

# Top Quark Physics Lecture

## Motivation

Material to be included

- 1) Profile of  $t$  : decay modes
- 2) Threshold production : top mass
- 3) Continuum  $t\bar{t}$  production  
 $\sigma_{t\bar{t}}$  ,  $t$  decays  
(anomalous) couplings in  $t\bar{t}$  prod. & decay
- 4) polarisation issues (to be included)

Comparison with LHC

$t$  most massive matter particle known to date  
 $m_t$  curiously close to scale of EWIB  
 likely to play key role in  
 pinning down origin of EWIB  
 e.g. measurement of  $\gamma_t$   
 search for clues to solve flavour problem  
 precision measurements of its properties and int.  
 mandatory for any future collider  
 $e^+e^-$  LCs most suitable instruments  
 to study top under clean up. cond.

Importance of precise measurement of  $m_t$   
 which can be made at LC :  
 important in { EW precision analysis  
 test diff. meth. at quantum level  
 theory of flavour

precision measurement of NC coupling to  $\gamma, Z$   
 helicity analysis

# 1) Profile of top

SM decay

with  $\Gamma_{SM}$

decay distrib. of (polarised)  $t \rightarrow b l \nu_e$

with  $\Gamma_t$  from  $A_{FB}$  near threshold

previous simulation:

$$\frac{\delta \Gamma_t}{\Gamma_t} = 10-20\%$$

will be updated

non-SM decays

examples:  $t \rightarrow H^+ b$  &  $t \rightarrow \tilde{t} \chi^0$  within MDM

plots of  $B_r$

7. 5 marks

incl. LHC exp. constraints

$$B_r(t \rightarrow H^+ b) \geq 1\%$$

assume: seen at LHC and mass  $m_{H^+}$  known

LC: measure  $B_r$

previous simulation:

$$\frac{\delta B_r}{B_r}$$

as function of  $B_r$

simul.  $B_r(t \rightarrow \tilde{t} \chi^0) > 0.6\%$

with  $100 \text{ fb}^{-1}$

2) t-tbar threshold : top mass

emphasize:  $m_t$  from counting  $t\bar{t}$  (color singlet)  
as opposed to  $t \rightarrow j\bar{t}$

theory input: recent calcs. of  $\sigma_{t\bar{t}}^{\text{threshold}}$   
at NNLO

using proper mass definitions  
 $M_t^{1S}, M_t^{Pf}, \dots$

top momentum dist.

theory plot of  $\sigma_{t\bar{t}}^{\text{threshold}}$

simulation: see plot

• 2 parameter fit:  $\alpha_s, M_t$

•  $\alpha_s$  input: fit to  $M_t$

simulation:

Pavella, Martinez, Mignel

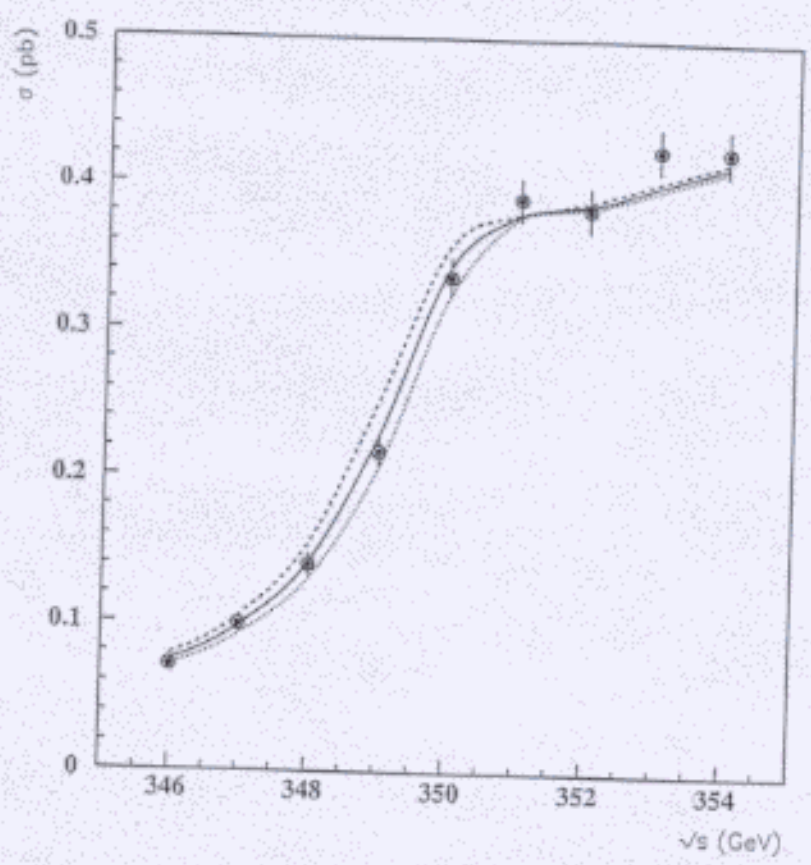
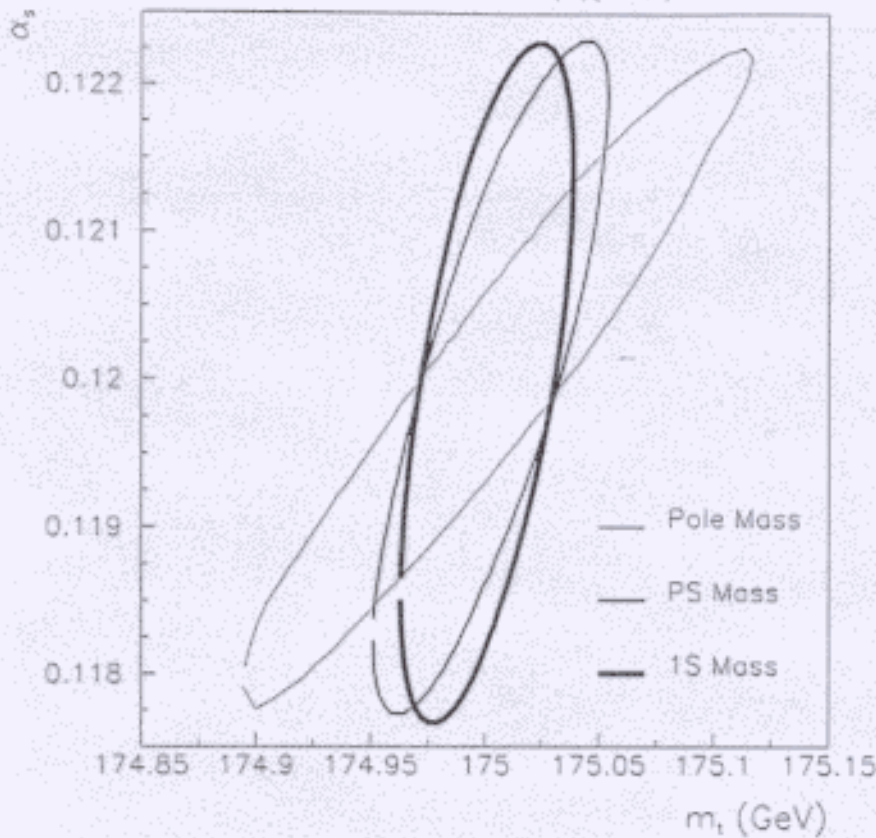


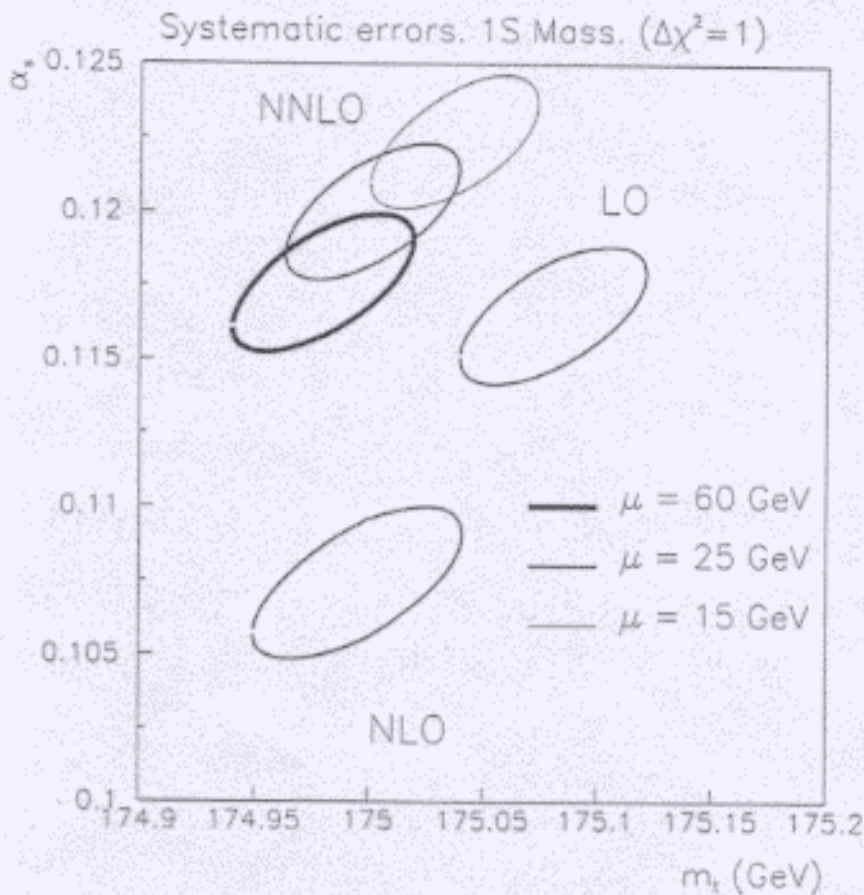
Figure 3.3.4: Excitation curve of the top quarks including initial-state radiation and beamstrahlung [32]. The errors of the data points correspond to an integrated luminosity of  $\int \mathcal{L} = 100 \text{ fb}^{-1}$ . The dotted curves indicate shifts of the top mass by  $\pm 100 \text{ MeV}$ .



2 parameter fit

will be updated

3.3.5: Statistical errors on  $\alpha_s$  and the top mass resulting from a 2-parameter fit to simulated data of the  $t\bar{t}$  excitation curve, using the NNLO cross-section prediction with the top threshold mass parameters indicated. Here  $m_t$  denotes the top mass of the conventions given in the figure. An integrated luminosity of  $100 \text{ fb}^{-1}$  was used. From Ref.[32].



3.3.6: Theoretical errors on the fitted values of  $\alpha_s$  and the so-called 1S mass, arising from the dependence of the NNLO cross-section prediction on the renormalization scale  $\mu$ . From Ref.[32].

Results:

17

2 parameter fit:

$$(\delta M_t^{IS})_{sim} \approx 40 \text{ MeV}, (\delta \alpha_s)_{sim} \approx 0.0024$$

$$(\delta M_t^{II})_{th} \approx 40 \text{ MeV}, (\delta \alpha_s)_{th} \approx 0.013$$

1 parameter fit:

input  $\alpha_s$  with  $\delta \alpha_s = 0.001$

$$(\delta M_t^{IS})_{sim} \approx 30 \text{ MeV}, (\delta M_t^{PIS})_{sim} \approx 40 \text{ MeV}$$

$$(\delta M_t^{II})_{th} \approx 110 \text{ MeV}, (\delta M_t^{PIS})_{th} \approx 120 \text{ MeV}$$

will be updated

eventually convert into  $\overline{MS}$  mass  $\overline{m}_t(\overline{m}_t)$

### 3) Continuum $t\bar{t}$ production

theory plot of  $\sigma_{t\bar{t}}(s)$  including  $O(\alpha_s^2)$  corr.  
+ 1 loop EW corr.

plot will be provided by  
Kühn et al.

top couplings:

LR asymmetry at threshold

$$\frac{\sigma_L - \sigma_R}{\sigma} \propto g_{Vt}^2 / Q_t$$

$e^-_L e^- \rightarrow t\bar{t}$  at threshold

100% polarized  $t$  decay

ideal to study decay coupl.

search for anomalous couplings:

helicity analysis in coll. (using pol.  $e^-$ )

form factor decomp. of  $t\bar{t}$  prod. & decay  
vertices

chirality conserving / flipping CP-odd,  $t\bar{t}$

$(g-2)_t$ ,  $EPN_t$ , V+A admixture, ...



analysis done mainly at parton level

possible strategy: first  $\mathcal{F}$

then input to determine CP-inv. couplings

Form factor	SM value	$\sqrt{s} = 500 \text{ GeV}$		$\sqrt{s} = 800 \text{ GeV}$	
		$p = 0$	$p = -0.8$	$p = 0$	$p = -0.8$
$F_{1V}^\gamma$	1				
$F_{1V}^Z$	1		0.019		
$F_{1A}^Z$	1		0.016		
$F_{1A}^\gamma$	0				
$F_{2V}^{\gamma,Z}$	0	0.015	0.011	0.011	0.008
$\text{Re}F_{2A}^\gamma$	0	0.035	0.007	0.015	0.004
$\text{Re}F_{2A}^Z$	0	0.012	0.008	0.008	0.007
$\text{Im}F_{2A}^\gamma$	0	0.010	0.008	0.006	0.005
$\text{Im}F_{2A}^Z$	0	0.055	0.010	0.037	0.007
$F_{1R}^W$	0	0.030	0.012		
$\text{Im}F_{2R}^W$	0	0.025	0.010		

theory at 500 GeV

← from R. Frey

0(N<sub>c</sub>) QCD

-0.009

0.02  $\delta_{CP}$

high res.  $\mathcal{F}$

$\gamma-Z$

$\mathcal{F}$

V+A

$\mathcal{F}$

Table 3.3.1: 1 s.d. statistical sensitivities to (non) SM form factors in  $t\bar{t}$  production [9, 19] and in  $t$  decay to  $Wb$  [9, 18]. The second column contains the respective SM value to lowest order,  $p$  denotes the polarisation of the electron beam. For the c.m. energy  $\sqrt{s} = 500 \text{ GeV}$  ( $800 \text{ GeV}$ ) an integrated luminosity of  $300 \text{ fb}^{-1}$  ( $500 \text{ fb}^{-1}$ ) was used.

#### 4) Polarisation issues

- beam pol. obvious tool  
for top physics
- $e^-$  pol. has been used  
to some extent
- $\frac{\delta Pol}{Pol} \approx 1\%$  seems  
sufficient  
for top studies

# Comparison with LHC

	LC	LHC
$m_t$	$\leq 200 \text{ MW}$ (Kishimoto)	1-2 GW
$\Gamma_t$	$\sim 10\%$	no, but $ V_{tb} ^2 \sim 10\%$ (stat.) from single top
"static" parameters ( $g-2$ , EDM, $V_{tb}$ )	$\leq \text{few } \%$	
$t \rightarrow H^+ b$	tree decay $B_r \leq 1\%$	$\sim 3\%$
$t \rightarrow \tilde{t} X^0$	$B_r < 1\%$	no
$t \rightarrow c Z$	$\sim 10^{-3}$	$\sim 10^{-4}$
$t \rightarrow c \gamma$	not studied	$\sim 10^{-4}$