

Status of Little Higgs Models in 2013

Jürgen Reuter

DESY

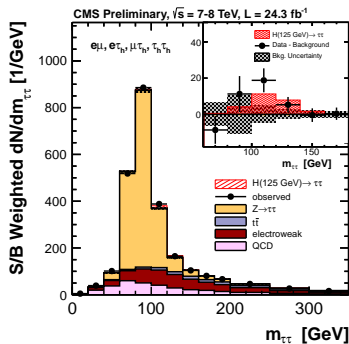
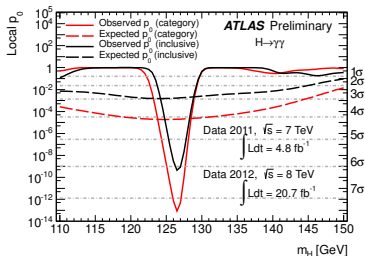
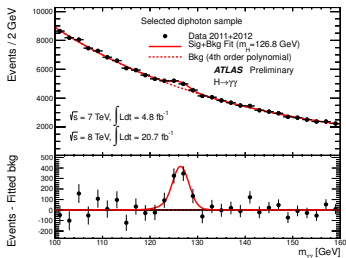


JRR/Tonini/de Vries, arXiv:1309.xxxx; arXiv:1307.5010; JRR/Tonini, JHEP **1302** (2013) 077; Kilian/JRR/Rainwater **PRD 74** (2006), 095003; **PRD 71** (2005), 015008; Kilian/JRR **PRD 70** (2004), 015004

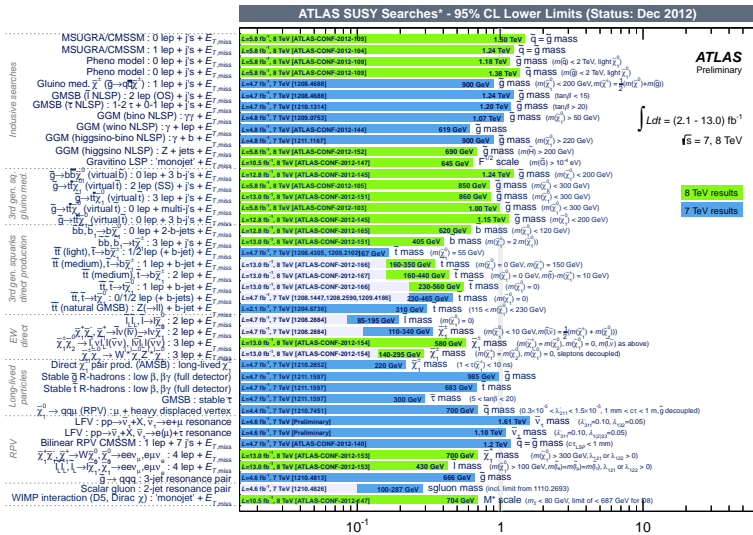
Seminar, U. of Pittsburgh, Pittsburgh, 17.9.2013

Standard Model Triumph:

- ▶ 2012: Discovery of a Higgs boson

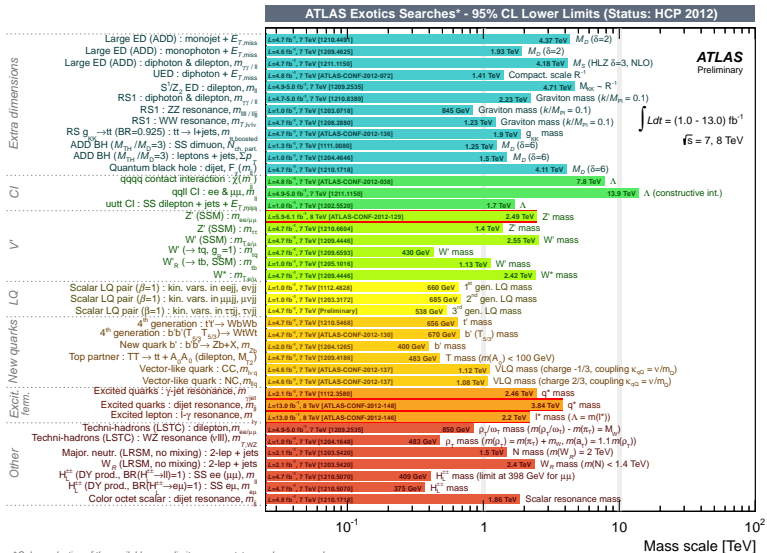


... and what now?



* Only a selection of the available mass limits on new states or phenomena shown.
All limits quoted are observed minus 1 σ theoretical signal cross section uncertainty.

... and what now?

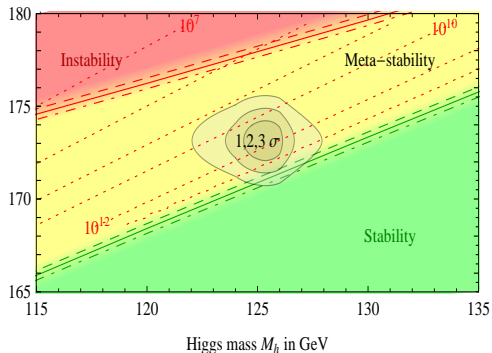
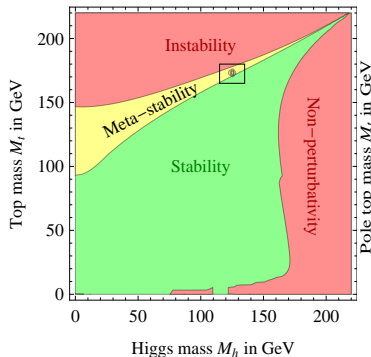


Electroweak vacuum stability

- ▶ Most recent analysis: **Metastable vacuum with lifetime longer than the age of the universe** Degrassi et al., arXiv:1205.6497

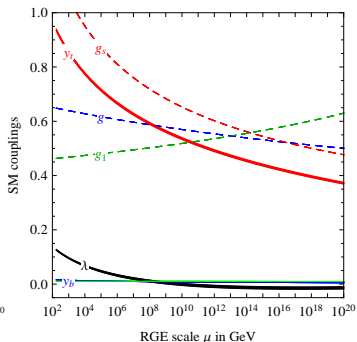
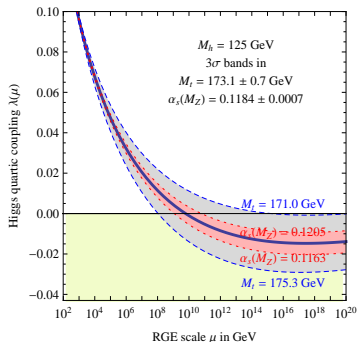
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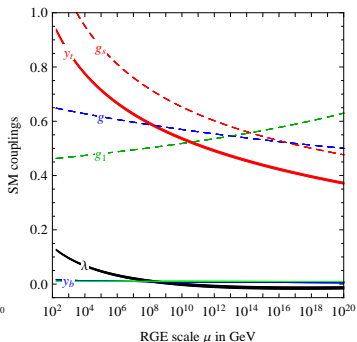
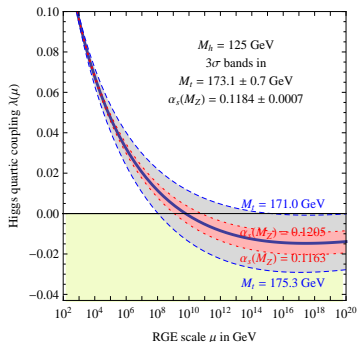
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- Could the Higgs field ever have fallen in the correct vacuum?** Hertzberg, arXiv:1210.3624

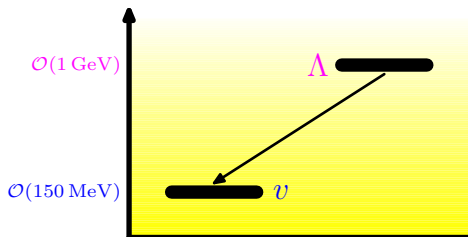
Higgs as Pseudo-Goldstone boson

Nambu-Goldstone Theorem: For each *spontaneously broken global symmetry generator* there is a **massless boson** in the spectrum.

Old idea:

Georgi/Pais, 1974; Georgi/Dimopoulos/Kaplan, 1984

Light Higgs as **(Pseudo)-Goldstone boson** of a spontaneously broken global symmetry



Analogous: QCD

Scale Λ : chiral symmetry breaking, quarks, $SU(3)_c$

Scale v : pions, kaons, ...

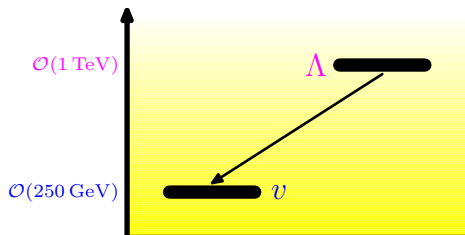
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Scale Λ : global symmetry breaking, new particles, new (gauge) IA

Scale v : Higgs, W/Z , ℓ^\pm , ...

Without Fine-Tuning: experimentally excluded

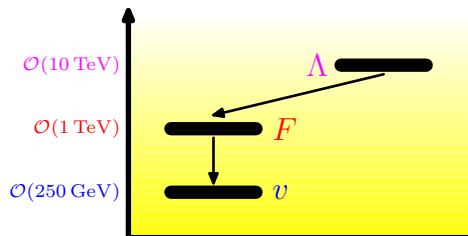
Collective symmetry breaking and 3-scale models

Collective symmetry breaking: Arkani-Hamed/Cohen/Georgi/Nelson/..., 2001

2 different global symmetries; one of them unbroken \Rightarrow Higgs
exact Goldstone boson

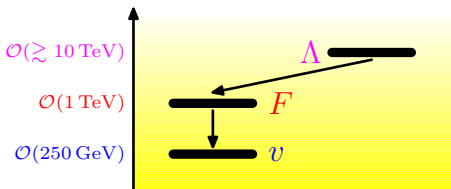
Coleman-Weinberg: boson masses by radiative corrections, but: m_H only at 2-loop level

$$m_H \sim \frac{g_1}{4\pi} \frac{g_2}{4\pi} \Lambda$$



Scale Λ : global SB, new IA
Scale F : Pseudo-Goldstone bosons, new vectors/fermions
Scale v : Higgs, W/Z , ℓ^\pm , ...

Characteristics and Spectra



Scale Λ : “hidden sector”,
symmetry breaking

Scale F : new particles

Scale v : $h, W/Z, \ell^\pm, \dots$

Terascale: new particles to stabilize the hierarchy

SUSY

\tilde{q}_L ——— \tilde{t}_2
 \tilde{b}_2 ——— \tilde{q}_R
 \tilde{b}_1 ———
 ——— \tilde{t}_1

H, A ——— H^\pm

h ———

$\tilde{\tau}_2$ ——— $\tilde{\ell}_L$
 $\tilde{\nu}_\ell$ ——— $\tilde{\ell}_R$
 $\tilde{\tau}_1$ ——— $\tilde{\ell}_R$

$\tilde{\chi}_4^0, \tilde{\chi}_2^\pm$ ———
 $\tilde{\chi}_3^0$ ———

$\tilde{\chi}_2^0, \tilde{\chi}_1^\pm$ ———
 t ———
 $\tilde{\chi}_1^0$ ———

$M[\text{TeV}]$

Φ ———
 Φ^\pm ——— $\Phi^{\pm\pm}$
 Φ_P ———

h ———

η ———

Little Higgs

Z' ——— W'^\pm ——— T ———

γ' ———

U, C ———

W^\pm ——— Z ———

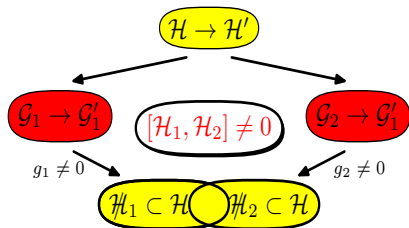
t ———

Generic properties of Little-Higgs models

- Extended global symmetry (extended scalar sector)
- **Specific functional form of the potential**
- Extended gauge symmetry: $\gamma' \equiv A_H, Z' \equiv Z_H, W'^{\pm} \equiv W_H$
- New heavy fermions: T , but also U, C, \dots

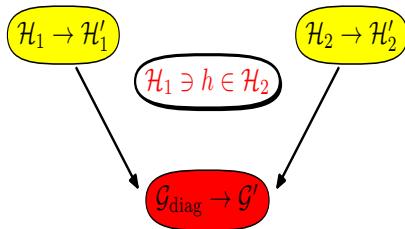
Product Group Models

(e.g. Littlest Higgs)



Simple Group Models

(e.g. Simplest Little Higgs)



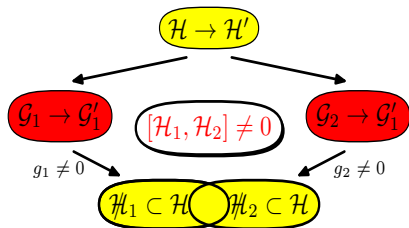
- discrete $T(\text{TeV})$ parity: pair production, cascades, DM

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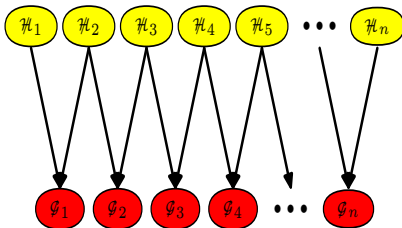
Product Group Models

(e.g. Littlest Higgs)



Moose Models

(e.g. Minimal Moose Model)



- **discrete $T(\text{TeV})$ parity: pair production, cascades, DM**

Prime Example: Simple Group Model

- ▶ enlarged gauge group: $SU(3) \times U(1)$; globally $U(3) \rightarrow U(2)$
- ▶ **Two** nonlinear Φ representations $\mathcal{L} = |D_\mu \Phi_1|^2 + |D_\mu \Phi_2|^2$

$$\Phi_{1/2} = \exp \left[\pm i \frac{f_{2/1}}{f_{1/2}} \Theta \right] \begin{pmatrix} 0 \\ 0 \\ f_{1/2} \end{pmatrix} \quad \Theta = \frac{1}{\sqrt{f_1^2 + f_2^2}} \begin{pmatrix} \eta & 0 & h^* \\ 0 & \eta & \\ h^T & & \eta \end{pmatrix}$$

Coleman-Weinberg mechanism: Radiative generation of potential

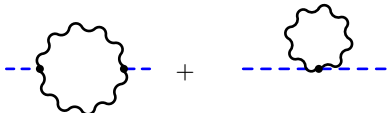
$$= \frac{g^2}{16\pi^2} \Lambda^2 (|\Phi_1|^2 + |\Phi_2|^2) \sim \frac{g^2}{16\pi^2} f^2$$

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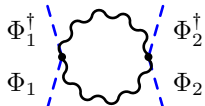
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$$= \frac{g^2}{16\pi^2} \Lambda^2 (|\Phi_1|^2 + |\Phi_2|^2) \sim \frac{g^2}{16\pi^2} f^2$$

but:



$$= \frac{g^4}{16\pi^2} \log \left(\frac{\Lambda^2}{\mu^2} \right) |\Phi_1^\dagger \Phi_2|^2 \Rightarrow \frac{g^4}{16\pi^2} \log \left(\frac{\Lambda^2}{\mu^2} \right) f^2 (h^\dagger h)$$

Cancellations of Divergencies in Yukawa sector

$$\propto \int \frac{d^4 k}{(2\pi)^4} \frac{1}{k^2(k^2 - m_T^2)} \left\{ \lambda_t^2(k^2 - m_T^2) + k^2 \lambda_T^2 - \frac{m_T}{F} \lambda_T k^2 \right\}$$

Little Higgs global symmetry imposes relation

$$\frac{m_T}{F} = \frac{\lambda_t^2 + \lambda_T^2}{\lambda_T}$$

 \Rightarrow

Quadratic divergence cancels

Collective Symm. break-

ing: $\lambda_t \propto \lambda_1 \lambda_2$, $\lambda_1 = 0$
 or $\lambda_2 = 0 \Rightarrow SU(3) \rightarrow [SU(3)]^2$

$$\sim \frac{\lambda_1^2 \lambda_2^2}{16\pi^2} \log \left(\frac{\Lambda^2}{\mu^2} \right) |\Phi_1^\dagger \Phi_2|^2$$

Constraints from Oblique Corrections: S, T, U

$$\Delta T \sim \Delta\rho \sim \Delta M_Z^2 Z \cdot Z$$

$$\Delta S \sim W^0{}_{\mu\nu} B^{\mu\nu}, \Delta U \sim W^0{}_{\mu\nu} W^{0\mu\nu}$$

◇ All low-energy effects order v^2/F^2 (Wilson coefficients)

$\Delta S, \Delta T$ in the Littlest Higgs model, violation of **Custodial SU(2)**: Csáki et al., 2002; Hewett et al., 2002; Han et al., 2003; Chen/Dawson, 2003; Kilian/JRR, 2003

$$\frac{\Delta S}{8\pi} = - \left[\frac{c^2(c^2-s^2)}{g^2} + 5 \frac{c'^2(c'^2-s'^2)}{g'^2} \right] \frac{v^2}{F^2} \rightarrow 0 \quad \alpha \Delta T \rightarrow \frac{5}{4} \frac{v^2}{F^2} - \frac{2v^2 \lambda_{2\phi}^2}{M_\phi^4} \gtrsim \frac{v^2}{F^2}$$

Constraints from **contact IA**: $(f_{JJ}^{(3)}, f_{JJ}^{(1)})$ $4.5 \text{ TeV} \lesssim F/c^2$ $10 \text{ TeV} \lesssim F/c'^2$

◇ **Constraints evaded** $\iff c, c' \ll 1$
 B', Z', W'^{\pm} superheavy ($\mathcal{O}(\Lambda)$) decouple from fermions

Motivation

How to constrain a generic model in *HEP*?

- ▶ direct searches of resonances
- ▶ electroweak precision tests
- ▶ flavour constraints
- ▶ nowadays: Higgs sector

Higgs sector is the key to understand EW-scale physics (and beyond?)

Statistical analysis

We considered the three most popular Little Higgs models:

- ▶ Simplest Little Higgs (*SLH*) [Schmaltz]
- ▶ Littlest Higgs (*L²H*) [Arkani-Hamed et al.]
- ▶ Littlest Higgs with *T*-parity (*LHT*) [Low et al.]

and realized a χ^2 analysis on their parameter spaces, taking into account the whole set of 7+8 TeV Higgs searches by *ATLAS* and *CMS*, and by fitting 21 different *EW* Precision Observables:

$$\chi^2 = \sum_i \frac{(\mathcal{O}_i - \mathcal{O}_i^{\text{exp}})^2}{\sigma_i^2}$$

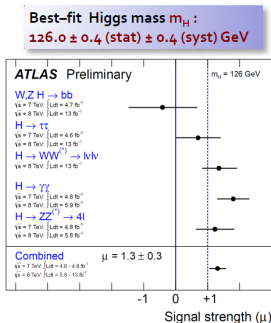
where \mathcal{O}_i depends on the free parameters of the model considered.

Data used: Higgs sector

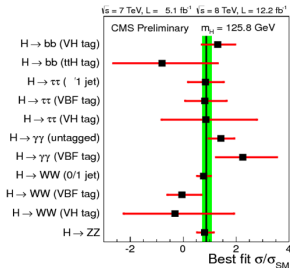
the Higgs results are expressed in terms of a *signal strength modifier*

$$\mu_i = \frac{\sum_p \epsilon^p_i \sigma_p}{\sum_p \epsilon^p_i \sigma_p^{SM}} \cdot \frac{BR(h \rightarrow X_i X_i)}{BR(h \rightarrow X_i X_i)_{SM}}$$

we included in our χ^2 analysis the best-fit values of μ_i reported by the Collaborations for all the different 7+8 TeV channels i :



- $M=125.8 \pm 0.4$ (stat) ± 0.4 (syst) GeV



- $\sigma/\sigma_{SM}=0.88 \pm 0.21$

Data used: *EWPD*

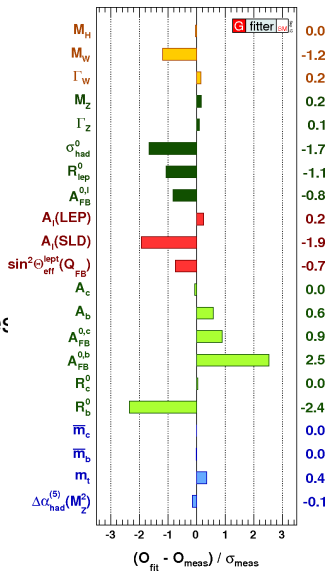
every extension of *SM* has to satisfy at least the precision constraints of the electroweak sector:

- ▶ low-energy observables

e.g. ν -scattering, parity violation observables

- ▶ Z -pole observables

e.g. m_Z , Γ_Z , Z -pole asymmetries...



LH Smoking guns

Where do the LH corrections to the SM quantities come from?

- ▶ new decay channels of the Higgs, e.g. $h \rightarrow A_H A_H$ in LHT
- ▶ modified Higgs couplings with SM fermions and vector bosons

$$\text{e.g. } 2 \frac{m_W^2}{v} y_W h W^+ W^-, \quad y_W = \begin{cases} 1 & SM \\ 1 + \mathcal{O}(v^2/f^2) & LH \end{cases}$$

- ▶ interaction terms of Higgs with new fermions/vector bosons

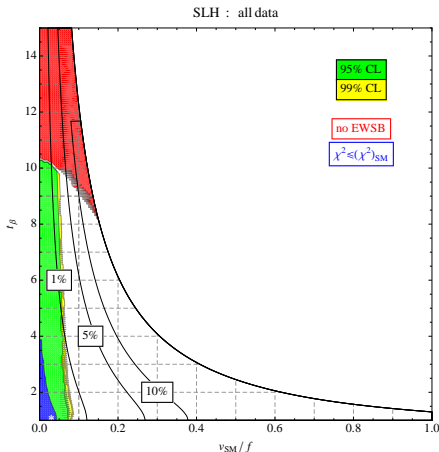
$$\text{e.g. } \frac{m_T}{v} y_T h \bar{T} T \quad m_T \sim f, \quad y_T \sim \mathcal{O}(v^2/f^2)$$

- ▶ modified neutral- and charged-currents

$$\text{e.g. } \frac{g}{c_W} \sum_f \bar{f} \gamma^\mu \left((g_L^{SM} + \delta g_L) P_L + (g_R^{SM} + \delta g_R) P_R \right) f Z_\mu$$

SLH results

JRR/Tonini, JHEP 1302 (2013) 077



- ▶ free parameters: f SSB scale, t_{β} ratio of vevs of scalar fields $\phi_{1,2}$
- ▶ $f_{\min}^{99\%} = 2.88$ TeV, translates into lower bounds on new states' masses, e.g.

$$m_{W'} \gtrsim 1.35 \text{ TeV}$$

$$m_T \gtrsim 2.81 \text{ TeV}$$

- ▶ min. required fine tuning: $\sim 1\%$, defined as

$$\Delta = \frac{|\delta\mu^2|}{\mu_{\text{obs}}^2}$$

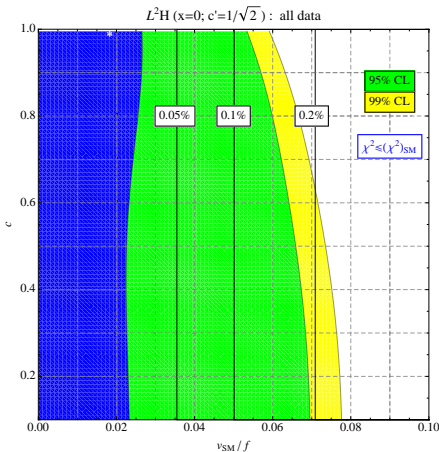
- ▶ results mainly driven by *EWPD*

$$\chi_{\min}^2/\text{d.o.f.} = 1.043$$

$$\chi_{SM}^2/\text{d.o.f.} = 1.048$$

L^2H results

JRR/Tonini, JHEP 1302 (2013) 077



- ▶ free parameters: f SSB scale, c mixing angle in gauge sector
- ▶ $f_{\min}^{99\%} = 3.20$ TeV, translates into lower bounds on new states' masses, e.g.

$$m_{W'} \gtrsim 2.13 \text{ TeV}$$

$$m_T \gtrsim 4.50 \text{ TeV}$$

- ▶ min. required fine tuning: $\sim 0.1\%$, defined as

$$\Delta = \frac{|\delta\mu^2|}{\mu_{\text{obs}}^2}$$

- ▶ results mainly driven by *EWPD*

$$\chi_{\min}^2/\text{d.o.f.} = 1.048$$

$$\chi_{SM}^2/\text{d.o.f.} = 1.049$$

Partial decay widths in LH

- ▶ 1-loop decays

$$\Gamma(h \rightarrow gg)_{LH} \sim \frac{\alpha_s^2 m_h^3}{32\pi^3 v^2} \left| \sum_{f, \text{col}} -\frac{1}{2} F_{\frac{1}{2}}(x_f) y_f \right|^2$$

$$\Gamma(h \rightarrow \gamma\gamma)_{LH} \sim \frac{\alpha^2 m_h^2}{256\pi^3 v^2} \left| \sum_{f, \text{ch}} \frac{4}{2} F_{\frac{1}{2}}(x_f) y_f + \sum_{v, \text{ch}} F_1(x_v) y_v + \sum_{s, \text{ch}} F_0(x_s) y_s \right|^2$$

where $x_i = \frac{4m_i^2}{m_h^2}$, $F_i(x_i)$ are loop functions, y_i the modified Yuk. coupl.

$$\Rightarrow \text{ narrow-width approximation: } \frac{\sigma_{LH}}{\sigma_{SM}}(gg \rightarrow h) = \frac{\Gamma(h \rightarrow gg)_{LH}}{\Gamma(h \rightarrow gg)_{SM}}$$

- ▶ tree-level decays

$$\Gamma(h \rightarrow VV)_{LH} \sim \Gamma(h \rightarrow VV)_{SM} \left(\frac{g_{hVV}}{g_{hVV}^{SM}} \right)^2$$

$$\Gamma(h \rightarrow f\bar{f})_{LH} \sim \Gamma(h \rightarrow f\bar{f})_{SM} \left(\frac{g_{hff}}{g_{hff}^{SM}} \right)^2$$

where $g_{hVV} = \frac{m_V^2}{v} y_V$ and $g_{hff} = \frac{m_f}{v} y_f$

LHT: Littlest Higgs with T parity

- ▶ Goldstone boson matrix:

$$\Sigma = e^{2i\Pi/f} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & H & \sqrt{2}\Phi \\ H^\dagger & 0 & H^t \\ \sqrt{2}\Phi^\dagger & H^* & 0 \end{pmatrix} \quad \Phi \propto \begin{pmatrix} \sqrt{2}\phi^{++} & \phi^+ \\ \phi^+ & \phi^0 + i\phi^P \end{pmatrix}$$

- ▶ Discrete T parity:

$$T : \quad \Pi \rightarrow -\Omega \Pi \Omega \quad \Omega = \text{diag}(1, 1, -1, 1, 1)$$

$$V_{CW} = \lambda_{\phi^2} f^2 \text{Tr}(\phi^\dagger \phi) + i\lambda_{h\phi h} f (H\phi^\dagger H^t - H^* \phi H^\dagger) - \mu^2 H H^\dagger + \lambda_{h^4} (H H^\dagger)^2 + \\ + \lambda_{h\phi\phi h} H\phi^\dagger \phi H^\dagger + \lambda_{h^2\phi^2} H H^\dagger \text{Tr}(\phi^\dagger \phi) + \lambda_{\phi^2\phi^2} [\text{Tr}(\phi^\dagger \phi)]^2 + \lambda_{\phi^4} \text{Tr}(\phi^\dagger \phi \phi^\dagger \phi).$$

$$\lambda_{\phi^2} = 2(g^2 + g'^2) + 8\lambda_1^2 \quad \lambda_{h^4} = \frac{1}{4}\lambda_{\phi^2} \quad \lambda_{h\phi\phi h} = -\frac{4}{3}\lambda_{\phi^2} \\ \lambda_{h^2\phi^2} = -16\lambda_1^2 \quad \lambda_{\phi^4} = -\frac{8}{3}(g^2 + g'^2) + \frac{16}{3}\lambda_1^2$$

- ▶ Yukawa couplings $k, R \equiv \lambda_1/\lambda_2$

$$\mathcal{L}_k = -kf \left(\bar{\Psi}_2 \xi \Psi_c + \bar{\Psi}_1 \langle \Sigma \rangle \Omega \xi^\dagger \Omega \Psi_c \right) - m_q \bar{u}'_c u_c - m_q \bar{d}'_c d_c - m_\chi \bar{\chi}'_c \chi_c + \text{h.c.}$$

$$\mathcal{L}_t = -\frac{\lambda_1 f}{2\sqrt{2}} \epsilon_{ijk} \epsilon_{xy} \left[(\bar{\Psi}_{1,t})_i \Sigma_{jx} \Sigma_{ky} - (\bar{\Psi}_{2,t} \langle \Sigma \rangle)_i \Sigma'_{jx} \Sigma'_{ky} \right] t'_R - \lambda_2 f (\bar{T}_{L1} T_{R1} + \bar{T}_{L2} T_{R2})$$

T parity and Dark Matter

Cheng/Low, 2003; Hubisz/Meade, 2005; Wang/Yang/Zhu,

2013

- ▶ **T parity**: $T^a \rightarrow T^a$, $X^a \rightarrow -X^a$, automorphism of coset space analogous to R parity in SUSY, KK parity in extra dimensions
- ▶ Bounds on F MUCH relaxed, $F \sim 0.5 - 1 \text{ TeV}$
but: Pair production!, typical **cascade decays**
- ▶ Lightest T -odd particle (LTP) \Rightarrow **Candidate for Cold Dark Matter**

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Littlest Higgs: A' LTP

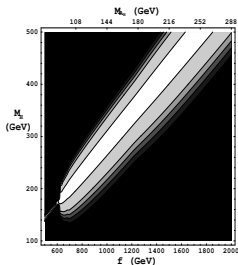
$W', Z' \sim 650 \text{ GeV}$, $\Phi \sim 1 \text{ TeV}$

$T, T' \sim 0.7-1 \text{ TeV}$

Annihilation: $A'A' \rightarrow h \rightarrow WW, ZZ, hh$

Hubisz/Meade, 2005

0/10/50/70/100



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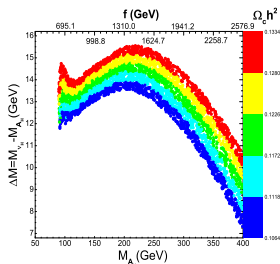
$W', Z' \sim 650 \text{ GeV}$, $\Phi \sim 1 \text{ TeV}$

$T, T' \sim 0.7-1 \text{ TeV}$

Annihilation: $A'A' \rightarrow h \rightarrow WW, ZZ, hh$

Wang/Yang/Zhu, 2013

Relic density/SI cross section



T parity and Dark Matter

Cheng/Low, 2003; Hubisz/Meade, 2005; Wang/Yang/Zhu,

2013

- ▶ T parity: $T^a \rightarrow T^a$, $X^a \rightarrow -X^a$, automorphism of coset space analogous to R parity in SUSY, KK parity in extra dimensions
- ▶ Bounds on F MUCH relaxed, $F \sim 0.5 - 1 \text{ TeV}$
but: Pair production!, typical **cascade decays**
- ▶ Lightest T -odd particle (LTP) \Rightarrow **Candidate for Cold Dark Matter**

Littlest Higgs: A' LTP

$W', Z' \sim 650 \text{ GeV}$, $\Phi \sim 1 \text{ TeV}$

$T, T' \sim 0.7-1 \text{ TeV}$

Annihilation: $A'A' \rightarrow h \rightarrow WW, ZZ, hh$

Wang/Yang/Zhu, 2013

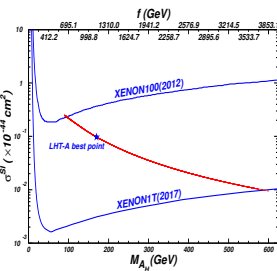
Relic density/SI cross section

- ▶ T parity Simplest LH: **Pseudo-Axion η LTP**

Z' remains odd: good or bad (?)

Martin, 2006; JRR/Tonini, in prep.

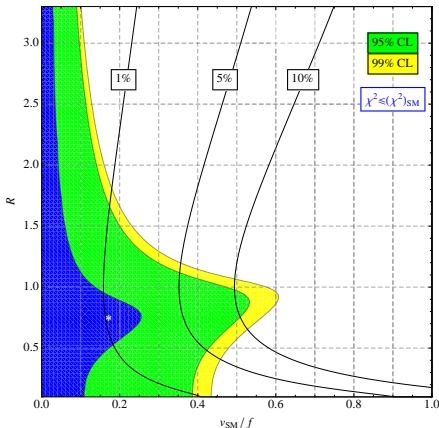
- ▶ T parity might be anomalous (???)



Hill/Hill, 2007

LHT results

LHT (Case A) : all data



$$\chi_{\min}^2/\text{d.o.f.} = 1.048$$

$$\chi_{SM}^2/\text{d.o.f.} = 1.053$$

- ▶ free parameters: f SSB scale, R ratio of Yukawa couplings in top sector
- ▶ $f_{\min}^{99\%} = 405.9$ GeV, translates into lower bounds on new states' masses, e.g.

$$m_{W'} \gtrsim 269.6 \text{ GeV}$$

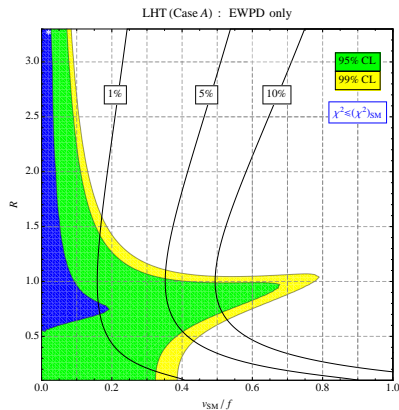
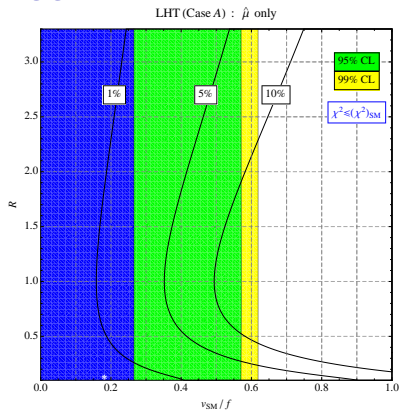
$$m_T \gtrsim 553.6 \text{ GeV}$$

- ▶ min. required fine tuning: $\sim 10\%$, defined as

$$\Delta = \frac{|\delta\mu^2|}{\mu_{\text{obs}}^2}$$

- ▶ results mainly driven by EWPD (see next slide)

Higgs data vs. $EWPD$

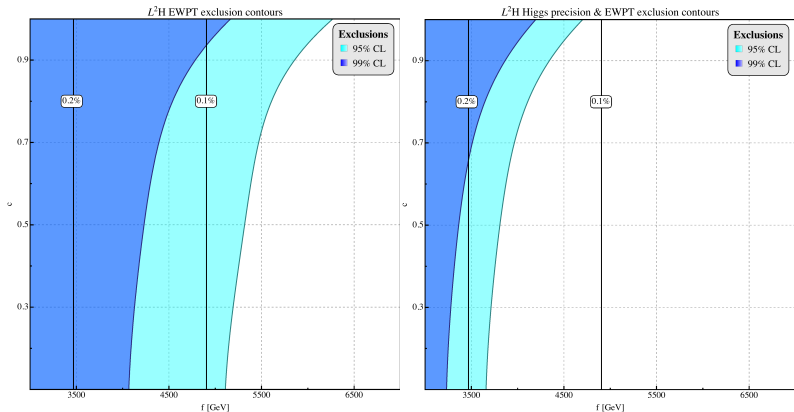


- ▶ the shape of the combined result is driven by the EW constraints (much smaller uncertainties)
- ▶ Higgs data only: for $v/f \gtrsim 0.6$ decay $h \rightarrow A_H A_H$ open and dominant
- ▶ Higgs data only: subdominant dependence on R w.r.t. f is a consequence of the Collective Symmetry Breaking mechanism

New Results (incl. Moriond '13)

JRR/Tonini/de Vries, 1307.5010

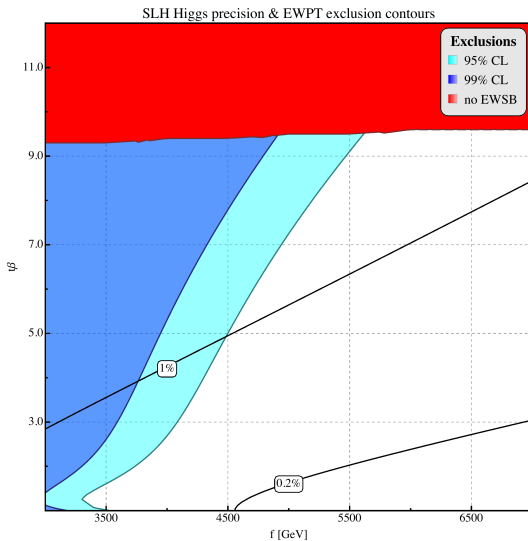
Littlest Higgs Model



New Results (incl. Moriond '13)

Simplest Little Higgs

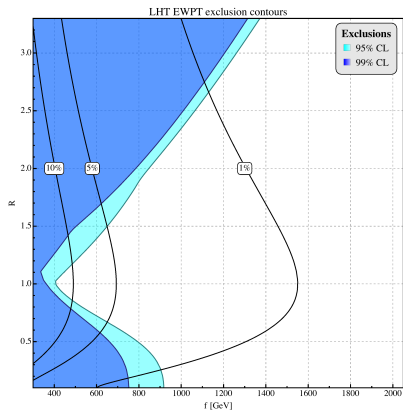
JRR/Tonini/de Vries, 1307.5010



New Results (incl. Moriond '13)

JRR/Tonini/de Vries, 1307.5010

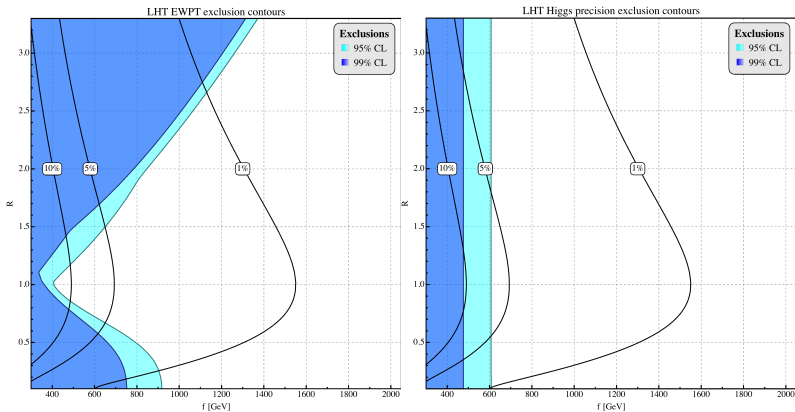
Littlest Higgs with T Parity



New Results (incl. Moriond '13)

JRR/Tonini/de Vries, 1307.5010

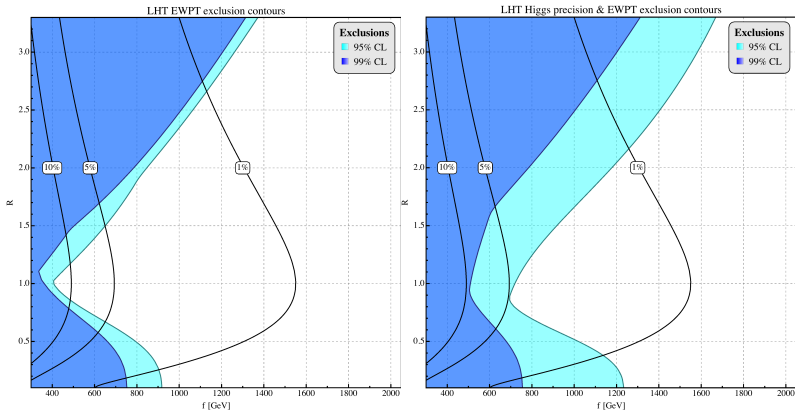
Littlest Higgs with T Parity



New Results (incl. Moriond '13)

JRR/Tonini/de Vries, 1307.5010

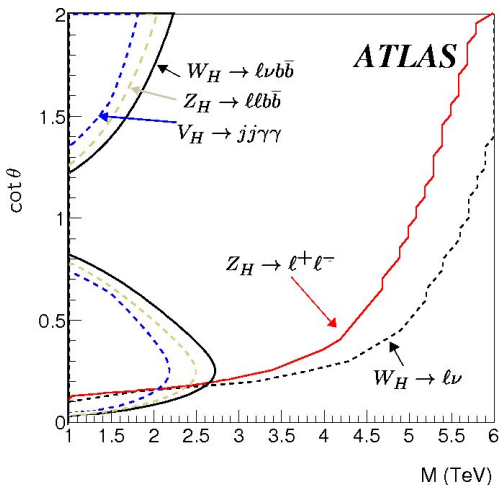
Littlest Higgs with T Parity



▶ EWPT and Higgs data \Rightarrow

$$f \gtrsim 694 \text{ GeV}$$

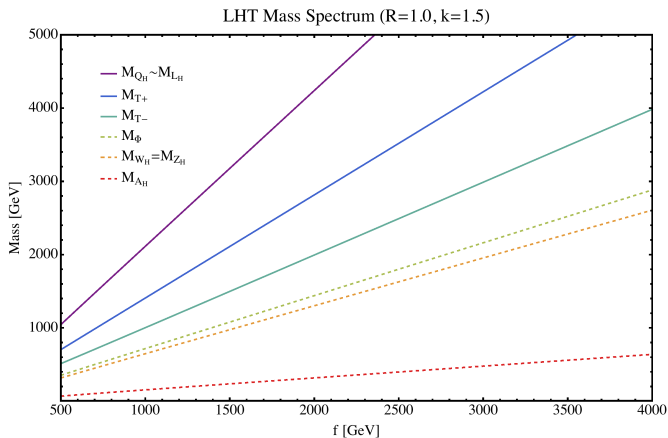
Direct searches: Drell-Yan mainly



Reach in the gauge boson sector: depends on mixing angle

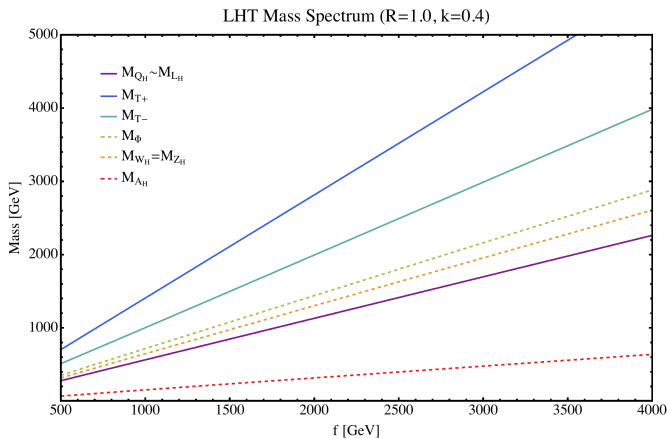
Direct Searches: Focus on LHT

- ▶ Defining two benchmark scenarios: 1. heavy quarks



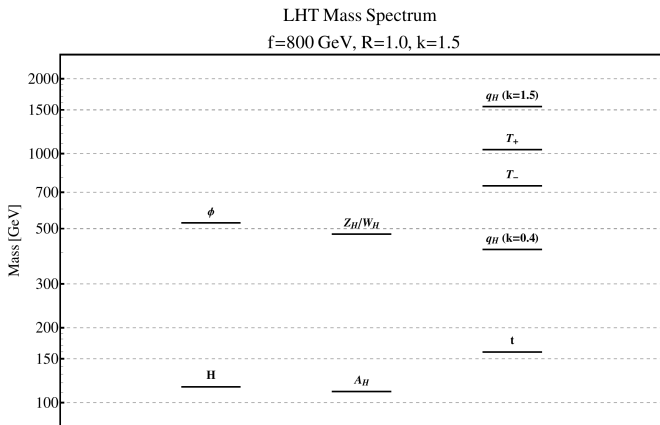
Direct Searches: Focus on LHT

- ▶ Defining two benchmark scenarios: 2. heavy top/vectors



Direct Searches: Focus on LHT

- Defining two benchmark scenarios: 1. $k = 1.5$, 2. $k = 0.4$



Branching Ratios

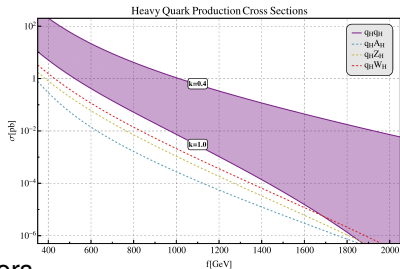
► Decay patterns:

Particle	Decay	BR _{k=1.0}	BR _{k=0.4}
l_H^\pm	$W_H^\pm \nu$	62%	0%
	$Z_H l^\pm$	31%	0%
	$A_H l^\pm$	6%	100%
ν_H^\pm	$W_H^\pm l^\mp$	61%	0%
	$Z_H \nu$	30%	0%
	$A_H \nu$	9%	100%
T_H^+	$W^+ b$	46%	45%
	$Z t$	22%	22%
	$H t$	21%	21%
	$T_H^- A_H$	11%	11%
A_H	stable		
Z_H	$A_H H$	100%	2%
	$d_H d$	0%	41%
	$u_H u$	0%	30%
	$l_H^\pm l^\mp$	0%	14%
	$\nu_H \nu$	0%	14%

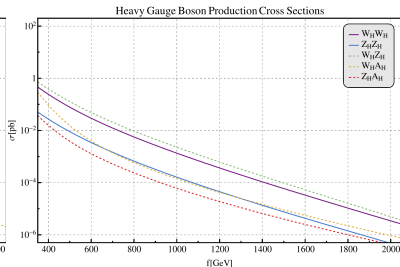
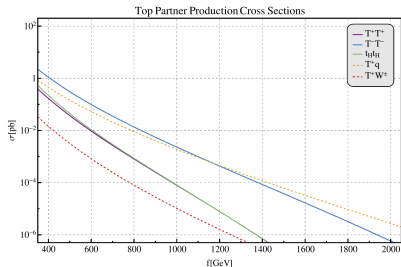
Particle	Decay	BR _{k=1.0}	BR _{k=0.4}
d_H	$W_H^- u$	62%	0%
	$Z_H d$	30%	0%
	$A_H d$	6%	100%
u_H	$W_H^+ d$	58%	0%
	$Z_H u$	30%	0%
	$A_H u$	9%	100%
T_H^-	$A_H t$	100%	100%
	$Z_H t$	0%	0%
$\Phi^{0/P}$	$A_H H$	100%	100%
Φ^\pm	$A_H W^\pm$	100%	100%
$\Phi^{\pm\pm}$	$A_H (W^\pm)^2$	100%	96%
W_H^\pm	$A_H W^\pm$	100%	2%
	$u_H d$	0%	44%
	$d_H u$	0%	27%
	$l_H^\pm \nu$	0%	16.5%
	$\nu_H l^\pm$	0%	16.5%

Cross Sections (I)

► Heavy Quarks



► Heavy Top and Vectors



Channels and signatures: Parameters

final state			modes	params	final state			modes	params
leptons	# jets	\cancel{E}_T			leptons	# jets	\cancel{E}_T		
0	1	✓	$q_H A_H$	f, k	l^\pm	2	✓	$W_H^\pm W_H^\mp$ $W_H^\pm Z_H$ $q_H q_H$	f, k f, k f, k
0	2	✓	$q_H q_H$	f, k	l^\pm	3	✓	$q_H W_H^\pm$ $T^+ q$	f, k f, k, R
0	3	✓	$q_H W_H^\pm$	f, k	l^\pm	4	✓	$q_H q_H$ $T^- T^-$	f, k f, k, R
0	4	✓	$q_H q_H$ $W_H^\pm W_H^\mp$ $W_H^\pm Z_H$ $Z_H Z_H$	f, k f, k f, k f, k	$l^+ l^-$	0	✓	$W_H^\pm W_H^\mp$	f, k
0	4	✗	$T^+ q$	f, k, R	$l^+ l^-$	1	✓	$q_H W_H^\pm$	f, k
0	5	✓	$q_H W_H^\pm$	f, k	$l^+ l^-$	2	✓	$q_H q_H$ $T^- T^-$	f, k f, k, R
0	6	✓	$q_H q_H$ $T^- T^-$	f, k f, k, R	$l^\pm l^\pm$	2	✓	$q_H q_H$	f, k

Channels and signatures (I)

final state			production modes	$\sigma_{8\text{ TeV}} \times \text{Br (fb)}$		$\sigma_{14\text{ TeV}} \times \text{Br (fb)}$	
$\# l^\pm$	$\# \text{jets}$	\cancel{E}_T		$k = 1.0$	$k = 0.4$	$k = 1.0$	$k = 0.4$
0	1	✓	$q_H A_H$	0.24	1.1×10^2	2.1	4.5×10^2
0	2	✓	$q_H q_H$	0.56	5.6×10^3	5.2	3.2×10^4
0	3	✓	$q_H W_H^\pm$	0.73	14	8.0	77
			$q_H Z_H$	0.76	8.6	8.0	49
0	4	✓	$q_H q_H$	4.0	9.1×10^2	35	5.6×10^3
			$W_H^\pm W_H^\mp$	1.9	low	9.1	low
			$W_H^\pm Z_H$	4.8	low	23	low
			$Z_H Z_H$	0.56	low	3.0	low
0	4	✗	$T^+ q$	2.0	2.0	17	17
0	5	✓	$q_H W_H^\pm$	5.1	✗	54	✗
			$q_H Z_H$	4.1	✗	44	✗
0	6	✓	$q_H q_H$	1.6	9.7×10^2	1.7×10^2	6.0×10^3
			$T^- T^-$	2.5	2.5	25	25

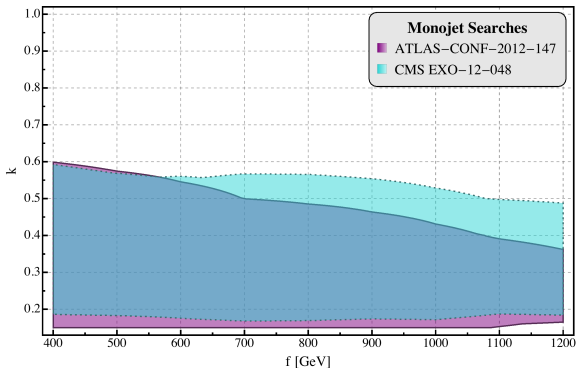
Channels and signatures (II)

final state			production modes	$\sigma_{8 \text{ TeV}} \times \text{Br (fb)}$		$\sigma_{14 \text{ TeV}} \times \text{Br (fb)}$	
# l^\pm	# jets	\cancel{E}_T		$k = 1.0$	$k = 0.4$	$k = 1.0$	$k = 0.4$
l^\pm	2	✓	$q_H q_H$	0.058	9.0×10^2	1.1	5.6×10^3
			$W_H^\pm W_H^\mp$	0.77	low	3.9	low
			$W_H^\pm Z_H$	2.1	low	10	low
			$T^+ q$	1.3	1.2	10	10
l^\pm	3	✓	$q_H W_H^\pm$	3.5	✗	37	✗
			$q_H Z_H$	0.99	✗	11	✗
l^\pm	4	✓	$q_H q_H$	7.4	9.7×10^2	82	6.0×10^3
			$T^- T^-$	2.2	2.2	21	21
$l^+ l^-$	0	✓	$W_H^\pm W_H^\mp$	0.32	low	1.7	low
$l^+ l^-$	1	✓	$q_H W_H^\pm$	0.54	✗	5.8	✗
$l^+ l^-$	2	✓	$q_H q_H$	1.1	✗	11	✗
			$T^- T^-$	0.47	0.47	4.6	4.6
$l^\pm l^\pm$	2	✓	$q_H q_H$	0.37	✗	2.7	✗

Recasting results

JRR/Tonini/deVries,2013

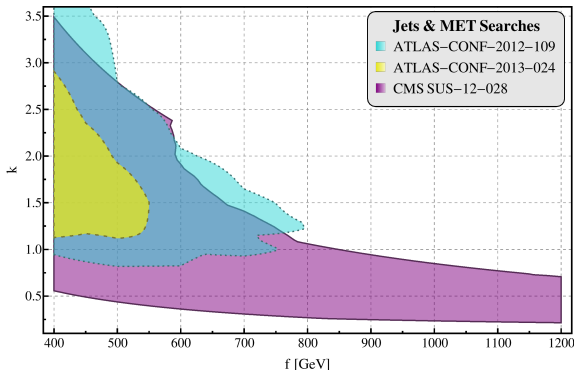
- **95% CL from Monojets + \cancel{E}_T from LHC8**
- 1 hard jet, \cancel{E}_T , no leptons, 2nd jet w. $p_T > 30$ GeV
signal regions: ATLAS (p_T, \cancel{E}_T) > 120/220/350/500 GeV, CMS: $\cancel{E}_T > 250/300/350/400/450/500/550$ GeV
- Dijet suppression: ATLAS $\Delta\phi(\cancel{E}_T, j_2) > 0.5$, CMS $\Delta\phi(j_1, j_2) < 2.5$
- $pp \rightarrow q_H q_H, pp \rightarrow q_H A_H$



Recasting results

JRR/Tonini/deVries,2013

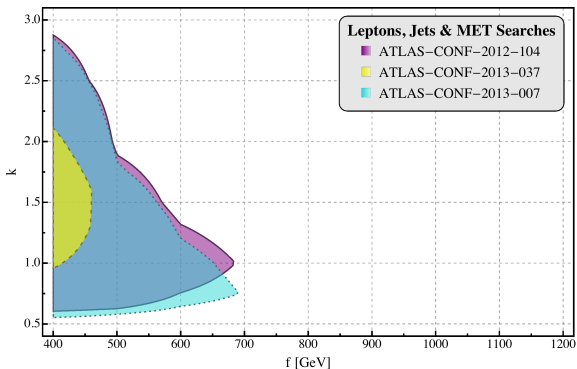
- 95% CL from Jets + \cancel{E}_T from LHC8
- ≥ 2 hard jets, \cancel{E}_T , no leptons
- signal regions: ATLAS $\cancel{E}_T > 200/300/350$ GeV, CMS:
 $(N_j, N_b) = (2 - 3, 0); (2 - 3, 1 - 2); (\geq 4, 1 - 2); (\geq 4, 0); (\geq 4, \geq 2)$
- QCD suppression: ATLAS $\Delta\phi(\cancel{E}_T, j_2) > 0.5$, \cancel{E}_T/m_{eff} , CMS $\Delta\phi(j_1, j_2) < 2.5$
- $pp \rightarrow q_H q_H \rightarrow (j A_H)(j A_H)$



Recasting results

JRR/Tonini/deVries, 2013

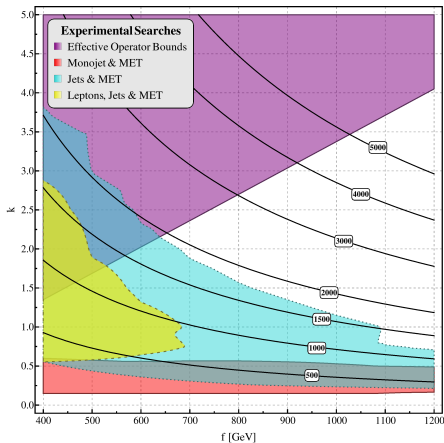
- 95% CL from Leptons + Jets + \cancel{E}_T from LHC8
- single isolated lepton, ≥ 2 hard jets, \cancel{E}_T ,
- signal regions: ATLAS $\cancel{E}_T > 200/300/350$ GeV
- Cuts: $\cancel{E}_T > 250$ GeV, $m_T(l, \cancel{E}_T) > 250$ GeV, $\cancel{E}_T/m_{\text{eff}} > 0.2$, $m_{\text{eff}}^{\text{inc}} > 800$ GeV
- $pp \rightarrow q_H q_H$ with $q_H \rightarrow W_H q, Z_H q, t_H \rightarrow t A_H, Z_H \rightarrow H A_H$



Combined analysis

JRR/Tonini/deVries, 2013

- Operator bounds: $\mathcal{O}_{4f} = -\frac{k^2}{128\pi^2 f^2} \bar{\psi}_L \gamma^\mu \psi_L \bar{\psi}'_L \gamma_\mu \psi'_L + \mathcal{O}\left(\frac{g}{k}\right)$
 Hubisz/Meade/Noble/Perelstein, 2005



- Bound from combined analysis: $f \gtrsim 638\text{GeV}$

Conclusions

- ▶ *Little Higgs* models are an appealing solution to the hierarchy problem, alternative to weakly coupled solutions like *SUSY*
- ▶ most of the parameter space of three popular *Little Higgs* models is still compatible at $\sim 99\%$ *CL* with the early results of the 7+8 TeV Higgs searches
- ▶ electroweak precision data represent still the most severe constraints
- ▶ fine-tuning as a guideline to understand the naturalness of a model: *Little Higgs* models require a minimum level of $\sim 10\%$ of fine tuning
- ▶ Limits on the LHT:

1. EWPO:

$$f \gtrsim 405 \text{ GeV@95\% CL}$$

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4. Direct searches:

$$f \gtrsim 638 \text{ GeV@95\% CL}$$

- ▶ We need more data!

Lessons from Lepton Photon 2013 ...

There are either colored exotics ...



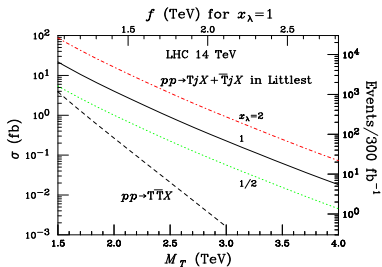
Lessons from Lepton Photon 2013 ...

... or the world is fine tuned



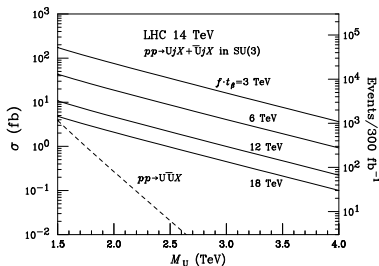
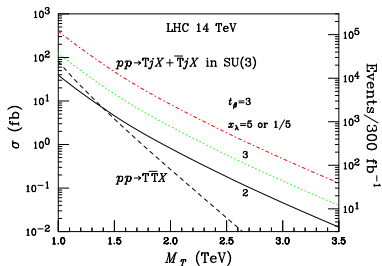
Direct Searches – Heavy Quark States

- EW single dominates QCD pair production: Perelstein/Peskin/Pierce, '03



Direct Searches – Heavy Quark States

- EW single dominates QCD pair production: Perelstein/Peskin/Pierce, '03



- Characteristic branching ratios :

$$\Gamma(T \rightarrow th) \approx \Gamma(T \rightarrow tZ) \approx \frac{1}{2} \Gamma(T \rightarrow bW^+) \approx \frac{M_T \lambda_T^2}{64\pi}, \quad \Gamma_T \sim 10-50 \text{ GeV}$$

- Proof of T as EW singlet; but: $T \rightarrow Z'T, W'b, t\eta$!

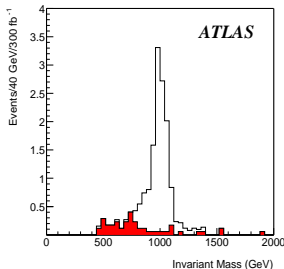
AIM: Determination of $M_T, \lambda_T, \lambda_{T'}$

$\lambda_{T'}$ indirect ($T\bar{T}h$ impossible)

$$T \rightarrow Zt \rightarrow \ell^+ \ell^- \ell \nu b$$

SN-ATLAS-2004-038

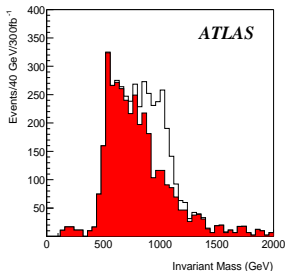
-
- ▶ $\cancel{E}_T > 100 \text{ GeV}$, $l\ell l$, $p_T > 100/30 \text{ GeV}$,
 b , $p_T > 30 \text{ GeV}$
 - ▶ Bkgd.: WZ , ZZ , btZ
 - ▶ Observation for $M_T \lesssim 1.4 \text{ TeV}$



$$T \rightarrow Wb \rightarrow \ell\nu b$$

SN-ATLAS-2004-038

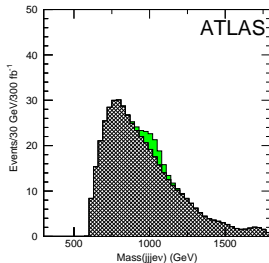
-
- ▶ $\cancel{E}_T > 100 \text{ GeV}$, $\ell, p_T > 100 \text{ GeV}$,
 $b, p_T > 200 \text{ GeV}$, max. $jj, p_T > 30 \text{ GeV}$
 - ▶ Bkgd.: $t\bar{t}$, $Wb\bar{b}$, single t
 - ▶ Observation for $M_T \lesssim 2.5 \text{ TeV}$



$$T \rightarrow th \rightarrow \ell\nu bbb$$

SN-ATLAS-2004-038

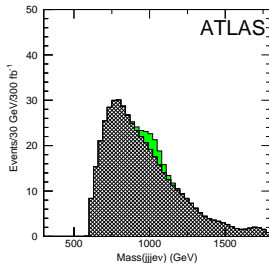
-
- ▶ $\ell, p_T > 100 \text{ GeV}, jjj, p_T > 130 \text{ GeV}$,
at least 1 b -tag
 - ▶ Bkgd.: $t\bar{t}, Wb\bar{b}$, single t
 - ▶ Observation for $M_T \lesssim 2.5 \text{ TeV}$



$$T \rightarrow th \rightarrow \ell\nu bbb$$

SN-ATLAS-2004-038

- ▶ $\ell, p_T > 100 \text{ GeV}$, $jjj, p_T > 130 \text{ GeV}$, at least 1 b -tag
- ▶ Bkgd.: $t\bar{t}$, $Wb\bar{b}$, single t
- ▶ Observation for $M_T \lesssim 2.5 \text{ TeV}$

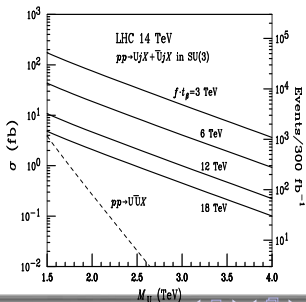


Additional heavy quarks (Simple Group Models): U, C or D, S

Han et al.,

05

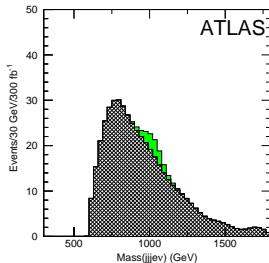
- ▶ Large cross section: u or d PDF
- ▶ Huge final state ℓ charge asymmetry
- ▶ Good mass reconstruction



$$T \rightarrow th \rightarrow l\nu bbb$$

SN-ATLAS-2004-038

- ▶ $l, p_T > 100 \text{ GeV}$, $jjj, p_T > 130 \text{ GeV}$, at least 1 b -tag
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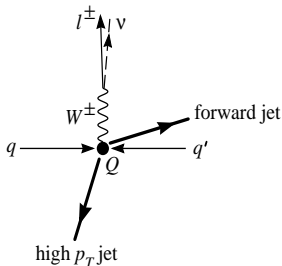


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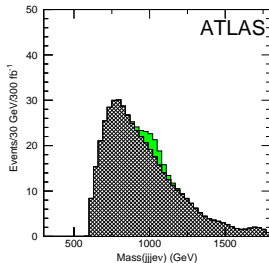
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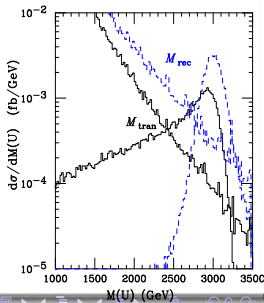
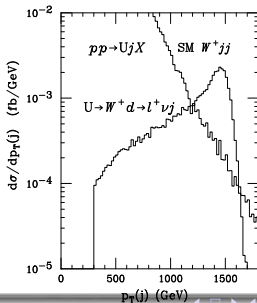


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Direct Searches – Heavy Vectors

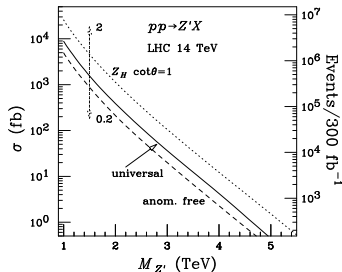
Drell-Yan Production: Tevatron Limits $\sim 500 - 600$ GeV

► **Dominant decays:**

Product group: $Z' \rightarrow Zh, WW,$

$W' \rightarrow Wh, WZ$

Simple group: $Z' \rightarrow qq, \quad X \rightarrow fF$



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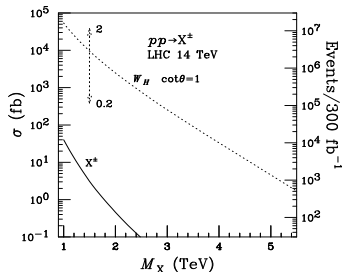
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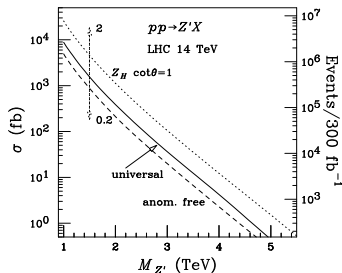
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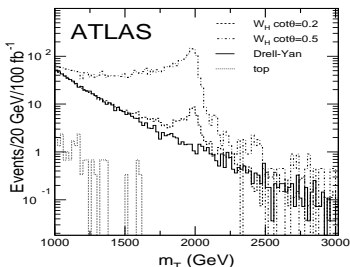
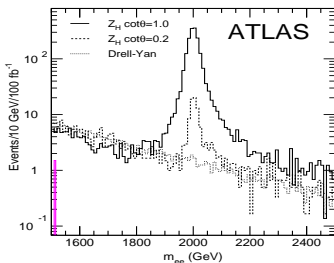
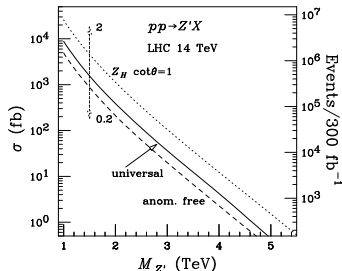
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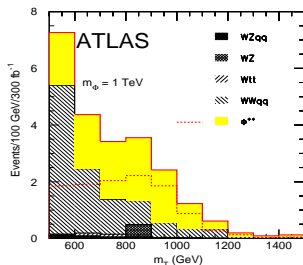


Direct Searches – Heavy Scalars

Generally: **Large model dependence**

no states complex singlet **complex triplet**

- ▶ **Littlest Higgs**, complex triplet:
 $\Phi^0, \Phi_P, \Phi^\pm, \Phi^{\pm\pm}$
- ▶ Cleanest channel: $q\bar{q} \rightarrow \Phi^{++}\Phi^{--} \rightarrow llll$:
Killer: PS
- ▶ WW -Fusion: $dd \rightarrow uu\Phi^{++} \rightarrow uuW^+W^+$
- ▶ 2 hard forward jets, hard close l^+l^+
 p_T -unbalanced



Alternative: Model-Independent search in WW fusion:

ILC: Beyer/Kilian/Krstonosic/Mönig/JRR/Schmidt/Schröder, 2006

LHC: Alboteanu/Kilian/JRR, 2008; Kilian/JRR/Sekulla, 2013

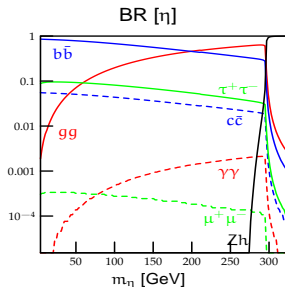
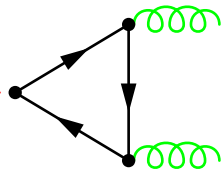
Pseudo-Axions in Little Higgs

Kilian/Rainwater/JRR, 2004, 2006; JRR,

2007

- gauged $U(1)$ group: Z' \longleftrightarrow ungauged: η
- couples to fermions like a pseudoscalar
- $m_\eta \lesssim 400$ GeV
- SM singlet, couplings to SM particles v/F suppressed
- η axion-like particle:

Anomalous $U(1)$: $---$



$$\longrightarrow \frac{1}{F} \frac{\alpha_s}{8\pi^2} \eta F_{\mu\nu} F_{\rho\sigma} \epsilon^{\mu\nu\rho\sigma}$$

- $U(1)$ explicitly broken \Rightarrow Axion limits from astroparticle physics not applicable

Classification of Axions in Little Higgs Models

Number of Pseudo-Axions: $n = g - l$

Mismatch between global (g) and local rank reduction (l)

Product Group Models Arkani-Hamed, ...

- ▶ Doubling of electroweak gauge group: $SU(2) \times SU(2) \rightarrow SU(2)_L$,
 $U(1) \times U(1) \rightarrow U(1)_Y$ (latter not necessary) $\Rightarrow l = 1$
 - ▶ Littlest Higgs, $g: SU(5) \rightarrow SO(5) \Rightarrow n = (4 - 2) - 1 = 1$
 - ▶ antisymmetric, $g: Sp(6)/SO(6)$, $n = (3 - 2) - 1 = 0$

Simple Group Models Kaplan, Schmaltz, ...

- ▶ Simple gauge group: $SU(N) \times U(1) \rightarrow SU(2) \times U(1) \Rightarrow l = N - 2$
- ▶ Higgs is distributed over several global symmetry multiplets
- ▶ Simplest Little Higgs, $g: [SU(3)]^2/[SU(2)]^2$ $n = g - l = 2 - 1 = 1$
- ▶ Original Simple Group Model, $g: [SU(4)]^3/[SU(3)^3 \times SU(2)]$,
 $l: SU(4) \rightarrow SU(2)$ $n = g - l = 4 - 2 = 2$

Moose Models Arkani-Hamed, ...

- ▶ "Minimal" Moose: $g [SU(3)]^4 \rightarrow SU(3)$, $l [SU(3) \times SU(2)]/SU(2)$
 $n = g - l = 6 - 2 = 4$
- ▶ 3-site model: $g [SU(2)]^4/[SU(2)]^2$, $l [SU(2)]^2 \rightarrow SU(2)$, $n = 2 - 1 = 1$

$ZH\eta$ coupling as a discriminator

Kilian/Rainwater/JRR, 2006

- ▶ pseudo-axion: $\xi = \exp[i\eta/F]$, $\Sigma = \exp[i\Pi/F]$ non-linear representation of the remaining Goldstone multiplet Π

$$\mathcal{L}_{\text{kin.}} \sim F^2 \text{Tr} [(D^\mu(\xi\Sigma))^\dagger (D_\mu(\xi\Sigma))] = \dots - 2F(\partial_\mu\eta) \text{Im Tr} [(D^\mu\Sigma)^\dagger \Sigma] + O(\eta^2)$$

- ▶ Use special structure of covariant derivatives:

$$D_\mu \Sigma = \partial_\mu \Sigma + A_{1,\mu}^a (T_1^a \Sigma + \Sigma (T_1^a)^T) + A_{2,\mu}^a (T_2^a \Sigma + \Sigma (T_2^a)^T),$$

$$\text{Tr} [(D^\mu \Sigma)^\dagger \Sigma] \sim W_\mu^a \text{Tr} [\Sigma^\dagger (T_1^a + T_2^a) \Sigma + (T_1^a + T_2^a)^*] = 0.$$

- ▶ Little Higgs mechanism cancels this coupling
- ▶ Simple Group Models: $\Phi = \exp[i\Sigma/F]$, $\zeta = (0, \dots, 0, F)^T$ VEV directing in the N direction

$$\begin{aligned}\mathcal{L}_{\text{kin.}} &\sim F^2 D^\mu (\zeta^\dagger \Phi^\dagger) D_\mu (\Phi \zeta) = \dots + \frac{i}{F} (\partial_\mu \eta) \zeta^\dagger (\Phi^\dagger (D_\mu \Phi) - (D_\mu \Phi^\dagger) \Phi) \zeta \\ &= \dots + iF (\partial_\mu \eta) (\Phi^\dagger (D_\mu \Phi) - (D_\mu \Phi^\dagger) \Phi)_{N,N} .\end{aligned}$$

$$\Sigma = \begin{pmatrix} 0 & h \\ h^\dagger & 0 \end{pmatrix}, \quad \mathbb{V}_\mu = \begin{pmatrix} \mathbb{W}_\mu & 0 \\ 0 & 0 \end{pmatrix} + \text{heavy vector fields}$$

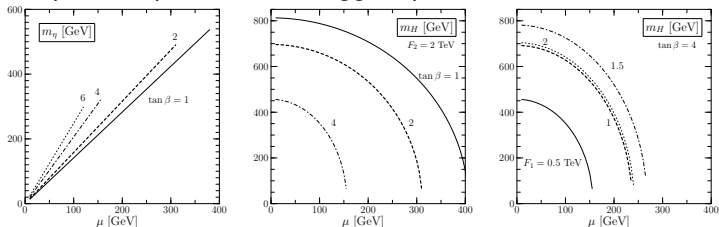
$$\begin{aligned}&\mathbb{V}_\mu + \frac{i}{F} [\Sigma, \mathbb{V}_\mu] - \frac{1}{2F^2} [\Sigma, [\Sigma, \mathbb{V}_\mu]] + \dots \\ &= \begin{pmatrix} \mathbb{W}_\mu & 0 \\ 0 & 0 \end{pmatrix} + \frac{i}{F} \begin{pmatrix} 0 & -\mathbb{W}_\mu h \\ h^\dagger \mathbb{W}_\mu & 0 \end{pmatrix} - \frac{1}{2F^2} \begin{pmatrix} hh^\dagger \mathbb{W} + \mathbb{W} h h^\dagger & 0 \\ 0 & -2h^\dagger \mathbb{W} h \end{pmatrix} + \dots\end{aligned}$$

- ▶ 1st term cancels by multiple Goldstone multiplets
- ▶ 2st term cancels by EW symmetry
- ▶ 3rd term

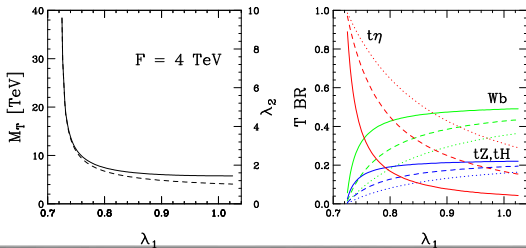
$$(\partial^\mu \eta) h^\dagger \mathbb{W}_\mu h \sim v H Z_\mu \partial^\mu \eta .$$

More properties of Pseudo-Axions

- ▶ Take e.g. one specific model: Simplest Little Higgs Schmalz, 2004
- ▶ Simple Group Model, two Higgs-triplets with a $\tan\beta$ -like mixing angle



- ▶ $\tan\beta \sim 1$: heavy Higgs, (very) light pseudoscalar
- ▶ Heavy top decays: Kilian/Rainwater/JRR, 2006



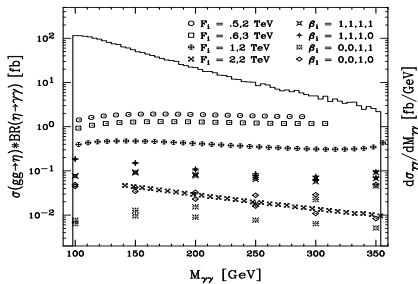
Discovery of Pseudo-axions

Kilian/Rainwater/JRR, 2004, 2006

LHC: Gluon fusion, diphoton
signal for $m_\eta \gtrsim 200$ GeV, 7σ
possible

LHC: $T \rightarrow t\eta$

ILC: $e^+e^- \rightarrow t\bar{t}\eta$



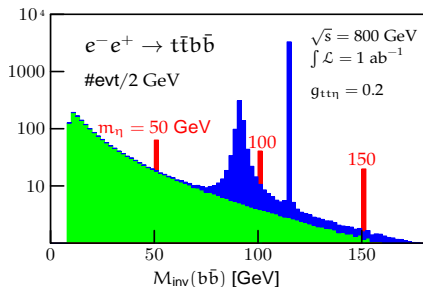
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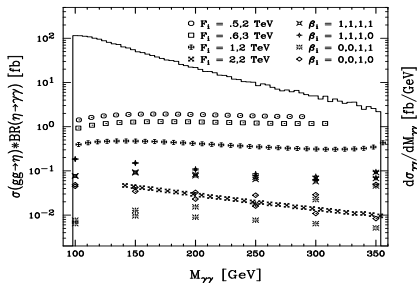
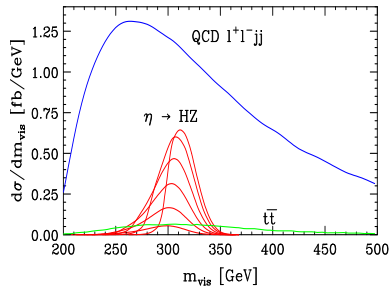
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$ZH\eta$ coupling

forbidden in Product Group Models

Discriminator of diff. model classes

$$gg \rightarrow \left\{ \begin{array}{ll} H \rightarrow Z\eta & \rightarrow llbb \\ \eta \rightarrow ZH & \rightarrow llbb, llljj \end{array} \right\}$$

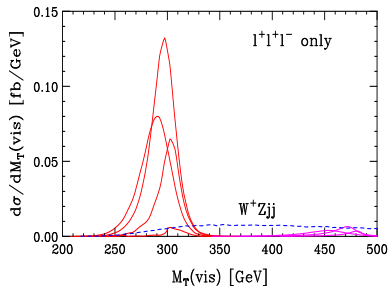
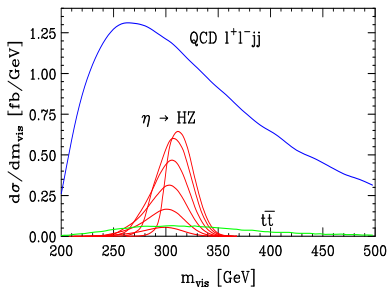
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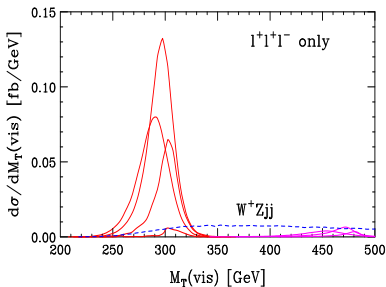
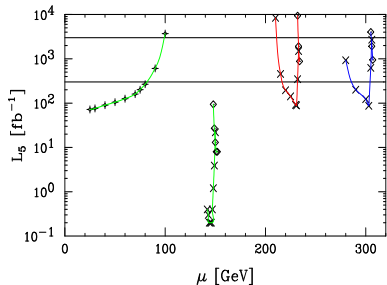
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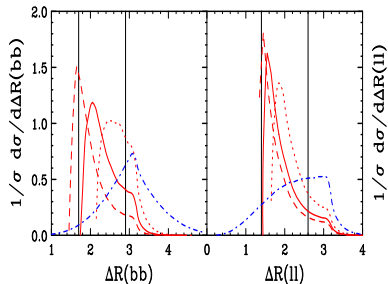
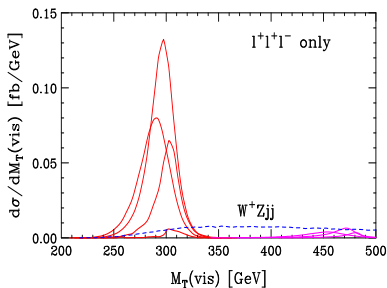
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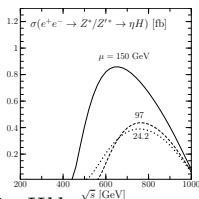
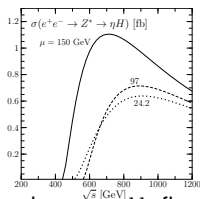
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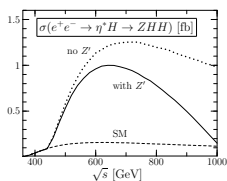
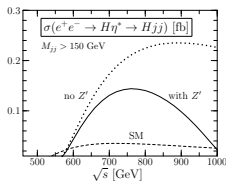
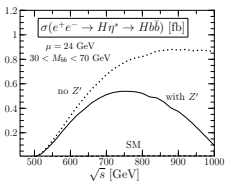
η pheno at ILC

Kilian/Rainwater/JRR, 2006

If $ZH\eta$ coupling present: $H\eta$ production in analogy to HA :



- Light pseudoaxion, $\eta \rightarrow b\bar{b}$, final state $Hb\bar{b}$
- Intermediate range, $\eta \rightarrow gg$, final state Hjj
- $\eta \rightarrow ZH$: ZHH final state

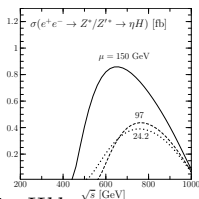
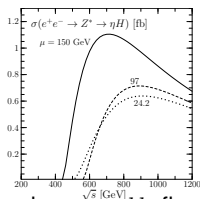


More detailed insights from photon collider option

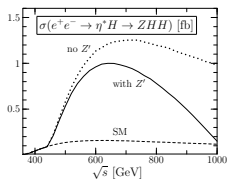
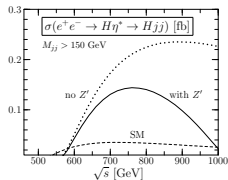
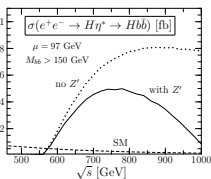
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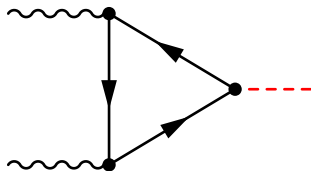
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More detailed insights from photon collider option

Pseudo Axions at the Photon Collider

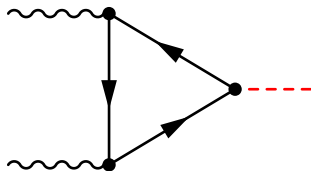
- ▶ **Photon Collider** as precision machine for Higgs physics (s channel resonance, anomaly coupling)



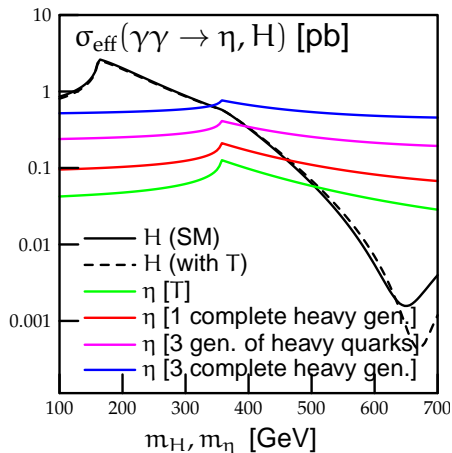
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- ▶ η in the μ model with (almost) identical parameters as A in MSSM
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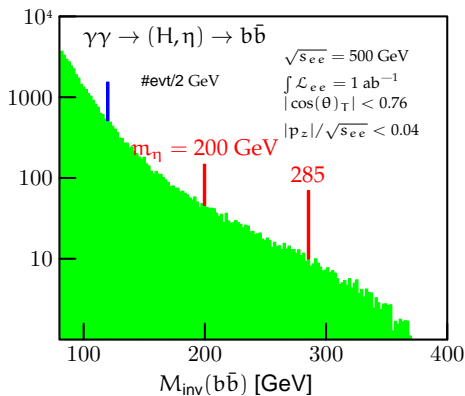
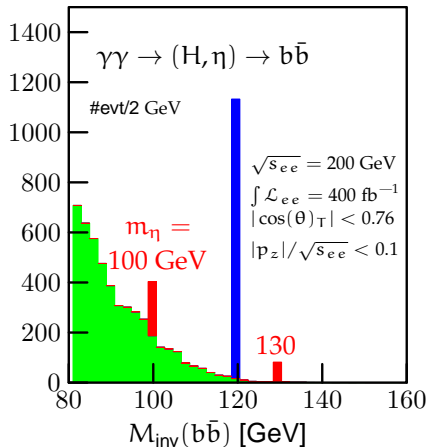


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$$g_{bb\eta} = 0.4 \cdot g_{bbh}$$

m_η	100	130	200	285
$\Gamma_{\gamma\gamma}$ [keV]	0.15	0.27	1.1	3.6



Simplest Little Higgs (“ μ Model”)

Schmaltz '04, Kilian/Rainwater/JRR '04

Field content ($SU(3)_c \times SU(3)_w \times U(1)_X$ quantum numbers)

$$\begin{array}{lll}
 \Phi_{1,2} & : & (1, 3)_{-\frac{1}{3}} \\
 \Psi_Q & : & (3, 3)_{\frac{1}{3}} \\
 \Psi_\ell & : & (1, 3)_{-\frac{1}{3}} \\
 d^c & : & (\bar{3}, 1)_{\frac{1}{3}} \\
 u_{1,2}^c & : & (\bar{3}, 1)_{-\frac{2}{3}} \\
 e^c, n^c & : & (1, 1)_{1,0}
 \end{array}$$

Lagrangian $\mathcal{L} = \mathcal{L}_{\text{kin.}} + \mathcal{L}_{\text{Yuk.}} + \mathcal{L}_{\text{pot.}}$ $\Psi_{Q,L} = (u, d, U)_L, \Psi_\ell = (\nu, \ell, N)_L$:

$$\begin{aligned}
 \mathcal{L}_{\text{Yuk.}} = & -\lambda_1^u \bar{u}_{1,R} \Phi_1^\dagger \Psi_{T,L} - \lambda_2^u \bar{u}_{2,R} \Phi_2^\dagger \Psi_{T,L} - \frac{\lambda^d}{\Lambda} \epsilon^{ijk} \bar{d}_R^b \Phi_1^i \Phi_2^j \Psi_{T,L}^k \\
 & - \lambda^n \bar{n}_{1,R} \Phi_1^\dagger \Psi_{Q,L} - \frac{\lambda^e}{\Lambda} \epsilon^{ijk} \bar{e}_R \Phi_1^i \Phi_2^j \Psi_{Q,L}^k + \text{h.c.},
 \end{aligned}$$

$$\mathcal{L}_{\text{pot.}} = \mu^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}$$

Hypercharge embedding ($\text{diag}(1, 1, -2)/(2\sqrt{3})$):

$$Y = X - T^8/\sqrt{3} \qquad D_\mu \Phi = (\partial_\mu - \frac{1}{3} g_X B_\mu^X \Phi + i g W_\mu^w) \Phi$$