

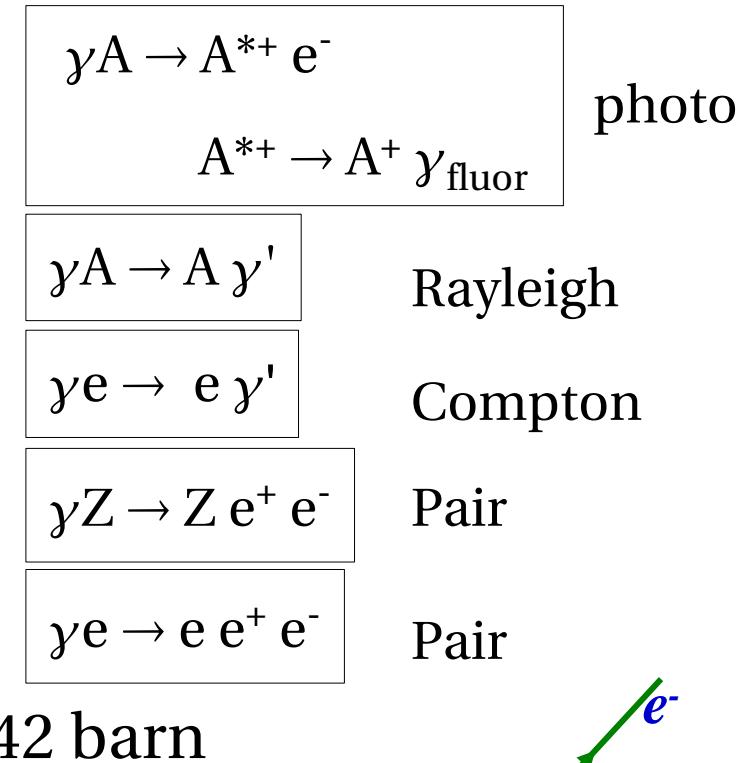
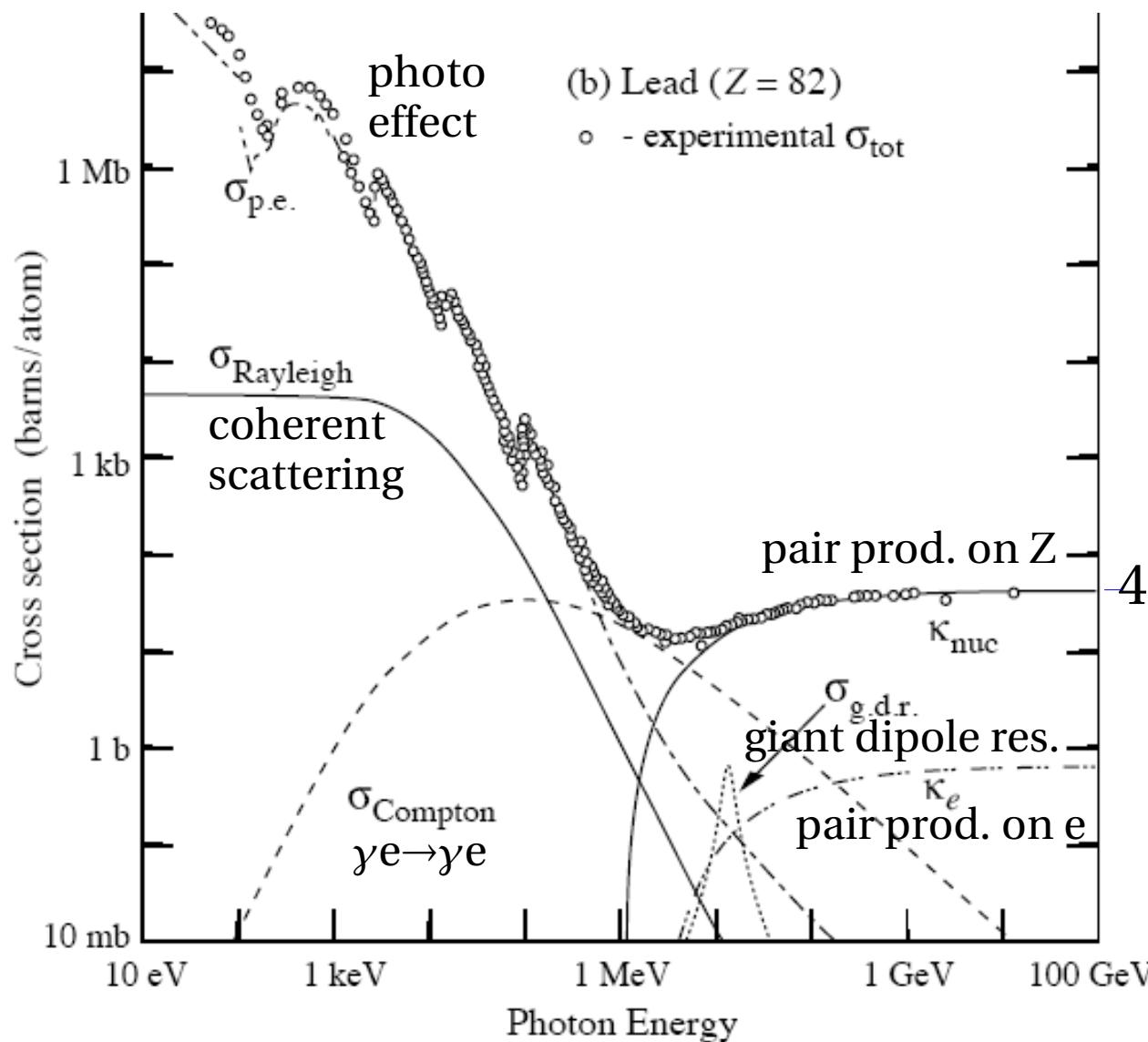
# **Detectors for Particle Physics**

## **Lecture 3: Showers and calorimeters Particle flow**

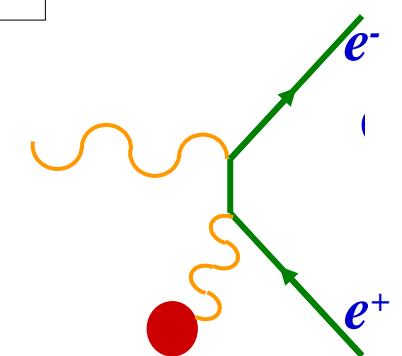
# Outline

- Lecture 1:
  - ▶ Collider detectors
  - ▶ Charged particles in a magnetic field
  - ▶ Silicon detectors
- Lecture 2:
  - ▶ Drift tubes
  - ▶ Muon systems
  - ▶ MWPCs, CSCs, RPCs, TRTs, TPCs, Cherenkovs
- Lecture 3:
  - ▶ Electromagnetic showers and calorimeters
  - ▶ Photon detectors
  - ▶ Hadronics showers and calorimeters
  - ▶ Particle flow technique
- Discussion session:
  - ▶ Your questions, please

# Photon interactions in matter (A, Z)



42 barn



Pair production  
 $\gamma Z \rightarrow Ze^+e^-$  dominates  
above  $\sim 4$  MeV

# Radiation length

High energy photon cross section in lead:  $\sigma_\gamma = 42 \text{ barn/atom}$

Convert to photon absorption coefficient:

$$\mu_\gamma [\text{1/cm}] = \sigma_\gamma [\text{cm}^2/\text{atom}] \cdot N_A [\text{atoms/mol}] / A [\text{g/mol}] \cdot \rho [\text{g/cm}^3]$$

Define interaction length:  $\lambda_\gamma = 1/\mu_\gamma$

Define radiation length:  $X_0 = 7/9 \cdot \lambda_\gamma$

Plug in some numbers: 1 barn =  $10^{-24} \text{ cm}^2$

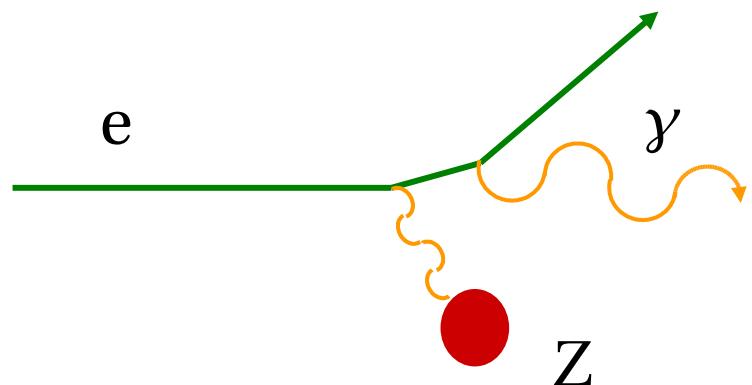
$$N_A = 6 \cdot 10^{23} \text{ atoms/mol}$$

$$A = 207 \text{ for lead}$$

$$\rho = 11.35 \text{ g/cm}^3 \text{ for lead}$$

$\Rightarrow$  radiation length of lead:  $X_0 = 0.56 \text{ cm.}$

# Radiation Loss for electrons in matter



- Bremsstrahlung:  $e Z \rightarrow Z e \gamma$   
electromagnetic radiation produced by the deceleration of an **electron**, when deflected by an **atomic nucleus**.

$$-\frac{dE}{dx} = \frac{E}{X_0}$$

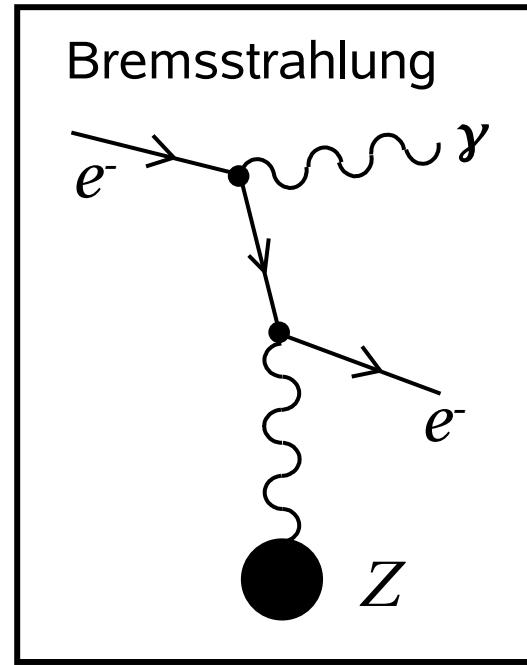
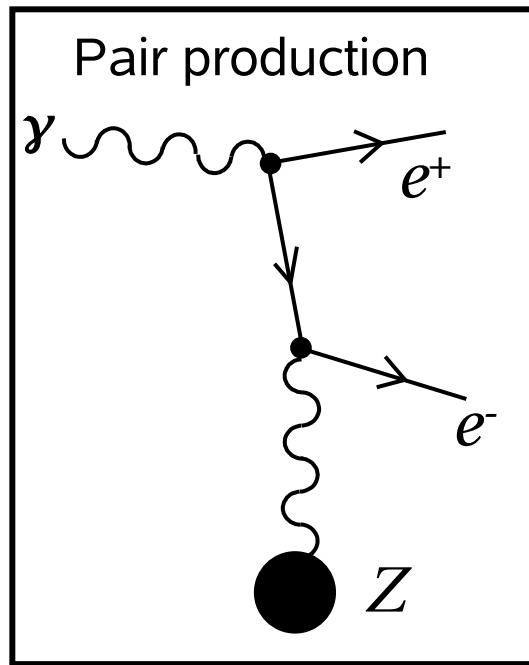
$$X_0 [cm] = \frac{716}{\rho [g/cm^3]} \frac{A}{Z} \frac{1}{(Z+1) \ln(287/\sqrt{Z})}$$

$$\Leftrightarrow E = E_0 e^{-x/X_0}$$

$$\text{Pb: } X_0 = 0.56 \text{ cm}$$

$$\text{Si: } X_0 = 8.9 \text{ cm}$$

# Pair production and Bremsstrahlung



- Very similar Feynman diagrams
- Just two arms swapped.

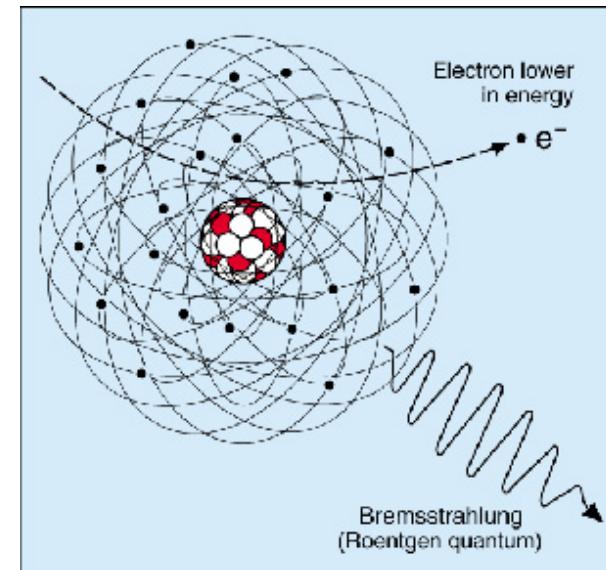
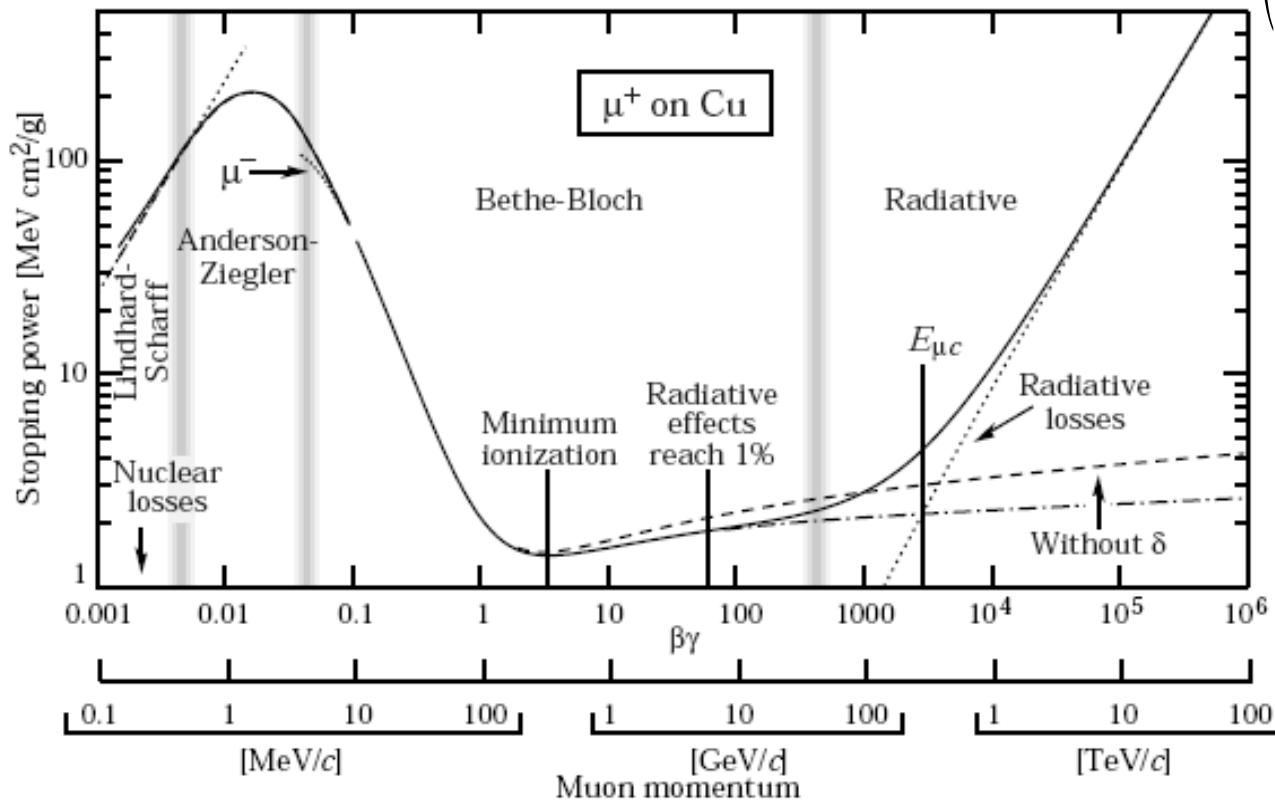
**At high energy:**  $\sigma_\gamma = 7/9 \sigma_e$

# Muons radiate only at extreme energies

A particle of mass **m** may radiate a photon while being decelerated in the Coulomb field of a nucleus **Z**:

$$\frac{d\sigma}{dE} \propto \frac{Z^2}{m^2} \frac{\ln E}{E}$$

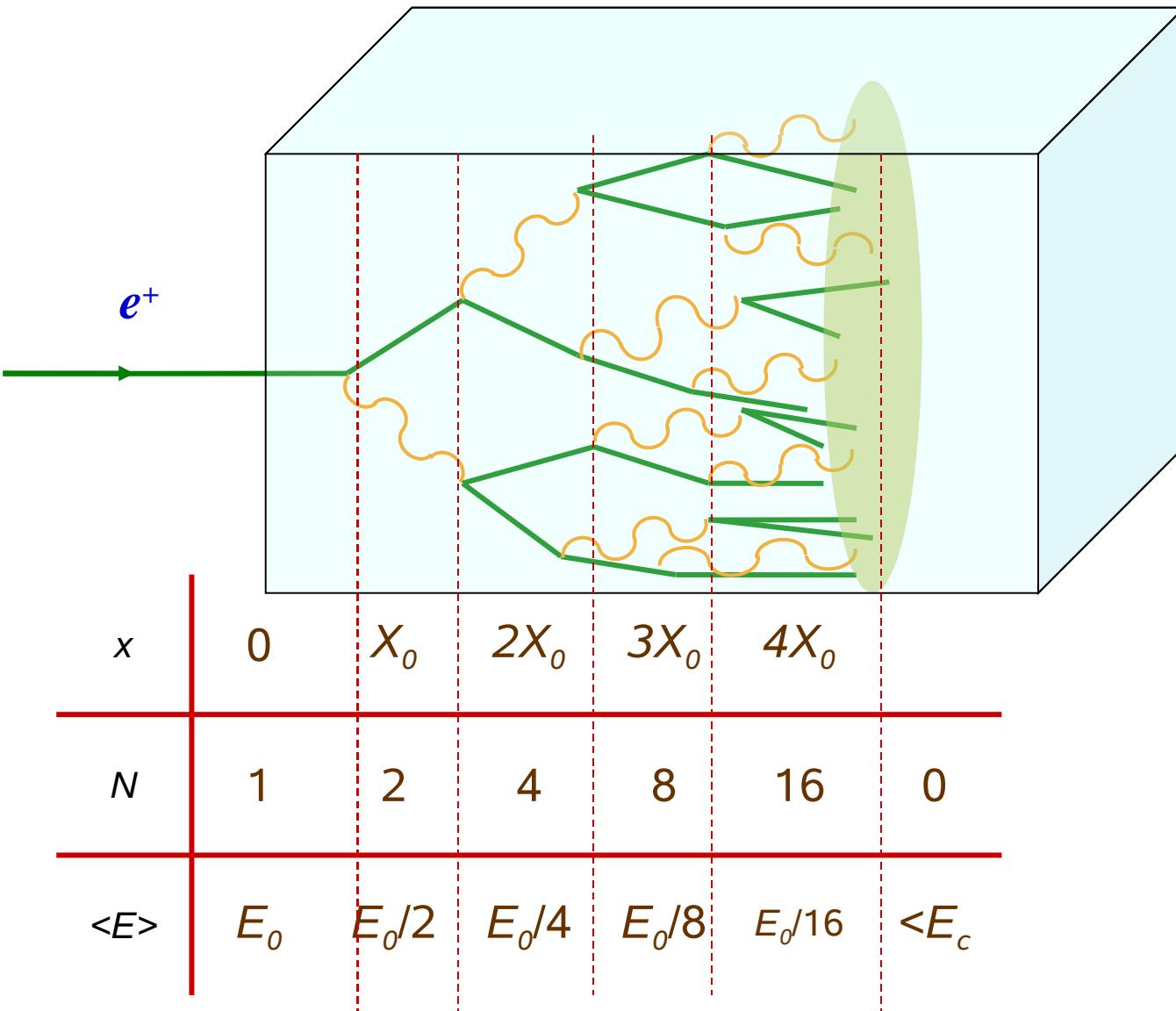
classically, radiation power  $P \propto a^2 = \left(\frac{F}{m}\right)^2$



$$\frac{m_e^2}{m_\mu^2} = 2.3 \cdot 10^{-5}$$

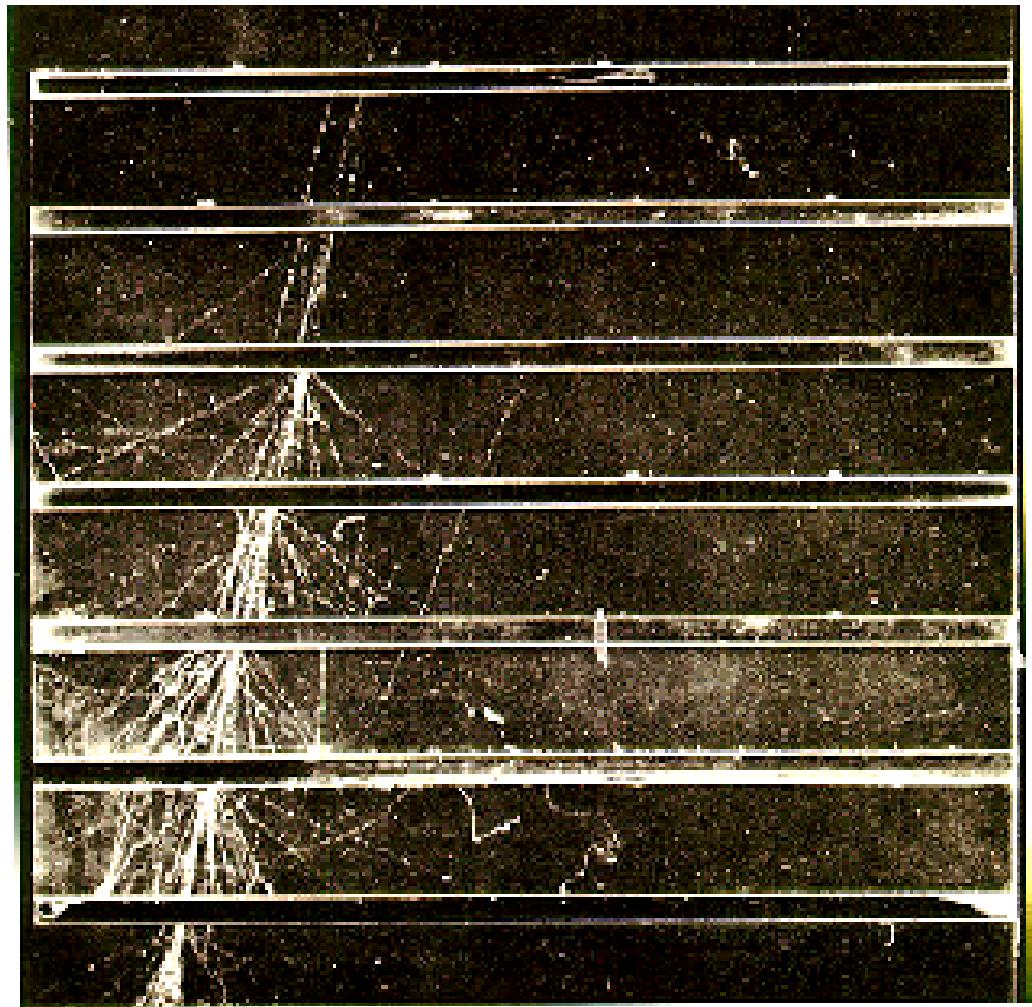
critical energy for muons  
is 450 GeV in copper,  
200 GeV in lead.

# Electromagnetic Showers



# Shower in a cloud chamber

- Cloud chamber image of a shower between lead plates.



# A simple shower model

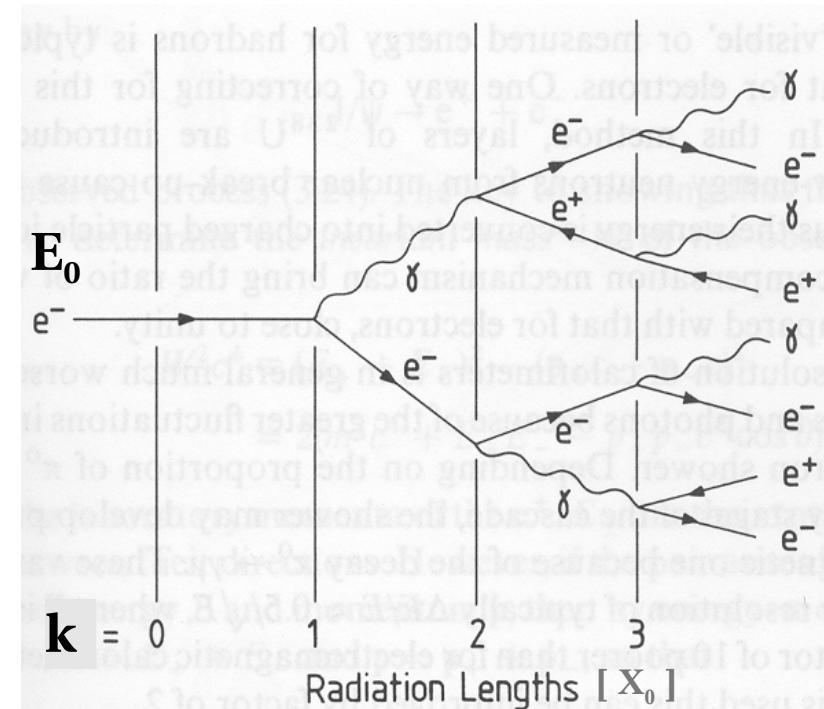
Start with a high energy electron:  $E_0$

⇒ After  $1X_0$ : 1  $e^-$  and 1  $\gamma$ , each with  $E_0/2$

⇒ After  $2X_0$ : 2  $e^-$ , 1  $e^+$  and 1  $\gamma$ , each with  $E_0/4$

•

⇒ After  $kX_0$ : total  $N = 2^k$ , each with  $\langle E \rangle = E_0/2^k$



At  $\langle E \rangle = E_c$  pair production and bremsstrahlung stop.

Compton- or photoeffect and ionization take over. The shower ranges out.

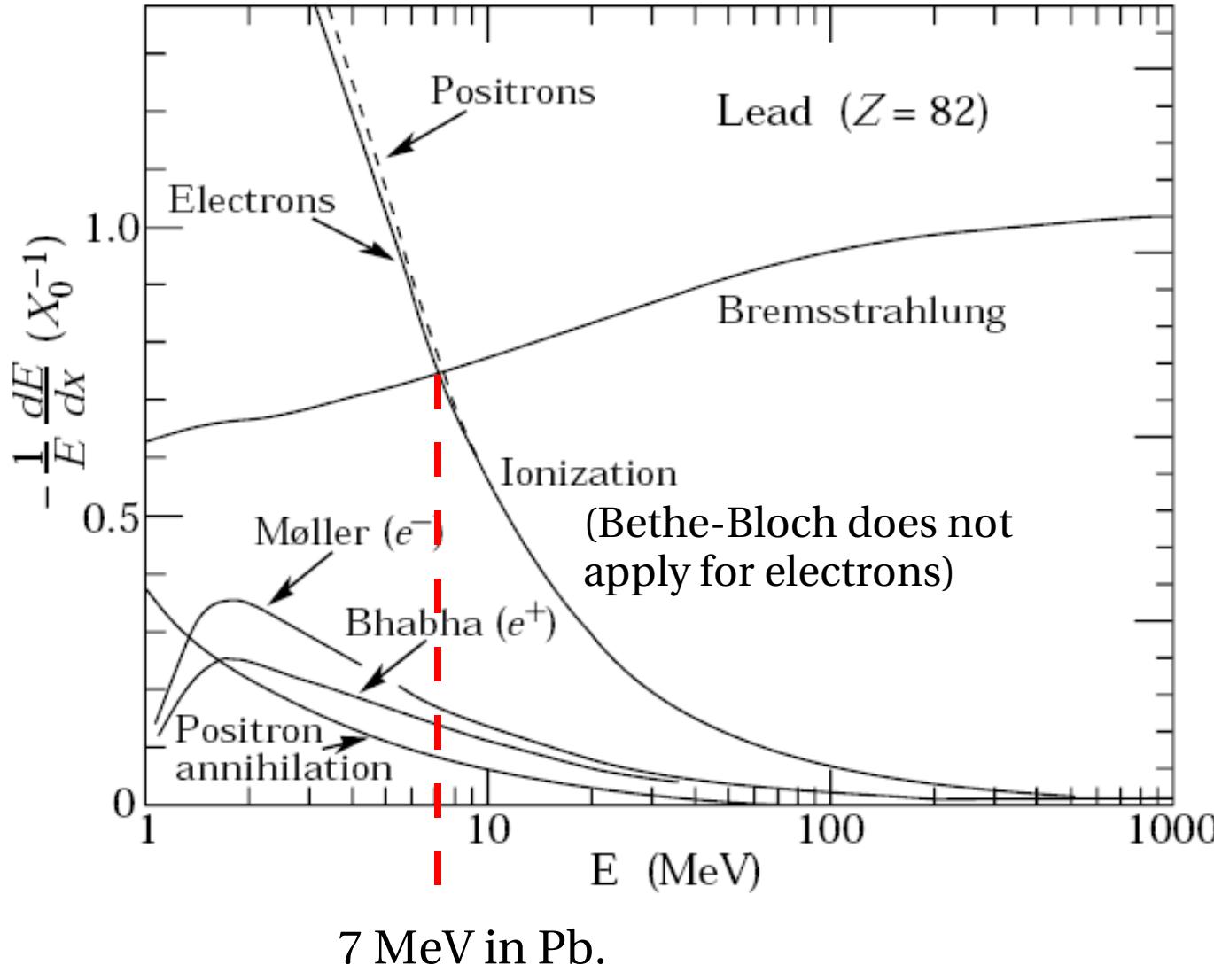
$E_c = 0.6 \text{ GeV} / (Z+1.24) = 7 \text{ MeV}$  for lead. (empirical fit by the PDG)

⇒  $k_{\max} = \lg_2(E_0/E_c)$ . **Shower depth grows logarithmically with  $E_0$ .**

⇒  $N_{\max} = 2^{k_{\max}} = E_0/E_c$ . **Number of shower particles grows linearly with  $E_0$ .**

# Electron energy loss and critical energy

relative energy loss for electrons:

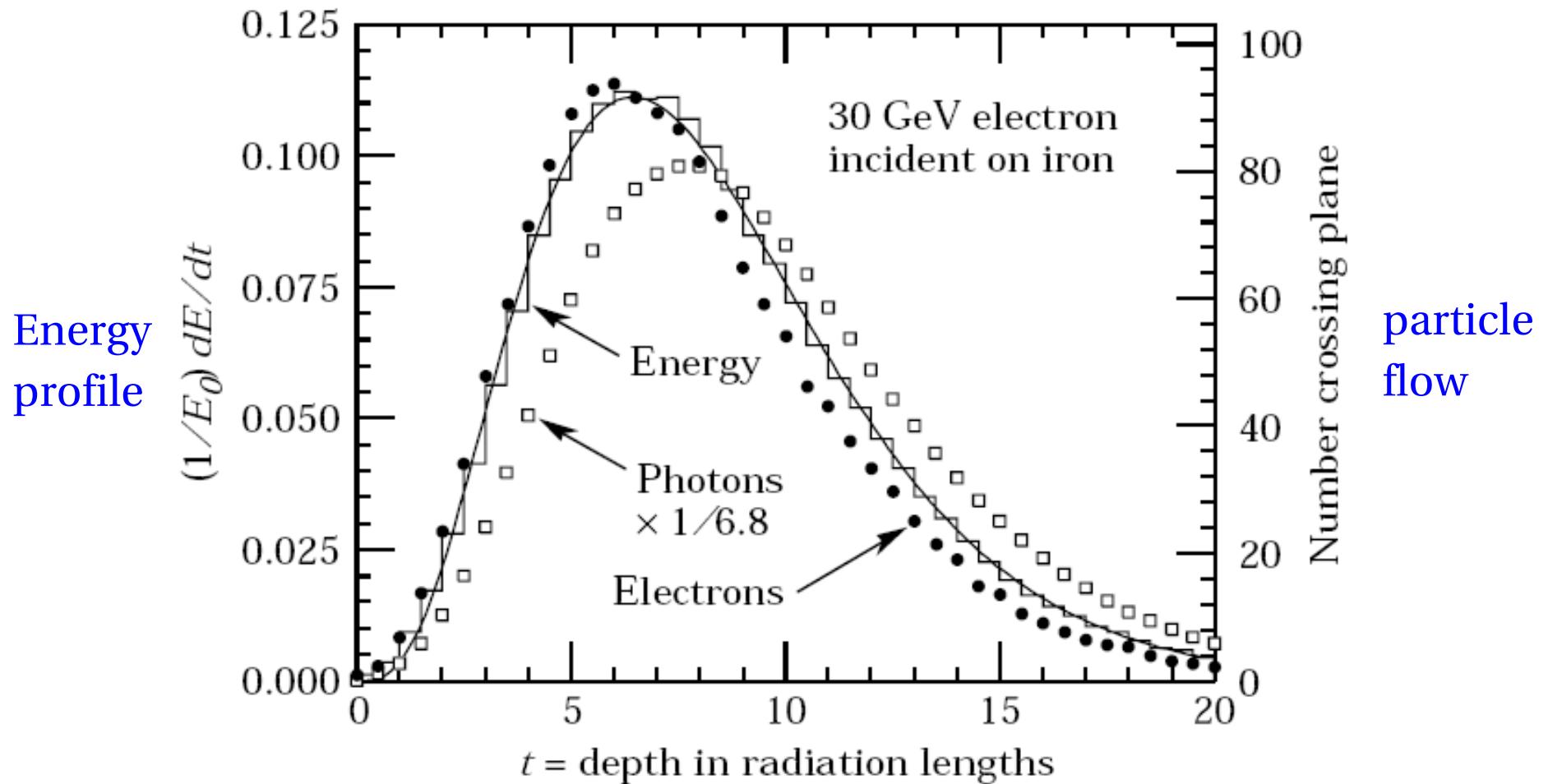


Critical energy:  
energy loss due to  
Bremstrahlung and  
ionization are equal:

$$E_c \approx \frac{610 \text{ MeV}}{Z + 1.24}$$

High Z material gives  
more signal: shower  
stops later

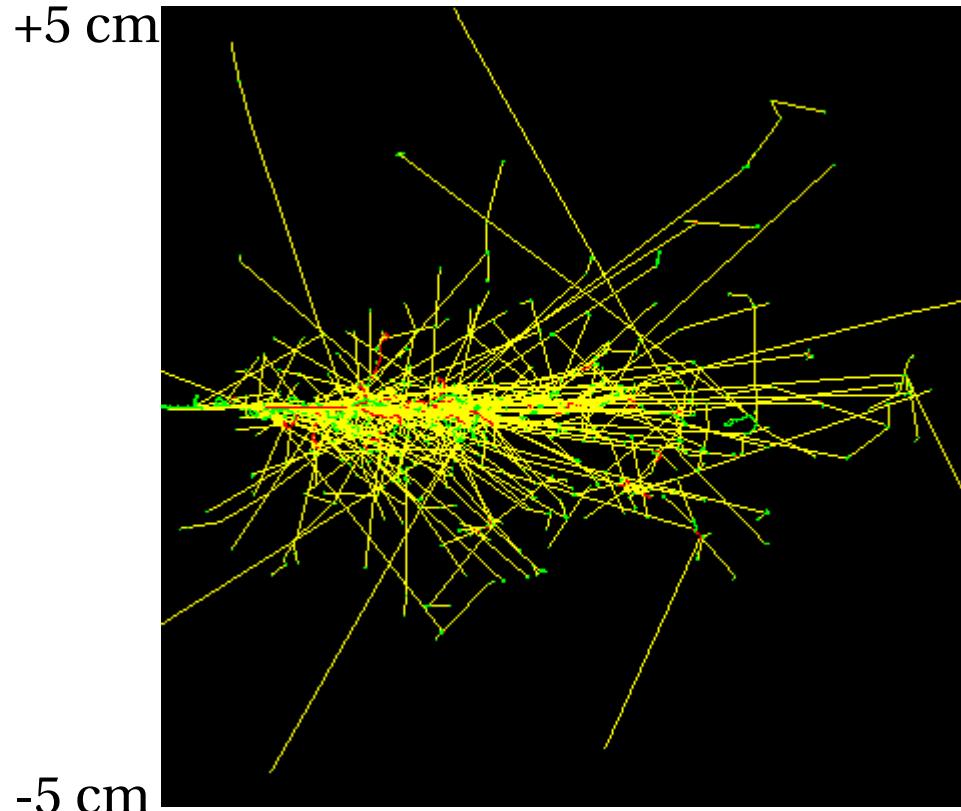
# A sophisticated shower simulation



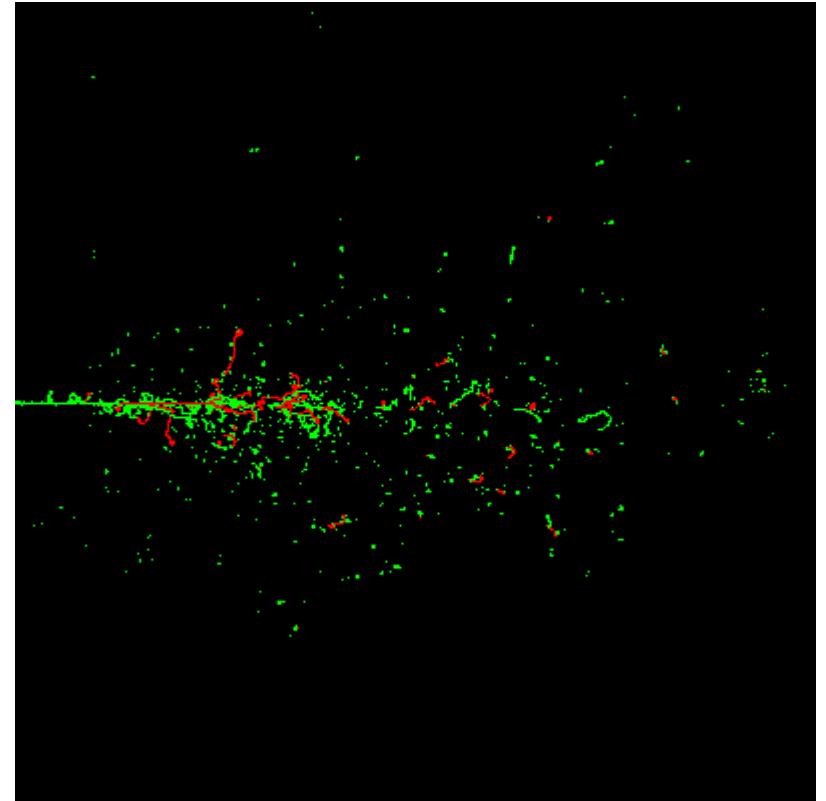
$$\frac{dE}{dt} \triangleq E_0 b \frac{(bt)^{a-1} e^{-bt}}{\Gamma(a)}, \quad t = \frac{x}{X_0}$$

# Shower simulation

1 GeV e<sup>-</sup> in lead



photons  
electrons  
positrons



electrons  
positrons

interactive at <http://www2.slac.stanford.edu/vvc/egs/basicsimtool.html>

# Energy measurement

Total number of particles in the shower in the simple model:

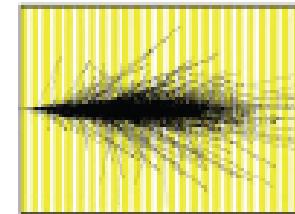
$$N_{\text{tot}} = \sum_k 2^k = 2 k_{\text{max}} - 1 \approx 2 E_0 / E_c$$

2/3 of  $N_{\text{tot}}$  are charged ( $e^+ + e^-$ ).

$$\Rightarrow N_{\text{ch}} \approx 4/3 E_0 / E_c$$

Each  $e$  travels  $1 X_0$  between interactions.

$$\Rightarrow \text{total path length: } L_{\text{ch}} \approx 4/3 X_0 E_0 / E_c$$



Electrons and positrons also **ionize** the medium.

collect charge or fluorescent light signal:  $S \sim X_0 E_0 / E_c$

**After calibration,  $S$  is an energy measurement!**

Shower fluctuations: particle production is a **Poisson** process.

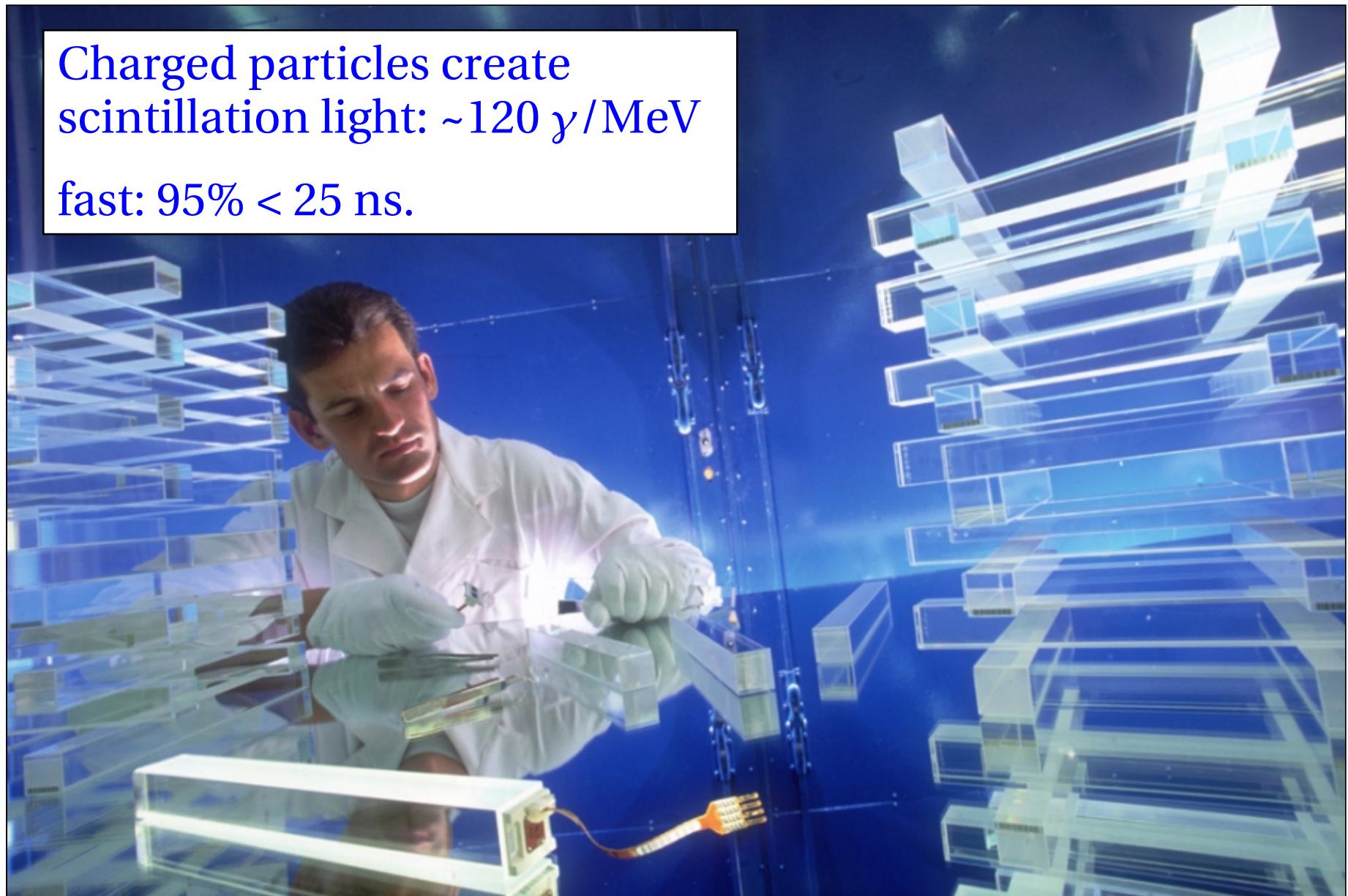
$$\Rightarrow \sigma(N) = \sqrt{N}$$

$$\Rightarrow \sigma(S) / S = 1 / \sqrt{S}$$

**The relative energy resolution improves with  $E_0$ !**

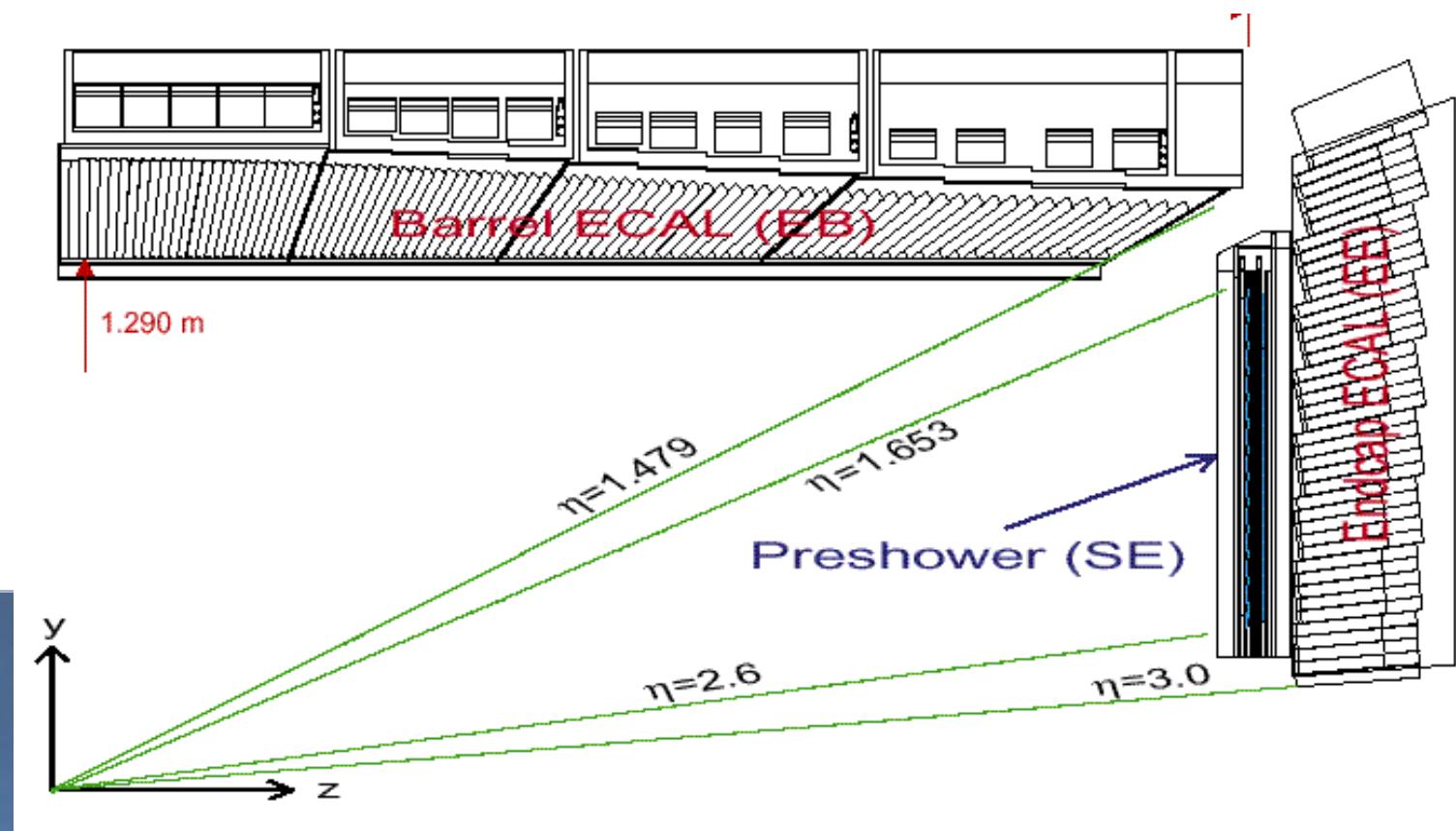
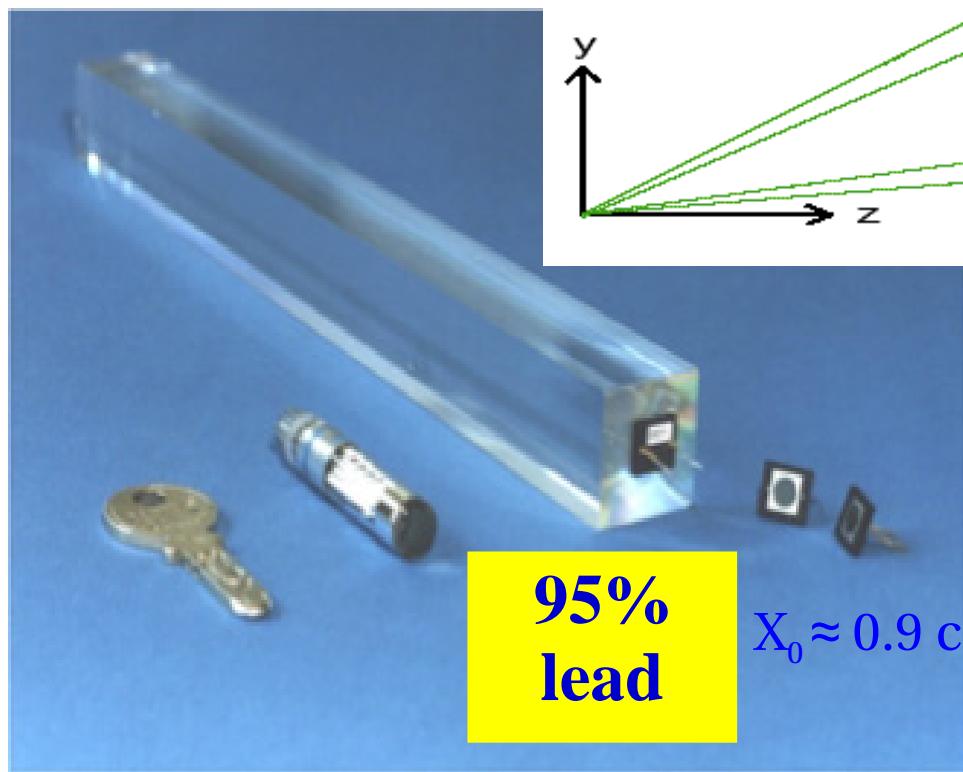
# CMS PbWO Crystals

Charged particles create  
scintillation light:  $\sim 120 \text{ } \gamma/\text{MeV}$   
fast:  $95\% < 25 \text{ ns.}$



# CMS ECAL

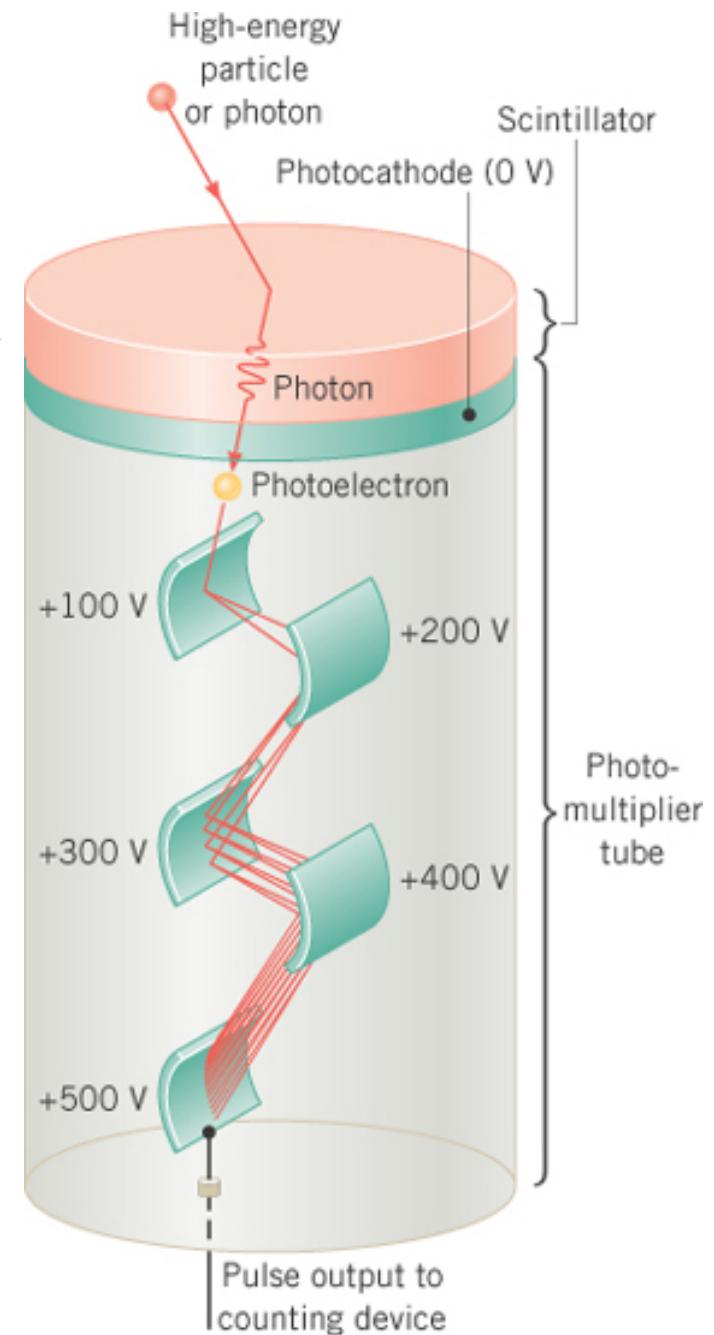
CMS  
 $\text{PbWO}_4$   
crystal  
calorimeter



- Barrel: 62k crystals  $2.2 \times 2.2 \times 23 \text{ cm}$
- End-caps: 15k crystals  $3 \times 3 \times 22 \text{ cm}$

# Photomultiplier Tube

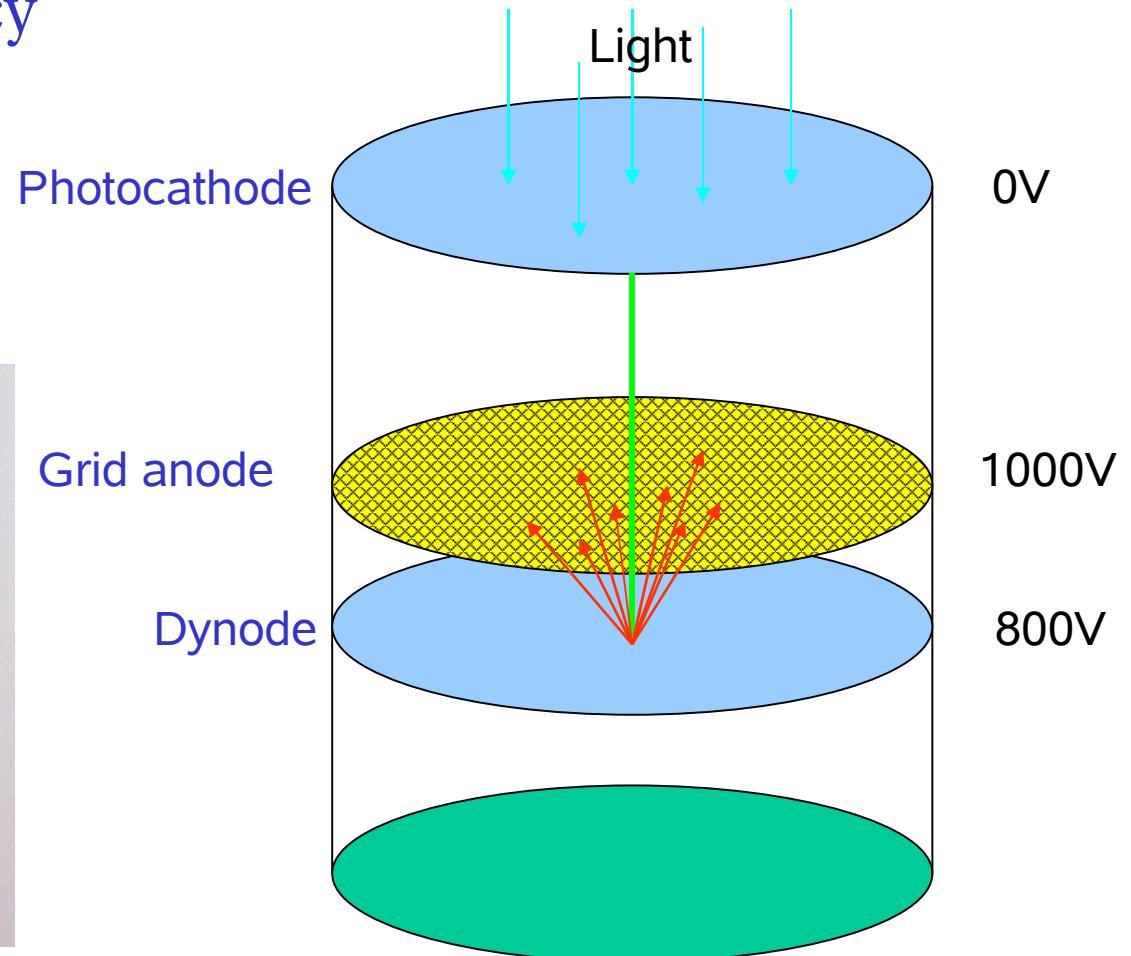
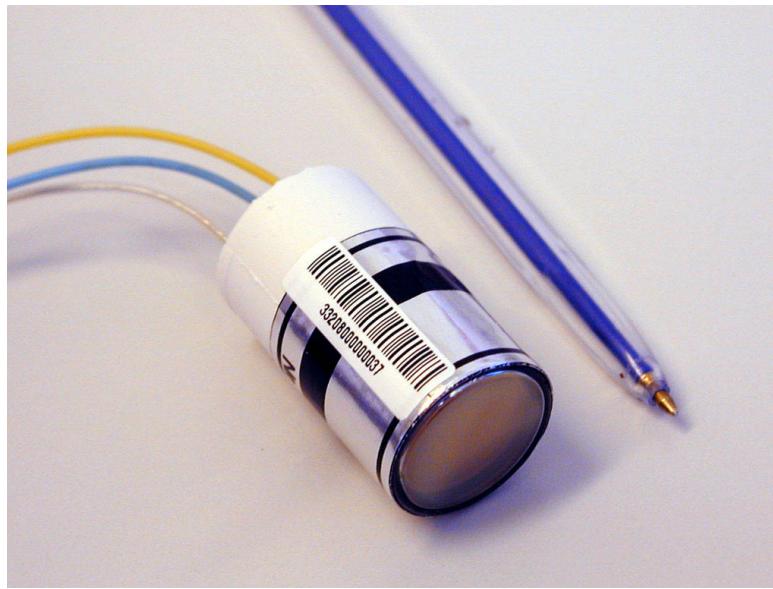
- Light falls on a photocathode and a photoelectron is emitted (photo effect)
  - ▶ **Quantum Efficiency** depends on cathode material and wavelength ( QE ~ 25% )
- Photoelectron focused and accelerated towards the first **dynode** by electric field.
- Photoelectron strikes dynode and several electrons are emitted (on average n ~ 5)
- Several dynodes (~ 10-15) give high gain (~  $10^7$ )
- High speed: few ns transit time.
- Gain can be much lower in magnetic fields, depending on orientation.



Source: Cutnell and Johnson, 7th edition image gallery

# Vacuum photo-triodes

- ~20% quantum efficiency
- Single-stage photomultiplier
- Gain  $\sim 10$  at  $B = 4$  T



radiation-resistant UV glass window  
used in the CMS endcap ECAL.

# Avalanche Photodiode

85% quantum efficiency

300-400 V reverse bias:

photoelectrons create cascade of electron-hole pairs in the bulk.

Gain ~100 in linear mode.

Low sensitivity to magnetic field.

**APD gain decreases by 2.3%/°C.**

**Crystal light yield decreases by 2.2%/°C**

**Need temperature stabilization  
within 0.1°C in the ECAL!**

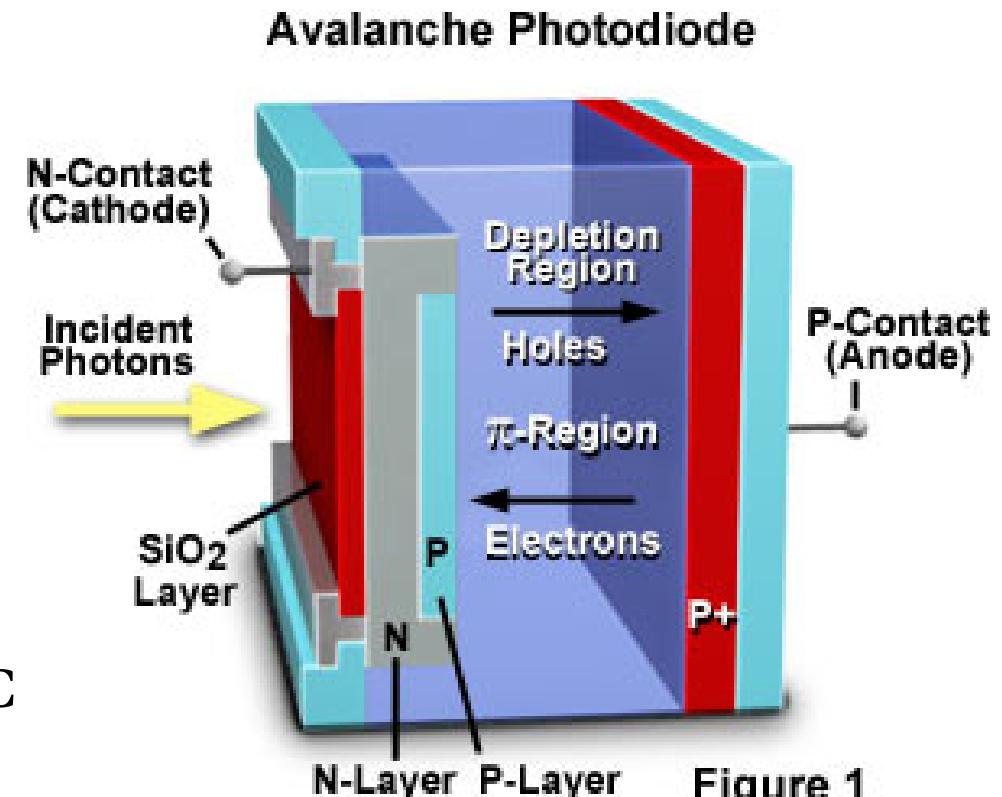
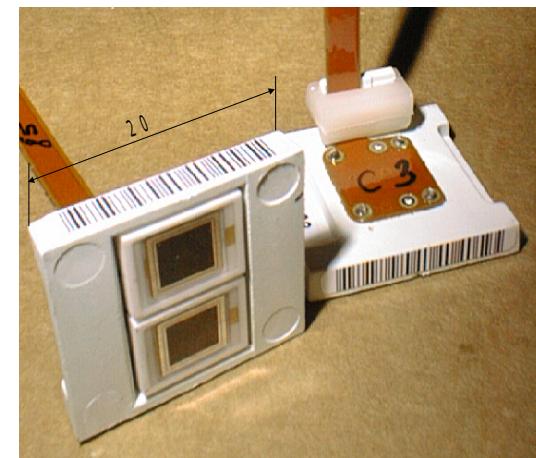
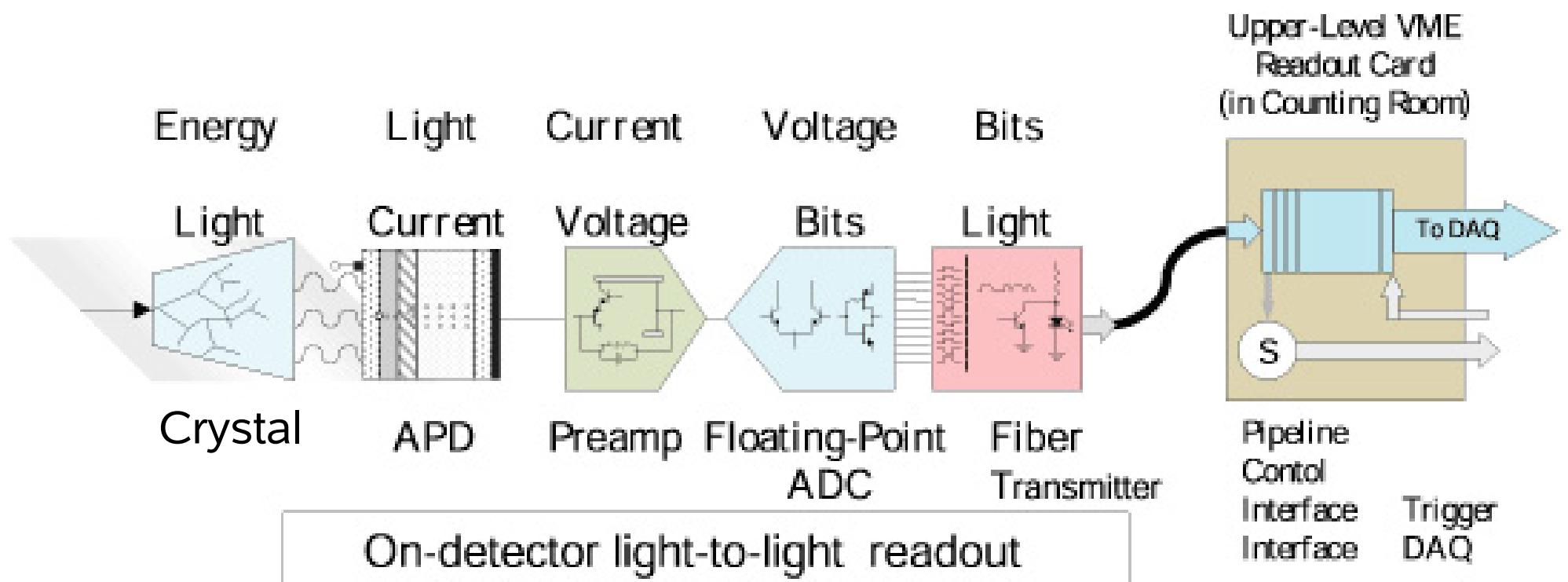


Figure 1

2 avalanche photodiodes  
per crystal in the barrel:

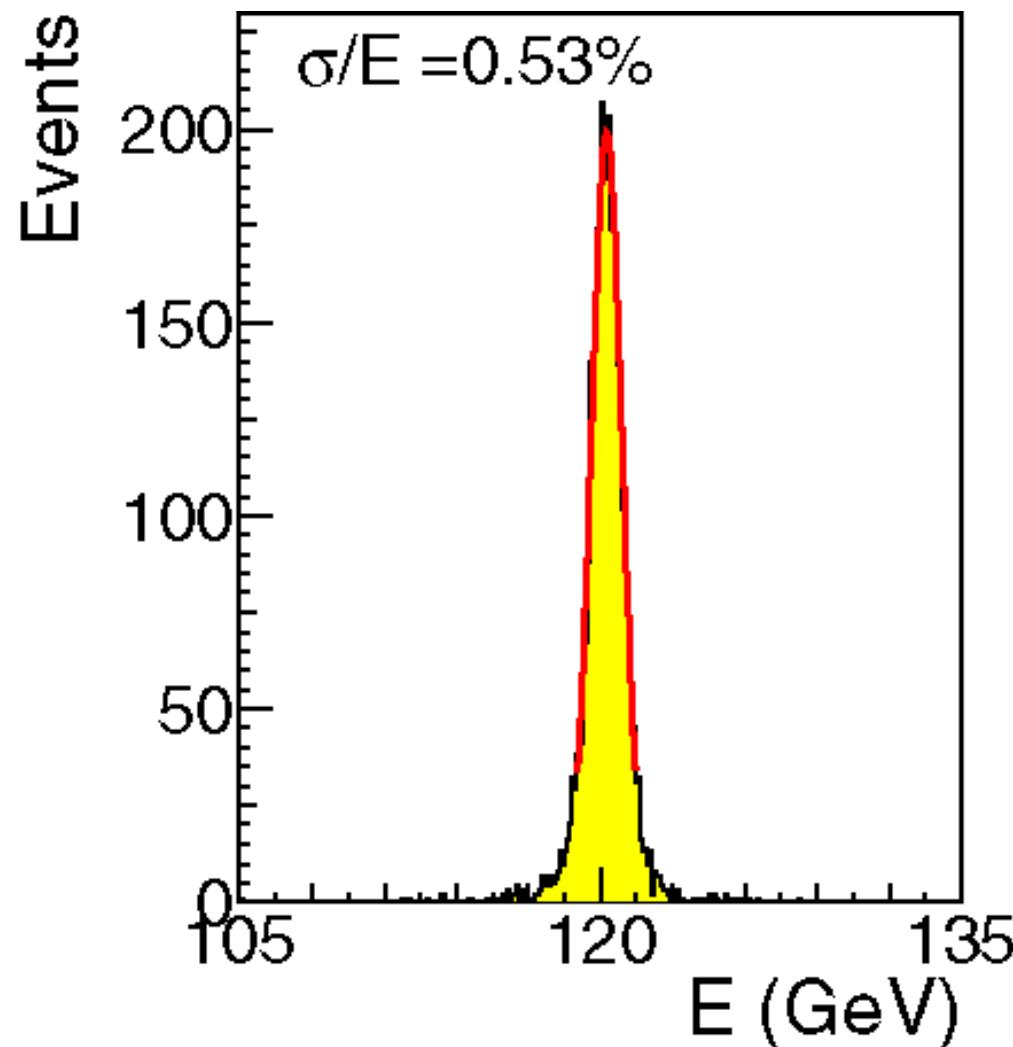


# CMS EM Calorimeter Readout



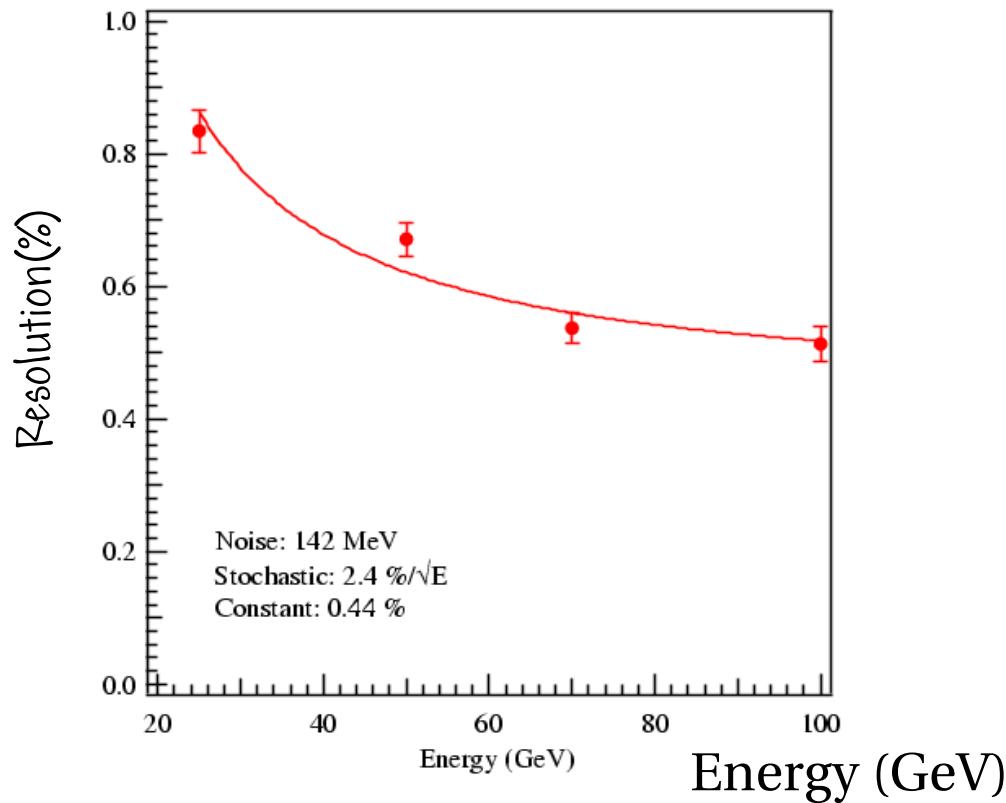
# Test beam calibration

Response of a  $\text{PbWO}_4$  calo to a  
120 GeV  $e^-$  test beam:

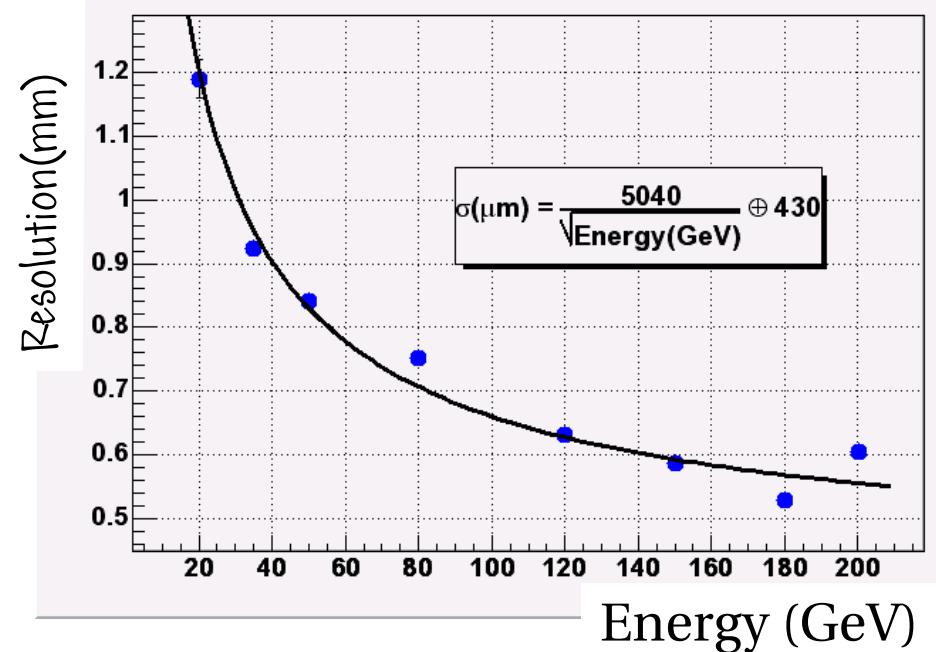


# CMS ECAL Test beam with final electronics.

*Energy*



*Position*



$$\frac{\sigma(E)}{E} = \frac{2.4 \%}{\sqrt{E}} \oplus \frac{142 \text{ MeV}}{E} \oplus 0.44 \%$$

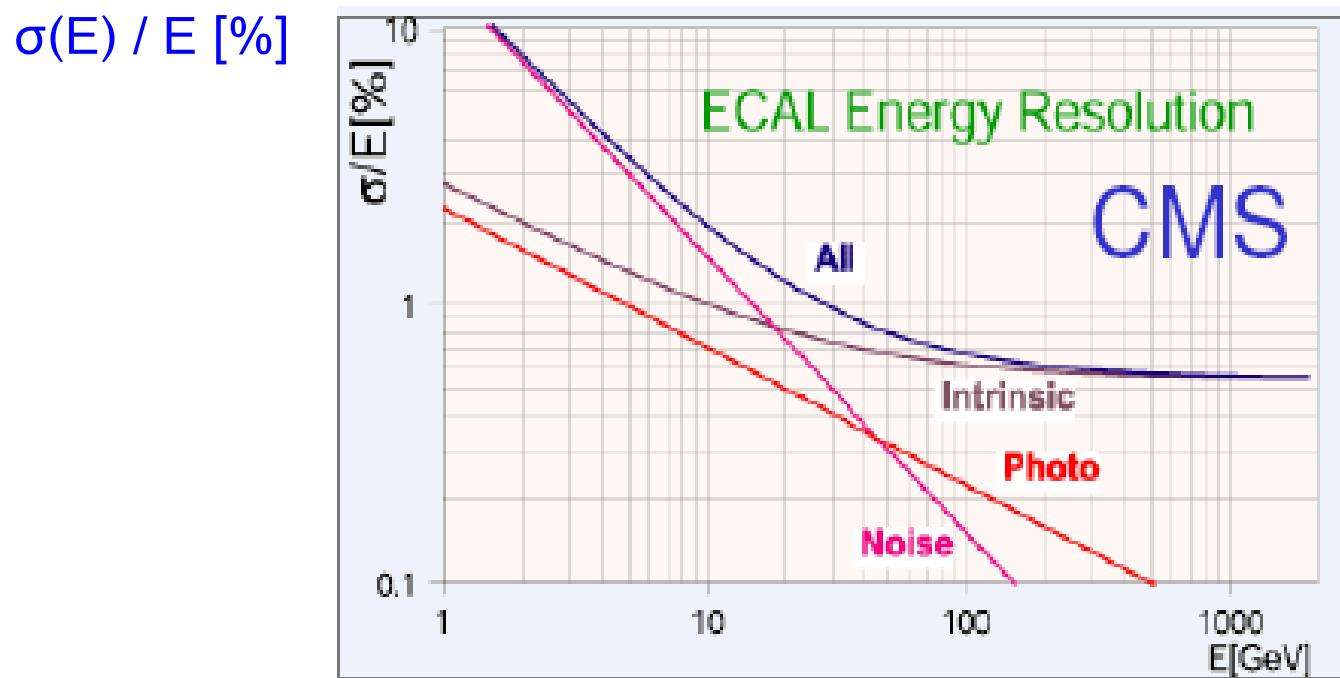
*0.6% at 50 GeV.*

$$\sigma_Y (\mu\text{m}) = \frac{5040}{\sqrt{E}} + 430$$

*0.85 mm at 50 GeV.*

# Energy resolution terms

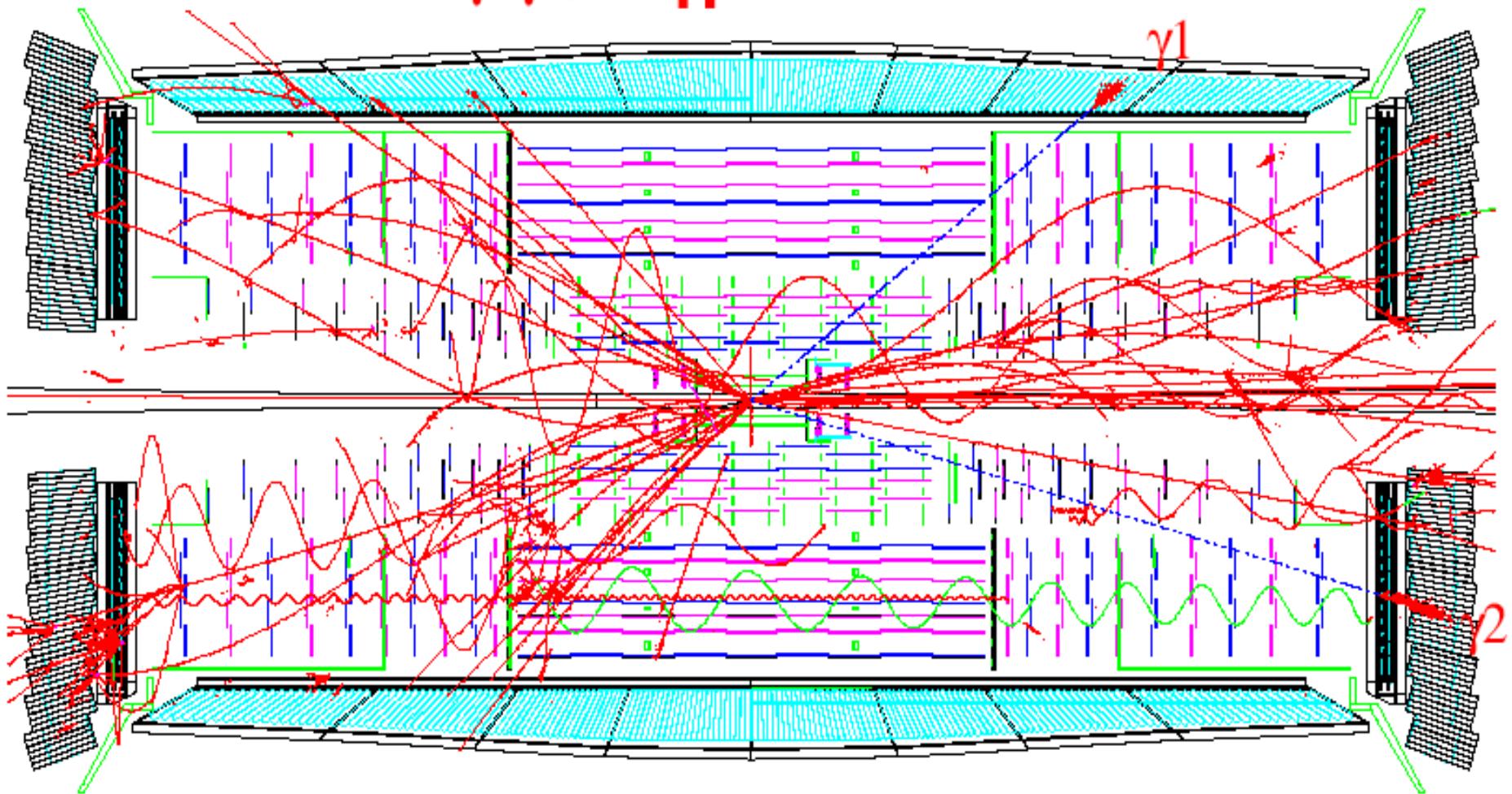
- The intrinsic shower fluctuations give  $\sigma(E) \sim \sqrt{E}$
- Fluctuations in the photo-electron yield also give  $\sigma(E) \sim \sqrt{E}$
- Noise (electronics, radiation) gives a constant term:  $\sigma(E) = c$
- Inhomogeneities and leakage give  $\sigma(E) \sim E$



$$\frac{\sigma(E)}{E} = \frac{2.4\%}{\sqrt{E}} \oplus \frac{142 \text{ MeV}}{E} \oplus 0.44\%$$

# Higgs decay into two Photons

$H \rightarrow \gamma\gamma, M_H = 100 \text{ GeV}$

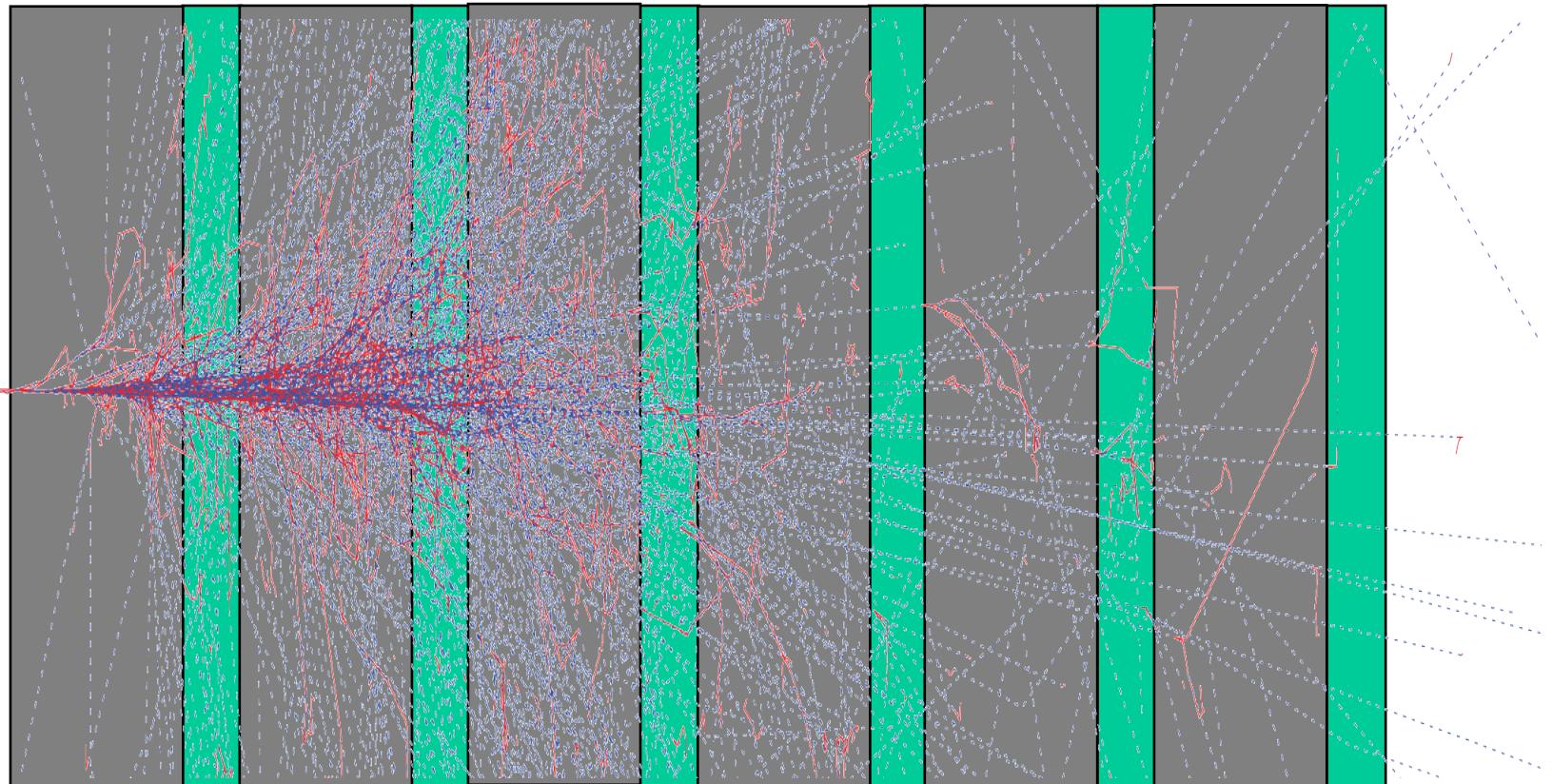


# Sampling calorimeter

Absorber and detector are separated as passive and active layers.

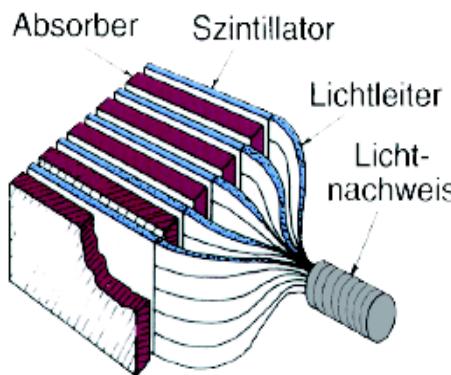
**Absorber:**  
Lead,  
Tungsten,  
Uranium

**Detector:**  
MWPC,  
scintillator,  
silicon pads,  
noble liquid

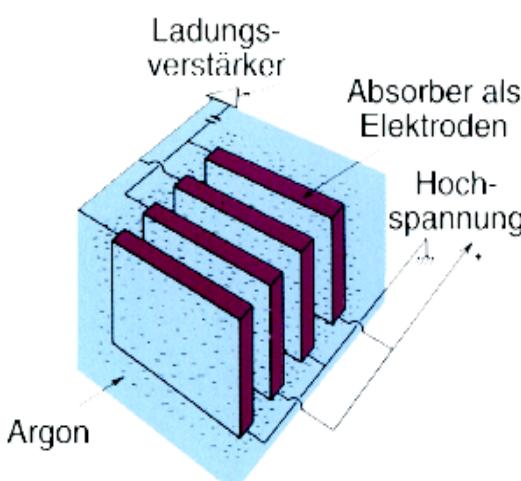


The active detector material **samples** a fraction  $F$  of the shower.  
The detector signal is still proportional to the incident energy.  
Allows longitudinal segmentation, good for hadrons.  
Energy resolution is degraded  $\sim 1/\sqrt{F}$  ('sampling fluctuations').  
Less expensive.

# varieties of sampling calorimeters

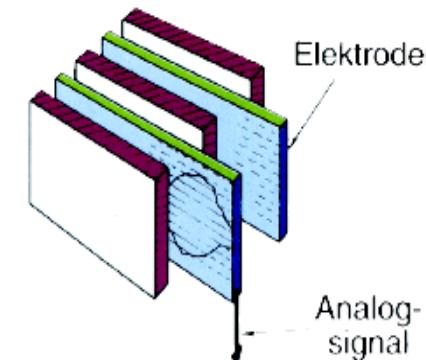
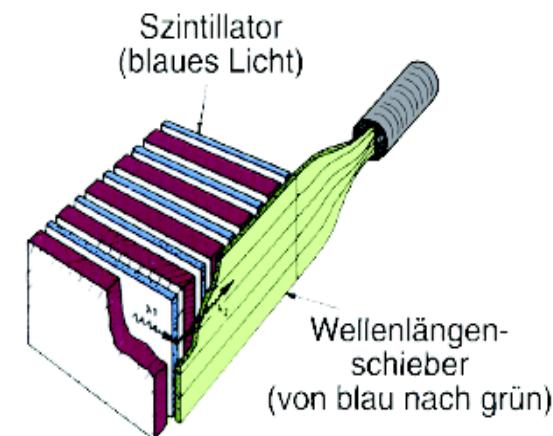


Absorber + scintillor  
with photomultiplier readout  
Fixed target experiments

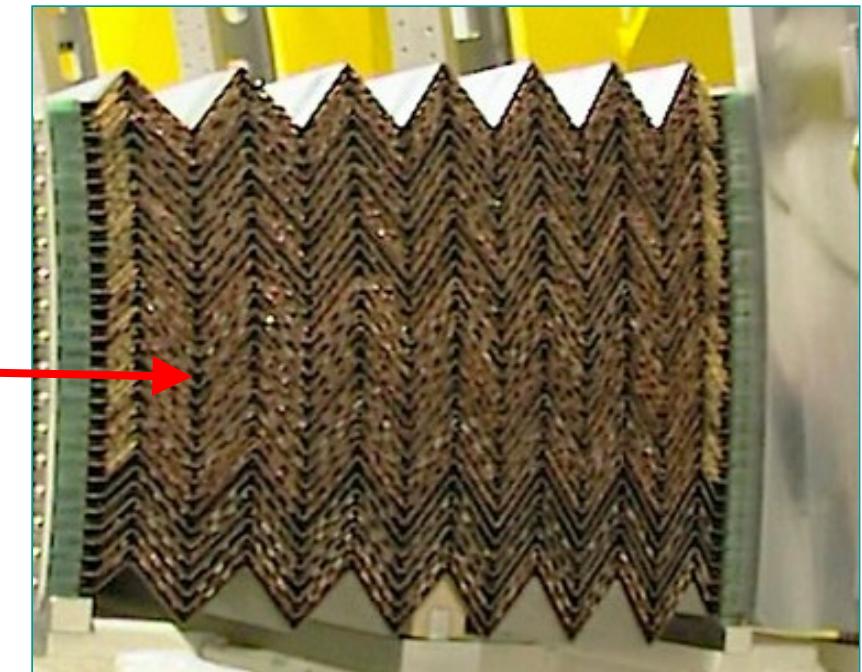
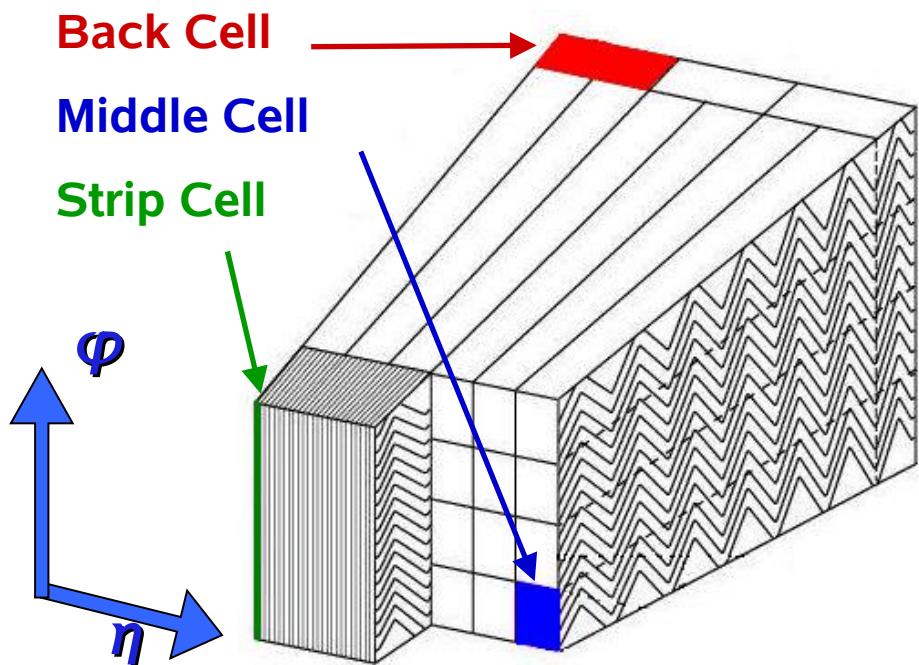


Absorber and liquid argon  
electronic readout of ionization signal  
H1 at HERA, D0 at Tevatron, ATLAS

Gas ionisation chamber:  
DELPHI and ALEPH at LEP



# ATLAS LAr ECAL

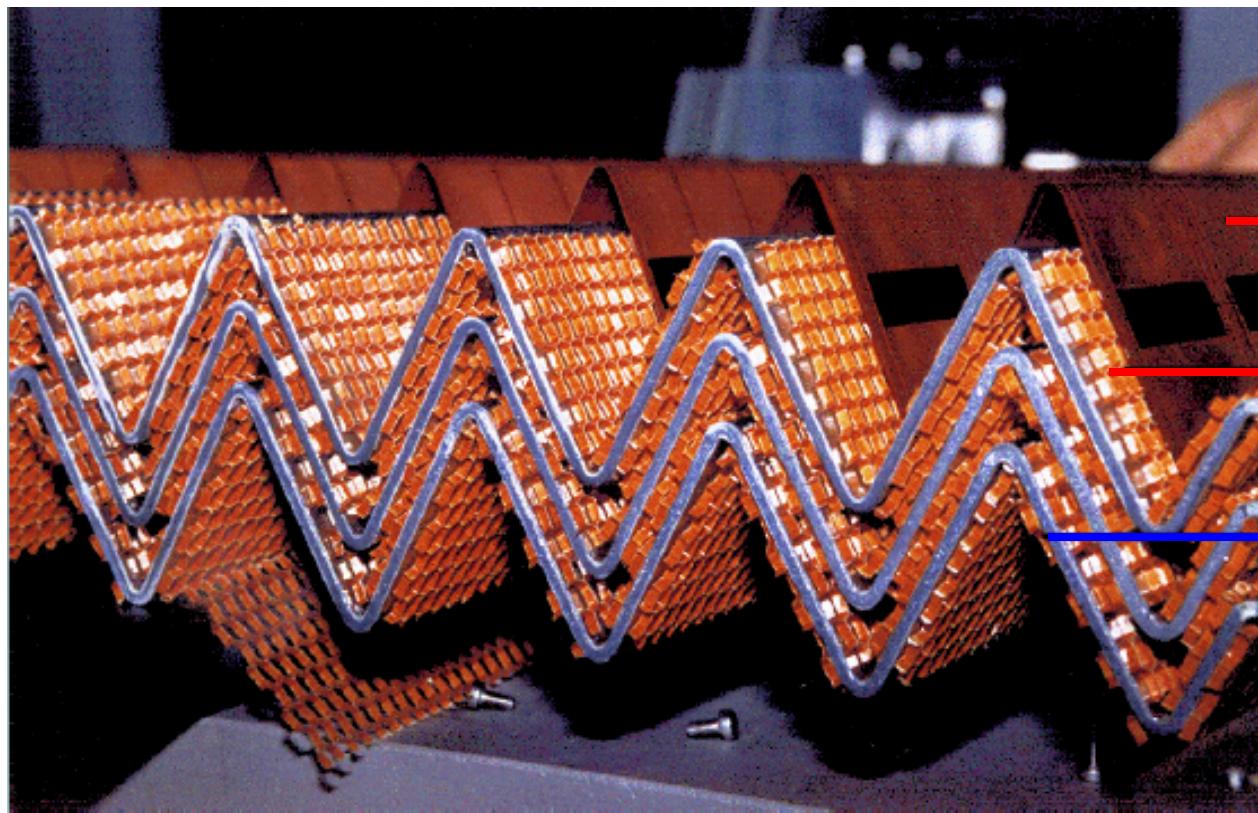


3 sections:

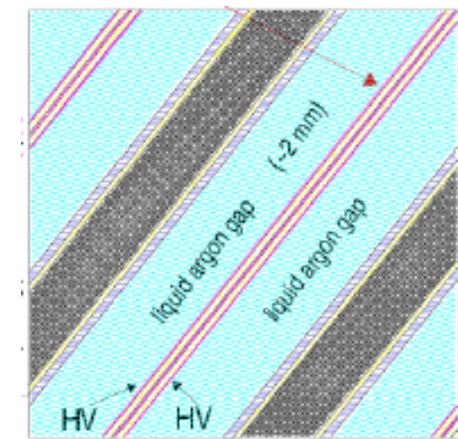
- strips for position resolution
- middle for energy measurement
- back for leakage control

- Pb absorber in LAr
- Accordion geometry for routing of readout signals to the back
- Allows dense packing and fine granularity.

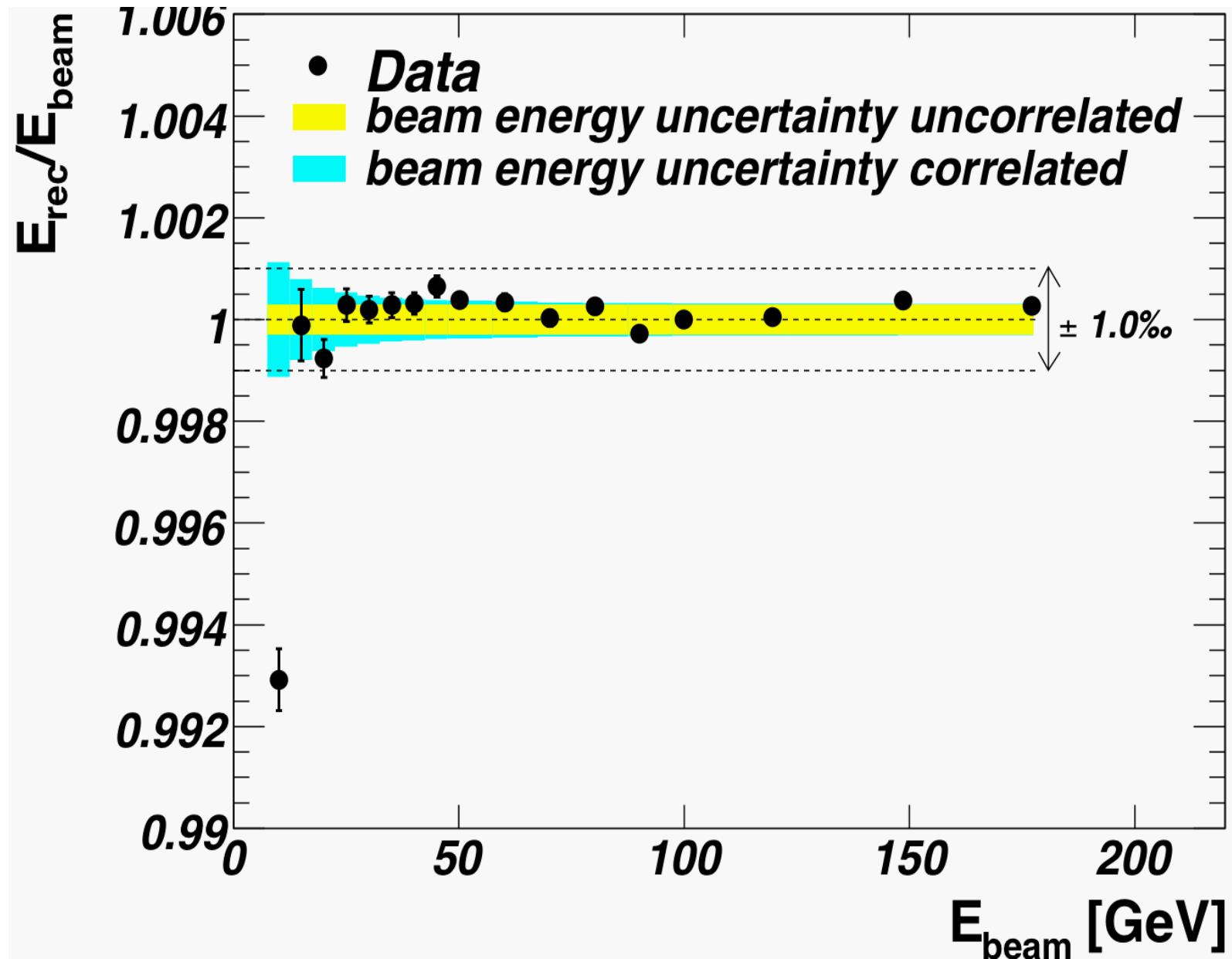
# ATLAS LAr ECAL



- Cu electrodes at +HV
- Spacers define LAr gap  
 $2 \times 2$  mm
- 2 mm Pb absorber  
clad in stainless steel.

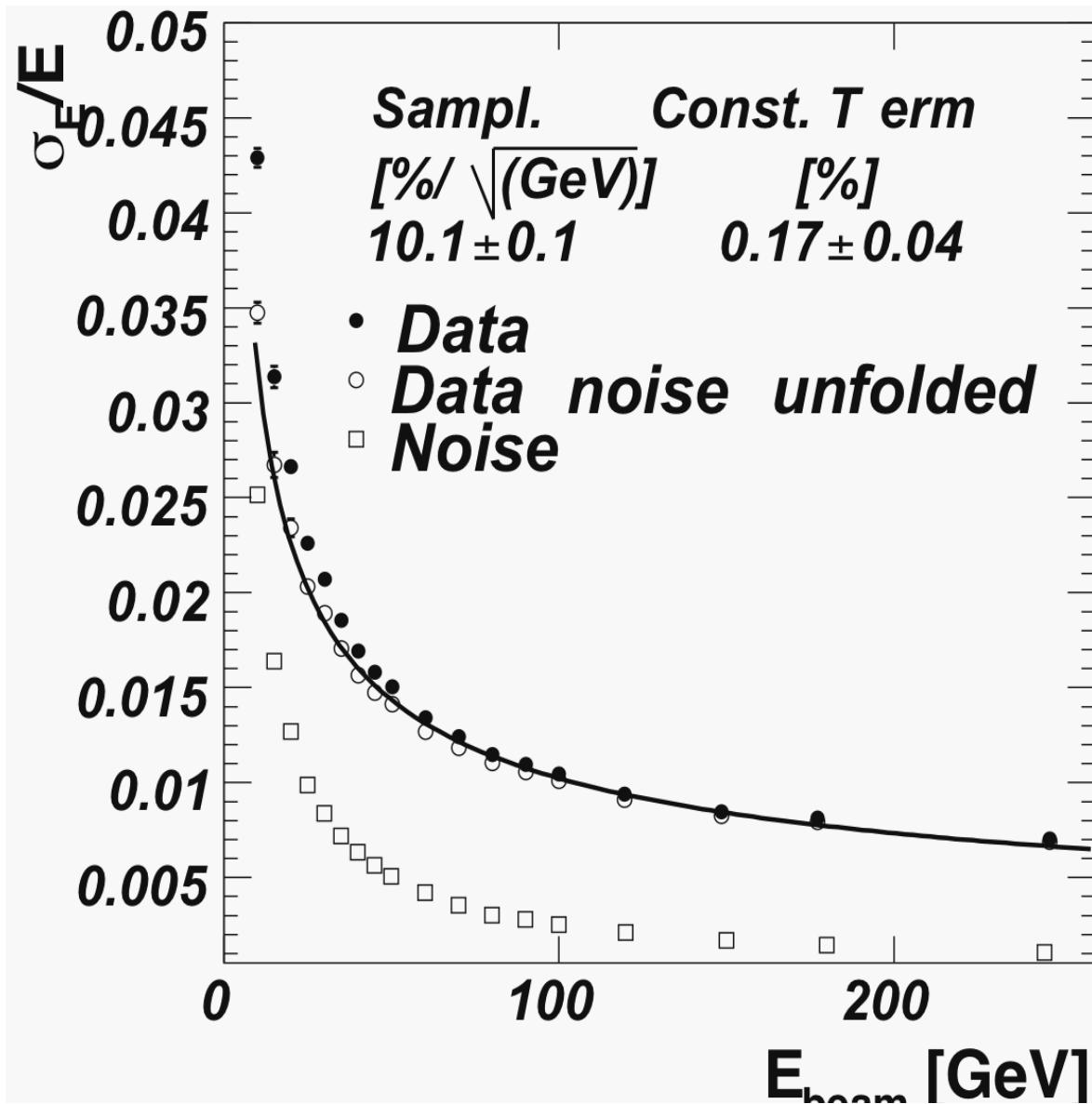


# ATLAS LAr Barrel ECAL Linearity

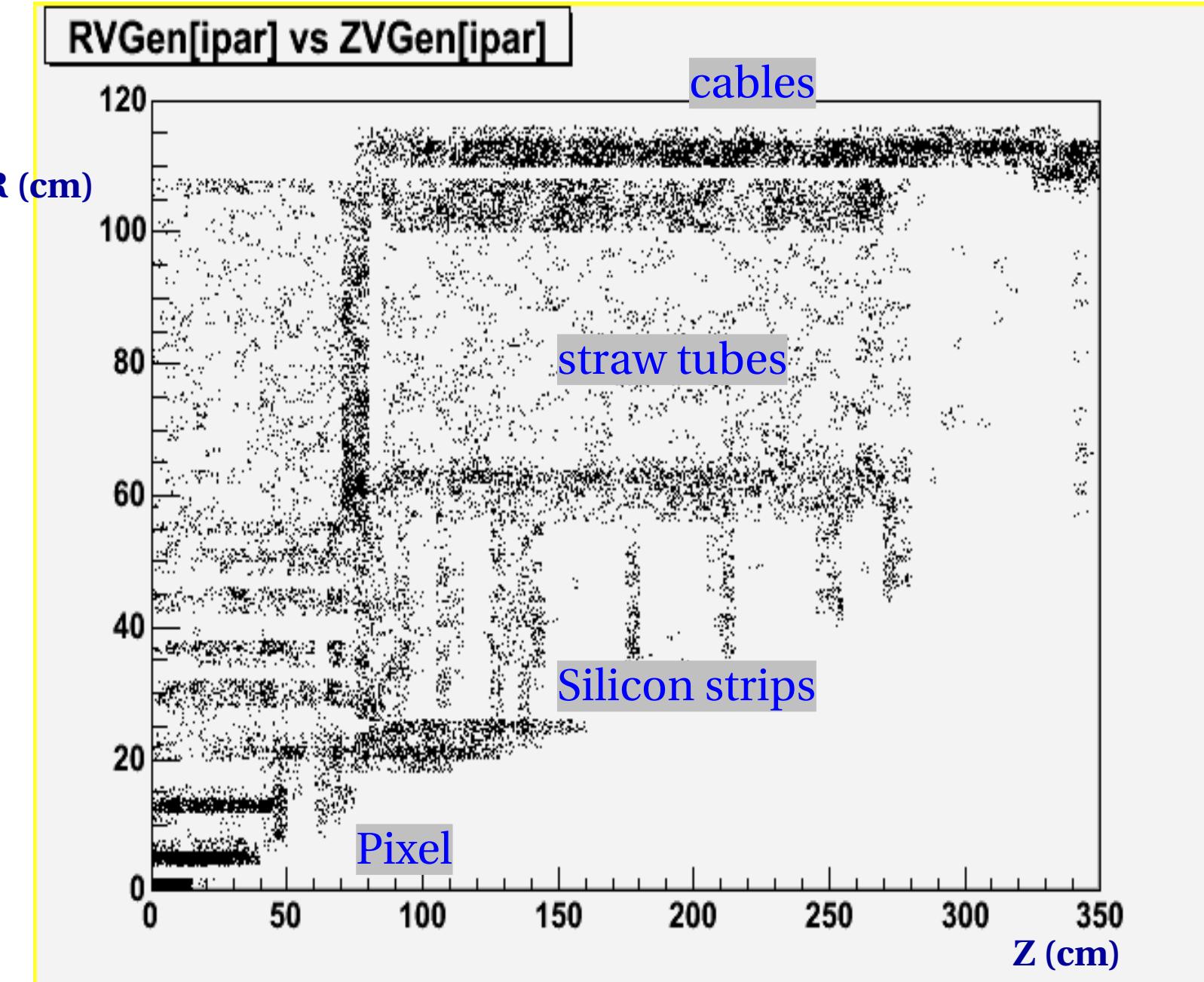


within 0.1% for 15-180 GeV,  $E=10$  GeV 4 per mil too low, reason unclear&

# ATLAS LAr Barrel ECAL resolution



# Photon conversions in the ATLAS tracker simulation



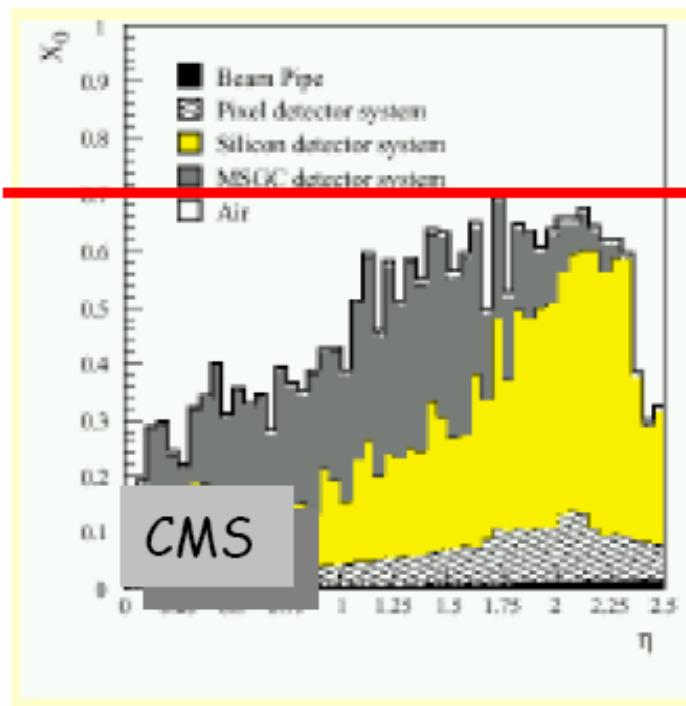
$\gamma Z \rightarrow Z e^+ e^-$

30% - 50% of all photons convert in front of the calorimeter!

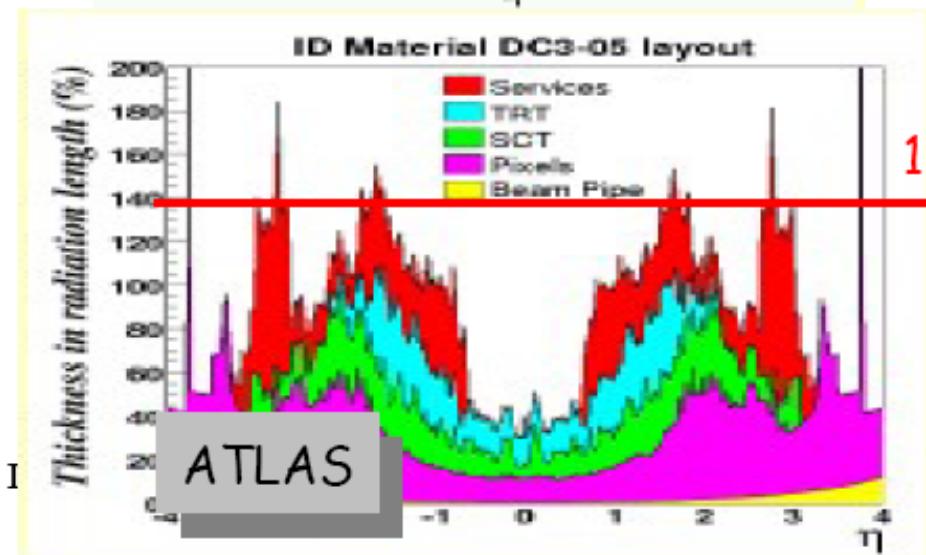
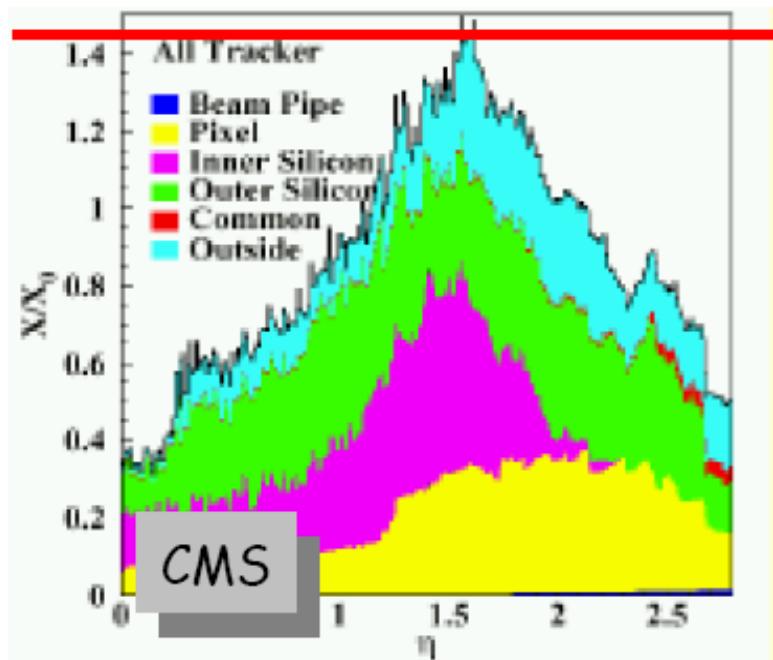
# LHC tracker material budget

Major difference / advance to LHC detectors is needed:

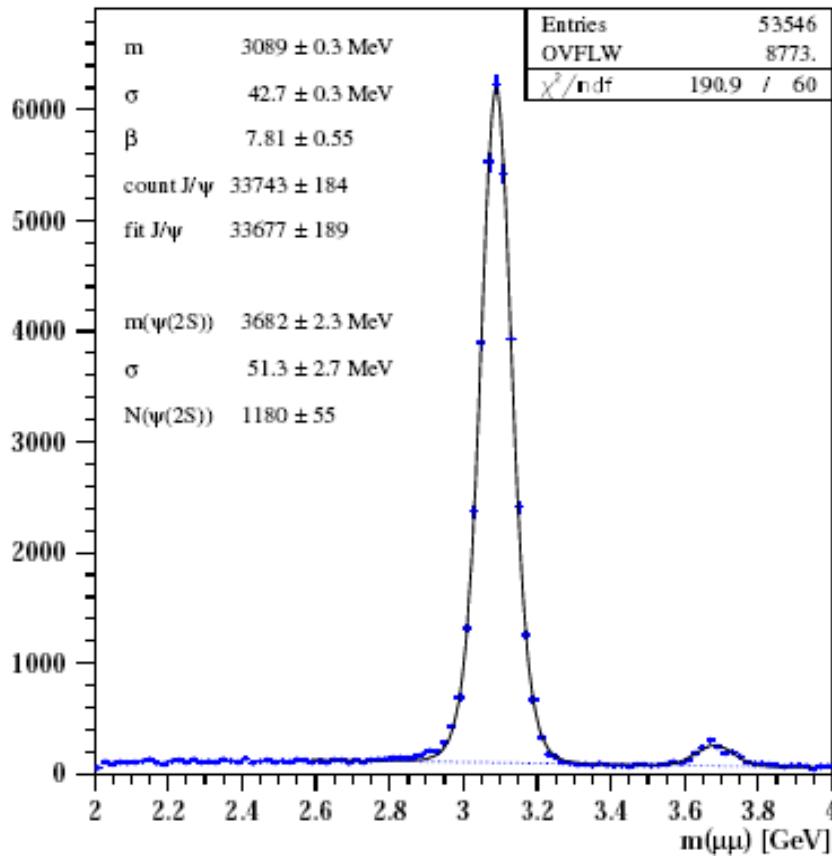
The detector TDR 1996



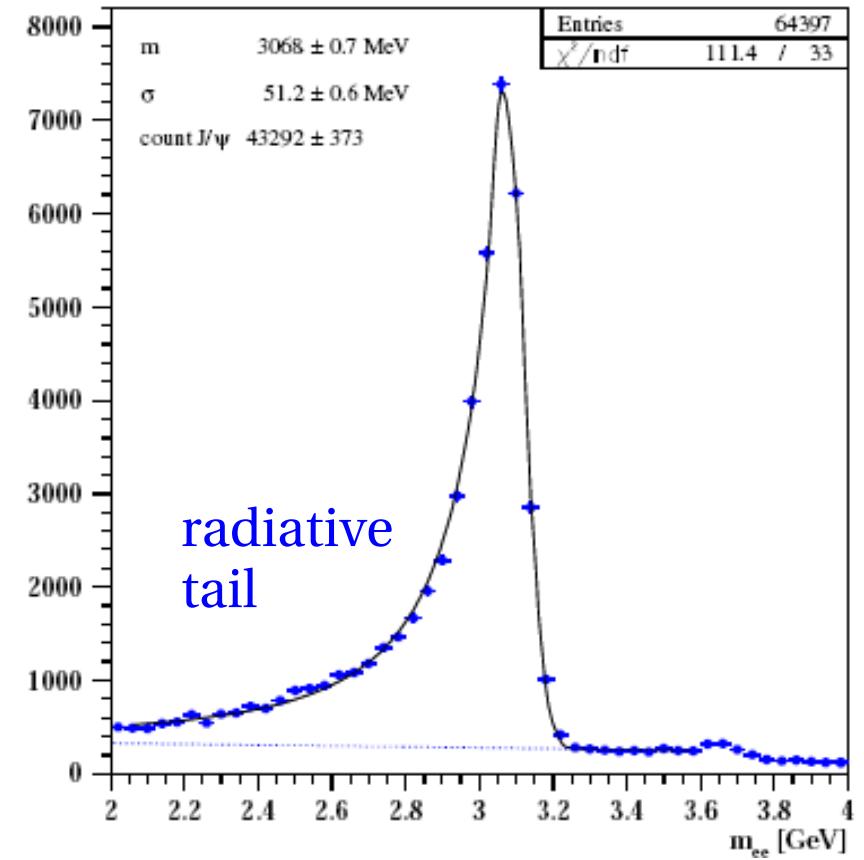
... and the reality 10 years later



# Electron tracks radiate



$J/\psi \rightarrow \mu\mu$



$J/\psi \rightarrow ee$

$e \rightarrow e\gamma$  in front of the tracker,  
e track has lower momentum.

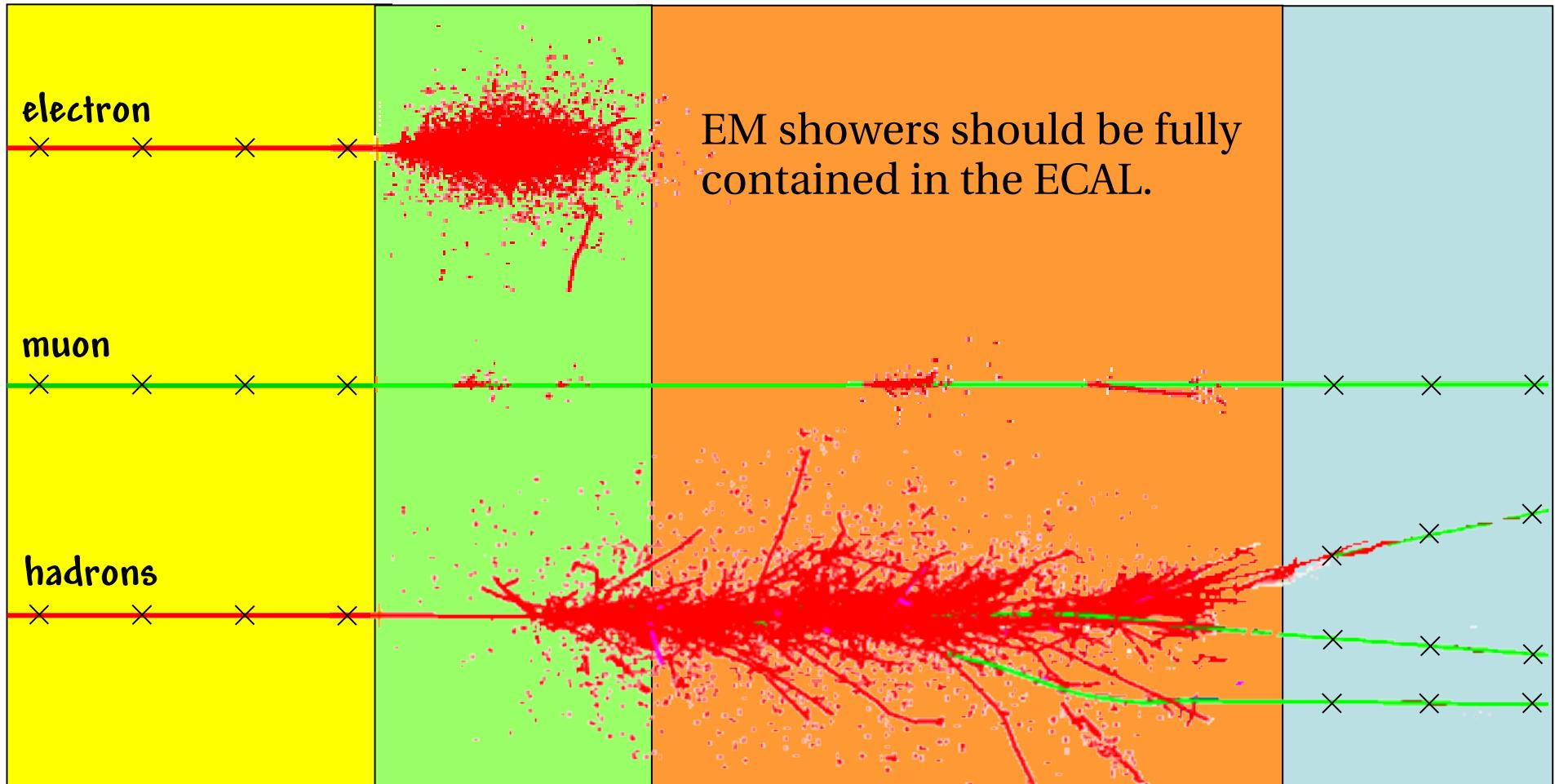
# Hadronic showers

Tracker

EM cal

Hadronic calorimeter

Muon  
tracker



Hadronic showers may already  
start in the ECAL and extend into the HCAL.

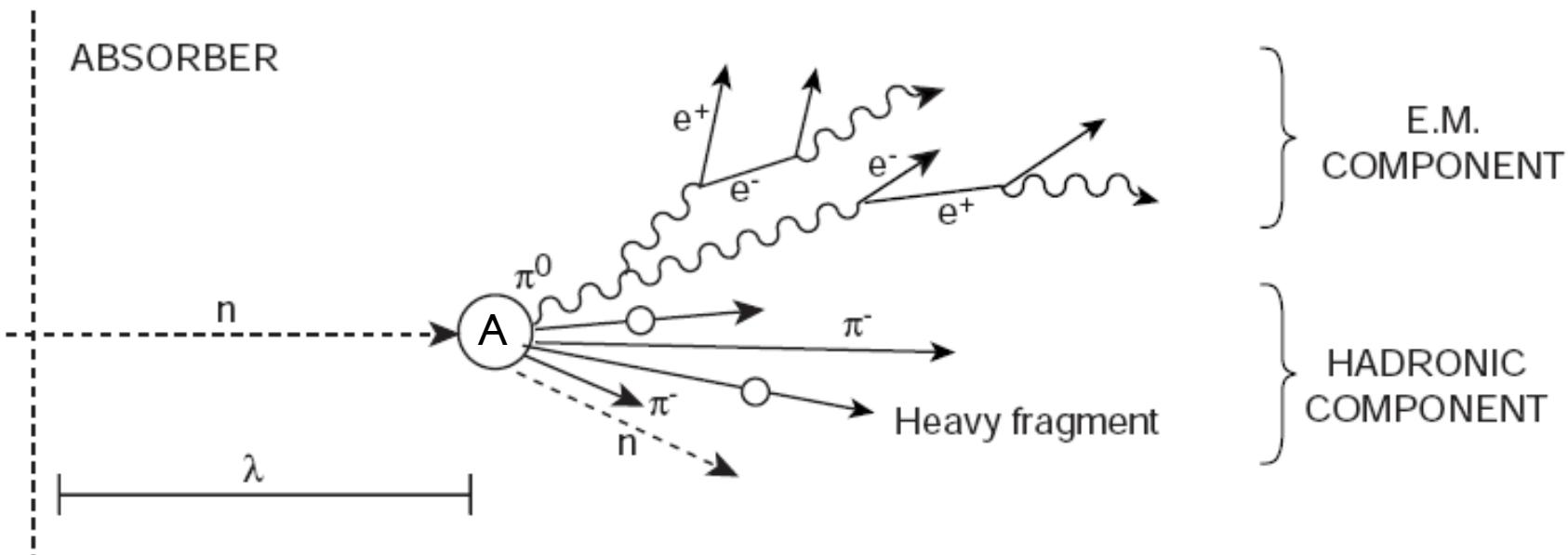
# Hadronic interaction length

- Pion-proton cross section  $\sigma(\pi p) \approx 25$  mbarn above a few GeV.
- $\sigma(\pi A) \approx \sigma(\pi p) A^{2/3}$  (black disk limit).
- $\Rightarrow$  hadronic interaction length:

$$\lambda_I = \frac{A}{\sigma N_A \rho} = \frac{35 \text{ cm}}{\rho} A^{1/3}$$

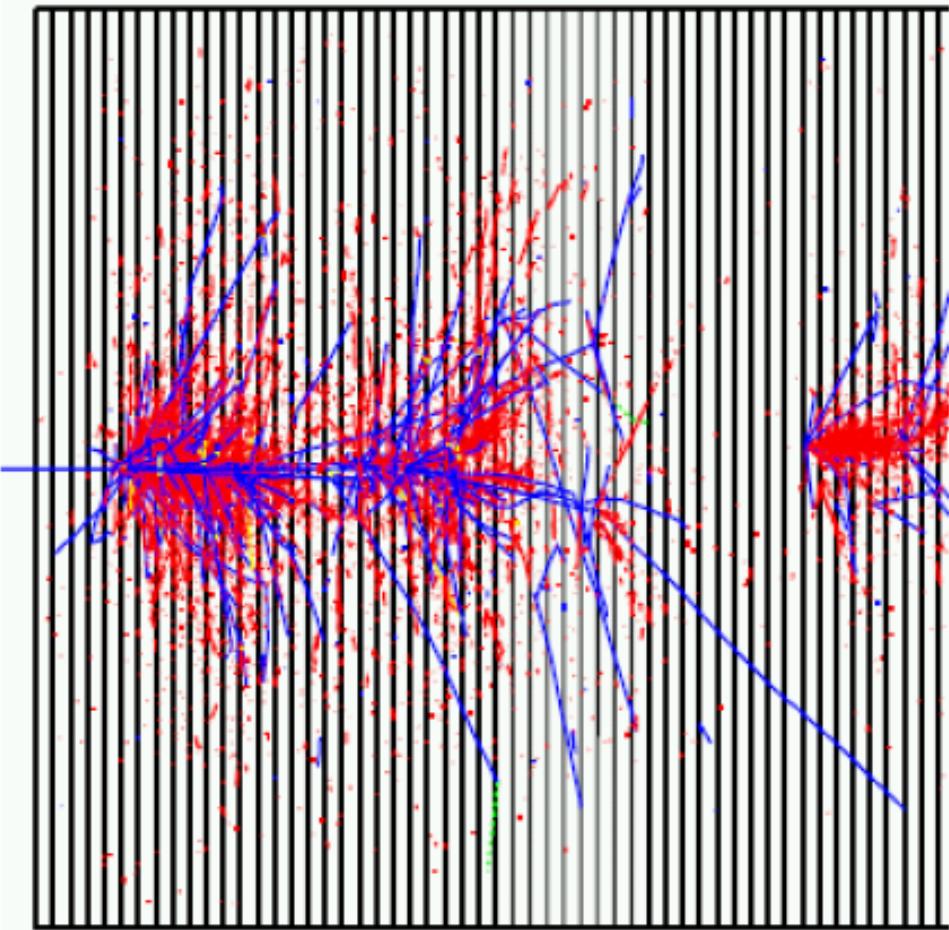
- $\lambda_I = 17$  cm in Fe or Pb.
- Much larger than  $X_0$ .

# Hadronic showers

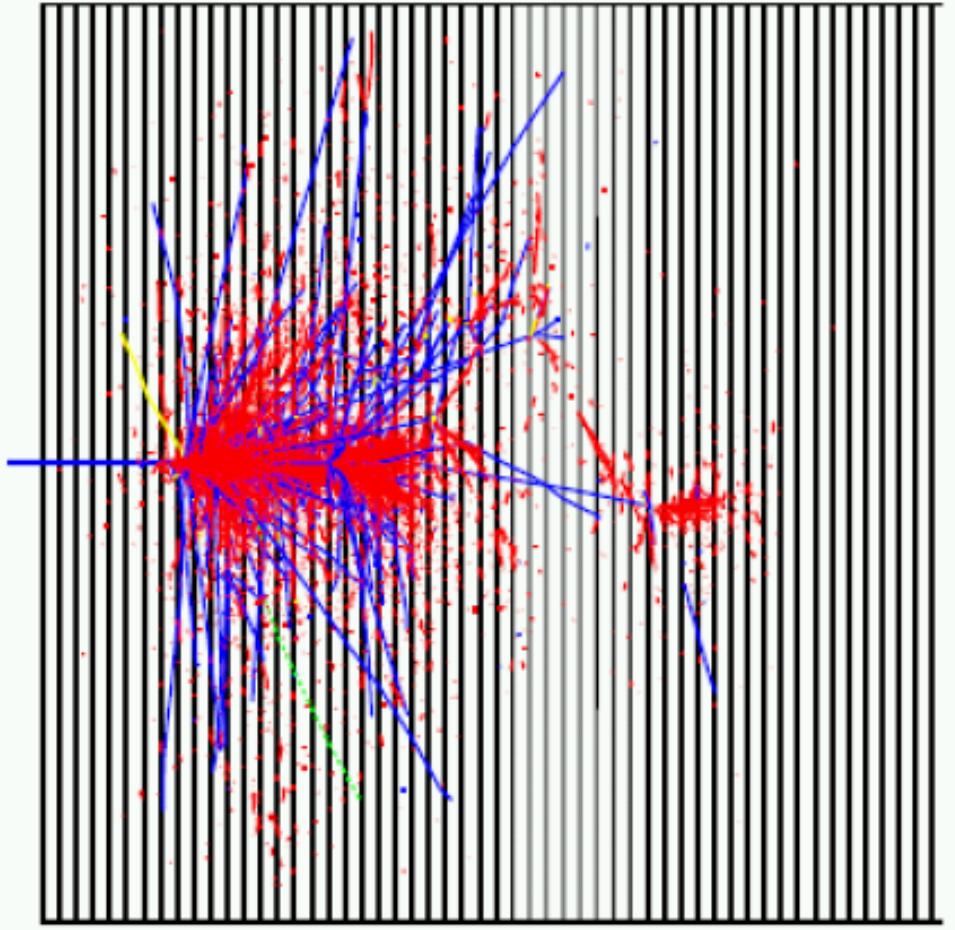


- Hadronic interaction have high multiplicity:
  - ▶ Shower is to 95% contained in  $\sim 7\lambda$  at 50 GeV (1.2m of iron).
- Hadronic interactions produce  $\pi^0$ :
  - ▶  $\pi^0 \rightarrow \gamma\gamma$ , leading to local EM showers ('hot spots', ~30%)
- Some energy lost in nuclear breakup and neutrons ('invisible energy', 15-35%).
- Stronger fluctuations in a hadronic shower:
  - ▶ Worse energy resolution.

## 2 hadronic showers



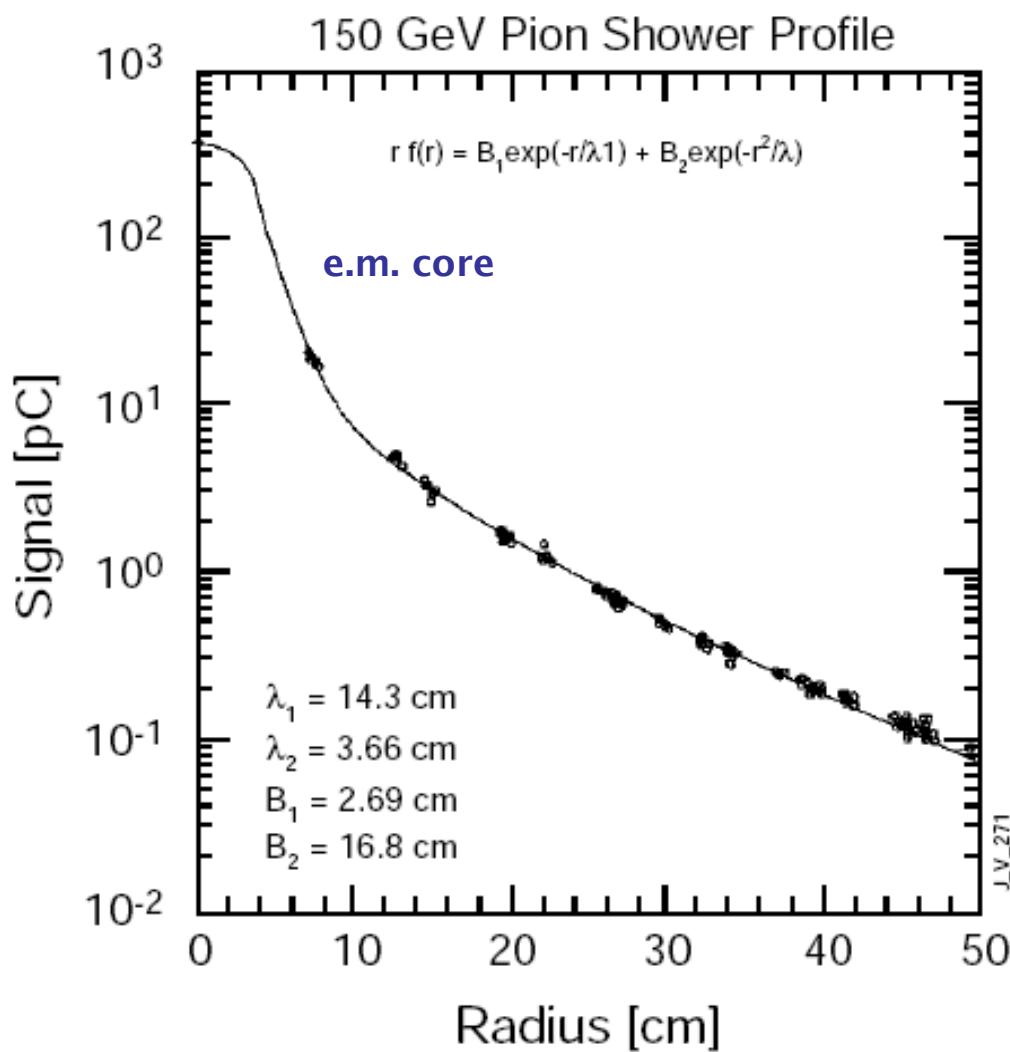
blue = hadronic component



red = electromagnetic component

A good hadron calorimeter should have  
equal response to hadrons and electrons ('hardware compensation')  
or high granularity to isolate the hot spots ('software compensation')

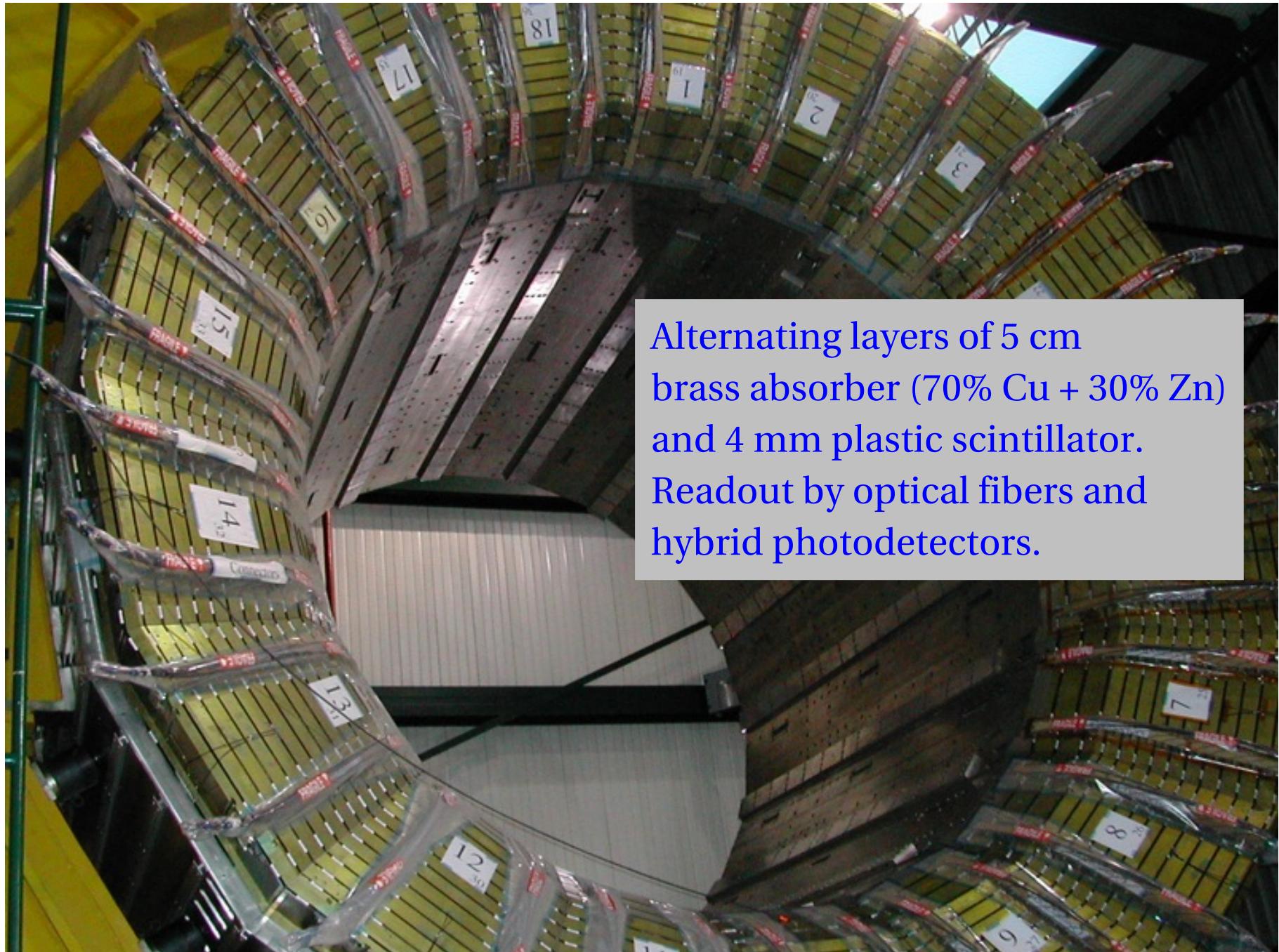
# Hadron shower transverse size



- Transverse shower development:
  - ▶ The secondaries have significant transverse momenta and produce a wide shower (compared with EM showers)
  - ▶ Part of the shower gets an electromagnetic nature (i.e. The decay of the  $\pi^0$  produced in the interaction) and does remain inside a narrow cylinder (two times the Moliere radius)

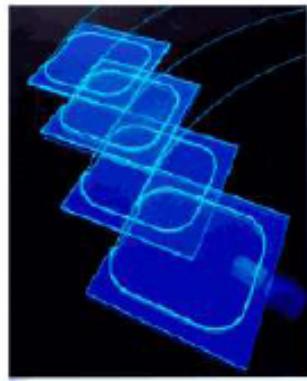
T.S.Virdee, Proc. of the 1998 European School of High-Energy Physics, CERN 99-04

# CMS Hadron calorimeter



Alternating layers of 5 cm brass absorber (70% Cu + 30% Zn) and 4 mm plastic scintillator.  
Readout by optical fibers and hybrid photodetectors.

# CMS HCAL readout

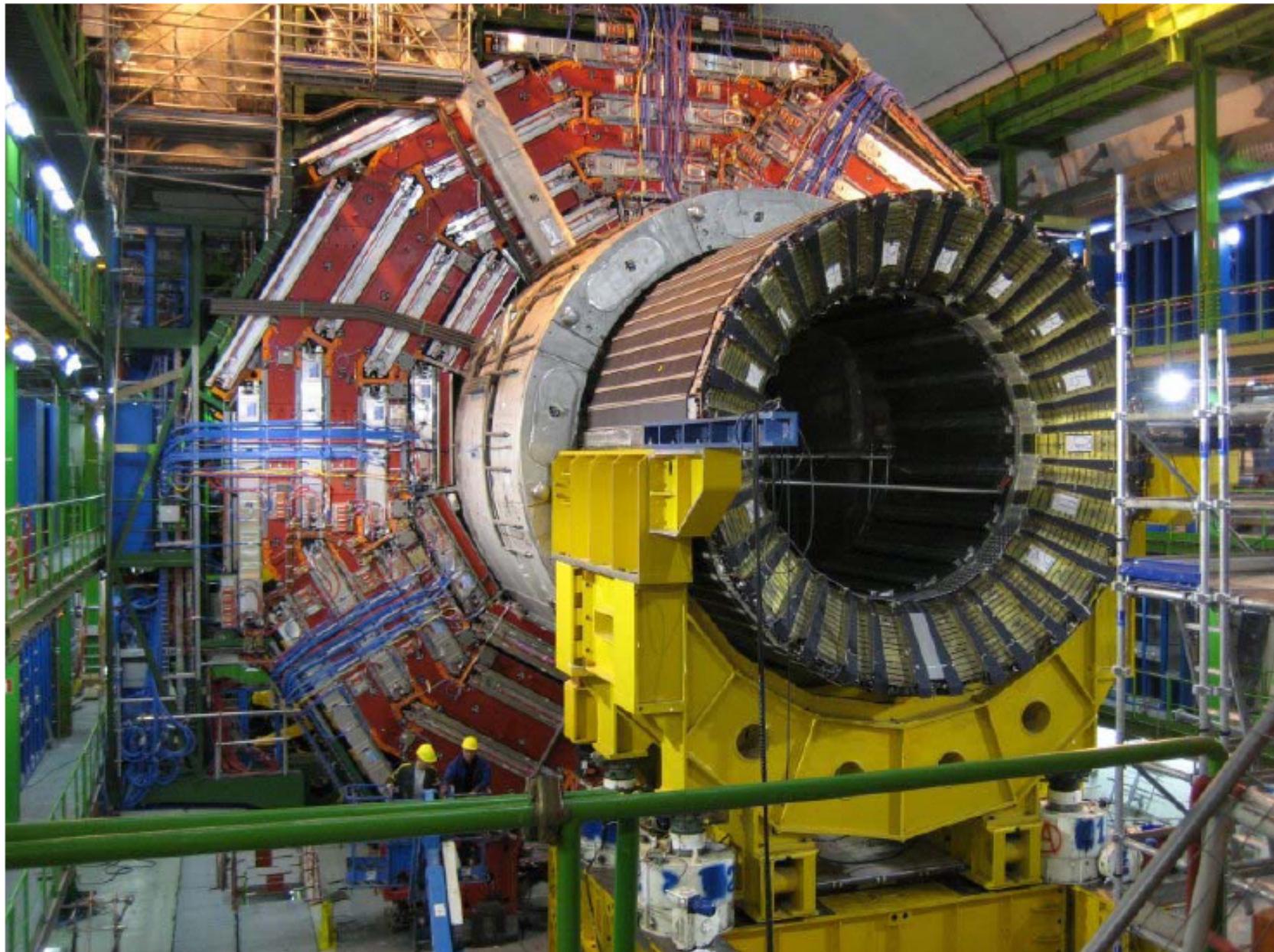


- Scintillators coupled to readout fibers.
- Bundles of fibers coupled to an avalanche photodiode
- ECAL+HCAL energy resolution for pions:

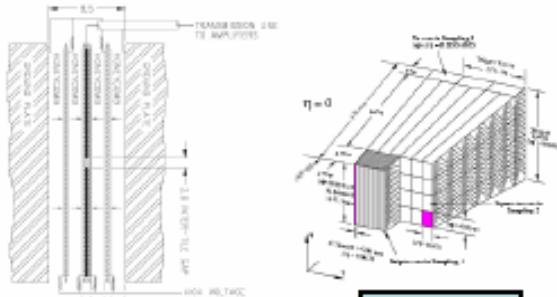
$$\frac{\sigma(E)}{E} = \frac{127\%}{\sqrt{E}} \oplus 6.5\%$$



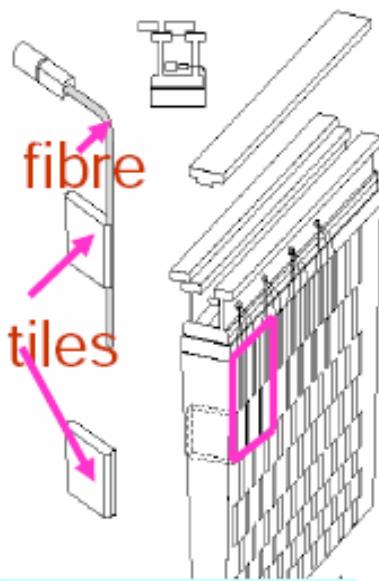
# Inserting the CMS Hadron Calorimeter



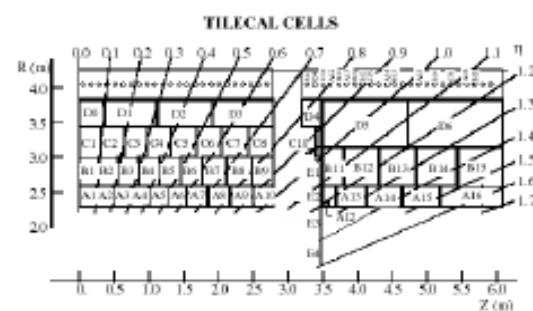
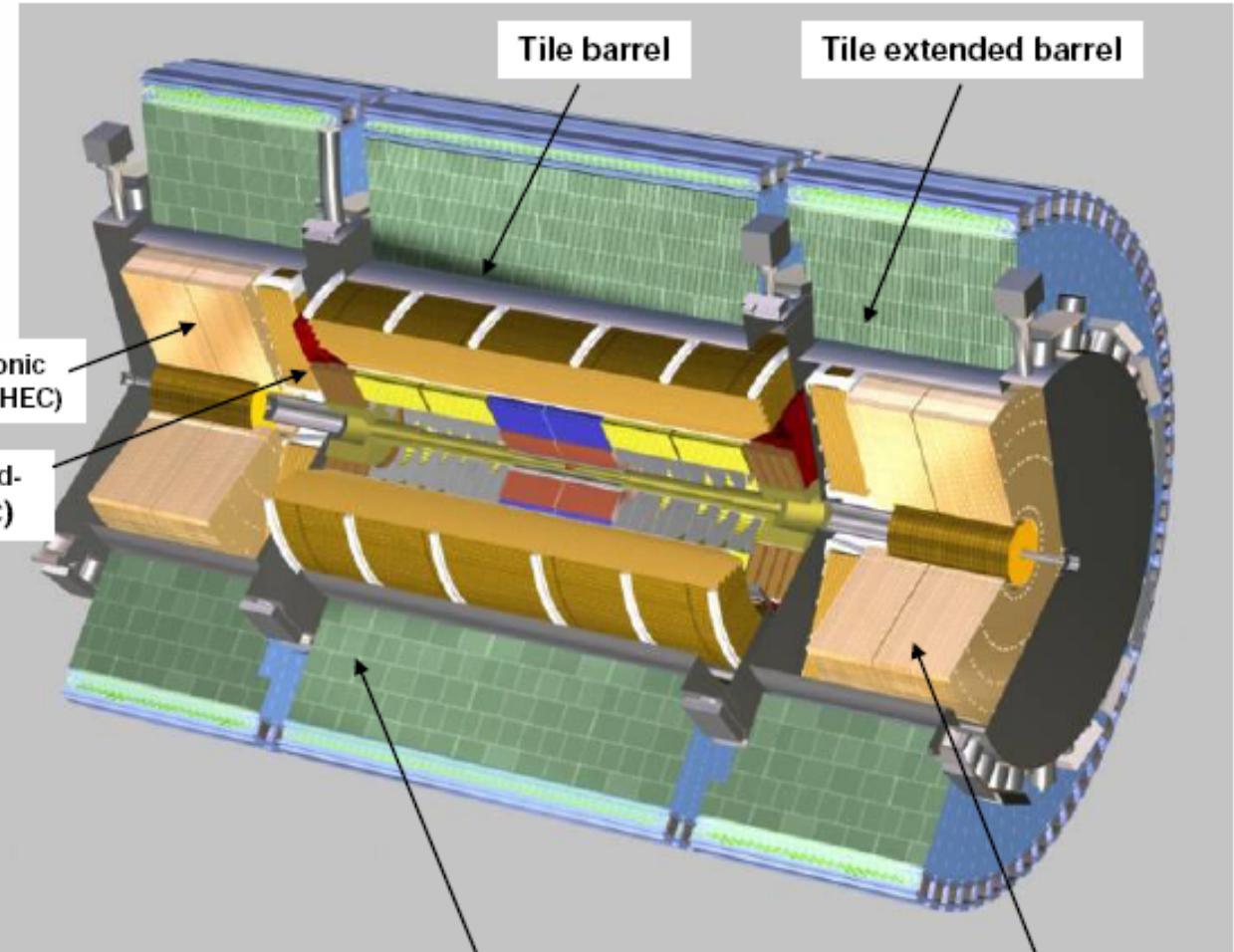
## LAr and Tile Calorimeters



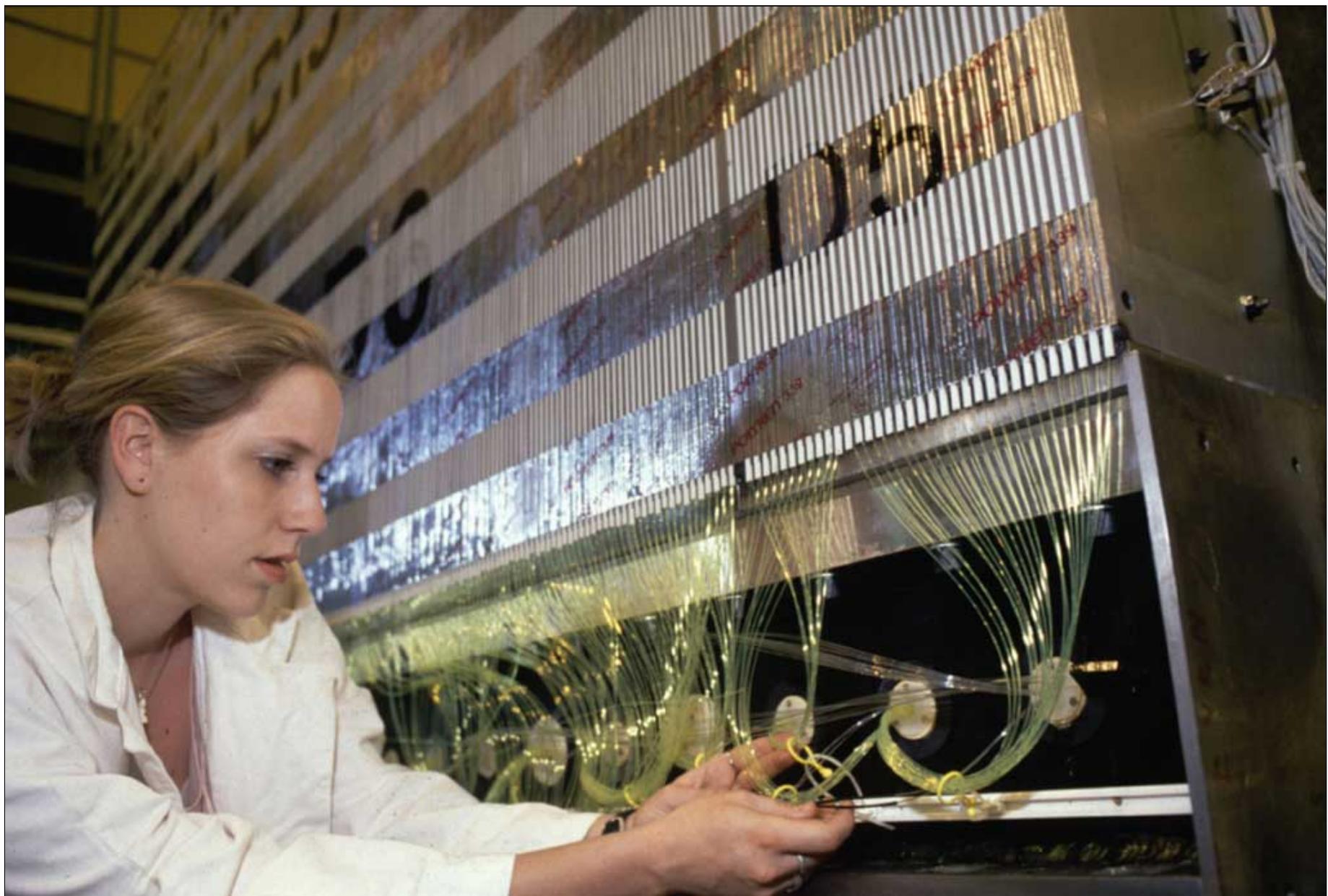
**L-Ar  
Acordeon  
module**



**A TileCal Module  
64 Barrel  
2x64 Ext. Barrel**



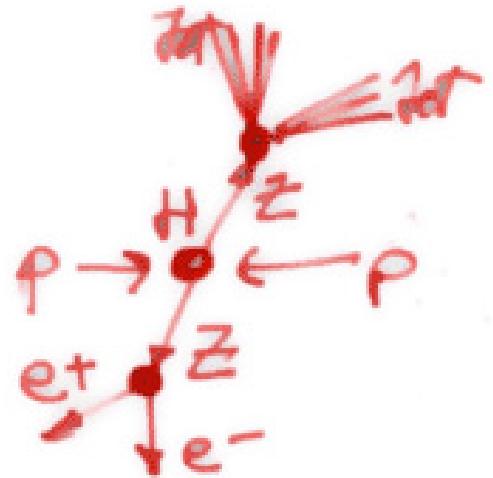
# ATLAS tile calorimeter



ATLAS LAr + Tile for pions:

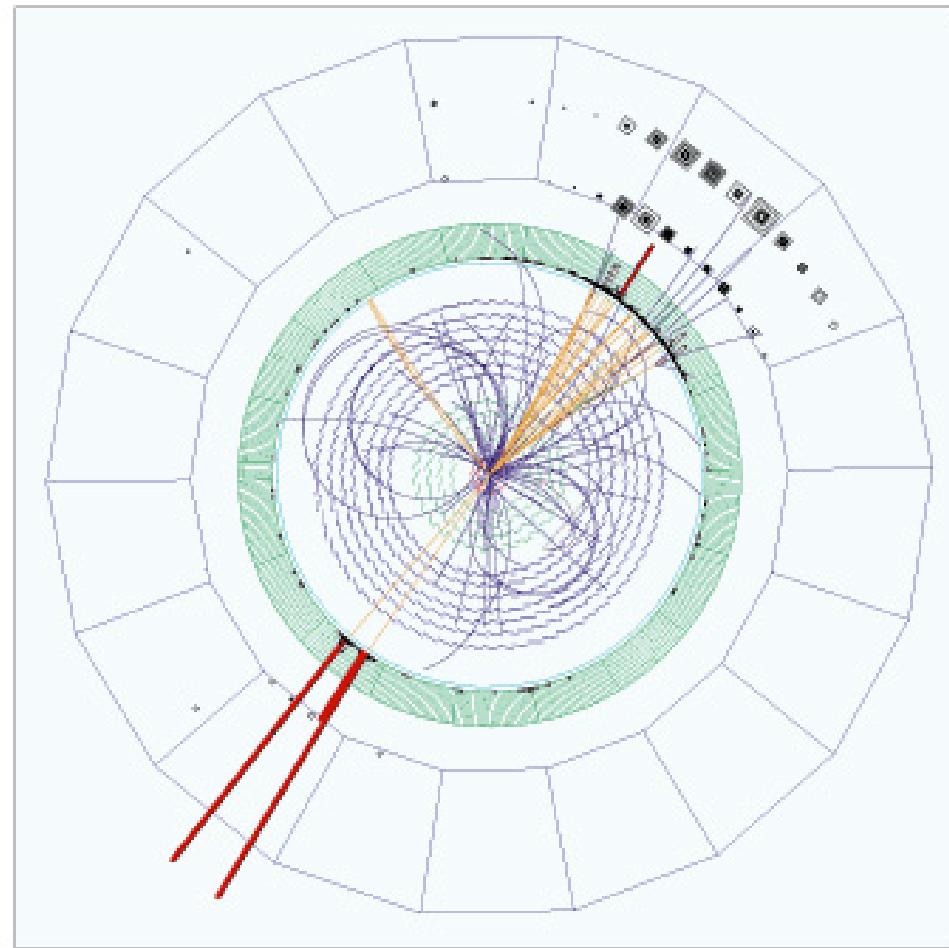
$$\frac{\sigma(E)}{E} = \frac{42\%}{\sqrt{E}} \oplus 2\%$$

# Jets in the CMS hadron Calorimeter

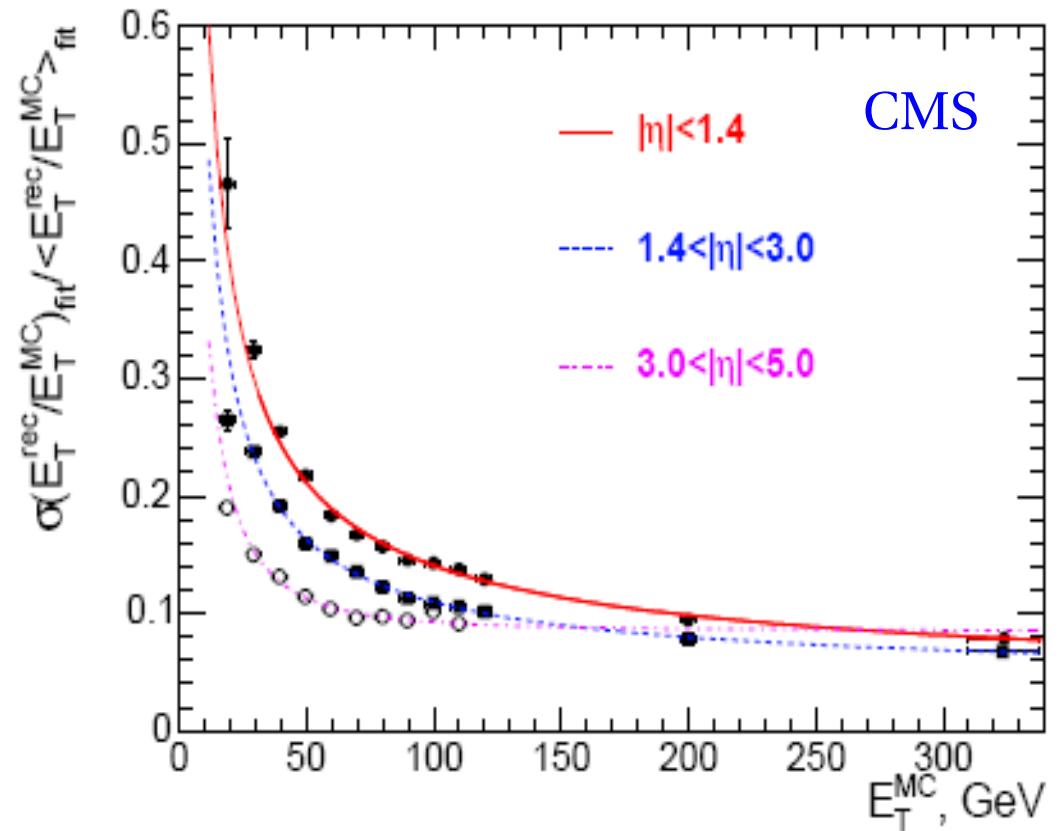
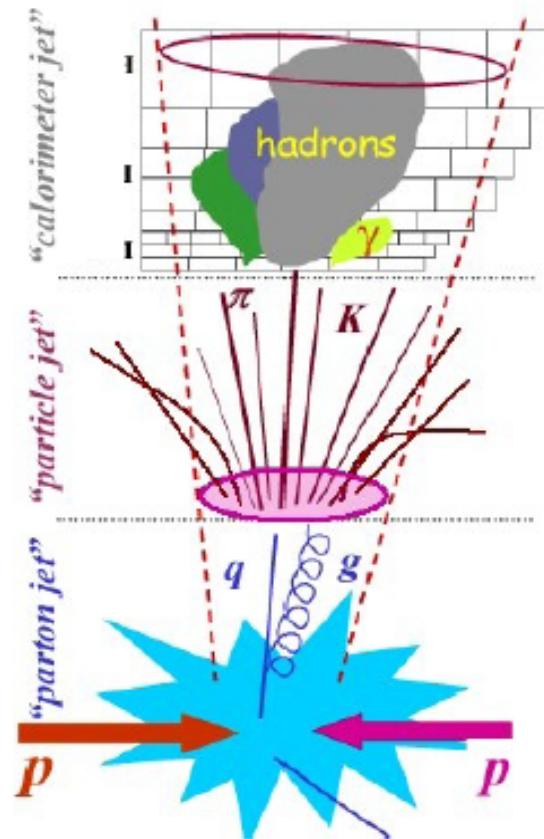


$p\ p \rightarrow H^0 \rightarrow Z\ Z$

↓      ↓  
jet jet  
↓      ↓  
e<sup>+</sup> e<sup>-</sup>

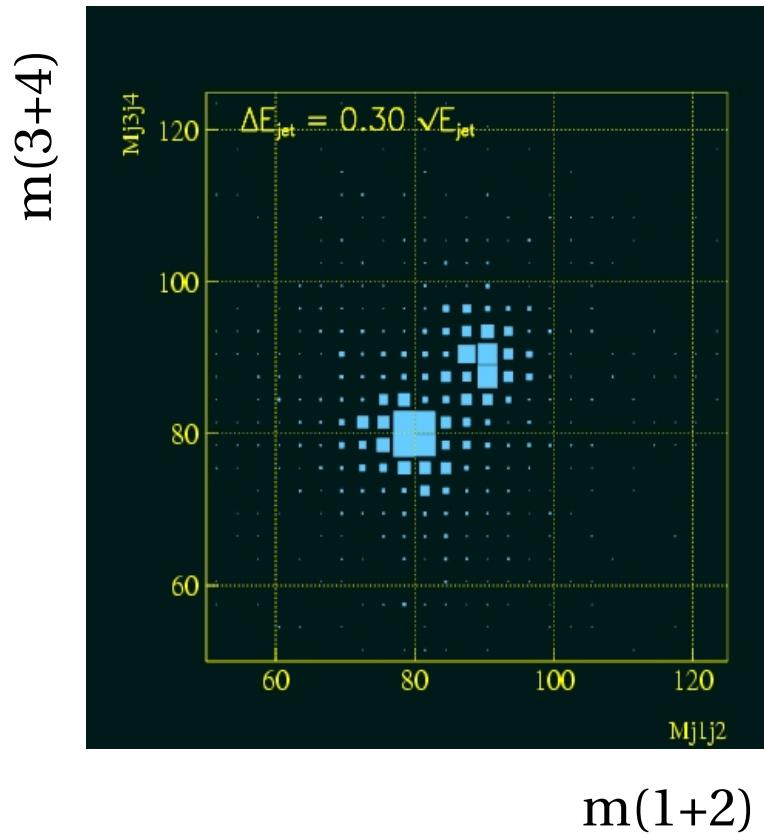
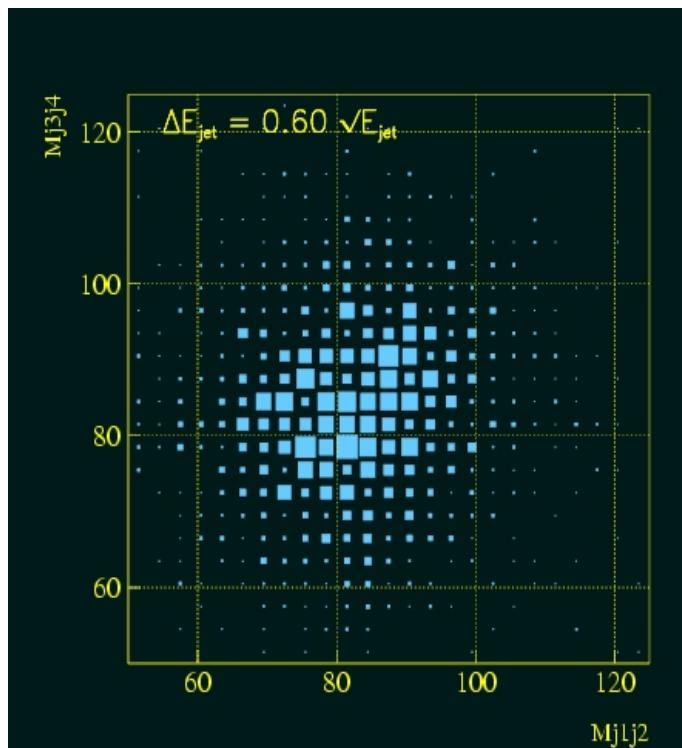


# Jet energy resolution



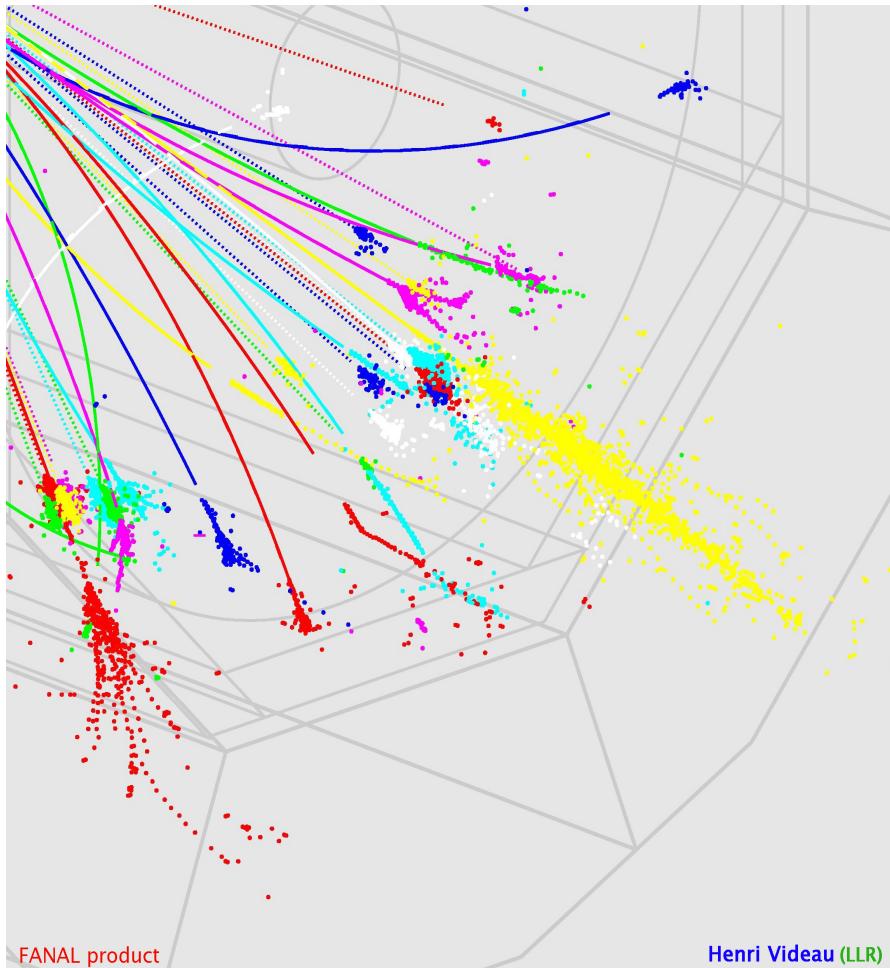
# A new concept: Particle Flow

- Goal: measure jets with  $30\% / \sqrt{E}$ 
  - ▶ Resolve  $W \rightarrow \text{jet jet}$  (80.4 GeV)
  - ▶ from  $Z \rightarrow \text{jet jet}$  (91.2 GeV)
  - ▶ in events with 4 jets:

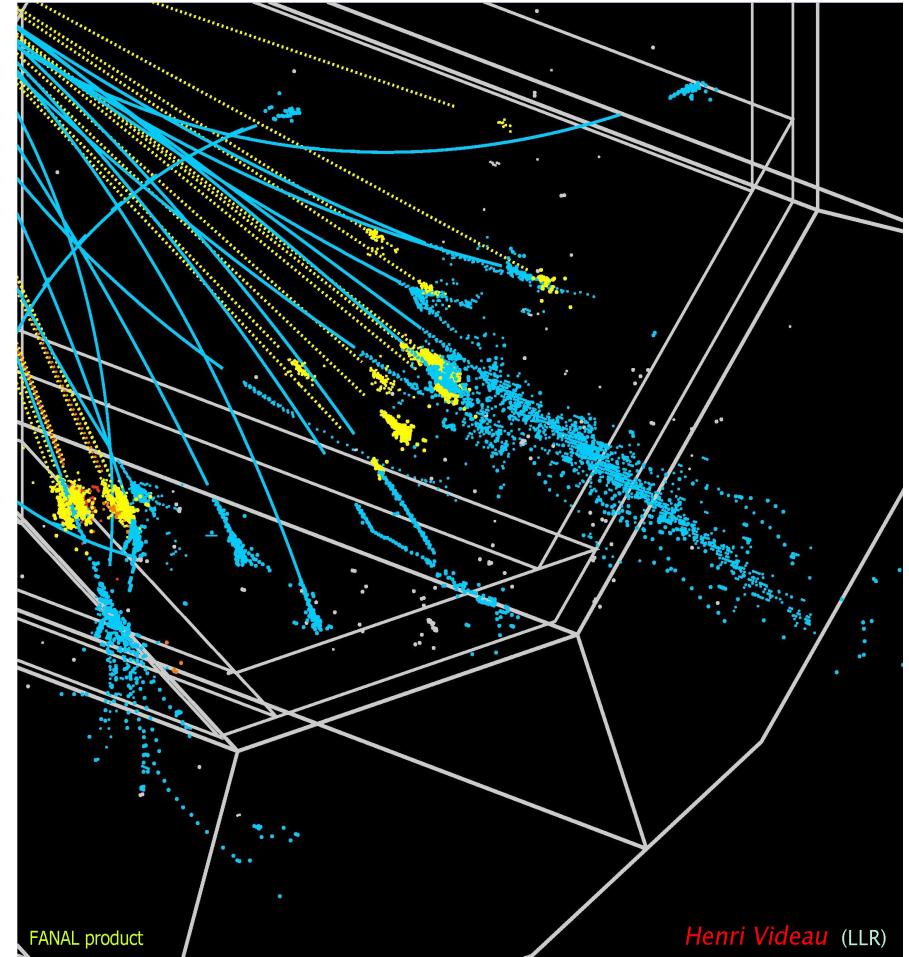


# Particle flow simulation

idea: reconstruct each particle separately: tracks,  $\gamma$ , n,  $K^0_L$ ,  $\mu$



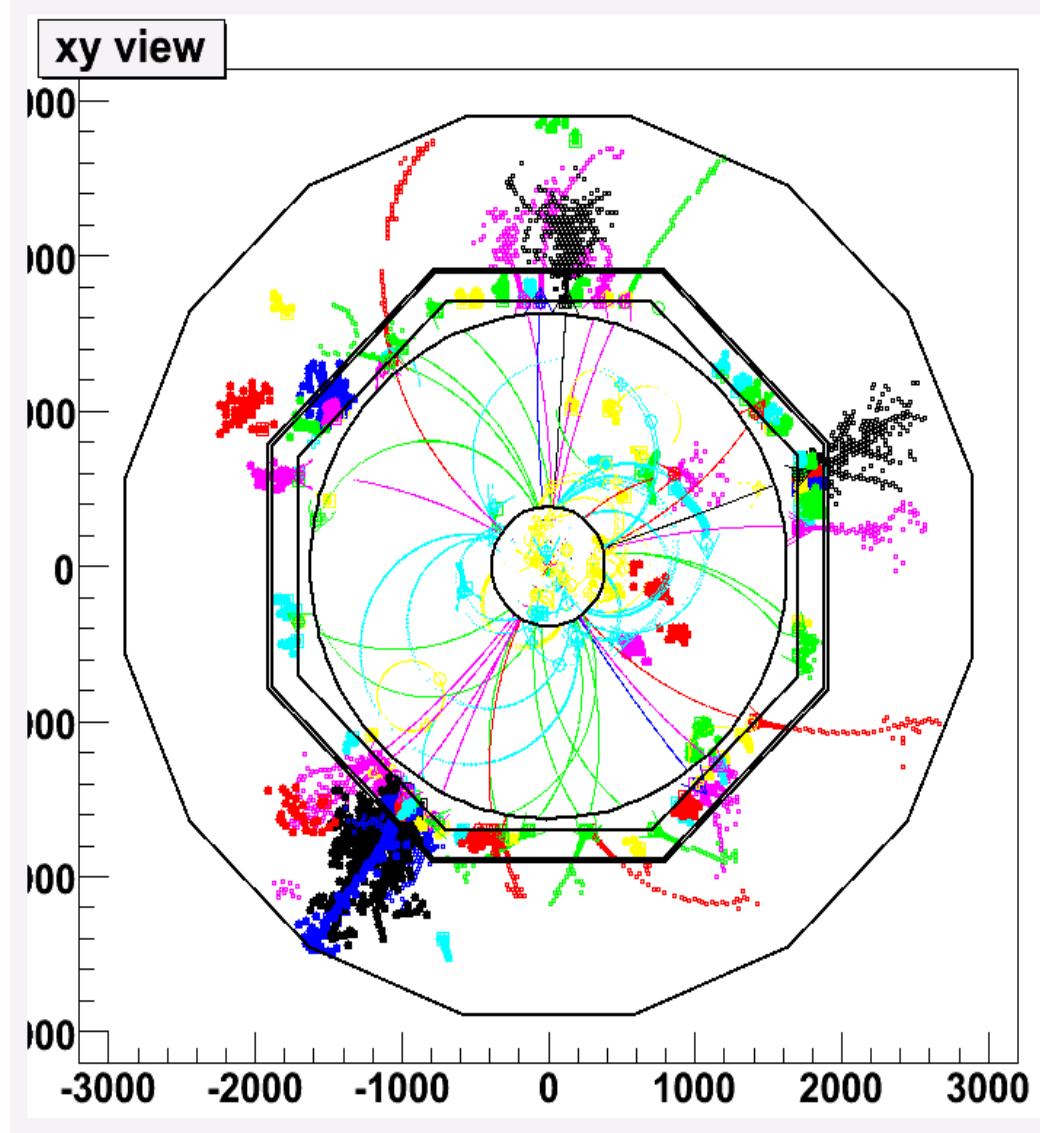
generated



reconstructed

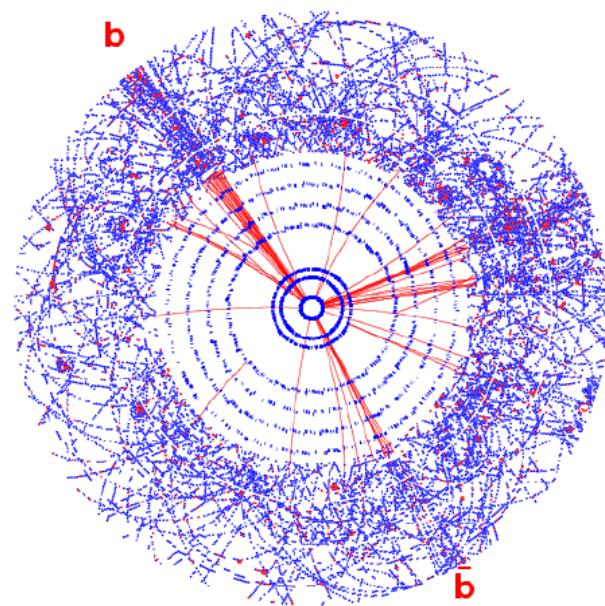
# Detector for a 500 GeV linear $e^+e^-$ collider

- Strong solenoid field
- Thin silicon pixel vertex detector
- Large TPC drift chamber
- High granularity Si-W EM calorimeter
- High granularity hadron calorimeter
- Muon detector
- Design studies in progress
- Prototypes in test beams.

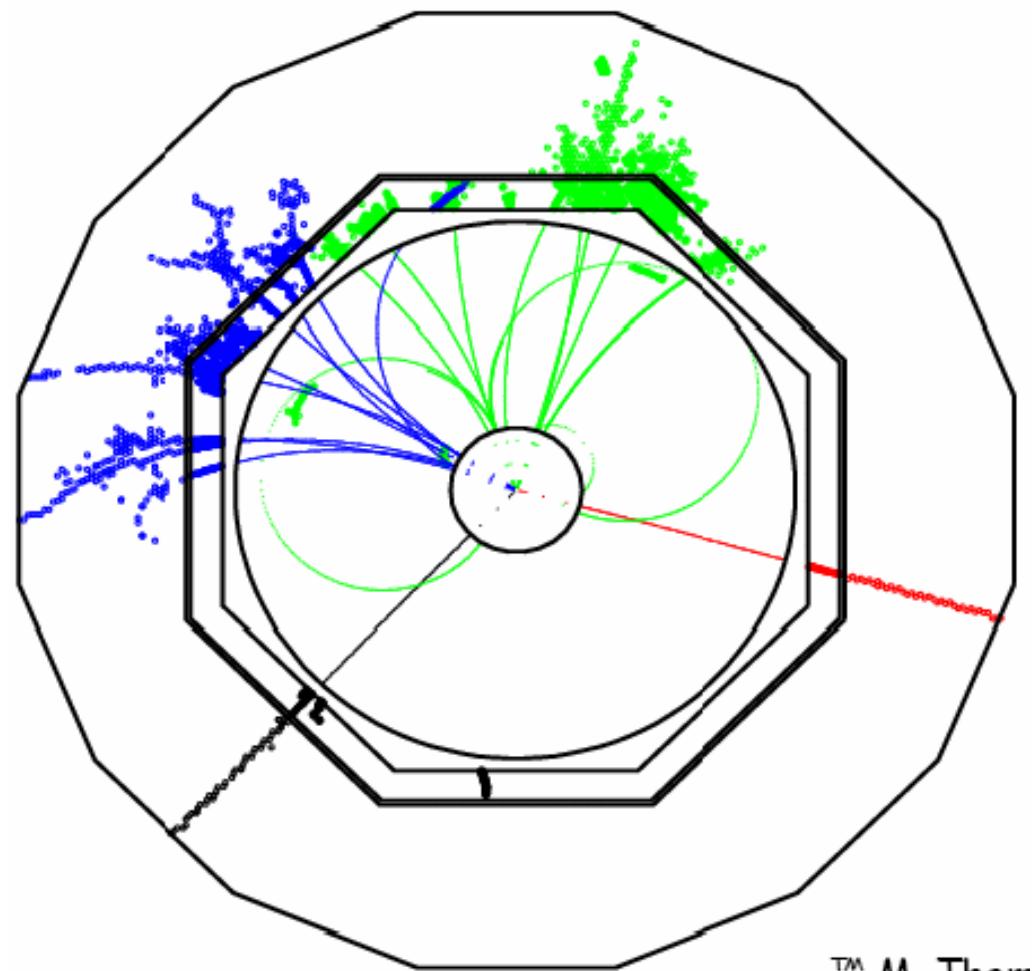


# ILC vs LHC

ATLAS, LHC  
tracking in a  $t\bar{t}$  event

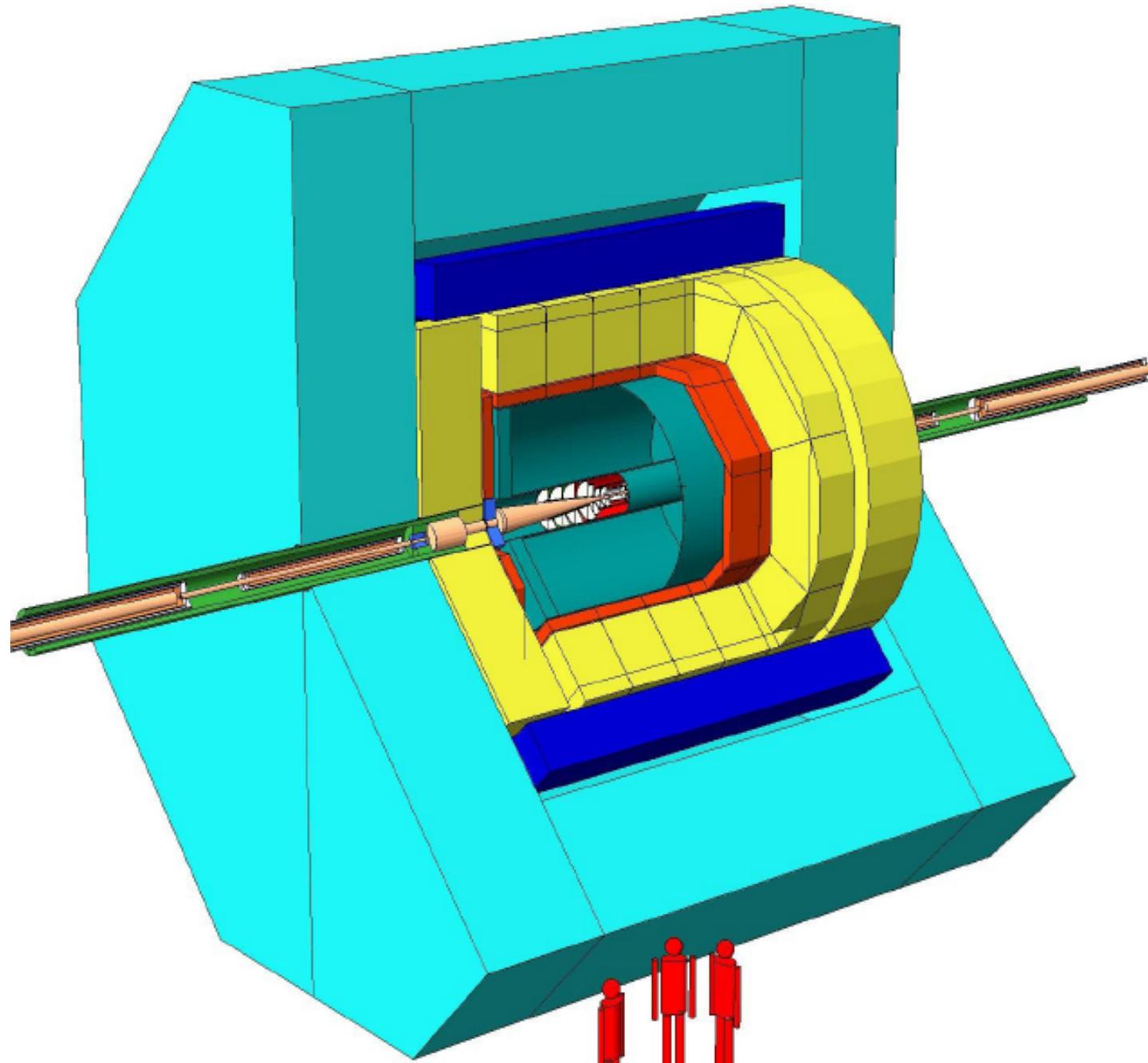


ILC tracking and  
calorimetry in a  $t\bar{t}$  event



TM M Thorw

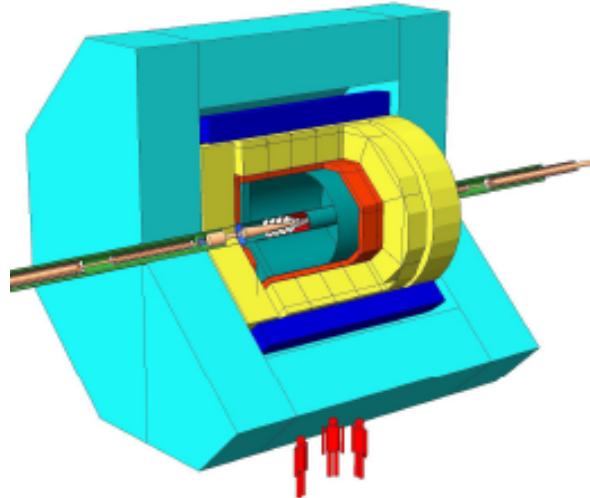
# Detector for a 500 GeV linear $e^+e^-$ collider



- Muon detector
- Strong solenoid field
- High granularity hadron calorimeter
- High granularity Si-W EM calorimeter
- Large TPC drift chamber
- Thin silicon pixel vertex detector

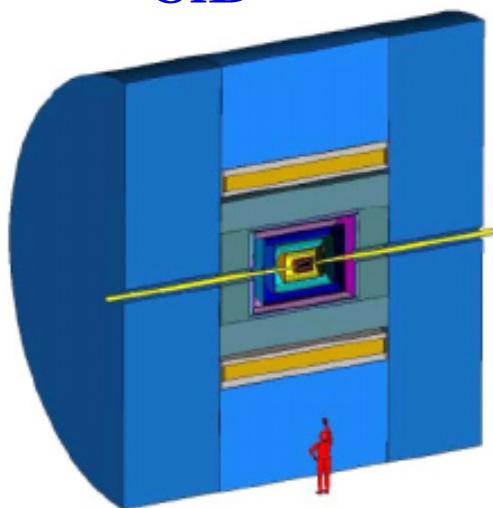
# Detectors for a 500 GeV linear $e^+e^-$ collider

ILD



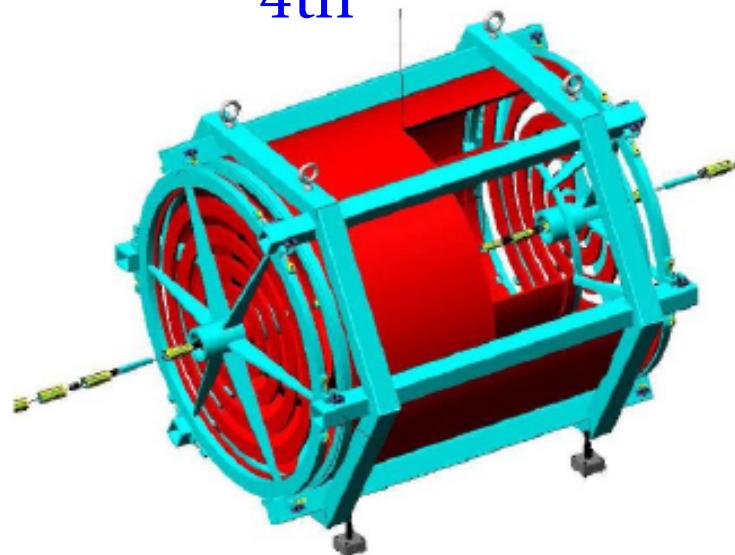
silicon pixel  
large TPC  
SiW EM calo  
Fe-scint pad HCAL  
4T solenoid  
iron yoke  
696 physicists

SiD



silicon pixel  
Si strip tracker  
SiW EM calo  
Fe-gas pad HCAL  
5T solenoid  
iron yoke  
234 physicists

4th



silicon pixel  
drift tracker  
crystal EM calo  
dual fiber HCAL  
4T solenoid  
anti-solenoid  
140 physicists

3/2009: Letters of intent. 2012: Design reports, 201?: start construction

# Summary

- Lecture 1:
  - ▶ Collider detectors
  - ▶ Charged particles in a magnetic field
  - ▶ Silicon detectors
- Lecture 2:
  - ▶ Drift tubes
  - ▶ Muon systems
  - ▶ MWPCs, CSCs, RPCs, TRTs, TPCs, Cherenkovs
- Lecture 3:
  - ▶ Electromagnetic showers and calorimeters
  - ▶ Photon detectors
  - ▶ Hadronic showers and calorimeters
  - ▶ Particle flow technique
- Discussion session:
  - ▶ Your questions, please