

# 2HDM+COMPLEX SINGLET AND INFLATION

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- Extensions of the 2HDM are motivated from baryogenesis, gravitational waves, dark matter and inflationary point of view.
- Inflation and 2HDM studied in Gong et.al.
- We extend their computation in the context of 2HDM+ complex singlet. (ongoing)

# Most general 2HDM+ complex Singlet Lagrangian

$$\mathcal{V}_{THDMCS} = \mathcal{V}_{2HDM} + \mathcal{V}_S + \mathcal{V}_{HS} \quad (1)$$

where

$$\begin{aligned} \mathcal{V}_{2HDM} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - (m_{12}^2 \Phi_1^\dagger \Phi_2 + h.c) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 \\ & + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + [\lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \\ & \lambda_6 (\Phi_1^\dagger \Phi_1) (\Phi_1^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2) (\Phi_1^\dagger \Phi_2) + h.c] \end{aligned}$$

$$\begin{aligned}
\mathcal{V}_S = & (\zeta S + h.c.) + m_S^2 S^\dagger S + \left(\frac{m'^2}{2} S^2 + h.c.\right) + \left(\frac{\mu_{S1}}{6} S^3 + h.c.\right) + \left(\frac{\mu_{S2}}{6} S S^\dagger S + h.c.\right) \\
& + \left(\frac{\lambda_1''}{24} S^4 + h.c.\right) + \left(\frac{\lambda_2''}{6} S^2 S^\dagger S + h.c.\right) + \frac{\lambda_3''}{4} (S^\dagger S)^2 \\
& + [S(\mu_{11} \Phi_1^\dagger \Phi_1 + \mu_{22} \Phi_2^\dagger \Phi_2 + \mu_{12} \Phi_1^\dagger \Phi_2 + \mu_{21} \Phi_2^\dagger \Phi_1) + h.c.]
\end{aligned}$$

$$\begin{aligned}
V_{HS} = & [S^\dagger S(\lambda'_1 \Phi_1^\dagger \Phi_1 + \lambda'_2 \Phi_2^\dagger \Phi_2 + (\lambda'_3 \Phi_1^\dagger \Phi_2 + h.c))] \\
& + [S^2(\lambda'_4 \Phi_1^\dagger \Phi_1 + \lambda'_5 \Phi_2^\dagger \Phi_2 + \lambda'_6 \Phi_1^\dagger \Phi_2 + \lambda'_7 \Phi_2^\dagger \Phi_1) + h.c.]
\end{aligned}$$

Imposing softly broken  $Z_2$  symmetry would imply setting coefficients of terms  $\propto (\Phi_1^\dagger \Phi_2) = 0$

$$\implies \lambda_6, \lambda_7 = 0 \text{ in } V_{2HDM}$$

We retain these terms presently for the most general case now.

# Calculations for inflationary conditions

Ref: Inflation and dark matter in IDM, (Gong et.al)

The Jordan frame potential:  $V$  transformed to the Einstein frame by introducing a Weyl Transformation:

$$\Omega^2 = 1 + 2\zeta_1|\Phi_1|^2 + 2\zeta_2|\Phi_2|^2 + 2\zeta_4|S|^2$$

where  $\zeta_i$  are the non-minimal coupling of  $\Phi_i$  and  $S$  to gravity.  
After the Weyl transformation,  $V_E = \frac{V}{\Omega^4}$ .

For working out the inflationary conditions,

$$\Phi_1^T = \frac{1}{\sqrt{2}}(0 \ h_1)^T,$$

$$\Phi_2^T = \frac{1}{\sqrt{2}}(0 \ h_2 e^{i\theta_1})^T \text{ and}$$

$$S = \frac{1}{\sqrt{2}} S e^{i\theta_2}$$

Working in the large field limit:  $\zeta_1 h_1^2 + \zeta_2 h_2^2 + \zeta_4 S^2 \gg 1$  as relevant for inflation and introducing the following parameterisation:

$$\phi = \sqrt{\frac{3}{2}} \log[1 + \zeta_1 h_1^2 + 2\zeta_2 h_2^2 + 2\zeta_4 S^2], \ r_1 = \frac{h_2}{h_1}, \ r_2 = \frac{S}{h_1} \text{ and} \\ r_3 = \frac{S}{h_2} = \frac{r_2}{r_1}$$

Recall,  $V_E = \frac{V}{\Omega^4} = \frac{V'_{2HDM}}{\Omega^4} + \frac{V'_S}{\Omega^4} + \frac{V'_{HS}}{\Omega^4}$  Using the parametrisation,  
where ignoring the mass terms,

$$V'_{2HDM} = \frac{1}{8}(\lambda_1 + \lambda_2 r_1^4 + 2r_1^2(\lambda_3 + \lambda_4) + 2r_1^2 \lambda_5 \cos 2\theta_1) + \frac{r_1}{2}(\lambda_6 + \lambda_7 r_1^2) \cos \theta_1$$

$$V'_{HS} = \frac{\lambda'_3}{4} r_1 r_2^2 \cos \theta_1 + \cos \theta_2 \left[ \left( \frac{\mu_{12}}{\sqrt{2} h_1} \right) r_2 \right] + \frac{\mu_{22}}{\sqrt{2} h_1} r_1^2 r_2 + \frac{\mu_{12}}{\sqrt{2} h_1} r_1 r_2 \Big] +$$

$$\cos 2\theta_2 \left( \frac{\lambda'_4}{4} r_2^2 + \frac{\lambda'_5}{4} r_2^2 r_1^2 + \frac{\lambda'_6}{4} r_1 r_2^2 \right) + \lambda'_7 r_2^2 r_1 \cos(2\theta_2 - \theta_1)$$

$$V'_S = \frac{\mu_{S1}}{6} S^3 (\cos 3\theta_2) + \frac{\mu_{S2}}{2\sqrt{2}} S^3 \cos \theta_2 + \frac{\lambda''_1}{48} \cos 4\theta_2 + \frac{\lambda'_2}{12} S^4 \cos \theta_2$$

(where the mass terms are ignored for large  $S$  limit and the tadpole term while  $\zeta S$  has been ignored by shift symmetry of  $S$ )

Currently obtaining the extrema of the potential to obtain the inflationary conditions keeping the most general case.

Few assumptions made:

Ignored terms like  $\zeta_3 S^\dagger S \Phi_1^\dagger \Phi_1$  in the Weyl transformation  $\Omega^2$ .

Thank you!