

# From HERA to the LHC II

H. Jung (DESY)

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- Yesterday: HERA and the structure of the proton
- TODAY:
  - from inclusive x-section measurements to detailed investigations of QCD
    - measurements of hadronic final states:
      - lead to a detailed understanding of QCD
  - QCD is challenging
    - implications and applications for LHC
    - PDFs, multiparton interactions, etc

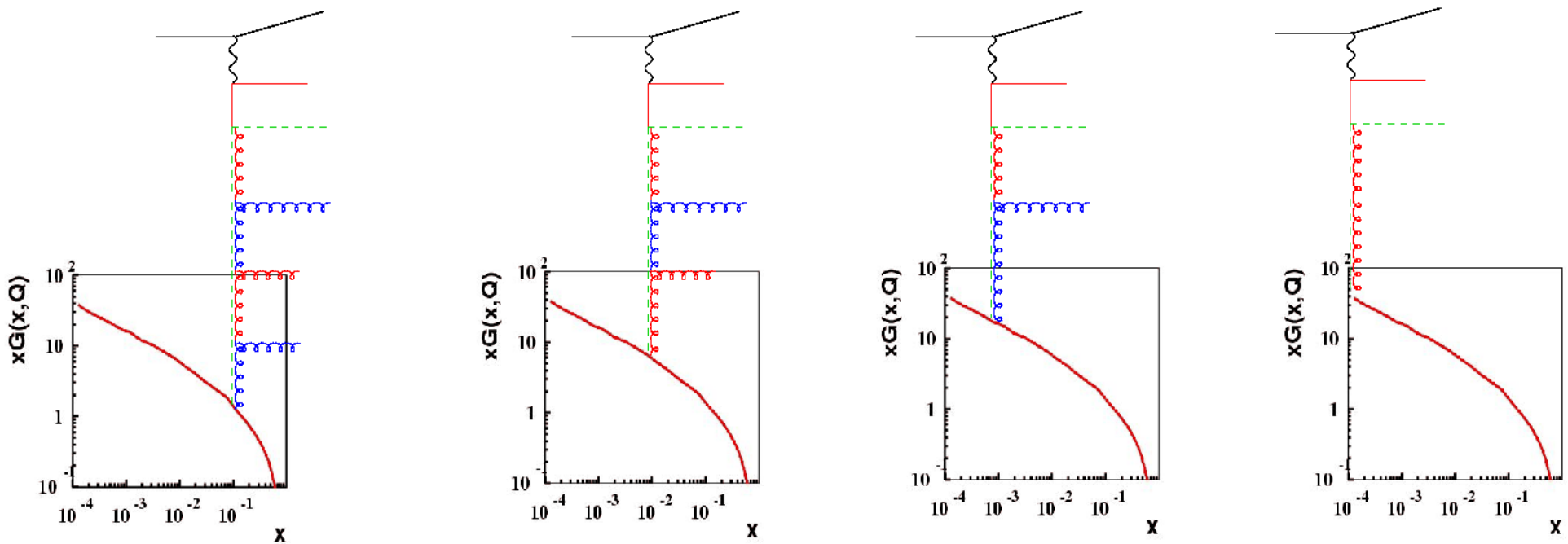
lectures based on lecture series:

"QCD & collider physics" H.Jung, J. Bartels University HH, 2005 -2007

Contributions to "HERA and the LHC" workshops: [www,desy.de/~heralhc](http://www.desy.de/~heralhc)

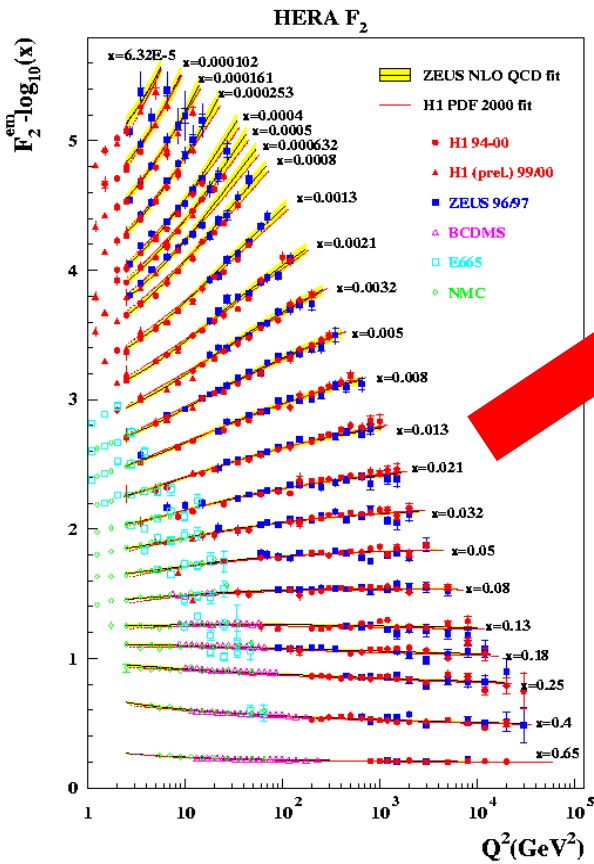
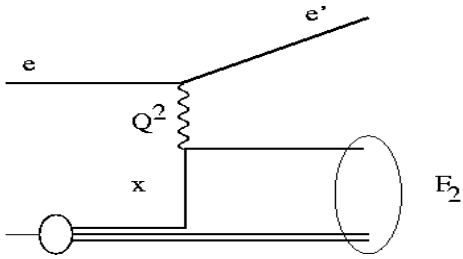
# DGLAP evolution equation... again...

- for fixed  $x$  and  $Q^2$  chains with different branchings contribute
- iterative procedure, **spacelike** parton showering

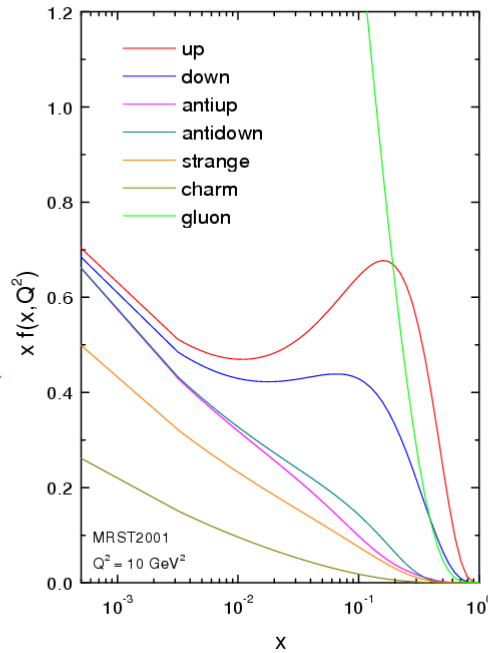


$$f(x, t) = \sum_{k=1}^{\infty} f_k(x_k, t_k) + f_0(x, t_0) \Delta_s(t)$$

# From HERA $F_2$ to Higgs at LHC



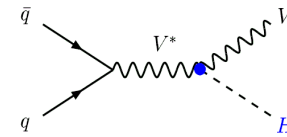
total x-section,  $F_2$



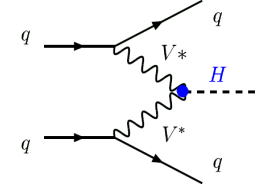
extract parton densities

from J. Stirling

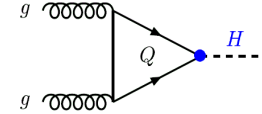
Higgs-strahlung



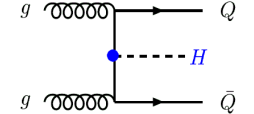
Vector boson fusion



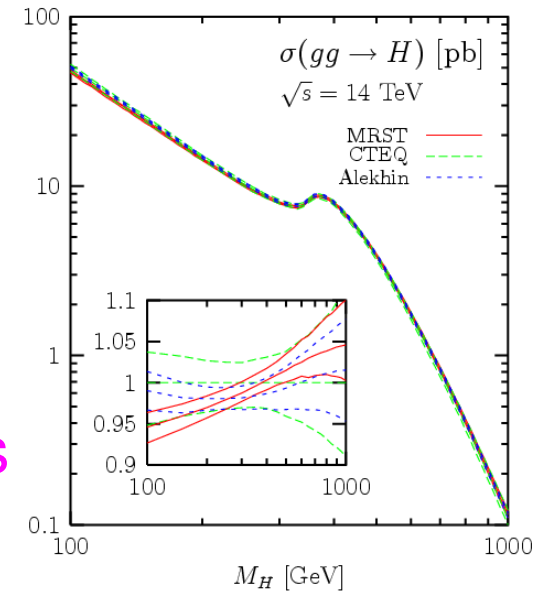
gluon-gluon fusion



in associated with  $Q\bar{Q}$

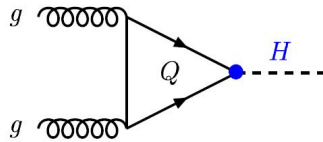


calculate Higgs prod



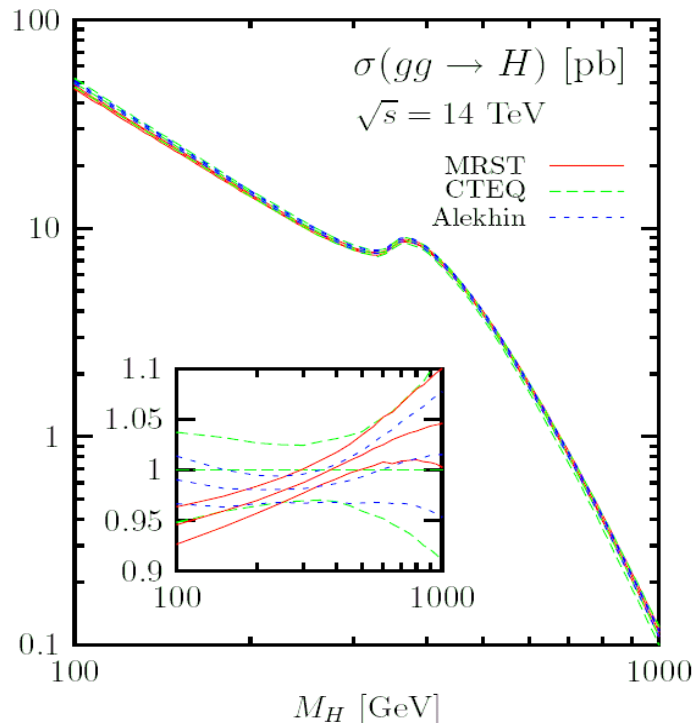
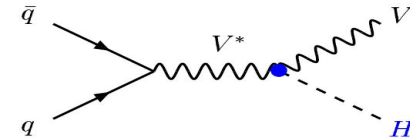
# PDF uncertainty for Higgs prod.

gluon-gluon fusion

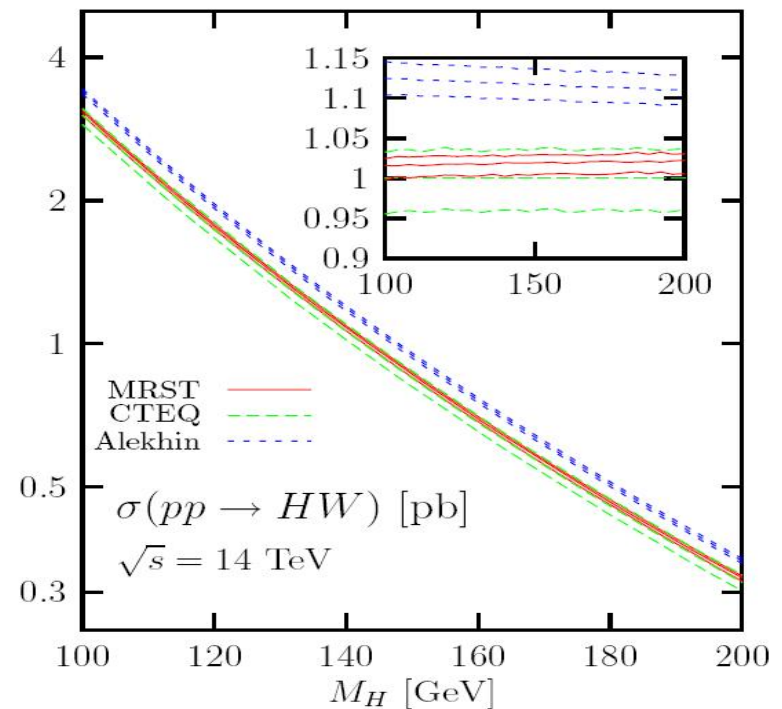


from Djouadi & Ferrag

Higgs-strahlung



Gluon induced... ~ 10 %

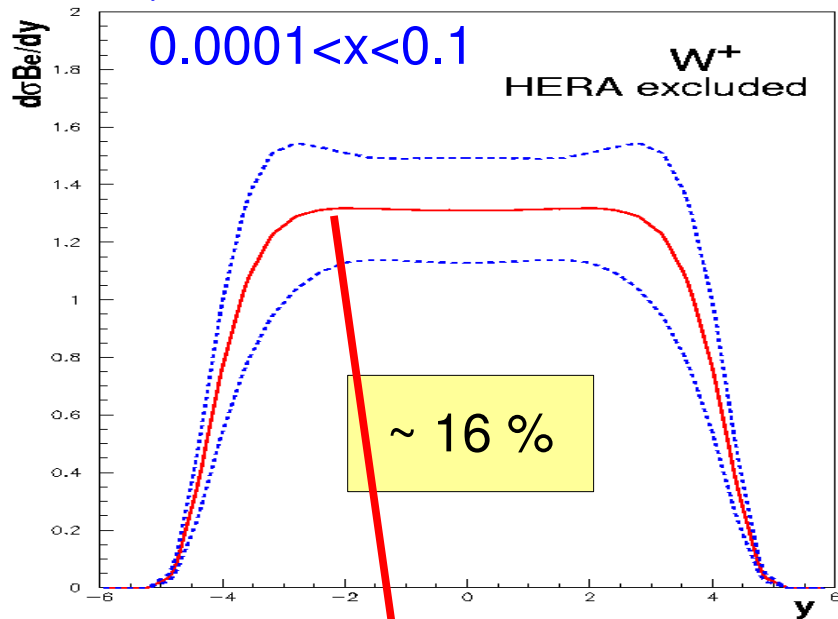


Quark induced ~ 10 % difference

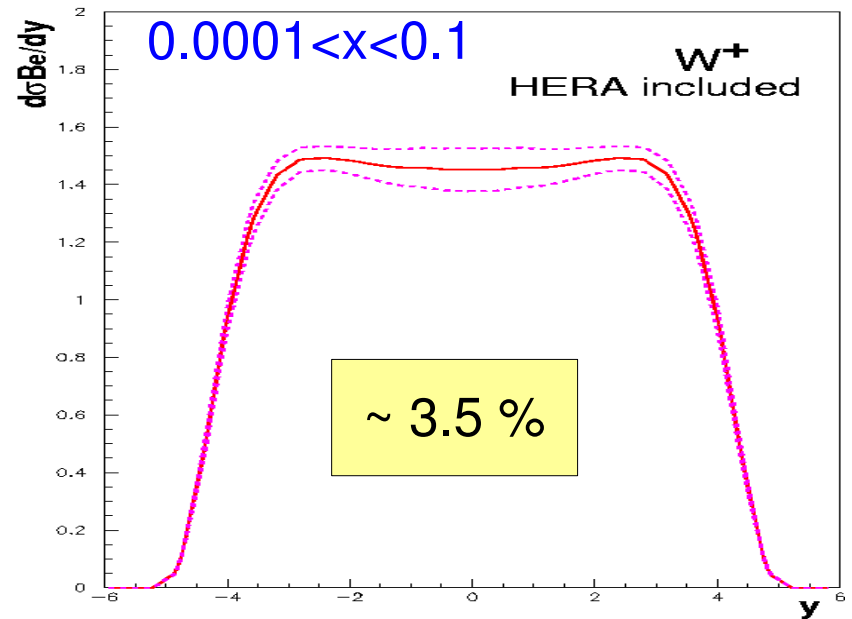
**In 2004:** PDFs did not agree within respective errors (J. Stirling) !!!!!

# Does LHC really need HERA ?

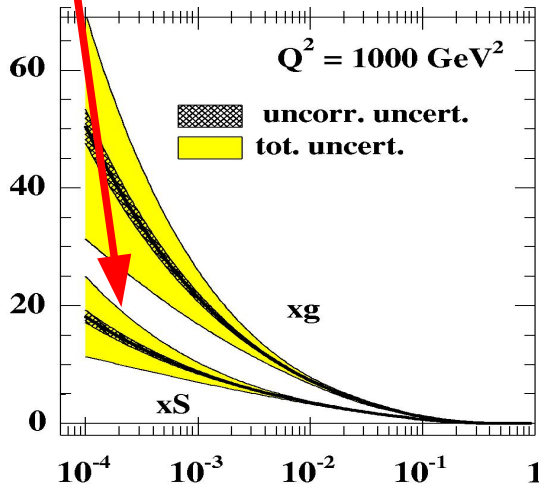
- W prod. at LHC without HERA:



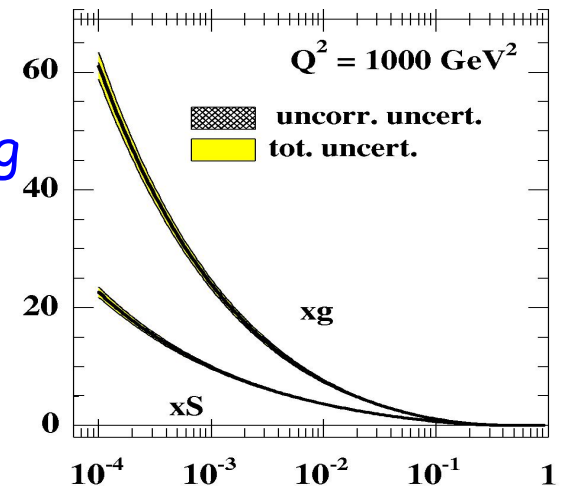
- W prod. at LHC including HERA



- PDFs without HERA:



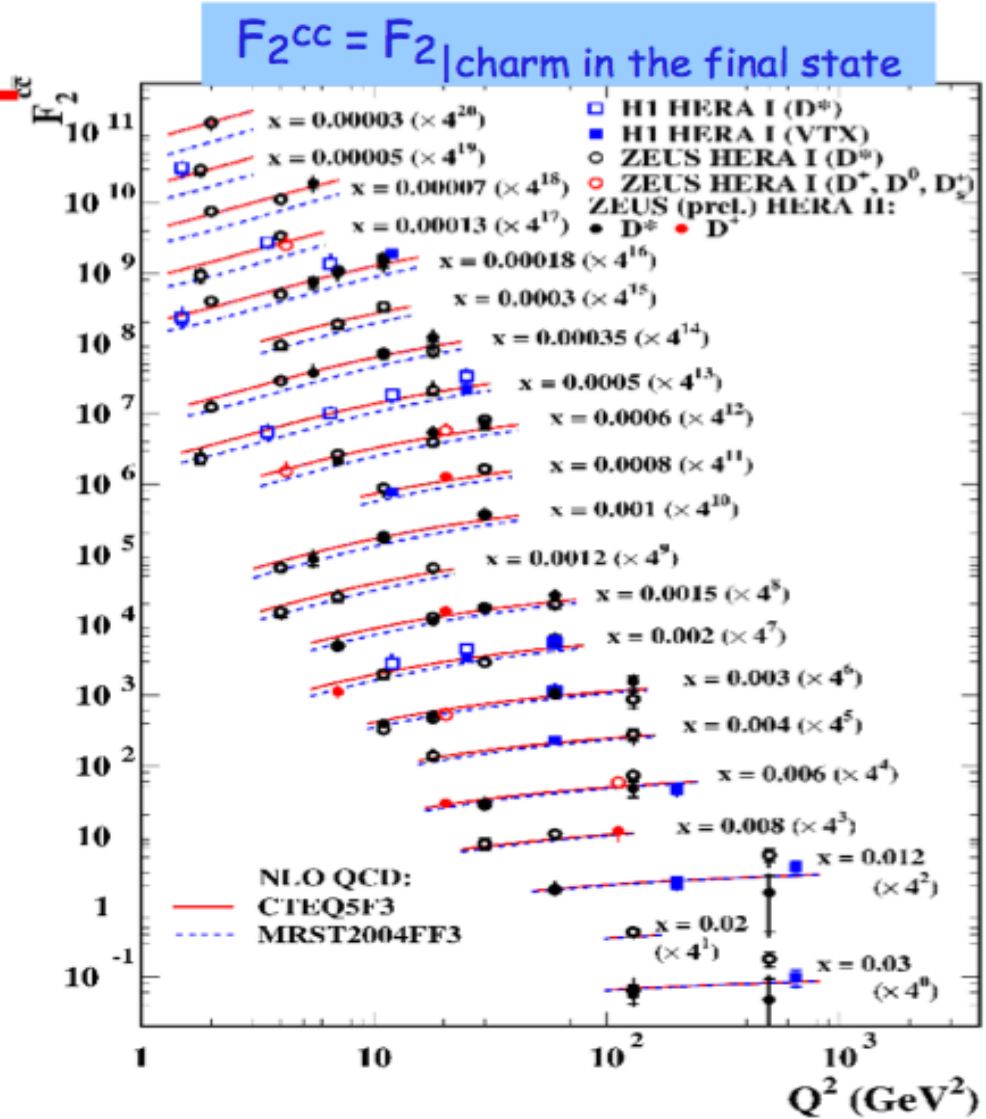
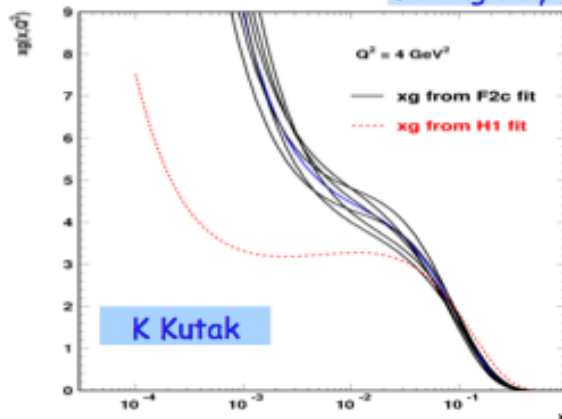
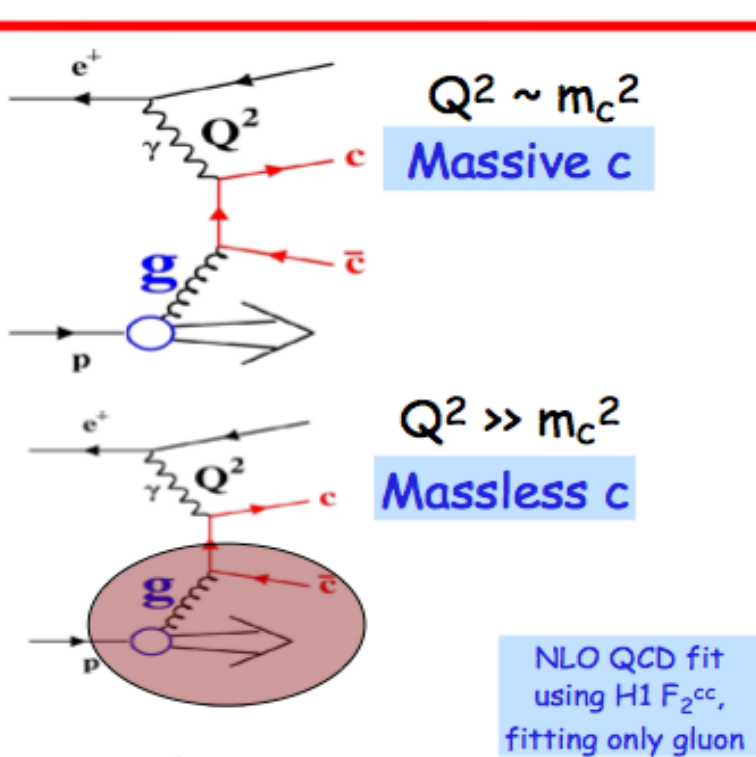
- PDFs including HERA:



# Heavy Flavor measurements

from O. Behnke, EPS07

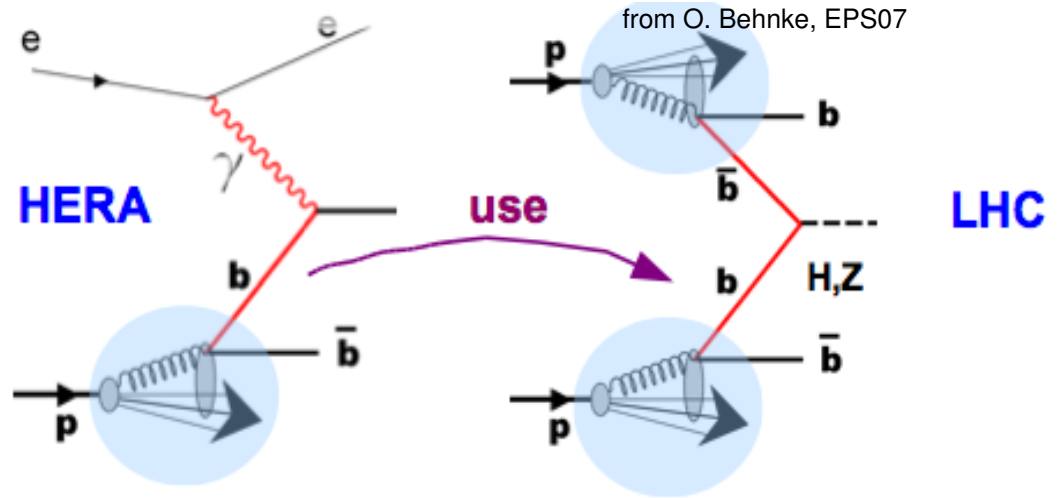
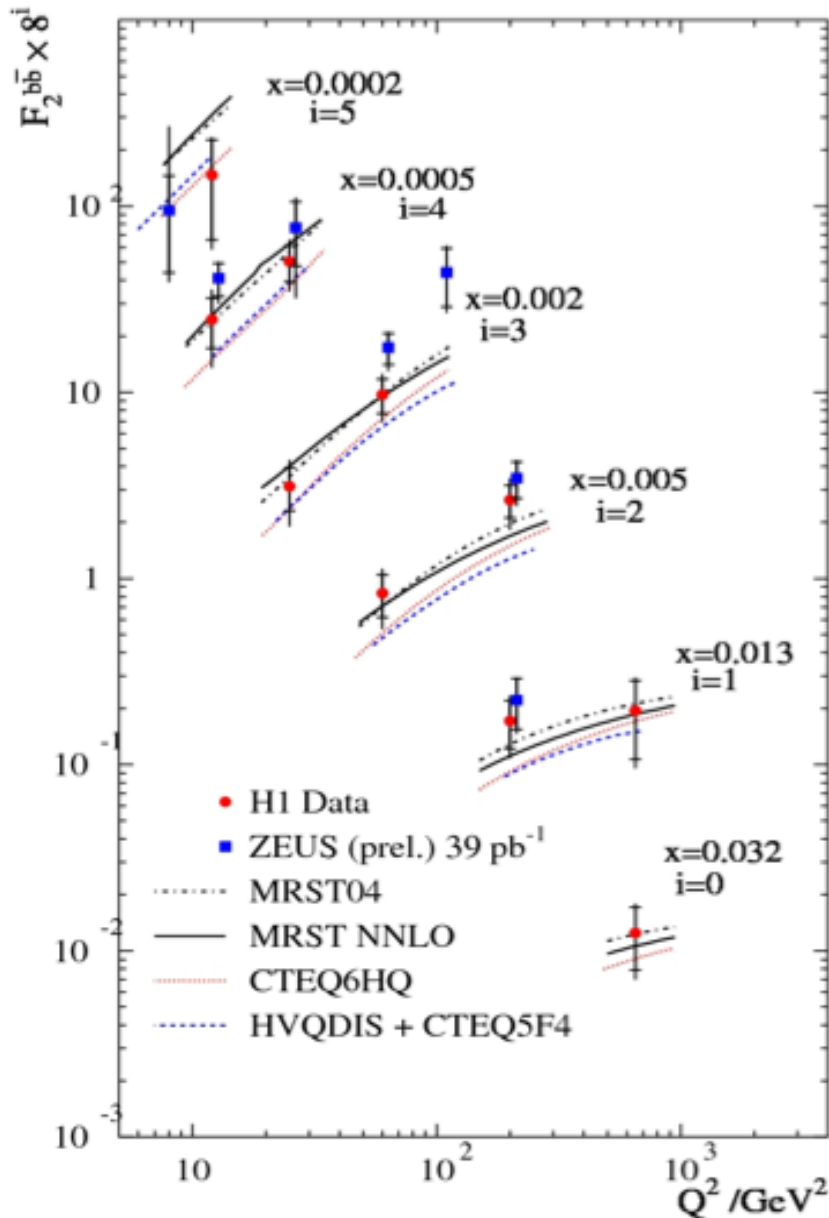
## Gluon via charm @ HERA



→  $F_2^{cc}$  data can constrain the proton gluon density at small  $x$

# Heavy Flavor measurements

## Beauty contribution to F2



- ➔ 'Beautiful' new HERA II data
- ➔ Astonishing spread of model predictions!

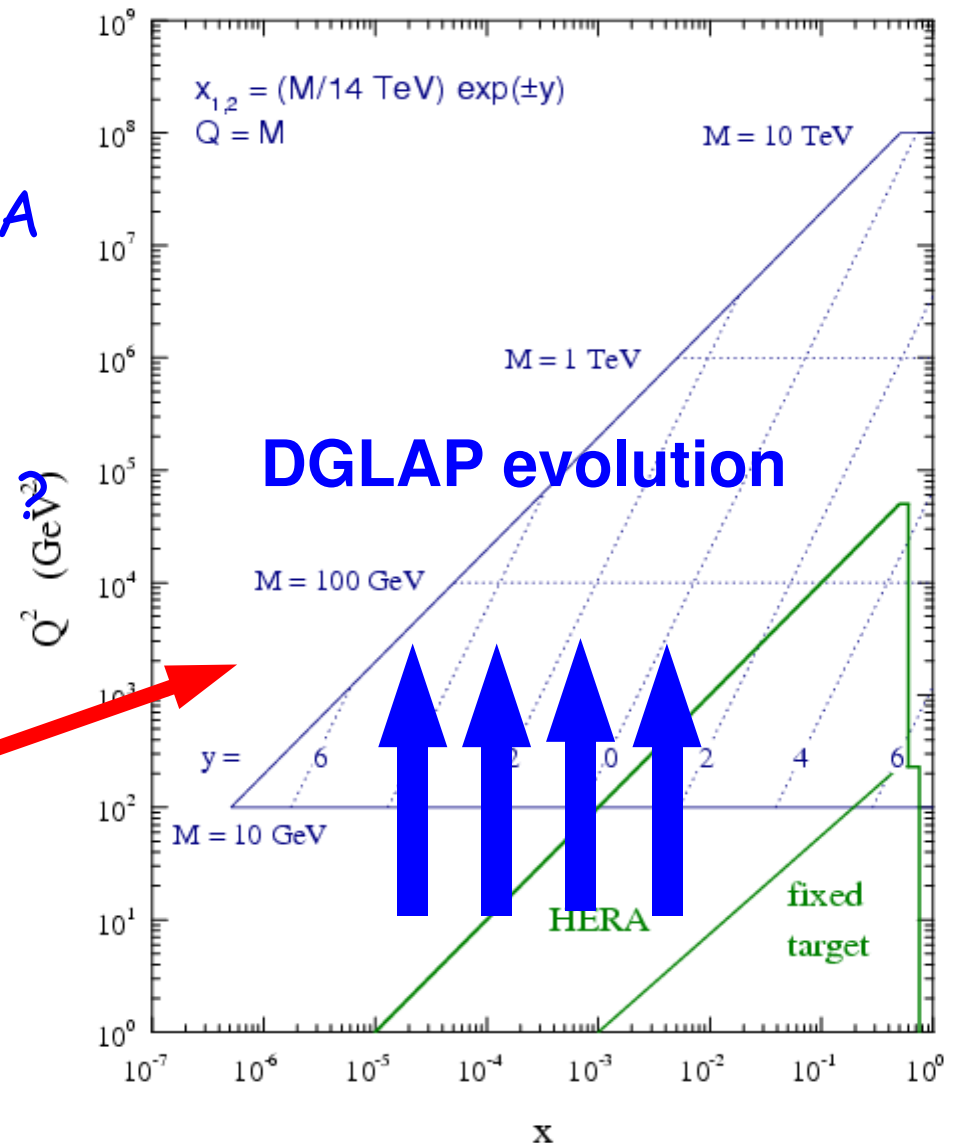


# Is DGLAP all ??????

from J. Stirling

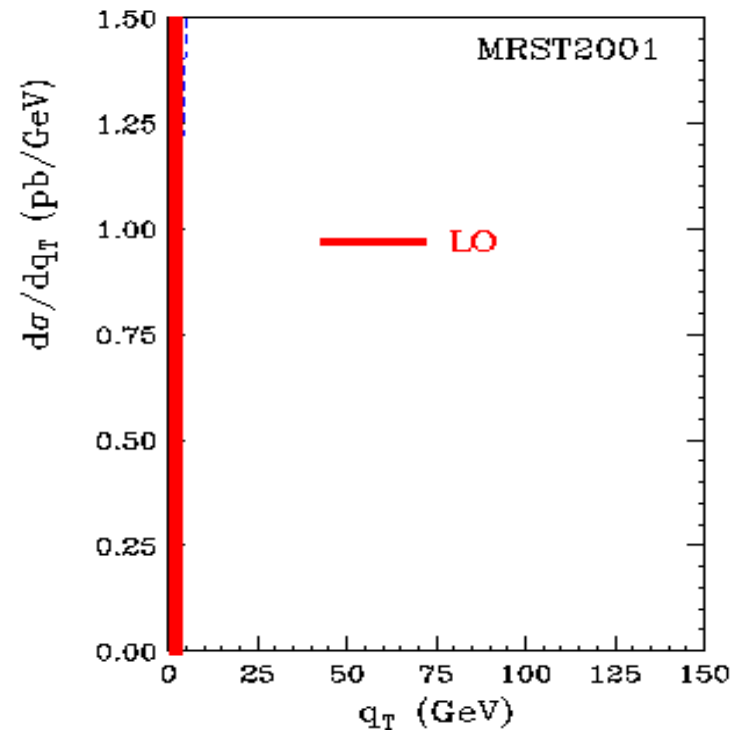
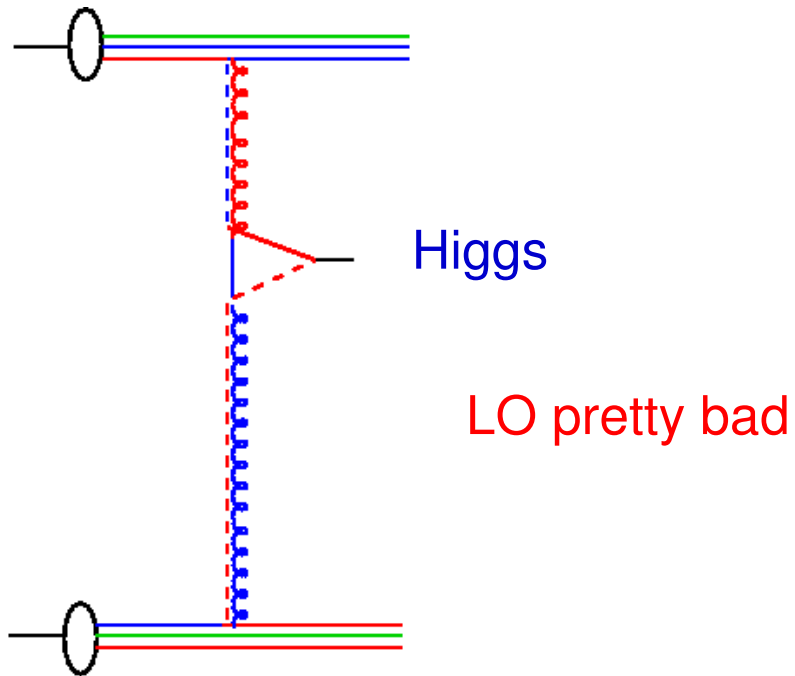
## LHC parton kinematics

- Can we just assume DGLAP
- is ok also at highest energies ?
- remember surprises from HERA
- Is factorization valid ?
- What about  $k_T$ -factorization ?
- What about non-linear effects

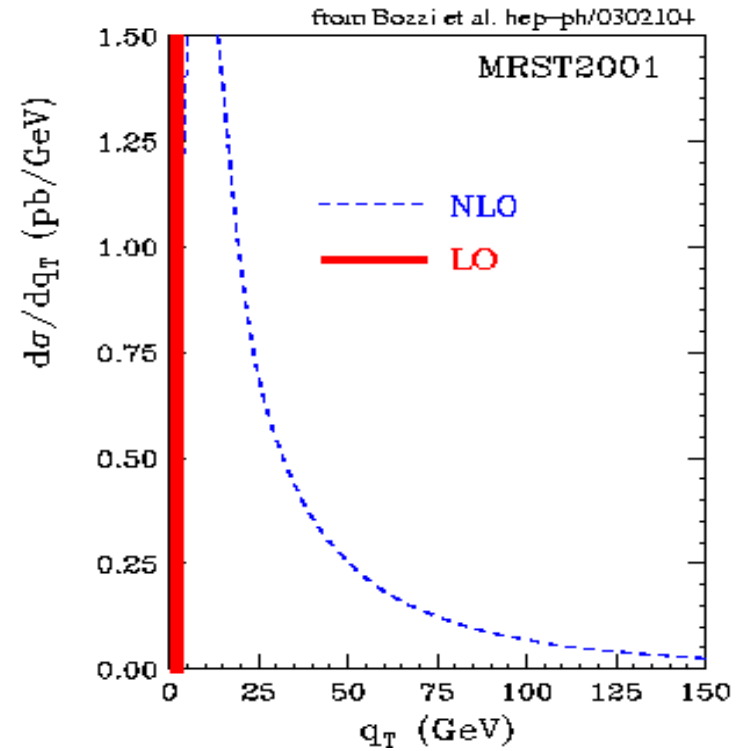
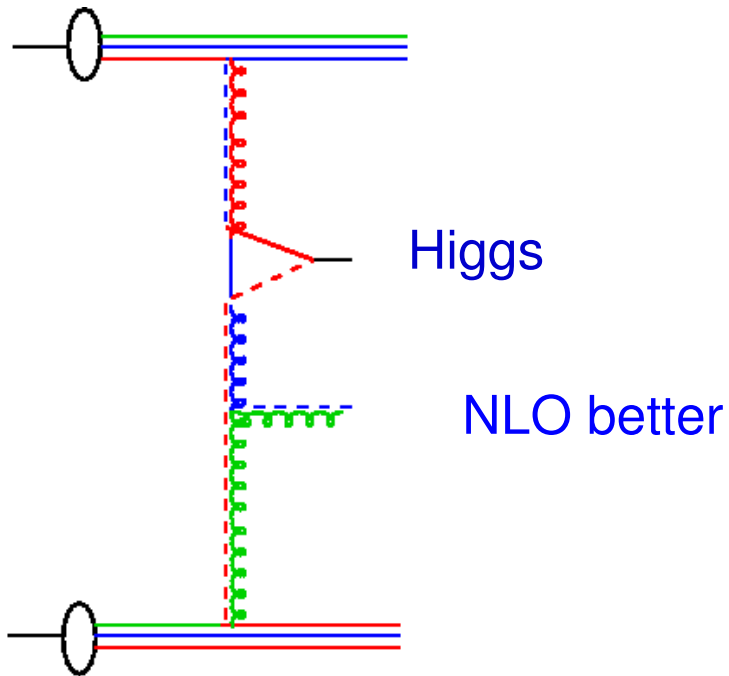


Is NLO (or NNLO) DGLAP sufficient at small  $x$ ?  
 Are higher orders important ?

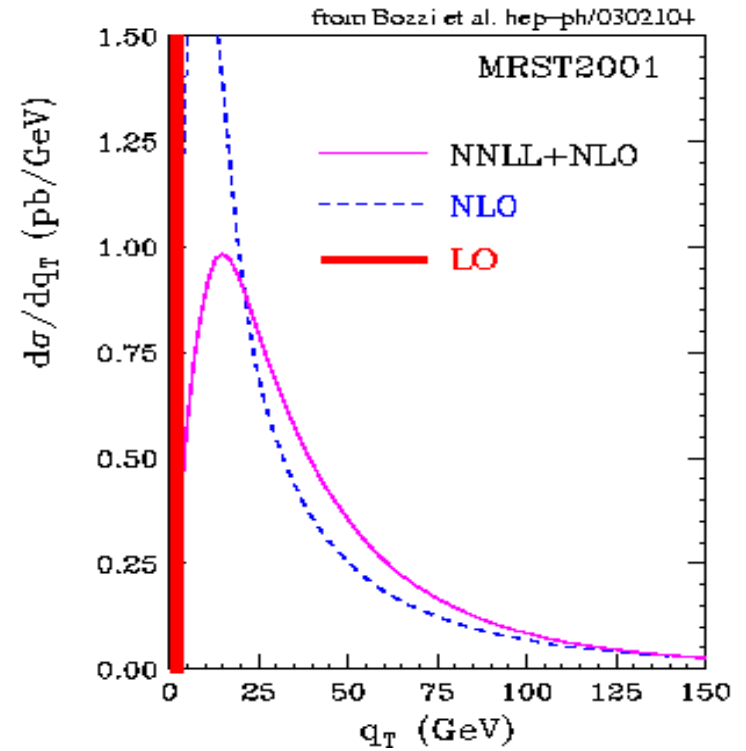
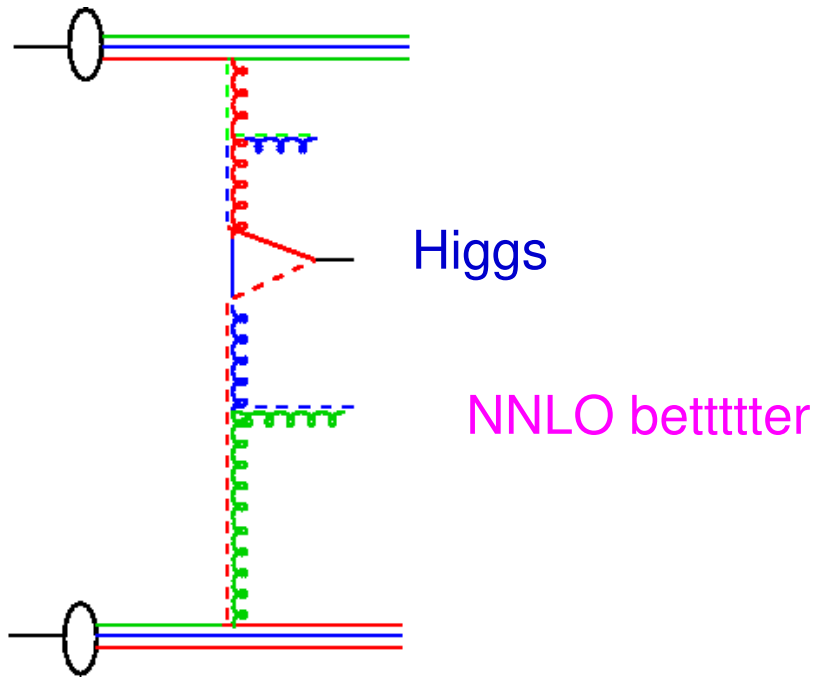
# $k_t$ effects at HERA and LHC



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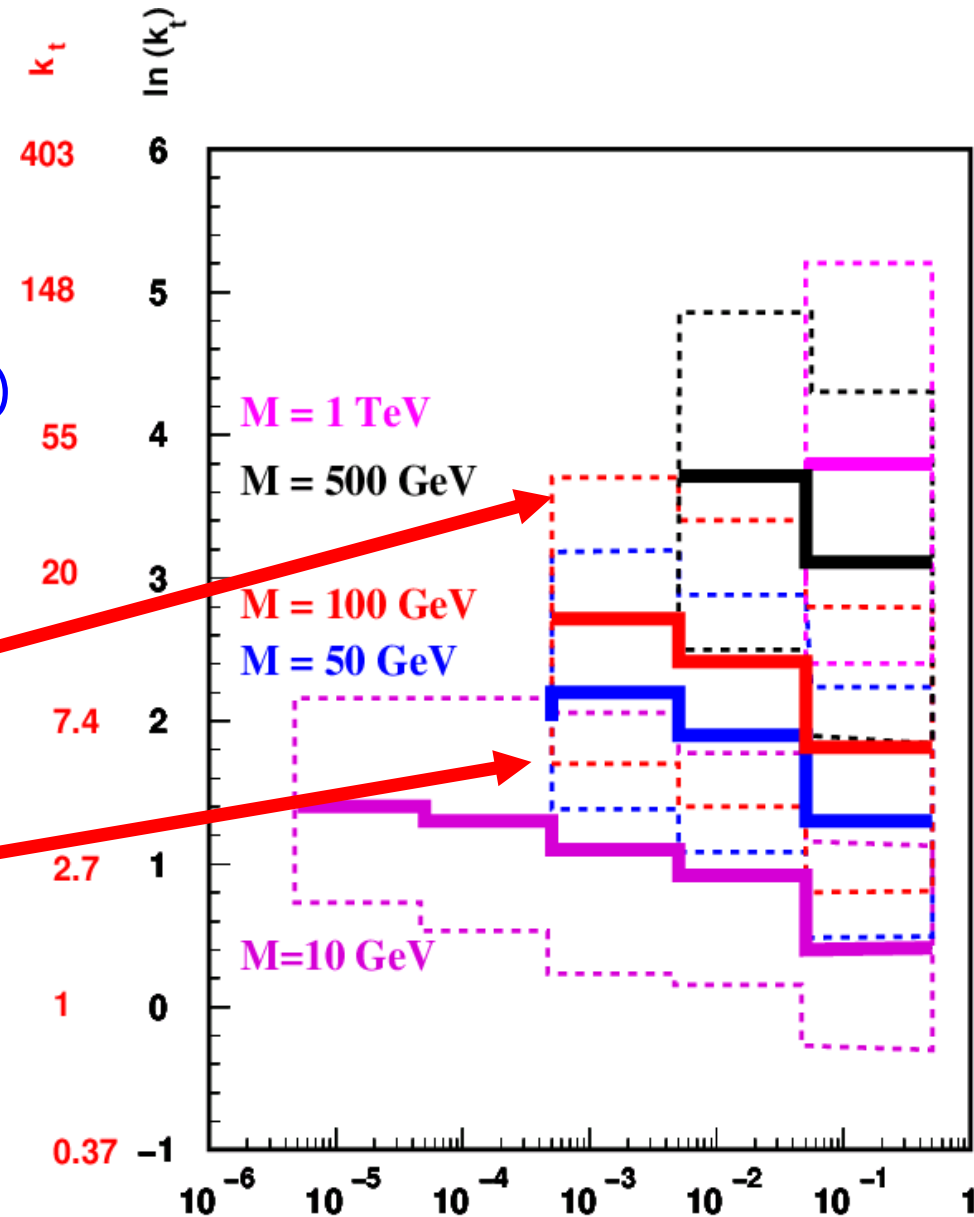
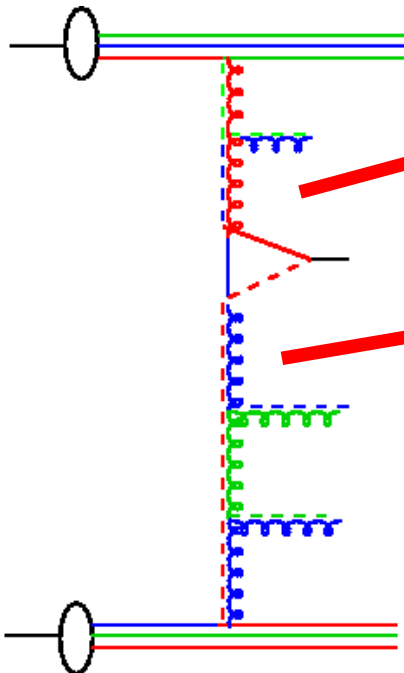
# $k_T$ effects at HERA and LHC



# Parton Density Functions and all that

- collinear PDFs
- uPDFs (single and double unintegrated)

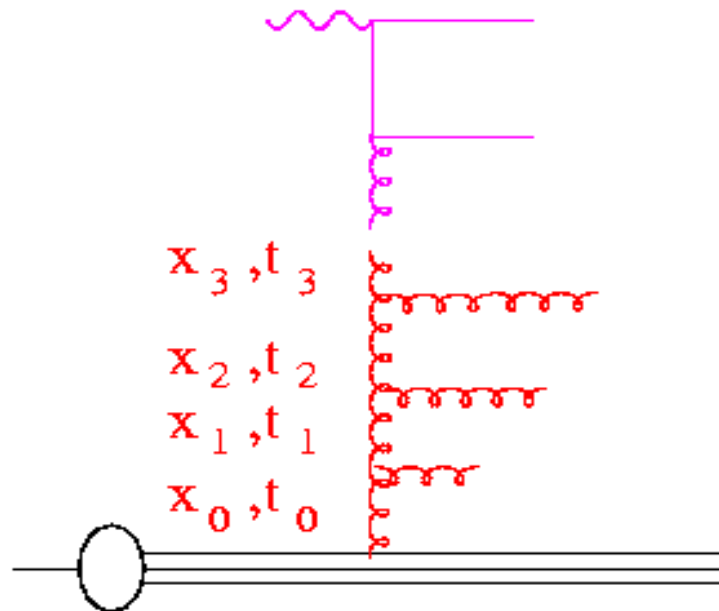
Higgs production et al



# Approximations so far ....

- Only inclusive quantities were considered:
  - nothing was said about "real" emissions of gluons or quarks although implicitly assumed....
  - in deriving DGLAP splitting functions we assumed:  $\hat{t} \ll \hat{s}$

- and also in the small  $t$  limit:  $\hat{t} \sim \frac{-k_t^2}{1-z}$



- neglect  $t$  in previous branchings
  - $t_0 \ll t_1 \ll t_2 \ll t_3 \dots \ll \mu^2$
  - strong ordering condition
  - strong ordering: neglect all kinematics of previous branchings...
- ordering in  $x$ 
  - $x_0 > x_1 > x_2 > x_3$

# Kinematic regions: new evolution ..

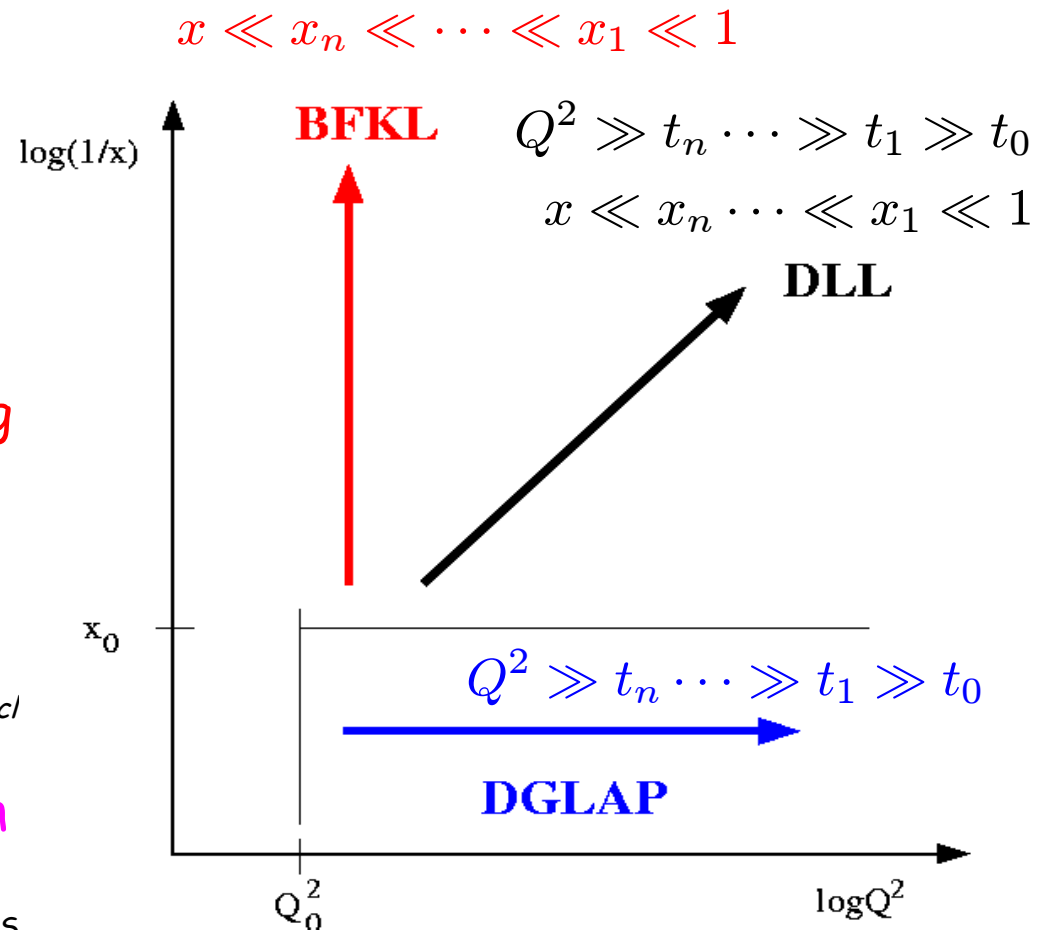
- DGLAP:  
strong ordering in  $t$
- DLL:  
strong ordering in  $t$   
strong ordering in  $x$
- what happens if strong  $t$  ordering relaxed?

- **Balitskii Fadin Kuraev Lipatov evolution**

E. Kuraev, L. Lipatov, V. Fadin, *Sov. Phys. JETP* 44 (1976), 443., E. Kuraev, L. Lipatov, V. Fadin, *Sov. Phys. JETP* 45, (1977), 199., Y. Balitskii, L. Lipatov, *Sov. J. Nucl. Phys.* 28, (1978), 822.

- **Catani Ciafaloni Fiorani Marchesini evolution**

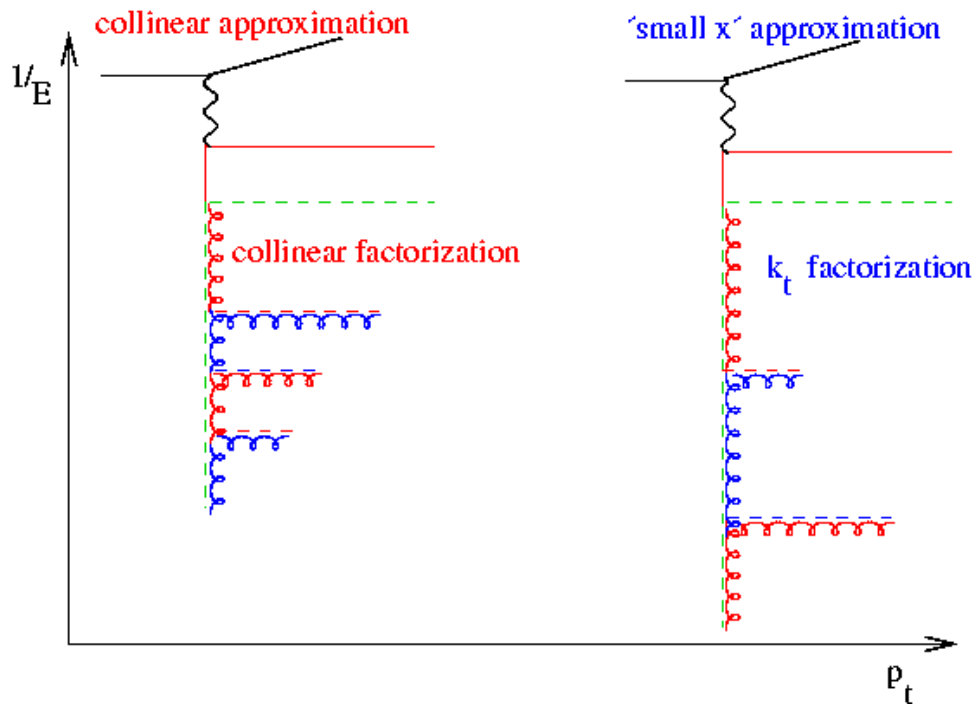
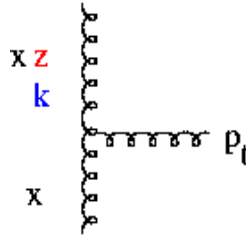
M. Ciafaloni, *Nucl. Phys. B* 296, (1988), 49. S. Catani, F. Fiorani, G. Marchesini, *Phys. Lett. B* 234, (1990), 339, S. Catani, F. Fiorani, G. Marchesini, *Nucl. Phys. B* 336, (1990), 18, G. Marchesini, *Nucl. Phys. B* 445, (1995), 49.



# Approximations to higher orders ...

gluon bremsstrahlung

$$\sim \frac{1}{k^2} \left( \frac{1}{z} + \dots \right)$$



Dokshitzer Gribov Lipatov Altarelli Parisi

- collinear singularities factorized in pdf  $Q^2 \sim k^2$ , or  $k_t^2$  or ?
  - evolution in
- $$\sigma = \sigma_0 \int \frac{dz}{z} C^a \left( \frac{x}{z} \right) f_a(z, Q^2)$$

Balitski Fadin Kuraev Lipatov

- $k_t$  dependent pdf  $\rightarrow$  unintegrated pdf
  - evolution in  $x$
- $$\sigma = \int \frac{dz}{z} d^2 k_t \hat{\sigma} \left( \frac{x}{z}, k_t \right) \mathcal{F}(z, k_t)$$



# The problem of asymptotia

DGLAP is great  
at highest  $Q^2 \rightarrow \infty$   
for inclusive quantities

BUT has problems

- heavy quarks
- jets
- particle spectra
- small  $x$  processes

BFKL is great  
at small  $x \rightarrow 0$   
or highest  $W \rightarrow \infty$   
for inclusive quantities

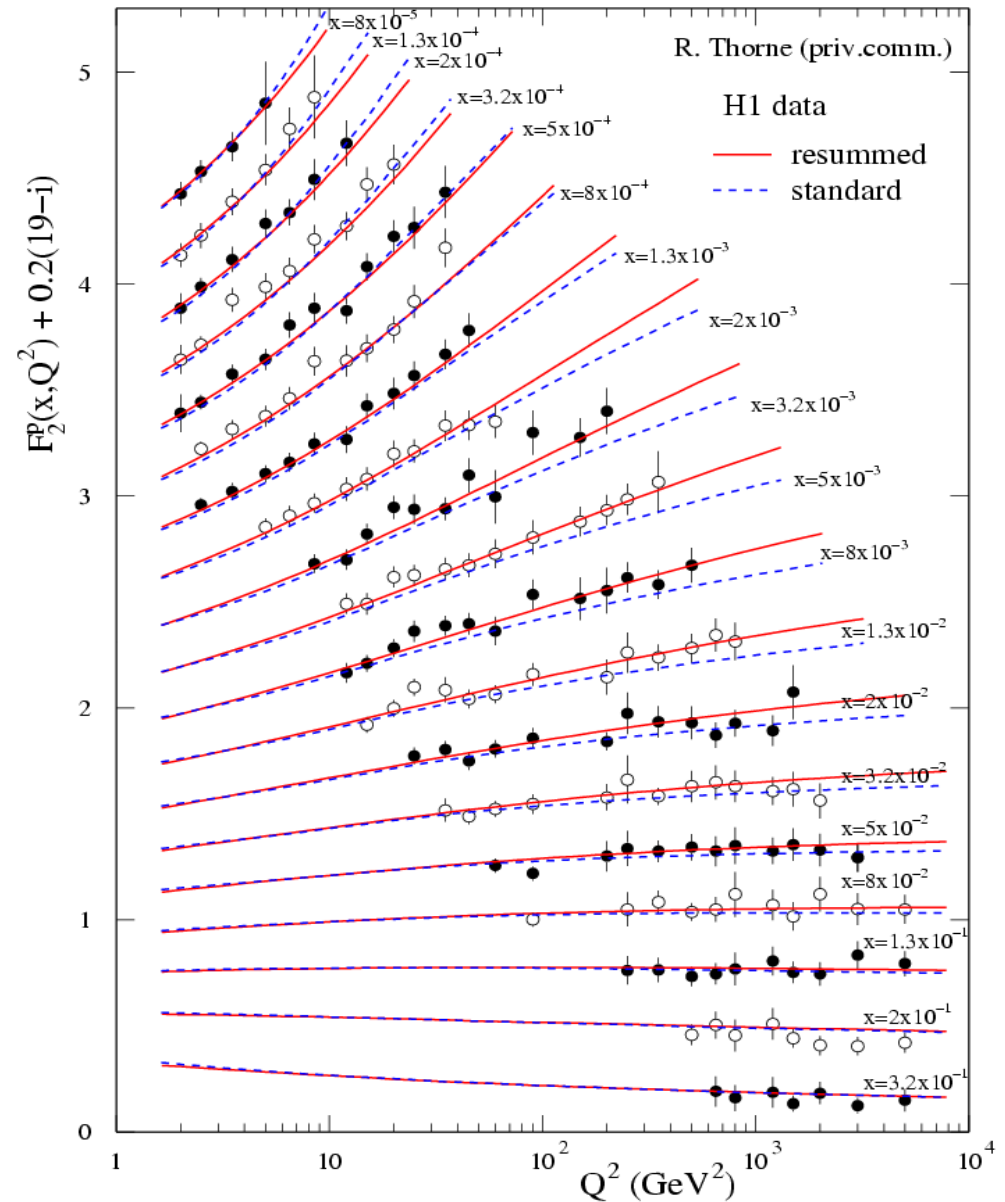
BUT has problems

- finite  $x$
- NL corrections
- final states

BUT asymptotia still far away  
even for LHC or cosmic energies

# From asymptotia to total x-section

- Description of inclusive processes:
- DGLAP for high  $Q^2$
- BFKL for small  $x$
- matched DGLAP/BFKL for  $F_2$   
(R. Thorne, Kimber, Martin, Stasto, etc)
- resummed gives better fit
- .... not a big effect at HERA !!!
- where is asymptotia ?

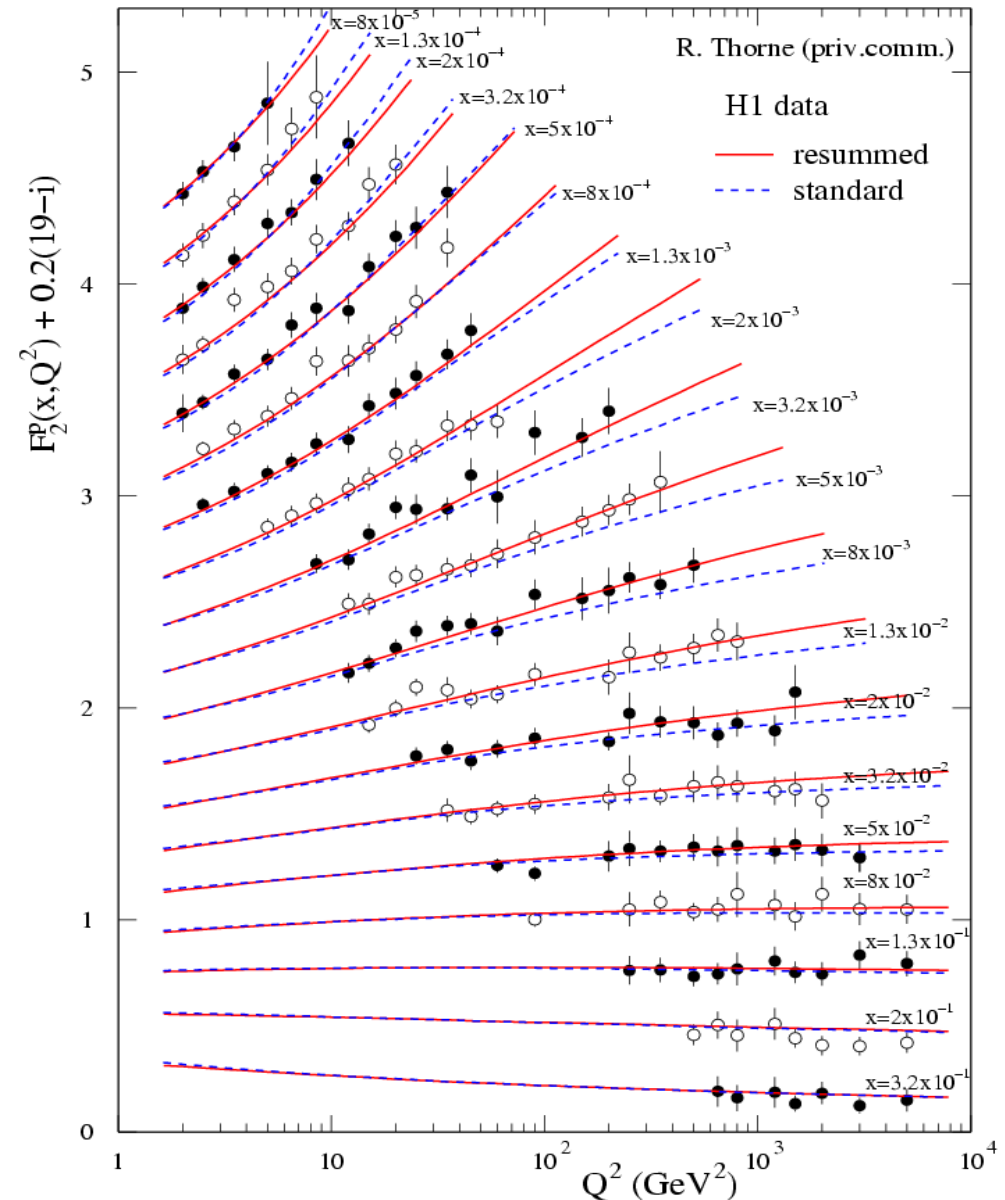


# From asymptotia to exclusivity

- Description of inclusive processes:
- DGLAP for high  $Q^2$
- BFKL for small  $x$
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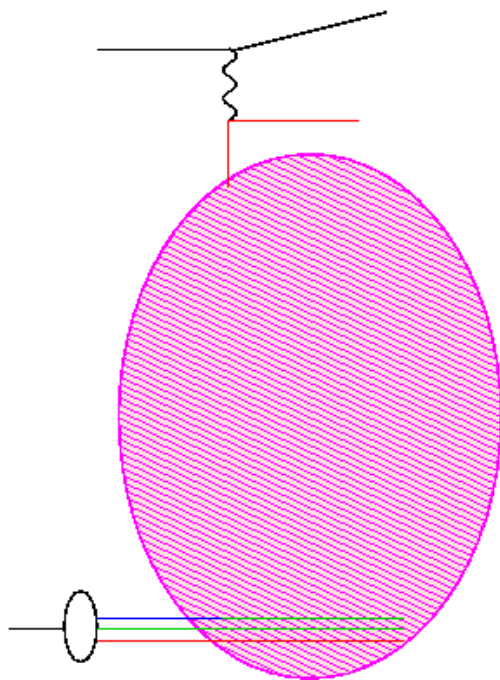
## Building up the final states

- Monte Carlo event generators
- fixed order parton level calculations at NLO

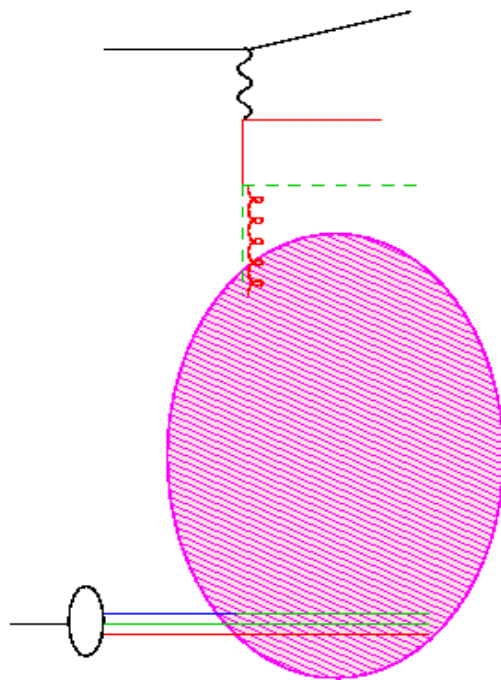


**Howto investigating in detail  
small  $x$  behavior ?**

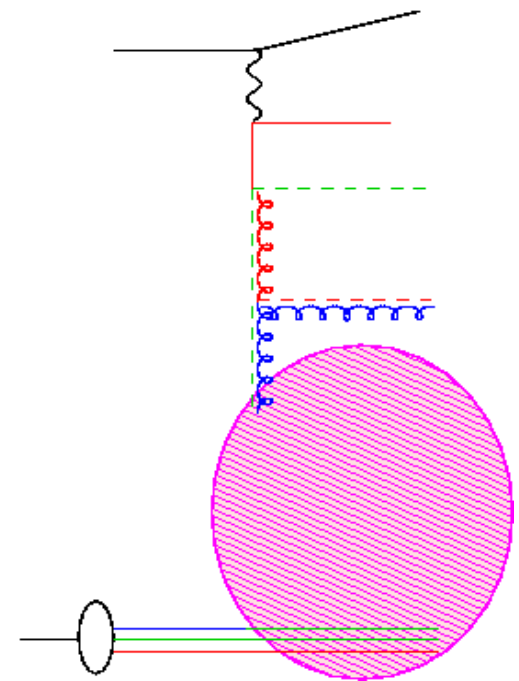
# How to investigate this ?



QPM process  
total x-section

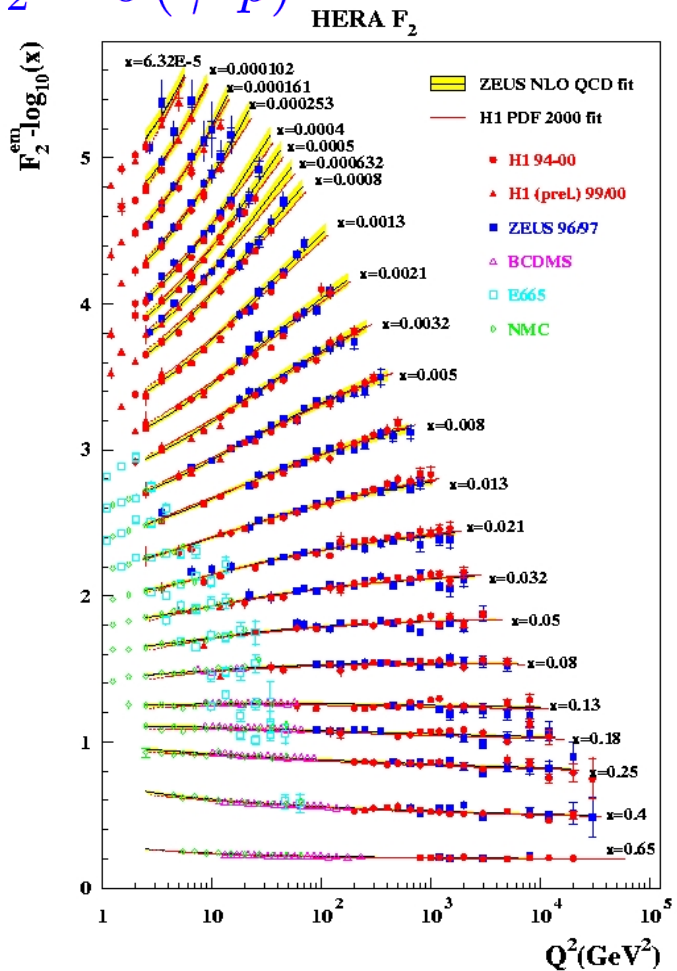


BGF  $\mathcal{O}(\alpha_s)$  process  $\mathcal{O}(\alpha_s^2)$  process  
heavy quarks (charm & bottom)  
2-jet 3-jet

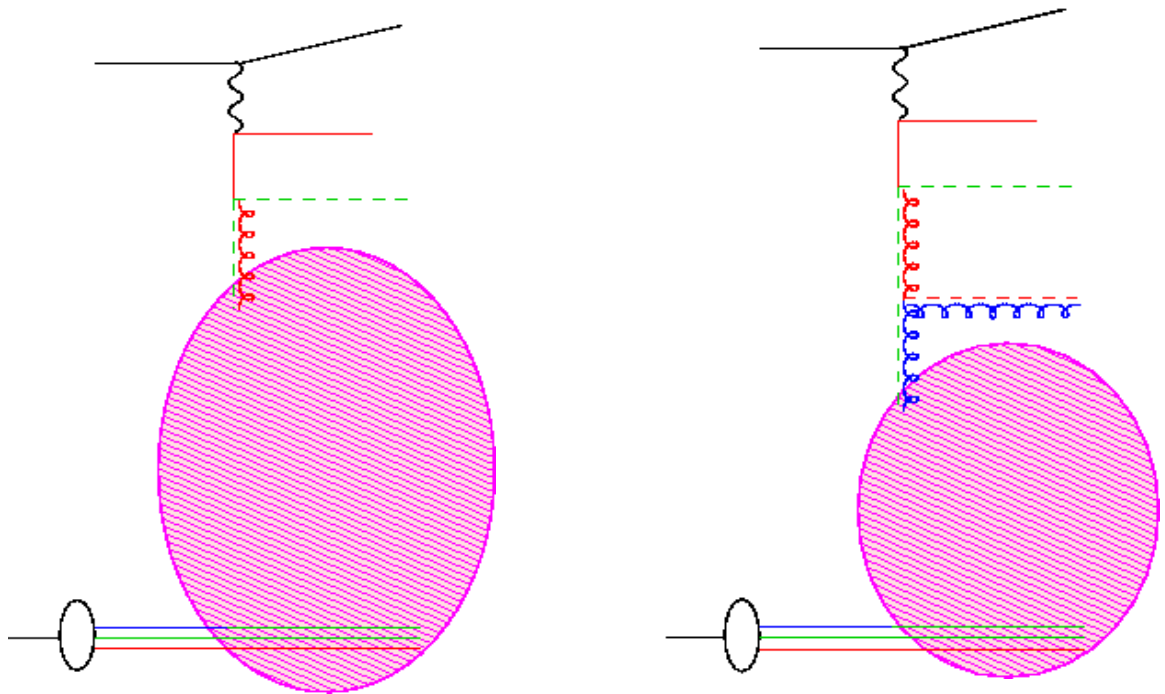


# Howto investigate this ?

$$F_2 \sim \sigma(\gamma^* p)$$



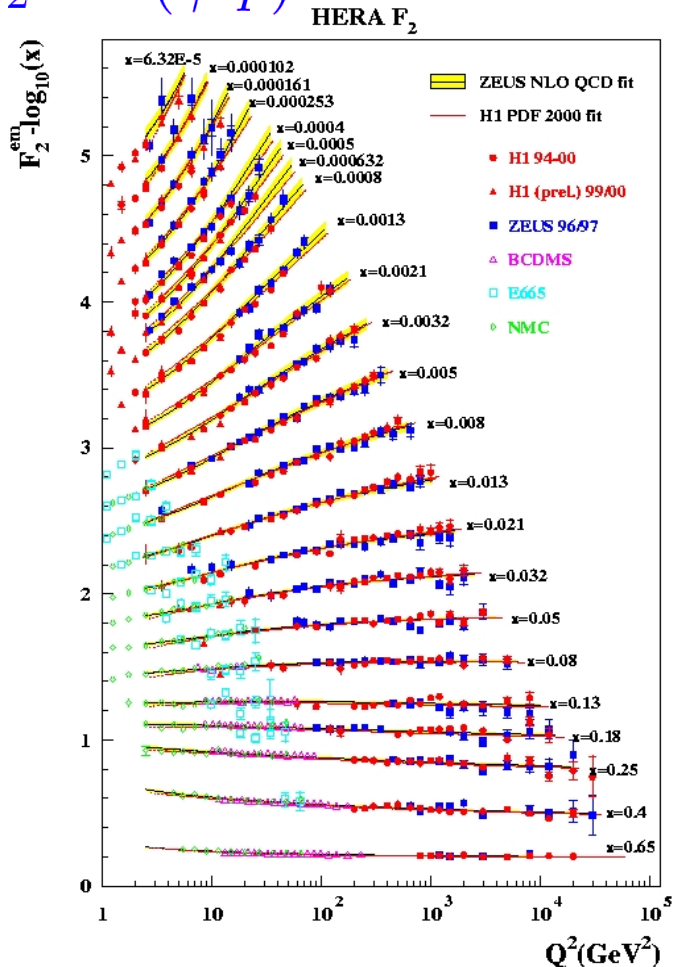
QPM process  
total x-section



BGF  $\mathcal{O}(\alpha_s)$  process  $\mathcal{O}(\alpha_s^2)$  process  
heavy quarks (charm & bottom)  
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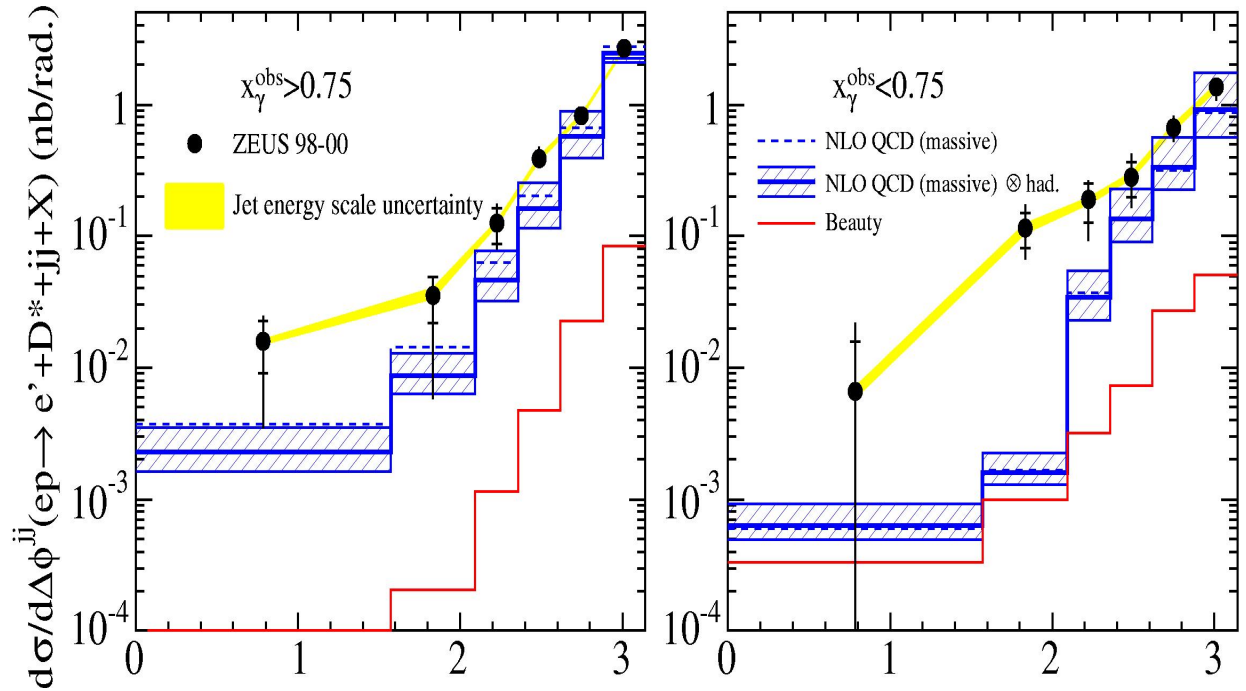
# How to investigate this ?

$$F_2 \sim \sigma(\gamma^* p)$$



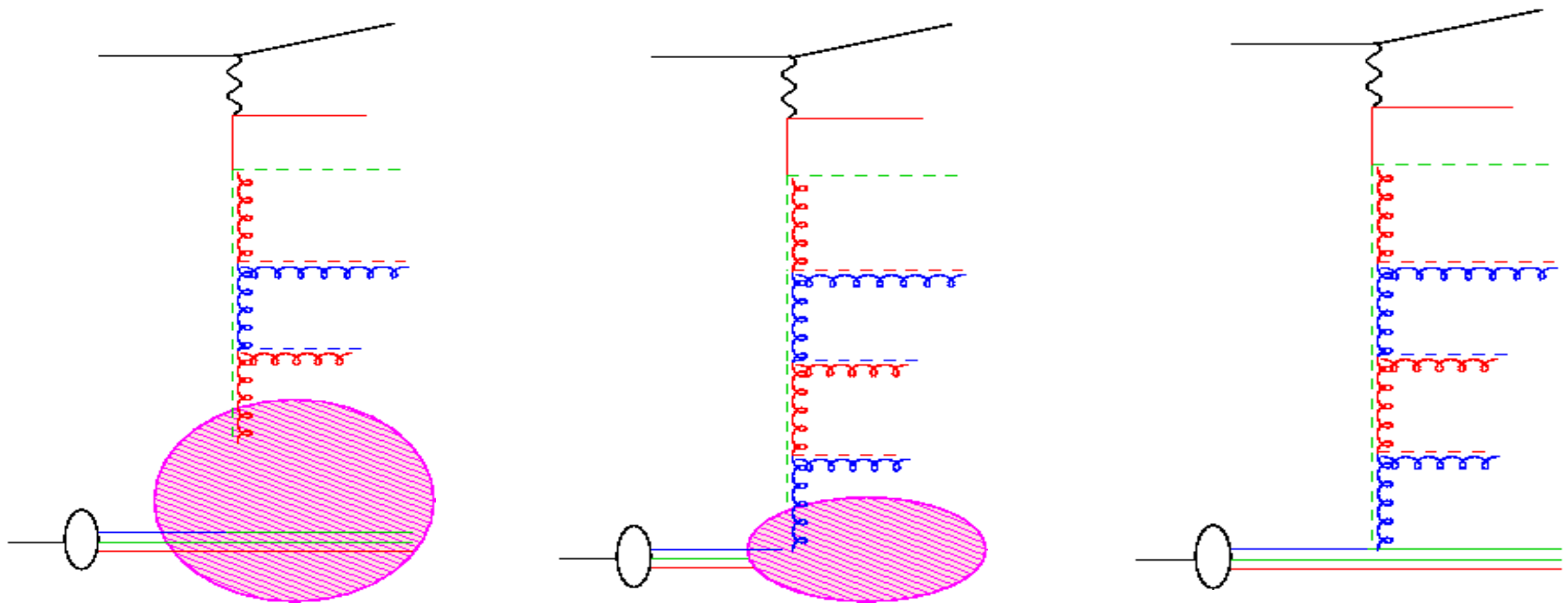
QPM process  
total x-section

## ZEUS



BGF  $\mathcal{O}(\alpha_s)$  process  $\mathcal{O}(\alpha_s^2)$  process  
heavy quarks (charm & bottom)  
2-jet 3-jet

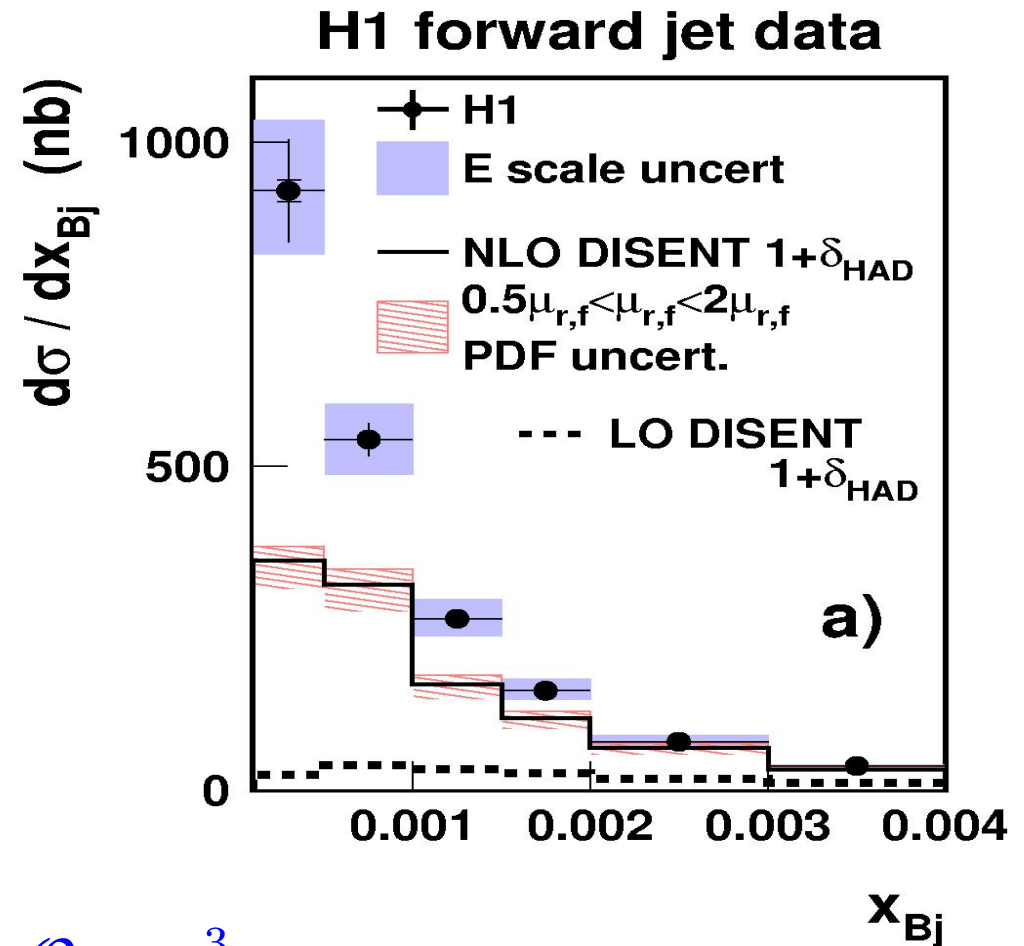
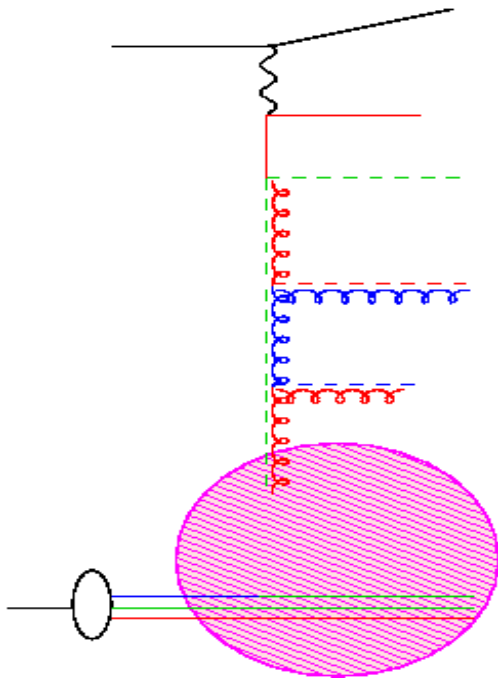
# Howto investigate this ?



- processes of  $\mathcal{O} > \alpha_s^3$  have not yet been calculated ...
- interesting to go closer to outgoing proton remnant

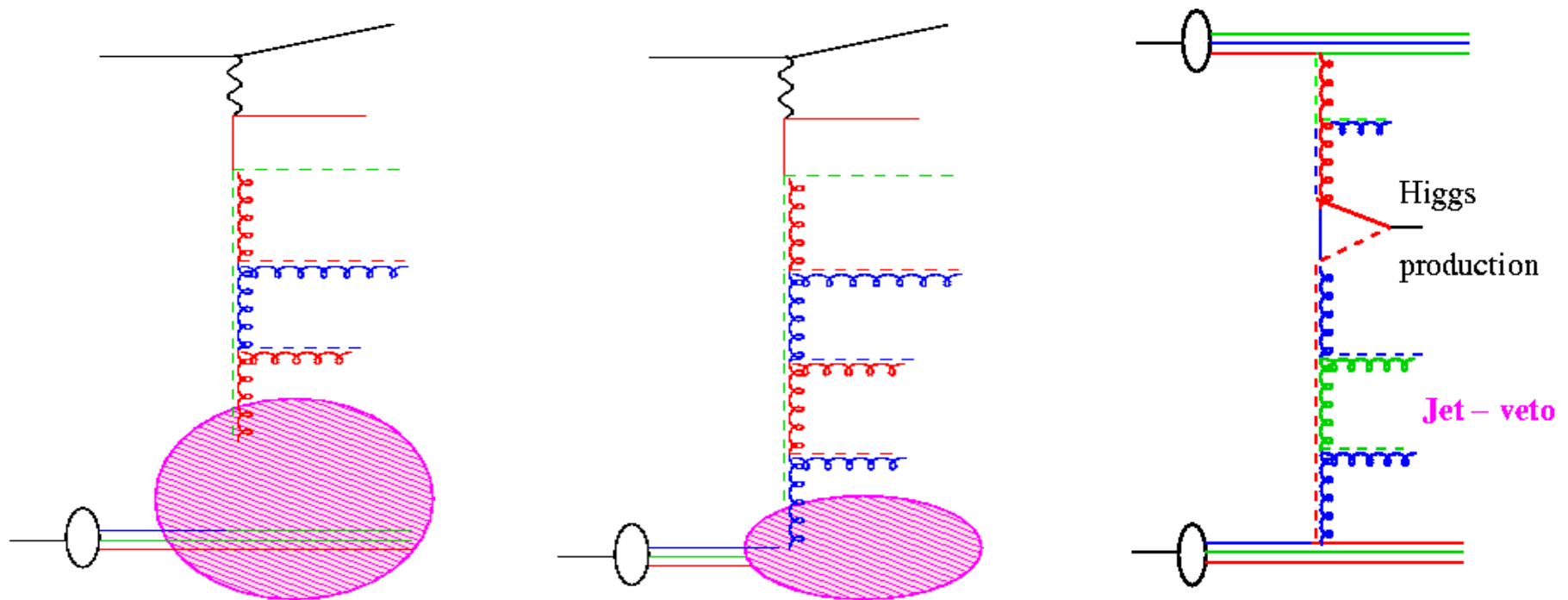


# Howto investigate this ?



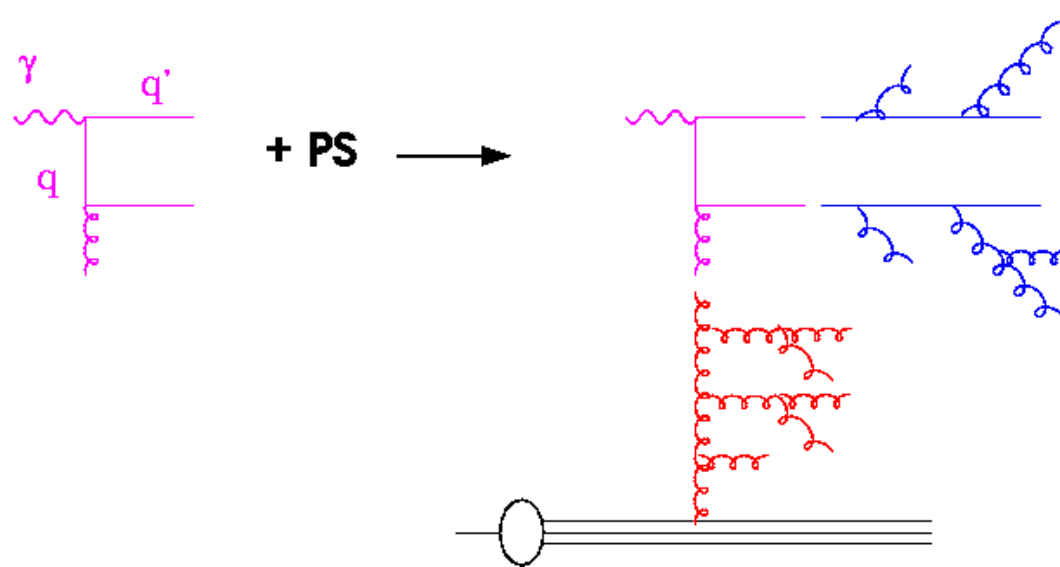
- processes of  $\mathcal{O} > \alpha_s^3$  have not yet been calculated ...
- interesting to go closer to outgoing proton remnant
- forward jets

# Howto investigate this ?



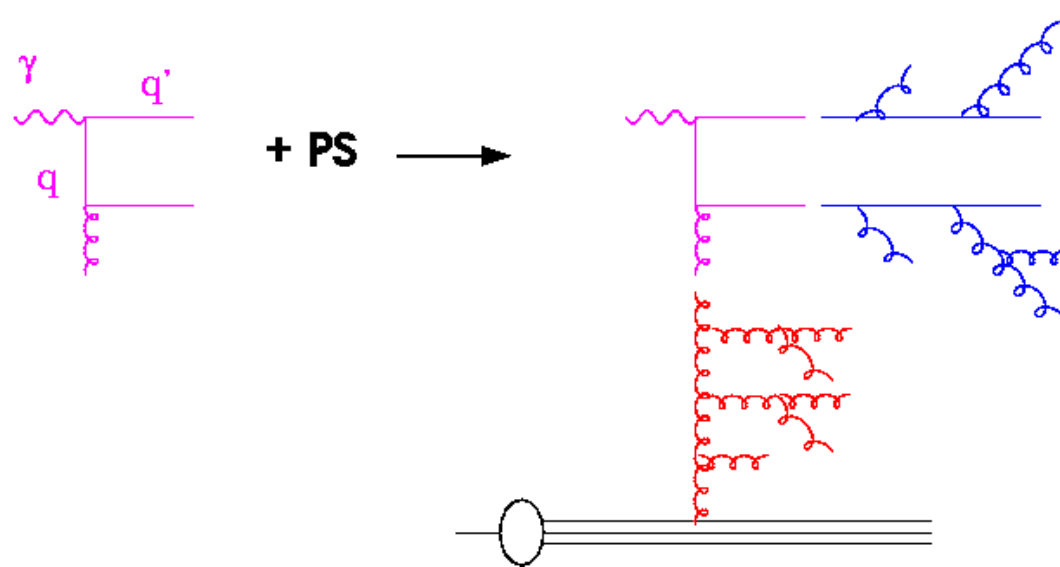
- processes of  $\mathcal{O} > \alpha_s^3$  have not yet been calculated ...
- interesting to go closer to outgoing proton remnant
- jet veto in Higgs production at LHC

# DGLAP Monte Carlo event generators



- use LO (NLO) matrix elements
- apply initial and final state parton showers
  - a la DGLAP or BFKL/CCFM
  - matching of ME with parton showers
- apply hadronization
- obtain cross sections fully differential in any observable
- **BUT:**
  - mainly LO (attempts to include NLO: Collins et al, MC@NLO, etc )

# Inconsistency: example from HERA



- **Collinear approach:** incoming/outgoing partons are on mass shell  
 $(y+q)^2 = q'^2$ ,  $-Q^2 + x y s = 0 \Rightarrow x = Q^2/(ys)$
- **BUT** final state radiation:  
 $(y+q)^2 = q'^2$ ,  $-Q^2 + x y s = m^2 \Rightarrow x = (Q^2+m^2)/(ys)$
- **AND** initial state radiation:  
 $(y+q)^2 = q'^2$ ,  $-Q^2 + x y s + q^2 = 0 \Rightarrow x = (Q^2-q^2)/(ys)$
- **Collinear approach:**  $q'^2 = q^2 = 0$ , order by order ....
- Well known.... since years....
- NLO corrections... better treatment of kinematics... but still not all....

# Arguments for PDF4MC

Campbell, Huston Stirling  
Rep.Prog.Phys 70 (2007) 89

In addition, it is often useful to examine variations in acceptances in Monte Carlos using the families of NLO error pdfs; thus, it is important to also compare with the predictions using the central (NLO) pdf. It is our recommendation, then, that NLO pdfs be used for predictions at the LHC, even with LO matrix element programs and parton shower Monte Carlos. There are two consequences: (1) the pdfs must be positive-definite in the kinematic regions of interest as they will be used to develop the initial-state showering history and (2) underlying event tunes must be available using the NLO pdfs. An underlying event model that uses multiple-parton interactions depends strongly on the slope of the low  $x$  gluon distribution. The NLO gluon distribution tends to have a much shallower slope than does the LO gluon and thus a different set

Is that the end of the story ?

# Which PDFs to be used in MC's ?

arguments by T. Sjostrand

General purpose event generators provide

$$\hat{\sigma}(\text{LO}) \otimes \text{PDF}(\text{LO}) \otimes \text{showers}$$

Each component separately is positive

**BUT ...**

- PDF fits using LO are bad
- no uncertainty estimate for LO PDFs
- Often NLO PDFs are used....

**BUT**

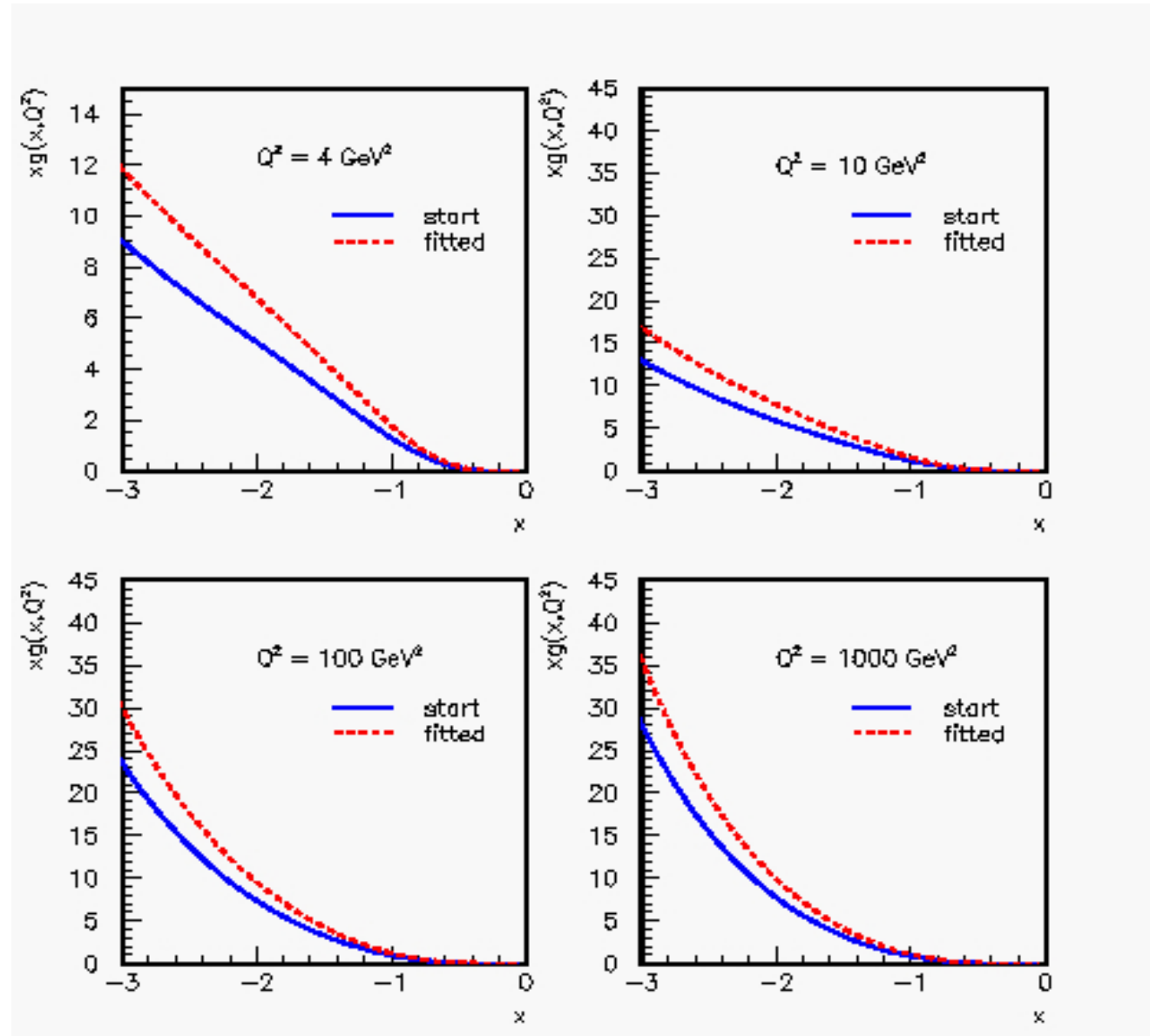
- PDFs are not physical observables ... not necessarily positive
- $\hat{\sigma}(\text{LO}) \otimes \text{PDF}(\text{NLO})$  may be **grap**

- Different solutions proposed
- determine new LO\* PDFs by relaxing momentum sum rule
  - .... hack ....
- use NLO PDFs for hard process, and LO PDFs for showering
  - .... hack ....
- determine special PDFs: PDF4MC

# PDFs after fitting $F_2$ with PYTHIA

- Use LO fit....
- Fit  $F_2$  by varying  

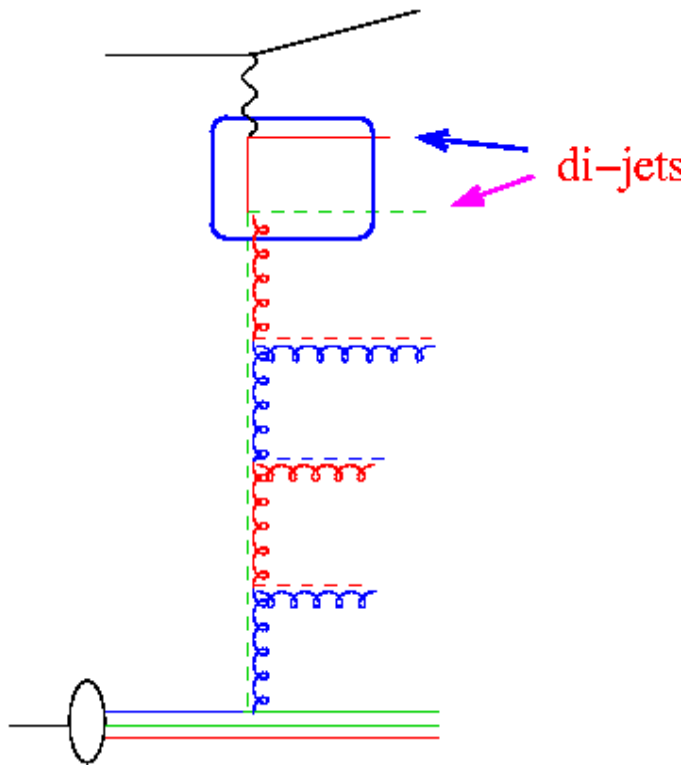
$$xg(x, \mu) = A_0 x^{A_1} \dots$$
 and  $\alpha_s(\mu)$
- Fit changes normalization and slope of gluon ... as seen in the scan....
- $\chi^2/ndf$  improves...., but can still be better....
- Seems to be a bit different ...



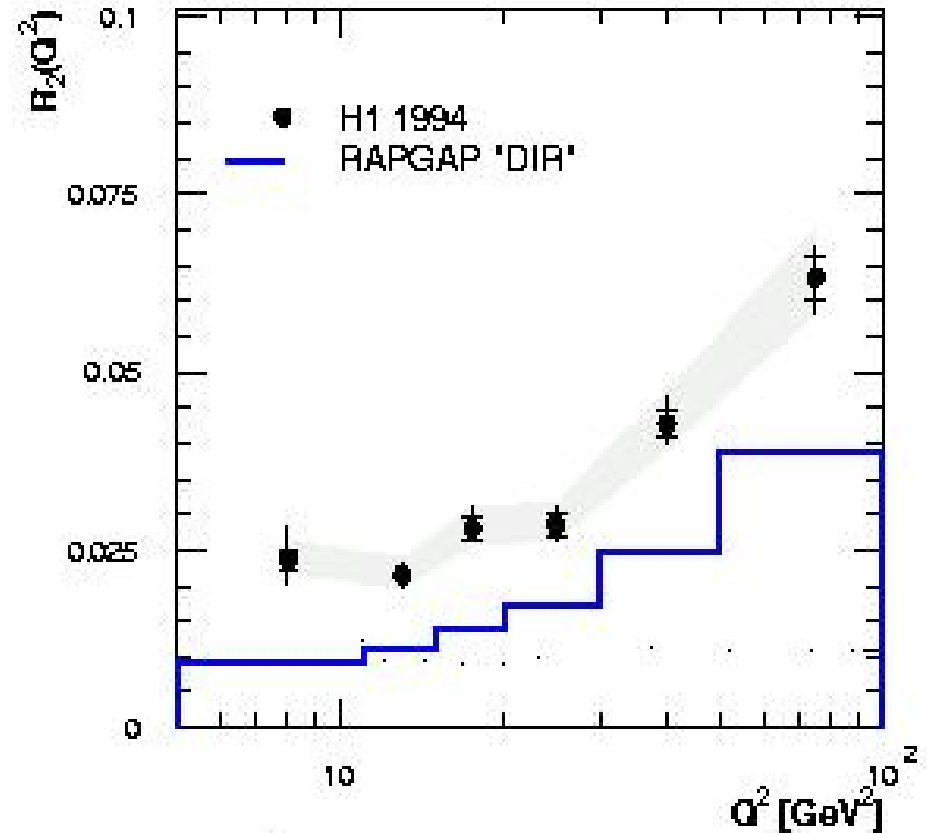
**How well do we  
understand the  
hadronic final state ?**



# Do we understand di-jet production?

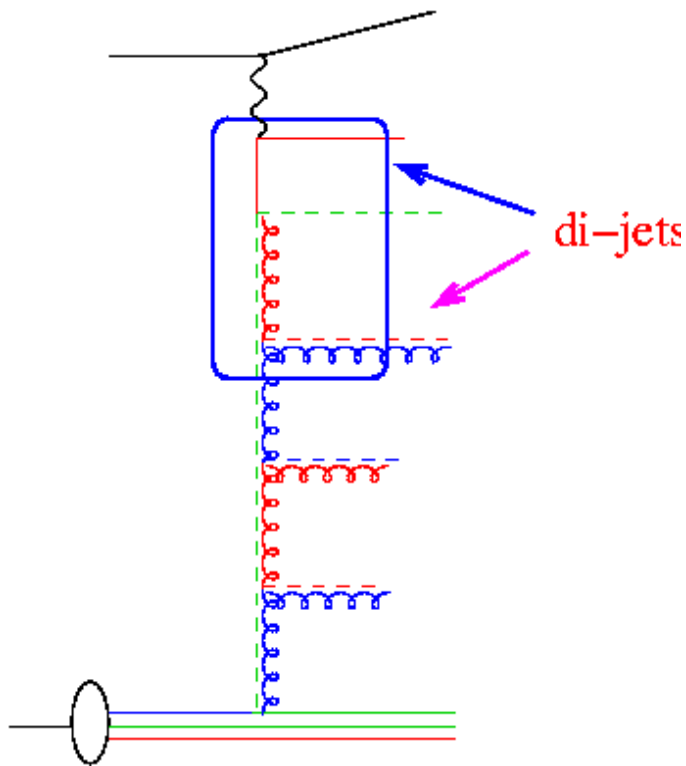


asymmetric ( $5/7 \text{ GeV}$ )

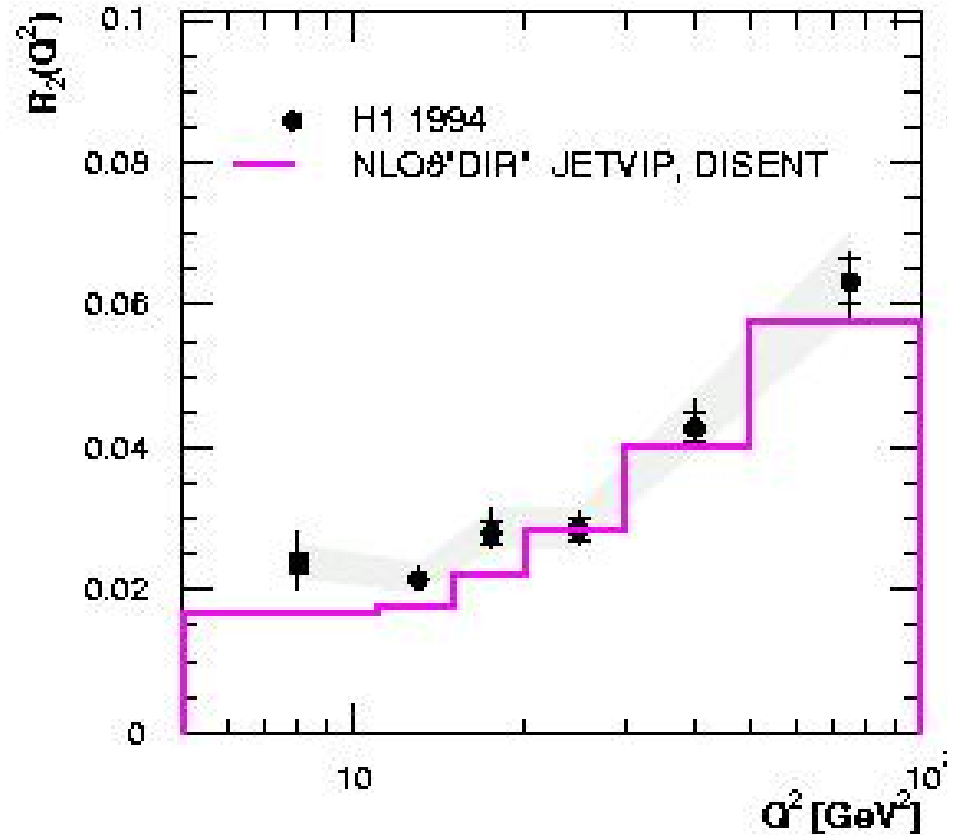


- (2+remnant) jets in DIS for  $Q^2 > 5 \text{ GeV}^2$ ,  $p_{\text{T}}^{\text{jets}} > 5 \text{ GeV}$
- use perturbative expansion:  $\sigma_{\text{true}} = \sigma(\mathcal{O}(\alpha_s)) + \sigma(\mathcal{O}(\alpha_s^2)) + \dots$
- $\mathcal{O}(\alpha_s)$  processes not enough  
 → need higher order contributions

# Doing better for di-jets ...



asymmetric (5/7 GeV)

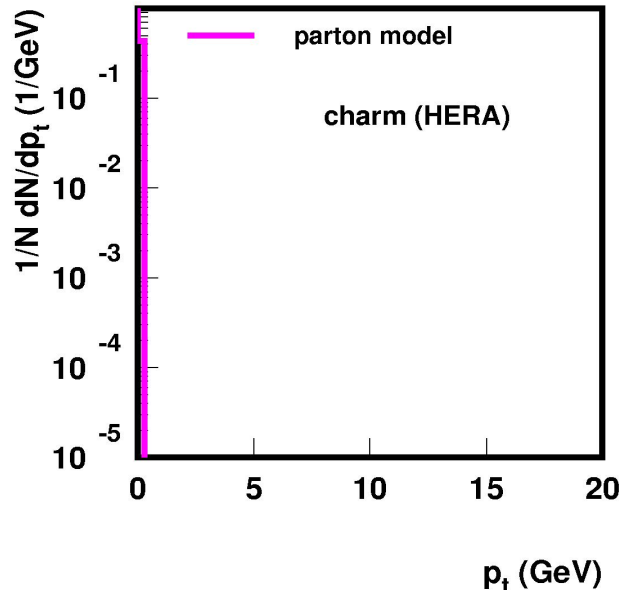
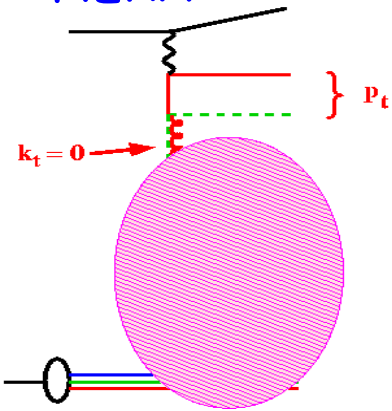


- (2+remnant) jets in DIS for  $Q^2 > 5 \text{ GeV}^2$ ,  $p_{\perp}^{\text{jets}} > 5 \text{ GeV}$
- use perturbative expansion:  $\sigma_{\text{true}} = \sigma(\mathcal{O}(\alpha_s)) + \sigma(\mathcal{O}(\alpha_s^2)) + \dots$
- NLO calculations are ok, if  $p_{t1} \neq p_{t2}$

# Problems in Collinear Approximation

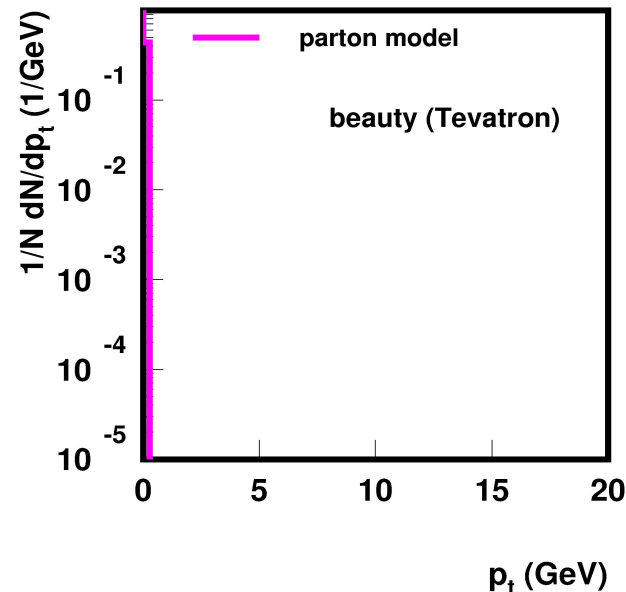
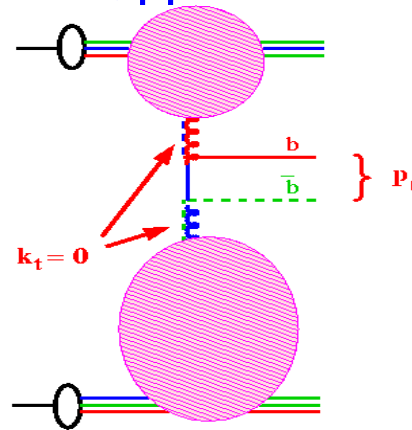
Jets/ heavy quarks at

HERA



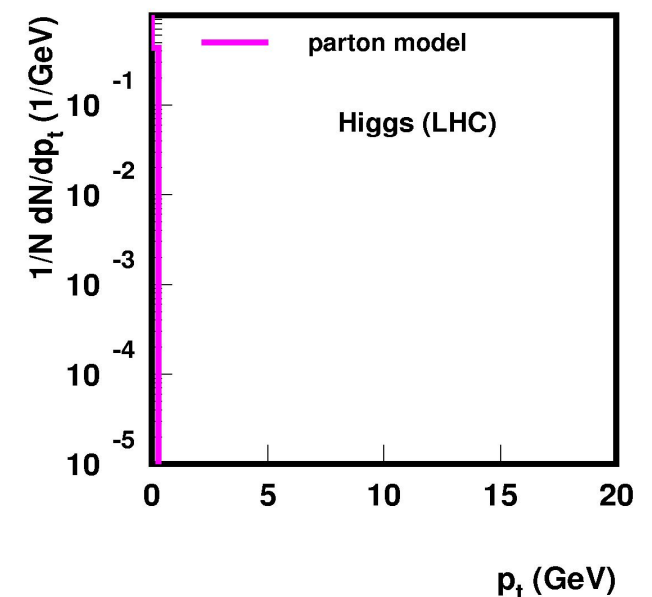
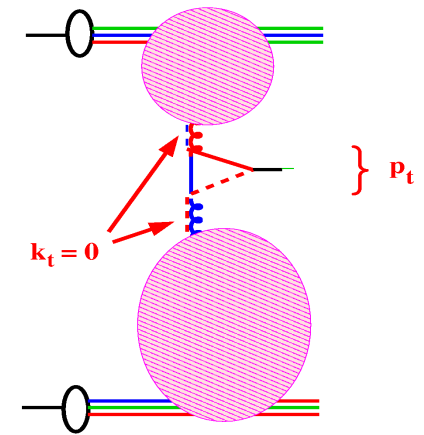
Jets/ heavy quarks

in pp



J. Collins, H. Jung hep-ph/0508280

Higgs in pp

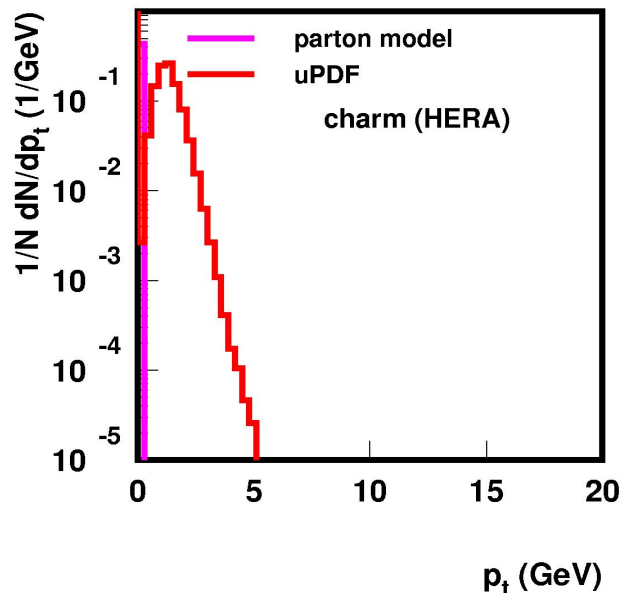
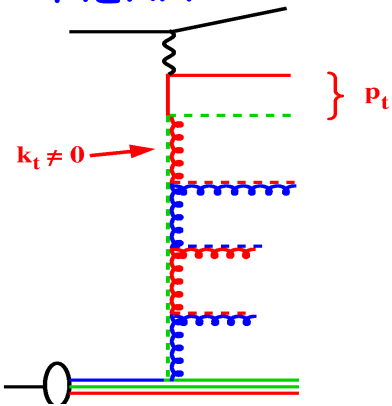


➔ NLO corrections will be very large for these LO processes .....

# Doing much better with uPDFs ...

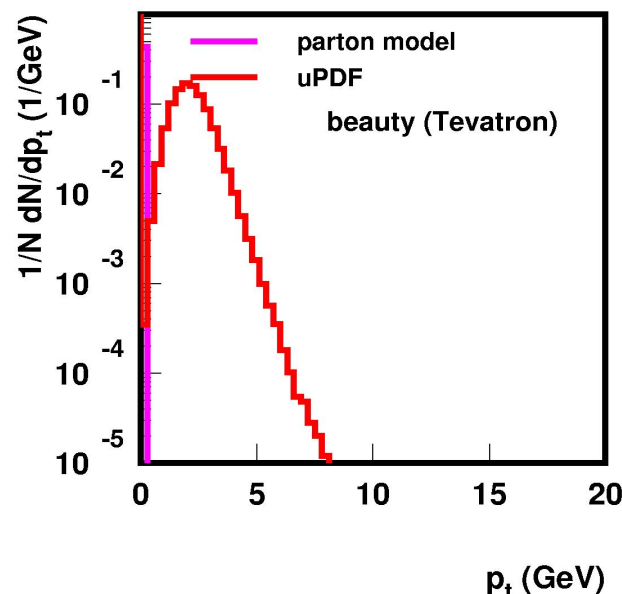
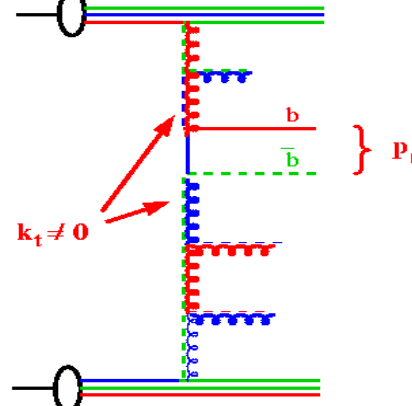
Jets/ heavy quarks at

HERA



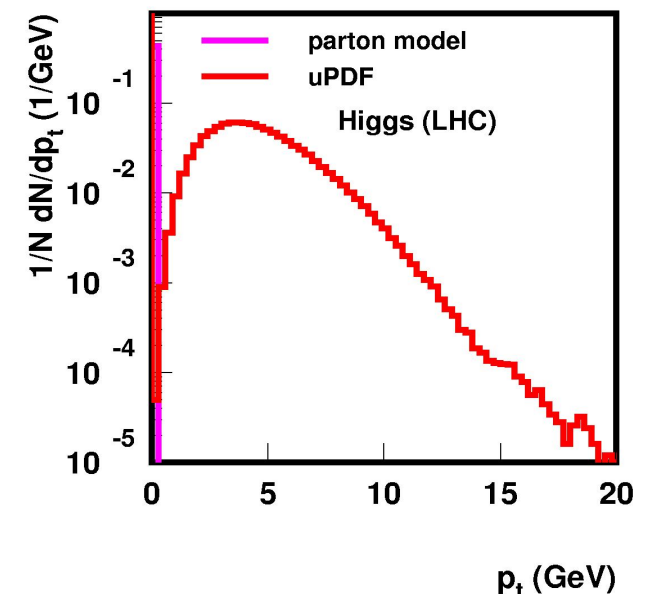
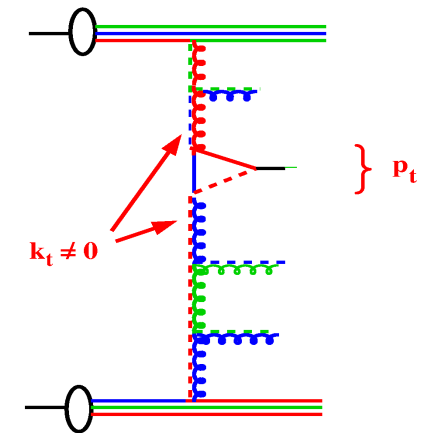
Jets/ heavy quarks

in pp



J. Collins, H. Jung hep-ph/0508280

Higgs in pp



→ doing kinematics correct at LO, reduces NLO corrections ... **NEED uPDFs !!!!**

# uPDF fit to $F_2$ HERA data

- fit parameters of starting distribution

$$x g(x, \mu_0^2) = N x^{-B_g} \cdot (1-x)^4$$

- using  $F_2$  data

(H1 Eur. Phys. J. C21 (2001) 33-61, DESY 00-181)

$$x < 0.05 \quad Q^2 > 5 \text{ GeV}^2$$

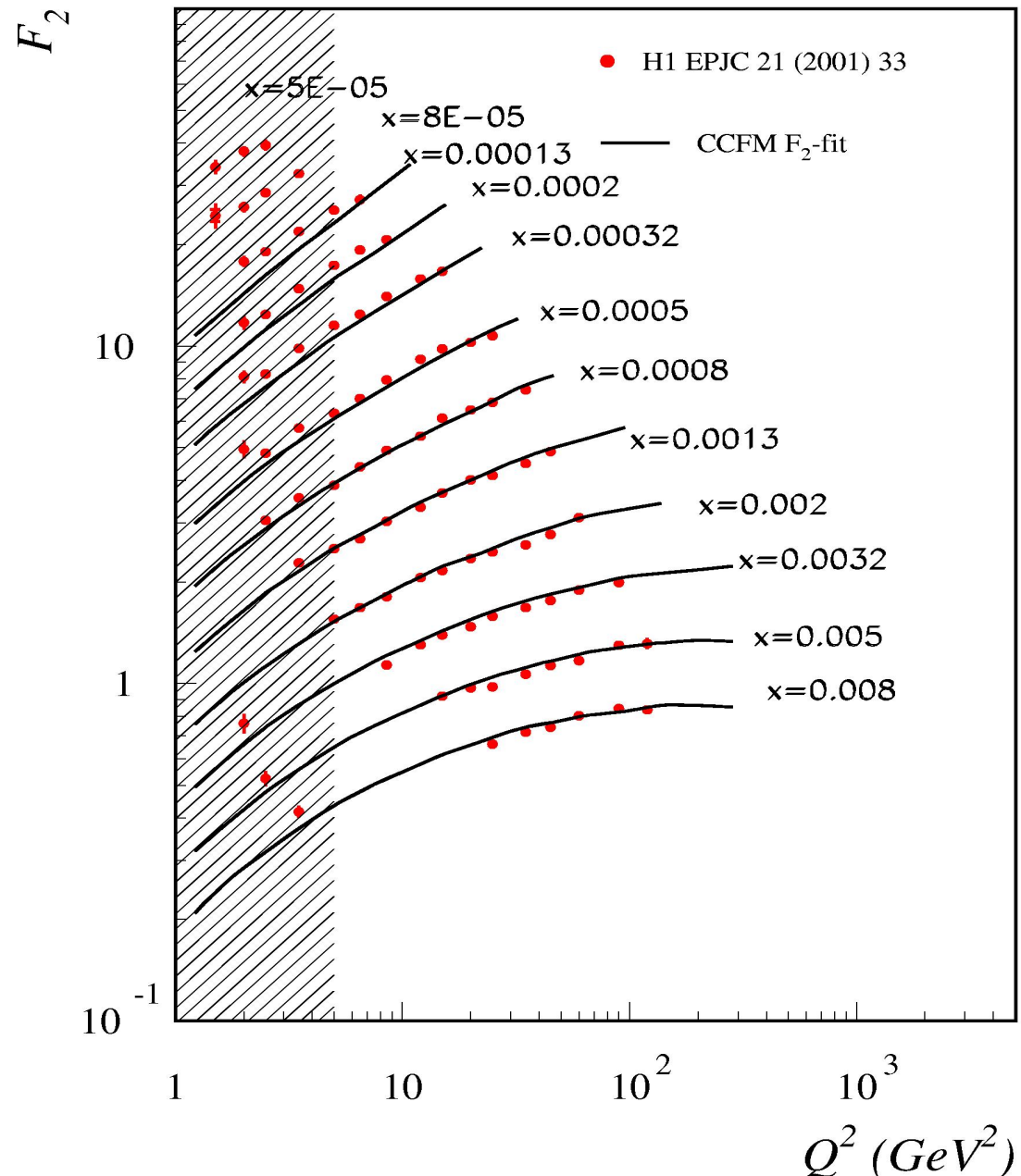
- parameters:  $\mu_r^2 = p_t^2 + m_{q,Q}^2$

$$m_q = 250 \text{ MeV}, m_c = 1.5 \text{ GeV}$$

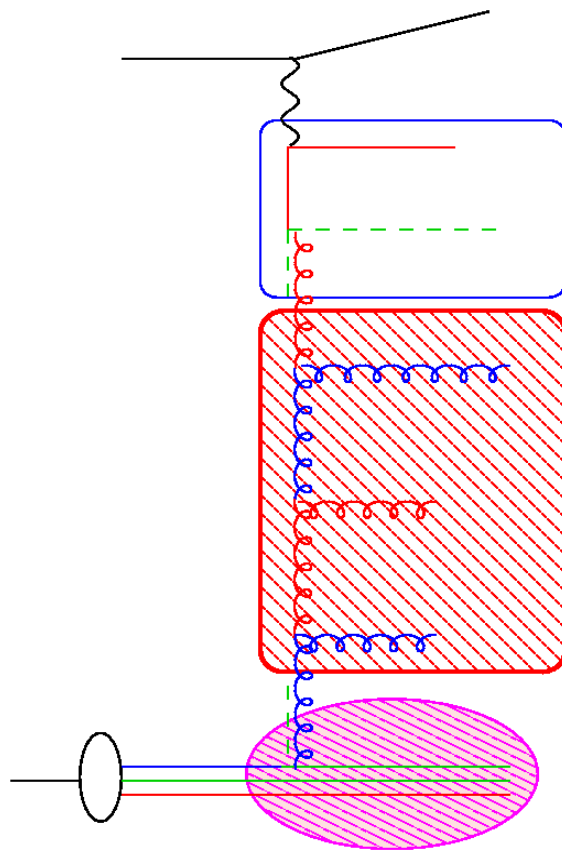
- Fit (only stat+uncorr):

$$\frac{\chi^2}{\text{ndf}} = \frac{1118}{61} = 1.83$$

- similar to NLO DGLAP fits (~1.5)



# CASCADE - C<sub>atani</sub> C<sub>iafaloni</sub> F<sub>iorani</sub> M<sub>archesini</sub> evolution



BGF matrix element  
off shell

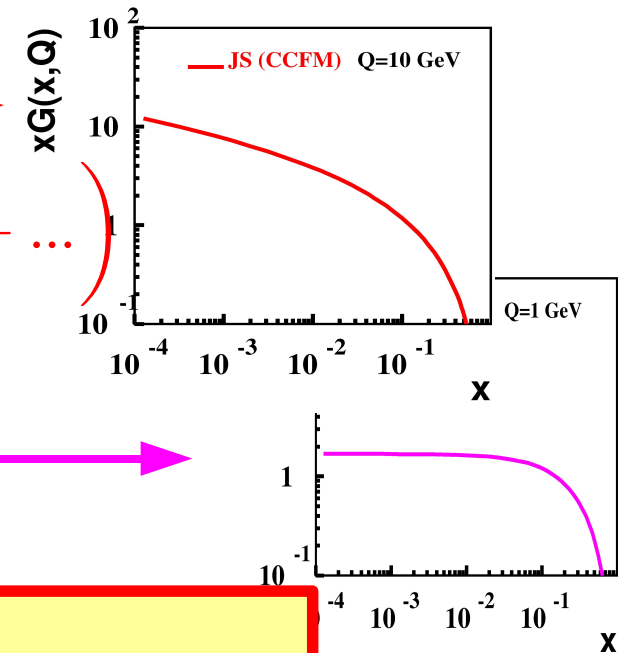
evolution of parton  
cascade:

$$\tilde{P} = \bar{\alpha}_s \left( \frac{1}{1-z} + \frac{1}{z} \Delta_{ns} + \dots \right)$$

initial distribution  
~ flat

CCFM (all loops)

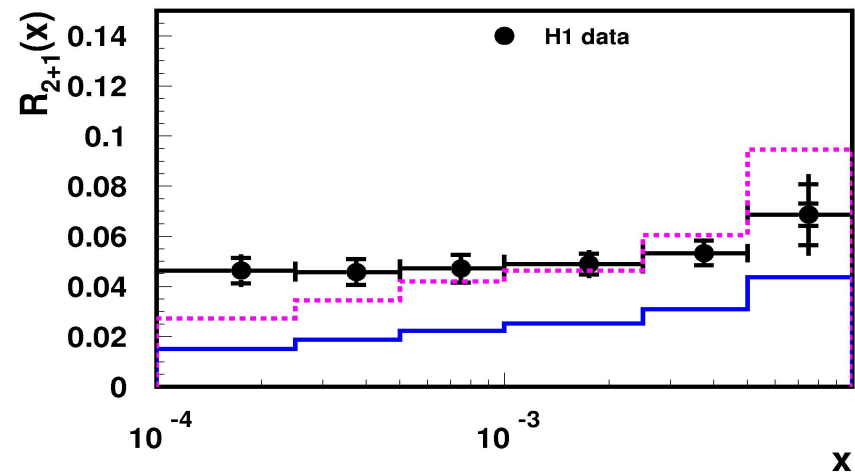
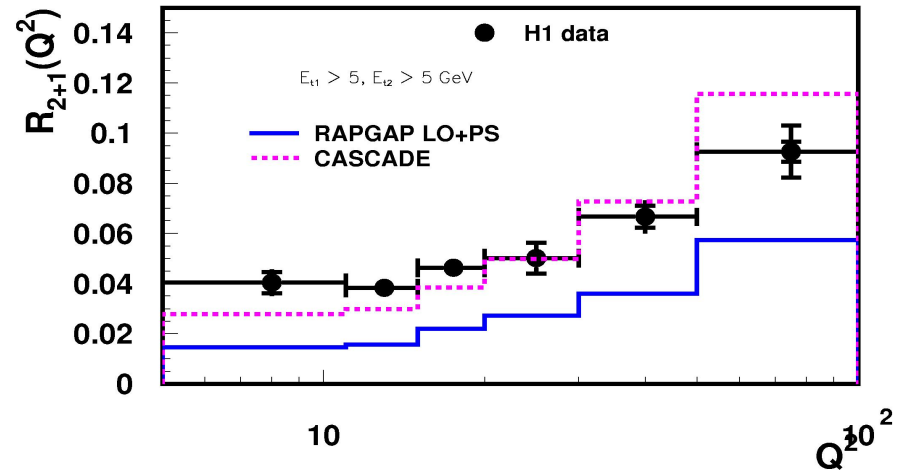
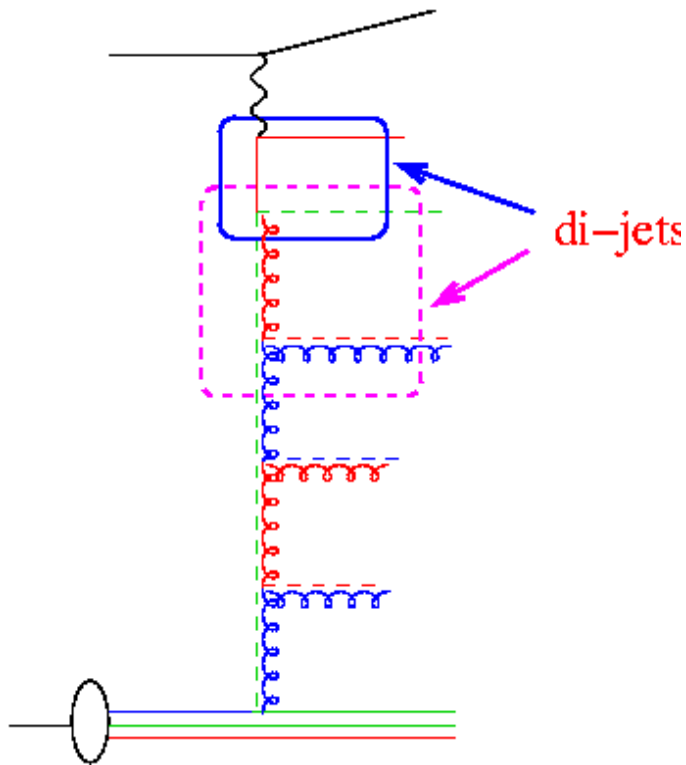
- angular ordering
- non - Sudakov  $\Delta_{ns}$



$$\sigma(ep \rightarrow e'q\bar{q}) = \int \frac{dy}{y} d^2 Q \frac{dx_g}{x_g} \int d^2 k_t \hat{\sigma}(\hat{s}, k_t, Q) x_g \mathcal{A}(x_g, k_t, \bar{q})$$

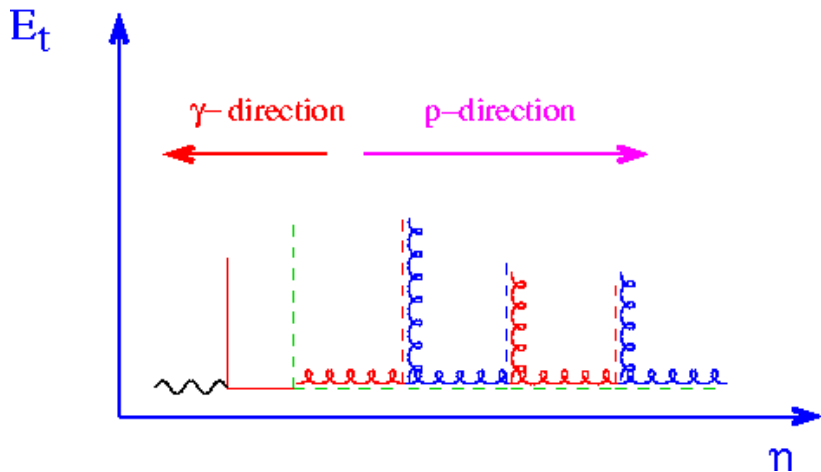
$$\int d^2 k_t x_g \mathcal{A}(x_g, k_t, \bar{q}) \simeq x_g G(x_g, Q^2)$$

# Doing easier for dijets ...

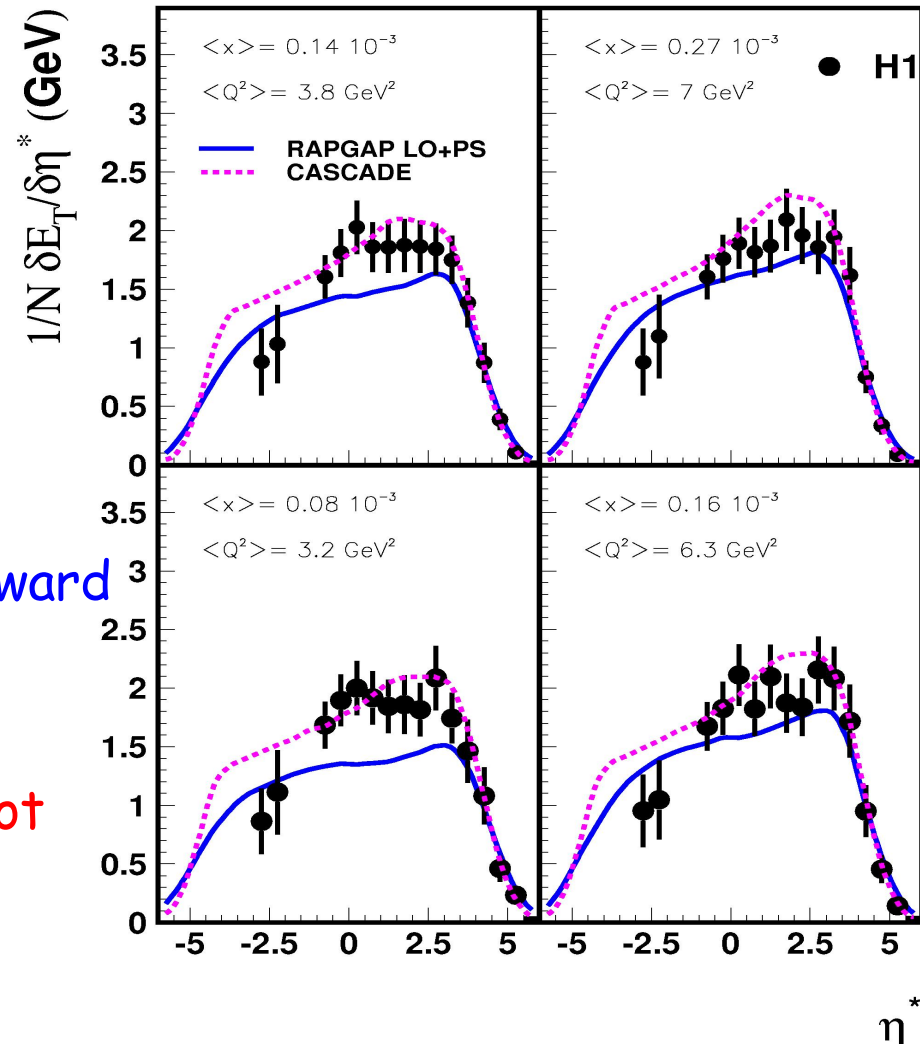


- (2+remnant) jets in DIS for  $Q^2 > 5 \text{ GeV}^2$ ,  $p_{\perp}^{\text{jets}} > 5 \text{ GeV}$
- $\mathcal{O}(\alpha_s)$  processes not enough
  - needs  $\mathcal{O}(\alpha_s^2)$  NLO calculations .... or ....
  - using uPDFs is as good as NLO !!!

# Hadronic final state: Energy flow



- $E_t$  flow in DIS at small  $x$  and forward angle (p-direction):
- $\mathcal{O}(\alpha_s)$  processes not enough
- even DGLAP parton showers do not help

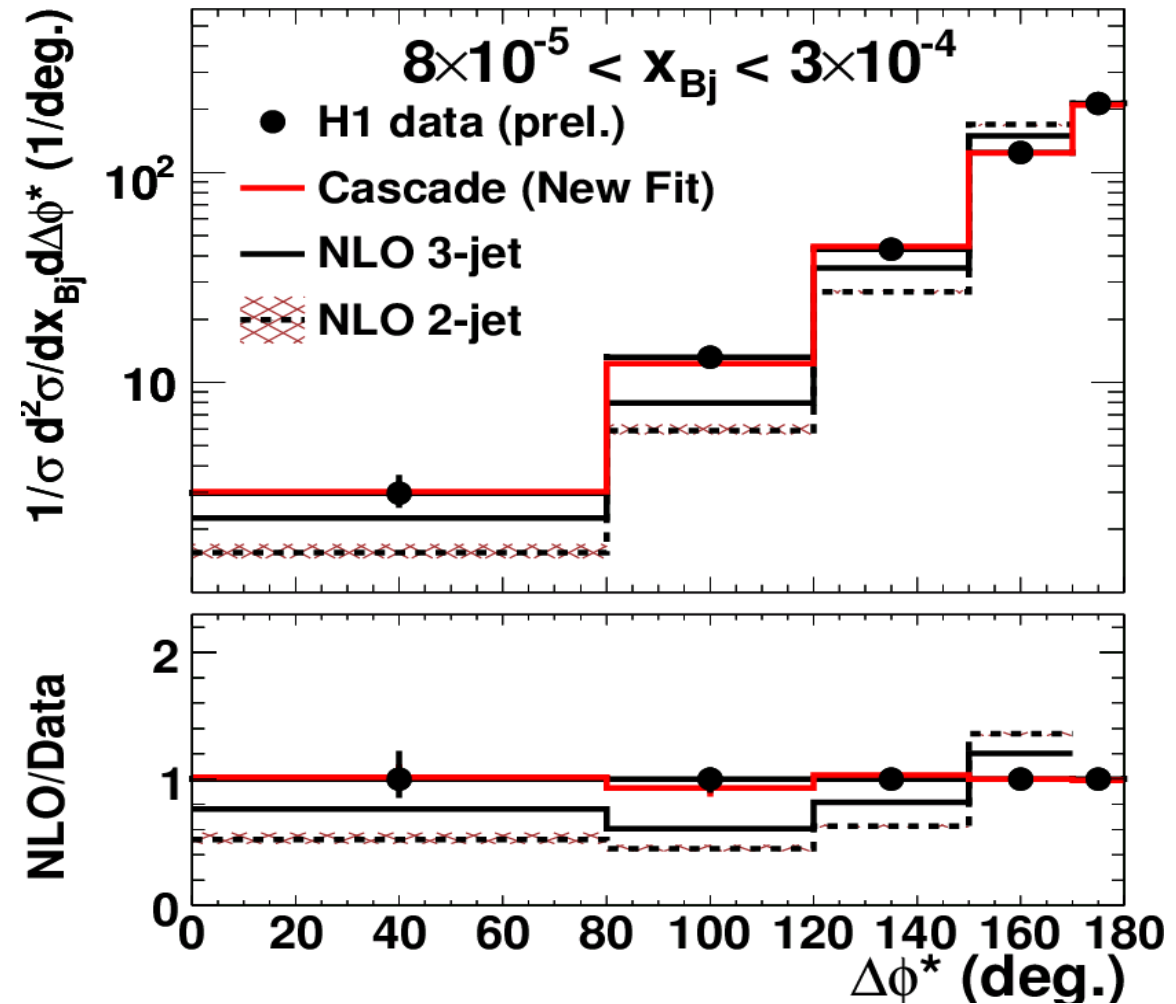
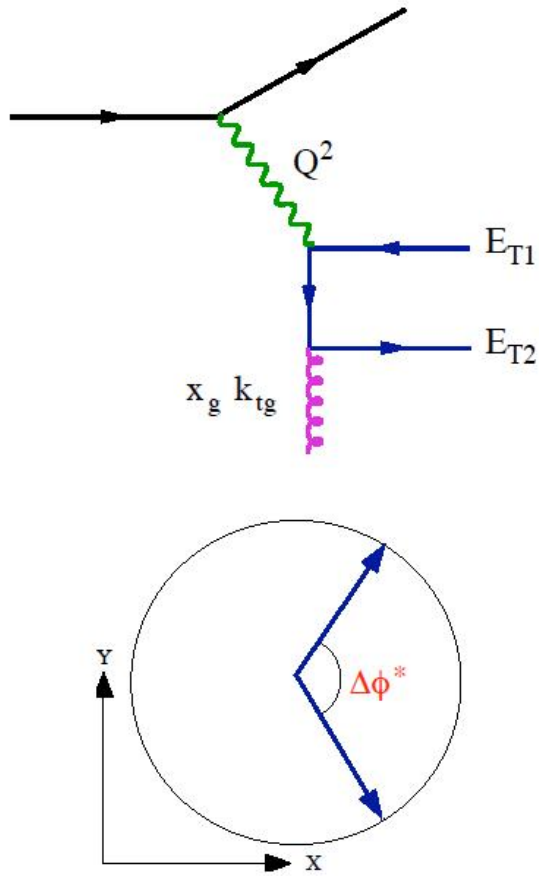


- need higher order contributions...
- using uPDFs with detailed parton showers ala CCFM very good !!!!!



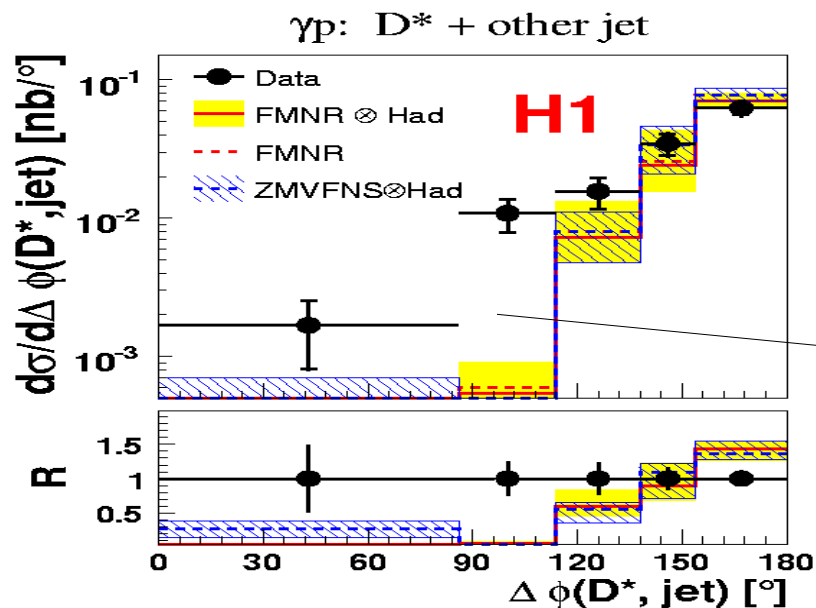
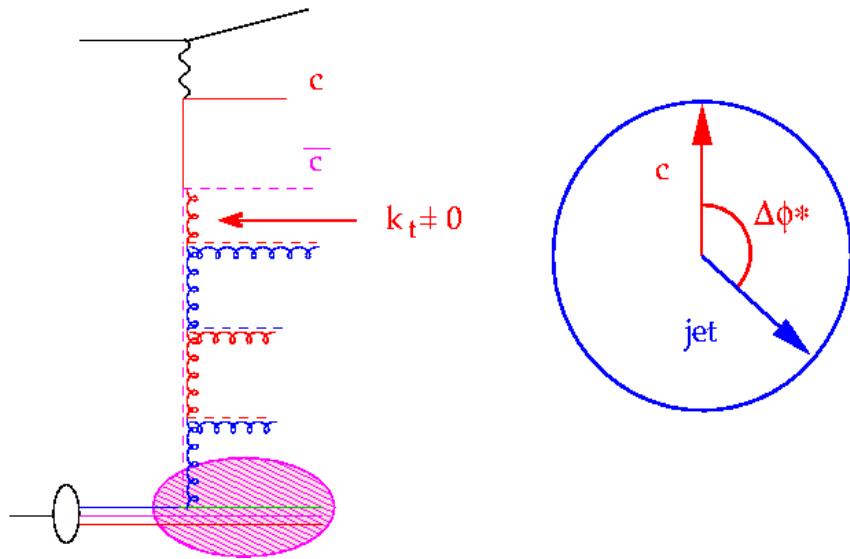
# Dijets and uPDFs: azimuthal correlations

M. Hansson (Lund)

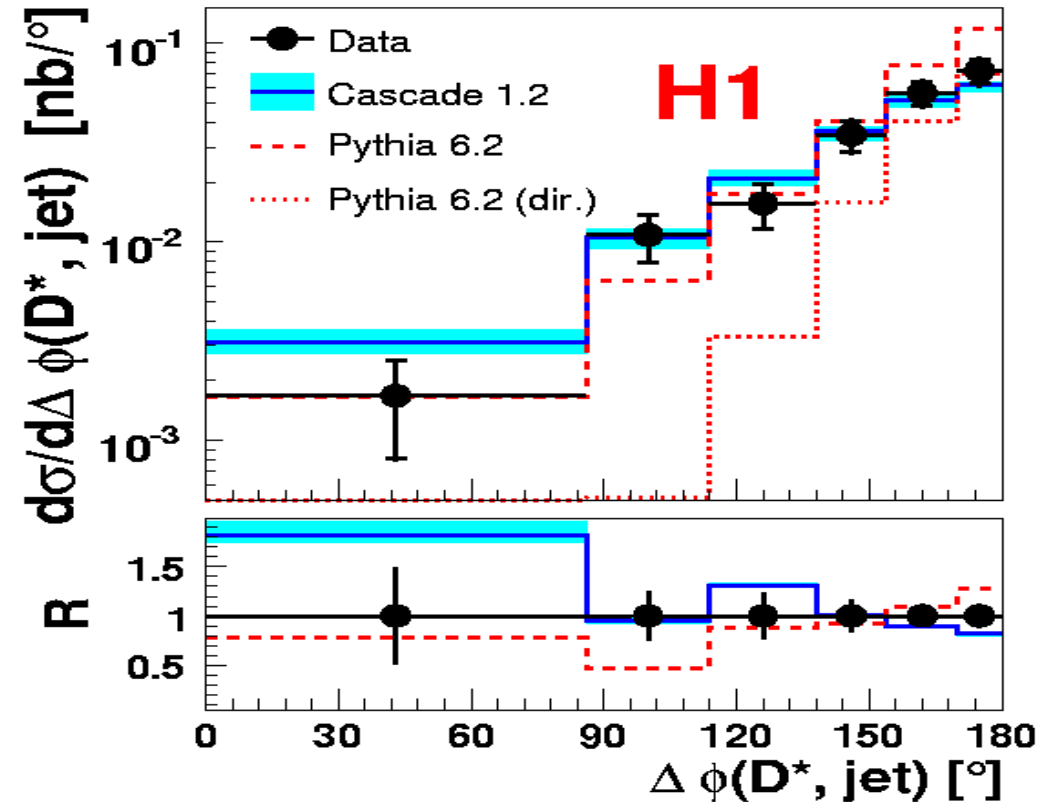


- **uPDF is much better than NLO calculations !!!!**

# Charm production: another problem

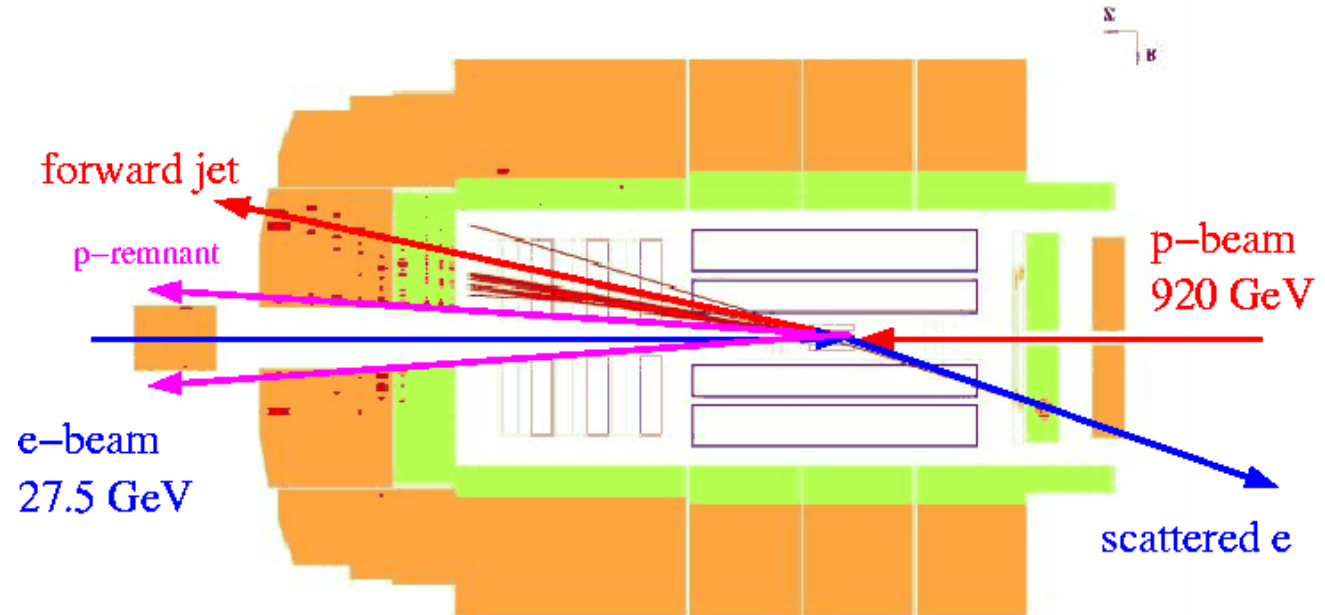
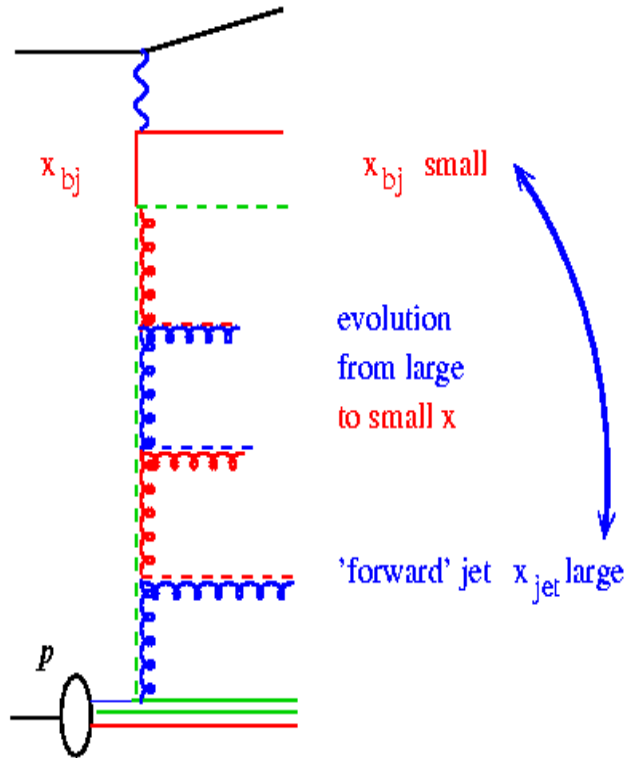


$\gamma p: D^* + \text{other jet}$



- problems at small and large  $\Delta\phi$  in NLO calc.
- $\Delta\phi$  x-section better described by MC event generators and  $uPDFs$  !

# forward jets: another problem



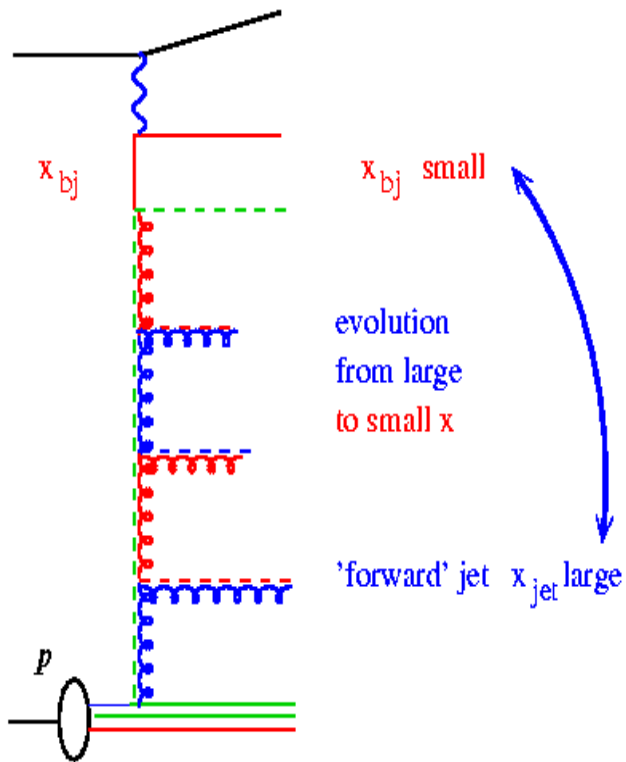
- DIS and forward jet:

$$1.7 < \eta_{jet} < 2.8$$

$$x_{jet} > 0.035$$

$$0.5 < \frac{p_{t\ jet}^2}{Q^2} < 5$$

# forward jets: another problem



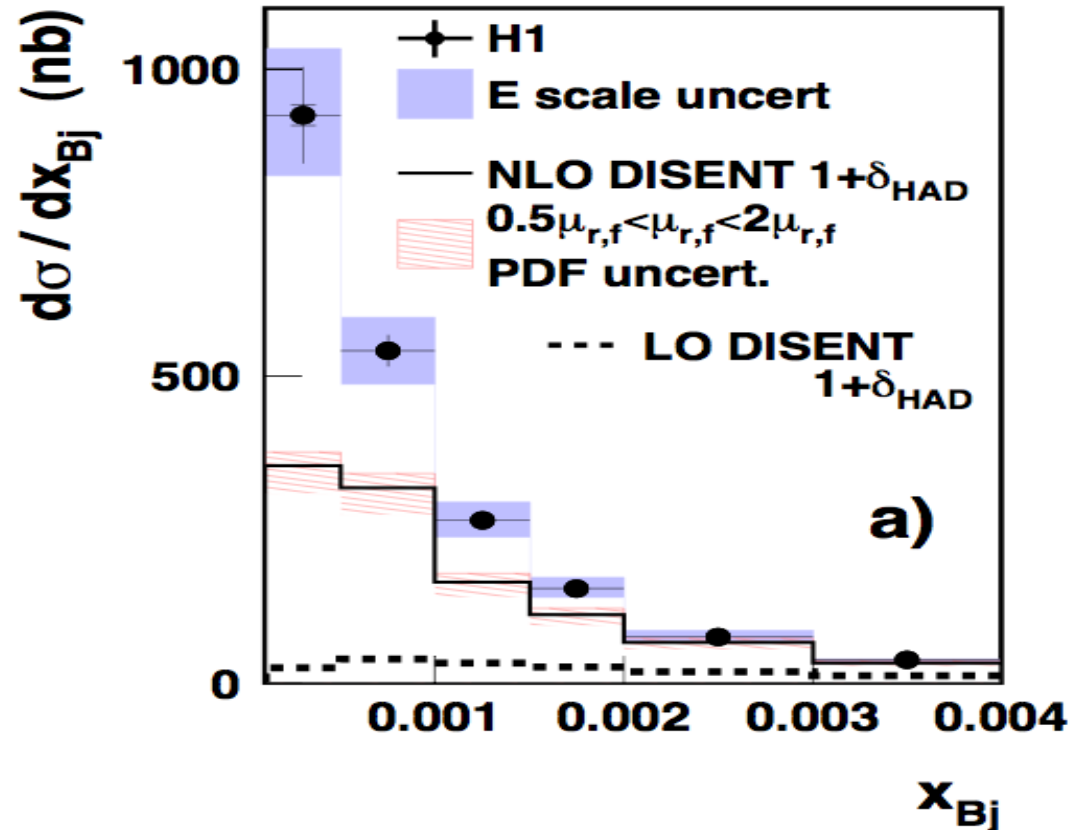
- DIS and forward jet:

$$1.7 < \eta_{jet} < 2.8$$

$$x_{jet} > 0.035$$

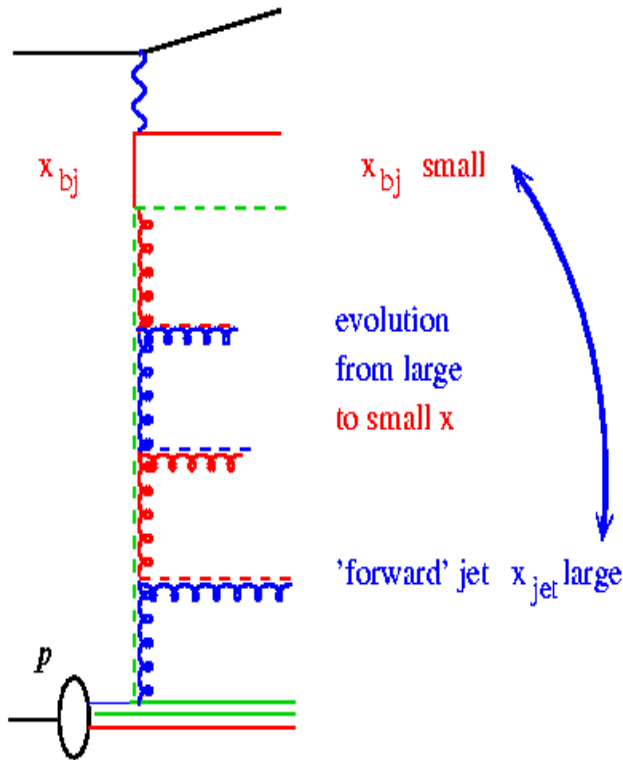
$$0.5 < \frac{p_{t,jet}^2}{Q^2} < 5$$

## H1 forward jet data



- "NLO" too low

# forward jets: another problem



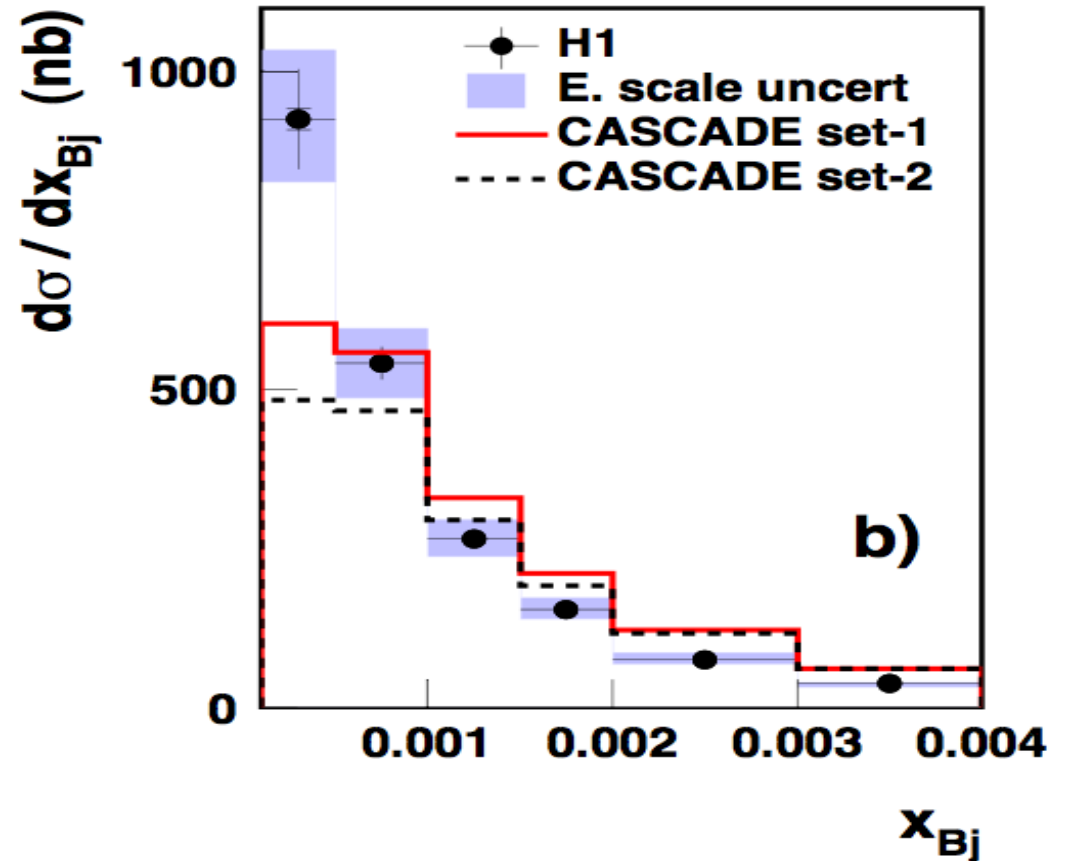
- DIS and forward jet:

$$1.7 < \eta_{jet} < 2.8$$

$$x_{jet} > 0.035$$

$$0.5 < \frac{p_{t, jet}^2}{Q^2} < 5$$

## H1 forward jet data



- "NLO" too low
- Detailed modeling of parton cascades still challenging ...

# Hadronic final states at HERA

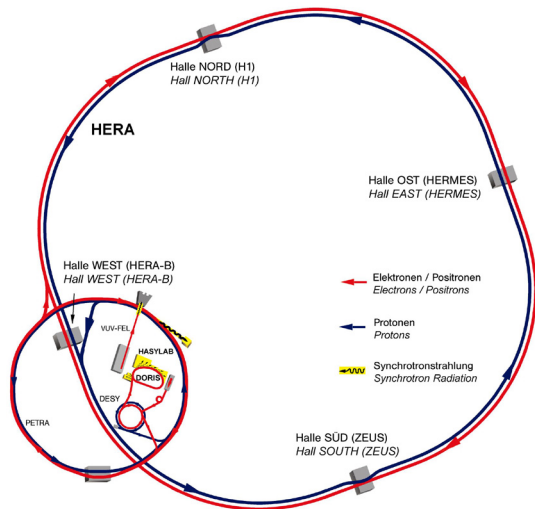
Is that all from HERA  
???

Implications for LHC

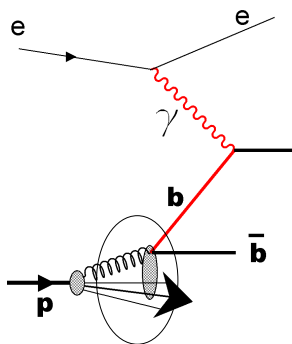
!!!!

# Why HERA and LHC ?

electron proton collider HERA  
 $\sqrt{s} = 320 \text{ GeV}$

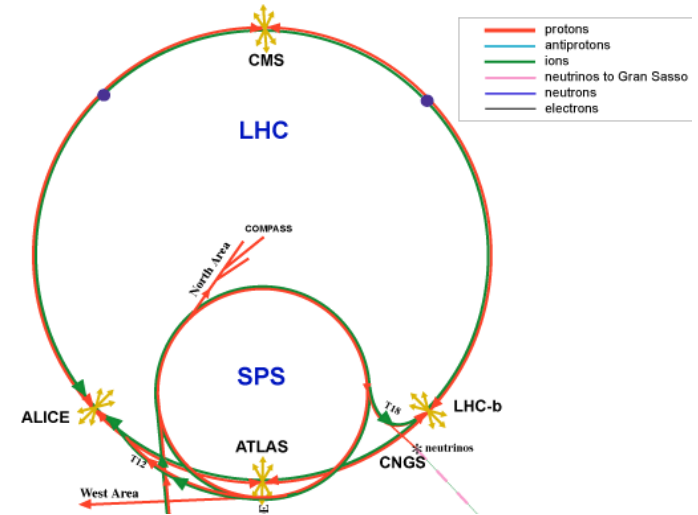


HERA: QCD  
 structure of the proton

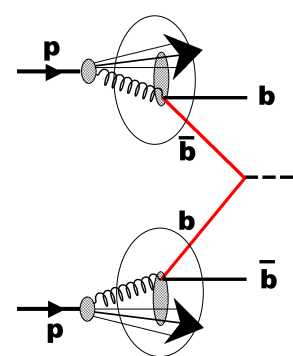


$\sqrt{\frac{Q^2}{s}} \sim 0.01$   
 for  $Q^2 \sim 10 \text{ GeV}^2$

proton proton collider LHC  
 $\sqrt{s} = 14 \text{ TeV}$



LHC: Higgs, SUSY etc.,  
 but mostly QCD...



$\sqrt{\frac{M^2}{s}} \sim 0.01$   
 for  $M \sim 140 \text{ GeV}$

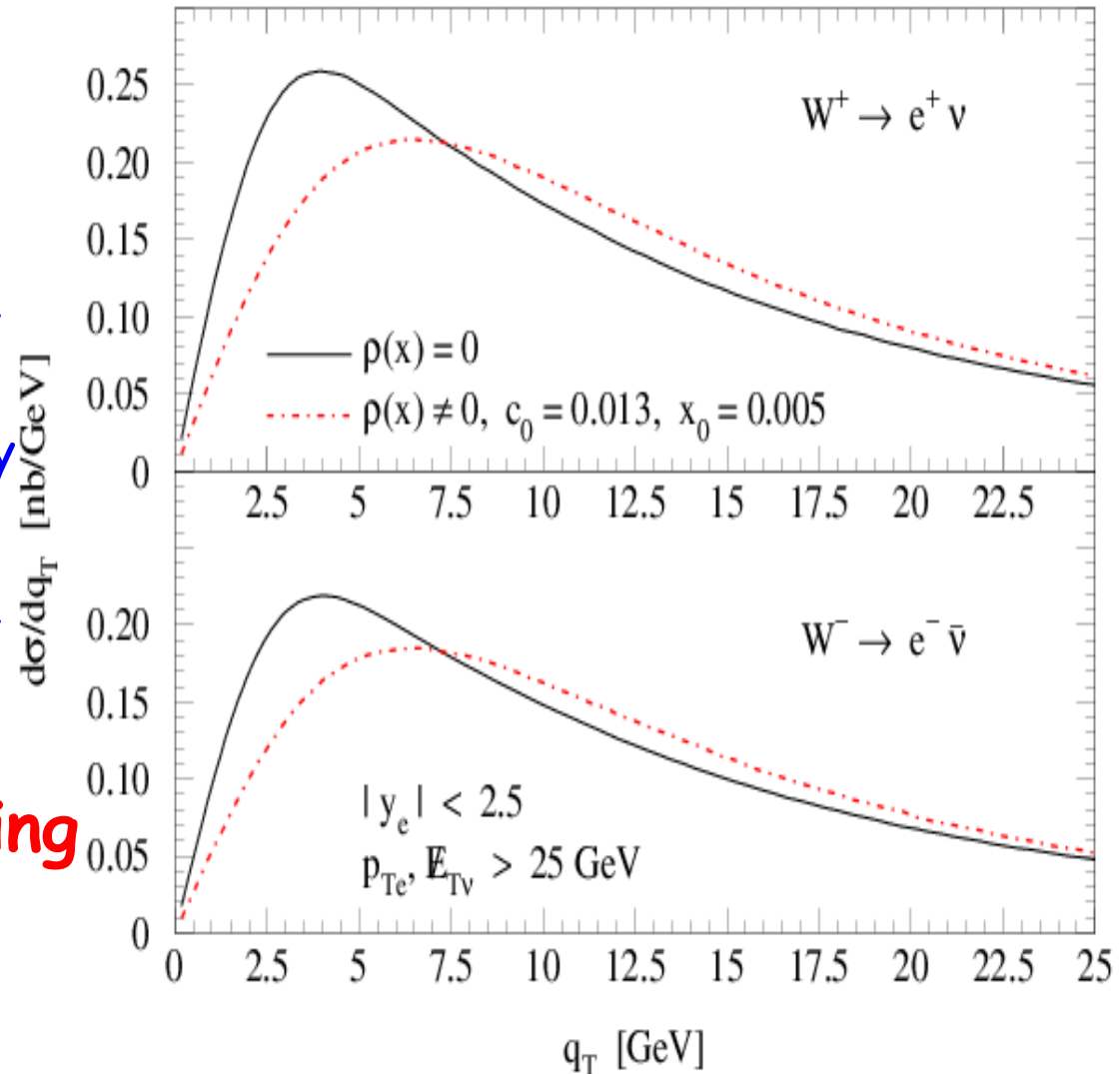
# Qt spectrum: small x improved ...

Berge, Nadolsky, Olness, Yuan  
hep-ph/0410375

- in standard  $p_+$  resummation, no small  $x$  effects are included.
- at large energies (small  $x$ ) BFKL effects might play a role... diffusion of transverse momenta,  $q_T$  broadening...
- obtain effective  $p_T$ -broadening by HERA data on transverse energy flow... include that for  $q_T$  spectra of  $W/Z$  (Berge, Nadolsky, Olness, Yuan hep-ph/0410375)

→ **Interesting physics coming with hard QCD processes !!!!**

$p\bar{p} \rightarrow W X \rightarrow e\nu X$  ( $\sqrt{s} = 14$  TeV)



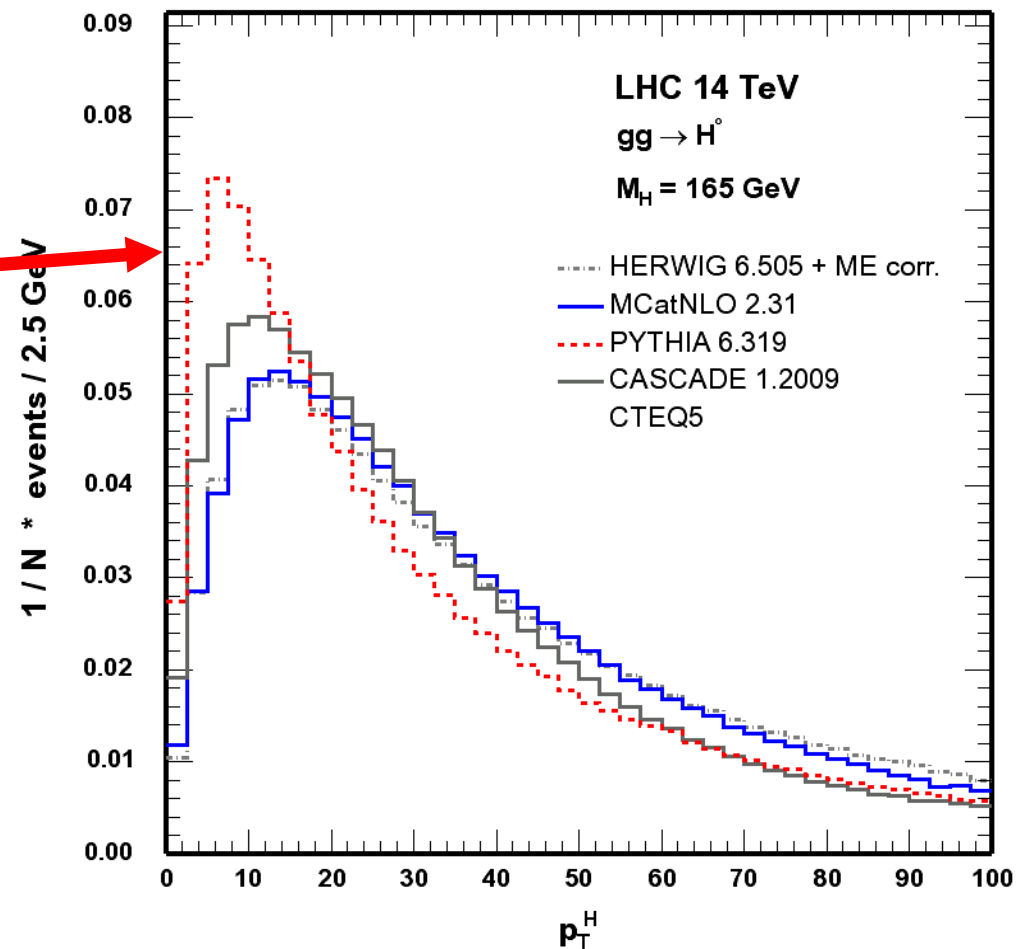
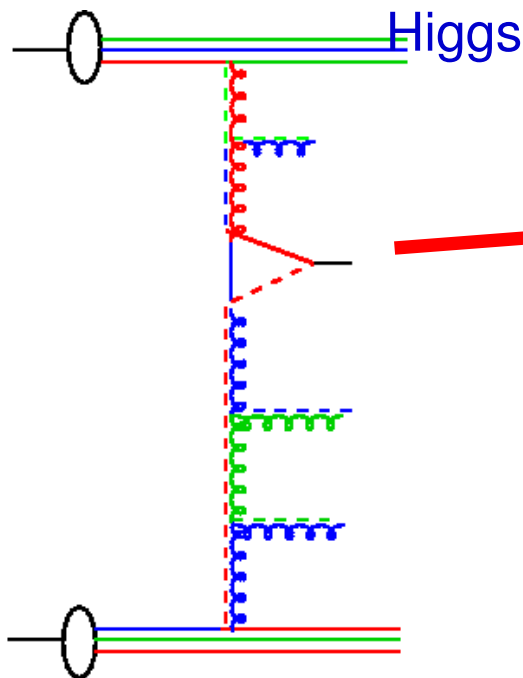


# $k_{\perp}$ effects at HERA and LHC

from G. Davatz

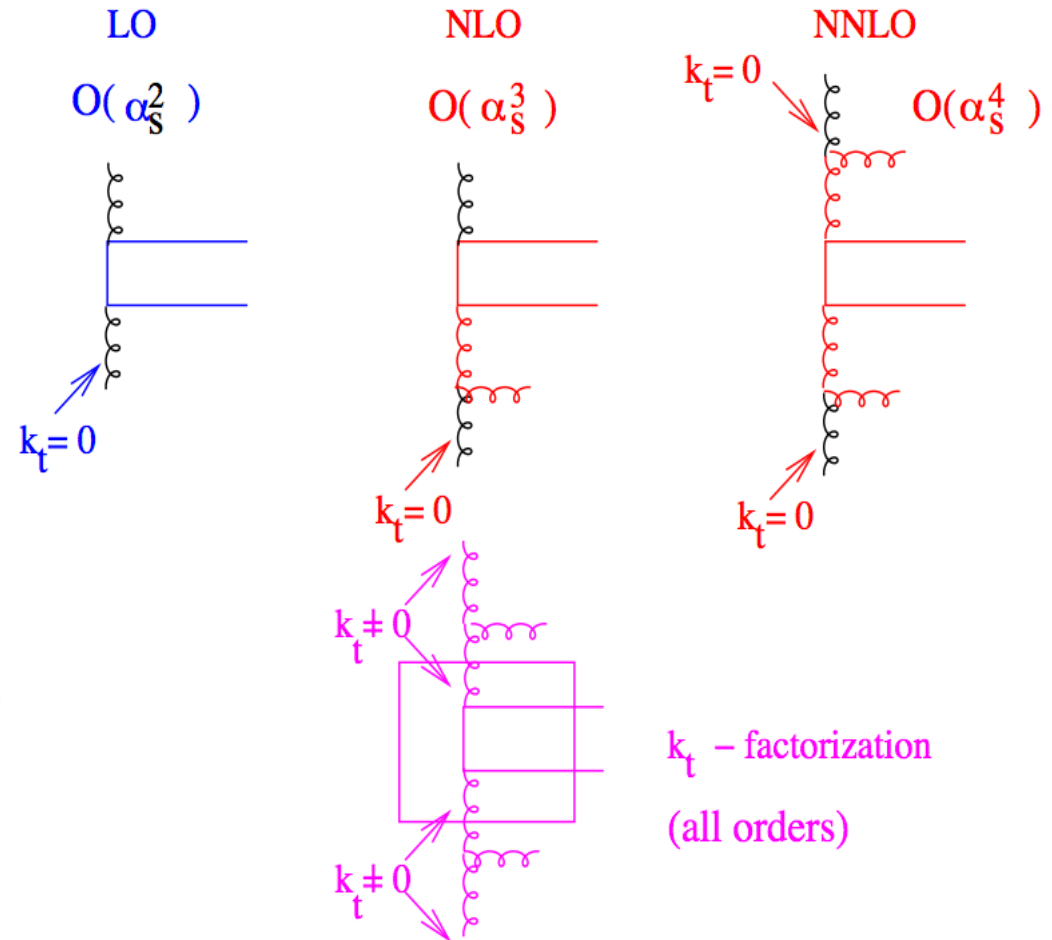
Do we understand the  $p_{\perp}$  spectrum of Higgs at LHC?

Important for the  $gg \rightarrow \text{Higgs} \rightarrow WW \rightarrow l\nu l\nu$  to understand the jet-veto for  $tt$  suppression...



# uPDFs and NLO calculations

- fit of uPDF to inclusive structure functions / x-sections used to determine normalization
  - includes "all-orders" !!!!
- off-shell matrix element simulates part of real NLO corrections
  - study of scale dependence
  - compare to coll. NLO calculations
  - check with benchmark x-sections

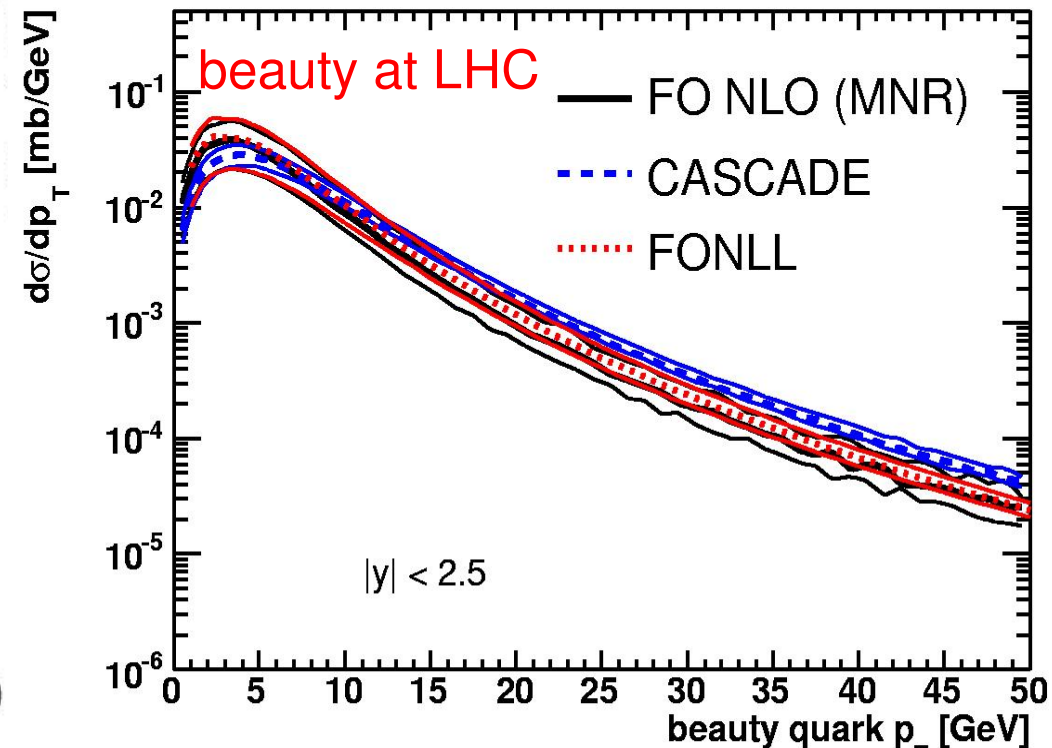
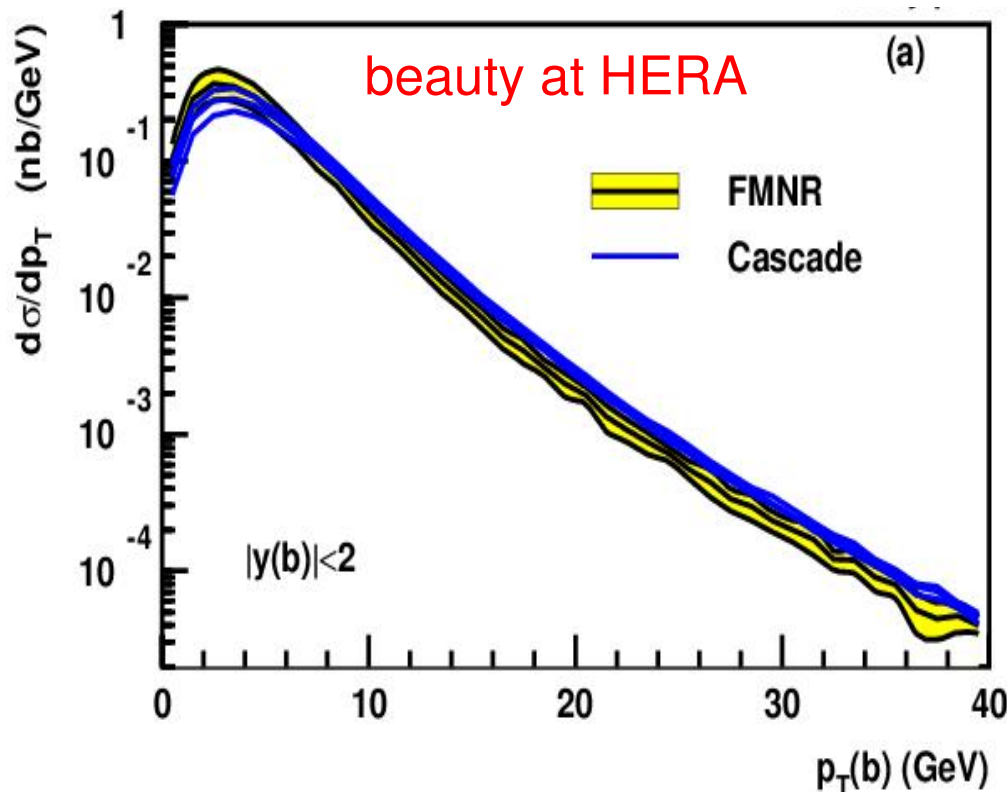


# Benchmarks: beauty at HERA and LHC

from Proceedings of the HERA-LHC workshop hep-ph/0601013

## Cross sections at parton level in central region

MNR (massive NLO) - FONLL (matched NLL) - CASCADE (uPDF)



➔ **“Perfect” agreement of NLO(FMNR) calculation with CASCADE using uPDFs !!!**

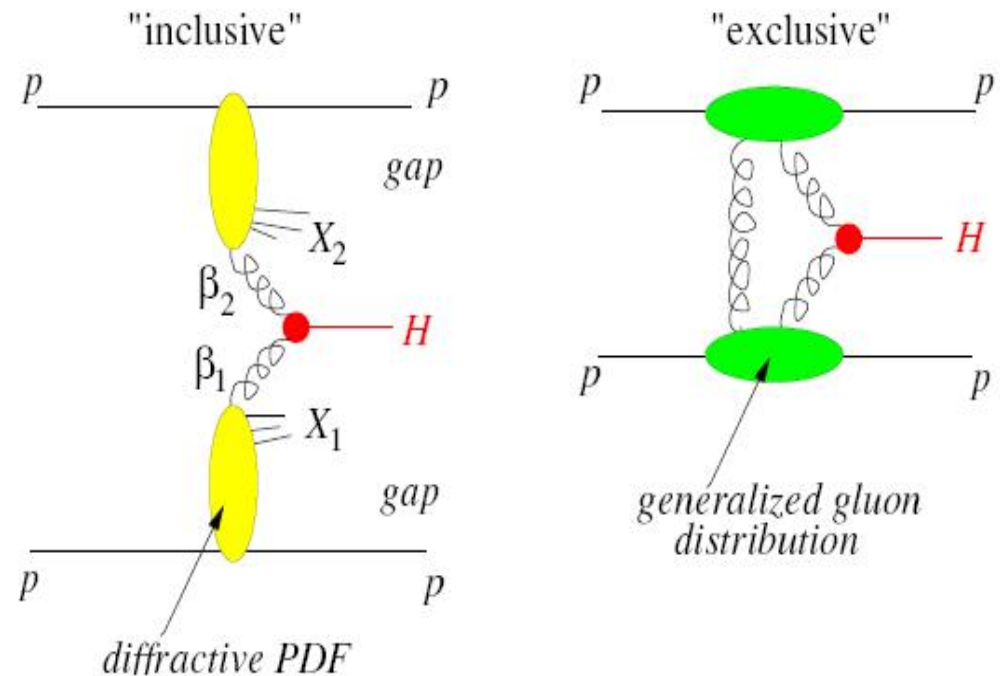
Do we have now all  
parton densities  
considered ?

# Parton Density Functions and all that

- collinear PDFs
- uPDFs (single and double unintegrated)

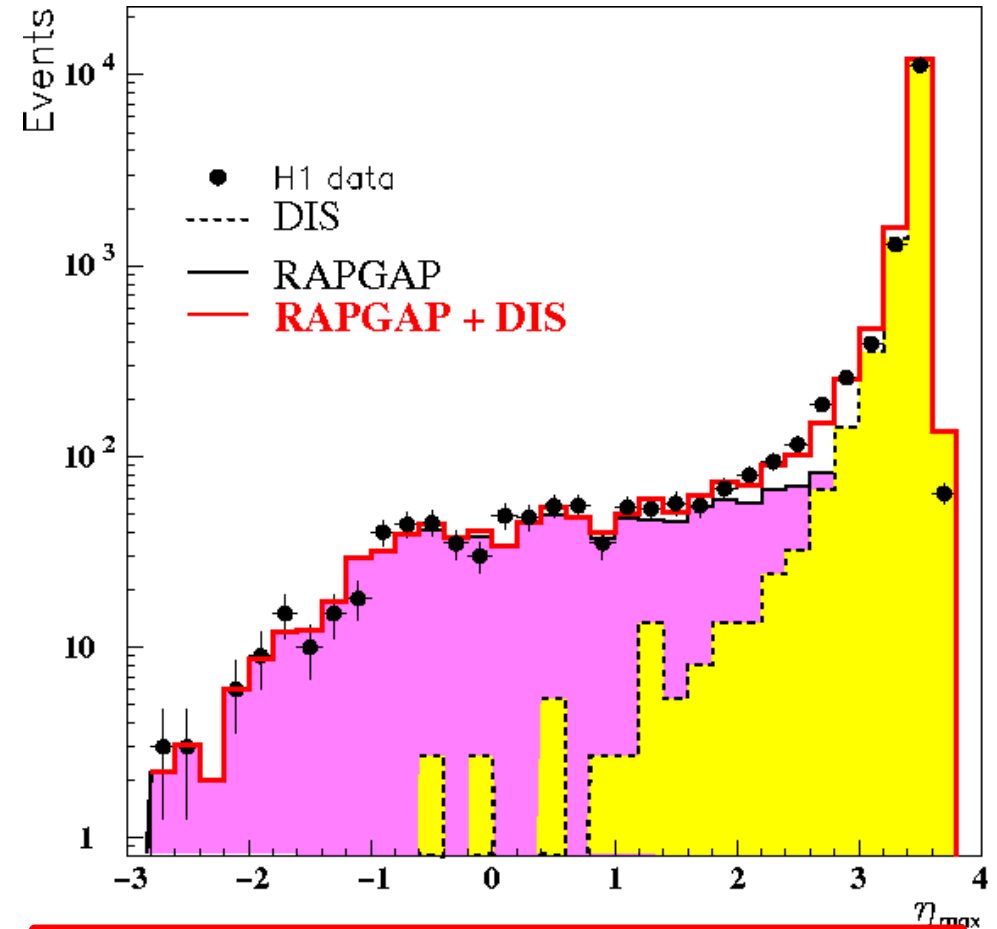
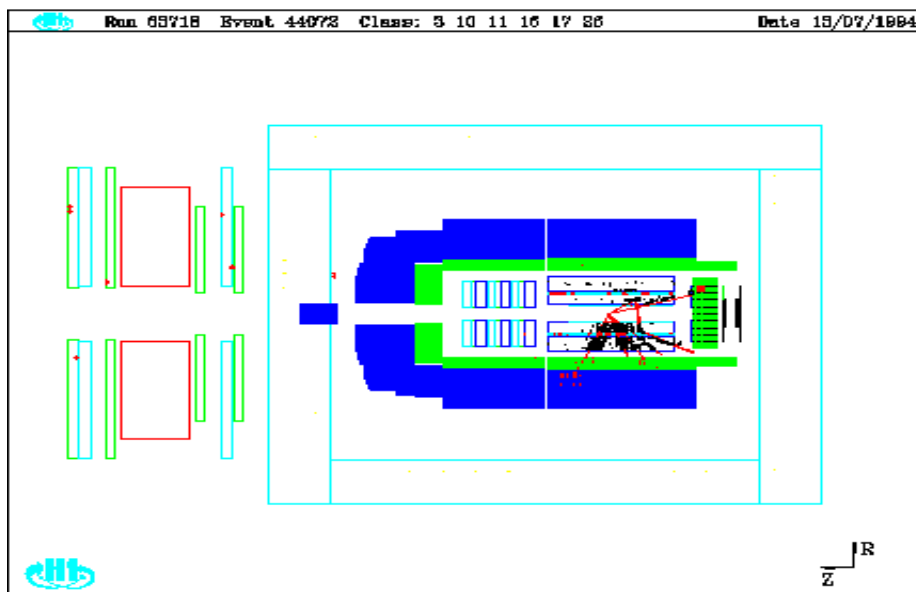
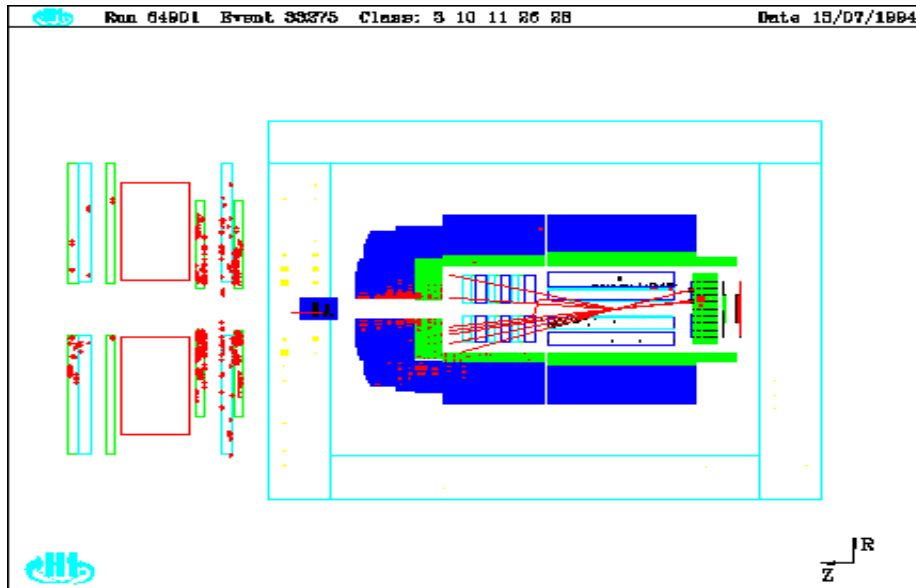
## Exclusive Higgs production

- diffractive and generalized PDFs



# Rapidity Gap Events

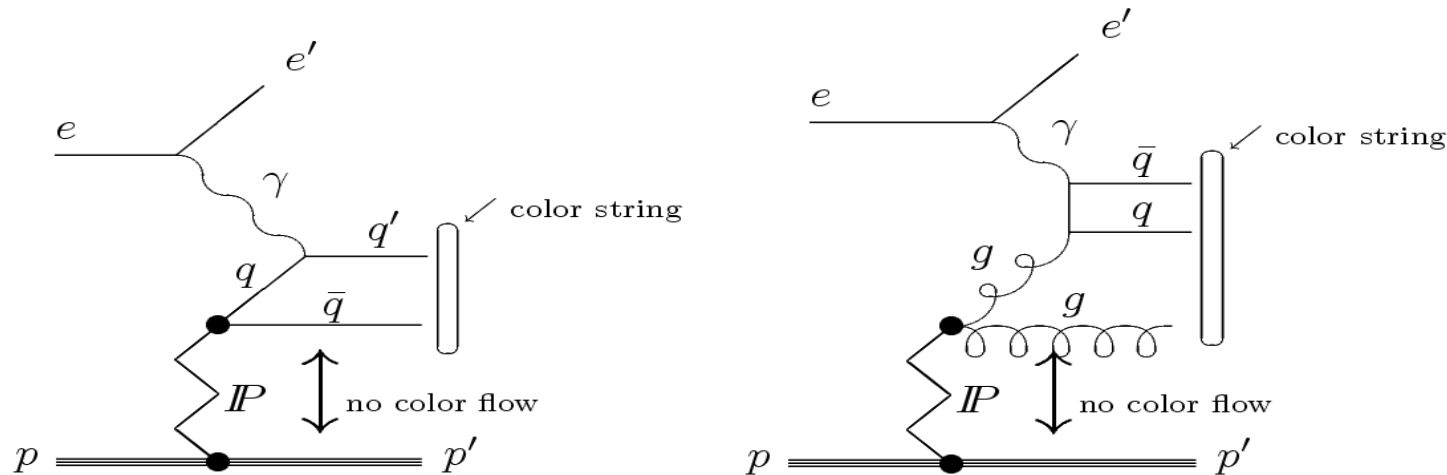
H1 Collaboration, desy 94-133



- (Re)Discoveries at HERA  
.... in 1994 ..
- Diffraction in DIS !!!!!

# The Ingelman-Schlein of diffraction

- Ingelman Schlein (IS) model for diffractive DIS



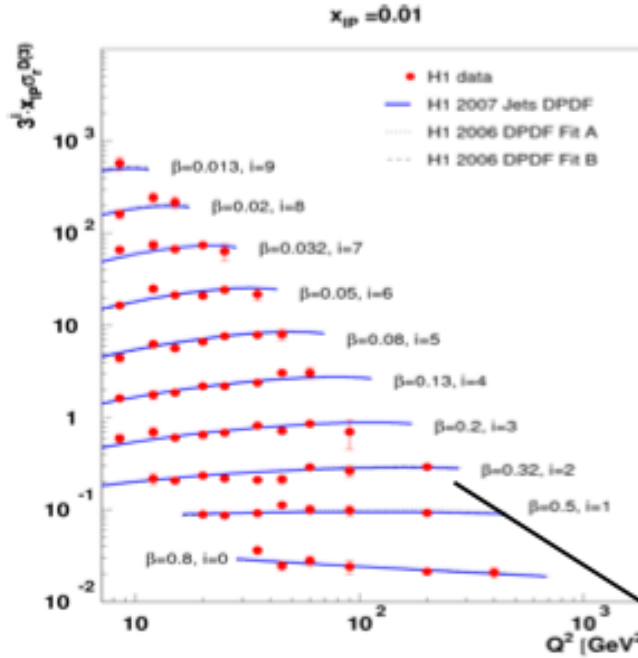
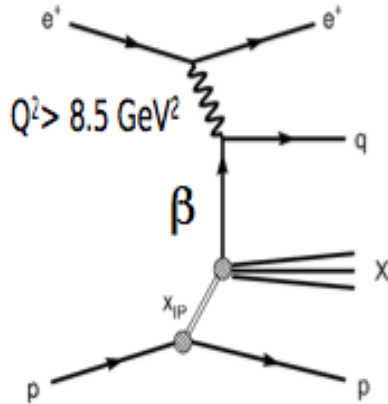
- use hard processes as in non-diffractive DIS
- use diffractive PDFs (example pomeron flux and  $F_2^{\text{pom}}$ )
- additional variables:

$$x_{IP} \beta = x_{Bj} = \frac{Q^2}{2p \cdot q}$$

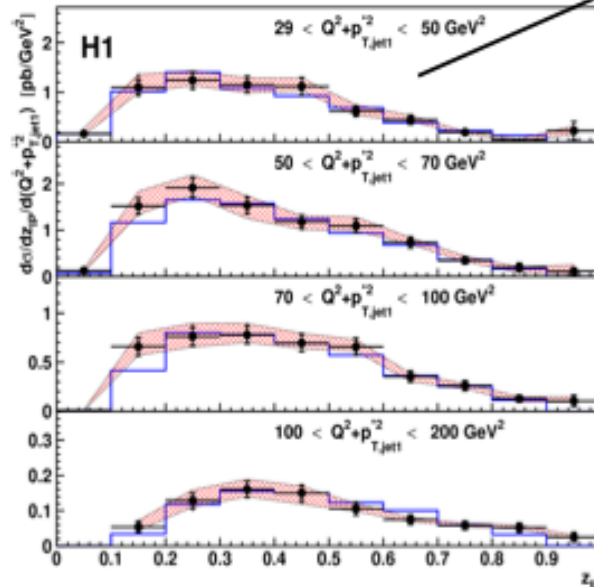
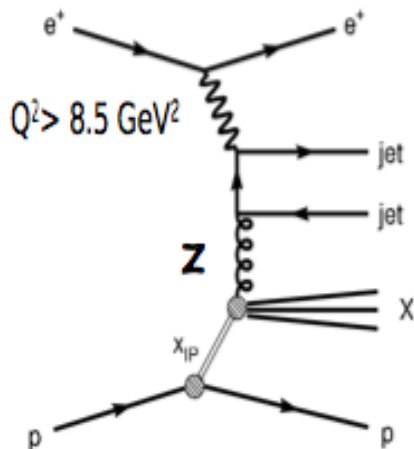
# Diffraction PDF

from O. Behnke, eds07

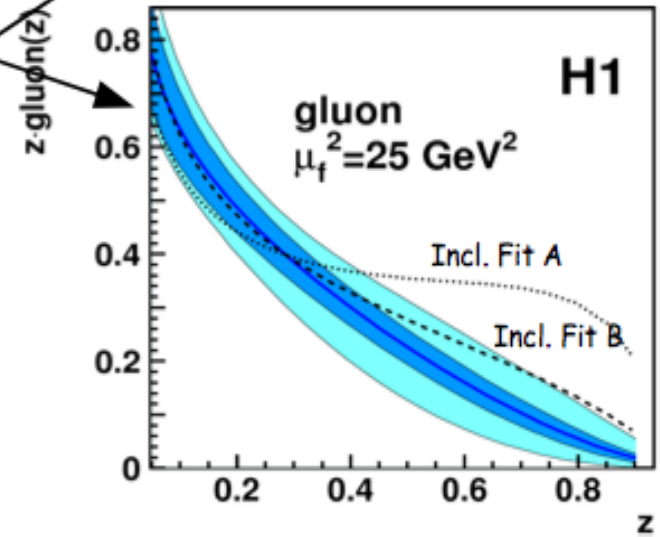
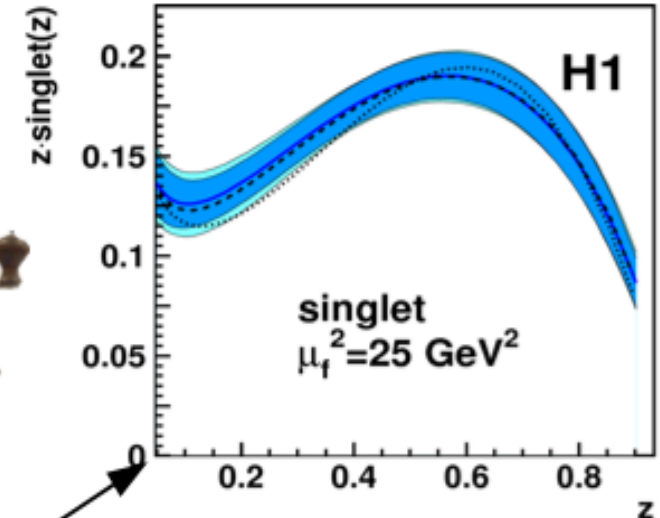
## Inclusive diffr.



## New: add info from diffractive dijets



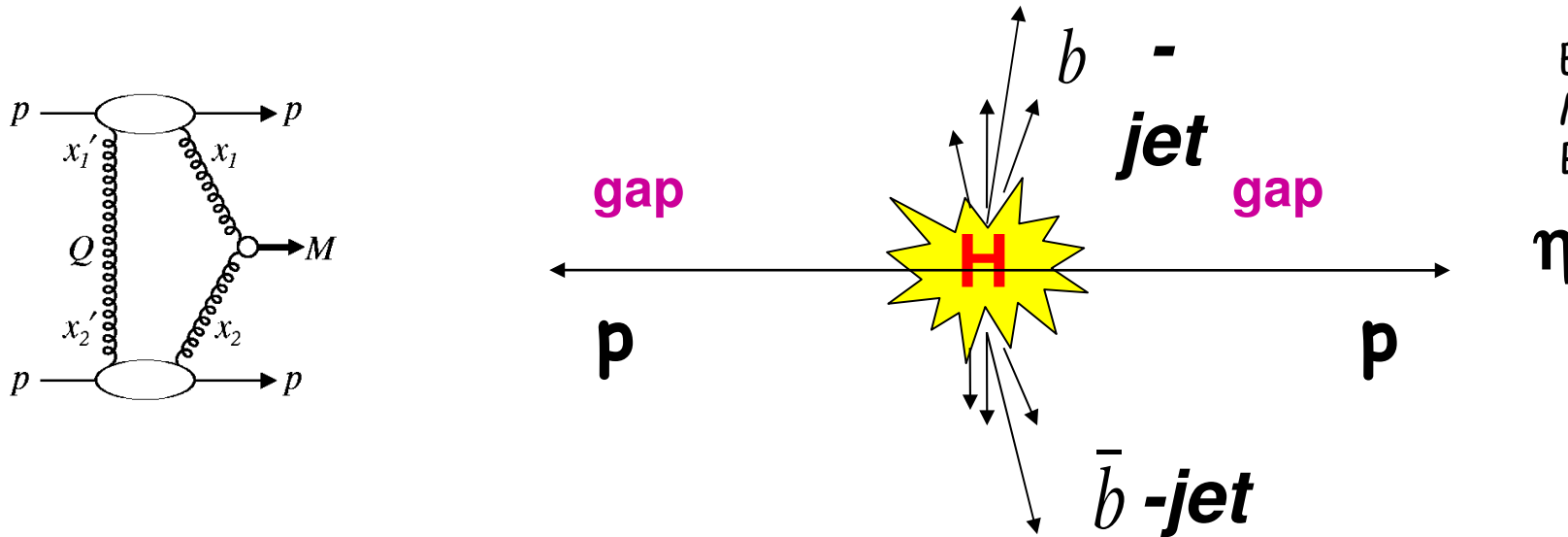
**NLO  
FIT**



→ Consistent picture, improved gluon density



# Diffractive Higgs Production



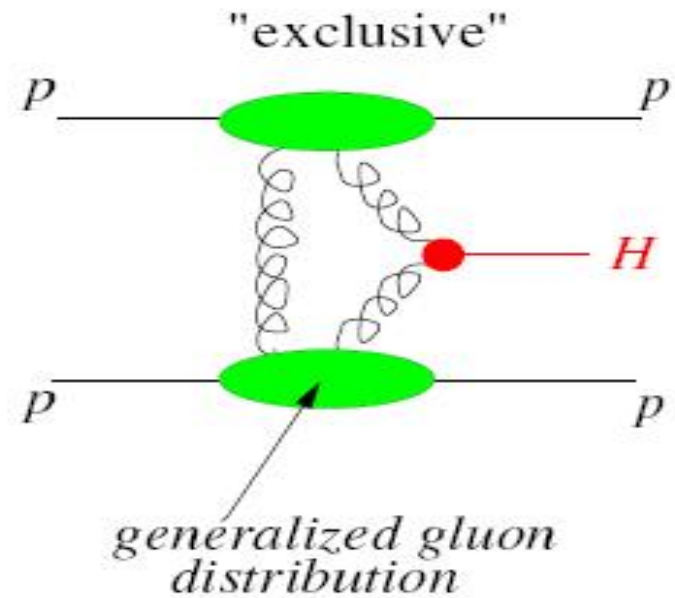
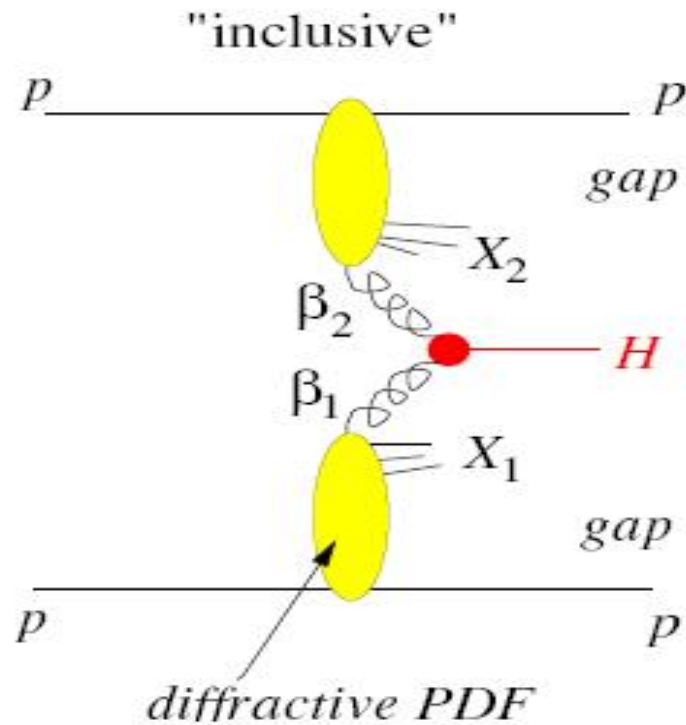
E.g. V. Khoze et al  
M. Boonekamp et al.  
B. Cox et al. ...

$$M_H^2 = (p + \bar{p} - p' - \bar{p}')^2$$

- Exclusive diffractive Higgs production  $p + p \rightarrow p + H + p$  2-10 fb
- Inclusive diffractive Higgs production  $pp \rightarrow p + X + H + Y + p$  O(100) fb
- Advantages: Mass resolution  
from energy of protons determine mass  
precise mass determination
- Sensitive to un-integrated pdfs

# Exclusive Higgs and diff. at HERA

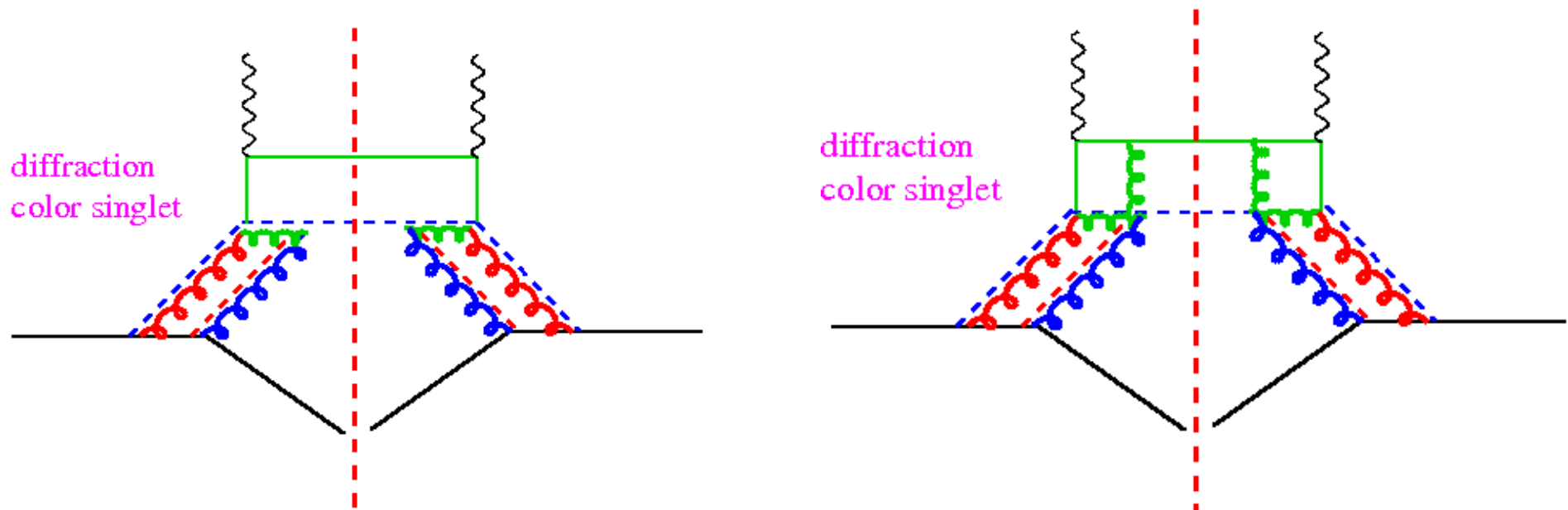
from M. Diehl



- Inclusive diff. events become background to exclusive one, when remnant systems  $X$  become soft...
- relevant region for diff. Pdfs:
- $\beta \rightarrow 1$  and  $Q^2 \sim M_h^2$
- measure diff pdf at highest  $Q^2$  and highest  $\beta$  ....

# Understanding diffraction

- simplest model for Pomeron: 2 gluon system



Why we need to care  
about diffraction  
and all that ?

# Towards understanding of all that ...

Bartels, Kowalski, Sabio-Vera

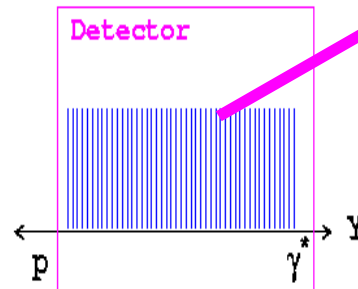
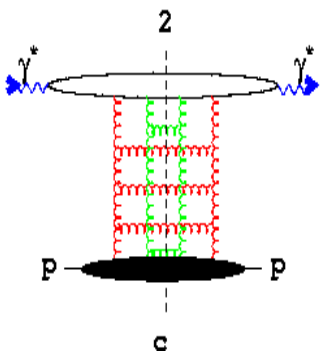
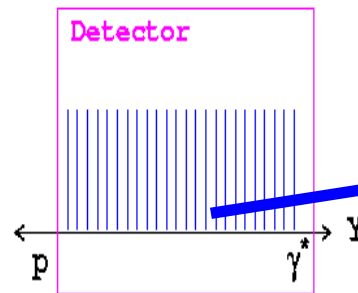
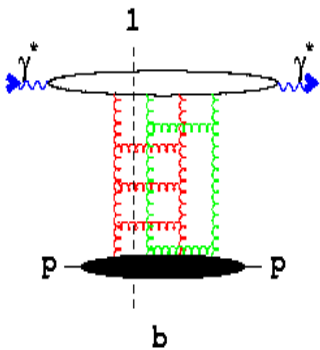
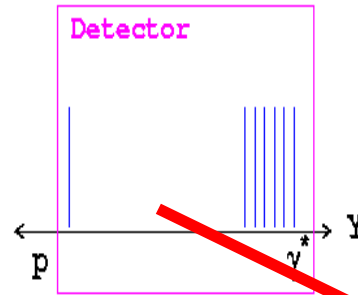
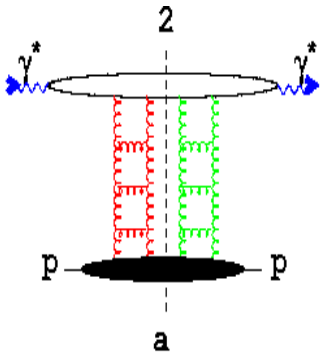
- Cutting rules (AGK) extended to QCD
- Relate **diffraction**, saturation and **multiple scatterings**
- All from the same amplitude, but different factors:

- +1 **Diffraction**
- - 4 **Saturation**
- +2 **Multiple Interactions**

- Extended now also to pp !!!!
- further work needed ...

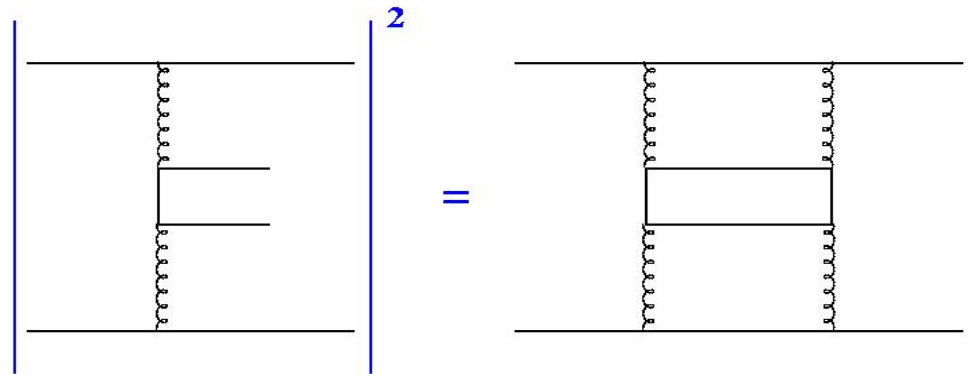
→ **HERA is the place to understand MI !!!!**

→ **Towards the description of "everything" !!!!!**

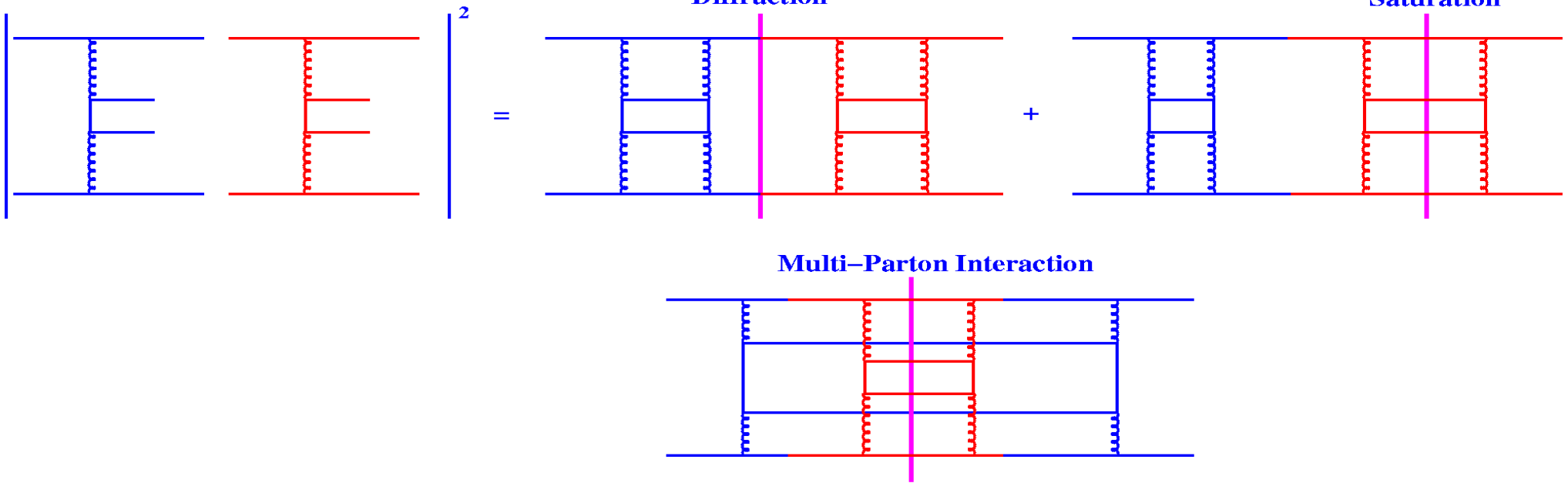


# Toy Model for multi-parton scattering

- where is relation of diffraction - multiple scatterings - saturation coming from ?
- single parton exchange:



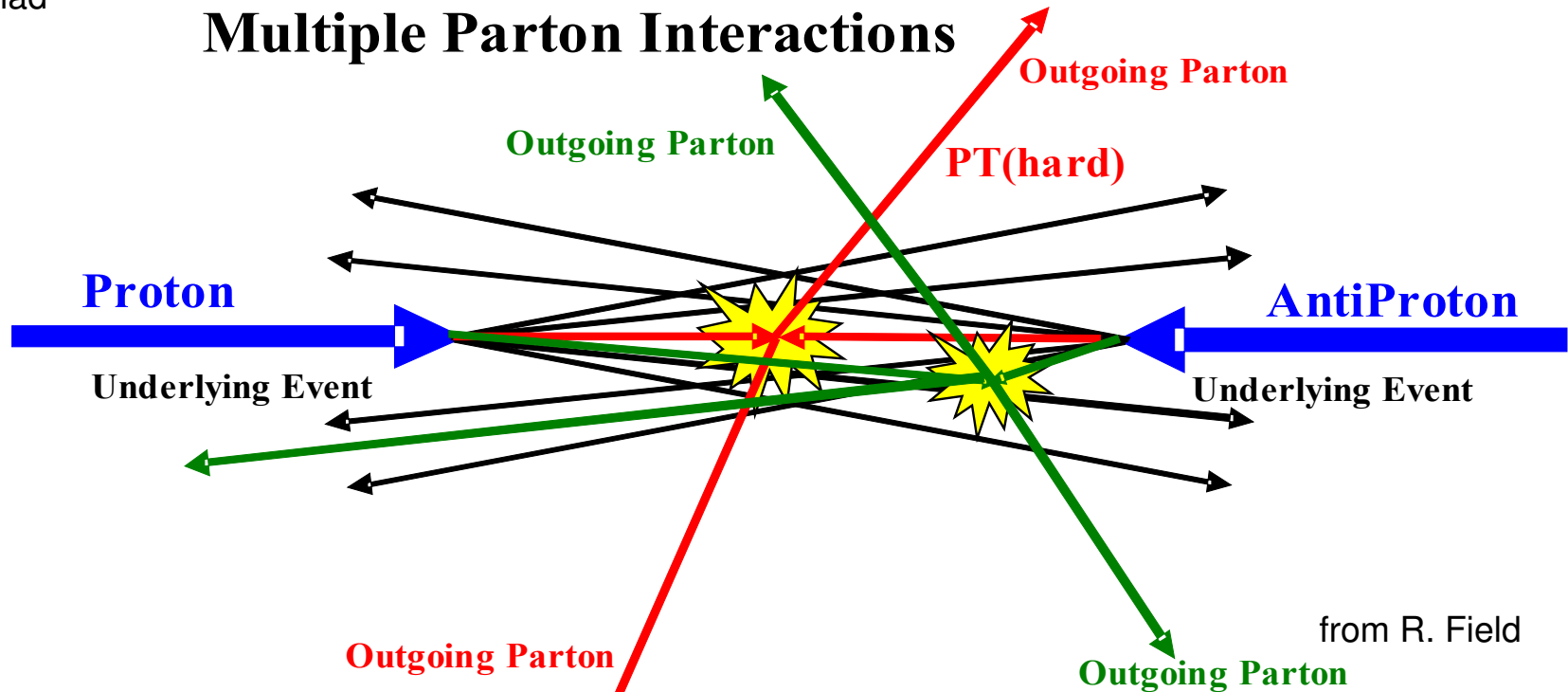
- 2-parton exchange:



Is this at all  
relevant at LHC?

# Multiparton Interactions

from L. Loennblad



What is the underlying event (UE)?

→ Everything, except the *LO* process we're currently interested in

- *parton showers*
- *additional remnant - remnant interactions (multi-parton interactions, soft/hard)*

**X** NOT pile-up events (luminosity dependent)



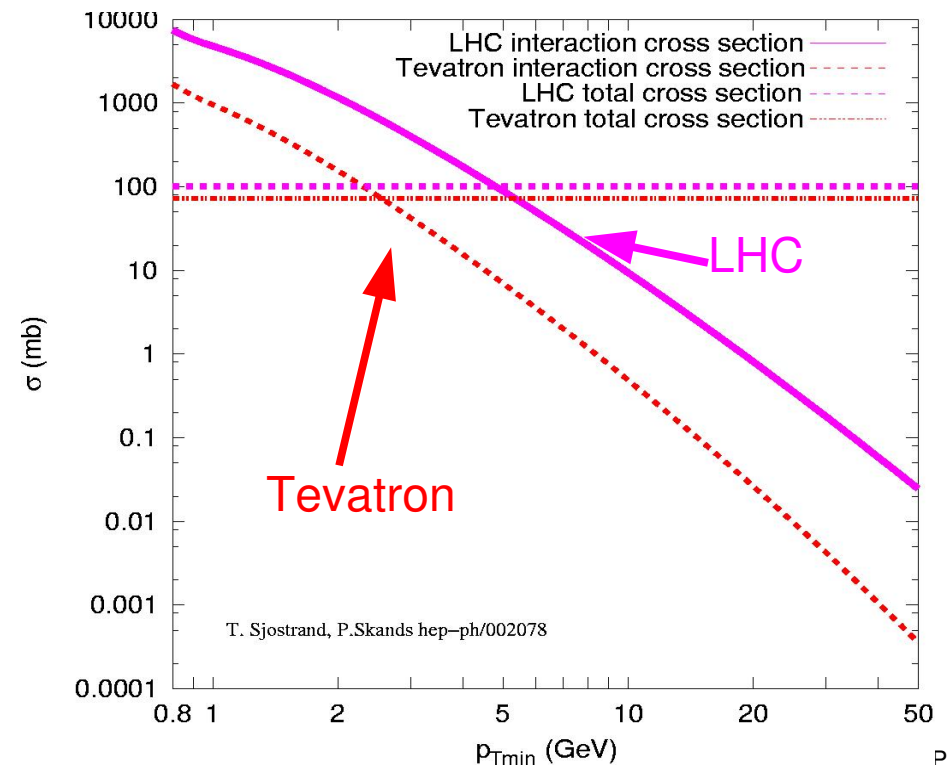
# Underlying event - Multiple Interaction

- Basic partonic perturbative cross section

$$\sigma_{\text{hard}}(p_{\perp \text{min}}^2) = \int_{p_{\perp \text{min}}^2} \frac{d\sigma_{\text{hard}}(p_{\perp}^2)}{dp_{\perp}^2} dp_{\perp}^2$$

- diverges faster than  $1/p_{\perp \text{min}}^2$  as  $p_{\perp \text{min}} \rightarrow 0$  and exceeds eventually total inelastic (non-diffractive) cross section

- Interaction x-section exceeds total xsection
- happens well above  $\lambda_{QCD}$
- still in perturbative region



# Underlying event–Multiparton Interaction

- Basic partonic perturbative cross section

$$\sigma_{\text{hard}}(p_{\perp \text{min}}^2) = \int_{p_{\perp \text{min}}^2} \frac{d\sigma_{\text{hard}}(p_{\perp}^2)}{dp_{\perp}^2} dp_{\perp}^2$$

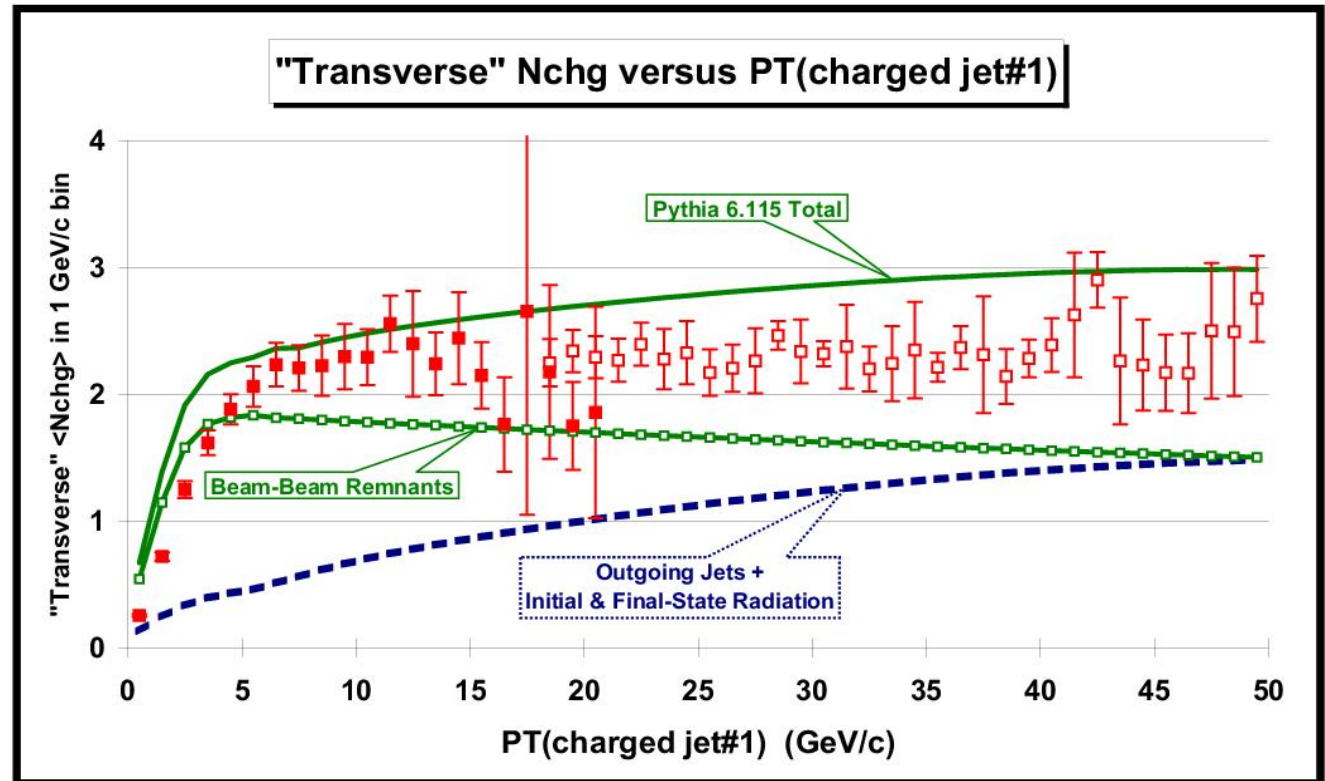
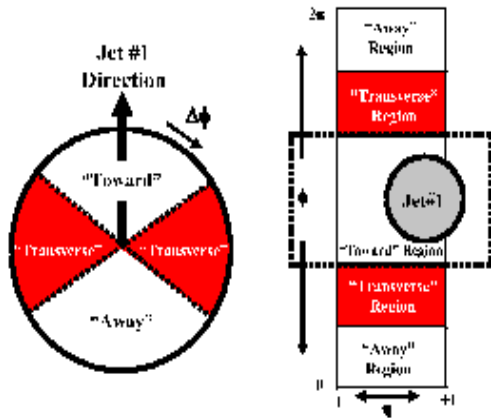
- diverges faster than  $1/p_{\perp \text{min}}^2$  as  $p_{\perp \text{min}} \rightarrow 0$  and exceeds eventually total inelastic (non-diffractive) cross section, resulting in more than 1 interaction per event (multiparton interactions, MI).
- Average number of interactions per event is given by:

$$\langle n \rangle = \frac{\sigma_{\text{hard}}(p_{\perp \text{min}})}{\sigma_{nd}}$$

- It depends on how soft interactions are treated, **BUT** also on the parton densities and factorization scheme, parton evolution (DGLAP/BFKL) !!!!!!!

# Multiparton Interactions at CDF

CDF coll. PRD 65, 092002 (2002)



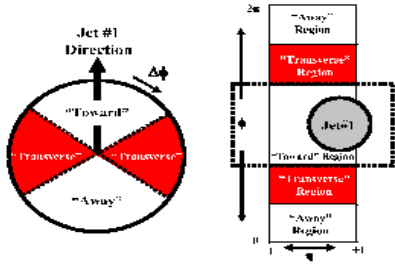
- Multiplicity distribution in region transverse to jet can only be described by adding multi-parton interactions (Remnant- Remnant Interactions)



# Multiparton Interactions at LHC

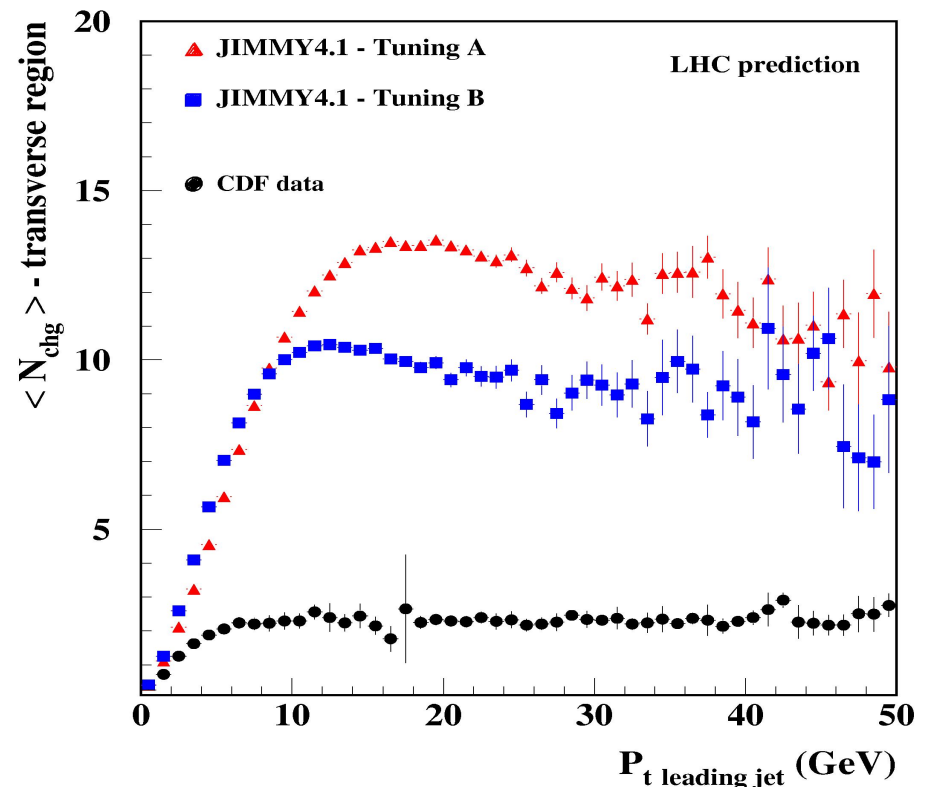
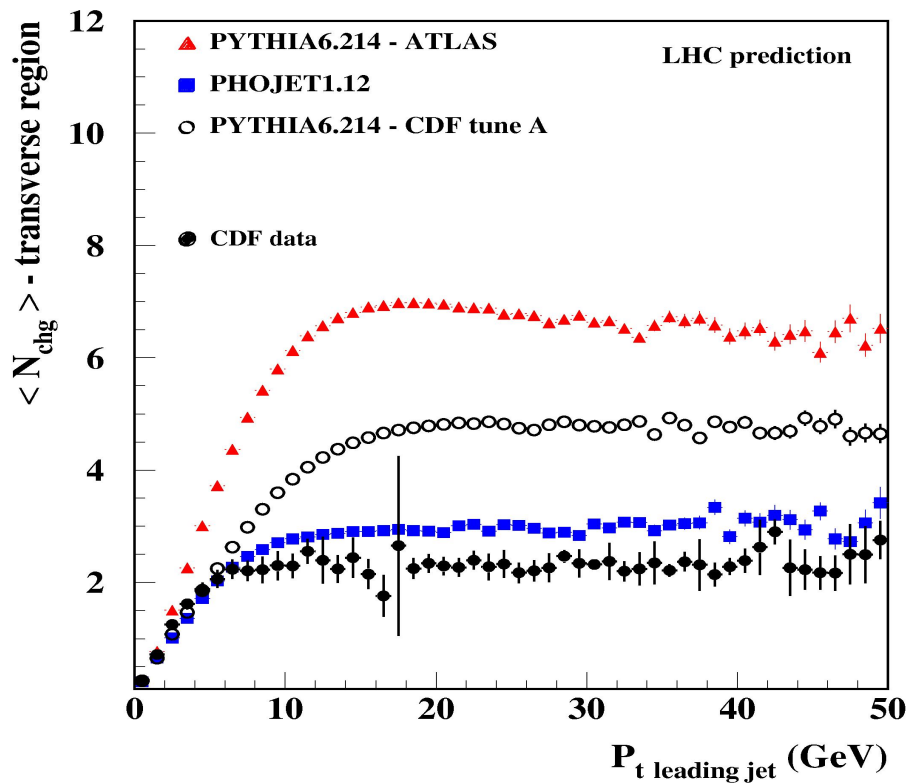
C. Buttar et al in HERA – LHC workshop proceedings hep-ph/0601012

## Charged multiplicities in transverse region



region

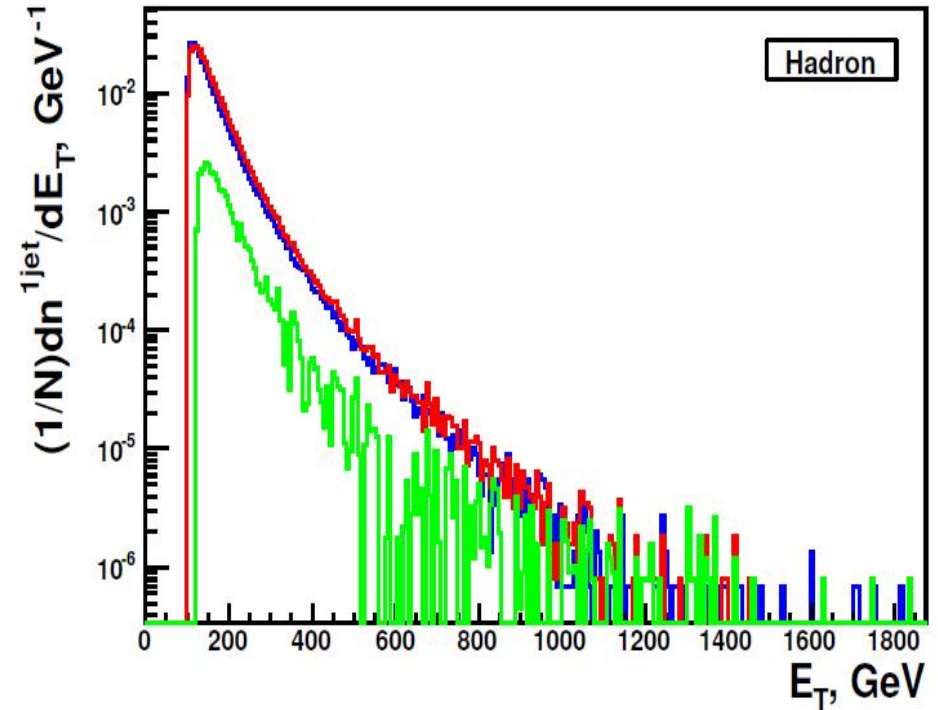
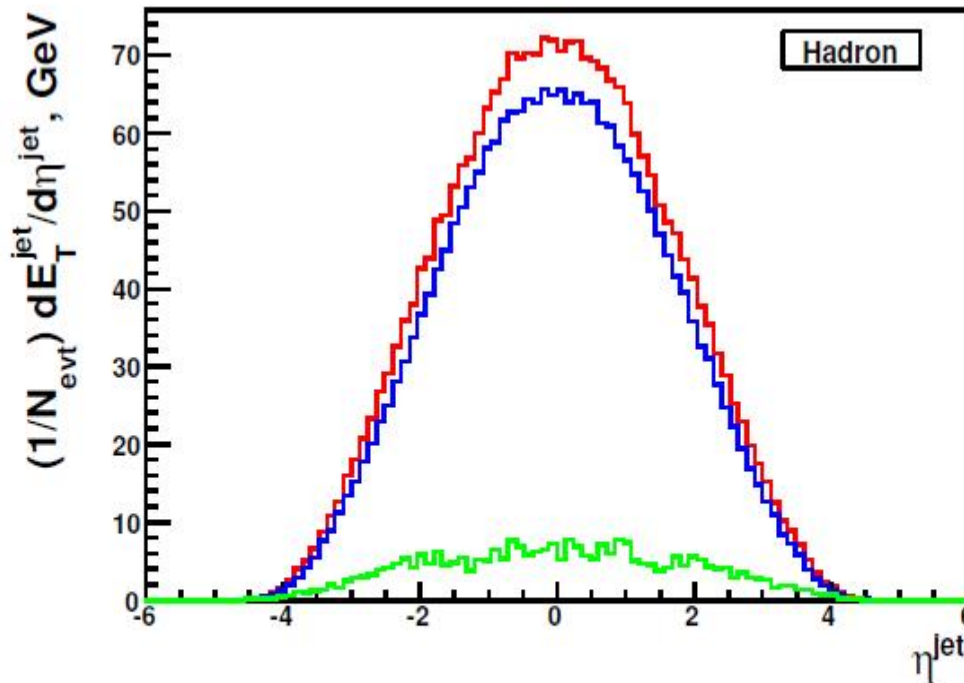
- Models tuned to TeVatron data
- give **HUGE** differences at LHC ...
- **better understand multiple interactions ...**
- **photo-production of jets at HERA** T. Namssoo



# Multiparton Interactions and Jets

P. Starovoitov, T. Carli  
HERA-LHC WS, June 2006

- SHERPA:  $E_T > 100 \text{ GeV}, |\eta| < 5$

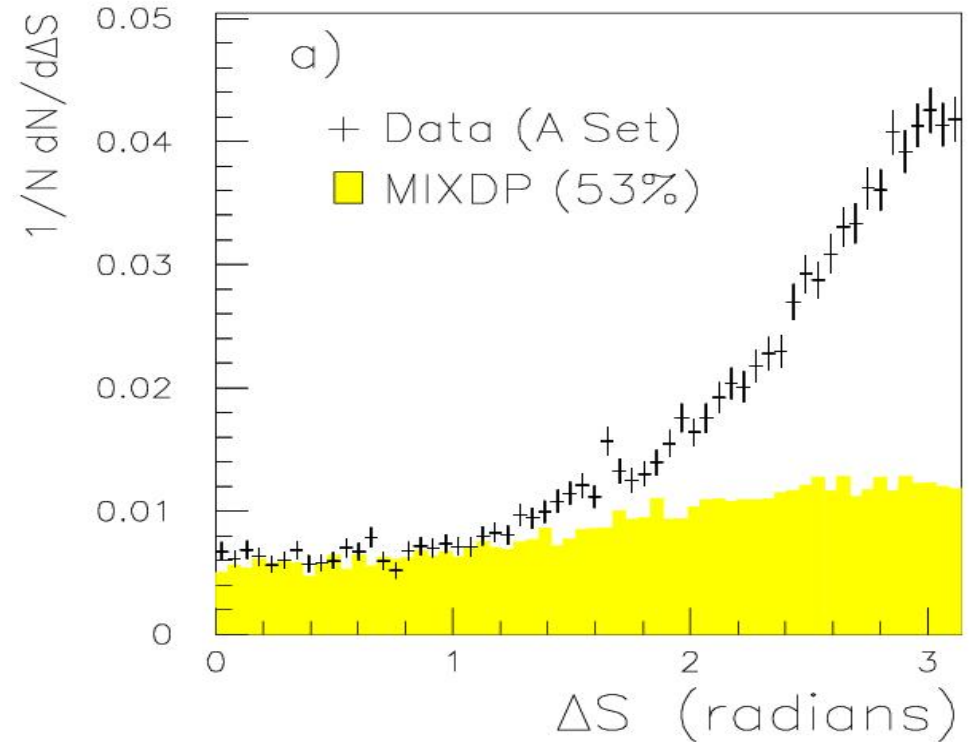
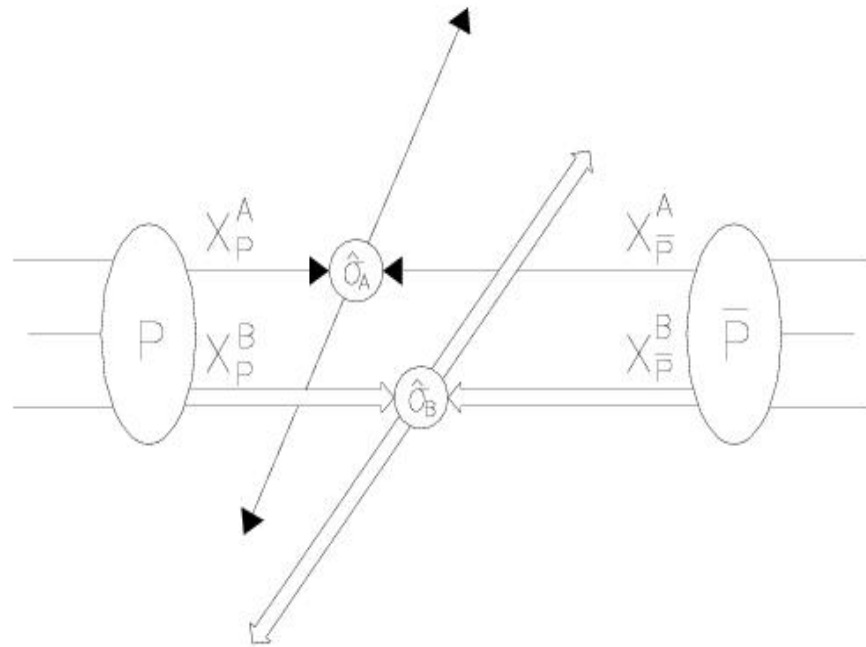


Hard Scale, HS+UE, Difference

- UE contributes  $\sim 10 - 30 \%$  to Jets, even at large  $E_T$  !!!!
- need reliable model for UE
- Factorization ??!!??

# Evidence for Multi-Parton Interactions

CDF coll. PRD 56, 3811 (1997)



- look at  $\gamma + 3$  Jets with

$$E_T^\gamma > 16\text{GeV}$$

$$E_T^{\text{Jets}} > 5\text{GeV}$$

- angular correlation of jet/photon pairs  $\Delta S$
- compare to  $\gamma + 3$  Jets calculation
- **Need > 50 % double parton interaction to describe data**

# Double-Parton Interactions at LHC

- xsection for  $p + p \rightarrow b\bar{b}b\bar{b}$   
single parton exchange (SP)

$$\sigma^{SP} \sim f^2 \hat{\sigma}(2 \rightarrow 4)$$

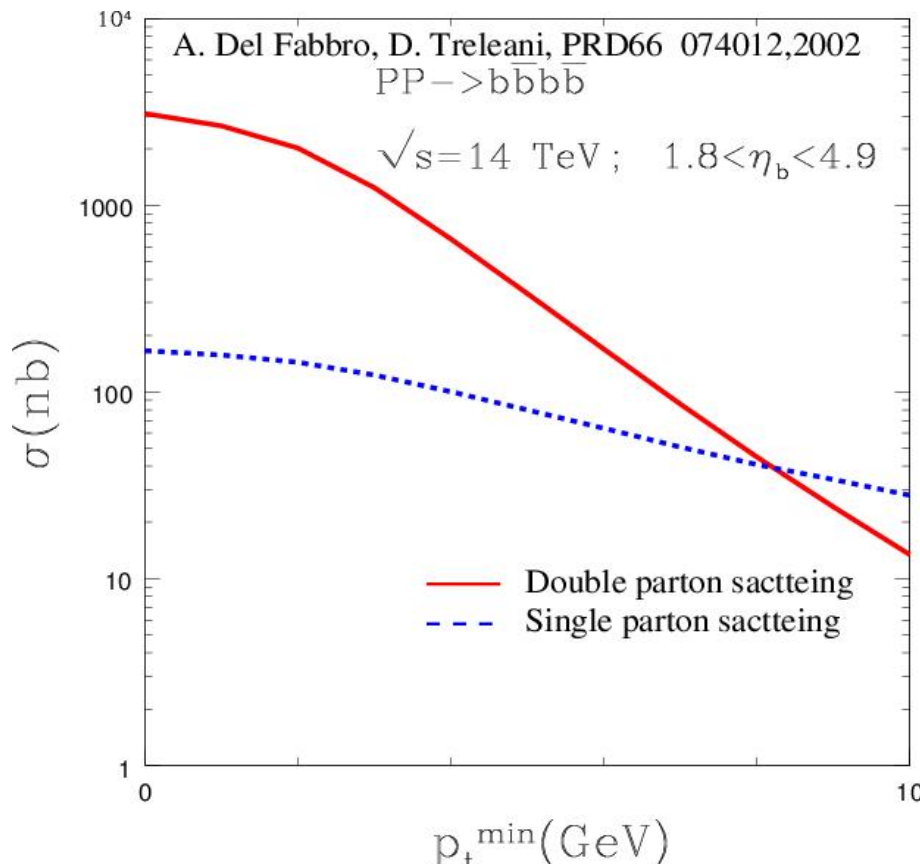
- double parton exchange (DP)

$$\sigma^{DP} \sim f^4 \hat{\sigma}^2(2 \rightarrow 2)$$

- PYTHIA predictions:

$$\sigma^{DP} = 0.8 \dots 11.1 \mu b$$

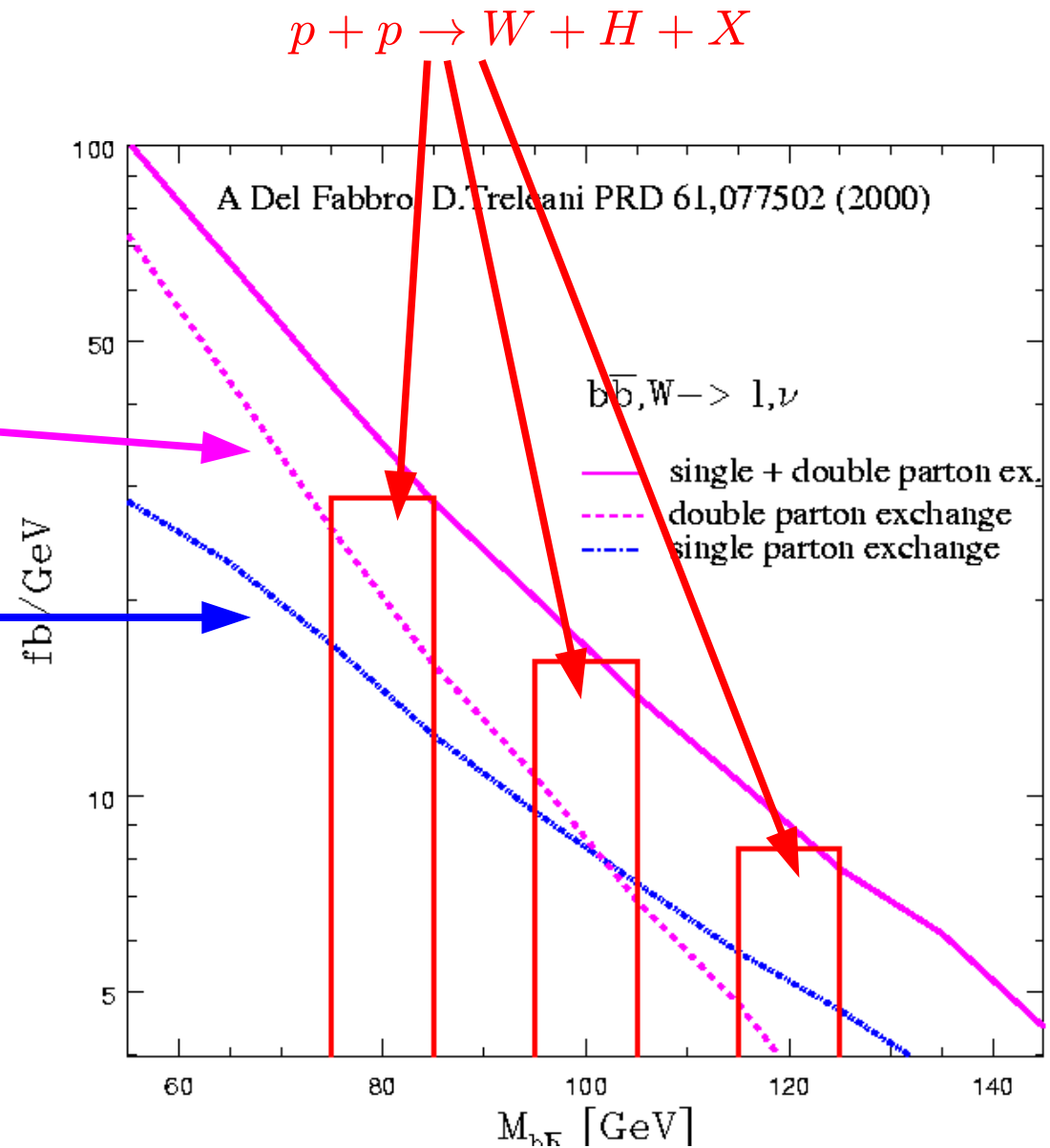
- Depending on model for underlying event/multi-parton interactions...



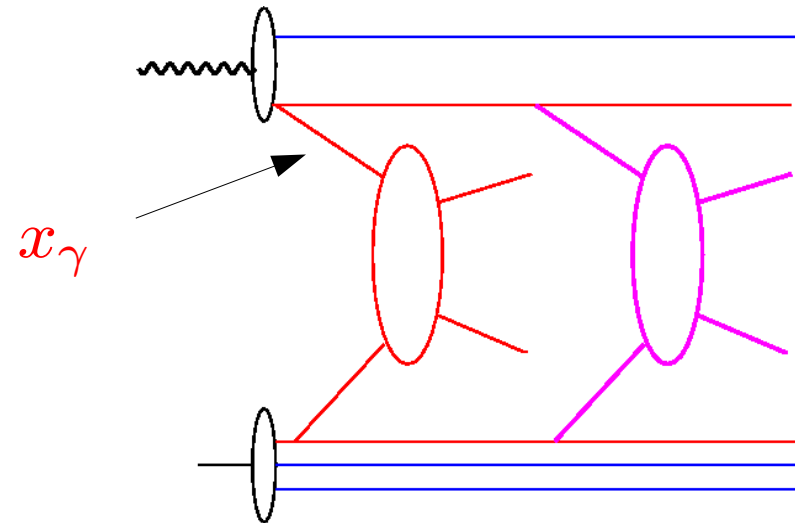
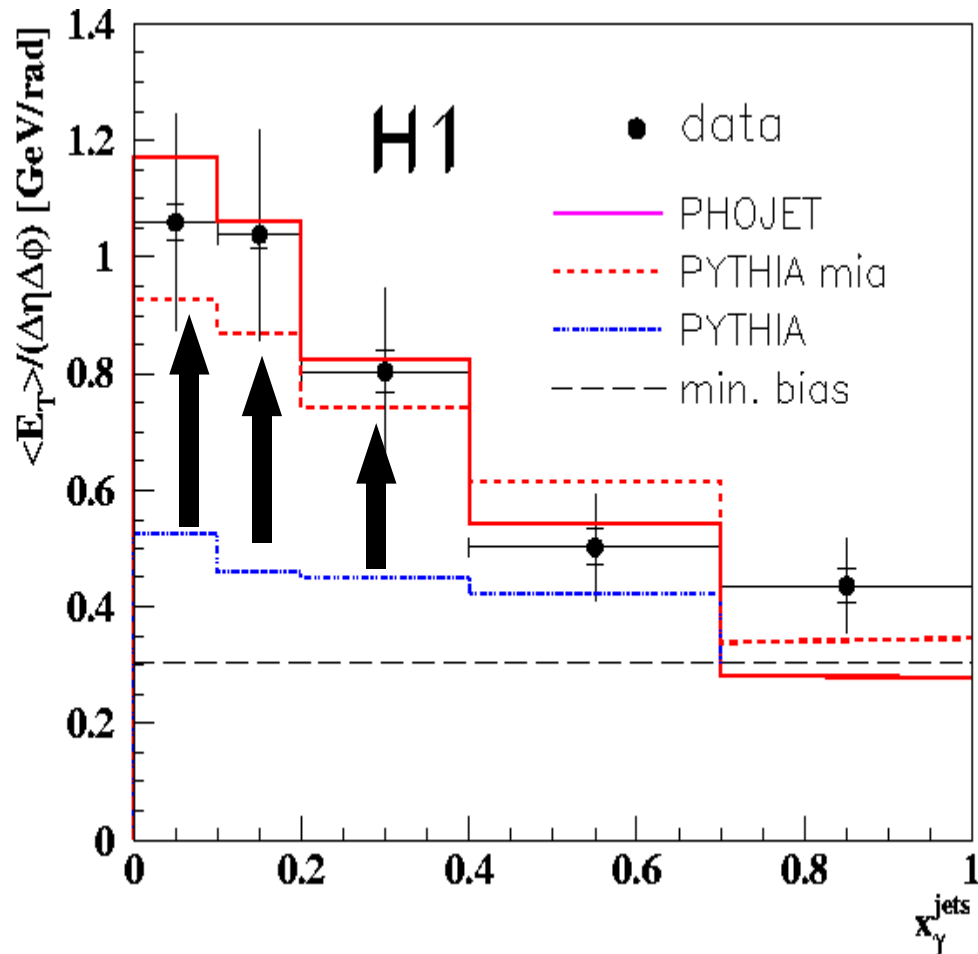


# Multi-Parton Interactions at LHC

- Higgs:  $p + p \rightarrow W + H + X$   
with  $W \rightarrow l\nu$ ,  $H \rightarrow b\bar{b}$
- Double parton scattering:  
→  $p + p \rightarrow b\bar{b}X$   
 $p + p \rightarrow W + X$
- $p + p \rightarrow W + b\bar{b} + X$

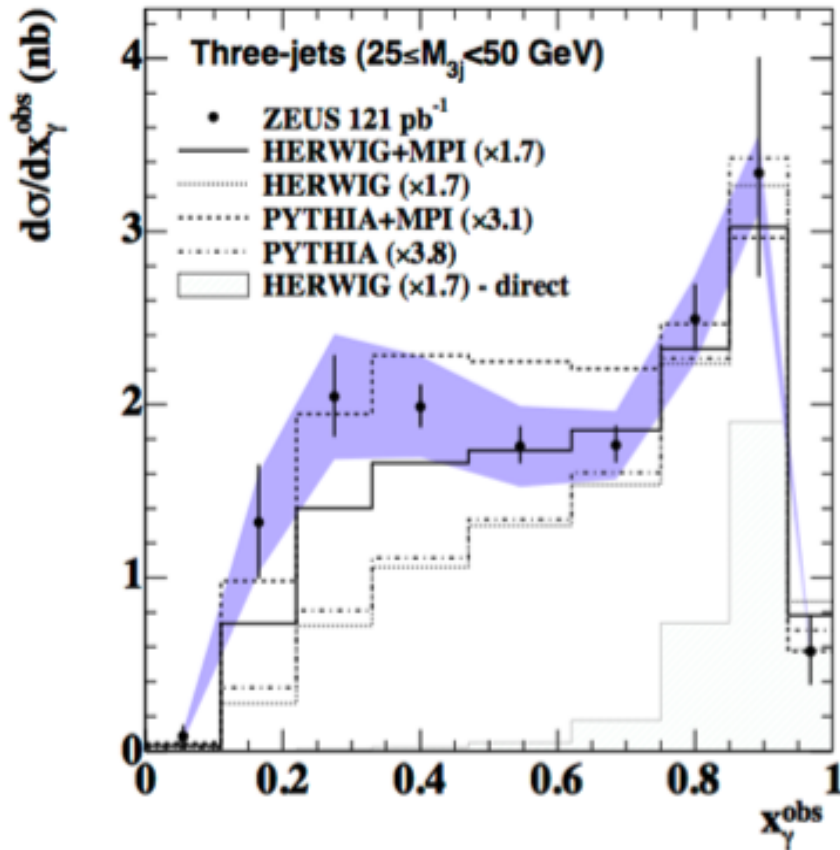


# Multiple Interactions at HERA

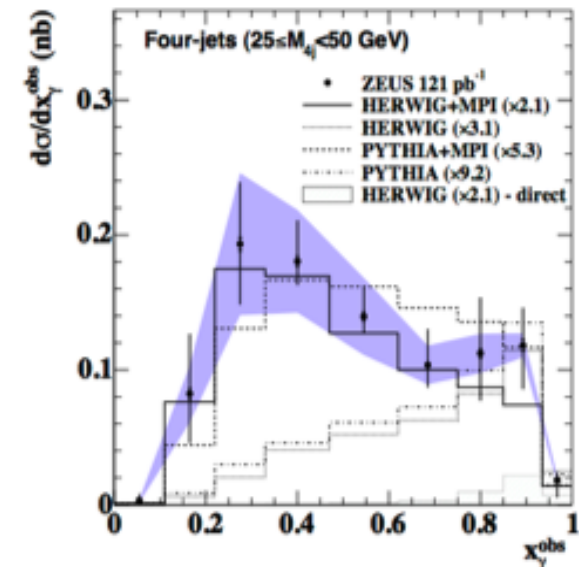
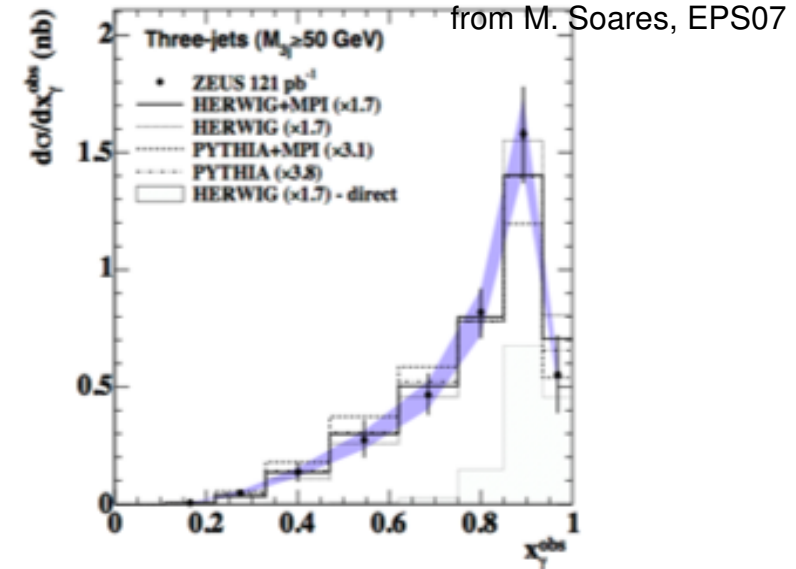


photoproduction is effectively hadron-hadron production...  
 Test and understand multiple interactions at HERA !!!

# Multiple Interactions at HERA



General improvement  
adding MPIs to LO MC



EPS07

Multijet production at HERA

# Multiparton Interactions at LHC

- Multiparton Interactions play a role in soft **BUT** also in high  $p_t$  processes
- Theoretical description is tricky ...
- Models can be tuned to describe TeVatron measurements
  - at the price of "just reasonable" parameters
- **Extrapolation to LHC:**
  - questionable, because of high parton densities at small  $x$
  - possible non-linear effects: saturation, small  $x$  increase
  - Color flow is far from clear...
  - Stay tuned to surprises ...

# Conclusions

- HERA physics is very rich:
  - from inclusive x-section measurements to detailed investigations of QCD
  - measurements of hadronic final states:
    - jets, heavy flavors
    - leads to a detailed understanding of QCD
    - new issues addressed:  
integrated PDFs, uPDFs, etc ...  
saturation, diffraction, multi-parton interactions...
- HERA implications for LHC
  - PDFs, small x, multiple interactions, diffraction

It all comes from the high gluon density ....

Understanding of QCD at  
high energies is still challenging !