



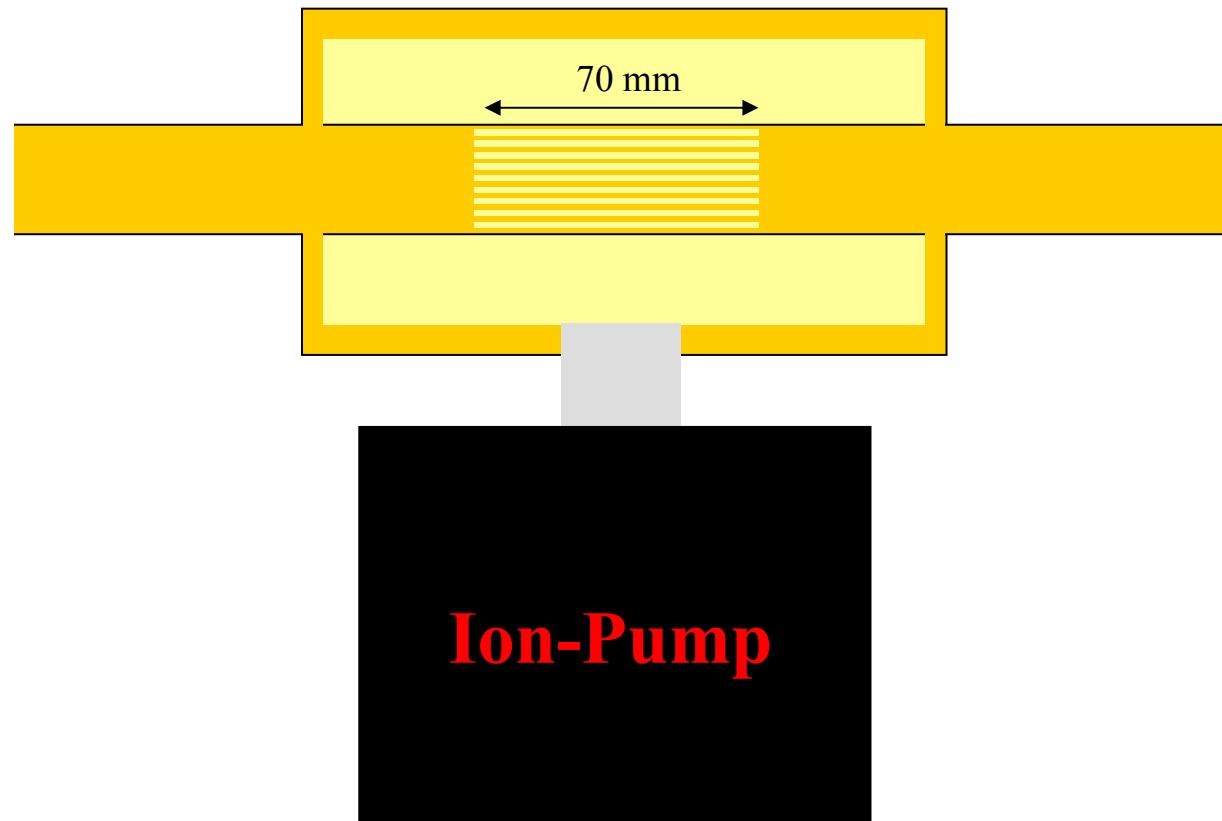
# Wakefields of different elements

Igor Zagorodnov

28.04.07

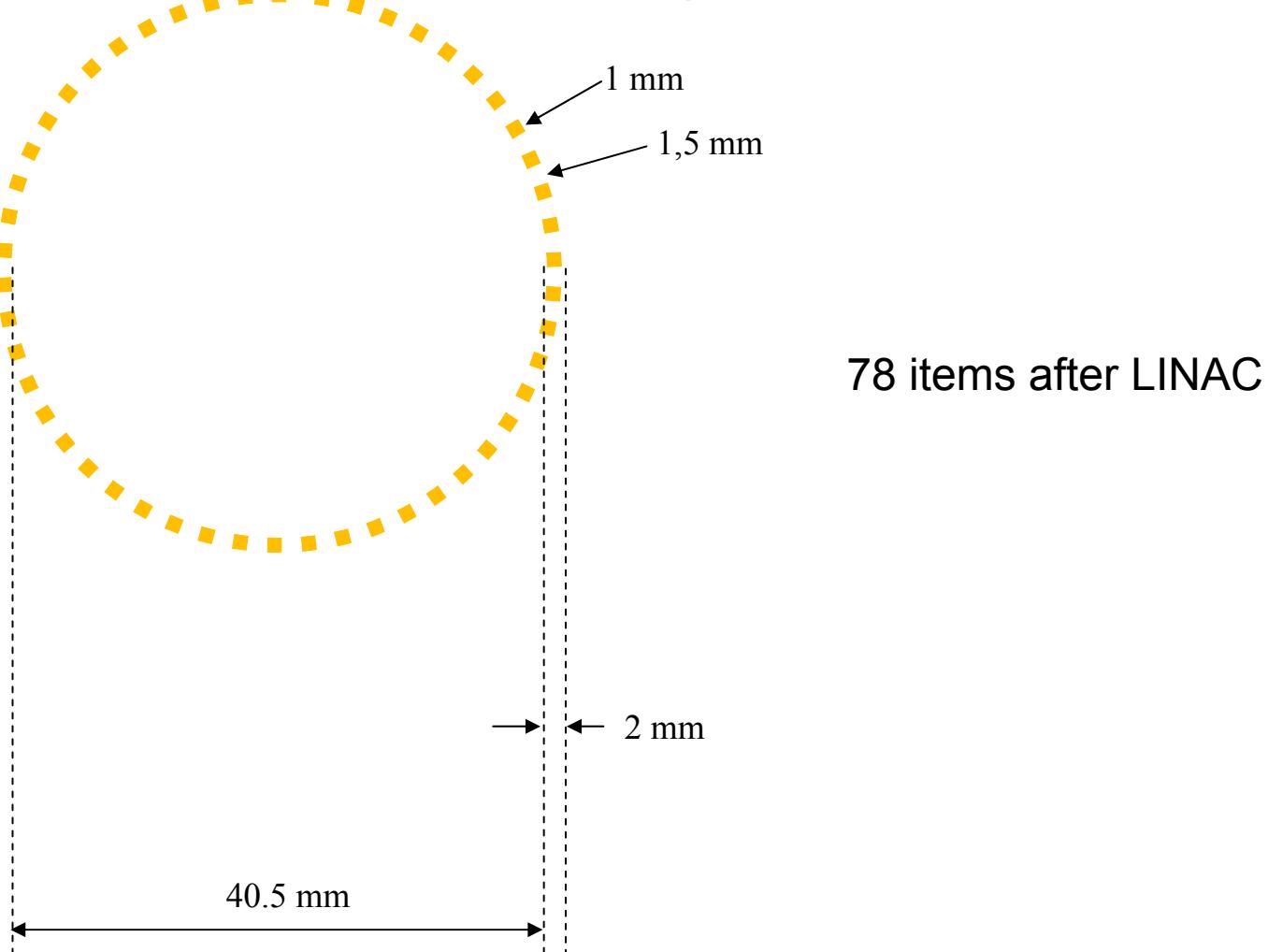
BD meeting, DESY

# Pumping slots



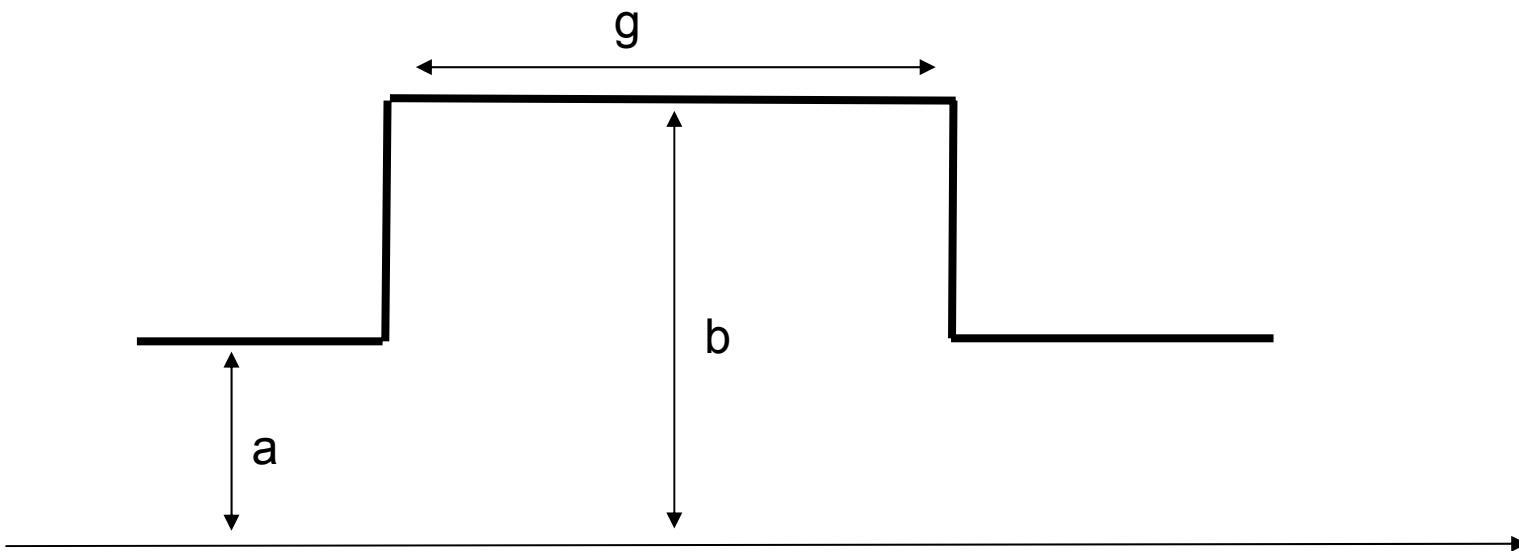
Boris Nagorny

# Pumping slots



Boris Nagorny

# Pumping slots: cavity model



# Pumping slots: cavity model

(1) Analytical estimation for cavity (g - finite)

$$w_{\parallel}^{\delta}(s) = \frac{Z_0 c}{\sqrt{2\pi^2 a}} \sqrt{\frac{g}{s}}$$

$$k_{\parallel} = \frac{Z_0 c}{4a\pi^{2.5}} \Gamma\left(\frac{1}{4}\right) \sqrt{\frac{g}{\sigma_z}}$$

$$k_{\text{rms}} = \frac{k_{\parallel}}{2.467}$$

$$w_{\perp}^{\delta}(s) = \frac{2}{a^2} \frac{\sqrt{2} Z_0 c}{\pi^2 a} \sqrt{gs}$$

$$k_{\perp} = \frac{2}{a^3} \frac{Z_0 c}{\pi^{2.5}} \Gamma\left(\frac{3}{4}\right) \sqrt{g\sigma_z}$$

(2) Analytical estimation for step-out transition (g - infinite)

$$Z_{\parallel} = \frac{Z_0}{\pi} \ln\left(\frac{b}{a}\right)$$

$$k_{\parallel} = \frac{Z_{\parallel} c}{2\sqrt{\pi\sigma_z}}$$

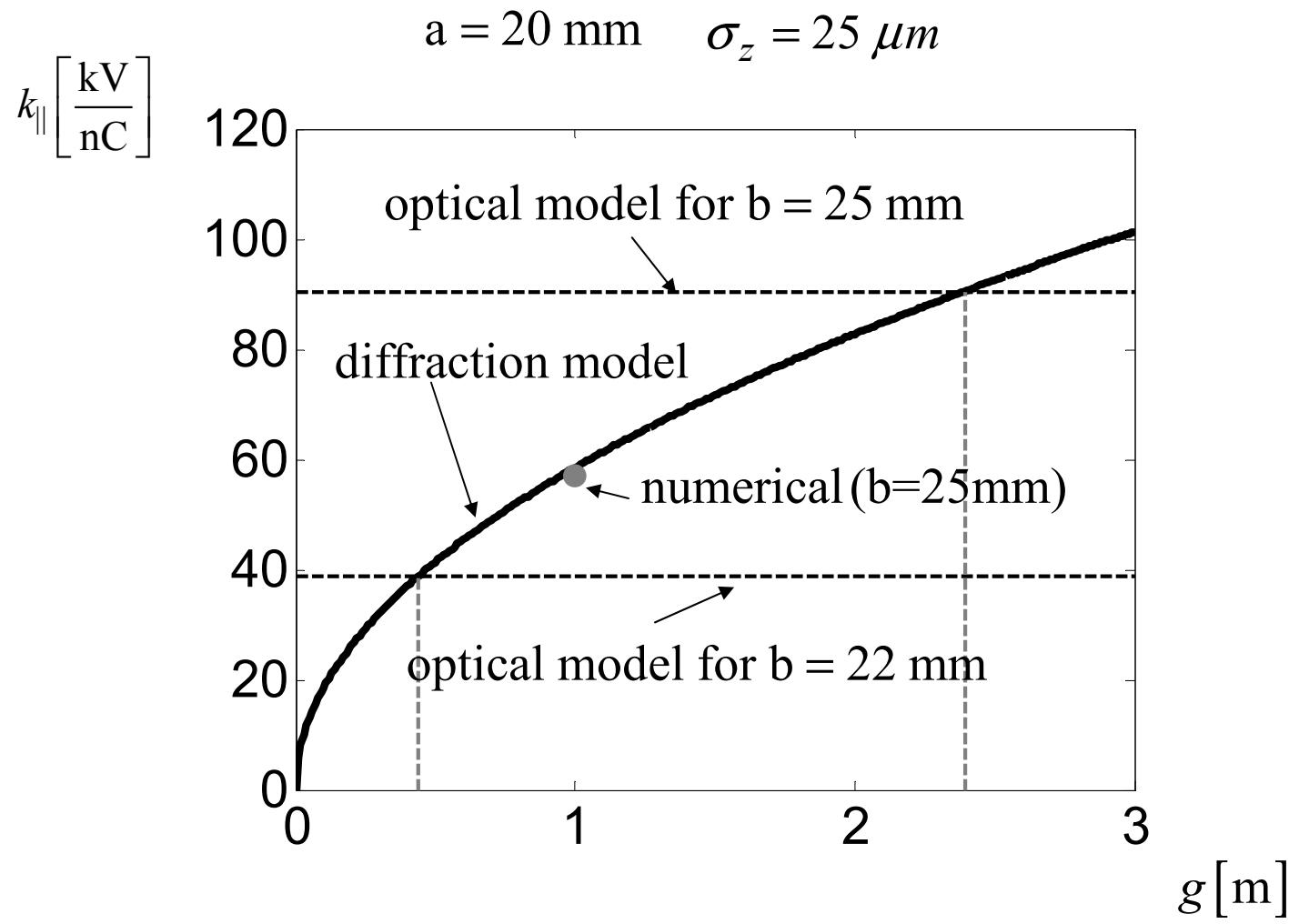
$$k_{\text{rms}} = k_{\parallel} \sqrt{\frac{2}{\sqrt{3}} - 1} \approx 0.4 k_{\parallel}$$

$$w_{\parallel}^{\delta}(s) = Z_{\parallel} c \delta(s)$$

$$w_{\perp}^{\delta}(s) = 2 * k_{\perp} * \theta(s)$$

$$k_{\perp} = \frac{Z_0 c}{2\pi} \left( \frac{1}{a^2} - \frac{1}{b^2} \right)$$

## Pumping slots: cavity model



$g = 70 \text{ mm}$    diffraction model ( $g$ -finite)

# Pumping slots

$$a = 20 \text{ mm}$$

$$\sigma_z = 25 \mu\text{m}$$

$$g = 70 \text{ mm}$$

$$\theta = \frac{3}{5} 2\pi$$

$$k_{\parallel} = \frac{Z_0 c}{4a\pi^{2.5}} \Gamma\left(\frac{1}{4}\right) \sqrt{\frac{g}{\sigma_z}}$$

$$\text{Spread} = \frac{k_{\parallel}}{2.467}$$

$$k_{\parallel}^{\text{cavity}} = 15.5 \frac{\text{kV}}{\text{nC}} \quad \text{Spread}^{\text{cavity}} = 6.3 \frac{\text{V}}{\text{pC}}$$

$$k_{\parallel}^{\text{pump}} \approx k_{\parallel}^{\text{cavity}} \frac{\theta}{2\pi} = 9.3 \frac{\text{kV}}{\text{nC}} \quad k_{rms}^{\text{pump}} \approx \text{Spread}^{\text{cavity}} \frac{\theta}{2\pi} = 3.8 \frac{\text{kV}}{\text{nC}}$$

$$k_{\parallel}^{\text{pump, total}} = k_{\parallel}^{\text{pump}} * 78 = 725 \frac{\text{kV}}{\text{nC}}$$

$$k_{rms}^{\text{pump, total}} = k_{rms}^{\text{pump}} * 78 = 296 \frac{\text{kV}}{\text{nC}}$$

# Pumping slots

$a = 20 \text{ mm}$

$\sigma_z = 25 \mu\text{m}$

$g = 70 \text{ mm}$

$\theta = \frac{3}{5} 2\pi$

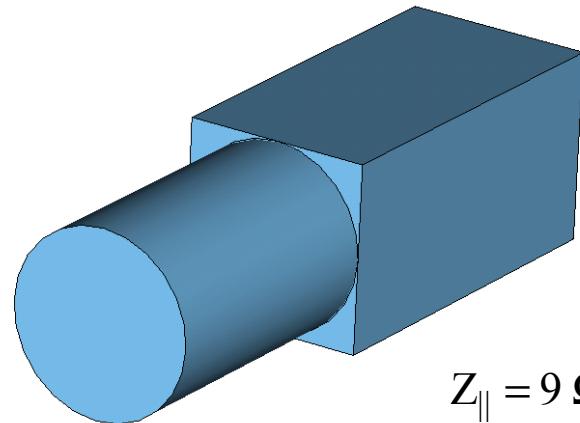
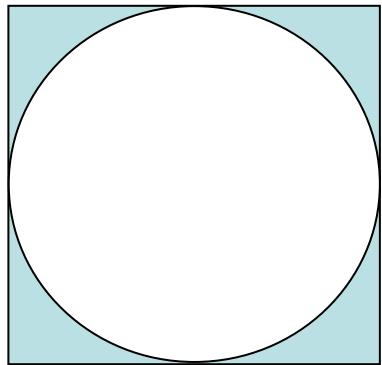
$$k_{\parallel}^{pump, total} = k_{\parallel}^{pump} * 78 = 725 \frac{\text{kV}}{\text{nC}} \%$$

$$k_{rms}^{pump, total} = k_{rms}^{pump} * 78 = 296 \frac{\text{kV}}{\text{nC}}$$

TOTAL (LINAC to SASE2)

	Pipe (456m)	Collimators (4 items)	Kickers (3*10m)	Pumps (78 items)	Total
Loss	3430	4343	2659	725 (6%)	10432+725 (+7%)
<b>Spread</b>	<b>4332</b>	<b>3164</b>	<b>1557</b>	<b>296 (3%)</b>	<b>8763+296 (+3%)</b>
Peak	-9048	-9088	-4633		

# Round to square transition in bunch compressor



$$w_{\parallel}^{\delta}(s) = Z_{\parallel} c \delta(s)$$

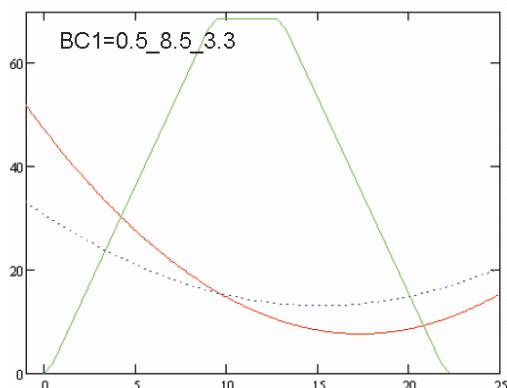
$$k_{\parallel} = \frac{Z_{\parallel} c}{2\sqrt{\pi}\sigma}$$

$$Z_{\parallel} = 9 \Omega$$

$$k_{\text{rms}} = k_{\parallel} \sqrt{\frac{2}{\sqrt{3}}} - 1$$

„size independent“

$$Z_{\parallel} = 80 \Omega$$

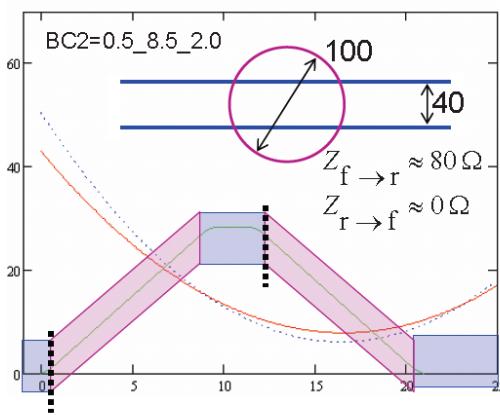


flat chamber in BC1

“2x20”       $I_{\text{peak}}/A = 1002$   
cu             $\text{emit\_hor}/\mu\text{m} = 1.56$

“inf”           $I_{\text{peak}}/A = 996$   
emit\_hor/ $\mu\text{m} = 1.61$

“2x20”       $I_{\text{peak}}/A = 1001$   
st             $\text{emit\_hor}/\mu\text{m} = 1.31$



BC2: flat & round

$I_{\text{peak}}/A = 5076$   
 $\text{emit\_hor}/\mu\text{m} = 1.36$

$I_{\text{peak}}/A = 5005$   
 $\text{emit\_hor}/\mu\text{m} = 1.12$

$I_{\text{peak}}/A = 5065$   
 $\text{emit\_hor}/\mu\text{m} = 1.59$

XFEL BC System  
BC lattice & chamber geometry

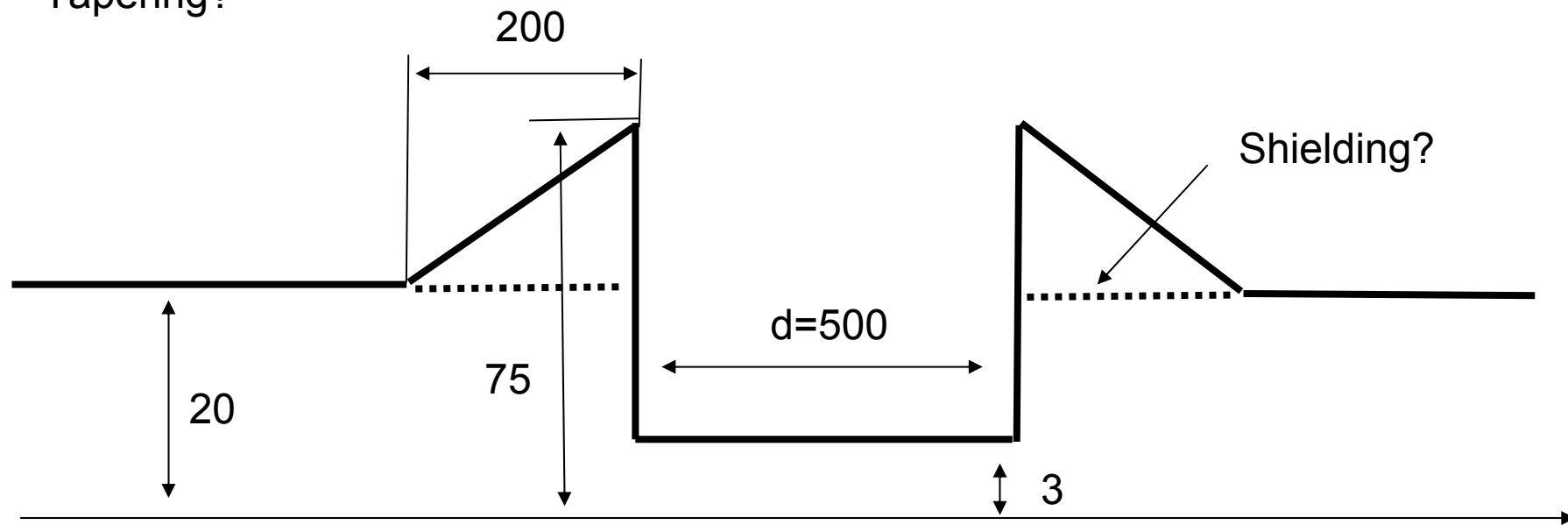
Martin Dohlus,  
BDM, 03.09.2007



Shielding?  
Coating?  
Tapering?

## Collimator

$$\sigma_z = 25 \mu m$$

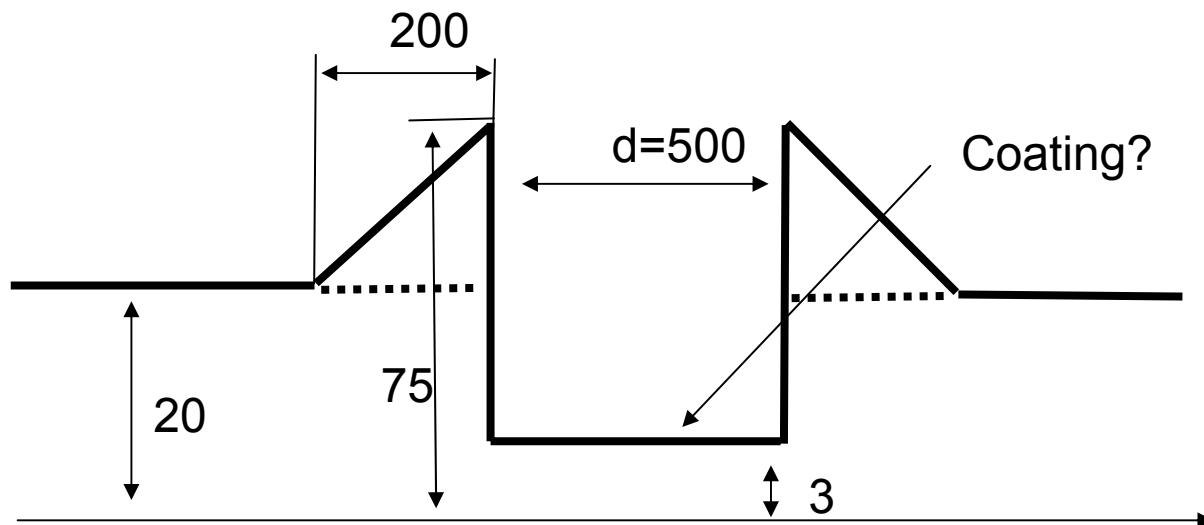


	Analytical (optical)	Numerical (ECHO)	
	Step-out	Collimator with shielding	Collimator without shielding
Loss, kV/nC	934	929	929
Kick, kV/nC/mm	4.5	4.2	4.2

The shielding has no effect on short range wake

$$\sigma_z = 25 \mu m$$

## Collimator



$$\tau = 0 [\text{sec}]$$

$$\Delta_{rough} = 300 [\text{nm}] \quad \Delta_{oxid} = 5 [\text{nm}]$$

TIMETAL (Titanium)

$$\sigma = 0.6 \cdot 10^6 \Omega^{-1} m^{-1}$$

TiN (SLAC-PUB-7261)

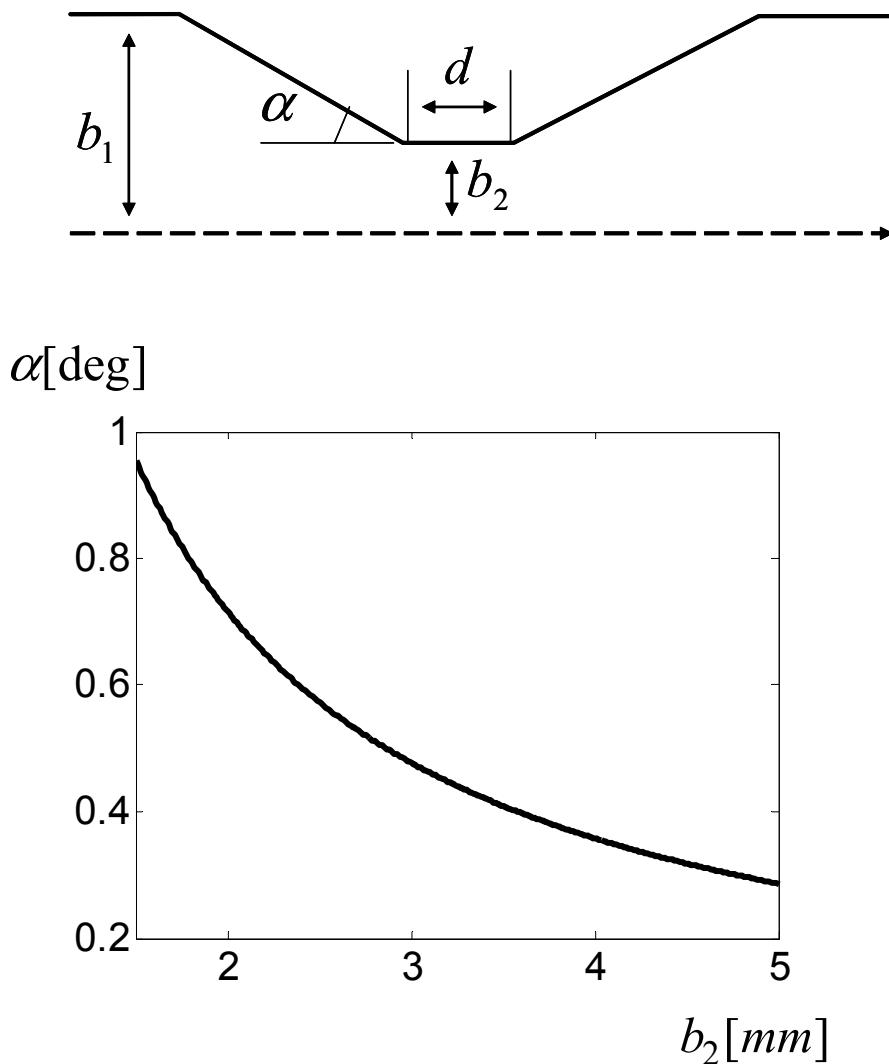
$$\sigma = 4.5 \cdot 10^6 \Omega^{-1} m^{-1}$$

	Geometrical	Resistive	
		TIMETAL (Titanium)	TiN
Loss, kV/nC	934	491	151
Spread, kV/nC	367	333	152 (-55%)

Coating reduces the energy spread due to resistive part by 55%.

Transverse kick?

## XFEL collimators. Tapering



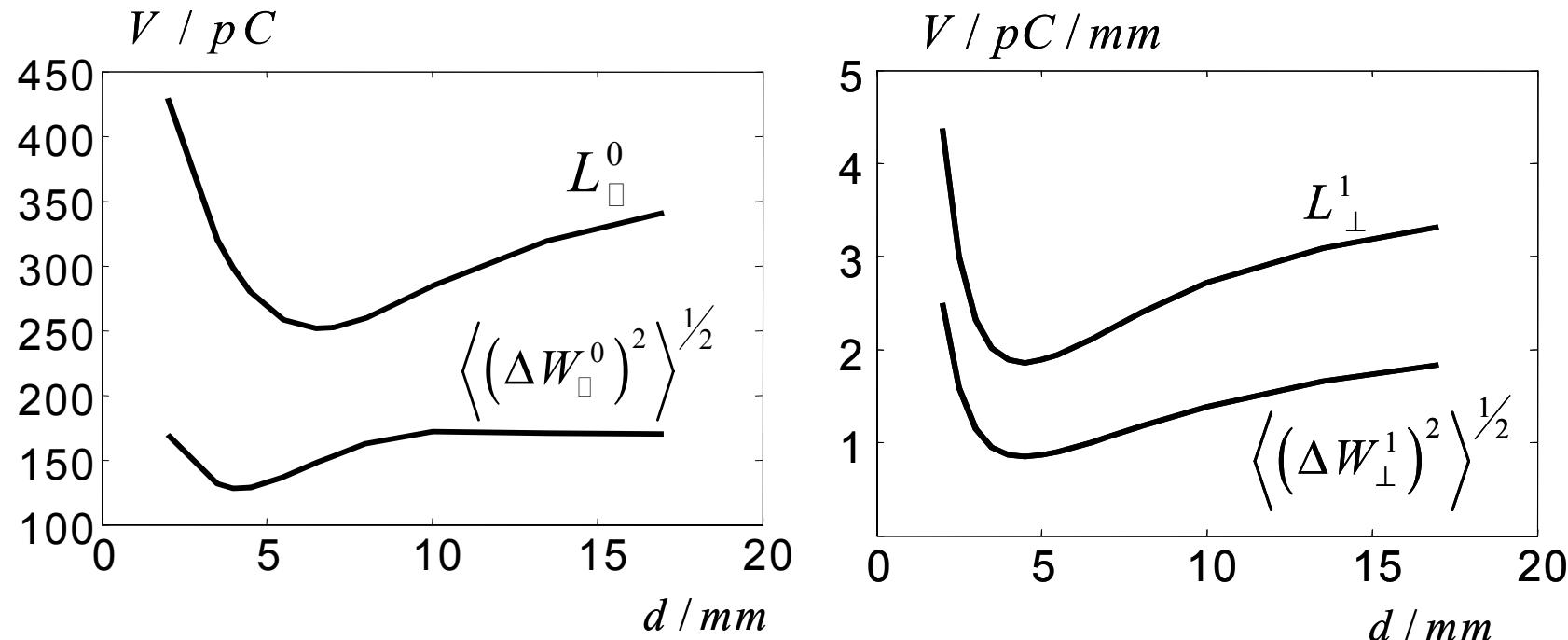
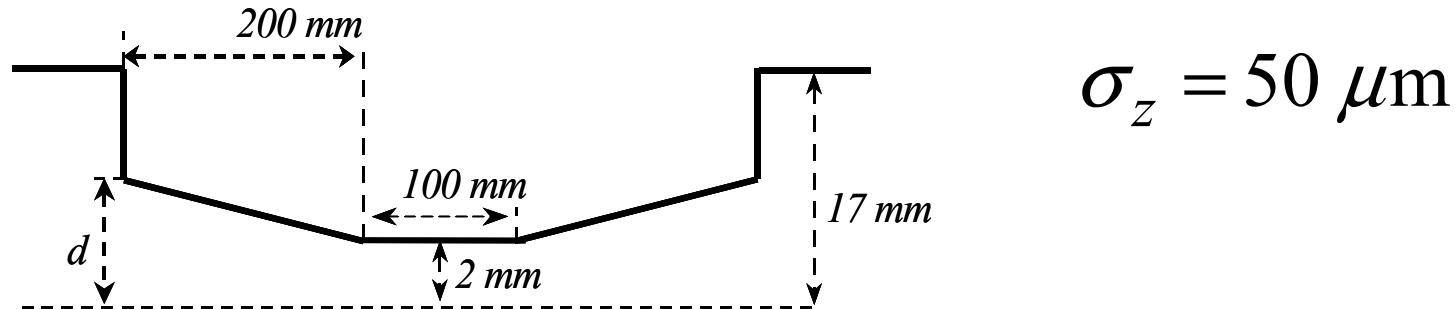
**When a short bunch passes by an out-transition, a significant reduction in the wake will not happen until the tapered walls cut into the cone of radiation, i.e until**

$$\tan \alpha \sim \sigma_z / b_2$$

$$\sigma_z = 0.025 \text{ mm}$$

## XFEL collimators. Tapering

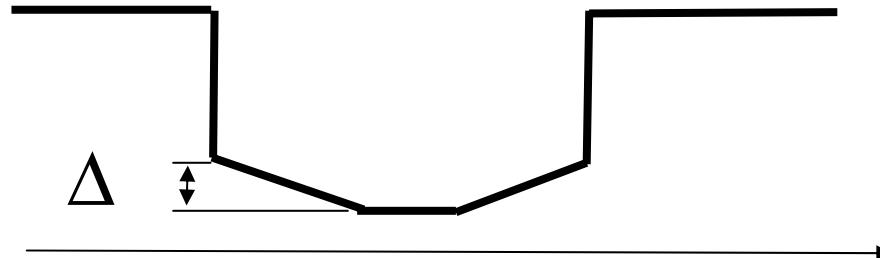
Geometry of the “step+taper” collimator for TTF2



Collimator geometry optimization.  
Optimum  $d \sim 4.5\text{mm}$

TESLA Report 2003-23

## XFEL collimators. Tapering

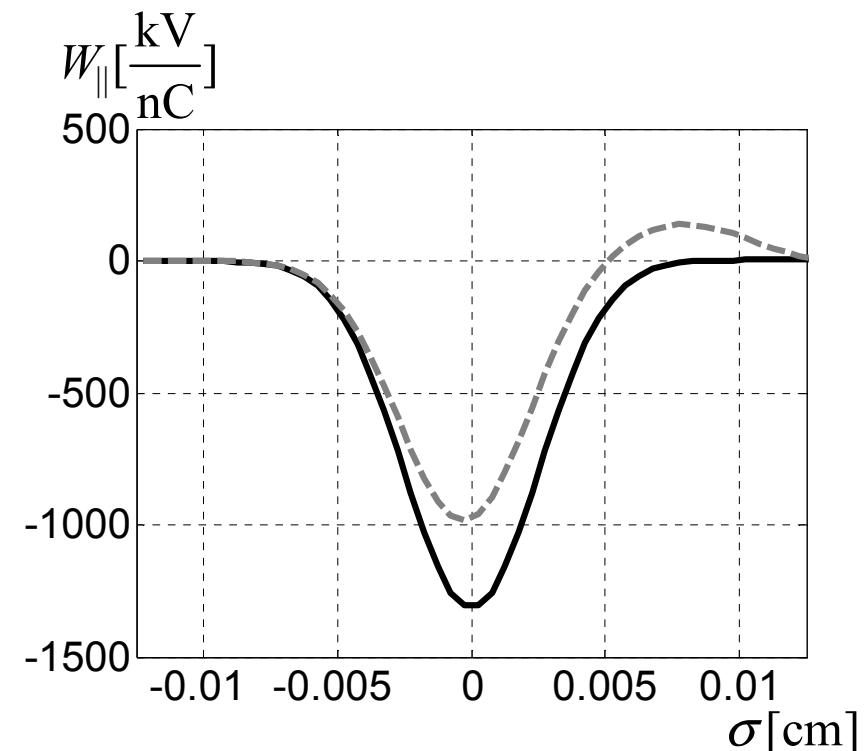


$$\sigma_z = 25 \mu\text{m}$$

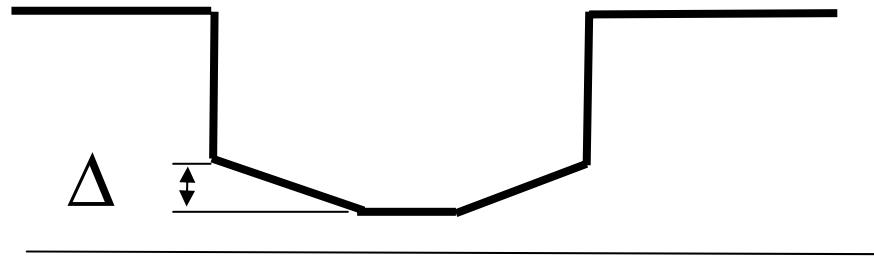
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The tapering can reduce the energy spread only by 20%.

$\Delta$ , mm	Loss, kV/nC	Spread, kV/nC
3.5	656	311
3	661	299
2.5	674	<b>294</b>
2	696	296
1.5	729	301
0	929	365

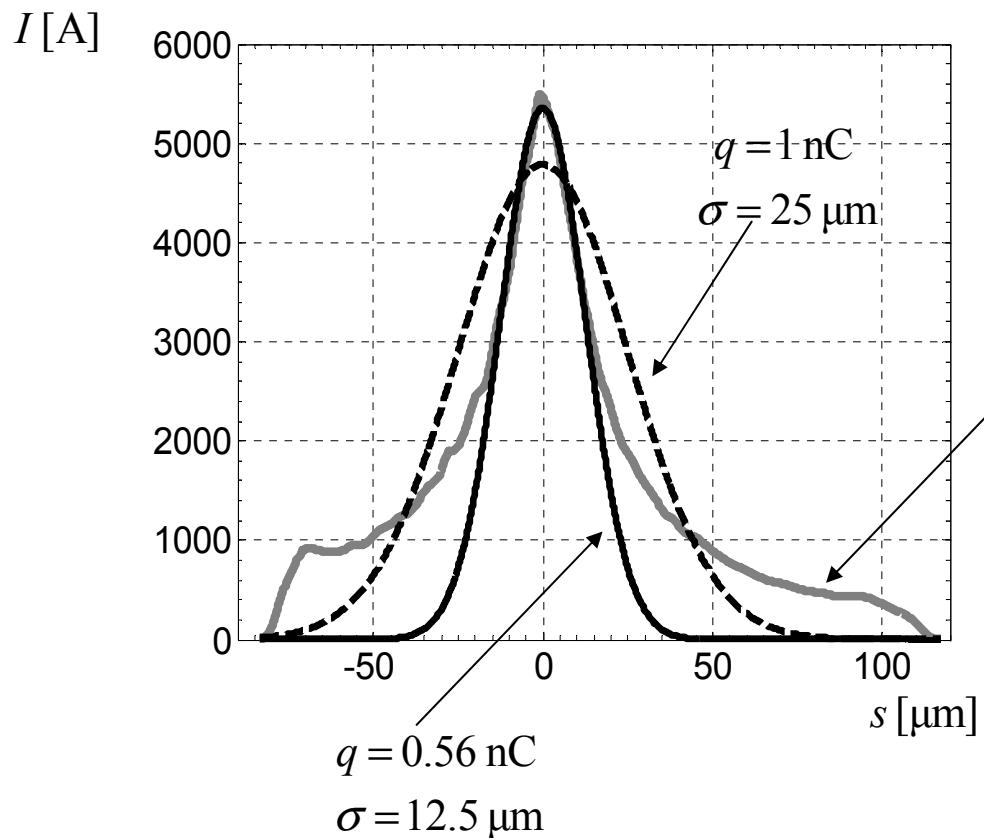


## XFEL collimators. Tapering



$$\sigma_z = 12.5 \mu\text{m}$$

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The tapering **does not reduce** the energy spread

Bunch shape  
from S2E simulations  
by Martin Dohlus