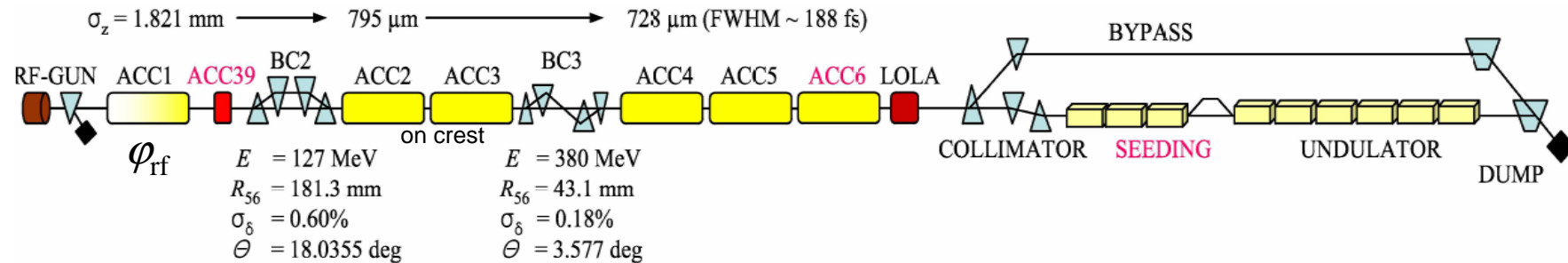
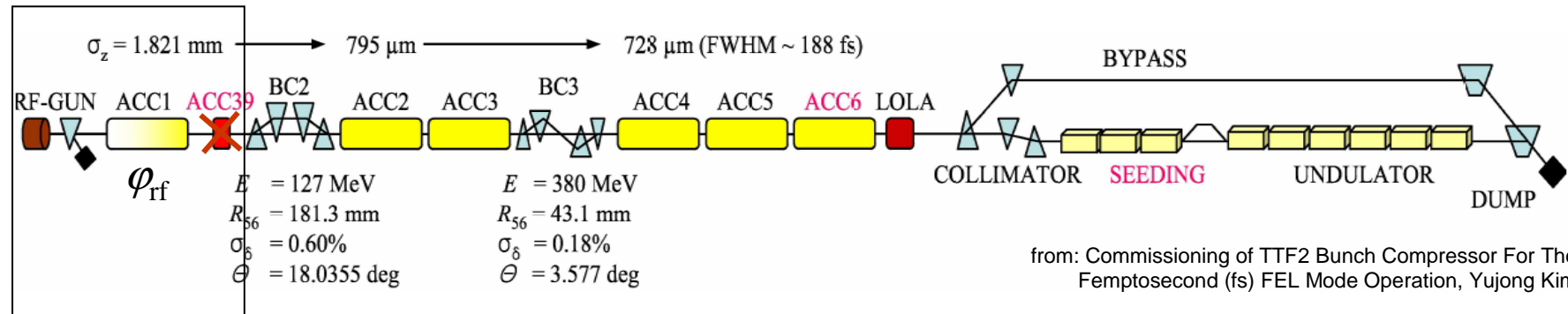


CSR Calculation for TTF2



1. method
2. no CSR, $\varphi_{\text{rf}} = 8 \text{ deg}$
3. CSR "projected", optics = option 1 & 2, $\varphi_{\text{rf}} = 8 \text{ deg}$
4. CSR "projected", optics = option 1 & 2, $\varphi_{\text{rf}} = 12 \text{ deg}$
5. CSR "projected", optics = option 1, $\varphi_{\text{rf}} = 7 \text{ deg}$
6. some LOLA pictures
7. conclusion / remarks

1. method



ASTRA distribution (xfel.1200.001.txt)
 1nC, 200000 particles

- 1) extract rf (longitudinal momentum)
- 2) add ACC1 rf as required

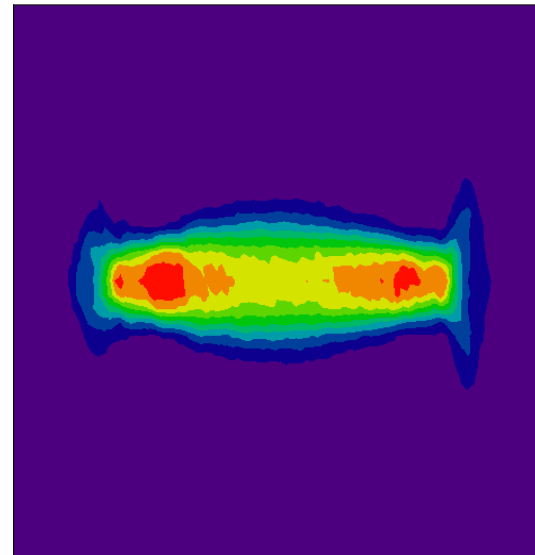
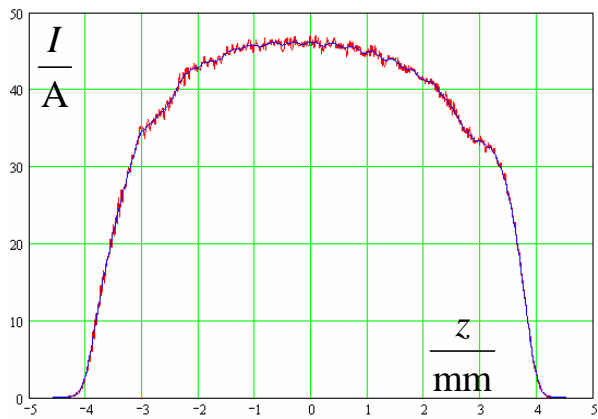
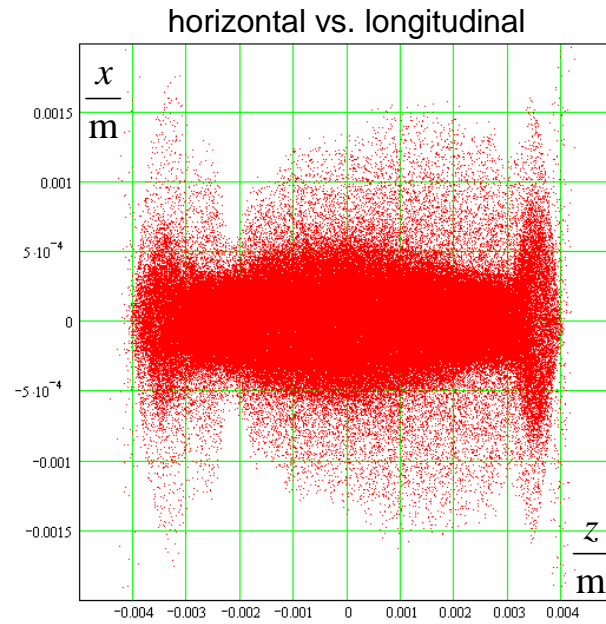
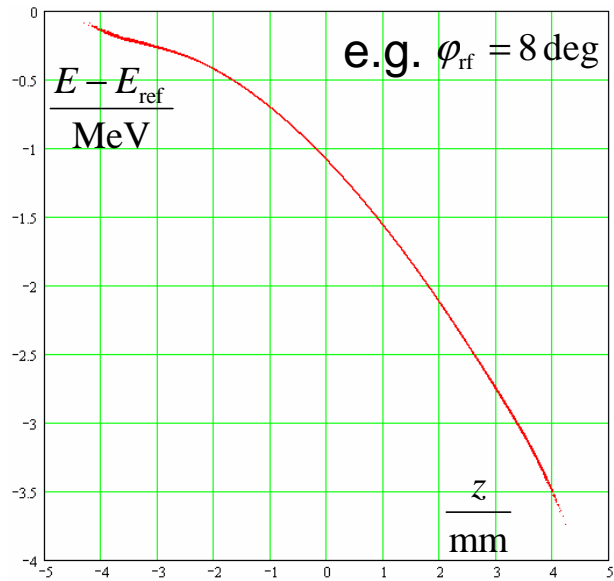
$$V(s) = V_{\text{acc}} \frac{\cos(ks + \varphi_{\text{rf}})}{\cos \varphi_{\text{rf}}}$$

- 3) calculate Twiss parameters from core of bunch (particles between $\pm 2\text{mm}$)
 use transport matrix for matching to required values (Nina Golubeva)

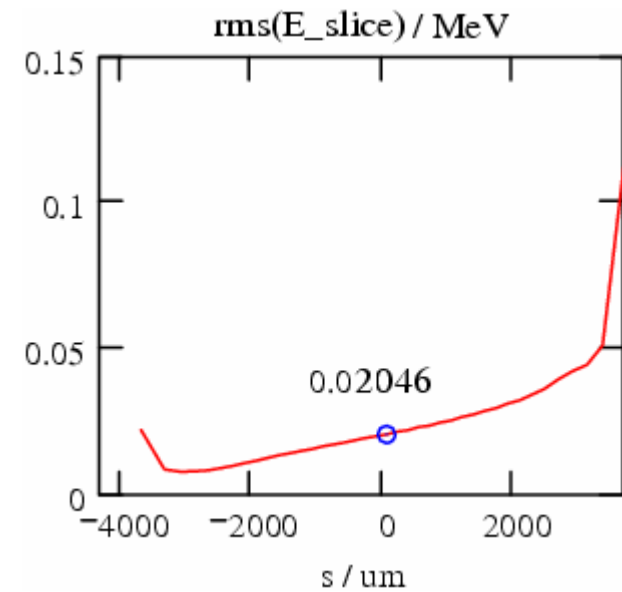
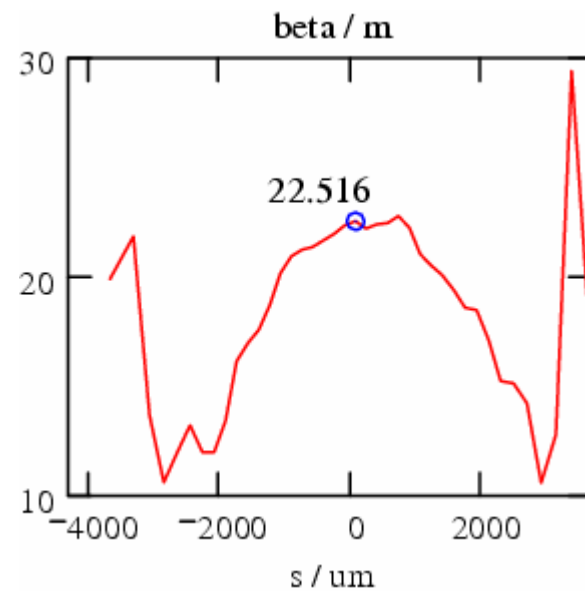
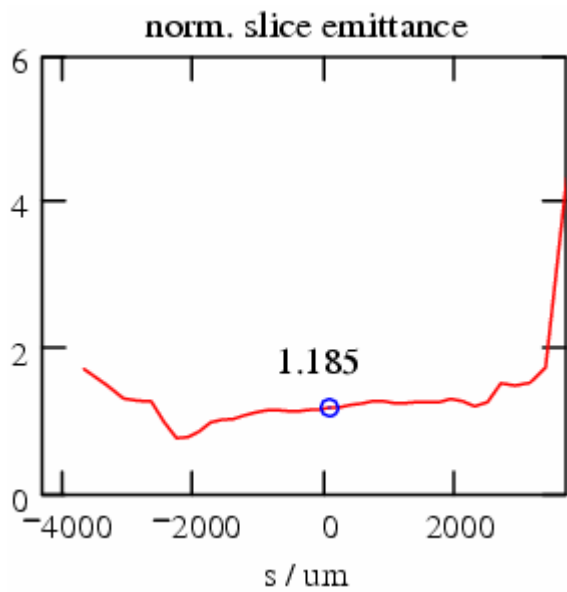
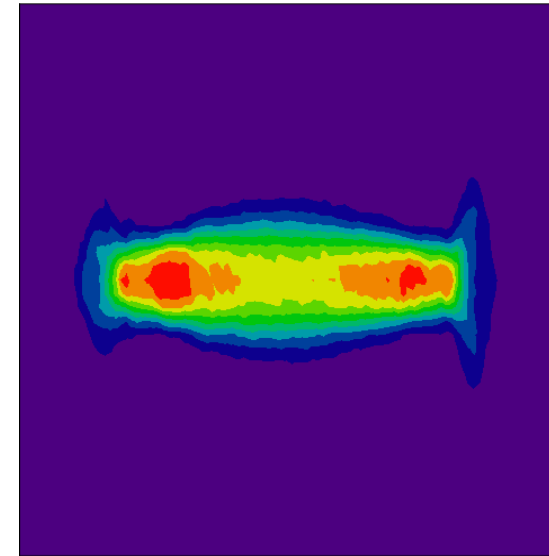
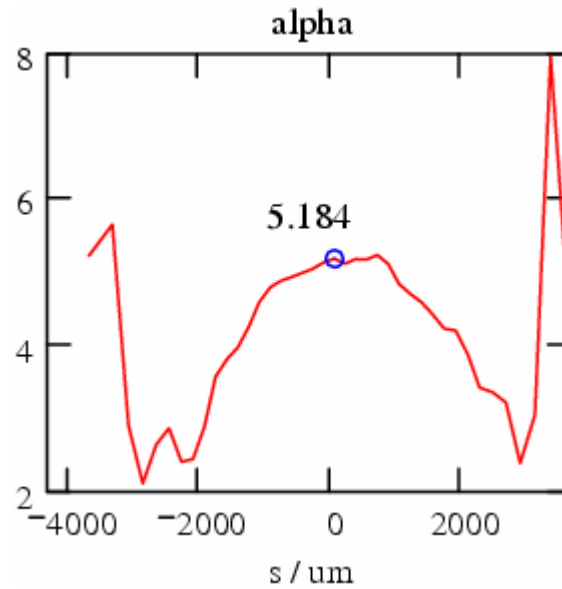
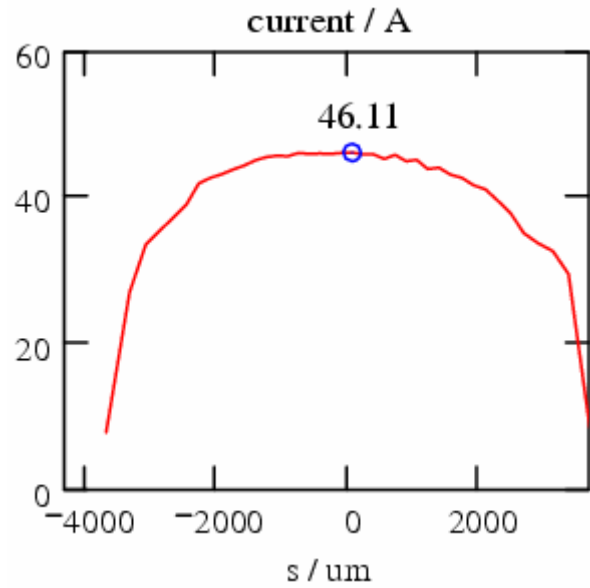
$$\alpha_x = 4.619 \quad \beta_x = 20.174 \text{ m}$$

$$\alpha_y = -0.012 \quad \beta_y = 2.809 \text{ m}$$

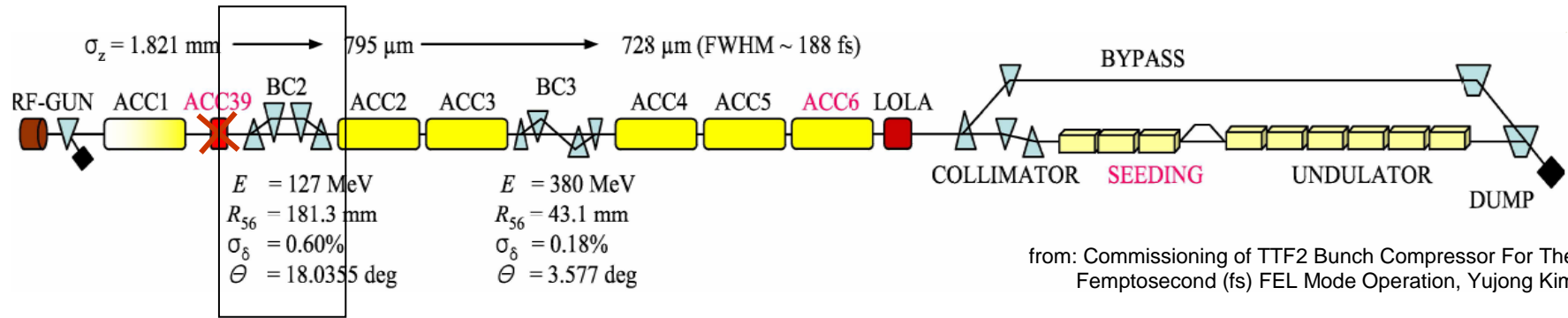
particles at entrance of BC1



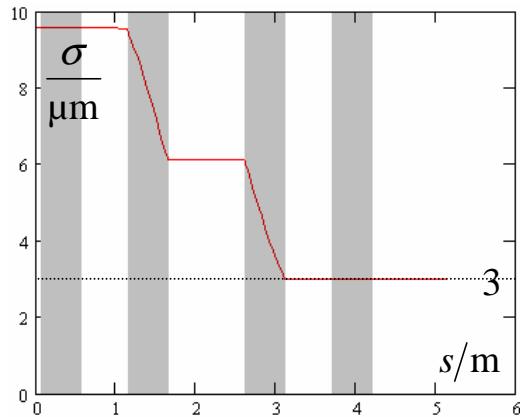
particles at entrance of BC1 ("slices" with 5000 particles)



method ...

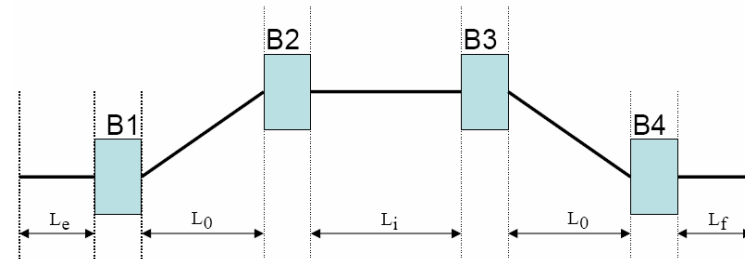


4) calculate BC2 with projected method
sub-bunch length:



reference plane = 1 m after BC

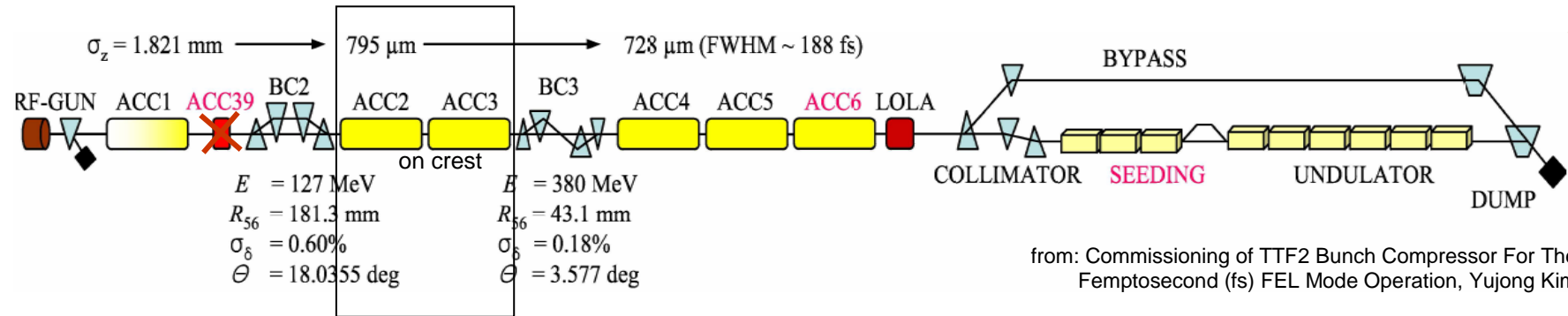
BC2 chicane description



Parameters	Symbol	Value	Unit
Bend magnet length (projected)	L_b	0.5	m
Drift length B1 \rightarrow B2 and B3 \rightarrow B4 (projected)	L_0	0.5	m
Drift length B2 \rightarrow B3	L_i	0.963	m
Pre chicane drift	L_e	0.1	m
Post chicane drift	L_f	0.1	m
Bend radius of each dipole magnet	R	2.40486	m
Bending Angle	Φ	12	deg
Momentum compaction	$ R_{56} $	76.17403	mm
2 nd order momentum compaction	$ T_{566} $	118.9555	mm
Total projected length of chicane	L_{tot}	4.163	m
Full gap height pole/chamber	g / h	25.0 / 8.0	mm

$R = 1.614955 \text{ m}$
 $r_{56} = -0.181496 \text{ m}$
 $t_{566} = 0.296575 \text{ m}$

method ...



5) transformation from exit BC2 to entrance BC3:

longitudinal: add rf-field and wake of two modules

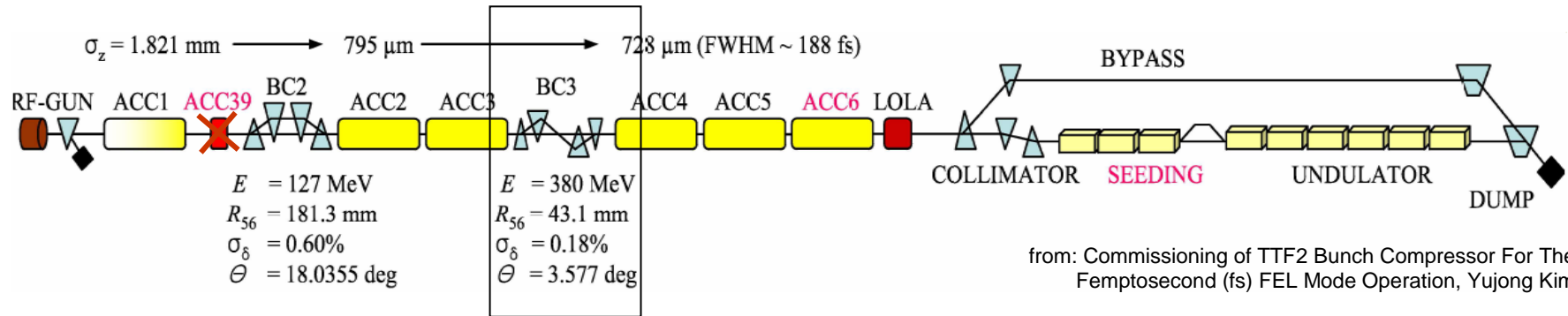
transverse: use transport matrix

option 1: $\alpha_x = -0.284$, $\beta_x = 0.976 \text{ m}$ $\mu_x = 0.328 * 2\pi$ to $\alpha_x = -0.284$, $\beta_x = 0.976 \text{ m}$ $\mu_x = 1.427 * 2\pi$
 $\alpha_y = 2$, $\beta_y = 31.037 \text{ m}$ $\mu_y = 1.427 * 2\pi$ $\alpha_y = 2$, $\beta_y = 30.021 \text{ m}$ $\mu_y = 1.465 * 2\pi$

option 2: ...

to $\alpha_x = -0.495$, $\beta_x = 17.150 \text{ m}$ $\mu_x = 1.478 * 2\pi$
 $\alpha_y = -0.152$, $\beta_y = 19.719 \text{ m}$ $\mu_y = 1.830 * 2\pi$

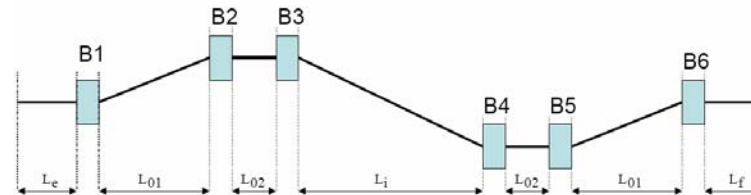
method ...



6) calculate BC3 with projected method
sub-bunch length = 3 μm

reference plane = 1 m after BC

BC3 chicane description



Parameters	Symbol	Value	Unit
Bend magnet length (projected)	L_b	0.3	m
Drift length B1 \rightarrow B2 and B5 \rightarrow B6 (projected)	L_{01}	3.6412	m
Drift length B2 \rightarrow B3 and B4 \rightarrow B5 (projected)	L_{02}	0.5	m
Drift length B3 \rightarrow B4	L_i	7.5824	m
Pre chicane drift	L_e	0.1	m
Post chicane drift	L_f	0.1	m
Bend radius of each dipole magnet	R	11.46046	m
Bending Angle	Φ	1.5	deg
Momentum compaction	$ R_{56} $	10.60772	m
2 nd order momentum compaction	$ T_{566} $	15.92241	m
Total projected length of chicane	L_{tot}	17.4648	m
Full gap height pole/chamber	g / h	25.0 / 8.0	mm

$R = 5.695 \text{ m}$

$r_{56} = -0.041226 \text{ m}$

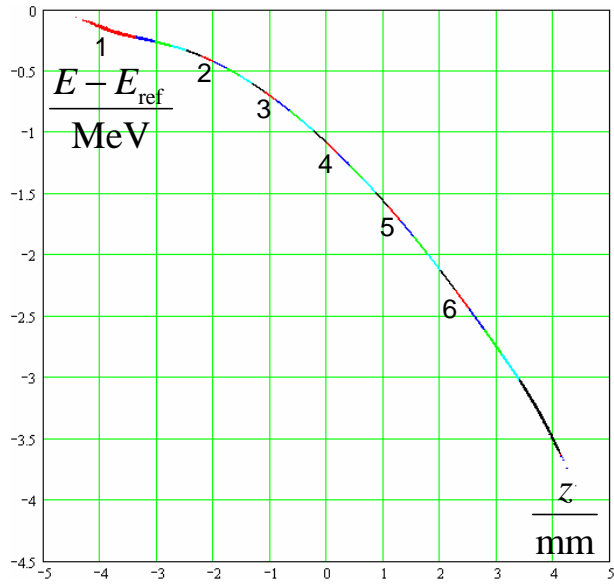
$r_{566} = 0.064860 \text{ m}$

2. no CSR

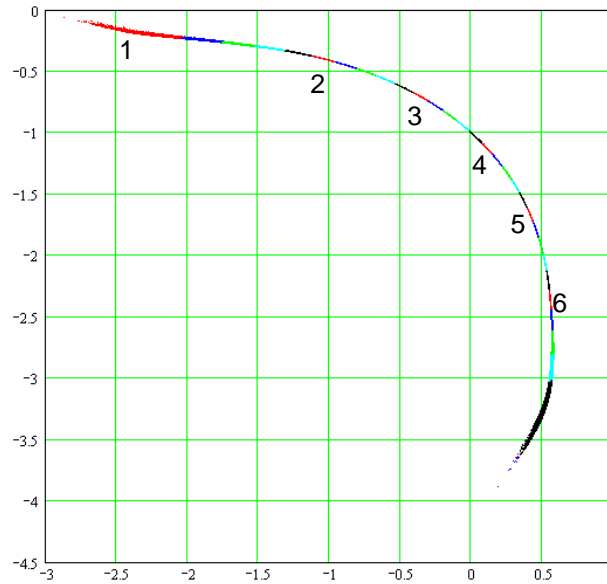
optics = option 1

$\varphi_{rf} = 8 \text{ deg}$

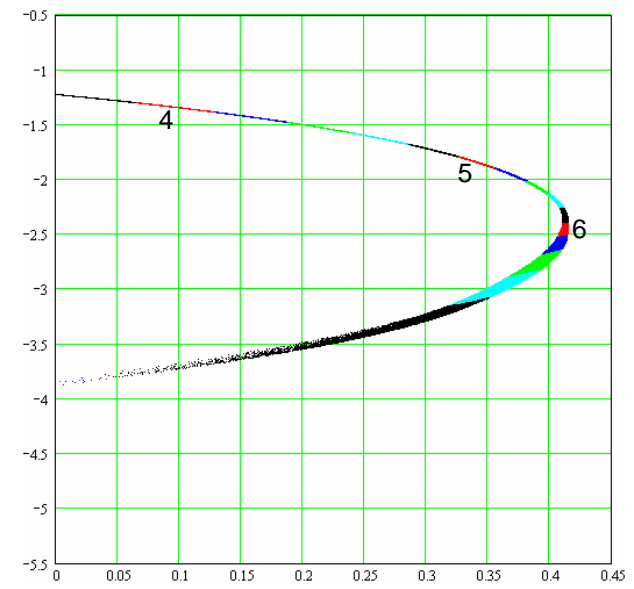
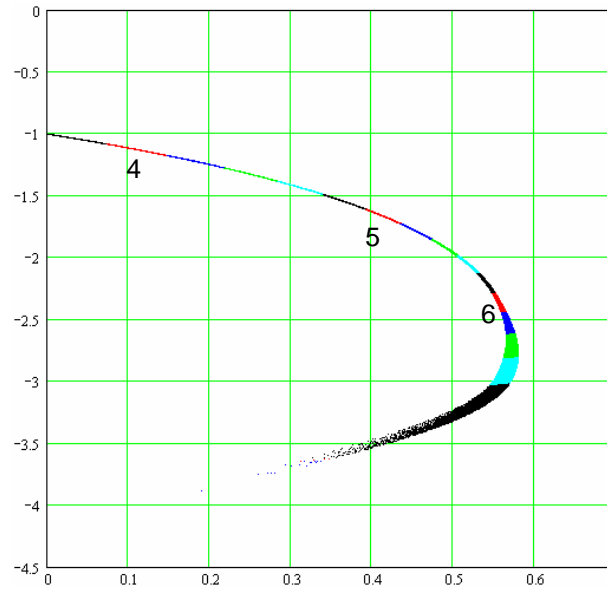
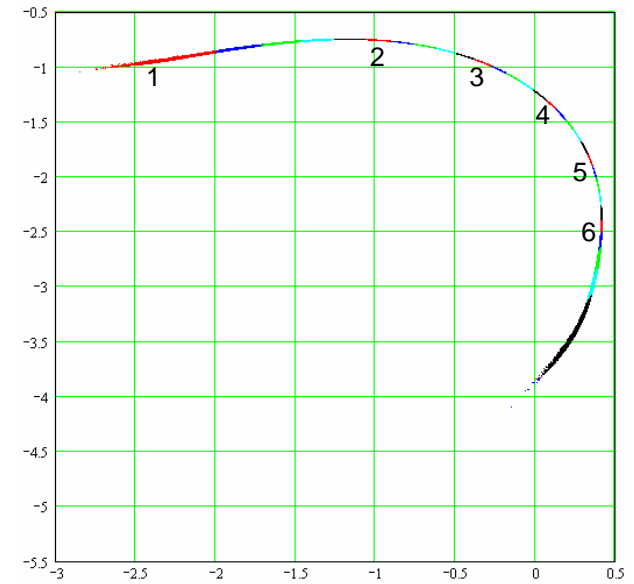
before BC2



1m after BC2



1m after BC3



no CSR

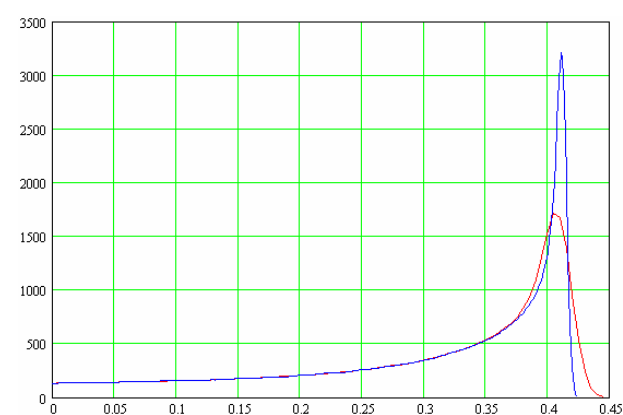
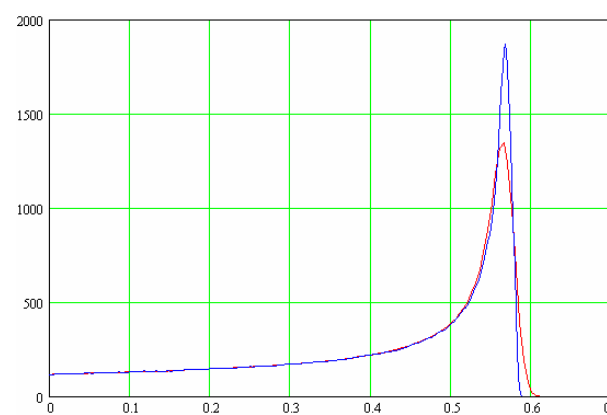
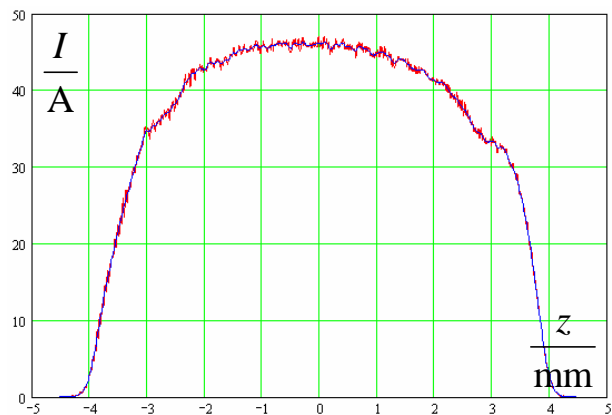
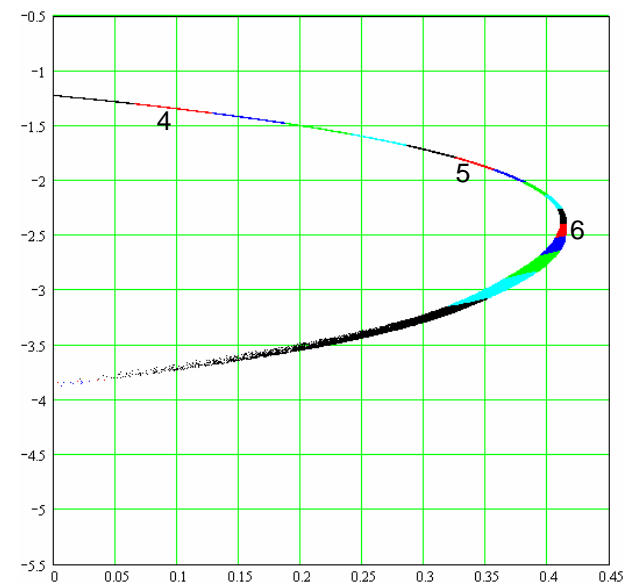
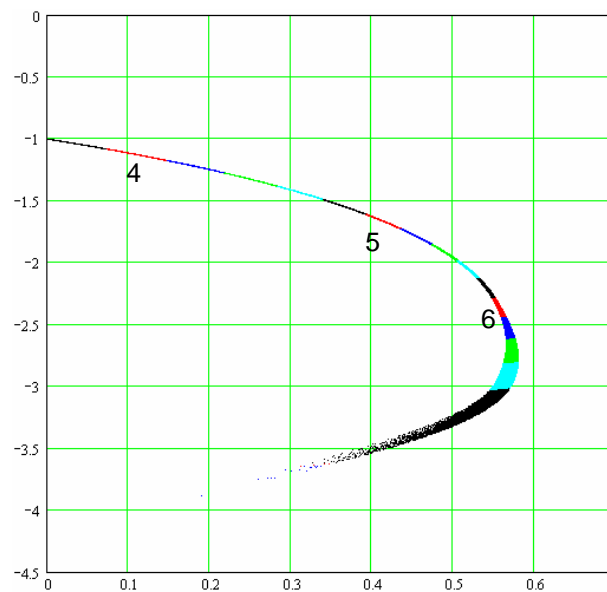
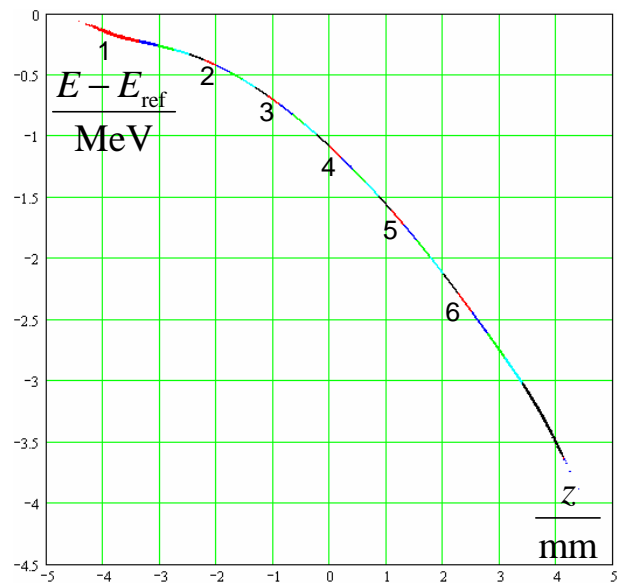
optics = option 1

$\varphi_{rf} = 8 \text{ deg}$

before BC2

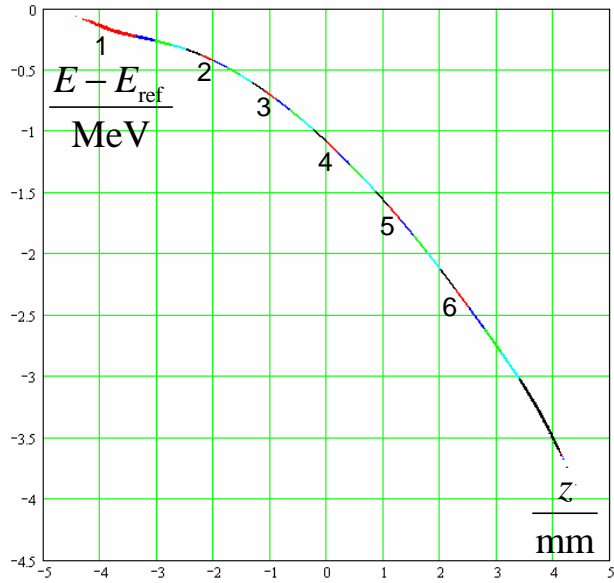
1m after BC2

1m after BC3

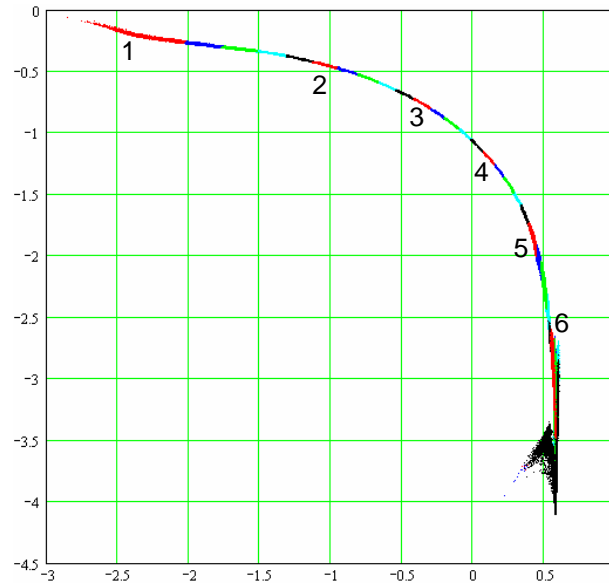


3. CSR “projected” optics = option 1 $\phi_{rf} = 8 \text{ deg}$

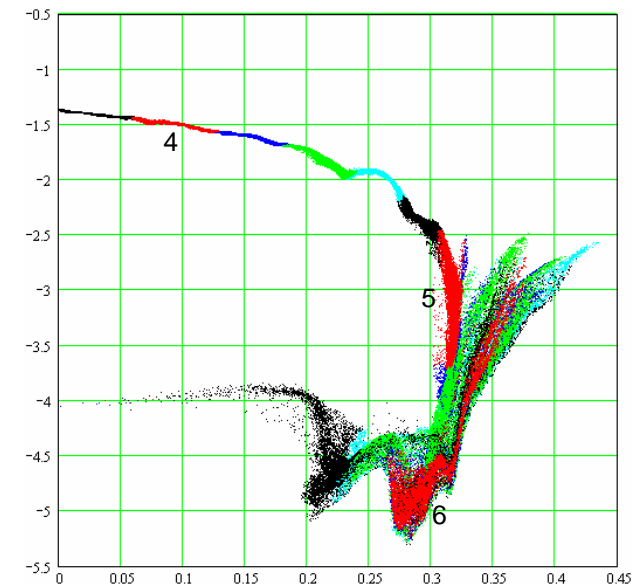
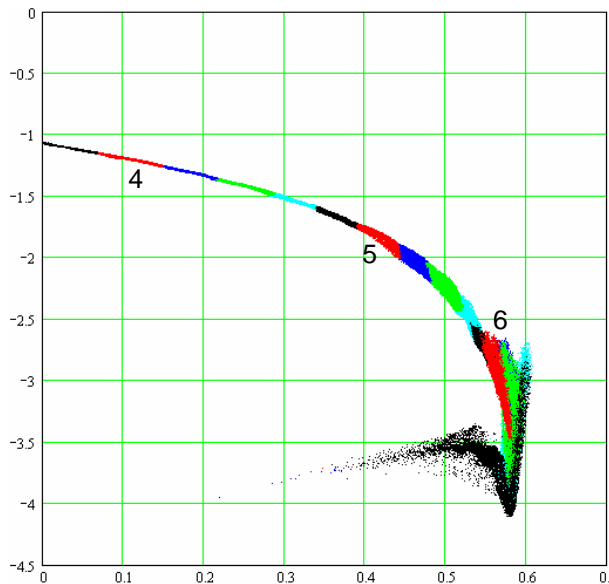
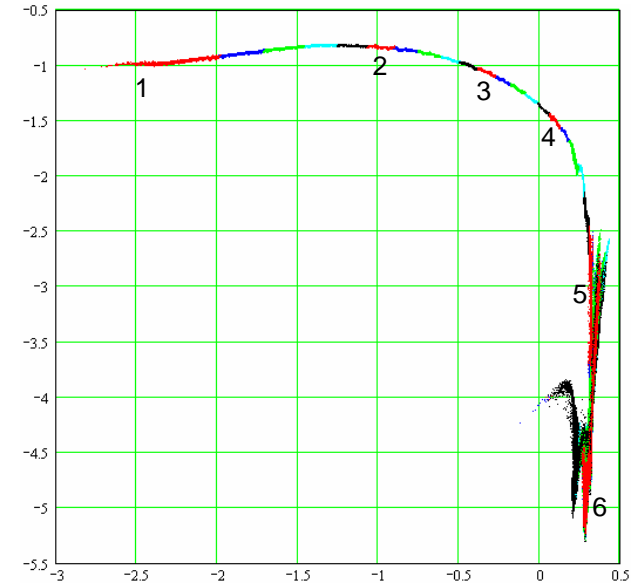
before BC2



1m after BC2



1m after BC3



CSR "projected"

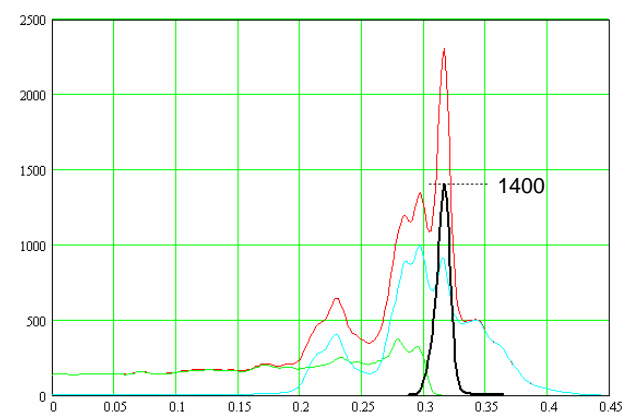
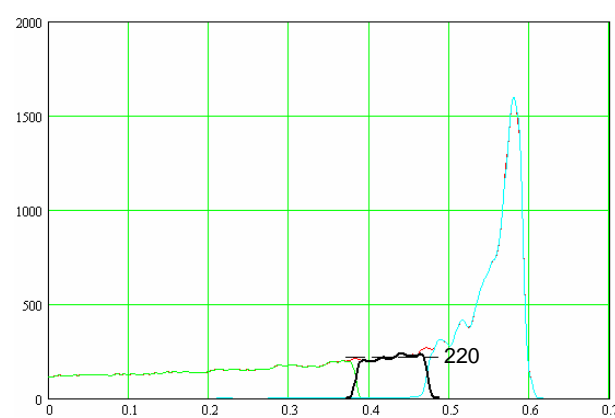
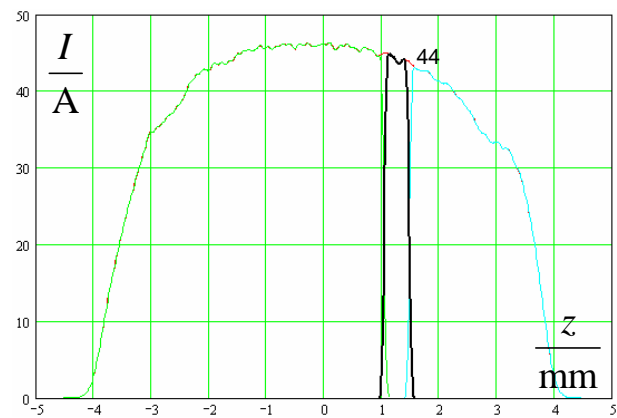
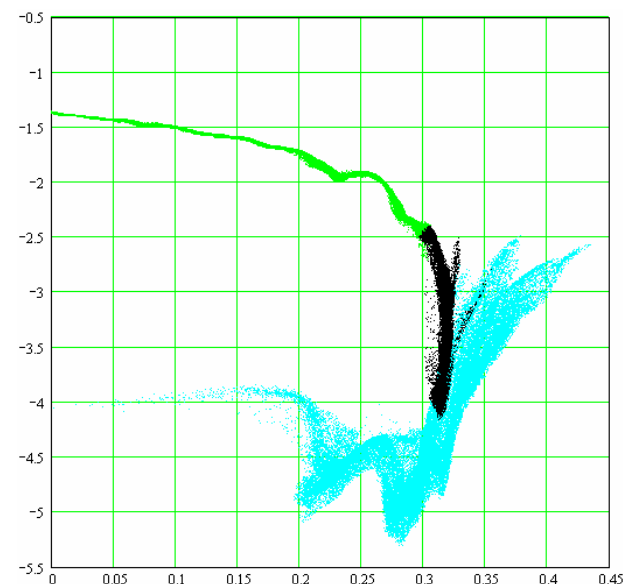
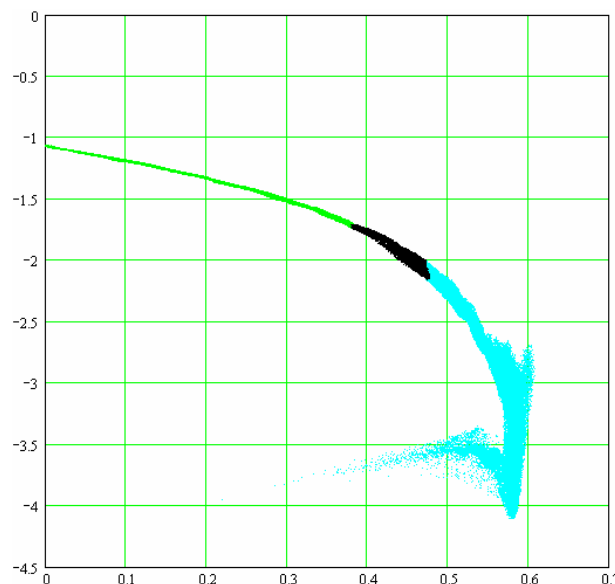
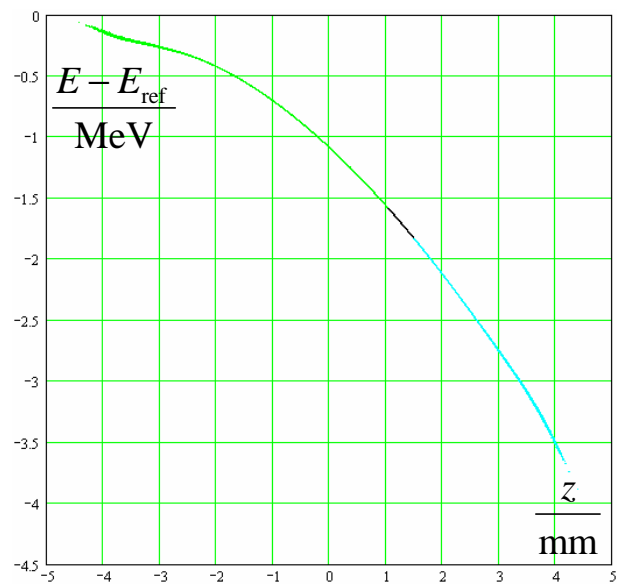
optics = option 1

$\varphi_{rf} = 8 \text{ deg}$

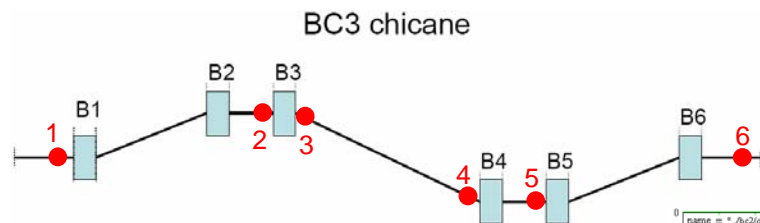
before BC2

1m after BC2

1m after BC3

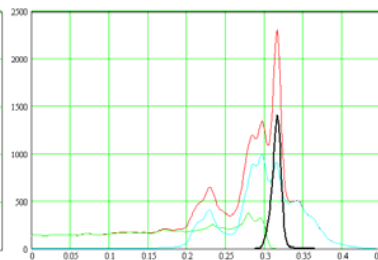
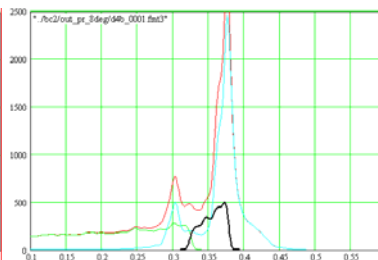
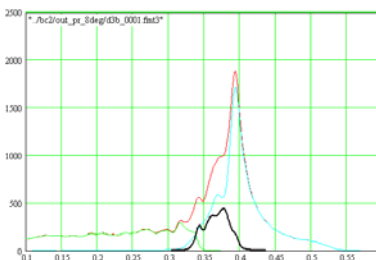
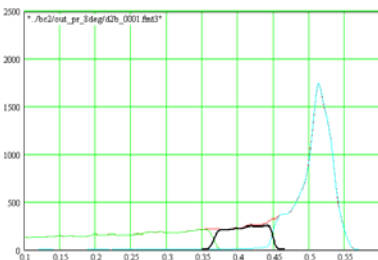
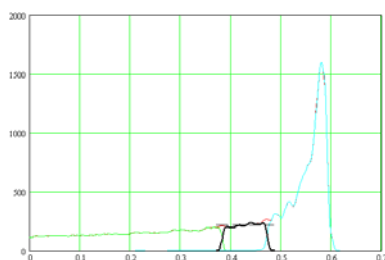
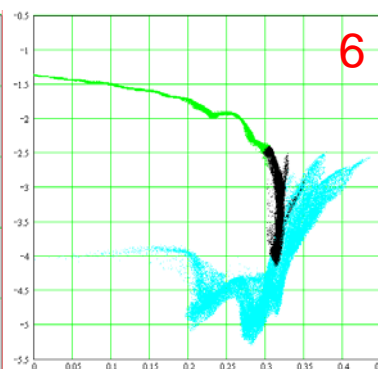
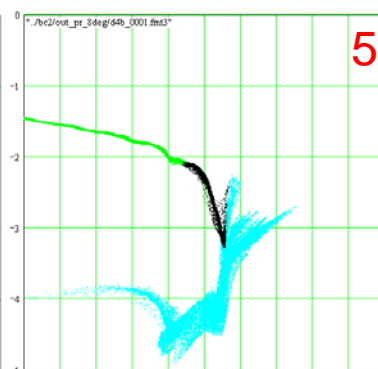
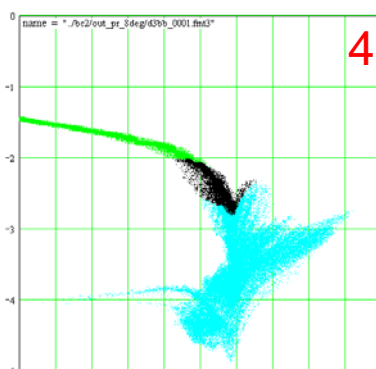
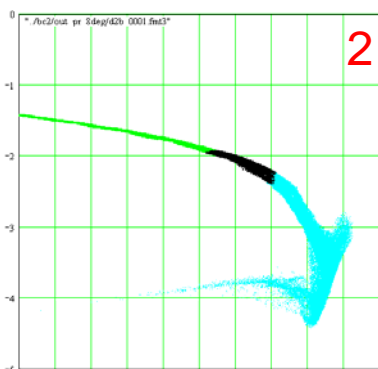
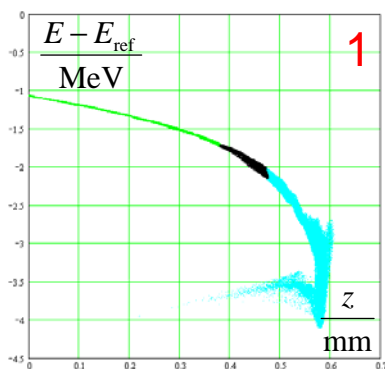
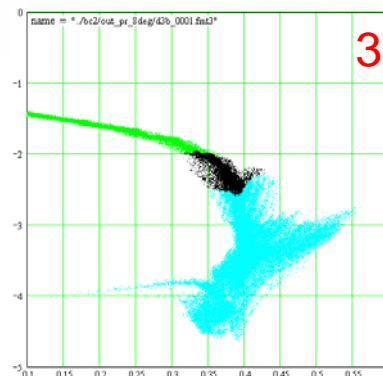


long. phase space in BC3



optics = option 1

$$\varphi_{\text{rf}} = 8 \text{ deg}$$

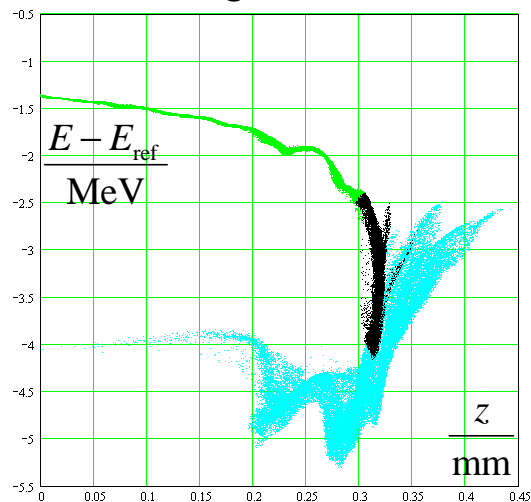


CSR "projected"

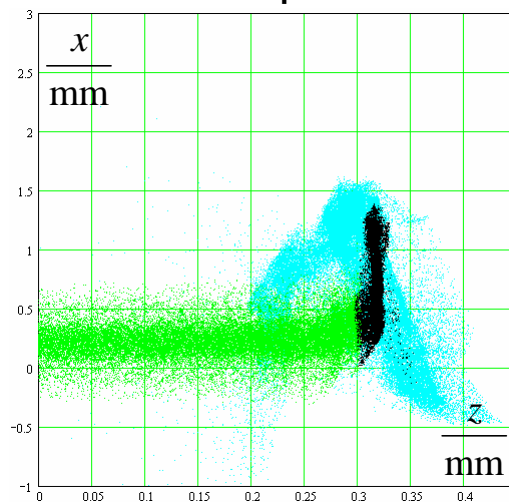
optics = option 1

$\phi_{rf} = 8 \text{ deg}$

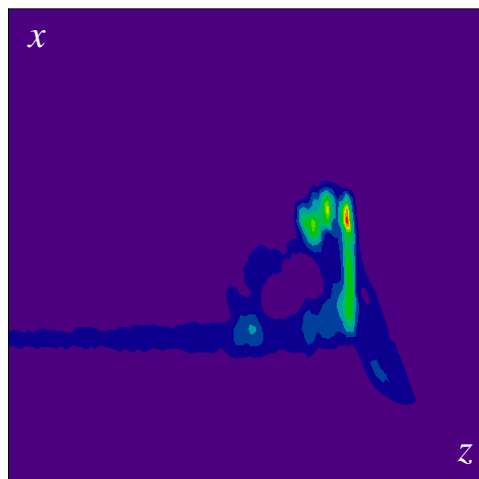
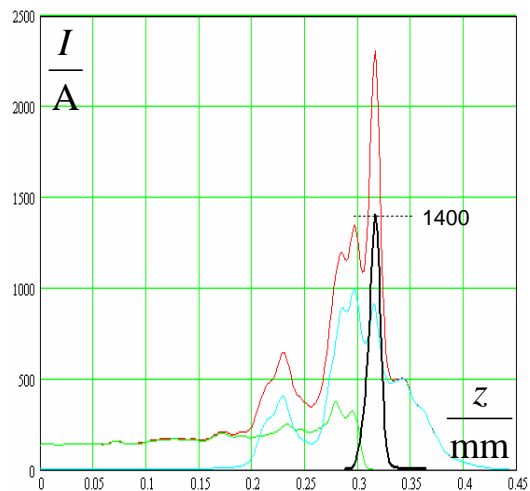
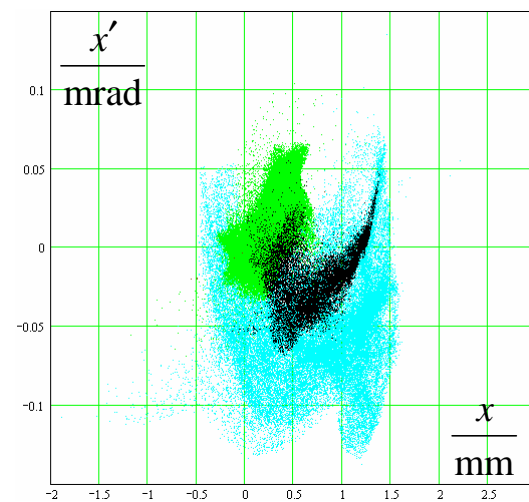
longitudinal



"top"



horizontal



all particles:

emittance/ μm = 10.1
rms-length/ μm = 722
rms-energy spread/keV = 1450

"black" particles:

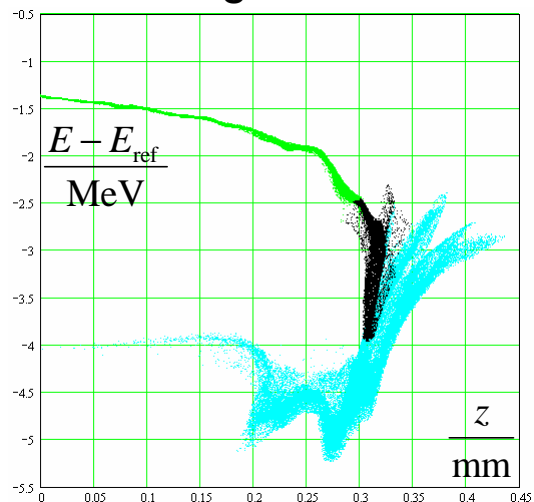
emittance/ μm = 4.13
rms-length/ μm = 5.6
rms-energy spread/keV = 476

CSR "projected"

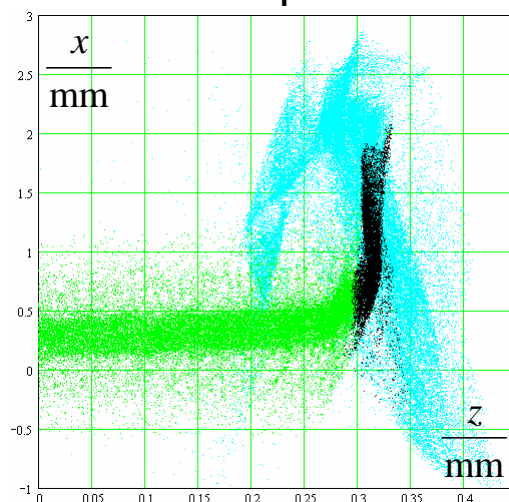
optics = option 2

$\phi_{rf} = 8 \text{ deg}$

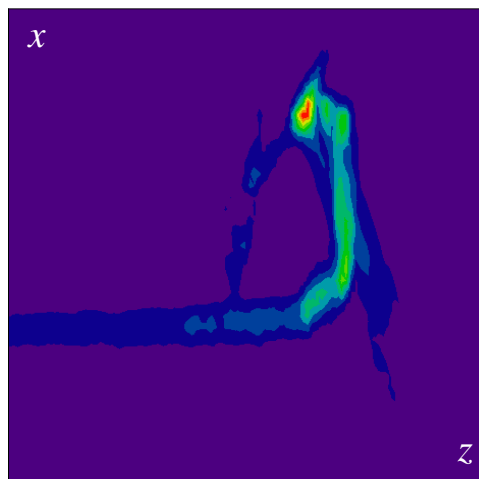
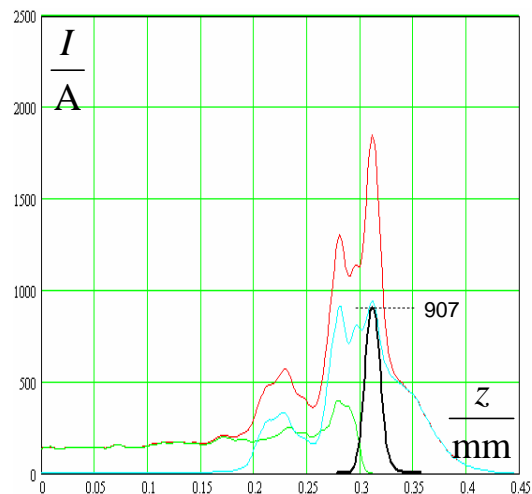
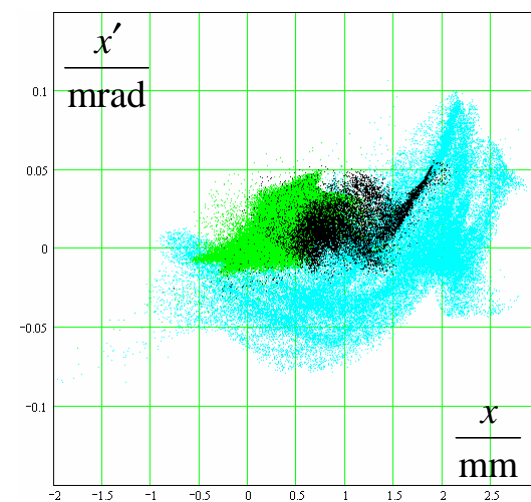
longitudinal



"top"



horizontal



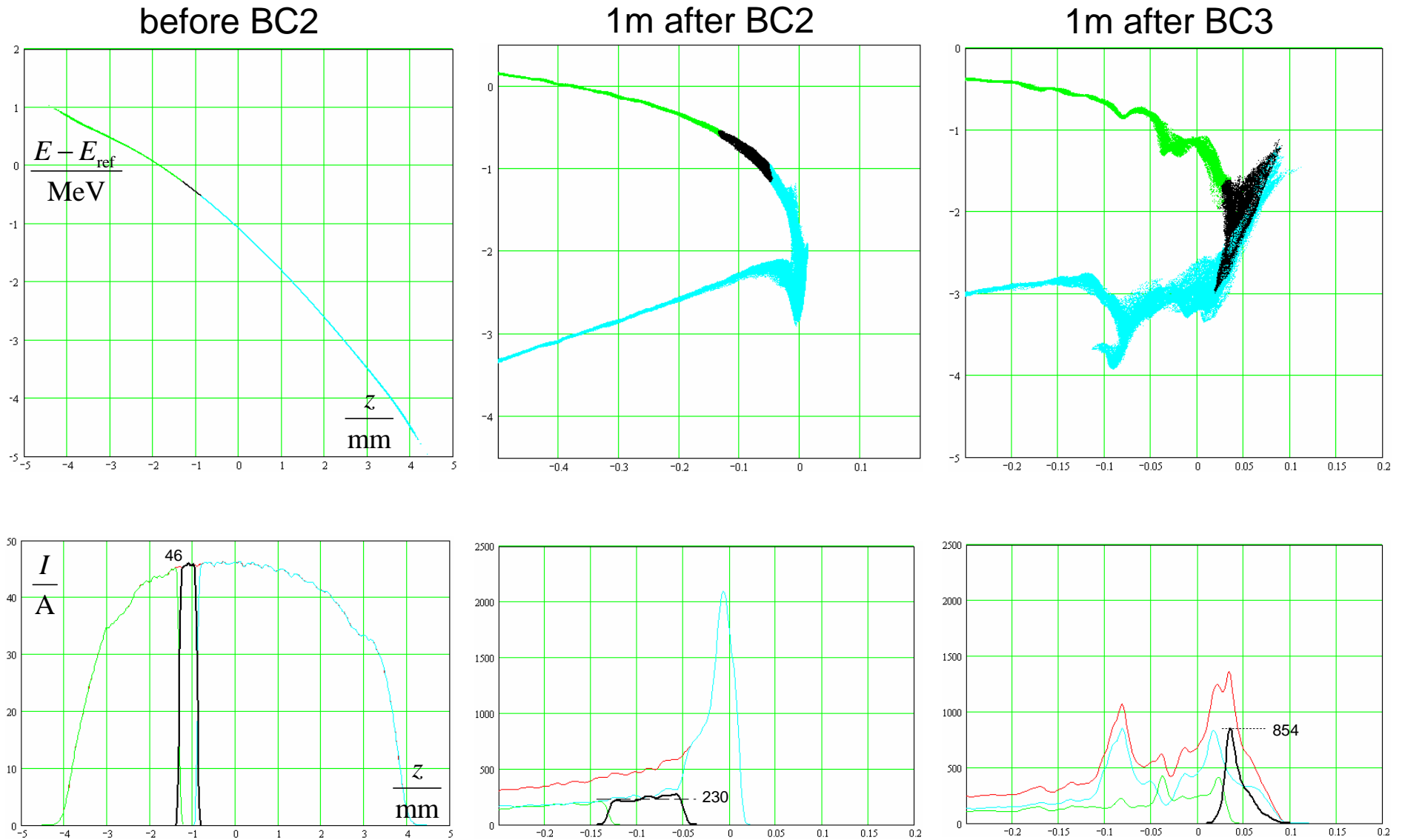
all particles:

emittance/ μm = 10.6
rms-length/ μm = 722
rms-energy spread/keV = 1419

"black" particles:

emittance/ μm = 3.63
rms-length/ μm = 6.8
rms-energy spread/keV = 418

4. CSR “projected” optics = option 1 $\varphi_{rf} = 12$ deg

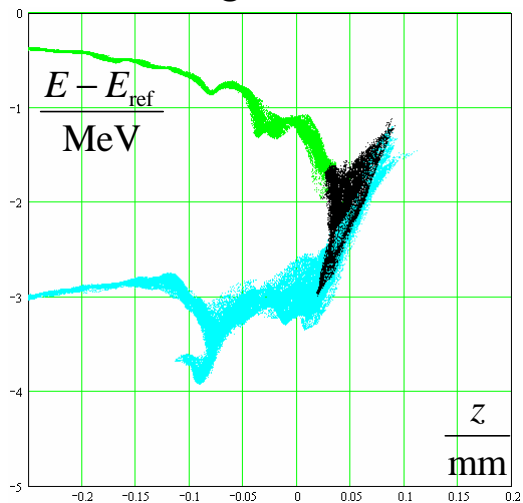


CSR "projected"

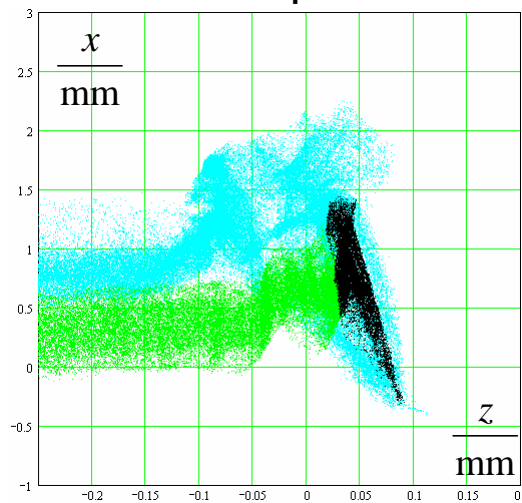
optics = option 1

$\phi_{rf} = 12$ deg

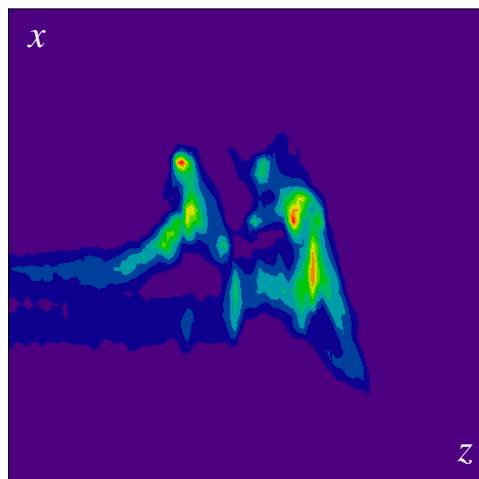
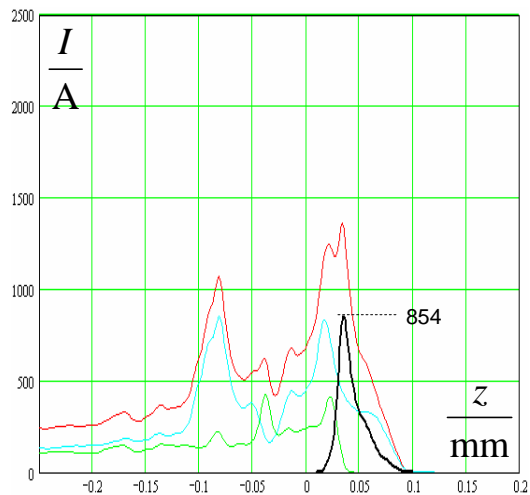
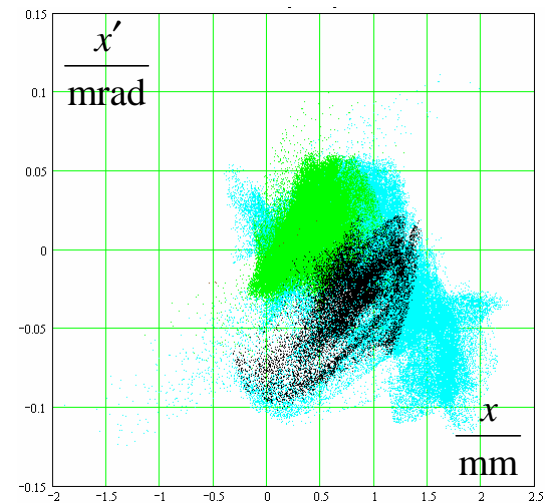
longitudinal



"top"



horizontal



all particles:

emittance/ μm = 10.55
rms-length/ μm = 339
rms-energy spread/keV = 1380

"black" particles:

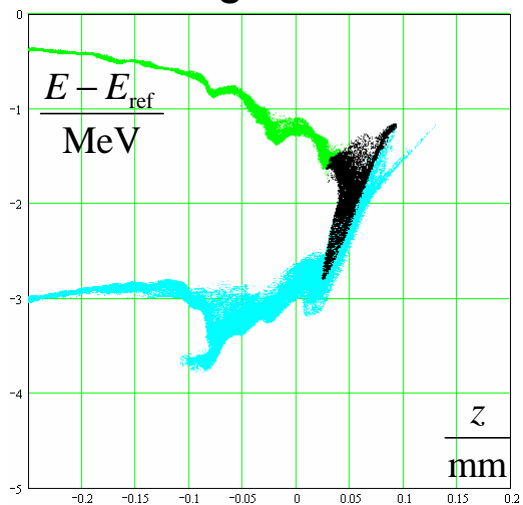
emittance/ μm = 4.56
rms-length/ μm = 13.0
rms-energy spread/keV = 324

CSR “projected”

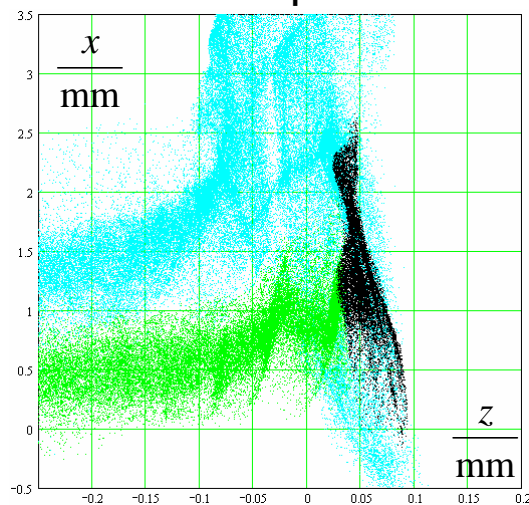
optics = option 2

$\phi_{rf} = 12$ deg

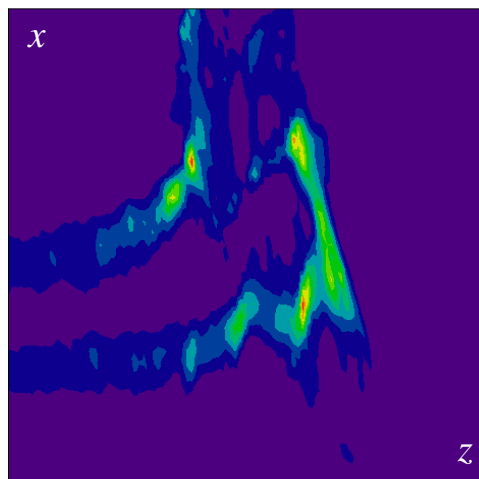
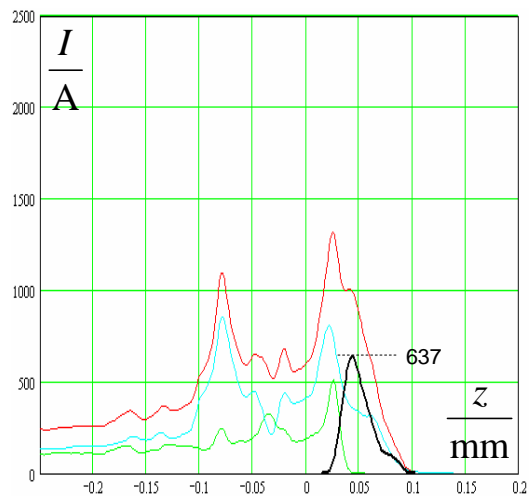
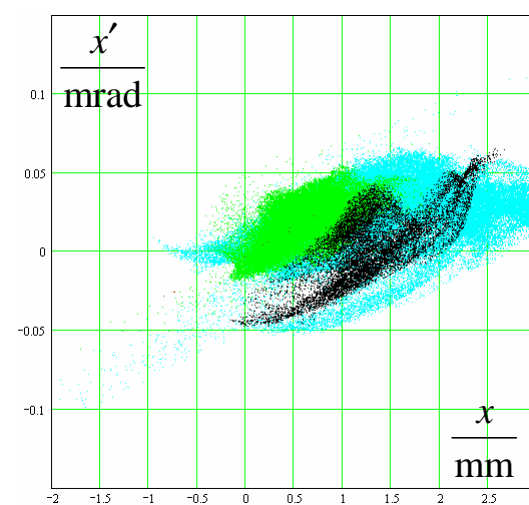
longitudinal



“top”



horizontal



all particles:

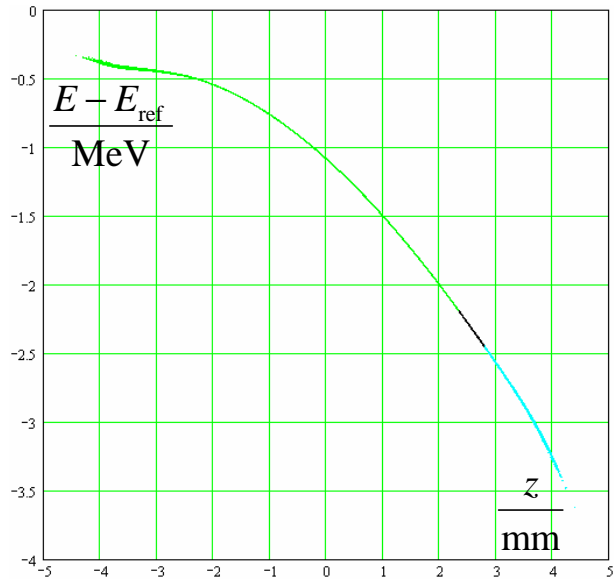
emittance/ μm = 10.74
rms-length/ μm = 338
rms-energy spread/keV = 1380

“black” particles:

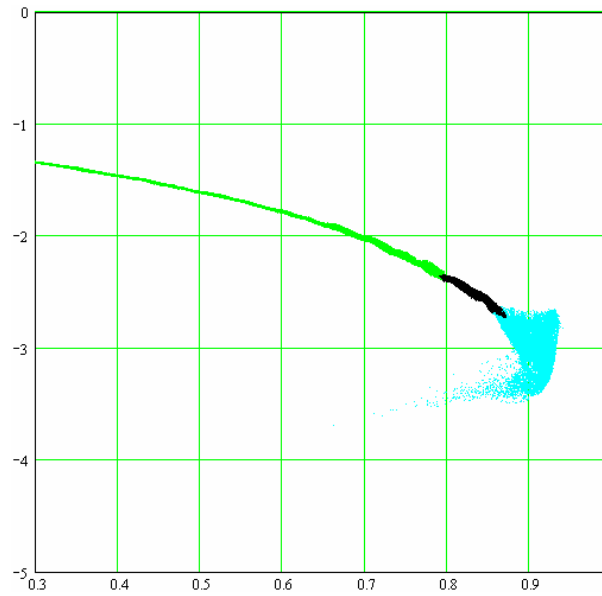
emittance/ μm = 5.43
rms-length/ μm = 13.8
rms-energy spread/keV = 313

5. CSR "projected" optics = option 1 $\phi_{rf} = 7 \text{ deg}$

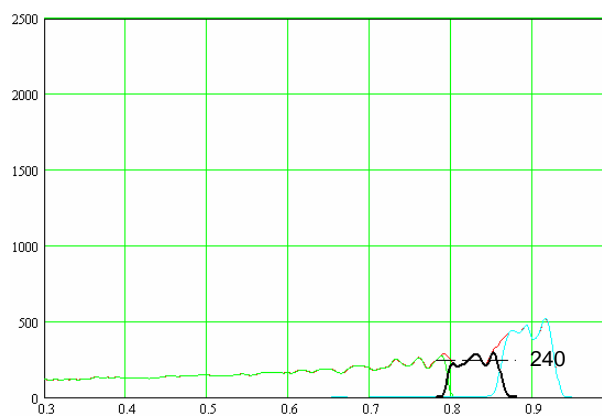
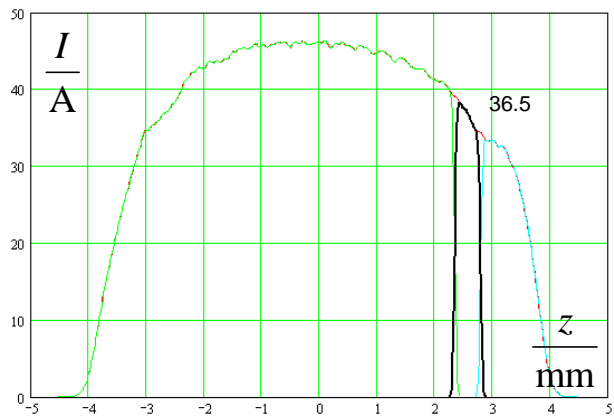
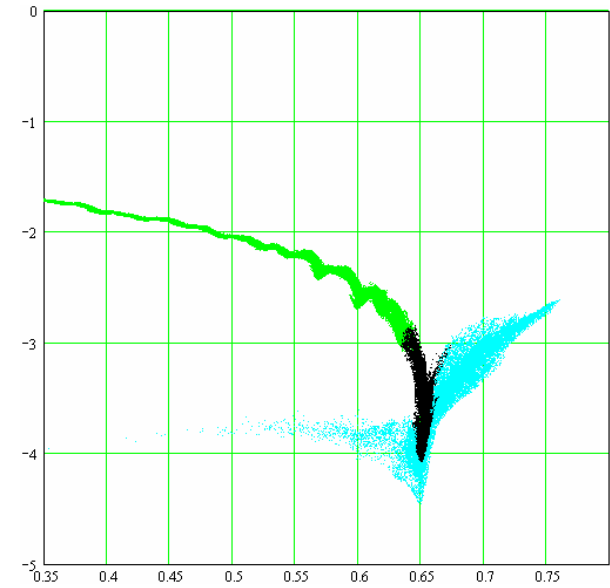
before BC2



1m after BC2



1m after BC3

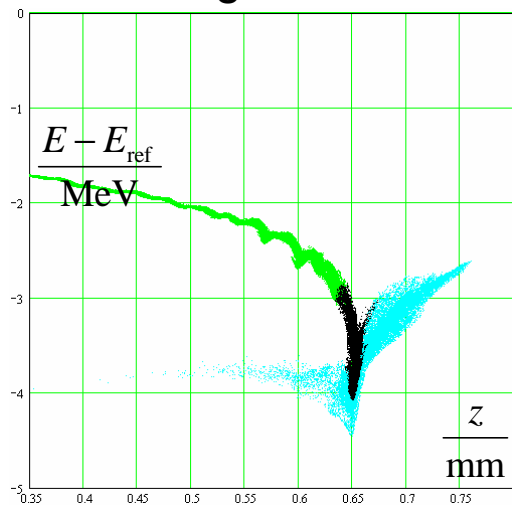


CSR "projected"

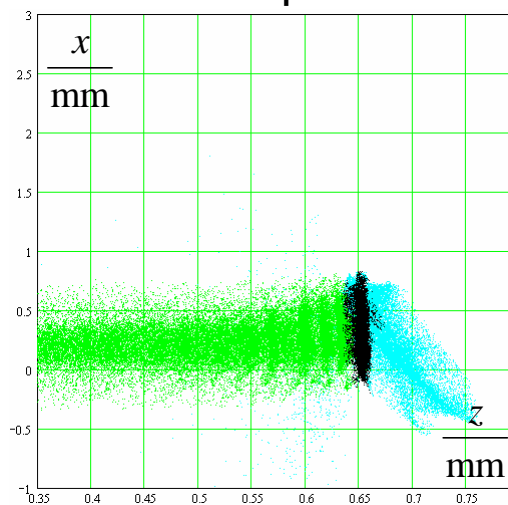
optics = option 1

$\phi_{rf} = 7 \text{ deg}$

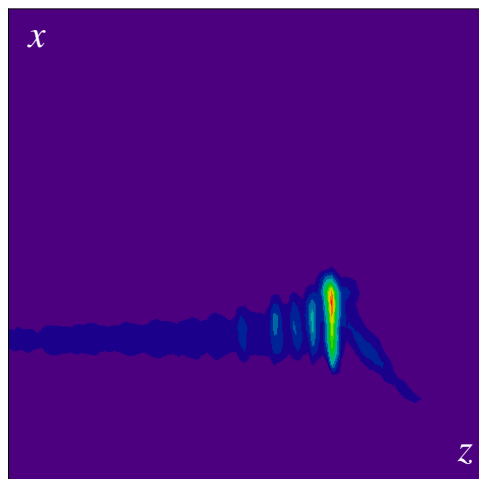
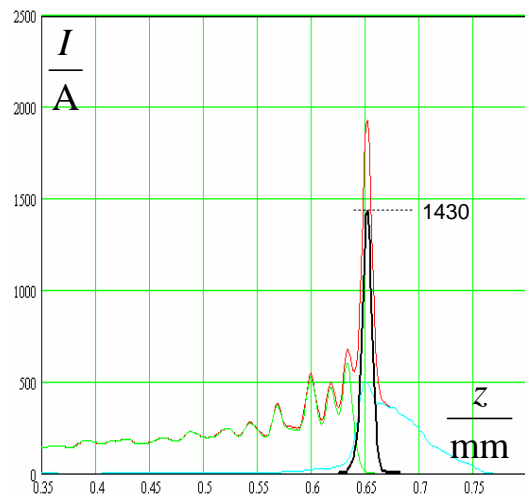
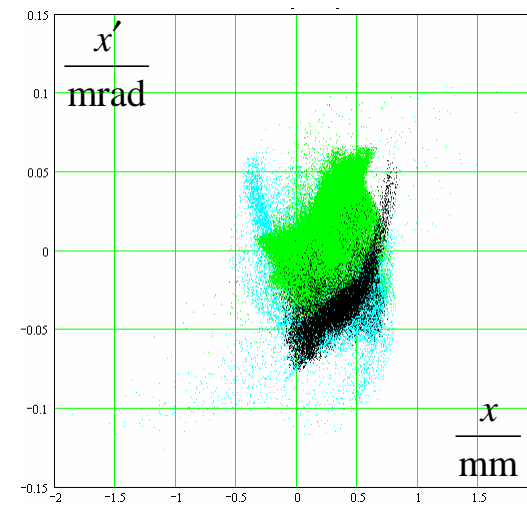
longitudinal



"top"



horizontal



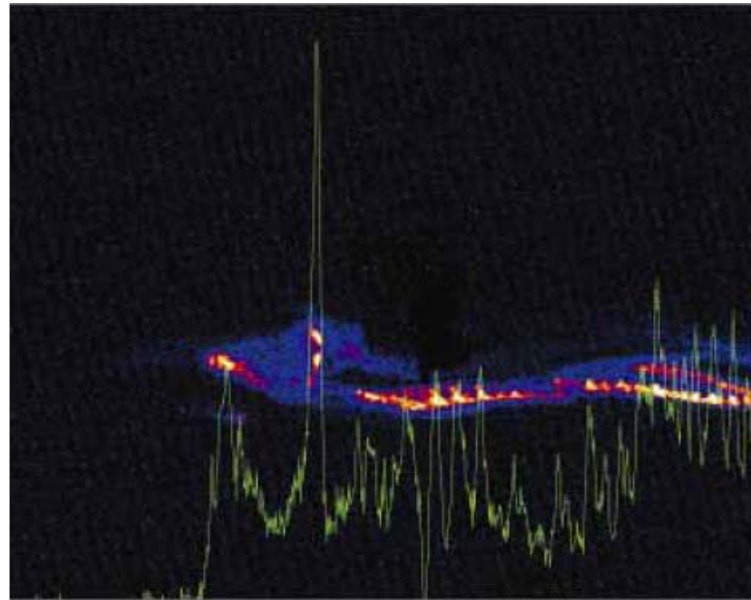
all particles:

emittance/ μm = 3.38
rms-length/ μm = 923
rms-energy spread/keV = 880

"black" particles:

emittance/ μm = 2.06
rms-length/ μm = 4.2
rms-energy spread/keV = 256

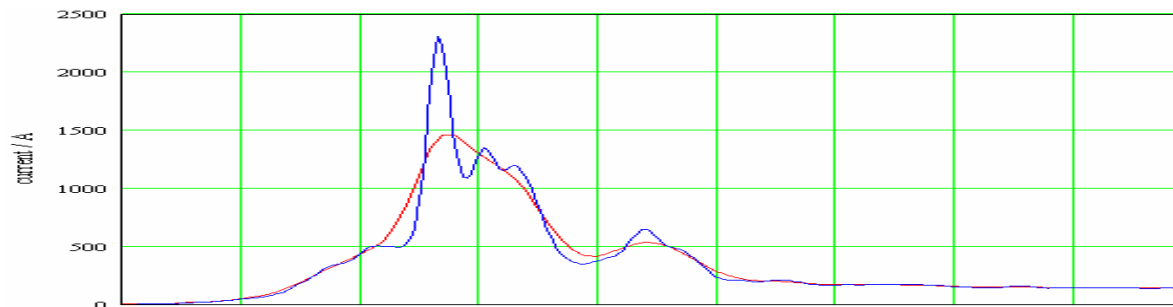
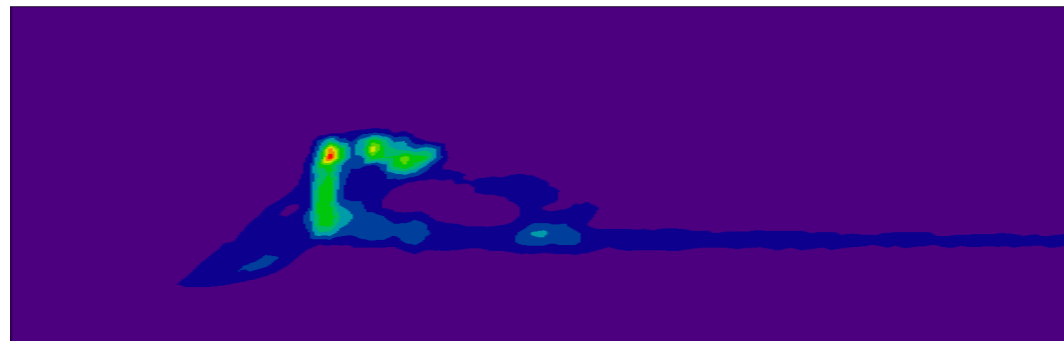
6. some LOLA pictures

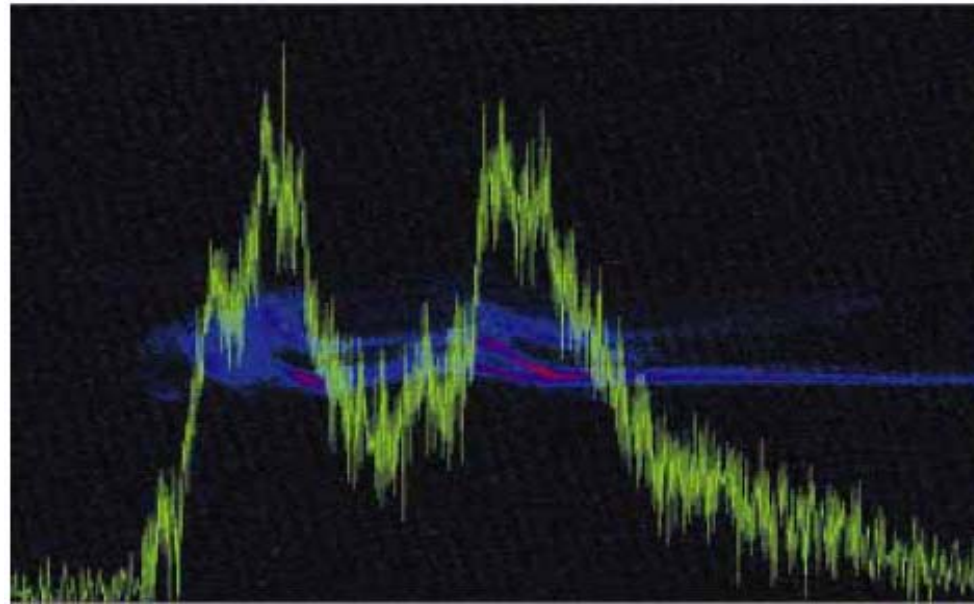


← 1 picosecond →

optics = option 1

$\varphi_{rf} = 8 \text{ deg}$

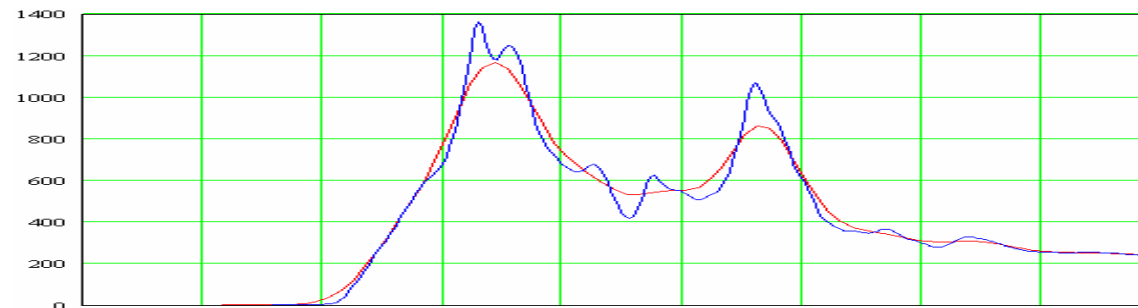
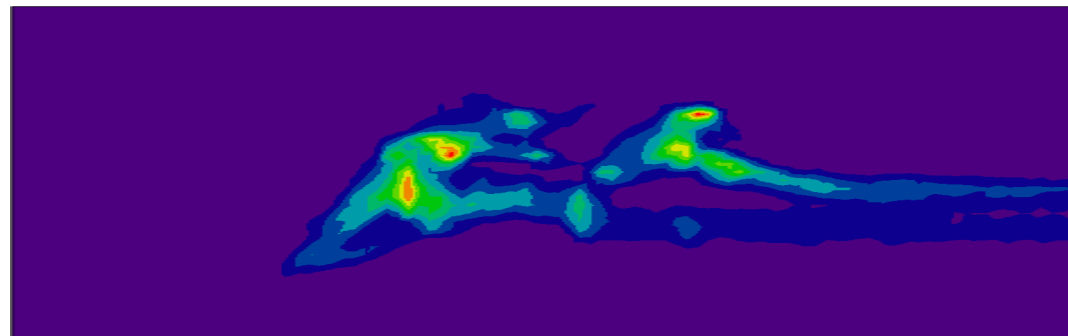




← 1 picosecond →

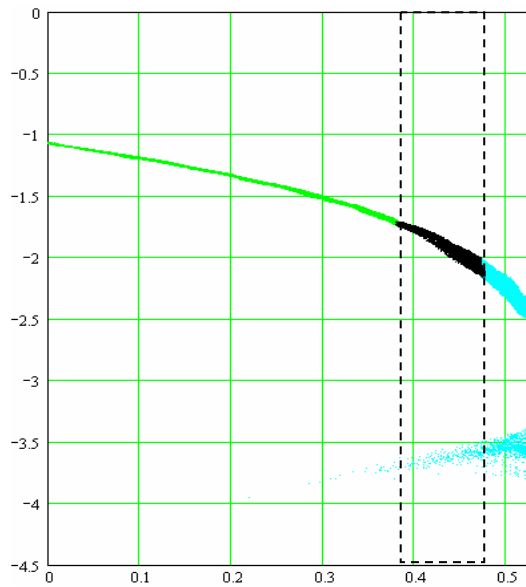
optics = option 1

$\varphi_{\text{rf}} = 12 \text{ deg}$



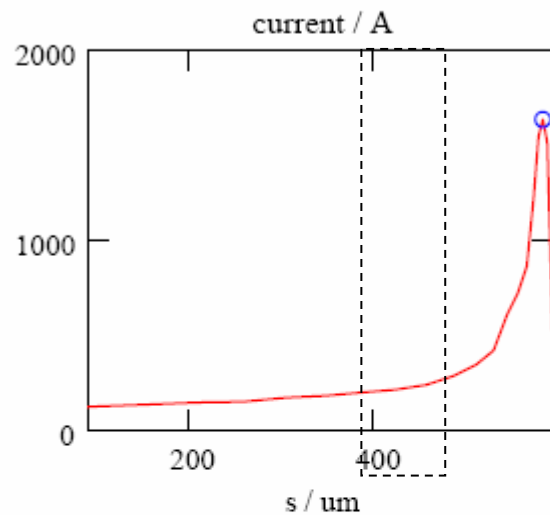
7. conclusion / remarks

1. settings and beam parameters only known to a certain precision
2. CSR model for TTF2 with space charge in ACC1,
“projected” method in BC2 & BC3,
transport matrix for BC2 → BC3,
ACC4 → undulator not considered jet
3. ASTRA calculations for BC2 → BC3 and ACC4 → undulator in preparation
“projected” CSR calculations in ASTRA in principle possible
4. “3D” CSR calculations with full- & over-compression difficult
(variable sub-bunch needed due to long tails ↔ meshed green’s function)
“projected” CSR calculations need better smoothing/filter-algorithms
5. qualitative understanding of compression process,
complicated interaction of “full” compressed part to rest of bunch
6. qualitative agreement with LOLA pictures
7. optics “option 1” and “weak over-compression” in BC2 seems preferable

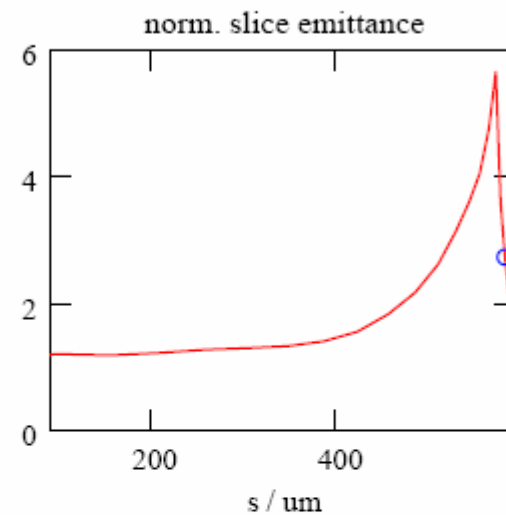


in_file = "../bc1/out_pr_8deg/end.fmt3"

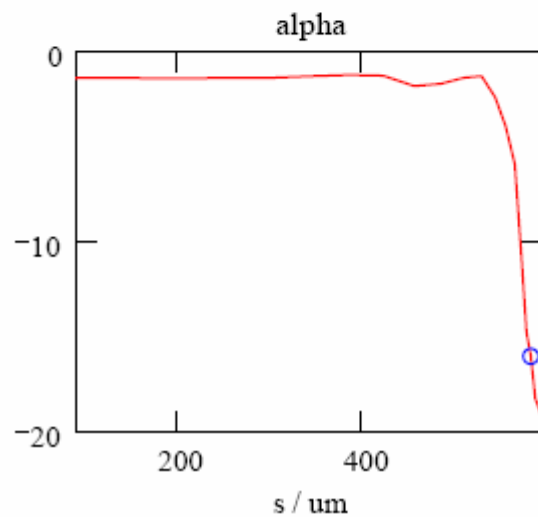
$$T_{k,4} \cdot x = 1.636 \times 10^3$$



$$T_{k,5} \cdot 10^6 = 2.738$$



$$T_{k,6} = -16.013$$



$$T_{k,7} = 21.86$$

