

Zusammenfassung 17.12.

11.5. Eichboson-Massen

Higgsfeld $\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$ $T = \frac{1}{2}, Y = 1$

Lagrangian:

$$\mathcal{L}_{\text{Higgs}} = (\partial^\mu \phi)^\dagger (\partial_\mu \phi) + \mu^2 \phi^\dagger \phi - \lambda^2 (\phi^\dagger \phi)^2$$

und $\mathcal{L}_{\text{gauge}} = -\frac{1}{4} F_{\mu\nu}^i F^{\mu\nu i} - \frac{1}{4} f_{\mu\nu} f^{\mu\nu}$

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mit $f_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu$

und $\vec{F}_{\mu\nu} = \partial_\mu \vec{W}_\nu - \partial_\nu \vec{W}_\mu - \underbrace{g \vec{W}_\mu \times \vec{W}_\nu}_{\text{aus nicht-Kommutativitt §4.6}}$

Wechselwirkung von Higgs- und Eichfeldern:

$$\partial^\mu \rightarrow D^\mu = \partial^\mu + i \frac{g}{2} \vec{\tau} \cdot \vec{W}^\mu + i \frac{g'}{2} B^\mu$$

Vakuum-Erwartungswert:

$$\boxed{\Phi_0 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}} \quad v = \mu/\lambda$$

$$\Phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + \eta(x) \end{pmatrix}$$

$$\Rightarrow \mathcal{L} = \underbrace{\left[\frac{1}{2} (\partial^\mu \eta)(\partial_\mu \eta) - \mu^2 \eta^2 \right]}_{\textcircled{1}} - \frac{1}{4} F_{\mu\nu}^i F^{\mu\nu i} - \frac{1}{4} f_{\mu\nu} f^{\mu\nu} \\ + \underbrace{\frac{1}{2} \frac{g^2 v^2}{4} (|W_\mu^+|^2 + |W_\mu^-|^2)}_{\textcircled{2}} + \underbrace{\frac{1}{2} \frac{v^2 g^2}{4 \cos^2 \theta_W} |Z_\mu|^2}_{\textcircled{3}}$$

① Massives Higgs - Boson $m_H = \sqrt{2} \mu$

② Massive W - Bosonen $m_W = \frac{gv}{2}$

③ Massives Z - Boson $m_Z = \frac{gv}{2 \cos \theta_W} = \frac{m_W}{\cos \theta_W}$

④ kein Masse term f. Photon

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