

# An Introduction to HERA Physics

DESY Summer Student Program  
23 August, 2005  
Tobias Haas  
DESY, Hamburg

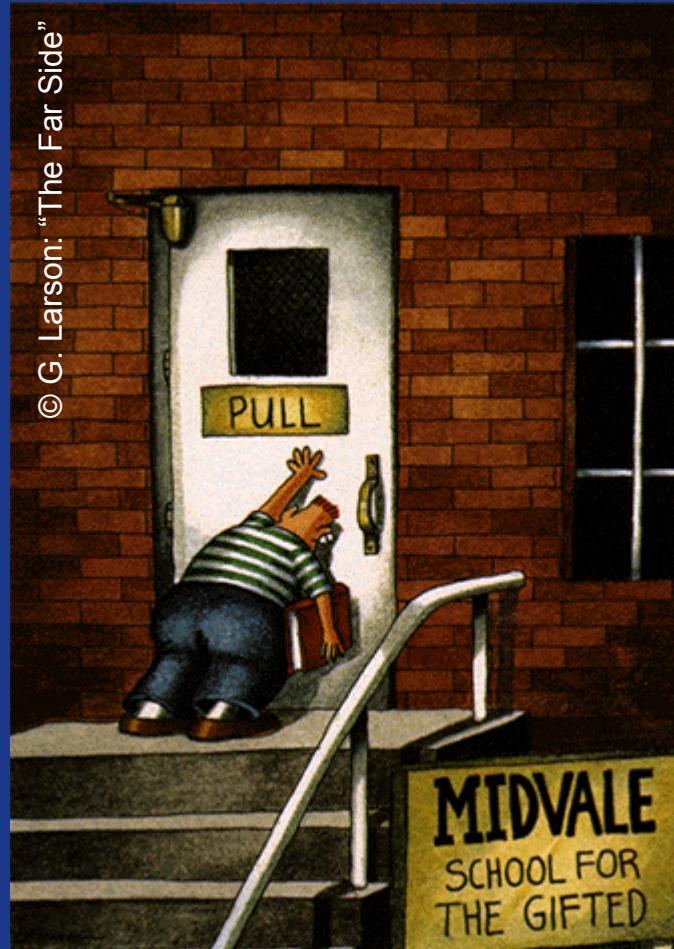
# Overview

## Part 1:

- What is HERA?
- Kinematics
- Structure Functions and QCD evolution

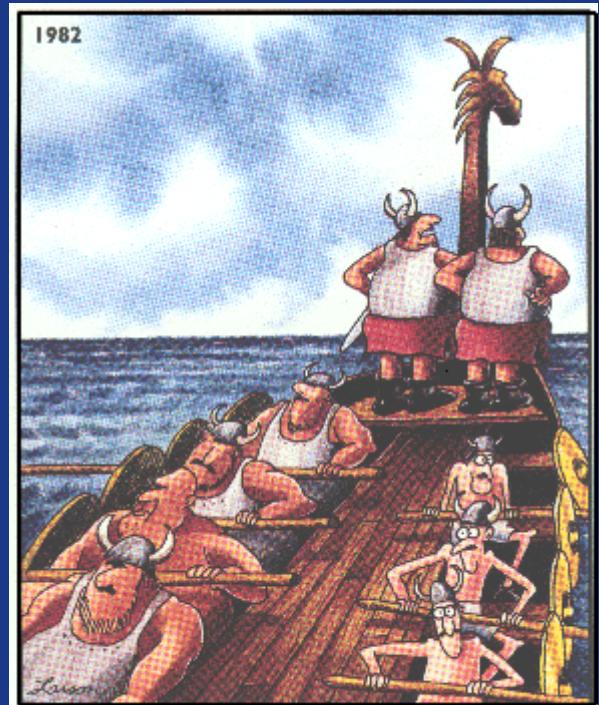
## Part 2:

- Selected HERA Results:
  - Structure Functions
  - High  $Q^2$  and EW precision measurements
  - Jets and the strong coupling  $\alpha_s$
  - Exotics (Pentaquarks et al...)



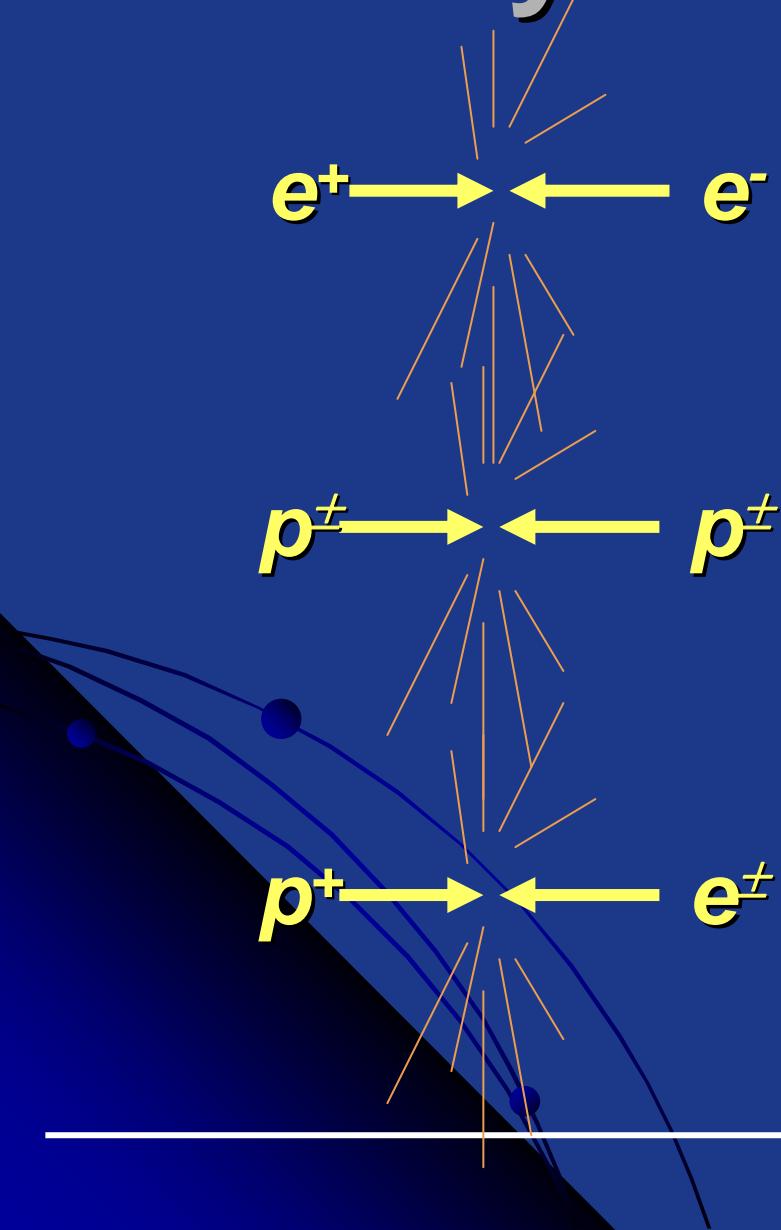
# Part 1

# What is HERA?



Tobias Haas: Introduction to HERA

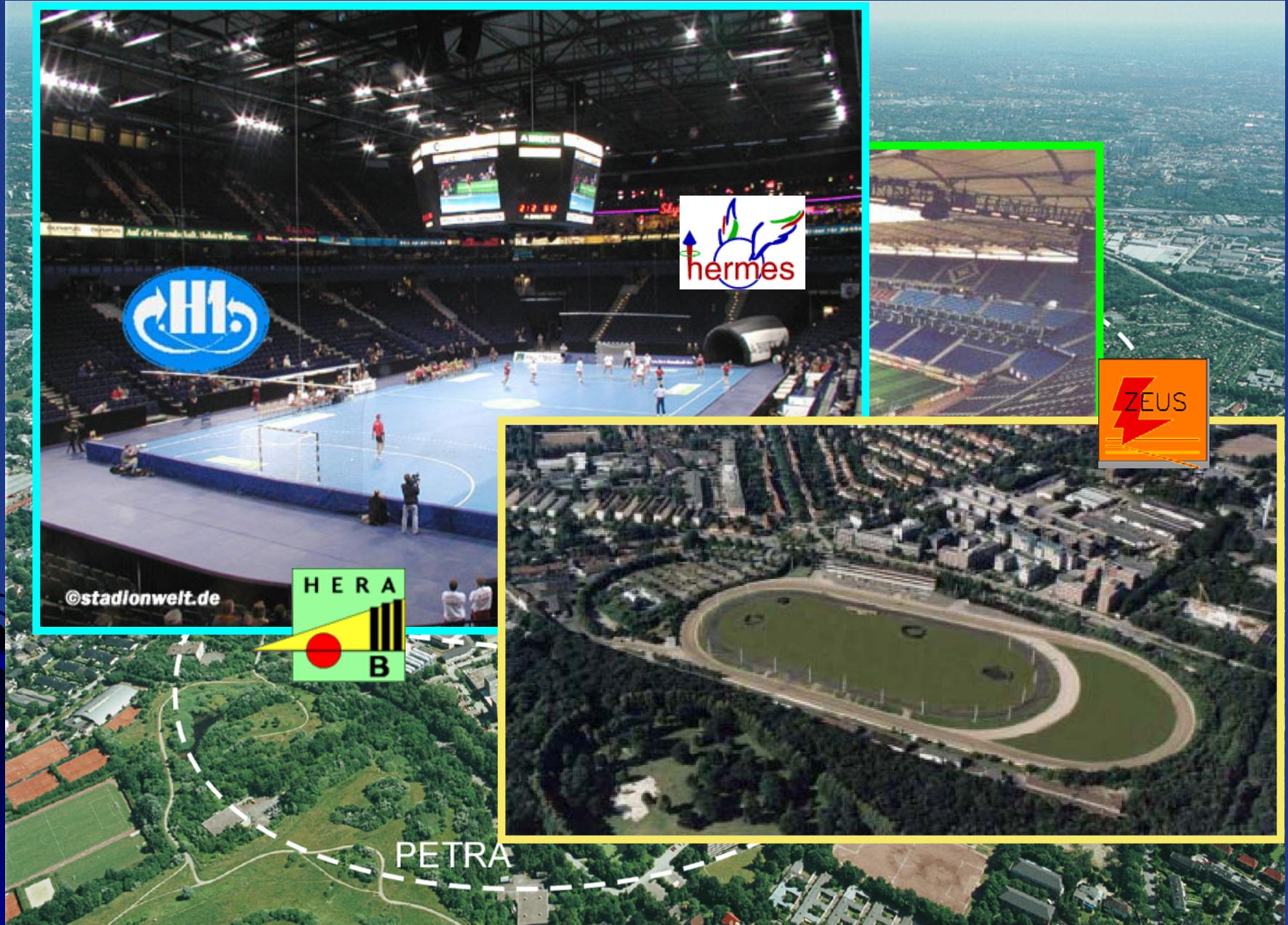
# Physics @ Colliders



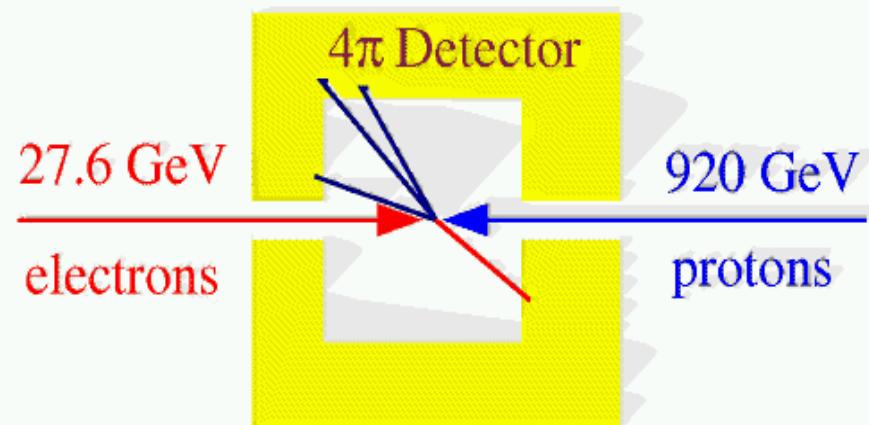
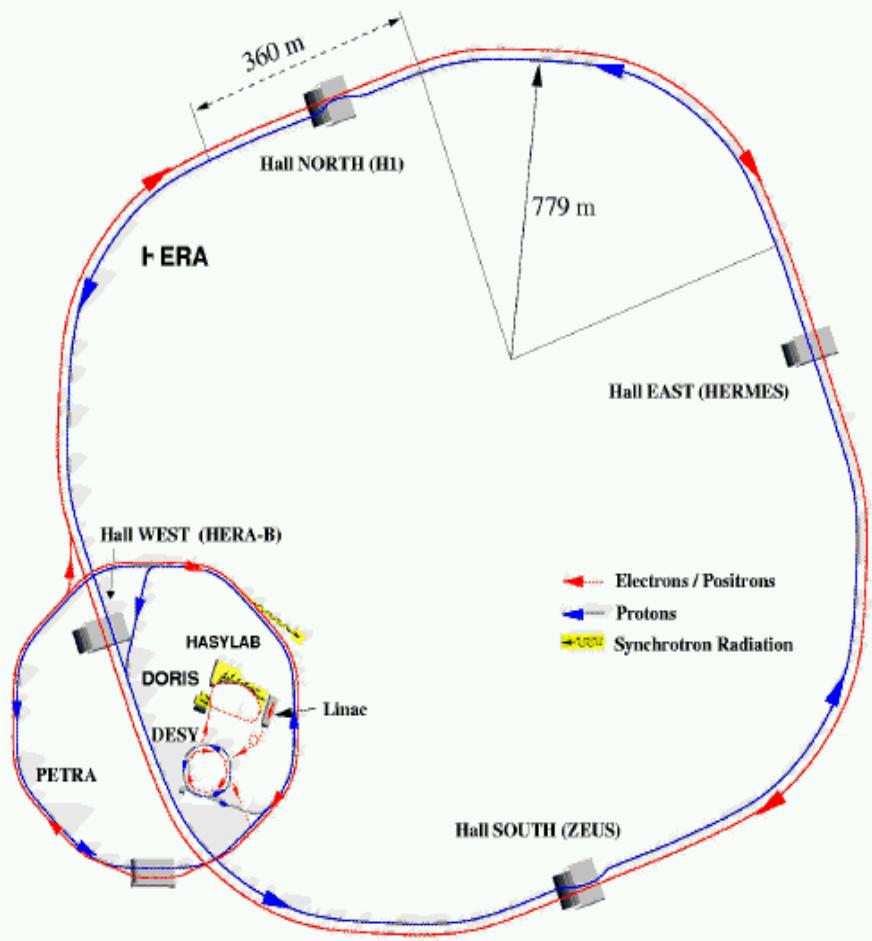
- + Simple initial state
- + Clean final states
- + Little background
- Limited energy
  - e.g. LEP(200 GeV), ILC(1 TeV)

- + High energy (no synch rad)
- Complicated initial state
- Large and complicated backgrounds
- e.g. TEVATRON(2 TeV), LHC(14 TeV)

- + Unique initial state
- two accelerators
- HERA (300 GeV)

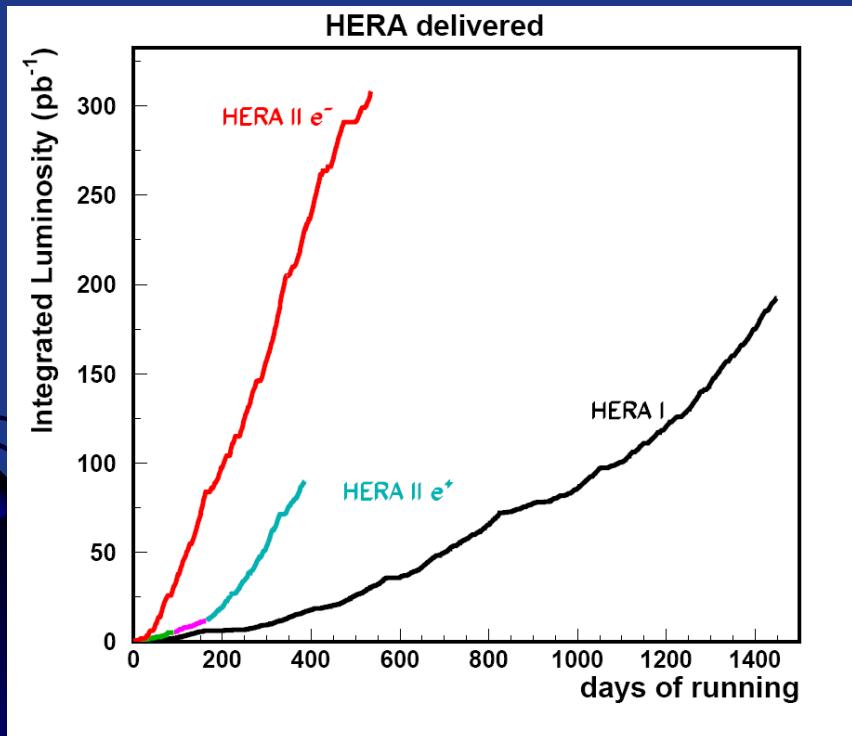


# HERA: The only $ep$ Collider on the Planet



$$\sqrt{s} \approx 320 \text{ GeV}$$

# HERA



## ● Highlights:

- Started operation in 1992
- 4 Experiments:
  - H1 and ZEUS (ep)
  - HERMES (e)
  - HERA-B (p) (until 2003)
- $\sqrt{s} = 300 \text{ GeV} (\rightarrow 1997)$
- $\sqrt{s} = 318 \text{ GeV} (1998 \rightarrow )$
- $e^+$  and  $e^-$  beams
- up to 60% lepton polarization
- > 600 Mio ep collisions recorded per experiment

# Physics Topics of HERA

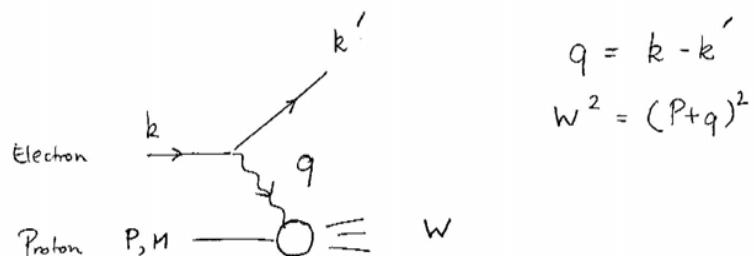
- Proton Structure
  - Parton densities
    - gluon density ( $xg(x)$ )
    - Valence quark distributions
  - QCD evolution
  - Different evolution schemes (e.g. BFKL)
  - Strangeness and charm
  - $\alpha_s$
- Perturbative QCD
  - Jets
    - Gluon density
    - $\alpha_s$
  - Multiparticle Observables:
    - Multiplicity distributions
    - Event shapes
    - Multiparticle Correlations
- Border between pQCD and non-perturbative QCD
- Photon Structure
- Diffraction
- EW
- BSM and Exotics
  - Leptoquarks
  - Excited Quarks and Fermions
  - FCNC
  - MSSM Searches
  - R-parity violation SUSY
  - Contact Interactions
  - ...
- Spectroscopy

# Kinematics

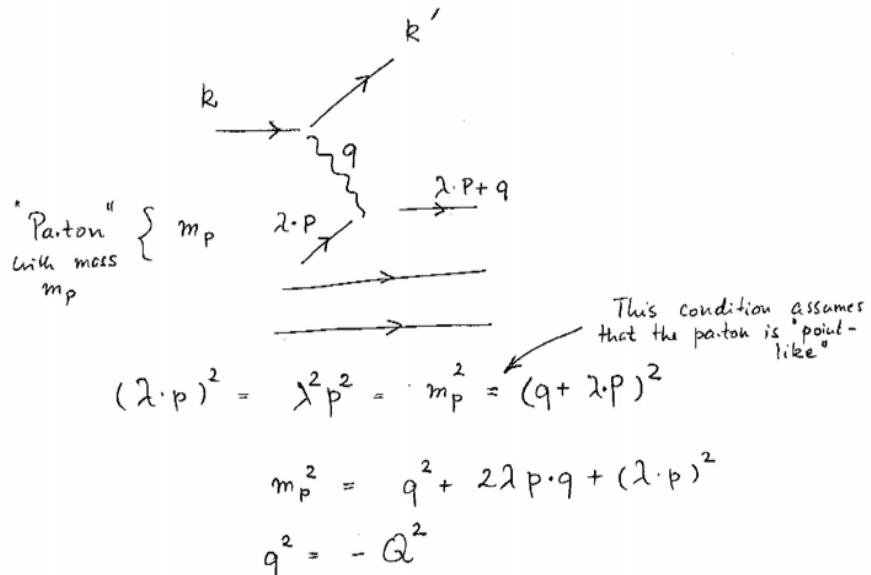


© Gary Larson, The Far Side

## Kinematics of Deep Inelastic Scattering:



We want to view this process like this



Note: Since  $q$  is space-like ( $q^2 < 0$ ) we choose a positive quantity  $Q^2 = -q^2$

$$m_p^2 = -Q^2 + 2\lambda p \cdot q + m_p^2$$

$$\Rightarrow \lambda = \frac{Q^2}{2 p \cdot q}$$

This quantity  $\lambda$  is the fractional momentum of a parton inside the proton. We call this quantity  $x_{Bj}$

Note that with these two Lorentz-invariant quantities ( $x_{Bj}, Q^2$ ) the "inclusive" scattering process is completely described.

Properties of  $x$  and  $Q^2$ : go to the proton rest frame: metric:  $g = \begin{pmatrix} 1 & -1 & -1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$

$$P = \begin{pmatrix} M_p \\ 0 \\ 0 \\ 0 \end{pmatrix}, \quad k = \begin{pmatrix} E \\ 0 \\ 0 \\ E \end{pmatrix}, \quad k' = \begin{pmatrix} E' \\ 0 \\ E' \sin \theta \\ E' \cos \theta \end{pmatrix}$$

$$q = k - k' = \begin{pmatrix} E - E' \\ 0 \\ -E' \sin \theta \\ E' \cos \theta \end{pmatrix}$$

$$p \cdot q = M_p (E - E')$$

The electron loses energy to the proton, so  $E' < E \Rightarrow p \cdot q > 0$

Minimum energy loss:  $E' = E$  (ignore mass)

$$0 \leq x \leq 1$$

(3)

One more variable

$$y = \frac{P \cdot q}{P \cdot k}$$

Properties of  $y$

Proton rest frame:

$$P = \begin{pmatrix} M_p \\ 0 \\ 0 \\ 0 \end{pmatrix}; k = \begin{pmatrix} E \\ 0 \\ 0 \\ E \end{pmatrix}; k' = \begin{pmatrix} E' \\ 0 \\ +E's\sin\theta \\ E'c\cos\theta \end{pmatrix}$$

$$q = k - k' = \begin{pmatrix} E - E' \\ 0 \\ -E's\sin\theta \\ E - E'c\cos\theta \end{pmatrix}$$

$$y = \frac{P \cdot q}{P \cdot k} = \frac{M_p(E - E')}{M_p \cdot E} = \frac{E - E'}{E}$$

"Scaled momentum transfer"

$$0 \leq y \leq 1$$

$$W^2 = (P+q)^2$$

$$= P^2 + 2P \cdot q - Q^2$$

$$= M_p^2 + \frac{Q^2}{x} - Q^2$$

$\sim 0$   $\nearrow$  deep inelastic

$$W^2 = Q^2 \left( \frac{1}{x} - 1 \right)$$

At HERA where  $x$  is small ( $\sim 10^{-3}$ )

$$W^2 \sim \frac{Q^2}{x}$$

Deep inelastic means:

$$\frac{Q^2}{x} \gg M_p^2 \sim 18x^2$$

... and one more useful relationship. ④

total energy:

$$S = (P+k)^2$$

$$S = P^2 + 2P \cdot k + k^2 = m_p^2 + m_e^2$$

ignore masses

$$S = 2 \cdot P \cdot k$$

$$y \cdot x = \frac{P \cdot q}{P \cdot k} \cdot \frac{Q^2}{2P \cdot q} = \frac{Q^2}{2 \cdot P \cdot k}$$

$$P \cdot k = \frac{Q^2}{2 \cdot y \cdot x}$$

$$S = \frac{Q^2}{y \cdot x}$$

$$Q^2_{\max} \Leftrightarrow y = x = 1$$

$$Q^2_{\max} = S$$

For Hera: Calculate in lab frame

$$P = \begin{pmatrix} E_p \\ 0 \\ 0 \\ E_p \end{pmatrix} \quad k = \begin{pmatrix} E_e \\ 0 \\ 0 \\ -E_e \end{pmatrix}$$

$$E_p = 920 \text{ GeV}$$

$$S = 2 P \cdot k$$

$$= 4 E_p \cdot E_e = 101200 \text{ GeV}^2$$

$$\Rightarrow Q^2_{\max} \sim 0000 \text{ GeV}^2$$

Now we come back to inclusive deep inelastic scattering:

Cross section for deep inelastic electron-proton scattering is given by

$$\frac{d^2\sigma}{dx dy} = \frac{4\pi\alpha^2 s}{Q^4} \left( (1-y) F_2(x, Q^2) + xy F_1(x, Q^2) \right)$$

I shall not derive this result but a simple motivation is given in my slides which will be on the web.

Note: Details of the proton internal structure are hidden in  $F_2$  and  $F_1$

$\Rightarrow$  Structure functions

In general  $F_1$  and  $F_2$  depend on  $x$  and  $Q^2$

If you assume that there is  
in coherent scattering on constituent quarks  
in the proton

$\Rightarrow F_1, F_2$  do not depend on  $Q^2$

$\Rightarrow$  Scaling

Crucial observation at SLAC 1969

### Interpretation:

$Q^2$  corresponds to the resolution according  
to the Heisenberg uncertainty principle

$$\Delta x \cdot \Delta p \geq \hbar$$

Something which shows no structure (independent  
of the resolution) must be pointlike.

At Hera.  $Q^2_{\text{max}} = 100\,000 \text{ GeV}^2$

$$\Rightarrow \Delta Q \sim 300 \text{ GeV}/c$$

$$\Delta x \sim 200 \text{ MeV fm}$$

$$\Delta x \gtrsim \frac{200 \text{ MeV fm}}{300 \text{ GeV}} \sim 10^{-3} \text{ fm}$$

Proton radius 0.8 fm.

(6)

$\Rightarrow$  HERA can check the size of  
the proton's constituents down to  
 $1/1000$  of the proton size:  
 $\sim 10^{-18} \text{ m}$ .

### Remark on $F_1$ :

$F_1$ : related to the scattering on the  
magnetic moment.

For Spin  $1/2$  parton  $F_2(x) = 2x F_1(x)$   
"Callan-Frog" relation.

For spin  $0$  parton:  $F_1(x) = 0$

### $F_2$ and parton content:

$x F_2$  is the density of partons in momentum  
space:

$$F_2(x) = \sum_{i \text{ quark species.}} e_i^2 (q_i(x) + \bar{q}_i(x))$$

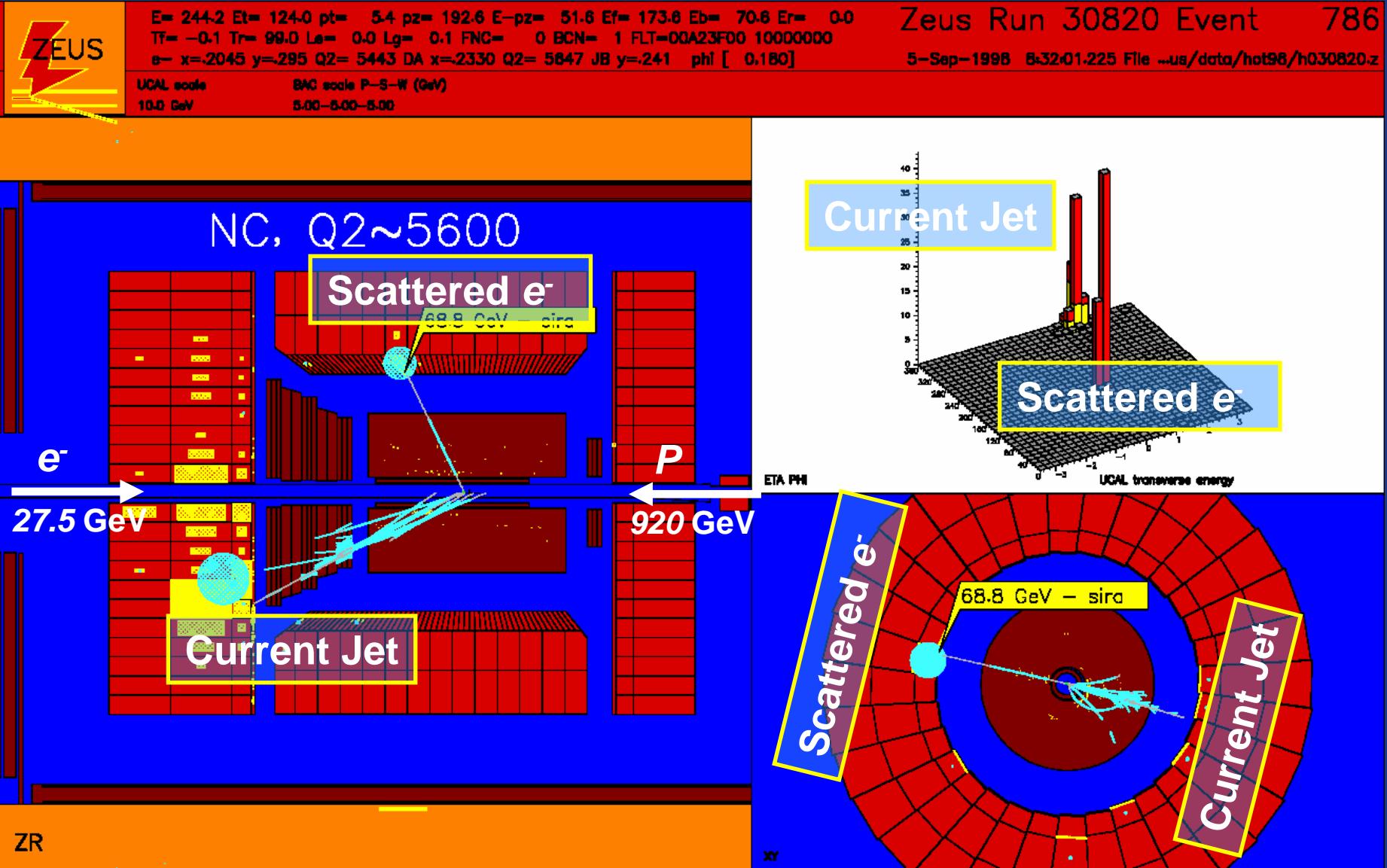
# “Bj” (aka James Daniel Bjorken)



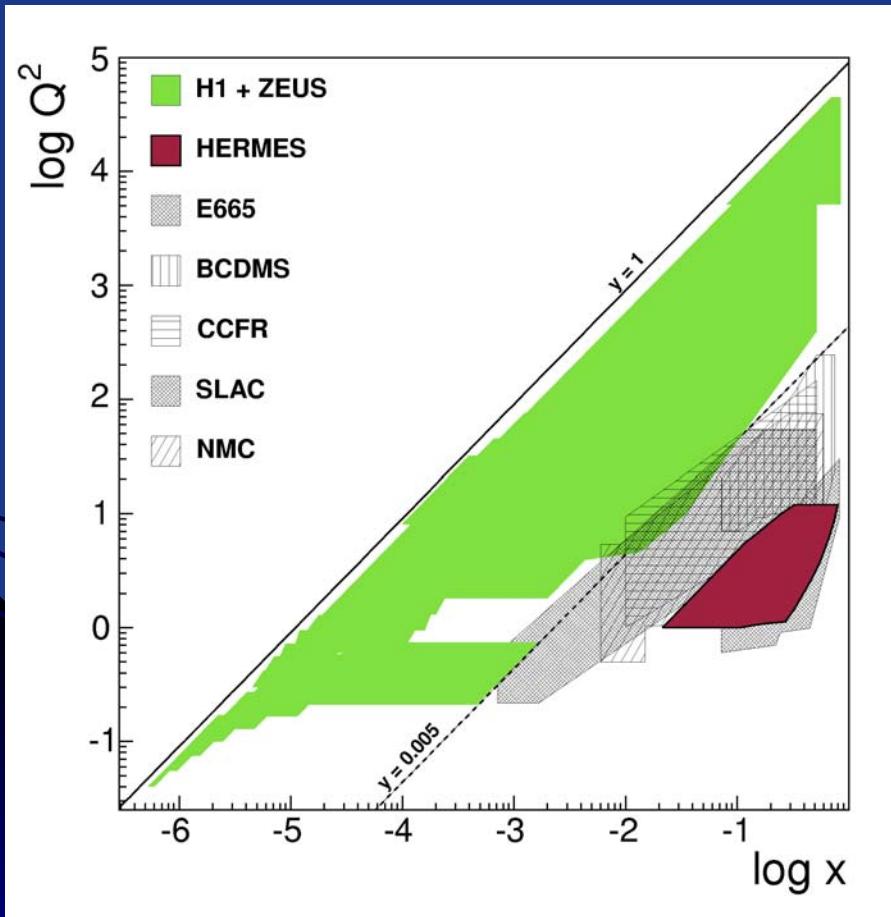
# ... a guided tour around the HERA phase space ...



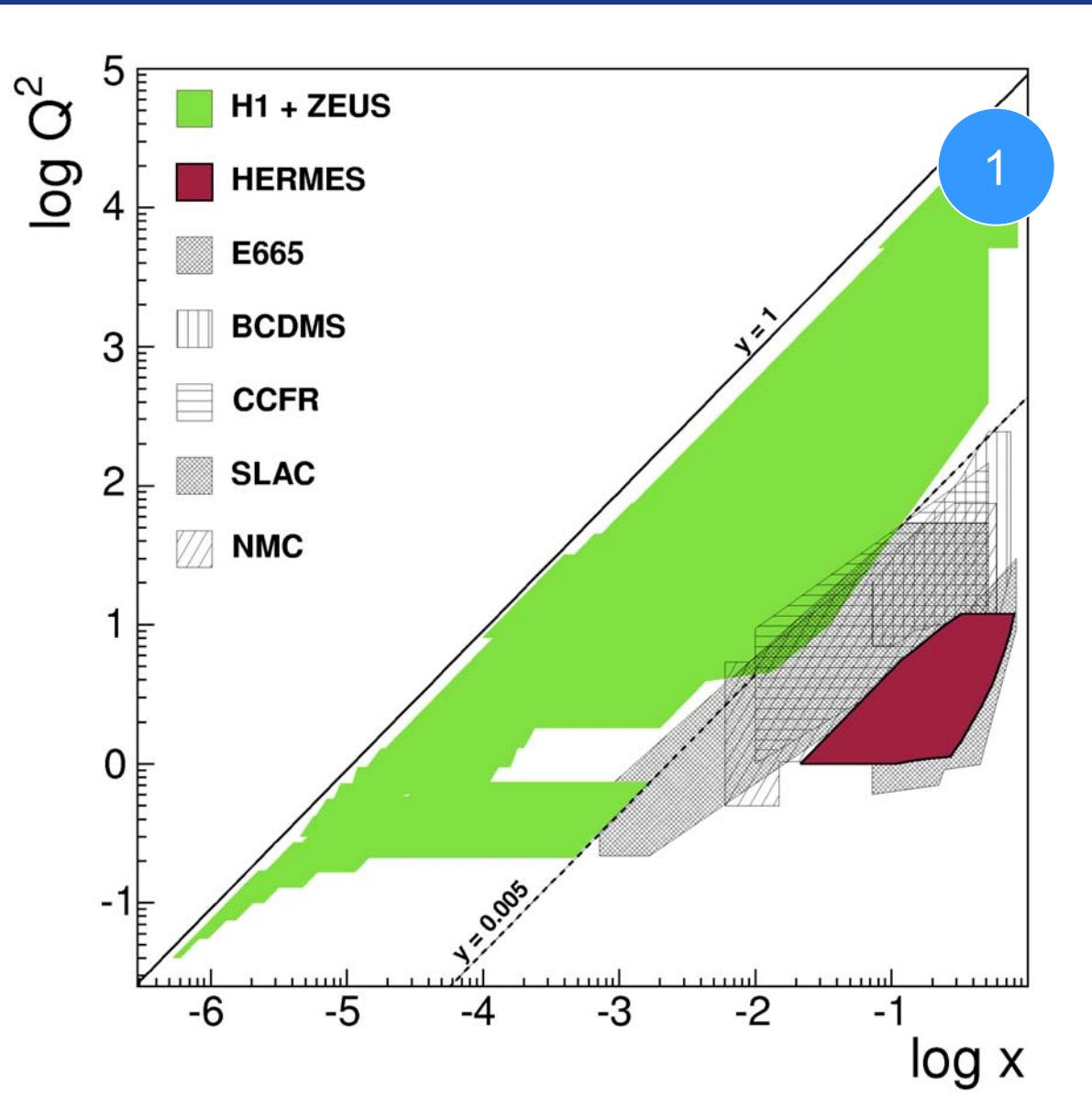
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# HERA I Kinematic Range



- Huge extension of kinematic reach:
  - $x_{Bj}$ : 6 orders
  - $Q^2$ : 6 orders
- Overlap with previous (fixed target) experiments



# Very High $Q^2$



E= 557.7 Et= 225.9 pt= 3.1 pz= 503.4 E-pz= 54.4 Ef= 555.4 Eb= 2.3 Er= 0.1  
 Tf= 1.7 Tr= 99.0 Le= 0.2 Lg= 0.0 FNC= 0 BCN=157 FLT=90A22F00 10000000  
 e- x=-5720 y=.410 Q2=21154 DA x=-5824 Q2=21310 JB y=.394 phi [ 0.180]

UCAL scale  
20.0 GeV

BAC scale P-S-W (GeV)  
5.00-5.00-5.00

Zeus Run 31244 Event 31806  
13-Oct-1998 1:38:13.560 File -s/data/minib98/r031244-z

$$Q^2 \approx 20000 - \text{GeV}^2, x \approx 0.6$$

Current Jet

$e^-$

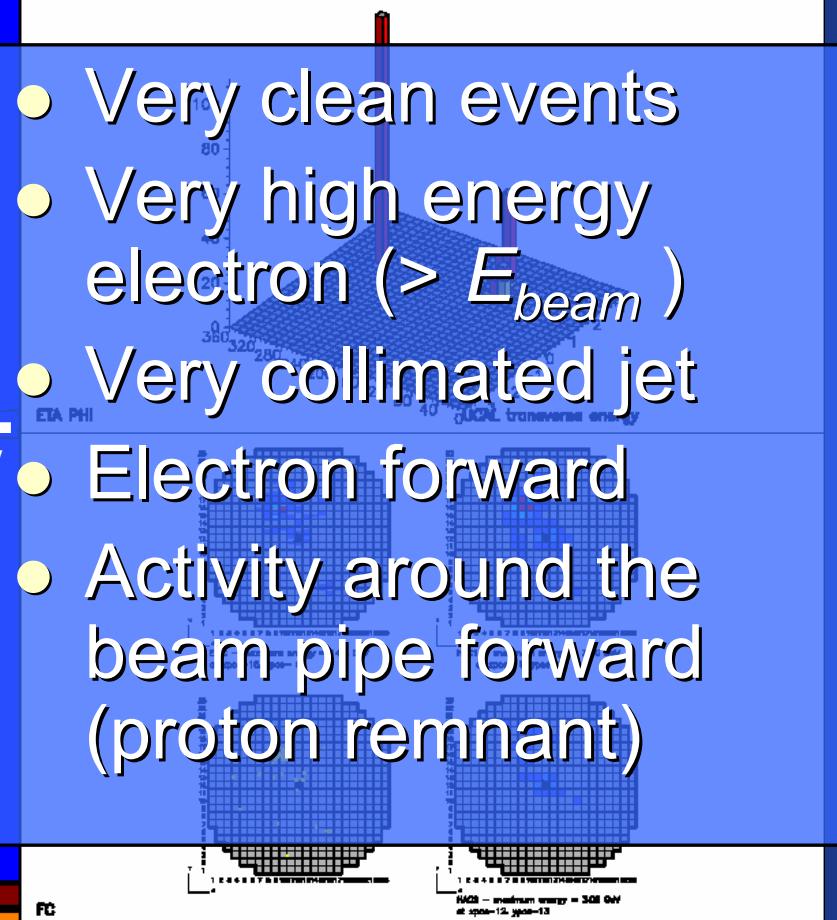
27.5 GeV

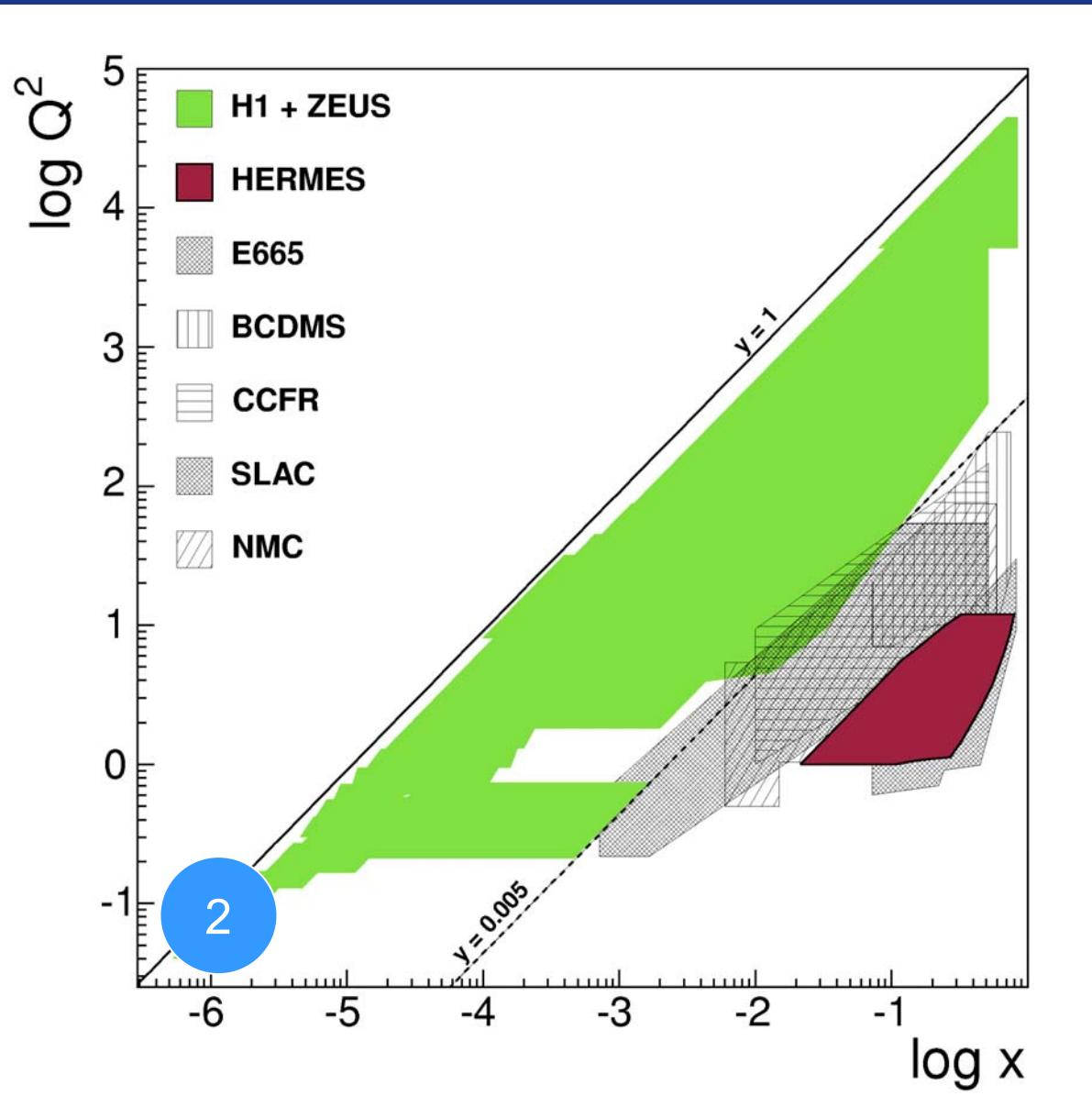
208. GeV – sira

Scattered  $e^-$

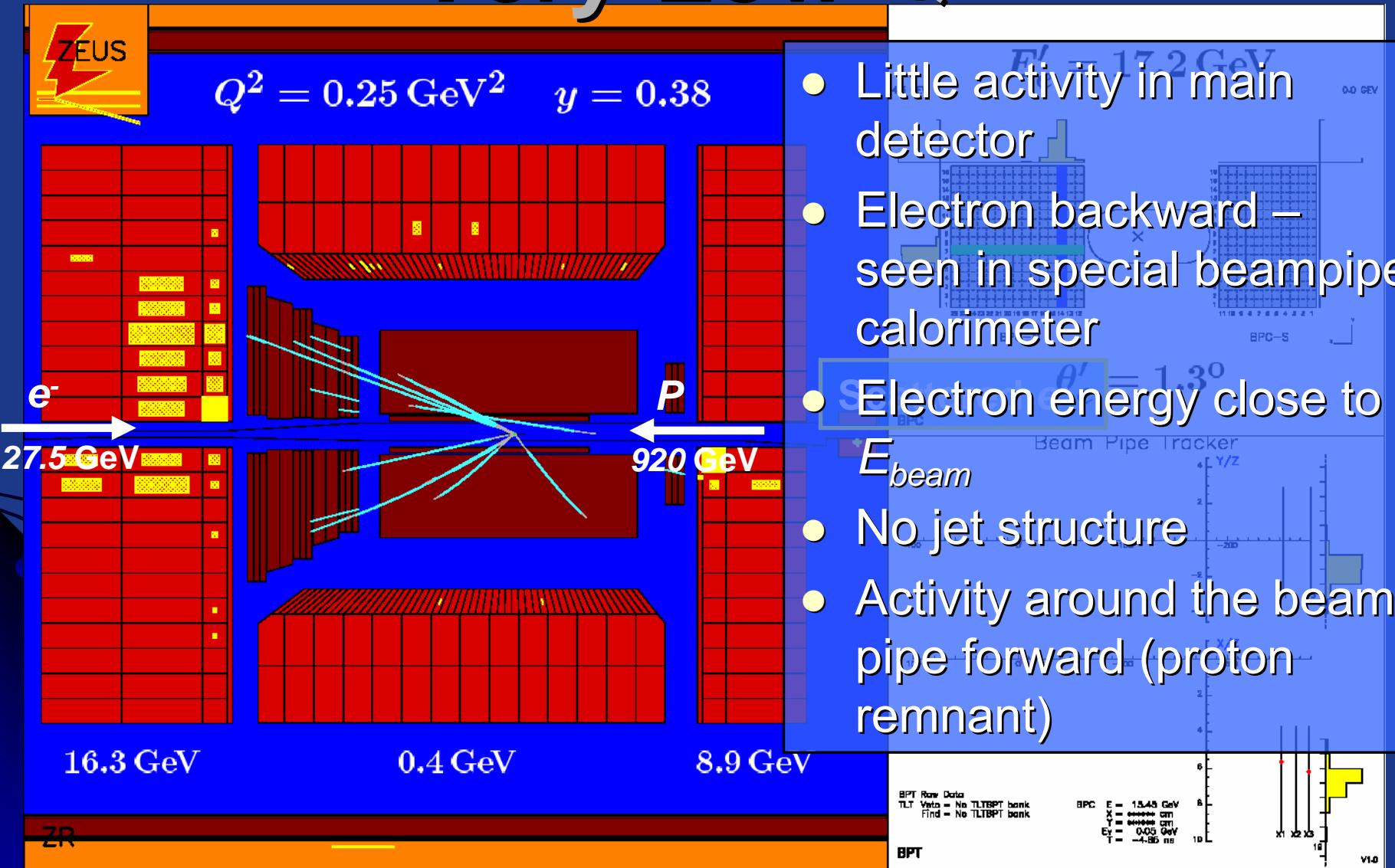
$P$

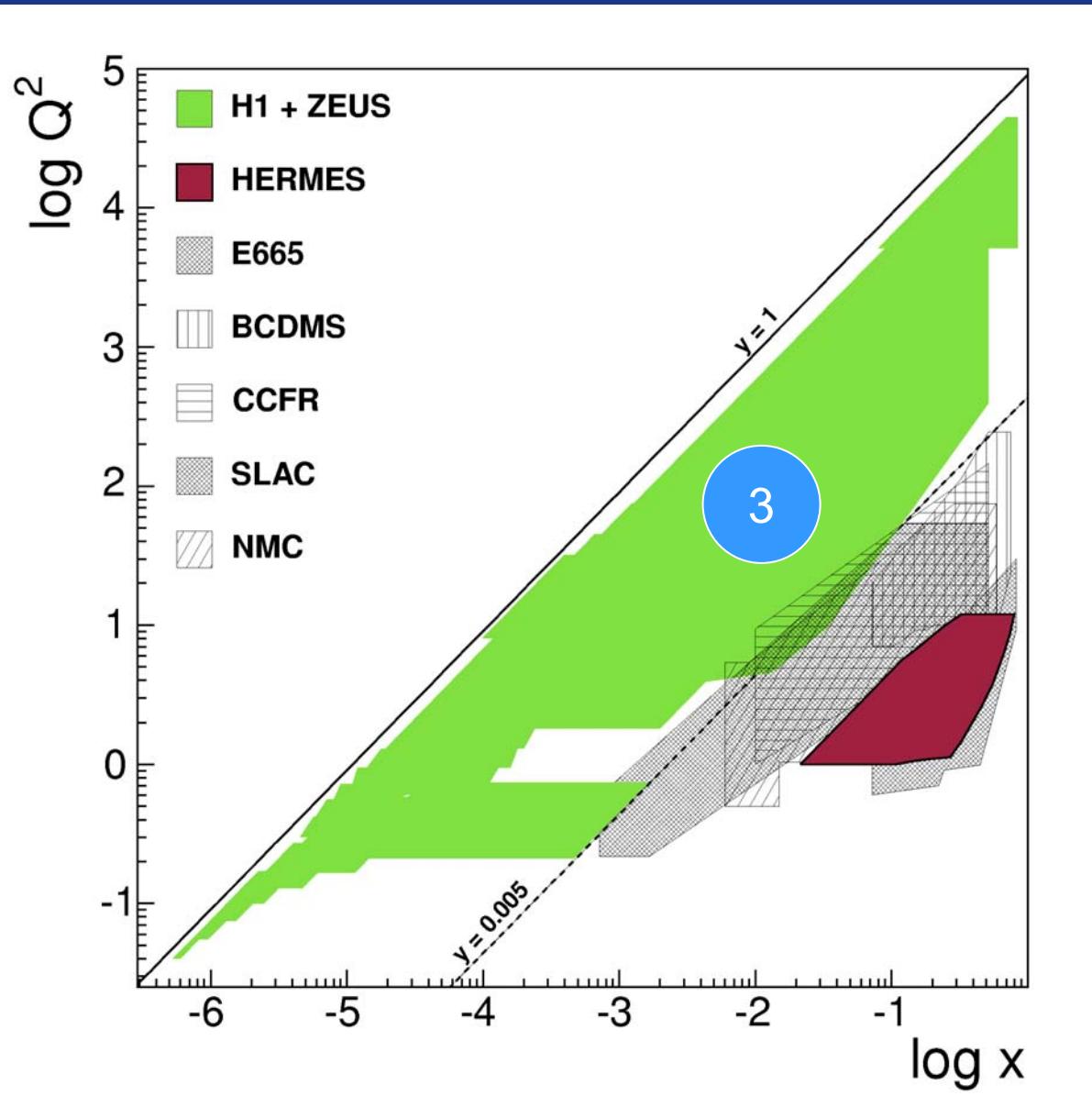
920 GeV





# Very Low $Q^2$

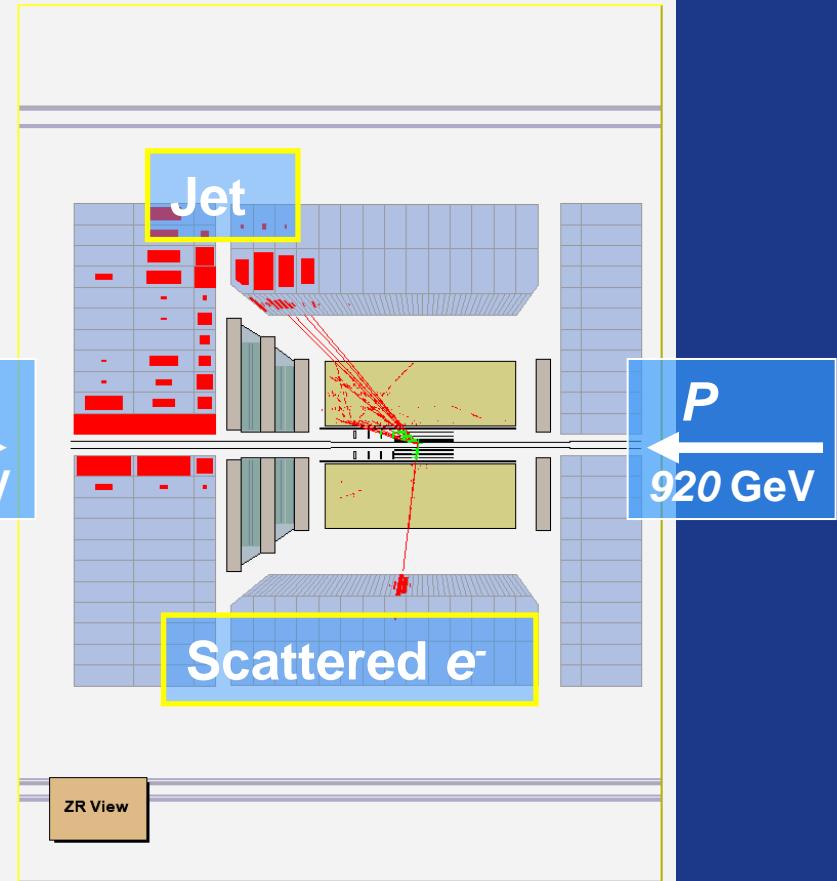
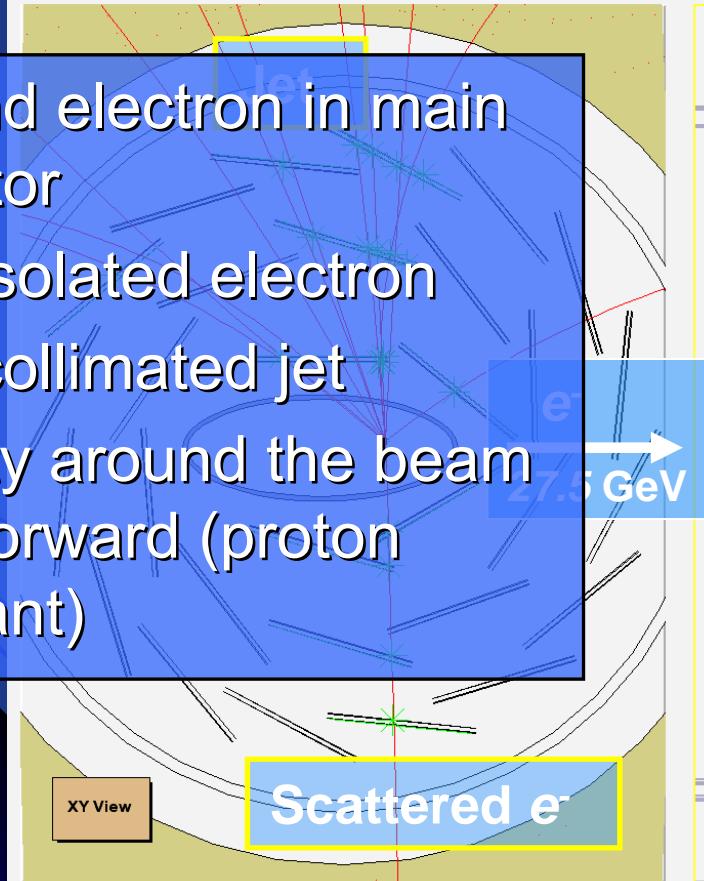




# Medium $Q^2$

Zeus Run 44699 Event 839					date: 15-02-2003	time: 18:43:32
$E=175.73 \text{ GeV}$	$E_t = 86.90 \text{ GeV}$	$E-p_z = 51.14 \text{ GeV}$	$E_f = 106.68 \text{ GeV}$	$E_b = 69.06 \text{ GeV}$		
$E_r = 0.00 \text{ GeV}$	$p_t = 5.96 \text{ GeV}$	$p_x = -1.97 \text{ GeV}$	$p_y = -5.62 \text{ GeV}$	$p_z = 124.60 \text{ GeV}$		
$\phi = -1.91$	$t_f = 3.22 \text{ ns}$	$t_b = 2.42 \text{ ns}$	$t_r = -100.00 \text{ ns}$	$t_g = 2.95 \text{ ns}$		

- Jet and electron in main detector
- Well isolated electron
- Well collimated jet
- Activity around the beam pipe forward (proton remnant)



# Structure Function Formalism

See e.g. David J Griffiths: "Introduction to elementary particles", New York, 1987



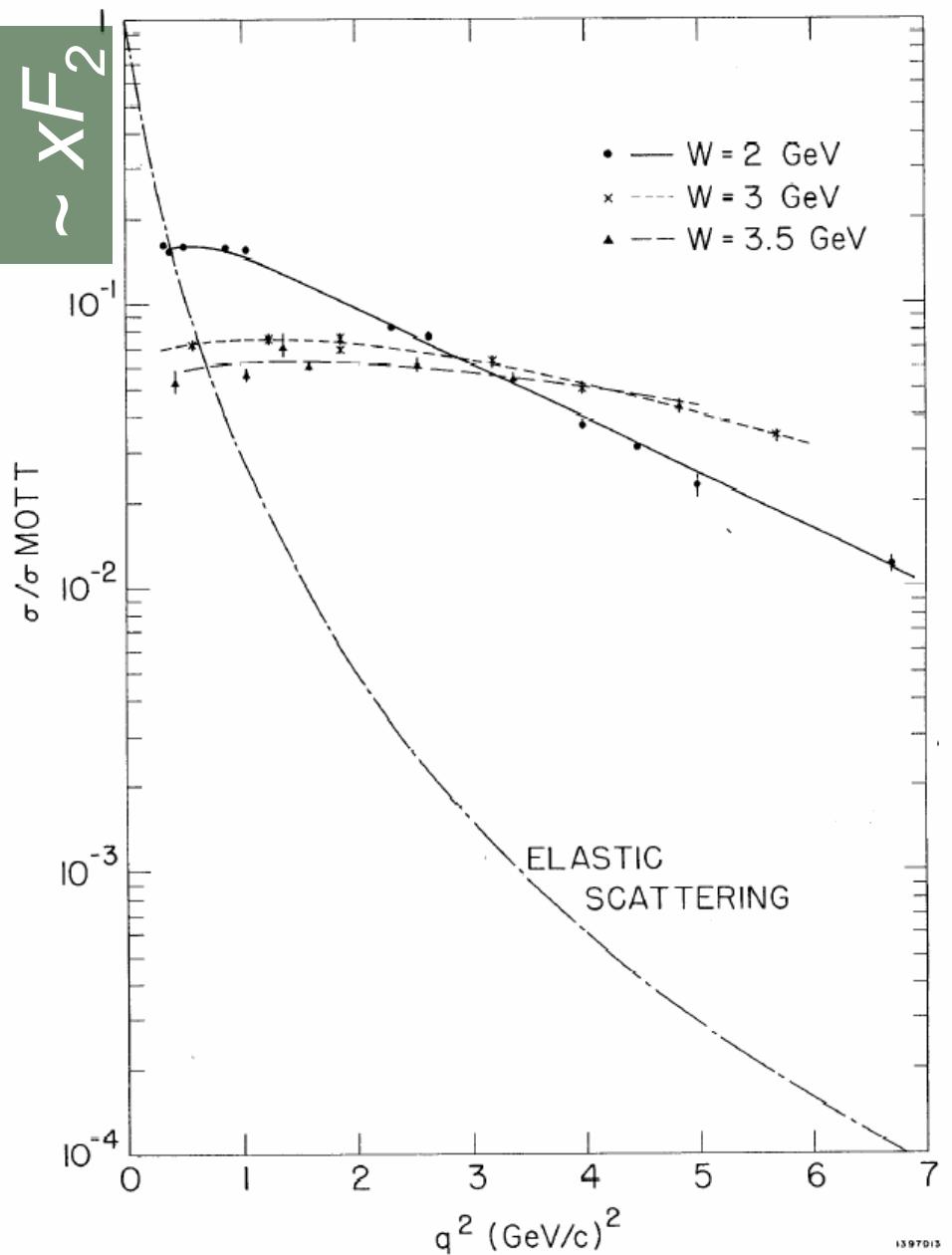
OBSERVED BEHAVIOR OF HIGHLY INELASTIC  
ELECTRON-PROTON SCATTERING

M. Breidenbach, J. I. Friedman, H. W. Kendall

Department of Physics and Laboratory for Nuclear Science,\*  
Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

E. D. Bloom, D. H. Coward, H. DeStaeler,  
J. Drees, L. W. Mo, R. E. Taylor

Stanford Linear Accelerator Center,† Stanford, California 94305



- Deep inelastic:
  - $W \gg M_P$
  - $xF_2 \approx \text{const.}$

## HIGH-ENERGY ELECTROPRODUCTION AND THE CONSTITUTION OF THE ELECTRIC CURRENT\*

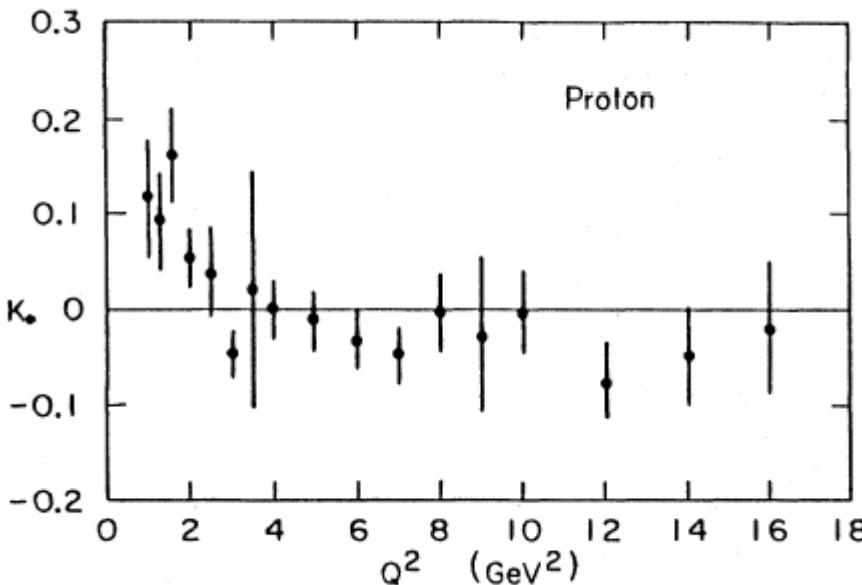
C. G. Callan, Jr.,<sup>†</sup> and David J. Gross<sup>‡</sup>

Lyman Laboratory, Harvard University, Cambridge, Massachusetts

(Received 18 November 1968)

The asymptotic behavior of electroproduction cross sections is shown to contain information about the constitution of the electric current.

$$K_0 = F_2 / (xF_1) - 1$$



## Experimental studies of the neutron and proton electromagnetic structure functions

A. Bodek,\* M. Breidenbach,<sup>†</sup> D. L. Dubin, J. E. Elias,<sup>‡</sup> J. I. Friedman, H. W. Kendall, J. S. Poucher,<sup>§</sup>  
E. M. Riordan,<sup>||</sup> and M. R. Sogard<sup>¶</sup>

Physics Department and Laboratory for Nuclear Science, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

D. H. Coward and D. J. Sherden

Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305

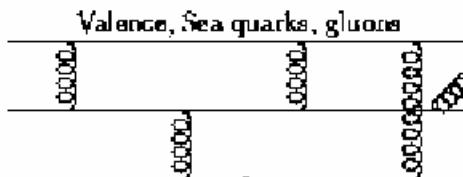
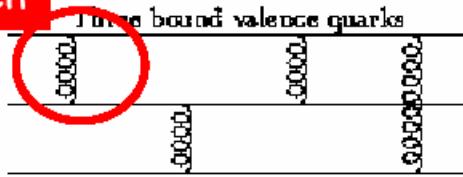
(Received 23 March 1979)

If the Proton is:

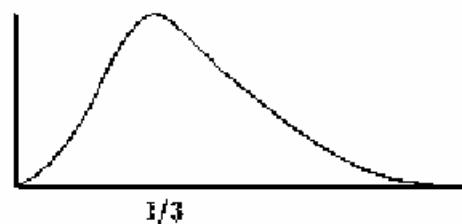
A quark

Three valence quarks

Gluonen

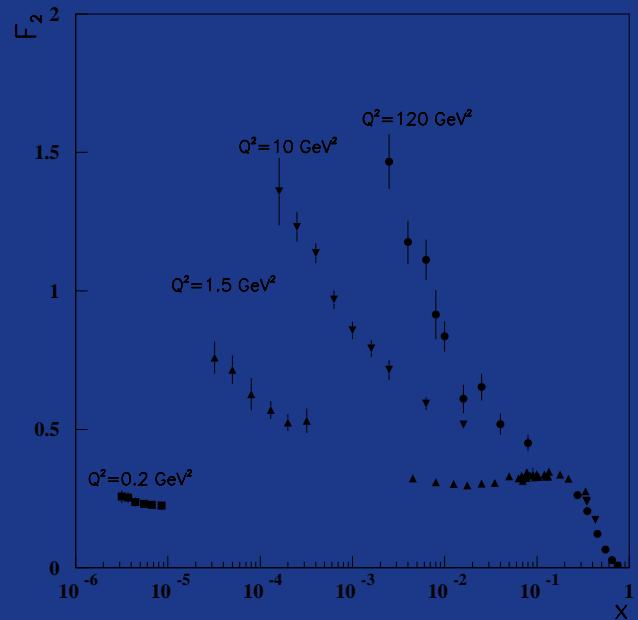


$$xF_2(x) = \sum e_i^2 (q_i(x) + \bar{q}_i(x))$$



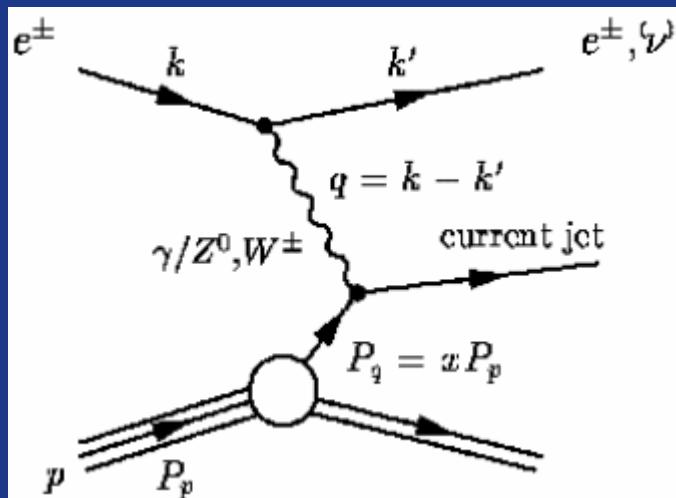
# HERA Results for $F_2$

Sample  $F_2$  data



*Dramatic Scaling Violations!*

# NC Cross Section and Structure Functions



$$Q^2 = -q^2 = -(k-k')^2$$

x: momentum fraction of the struck parton

y =  $Q^2/xs$

NC Reduced cross section:  $\tilde{\sigma}_{NC}(x, Q^2)$

NC Cross Section:

$$\frac{d^2 \sigma_{NC}(e^\pm p)}{dx dQ^2} = \frac{2\pi \alpha^2}{x Q^4} Y_+ [F_2 - \frac{y^2}{Y_+} F_L \mp \frac{Y_-}{Y_+} x F_3]$$

Dominant contribution

Sizeable only at high  $y$  ( $y \gtrsim 0.6$ )

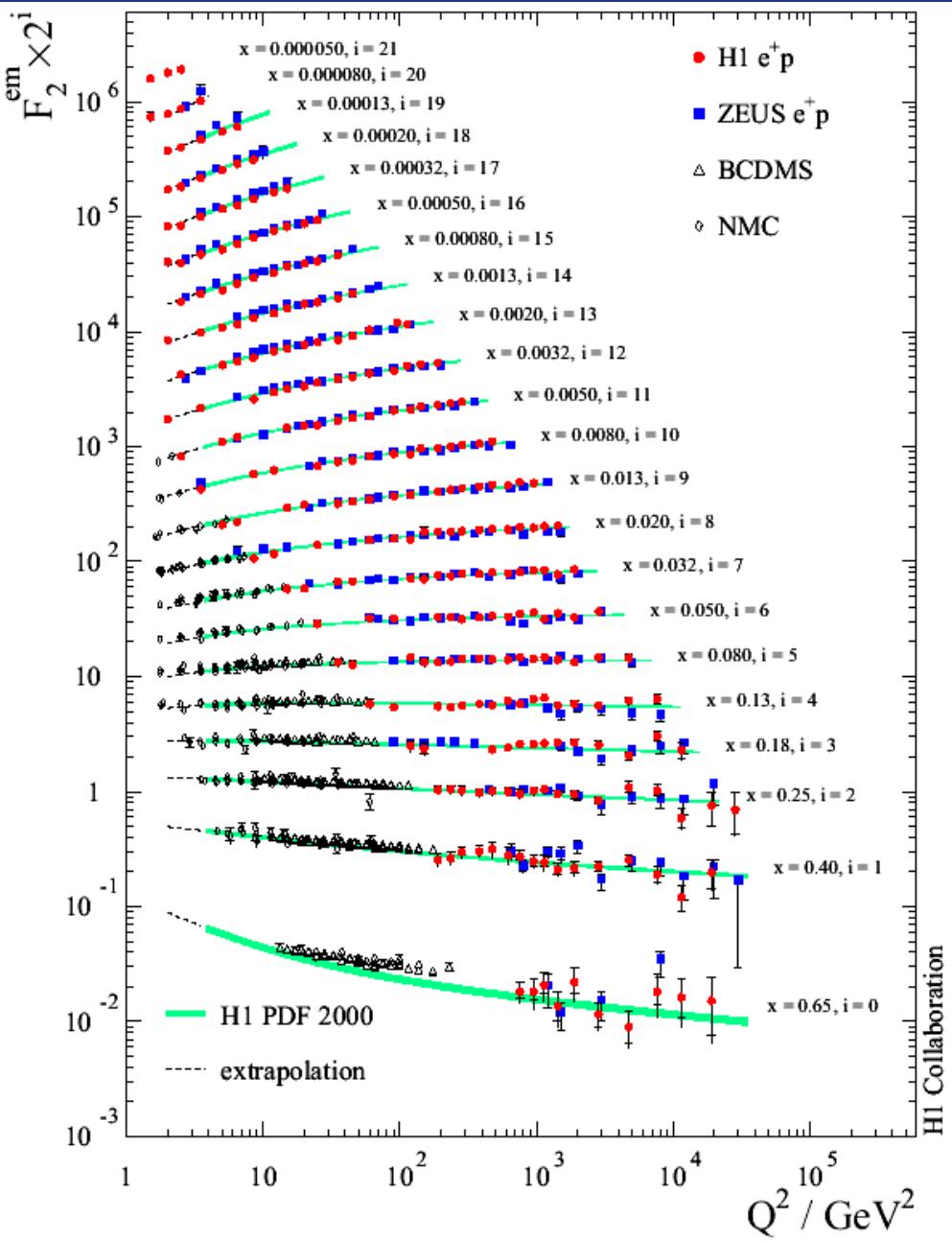
Contribution only important at high  $Q^2$

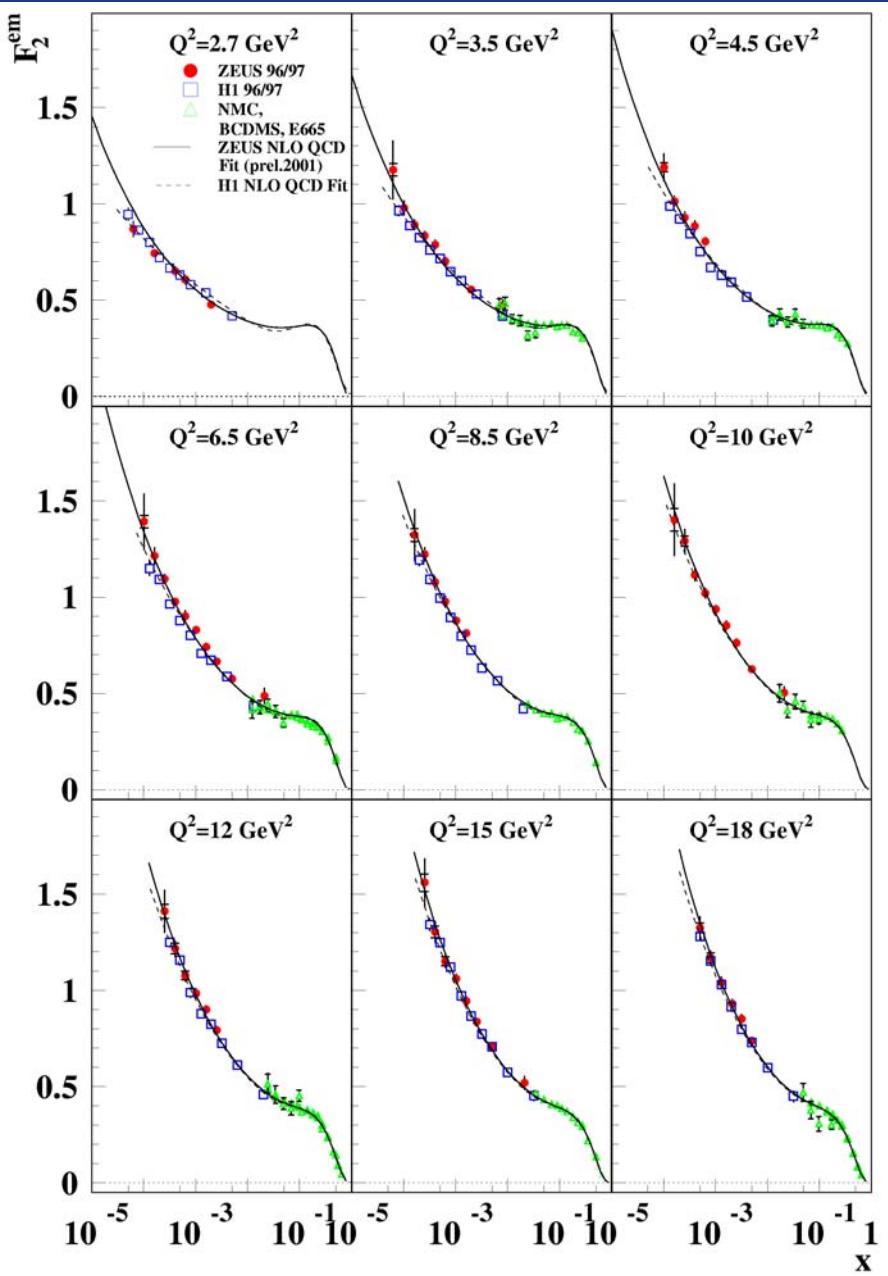
$$Y_\pm = 1 \pm (1-y)^2$$

# $F_2$ vs $Q^2$

- Note:

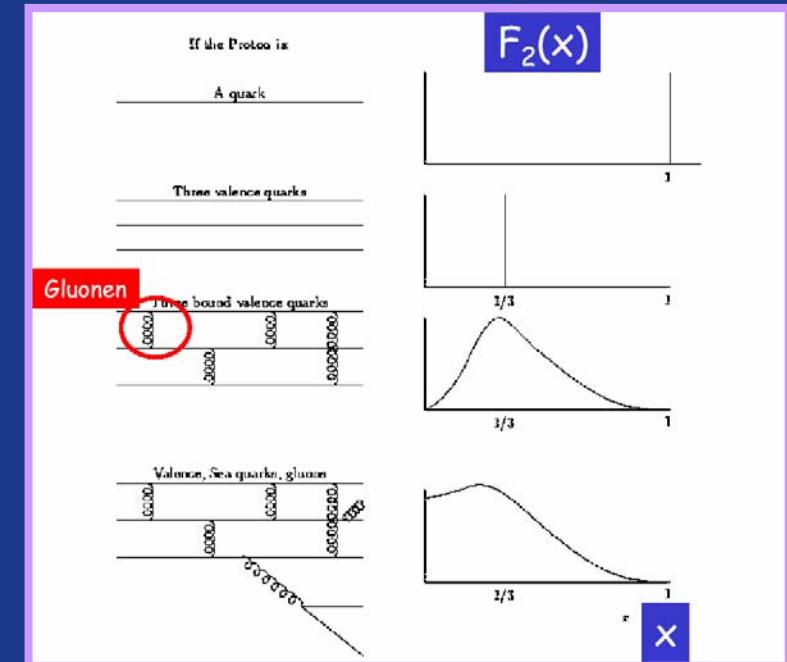
- Enormous range of data (5 orders in  $Q^2$  and 8 orders in  $x$ )
- Approximate scaling at high  $Q^2$
- Scaling violations at low  $Q^2$



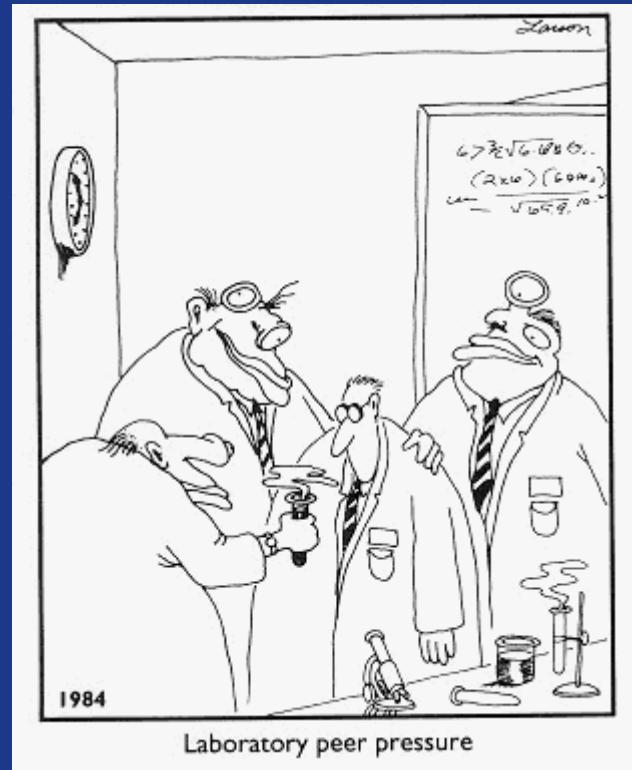


# $F_2$ VS $x_{Bj}$

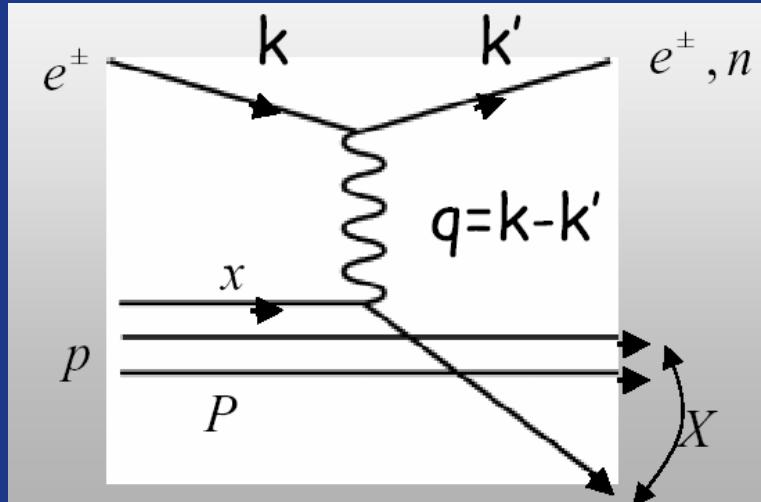
- Dramatic rise at low  $x_{Bj}$
- Note previous picture:



# Structure Function Evolution



# Reminder: Nomenclature/Kinematics



$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{x Q^4} \left\{ -y^2 F_L(x, Q^2) + Y F_2(x, Q^2) - Y x F_3(x, Q^2) \right\}$$

= 0 in the QPM

$$F_2(x) = x \cdot \sum_f z_f^2 (q_f(x) + \bar{q}_f(x))$$

$Z^0$  Exchange

$$Q^2 = -(k - k')^2$$

$$= -q^2$$

$$y = \frac{P \cdot q}{P \cdot k}$$

$$x = \frac{Q^2}{2P \cdot q}$$

$$s = (k + P)^2$$

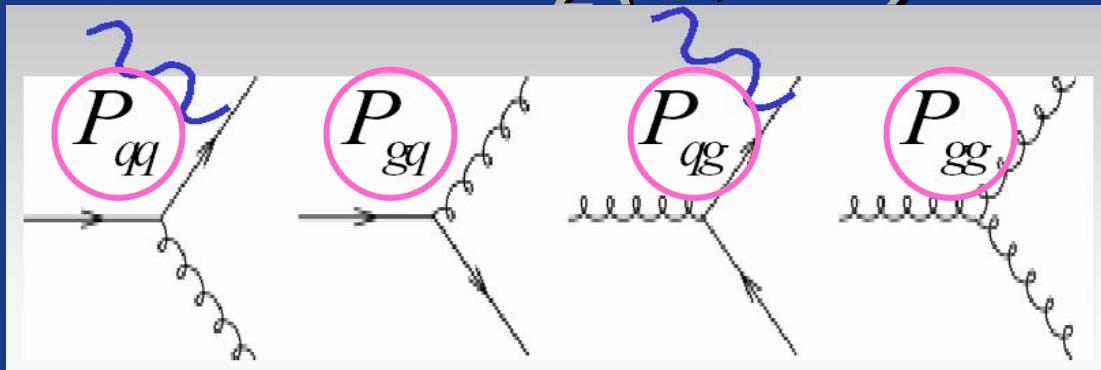
$$W^2 = M_X^2$$

$$= (q + P)^2$$

$$F_L = F_2 - 2x F_1$$

$$Y_\pm(y) = 1 \pm (1 - y)^2$$

# What QCD tells about $F_2(x, Q^2)$ ?



Splitting functions:  
Can be calculated  
in pQCD

$$\frac{d}{d \ln Q^2} \begin{pmatrix} q(x, Q^2) \\ g(x, Q^2) \end{pmatrix} = \frac{\alpha_s(Q^2)}{2\pi} \begin{pmatrix} P_{qq} & P_{qg} \\ P_{gq} & P_{gg} \end{pmatrix} \otimes \begin{pmatrix} q \\ g \end{pmatrix}$$

DGLAP Equation:

- Integral-Differential equation for the dependence of  $q(x, Q^2)$ ,  $g(x, Q^2)$  on  $Q^2$
- Need an initial condition!

$$(a \otimes b)(x) = \int_0^1 dy a\left(\frac{x}{y}\right) \frac{b(x)}{y}$$

# QCD Fits

- Make an ansatz at a fixed value of  $Q^2 = Q_0^2$

$$xq(x, Q_0) = Ax^B(1-x)^C \left[ 1 + D\sqrt{x} + Ex \right]$$

- Write  $F_2$  simpler:

$$\textcolor{red}{F}_2 \sim \frac{4}{9} (\bar{U} + \bar{\bar{U}}) + \frac{1}{9} (\bar{D} + \bar{\bar{D}})$$

with

$$\begin{aligned}\bar{D} &= \bar{d} + \bar{s} & \bar{U} &= \bar{u} + \bar{c} \\ U &= u + c & D &= d + s\end{aligned}$$

- Ignore  $F_3$  and  $F_L$  (for the moment)

# Parton Distribution Functions

**QCD fits** to structure functions:

$$F_2 \sim 4/9 (U + \bar{U}) + 1/9 (D + \bar{D})$$

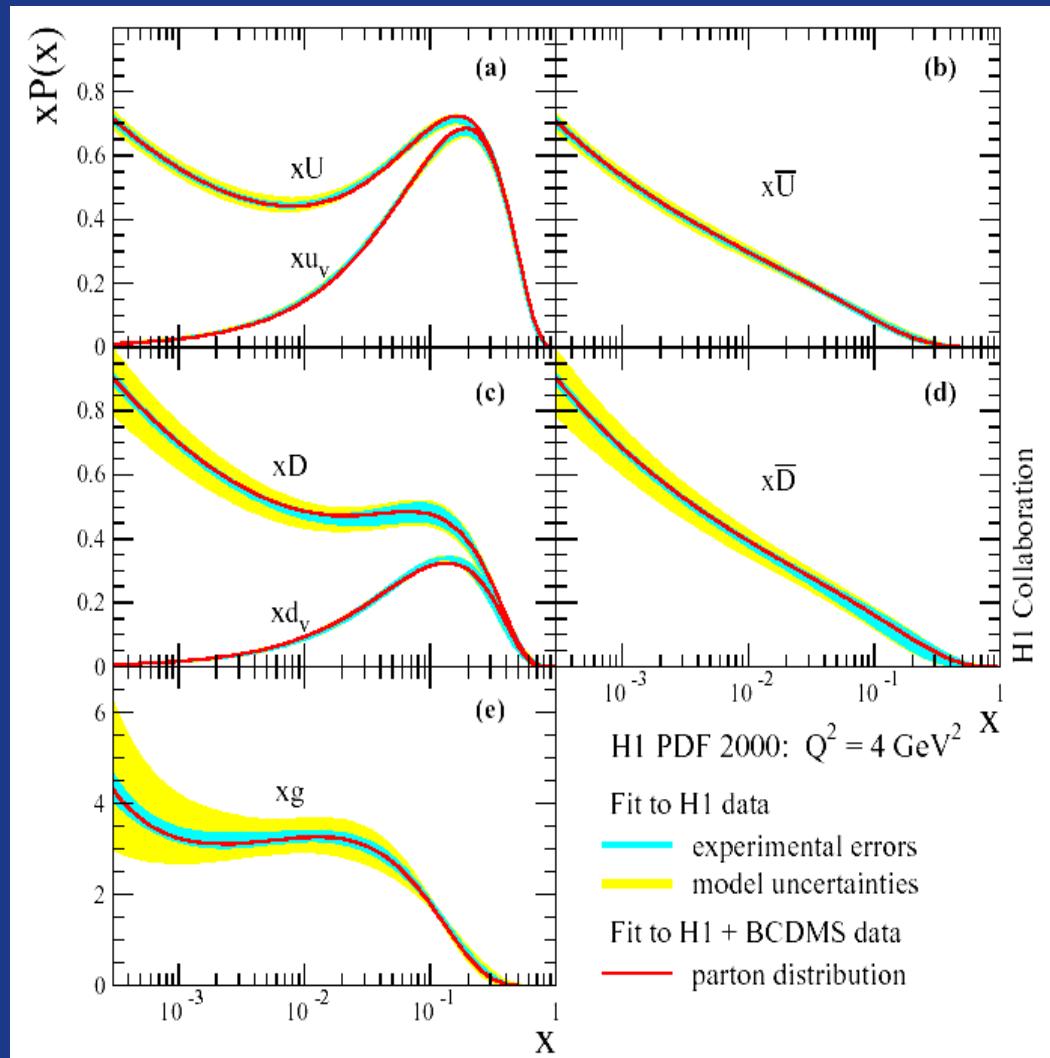
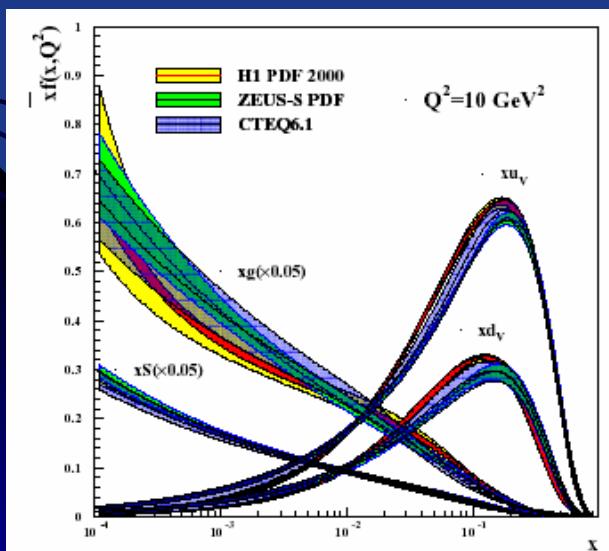
**Valence quarks:**

$$2 (U - \bar{U}) + (D - \bar{D})$$

$$\bar{D} = \bar{d} + \bar{s}$$

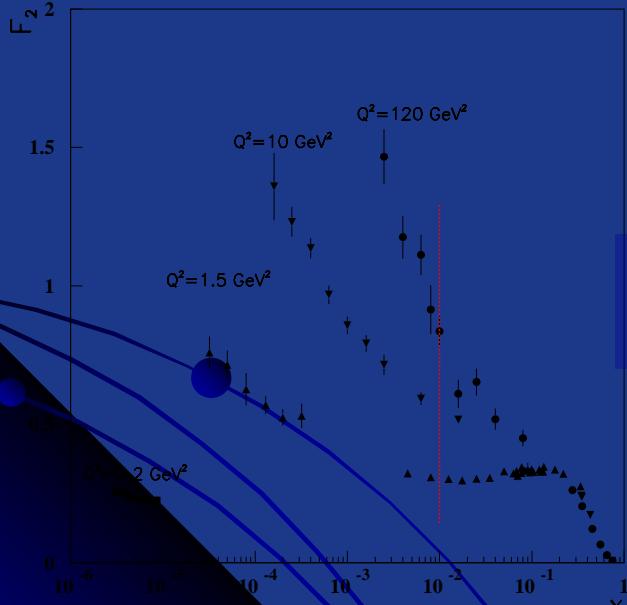
$$U = u + c$$

$$D = d + s$$

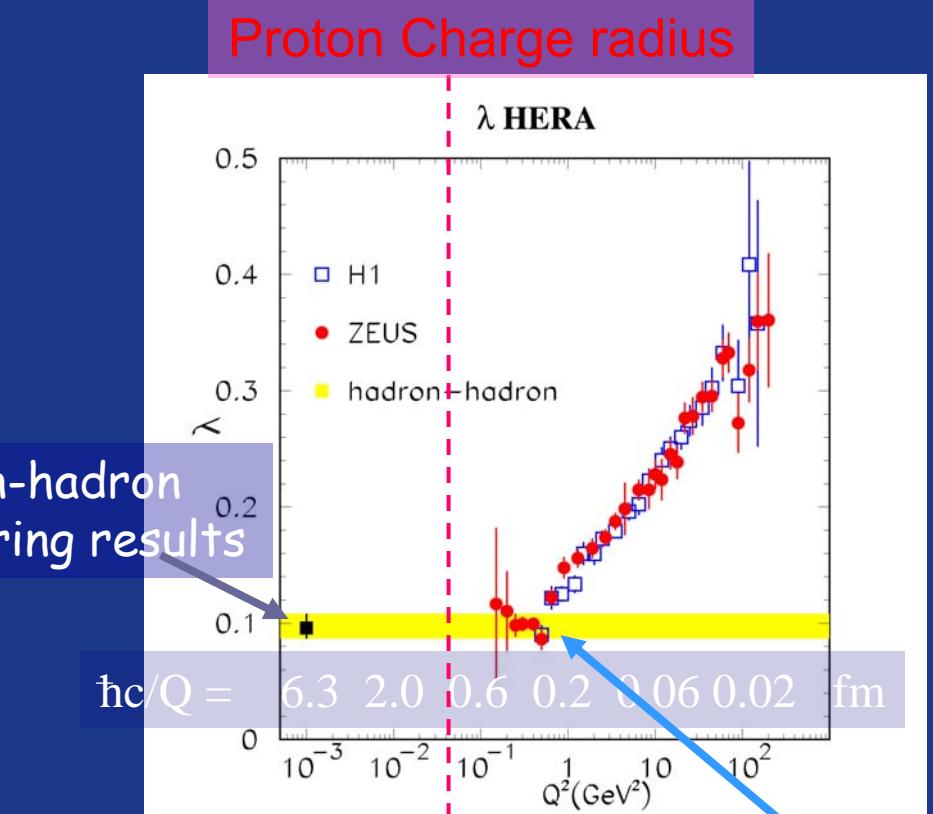


# ... another way to look at it ...

Sample  $F_2$  data



Hadron-hadron  
scattering results



$F_2 \propto x^{-\lambda}$  at small  $x$

Observation of hadron to parton transition