

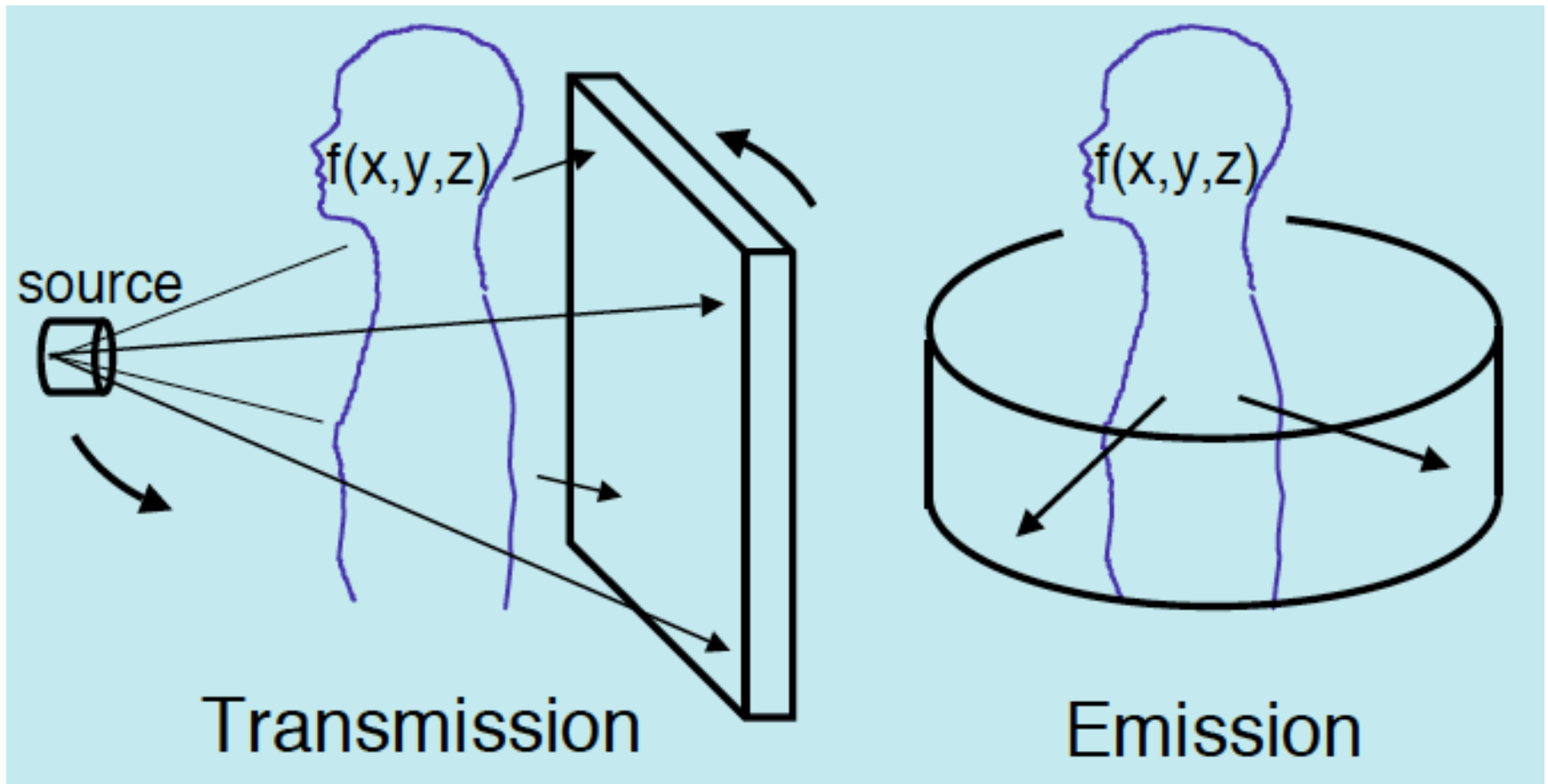
# Structure of the course

- 1) Introduction
- 2) Interaction of particles with matter } principles / tools
- 3) Therapy with proton and ion beams
- 4) Sources for nuclear medicine }  
5) X- ray sources } sources
- 6) Image quality } objective
- 7) X-ray imaging }  
8) Computed tomography }  
9) Planar scintigraphy } imaging modalities
- 10) Emission tomography }  
11) Magnetic Resonance Imaging }  
12) Multimodal systems }

Medical imaging

The course will not cover ultrasound and optical imaging

# External versus internal radiation sources



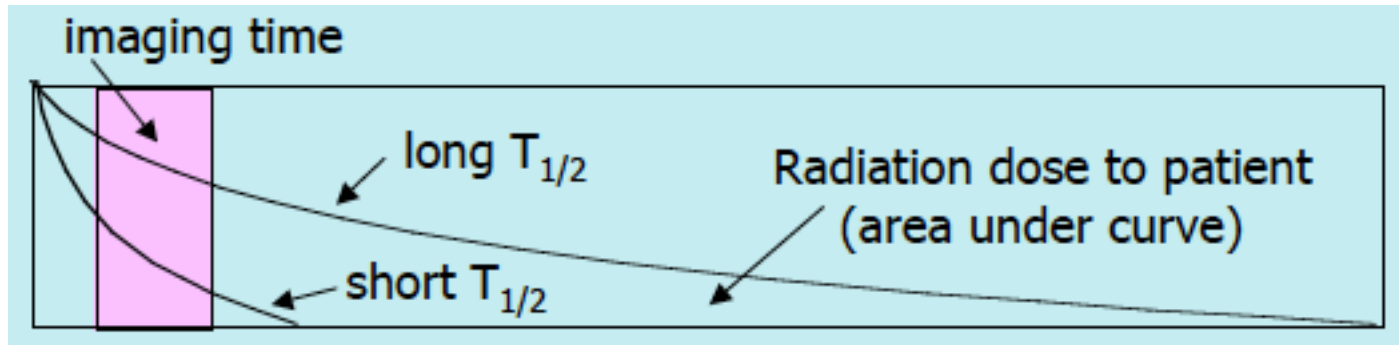
# Internal radiation sources

- Inject the patient with a “source of radiation” → define later

## Problem:

Unlike an X-ray device, we cannot turn off the radiation after the image is taken.

Radiation decays exponentially (characterized by “half-time”  $T_{1/2}$ )



**Solution:** use short lived isotopes

**Problem:** short lived isotopes do not exist (obviously) in nature

**Solution:** we need to produce them ad hoc for the exam

# Nuclear physics (recap)

**Nuclide:** unique combination of protons and neutrons in a nucleus

- mass number **A** = # nucleons
- atomic number **Z** = # protons = # electrons
- An element is denoted by  ${}^A_Z X$ , *i.e.*  ${}^{12}_6 C$

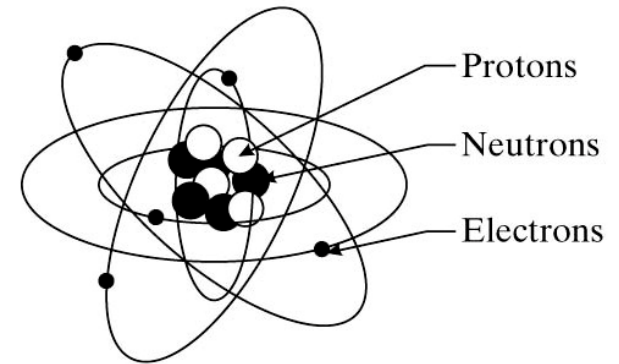
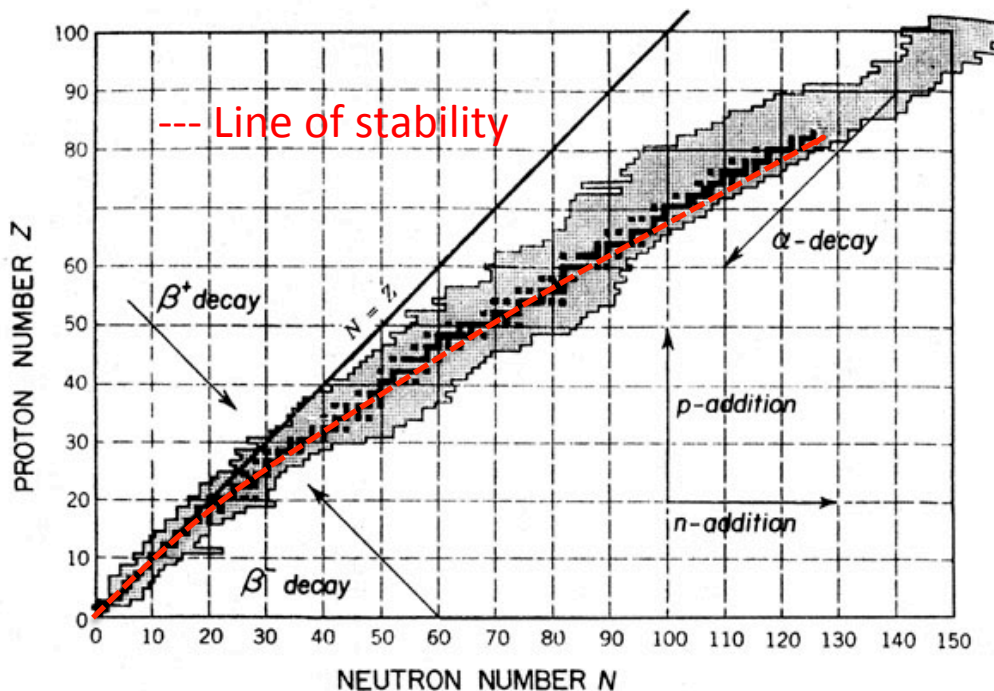


Figure 4.1



- Stable nuclides:
  - $N \approx Z$  ( $A \approx 2Z$ ) for small  $Z$
  - $N > Z$  for large  $Z$
- Unstable nuclides (radionuclides, radioactive atoms)
  - Likely to undergo radioactive decay, which gives off energy and results in a more stable nucleus

# Binding energy

Mass defect in an atom: 
$$\Delta M = \left( \sum_Z M_p + \sum_N M_n + \sum_Z M_e \right) - M_{atom}$$

ex.  ${}^1_6\text{C}$ :  $\Delta M = \text{constituent sum} - M_{atom} =$   
 $= 6 \times 1.007276 + 6 \times 1.008665 + 6 \times 0.000548 \text{ u} - 12 = 0.098934 \text{ u}$

Binding energy:

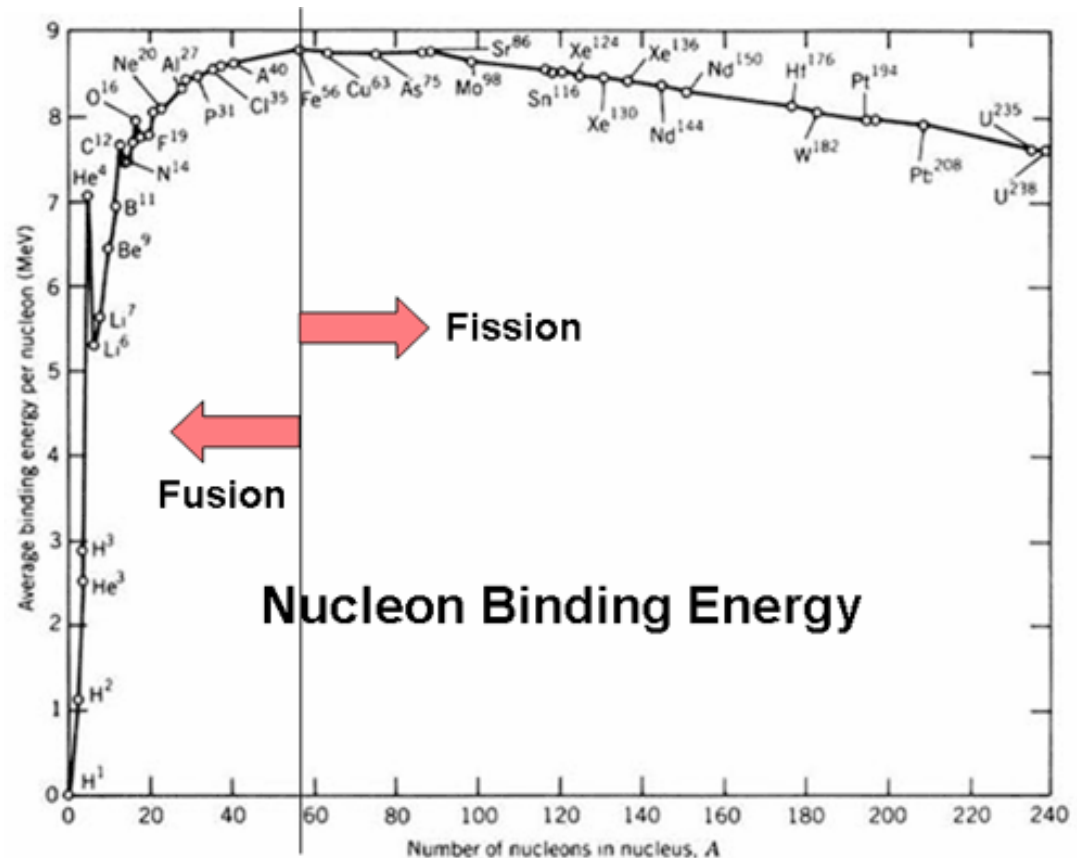
$$E = \Delta M c^2$$

More commonly quoted  $E/A$

ex.  ${}^1_6\text{C}$ :

$$E/A = 0.098934 \times 931 / 12 \text{ MeV/A}$$

$$= 7.67 \text{ MeV/nucleon}$$

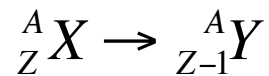
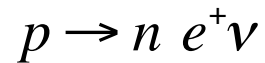


# Radioactive decay

- The greater the binding energy/nucleon the more stable is the atom.
- Atoms in a state away from the line of stability can rearrange their nuclei to gain more stability.
- The daughter products of a radioactive decay have higher binding energy/nucleon = greater mass defect.
- In a radioactive decay energy is released from the atom.
- Four types of radioactive decays:
  - Alpha decay (2 protons, 2 neutrons)
  - Beta- decay (electron emission)
  - Beta+ decay (positron emission)
  - Gamma decay (emission of a gamma ray\*)

# Beta+ decay

Within a nucleus:



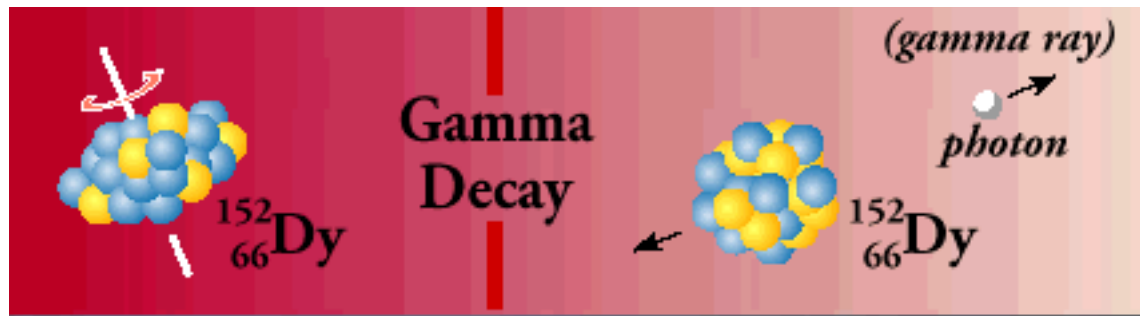
Mass number A does not change,  
proton number Z reduces by one unit



Application → positron emission tomography (PET)

# Gamma decay

- An unstable nucleus changes from a higher energy state to a lower energy state through the emission of electromagnetic radiation (called gamma rays).
- The daughter and parent atoms are isomers (same A, same Z).
- Gamma-rays and X-rays used in medical applications are both photons in the energy range 20-600 keV, but generated by different processes:
  - X-ray are produced by energetic electron interactions
  - Gamma-ray through isometric transition in nucleus



- Application → Single photon emission computed tomography (SPECT)



# Radioactivity

Radioactivity:  $A = \#$  of radioactive decays per second

$$1\text{Bq} = 1 \text{ dps}$$

$$1 \text{ Ci} = 3.7 \times 10^{10} \text{ Bq}$$



Radioactivity in nuclear medicine is in the range of 100 mCi or 100 MBq.

- Naturally occurring radioisotopes discovered 1896 by Becquerel
- First artificial radioisotopes produced by the Curie 1934

The intensity of radiation incident on a detector at range  $r$  from a radioactive source is:

$$I = \frac{AE}{4\pi r^2}$$

A: radioactivity of the material

E: energy of each photon

*Ex. Intensity of 100mCi of Technetium-99m at 20 cm distance? ( $E_\gamma=140 \text{ keV}$ )*

$$I = 0.37 \times 10^{10} \text{ Bq} \times 140 \text{ keV} / 4\pi (0.2)\text{m}^2 = 0.1 \times 10^{10} \text{ keV/s/m}^2 \sim 10^3 \text{ GeV/s/m}^2$$

# Radioactive Decay Law

$N(t)$ : the number of radioactive atoms at a given time

$A(t)$ : is proportional to  $N(t)$

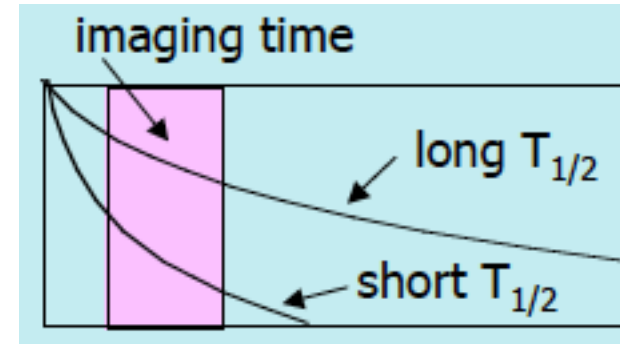
$$A = -\frac{dN}{dt} = \lambda N$$

$\lambda$ : decay constant

Integrating one obtains:

$$N(t) = N_0 e^{-\lambda t}$$

$$A(t) = A_0 e^{-\lambda t} = \lambda N_0 e^{-\lambda t}$$



Radioactivity  
always remains

Half-life is the time it takes for the radioactivity to decrease by  $\frac{1}{2}$ .

$$\frac{A_{T_{1/2}}}{A_0} = \frac{1}{2} = e^{-\lambda T_{1/2}} \quad \rightarrow \quad T_{1/2} = \frac{0.693}{\lambda}$$

half-life

The number of photons generated (= # of disintegrations) during time  $T$  is:



$$\Delta N = \int_0^T A(t) dt = \int_0^T \lambda N_0 e^{-\lambda t} dt = N_0 (1 - e^{-\lambda T})$$

# Statistics of decay

- ! Radioactive decay is a random process so the exponential decay law only gives the **average** expected number of atoms (or the average expected radioactivity) at a certain time  $t$ .

The number of disintegrated atoms over a short time  $\Delta t \ll T_{1/2}$  after time  $t=0$  with  $N_0$  atoms follows Poisson distribution:

$$\Pr\{\Delta N = k\} = \frac{a^k e^{-a}}{k!}; \quad a = \lambda N_0 \Delta t; \quad \text{valid for a very short } \Delta t$$

$\lambda N_0$  is called the Poisson rate.

# Example

A patient study needs to be completed in 10 min. and requires a statistics of 3.5 million photon counts to achieve the desired image quality.

**Q:** 6 K photons are detected in the first 1 sec. What is the half-life of the radionuclide for a successful study?

**A:** in 1 sec the number of detected photons (100% detection efficiency) is:

$$\Delta N = \int_0^1 \lambda N_0 e^{-\lambda t} dt = N_0 (1 - e^{-\lambda}) = 6K$$

To get 3.5 millions counts in 10 min (600 sec)

$$\Delta N = \int_0^{600} \lambda N_0 e^{-\lambda t} dt = N_0 (1 - e^{-600\lambda}) = 3500K$$

$$\frac{1 - e^{-600\lambda}}{1 - e^{-\lambda}} = \frac{3500}{6}$$

$$\rightarrow \lambda = 9.45 \times 10^{-5} s^{-1}$$

The minimal half-life needed is:

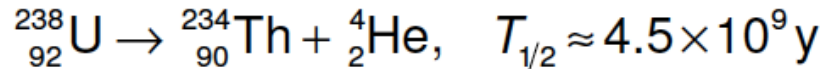
$$T_{1/2} = \frac{0.693}{\lambda} = 7333s \sim 2h$$

# Radionuclides for medicine

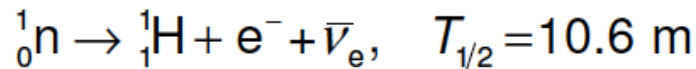
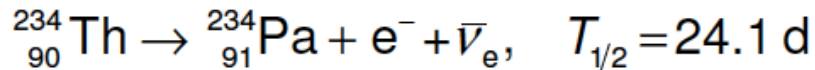
- About 1500 known **radionuclides**, about 200 can be purchased
- About 12 **suitable for nuclear medicine**:
  - **Clean**  $\gamma$  emitters = no  $\alpha$  or  $\beta$  emission / or  $\beta$  emitters
  - Energy high enough to have minimum attenuation in the body
  - Energy low enough to interact in the detector and be detected
    - ➔ typical accepted **energy range**  $50 < E_{\gamma} < 511 \text{ keV}$ .
  - **Acceptable half-life**, order of minutes (long enough to prepare and perform the exam, short enough that exam can be short to minimize patient motion effects.
- **Mono-energetic**: Energy sensitive detectors can discriminate the primary photons from scattered ones.
- Generation of radiotracers: on-site generators, cyclotrons, radio pharmacy

# Examples of decay processes

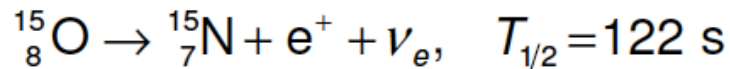
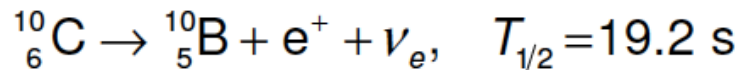
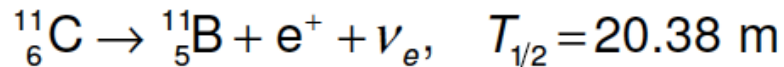
$\alpha$  decay



$\beta^-$  decay



$\beta^+$  decay



Most of these naturally occurring processes are not useful for medical imaging applications, with too long half-time, too high energy.

They can be used as radio-therapeutic agents, if they can be targeted to tumors, to destroy diseased tissue and stop the cancer from proliferating.

# How to produce (short-lived) isotopes

## Via nuclear bombardment:

Hit nucleus of stable atoms with sub-nuclear particles: neutrons, protons, alpha particles etc.

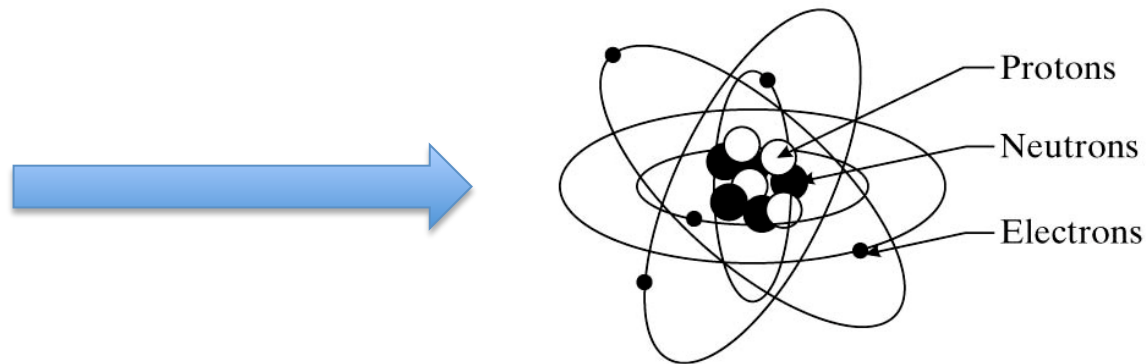
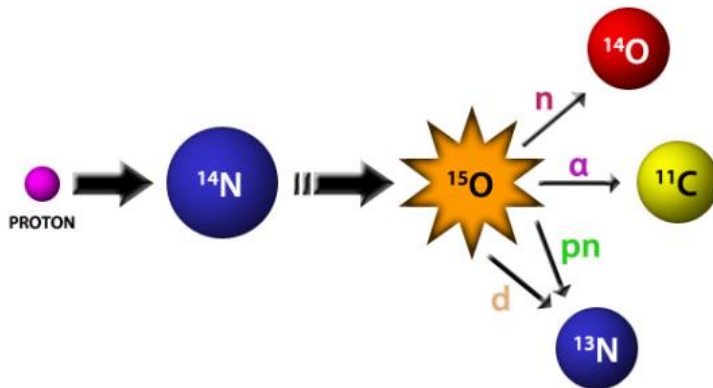


Figure 4.1

1. Inserting target in a nuclear reactor → produce longer-lived isotopes extract and ship them → Longer-lived isotopes decay to a short-lived ones (portable 'generator')
2. Using a charged-particle accelerator (cyclotron) – needed locally for short-lived isotopes ( $T_{1/2} \sim 1$  to 100 min).

# Radionuclides from cyclotron

- Produced by bombarding the target nucleus with charged particles (e.g. protons) of defined energy.
- Remember: binding energy / nucleon in the nucleus is  $\sim 8$  MeV.
- If  $E_{\text{projectile}} > E_{\text{binding}}$  particles will be ejected from the target nucleus.
- By carefully selecting the target nucleus, the bombarding particle and its energy, it is possible to produce a specific radionuclide.





# Types of accelerators routinely used for radioisotope production

Classification	Characteristics	Energy [MeV]	Major radionuclides produced
Level I	single particle* ( <i>d</i> )	< 4	<sup>15</sup> O
Level II	single particle ( <i>p</i> )	≤ 11	<sup>11</sup> C, <sup>13</sup> N, <sup>15</sup> O, <sup>18</sup> F
Level III	single or two particle ( <i>p, d</i> )	≤ 20	<sup>11</sup> C, <sup>13</sup> N, <sup>15</sup> O, <sup>18</sup> F ( <sup>123</sup> I, <sup>67</sup> Ga, <sup>111</sup> In)
Level IV	single or multiple particle ( <i>p, d, <sup>3</sup>He, <sup>4</sup>He</i> )	≤ 40	<sup>38</sup> K, <sup>73</sup> Se, <sup>75–77</sup> Br, <sup>123</sup> I, <sup>81</sup> Rb ( <sup>81</sup> Kr), <sup>67</sup> Ga, <sup>111</sup> In, <sup>201</sup> Tl, <sup>22</sup> Na, <sup>57</sup> Co
Level V	single or multiple particle ( <i>p, d, <sup>3</sup>He, <sup>4</sup>He</i> )	≤ 100	<sup>28</sup> Mg, <sup>72</sup> Se ( <sup>72</sup> As), <sup>82</sup> Sr ( <sup>82</sup> Rb), <sup>117m</sup> Sn, <sup>123</sup> I
Level VI	single particle ( <i>p</i> )	≥ 200	<sup>26</sup> Al, <sup>32</sup> Si, <sup>44</sup> Ti, <sup>67</sup> Cu, <sup>68</sup> Ge ( <sup>68</sup> Ga), <sup>82</sup> Sr ( <sup>82</sup> Rb), <sup>109</sup> Cd, <sup>95m</sup> Tc, etc.

# Cyclotron

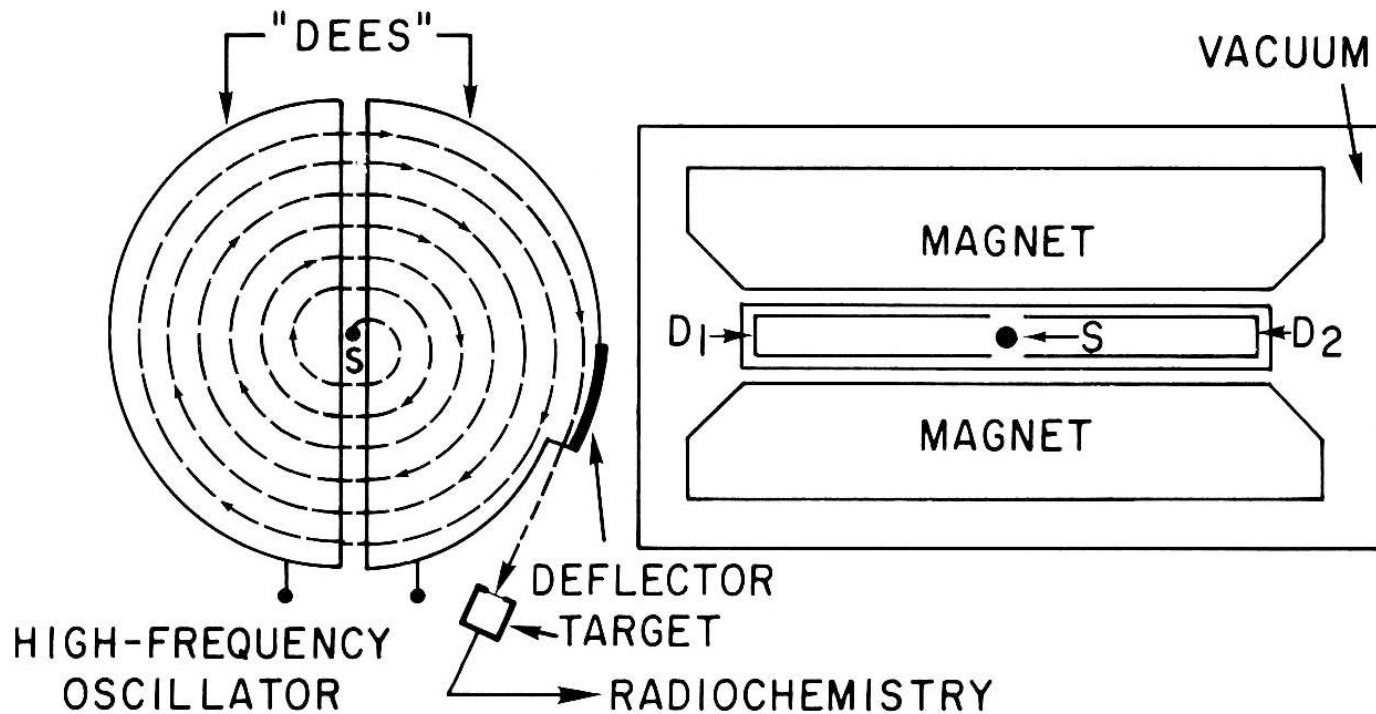


Fig. 7-2. Schematic representation of a cyclotron; top (left) and side (right) views.  $D_1$  and  $D_2$  are the "dees" to which the accelerating voltage is applied by a high-frequency oscillator. Target line may feed directly to a radiochemistry area.

# Radionuclides from reactor

- The fission process is a source of a number of widely used radionuclides (e.g.  $^{90}\text{Sr}$ ,  $^{99}\text{Mo}$ ,  $^{131}\text{I}$  and  $^{133}\text{Xe}$ )
- They can be separated from uranium fuel cells or from targets of enriched  $^{235}\text{U}$  placed in the reactor for radionuclide production directly.
- Highest efficiency for  $^{99}\text{Mo}$  production → most widely used in nucl. med.

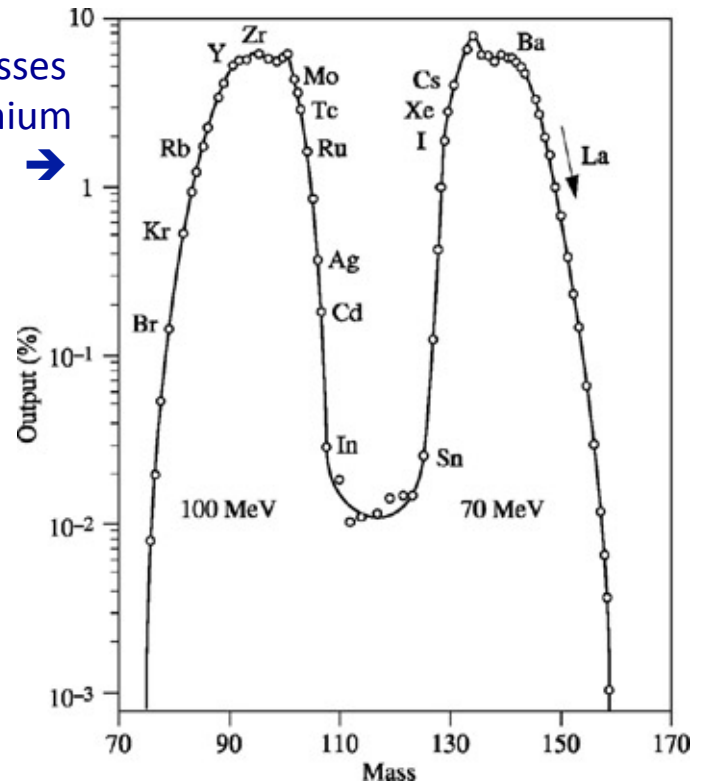
## Drawbacks:

- Nuclear waste
- Contamination with other isotopes
- Needs running reactors (!!)

## Advantages:

- Passive mode production (if nuclear plants are running)

Distribution of atomic masses  
of fission products of uranium



# Radionuclide generators

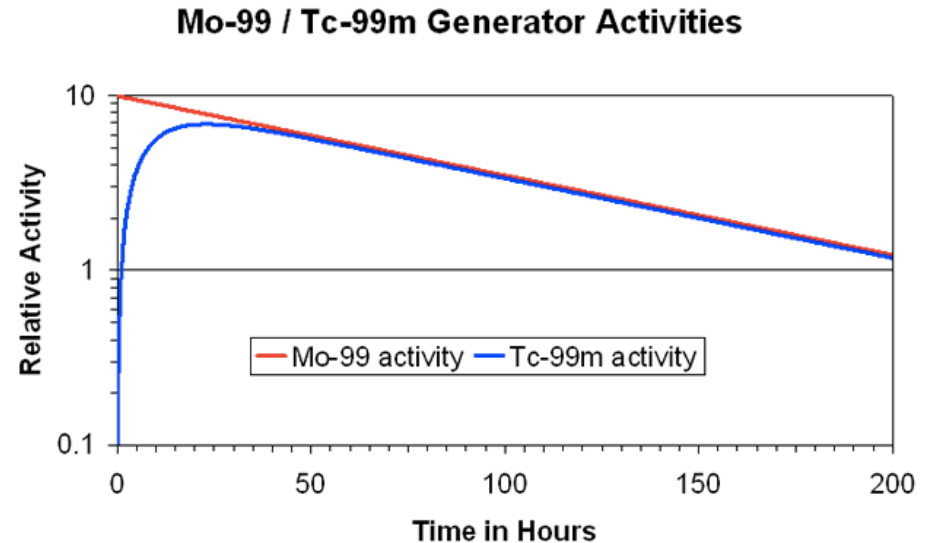
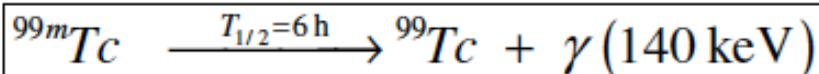
A long-lived radionuclide ("parent") decays into a short-lived radionuclide ("daughter") of interest.

In "transient equilibrium generator" the parent radionuclide half-life is greater than the daughter's.

e.g.  $^{99}\text{Mo}$  ( $T_{1/2} = 66 \text{ h}$ )  $\rightarrow$   $^{99\text{m}}\text{Tc}$  ( $T_{1/2} = 6 \text{ h}$ )

the daughter will have different physical and chemical properties and can be eluted from the parent-daughter mixture.

Decay characteristics of  $^{99\text{m}}\text{Tc}$ :



Over 80% of all nuclear medicine Procedures performed worldwide use  $^{99\text{m}}\text{Tc}$  as the imaging radionuclide.

Specific tracers are produced to examine the brain, kidney, heart, bone, liver, lung, red blood cells, and thyroid ( $\text{TcO}_4$ )

# Generator

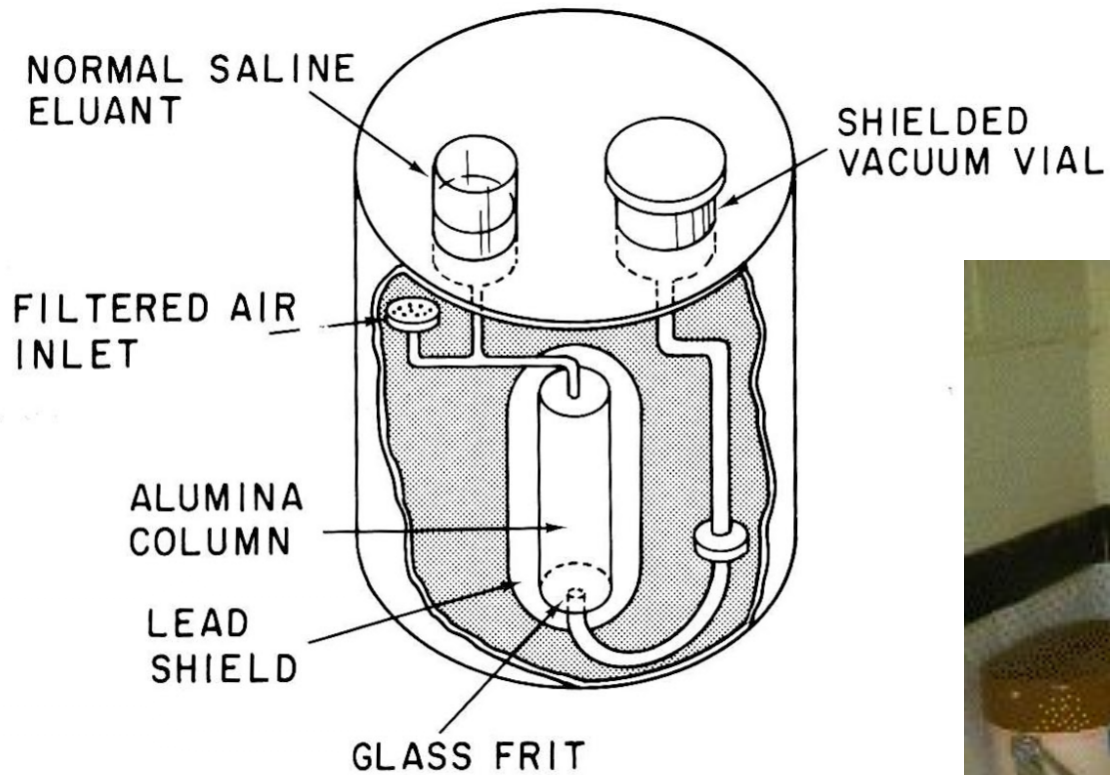


Fig. 7-5. Cross-sectional drawing of a  $^{99}\text{Mo}$ - $^{99\text{m}}\text{Tc}$  generator. (Society of Nuclear Medicine and Thomas R. Gnau.)



# Radiotracers

To be usable **in medical imaging** the radionuclides and the compounds to which they are attached must obey the three tracer principles:

- the tracer behaves or interacts with the system to be probed in a known, reproducible fashion,
- the tracer does not alter or perturb the system in any measurable fashion,
- the tracer concentration can be measured.

In order to be used **for therapy** the second principle must be broken (damage the unwanted tissues)

# Radiotracers

- Radionuclide bound to pharmaceuticals specific to metabolic activities (cancer, myocardial perfusion, brain perfusion) are called **radiotracers**.
- The radiotracers that can be safely administered to humans are referred to as **radiopharmaceuticals** (radiochemical purity, sterile and free from micro-organisms that can cause fever)
- 95% of the radiopharmaceuticals are used for diagnostic purposes, the remainders are used in therapy.
- A large number of radiotracers have been synthesized to probe metabolic turnover such as oxygen consumption, glucose utilization and amino acid synthesis → **biochemistry**

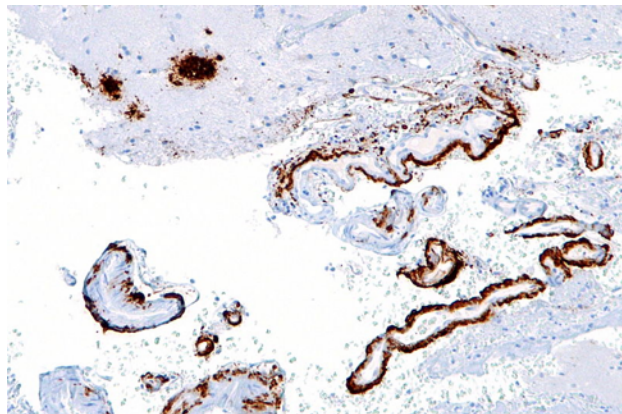
# Radiopharmaceuticals

- Gamma emitter
  - $^{99m}\text{Tc}$ -Sestamibi (myocardial perfusion, cancer)
  - $^{99m}\text{Tc}$ -labeled hexamethyl-propyleneamine (brain perfusion)
- Positron emitters
  - $^{11}\text{C}$ ,  $T_{1/2} = 20$  min      [ $^{12}\text{C}$  ( $p,pn$ )  $^{11}\text{C}$ ;  $^{14}\text{N}$  ( $p,\alpha$ )  $^{11}\text{C}$ ]:
    - many organic compounds (binding to nerve receptors, metabolic activity)
  - $^{13}\text{N}$ ,  $T_{1/2} = 10$  min      [ $^{16}\text{O}$  ( $p,\alpha$ )  $^{13}\text{N}$ ;  $^{13}\text{C}$  ( $p,n$ )  $^{13}\text{N}$ ]:
    - $\text{NH}_3$  (blood flow, regional myocardial perf.)
  - $^{15}\text{O}$ ,  $T_{1/2} = 2.1$  min      [ $^{15}\text{N}$  ( $p,n$ )  $^{15}\text{O}$ ;  $^{14}\text{N}$  ( $d,n$ )  $^{15}\text{O}$ ]:
    - $\text{CO}_2$  (cerebral blood flow),  $\text{O}_2$  (myoc.  $\text{O}_2$  consumption),  $\text{H}_2\text{O}$  (myoc.  $\text{O}_2$  consumption & blood perfusion)
  - $^{18}\text{F}$ ,  $T_{1/2} = 110$  min      [ $^{18}\text{O}$  ( $p,n$ )  $^{18}\text{F}$ ;  $^{20}\text{Ne}$  ( $d,\alpha$ )  $^{18}\text{F}$ ]:
    - 2-deoxy-2- $^{18}\text{F}$ -fluoroglucose (FDG, neurology, cardiology, oncology, metabolic activity)

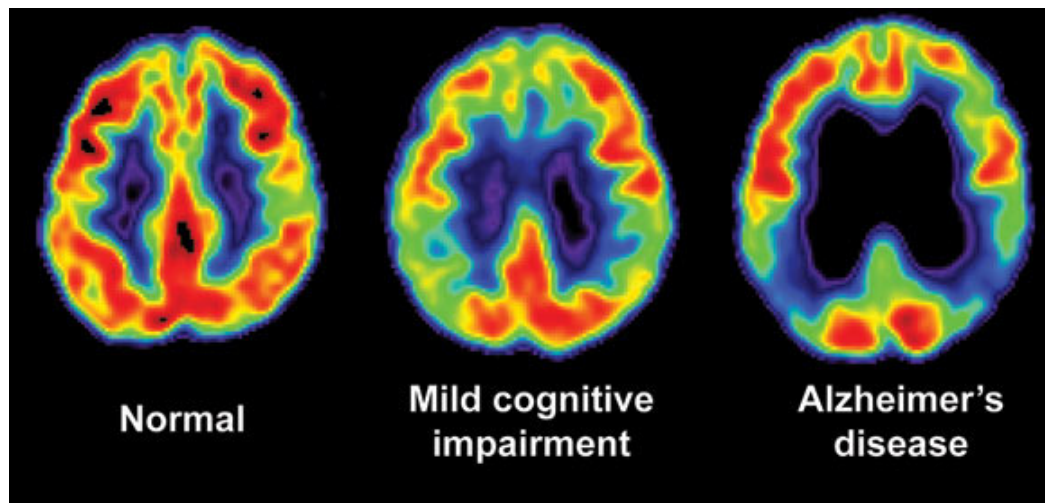
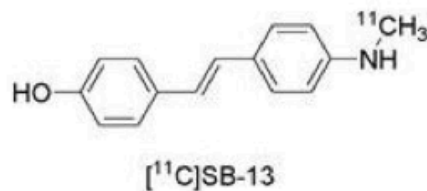
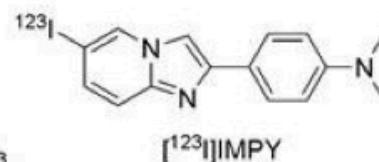
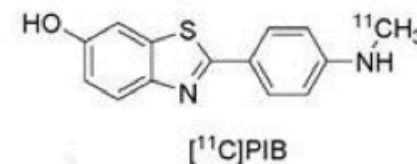
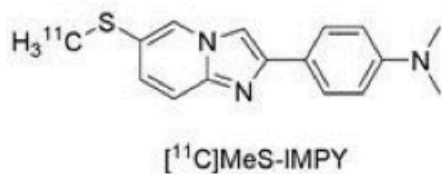
From H. Graber, Lecture Note, F05



# PET radio-ligands for Imaging of $\beta$ -Amyloid in Human



amyloid beta peptide (brown) in senile plaques of the cerebral cortex (upper left of image)



# Key points of this lecture



- Nuclear medicine relies on radiation (gamma rays) generated through radioactive decay
- Radioactive decay is the process when an unstable nuclide is changed to a more stable one
  - Four modes of decay exist generating alpha particles, beta particles, positrons and gamma rays respectively
- Radioactivity follows an exponential decay law, characterized by the decay constant ( $\lambda$ ) or the half-life ( $T_{1/2}$ )
- Desired properties for radio tracers
- Common radiotracers in nuclear medicine

# Units for therapy

The gray measures the absorbed energy of radiation

$$1 \text{ Gy} = 1 \frac{\text{J}}{\text{kg}} = 1 \frac{\text{m}^2}{\text{s}^2}$$

The biological effects vary by the type and energy of the radiation and the organism and tissues involved.

- A whole-body exposure to 5 or more gray of high-energy radiation at one time usually leads to death within 14 days.
- In radiation therapy, the amount of radiation varies depending on the type and stage of cancer being treated. For curative cases, the typical dose for a solid epithelial tumor ranges from 60 to 80 Gy, while lymphomas are treated with 20 to 40 Gy.
- The average radiation dose from an abdominal X-ray is 1.4 mGy, that from an abdominal CT scan is 8.0 mGy, that from a pelvic CT scan is 25 mGy, and that from a selective CT scan of the abdomen and the pelvis is 30 mGy.

# Litterature

- Prince and Links, Medical Imaging Signals and Systems, Chap 7.
- “The uses of radiotracers in the life sciences” by Thomas J. Ruth (2008), online at [stacks.iop.org/RoPP/72/016701](http://stacks.iop.org/RoPP/72/016701)

Table of nuclides:

- <http://atom.kaeri.re.kr/ton/>