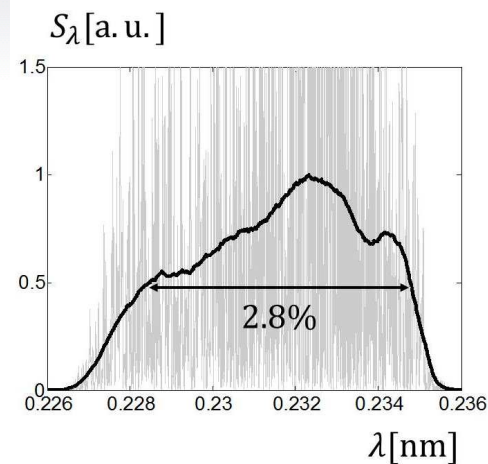
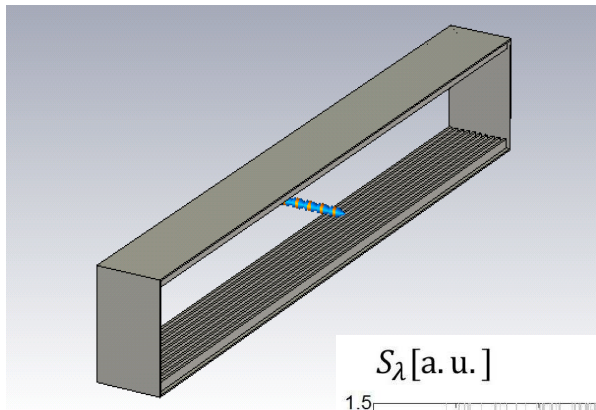


Passive Wakefield Structure Insertion for the European XFEL

Beam Dynamics and FEL Simulations



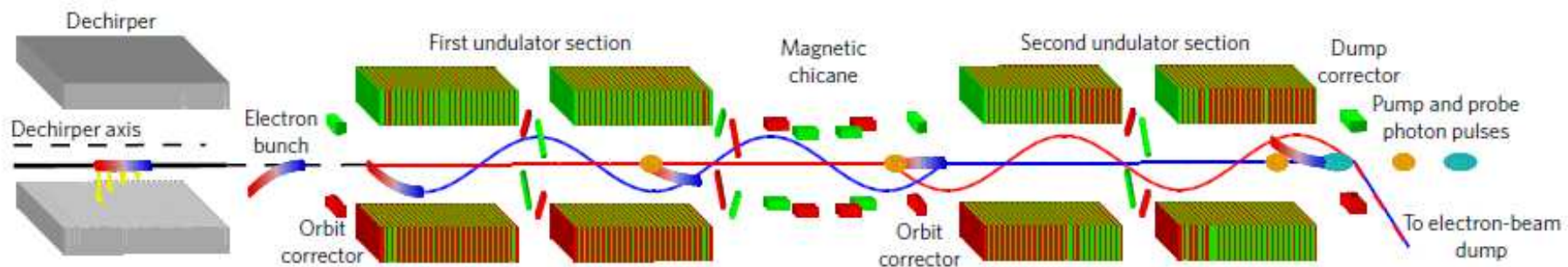
Igor Zagorodnov, Guangyao Feng
and Torsten Limberg

DESY-TEMF-Meeting

DESY, Hamburg
23. January 2017

Motivation

- Passive Wakefield Structure Insertion (PWSI) can be used as “dechirper” **to reduce the bandwidth** of SASE.
- The PWSI can be used as “chirper” **to increase considerably the bandwidth** of SASE radiation.
- The PWSI can be used as **passive deflector** for electron beam diagnostics (like Transverse Deflecting Cavity).
- The PWSI can be used as a **source of THz-radiation** .
- The PWSI allows fresh-slice technique for **multicolor pulse production**.



*A. Lutman, et al, **Fresh-slice multicolour X-ray free-electron lasers**, Nature Photonics 10 (2016) 745–750

Motivation

- The natural bandwidth of the SASE-XFEL pulses is on the order of the Pierce parameter ρ , with values between $10e-3$ and $10e-4$ for the European XFEL.
- There is a scientific demand to obtain **broadband XFEL radiation** for certain applications such as
 - ✓ X-ray crystallography,
 - ✓ X-ray absorption spectroscopy,
 - ✓ multi-wavelength anomalous diffraction,
 - ✓ stimulated Raman spectroscopy.

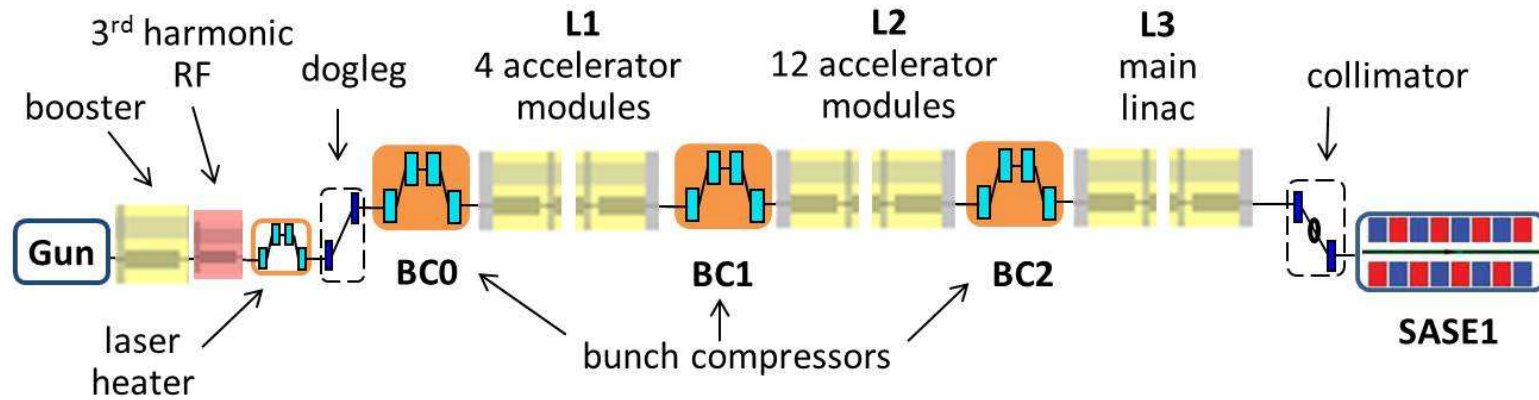
$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} \right) \quad \longrightarrow \quad \frac{\gamma - \gamma_0}{\gamma_0} \approx \frac{\omega - \omega_0}{2\omega_0}$$

3% in bandwidth \sim 1.5% in energy spread

For 14 GeV we need the energy spread above **210 MeV**.



Beam dynamics in linac



$R_{56} = 30-90$ mm

$R_{56} = 20-80$ mm

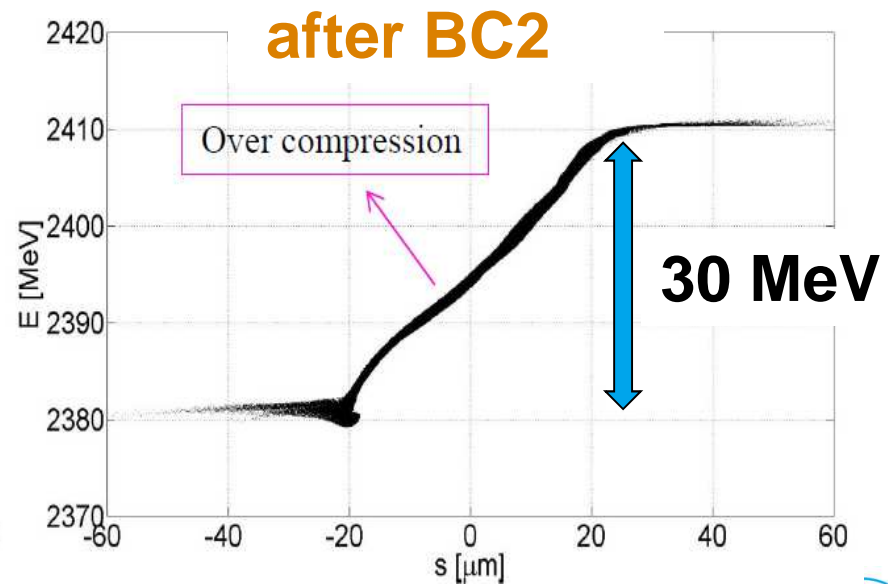
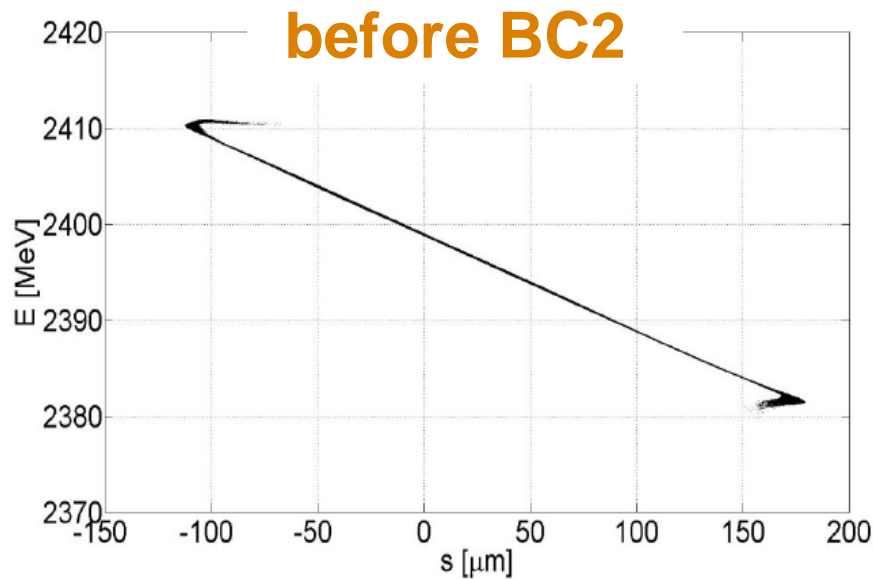
$R_{56} = 10-60$ mm

$I_{\text{peak}} \sim 30$ A
 $Q = 0.5$ nC

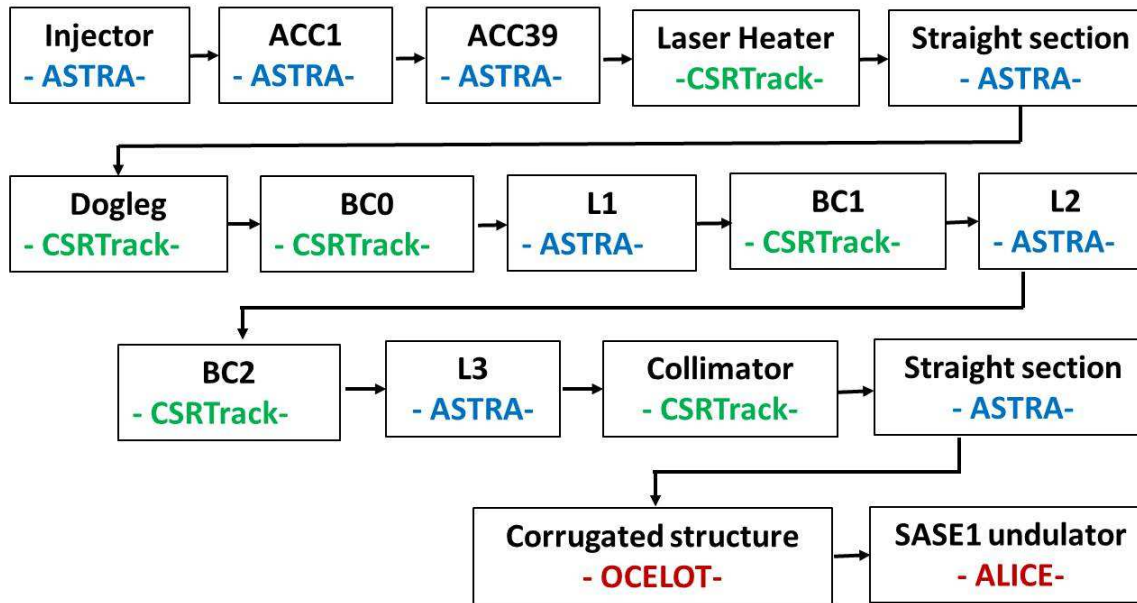
$I_{\text{peak}} \sim 100$ A
 $E = 130$ MeV

$I_{\text{peak}} \sim 1$ kA
 $E = 700$ MeV

$I_{\text{peak}} \sim 5$ kA
 $E = 2400$ MeV



Beam dynamics in linac

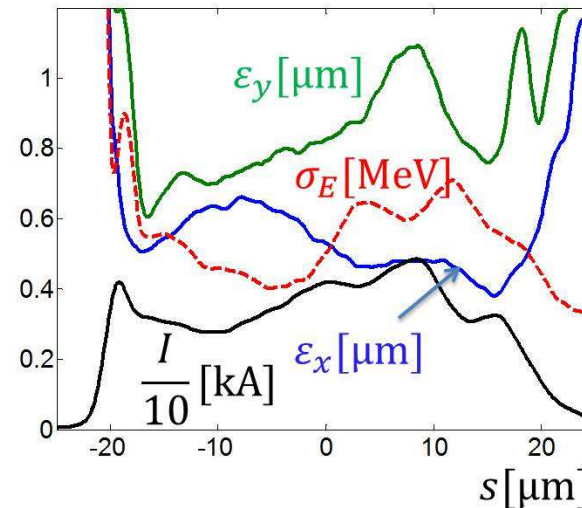
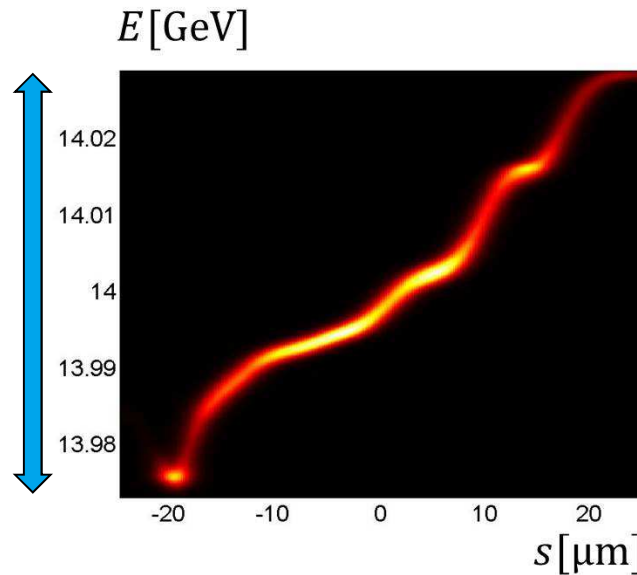


after collimator

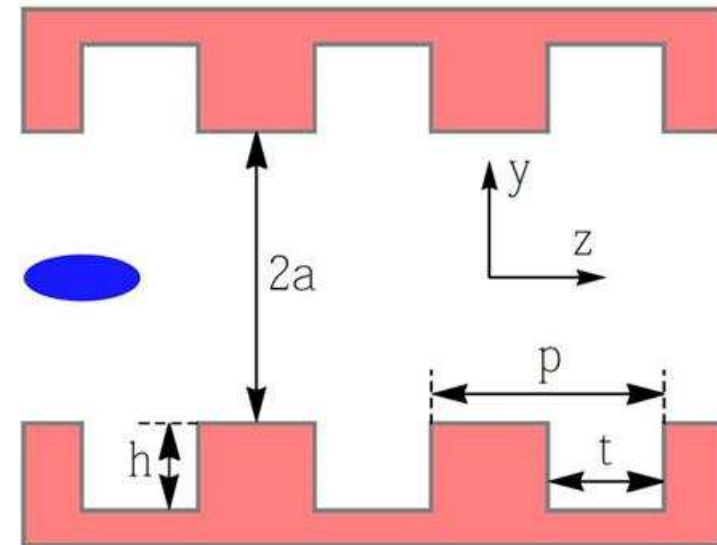
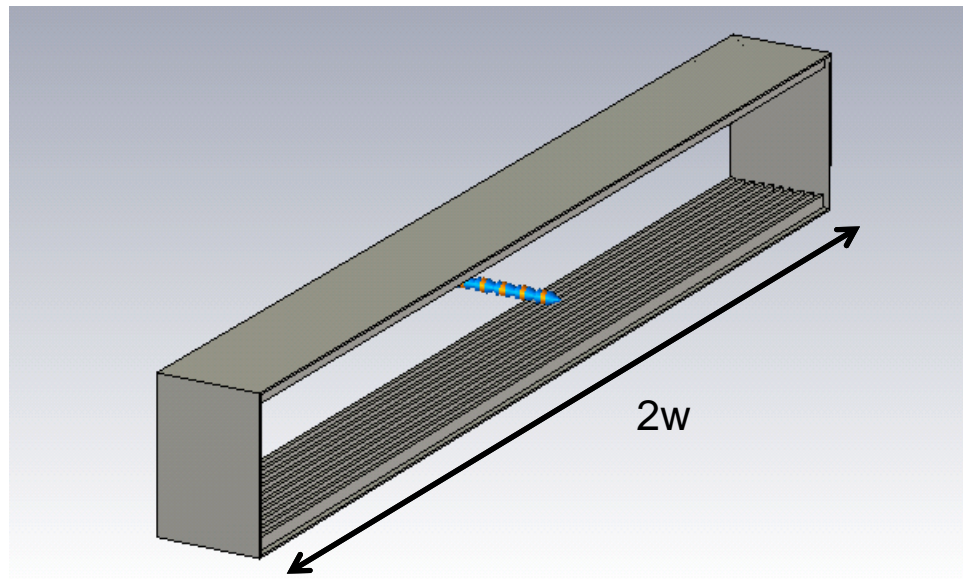
projected emittance:
in x-plane - $0.72 \mu\text{m}$
in y-plane - $1.17 \mu\text{m}$.

energy drop $\sim 0.4\%$.

55 MeV



Wake function of the corrugated structure



K. Bane and G. Stupakov, *Corrugated pipe as a beam dechirper*, NIM A **690** (2012) 106.

Z. Zhang et al, *Electron beam energy chirp control with a rectangular corrugated structure at the Linac Coherent Light Source*, PR STAB **18** (2015) 010702.

Parameter	Value	Unit
Depth, h	0.5	mm
Gap, t	0.25	mm
Period, p	0.5	mm
Half aperture, a	0.7	mm
Half width, w	6	mm
Length, L	2	m

Wake function of the corrugated structure

$$W(x_0, y_0, x, y, s) = \frac{1}{w} \sum_{m=1}^{\infty} W(y_0, y, k_{x,m}, s) \sin(k_{x,m} x_0) \sin(k_{x,m} x), \quad k_{x,m} = \frac{\pi m}{2w}$$

$$W(y_0, y, k_x, s) = W^{cc}(k_x, s) \cosh(k_x y_0) \cosh(k_x y) + W^{ss}(k_x, s) \sinh(k_x y_0) \sinh(k_x y)$$

0th - order model

K. Bane and G. Stupakov, *Dechirper wakefields for short bunches*, NIM A 820 (2016) 156.

$$W_a^{cc}(k_x, s) = W_a^{ss}(k_x, s) = Z_0 c \frac{k_x}{\sinh(2k_x a)} \quad s \equiv z_0 - z$$

1st - order model

K. Bane, G. Stupakov, I. Zagorodnov, *Analytical formulas for short bunch wakes in a flat dechirper*, PR STAB 19 (2016) 084401

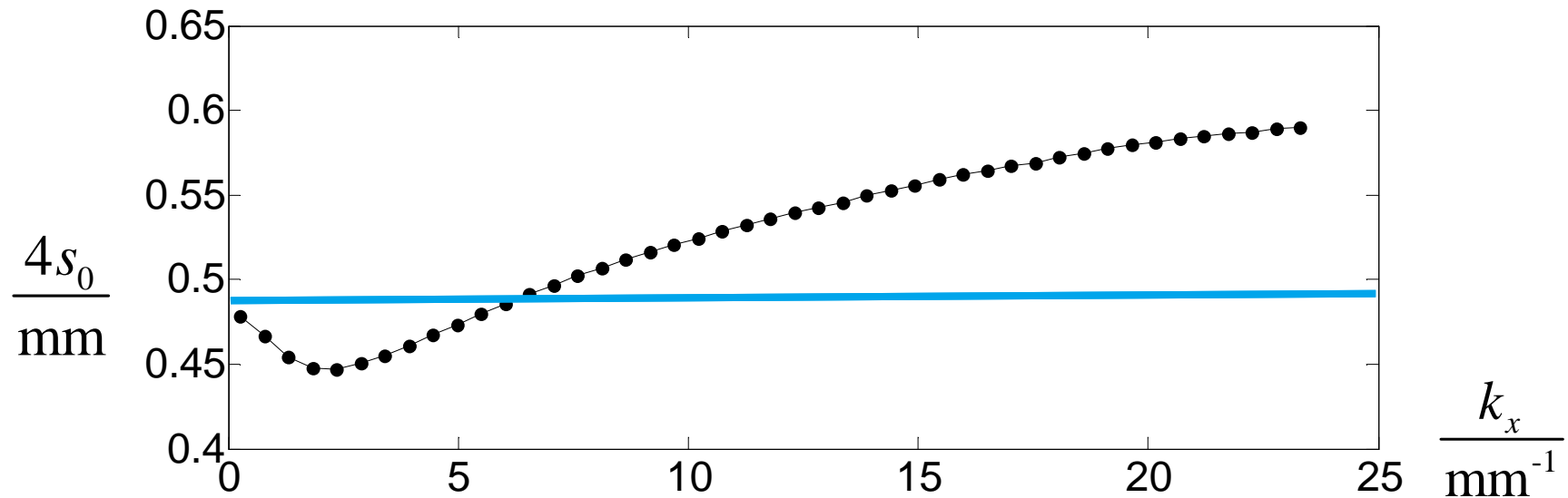
$$W_a^{cc}(k_x, s) = Z_0 c \frac{k_x}{\sinh(2k_x a)} e^{-\frac{k_x a}{\tanh(k_x a)} \sqrt{\frac{s}{4s_0}}}$$

$$W_a^{ss}(k_x, s) = Z_0 c \frac{k_x}{\sinh(2k_x a)} e^{-\frac{k_x a}{\coth(k_x a)} \sqrt{\frac{s}{4s_0}}}$$



Wake function of the corrugated structure

Fitting to ECHO calculations for bunches with up to 2 μm RMS.



K.Bane, *Short-range dipole wakefields in accelerating structures for the NLC*, SLAC-PUB-9663, 2003

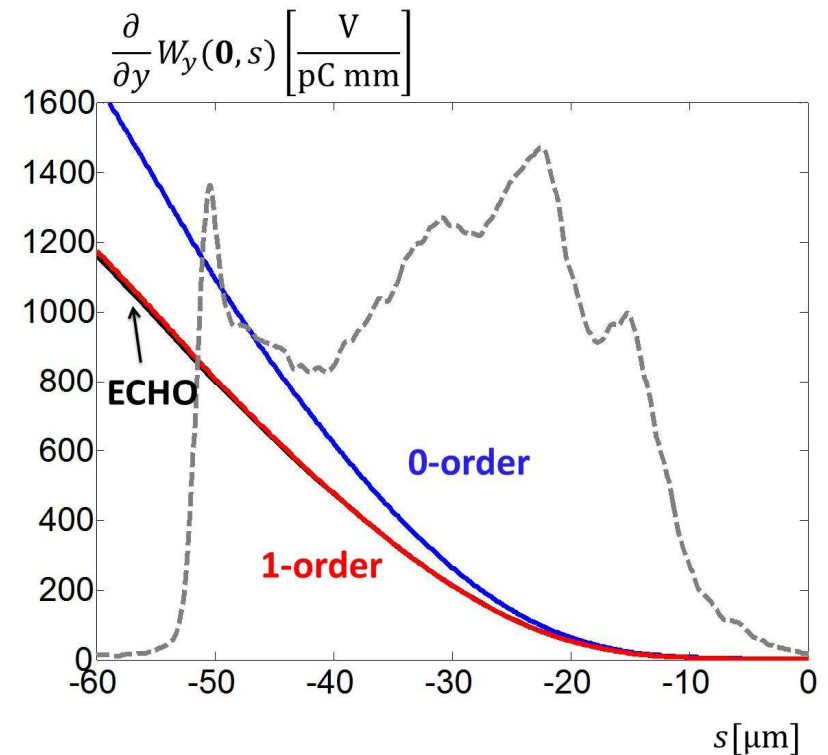
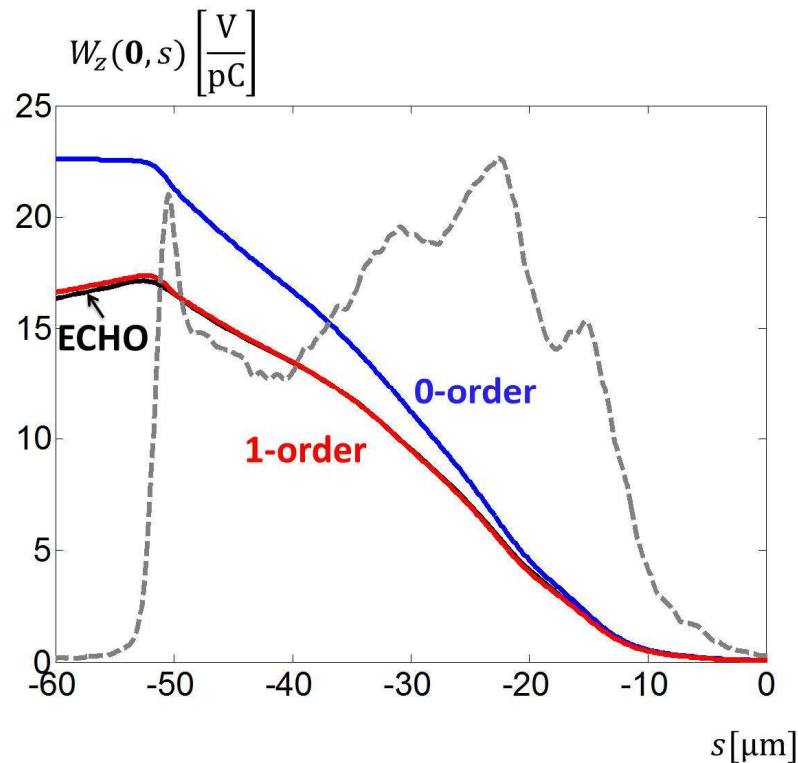
$$s_0 = \frac{g}{8} \left(\frac{a}{\alpha(g/p)p} \right)^2 = 0.15\text{mm}$$

K. Bane et al, *Calculations of the short-range longitudinal wake fields in the NLC Linac*, SLAC-PUB-7862, 1998.

$$s_0 = 0.41 \frac{a^{1.8} g^{1.6}}{p^{2.4}} = \mathbf{0.12\text{mm}}$$



Wake function of the corrugated structure



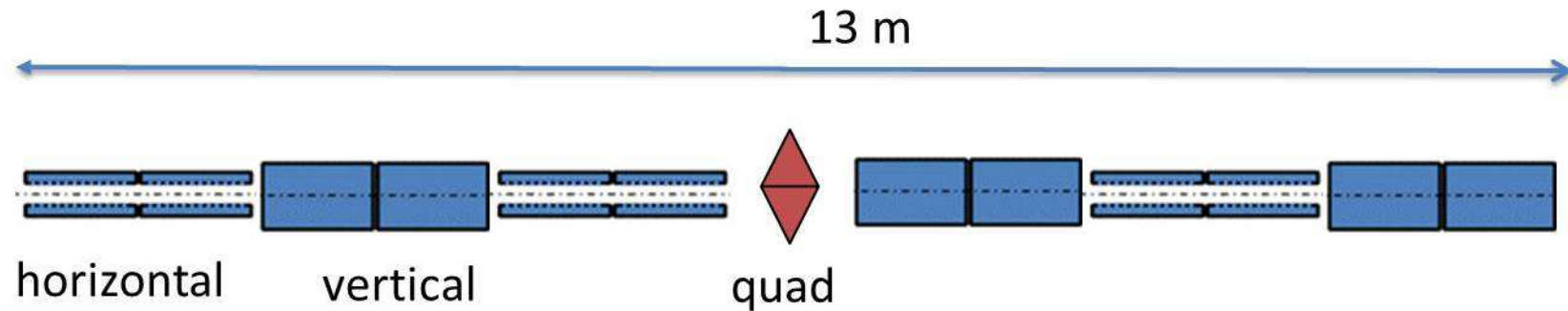
$$W_z(x_0, y_0, x, y, s) = W_z(\mathbf{0}, s) + h_{11}(s) \left(x_0^2 - y_0^2 + x^2 - y^2 \right) + h_{13}(s) x_0 x + h_{24}(s) y_0 y + O(3)$$

M. Dohlus et al, *Fast particle tracking with wake fields*, DESY 12-012, 2012.

I. Agapov et al., *OCELOT: a software framework for synchrotron light source and FEL studies*, NIM A 768 (2014)

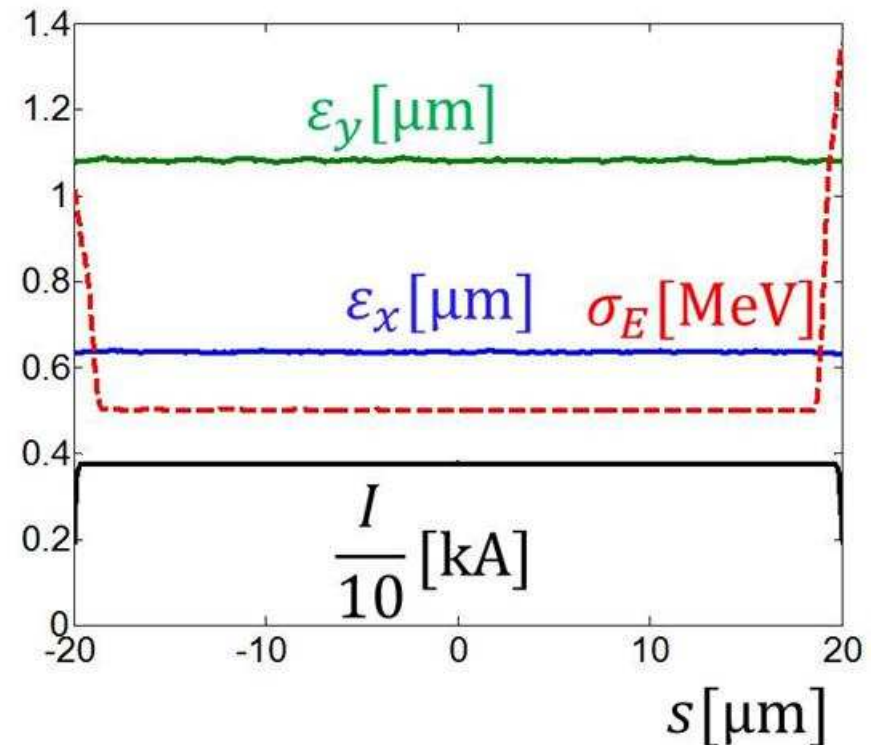


Beam dynamics in corrugated structure



“Ideal” beam

Parameter	Value	Unit
Emittance, $\epsilon_{0x}/\epsilon_{0y}$	0.64/1.09	μm
RMS size, σ_x/σ_y	30.9/16.8	μm
Beta function, β_x/β_y	22.6	m
Alpha function, α_x/α_y	-1.43/1.43	
Energy, E	14	GeV
Length, l	40	μm
Length, Q	0.5	nC



Beam dynamics in corrugated structure

“Ideal” beam, only one kick without tracking

Parameter	Analytical (0 order)*	Numerical, OCELOT (0 order)	Numerical, OCELOT (1st order)	Units
Emittance growth, $\varepsilon/\varepsilon_0$	1.484	1.479	1.29	
Energy spread in tail, $\sigma_E(l)$	80.2	81	56	keV
Energy loss in tail, $W_{ }(l)$	45.3	45	35	MeV

$$\frac{\varepsilon}{\varepsilon_0} = \sqrt{1 + \left(\frac{\pi^3 Z_0 c e Q \beta L l}{384 \sqrt{5} a^4 E} \right)^2}$$

$$W_{||}(l) = \frac{\pi Z_0 c e Q L}{16 a^2}$$

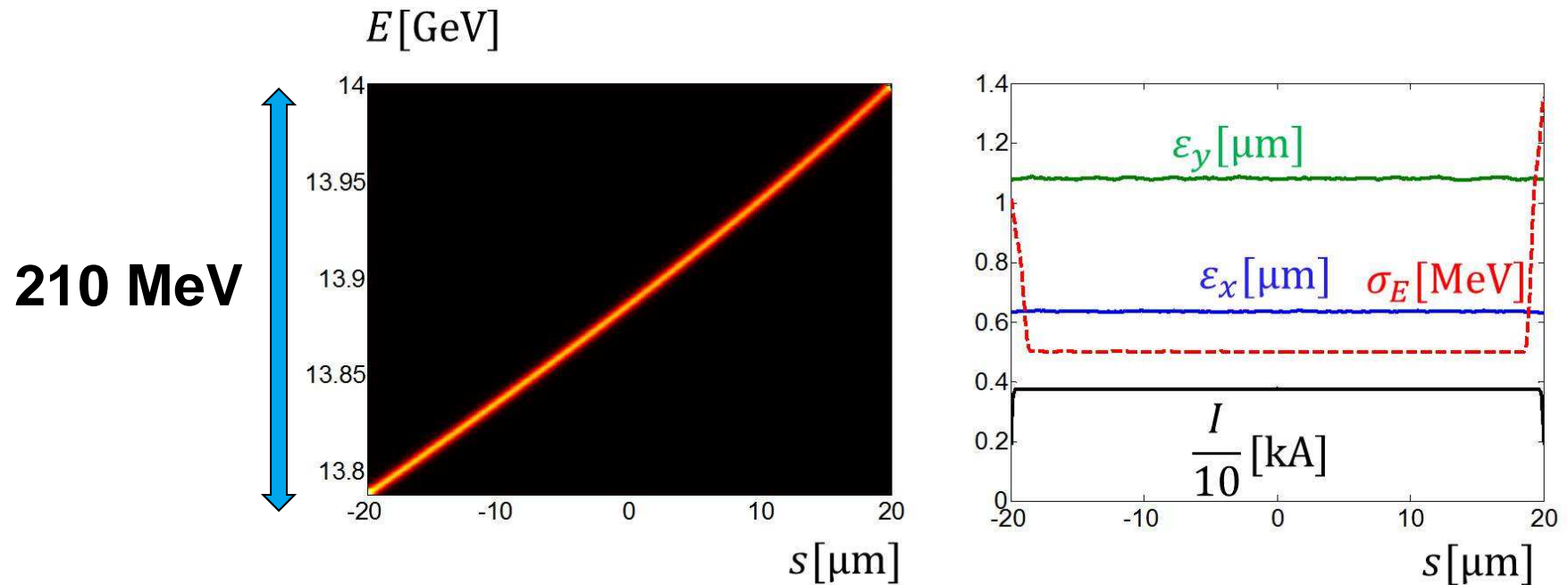
$$\sigma_E(l) = \frac{\sqrt{2} \pi^3 Z_0 c e Q L}{256 a^4} \sqrt{\sigma_x^4 + \sigma_y^4}$$

*K. Bane and G. Stupakov, *Dechirper wakefields for short bunches*, NIM A **820** (2016) 156.



Beam dynamics in corrugated structure

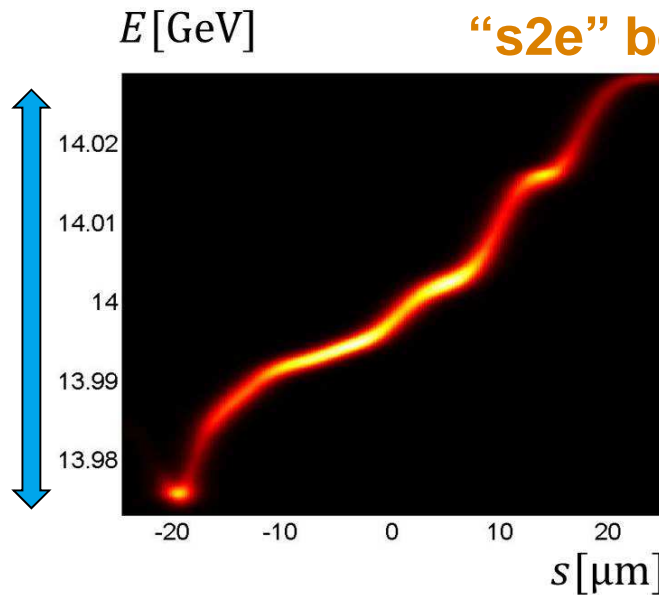
“Ideal” beam after the insertion



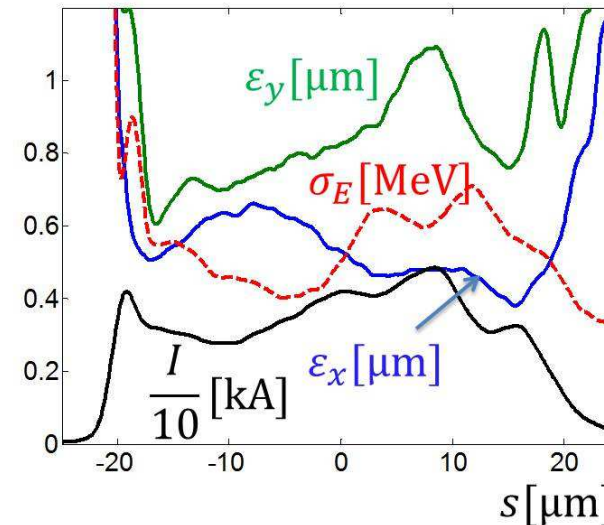
The change in the slice parameters is negligible.

Beam dynamics in corrugated structure

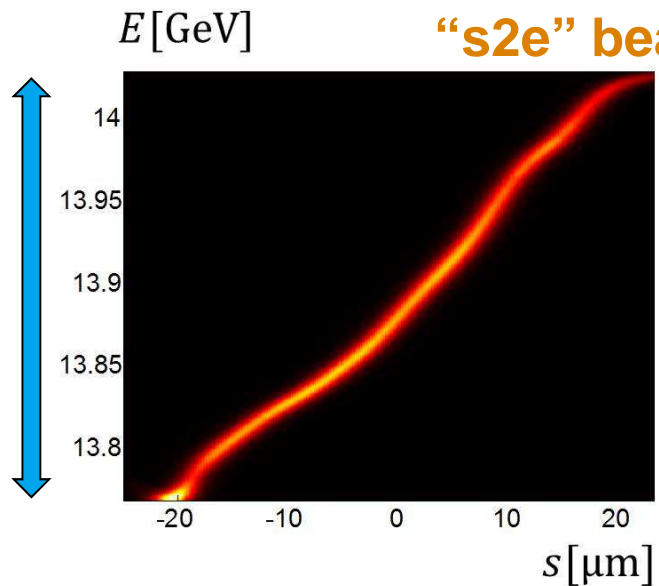
55 MeV



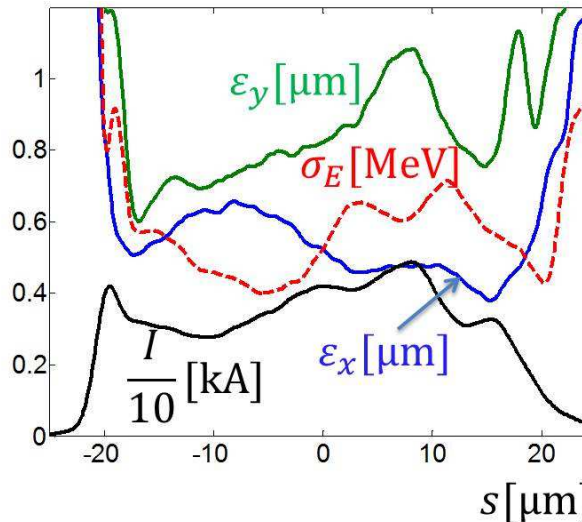
“s2e” beam before the insertion



255 MeV

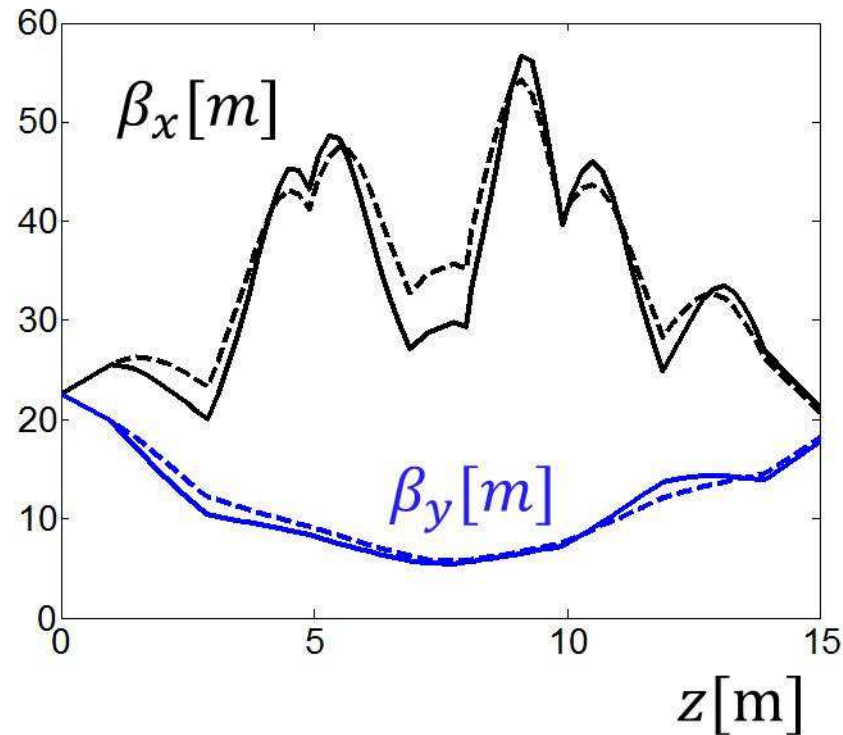


“s2e” beam after the insertion



Beam dynamics in corrugated structure

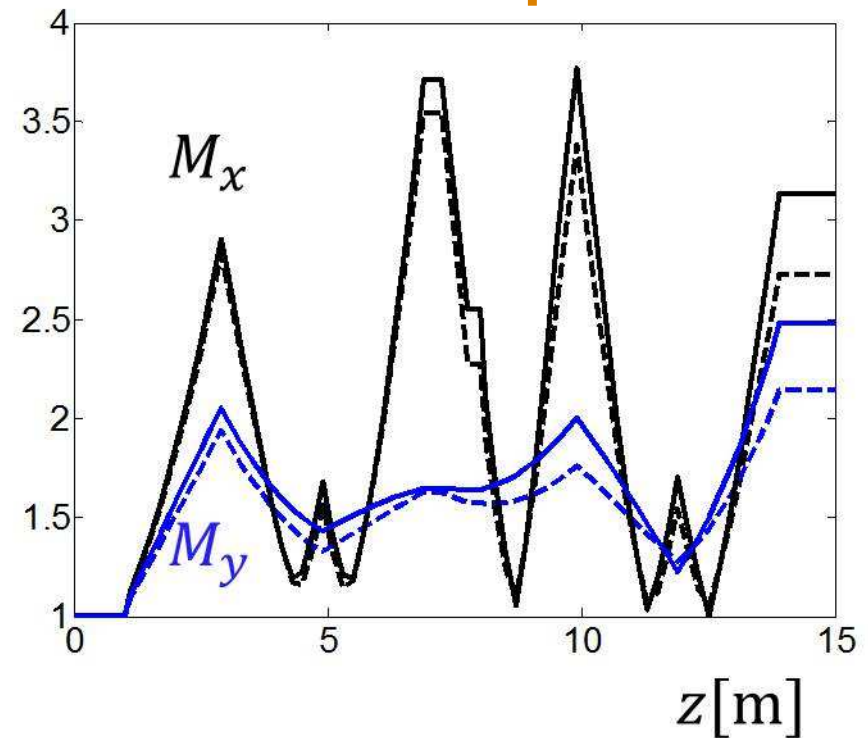
Beta function



solid lines – “S2E” beam

dashed lines – “ideal” beam

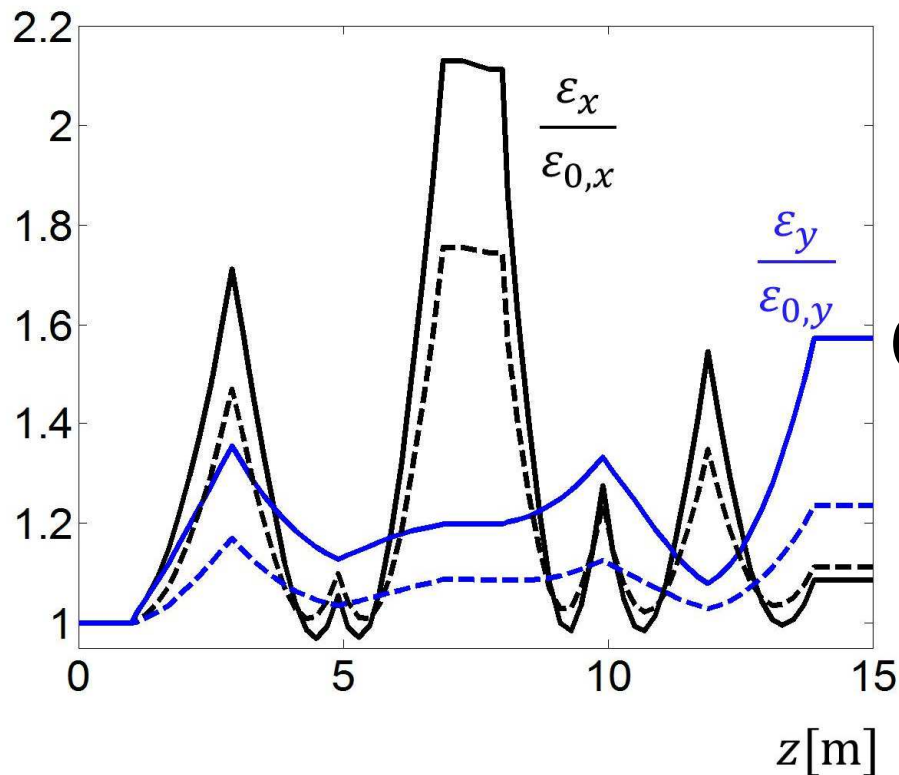
Beta mismatch parameter



$$M = \frac{1}{2} \left(\tilde{\beta}_e + \tilde{\gamma}_e + \sqrt{(\tilde{\beta}_e + \tilde{\gamma}_e)^2 - 4} \right)$$

$$\tilde{\gamma}_e = \frac{1 + \tilde{\alpha}_e^2}{\tilde{\beta}_e}, \quad \tilde{\alpha}_e = \alpha_e - \alpha \tilde{\beta}_e, \quad \tilde{\beta}_e = \frac{\beta_e}{\beta}$$

Beam dynamics in corrugated structure



Projected emittance growth

60%

solid lines – “S2E” beam

dashed lines – “ideal” beam

Parameter	“ideal” beam	“S2E” beam	Units
Initial/final projected x -emittance	0.64/0.70	0.72/0.77	μm
Initial/final projected y -emittance	1.09/1.33	1.18/1.82	μm
Initial/final energy loss in tail	0/212	50/255	MeV

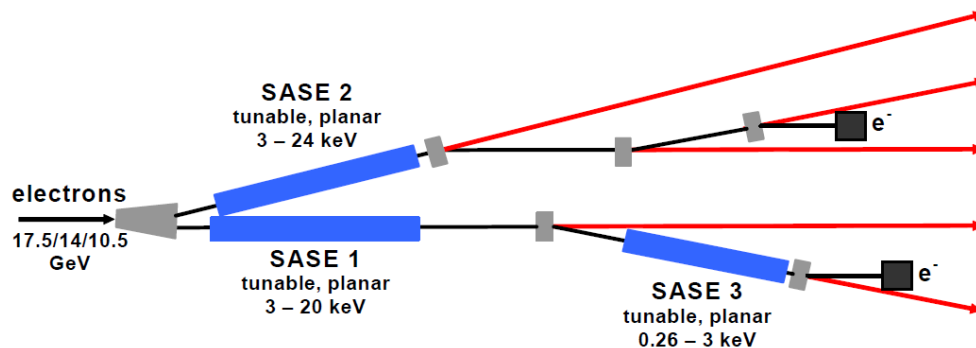


Broadband SASE radiation

The European XFEL undulator lines

Parameter	SASE1/SASE2	SASE3	Units
Undulator wavelength	40	68	mm
K-range	3.9-1.65	99.3-4	
Wavelength at 17.5 GeV	0.147-0.040	1.22-0.27	nm
Wavelength at 14.0 GeV	0.230-0.063	1.90-0.42	nm
Wavelength at 8.5 GeV	0.625-0.171	5.17-1.15	nm
Active undulator length	175	105	m

SASE1 line in the simulation

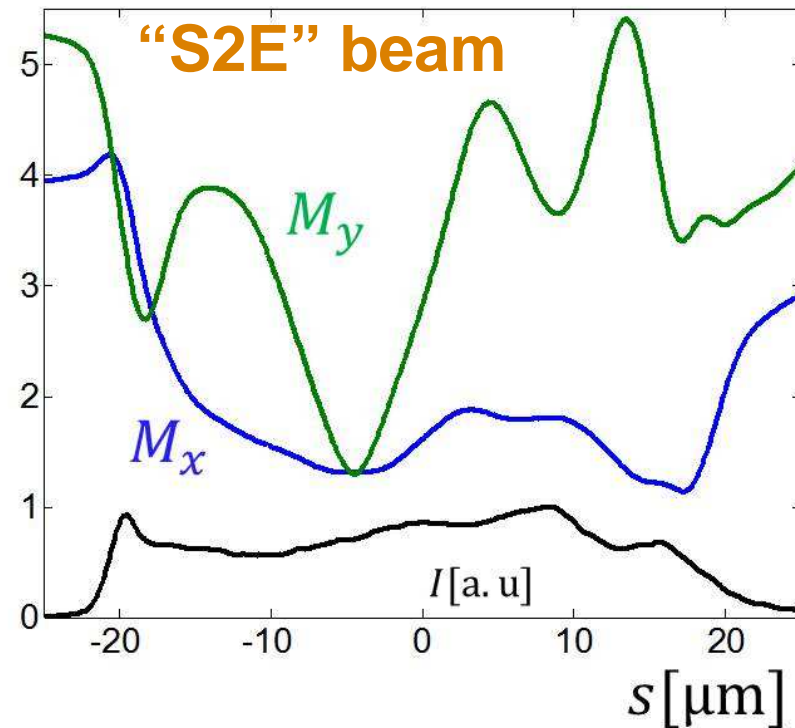
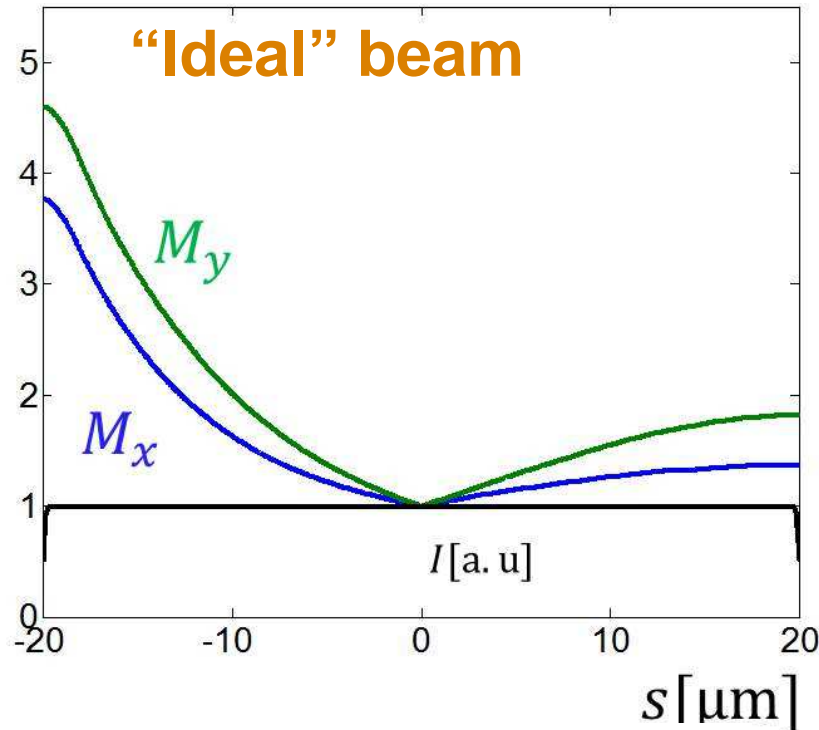


Parameter	Value	Units
Undulator wavelength	40	mm
K averaged	2.76	
Radiation wavelength	0.23	nm
Averaged beta function	16	m



Broadband SASE radiation

Beta mismatch parameter along the beams



$$M = \frac{1}{2} \left(\tilde{\beta}_e + \tilde{\gamma}_e + \sqrt{(\tilde{\beta}_e + \tilde{\gamma}_e)^2 - 4} \right)$$

$$\tilde{\gamma}_e = \frac{1 + \tilde{\alpha}_e^2}{\tilde{\beta}_e}, \quad \tilde{\alpha}_e = \alpha_e - \alpha \tilde{\beta}_e, \quad \tilde{\beta}_e = \frac{\beta_e}{\beta}$$

The "ideal" beam can be matched well even at the tail.

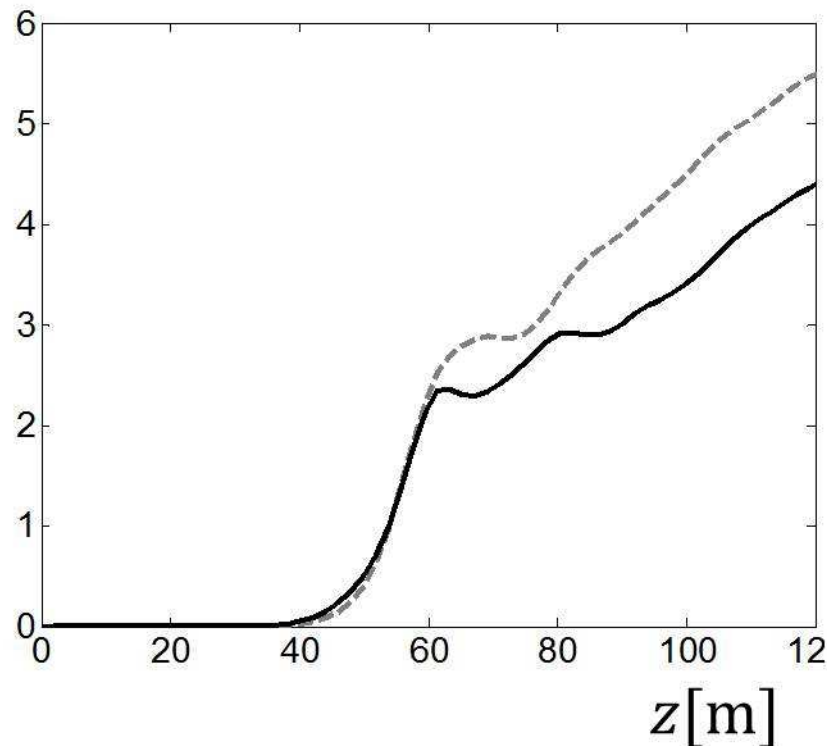
The "S2E" beam has a larger mismatch at the head and at the tail.



Broadband SASE radiation

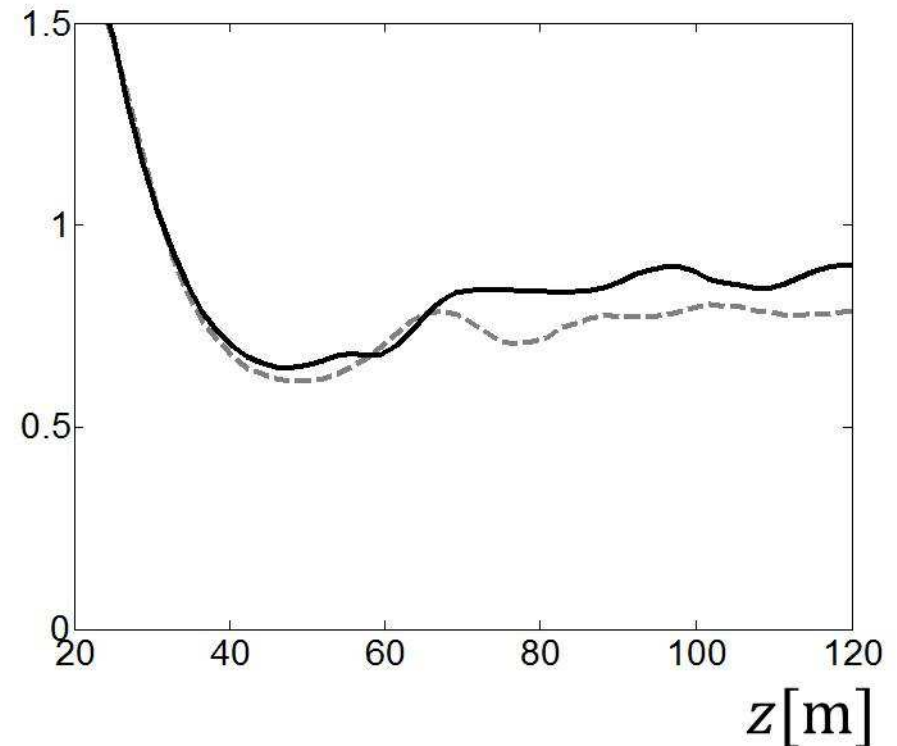
Radiation energy

$\langle E \rangle$ [mJ]



RMS bandwidth

σ_ω [%]



solid lines

– “S2E” beam

dashed lines

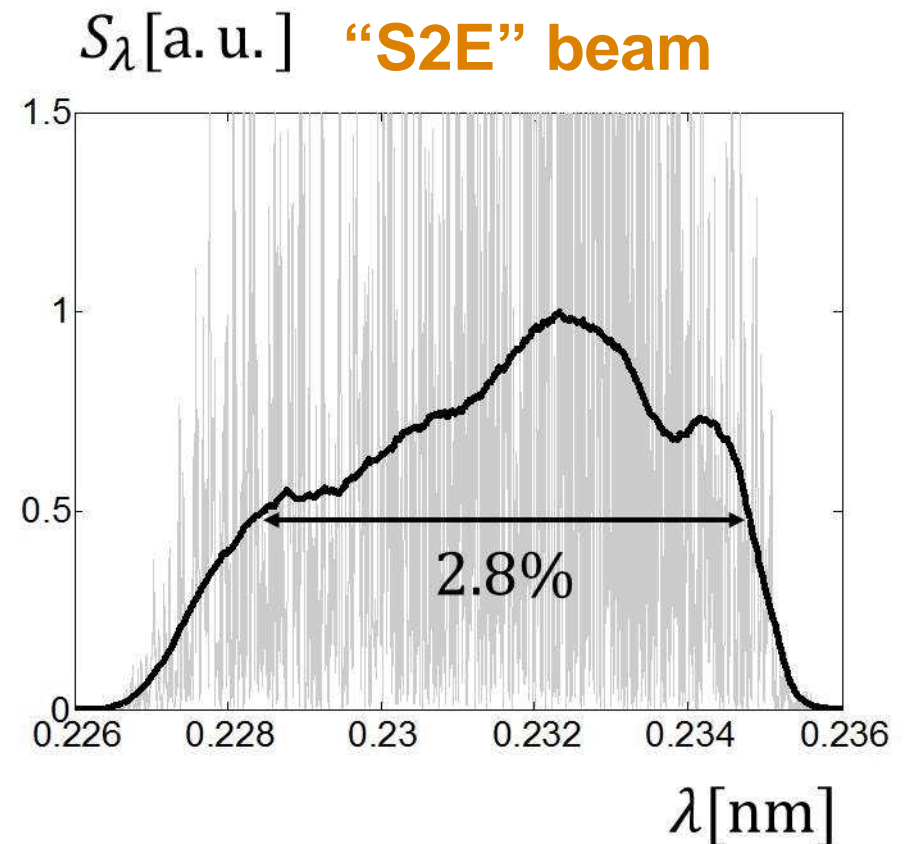
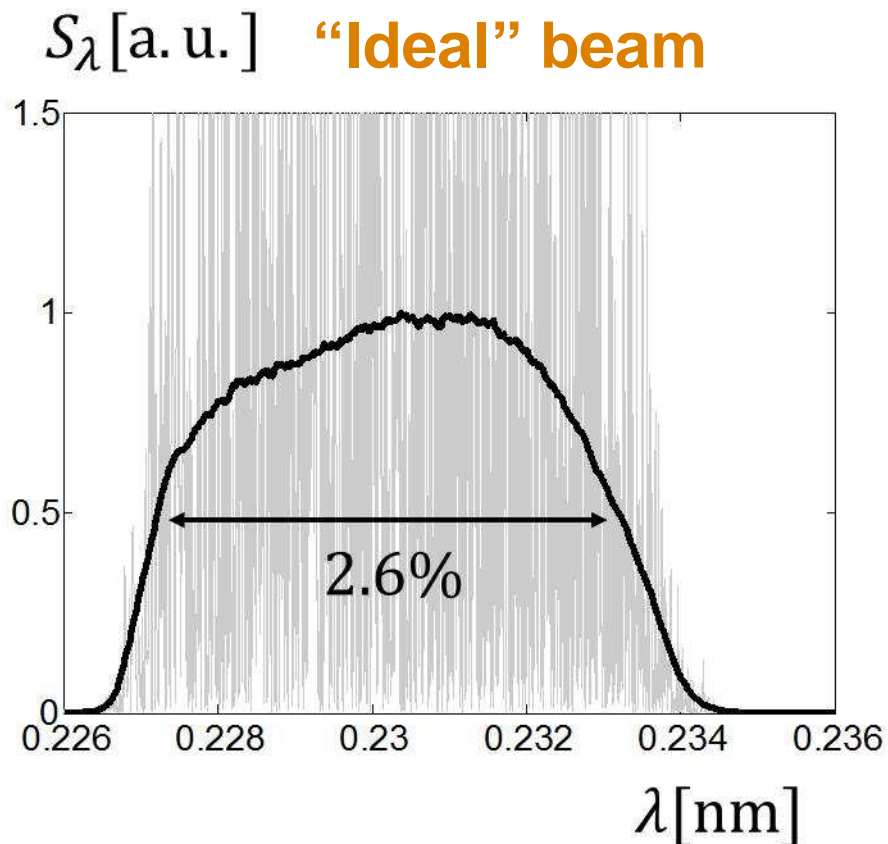
– “ideal” beam

We do not use an undulator tapering. The tapering could increase the radiation power yet by order of magnitude but the radiation bandwidth can be reduced because of it.



Broadband SASE radiation

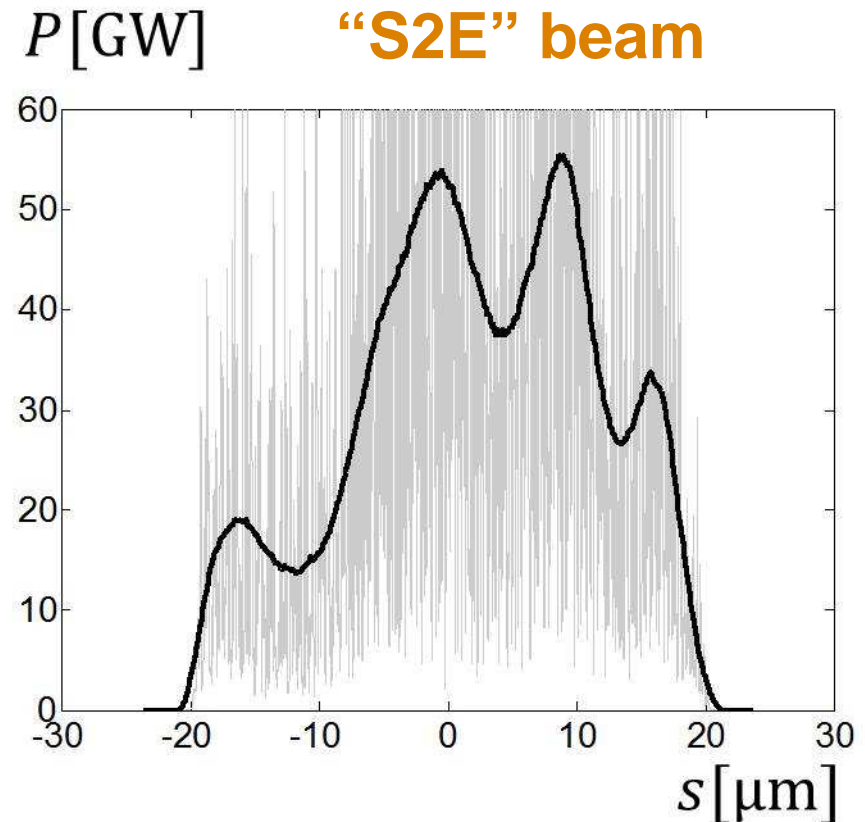
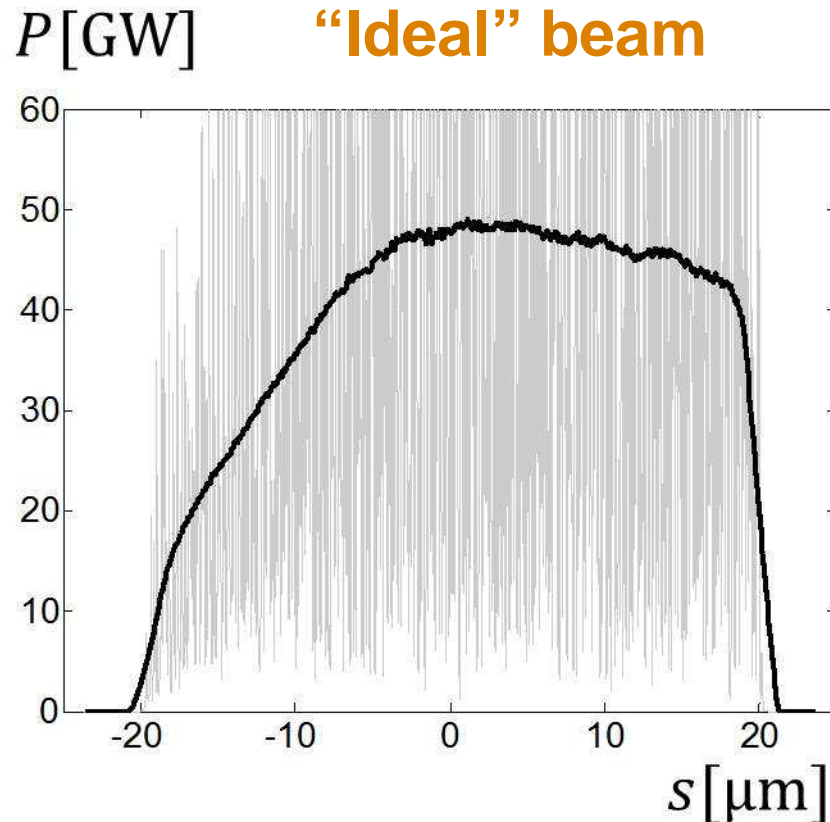
Full-Width-Half-Maximum bandwidth at $z = 115$ m



The solid lines present the spectrum averaged over many shots. The oscillating gray lines show an one shot spectrum.

Broadband SASE radiation

Radiation power at $z = 115$ m



The radiation from the beam tail and head are suppressed partially due to impact of the wake fields on the beam quality in the corrugated structure insertion. The solid lines present the averaging over many shots.

Conclusion

With 6 corrugated modules we can obtain 3% radiation bandwidth at 14 GeV (0.23 nm radiation wavelength).

Parameter	Value	Units
Bunch charge	500	pC
Bunch energy	14	GeV
Radiation wavelength	0.23	nm
Pulse energy	~4	mJ
Bandwidth	~3	%

I. Zagorodnov, G. Feng, T. Limberg, **Corrugated structure insertion for extending the SASE bandwidth up to 3% at the European XFEL**, Nuclear Instruments and Methods in Physics Research Section A 837 (2016) 69-79.



Conclusion

- The principal choice between **dielectric or corrugated metallic** layers has to be done. The required wakefields can be produced by many kinds of materials. SLAC uses the metallic corrugated structure. Another attractive possibility, which could reduce the costs and the dimensions of PWSI, could be a dielectric layer.
- The geometry of the layer, **length of one module and number of modules** should be chosen from material and beam dynamics studies.
- The important issues of **heating and survival** at the high bunch repetition rate have to be studied and technical decisions about cooling and protection have to be done.
- Simulations with PWSI at fresh-slice technique for **multicolor pulse production** etc. are required.

