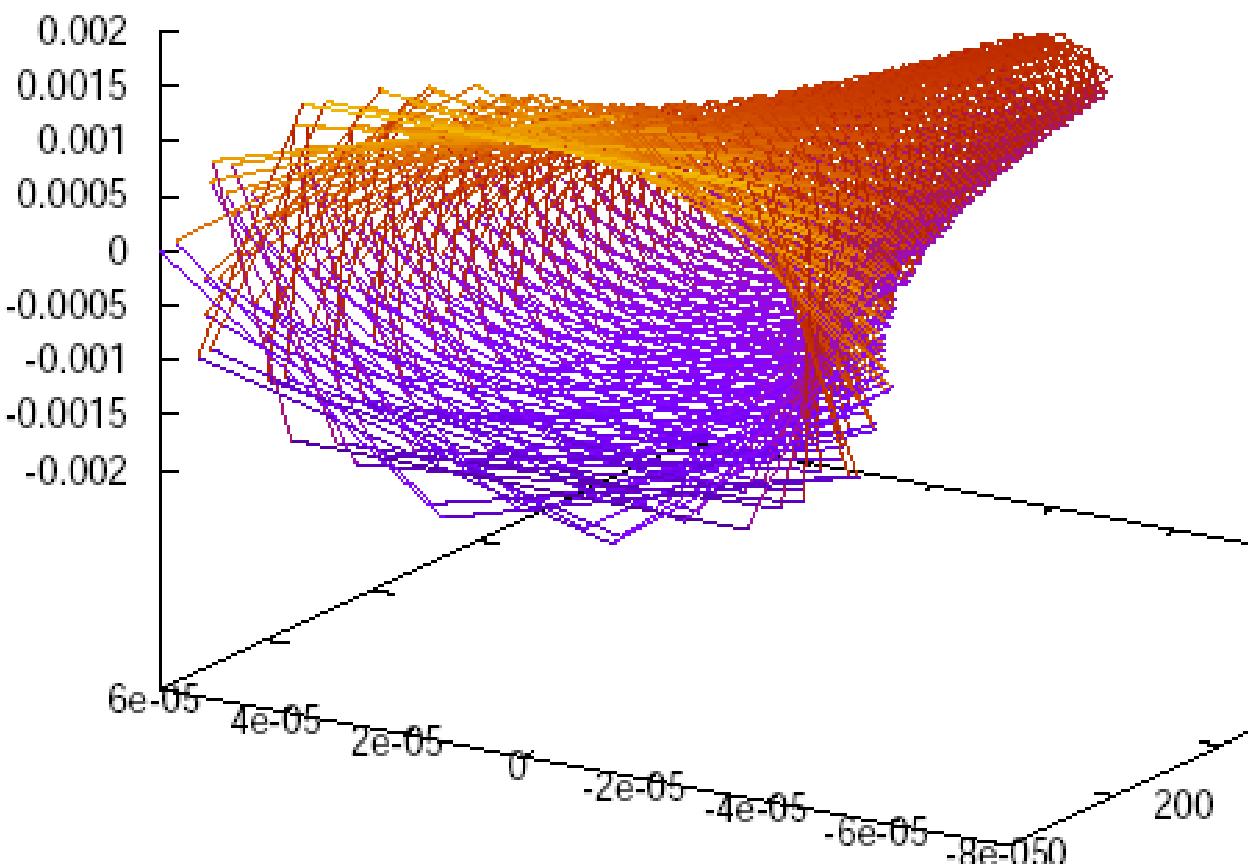


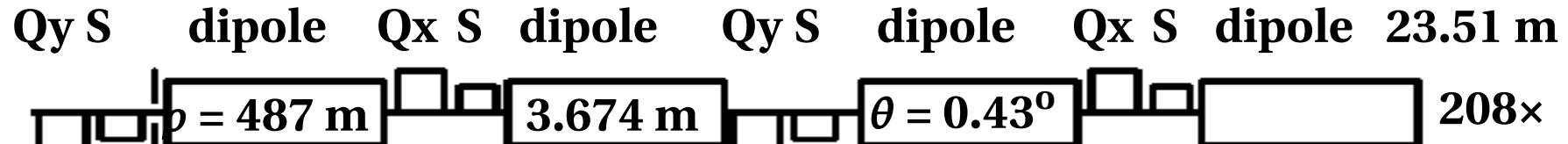
# Multi-turn tracking studies for HERA-e

Botho Paschen, Uni HD  
Z-study meeting 13.10.2010



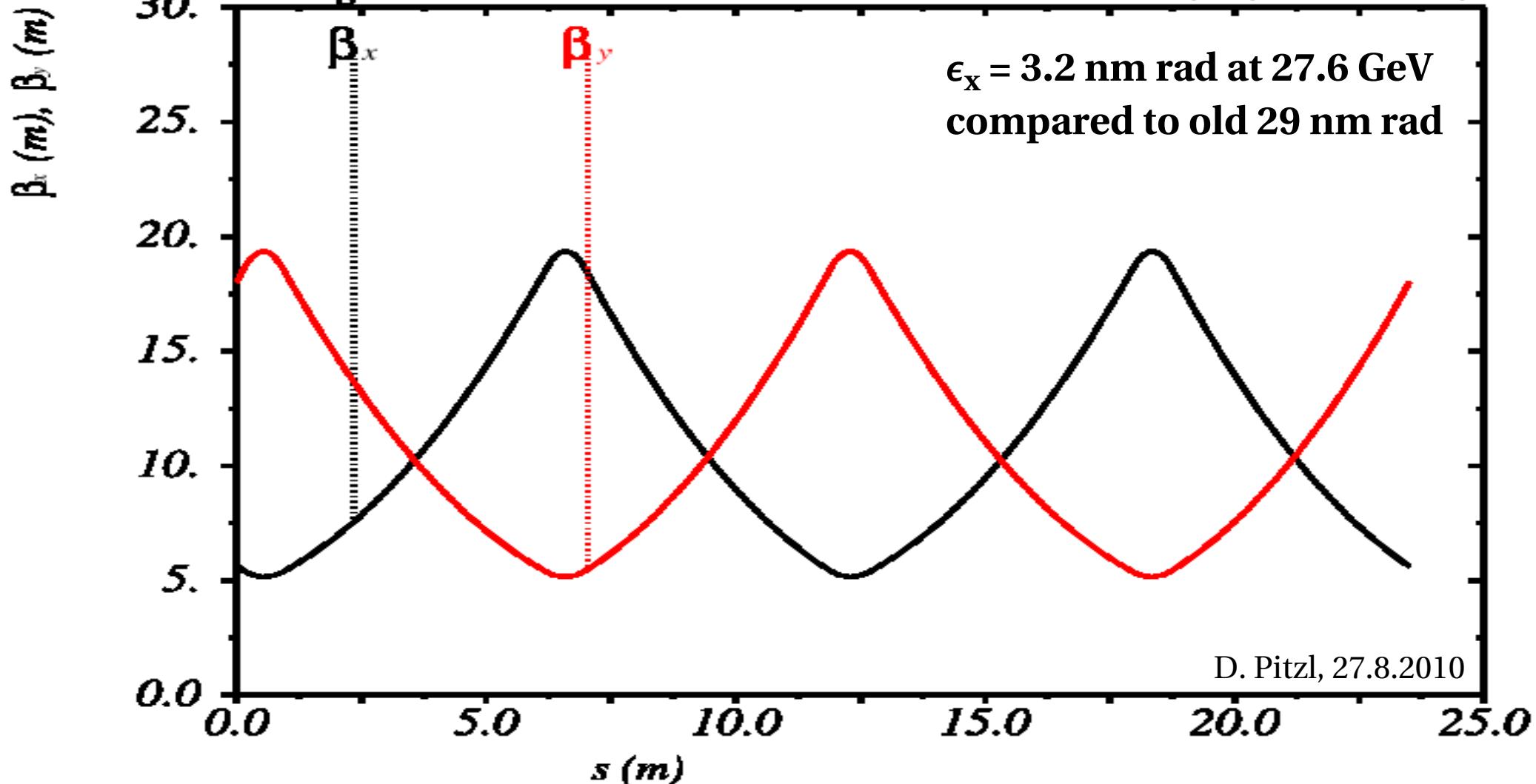
- new HERA-e
- working point
- multi-turn tracking
- dynamic aperture

# new HERA-e arc cell



72 deg arc cell 4

MAD-X 4.01.28 30/08/10 14.42.59

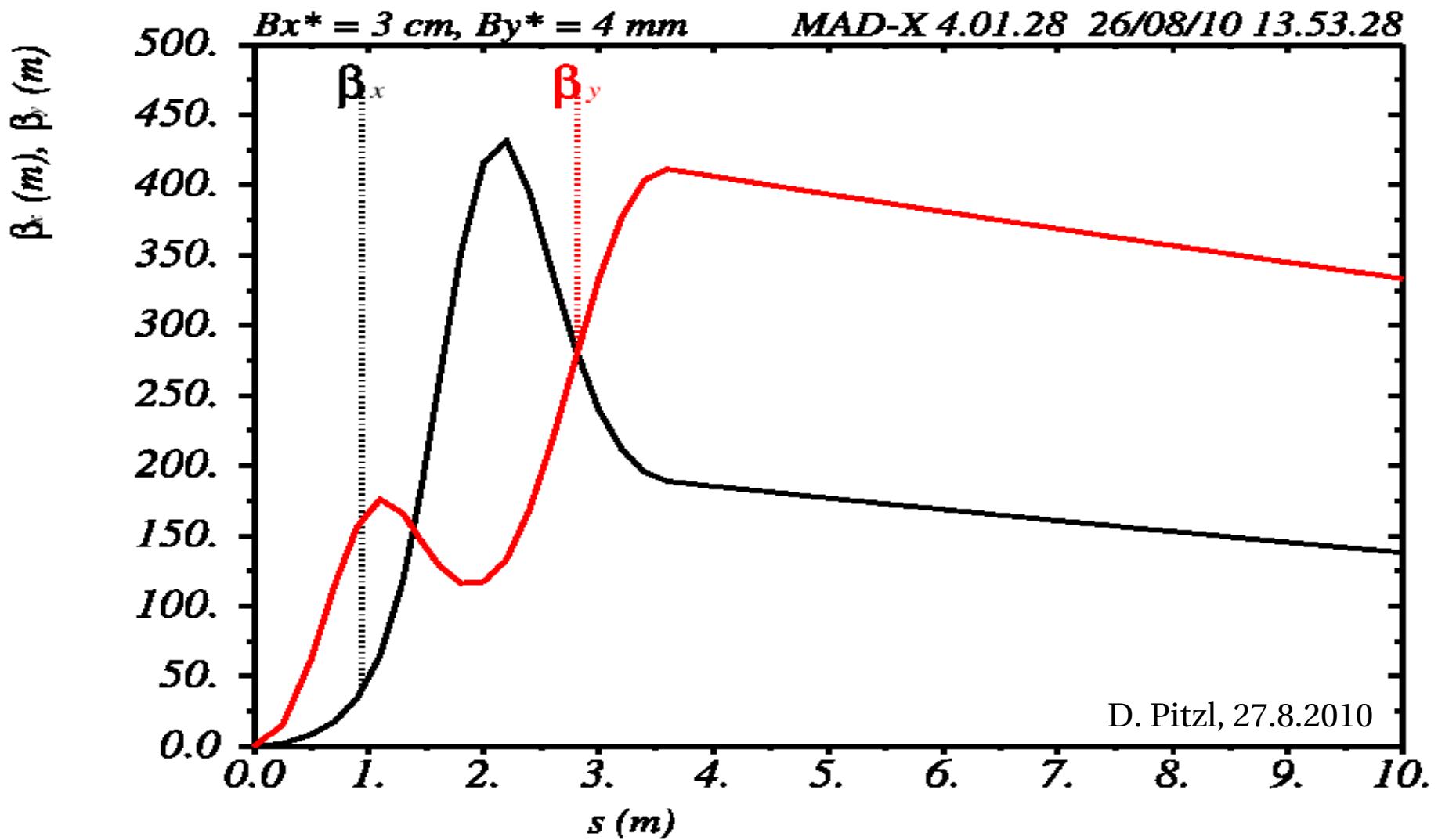


# Interaction region

strong focusing super conducting quadrupole triplet

$\beta_x^* = 3 \text{ cm}$

$\beta_y^* = 4 \text{ mm}$

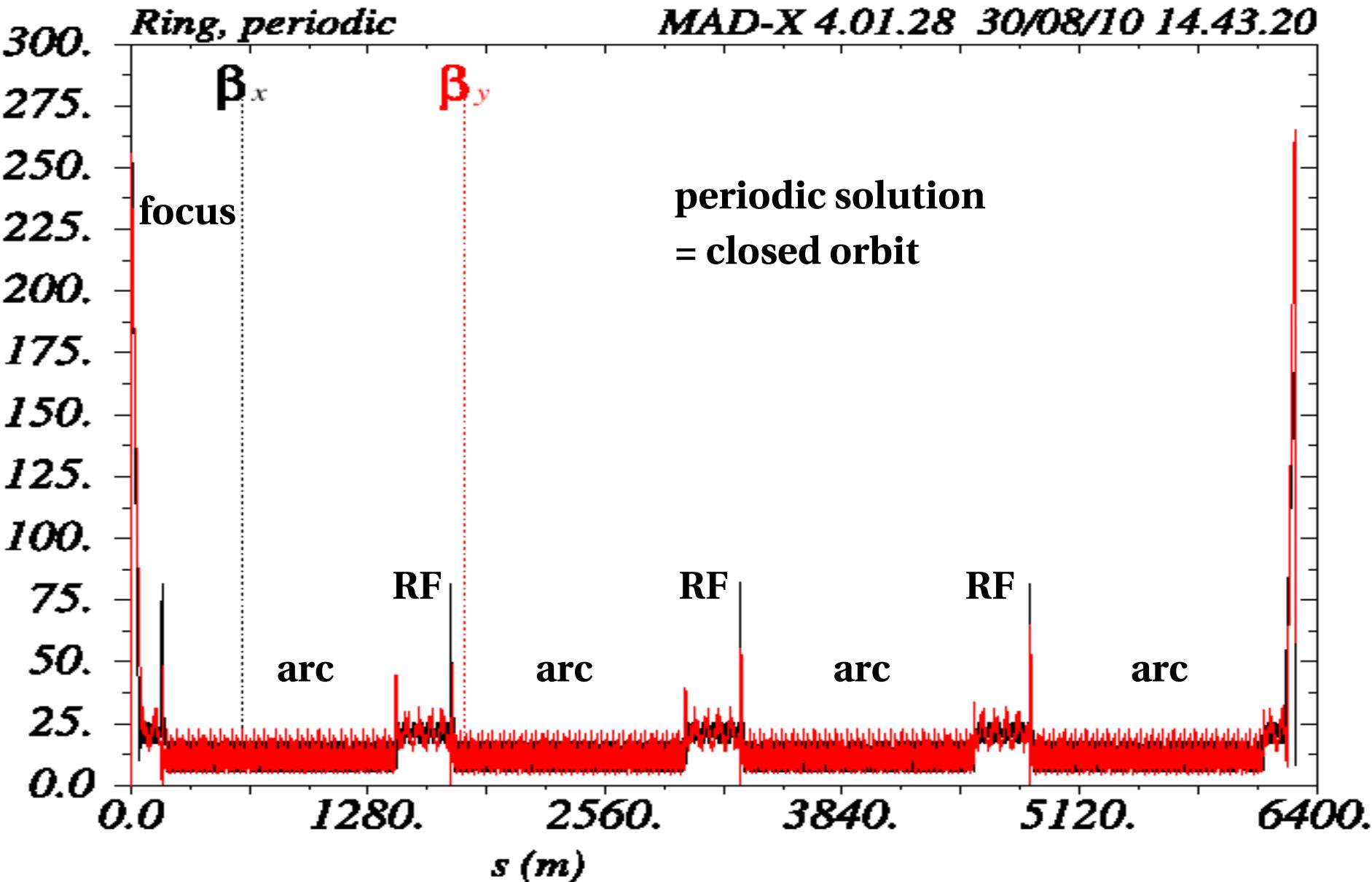


# entire ring

from MAD-X:

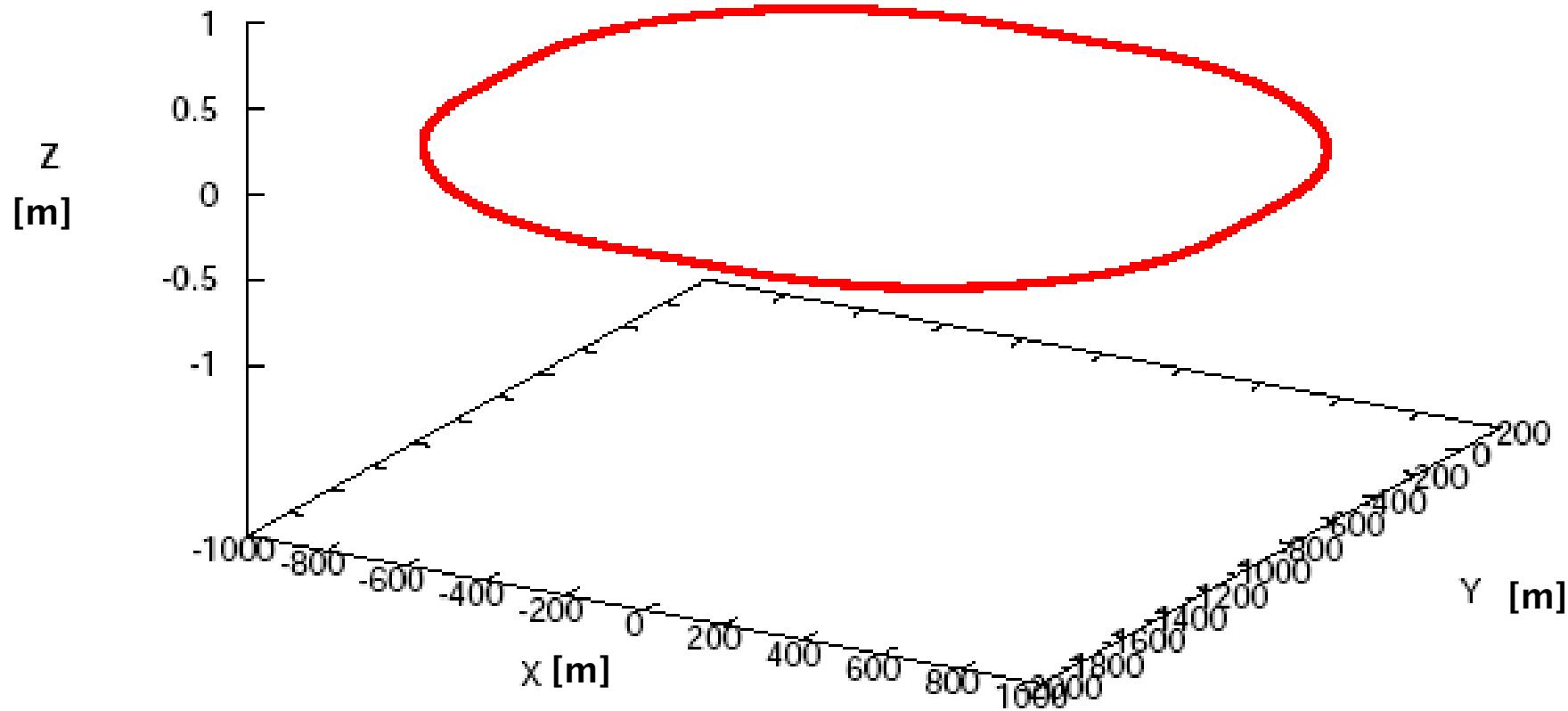
$$\beta_x^* = 3.0 \text{ cm}$$

$$\beta_y^* = 4.6 \text{ mm}$$



# entire ring

MAD-X survey:



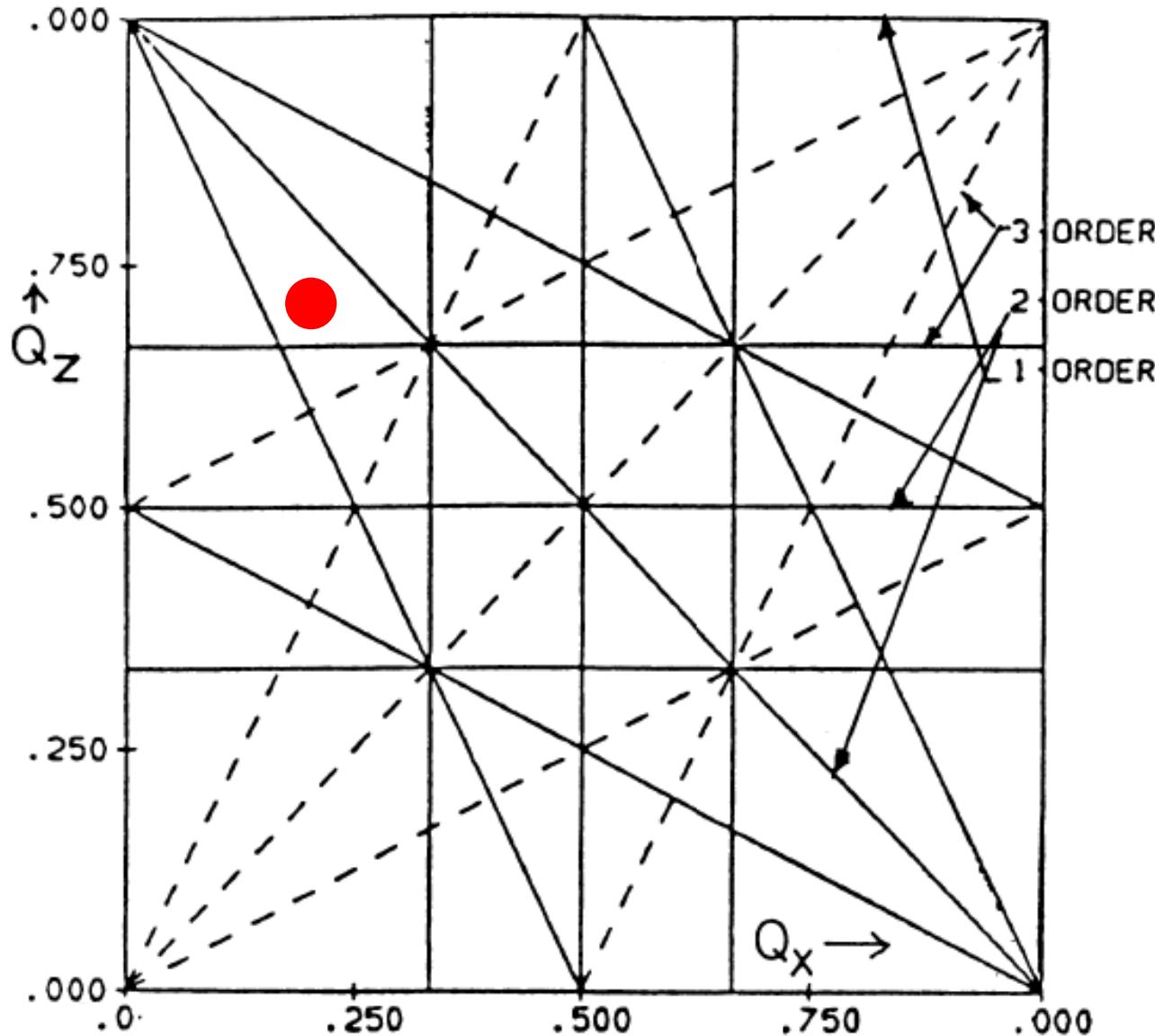
# Open questions

- What is the dynamic aperture of the new e ring?
  - ▶ Beta function describes the 1 sigma envelope for nominal energy particles in linear approximation.
  - ▶ Strong sextupoles introduce  $x-y$  coupling and non-linear fields.
  - ▶ Beam has spread in position, angles, and energy.
  - ▶ Need to track individual particles with varying starting values for many turns to study non-linear effects.
- Goal:
  - ▶ Find parameter space for stable orbits.
  - ▶ Decide on viability of the new optics.
- Use old HERA-e as reference.

# MAD-X

- Code for Methodical Accelerator Design MAD developed at CERN:  
<http://mad.web.cern.ch/mad/>
- Use PTC thick lens tracking:
  - ▶ PTC = polymorphic tracking code by Etienne Forest.
  - ▶ ICASE = 6 = dimensions ( $x, x', y, y', t, E$ )
  - ▶ Model = 2 = Matrix-kick-matrix
  - ▶ Method = 2 = integration order
  - ▶ NST = 1 = integration steps
  - ▶ Radiation on: damping by synchrotron emission and RF cavity
  - ▶ turns = 1000

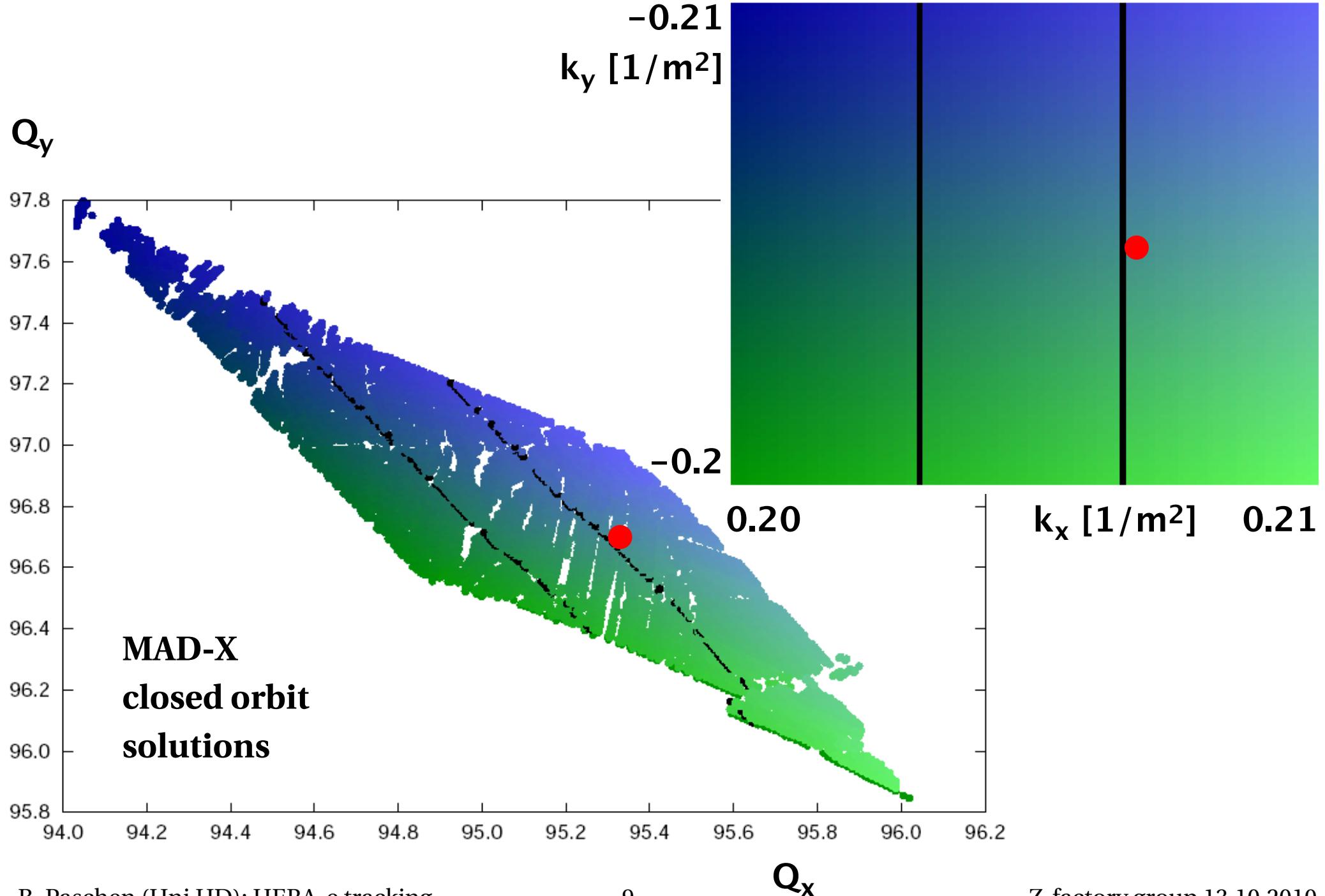
# Working point in tune diagram



$$Q = \frac{1}{2\pi} \oint \frac{1}{\beta(s)} ds$$

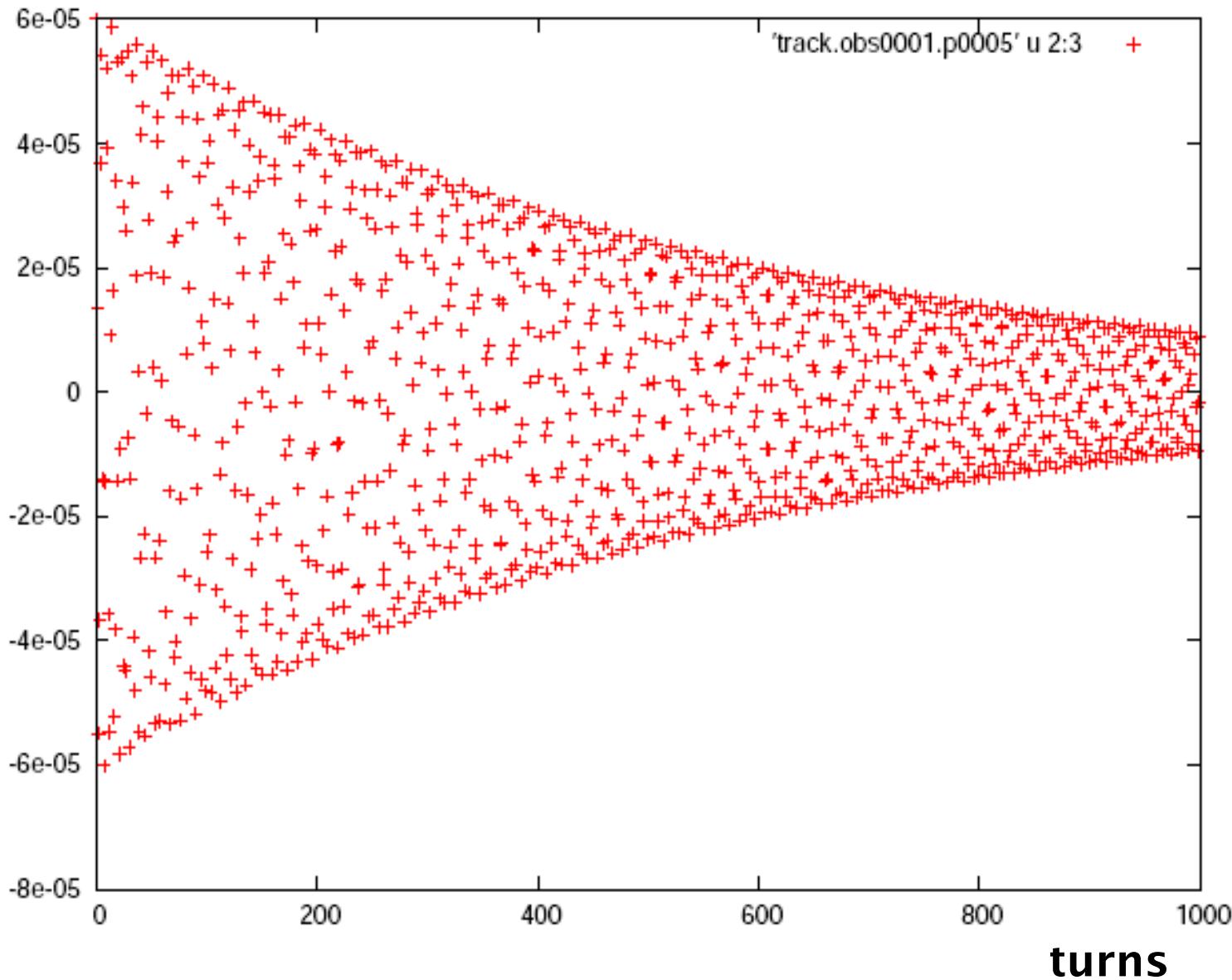
- must avoid betatron resonances for the periodic closed orbit solution.
- Use quadrupoles in the straight sections to adjust fractional part of  $Q$ .

# From quad strength to tune



# multi-turn damping of betatron oscillations

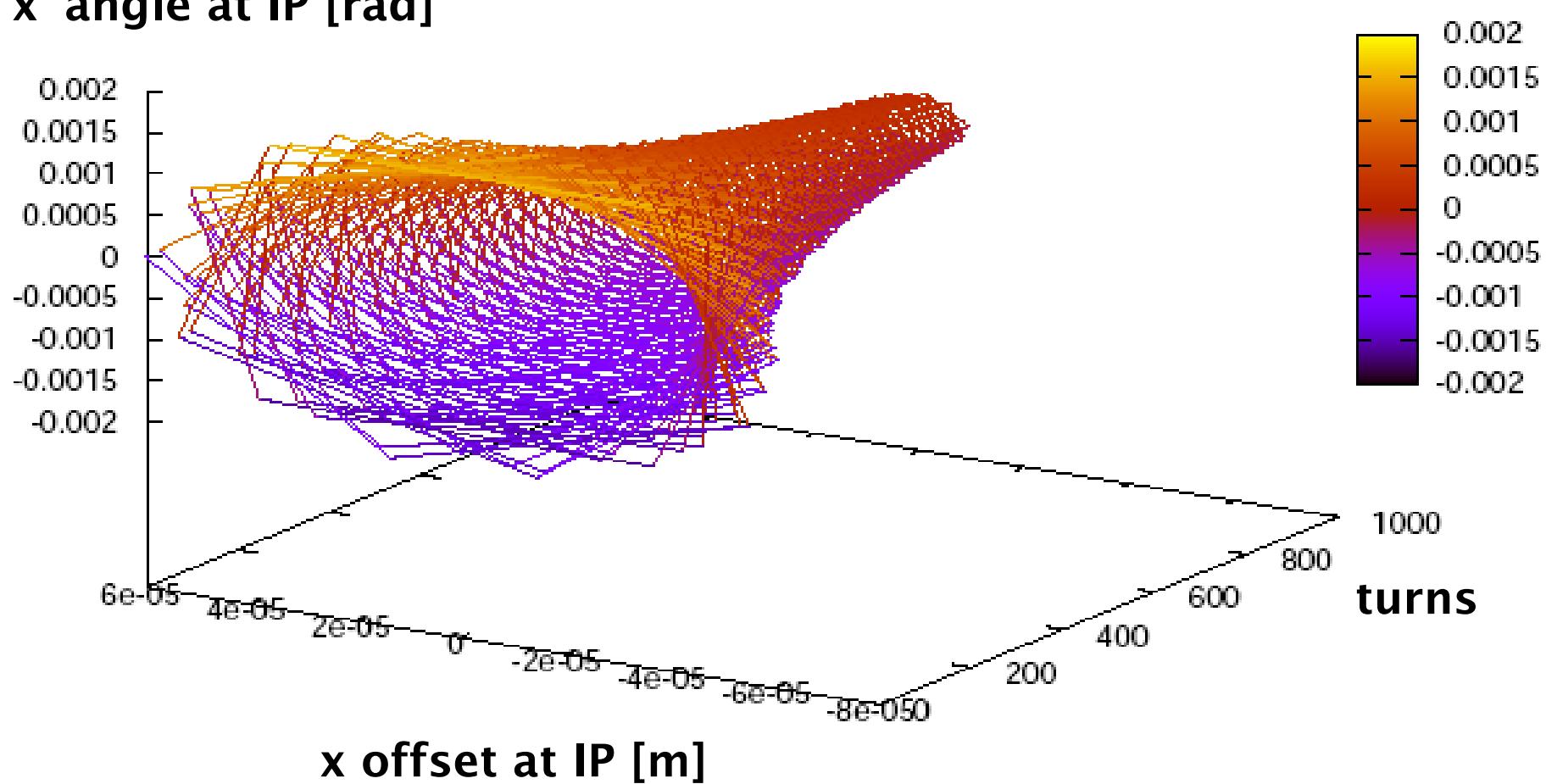
x offset at IP [m]



- Damping time constant from MAD-X:
  - ▶  $\tau_x = 11 \text{ ms} = 520 \text{ turns.}$

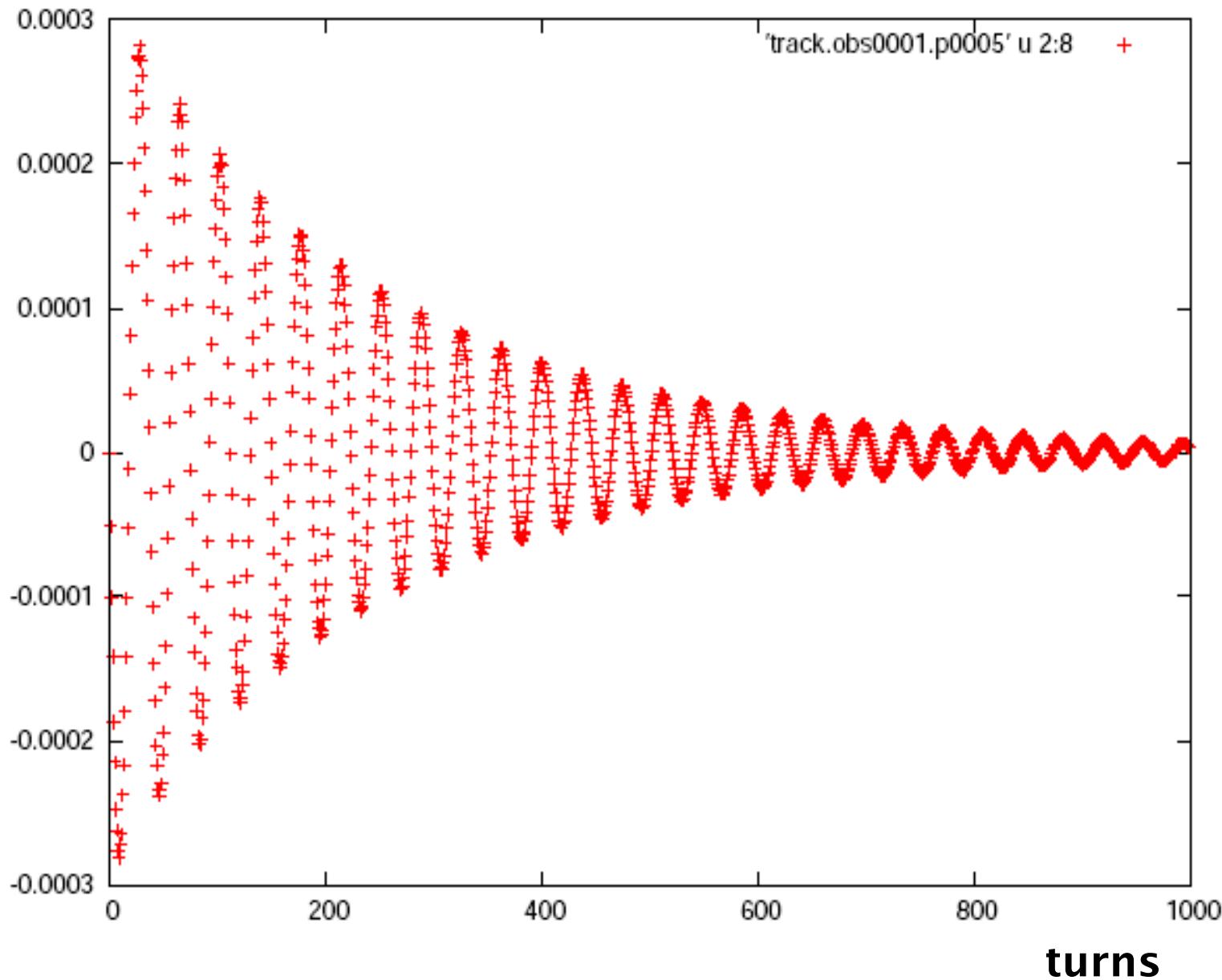
# multi-turn damping of betatron oscillations

x' angle at IP [rad]



# multi-turn damping of synchrotron oscillations

$\delta E/E$



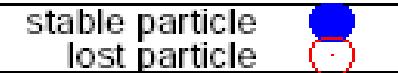
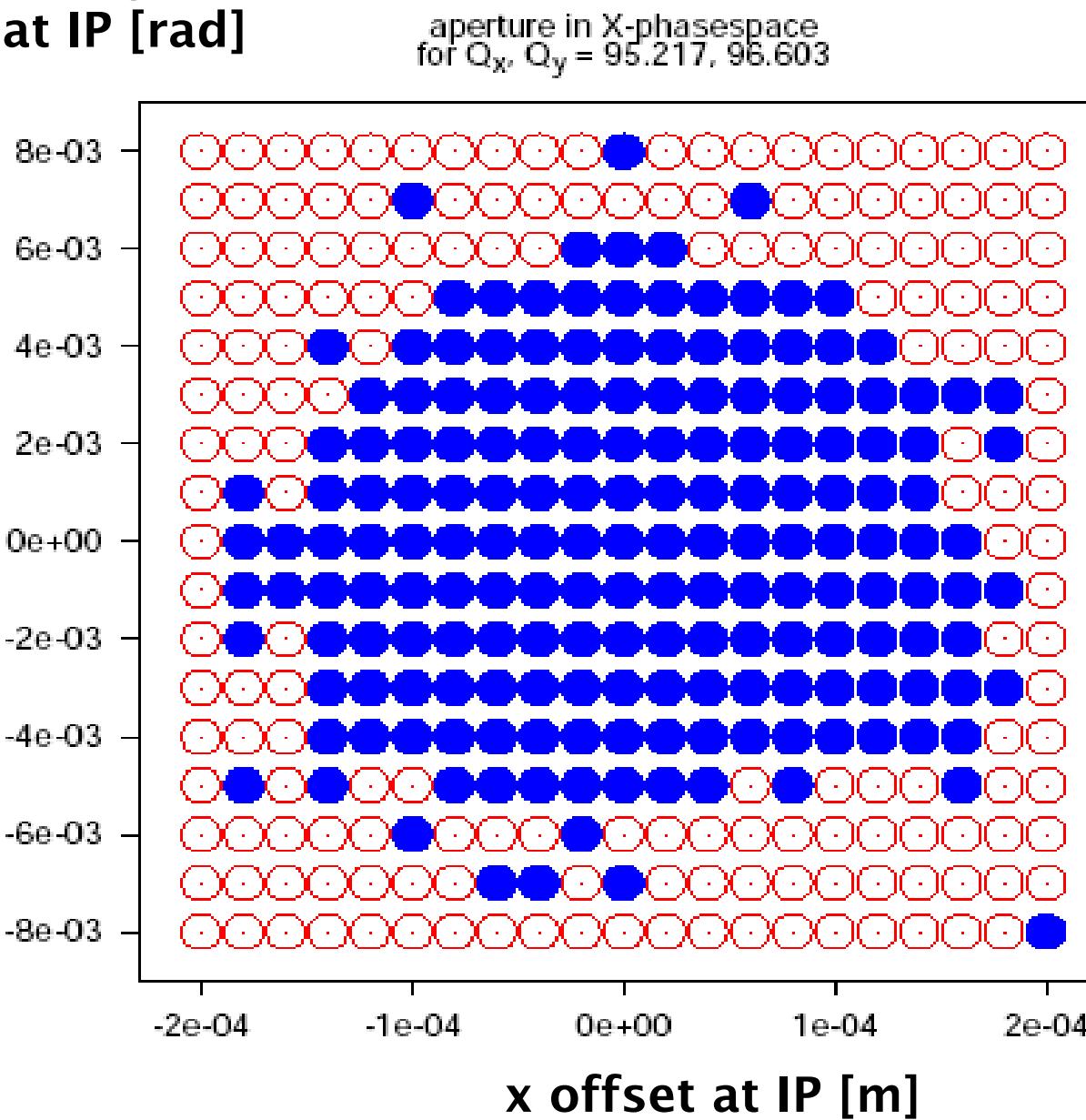
Damping time constant from MAD-X:

- ▶  $\tau_E = 5.5 \text{ ms} = 260 \text{ turns.}$
- ▶ Damping partition 1:1:2 (Robinson theorem).

# dynamic aperture

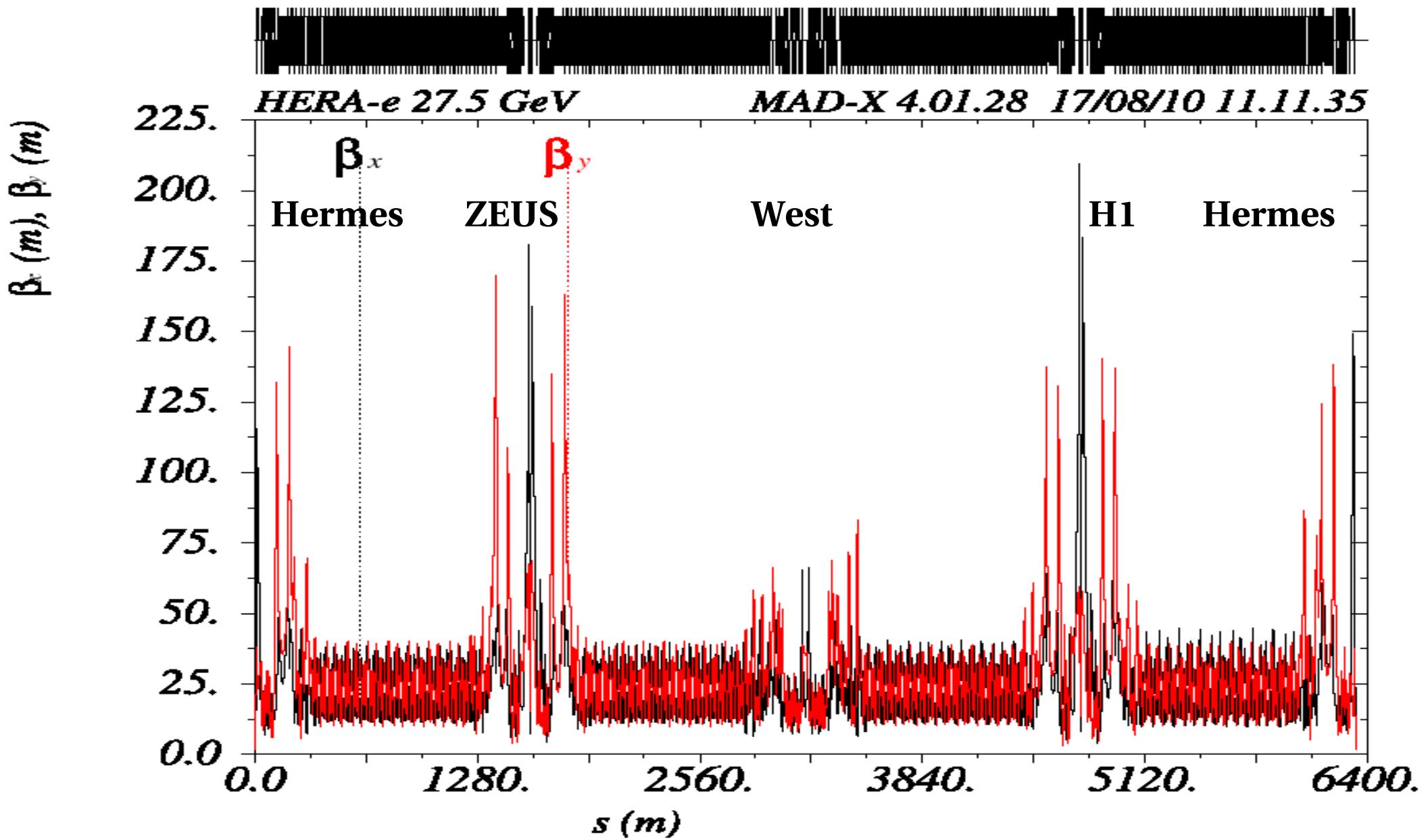
x' angle  
at IP [rad]

72° low emittance lattice



- At IP:
  - ▶  $\sigma_x = \sqrt{\epsilon_x \beta_x^*}$
  - ▶  $= 10 \mu\text{m}$ .
  - ▶  $15 \sigma$  aperture.
- angle:
  - ▶  $\sigma_{x'} = \sqrt{\epsilon_x / \beta_x^*}$
  - ▶  $= 0.33 \text{ mrad}$
  - ▶  $15 \sigma$  aperture.

# Old HERA-e

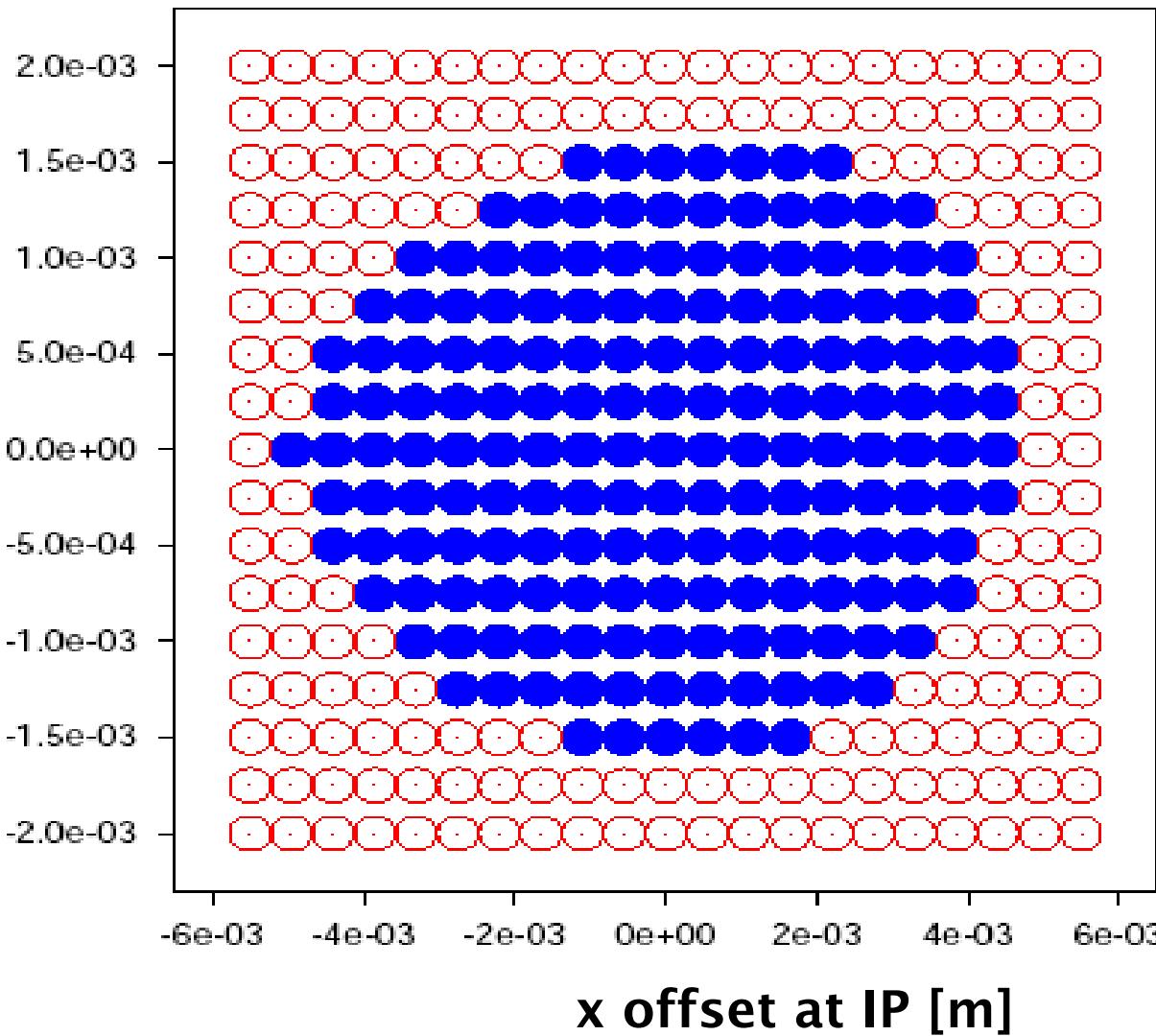


# dynamice aperture for old HERA-e

x' angle  
at IP [rad]

IP East (Hermes)

HERA aperture in X-phasespace



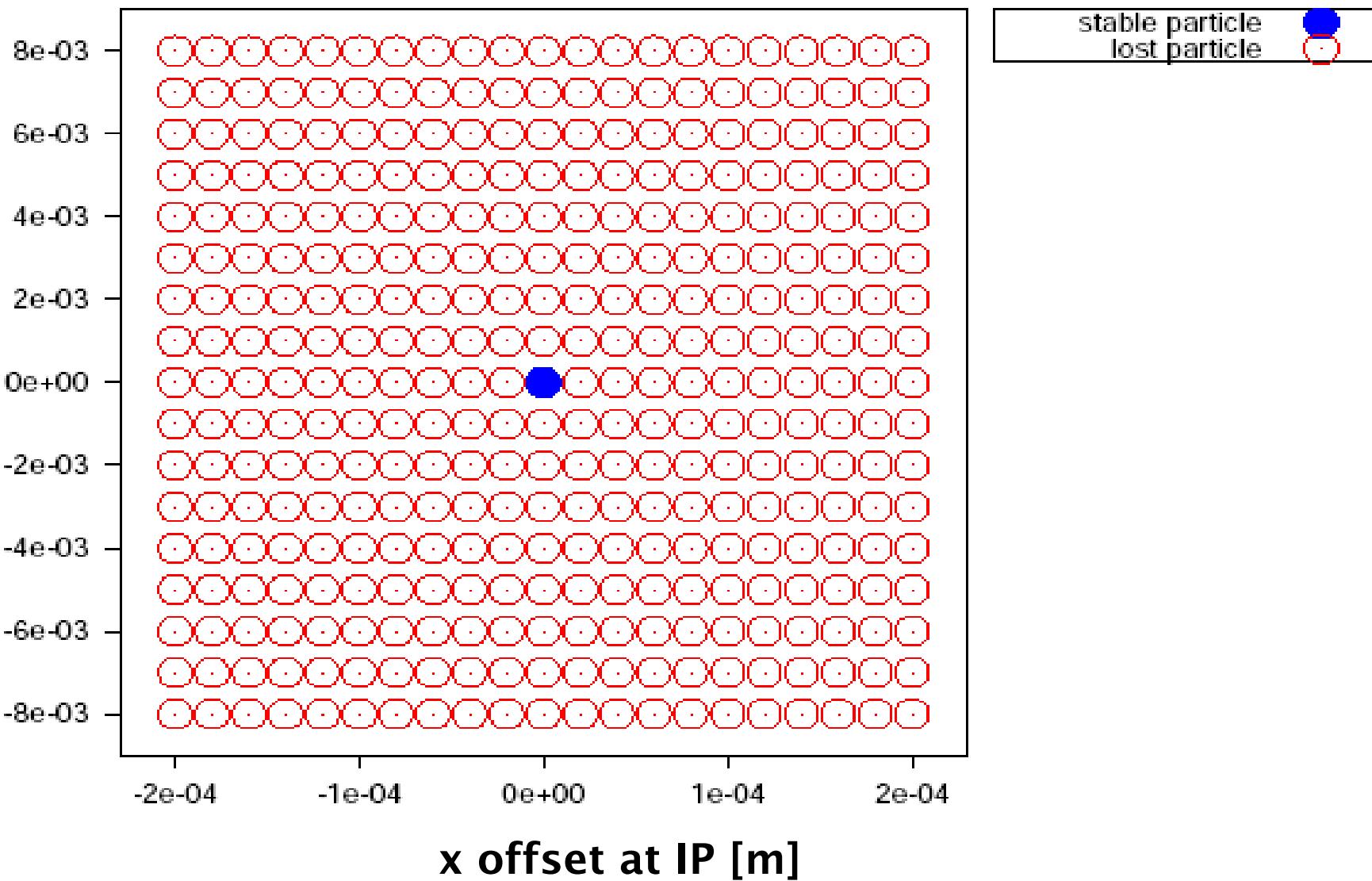
- At IP:
  - ▶  $\sigma_x = \sqrt{\epsilon_x \beta_x^*}$
  - ▶  $= 0.30 \text{ mm.}$
  - ▶  $13 \sigma$  aperture.
- angle:
  - ▶  $\sigma_{x'} = \sqrt{\epsilon_x / \beta_x^*}$
  - ▶  $= 0.10 \text{ mrad}$
  - ▶  $15 \sigma$  aperture.

# dynamic aperture close to resonance

## Tune at integer betatron resonance

x' angle  
at IP [rad]

aperture in X-phasespace  
for  $Q_x, Q_y = 94.996, 96.992$

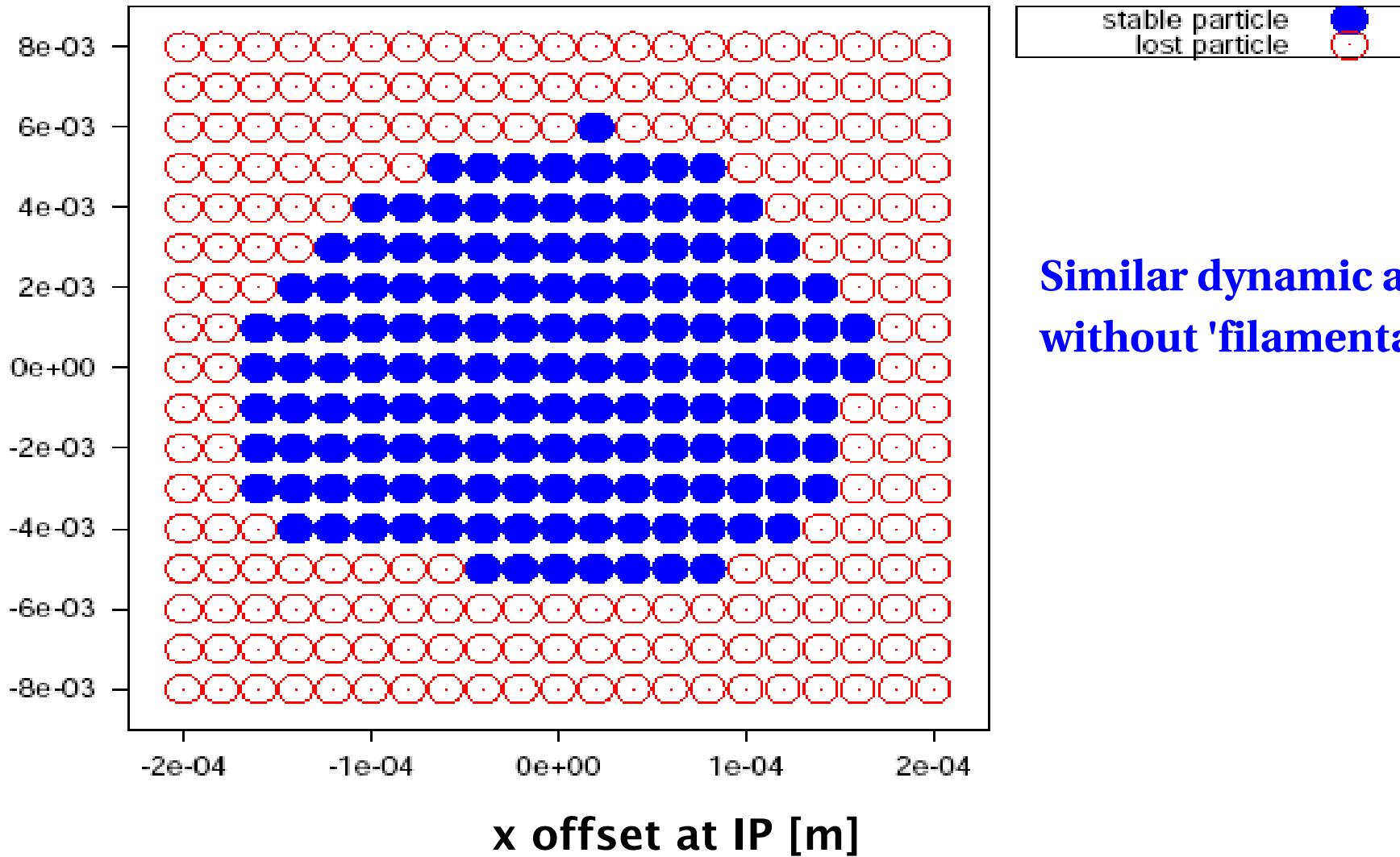


# dynamic aperture

x' angle  
at IP [rad]

72° low emittance lattice  
different working point

aperture in X-phasespace  
for  $Q_x, Q_y = 95.300, 96.697$



Similar dynamic aperture,  
without 'filamentation'.

# old and new HERA-e

	<b>old</b>	<b>new</b>
• MAD-X		
• Dipole bend:	$0.86^\circ$	$0.43^\circ$
• Emittance:		
▶ $\epsilon_x$ [nm rad]	29.8	<b>3.2</b>
• Tune:		
▶ $Q_x$	53.27	95.2
▶ $Q_y$	51.41	98.6
• Dynamic aperture:		
▶ $x$	$13 \sigma$	$15 \sigma$
▶ $x'$	$15 \sigma$	$15 \sigma$
▶ $\delta E/E$	$0.005 = 5 \sigma$	$0.005 = 5 \sigma$

# Summary

- Dynamic aperture of the lower emittance HERA-e lattice studied with tracking in MAD-X:
  - ▶ seems to be similar to old HERA-e, at least in  $x-x'$ .
- Next:
  - ▶ Explore full 6-D parameter space ( $x, x', y, y', t, E$ )
  - ▶ Try 108° optics (factor 2.5 smaller emittance, stronger focussing, larger chromaticity).
- Further:
  - ▶ Study beam-beam interactions.