

# Structure Function Measurements at HERA



## Benno List



for the H1 and ZEUS Collaborations

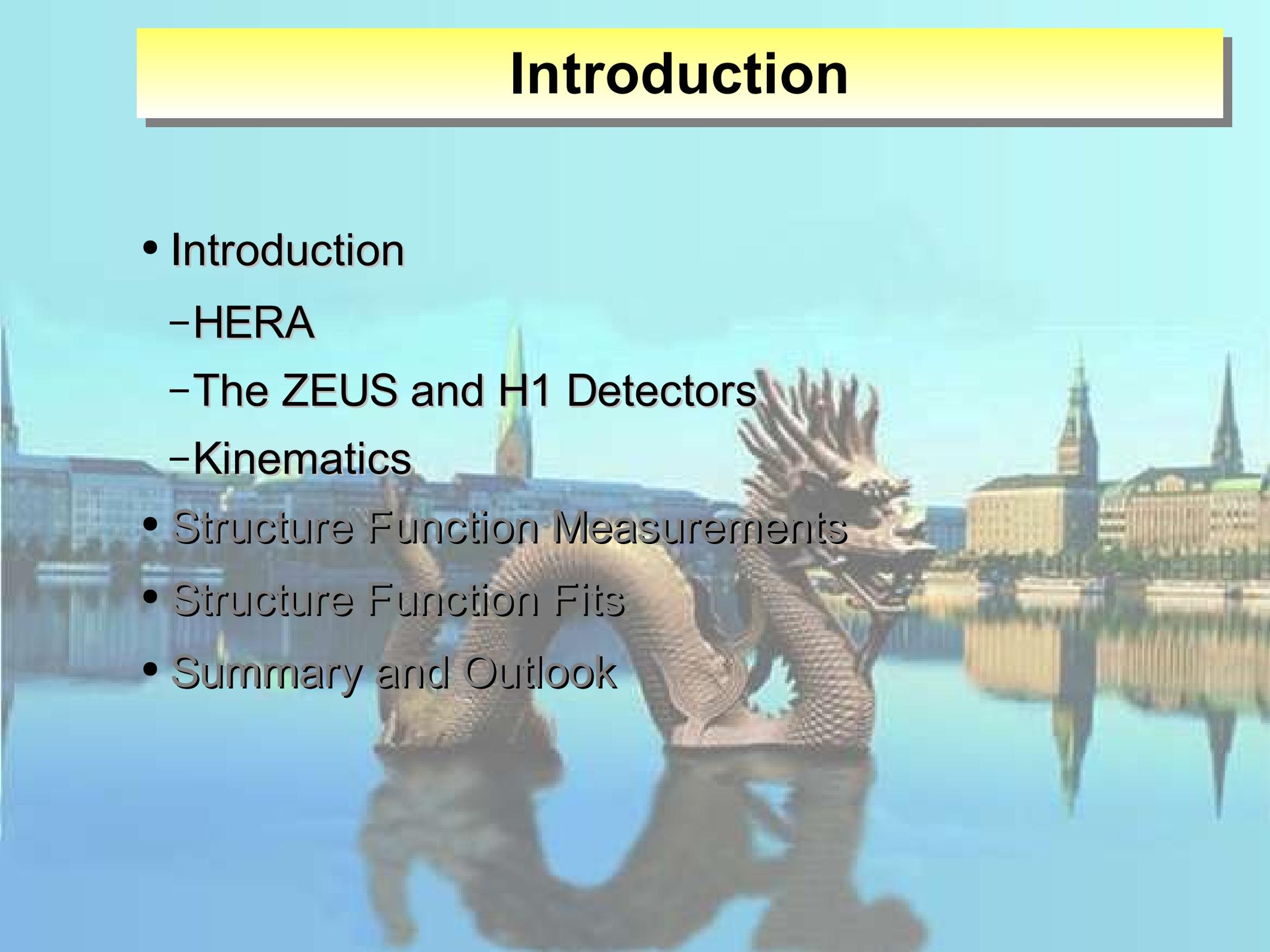
## Sino-German Workshop on Frontiers in QCD

21.9.2006

- Introduction
- Structure function measurements
- Structure function fits: parton densities and  $\alpha_s$
- Summary and outlook

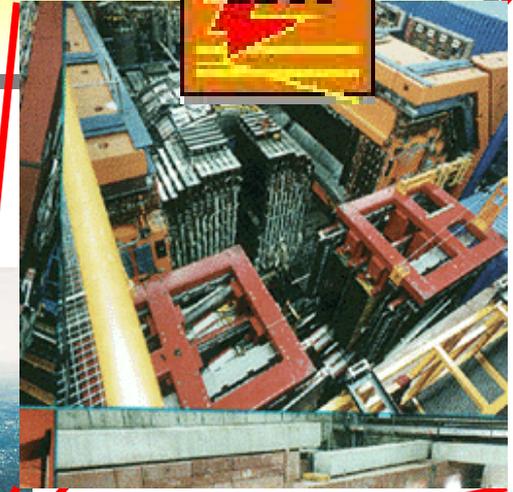
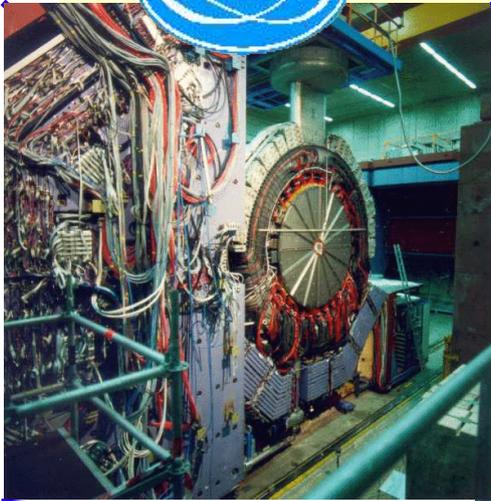
# Introduction

- Introduction
  - HERA
  - The ZEUS and H1 Detectors
  - Kinematics
- Structure Function Measurements
- Structure Function Fits
- Summary and Outlook





# HERA



27.5GeV electrons/positrons on 920GeV protons  $\rightarrow \sqrt{s} = 318\text{GeV}$

2 Collider experiments: H1 und ZEUS

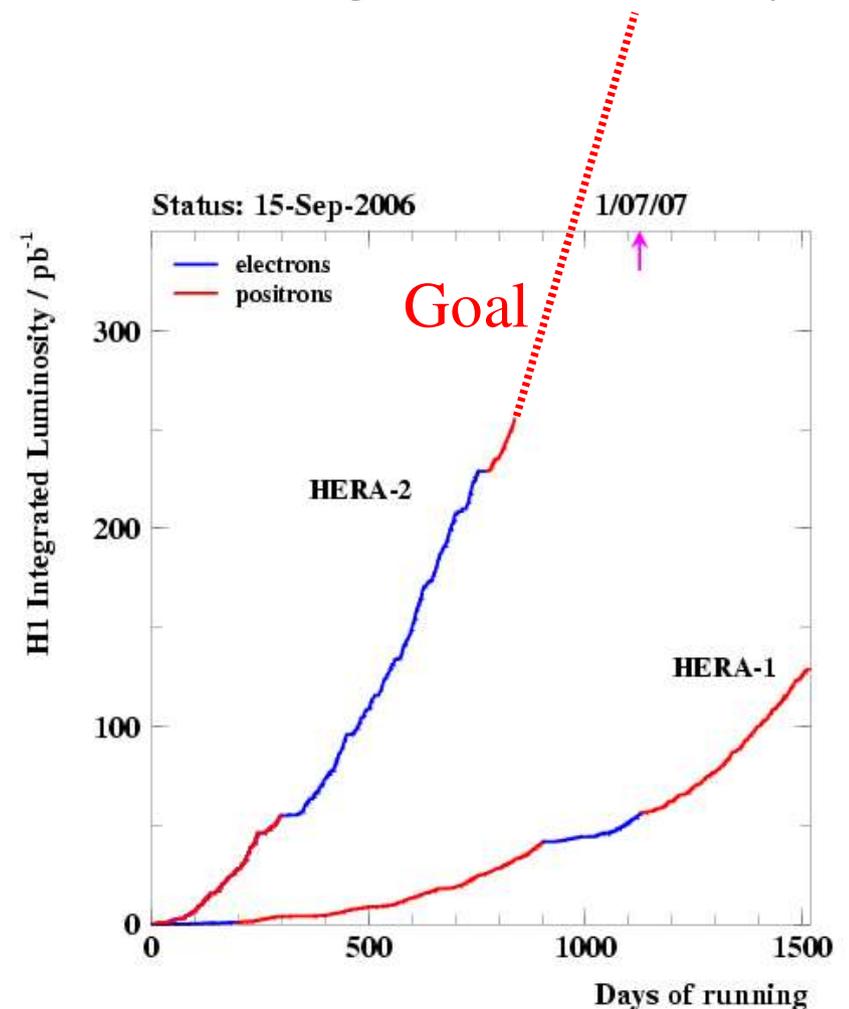
HERA-I:  $16\text{pb}^{-1} e^-p$ ,  $120\text{pb}^{-1} e^+p$

HERA-II: ca.  $500\text{pb}^{-1}$ , ca. 40% polarisation

# Status of HERA-II

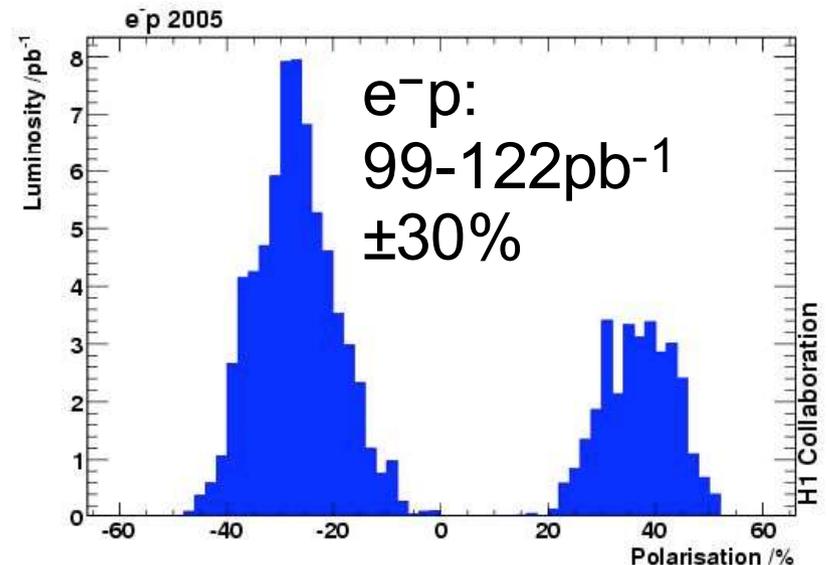
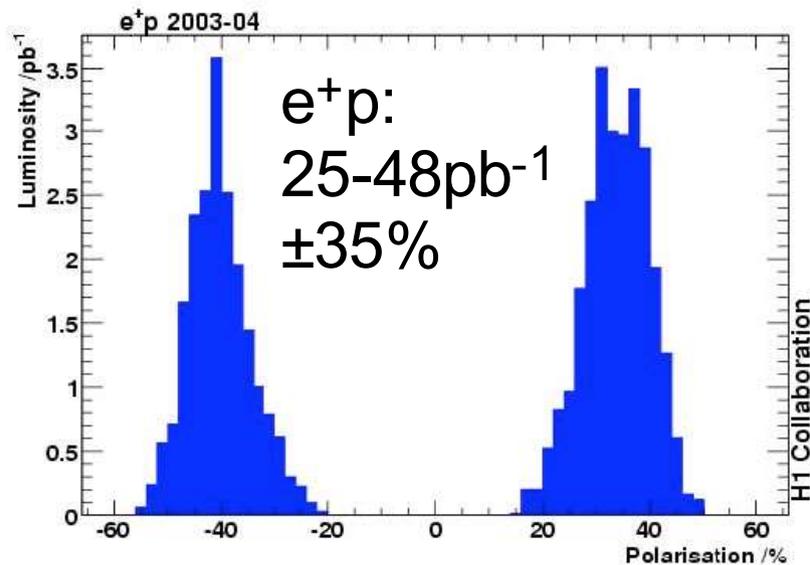
- HERA-I: 1992-2000:  
 $16\text{pb}^{-1} e^-p$ ,  $120\text{pb}^{-1} e^+p$
- Upgrade 2001-2002,  
slow startup
- HERA-II: 2003 - July 2007  
up to now:  
 $\sim 175\text{pb}^{-1} e^-p$ ,  $105\text{pb}^{-1} e^+p$
- $e^+$  running will continue for 6  
more months, then 3 months low  
energy run

## HERA: Integrated Luminosity



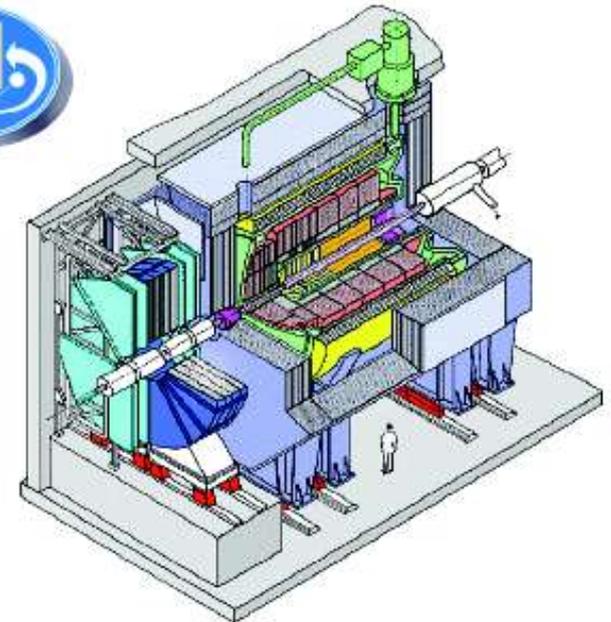
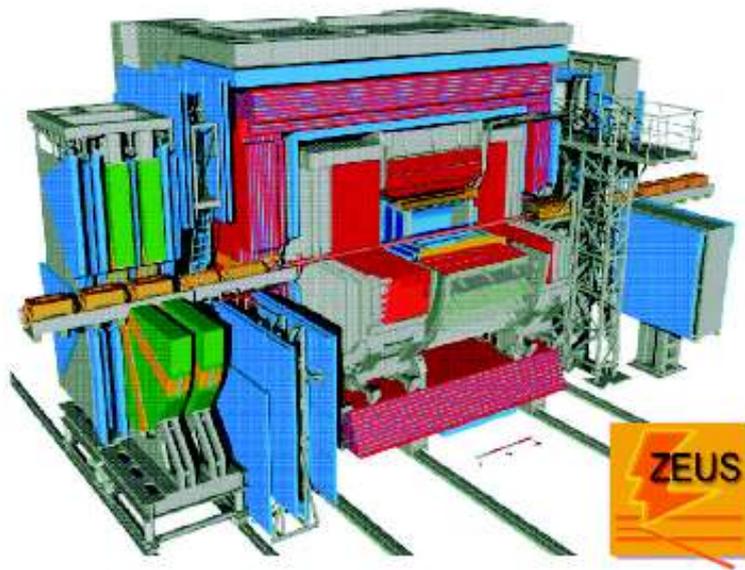
# Lepton Polarization at HERA-II

- New HERA-II feature:  
Use spin rotators to produce longitudinal polarization in experiments
- Allows to measure polarization dependence of high- $Q^2$  processes:
  - Charged currents: limits on right-handed currents
  - Neutral current:  $\gamma Z$  interference



# ZEUS and H1

- Omni-purpose detectors:  
silicon tracking, drift chambers, calorimeter, muon system



Uranium-Scintillator calorimeter:

em:  $\sigma(E)/E = 18\%/\sqrt{E}$

had:  $\sigma(E)/E = 35\%/\sqrt{E}$

Fine-grained LAr calorimeter:

em:  $\sigma(E)/E = 12\%/\sqrt{E} \oplus 1\%$

had:  $\sigma(E)/E = 55\%/\sqrt{E} \oplus 1\%$

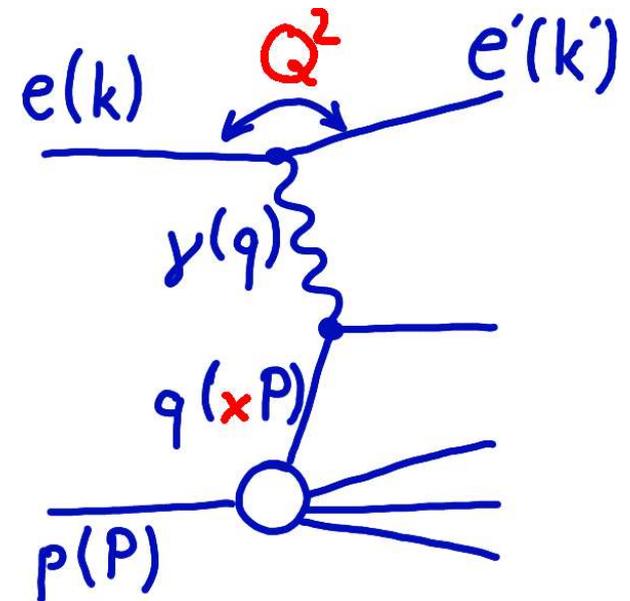
Backward lead-scintillator calo:

em:  $\sigma(E)/E = 7\%/\sqrt{E} \oplus 1\%$

# Kinematics

Quark Parton Model: „Scattering on asymptotically free quarks“

- Photon momentum  $q=k'-k$
- Squared center-of-mass energy  $s=(k+P)^2 \approx 2k \cdot P$
- **Virtuality**  $Q^2 = -q^2$
- **Quark momentum**  $x \cdot P$ :  
Bjorken- $x = Q^2 / (2q \cdot P)$
- Inelasticity  $y = q \cdot P / k \cdot P$   
( $E_\gamma / E_e$  in proton rest system)
- „Master formula“:  $Q^2 = x \cdot y \cdot s$   
 $\Rightarrow$  only 2 independent variables, normally  $x$  und  $Q^2$



**Kinematics can be reconstructed from electron or hadronic final state alone  $\Rightarrow$  over constrained!**

# Structure Functions, Parton Densities

- Hadron tensor is expressed in terms of structure functions  $F_1$ ,  $F_2$ ,  $F_3$

Resulting ep cross section

( $F_3$  is parity violating, vanishes for pure  $\gamma$  exchange):

$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{xQ^4} \left( (1-y)\tilde{F}_2 + y^2 x \tilde{F}_1 \mp \left( y - \frac{y^2}{2} \right) x \tilde{F}_3 \right)$$

- Contributions from  $\gamma$ ,  $Z^0$  exchange and  $\gamma Z$  interference:

$$\begin{aligned} \tilde{F}_2 &= F_2 + k(-v_e \mp P a_e) x F_2^{\gamma Z} + k^2(v_e^2 + a_e^2 \pm P v_e a_e) x F_2^Z \\ x \tilde{F}_3 &= k(-a_e \mp P v_e) x F_3^{\gamma Z} + k^2(2v_e a_e \pm P(v_e^2 + a_e^2)) x F_3^Z \end{aligned}$$

- Structure functions are calculated from parton densities:

$$F_2 = x \sum_q e_q^2 (q + \bar{q})$$

- Parton densities depend on  $x$  and  $Q^2$ ,  
they can be evolved in  $Q^2$  using the DGLAP equations

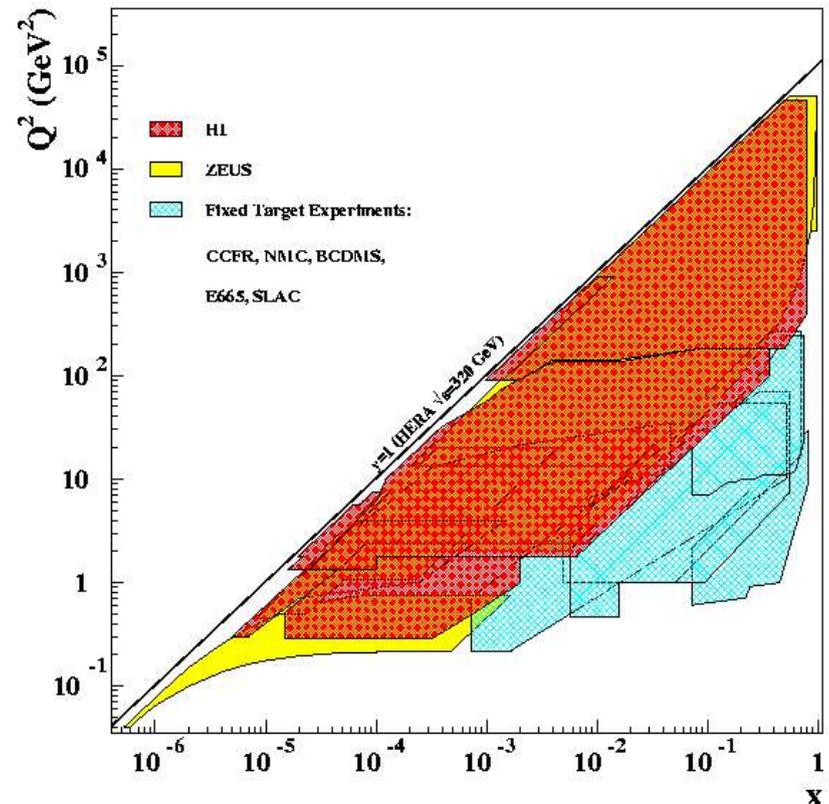
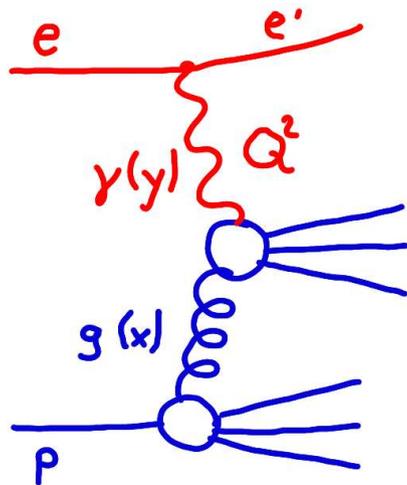
# Kinematic Plane

HERA covers more than 5 orders of magnitude in  $x$  und  $Q^2$

- Opens region at very low  $x \Rightarrow$  high parton densities
- Tests evolution of parton densities over a wide  $Q^2$  region

$$Q^2 = x \cdot y \cdot s$$

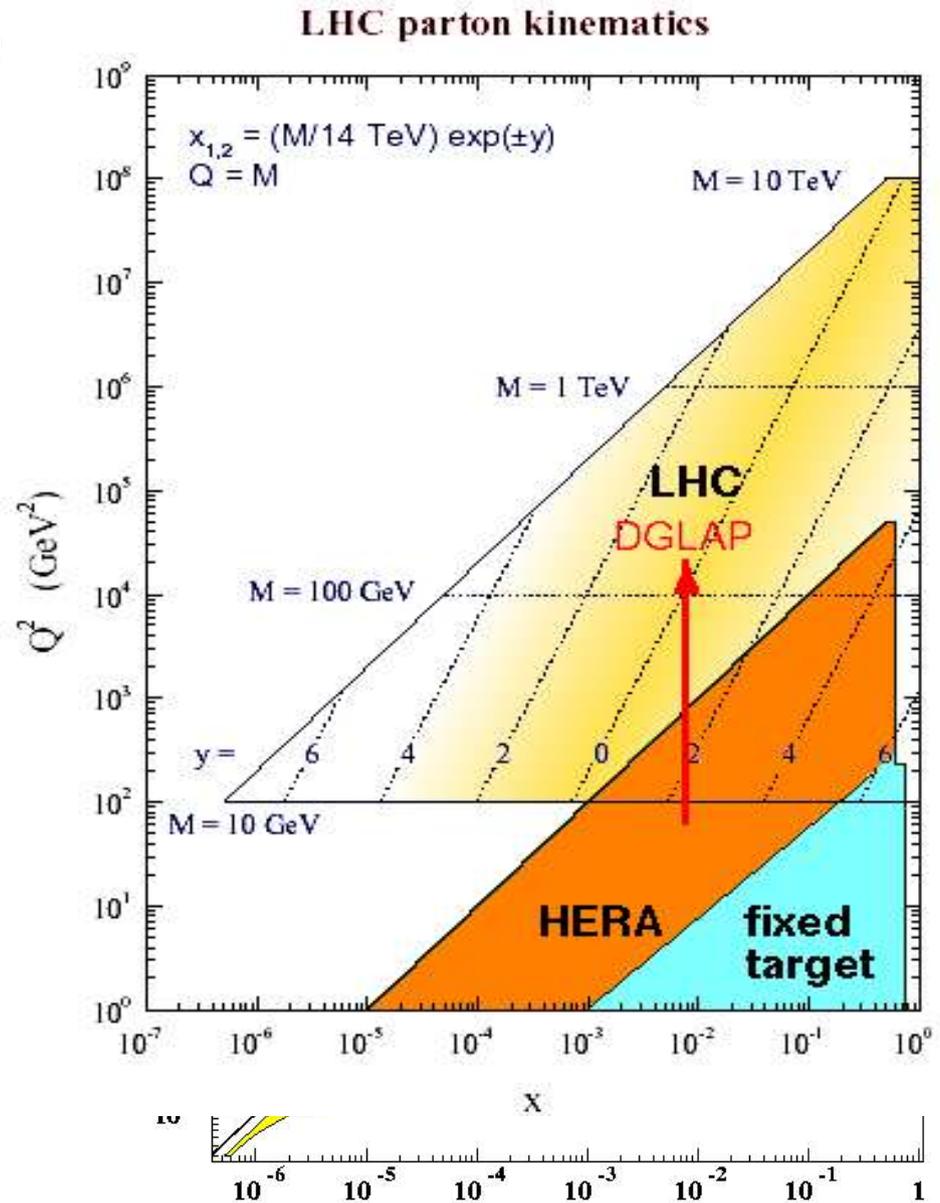
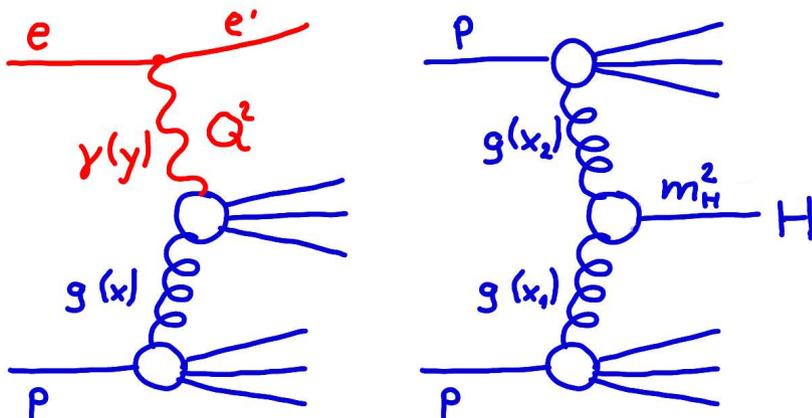
$\Rightarrow$  Usable  $y$  range determines kinematically accessible range



# HERA and LHC

HERA results essential for predictions of LHC processes:

- Gluon density
- Quark density at large  $x$   
 $\Rightarrow$  Discovery potential!  
 Needs high Luminosity:  
 HERA-II!



# Structure Function Measurements

- Introduction
- Structure Function Measurements
  - $F_2$  in the bulk data
  - $F_2$  in corners of phase space
  - $F_1 / F_L$  measurements
  - $F_3$  measurements
  - Flavour-exclusive measurements:  $F_2^{c\bar{c}}$ ,  $F_2^{b\bar{b}}$
  - Charged current measurements
- Structure Function Fits
- Summary and Outlook

# The Bulk Data: $F_2$

- Large part of phase:  $F_2$  dominates cross section

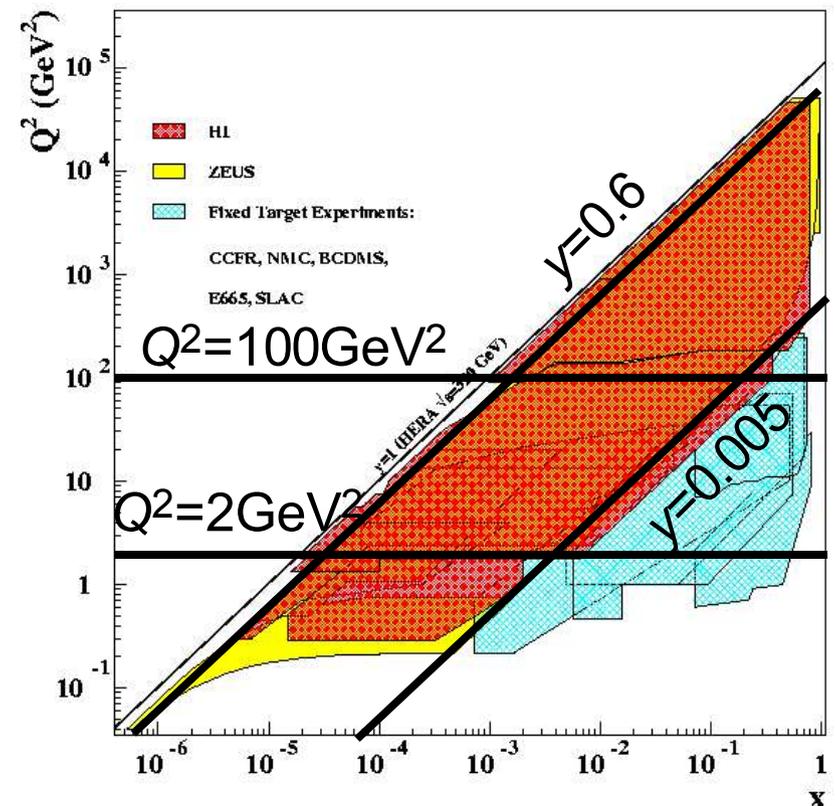
$$\frac{d^2\sigma_{\text{NC}}^{\pm}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left( Y_+ F_2 \mp Y_- F_3 - y^2 F_L \right) \quad Y_{\pm} = 1 \pm (1-y)^2$$

- Bulk data:

- $0.005 < y < 0.6$ :  
Electron well measured
- $Q^2 > 2 \text{ GeV}^2$ :  
Electron in main detector  
( $Q^2 < 100 \text{ GeV}^2$ : rear calorimeter)

- $F_L, xF_3 \ll F_2$

$$F_2 = x \sum_q e_q^2 (q + \bar{q})$$

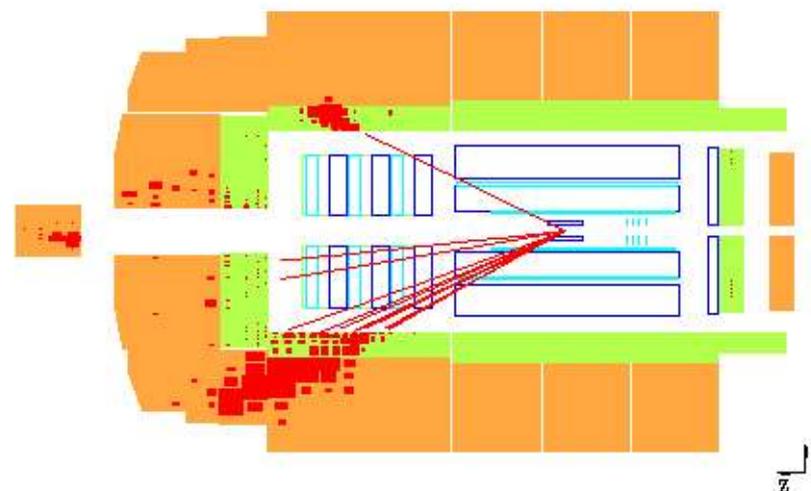


# Typical DIS Events



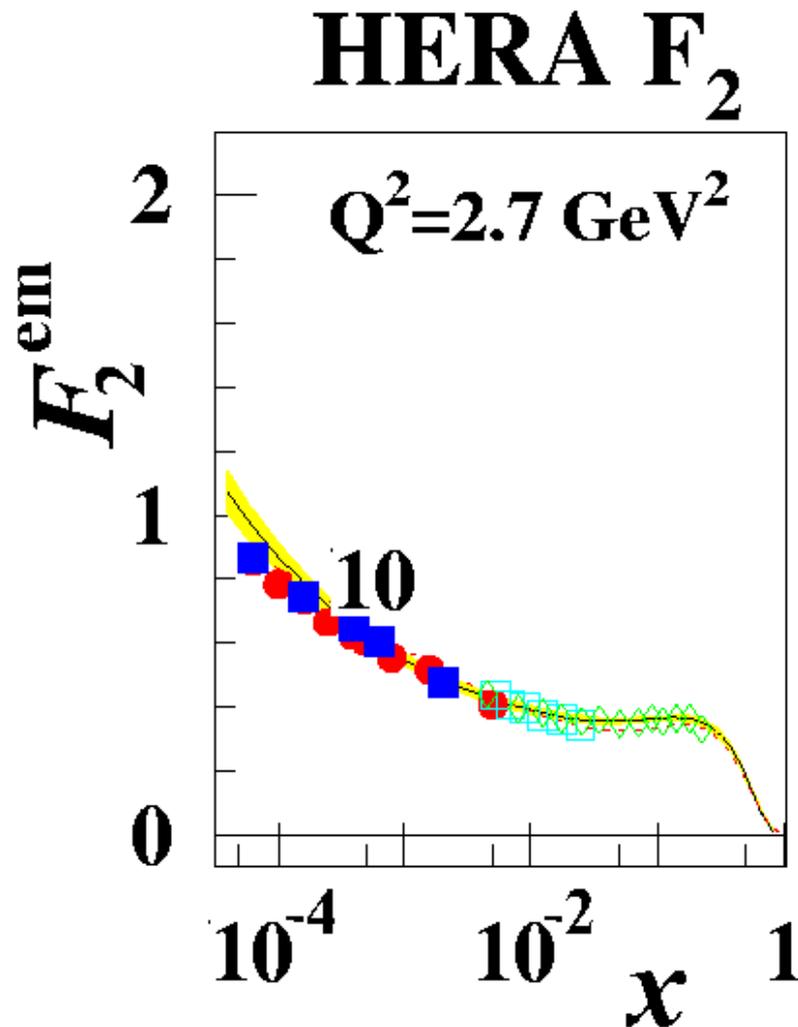
A low- $Q^2$  event in ZEUS:  
electron in rear calorimeter

$$Q^2 = 25030 \text{ GeV}^2, \quad \gamma = 0.56, \quad M = 211 \text{ GeV}$$



A high- $Q^2$  event in H1:  
electron in central calorimeter

# Measurement of $F_2$



- Precise data of high quality:  
Error 2-5% of  
 $2.7 < Q^2 < 120 \text{ GeV}^2$
- Foundation for precise parton density fits and determination of  $\alpha_s$
- Excellent description by NLO-QCD-fit: Test of QCD!

 ZEUS NLO QCD fit

 H1 PDF 2000 fit

 H1 96/97

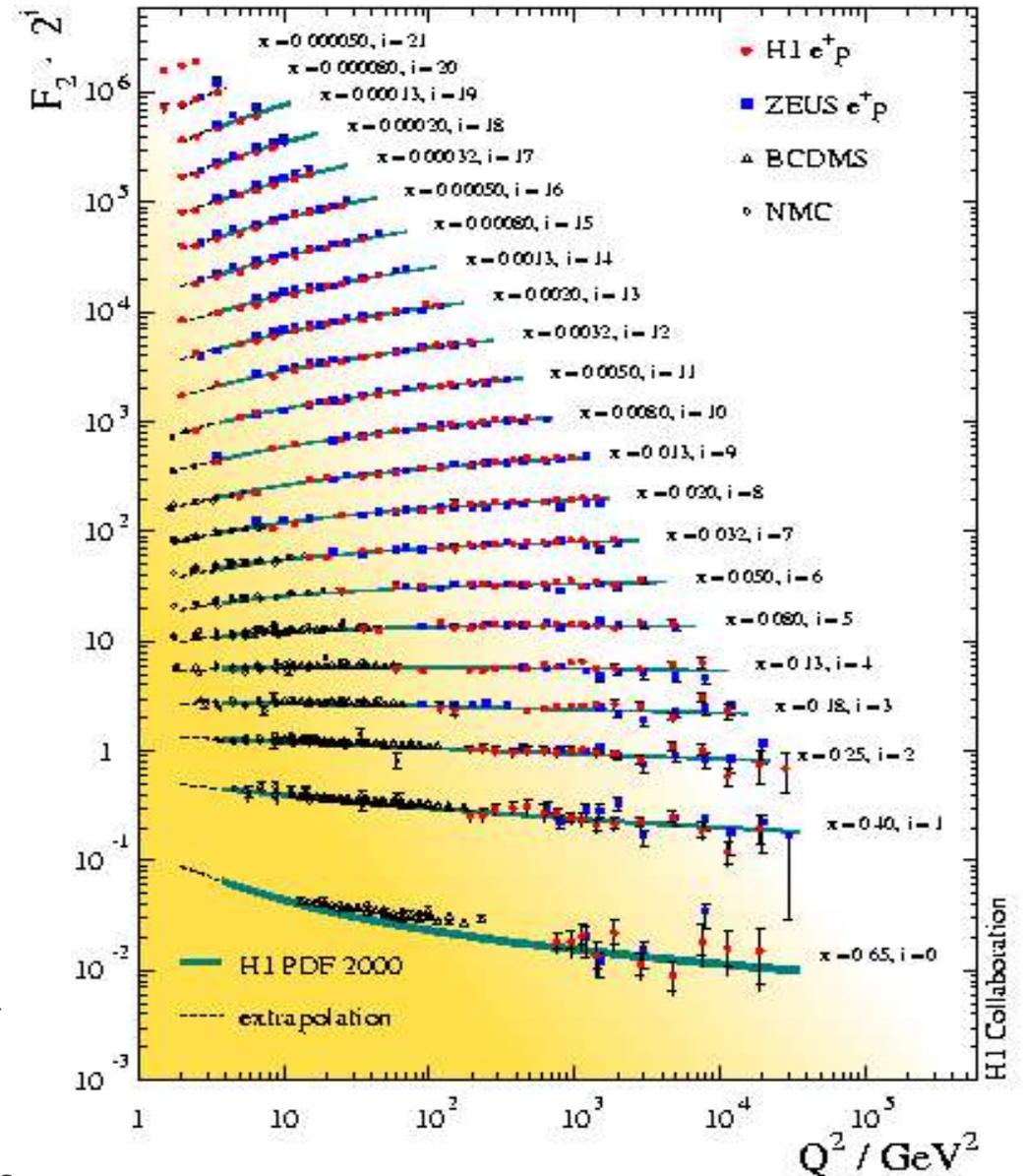
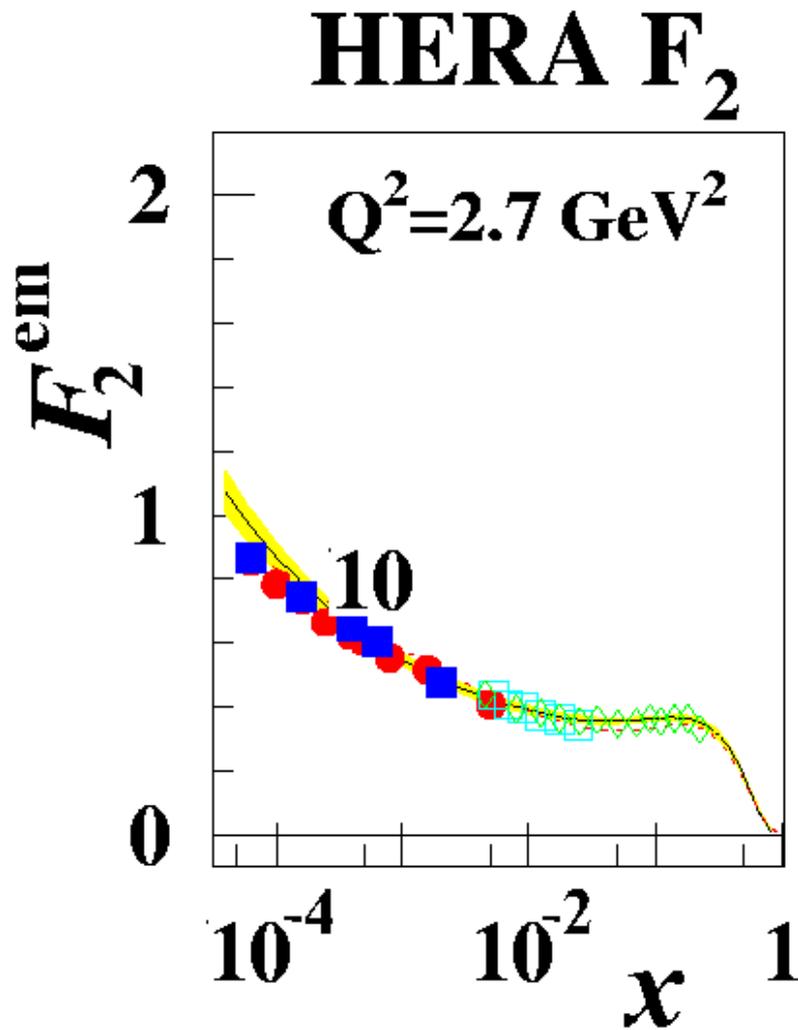
 BCDMS

 ZEUS 96/97

 E665

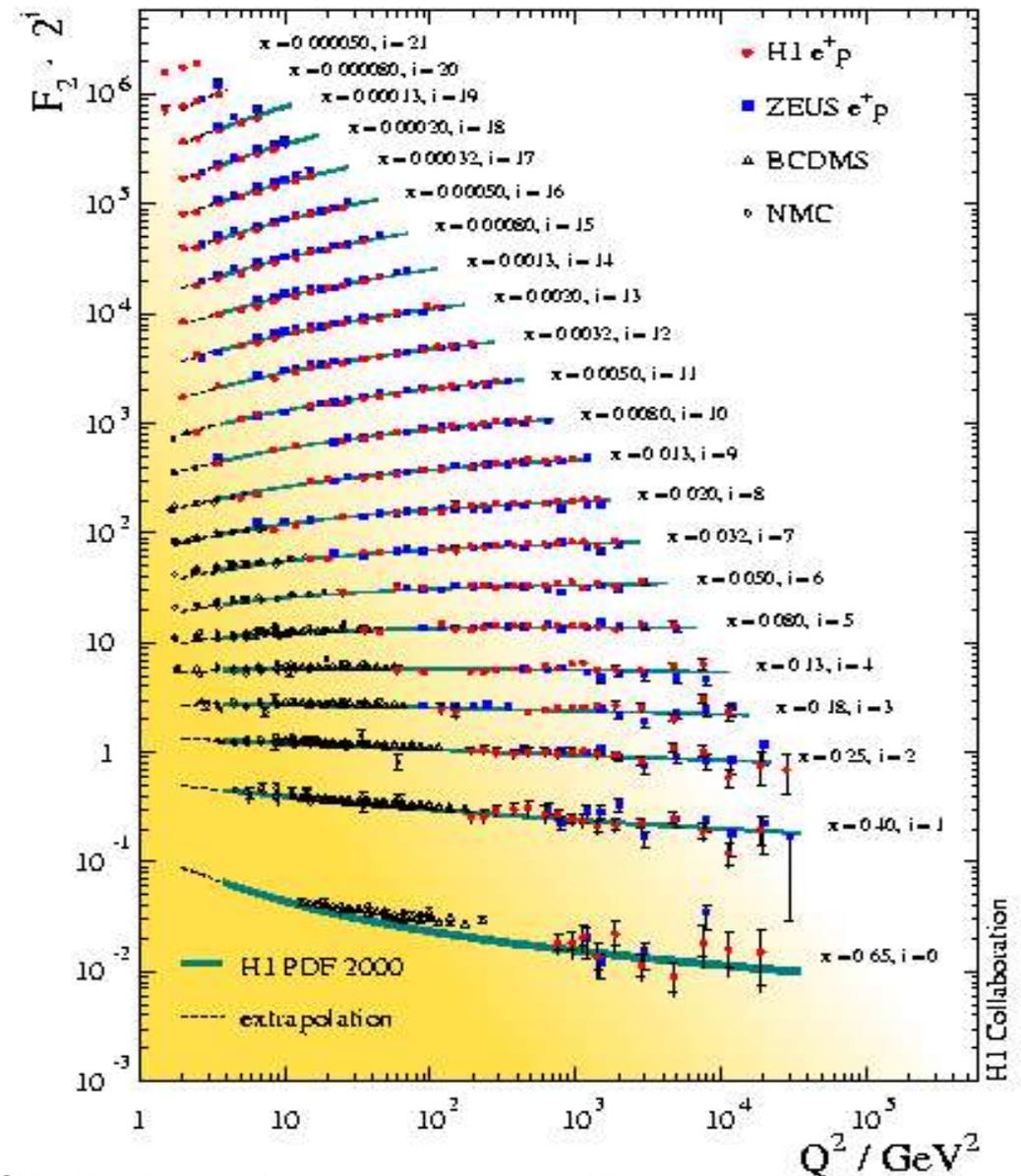
 NMC

# Measurement of $F_2$



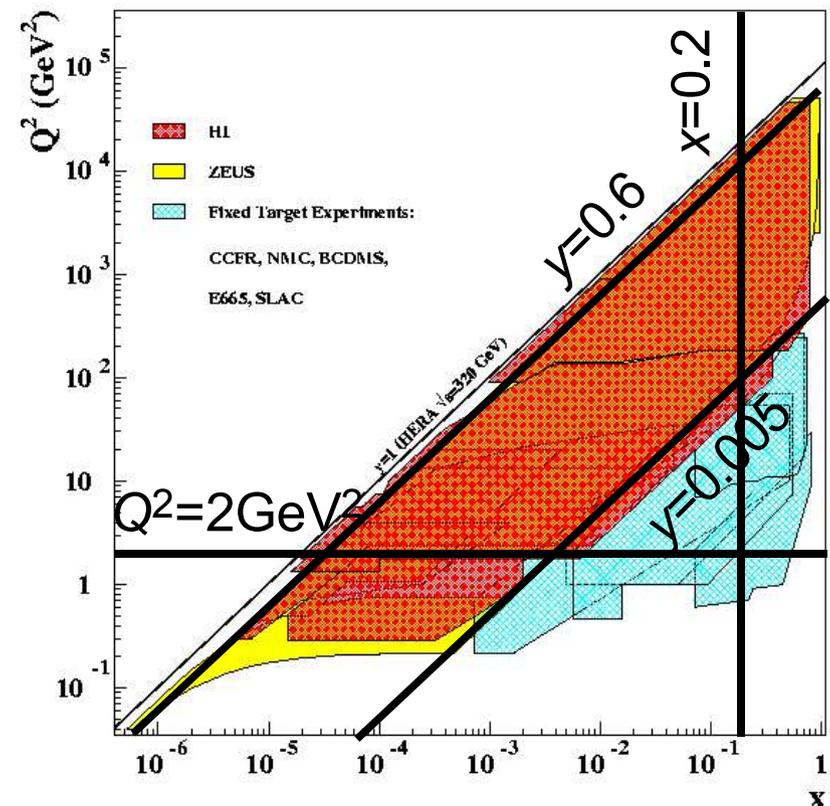
# Overview over $F_2$

- Kinematic region:
  - 4 decades in  $x$ :  
 $0.000065 < x < 0.65$
  - $Q^2$  up to  $30000 \text{ GeV}^2$
- HERA-I data completely analysed
- HERA-II:
  - 3 times ( $e^+$ ) to 10 times ( $e^-$ ) more data
  - => better accuracy at small  $x$ , large  $Q^2$



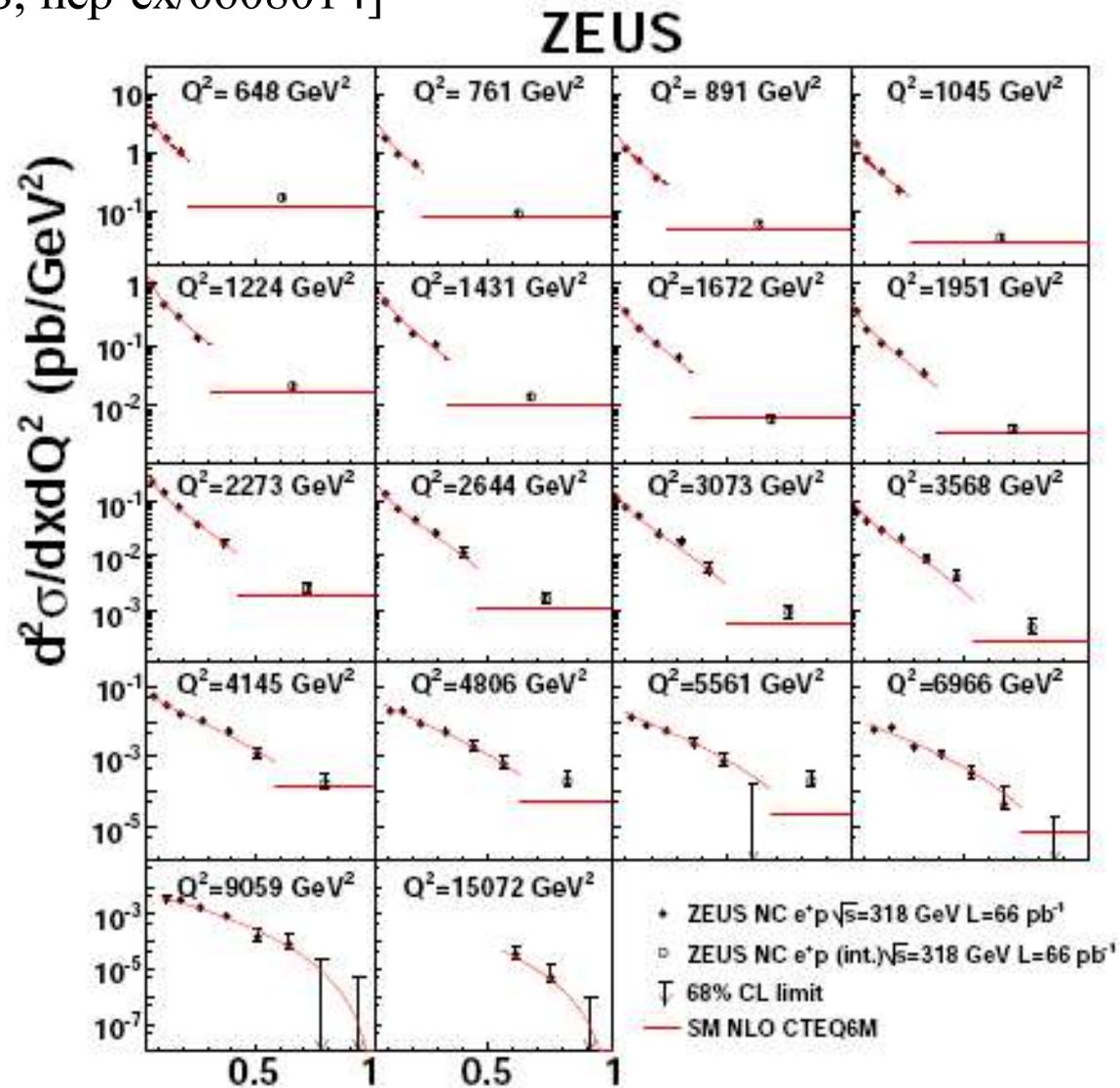
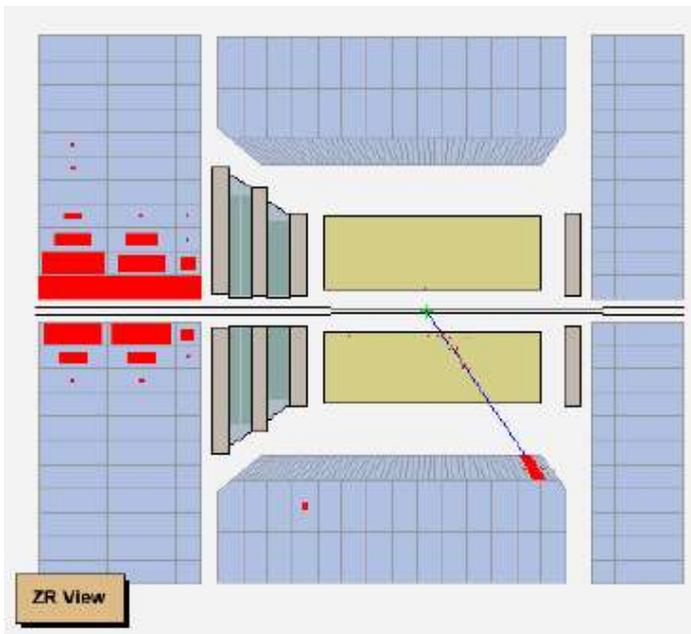
# $F_2$ in Corners of Phase Space

- Very high  $x > 0.2$ : Hadronic final state very close to beam pipe
- Very low  $Q^2 < 2\text{GeV}^2$ : Electron escapes main detector
  - Events with QED radiation
  - Special beam pipe calorimeter (ZEUS)
  - Shifted vertex runs: vertex shifted by 70cm
- Very high  $y > 0.6$  at moderate  $Q^2$ : Small electron energy  $\Rightarrow$  large background



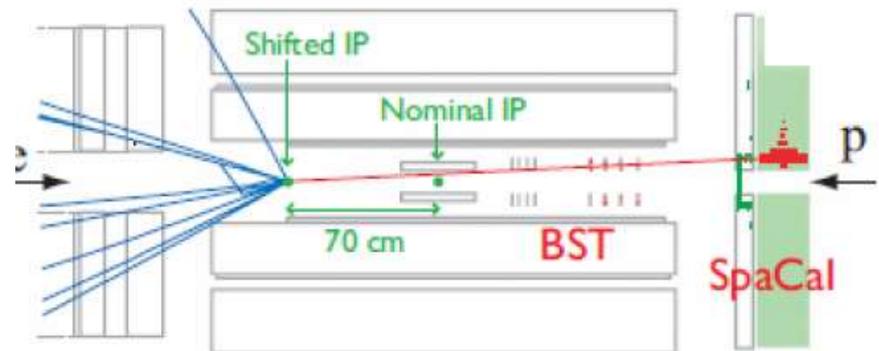
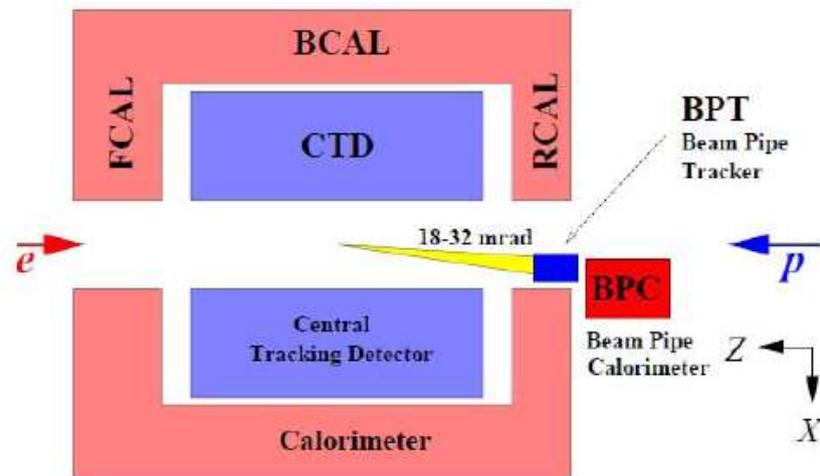
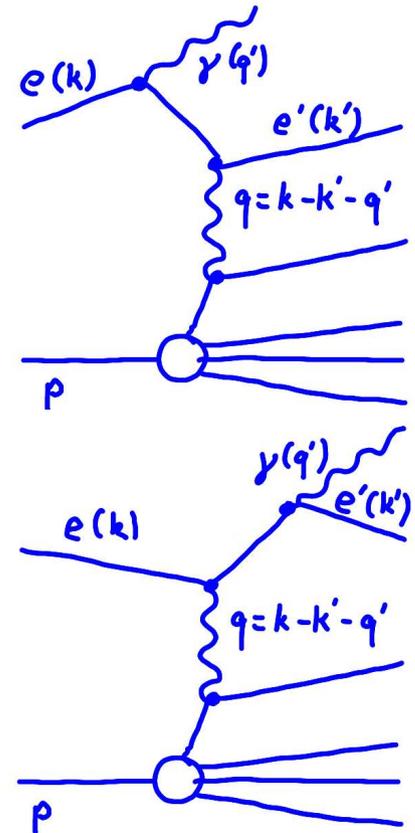
# ZEUS: High $x$ Analysis

- High  $x$ : Hadronic final state very close to forward beam pipe  
New ZEUS analysis [ZEUS, hep-ex/0608014]
- Data agree with SM expectation, but are on the high side



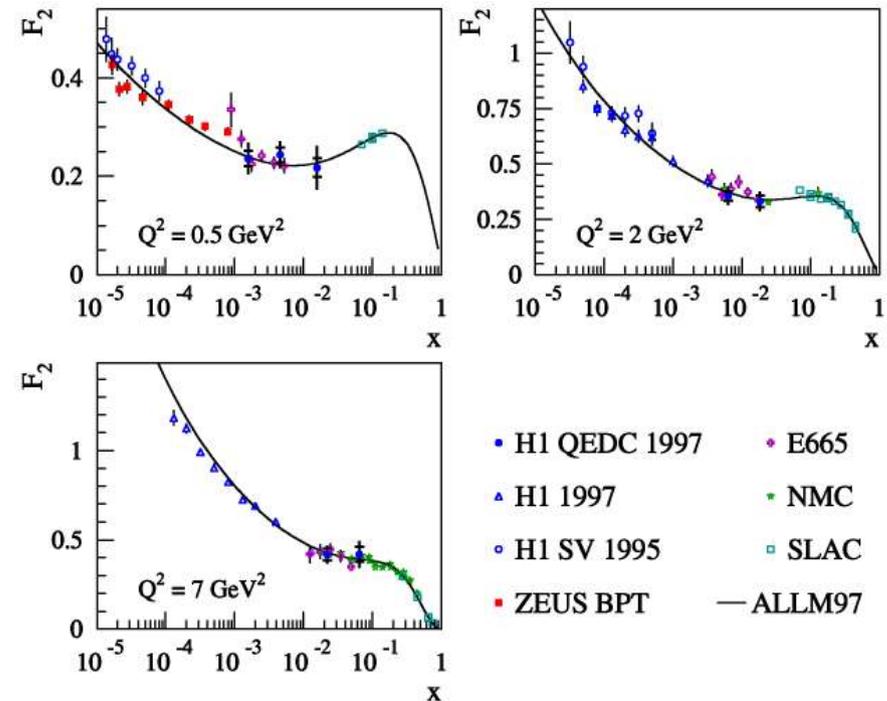
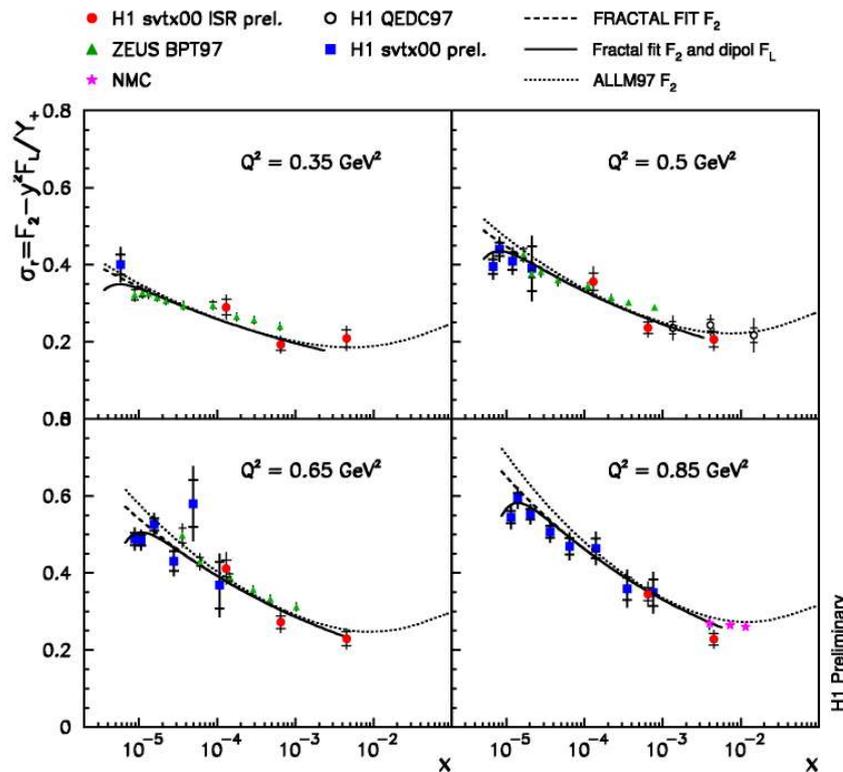
# Accessing Low $Q^2$

- Radiative events: Momentum of exchanged photon reduced by QED radiation
- ZEUS: BeamPipe Calorimeter BPC plus BeamPipe Tracker BPT
- H1: Backward Silicon Tracker BST + data from shifted vertex runs



# Result of Low- $Q^2$ Measurements

- Overlap with fixed target data (E665, NMC, SLAC): consistent results
- Data agree with parametrization ALLM97 [Abramowitz & Levi, hep-ph/9712415]



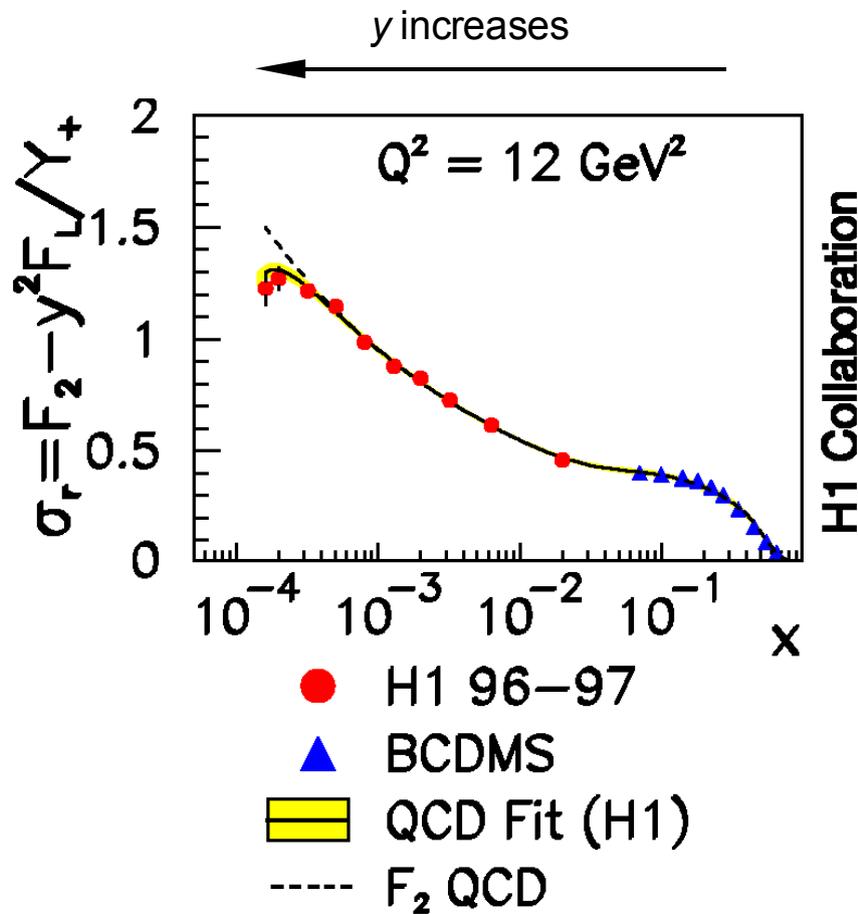
HERA Data: ZEUS, PL B487(2000)53; H1, PL B598(2004)159; H1, EPJ C21(2001) 33; H1prelim-04-042.

# Measuring $F_1/F_L$

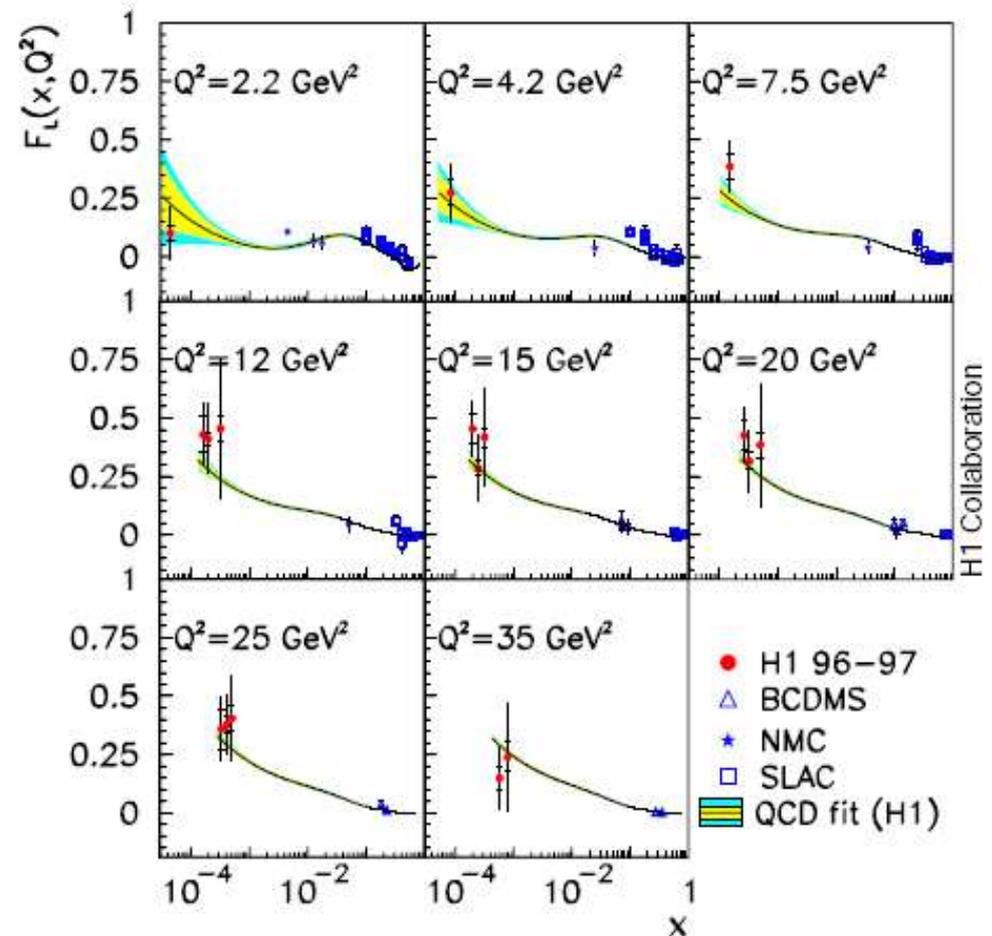
- Callan-Gross-Relation:  $F_L = F_2 - 2xF_1 = 0$   
valid in naive Quark-Parton-Model (QPM)
- QCD predicts nonzero  $F_L$
- True  $F_L$  measurement needs cross section measurements at same  $x$ ,  $Q^2$ , but different  $y \Rightarrow$  Vary beam energies!  
 $\Rightarrow$  Planned for last 3 months of HERA-II data taking (next summer)
- Other method: Measure ,  $\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} Y_+ \underbrace{\left( F_2 - \frac{y^2}{Y_+} F_L \right)}_{\sigma_r}$   
evolve  $F_2$  from at fixed  $x$  from low  $Q^2 =$  low  $y$  to high  $y$   
 $\Rightarrow$  difference between  $F_2$  and  $\sigma_r$  gives  $F_L$
- High  $y \Rightarrow$  low electron energy  $\Rightarrow$  high background  
needs excellent understanding of photoproduction background

# $F_L$ Determination

- $F_L$  results in agreement with QCD expectations
- True measurement next summer



H1, EPJ C21(2001)33



# $F_3$

- Remember:

$$\frac{d^2\sigma_{\text{NC}}^{\pm}}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left( Y_+ \tilde{F}_2 \mp Y_- x\tilde{F}_3 - y^2 \tilde{F}_L \right) \quad Y_{\pm} = 1 \pm (1-y)^2$$

- $F_3$  enters with different sign for  $e^-p$  and  $e^+p$  scattering:  
measured from difference of  $e^-p$  and  $e^+p$  cross sections  
 $\Rightarrow$  needs high accuracy data with both lepton charges!
- $F_3$  dominated by  $\gamma Z$  interference,  
measures difference of quark and antiquark densities: valence quarks

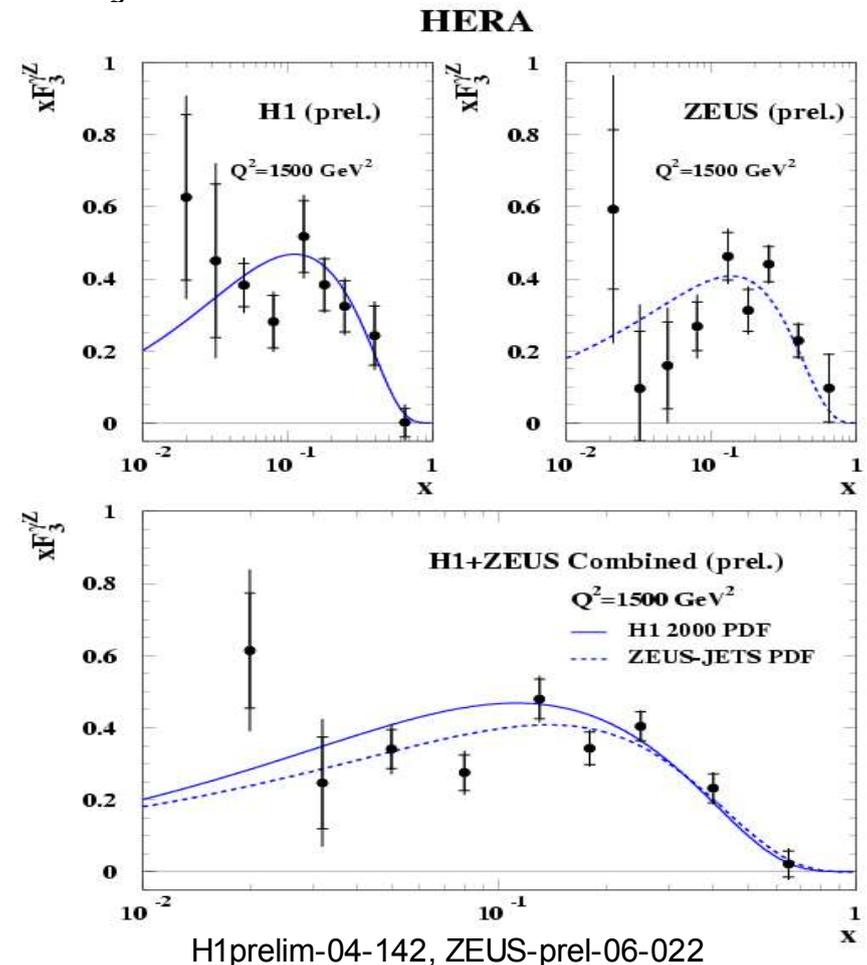
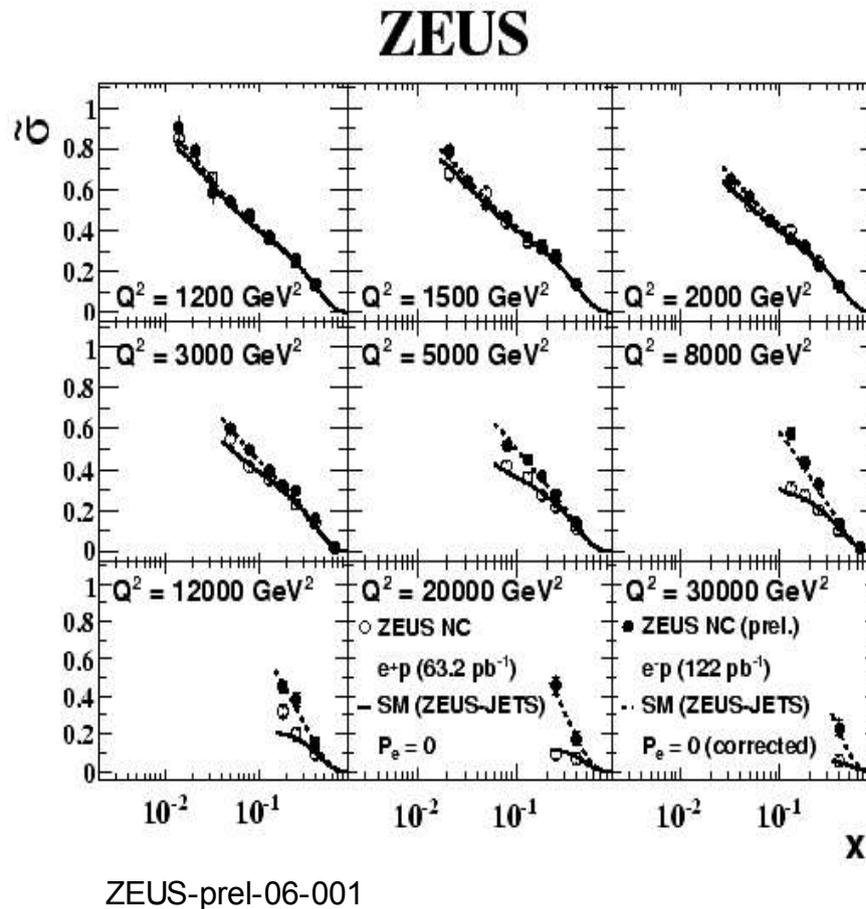
$$x\tilde{F}_3 = k(-a_e)x F_3^{\gamma Z} + k^2(2v_e a_e)x F_3^Z$$

$$x F_3^{\gamma Z} = 2x \sum_q (e_q a_q)(q - \bar{q}) = 2x(2u_v + d_v)$$

- **Dominated by u quark contribution:** larger charge and 2 u quarks

# Measurements of $F_3$

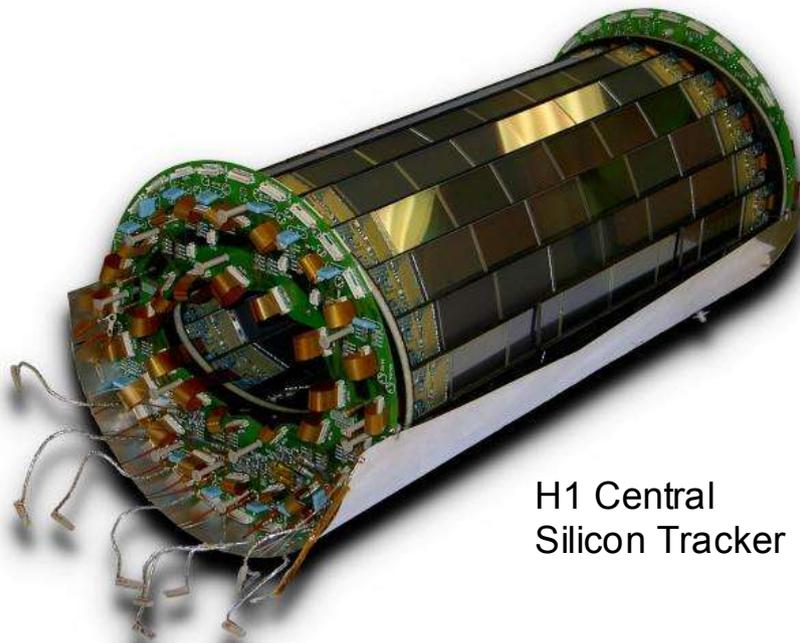
- ZEUS and H1 have measured  $F_3$ , using latest HERA-II  $e^-p$  data
- First combined H1/ZEUS measurement  $\Rightarrow$  overall  $478.8\text{pb}^{-1}$
- Measurement of u valence quark density



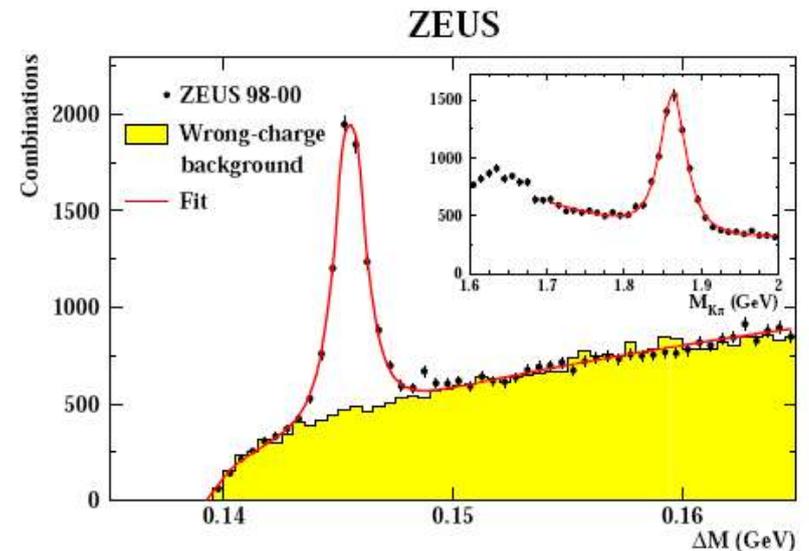


# Flavour-Exclusive Measurements

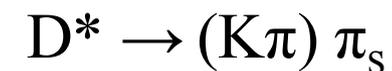
- Define structure functions  $F_2^{c\bar{c}}$ ,  $F_2^{b\bar{b}}$  for charm and beauty production
- Charm tagging:  $D^*$  or lifetime tag; beauty: lifetime tag



H1 Central  
Silicon Tracker



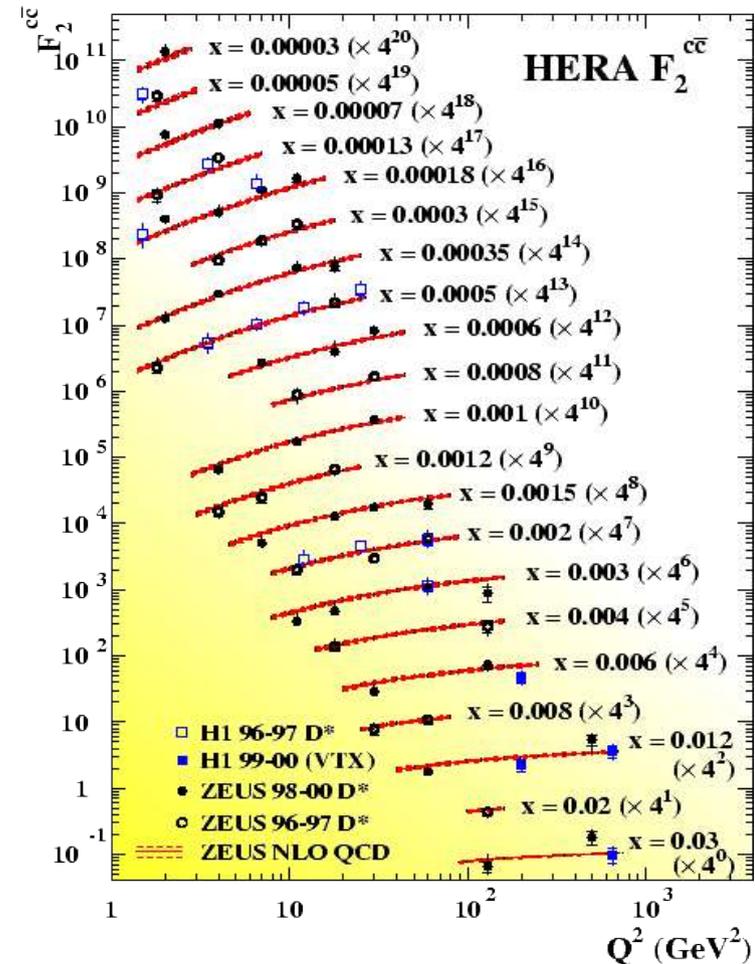
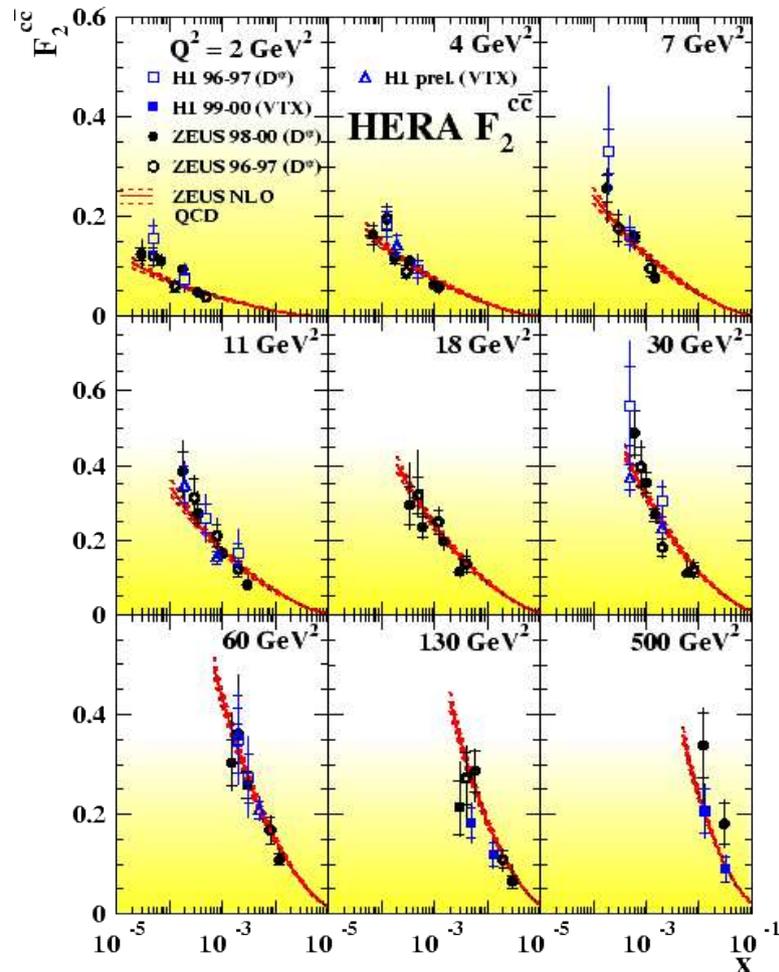
ZEUS, PR **D69** (2004) 012004.



ZEUS BOTTOM MICRO VERTEX DETECTOR

# Charm Contribution

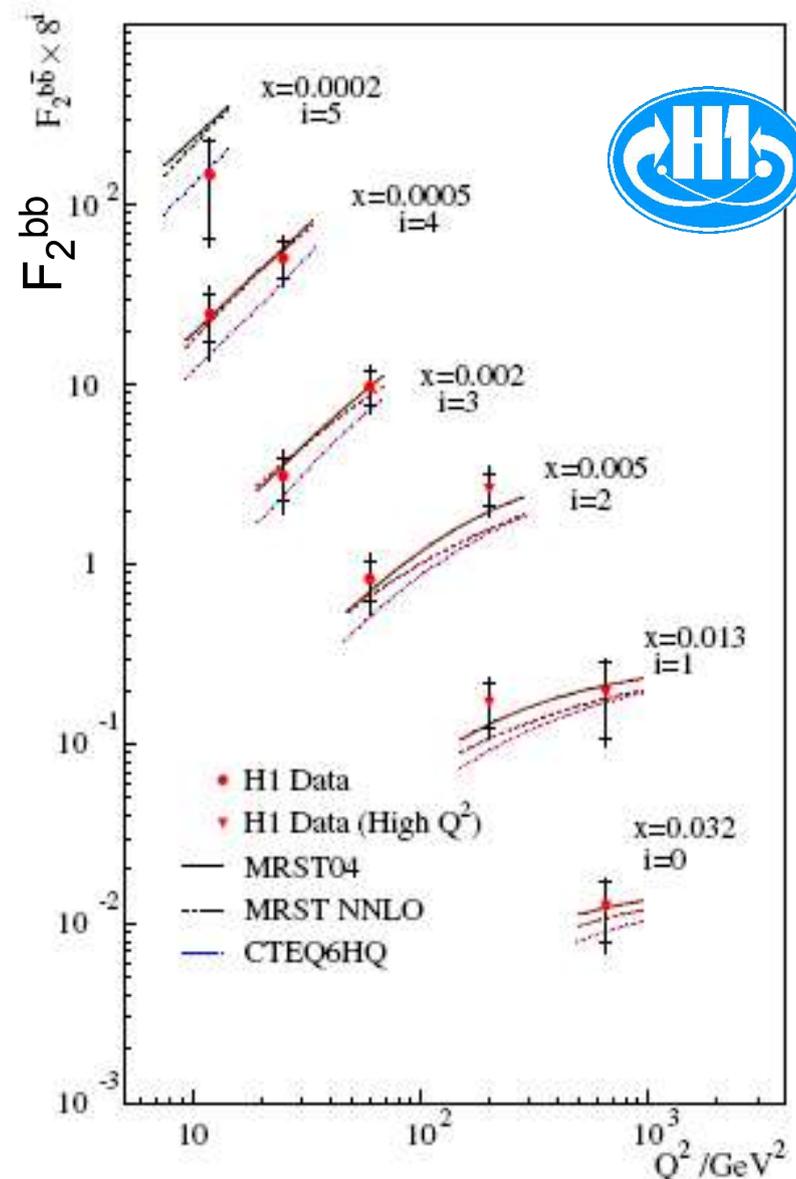
- Charm well described by NLO QCD; at low  $Q^2$ : slight deviations
- Precise enough to constrain the gluon, but: theory uncertainties!



ZEUS, PR D69(2000)012004. H1, EPJ C40 (2005) 349. H1, EPJ C45 (2006) 23.

# Beauty Contribution

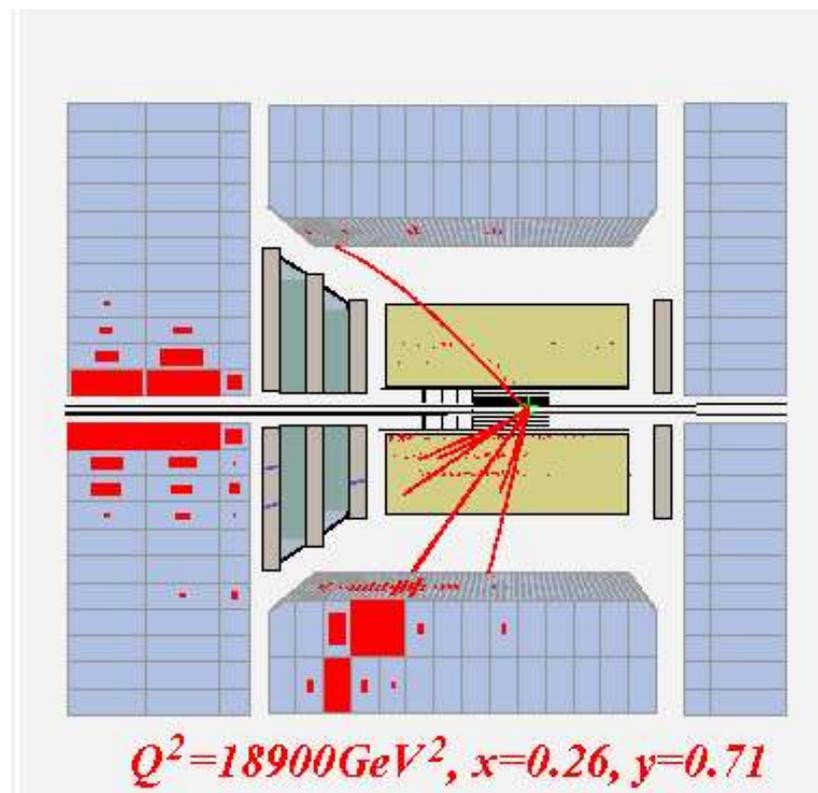
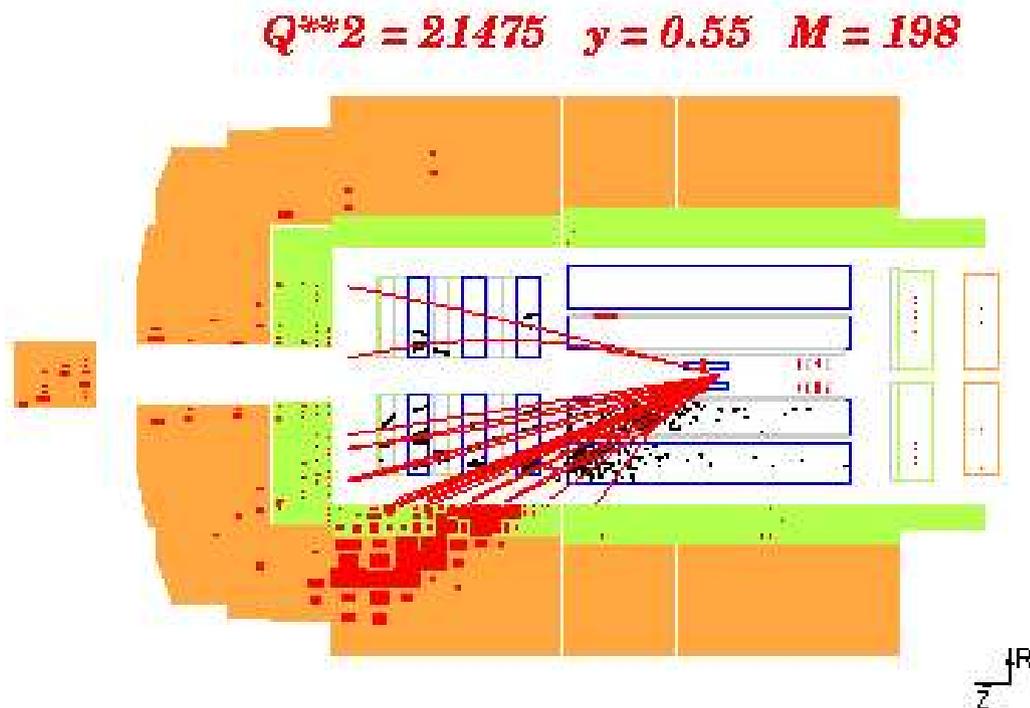
- H1 uses lifetime tagging to extract charm and beauty contribution to  $F_2$  in one measurement
- Reasonably well described by NLO QCD
- NNLO calculations available! [Thorne hep-ph/0506251].
- More data to come from HERA-II



H1, EPJ **C40** (2005) 349. H1, EPJ **C45** (2006) 23.

# Charge Current Interactions

- Neutrino escapes the detector  
=> reconstruct event from hadronic final state  
=> need excellent energy and spatial resolution



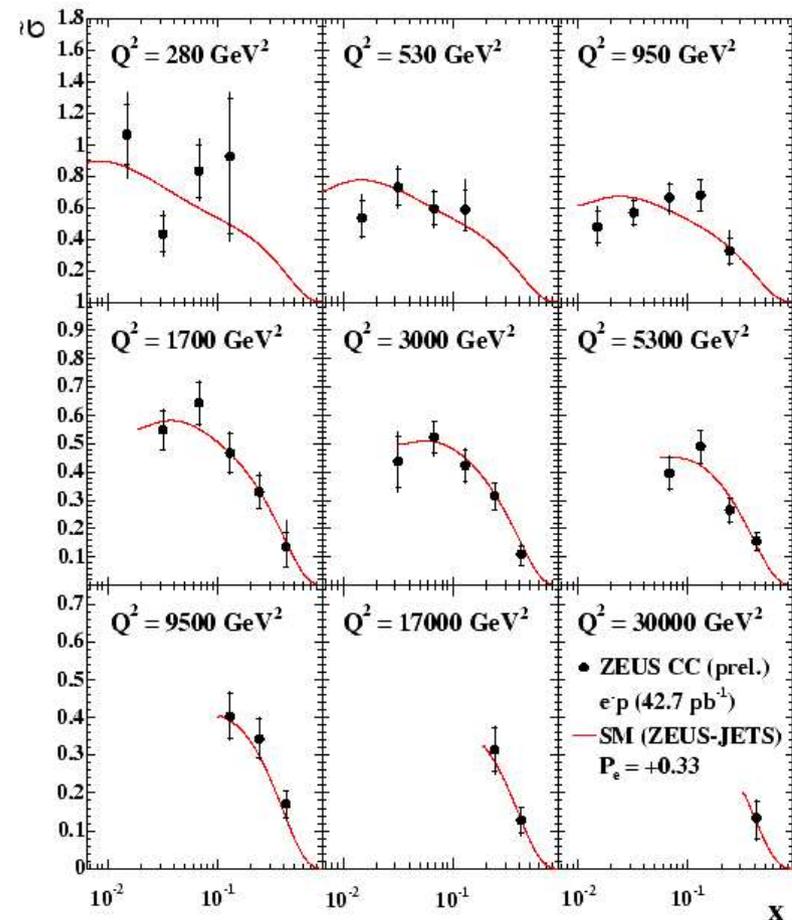
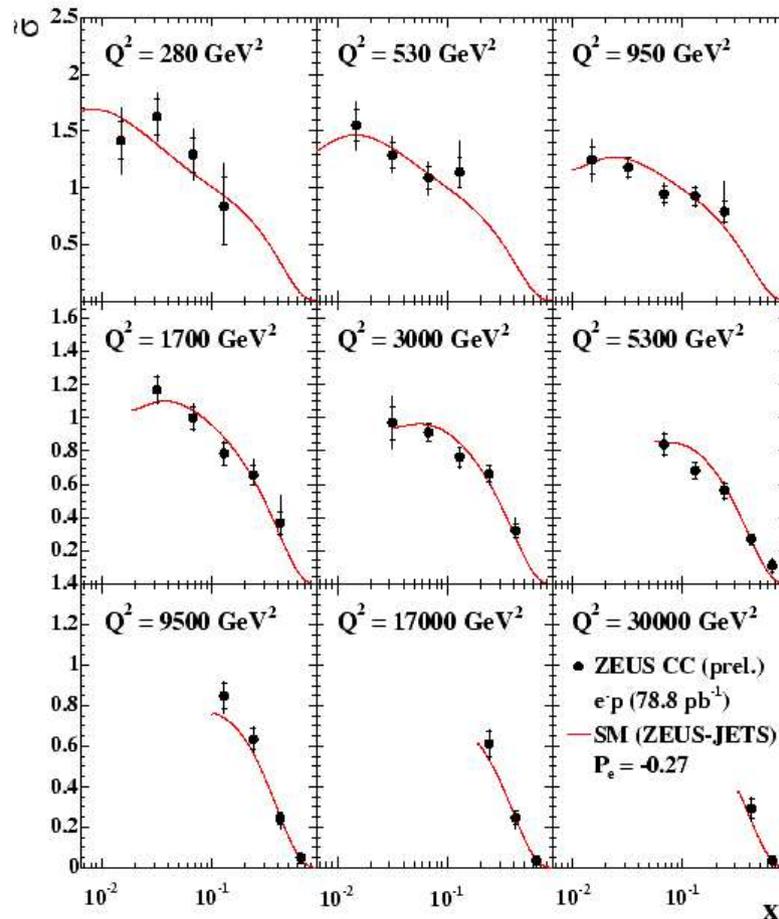
# Double Differential Cross Sections

- Reduced cross section: 
$$\frac{d^2\sigma_{CC}(e^-p)}{dx dQ^2} = \frac{G_F^2}{4\pi x} \underbrace{(1 - P_e) (Y_+ F_2^{CC} + Y_- xF_3^{CC})}_{\tilde{\sigma}_r}$$

## HERA-II Data

ZEUS Left-handed

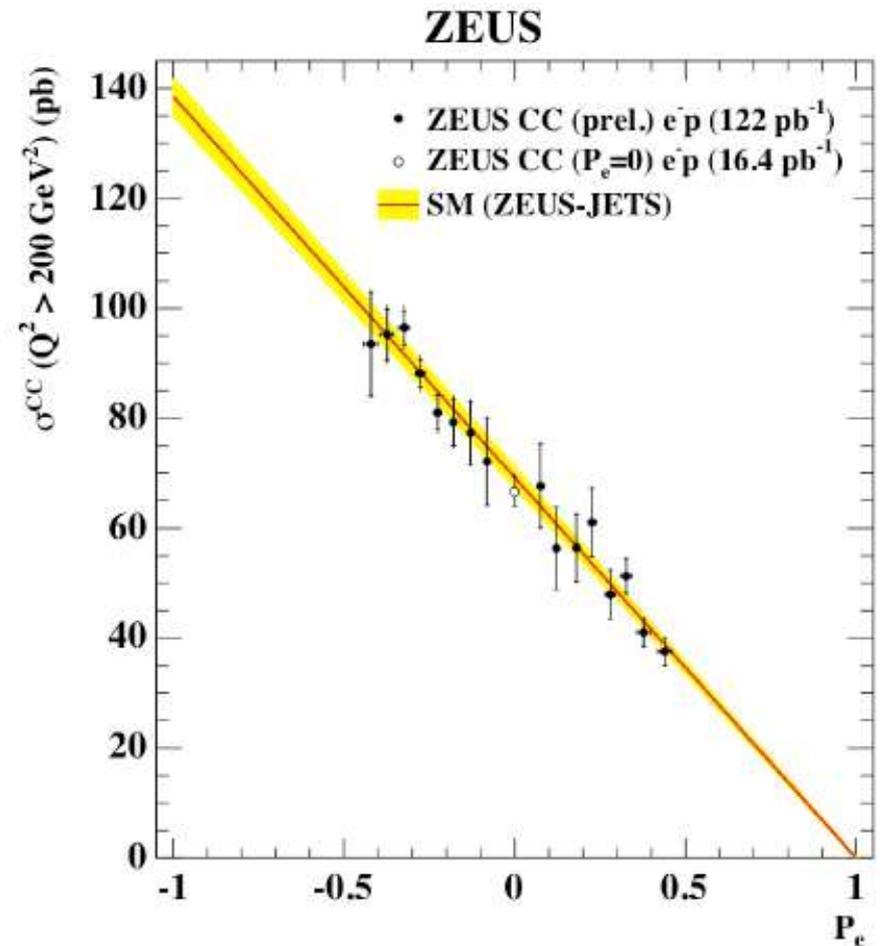
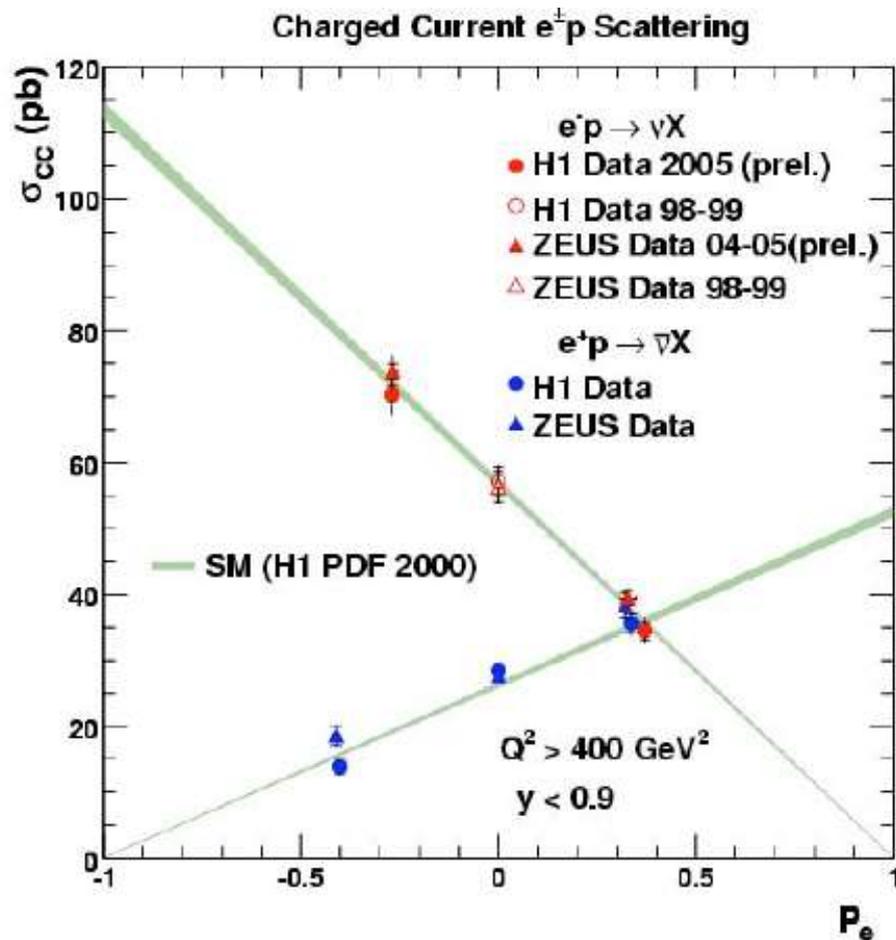
ZEUS Right-handed



ZEUS-prel-06-002

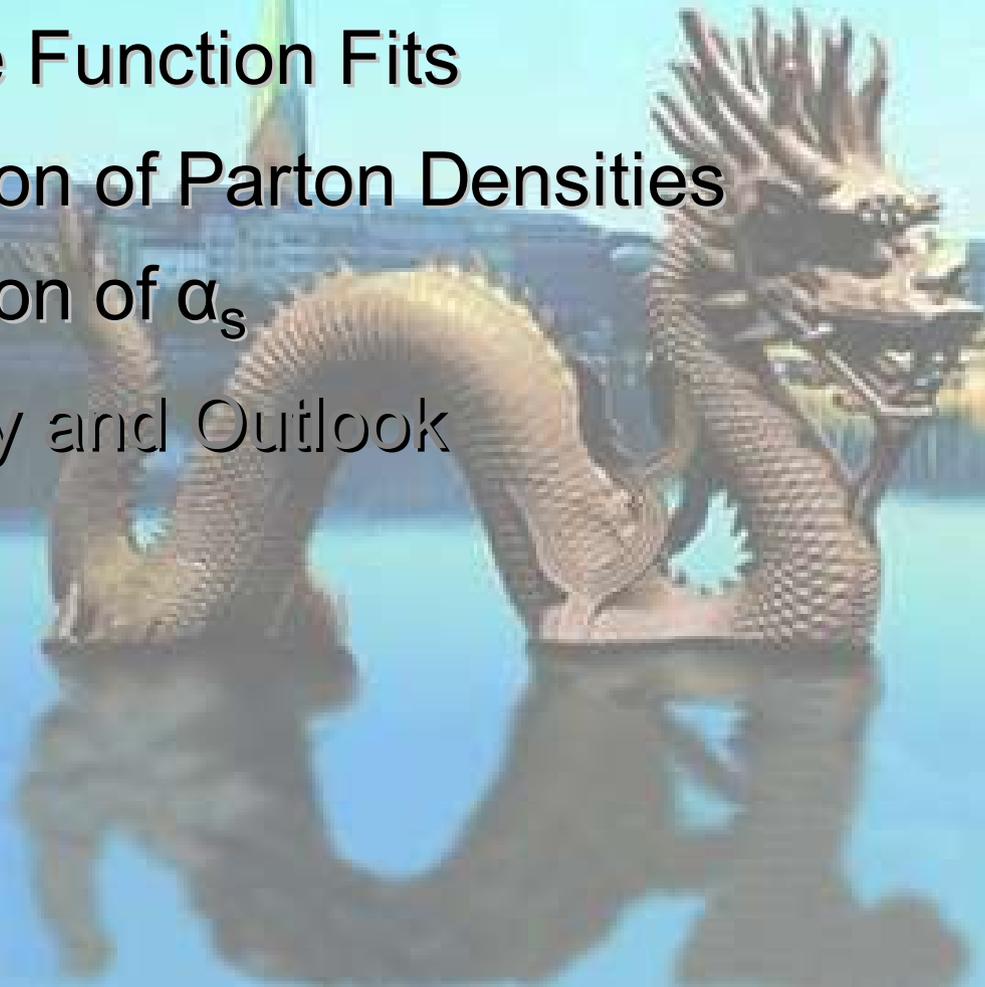
# Probing the Helicity Structure

- Integrated CC cross section proportional to  $(1 \pm P_e)$ :  
A textbook plot!



# Structure Function Fits

- Introduction
- Structure Function Measurements
- Structure Function Fits
  - Extraction of Parton Densities
  - Extraction of  $\alpha_s$
- Summary and Outlook



# Fitting Parton Densities

Theoretical Input:

- Sum rules
- Isospin relations
- Prejudice

Parametrization at  
starting scale  $Q_0^2$

$\alpha_s$

Parton density  
evolution code  
(NLO DGLAP)

Data:

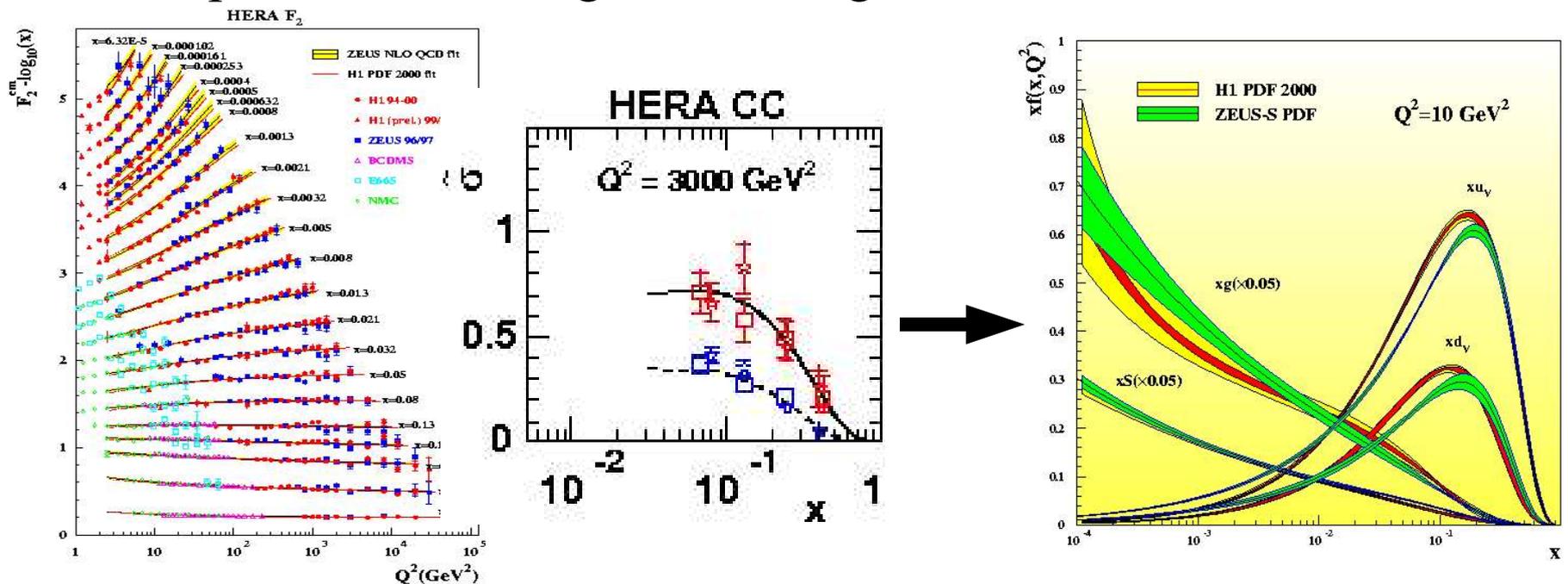
- Neutral current F2
- Charged Current
- Deuteron Data
- Jets
- ...

Fit Machinery

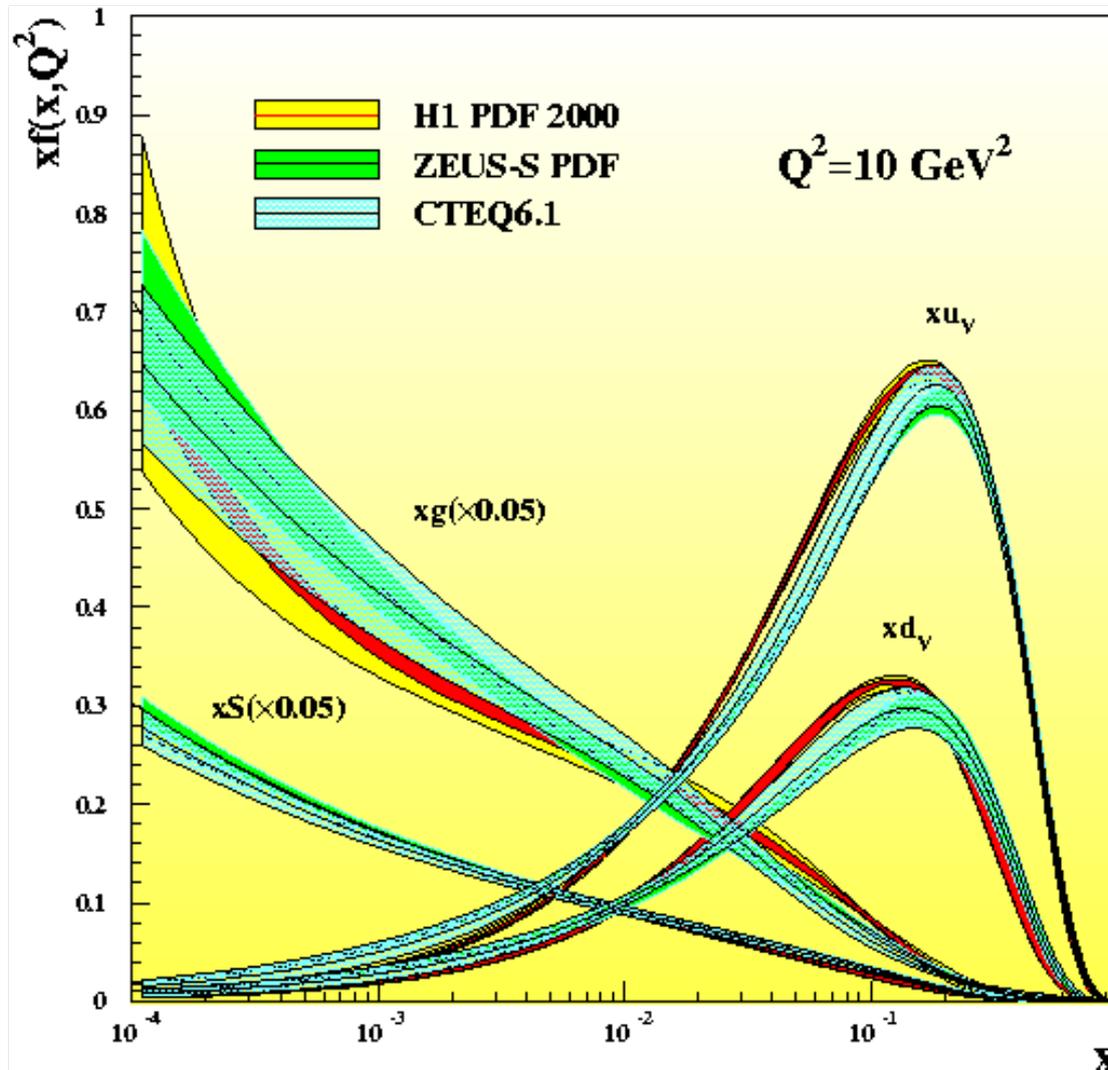
Parton  
Densities

# Extraction of Parton Densities

- Analyses by H1 [EPJ C30(2003)1] and ZEUS [PR D67(2003)012007]:
  - Use  $F_2$  data from own experiment
  - Plus CC data (constraints on u, d at high x)
  - Plus fixed target data (ZEUS only)
- Similar results, but significant differences: are the parametrizations general enough?



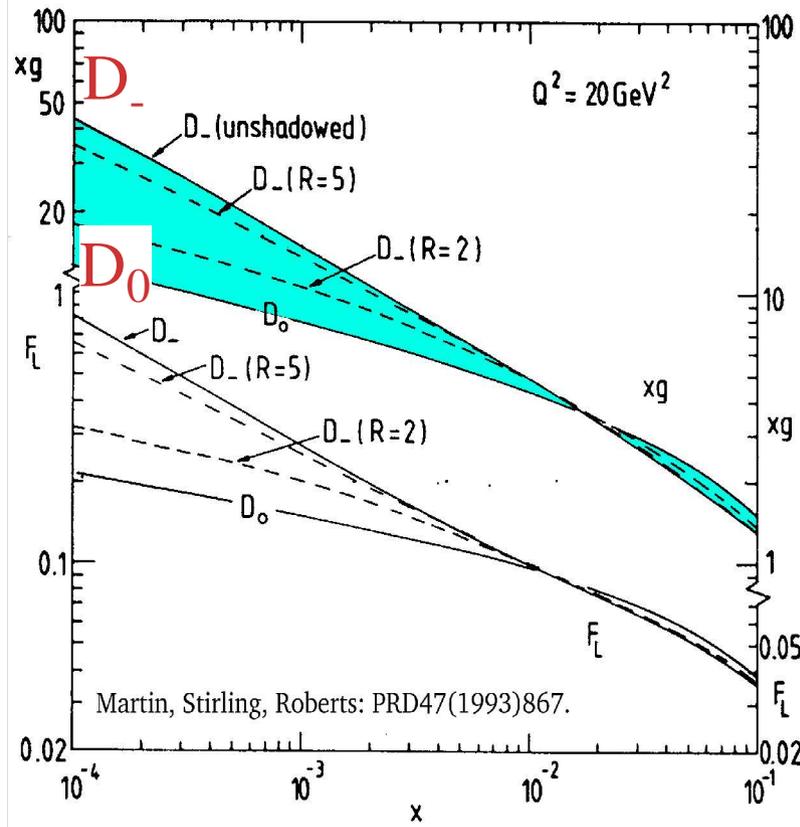
# Parton Densities



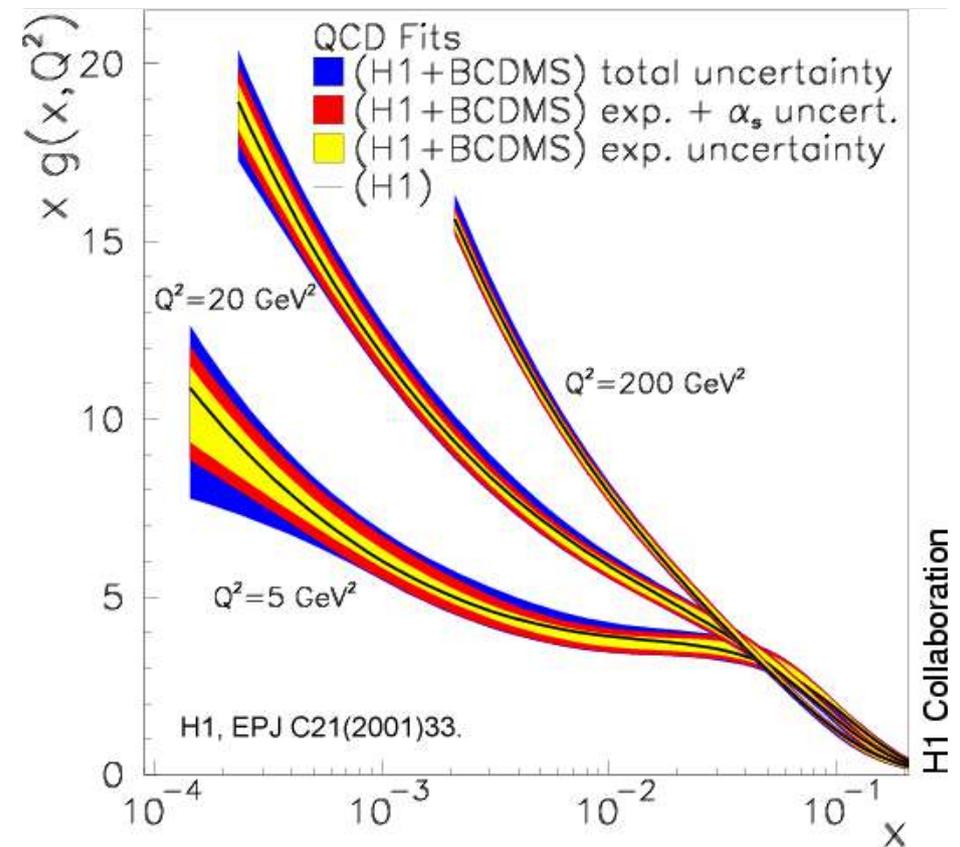
- Qualitative Agreement H1-ZEUS
- Differences due to different methods and data sets

Note: sea quark density  $S$  and gluon density  $g$  scaled down by faktor 20!

# Gluon Densities before/after HERA



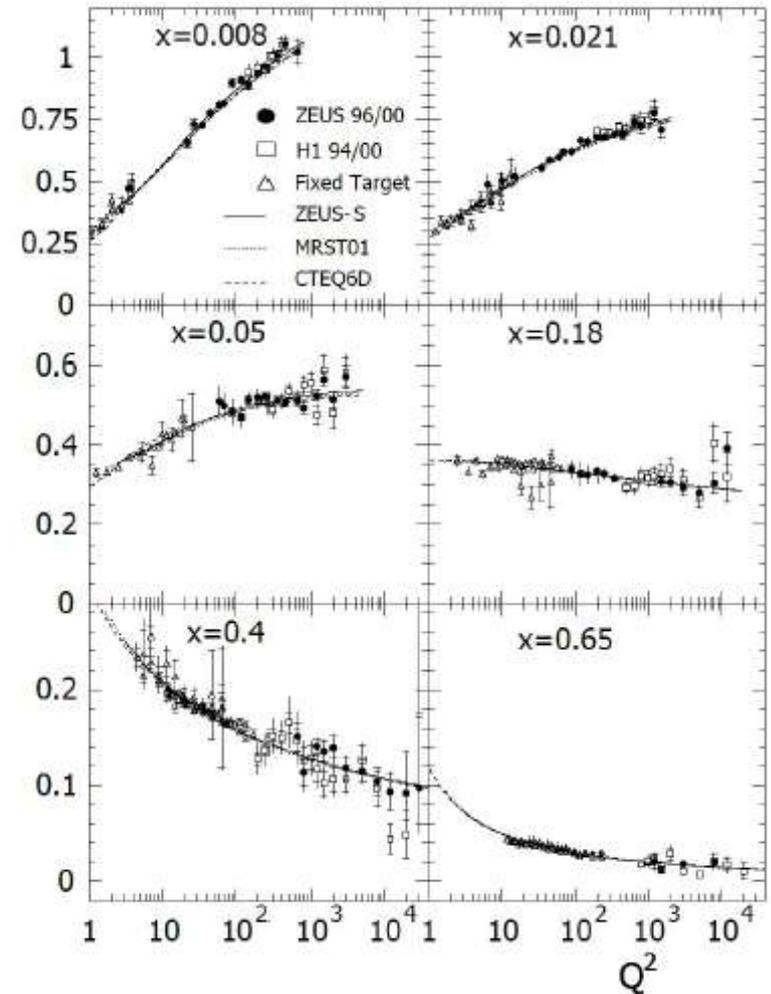
1993: Uncertainty factor 3  
 at  $x=2 \cdot 10^{-4}$ ,  $Q^2=20 \text{ GeV}^2$   
 (theoretical estimate only!)



2001:  $\pm 5\%$  uncertainty,  
 based on measurement!

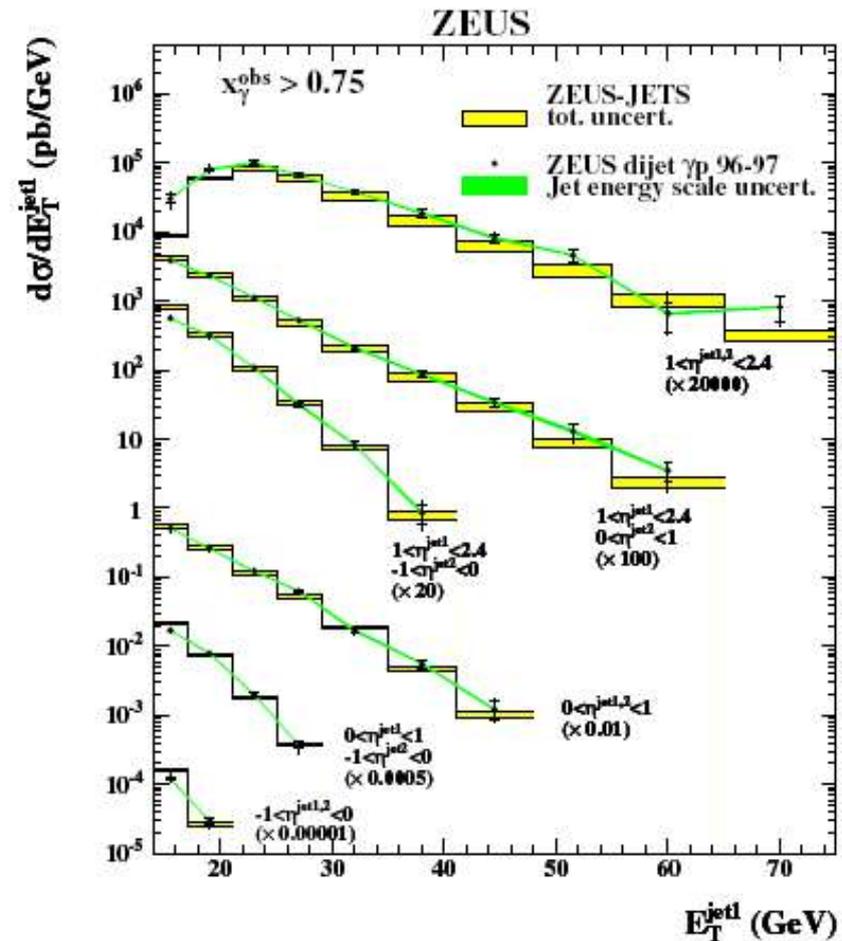
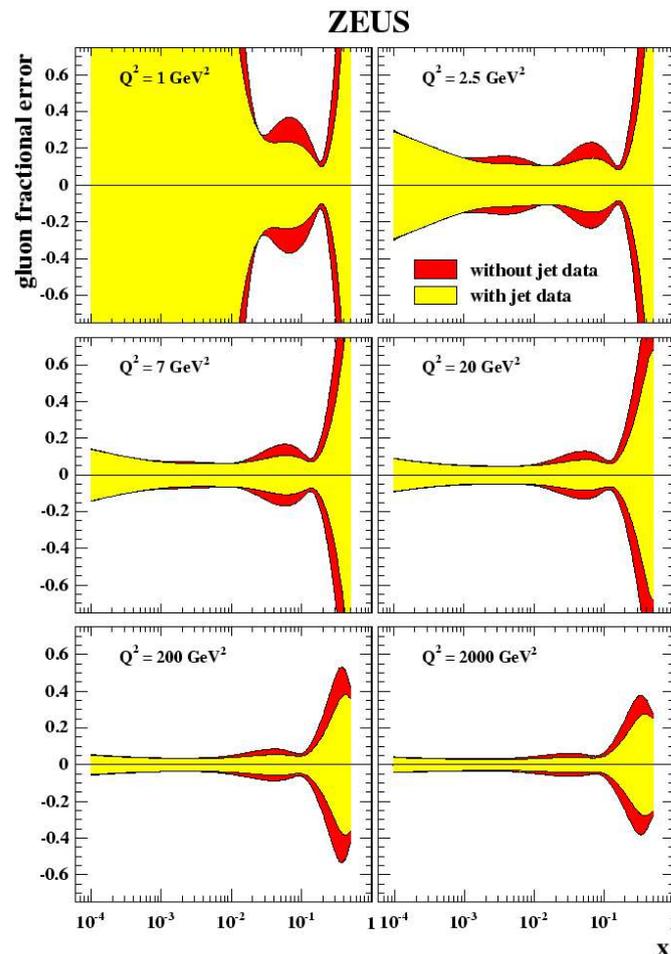
# A Success for DGLAP

- Together with fixed target data: Test of scaling violations over 4 orders of magnitude in  $Q^2$  at fixed  $x$
- NLO-QCD fits based on DGLAP-evolution describe data very well
- No obvious deviations from “Standard Model of Parton Densities”



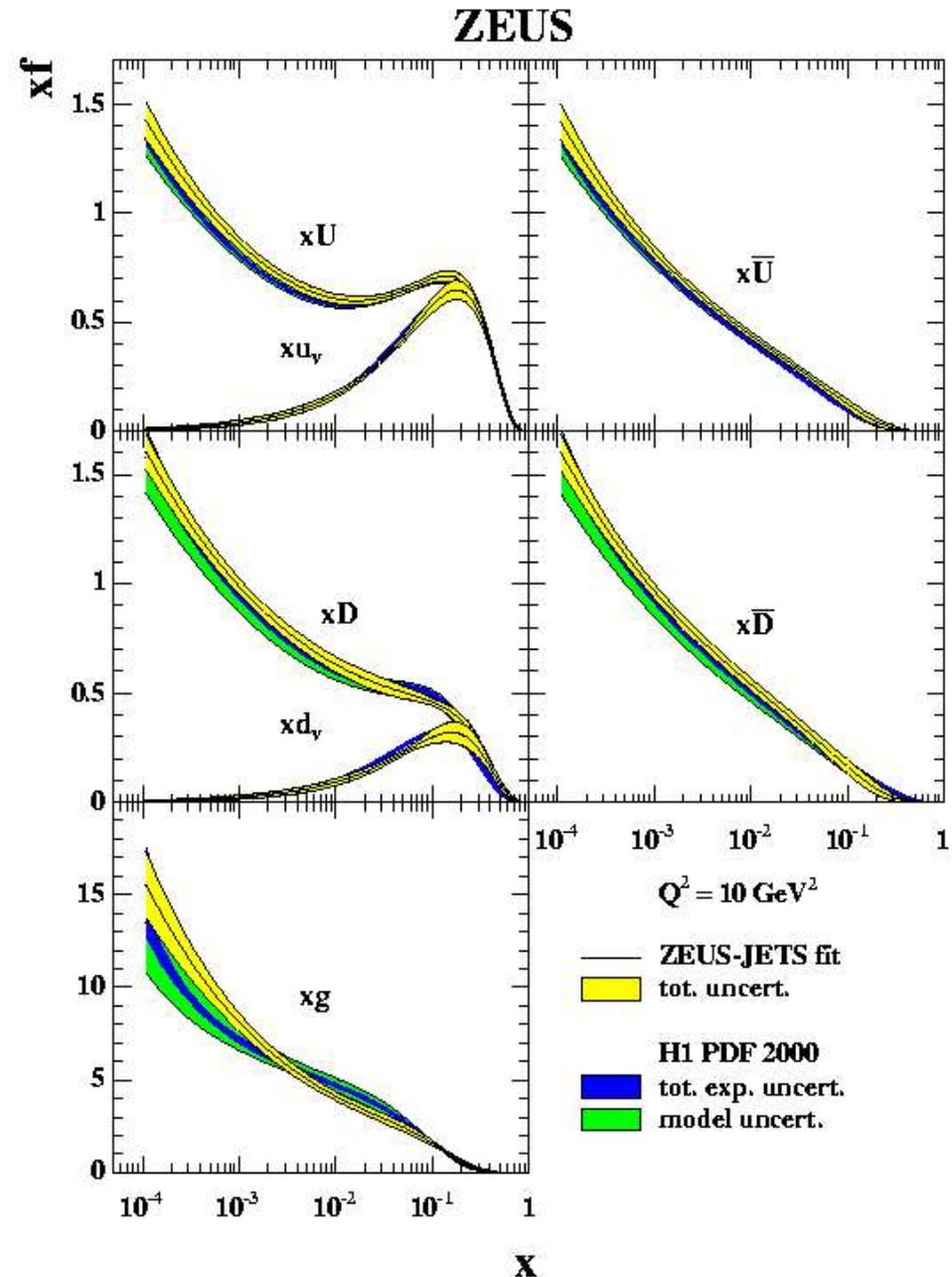
# Adding Jet Data

- New ZEUS analysis [EPJ C42(2005)1]:
- Add DIS and  $\gamma p$  dijet data (direct photoproduction): adds to knowledge of gluon density at large  $x$



# ZEUS-Jets vs. H1-2000

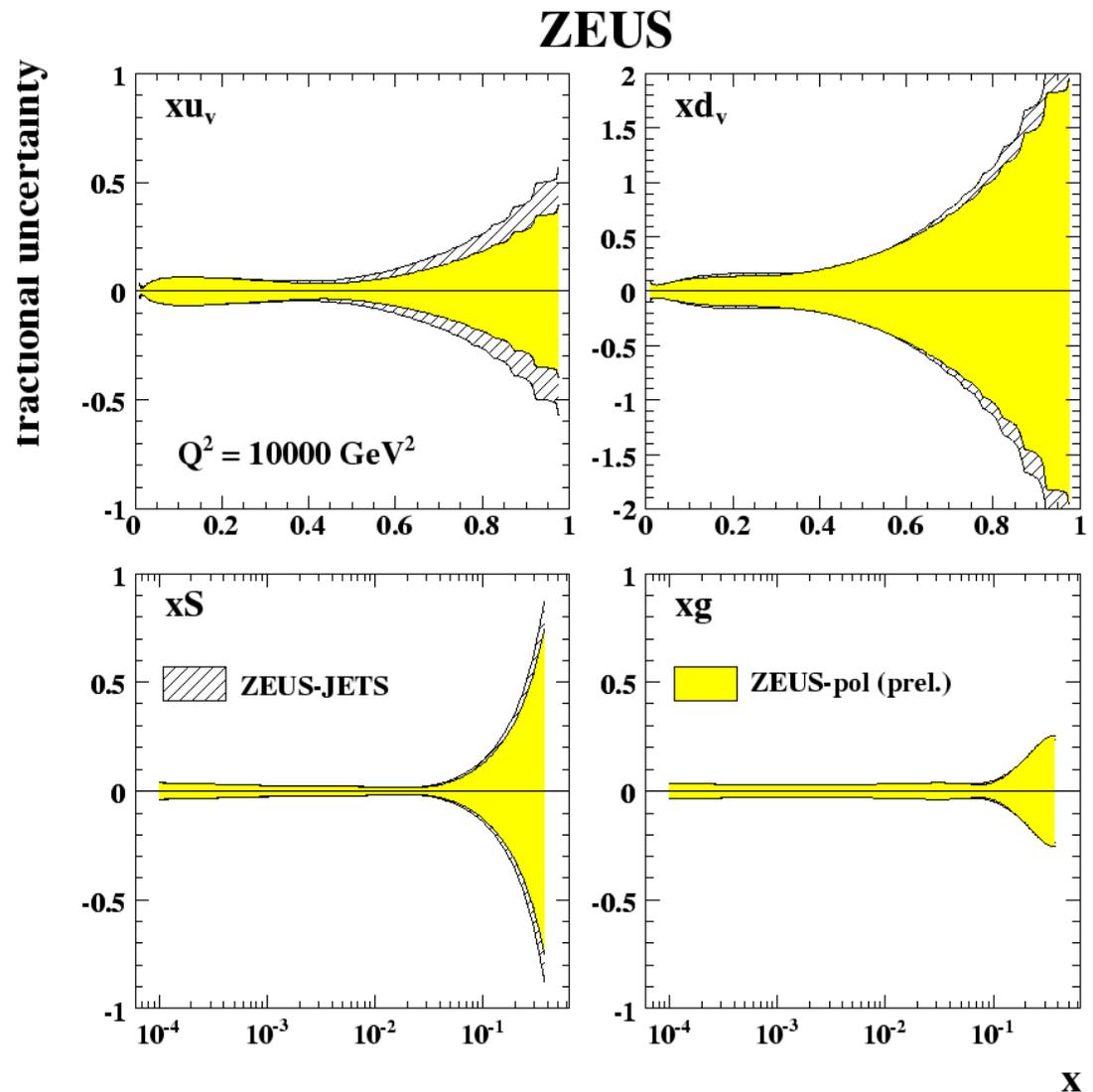
- After inclusion of Jets data by ZEUS, H1 and ZEUS pdf fits agree well
- Still differences for gluon



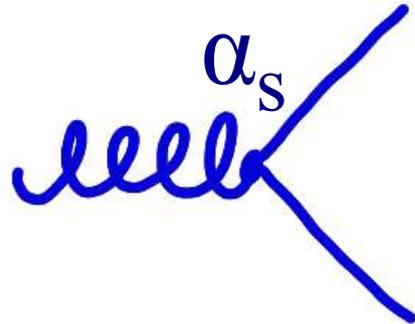
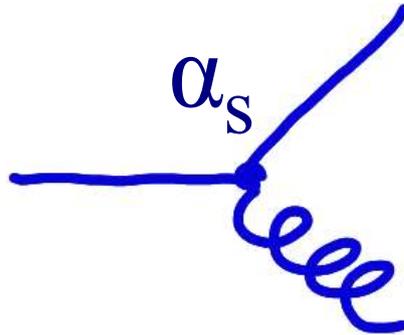
# Using Polarized Data

- Preliminary ZEUS result (ZEUS-prel-006-03):
- Polarized HERA-II data improves valence quark uncertainty at large  $x$
- Central values unchanged compared to ZEUS-Jets fit

$Q^2=10000\text{GeV}^2$



# Extraction of $\alpha_s$



Scaling violations:

- Proportional to  $\alpha_s$  and gluon density
- At large  $x$ : Gluon radiation off quarks dominates,  $\partial F_2 / \partial \ln Q^2$  allows measurement of  $\alpha_s$
- *Gluon Splitting* damps scaling violations from gluon radiation  
=> Reliable determination of  $\alpha_s$  from DIS needs very good understanding of gluon densities over a wide  $x$  range

# $\alpha_s$ from Structure Function Fits

- H1: Combine with fixed target data (BCDMS) to pin down scaling violations at large/medium  $x$  (disentangle gluon density and  $\alpha_s$ )

$$\Rightarrow \alpha_s(M_Z) = 0.1150 \pm 0.0017 \begin{matrix} +0.0009 \\ -0.0005 \end{matrix}$$

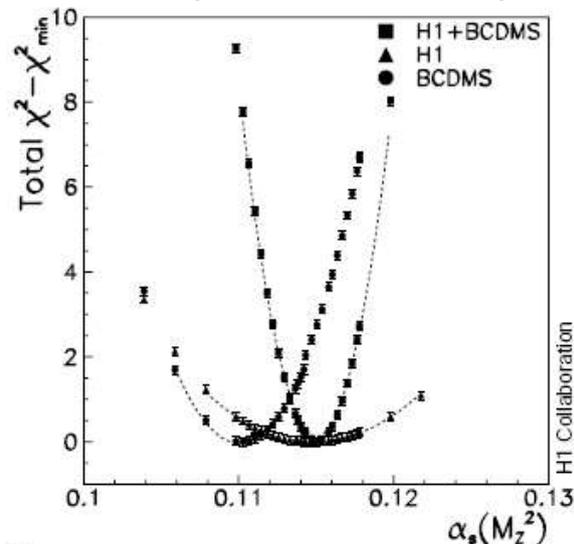
*exp.*      *model*

- ZEUS: Jet data make external input unnecessary

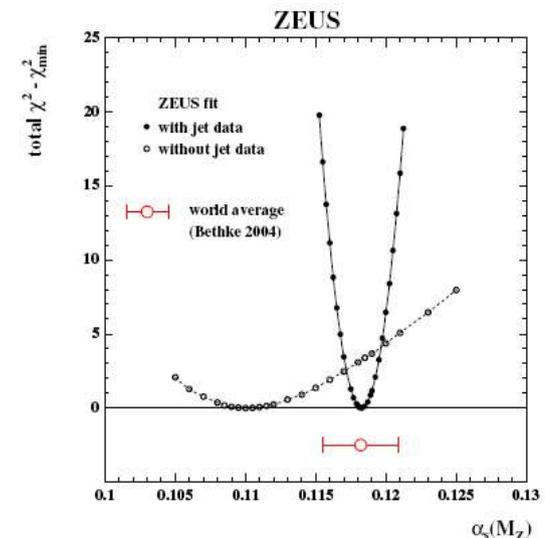
$$\Rightarrow \alpha_s(M_Z) = 0.1183 \pm 0.0007 \pm 0.0022 \pm 0.0016 \pm 0.0008$$

*uncorr.*    *corr.*      *norm.*      *model*

- *Theory uncertainty:  $\pm 0.005$  (dominates)*



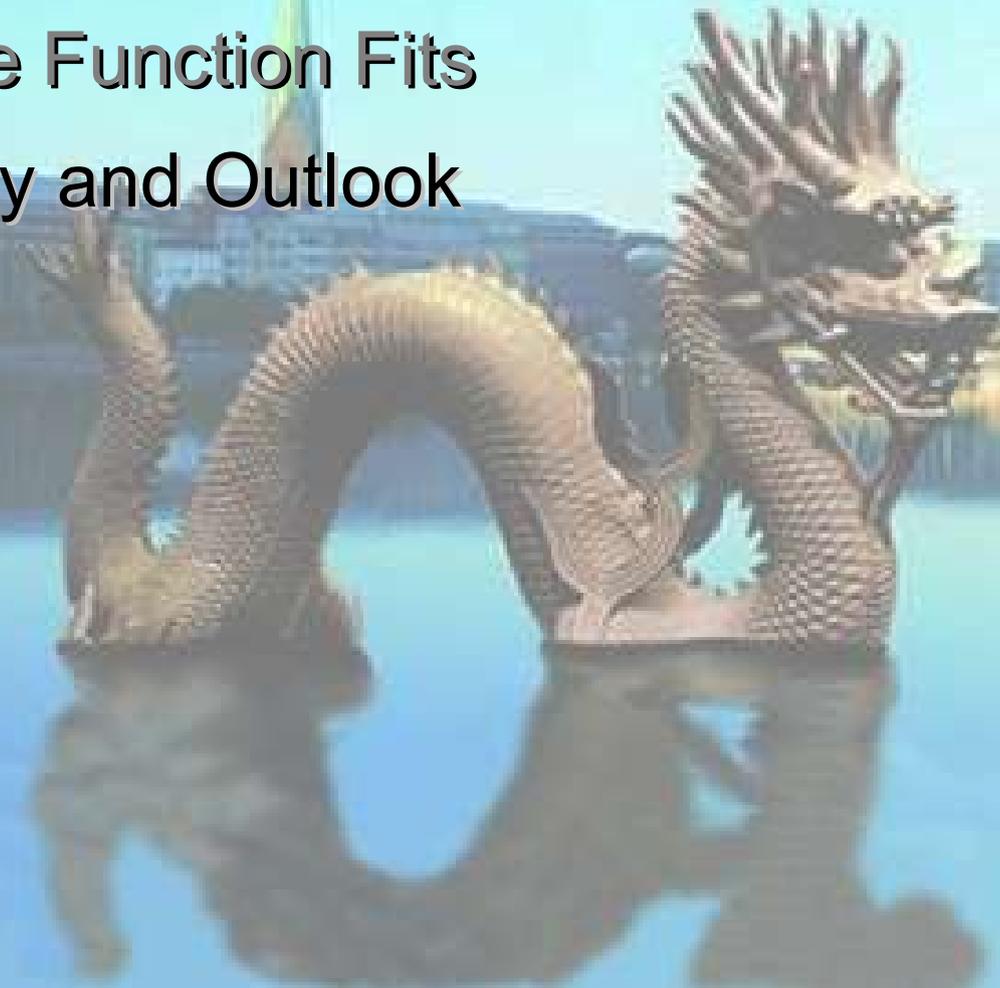
H1, EPC **C21** (2001) 33.



ZEUS, EPJ **C42**(2005)1

# Summary and Outlook

- Introduction
- Structure Function Measurements
- Structure Function Fits
- Summary and Outlook



# Summary

- HERA-II is running well, producing lots of new data:
  - 10-fold increase of e-p data set
  - polarized ep scattering data
- High-precision F2 data over a large range of  $x$  and  $Q^2$
- Polarized Charged Current Data test helicity structure of W exchange
- F3 measurements become significant:  
Combination of ZEUS and H1 data has started
- Flavour-exclusive measurements for charm and beauty available
- Polarization effects in Neutral Current data become visible
- $\alpha_s$  measurements compatible and competitive with world average,  
profit from understanding of gluon at high  $x$

# Outlook

- More data coming in: 3-fold increase of  $e^+p$  data set possible
- Data analysis of final  $e-p$  data set to come
- Low energy run in summer 2007: a real  $F_L$  measurement
- Parton density determination can still be improved:
  - NNLO evolution
  - Improved data and theory: include charm and beauty data in fits

**HERA data analysis will deliver interesting results for many years!**