Coupler Kicks, CSR and Petra-Cavity

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Effect of Coupler Kicks before BC1from page 2

Spherical- and disc-bunch in shift-motion from page 8

Eigenmode Computation for Petra 7-cell cavity from page 15



Effect of Coupler Kicks before BC1





horizontal and vertical offset

no kicks

3 🖵 10⁻³ hor and vert offset, rms bunch length dogleg 2 BC0 LH 1 0 -1 -2 -3 -4 b 20 60 120 140 40 80 100 160







horizontal and vertical normalized projected emittance

no kicks







longitudinal phase space and top view

no kicks

with kicks: matched, 6 mm penetration depth



"top view"







effect of one corrector: horizontal and vertical offset

no kicks



effect of one corrector: emittances

no kicks



Question from 2012:

EM Field for some (predefined) Source Fields

field 2d object: solve 2d integral

a) stiff 2d object f.i. disc



b) time dependent 2d object



Gaussian spherical bunch in shift-motion

see: TESLA-FEL-2003-05

M. Dohlus, Two Methods for the Calculation of CSR Fields

Gaussian spherical bunch:
$$\rho_s(\mathbf{r}) = \frac{q}{(2\pi)^{3/2}\sigma^3} \exp\left(-\frac{1}{2}\frac{\|\mathbf{r}\|^2}{\sigma^2}\right)$$

"shift-motion":
$$\rho(\mathbf{r},t) = \rho_s(\mathbf{r} - \mathbf{r}_t(t))$$
,

$$\mathbf{J}(\mathbf{r},t) = \rho_{s}(\mathbf{r} - \mathbf{r}_{t}(t))\mathbf{v}_{t}(t)$$

for arbitrary trajectory: $\mathbf{r}_t(t)$

$$\Phi(\mathbf{r},t) = \frac{1}{4\pi\varepsilon} \int \frac{\rho(\mathbf{r}',t')}{\|\mathbf{r}-\mathbf{r}'\|} dV' = \frac{q}{\varepsilon(2\pi)^{3/2}\sigma^2} \int_{0}^{\infty} f\left(\frac{r'}{\sigma},\frac{R(r',\mathbf{r},t)}{\sigma}\right) dr'$$
1D integration



1D integration
$$\Phi(\mathbf{r},t) = \frac{q}{\varepsilon(2\pi)^{3/2}\sigma^2} \int_0^{\infty} f\left(\frac{r'}{\sigma},\frac{R(r',\mathbf{r},t)}{\sigma}\right) dr'$$

with
$$f(a,b) = \exp\left(-\frac{a^2 + b^2}{2}\right) \frac{\sinh(ab)}{b}$$

 $R(r',\mathbf{r},t) = \left\|\mathbf{r} - \mathbf{r}_t \left(t - r'/c\right)\right\|$

vector potential and E-, B-fields correspondingly

needs some skill in analysis

as
$$\mathbf{B}(\mathbf{r},t) = \frac{q\mu}{(2\pi)^{3/2}\sigma^3} \int_0^{\infty} \mathbf{n} \times \mathbf{v} \, \widetilde{f}\left(\frac{r'}{\sigma}, \frac{R(r',\mathbf{r},t)}{\sigma}\right) dr'$$

with $\widetilde{f}(a,b) = \frac{\partial}{\partial b} f(a,b)$



example: 4-magnet bunch compressor chicane



longitudinal and transverse component of Lorenz-force, In bunch center, along trajectory





1D integration needs some skill in numerical computation

a) boundaries

$$\Phi(\mathbf{r},t) = \frac{q}{\varepsilon (2\pi)^{3/2} \sigma^2} \int_{0}^{t} f\left(\frac{r'}{\sigma}, \frac{R(r',\mathbf{r},t)}{\sigma}\right) dr'$$

$$r_{\min}$$

search problem "find retarded source"

b) complicated integrand: sharp spikes or long weak tails

adaptive integrator

c) simultaneous integrations of all quantities and components

vector integrator

adaptive vector integrator: VASimps (needs definition of a scalar error function)



Uniform disc bunch in shift-motion

uniform disc bunch: $\rho_d(\mathbf{r}) = q \delta(z) \psi(\mathbf{r}_\perp)$

with
$$\psi(\mathbf{r}_{\perp}) = \frac{1}{\pi R^2} \begin{cases} 1 & \text{if } \|\mathbf{r}_{\perp}\| \le R \\ 0 & \text{otherwise} \end{cases}$$

"shift-motion":
$$\rho(\mathbf{r},t) = \rho_d(\mathbf{r} - \mathbf{r}_t(t))$$

 $\mathbf{J}(\mathbf{r},t) = \rho_d(\mathbf{r} - \mathbf{r}_t(t))\mathbf{v}_t(t)$

1D integration:

$$V(\mathbf{r},t) = \frac{1}{4\pi\varepsilon} \frac{q}{\pi R^2} \int_{0}^{\infty} f\left(\frac{r'}{R}, \frac{\mathbf{r} - \mathbf{r}_t(t - r'/c)}{R}\right) dr'$$



function:
$$f(a, \mathbf{b}) = \begin{cases} 0 & \text{if } a \leq |b_z| \\ g(\tilde{c}, d) & \text{otherwise} \end{cases}$$

$$\widetilde{c} = \|\mathbf{b}_{\perp}\|$$

$$d = \sqrt{a^2 - b_z^2}$$

$$\int_{0}^{1} \frac{g(\widetilde{c}, d)}{(1 - c_z)^2 - c_z^2} \int_{0}^{1} \frac{1 - c_z^2 - d^2}{2cd} \int_{0}^{1} \frac{1 - c_z^$$

derivatives include Dirac-function



Eigenmode Computation for Petra 7-cell cavity

compare: DESY M-84-006

T. Weiland, On the numerical solution of Maxwell's equations and applications in the field of accelerator physics







http://mhf-e.desy.de/e5/e63/ --> Datenblätter / Data Sheets Data Sheet 500MHz 7-Cell Cavity





input coupler waveguide transition, doorknob

tuning plunger

cavity pick-up loop (Messschleife)



http://mhf-e.desy.de/e5/e63/

--> Übersichtszeichnungen / Overview Drawings

7-Cell Cavity, Type PETRA (7-zelliges 500-MHz Cavity)



Flansche fir Feinabstimmungen FA und

··· umpen GP in Zeichenebene gedreht.







http://mhf-e.desy.de/e5/e63/

--> Übersichtszeichnungen / Overview Drawings

7-Cell Cavity, Type PETRA (7-zelliges 500-MHz Cavity) Input Coupler and Waveguide Transition (Einkopplung mit Übergang) Tuning Plunger (Feinabstimmung, Abstimmstempel) Cavity Pick-Up Loop (Messschleife)



