCD color algebra \Leftrightarrow high-dimensional color flow matrices
- Light flavor degeneracies in jets

$$\sigma \sim \int \sum_{h_k, c_k} |\mathcal{M}(p_k, h_k, c_k)|^2 \prod_i \frac{d^3 p_i}{(2\pi)^3 2p_i^0}$$

Higher Order Calculations

- ▶ Large (QCD) corrections at hadron colliders
- ▶ Example: Higgs production in gluon fusion
[K factor: $\sigma_{\text{NLO}}/\sigma_{\text{LO}}$ or $\sigma_{\text{NNLO}}/\sigma_{\text{LO}}$]
- ▶ Virtual corrections: loop diagrams

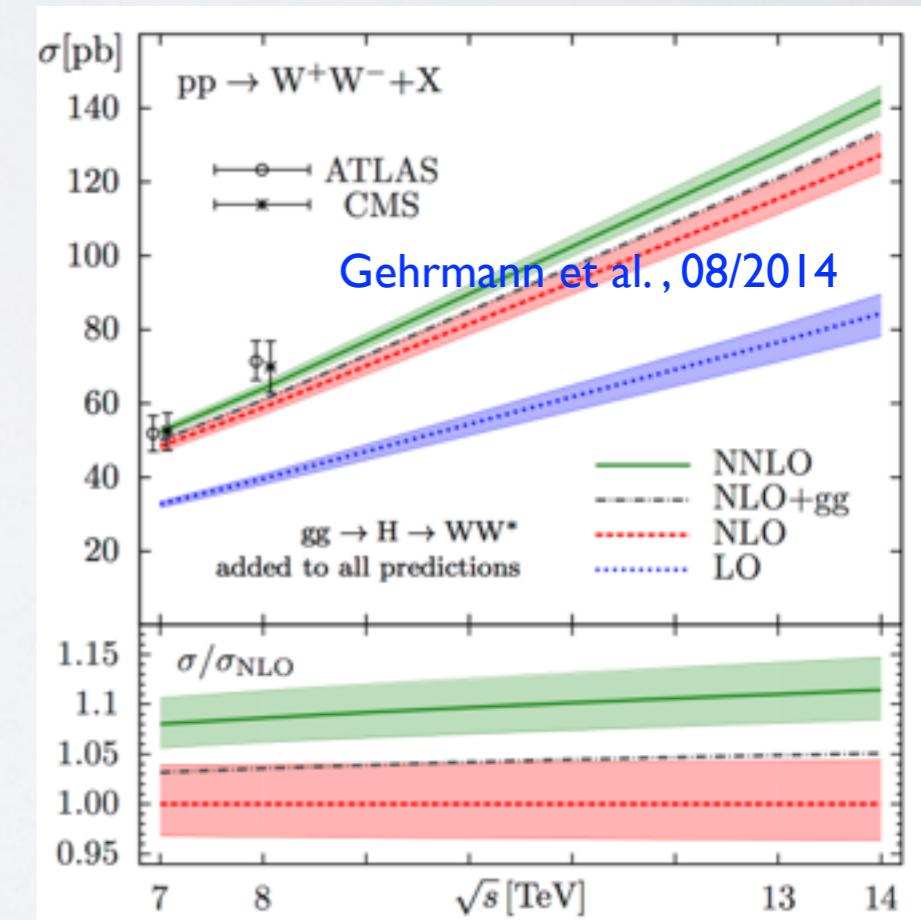
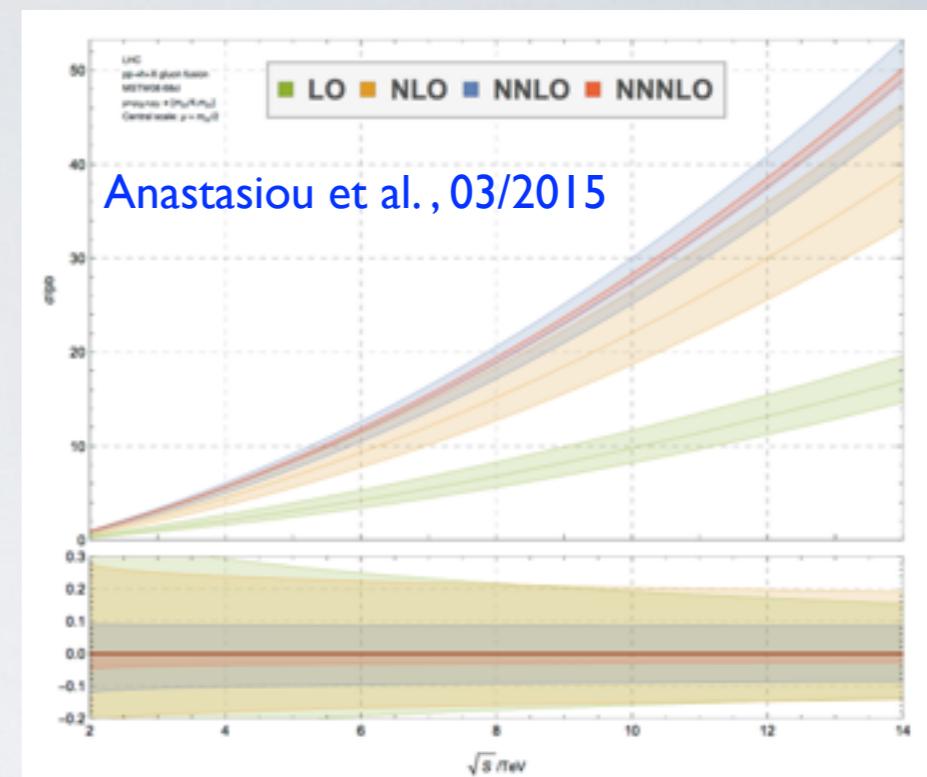
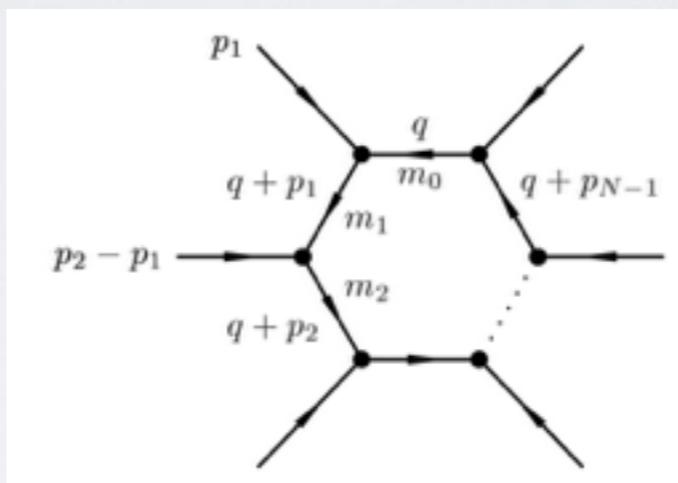


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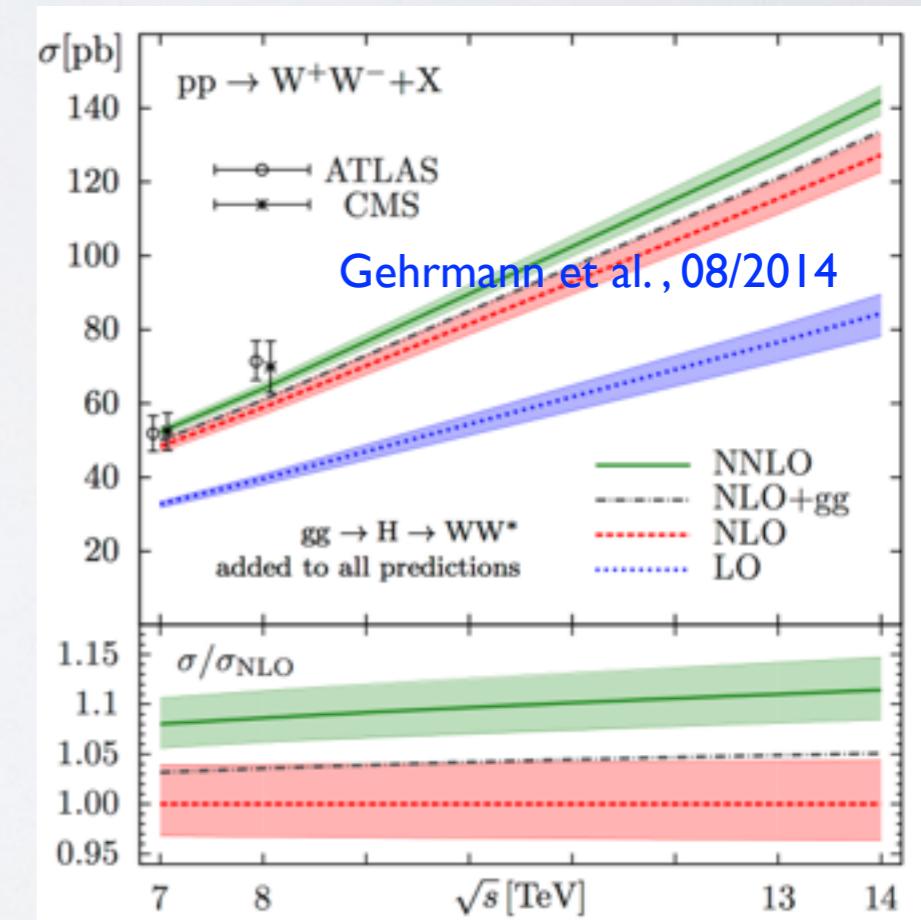
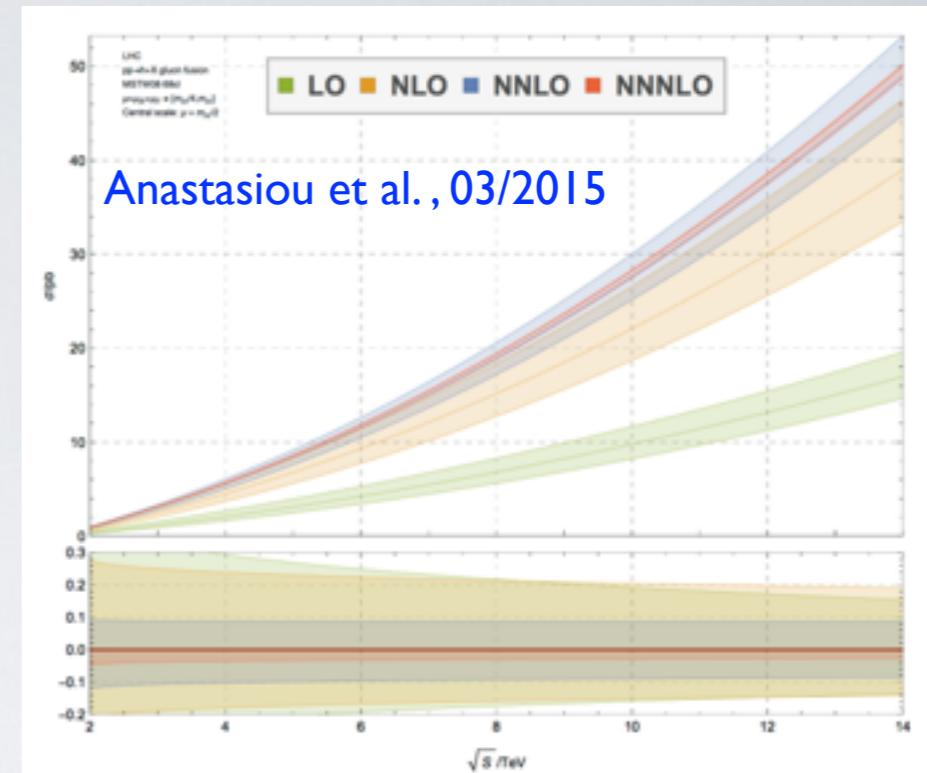
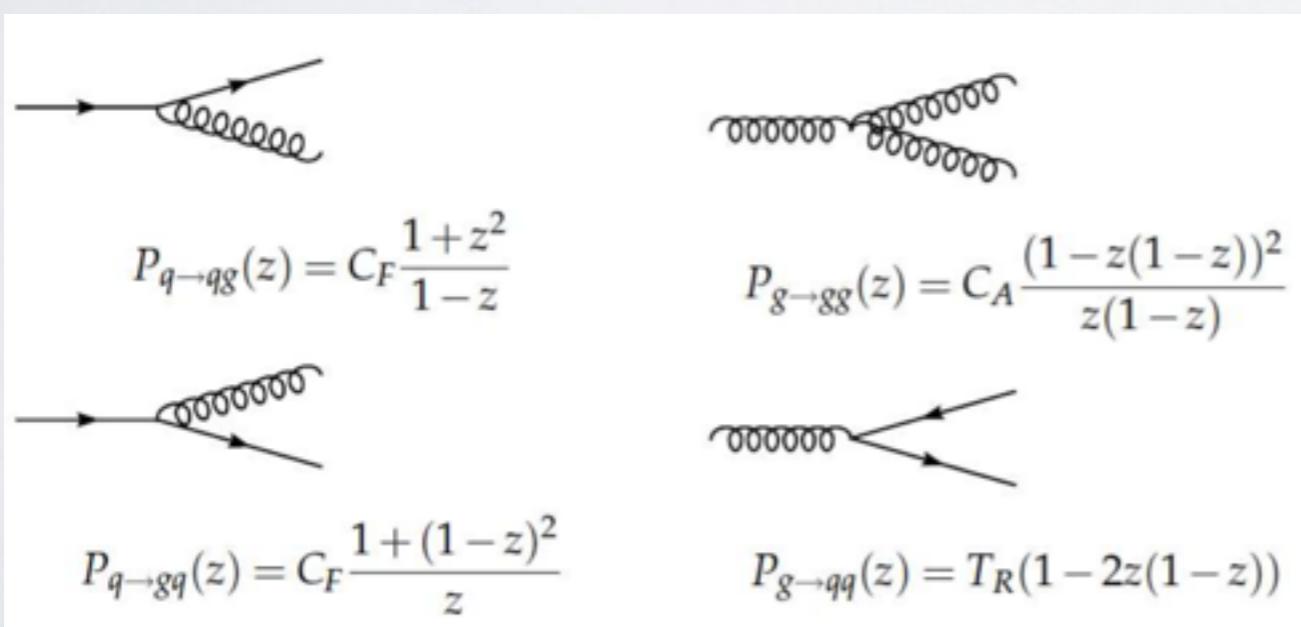
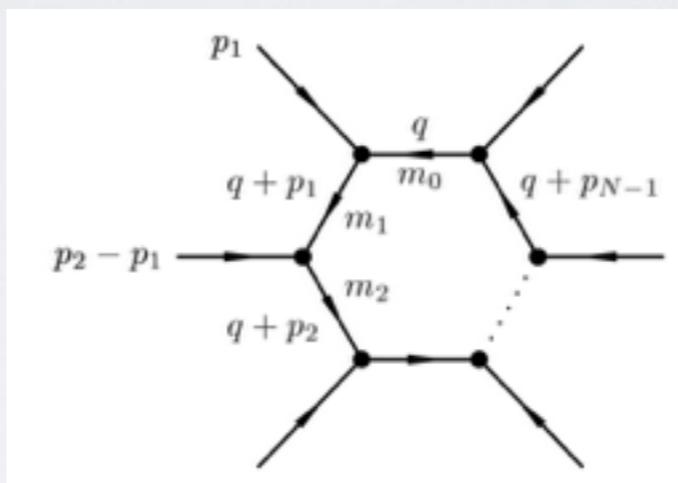
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- ▶ Soft and collinear singularities given by QCD splittings:



“Automation”

- ## □ General structure of NLO cross section:

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- 1990's: "Subtraction algorithms" (process independently cancel IR-divergences exactly)

FKS [Frixione/Kunszt/Signer, '96], CS-Dipoles [Catani/Seymour, '98] [FKS: Kinematics vs. Dipoles/CS: shower]

$$d\sigma_n^{\text{NLO}} = d\Phi_n \left[\mathcal{B}_n + \mathcal{V}_n + \mathcal{B}_n \otimes S \right] + d\Phi_{n+1} \left[\mathcal{R}_{n+1} - \mathcal{B}_n \otimes dS \right]$$



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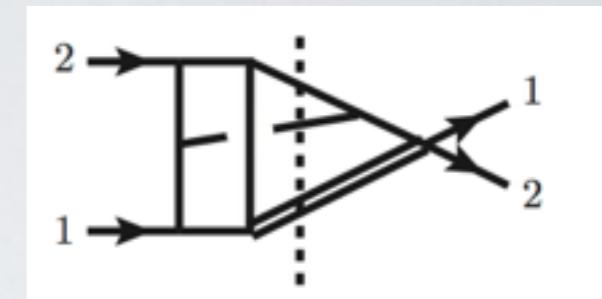
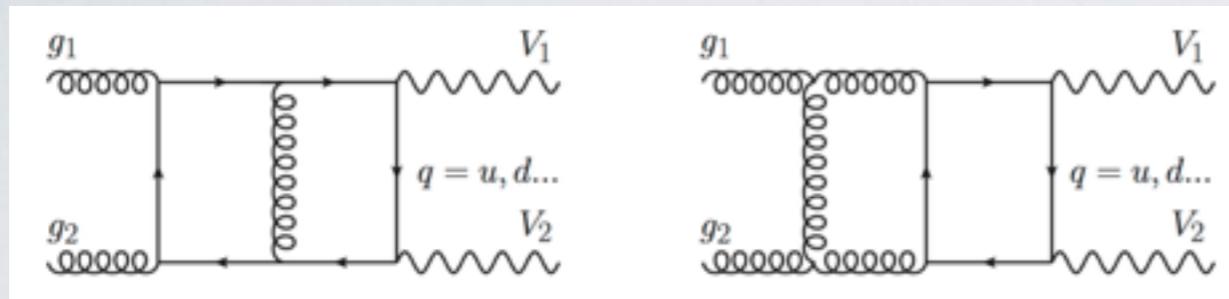
- “Automation” is rather simplification: never switch off your brain !!!



NNLO QCD (and beyond)



Battlefront of precision calculations: virtual NNLO $2 \rightarrow 2$, NNNLO $2 \rightarrow 1$

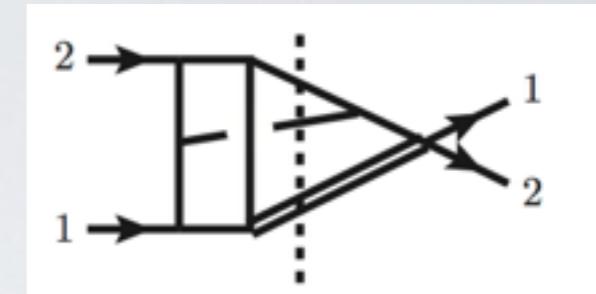
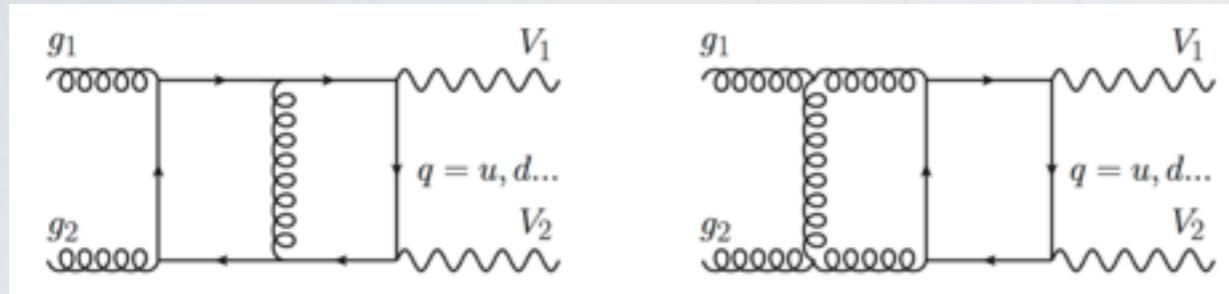


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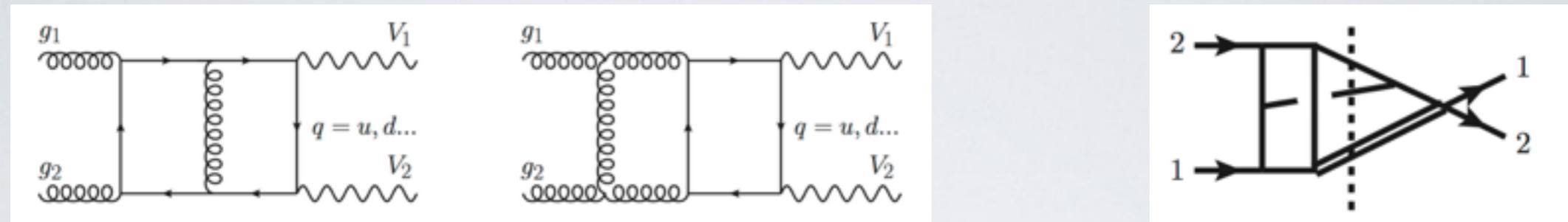
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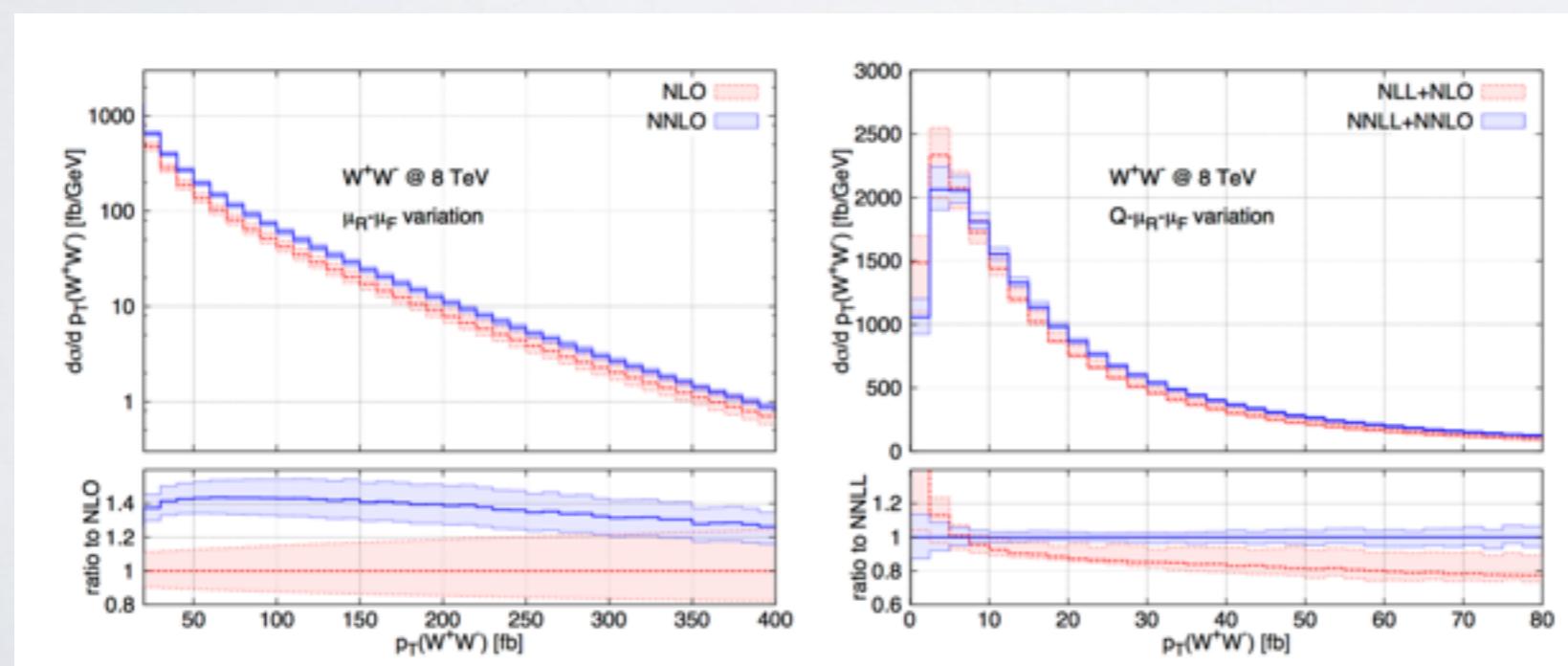
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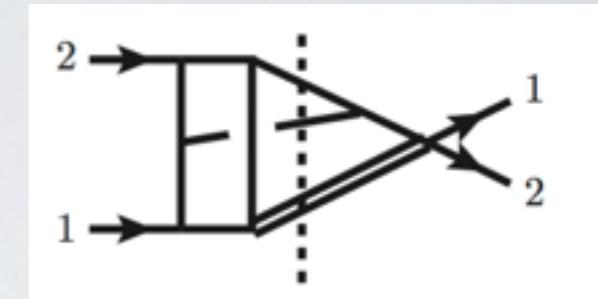
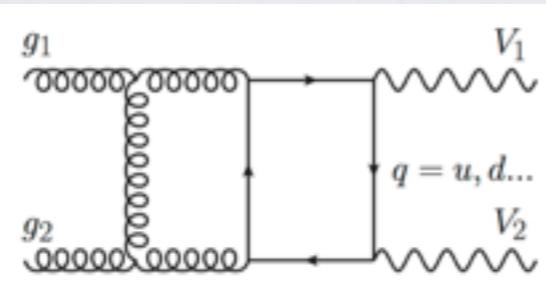
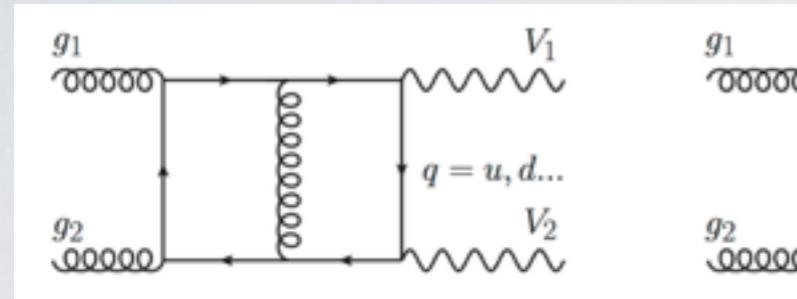
Grazzini/Kallweit/Rathlev/Wiesemann, 07/2015



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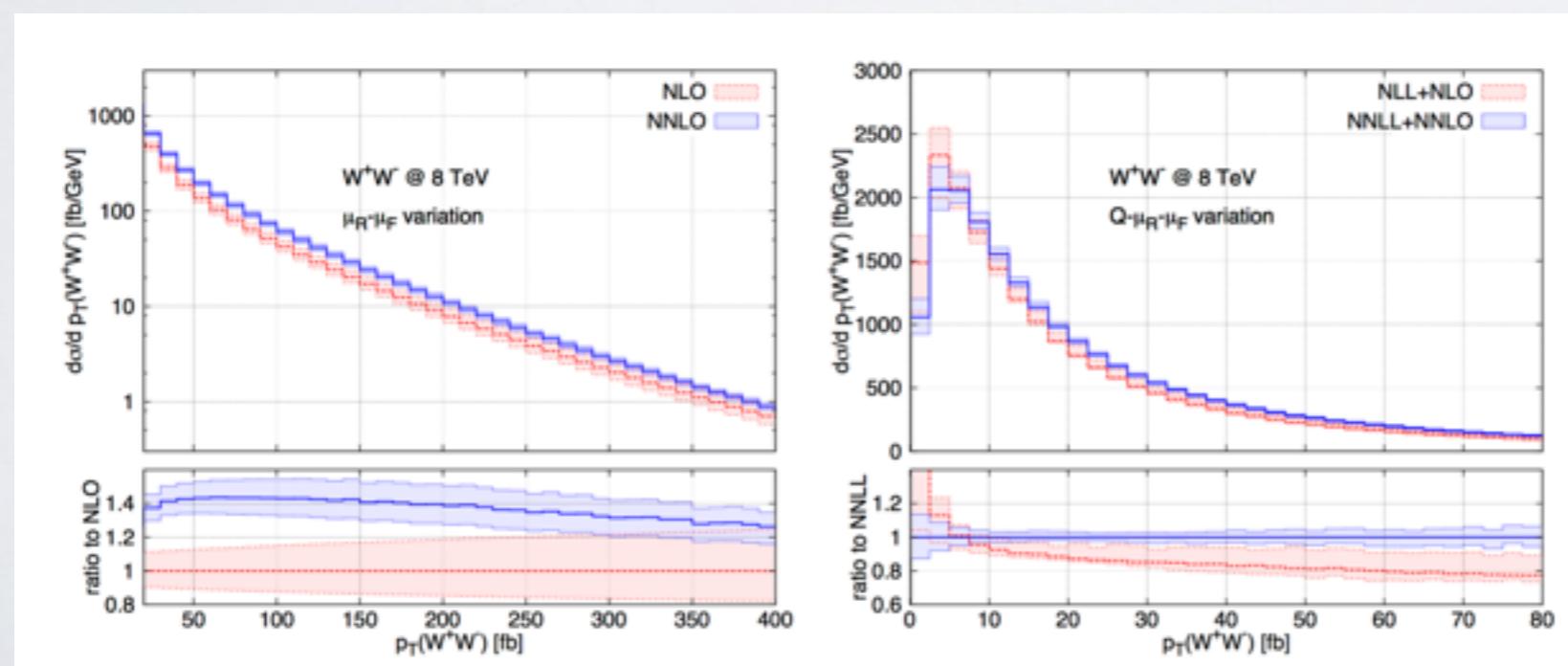
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Resummation for phase-space regions with badly behaved perturbative series (large logs)



Crucial for exclusive measurements (jet vetoes)

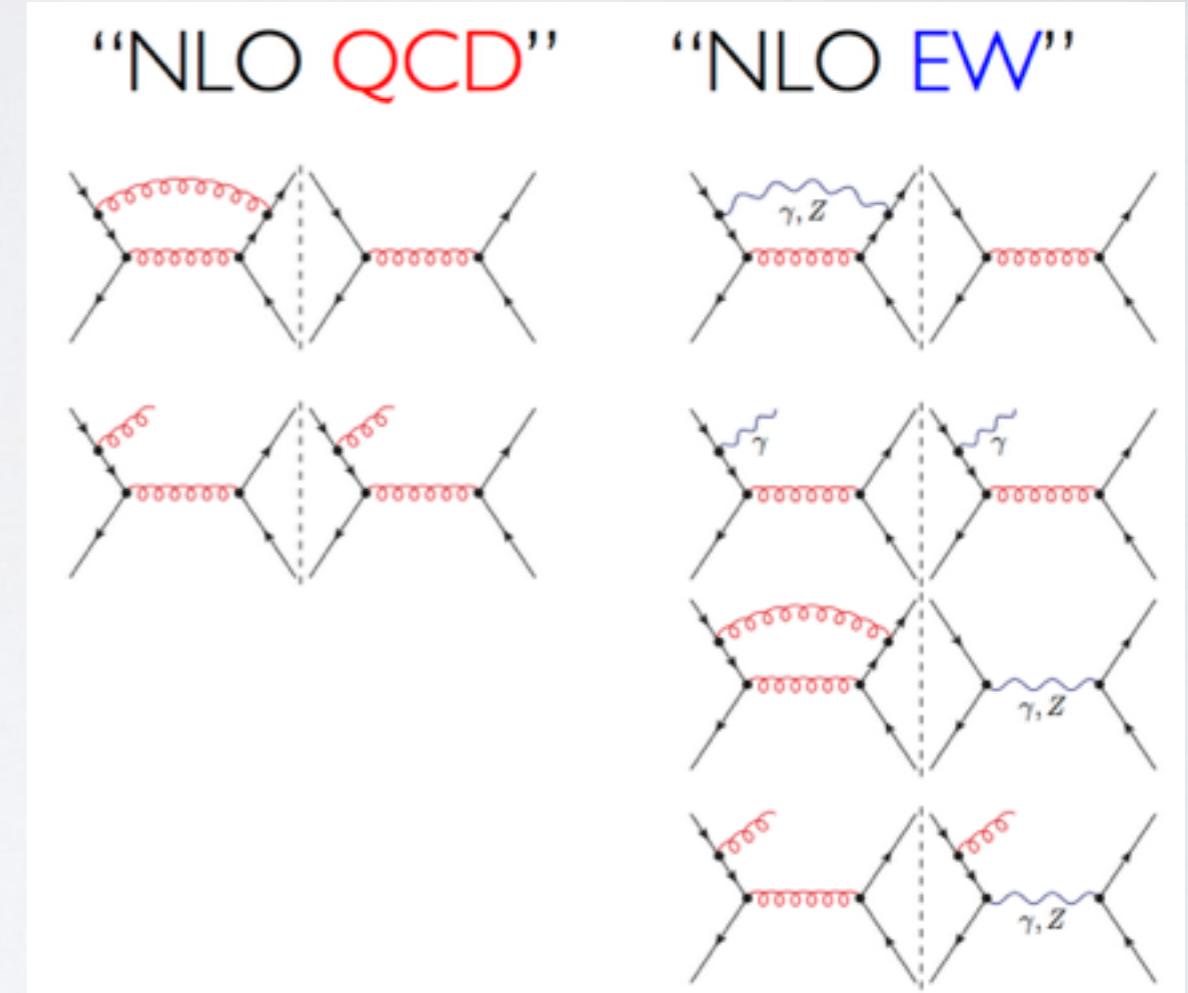
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Electroweak Corrections

- Rule of thumb: NNLO QCD \sim NLO Electroweak $\quad \alpha_s \sim 0.1, \quad \alpha \sim 0.01$
- Several tools deliver EW NLO: [Gosam], OpenLoops, Recola [not public]
- Master integrals more complicated [several different mass scales]
- Subtraction formalism tedious [interference of different QCD and EW orders]
- Big effects at high energies:
EW Sudakov logarithms
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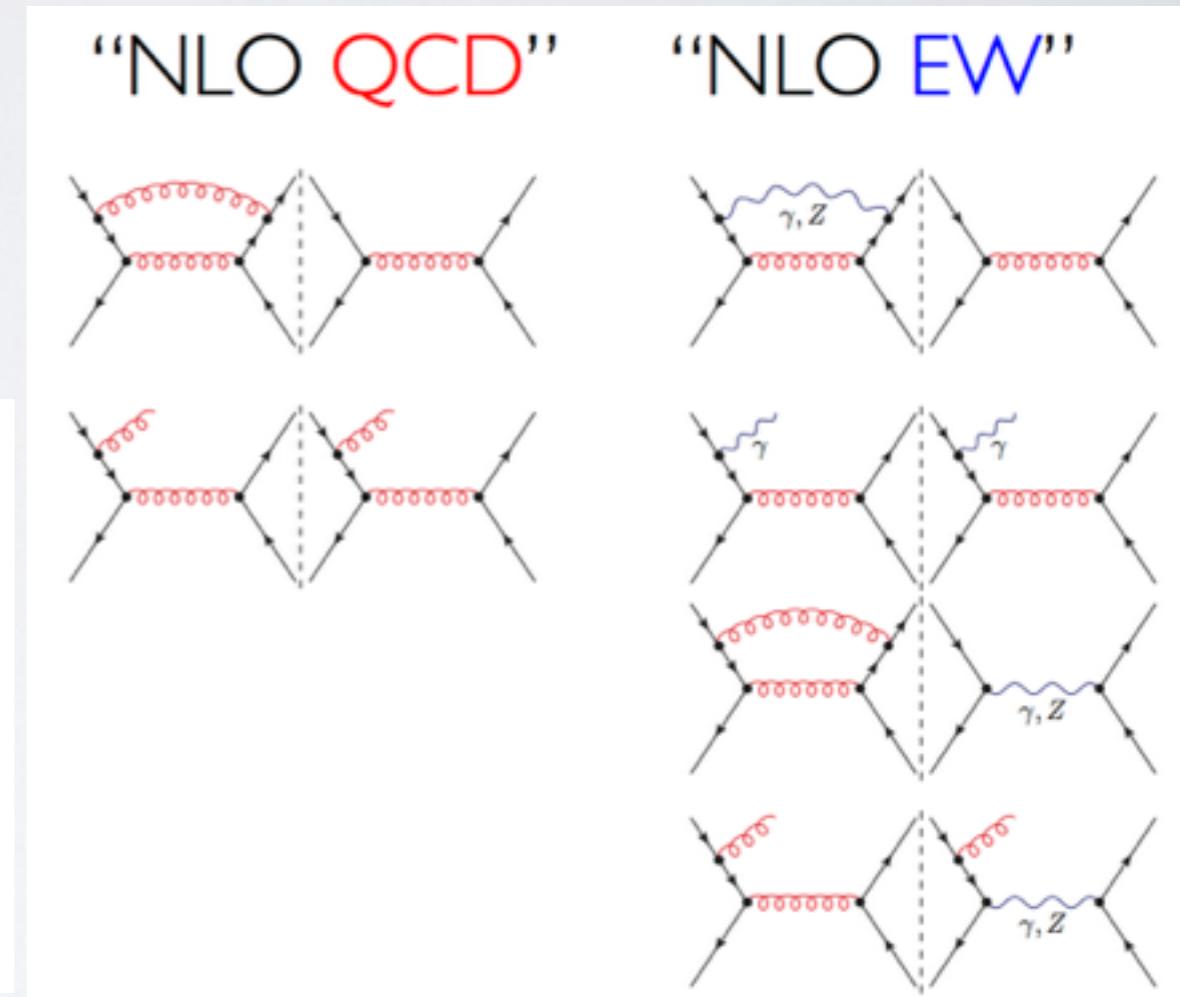
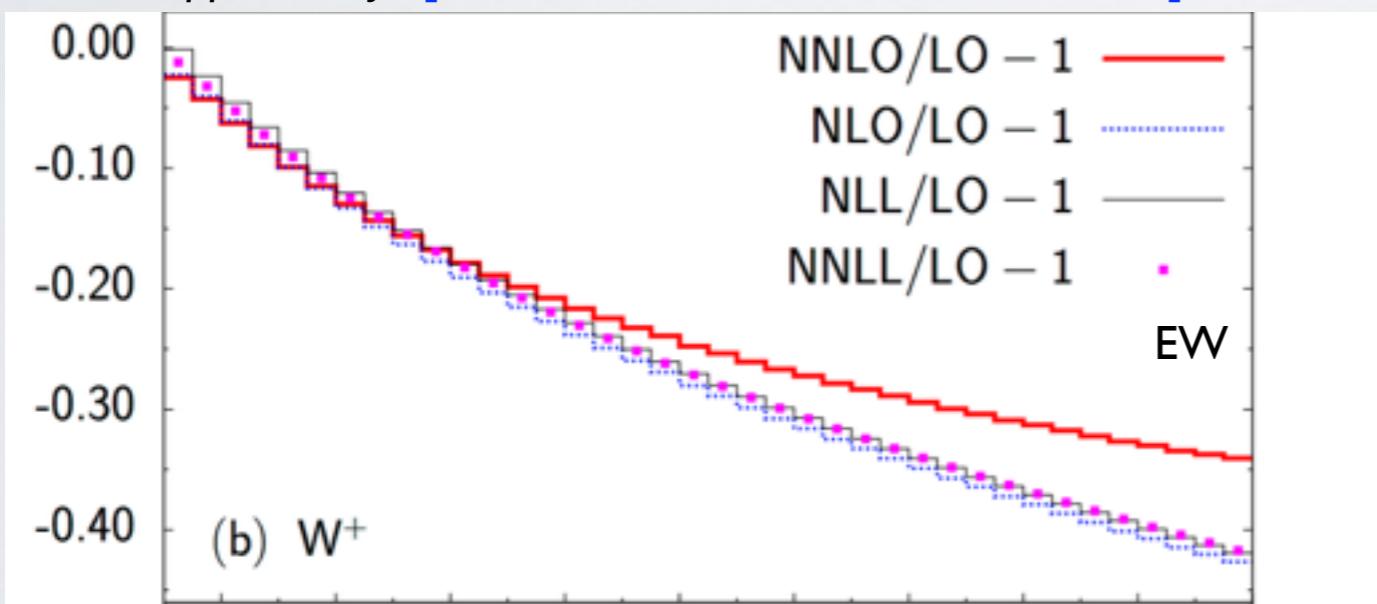


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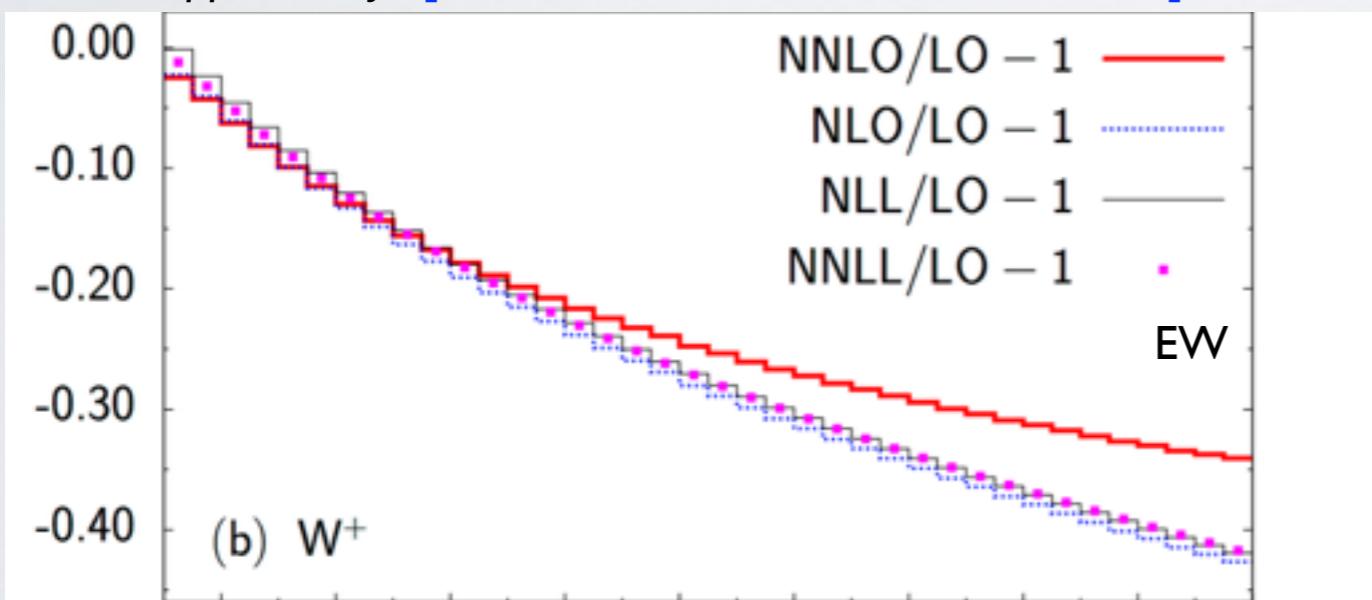


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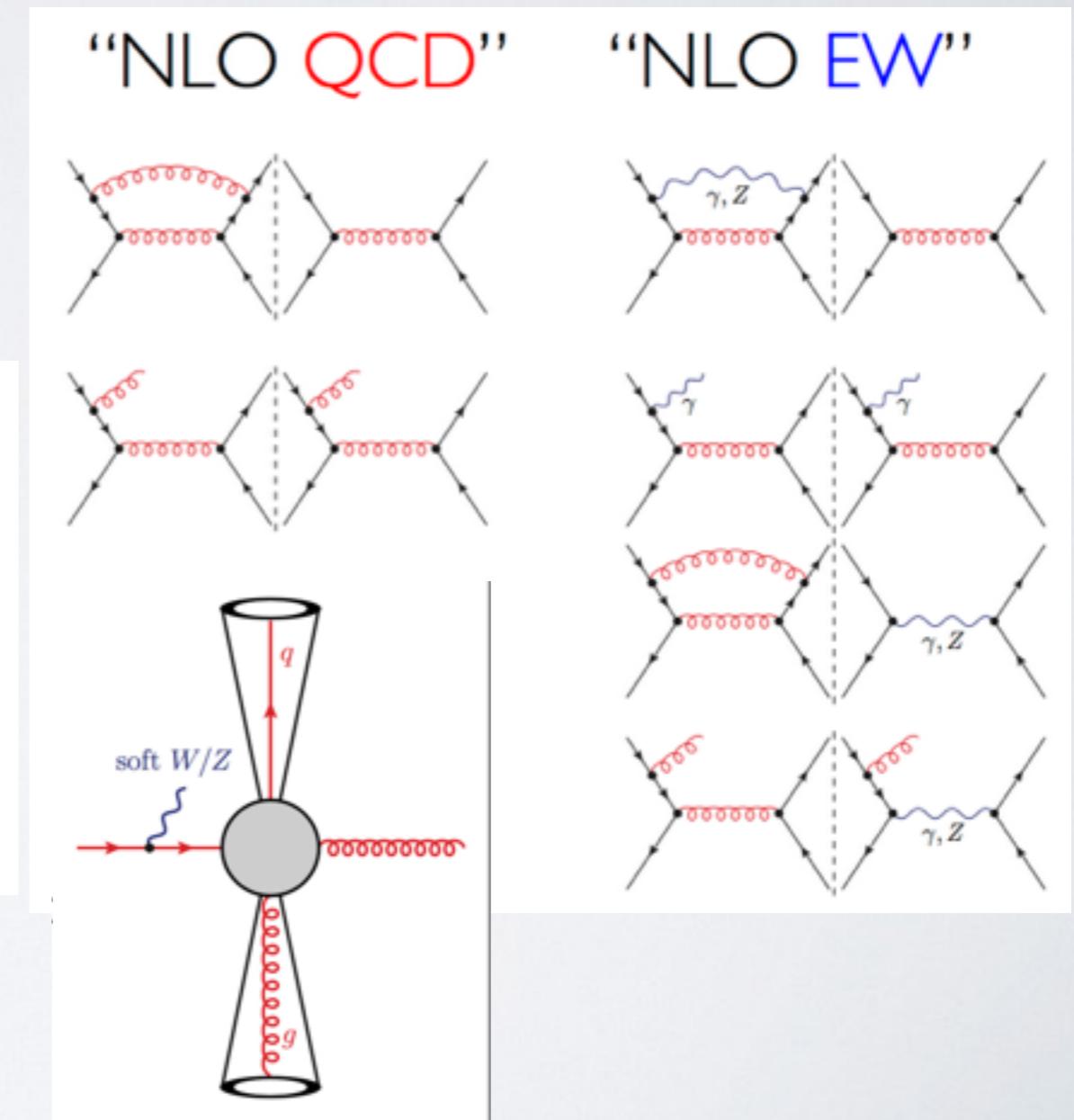
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Tricky QCD/EW interplay: Wjj NLO vs. Dijet NLO



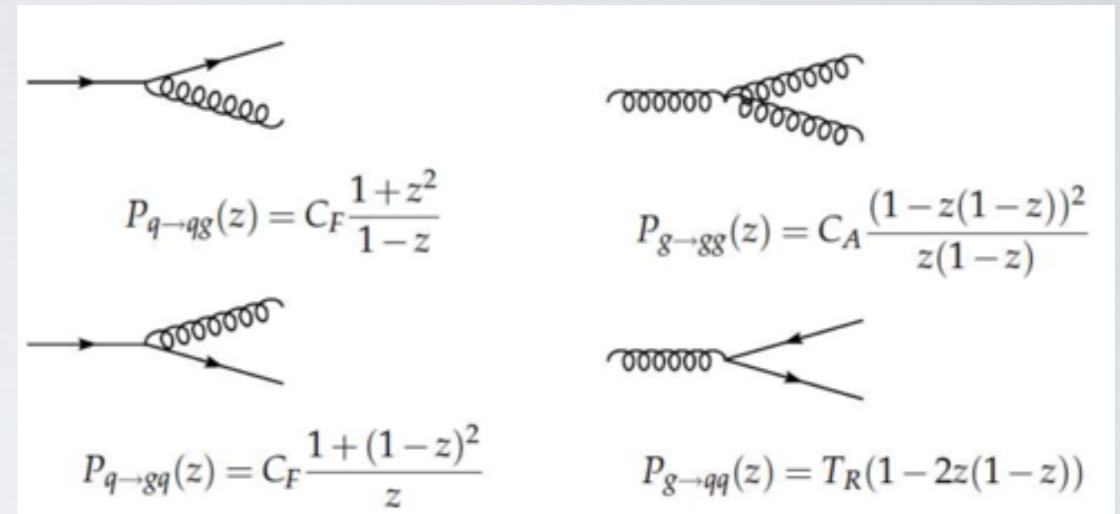
Loops and legs ...



ISR & FSR: Parton Showers

- Full matrix elements for processes with up to 100 partons are not feasible
- Approximation by parton showers
- Splitting probability $i \rightarrow jk$

$$d\Gamma_{i \rightarrow jk}(t) = \frac{dt}{t} \frac{\alpha_s}{2\pi} \int dz \frac{d\phi}{2\pi} P_{i \rightarrow jk}(t, z, \phi)$$



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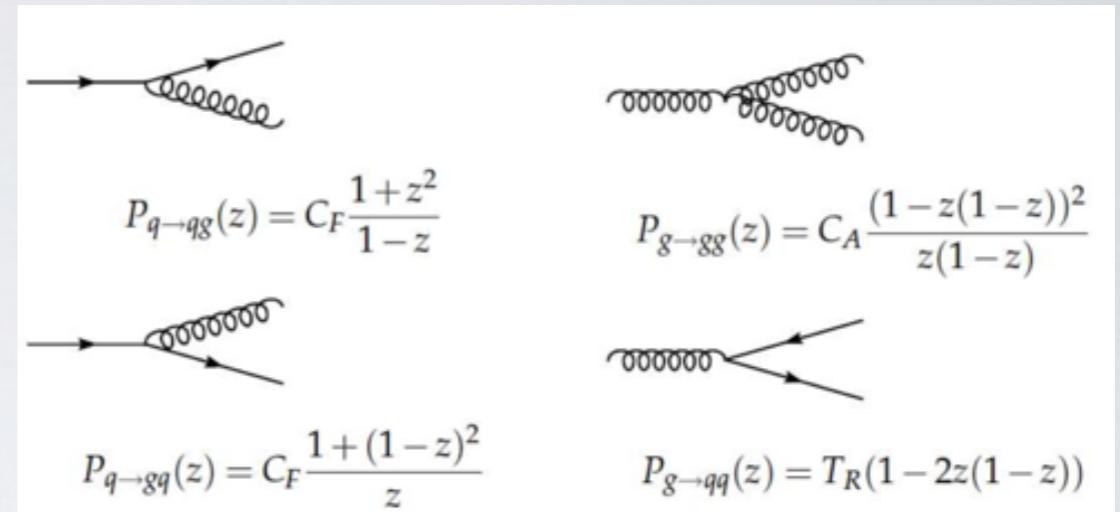
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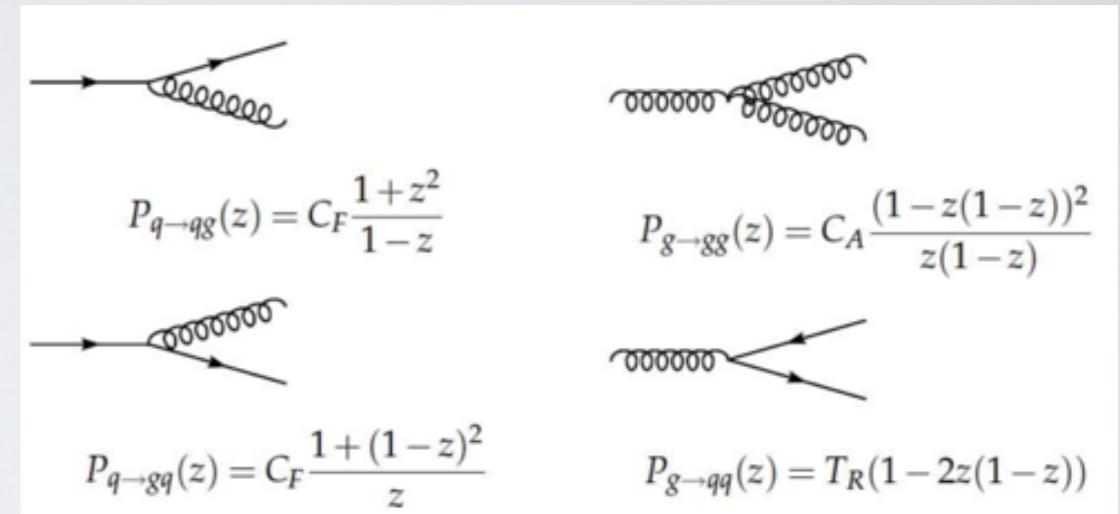
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- Evolution parameter t : angle, transverse momentum, virtuality
- Exclusive QCD radiation does not change cross section norm (**parton shower unitarity**)
- Parton showers quasi-classical approximations: no color correlations, no interference
- Parton shower resum large logarithms

ISR & FSR: Parton Showers

- Full matrix elements for processes with up to 100 partons are not feasible

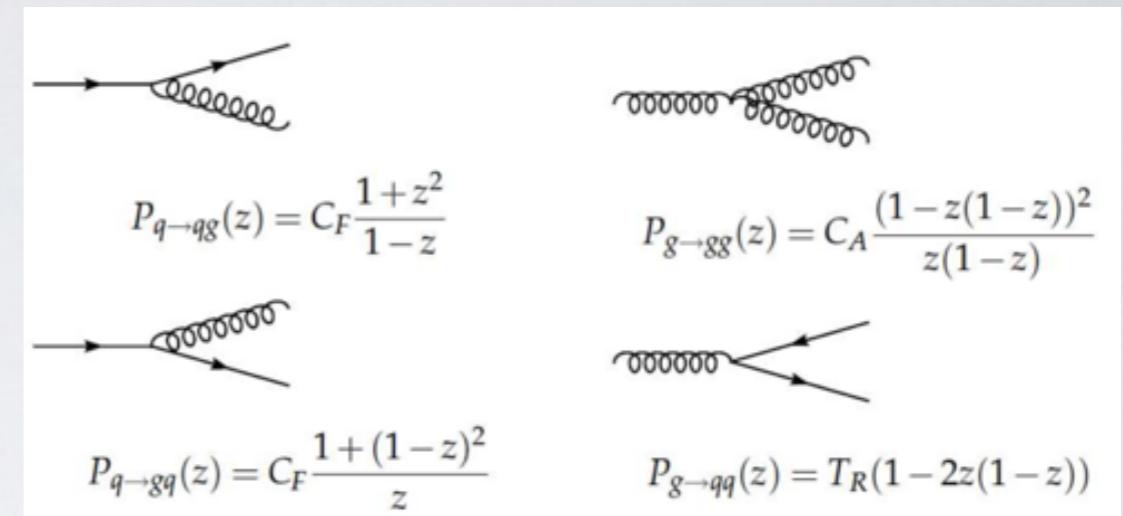
- Approximation by parton showers

- Splitting probability $i \rightarrow jk$

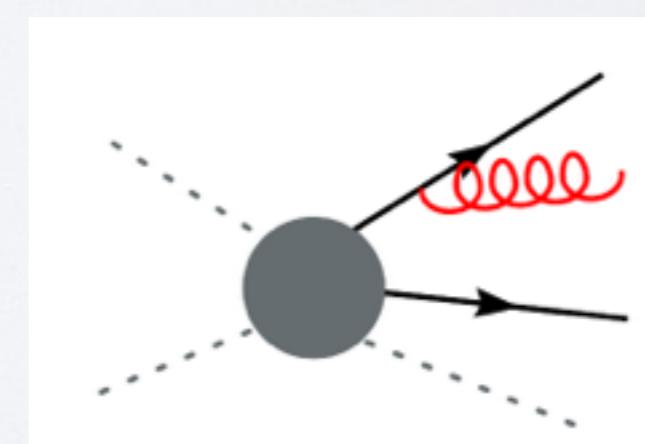
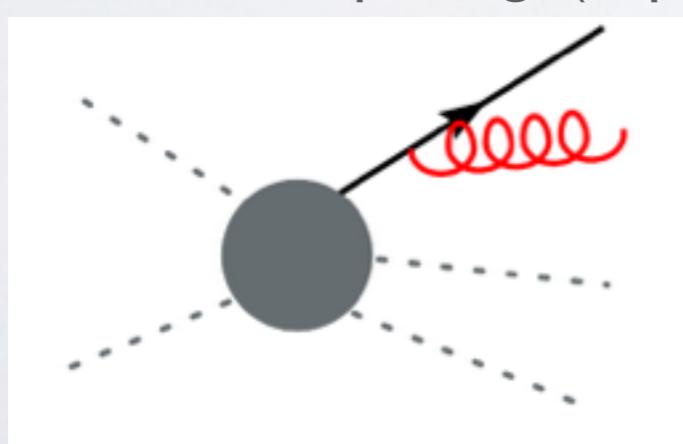
$$d\Gamma_{i \rightarrow jk}(t) = \frac{dt}{t} \frac{\alpha_s}{2\pi} \int dz \frac{d\phi}{2\pi} P_{i \rightarrow jk}(t, z, \phi)$$

- Probability of no splitting: Sudakov form factor

$$\Delta_{i \rightarrow jk}(t, t_0) = \exp \left[- \int_{t_0}^t d\Gamma_{i \rightarrow jk}(t') \right]$$



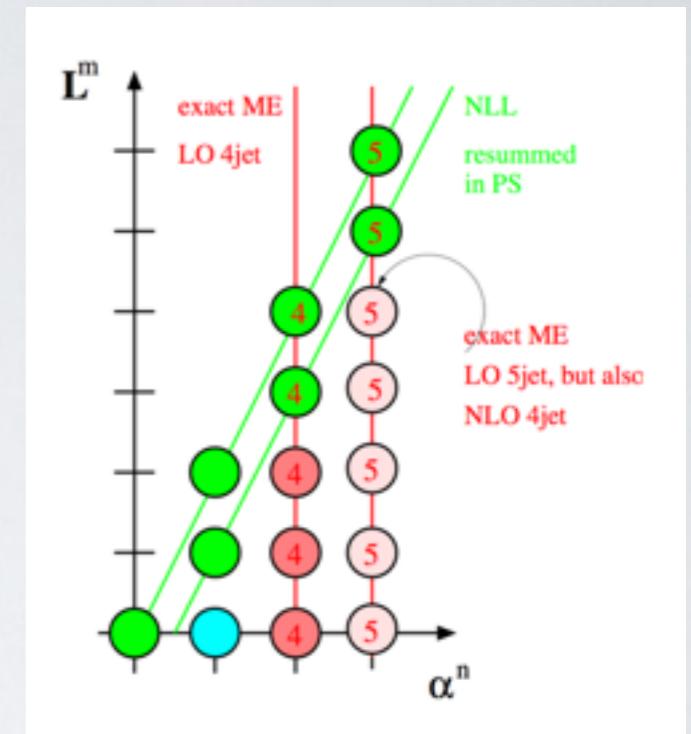
- Evolution parameter t : angle, transverse momentum, virtuality
- Exclusive QCD radiation does not change cross section norm (**parton shower unitarity**)
- Parton showers quasi-classical approximations: no color correlations, no interference
- Parton shower resum large logarithms
- Final state radiation (FSR): **time-like showers**
- Initial state radiation (ISR): **space-like showers** (**PDF reweighting, makes time-like shower again**)
- $1 \rightarrow 2$ vs. $2 \rightarrow 3$ splitting (Dipoles, antennae)



Matching and Merging

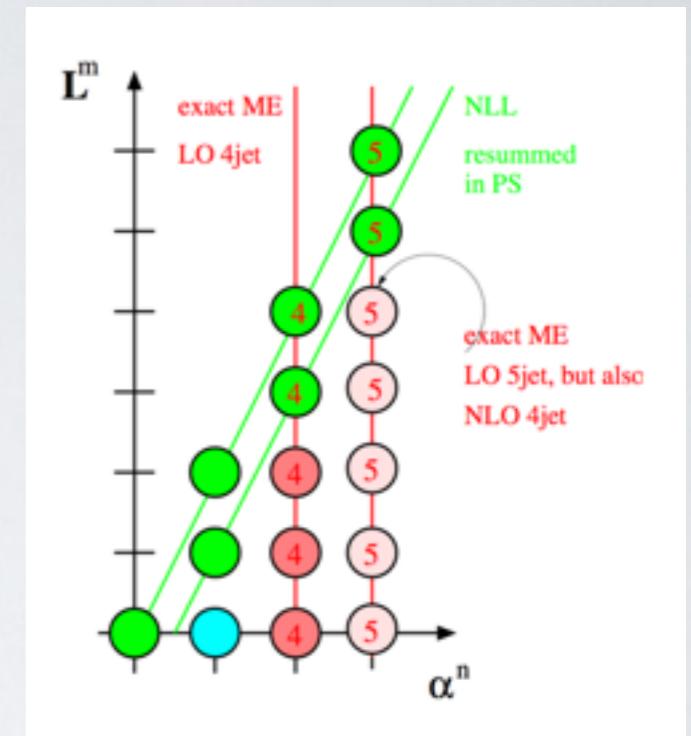
- Jet production: matrix elements (ME) exact at fixed order, good description of hard/large-angle emissions
- Jet evolution: parton shower (PS) resum logarithms, good description of soft/collinear emissions
- **Matching @ LO/NLO:** [MLM, Powheg, CKKW, GKS]

- Cross section at LO/NLO accuracy
- Hardest emission in PS corrected to reproduce ME exactly at order α_s (\mathcal{R} -part of NLO)



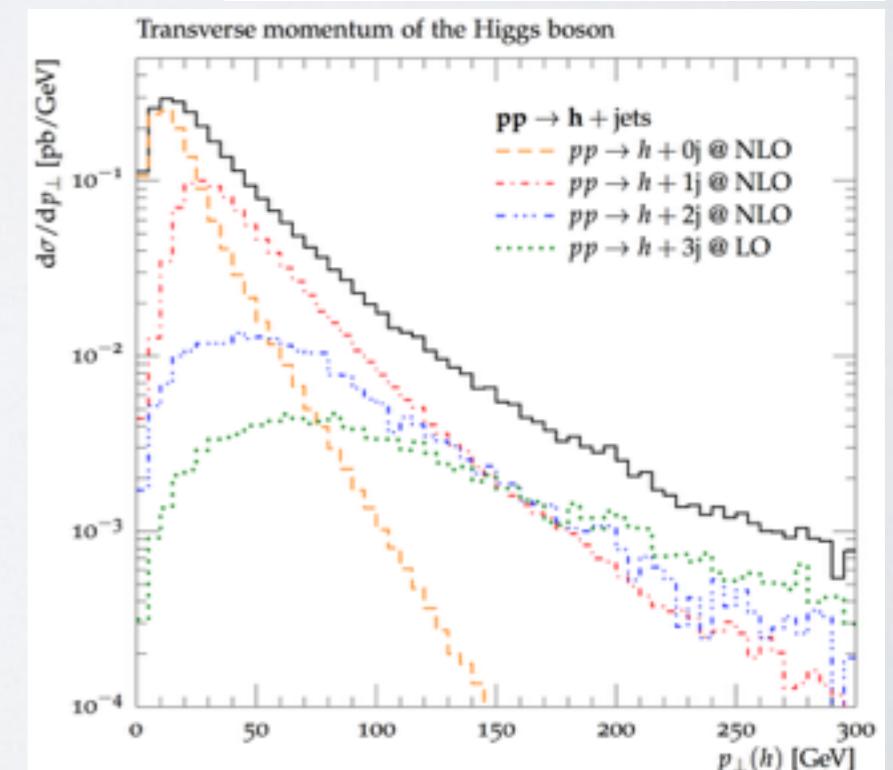
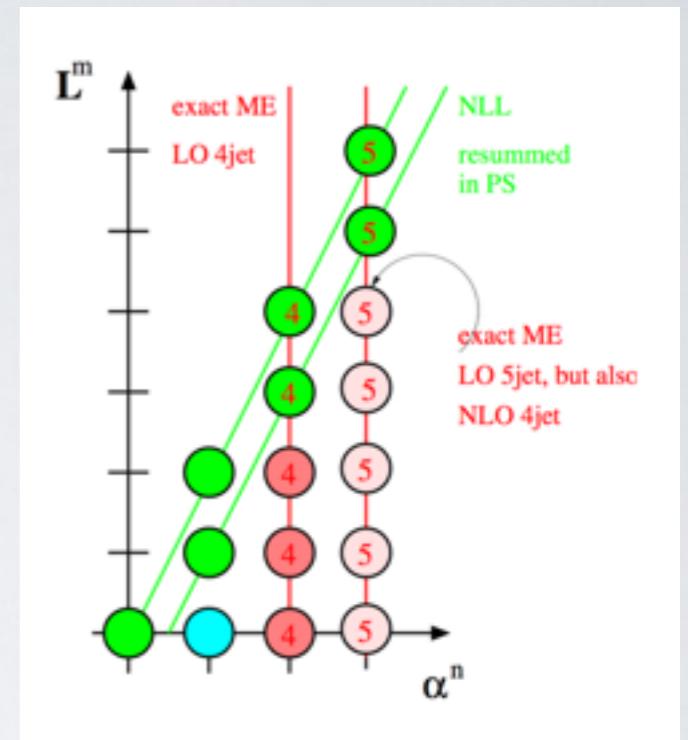
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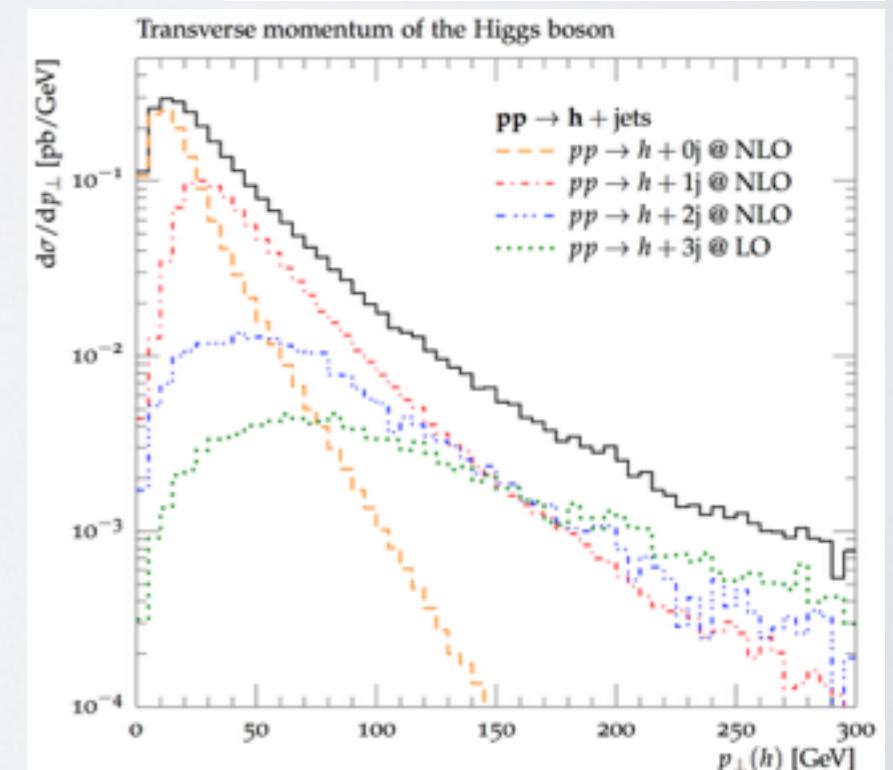
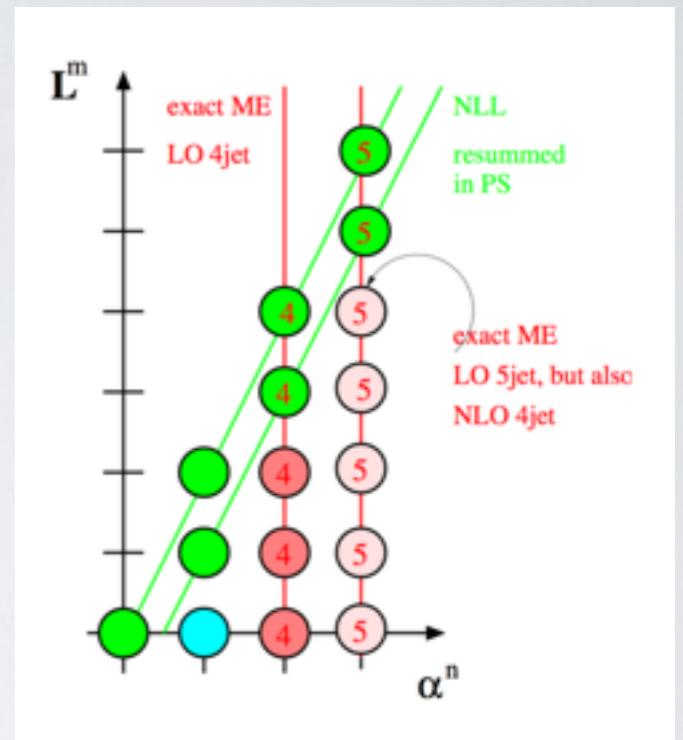


Inclusive jet samples: avoid double-counting

- Matrix elements populate hard regime
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- Separate regions by jet measure Q_j

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WIP: non-leading color, EW showers, access higher logs, spin



Hadronization / Fragmentation

- ▶ Quark and gluon jets hadronize at low energy scales (fragmentation)
- ▶ Non-perturbative physics: has to be extracted from experiment [mainly $e^+e^- \rightarrow$ hadrons, DIS]
- ▶ Old models [1970s]: flux tubes, independent fragmentation [Feynman/Field, 1970; Isajet]
- ▶ Independent fragmentation dresses bare quarks: “**last quark**”, Lorentz invariance, infrared safety

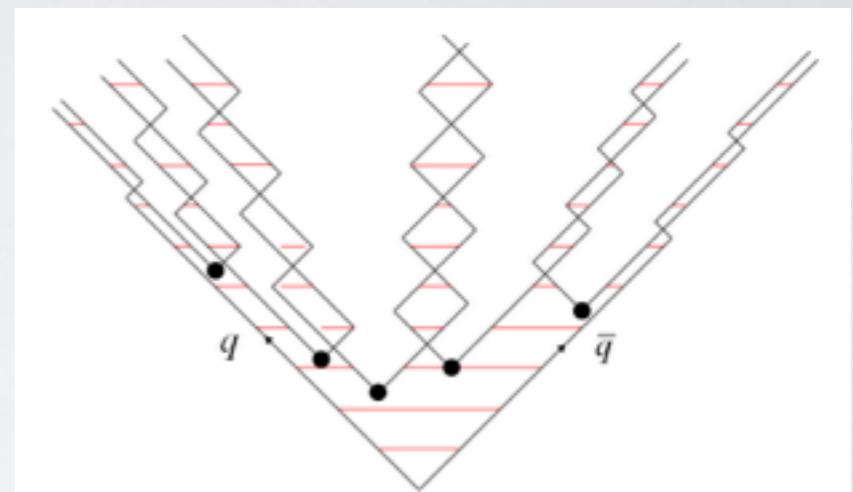


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Lund string fragmentation model [Pythia]

- based on old string model of strong interactions
- Strong physical motivation, but: invented without PS in mind
- Universal description of data (ee fit \rightarrow hadrons)
- Plethora of parameters: $\sim O(1)$ per hadron
- Baryon production difficult [string junctions, popcorn]

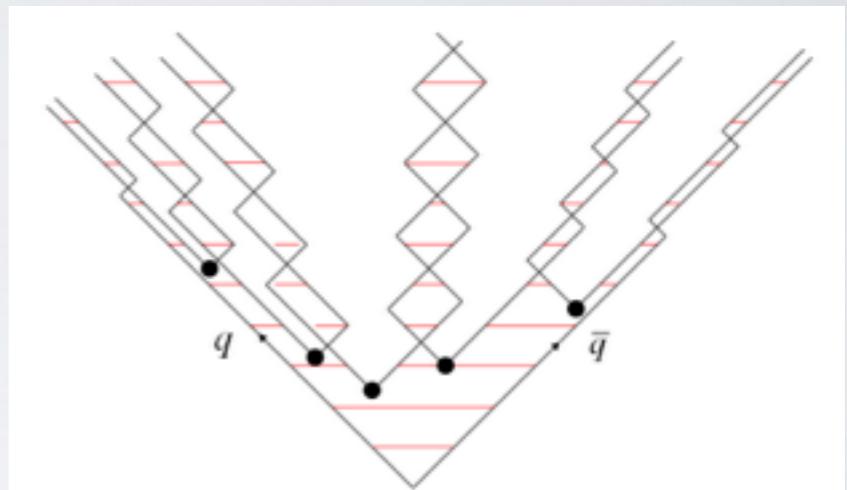


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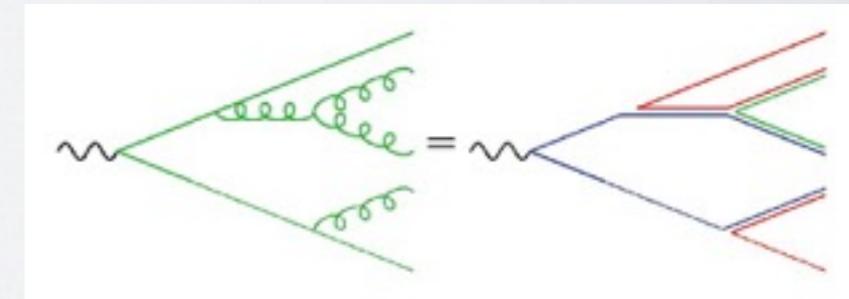
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Cluster fragmentation model [Herwig]

- ➊ Parton shower orders partons in color space
- ➋ Large N_c limit: planar graphs dominate
- ➌ Cluster: continuum of high-mass resonances, decay to hadrons
- ➍ No spin info, just plain phase space
- ➎ Cluster spectrum determined by PS (perturbation theory)

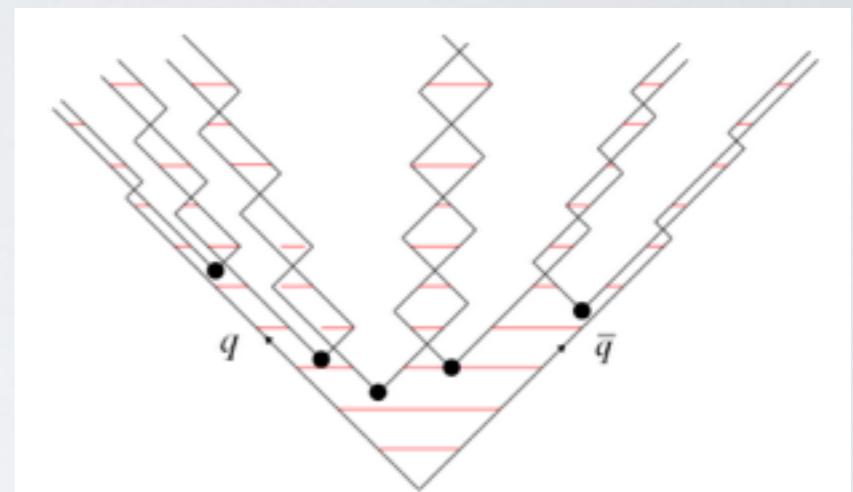


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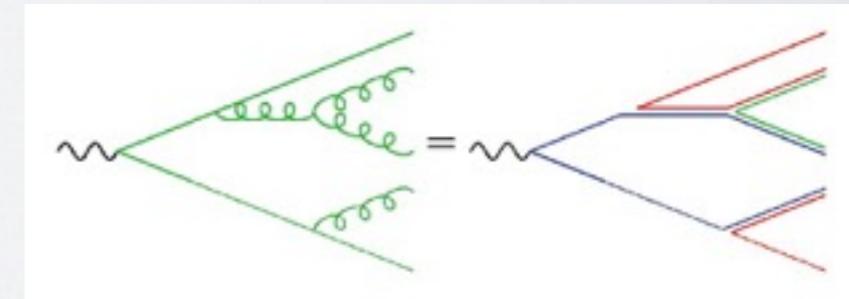
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All programs use either Lund or Cluster or a Hybrid version of both!



Hadronic decays / Hadronic radiation

A hadronic decay chain of typical complexity:

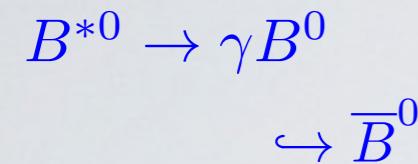


Radiative electromagnetic decay



Hadronic decays / Hadronic radiation

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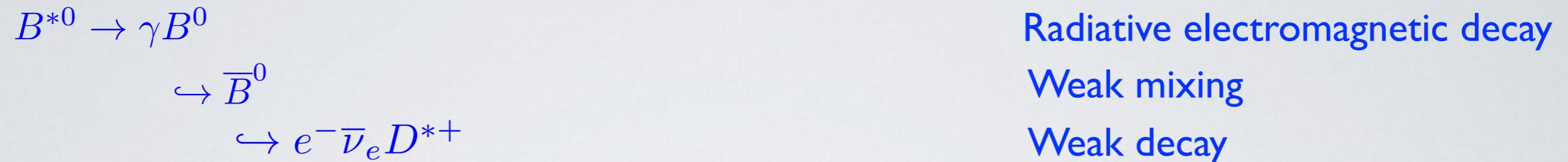


Radiative electromagnetic decay
Weak mixing



Hadronic decays / Hadronic radiation

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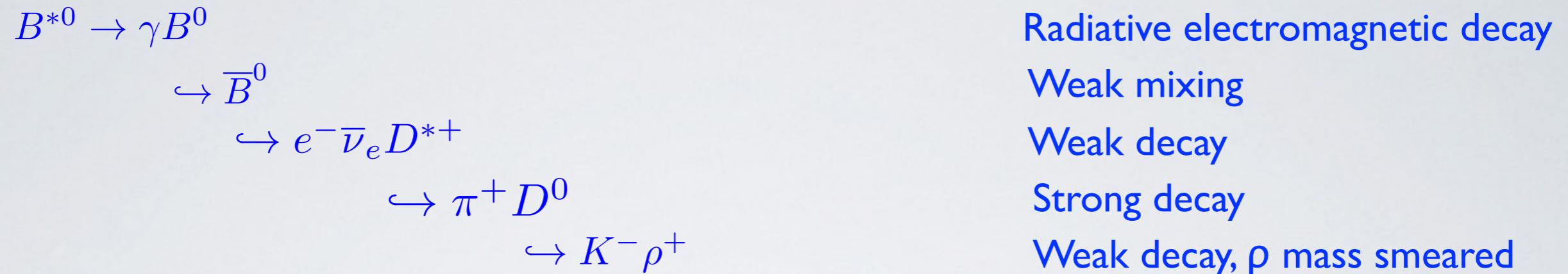
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$B^{*0} \rightarrow \gamma B^0$	Radiative electromagnetic decay
$\hookrightarrow \bar{B}^0$	Weak mixing
$\hookrightarrow e^- \bar{\nu}_e D^{*+}$	Weak decay
$\hookrightarrow \pi^+ D^0$	Strong decay
$\hookrightarrow K^- \rho^+$	Weak decay, ρ mass smeared
$\hookrightarrow \pi^+ \pi^0$	ρ^+ polarized, angular correlations



Hadronic decays / Hadronic radiation

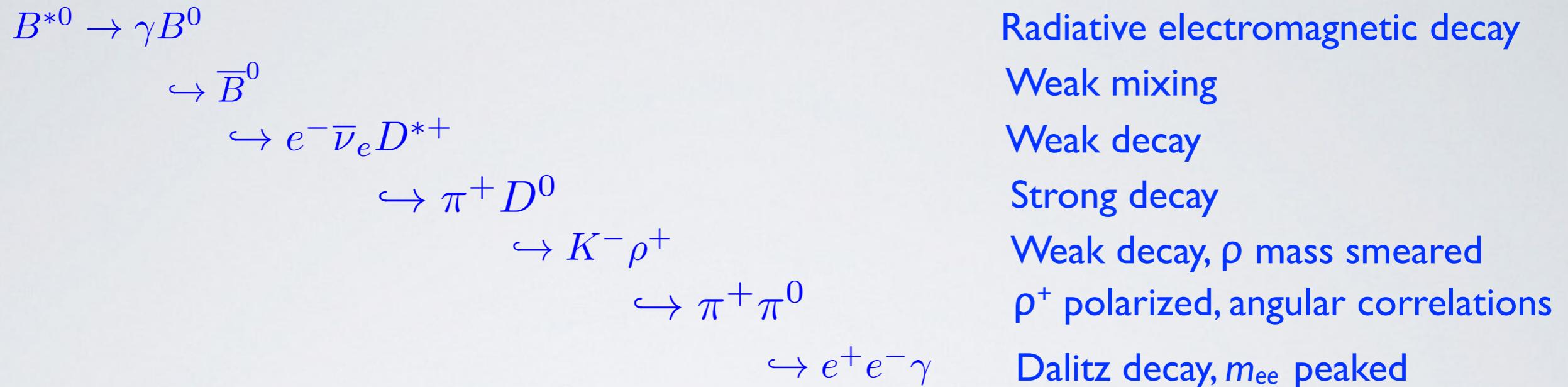
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Hadronic decays / Hadronic radiation

A hadronic decay chain of typical complexity:



PDG: 100s of particles, 1000s of decay modes, form factors, peak shapes, special cases, “PDG unitarity violation”



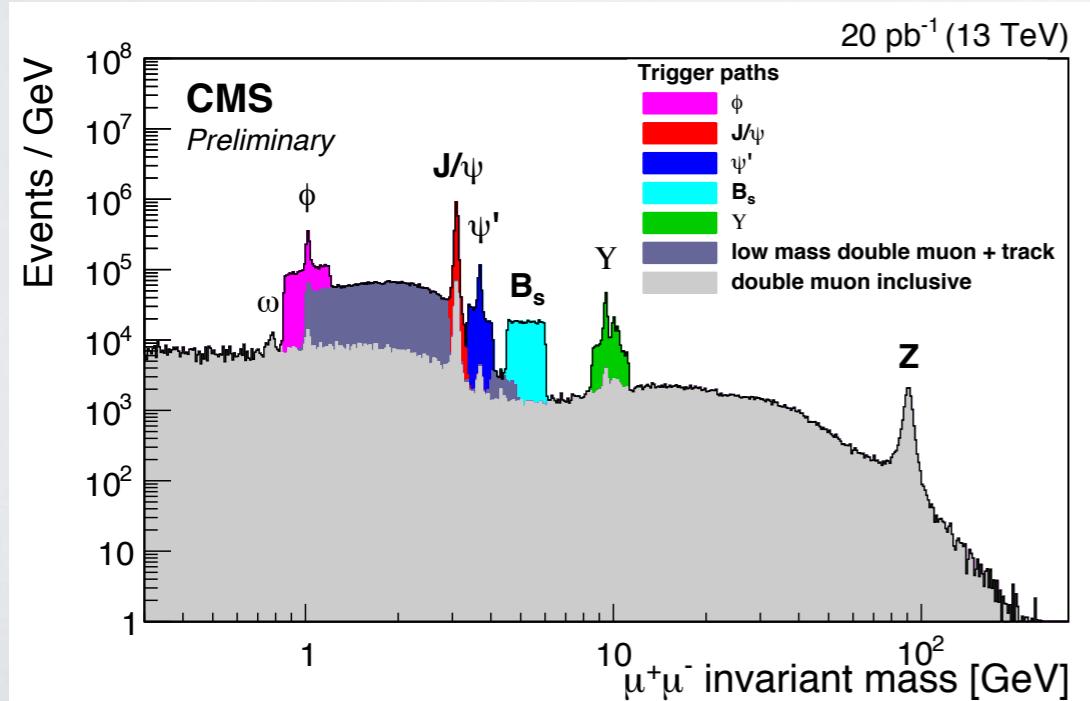
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A hadronic decay chain of typical complexity:

$$\begin{aligned} B^{*0} &\rightarrow \gamma B^0 && \text{Radiative electromagnetic decay} \\ &\rightarrow \bar{B}^0 && \text{Weak mixing} \\ &\rightarrow e^- \bar{\nu}_e D^{*+} && \text{Weak decay} \\ &\rightarrow \pi^+ D^0 && \text{Strong decay} \\ &\rightarrow K^- \rho^+ && \text{Weak decay, } \rho \text{ mass smeared} \\ &\rightarrow \pi^+ \pi^0 && \rho^+ \text{ polarized, angular correlations} \\ &\rightarrow e^+ e^- \gamma && \text{Dalitz decay, } m_{ee} \text{ peaked} \end{aligned}$$

Final-state hadronic QED
radiation for shower shapes
and correct distributions

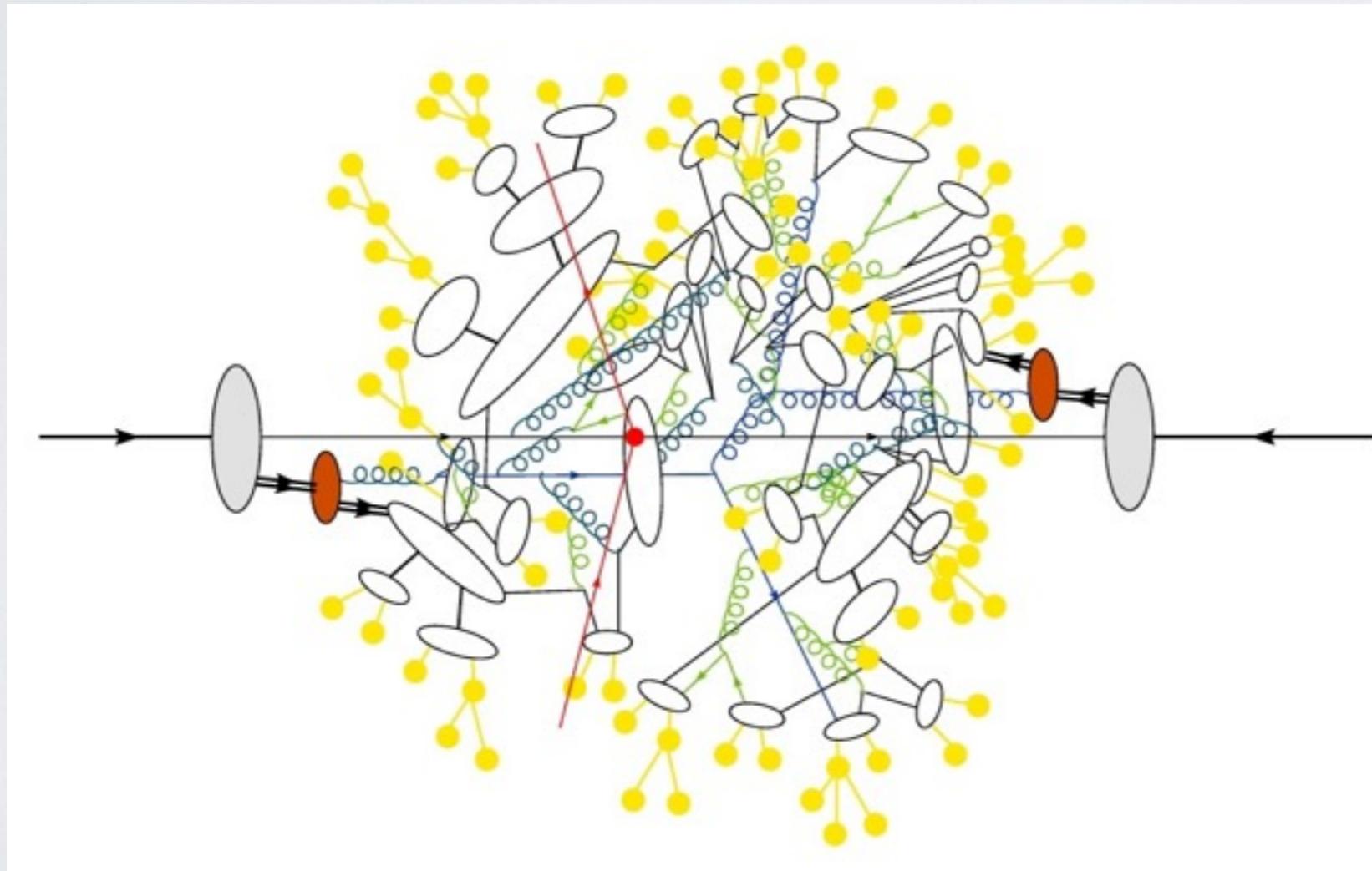
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Underlying Event

Many different definitions and names: UE, Multi-Parton interactions (MI, MPI), Minimum Bias

- “everything that is not of interest”
- multiple parton interaction from same hadron
- Beam remnants: soft interactions with interleaved ISR
- **Phenomenological models**
- e.g. eikonal approximation to optical theorem
- Lots of dirty details



Best reference:
[Pythia manual \[Sjöstrand et al.\]](#)

General Searches for New Physics

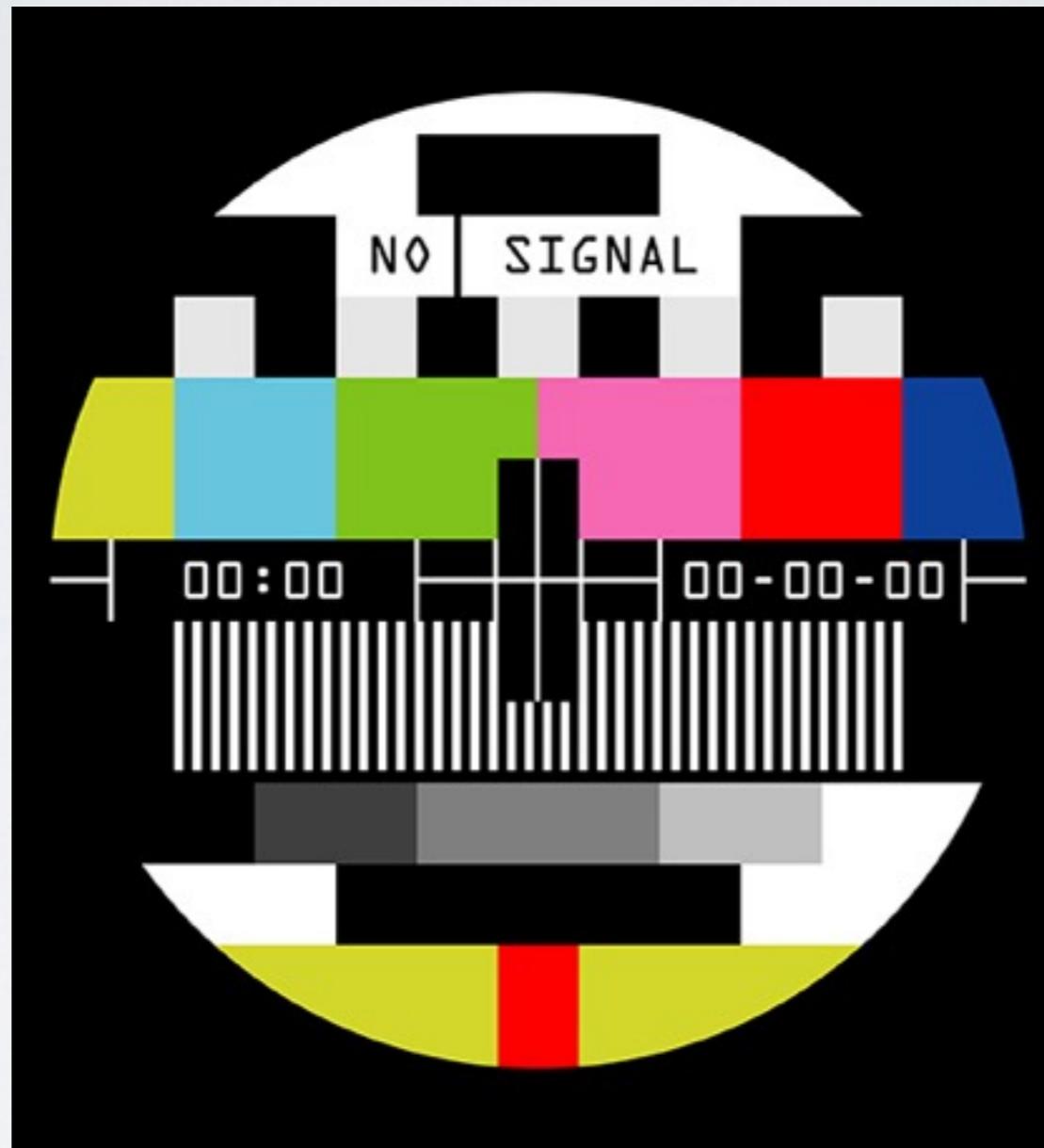


*“If I’d only knew **which** haystack....”*

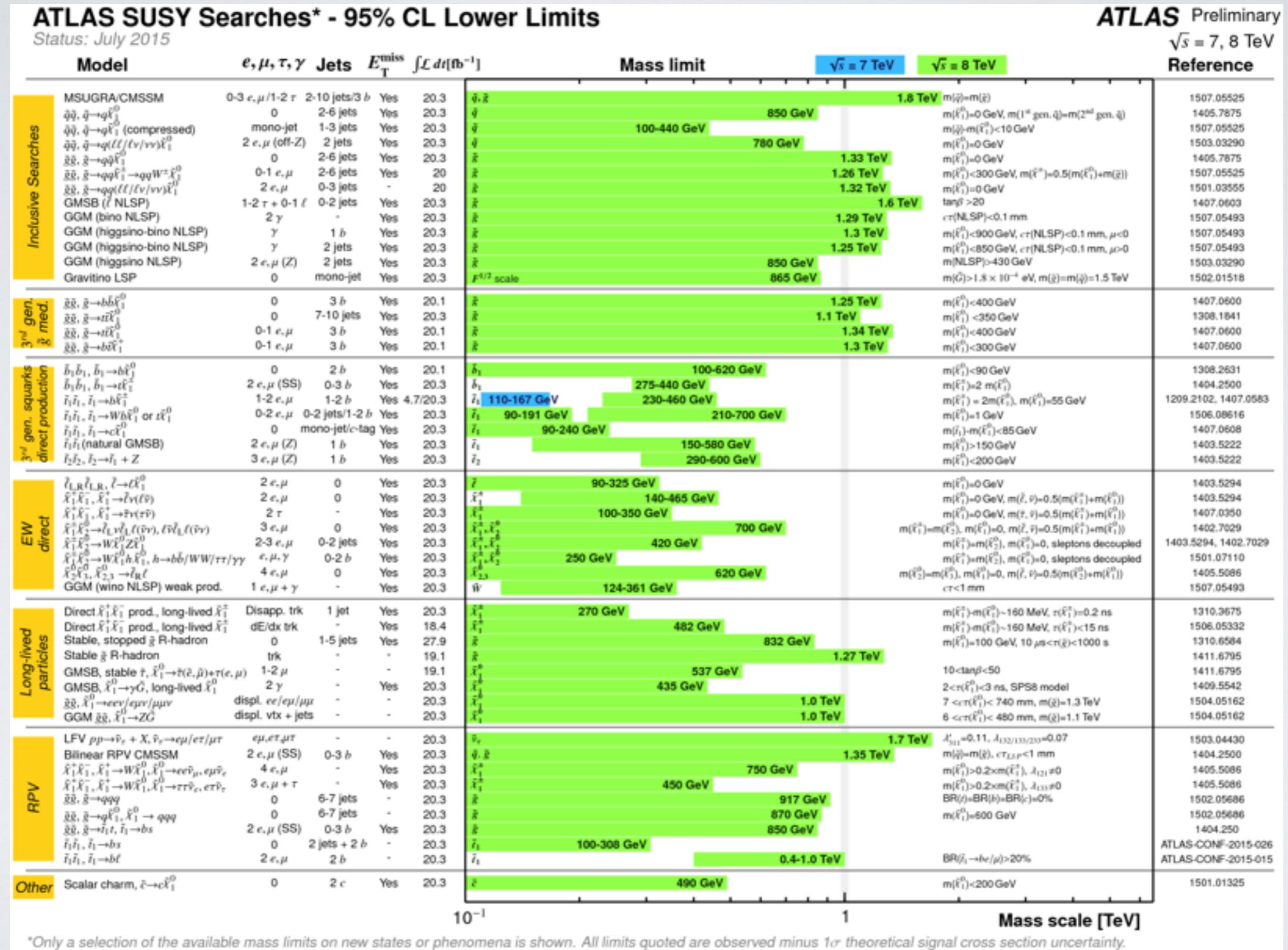
Status in 2015, incl. 13 TeV data



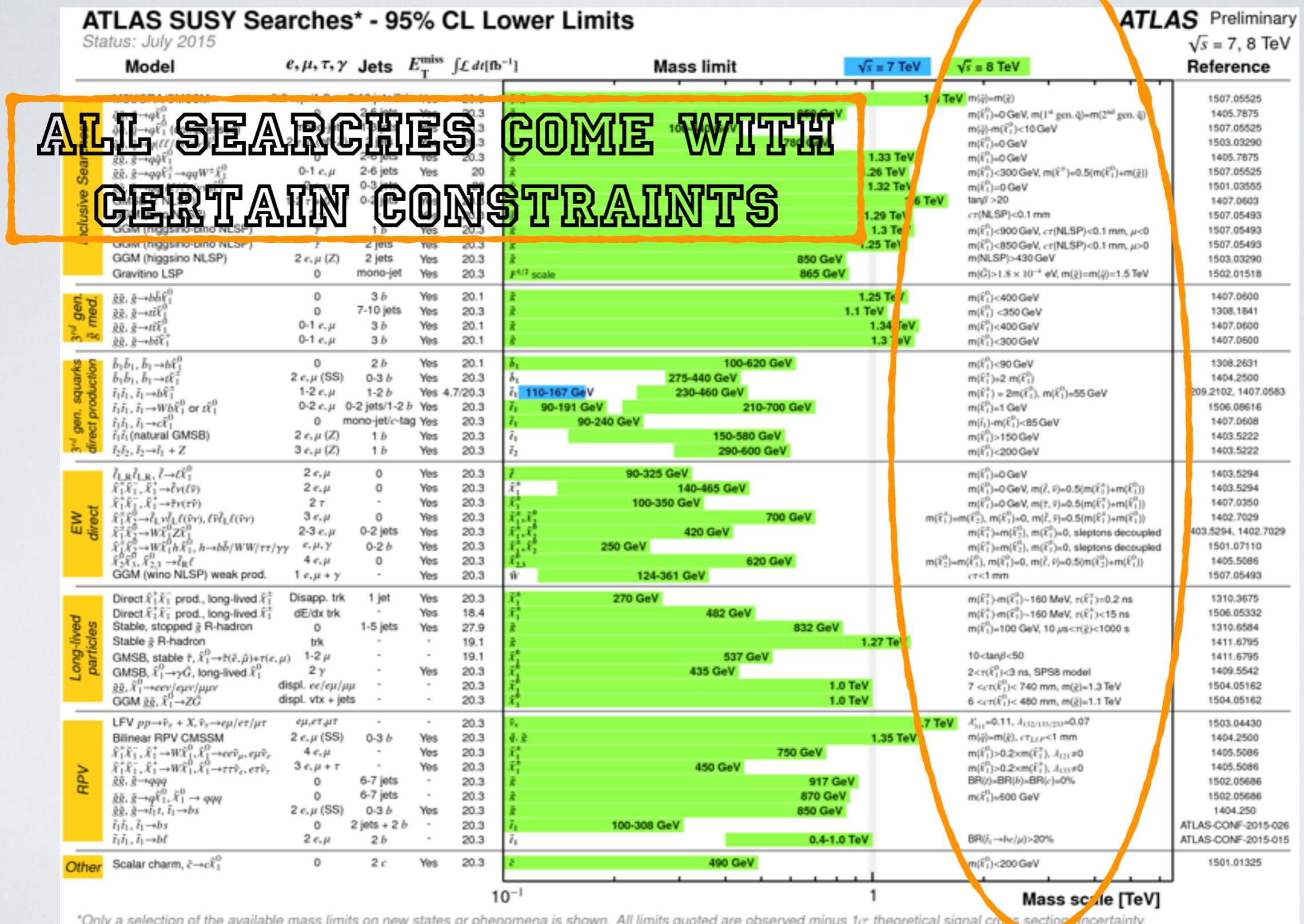
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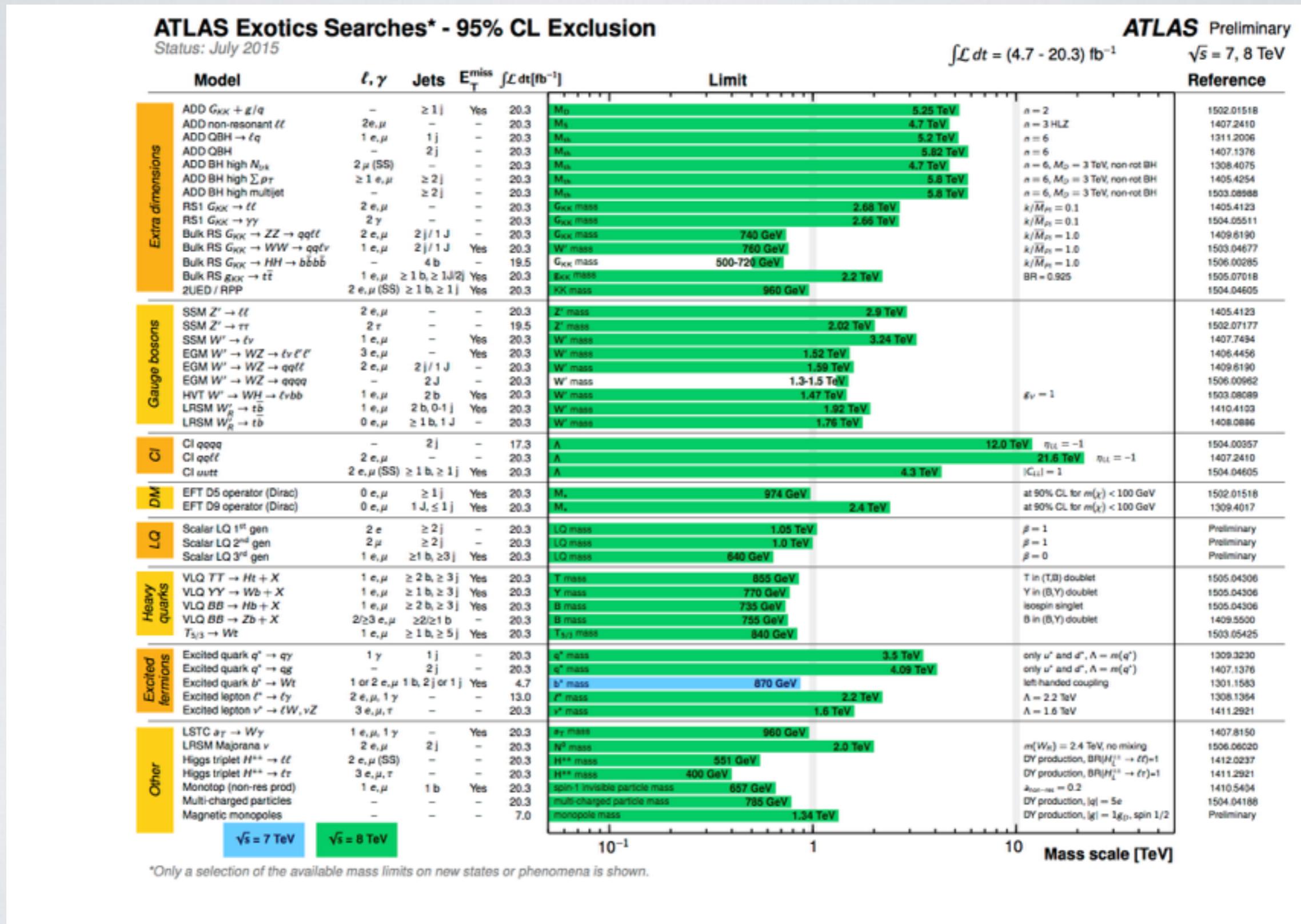
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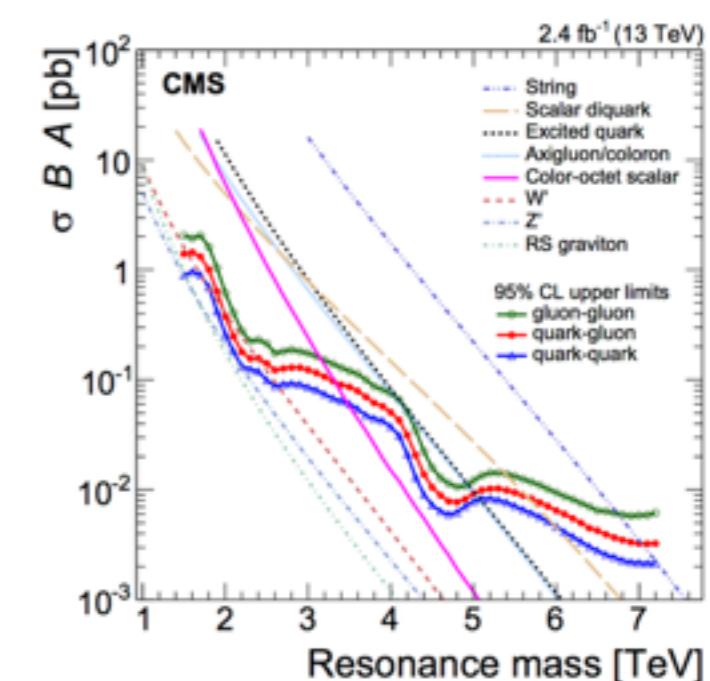
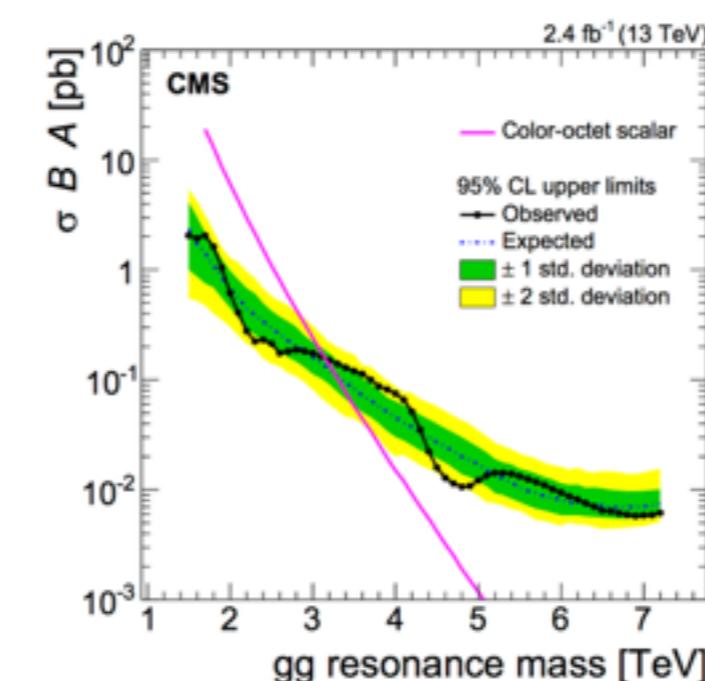
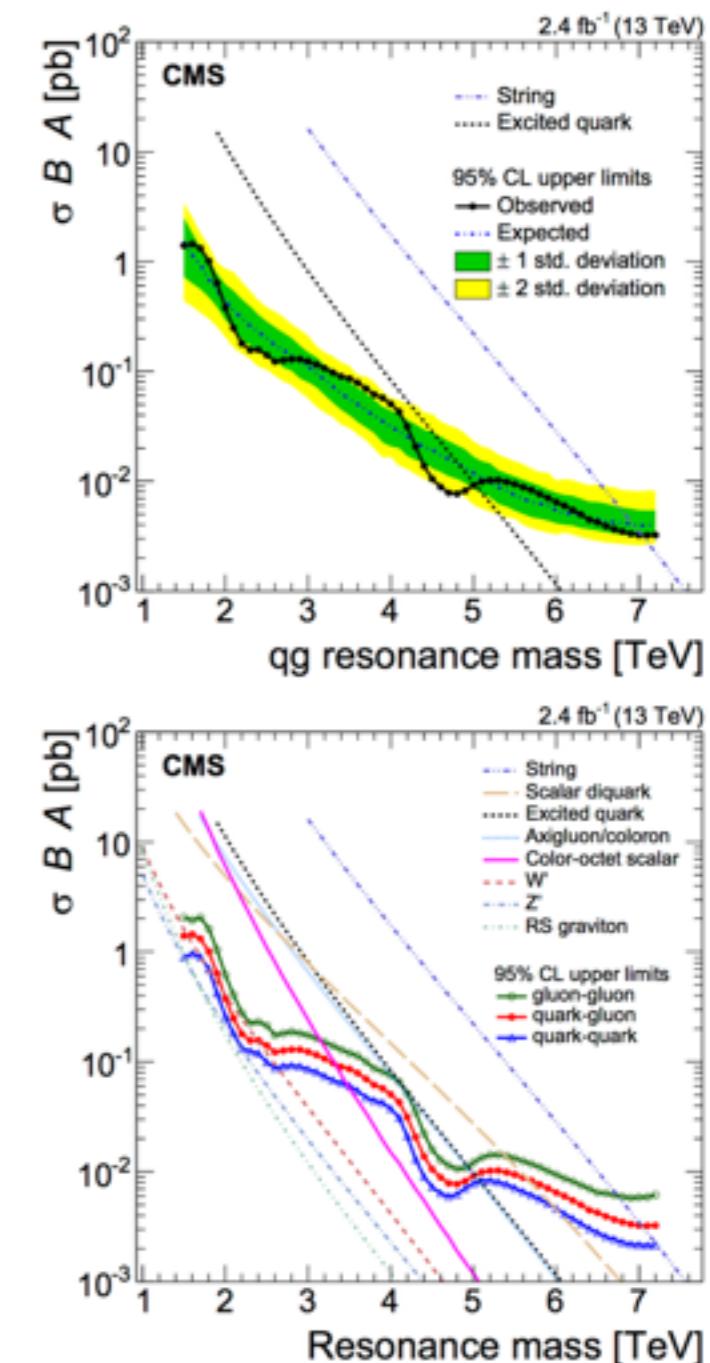
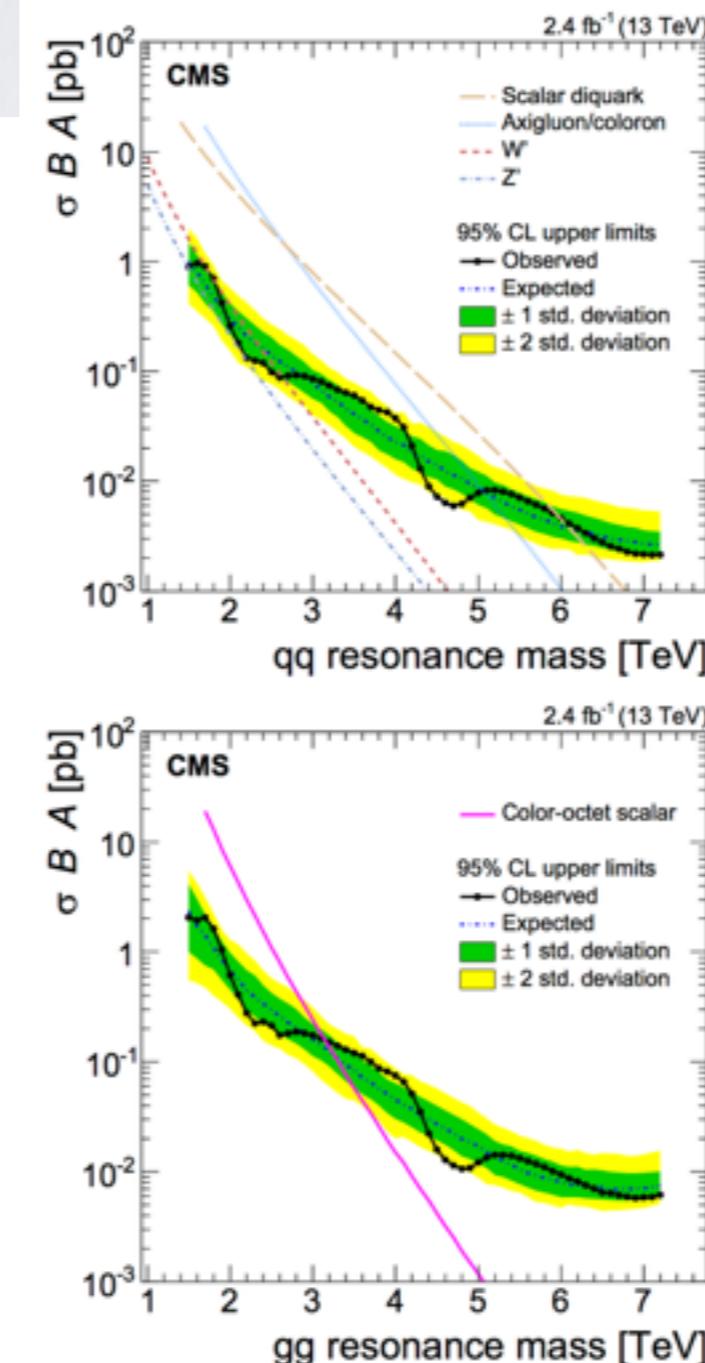
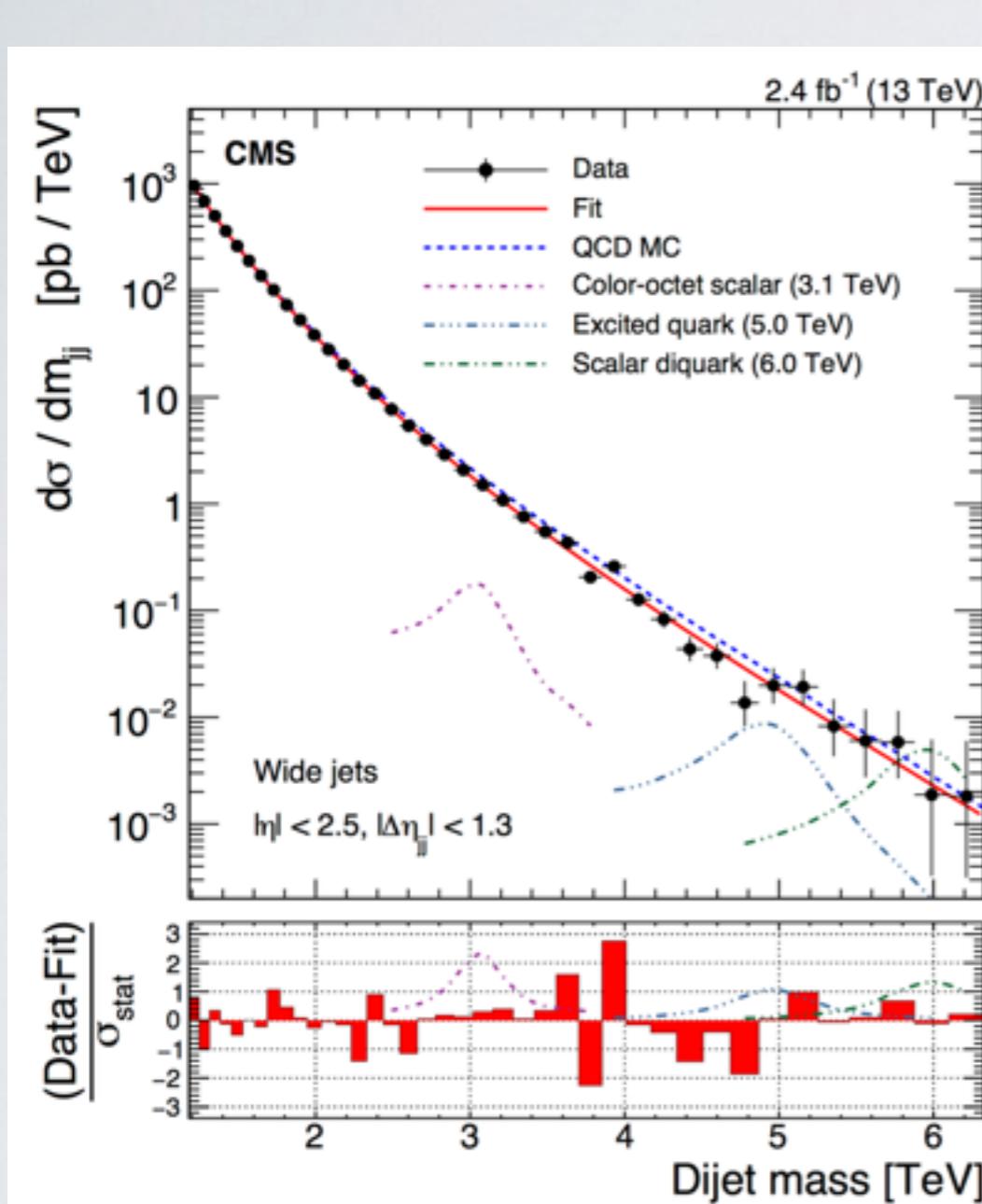
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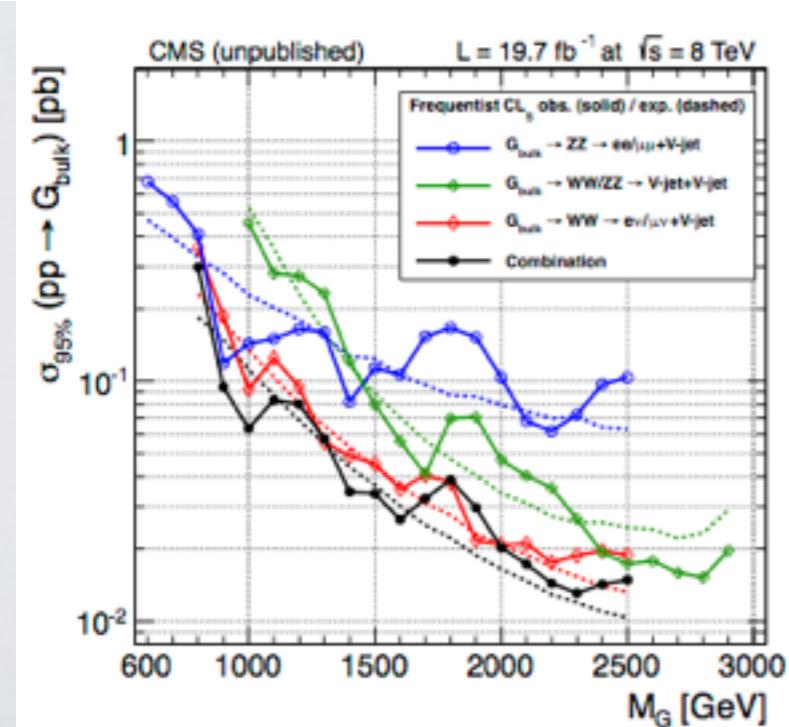
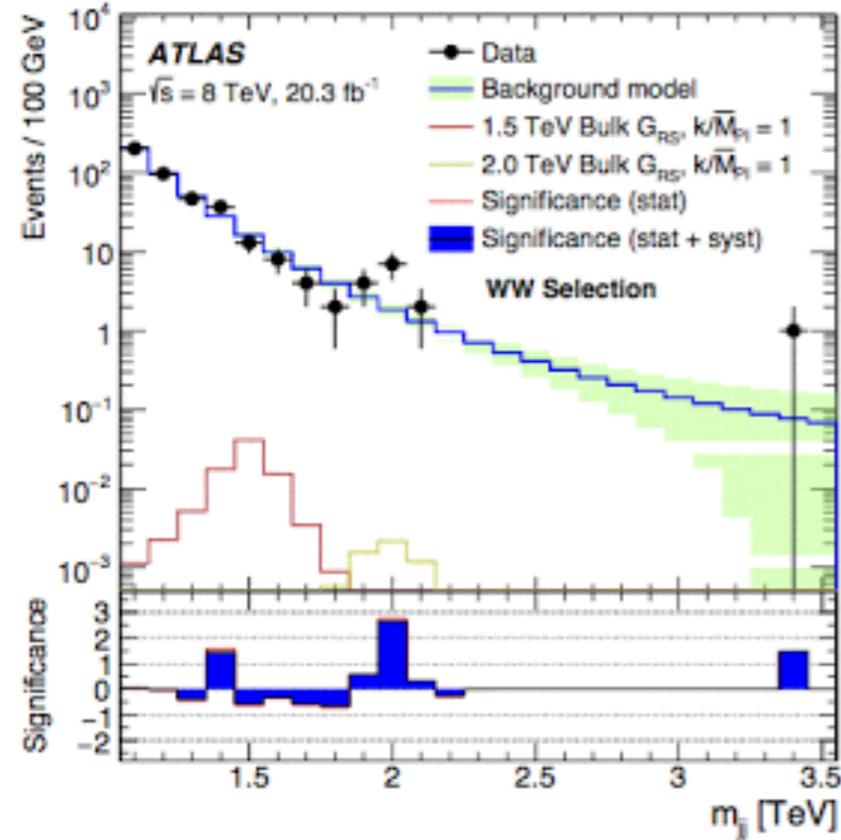


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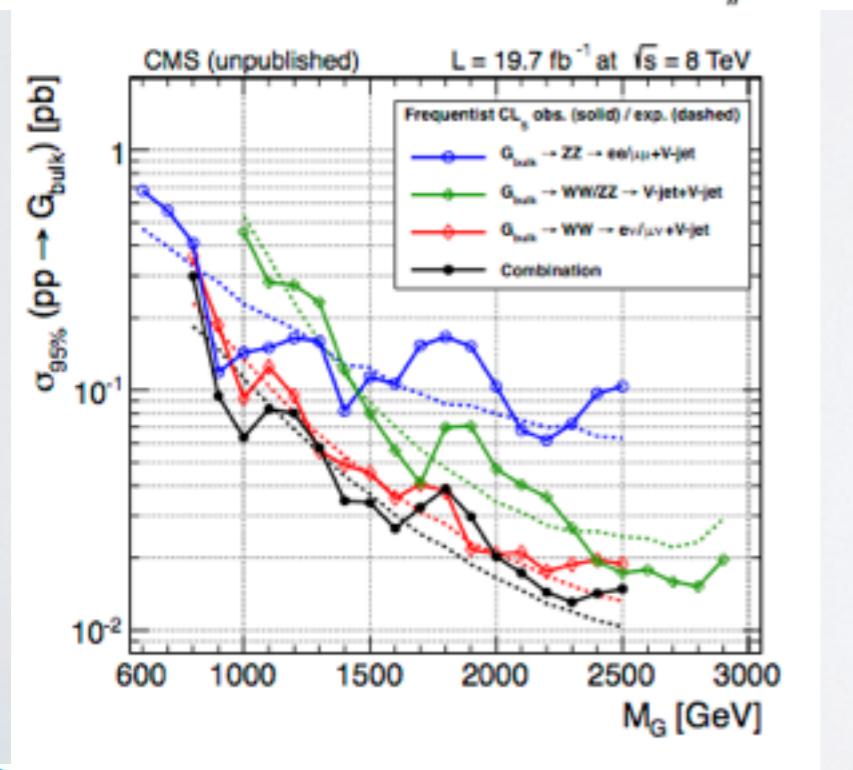
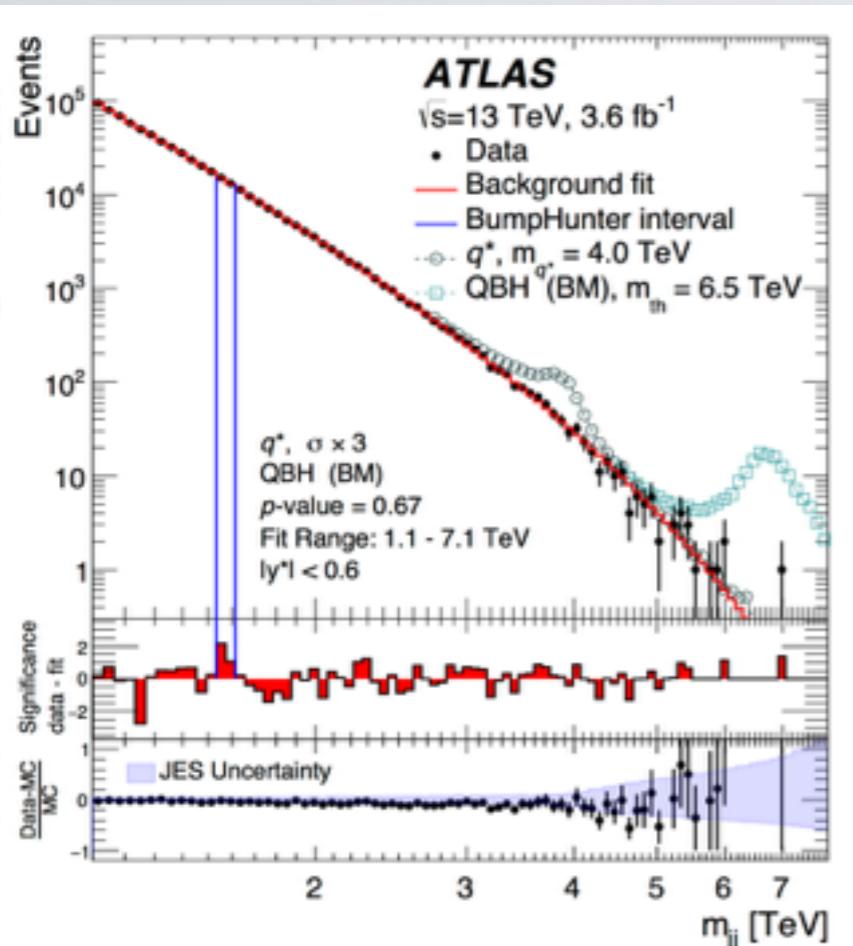
CMS, 12/2015

A new hope or the SM strikes back?



ATLAS diboson “bump”; CMS upward fluctuation [gone for the moment @ 13 TeV]

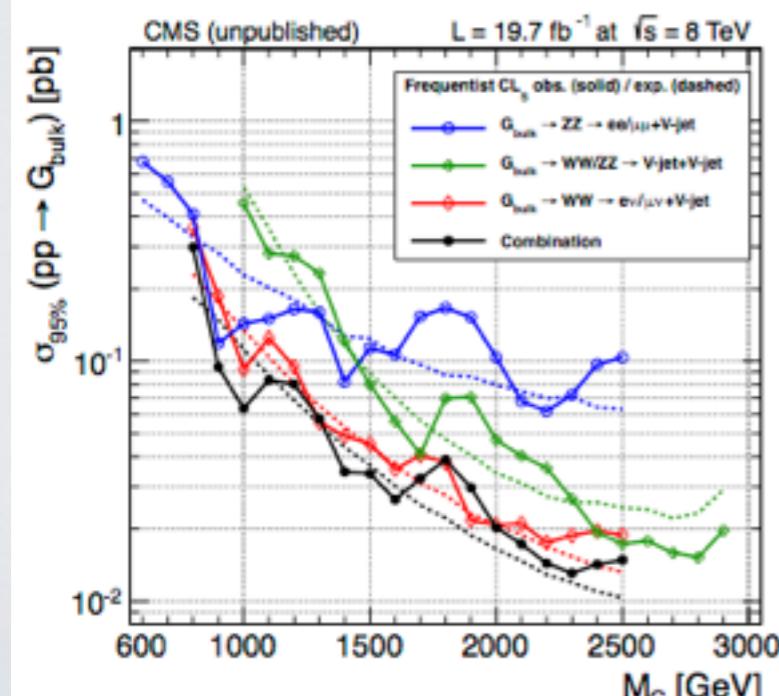
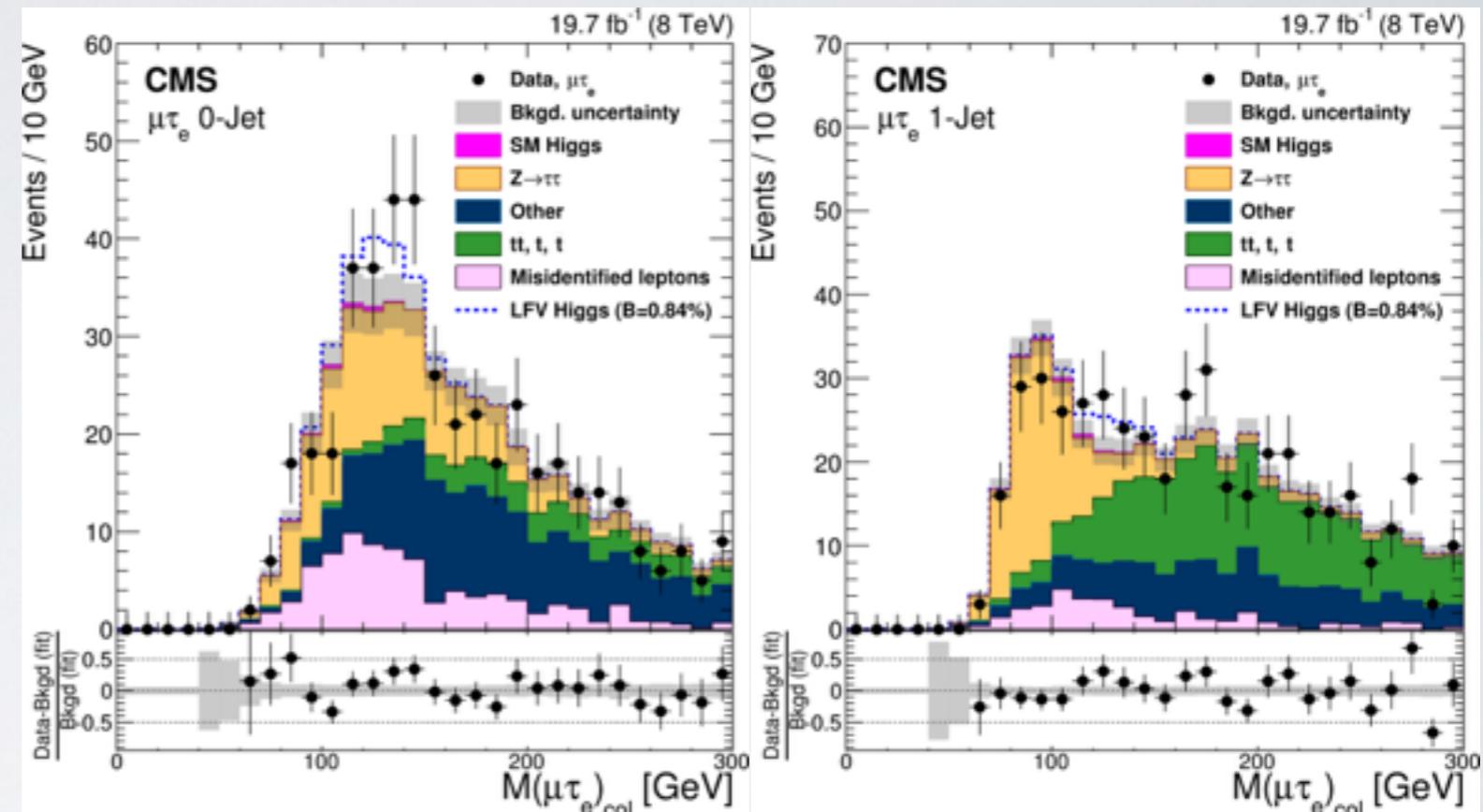
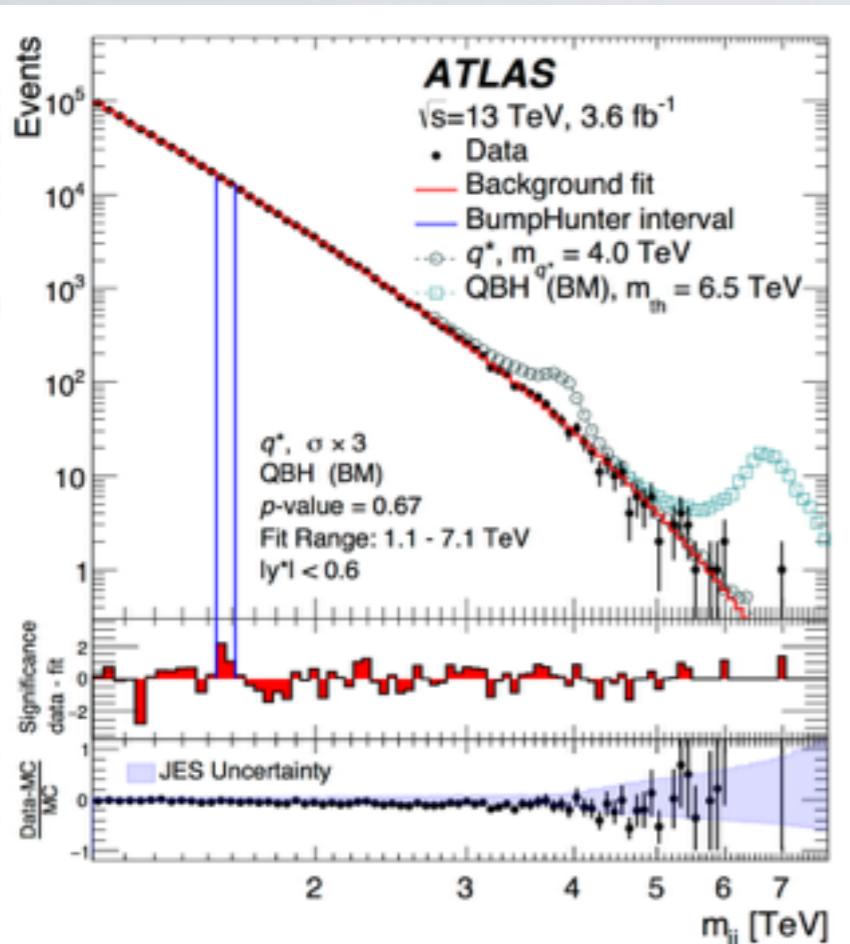
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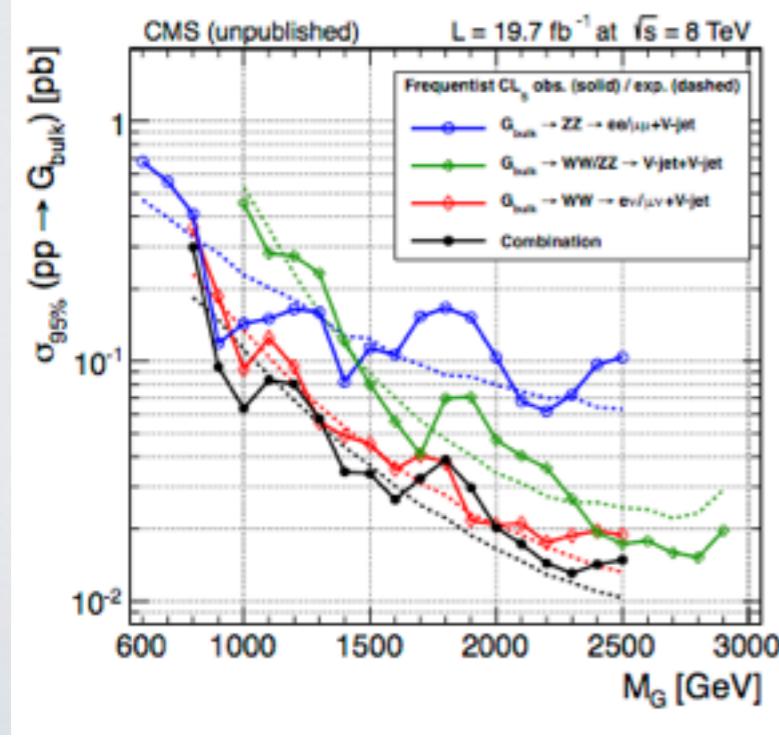
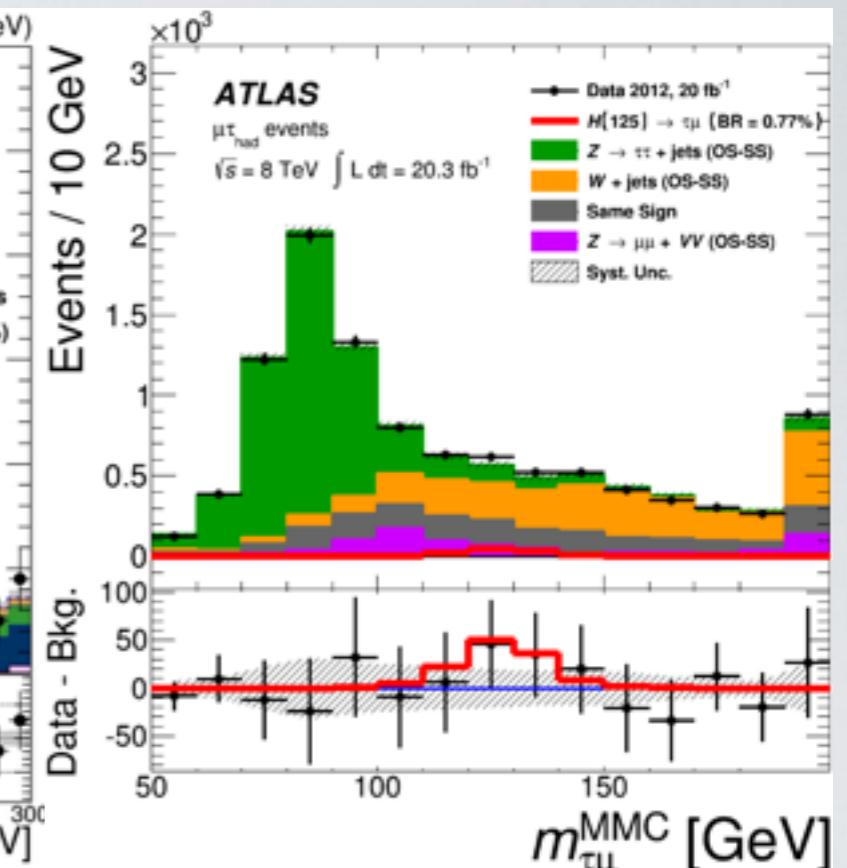
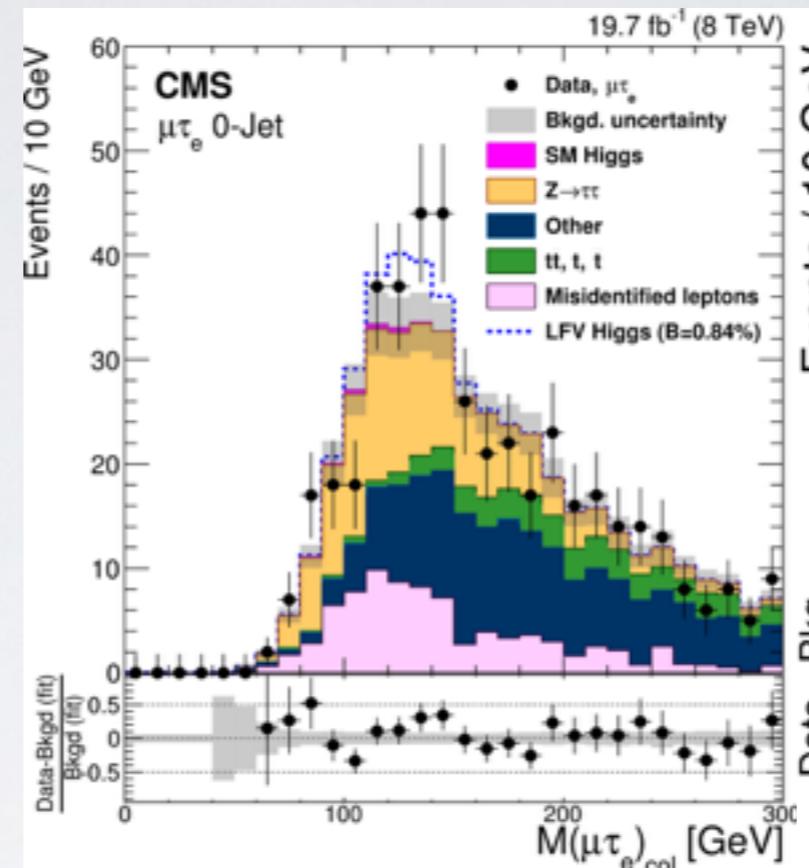
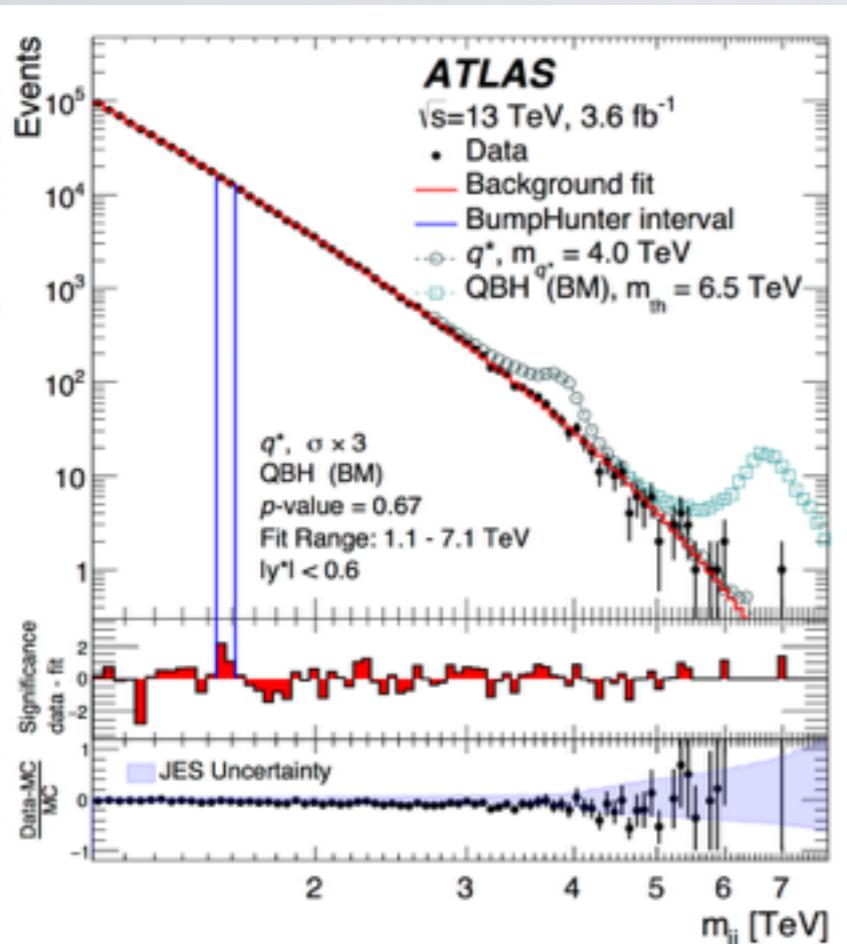
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Flavour-Violating Higgs decay $h(125) \rightarrow \mu\tau$ in ATLAS/CMS

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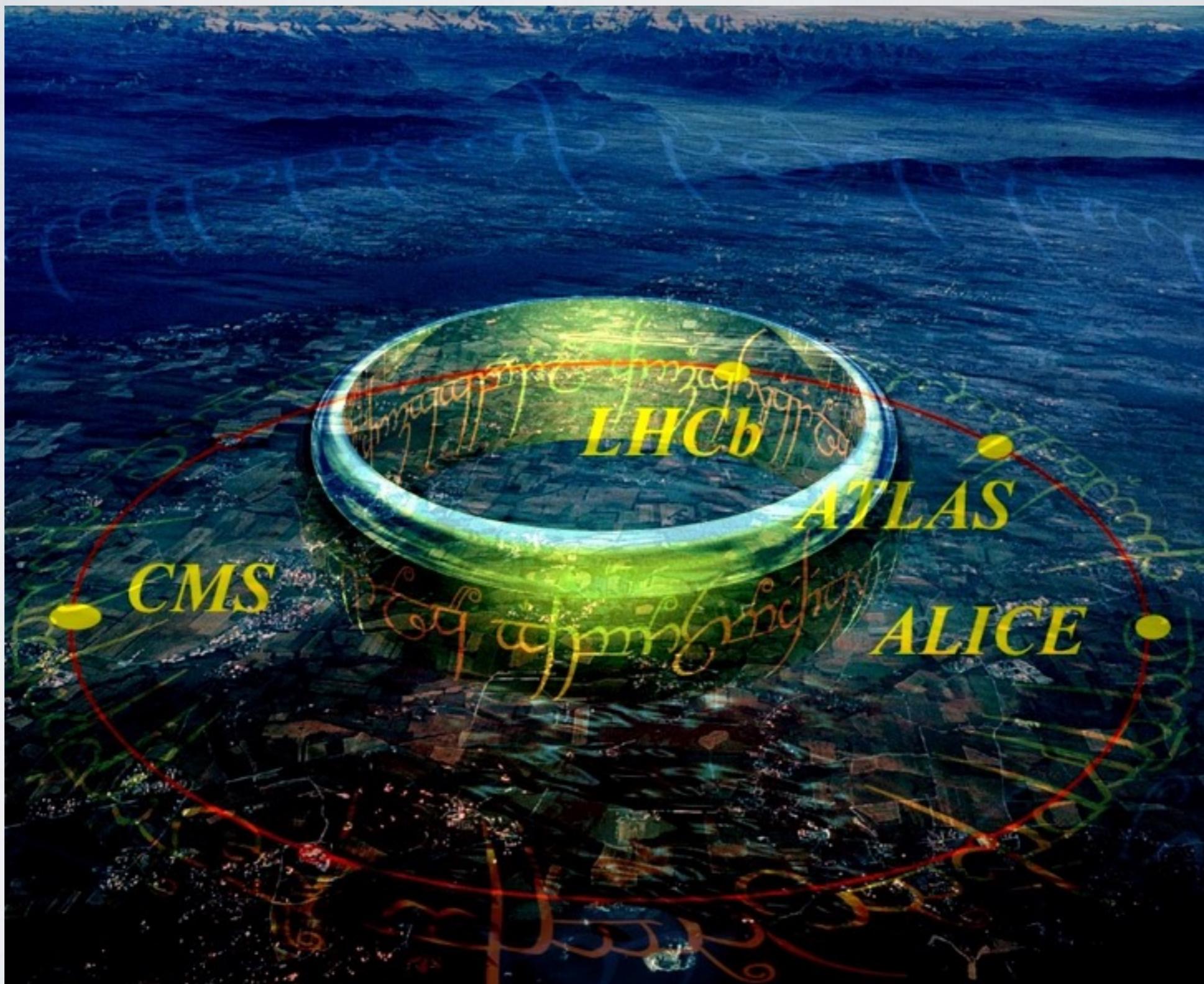
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Conclusions and Outlook



One Ring to Find Them ... One Ring to Rule Them Out?



... and the future comes ...

ILC Candidate site in Kitakami, Tohoku

