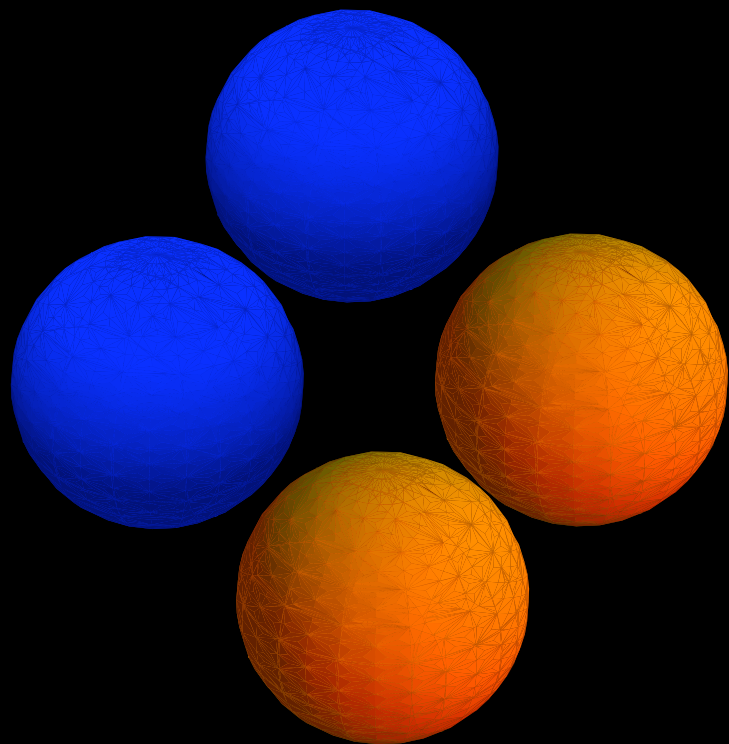


Hints of a 4-quark Spectroscopy

AD Polosa, INFN Roma



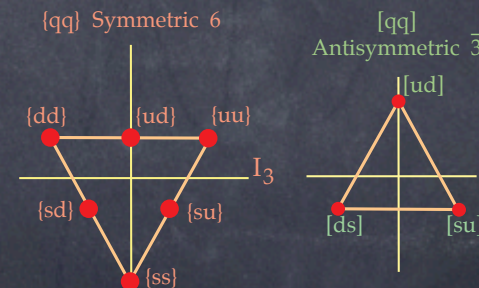
Hints of a 4-quark Spectroscopy

AD Polosa, INFN Roma

Why diquarks?

- diquarks are **bound states** in color **anti-triplet channel**: 3^* (lattice, group-theory arguments and $x \rightarrow 1$ DIS)
- a **diquark-anti-diquark** (dq-adq) state is bound by **color forces**
- spin 0 (the `good` ones)** diquarks are 3_f . The spin 1 are less bound (Sakharov Λ - Σ puzzle) :: 6_f .
- the exotic spectrum is reduced because $3 \times 3^* < 3 \times 3 \times 3^* \times 3^*$:: **crypto-exotic light scalar hadrons**

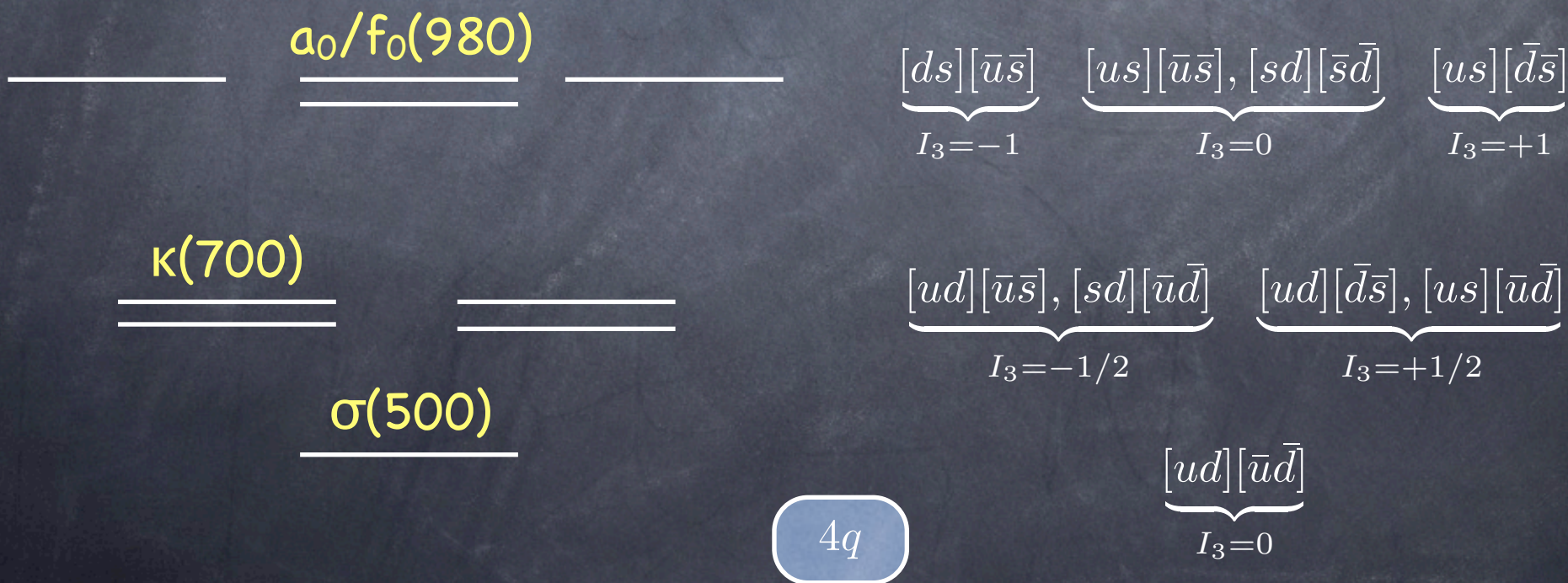
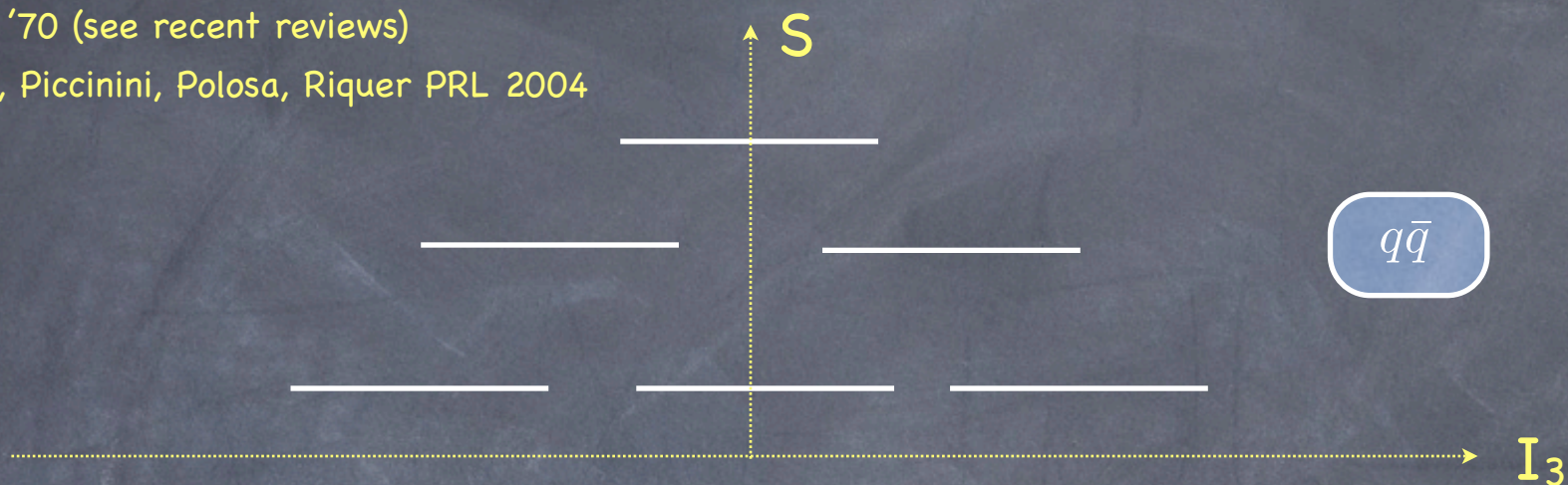
$$[qq]_{ia}^{\text{good}} = \epsilon_{ijk}^{(\text{col})} \epsilon_{abc}^{(\text{flav})} (-i\sigma_2)_{rt} q_r^{jb} q_t^{kc}$$

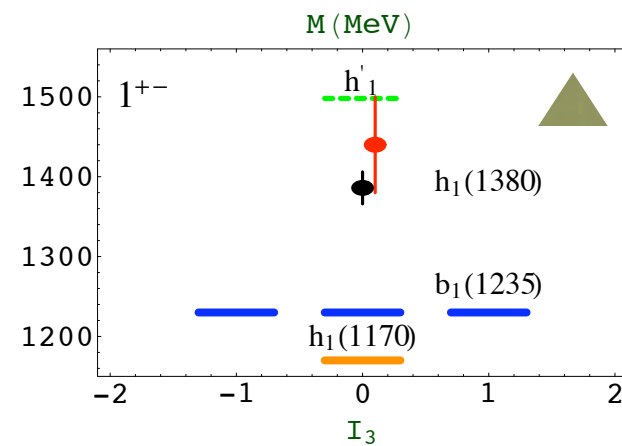
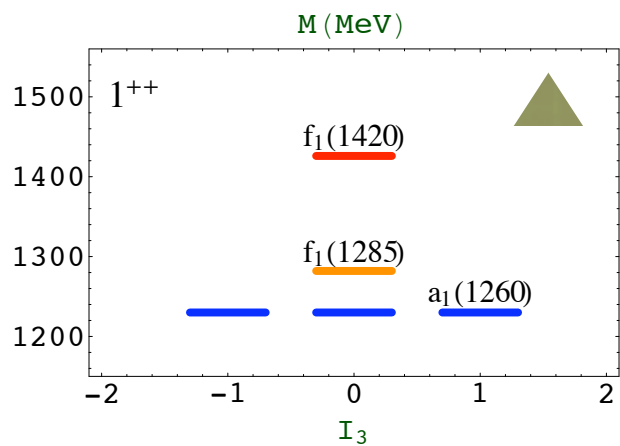
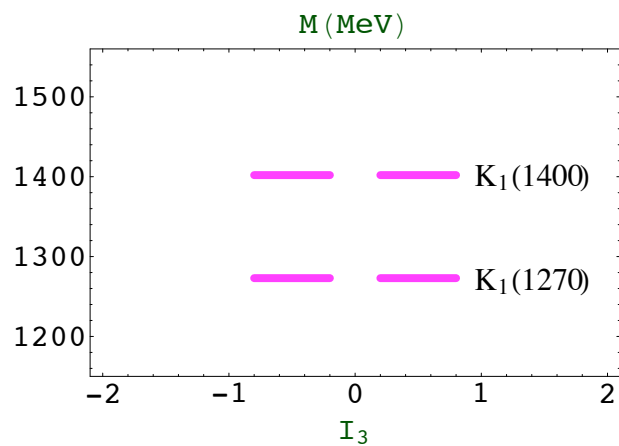
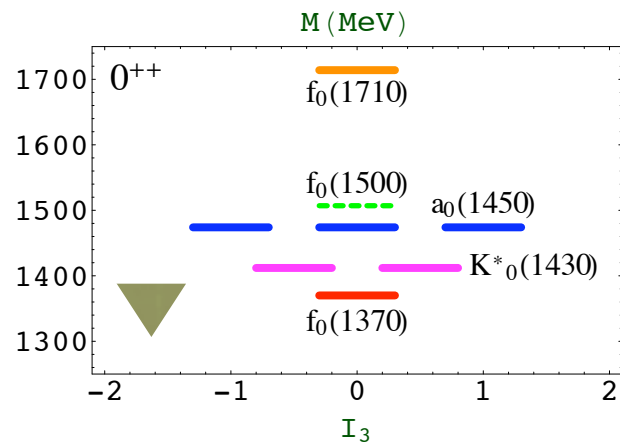
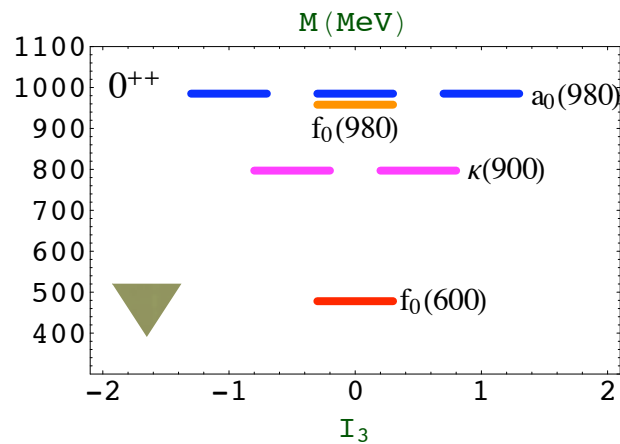
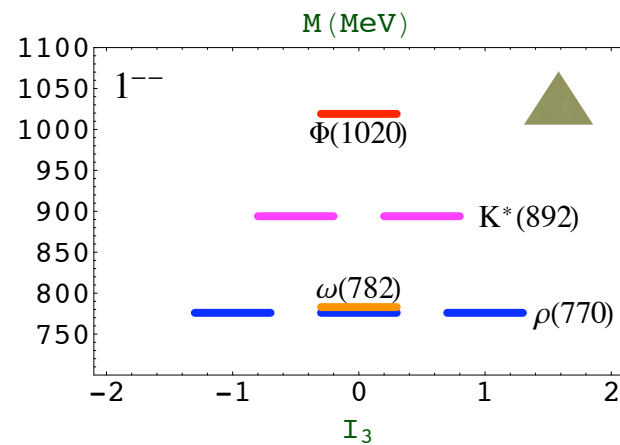
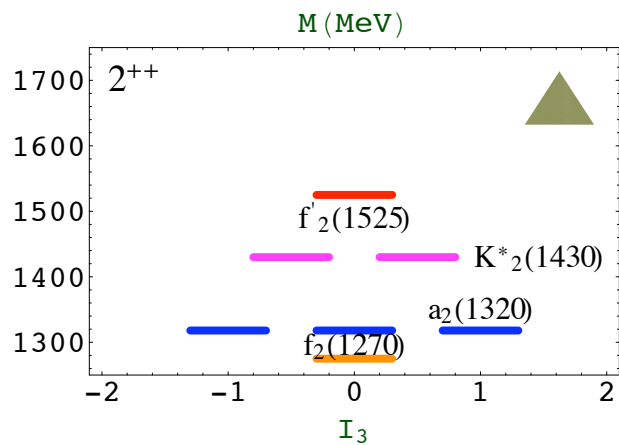
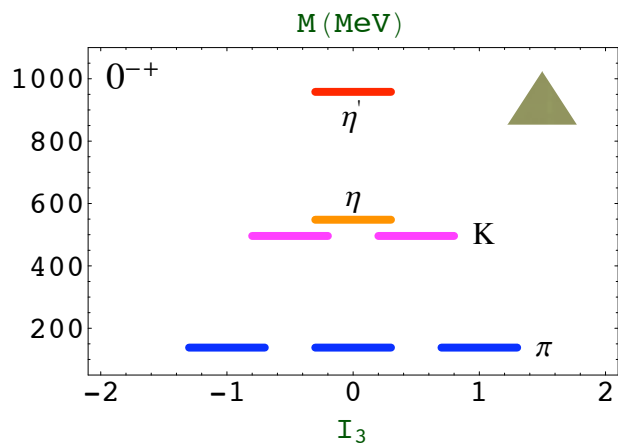


The inverted mass spectrum

Jaffe, '70 (see recent reviews)

Maiani, Piccinini, Polosa, Riquer PRL 2004





Scalars from Theory

(1) Caprini, Colangelo, Leutwyler PRL 2005 -- the sigma

(2) Descotes-Genon, Moussallam EPJC 2006 -- the kappa

Partial wave S-matrix elements are real-analytic

$$S^*(s) = S(s^*)$$

and from unitarity

$$S(s) = 1/S(s^*)$$

zeroes from the first sheet \rightarrow poles on the second

Dispersion equation analysis of $\pi\pi$ scattering in S-wave indicate a broad **resonance** around **500 MeV**

(1)

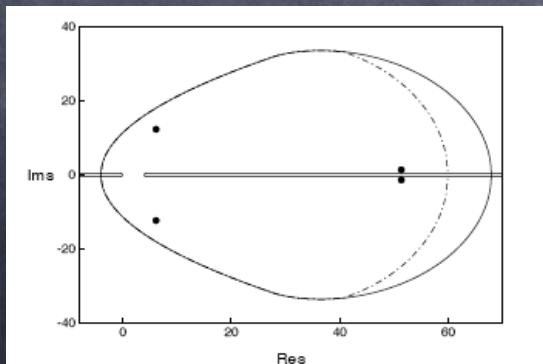
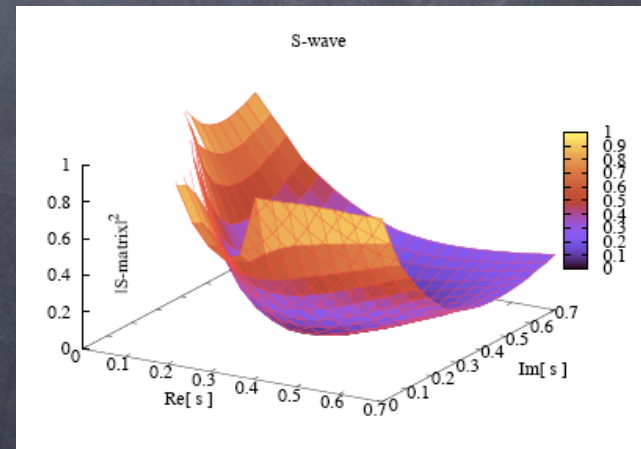


FIG. 2: Domain of validity of the Roy equations.

(2)



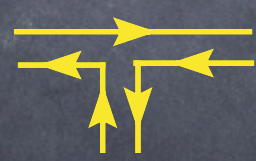
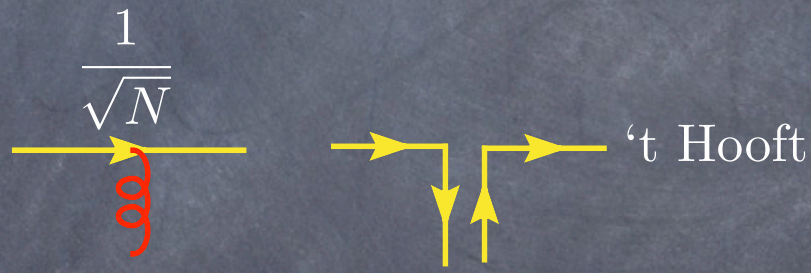
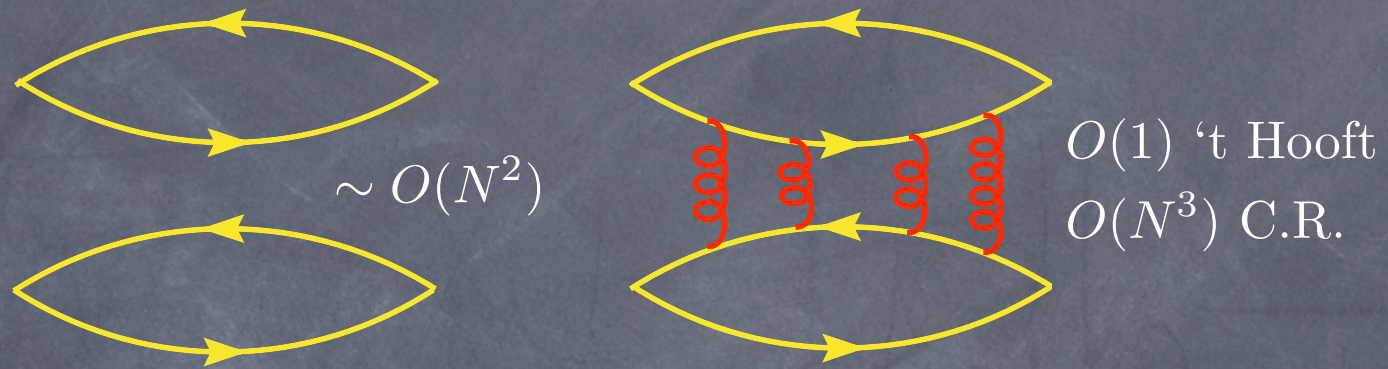
Can dq - adq hadrons exist?

In the 't Hooft large N limit they do not exist since the leading term in the $1/N$ expansion of any two-point correlation function of a 4 - q operator is a disconnected graph

But:

1. $N=3$
2. other large N limits exist (Carrigan-Ramond) where the quark is in the 3^*

in diagrams...



Carrigan – Ramond

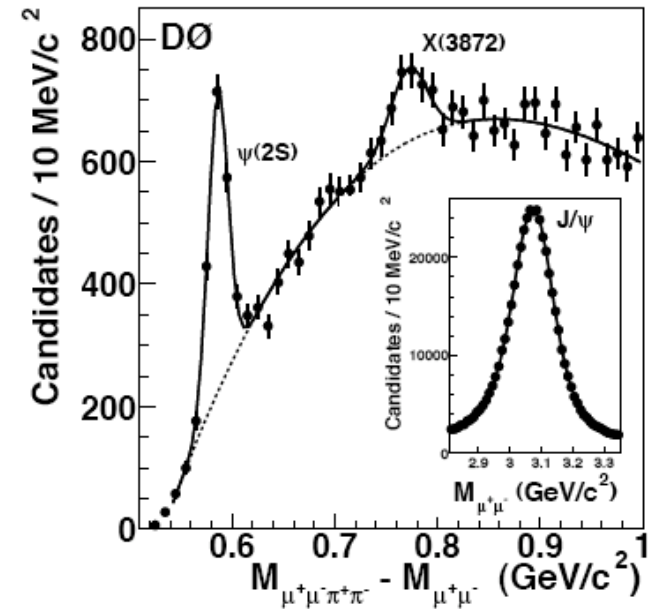
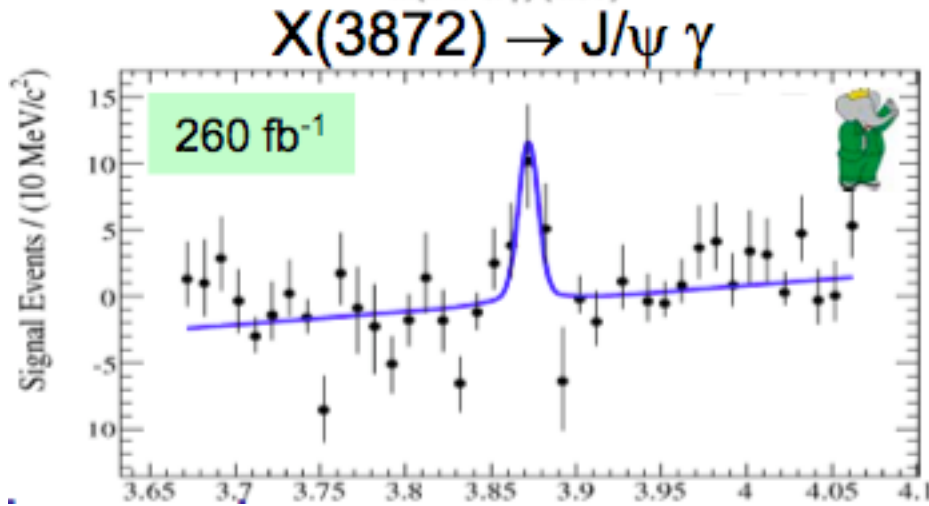
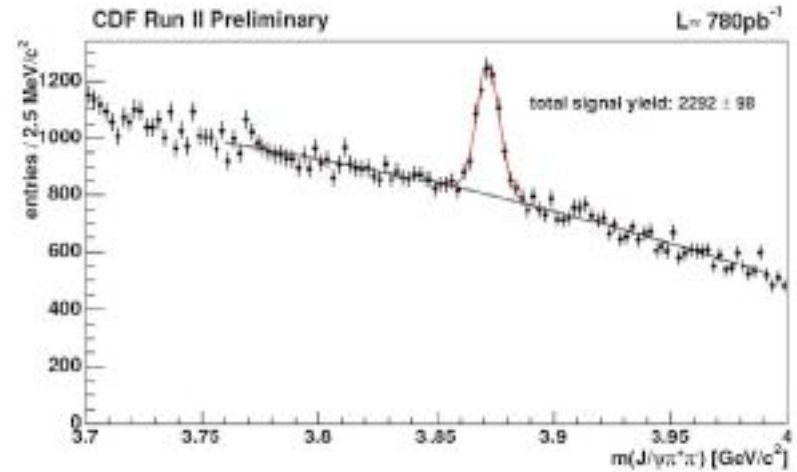
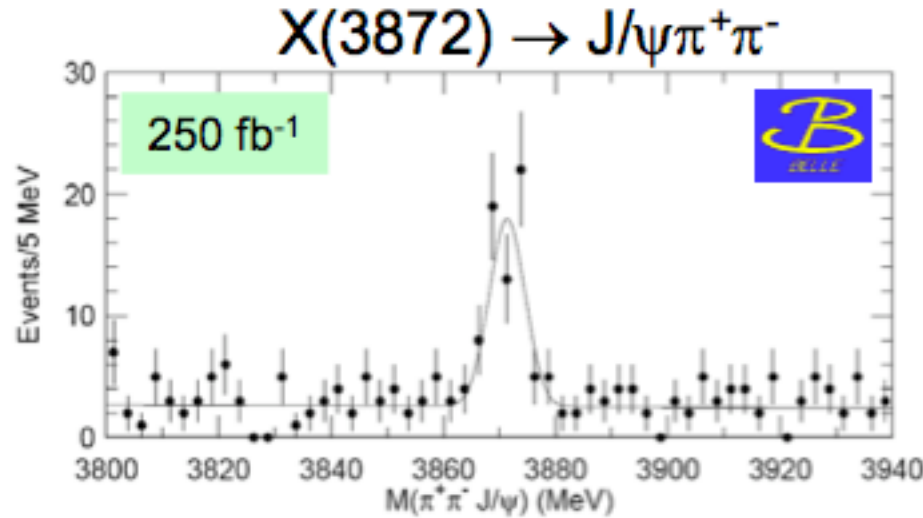
Stems from the fact that there are no color singlets made up of 3 fermions (baryons) for $N > 3$. C-G introduce quarks and 'larks' transforming as N and $1/2 N(N-1)$ of $SU(N)$ respectively. In $SU(3)$, a lark=antiquark. In $SU(N)$ a baryon is a qqL^* .

dq-adq :: where else?

- For some time they played a role to understand the so called **pentaquark** baryons (Wilczek & Jaffe)
- The newly discovered **X,Y,Z** particles [Belle & BaBar].

$$B^\pm \rightarrow K^\pm \underbrace{\pi^+ \pi^- J/\psi}_{X \rightarrow \rho J/\psi}$$

$$pp \rightarrow X \rightarrow \underbrace{\pi^+ \pi^- J/\psi}_{X \rightarrow \rho J/\psi}$$



$$X \rightarrow \gamma J/\psi \mapsto C = +1 \quad \text{and} \quad X \rightarrow \rho^0 J/\psi \rightarrow (\pi^+ \pi^-)_S J/\psi \mapsto P = 1$$

X(3872) is a 1^{++} state

Is this compatible with a good dq-adq structure?

NO!

We need bad, spin 1 diquarks

But bad diquarks are less bound (lattice)...

Anyway X must contain charm quarks!

$$\text{spin - spin interactions} \sim \frac{1}{m_Q}$$

Building the states (L=0)

J^{PC}	wave functs.
0^{++}	$[cq]_0[\bar{c}\bar{q}]_0 \vee ([cq]_1[\bar{c}\bar{q}]_1)_0$
1^{++}	$\frac{[cq]_1[\bar{c}\bar{q}]_0 + [cq]_0[\bar{c}\bar{q}]_1}{\sqrt{2}}$
1^{+-}	$\frac{[cq]_1[\bar{c}\bar{q}]_0 - [cq]_0[\bar{c}\bar{q}]_1}{\sqrt{2}} \vee ([cq]_1[\bar{c}\bar{q}]_1)_1$
2^{++}	$([cq]_1[\bar{c}\bar{q}]_1)_2$

$$([\]_s [\]_s)_J$$

Isospin & 2 * X(387_) states

We set in the flavor basis X_u, X_d

$$M = \begin{pmatrix} 2m_u & 0 \\ 0 & 2m_d \end{pmatrix} + \delta \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix}$$

where the mixing matrix has a diagonal structure in the Isospin $I = 0, 1$ basis, its eigenvectors being

$$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

At the charmonium scale we expect the annihilations to be small and quark mass to dominate :: *observed* $X \rightarrow \omega/\rho$ isospin breaking

$$\frac{\mathcal{B}(X \rightarrow \pi^+ \pi^- \pi^0 J/\psi)}{\mathcal{B}(X \rightarrow \pi^+ \pi^- J/\psi)} = 1.0 \pm 0.4 \pm 0.3$$

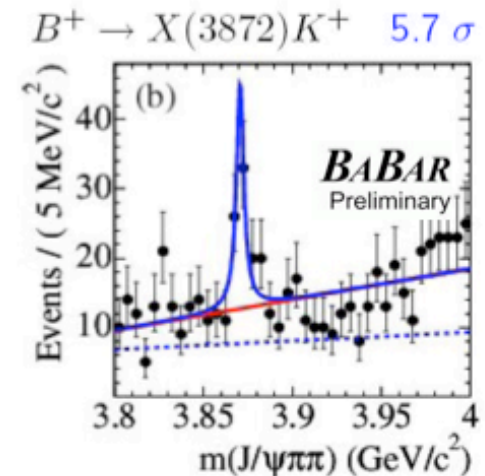
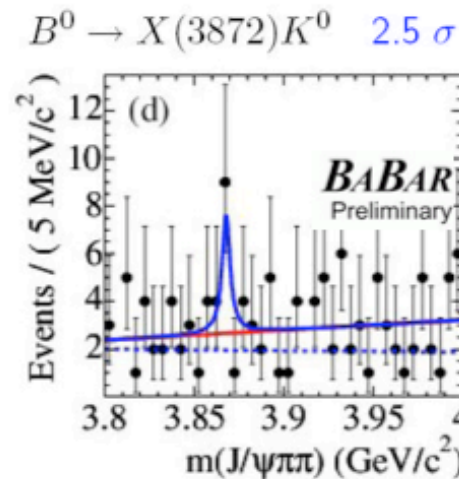
FIND THESE TWO X'S IN DATA

(MPPR '05)

A **MASS DIFFERENCE** $X_U - X_D$ OF ABOUT ~ 5 MEV WAS PREDICTED :: THEY COULD APPEAR IN B^+ AND B^0 SEPARATELY

$B^+ \rightarrow K^+ X_u$ with rate Γ_1
 $B^+ \rightarrow K^+ X_d$ with rate Γ_2
 suppose $\Gamma_1 \gg \Gamma_2 \triangleright \Gamma_4 \gg \Gamma_3$
 $B^0 \rightarrow K^0 X_u$ with rate Γ_3
 $B^0 \rightarrow K^0 X_d$ with rate Γ_4

Properties of the X(3872)



211 fb⁻¹

$$\left\{ \begin{array}{l} R = B^0/B^+ = 0.61 \pm 0.36 \pm 0.06 \\ \Delta m = 2.7 \pm 1.3 \pm 0.2 \text{ MeV}/c^2 \end{array} \right.$$



September 20, 2005

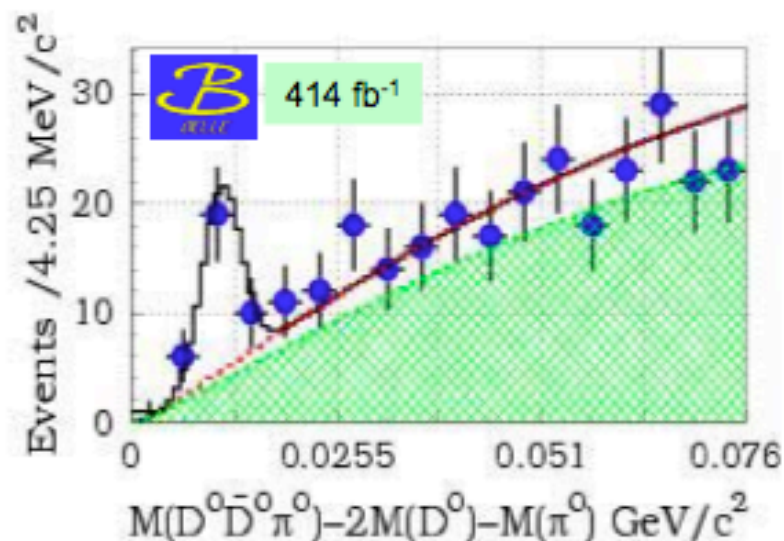
Milos Workshop



DIFFERENCE IN MASS FROM DATA **NOT SIGNIFICATIVE!**

X(3872): STILL SOME SURPRISES

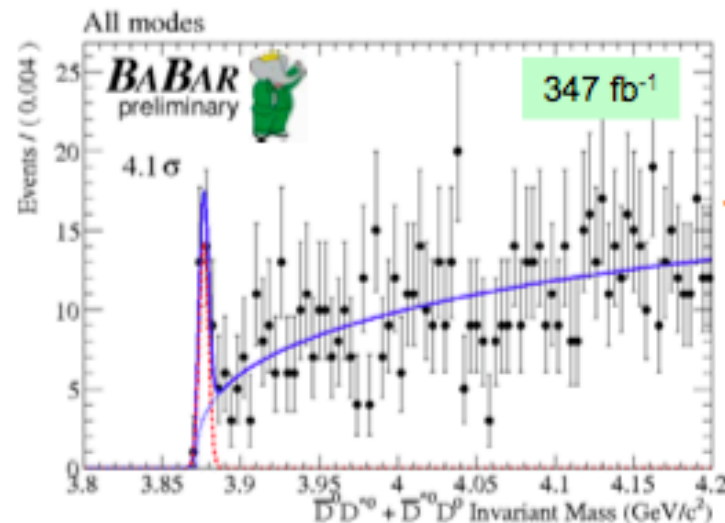
- Belle: looking at $B \rightarrow \bar{D}^0 D^0 \pi^0 K$



- Excess in the $\bar{D}^0 D^0 \pi^0$ invariant mass

- $M = 3875.4 \pm 0.7^{+1.2}_{-2.0}$ MeV/c²

- BaBar: looking at $B \rightarrow \bar{D}^0 D^{*0} K$
($D^{*0} \rightarrow D^0 \pi^0 / \gamma$)



New result
preliminary

- Excess in the $\bar{D}^0 D^{*0}$ invariant mass

- $M = 3875.6 \pm 0.7^{+1.4}_{-1.5}$ MeV/c²

- Masses between Belle and BaBar in good agreement
- 2.5 σ away from the X(3872) world average!
- If X(3872), $J^P = 2^+$ disfavored

$M(J/\psi \pi^+ \pi^-) = 3871.2 \pm 0.5$ MeV (World Average)

hep-ex/0606055

ARE THERE TWO DIFFERENT X PARTICLES?

(MAIANI, POLOSA, RIQUER PRL '07)

:: OUR **NEW** HYPOTHESIS: TWO X, GENERICALLY PRODUCED IN $B^{+,0}$::

$$X_u \equiv X \text{ state decaying into } D^0 \bar{D}^0 \pi^0 = X(3876)$$

$$X_d \equiv X \text{ state decaying into } J/\psi \pi^+ \pi^- = X(3872)$$

:: THE TWO NEUTRAL STATES IN THE 4Q-COMPLEX ::

$$X^+ = [cu][\bar{c}\bar{d}] \quad X^- = [cd][\bar{c}\bar{u}]$$

$$X_u = [cu][\bar{c}\bar{u}] \quad X_d = [cd][\bar{c}\bar{d}]$$

IT IS TRICKY THAT **X_D** TURNS OUT TO BE LIGHTER THAN **X_U**

(MAYBE ELECTROSTATICS IS RESPONSIBLE FOR THIS)

HOW FAR IS THIS PICTURE CONSISTENT WITH A FOUR QUARK MODEL?

HOWEVER, THE ASSUMPTION, THAT X_u AND X_d WOULD DECAY IN J WITH SIMILAR BRANCHING RATIOS WAS NOT JUSTIFIED AND THE EARLIER SCHEME IS SUPERSEDED BY THE ONE PRESENTED HERE.

A REMARKABLE FACT

$$\bar{b} + (u) \rightarrow \bar{c} + c\bar{s} + (u) + q\bar{q} \quad (\Delta I = 0)$$

(V)alence and (S)ea needed to build the final state Kaons :: observe that the inverted pattern with B^0 was already observed in our first paper

$$\mathcal{A}(B^+ \rightarrow K^+ X_u) = V + S = \mathcal{A}(B^0 \rightarrow K^0 X_d)$$

$$\mathcal{A}(B^+ \rightarrow K^+ X_d) = V = \mathcal{A}(B^0 \rightarrow K^0 X_u)$$

$$\mathcal{A}(B^+ \rightarrow K^0 X^+) = S = \mathcal{A}(B^0 \rightarrow K^+ X^-)$$

AS A CONSEQUENCE WE HAVE

$$\begin{aligned} \left(\frac{B^0}{B^+}\right)_{J/\psi} &= \frac{\mathcal{B}(B^0 \rightarrow K^0 X_d)\mathcal{B}(X_d \rightarrow J/\psi\pi^+\pi^-)}{\mathcal{B}(B^+ \rightarrow K^+ X_d)\mathcal{B}(X_d \rightarrow J/\psi\pi^+\pi^-)} = \frac{\mathcal{B}(B^0 \rightarrow K^0 X_d)}{\mathcal{B}(B^+ \rightarrow K^+ X_d)} = \\ &= \frac{\mathcal{B}(B^+ \rightarrow K^+ X_u)}{\mathcal{B}(B^0 \rightarrow K^0 X_u)} = \frac{\mathcal{B}(B^+ \rightarrow K^+ X_u)\mathcal{B}(X_u \rightarrow D\bar{D}\pi)}{\mathcal{B}(B^0 \rightarrow K^0 X_u)\mathcal{B}(X_u \rightarrow D\bar{D}\pi)} = \left[\left(\frac{B^0}{B^+}\right)_{D\bar{D}\pi}\right]^{-1} \end{aligned}$$

WHAT DATA TELL (X(3872) AND X(3876) APPEAR TO BE RELATED BY $U \Leftrightarrow D$ SYMMETRY!)

	$f = J/\psi\pi^+\pi^-$	$f = D^0\bar{D}^0\pi^0$
$\mathcal{B}(B^\pm \rightarrow K^\pm X)\mathcal{B}(X \rightarrow f) \times 10^5$	1.05 ± 0.18 $1.01 \pm 0.25 \pm 0.10$	$10.7 \pm 3.1_{3.3}^{1.9}$ -----
$\mathcal{B}(B^0 \rightarrow K^0 X)\mathcal{B}(X \rightarrow f) \times 10^5$	----- $0.51 \pm 0.28 \pm 0.07$	$17.3 \pm 7.0_{5.3}^{3.1}$ -----
$(B^0/B^+)_f$	----- $0.50 \pm 0.30 \pm 0.05$	1.62 ± 0.80 $2.23 \pm 0.93 \pm 0.55$

A REMARKABLE FACT

$$\bar{b} + (u) \rightarrow \bar{c} + c\bar{s} + (u) + q\bar{q} \quad (\Delta I = 0)$$

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$$\mathcal{A}(B^+ \rightarrow K^+ X_d) = V = \mathcal{A}(B^0 \rightarrow K^0 X_u)$$

$$\mathcal{A}(B^+ \rightarrow K^0 X^+) = S = \mathcal{A}(B^0 \rightarrow K^+ X^-)$$

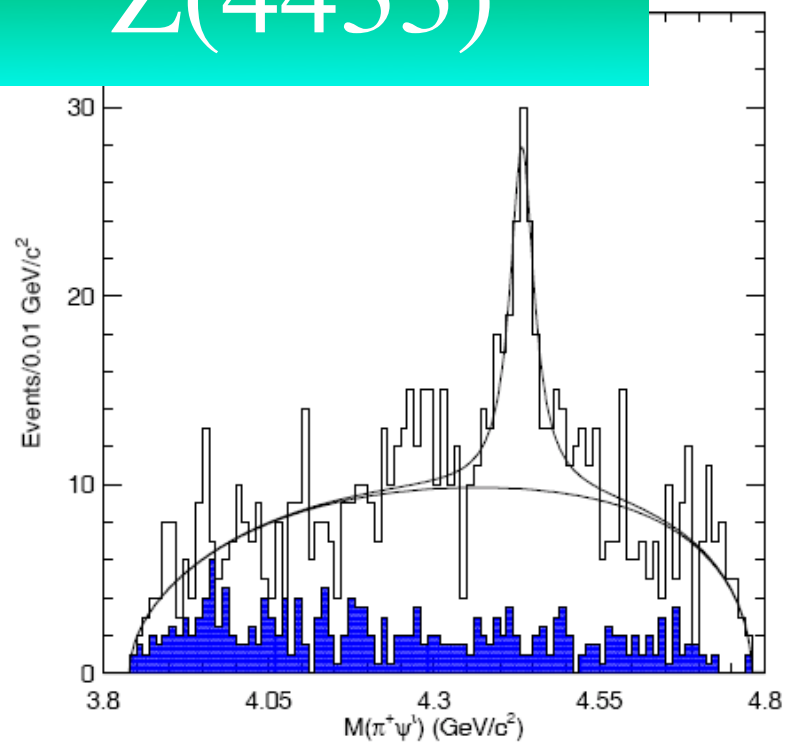
AS A CONSEQUENCE WE HAVE

$$\begin{aligned} \left(\frac{B^0}{B^+}\right)_{J/\psi} &= \frac{\mathcal{B}(B^0 \rightarrow K^0 X_d)\mathcal{B}(X_d \rightarrow J/\psi\pi^+\pi^-)}{\mathcal{B}(B^+ \rightarrow K^+ X_d)\mathcal{B}(X_d \rightarrow J/\psi\pi^+\pi^-)} = \frac{\mathcal{B}(B^0 \rightarrow K^0 X_d)}{\mathcal{B}(B^+ \rightarrow K^+ X_d)} = \\ &= \frac{\mathcal{B}(B^+ \rightarrow K^+ X_u)}{\mathcal{B}(B^0 \rightarrow K^0 X_u)} = \frac{\mathcal{B}(B^+ \rightarrow K^+ X_u)\mathcal{B}(X_u \rightarrow D\bar{D}\pi)}{\mathcal{B}(B^0 \rightarrow K^0 X_u)\mathcal{B}(X_u \rightarrow D\bar{D}\pi)} = \left[\left(\frac{B^0}{B^+}\right)_{D\bar{D}\pi}\right]^{-1} \end{aligned}$$

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$\mathcal{B}(B^0 \rightarrow K^0 X)\mathcal{B}(X \rightarrow f) \times 10^5$	----- $0.51 \pm 0.28 \pm 0.07$	$17.3 \pm 7.0^{3.1}_{5.3}$ -----
$(B^0/B^+)_f$	-----	1.62 ± 0.80
	$0.94 \pm 0.24 \pm 0.10$	$1.33 \pm 0.69 \pm 0.52$

Z(4433)

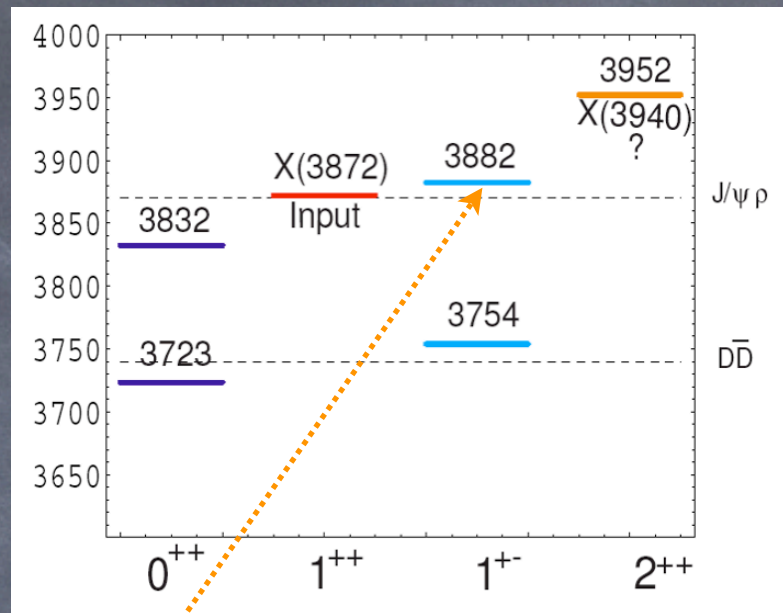


$$B^\pm \rightarrow Z^\pm K_s ; Z^\pm \rightarrow \psi(2S)\pi^\pm$$

This is the first charged state observed. A 2S state?

$$[cu][\bar{c}\bar{d}]$$

Z(4433) as a 1^{+-}



$J/\psi \pi(\eta)$,
 $\eta_c \rho(\omega)$
 (MPPR 05)

Is the Z(4433) the 2S radial excitation of the 3880?

Z is 600 MeV higher than the X(1^{+-} ,1S) and decays to $\psi(2S)$ rather than ψ :: $M(\psi(2S)) - M(\psi(1S)) \sim 590$ MeV

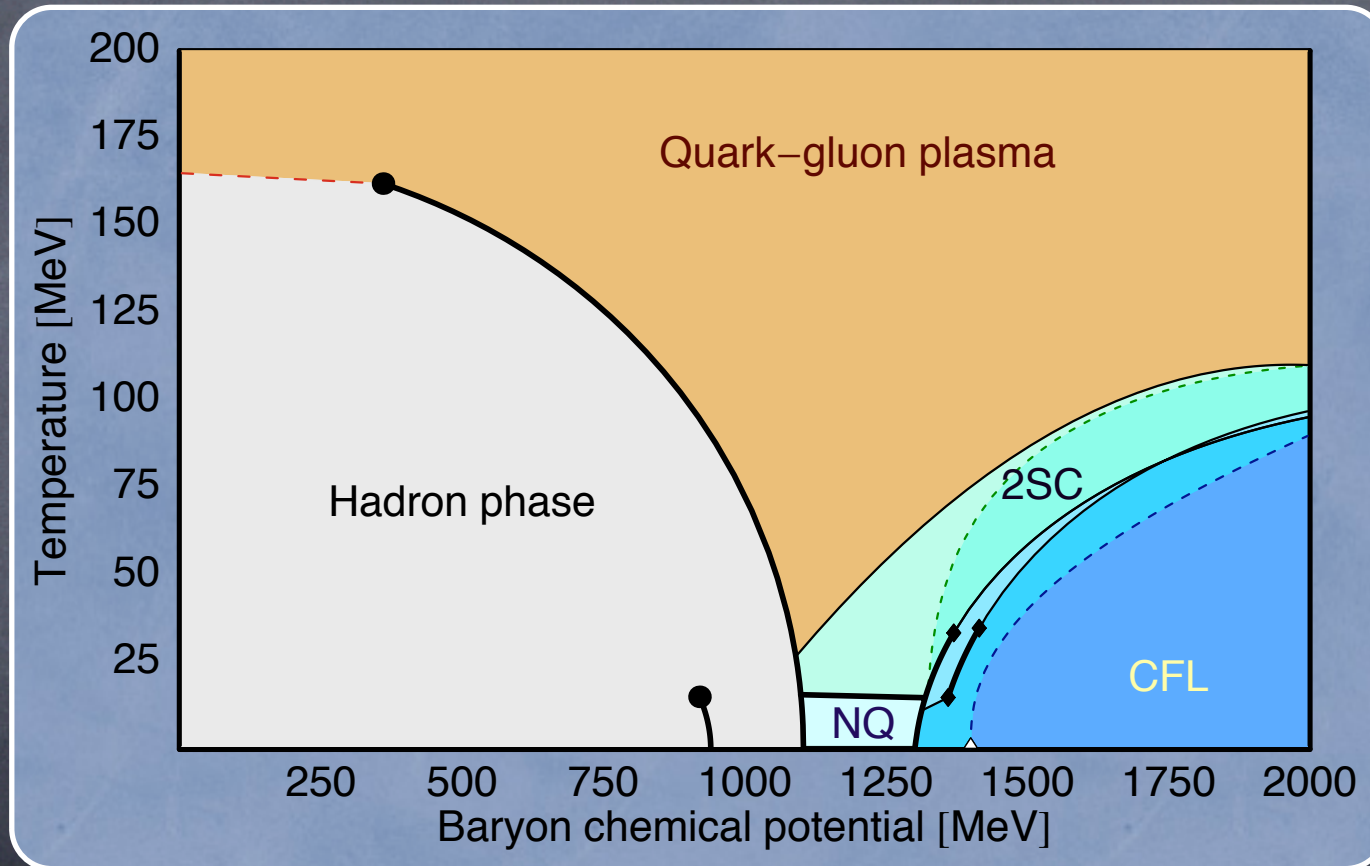
What to look for

- Neutral partners of $Z(4433) \sim X(1^{+-}, 2S)$ should be close by few MeV and decaying to $\psi(2S) \pi/\eta$ or $\eta_c(2S) \rho/\omega$
- What about $X(1^{+-}, 1S)$? Look for any charged state at ≈ 3880 MeV (decaying to $\psi\pi$ or $\eta_c\rho$)
- Similarly one expects $X(1^{++}, 2S)$ states. Look at $M \sim 4200-4300$: $X(1^{++}, 2S) \rightarrow D^{(*)} D^{(*)}$
- Baryon-anti-baryon thresholds at hand (4572 MeV for $2M_{\Lambda_c}$ and 4379 MeV for $M_{\Lambda_c} + M_{\Sigma_c}$). $X(2^{++}, 2S)$ might be over bb -threshold.

The condensed matter physics of QCD

Alford, Rajagopal, Wilczek, '98-'00 and many others

Diquarks play a crucial role



Astrophysical applications (glitches in pulsars...!)

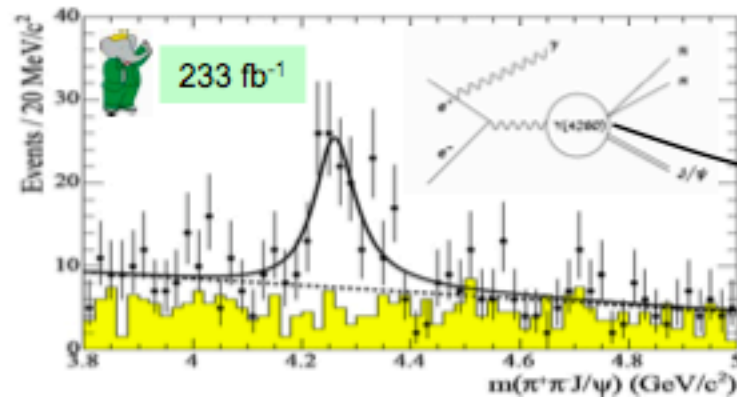
Conclusions

- The 4q-model gives the simplest interpretation of sub-GeV scalar mesons, of the 2-X's observed (prediction), and of the charged state (prediction).
- Still other particles have to be found to firmly assess this interpretation for the heavy-light states.
- If confirmed it has strong implications on various theoretical aspects of QCD.

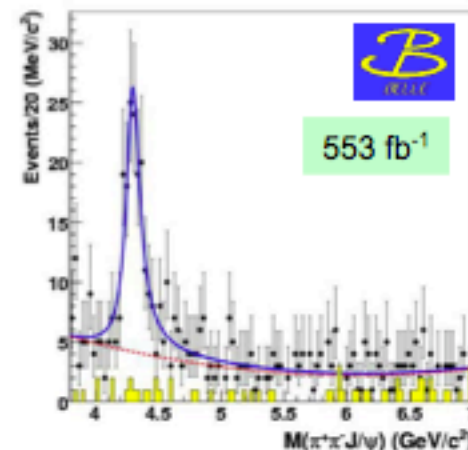
some back up slides

Y(4260): ANOTHER MYSTERY

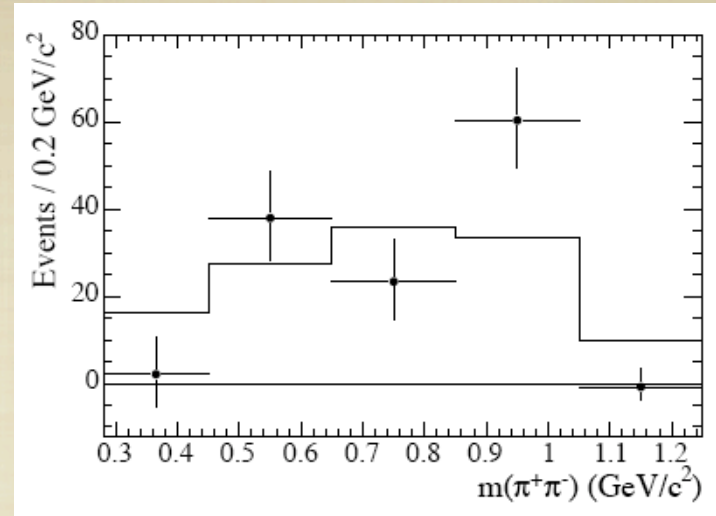
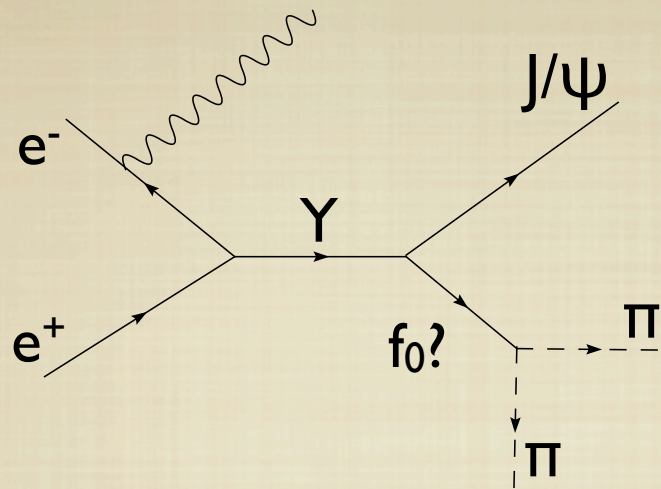
- New resonance discovered in $e^+e^- \rightarrow \gamma_{ISR}(J/\psi\pi^+\pi^-)$ by BaBar



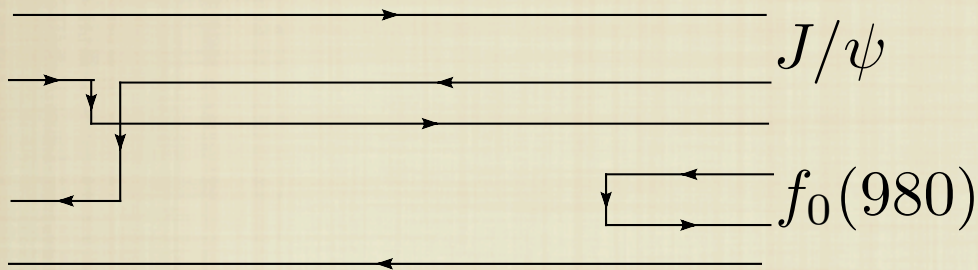
$J^{PC}=1^{--}$



- BaBar** measures: $M = (4259 \pm 8) \text{ MeV}/c^2$, $\Gamma = (88 \pm 23) \text{ MeV}$
- Belle** measures: $M = (4295 \pm 10^{+10}_{-3}) \text{ MeV}/c^2$, $\Gamma = (133^{+26}_{-22}{}^{+13}_{-6}) \text{ MeV}$
- Confirmed by **CLEO**: $M = (4283^{+17}_{-16} \pm 4) \text{ MeV}/c^2$
- No evidence for:
 - $e^+e^- \rightarrow \gamma_{ISR}(D\bar{D})$, $e^+e^- \rightarrow \gamma_{ISR}(\phi\pi^+\pi^-)$, $e^+e^- \rightarrow \gamma_{ISR}(p\bar{p})$, $e^+e^- \rightarrow \gamma_{ISR}(J/\psi\gamma\gamma)$
- 3σ enhancement in B decays
 - $B^- \rightarrow YK^-$, $Y \rightarrow J/\psi\pi^+\pi^-$
 - Needs **confirmation**

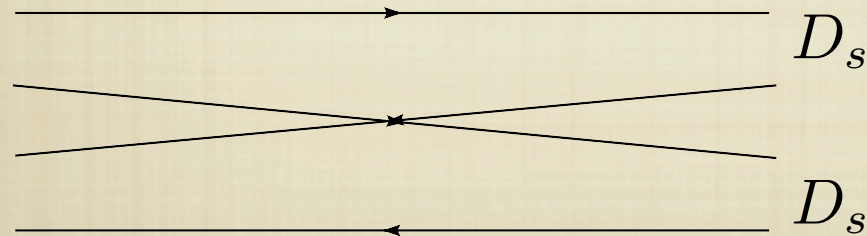


OUR INITIAL BIAS



Negative Parity 1^{--} ▶ one unit of ℓ

$f_0(980)$ (as $[sq][\bar{s}\bar{q}]_{S\text{-wave}}$) ▶ $[sc][\bar{s}\bar{c}]_{P\text{-wave}}$



DIQUARK-ANTIDIQUARK IN A RISING CONFINING POTENTIAL IS EXPECTED TO HAVE A SERIES OF ORBITAL ANGULAR MOMENTUM EXCITATIONS.

BOUND OBJECTS OF COLOR NEUTRAL STATES SHOULD HAVE A LIMITED SPECTRUM (POSSIBLY S-WAVE ONLY)

RESPONSIBLE OF GOOD PART OF THE WIDTH

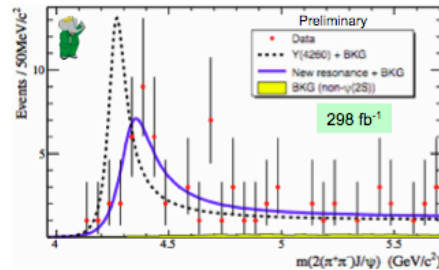
SATELLITES?

Call in Bad Diquarks :: $S = 2 \wedge L = 1$ possible

$S = 2 = 1 \oplus 1$:: decay preferably to $D_s^* D_s^*$ ► reduction of decay width

Y(4260)... AND Y(4325)?

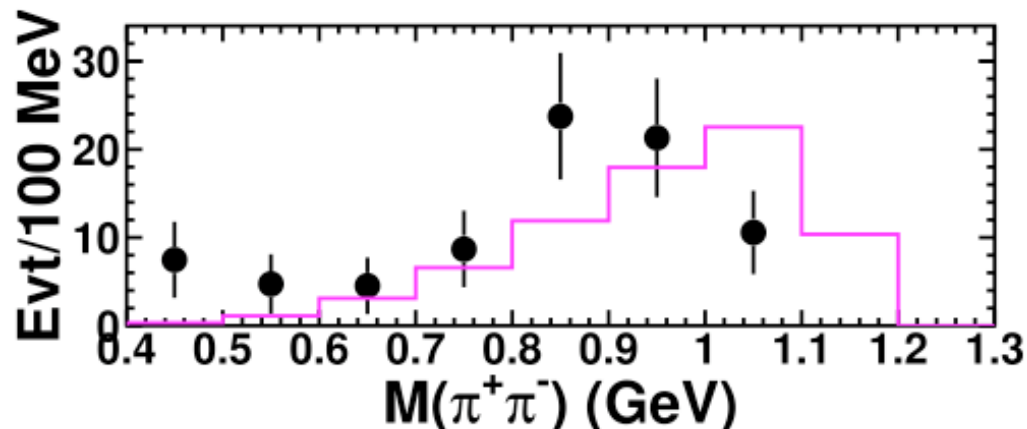
- Study of $Y(4260) \rightarrow \psi(2S)\pi\pi$ in ISR production



$M = (4324 \pm 24) \text{ MeV}/c^2$
 $\Gamma = (172 \pm 33) \text{ MeV}$

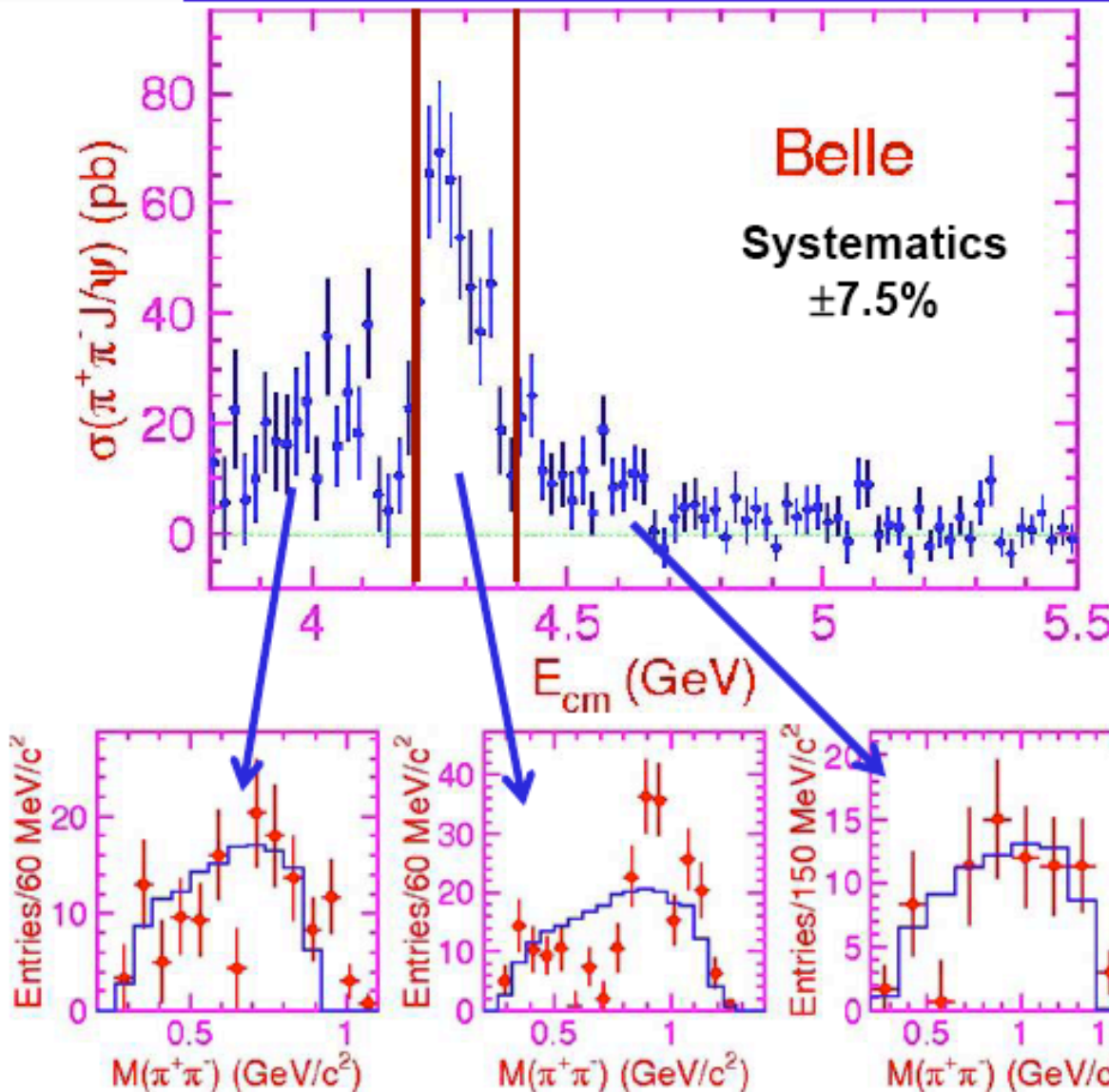
- Incompatible
 - with BaBar Y(4260), $\psi(4415)$ or 3-body phase space
- Compatible
 - with Belle Y("4295")

BUT CLEO FINDS NO F_0





$ee \rightarrow J/\psi \pi\pi$ cross-section



Bg subtracted $M(J/\psi\pi\pi)$
corrected for efficiency
and differential
luminosity

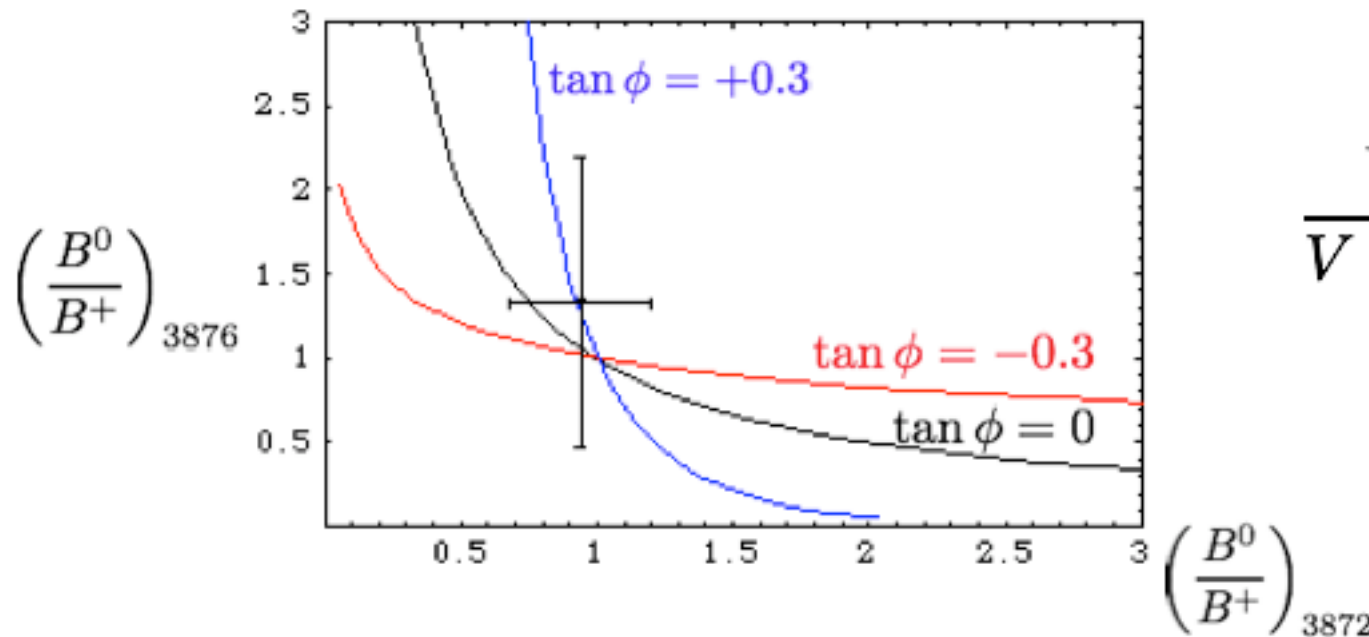
Cross-check:
measurement of cross
section at ψ' peak:

- $\Gamma_{ee}(\psi') = 2.54 \pm 0.12 \pm 0.89$
- **PDG'06:**
 $\Gamma_{ee}(\psi') = 2.43 \pm 0.05$

$M_{\pi\pi}$ spectra in different
 \sqrt{s} regions:

- \sqrt{s} 3.8 -4.2 & 4.4-4.6 GeV in
agreement with 3-body
phase space
- Y(4260) region
 \sqrt{s} 3.8 -4.15 GeV: two
clusters at low and high
masses

We did not yet consider any mixing between X_u & X_d



$$\frac{V}{V+S} = 1.0 \pm 0.25$$

S very small,
not much space
to see X^+ !!

$$\mathcal{A}(B^+ \rightarrow K^+ X_u) = V + S = \mathcal{A}(B^0 \rightarrow K^0 X_d)$$

$$\mathcal{A}(B^+ \rightarrow K^+ X_d) = V = \mathcal{A}(B^0 \rightarrow K^0 X_u)$$

$$\mathcal{A}(B^+ \rightarrow K^0 X^+) = S = \mathcal{A}(B^0 \rightarrow K^+ X^-)$$

DECAYS

≥ 3 for
spin
parity 1^+

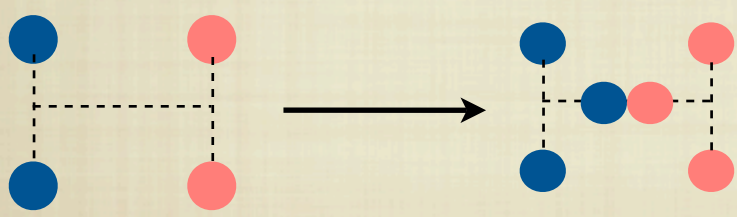
POSSIBLE DECAY MODES:

1 :: ANNIHILATION INTO GLUONS (> 2) GIVING A MULTIHADRON UNCHARGED FINAL STATE

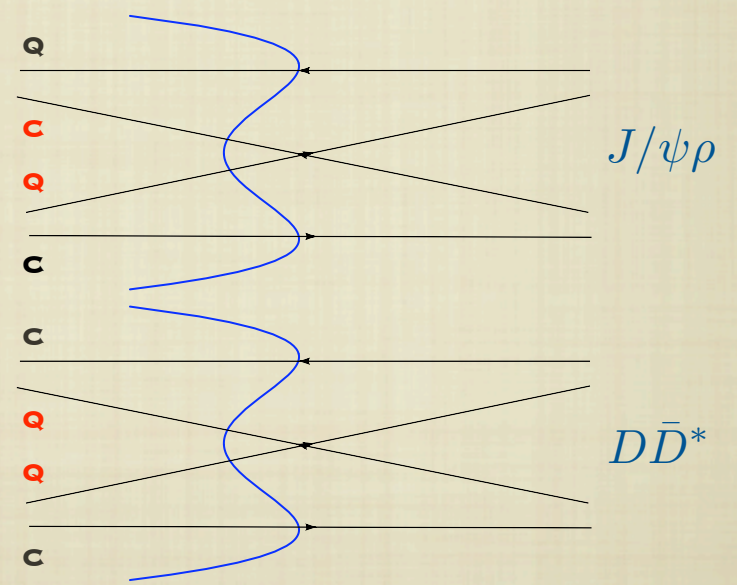
RATE EXPECTED TO BE SIMILAR TO: $\Gamma_{ann}(X) \simeq \Gamma(\chi_{c1}) = 0.96 \text{ MeV}$

2 :: ANNIHILATION $X \rightarrow gg + q\bar{q}$ BUT CCB ARE $J=1$ (VOLOSHIN), SO \Rightarrow TO TWO GLUONS

3 :: QUARK REARRANGEMENT (VIA TUNNELING) GIVING OPEN CHARM OR ψ



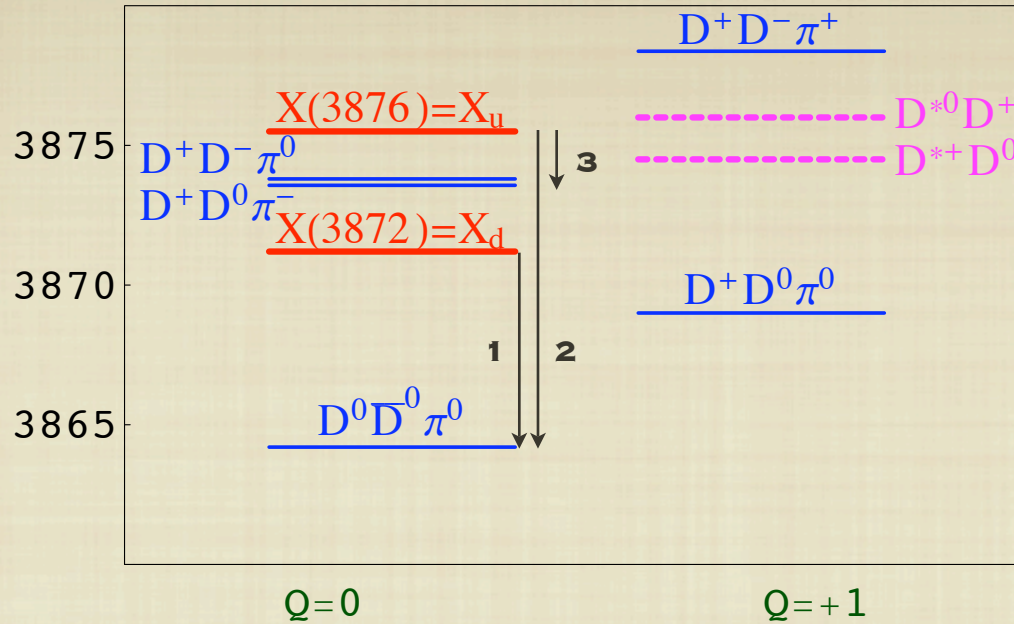
OR



(RED TWISTS)

1MeV sets the
scale of the
background of
multihadronic
decays

DECAYS



QUALITATIVELY WE EXPECT THAT :: (1) MUST BE SMALL (FLAVOR) :: (2) IS LARGER THAN (3)

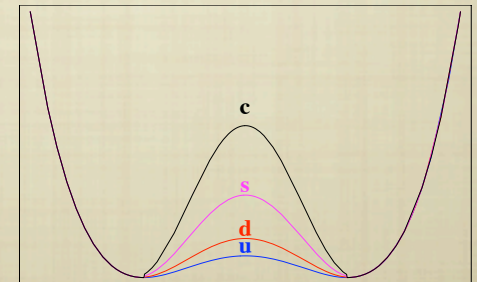
ALTERNATIVE: TWIST C
AND MAKE J/ψ

BY QUARK FLAVOR CONSERVATION X_D SHOULD
DECAY IN D^+D^{*-} :: PHASE SPACE FORBIDDEN.
 $D^0\bar{D}^0$ IS SUPPRESSED TWICE BECAUSE $UU \leftrightarrow DD$
& BECAUSE OF A SMALL 'REDUCED RATE'

WE COULD TWIST HERE C AS
WELL; BUT THE *CHEAPEST*
ALTERNATIVE IS STILL DD^*

$$\Gamma(X_u \rightarrow D^0\bar{D}^0\pi^0) \gg \Gamma(X_u \rightarrow J/\psi\pi^+\pi^-) \simeq \Gamma(X_d \rightarrow J/\psi\pi^+\pi^-) \gg \Gamma(X_d \rightarrow D^0\bar{D}^0\pi^0)$$

A QUALITATIVE PICTURE
OF THE BARRIERS



THE YET UNOBSERVED X^{+-}

EXPERIMENTAL BOUNDS

$$\mathcal{B}(B^+ \rightarrow K^0 X^+) \mathcal{B}(X^+ \rightarrow J/\psi \pi^+ \pi^0) \leq 2.2 \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow K^+ X^-) \mathcal{B}(X^- \rightarrow J/\psi \pi^- \pi^0) \leq 0.54 \times 10^{-5}$$

USING PREVIOUS RESULTS WE GET

$$\begin{aligned} \frac{\mathcal{B}(X^- \rightarrow \psi \pi^- \pi^0)}{\mathcal{B}(X_d \rightarrow \psi \pi \pi)} &\equiv \frac{\mathcal{B}(B^0 \rightarrow K^+ X^-) \mathcal{B}(X^- \rightarrow \psi \pi^- \pi^0)}{\mathcal{B}(B^0 \rightarrow K^+ X^-) \mathcal{B}(X_d \rightarrow \psi \pi \pi)} \leq \\ &\leq \frac{0.54 \times 10^{-5}}{\mathcal{B}(B^0 \rightarrow K^+ X^-) \mathcal{B}(X_d \rightarrow \psi \pi \pi)} \frac{\mathcal{B}(B^0 \rightarrow K^0 X_d)}{\mathcal{B}(B^0 \rightarrow K^0 X_d)} = \frac{0.54}{0.51} \frac{\mathcal{B}(B^0 \rightarrow K^0 X_d)}{\mathcal{B}(B^0 \rightarrow K^+ X^-)} \approx \\ &\approx \left| \frac{V+S}{S} \right|^2 \times \frac{0.54}{0.51} \end{aligned}$$

I.E., THE LIMIT

$$\mathcal{B}(X^+ \rightarrow J/\psi \pi^+ \pi^0) \leq \left(\underbrace{\left| \frac{V+S}{S} \right|}_{?} \right)^2 \times \frac{0.54}{0.51} \times \mathcal{B}(X(3872) \rightarrow J/\psi \pi^+ \pi^-)$$

The constituent quark model

$$H = \sum_i m_i + \sum_{i < j} 2\kappa_{ij}(S_i \cdot S_j)$$

De Rujula-Georgi-Glashow

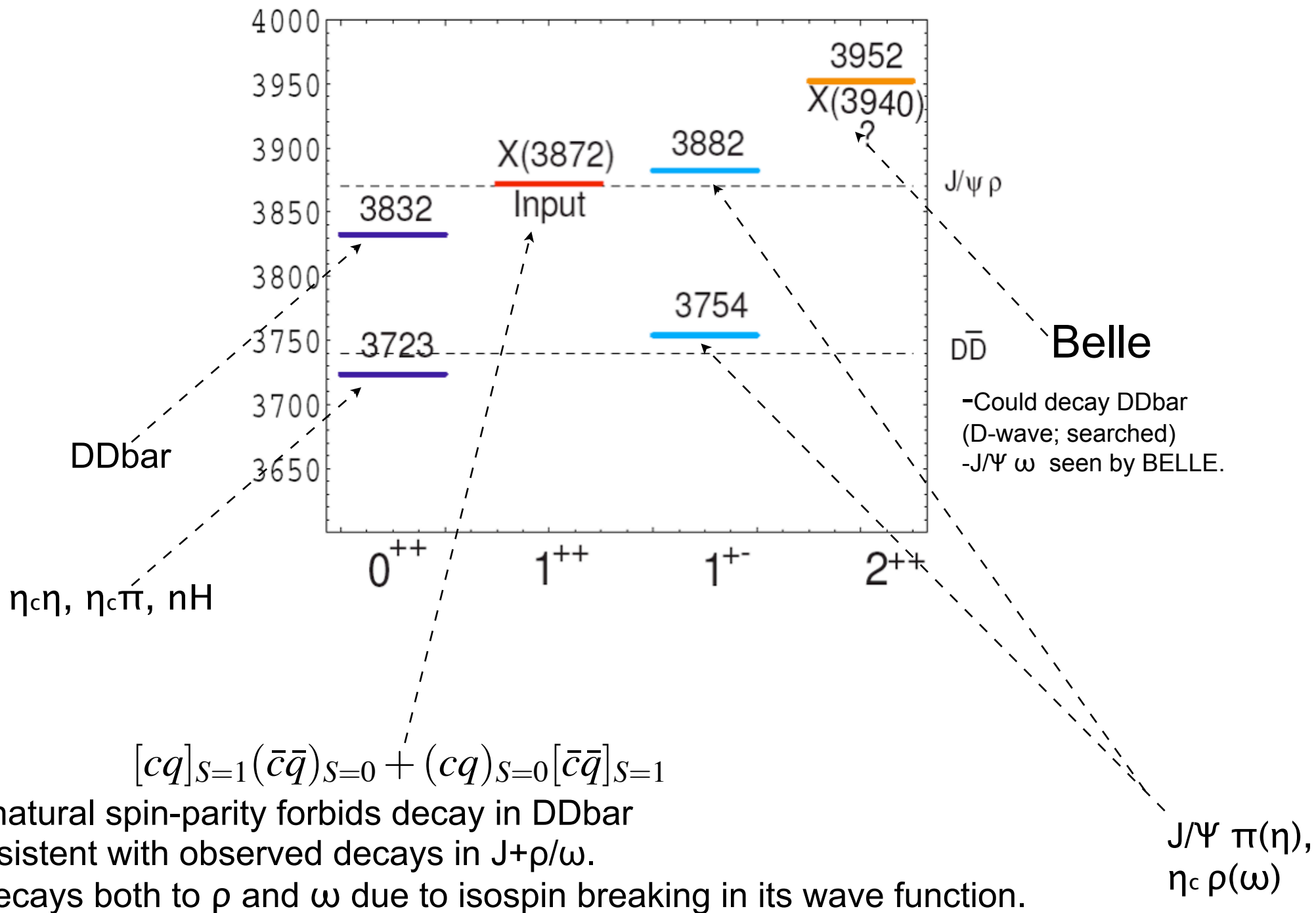
$$H([cq][\bar{c}\bar{q}']) = 2m_{[cq]} + 2\kappa_{cq} [S_c \cdot S_q + S_{\bar{c}} \cdot S_{\bar{q}'}] + \\ + 2\kappa_{q\bar{q}'} S_q \cdot S_{\bar{q}'} + 2\kappa_{c\bar{q}'} [S_c \cdot S_{\bar{q}'} + S_{\bar{c}} \cdot S_q] + 2\kappa_{c\bar{c}} S_c \cdot S_{\bar{c}}$$

	<i>q</i>	<i>s</i>	<i>c</i>		<i>q</i> \bar{q}	<i>s</i> \bar{q}	<i>s</i> \bar{s}	<i>c</i> \bar{q}	<i>c</i> \bar{s}	<i>c</i> \bar{c}
constituent	305	490	1670	$(\kappa_{ij})_0$ (MeV)	315	195	121*	70	72	59
mass (MeV)	362	546	1721	$(\kappa_{ij})_0 m_i m_j$ (GeV) ³	0.029	0.029		0.036	0.059	0.16

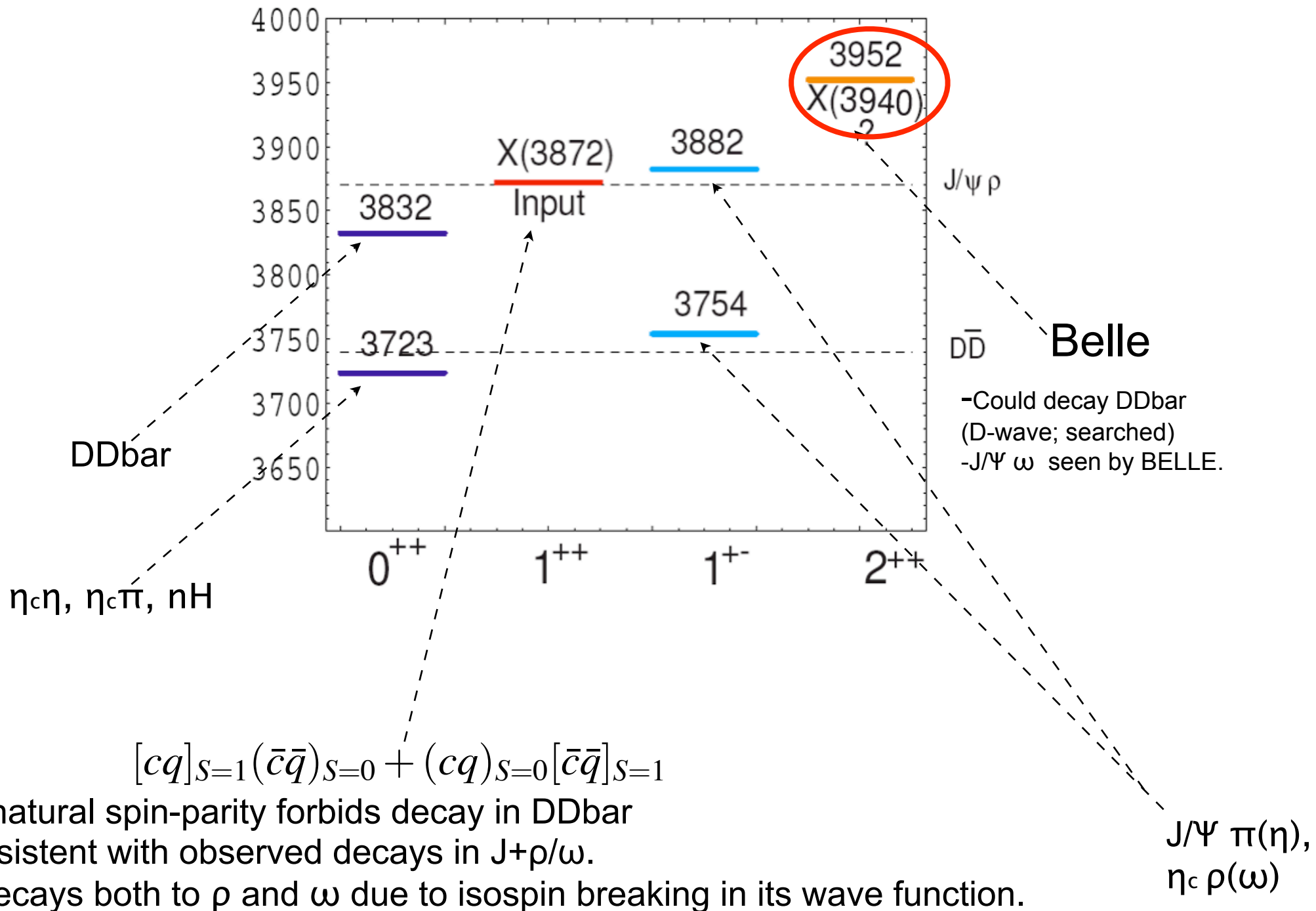
	<i>qq</i>	<i>sq</i>	<i>cq</i>	<i>cs</i>
$(\kappa_{ij})_{\bar{3}}$ (MeV)	103	64	22	25
$(\kappa_{ij})_{\bar{3}} m_i m_j$ (GeV) ³	0.014	0.013	0.014	0.024

From data on L=0 mesons and baryons we find relations for the constituent masses and for the couplings.

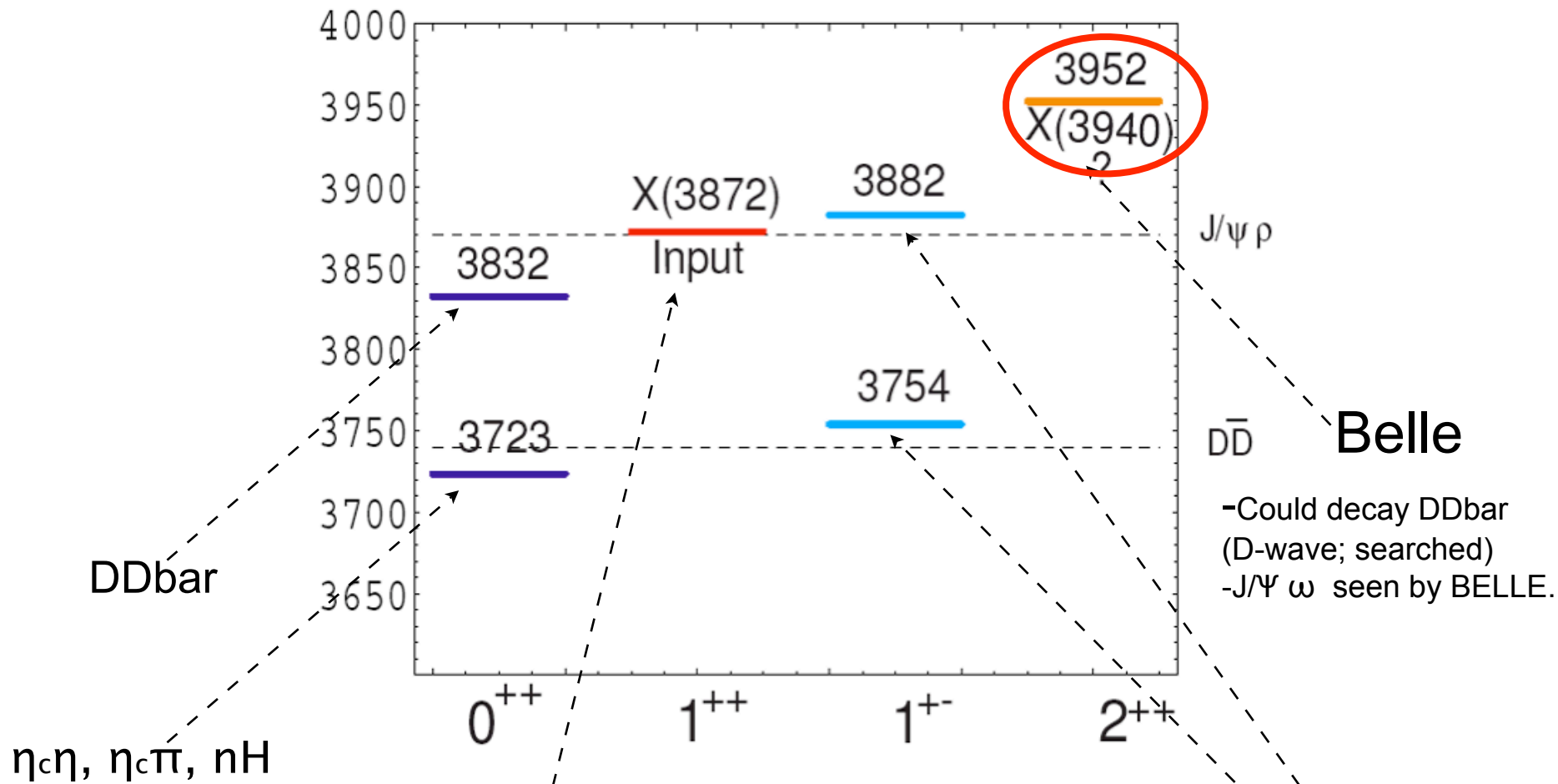
The X Mass Spectrum



The X Mass Spectrum



The X Mass Spectrum



$\eta_c \eta, \eta_c \pi, nH$

DDbar

D \bar{D} Belle

- Could decay DDbar (D-wave; searched)
- J/ Ψ ω seen by BELLE.

$$[cq]_{s=1}(\bar{c}\bar{q})_{s=0} + (cq)_{s=0}[\bar{c}\bar{q}]_{s=1}$$

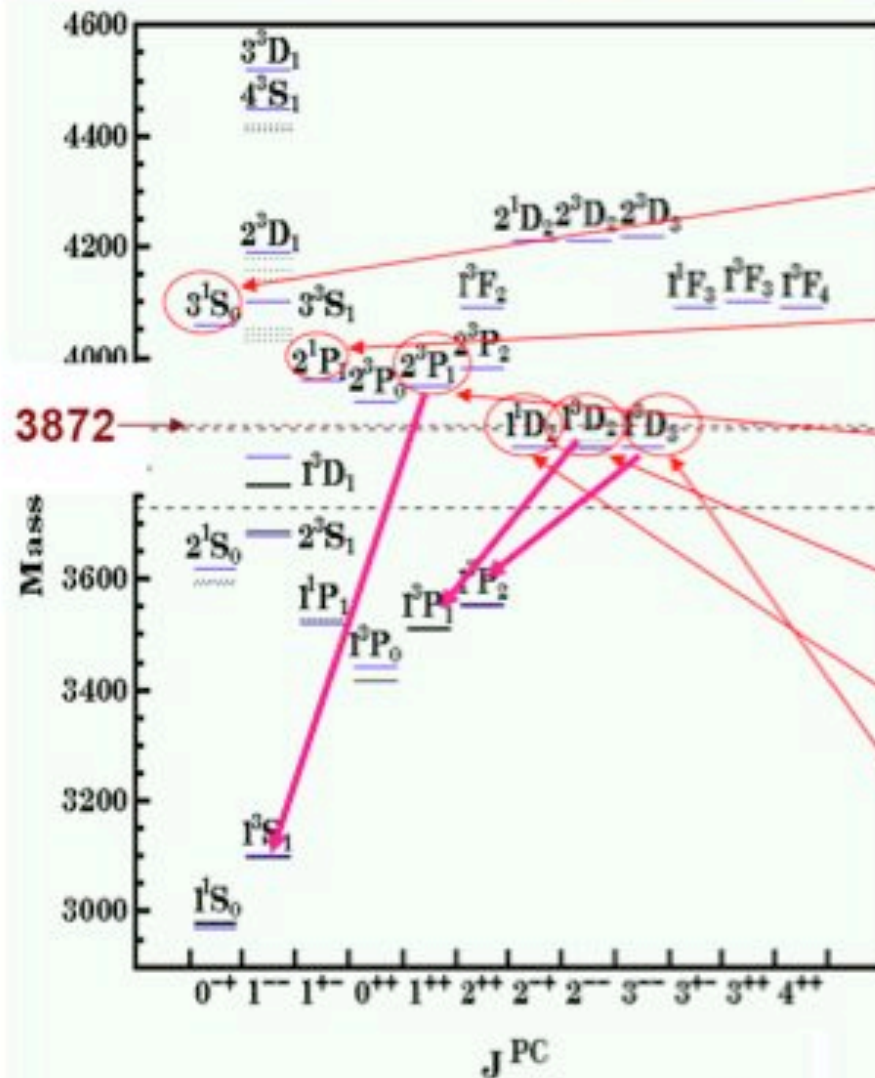
-Unnatural spin-parity forbids decay in DDbar

Consistent with observed decays in J+ ρ / ω .

-It decays both to ρ and ω due to isospin breaking in its wave function.

J/ Ψ $\pi(\eta)$,
 $\eta_c \rho(\omega)$

X(3872): charmonio?



$\eta_c(3S)$: massa e larghezza troppo piccole

$h_c(2P)$: distribuzioni angolari non compatibili con $J^{PC} = 1^{+-}$

$\chi_{c1}(2P)$: $\mathcal{B}(X \rightarrow J/\psi \gamma)$ troppo piccolo

ψ_2 : $\mathcal{B}(X \rightarrow \chi_{c1} \gamma)$ troppo piccolo; $m(\pi^+ \pi^-)$ non compatibile

η_{c2} : dovrebbe dominare $X \rightarrow \eta_c \pi^+ \pi^-$

ψ_3 : $\mathcal{B}(X \rightarrow \chi_{c2} \gamma)$ e $\mathcal{B}(X \rightarrow \bar{D}D)$ troppo piccoli

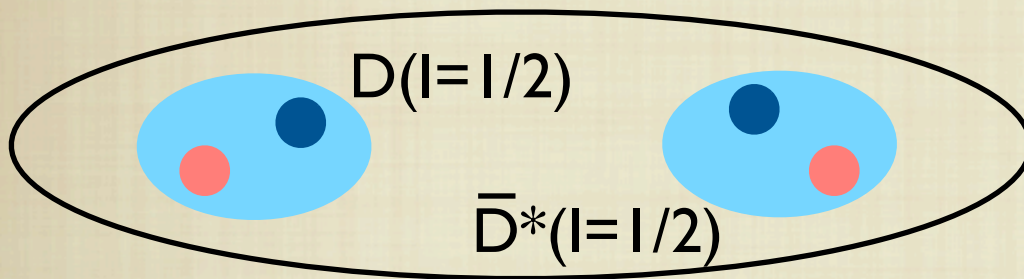
ISOSPIN VIOLATION AND TWO X'S

(MPPR '05)

$$\frac{\mathcal{B}(X \rightarrow \pi^+ \pi^- \pi^0 J/\psi)}{\mathcal{B}(X \rightarrow \pi^+ \pi^- J/\psi)} = 1.0 \pm 0.4 \pm 0.3$$

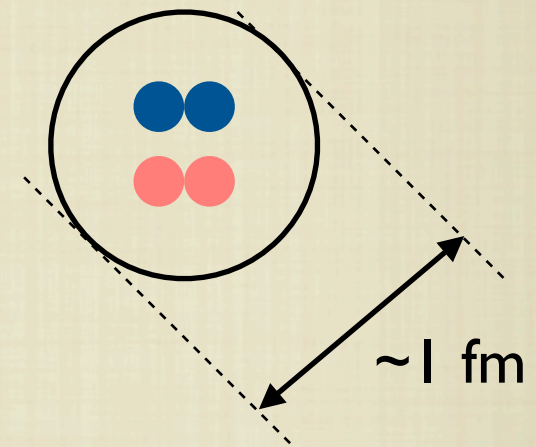
FROM EARLY OBSERVATIONS BY BELLE AND BABAR ('03-'04)

MOLECULES



NO PROBLEM WITH ISOSPIN VIOLATION :: 1 STATE ::
SMALL DECAY RATE TO DD π

4-QUARKS



NEED TWO STATES, AND MAKE
 ISOSPIN VIOLATION POSSIBLE

$$X_u = [cu][\bar{u}\bar{c}]$$

$$X_d = [cd][\bar{d}\bar{c}]$$

THESE TWO INTERPRETATIONS ARE NOT `COMPLEMENTARY` OR
 `UNRESOLVABLE`. **THEY YIELD DIFFERENT PREDICTIONS.**