

# Simulations on multi bunch dynamics at FLASH with different damping of the HOM at 3,9GHz cavities

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# Problem description

- The 3rd harm cavity is planned to be installed in order to provide better bunch qualities.
- HOM could affect the transverse MB dynamics of the bunches thus causing an additional MB emittance.
- HOM are planned to be suppressed by the HOM couplers with an average damping factor of  $10^{-5}$
- The question in this context: how strong should be the damping of the HOM of the 3,9GHz cavities to provide the suitable multi bunch dynamics (i.e  $\varepsilon_{MB} \ll \varepsilon_{SB}$ ) and to verify if it is a possible option to use the 3,9GHz cavities without HOM couplers.

# Background

- HOM of the 3,9GHz cavities: described in  
*„A Design of a 3rd Harmonic Cavity for the TTF 2 Photoinjector“* J. Sekutowicz, R. Wanzenberg  
*„Higher Order Modes of a 3rd Harmonic Cavity with an Increased End-cup Iris“* T. Khabibouline, N. Solyak, R. Wanzenberg
- HOM of the 1,3GHz cavities:  
*„Monopole, Dipole and Quadrupole Passbands of the TESLA 9-cell Cavity“* R. Wanzenberg
- Passage between cavities:  
*„Matlab Functions for Calculations of the Linear Beam Optics of FLASH Linac“* V. Balandin, N. Golubeva.

## Main Formulas of the Model

Wake fields:

$$W_{\parallel}^{(m)}(s) = -\sum_n \omega_n \left( \frac{R^{(m)}}{Q} \right)_n \cos(\omega_n \cdot s/c) \exp\left(-\frac{1}{\tau_n} \cdot s/c\right)$$

$$W_{\perp}^{(m)}(s) = c \sum_n \left( \frac{R^{(m)}}{Q} \right)_n \sin(\omega_n \cdot s/c) \exp\left(-\frac{1}{\tau_n} \cdot s/c\right)$$

Energy deviation due to wake fields:

$$\Delta E(s_j) = -eq \sum_{i < j} W_{\parallel}^{(0)}(s_j - s_i) - eq \sum_{i < j} (x_j x_i + y_j y_i) W_{\parallel}^{(1)} + \dots$$

Transverse kick due to wake fields:

$$\vec{\theta}_j = \frac{eq}{E_j} \sum_{i < j} (x_i \vec{e}_x + y_i \vec{e}_y) W_{\perp}^{(1)}(s_j - s_i)$$

Damping of the HOM:

$$\tau_n \rightarrow \text{dampingfactor} \cdot \tau_{n0}$$

# Assumptions

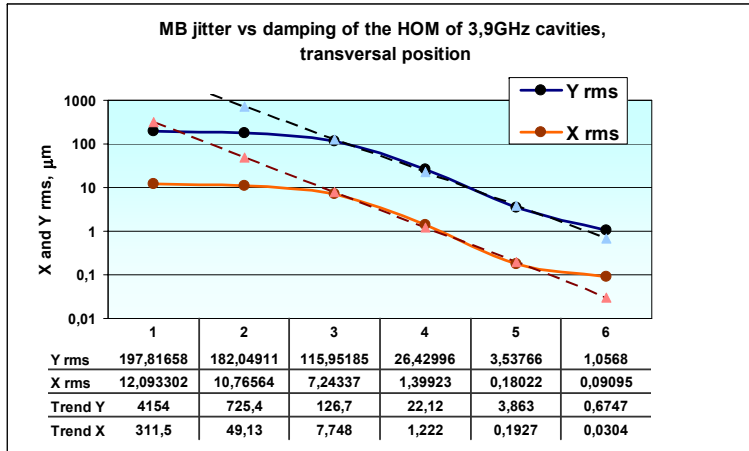
- Simulation region: from the quadrupole Q9ACC1 at 13,5827m (right after the ACC1) to the entrance into the Undulator 1 at 203,3288m (Q22SEED)
- Supposed place for the 3,9GHz cavities: between V10ACC1 at 14,0177m and 1UBC2 at 19,235m.
- Amount of 3,9GHz cavities: 4 cavities with 9 cells each.
- HOM of the 1,3GHz cavities are damped by the order of  $10^{-5}$
- Decouple single bunch effects from MB effects
- All monopole and dipole modes from the first four passbands for both cavities (1,3GHz and 3,9GHz) have been taken into account.
- Inject bunches on crest ideally i.e. without slope divergence and without transverse offsets.

## Parameters for Simulations

<b>bunch charge</b>	<b>1nC</b>
<b>pulse length</b>	<b>120<math>\mu</math>m</b>
<b>bunch spacing</b>	<b>200ns</b>
<b>number of bunches per train</b>	<b>600</b>
<b>cavity misalignment</b>	<b>0,5mm rms</b>
<b>cavity detuning</b>	<b>0,1% rms</b>
<b>normalized SB emittance</b>	<b>1,4mm mrad</b>

➤ 100 linacs have been simulated and averaged for each measurement.

# MB Jitter as a Function of Damping of the HOM in the 3,9GHz Cavities

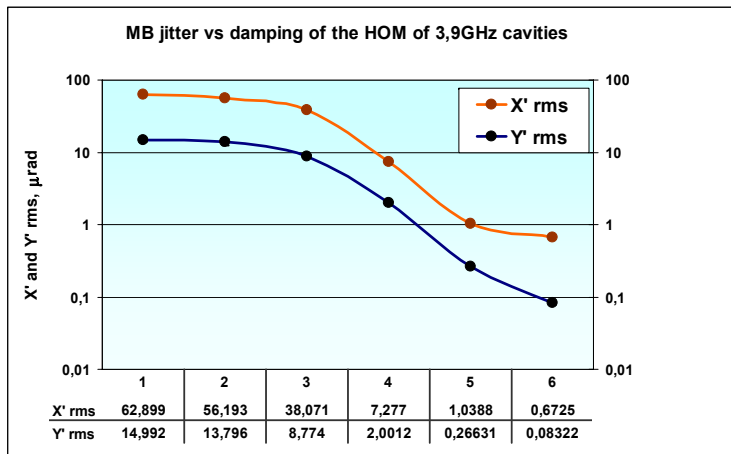


- Almost no influence of damping on MB emittance up to damping factor of  $10^{-3}$
- Linear dependence of the MB rms size on the damping of the HOM in the region  $10^{-3} - 10^{-5}$ . It could be approximately described by the equation:

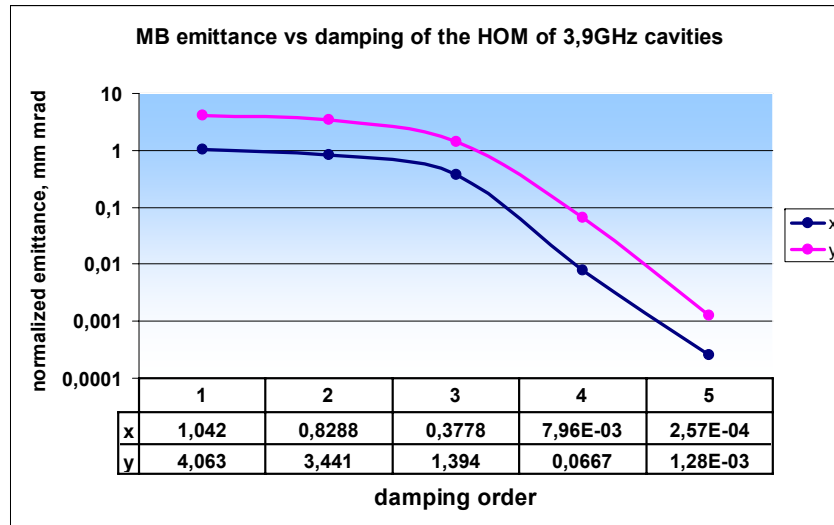
$$y_{rms} = 27787 \cdot (0,1746)^{1/dampingfactor} \mu m$$

$$x_{rms} = 1975 \cdot (0,1577)^{1/dampingfactor} \mu m$$

- The effect of damping decreases after  $10^{-5} \rightarrow$  comprehensible since 1,3GHz cavities are damped only by the order of  $10^{-5}$ .



# MB emittance as a function of damping



Design normalized single-bunch emittance 1,4mm mrad assumed.  
 Combined emittance calculated according to

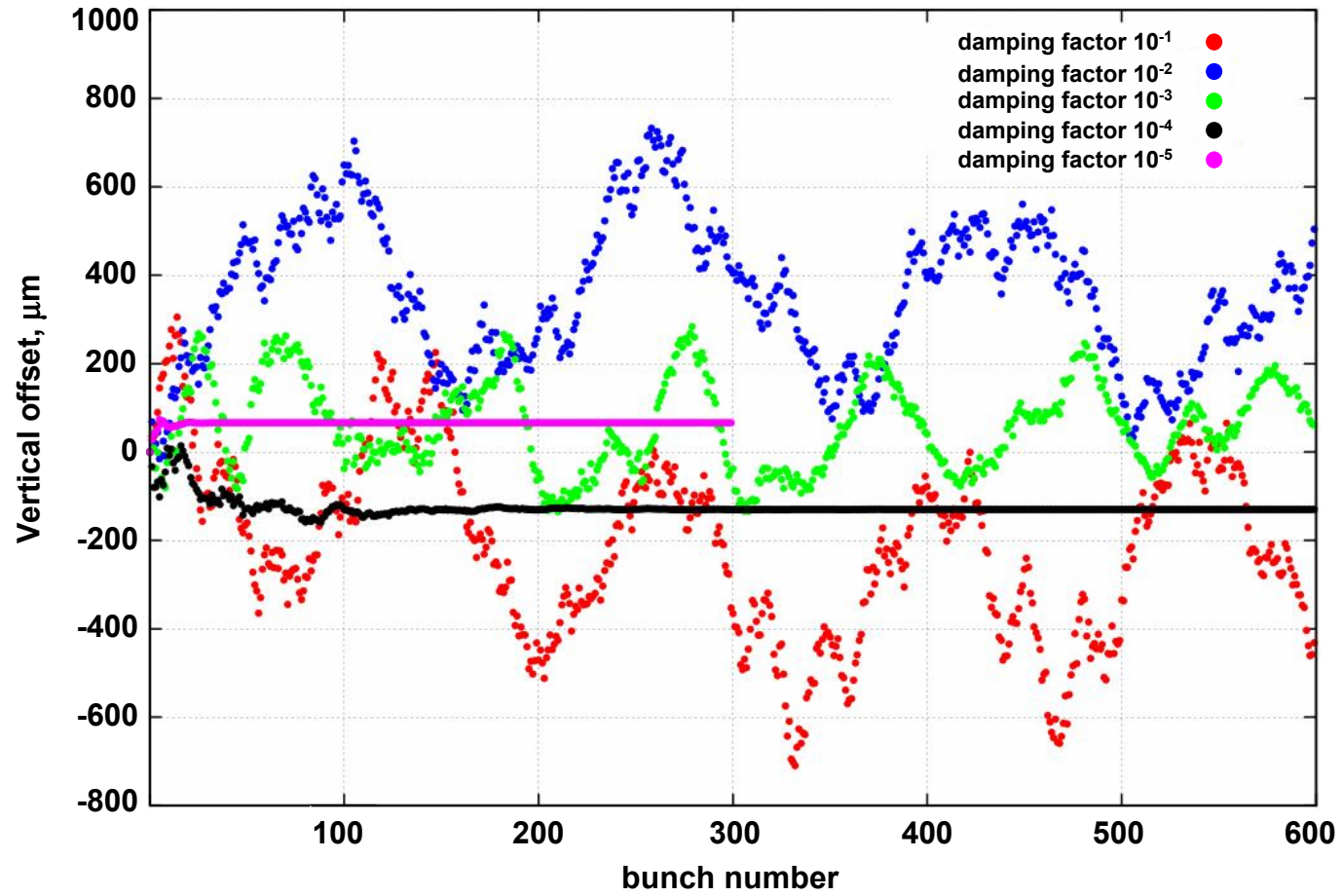
$$\mathcal{E} = \sqrt{\mathcal{E}_{MB}^2 + \mathcal{E}_{SB}^2}$$

Table: Emittance blow up vs damping of the HOM of the 3,9GHz cavities  
 Design emittance of 1,4mm mrad assumed

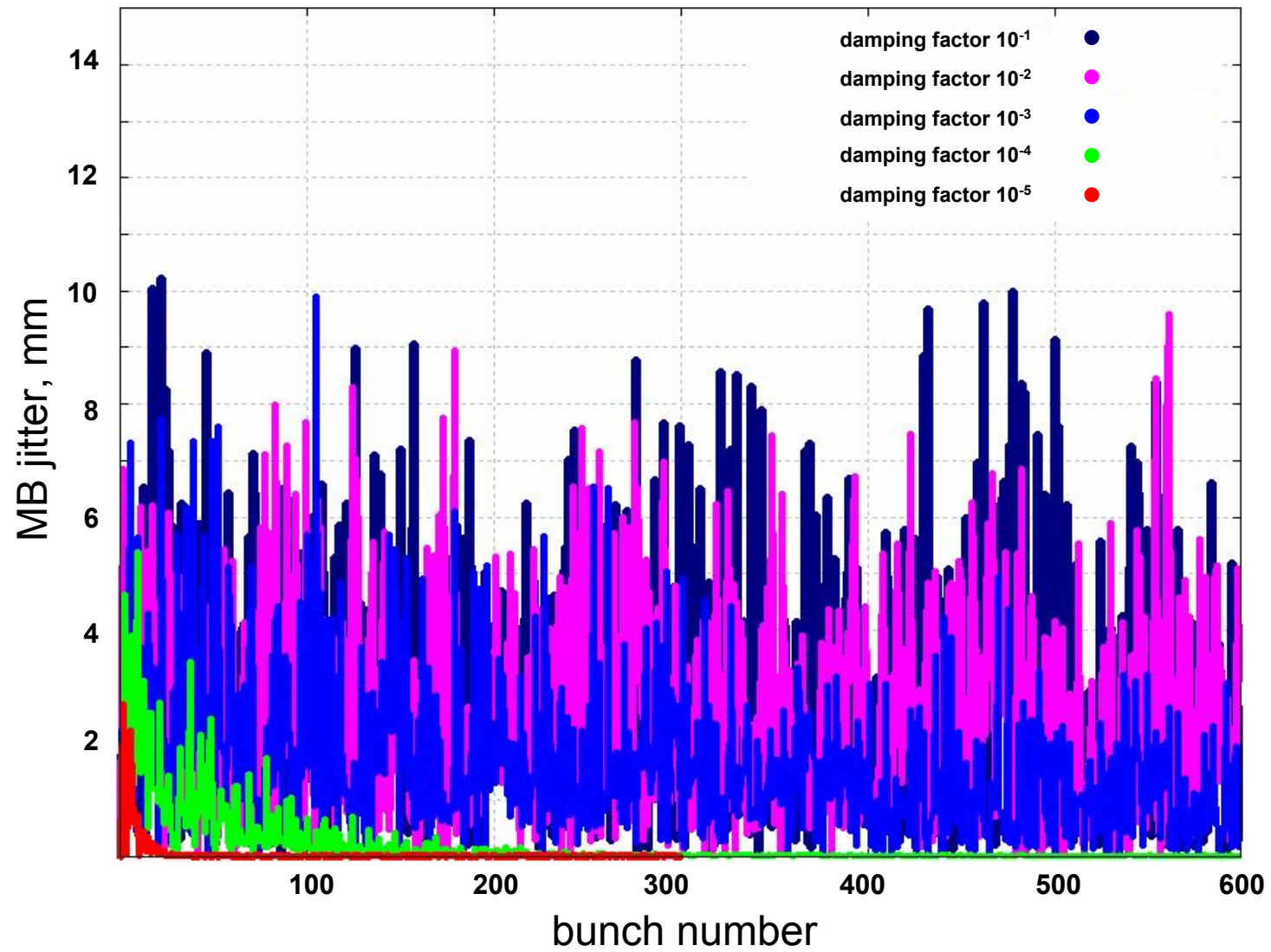
Damping	10 <sup>-1</sup>	10 <sup>-2</sup>	10 <sup>-3</sup>	10 <sup>-4</sup>	10 <sup>-5</sup>
$\Delta\epsilon_x, \%$	<b>24,66</b>	<b>16,21</b>	<b>3,58</b>	<b>1,616e-3</b>	<b>1,642e-6</b>
$\Delta\epsilon_y, \%$	<b>206,96</b>	<b>165,35</b>	<b>41,12</b>	<b>0,113</b>	<b>4,171e-5</b>



**Vertical offsets at the entrance in undulator 1  
for different damping of the HOM of the 3,9GHz cavities**

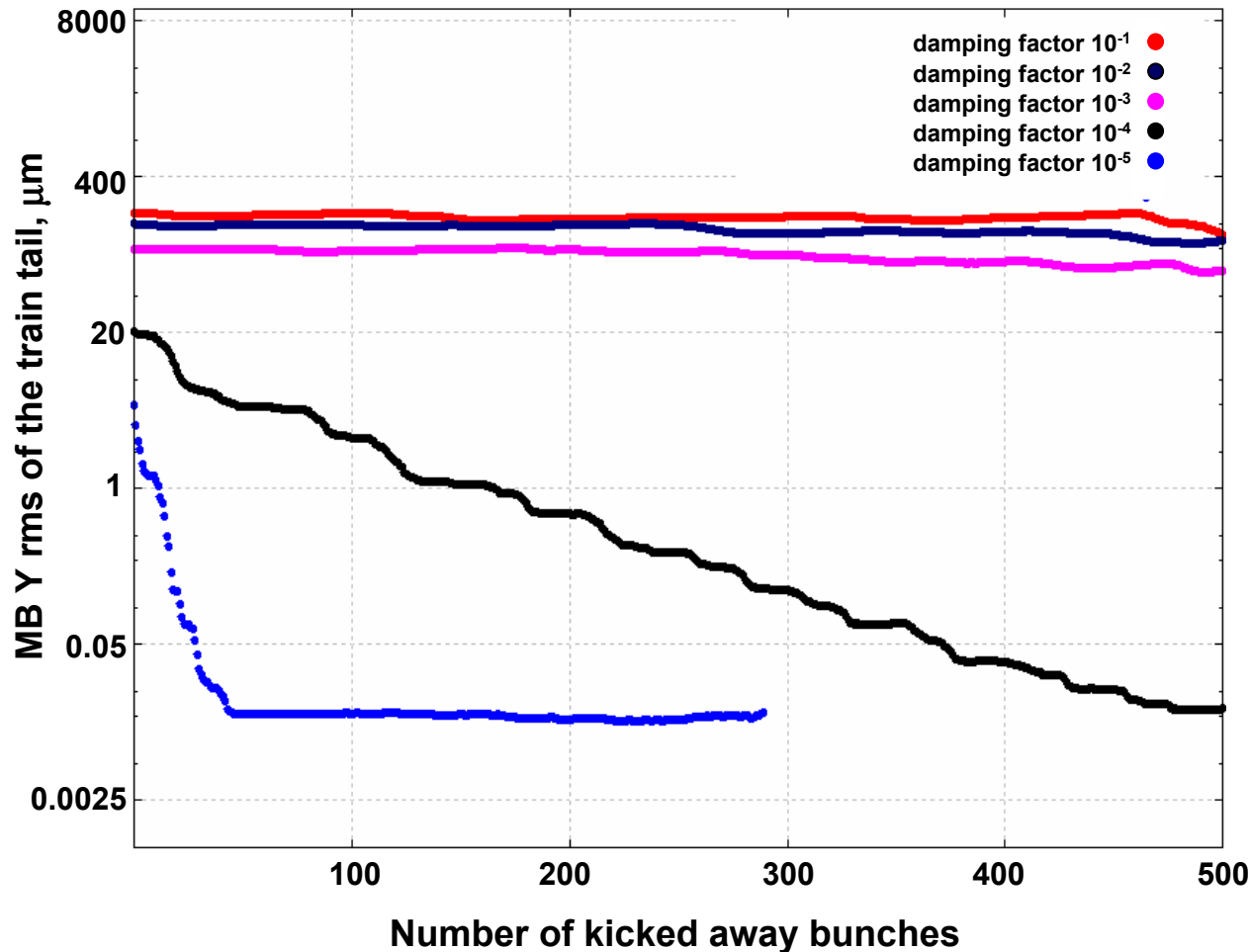


# MB jitter in vertical direction at the entrance in undulator 1



B  
u

# Vertical MB rms after cutting off the first bunches



## Simulation settings:

*Bunch train: 600 bunches*

*Bunch spacing: 200ns*

*Bunch charge: 1nC*

*Vertical mb rms calculated after kicking away the first bunches of the train head*

## Results:

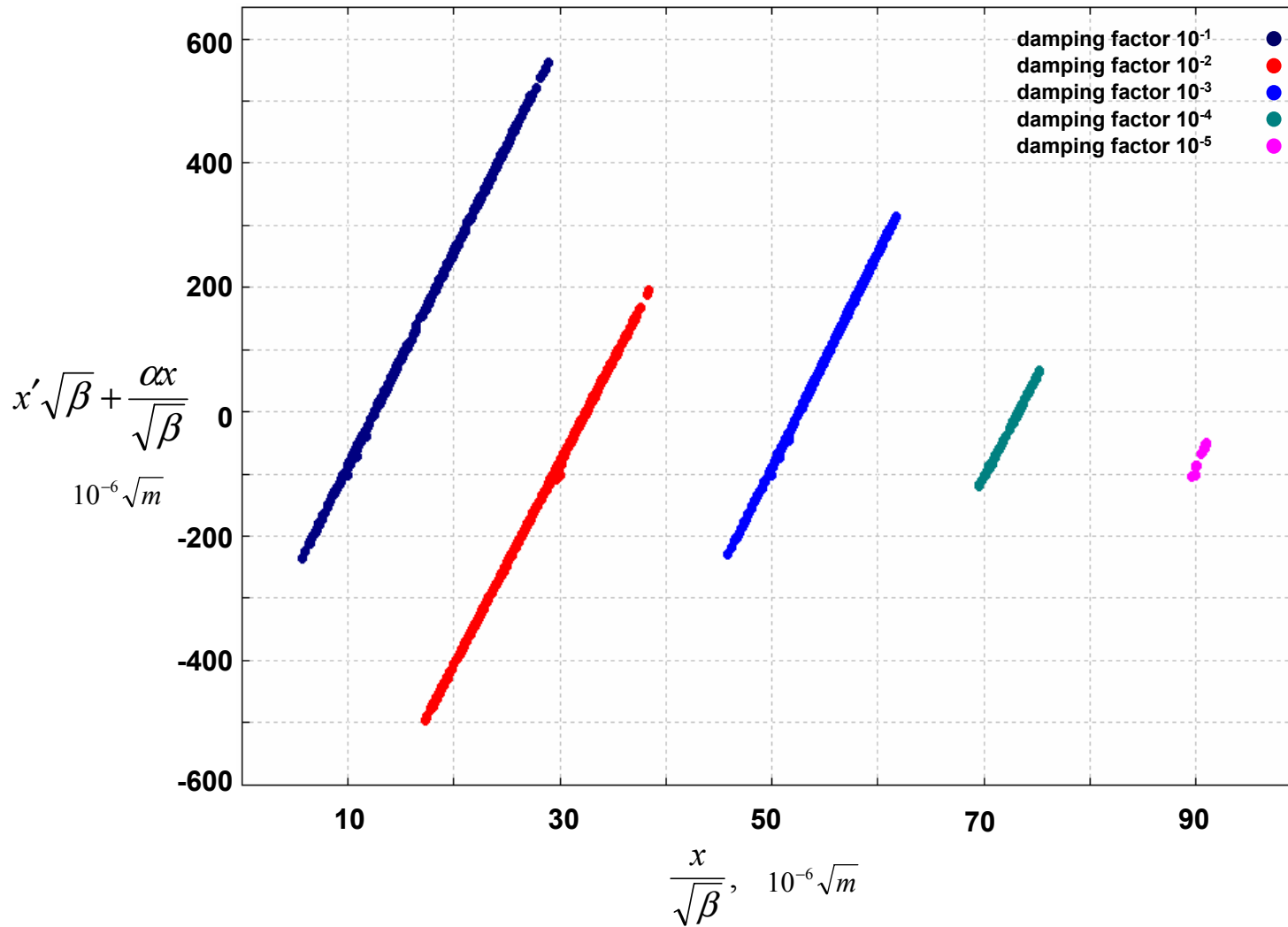
**for the design damping of the HOM:**

Kicking away the first 50 bunches leads to absolutely stable conditions. The jitter of the whole bunch train is in any case negligible.

**Damping by the order of up to 10<sup>3</sup>:**

doesn't lead to significant effect by suppressing the MB jitter.

# phase space for horizontal plane



**Phase space for different cases of damping of the HOM of the 3,9GHz cavities**

# Conclusions

- MB emittance blow up of up to 200% is possible if the 3<sup>rd</sup> harmonic cavities are operated without HOM couplers.
- Damping of the HOM by  $10^{-4}$ - $10^{-5}$  required for the stable operating conditions with negligible mb effects. Since HOM couplers provide the damping of  $10^{-5}$  no problems about mb dynamics are expected in this case.