Measurement of charm fragmentation ratios and fractions in photoproduction at HERA

ZEUS Collaboration

Abstract

The production of D^{*+} , D^0 , D^+ , D^+_s and Λ^+_c charm hadrons and their antiparticles in ep scattering at HERA was measured with the ZEUS detector using an integrated luminosity of $79 \,\mathrm{pb}^{-1}$. The measurement has been performed in the photoproduction regime with the exchanged-photon virtuality $Q^2 < 1 \,\text{GeV}^2$ and for photon-proton centre-of-mass energies in the range 130 < W < 300 GeV. The charm hadrons were reconstructed in the range of transverse momentum $p_T(D, \Lambda_c) > 3.8 \,\text{GeV}$ and pseudorapidity $|\eta(D, \Lambda_c)| < 1.6$. The production cross sections were used to determine the ratio of neutral and charged D-meson production rates, $R_{u/d}$, the strangeness-suppression factor, γ_s , and the fraction of charged D mesons produced in a vector state, $P_{\rm v}^d$. The measured $R_{u/d}$ and γ_s values agree with those obtained in deep inelastic scattering and in e^+e^- annihilations. The measured $P_{\rm v}^d$ value is smaller than, but consistent with, the previous measurements. The fractions of c quarks hadronising as a particular charm hadron, $f(c \to D, \Lambda_c)$, were derived in the given kinematic range. The measured open-charm fragmentation fractions are consistent with previous results, although the measured $f(c \to D^{*+})$ is smaller and $f(c \to \Lambda_c^+)$ is larger than those obtained in e^+e^- annihilations. These results generally support the hypothesis that fragmentation proceeds independently of the hard sub-process.

1 Introduction

Charm quark production has been extensively studied at HERA using $D^{*\pm}$ and D_s^{\pm} mesons [1–5]. The data have been compared with theoretical predictions by assuming the universality of charm fragmentation and using the charm fragmentation characteristics obtained in e^+e^- annihilation for the calculations of charm production in ep scattering. Measuring the charm fragmentation characteristics at HERA tests charm-fragmentation universality.

In this paper, the measurement of the production of the weakly decaying charm ground states, the D^0 , D^+ , D_s^+ pseudo-scalar mesons and the Λ_c^+ baryon, is presented. The production of the charm vector meson D^{*+} has also been studied. The antiparticles of these charm hadrons have been measured as well¹. The measurement has been performed in *ep* scattering at HERA in the photoproduction regime with exchanged-photon virtuality, Q^2 , close to zero and for photon-proton centre-of-mass energies in the range $130 < W < 300 \,\text{GeV}$. The measured production cross sections have been used to determine the ratio of neutral and charged D meson production rates, $R_{u/d}$, the strangenesssuppression factor, γ_s , and the fraction of charged D mesons produced in a vector state, $P_{\rm v}^d$. The fractions of c quarks hadronising as a particular charm hadron, $f(c \to D, \Lambda_c)$, have been calculated in the accepted kinematic range. The results have been compared with the previous HERA measurements of the charm fragmentation characteristics in photoproduction [4] and in deep inelastic scattering (DIS) with $Q^2 > 2 \,\mathrm{GeV}^2$ [6]. To compare the results with those obtained in charm production in e^+e^- annihilations, the $f(c \to D, \Lambda_c)$ fractions compiled previously [7] have been updated using recent values [8] of the relevant branching ratios.

2 Experimental set-up

The analysis was performed with data taken by the ZEUS Collaboration from 1998 to 2000. In this period, HERA collided electrons or positrons² with energy $E_e = 27.5 \text{ GeV}$ and protons with energy $E_p = 920 \text{ GeV}$. The results are based on a sum of the e^-p and e^+p samples corresponding to a total integrated luminosity of $78.6 \pm 1.7 \text{ pb}^{-1}$. Due to trigger considerations, D^+ and Λ_c^+ production was measured using only the e^+p sample corresponding to an integrated luminosity of $65.1 \pm 1.5 \text{ pb}^{-1}$.

A detailed description of the ZEUS detector can be found elsewhere [9]. A brief outline of the components most relevant to this analysis is given below.

¹ Hereafter, charge conjugation is implied.

 $^{^{2}}$ From now on, the word "electron" is used as a generic term for electrons and positrons.

Charged particles are tracked in the central tracking detector (CTD) [10], which operates in a magnetic field of 1.43 T provided by a thin superconducting solenoid. The CTD consists of 72 cylindrical drift chamber layers, organized in nine superlayers covering the polar-angle³ region $15^{\circ} < \theta < 164^{\circ}$. The transverse-momentum resolution for full-length tracks is $\sigma(p_T)/p_T = 0.0058p_T \oplus 0.0065 \oplus 0.0014/p_T$, with p_T in GeV. To estimate the energy loss per unit length, dE/dx, of particles in the CTD [4,11], the truncated mean of the anode-wire pulse heights was calculated, which removes the lowest 10% and at least the highest 30% depending on the number of saturated hits. The measured dE/dx values were normalised to the dE/dx peak position for tracks with momenta 0.3 GeV, theregion of minimum ionisation for pions. Henceforth <math>dE/dx is quoted in units of minimum ionising particles (mips). The resolution of the dE/dx measurement for full-length tracks is about 9%.

The high-resolution uranium-scintillator calorimeter (CAL) [12] consists of three parts: the forward (FCAL), the barrel (BCAL) and the rear (RCAL) calorimeters. Each part is subdivided transversely into towers and longitudinally into one electromagnetic section (EMC) and either one (in RCAL) or two (in BCAL and FCAL) hadronic sections (HAC). The smallest subdivision of the calorimeter is called a cell. The CAL energy resolutions, as measured under test-beam conditions, are $\sigma(E)/E = 0.18/\sqrt{E}$ for electrons and $\sigma(E)/E = 0.35/\sqrt{E}$ for hadrons, with E in GeV.

The luminosity was determined from the rate of the bremsstrahlung process $ep \rightarrow e\gamma p$, where the photon was measured with a lead-scintillator calorimeter [13] located at Z = -107 m.

3 Event simulation

Monte Carlo (MC) samples of charm and beauty events were produced with the PYTHIA 6.156 [14], RAPGAP 2.0818 [15] and HERWIG 6.301 [16] event generators. The generation, based on leading-order matrix elements, includes direct photon processes, in which the photon couples as a point-like object in the hard scatter, and resolved photon processes, where the photon acts as a source of partons, one of which participates in the hard scattering process. Initial- and final-state parton showering is added to simulate higher-order processes. The CTEQ5L [17] and GRV LO [18] parametrisations were used for the proton and photon structure functions, respectively. The charm and bottom quark masses were set to 1.5 GeV and 4.75 GeV, respectively. Events for all processes were

³ The ZEUS coordinate system is a right-handed Cartesian system, with the Z axis pointing in the proton beam direction, referred to as the "forward direction", and the X axis pointing left towards the centre of HERA. The coordinate origin is at the nominal interaction point.

generated in proportion to the predicted MC cross sections. The Lund string model [19] as implemented in JETSET [14] was used for hadronisation in PYTHIA and RAPGAP. The Bowler modification [20] of the Lund symmetric fragmentation function [21] was used for the charm and bottom quark fragmentation. In HERWIG, the cluster model [22] was used for hadronisation. The fraction of charged D mesons produced in a vector state was set to 0.6 for all MC samples.

The PYTHIA and RAPGAP generators were tuned to describe the photoproduction and DIS regimes, respectively. Consequently, the PYTHIA events, generated with $Q^2 < 0.6 \text{ GeV}^2$, were combined with the RAPGAP events, generated with $Q^2 > 0.6 \text{ GeV}^2$. Diffractive events, characterised by a large rapidity gap between the proton at high rapidities and the centrally-produced hadronic system, were generated using the RAPGAP generator in the diffractive mode and combined with the non-diffractive MC sample. The contribution of diffractive events was estimated by fitting the η_{max} distribution⁴ of the data with a linear combination of the non-diffractive and diffractive MC samples. The combined sample was used to evaluate the nominal acceptances. The HERWIG MC sample, generated over the full range of Q^2 values, was used to estimate the model dependence of the acceptance corrections.

To ensure a good description of the data, the transverse momenta, $p_T(D, \Lambda_c)$, and pseudorapidity, $\eta(D, \Lambda_c)$, distributions were reweighted for both combined PYTHIA+RAPGAP and HERWIG MC samples. The reweighting factors were tuned using a large $D^{*\pm}$ sample [23]. The effect of the reweighting on the measured fragmentation ratios and fractions was small; the reweighting uncertainty was included when estimating the model dependence of the acceptance corrections.

The generated events were passed through a full simulation of the detector using GEANT 3.13 [24] and processed with the same reconstruction program as used for the data.

4 Event selection

A three-level trigger system was used to select events online [9,25]. The first- and secondlevel trigger used CAL and CTD data to select ep collisions and to reject beam-gas events. At the third level, where the full event information was available, at least one reconstructed charm-hadron candidate was required. The efficiency of the online charmhadron reconstruction, determined relative to the efficiency of the offline reconstruction, was above 95%.

⁴ The quantity η_{max} is defined as the pseudorapidity of the CAL energy deposit with the lowest polar angle and an energy above 400 MeV.

Photoproduction events were selected by requiring that no scattered electron was identified in the CAL [26]. The Jacquet-Blondel [27] estimator of W, $W_{\rm JB} = \sqrt{2E_p(E - p_Z)}$, was used, where $E - p_Z = \Sigma_i (E - p_Z)_i$ and the sum *i* runs over all final state energy-flow objects [28] produced from charged tracks, as measured in the CTD, and energy clusters measured in the CAL. After correcting for detector effects, the most important of which were energy losses in inactive material in front of the CAL and particle losses in the beam pipe [26, 29], events were selected in the interval 130 < W < 300 GeV. The lower limit was set by the trigger requirements, while the upper limit was imposed to suppress remaining DIS events with an unidentified scattered electron in the CAL [26]. Under these conditions, the photon virtuality lies below 1 GeV². The median Q^2 value was estimated from a Monte Carlo simulation to be about 3×10^{-4} GeV².

5 Reconstruction of charm hadrons

The production of D^{*+} , D^0 , D^+ , D_s^+ and Λ_c^+ charm hadrons was measured in the range of transverse momentum $p_T(D, \Lambda_c) > 3.8 \text{ GeV}$ and pseudorapidity $|\eta(D, \Lambda_c)| < 1.6$. Charm hadrons were reconstructed using tracks measured in the CTD and assigned to the reconstructed event vertex. To ensure good momentum resolution, each track was required to reach at least the third superlayer of the CTD. The combinatorial background was significantly reduced by requiring $p_T(D)/E_T^{\theta>10^\circ} > 0.2$ and $p_T(\Lambda_c)/E_T^{\theta>10^\circ} > 0.25$ for charm mesons and baryons, respectively. The transverse energy was calculated as $E_T^{\theta>10^\circ} = \sum_{i,\theta_i>10^\circ} (E_i \sin \theta_i)$, where the sum runs over all energy deposits in the CAL with the polar angle θ above 10°. Further background reduction was achieved by imposing cuts on the transverse momenta and decay angles of the charm-hadron decay products. The cut values were tuned using MC simulation to enhance signal over background ratios while keeping acceptances high.

The details of the reconstruction of the five charm-hadron samples are given in the next sub-sections.

5.1 Reconstruction of D^0 mesons

The D^0 mesons were reconstructed from the decay $D^0 \to K^-\pi^+$. In each event, tracks with opposite charges and $p_T > 0.8 \text{ GeV}$ were combined in pairs to form D^0 candidates. The nominal kaon and pion masses were assumed in turn for each track and the pair invariant mass, $M(K\pi)$, was calculated. The distribution of the cosine of the D^0 decay angle (defined as the angle $\theta^*(K)$ between the kaon in the $K\pi$ rest frame and the $K\pi$ line of flight in the laboratory frame) is flat, whereas the combinatorial background peaks in the forward and backward directions. To suppress the background, $|\cos \theta^*(K)| < 0.85$ was required.

For selected D^0 candidates, a search was performed for a track that could be a "soft" pion (π_s) in a $D^{*+} \rightarrow D^0 \pi_s^+$ decay. The soft pion was required to have $p_T > 0.2 \,\mathrm{GeV}$ and a charge opposite to that of the particle taken as a kaon. The p_T cut was raised to 0.25 GeV for a data subsample, corresponding to an integrated luminosity of $16.9 \pm 0.4 \,\mathrm{pb}^{-1}$, for which the low-momentum track reconstruction efficiency was smaller due to the operating conditions of the CTD [30]. The corresponding D^0 candidate was assigned to a class of candidates "with ΔM tag" if the mass difference, $\Delta M = M(K\pi\pi_s) - M(K\pi)$, was in the range $0.143 < \Delta M < 0.148$ GeV. All remaining D^0 candidates were assigned to a class of candidates "without ΔM tag". For D^0 candidates with ΔM tag, the kaon and pion mass assignment was fixed by the track-charge requirements. For D^0 mesons without ΔM tag, the mass assignment is ambiguous. The pion and kaon masses can therefore be assigned to two tracks either correctly, producing a signal peak, or incorrectly, producing a wider reflected signal. To remove this reflection, the mass distribution, obtained for D^0 candidates with ΔM tag and an opposite mass assignment to the kaon and pion tracks, was subtracted from the $M(K\pi)$ distribution for all D^0 candidates without ΔM tag. The subtracted mass distribution was normalised to the ratio of numbers of D^0 mesons without and with ΔM tag obtained from a fit described below.

Figure 1 shows the $M(K\pi)$ distribution for D^0 candidates without ΔM tag, obtained after the reflection subtraction, and the $M(K\pi)$ distribution for D^0 candidates with ΔM tag. Clear signals are seen at the nominal value of $M(D^0)$ in both distributions. The distributions were fitted simultaneously assuming the same shape for signals in both distributions. To describe the shape, a "modified" Gaussian function was used:

Gauss^{mod}
$$\propto \exp[-0.5 \cdot x^{1+1/(1+0.5 \cdot x)}],$$
 (1)

where $x = |[M(K\pi) - M_0]/\sigma|$. This functional form described both data and MC signals well. The signal position, M_0 , and width, σ , as well as the numbers of D^0 mesons in each signal were free parameters of the fit. Monte Carlo studies showed that background shapes in both distributions are compatible with being linear in the mass range above the signals. For smaller $M(K\pi)$ values, the background shapes exhibit an exponential enhancement due to contributions from other D^0 decay modes and other D mesons. Therefore the background shape in the fit was described by the form $[A + B \cdot M(K\pi)]$ for $M(K\pi) > 1.86$ GeV and $[A+B \cdot M(K\pi)] \cdot \exp\{C \cdot [M(K\pi)-1.86]\}$ for $M(K\pi) < 1.86$ GeV. The free parameters A, B and C were assumed to be independent for the two $M(K\pi)$ distributions. The numbers of D^0 mesons yielded by the fit were $N^{\text{untag}}(D^0) = 11430\pm 540$ and $N^{\text{tag}}(D^0) = 3259 \pm 91$ for selections without and with ΔM tag, respectively.

5.2 Reconstruction of additional D^{*+} mesons

The $D^{*+} \to D^0 \pi_s^+$ events with $p_T(D^{*+}) > 3.8 \,\text{GeV}$ and $|\eta(D^{*+})| < 1.6$ can be considered as a sum of two subsamples: events with the D^0 having $p_T(D^0) > 3.8 \,\text{GeV}$ and $|\eta(D^0)| < 1.6$, and events with the D^0 outside of that kinematic range. The former sample is represented by D^0 mesons reconstructed with ΔM tag, as discussed in the previous section. The latter sample of "additional" D^{*+} mesons was obtained using the same $D^0 \to K^-\pi^+$ decay channel and an independent selection described below.

In each event, tracks with opposite charges and $p_T > 0.4 \,\text{GeV}$ were combined in pairs to form D^0 candidates. To calculate the pair invariant mass, $M(K\pi)$, kaon and pion masses were assumed in turn for each track. Only D^0 candidates which satisfy 1.81 < $M(K\pi) < 1.92 \,\text{GeV}$ were kept. Moreover, the D^0 candidates were required to have either $p_T(D^0) < 3.8 \,\text{GeV}$ or $|\eta(D^0)| > 1.6$. Any additional track, with $p_T > 0.2 \,\text{GeV}$ and a charge opposite to that of the kaon track, was assigned the pion mass and combined with the D^0 candidate to form a D^{*+} candidate with invariant mass $M(K\pi\pi_s)$. Here again the p_T cut was raised to 0.25 GeV for the data subsample for which the low-momentum track reconstruction efficiency was smaller.

Figure 2 shows the ΔM distribution for the D^{*+} candidates after all cuts. A clear signal is seen at the nominal value of $M(D^{*+}) - M(D^0)$. The combinatorial background was estimated from the mass-difference distribution for wrong-charge combinations, in which both tracks forming the D^0 candidate have the same charge and the third track has the opposite charge. The same tracks from a wrong-charge combination can produce two D^0 candidates due to an ambiguity in the kaon and pion mass assignment to tracks with the same charge. To exclude double counting, the multiple combinations of the same tracks which passed all cuts, including the $M(K\pi)$ requirement, were included with a weight 1/2.

The number of reconstructed additional D^{*+} mesons was determined by subtracting the wrong-charge ΔM distribution after normalising it to the distribution of D^{*+} candidates with the appropriate charges in the range $0.15 < \Delta M < 0.17$ GeV. The subtraction, performed in the signal range $0.143 < \Delta M < 0.148$ GeV, yielded $N^{\text{add}}(D^{*+}) = 826 \pm 40$.

The ΔM distribution was also fitted to a sum of the modified Gaussian function (Eq. (1)) describing the signal and a threshold function describing the non-resonant background. The threshold function had a form $A \cdot (\Delta M - m_{\pi})^B$, where m_{π} is the pion mass [8] and A and B were free parameters. The results obtained using the fit instead of the subtraction procedure were used to estimate the systematic uncertainty of the signal extraction procedure.

5.3 Reconstruction of D^+ mesons

The D^+ mesons were reconstructed from the decay $D^+ \to K^-\pi^+\pi^+$. In each event, two tracks with the same charges and $p_T > 0.5 \,\text{GeV}$ and a third track with opposite charge and $p_T > 0.7 \,\text{GeV}$ were combined to form D^+ candidates. The pion masses were assigned to the two tracks with the same charges and the kaon mass was assigned to the third track, after which the candidate invariant mass, $M(K\pi\pi)$, was calculated. To suppress the combinatorial background, a cut of $\cos \theta^*(K) > -0.75$ was imposed, where $\theta^*(K)$ is the angle between the kaon in the $K\pi\pi$ rest frame and the $K\pi\pi$ line of flight in the laboratory frame. To suppress background from D^{*+} decays, combinations with $M(K\pi\pi) - M(K\pi) < 0.15 \,\text{GeV}$ were removed. The background from $D_s^+ \to \phi \pi^+$ with $\phi \to K^+K^-$ was suppressed by requiring that the invariant mass of any two D^+ candidate tracks with opposite charges was not within $\pm 8 \,\text{MeV}$ of the ϕ mass [4] when the kaon mass was assigned to both tracks.

Figure 3 shows the $M(K\pi\pi)$ distribution for the D^+ candidates after all cuts. Reflections from D_s^+ and Λ_c^+ decays to three charged particles were subtracted using the simulated reflection shapes normalised to the measured D_s^+ and Λ_c^+ production rates. A clear signal is seen at the nominal value of D^+ mass. The mass distribution was fitted to a sum of a modified Gaussian function (Eq. (1)) describing the signal and a linear function describing the non-resonant background. The number of reconstructed D^+ mesons yielded by the fit was $N(D^+) = 8950 \pm 600$.

5.4 Reconstruction of D_s^+ mesons

The D_s^+ mesons were reconstructed from the decay $D_s^+ \to \phi \pi^+$ with $\phi \to K^+ K^-$. In each event, tracks with opposite charges and $p_T > 0.7 \,\text{GeV}$ were assigned the kaon mass and combined in pairs to form ϕ candidates. The ϕ candidate was kept if its invariant mass, M(KK), was within $\pm 8 \,\text{MeV}$ of the ϕ mass [4]. Any additional track with $p_T > 0.5 \,\text{GeV}$ was assigned the pion mass and combined with the ϕ candidate to form a D_s^+ candidate with invariant mass $M(KK\pi)$. To suppress the combinatorial background, the following requirements were applied:

- $\cos \theta^*(\pi) < 0.85$, where $\theta^*(\pi)$ is the angle between the pion in the $KK\pi$ rest frame and the $KK\pi$ line of flight in the laboratory frame;
- $|\cos^3 \theta'(K)| > 0.1$, where $\theta'(K)$ is the angle between one of the kaons and the pion in the KK rest frame. The decay of the pseudoscalar D_s^+ meson to the ϕ (vector) plus π^+ (pseudoscalar) final state results in an alignment of the spin of the ϕ meson with respect to the direction of motion of the ϕ relative to D_s^+ . Consequently, the distribution of $\cos \theta'(K)$ follows a $\cos^2 \theta'(K)$ shape, implying a flat distribution for

 $\cos^3 \theta'(K)$. In contrast, the $\cos \theta'(K)$ distribution of the combinatorial background is flat and its $\cos^3 \theta'(K)$ distribution peaks at zero. The cut suppressed the background significantly while reducing the signal by 10%.

Figure 4 shows the $M(KK\pi)$ distribution for the D_s^+ candidates after all cuts. Reflections from D^+ and Λ_c^+ decays to three charged particles were subtracted using the simulated reflection shapes normalised to the measured D^+ and Λ_c^+ production rates. A clear signal is seen at the nominal D_s^+ mass. There is also a smaller signal around the nominal D^+ mass as expected from the decay $D^+ \to \phi \pi^+$ with $\phi \to K^+K^-$. The mass distribution was fitted to a sum of two modified Gaussian functions (Eq. (1)) describing the signals and an exponential function describing the non-resonant background. To reduce the number of free parameters, the width of the D^+ signal was constrained to 8/9 of the D_s^+ signal width; the constraint was verified by MC studies. The number of reconstructed D_s^+ mesons yielded by the fit was $N(D_s^+) = 1102 \pm 83^{-5}$.

5.5 Reconstruction of Λ_c^+ baryons

The Λ_c^+ baryons were reconstructed from the decay $\Lambda_c^+ \to K^- p \pi^+$. In each event, two same-charge tracks and a third track with opposite charge were combined to form Λ_c^+ candidates. Due to the large difference between the proton and pion masses, the proton momentum is typically larger than that of the pion. Therefore, the proton (pion) mass was assigned to those of the two tracks with the same charges which had larger (smaller) momentum. The kaon mass was assigned to the third track and the candidate invariant mass, $M(Kp\pi)$, was calculated. Only candidates with $p_T(K) > 0.75$ GeV, $p_T(p) > 1.3$ GeV and $p_T(\pi) > 0.5$ GeV were kept. To suppress the combinatorial background, the following requirements, motivated by MC studies, were applied:

- $\cos \theta^*(K) > -0.9$, where $\theta^*(K)$ is the angle between the kaon in the $Kp\pi$ rest frame and the $Kp\pi$ line of flight in the laboratory frame;
- $\cos \theta^*(p) > -0.25$, where $\theta^*(p)$ is the angle between the proton in the $Kp\pi$ rest frame and the $Kp\pi$ line of flight in the laboratory frame;
- $p^*(\pi) > 90$ MeV, where $p^*(\pi)$ is the pion momentum in the $Kp\pi$ rest frame.

To suppress the combinatorial background further, the measured dE/dx values of the three Λ_c^+ candidate tracks were used. The parametrisations of the dE/dx expectation values and the χ_1^2 probabilities l_p , l_K and l_{π} of the proton, kaon and pion hypotheses, respectively, were obtained in the same way as described in a previous publication [23]. The l_p , l_K and l_{π} distributions for the Λ_c^+ candidate tracks show sharp peaks around

⁵ The number of D^+ mesons, 239 ± 63 , was not used further in the analysis.

zero and become relatively flat towards one. To maximise the ratios of the numbers of correctly assigned protons, kaons and pions to the square roots of the numbers of background particles, the cuts $l_p > 0.15$, $l_K > 0.03$ and $l_{\pi} > 0.01$ were applied. The cuts rejected those ranges where the l_p , l_K and l_{π} distributions were at least twice as high as in the range 0.8 - 1.

Figure 5 shows the $M(Kp\pi)$ distribution for the Λ_c^+ candidates after all cuts. Reflections from D^+ and D_s^+ decays to three charged particles were subtracted using the simulated reflection shapes normalised to the measured D^+ and D_s^+ production rates. A clear signal is seen at the nominal Λ_c^+ mass. The mass distribution was fitted to a sum of a modified Gaussian function (Eq. (1)) describing the signal and a linear function describing the non-resonant background. The number of reconstructed Λ_c^+ baryons yielded by the fit was $N(\Lambda_c^+) = 1440 \pm 220$.

6 Charm-hadron production cross sections

The charm-hadron cross sections were calculated for the process $ep \rightarrow eD(\Lambda_c)X$ in the kinematic region $Q^2 < 1 \text{ GeV}^2$, 130 < W < 300 GeV, $p_T(D, \Lambda_c) > 3.8 \text{ GeV}$ and $|\eta(D, \Lambda_c)| < 1.6$. The cross section for a given charm hadron was calculated from

$$\sigma(D, \Lambda_c) = \frac{N(D, \Lambda_c)}{\mathcal{A} \cdot \mathcal{L} \cdot \mathcal{B}},$$

where $N(D, \Lambda_c)$ is the number of reconstructed charm hadrons, \mathcal{A} is the acceptance for this charm hadron, \mathcal{L} is the integrated luminosity and \mathcal{B} is the branching ratio or the product of the branching ratios [8] for the decay channel used in the reconstruction. The third uncertainties quoted below for the measured cross sections and charm fragmentation ratios and fractions are due to the branching-ratio uncertainties⁶.

The combined PYTHIA+RAPGAP MC sample was used to evaluate the nominal acceptances. Small admixtures to the reconstructed signals from other decay modes were taken into account in the acceptance correction procedure. To correct from $N^{\text{tag}}(D^0)$ $(N^{\text{untag}}(D^0))$ to the production cross sections for D^0 mesons originating (not originating) from D^{*+} decays, small migrations between the two samples were taken into account. The *b*-quark relative contributions, predicted by the MC simulation using branching ratios of *b*-quark decays to the charmed hadrons measured at LEP [31,32], were subtracted from all measured cross sections⁷. Subtraction of the *b*-quark contribution reduced the

 $^{^{6}}$ Contributions from uncertainties of different branching ratios were added in quadrature.

⁷ The branching ratios of the *b*-quark decays were updated using recent values [8] of the relevant charmhadron decay branching ratios.

measured cross sections by 3-7% and changed the measured charm fragmentation ratios and fractions by less than 4%.

Using the reconstructed signals (see Section 5) the following cross sections for the sum of each charm hadron and its antiparticle were calculated:

• the production cross section for D^0 mesons not originating from the $D^{*+} \to D^0 \pi_s^+$ decays:

$$\sigma^{\text{untag}}(D^0) = 8.49 \pm 0.44 (\text{stat.})^{+0.47}_{-0.48} (\text{syst.})^{+0.20}_{-0.19} (\text{br.}) \text{ nb};$$

• the production cross section for D^0 mesons originating from the $D^{*+} \to D^0 \pi_s^+$ decays:

$$\sigma^{\text{tag}}(D^0) = 2.65 \pm 0.08(\text{stat.})^{+0.11}_{-0.10}(\text{syst.}) \pm 0.06(\text{br.}) \,\text{nb.}$$

The ratio $\sigma^{\text{tag}}(D^0)/\mathcal{B}_{D^{*+}\to D^0\pi^+}$ gives the D^{*+} cross section, $\sigma(D^{*+})$, corresponding to D^0 production in the kinematic range $p_T(D^0) > 3.8 \text{ GeV}$ and $|\eta(D^0)| < 1.6$ for the $D^{*+} \to D^0\pi^+_s$ decay. Here $\mathcal{B}_{D^{*+}\to D^0\pi^+} = 0.677 \pm 0.005$ [8] is the branching ratio of the $D^{*+} \to D^0\pi^+_s$ decay;

• the production cross section for additional D^{*+} mesons:

$$\sigma^{\text{add}}(D^{*+}) = 1.05 \pm 0.07 (\text{stat.})^{+0.09}_{-0.04} (\text{syst.}) \pm 0.03 (\text{br.}) \text{ nb.}$$

The sum $\sigma^{\text{add}}(D^{*+}) + \sigma^{\text{tag}}(D^0)/\mathcal{B}_{D^{*+}\to D^0\pi^+}$ gives the production cross section for D^{*+} mesons in the kinematic range $p_T(D^{*+}) > 3.8 \text{ GeV}$ and $|\eta(D^{*+})| < 1.6$:

$$\sigma^{\rm kin}(D^{*+}) = 4.97 \pm 0.14 ({\rm stat.})^{+0.23}_{-0.18} ({\rm syst.})^{+0.13}_{-0.12} ({\rm br.}) {\rm nb};$$

• the production cross section for D^+ mesons:

$$\sigma(D^+) = 5.07 \pm 0.36(\text{stat.})^{+0.44}_{-0.23}(\text{syst.})^{+0.34}_{-0.30}(\text{br.}) \text{ nb};$$

• the production cross section for D_s^+ mesons:

$$\sigma(D_s^+) = 2.37 \pm 0.20 (\text{stat.}) \pm 0.20 (\text{syst.})^{+0.72}_{-0.45} (\text{br.}) \text{ nb};$$

• the production cross section for Λ_c^+ baryons:

$$\sigma(\Lambda_c^+) = 3.59 \pm 0.66 (\text{stat.})^{+0.54}_{-0.66} (\text{syst.})^{+1.15}_{-0.70} (\text{br.}) \text{ nb.}$$

7 Charm fragmentation ratios and fractions

7.1 Ratio of neutral to charged *D*-meson production rates

Neglecting influences from decays of heavier excited D mesons, the ratio of neutral to charged D-meson production rates is given by the ratio of the sum of D^{*0} and direct D^0 production cross sections to the sum of D^{*+} and direct D^+ production cross sections:

$$R_{u/d} = \frac{\sigma(D^{*0}) + \sigma^{\operatorname{dir}}(D^0)}{\sigma(D^{*+}) + \sigma^{\operatorname{dir}}(D^+)},$$

where $\sigma^{\text{dir}}(D^0)$ and $\sigma^{\text{dir}}(D^+)$ are those parts of the D^0 and D^+ inclusive cross sections which do not originate from D^{*0} and D^{*+} decays. Since all D^{*0} decays produce a D^0 meson [8], the sum of $\sigma(D^{*0})$ and $\sigma^{\text{dir}}(D^0)$ is the production cross section for D^0 mesons not originating from D^{*+} decays:

$$\sigma(D^{*0}) + \sigma^{\operatorname{dir}}(D^0) = \sigma^{\operatorname{untag}}(D^0).$$
⁽²⁾

Subtracting from $\sigma(D^+)$ the contribution from D^{*+} decays gives

$$\sigma^{\rm dir}(D^+) = \sigma(D^+) - \sigma(D^{*+}) \cdot (1 - \mathcal{B}_{D^{*+} \to D^0 \pi^+}).$$
(3)

Thus, the ratio of neutral and charged *D*-meson production rates can be calculated as

$$R_{u/d} = \frac{\sigma^{\mathrm{untag}}(D^0)}{\sigma(D^+) + \sigma(D^{*+}) \cdot \mathcal{B}_{D^{*+} \to D^0 \pi^+}} = \frac{\sigma^{\mathrm{untag}}(D^0)}{\sigma(D^+) + \sigma^{\mathrm{tag}}(D^0)}.$$

Using the measured cross sections, the ratio of neutral to charged *D*-meson production rates, obtained for the kinematic region $Q^2 < 1 \text{ GeV}^2$, 130 < W < 300 GeV, $p_T(D) > 3.8 \text{ GeV}$ and $|\eta(D)| < 1.6$, is

$$R_{u/d} = 1.100 \pm 0.078 \,(\text{stat.})^{+0.038}_{-0.061} \,(\text{syst.})^{+0.047}_{-0.049} \,(\text{br.}).$$

The measured $R_{u/d}$ value agrees with unity, i.e. it is consistent with isospin invariance, which implies that u and d quarks are produced equally in charm fragmentation.

Table 1 compares the measurement with the values obtained in DIS [6] and in e^+e^- annihilations. The latter value was calculated as

$$R_{u/d} = \frac{f(c \to D^0) - f(c \to D^{*+}) \cdot \mathcal{B}_{D^{*+} \to D^0 \pi^+}}{f(c \to D^+) + f(c \to D^{*+}) \cdot \mathcal{B}_{D^{*+} \to D^0 \pi^+}}$$

using fragmentation fractions compiled previously [7] and updated with the recent branching ratio values [8]. All measurements agree with unity within experimental uncertainties. The branching ratio uncertainties of all measurements are highly correlated.

7.2 Equivalent phase-space treatment

In the subtraction of the D^{*+} contribution to D^+ production in Eq. (3), the cross-section $\sigma(D^{*+})$, corresponding to D^0 production in the kinematic range $p_T(D^0) > 3.8 \,\text{GeV}$ and $|\eta(D^0)| < 1.6$ for the $D^{*+} \to D^0 \pi_s^+$ decay, was used. Replacing $\sigma(D^{*+})$ with $\sigma^{\text{tag}}(D^0)/\mathcal{B}_{D^{*+}\to D^0\pi^+}$ gives

$$\sigma^{\rm dir}(D^+) = \sigma(D^+) - \sigma^{\rm tag}(D^0) \cdot (1 - \mathcal{B}_{D^{*+} \to D^0 \pi^+}) / \mathcal{B}_{D^{*+} \to D^0 \pi^+} .$$

To compare direct D^+ and D^{*+} production, the cross section $\sigma^{\text{kin}}(D^{*+})$ for $p_T(D^{*+}) > 3.8 \text{ GeV}$ and $|\eta(D^{*+})| < 1.6$ is used in Section 7.4. To compare the inclusive D^+ and D^0 cross sections with each other and with the inclusive D^{*+} cross section it is necessary to take into account that only a fraction of the parent D^* momentum is transferred to the daughter D meson. For such comparisons, the "equivalent" D^+ and D^0 cross sections were defined as the sums of their direct cross sections and contributions from D^* decays calculated using $\sigma^{\text{kin}}(D^{*+})$ and $\sigma^{\text{kin}}(D^{*0})$:

$$\sigma^{\rm eq}(D^+) = \sigma^{\rm dir}(D^+) + \sigma^{\rm kin}(D^{*+}) \cdot (1 - \mathcal{B}_{D^{*+} \to D^0 \pi^+}),
\sigma^{\rm eq}(D^0) = \sigma^{\rm dir}(D^0) + \sigma^{\rm kin}(D^{*+}) \cdot \mathcal{B}_{D^{*+} \to D^0 \pi^+} + \sigma^{\rm kin}(D^{*0}),$$

where $\sigma^{\text{kin}}(D^{*0})$ is the inclusive D^{*0} cross section for $p_T(D^{*0}) > 3.8 \text{ GeV}$ and $|\eta(D^{*0})| < 1.6$. This cross section can be written as the sum $\sigma(D^{*0}) + \sigma^{\text{add}}(D^{*0})$, where $\sigma(D^{*0})$ is the part contributing to the D^0 production in the nominal kinematic range (as in Eq. (2)) and $\sigma^{\text{add}}(D^{*0})$ is the production cross section for "additional" D^{*0} mesons producing D^0 mesons outside of that kinematic range. The latter cross section was calculated using $\sigma^{\text{add}}(D^{*+})$ and the expression for $R_{u/d}$:

$$\sigma^{\mathrm{add}}(D^{*0}) = \sigma^{\mathrm{add}}(D^{*+}) \cdot R_{u/d} = \sigma^{\mathrm{add}}(D^{*+}) \cdot \frac{\sigma^{\mathrm{untag}}(D^0)}{\sigma(D^+) + \sigma^{\mathrm{tag}}(D^0)}.$$

Using Eqs. (2) and (3) for $\sigma^{\text{dir}}(D^0)$ and $\sigma^{\text{dir}}(D^+)$, respectively, and the expressions for $\sigma^{\text{kin}}(D^{*0})$ and $\sigma^{\text{kin}}(D^{*+})$ gives

$$\sigma^{\rm eq}(D^0) = \sigma^{\rm untag}(D^0) + \sigma^{\rm tag}(D^0) + \sigma^{\rm add}(D^{*+}) \cdot (R_{u/d} + \mathcal{B}_{D^{*+} \to D^0 \pi^+}),$$

$$\sigma^{\rm eq}(D^+) = \sigma(D^+) + \sigma^{\rm add}(D^{*+}) \cdot (1 - \mathcal{B}_{D^{*+} \to D^0 \pi^+}).$$

MC studies show that such "equivalent phase-space treatment" for the non-strange D and D^* mesons minimises differences between the fragmentation ratios and fractions measured in the accepted $p_T(D, \Lambda_c)$ and $\eta(D, \Lambda_c)$ kinematic region and those in the full phase space (see Section 7.6).

7.3 Strangeness-suppression factor

The strangeness-suppression factor for charm mesons is given by the ratio of twice the production rate of charm-strange mesons to the production rate of non-strange charm mesons. All D^{*+} and D^{*0} decays produce either a D^+ or a D^0 meson, while all D_s^{*+} decays produce a D_s^+ meson [8]. Thus, neglecting decays of heavier excited charm-strange mesons to non-strange charm mesons, the strangeness-suppression factor can be calculated as a ratio of twice the D_s^+ production cross section to the sum of D^0 and D^+ production cross sections. Using the equivalent D^0 and D^+ cross sections gives

$$\gamma_s = \frac{2\,\sigma(D_s^+)}{\sigma^{\rm eq}(D^+) + \sigma^{\rm eq}(D^0)} = \frac{2\,\sigma(D_s^+)}{\sigma(D^+) + \sigma^{\rm untag}(D^0) + \sigma^{\rm tag}(D^0) + \sigma^{\rm add}(D^{*+}) \cdot (1 + R_{u/d})}$$

Using the measured cross sections, the strangeness-suppression factor, obtained for the kinematic region $Q^2 < 1 \text{ GeV}^2$, 130 < W < 300 GeV, $p_T(D) > 3.8 \text{ GeV}$ and $|\eta(D)| < 1.6$, is

 $\gamma_s = 0.257 \pm 0.024 \,(\text{stat.})^{+0.013}_{-0.016} \,(\text{syst.})^{+0.078}_{-0.049} \,(\text{br.}).$

Thus, charm-strange meson production is suppressed by a factor ≈ 3.9 in charm fragmentation. In simulations based on the Lund string fragmentation scheme [33], strangeness suppression is a free parameter which determines the ratio of probabilities to create sto u and d quarks during the fragmentation processes. In the absence of excited charmstrange meson decays to non-strange charm mesons, the Lund strangeness-suppression parameter would be effectively the observable, γ_s . In fact, production rates of the excited charm-strange mesons are poorly known; varying these rates in wide ranges in the PYTHIA simulation suggests that the Lund strangeness-suppression parameter is 10 - 30% larger than the observable, γ_s .

Table 2 compares the measurement with the previous ZEUS 96-97 result, calculated from the ratio of D_s^+ to D^{*+} cross sections [4], and with the values obtained for charm production in DIS [6] and in e^+e^- annihilations. The e^+e^- value was calculated as

$$\gamma_s = \frac{2f(c \to D_s^+)}{f(c \to D^+) + f(c \to D^0)}$$

using fragmentation fractions compiled previously [7] and updated with the recent branching ratio values [8]. All measurements agree within experimental uncertainties. The large branching-ratio uncertainties are dominated by the common uncertainty of the $D_s^+ \to \phi \pi^+$ branching ratio. This uncertainty can be ignored in the comparison with other measurements using the same branching ratios.

7.4 Fraction of charged D mesons produced in a vector state

Neglecting influences from decays of heavier excited D mesons, the fraction of D mesons produced in a vector state is given by the ratio of vector to (vector+pseudoscalar) charm meson production cross sections. Only direct parts of the production cross sections for pseudoscalar charm mesons should be used. Using the expressions for $\sigma^{\text{kin}}(D^{*+})$ and $\sigma^{\text{dir}}(D^+)$, the fraction for charged charm mesons is given by

$$P_{\rm v}^{d} = \frac{\sigma^{\rm kin}(D^{*+})}{\sigma^{\rm kin}(D^{*+}) + \sigma^{\rm dir}(D^{+})} = \frac{\sigma^{\rm tag}(D^{0})/\mathcal{B}_{D^{*+}\to D^{0}\pi^{+}} + \sigma^{\rm add}(D^{*+})}{\sigma(D^{+}) + \sigma^{\rm tag}(D^{0}) + \sigma^{\rm add}(D^{*+})}.$$

Using the measured cross sections, the fraction of charged D mesons produced in a vector state, obtained for the kinematic region $Q^2 < 1 \text{ GeV}^2$, 130 < W < 300 GeV, $p_T(D) > 3.8 \text{ GeV}$ and $|\eta(D)| < 1.6$, is

$$P_{\rm v}^d = 0.566 \pm 0.025 \,(\text{stat.})^{+0.007}_{-0.022} \,(\text{syst.})^{+0.022}_{-0.023} \,(\text{br.}).$$

The measured P_v^d fraction is considerably smaller than the naive spin-counting prediction of 0.75. The predictions of the thermodynamical approach [34] and the string fragmentation approach [35], which both predict 2/3 for the fraction, are closer to, but still above, the measured value. The BKL model [36, 37], based on a tree-level perturbative QCD calculation with the subsequent hadronisation of the (c, \bar{q}) state, predicts $P_v^d \approx 0.6$ for charm production in e^+e^- annihilations where only fragmentation diagrams contribute. For charm photoproduction, where both fragmentation and recombination diagrams contribute, the BKL prediction is $P_v^d \approx 0.66$ in the measured kinematic range.

Table 3 compares the measurement with the values obtained in DIS [6] and in e^+e^- annihilations. The latter value was calculated as

$$P_{\mathbf{v}}^{d} = \frac{f(c \to D^{*+})}{f(c \to D^{*}) + f(c \to D^{*+}) \cdot \mathcal{B}_{D^{*+} \to D^{0} \pi^{+}}}$$

using fragmentation fractions compiled previously [7] and updated with the recent branching ratio values [8]. The measured P_v^d value is smaller than, but consistent with, the previous measurements. The branching-ratio uncertainties of all measurements are highly correlated.

7.5 Charm fragmentation fractions

The fraction of c quarks hadronising as a particular charm hadron, $f(c \to D, \Lambda_c)$, is given by the ratio of the production cross section for the hadron to the sum of the production cross sections for all charm ground states that decay weakly. In addition to the measured D^0 , D^+ , D_s^+ and Λ_c^+ charm ground states, the production cross sections of the charmstrange baryons Ξ_c^+ , Ξ_c^0 and Ω_c^0 should be included in the sum. The production rates for these baryons are expected to be much lower than that of the Λ_c^+ due to strangeness suppression. The relative rates for the charm-strange baryons which decay weakly were estimated from the non-charm sector following the LEP procedure [38]. The measured Ξ^-/Λ and Ω^-/Λ relative rates are $(6.65 \pm 0.28)\%$ and $(0.42 \pm 0.07)\%$, respectively [8]. Assuming equal production of Ξ^0 and Ξ^- states and that a similar suppression is applicable to the charm baryons, the total rate for the three charm-strange baryons relative to the Λ_c^+ state is expected to be about 14%. Therefore the Λ_c^+ production cross section was scaled by the factor 1.14 in the sum of the production cross sections. An error of ± 0.05 was assigned to the scale factor when evaluating systematic uncertainties.

Using the equivalent D^0 and D^+ cross sections, the sum of the production cross sections for all open-charm ground states (gs) is given by

$$\sigma_{\rm gs} = \sigma^{\rm eq}(D^+) + \sigma^{\rm eq}(D^0) + \sigma(D_s^+) + \sigma(\Lambda_c^+) \cdot 1.14,$$

which can be expressed as

$$\sigma_{\rm gs} = \sigma(D^+) + \sigma^{\rm untag}(D^0) + \sigma^{\rm tag}(D^0) + \sigma^{\rm add}(D^{*+}) \cdot (1 + R_{u/d}) + \sigma(D_s^+) + \sigma(\Lambda_c^+) \cdot 1.14.$$

For the measured cross sections,

$$\sigma_{\rm gs} = 24.9 \pm 1.0 \,({\rm stat.})^{+1.7}_{-1.4} \,({\rm syst.})^{+1.6}_{-1.0} \,({\rm br.}) \,{\rm nb.}$$

The fragmentation fractions for the measured charm ground states are given by

$$\begin{split} f(c \to D^+) &= \sigma^{\mathrm{eq}}(D^+) / \sigma_{\mathrm{gs}} = [\sigma(D^+) + \sigma^{\mathrm{add}}(D^{*+}) \cdot (1 - \mathcal{B}_{D^{*+} \to D^0 \pi^+})] / \sigma_{\mathrm{gs}}, \\ f(c \to D^0) &= \sigma^{\mathrm{eq}}(D^0) / \sigma_{\mathrm{gs}} \\ &= [\sigma^{\mathrm{untag}}(D^0) + \sigma^{\mathrm{tag}}(D^0) + \sigma^{\mathrm{add}}(D^{*+}) \cdot (R_{u/d} + \mathcal{B}_{D^{*+} \to D^0 \pi^+})] / \sigma_{\mathrm{gs}}, \\ f(c \to D_s^+) &= \sigma(D_s^+) / \sigma_{\mathrm{gs}}, \\ f(c \to \Lambda_c^+) &= \sigma(\Lambda_c^+) / \sigma_{\mathrm{gs}}. \end{split}$$

Using $\sigma^{\text{kin}}(D^{*+})$, the fragmentation fraction for the D^{*+} state is given by

$$f(c \to D^{*+}) = \sigma^{\rm kin}(D^{*+}) / \sigma_{\rm gs} = [\sigma^{\rm tag}(D^0) / \mathcal{B}_{D^{*+} \to D^0 \pi^+} + \sigma^{\rm add}(D^{*+})] / \sigma_{\rm gs}.$$

The open-charm fragmentation fractions, measured in the kinematic region $Q^2 < 1 \text{ GeV}^2$, 130 < W < 300 GeV, $p_T(D, \Lambda_c) > 3.8 \text{ GeV}$ and $|\eta(D, \Lambda_c)| < 1.6$, are summarised in Table 4. The results are compared with the values obtained in DIS [6] and with the combined fragmentation fractions for charm production in e^+e^- annihilations compiled previously [7] and updated with the recent branching-ratio values [8]. The branching-ratio uncertainties of all measurements are highly correlated. The measurements are consistent although the measured $f(c \to D^{*+})$ is smaller and $f(c \to \Lambda_c^+)$ is larger than those obtained in e^+e^- annihilations. About half of the difference in the $f(c \to D^{*+})$ values is due to the difference in the $f(c \to \Lambda_c^+)$ values. The measurement may indicate an enhancement of Λ_c^+ production in ep collisions with respect to e^+e^- . However, this is unlikely to be a consequence of the baryon-number-flow effect [39] because no significant asymmetry between the Λ_c^+ and $\bar{\Lambda}_c^-$ production rates was observed⁸.

7.6 Discussion of extrapolation effects

The charm fragmentation ratios and fractions were measured in the region $p_T(D, \Lambda_c) > 3.8 \text{ GeV}$ and $|\eta(D, \Lambda_c)| < 1.6$. To minimise differences between the values measured in the accepted $p_T(D, \Lambda_c)$ and $\eta(D, \Lambda_c)$ kinematic region and those in the full phase space, the equivalent phase-space treatment for the non-strange D and D^* mesons was used (see Section 7.2).

Table 5 shows estimates of extrapolation factors correcting the values measured in the accepted $p_T(D, \Lambda_c)$ and $\eta(D, \Lambda_c)$ region to the full phase space. The extrapolation factors were determined using three different fragmentation schemes: the Peterson parameterisation [40] of the charm fragmentation function as implemented in PYTHIA, the Bowler modification [20] of the LUND symmetric fragmentation function [21] as implemented in PYTHIA and the cluster model [22] as implemented in HERWIG. The quoted uncertainties were obtained by varying relevant parameters in the PYTHIA and HERWIG MC generators. The extrapolation factors obtained are generally close to unity. The only exceptions are the factors given by the cluster model for $f(c \to \Lambda_c^+)$ and, to a lesser extent, for γ_s and $f(c \to D_s^+)$.

This MC study suggests that the measured charm fragmentation ratios and fractions are close to those in the full $p_T(D, \Lambda_c)$ and $\eta(D, \Lambda_c)$ phase space.

8 Systematic uncertainties

The systematic uncertainties of the measured cross sections and fragmentation ratios and fractions were determined by changing the analysis procedure and repeating all calculations. The following groups of the systematic uncertainty sources were considered:

⁸ Separate fits of the $M(K^-p\pi^+)$ and $M(K^+\bar{p}\pi^-)$ distributions yielded $N(\Lambda_c^+)/N(\bar{\Lambda}_c^-) = 0.8 \pm 0.2$.

- $\{\delta_1\}$ the model dependence of the acceptance corrections was estimated using the HERWIG MC sample, varying the $p_T(D, \Lambda_c)$ and $\eta(D, \Lambda_c)$ distributions of the reference MC sample and by changing the MC fraction of charged D mesons produced in a vector state from 0.6 to 0.5 or 0.7;
- $\{\delta_2\}$ the uncertainty of the beauty subtraction was determined by varying the *b*quark cross section by a factor of two in the reference MC sample and by varying the branching ratios of *b*-quarks to charm hadrons by their uncertainties [31, 32];
- $\{\delta_3\}$ the uncertainty of the tracking simulation was obtained by varying all momenta by $\pm 0.3\%$ (magnetic field uncertainty), varying the track-loss probabilities by $\pm 20\%$ of their values and by changing the track momentum and angular resolutions by $^{+20}_{-10}\%$ of their values. The asymmetric resolution variations were used since the MC signals typically had somewhat narrower widths than observed in the data;
- $\{\delta_4\}$ the uncertainty of the CAL simulation was determined by varying the CAL energy scale by $\pm 2\%$, by changing the CAL energy resolution by $\pm 20\%$ of its value and by varying the first-level trigger CAL efficiencies;
- $\{\delta_5\}$ the uncertainties related to the signal extraction procedures were obtained as follows:
 - for the D^0 signals with and without ΔM tag: the background parametrisation and the range used for the signal fits were varied;
 - for the additional D^{*+} signal: the range used for the background normalisation was varied or the fit was used instead of the subtraction procedure;
 - for the D^+ , D_s^+ and Λ_c^+ signals: the background parametrisations, ranges used for the signal fits and amounts of the mutual reflections were varied. In addition, in the D_s^+ signal-extraction procedure, the constraint used for the $D^+ \to KK\pi$ signal width was varied. In the Λ_c^+ signal extraction procedure, an uncertainty in the dE/dx simulation was estimated by changing the dE/dx cut values in the MC and checking the effects with respect to changes expected from the χ_1^2 distribution.
- { δ_6 } the uncertainties of the luminosities of the e^-p (±1.8%) and e^+p (±2.25%) data samples were included taking into account their correlations;
- $\{\delta_7\}$ the uncertainty in the rate of the charm-strange baryons (see Section 7.5).

Contributions from the different systematic uncertainties were calculated and added in quadrature separately for positive and negative variations. The total and δ_1 - δ_7 systematic uncertainties for the charm-hadron cross sections and charm fragmentation ratios and fractions are summarised in Table 6. Correlated systematic uncertainties largely cancelled in the calculation of the fragmentation ratios and fractions.

To check the hadron-mass effects on the measured charm fragmentation ratios and fractions, the analysis was repeated using the charm-hadron transverse energy instead of the transverse momentum in the definition of the kinematic range of the measurement; the results obtained agreed with the reported values within statistical errors. The charm fragmentation ratios and fractions were also calculated separately for two W sub-ranges; no significant variations were observed.

9 Summary

The production of the charm hadrons D^{*+} , D^0 , D^+ , D_s^+ and Λ_c^+ has been measured with the ZEUS detector in the kinematic range $p_T(D, \Lambda_c) > 3.8 \text{ GeV}$, $|\eta(D, \Lambda_c)| < 1.6$, 130 < W < 300 GeV and $Q^2 < 1 \text{ GeV}^2$. The cross sections have been used to determine the charm fragmentation ratios and fractions with comparable precision to the e^+e^- results.

The ratio of neutral to charged *D*-meson production rates is

$$R_{u/d} = 1.100 \pm 0.078 \,(\text{stat.})^{+0.038}_{-0.061} \,(\text{syst.})^{+0.047}_{-0.049} \,(\text{br.}).$$

The measured $R_{u/d}$ value agrees with unity, i.e. it is consistent with isospin invariance, which implies that u and d quarks are produced equally in charm fragmentation.

The strangeness-suppression factor is

$$\gamma_s = 0.257 \pm 0.024 \,(\text{stat.})^{+0.013}_{-0.016} \,(\text{syst.})^{+0.078}_{-0.049} \,(\text{br.}).$$

Thus, D_s -meson production is suppressed by a factor ≈ 3.9 in charm fragmentation.

The fraction of charged D mesons produced in a vector state is

$$P_{\rm v}^d = 0.566 \pm 0.025 \,(\text{stat.})^{+0.007}_{-0.022} \,(\text{syst.})^{+0.022}_{-0.023} \,(\text{br.}).$$

The measured fraction is considerably smaller than the naive spin-counting prediction of 0.75. The predictions of the thermodynamical approach [34] and the string fragmentation approach [35], which both predict 2/3 for the fraction, and the BKL model [36, 37] prediction (≈ 0.66) are closer to, but still above, the measured value.

The measured $R_{u/d}$ and γ_s values agree with those obtained in DIS and in e^+e^- annihilations. The measured P_v^d value is smaller than, but consistent with, the previous measurements.

The fractions of c quarks hadronising as D^{*+} , D^0 , D^+ , D^+_s and Λ^+_c hadrons have been calculated in the accepted kinematic range. The measured open-charm fragmentation fractions are consistent with previous results although the measured $f(c \to D^{*+})$ is smaller

and $f(c \to \Lambda_c^+)$ is larger than those obtained in e^+e^- annihilations. About half of the difference in the $f(c \to D^{*+})$ values is due to the difference in the $f(c \to \Lambda_c^+)$ values.

These measurements generally support the hypothesis that fragmentation proceeds independently of the hard sub-process.

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	$R_{u/d}$
ZEUS (γp)	$1.100 \pm 0.078 (\text{stat.})^{+0.038}_{-0.061} (\text{syst.})^{+0.047}_{-0.049} (\text{br.})$
H1 (DIS) $[6]$	1.26 ± 0.20 (stat.) ± 0.11 (syst.) ± 0.04 (br. \oplus theory)
combined e^+e^- data [7]	$1.020 \pm 0.069 (\text{stat.} \oplus \text{syst.})^{+0.045}_{-0.047} (\text{br.})$

Table 1: The ratio of neutral to charged D-meson production rates, $R_{u/d}$.

	γ_s
ZEUS (γp)	$0.257 \pm 0.024 (\text{stat.})^{+0.013}_{-0.016} (\text{syst.})^{+0.078}_{-0.049} (\text{br.})$
ZEUS 96-97 [4]	$0.27 \pm 0.04 (\text{stat.})^{+0.02}_{-0.03} (\text{syst.}) \pm 0.07 (\text{br.})$
H1 (DIS) $[6]$	0.36 ± 0.10 (stat.) ± 0.01 (syst.) ± 0.08 (br. \oplus theory)
combined e^+e^- data [7]	$0.259 \pm 0.023 (\text{stat.} \oplus \text{syst.})^{+0.087}_{-0.052} (\text{br.})$

Table 2: The strangeness-suppression factor in charm fragmentation, γ_s .

	P_{v}^{d}
ZEUS (γp)	$0.566 \pm 0.025 (\text{stat.})^{+0.007}_{-0.022} (\text{syst.})^{+0.022}_{-0.023} (\text{br.})$
H1 (DIS) $[6]$	$0.693 \pm 0.045 (\text{stat.}) \pm 0.004 (\text{syst.}) \pm 0.009 (\text{br.} \oplus \text{theory})$
combined e^+e^- data [7]	$0.614 \pm 0.019 (\text{stat.} \oplus \text{syst.})^{+0.023}_{-0.025} (\text{br.})$

Table 3: The fraction of charged D mesons produced in a vector state, P_v^d .

	ZEUS (γn)	Combined	H1 (DIS)	
	$= (D \Lambda) > 28 C eV$	a^+a^- data $[7]$	[c]	
	$p_T(D,\Lambda_c) > 5.8 \mathrm{GeV}$	$e^{+}e^{-}$ data $[7]$	[၀]	
	$ \eta(D,\Lambda_c) < 1.6$			
	stat. syst. br.	stat. \oplus syst. br.	total	
$f(c \to D^+)$	$0.217 \pm 0.014 {}^{+0.013}_{-0.005} {}^{+0.014}_{-0.005}$	$0.226\ \pm 0.010\ ^{+0.016}_{-0.014}$	0.203 ± 0.026	
$f(c \rightarrow D^0)$	$0.523 \pm 0.021 \begin{array}{c} ^{+0.018}_{-0.017} \begin{array}{c} ^{+0.018}_{-0.022} \end{array}$	$0.557 \ \pm 0.023 \ \ {}^{+0.014}_{-0.013}$	0.560 ± 0.046	
$f(c \to D_s^+)$	$0.095 \pm 0.008 {}^{+0.005 +0.026}_{-0.005 -0.017}$	$0.101 \ \pm 0.009 \ ^{+0.034}_{-0.020}$	0.151 ± 0.055	
$f(c \to \Lambda_c^+)$	$0.144 \pm 0.022 \begin{array}{c} ^{+0.013} {}^{+0.037} \\ ^{-0.022} {}^{-0.025} \end{array}$	$0.076 \pm 0.007 \stackrel{+0.027}{_{-0.016}}$		
$f(c \to D^{*+})$	$0.200 \pm 0.009 {}^{+0.008}_{-0.006} {}^{+0.008}_{-0.012}$	$0.238 \pm 0.007 \stackrel{+0.003}{_{-0.003}}$	0.263 ± 0.032	

Table 4: The fractions of c quarks hadronising as a particular charm hadron, $f(c \to D, \Lambda_c)$. The fractions are shown for the D^+ , D^0 , D_s^+ and Λ_c^+ charm ground states and for the D^{*+} state.

	Peterson	Bowler	Cluster model		
	(Pythia)	(Pythia)	(HERWIG)		
$R_{u/d}$	$0.99^{+0.02}_{-0.00}$	$0.99^{+0.02}_{-0.00}$	$1.00\substack{+0.01\\-0.00}$		
γ_s	$1.04_{-0.07}^{+0.04}$	$1.00\substack{+0.05\\-0.04}$	$1.18\substack{+0.07\\-0.05}$		
$P^d_{\rm v}$	1.00 ± 0.02	$0.97\substack{+0.01 \\ -0.00}$	$0.96\substack{+0.02\\-0.01}$		
$f(c \to D^+)$	$1.00^{+0.02}_{-0.01}$	$1.02\pm^{+0.01}_{-0.02}$	$0.99\substack{+0.01\\-0.03}$		
$f(c \rightarrow D^0)$	0.99 ± 0.01	0.98 ± 0.01	$0.96\substack{+0.00\\-0.02}$		
$f(c \to D_s^+)$	$1.03\substack{+0.03\\-0.06}$	$1.00\substack{+0.04\\-0.03}$	$1.15_{-0.05}^{+0.06}$		
$f(c \to \Lambda_c^+)$	$1.01_{-0.05}^{+0.02}$	$1.08^{+0.03}_{-0.02}$	$1.46_{-0.09}^{+0.03}$		
$f(c \to D^{*+})$	$1.00^{+0.02}_{-0.03}$	$0.96^{+0.00}_{-0.02}$	$0.93_{-0.02}^{+0.01}$		

Table 5: The estimates of extrapolation factors which correct charm fragmentation ratios and fractions measured in the accepted $p_T(D, \Lambda_c)$ and $\eta(D, \Lambda_c)$ region to the full phase space. For further details, see text.

	total	δ_1	δ_2	δ_3	δ_4	δ_5	δ_6	δ_7
	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)
$\sigma^{\mathrm{untag}}(D^0)$	$^{+5.5}_{-5.6}$	$^{+2.8}_{-0.6}$	$^{+1.8}_{-3.4}$	$^{+1.1}_{-1.4}$	$^{+1.3}_{-1.2}$	$^{+3.4}_{-3.4}$	$^{+2.2}_{-2.2}$	
$\sigma^{ m tag}(D^0)$	$^{+4.0}_{-3.7}$	$^{+2.5}_{-1.2}$	$^{+1.1}_{-2.1}$	$^{+1.4}_{-1.3}$	$^{+1.4}_{-1.1}$	$^{+0.7}_{-0.4}$	$^{+2.2}_{-2.2}$	
$\sigma^{\rm add}(D^{*\pm})$	$^{+8.4}_{-3.6}$	$^{+5.8}_{-0.4}$	$^{+1.0}_{-1.9}$	$+3.3 \\ -1.6$	$^{+1.8}_{-1.4}$	$^{+4.2}_{-0.1}$	$^{+2.2}_{-2.2}$	
$\sigma^{\rm kin}(D^{*\pm})$	$^{+4.6}_{-3.6}$	$^{+3.1}_{-1.0}$	$^{+1.1}_{-2.0}$	$^{+1.6}_{-1.3}$	$^{+1.4}_{-1.1}$	$^{+1.1}_{-0.3}$	$^{+2.2}_{-2.2}$	
$\sigma(D^{\pm})$	$^{+8.7}_{-4.5}$	$^{+4.5}_{-0.3}$	$+1.8 \\ -3.3$	$^{+1.0}_{-1.6}$	$^{+1.3}_{-1.0}$	$^{+6.7}_{-0.6}$	$+2.3 \\ -2.3$	
$\sigma(D_s^{\pm})$	$^{+8.3}_{-8.5}$	$^{+6.0}_{-0.0}$	$+3.9 \\ -7.0$	$^{+1.4}_{-1.3}$	$^{+1.8}_{-1.0}$	$^{+2.9}_{-4.0}$	$^{+2.2}_{-2.2}$	
$\sigma(\Lambda_c^{\pm})$	$^{+15.1}_{-18.3}$	$^{+13.2}_{-0.6}$	$+3.1 \\ -5.6$	$^{+4.8}_{-1.5}$	$+2.2 \\ -3.0$	$+3.3 \\ -16.9$	$+2.3 \\ -2.3$	
$R_{u/d}$	$^{+3.5}_{-5.5}$	$^{+0.0}_{-0.9}$	$^{+0.4}_{-0.7}$	$^{+0.6}_{-0.6}$	$^{+0.1}_{-0.3}$	$^{+3.4}_{-5.4}$	$^{+0.2}_{-0.2}$	
γ_s	$^{+5.0}_{-6.3}$	$^{+2.4}_{-0.2}$	$^{+2.4}_{-4.1}$	$^{+0.9}_{-0.8}$	$^{+0.8}_{-0.0}$	$^{+3.5}_{-4.7}$	$^{+0.1}_{-0.1}$	
$P^d_{ m v}$	$^{+1.2}_{-3.9}$	$^{+0.4}_{-1.0}$	$^{+0.8}_{-0.5}$	$^{+0.5}_{-0.1}$	$^{+0.1}_{-0.1}$	$^{+0.6}_{-3.7}$	$^{+0.1}_{-0.1}$	
$\sigma_{ m gs}$	$^{+6.8}_{-5.7}$	$^{+5.3}_{-0.4}$	$^{+2.0}_{-3.8}$	$^{+1.8}_{-1.0}$	$^{+1.2}_{-1.1}$	$^{+1.9}_{-3.1}$	$^{+2.2}_{-2.2}$	$^{+0.7}_{-0.7}$
$f(c \to D^+)$	$^{+6.1}_{-2.1}$	$^{+0.3}_{-0.8}$	$^{+0.7}_{-0.4}$	$^{+0.2}_{-1.0}$	$^{+0.6}_{-0.3}$	$^{+6.0}_{-1.5}$	$^{+0.1}_{-0.1}$	$^{+0.7}_{-0.7}$
$f(c \to D^0)$	$^{+3.4}_{-3.2}$	$^{+0.2}_{-2.2}$	$^{+0.9}_{-0.5}$	$^{+0.3}_{-0.8}$	$^{+0.5}_{-0.4}$	$^{+3.1}_{-2.1}$	$^{+0.1}_{-0.1}$	$^{+0.7}_{-0.7}$
$f(c \to D_s^+)$	$^{+4.9}_{-5.4}$	$^{+0.8}_{-0.2}$	$^{+1.9}_{-3.3}$	$^{+0.3}_{-0.8}$	$^{+1.2}_{-0.3}$	$^{+4.1}_{-4.1}$	$^{+0.1}_{-0.1}$	$^{+0.7}_{-0.7}$
$\overline{f(c \to \Lambda_c^+)}$	$+9.1 \\ -15.1$	$+7.4 \\ -0.3$	$^{+1.2}_{-1.9}$	$+3.5 \\ -0.7$	$+1.7 \\ -2.9$	$+3.1 \\ -14.6$	$+0.2 \\ -0.2$	$+0.7 \\ -0.7$
$f(c \to D^{*+})$	$+3.9 \\ -3.2$	$+0.4 \\ -2.2$	$^{+1.9}_{-1.0}$	$^{+0.6}_{-0.5}$	$^{+0.7}_{-0.5}$	$+3.1 \\ -1.9$	$^{+0.1}_{-0.1}$	$^{+0.7}_{-0.7}$

Table 6: The total and δ_1 - δ_7 (see text) systematic uncertainties for the charm hadron cross sections and charm fragmentation ratios and fractions.



Figure 1: The $M(K\pi)$ distributions (dots) for (a) the D^0/\bar{D}^0 candidates without ΔM tag, obtained after the reflection subtraction (see text), and for (b) the D^0/\bar{D}^0 candidates with ΔM tag. The solid curves represent a fit to the sum of a modified Gaussian function and a background function.



Figure 2: The distribution of the mass difference, $\Delta M = M(K\pi\pi_s) - M(K\pi)$, for the "additional" $D^{*\pm}$ candidates (dots). The histogram shows the ΔM distribution for wrong-charge combinations. The shaded band shows the signal range in which the wrong-charge background subtraction was performed.



Figure 3: The $M(K\pi\pi)$ distribution for the D^{\pm} candidates (dots). The solid curve represents a fit to the sum of a modified Gaussian function and a linear background function.



Figure 4: The $M(KK\pi)$ distribution for the D_s^{\pm} candidates (dots). The solid curve represents a fit to the sum of two modified Gaussian functions and an exponential background function.



Figure 5: The $M(Kp\pi)$ distribution for the $\Lambda_c^+/\bar{\Lambda}_c^-$ candidates (dots). The solid curve represents a fit to the sum of a modified Gaussian function and a linear background function.