

Simulation of Dispersion Correction at the VUV-FEL

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 - All BPM's, undulator BPM's...
 - Sensitivity to BPM noise and off-sets
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Dispersion correction algorithm

It corrects both **orbit** and **dispersion**, using the orbit and dispersion **response matrices**

Steerer

➤ Orbit response term

$$O_{i,j} = \frac{\Delta x_i}{\Delta \theta_j}$$

➤ Dispersion response term

$$D_{i,j} = \frac{\Delta D_i}{\Delta \theta_j}$$

Quad mover

➤ Orbit response term

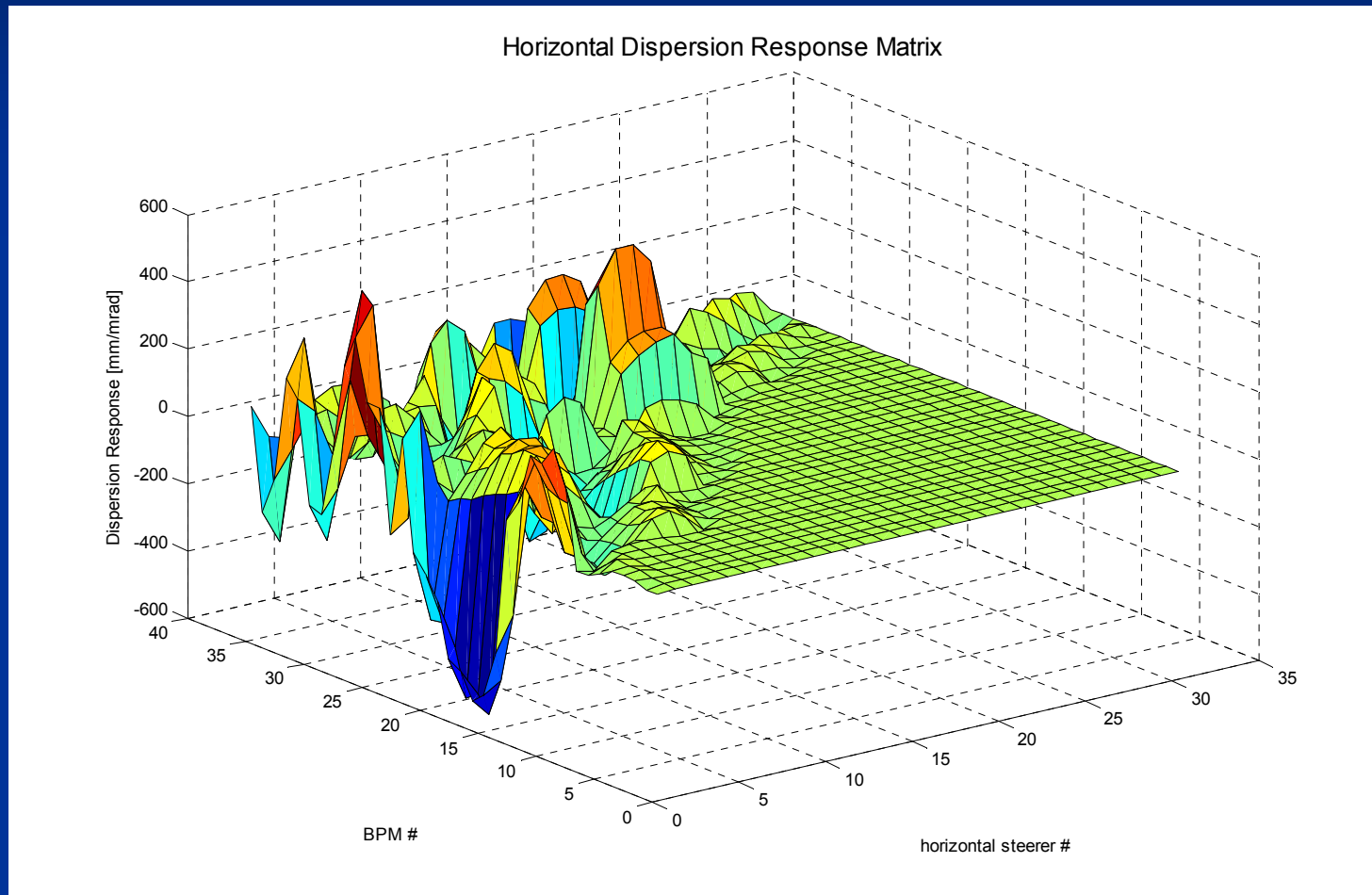
$$O_{i,j} = \frac{\Delta x_i}{\Delta x_j}$$

➤ Dispersion response term

$$D_{i,j} = \frac{\Delta D_i}{\Delta x_j}$$

$\Delta x_i / \Delta D_i$ -----> change of the orbit / dispersion at the BPM i
 $\Delta \theta_j / \Delta x_j$ -----> change of the kick angle of the steerer j /
change of transverse position of quad j

Response matrix example



Dispersion correction algorithm

$$\begin{pmatrix} \underline{\underline{O}} \cdot (1-w) \\ \underline{\underline{D}} \cdot w \end{pmatrix} \cdot \underline{\underline{\Delta\theta}} = \begin{pmatrix} \underline{x} \cdot (1-w) \\ \underline{d} \cdot w \end{pmatrix}$$

Response matrices

Orbit

Dispersion

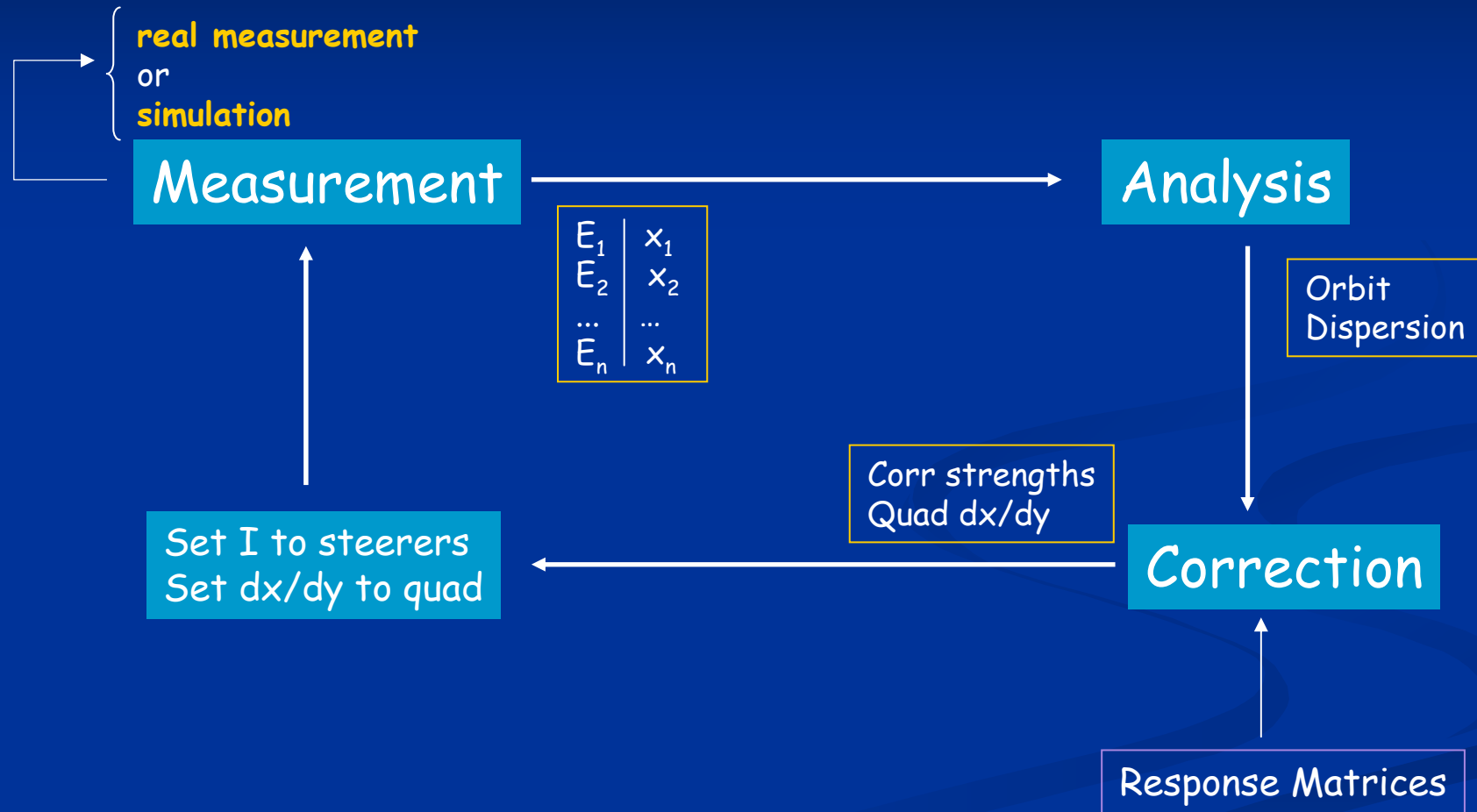
Weighting factor

Corrector strengths
(& quad displacements)

Measurements

$$\sum \left[\begin{pmatrix} \underline{x}_{meas} \\ \underline{d}_{meas} \end{pmatrix} - \begin{pmatrix} \underline{x} \\ \underline{d} \end{pmatrix} \right]^2 = \min \Rightarrow \underline{\underline{\Delta\theta}}$$

Dispersion correction sketch



Simulations

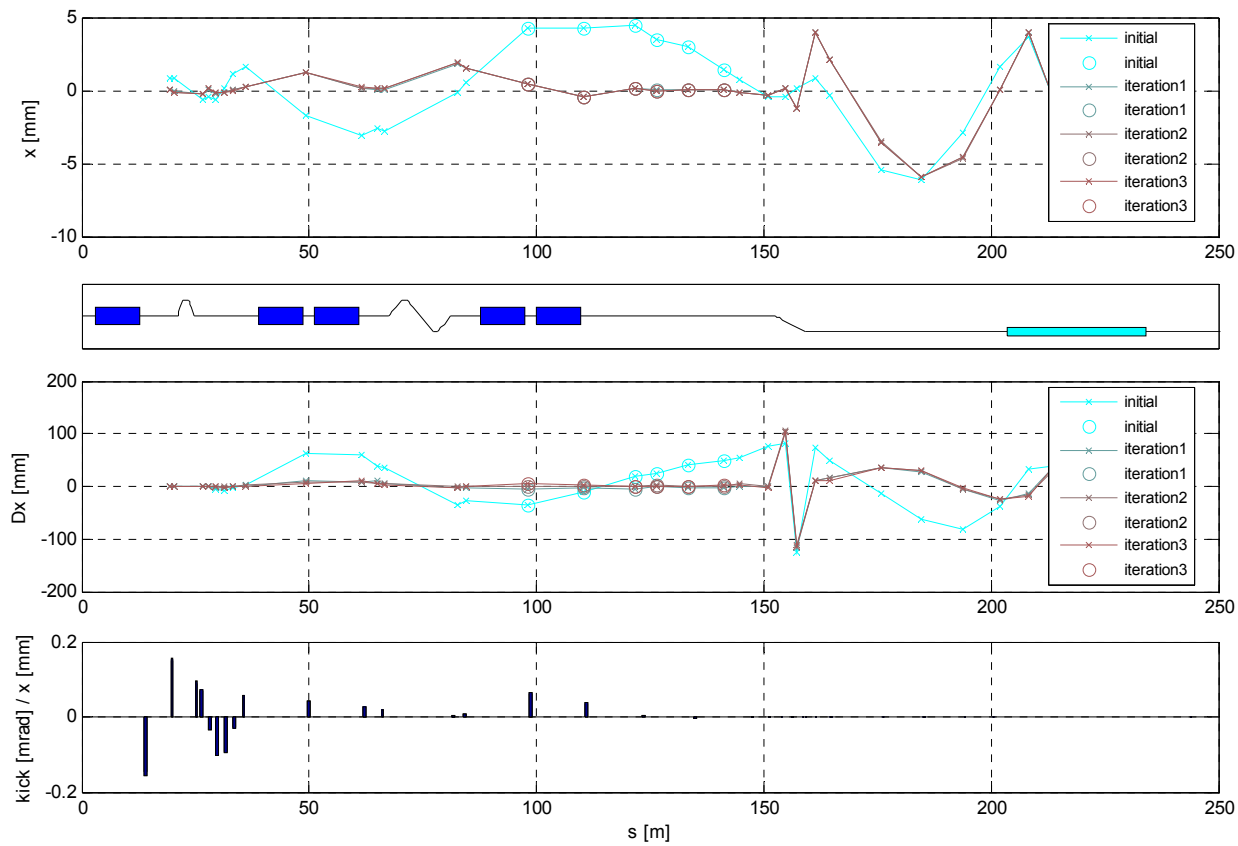
Basic set

Quad misalignments	200um
BPM off-sets	100um
BPM noise	20um
Weighting factor	0.1

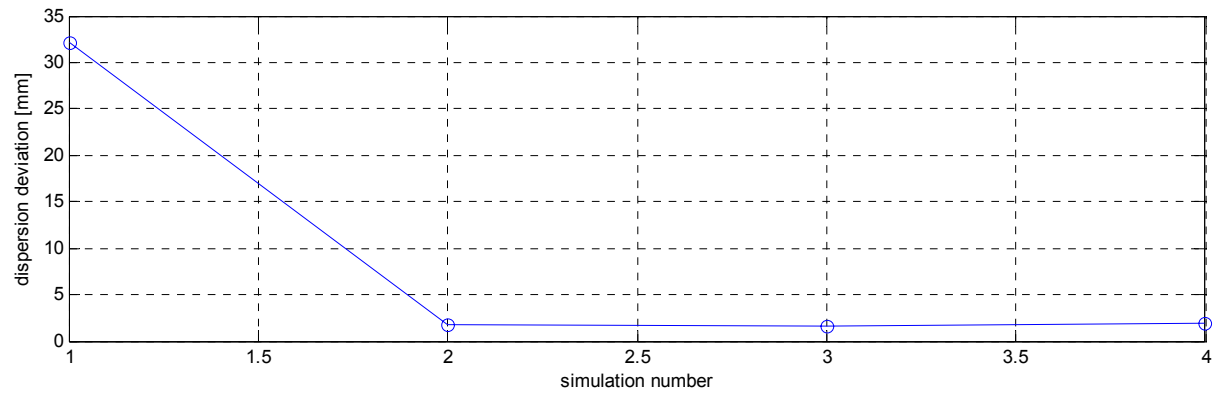
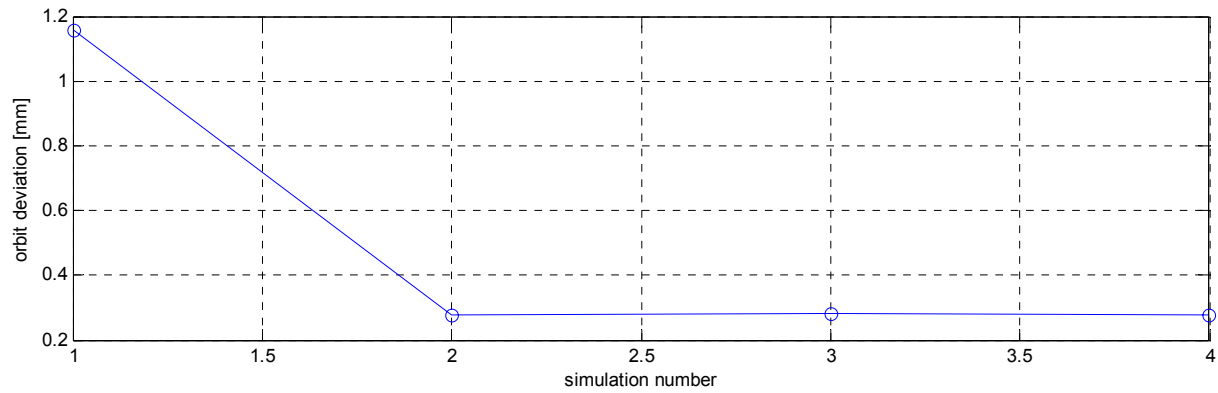
-Not considered effects

- Coupler kicks
- Dipole and quadrupole field errors
- Response matrix errors
- ...

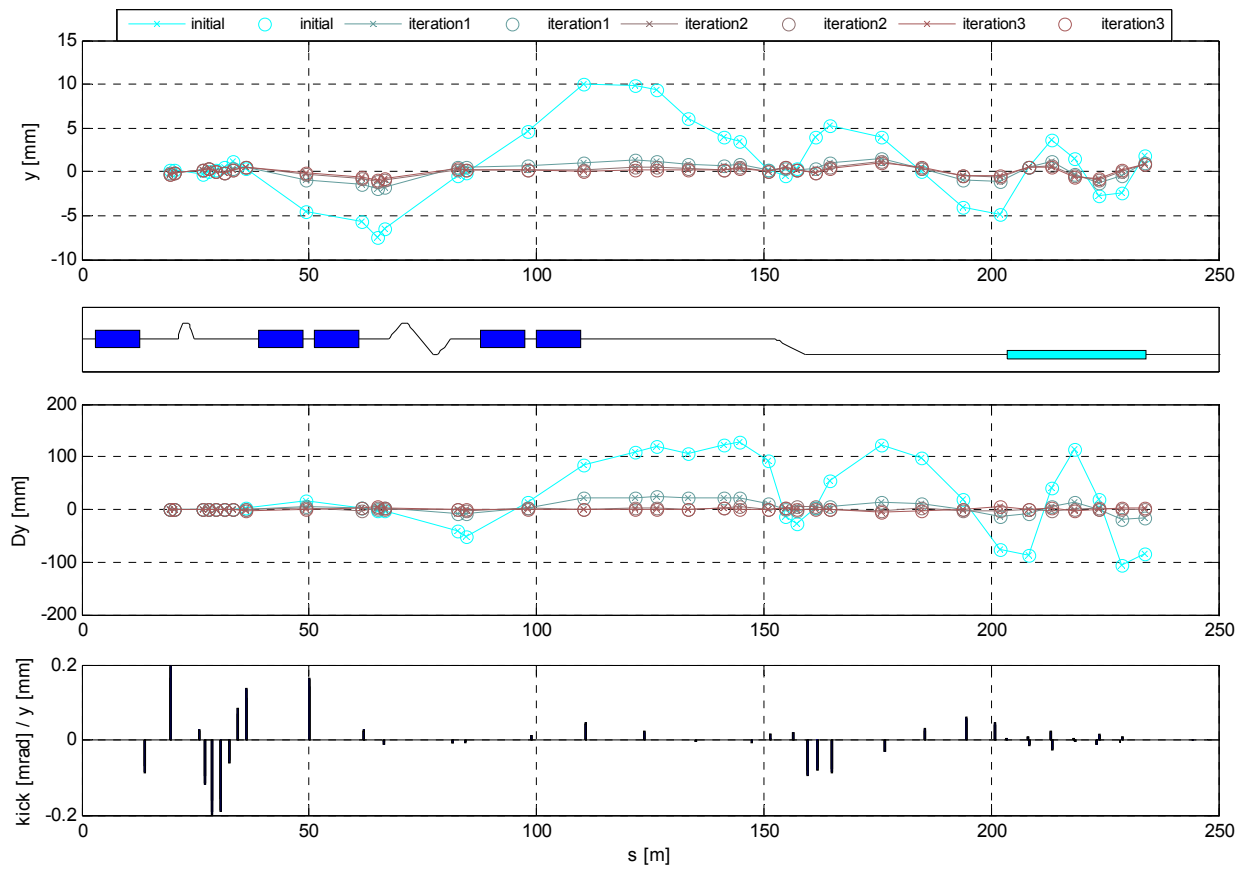
Basic set / BPM=15:20



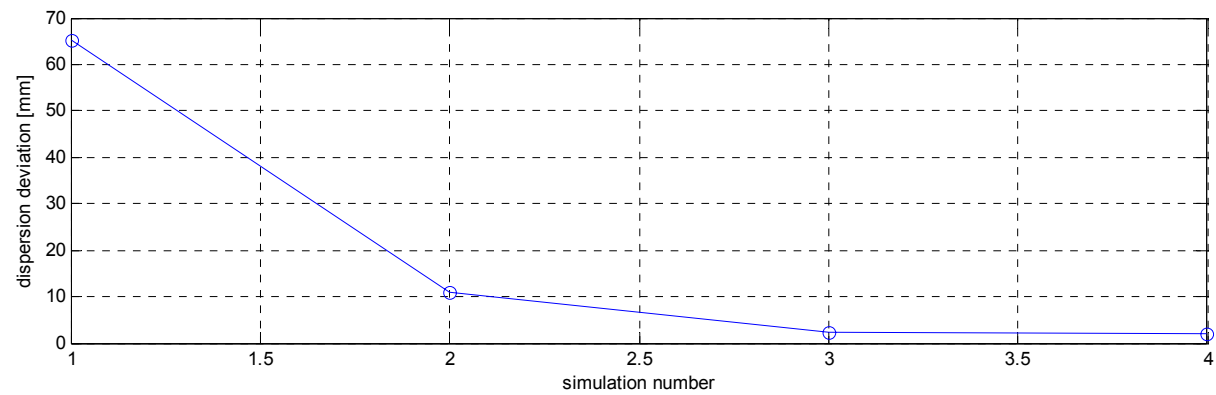
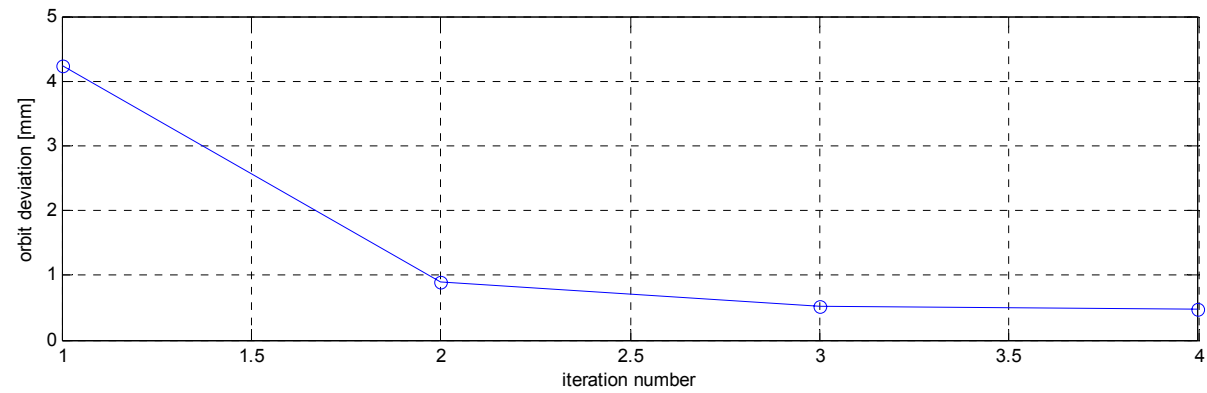
Basic set / BPM=15:20



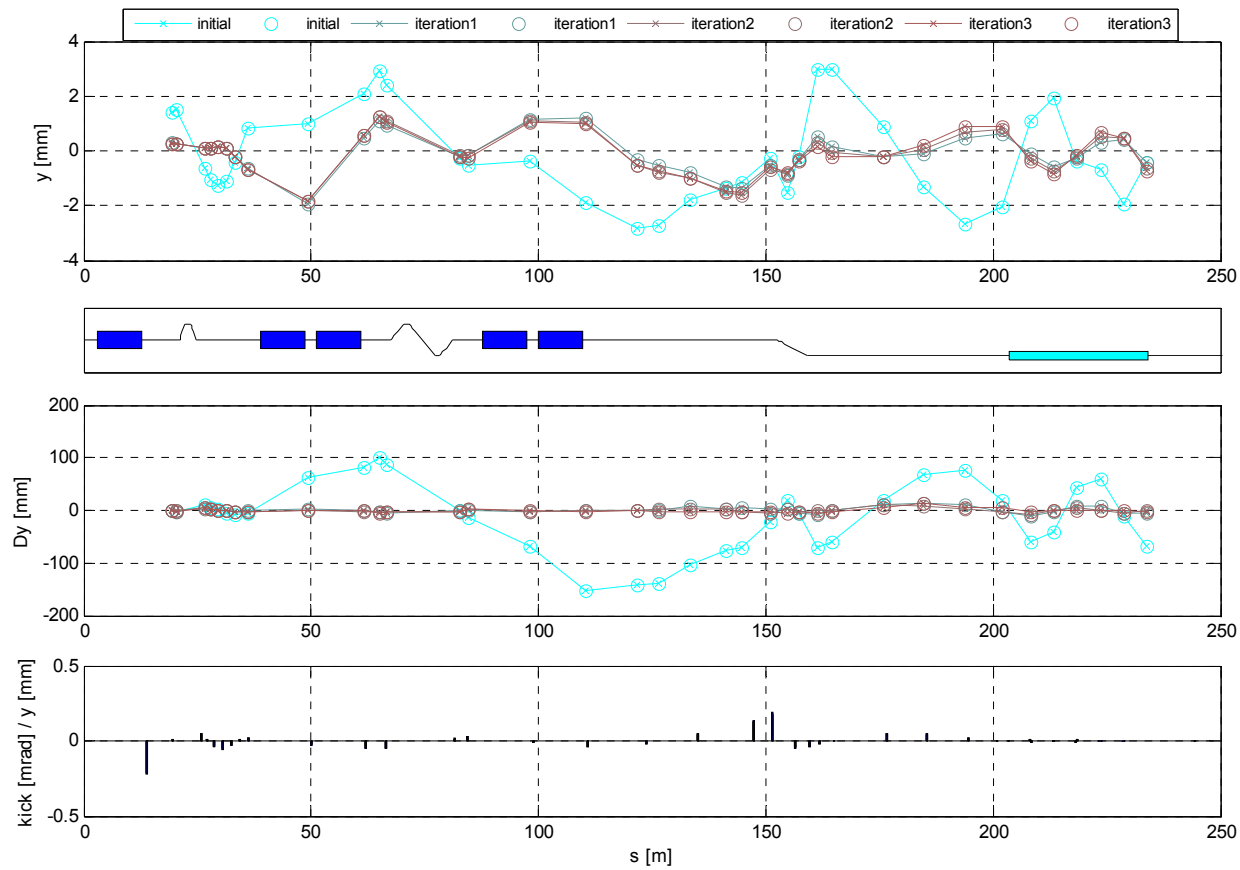
Basic set / All BPM's



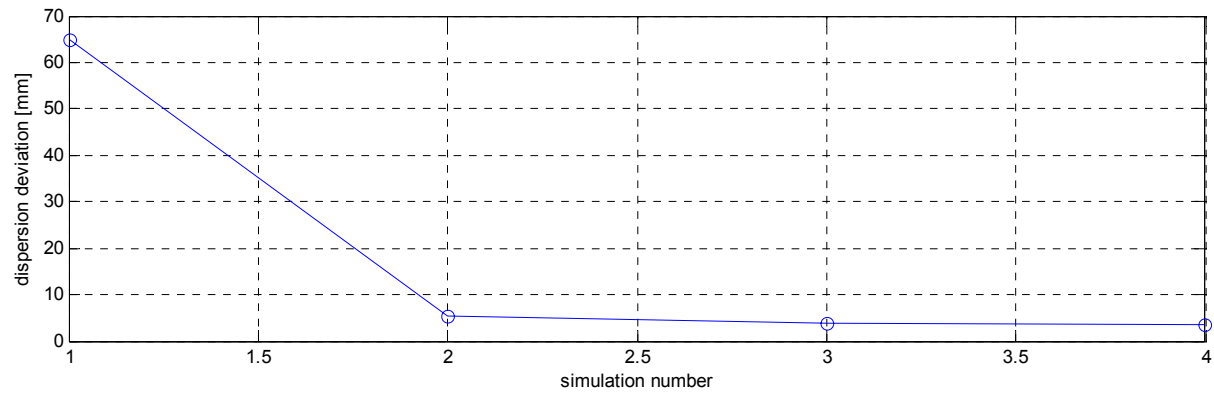
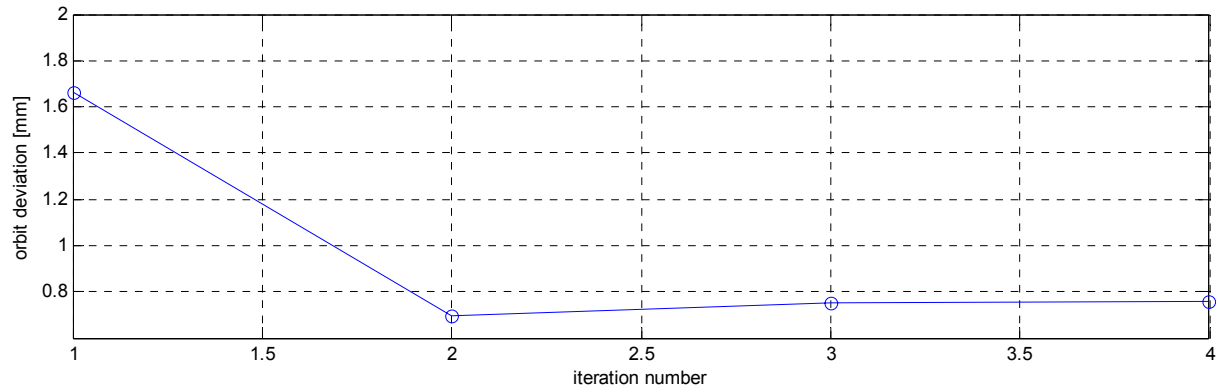
Basic set / All BPM's



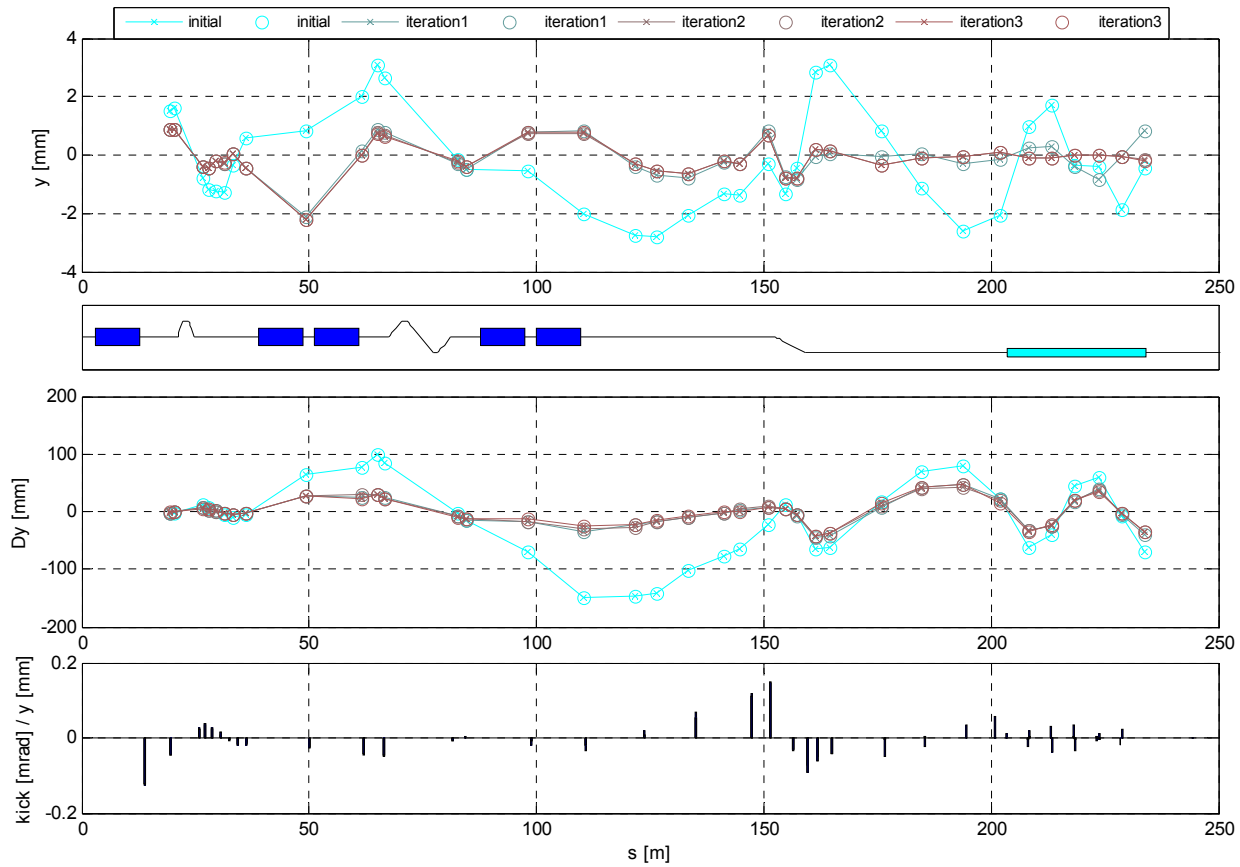
Basic set / All BPM's



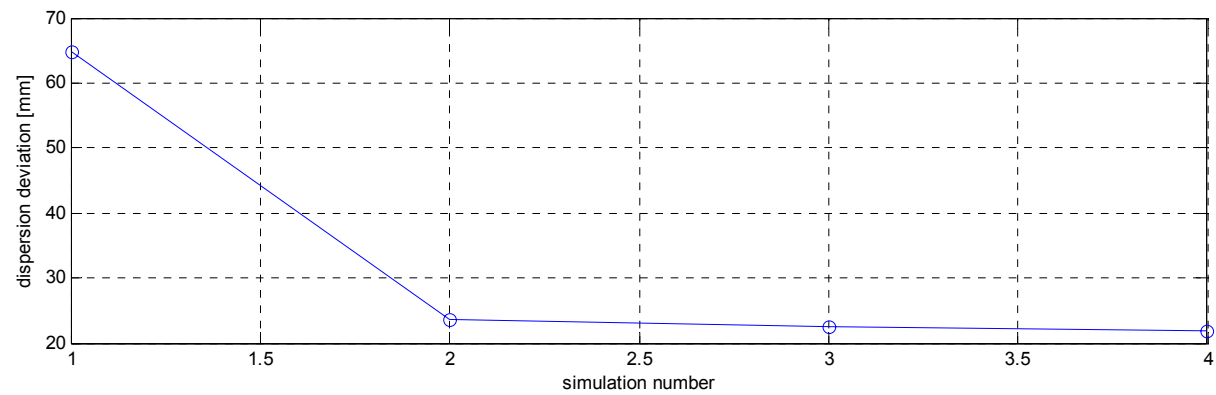
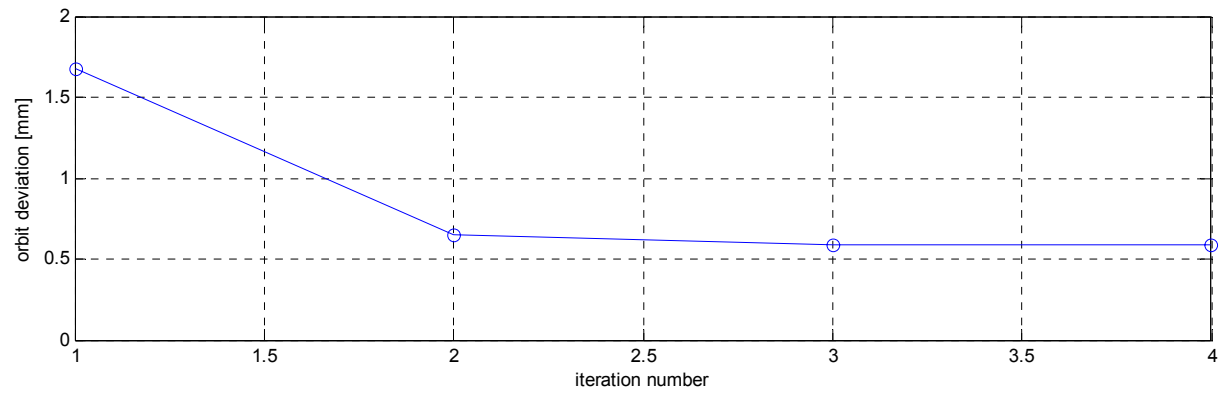
Basic set / All BPM's



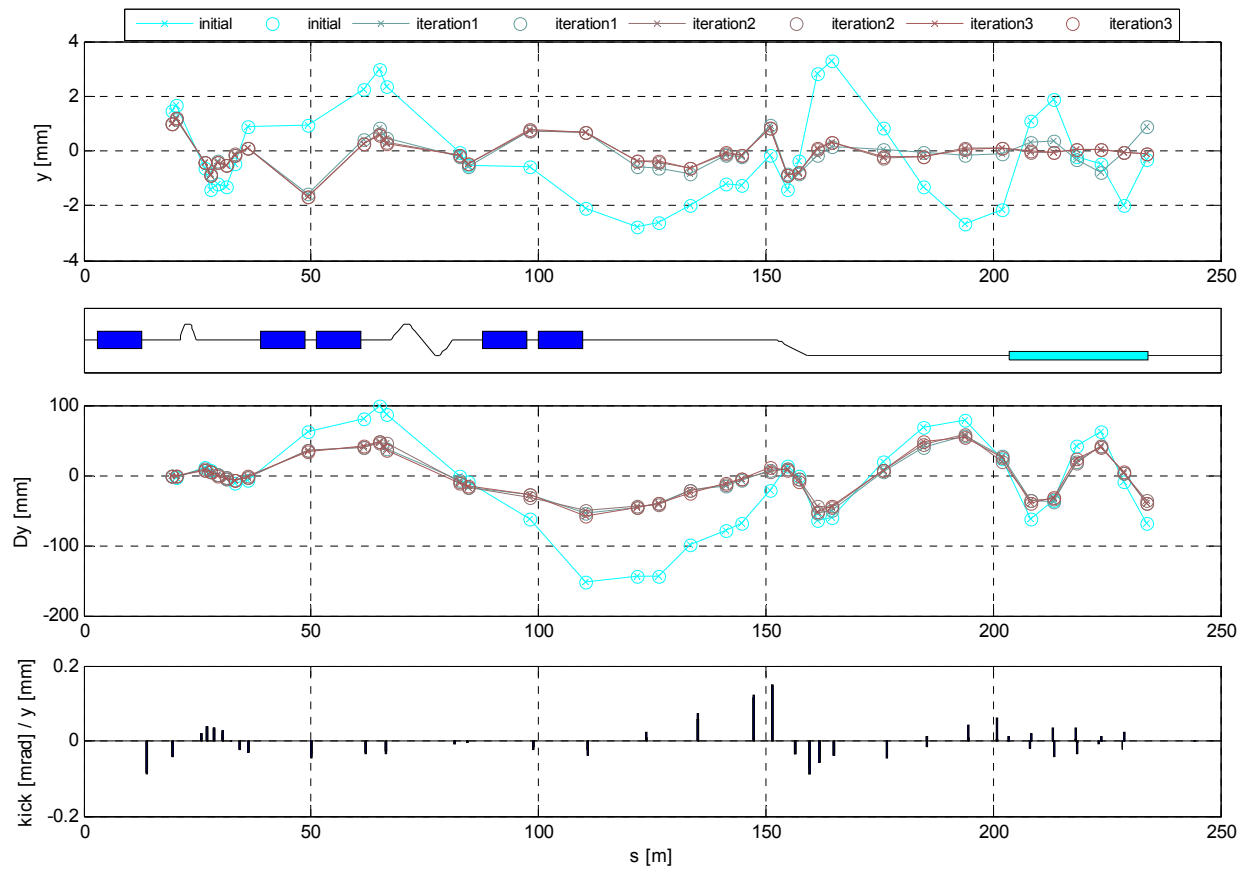
w=0.01 / All BPM's



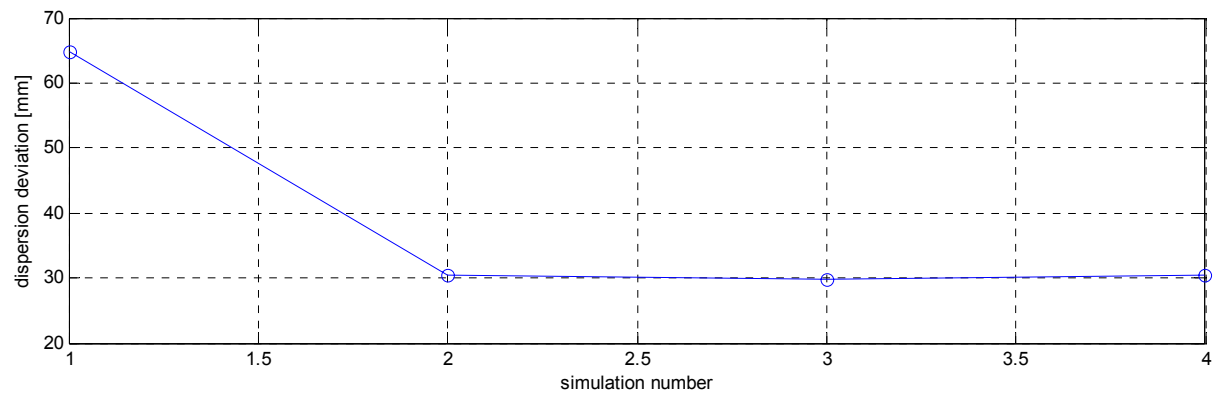
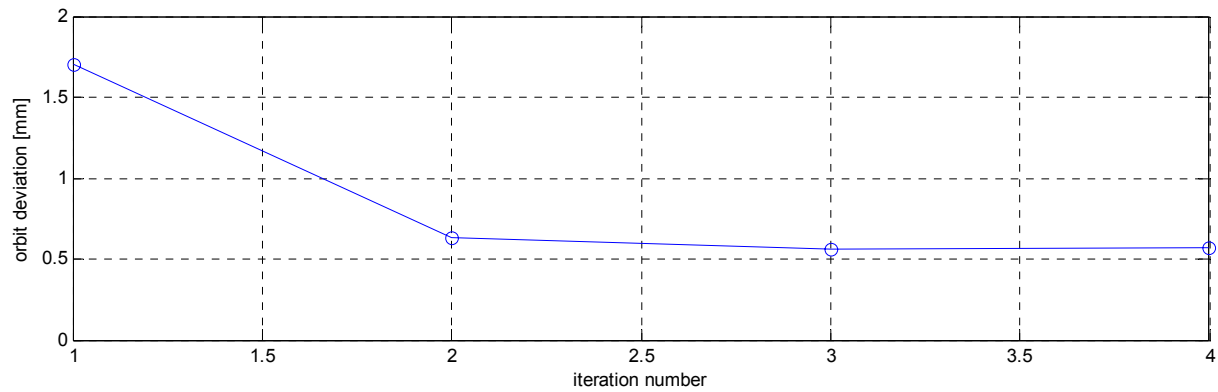
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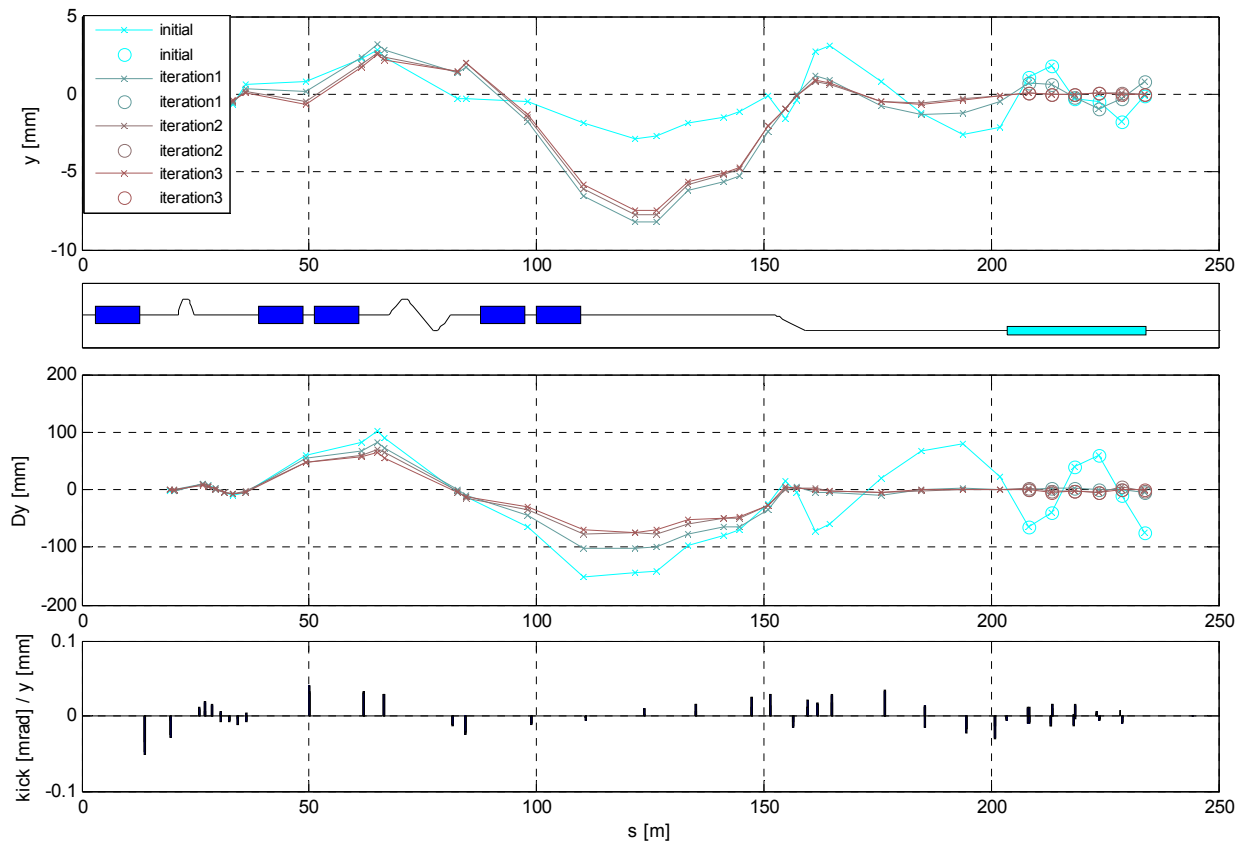
w=0.0 / All BPM's



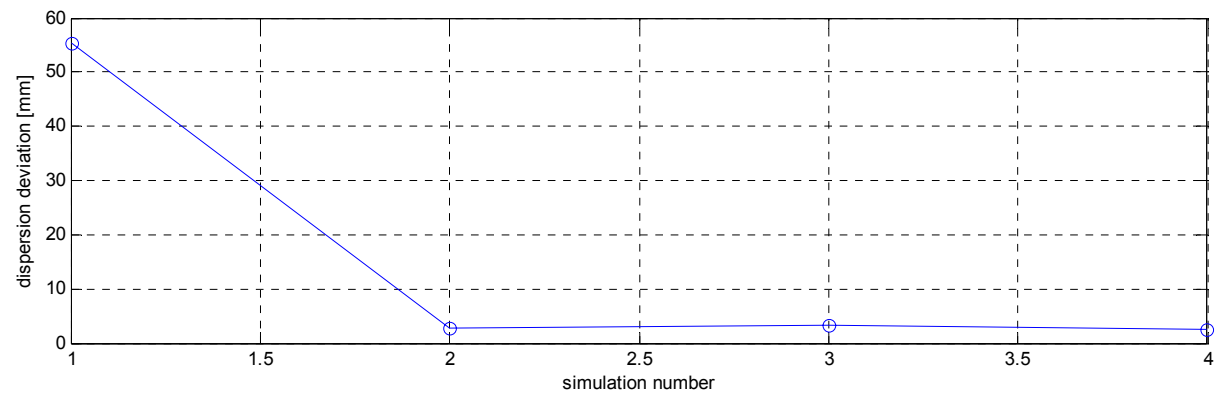
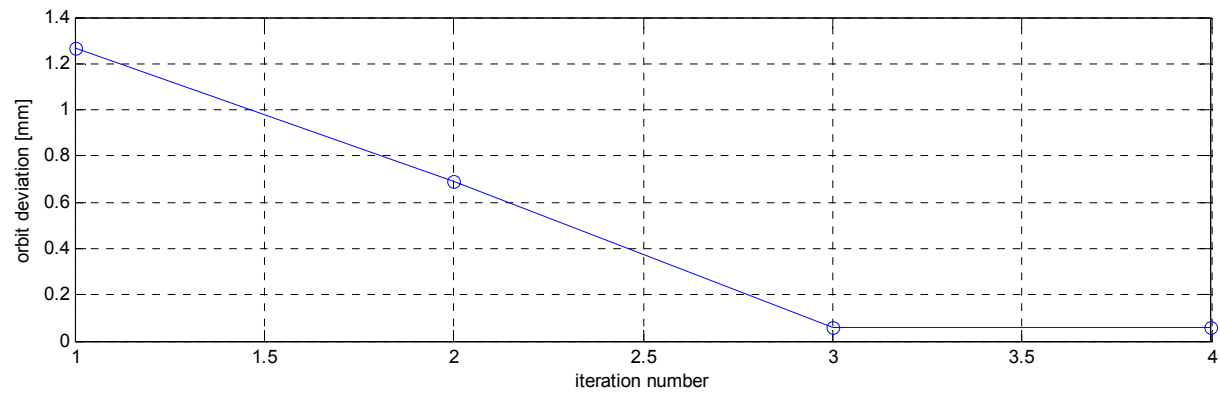
w=0.0 / All BPM's



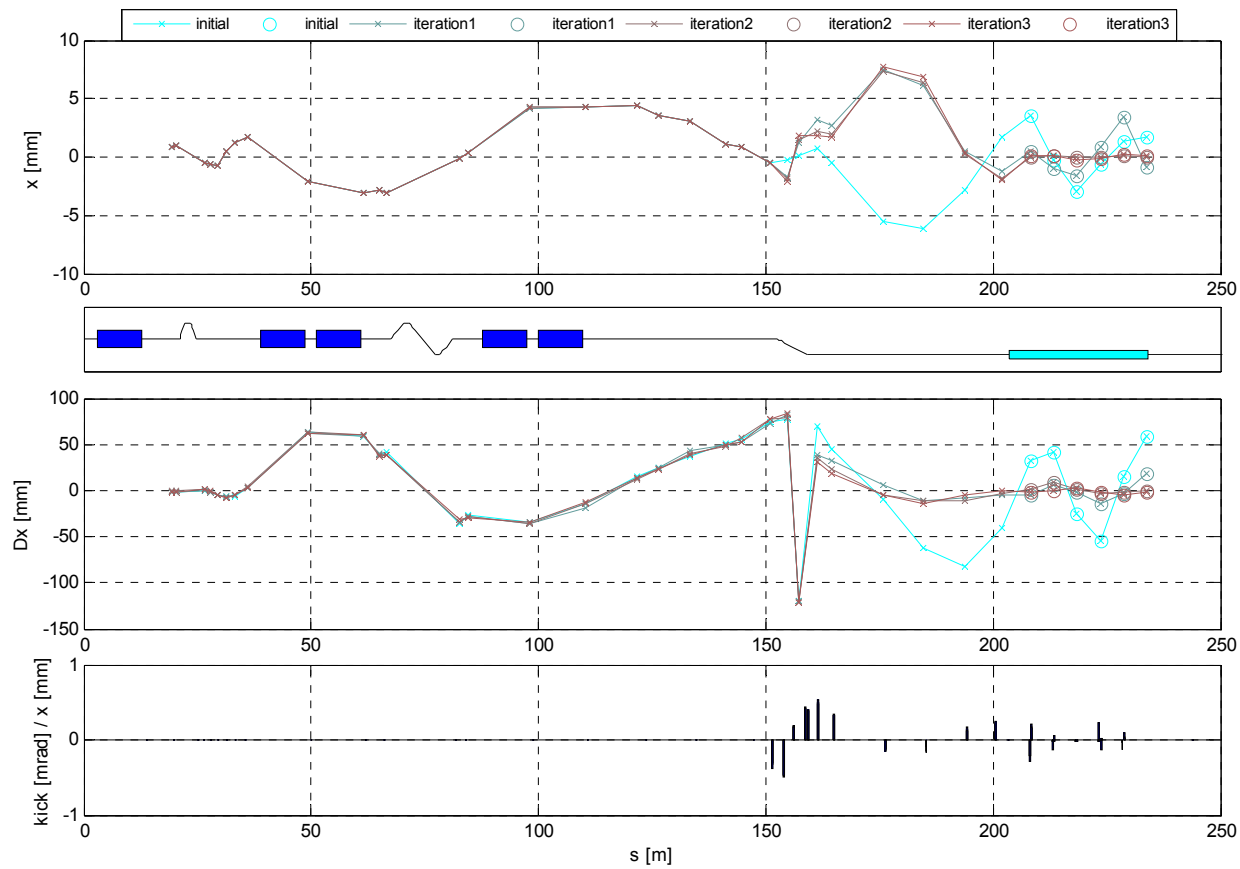
Basic set / undulator BPM's - all steerers



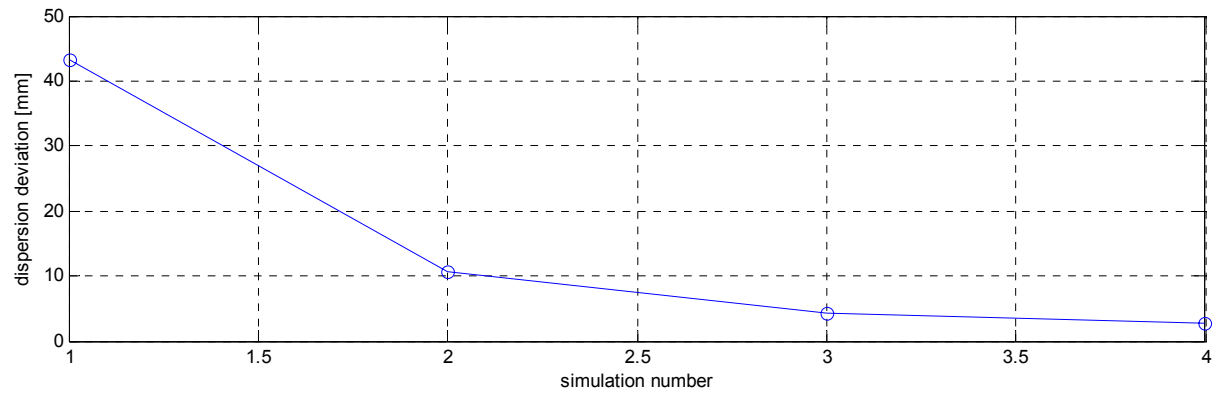
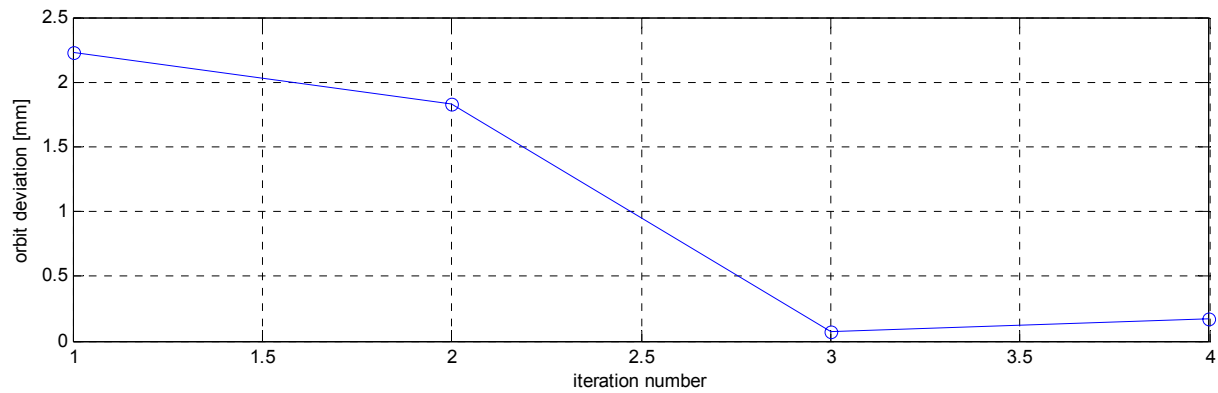
Basic set / undulator BPM's - all steerers



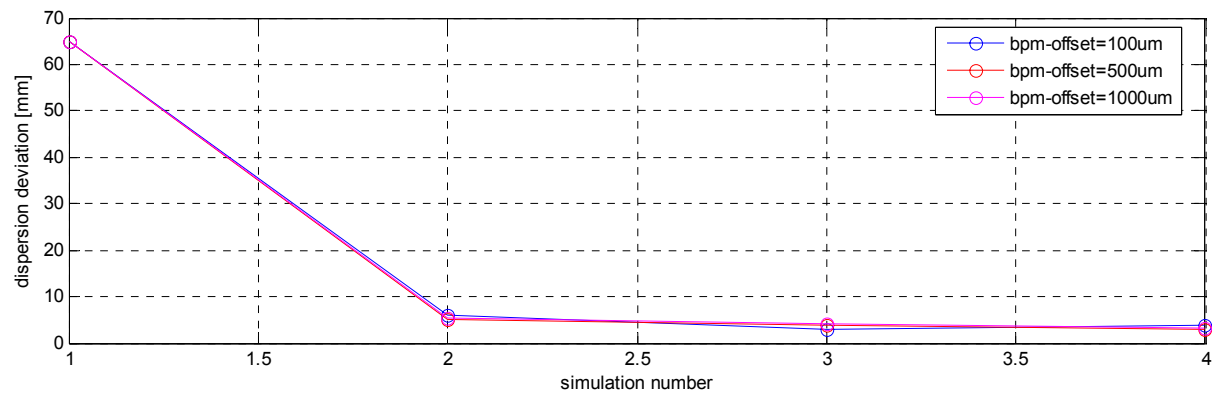
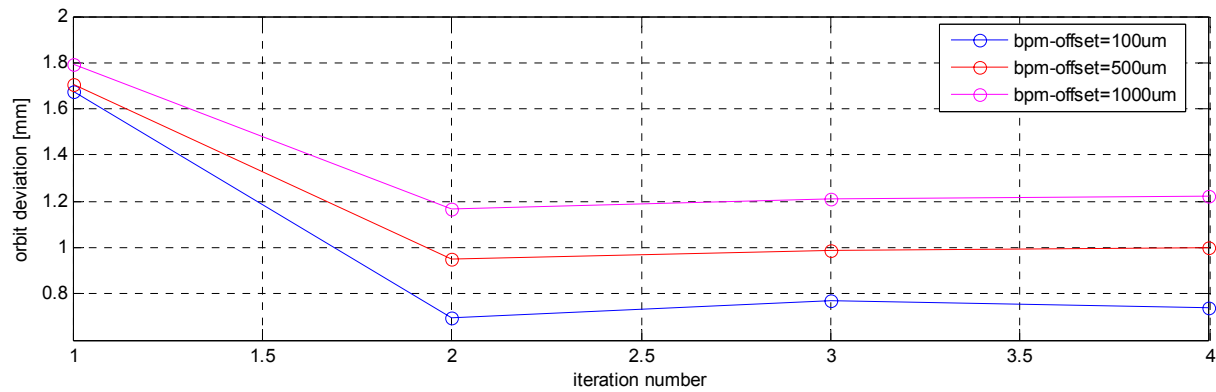
Basic set / undulator BPM's -steerers 20:end



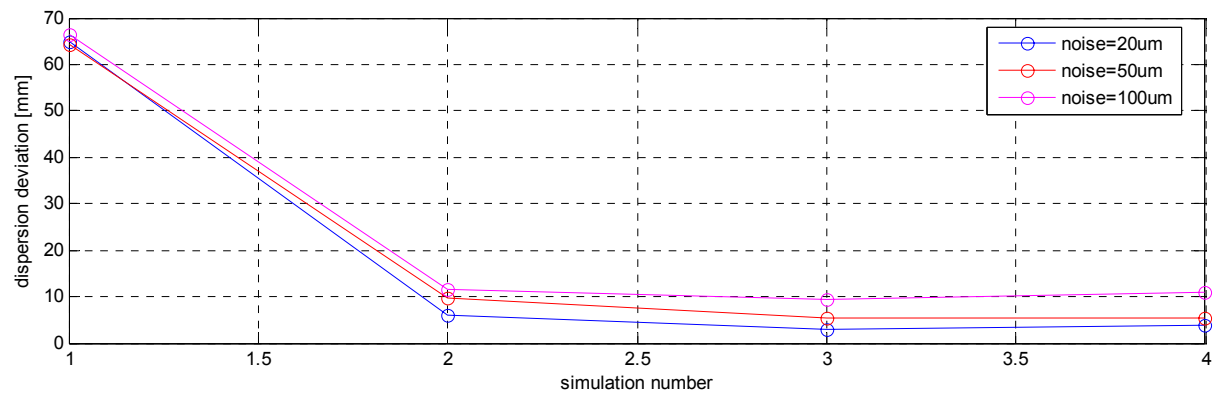
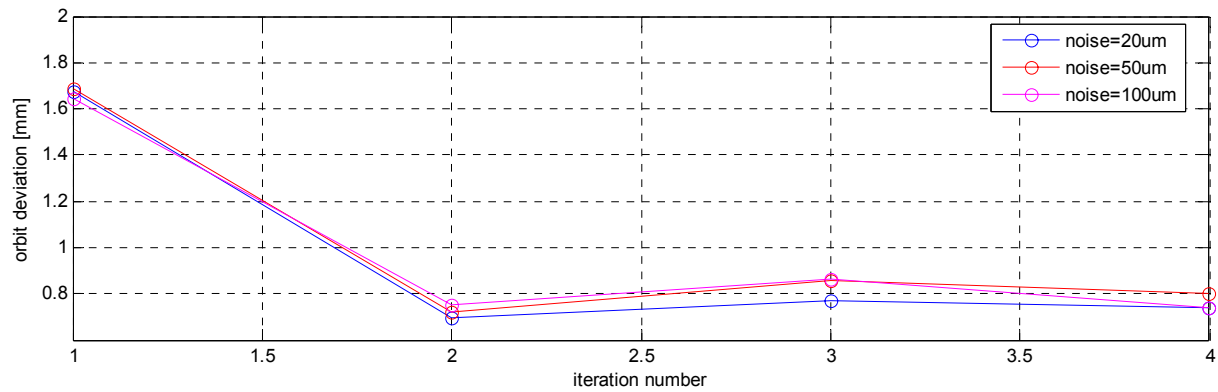
Basic set / undulator BPM's - steerers 20:end



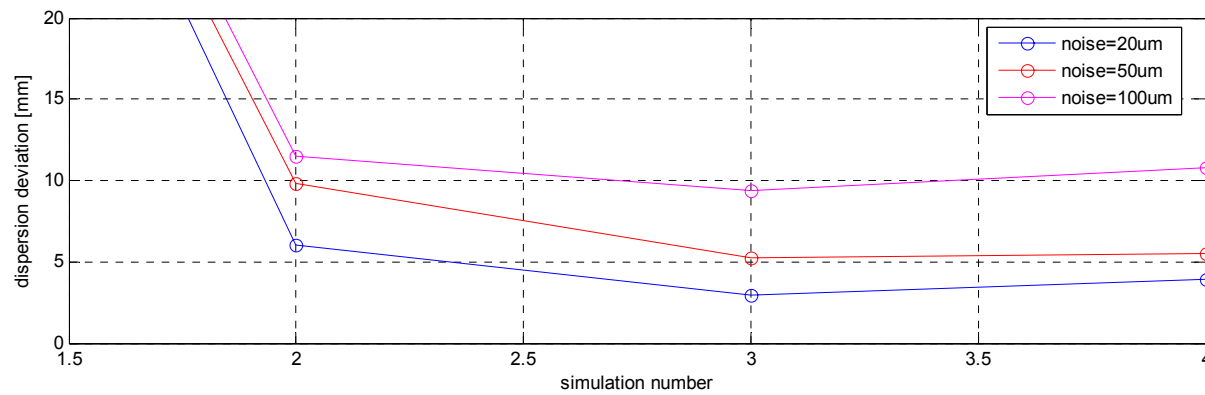
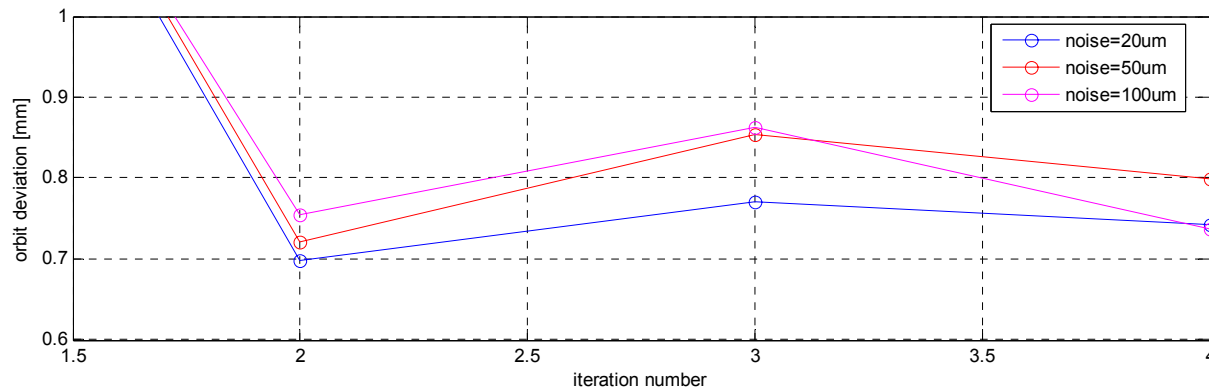
Sensitivity to BPM off-sets



Sensitivity to BPM noise



Sensitivity to BPM noise All BPM's



Summary/conclusions

- Dispersion correction simulation works properly
- Good results can be achieved in the undulator
- Next steps: include more effects, analyses sensitivity to more errors, adapt tool to real machine.

Thank you!