

# Semileptonic $bc$ to $cc$ Baryon Decay and Heavy Quark Spin Symmetry

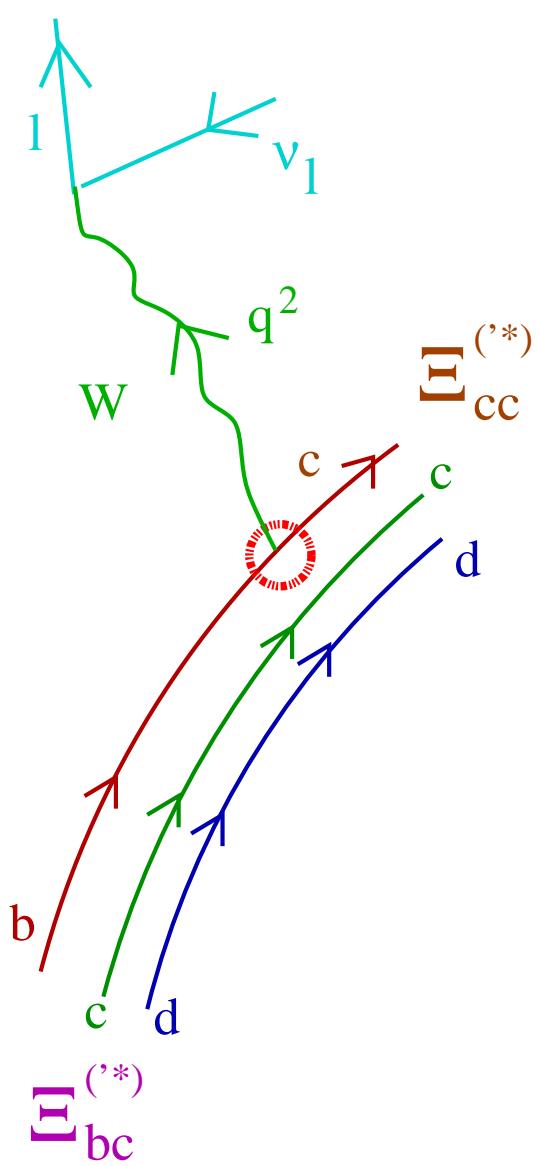
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- arXiv:0706.2805 [hep-ph]: PRD 76 (2007) 017502
- arXiv:0710.1186 [hep-ph]: Submitted to PLB (QM)

**Motivation :** Separate **heavy quark spin symmetries**  
make it possible to describe the **semileptonic decays**

$$\Xi_{bc}^{(\prime*)} \rightarrow \Xi_{cc}^{(*)} l \bar{\nu}_l, \quad \Omega_{bc}^{(\prime*)} \rightarrow \Omega_{cc}^{(*)} l \bar{\nu}_l$$

in the limit  $\mathbf{m}_{b,c} \gg \Lambda_{\text{QCD}}$  and close to the zero recoil point

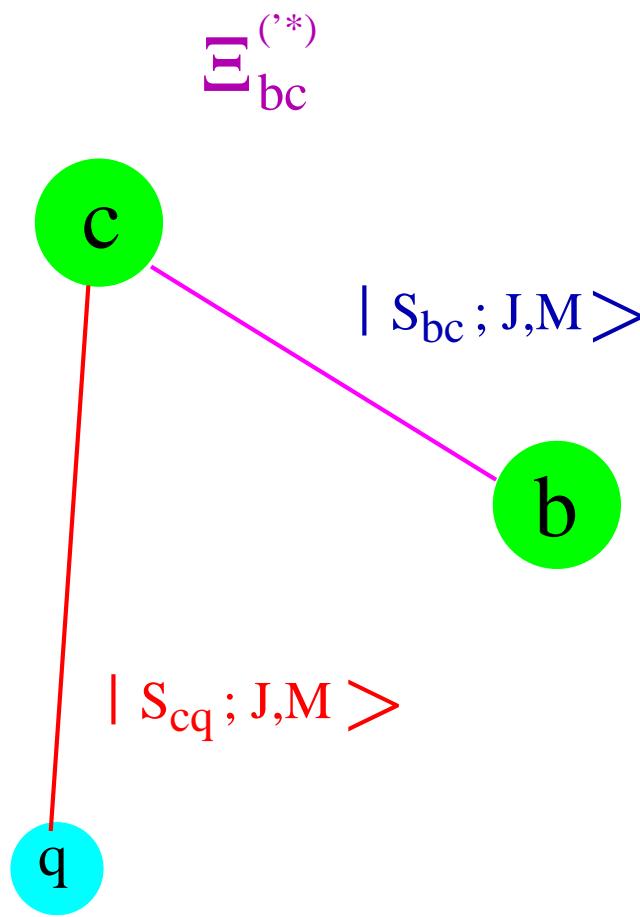


$$\mathbf{q}^2 = m_{bc}^2 + m_{cc}^2 - 2m_{bc}m_{cc}\omega, \quad \boxed{1} \leq \omega \leq \frac{m_{bc}^2 + m_{cc}^2 - m_l^2}{2m_{bc}m_{cc}}$$

zero recoil

	$S$	$J^P$	$I$	$S^\pi_{hh}$		$S$	$J^P$	$I$	$S^\pi_{hh'}$		
$\Xi_{cc}$	0	$\frac{1}{2}^+$	$\frac{1}{2}$	$\mathbf{1}^+$	$ccl$	$\Xi'_{bc}$	$0$	$\frac{1}{2}^+$	$\frac{1}{2}$	$\mathbf{0}^+$	$bcl$
$\Xi_{cc}^*$	0	$\frac{3}{2}^+$	$\frac{1}{2}$	$\mathbf{1}^+$	$ccl$	$\Xi_{bc}$	$0$	$\frac{1}{2}^+$	$\frac{1}{2}$	$\mathbf{1}^+$	$bcl$
$\Omega_{cc}$	-1	$\frac{1}{2}^+$	0	$\mathbf{1}^+$	$ccs$	$\Xi_{bc}'$	$0$	$\frac{3}{2}^+$	$\frac{1}{2}$	$\mathbf{1}^+$	$bcl$
$\Omega_{cc}^*$	-1	$\frac{3}{2}^+$	0	$\mathbf{1}^+$	$ccs$	$\Omega'_{bc}$	-1	$\frac{1}{2}^+$	0	$\mathbf{0}^+$	$bcs$
$\Xi_{bb}$	0	$\frac{1}{2}^+$	$\frac{1}{2}$	$\mathbf{1}^+$	$bbl$	$\Omega_{bc}$	-1	$\frac{1}{2}^+$	0	$\mathbf{1}^+$	$bcs$
$\Xi_{bb}^*$	0	$\frac{3}{2}^+$	$\frac{1}{2}$	$\mathbf{1}^+$	$bbl$	$\Omega_{bc}^*$	-1	$\frac{3}{2}^+$	0	$\mathbf{1}^+$	$bcs$
$\Omega_{bb}$	-1	$\frac{1}{2}^+$	0	$\mathbf{1}^+$	$bbs$						
$\Omega_{bb}^*$	-1	$\frac{3}{2}^+$	0	$\mathbf{1}^+$	$bbs$						

HQS constraints on SL FF's and  $\Gamma$ 's of doubly heavy baryons.



For instance, let us study  $\Xi_{bc}^{(*)} \rightarrow \Xi_{cc}^{(*)}$  SL decays,

$$p_\mu = m_{\Xi_{bc}^{(*)}} \mathbf{v}_\mu, \quad p'_\mu = m_{\Xi_{cc}^{(*)}} v'_\mu = m_{\Xi_{cc}^{(*)}} \mathbf{v}_\mu + \mathbf{k}_\mu$$

Near the zero-recoil point  $\omega = 1$  ( $\omega = \mathbf{v} \cdot \mathbf{v}'$ ) **k small residual momentum**  $\Rightarrow \mathbf{k} \cdot \mathbf{v} = \mathcal{O}(1/m_{\Xi_{cc}^{(*)}})$ .

To represent the **lowest-lying S-wave  $bcq$  baryons** we use **wavefunctions comprising tensor products of Dirac matrices and spinors**, namely:

$$\begin{aligned} \mathbf{B}'_{bc} &= - \left[ \frac{(1+\psi)}{2} \gamma_5 \right]_{\alpha\beta} u_\gamma(v, r) \\ \mathbf{B}_{bc} &= \left[ \frac{(1+\psi)}{2} \gamma_\mu \right]_{\alpha\beta} \left[ \frac{1}{\sqrt{3}} (v^\mu + \gamma^\mu) \gamma_5 u(v, r) \right]_\gamma \\ \mathbf{B}_{bc}^* = \Xi_{bc}^* &= \left[ \frac{(1+\psi)}{2} \gamma_\mu \right]_{\alpha\beta} u_\gamma^\mu(v, r) \end{aligned}$$

$\alpha, \beta, \gamma$  Dirac indices and  $r$  baryon helicity label. These **wavefunctions** can be considered as **matrix elements of the form**  $\langle 0 | c_\alpha \bar{q}^c \beta b_\gamma | B_{bc}^{(*)} \rangle$  where  $\bar{q}^c = q^T C$  with  $C$  the charge-conjugation matrix.

Under a Lorentz ( $\Lambda$ ), and  $b$  and  $c$  quark spin ( $S_b$  and  $S_c$ ) transformations, **a wavefunction**  $\Gamma_{\alpha\beta} u_\gamma$  transforms as:

$$\begin{aligned}\Gamma u &\rightarrow S(\Lambda)\Gamma S^{-1}(\Lambda) S(\Lambda)u \\ \Gamma u &\rightarrow S_c \Gamma S_b u\end{aligned}$$

**States** normalised using  $\bar{u}u\text{Tr}(\Gamma\bar{\Gamma})$ : **mutually orthogonal and have a common normalisation** ( $\bar{\Gamma} = \gamma^0\Gamma^\dagger\gamma^0$ ). States where the  $b$  and  $c$  quarks are coupled to definite spin,

$$\begin{aligned}|\mathbf{S}_{bc} = 0; J = \frac{1}{2}\rangle &= -\frac{1}{2}|S_{cq} = 0; J = \frac{1}{2}\rangle + \frac{\sqrt{3}}{2}|S_{cq} = 1; J = \frac{1}{2}\rangle \\ |\mathbf{S}_{bc} = 1; J = \frac{1}{2}\rangle &= \frac{\sqrt{3}}{2}|S_{cq} = 0; J = \frac{1}{2}\rangle + \frac{1}{2}|S_{cq} = 1; J = \frac{1}{2}\rangle \\ |\mathbf{S}_{bc} = 1; J = \frac{3}{2}\rangle &= |S_{cq} = 1; J = \frac{3}{2}\rangle\end{aligned}$$

## Remarks:

- We have not used definite spin combinations directly for the  $b$  and  $c$  quarks. The reason is **to make both the spin transformations on the heavy quarks and the Lorentz transformation of the states convenient**, making it straightforward to build spin-invariant and Lorentz covariant quantities.
- **We could have combined the  $b$  quark with the light quark to a definite spin.** This would clearly interchange the spin transformations and alter the appearance of spin-invariant and Lorentz covariant quantities. **Physical results should of course be unchanged.**

For the  $cc$  baryons,

$$\begin{aligned} \mathbf{B}'_{cc} &= -\sqrt{\frac{2}{3}} \left[ \frac{(1+\psi)}{2} \gamma_5 \right]_{\alpha\beta} u_\gamma(v, r) \\ \mathbf{B}_{cc} &= \sqrt{2} \left[ \frac{(1+\psi)}{2} \gamma_\mu \right]_{\alpha\beta} \left[ \frac{1}{\sqrt{3}} (v^\mu + \gamma^\mu) \gamma_5 u(v, r) \right]_\gamma \\ \mathbf{B}_{cc}^* = \Xi_{cc}^* &= \sqrt{\frac{1}{2}} \left[ \frac{(1+\psi)}{2} \gamma_\mu \right]_{\alpha\beta} u_\gamma^\mu(v, r) \end{aligned}$$

- the two charm quarks can only be in a symmetric spin-1 state:  $B'_{cc}$  and  $B_{cc}$  correspond to the same baryon state  $\Xi_{cc}$ .
- normalisation: there are two ways to contract the charm quark indices, leading to  $\bar{u}u \text{Tr}(\Gamma \bar{\Gamma}) + \bar{u} \Gamma \bar{\Gamma} u$ . To have the same normalisation as for the  $bc$  case, we have to **include extra numerical factors**

... construct spin-invariant and Lorentz covariant amplitudes for the weak transition matrix elements,

SL  $\Xi_{bc}^{(*)} \rightarrow \Xi_{cc}^{(*)}$  decays  $\leftrightarrow$  ME **weak current**  $J^\mu = \bar{c}\gamma^\mu(1-\gamma_5)b$

We first build transition amplitudes between the  $B_{bc}^{(*)}$  and  $\Xi_{cc}^{(*)}$  states and subsequently take linear combinations to obtain transitions from  $\Xi_{bc}^{(*)}$  states. **The most general form for the ME respecting the HQSS is** ( $j^\mu = \gamma^\mu(1 - \gamma_5)$ ):

$$\begin{aligned} \langle \Xi_{cc}^{(*)}, v, k, M' | J^\mu(0) | B_{bc}^{(*)}, v, M \rangle &= \bar{u}_{cc}(v, k, M') j^\mu u_{bc}(v, M) \text{Tr}[\Gamma_{bc} \Omega \bar{\Gamma}_{cc}] \\ &\quad + \bar{u}_{cc}(v, k, M') \Gamma_{bc} \Omega \bar{\Gamma}_{cc} j^\mu u_{bc}(v, M) \end{aligned}$$

$$\begin{aligned} \Gamma_{bc} &\rightarrow S_c \Gamma_{bc}, \quad u_{bc} \rightarrow S_b u_{bc} \\ \bar{\Gamma}_{cc} &\rightarrow \bar{\Gamma}_{cc} S_c^\dagger, \quad \bar{u}_{cc} \rightarrow \bar{u}_{cc} S_c^\dagger \\ \bar{c} j^\mu b : j^\mu &\rightarrow S_c j^\mu S_b^\dagger \end{aligned}$$

... construct spin-invariant and Lorentz covariant amplitudes for the weak transition matrix elements,

SL  $\Xi_{bc}^{(*)} \rightarrow \Xi_{cc}^{(*)}$  decays  $\leftrightarrow$  ME **weak current**  $J^\mu = \bar{c}\gamma^\mu(1-\gamma_5)b$

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$$\begin{aligned} \langle \Xi_{cc}^{(*)}, v, k, M' | J^\mu(0) | B_{bc}^{(*)}, v, M \rangle &= \bar{u}_{cc}(v, k, M') S_c^\dagger S_c j^\mu S_b^\dagger S_b u_{bc}(v, M) \text{Tr}[S_c \Gamma_{bc} \Omega \bar{\Gamma}_{cc} S_c^\dagger] \\ &\quad + \bar{u}_{cc}(v, k, M') S_c^\dagger S_c \Gamma_{bc} \Omega \bar{\Gamma}_{cc} S_c^\dagger S_c j^\mu S_b^\dagger S_b u_{bc}(v, M) \end{aligned}$$

$$\Gamma_{bc} \rightarrow S_c \Gamma_{bc}, \quad u_{bc} \rightarrow S_b u_{bc}$$

$$\bar{\Gamma}_{cc} \rightarrow \bar{\Gamma}_{cc} S_c^\dagger, \quad \bar{u}_{cc} \rightarrow \bar{u}_{cc} S_c^\dagger$$

$$\bar{c} j^\mu b : j^\mu \rightarrow S_c j^\mu S_b^\dagger$$

where  $M$  and  $M'$  are the helicities of the initial and final states

$$\Omega = -\frac{1}{\sqrt{2}} \eta (\mathbf{v} \cdot \mathbf{v}')$$

is the most general Dirac matrix that can be written in terms of the vectors  $k$  and  $v$ .

- terms with a factor of  $\psi$  can be omitted because of the equations of motion ( $\psi u = u$ ,  $\psi \Gamma = \Gamma$ ,  $\gamma_\mu u^\mu = 0$ ,  $v_\mu u^\mu = 0$ ),
- terms with  $\not{k}$  will always lead to contributions proportional to  $v \cdot k = \mathcal{O}(1/m_{\Xi_{cc}^{(*)}})$ .

$\Xi_{bc} \rightarrow \Xi_{cc}$	$\eta \bar{u}_{cc} \left( 2\gamma^\mu - \frac{4}{3}\gamma^\mu\gamma_5 \right) u_{bc}$
$\Xi'_{bc} \rightarrow \Xi_{cc}$	$\frac{-2}{\sqrt{3}}\eta \bar{u}_{cc} \left( -\gamma^\mu\gamma_5 \right) u_{bc}$
$\Xi_{bc} \rightarrow \Xi^*_{cc}$	$\frac{-2}{\sqrt{3}}\eta \bar{u}_{cc}^\mu u_{bc}$
$\Xi'_{bc} \rightarrow \Xi^*_{cc}$	$-2\eta \bar{u}_{cc}^\mu u_{bc}$
$\Xi^*_{bc} \rightarrow \Xi_{cc}$	$\frac{-2}{\sqrt{3}}\eta \bar{u}_{cc} u_{bc}^\mu$
$\Xi^*_{bc} \rightarrow \Xi^*_{cc}$	$-2\eta \bar{u}_{cc}^\lambda \left( \gamma^\mu - \gamma^\mu\gamma_5 \right) u_{bc\lambda}$

## Remarks:

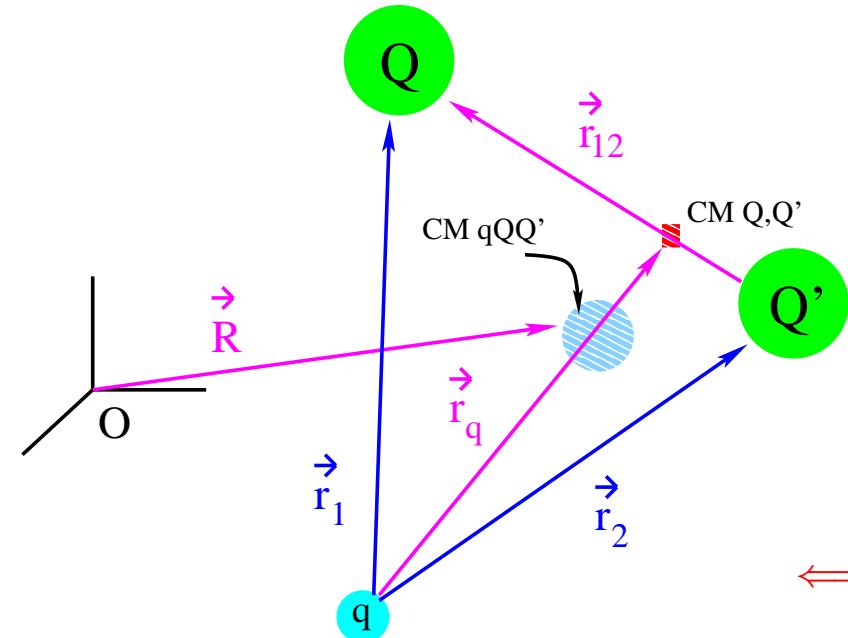
- If the  $b$  and  $c$  quarks become degenerate, then vector current conservation ensures that  $\eta(1) = 1$ .
- **Savage and White (PLB 271 (1991) 410)** found similar results: approach where the two heavy quarks bind into a colour antitriplet which appears as a pointlike colour source to the light degrees of freedom + “**superflavor**” formalism of Georgi and Wise. We find two differences to their results (one of these was already pointed out by Sanchis-Lozano PLB 321 (1994) 407).
- Our approach, where we consider the spin transformations of each heavy quark explicitly, is **straightforward and similar** to that used to describe  **$B_c$  meson decays**: Jenk-

ins, Luke, Manohar and Savage, NPB 390 (1993) 463.

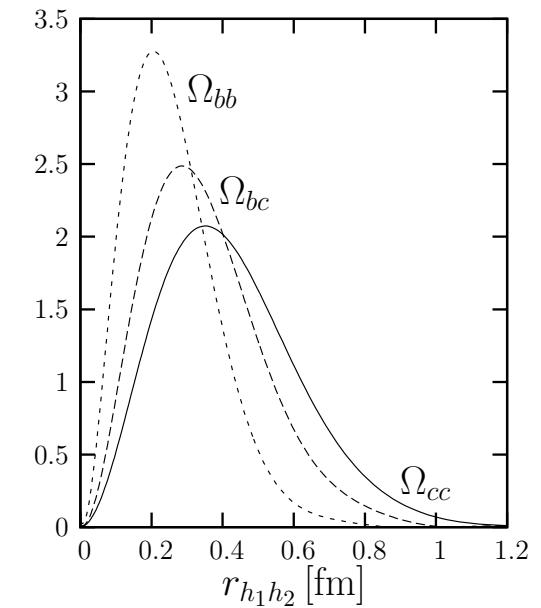
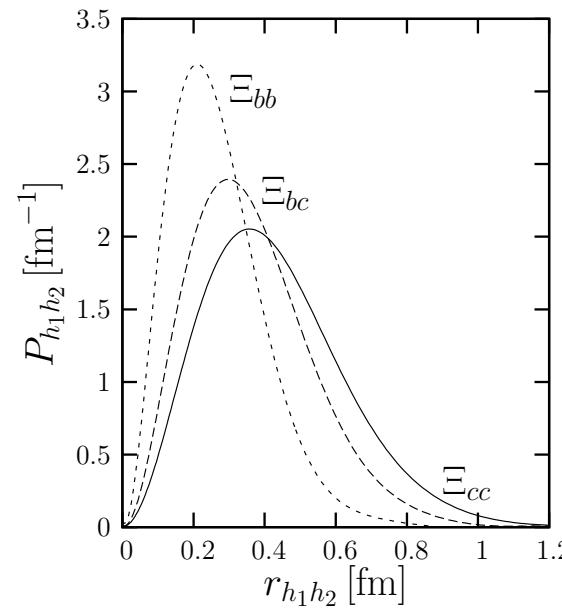
- **Spin symmetry** for both the  $b$  and  $c$  quarks **enormously simplifies** the description of all  $\Xi_{bc}^{(\prime*)} \rightarrow \Xi_{cc}^{(*)} l \bar{\nu}_l$  decays in the heavy quark limit and near the zero recoil point. **All the weak transition matrix elements are given in terms of a single universal function.** Lorentz covariance alone allows a large number of form factors (six form factors to describe  $\Xi_{bc} \rightarrow \Xi_{cc}$ , another six for  $\Xi'_{bc} \rightarrow \Xi_{cc}$ , eight each for  $\Xi_{bc} \rightarrow \Xi_{cc}^*$ ,  $\Xi'_{bc} \rightarrow \Xi_{cc}^*$  and  $\Xi_{bc}^* \rightarrow \Xi_{cc}$ , and even more for  $\Xi_{bc}^* \rightarrow \Xi_{cc}^*$ ).

Test: QM [EPJA 32 (2007) 183 ]

$$\eta(\mathbf{v} \cdot \mathbf{v}') = \int d^3r_1 d^3r_2 \exp[-i\vec{k} \cdot \vec{r}_{12}/2] [\Psi_{cc}^\Xi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_{12})]^* \Psi_{bc}^\Xi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_{12})$$

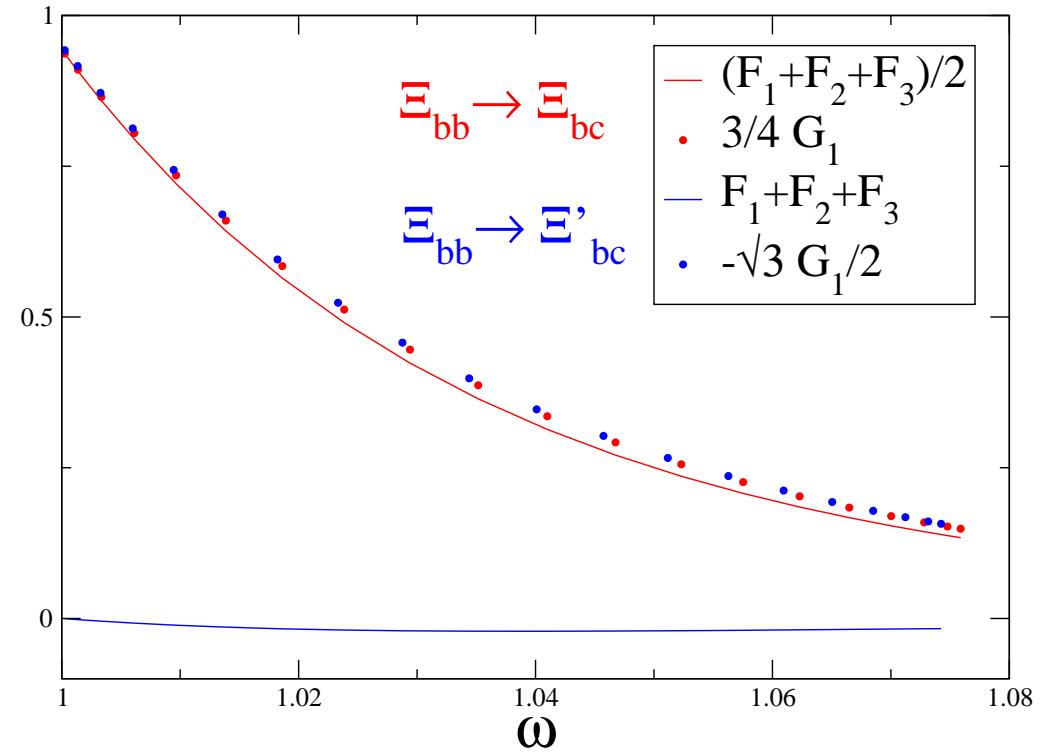
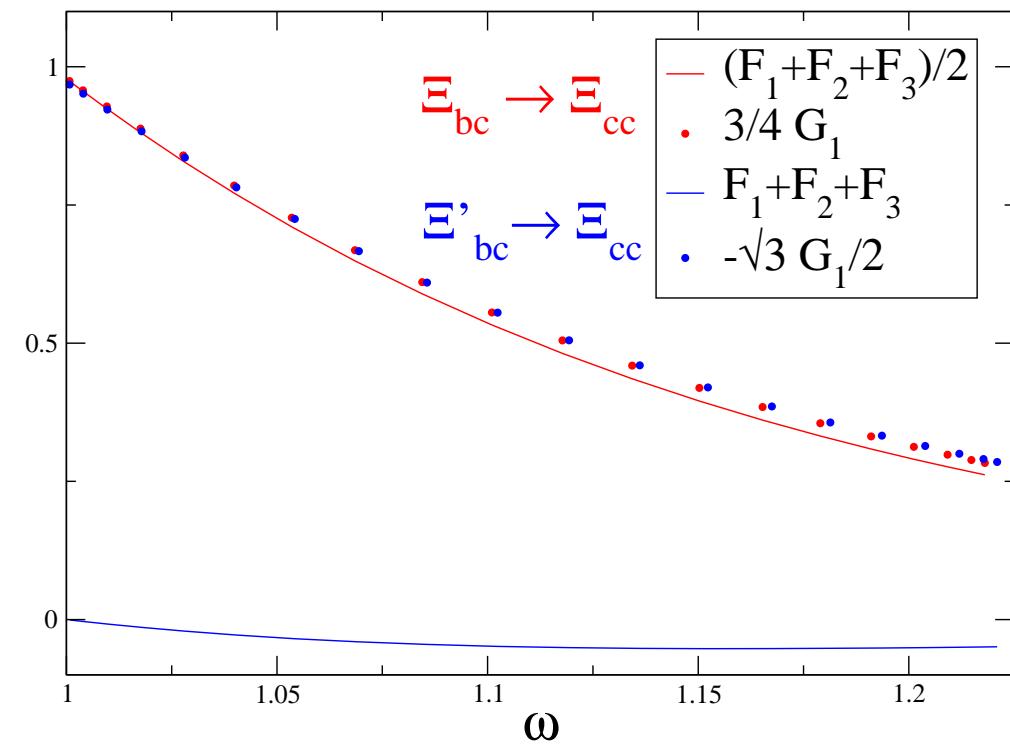


$\Leftarrow$  Jacobi's coordinates,  $Q, Q' = c, b$ .



$$r_{12} \ll r_1, r_2 \rightarrow \Psi_{Qc}^\Xi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_{12}) \approx \underbrace{\Phi_{Qc}(r_{12})}_{\text{RELATIVE MOTION OF } \mathbf{q} \text{ AND A POINTLIKE } \mathbf{Qc} \text{ DIQUARK}} \underbrace{\phi(r_{Qcq})}_{\text{Qc DIQUARK}} \underbrace{\varphi_{Qc}(\vec{r}_{12} \cdot \vec{r}_{Qcq})}_{\text{VARIATIONAL}}$$

$$\begin{aligned}
 \left\langle \Xi_{cc}, r' \vec{p}' \mid \bar{c} \gamma^\mu (1 - \gamma_5) b(0) \mid \Xi_{bc}^{(\prime)}, r \vec{p} \right\rangle = & \bar{u}_{r'}^{\Xi_{cc}}(\vec{p}') \left\{ \gamma^\mu (\mathbf{F}_1(\mathbf{w}) - \gamma_5 \mathbf{G}_1(\mathbf{w})) \right. \\
 & \left. + v^\mu (\mathbf{F}_2(\mathbf{w}) - \gamma_5 \mathbf{G}_2(\mathbf{w})) + v'^\mu (\mathbf{F}_3(\mathbf{w}) - \gamma_5 \mathbf{G}_3(\mathbf{w})) \right\} u_r^{\Xi_{bc}}(\vec{p})
 \end{aligned}$$



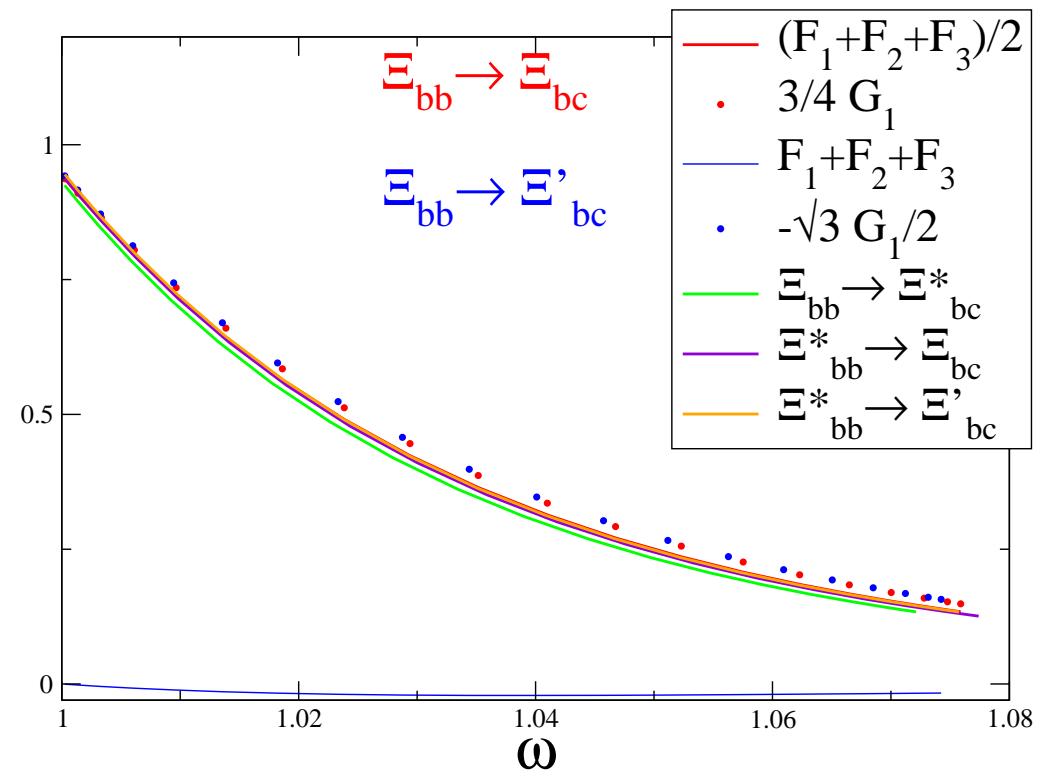
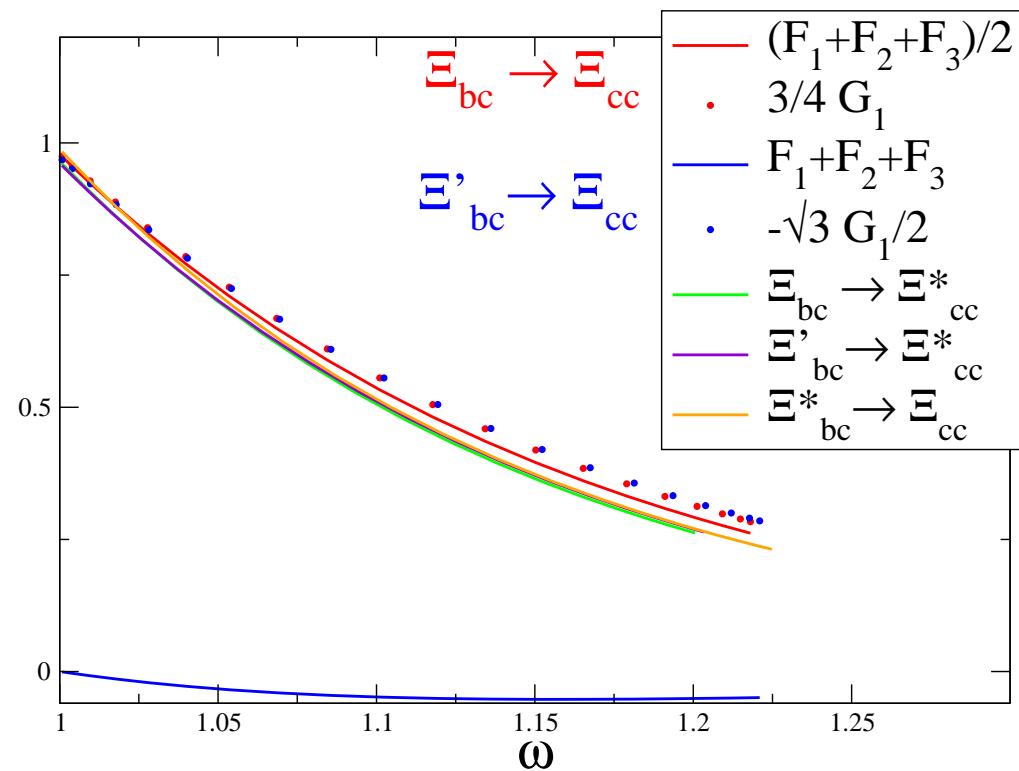
...  $1/2 \rightarrow 3/2$  spin transitions

$$\left\langle \Xi_{cc}^*, r' \vec{p}' | \bar{c} \gamma^\mu (1 - \gamma_5) b(0) | \Xi_{bc}^{(\prime)}, r \vec{p} \right\rangle = \bar{u}_{\lambda r'}^{\Xi_{cc}^*}(\vec{p}') \Gamma^{\lambda \mu} u_r^{\Xi_{bc}^{(\prime)}}(\vec{p})$$

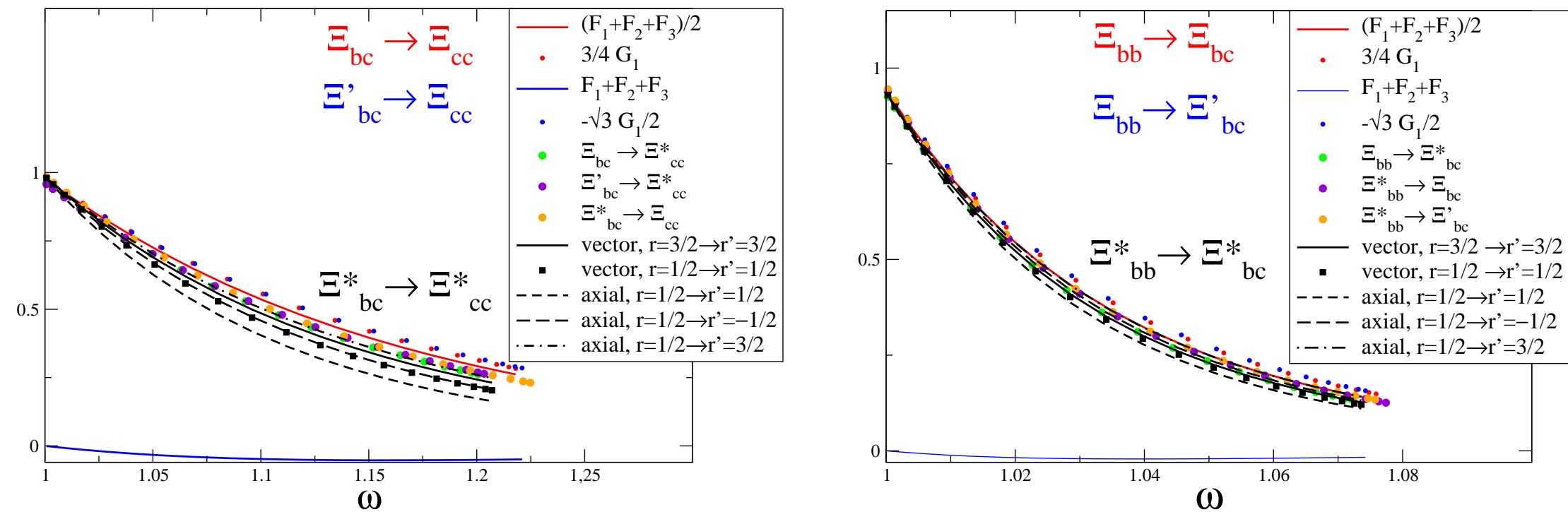
$$\begin{aligned} \Gamma^{\lambda \mu} = & \left( \frac{\mathbf{C}_3^V(\omega)}{m_{\Xi_{bc}^{(\prime)}}} (g^{\lambda \mu} q^\mu - q^\lambda \gamma^\mu) + \frac{\mathbf{C}_4^V(\omega)}{m_{\Xi_{bc}^{(\prime)}}^2} (g^{\lambda \mu} q p' - q^\lambda p'^\mu) \right. \\ & \left. + \frac{\mathbf{C}_5^V(\omega)}{m_{\Xi_{bc}^{(\prime)}}^2} (g^{\lambda \mu} q p - q^\lambda p^\mu) + \mathbf{C}_6^V(\omega) g^{\lambda \mu} \right) \gamma_5 \\ & + \left( \frac{\mathbf{C}_3^A(\omega)}{m_{\Xi_{bc}^{(\prime)}}} (g^{\lambda \mu} q^\mu - q^\lambda \gamma^\mu) + \frac{\mathbf{C}_4^A(\omega)}{m_{\Xi_{bc}^{(\prime)}}^2} (g^{\lambda \mu} q p' - q^\lambda p'^\mu) + \mathbf{C}_5^A(\omega) g^{\lambda \mu} + \frac{\mathbf{C}_6^A(\omega)}{m_{\Xi_{bc}^{(\prime)}}^2} q^\lambda q^\mu \right) \end{aligned}$$

and  $3/2 \rightarrow 1/2$  transitions...

$$\langle \Xi_{cc}, r' \vec{p}' | \bar{c} \gamma^\mu (1 - \gamma_5) b(0) | \Xi_{bc}^*, r \vec{p} \rangle = \bar{u}_{r'}^{\Xi_{cc}}(\vec{p}') \hat{\Gamma}^{\lambda \mu} u_{\lambda, r}^{\Xi_{bc}^*}(\vec{p})$$



and  $3/2 \rightarrow 3/2$  transitions,  $\Xi_{bc}^* \rightarrow \Xi_{cc}^* \sim 50$  FF's



## HQSS constraints on semileptonic decay widths

$$\Gamma = \frac{G_F^2}{32\pi^4} |V_{cb}|^2 \frac{m_{\Xi_{cc}^{(*)}}}{m_{\Xi_{bc}^{(*)}}^2} \int_1^{\omega_{max}} d\omega \sqrt{\omega^2 - 1} \underbrace{\mathcal{L}^{\mu\nu} \mathcal{H}_{\mu\nu}}_{\text{hadron FF's}}$$

$$\begin{aligned} \mathcal{L}^{\mu\nu} &= \int \frac{d^3 k_1}{2E_1} \frac{d^3 k_2}{2E_2} \delta^{(4)}(q - k_1 - k_2) (k_1^\mu k_2^\nu + k_1^\nu k_2^\mu - g^{\mu\nu} k_1 \cdot k_2 + i\epsilon^{\mu\nu\alpha\beta} k_{1\alpha} k_{2\beta}) \\ &= A(q^2) g^{\mu\nu} + B(q^2) \frac{q^\mu q^\nu}{q^2} \end{aligned}$$

For the actual doubly heavy baryon masses  $\omega_{max} \approx 1.22$  (1.08) for  $bc \rightarrow cc$  ( $bb \rightarrow bc$ ) transitions. The different differential decay widths  $d\Gamma/d\omega$  show a maximum at around  $\omega \approx 1.05$  (1.01)  $\Rightarrow$

$$\boxed{\eta(\omega) \rightarrow \mathcal{H}_{\mu\nu}} \quad \text{and approximating}$$

$$m_{\Xi_{bb}} \approx m_{\Xi_{bb}^*} ; \quad m_{\Xi_{bc}} \approx m_{\Xi'_{bc}} \approx m_{\Xi_{bc}^*} ; \quad m_{\Xi_{cc}} \approx m_{\Xi_{cc}^*}$$

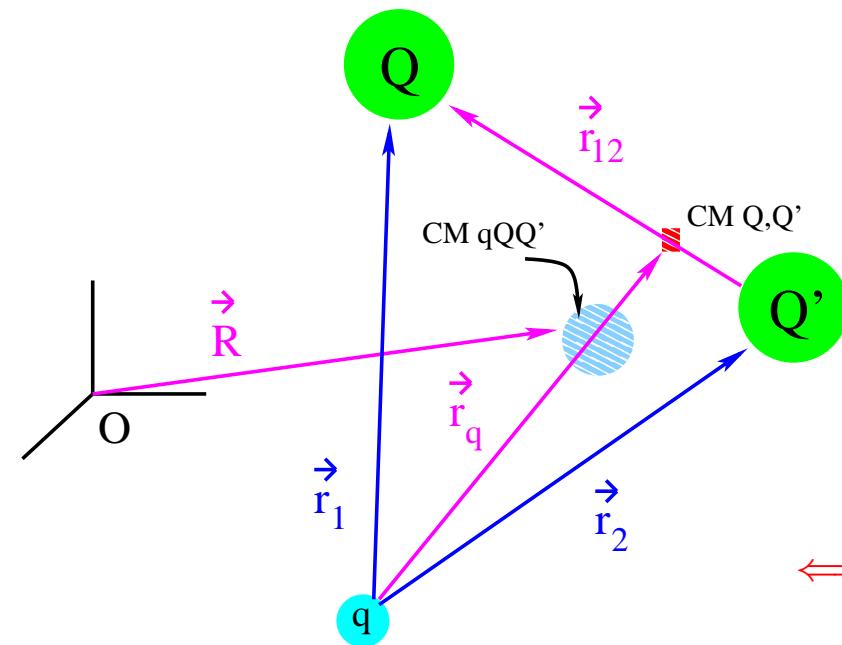
**predict that some ratios between different decay widths  
should be approximately 1...**

$b\bar{c} \rightarrow c\bar{c}$	Hernández et al. arXiv:0706.2805 [hep-ph]	Ebert et al. PRD70 (2004) 014018	Guo et al. PRD58 (1998) 114007	
	$\Xi$	$\Omega$	$\Xi$	$\Omega$
$\frac{\Gamma(B'_{bc} \rightarrow B^*_{cc} l\bar{\nu}_l)}{3 \Gamma(B_{bc} \rightarrow B^*_{cc} l\bar{\nu}_l)}$	$1.04^{+0.03}_{-0.01}$	$1.04^{-0.03}$	0.79	0.82
$\frac{\Gamma(B_{bc} \rightarrow B^*_{cc} l\bar{\nu}_l)}{\frac{2}{3} \Gamma(B'_{bc} \rightarrow B_{cc} l\bar{\nu}_l)}$	$0.82^{+0.06}_{-0.01}$	$0.84^{+0.13}_{-0.01}$	1.22	1.17
$\frac{\Gamma(B^*_{bc} \rightarrow B_{cc} l\bar{\nu}_l)}{\frac{1}{2} \Gamma(B_{bc} \rightarrow B^*_{cc} l\bar{\nu}_l)}$	$1.14^{+0.08}$	$1.16^{+0.04}_{-0.06}$	1.05	1.08
$\frac{\Gamma(B^*_{bc} \rightarrow B^*_{cc} l\bar{\nu}_l)}{\Gamma(B_{bc} \rightarrow B_{cc} l\bar{\nu}_l) + \frac{1}{2} \Gamma(B_{bc} \rightarrow B^*_{cc} l\bar{\nu}_l)}$	$0.89^{+0.11}$	$0.94^{+0.13}_{-0.01}$	1.01	1.01
				1.08

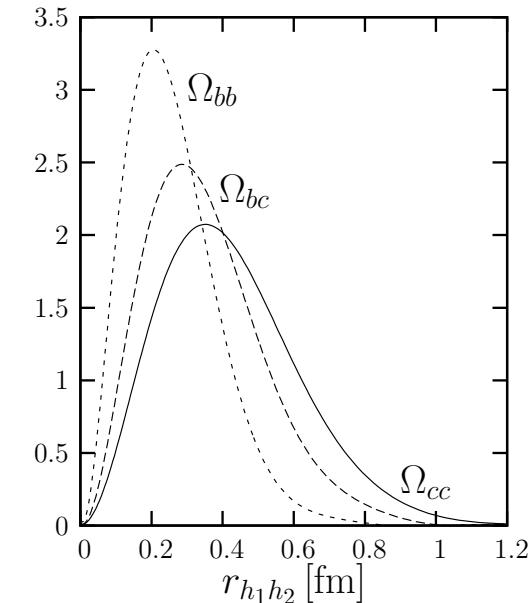
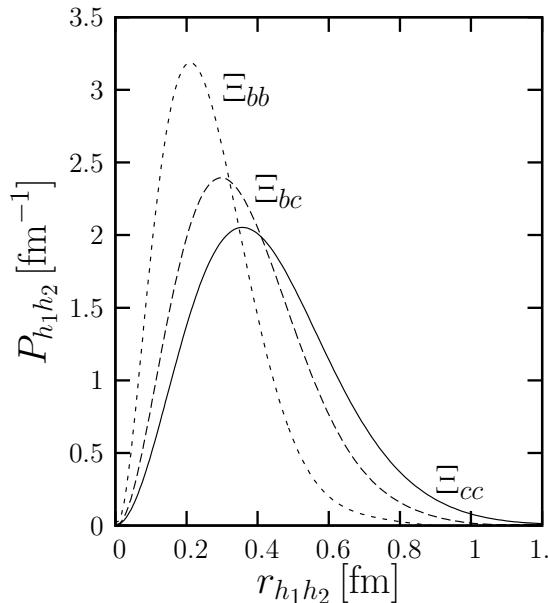
$bb \rightarrow bc$	Hernández et al. arXiv:0706.2805 [hep-ph]	Ebert et al. PRD70 (2004) 014018	Guo et al. PRD58 (1998) 114007			
	$\Xi$	$\Omega$	$\Xi$	$\Omega$	$\Xi$	$\Omega$
$\frac{\Gamma(B_{bb}^* \rightarrow B'_{bc} l\bar{\nu}_l)}{3 \Gamma(B_{bb}^* \rightarrow B_{bc} l\bar{\nu}_l)}$	$1.00^{+0.01}_{-0.04}$	$1.00^{+0.03}_{-0.01}$	0.99	0.99	<b>0.05</b>	—
$\frac{\Gamma(B_{bb} \rightarrow B_{bc}^* l\bar{\nu}_l)}{\frac{2}{3} \Gamma(B_{bb} \rightarrow B'_{bc} l\bar{\nu}_l)}$	$0.86^{+0.08}_{-0.06}$	$0.86^{+0.05}_{-0.05}$	0.96	0.99	<b>9.53</b>	—
$\frac{\Gamma(B_{bb}^* \rightarrow B_{bc} l\bar{\nu}_l)}{\frac{1}{2} \Gamma(B_{bb} \rightarrow B_{bc}^* l\bar{\nu}_l)}$	$1.14^{+0.04}_{-0.05}$	$1.13^{+0.01}_{-0.17}$	1.05	1.04	<b>3.82</b>	—
$\frac{\Gamma(B_{bb}^* \rightarrow B_{bc}^* l\bar{\nu}_l)}{\Gamma(B_{bb} \rightarrow B_{bc} l\bar{\nu}_l) + \frac{1}{2} \Gamma(B_{bb} \rightarrow B_{bc}^* l\bar{\nu}_l)}$	$0.94^{+0.07}_{-0.06}$	$0.93^{+0.11}_{-0.10}$	1.01	1.01	<b>0.31</b>	—

Diquark Picture and Link to  $B_c$  Meson Decays

$$\eta(\mathbf{v} \cdot \mathbf{v}') = \int d^3r_1 d^3r_2 \exp[-i\vec{k} \cdot \vec{r}_{12}/2] [\Psi_{cc}^\Xi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_{12})]^* \Psi_{bc}^\Xi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_{12})$$



$\Leftarrow$  Jacobi's coordinates,  $Q, Q' = c, b$ .



$$r_{12} \ll r_1, r_2 \rightarrow \Psi_{Qc}^\Xi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_{12}) \approx \underbrace{\Phi_{Qc}(r_{12})}_{\text{RELATIVE MOTION OF } \mathbf{q} \text{ AND A POINTLIKE } \mathbf{Qc} \text{ DIQUARK}} \underbrace{\phi(r_{Qcq})}_{\text{Qc DIQUARK}} \underbrace{\varphi_{Qc}(\vec{r}_{12} \cdot \vec{r}_{Qcq})}_{\text{VARIATIONAL} \approx 1}$$

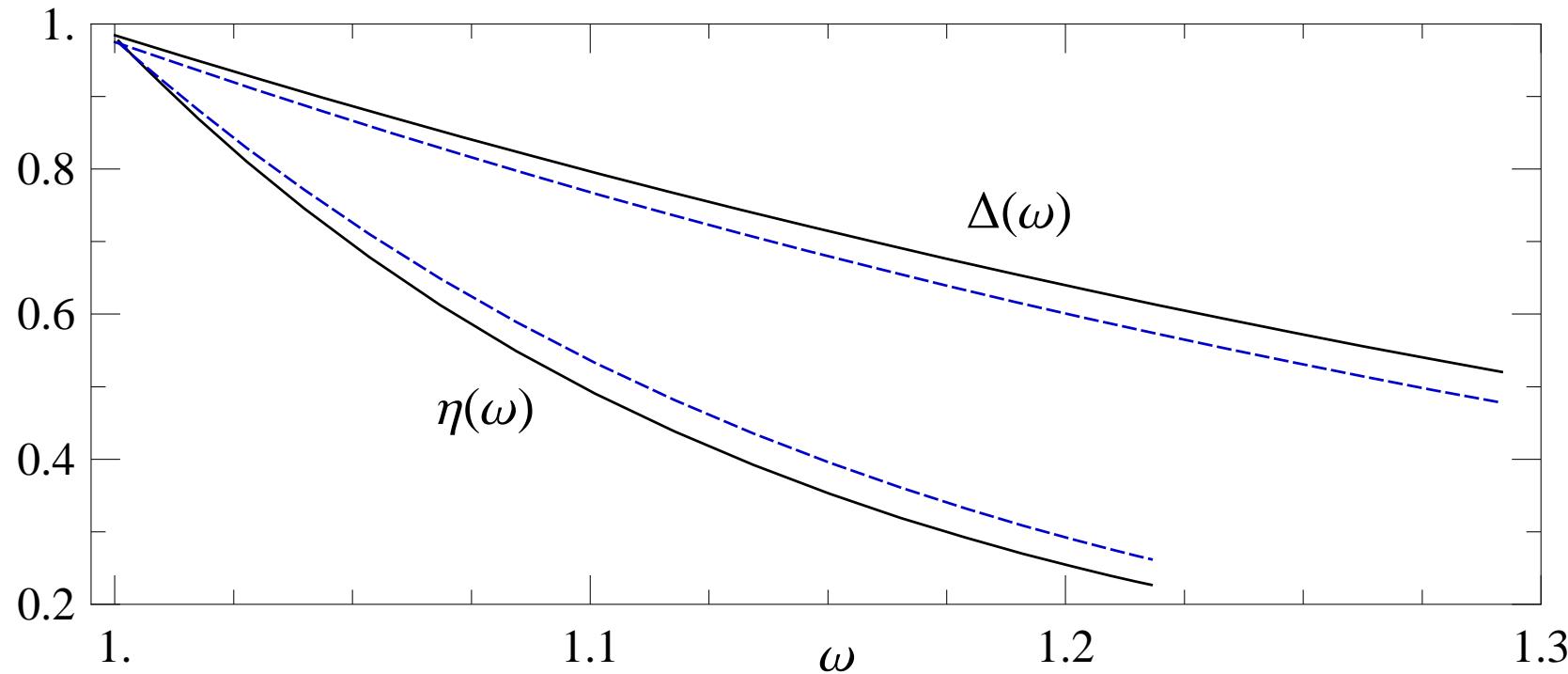
$$\eta(\mathbf{v} \cdot \mathbf{v}') = \int d^3\mathbf{r}_{12} \exp[-ik \cdot \vec{\mathbf{r}}_{12}/2] [\Phi_{cc}(\mathbf{r}_{12})]^* \Phi_{bc}(\mathbf{r}_{12}) \underbrace{\int d^3r \phi^*(r) \phi(r)}_1$$

where  $\vec{r} = \vec{r}_{ccq}$  and in the  $d^3r$  integral we have replaced  $\phi(r_{bcq})$  by  $\phi(r)$  since  $\vec{r}_{bcq} = \vec{r}_{ccq} + \mathcal{O}(\vec{r}_{12})$ . **This approximation leads to uncertainties of  $\mathcal{O}(r_{12}^2)$  after integration,**

$$\eta(\mathbf{v} \cdot \mathbf{v}') = \int d^3\mathbf{r}_{12} \exp[-ik \cdot \mathbf{r}_{12}/2] [\Phi_{cc}(\mathbf{r}_{12})]^* \Phi_{bc}(\mathbf{r}_{12})$$

which has an **identical form to the expression of the form factor  $\Delta$ , unique form factor which describes the  $B_c$  to  $\eta_c$  and  $J/\psi$  semileptonic decays**, in terms of wavefunctions of the  $\bar{b}c$  and  $\bar{c}c$  bound states (Jenkins et al., NPB 390 (1993) 463).

This does not mean that  $\eta$  and  $\Delta$  are identical because the  $QQ$  and  $Q\bar{Q}$  potentials used to compute the diquark and meson wavefunctions are not the same. For example a  $\lambda_i \lambda_j$  colour dependence ( $\lambda_i$  are the usual Gell-Mann matrices) would lead to  $V^{QQ} = V^{Q\bar{Q}}/2$ . [approx wfnt overlaps (solid lines) vs IW funcs (dashed lines)]



The  $\omega^2$  slope of the  $\Delta$  form factor is indeed smaller than that of  $\eta$ , but the ratio is around 1 to 3 rather than 1 to 6, so there are significant corrections to the Coulomb wavefunction description.

## Conclusions

- Separate HQSS make it possible to describe all SL

$$\Xi_{bc}^{(\prime*)} \rightarrow \Xi_{cc}^{(*)} l \bar{\nu}_l, \quad \Omega_{bc}^{(\prime*)} \rightarrow \Omega_{cc}^{(*)} l \bar{\nu}_l$$

decays using a single form factor. Similarly for  $bb \rightarrow bc$  decays.

- We have discussed the resemblance of the  $bc$  baryon decays to those of  $B_c$  mesons to  $\eta_c$  and  $J/\psi$  mesons

- Lattice QCD simulations work best near the zero-recoil point and thus are well-suited to check the validity of the results.
- QM calculations consistent with HQSS ?
  - Results by Hernández et al. (FF's and decay width ratios), and Ebert et al. (decay width ratios), compare well, within expectations with HQSS
  - We detect problems either in the model or in the calculation performed by Guo et al.