

problem 1:

$$\Delta_{ij,ek} = D_{ij} D_{ek}^*$$

$$\Delta_{ij,ek} = P_{ie} P_{jk} - \frac{1}{2} P_{ij} P_{ek}$$

$$P_{ie} = \delta_{ie} - \hat{k}_i \hat{k}_e \rightarrow \text{projection into the plane orthogonal to } \hat{k}$$

$$D_{ij} = \begin{pmatrix} 1 & i \\ i & -1 \\ & & 0 \end{pmatrix}$$

z-direction:

$$P_{ie} = \begin{pmatrix} 1 & & \\ & 1 & \\ & & 0 \end{pmatrix}$$

$$P_{ie} D_{ij} = D_{ej}$$

$$\begin{aligned} \Delta_{ij,ij} &= D_{ij} D_{ij}^* - 0 \\ &= 4 \end{aligned}$$

y-direction: $P_{ie} = \begin{pmatrix} 1 & & \\ & 0 & \\ & & 1 \end{pmatrix}$

$$P_{ic} D_{ij} P_{jk} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}_{jk}$$

$$\Delta DD = 1 - \frac{1}{2} = \frac{1}{2}$$

$$\Delta DD = \text{Tr} P D P D - \frac{1}{2} (\text{Tr} P D)^2$$

There is a factor 8 between the radiation in the plane compared to the radiation orthogonal to the plane of the binary system.

problem 2:

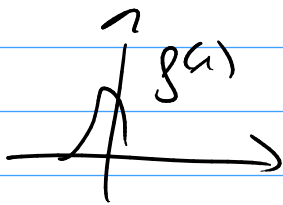
$$\vec{x} \rightarrow \vec{x} + \vec{a} = \vec{x}'$$

$$g'(\vec{x}') = g'(\vec{x} + \vec{a}) = g(\vec{x})$$

$$D'_i = \int dx' x' g'(x')$$

$$= \int dx x g(x)$$

$$= \int dx (\vec{x} + \vec{a}) g(x) = D + \vec{a} M$$



One of the standard arguments is that the monopole vanishes for the system and the radiation does not depend on the coordinate system chosen!

problem 3:

$$M = \int d^3x T^{00}$$

$$\partial_t M = \int d^3x \partial_0 T^{00}$$

$$= - \int d^3x \partial_i T^{i0} = \text{surface term}$$

$$D^i = \int d^3x x^i T^{00} = 0$$

$$\partial_0^2 T^{00} = \partial_i \partial_i T^{i1}$$

$$\partial_0^2 D^i = \int d^3x x^i \partial_j \partial_0 T^{j1} = \text{surface term} \\ = 0$$

$$M = \text{const}$$

$$D^i = \text{const} + t \times \text{const.}$$

$$P \propto \frac{2G\omega^4}{5} \Delta(k) D(\omega) D^*(\omega)$$

$$D(\omega) = \sum \dots D(\omega_i)$$

Fourier transform:

$$FT(1) = \delta(\omega)$$

$$FT(t) = \partial_{\omega} \delta(\omega)$$

the support of these function is basically $\omega = 0$ and hence there is no radiation produced.

The same argument can also be applied in ED.

$$\partial_r \gamma^{\alpha} = 0 \quad \int \epsilon_0 = \gamma^0$$

So the ED radiation is also not coordinate dependent even if the monopole (the total charge of the system) does not vanish.