

# Eigenmode Analysis for the PETRA III Cavity



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Status Report  
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TEMF, Darmstadt



# Outline



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- Motivation
- Computational Model
  - Drawings and geometry information
  - Numerical problem formulation
- Cavity tuning
  - Cell radius variation for the “reliable” and “spark” models
- Simulation results
  - Mode pattern and characteristic data for the “reliable” and “spark” models
- Summary / Outlook

# Outline



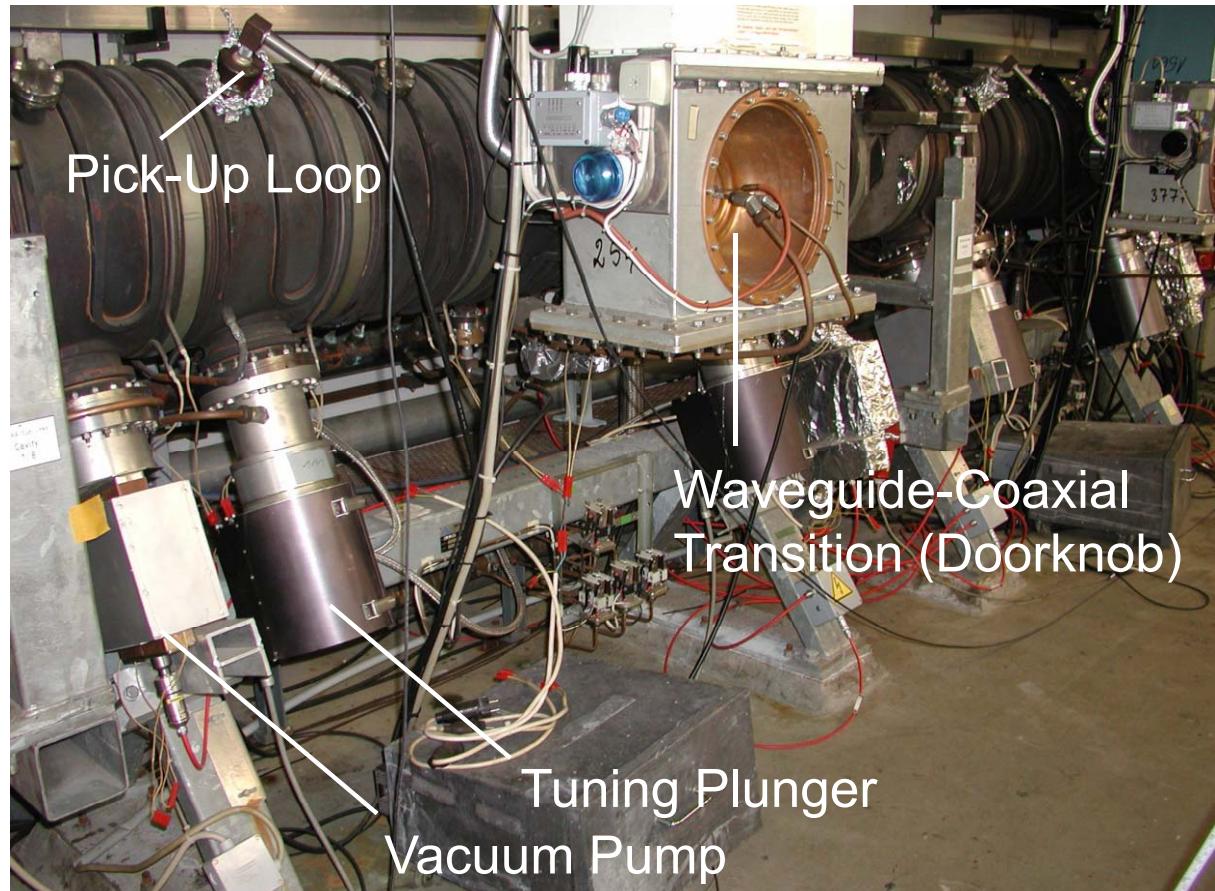
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# Motivation



- PETRA Cavities
  - Photographs



From time to time automatic switch-off of the power supply due to unexpected high fields in the cavity or waveguide system.

# Motivation



## ▪ Investigation Strategy

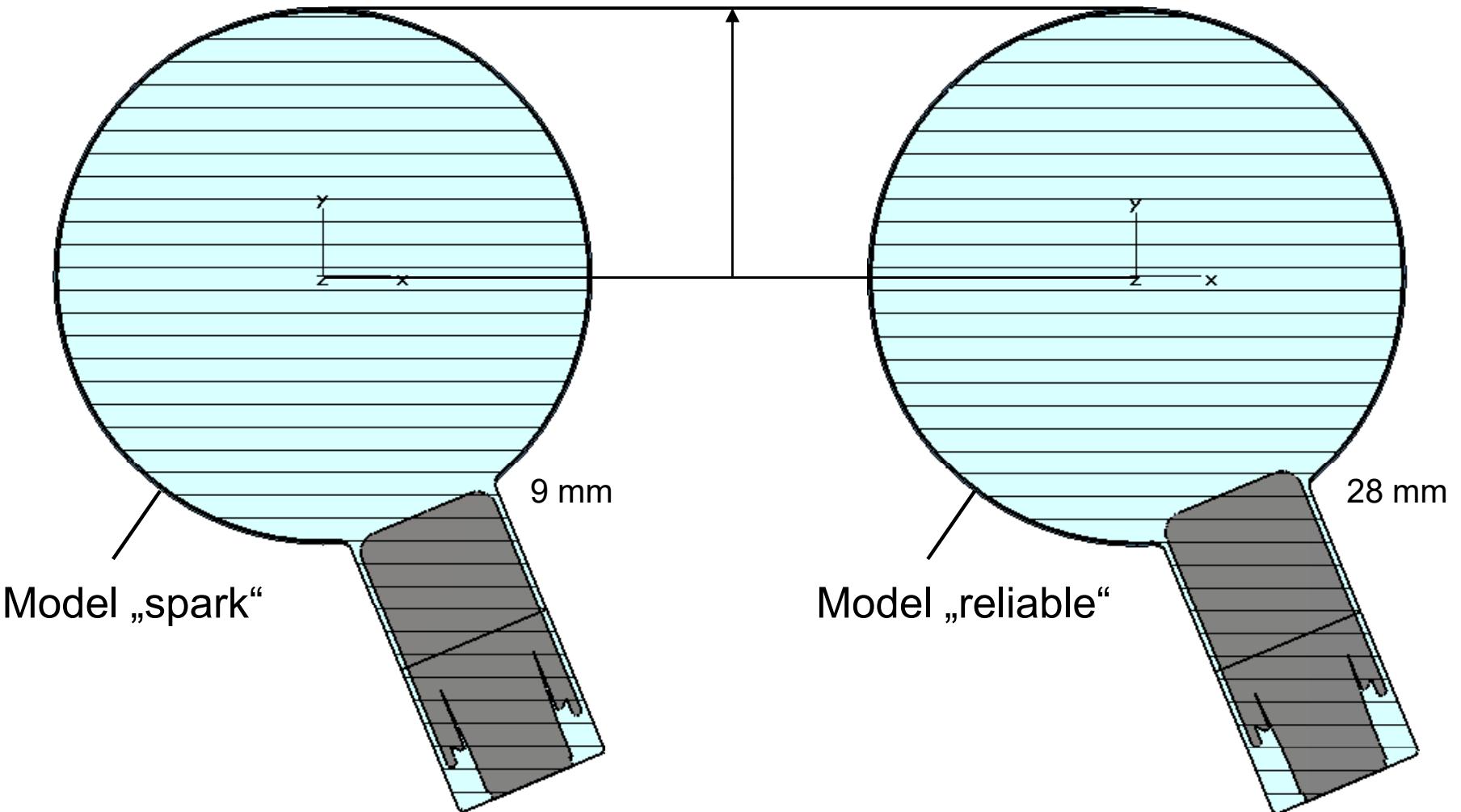
- Set up model “**spark**” with plunger positions 9 mm, modify radii  $r_1$  to  $r_7$  such, that the fundamental mode oscillates at 499,65 MHz and the bead-pull measurement “Cavity Nr. 23” is reproduced.
- Set up model “**reliable**” with plunger positions 28 mm, modify radii  $r_1$  to  $r_7$  such, that the fundamental mode oscillates at 499,65 MHz and the bead-pull measurement “Cavity Nr. 48” is reproduced.
- Use a port boundary condition for the waveguide during the tuning procedure.
  
- Calculate R/Q and Q values for all modes up to 1,2 GHz.
- Determine max. E and max. H in the plunger slits for all nodes. Keep the energy per mode constant.
- Use either PEC or PMC boundary conditions instead of the port boundary condition for the waveguide during the mode calculations.

# Motivation



- PETRA Cavities

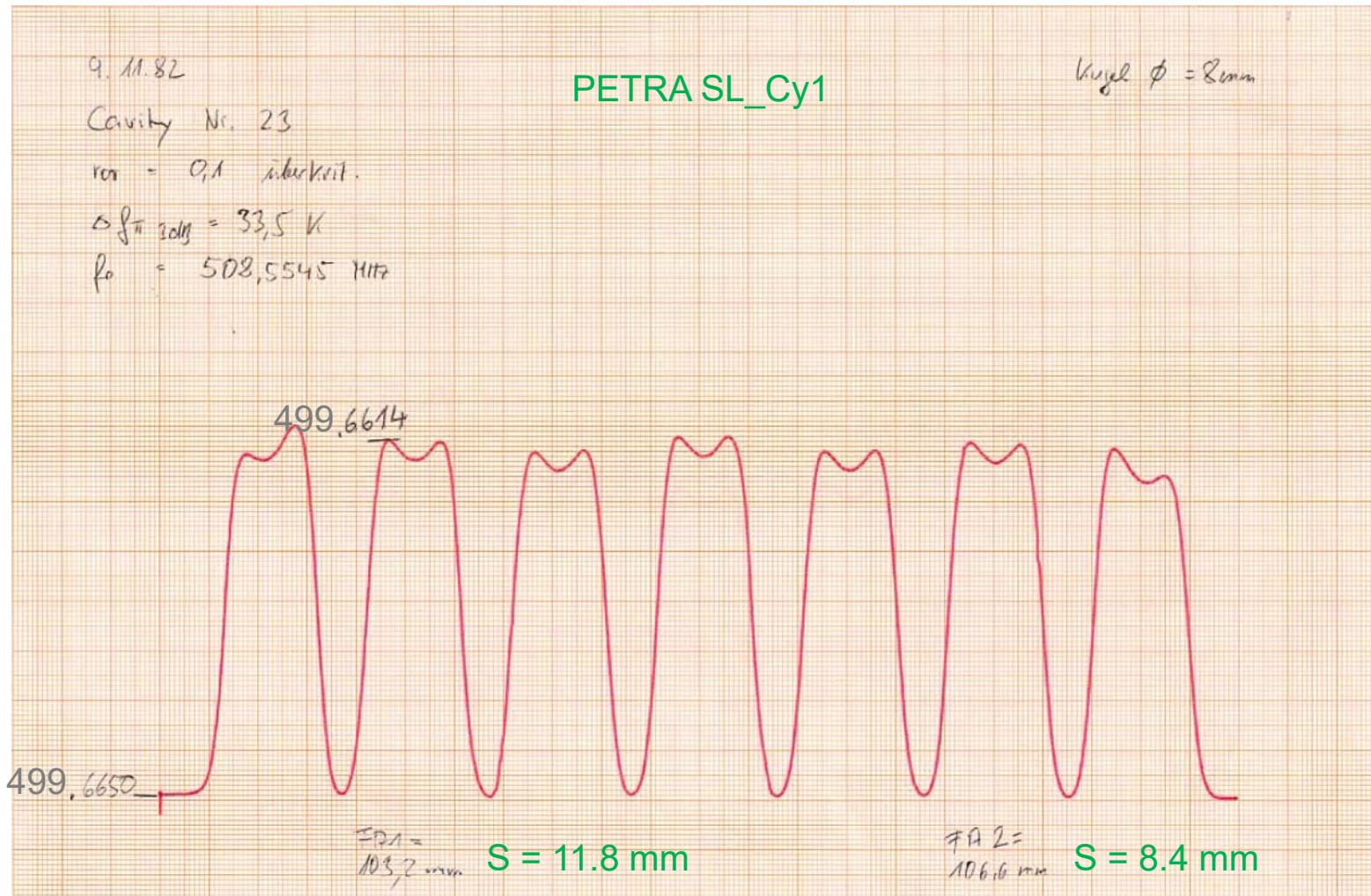
Design cavity radius  
 $r_2 = r_6 = 210,85 \text{ mm}$



# Motivation



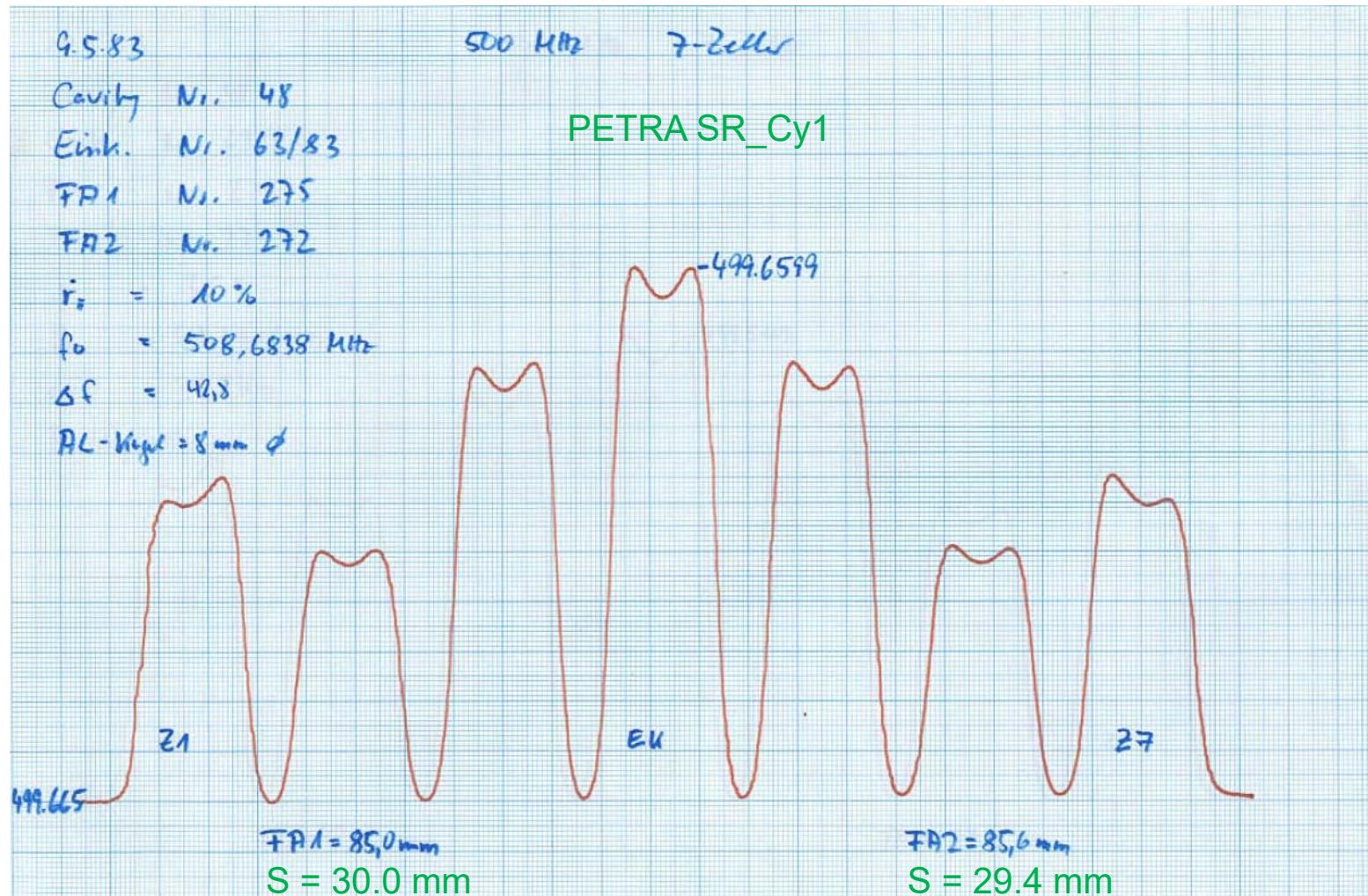
- Bead-pulling measurement for the model “spark”



# Motivation



- Bead-pulling measurement for the model “reliable”



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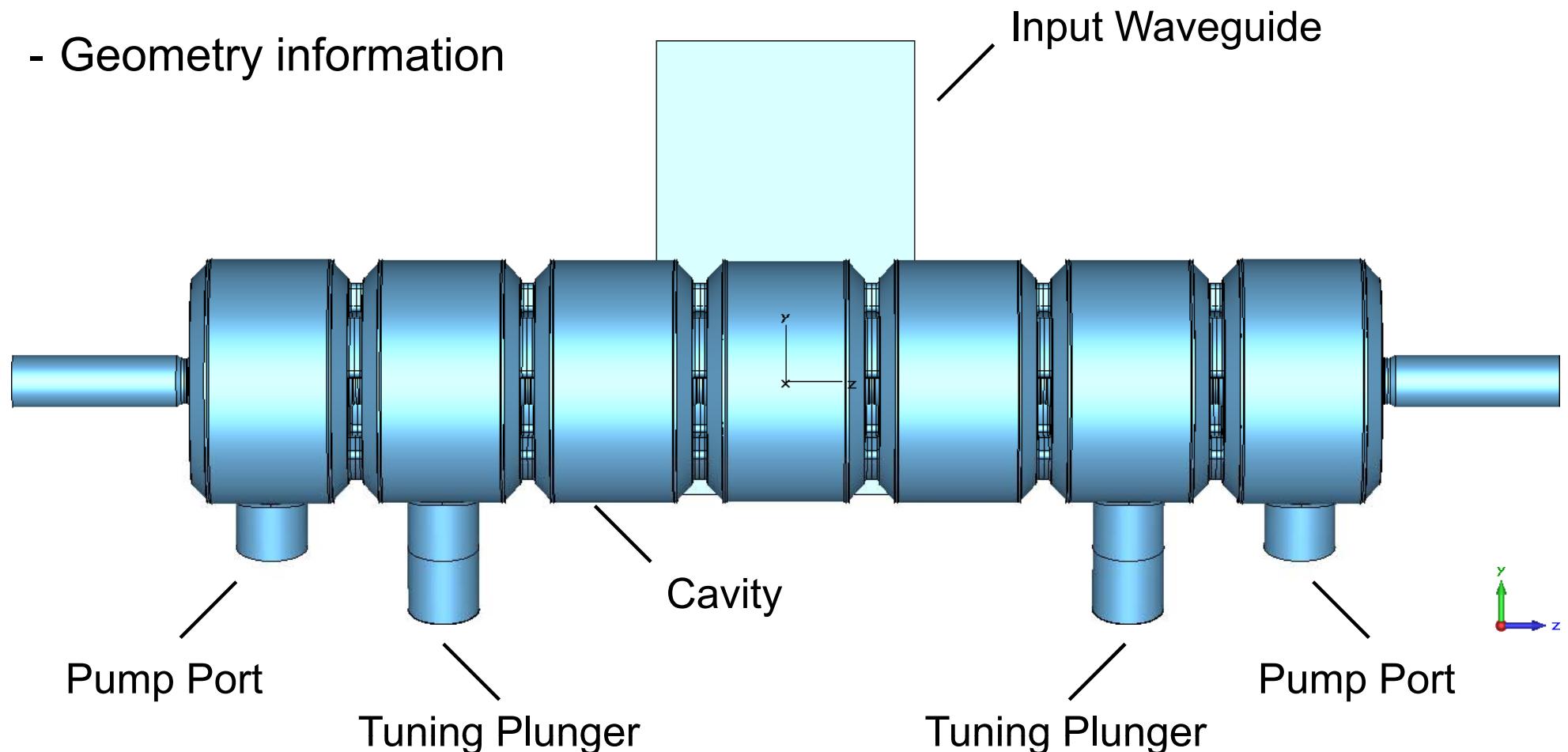
# Computational Model



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- PETRA III, 500 MHz, 7-cell Cavity

- Geometry information

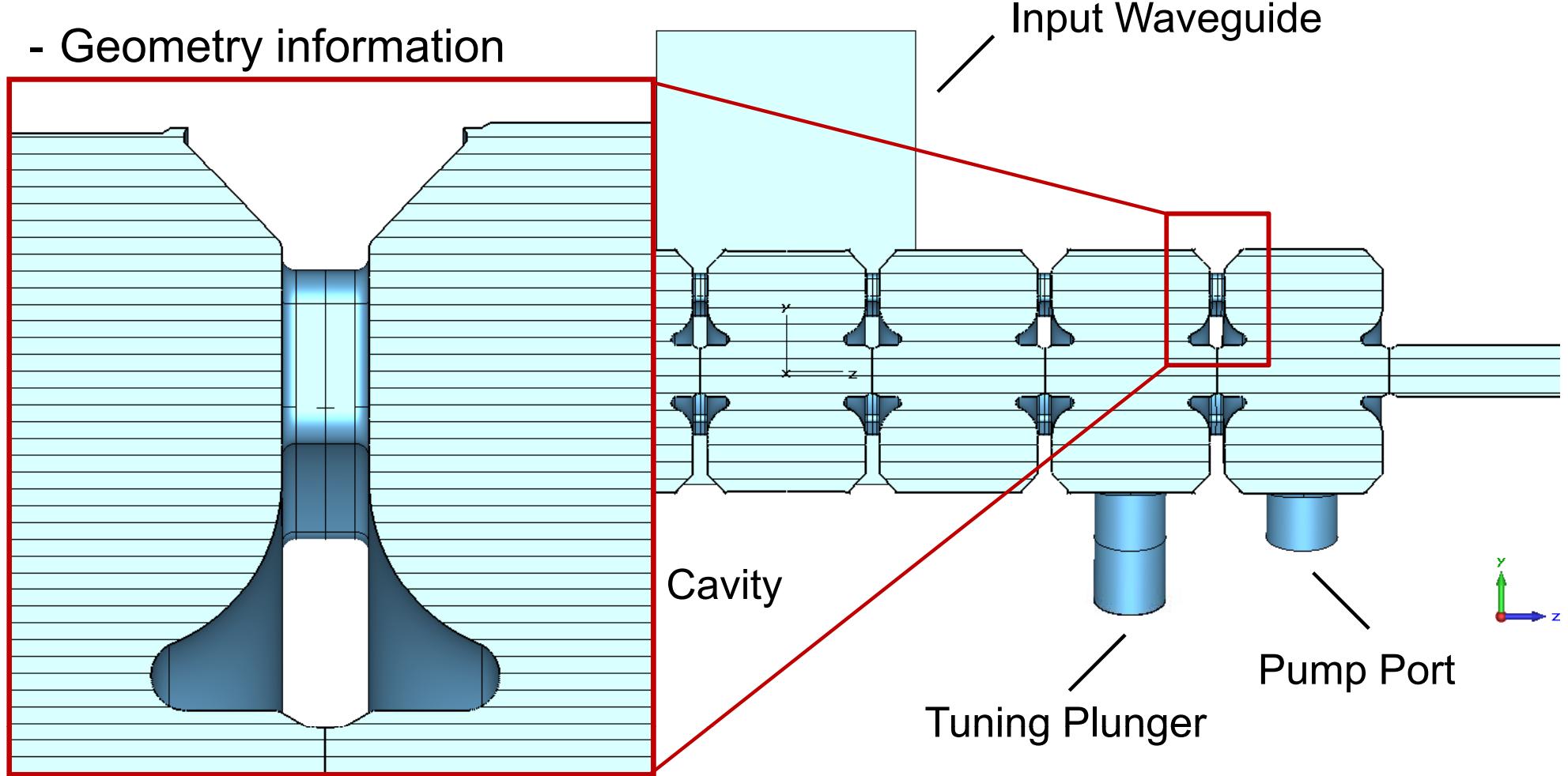


# Computational Model



- PETRA III, 500 MHz, 7-cell Cavity

- Geometry information

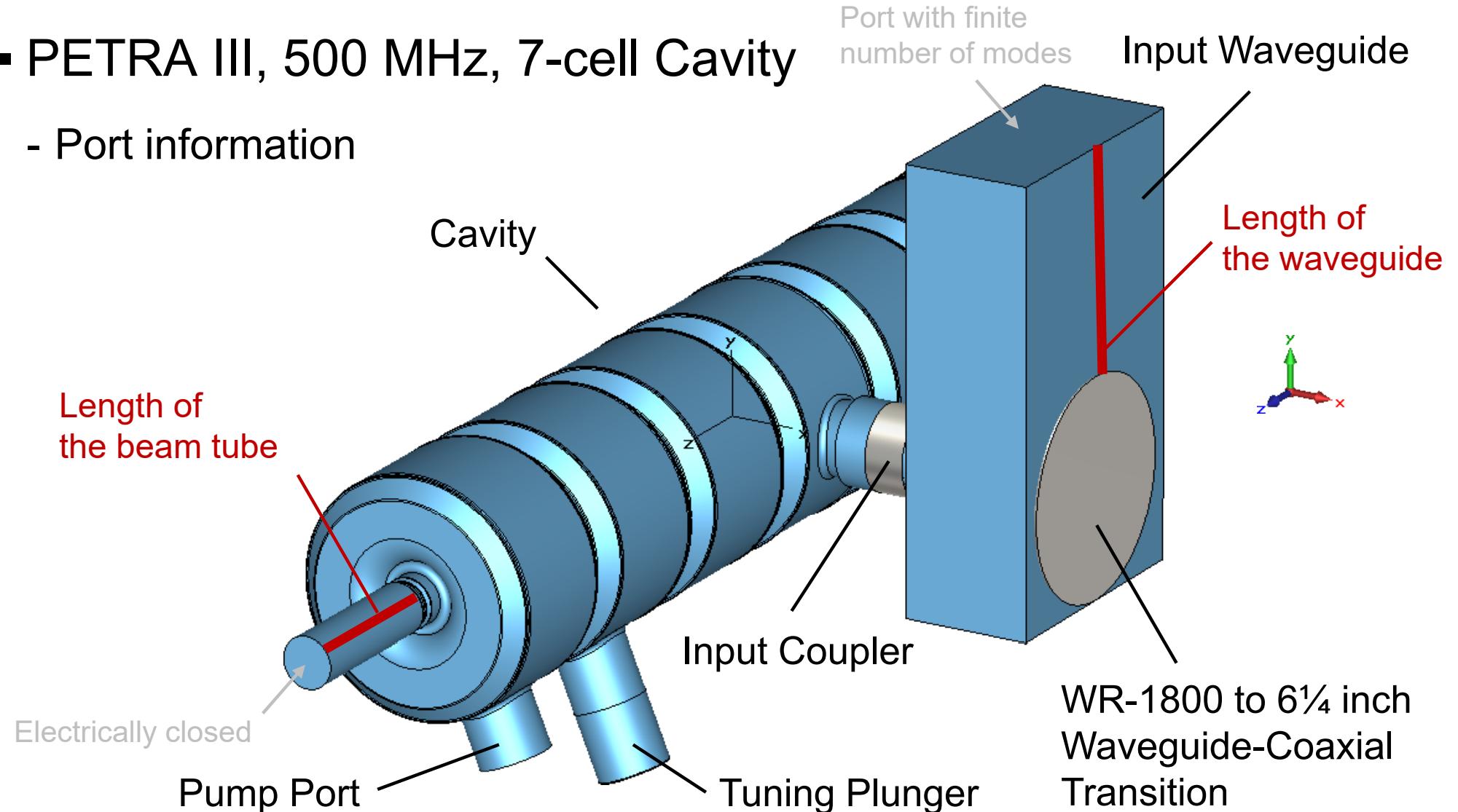


# Computational Model



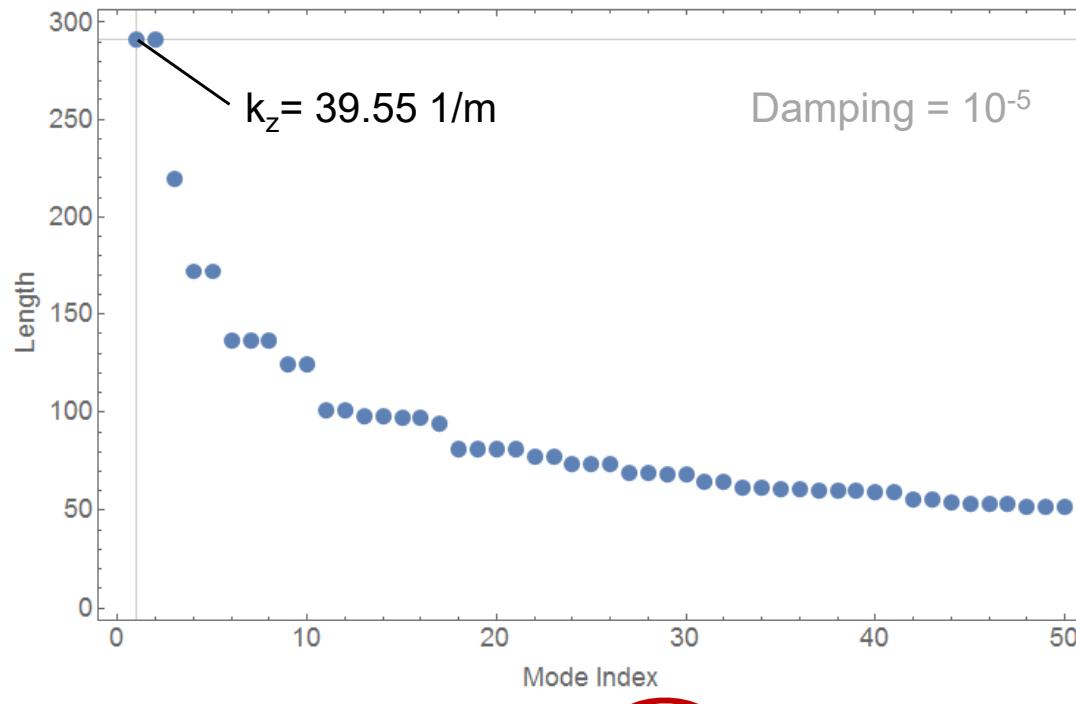
- PETRA III, 500 MHz, 7-cell Cavity

- Port information



# Computational Model

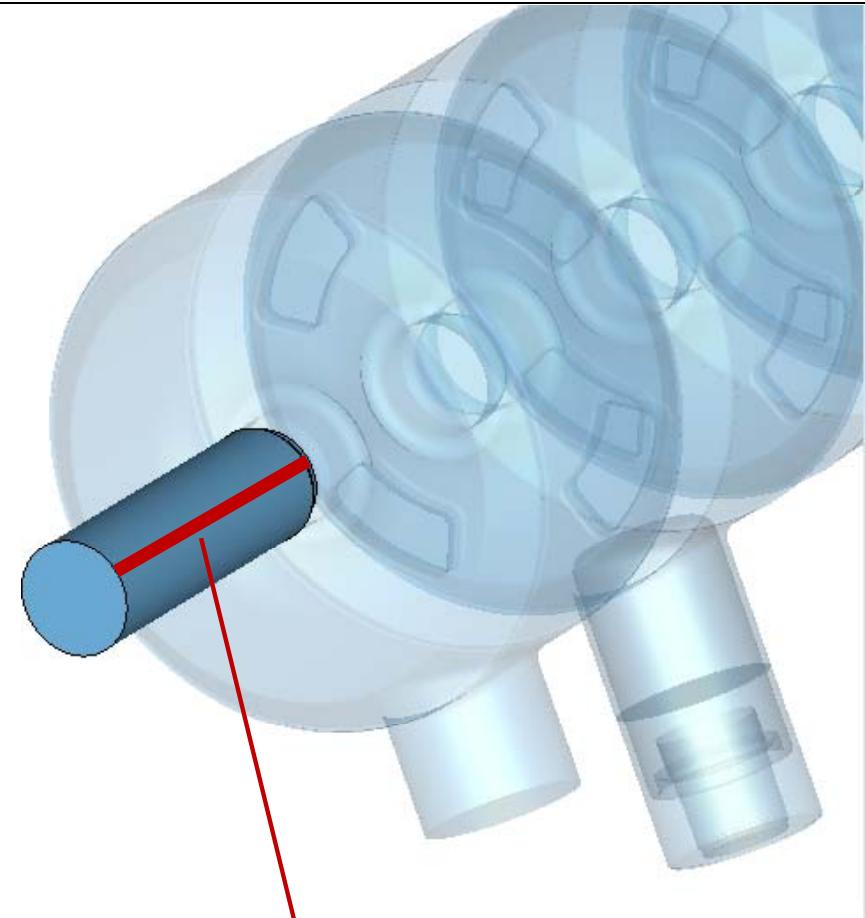
- PETRA III, 500 MHz, 7-cell Cavity
    - Beam-tube length



Damping  $10^{-3}$   $10^{-4}$   $10^{-5}$   $10^{-6}$

Length = { 174.6, 232.9, 291.1, 349.3 } mm

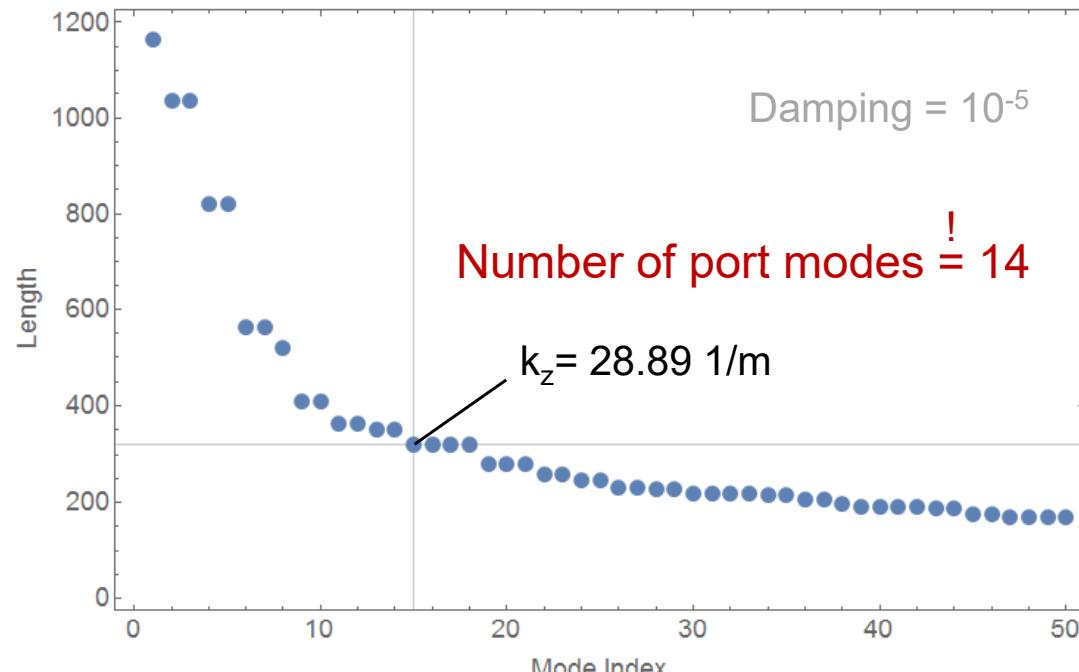
Length = 300 mm



# Computational Model

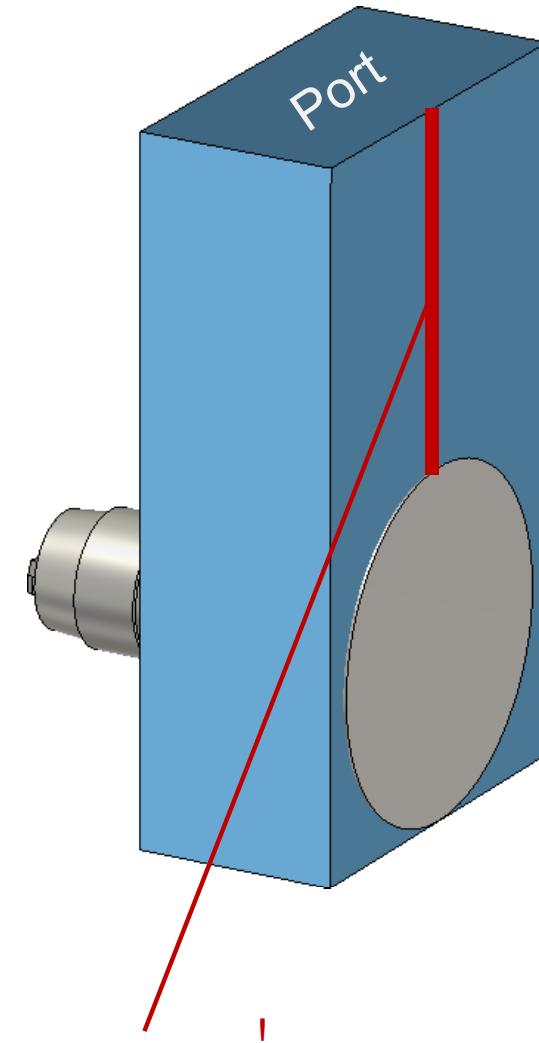


- PETRA III, 500 MHz, 7-cell Cavity
  - Waveguide length



Damping  $10^{-3} \quad 10^{-4} \quad 10^{-5} \quad 10^{-6}$

Length = { 239.1, 318.8, 398.5, 478.2 } mm



Length = 400 mm

# Computational Model

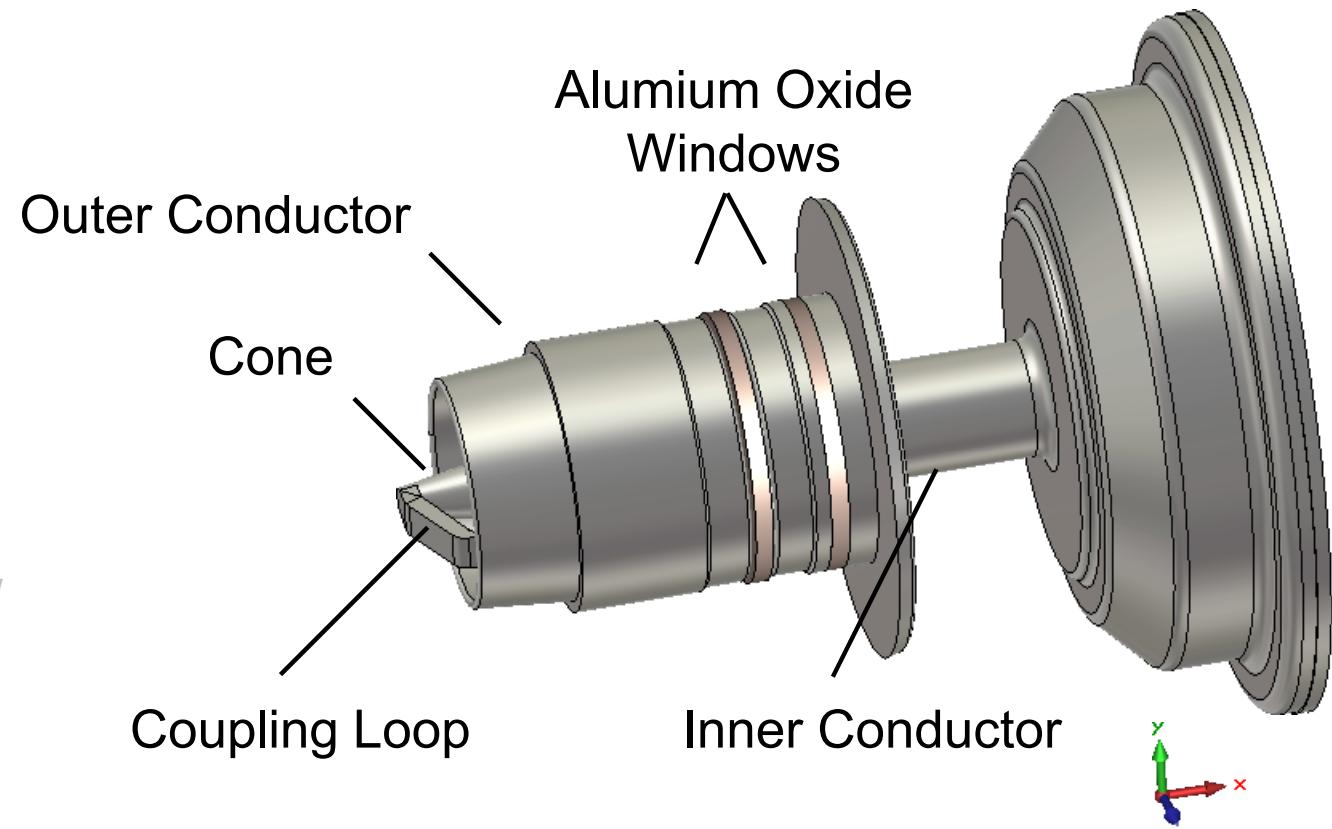
- PETRA III, 500 MHz, 7-cell Cavity
  - Geometry information (Details of the input coupler)

Photograph



<http://mhf-e.desy.de/e5/e63/>

Courtesy of  
Kathrin Cottel



# Computational Model

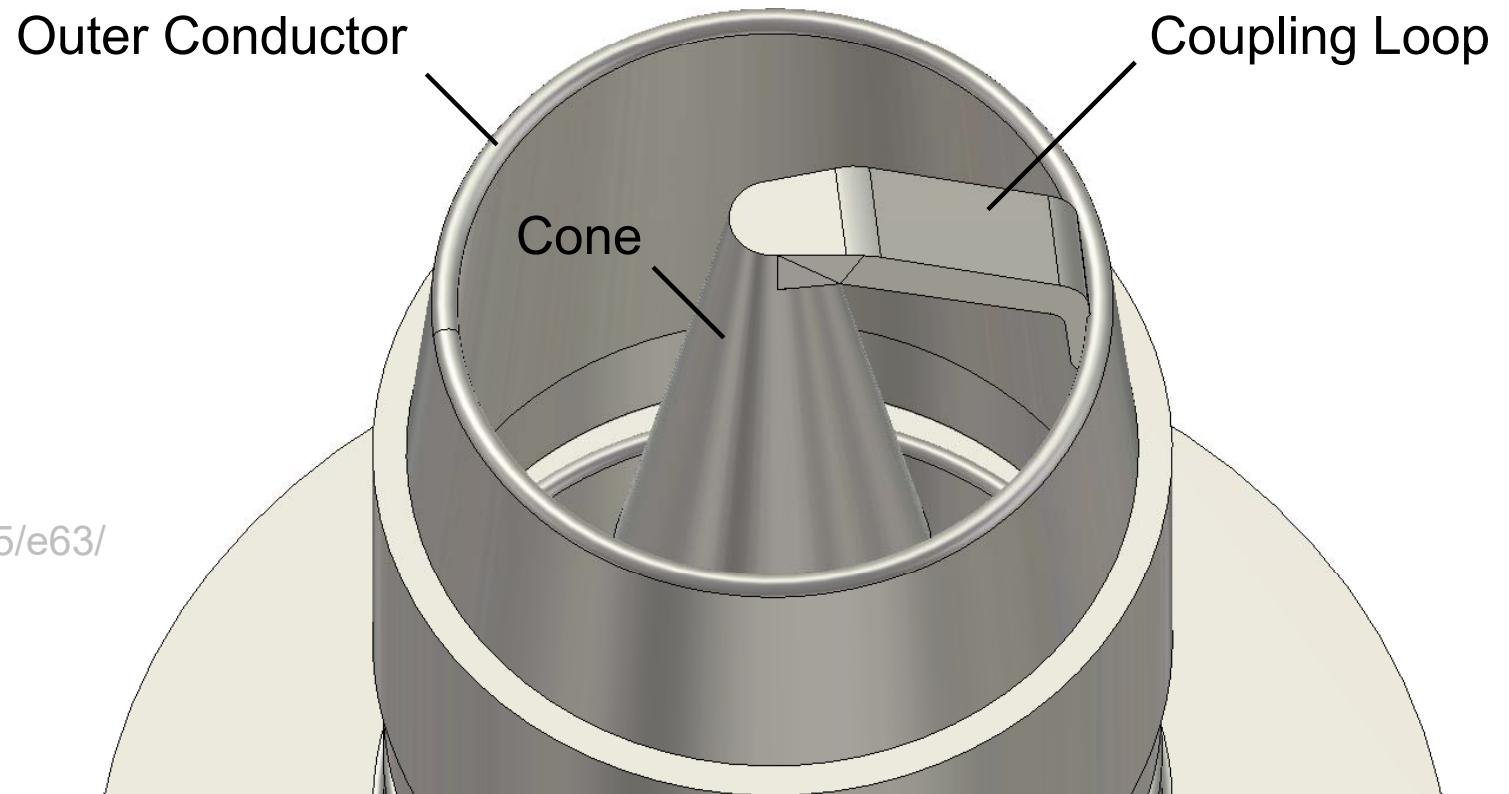
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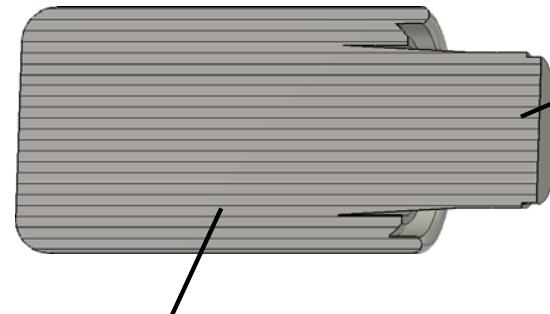


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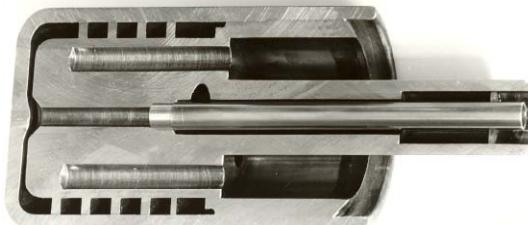
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- PETRA III, 500 MHz, 7-cell Cavity
  - Geometry information (Details of the tuning plungers)

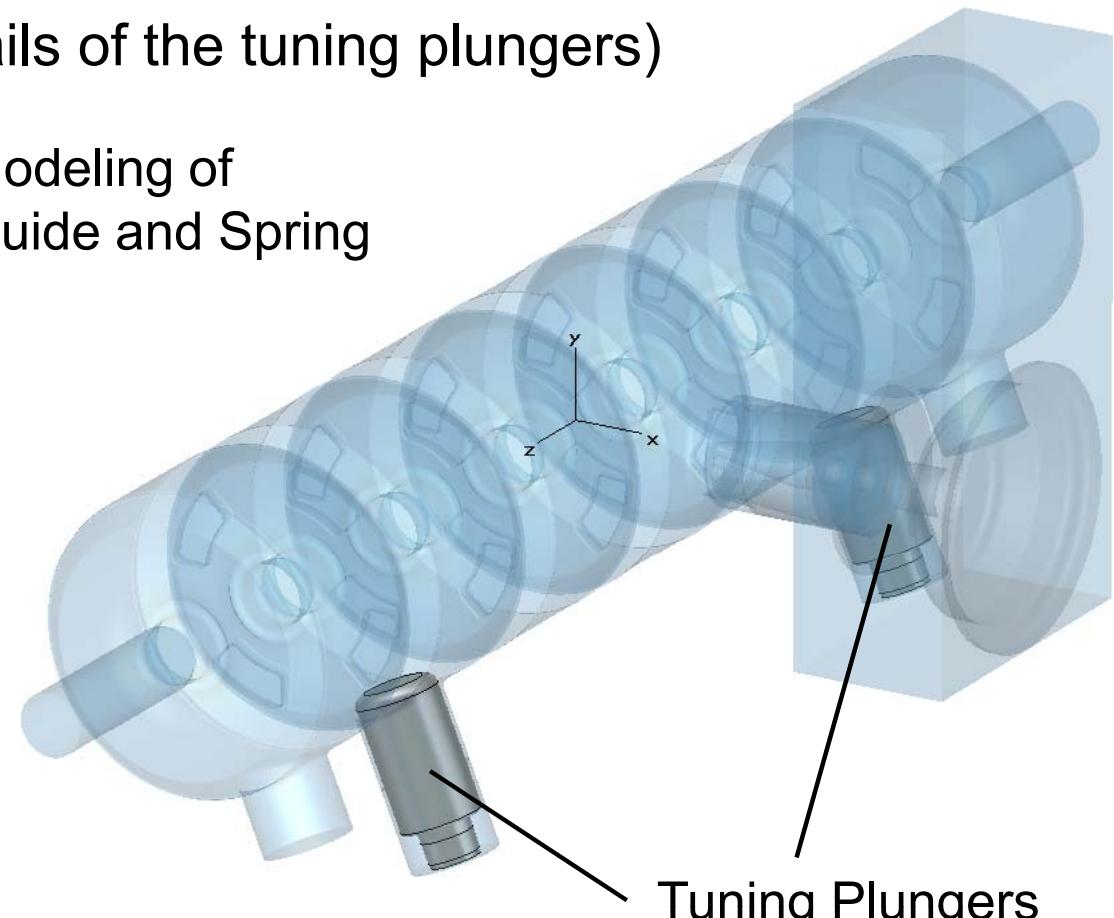


Neglect Cooling Channels

Photograph



<http://mhf-e.desy.de/e519/e187129/>

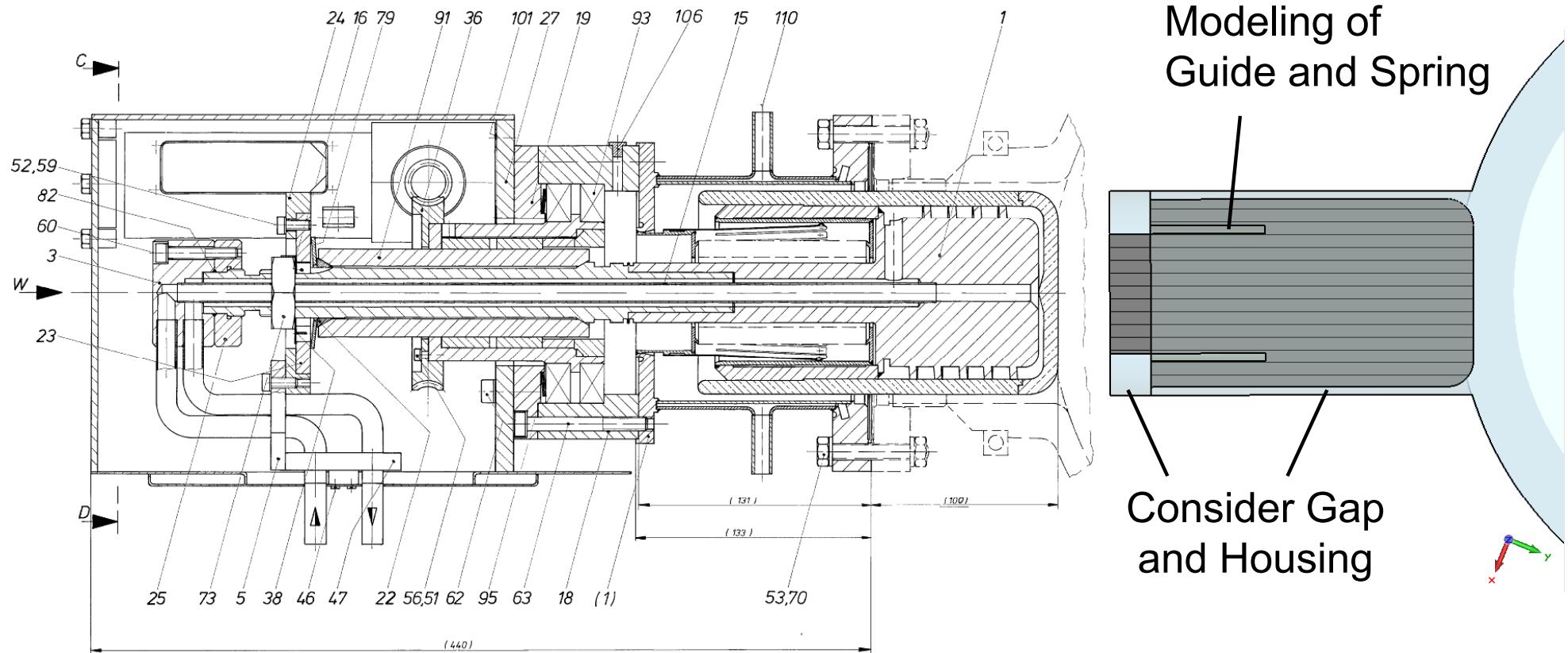


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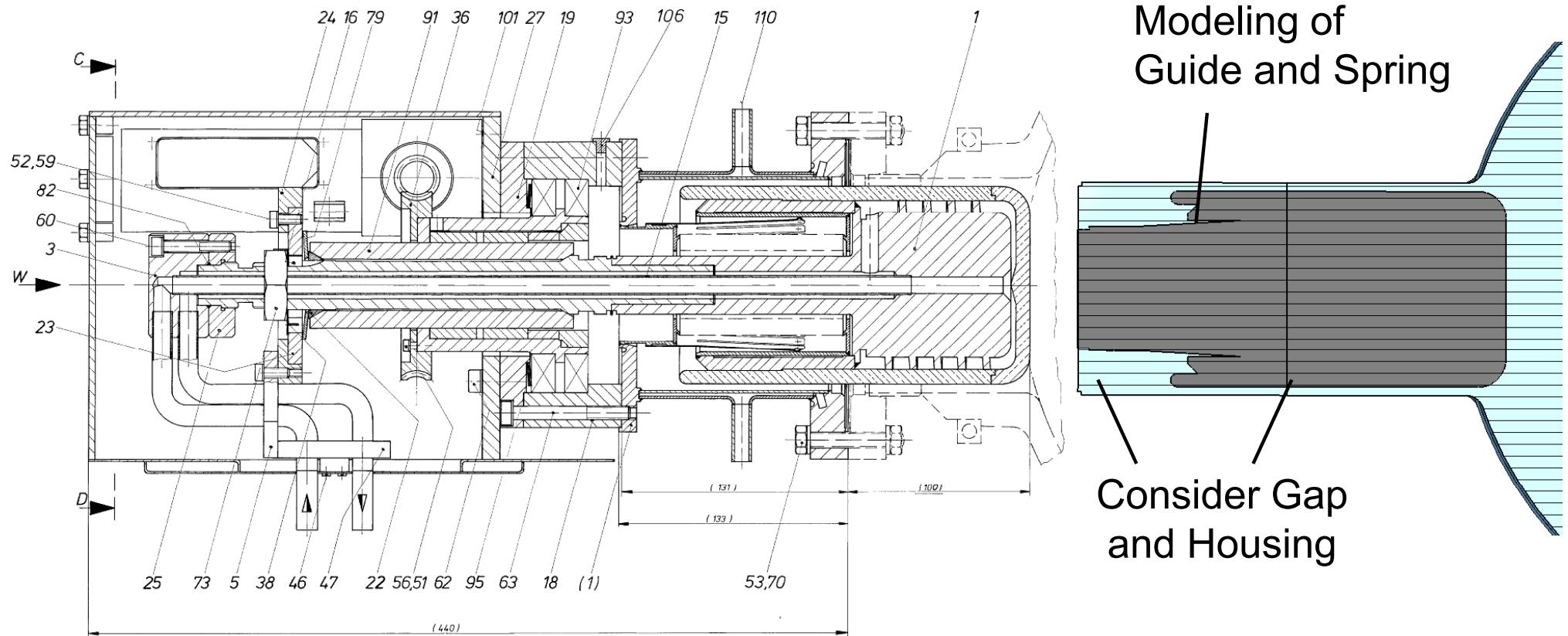
- PETRA III, 500 MHz, 7-cell Cavity
  - Geometry information (Details of the tuning plungers)



Courtesy of Michael Ebert

# Computational Model

- PETRA III, 500 MHz, 7-cell Cavity
  - Geometry information (Details of the tuning plungers)

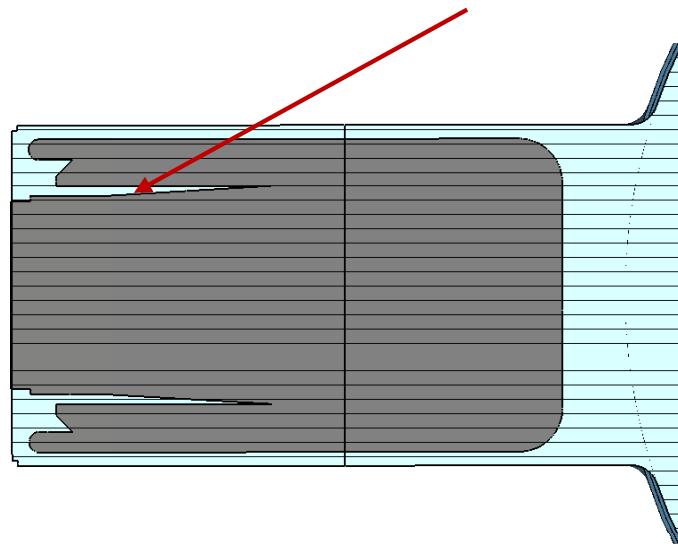


Courtesy of Michael Ebert

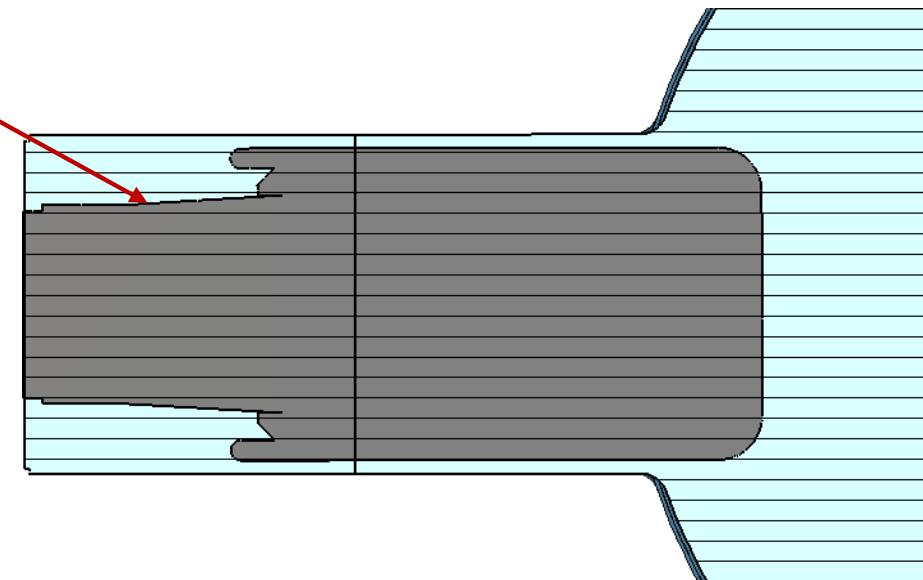
# Computational Model

- PETRA III, 500 MHz, 7-cell Cavity
  - Geometry information (Details of the tuning plungers)

Spring is now fixed (only plunger movable)



Plunger position = -20 mm



Plunger position = 50 mm

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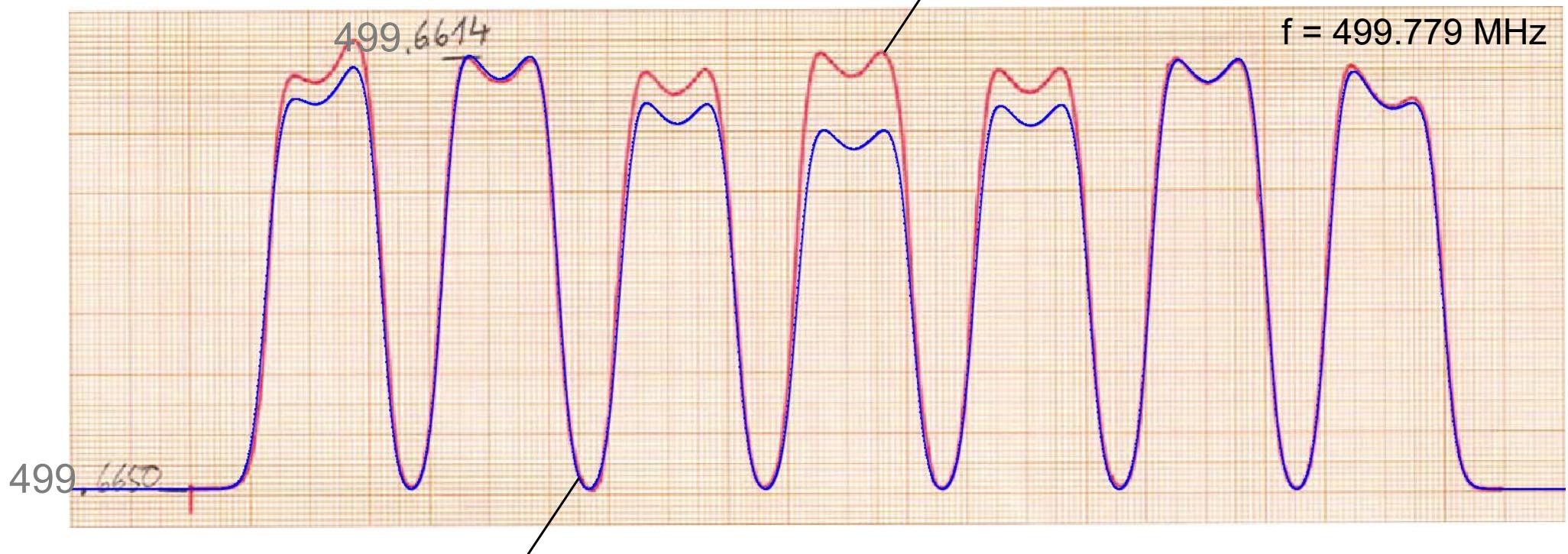
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# Cavity Tuning



- Model “spark”

Red: Bead-pulling **measurement** of the frequency shift



Blue: Bead-pulling **simulation** of the frequency shift (scaled  $|\vec{E}|^2$  vs. position)

$$R = \{ 213.65, 210.85, 210.90, 209.85, 210.90, 210.85, 213.65 \} \text{ mm}$$

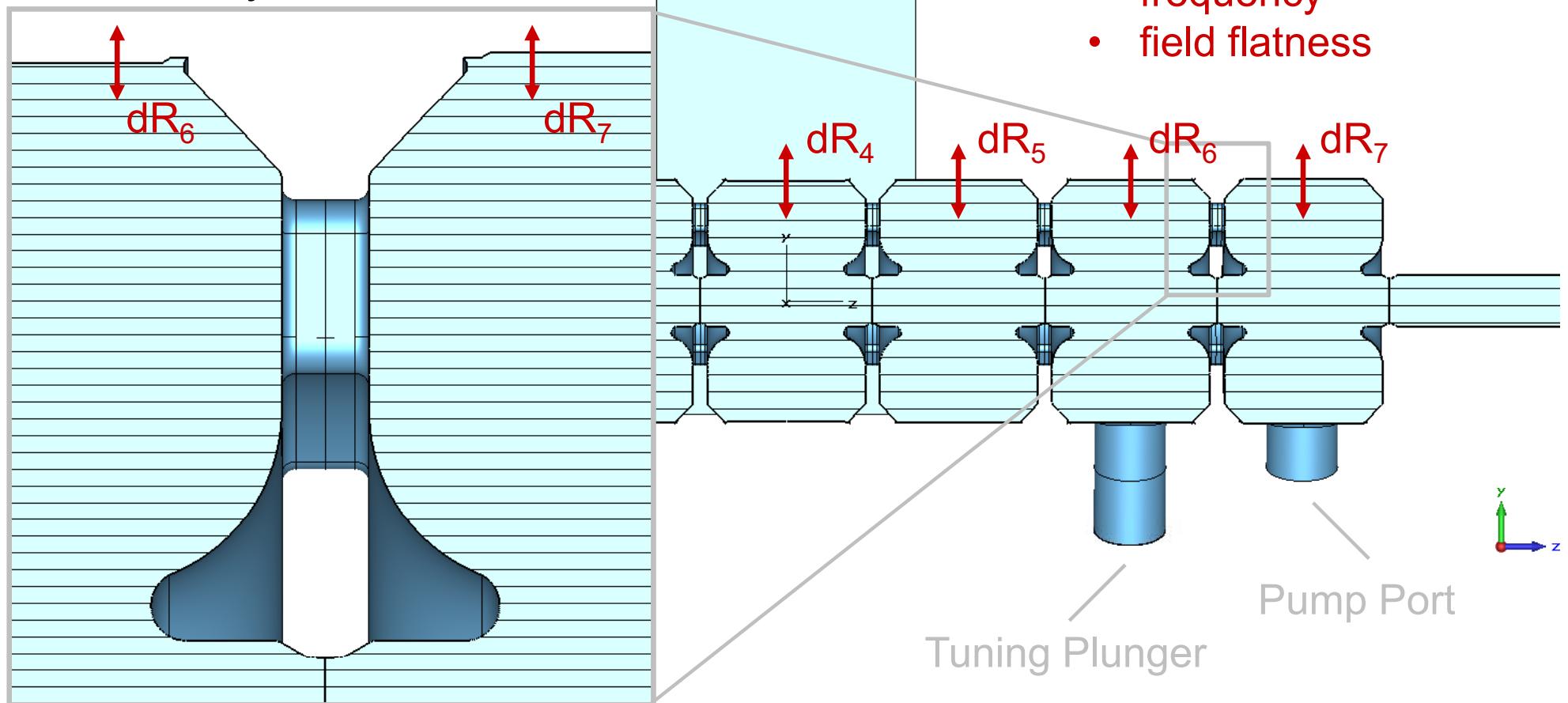
$$dR = \{ 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0 \} \text{ mm}$$

# Cavity Tuning



- Model “spark”

- Sensitivity information



# Cavity Tuning



## ▪ Model “spark”

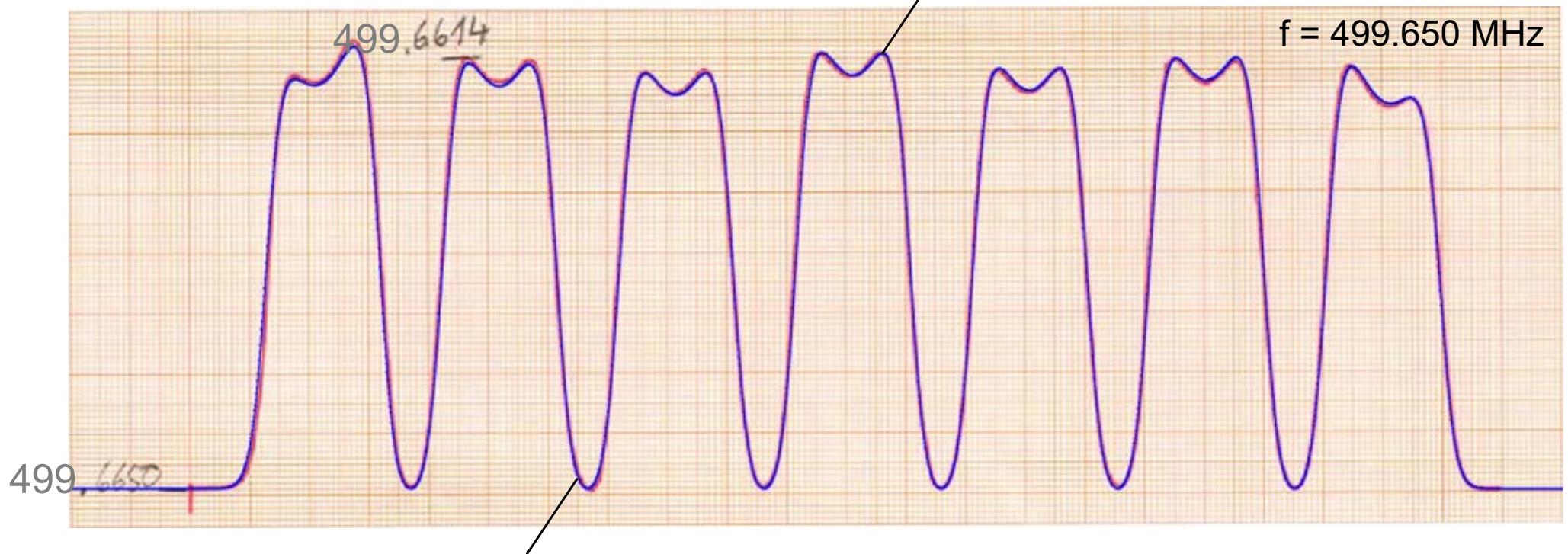
|    | A      | B        | C         | D        | E        | F        | G        | H        | M            | P              | Q                        |
|----|--------|----------|-----------|----------|----------|----------|----------|----------|--------------|----------------|--------------------------|
| 1  | Run ID | dR1      | dR2       | dR3      | dR4      | dR5      | dR6      | dR7      | Tetrahedrons | Frequenz / MHz | Frequenzabweichung / kHz |
| 2  | 1      | 0,000    | 0,000     | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 1.201.788    | 499,778921     | 128,921                  |
| 3  | 2      | 0,100    | 0,000     | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 1.203.759    |                |                          |
| 4  | 3      | 0,000    | 0,100     | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 1.203.385    |                |                          |
| 5  | 4      | 0,000    | 0,000     | 0,100    | 0,000    | 0,000    | 0,000    | 0,000    | 1.203.963    |                |                          |
| 6  | 5      | 0,000    | 0,000     | 0,000    | 0,100    | 0,000    | 0,000    | 0,000    | 1.203.160    |                |                          |
| 7  | 6      | 0,000    | 0,000     | 0,000    | 0,000    | 0,100    | 0,000    | 0,000    | 1.203.386    |                |                          |
| 8  | 7      | 0,000    | 0,000     | 0,000    | 0,000    | 0,000    | 0,100    | 0,000    | 1.203.552    |                |                          |
| 9  | 8      | 0,000    | 0,000     | 0,000    | 0,000    | 0,000    | 0,000    | 0,100    | 1.205.016    |                |                          |
| 10 | 9      | 0,119    | -0,005    | 0,055    | 0,246    | 0,062    | 0,020    | 0,074    | 1.204.470    | 499,654467     | 4,467                    |
| 11 | 10     | 0,219    | -0,005    | 0,055    | 0,246    | 0,062    | 0,020    | 0,074    | 1.203.479    |                |                          |
| 12 | 11     | 0,119    | 0,095     | 0,055    | 0,246    | 0,062    | 0,020    | 0,074    | 1.204.842    |                |                          |
| 13 | 12     | 0,119    | -0,005    | 0,155    | 0,246    | 0,062    | 0,020    | 0,074    | 1.204.895    |                |                          |
| 14 | 13     | 0,119    | -0,005    | 0,055    | 0,346    | 0,062    | 0,020    | 0,074    | 1.203.122    |                |                          |
| 15 | 14     | 0,119    | -0,005    | 0,055    | 0,246    | 0,162    | 0,020    | 0,074    | 1.205.044    |                |                          |
| 16 | 15     | 0,119    | -0,005    | 0,055    | 0,246    | 0,062    | 0,120    | 0,074    | 1.205.204    |                |                          |
| 17 | 16     | 0,119    | -0,005    | 0,055    | 0,246    | 0,062    | 0,020    | 0,174    | 1.205.856    |                |                          |
| 18 | 17     | 0,131634 | -0,030270 | 0,067898 | 0,247176 | 0,071430 | 0,016050 | 0,086529 | 1.204.205    | 499,651077     | 1,077                    |
| 19 | 18     | 0,232    | -0,030    | 0,068    | 0,247    | 0,071    | 0,016    | 0,087    | 1.205.382    |                |                          |
| 20 | 19     | 0,132    | 0,070     | 0,068    | 0,247    | 0,071    | 0,016    | 0,087    | 1.204.426    |                |                          |
| 21 | 20     | 0,132    | -0,030    | 0,168    | 0,247    | 0,071    | 0,016    | 0,087    | 1.203.930    |                |                          |
| 22 | 21     | 0,132    | -0,030    | 0,068    | 0,347    | 0,071    | 0,016    | 0,087    | 1.205.444    |                |                          |
| 23 | 22     | 0,132    | -0,030    | 0,068    | 0,247    | 0,171    | 0,016    | 0,087    | 1.204.128    |                |                          |
| 24 | 23     | 0,132    | -0,030    | 0,068    | 0,247    | 0,071    | 0,116    | 0,087    | 1.204.482    |                |                          |
| 25 | 24     | 0,132    | -0,030    | 0,068    | 0,247    | 0,071    | 0,016    | 0,187    | 1.204.001    |                |                          |
| 26 | 25     | 0,133614 | -0,031288 | 0,068746 | 0,246354 | 0,075181 | 0,013435 | 0,088617 | 1.203.513    | 499,649611     | -0,389                   |
| 27 |        |          |           |          |          |          |          |          |              |                |                          |

# Cavity Tuning



- Model “spark”

Red: Bead-pulling **measurement** of the frequency shift



Blue: Bead-pulling **simulation** of the frequency shift (scaled  $|\vec{E}|^2$  vs. position)

$$R = \{ 213.65, 210.85, 210.90, 209.85, 210.90, 210.85, 213.65 \} \text{ mm}$$

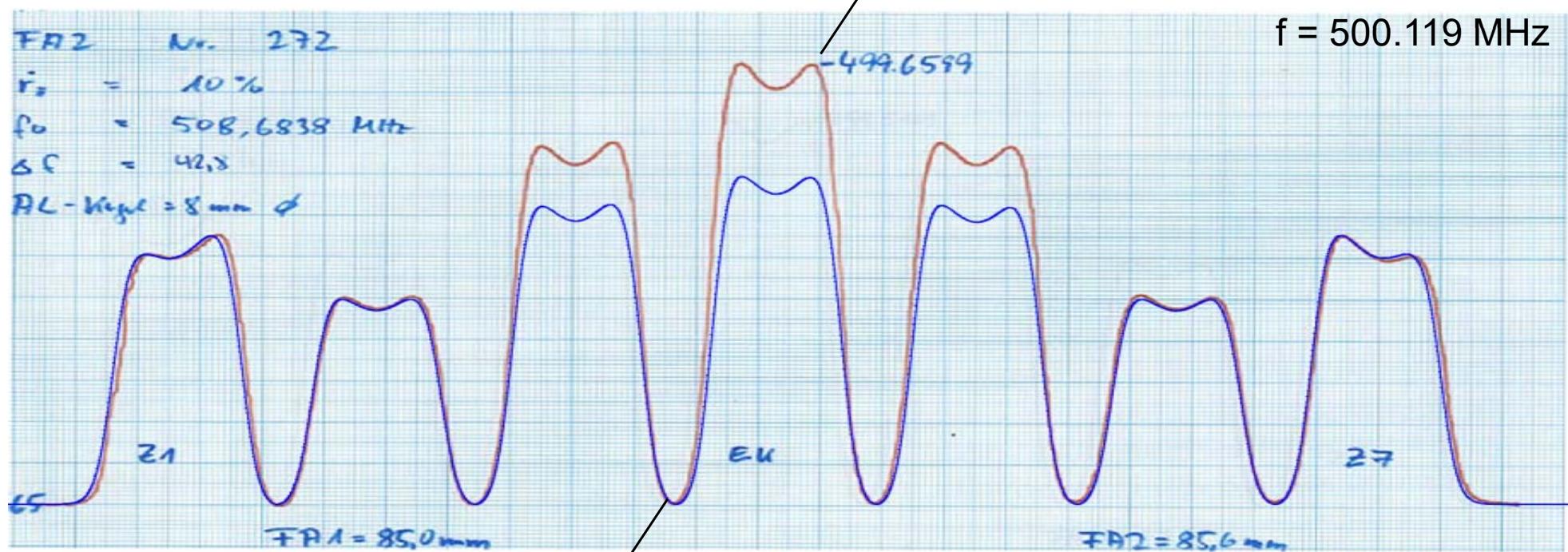
$$dR = \{ 0.134, -0.031, 0.069, 0.246, 0.075, 0.013, 0.087 \} \text{ mm}$$

# Cavity Tuning



- Model “reliable”

Red: Bead-pulling **measurement** of the frequency shift



Blue: Bead-pulling **simulation** of the frequency shift (scaled  $|\vec{E}|^2$  vs. position)

$$R = \{ 213.65, 210.85, 210.90, 209.85, 210.90, 210.85, 213.65 \} \text{ mm}$$

$$dR = \{ 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0 \} \text{ mm}$$

# Cavity Tuning



- Model “reliable”

|    | A      | B        | C        | D        | E        | F        | G        | H        | P              | Q                        |
|----|--------|----------|----------|----------|----------|----------|----------|----------|----------------|--------------------------|
| 1  | Run ID | dR1      | dR2      | dR3      | dR4      | dR5      | dR6      | dR7      | Frequenz / MHz | Frequenzabweichung / kHz |
| 2  | 1      | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 500,119049     | 469,049                  |
| 3  | 2      | 0,100    | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    |                |                          |
| 4  | 3      | 0,000    | 0,100    | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    |                |                          |
| 5  | 4      | 0,000    | 0,000    | 0,100    | 0,000    | 0,000    | 0,000    | 0,000    |                |                          |
| 6  | 5      | 0,000    | 0,000    | 0,000    | 0,100    | 0,000    | 0,000    | 0,000    |                |                          |
| 7  | 6      | 0,000    | 0,000    | 0,000    | 0,000    | 0,100    | 0,000    | 0,000    |                |                          |
| 8  | 7      | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 0,100    | 0,000    |                |                          |
| 9  | 8      | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 0,000    | 0,100    |                |                          |
| 10 | 9      | 0,216    | 0,163    | 0,324    | 0,451    | 0,285    | 0,162    | 0,272    | 499,676489     | 26,489                   |
| 11 | 10     | 0,316    | 0,163    | 0,324    | 0,451    | 0,285    | 0,162    | 0,272    |                |                          |
| 12 | 11     | 0,216    | 0,263    | 0,324    | 0,451    | 0,285    | 0,162    | 0,272    |                |                          |
| 13 | 12     | 0,216    | 0,163    | 0,424    | 0,451    | 0,285    | 0,162    | 0,272    |                |                          |
| 14 | 13     | 0,216    | 0,163    | 0,324    | 0,551    | 0,285    | 0,162    | 0,272    |                |                          |
| 15 | 14     | 0,216    | 0,163    | 0,324    | 0,451    | 0,385    | 0,162    | 0,272    |                |                          |
| 16 | 15     | 0,216    | 0,163    | 0,324    | 0,451    | 0,285    | 0,262    | 0,272    |                |                          |
| 17 | 16     | 0,216    | 0,163    | 0,324    | 0,451    | 0,285    | 0,162    | 0,372    |                |                          |
| 18 | 17     | 0,292    | 0,143    | 0,320    | 0,460    | 0,317    | 0,156    | 0,289    | 499,653842     | 3,842                    |
| 19 | 18     | 0,392    | 0,143    | 0,320    | 0,460    | 0,317    | 0,156    | 0,289    |                |                          |
| 20 | 19     | 0,292    | 0,243    | 0,320    | 0,460    | 0,317    | 0,156    | 0,289    |                |                          |
| 21 | 20     | 0,292    | 0,143    | 0,420    | 0,460    | 0,317    | 0,156    | 0,289    |                |                          |
| 22 | 21     | 0,292    | 0,143    | 0,320    | 0,560    | 0,317    | 0,156    | 0,289    |                |                          |
| 23 | 22     | 0,292    | 0,143    | 0,320    | 0,460    | 0,417    | 0,156    | 0,289    |                |                          |
| 24 | 23     | 0,292    | 0,143    | 0,320    | 0,460    | 0,317    | 0,256    | 0,289    |                |                          |
| 25 | 24     | 0,292    | 0,143    | 0,320    | 0,460    | 0,317    | 0,156    | 0,389    |                |                          |
| 26 | 25     | 0,295    | 0,147    | 0,320    | 0,462    | 0,322    | 0,152    | 0,292    | 499,649023     | -0,977                   |
| 27 | 26     | 0,295461 | 0,147189 | 0,320166 | 0,462386 | 0,321769 | 0,152284 | 0,292034 | 499,650115     | 0,115                    |
| 28 |        |          |          |          |          |          |          |          |                |                          |

# Cavity Tuning



- Model “reliable”

Red: Bead-pulling **measurement** of the frequency shift



Blue: Bead-pulling **simulation** of the frequency shift (scaled  $|\vec{E}|^2$  vs. position)

$$R = \{ 213.65, 210.85, 210.90, 209.85, 210.90, 210.85, 213.65 \} \text{ mm}$$

$$dR = \{ 0.295, 0.147, 0.320, 0.462, 0.322, 0.152, 0.292 \} \text{ mm}$$

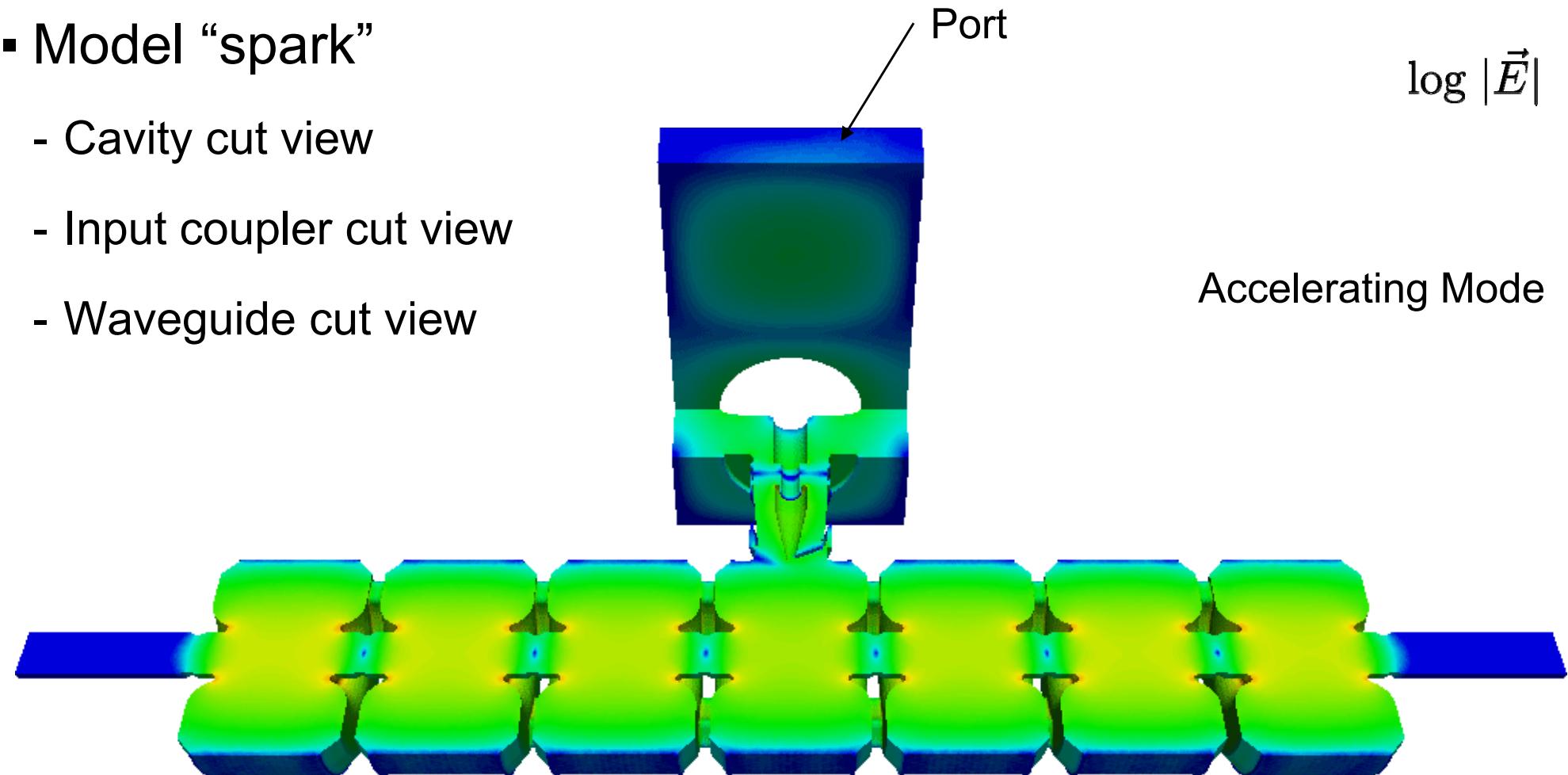
# Cavity Tuning



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- Model “spark”

- Cavity cut view
- Input coupler cut view
- Waveguide cut view



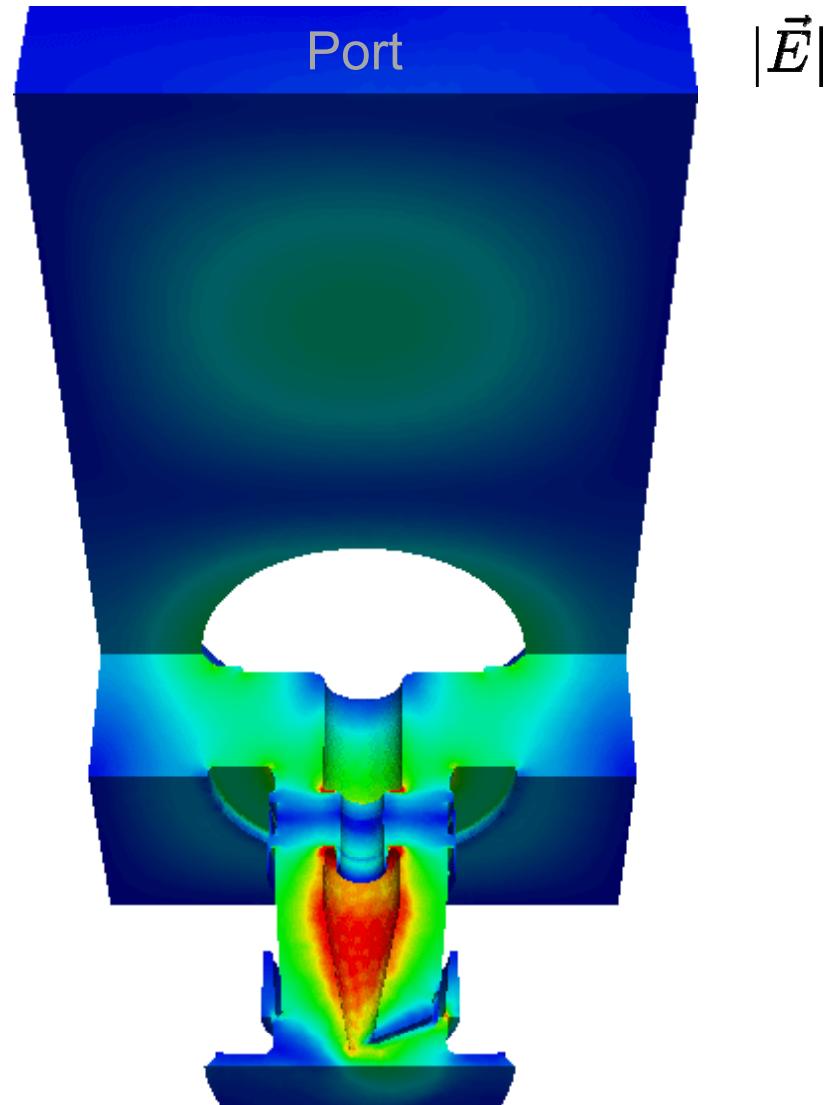
# Cavity Tuning



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- Model “spark”
  - Cavity truncated
  - Input coupler cut view
  - Waveguide cut view

Accelerating Mode



# Outline

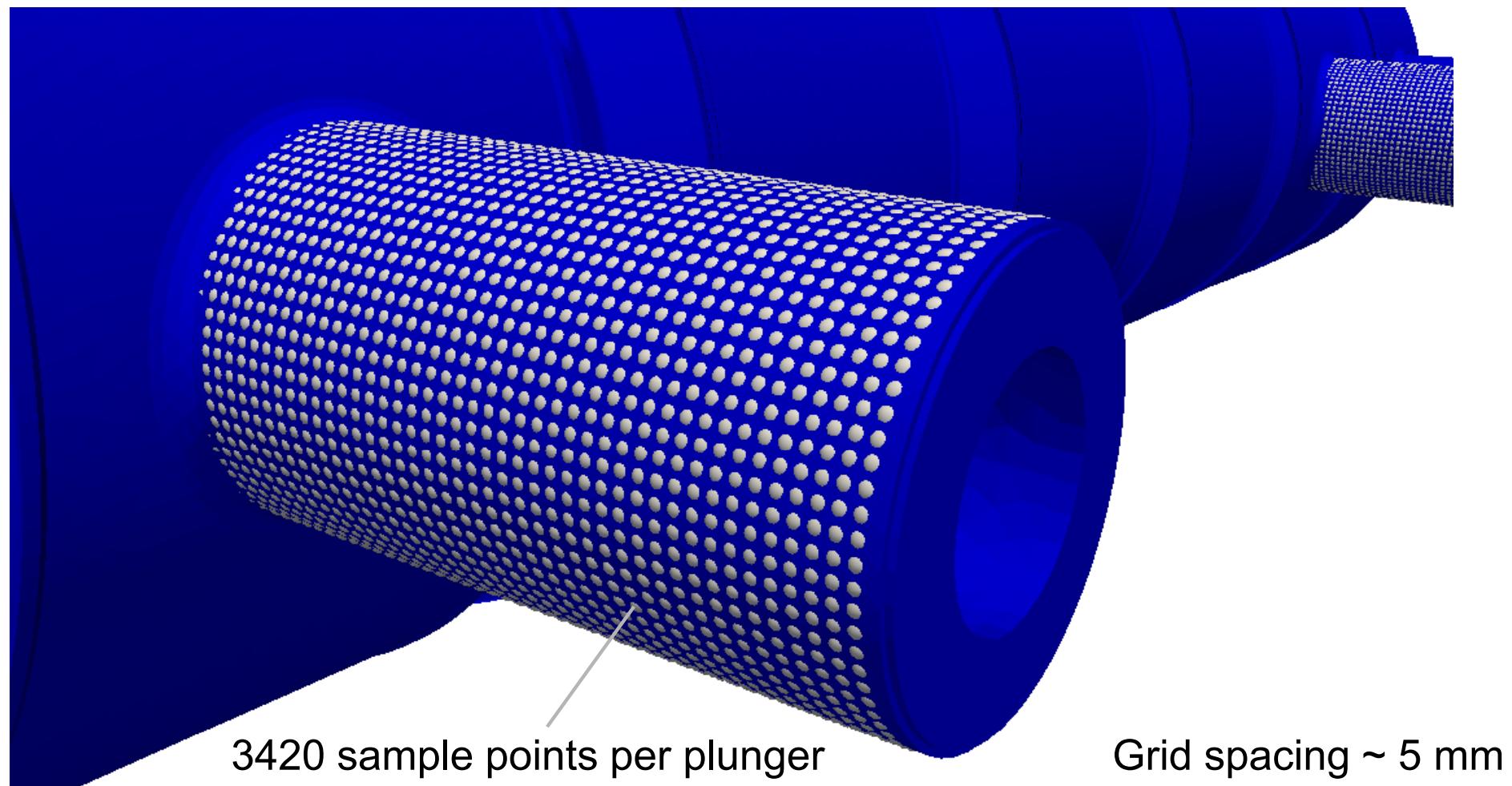


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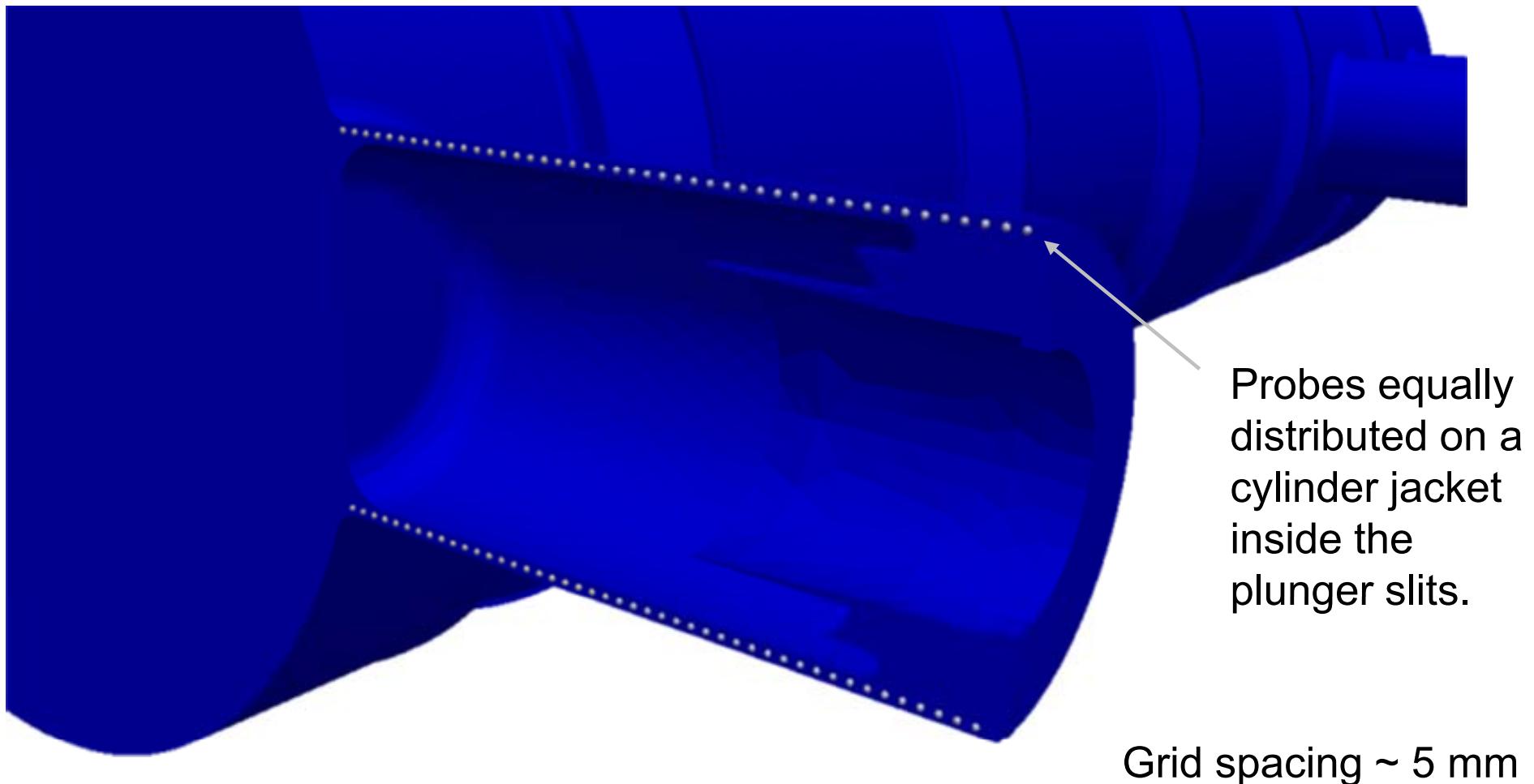
# Simulation Results

- Probe Locations for Maximum Field Determination



# Simulation Results

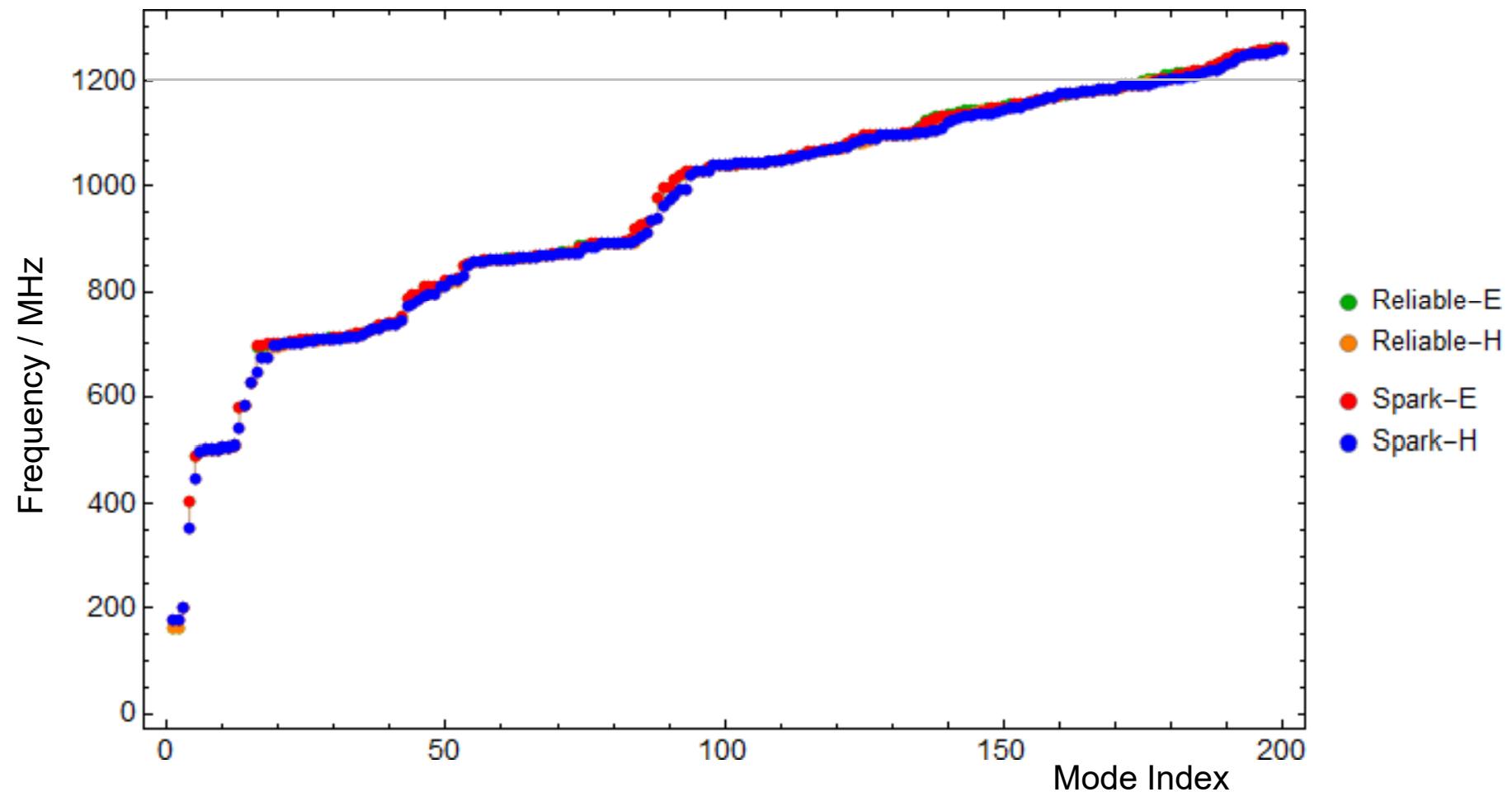
- Probe Locations for Maximum Field Determination



# Simulation Results



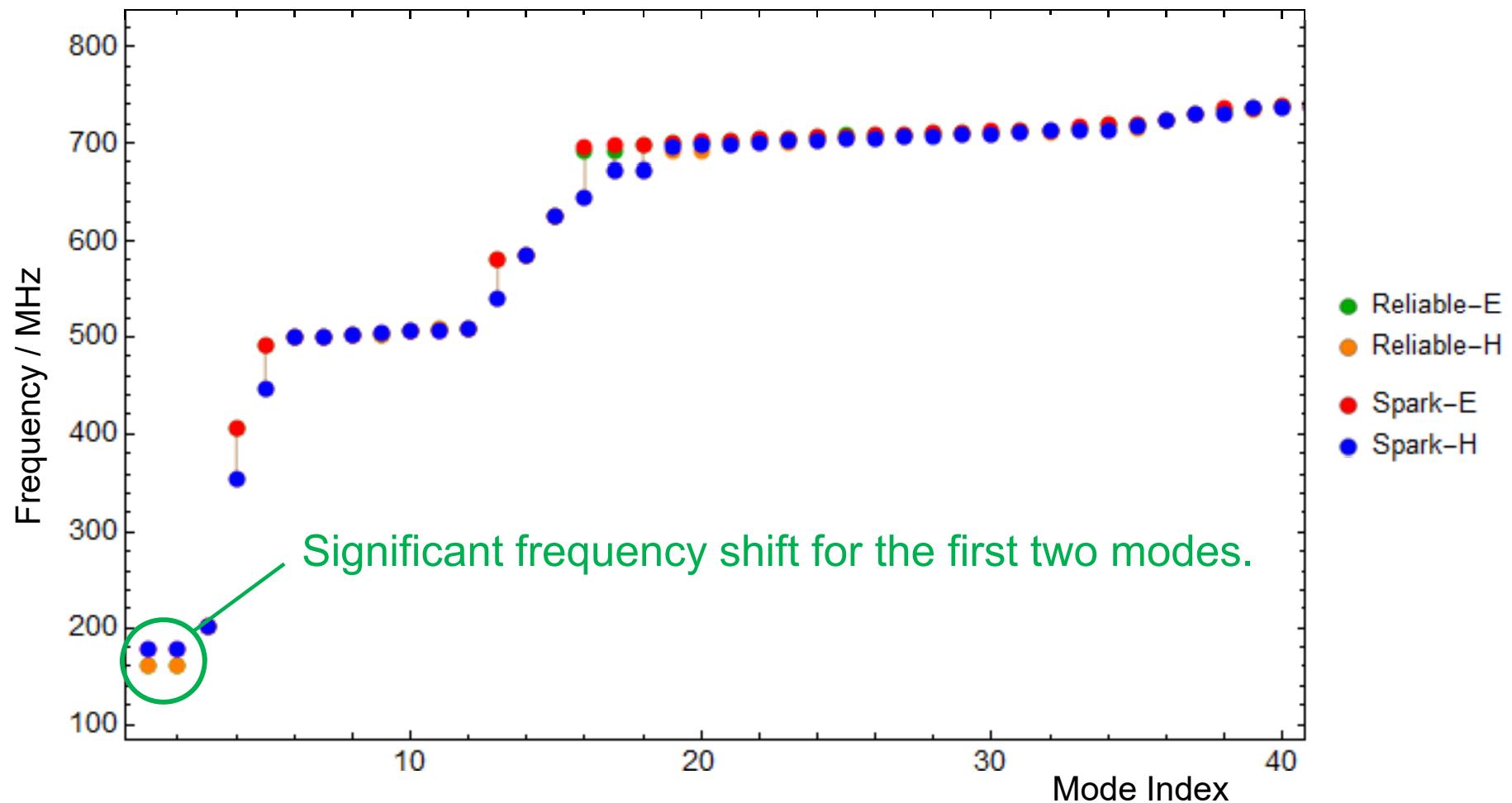
- Resonance Frequency (all calculated modes)



# Simulation Results



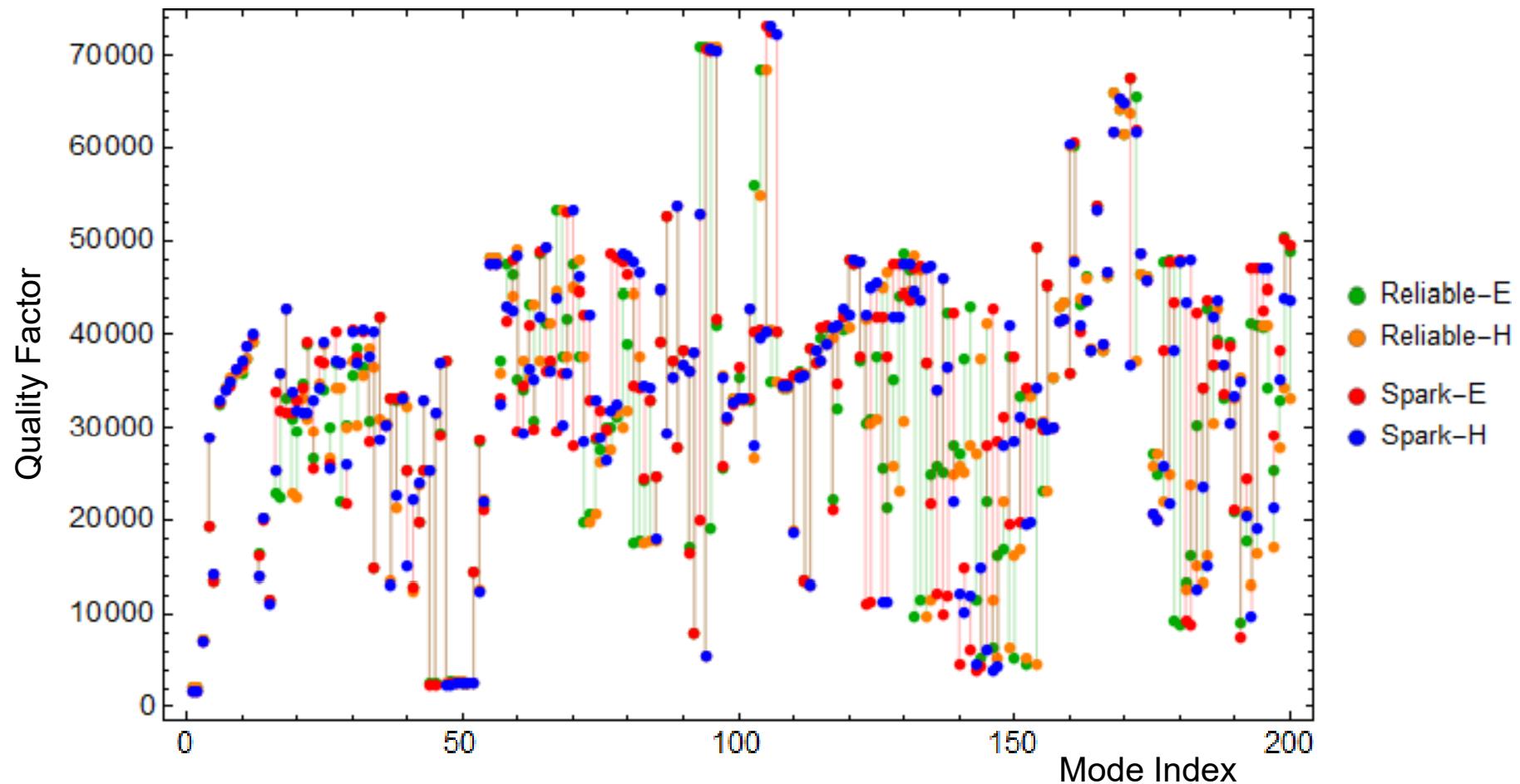
- Resonance Frequency (first forty modes)



# Simulation Results



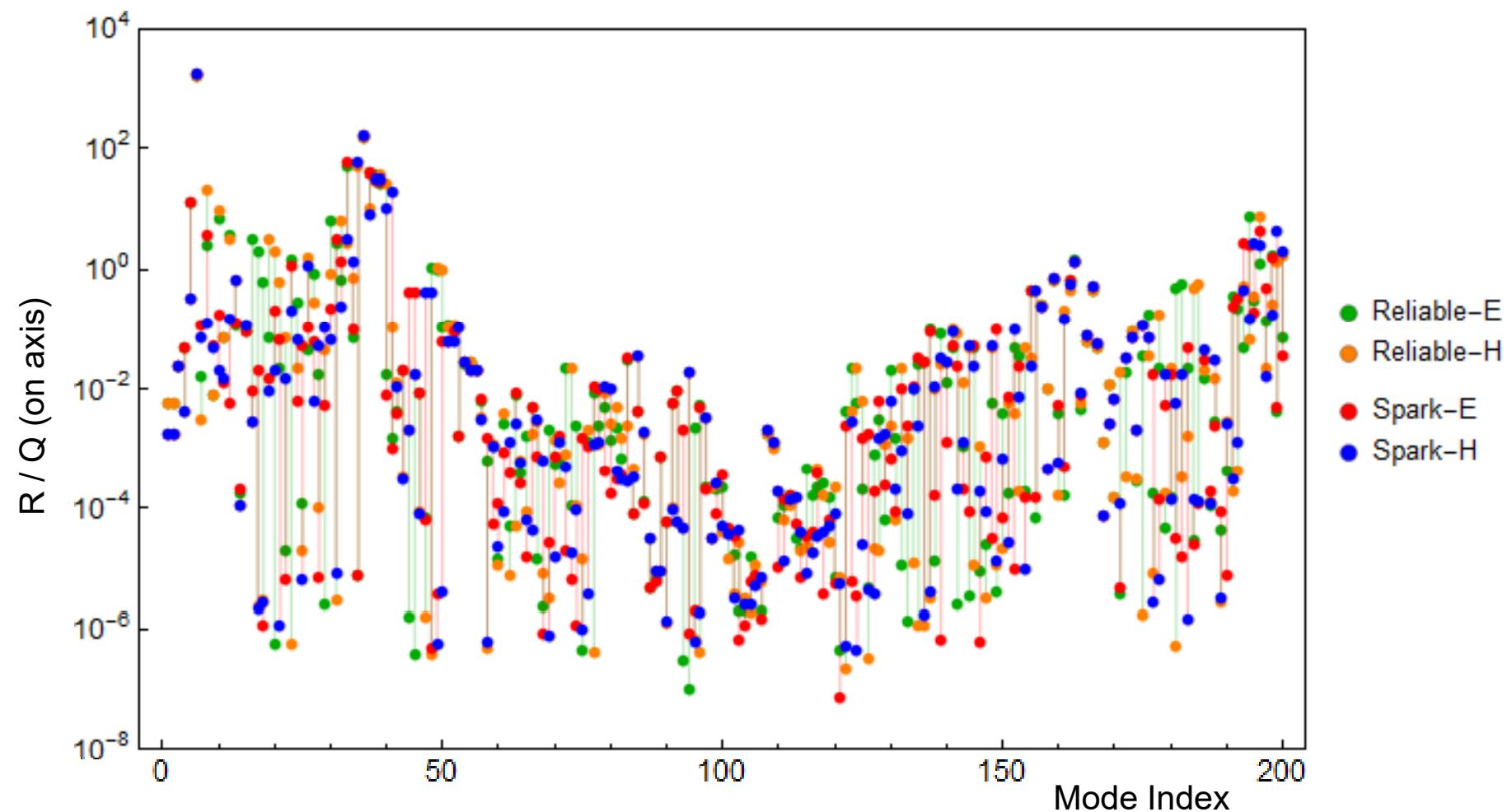
- Quality Factor (all calculated modes)



# Simulation Results



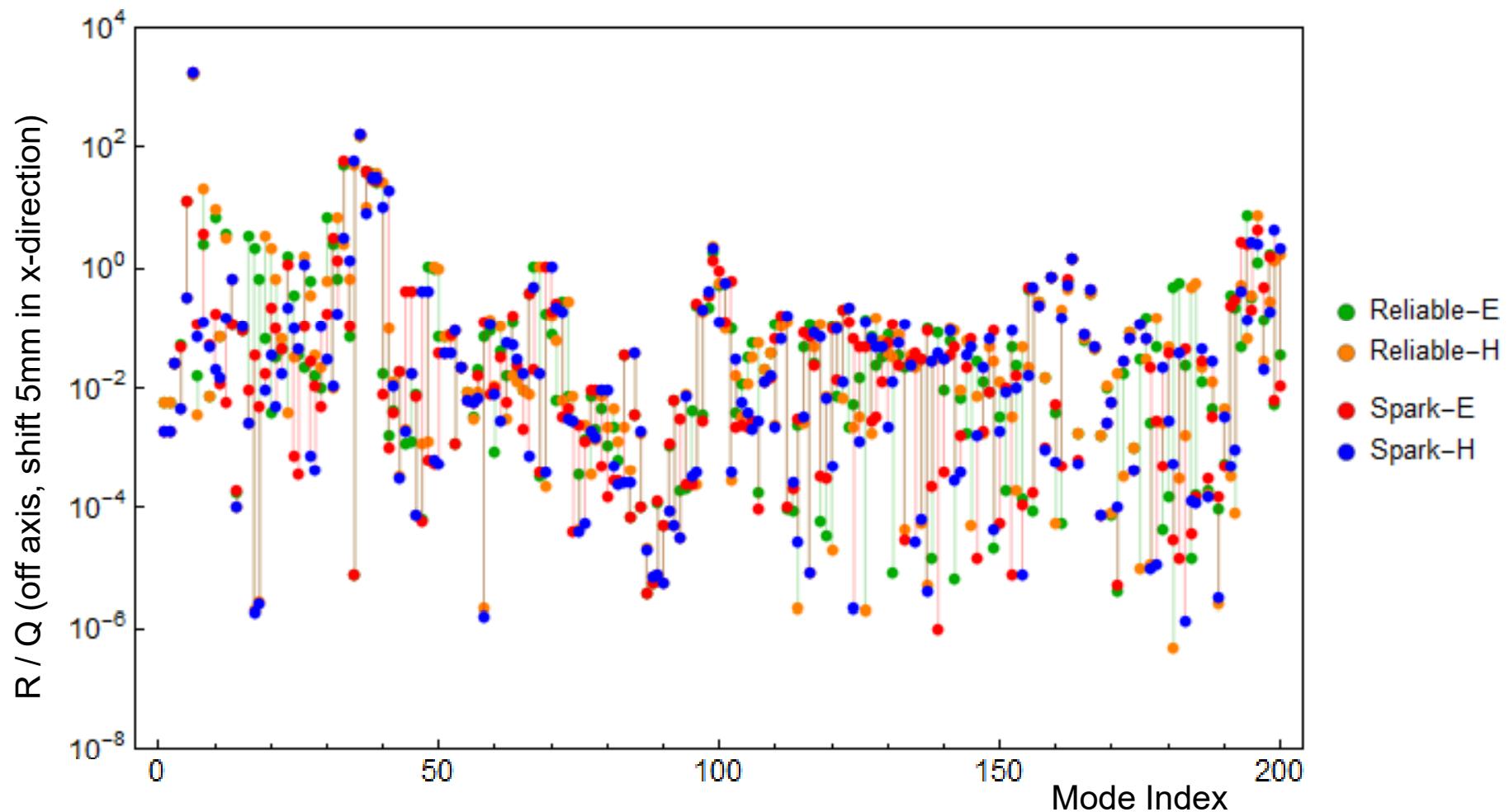
- On Axis R / Q (all calculated modes)



# Simulation Results

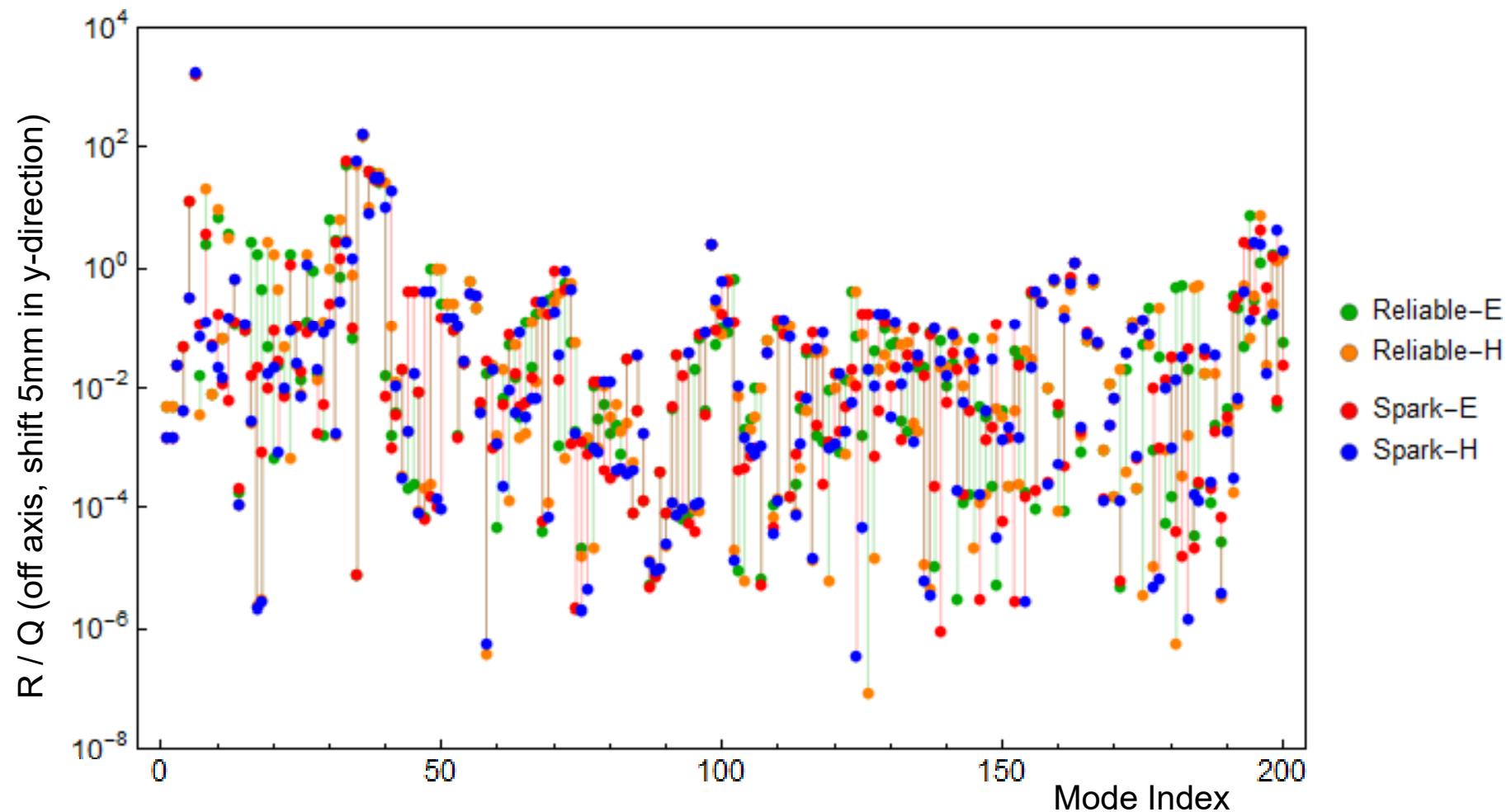


- Off Axis R / Q (all calculated modes)



# Simulation Results

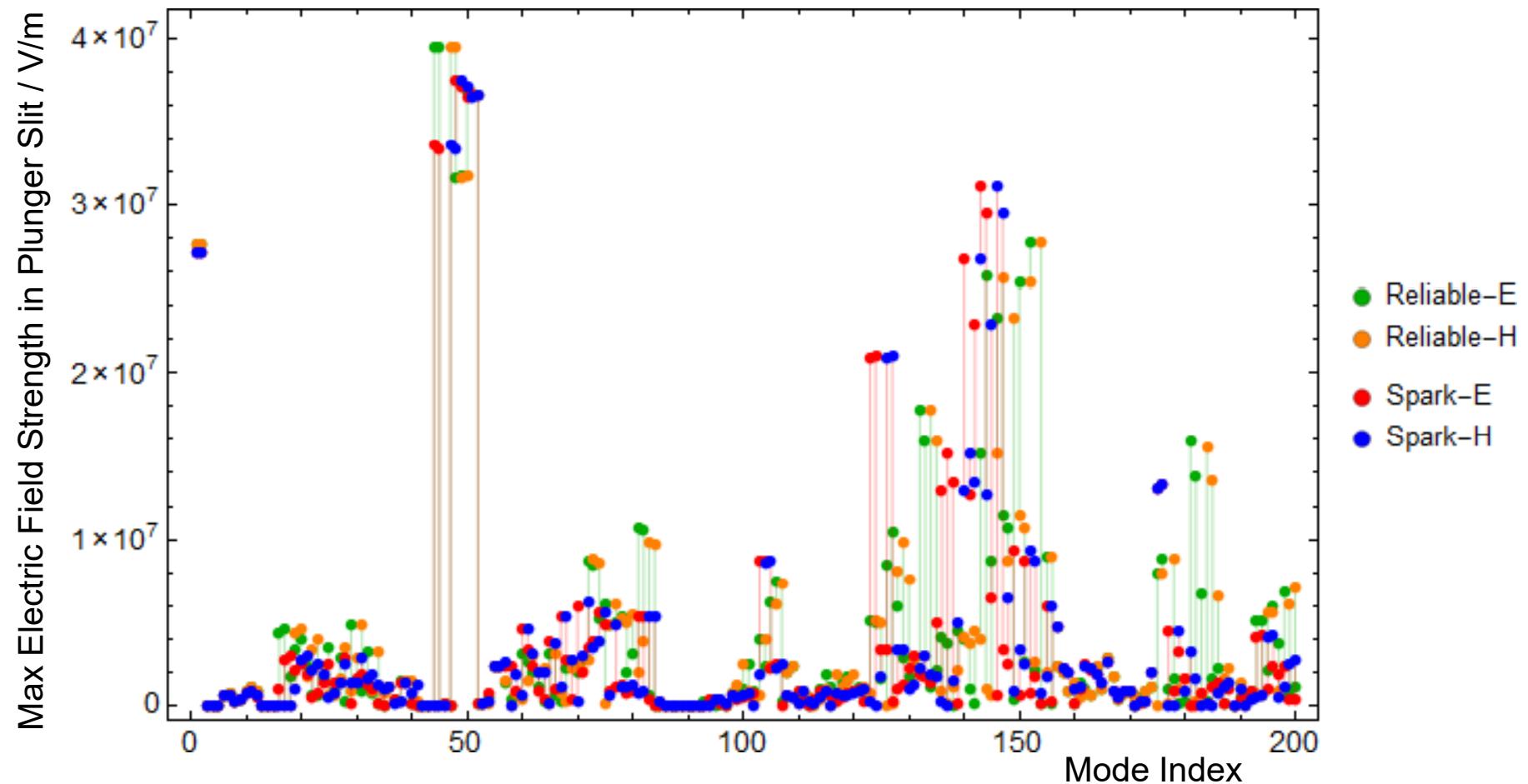
- Off Axis R / Q (all calculated modes)



# Simulation Results



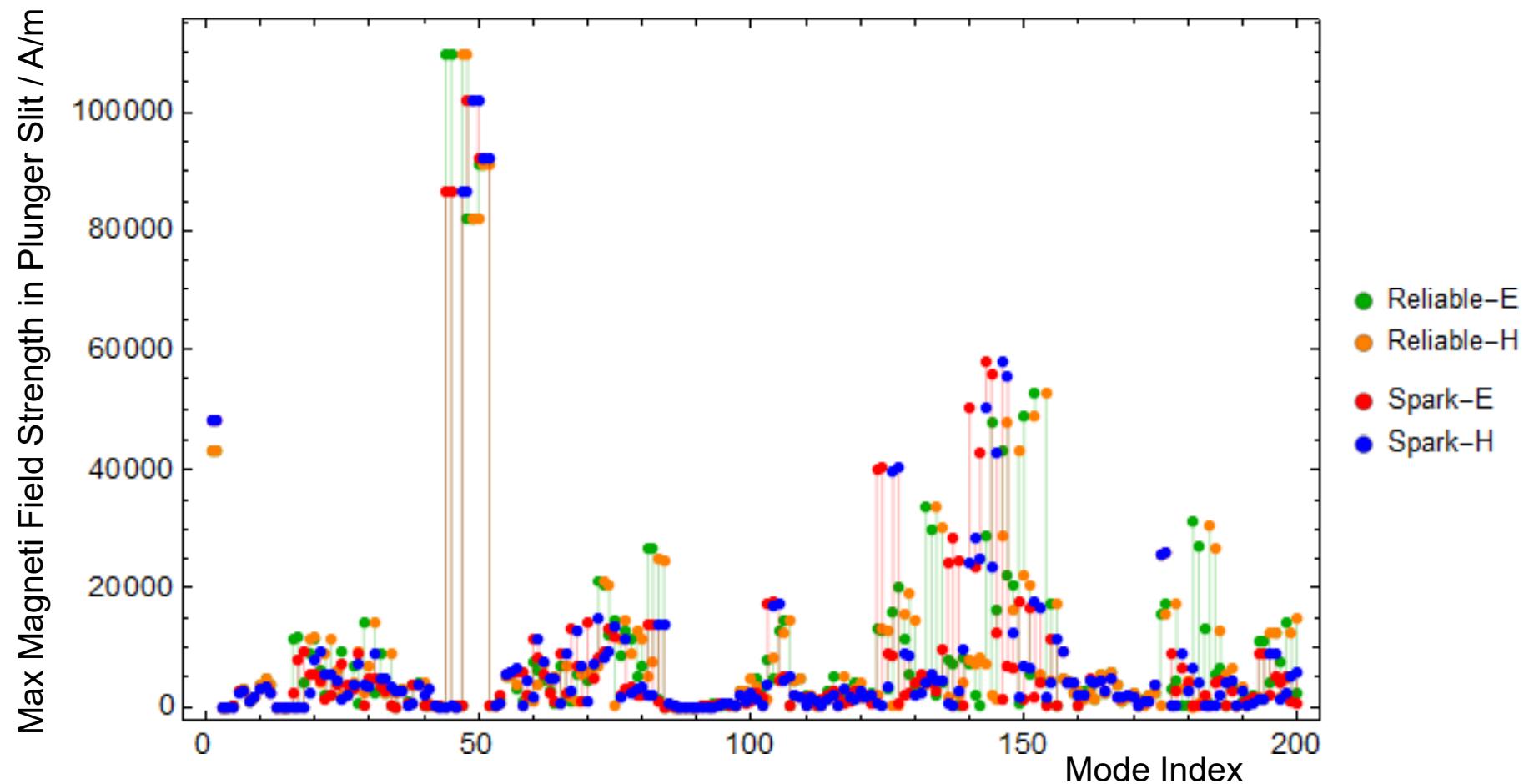
- Maximum Field Values in the Plunger Slits (all modes)



# Simulation Results



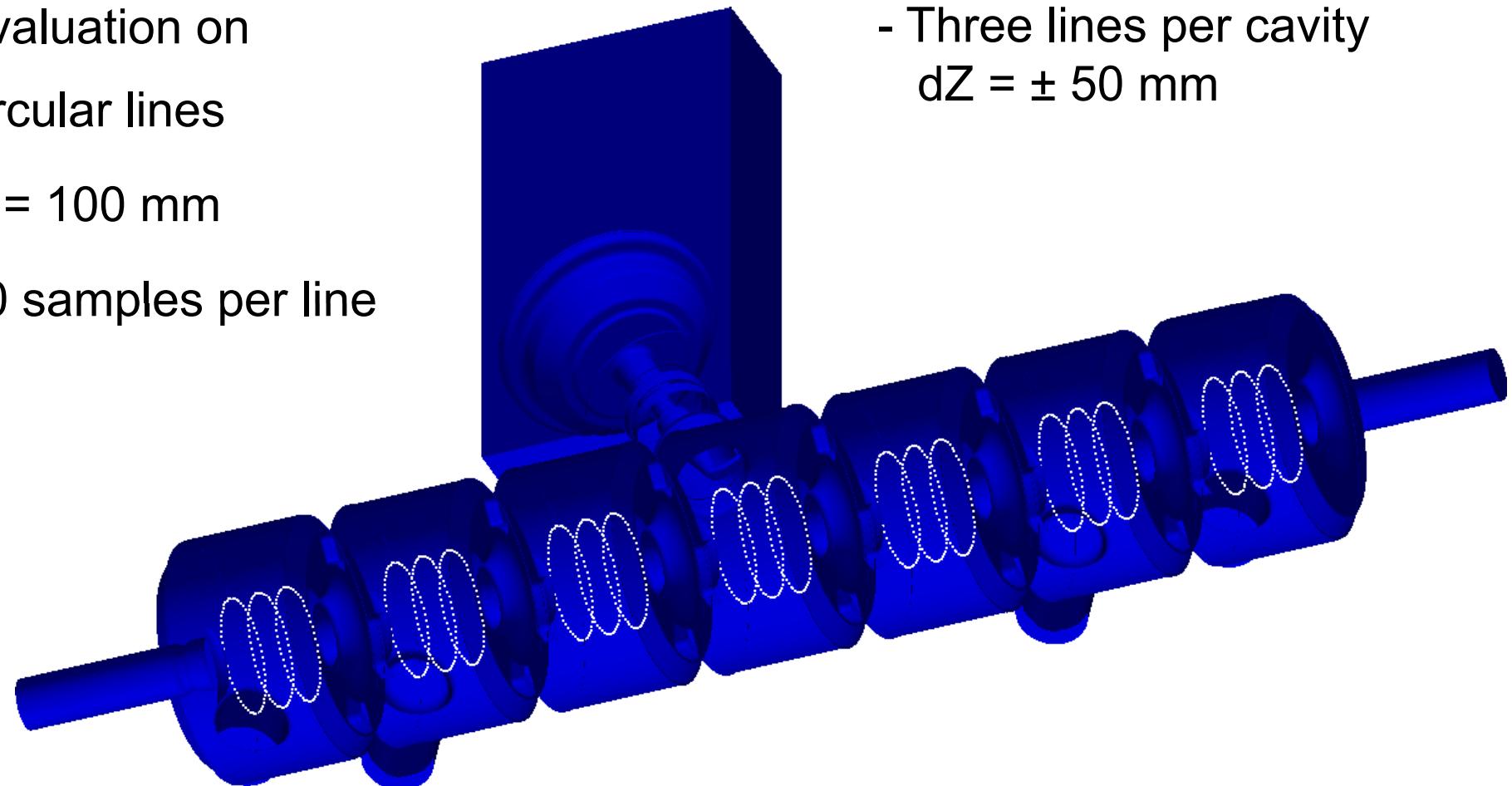
- Maximum Field Values in the Plunger Slits (all modes)



# Simulation Results

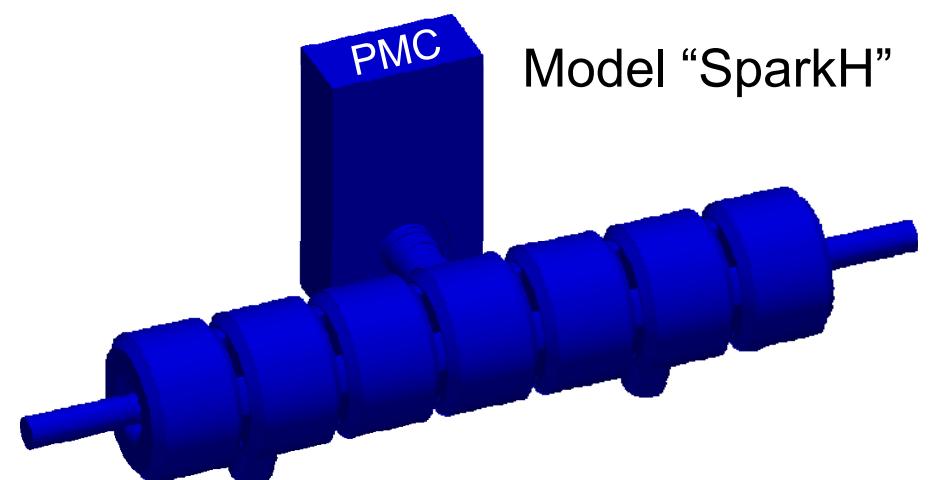
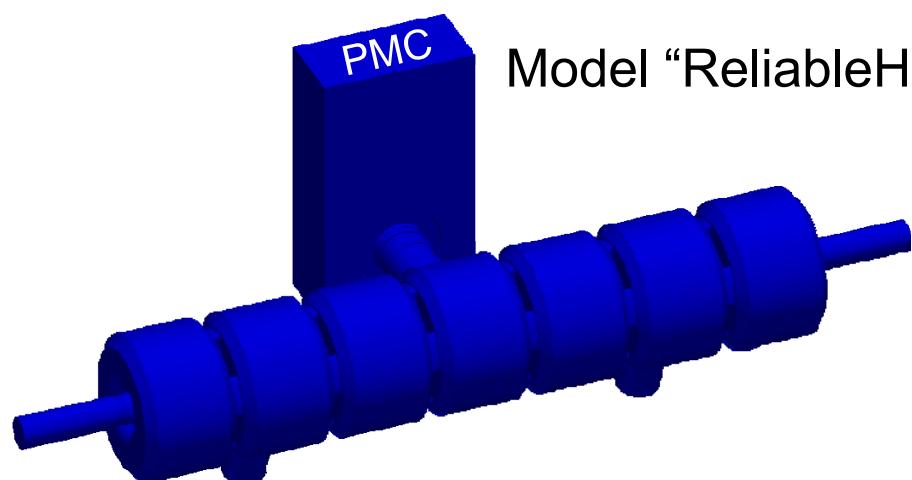
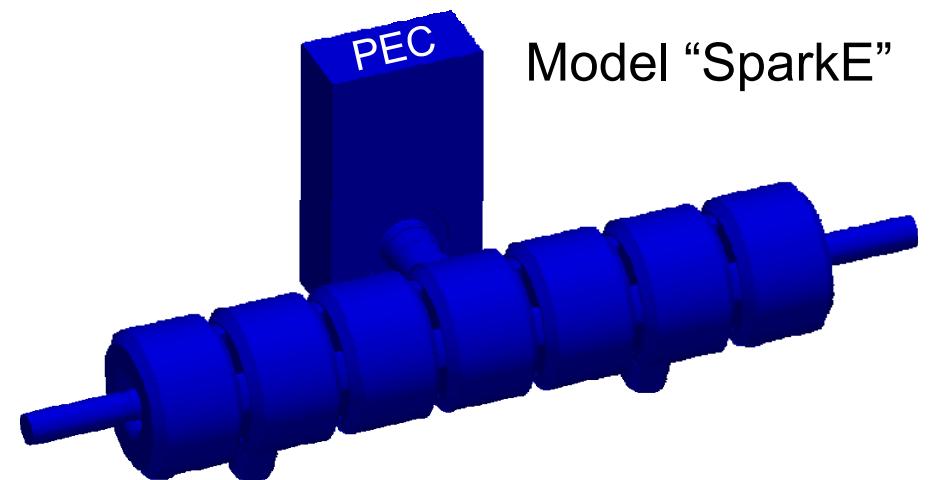
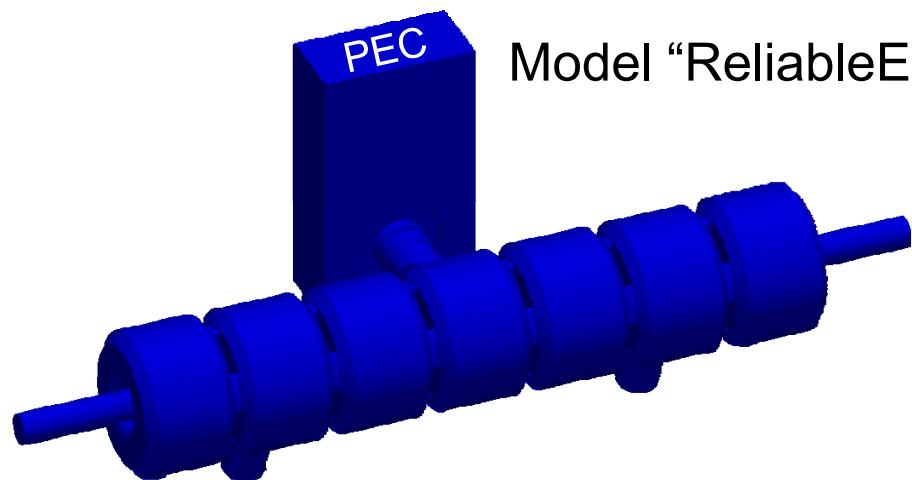
- Field Classification and Mode Correlation

- Evaluation on circular lines
- $R = 100 \text{ mm}$
- 60 samples per line



# Simulation Results

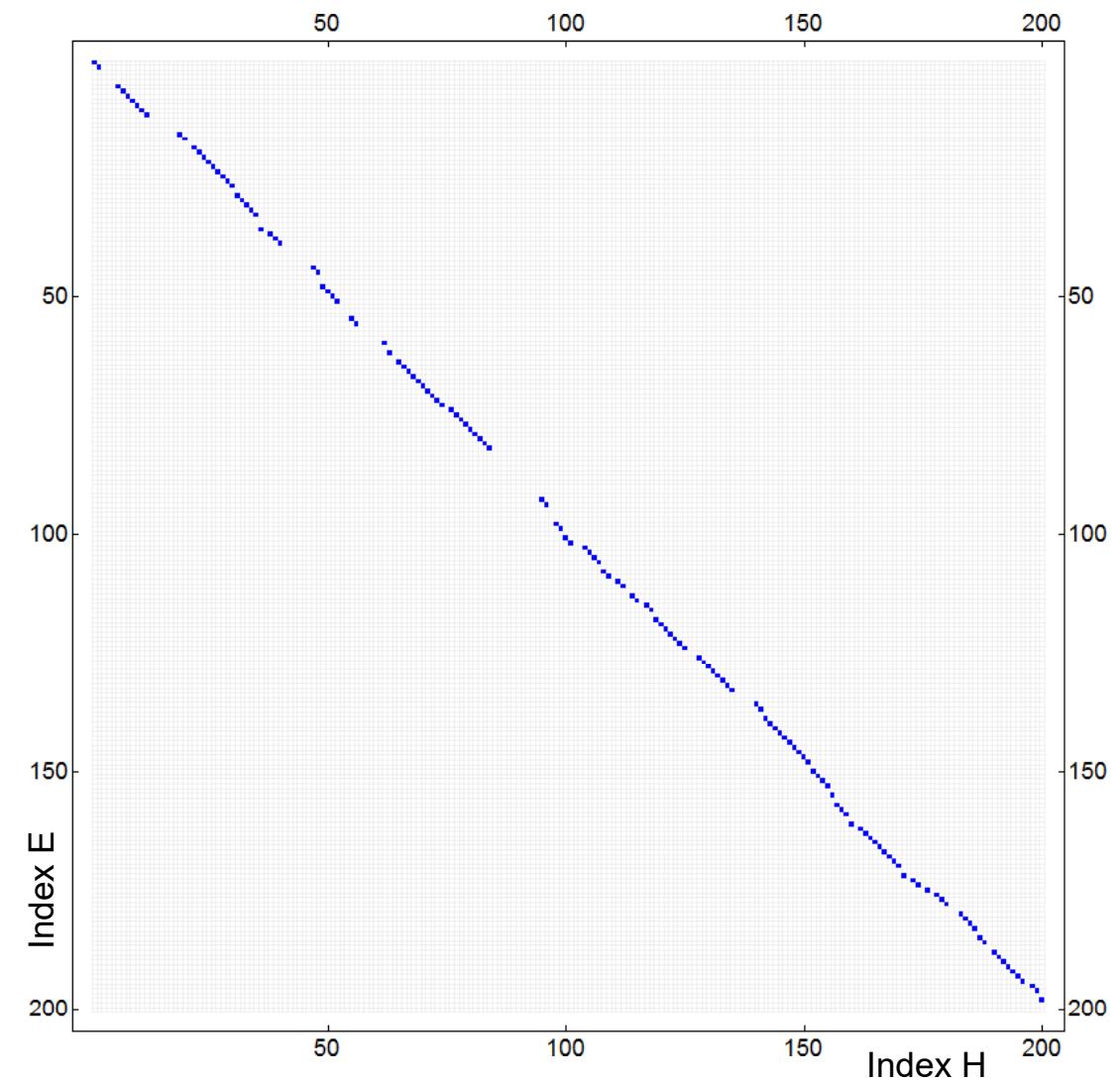
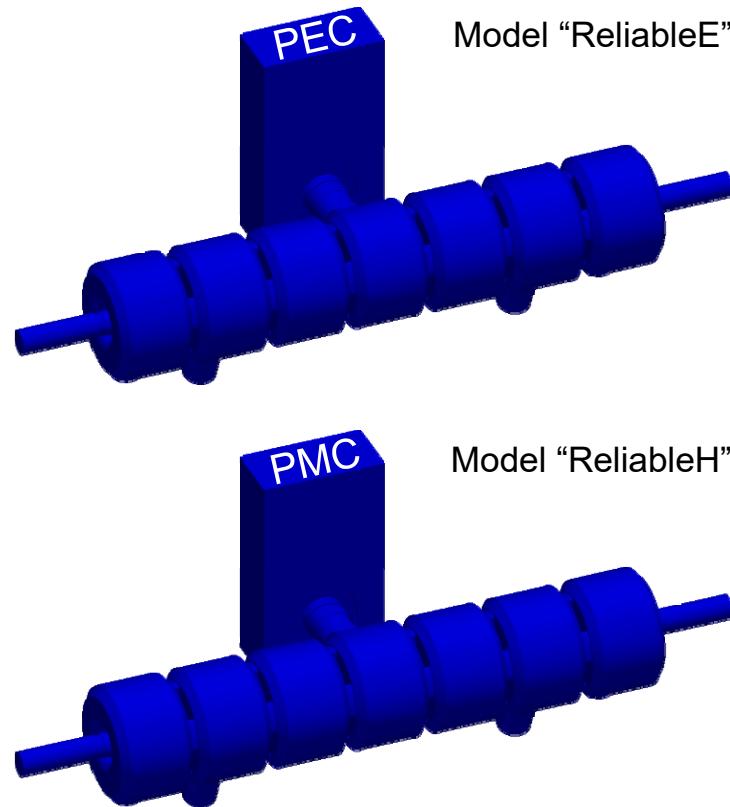
- Field Classification and Mode Correlation



# Simulation Results



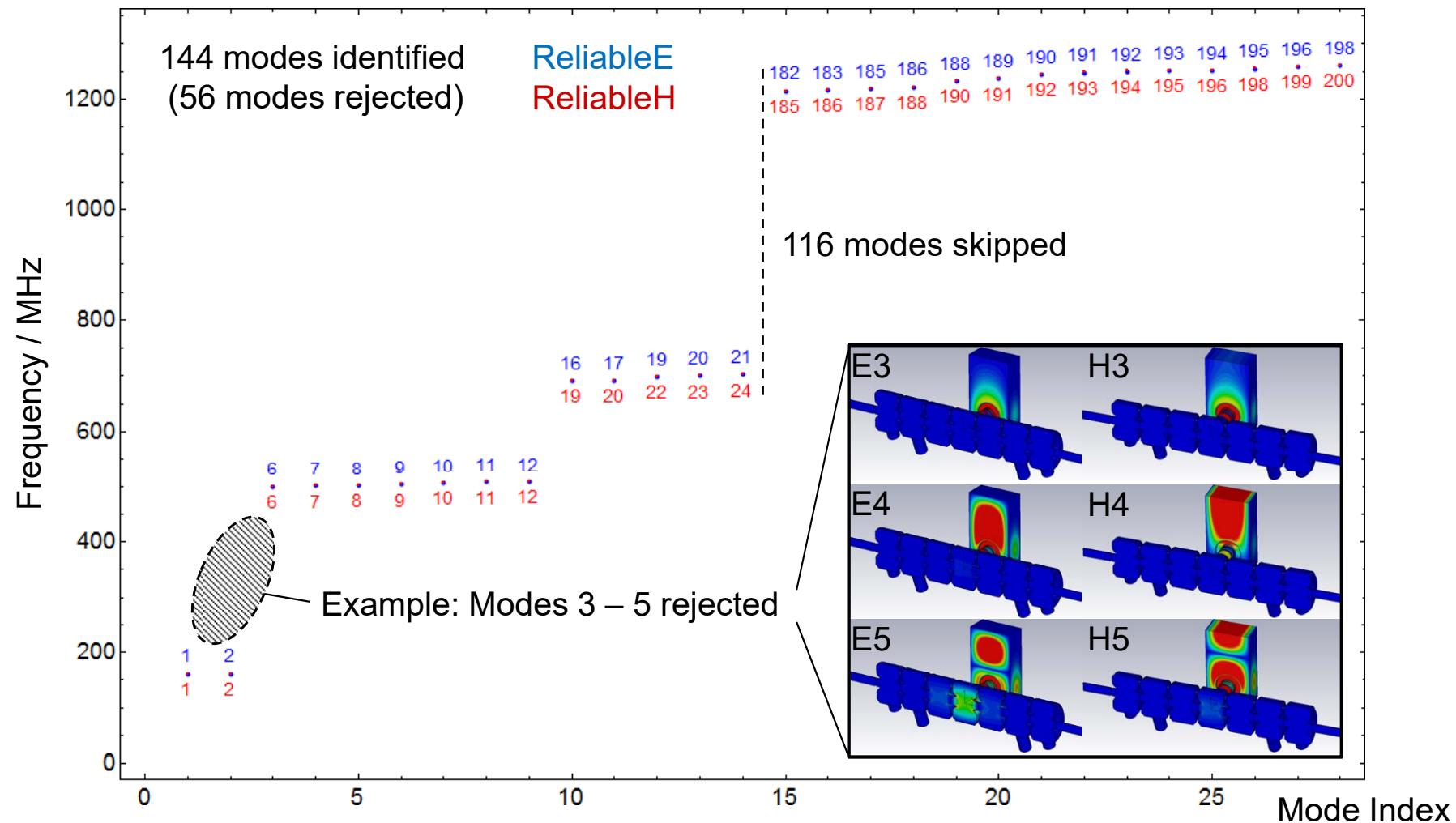
- Mode Correlation
  - Model “reliable”



# Simulation Results



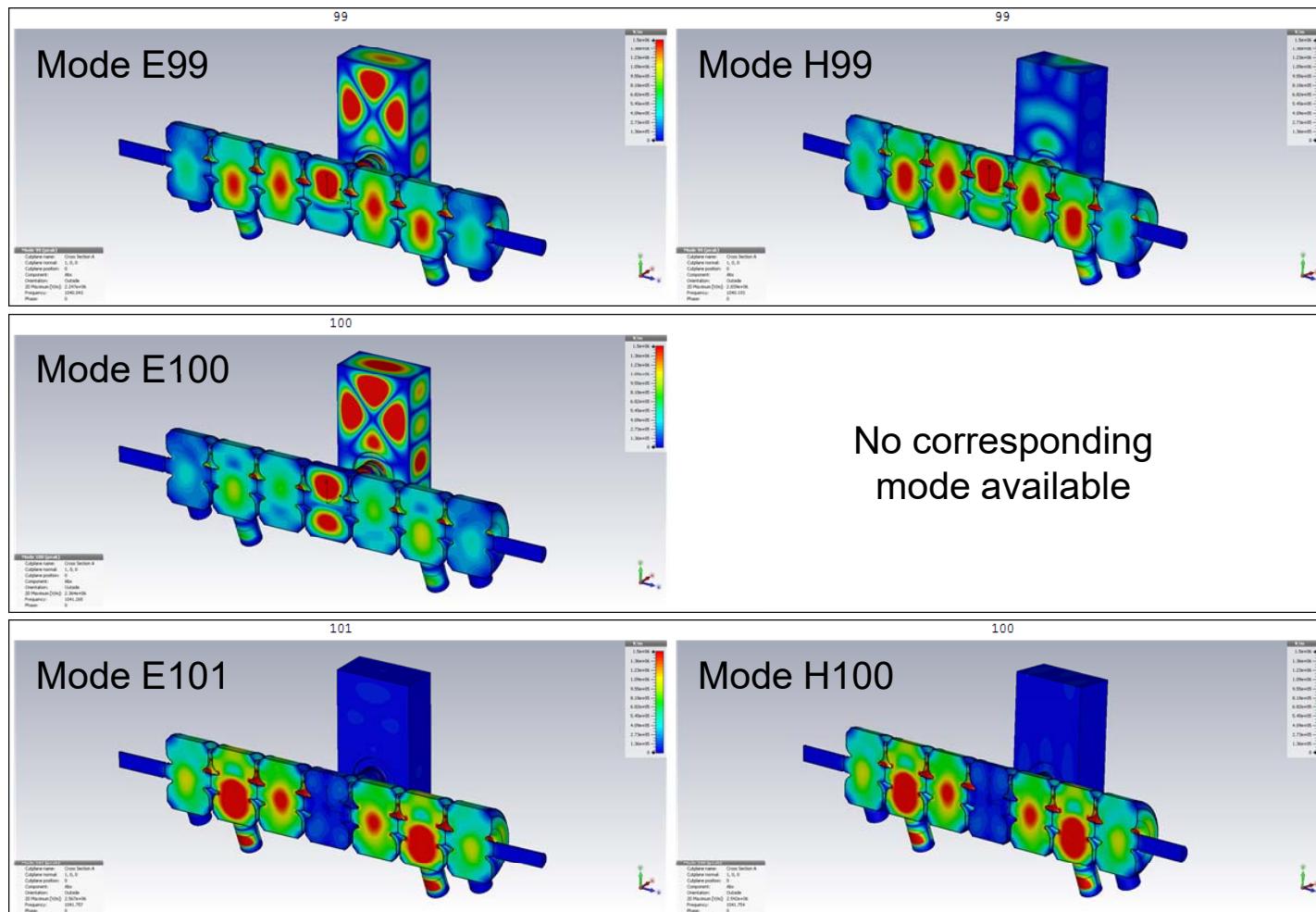
## ▪ Mode Correlation



# Simulation Results



## ▪ Mode Correlation

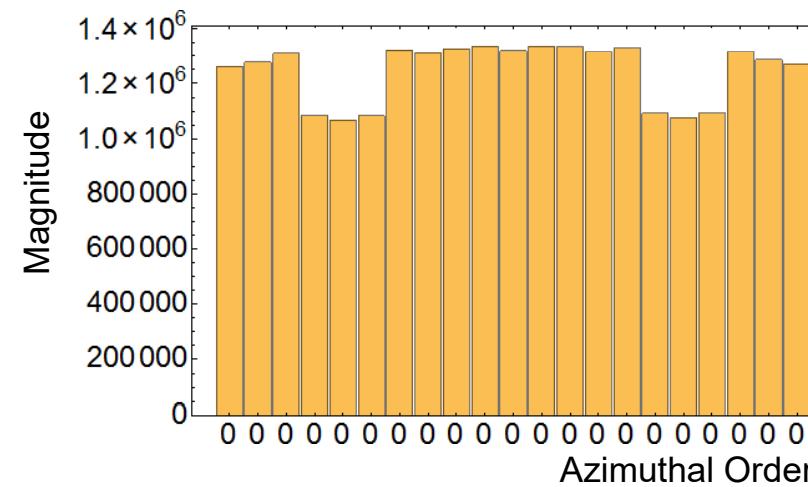
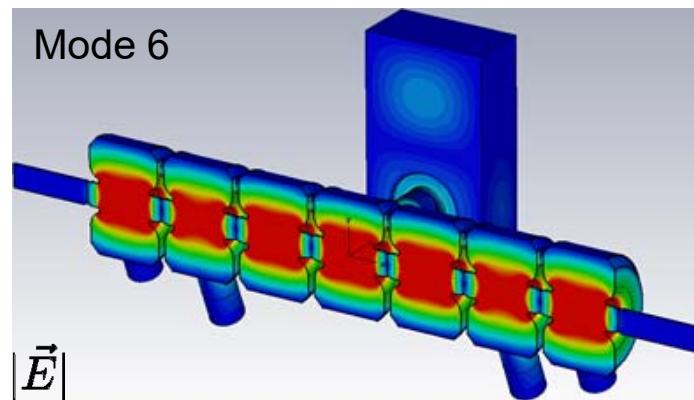


# Simulation Results

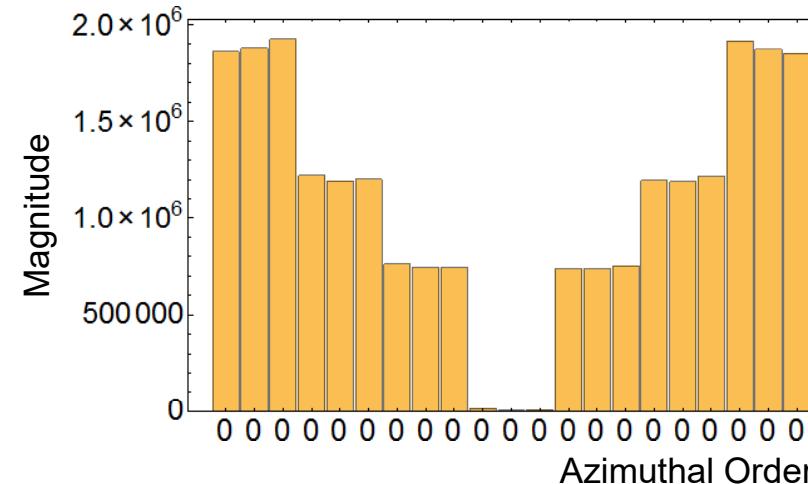
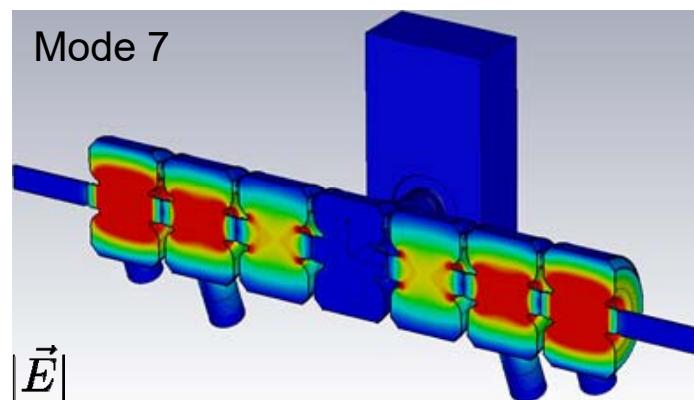


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## ▪ Field Classification



Monopole



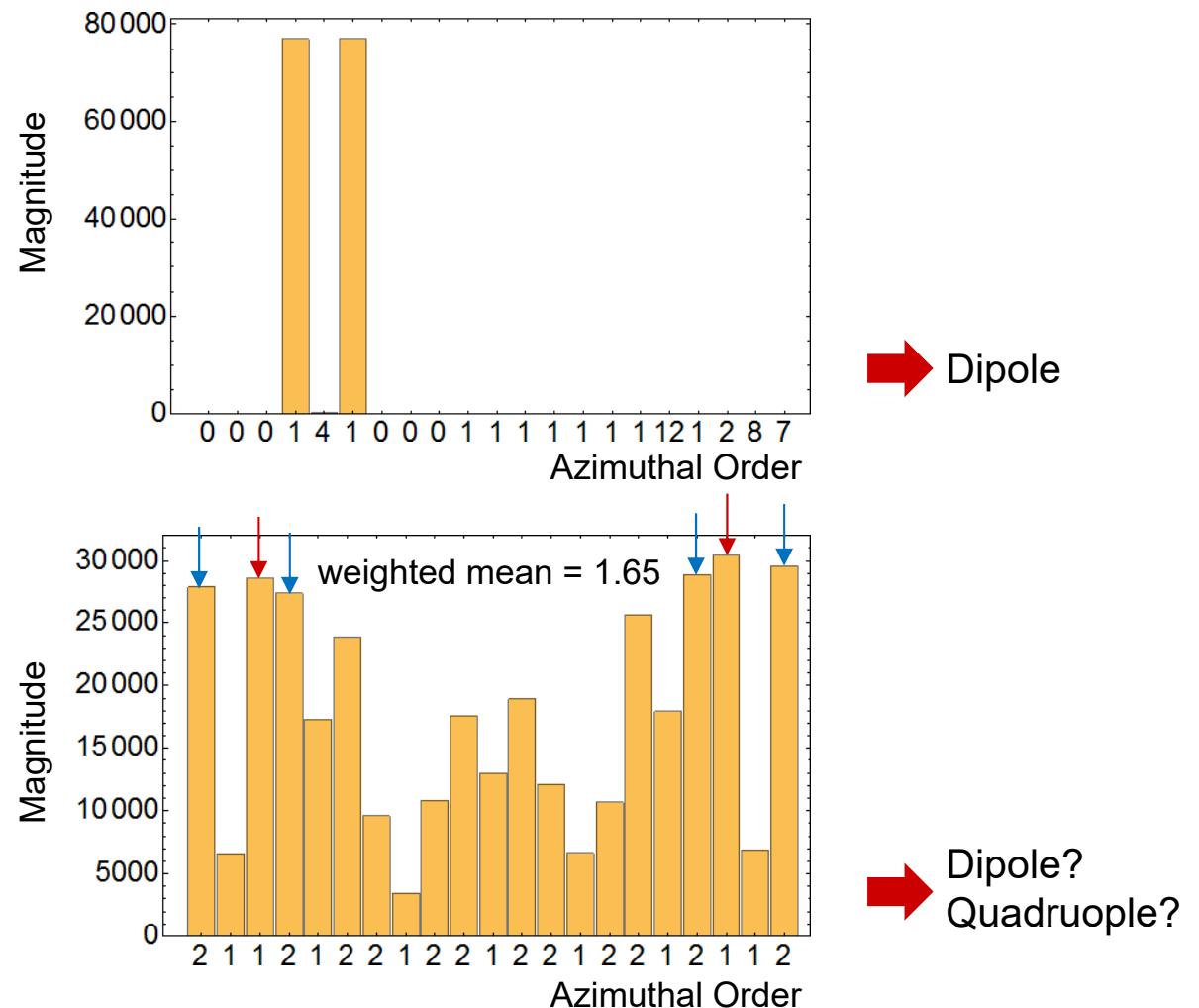
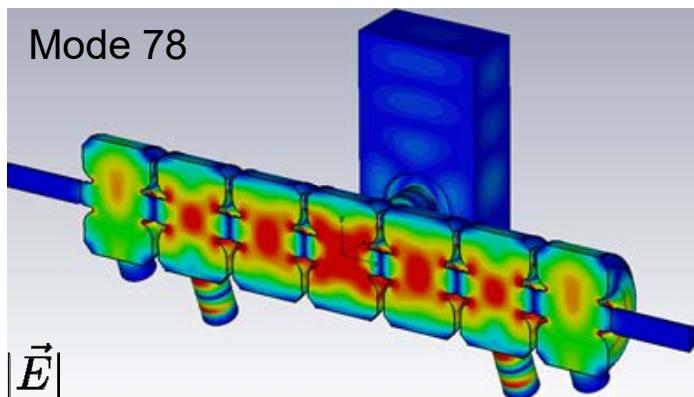
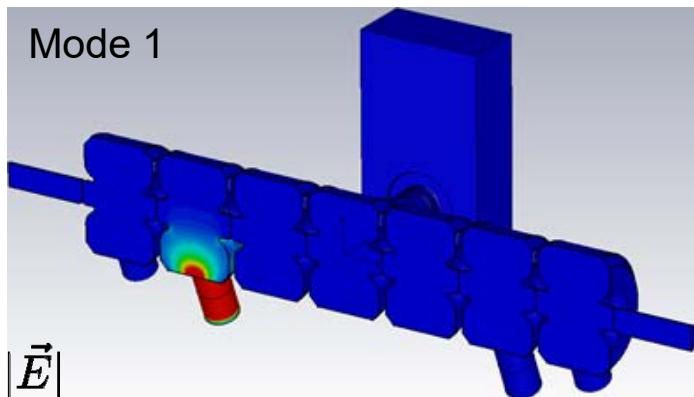
Monopole

# Simulation Results



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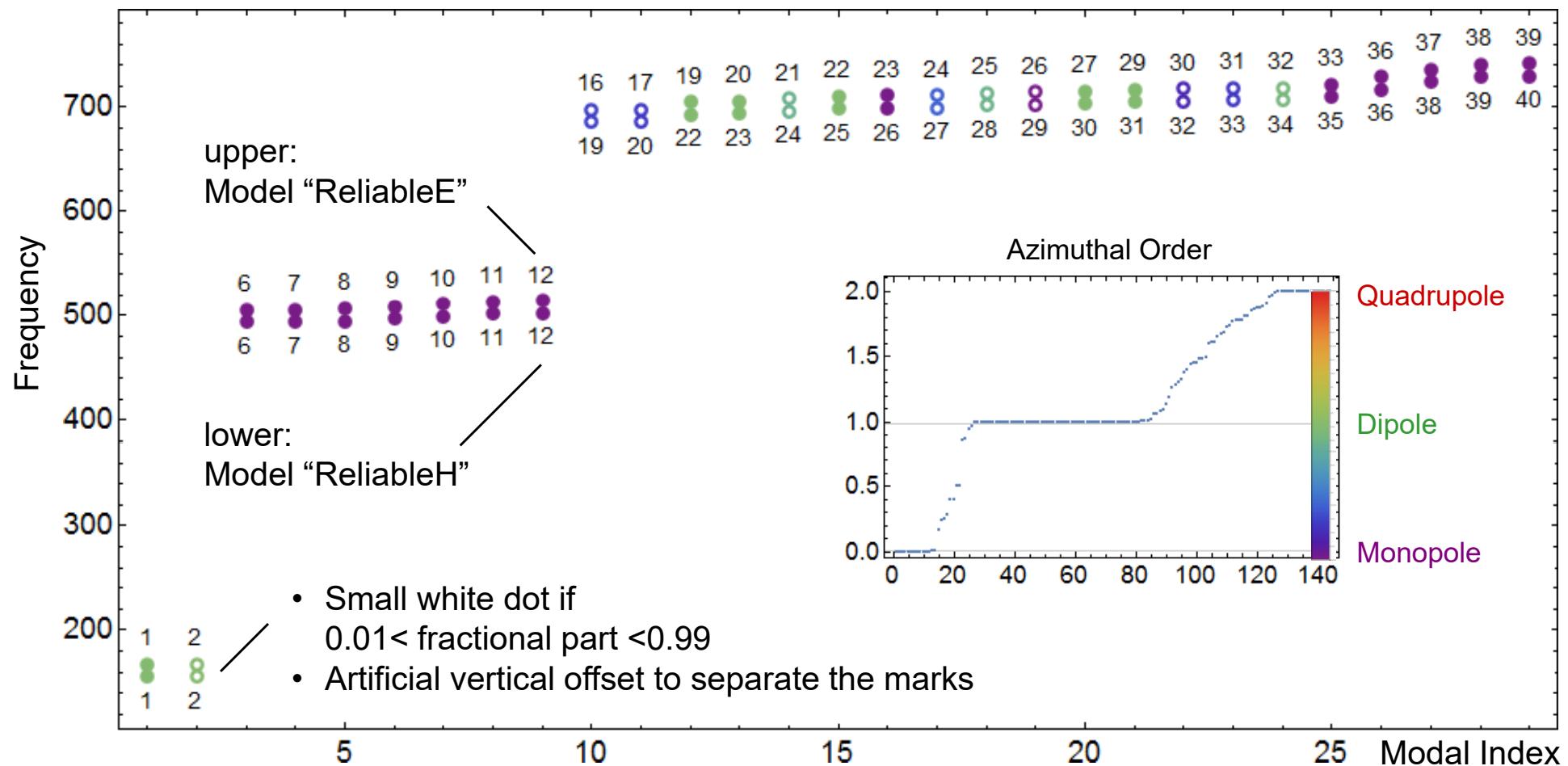
## ▪ Field Classification



# Simulation Results



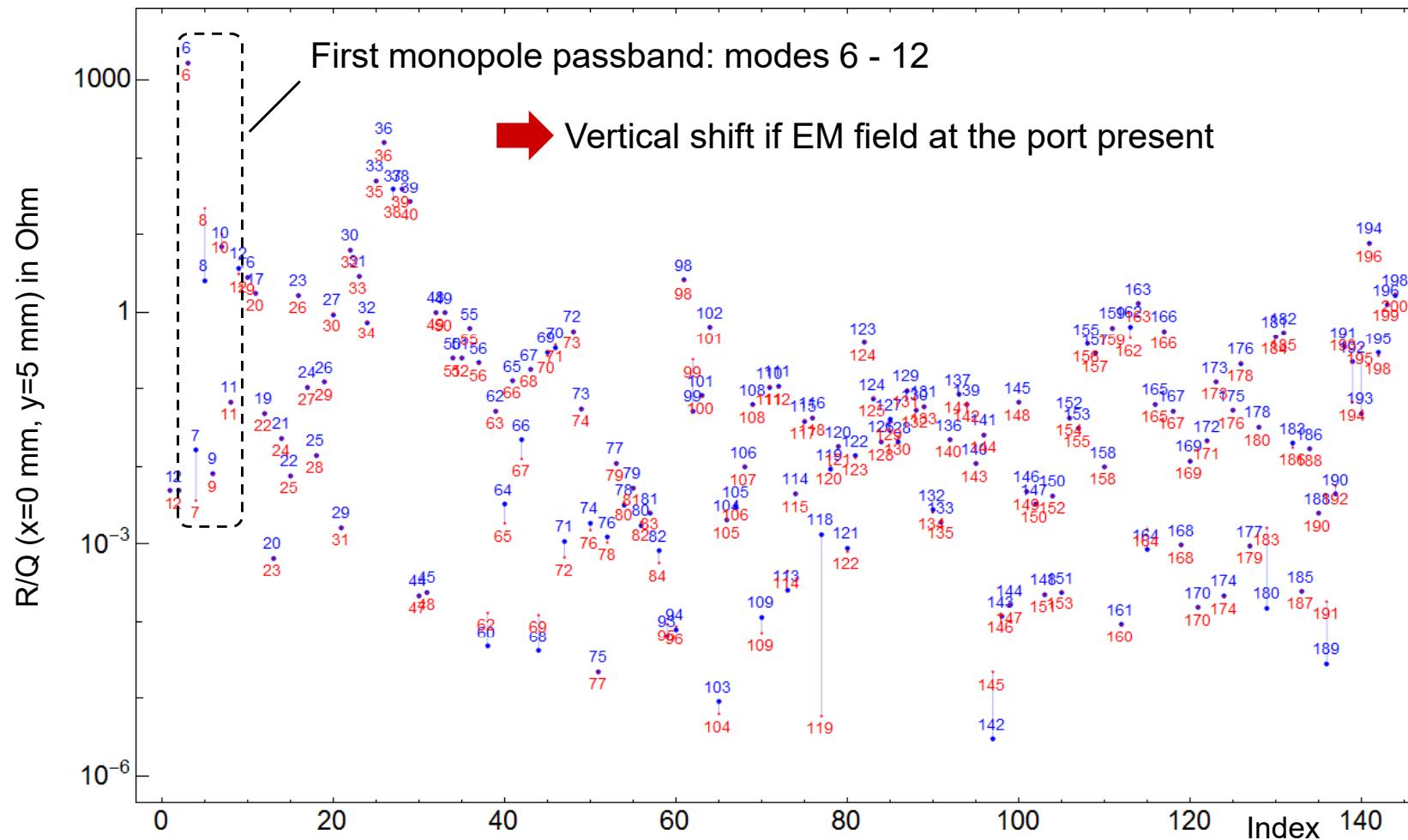
## ▪ Field Classification



# Simulation Results



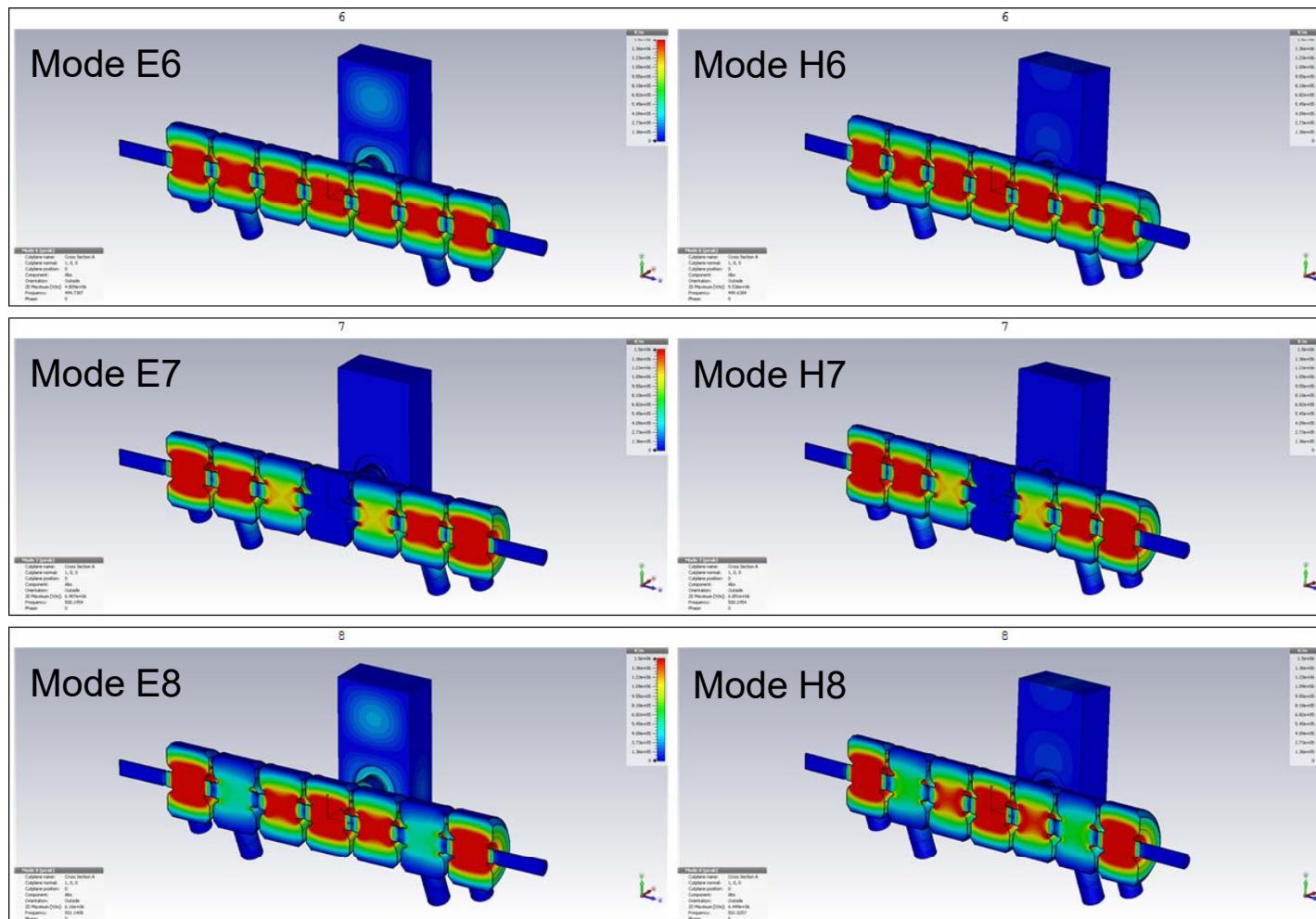
- Mode Correlation (“reliable E, reliable H”)



# Simulation Results

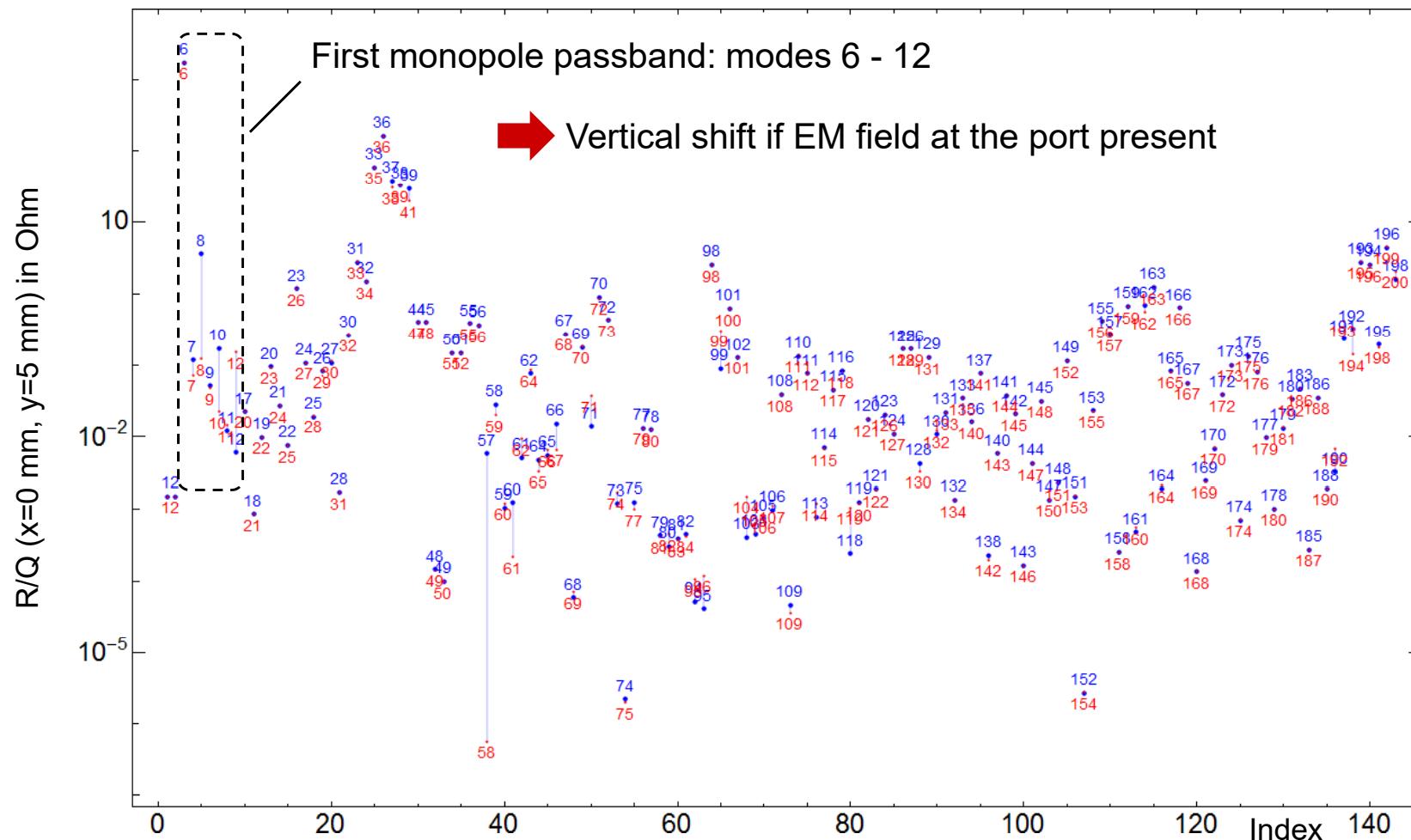


- Mode Correlation (“reliable E, reliable H”)



# Simulation Results

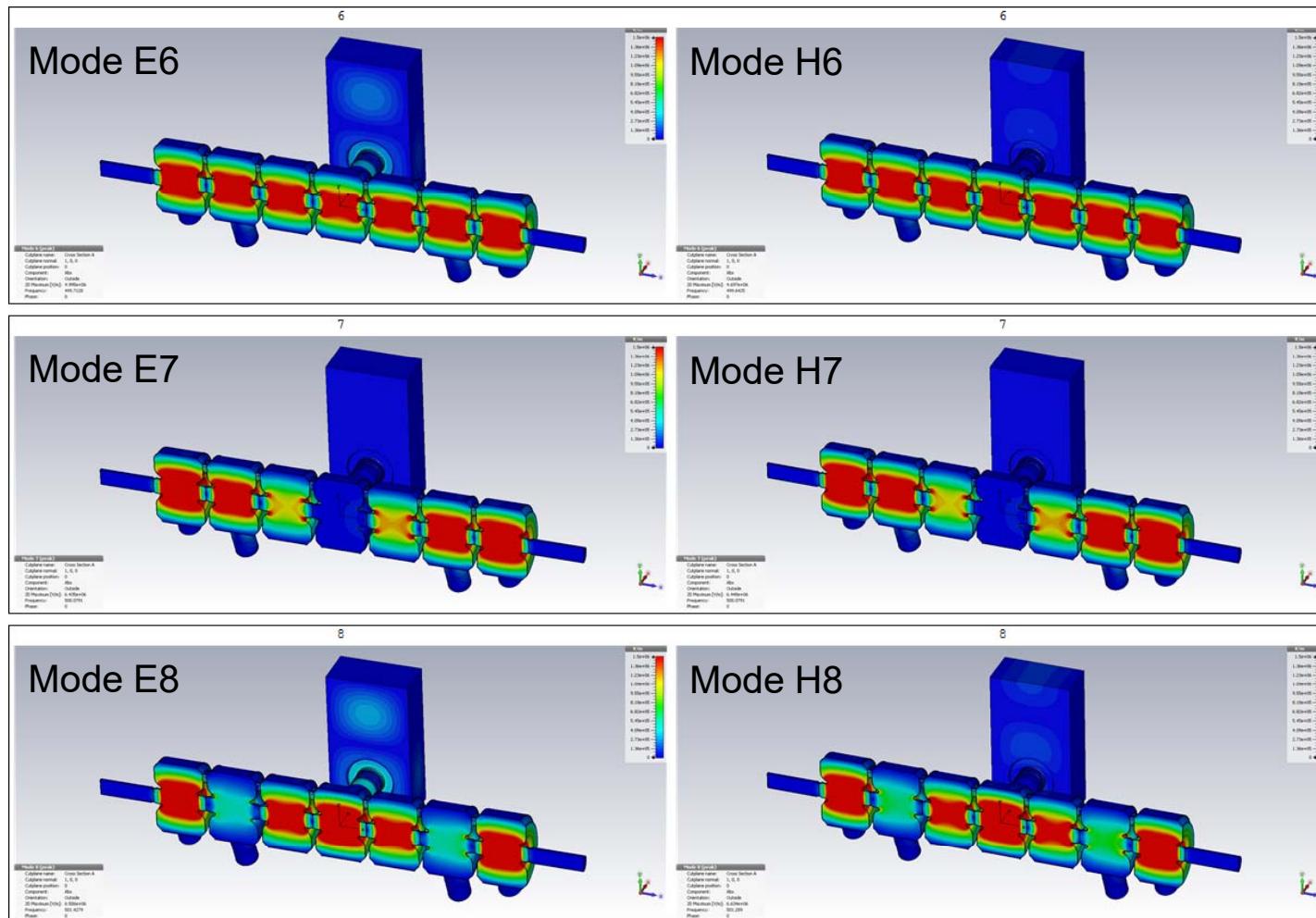
- Mode Correlation (“spark E, spark H”)



# Simulation Results

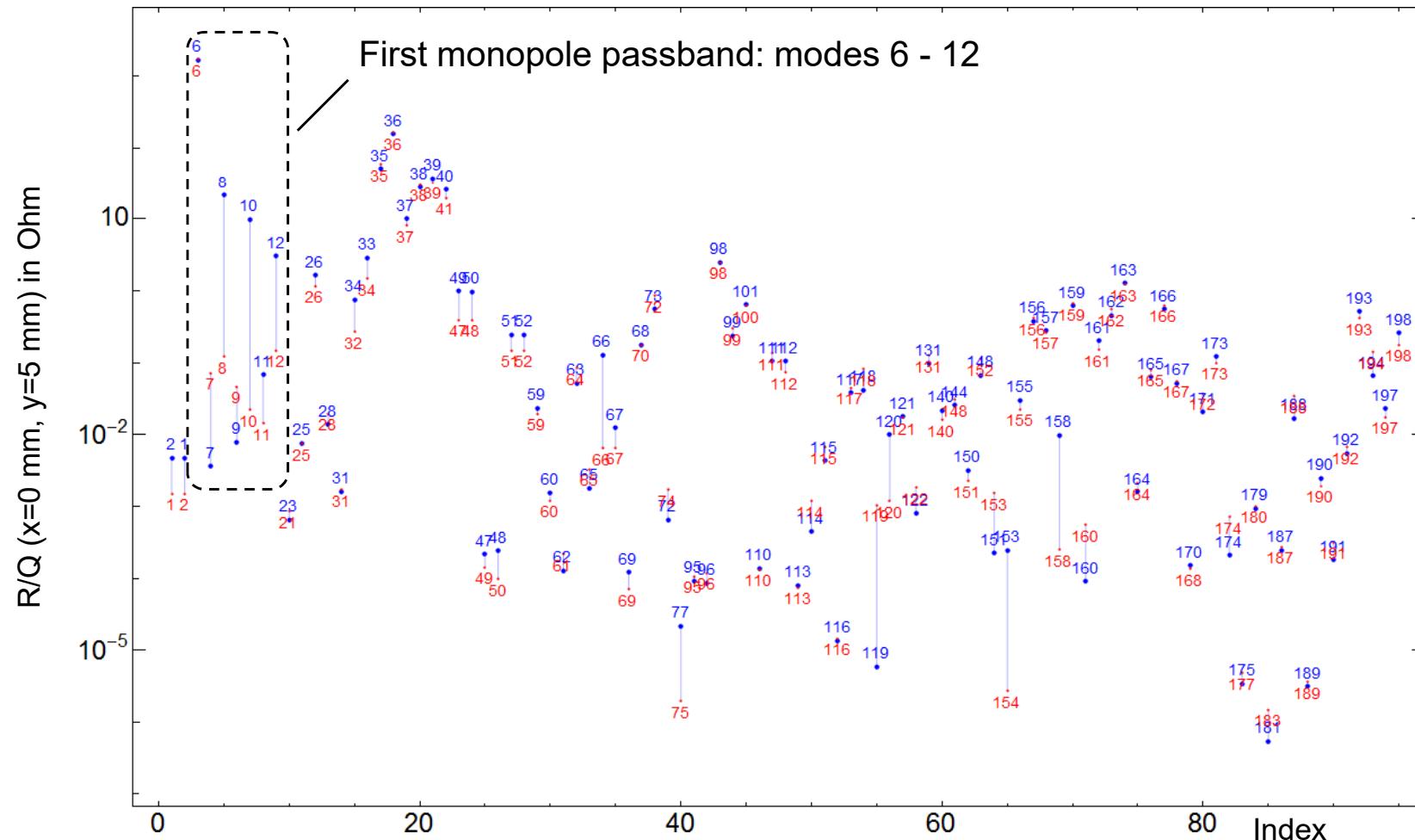


- Mode Correlation (“spark E, spark H”)



# Simulation Results

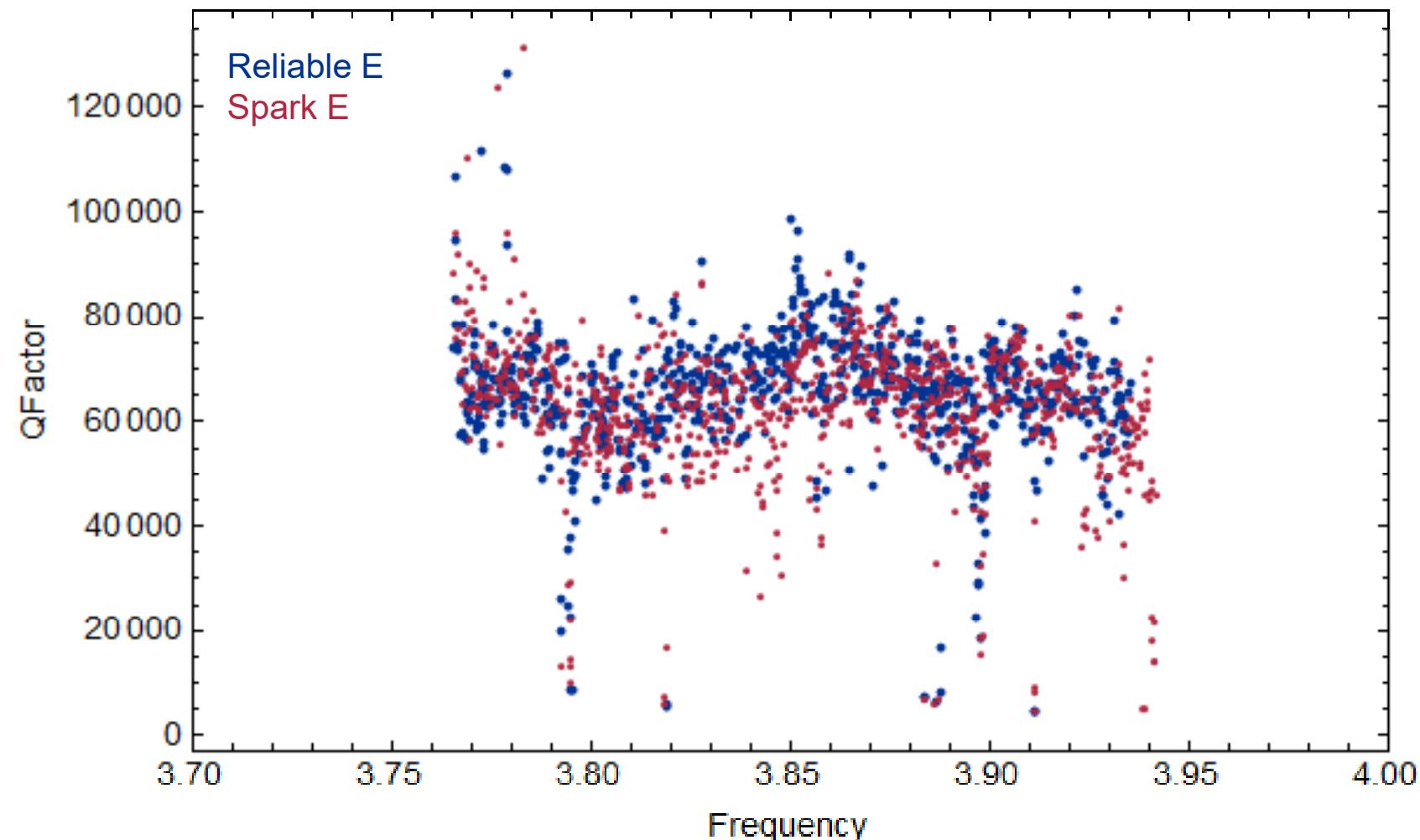
- Mode Correlation (“reliable H, spark H”)



# Simulation Results



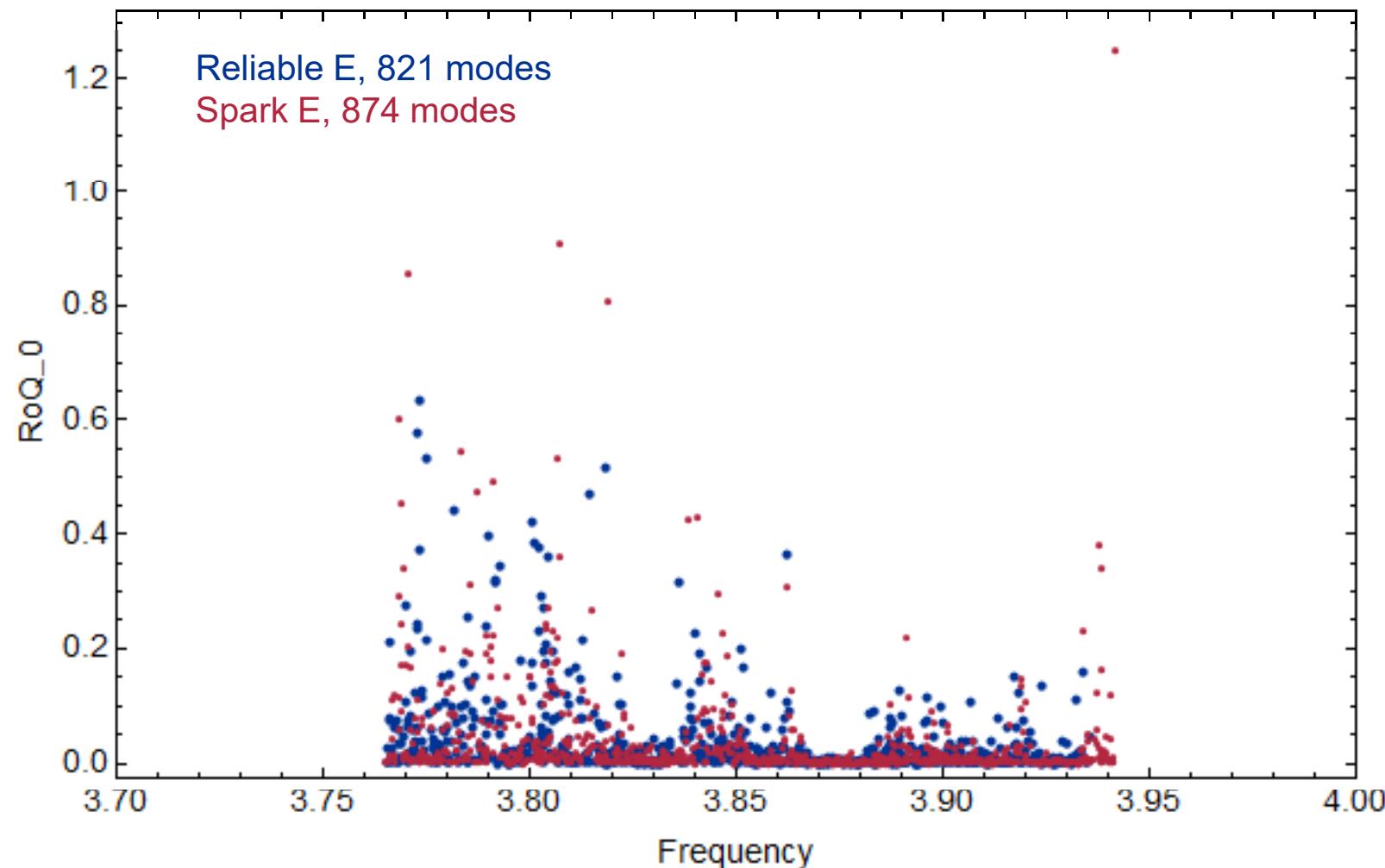
- Eigenmodes in the Frequency Range from 3.8 to 3.9 GHz



# Simulation Results



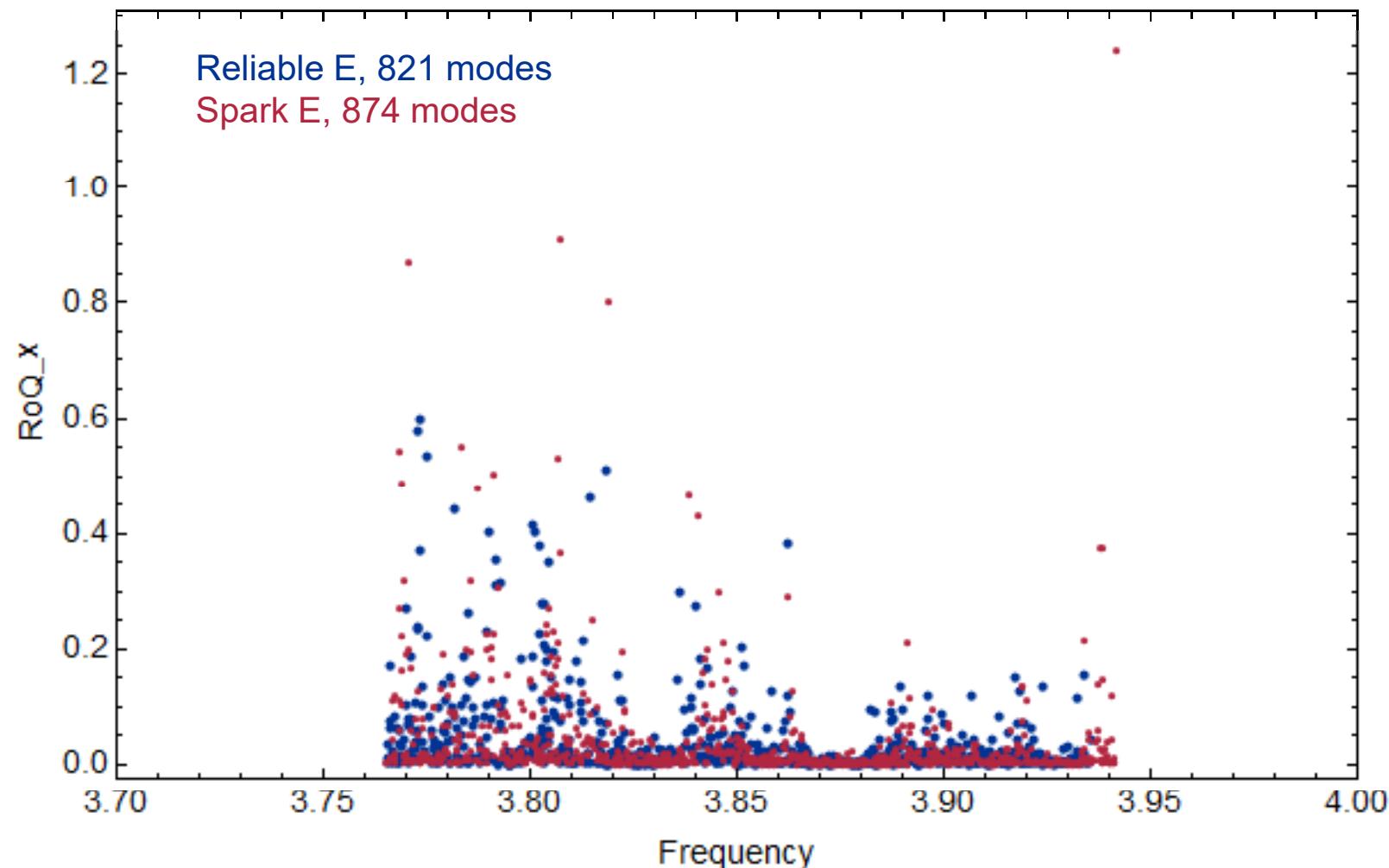
- Eigenmodes in the Frequency Range from 3.8 to 3.9 GHz



# Simulation Results



- Eigenmodes in the Frequency Range from 3.8 to 3.9 GHz

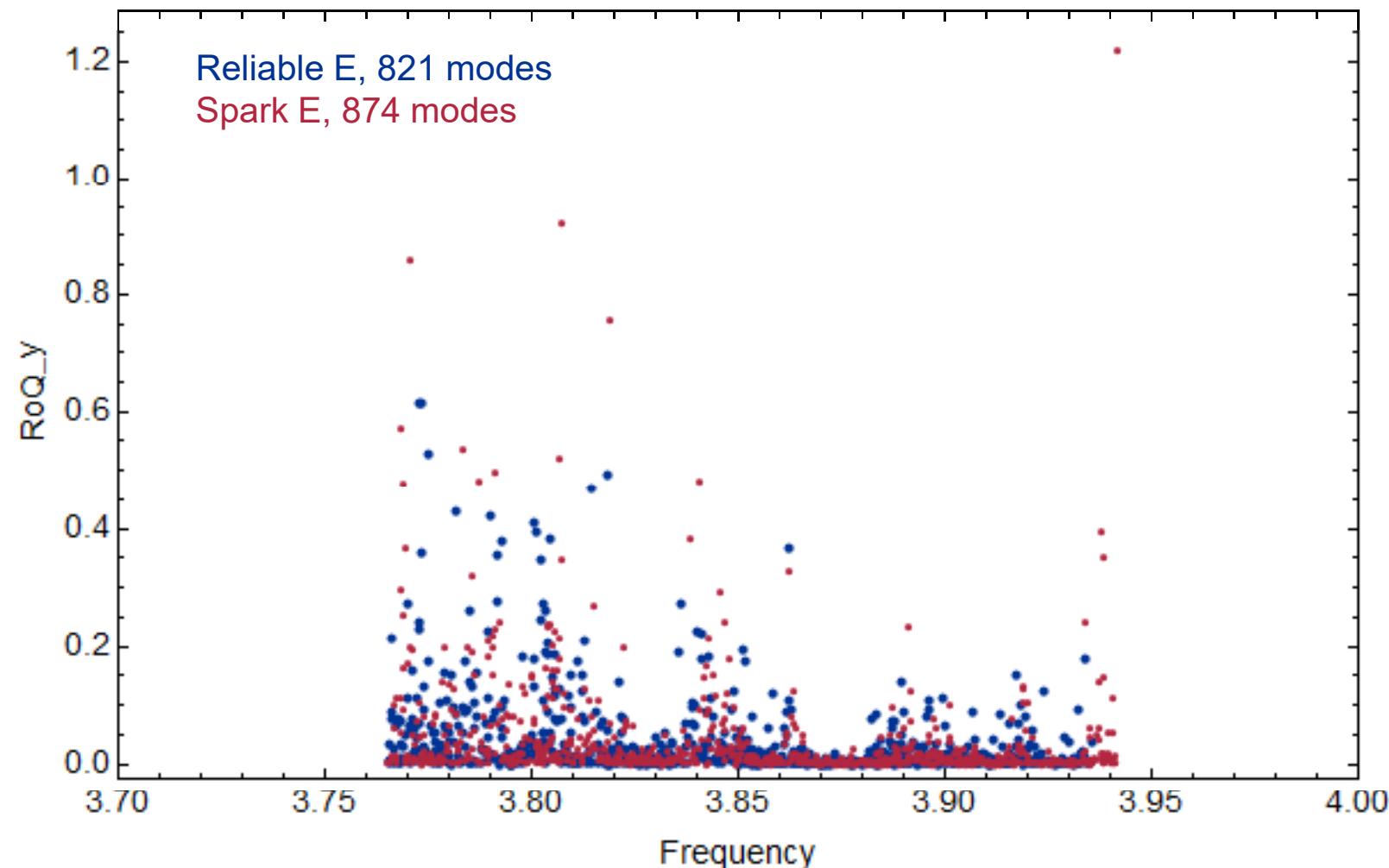


# Simulation Results



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- Eigenmodes in the Frequency Range from 3.8 to 3.9 GHz



# Outline



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- Motivation
- Computational Model
  - Drawings and geometry information
  - Numerical problem formulation
- Cavity tuning
  - Cell radius variation for the “reliable” and “spark” models
- Simulation results
  - Mode pattern and characteristic data for the “reliable” and “spark” models
- Summary / Outlook



- **Summary:**

- Precise modeling of the PETRA III cavity including pump ports, tuning plunger and input coupler
- Eigenmode analysis performed up to 1.2 GHz (mode pattern, frequency, R/Q, Q via power loss, slit field)
- Mode classification w.r.t. the azimuthal order
- R/Q of the fundamental monopole passband sensitive to model change from “spark” to “reliable”

- **Outlook:**

- Calculation of monopole passband with port BC?

