

# Wakes in 3<sup>rd</sup> Harmonic RF Modules

## FLASH

4 cavities  
at ~ 130 MV  
~ 4 MV / cavity

single bunch effects  
multi bunch effects → Rainer Wanzenberg

## XFEL

12 .. 24 cavities  
at ~ 500 MV  
~ 8 (4) .. 10 MV / cavity

single bunch effects  
multi bunch effects

summary



## 3<sup>rd</sup> harmonic cavities in FLASH

possible working point

1.3 GHz system: 136.39 MV @ 10.82 deg --> 133.66 MeV

3.9 GHz system: 16 MV @ -176.2 deg --> 118 MeV

BC2 r56 = -165.1 mm --> compression factor = 7

1.3 GHz system: 338.15 MV @ 10.98 deg --> 450 MeV

BC3 r56 = -63.8 mm --> compression factor = 7

(r56 values from TESLA-FEL-06, page9)

sensitivity (10% change of compression)

1.3 GHz system before BC2:  $|\Delta V| < 0.76$  MV,  $|\Delta\phi| < 0.025$  deg

3.9 GHz system:  $|\Delta V| < 0.83$  MV,  $|\Delta\phi| < 0.075$  deg



## 3<sup>rd</sup> harmonic cavities in FLASH

transverse effects due to rf

a) cavity

rf focusing and rf kick (due to misalignment) are **comparable to TESLA cavity**

for large gamma:  $V_x \rightarrow \frac{x'}{2} V_{acc}$  (independent on frequency)

b) couplers (scaling)

main coupler:  $P = \int (\mathbf{E} \times \mathbf{B}) d\mathbf{A} \rightarrow E_{\perp}^2 r_{\text{pipe}}^2 \propto P \propto V_{acc}$

$$V_{\perp} = \int (\mathbf{E} + \mathbf{v} \times \mathbf{B})_{\perp} dz \propto E_{\perp} \cdot \lambda \propto \sqrt{P} \cdot \frac{\lambda}{r_{\text{pipe}} \propto \lambda} \propto \sqrt{V_{acc}}$$

**4x3rd harm.  $\sim 4\sqrt{4\text{MV}} \leftrightarrow 2\sqrt{16\text{MV}} \sim 2\text{xTESLA}$**

HOM coupler:

**?**  $E_{\perp} \propto E_{acc}$   
 $V_{\perp} \propto E_{acc} \cdot \lambda \propto \lambda$  **4x3rd harm.  $\sim 1.33 \text{ x TESLA}$**



## 3<sup>rd</sup> harmonic cavities in FLASH

transverse effects due to wakes

a) cavity

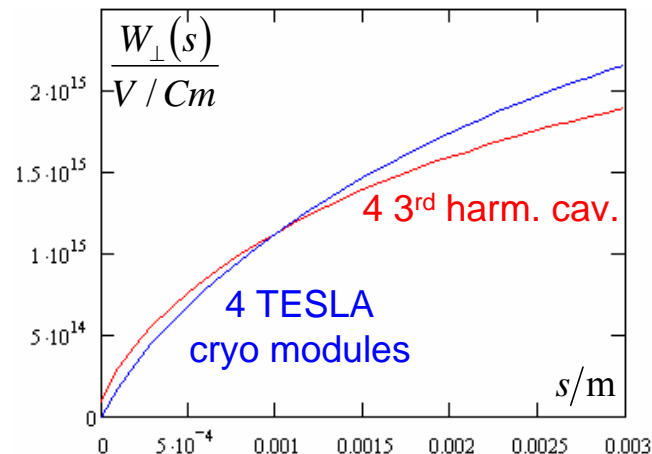
wake field / length scales with fundamental mode frequency \*\* 3

wake field / **cavity** scales with fundamental mode frequency \*\* 2

→ kick of 4 third harmonic cavities corresponds to kicks of 36 TESLA cavities (all between 118 and 134 MeV with a localization that is not long compared to the betatron wavelength)

I. Zagorodnov: TESLA Report 2003-19 (TESLA module)

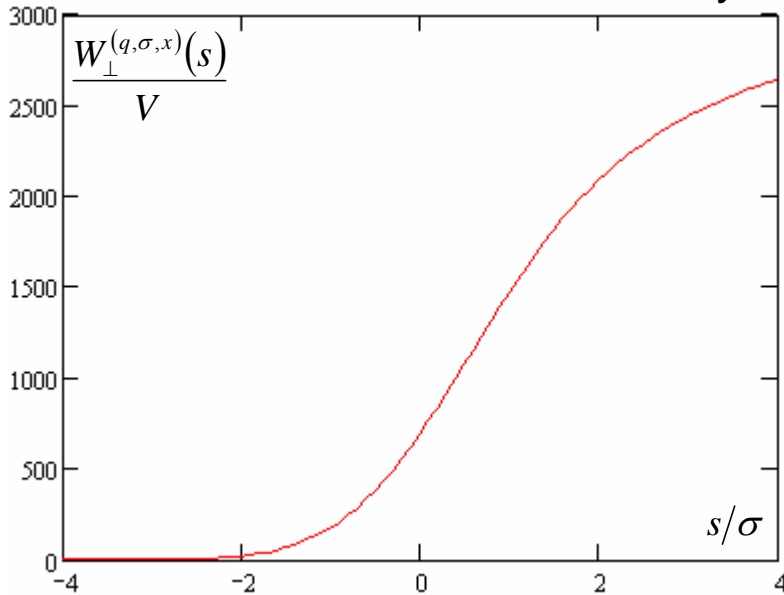
TESLA Report 2004-01 (LOLA & 3<sup>rd</sup> harm. cavity)



### 3<sup>rd</sup> harmonic cavities in FLASH

single bunch effect for  $q = 1\text{ nC}$ ,  $\sigma = 2.4\text{ mm}$ ,  $x = 1\text{ mm}$   
 ( $I = 50\text{ A}$  compression to 2.5 kA)

transv. wake of 3<sup>rd</sup> harm. cavity



$$av\{W_{\perp}\} = \frac{1}{q} \int W_{\perp}(s) \lambda(s) ds = 0.8\text{ kV}$$

$$rms\{W_{\perp}\} = \sqrt{\frac{1}{q} \int (W_{\perp}(s) - av\{W_{\perp}\})^2 \lambda(s) ds} = 0.59\text{ kV}$$

rms centroid kick:

$$\sqrt{\overline{x'_c x'_c}} \approx \frac{rms\{W_{\perp}^{q, \sigma, x}\}}{V_{\parallel}} = \frac{0.59\text{ kV}}{118\text{ MV}} = 5\text{ }\mu\text{rad}$$

emittance growth due to centroid kick:  
 (for  $\overline{x'_c x'_c} = 0$ ,  $\overline{x_c x_c} = 0$ )

$$\tilde{\varepsilon} \approx \varepsilon \sqrt{1 + \frac{\beta}{\varepsilon} \overline{x'_c x'_c}}$$

$$\varepsilon = \frac{2\text{ }\mu\text{m}}{\gamma_L = 235} \quad \beta \approx 20\text{ m} \quad \rightarrow \tilde{\varepsilon} \approx 1.03\text{ }\varepsilon$$

$$\varepsilon = \frac{1\text{ }\mu\text{m}}{\gamma_L = 235} \quad \rightarrow \tilde{\varepsilon} \approx 1.06\text{ }\varepsilon$$



# Higher Order Mode Measurements in Superconducting Accelerating Cavities

22-23 January 2007

DESY, Hamburg

## Asymptotic and rms Kicks due to HOMs in 3.9 GHz cavity

**Id:** 18

**Place:** DESY, Hamburg

Notkestrasse 85  
22607 Hamburg  
GERMANY

Room: Bldg. 24, Rm 200

**Starting date:** 22-Jan-2007 14:00

**Duration:** 25'

**Primary Authors:** Dr. WANZENBERG, Rainer (DESY)

**Presenters:** Dr. WANZENBERG, Rainer

**Material:**  Slides

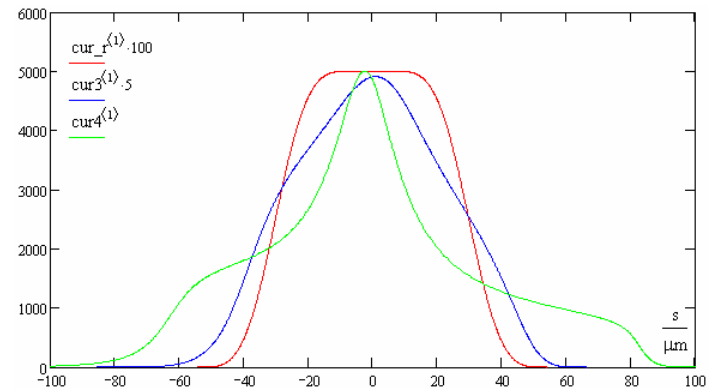
## Conclusions

- The kicks due to HOMs in the 3.9 GHz cavity have been calculated for a constant offset of all bunches
- Analytic formulas have been obtained for different cases
  1. Asymptotic kick
  2. Average and rms kick
  3. Average and rms kick with no damping
  4. Average and rms kick with no damping and many bunches  $N \rightarrow \infty$
- Even a small dumping constant seems to be acceptable, if only short bunch trains are used (say  $< 100$  bunches) Further investigations are required
- The operation with long bunch trains requires HOM dampers
- A possible solution if one hits a HOM resonance:  
a small change in the bunch-to-bunch spacing (one 1.3 GHz bucket), say 3903 instead of 3900 free 3.9 GHz buckets gives a large change of phase  $\delta$ )



possible working point

- 1.3 GHz system: 130 MV @ 0 deg --> 130 MeV  
447.5 MV @ 0.74 deg --> 577.5 MeV
- 3.9 GHz system: 97.3 MV @ -142.2 deg --> 500 MeV
- BC2 r56 = -103.5 mm --> compression factor = 20
- 1.3 GHz system: 1500 MV @ 0 deg --> 2000 MeV
- BC3 r56 = -20.7 mm --> compression factor = 5



sensitivity (10% change of compression)

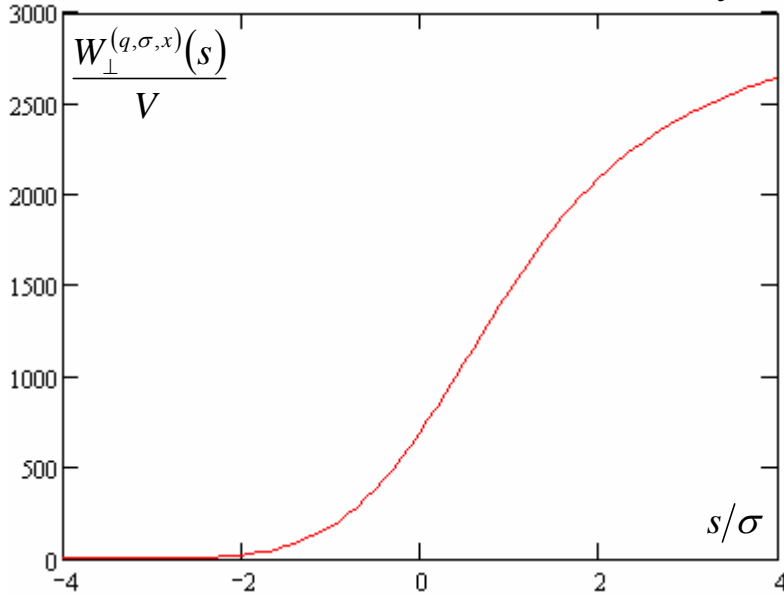
- 1.3 GHz system before BC2:  $|\Delta V| < 0.19$  MV,  $|\Delta\phi| < 0.023$  deg
- 3.9 GHz system:  $|\Delta V| < 0.071$  MV,  $|\Delta\phi| < 0.060$  deg



# 3<sup>rd</sup> harmonic cavities in XFEL

single bunch effect for  $q = 1\text{nC}$ ,  $\sigma = 2.4\text{ mm}$ ,  $x = 1\text{ mm}$   
 ( $I = 50\text{ A}$  compression to 5 kA), 12 / 24 cavities

transv. wake of 3<sup>rd</sup> harm. cavity



$$av\{W_{\perp}\} = \frac{1}{q} \int W_{\perp}(s)\lambda(s)ds = 2.4 / 4.8\text{ kV}$$

$$rms\{W_{\perp}\} = \sqrt{\frac{1}{q} \int (W_{\perp}(s) - av\{W_{\perp}\})^2 \lambda(s)ds} = 1.76 / 3.5\text{ kV}$$

rms centroid kick:

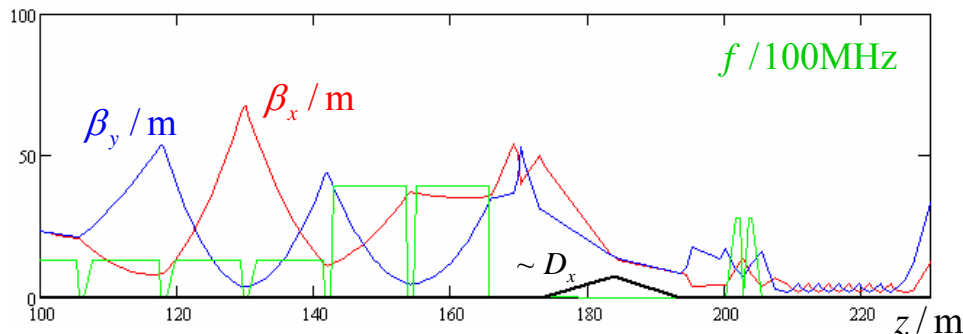
$$\sqrt{\overline{x'_c x'_c}} \approx \frac{rms\{W_{\perp}^{q,\sigma,x}\}}{V_{\parallel}} = \frac{\dots}{500\text{ MV}} = 3.5 / 7.0\ \mu\text{rad}$$

emittance growth due to centroid kick:  $\tilde{\varepsilon} \approx \varepsilon \sqrt{1 + \frac{\beta}{\varepsilon} \overline{(x'_c x'_c)}}$   
 (for  $\overline{x_c x'_c} = 0$ ,  $\overline{x_c x_c} = 0$ )

$$\varepsilon = \frac{1\ \mu\text{m}}{\gamma_L = 978}$$

$$\beta \approx 40\text{ m}$$

$$\rightarrow \tilde{\varepsilon} \cdot \gamma_L \approx 1.22 / 1.72\ \mu\text{m}$$



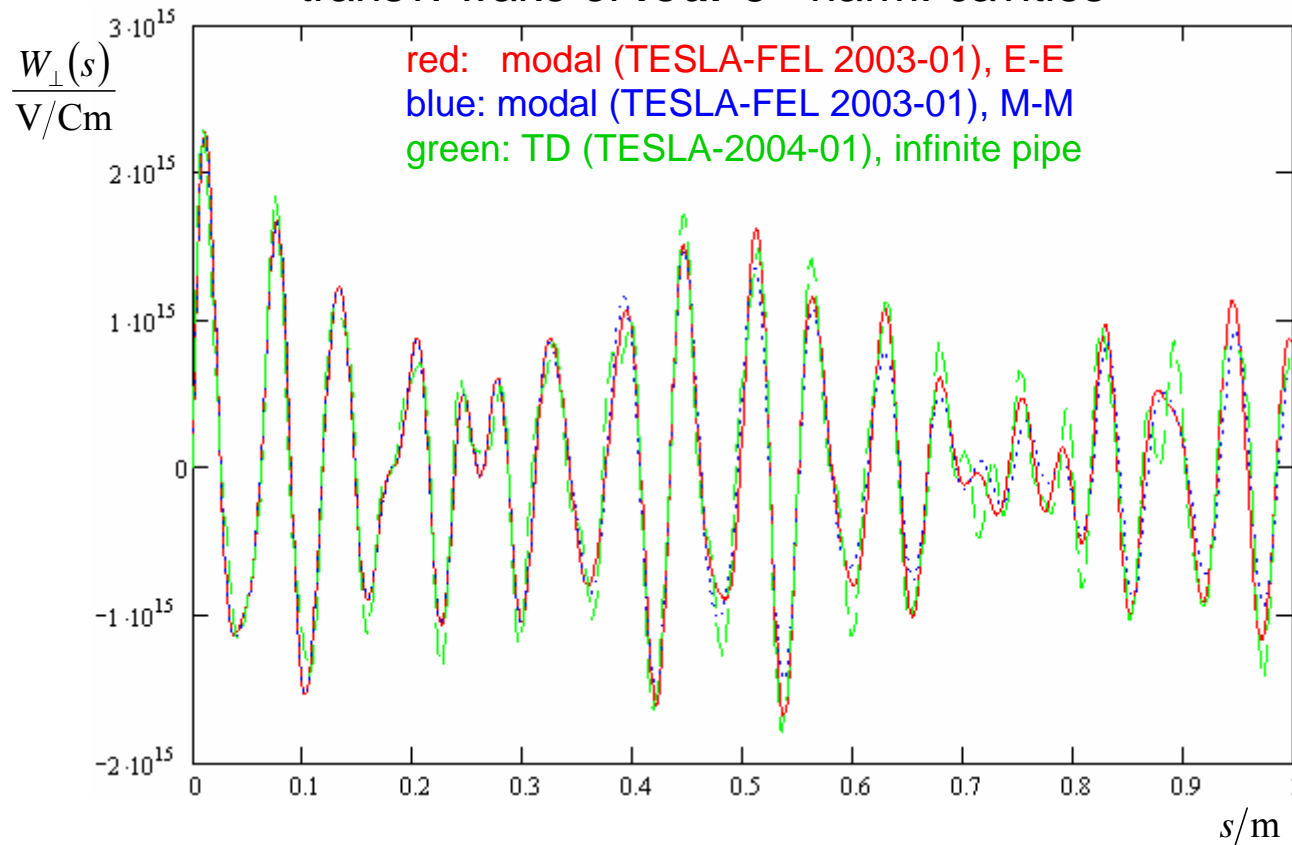
(BC1@400MeV  $\rightarrow \varepsilon = 1.27/1.85$ )





short range ---> longer ---> longer ---> multi-bunch

### transv. wake of **four** 3<sup>rd</sup> harm. cavities

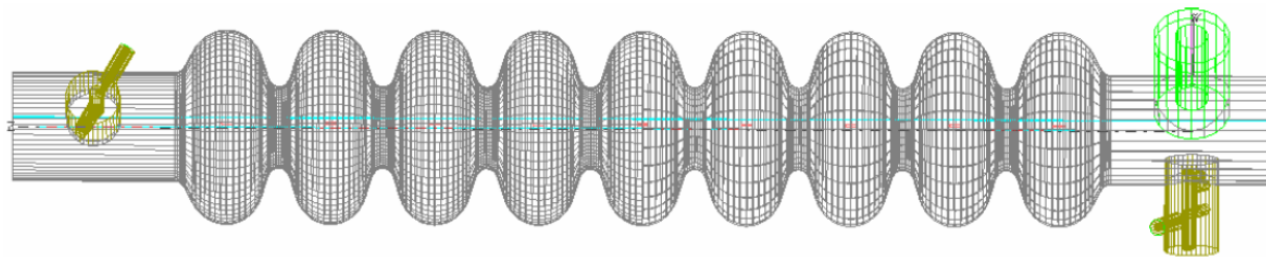


bunch distance: 30 m or 1nC & 10mA  
60 m 5mA  
300 m 1mA



# Higher Order Modes of a 3<sup>rd</sup> Harmonic Cavity with an Increased End-cup Iris

T. Khabibouline N. Solyak R. Wanzenberg



$r_{\text{pipe}} = 20 \text{ mm}$   
cutoff frequencies:

**dipoles**

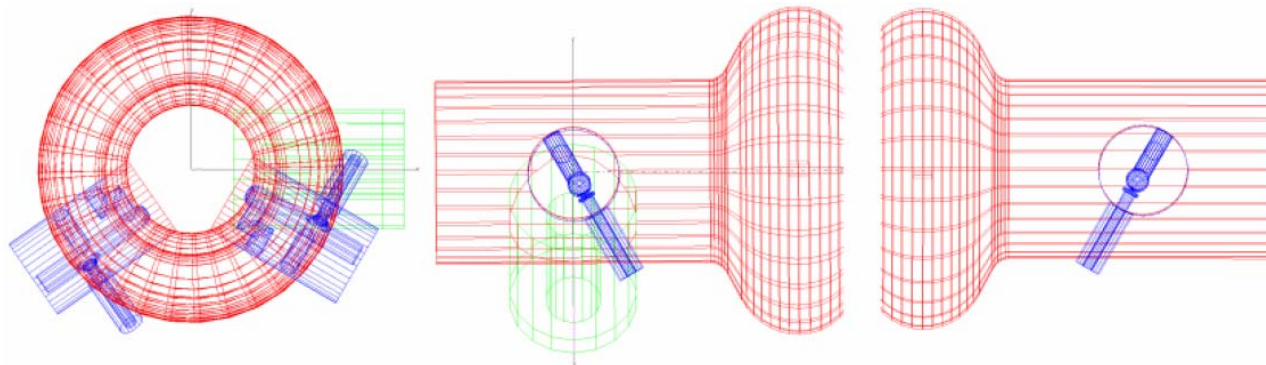
**4.4 GHz (TM)**

9.1 GHz (TE)

monopole

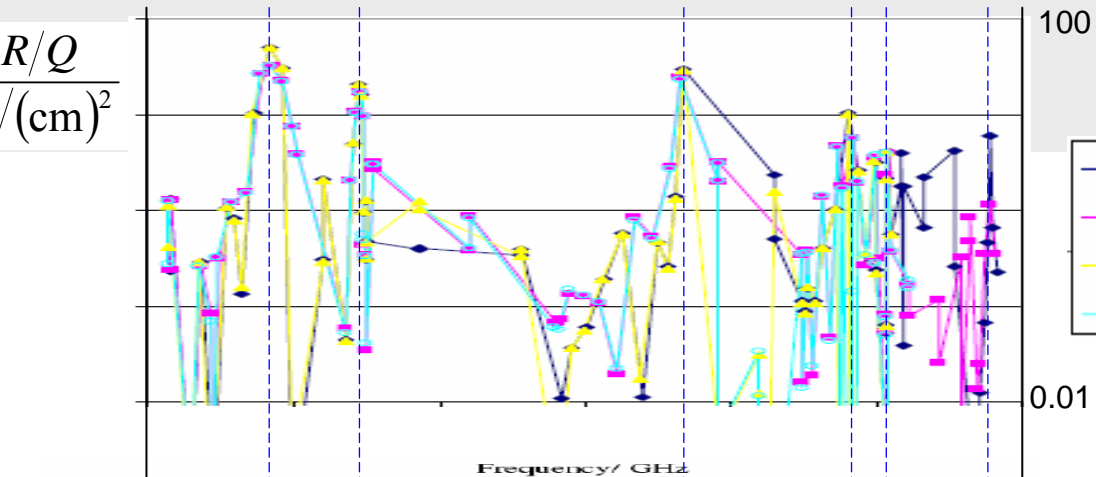
5.7 GHz (TM)

9.1 GHz (TE)

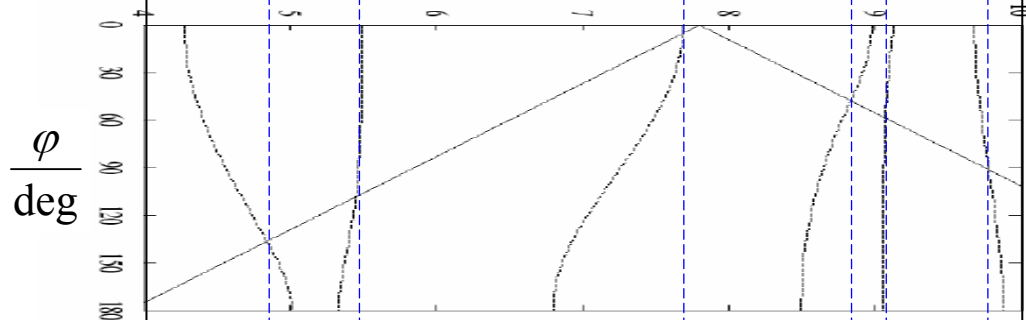


$$\frac{R/Q}{\Omega/(\text{cm})^2}$$

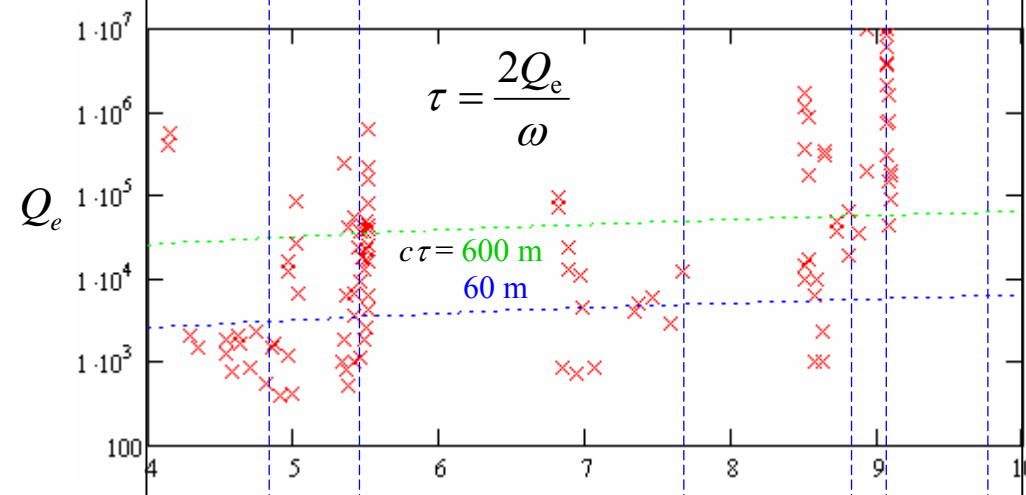
shunt impedance  
of dipole modes



phase advance  
in periodic structure  
of middle cells



quality  
(HFSS calc.  
with ee or mm  
boundary cond.)



$$\sum_{f_i < f} \left( \frac{R}{Q} \right)_i$$

EE/MM HFSS

Frequency / GHz

phase advance  
in periodic structure  
of middle cells

$\frac{\phi}{\text{deg}}$

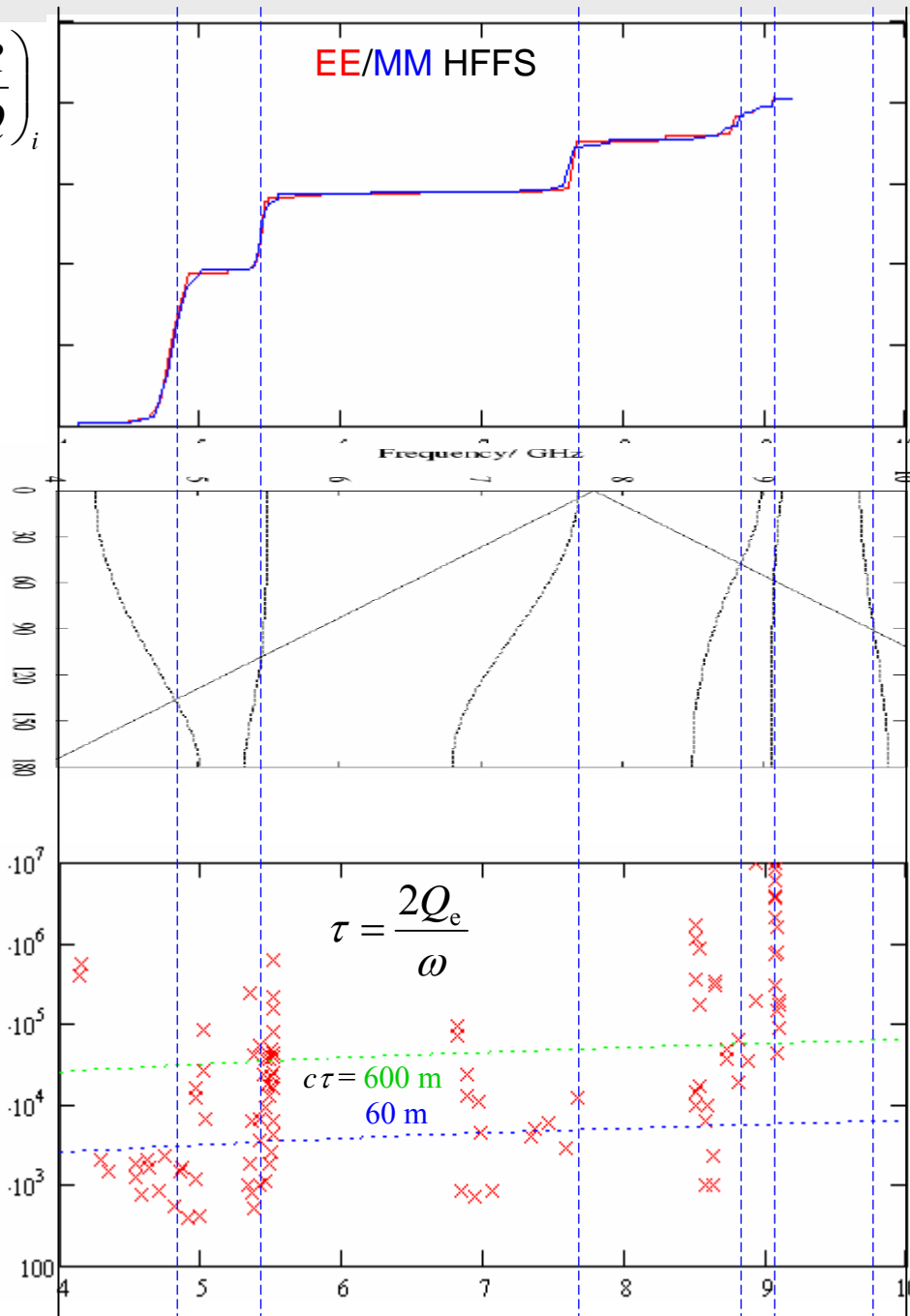
quality  
(HFSS calc.  
with ee or mm  
boundary cond.)

$Q_e$

$$\tau = \frac{2Q_e}{\omega}$$

$$c\tau = 600 \text{ m}$$

$$60 \text{ m}$$



f / GHz



$$\sum_{f_i < f} \left( \frac{R}{Q} \right)_i$$

EE/MM HFSS

phase advance  
in periodic structure  
of middle cells

$\frac{\varphi}{\text{deg}}$

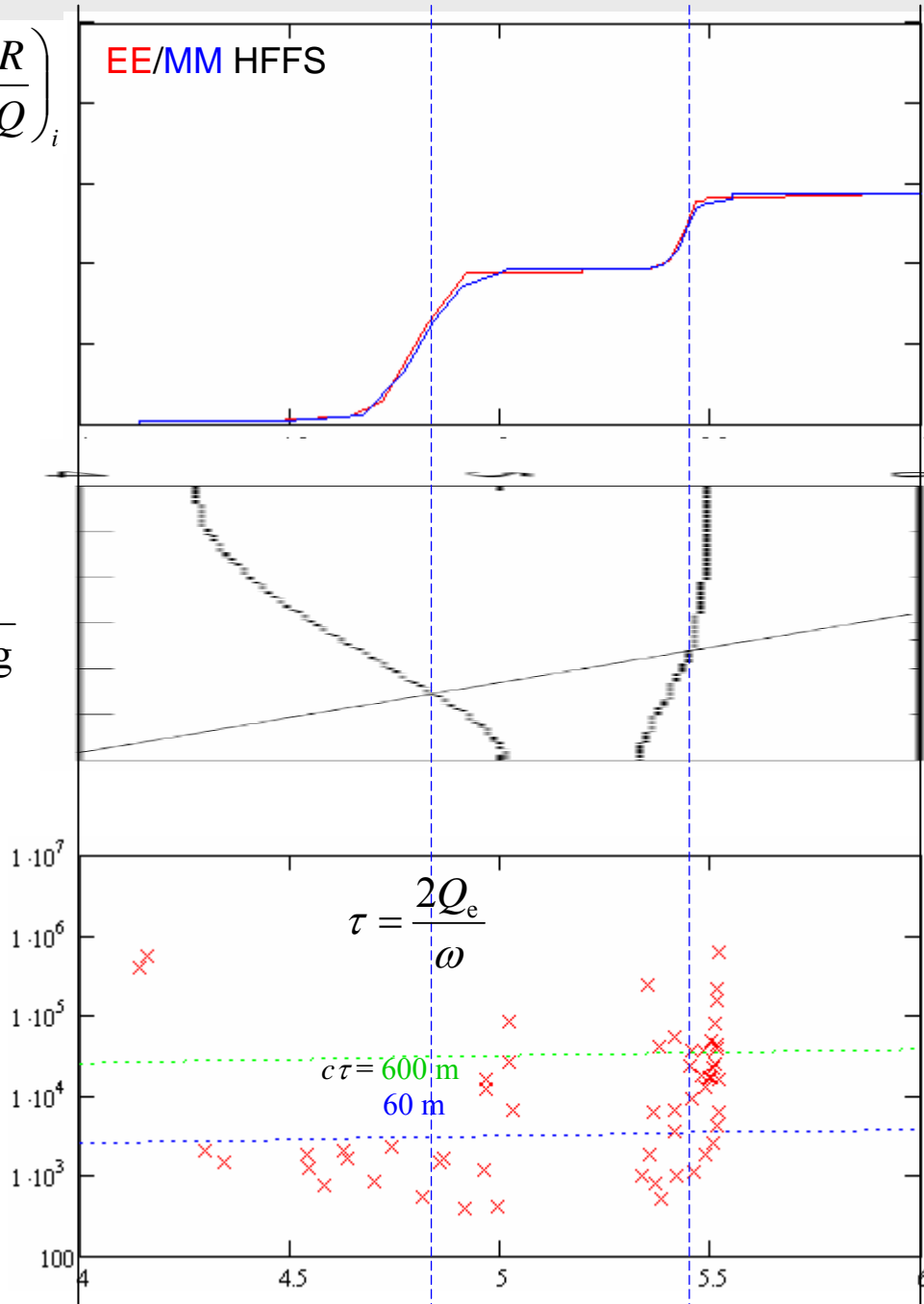
quality  
(HFSS calc.  
with ee or mm  
boundary cond.)

$Q_e$

$$\tau = \frac{2Q_e}{\omega}$$

$$c\tau = 600 \text{ m}$$

$$60 \text{ m}$$



f / GHz



$$\sum_{f_i < f} \left( \frac{R}{Q} \right)_i$$

EE/MM HFFS

phase advance  
in periodic structure  
of middle cells

$$\frac{\varphi}{\text{deg}}$$

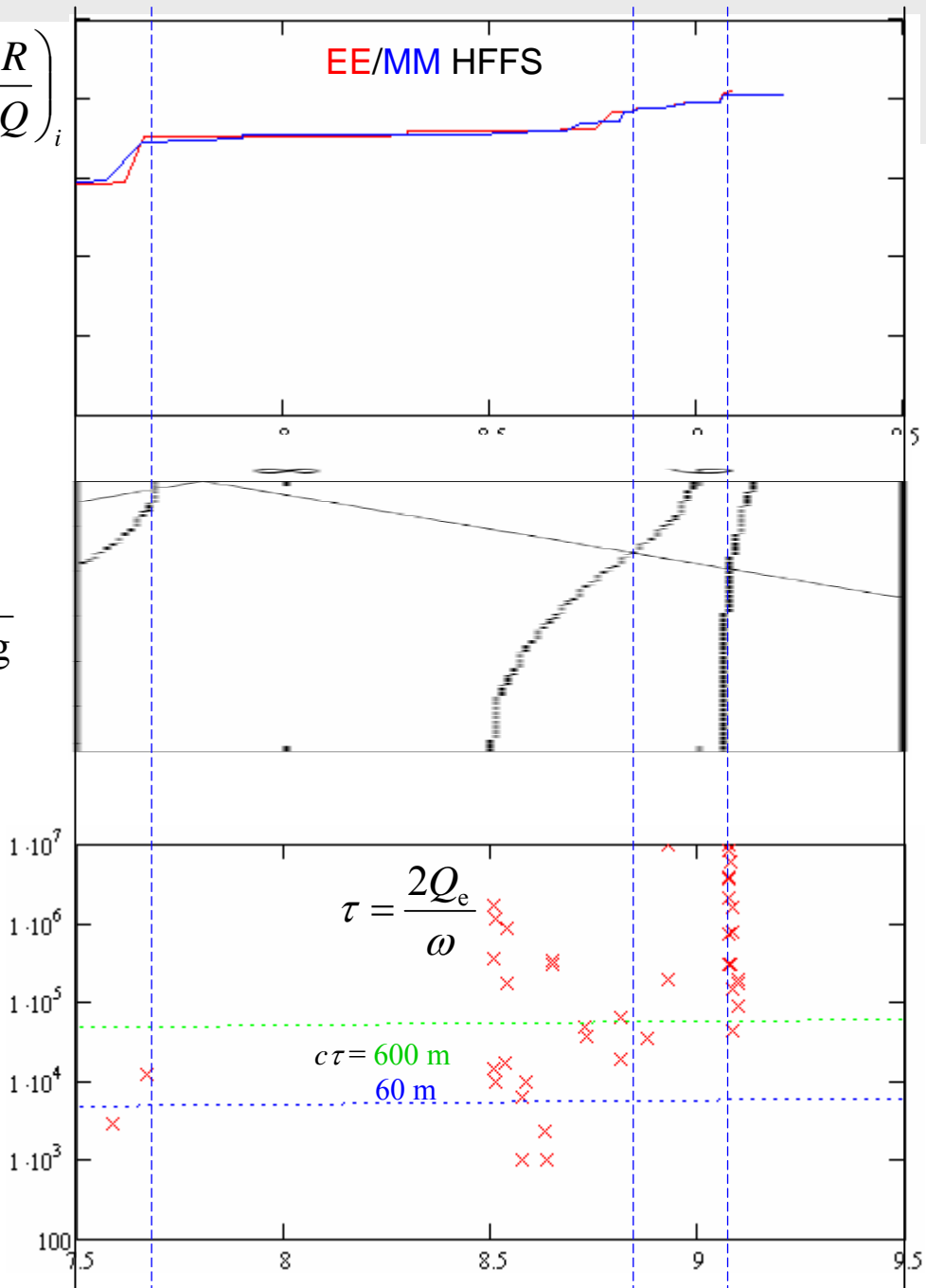
quality  
(HFSS calc.  
with ee or mm  
boundary cond.)

$$Q_e$$

$$\tau = \frac{2Q_e}{\omega}$$

$$c\tau = 600 \text{ m}$$

$$60 \text{ m}$$



f / GHz



## XFEL summary

**number of cavities** & possible **gradient** have to be determined  
(so far  $\geq 100$  MV assumed for optimization of WP)

the knowledge of limitations (as gradient, r56 range etc.)  
is substantial for further optimizations

single bunch: significant growth of projected emittance  
(for 1 mm beam offset to structure axis)  
→ **alignment & optics**

all dipole modes above  $f_c$ , most modes are well damped  
no investigation of multi-bunch effects (so far)

