

# *Physics at $e^+e^-$ Colliders*

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- Introduction
- Achievements with LEP, SLC
- Physics beyond the Standard Model: supersymmetry
- Techniques at the high-energy  $e^+e^-$  collider
- ILC physics potential in view of LHC expectations
- Summary and some literature for further studies

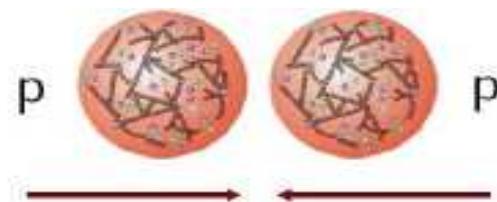
## *Few words before ...*

- You heard already a lot about
  - how e+e- colliders work
  - how they are limited
  - how the physics is detected
  - how we describe the physics theoretically
  - summary on physics issues

*I do not want to repeat the things, therefore I will focus on only a few physics topics (top, Higgs, SUSY, ED) and a few technical tools (threshold scans, continuums measurements, beam polarization)*

- Discussion: calculate problems together + all your questions....*

# *Introduction*



**Characteristics of pp collider**  
composite particles collide  
 $E(CM) < 2 E(\text{beam})$   
**strong interaction in initial state**  
superposition with spectator jets  
**LHC:  $\sqrt{s} = 14 \text{ TeV}$ ,**  
used  $\hat{s} = x_1 x_2 s$  few TeV  
small fraction of events analyzed  
multiple triggers  
'no' polarization applicable



and of the  $e^+e^- (\gamma e, \gamma\gamma)$  collider  
Pointlike particles collide  
 $E(CM) = 2 E(\text{beam})$   
**well defined initial state**  
clean final state  
**ILC:  $\sqrt{s} = 500 \text{ GeV -- } 1 \text{ TeV}$**   
  
most events in detector analyzed  
**no triggers required**  
**polarized initial beams** possible

**Large potential for  
direct discovery**

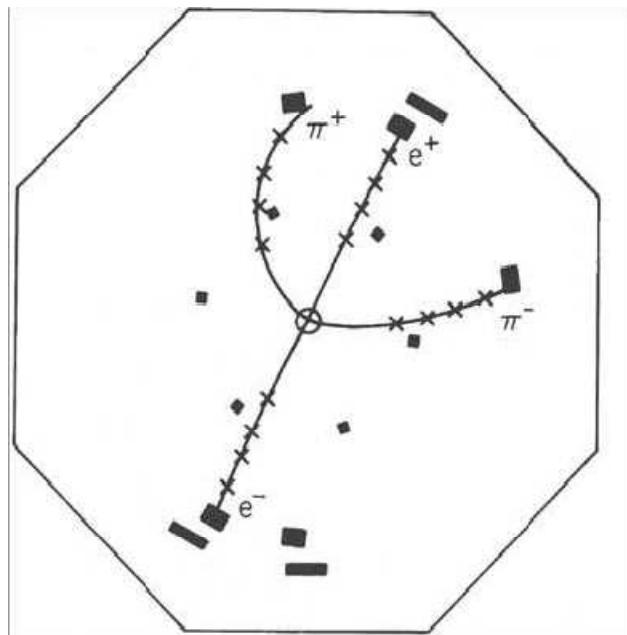
DESY Summer Program 2009

**Large potential for discovery  
via high precision**

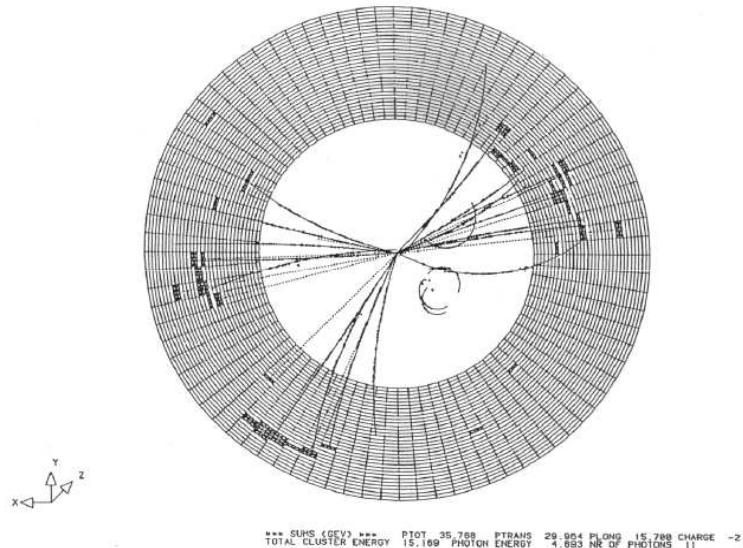
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# *Discoveries at e+e- colliders*

- Of course, also direct discoveries happened at e+e- colliders:



J/  $\Psi$  at SPEAR at SLAC (1974)

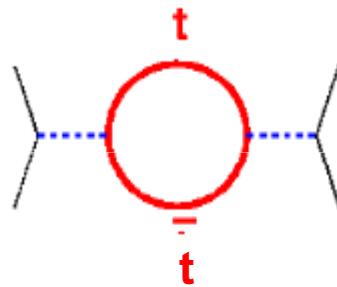


Gluons at PETRA at DESY (1979)

- famous '3 jet events'

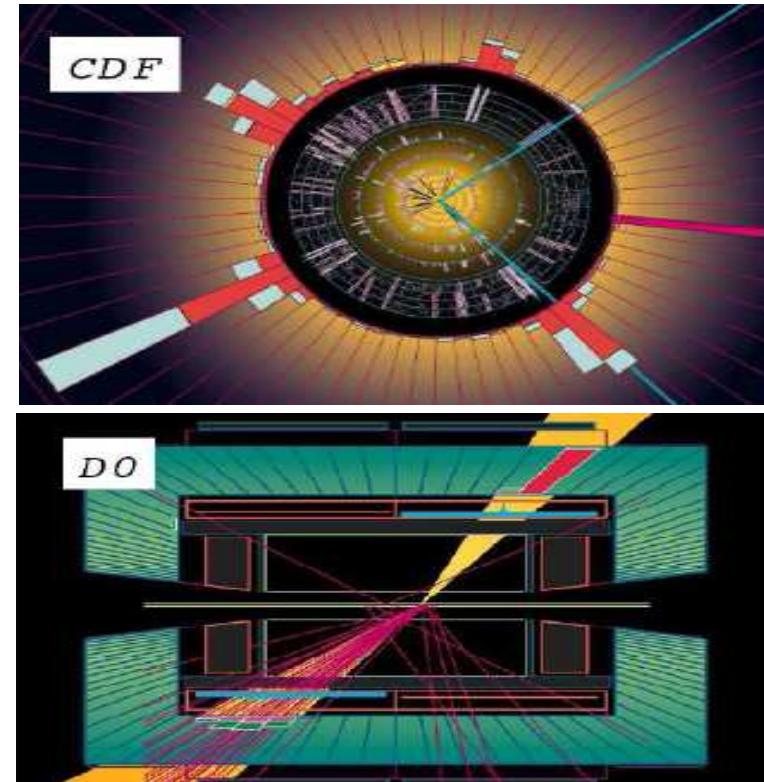
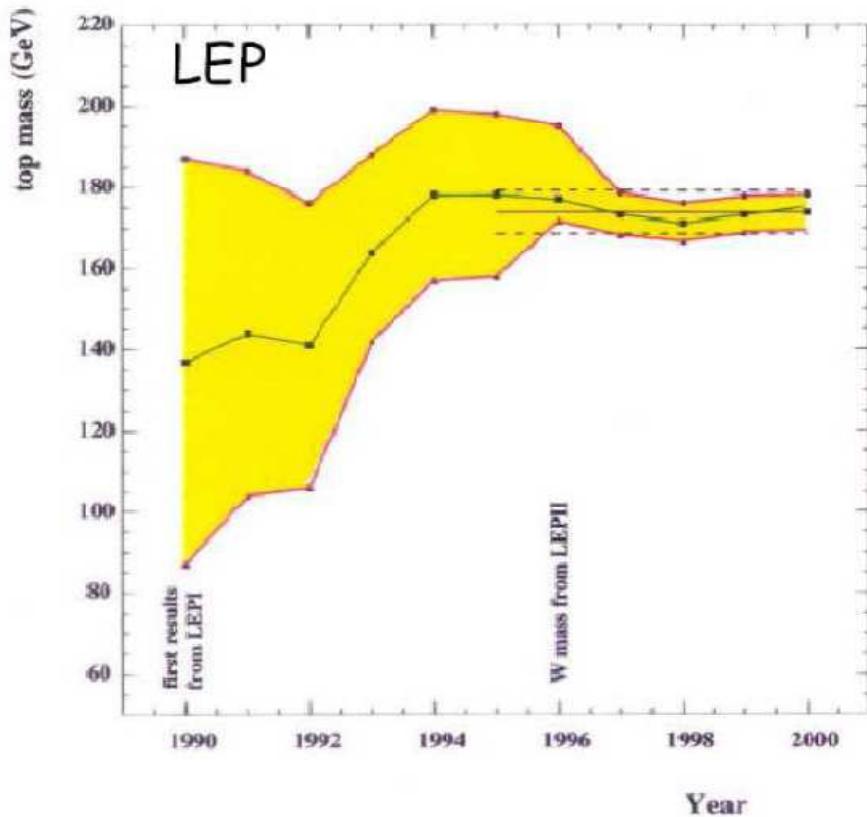
# *The unique advantage of e+e-*

- Their clean signatures allow precision measurements
  - Sensitive to the theory at quantum level (i.e. contributions of virtual particles, ‘higher orders’)!



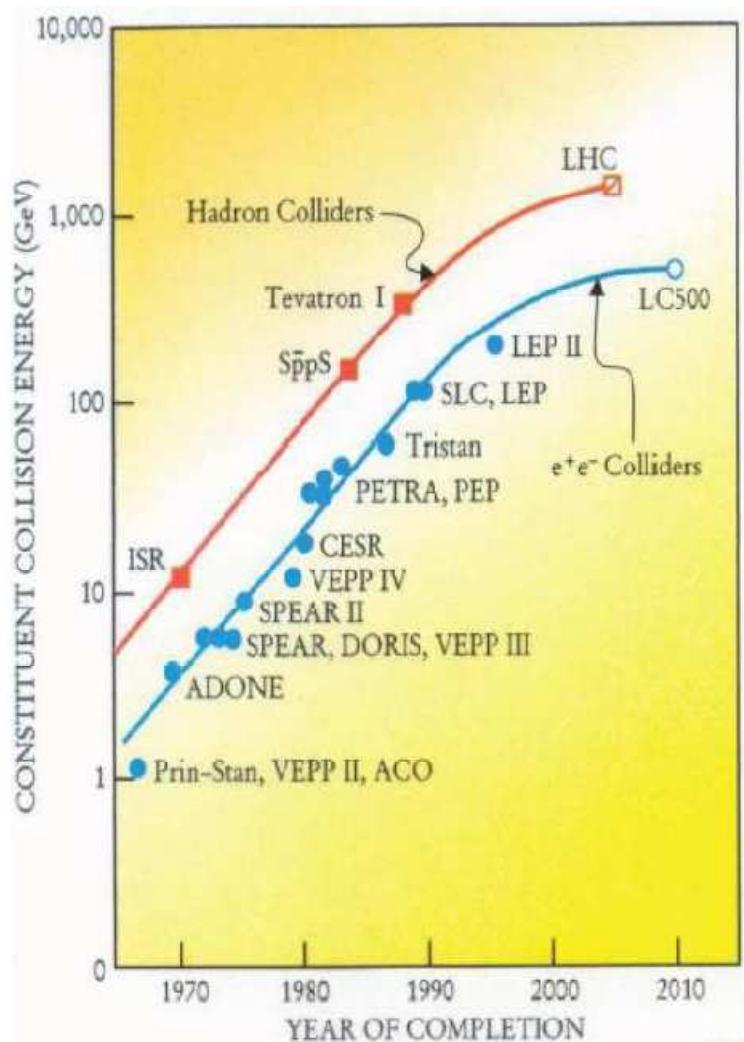
- Such measurements allow predictions for further, still undiscovered particles, but whose properties are defined by theory at quantum level

# *Predictions of top mass*



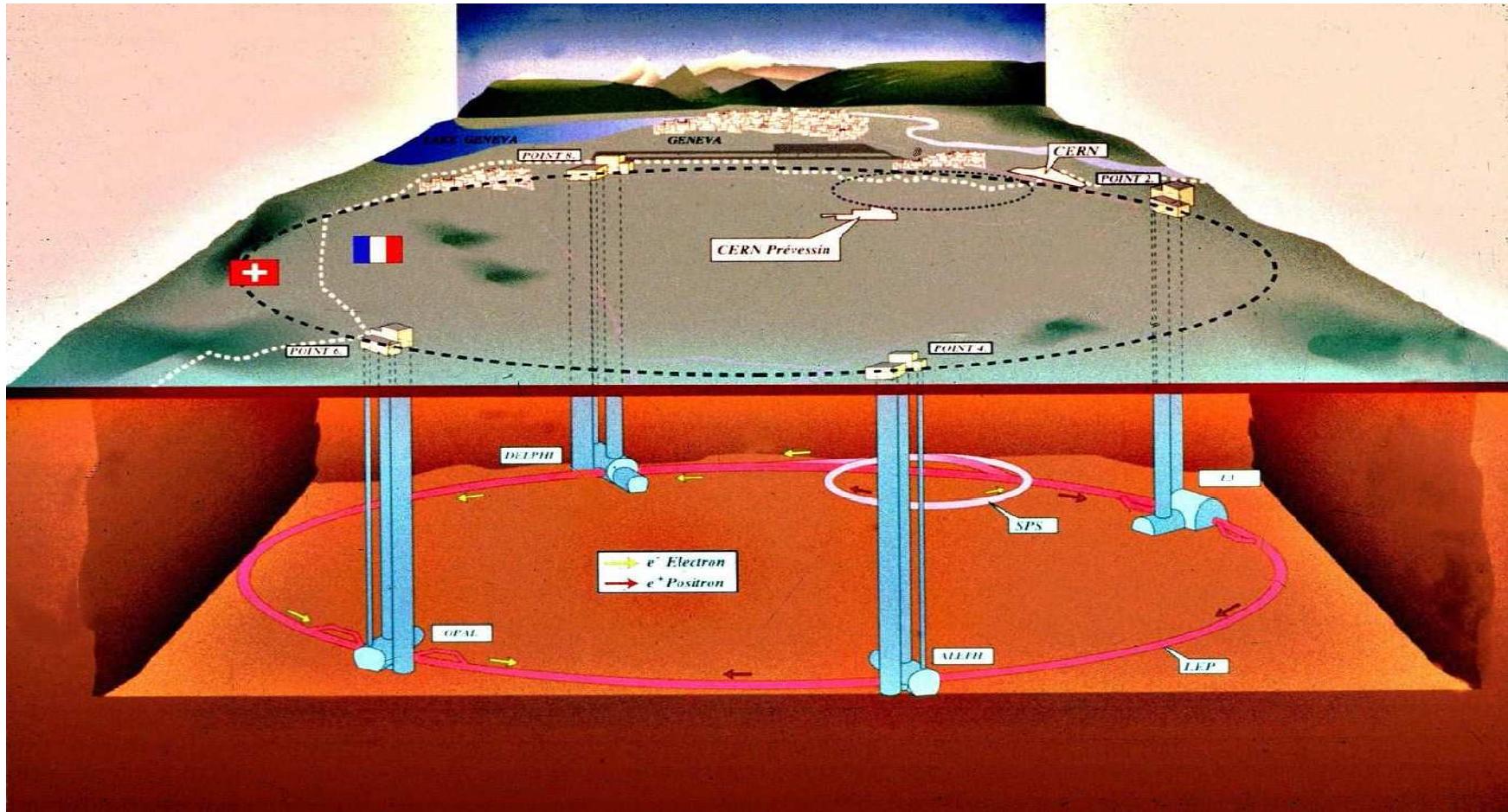
- Predicted discovery of the top quark at the Tevatron 1995:
- The history of physics is full of predicted discoveries:
- $e^+$ ,  $n$ ,  $\Pi$ ,  $q$ ,  $g$ ,  $W$ ,  $Z$ ,  $c$ ,  $b$ ,  $t$
- Future examples: Higgs, SUSY ??? -- see later

# *Interplay: hadron and e+e- colliders*



- The interplay between electron and hadron machines has a long and fruitful tradition
  - J/ $\psi$  at SPEAR (e+e-) and AGS (proton fixed target)
  - 'Y discovery at E288 (p fixed target), precision B studies at the e+e- B factories
  - top quark at LEP and Tevatron
- To be continued in the form of LHC and ILC -- see examples later

# *History from LEP: results, techniques*

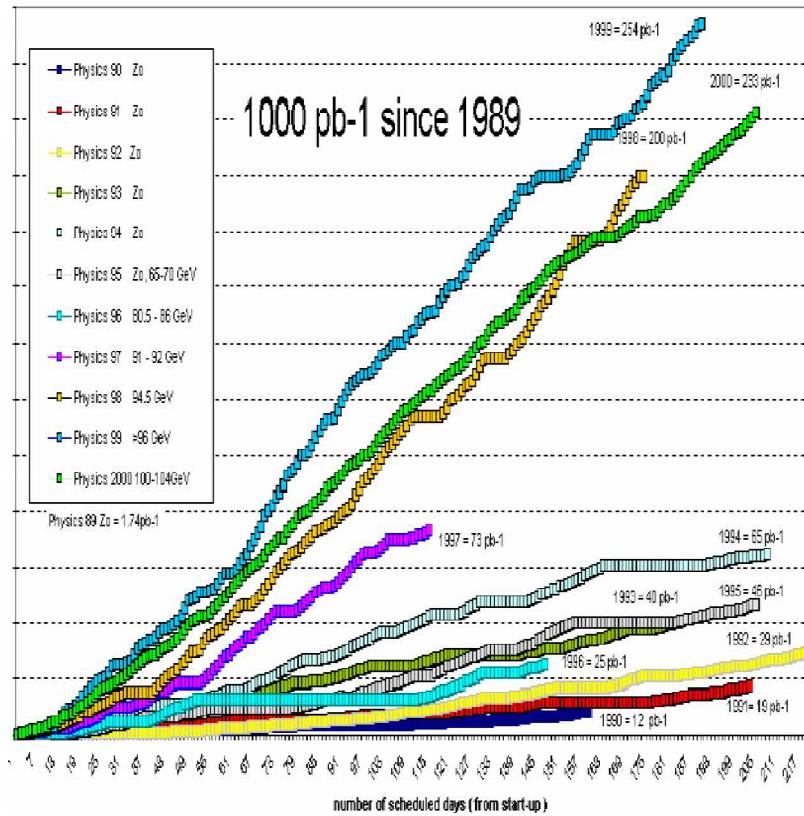


‘LEP Tunnel’ = now ‘LHC tunnel’

## *Some LEP data*

- Circumference 27 km
- $\sqrt{s}$  91.2 GeV (LEP1) to 209 GeV(LEP2)
- Accelerating Gradient Up to 7MV/m (Superconducting cavities)
- Number of Bunches  $4 \times 4$
- Current per Bunch  $\approx 750 \mu\text{A}$
- Luminosity at LEP1  $24 \times 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$  ( $\approx 1 Z^0/\text{s}$ )
- Luminosity at LEP2  $50 \times 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$   
 $(\approx 3 W^+W^-/\text{h})$
- Interaction regions 4 (ALEPH,DELPHI,L3,OPAL)
- Energy calibration < 1MeV (at  $Z^0$ )

# *LEP data*

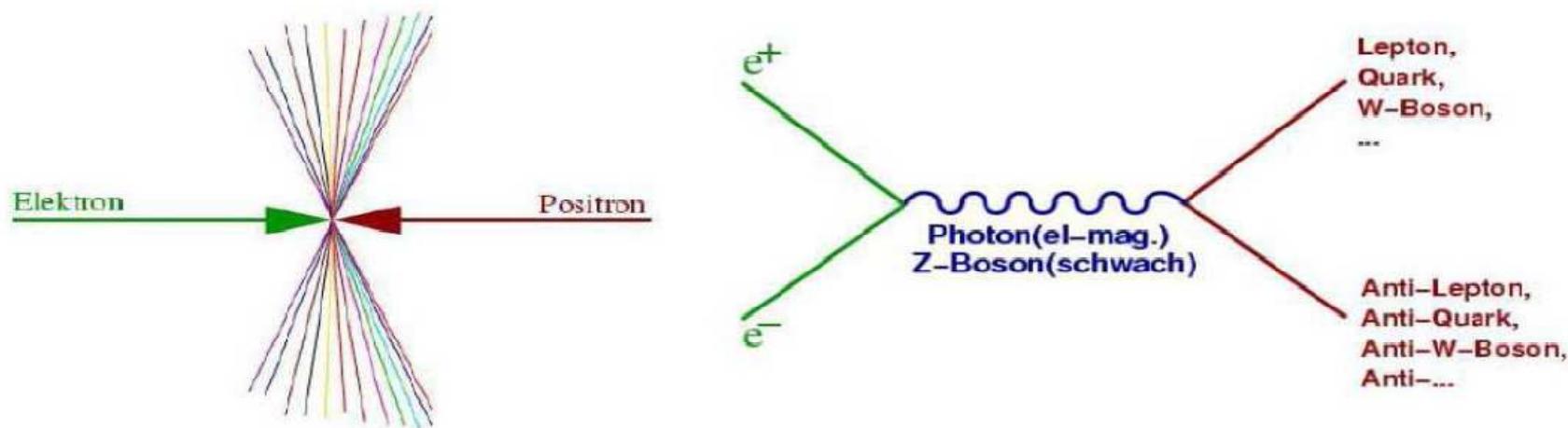


1990 – ≈ 91 GeV  
1995 5 Million  $Z^0/\text{exp.}$   
1995 Test phase for  
LEP2 130GeV  
1996 161 – 172 GeV  
WW-Threshold  
1997 183 – 209 GeV  
2000 10 000 WW-pairs/exp.  
Searches for  
new physics  
0 (?) Higgs bosons  
LEP was shut down and dismantled to  
make room for LHC in Nov. 2000

## Integrated Luminosities

LEP was dismantled to make room for LHC in November 2000 ... now first injection

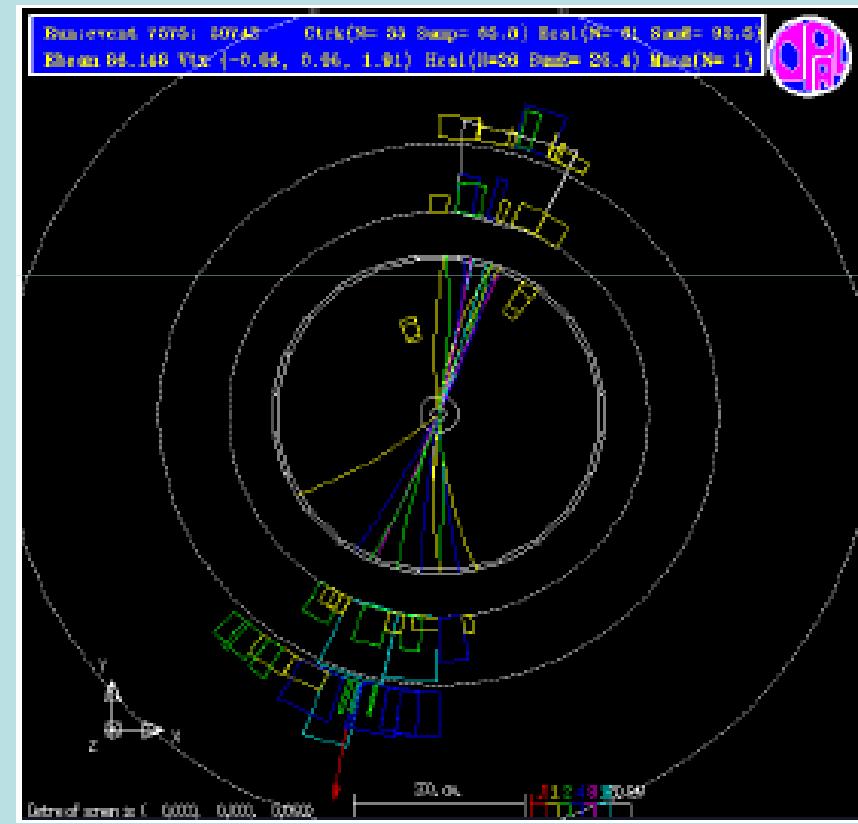
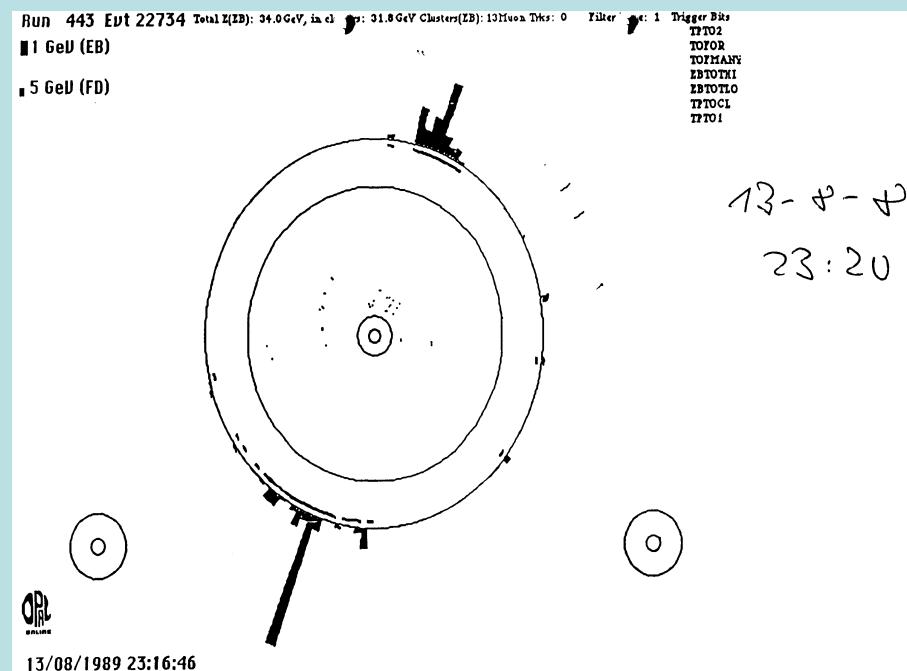
# *The Basic Process at LEP1*



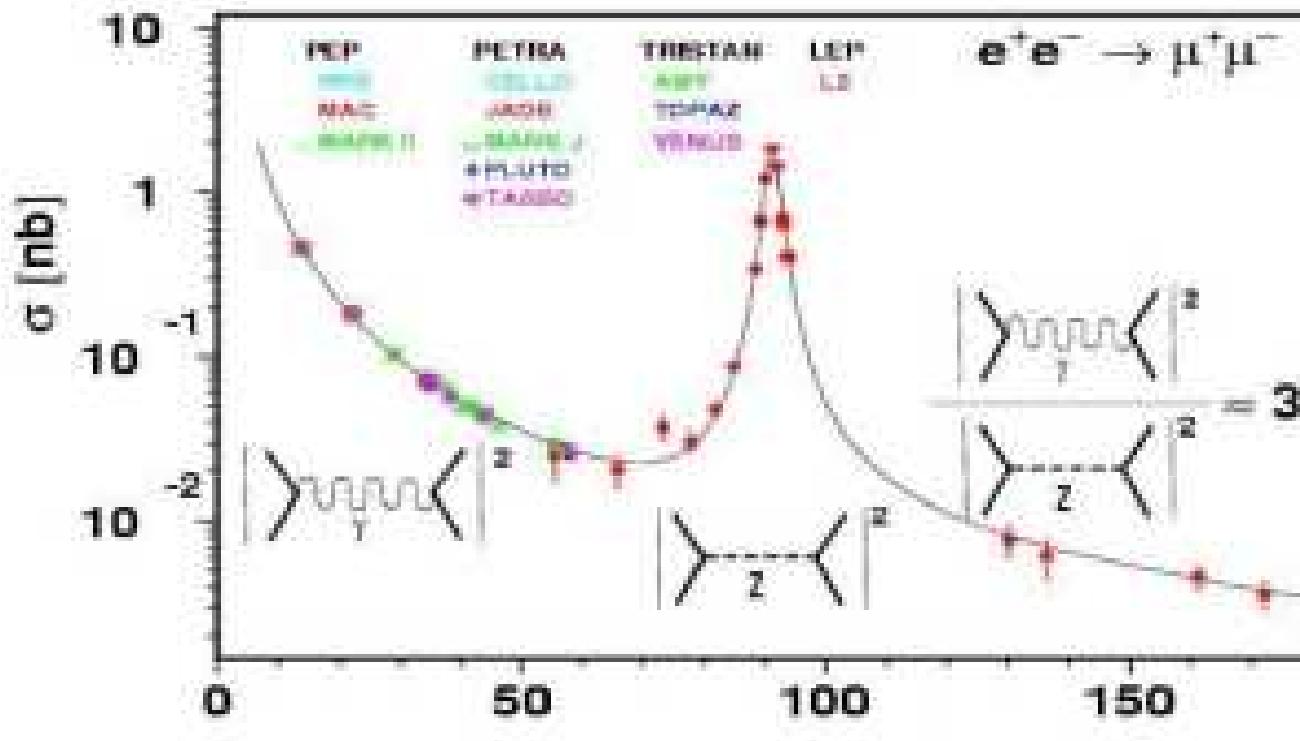
- $Z^0$  lineshape:  $Z^0$  mass,  $Z^0/\gamma$ -interference
- Number of neutrinos, etc.
- Precision tests of the QFD: forward-backward asymmetries
- Precision tests of QCD: Confirmation of SU(3)
- Together with  $m_W$ : Prediction of the top quark mass
- Many other precision tests of the SM
- **Very successful: more than 2400 publications from 4 collaborations !**

# First Z - event

- $e^+e^- \rightarrow Z \rightarrow q\bar{q}$  (13.8.89 !)
  - Tracking chambers not yet fully operational, therefore only ECAL

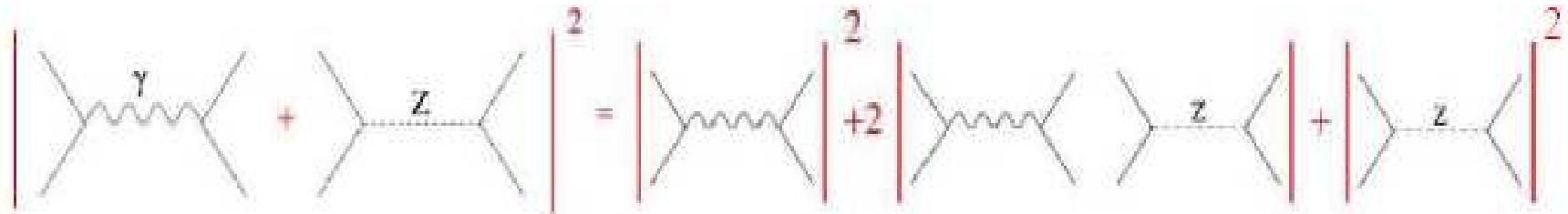


# Total cross section



- $Z^0$  gives a dramatic resonance
- cross section well described (at quantum level, not only at tree level!)

# Differential cross section (tree level)



$$\frac{d\sigma}{d\Omega} = N_C \frac{\alpha_{em}^2}{4s} \left\{ (1 + \cos^2 \theta) [Q_f^2 - 2\chi_1 v_e v_f Q_f - \chi_2 (a_e^2 + v_e^2)(a_f^2 + v_f^2)] + 2 \cos \theta [-2\chi_1 a_e a_f Q_f + 4\chi_2 a_e a_f v_e v_f] \right\}$$

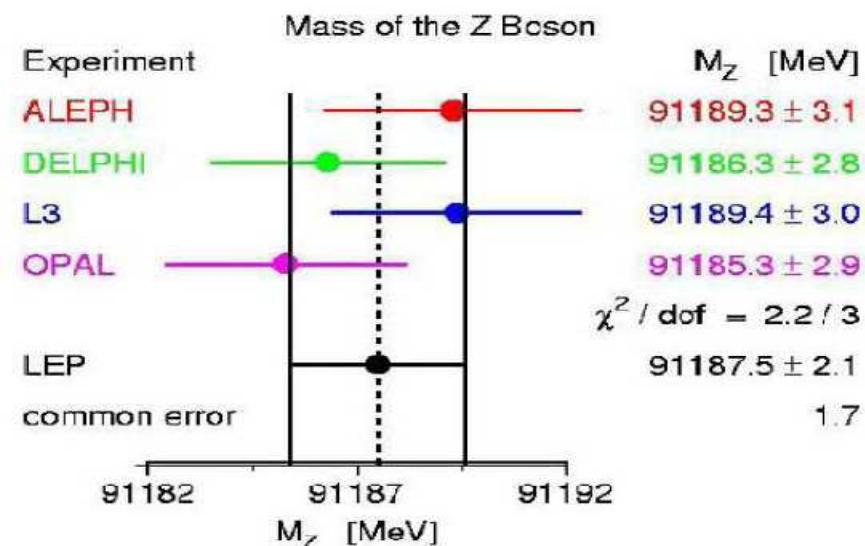
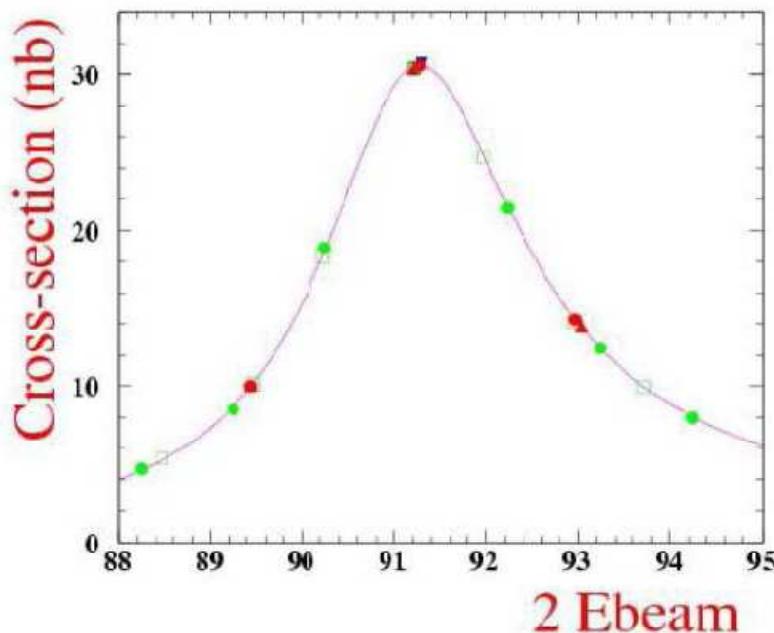
$$\chi_1 = \frac{s(s - M_Z^2)}{16 \sin^2 \theta_W \cos^2 \theta_W ((s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2)}$$

$$\chi_2 = \frac{s^2}{256 \sin^4 \theta_W \cos^4 \theta_W ((s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2)}$$

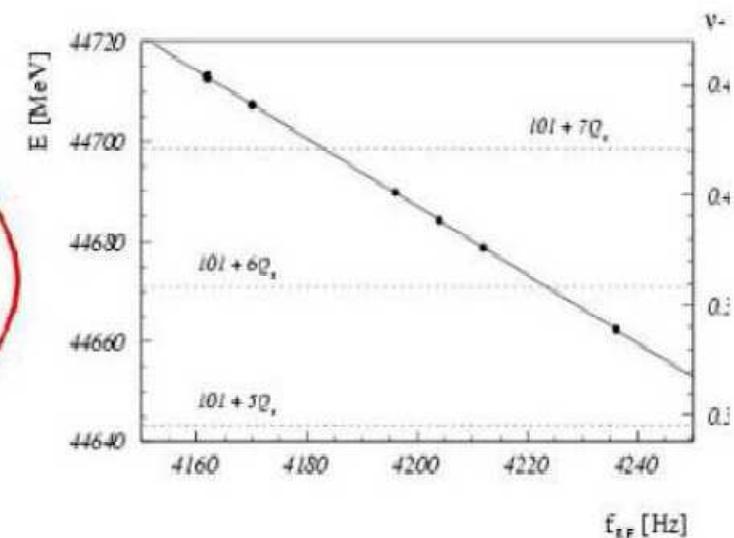
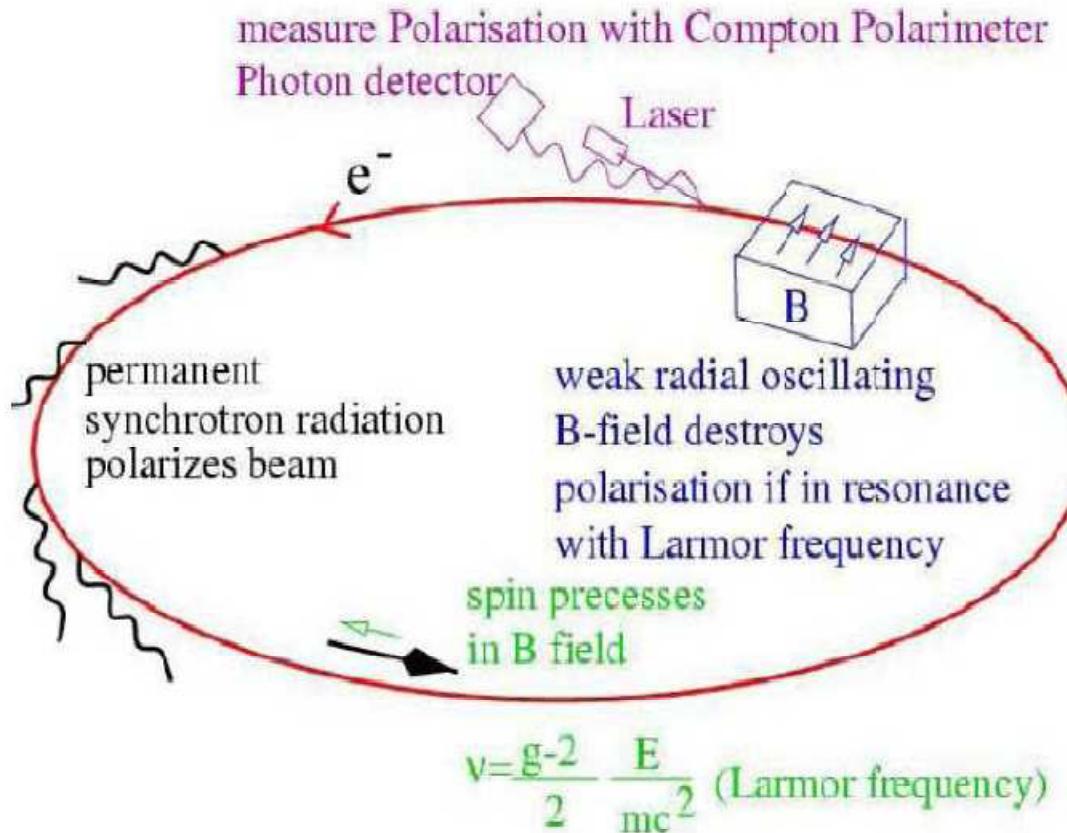
$$a_e = -1; \quad v_e = -1 + 4 \sin^2 \theta_W; \quad a_f = 2l_f; \quad v_f = 2l_f - 4Q_f \sin^2 \theta_W$$

# $Z^0$ Mass Measurement

- Very important input to SM fits !
- Uncertainty is only  $\Delta m_Z \sim 2.1 \text{ MeV}$
- Important to understand **systematics** of the beam energy measurement!



# Systematics: Beam Energy Measurement



- Uncertainty is only 1 MeV !
- Further systematics have been: water level, tides, TGV
- Remark: polarization not used for physics, but for calibration!

# $Z^0$ branching ratios: neutrinos

- SM makes precise predictions for the branching ratios of the  $Z^0$

$$\Gamma_{\nu\nu} = \frac{G_F M_Z^3}{12\pi\sqrt{2}} \approx 162 \text{ MeV}$$

$$\Gamma_{ee} = \Gamma_{\mu\mu} = \Gamma_{\tau\tau} = 4 \sin^4 \theta_W \Gamma_{\nu\nu} \approx 84 \text{ MeV}$$

$$\Gamma_{uu} = \Gamma_{cc} = 3 \left( \frac{32}{9} \sin^4 \theta_W - \frac{8}{3} \sin^2 \theta_W + 1 \right) \Gamma_{\nu\nu} \approx 287 \text{ MeV}$$

$$\Gamma_{dd} = \Gamma_{ss} = \Gamma_{bb} = 3 \left( \frac{8}{9} \sin^4 \theta_W - \frac{4}{3} \sin^2 \theta_W + 1 \right) \Gamma_{\nu\nu} \approx 370 \text{ MeV}$$

(here: neglecting the quark masses)

- How can we measure the  $\Gamma$ , especially  $\Gamma_{\nu\nu}$ ?

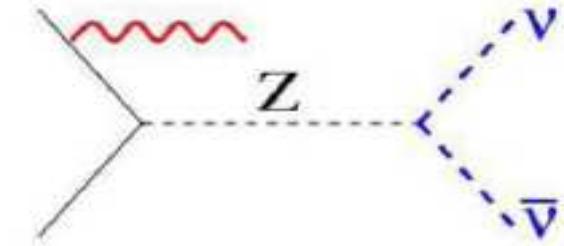
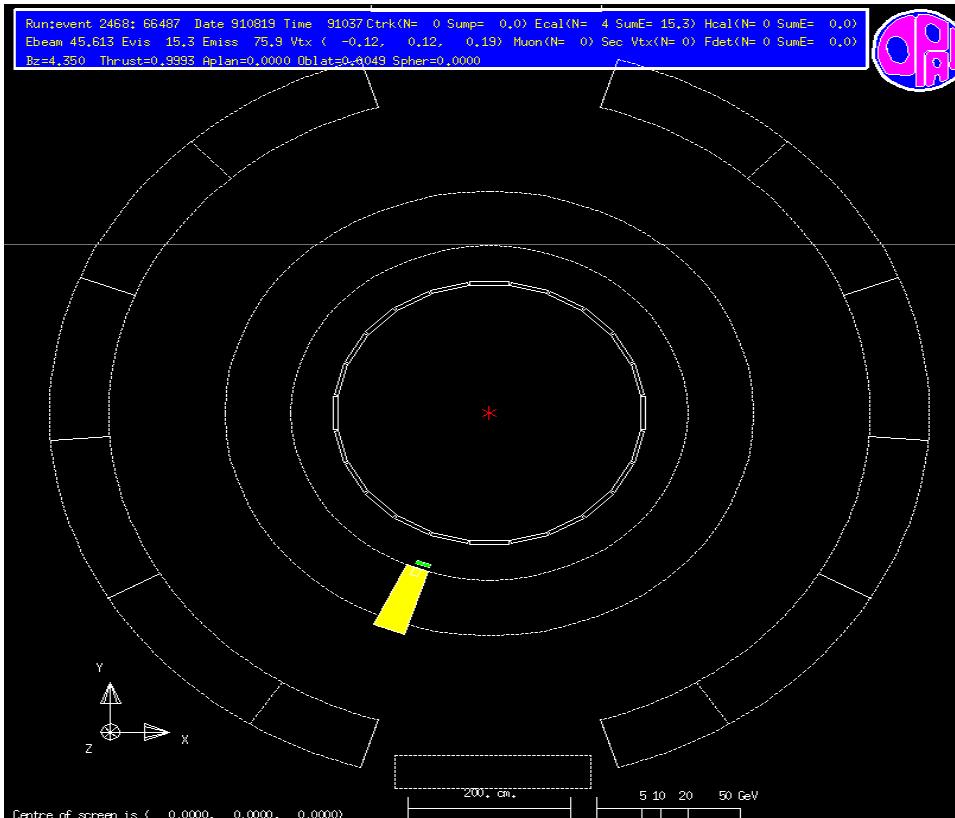
- measure ‘invisible’ events !** (also important for SUSY, see later)

...

# *Counting neutrinos via photons!*

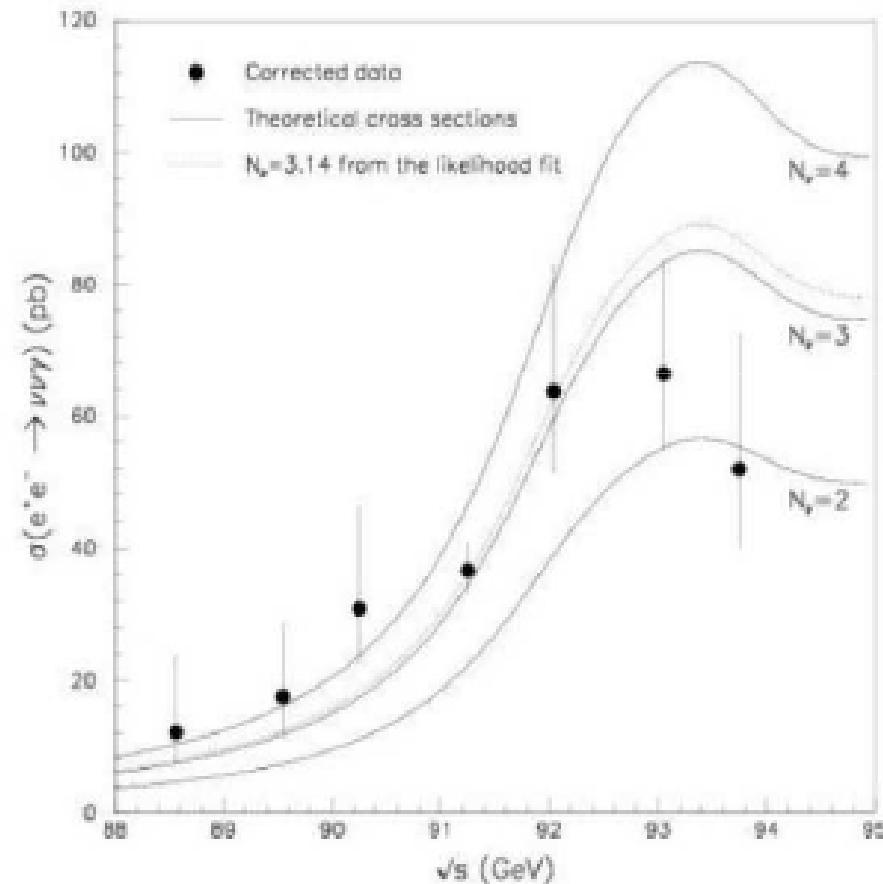
- *Using radiative neutrino production:*

- leads to signal only in ECAL



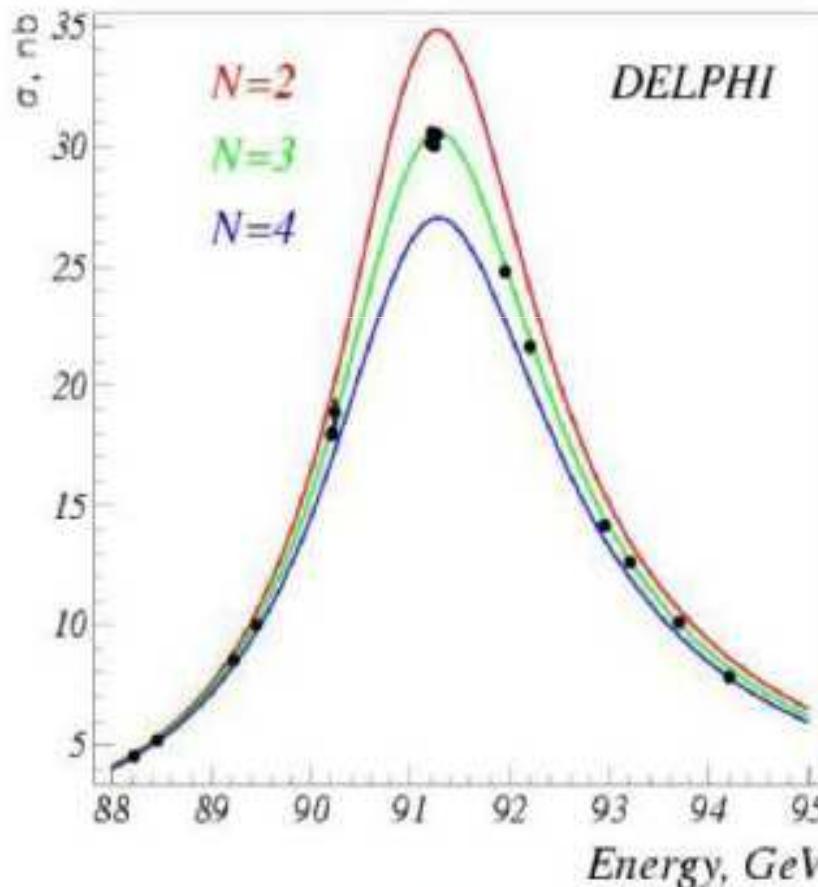
# *Fitting the cross section:*

- Fit prefers 3 families
  - but rather large error
- Some theory assumptions
  - but better than nothing...



# *Other method for counting neutrinos*

- Measuring the total width of the Z-boson



$$\Gamma_{\text{tot}} = \Gamma_{\ell\ell} + \Gamma_{qq} + N_{\text{fam}} \Gamma_{\nu\nu}$$

- Total width depends on the number of neutrino families!
- Result:  
 $N_{\text{fam}} = 2.9841 \pm 0.0083$
- Result before LEP:  $N_{\text{fam}} < 5.9$

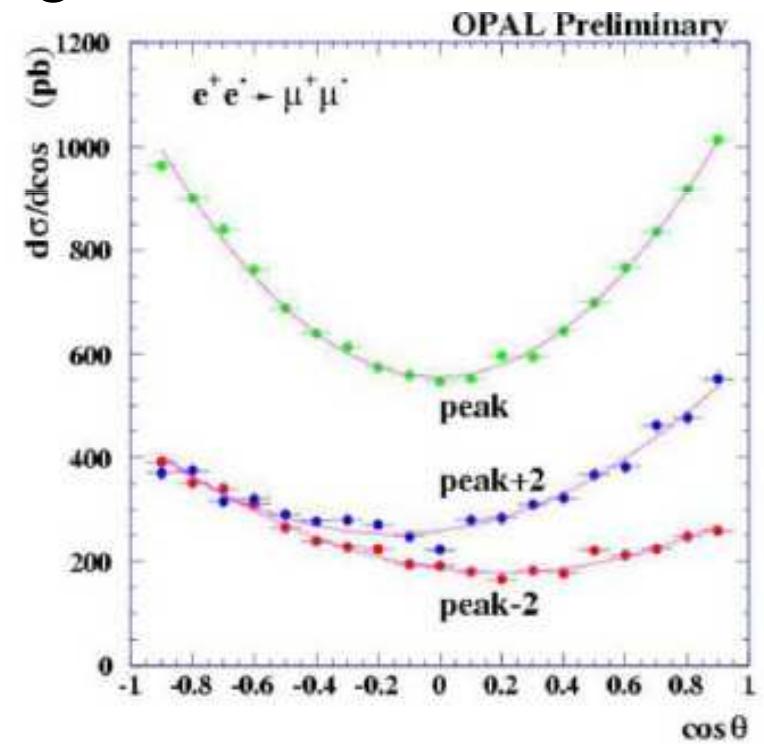
# *Exploiting further observables: angular distributions!*

- As shown in tree-level formulae before: linear dependence on scattering angle  $\cos\theta$

- a forward-backward Asymmetry  $A_{FB}$ :

$$A_{FB} = \frac{\sigma(\cos\theta > 0) - \sigma(\cos\theta < 0)}{\sigma(\cos\theta > 0) + \sigma(\cos\theta < 0)}$$

- Pure  $A_{FB}$  is better than a fit to the whole distribution, since detector systematics cancels



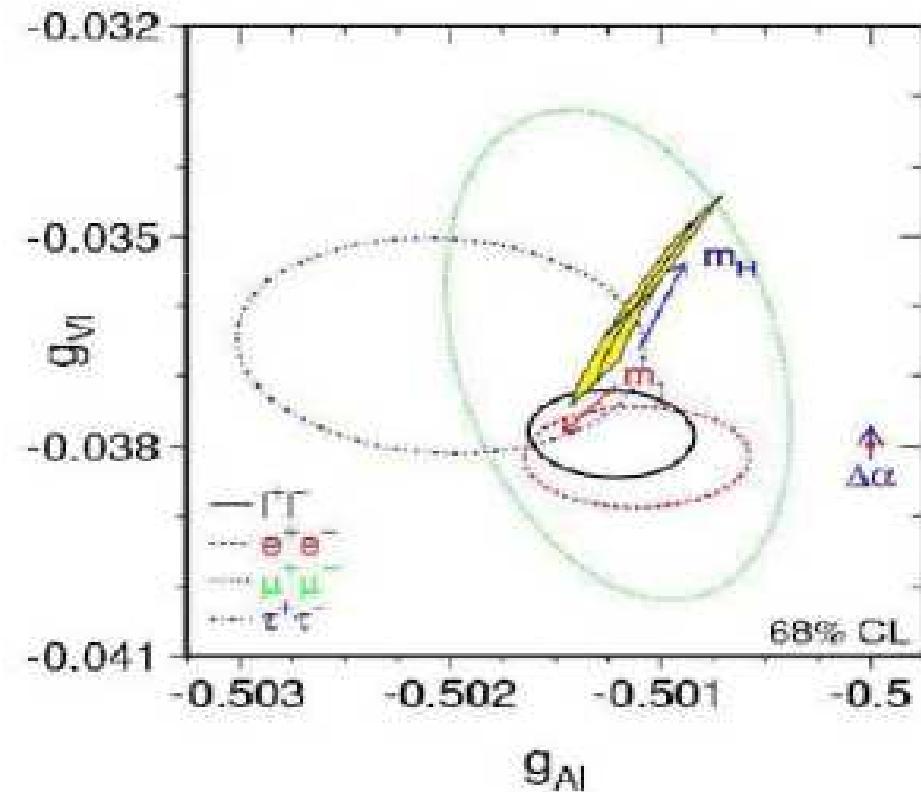
# *Measuring $Z^0$ couplings*

- Vector- and axial-vector couplings:

$$- g_{VI} = T_{3I} - 2e \sin^2 \theta_W$$

$$- g_{AI} = T_{3I}$$

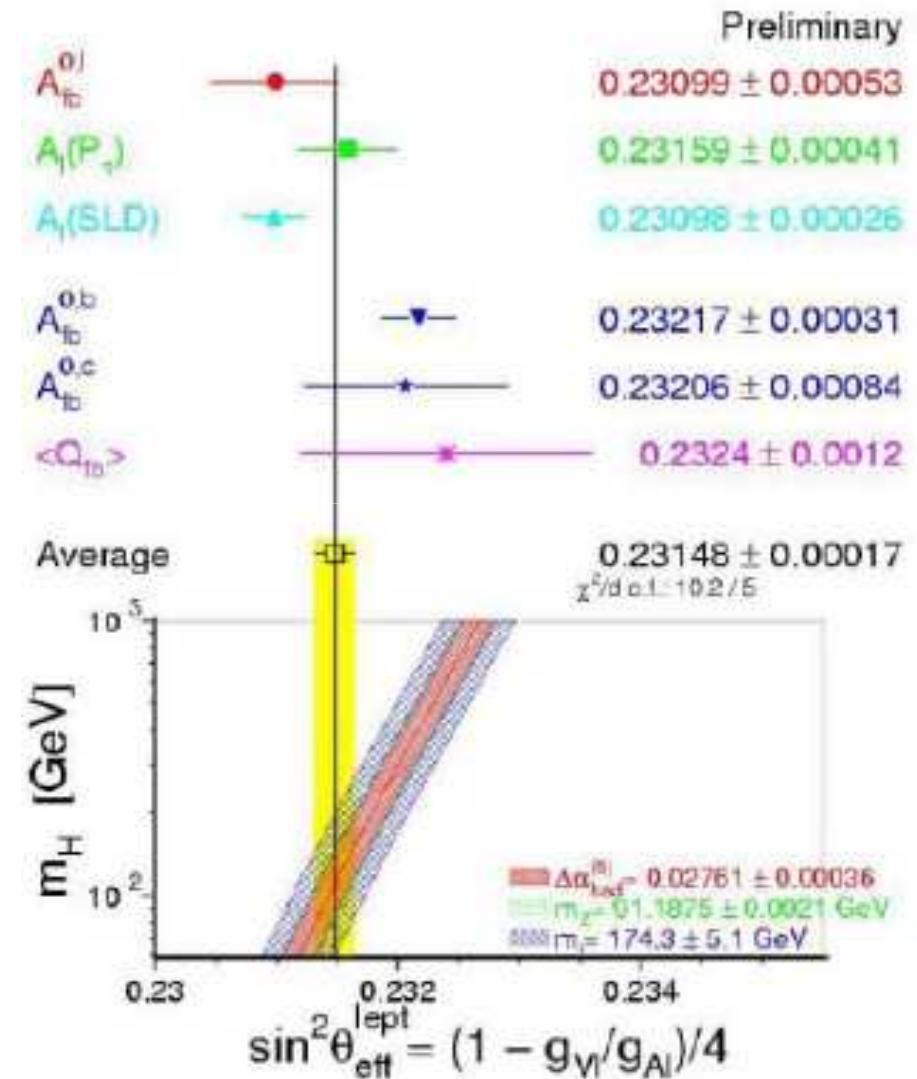
$T_{3I}$ =weak isospin  
= -1/2 for e



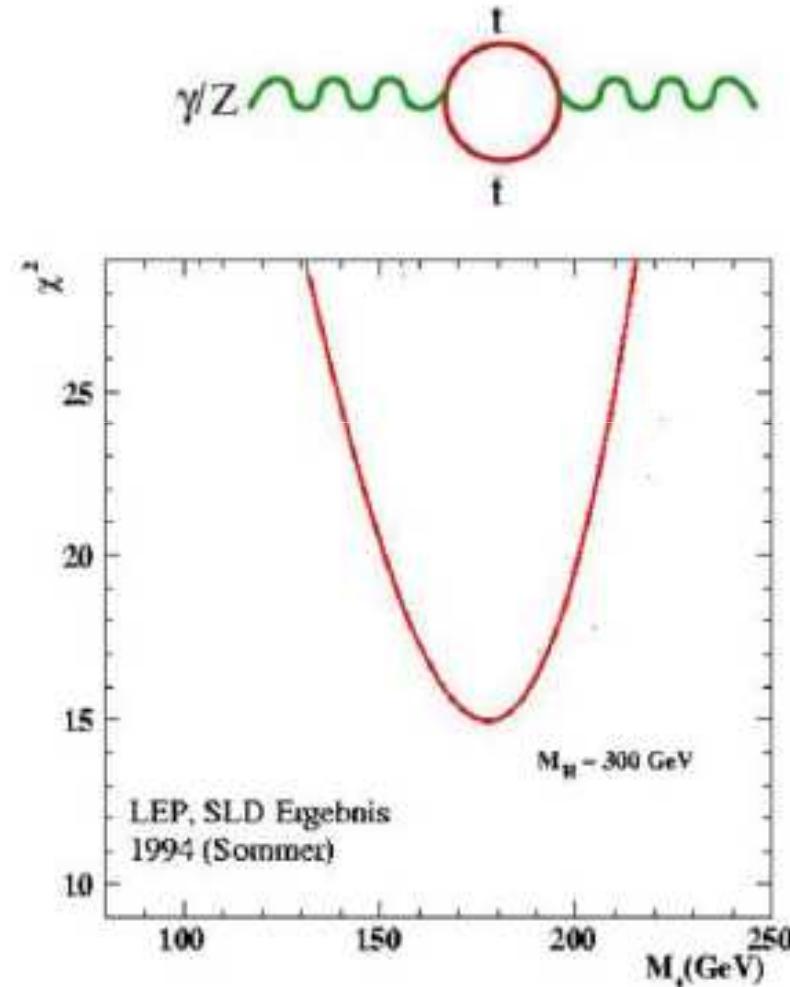
# *Measuring the ew mixing angle*

- Measuring the AFB can be interpreted as measuring  $\sin^2\theta_W$

- Result (only LEP):  
 $\sin^2\theta_W = 0.23221 \pm 0.00029$ 
  - Result improved by inclusion of other experiments, e.g. SLD (see later)



# Top mass prediction

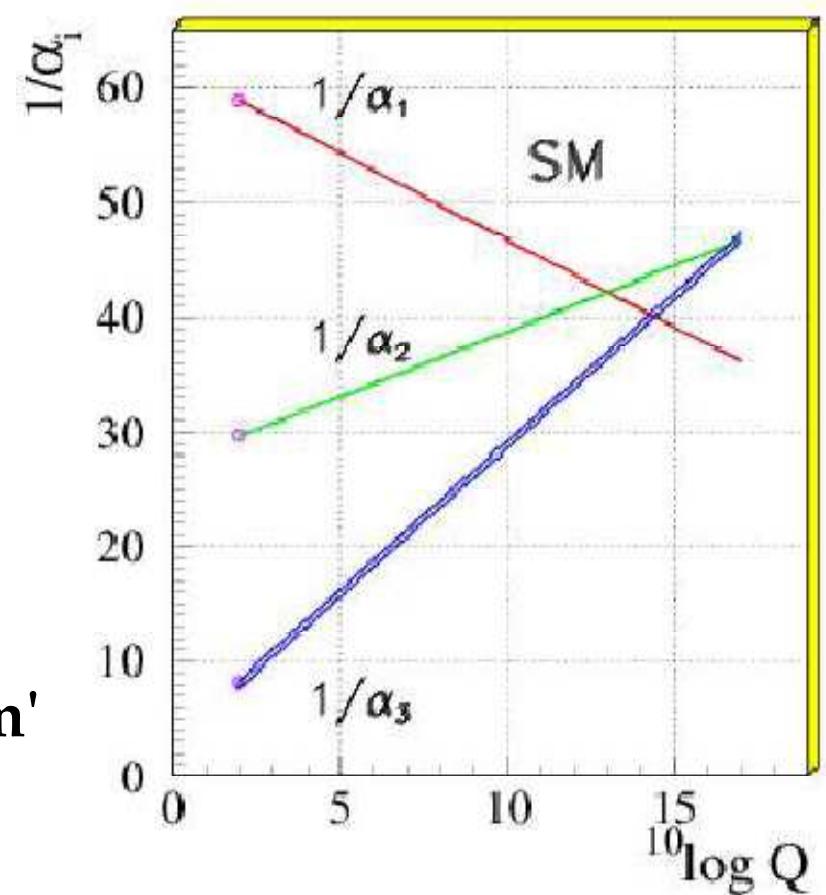


# *So far we have done ...*

- Discussion of LEP1 results, only as an example
- Because of time: not mentioned details from other  $e^+e^-$  experiments
  - SLD: very important also for  $\sin^2\theta_W$  (used polarized beams, see tomorrow)
  - LEP2: but also very rich program, as e.g. precision W mass measurement, searches for the Higgs boson, but also for new physics ....negative, so far
- *But why do we need physics beyond the SM and what are the experimental challenges?*

# *Shortcomings of the Standard Model*

- doesn't contain gravity
- doesn't explain neutrino masses
- doesn't have candidate for dark matter  
**23% of universe is cold dark matter!**
- no unification of gauge couplings possible
- further problem: 'hierarchy problem'  
Higgs mass unstable w.r.t. large quantum corrections:  
 $\delta M_H^2 \sim \Lambda^2$

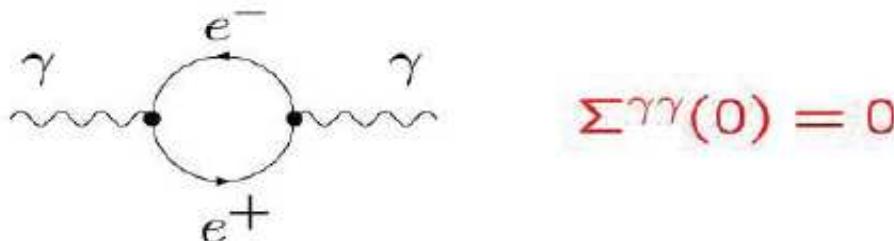


# *The Hierarchy Problem*

Consider loop corrections to propagators  $\longleftrightarrow$  corrections to masses

$$\Delta(p^2) \sim \frac{1}{p^2 - m^2 + \Sigma(p^2)}$$

- Photon self-energy in QED:

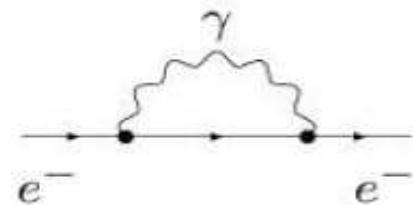


- consequence of U(1) gauge invariance of QED  $\rightarrow$  photon stays massless

$$\Delta_{\gamma\gamma}^{-1}(p^2) \rightarrow 0 \text{ for } p^2 \rightarrow 0$$

# Hierarchy Problem 2

- Electron self-energy in QED:



for  $\Lambda \rightarrow \infty$ :  $\Sigma^{ee} \sim m_e \int^{\Lambda} \frac{dk}{k} \rightarrow \ln \Lambda$

→ logarithmically divergent correction to electron mass  $\delta m_e$

Within QED: divergence can be removed via renormalization  
⇒  $k \rightarrow \infty$  possible

QED as effective theory, underlying more fundamental theory at scale  $\Lambda \Rightarrow$  cutoff scale

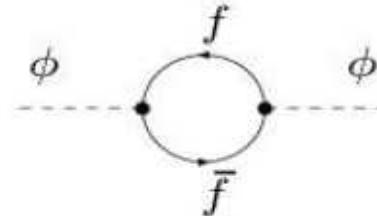
For  $\Lambda = M_{PL}$ :  $\delta m_e \approx 2\frac{\alpha}{\pi} m_e \log(M_{PL}/m_e) \approx 0.2 m_e$

→ modest correction, proportional to  $m_e$   
reason: chiral symmetry in limit  $m_e \rightarrow 0$ ,  $\psi_e \rightarrow \exp(i\gamma_5 \theta)\psi_e$

→ breaking proportional to  $m_e$  → symmetry protects  $m_e$

# Hierarchy Problem 3

Contribution of heavy fermions to Higgs self-energy:



$$\Sigma_f^{\phi\phi} \sim -2 N(f) \lambda_f^2 \int d^4 k \left( \frac{1}{k^2 - m_f^2} + \frac{2m_f^2}{(k^2 - m_f^2)^2} \right)$$

for  $\Lambda \rightarrow \infty$ :

$$\Sigma_f^{\phi\phi} \sim -2 N(f) \lambda_f^2 \left( \underbrace{\int \frac{d^4 k}{k^2}}_{\sim \Lambda^2} + 2m_f^2 \underbrace{\int \frac{dk}{k}}_{\sim \ln \Lambda} \right)$$

→ quadratically divergent!

For  $\Lambda = M_P$ :  $\delta M_\phi^2 \sim M_P^2 \Rightarrow \delta M_\phi^2 \approx 10^{30} M_\phi^2$  ( $M_\phi \lesssim 1$  TeV)

no additional symmetry for  $M_\Phi = 0$ , no protection against large corrections

- in general: scalar masses tend to be near highest theory mass scale
- hierarchy problem, extreme fine-tuning necessary to get small  $M_\Phi$

## *Hierarchy Problem 4*

- Hierarchy problem is instability of small Higgs mass to large corrections in a theory with a large mass scale in addition to the weak scale!
- E.g.: Grand unified Theory (GUT):  $\delta M_\Phi^2 \approx \lambda < v_{\text{GUT}} >^2$

Hierarchy problem is not just a problem of the Higgs mass;  
problem: why is  $M_W \ll M_{\text{GUT}}, M_{\text{PL}}$  why is  $V_{\text{Coulomb}} \gg V_{\text{Newton}}$ ?

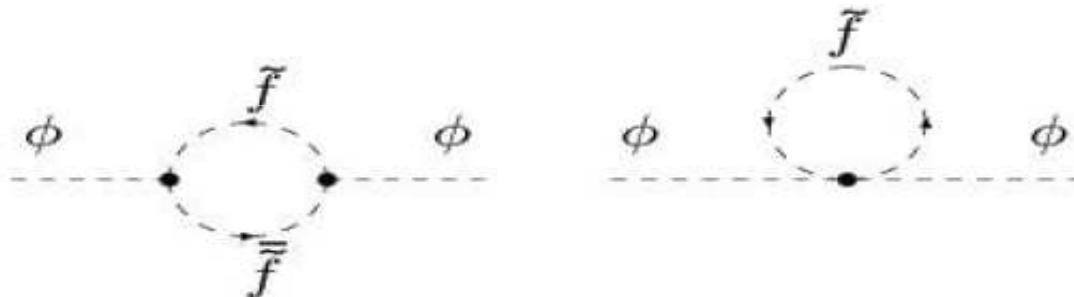
- Note however: there is another fine-tuning problem in nature, for which we have no clue so far ---- cosmological constant

# *Supersymmetry – intro 1*

- Symmetry between fermions and bosons

- ⇒  $Q | \text{boson} \rangle = | \text{fermion} \rangle$  and  $Q | \text{fermion} \rangle = | \text{boson} \rangle$
- ⇒ In other words: SM particles have SUSY partners (e.g.  $f_{L,R} \rightarrow \tilde{f}_{L,R}$ )

- SUSY:



$$\Sigma_{\tilde{f}}^{\phi\phi} \sim N(\tilde{f}) \tilde{\lambda}_f \int d^4k \left( \frac{1}{k^2 - m_{\tilde{f}_L}^2} + \frac{1}{k^2 - m_{\tilde{f}_R}^2} \right) + \text{terms without quadratic divergencies}$$

for  $\Lambda \rightarrow \infty$ :  $\Sigma_{\tilde{f}}^{\phi\phi} \sim 2 N(\tilde{f}) \tilde{\lambda}_f \Lambda^2$

# *Supersymmetry – intro 2*

- Quadratic divergencies cancel for:  $N(\tilde{f}_L) = N(\tilde{f}_R) = N(f)$   
 $\tilde{\lambda}_f = \lambda_f^2$

complete correction vanishes if furthermore:  $m_{\tilde{f}} = m_f$

For  $m_{\tilde{f}}^2 = m_f^2 + \Delta^2$ ,  $\tilde{\lambda}_f = \lambda_f^2$ , "soft SUSY breaking"

$$\Rightarrow \Sigma_{f+\tilde{f}}^{\phi\phi} \sim N(f) \lambda_f^2 \Delta^2 + \dots$$

→ correction acceptable small if mass splitting is of weak scale

- realized if mass scale of SUSY partners

$$M_{\text{SUSY}} \lesssim 1 \text{ TeV}$$

→ SUSY at TeV scale provides attractive solution of hierarchy problem

# *Supersymmetry – intro 3*

- Symmetry: group of transformations that leave Lagrangian invariant
  - ⇒ generators of the group fulfill certain algebra
  - ⇒ Noether's theorem: symmetries  $\longleftrightarrow$  conservation laws
- How to get unification of fundamental interactions?
  - ⇒ electroweak and strong interactions:
    - described by gauge theories: internal symmetries
    - $\gamma, Z, W^\pm$  : spin 1
  - ⇒ gravity:
    - described by general relativity: invariance under space-time transformations
    - graviton G : spin 2

# *Supersymmetry – intro 4*

- Haag, Lopuszanski, Sohnius theorem '75:

*'no direct symmetry transformations between fields with different integer spins'*

particles with different spin in the same multiplet only possible for SUSY theories,  $Q | \text{boson} \rangle = | \text{fermion} \rangle$  and  $Q | \text{fermion} \rangle = | \text{boson} \rangle$

→ symmetry generator  $Q$ : fermionic operator, needs to have spin  $\frac{1}{2}$

spin 2 → spin 3/2 → spin 1

graviton      gravitino      photon

- $Q$  changes spin (behaviour under spatial rotations) by  $\frac{1}{2}$

→ SUSY transformation influences in general both space-time and internal quantum numbers!

# *Supersymmetry – intro 5*

## ● Consequences of the SUSY algebra:

- Global SUSY transformation:  $\{Q_\alpha, \bar{Q}_{\dot{\alpha}}\} = \underbrace{2(\sigma^\mu)_{\alpha\dot{\alpha}} P_\mu}_{\text{constant translation in space-time}}$
- If SUSY transformations are made local:
  - space-time transformation differing from point to point

## ● Invariance under local SUSY transformations:

- invariance under local coordinate change
- general relativity
- local SUSY includes gravity, called 'supergravity' !

# *Supersymmetry – intro 6*

- $Q_\alpha$  changes spin of particle by  $\frac{1}{2}$   
 $Q_\alpha | \text{boson} \rangle = | \text{fermion} \rangle$  and  $Q_\alpha | \text{fermion} \rangle = | \text{boson} \rangle$
- Consider fermionic state  $| f \rangle$  with mass  $m$ :  
 $\Rightarrow P^2|f\rangle = m^2|f\rangle$
- Bosonic state:  $| b \rangle = Q_\alpha | f \rangle$   
 $\Rightarrow P^2|b\rangle = P^2Q_\alpha|f\rangle = Q_\alpha P^2|f\rangle = Q_\alpha m^2|f\rangle = m^2|b\rangle$
- For each fermionic state there is a bosonic state with the same mass  
→ states are paired bosonic ↔ fermionic
- Experimentally excluded, so SUSY must be broken symmetry!

# *Soft SUSY Breaking*

- Exact SUSY:  $m_f = m_{\tilde{f}}$   $\longrightarrow$  SUSY must be broken in nature!
- Only way for model of SUSY breaking:
  - spontaneous SUSY breaking

specific SUSY-breaking schemes yield effective Lagrangian at low energies, which is supersymmetric except for explicit soft breaking terms

- Soft SUSY-breaking terms: do not alter dimensionless couplings (i.e. dimension of coupling constants of soft SUSY-breaking terms  $> 0$ )

→ no quadratic divergences (in all orders of perturbation theory)  
scale of SUSY-breaking terms:

$$M_{\text{SUSY}} \leq 1 \text{ TeV}$$

# *Free parameters in the MSSM*

- mass matrices are  $3 \times 3$  hermitian
    - $m_Q^2, m_u^2, m_d^2, m_L^2, m_e^2$ : 45 parameters
  - gaugino masses  $M_1, M_2, M_3$  are complex numbers: 6
  - trilinear couplings  $a_u, a_d, a_e$  are  $3 \times 3$  complex matrices: 54
  - bilinear coupling  $b$  is  $2 \times 2$  matrix: 4
  - Higgs masses  $m_{Hu}^2, m_{Hd}^2$ : 2
- altogether 111 parameter ???

Symmetries (lepton + baryon number, Peccei-Quinn, R symmetry) lead to 'rotations':

- 4 non-trivial field redefinitions
  - 2 in the Higgs sector (since minimal model only 2 parameters in the Higgs sector)
- remain 105 free new parameters in the MSSM!

# *Unconstrained MSSM*

- no particular SUSY breaking mechanism assumed, parametrization of possible soft SUSY-breaking terms
  - relations between dimensionless couplings unchanged
  - no quadratic divergencies
- most general case:
  - 105 new parameters: masses, mixing angles, phases
  - Good phenomenological description for universal breaking terms (FCNC, etc.)
- Constrained models (e.g. CMSSM, mSUGRA, etc.):
  - assumption on the scheme of SUSY breaking
  - unification assumptions
  - prediction of soft SUSY-breaking terms in terms of small set of parameters

## **Experimental determination of SUSY parameters: patterns of breaking**

# Particle content in the MSSM

- Superpartners for Standard Model particles

$$[u, d, c, s, t, b]_{L,R} \quad [e, \mu, \tau]_{L,R} \quad [\nu_{e,\mu,\tau}]_L \quad \text{Spin } \frac{1}{2}$$

$$[\tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b}]_{L,R} \quad [\tilde{e}, \tilde{\mu}, \tilde{\tau}]_{L,R} \quad [\tilde{\nu}_{e,\mu,\tau}]_L \quad \text{Spin 0}$$

$$g \quad \underbrace{W^\pm, H^\pm}_{\gamma, Z, H_1^0, H_2^0} \quad \text{Spin 1 / Spin 0}$$

$$\tilde{g} \quad \tilde{\chi}_{1,2}^\pm \quad \tilde{\chi}_{1,2,3,4}^0 \quad \text{Spin } \frac{1}{2}$$

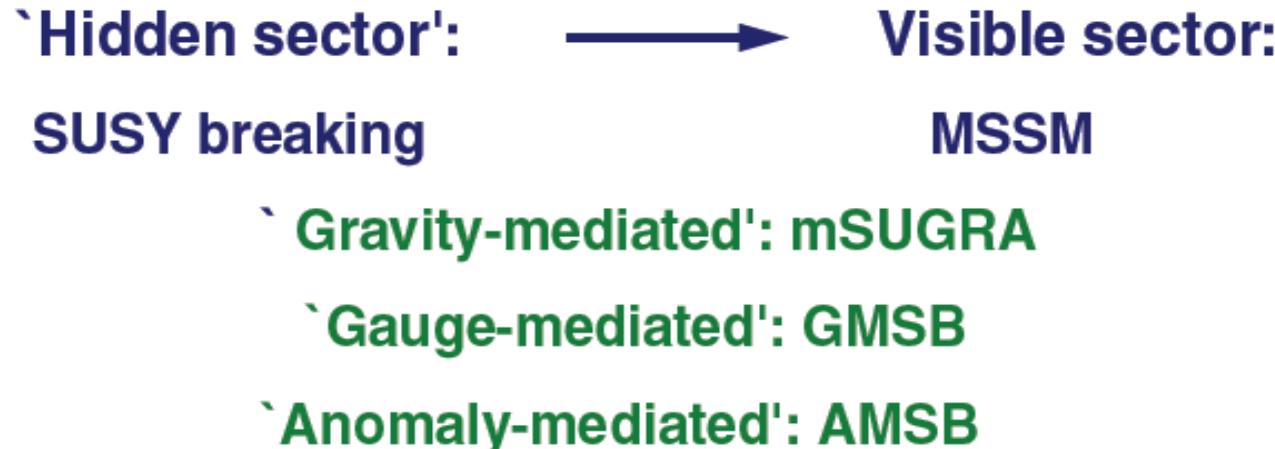
- Enlarged Higgs sector:

→ Two Higgs doublets, physical states:  $h^0, H^0, A^0, H^\pm$

- Breaking of  $SU(2) \times U(1)_Y$  (electroweak symmetry breaking)

→ fields with different  $SU(2) \times U(1)_Y$  quantum numbers can mix if they have the same  $SU(3)_c, U(1)_{em}$  quantum numbers →  $\tilde{\chi}_{1,2}^\pm, \tilde{\chi}_{1,2,3,4}^0$

# *SUSY breaking schemes*



- ⇒ **SUGRA:** mediating interactions are gravitational
- ⇒ **GMSB:** mediating interactions are ordinary electroweak and QCD gauge interactions
- ⇒ **AMSB:** SUSY breaking happens on a different brane in a higher-dimensional theory

- **Feature of schemes: lead to ‘characteristic’ mass spectra**

# *Gravity-mediated SUSY breaking*

- Quantum field theory of supergravity:

**QFT with spin 2 (and spin 3/2) field is not renormalizable**

→ cannot be extended to **arbitrarily high energies**

→ QFT of supergravity has to be interpreted as **effective theory**

contains non-renormalizable terms prop. to inverse powers of  $M_{\text{Pl}}$

- Best candidate for fundamental theory: string theory

- SUSY breaking in hidden sector:

→ supergravity Lagragian contains non-renormalizable terms that communicate between hidden and visible sector  $\sim 1/M_{\text{Pl}}^n$

# *Gravity-mediated SUSY*

- CMSSM -- five independent parameters:

$m_0^2, m_{1/2}, A_0, \tan \beta, \text{sign } \mu$

$m_0$ : universal scalar mass parameter

$m_{1/2}$ : universal gaugino mass parameter

$A_0$ : universal trilinear coupling

$\tan \beta$ : ratio of Higgs vacuum expectation values

$\text{sign}(\mu)$ : sign of supersymmetric Higgs parameter

- mSUGRA, if:  $m_{\frac{3}{2}} = m_0$  and  $b = A_0 - 1$

- Typical CMSSM or mSUGRA features:

- ⇒ lightest stable SUSY particle is the neutralino and is bino-like
- ⇒ almost mass degenerated  $\tilde{\chi}_1^\pm$  and  $\tilde{\chi}_2^0$  and are mainly wino-like
  - phenomenologically interesting: couple only 'left-handed'
- ⇒ light gaugino/higgsino and slepton spectrum but rather heavy coloured particles

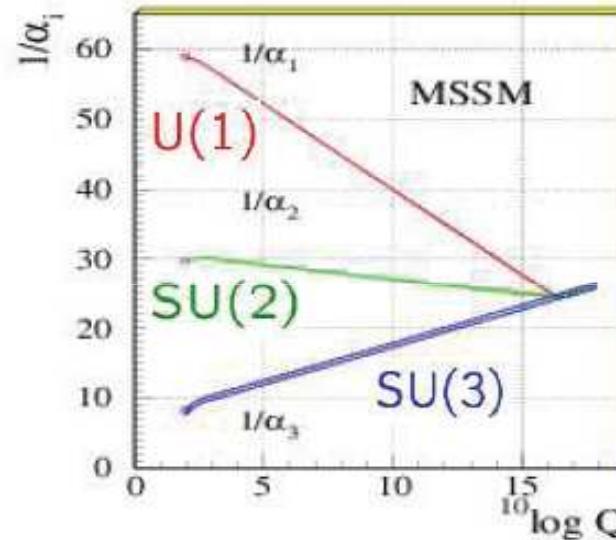
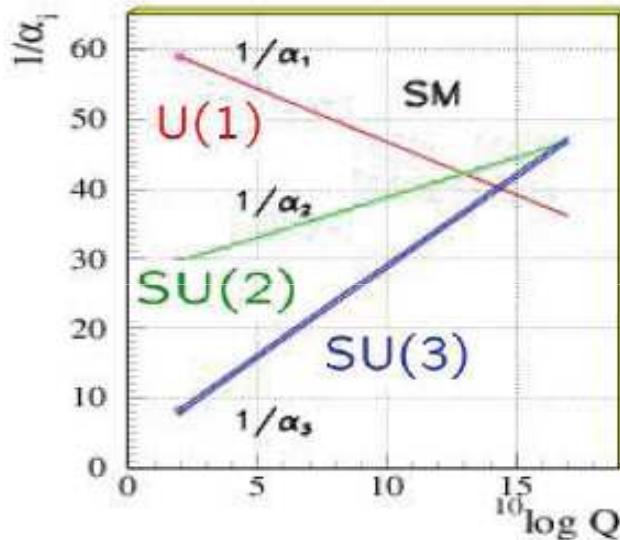
- Most studies done in this class of scenarios!

# *Properties of SUSY - Unification*

- **Gauge coupling unification:**

- ⇒ **Running of gauge couplings:**

$$\frac{1}{g^2(\mu^2)} = \frac{1}{g^2(\mu_0^2)} + \beta \ln \left( \frac{\mu^2}{\mu_0^2} \right)$$



- ⇒ coupling constant unification in MSSM for  $M_{\text{SUSY}} \lesssim 1 \text{ TeV}$

**Unification of couplings at high scale**  $\leftrightarrow$  'Grand unified theories' (GUT)

- ⇒ E.g. SO(10) GUTs, can naturally accommodate right-handed neutrinos

# New quantum number R-parity

- Most general gauge-invariant and renormalizable superpotential with chiral superfields in the MSSM:

$$\mathcal{V} = \mathcal{V}_{\text{MSSM}} + \underbrace{\frac{1}{2}\lambda^{ijk}L_iL_jE_k + \lambda'^{ijk}L_iQ_jD_k + \mu^iL_iH_u}_{\text{violate lepton number}} + \underbrace{\frac{1}{2}\lambda''^{ijk}U_iD_jD_k}_{\text{violates baryon number}}$$

- If both lepton+baryon number violated: rapid proton decay!
- Minimal choice contains only terms with even number of SUSY particles → new quantum number R-parity (SM=+1, SUSY=-1)

If conserved: -- SUSY only in pairs produced

- decays in SM particles + odd number of SUSY particles
- lightest SUSY particle (LSP) has to be stable (cold dark matter?)
- LSP: neutral, uncoloured → signatures with missing energy

# *Relations between SUSY parameters*

- Symmetry properties of MSSM Lagragian (SUSY, gauge invariance) give conditions to couplings and mass relations

- z.B. gauge-boson-fermion coupling = gaugino-fermion-sfermion coupling for U(1), SU(2) and SU(3) gauge groups
  - In SM: all masses are free input parameters (except  $m_w - m_z$  interdependence)

- MSSM:

- relations between chargino and neutralino masses (soft breaking+ew breaking)

- sfermion mass relations (gauge invariance):  $m_{\tilde{e}_L}^2 = m_{\tilde{\nu}_L}^2 - M_W^2 \cos(2\beta)$

- upper bound on mass of lightest CP-even Higgs boson

- All relations receive contributions from loop effects

→ experimental verification of relations is crucial test of SUSY

# *Prospects of SUSY at future colliders*

- Tevatron: slightly increased 1.8 -> 2 TeV, but 100 x higher lumi
  - ⇒ best prospects for trilepton signal:  $\tilde{\chi}_2^0 \tilde{\chi}_1^+ \rightarrow \ell^+ \ell^- \tilde{\chi}_1^0 \ell^+ \nu \chi_1^0$
  - ⇒  $\tilde{t}$ ,  $\tilde{b}$  searches, light SUSY Higgs in large tanbeta region
- LHC: direct production of 'couloured' particles  $\tilde{q}$ ,  $\tilde{g}$ 
  - ⇒ Very large mass range in searches for jets+missing energy up to 2-3 TeV
  - ⇒ electroweak-interacting particles as neutralinos/charginos mainly in decays!
  - ⇒ e.g. at the LHC in cascades:  $\tilde{g} \rightarrow \bar{q}\tilde{q} \rightarrow \bar{q}q\tilde{\chi}_2^0 \rightarrow \bar{q}q\tilde{\tau}\tau \rightarrow \bar{q}q\tau\tau\tilde{\chi}_1^0$
  - ⇒ assumption about particle identities in chains
  - ⇒ problem: main background of SUSY is SUSY itself !  
→ Test of SUSY relations not easy!
- ILC: direct production of all particles up to kinematical limit
  - ⇒ clean signatures: precise tests of all SUSY assumptions!

# *Goals of physics at the Linear Collider*

- **Discovery of New Physics (NP)**
  - complementary to the LHC
  - large potential for **direct searches**
  - impressive potential also for **indirect searches via precision**
- **Unraveling the structure of NP**
  - precise determination of **underlying dynamics and parameters**
  - **model distinction** through model independent searches
- **High precision measurements**
  - **test of the Standard Model (SM)** with unprecedented precision
  - even smallest hints of NP could be observed
- **Discovery of new phenomena via high energy and high precision!**

# *Needed ILC tools for all searches*

- **High statistics** needed
  - $L = 2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- Clean experimental environment
  - **low beamstrahlung** ( $\langle Y_{\text{ave}} \rangle = 0.048$ )
  - precise **luminosity** ( $\Delta L < 10^{-3}$ ) and  
**energy** ( $\Delta \sqrt{s} < 200 \text{ ppm}$ ) **measurement**
- Excellent detector resolution
  - **b-, c-tagging**, even the charge!
  - **$\tau$ -polarization**
  - $4\pi - \varepsilon$  angle coverage
  - exploitation of angular distributions

# *ILC features, cont.*

- **Threshold scans**
  - **Tunable energy** allows to vary energy around the mass threshold of new particles
  - Cost luminosity
  - Optimization of required energy steps a priori possible via rather accurate continuums measurements
- **Beam polarization**
  - Polarized e- with  $P(e^-) \sim 90\%$  expected
  - Polarized e+ with  $P(e^+) \sim 60\%$  (even in baseline ~40% expected !)
  - Enable to reveal underlying structure of new physics
  - Enhance statistics

# *Beam polarization at colliders*

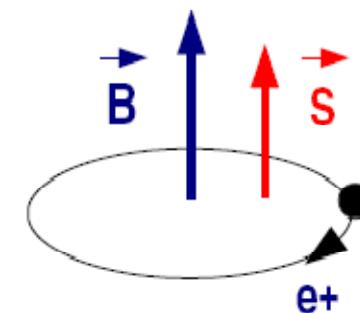
- **Polarization** = ensemble of particles with definite helicity  $\lambda = -\frac{1}{2}$  left- or  $+\frac{1}{2}$  right-handed :

$$P = \frac{\#N_R - \#N_L}{\#N_R + \#N_L}$$

→ beam polarization gives access to the couplings and unravels the structure of interactions

## ★ Polarized beams at circular e<sup>-</sup>e<sup>+</sup> colliders:

- Polarization of both beams via **Sokolov-Ternov effect**  
(= spin-flip effect due to synchrotron radiation)
- At **LEP (e<sup>+</sup>e<sup>-</sup>)**: massive depolarization effects; low polarization; not used for physics
- At **HERA (ep)**: excellent e<sup>-</sup>/ e<sup>+</sup> polarization reached, ~50%-70%; spin rotators used to produce longitudinally polarized beams for physics studies



# **Beam polarization at linear colliders**

## ★ Polarized beams at linear e<sup>-</sup>e<sup>+</sup> colliders:

- synchrotron radiation due to longitudinal acceleration negligible
- beams have to be polarized at the source !

## ● Polarized e<sup>-</sup> source:

- at the **SLAC Linear Collider (SLC)**: excellent e<sup>-</sup> polarization of about 78%
- led to **precision measurement** of the weak mixing angle:  
 $\sin\theta_{eff} = 0.23098 \pm 0.00026$  (SLD)    (LEP:  $0.23221 \pm 0.00029$ )

## ● Polarized sources at the ILC:

- expected e<sup>-</sup> polarization between 80% and 90%
- e<sup>+</sup> polarization is an absolute novelty! Expected P(e<sup>+</sup>) ~ 60%**

# Electron polarization

Remember again: First polarised  $e^-$  beam at a LC at SLAC (1992-98)  
with  $P(e^-) = [60\%, 78\%]$

How did they polarise the  $e^-$ ?

→ circ. polarised light ( $I_z = +1$  or  $-1$ )  
on GaAs cathode

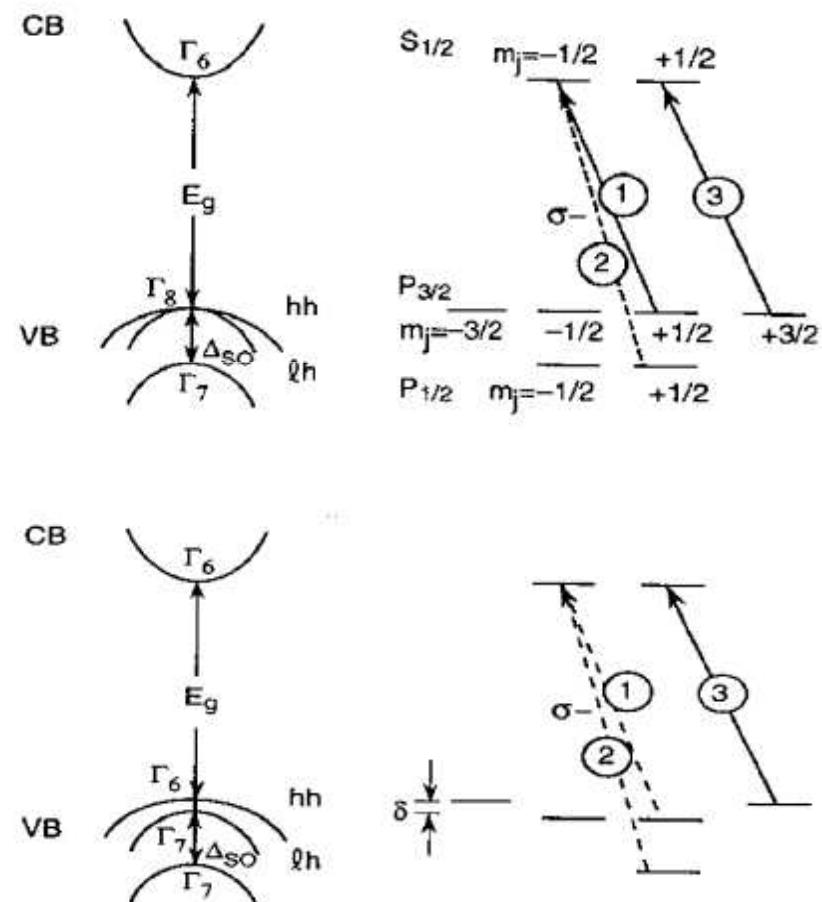
$$\Rightarrow P^{-1} = \frac{N_+ - N_-}{N_+ + N_-} = \frac{3-1}{3+1} = +0.5$$

How to get higher polarisation?

→ use strained lattice: grow GaAs on  
substrate with diff. crystal spacing  
⇒ removes degeneracy in lower level

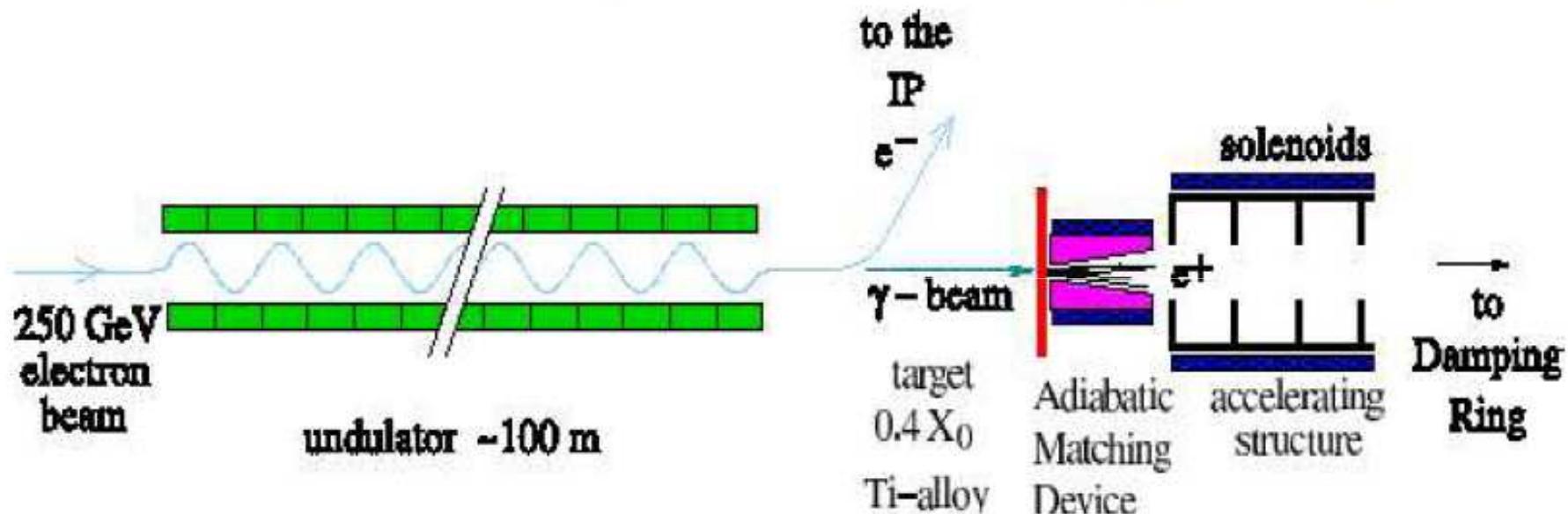
If  $h\nu = [E_g, (E_g + \delta)]$ :

→ in principle  $P^{-1} = 100\%$  possible...  
 $\Rightarrow P^{-1} = 80 - 90\%$  expected at LC



# Polarized positrons

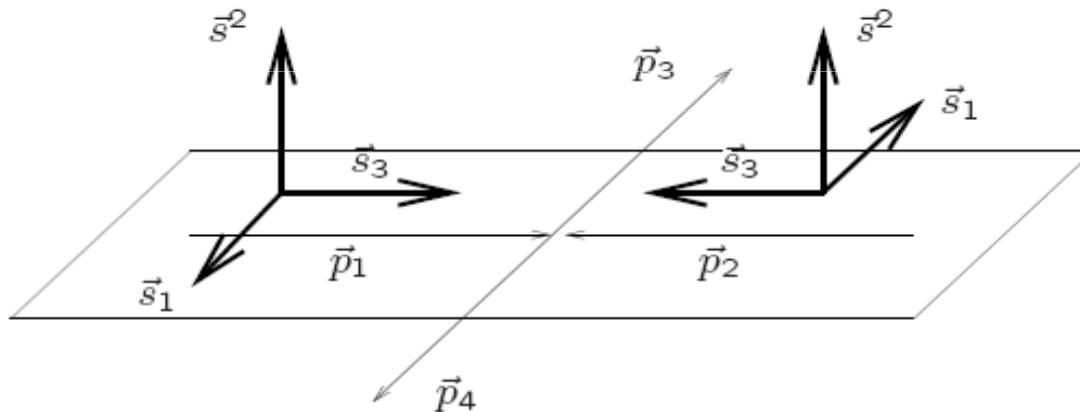
- Conventional source:  $e^-$  scattering in target  $\rightarrow$  pair production  $\rightarrow e^+$
- Undulator-based scheme: **polarized  $e^+$**  via circularly polarized photons



- deviation of  $e^-$  beam via helical magnetic field in undulator
- radiated circularly polarized photons onto thin target, pair production
- **$e^+$  polarization depends on undulator length**

# How to describe the spin?

- Definition: Basis of Spinvektors  $s^a$ ,  $a = 1, 2, 3$  with  $(s^a p) = 0$ :  
 build 'right-hand-system' in the CMS of  $e^-(p_1)e^+(p_2) \rightarrow X(p_3)Y(p_4)$   
 longitudinal Spinvektors:  $s^{3\mu}(p_{1,2}) := \frac{1}{m_{1,2}}(|\vec{p}_{1,2}|, E\hat{p}_{1,2})$   
 transverse Spinvektors:  $s^{2\mu}(p_1) := (0, \vec{p}_1 \times \vec{p}_3)$ ,  $s^{2\mu}(p_2) = s^{2\mu}(p_1)$   
 $s^{1\mu}(p_1) := (0, \vec{p}_1 \times \vec{s}^2(p_1))$ ,  $s^{1\mu}(p_2) = -s^{1\mu}(p_1)$



- Definition: 'left-handed' and 'right-handed'  $\equiv$  with respect to  $\hat{p}$   
 If Spinvektor  $\vec{s}^3 = \begin{pmatrix} \text{parallel } \vec{p} \\ \text{antiparallel } \vec{p} \end{pmatrix} \equiv \begin{pmatrix} \text{'right-handed': } P > 0 \\ \text{'left-handed': } P < 0 \end{pmatrix}$

# *Remarks about couplings structure*

Definition: Helicity  $\lambda = \vec{s} \cdot \vec{p}/|\vec{p}|$  ‘projection of spin’

Chirality = handedness is equal to helicity only if  $m=0$ !

Def.: left-handed  $\equiv P(e^\pm) < 0$

right-handed  $\equiv P(e^\pm) > 0$

Which configurations are possible in principle?

s-channel:

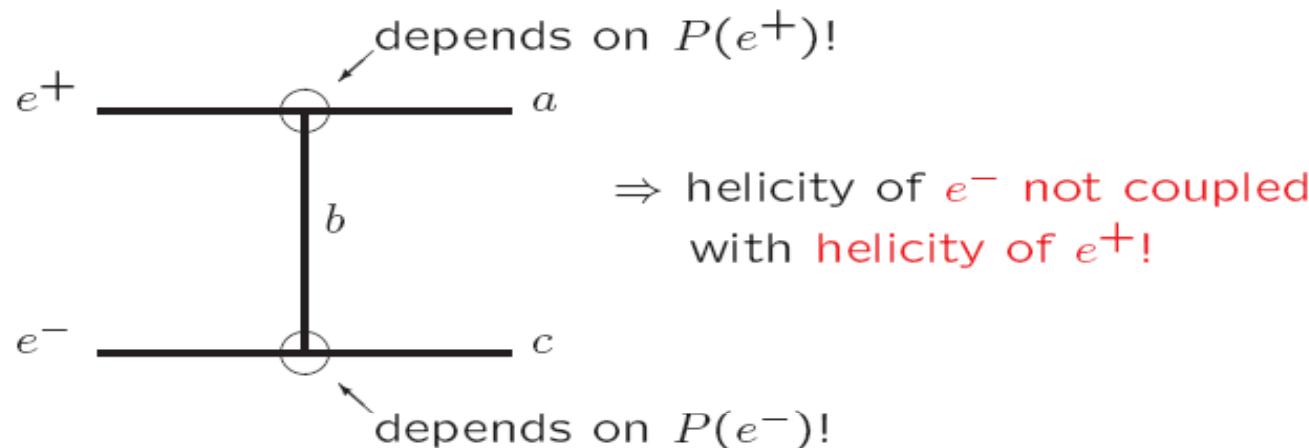


⇒ In principle:  $P(e^-)$  fixes also helicity of  $e^+$ !

# General remarks, cont.

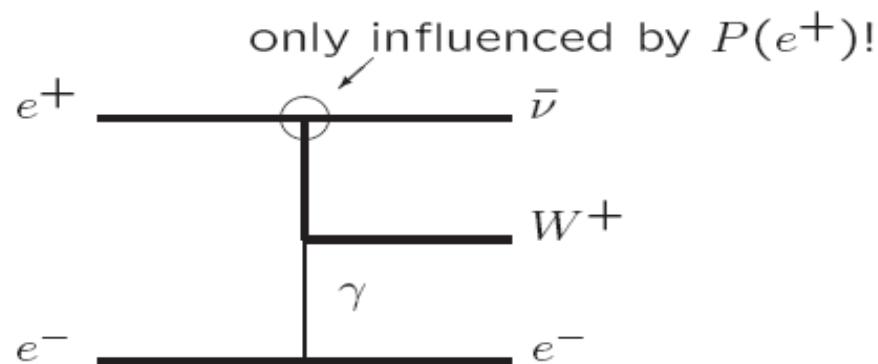
Which configurations are possible in the crossed channels?

t-channel:



Two examples:

a) Single  $W$  production



b) Bhabha scattering

$\Rightarrow \gamma, Z$  exchange in s-channel:

selects LR, RL

$\Rightarrow \gamma, Z$  exchange in t-channel:

LL,RR possible!

unpolarised	4.50 pb
$P_{e^-} = -80\%$	4.63 pb
$P_{e^-} = -80\%, P_{e^+} = -60\%$	4.69 pb
$P_{e^-} = -80\%, P_{e^+} = +60\%$	4.58 pb

# *Statistical arguments for $P(e+)$*

Polarized cross sections can be subdivided in:

$$\begin{aligned}\sigma_{P_{e^-} P_{e^+}} &= \frac{1}{4} \left\{ (1 + P_{e^-})(1 + P_{e^+})\sigma_{RR} + (1 - P_{e^-})(1 - P_{e^+})\sigma_{LL} \right. \\ &\quad \left. + (1 + P_{e^-})(1 - P_{e^+})\sigma_{RL} + (1 - P_{e^-})(1 + P_{e^+})\sigma_{LR} \right\},\end{aligned}$$

$\sigma_{RR}$ ,  $\sigma_{LL}$ ,  $\sigma_{RL}$ ,  $\sigma_{LR}$  are contributions with fully polarized L, R beams.

In case of a vector particle only (LR) and (RL) configurations contribute:

$$\begin{aligned}\sigma_{P_{e^-} P_{e^+}} &= \frac{1 + P_{e^-}}{2} \frac{1 - P_{e^+}}{2} \sigma_{RL} + \frac{1 - P_{e^-}}{2} \frac{1 + P_{e^+}}{2} \sigma_{LR} \\ &= (1 - P_{e^-} P_{e^+}) \frac{\sigma_{RL} + \sigma_{LR}}{4} \left[ 1 - \frac{P_{e^-} - P_{e^+}}{1 - P_{e^+} P_{e^-}} \frac{\sigma_{LR} - \sigma_{RL}}{\sigma_{LR} + \sigma_{RL}} \right] \\ &= (1 - P_{e^+} P_{e^-}) \sigma_0 [1 - P_{\text{eff}} A_{LR}],\end{aligned}$$

# Statistics 2

- Polarized cross section reads:  $\sigma_{P_e^- P_e^+} = (1 - P_{e^+} P_{e^-}) \sigma_0 [1 - P_{\text{eff}} A_{\text{LR}}]$

the unpolarized cross section:  $\sigma_0 = \frac{\sigma_{\text{RL}} + \sigma_{\text{LR}}}{4}$

the left-right asymmetry:  $A_{\text{LR}} = \frac{\sigma_{\text{LR}} - \sigma_{\text{RL}}}{\sigma_{\text{LR}} + \sigma_{\text{RL}}}$

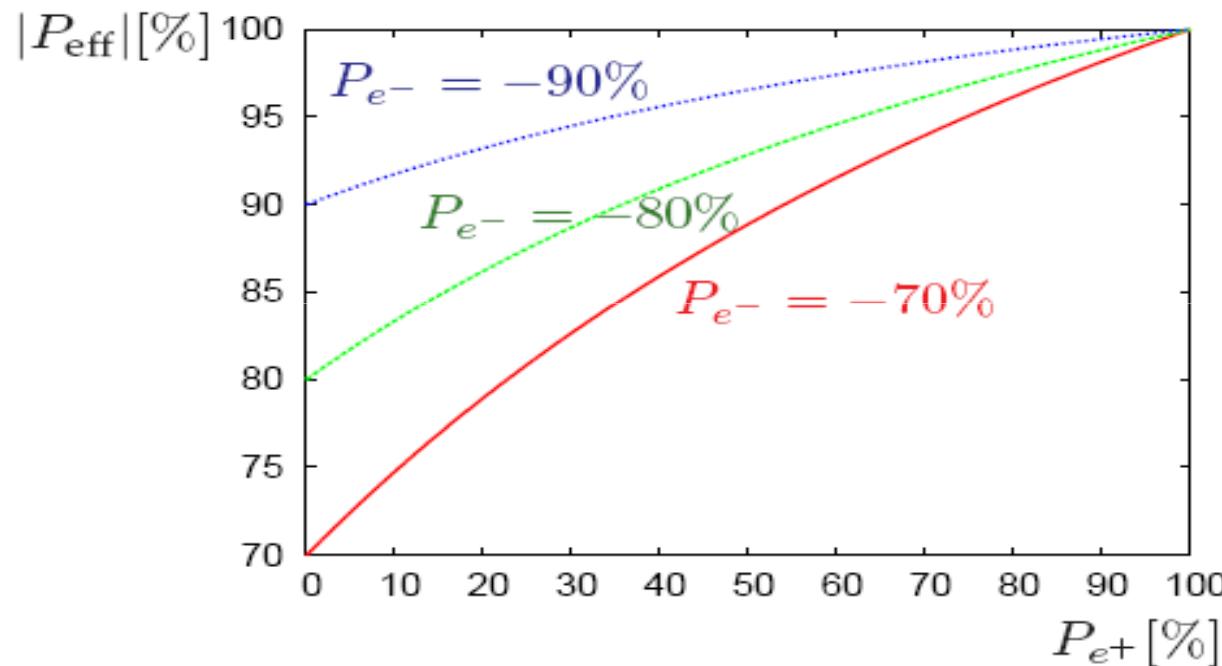
and the effect  $\mathcal{L}_{\text{eff}} = \frac{1}{2}(1 - P_{e^-} P_{e^+})\mathcal{L}$        $P_{\text{eff}} = \frac{P_{e^-} - P_{e^+}}{1 - P_{e^+} P_{e^-}}$

- With effective luminosity  $\mathcal{L}_{\text{eff}} = \frac{1}{2}(1 - P_{e^-} P_{e^+})\mathcal{L}$

→  $\sigma_{P_e^- P_e^+} = 2\sigma_0(\mathcal{L}_{\text{eff}}/\mathcal{L}) [1 - P_{\text{eff}} A_{\text{LR}}]$

# *Statistics 3*

**Effective polarization:**  $P_{\text{eff}} = \frac{P_{e^-} - P_{e^+}}{1 - P_{e^+}P_{e^-}}$



- (80%,60):  $P_{\text{eff}} = 95\%$
- (90%,60%):  $P_{\text{eff}} = 97\%$
- (90%, 30%):  $P_{\text{eff}} = 94\%$

# Statistics 4

- Effective polarization

$$P_{eff} := (P_{e^-} - P_{e^+})/(1 - P_{e^-} - P_{e^+}) \\ = (\#LR - \#RL)/(\#LR + \#RL)$$

- Fraction of colliding particles

$$\mathcal{L}_{eff}/\mathcal{L} := \frac{1}{2}(1 - P_{e^-} - P_{e^+}) = (\#LR + \#RL)/(\#all)$$

Colliding particles:

	RL	LR	RR	LL	$P_{eff}$	$\mathcal{L}_{eff}/\mathcal{L}$
$P(e^-) = 0,$ $P(e^+) = 0$	0.25	0.25	0.25	0.25	0.	0.5
$P(e^-) = -1,$ $P(e^+) = 0$	0	0.5	0	0.5	-1	0.5
$P(e^-) = -0.8,$ $P(e^+) = 0$	0.05	0.45	0.05	0.45	-0.8	0.5
$P(e^-) = -0.8,$ $P(e^+) = +0.6$	0.02	0.72	0.08	0.18	-0.95	0.74

⇒ Enhancing of  $\mathcal{L}_{eff}$  with  $P(e^-)$  and  $P(e^+)$ !

# Statistics 5

How are  $P_{\text{eff}}$  and  $A_{\text{LR}}$  related?

$$A_{\text{LR}} = \frac{1}{P_{\text{eff}}} A_{LR}^{\text{obs}} = \frac{1}{P_{\text{eff}}} \frac{\sigma_{-+} - \sigma_{+-}}{\sigma_{-+} + \sigma_{+-}},$$

That means:

$$\left| \frac{\Delta A_{\text{LR}}}{A_{\text{LR}}} \right| = \left| \frac{\Delta P_{\text{eff}}}{P_{\text{eff}}} \right|$$

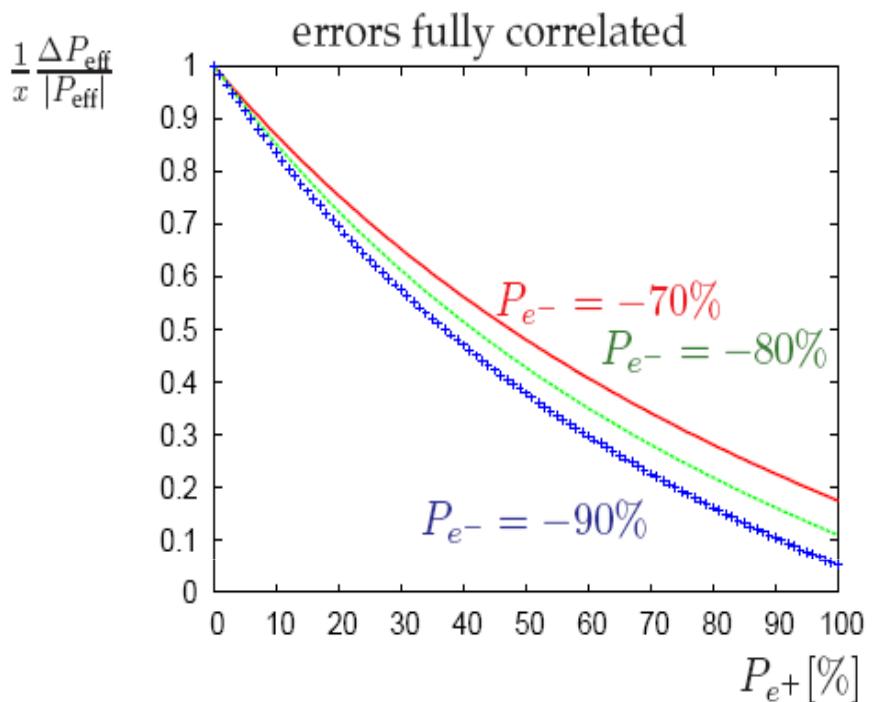
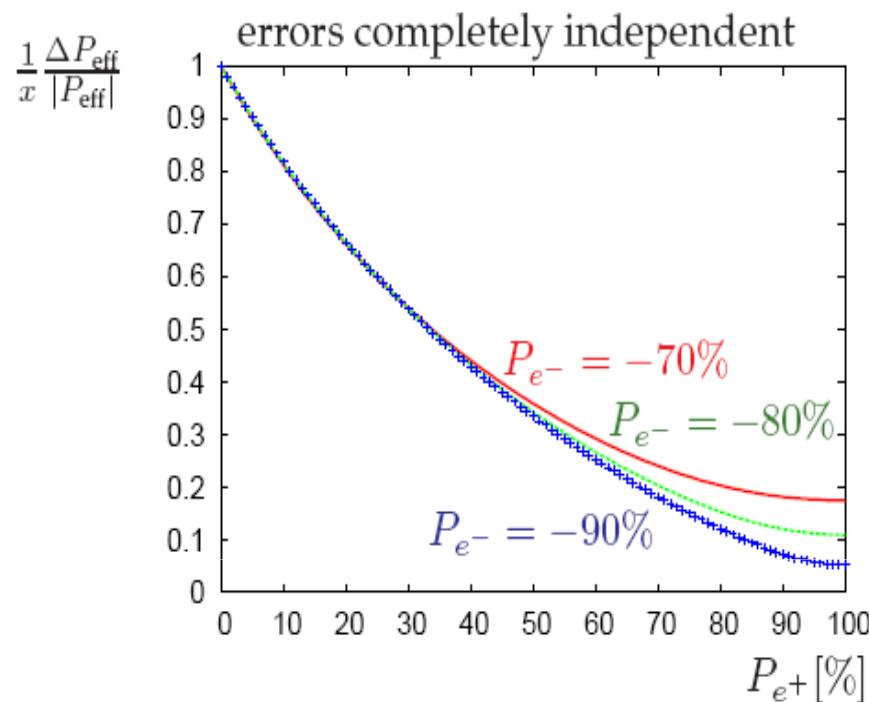
With pure error propagation (and errors uncorrelated), one obtains:

$$\frac{\Delta P_{\text{eff}}}{P_{\text{eff}}} = \frac{x}{(|P_{e^+}| + |P_{e^-}|) (1 + |P_{e^+}| |P_{e^-}|)} \sqrt{(1 - |P_{e^-}|^2)^2 P_{e^+}^2 + (1 - |P_{e^+}|^2)^2 P_{e^-}^2}$$

With

$$x \equiv \Delta P_{e^-} / P_{e^-} = \Delta P_{e^+} / P_{e^+}$$

# Statistics 6



● (80%,60):  $P_{\text{eff}} = 95\%$

$$\Delta A_{\text{LR}}/A_{\text{LR}} = 0.3$$

gain: factor~3

(90%,60%):  $P_{\text{eff}} = 97\%$

$$\Delta A_{\text{LR}}/A_{\text{LR}} = 0.27$$

factor>3

(90%, 30%):  $P_{\text{eff}} = 94\%$

$$\Delta A_{\text{LR}}/A_{\text{LR}} = 0.5$$

factor~2

→ NO gain with only polarized  $e^-$  !

# *Background suppression*

$WW$ ,  $ZZ$  production = large background for NP searches!

$W^-$  couples only **left-handed**:

→  $WW$  background strongly suppressed with right polarized beams!

Scaling factor =  $\sigma^{pol}/\sigma^{unpol}$  for  $WW$  and  $ZZ$ :

$P_{e^-} = \mp 80\%$ , $P_{e^+} = \pm 60\%$	$e^+e^- \rightarrow W^+W^-$	$e^+e^- \rightarrow ZZ$
(+0)	0.2	0.76
(-0)	1.8	1.25
(+-)	0.1	1.05
(-+)	2.85	1.91

## *Back to the ILC physics case....*

- But since the ILC can not start before 2015+, all physics issues have to be seen in view of expected LHC results
- In the following we discuss several physics topics, starting at 500 GeV, 1TeV, multi-TeV
- Applying the mentioned tools, threshold scans, beam polarization, precision measurements
- But only a personal selection of examples .....

# *Physics up to $\sqrt{s}=500$ GeV: top*

- Current average:  $m_{\text{top}} = 172.4 \pm 1.2 \text{ GeV}$

- Expectations at the LHC:

- ⇒  $\Delta m_{\text{top}} \sim 1 \text{ GeV}$
  - ⇒ Yukawa couplings  $\sim 20 \%$  (with slight model assumptions)

- Expectations at the ILC:

- ⇒ Mass via threshold scans:  $m_{\text{top}} \sim 100 \text{ MeV}$  (dominated by theory)
  - ⇒ Yukawa couplings via  $t\bar{t}H$ : difficult due to small rates, but  $< 20\%$
  - ⇒ Unique access to electroweak couplings

- Why are top properties so important?

- ⇒ heaviest detected elementary particle up to now
  - ⇒ opens unique window to physics beyond the SM

## *Top mass, 2*

Additional problem for  $m_t$ : what is the mass of a coloured object?

Top pole mass is not “IR safe” (affected by large long-distance contributions), cannot be determined to better than  $\mathcal{O}(\Lambda_{\text{QCD}})$

Current exp. error on  $m_t$  from the Tevatron:  $\delta m_t^{\text{exp}} = 1.2 \text{ GeV}$

Which mass is actually measured at the Tevatron and the LHC?

Measured mass should be “close to the pole mass”, but how close?

Issue not yet settled, effects of  $\mathcal{O}(\Gamma_t)$  are not fully under control

## *Top mass 3*

From running at the  $t\bar{t}$  threshold:

- ⇒ Measurement of a “threshold mass parameter” with high precision:  $\lesssim 20$  MeV
- + transition to suitably defined (short-distance) top-quark mass, e.g.  $\overline{\text{MS}}$  mass

We expect at the LC:

$$\Rightarrow \delta m_t^{\text{exp}} \lesssim 100 \text{ MeV} \text{ (dominated by theory uncertainty)}$$

# *Importance of 'top' mass*

- Top mass is important input parameter for electroweak precision tests
  - SM prediction for  $m_W$  and  $\sin^2 \theta_{\text{eff}}$ : consistency checks, sensitivity to  $m_{\text{Higgs}}$
  - compare  $m_W$  and  $\sin^2 \theta_{\text{eff}}$ : experimental accuracy with theoretical prediction
- Theoretical uncertainties
  1. unknown higher orders:  $\Delta \sin^2 \theta_{\text{eff}}^{\text{ho}} \sim 5 \times 10^{-5}$ ,  $\Delta m_W^{\text{ho}} \sim 4 \text{ MeV}$
- High precision of top mass mandatory to exploit theory at quantum level!

If  $\Delta m_{\text{top}} \sim 1 \text{ GeV}$  (LHC):  $\Delta \sin^2 \theta_{\text{eff}}^{\text{input}} \sim 3 \times 10^{-5}$ ,  $\Delta m_W^{\text{input}} \sim 6 \text{ MeV}$

If  $\Delta m_{\text{top}} \sim 0.1 \text{ GeV}$  (ILC):  $\Delta \sin^2 \theta_{\text{eff}}^{\text{input}} \sim 0.3 \times 10^{-5}$ ,  $\Delta m_W^{\text{input}} \sim 1 \text{ MeV}$

# *Electroweak symmetry breaking / Higgs*

- Where do we expect the Higgs?

$M_h < 186 \text{ GeV}$

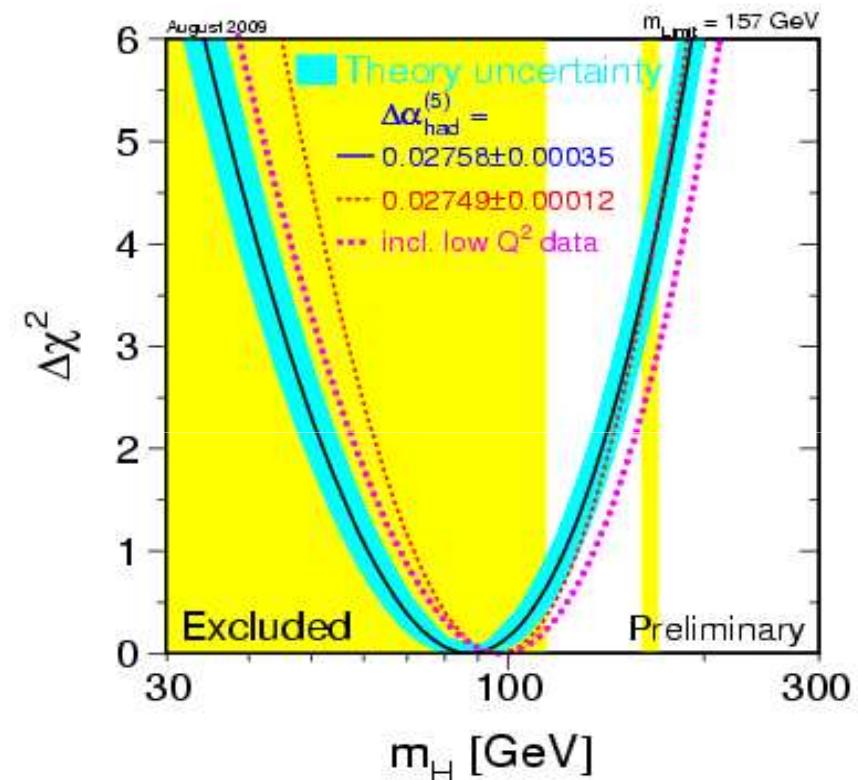
(LEP, SLD, CDF, D0 + LEP-2 direct limit)

- Light Higgs expected but heavier

SM-Higgs not excluded!

- SUSY Higgs  $< 135 \text{ GeV}!$

- 'Higgs' task for the LC:  
*mass measurement, spin verification,  
couplings determination*



→ Establish the mechanism of electroweak symmetry breaking!

# *Determination of Higgs properties*

- **Expectations at the LHC:**

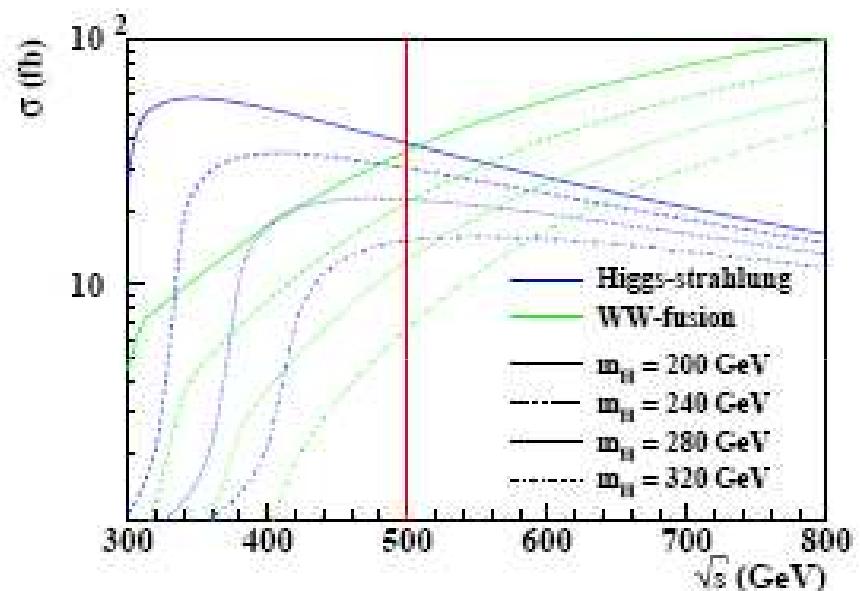
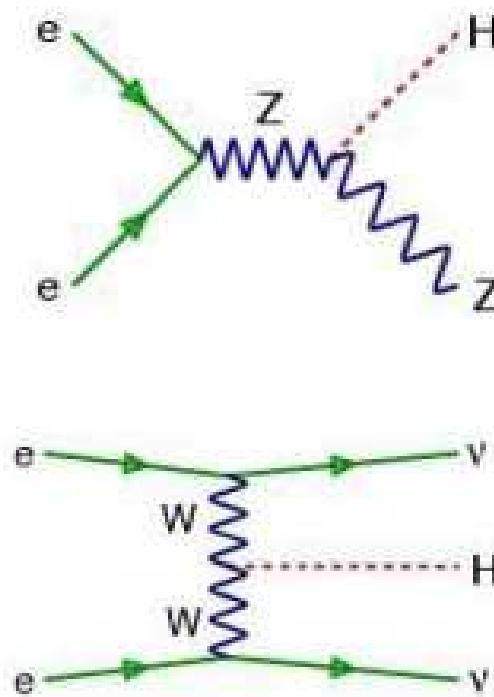
- Higgs mass: up to  $\Delta m_H = 100\text{-}200 \text{ MeV}$
- Higgs couplings: 15%-40% (with some model assumptions)

- **Expectations at the ILC:**

- absolute couplings: 1-5 %
- Establishing of ew sym. breaking: triple Higgs couplings at 500 GeV up to 22%
- estimate: further gain of 30%-50% precision if both beams polarized
- process  $t\bar{t}H$ : difficult due to small rates (but threshold effects!)
- accuracy about 24% for  $m_H=120 \text{ GeV}$  (unpolarized beams)
- improvement factor 2.5 when (80%, 0%)  $\rightarrow$  (80%,60%)

**LHC input for optimal choices of running scenarios !**

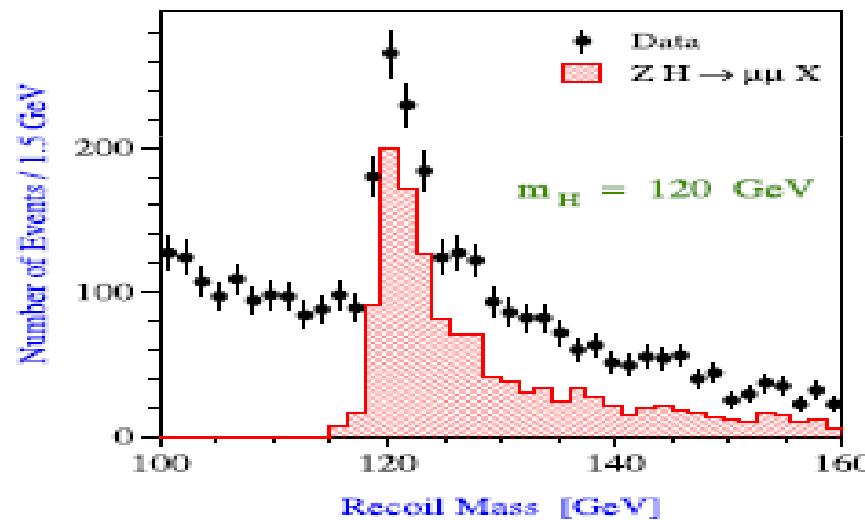
# *Higgs mass at ILC*



- Dominant production mechanisms: Higgsstrahlung and WW-fusion

## *Higgs mass, 2*

- Use Higgsstrahlung: due to well-known initial state and well-observed Z-decays
  - Derive Higgs mass **independently from decay**

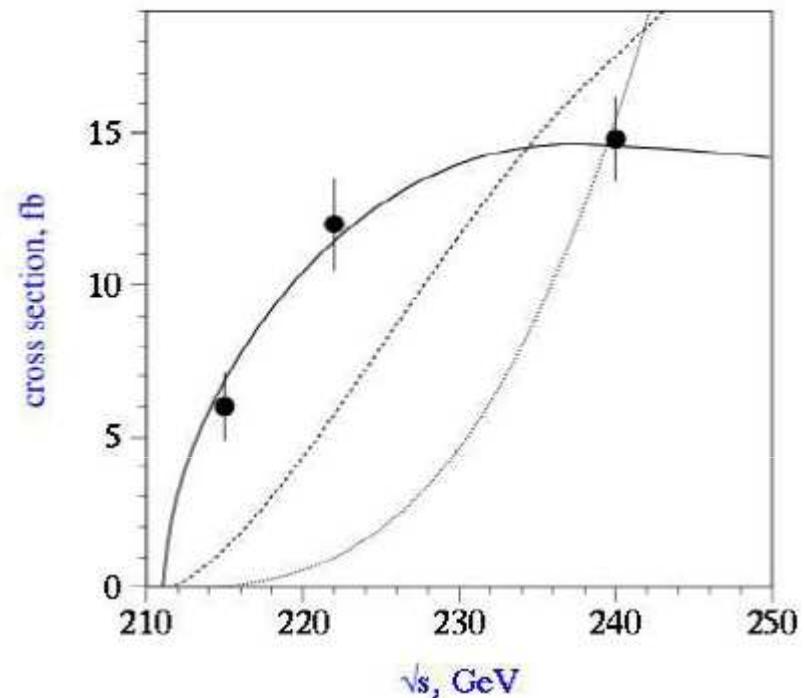


- Only possible at a LC!

# Higgs properties

## Spin verification

- threshold scans (i.e. at  $\sqrt{s}=205\text{-}300 \text{ GeV}$ ) mainly needed for spin verification
- due to excellent masses from continuum, only about 3 energy steps needed

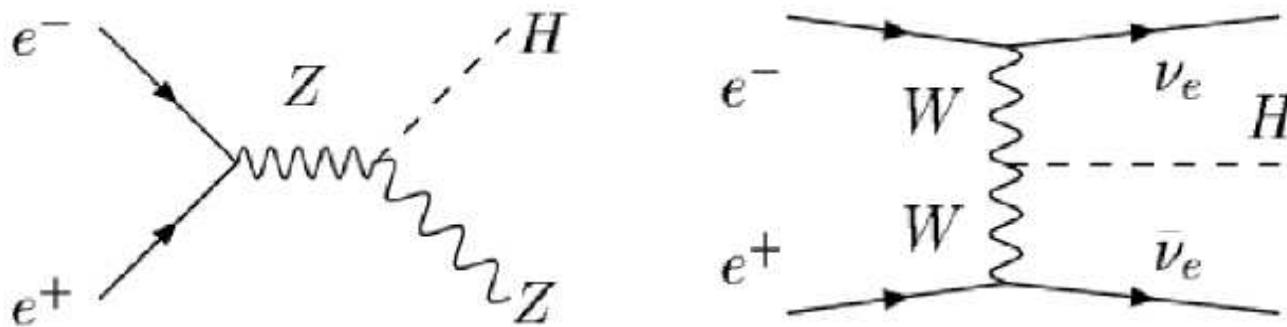


## Parity Measurement

- in  $H\tau\tau$  decay
- distinguish between CP-odd and even via angular distributions
- independent from production process

# Technical requirements – Higgs sector

- Couplings determination: high rates and lumi needed



- ⇒ measurement of couplings in Higgs-strahlungs process at  $\sqrt{s}=350$  GeV
- ⇒ beam polarization (80%,0) → (80%, 60%): improvement by about 30%
- ⇒ triple Higgs couplings: e.g. in HHZ at  $\sqrt{s}=500$  up to 22% (unpolarized beams)
- ⇒ estimate: further gain of 30%-50% precision if both beams polarized
- Polarized  $e^+$  very useful even in Higgs physics (factor 4 in separation, 30% in couplings, etc.), in particular at  $\sqrt{s}=350$  GeV and 500 GeV

# New Physics -- Supersymmetry

**Remember: free parameters in the MSSM:**

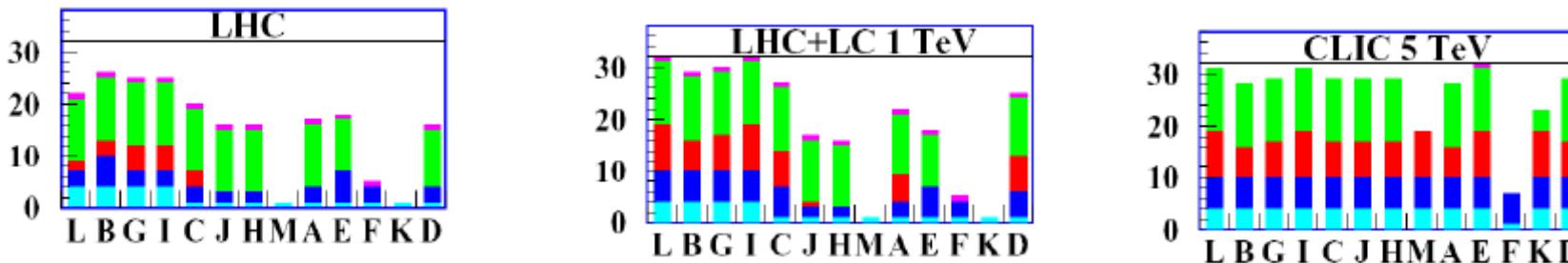
- mass matrices are  $3 \times 3$  hermitian  
→  $m_Q^2, m_u^2, m_d^2, m_L^2, m_e^2$ : 45 parameters
- gaugino masses  $M_1, M_2, M_3$  are complex numbers: 6
- trilinear couplings  $a_u, a_d, a_e$  are  $3 \times 3$  complex matrices: 54
- bilinear coupling  $b$  is  $2 \times 2$  matrix: 4
- Higgs masses  $m_{H_u}^2, m_{H_d}^2$ : 2  
→ altogether 111 parameter ???

Symmetries (lepton + baryon number, Peccei-Quinn, R symmetry) lead to 'rotations':

- 4 non-trivial field redefinitions
- 2 in the Higgs sector (since minimal model only 2 parameters in the Higgs sector)  
→ remain 105 free new parameters in the MSSM!

# *DisneyWorld of SUSY scenarios*

- Often (ab)used: Manhattan plots



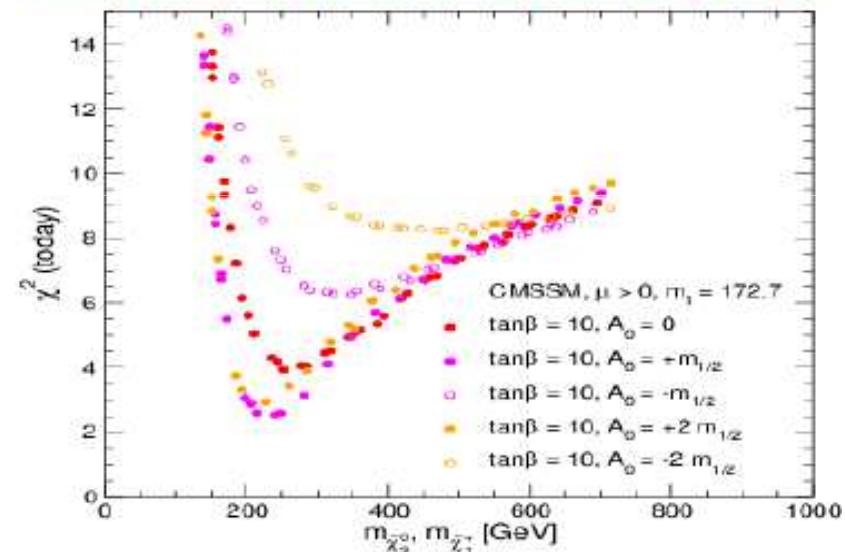
- 13 SUSY ‘benchmarks’ scenarios out of millions ...  
*really a true representative choice ?*
- heavy masses often mass degenerated: no resolution  
(beamstrahlung!) has been taken into account...  
*really a reliable ‘counting’ ?*
- experimental verification of properties not studied ...  
*really a useful basis for future decisions?*

**Physics or just propaganda?**

# *SUSY scale expectations*

- In which range do we expect SUSY?
  - at least some light particles should be accessible at 500 GeV
  - best possible tools needed to get maximal information out of only the part of the spectrum
- To reveal the structure of the underlying physics, it is important to determine the parameters in a model-independent way and test all model assumptions experimentally
- Soon we will have LHC data, but LHC/ILC interplay will be essential and both machines cover a large range of the parameter space !

*Ellis, Heinemeyer, Olive, Weber, Weiglein '07*



# *Discovery of SUSY*

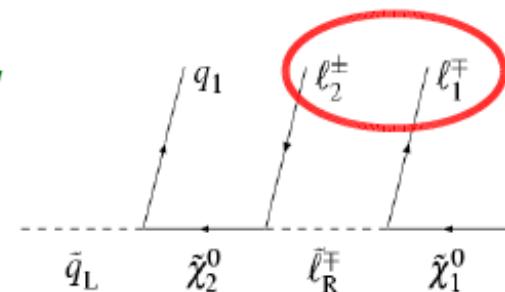
- What's needed for establishing SUSY?

- Spin verification: via analysis of angular distributions
- Couplings measurement: Yukawa couplings = gauge couplings
- Precise mass measurements
- Unraveling the SUSY breaking mechanism and test unification
- 'model- independent' determination of the parameters (105 already in the MSSM!)

- Expectations at the LHC:

- Coloured SUSY partners: discovery reach  $m_{\tilde{q}, \tilde{g}} < 2-2.5$  TeV
- Non-coloured partners:
  - a) via Drell-Yan  $m_\chi < 250$  GeV
  - b) via cascade decay chains
- Parameter determinations: in specific SUSY breaking models

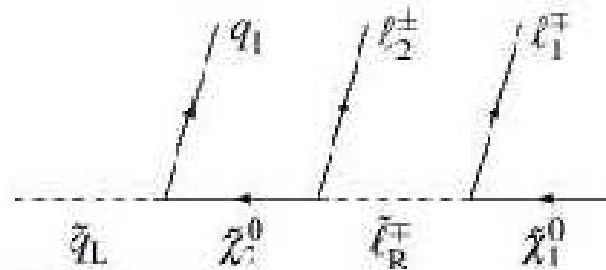
- Particularly promising field for LHC/ILC interplay studies !



# SUSY mass determinations at the LHC

Analysis of cascade decays:

$$\bar{q}_L \rightarrow q\tilde{\chi}_2^0 \rightarrow \ell_2^\pm \bar{\ell}^\mp \rightarrow \ell_1^\mp \tilde{\chi}_1^0$$



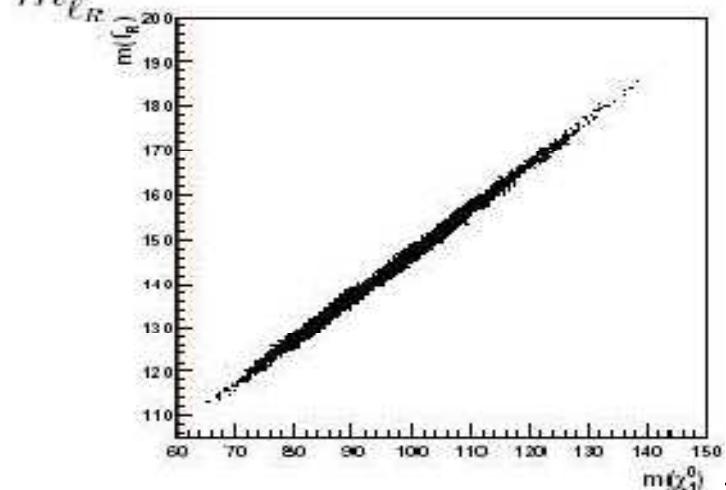
⇒ Mass determination from kinematical endpoints

invariant mass distribution:

$$m_{\ell\ell}^{\max} \sim \sqrt{\frac{(m_{\tilde{\chi}_2^0}^2 - m_\ell^2)(m_\ell^2 - m_{\tilde{\chi}_1^0}^2)}{m_\ell^2}}$$

⇒ Difference of masses are measured

⇒ strong dependence on the LSP mass:



# SUSY mass measurement im continuum

- To optimize threshold scans: precise continuum measurements important!
- Worst SM background is WW-pair production

⇒ e.g.  $e^+e^- \rightarrow \tilde{\mu}_{L,R}^+\tilde{\mu}_{L,R}^-$

Muon energy spectrum:  $\mu^+\mu^-$  events (incl.  $W^+W^-$ ) at  $\sqrt{s} = 750$  GeV

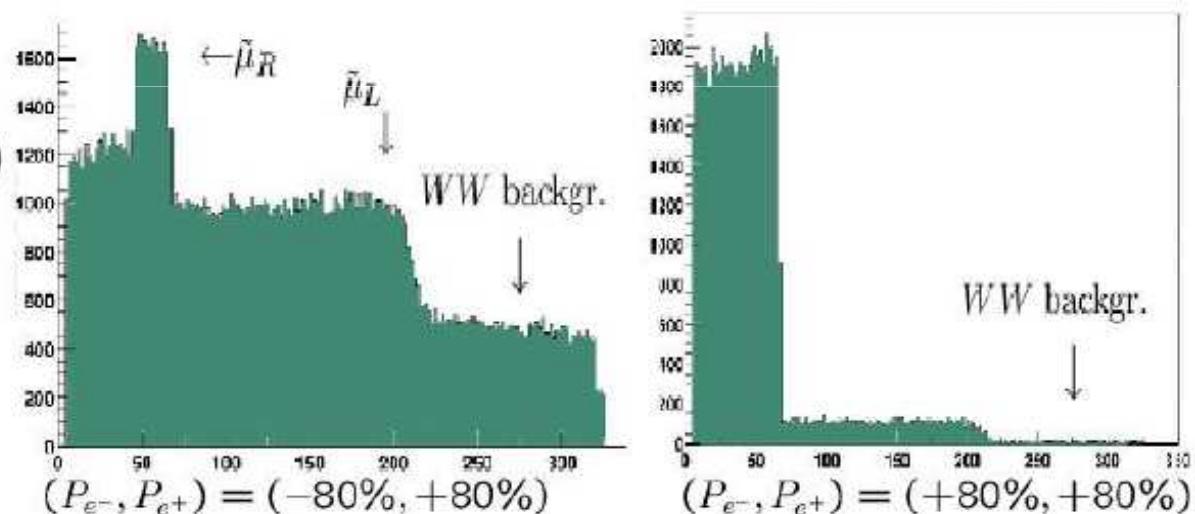
- Strong WW-backgr.:

⇒ all edges observable  
only with  $P(e^-)$  and  $P(e^+)$

⇒ at 65 GeV and 220 GeV

$S/B = 0.07 (+80\%, 0)$

$S/B = 0.46 (+80\%, -80\%)$



- $\Delta(m_{\tilde{\mu}_{L,R}}) \sim \text{few GeV if both beams are polarized!}$

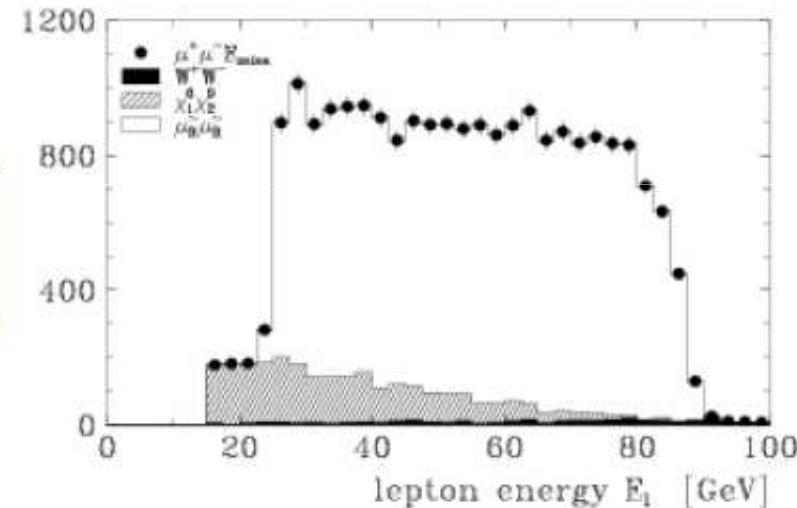
# *Mass measurement of the LSP mass*

- A promising cold dark matter candidate = lightest SUSY particle (LSP)

→ in many scenarios:  $\tilde{\chi}_1^0$

→ excellent mass resolution e.g. in slepton decays  $\tilde{\mu}_R \tilde{\mu}_R \rightarrow \mu \mu \tilde{\chi}_1^0 \tilde{\chi}_1^0$

→  $\Delta m \tilde{\chi}_1^0$  up to 0.3%, here 100 MeV!



- Further improvement in mass measurements via threshold scans possible !
  - costs luminosity, therefore should be optimized via excellent measurements in the continuum

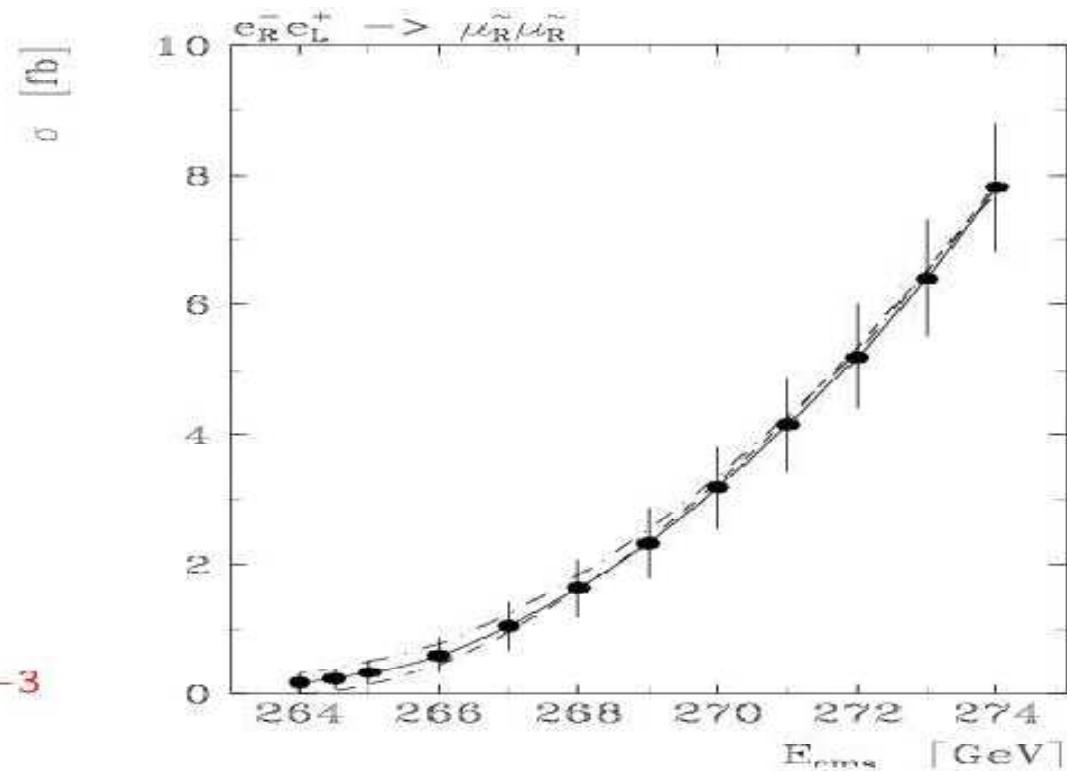
# *Test off spin quantum number at ILC*

- Clean signatures, known initial state, tunable energy:

Determination of mass and spin of  $\tilde{\mu}_R$  from production at threshold:

[TESLA TDR '01]

$$\Rightarrow \frac{\Delta m_{\tilde{\mu}_R}}{m_{\tilde{\mu}_R}} < 1 \times 10^{-3}$$



⇒ test of  $J = 0$  hypothesis

DESY Summer Program 2009

g.a.moortgat-pick@durham.ac.uk

Gudrid Moortgat-Pick

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# One more SUSY Test at the ILC

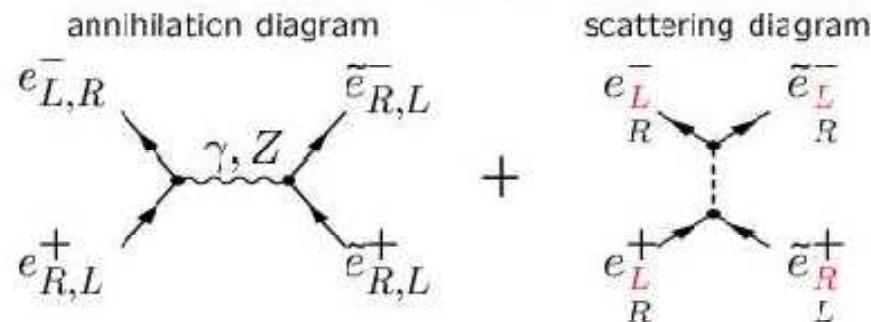
Test of SUSY assumption: SM  $\leftrightarrow$  SUSY have same quantum numbers!

$$\Rightarrow e_{L,R}^- \leftrightarrow \tilde{e}_{L,R}^- \quad \text{and} \quad e_{L,R}^+ \leftrightarrow \tilde{e}_{R,L}^+$$

Scalar partners  $\leftrightarrow$  chiral quantum numbers!

How to test this association?

Strategy:  $\sigma(e^+e^- \rightarrow \tilde{e}_{L,R}^+ \tilde{e}_{L,R}^-)$  with polarised beams



$\Rightarrow$  2nd diagram: unique relation between chiral fermion  $\longleftrightarrow$  scalar partner

$$\rightarrow \text{scattering diagram: } \tilde{e}_R^+ \tilde{e}_L^- \longrightarrow \tilde{e}_R^+ \leftrightarrow \tilde{e}_L^-$$

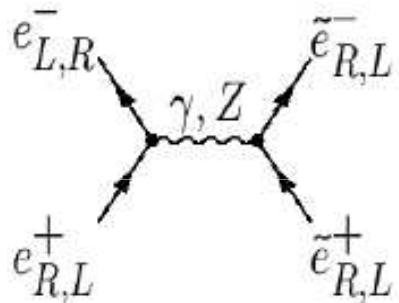
Use e.g.  $e_L^+ e_L^-$

$\rightarrow$  no annihilation diagram

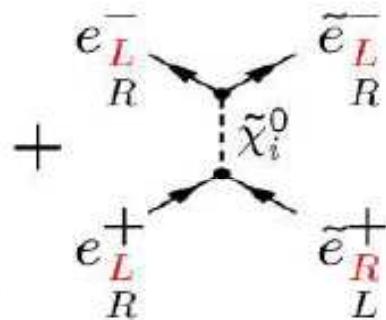
# Chiral quantum numbers, 2

- Association of chiral electrons to scalar partners  $e_{L,R}^- \leftrightarrow \tilde{e}_{L,R}^-$  and  $e_{L,R}^+ \leftrightarrow \tilde{e}_{R,L}^+$ :

s-channel

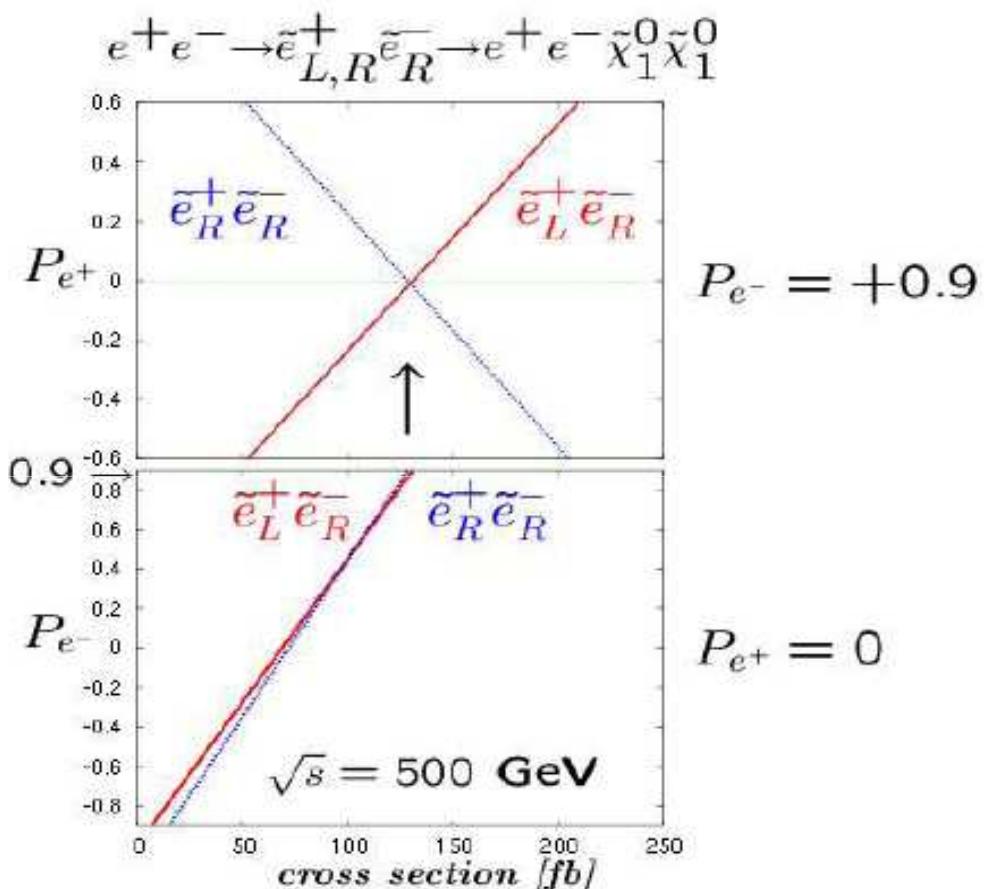


t-channel



- separation of scattering versus annihilation channel

- test of 'chirality': only  $\tilde{e}_L^+ \tilde{e}_R^-$  may survive at  $P(e^-) > 0$  and  $P(e^+) > 0$ !

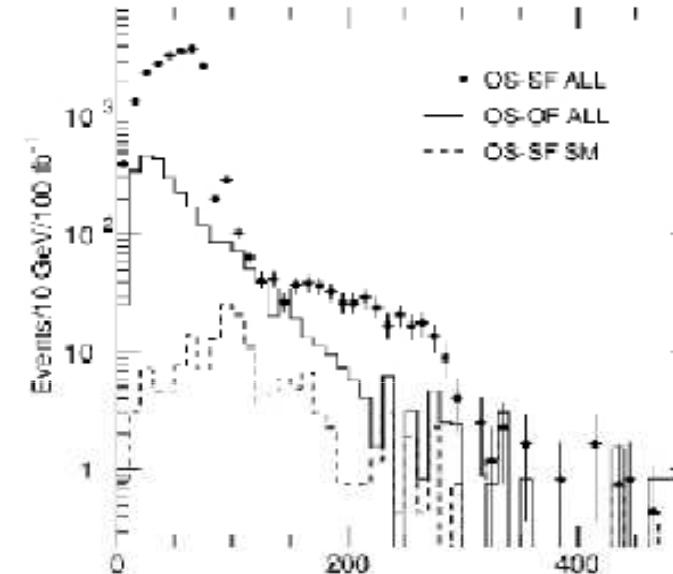


- Even high  $P(e^-)$  not sufficient,  $P(e^+)$  is substantial!**

# LHC/ILC interplay

- If fundamental parameters determined: allows mass predictions for heavier particles

- significant increase of sensitivity for searches at the LHC and unique identification of particles in decay chain
- powerful test of the model and distinction between e.g. MSSM vs. NMSSM model!



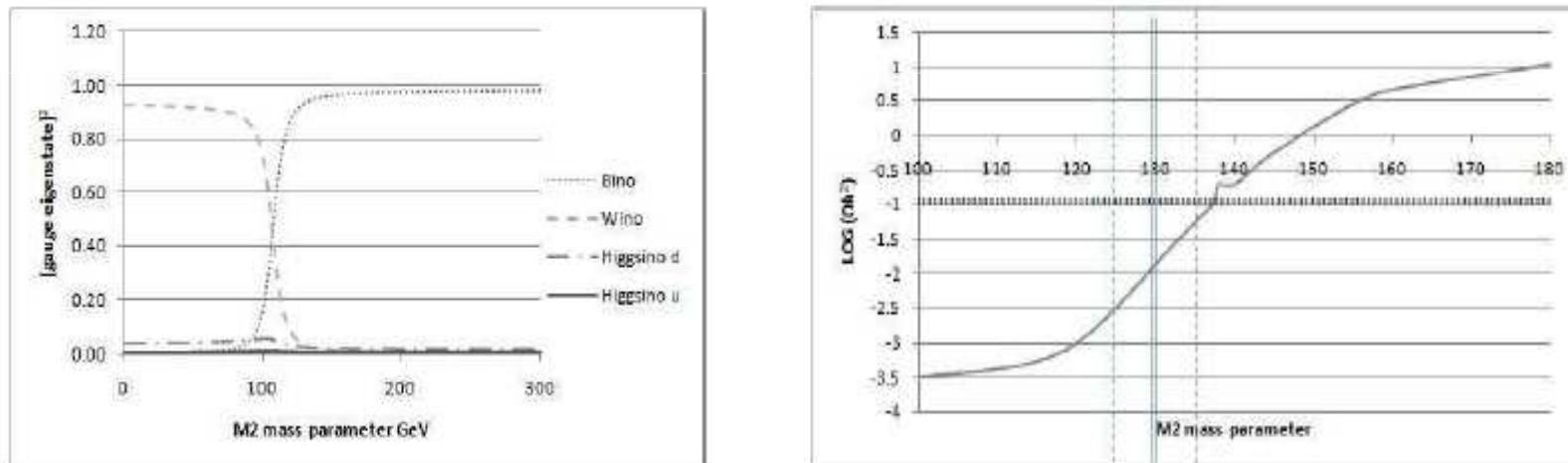
	$M_1$	$M_2$	$\mu$	$\tan \beta$
input	99.1	192.7	352.4	10
LC <sub>500</sub>	$99.1 \pm 0.2$	$192.7 \pm 0.6$	$352.8 \pm 8.9$	$10.3 \pm 1.5$
LHC+LC <sub>500</sub>	$99.1 \pm 0.1$	$192.7 \pm 0.3$	$352.4 \pm 2.1$	$10.2 \pm 0.6$

- strong improvement in parameter determination via LHC/ILC interplay!

# *Dark matter analysis at LC*

- **High precision in parameter determination required for reliable DM prediction**
  - Parameter ranges where abrupt changes of neutralino character happen

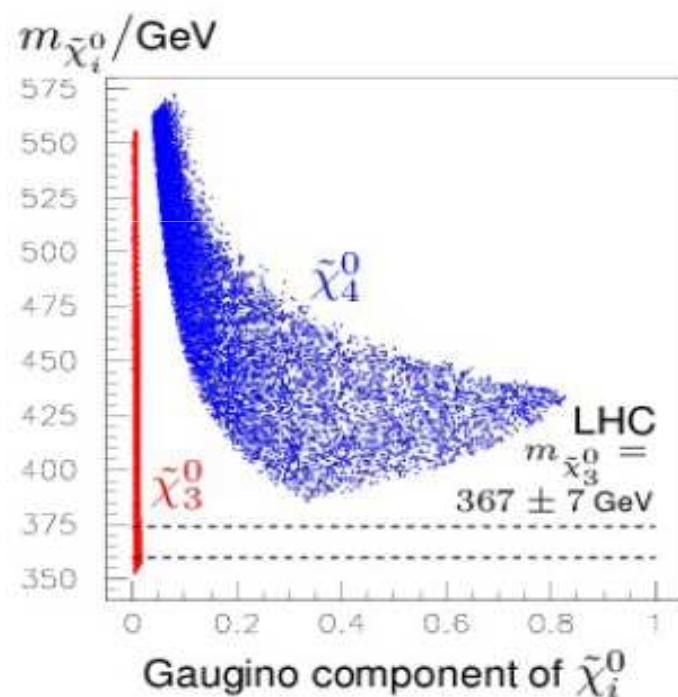
V. Morton-Thurtle



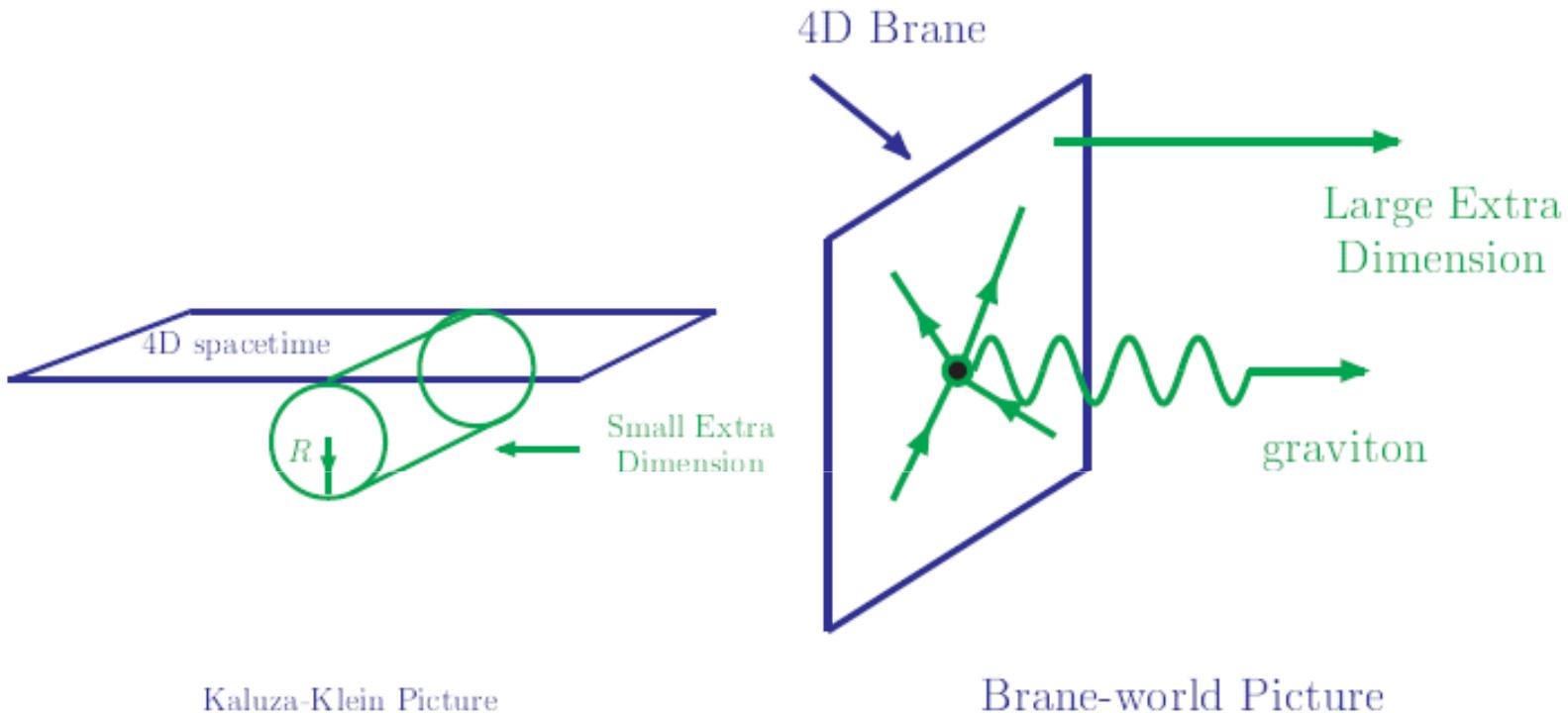
- Precise determination of  $M_1, M_2, \dots$  required

# *SUSY model distinction*

- SUSY scenario in the NMSSM: Higgs and light particle sector (neutralino / chargino) show no hints for model distinction
- measured at ILC (500 GeV):  $m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_{1,2}^0}, \sigma(e^+e^- \rightarrow \tilde{\chi}_1^+\tilde{\chi}_1^-, \tilde{\chi}_1^0\tilde{\chi}_2^0)$ 
  - Consistent within MSSM-analysis
  - Predictions:
    - $m_{\tilde{\chi}_3^0} = [352, 555]$  GeV  $\rightarrow$  pure higgsino
    - $m_{\tilde{\chi}_4^0} = [386, 573]$  GeV  $\rightarrow$  larger gaugino comp.
    - $m_{\tilde{\chi}_2^\pm} = [450, 600]$  GeV
  - $\Rightarrow \tilde{\chi}_3^0$  not accessible at LHC
  - However:  $\tilde{\chi}_3^0$  in underlying NMSSM scenario has large gaugino component
  - $\rightarrow$  visible at LHC  $\rightarrow$  inconsistency
- Model inconsistency determined via LHC/ILC



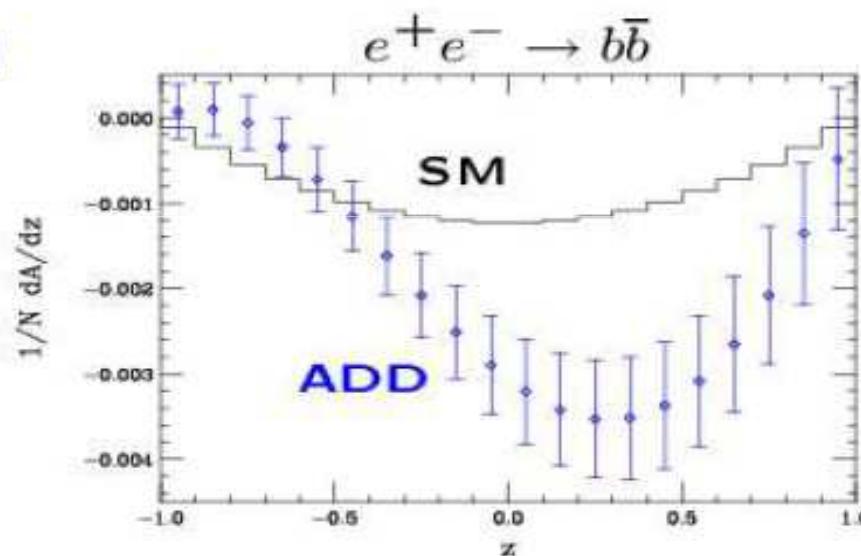
# *Indirect searches: extra dimensions*



Hierarchy between  $M_{\text{Planck}}$  and  $M_{\text{weak}}$  is related to the volume or the geometrical structure of additional dimensions of space  
⇒ observable effects at the TeV scale

# *Extra dimensions*

- Models with extra dimension allow also to solve the hierarchy problem
- Transversely polarized beams (only effects detectable with  $P(e^-) \times P(e^+)$  !)**
  - enables to exploit azimuthal asymmetries in fermion production !
- Distinction between SM and different models of extra dimension:**
  - asymmetry signals contribution from spin-2 graviton



→ Detect new kind of physics even if new scale is in the multi-TeV range, but transversely polarized beams need polarized  $e^-$  and  $e^+$  !

# *EW precision measurements*

- **GigaZ option at the ILC:**
  - high-lumi running on Z-pole/WW
  - $10^9$  Z in 50-100 days of running
  - Needs machine changes (bypass in the current outline)
- **High precision needs polarized beams**
- **Provides measurement of  $\sin^2\theta_W$  with unprecedented precision!**

# *Electroweak precision tests*

## Electroweak precision measurements:

$M_Z$ [GeV]	$= 91.1875 \pm 0.0021$	0.002%
$G_\mu$ [GeV $^{-2}$ ]	$= 1.16637(1) 10^{-5}$	0.0009%
$m_t$ [GeV]	$= 178.0 \pm 4.3$	2.4%
$M_W$ [GeV]	$= 80.426 \pm 0.034$	0.04%
$\sin^2 \theta_{\text{eff}}^{\text{lept}}$	$= 0.23150 \pm 0.00016$	0.07%
$\Gamma_Z$ [GeV]	$= 2.4952 \pm 0.0023$	0.09%

...

## Quantum effects of the theory: loop corrections: $\sim \mathcal{O}(1\%)$

SM:  $M_H$  is free parameter

precise measurement of  $M_W$ ,  $\sin^2 \theta_{\text{eff}}$ , ...  $\Rightarrow$  constraints on  $M_H$

MSSM:  $m_h$  is predicted

precise meas. of  $M_W$ ,  $\sin^2 \theta_{\text{eff}}$ ,  $m_h$ , ...  $\Rightarrow$  constr. on  $m_t$ ,  $\theta_t$ ,  $m_b$ ,  $\theta_b$ , ...

# *Electroweak precision test 2*

Comparison of ew precision data with theory:

EW precision data:

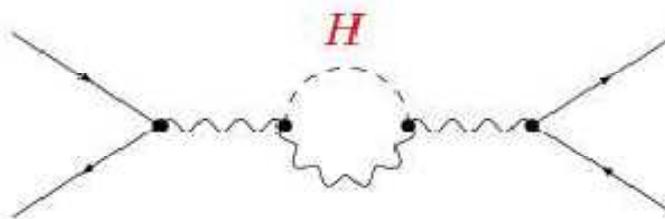
$M_Z, M_W, \sin^2 \theta_{\text{eff}}^{\text{lept}}, \dots$

Theory:

SM, MSSM, ...



Test of theory at quantum level:



Improve indirect constraints on unknown parameters:  $M_H, m_{\tilde{t}}, \dots$

# Blondel scheme for GigaZ

- Measurement of  $\sin^2 \theta_{\text{eff}}$  in  $e^+ e^- \rightarrow Z \rightarrow f\bar{f}$ :

usually  $\Delta P/P \sim 0.5\%$  sufficient  
 (maybe  $\Delta P/P \sim 0.25\%$  reachable !)

$$A_{LR} = \frac{2(1 - 4 \sin^2 \Theta_{\text{eff}}^\ell)}{1 + (1 - 4 \sin^2 \Theta_{\text{eff}}^\ell)^2}$$

$$\text{Blondel} = \sqrt{\frac{(\sigma^{RR} + \sigma^{RL} - \sigma^{LR} - \sigma^{LL})(-\sigma^{RR} + \sigma^{RL} - \sigma^{LR} + \sigma^{LL})}{(\sigma^{RR} + \sigma^{RL} + \sigma^{LR} + \sigma^{LL})(-\sigma^{RR} + \sigma^{RL} + \sigma^{LR} - \sigma^{LL})}}$$

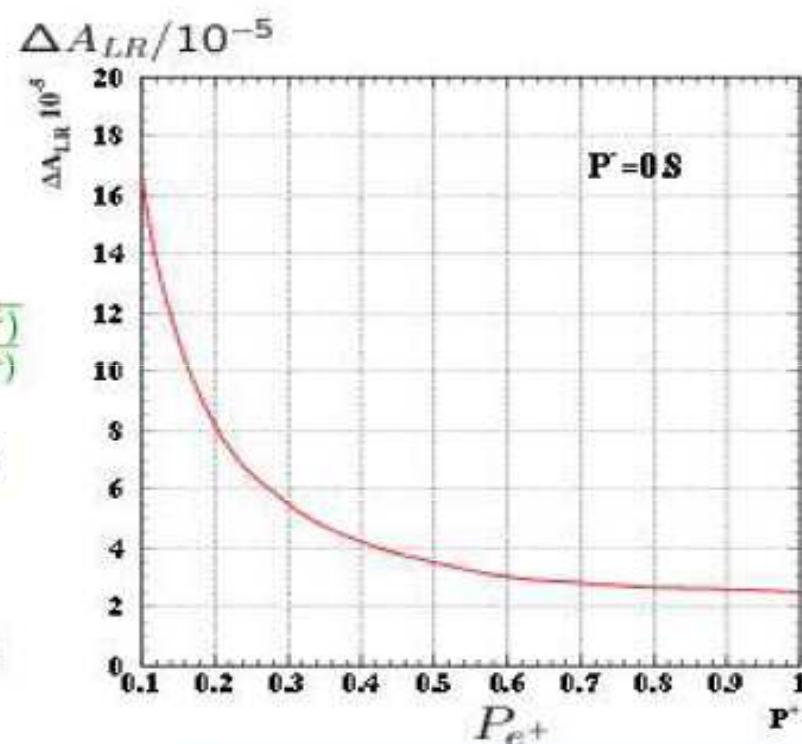
- with  $\Delta P/P \sim 0.5\%$  and  $P(e^-) = 80\%$  only:

$$\Rightarrow \Delta \sin^2 \theta_{\text{eff}}^\ell = 9.5 \times 10^{-5}$$

- with  $\Delta P/P = 0.25\%$  and  $P_{e^-} = 90\%$ :

$$\Rightarrow \Delta \sin^2 \theta_{\text{eff}}^\ell = 5 \times 10^{-5}$$

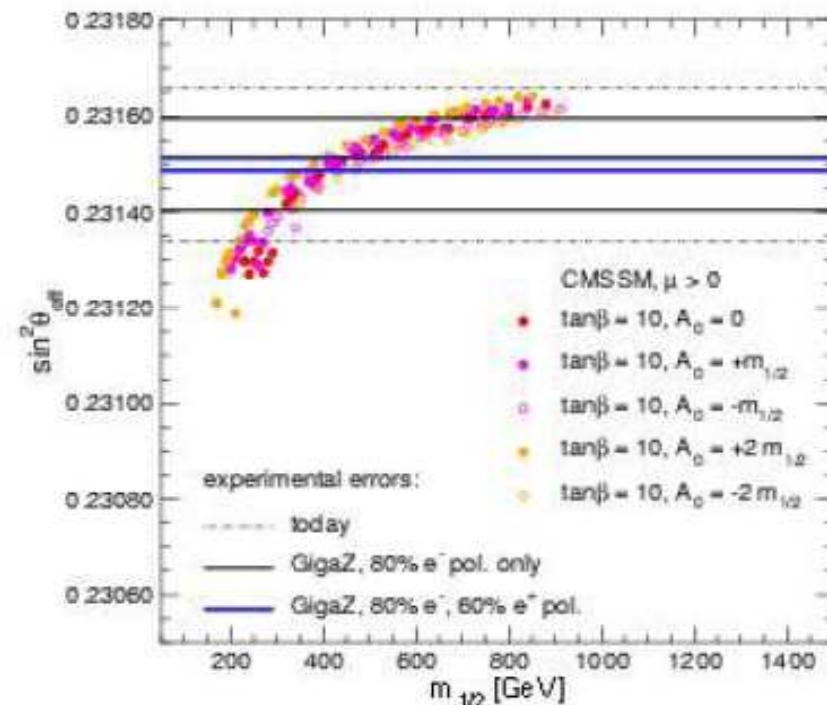
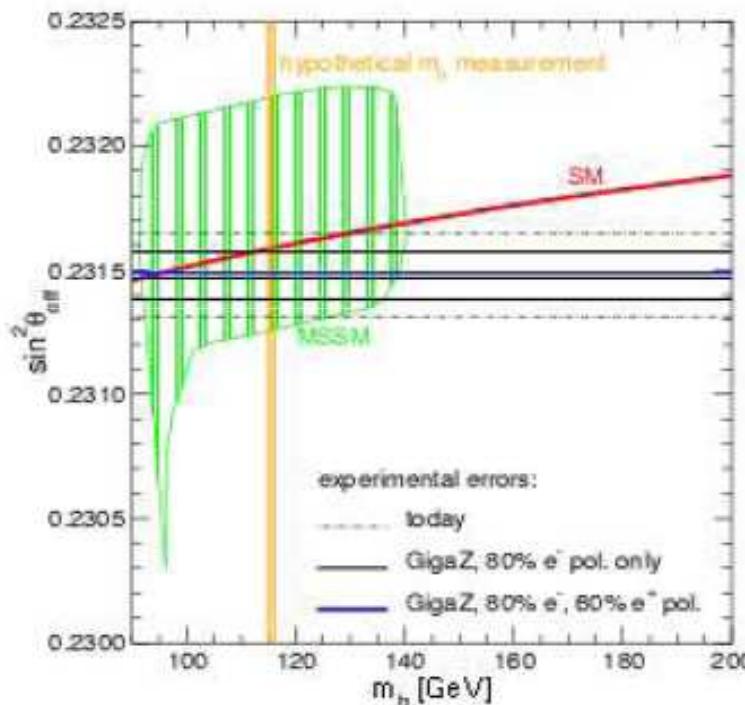
- with Blondel scheme:  $[P(e^-), P(e^+)] = [80\%, 60\%]$  :  $\Rightarrow \Delta \sin^2 \theta_{\text{eff}}^\ell = 1.3 \times 10^{-5}$



# SUSY Constraints from GigaZ

- Gain of about one order of magnitude in  $\sin^2\theta_{\text{eff}}$ :

→ Prediction / constraints for  $m_h$  and  $m_{1/2}$



- 'Gain' of P(e+): bounds on SM  $m_H$  ~ order of magnitude, on  $m_{1/2}$  ~ factor 5!

# *Physics up to 1 TeV*

- **Top couplings**

- improvement of top Yukawa couplings
- higher cross sections (depends on Higgs mass)
- **couplings up to 5% !**

- **Direct search for SUSY particles**

- high probability for access to almost the full gaugino/higgsino SUSY spectrum
- **powerful consistency tests and model determination**

- **Extrapolation of masses and gauge couplings to high scales**

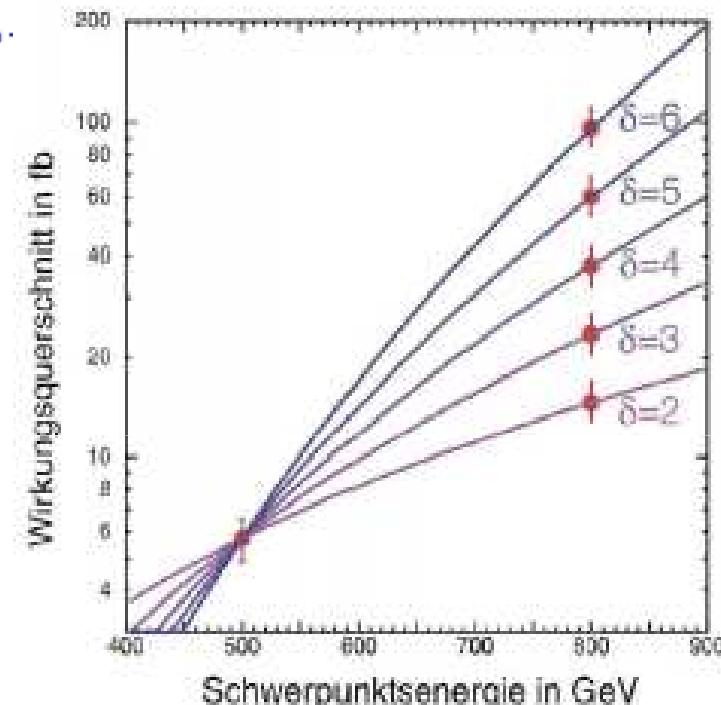
- consistency tests for the **underlying SUSY breaking scheme**
- **consistency check for gauge unification**

- **Direct search for extra dimensions**

# *Direct search for extra dimensions*

## ● Direct search for gravitons in the process $e^+e^-$

- measuring the cross sections at **two different cms energies**, allows to **determine the number of extra dim !**
- ILC with polarized beams exceeds / complements discovery region of LHC



## ● serious background from $\gamma\gamma\nu\nu$ , similar behaviour

- polarized  $e^-$  and  $e^+$  **essential for background suppression**
- $(Pe^-, Pe^+) = (+80\%, +60\%) / (+80\%, 0)$  : suppresses B by factor 2, enhances S by 1.5

# *Multi-TeV option at CLIC - Higgs*

- Needed scale and physics case for the multi-TeV option depends on results at LHC and ILC
- Improvement in all sectors (direct and indirect searches) if
  - same precision available as at ILC
  - beamstrahlung fully under control
- Triple Higgs couplings: improvement by about a factor 2
  - enhancement of cross sections of WW-fusion process
  - uncertainty of **triple Higgs couplings up to 13%**
  - **important for further understanding of the electroweak symmetry mechanism !**

# *Summary*

- e+e- physics has been *the core of high precision physics* over the last decade
- Results from LEP, SLD, B-factories provide *tests of the SM at quantum level!*
- We expect a fascinating future in the next years:  
*LHC will shed first light on* the mysteries of *EW symmetry breaking*
- Rich program and high physics potential of the  
*ILC will unravel the new physics and enter a new precision frontier!*

***Stay tuned for the LHC and ILC!***

## *Some literature*

- ILC physics: *TESLA TDR, physics part hep-ph/0106315*  
*ILC RDR, arXiv:0712.1950*
- LHC/ILC interplay:  
*G. Weiglein, Phys. Rept. 426, 47 (2006), hep-ph/0410364*
- Supersymmetry: introduction  
*M. Drees, hep-ph/9611409, S. Martin, hep-ph/9709356*
- Polarization+Spin:  
*GMP, POWER report, Phys. Rept. 460, 131 (2008), hep-ph/0507011*  
*webpage: [www.ippp.dur.ac.uk/LCsources](http://www.ippp.dur.ac.uk/LCsources)*

# *Ex: Harmonic oscillator in SUSY*

## • **Harmonic oscillator in SUSY:**

- a) **Choose:**  $\hbar = c = \omega = \dots = 1$

**We have:**  $[q, p] = i, \quad a = \frac{1}{\sqrt{2}}(q + ip), \quad a^+ = \frac{1}{\sqrt{2}}(q - ip), \quad [a, a^+] = 1$

**Eigenstates In>:**  $a |n\rangle = \sqrt{n} |n-1\rangle, \quad a^+ |n\rangle = \sqrt{n+1} |n+1\rangle$

**Everything bosonic:**  $N_B = a^+ a, \quad H_B = \frac{1}{2}(p^2 + q^2) = ?$

**What gives**  $[N_B, a], [N_B, a^+], N_B |n\rangle$  **and**  $H_B |n\rangle$  ?

- b) **Now two-state system (as  $|S^2, S_z\rangle$ ):**  $\left| \frac{1}{2}, +\frac{1}{2} \right\rangle = |+\rangle, \quad \left| \frac{1}{2}, -\frac{1}{2} \right\rangle = |-\rangle$

**What's the algebra?**

**Define with**  $S_{\pm} = S_x \pm iS_y$  **a fermionic generator+annihilation operators:**

$$d^+ := S_+, \quad d := S_-$$

**What's the (anti-commuting) algebra of  $d^+$  and  $d$ ?**

**Define:**  $N_F = d^+ d, \quad H_F = S_z = ?$  **What happens if**  $d^+, d, N_F$  **act on**  $|+\rangle, |-\rangle$  ?

# *Harmonic Oscillator II*

– c) Couple fermionic with bosonic system:  $H := H_B + H_F = ?$

**States are:**  $|n,+\rangle = |n\rangle \otimes |+\rangle$ ,  $|n,-\rangle = |n\rangle \otimes |-\rangle$

**How is the spectrum of H? What's about degeneracy?**

– d) Derive SUSY generators which fulfill:

$$Q |1,+\rangle = |2,-\rangle \quad (\text{allg.: } Q |n,+\rangle \rightarrow |n+1,-\rangle)$$

$$Q^+ |2,-\rangle = |1,+\rangle \quad (\text{allg.: } Q^+ |n+1,-\rangle \rightarrow |n,+\rangle)$$

**What's about  $Q, Q^+$ ? Calculate  $[N_{B,F}, Q^{(+)})]$ .**

**What is  $\{Q^{(+)}, Q^{(+)}\}$ ,  $[H, Q^{(+)})]$ ?**

**And what are the eigenvalues of the energy?**