

# Resonant modes of coupled magnetic nanodisks

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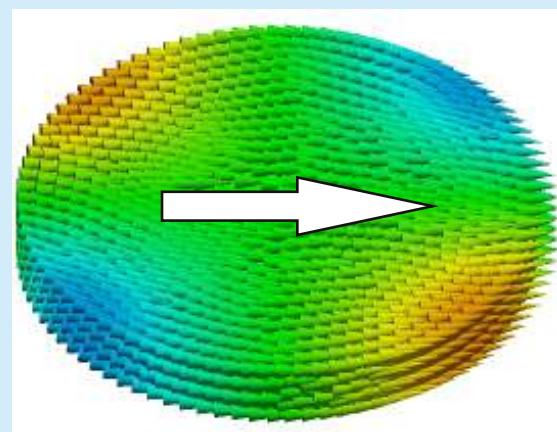
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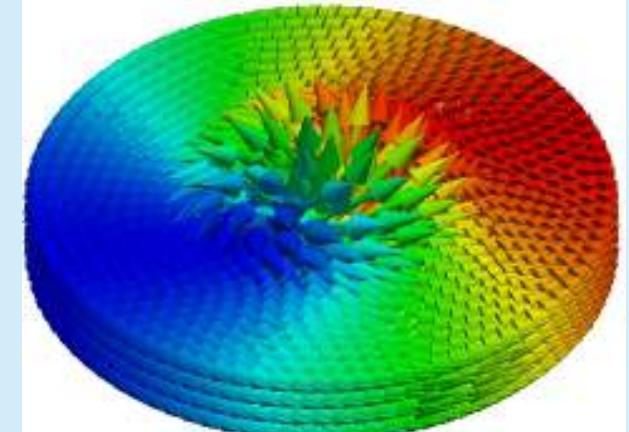
## Motivation

Interacting magnetic nano-elements with tailored magnetic configurations [1] have a wide range of applications, from magnetic logic [2] to radio-frequency and microwave signal generation, in particular if they are incorporated into spin torque nano-oscillators (STNOs). [3,4]. Here we study the stability and resonant modes of metastable states in coupled nanodisks in view of these applications.

## Ground states of individual nanodisks



Quasi-uniform state  
(small diameter)

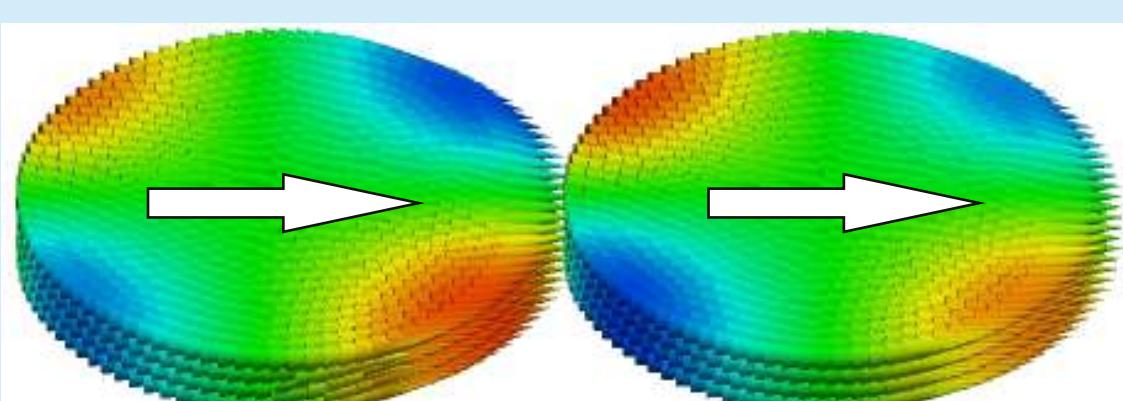


Vortex state  
(larger diameter)

There exists a transition region of intermediate diameter where both states are metastable.

## Pairs of nanodisks: metastable coupled states

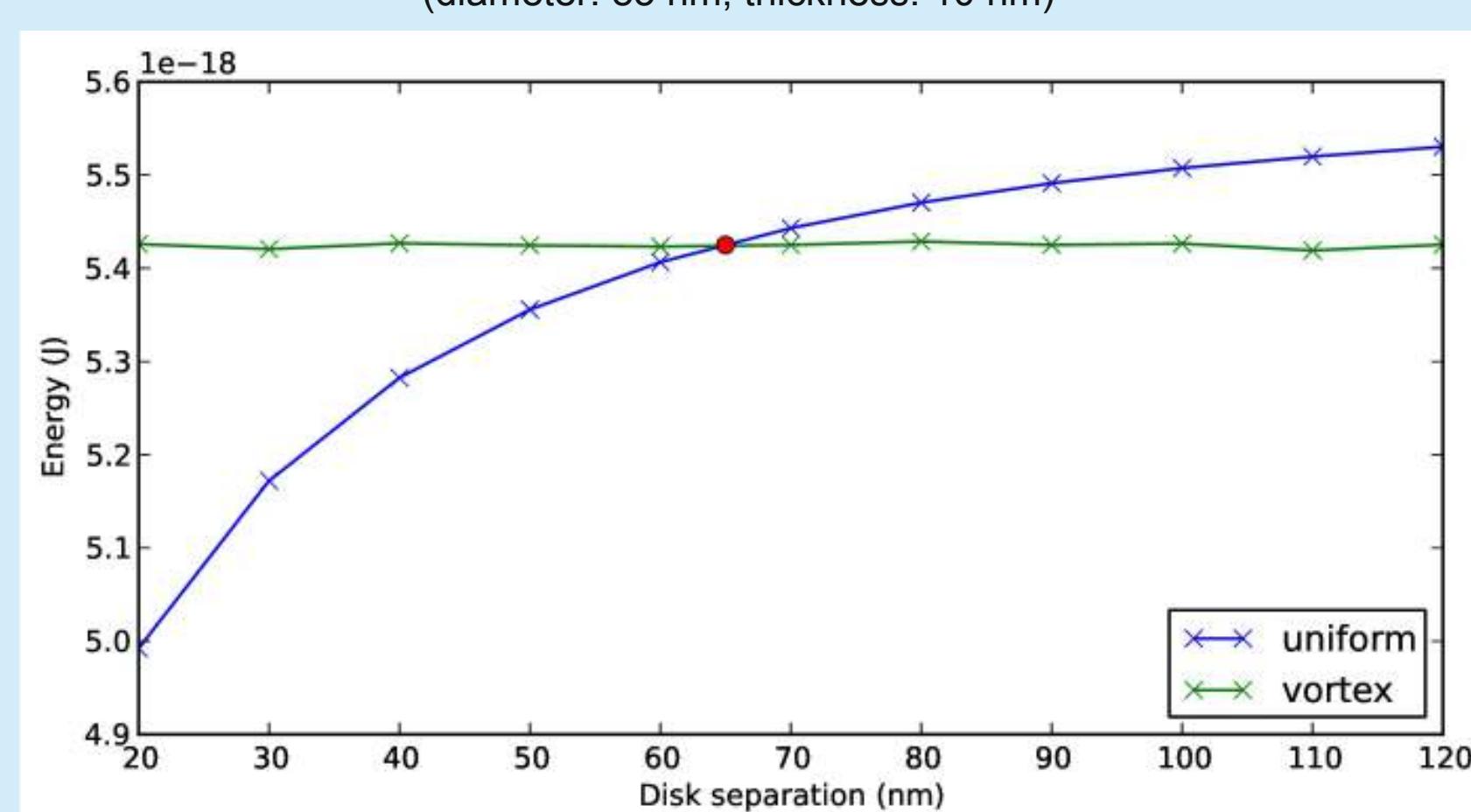
- Uniform state is stabilized in closely spaced disks through flux closure of the stray fields near the edges:



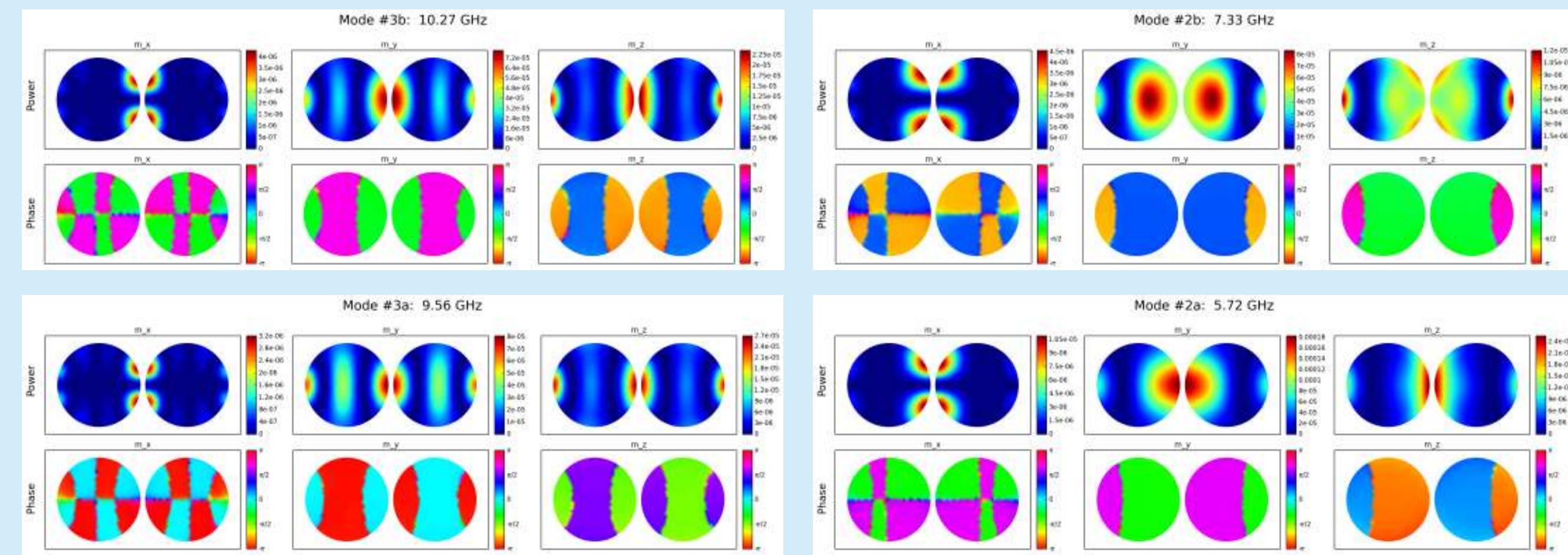
- Vortex state is favourable in disks that are far apart:



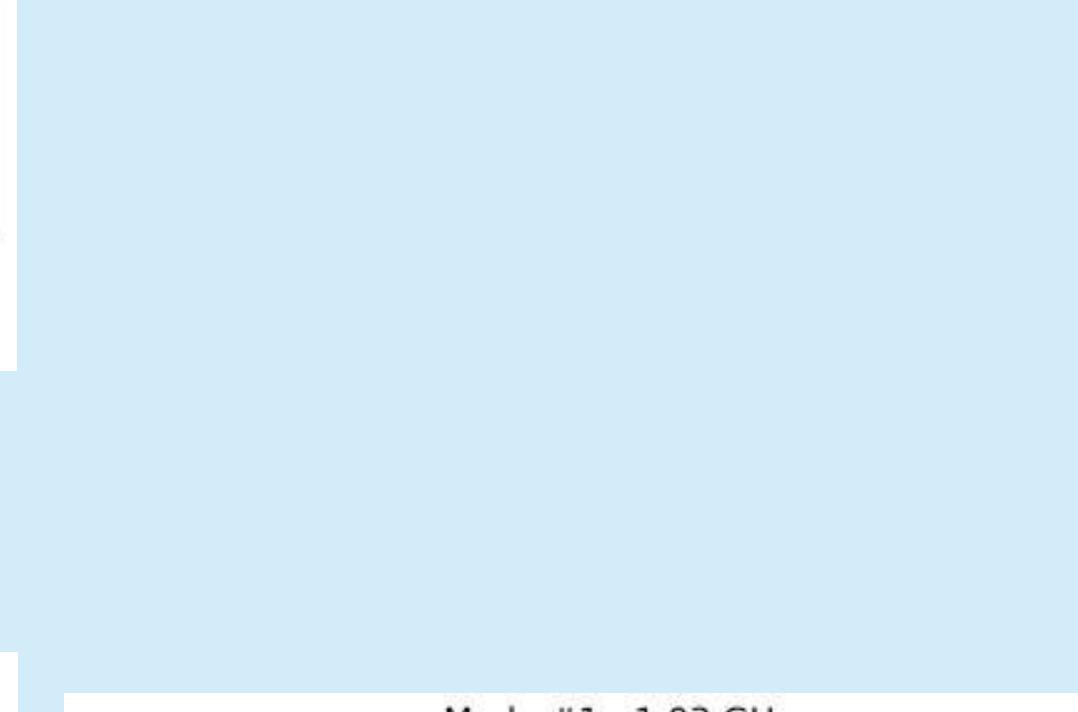
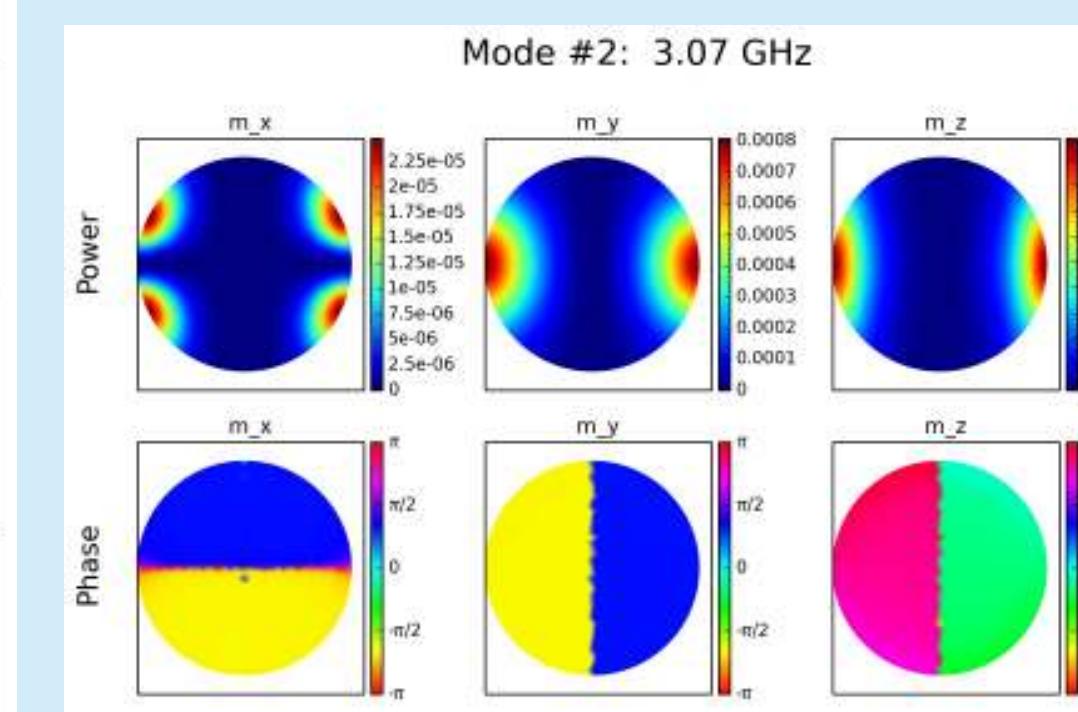
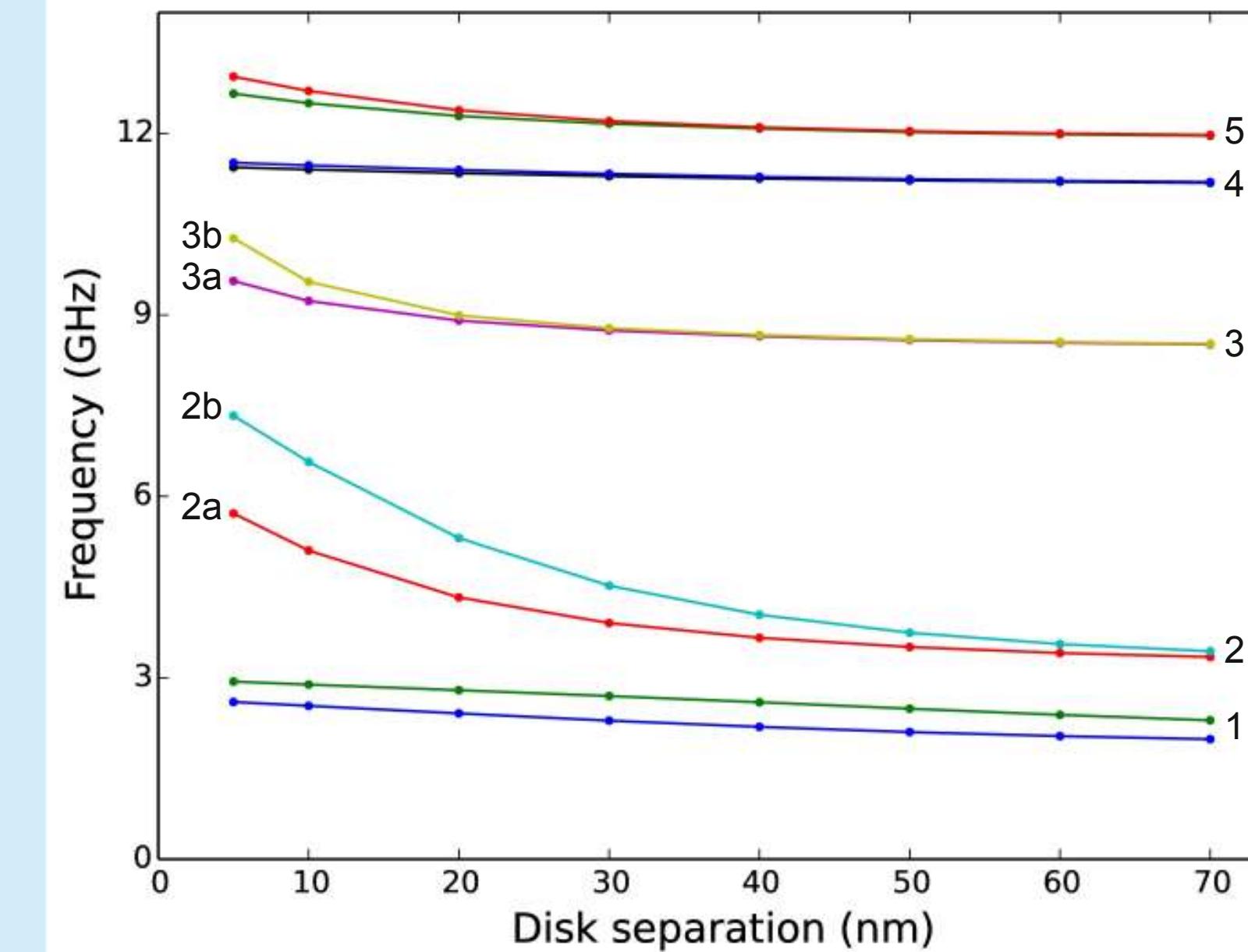
Dependence of coupled disk energy on distance  
(diameter: 85 nm, thickness: 10 nm)



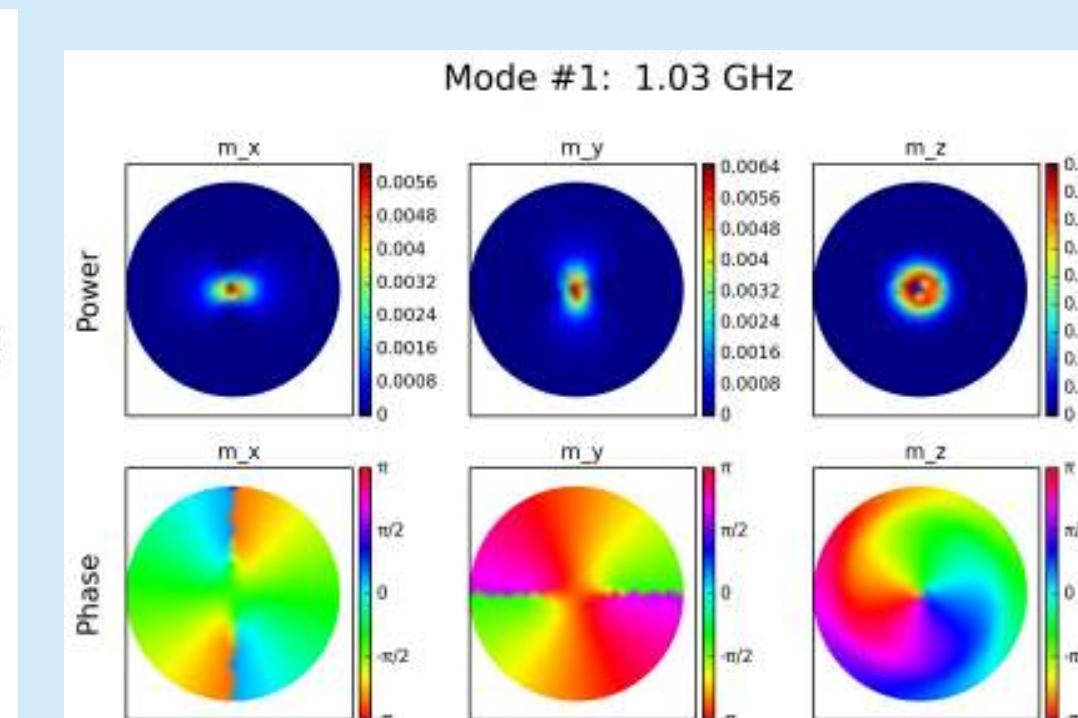
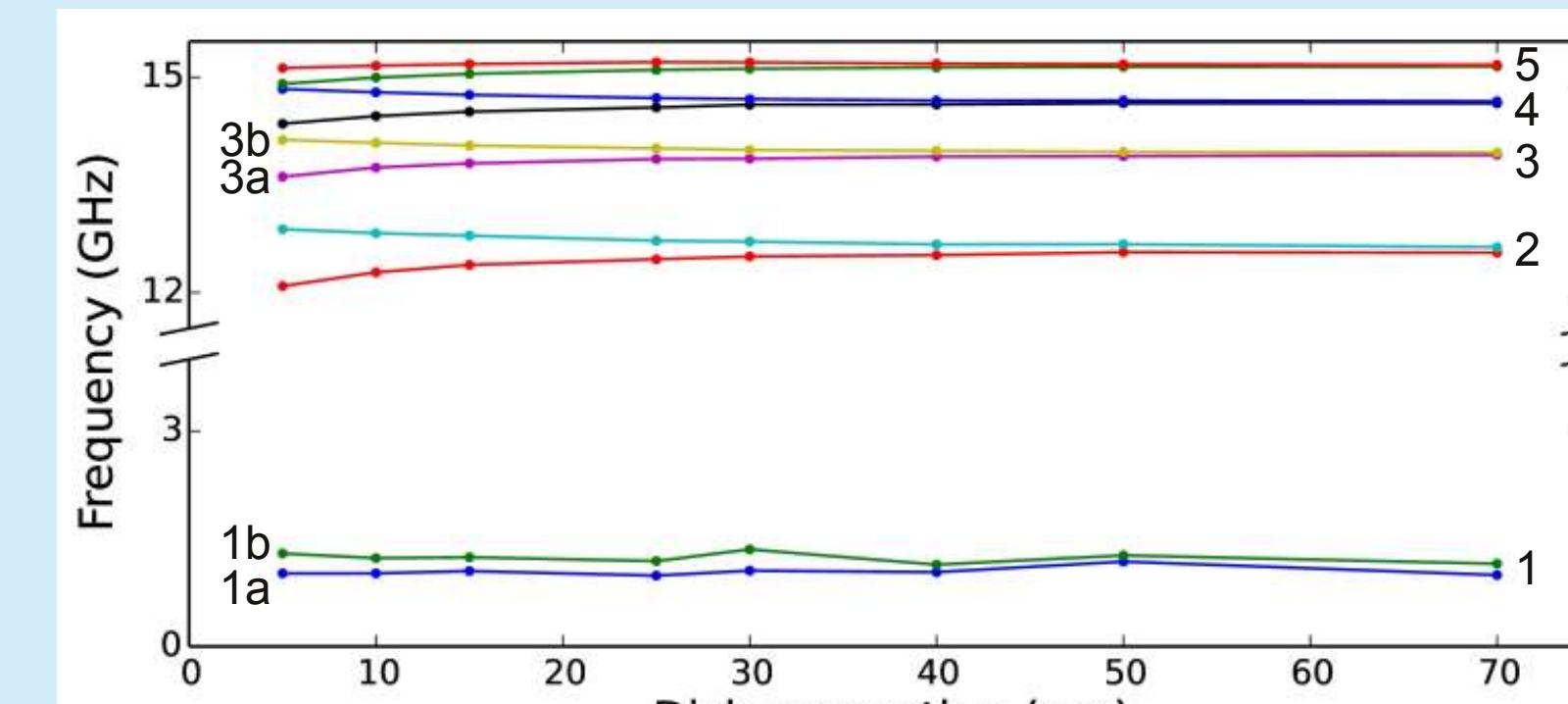
## Strong coupling: frequency splitting and mode deformation



## Uniform state



## Vortex state



## Computation of resonant modes

All calculations were performed using the finite-element based micromagnetic simulation framework "Finmag" (successor of Nmag [5]).

### (i) Ringdown method: [6]

- Relax into desired equilibrium state in presence of small perturbing field.
- Switch off field & record dynamics as  $m$  relaxes back into equilibrium.
- Compute power spectrum via Fourier transform of magnetisation dynamics.

### (ii) Eigenvalue method: [7]

- Linearize Landau-Lifshitz-Gilbert equation around equilibrium state  $m_0$ .
- Sinusoidal ansatz solution for  $\Delta m$  (where  $m = m_0 + \Delta m$ ) leads to a (generalized) eigenvalue problem.
- The resulting eigenvalues and eigenvectors yield the resonant frequencies and mode profiles.

## Conclusions

- Dipolar coupling between closely spaced nanodisks leads to stabilization of the single-domain state.
- Magnetostatic coupling also results in deformations of the resonant modes & frequency splitting ( $\Rightarrow$  in-phase vs. out-of-phase oscillations of neighbouring edges) — both in the uniform and vortex state.
- Coupled modes converge towards the single-disk modes as the disk separation increases.
- Stronger coupling effects & mode alterations are observed for uniform configuration than vortex configuration.

## References

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