

# Subterahertz Radiation from Corrugated Pipe

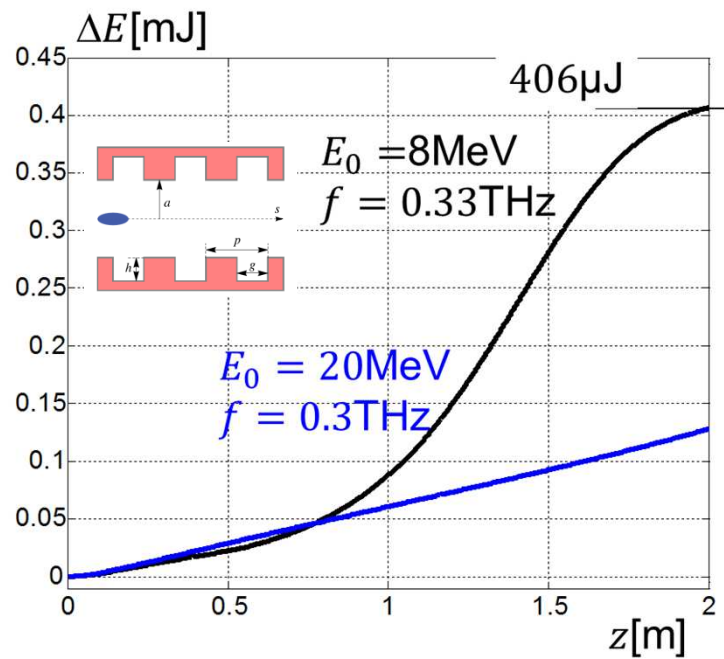
## Self-Consistent Simulation of Longitudinal Dynamics

Igor Zagorodnov

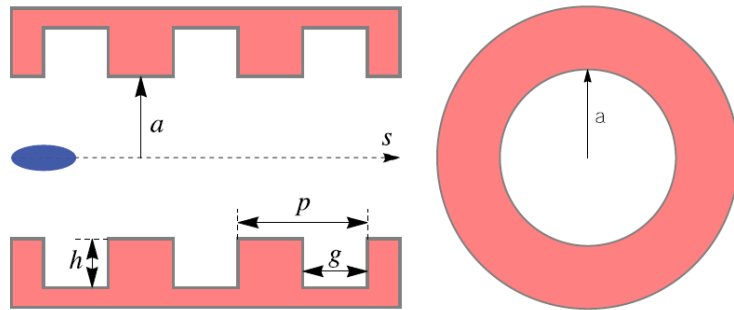
Mini-workshop on THz option at  
PITZ (piTHz)

Zeuthen

22. September 2015



# Problem fomulation. Relativistic bunch.



Nuclear Instruments and Methods in Physics Research A 677 (2012) 67–73

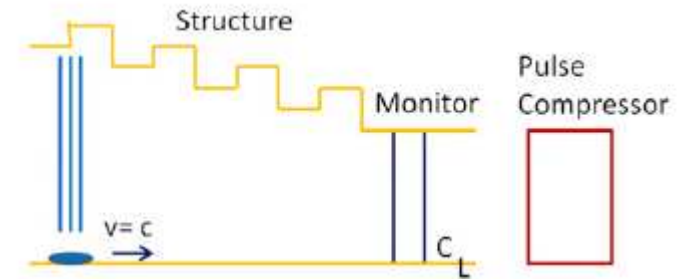
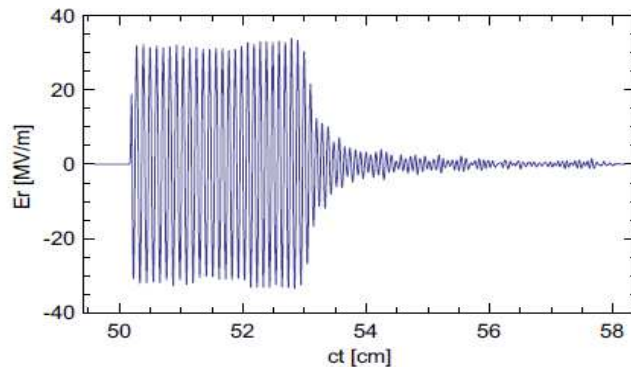


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 Physics Research A**  
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## Terahertz radiation from a pipe with small corrugations<sup>☆</sup>

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**Table 1**

Parameters for the standard tapered, corrugated structure and for the exciting bunch, to be used in simulations given in the next section.

Pipe radius $a$ , mm	2–1
Pipe length $L$ , cm	50
Depth $\delta$ , $\mu\text{m}$	50
Period $p$ , $\mu\text{m}$	40
Gap $g$ , $\mu\text{m}$	20
Bunch charge $Q$ , nC	1
Bunch length $\sigma_2$ , $\mu\text{m}$	100

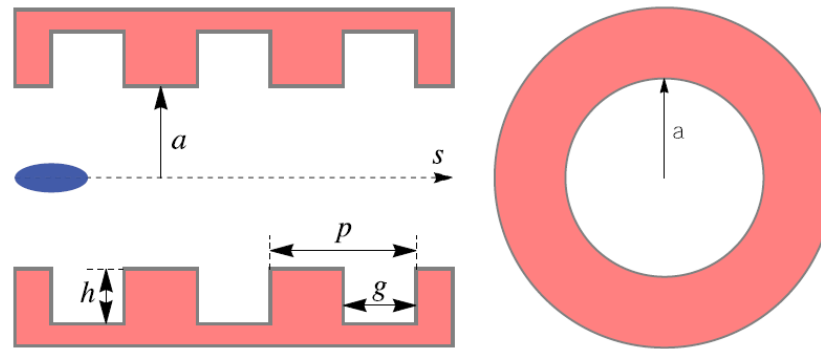
**Table 2**

Radiation properties (numerical results).

Frequency $f$ , THz	0.30–0.44
Pulse energy $U$ , mJ	2.3
<b>Pre-compression</b>	
Peak power $P$ , MW	20
Pulse length $\ell$ , cm	3.5
<b>Post-compression</b>	
Peak power $P$ , MW	250
Pulse length $\ell$ , cm	0.3



# Problem fomulation. Low energy



PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS 18, 030709 (2015)

## Using pipe with corrugated walls for a subterahertz free electron laser

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(Received 1 January 2015; published 18 March 2015)

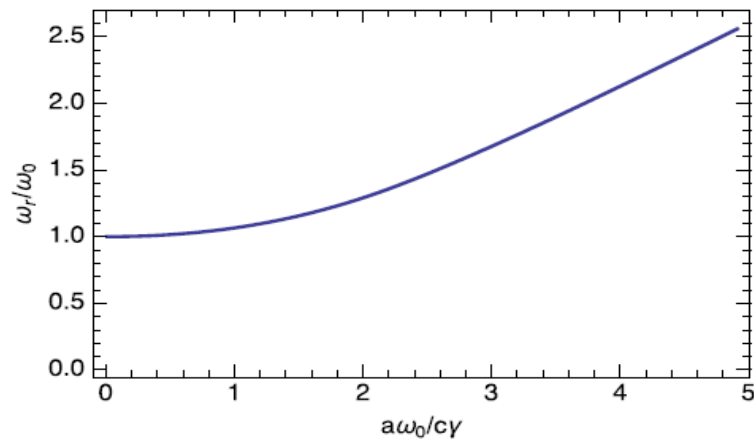
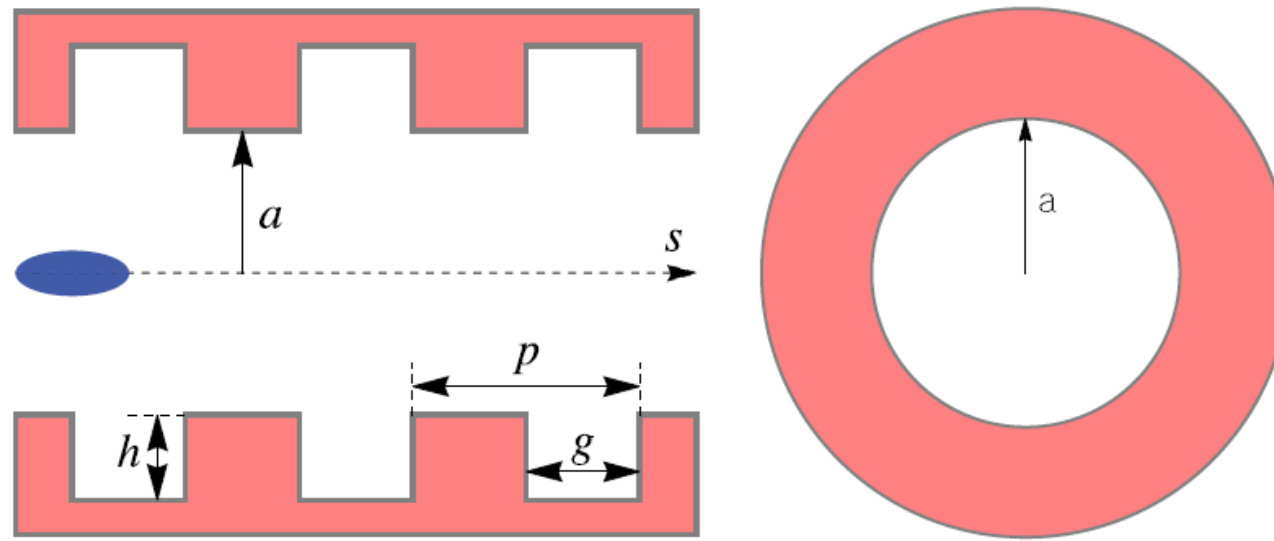


TABLE I. Corrugation and beam parameters.

Pipe radius (mm)	2
Depth $h$ ( $\mu\text{m}$ )	50
Period $p$ ( $\mu\text{m}$ )	40
Gap $g$ ( $\mu\text{m}$ )	10
Bunch charge (nC)	1
Energy (MeV)	5
Bunch length (ps)	10

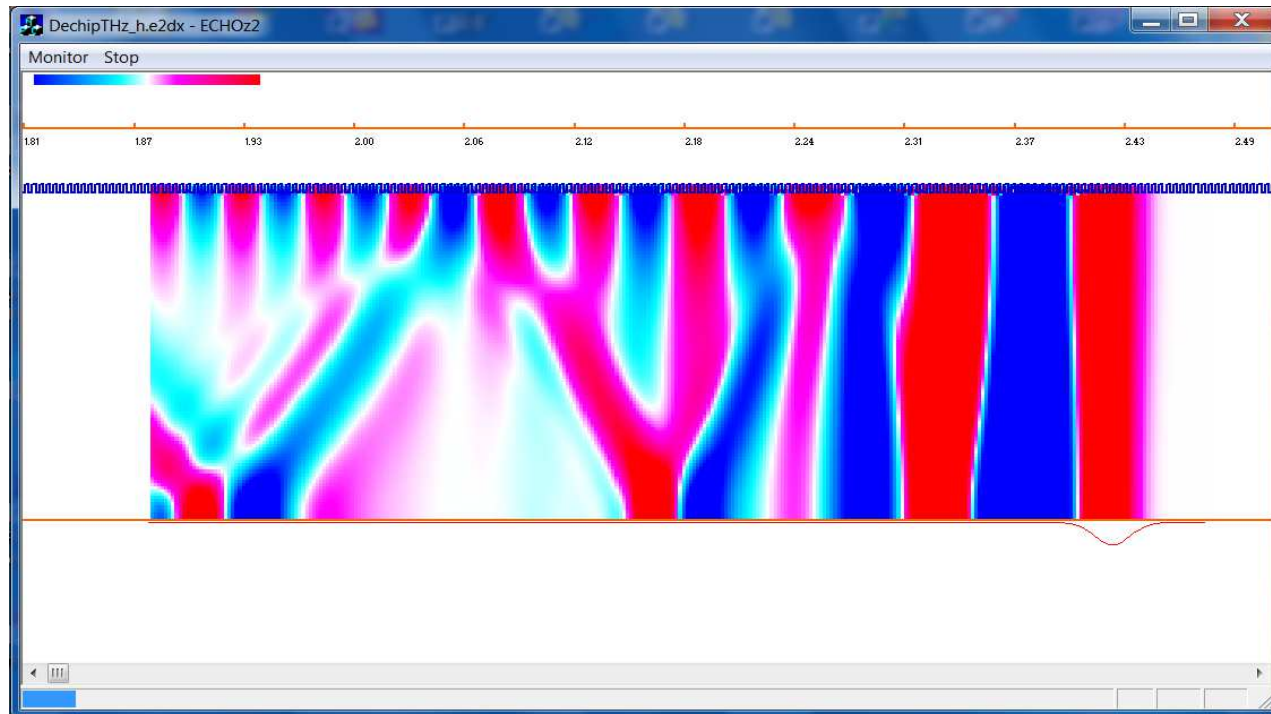


# Problem fomulation. Geometry



Pipe radius $a$ , mm	2
Pipe length $L$ , m	0.5-2
Corrugation depth $h$ , mm	0.05
Corrugation period $p$ , mm	0.04
Corrugation gap $g$ , mm	0.02
Gaussian bunch rms $\sigma$ , mm	0.1-0.3(*8)

# Code modification



Wakefield code ECHO  
(with resistivity)



Particle-in-Cell code ECHO-PIC  
(only longitudinal dynamics)

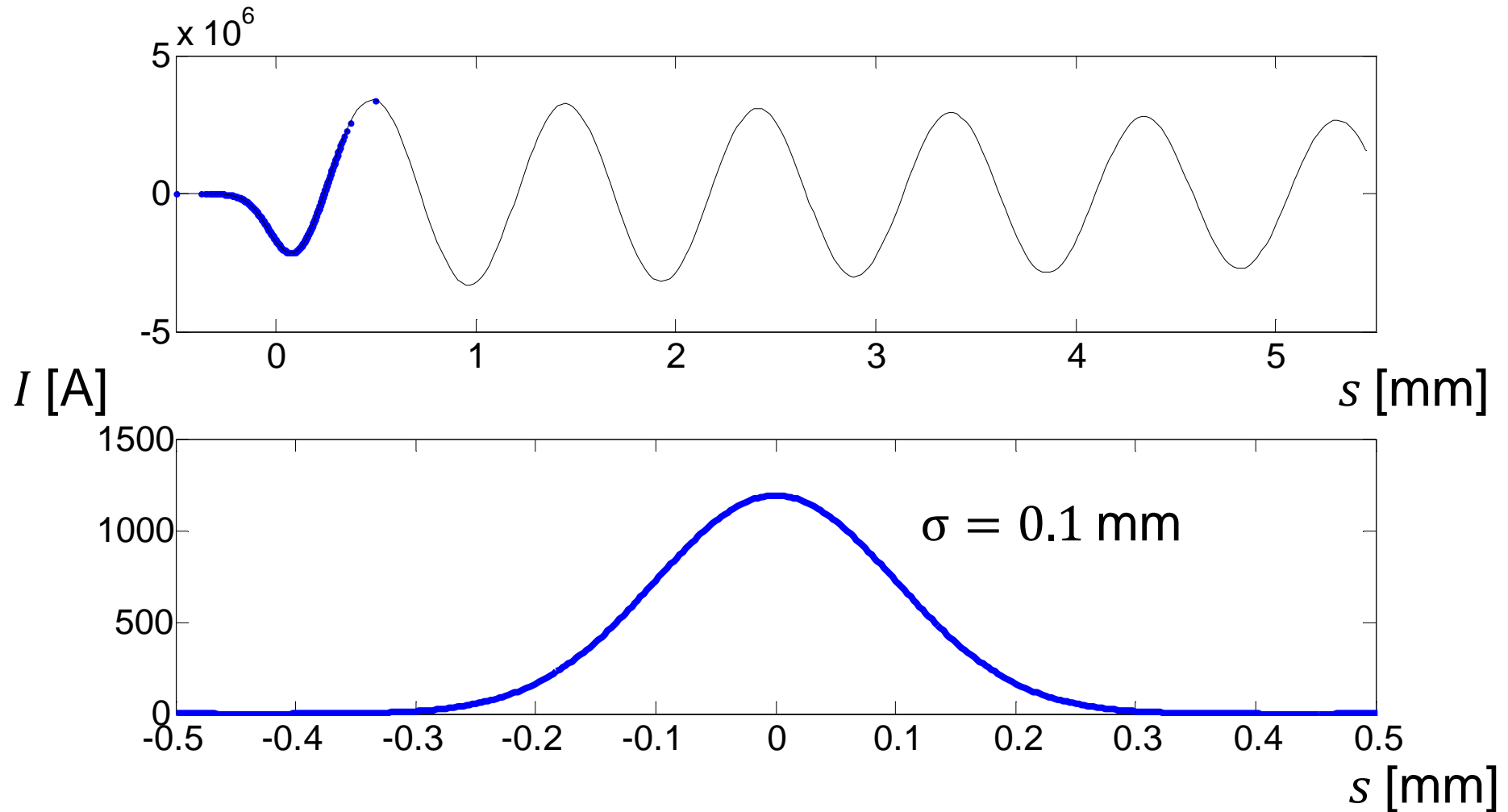
# Short bunch. High charge. High Energy

Pipe length $L$ , m	0.5
Bunch energy $E_0$ , MeV	14000
Gaussian bunch rms $\sigma$ , mm	0.1
Charge $Q$ , nC	1



# Short bunch. High charge. High Energy

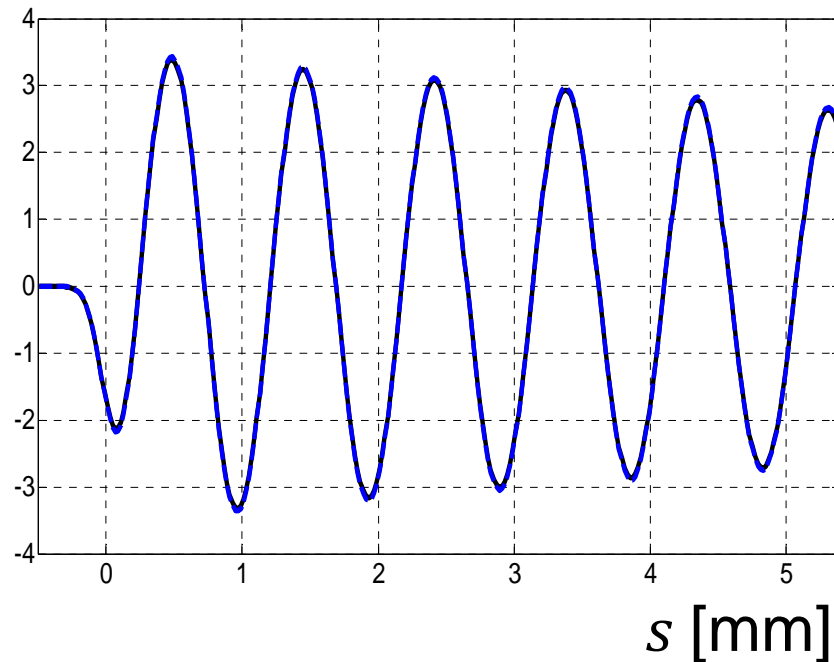
$2\Delta E$  [eV/m]       $Q = 1$  nC       $E_0 = 14$  GeV



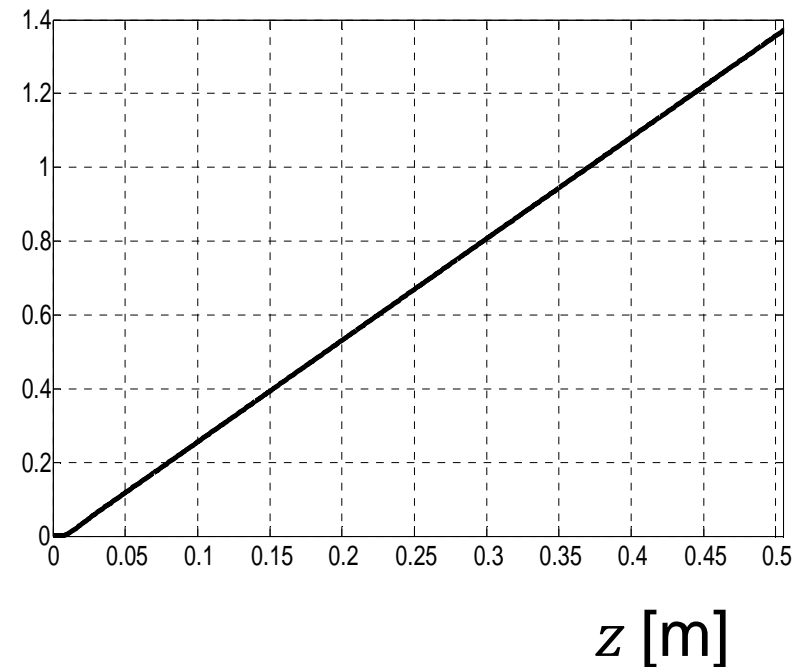
# Short bunch. High charge. High Energy

$$Q = 1 \text{ nC} \quad E_0 = 14 \text{ GeV} \quad \sigma = 0.1 \text{ mm}$$

$\Delta E$  [MeV]



$\Delta E$  [mJ]





# Short bunch. High charge. Low Energy

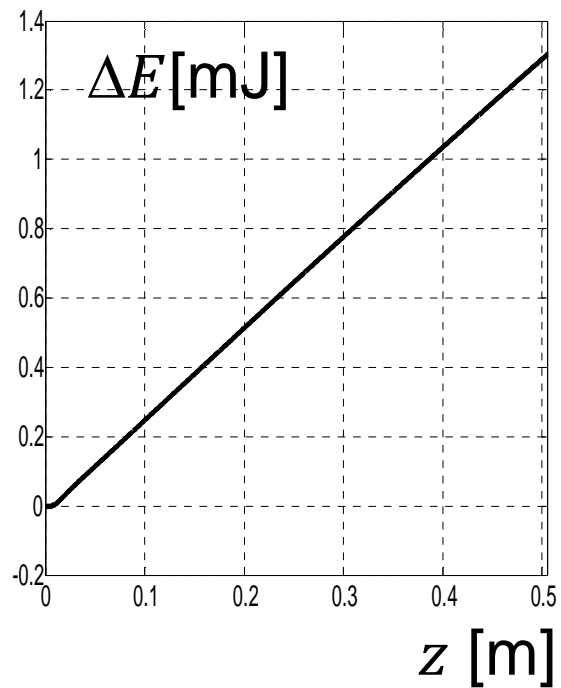
Pipe length $L$ , m	0.5
Bunch energy $E_0$ , MeV	5-20
Gaussian bunch rms $\sigma$ , mm	0.1
Charge $Q$ , nC	1



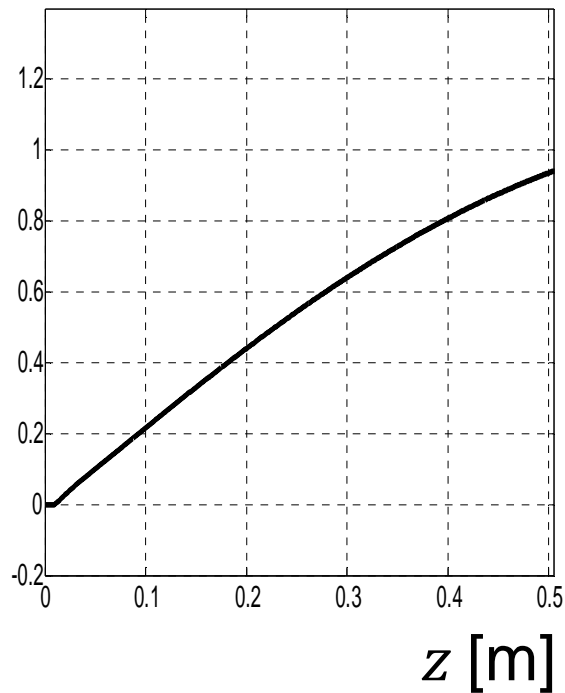
# Short bunch. High charge. Low Energy

$$Q = 1 \text{ nC} \quad \sigma = 0.1 \text{ mm}$$

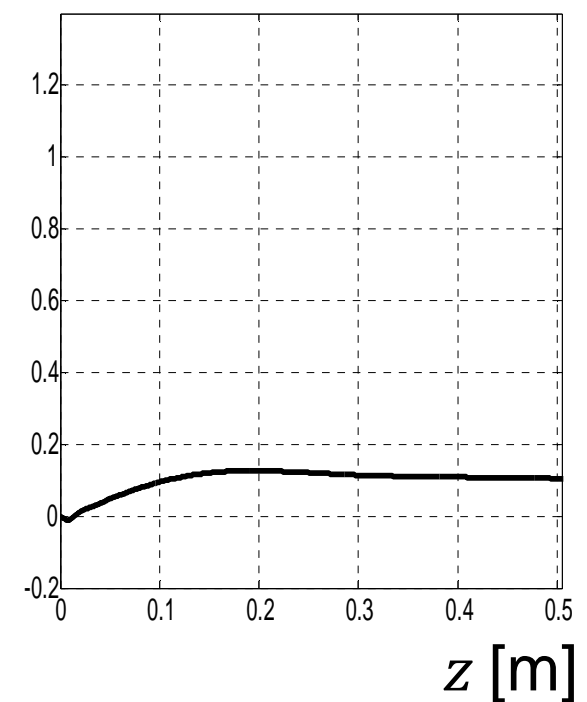
$$E_0 = 20 \text{ MeV}$$



$$E_0 = 10 \text{ MeV}$$

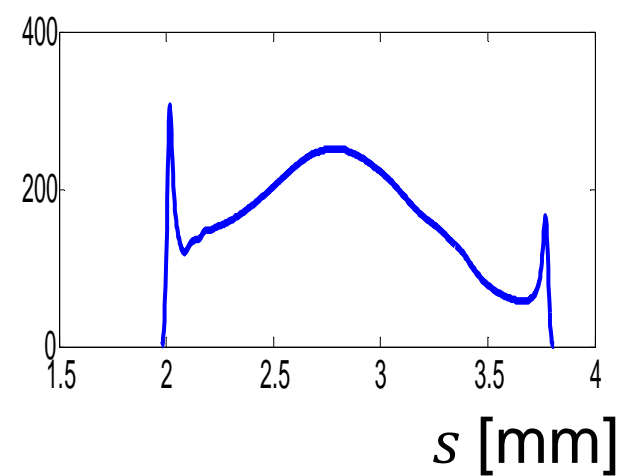
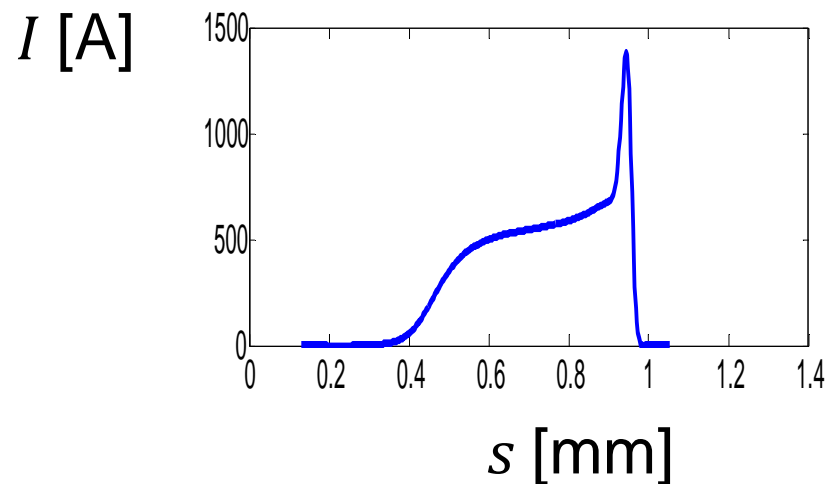
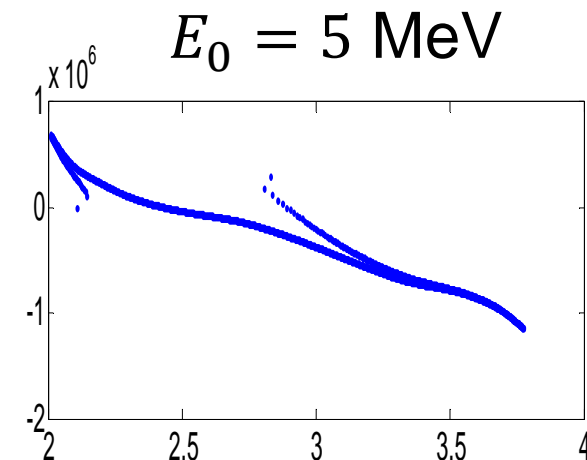
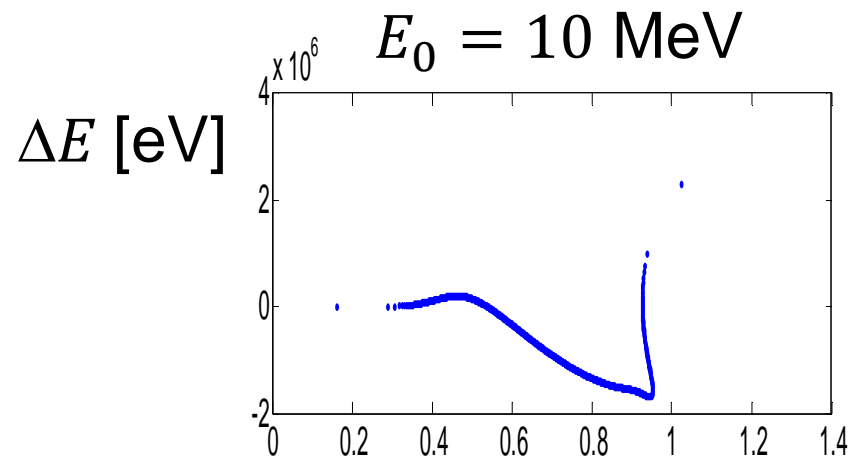


$$E_0 = 5 \text{ MeV}$$



# Short bunch. High charge. Low Energy

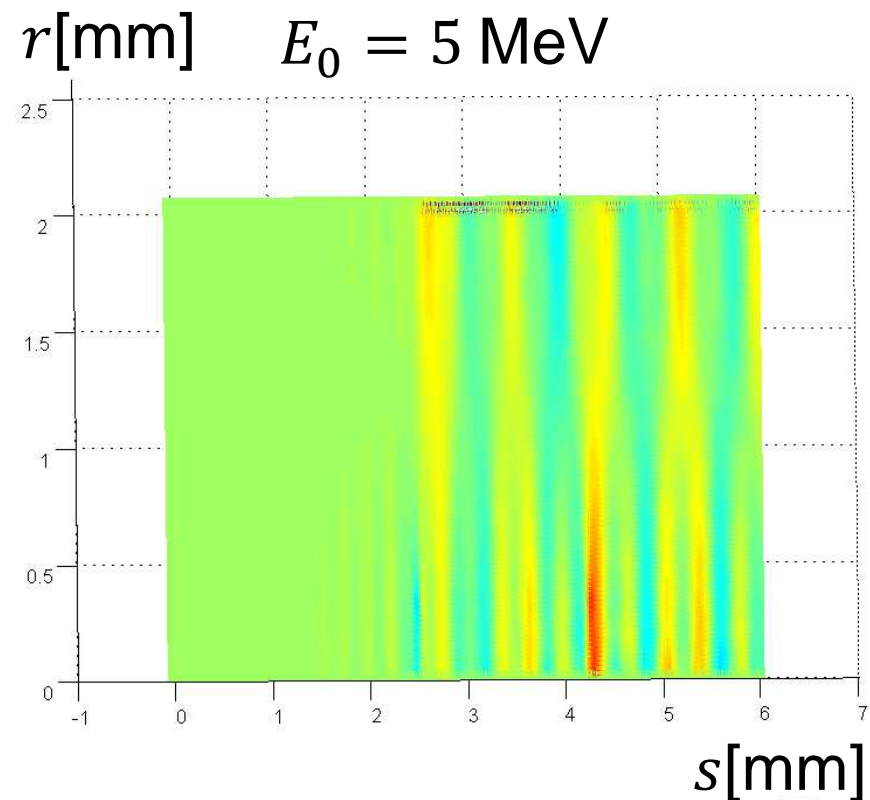
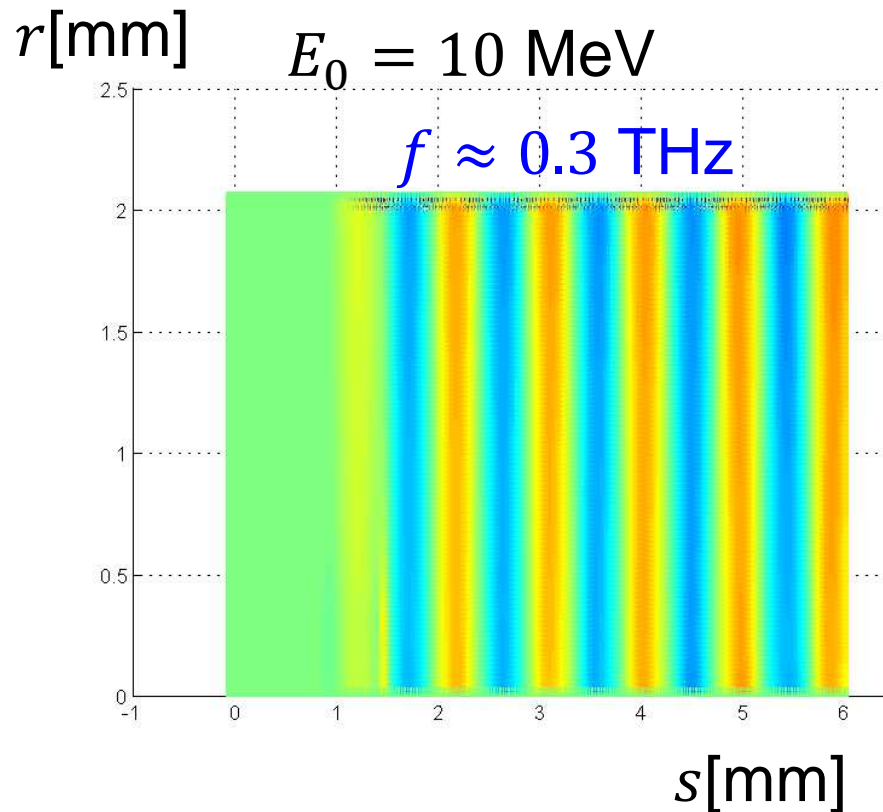
$$Q = 1 \text{ nC} \quad \sigma = 0.1 \text{ mm} \quad I_0 = 1200 \text{ A}$$



# Short bunch. High charge. Low Energy

Longitudinal electric field component  $E_z$

$$Q = 1 \text{ nC} \quad \sigma = 0.1 \text{ mm}$$



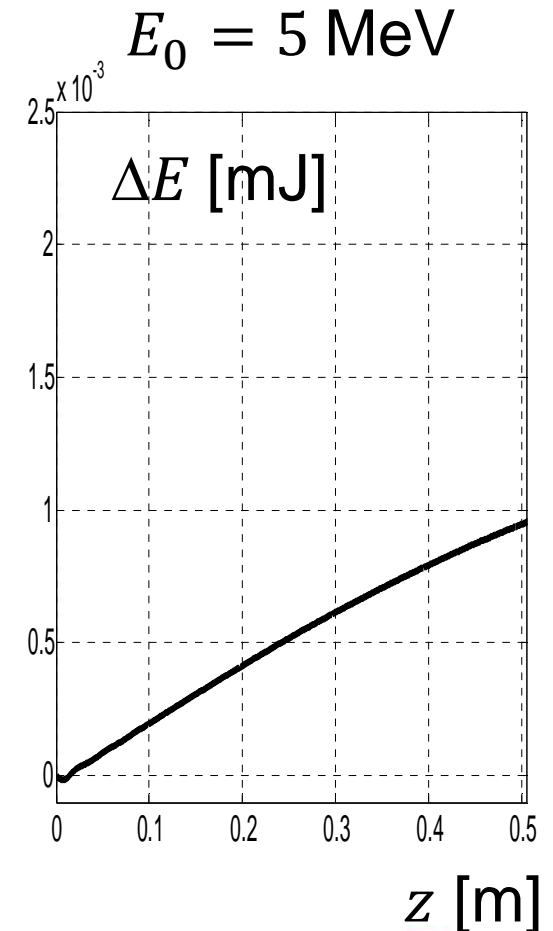
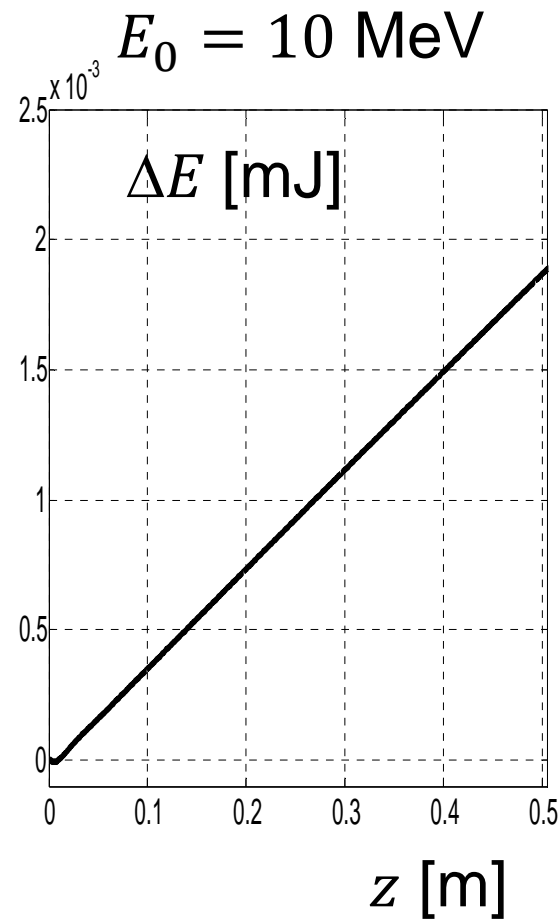
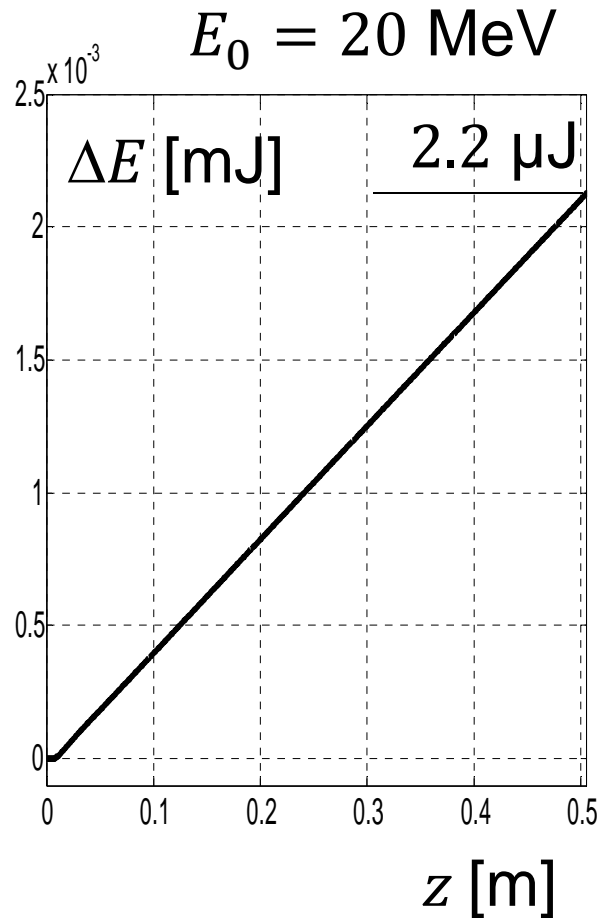
# Short bunch. Low charge. Low Energy

Pipe length $L$ , m	0.5
Bunch energy $E_0$ , MeV	5-20
Gaussian bunch rms $\sigma$ , mm	0.1
Charge $Q$ , nC	0.04



# Short bunch. Low charge. Low Energy

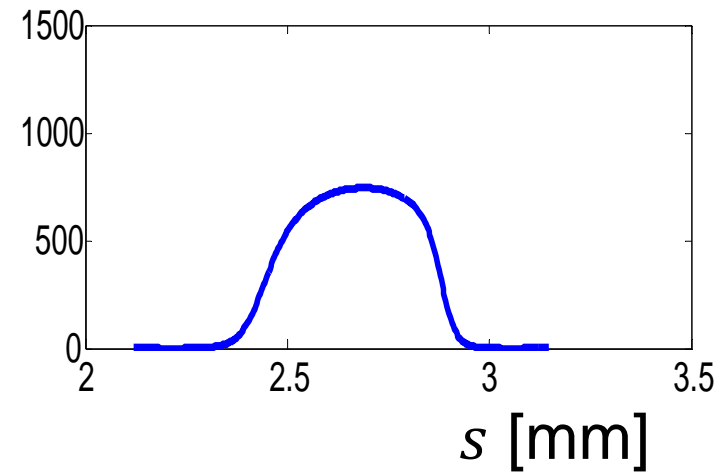
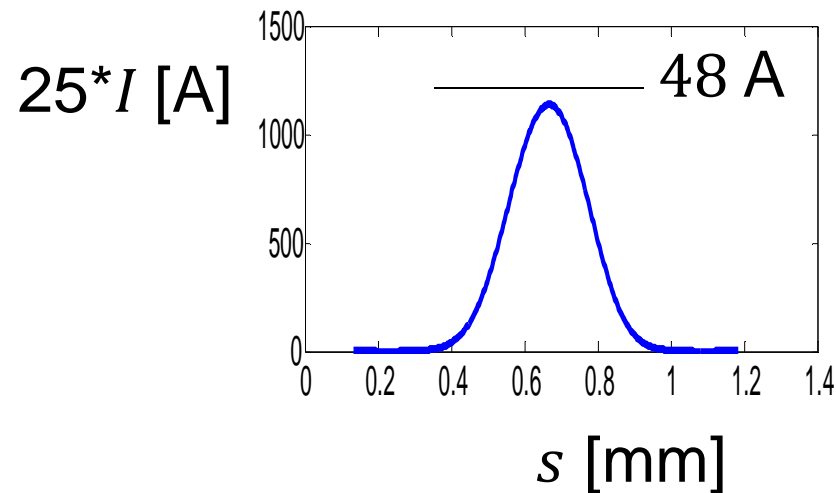
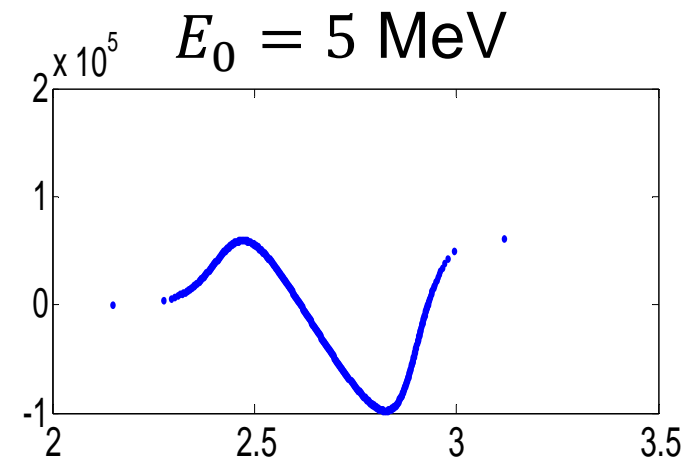
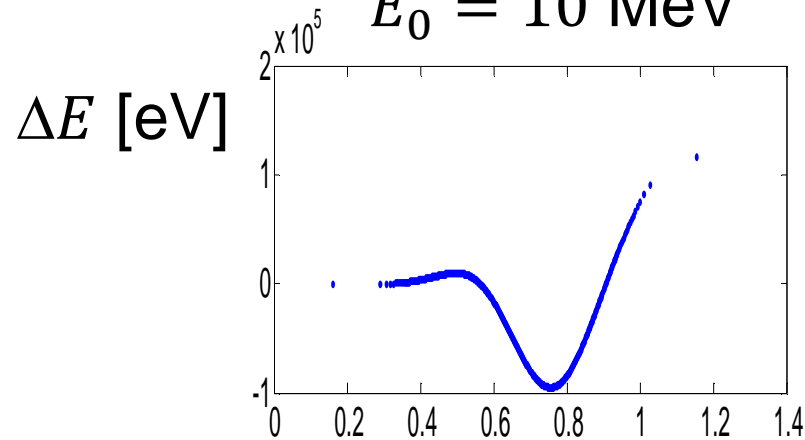
$$Q = 40 \text{ pC} \quad \sigma = 0.1 \text{ mm} \quad I_0 = 48 \text{ A}$$



# Short bunch. Low charge. Low Energy

$$Q = 40 \text{ pC} \quad \sigma = 0.1 \text{ mm} \quad I_0 = 48 \text{ A}$$

$$E_0 = 10 \text{ MeV}$$

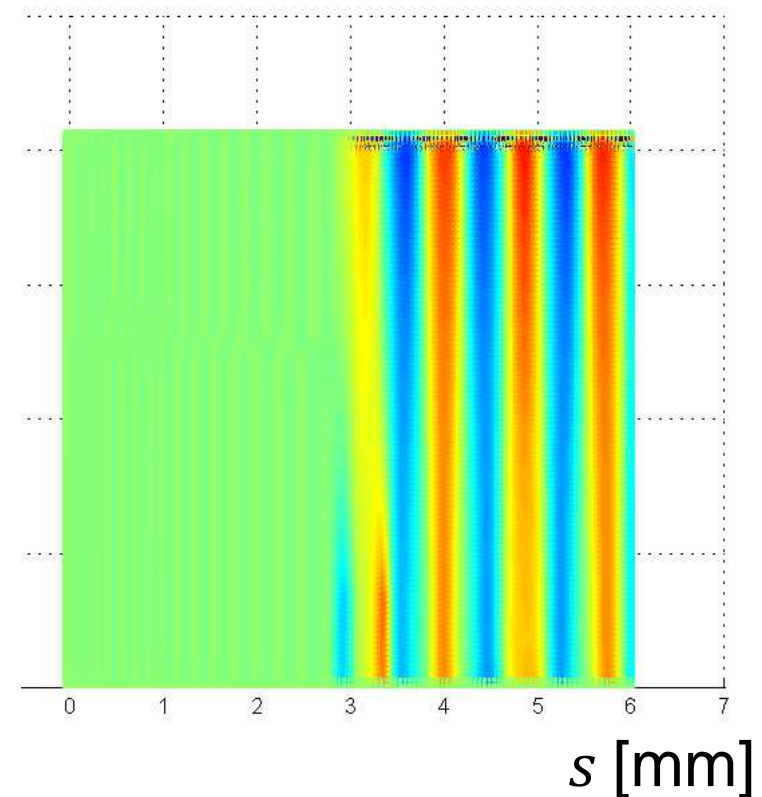
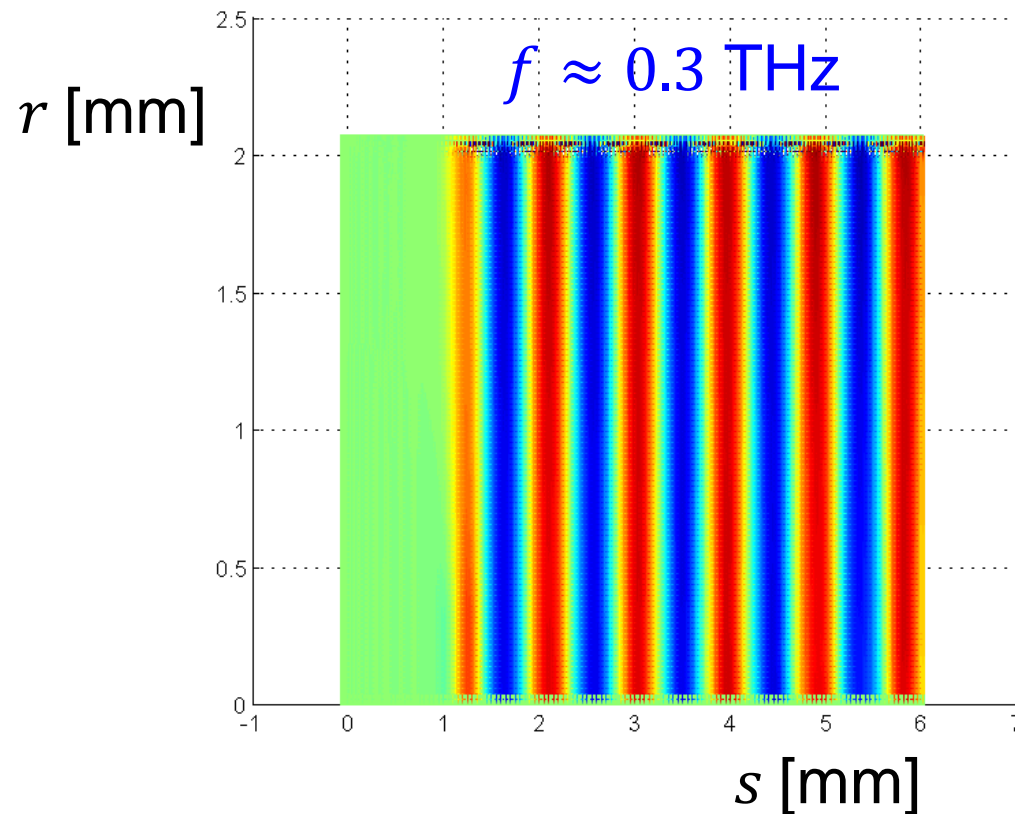


# Short bunch. Low charge. Low Energy

Longitudinal electric field component  $E_z$

$$E_0 = 10 \text{ MeV}$$

$$E_0 = 5 \text{ MeV}$$





# Middle bunch. Middle charge. Low Energy

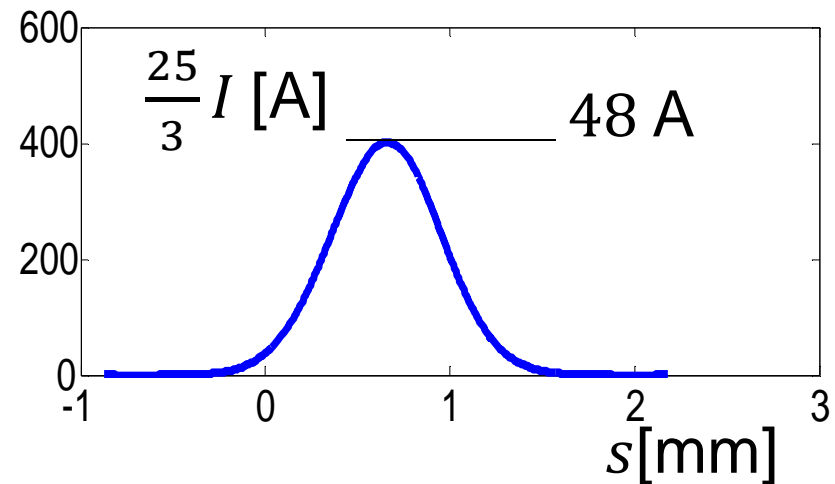
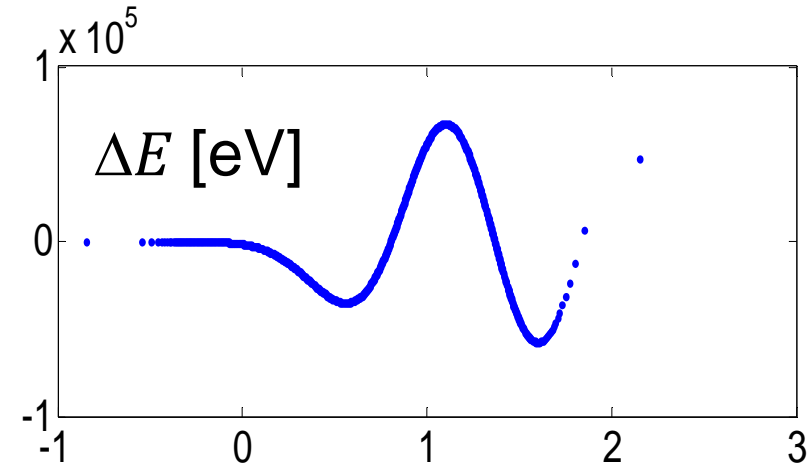
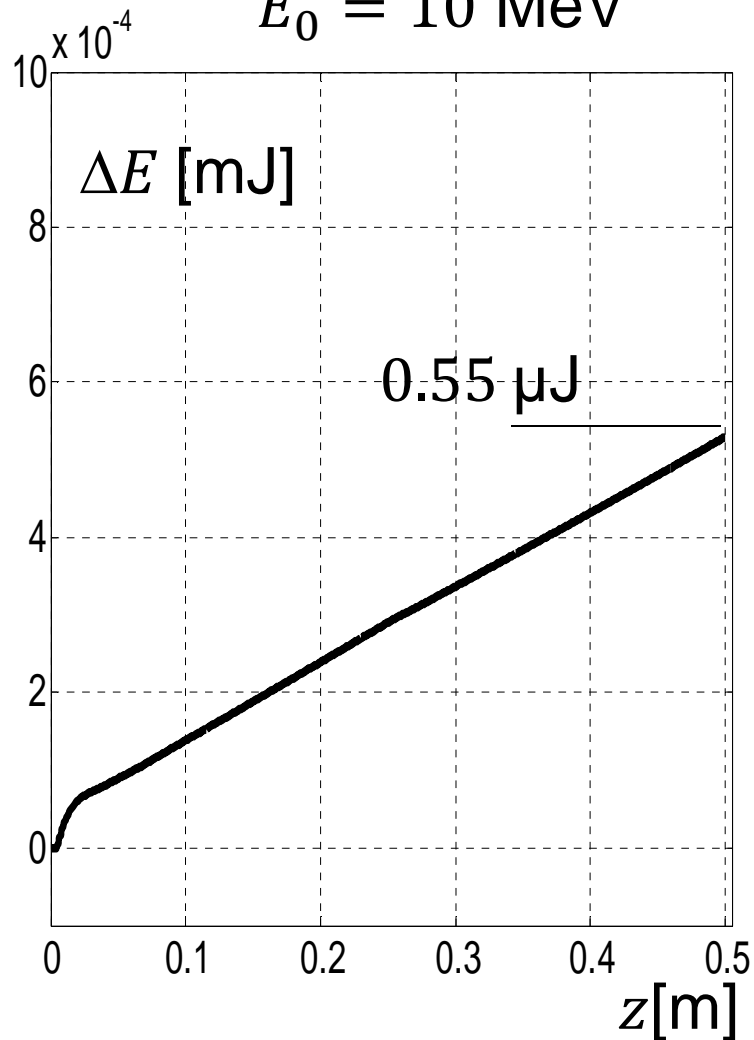
Pipe length $L$ , m	0.5
Bunch energy $E_0$ , MeV	10
Gaussian bunch rms $\sigma$ , mm	0.3
Charge $Q$ , nC	0.12



# Middle bunch. Middle charge. Low Energy

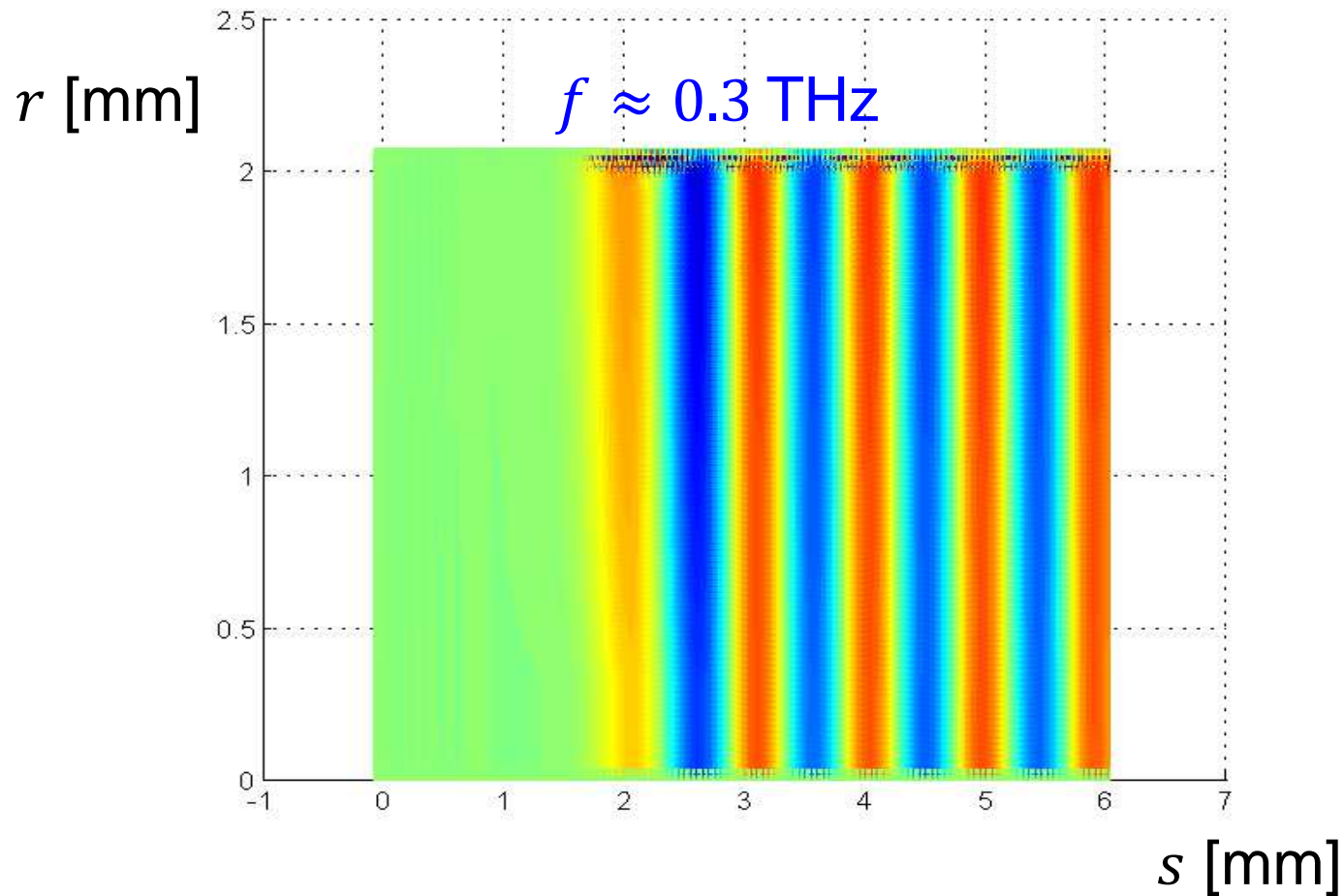
$$Q = 120 \text{ pC} \quad \sigma = 0.3 \text{ mm} \quad I_0 = 48 \text{ A}$$

$$E_0 = 10 \text{ MeV}$$

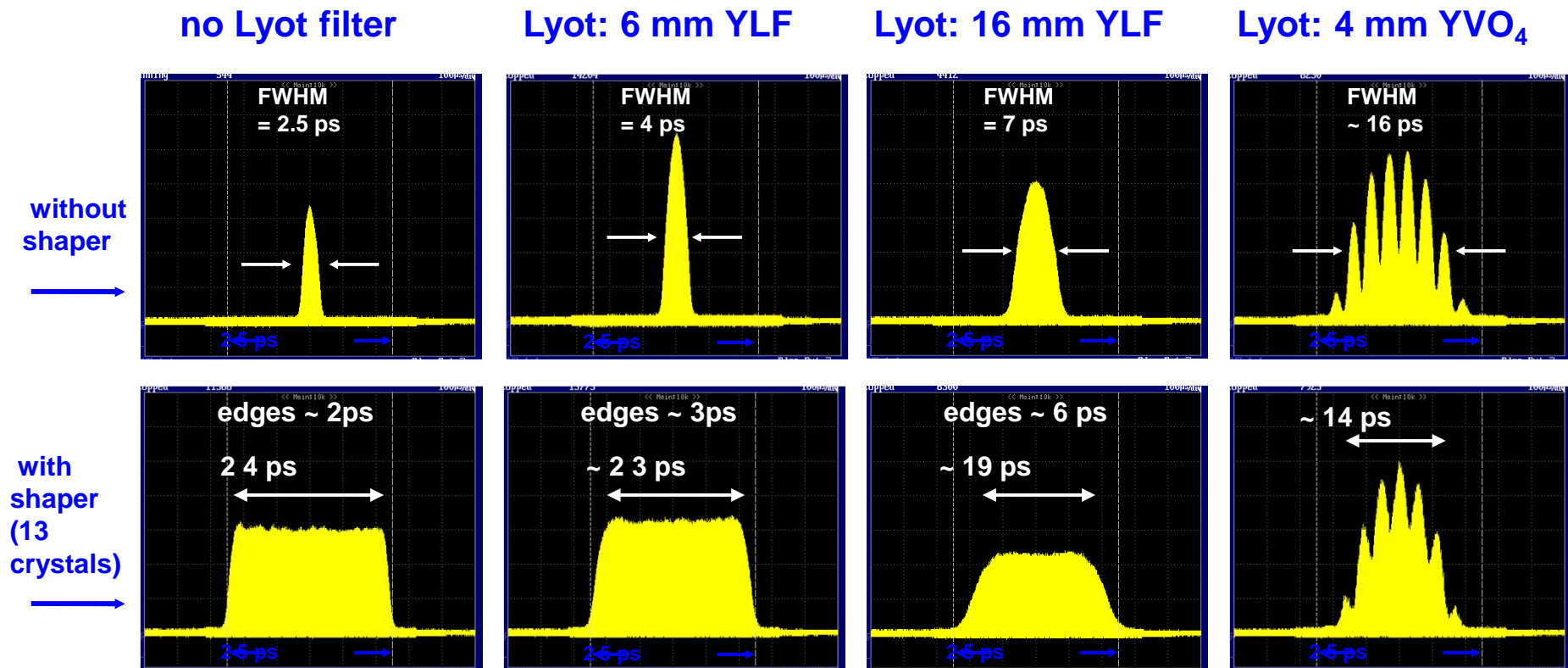


# Middle bunch. Middle charge. Low Energy

Longitudinal electric field component  $E_z$



# Premodulated bunch (from M. Krasilnikov)

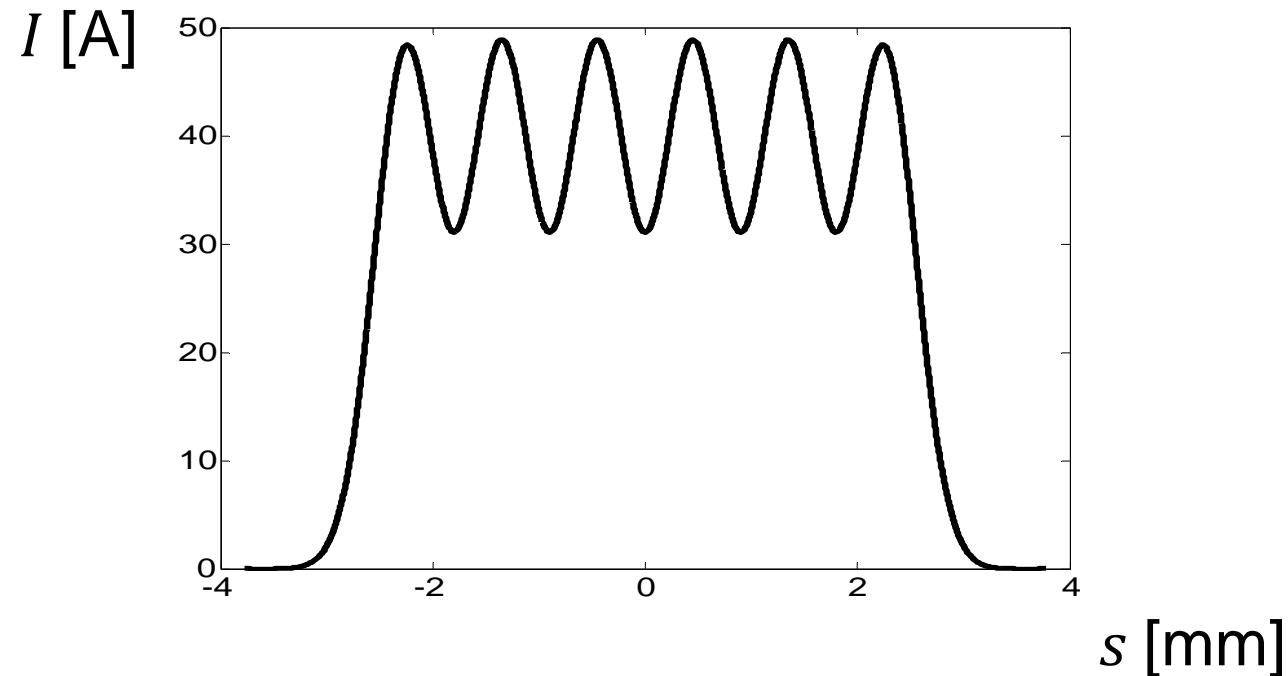


- Edges of the flat-top pulses are slightly shorter than FWHM of the Gaussian pulse (measured without shaper)
- **“Smoothing” of the Modulations** in the flat-top region of the pulse

I. Will, G. Klemz „Increasing the flexibility in pulse shape of a Yb:YAG photocathode laser” 20.06.2009

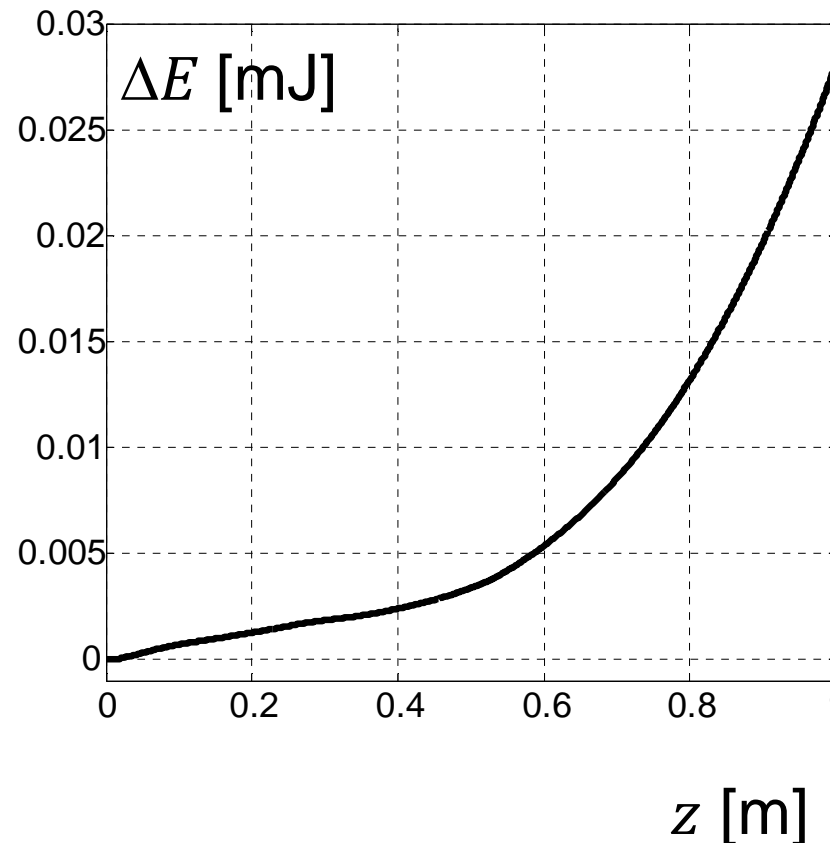
# Premodulated bunch. 6 microbunches

Pipe length $L$ , m	0.5
Bunch energy $E_0$ , MeV	5
Gaussian bunch rms $\sigma$ , mm	$0.3 \cdot 6$
Charge $Q$ , nC	$0.12 \cdot 6$

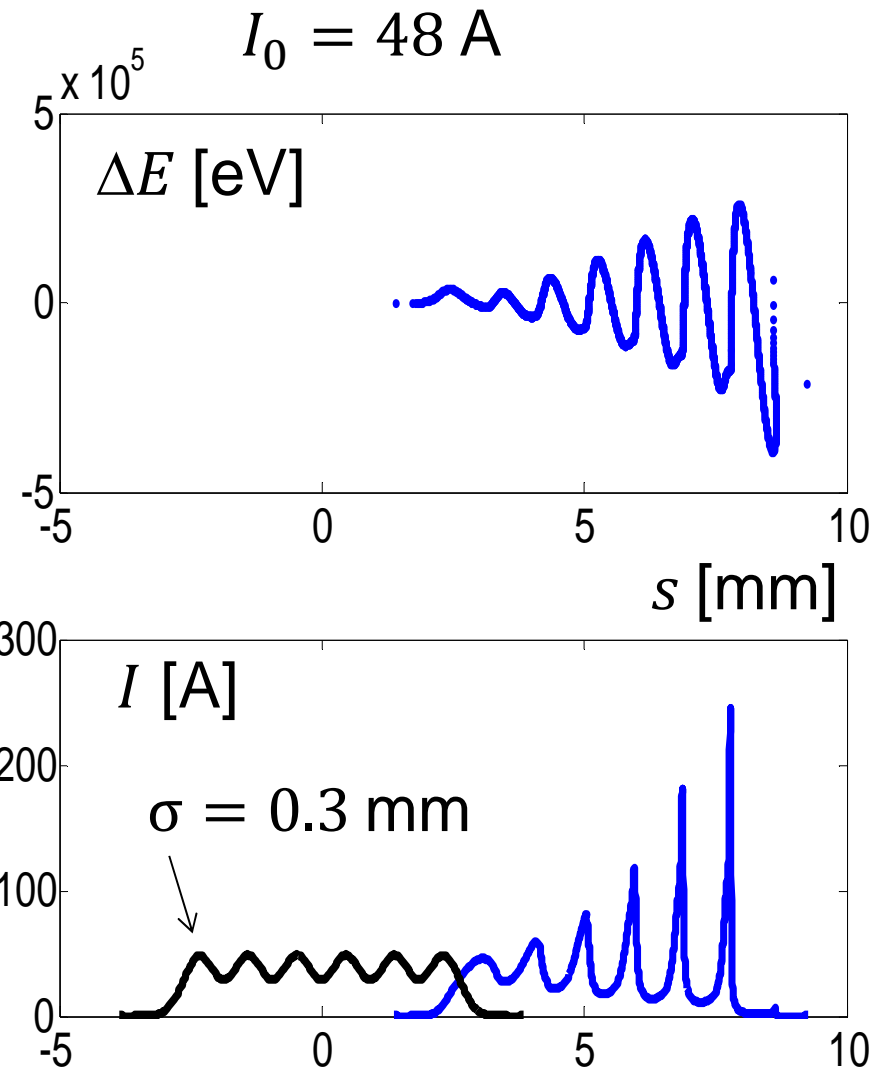


# Premodulated bunch. 6 microbunches

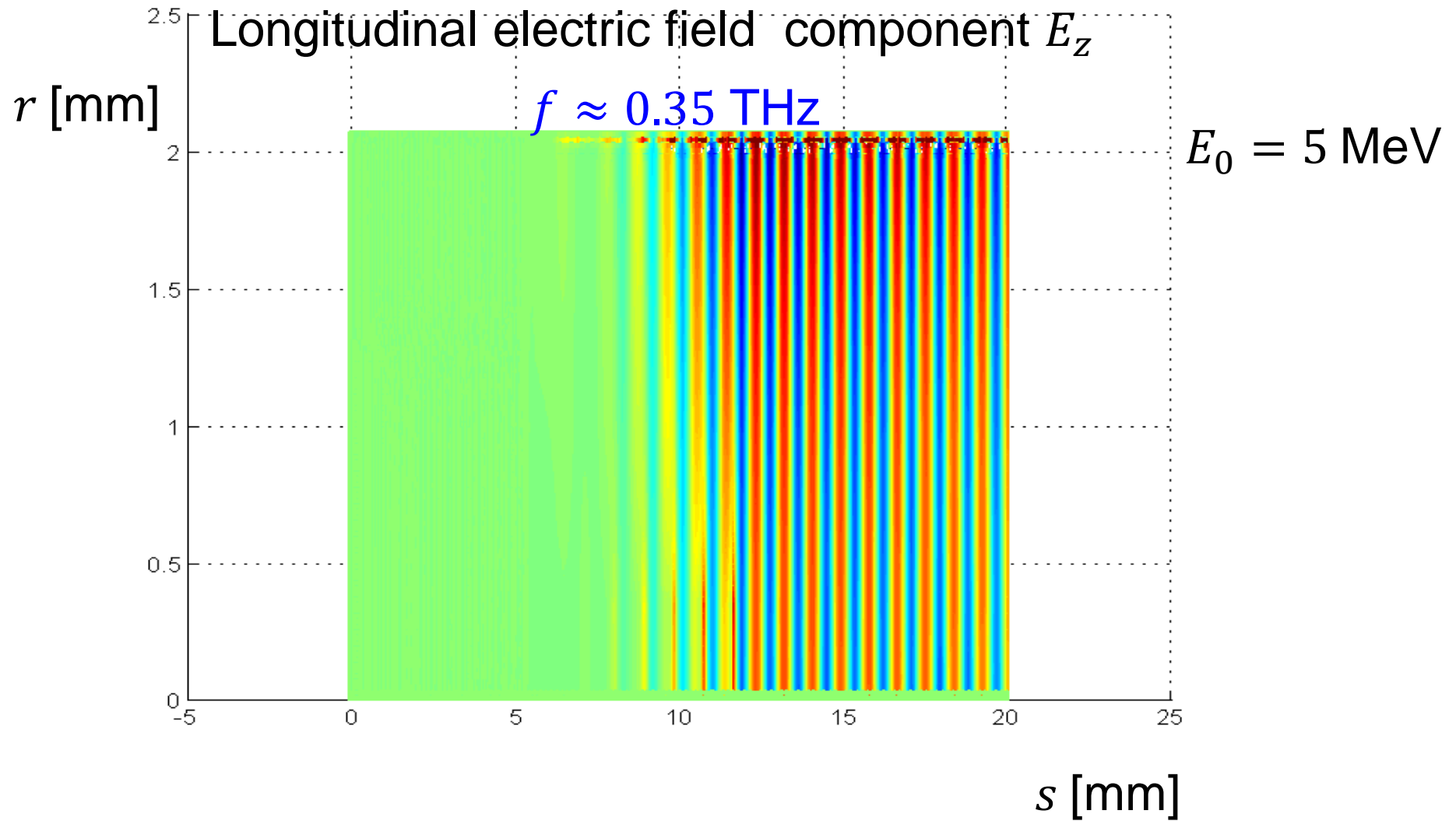
$$E_0 = 5 \text{ MeV}$$
$$Q = 6 * 120 \text{ pC}$$



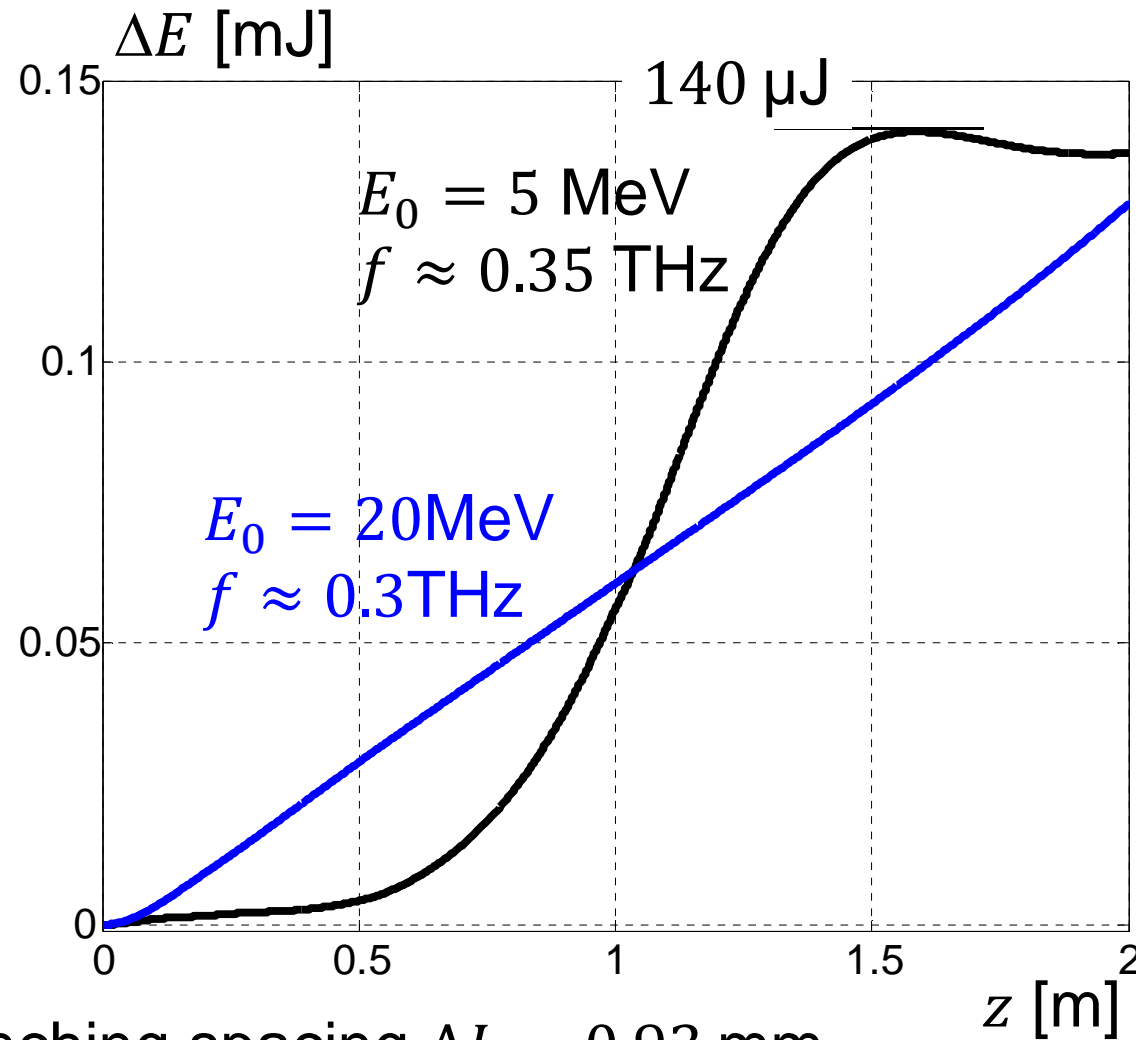
Microbunching spacing  $\Delta L = 0.93 \text{ mm}$



# Premodulated bunch. 6 microbunches



# Premodulated bunch. 8 microbunches



Microbunching spacing  $\Delta L = 0.93 \text{ mm}$

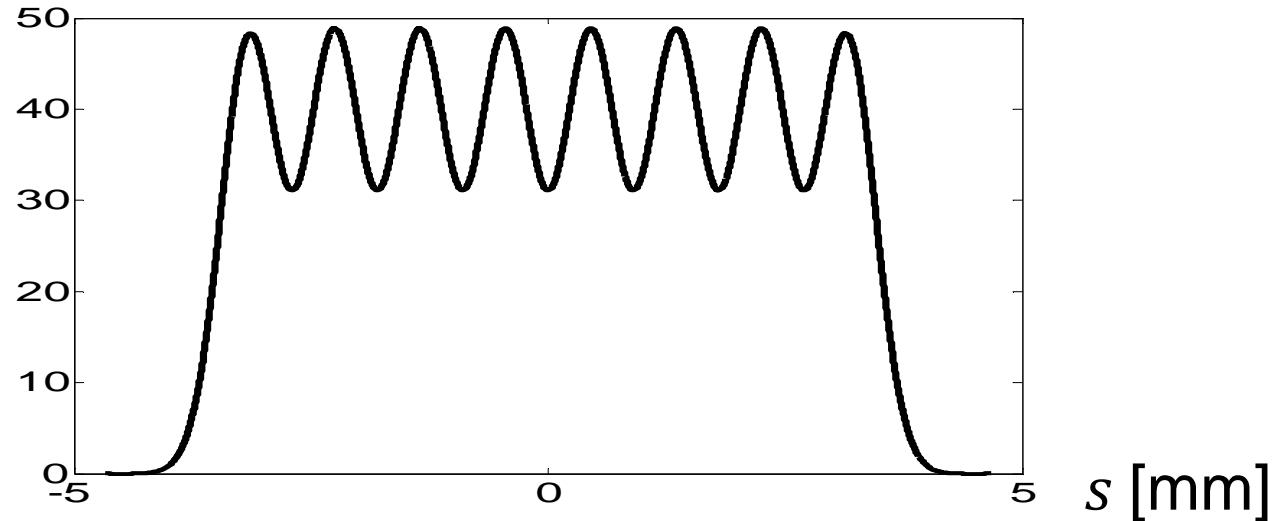




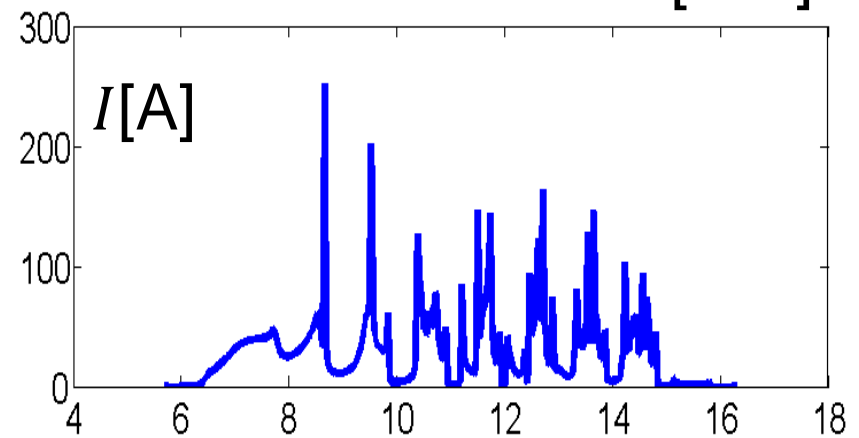
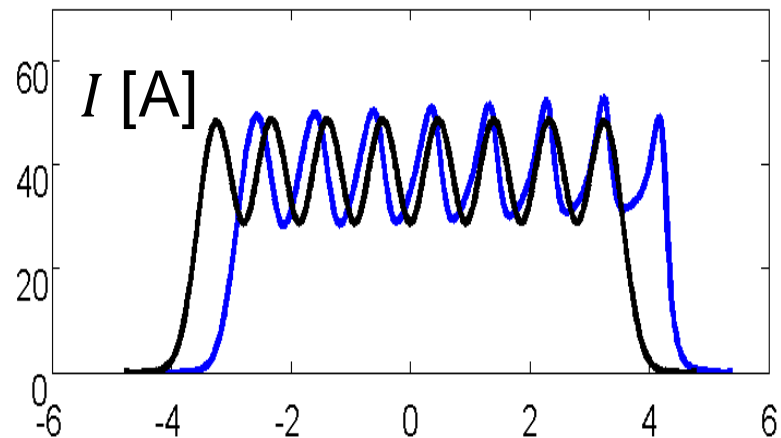
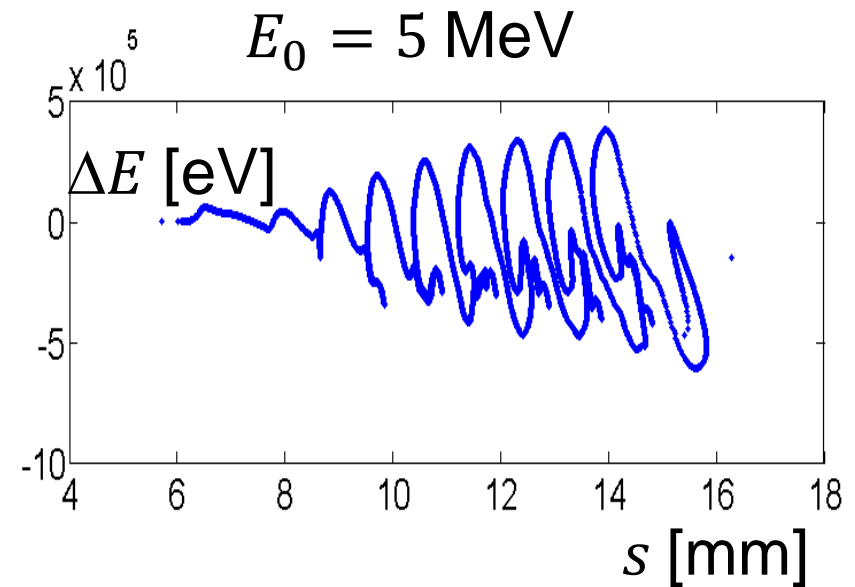
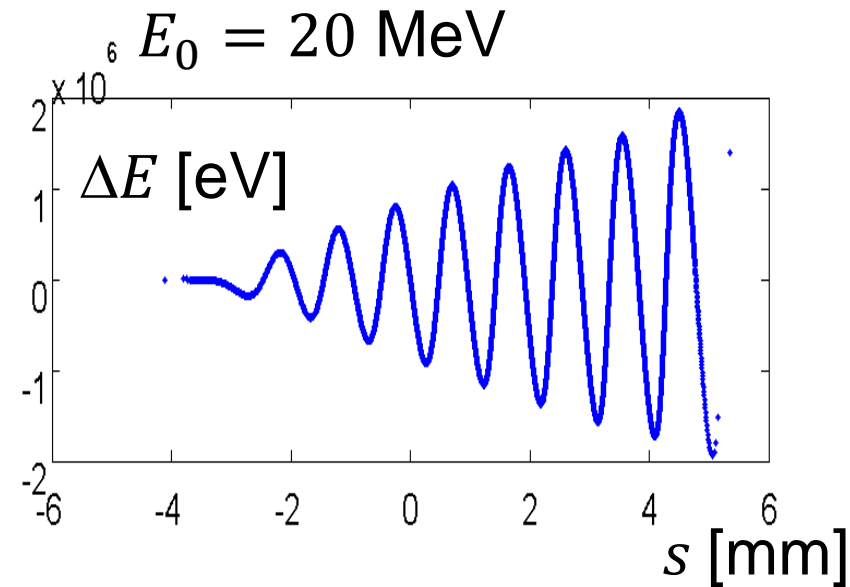
# Premodulated bunch. 8 microbunches

Pipe length $L$ , m	1.5-2
Bunch energy $E_0$ , MeV	5
Gaussian bunch rms $\sigma$ , mm	$0.3 \cdot 8$
Charge $Q$ , nC	$0.12 \cdot 8$

$I$  [A]

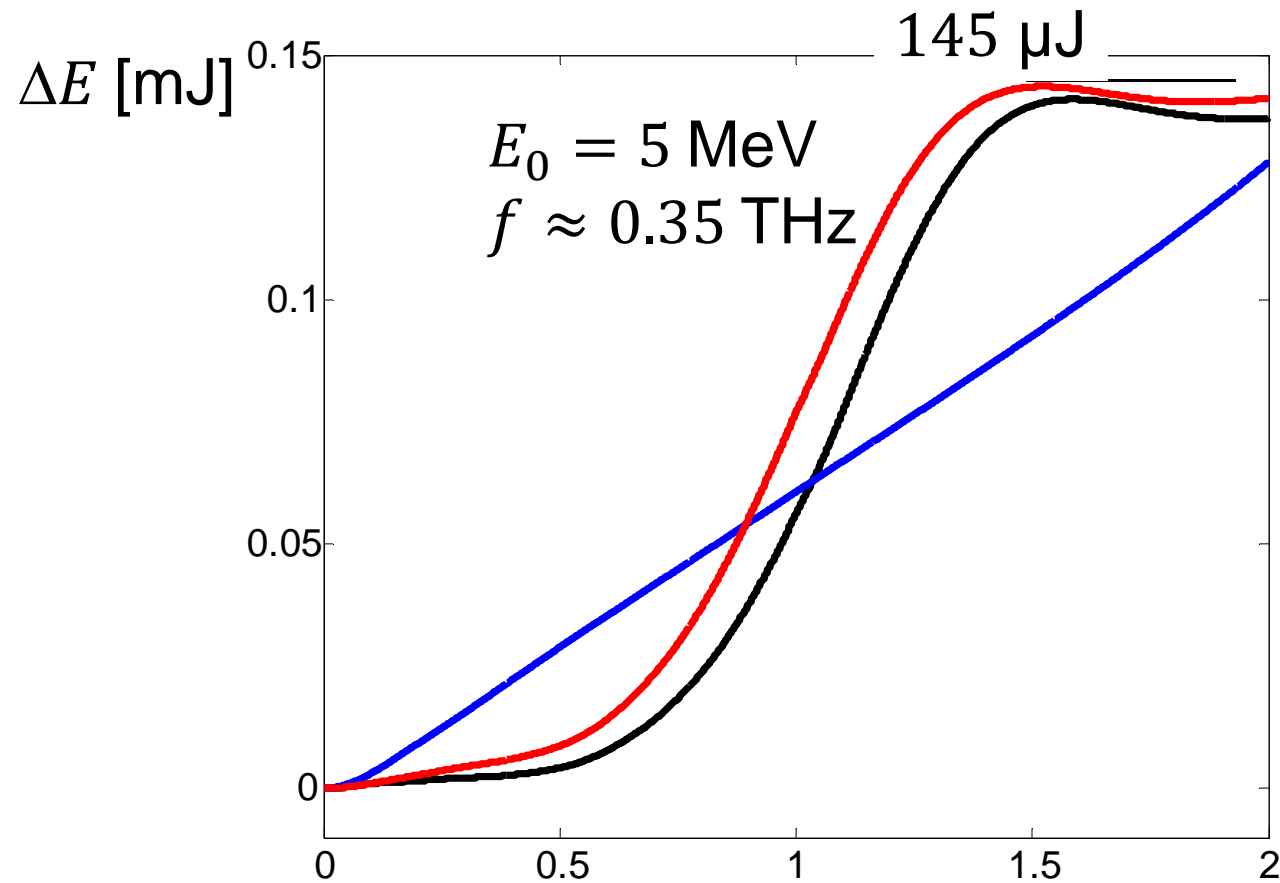


# Premodulated bunch. 8 microbunches



Microbunching spacing  $\Delta L = 0.93 \text{ mm}$

# Premodulated bunch. 8 microbunches



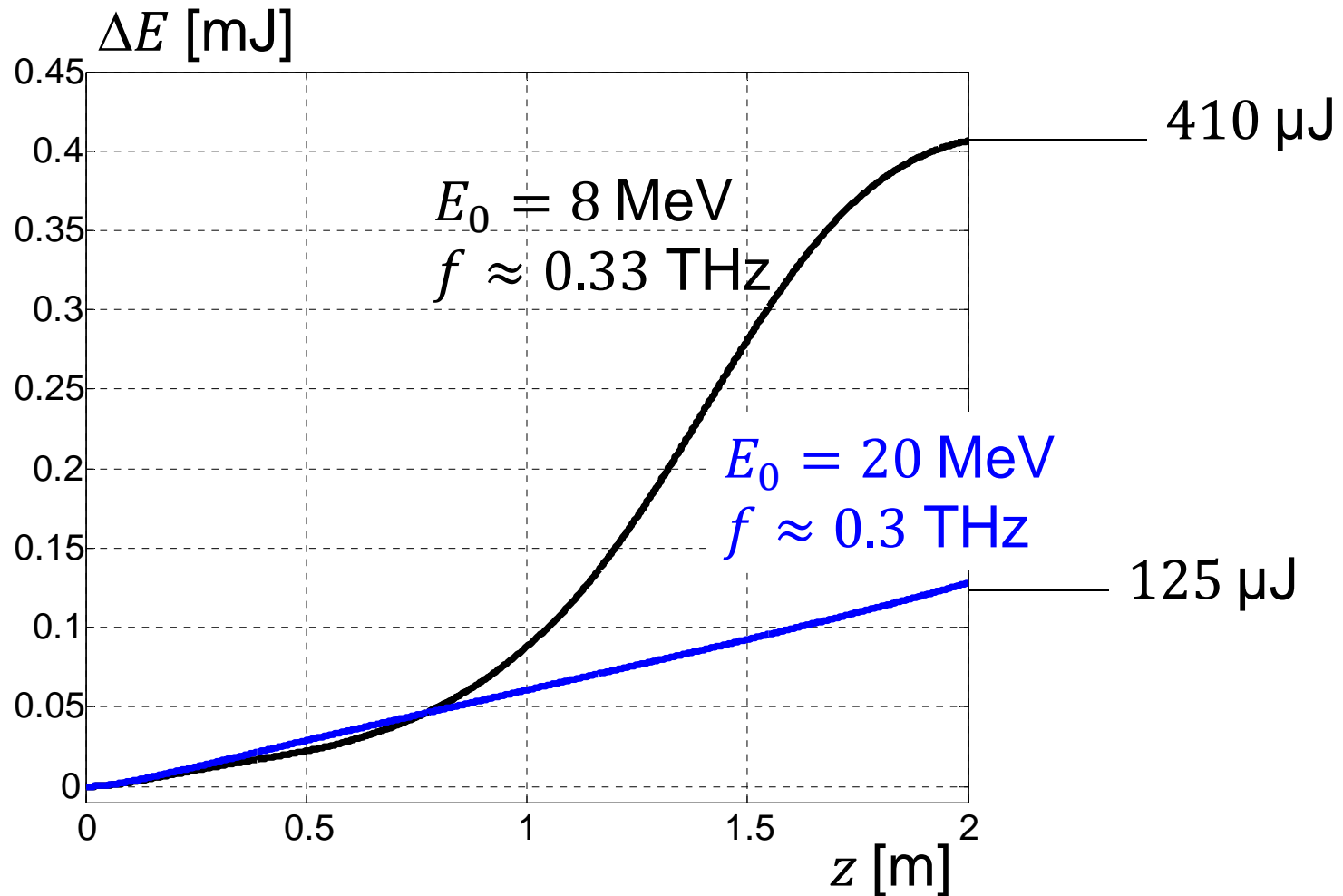
Microbunching spacing  $\Delta L = 0.88$ mm  $z$  [m]

# Premodulated bunch. 8 microbunches

Pipe length $L$ , m	2
Bunch energy $E_0$ , MeV	8
Gaussian bunch rms $\sigma$ , mm	$0.3 \cdot 8$
Charge $Q$ , nC	$0.12 \cdot 8$



# Premodulated bunch. 8 microbunches



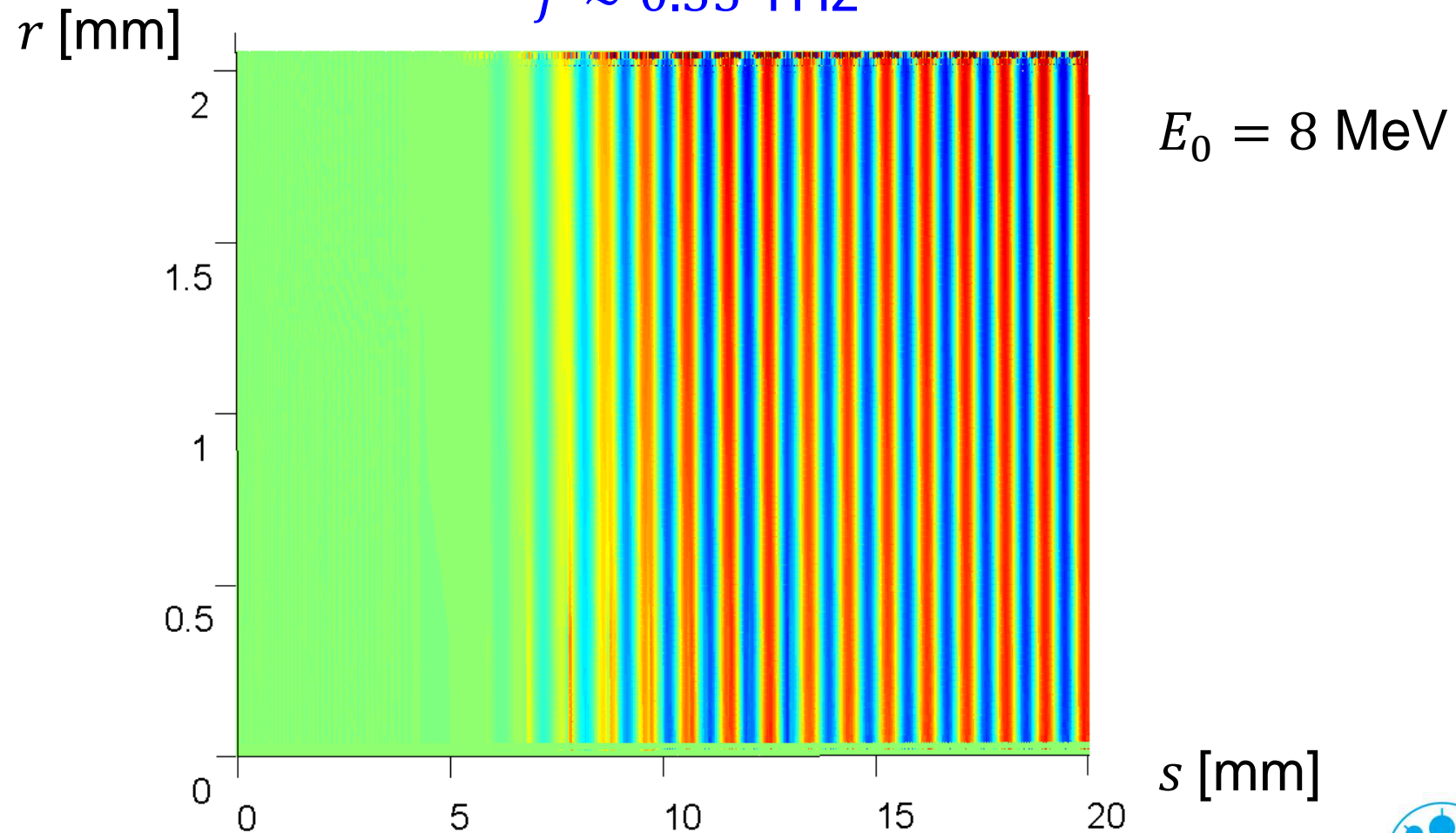
Microbunching spacing  $\Delta L = 0.93$  mm



# Premodulated bunch. 8 microbunches

Longitudinal electric field component  $E_z$

$$f \approx 0.33 \text{ THz}$$



# Summary

Charge, [pC]	Beam energy, [MeV]	RMS length, [mm]	Number of bunches	Pipe Length [m]	Field energy, [uJ]	Frequ-ency, [THz]
1000	14000	0.1	1	0.5	1400	0.3
1000	20	0.1	1	0.5	1300	0.3
40	10	0.1	1	0.5	2	0.3
120	10	0.3	1	0.5	0.55	0.3
120*8	20	0.3	8	1.5	85	0.3
120*8	5	0.3	8	1.5	140	0.35
120*8	8	0.3	8	2	410	0.33



# Summary

To consider:

- transverse dynamics,
- tapering, resonance condition,
- resistivity (already implemented in code),
- rectangular pipe (wakefield code available),
- start from shot noise,
- start with short driving bunch,
- optimal prebunching, optimal energy.

