

**HERA end of data taking**

**2<sup>nd</sup> anniversary symposium - July 7<sup>th</sup>, 2009 - DESY**

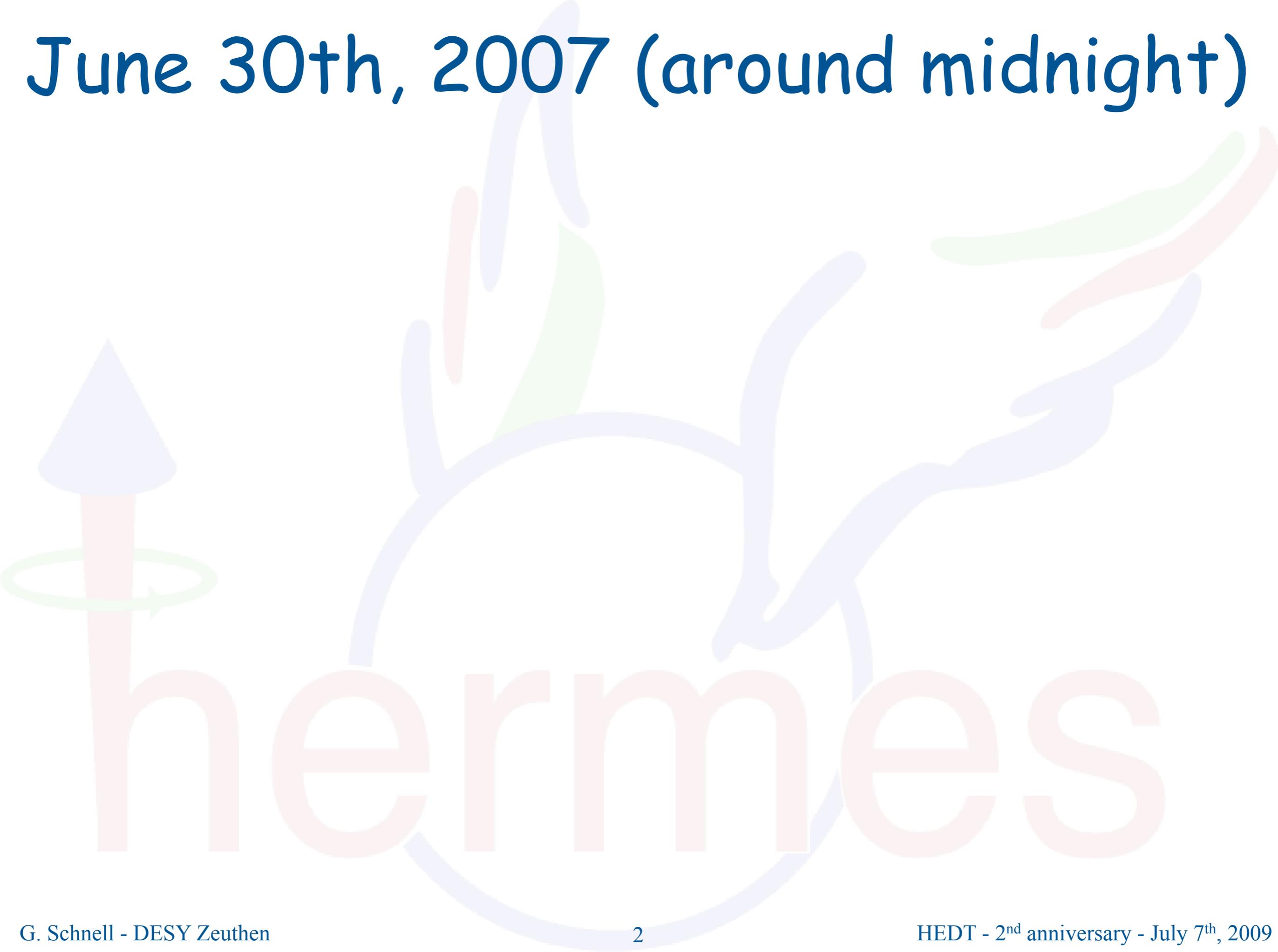
**from solving the spin “crisis”  
to 3-D pictures of the nucleon**

selected highlights from the  **hermes** collaboration

**Gunar.Schnell @ desy.de**  
**DESY Zeuthen**



June 30th, 2007 (around midnight)

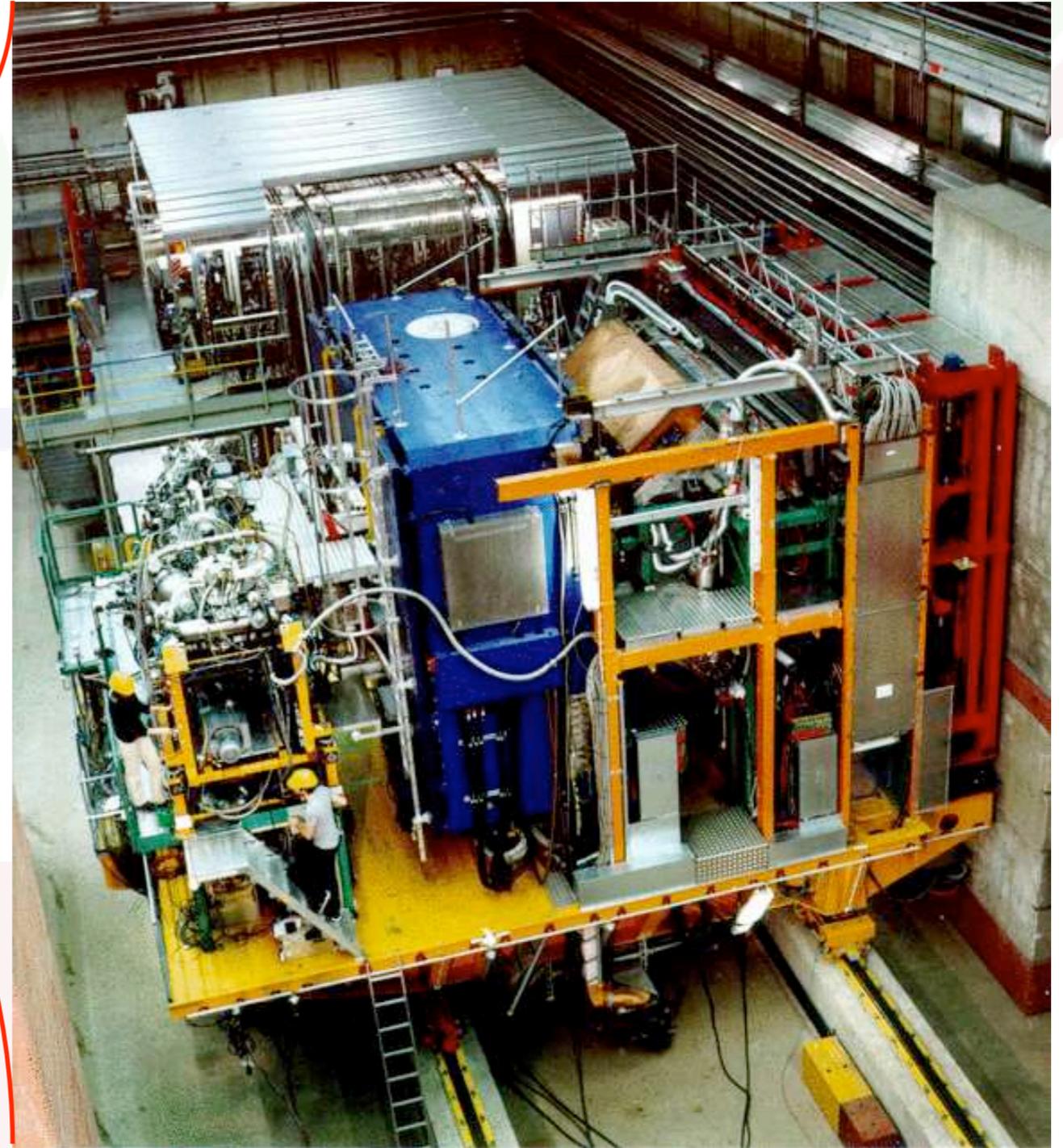


# June 30th, 2007 (around midnight)



# The HERMES experiment

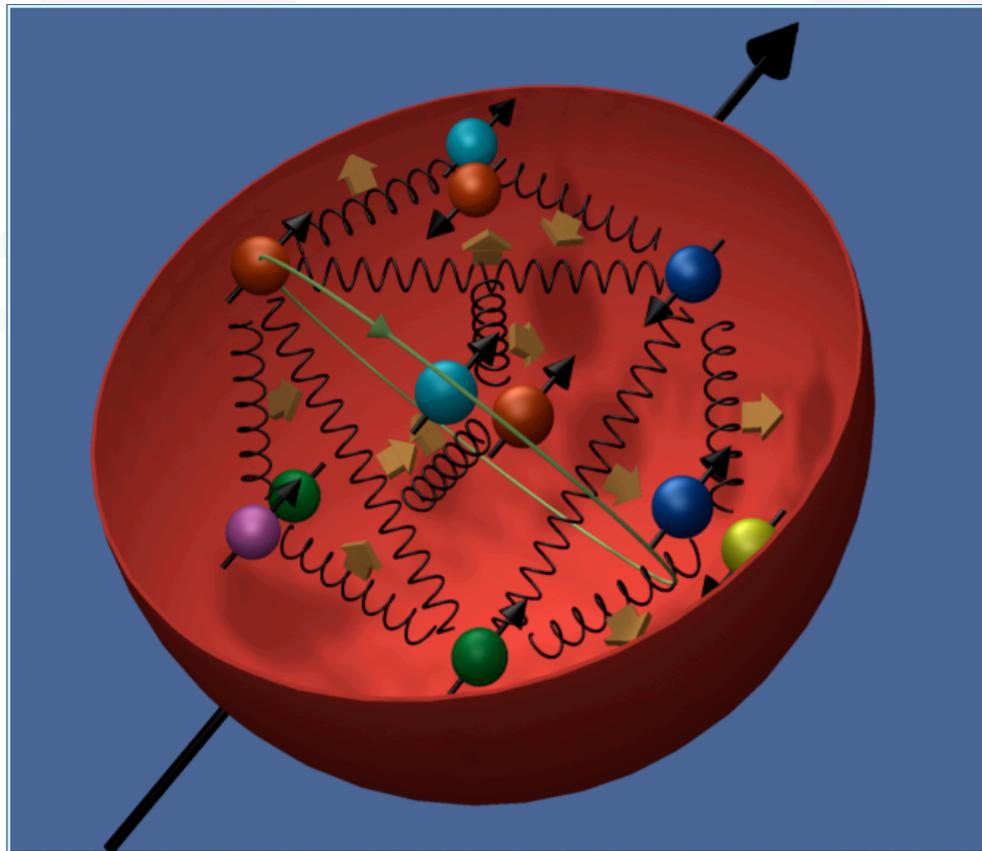
27.5 GeV  $e^+/e^-$  beam of HERA



transversely/longitudinally  
polarized as well as unpolarized  
internal gas targets  
(H, D, He, N, ..., Xe)

# The (original) quest: proton spin

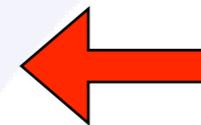
our understanding of the proton changed dramatically with the finding of EMC that the proton spin hardly comes from spin of quarks



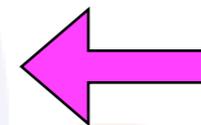
$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma$$

$$+ \Delta G$$

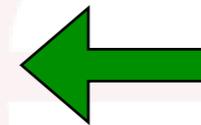
$$+ L_q + L_g$$



quark spin



gluon spin

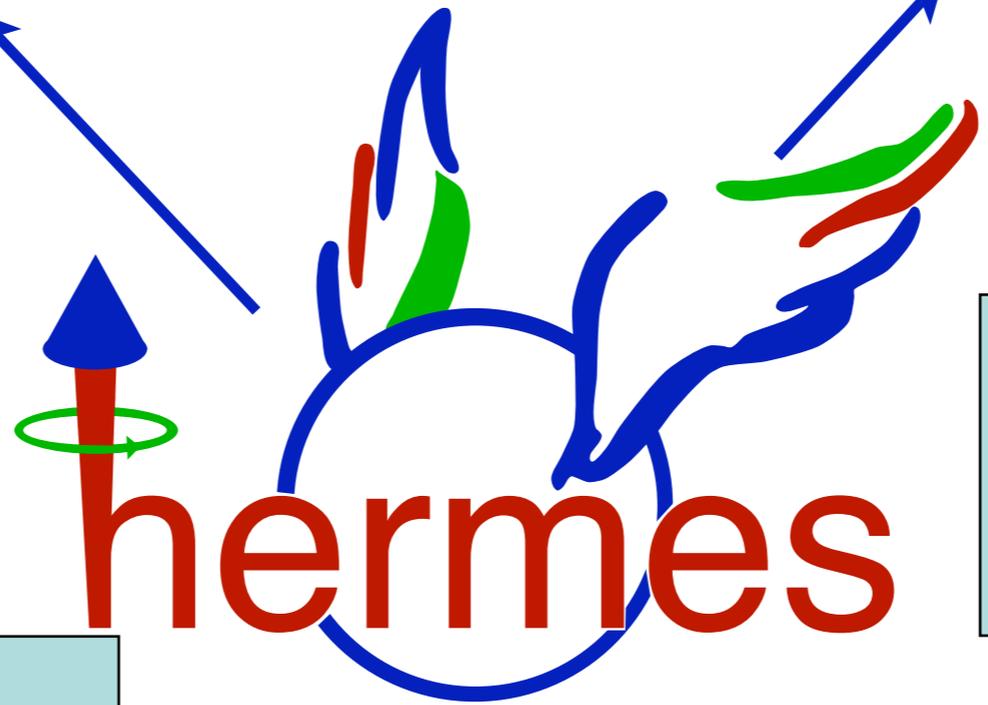


orbital angular momentum

*Longitudinal Spin/  
Momentum Structure,  
Hadronization*

*Transverse Spin/  
Momentum  
Structure*

DVCS



**Transversity  
TMDs**

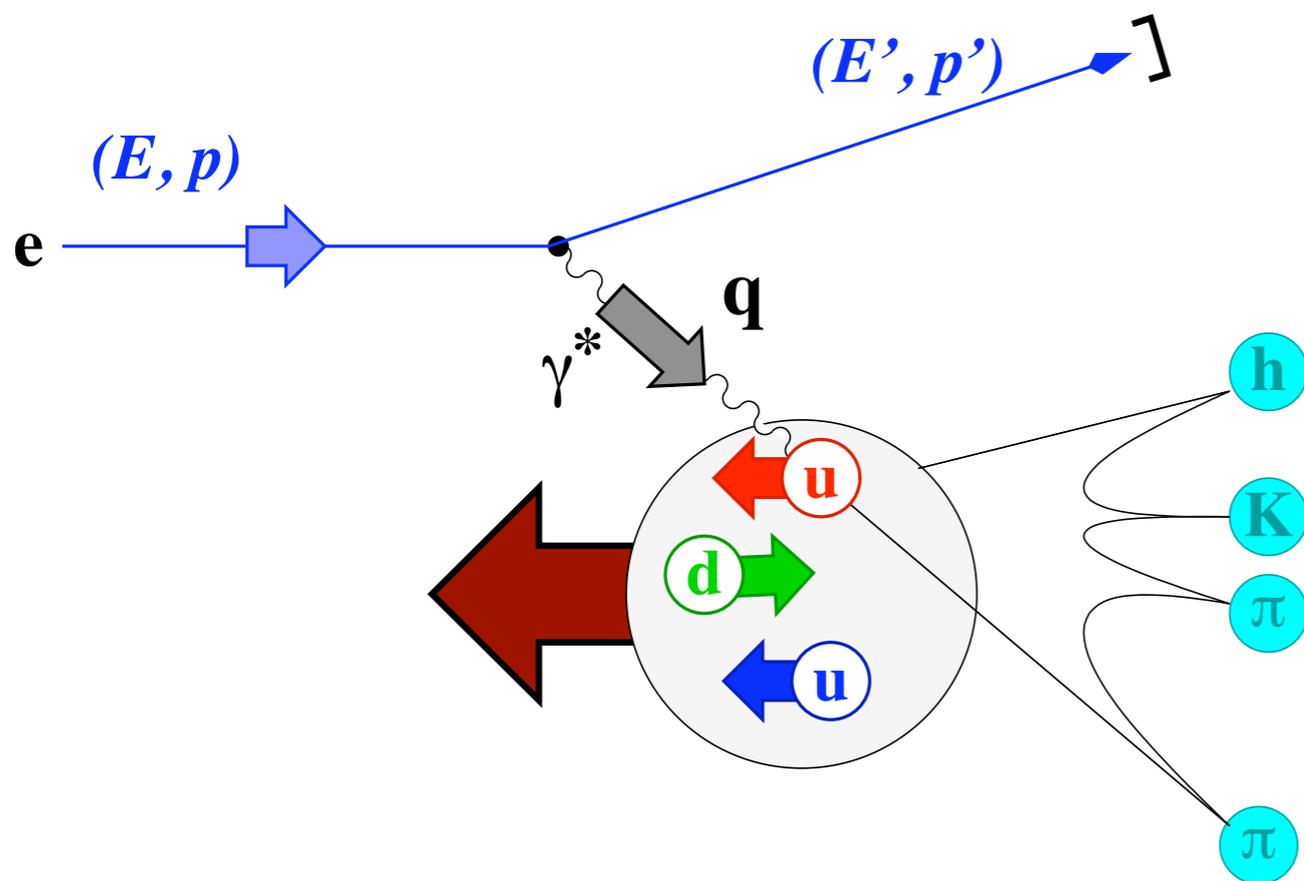
**GPDs  
“Nucleon Tomography”**

*Exclusive Meson  
Production*

*Strange-Baryon  
Production*

# Deep-Inelastic Scattering

use well-known probe to study hadronic structure:

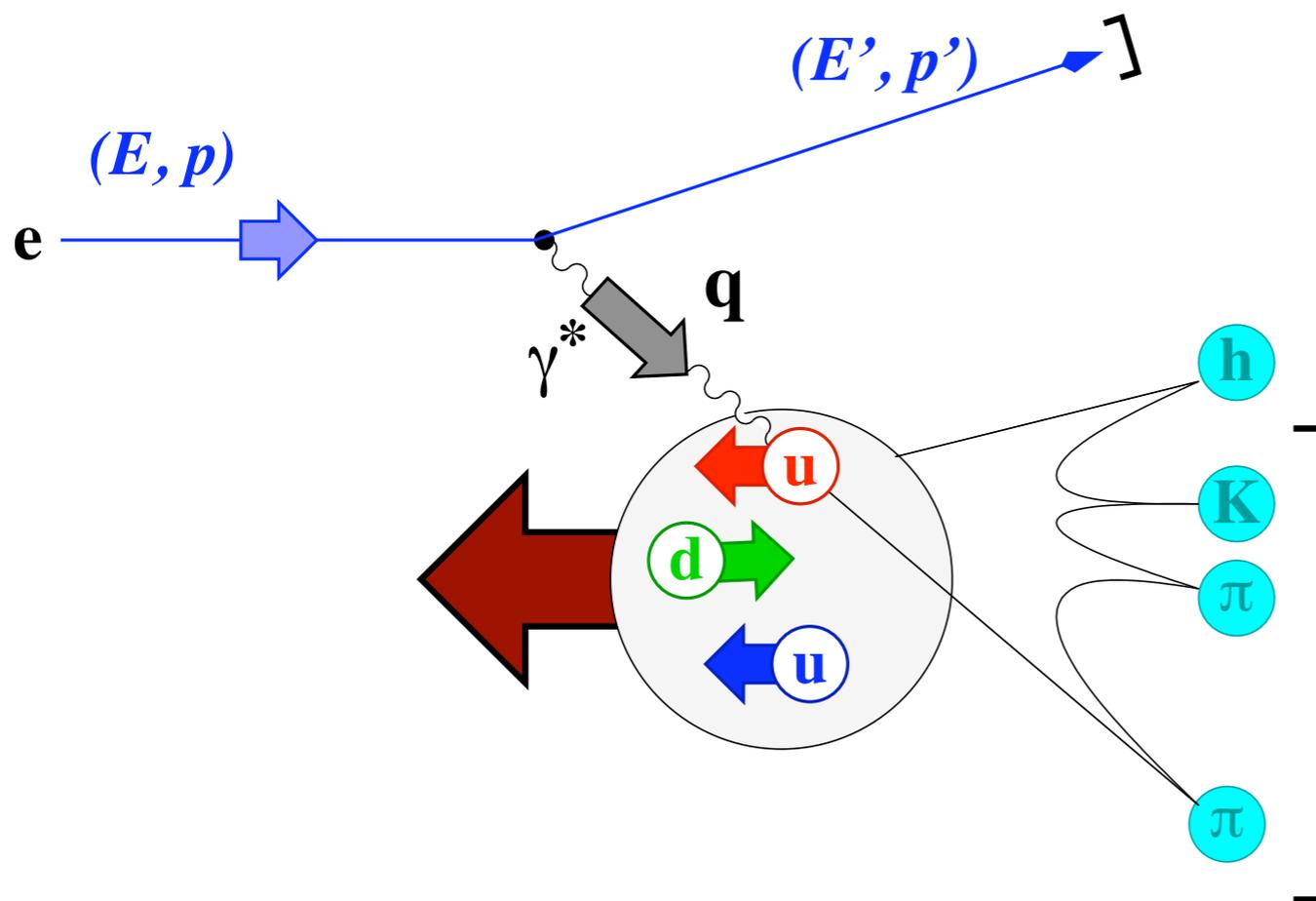


$Q^2$	$\stackrel{\text{lab}}{=}$	$4EE' \sin^2\left(\frac{\Theta}{2}\right)$
$\nu$	$\stackrel{\text{lab}}{=}$	$E - E'$
$W^2$	$\stackrel{\text{lab}}{=}$	$M^2 + 2M\nu - Q^2$
$y$	$\stackrel{\text{lab}}{=}$	$\frac{\nu}{E}$
$x$	$\stackrel{\text{lab}}{=}$	$\frac{Q^2}{2M\nu}$

**inclusive DIS: detect scattered lepton**

# Deep-Inelastic Scattering

use well-known probe to study hadronic structure:



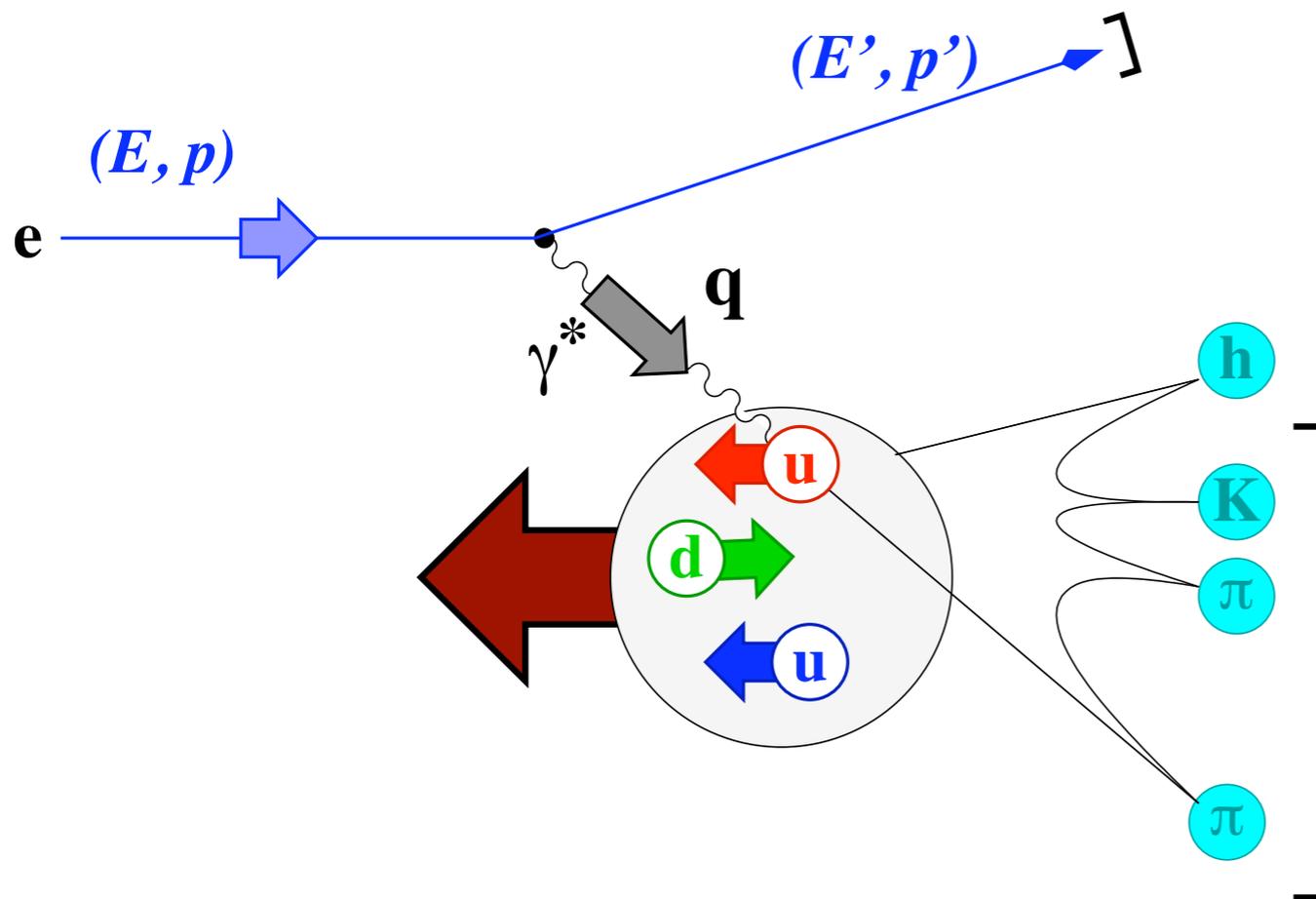
$Q^2$	$\stackrel{\text{lab}}{=}$	$4EE' \sin^2\left(\frac{\Theta}{2}\right)$
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$W^2$	$\stackrel{\text{lab}}{=}$	$M^2 + 2M\nu - Q^2$
$y$	$\stackrel{\text{lab}}{=}$	$\frac{\nu}{E}$
$x$	$\stackrel{\text{lab}}{=}$	$\frac{Q^2}{2M\nu}$
$z$	$\stackrel{\text{lab}}{=}$	$\frac{E_h}{\nu}$

**inclusive DIS: detect scattered lepton**

**semi-inclusive DIS: detect scattered lepton and some fragments**

# Deep-Inelastic Scattering

use well-known probe to study hadronic structure:



$Q^2$	$\stackrel{\text{lab}}{=}$	$4EE' \sin^2\left(\frac{\Theta}{2}\right)$
$\nu$	$\stackrel{\text{lab}}{=}$	$E - E'$
$W^2$	$\stackrel{\text{lab}}{=}$	$M^2 + 2M\nu - Q^2$
$y$	$\stackrel{\text{lab}}{=}$	$\frac{\nu}{E}$
$x$	$\stackrel{\text{lab}}{=}$	$\frac{Q^2}{2M\nu}$
$z$	$\stackrel{\text{lab}}{=}$	$\frac{E_h}{\nu}$

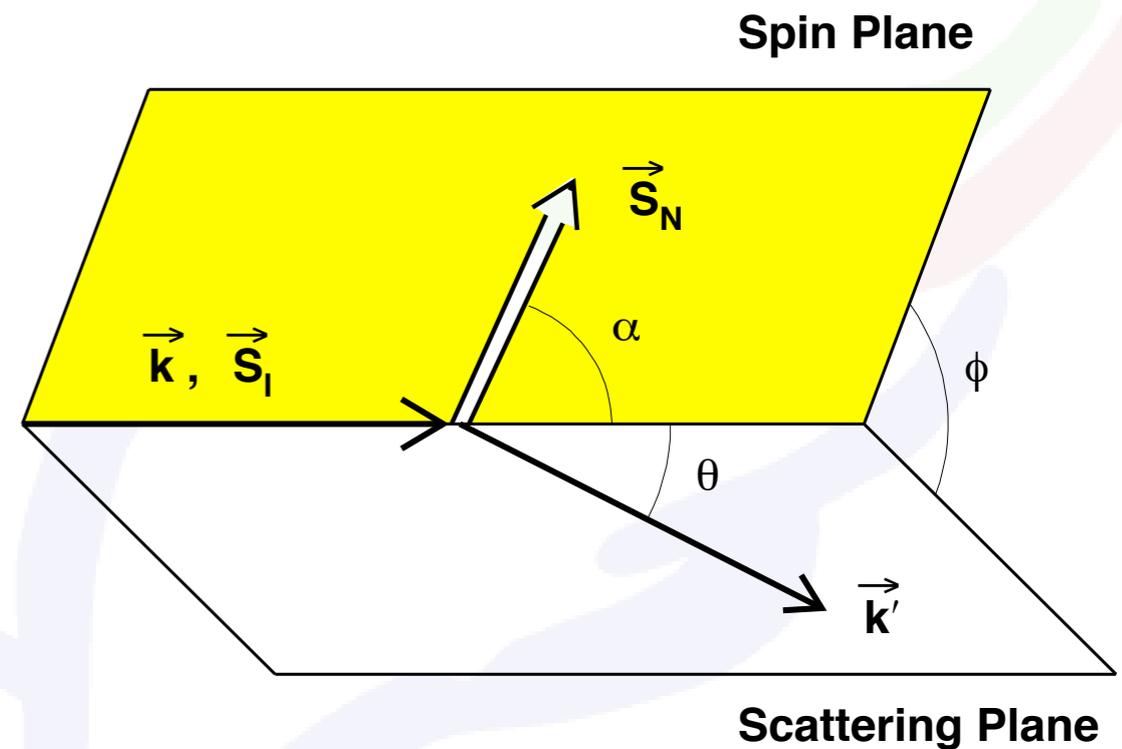
$$\text{Factorization} \Rightarrow \sigma^{ep \rightarrow ehX} = \sum_q DF^{p \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}$$

exploit strong correlation between flavor structure of leading hadron and struck quark

# Inclusive DIS

# Inclusive DIS

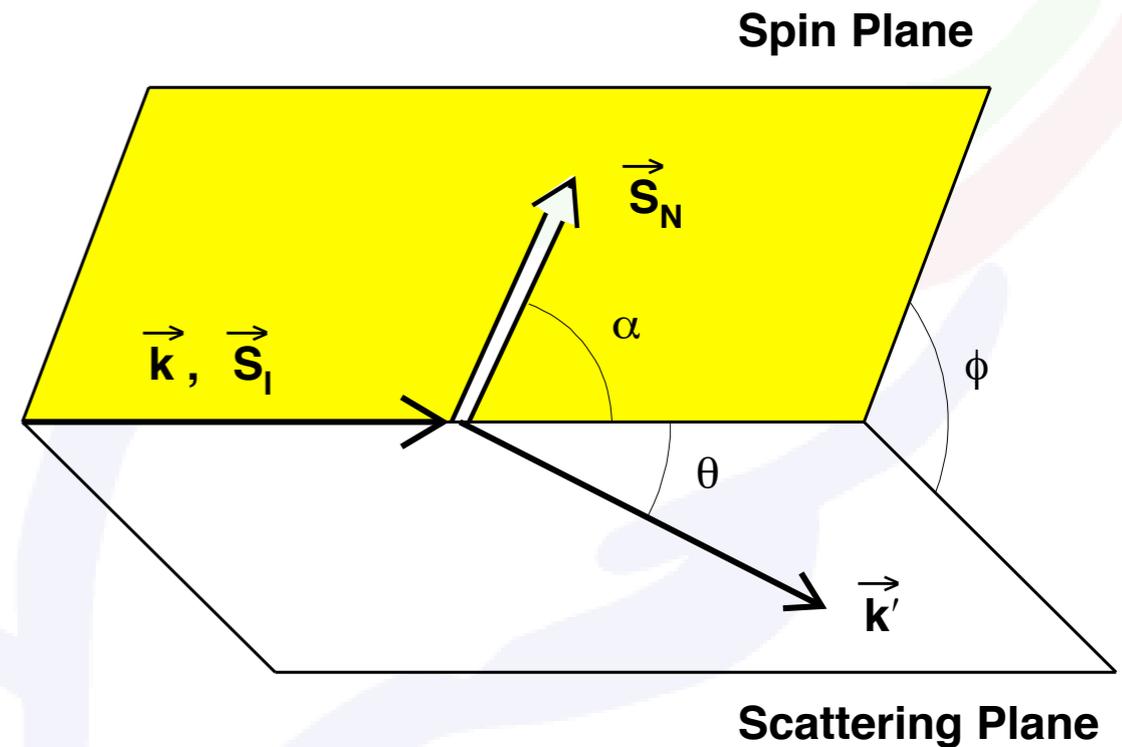
$$\frac{d^2\sigma(s, S)}{dx dQ^2} = \frac{2\pi\alpha^2 y^2}{Q^6} \mathbf{L}_{\mu\nu}(s) \mathbf{W}^{\mu\nu}(S)$$



# Inclusive DIS

$$\frac{d^2\sigma(s, S)}{dx dQ^2} = \frac{2\pi\alpha^2 y^2}{Q^6} \mathbf{L}_{\mu\nu}(s) \mathbf{W}^{\mu\nu}(S)$$

Lepton Tensor



# Inclusive DIS

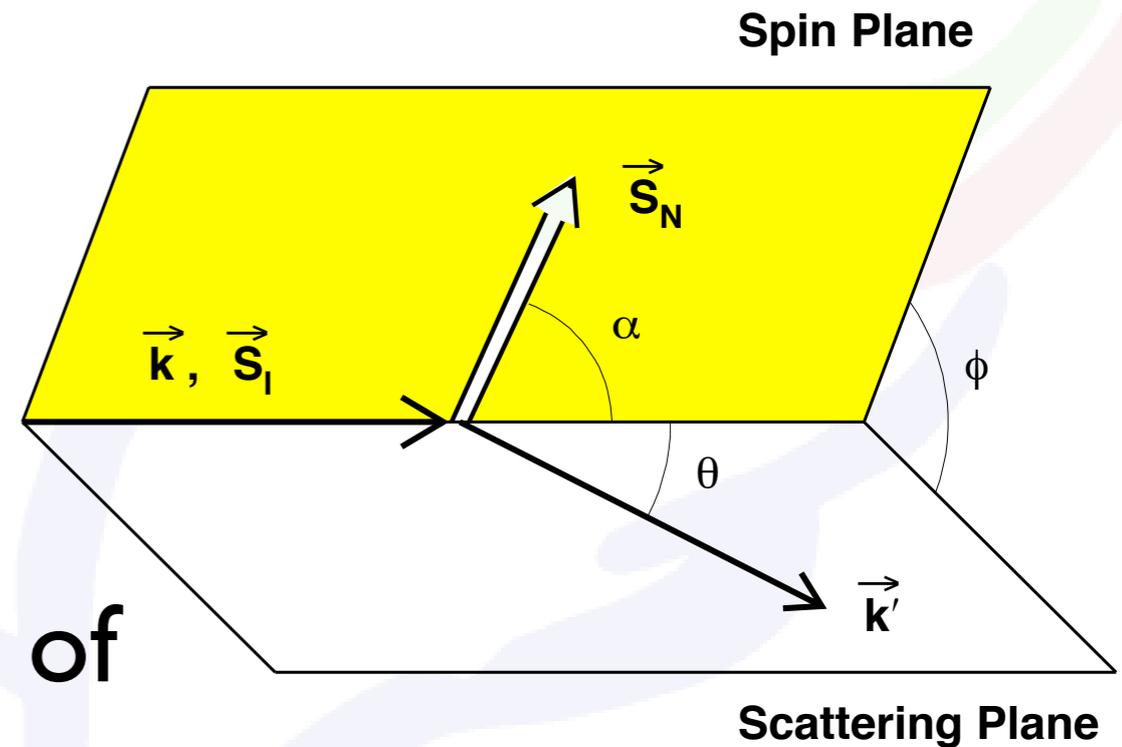
$$\frac{d^2\sigma(s, S)}{dx dQ^2} = \frac{2\pi\alpha^2 y^2}{Q^6} \mathbf{L}_{\mu\nu}(s) \mathbf{W}^{\mu\nu}(S)$$

Lepton Tensor

Hadron Tensor

parametrized in terms of

**Structure Functions**



# Inclusive DIS

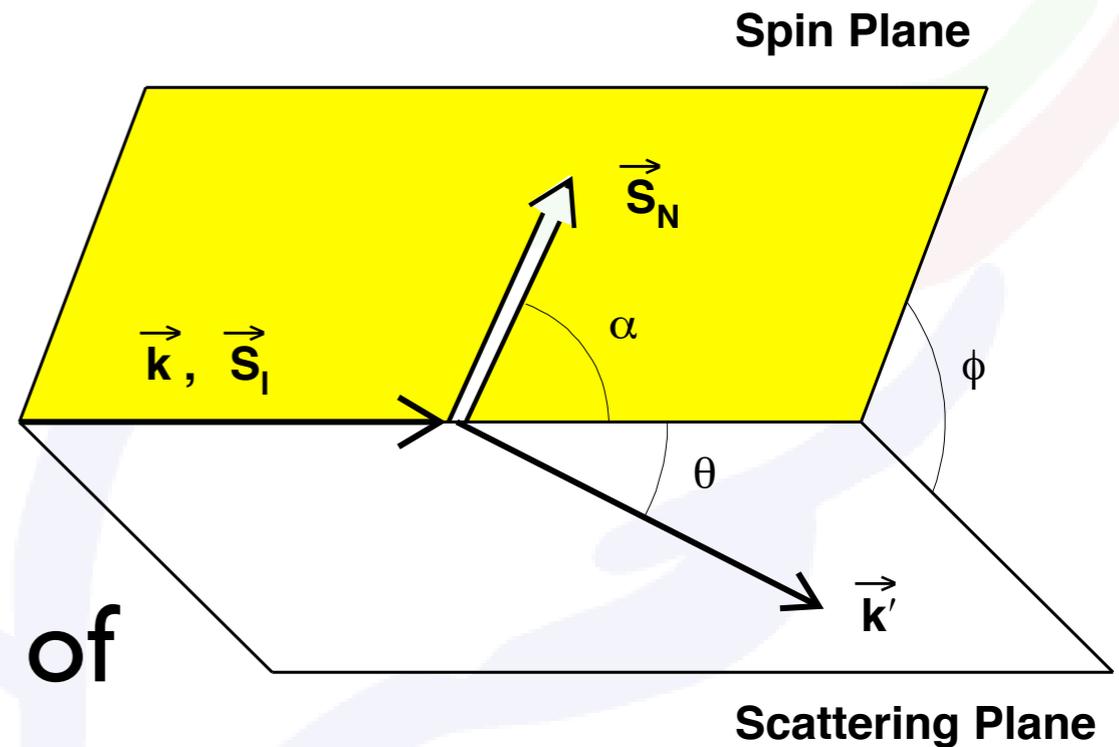
$$\frac{d^2\sigma(s, S)}{dx dQ^2} = \frac{2\pi\alpha^2 y^2}{Q^6} \mathbf{L}_{\mu\nu}(s) \mathbf{W}^{\mu\nu}(S)$$

Lepton Tensor

Hadron Tensor

parametrized in terms of

**Structure Functions**



$$\frac{d^3\sigma}{dxdy d\phi} \propto \frac{y}{2} F_1(x, Q^2) + \frac{1 - y - \gamma^2 y^2 / 4}{2xy} F_2(x, Q^2) - P_l P_T \cos \alpha \left[ \left( 1 - \frac{y}{2} - \frac{\gamma^2 y^2}{4} \right) g_1(x, Q^2) - \frac{\gamma^2 y}{2} g_2(x, Q^2) \right] + P_l P_T \sin \alpha \cos \phi \gamma \sqrt{1 - y - \frac{\gamma^2 y^2}{4}} \left( \frac{y}{2} g_1(x, Q^2) + g_2(x, Q^2) \right)$$

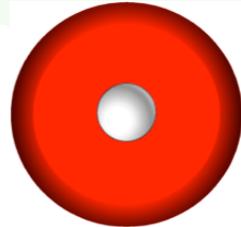
# Parton-Model Interpretation of Structure

structure function

$\leftrightarrow$

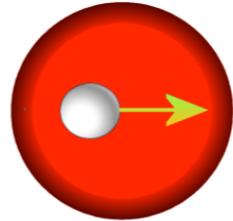
parton distribution

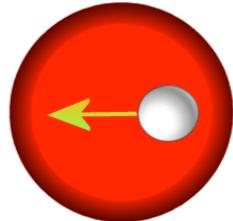
$$F_1(x) = \frac{1}{2} \sum_q e_q^2 f_1^q(x)$$

$$f_1^q =$$


$$F_2(x) = x \sum_q e_q^2 f_1^q(x)$$

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 g_1^q(x)$$

$$g_1^q =$$


$$-$$


$$g_2(x) = 0$$

# Parton-Model Interpretation of Structure

structure function



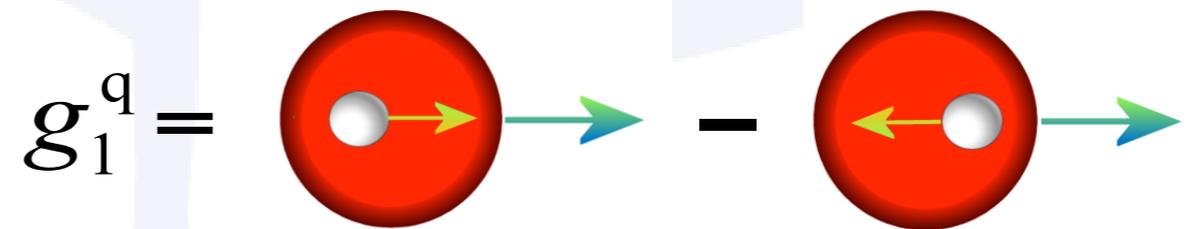
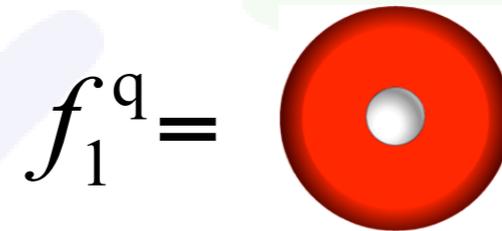
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$$F_2(x) = x \sum_q e_q^2 f_1^q(x)$$

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 g_1^q(x)$$

$$g_2(x) = 0$$



quark-spin contribution to nucleon spin

# Parton-Model Interpretation of Structure

structure function

$\leftrightarrow$

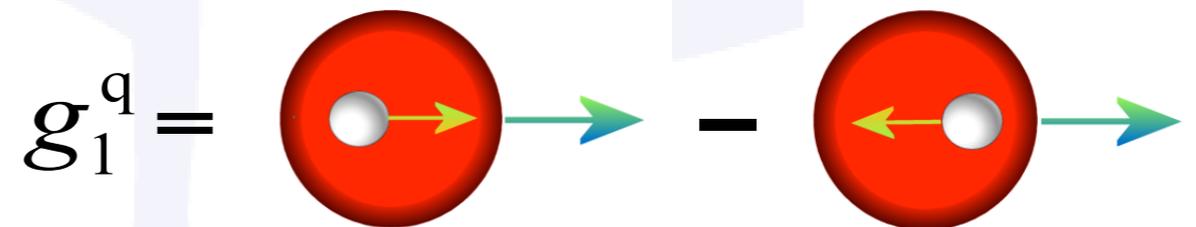
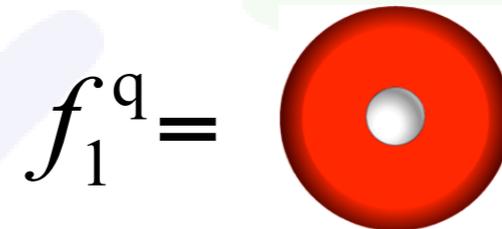
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$$F_1(x) = \frac{1}{2} \sum_q e_q^2 f_1^q(x)$$

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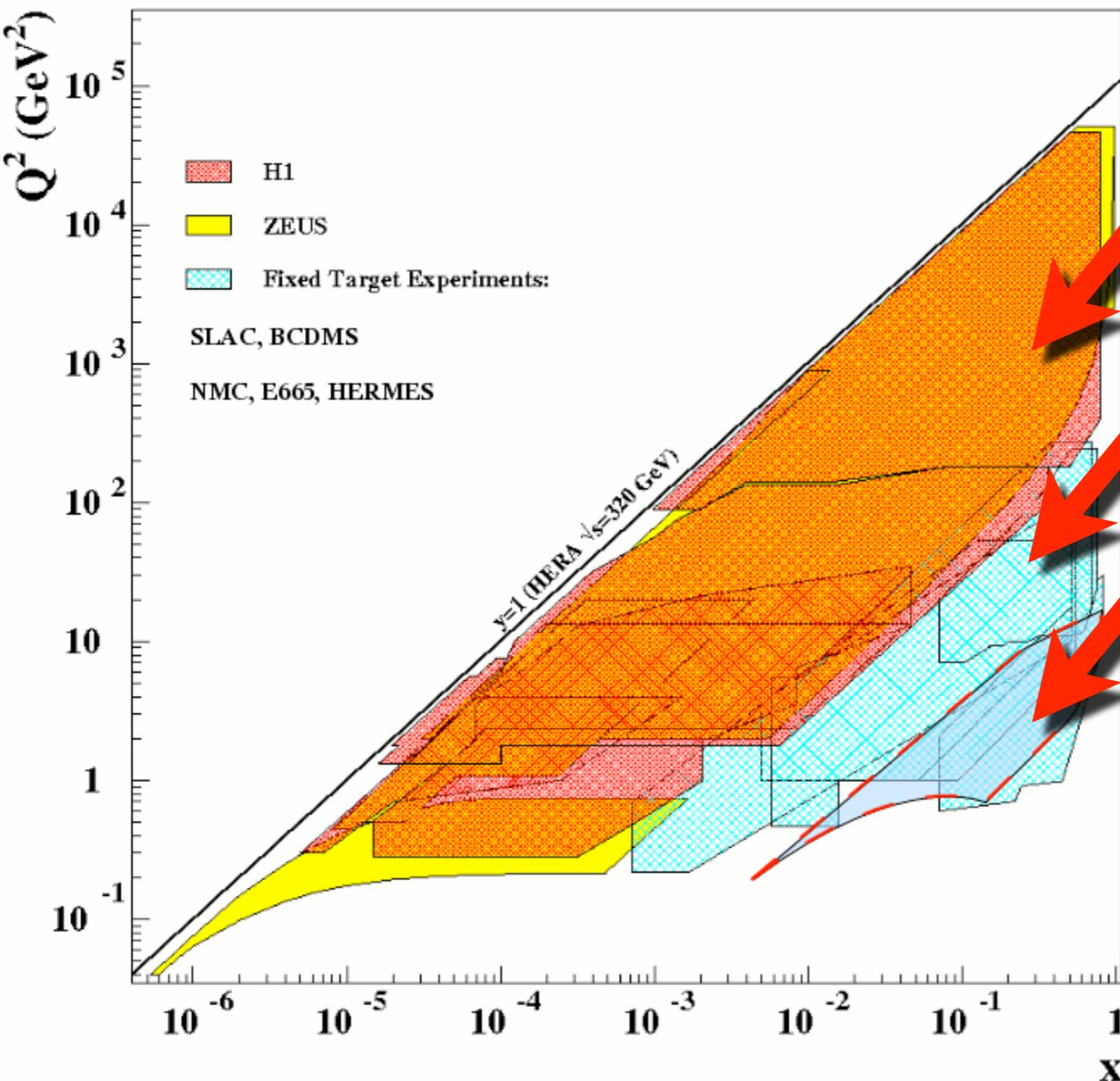
$$g_2(x) = 0$$



quark-spin contribution to nucleon spin

related to transverse force on struck quark

# Why measure $F_2$ at HERMES?



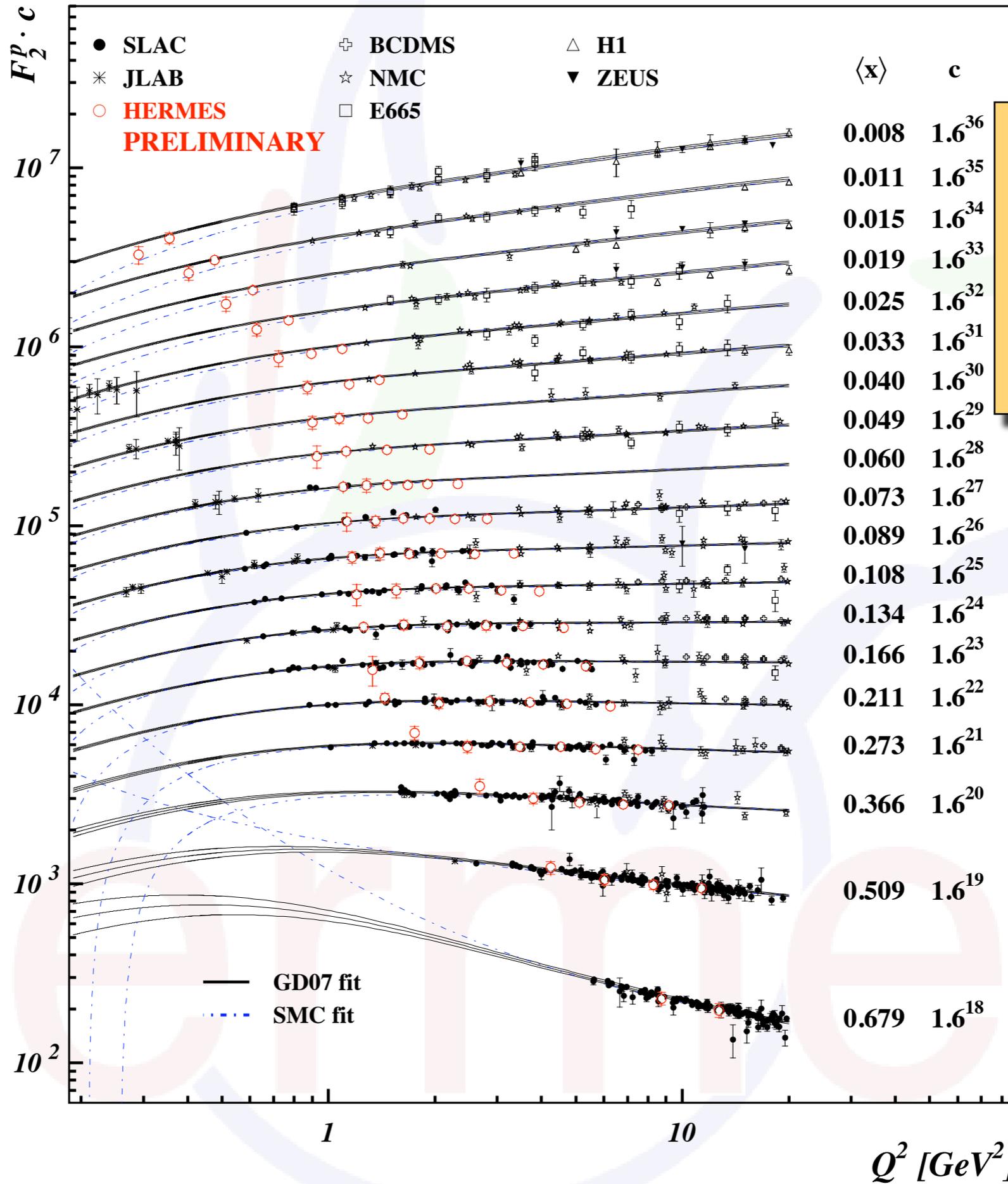
Collider experiments

Fixed target experiments

HERMES

- complementary kinematic coverage compared to colliders
- higher statistics compared to other fixed target experiments:
  - ▶ HERMES: 58 million DIS (P+D)
  - ▶ NMC: 9 million DIS (P+D)

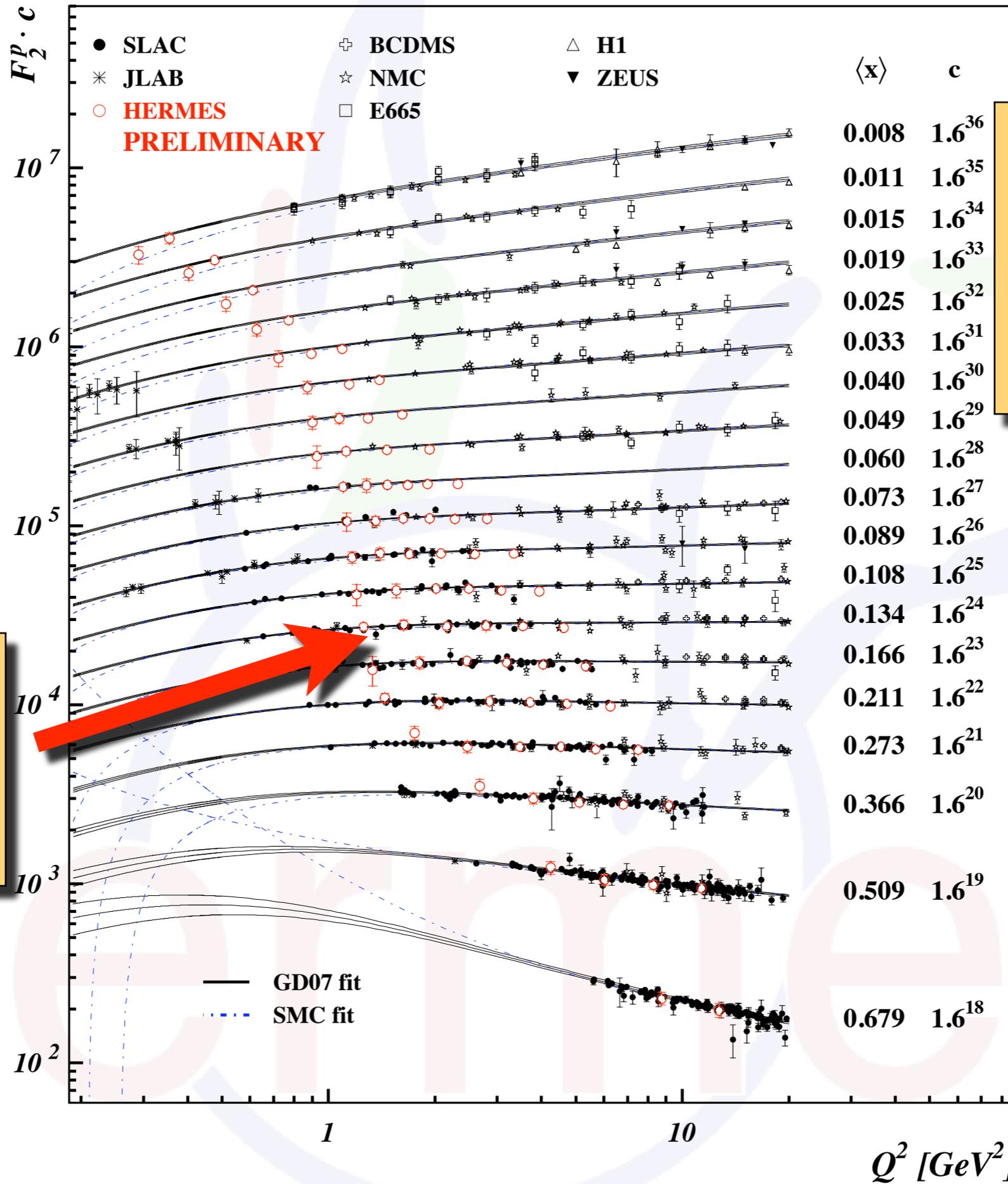
# $F_2$ proton



Comparison with parameterization by SMC and GD07

GD07: hep-ph0708.3196  
SMC: Phys. Rev. D, Vol. 58, 112001

# F<sub>2</sub> proton



Agreement with world data in the overlap region

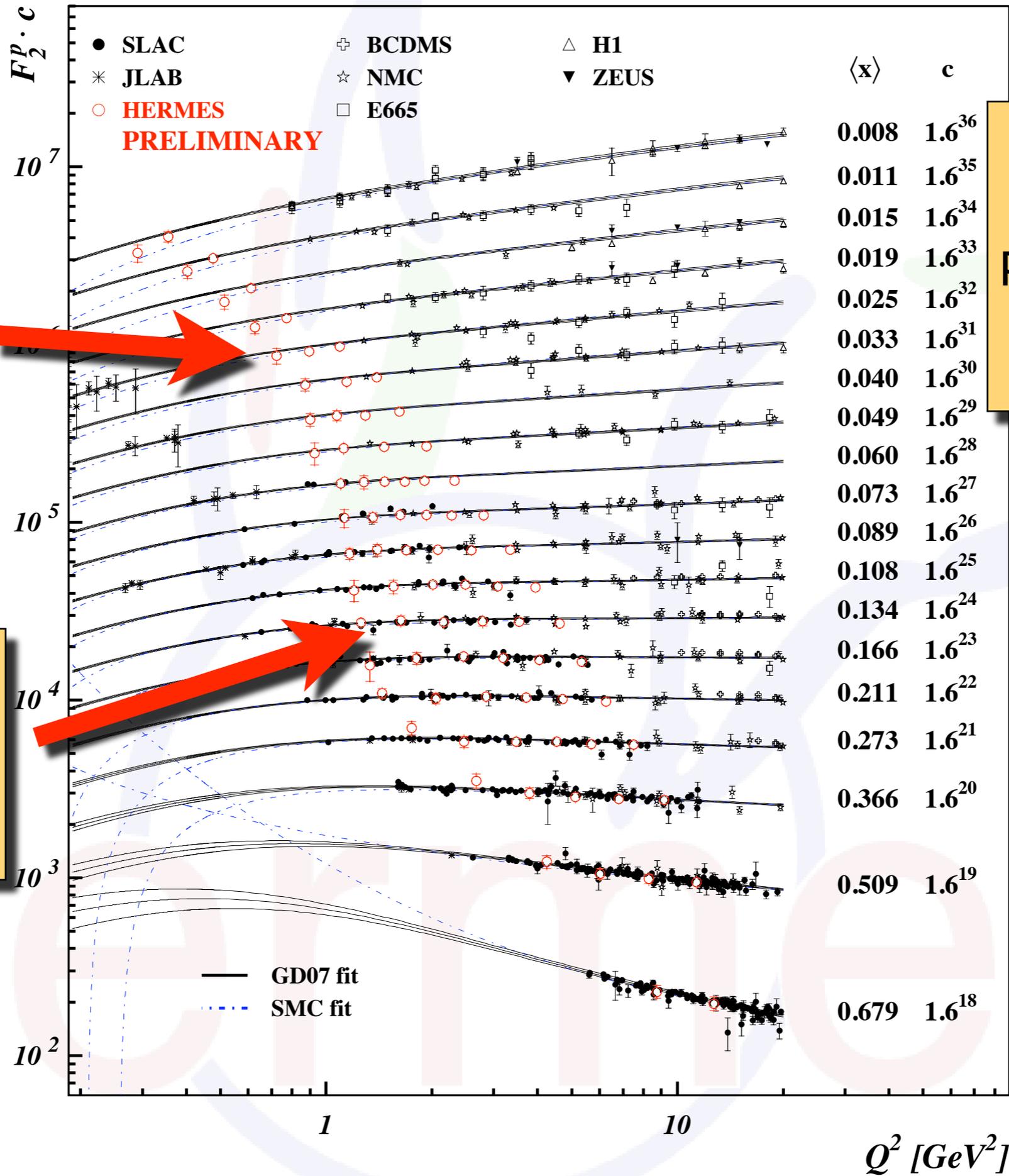
Comparison with parameterization by SMC and GD07

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# $F_2$ proton

New region covered by HERMES

Agreement with world data in the overlap region



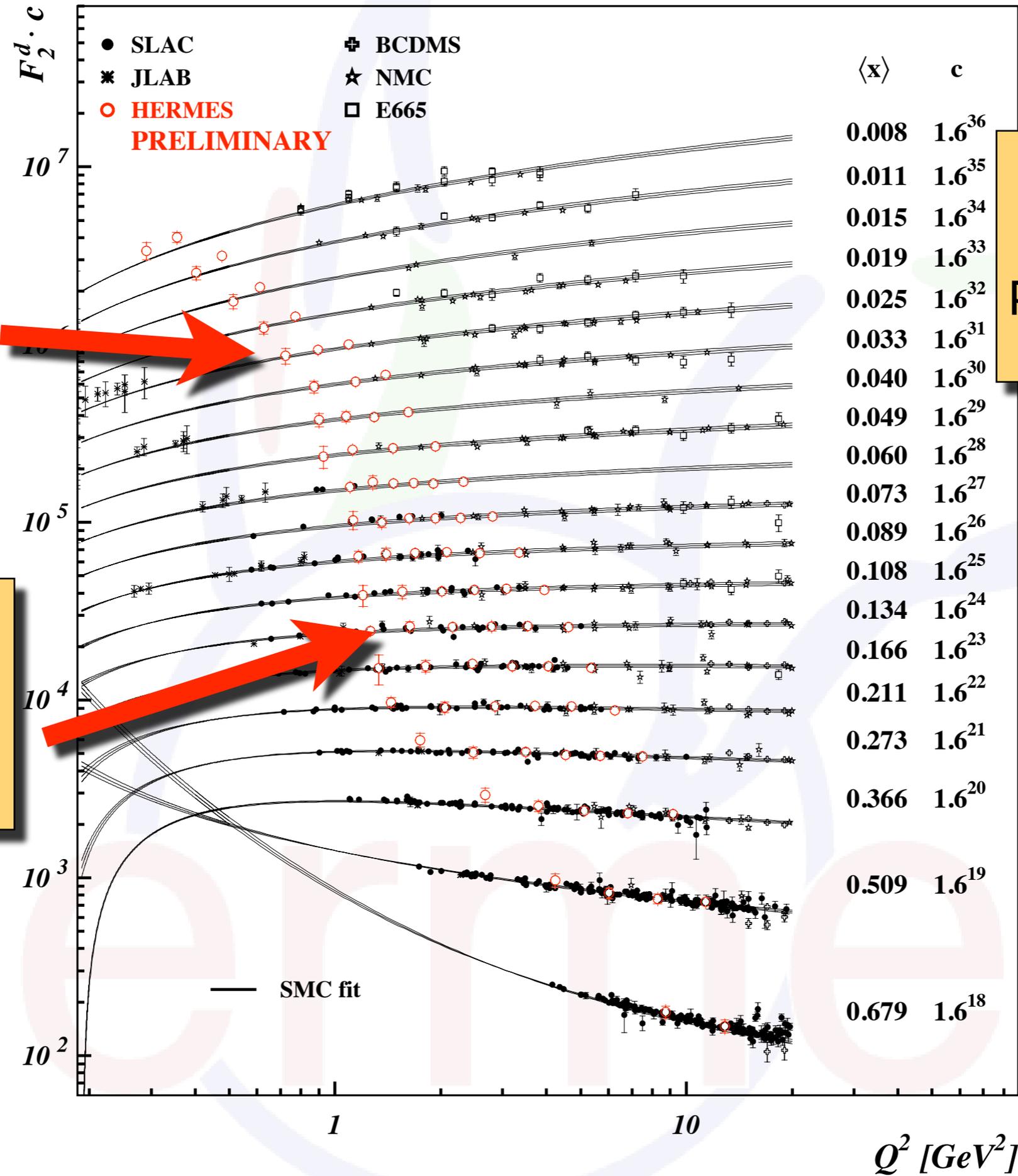
Comparison with parameterization by SMC and GD07

GD07: hep-ph0708.3196  
SMC: Phys. Rev. D, Vol. 58, 112001

# $F_2$ deuteron

New region covered by HERMES

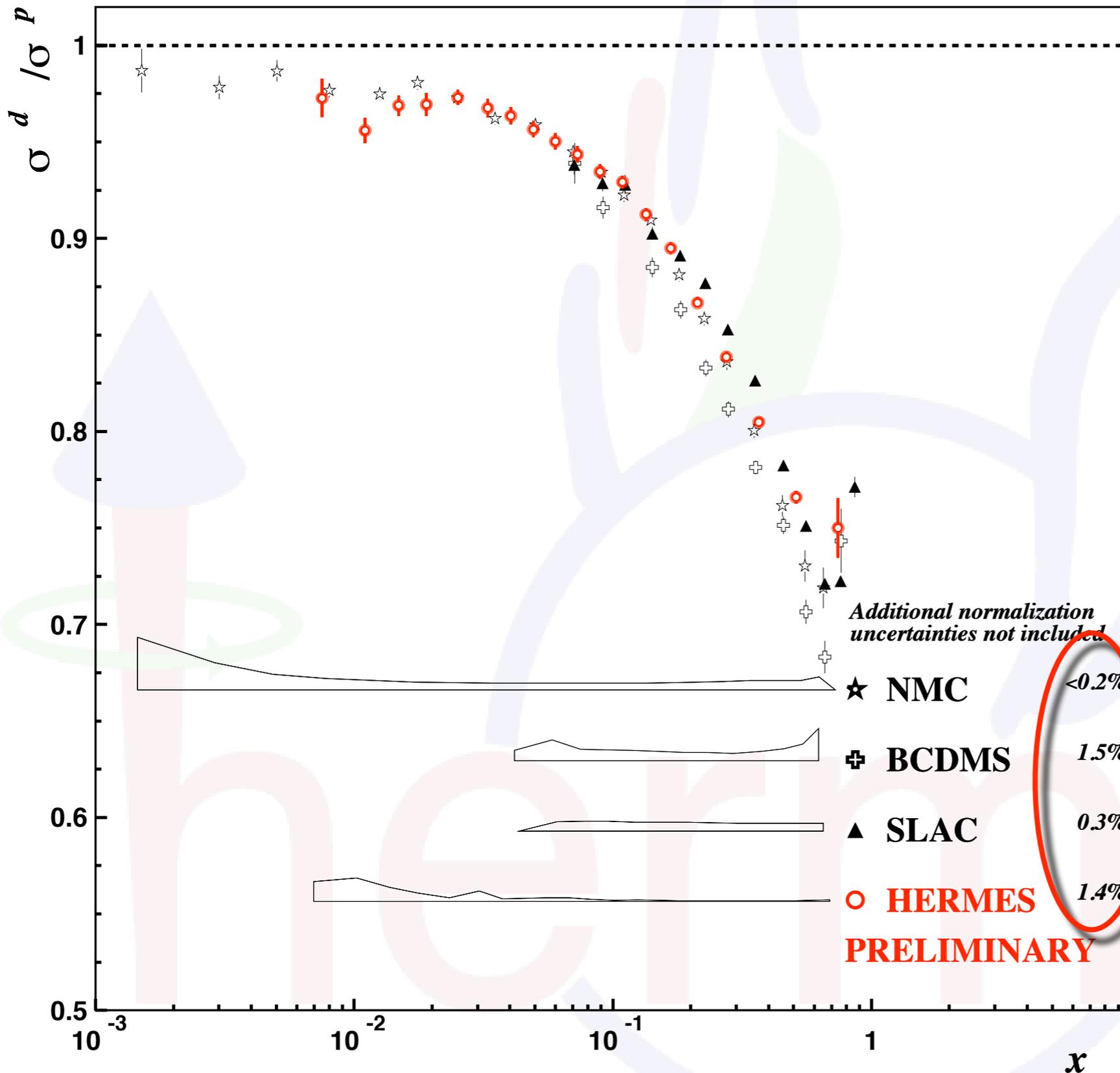
Agreement with world data in the overlap region



Comparison with parameterization by SMC

SMC: Phys. Rev. D, Vol. 58, I12001

# World data on $\sigma^d / \sigma^p$

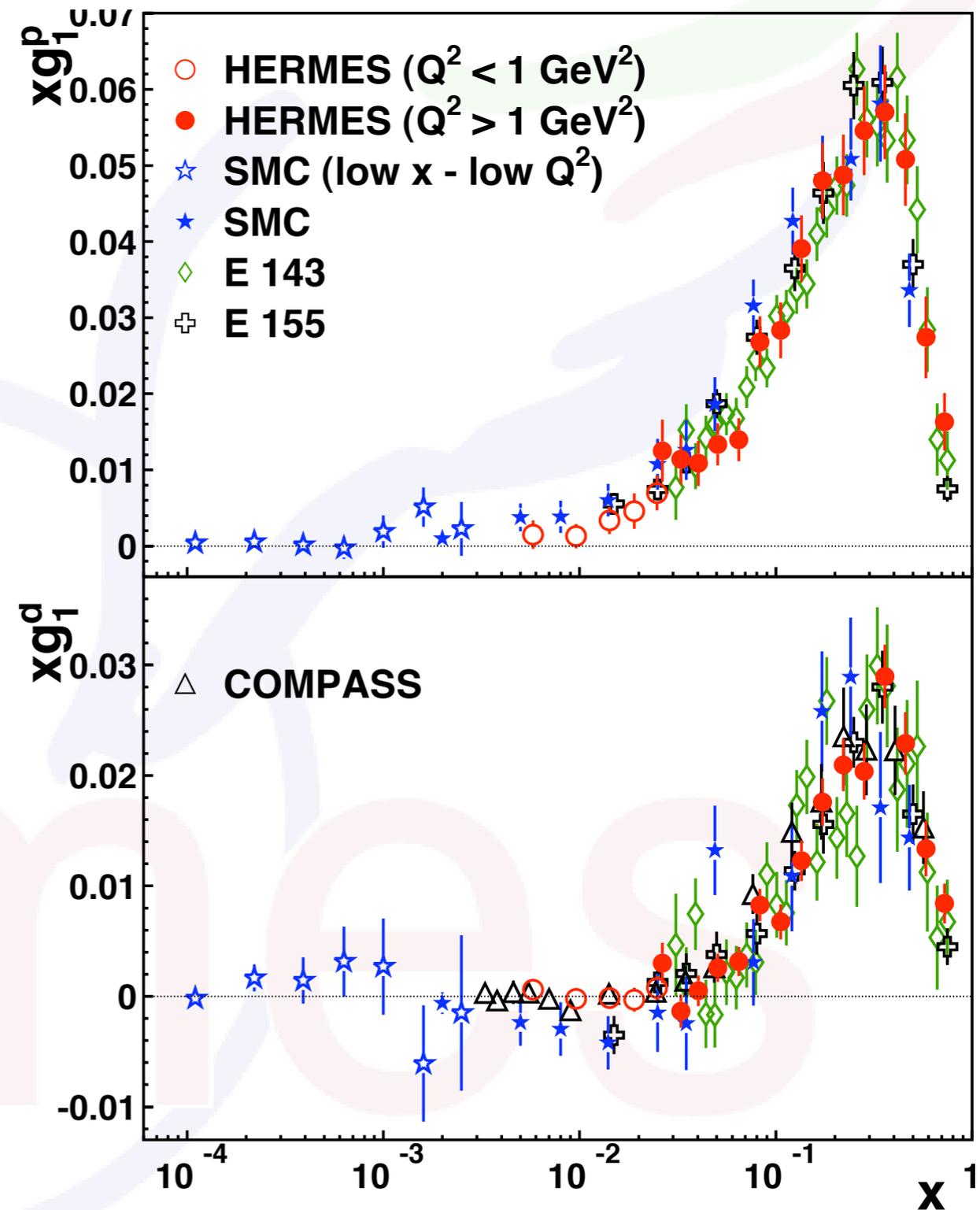
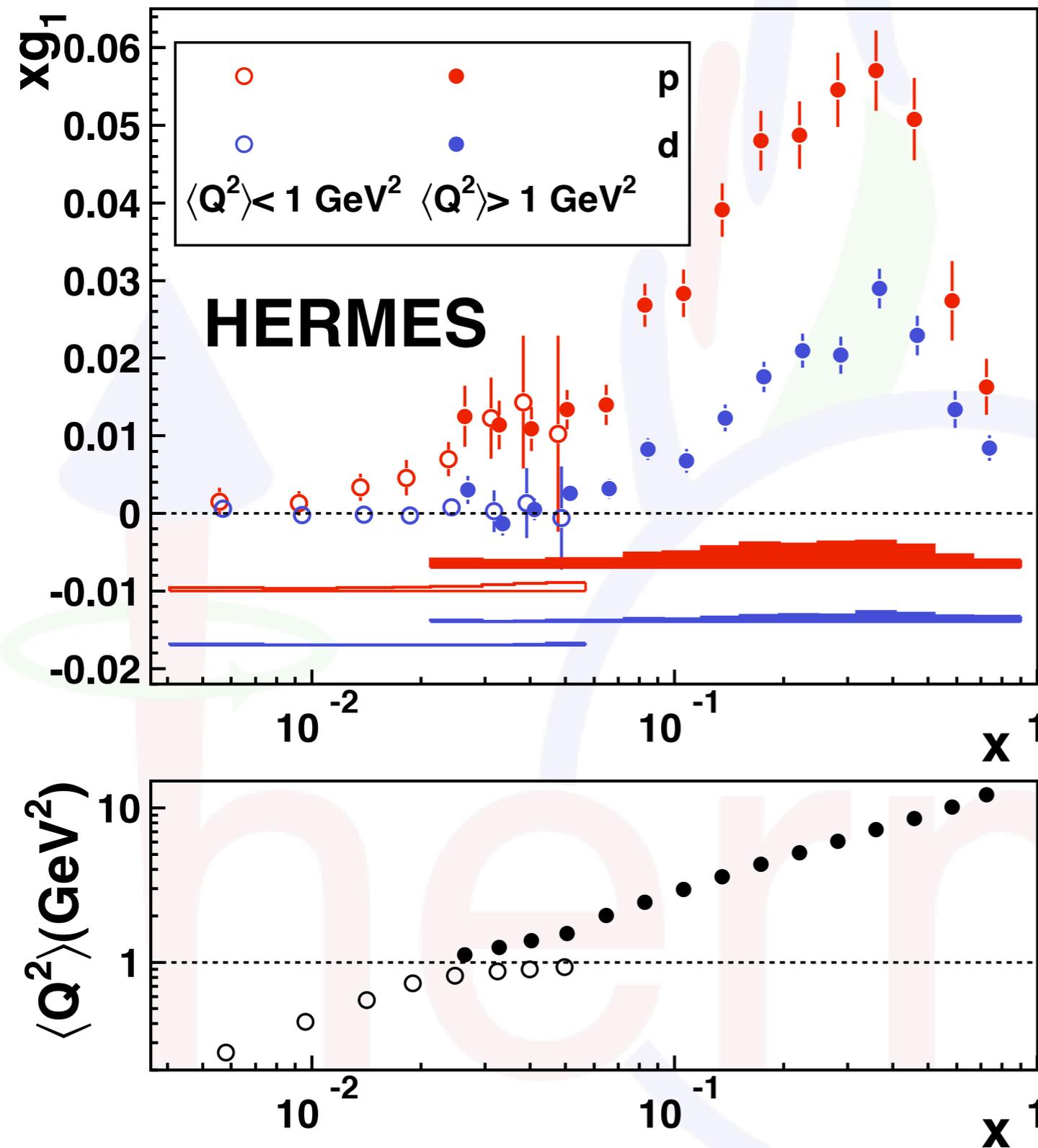


Many systematic errors common to proton and deuteron cross sections cancel in ratio

**Normalization uncertainties**

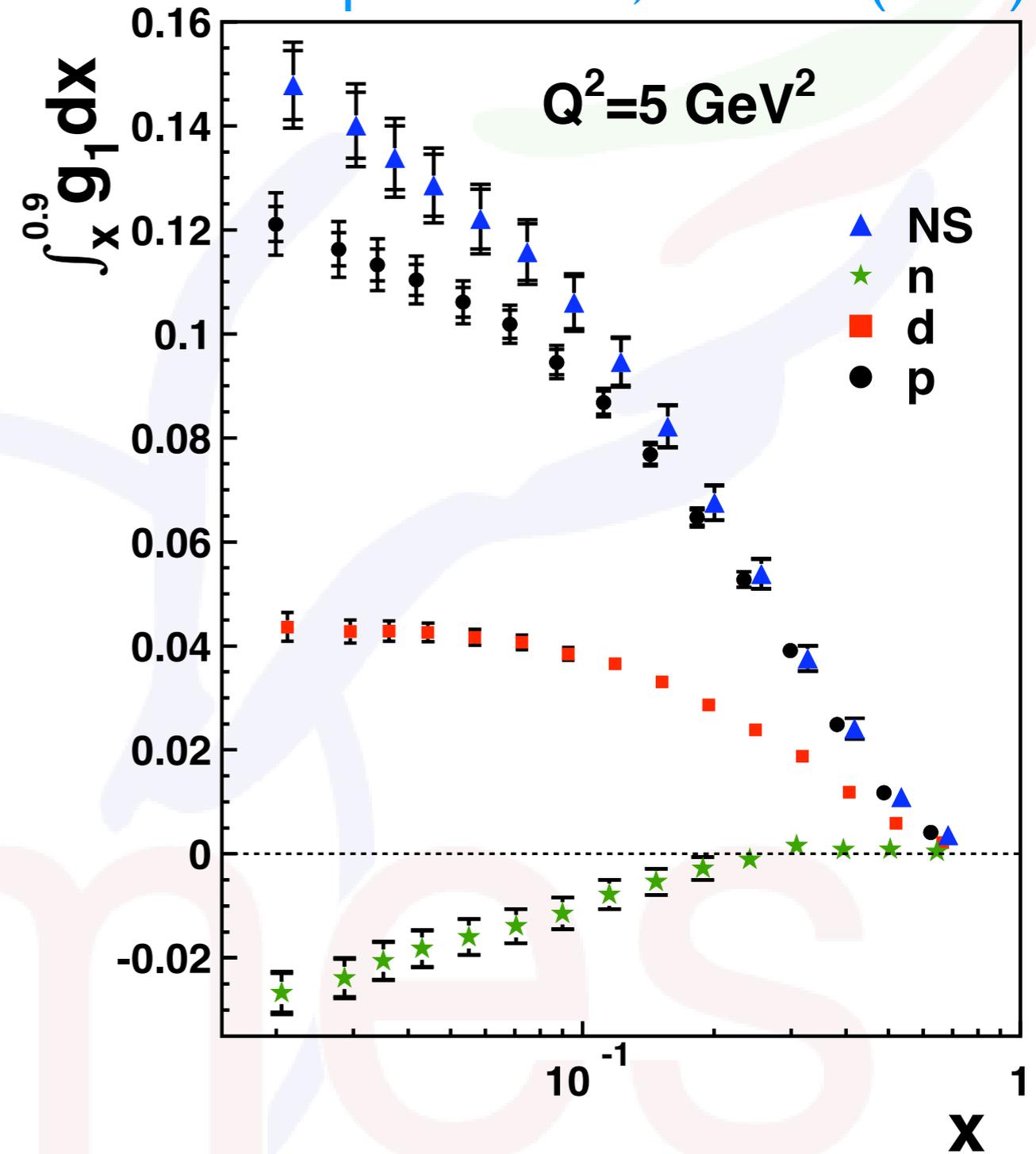
# Polarized Structure Function $g_1$

A. Airapetian et al., PRD 75 (2007)



# Integral of $g_1(x)$

A. Airapetian et al., PRD 75 (2007)



# Integral of $g_1(x)$

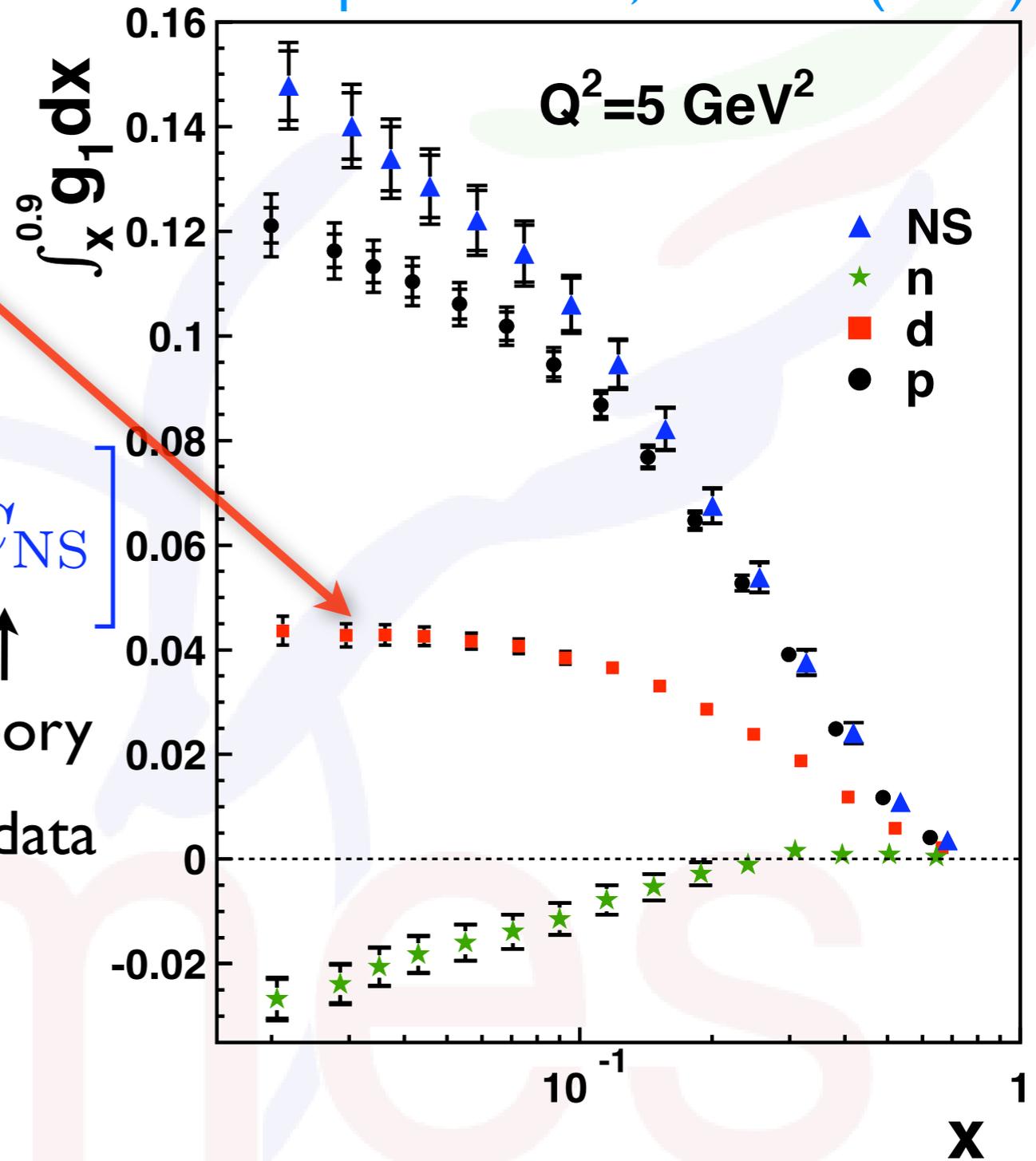
A. Airapetian et al., PRD 75 (2007)

**Saturation**

→ **close to full integral?**

$$\Delta\Sigma \stackrel{\overline{\text{MS}}}{=} \frac{1}{\Delta C_S} \left[ \frac{9\Gamma_1^d}{1 - \frac{3}{2}\omega_D} - \frac{1}{4} a_8 \Delta C_{NS} \right]$$

$\uparrow$  theory                       $\uparrow$   $0.05 \pm 0.05$                        $\uparrow$  theory  
 hyperon-decay data

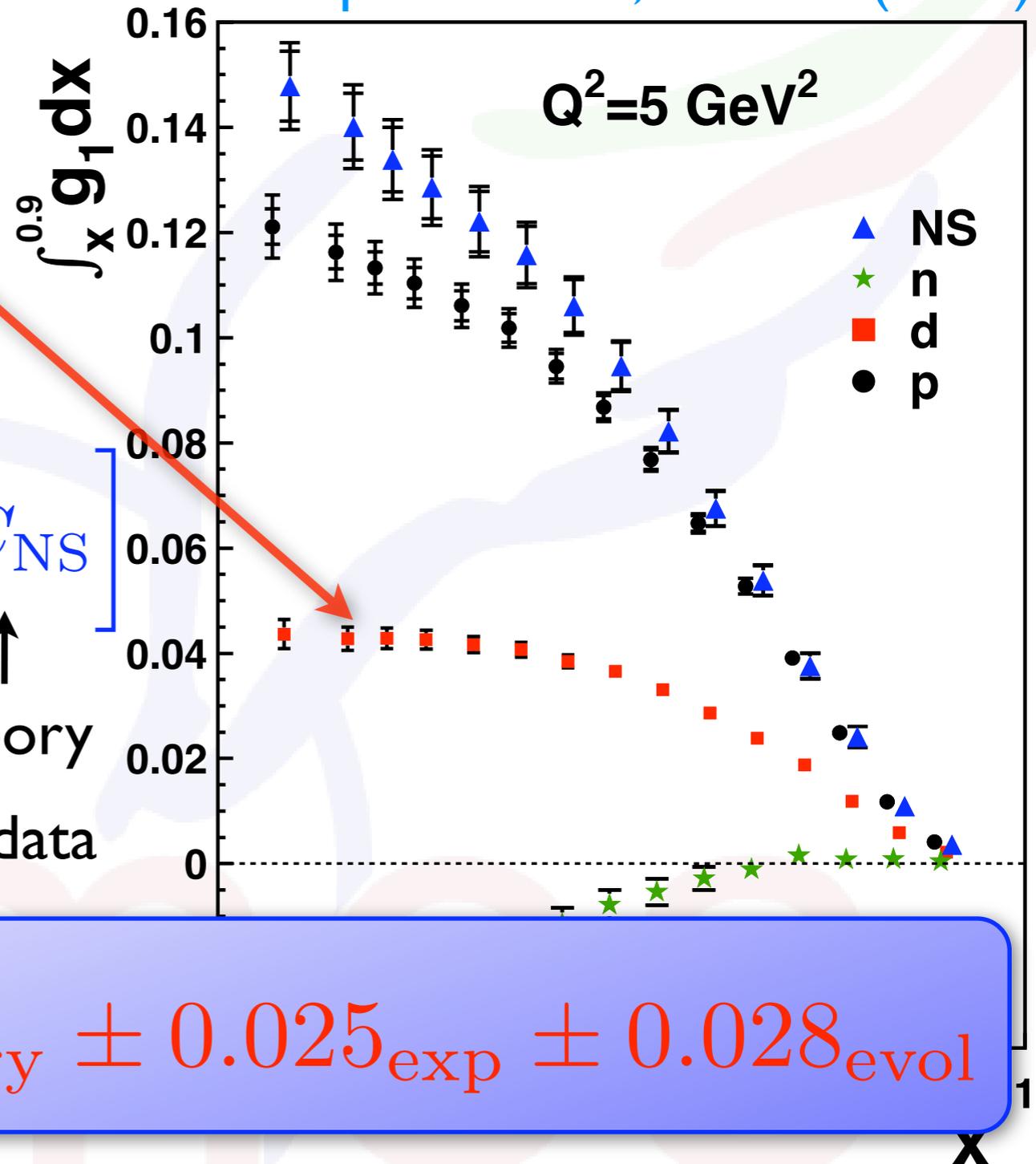


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A. Airapetian et al., PRD 75 (2007)

**Saturation**

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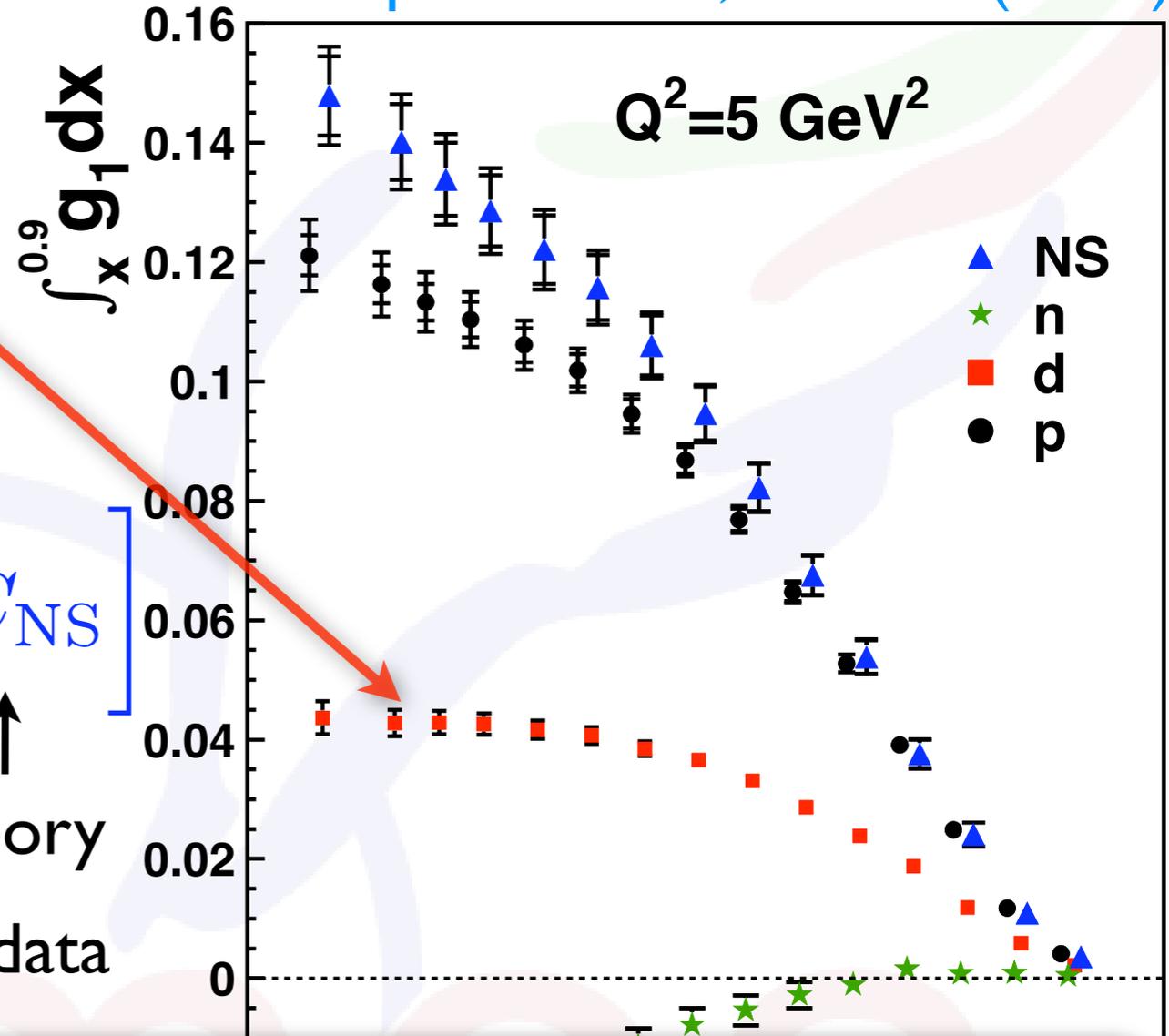
$$\Delta\Sigma \stackrel{\overline{\text{MS}}}{=} 0.330 \pm 0.011_{\text{theory}} \pm 0.025_{\text{exp}} \pm 0.028_{\text{evol}}$$

# Integral of $g_1(x)$

A. Airapetian et al., PRD 75 (2007)

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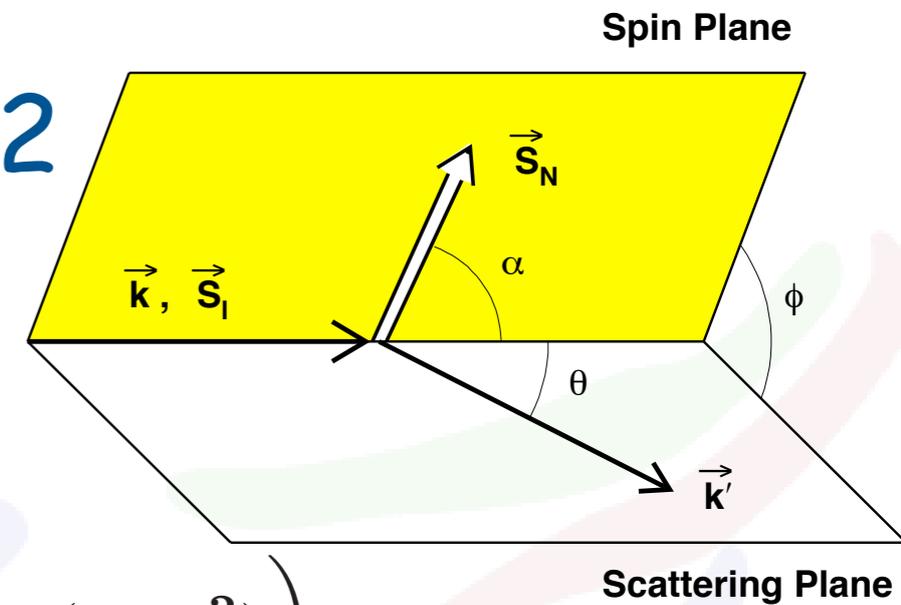
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$\uparrow$  theory                       $\uparrow$  0.05±0.05                       $\uparrow$  theory  
 hyperon-decay data

$$\Delta\Sigma \stackrel{\overline{\text{MS}}}{=} 0.330 \pm 0.011_{\text{theory}} \pm 0.025_{\text{exp}} \pm 0.028_{\text{evol}}$$

**most precise result; only 1/3 of nucleon spin from quarks**

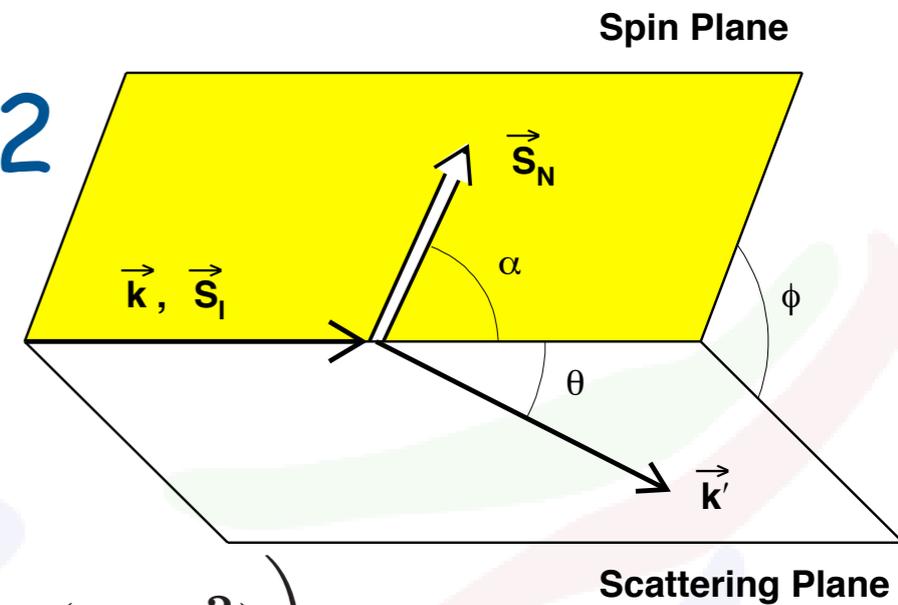
# Extraction of $g_2$



$$\frac{\sigma^{\rightarrow\downarrow}(\phi) - \sigma^{\rightarrow\uparrow}(\phi)}{\sigma^{\rightarrow\downarrow}(\phi) + \sigma^{\rightarrow\uparrow}(\phi)} = \frac{\Delta\sigma_T}{\bar{\sigma}} =$$

$$= \frac{-\gamma\sqrt{1-y-\frac{\gamma^2 y^2}{4}} \left( \frac{y}{2} g_1(x, Q^2) + g_2(x, Q^2) \right)}{\underbrace{\left[ \frac{y}{2} F_1(x, Q^2) + \frac{1}{2xy} \left( 1-y-\frac{\gamma^2 y^2}{4} \right) F_2(x, Q^2) \right]}_{A_T}} \cos\phi$$

# Extraction of $g_2$



$$\frac{\sigma^{\rightarrow\downarrow}(\phi) - \sigma^{\rightarrow\uparrow}(\phi)}{\sigma^{\rightarrow\downarrow}(\phi) + \sigma^{\rightarrow\uparrow}(\phi)} = \frac{\Delta\sigma_T}{\bar{\sigma}} =$$

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$A_T$

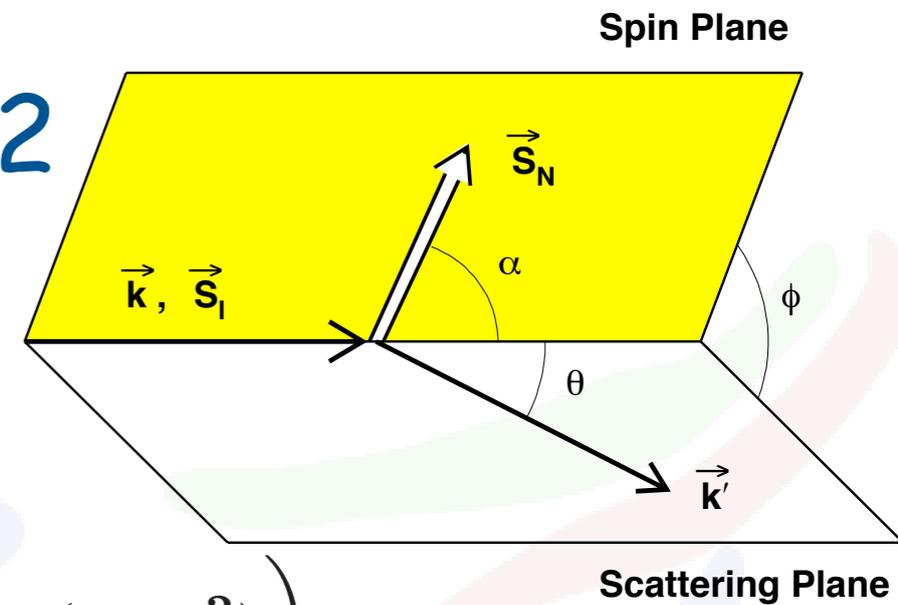


fit to double-spin asymmetry

$$A_2 = \frac{1}{d(1+\gamma\xi)} A_T + \frac{\xi(1+\gamma^2)}{1+\gamma\xi} \frac{g_1}{F_1}$$

$$g_2 = \frac{F_1}{\gamma d(1+\gamma\xi)} A_T - \frac{F_1(\gamma-\xi)}{\gamma(1+\gamma\xi)} \frac{g_1}{F_1}$$

# Extraction of $g_2$



$$\frac{\sigma^{\rightarrow\downarrow}(\phi) - \sigma^{\rightarrow\uparrow}(\phi)}{\sigma^{\rightarrow\downarrow}(\phi) + \sigma^{\rightarrow\uparrow}(\phi)} = \frac{\Delta\sigma_T}{\bar{\sigma}} =$$

$$= \frac{-\gamma\sqrt{1-y-\frac{\gamma^2 y^2}{4}} \left( \frac{y}{2} g_1(x, Q^2) + g_2(x, Q^2) \right)}{\left[ \frac{y}{2} F_1(x, Q^2) + \frac{1}{2xy} \left( 1-y-\frac{\gamma^2 y^2}{4} \right) F_2(x, Q^2) \right]} \cos\phi$$

$A_T$

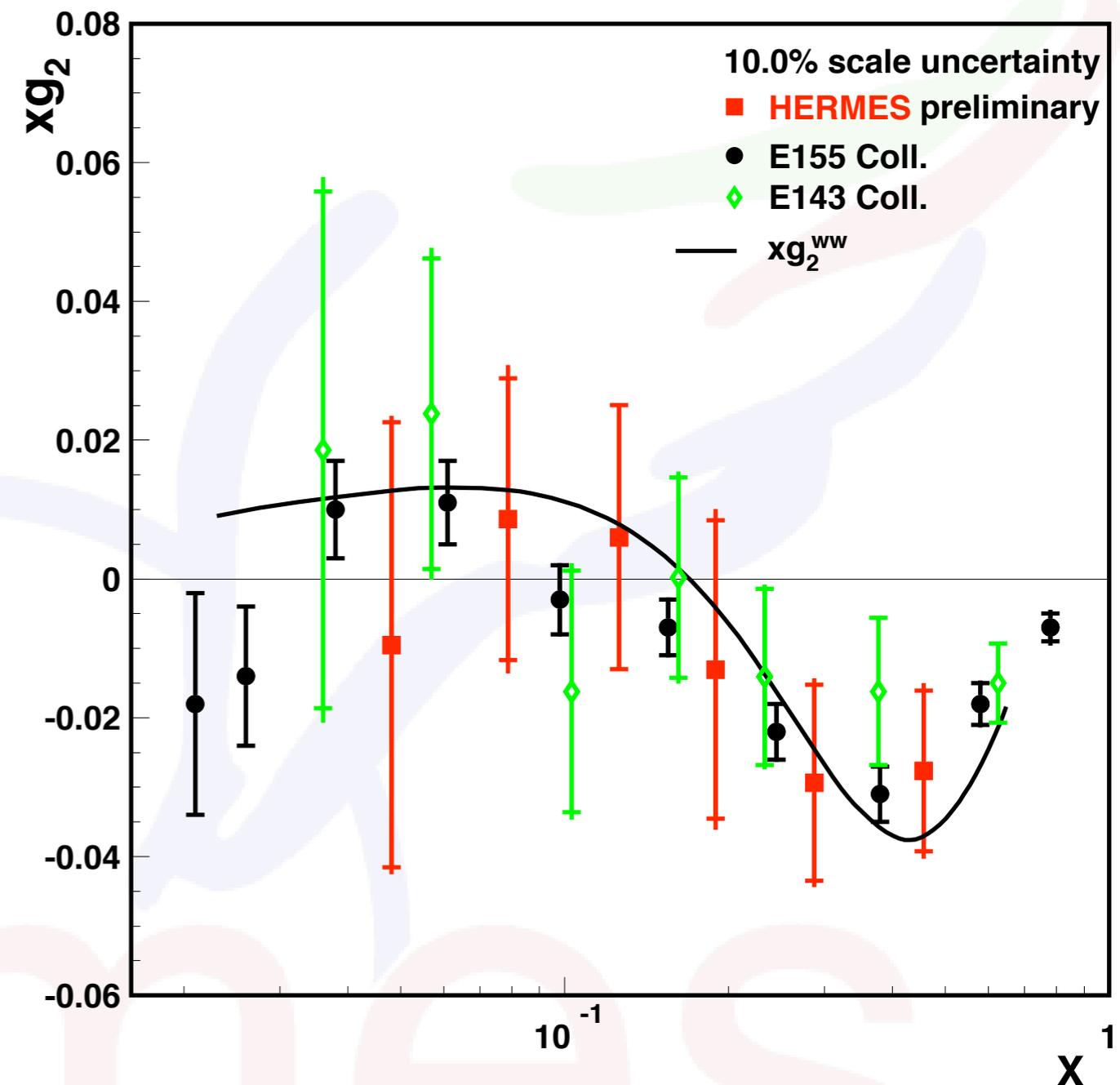
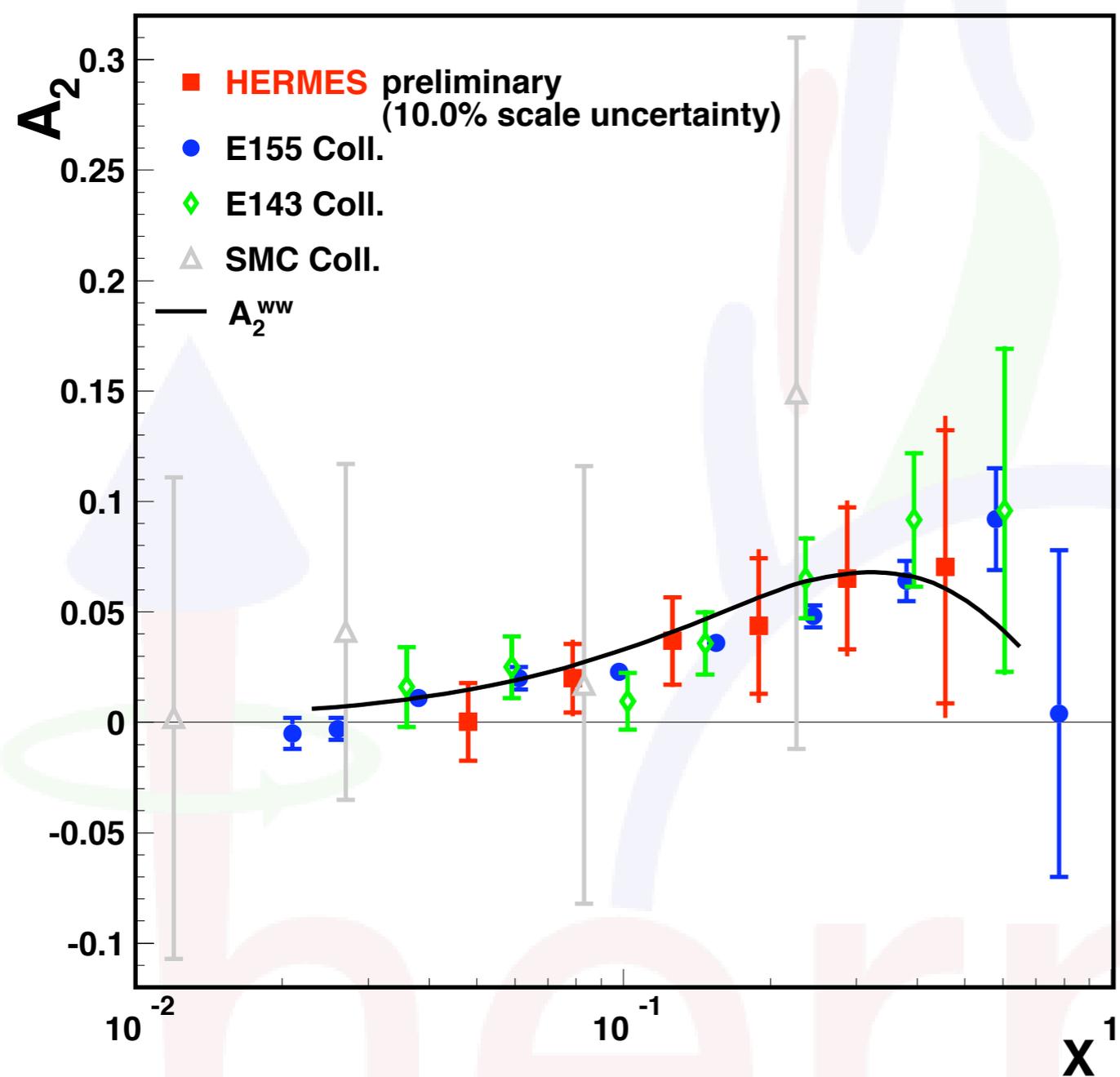
fit to double-spin asymmetry

parameterizations

$$A_2 = \frac{1}{d(1+\gamma\xi)} A_T + \frac{\xi(1+\gamma^2)}{1+\gamma\xi} \frac{g_1}{F_1}$$

$$g_2 = \frac{F_1}{\gamma d(1+\gamma\xi)} A_T - \frac{F_1(\gamma-\xi)}{\gamma(1+\gamma\xi)} \frac{g_1}{F_1}$$

# Results on $A_2$ and $xg_2$

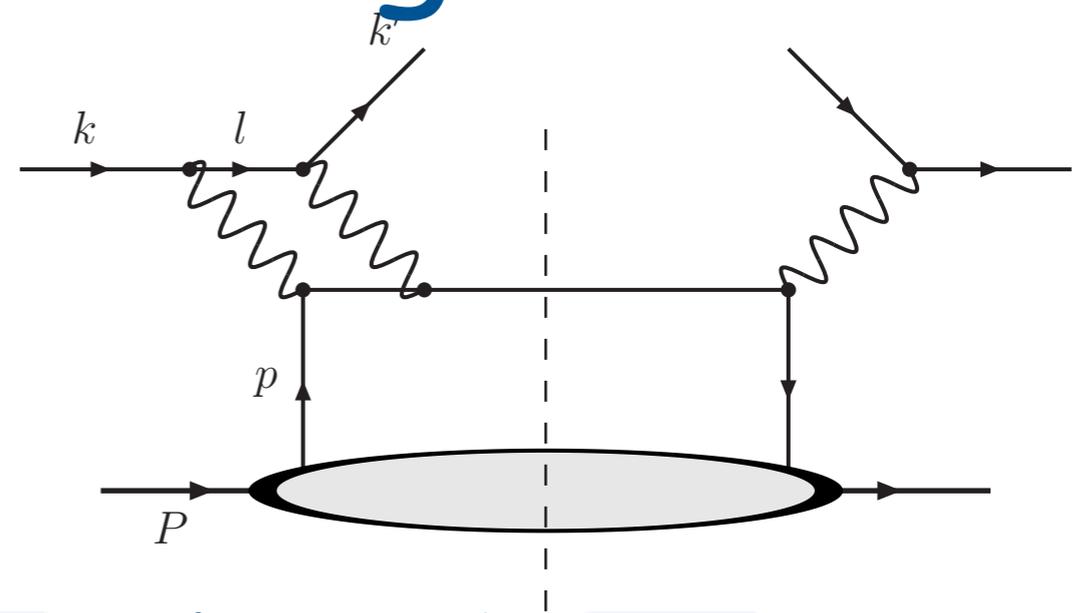


● consistent with (sparse) world data

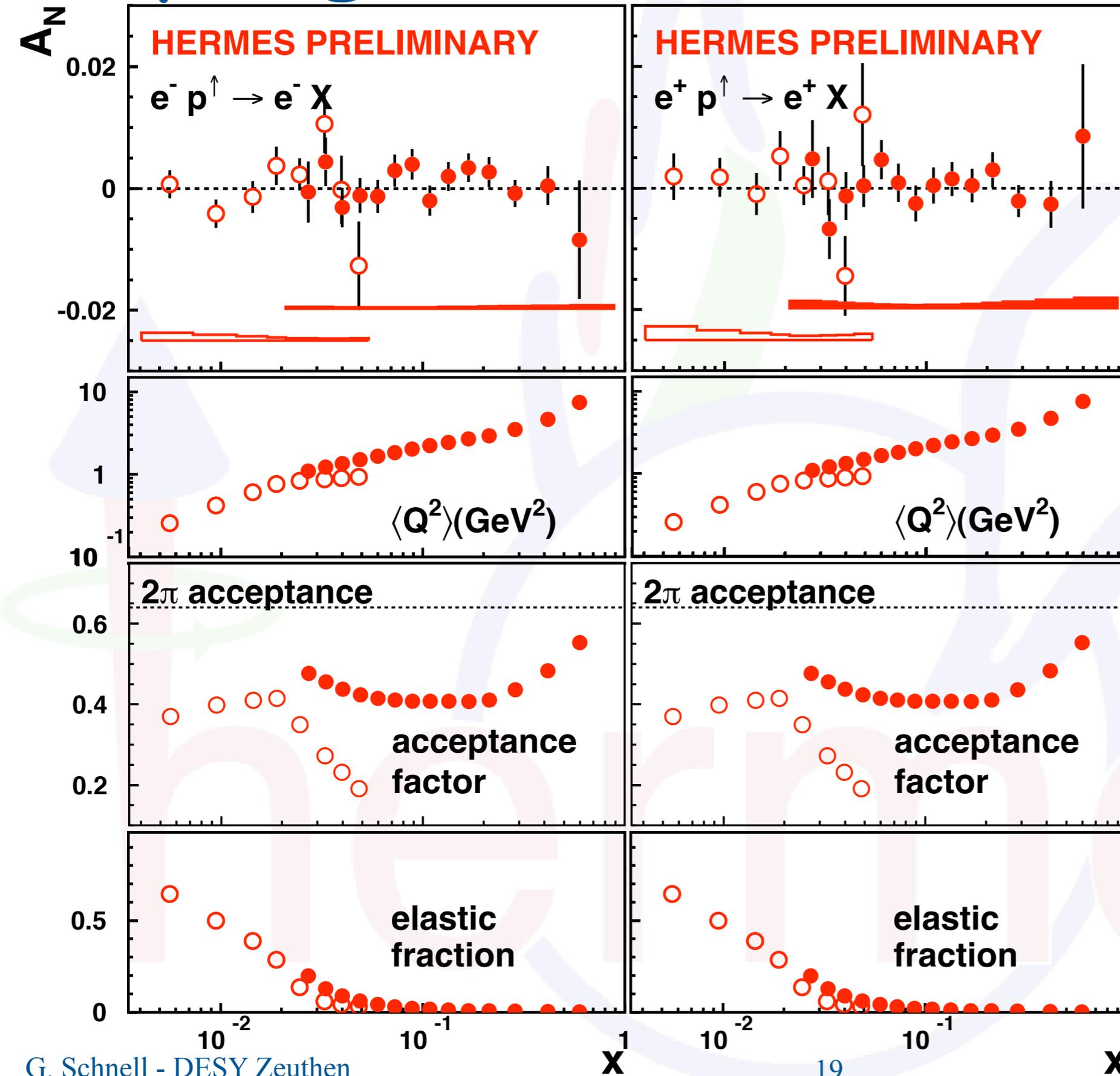
● low beam polarization during HERA II  $\rightarrow$  small f.o.m.

# Two-Photon Exchange

- interference between one- and two-photon exchange amplitudes leads to SSAs in inclusive DIS off transversely polarized targets
- interference sensitive to beam charge due to odd number of e.m. couplings to beam
- proportional to  $S(k \times k')$  - either measure left-right asymmetries or sine modulation
- two-photon exchange best candidate to explain discrepancy in form-factor measurements

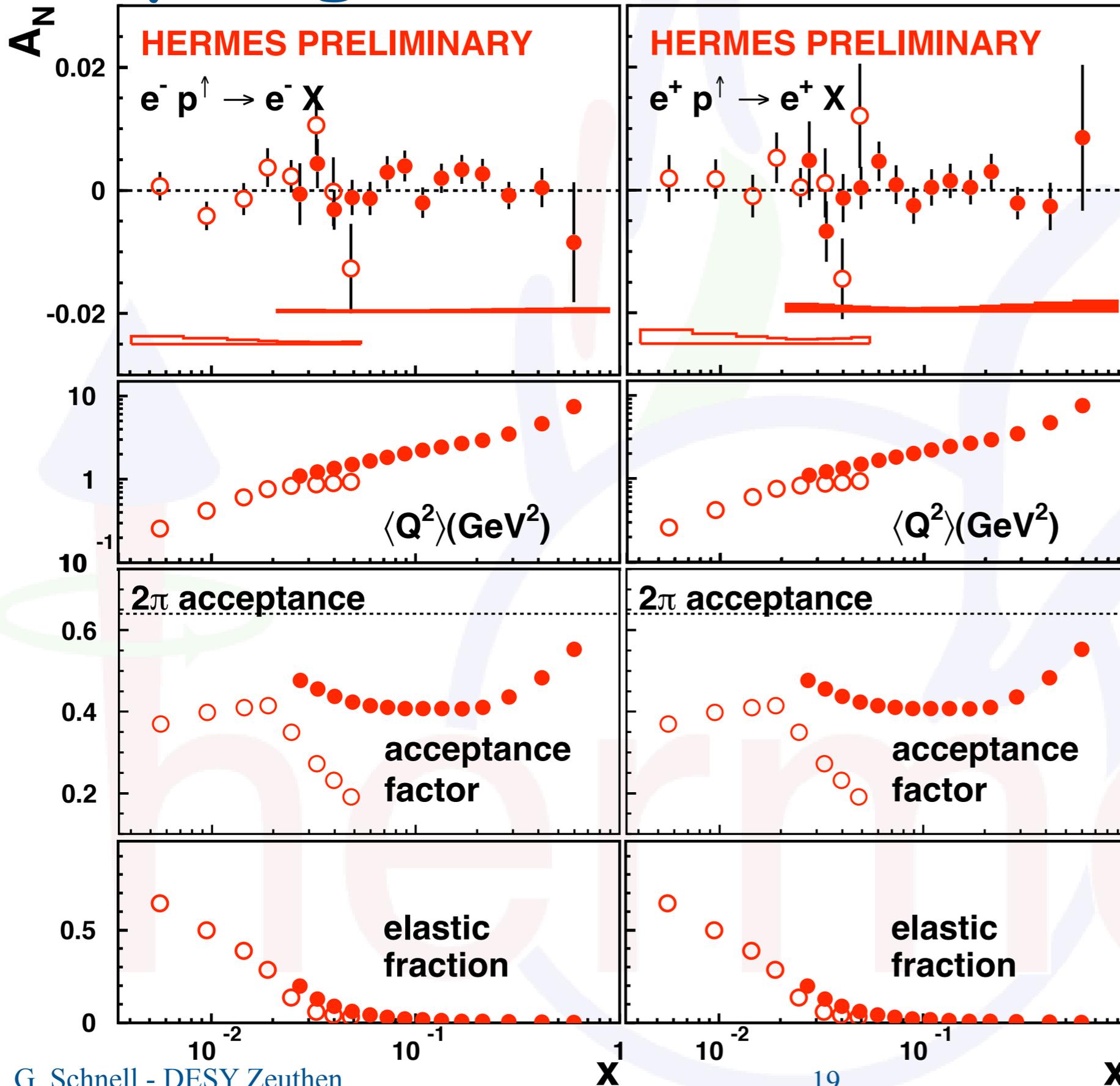


# Any Sign of Two-Photon Exchange?

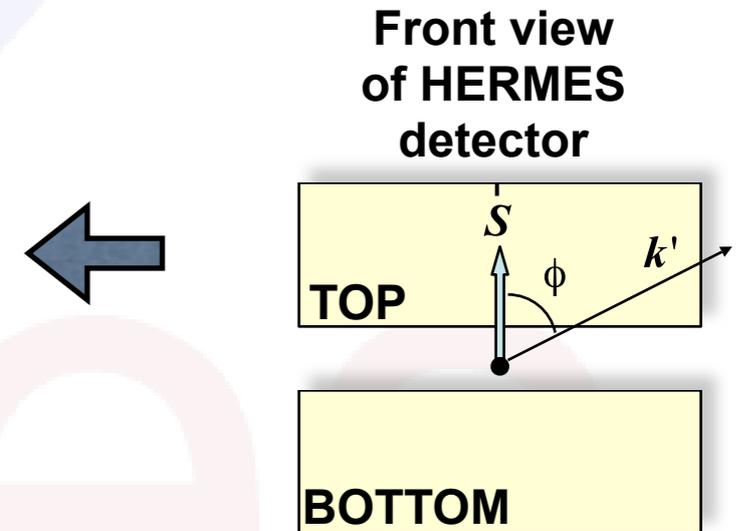


← consistent with zero at  $10^{-3}$  level

# Any Sign of Two-Photon Exchange?



← consistent with zero at  $10^{-3}$  level

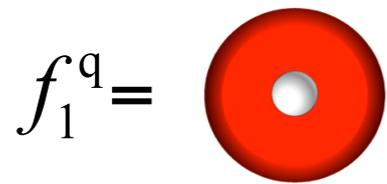


$$\text{acc.fac.} \equiv \frac{(A_N)_{\text{acc}}}{(A_{\text{UT}}^{\sin \phi})_{2\pi}}$$

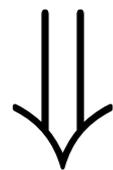
# Semi-Inclusive DIS

# Quark Structure of the Nucleon

(integrated over transverse momentum)



$f_1^q =$

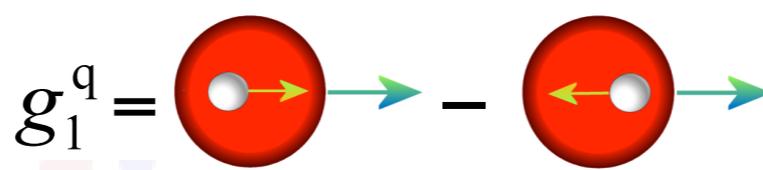


Unpolarized quarks  
and nucleons

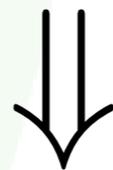
$f_1^q(x)$ : spin averaged  
(well known)

⇒ Vector Charge

$$\langle PS | \bar{\Psi} \gamma^\mu \Psi | PS \rangle = \int dx (f_1^q(x) - f_1^{\bar{q}}(x))$$



$g_1^q =$

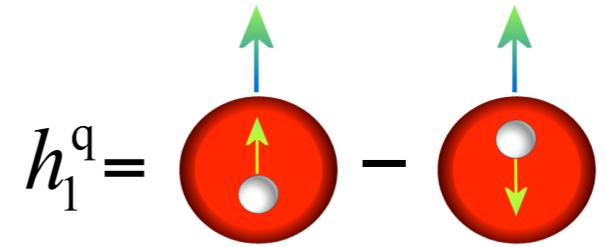


Longitudinally  
polarized quarks  
and nucleons

$g_1^q(x)$ : helicity  
difference (known)

⇒ Axial Charge

$$\langle PS | \bar{\Psi} \gamma^\mu \gamma_5 \Psi | PS \rangle = \int dx (g_1^q(x) + g_1^{\bar{q}}(x))$$



$h_1^q =$



Transversely  
polarized quarks  
and nucleons

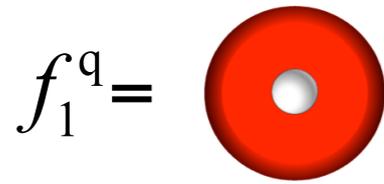
$h_1^q(x)$ : transversity  
(hardly known!)

⇒ Tensor Charge

$$\langle PS | \bar{\Psi} \sigma^{\mu\nu} \gamma_5 \Psi | PS \rangle = \int dx (h_1^q(x) - h_1^{\bar{q}}(x))$$

# Quark Structure of the Nucleon

(integrated over transverse momentum)

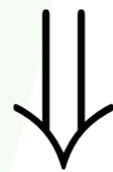
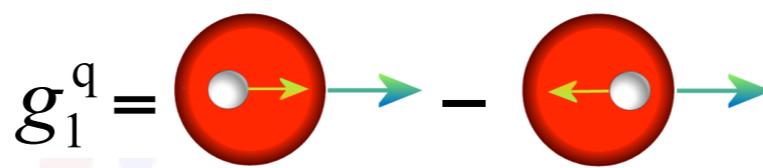


Unpolarized quarks  
and nucleons

$f_1^q(x)$ : spin averaged  
(well known)

⇒ Vector Charge

$$\langle PS | \bar{\Psi} \gamma^\mu \Psi | PS \rangle = \int dx (f_1^q(x) - f_1^{\bar{q}}(x))$$

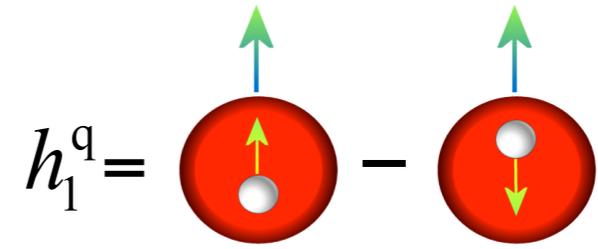


Longitudinally  
polarized quarks  
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$g_1^q(x)$ : helicity  
difference (known)

⇒ Axial Charge

$$\langle PS | \bar{\Psi} \gamma^\mu \gamma_5 \Psi | PS \rangle = \int dx (g_1^q(x) + g_1^{\bar{q}}(x))$$



Transversely  
polarized quarks  
and nucleons

$h_1^q(x)$ : transverse  
(hardly known)

⇒ Tensor Charge

$$\langle PS | \bar{\Psi} \sigma^{\mu\nu} \gamma_5 \Psi | PS \rangle = \int dx (h_1^q(x) - h_1^{\bar{q}}(x))$$

Chiral-odd!

# Strange-quark distributions

- use isoscalar probe and target to extract strange-quark distributions
- only need **inclusive asymmetries** and  **$K^+K^-$  asymmetries**, i.e.,  $A_{\parallel,d}(x, Q^2)$  and  $A_{\parallel,d}^{K^+K^-}(x, z, Q^2)$ , as well as  **$K^+K^-$  multiplicities on deuteron**

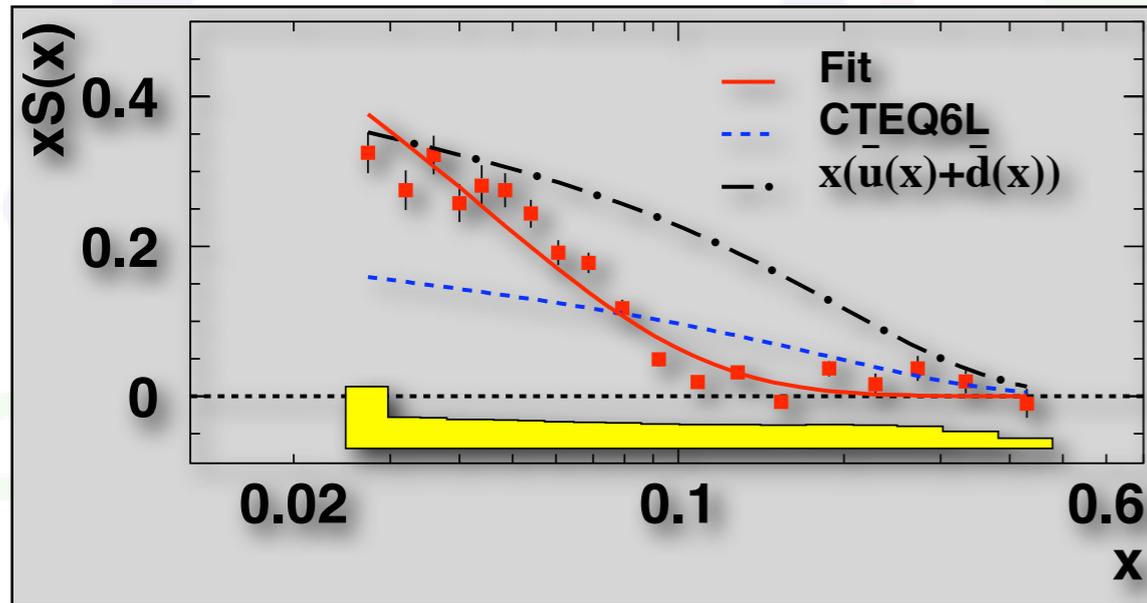
$$S(x) \int \mathcal{D}_S^K(z) dz \simeq Q(x) \left[ 5 \frac{d^2 N^K(x)}{d^2 N^{\text{DIS}}(x)} - \int \mathcal{D}_Q^K(z) dz \right]$$

$$A_{\parallel,d}(x) \frac{d^2 N^{\text{DIS}}(x)}{dx dQ^2} = \mathcal{K}_{LL}(x, Q^2) [5 \Delta Q(x) + 2 \Delta S(x)]$$

$$A_{\parallel,d}^{K^\pm} \frac{d^2 N^K(x)}{dx dQ^2} = \mathcal{K}_{LL}(x, Q^2) \left[ \Delta Q(x) \int \mathcal{D}_Q^K(z) dz + \Delta S(x) \int \mathcal{D}_S^K(z) dz \right]$$

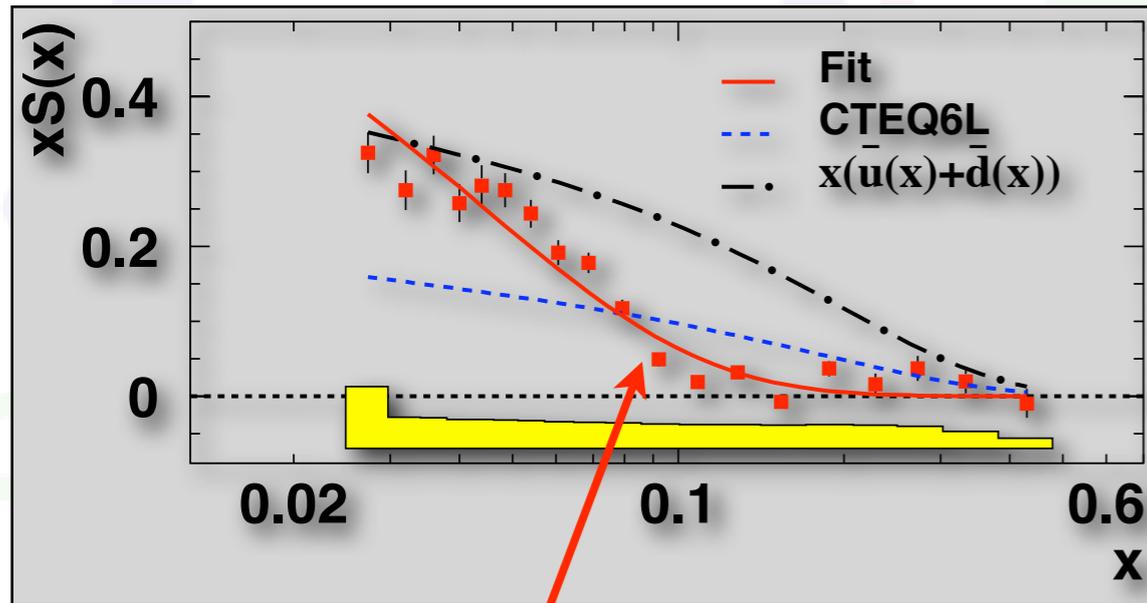
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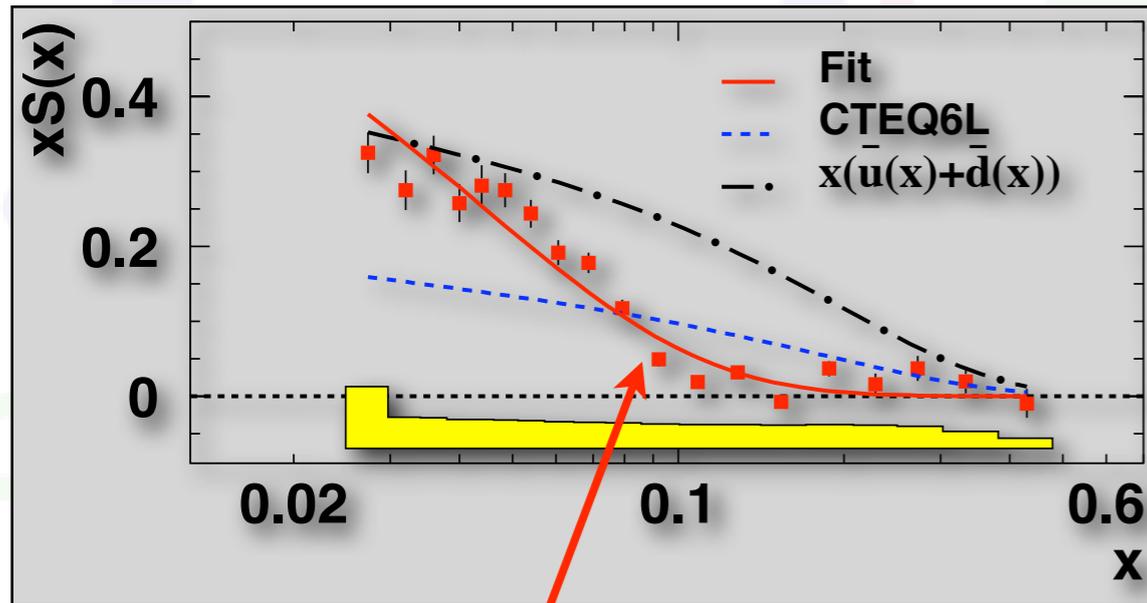


**Strange-quark distribution  
softer than (maybe) expected**

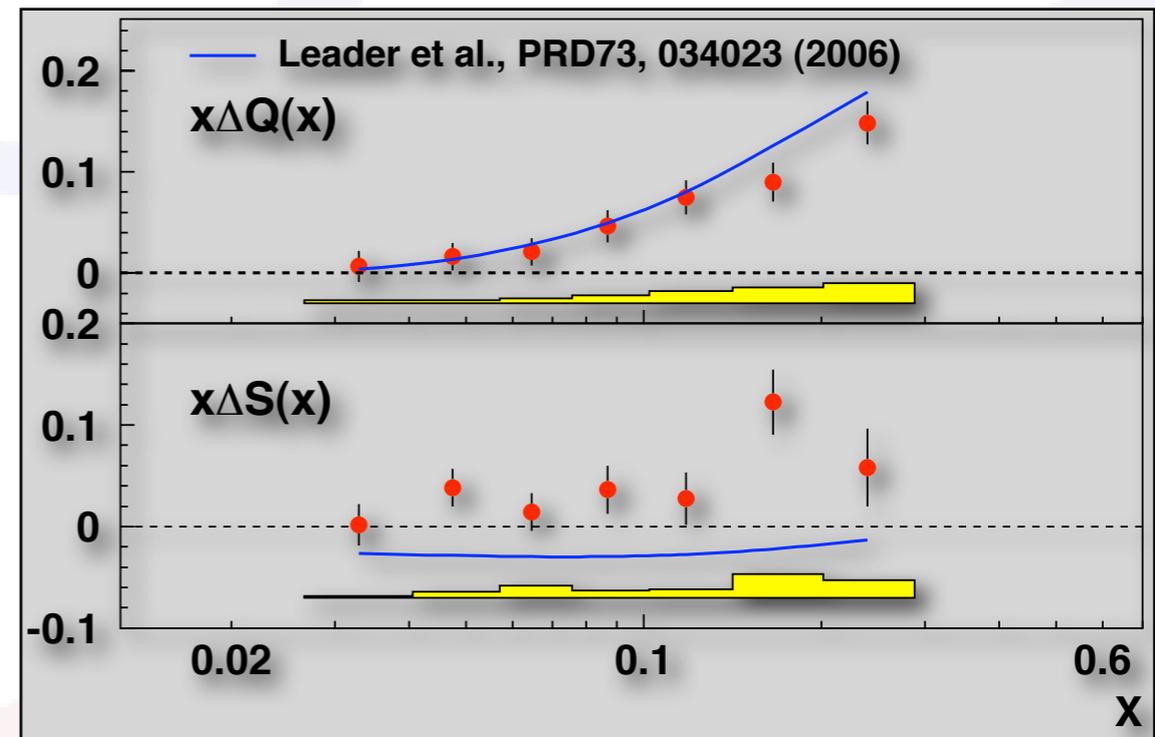
**A. Airapetian et al., PLB 666, 446 (2008)**

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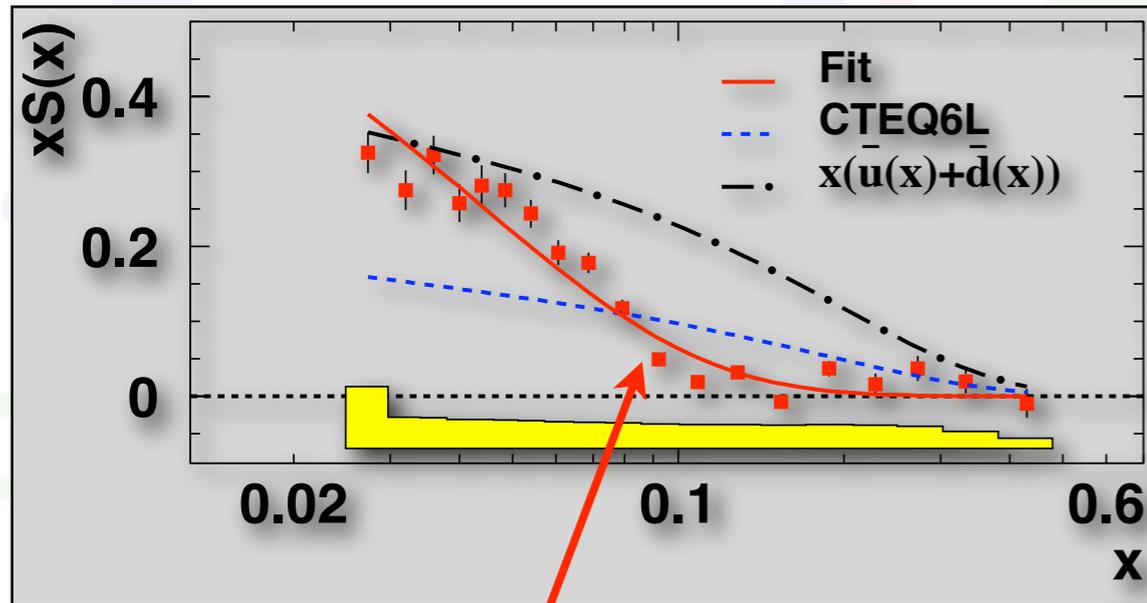


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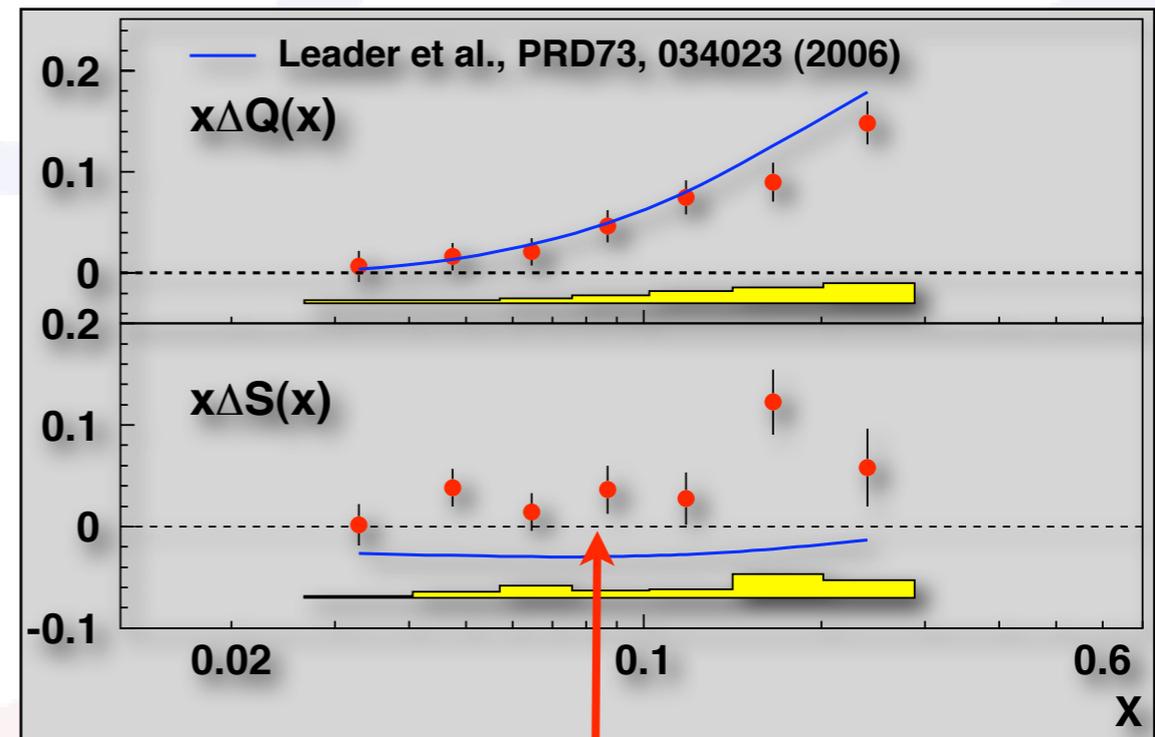


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Strange-quark distribution softer than (maybe) expected



Strange-quark helicity distribution consistent with zero or slightly positive in contrast to inclusive DIS analyses

A. Airapetian et al., PLB 666, 446 (2008)

# The "Trouble" with Transversity

chiral-odd transversity involves quark helicity flip

$$f_1^q = \text{[red circle with white center]}$$

$$g_1^q = \text{[red circle with white center and right-pointing arrow]} - \text{[red circle with white center and left-pointing arrow]}$$

$$h_1^q = \text{[red circle with white center and up-pointing arrow]} - \text{[red circle with white center and down-pointing arrow]}$$

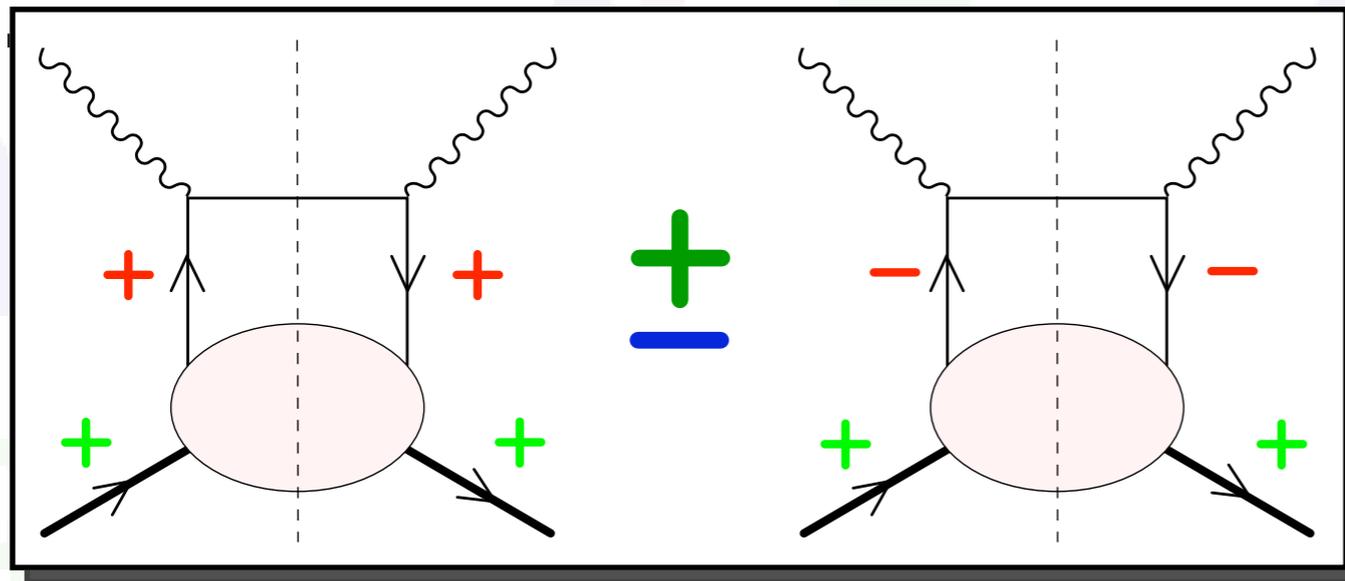
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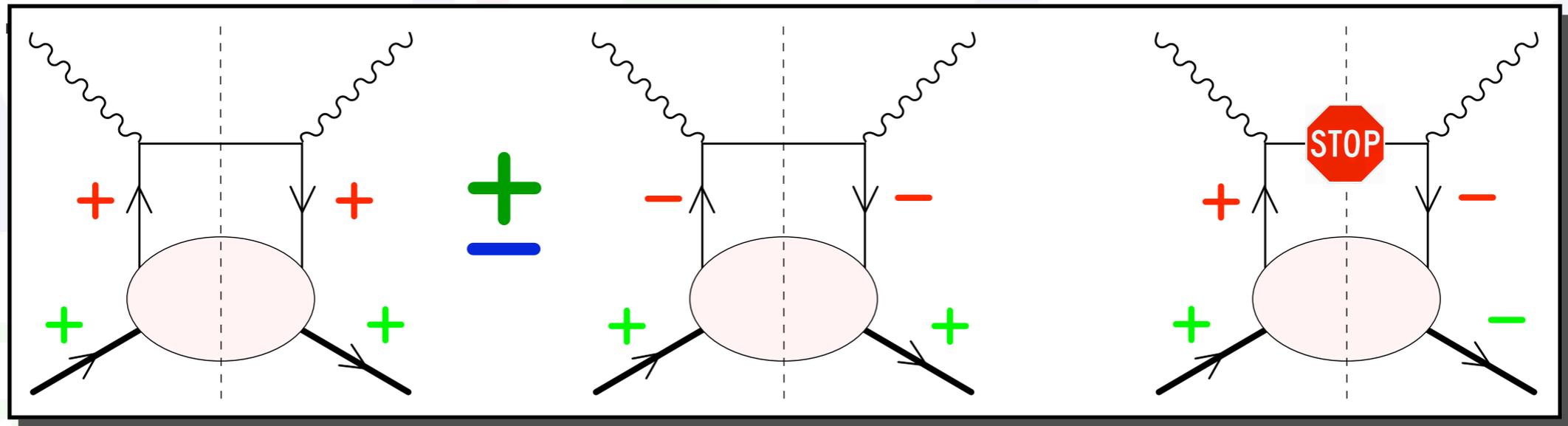
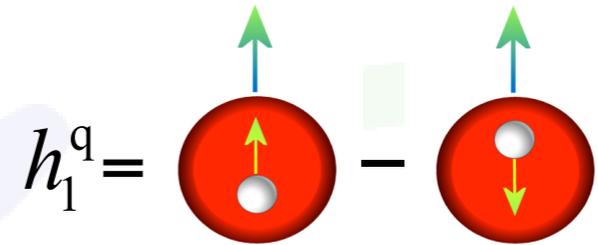
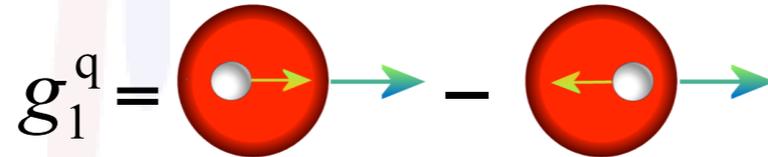
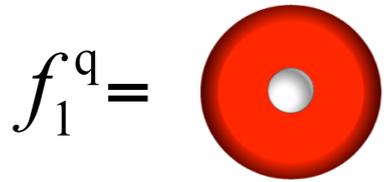
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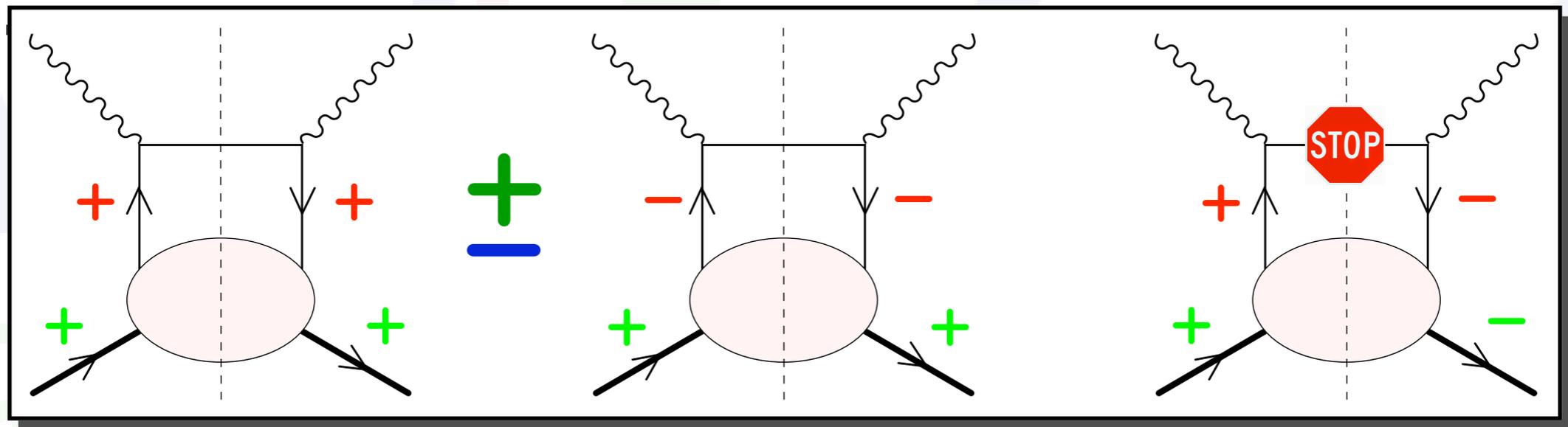
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need to couple to chiral-odd fragmentation function:

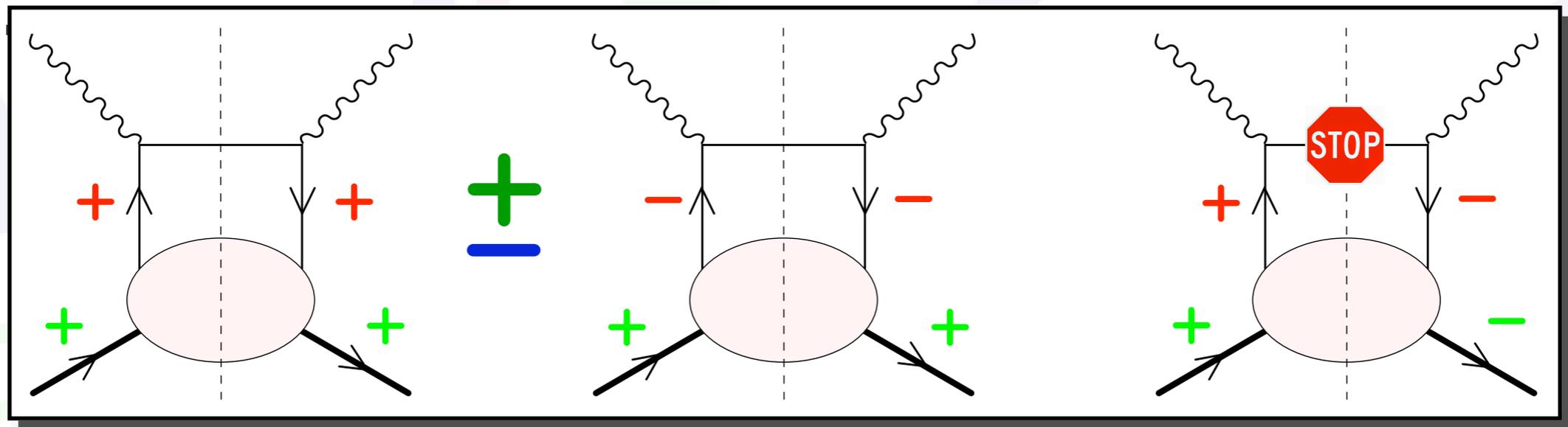
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- transverse spin transfer (polarized final-state hadron)

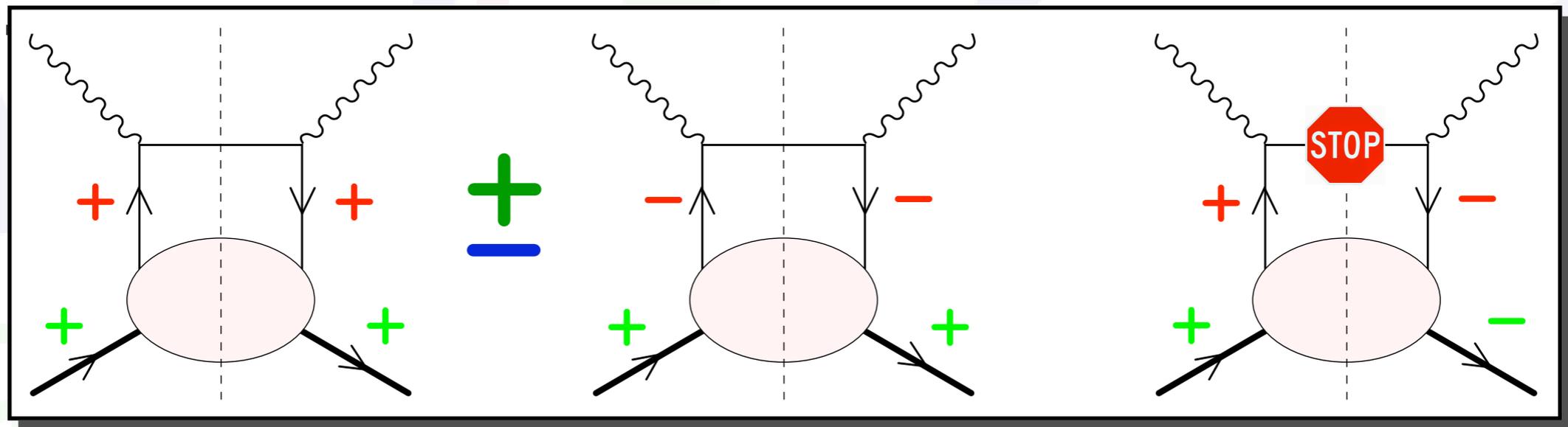
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- transverse spin transfer (polarized final-state hadron)
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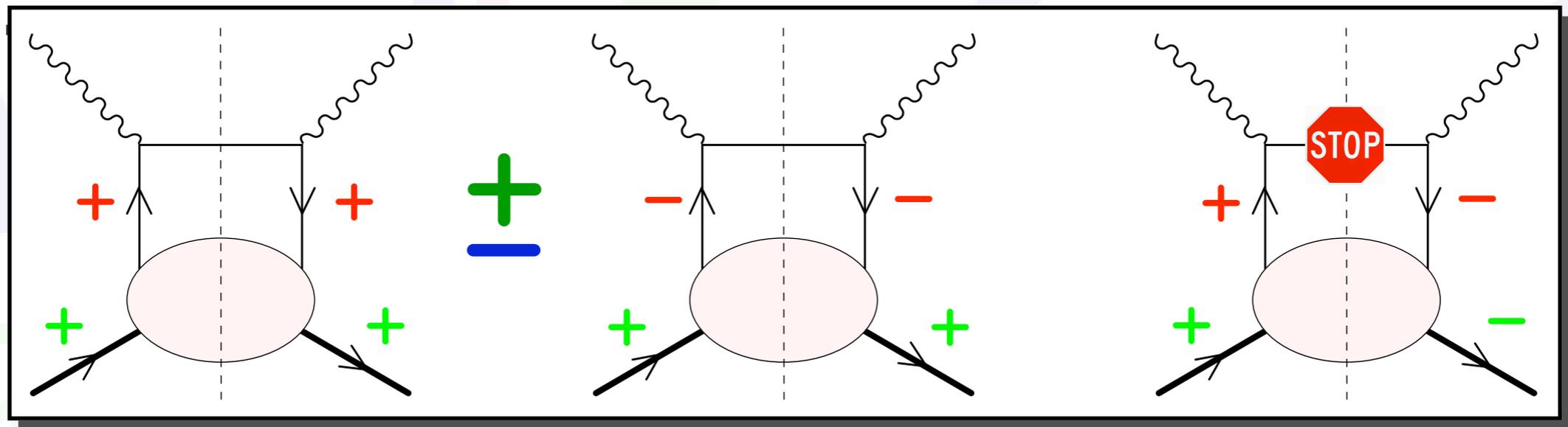
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need to couple to chiral-odd fragmentation function:

- transverse spin transfer (polarized final-state hadron)
- 2-hadron fragmentation
- Collins fragmentation

# 2-hadron fragmentation

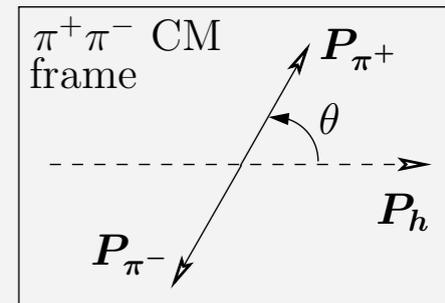
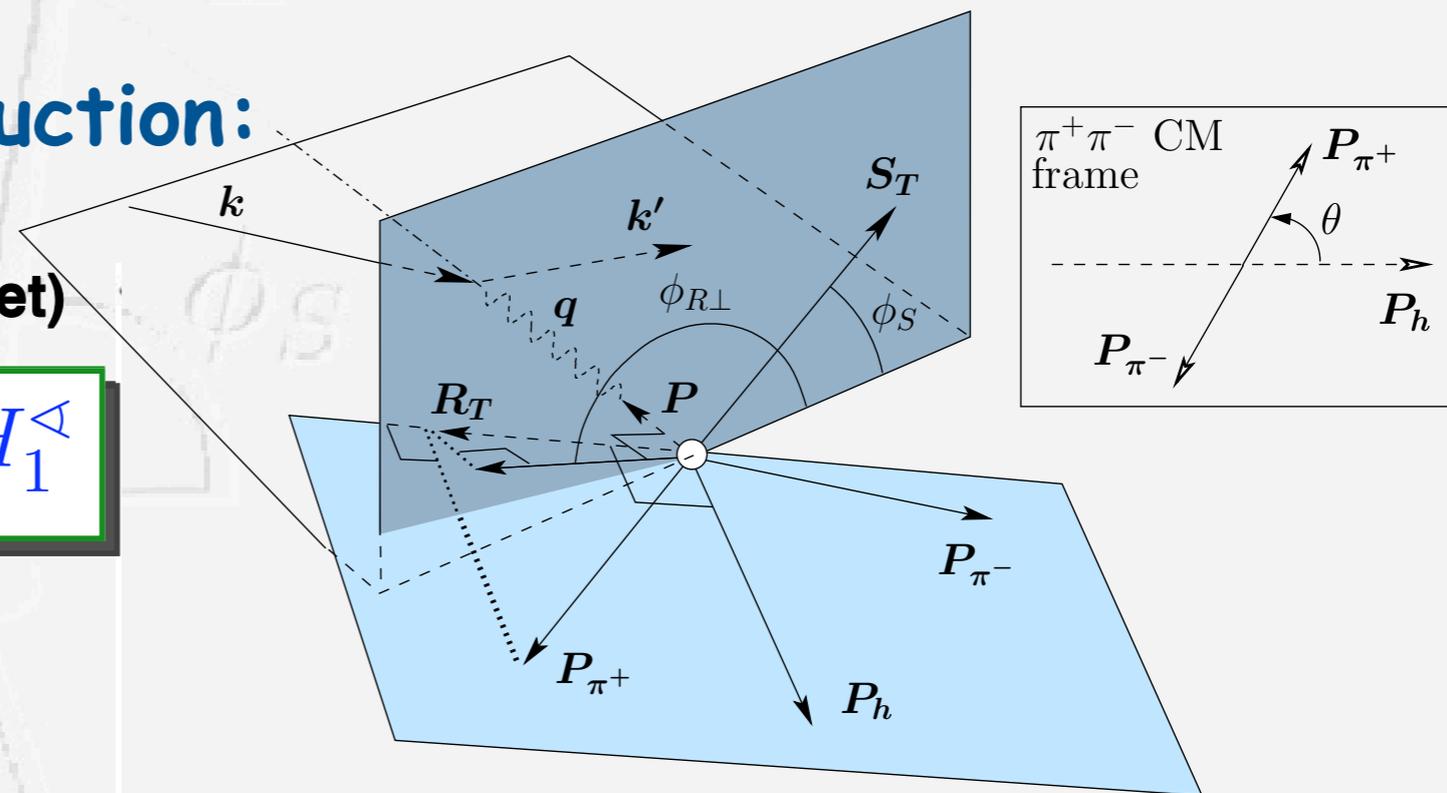
spin-dependent 2-hadron production:

(Unpolarized beam, Transversely pol. target)

$$\sigma_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sum e_q^2 h_1^q H_1^\Delta$$

$$H_1^\Delta = H_1^\Delta(z, \zeta, M_{\pi\pi}^2)$$

$$(\zeta \sim z_1/(z_1 + z_2))$$



# 2-hadron fragmentation

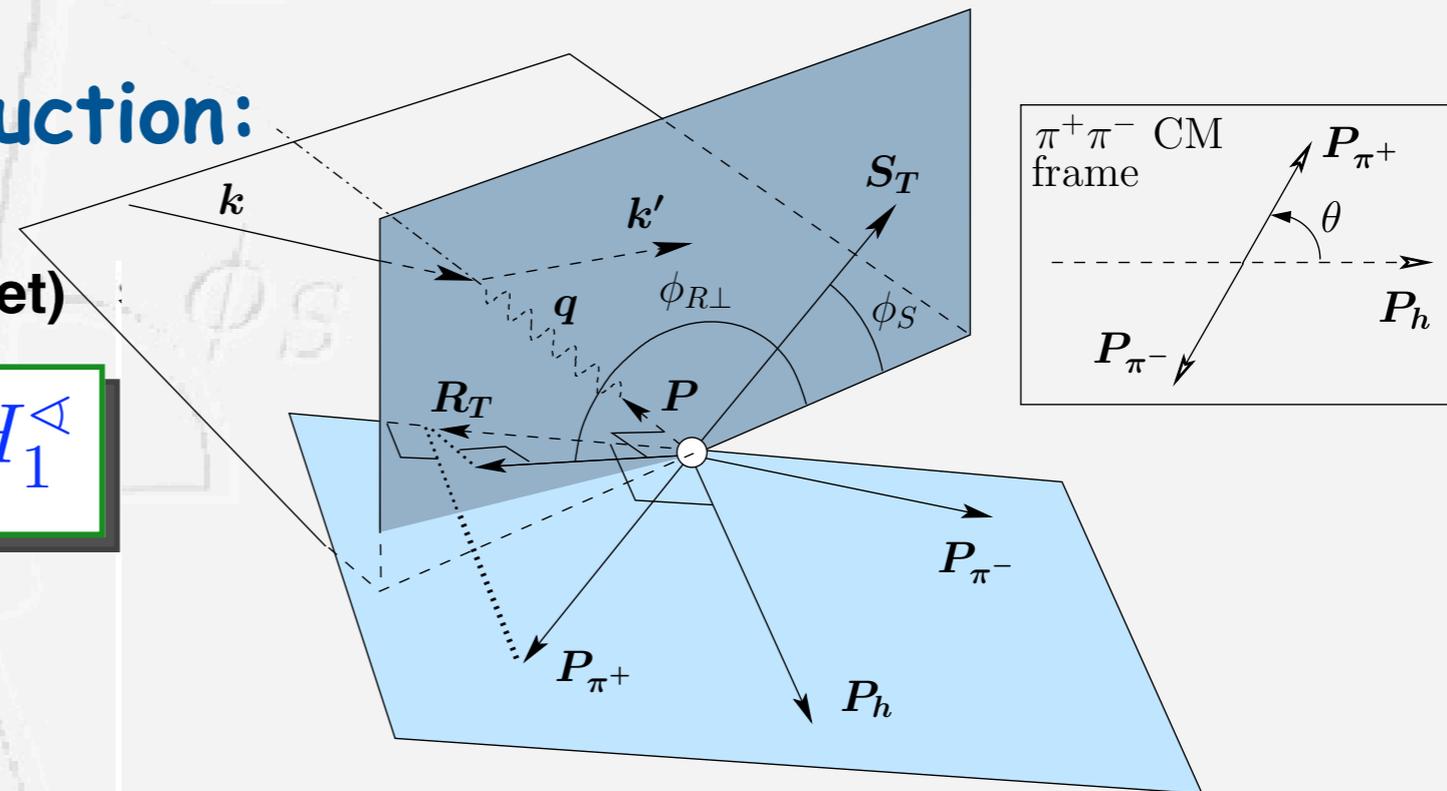
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😊 only relative momentum of hadron pair relevant

⇒ integration over transverse momentum of hadron pair simplifies factorization and  $Q^2$  evolution

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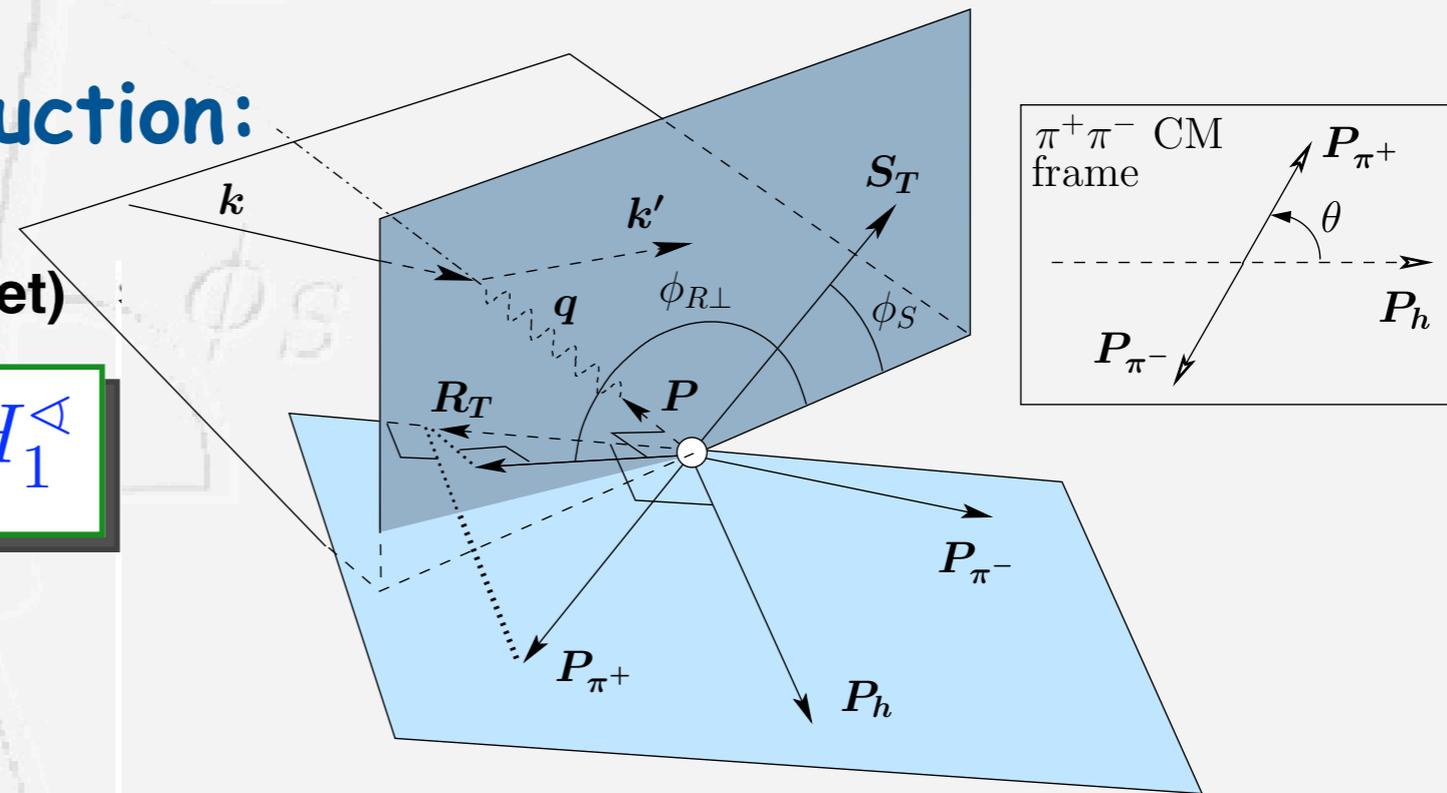
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$$H_1^{\triangleleft} = H_1^{\triangleleft}(z, \zeta, M_{\pi\pi}^2)$$

$$(\zeta \sim z_1/(z_1 + z_2))$$



😊 only relative momentum of hadron pair relevant

⇒ integration over transverse momentum of hadron pair simplifies factorization and  $Q^2$  evolution

😞 however, cross section becomes quite complex (differential in 9 variables)

# Model for two-pion fragmentation

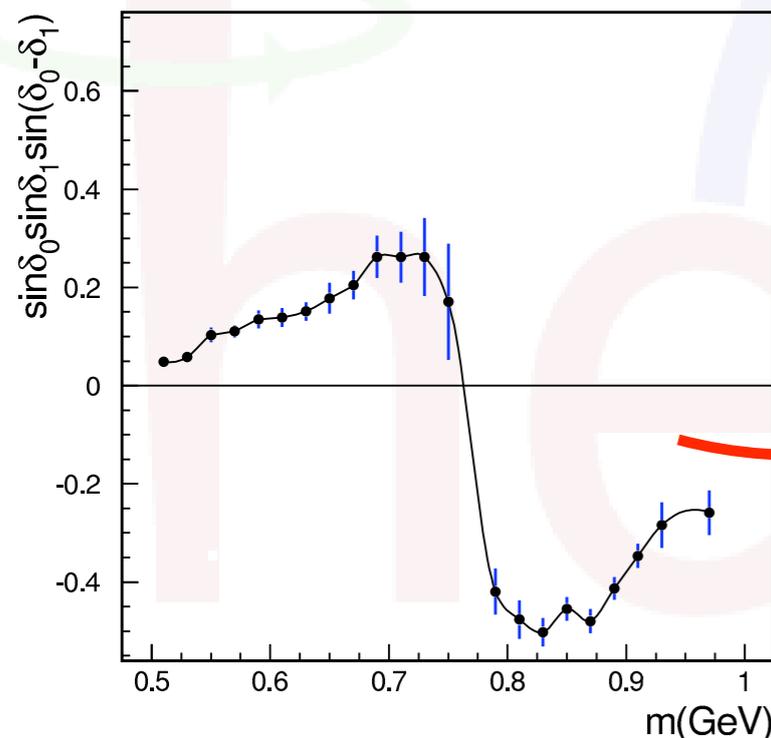
$$A_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sin \theta h_1 H_1^{\triangleleft}$$

Expansion of  $H_1^{\triangleleft}$  in Legendre moments:

$$H_1^{\triangleleft}(z, \cos \theta, M_{\pi\pi}^2) = H_1^{\triangleleft,sp}(z, M_{\pi\pi}^2) + \cos \theta H_1^{\triangleleft,pp}(z, M_{\pi\pi}^2)$$

describe interference between 2 pion pairs coming from different production channels.

about  $H_1^{\triangleleft,sp}$ :



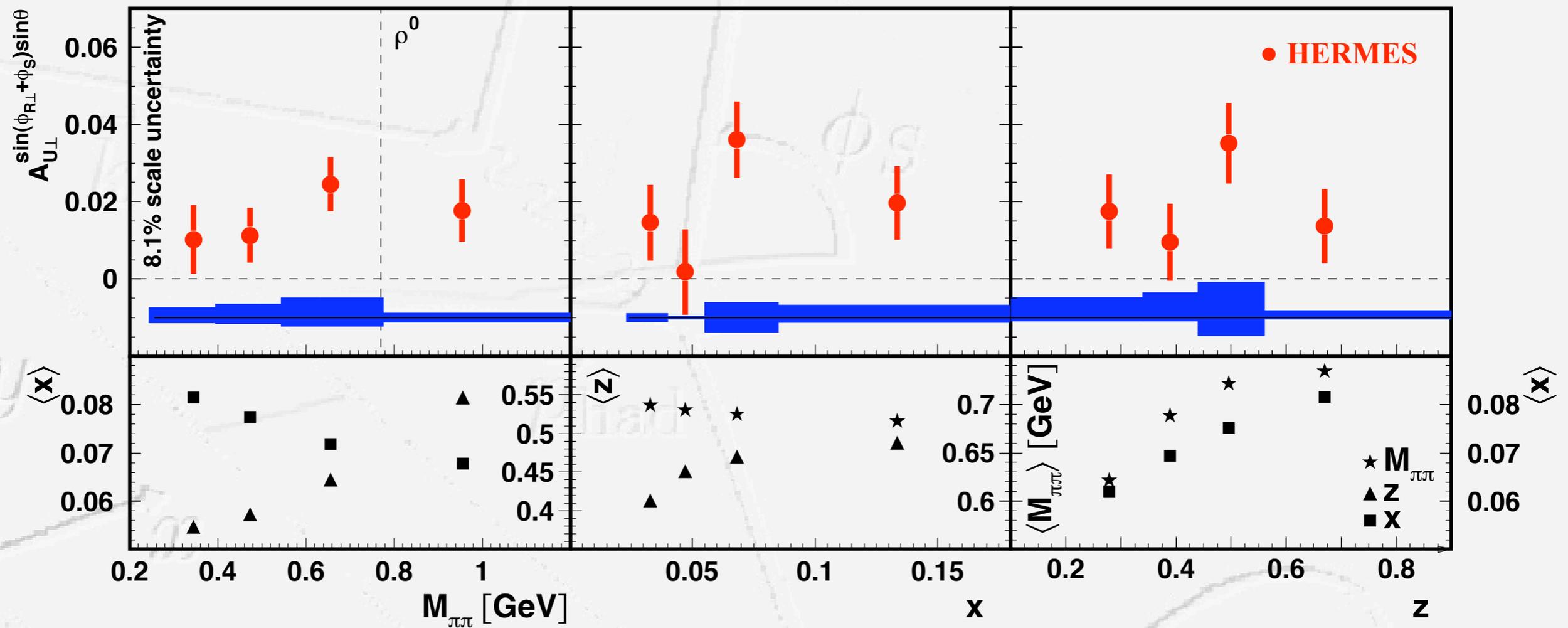
Jaffe et al. [[hep-ph/9709322](#)]:

$$H_1^{\triangleleft,sp}(z, M_{\pi\pi}^2) = \frac{\sin \delta_0 \sin \delta_1 \sin(\delta_0 - \delta_1) H_1^{\triangleleft,sp'}(z)}{\delta_0 (\delta_1) \rightarrow \text{S(P)-wave phase shifts}}$$

$$= \mathcal{P}(M_{\pi\pi}^2) H_1^{\triangleleft,sp'}(z)$$

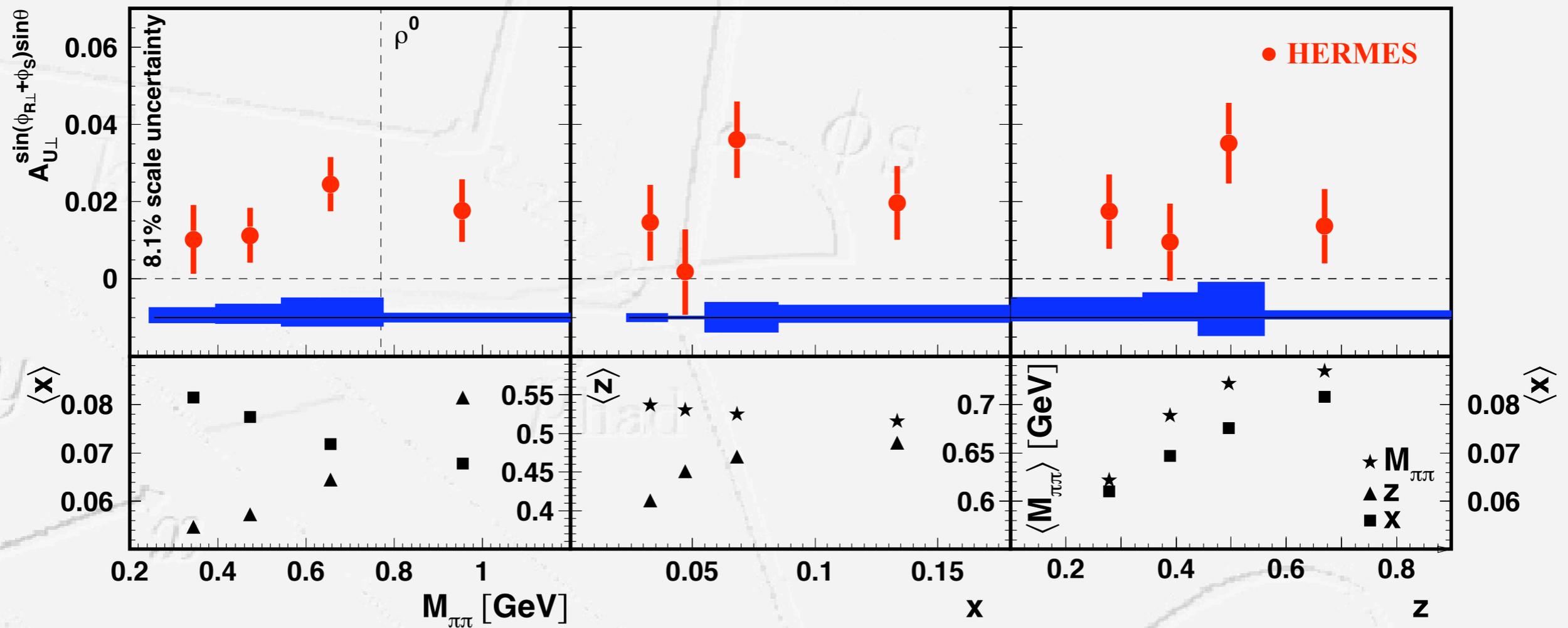
$\Rightarrow A_{UT}$  might depend strongly on  $M_{\pi\pi}$

# HERMES results (complete data)



A. Airapetian et al., JHEP 0806:017, 2008

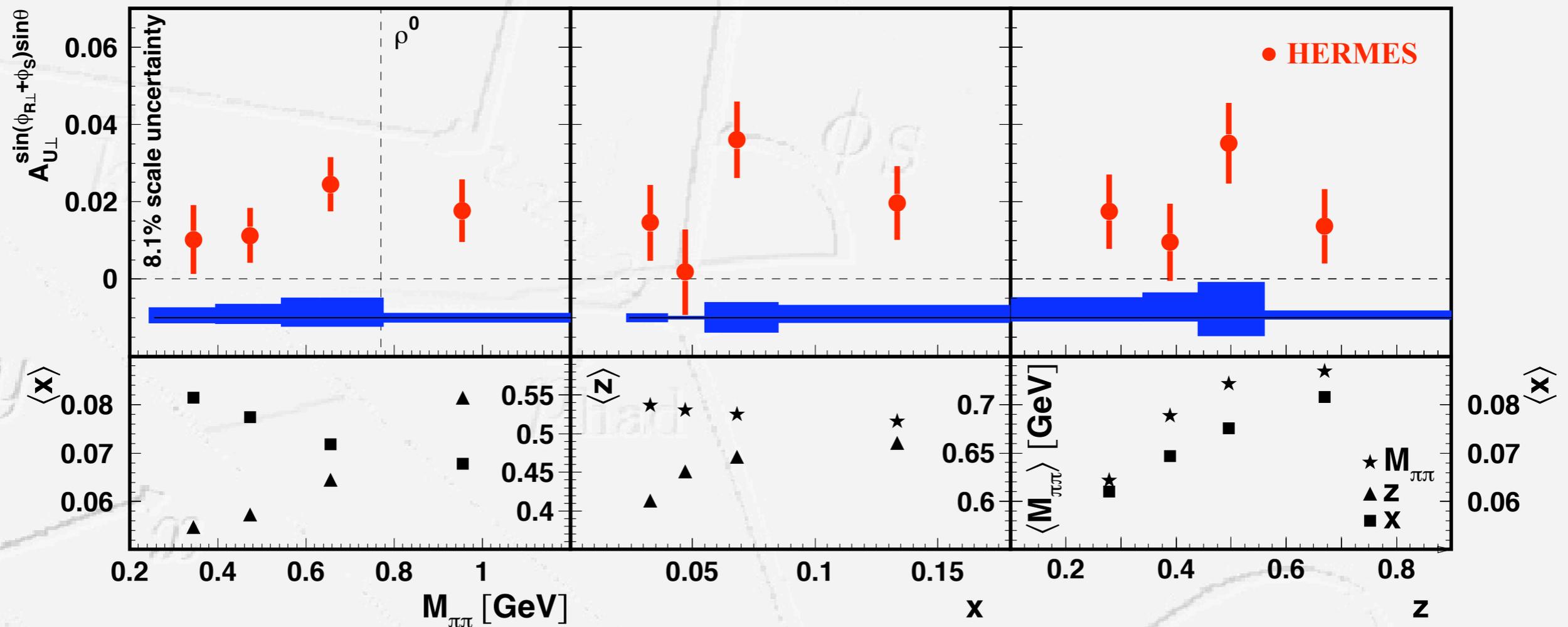
# HERMES results (complete data)



first evidence for T-odd 2-hadron fragmentation function in semi-inclusive DIS!

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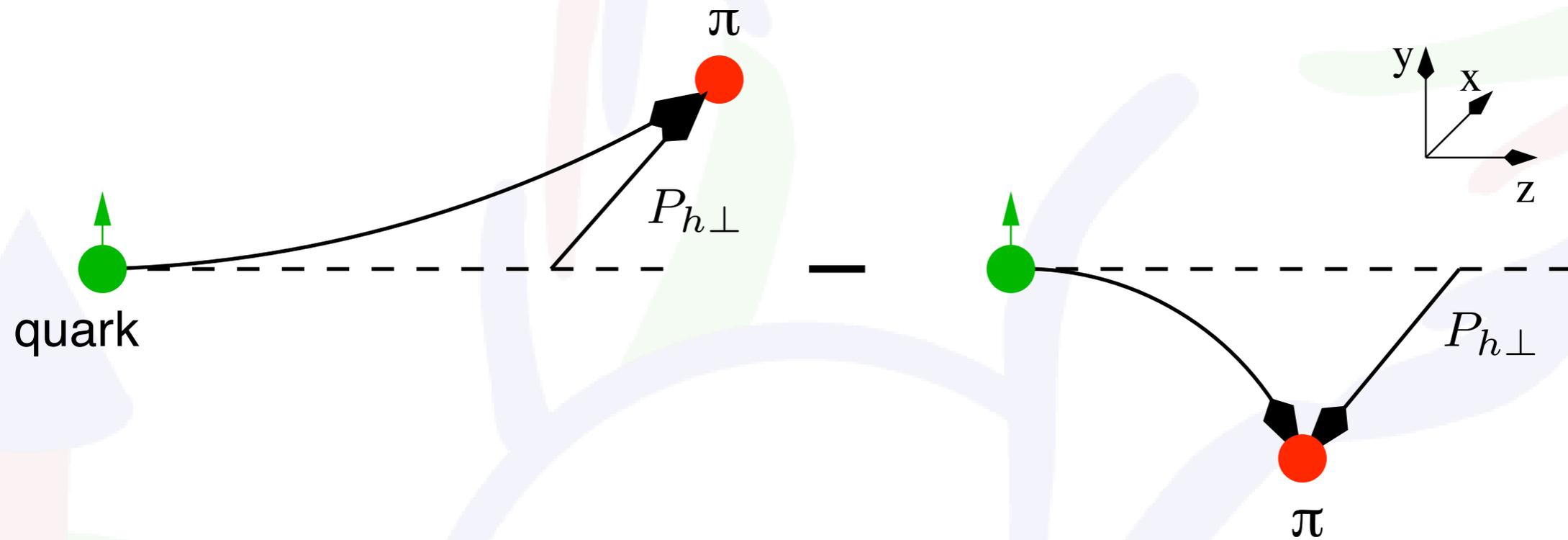
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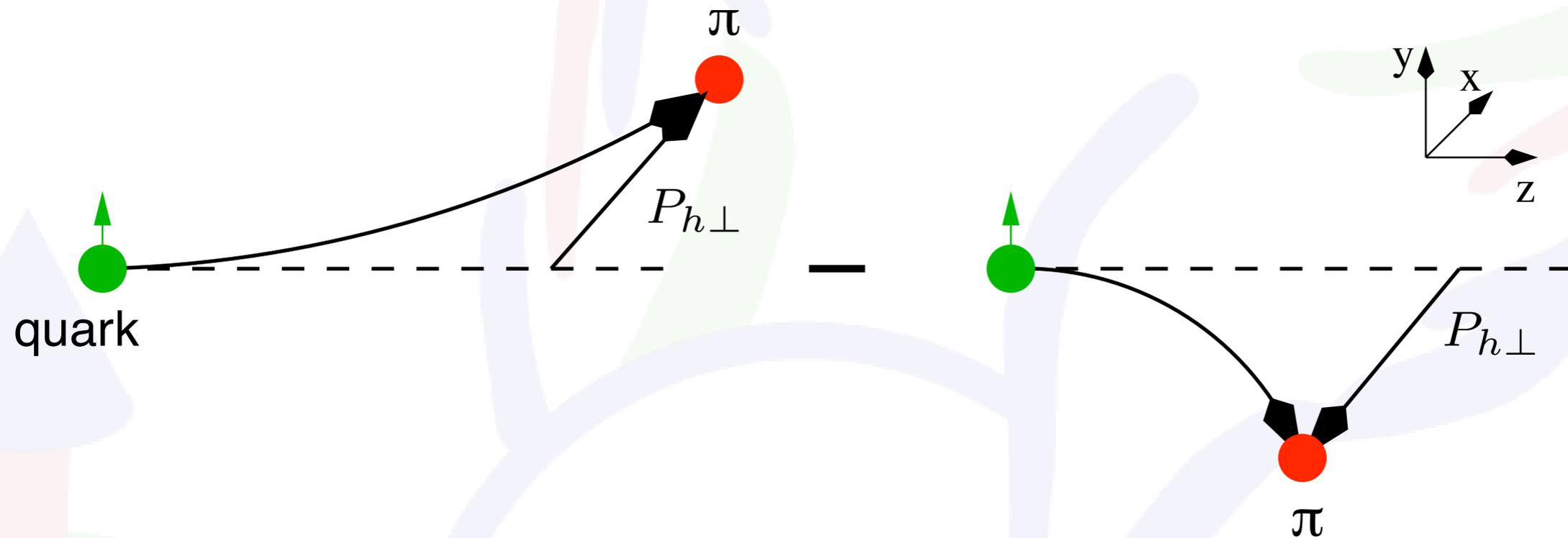
- ☑ first evidence for T-odd 2-hadron fragmentation function in semi-inclusive DIS!
- ☑ invariant-mass dependence rules out Jaffe model

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# Collins fragmentation function

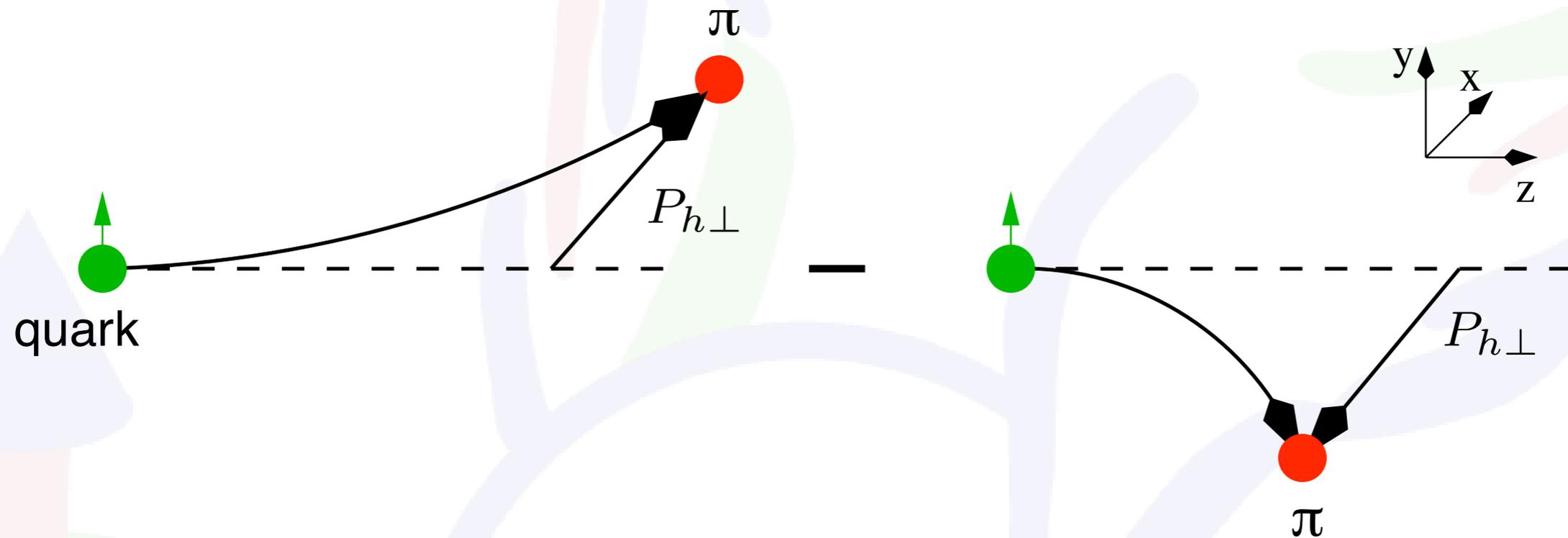


# Collins fragmentation function



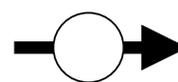
😊 provides a correlation between spin of quark and transverse momentum of produced hadron

# Collins fragmentation function



- 😊 provides a correlation between spin of quark and transverse momentum of produced hadron
- 😊 example of transverse-momentum-dependent ("unintegrated") parton distribution/fragmentation functions

# Unintegrated PDFs

  nucleon with transverse or longitudinal spin

  parton with transverse or longitudinal spin

 parton transverse momentum

$$f_1 = \text{[Diagram: Circle with red parton]}$$

$$g_1 = \text{[Diagram: Circle with nucleon and parton, spin up]} - \text{[Diagram: Circle with nucleon and parton, spin down]}$$

$$h_1 = \text{[Diagram: Circle with nucleon and parton, transverse spin right]} - \text{[Diagram: Circle with nucleon and parton, transverse spin left]}$$

$$f_{1T}^\perp = \text{[Diagram: Circle with nucleon and parton, transverse momentum down]} - \text{[Diagram: Circle with nucleon and parton, transverse momentum up]}$$

$$h_1^\perp = \text{[Diagram: Circle with nucleon and parton, transverse momentum down, transverse spin right]} - \text{[Diagram: Circle with nucleon and parton, transverse momentum up, transverse spin right]}$$

$$g_{1T} = \text{[Diagram: Circle with nucleon and parton, transverse momentum right, longitudinal spin up]} - \text{[Diagram: Circle with nucleon and parton, transverse momentum left, longitudinal spin up]}$$

$$h_{1L}^\perp = \text{[Diagram: Circle with nucleon and parton, transverse momentum right, longitudinal spin up]} - \text{[Diagram: Circle with nucleon and parton, transverse momentum left, longitudinal spin up]}$$

$$h_{1T}^\perp = \text{[Diagram: Circle with nucleon and parton, transverse momentum right, transverse spin right]} - \text{[Diagram: Circle with nucleon and parton, transverse momentum left, transverse spin right]}$$

# 1-hadron production ( $ep \rightarrow ehX$ )

$$d\sigma = d\sigma_{UU}^0 + \cos 2\phi d\sigma_{UU}^1 + \frac{1}{Q} \cos \phi d\sigma_{UU}^2 + \lambda_e \frac{1}{Q} \sin \phi d\sigma_{LU}^3$$

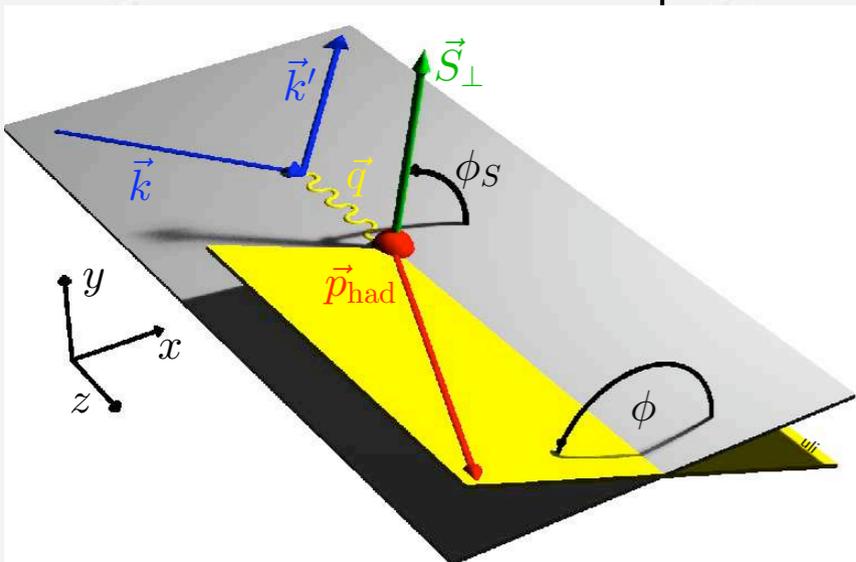
$$+ S_L \left\{ \sin 2\phi d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[ d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\}$$

$$+ S_T \left\{ \sin(\phi - \phi_S) d\sigma_{UT}^8 + \sin(\phi + \phi_S) d\sigma_{UT}^9 + \sin(3\phi - \phi_S) d\sigma_{UT}^{10} \frac{1}{Q} \right.$$

$$\left. + \frac{1}{Q} (\sin(2\phi - \phi_S) d\sigma_{UT}^{11} + \sin \phi_S d\sigma_{UT}^{12}) \right.$$

$\sigma_{XY}$   
 ↙ ↘  
**Beam Target**  
**Polarization**

$$+ \lambda_e \left[ \cos(\phi - \phi_S) d\sigma_{LT}^{13} + \frac{1}{Q} (\cos \phi_S d\sigma_{LT}^{14} + \cos(2\phi - \phi_S) d\sigma_{LT}^{15}) \right] \left. \right\}$$



**Mulders and Tangermann, Nucl. Phys. B 461 (1996) 197**

**Boer and Mulders, Phys. Rev. D 57 (1998) 5780**

**Bacchetta et al., Phys. Lett. B 595 (2004) 309**

**Bacchetta et al., JHEP 0702 (2007) 093**

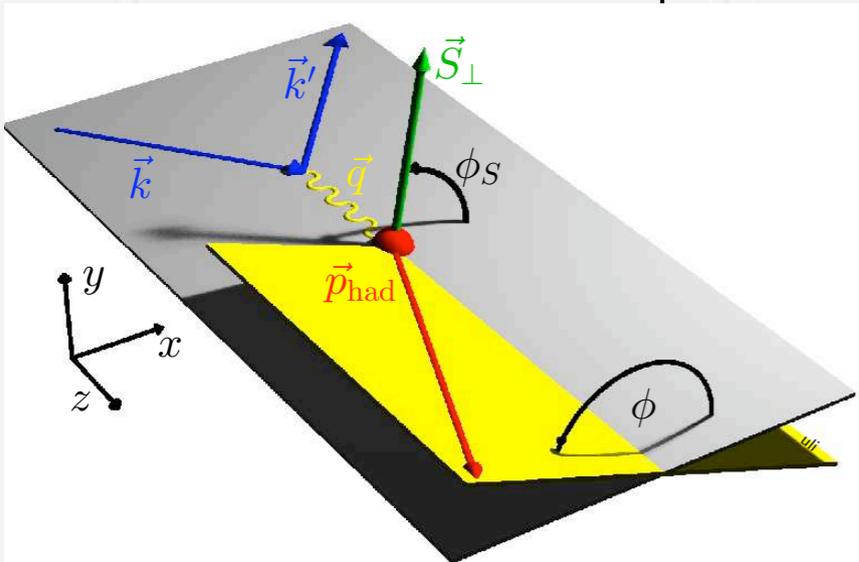
**“Trento Conventions”, Phys. Rev. D 70 (2004) 117504**

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 & + S_L \left\{ \sin 2\phi d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[ d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\} \\
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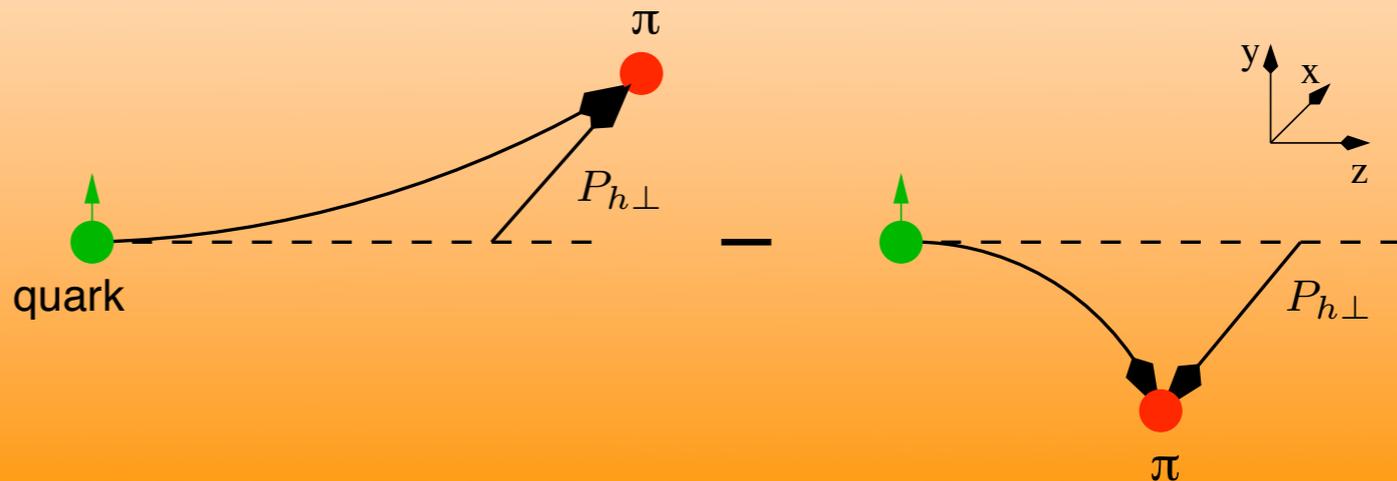
$\sigma_{XY}$   
 Beam Polarization  
 Target Polarization

$$+ \frac{1}{Q} + \lambda_e \left[ \cos(\phi - \phi_S) \right]$$



## Collins Effect:

sensitive to quark transverse spin

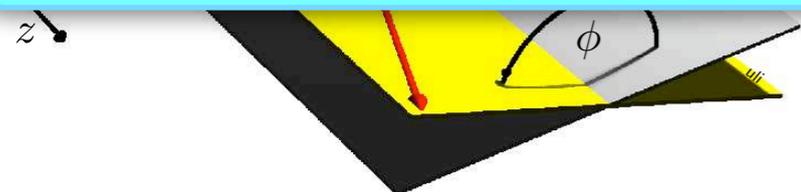


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 \end{aligned}$$

## Sivers Effect:

- correlates hadron's transverse momentum with nucleon spin
- requires orbital angular momentum



Bacchetta et al., JHEP 0702 (2007) 093

“Trento Conventions”, Phys. Rev. D 70 (2004) 117504

$d\sigma_{UT}^{12}$ )

$+ \cos(2\phi - \phi_S) d\sigma_{LT}^{15}$ )

Phys. B 461 (1996) 197

57 (1998) 5780

95 (2004) 309

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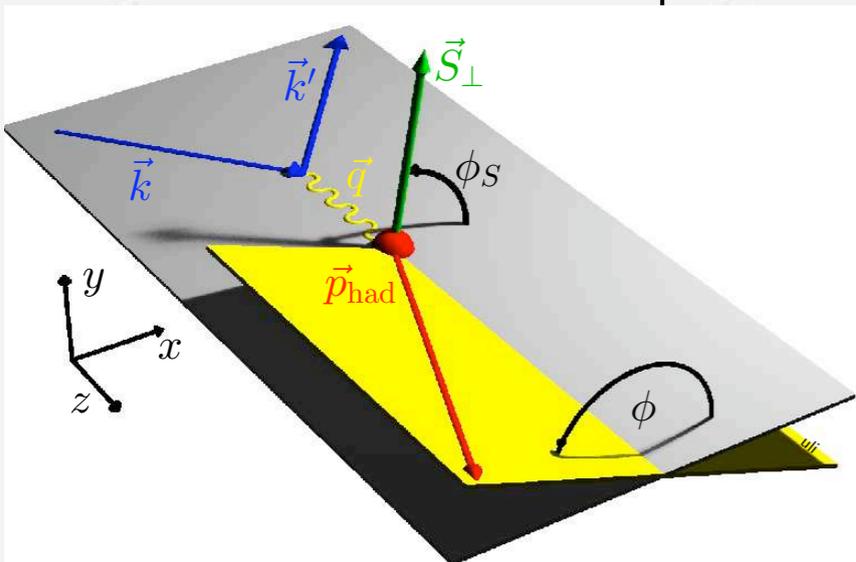
$$+ S_L \left\{ \sin 2\phi d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[ d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\}$$

$$+ S_T \left\{ \sin(\phi - \phi_S) d\sigma_{UT}^8 + \sin(\phi + \phi_S) d\sigma_{UT}^9 + \sin(3\phi - \phi_S) d\sigma_{UT}^{10} \frac{1}{Q} \right.$$

$$\left. + \frac{1}{Q} (\sin(2\phi - \phi_S) d\sigma_{UT}^{11} + \sin \phi_S d\sigma_{UT}^{12}) \right.$$

$\sigma_{XY}$   
 Beam Target  
 Polarization

$$\left. + \lambda_e \left[ \cos(\phi - \phi_S) d\sigma_{LT}^{13} + \frac{1}{Q} (\cos \phi_S d\sigma_{LT}^{14} + \cos(2\phi - \phi_S) d\sigma_{LT}^{15}) \right] \right\}$$



Mulders and Tangermann, Nucl. Phys. B 461 (1996) 197

Boer and Mulders, Phys. Rev. D 57 (1998) 5780

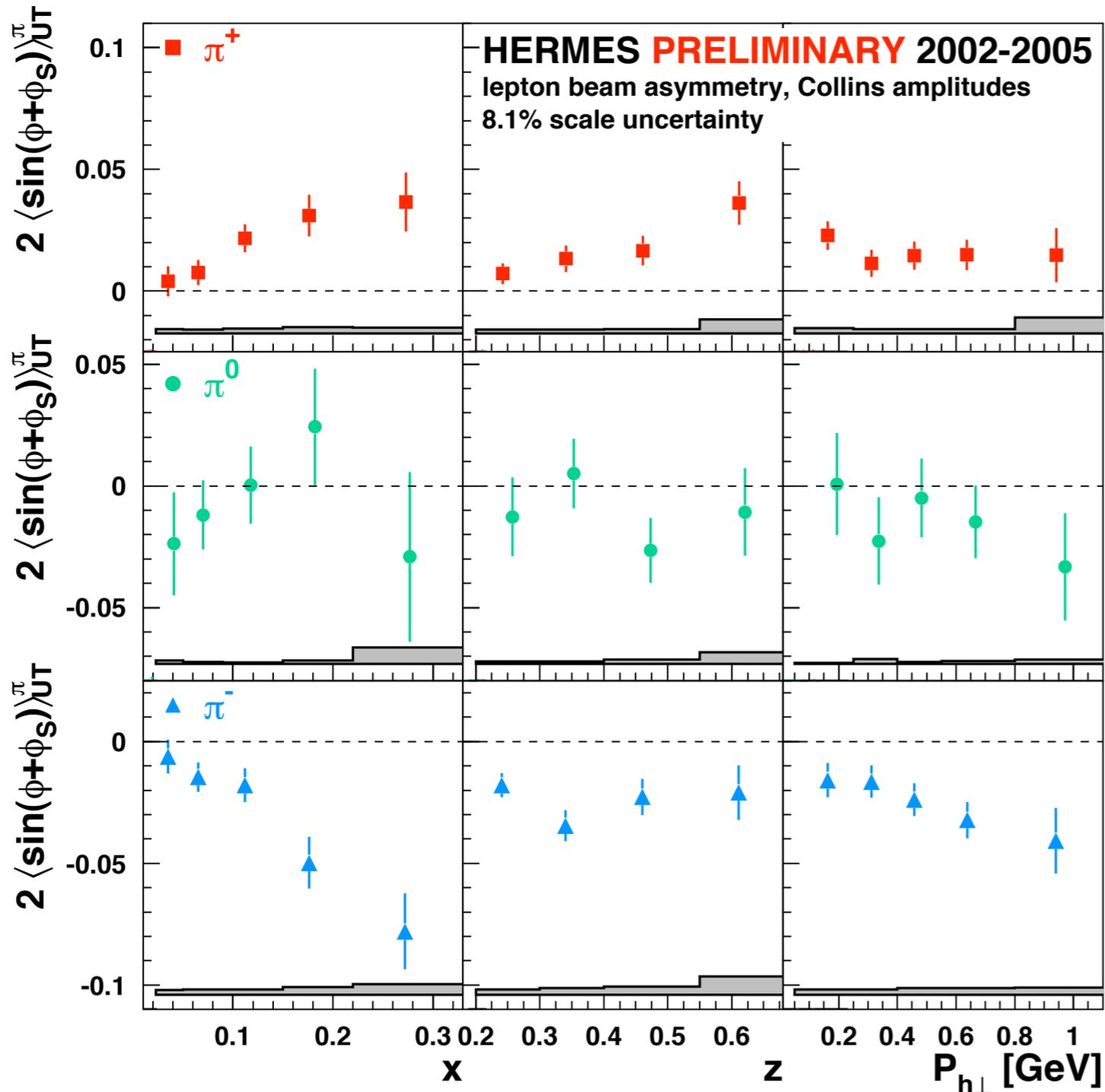
Bacchetta et al., Phys. Lett. B 595 (2004) 309

Bacchetta et al., JHEP 0702 (2007) 093

“Trento Conventions”, Phys. Rev. D 70 (2004) 117504

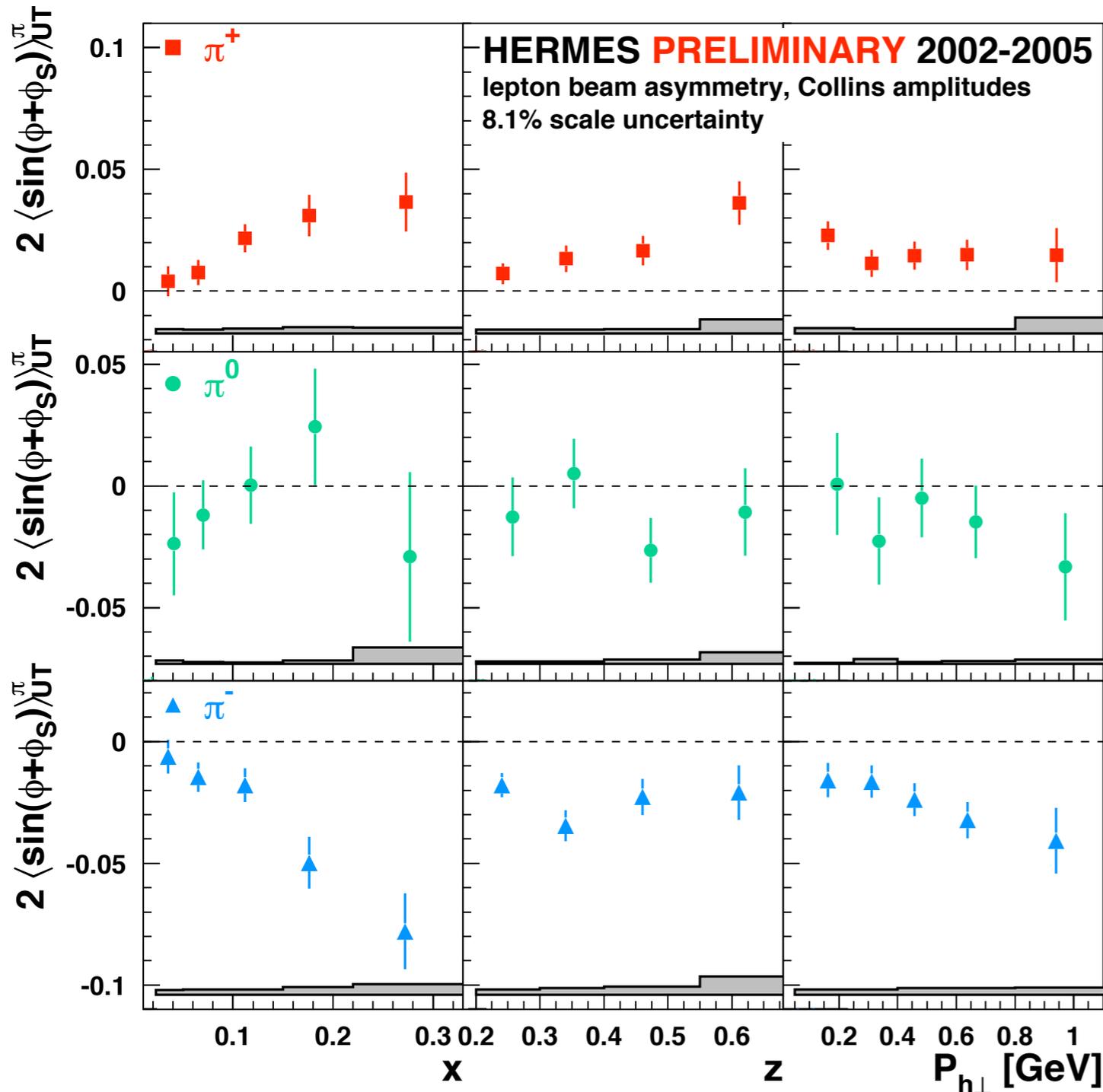
# The HERMES Collins amplitudes

$$2\langle \sin(\phi + \phi_S) \rangle_{\text{UT}} = - \frac{\sum_q e_q^2 h_1^q(x, p_T^2) \otimes H_1^{\perp,q}(z, K_T^2)}{\sum_q e_q^2 f_1^q(x) D_1^q(z)}$$



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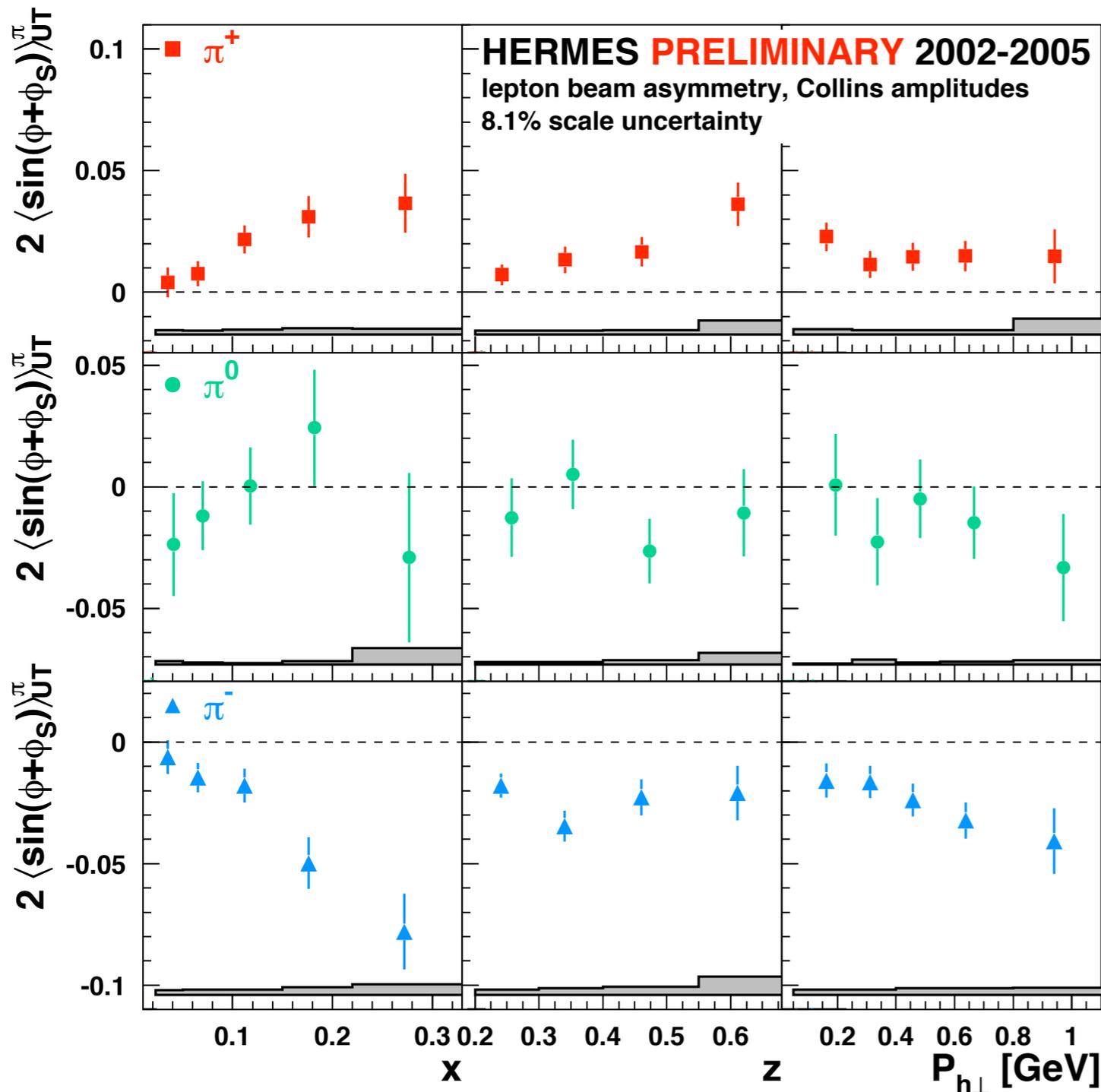
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☑ non-zero Collins effect observed!

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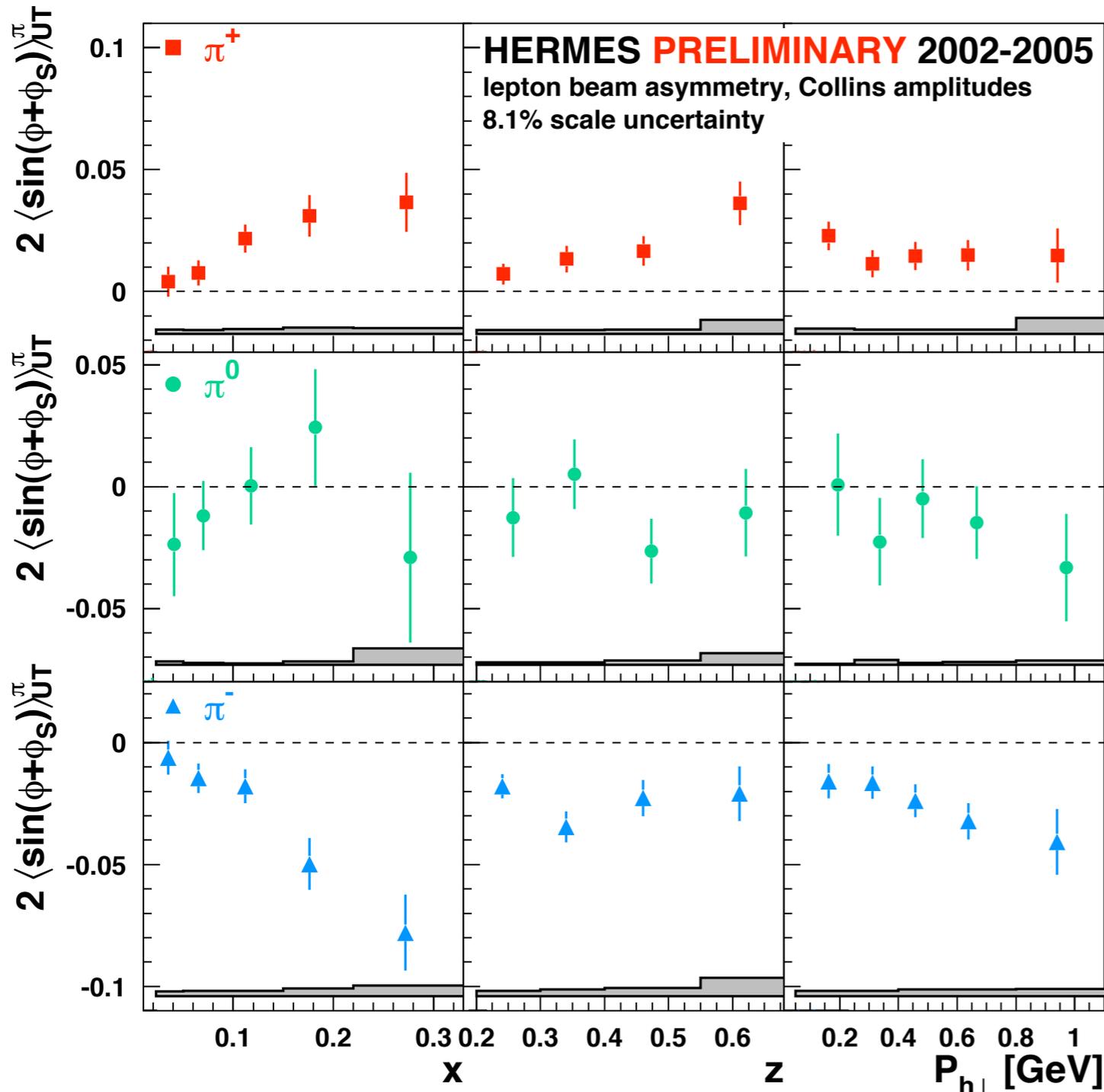
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- non-zero Collins effect observed!
- both Collins FF and transversity sizeable

# The HERMES Collins amplitudes

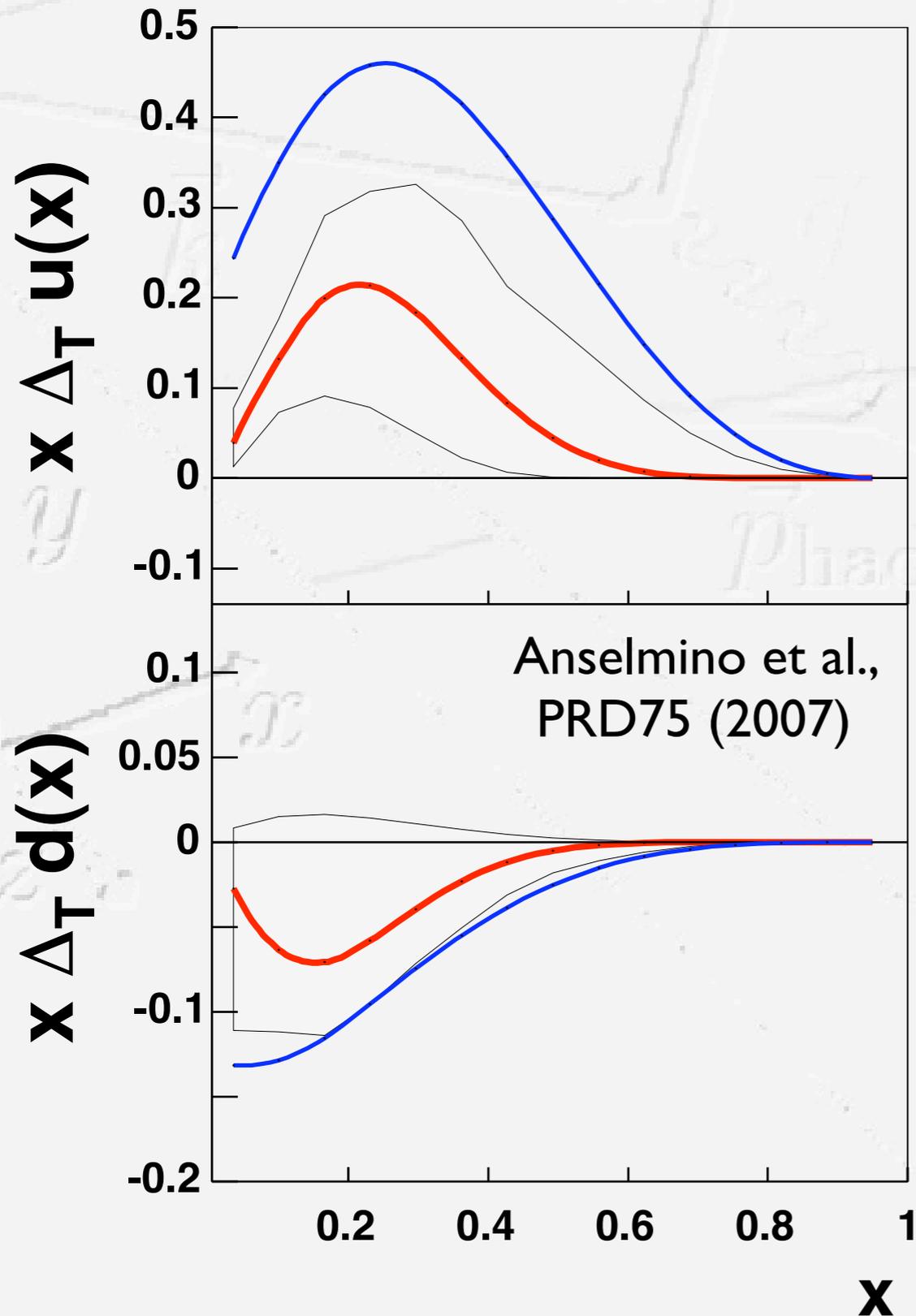
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- ☛ published<sup>†</sup> results **confirmed** with much higher statistical precision
- ☛ overall scale uncertainty of 8.1%
- ☛ positive for  $\pi^+$  and negative for  $\pi^-$  as maybe expected ( $\delta u \equiv h_1^u > 0$   
 $\delta d \equiv h_1^d < 0$ )
- ☛ unexpected **large  $\pi^-$  asymmetry**  
⇒ role of **disfavored Collins FF**  
most likely:  $H_1^{\perp,disf} \approx -H_1^{\perp,fav}$
- ☛ isospin symmetry among charged and neutral pions fulfilled

<sup>†</sup> [A. Airapetian et al, Phys. Rev. Lett. 94 (2005) 012002]

# First glimpse at transversity



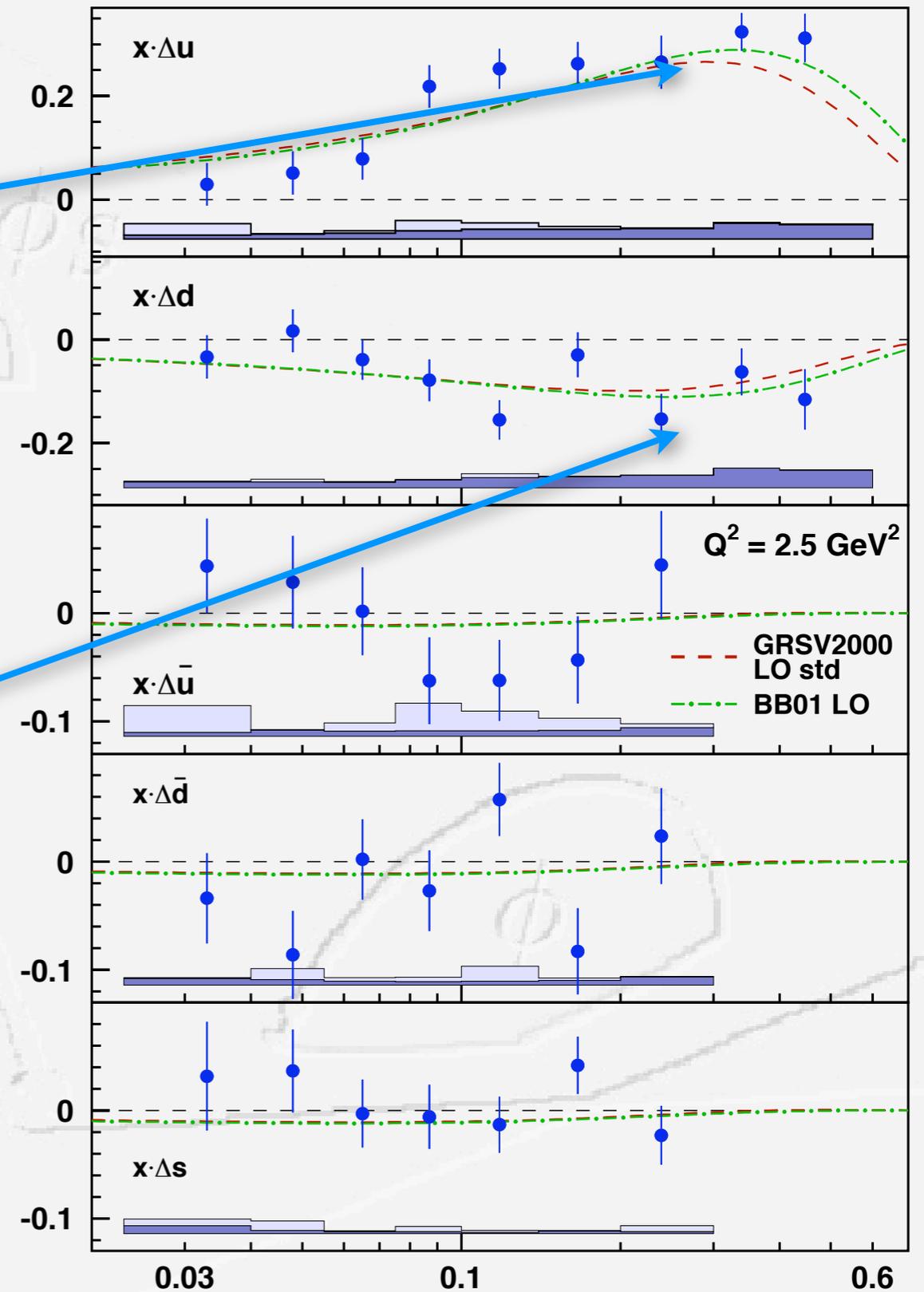
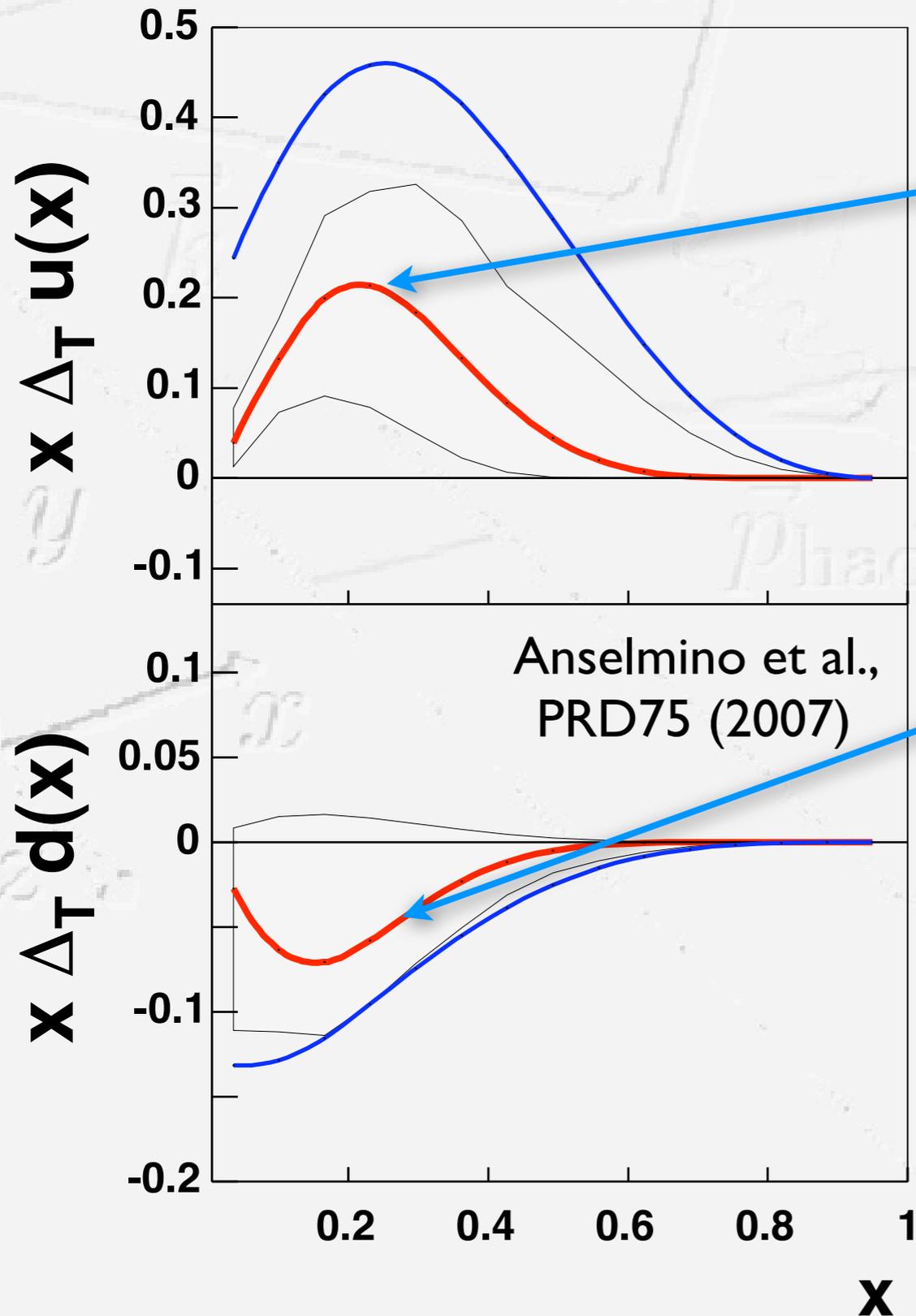
Combined analysis of data from:

● HERMES

● COMPASS

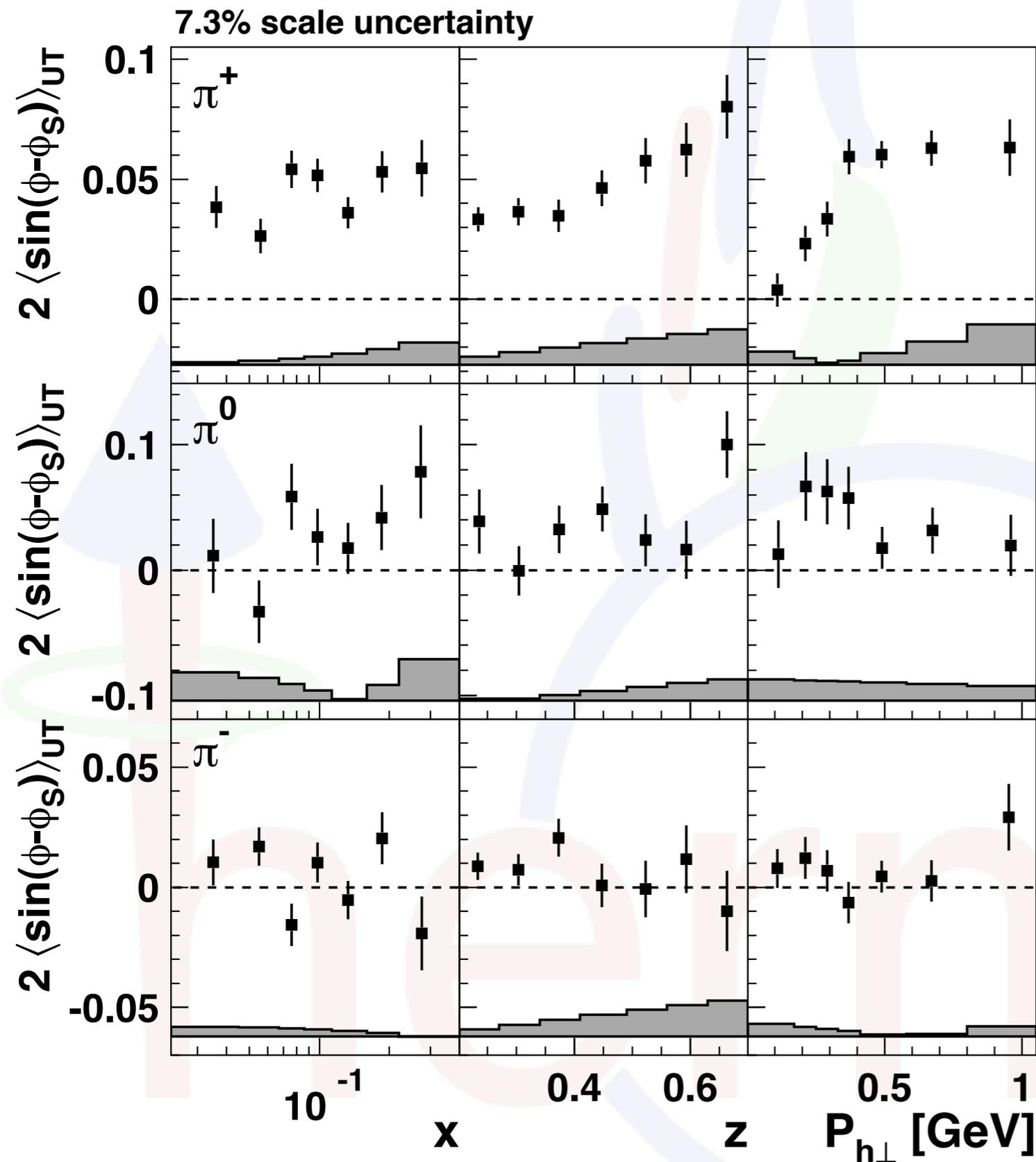
● BELLE

# First glimpse at transversity

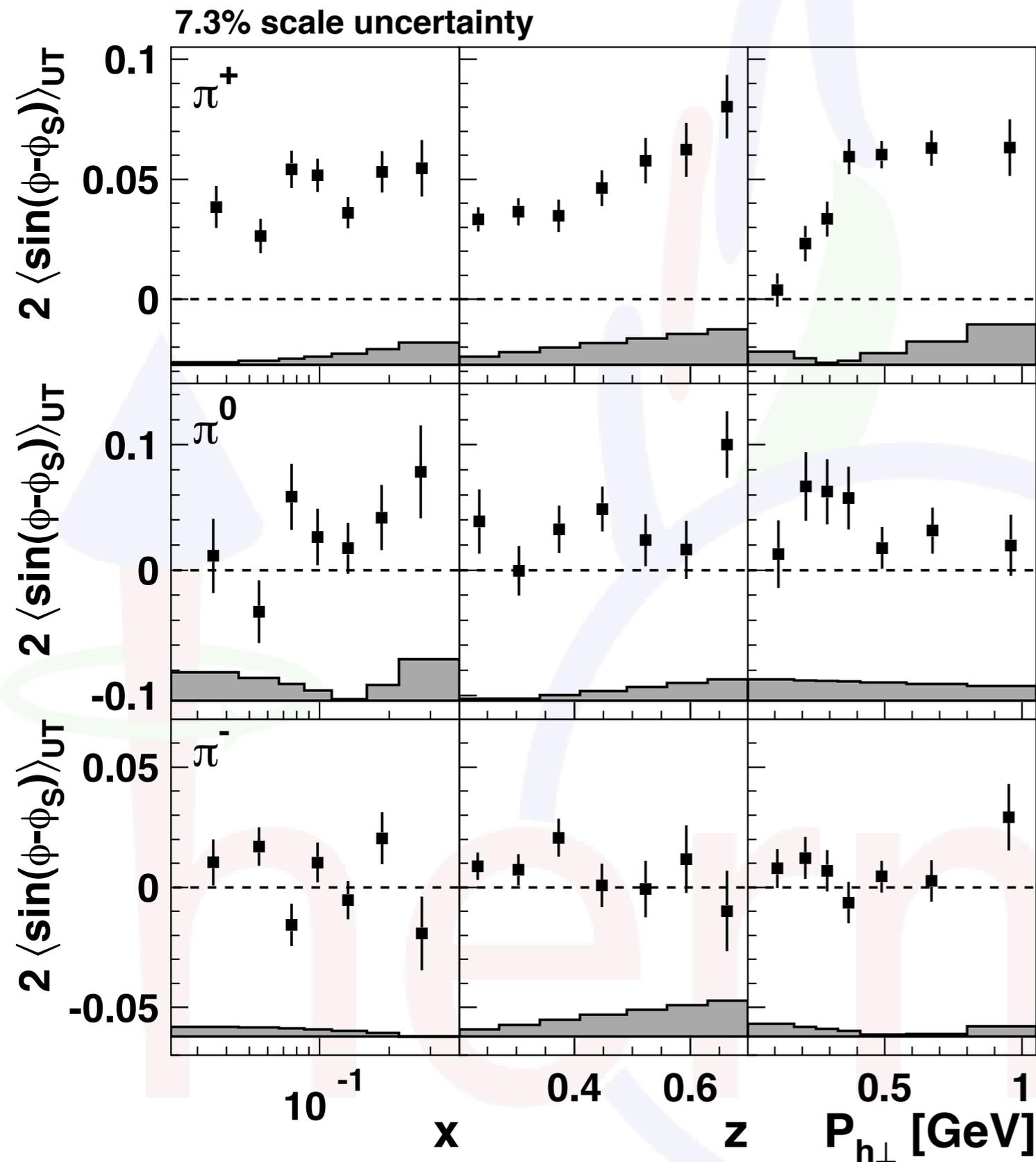


# Sivers amplitudes for pions

[A. Airapetian et al., arXiv:0906.3918]



# Sivers amplitudes for pions



[A. Airapetian et al., arXiv:0906.3918]

clear observation of T-odd Sivers effect in SIDIS!

u-quark dominance suggests sizeable u-quark orbital motion

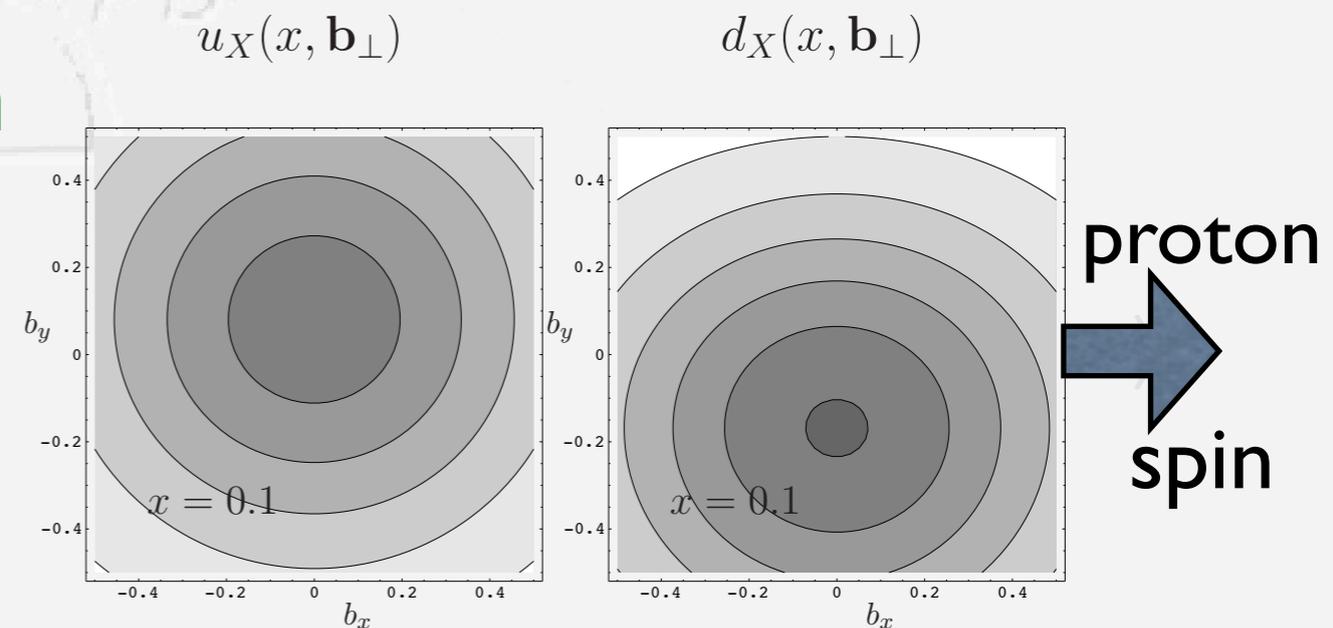
# "Chromodynamic Lensing"

approach by M. Burkardt:

spatial distortion of  $q$ -distribution

(obtained using anom. magn. moments  
& impact parameter dependent PDFs)

[hep-ph/0309269]



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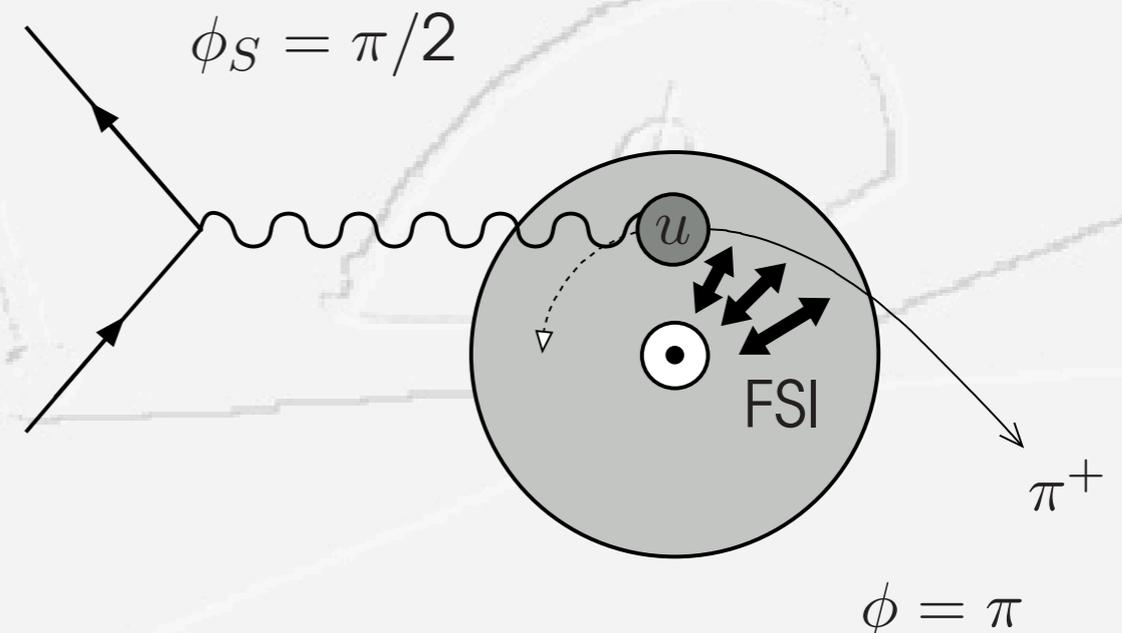
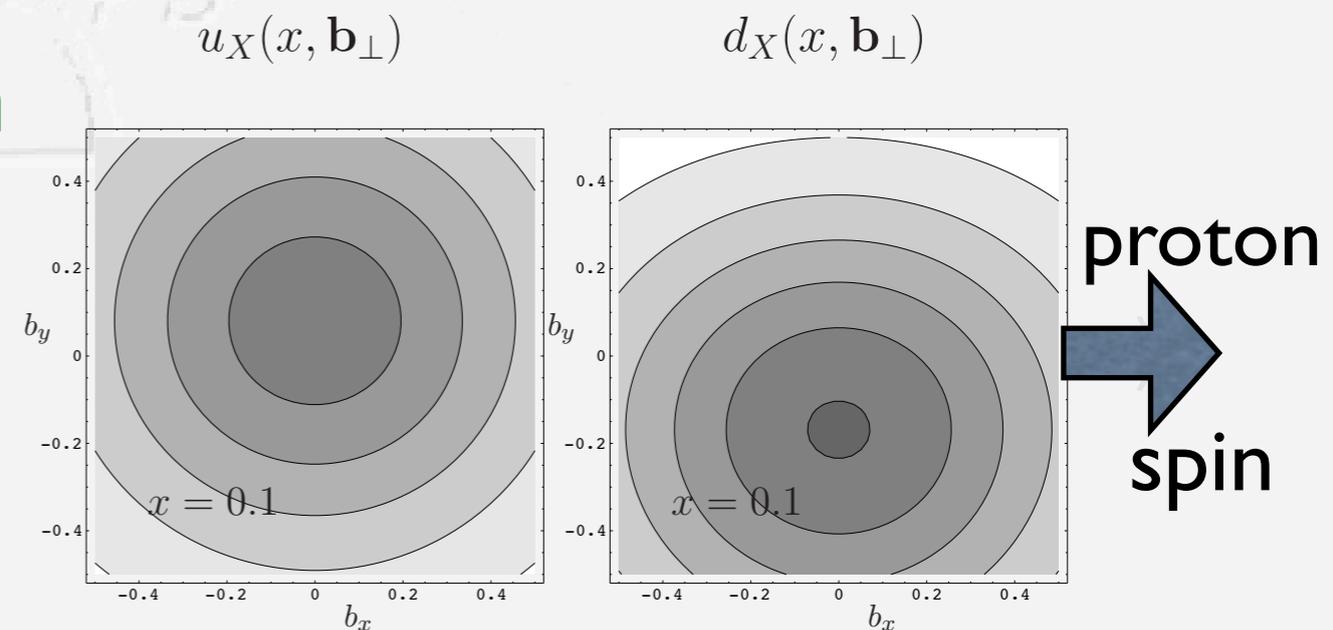
spatial distortion of q-distribution

(obtained using anom. magn. moments  
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+ attractive QCD potential

(gluon exchange)

⇒ transverse asymmetries



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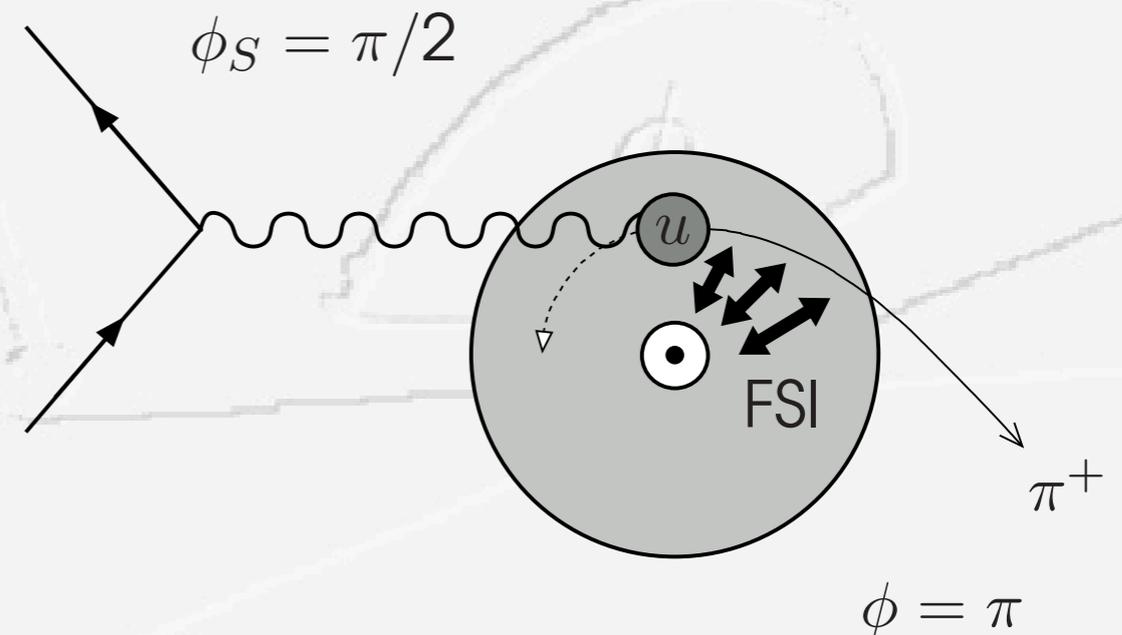
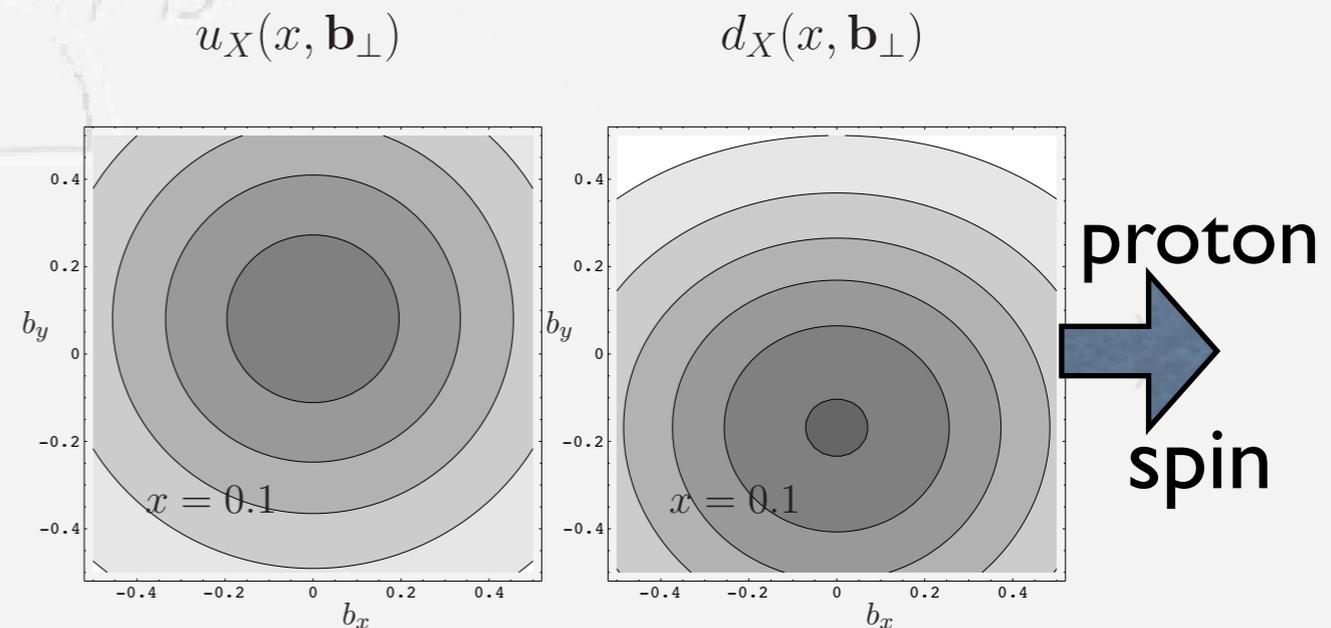
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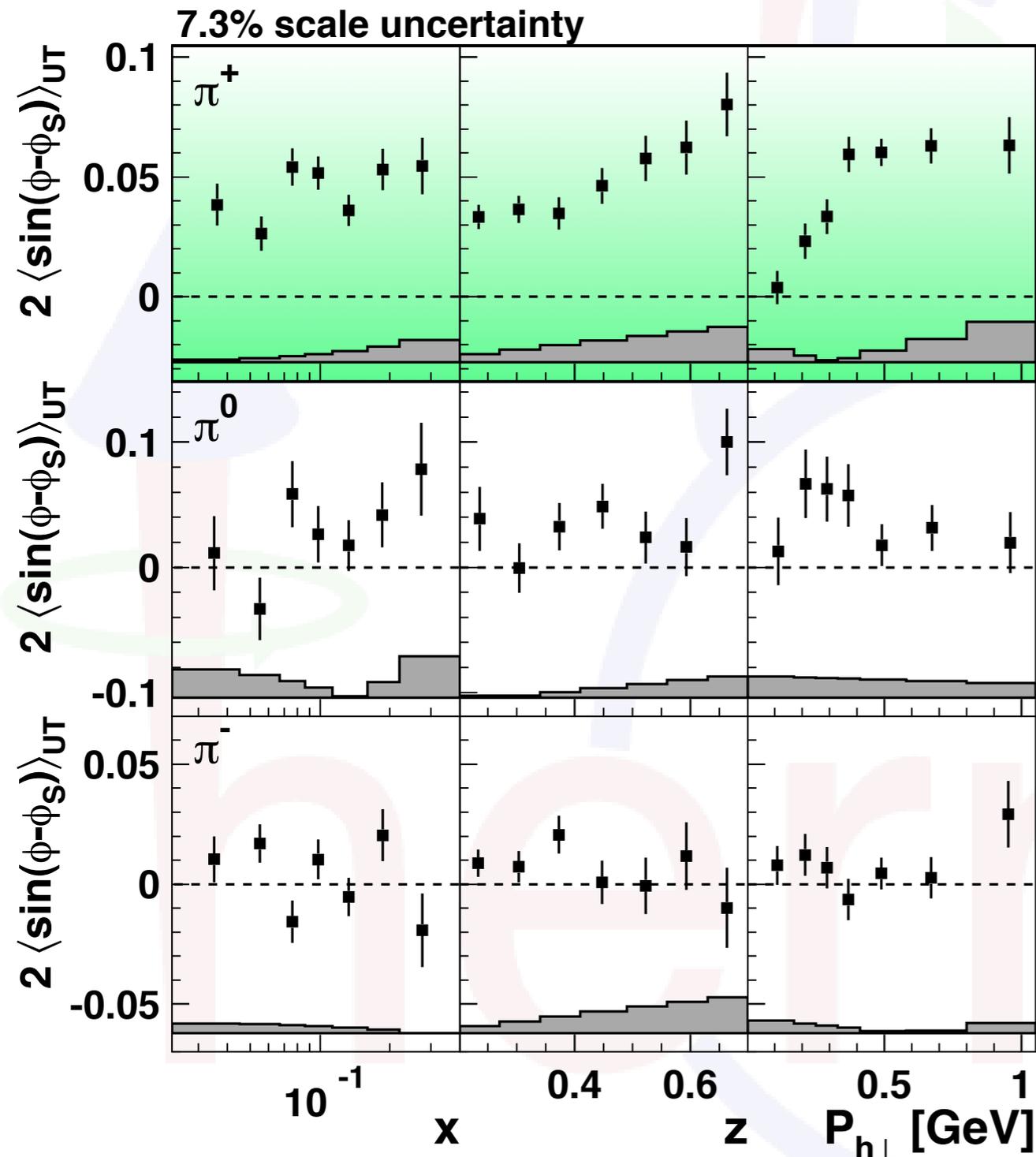
⇒ transverse asymmetries

$$L_z^u > 0$$



# Sivers amplitudes for pions

$$2\langle \sin(\phi - \phi_S) \rangle_{\text{UT}} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes D_1^q(z, K_T^2)}{\sum_q e_q^2 f_1^q(x) D_1^q(z)}$$

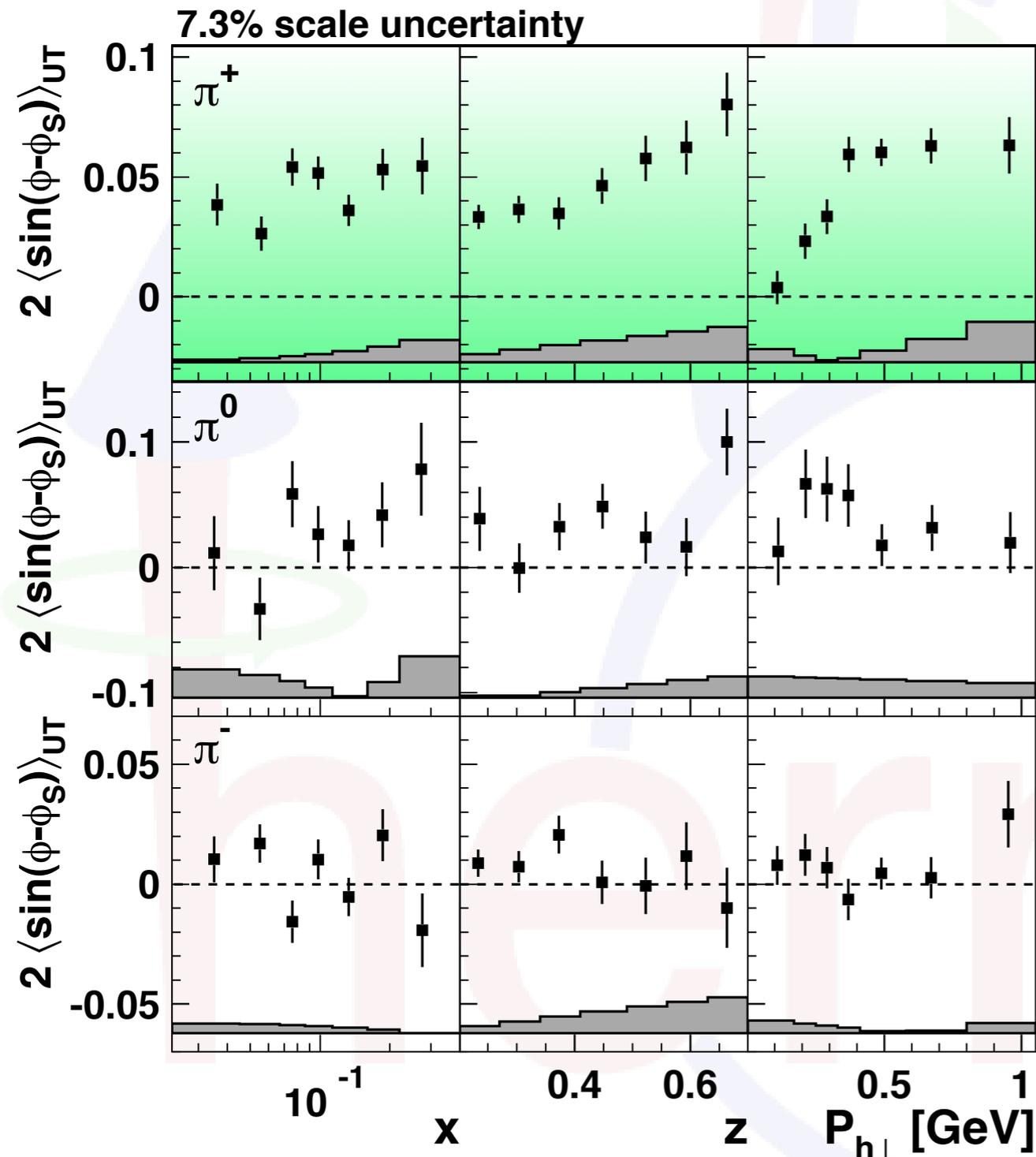


$$\approx - \frac{f_{1T}^{\perp,u}(x, p_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, K_T^2)}{f_1^u(x) D_1^{u \rightarrow \pi^+}(z)}$$

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$\pi^+$  dominated by u-quark scattering:

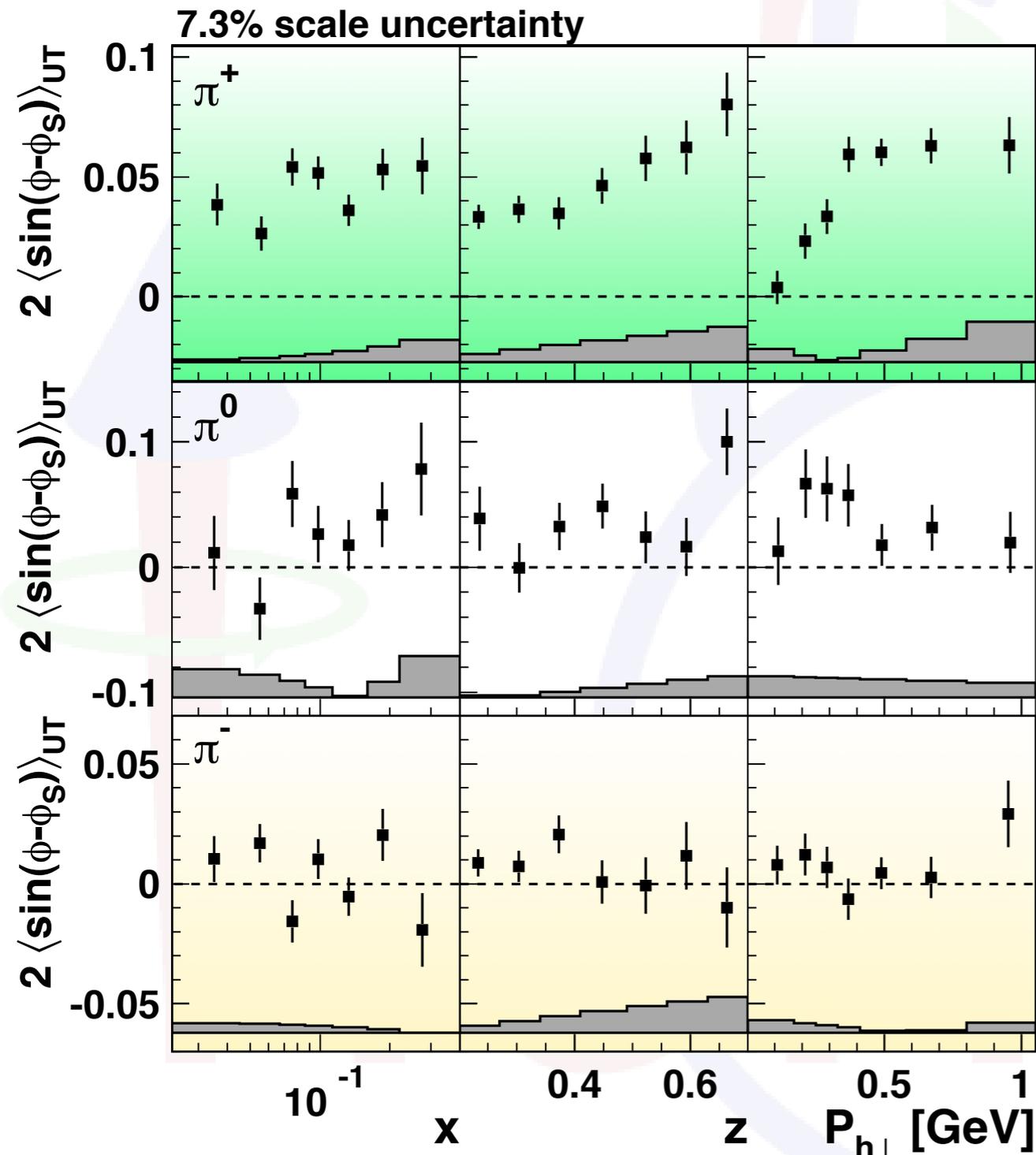
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👉 u-quark Sivers DF < 0

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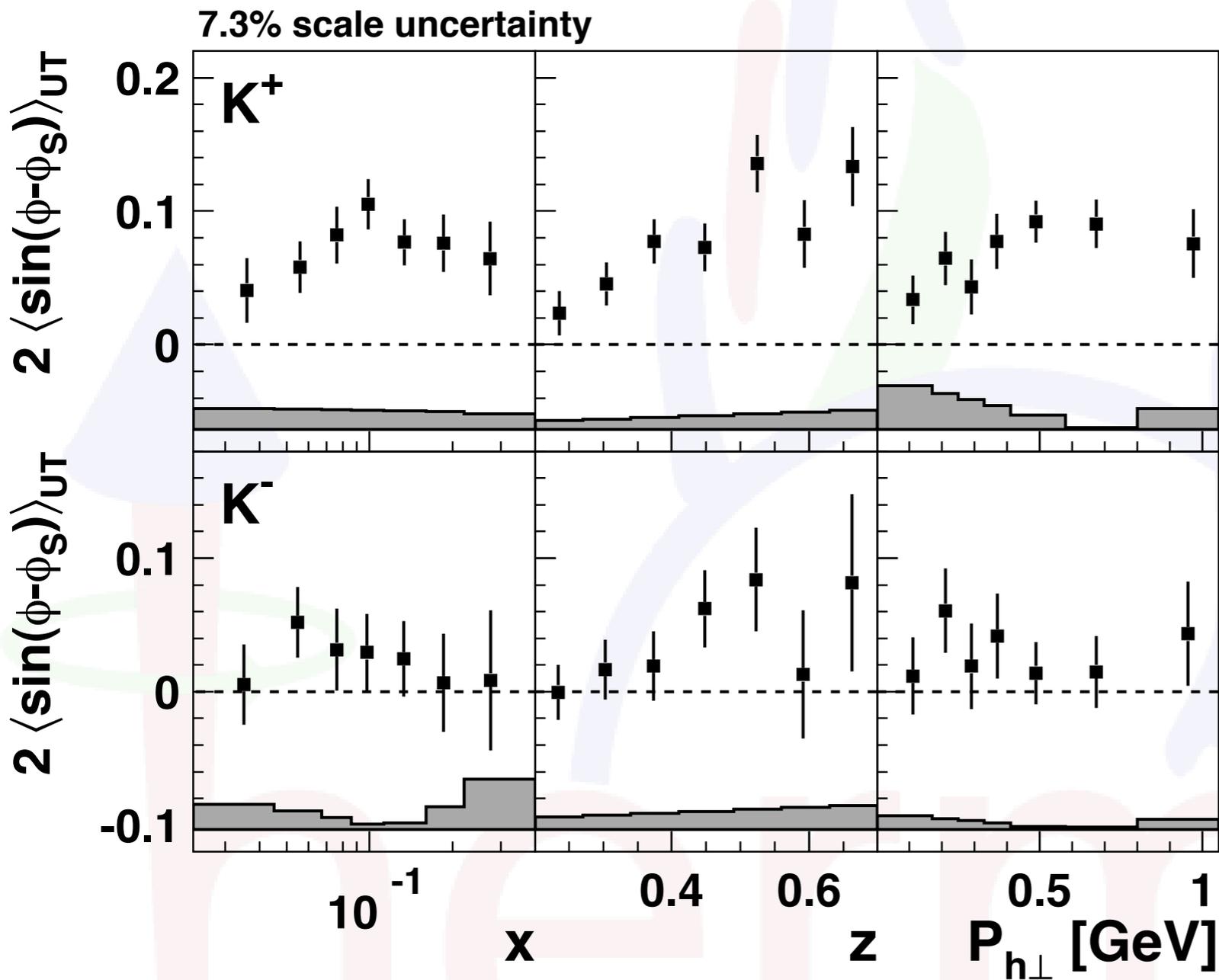
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👉 u-quark Sivers DF < 0

👉 d-quark Sivers DF > 0  
(cancelation for  $\pi^-$ )

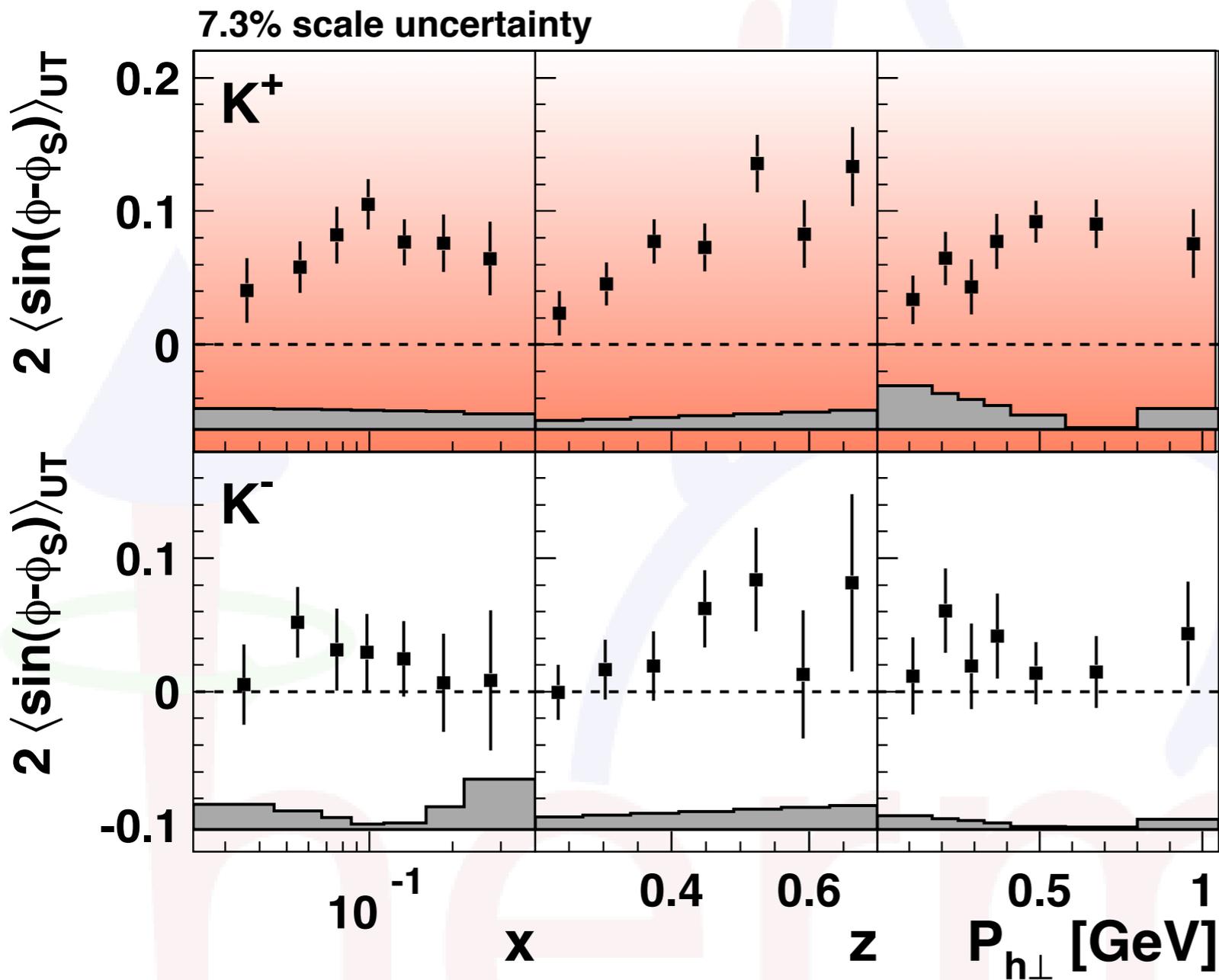
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# Sivers amplitudes for kaons



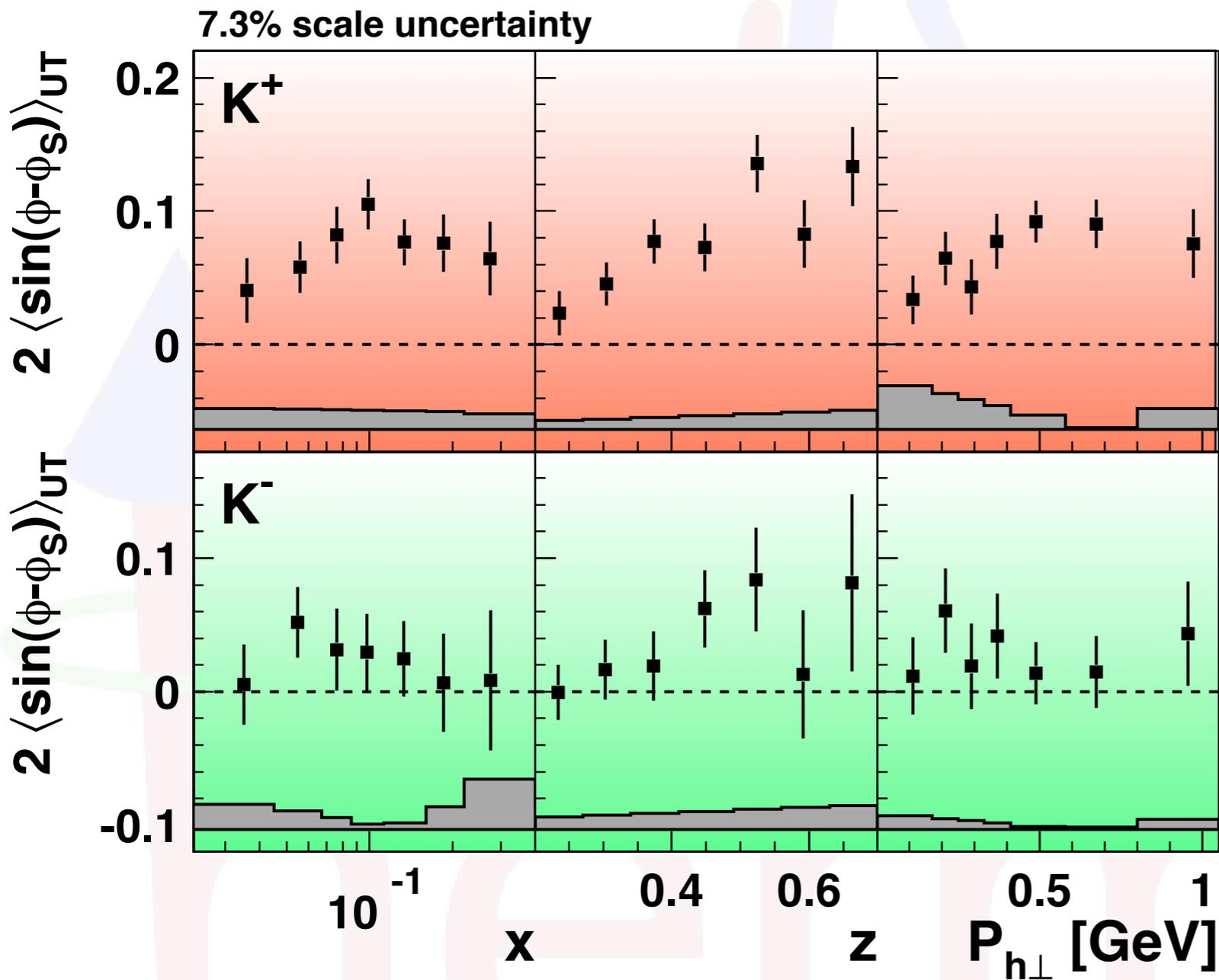
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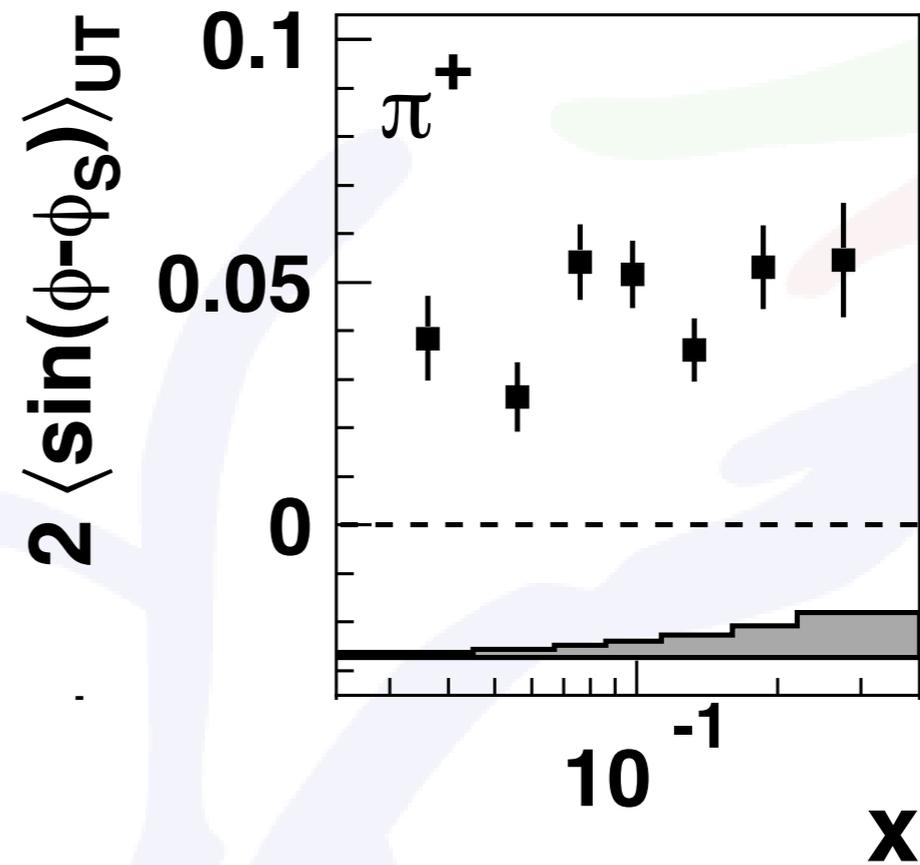
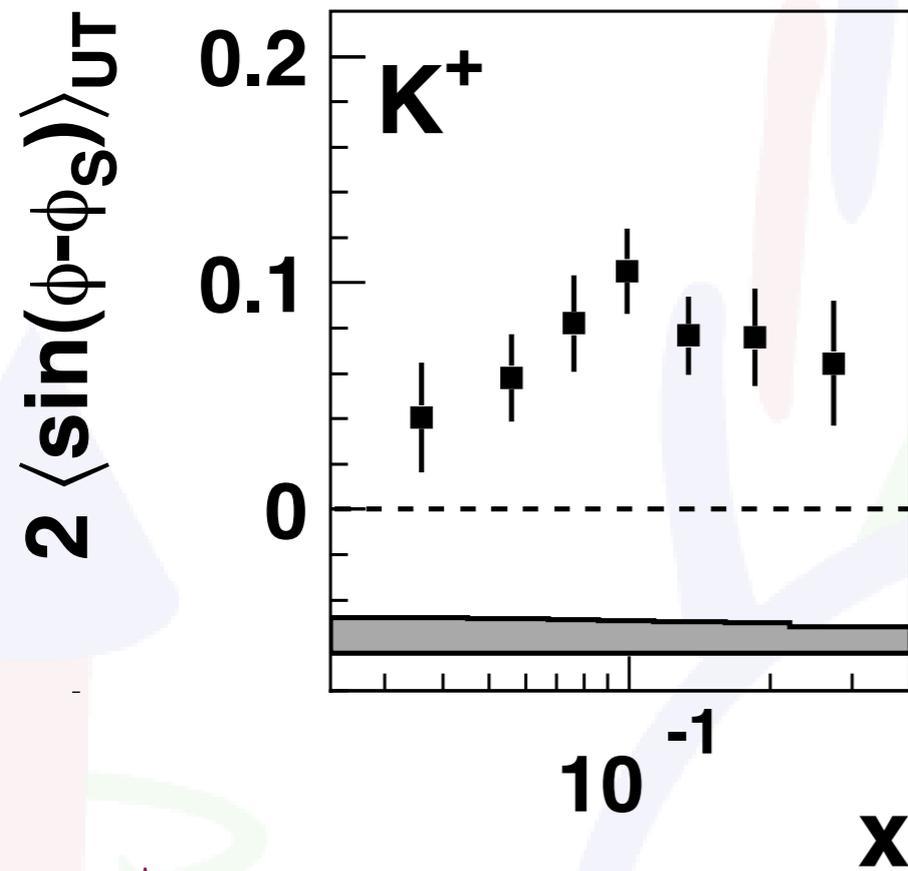


large & positive

slightly positive

[A. Airapetian et al., arXiv:0906.3918]

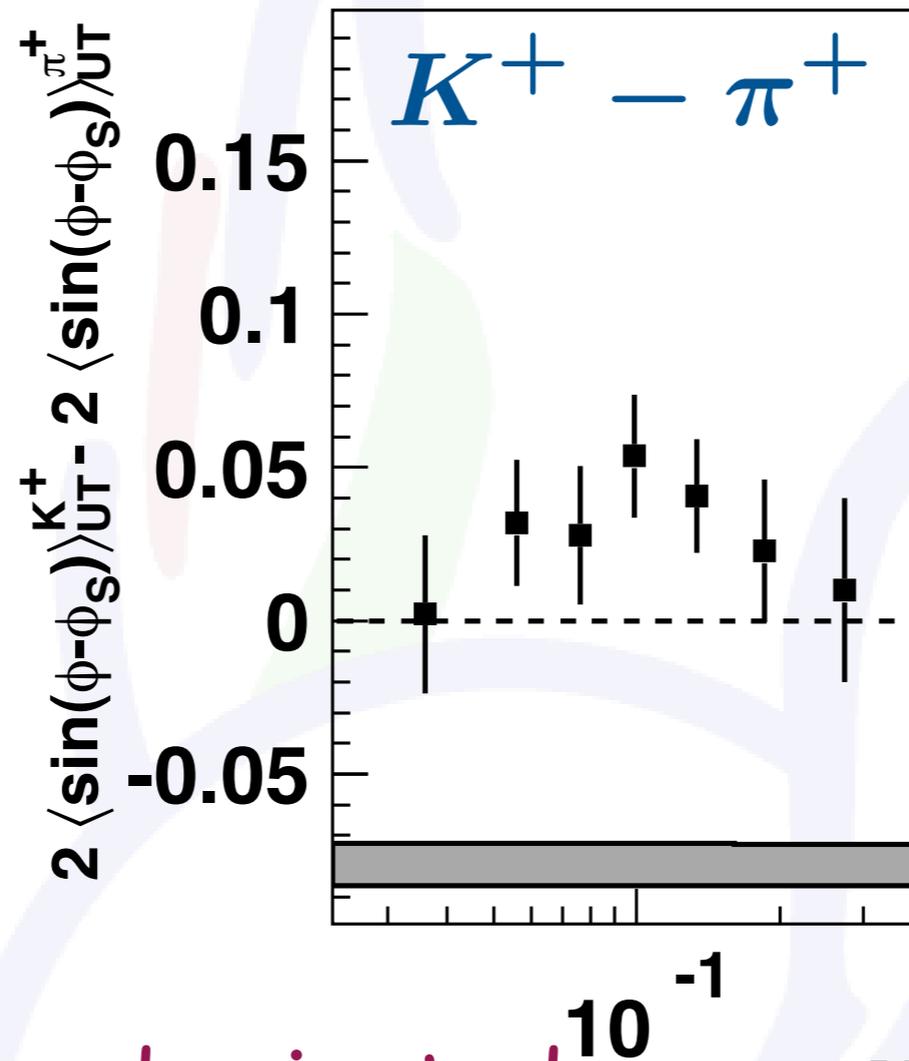
# The "Kaon Challenge"



$\pi^+ / K^+$  production dominated by scattering off u-quarks:  $\simeq$

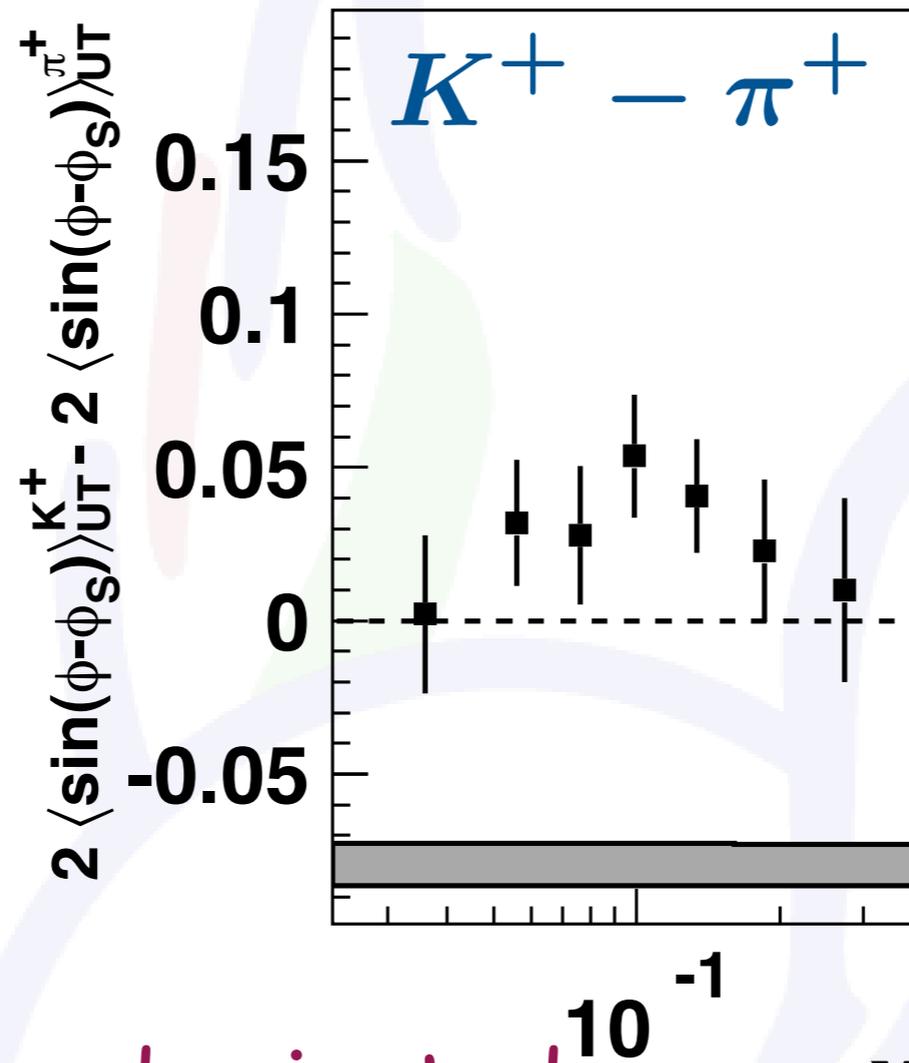
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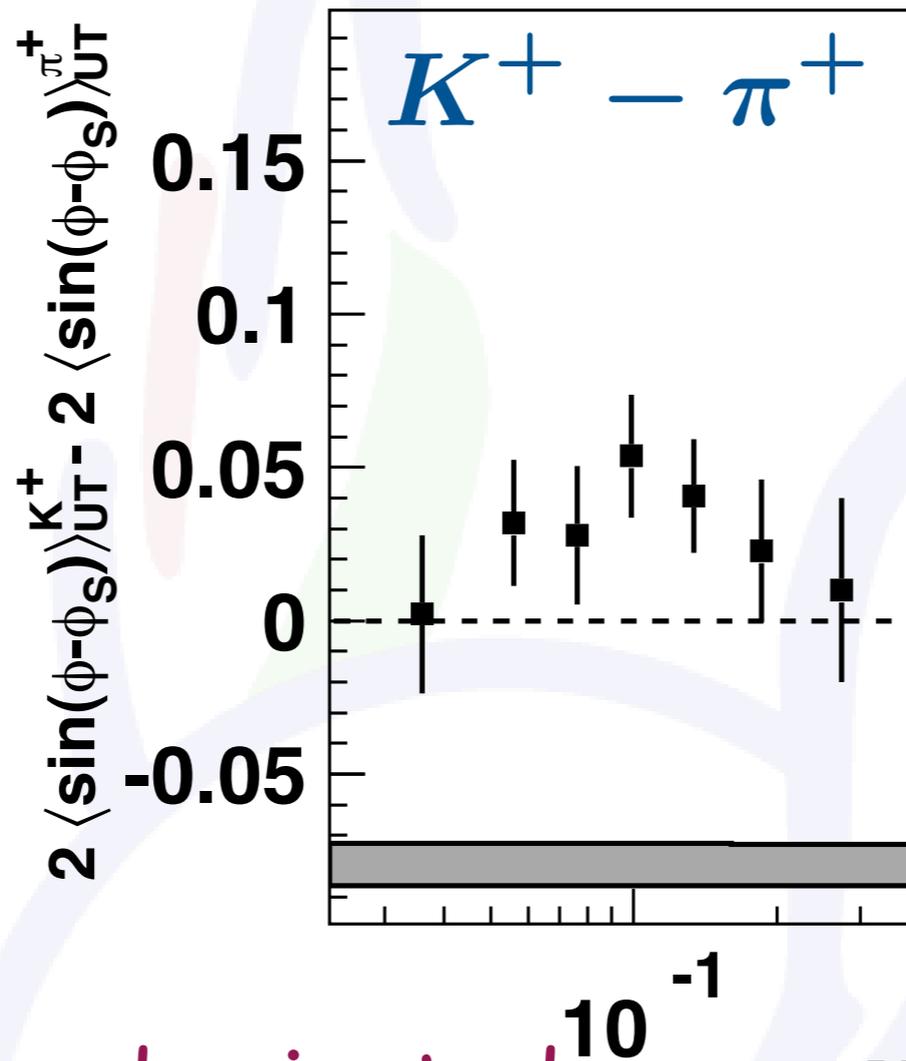
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□  $K^+ = |u\bar{s}\rangle$  &  $\pi^+ = |u\bar{d}\rangle$   $\rightarrow$  non-trivial role of sea quarks

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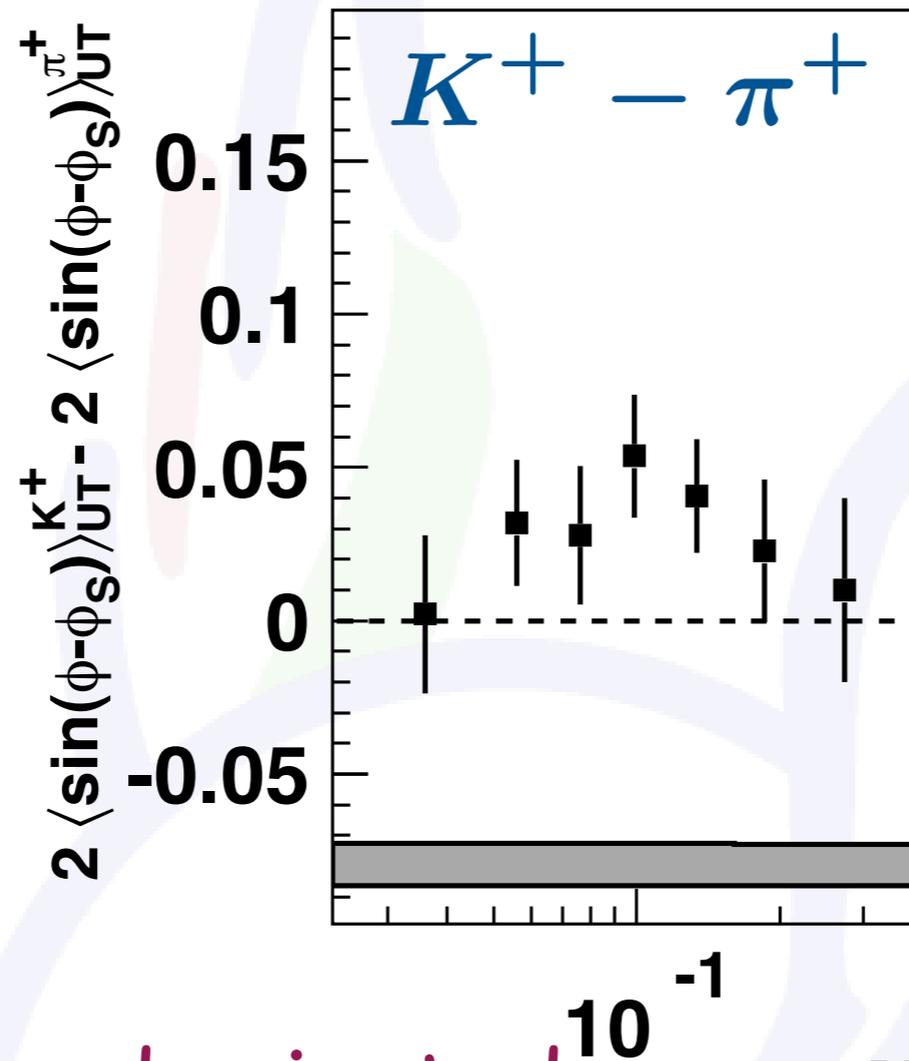


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- convolution integral in numerator depends on  $K_T$  dependence of FFs

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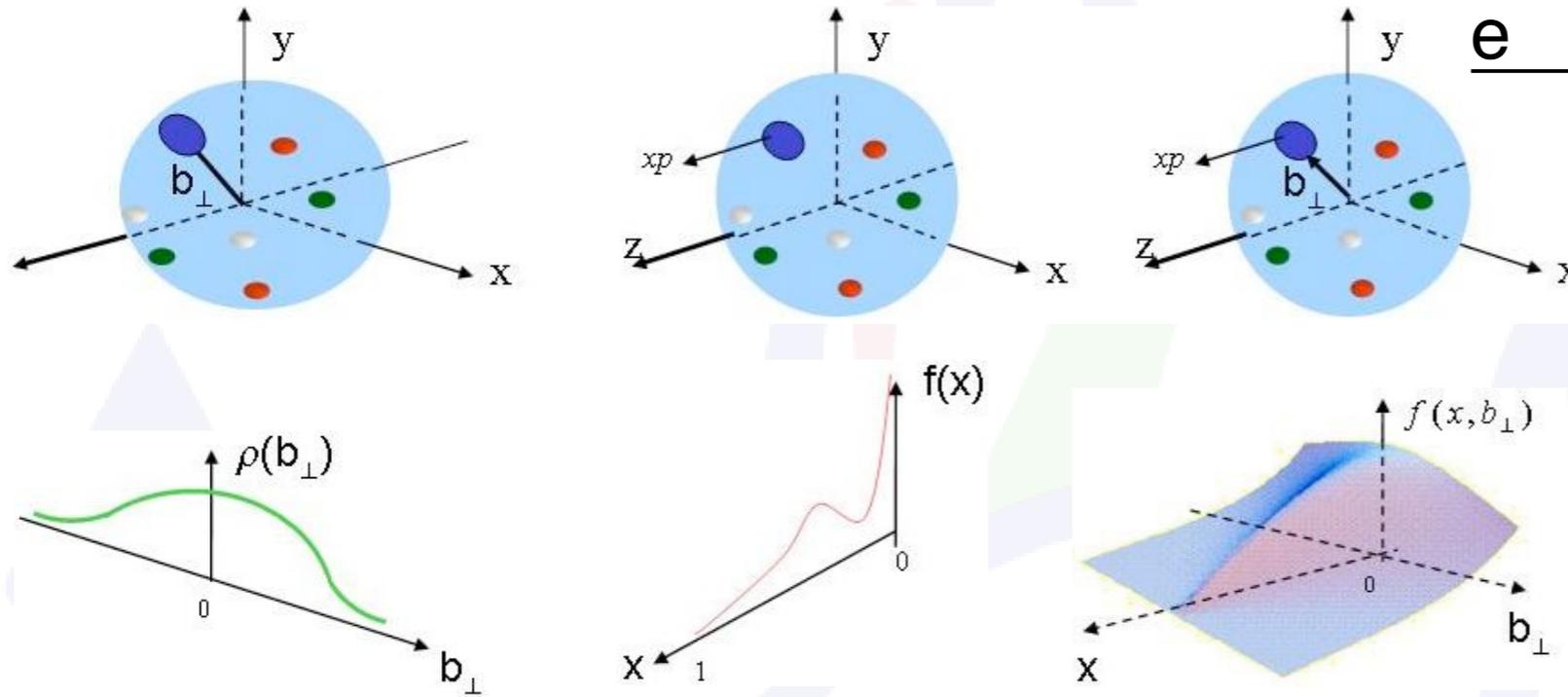
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- convolution integral in numerator depends on  $K_T$  dependence of FFs
- difference in dependences on kinematics integrated over

# Exclusive Reactions

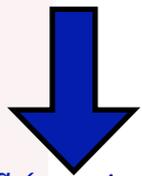
# Probing GPDs in Exclusive

## Generalized Parton Distributions



Form factors

Transverse distribution of quarks in space coordinates

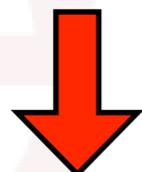


$$\int dx H^q(x, \xi, t) = F_1^q(t)$$

$$\int dx E^q(x, \xi, t) = F_2^q(t)$$

Parton Distribution Functions

Quark longitudinal momentum fraction distribution in the nucleon

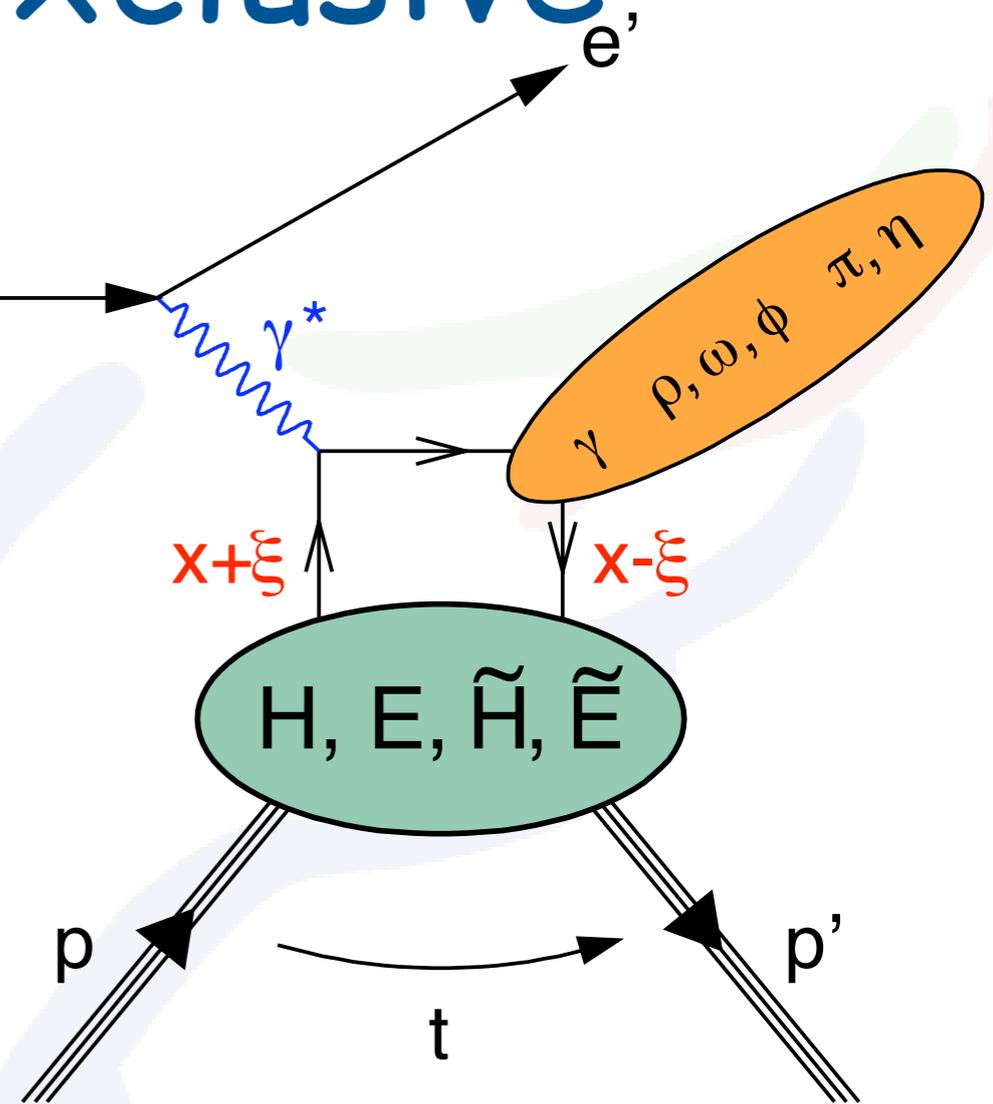


$$H^q(x, \xi = 0, t = 0) = q(x)$$

$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$$

GPDs

Correlation between transverse position and longitudinal momentum fraction of quark in the nucleon

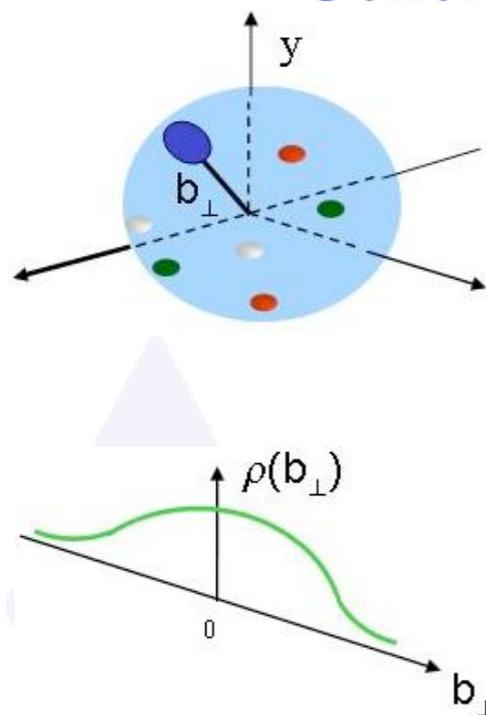


	unpolarized	polarized
no nucleon hel. flip	$H$	$\tilde{H}$
nucleon hel. flip	$E$	$\tilde{E}$

(+ 4 more chiral-odd functions)

# Probing GPDs in Exclusive

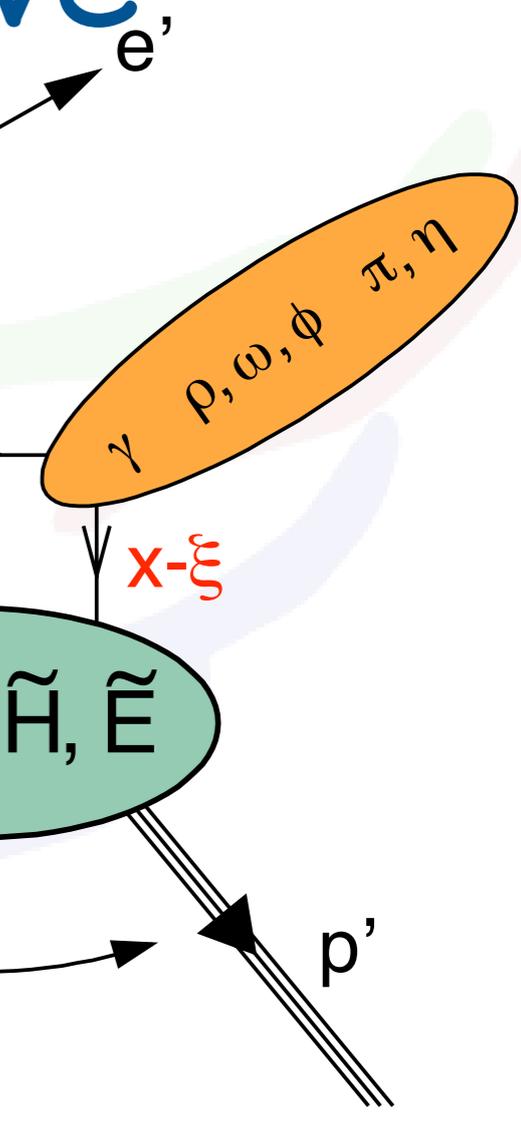
## Generalized Parton Distributions



**Ji relation (1996)**

$$J_q = \lim_{t \rightarrow 0} \int_{-1}^1 dx x (H_q(x, \xi, t) + E_q(x, \xi, t))$$

**→ Moments of certain GPDs relate directly to the total angular**



Form factors

Transverse distribution of quarks in space coordinates

Quark longitudinal momentum fraction distribution in the nucleon

Correlation between transverse position and longitudinal momentum fraction of quark in the nucleon

$$\int dx H^q(x, \xi, t) = F_1^q(t)$$

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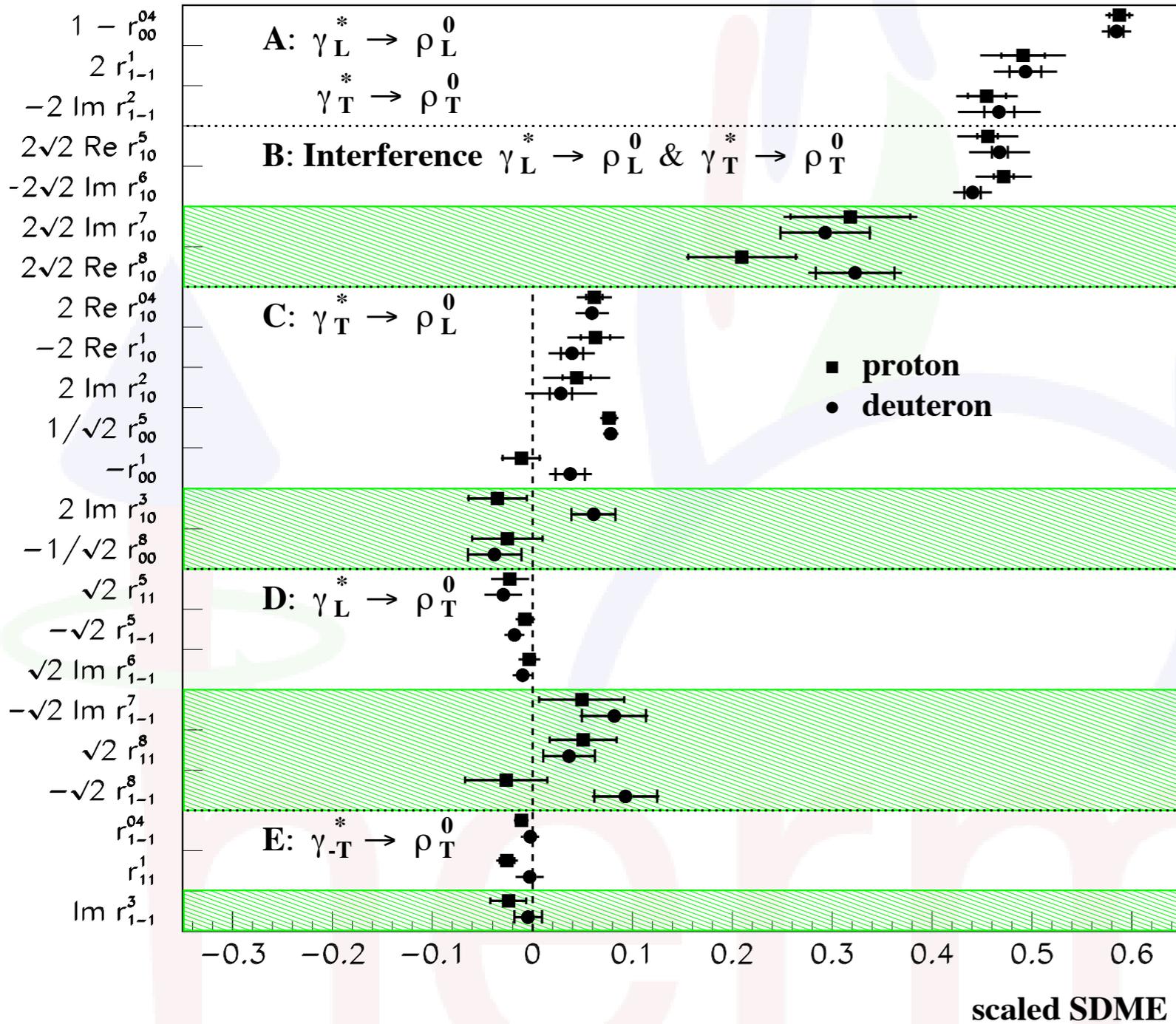
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	unpolarized	polarized
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# $\rho^0$ SDMEs from HERMES

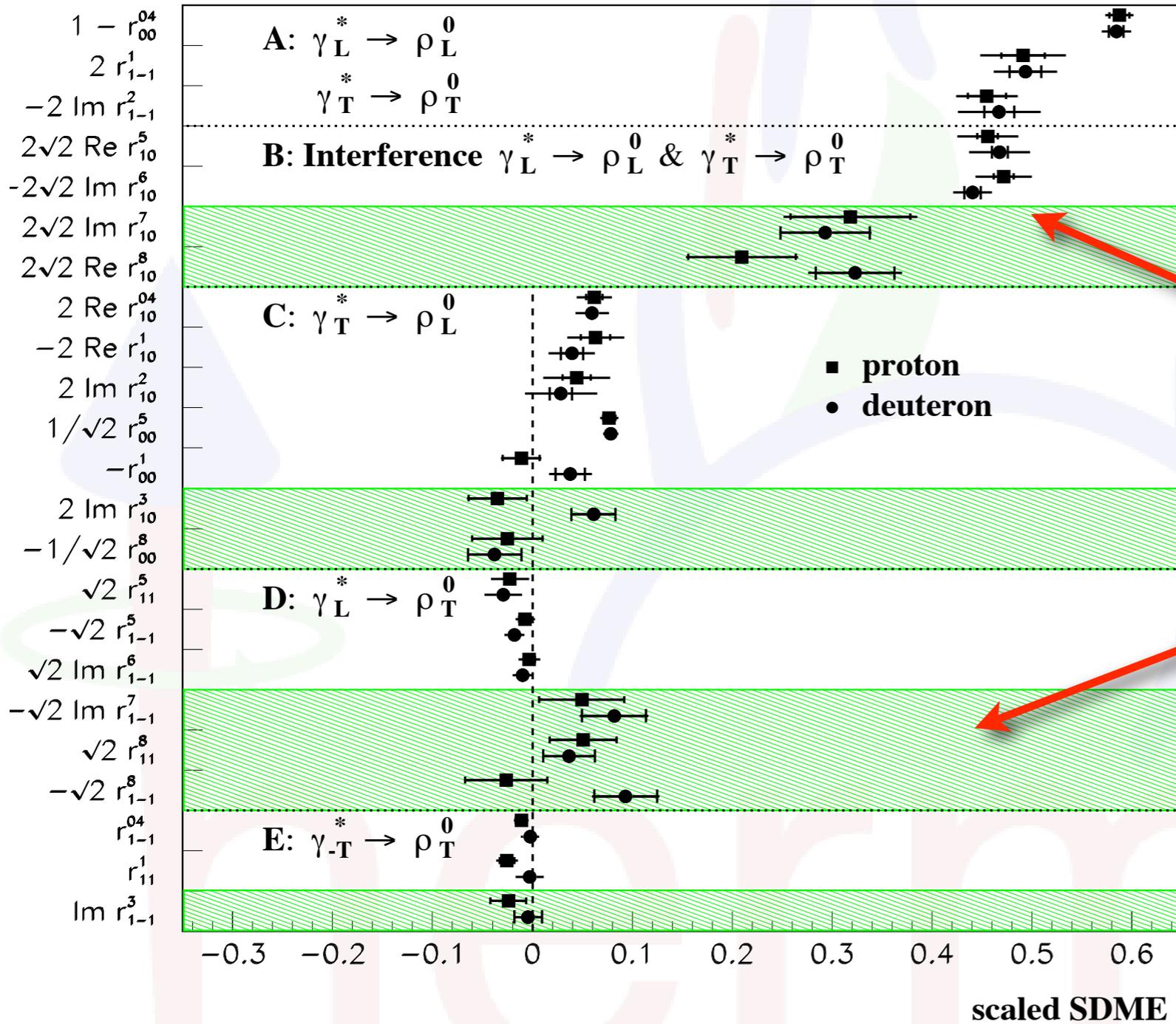
[A. Airapetian et al., arXiv:0901.0701]



target-polarization independent SDMEs

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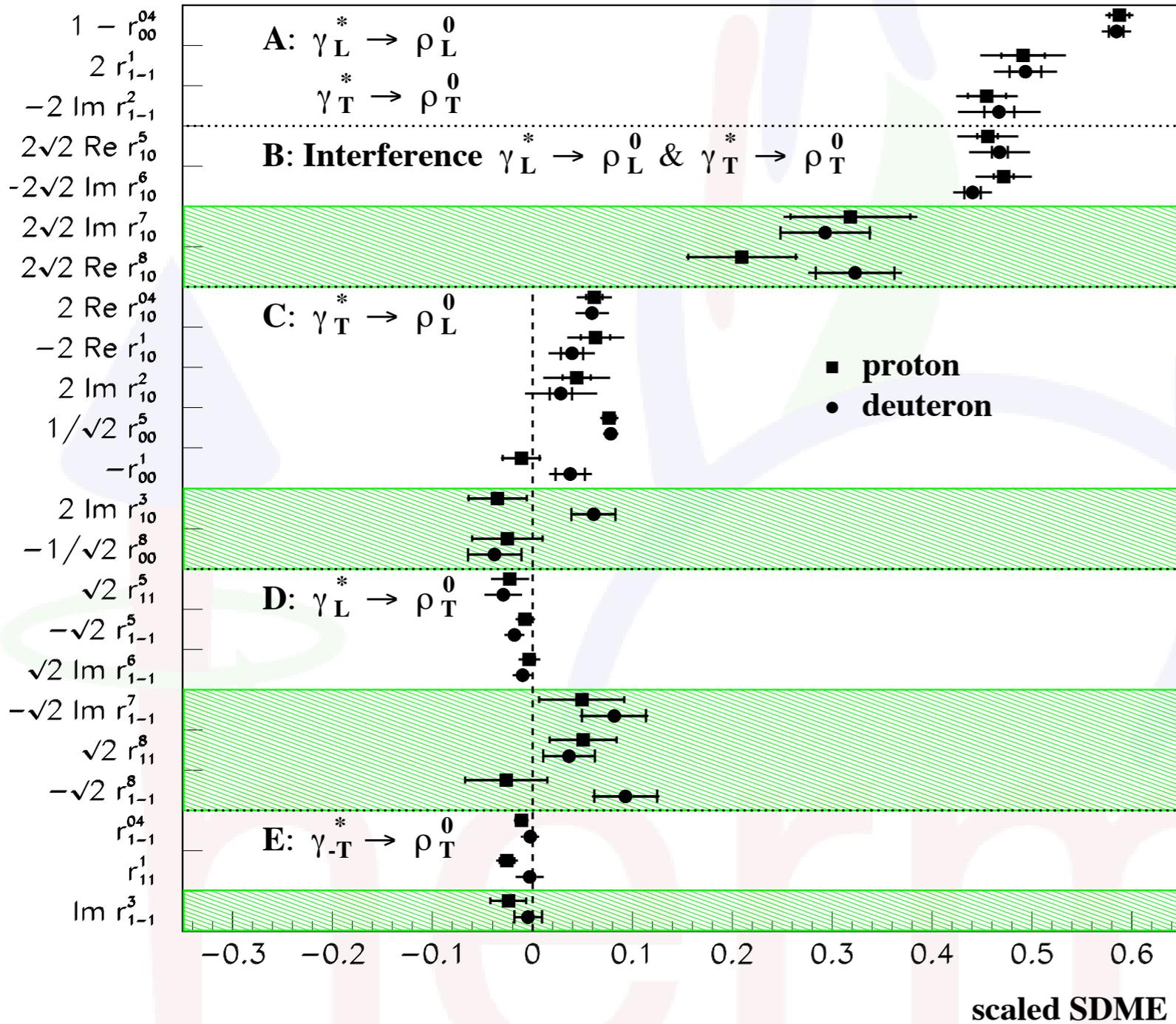
helicity non-flip much larger than helicity-flip and double helicity-flip

target-polarization independent SDMEs

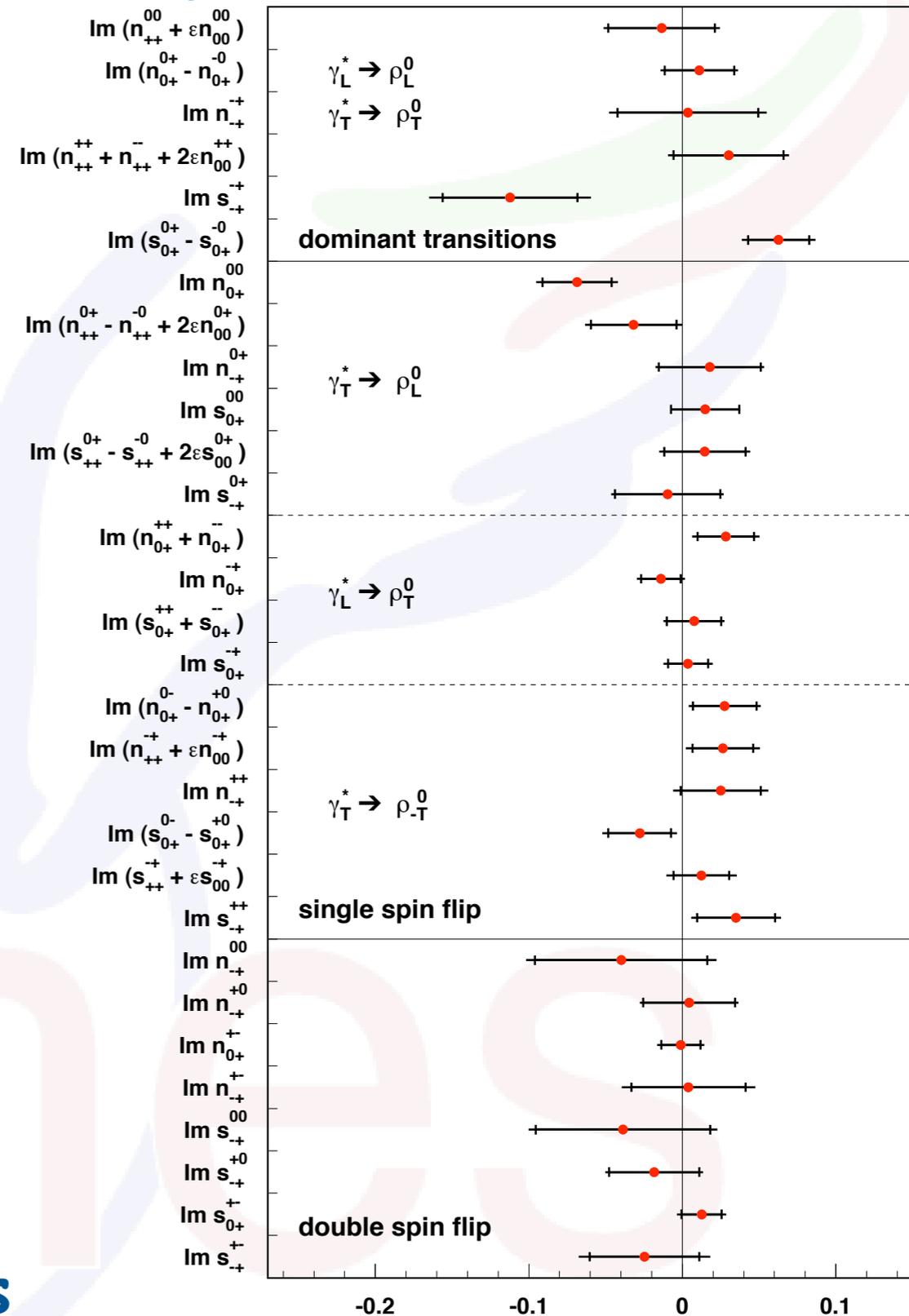
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[A. Airapetian et al., arXiv:0906.5160]

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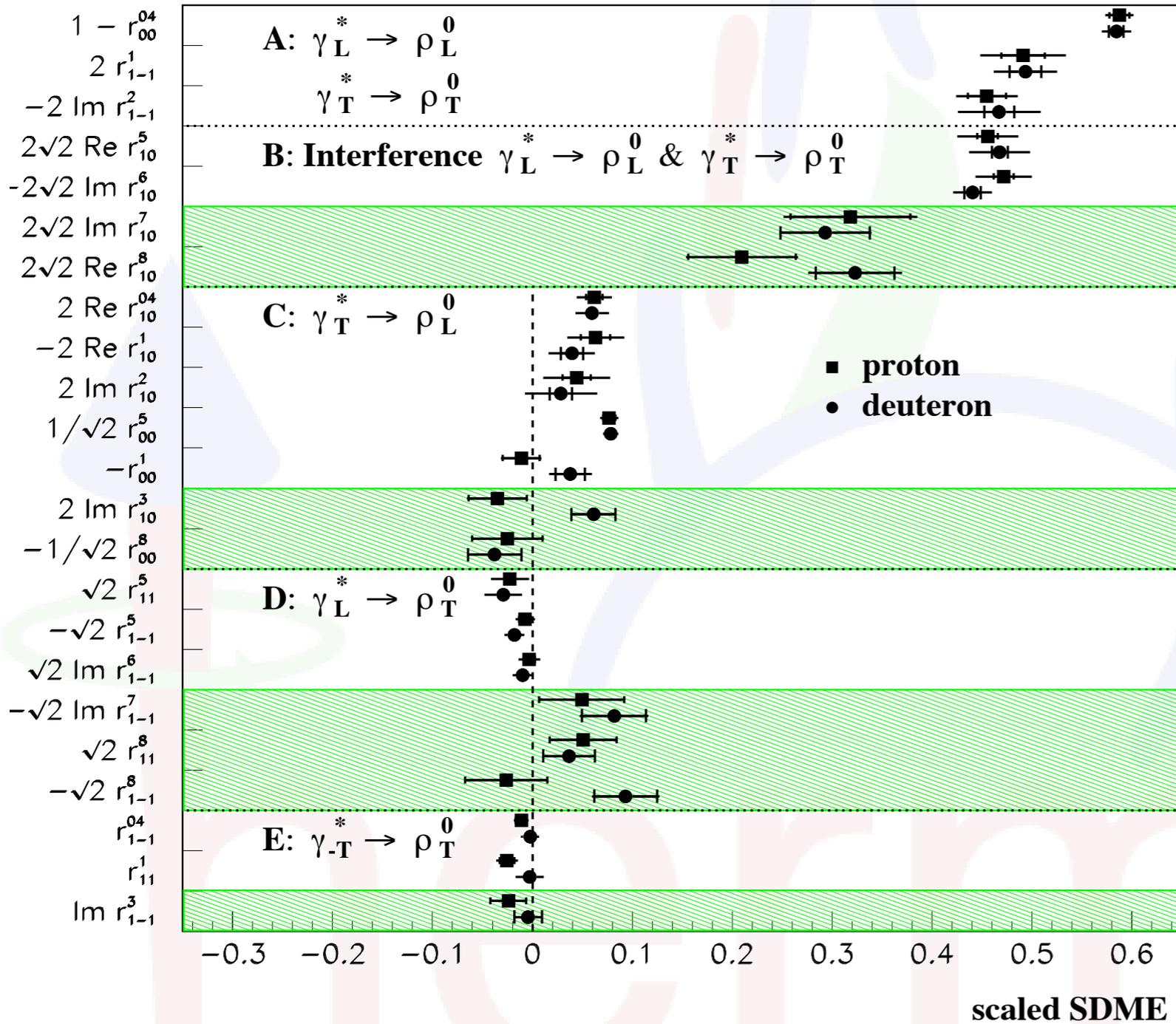


"transverse" SDMEs

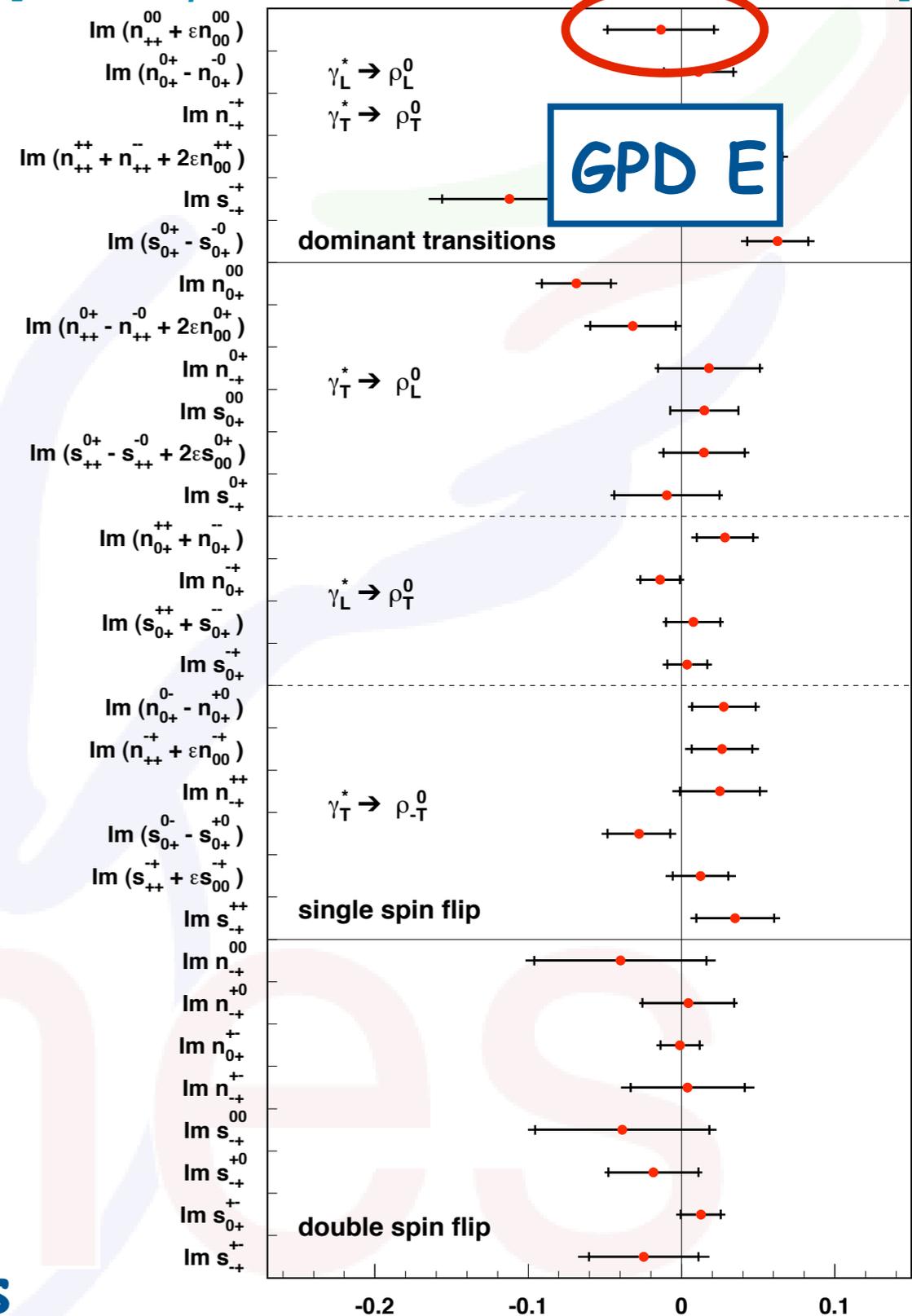
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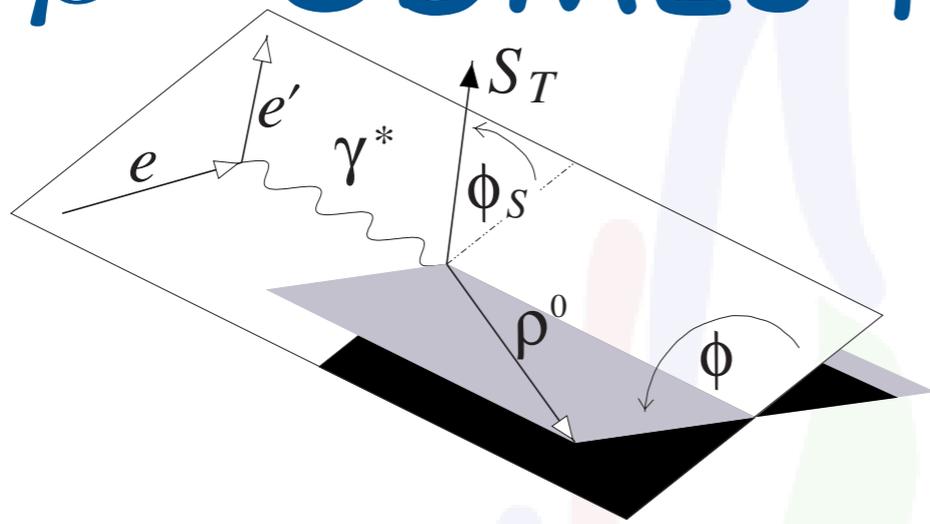


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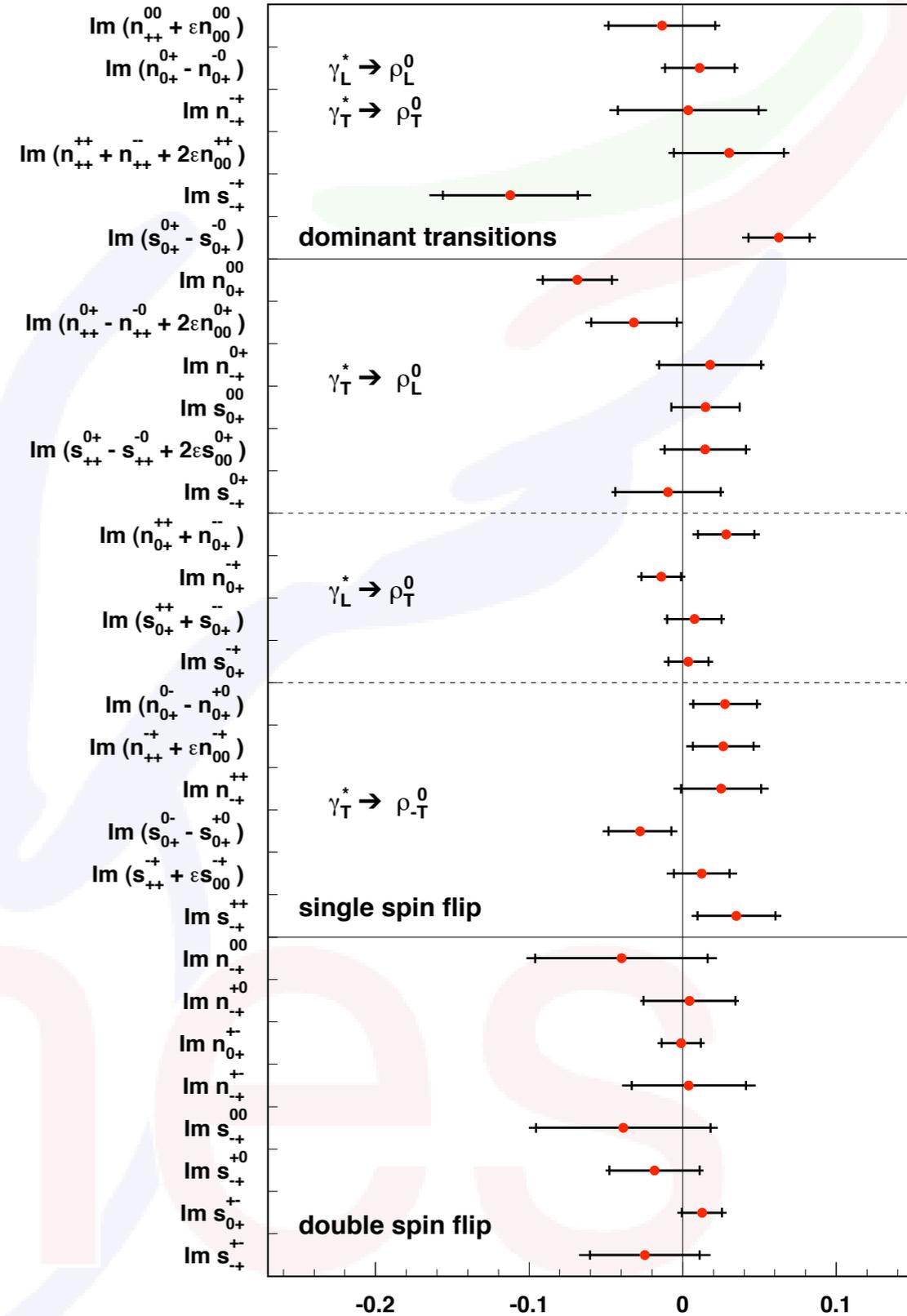
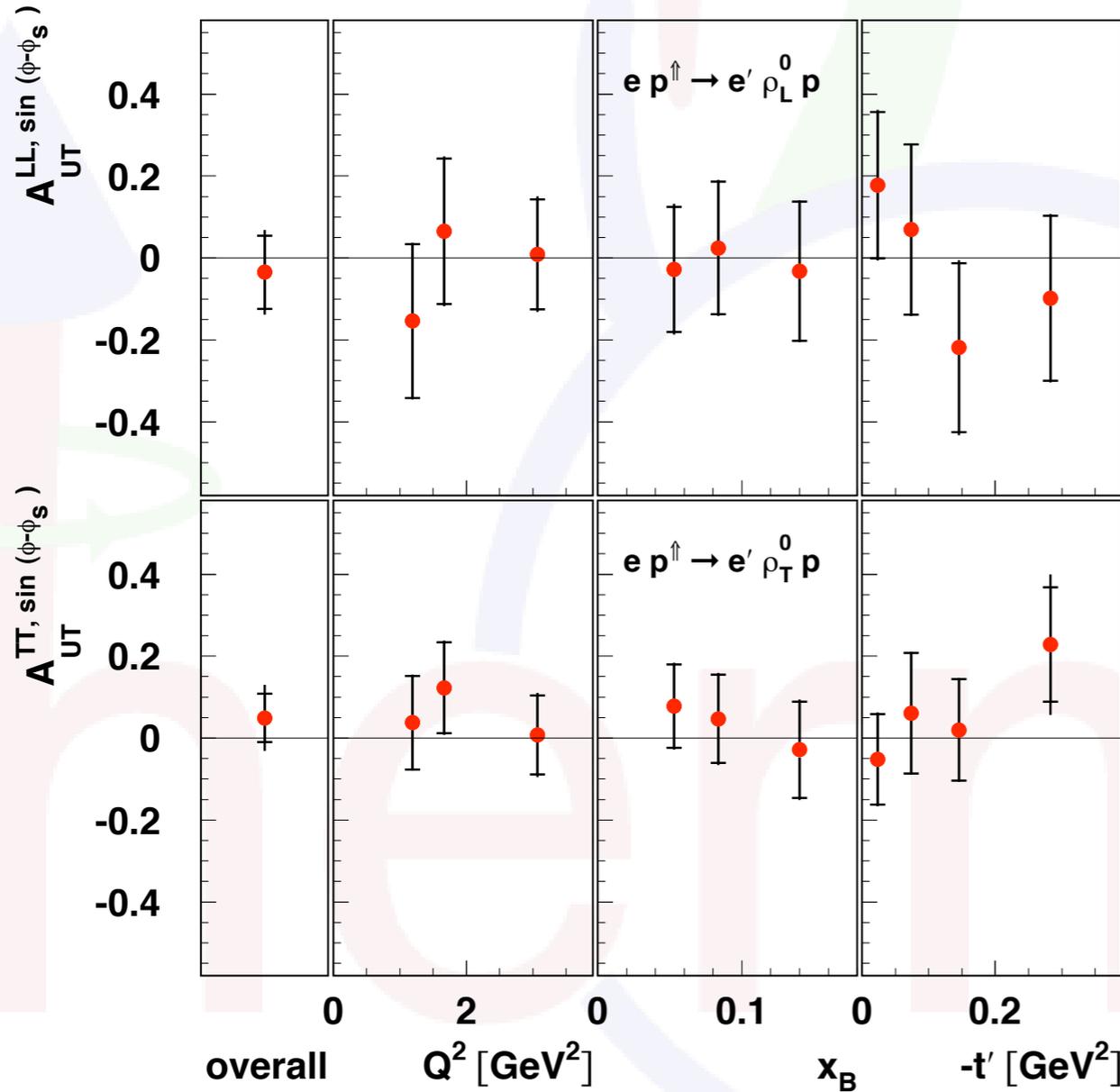
HEDT - 2<sup>nd</sup> anniversary - July 7<sup>th</sup>, 2009

# $\rho^0$ SDMEs from HERMES

[A. Airapetian et al., arXiv:0906.5160]



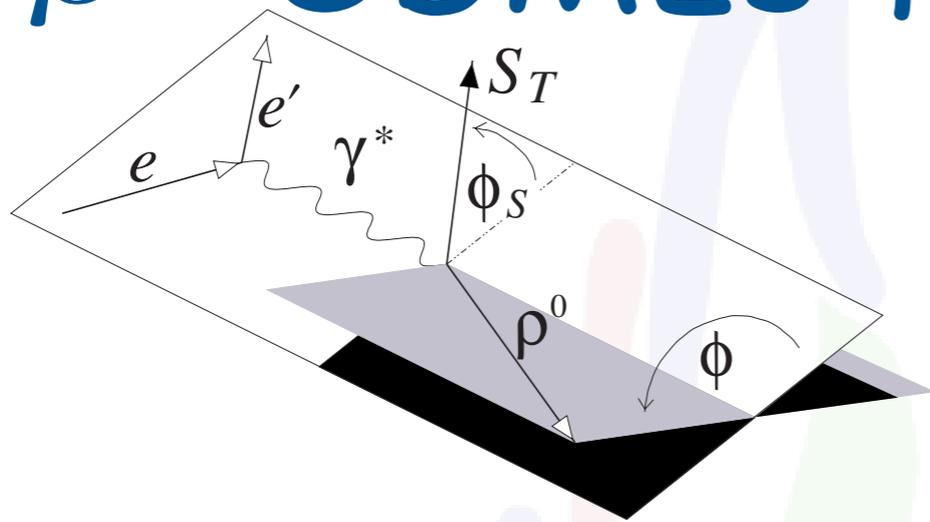
transverse  $\rho^0$  longitudinal  $\rho^0$



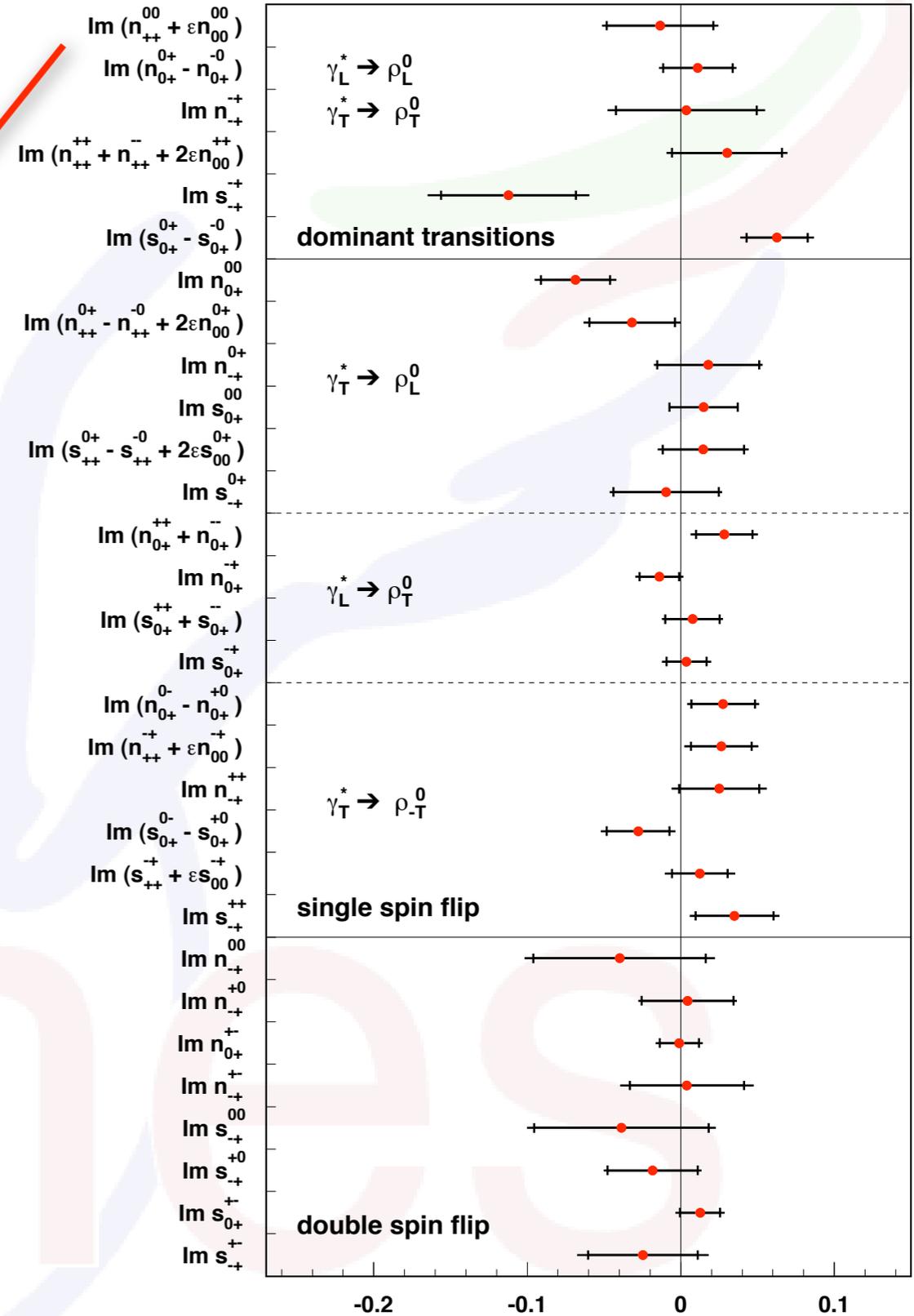
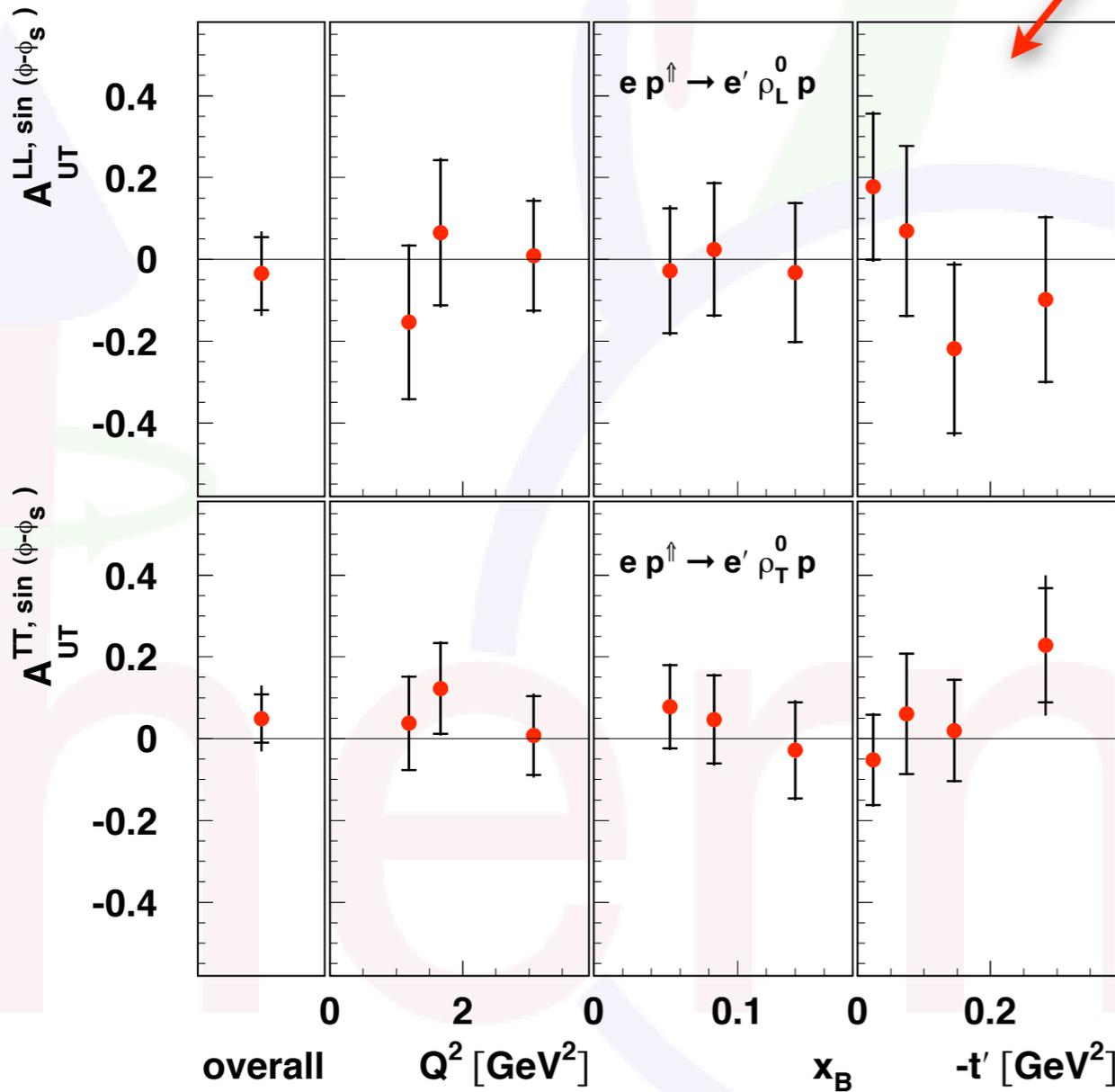
“transverse” SDMEs SDME values

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transverse  $\rho^0$  longitudinal  $\rho^0$

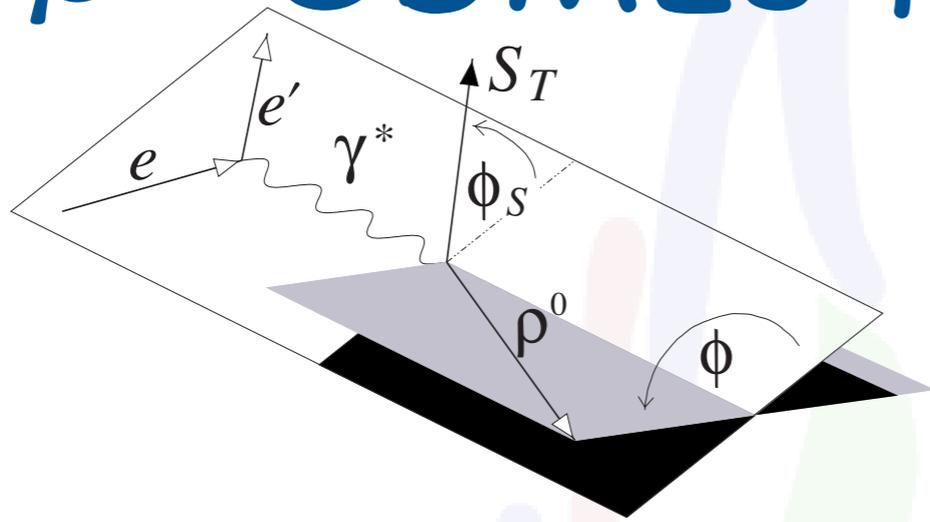


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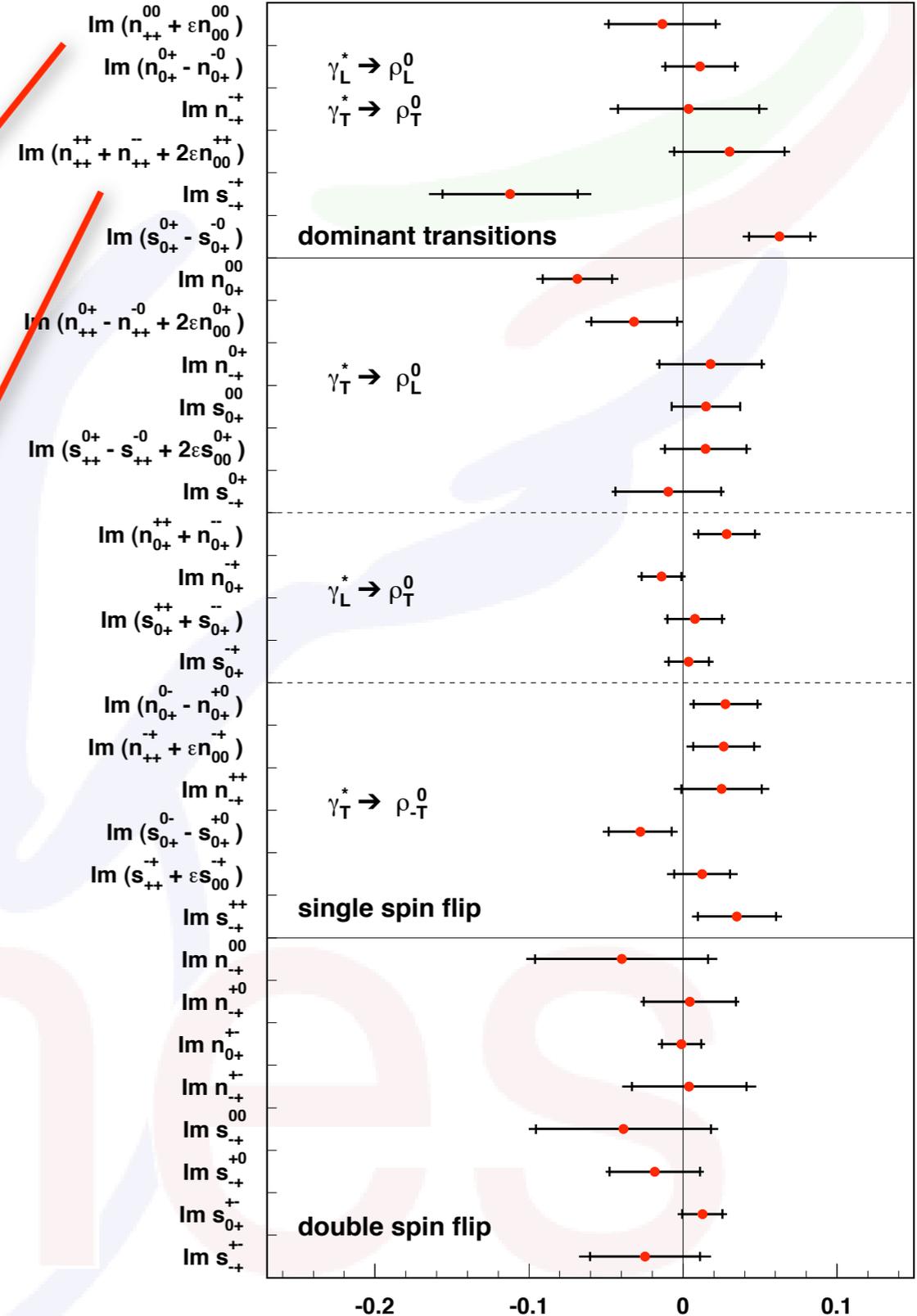
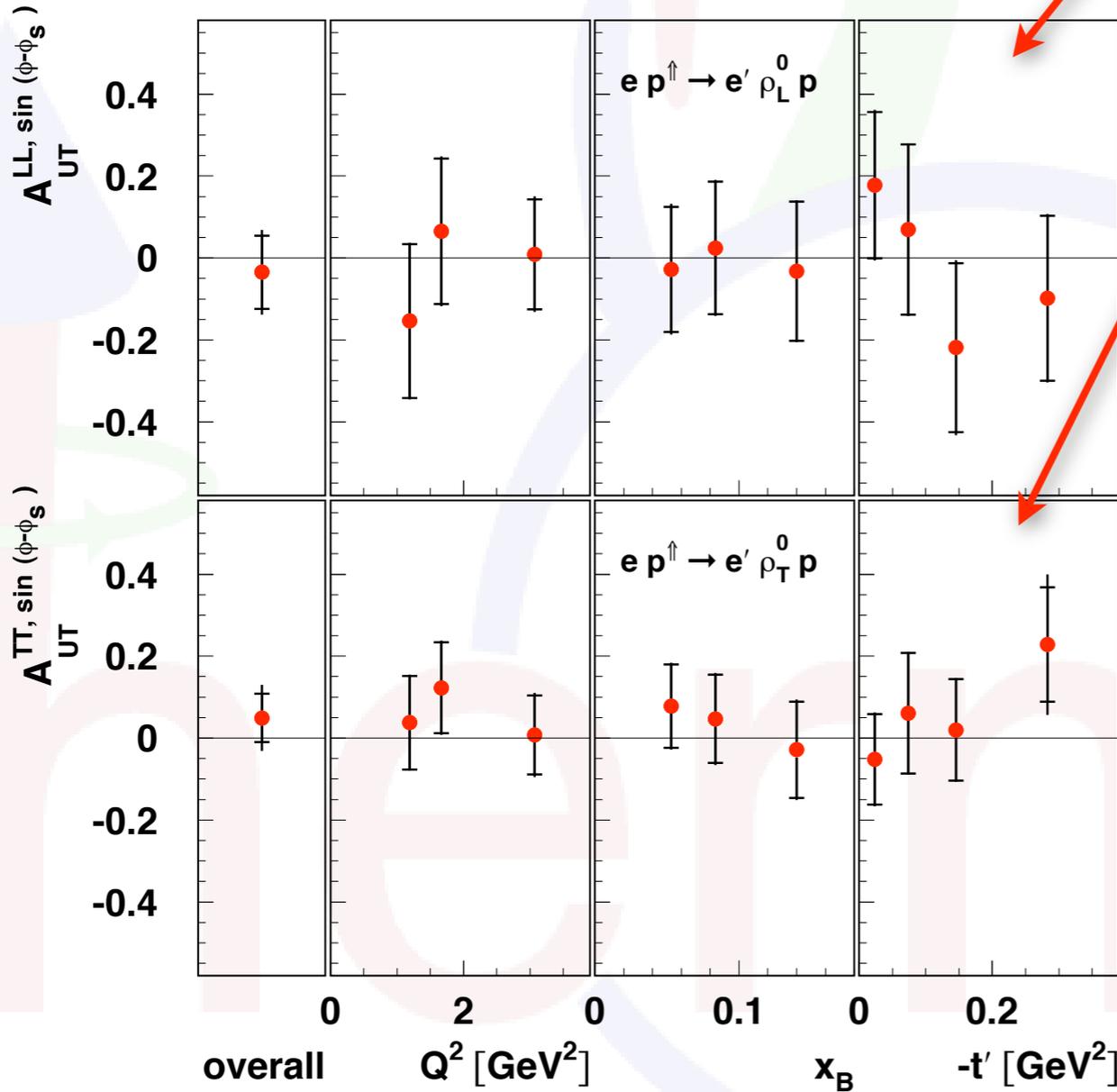
HERMES HEDT - 2<sup>nd</sup> anniversary - July 7<sup>th</sup>, 2009

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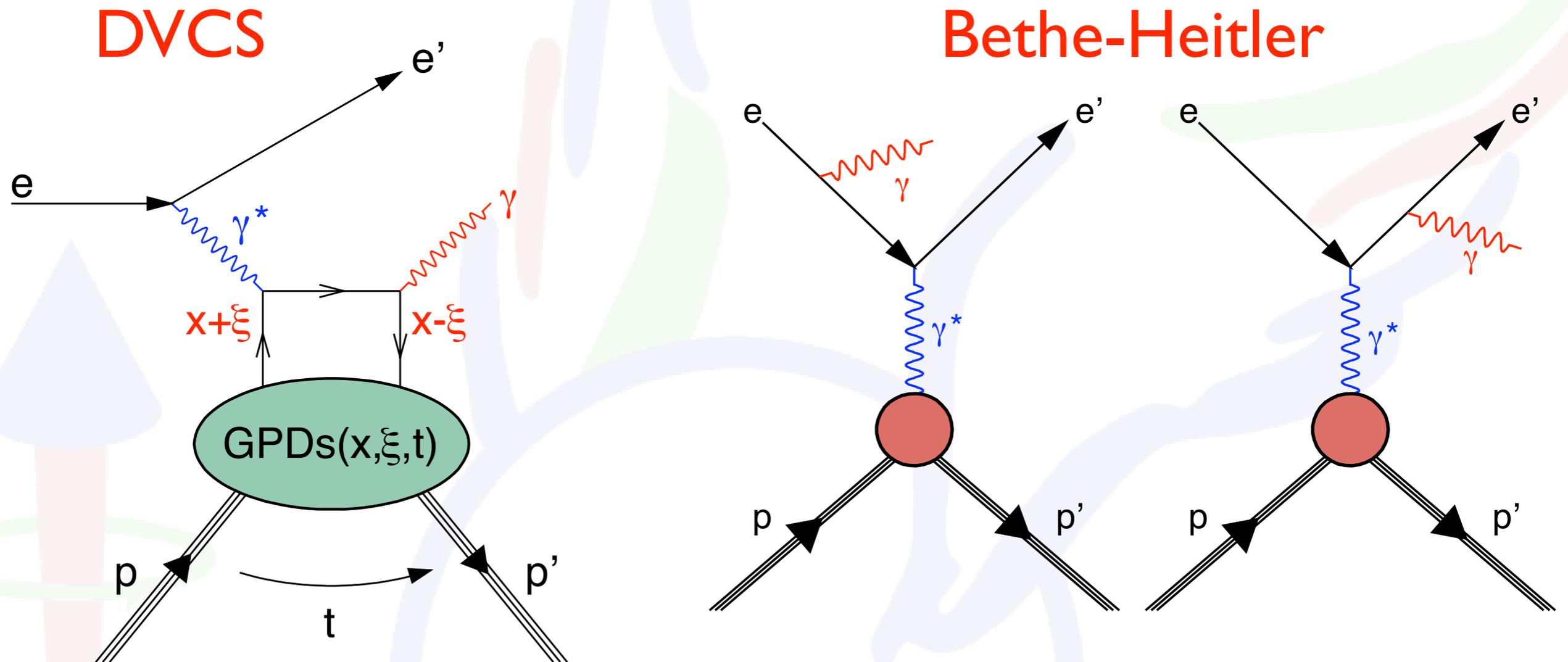


transverse  $\rho^0$  longitudinal  $\rho^0$



“transverse” SDMEs SDME values

# DVCS/Bethe-Heitler interference



$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} = \frac{y^2}{32(2\pi)^4 \sqrt{1 + \frac{4M^2 x_B^2}{Q^2}}} (|\mathcal{T}_{DVCS}|^2 + |\mathcal{T}_{BH}|^2 + \mathcal{I})$$

# Azimuthal asymmetries in DVCS

## Cross section:

$$\sigma(\phi, \phi_S, P_B, C_B, P_T) = \sigma_{UU}(\phi) \cdot \left[ 1 + P_B \mathcal{A}_{LU}^{\text{DVCS}}(\phi) + C_B P_B \mathcal{A}_{LU}^{\mathcal{I}}(\phi) + C_B \mathcal{A}_C(\phi) + P_T \mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) + C_B P_T \mathcal{A}_{UT}^{\mathcal{I}}(\phi, \phi_S) \right]$$

## Azimuthal asymmetries:

- **Beam-charge asymmetry  $\mathcal{A}_C(\Phi)$ :**

$$d\sigma(e^+, \phi) - d\sigma(e^-, \phi) \propto \text{Re}[F_1 \mathcal{H}] \cdot \cos \phi$$

- **Beam-helicity asymmetry  $\mathcal{A}_{LU}^{\mathcal{I}}(\Phi)$ :**

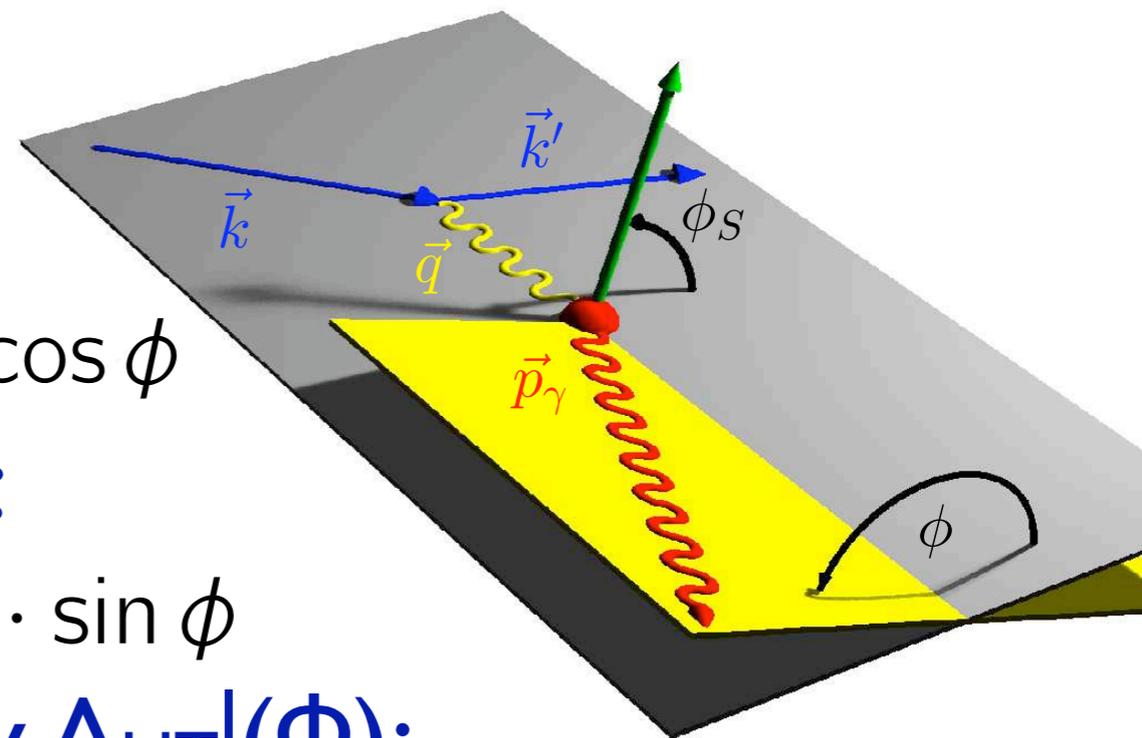
$$d\sigma(e^{\rightarrow}, \phi) - d\sigma(e^{\leftarrow}, \phi) \propto \text{Im}[F_1 \mathcal{H}] \cdot \sin \phi$$

- **Transverse target-spin asymmetry  $\mathcal{A}_{UT}^{\mathcal{I}}(\Phi)$ :**

$$d\sigma(\phi, \phi_S) - d\sigma(\phi, \phi_S + \pi) \propto \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}] \cdot \sin(\phi - \phi_S) \cos \phi + \text{Im}[F_2 \tilde{\mathcal{H}} - F_1 \xi \tilde{\mathcal{E}}] \cdot \cos(\phi - \phi_S) \sin \phi$$

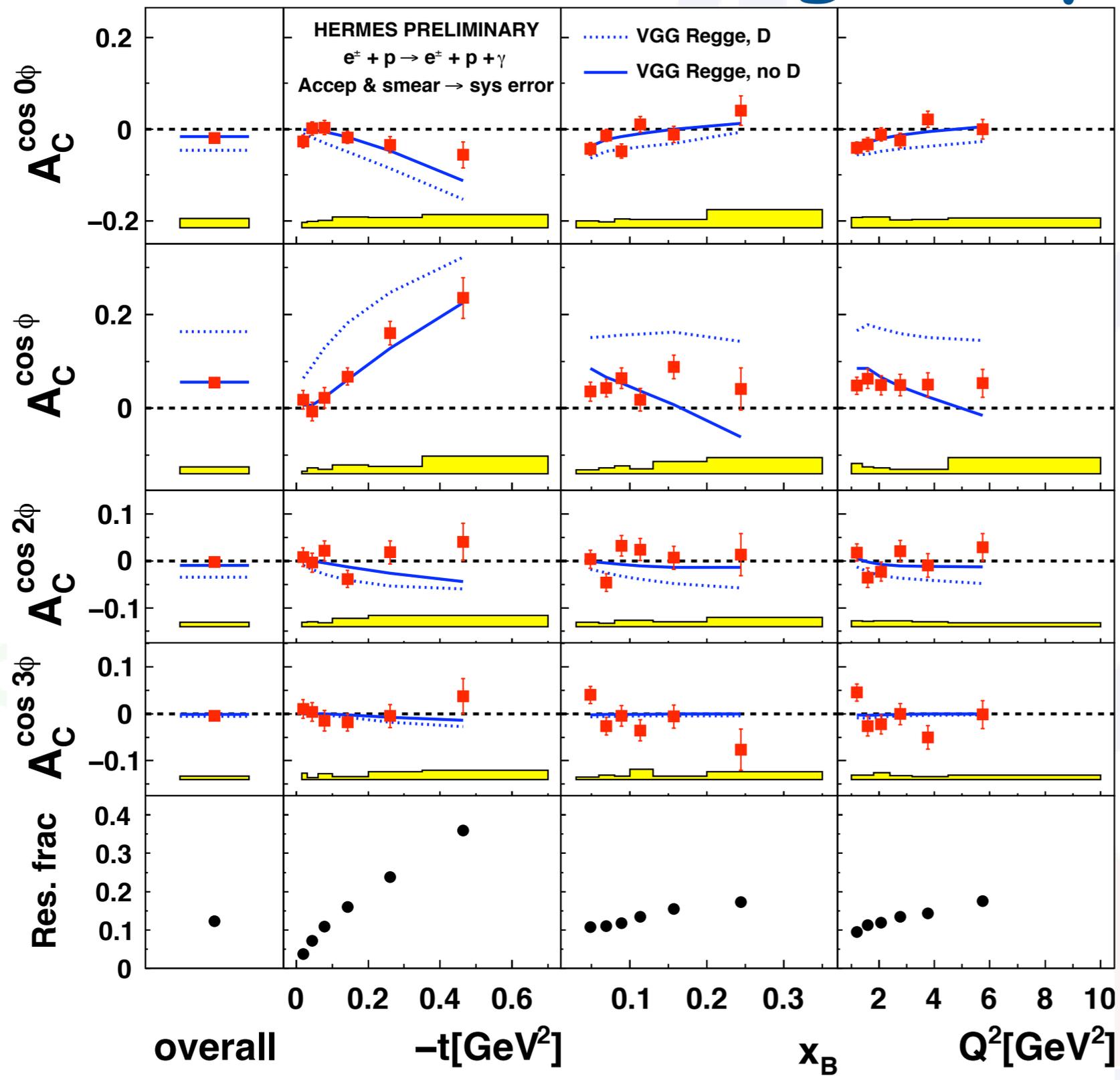
( $F_1, F_2$  are the Dirac and Pauli form factors)

( $\mathcal{H}, \mathcal{E} \dots$  Compton form factors involving GPDs  $H, E, \dots$ )



# Beam-charge asymmetry

All data  
1996-2005



constant term

$$\propto -A_C^{\cos \phi}$$

$$\propto \text{Re}[F_1 \mathcal{H}]$$

[higher twist]

[gluon leading twist]

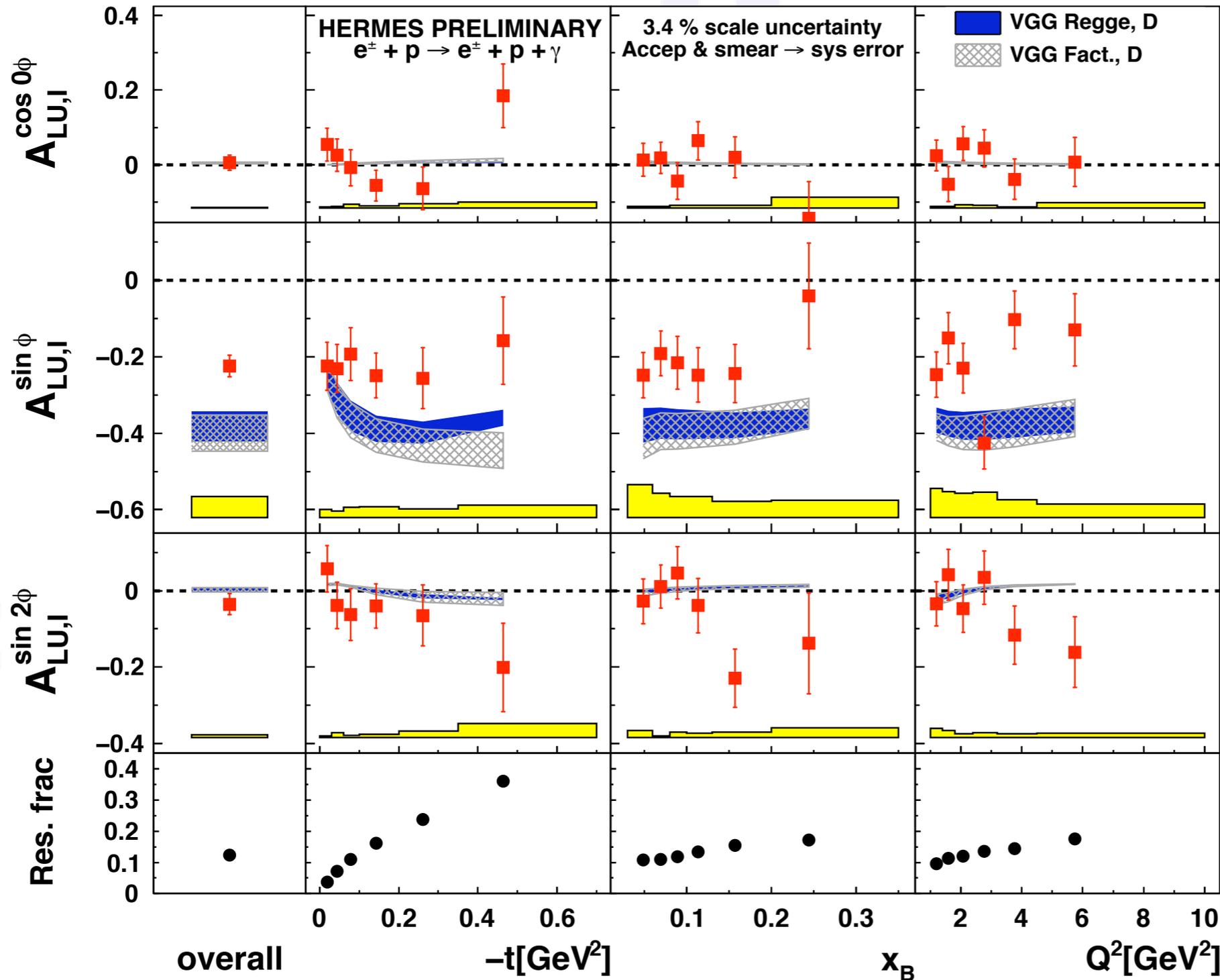
Resonant fraction:

$$ep \rightarrow e\Delta^+\gamma$$

GPD model: "VGG" Phys. Rev. D60 (1999) 094017 & Prog. Nucl. Phys. 47 (2001) 401

# Beam-spin asymmetry

All data  
1996-2005



$$\propto \text{Im}[F_1 \mathcal{H}]$$

[higher twist]

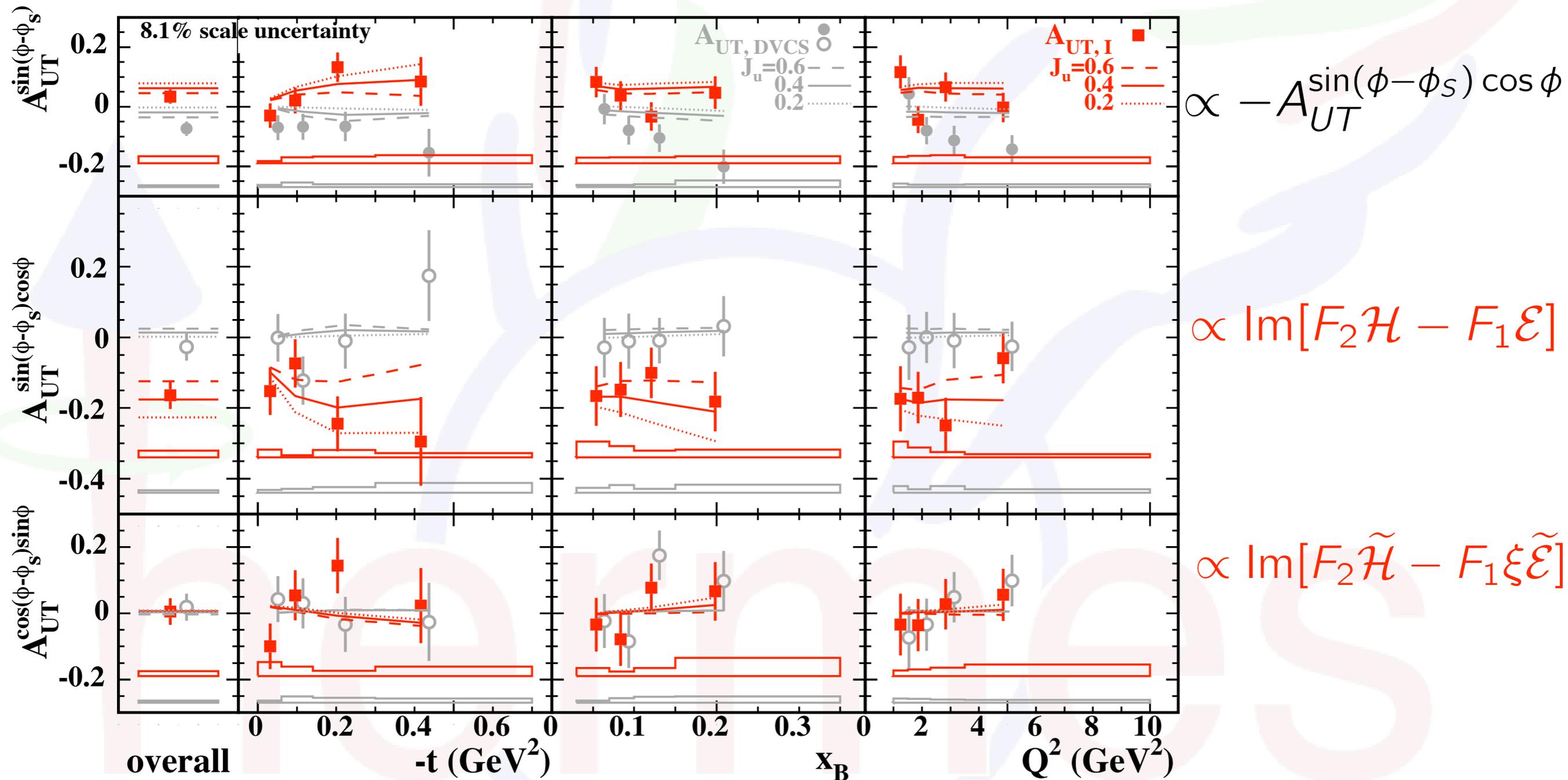
Resonant fraction:

$$ep \rightarrow e\Delta^+ \gamma$$

GPD model: "VGG" Phys. Rev. D60 (1999) 094017 & Prog. Nucl. Phys. 47 (2001) 401

# Transverse target-spin asymmetry

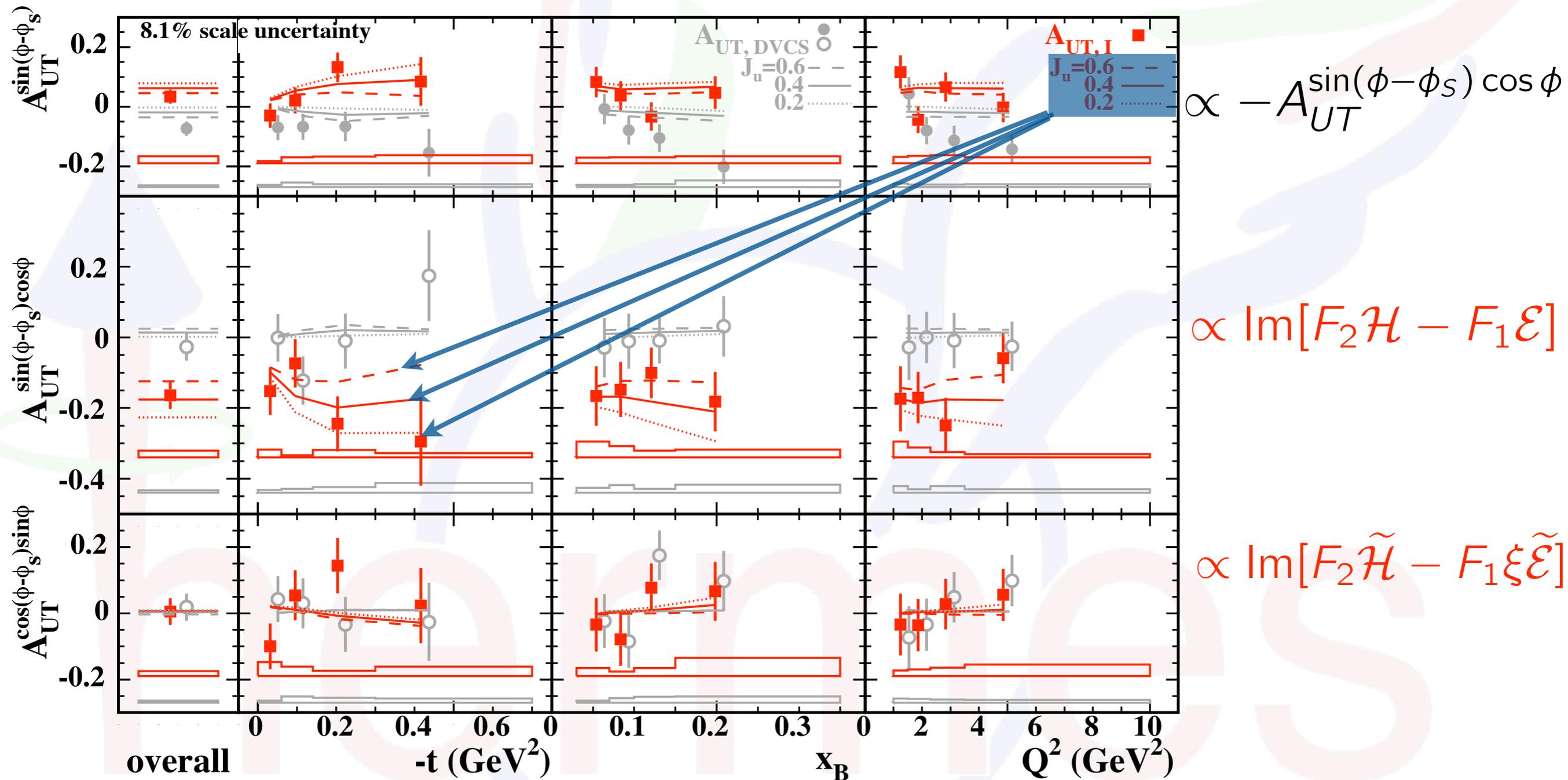
A. Airapetian et al., JHEP 0806:066, 2008



GPD model: "VGG" Phys. Rev. D60 (1999) 094017 & Prog. Nucl. Phys. 47 (2001) 401

# Transverse target-spin asymmetry

A. Airapetian et al., JHEP 0806:066,2008

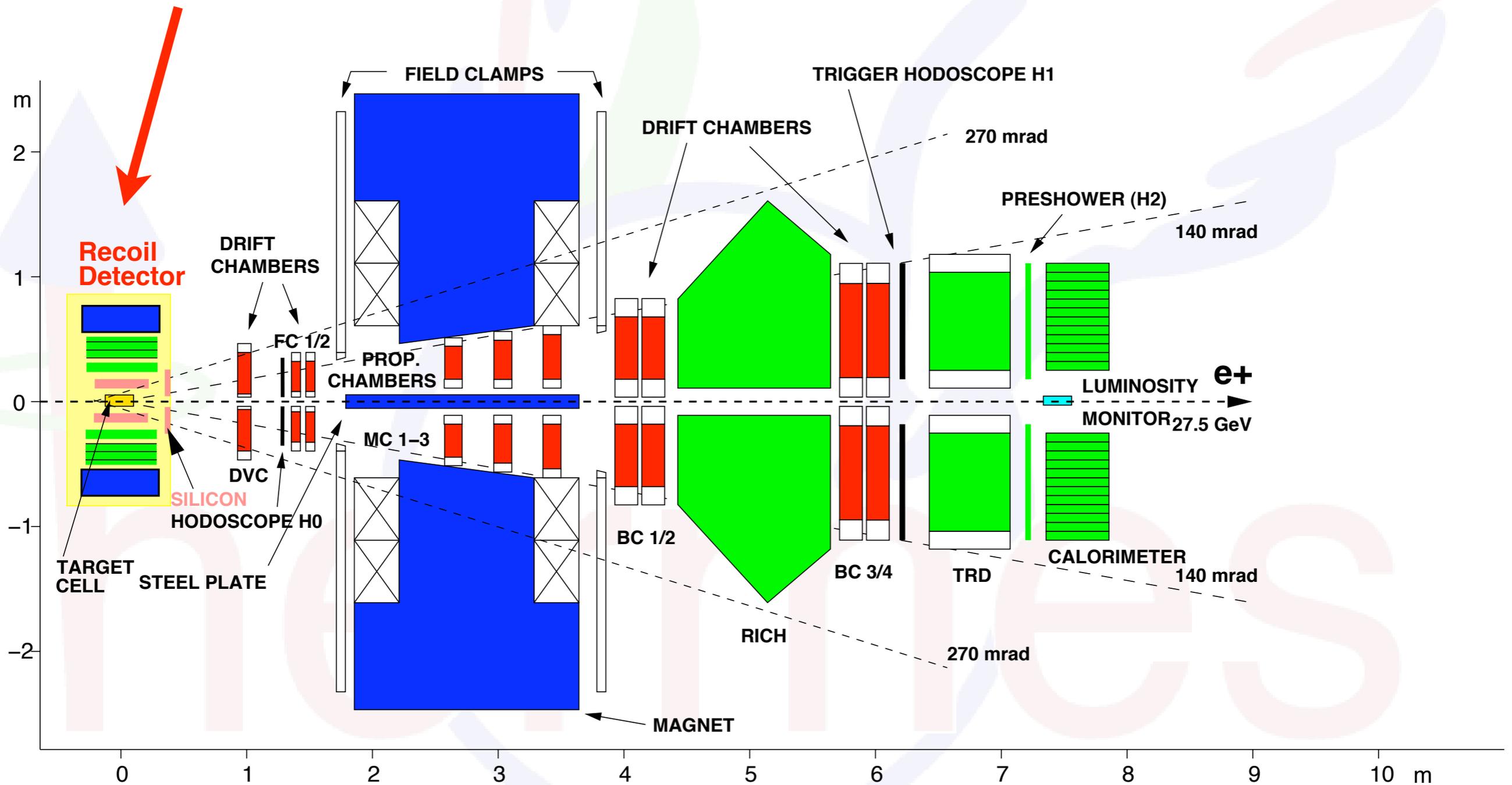


GPD model: "VGG" Phys. Rev. D60 (1999) 094017 & Prog. Nucl. Phys. 47 (2001) 401

# Outlook

# HERMES detector (2006/07)

detection of recoiling proton



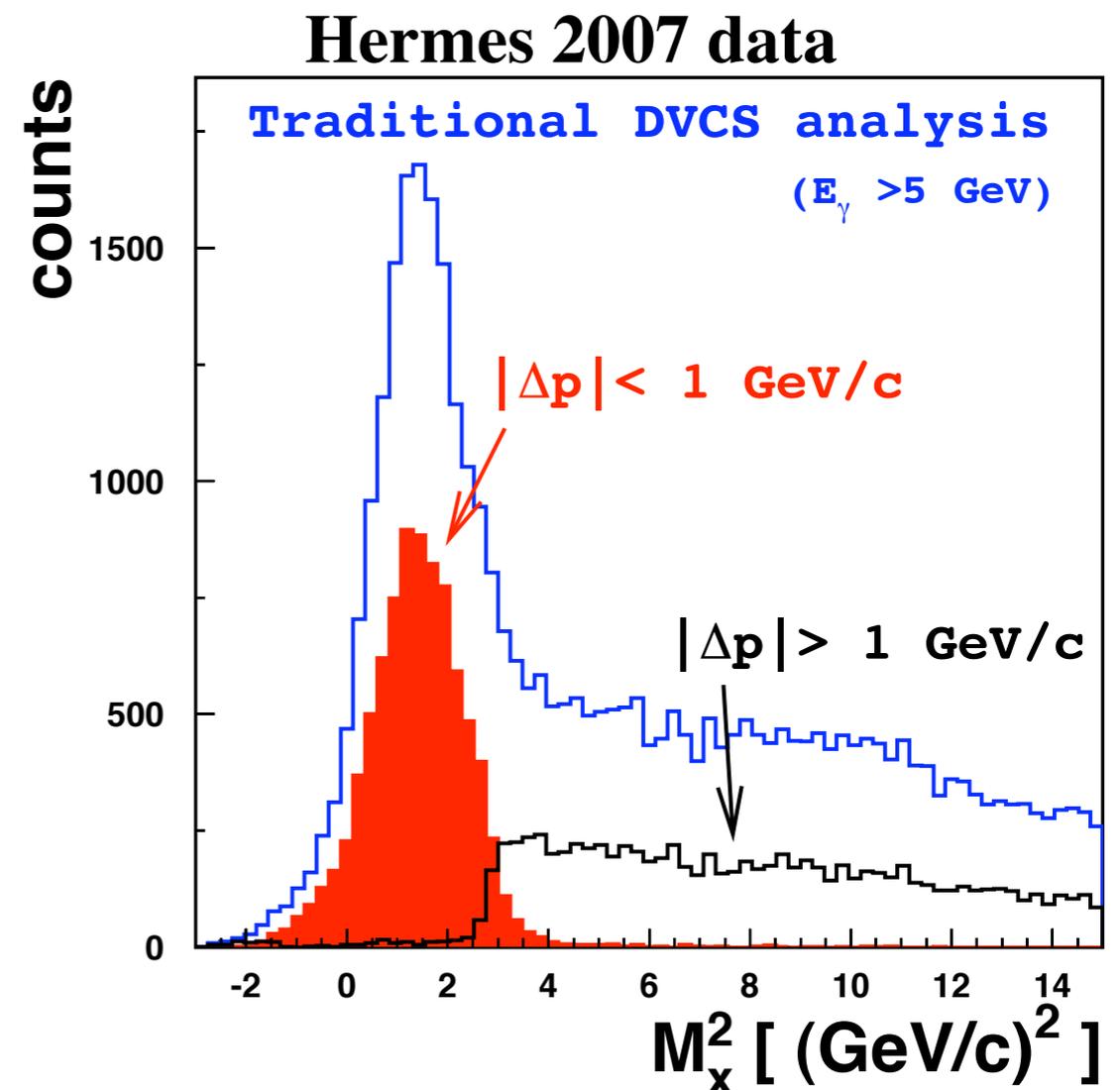
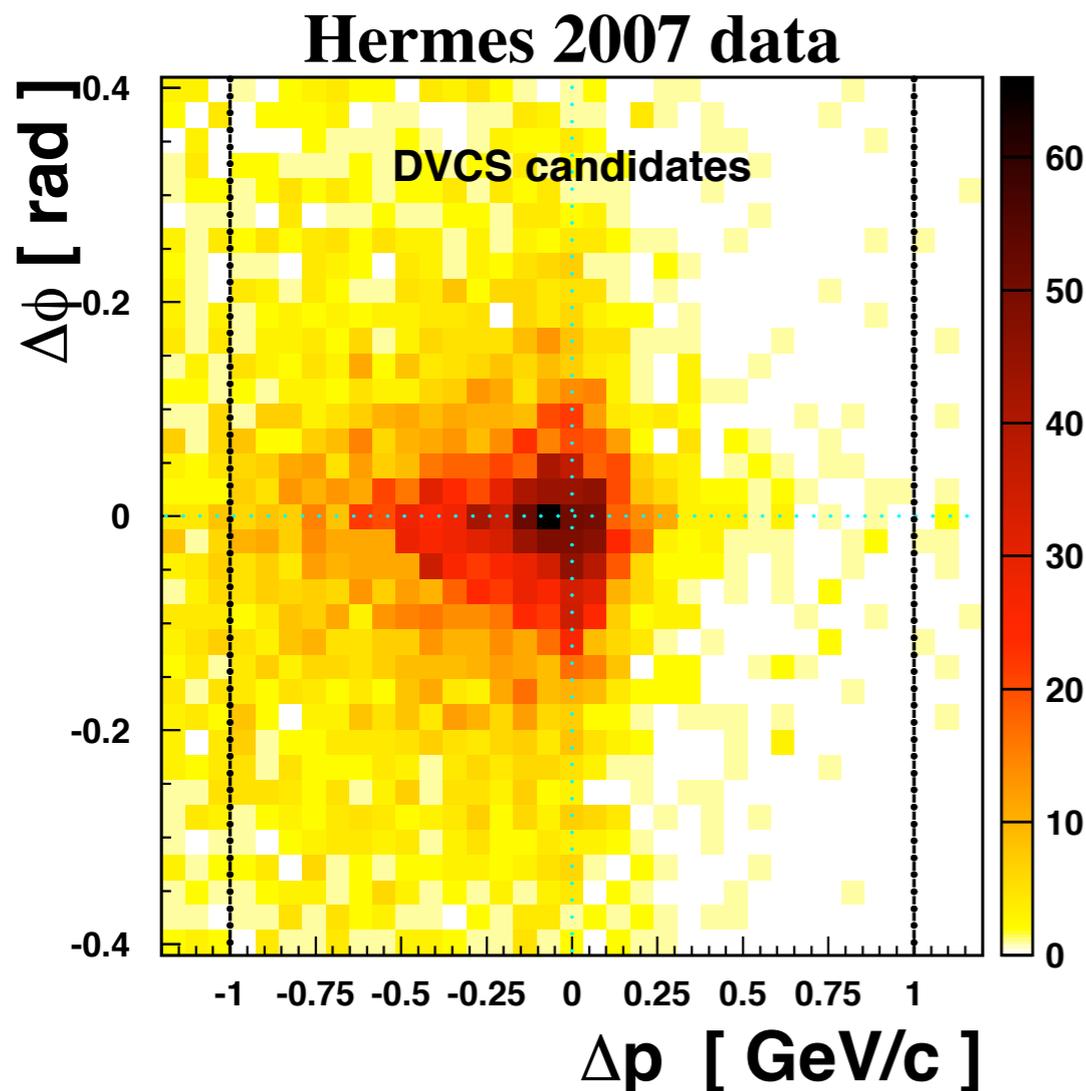
# DVCS event selection

measured with RD

inferred from forward spectrometer

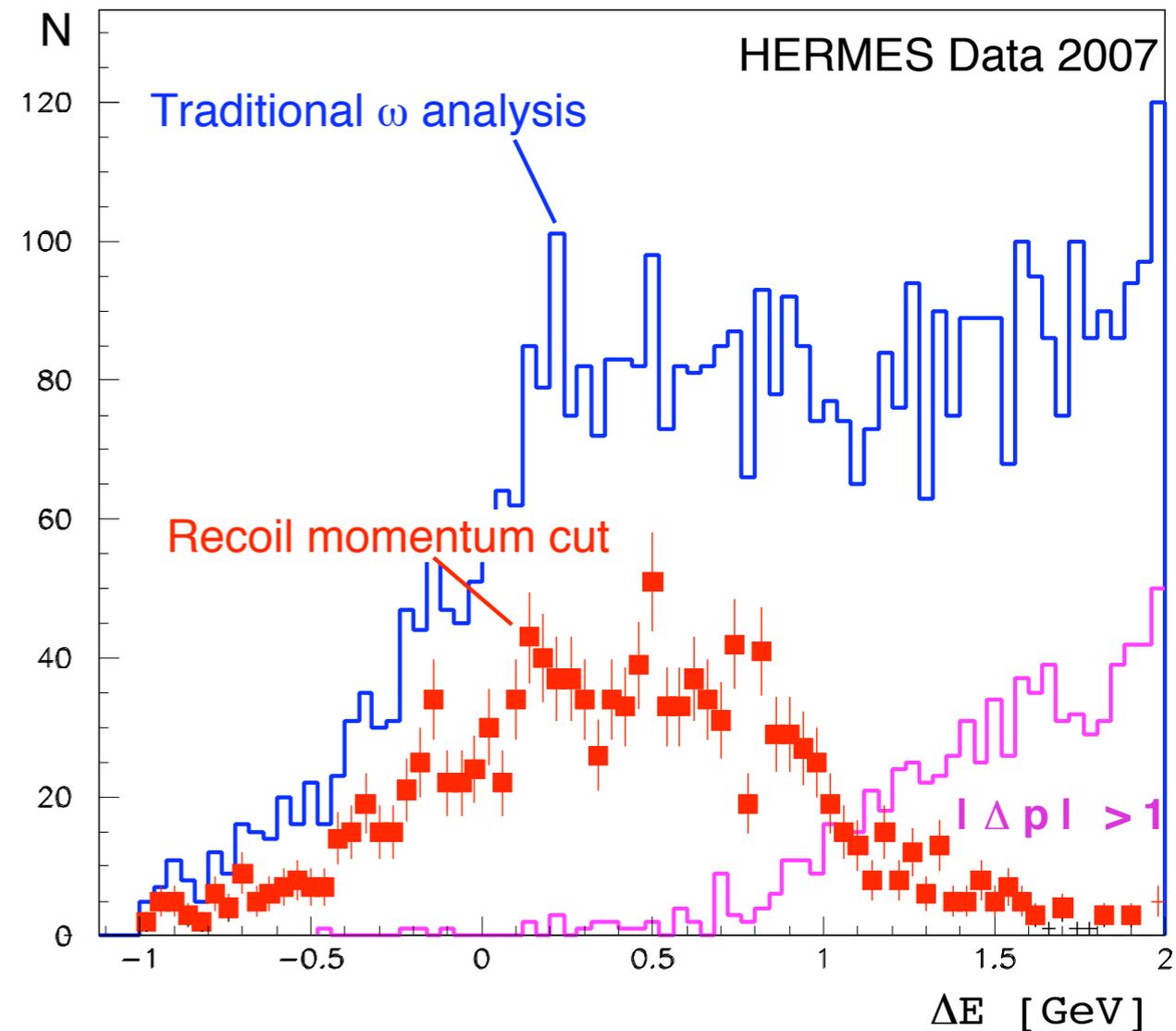
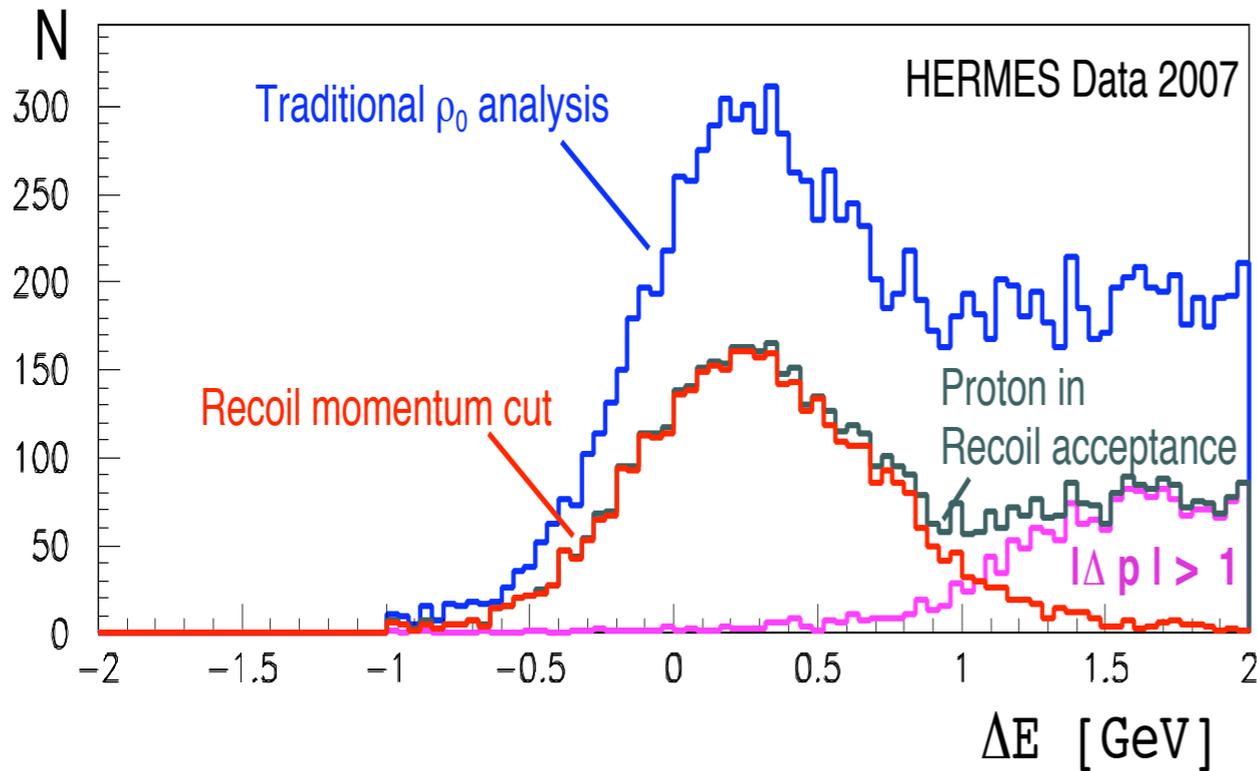
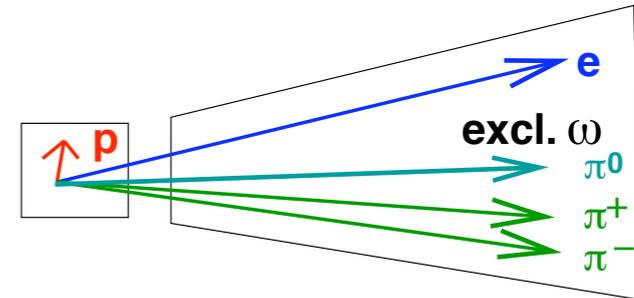
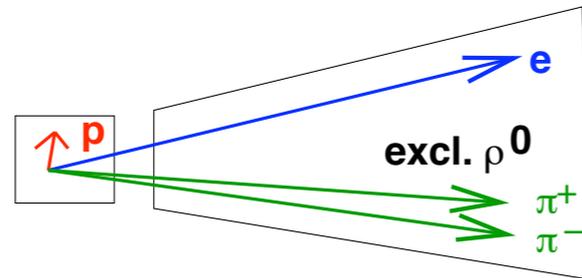
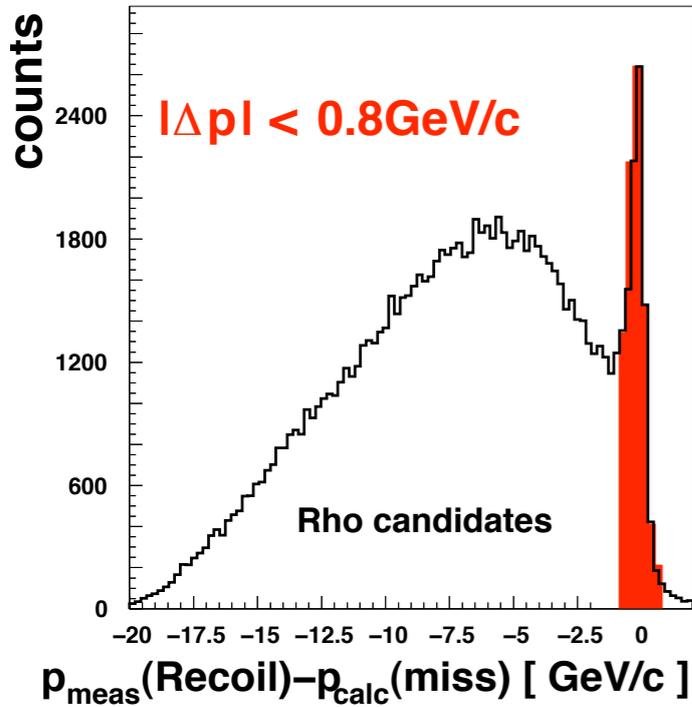
- ▶ Missing  $\phi$ :  $\Delta\phi = \phi_{\text{meas}} - \phi_{\text{calc}}$
- ▶ Missing  $p$ :  $\Delta p = p_{\text{meas}} - p_{\text{calc}}$

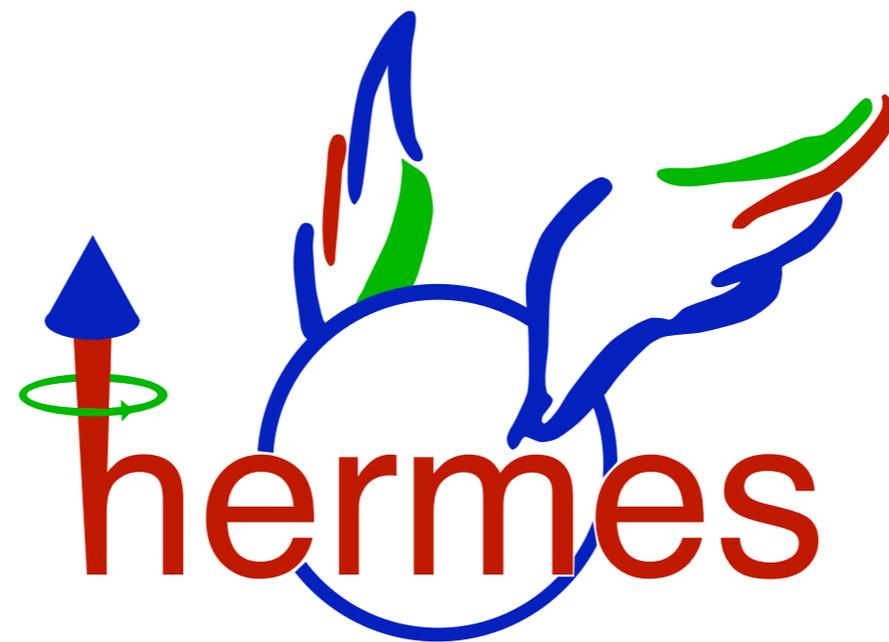
Missing Mass ( $\approx M_P^2$ ):  
 $M_X^2 = (p + p_{\gamma^*} - p_{\gamma})^2$

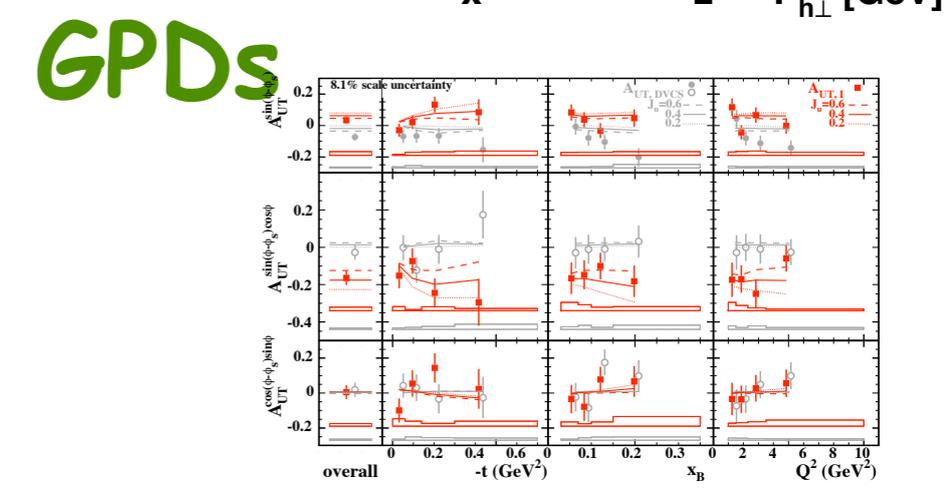
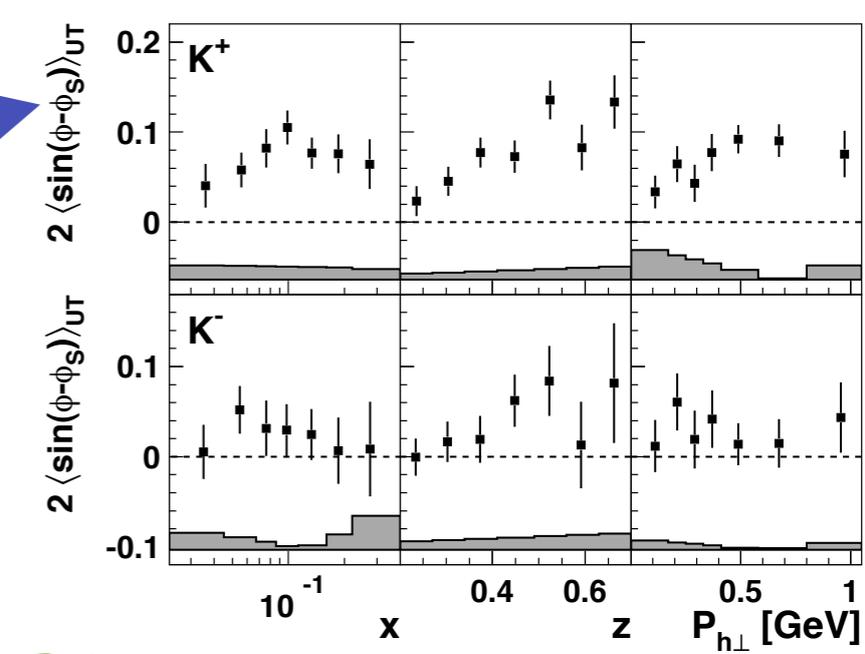
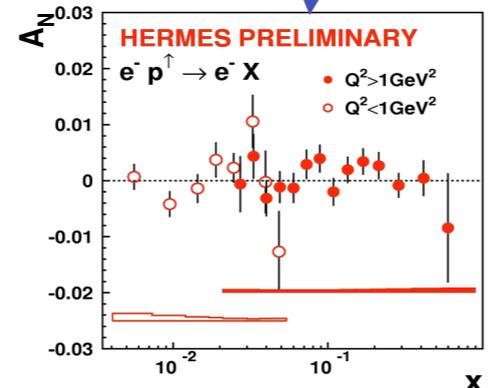
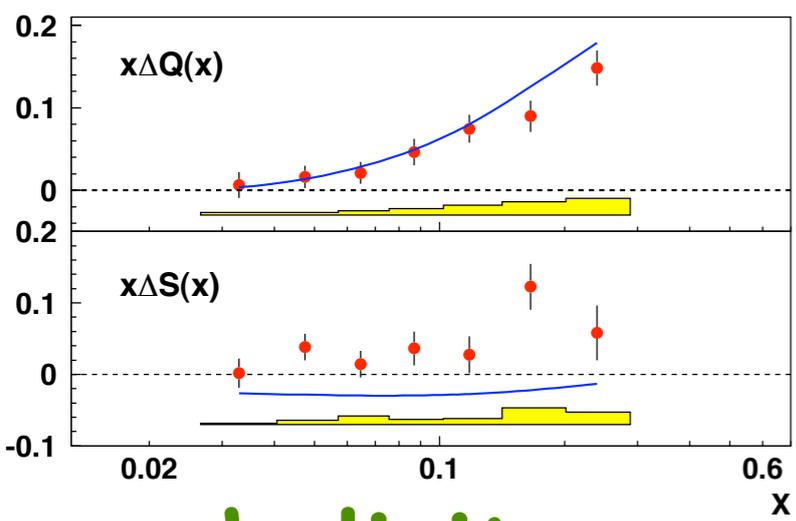
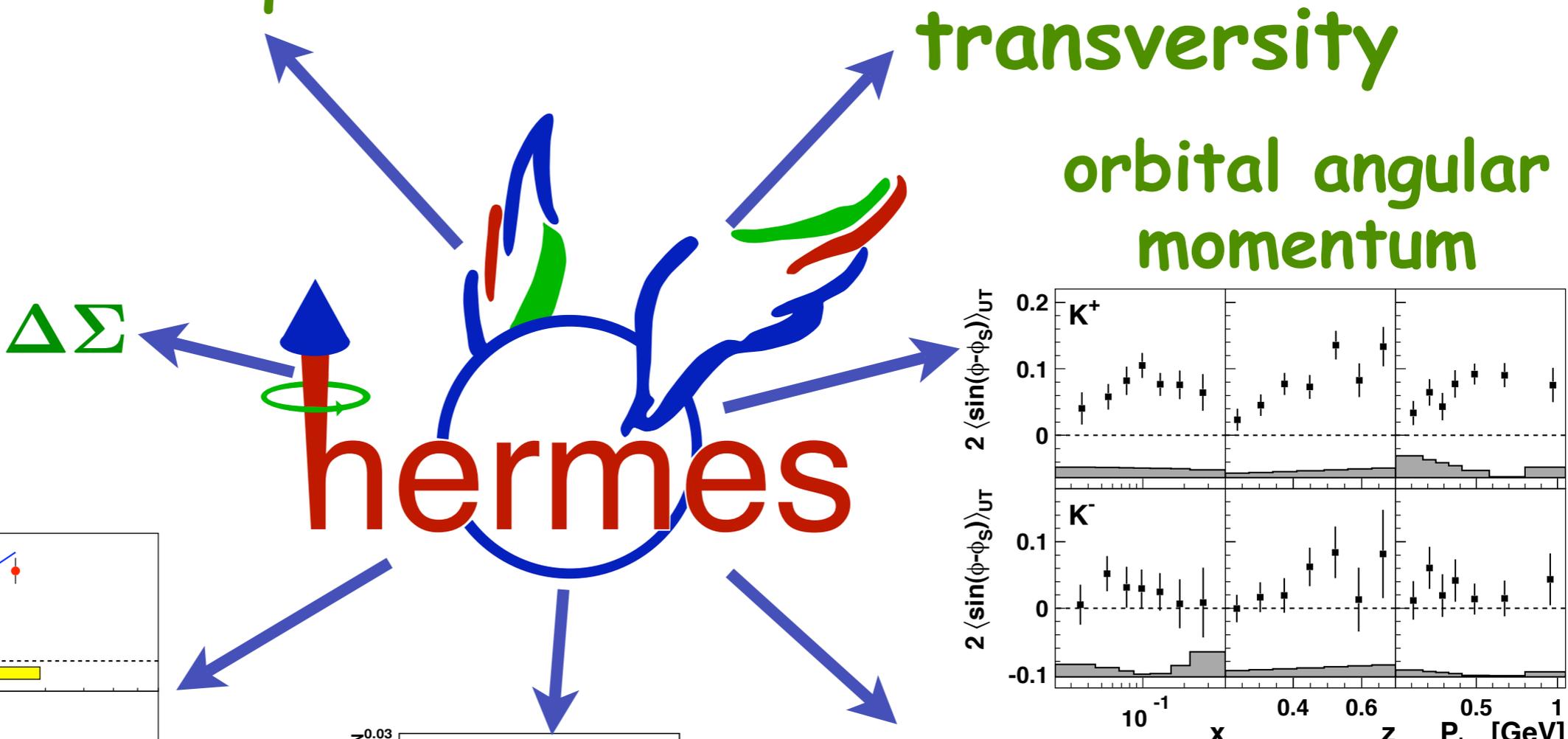
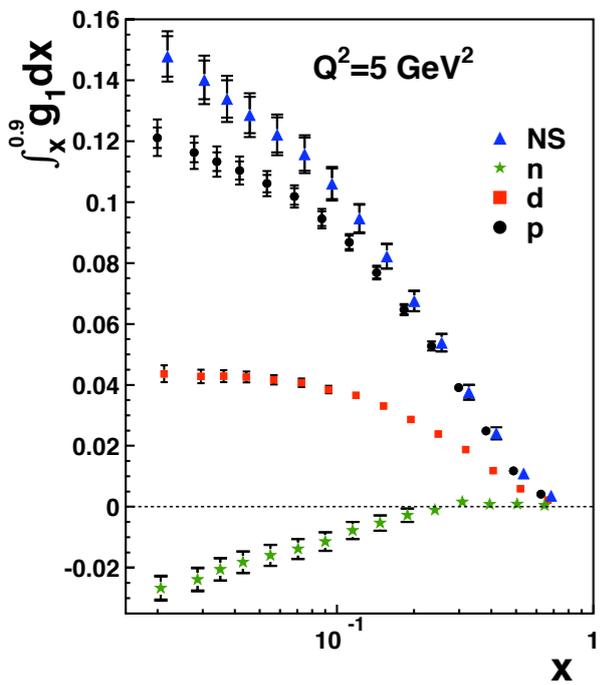
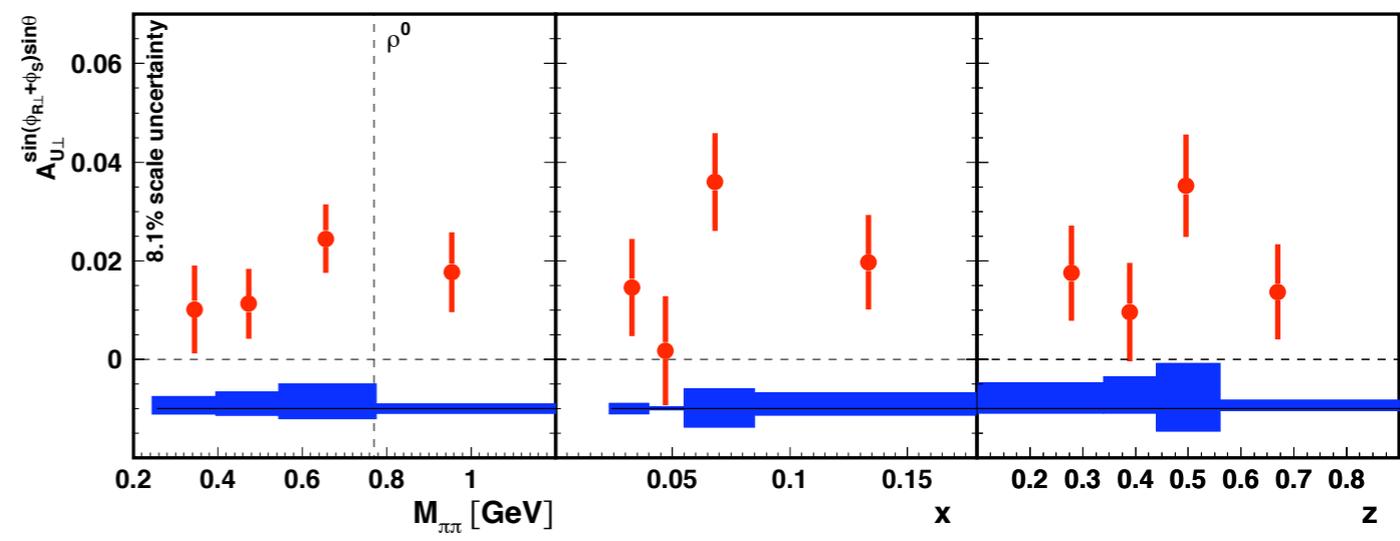
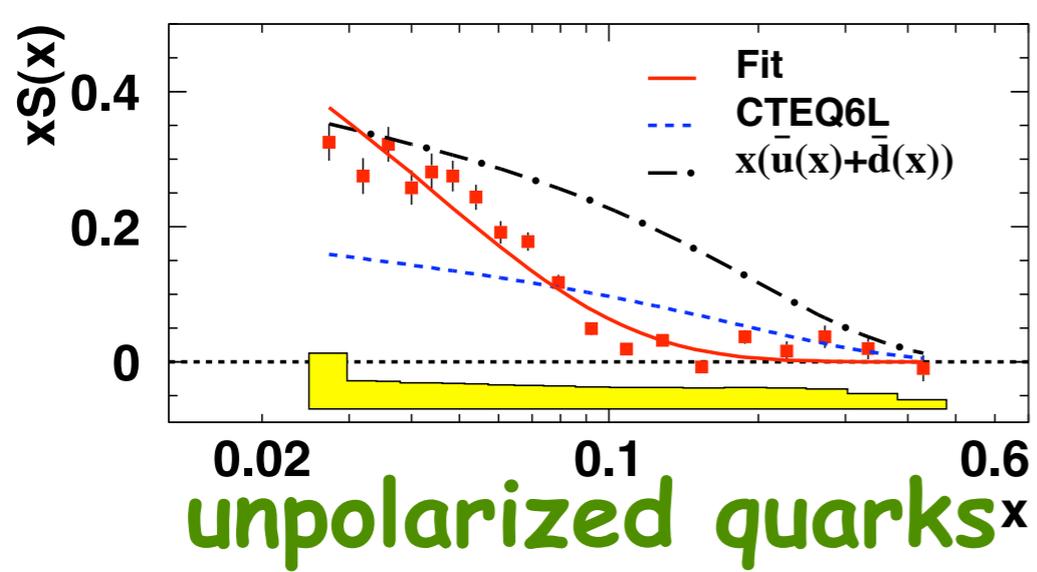


# Exclusive VM event selection

HERMES 2007 data







helicity  
 distributions

2-Photon Exchange