



Short-Range Wakes in Elliptical Pipe Geometry

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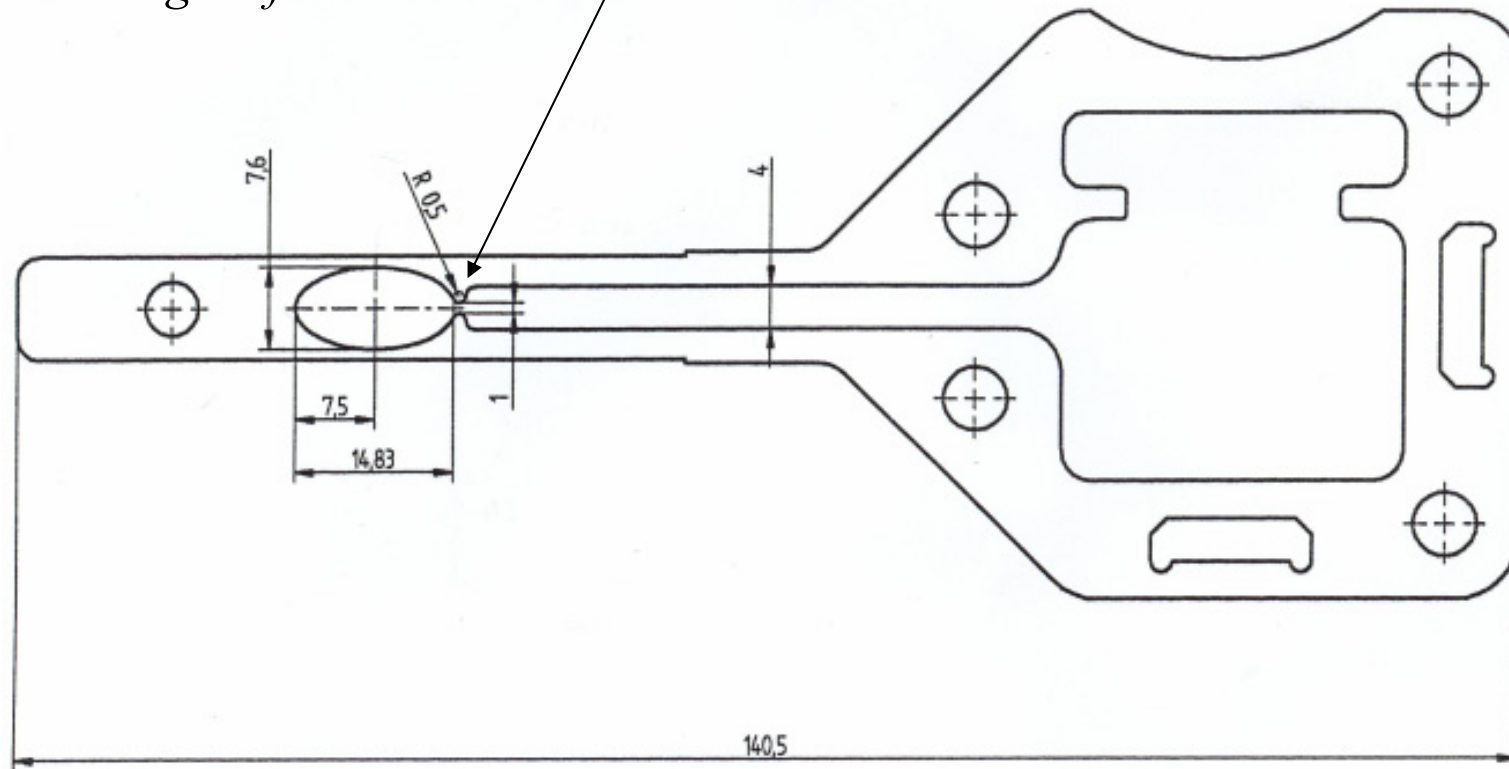
Beam Dynamics Group Meeting

05.09.05

Pumping slot

$w = 1\text{ mm}$ – width of the slot

$L = 5\text{ m}$ – length of the slot

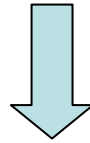


$$w ? \quad \sigma = 25\mu\text{m}$$

Theoretical results (Bethe theory) only for $w \leq \sigma$.

Pumping slot

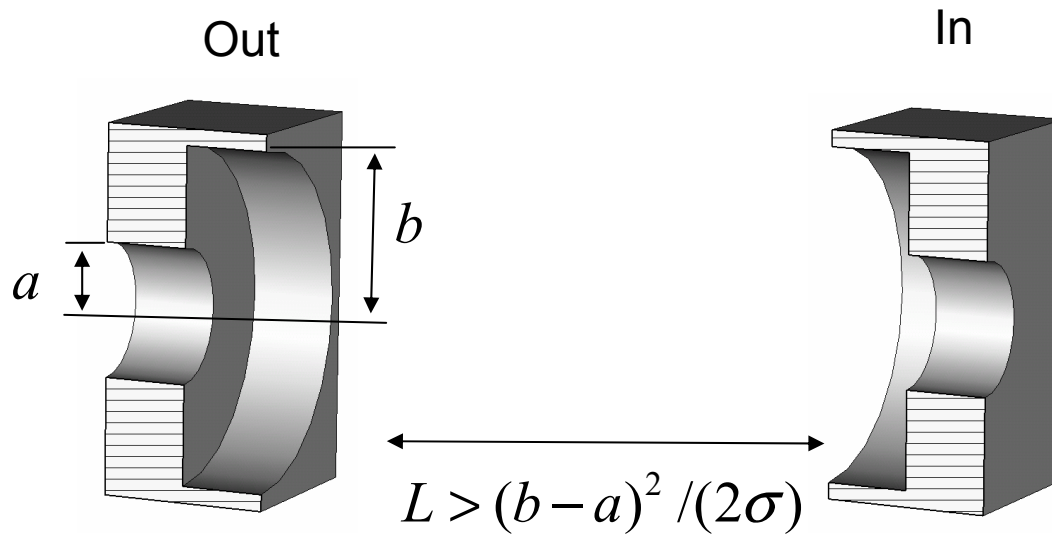
Effect of the slot is small.



- Accuracy estimation of the numerical results.
- Wake scaling for geometry parameters.

Used tools:

ECHO (time-domain),
CST Microwave Studio (modeling, meshing),
Matlab (pre- and postprocessing).



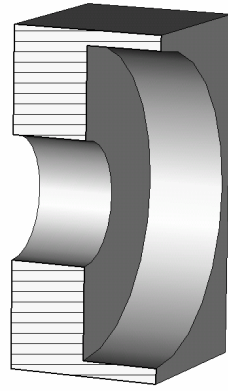
$$Z_{hi} = \frac{Z_0}{\pi} \ln\left(\frac{b}{a}\right) \quad k_{loss} = \frac{Z_{hi}c}{2\sqrt{\pi}\sigma_z} \quad k_{loss} = O(\sigma^{-1} \ln(b/a))$$

$$\sigma = 250 \mu m \quad k_{loss} = 37.2 [V / pC]$$

$$\sigma = 25 \mu m \quad k_{loss} = 372 [V / pC]$$

$$W = W^{in} + W^{out}$$

Accuracy of 3D calculations

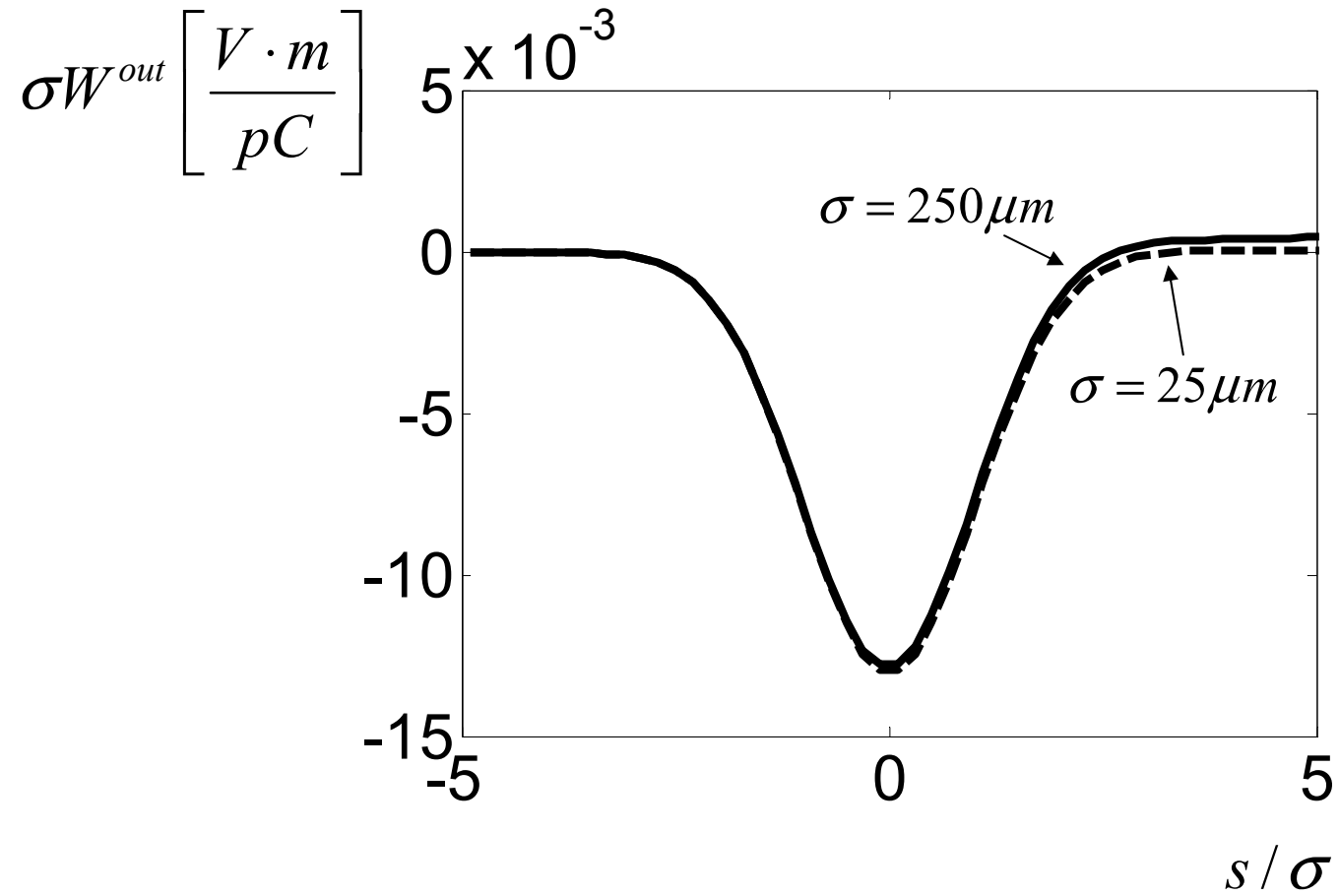


$$k_{loss}^{out}$$

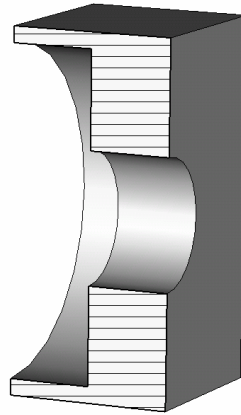
σ [μm]	dx [σ]	dy,dz [σ]	Loss,2D [V/pC]	Error, 2D [V/pC]	Loss, 3D [V/pC]	Error, 3D [V/pC]
250	1/40	1/40	36.3097	ref.		
250	1/20	1/20	36.2932	0.016		
250	1/5	1/5	36.2369	0.07	36.2265	0.1
25	1/20	1/20	370.77	ref.		
25	1/10	1/10	370.60	0.17		
25	1/5	1/5	369.96	0.8		
25	1/5	2			369.78	1

$$k_{loss}^{out} = O(\sigma^{-1} \ln(b/a))$$

$$W^{out} = O(\sigma^{-1})$$



Accuracy of 3D calculations



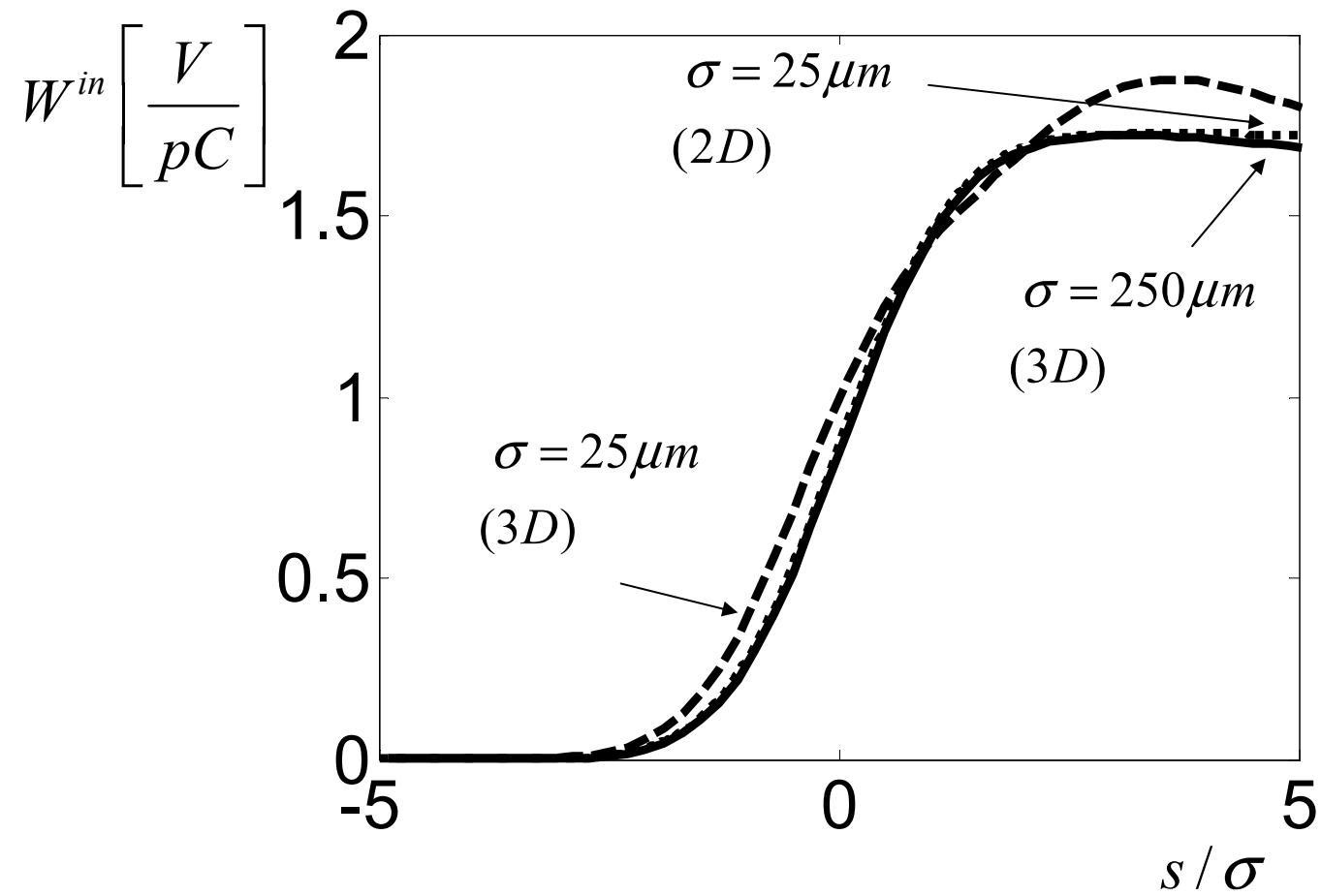
$$k_{loss}^{in}$$

σ [μm]	dx [σ]	dy,dz [σ]	Loss,2D [V/pC]	Error, 2D [V/pC]	Loss, 3D [V/pC]	Error, 3D [V/pC]
250	1/40	1/40	-0.8606	ref.		
250	1/10	1/10	-0.8678	0.001		
250	1/5	1/5	-0.8802	0.012	-0.8478	0.013
25	1/20	1/20	0.8639	ref.		
25	1/10	1/10	-0.8619	0.002		
25	1/5	1/5	-0.8859	0.02		
25	1/5	2			-0.9380	0.17

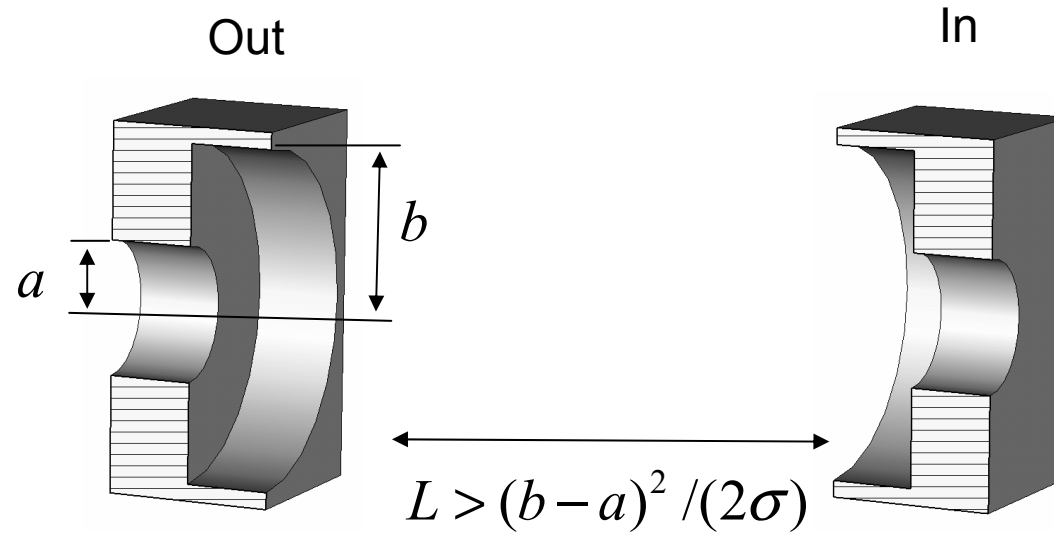
$$k_{loss}^{in} = O(a^{-1})$$

$$k_{loss}^{in} = k_{loss}^{out}$$

$$W^{in} = O(1), \quad \sigma \rightarrow 0$$



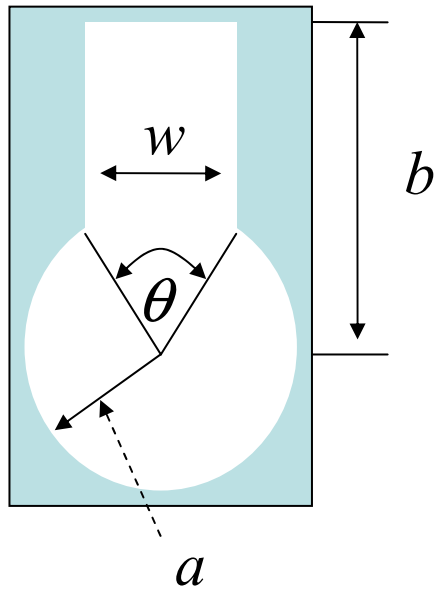
Scaling laws



$$k_{loss}^{out} = O\left(\sigma^{-1} \ln\left(\frac{b}{a}\right)\right)$$

$$k_{loss}^{in} = O\left(\frac{1}{a}\right)$$

Scaling laws ($w > \sigma$)

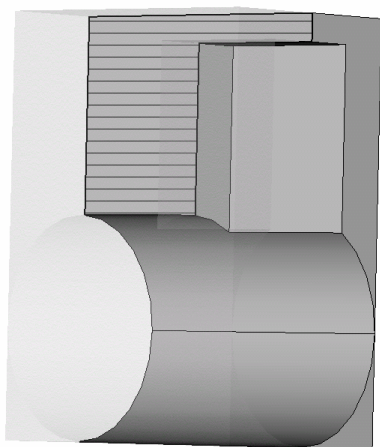


$$k_{loss}^{out} = O\left(\sigma^{-1} \theta^\alpha \ln\left(\frac{b}{a}\right)\right)$$

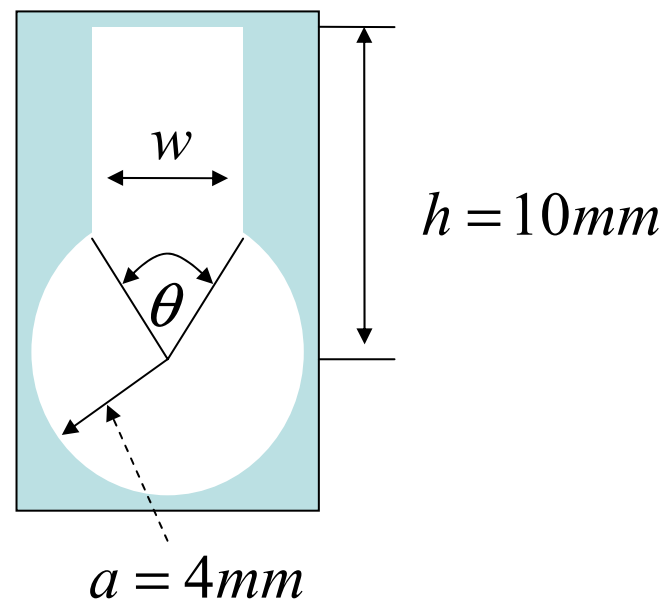
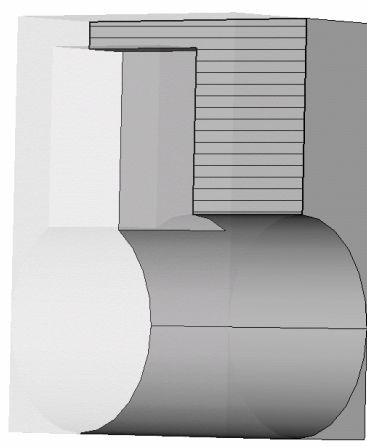
$$k_{loss}^{in} = O\left(\frac{\theta^\beta}{a}\right)$$

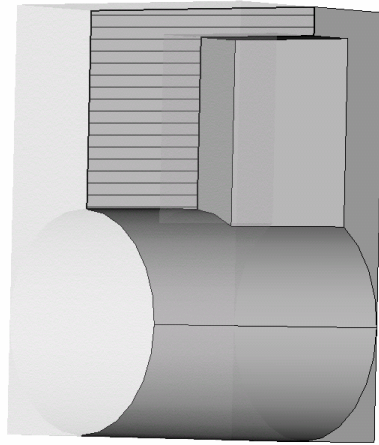
$\alpha, \beta?$

Out

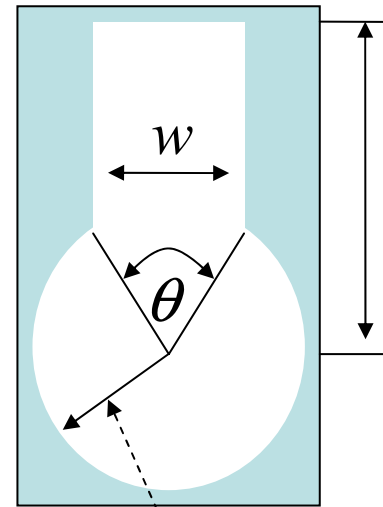


In





k_{loss}^{out}



$h = 10mm$

$w > \sigma$

$a = 4mm$

w [mm]	$\theta/(2\pi)$	σ [μm]	Loss [V/pC]
7	0.339	250	3.04+-0.1
4	0.167	250	0.91+-0.1
2	0.083	250	0.23+-0.1
7	0.339	25	31.8+-1
4	0.167	25	
2	0.083	25	2.8+-1

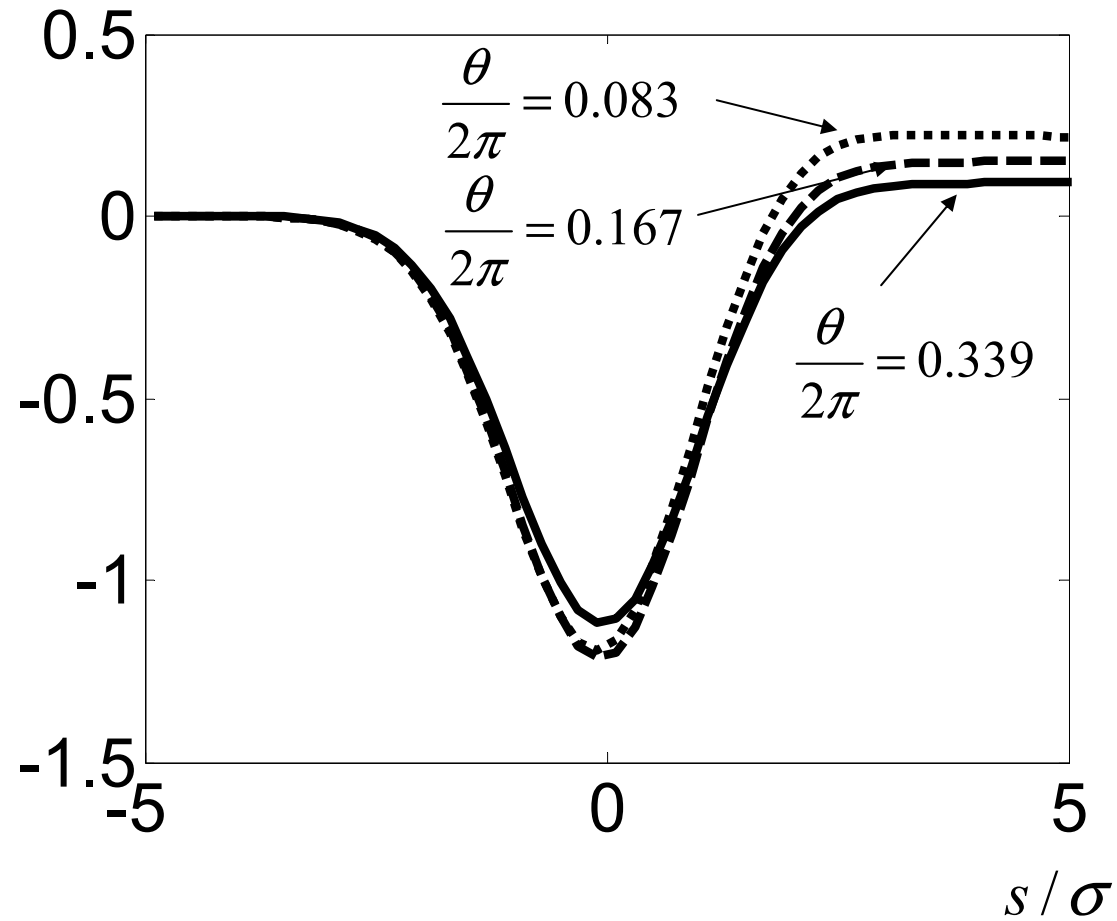
$$k_{loss}^{out} = O(\sigma^{-1})$$

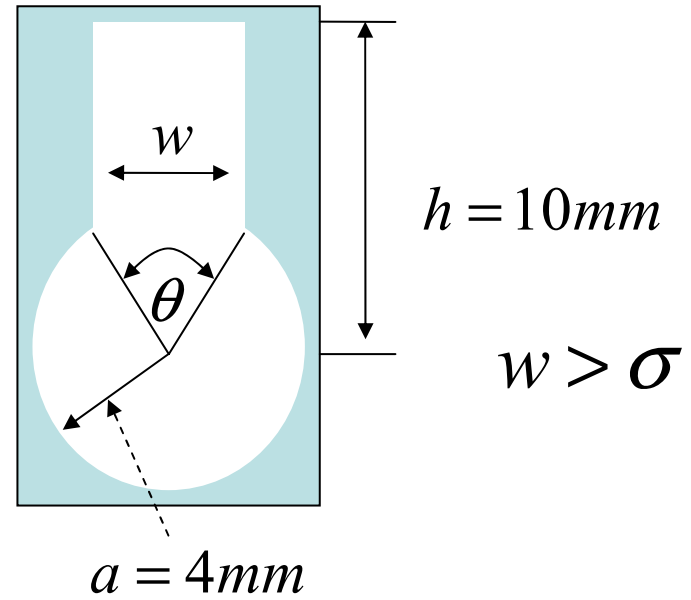
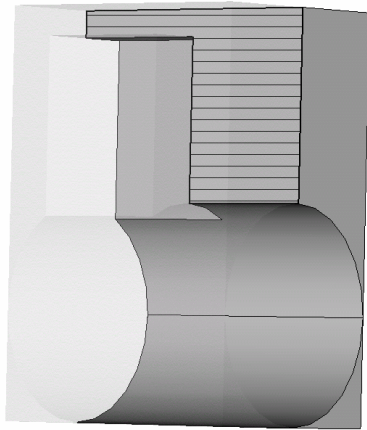
$$k_{loss}^{out} = O(\theta^{1.8}) \quad ?!$$

$$\sigma = 250 \mu\text{m}$$

$$W^{out} = O(\theta^{1.8}), \quad \theta \rightarrow 0, \quad w > \sigma$$

$$\frac{W^{out}}{\theta^{1.8}} \left[\frac{V}{\text{pC} \cdot \text{rad}^{1.8}} \right]$$





k_{loss}^{in}

w [mm]	$\theta/(2\pi)$	σ [μm]	Loss [V/pC]
7	0.339	250	-0.162+-0.013
4	0.167	250	-0.065+-0.013
2	0.083	250	-0.01+-0.013
7	0.339	25	-0.247+-0.17
4	0.167	25	
2	0.083	25	

$$k_{loss}^{in} = O(1), \quad \sigma \rightarrow 0$$

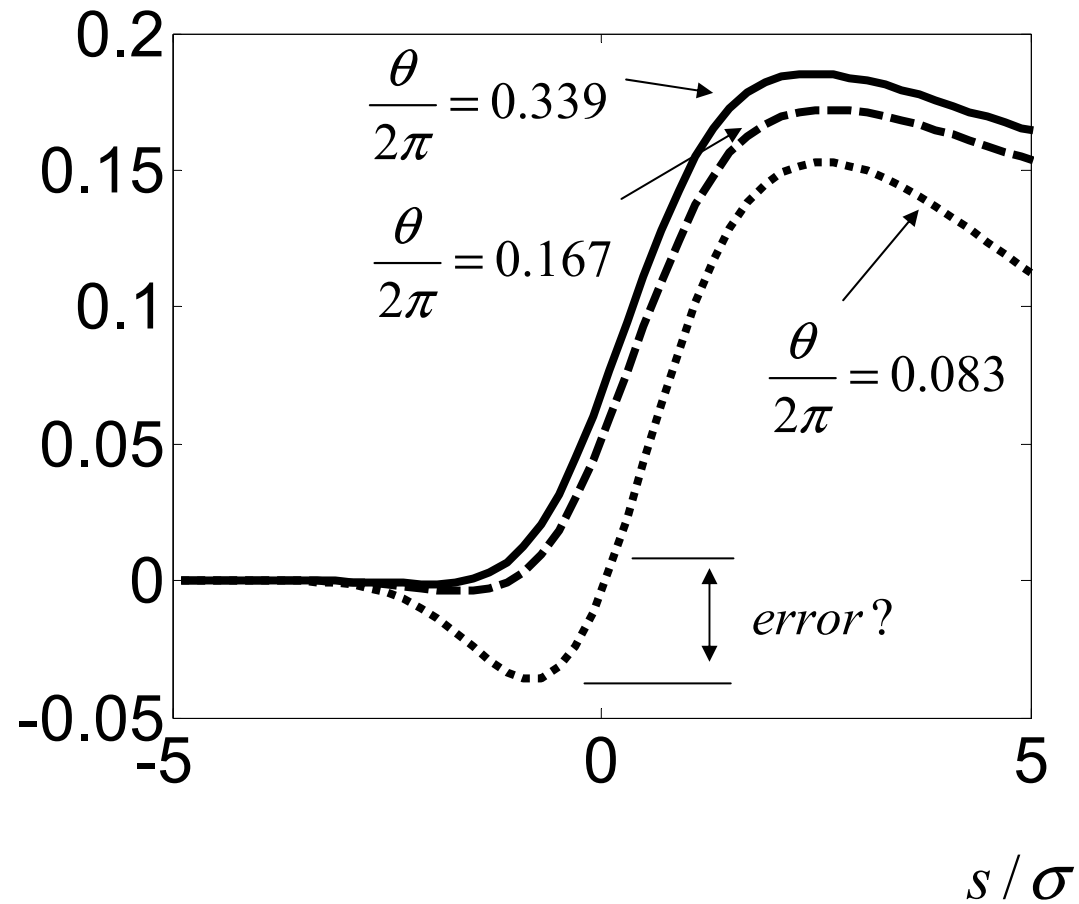
$$k_{loss}^{in} = k_{loss}^{out}$$

$$k_{loss}^{in} = O(\theta) \quad ?!$$

$$\sigma = 250 \mu m$$

$$W^{in} = O(\theta), \quad \theta \rightarrow 0, \quad w > \sigma$$

$$\frac{W^{in}}{\theta} \left[\frac{V}{pC \cdot rad} \right]$$



Scaling laws and extrapolation

$$w > \sigma$$

$$k_{loss}^{out} = O\left(\sigma^{-1} \theta^{1.8} \ln\left(\frac{b}{a}\right)\right)$$

$$k_{loss}^{in} = O\left(\frac{\theta}{a}\right)$$

w [mm]	b, [mm]	a, [mm]	$\theta/(2\pi)$	σ [μm]	Loss [V/pC]
7	10	4	0.339	250	3
1	20	7.5	0.021	25	0.2

w [mm]	a, [mm]	$\theta/(2\pi)$	σ [μm]	Loss [V/pC]
7	4	0.339	250	-0.16
1	7.5	0.021	25	-0.005

$$k_{loss}^{out} = 3 \cdot 10 \left(\frac{0.021}{0.339}\right)^{1.8} \frac{\ln\left(\frac{20}{7.5}\right)}{\ln\left(\frac{10}{4}\right)} = 0.2 \left[\frac{V}{pC}\right]$$

$$k_{loss}^{in} = -0.16 \cdot \left(\frac{0.021 \cdot 4}{0.339 \cdot 7.5}\right) = -0.005 \left[\frac{V}{pC}\right]$$

$$k_{loss} = 0.2 \left[\frac{V}{pC}\right]$$

$$w > \sigma$$

$$k_{loss}^{in} = k_{loss}^{out}$$



Energy method

$$W = W^{in} + W^{out} \quad W^{out} - W^{in} = 2W^e$$

$$W = 2W^{in} + 2W^e \approx 2W^e, \quad \text{if } W^{in} \approx 0$$

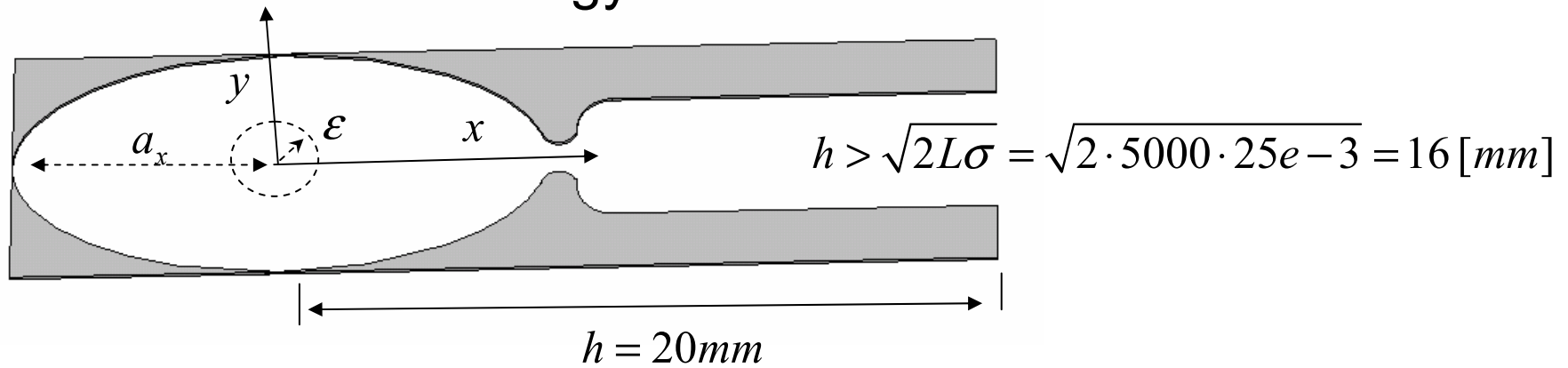
$$W^e = \lambda_z (\bar{w}_{ellipse} - \bar{w}_{ellipse+slot}) = \lambda_z \bar{w}$$

(K. Zotter et al. , Impedances and Wakes ..., 1998
and
K.L.F.Bane, I.A.Zagorodnov, SLAC-PUB-11388, 2005)

Accuracy of the energy method

w [mm]	σ [μm]	K_loss from time-domain [V/pC]	K_loss from energy [V/pC]	Error, [V/pC]
7	250	2.88	3.10	0.22
7	25	31.5	31.0	0.5
2	250	0.22	0.26	0.04
2	25	2.75	2.63	0.12

Energy method



ϵ [mm]	Mesh step in [σ]	Ellipse	Ellipse with slot	$\frac{2\pi}{Z_0 c} \bar{w}$
0.25	2	2.89161337	2.89165659	4.32e-5
0.25	1	2.90553777	2.90560728	6.95e-5

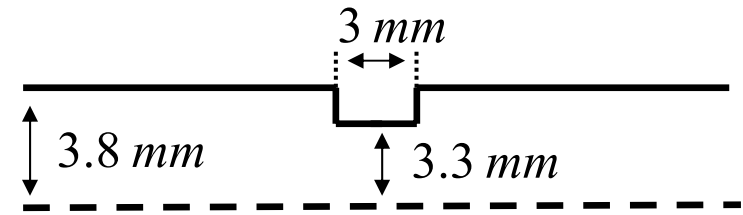
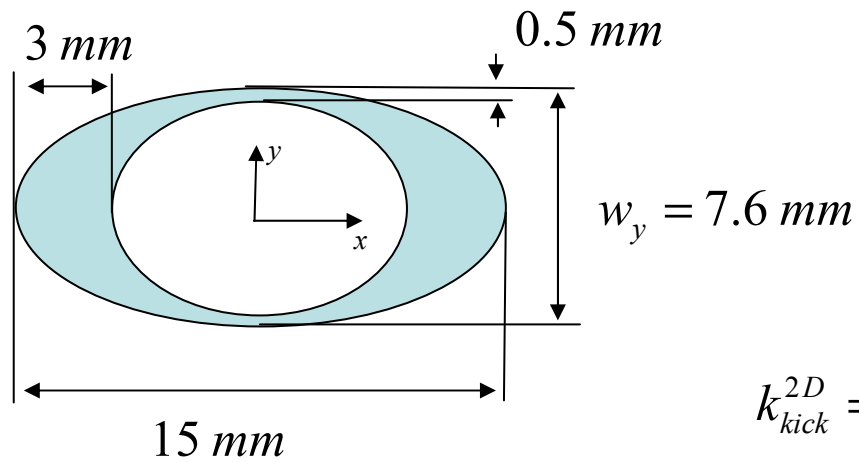
$$k_{loss} = 0.03 \pm 0.12 \text{ [V / pC]}$$

$$W_y(s, x=0, y=0) \approx \int_{-\infty}^s \frac{W(\bar{s}, x=0, y=0)}{a_x} d\bar{s}$$



$$k_{loss} < 0.2 \text{ [V / pC]}$$

$$k_{kick,x} < 0.001 \text{ [V / pC]}$$



Round (a=3.8, b=3.3)

$$k_{kick}^{2D} = 351 [V / (pC \cdot m)]$$

$$k_{kick}^{3D} = 359 [V / (pC \cdot m)] \quad \text{Error : 2\%}$$

Energy method

$$k_{loss} = 85 [V / pC]$$

Direct time-domain with ECHO

$$k_{loss} = 84 + 248x_s - 257y_s [V / pC]$$

$$k_{kick,x} = 390x_s + 46x_w = 436x [V / pC]$$

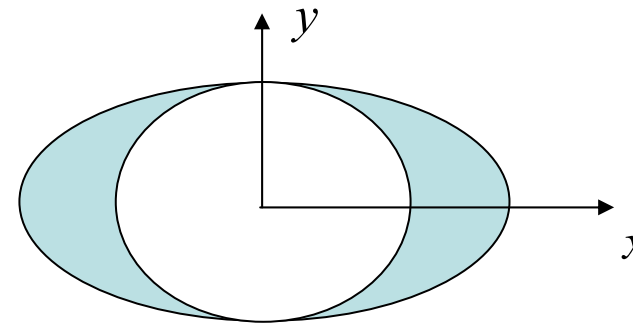
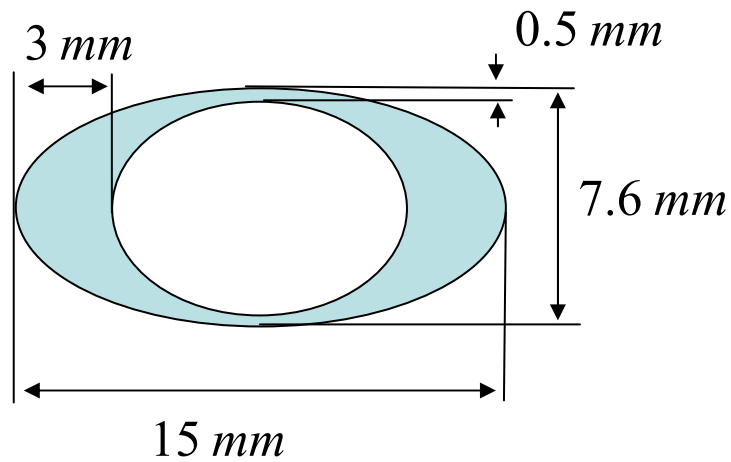
$$k_{kick,y} = 348y_s - 47y_w = 301y [V / pC]$$

Old pipe?

$$w_y = 7.8 \text{ mm} \quad k_{loss} = 85 [V / pC]$$

$$w_y = 9 \text{ mm} \quad k_{loss} = 91 [V / pC]$$

The energy loss for the new smaller pipe is a little smaller!



$$k_{loss} = 84 + 250x_s - 250y_s [V / pC]$$

$$k_{loss} = 42 + 1200x_s - 1200y_s [V / pC]$$

$$k_{kick,x} = 390x_s + 46x_w = 436x [V / pC]$$

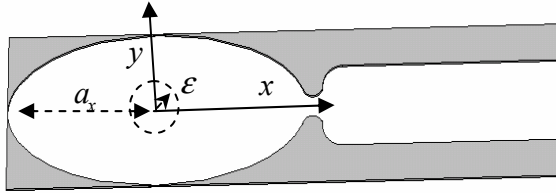
$$k_{kick,x} = 280x_s + 206x_w = 486x [V / pC]$$

$$k_{kick,y} = 348y_s - 47y_w = 301y [V / pC]$$

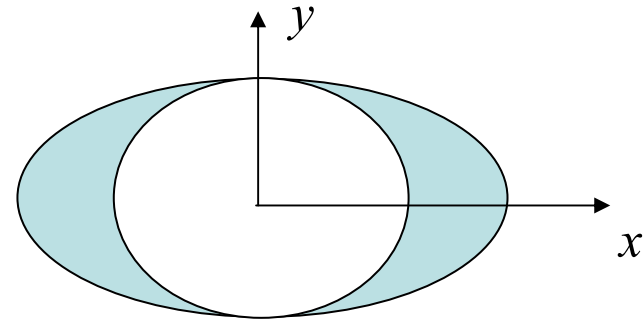
$$k_{kick,y} = 78y_s - 208y_w = -130y [V / pC]$$

	Loss, V/pC	Spread, V/pC	Peak, V/pC
var1	84	33	-118
var2	42	16	-58

Kick



$$k_{kick,x}^{slot} < 0.001 [V / pC]$$



$$k_{kick,x} = 486x [V / pC]$$

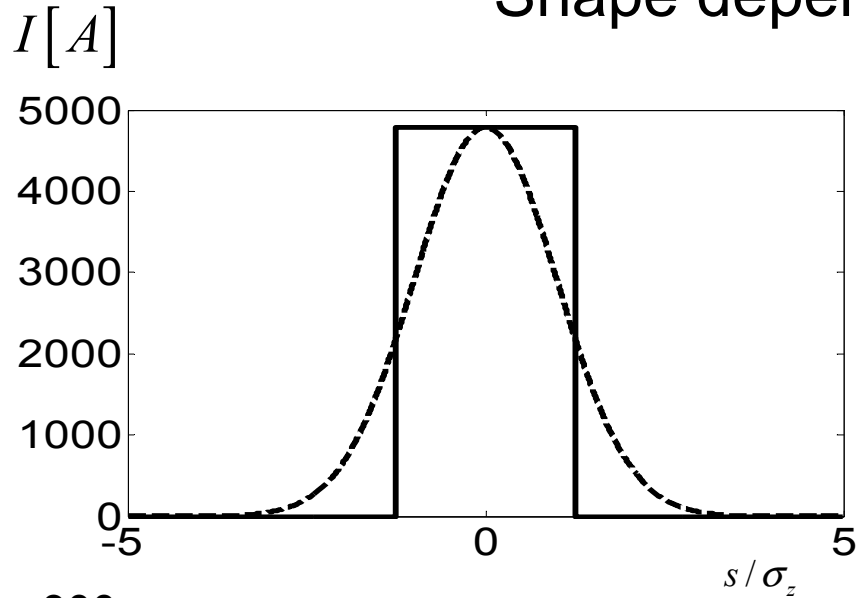
$$k_{kick,y} = -130y [V / pC]$$

$$k_{kick,x}^{slot} < 0.0001 = 0.01 = k_{kick,x}^{abs} \sigma [V / pC]$$

Longitudinal wake for the case of the elliptical pipe (3.8mm)

	pro section (6.1 m)	Loss, V/pC	Spread, V/pC	Peak, V/pC
absorber	1	42	16	-58
pumping slot	1	<0.2	<0.1	>-0.3
pump	1	9	4	-13
BPM	1			
bellow	1	13	5	-18
flange gap	1	6	2.4	-8.5
Total geom.		70	25	-95
resistive (Cu)	6.1m	220	279	-542
resistive (Al)	6.1m	303	325	-660

Shape dependence

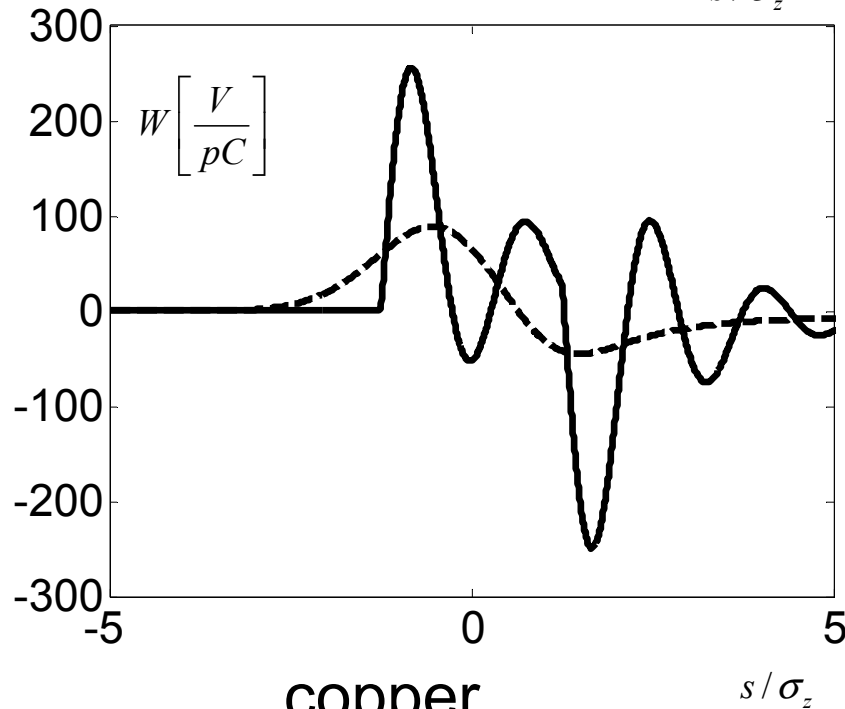


$$\sigma_z = 25 \mu m$$

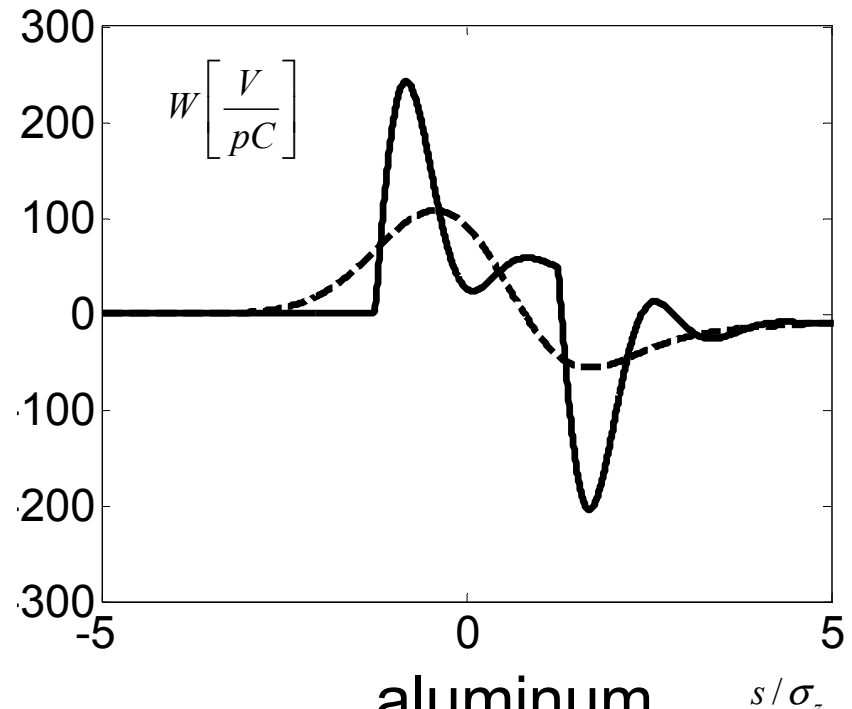
$$cu: \sigma_{cond} = 5.8e+7 [\Omega^{-1} \cdot m^{-1}], \quad \tau_{relax} = 2.46e-14 [sec]$$

$$al: \sigma_{cond} = 3.66e+7 [\Omega^{-1} \cdot m^{-1}], \quad \tau_{relax} = 7.1e-15 [sec]$$

	Loss, V/pC	Spread, V/pC	Peak, V/pC
Gauss, cu/al	36/50	46/53	-89/108
Rect, cu/al	79/93	90/72	-256/243



copper



aluminum

Power Loss (Gaussian bunch)

$$N_b = 4000 [\text{bunches}]$$

$$f_{rep} = 10 [\text{Hz}]$$

$$q = 1 [\text{nC}]$$

$$P = N_b f_{rep} q^2 k_{loss}$$

$$P_{geom} = 0.52 \left[\frac{W}{m} \right]$$

$$P_{res,Cu} = 1.4 \left[\frac{W}{m} \right]$$

$$P_{res,Al} = 2 \left[\frac{W}{m} \right]$$

Conclusion

- Loss and kick of the pumping slot are negligible
- Wake of the absorber is reduced by factor 2
- Resistive wake is dominant
- Non-smooth bunch shape (rectangular) increases the energy spread less than by factor 2