

Comp-Exe 5: Straight line trajectory fit

Physics example: A muon track is measured in four layers of streamer tube detectors at x positions of 4., 5., 6. and 7. (in cm), with a measurement precision for y of 0.5 cm. The goal is to determine its trajectory, assuming it to be a straight line.

Macro StraightLineFit.C, accessible at
<http://www.desy.de/~obehnke/stat/gean10/StraightLineFit.C>

fits a straight line track trajectory through four measured points.

- Steering parameters in the macro:
 - $xmin, xmax$ = Interval of the trajectory displayed
- Output:
 - Histogram *data* (it's of the type TGraphErrors)
 - Plots are drawn of the
 - * fitted histogram with error bands
 - * error ellipse of the two fitparameters

Tasks:

- Run the macro as it is by `.x StraightLineFit.C` and fill the fit results for $p0, p1$, their errors and correlation into the table below
- Precision of trajectory: Evaluate (by eye) from the shown error bands at which point roughly the trajectory is known best and with which precision (fill the results in the table below)
- Precision of extrapolated trajectory: Evaluate the precision of the extrapolated trajectory at $x = 100$ (Hint: Change $xmax$ to large value and run the macro again)

- d) Effect of shift of x coordinate origin: Shift all four $xVal$ points in the macro (simply by overwriting by hand) by a constant value -5.5 , set $xmin = -4$. and $xmax = 4$. and run the macro again. Fill the fit results in the table. Can you explain why the correlation of p_0 and p_1 has changed?
- e) Apply a very precise vertex constraint at the origin: Change N to 5 and add a new first point to the measurement points list with $xVal = 0.0$, $xErr = 0.0$, $yVal = 0.0$ and $yErr = 0.0001$ (just by hand). Run the macro again and write down the fitted results in the table. How much are the parameter errors reduced by adding this extra point?

| | Straight line fit trough four points |
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| Task a) | $p_0 =$ $p_1 =$ corr = |
| Task b) | x -best precision = y -error = |
| Task c) | y -error($x = 100$) = |
| Task d) | Shifting all x values by -5.5 : $p_0 =$ $p_1 =$ corr = |
| Task e) | Adding vertex constraint at $x = 0$: $p_0 =$ $p_1 =$ corr = |