

# Status of Little Higgs Models in 2013

Jürgen Reuter

DESY

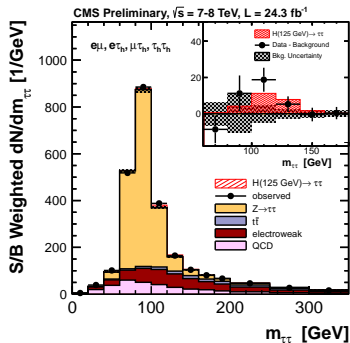
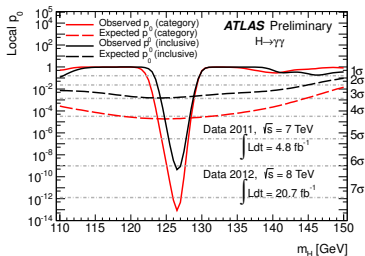
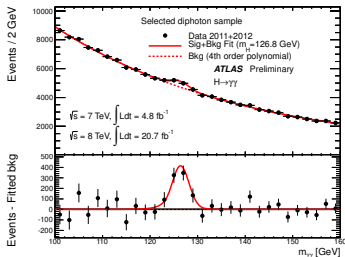


JRR/Tonini/de Vries, arXiv:1310.2918; arXiv:1307.5010; JRR/Tonini, JHEP **1302** (2013) 077; Kilian/JRR/Rainwater **PRD 74** (2006), 095003; **PRD 71** (2005), 015008; Kilian/JRR **PRD 70** (2004), 015004

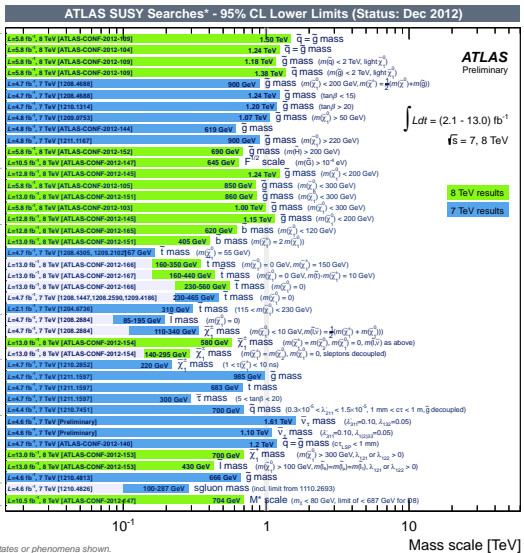
Theory Seminar, KEK, つくば市, 19.11.2013

# Standard Model Triumph:

- ▶ 2012: Discovery of a Higgs boson



# ... and now?



\* Only a selection of the available mass limits on new states or phenomena shown.  
 All limits quoted are observed minus  $1\sigma$  theoretical signal cross section uncertainty.

# ... and what now?

### ATLAS Exotics Searches\* - 95% CL Lower Limits (Status: HCP 2012)

| Category         | Search Description  | Mass Limit [TeV] | Notes   |
|------------------|---|------------------|---|
| Extra dimensions | Large ED (ADD) : monojet + $E_{T,miss}$   | 4.37 TeV         | $M_D$ ( $\delta=2$ )  |
|                  | Large ED (ADD) : monophoton + $E_{T,miss}$  | 1.93 TeV         | $M_D$ ( $\delta=2$ )  |
|                  | Large ED (ADD) : diphoton & dilepton, $m_{\gamma\gamma}/l$                              | 4.19 TeV         | $M_D$ (HLZ $\delta=3$ , NLO)  |
|                  | UED : diphoton + $E_{T,miss}$   | 1.41 TeV         | Compact. scale $R^2$  |
|                  | S/Z <sub>2</sub> ED : dilepton, $m_{ll}$  | 4.71 TeV         | $M_{KK} - R^{-1}$   |
|                  | RS1 : diphoton & dilepton, $m_{\gamma\gamma}/l$   | 2.23 TeV         | Graviton mass ( $k/M_{Pl} = 0.1$ )  |
|                  | RS1 : ZZ resonance, $m_{\gamma\gamma}/ll$   | 845 GeV          | Graviton mass ( $k/M_{Pl} = 0.1$ )  |
|                  | RS1 : WW resonance, $m_{\gamma\gamma}/ll$   | 1.23 TeV         | Graviton mass ( $k/M_{Pl} = 0.1$ )  |
|                  | RS g <sub>KK</sub> → tt (BR=0.925) : tt → H+jets, $m_{\gamma\gamma}/l$                  | 1.9 TeV          | $\tilde{g}_{KK}$ mass   |
|                  | ADD BH ( $M_{Th}/M_D=3$ ) : SS dimuon, $N_{ch,part}$                                    | 1.25 TeV         | $M_D$ ( $\delta=6$ )  |
| CI               | ADD BH ( $M_{Th}/M_D=3$ ) : leptons + jets, $\Sigma p_T$                                | 1.5 TeV          | $M_D$ ( $\delta=6$ )  |
|                  | Quantum black hole : dijet, $F(m_{ij})$   | 4.11 TeV         | $M_D$ ( $\delta=6$ )  |
|                  | qqqq contact interaction : $\chi^2(m_{ij})$   | 7.8 TeV          | $\Lambda$   |
|                  | qqll CI : ee & $\mu\mu$ , $m_{ij}$  | 13.9 TeV         | $\Lambda$ (constructive int.)   |
|                  | uutt CI : SS dilepton + jets + $E_{T,miss}$   | 1.7 TeV          | $\Lambda$   |
|                  | Z (SSM) : $m_{ee/\mu\mu}$   | 2.49 TeV         | Z mass  |
|                  | Z (SSM) : $m_{\tau\tau}$  | 1.4 TeV          | Z mass  |
|                  | W (SSM) : $m_{\tau\nu_{le}}$  | 2.55 TeV         | W mass  |
|                  | $W_R$ (→ tq, g=1) : $m_{\tau\nu_{le}}$  | 430 GeV          | W mass  |
|                  | $W_R$ (→ tb, SSM) : $m_{\tau\nu_{le}}$  | 1.13 TeV         | W mass  |
| LO               | $W^*$ : $m_{\tau\nu_{le}}$  | 2.42 TeV         | W* mass   |
|                  | Scalar LQ pair ( $\beta=1$ ) : kin. vars. in eejj, evjj                                 | 660 GeV          | 1 <sup>st</sup> gen. LQ mass  |
|                  | Scalar LQ pair ( $\beta=1$ ) : kin. vars. in $\mu\mu jj, \mu\nu jj$                     | 685 GeV          | 2 <sup>nd</sup> gen. LQ mass  |
|                  | Scalar LQ pair ( $\beta=1$ ) : kin. vars. in $\tau\tau jj, \tau\nu jj$                  | 538 GeV          | 3 <sup>rd</sup> gen. LQ mass  |
|                  | 4 <sup>th</sup> generation : $(T \rightarrow Wb)Wb$                                     | 656 GeV          | t mass  |
|                  | 4 <sup>th</sup> generation : $b\bar{b}(T_{5/3}, T_{5/3}) \rightarrow WW$                | 679 GeV          | b' ( $T_{5/3}$ ) mass   |
|                  | New quark b' : $b\bar{b}(T_{5/3}) \rightarrow Zb+X$ , $m_{23}$                          | 400 GeV          | b' mass   |
|                  | Top partner : $TT \rightarrow tt + A, A$ (dilepton), $M_{12}$                           | 483 GeV          | T mass ( $m(A) < 100$ GeV)  |
|                  | Vector-like quark : CC, $m_{\tau\nu_{le}}$  | 1.12 TeV         | VLQ mass (charge -1/3, coupling $\kappa_{q0} = v/m_{\nu}$ )               |
|                  | Vector-like quark : NC, $m_{\tau\nu_{le}}$  | 1.08 TeV         | VLQ mass (charge 2/3, coupling $\kappa_{q0} = v/m_{\nu}$ )                |
| Exotic ferm.     | Excited quarks : $\gamma$ -jet resonance, $m_{\gamma j}^{jet}$                          | 2.48 TeV         | q* mass   |
|                  | Excited quarks : dijet resonance, $m_{jj}^{jet}$  | 3.84 TeV         | q* mass   |
|                  | Excited lepton : $l$ - $\gamma$ resonance, $m_{l\gamma}$                                | 2.2 TeV          | l* mass ( $\Lambda = m(l^*)$ )  |
|                  | Techni-hadrons (LSTC) : dilepton, $m_{ll}^{hadron}$                                     | 850 GeV          | $\rho/\omega$ mass ( $m(\rho/\omega) - m(\pi_{\nu}) = M_{\nu}$ )          |
|                  | Techni-hadrons (LSTC) : WZ resonance ( $\nu ll$ ), $m_{ll}^{hadron}$                    | 483 GeV          | $\rho$ mass ( $m(\rho) = m(\pi_{\nu}) + m_{\nu}$ , $m(a) = 1.1 m(\rho)$ ) |
|                  | Major. neutr. (LRSM, no mixing) : 2-lep + jets  | 1.5 TeV          | N mass ( $m(W_{\nu}) = 2$ TeV)  |
|                  | $W_R$ (LRSM, no mixing) : 2-lep + jets  | 2.4 TeV          | $W_{\nu}$ mass ( $m(W_{\nu}) < 1.4$ TeV)                                  |
|                  | $H^{\pm}$ (DY prod., BR( $H^{\pm} \rightarrow ll$ )=1) : SS ee ( $\mu\mu$ ), $m_{ll}$   | 409 GeV          | $H^{\pm}$ mass (limit at 398 GeV for $\mu\mu$ )                           |
|                  | $H^{\pm}$ (DY prod., BR( $H^{\pm} \rightarrow e\mu$ )=1) : SS ee ( $\mu\mu$ ), $m_{ll}$ | 375 GeV          | $H^{\pm}$ mass  |
|                  | Color octet scalar : dijet resonance, $m_{jj}$  | 1.86 TeV         | Scalar resonance mass   |

ATLAS Preliminary

$\int Ldt = (1.0 - 13.0) \text{ fb}^{-1}$   
 $\sqrt{s} = 7, 8 \text{ TeV}$

Mass scale [TeV] (log scale from 10<sup>-1</sup> to 10<sup>2</sup>)

\*Only a selection of the available mass limits on new states or phenomena shown

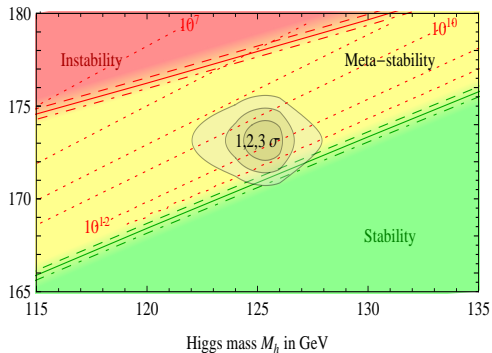
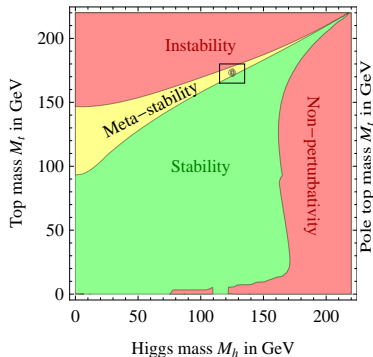


# Electroweak vacuum stability

- ▶ Most recent analysis: **Metastable vacuum with lifetime longer than the age of the universe**      Degrassi et al., arXiv:1205.6497

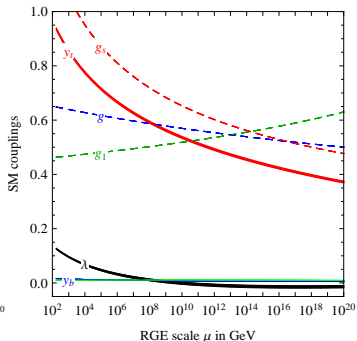
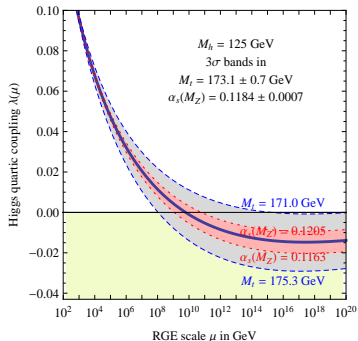
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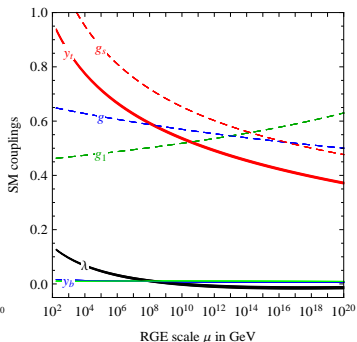
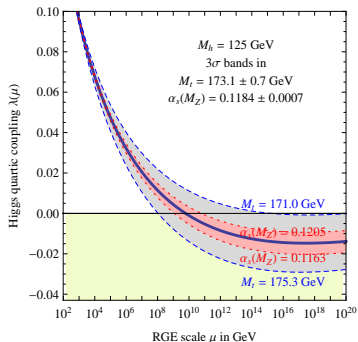
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- ▶ **Could the Higgs field ever have fallen in the correct vacuum?** Hertzberg, arXiv:1210.3624

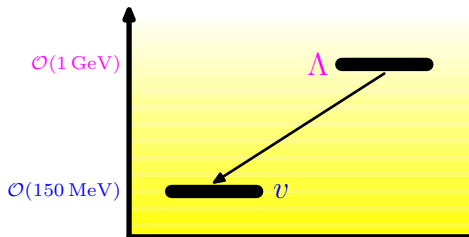
# Higgs as Pseudo-Goldstone boson

**Nambu-Goldstone Theorem:** For each *spontaneously broken global symmetry generator* there is a **massless boson** in the spectrum.

Old idea:

Georgi/Pais, 1974; Georgi/Dimopoulos/Kaplan, 1984

Light Higgs as **(Pseudo)-Goldstone boson** of a spontaneously broken global symmetry



Analogous: QCD

Scale  $\Lambda$ : chiral symmetry breaking, quarks,  $SU(3)_c$

Scale  $v$ : pions, kaons, ...

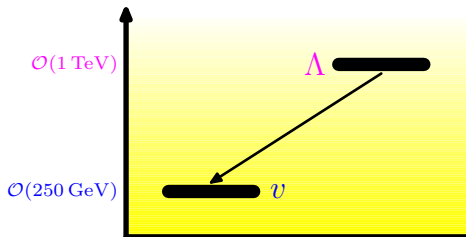
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Scale  $\Lambda$ : global symmetry breaking, new particles, new (gauge) IA

Scale  $v$ : Higgs,  $W/Z$ ,  $\ell^\pm$ , ...

Without Fine-Tuning: experimentally excluded

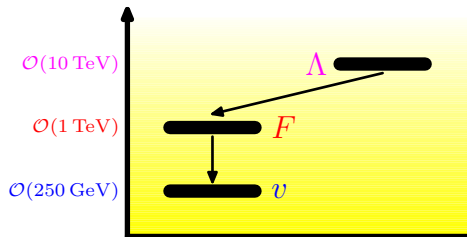
# Collective symmetry breaking and 3-scale models

**Collective symmetry breaking:** Arkani-Hamed/Cohen/Georgi/Nelson/..., 2001

2 different global symmetries; one of them unbroken  $\Rightarrow$  Higgs  
exact Goldstone boson

Coleman-Weinberg: boson masses by radiative corrections, but:  $m_H$  only at 2-loop level

$$m_H \sim \frac{g_1}{4\pi} \frac{g_2}{4\pi} \Lambda$$

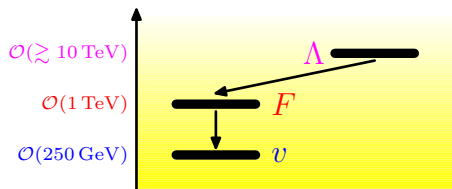


Scale  $\Lambda$ : global SB, new IA

Scale  $F$ : Pseudo-Goldstone bosons, new vectors/fermions

Scale  $v$ : Higgs,  $W/Z$ ,  $\ell^\pm$ , ...

# Characteristics and Spectra

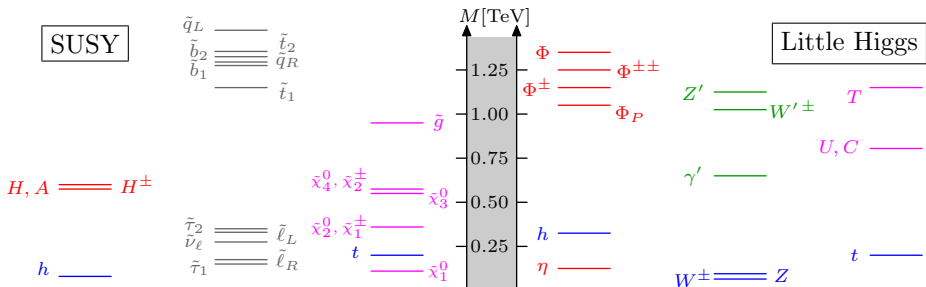


Scale  $\Lambda$ : “hidden sector”,  
symmetry breaking

Scale  $F$ : new particles

Scale  $v$ :  $h, W/Z, \ell^\pm, \dots$

Terascale: new particles to stabilize the hierarchy

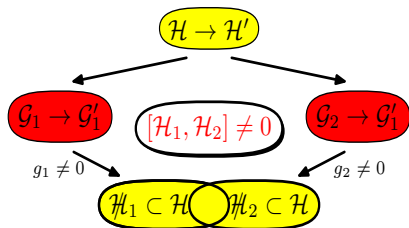


## Generic properties of Little-Higgs models

- Extended global symmetry (extended scalar sector)
- **Specific functional form of the potential**
- Extended gauge symmetry:  $\gamma' \equiv A_H, Z' \equiv Z_H, W'^{\pm} \equiv W_H$
- New heavy fermions:  $T$ , but also  $U, C, \dots$

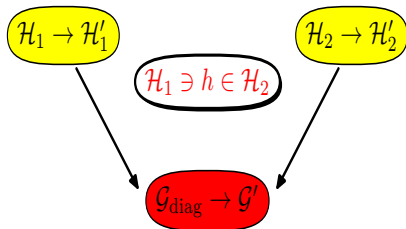
### Product Group Models

(e.g. Littlest Higgs)



### Simple Group Models

(e.g. Simplest Little Higgs)



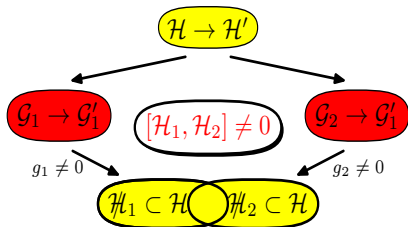
- discrete  $T(\text{TeV})$  parity: pair production, cascades, DM

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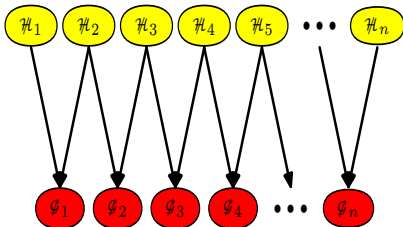
## Product Group Models

(e.g. Littlest Higgs)



## Moose Models

(e.g. Minimal Moose Model)



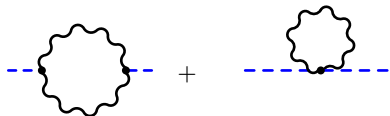
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## Prime Example: Simple Group Model

- ▶ enlarged gauge group:  $SU(3) \times U(1)$ ; globally  $U(3) \rightarrow U(2)$
- ▶ **Two** nonlinear  $\Phi$  representations  $\mathcal{L} = |D_\mu \Phi_1|^2 + |D_\mu \Phi_2|^2$

$$\Phi_{1/2} = \exp \left[ \pm i \frac{f_{2/1}}{f_{1/2}} \Theta \right] \begin{pmatrix} 0 \\ 0 \\ f_{1/2} \end{pmatrix} \quad \Theta = \frac{1}{\sqrt{f_1^2 + f_2^2}} \begin{pmatrix} \eta & 0 & h^* \\ 0 & \eta & \\ h^T & & \eta \end{pmatrix}$$

**Coleman-Weinberg mechanism:** Radiative generation of potential



The diagram shows two Feynman diagrams representing radiative corrections to a scalar potential. The first diagram is a tadpole diagram with a dashed external line and a loop of scalars. The second diagram is a sunset diagram with a dashed external line and a loop of scalars. The sum of these diagrams is equated to a mathematical expression for the radiatively generated potential.

$$= \frac{g^2}{16\pi^2} \Lambda^2 (|\Phi_1|^2 + |\Phi_2|^2) \sim \frac{g^2}{16\pi^2} f^2$$

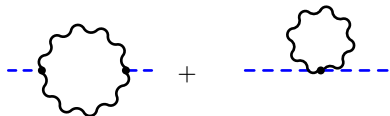


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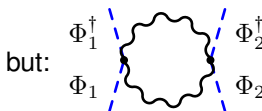
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**Coleman-Weinberg mechanism:** Radiative generation of potential



$$= \frac{g^2}{16\pi^2} \Lambda^2 (|\Phi_1|^2 + |\Phi_2|^2) \sim \frac{g^2}{16\pi^2} f^2$$

but:



$$= \frac{g^4}{16\pi^2} \log \left( \frac{\Lambda^2}{\mu^2} \right) |\Phi_1^\dagger \Phi_2|^2 \Rightarrow \frac{g^4}{16\pi^2} \log \left( \frac{\Lambda^2}{\mu^2} \right) f^2 (h^\dagger h)$$

# Cancellations of Divergencies in Yukawa sector

$$\propto \int \frac{d^4 k}{(2\pi)^4} \frac{1}{k^2(k^2 - m_T^2)} \left\{ \lambda_t^2(k^2 - m_T^2) + k^2 \lambda_T^2 - \frac{m_T}{F} \lambda_T k^2 \right\}$$

**Little Higgs global symmetry** imposes relation

$$\frac{m_T}{F} = \frac{\lambda_t^2 + \lambda_T^2}{\lambda_T}$$

$\Rightarrow$

**Quadratic divergence cancels**

**Collective Symm. break-**

**ing:**  $\lambda_t \propto \lambda_1 \lambda_2$ ,  $\lambda_1 = 0$   
 or  $\lambda_2 = 0 \Rightarrow SU(3) \rightarrow [SU(3)]^2$

$$\sim \frac{\lambda_1^2 \lambda_2^2}{16\pi^2} \log \left( \frac{\Lambda^2}{\mu^2} \right) |\Phi_1^\dagger \Phi_2|^2$$

# Constraints from Oblique Corrections: $S, T, U$



$$\Delta T \sim \Delta \rho \sim \Delta M_Z^2 Z \cdot Z$$



$$\Delta S \sim W^0{}_{\mu\nu} B^{\mu\nu}, \Delta U \sim W^0{}_{\mu\nu} W^{0\mu\nu}$$

◇ All low-energy effects order  $v^2/F^2$  (Wilson coefficients)

$\Delta S, \Delta T$  in the Littlest Higgs model, violation of **Custodial SU(2)**: Csáki et al., 2002; Hewett et al., 2002; Han et al., 2003; Chen/Dawson, 2003; Kilian/JRR, 2003

$$\frac{\Delta S}{8\pi} = - \left[ \frac{c^2(c^2-s^2)}{g^2} + 5 \frac{c'^2(c'^2-s'^2)}{g'^2} \right] \frac{v^2}{F^2} \rightarrow 0 \quad \alpha \Delta T \rightarrow \frac{5}{4} \frac{v^2}{F^2} - \frac{2v^2 \lambda_{2\phi}^2}{M_\phi^4} \gtrsim \frac{v^2}{F^2}$$

$$\text{Constraints from contact IA: } (f_{JJ}^{(3)}, f_{JJ}^{(1)}) \quad 4.5 \text{ TeV} \lesssim F/c^2 \quad 10 \text{ TeV} \lesssim F/c'^2$$

◇ **Constraints evaded**  $\iff c, c' \ll 1$

$B', Z', W'^{\pm}$  superheavy ( $\mathcal{O}(\Lambda)$ ) decouple from fermions

# Motivation

How to constrain a generic model in *HEP*?

- ▶ direct searches of resonances
- ▶ electroweak precision tests
- ▶ flavour constraints
- ▶ nowadays: Higgs sector

Higgs sector is the key to understand EW-scale physics (and beyond?)

# Statistical analysis

We considered the three most popular Little Higgs models:

- ▶ Simplest Little Higgs (*SLH*) [Schmaltz]
- ▶ Littlest Higgs (*L<sup>2</sup>H*) [Arkani-Hamed et al.]
- ▶ Littlest Higgs with *T*-parity (*LHT*) [Low et al.]

and realized a  $\chi^2$  analysis on their parameter spaces, taking into account the whole set of 7+8 TeV Higgs searches by *ATLAS* and *CMS*, and by fitting 21 different *EW* Precision Observables:

$$\chi^2 = \sum_i \frac{(\mathcal{O}_i - \mathcal{O}_i^{\text{exp}})^2}{\sigma_i^2}$$

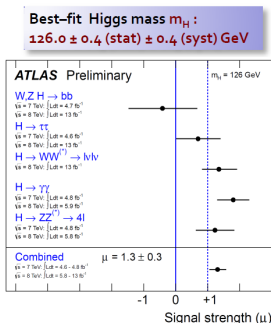
where  $\mathcal{O}_i$  depends on the free parameters of the model considered.

# Data used: Higgs sector

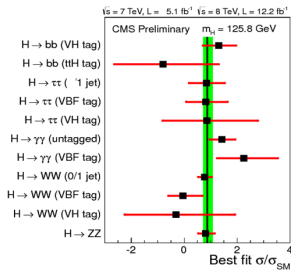
the Higgs results are expressed in terms of a *signal strength modifier*

$$\mu_i = \frac{\sum_p \epsilon^p_i \sigma_p}{\sum_p \epsilon^p_i \sigma_p^{SM}} \cdot \frac{BR(h \rightarrow X_i X_i)}{BR(h \rightarrow X_i X_i)_{SM}}$$

we included in our  $\chi^2$  analysis the best-fit values of  $\mu_i$  reported by the Collaborations for all the different 7+8 TeV channels  $i$ :



- $M = 125.8 \pm 0.4$  (stat)  $\pm 0.4$  (syst) GeV



- $\sigma/\sigma_{SM} = 0.88 \pm 0.21$

# Data used: *EWPD*

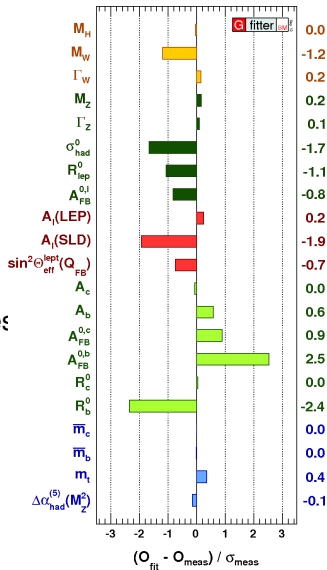
every extension of *SM* has to satisfy at least the precision constraints of the electroweak sector:

- ▶ low-energy observables

e.g.  $\nu$ -scattering, parity violation observables

- ▶  $Z$ -pole observables

e.g.  $m_Z$ ,  $\Gamma_Z$ ,  $Z$ -pole asymmetries...



# LH Smoking guns

Where do the  $LH$  corrections to the  $SM$  quantities come from?

- ▶ new decay channels of the Higgs, e.g.  $h \rightarrow A_H A_H$  in  $LHT$
- ▶ modified Higgs couplings with  $SM$  fermions and vector bosons

$$\text{e.g. } 2 \frac{m_W^2}{v} y_W h W^+ W^-, \quad y_W = \begin{cases} 1 & SM \\ 1 + \mathcal{O}(v^2/f^2) & LH \end{cases}$$

- ▶ interaction terms of Higgs with new fermions/vector bosons

$$\text{e.g. } \frac{m_T}{v} y_T h \bar{T} T \quad m_T \sim f, y_T \sim \mathcal{O}(v^2/f^2)$$

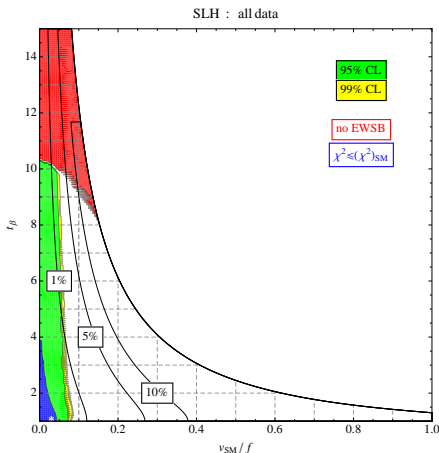
- ▶ modified neutral- and charged-currents

$$\text{e.g. } \frac{g}{c_W} \sum_f \bar{f} \gamma^\mu \left( (g_L^{SM} + \delta g_L) P_L + (g_R^{SM} + \delta g_R) P_R \right) f Z_\mu$$



# SLH results

JRR/Tonini, JHEP 1302 (2013) 077



- ▶ free parameters:  $f$  SSB scale,  $t_\beta$  ratio of vevs of scalar fields  $\phi_{1,2}$
- ▶  $f_{\min}^{99\%} = 2.88$  TeV, translates into lower bounds on new states' masses, e.g.

$$m_{W'} \gtrsim 1.35 \text{ TeV}$$

$$m_T \gtrsim 2.81 \text{ TeV}$$

- ▶ min. required fine tuning:  $\sim 1\%$ , defined as

$$\Delta = \frac{|\delta\mu^2|}{\mu_{\text{obs}}^2}$$

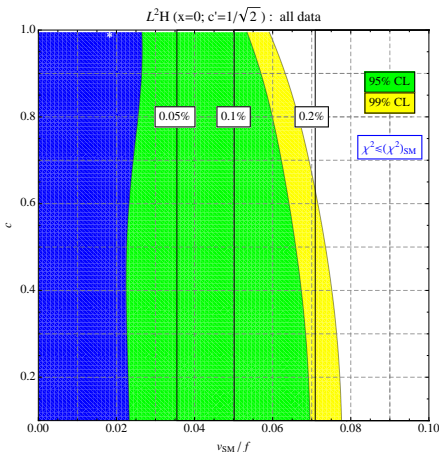
- ▶ results mainly driven by *EWPD*

$$\chi_{\min}^2/\text{d.o.f.} = 1.043$$

$$\chi_{SM}^2/\text{d.o.f.} = 1.048$$

# $L^2H$ results

JRR/Tonini, JHEP 1302 (2013) 077



- ▶ free parameters:  $f$  SSB scale,  $c$  mixing angle in gauge sector
- ▶  $f_{\min}^{99\%} = 3.20$  TeV, translates into lower bounds on new states' masses, e.g.

$$m_{W'} \gtrsim 2.13 \text{ TeV}$$

$$m_T \gtrsim 4.50 \text{ TeV}$$

- ▶ min. required fine tuning:  $\sim 0.1\%$ , defined as

$$\Delta = \frac{|\delta\mu^2|}{\mu_{\text{obs}}^2}$$

- ▶ results mainly driven by *EWPD*

$$\chi_{\min}^2/\text{d.o.f.} = 1.048$$

$$\chi_{SM}^2/\text{d.o.f.} = 1.049$$

## Partial decay widths in $LH$

- ▶ 1-loop decays

$$\Gamma(h \rightarrow gg)_{LH} \sim \frac{\alpha_s^2 m_h^3}{32\pi^3 v^2} \left| \sum_{f, \text{col}} -\frac{1}{2} F_{\frac{1}{2}}(x_f) y_f \right|^2$$

$$\Gamma(h \rightarrow \gamma\gamma)_{LH} \sim \frac{\alpha^2 m_h^2}{256\pi^3 v^2} \left| \sum_{f, \text{ch}} \frac{4}{2} F_{\frac{1}{2}}(x_f) y_f + \sum_{v, \text{ch}} F_1(x_v) y_v + \sum_{s, \text{ch}} F_0(x_s) y_s \right|^2$$

where  $x_i = \frac{4m_i^2}{m_h^2}$ ,  $F_i(x_i)$  are loop functions,  $y_i$  the modified Yuk. coupl.

$$\Rightarrow \text{ narrow-width approximation: } \frac{\sigma_{LH}}{\sigma_{SM}}(gg \rightarrow h) = \frac{\Gamma(h \rightarrow gg)_{LH}}{\Gamma(h \rightarrow gg)_{SM}}$$

- ▶ tree-level decays

$$\Gamma(h \rightarrow VV)_{LH} \sim \Gamma(h \rightarrow VV)_{SM} \left( \frac{g_{hVV}}{g_{hVV}^{SM}} \right)^2$$

$$\Gamma(h \rightarrow f\bar{f})_{LH} \sim \Gamma(h \rightarrow f\bar{f})_{SM} \left( \frac{g_{hff}}{g_{hff}^{SM}} \right)^2$$

where  $g_{hVV} = \frac{m_V^2}{v} y_V$  and  $g_{hff} = \frac{m_f}{v} y_f$

# LHT: Littlest Higgs with T parity

- ▶ Goldstone boson matrix:

$$\Sigma = e^{2i\Pi/f} \quad \Pi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & H & \sqrt{2}\Phi \\ H^\dagger & 0 & H^t \\ \sqrt{2}\Phi^\dagger & H^* & 0 \end{pmatrix} \quad \Phi \propto \begin{pmatrix} \sqrt{2}\phi^{++} & \phi^+ \\ \phi^+ & \phi^0 + i\phi^P \end{pmatrix}$$

- ▶ Discrete  $T$  parity:

$$T: \quad \Pi \rightarrow -\Omega \Pi \Omega \quad \Omega = \text{diag}(1, 1, -1, 1, 1)$$

$$V_{CW} = \lambda_{\phi^2} f^2 \text{Tr}(\phi^\dagger \phi) + i\lambda_{h\phi h} f (H\phi^\dagger H^t - H^* \phi H^\dagger) - \mu^2 H H^\dagger + \lambda_{h^4} (H H^\dagger)^2 + \\ + \lambda_{h\phi\phi h} H\phi^\dagger \phi H^\dagger + \lambda_{h^2\phi^2} H H^\dagger \text{Tr}(\phi^\dagger \phi) + \lambda_{\phi^2\phi^2} [\text{Tr}(\phi^\dagger \phi)]^2 + \lambda_{\phi^4} \text{Tr}(\phi^\dagger \phi \phi^\dagger \phi).$$

$$\lambda_{\phi^2} = 2(g^2 + g'^2) + 8\lambda_1^2 \quad \lambda_{h^4} = \frac{1}{4}\lambda_{\phi^2} \quad \lambda_{h\phi\phi h} = -\frac{4}{3}\lambda_{\phi^2} \\ \lambda_{h^2\phi^2} = -16\lambda_1^2 \quad \lambda_{\phi^4} = -\frac{8}{3}(g^2 + g'^2) + \frac{16}{3}\lambda_1^2$$

- ▶ Yukawa couplings  $k, R \equiv \lambda_1/\lambda_2$

$$\mathcal{L}_k = -kf \left( \bar{\Psi}_2 \xi \Psi_c + \bar{\Psi}_1 \langle \Sigma \rangle \Omega \xi^\dagger \Omega \Psi_c \right) - m_q \bar{u}'_c u_c - m_q \bar{d}'_c d_c - m_\chi \bar{\chi}'_c \chi_c + \text{h.c.}$$

$$\mathcal{L}_t = -\frac{\lambda_1 f}{2\sqrt{2}} \epsilon_{ijk} \epsilon_{xy} \left[ (\bar{\Psi}_{1,t})_i \Sigma_{jx} \Sigma_{ky} - (\bar{\Psi}_{2,t} \langle \Sigma \rangle)_i \Sigma'_{jx} \Sigma'_{ky} \right] t'_R - \lambda_2 f (\bar{T}_{L1} T_{R1} + \bar{T}_{L2} T_{R2})$$

# $T$ parity and Dark Matter

Cheng/Low, 2003; Hubisz/Meade, 2005; Wang/Yang/Zhu,

2013

- ▶  $T$  parity:  $T^a \rightarrow T^a$ ,  $X^a \rightarrow -X^a$ , automorphism of coset space analogous to  $R$  parity in SUSY, KK parity in extra dimensions
- ▶ Bounds on  $F$  MUCH relaxed,  $F \sim 0.5 - 1 \text{ TeV}$   
*but*: Pair production!, typical **cascade decays**
- ▶ Lightest  $T$ -odd particle (LTP)  $\Rightarrow$  **Candidate for Cold Dark Matter**

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Littlest Higgs:  $A'$  LTP

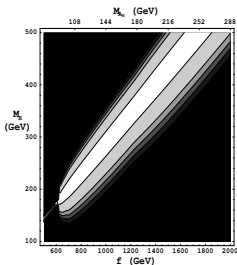
$W', Z' \sim 650 \text{ GeV}$ ,  $\Phi \sim 1 \text{ TeV}$

$T, T' \sim 0.7-1 \text{ TeV}$

Annihilation:  $A'A' \rightarrow h \rightarrow WW, ZZ, hh$

Hubisz/Meade, 2005

0/10/50/70/100



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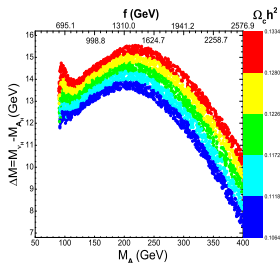
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Wang/Yang/Zhu, 2013

Relic density/SI cross section



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Wang/Yang/Zhu, 2013

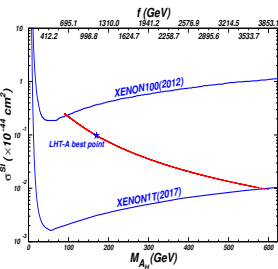
Relic density/SI cross section

- ▶  $T$  parity Simplest LH: **Pseudo-Axion  $\eta$  LTP**

$Z'$  remains odd: good or bad (?)

Martin, 2006; JRR/Tonini, in prep.

- ▶  $T$  parity might be anomalous (???)

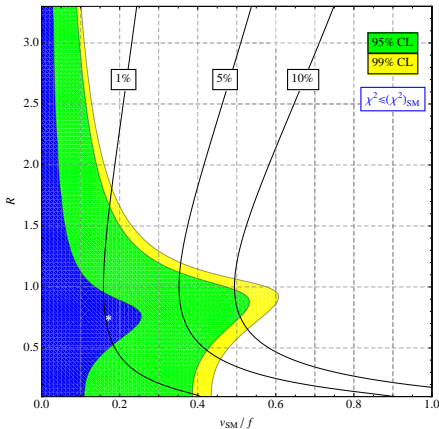


Hill/Hill, 2007



# LHT results

LHT (Case A) : all data



$$\chi_{\min}^2/\text{d.o.f.} = 1.048$$

$$\chi_{\text{SM}}^2/\text{d.o.f.} = 1.053$$

- ▶ free parameters:  $f$  SSB scale,  $R$  ratio of Yukawa couplings in top sector
- ▶  $f_{\min}^{99\%} = 405.9$  GeV, translates into lower bounds on new states' masses, e.g.

$$m_{W'} \gtrsim 269.6 \text{ GeV}$$

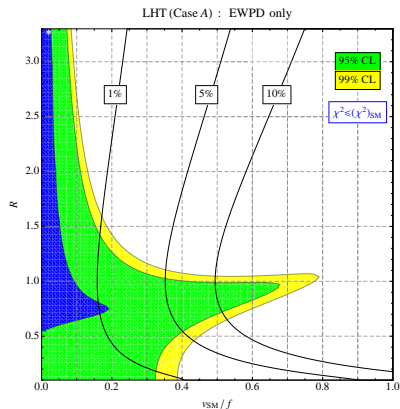
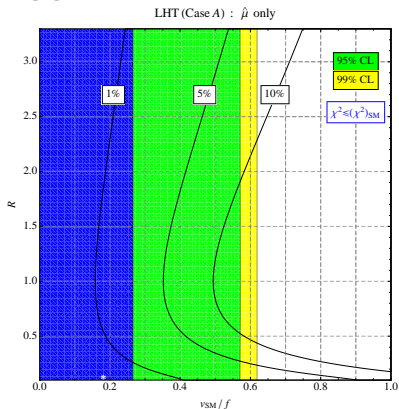
$$m_T \gtrsim 553.6 \text{ GeV}$$

- ▶ min. required fine tuning:  $\sim 10\%$ , defined as

$$\Delta = \frac{|\delta\mu^2|}{\mu_{\text{obs}}^2}$$

- ▶ results mainly driven by EWPD (see next slide)

# Higgs data vs. $EWPD$

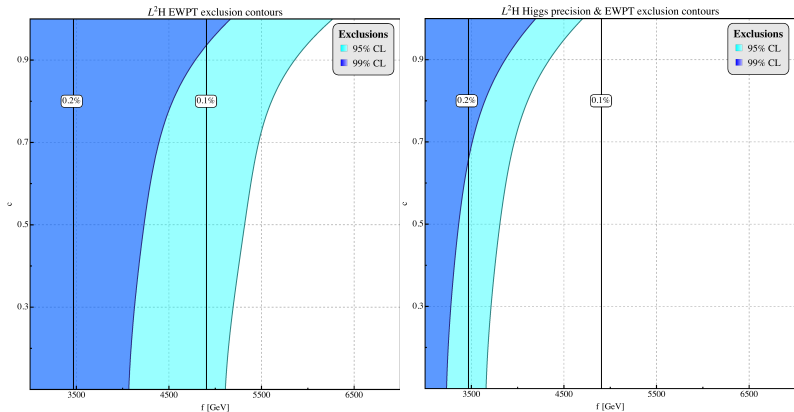


- ▶ the shape of the combined result is driven by the  $EW$  constraints (much smaller uncertainties)
- ▶ Higgs data only: for  $v/f \gtrsim 0.6$  decay  $h \rightarrow A_H A_H$  open and dominant
- ▶ Higgs data only: subdominant dependence on  $R$  w.r.t.  $f$  is a consequence of the Collective LHT Symmetry Breaking mechanism

# New Results (incl. Moriond '13)

JRR/Tonini/de Vries, 1307.5010

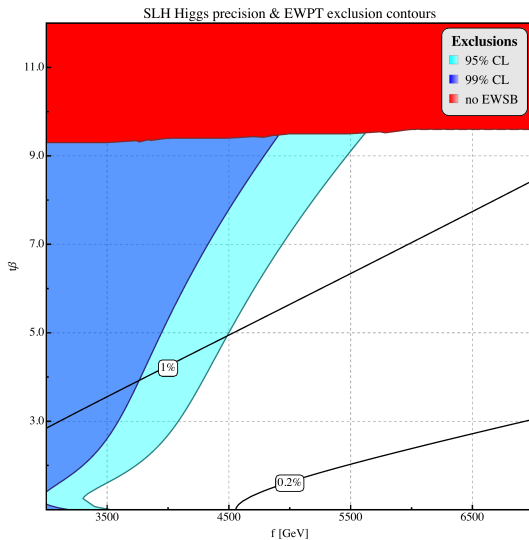
## Littlest Higgs Model



# New Results (incl. Moriond '13)

## Simplest Little Higgs

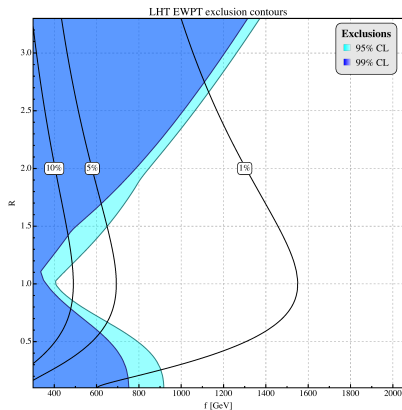
JRR/Tonini/de Vries, 1307.5010



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JRR/Tonini/de Vries, 1307.5010

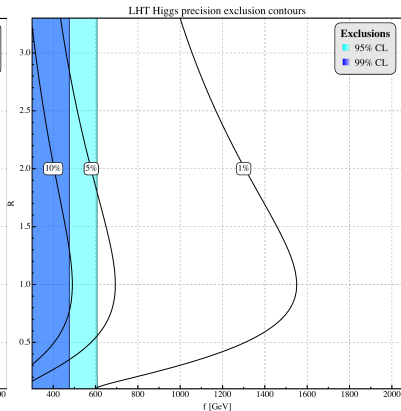
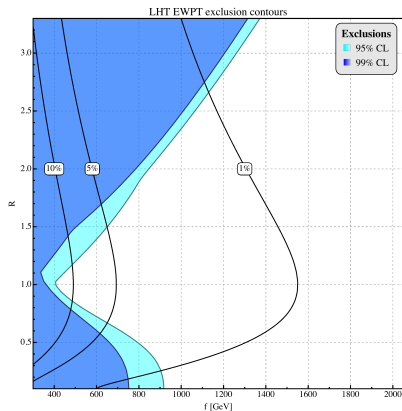
## Littlest Higgs with $T$ Parity



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JRR/Tonini/de Vries, 1307.5010

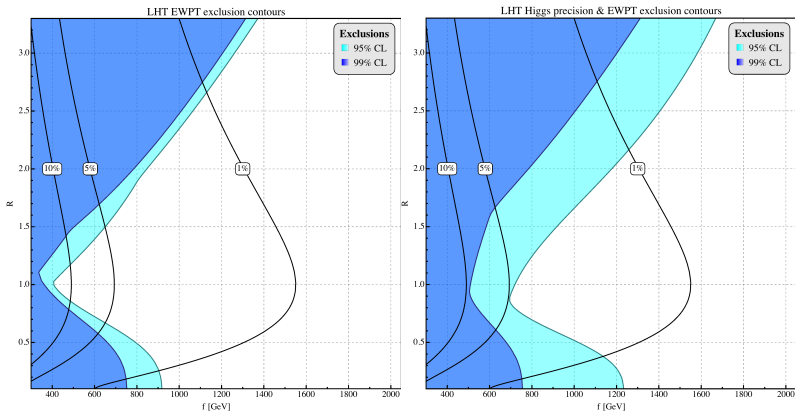
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JRR/Tonini/de Vries, 1307.5010

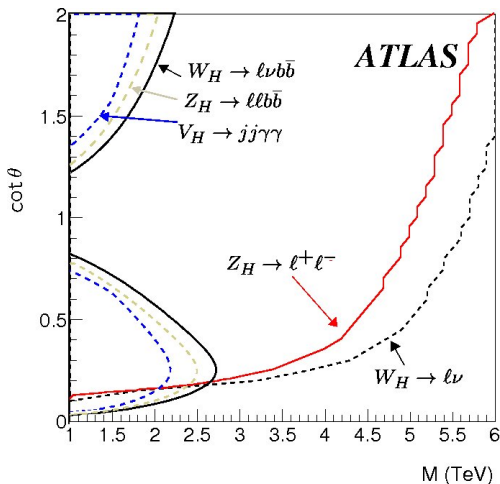
## Littlest Higgs with $T$ Parity



▶ EWPT and Higgs data  $\Rightarrow$

$$f \gtrsim 694 \text{ GeV}$$

## Direct searches: Drell-Yan mainly

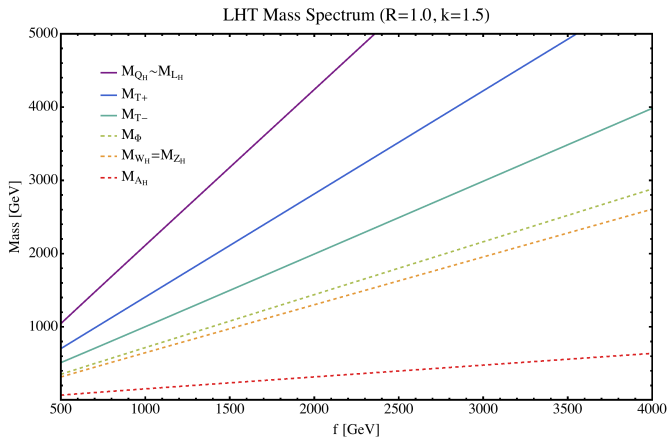


**Reach in the gauge boson sector:** depends on mixing angle



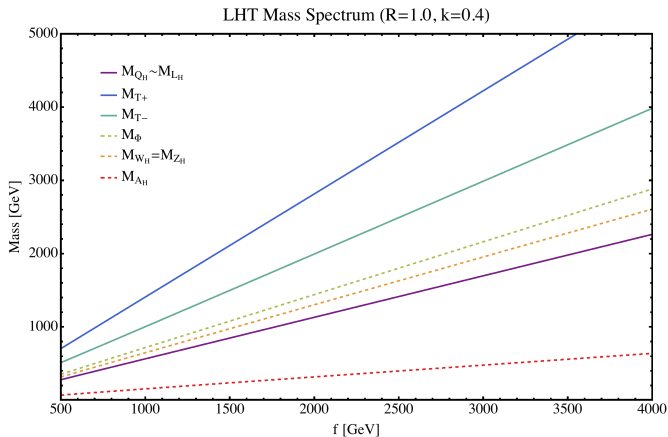
# Direct Searches: Focus on LHT

- ▶ Defining two benchmark scenarios: 1. heavy quarks



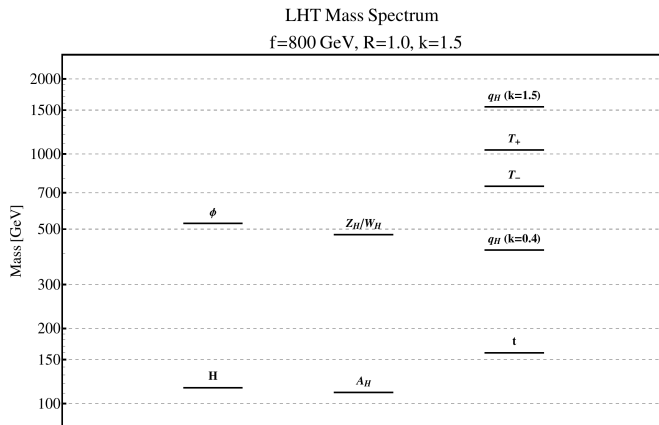
# Direct Searches: Focus on LHT

- ▶ Defining two benchmark scenarios: 2. heavy top/vectors



# Direct Searches: Focus on LHT

- Defining two benchmark scenarios: 1.  $k = 1.5$ , 2.  $k = 0.4$



# Branching Ratios

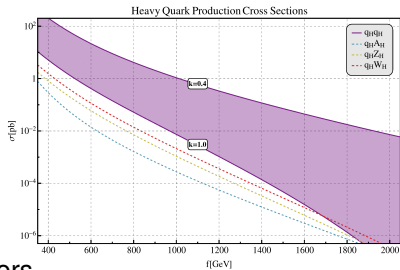
► Decay patterns:

| Particle    | Decay           | BR <sub>k=1.0</sub> | BR <sub>k=0.4</sub> |
|-------------|-----------------|---------------------|---------------------|
| $l_H^\pm$   | $W_H^\pm \nu$   | 62%                 | 0%                  |
|             | $Z_H l^\pm$     | 31%                 | 0%                  |
|             | $A_H l^\pm$     | 6%                  | 100%                |
| $\nu_H^\pm$ | $W_H^\pm l^\mp$ | 61%                 | 0%                  |
|             | $Z_H \nu$       | 30%                 | 0%                  |
|             | $A_H \nu$       | 9%                  | 100%                |
| $T_H^+$     | $W^+ b$         | 46%                 | 45%                 |
|             | $Z t$           | 22%                 | 22%                 |
|             | $H t$           | 21%                 | 21%                 |
|             | $T_H^- A_H$     | 11%                 | 11%                 |
| $A_H$       | stable          |                     |                     |
| $Z_H$       | $A_H H$         | 100%                | 2%                  |
|             | $d_H d$         | 0%                  | 41%                 |
|             | $u_H u$         | 0%                  | 30%                 |
|             | $l_H^\pm l^\mp$ | 0%                  | 14%                 |
|             | $\nu_H \nu$     | 0%                  | 14%                 |

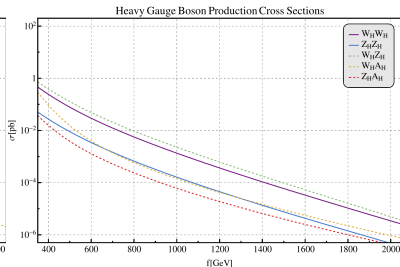
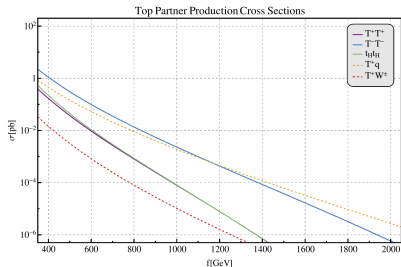
| Particle        | Decay           | BR <sub>k=1.0</sub> | BR <sub>k=0.4</sub> |
|-----------------|-----------------|---------------------|---------------------|
| $d_H$           | $W_H^- u$       | 62%                 | 0%                  |
|                 | $Z_H d$         | 30%                 | 0%                  |
|                 | $A_H d$         | 6%                  | 100%                |
| $u_H$           | $W_H^+ d$       | 58%                 | 0%                  |
|                 | $Z_H u$         | 30%                 | 0%                  |
|                 | $A_H u$         | 9%                  | 100%                |
| $T_H^-$         | $A_H t$         | 100%                | 100%                |
|                 | $Z_H t$         | 0%                  | 0%                  |
| $\Phi^{0/P}$    | $A_H H$         | 100%                | 100%                |
| $\Phi^\pm$      | $A_H W^\pm$     | 100%                | 100%                |
| $\Phi^{\pm\pm}$ | $A_H (W^\pm)^2$ | 100%                | 96%                 |
| $W_H^\pm$       | $A_H W^\pm$     | 100%                | 2%                  |
|                 | $u_H d$         | 0%                  | 44%                 |
|                 | $d_H u$         | 0%                  | 27%                 |
|                 | $l_H^\pm \nu$   | 0%                  | 16.5%               |
|                 | $\nu_H l^\pm$   | 0%                  | 16.5%               |

# Cross Sections (I)

## ► Heavy Quarks



## ► Heavy Top and Vectors



# Channels and signatures: Parameters

| final state |        |                | modes  | params                               | final state   |        |                | modes   | params                     |
|-------------|--------|----------------|--|--------------------------------------|---------------|--------|----------------|---|----------------------------|
| leptons     | # jets | $\cancel{E}_T$ |  |                                      | leptons       | # jets | $\cancel{E}_T$ |   |                            |
| 0           | 1      | ✓              | $q_H A_H$  | $f, k$                               | $l^\pm$       | 2      | ✓              | $W_H^\pm W_H^\mp$<br>$W_H^\pm Z_H$<br>$q_H q_H$ | $f, k$<br>$f, k$<br>$f, k$ |
| 0           | 2      | ✓              | $q_H q_H$  | $f, k$                               | $l^\pm$       | 3      | ✓              | $q_H W_H^\pm$<br>$T^+ q$                        | $f, k$<br>$f, k, R$        |
| 0           | 3      | ✓              | $q_H W_H^\pm$  | $f, k$                               | $l^\pm$       | 4      | ✓              | $q_H q_H$<br>$T^- T^-$                          | $f, k$<br>$f, k, R$        |
| 0           | 4      | ✓              | $q_H q_H$<br>$W_H^\pm W_H^\mp$<br>$W_H^\pm Z_H$<br>$Z_H Z_H$ | $f, k$<br>$f, k$<br>$f, k$<br>$f, k$ | $l^+ l^-$     | 0      | ✓              | $W_H^\pm W_H^\mp$                               | $f, k$                     |
| 0           | 4      | ✗              | $T^+ q$  | $f, k, R$                            | $l^+ l^-$     | 1      | ✓              | $q_H W_H^\pm$                                   | $f, k$                     |
| 0           | 5      | ✓              | $q_H W_H^\pm$  | $f, k$                               | $l^+ l^-$     | 2      | ✓              | $q_H q_H$<br>$T^- T^-$                          | $f, k$<br>$f, k, R$        |
| 0           | 6      | ✓              | $q_H q_H$<br>$T^- T^-$                                       | $f, k$<br>$f, k, R$                  | $l^\pm l^\pm$ | 2      | ✓              | $q_H q_H$                                       | $f, k$                     |

# Channels and signatures (I)

| final state |                   |                | production<br>modes | $\sigma_{8\text{ TeV}} \times \text{Br (fb)}$ |                   | $\sigma_{14\text{ TeV}} \times \text{Br (fb)}$ |                   |
|-------------|-------------------|----------------|---------------------|---|-------------------|--|-------------------|
| $\# l^\pm$  | $\# \text{ jets}$ | $\cancel{E}_T$ |                     | $k = 1.0$                                     | $k = 0.4$         | $k = 1.0$                                      | $k = 0.4$         |
| 0           | 1                 | ✓              | $q_H A_H$           | 0.24  | $1.1 \times 10^2$ | 2.1  | $4.5 \times 10^2$ |
| 0           | 2                 | ✓              | $q_H q_H$           | 0.56  | $5.6 \times 10^3$ | 5.2  | $3.2 \times 10^4$ |
| 0           | 3                 | ✓              | $q_H W_H^\pm$       | 0.73  | 14                | 8.0  | 77                |
|             |                   |                | $q_H Z_H$           | 0.76  | 8.6               | 8.0  | 49                |
| 0           | 4                 | ✓              | $q_H q_H$           | 4.0   | $9.1 \times 10^2$ | 35   | $5.6 \times 10^3$ |
|             |                   |                | $W_H^\pm W_H^\mp$   | 1.9   | low               | 9.1  | low               |
|             |                   |                | $W_H^\pm Z_H$       | 4.8   | low               | 23   | low               |
|             |                   |                | $Z_H Z_H$           | 0.56  | low               | 3.0  | low               |
| 0           | 4                 | ✗              | $T^+ q$             | 2.0   | 2.0               | 17   | 17                |
| 0           | 5                 | ✓              | $q_H W_H^\pm$       | 5.1   | ✗                 | 54   | ✗                 |
|             |                   |                | $q_H Z_H$           | 4.1   | ✗                 | 44   | ✗                 |
| 0           | 6                 | ✓              | $q_H q_H$           | 1.6   | $9.7 \times 10^2$ | $1.7 \times 10^2$                              | $6.0 \times 10^3$ |
|             |                   |                | $T^- T^-$           | 2.5   | 2.5               | 25   | 25                |

# Channels and signatures (II)

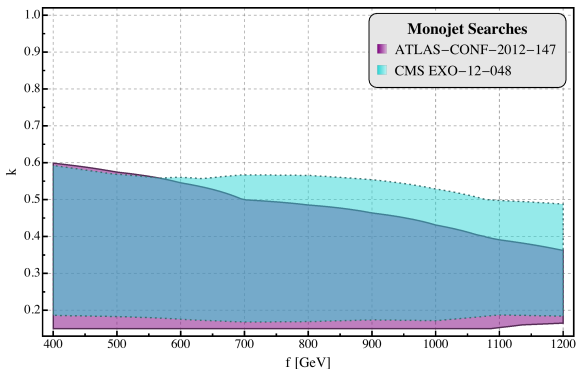
| final state   |        |                | production<br>modes | $\sigma_{8 \text{ TeV}} \times \text{Br (fb)}$ |                   | $\sigma_{14 \text{ TeV}} \times \text{Br (fb)}$ |                   |
|---------------|--------|----------------|---------------------|--|-------------------|---|-------------------|
| # $l^\pm$     | # jets | $\cancel{E}_T$ |                     | $k = 1.0$                                      | $k = 0.4$         | $k = 1.0$                                       | $k = 0.4$         |
| $l^\pm$       | 2      | ✓              | $q_H q_H$           | 0.058  | $9.0 \times 10^2$ | 1.1   | $5.6 \times 10^3$ |
|               |        |                | $W_H^\pm W_H^\mp$   | 0.77   | low               | 3.9   | low               |
|               |        |                | $W_H^\pm Z_H$       | 2.1  | low               | 10  | low               |
|               |        |                | $T^+ q$             | 1.3  | 1.2               | 10  | 10                |
| $l^\pm$       | 3      | ✓              | $q_H W_H^\pm$       | 3.5  | ✗                 | 37  | ✗                 |
|               |        |                | $q_H Z_H$           | 0.99   | ✗                 | 11  | ✗                 |
| $l^\pm$       | 4      | ✓              | $q_H q_H$           | 7.4  | $9.7 \times 10^2$ | 82  | $6.0 \times 10^3$ |
|               |        |                | $T^- T^-$           | 2.2  | 2.2               | 21  | 21                |
| $l^+ l^-$     | 0      | ✓              | $W_H^\pm W_H^\mp$   | 0.32   | low               | 1.7   | low               |
| $l^+ l^-$     | 1      | ✓              | $q_H W_H^\pm$       | 0.54   | ✗                 | 5.8   | ✗                 |
| $l^+ l^-$     | 2      | ✓              | $q_H q_H$           | 1.1  | ✗                 | 11  | ✗                 |
|               |        |                | $T^- T^-$           | 0.47   | 0.47              | 4.6   | 4.6               |
| $l^\pm l^\pm$ | 2      | ✓              | $q_H q_H$           | 0.37   | ✗                 | 2.7   | ✗                 |



# Recasting results

JRR/Tonini/deVries,2013

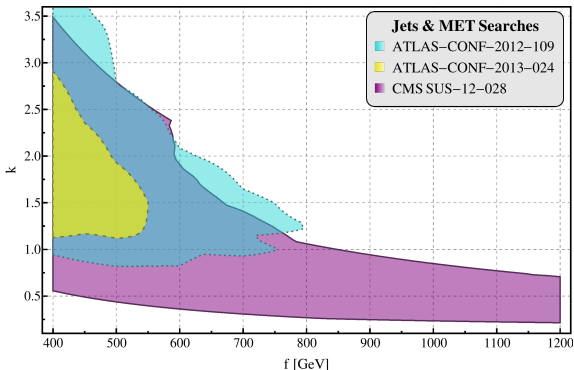
- **95% CL from Monojets +  $\cancel{E}_T$  from LHC8**
- 1 hard jet,  $\cancel{E}_T$ , no leptons, 2nd jet w.  $p_T > 30$  GeV  
signal regions: ATLAS ( $p_T, \cancel{E}_T$ ) > 120/220/350/500 GeV, CMS:  $\cancel{E}_T > 250/300/350/400/450/500/550$  GeV
- Dijet suppression: ATLAS  $\Delta\phi(\cancel{E}_T, j_2) > 0.5$ , CMS  $\Delta\phi(j_1, j_2) < 2.5$
- $pp \rightarrow q_H q_H, pp \rightarrow q_H A_H$



# Recasting results

JRR/Tonini/deVries,2013

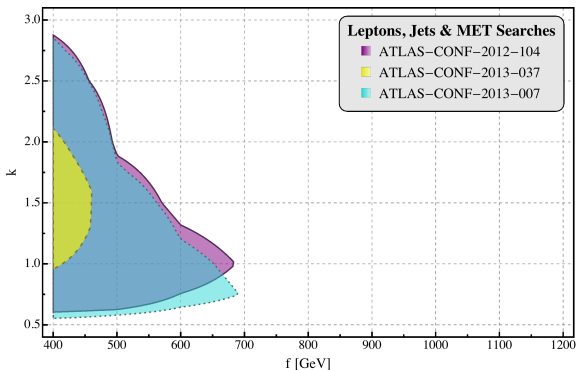
- 95% CL from Jets +  $\cancel{E}_T$  from LHC8
- $\geq 2$  hard jets,  $\cancel{E}_T$ , no leptons
- signal regions: ATLAS  $\cancel{E}_T > 200/300/350$  GeV, CMS:  
 $(N_j, N_b) = (2 - 3, 0); (2 - 3, 1 - 2); (\geq 4, 1 - 2); (\geq 4, 0); (\geq 4, \geq 2)$
- QCD suppression: ATLAS  $\Delta\phi(\cancel{E}_T, j_2) > 0.5$ ,  $\cancel{E}_T/m_{eff}$ , CMS  $\Delta\phi(j_1, j_2) < 2.5$
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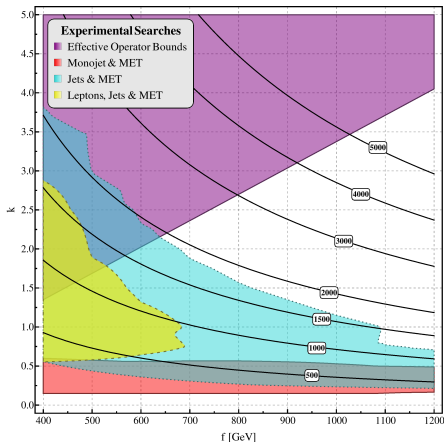
- 95% CL from Leptons + Jets +  $\cancel{E}_T$  from LHC8
- single isolated lepton,  $\geq 2$  hard jets,  $\cancel{E}_T$ ,
- signal regions: ATLAS  $\cancel{E}_T > 200/300/350$  GeV
- Cuts:  $\cancel{E}_T > 250$  GeV,  $m_T(l, \cancel{E}_T) > 250$  GeV,  $\cancel{E}_T/m_{\text{eff}} > 0.2$ ,  $m_{\text{eff}}^{\text{inc}} > 800$  GeV
- $pp \rightarrow q_H q_H$  with  $q_H \rightarrow W_H q, Z_H q, t_H \rightarrow t A_H, Z_H \rightarrow H A_H$



# Combined analysis

JRR/Tonini/deVries, 2013

- ▶ Operator bounds:  $\mathcal{O}_{4f} = -\frac{k^2}{128\pi^2 f^2} \bar{\psi}_L \gamma^\mu \psi_L \bar{\psi}'_L \gamma_\mu \psi'_L + \mathcal{O}\left(\frac{g}{k}\right)$   
Hubisz/Meade/Noble/Perelstein, 2005



- ▶ Bound from combined analysis:  $f \gtrsim 638\text{GeV}$

# Conclusions

- ▶ *Little Higgs* models are an appealing solution to the hierarchy problem, alternative to weakly coupled solutions like *SUSY*
- ▶ most of the parameter space of three popular *Little Higgs* models is still compatible at  $\sim 99\%$  *CL* with the early results of the 7+8 TeV Higgs searches
- ▶ electroweak precision data represent still the most severe constraints
- ▶ fine-tuning as a guideline to understand the naturalness of a model: *Little Higgs* models require a minimum level of  $\sim 10\%$  of fine tuning
- ▶ Limits on the LHT:

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$$f \gtrsim 405 \text{ GeV@95\% CL}$$

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- ▶ We need more data!



# Lessons from Lepton Photon 2013 ...

There are either colored exotics ...



# Lessons from Lepton Photon 2013 ...

... or the world is fine tuned



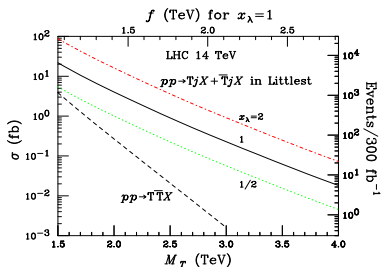


どうもありがとうございます



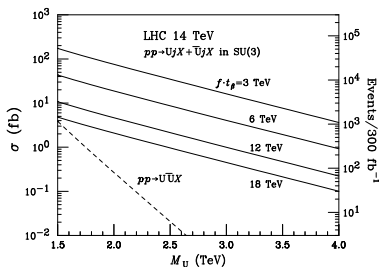
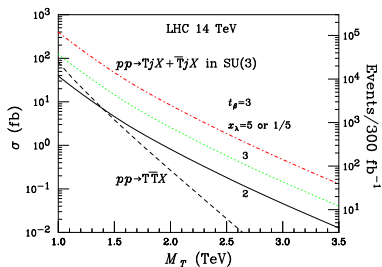
# Direct Searches – Heavy Quark States

- EW single dominates QCD pair production: Perelstein/Peskin/Pierce, '03



# Direct Searches – Heavy Quark States

- EW single dominates QCD pair production: Perelstein/Peskin/Pierce, '03



- Characteristic branching ratios :

$$\Gamma(T \rightarrow th) \approx \Gamma(T \rightarrow tZ) \approx \frac{1}{2} \Gamma(T \rightarrow bW^+) \approx \frac{M_T \lambda_T^2}{64\pi}, \quad \Gamma_T \sim 10-50 \text{ GeV}$$

- Proof of  $T$  as EW singlet; but:  $T \rightarrow Z'T, W'b, t\eta$  !

AIM: Determination of  $M_T, \lambda_T, \lambda_{T'}$

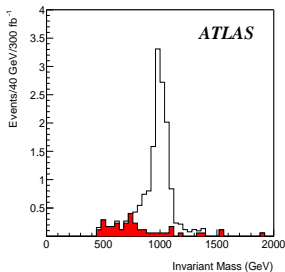
$\lambda_{T'}$  indirect ( $T\bar{T}h$  impossible)



$$T \rightarrow Zt \rightarrow \ell^+ \ell^- \ell \nu b$$

SN-ATLAS-2004-038

- 
- ▶  $E_T > 100 \text{ GeV}$ ,  $l\ell l$ ,  $p_T > 100/30 \text{ GeV}$ ,  
 $b$ ,  $p_T > 30 \text{ GeV}$
  - ▶ Bkgd.:  $WZ$ ,  $ZZ$ ,  $btZ$
  - ▶ Observation for  $M_T \lesssim 1.4 \text{ TeV}$

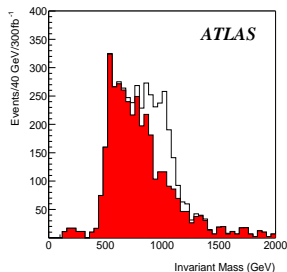


$$T \rightarrow Wb \rightarrow \ell\nu b$$

 SN-ATLAS-2004-038
 

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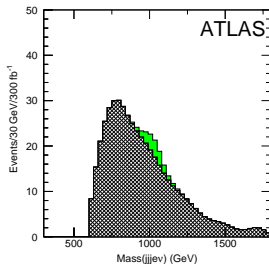
- ▶  $\cancel{E}_T > 100 \text{ GeV}$ ,  $\ell, p_T > 100 \text{ GeV}$ ,  
 $b, p_T > 200 \text{ GeV}$ , max.  $jj, p_T > 30 \text{ GeV}$
- ▶ Bkgd.:  $t\bar{t}$ ,  $Wb\bar{b}$ , single  $t$
- ▶ Observation for  $M_T \lesssim 2.5 \text{ TeV}$



$$T \rightarrow th \rightarrow \ell\nu bbb$$

SN-ATLAS-2004-038

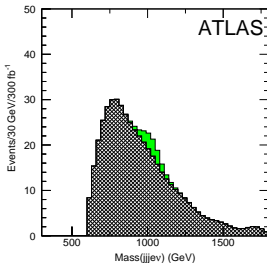
- 
- ▶  $\ell, p_T > 100 \text{ GeV}, jjj, p_T > 130 \text{ GeV},$   
at least 1  $b$ -tag
  - ▶ Bkgd.:  $t\bar{t}, Wb\bar{b},$  single  $t$
  - ▶ Observation for  $M_T \lesssim 2.5 \text{ TeV}$



$T \rightarrow th \rightarrow \ell\nu bbb$ 

SN-ATLAS-2004-038

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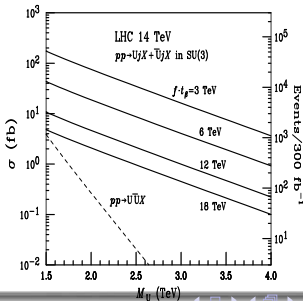


Additional heavy quarks (Simple Group Models):  $U, C$  or  $D, S$

Han et al.,

05

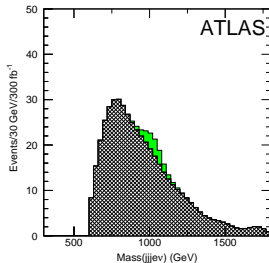
- ▶ Large cross section:  $u$  or  $d$  PDF
- ▶ Huge final state  $\ell$  charge asymmetry
- ▶ Good mass reconstruction



$T \rightarrow th \rightarrow l\nu bbb$ 

SN-ATLAS-2004-038

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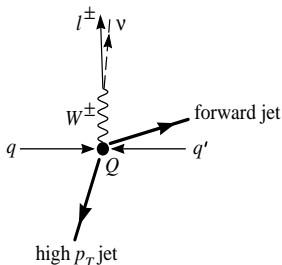


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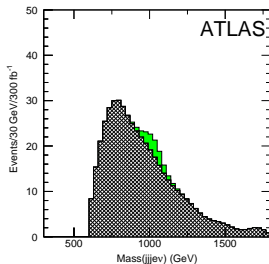
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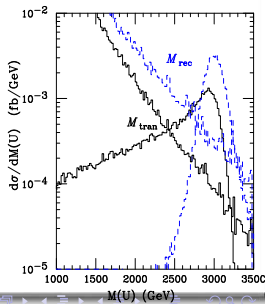
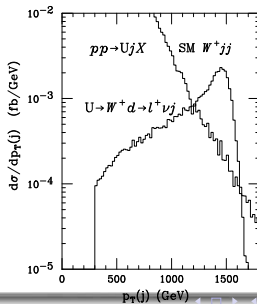


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# Direct Searches – Heavy Vectors

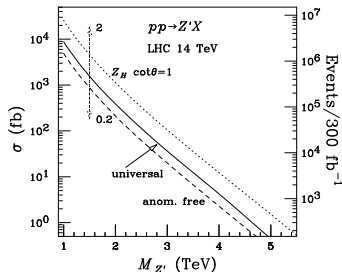
**Drell-Yan Production:** Tevatron Limits  $\sim 500 - 600$  GeV

► **Dominant decays:**

Product group:  $Z' \rightarrow Zh, WW,$

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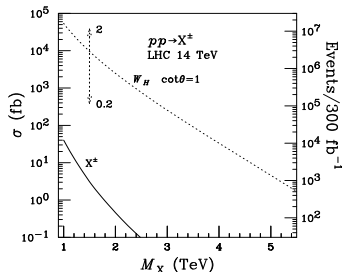
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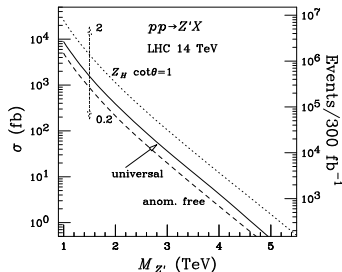




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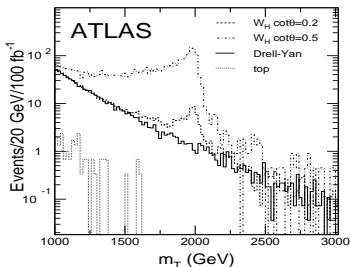
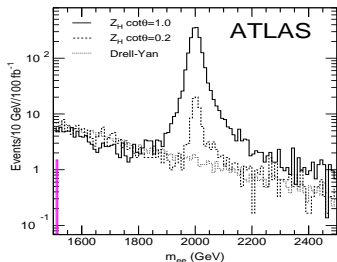
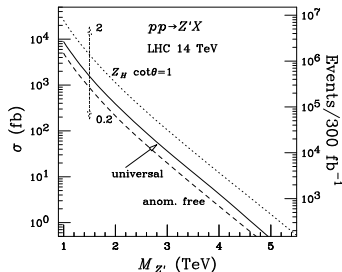
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- ▶  $\Gamma_{Z'} \sim 10 - 50$  GeV,  $\Gamma_X \sim 0.1 - 10$  GeV



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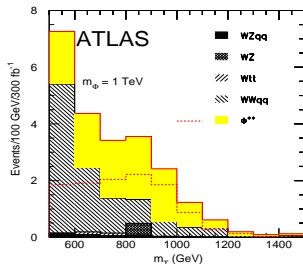


# Direct Searches – Heavy Scalars

Generally: **Large model dependence**

no states    complex singlet    **complex triplet**

- ▶ **Littlest Higgs**, complex triplet:  
 $\Phi^0, \Phi_P, \Phi^\pm, \Phi^{\pm\pm}$
- ▶ Cleanest channel:  $q\bar{q} \rightarrow \Phi^{++}\Phi^{--} \rightarrow llll$ :  
Killer: PS
- ▶  $WW$ -Fusion:  $dd \rightarrow uu\Phi^{++} \rightarrow uuW^+W^+$
- ▶ 2 hard forward jets, hard close  $l^+l^+$   
 $p_T$ -unbalanced



**Alternative: Model-Independent search** in  $WW$  fusion:

ILC: Beyer/Kilian/Krstonosic/Mönig/JRR/Schmidt/Schröder, 2006

LHC: Alboteanu/Kilian/JRR, 2008; Kilian/JRR/Sekulla, 2013

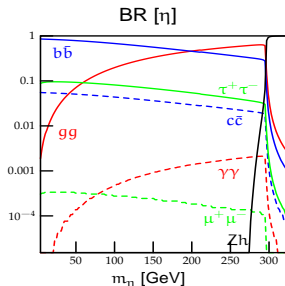
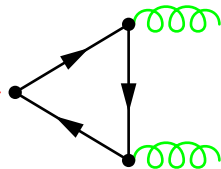
# Pseudo-Axions in Little Higgs

Kilian/Rainwater/JRR, 2004, 2006; JRR,

2007

- gauged  $U(1)$  group:  $Z'$   $\longleftrightarrow$  ungauged:  $\eta$
- couples to fermions like a pseudoscalar
- $m_\eta \lesssim 400$  GeV
- SM singlet, couplings to SM particles  $v/F$  suppressed
- $\eta$  axion-like particle:

Anomalous  $U(1)$ :  $---$



$$\longrightarrow \frac{1}{F} \frac{\alpha_s}{8\pi^2} \eta F_{\mu\nu} F_{\rho\sigma} \epsilon^{\mu\nu\rho\sigma}$$

- $U(1)$  explicitly broken  $\Rightarrow$  Axion limits from astroparticle physics not applicable

# Classification of Axions in Little Higgs Models

Number of Pseudo-Axions:  $n = g - l$

Mismatch between global ( $g$ ) and local rank reduction ( $l$ )

## Product Group Models

Arkani-Hamed, ...

- ▶ Doubling of electroweak gauge group:  $SU(2) \times SU(2) \rightarrow SU(2)_L$ ,  
 $U(1) \times U(1) \rightarrow U(1)_Y$  (latter not necessary)  $\Rightarrow l = 1$ 
  - ▶ Littlest Higgs,  $g: SU(5) \rightarrow SO(5) \Rightarrow n = (4 - 2) - 1 = 1$
  - ▶ antisymmetric,  $g: Sp(6)/SO(6)$ ,  $n = (3 - 2) - 1 = 0$

## Simple Group Models

Kaplan, Schmaltz, ...

- ▶ Simple gauge group:  $SU(N) \times U(1) \rightarrow SU(2) \times U(1) \Rightarrow l = N - 2$
- ▶ Higgs is distributed over several global symmetry multiplets
- ▶ Simplest Little Higgs,  $g: [SU(3)]^2/[SU(2)]^2$   $n = g - l = 2 - 1 = 1$
- ▶ Original Simple Group Model,  $g: [SU(4)]^3/[SU(3)^3 \times SU(2)]$ ,  
 $l: SU(4) \rightarrow SU(2)$   $n = g - l = 4 - 2 = 2$

## Moose Models

Arkani-Hamed, ...

- ▶ "Minimal" Moose:  $g [SU(3)]^4 \rightarrow SU(3)$ ,  $l [SU(3) \times SU(2)]/SU(2)$   
 $n = g - l = 6 - 2 = 4$
- ▶ 3-site model:  $g [SU(2)]^4/[SU(2)]^2$ ,  $l [SU(2)]^2 \rightarrow SU(2)$ ,  $n = 2 - 1 = 1$

# ZH $\eta$ coupling as a discriminator

Kilian/Rainwater/JRR, 2006

- ▶ pseudo-axion:  $\xi = \exp[i\eta/F]$ ,  $\Sigma = \exp[i\Pi/F]$  non-linear representation of the remaining Goldstone multiplet  $\Pi$

$$\mathcal{L}_{\text{kin.}} \sim F^2 \text{Tr} [(D^\mu(\xi\Sigma)^\dagger)(D_\mu(\xi\Sigma))] = \dots - 2F(\partial_\mu\eta) \text{Im Tr} [(D^\mu\Sigma)^\dagger\Sigma] + O(\eta^2)$$

- ▶ Use special structure of covariant derivatives:

$$D_\mu\Sigma = \partial_\mu\Sigma + A_{1,\mu}^a (T_1^a\Sigma + \Sigma(T_1^a)^T) + A_{2,\mu}^a (T_2^a\Sigma + \Sigma(T_2^a)^T),$$

$$\text{Tr} [(D^\mu\Sigma)^\dagger\Sigma] \sim W_\mu^a \text{Tr} [\Sigma^\dagger(T_1^a + T_2^a)\Sigma + (T_1^a + T_2^a)^*] = 0.$$

- ▶ Little Higgs mechanism cancels this coupling
- ▶ Simple Group Models:  $\Phi = \exp[i\Sigma/F]$ ,  $\zeta = (0, \dots, 0, F)^T$  VEV directing in the  $N$  direction

$$\begin{aligned}\mathcal{L}_{\text{kin.}} &\sim F^2 D^\mu (\zeta^\dagger \Phi^\dagger) D_\mu (\Phi \zeta) = \dots + \frac{i}{F} (\partial_\mu \eta) \zeta^\dagger (\Phi^\dagger (D_\mu \Phi) - (D_\mu \Phi^\dagger) \Phi) \zeta \\ &= \dots + iF (\partial_\mu \eta) (\Phi^\dagger (D_\mu \Phi) - (D_\mu \Phi^\dagger) \Phi)_{N,N} .\end{aligned}$$

$$\Sigma = \begin{pmatrix} 0 & h \\ h^\dagger & 0 \end{pmatrix}, \quad \mathbb{V}_\mu = \begin{pmatrix} \mathbb{W}_\mu & 0 \\ 0 & 0 \end{pmatrix} + \text{heavy vector fields}$$

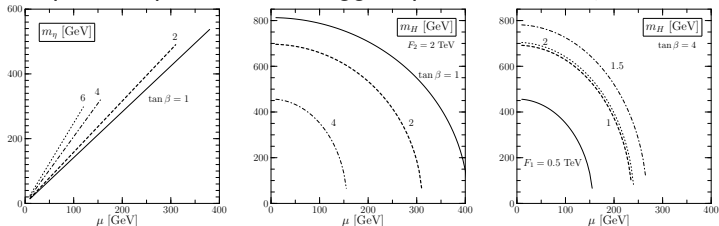
$$\begin{aligned}&\mathbb{V}_\mu + \frac{i}{F} [\Sigma, \mathbb{V}_\mu] - \frac{1}{2F^2} [\Sigma, [\Sigma, \mathbb{V}_\mu]] + \dots \\ &= \begin{pmatrix} \mathbb{W}_\mu & 0 \\ 0 & 0 \end{pmatrix} + \frac{i}{F} \begin{pmatrix} 0 & -\mathbb{W}_\mu h \\ h^\dagger \mathbb{W}_\mu & 0 \end{pmatrix} - \frac{1}{2F^2} \begin{pmatrix} hh^\dagger \mathbb{W} + \mathbb{W} h h^\dagger & 0 \\ 0 & -2h^\dagger \mathbb{W} h \end{pmatrix} + \dots\end{aligned}$$

- ▶ 1st term cancels by multiple Goldstone multiplets
- ▶ 2nd term cancels by EW symmetry
- ▶ 3rd term

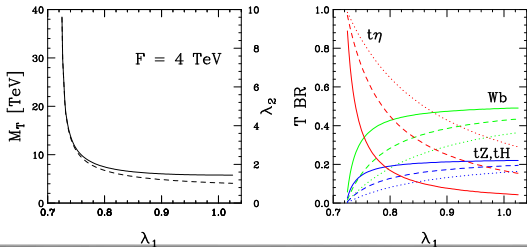
$$(\partial^\mu \eta) h^\dagger \mathbb{W}_\mu h \sim v H Z_\mu \partial^\mu \eta .$$

# More properties of Pseudo-Axions

- ▶ Take e.g. one specific model: Simplest Little Higgs Schmaltz, 2004
- ▶ Simple Group Model, two Higgs-triplets with a  $\tan \beta$ -like mixing angle



- ▶  $\tan \beta \sim 1$ : heavy Higgs, (very) light pseudoscalar
- ▶ Heavy top decays: Kilian/Rainwater/JRR, 2006





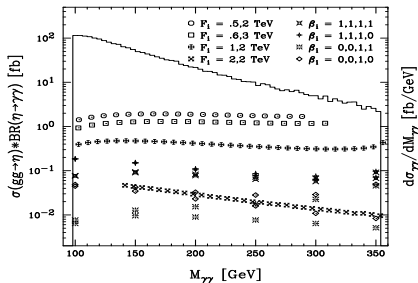
# Discovery of Pseudo-axions

Kilian/Rainwater/JRR, 2004, 2006

LHC: Gluon fusion, diphoton  
signal for  $m_\eta \gtrsim 200$  GeV,  $7\sigma$   
possible

LHC:  $T \rightarrow t\eta$

ILC:  $e^+e^- \rightarrow t\bar{t}\eta$



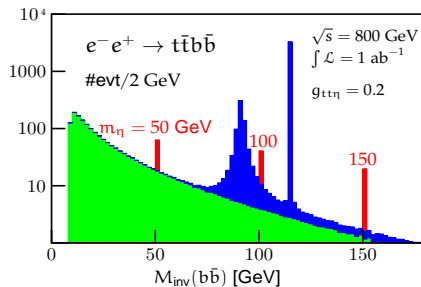
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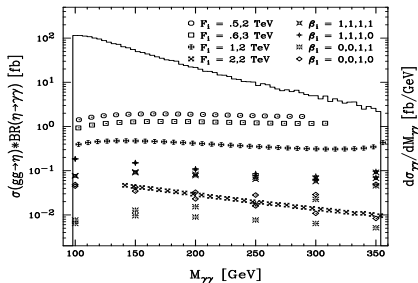
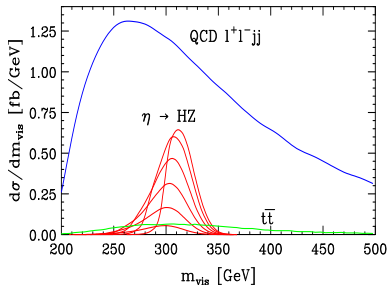
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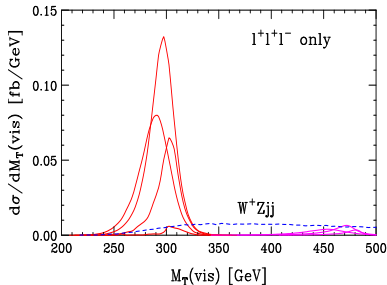
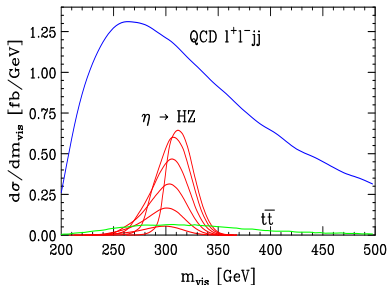
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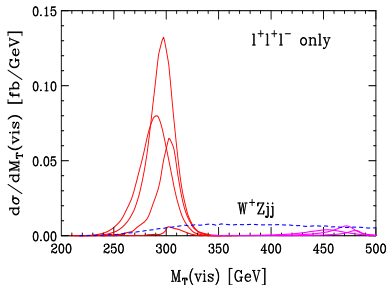
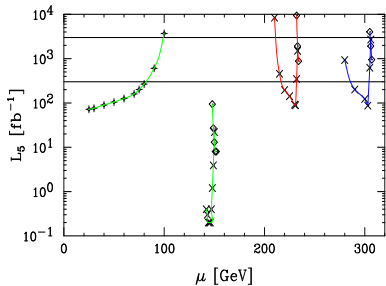
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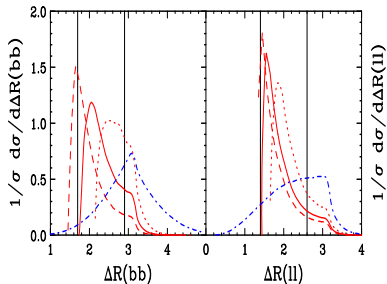
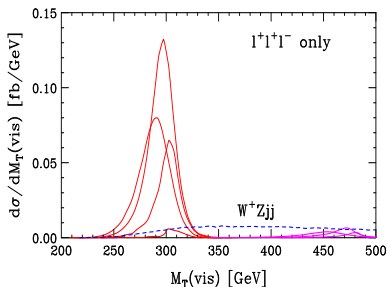
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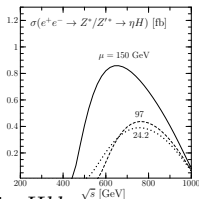
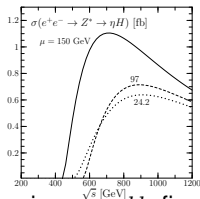
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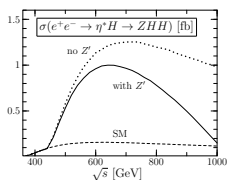
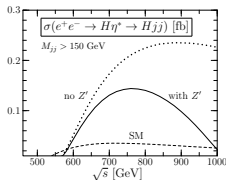
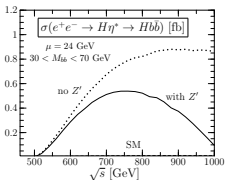
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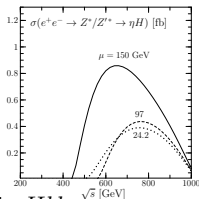
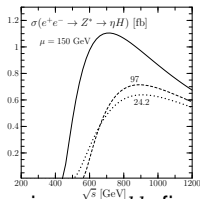


More detailed insights from photon collider option

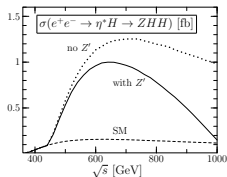
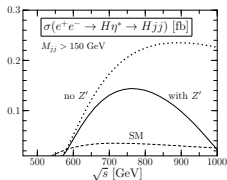
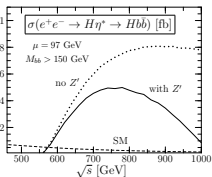
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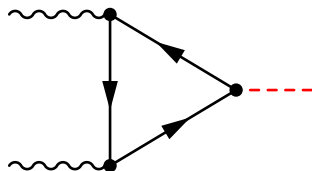


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# Pseudo Axions at the Photon Collider

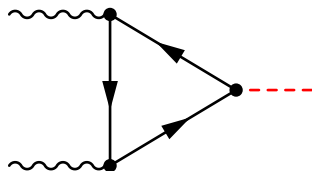
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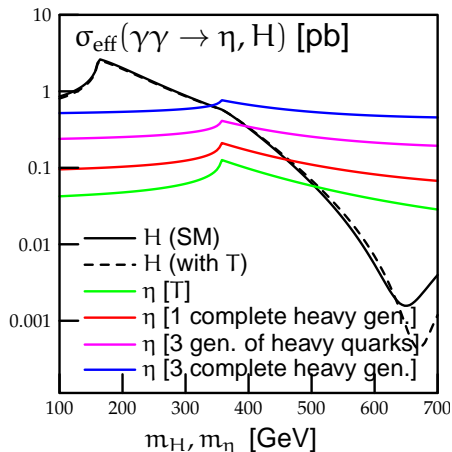
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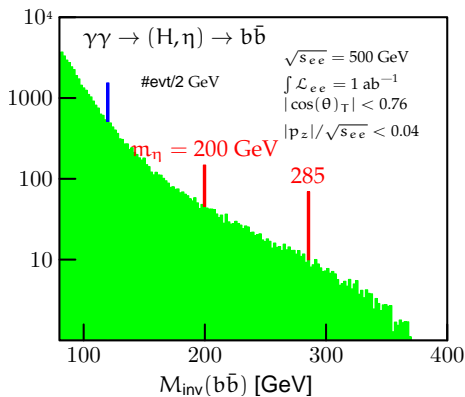
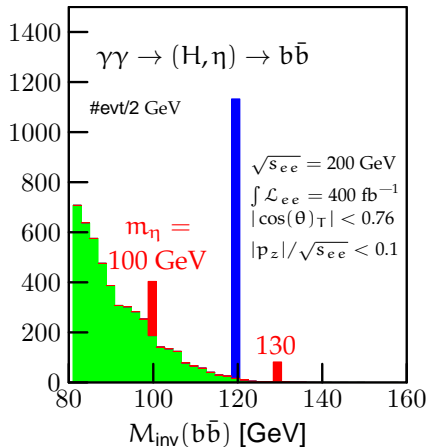


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$$g_{bb\eta} = 0.4 \cdot g_{bbh}$$

| $m_\eta$                      | 100  | 130  | 200 | 285 |
|-------------------------------|------|------|-----|-----|
| $\Gamma_{\gamma\gamma}$ [keV] | 0.15 | 0.27 | 1.1 | 3.6 |



# Simplest Little Higgs (“ $\mu$ Model”)

Schmaltz '04, Kilian/Rainwater/JRR '04

Field content ( $SU(3)_c \times SU(3)_w \times U(1)_X$  quantum numbers)

$$\begin{array}{lll}
 \Phi_{1,2} & : (1, 3)_{-\frac{1}{3}} & \Psi_\ell & : (1, 3)_{-\frac{1}{3}} & u_{1,2}^c & : (\bar{3}, 1)_{-\frac{2}{3}} \\
 \Psi_Q & : (3, 3)_{\frac{1}{3}} & d^c & : (\bar{3}, 1)_{\frac{1}{3}} & e^c, n^c & : (1, 1)_{1,0}
 \end{array}$$

Lagrangian  $\mathcal{L} = \mathcal{L}_{\text{kin.}} + \mathcal{L}_{\text{Yuk.}} + \mathcal{L}_{\text{pot.}}$        $\Psi_{Q,L} = (u, d, U)_L, \Psi_\ell = (\nu, \ell, N)_L$ :

$$\begin{aligned}
 \mathcal{L}_{\text{Yuk.}} = & -\lambda_1^u \bar{u}_{1,R} \Phi_1^\dagger \Psi_{T,L} - \lambda_2^u \bar{u}_{2,R} \Phi_2^\dagger \Psi_{T,L} - \frac{\lambda^d}{\Lambda} \epsilon^{ijk} \bar{d}_R^b \Phi_1^i \Phi_2^j \Psi_{T,L}^k \\
 & - \lambda^n \bar{n}_{1,R} \Phi_1^\dagger \Psi_{Q,L} - \frac{\lambda^e}{\Lambda} \epsilon^{ijk} \bar{e}_R \Phi_1^i \Phi_2^j \Psi_{Q,L}^k + \text{h.c.},
 \end{aligned}$$

$$\mathcal{L}_{\text{pot.}} = \mu^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}$$

Hypercharge embedding      ( $\text{diag}(1, 1, -2)/(2\sqrt{3})$ ):

$$Y = X - T^8/\sqrt{3} \qquad D_\mu \Phi = (\partial_\mu - \frac{1}{3} g_X B_\mu^X \Phi + ig W_\mu^w) \Phi$$