Superconducting Electron Linacs

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SC RF

Unlike the DC case (superconducting magnets), the surface resistance of a superconducting RF cavity is *not* zero:

$$R_{BCS} \propto \frac{f^2}{T} \exp\left(-1.76T_c / T\right)$$

Two important parameters:

- residual resistivity
- thermal conductivity













	Sc	me Numbers	
$f_{\rm RF} = 1.3 \rm GHz$		S.C. Nb (2K)	Cu
Q_0		5×10 ⁹	2×10 ⁴
R/Q		1 kΩ	
R_0		$5 \times 10^{12} \Omega$	$2 \times 10^7 \Omega$
P_{cav} (5 MV)	cw!	5 W	1.25 MW
P_{cav} (25 MV)	cw!	125 W	31 MW
$ au_{fill}$		1.2 s	5 µs
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Cryogenic Power Requirements

Basic Thermodynamics: Carnot Efficiency ($T_{cav} = 2.2$ K)

$$\eta_c = \frac{T_{cav}}{T_{room} - T_{cav}} = \frac{2.2}{300 - 2.2} \approx 0.7\%$$

System efficiency typically 0.2-0.3 (latter for large systems)

Thus total cooling efficiency is 0.14-0.2%

$$P_{cooling} = 5 \mathrm{W} / 0.002 \approx 2.5 \mathrm{kW}$$

Note: this represents *dynamic load*, and depends on Q_0 and V *Static load* must also be included (*i.e.* load at V = 0).







































Accelerating Electrons

Now let's calculate the RF→beam efficiency

power fed to beam:
$$P_{beam} = I_0 V_{acc} = \frac{4K\sqrt{\beta}}{1+\beta} P_{for} \left(1 - \frac{K}{\sqrt{\beta}}\right)$$

hence:

$$\eta_{RF \to beam} = \frac{P_{beam}}{P_{for}} = \frac{4K\sqrt{\beta}}{1+\beta} \left(1 - \frac{K}{\sqrt{\beta}}\right)$$

reflected power: $P_{ref} = P_{for} - P_{beam} - P_{cav} = (1 - \eta)P_{for} - \frac{V_{acc}^2}{2R}$

$$=P_{for}\left(\frac{\beta-1-2K\sqrt{\beta}}{1+\beta}\right)$$

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Accelerating Electrons

Note that if beam is off (*K*=0)

$$P_{ref} = P_{for} \left(\frac{\beta - 1}{\beta + 1}\right)^2$$
 previous result

For zero-beam loading case, we needed $\beta = 1$ for maximum power transfer (i.e. $P_{ref} = 0$)

Now we require $0 = \beta - 1 - 2K\sqrt{\beta}$

$$K = \frac{\beta - 1}{2\sqrt{\beta}}$$

Hence for a fixed coupler (β) , zero reflection only achieved at one specific beam current.









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From previous discussions:

$$V_{cav}(t) = 2V_{acc} \left(1 - e^{-t/\tau}\right) \qquad \tau = \frac{2Q_L}{\omega_0} = \frac{2Q_0}{\omega_0 \left(\beta + 1\right)}$$
$$V_{beam}(t) = \begin{cases} 0 & t \le t_{fill} \\ -V_{acc} \left(1 - e^{-(t - t_{fill})/\tau}\right) & t > t_{fill} \end{cases}$$

Allow cavity to charge for t_{fill} such that

$$V_{cav}(t_{fill}) = V_{acc} \Longrightarrow t_{fill} = \ln(2)\tau$$

For TESLA example: $\tau = 645 \,\mu s$ $t_{fill} = 447 \,\mu s$

















Lorentz Force Detuning cont.

Three fixes:

- mechanically stiffen cavity
- feed-forwarded (increase RF power during pulse)
- fast piezo tuners + feedback











Transverse HOMs

wake is sum over modes: $W_{\perp}(t) = \sum_{n} \frac{2k_n c}{\omega_n} e^{-\omega_n t/2Q_n} \sin(\omega_n t)$

 k_n is the *loss parameter* (units $V/pC/m^2$) for the *n*th mode

Transverse kick of *j*th bunch after traversing one cavity:

$$\Delta y'_{j} = \sum_{i=1}^{j-1} \frac{y_{i}q_{i}}{E_{i}} \frac{2k_{i}c}{\omega_{n}} e^{-\omega_{n}i\Delta t/2Q_{n}} \sin(\omega_{i}i\Delta t_{b})$$

where y_i , q_i , and E_{i} , are the offset *wrt* the cavity axis, the charge and the energy of the *i*th bunch respectively.









Consider the TESLA wake potential $W_{\parallel}(z = ct)$

$$W_{\parallel}(z) \approx -38.1 \left[\frac{V}{pC \cdot m} \right] \left[1.165 \exp\left(-\sqrt{\frac{s}{3.65 \times 10^{-3} [m]}} \right) - 0.165 \right]$$

wake over bunch given by convolution: ($\rho(z) = \text{long. charge dist.}$)











BNS Damping

If both macroparticles have an initial offset y_0 then particle 1 undergoes a sinusoidal oscillation, $y_1=y_0\cos(k_\beta s)$. What happens to particle 2?

$$y_{2} = y_{0} \left[\cos(k_{\beta}s) + s\sin(k_{\beta}s) \frac{W'_{\perp} q\sigma_{z}}{2k_{\beta}E_{beam}} \right]$$

Qualitatively: an additional oscillation out-of-phase with the betatron term which grows monotonically with s.

How do we beat it? Higher beam energy, stronger focusing, lower charge, shorter bunches, or a damping technique recommended by Balakin, Novokhatski, and Smirnov (*BNS Damping*) curtesy: P. Tenenbaum (SLAC)



BNS Damping

The wakefield can be locally cancelled (ie, cancelled at all points down the linac) if:

$$\frac{W'_{\perp} q \sigma_z}{E_{beam}} \frac{1}{k_{\beta 2}^2 - k_{\beta 1}^2} = 1$$

This condition is often known as "autophasing."

It can be achieved by introducing an energy difference between the head and tail of the bunch. When the requirements of discrete focusing (ie, FODO lattices) are included, the autophasing RMS energy spread is given by:

$$\frac{\sigma_E}{E_{beam}} = \frac{1}{16} \frac{W'_{\perp} q \sigma_z}{E_{beam}} \frac{L_{cell}^2}{\sin^2(\pi \nu_{\beta})}$$

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DFS

Problem:

$$\Delta \mathbf{y} = -\left[\mathbf{Q}\left(\frac{\Delta E}{E}\right) - \mathbf{Q}(0)\right] \left(\frac{\Delta E}{E}\right) \cdot \mathbf{Y}$$
$$\equiv \mathbf{M}\left(\frac{\Delta E}{E}\right) \cdot \mathbf{Y}$$

Note: taking difference orbit Δy removes \mathbf{b}_{offset}

Solution (trivial): $\mathbf{Y} = \mathbf{M}^{-1} \cdot \Delta \mathbf{y}$

Unfortunately, not that easy because of noise sources:

$$\Delta \mathbf{y} = \mathbf{M} \cdot \mathbf{Y} + \mathbf{b}_{\text{noise}} + \mathbf{R} \cdot \mathbf{y}_0$$

















Ballistic Alignment

- Turn of all components in section to be aligned [magnets, and RF]
- use 'ballistic beam' to define straight reference line (BPM offsets)

$$y_{\text{BPM},i} = y_0 + s_i y_0' + b_{\text{offset},i} + b_{\text{noise},i}$$

- Linearly adjust BPM readings to arbitrarily zero last BPM
- · restore components, steer beam to adjusted ballistic line





