

Micro-Bunching and increasing Energy Spread in Flash

Flash SC-impedances (end-energy = 700 MeV)

Astra bunch (one particular bunch 0.4nC)

methods

before BC3: LGM

periodic tracking

LGM with higher spatial resolution (--> PO2)

what we know so far

after BC3: LGM (not applicable)

periodic tracking

1-stage LG: BC3

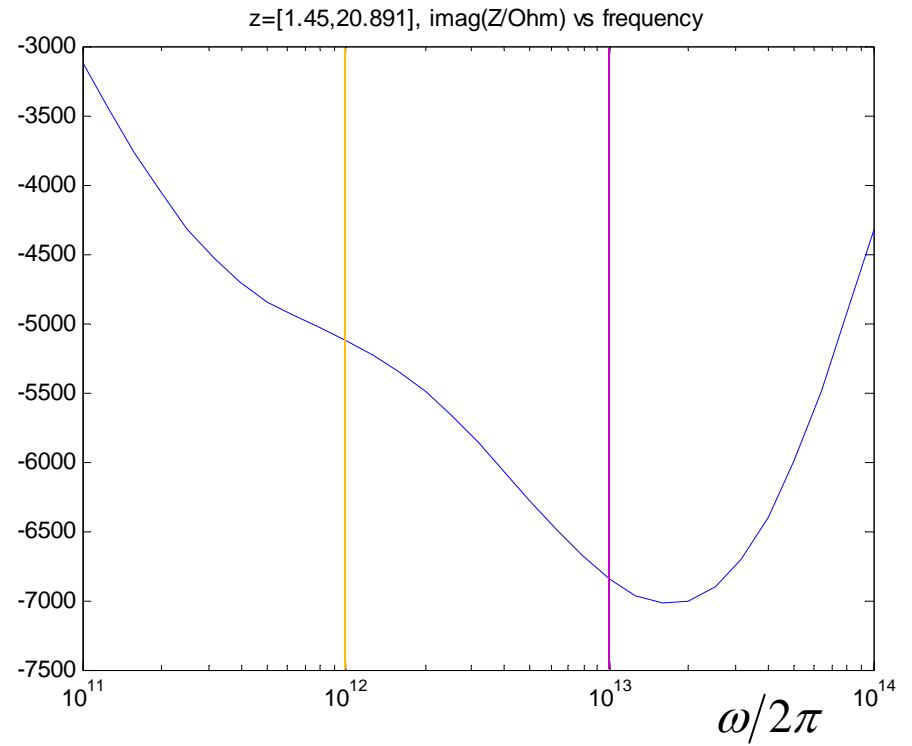
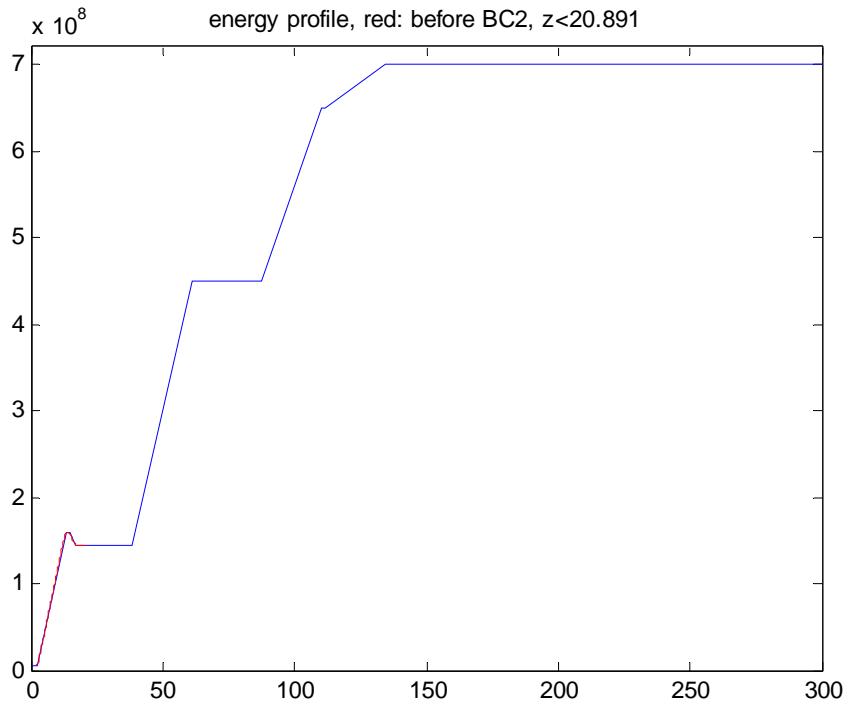
Flash2 seeding chicane

some numbers

FLASH SC-impedances

before BC2

SC impedance for emittance = 1 μ m
and beta_av = 10 m

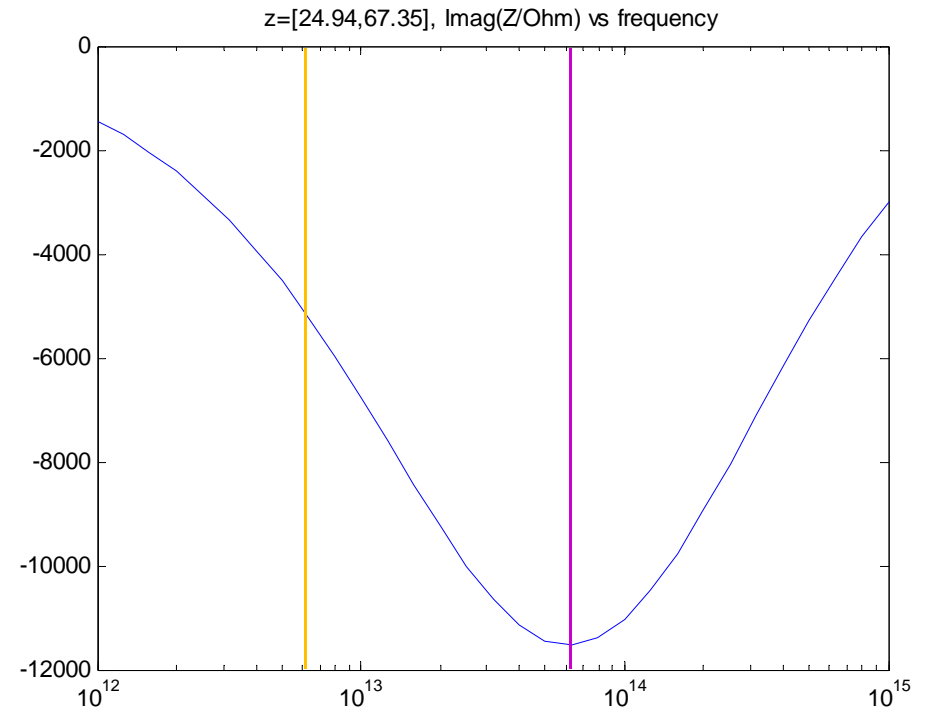
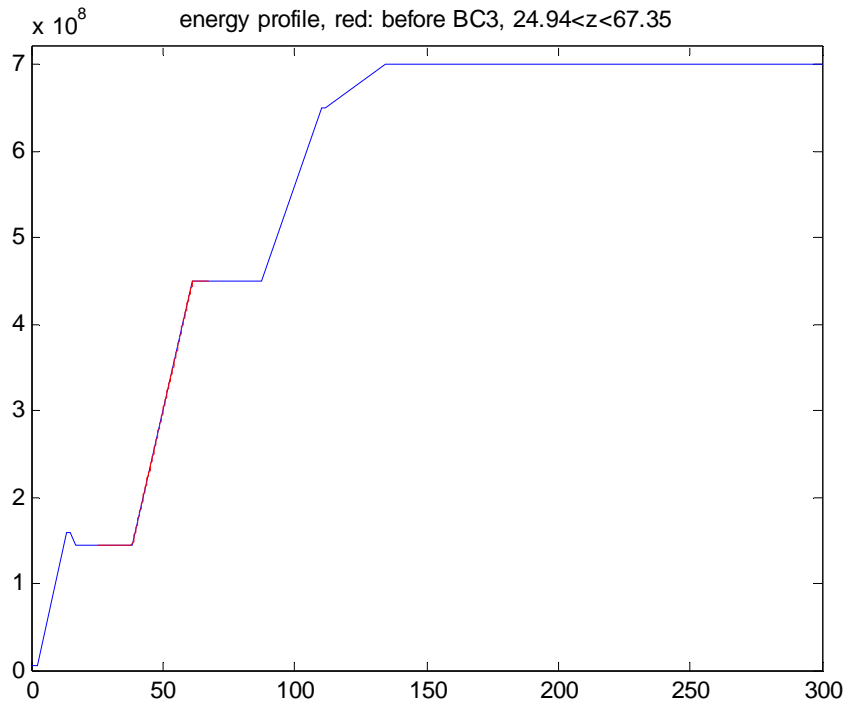


$$\lambda/\mu\text{m} = 300 = C1 \cdot 48 = C1 \cdot C2 \cdot 4.4$$

$$\lambda/\mu\text{m} = 30 = C1 \cdot 4.8 = C1 \cdot C2 \cdot 0.44$$

before BC3

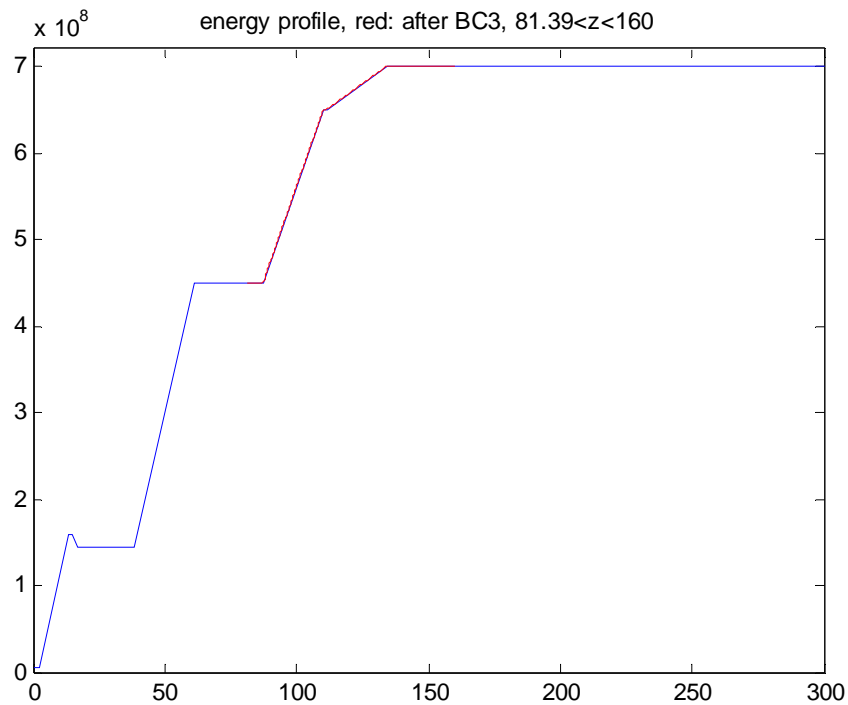
SC impedance for emittance = 1 μ m
and beta_av = 10 m



$$\lambda/\mu\text{m} = 300/C1 = 48 = C2 \cdot 4.4$$

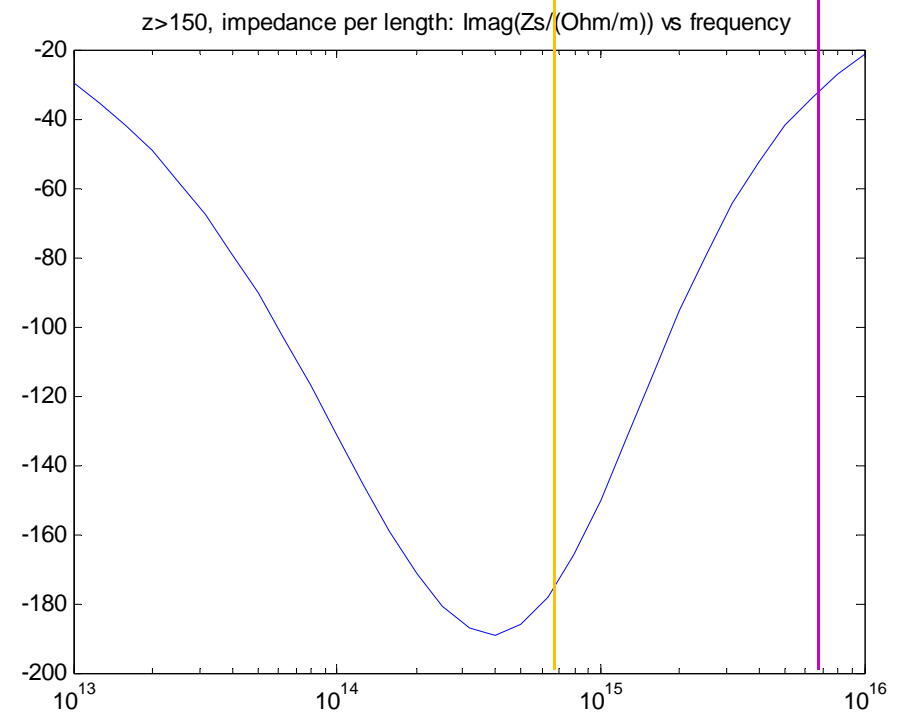
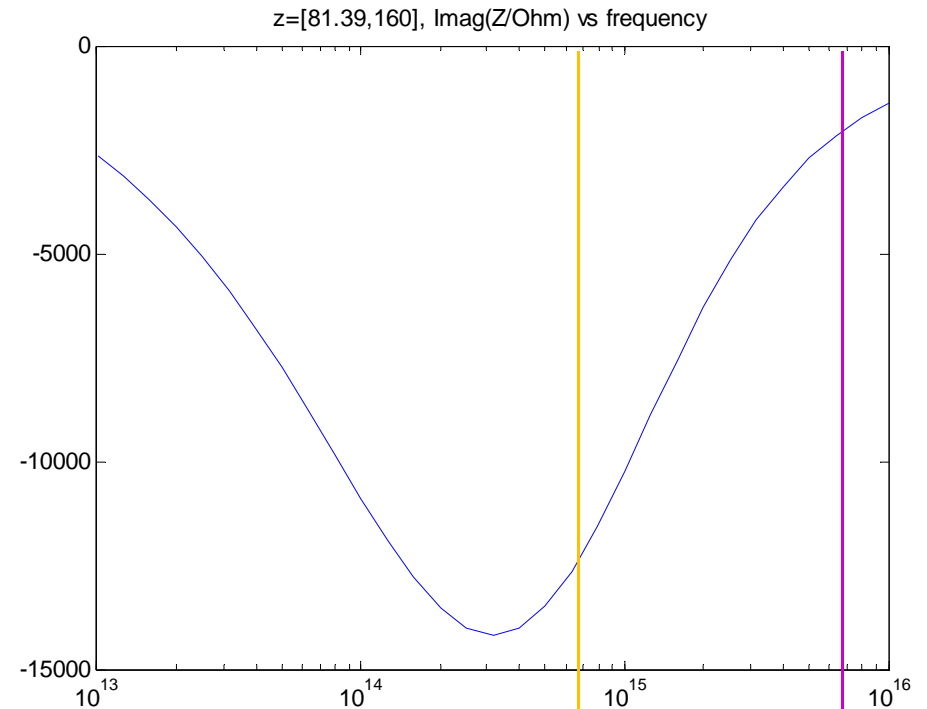
$$\lambda/\mu\text{m} = 30/C1 = 4.8 = C2 \cdot 0.44$$

SC impedance for emittance = 1 μ m
and beta_av = 10 m



$$\lambda/\mu\text{m} = 300/C1/C2 = 48/C2 = 4.4$$

$$\lambda/\mu\text{m} = 30/C1/C2 = 4.8/C1 = 0.44$$



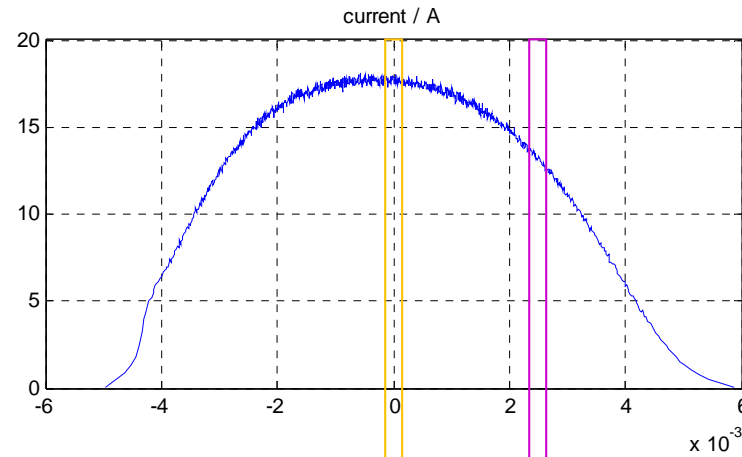
Astra bunch

Astra bunch 0.4 nC, at z=1.45 m

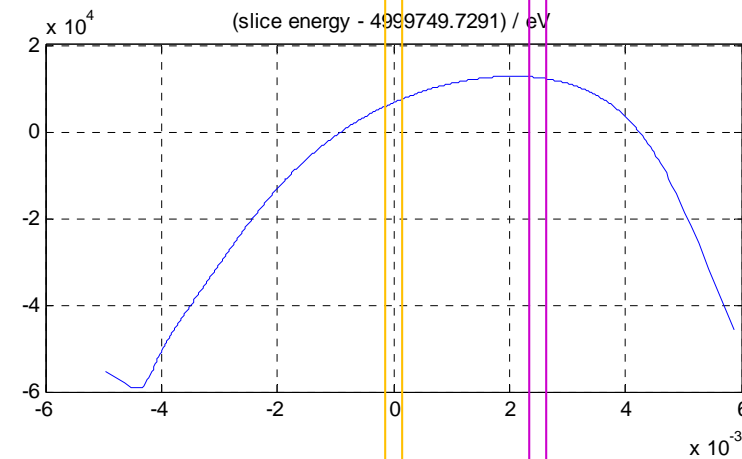
calculation with 10^7 particles

“slice 1”
(~1keV energy spread, I=17.6 A)

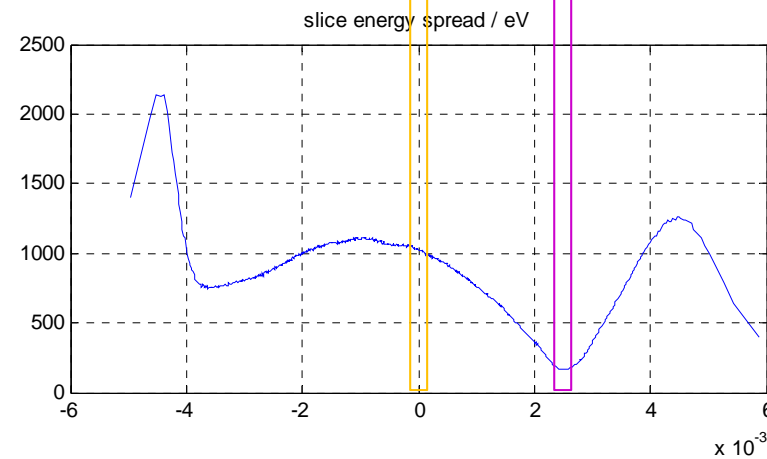
“slice 2”
(small energy spread, I=13.1 A)



I/A
bunch current



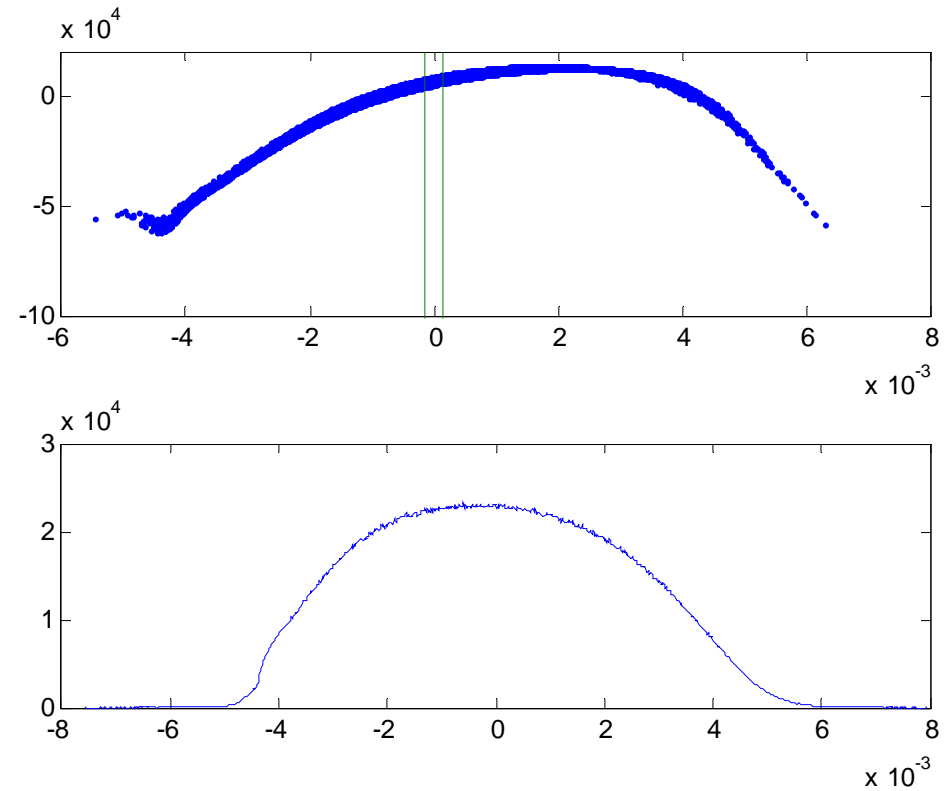
$(\langle E \rangle_s - E_0)/eV$
slice energy



σ_E/eV
slice energy spread

“slice” 1: Astra bunch 0.4 nC, at z=1.45 m

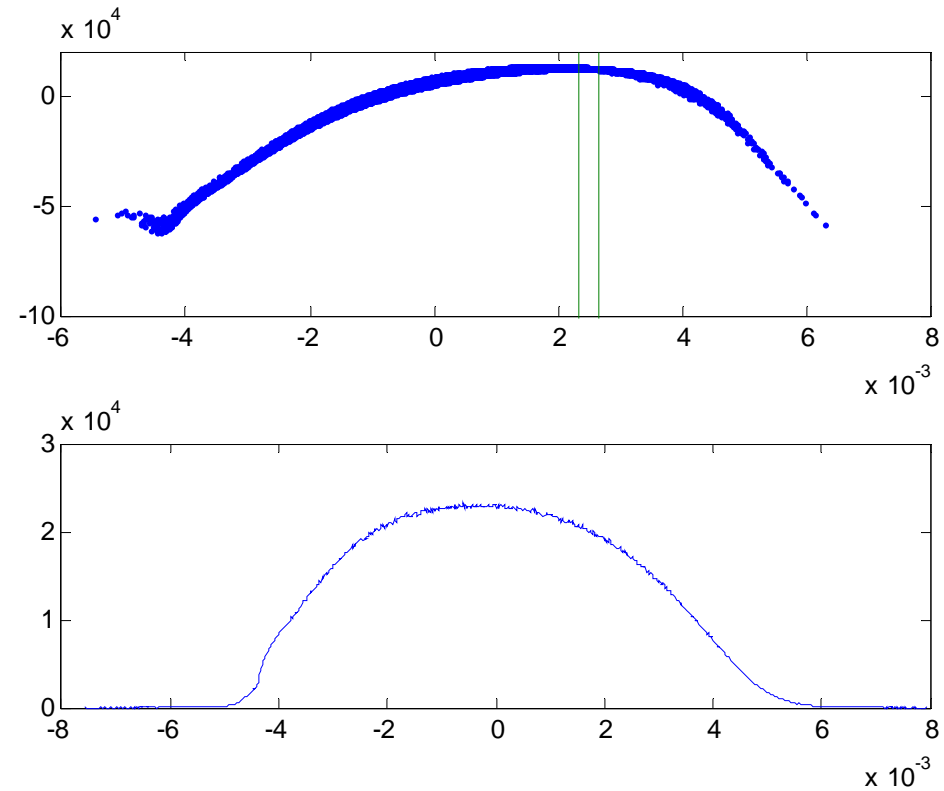
0.3mm “slice” with center at s=0mm (~1keV energy spread, I=17.6 A)
about 110E6 particles



compression: 17.7A --> 110A --> 1200A

“slice” 2: Astra bunch 0.4 nC, at z=1.45 m

0.3mm slice with center at s=2.5mm (small energy spread, I=13.1 A)
about 82E6 particles



compression: 13.1A --> 85.5A --> 944A

methods

linear gain model (LGM)

frequency of (small) initial density modulation ω

initial current (no modulation) I_0

linear gain function $G(\omega, S) = \tilde{I}(S) / (\tilde{I}(0)C(S))$

solve integral equation: $G(S) = G_0 + \int_0^S K(B, S)G(B)dB$

kernel depends on linear optics, local impedance
and (slice) energy distribution

rms amplitude of shot noise

$$i_{C,eff} = C \sqrt{\frac{eI_0}{\pi} \int |G(\omega)|^2 d\omega}$$

rms energy spread due to shot noise
(for a given impedance)

$$\sigma_E = eC \sqrt{\frac{eI_0}{\pi} \int |G(\omega)Z(C\omega)|^2 d\omega}$$

start at $z=0.40\text{m}$ (after Gun)

“periodic tracking”

here: tracking of a periodic distribution

real number of electrons --> real shot noise

short period ($\sim 0.3\text{mm}$, $\sim 100\text{E}6$ particles)

linear external forces, but **non-linear space charge forces** (periodic SC solver)

all lattice elements behave linear

rf curvature neglected (short period)

no wakes

no self-effects in chicanes

tricks: preparation of initial distribution (next slide)

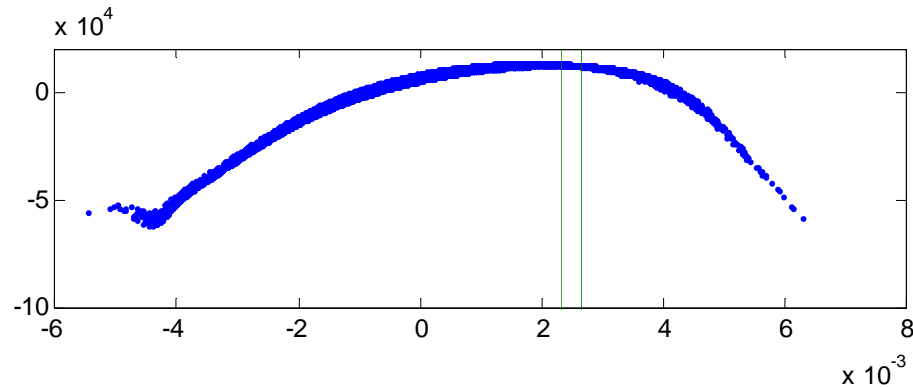
reduce number of particles **after BC2**: $\sim 100\text{E}6$ --> $10\text{E}6$ particles

density fluctuations are well above shot noise

(s2e full resolution calculation is possible!)

start at $z=1.45\text{m}$ (after solenoid)

preparation of phase space distribution:



Astra distribution with 10E6 particles, but $0.4 \text{ nC / e} = 2.5\text{E}9$
we need 250 particles per Astra-particles

procedure: select all particles in the given slice,
extract correlations with z (to 3rd order)
keep information about linear z-energy correlation
throw away z-information
multiply (replicate x 250) and mix the 5D-distribution
use random generator for z-coordinates
regenerate linear z-energy correlation

LGM before BC3

```

>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 6.25
Ctot*current_0 = 110
rms energy spread = 999.6854
rms energy spread @ end = 6248.0335
maximal gain = 41.226
integral(gain^2,domega) = 6.642e+16
Cnoise = Ctot*sqrt(...) = 1.525 (1.538 with CSR)

```

0.3mm slice with center at s=0mm
 (~1keV energy spread, I=17.6 A)

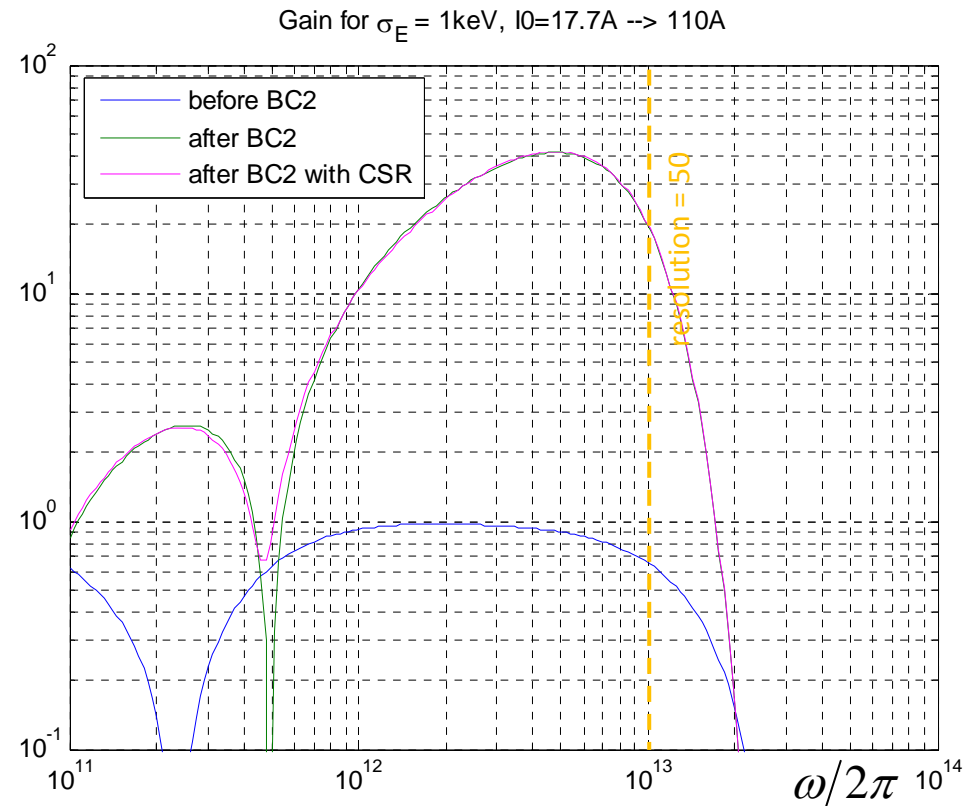
from initial energy spread

shot noise after BC2

$$i_{C,eff} = C \sqrt{\frac{eI_0}{\pi} \int |G(\omega)|^2 d\omega} = 1.53 \text{ A}$$

energy spread due to shot noise
 BC2 --> BC3

$$\sigma_E = eC \sqrt{\frac{eI_0}{\pi} \int |G(\omega)Z(C\omega)|^2 d\omega} = 16 \text{ keV}$$



0.3mm slice with center at s=2.5mm
(small energy spread, I=13.1 A)

```
>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 6.5267
Ctot*current_0 = 85.5
rms energy spread = 249.9379
rms energy spread @ end = 1631.2744
maximal gain = 92.2164
integral(gain^2,domega) = 1.344e+18
Cnoise = Ctot*sqrt(...) = 6.1809 (6.277 with CSR)
```

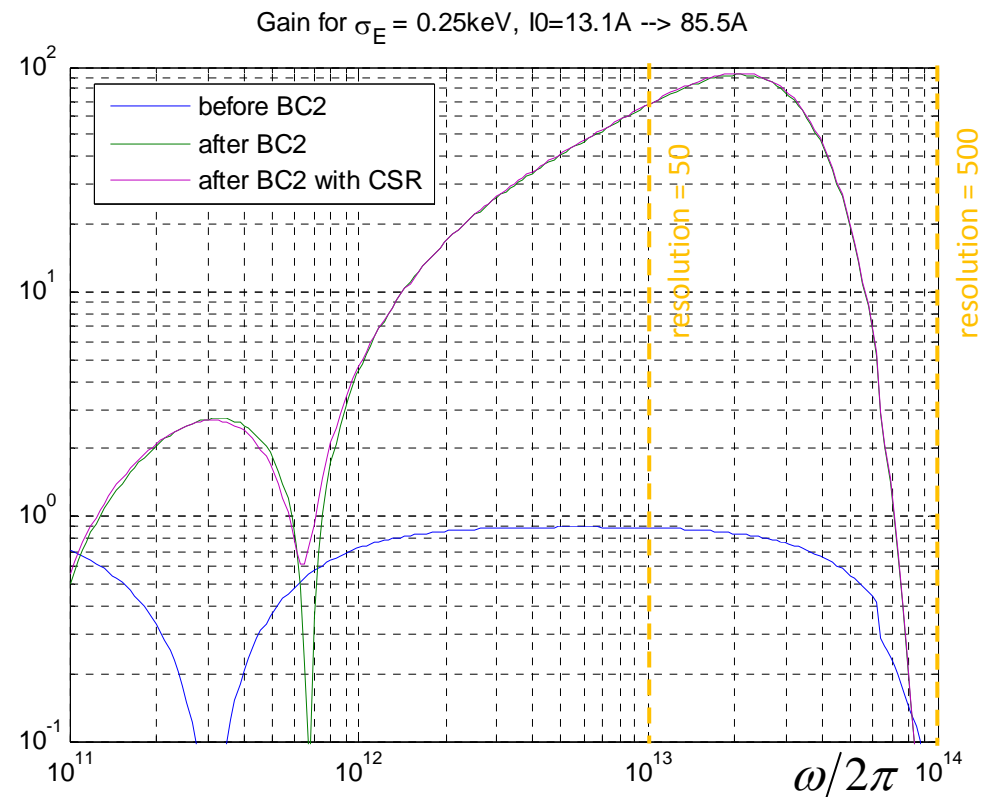
from initial energy spread

shot noise after BC2

$$i_{C,eff} = C \sqrt{\frac{eI_0}{\pi} \int |G(\omega)|^2 d\omega} = 6.18 \text{ A}$$

energy spread due to shot noise
BC2 --> BC3

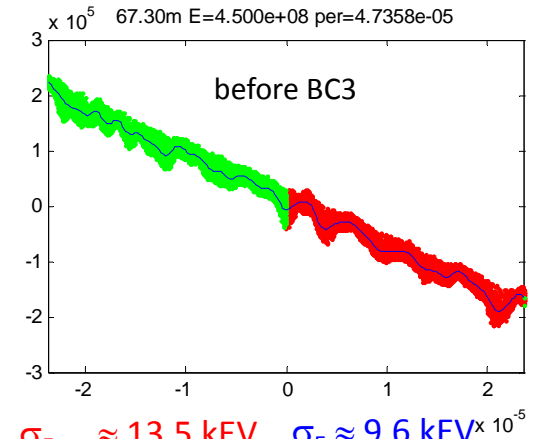
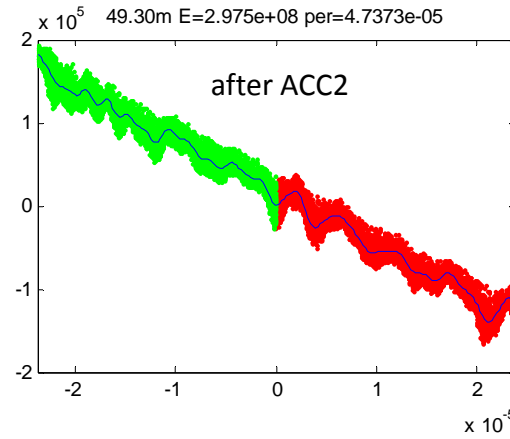
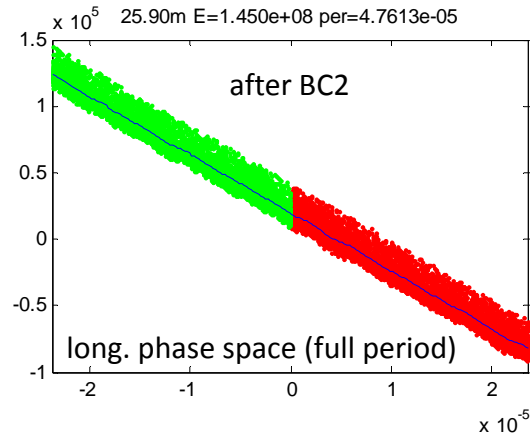
$$\sigma_E = eC \sqrt{\frac{eI_0}{\pi} \int |G(\omega)Z(C\omega)|^2 d\omega} = 62 \text{ keV}$$



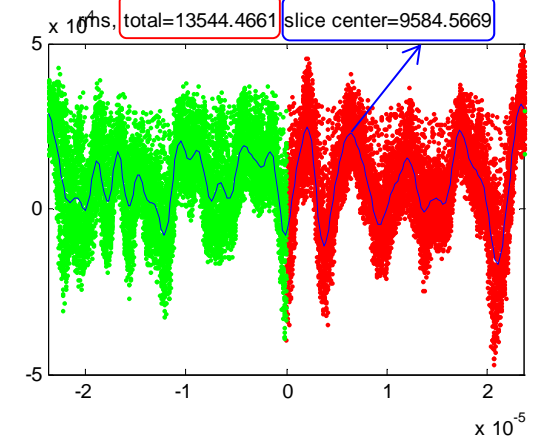
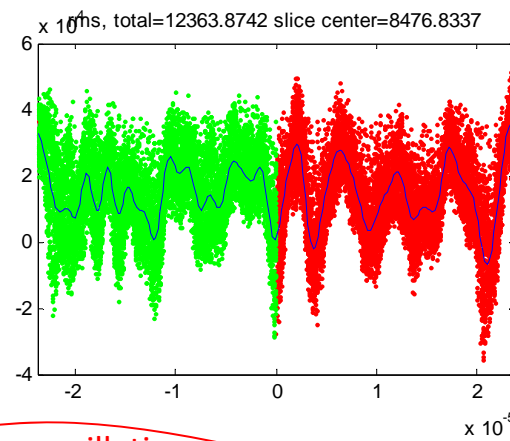
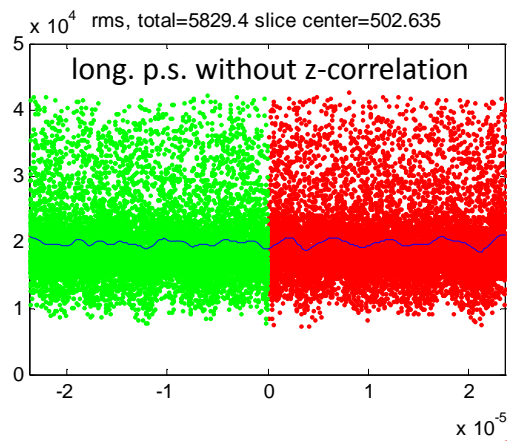
periodic tracking before BC3

24.90 after BC2
49.30 after ACC2
67.30 before BC3

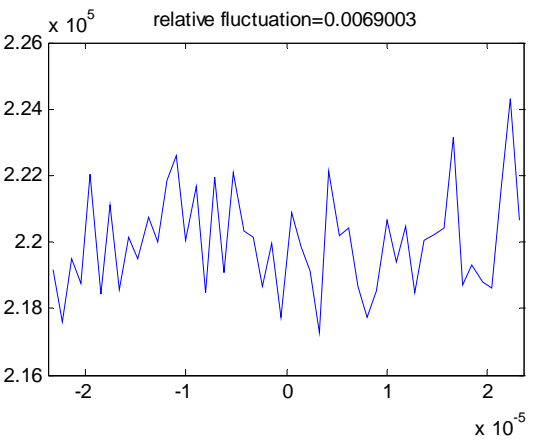
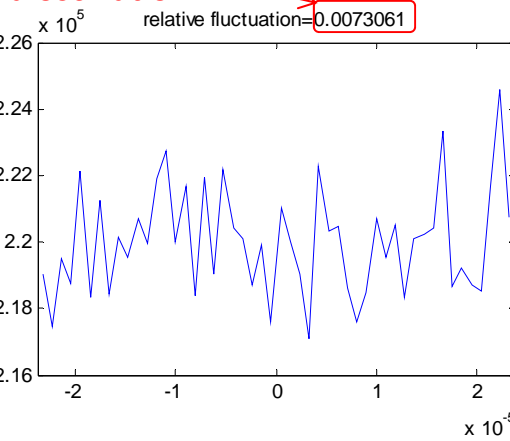
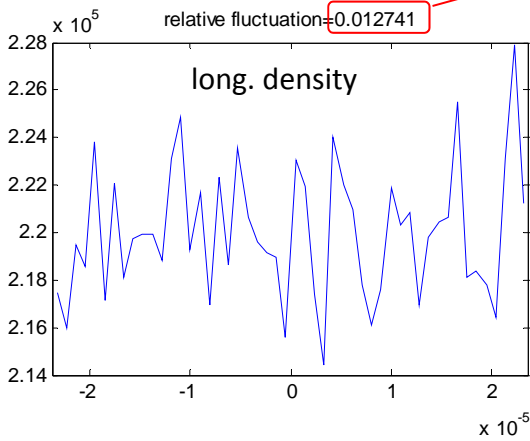
0.3mm slice with center at s=0mm (~1keV energy spread, I=17.6 A)



$\sigma_{E,tot} \approx 13.5 \text{ keV}$ $\sigma_E \approx 9.6 \text{ keV}$ $\times 10^{-5}$

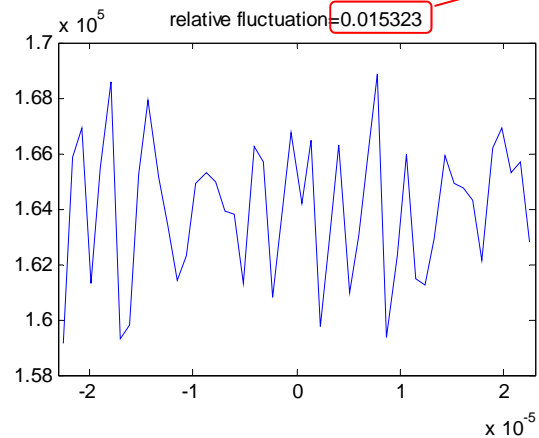
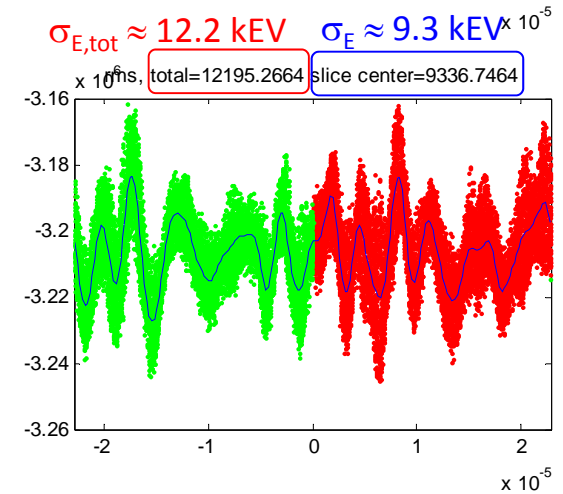
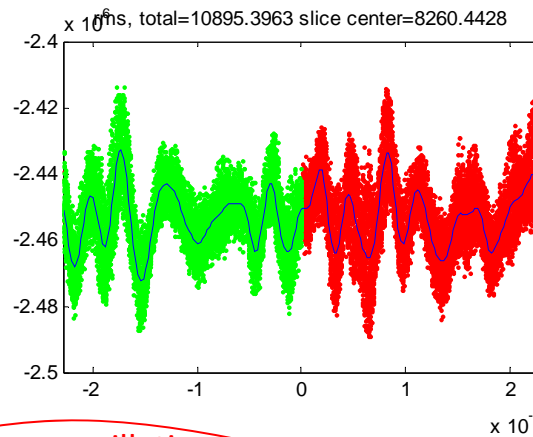
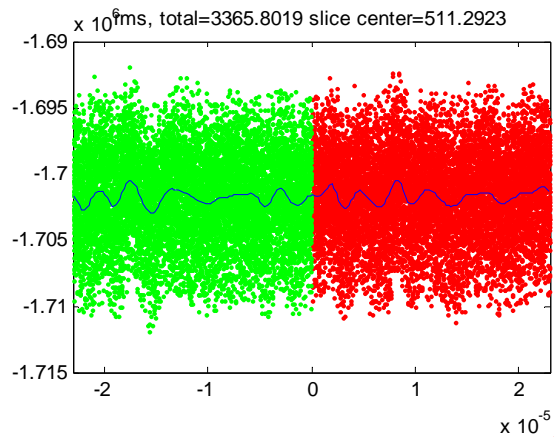
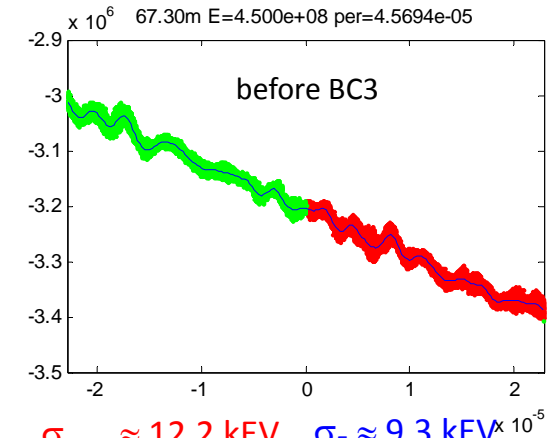
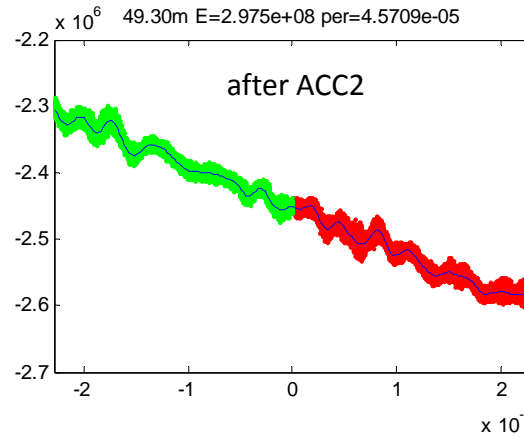
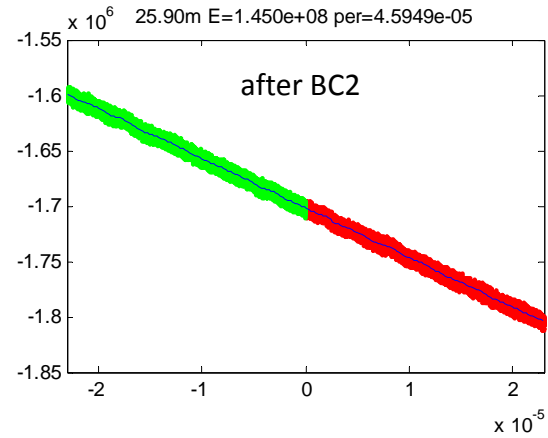


plasma oscillation

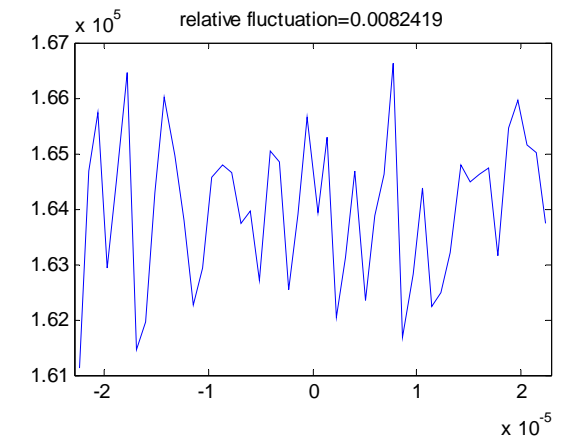
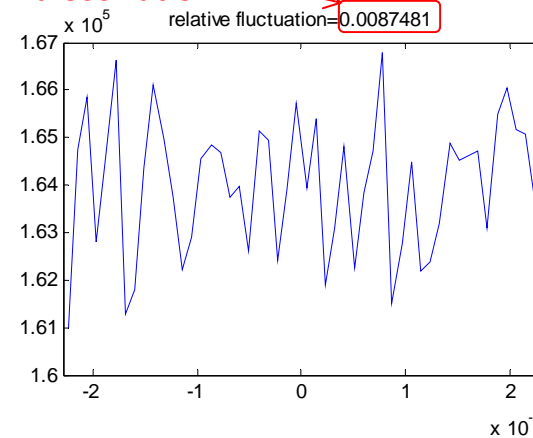


0.3mm slice with center at s=2.5mm (small energy spread, I=13.1 A)

resolution = 50

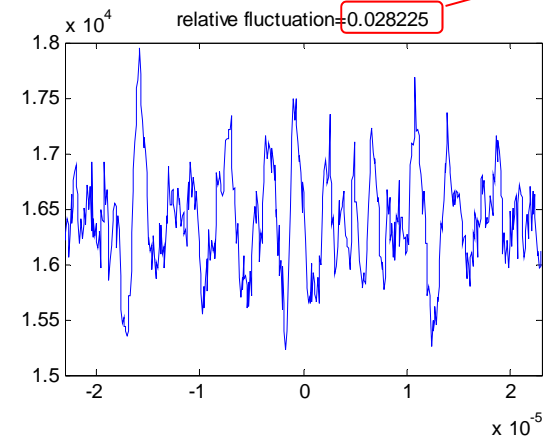
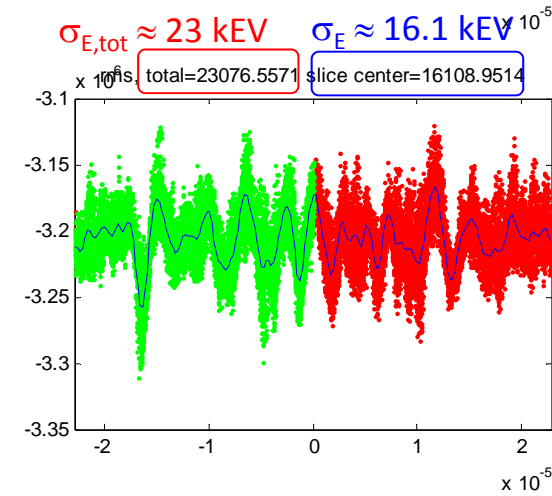
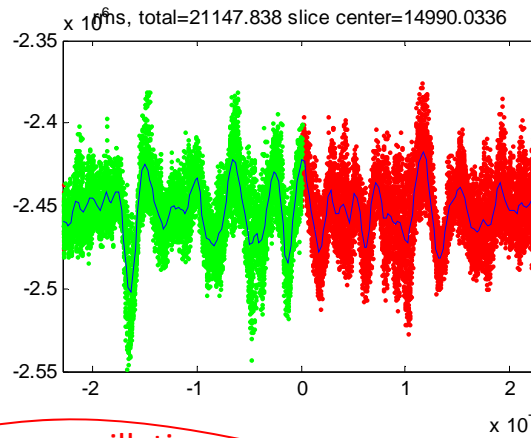
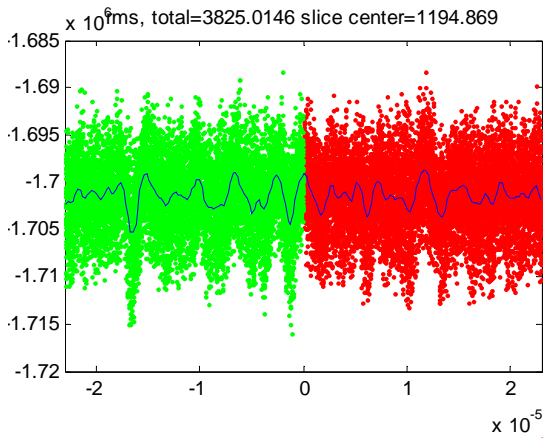
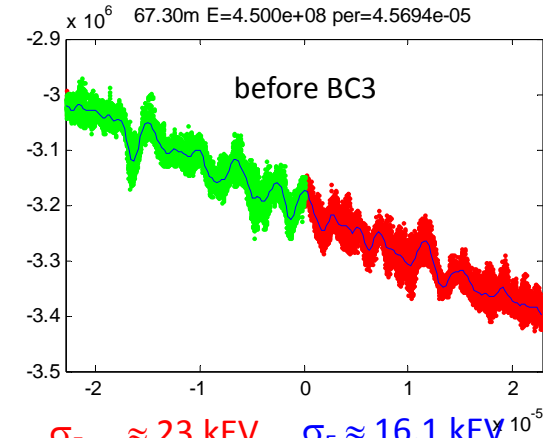
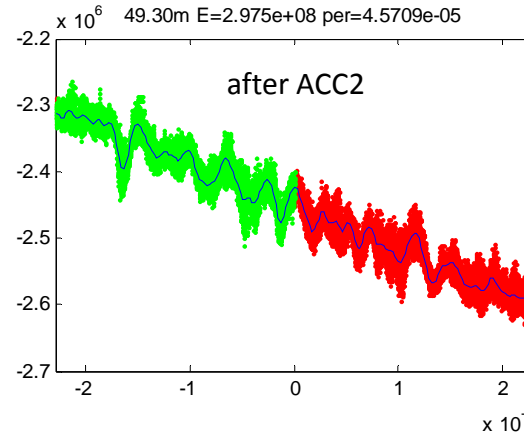
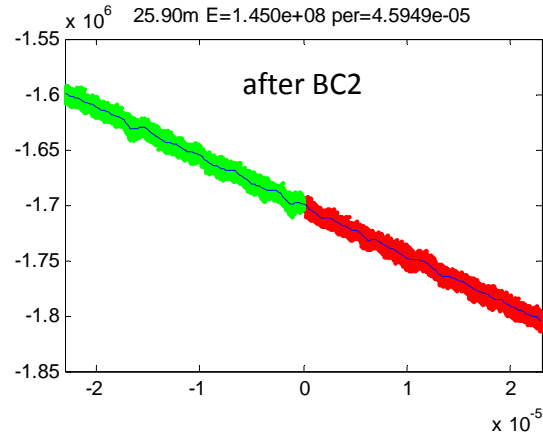


plasma oscillation

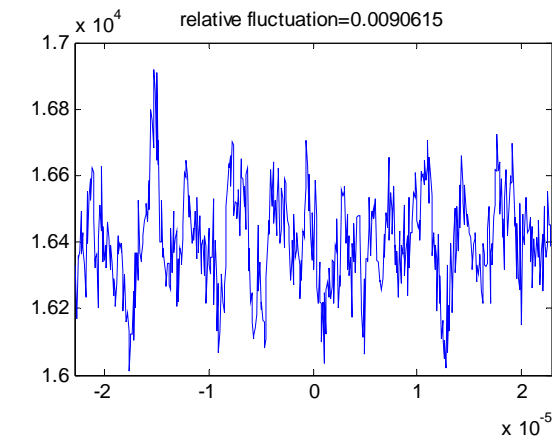
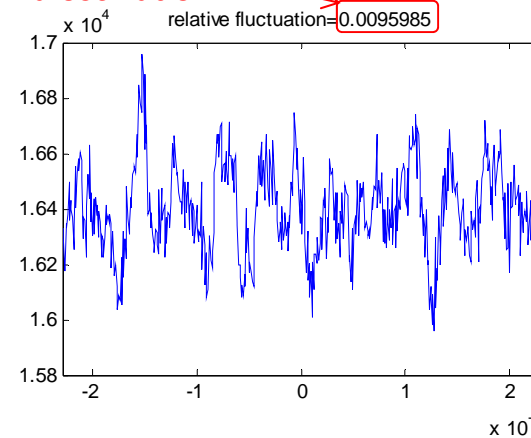


0.3mm slice with center at s=2.5mm (small energy spread, I=13.1 A)

resolution = 500



plasma oscillation



LGM before BC3 with PO2

PO1 = plasma oscillation before BC2

PO2 = plasma oscillation before BC3

```

>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 6.2891
Ctot*current_0 = 110.6883
rms energy spread = 999.6854
rms energy spread @ end = 6287.1265
maximal gain = 41.226
integral(gain^2,domega) = 1.77e+16
Cnoise = Ctot*sqrt(...) = 0.79228 (0.795 with CSR)

```

0.3mm slice with center at s=0mm
 (~1keV energy spread, I=17.6 A)

from initial energy spread

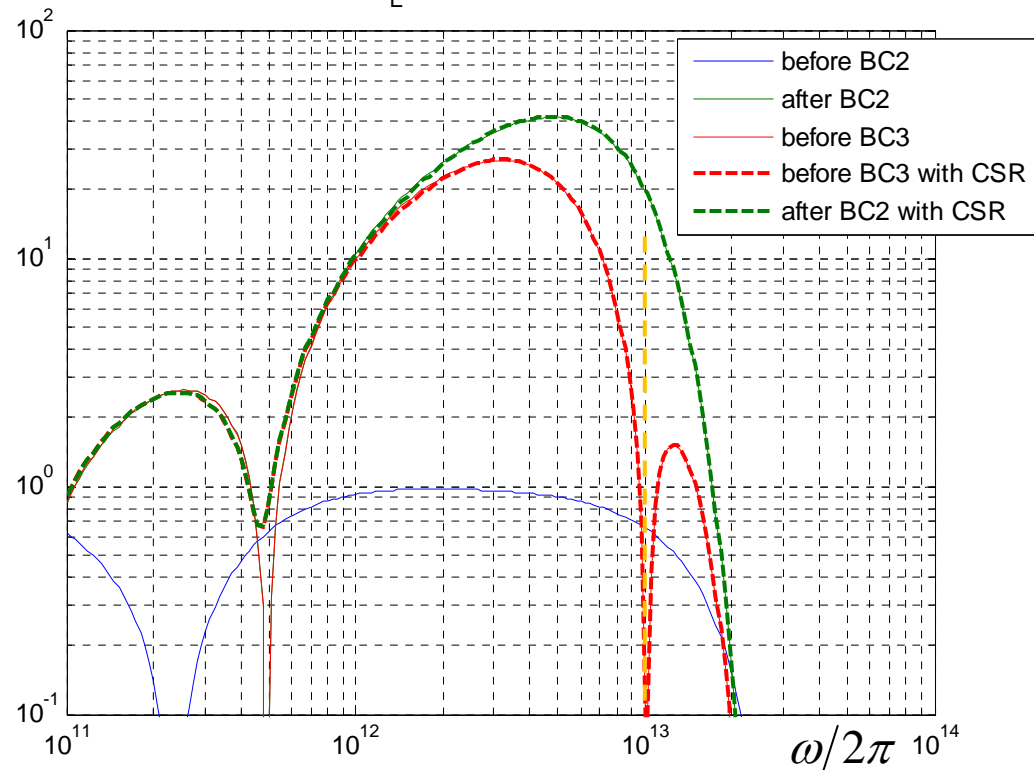
shot noise before BC3

$$i_{C,eff} = C \sqrt{\frac{eI_0}{\pi} \int |G(\omega)|^2 d\omega} = 0.792 \text{ A}$$

energy spread due to shot noise
 BC2 --> BC3

$$\sigma_E = eC \sqrt{\frac{eI_0}{\pi} \int \underbrace{\langle G(\omega) \rangle Z(C\omega)}_{\text{averaged!}}^2 d\omega} = 7.4 \text{ keV}$$

Fain for $\sigma_E = 1\text{keV}$, $I_0=17.7\text{A} \rightarrow 110\text{A}$



```

>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 6.5693
Ctot*current_0 = 86.0574
rms energy spread = 249.9377
rms energy spread @ end = 1641.9067
maximal gain = 113.7693
integral(gain^2,domega) = 2.589e+17
Cnoise = Ctot*sqrt(...) = 2.7303 (6.277 with CSR)

```

0.3mm slice with center at s=2.5mm
(small energy spread, I=13.1 A)

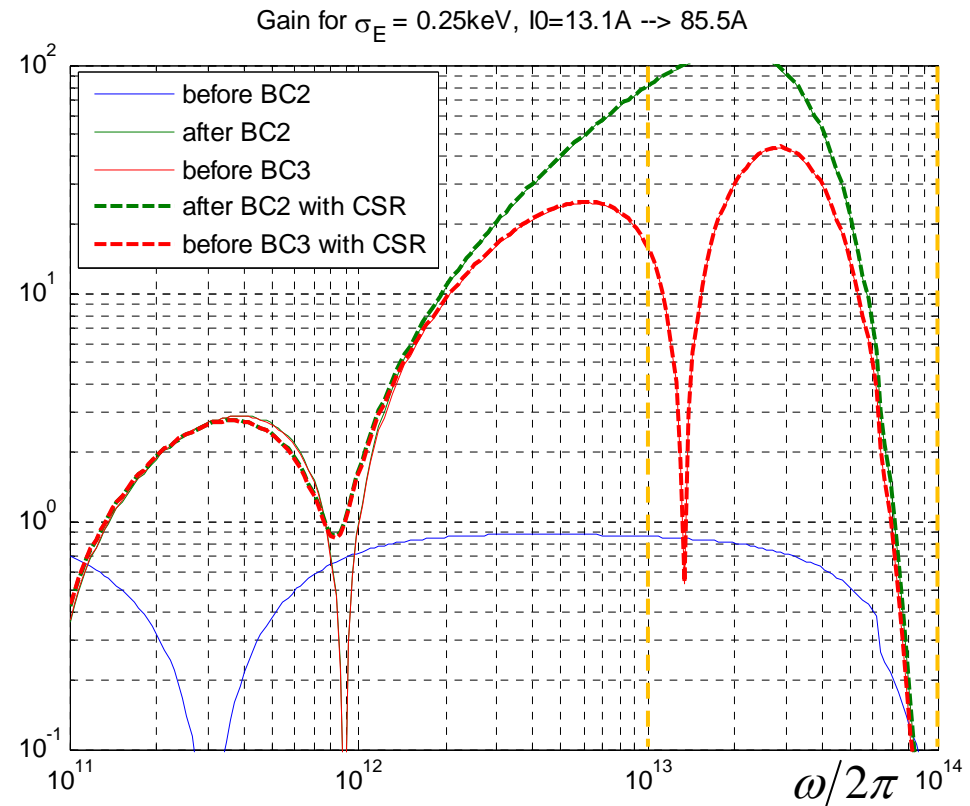
from initial energy spread

shot noise before BC3

$$i_{C,eff} = C \sqrt{\frac{eI_0}{\pi} \int |G(\omega)|^2 d\omega} = 2.73 \text{ A}$$

energy spread due to shot noise
BC2 --> BC3

$$\sigma_E = eC \sqrt{\frac{eI_0}{\pi} \int |\langle G(\omega) \rangle Z(C\omega)|^2 d\omega} = 25 \text{ keV}$$



what we know so far

total energy spread after BC3, without further effects

$$\sigma_{E,3} = C_2 \sqrt{(C_1 \sigma_{E,i})^2 + \sigma_{E,2}^2}$$

0.3mm slice with center at s=0mm
(~1keV energy spread, I=17.6 A)

$$C_1 = 110/17.7$$

$$C_2 = 1200/110$$

$$\sigma_{E,i} = 1 \text{ keV}$$

$$\sigma_{E,2} = 7.4 \text{ keV}$$

particle tracking → (9.6 keV)

$$\sigma_{E,3} = 105 \text{ keV}$$

(127 keV)

0.3mm slice with center at s=2.5mm
(small energy spread, I=13.1 A)

$$C_1 = 85.5/13.1$$

$$C_2 = 944/85.5$$

$$\sigma_{E,i} = 0.25 \text{ keV}$$

$$\sigma_{E,2} = 25 \text{ keV}$$

(9.3 keV*, 23 keV)

$$\sigma_{E,3} = 273 \text{ keV}$$

(133 keV*, 253 keV)

* too small due to limited bandwidth!

LGM after BC3

is not applicable, but look:

```

>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 70.784
Ctot*current_0 = 1245.7987
rms energy spread = 999.6854
rms energy spread @ end = 70761.7435
maximal gain = 622.6615
integral(gain^2,domega) = 2.635e+18
Cnoise = Ctot*sqrt(...) = 108.794

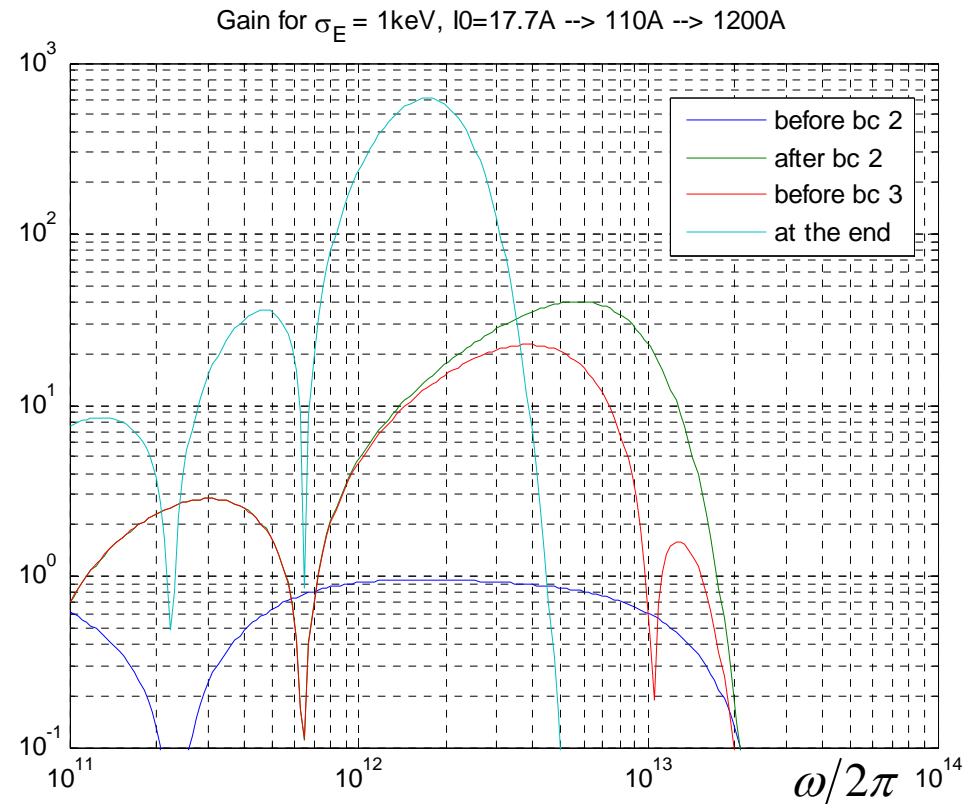
```

0.3mm slice with center at s=0mm
 (~1keV energy spread, I=17.6 A)

from initial energy spread

shot noise after BC3

$$i_{C,eff} = C_1 C_2 \sqrt{\frac{eI_0}{\pi} \int |G(\omega)|^2 d\omega} = 109 \text{ A}$$



```

>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 75.1269
Ctot*current_0 = 984.1623
rms energy spread = 249.9213
rms energy spread @ end = 18775.8132
maximal gain = 10085.6972
integral(gain^2,domega) = 2.522e+21
Cnoise = Ctot*sqrt(...) = 3081.4198

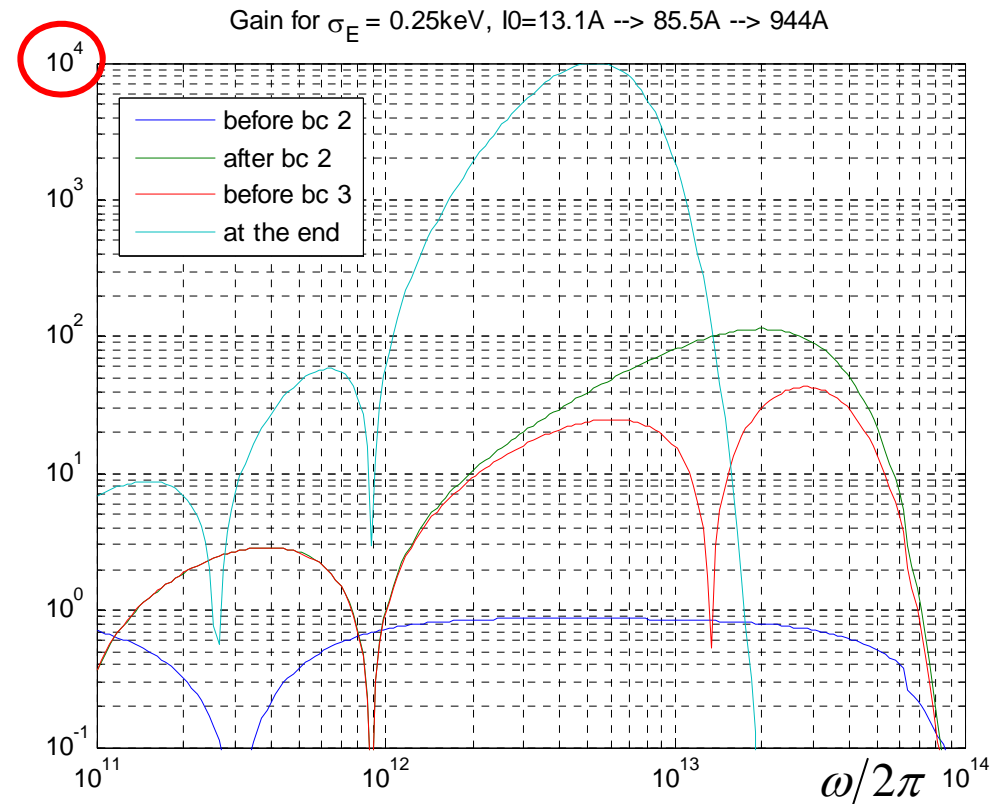
```

0.3mm slice with center at s=2.5mm
(small energy spread, I=13.1 A)

from initial energy spread

shot noise after BC3

$$i_{C,eff} = C_1 C_2 \sqrt{\frac{eI_0}{\pi} \int |G(\omega)|^2 d\omega} = 3 \text{ kA}$$



periodic tracking after BC3

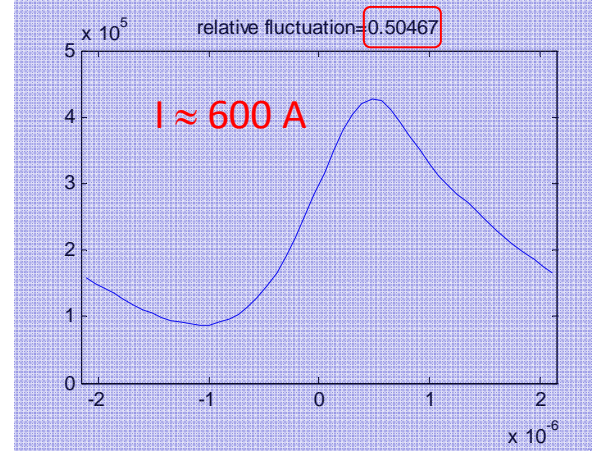
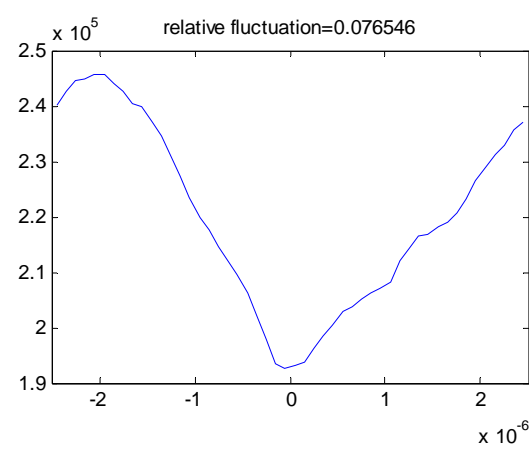
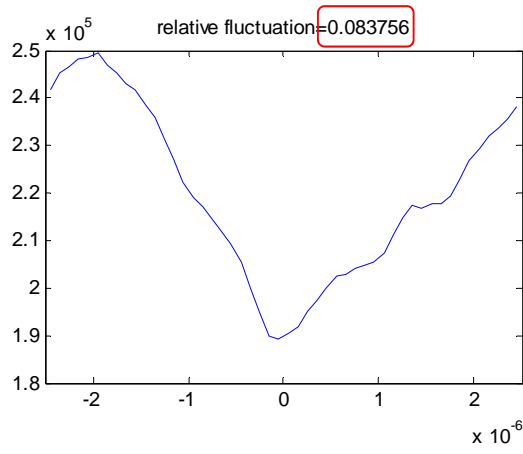
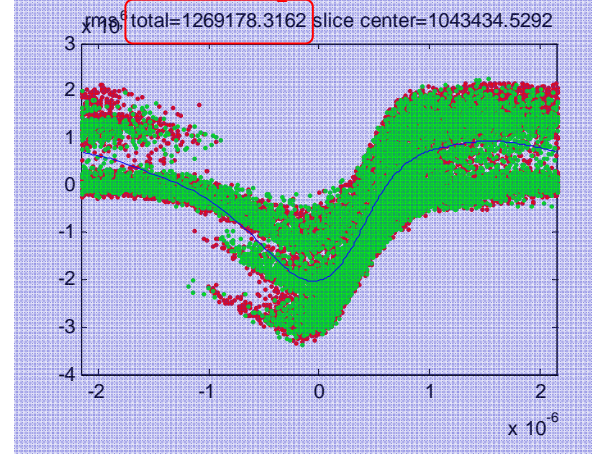
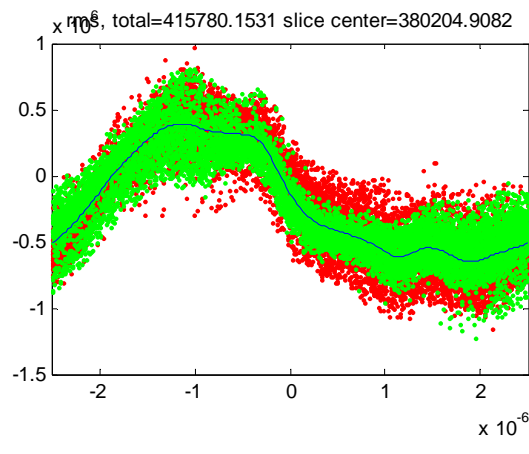
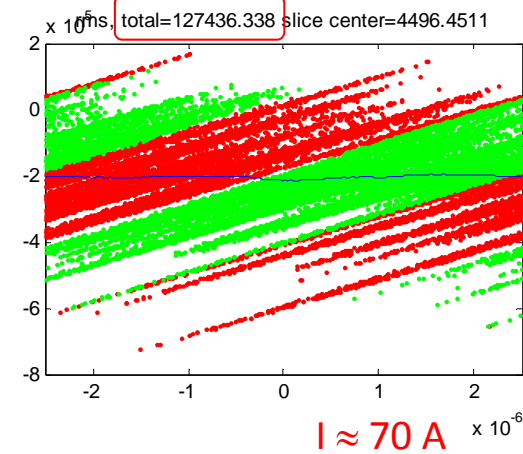
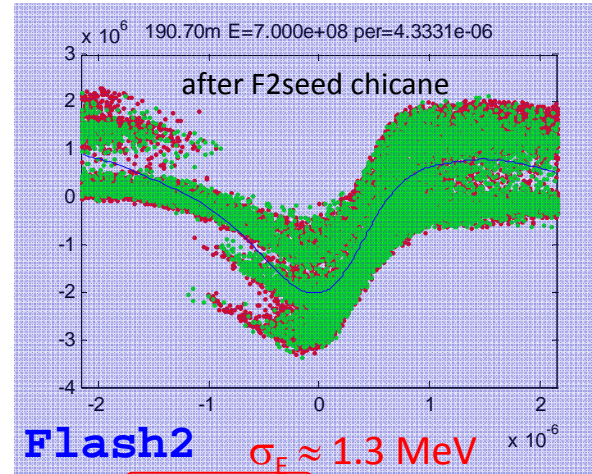
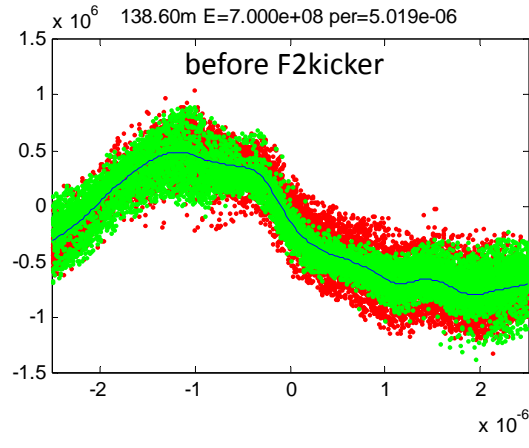
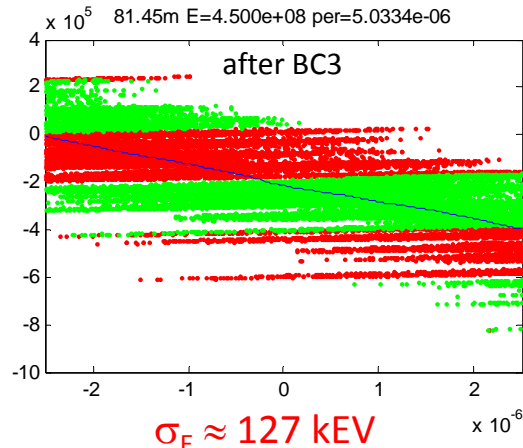
81.45 after BC3

138.60, 'before kicker, before septum,

Flash2 with seeding chicane, phi=20mrad, R56≈1..2mm

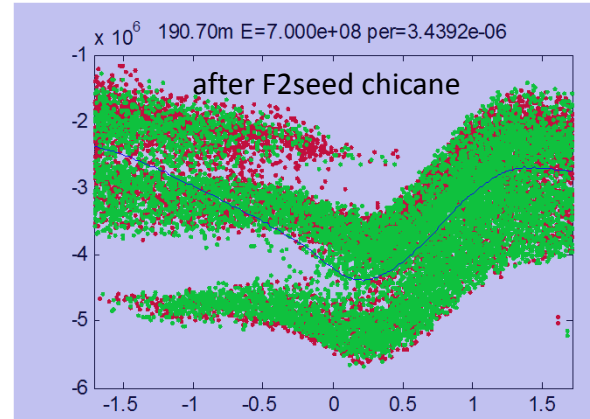
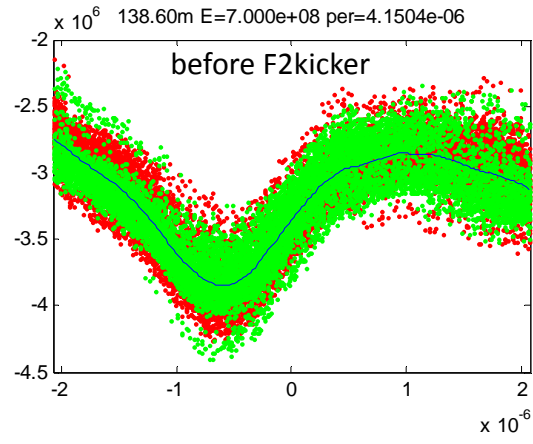
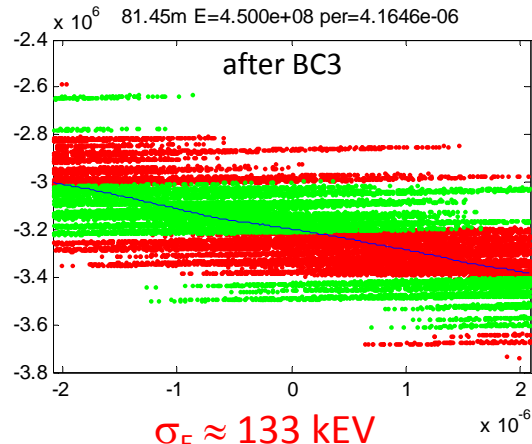
190.70, 'after V4FL2SEED6'

0.3mm slice with center at s=0mm (~1keV energy spread, I=17.6 A)

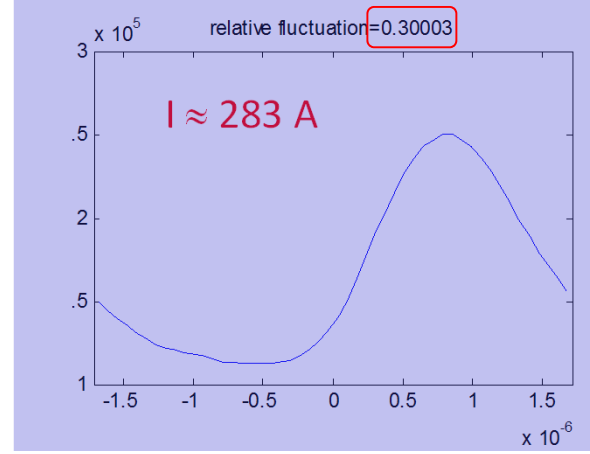
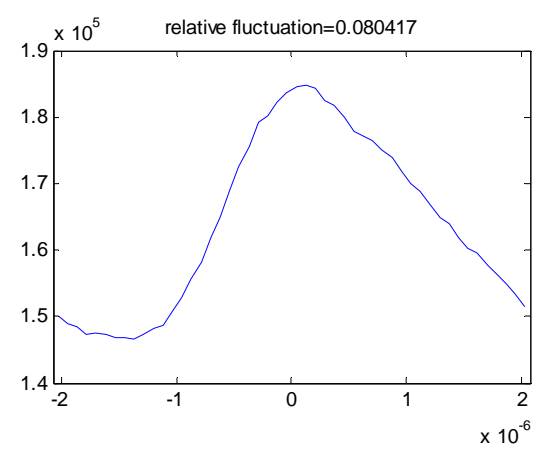
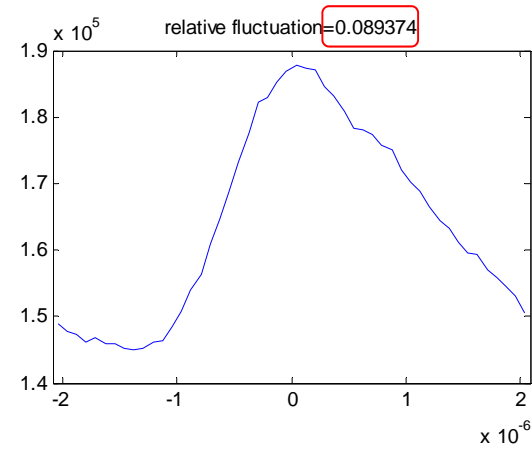
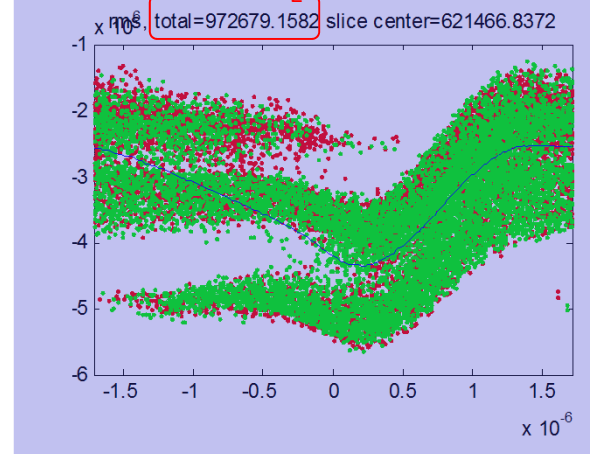
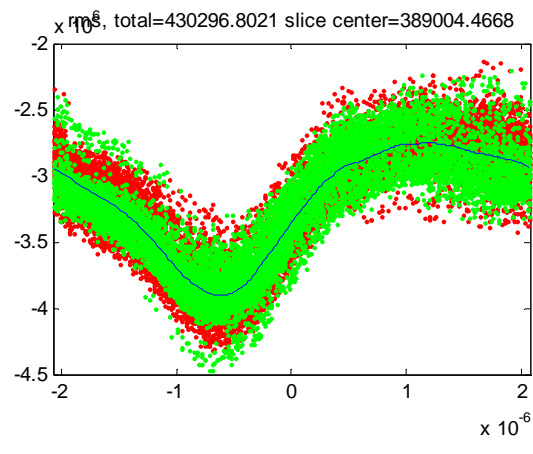
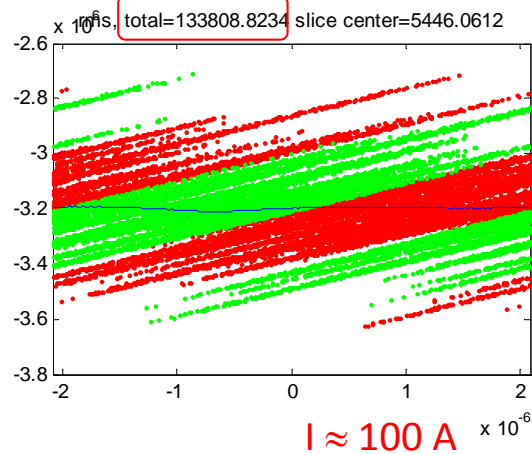


0.3mm slice with center at s=2.5mm (small energy spread, I=13.1 A)

resolution = 50

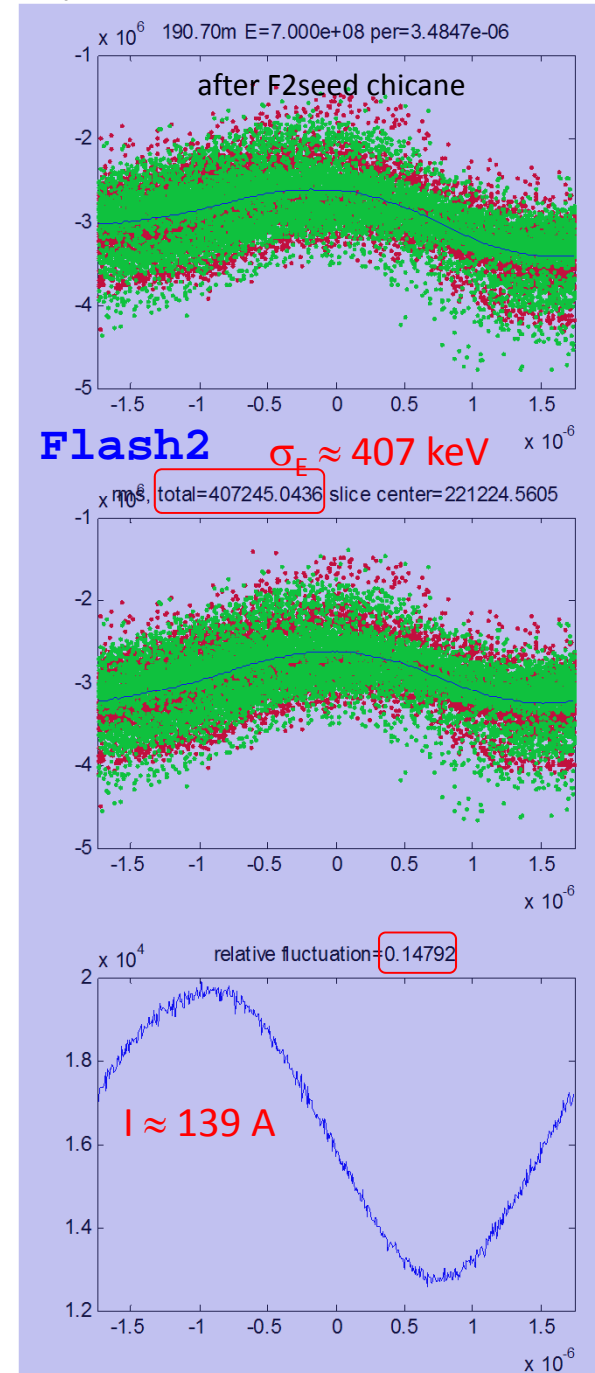
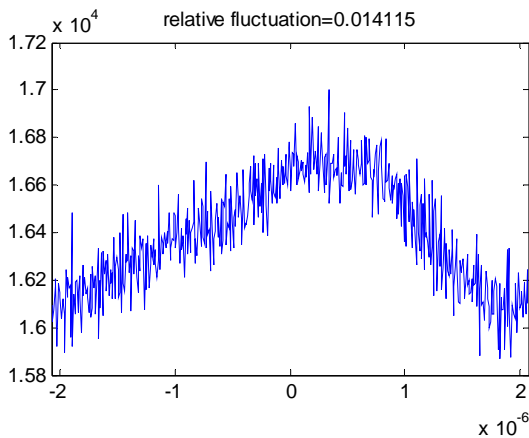
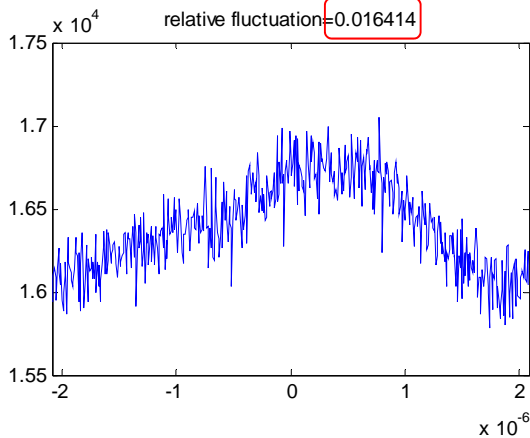
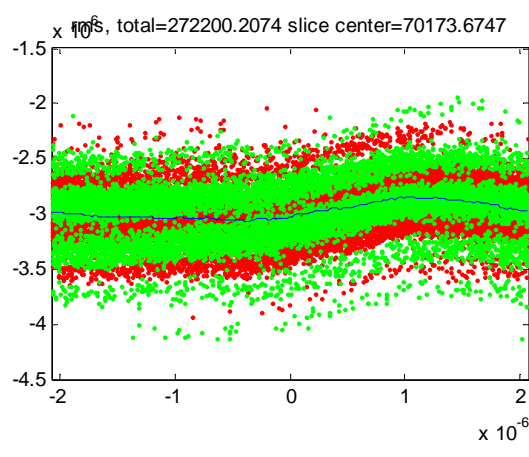
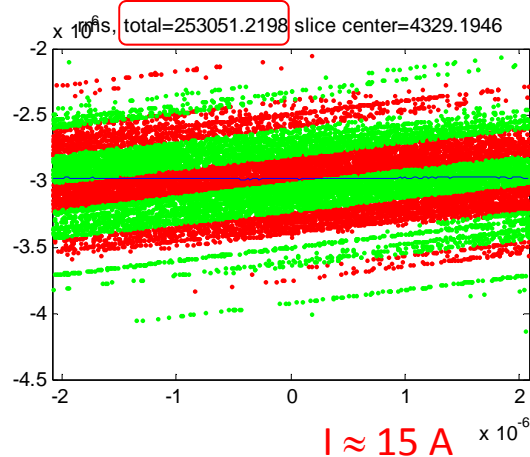
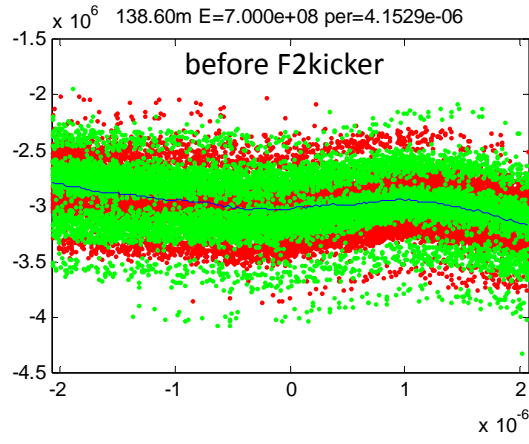
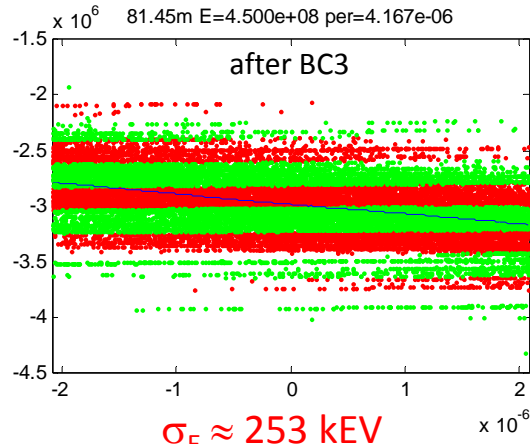


Flash2 $\sigma_E \approx 972$ keV



0.3mm slice with center at s=2.5mm (small energy spread, I=13.1 A)

resolution = 500



one stage LG

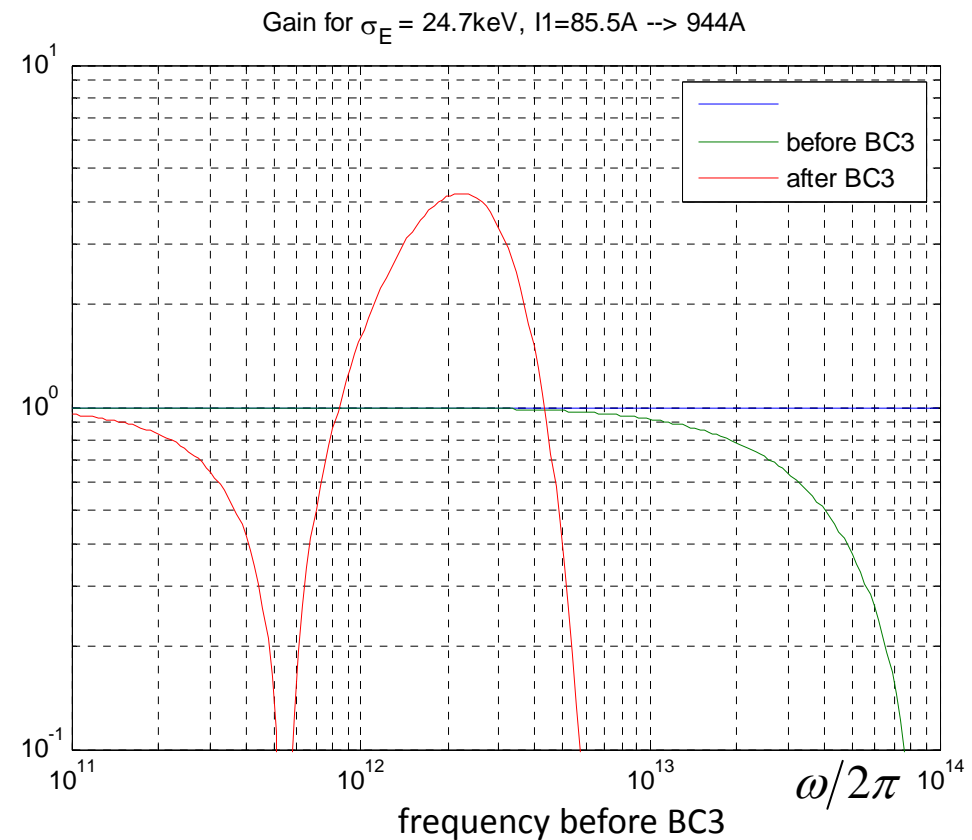
impedance (exit_BC2 --> start BC3) + R56_BC3

0.3mm slice with center at s=2.5mm
(small energy spread, I=13.1 A)

```
>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 11.0409
Ctot*current_0 = 944
rms energy spread = 24692.2283 <-- total energy spread from LGM before BC3!
rms energy spread @ end = 272625.3041
maximal gain = 6.4391
integral(gain^2,domega) = 2.102e+14
Cnoise = Ctot*sqrt(...) = 0.33401
```

maximal gain ≈ 4.2 @ 2.5 THz
--> 11 μm after BC3
780 μm before BC2 !

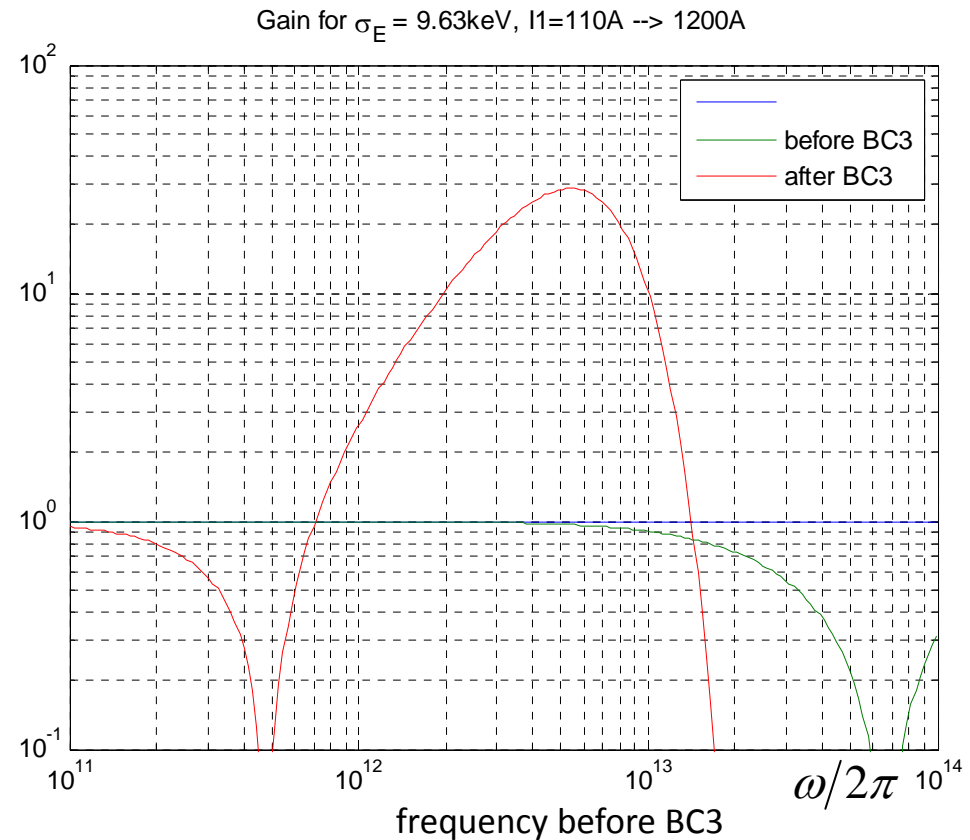
this is the macroscopic scale!



0.3mm slice with center at s=0mm
(~1keV energy spread, I=17.6 A)

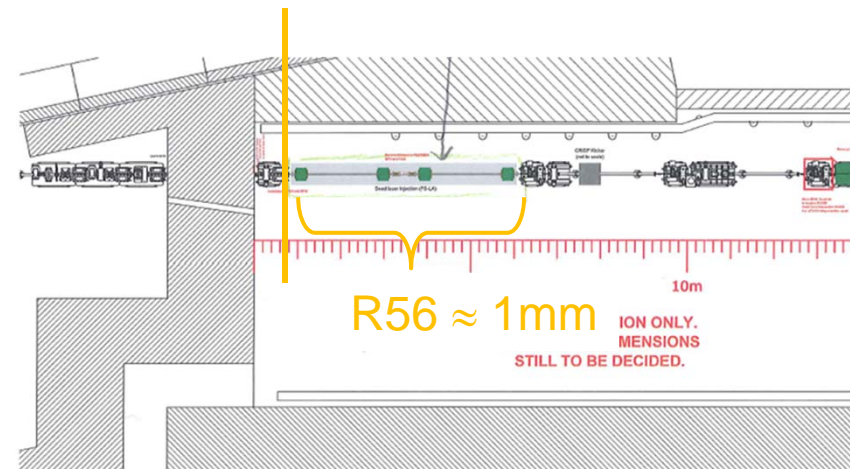
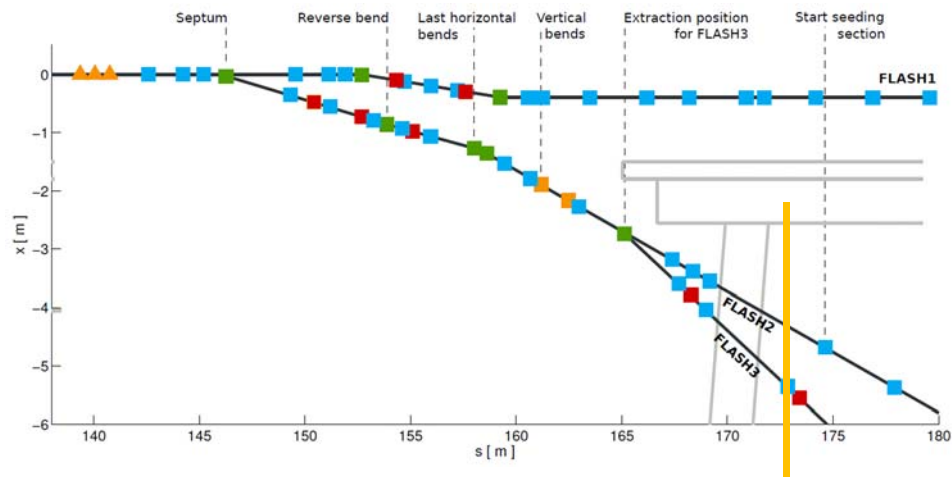
```
>> main_LGM
setup finished
number of frequency points = 200
integral equation finished
Ctot = 10.9091
Ctot*current_0 = 1200
rms energy spread = 9626.9945 <-- total energy spread from LGM before BC3!
rms energy spread @ end = 105021.7585
maximal gain = 28.6818
integral(gain^2,domega) = 2.572e+16
Cnoise = Ctot*sqrt(...) = 4.1412
```

maximal gain ≈ 28 @ 5.5 THz
--> 5 μm after BC3
340 μm before BC2 !



one stage LG

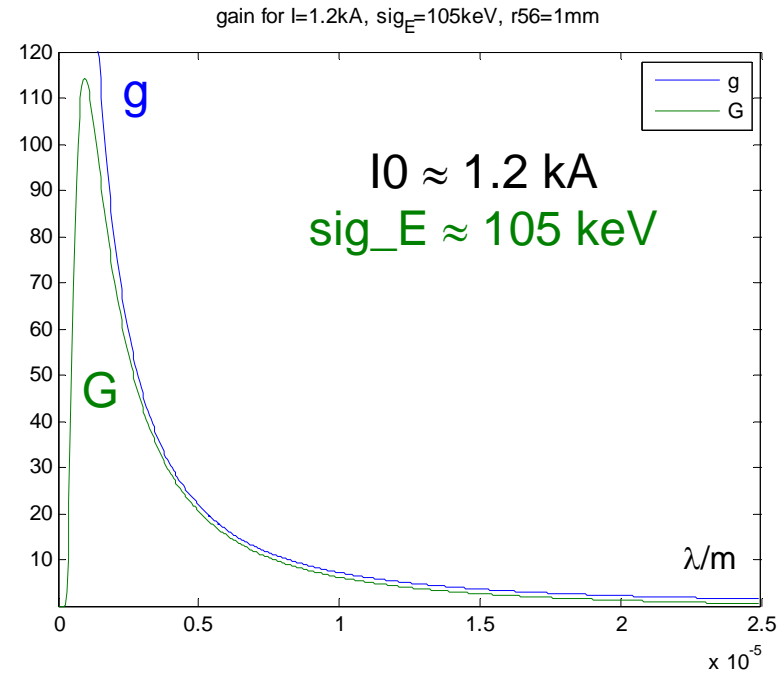
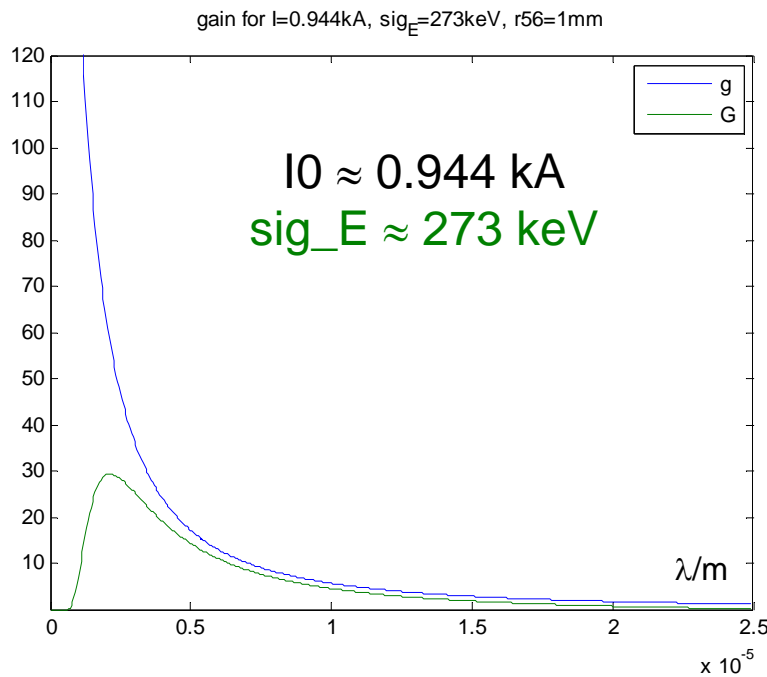
impedance (exit_BC3 --> 172m) + R56_seed



one-stage amplification

$$G = \left(1 - \underbrace{i \frac{Cr_{56}}{\mathcal{E}_{\text{ref}}/e} I_1 k_1 L_{sc} Z'(ck_1)}_g \right) \exp \left(-\frac{(Ck_1 r_{56} \sigma_\delta)^2}{2} \right)$$

impedance from 81m (450 MeV) --> 172.4 m (700 MeV)
 r56 = 1 mm



some numbers

total energy spread after BC3, without further effects

$$\sigma_{E,3} = C_2 \sqrt{(C_1 \sigma_{E,i})^2 + \sigma_{E,2}^2}$$

0.3mm slice with center at s=0mm
(~1keV energy spread, I=17.6 A)

0.3mm slice with center at s=2.5mm
(small energy spread, I=13.1 A)

$$C_1 = 110/17.7$$

$$C_1 = 85.5/13.1$$

$$C_2 = 1200/110$$

$$C_2 = 944/85.5$$

$$\sigma_{E,i} = 1 \text{ keV}$$

$$\sigma_{E,i} = 0.25 \text{ keV}$$

$$\sigma_{E,2} = 7.4 \text{ keV}$$

$$\sigma_{E,2} = 25 \text{ keV}$$

particle tracking → 9.6 keV

23 keV

$$\sigma_{E,3} = 105 \text{ keV}$$

$$\sigma_{E,3} = 273 \text{ keV}$$

127 keV

253 keV

further effects after BC3

modulation amplitude (given by maximal period length $300\mu\text{m}/C_{\text{tot}} \approx 4.3\mu\text{m}$)

before F2kicker {

$$I_{\text{mod}} = 70 \text{ A}$$

$$\sigma_{E,4} = 420 \text{ keV}$$

$$|I_{\text{mod}} Z| \approx 400 \text{ keV}$$

$$I_{\text{mod}} = 15 \text{ A}$$

$$\sigma_{E,4} = 270 \text{ keV}$$

$$|I_{\text{mod}} Z| \approx 100 \text{ keV}$$

& amplification in seeding chicane

