Astroparticle Physics and the ILC

Manuel Drees

Bonn University

1) Introduction: A brief history of the universe

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- 2) Dark Energy

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 - Energy density of the Universe begins to be dominated by (dark) matter

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 - In models with dynamical Dark Energy ("quintessence"): Can affect dynamics of BBN, creation of Dark Matter, ...

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- In models with extra dimensions: Connections to collider physics may exist (radion—Higgs mixing; spectrum of KK states), but no example is known (to me)

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- Some models work at rather low temperature: can be tested at colliders! Will discuss two such models.

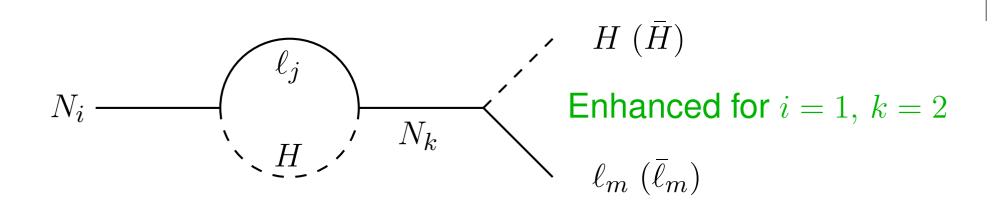
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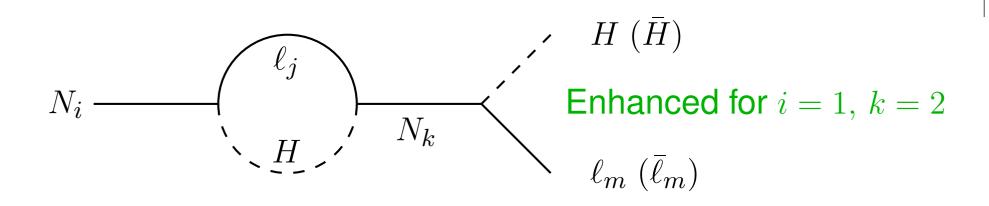
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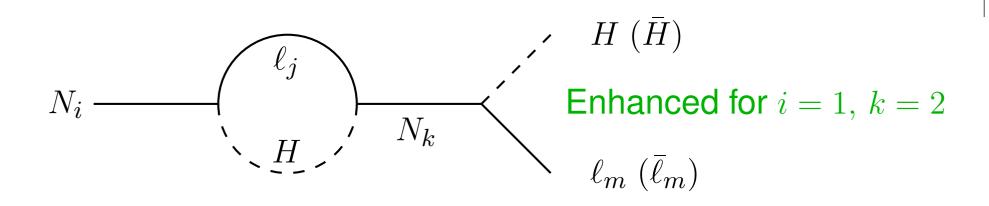
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- If $M_2-M_1\ll M_1$: effective CP violation enhanced: Can have $M_1\simeq \text{TeV}!$ Pilaftsis 1997/9; Pilaftsis & Underwood 2004

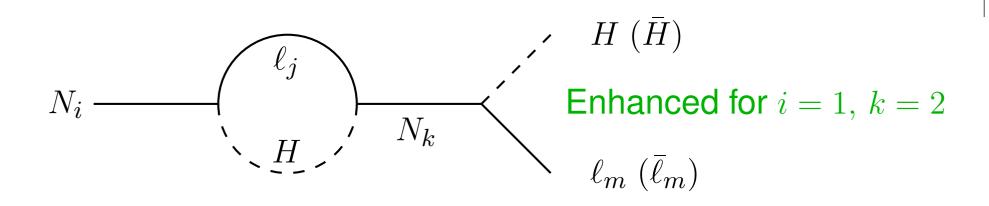




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- Other scenarios with low-scale leptogenesis: Grossman, Kashti, Nir, Roulet 2004; Hambye et al. 2003; Raidal, Strumia, Turzynski 2004

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- Does not work in SM: cross—over (no phase transition) for $m_H \gtrsim 60$ GeV!

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 - Determination of ϕ_{μ} in relevant region of parameter space

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- Models of structure formation, X ray temperature of clusters of galaxies, . . .
- Cosmic Microwave Background anisotropies (WMAP) imply $\Omega_{\rm DM}h^2=0.111\pm0.009$ Bennet et al., astro-ph/0302207

Density of thermal DM

Decoupling of DM particle χ defined by:

$$n_{\chi}(T_f)\langle v\sigma(\chi\chi\to\text{any})\rangle = H(T_f)$$

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Gives average relic mass density

$$\Omega_{\chi} \propto \frac{1}{\langle v\sigma(\chi\chi\to {\rm any})\rangle}$$

Gives roughly right result for weak cross section!

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$$\chi = \tilde{\chi}_1^0$$

(or in hidden sector)

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 \Longrightarrow Can determine decomposition of $\tilde{\chi}_1^0$ by studying $\tilde{\chi}_1^{\pm}$, $\tilde{\chi}_2^0$, $\tilde{\chi}_3^0$. Well studied in the MSSM, but not much is known about extensions (e.g. NMSSM)

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- Parameters in Higgs and squark sector are also needed to predict $\tilde{\chi}_1^0$ detection rate, i.e. $\sigma(\tilde{\chi}_1^0 N \to \tilde{\chi}_1^0 N)$

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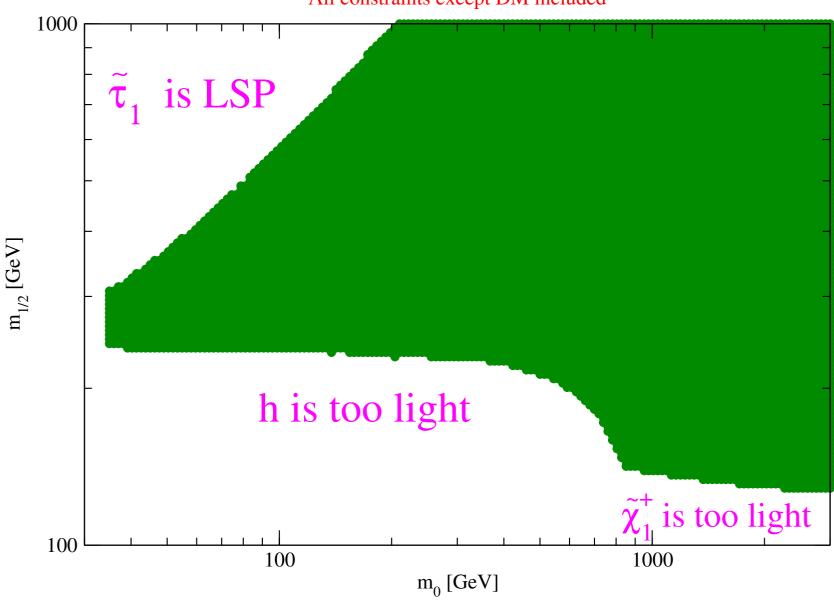
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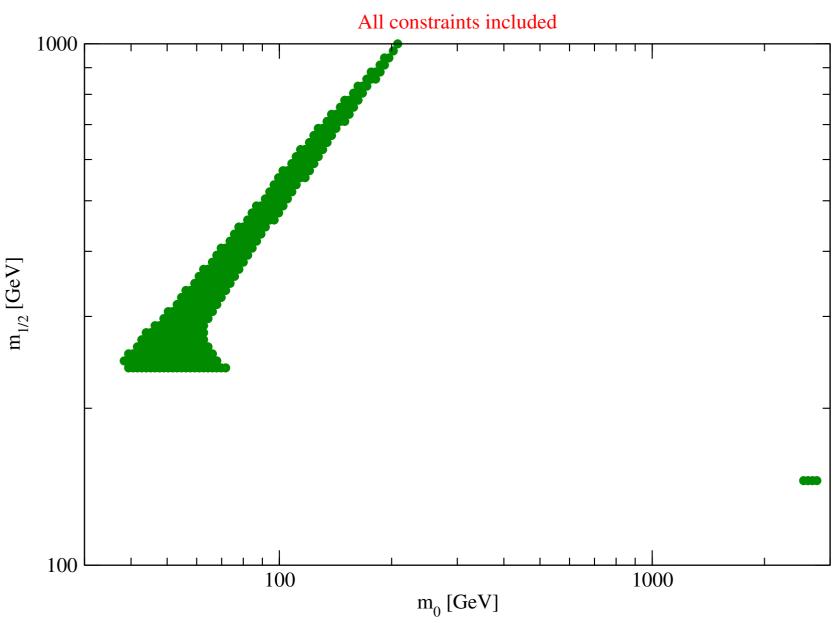
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- Simple CCB constraints (at weak scale only)

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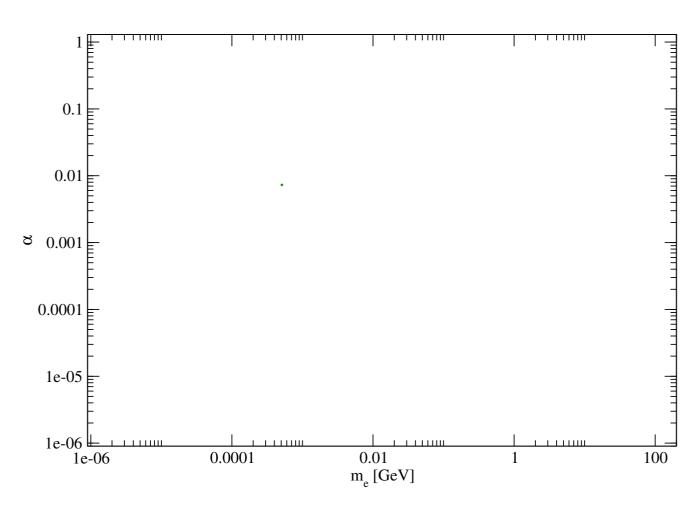
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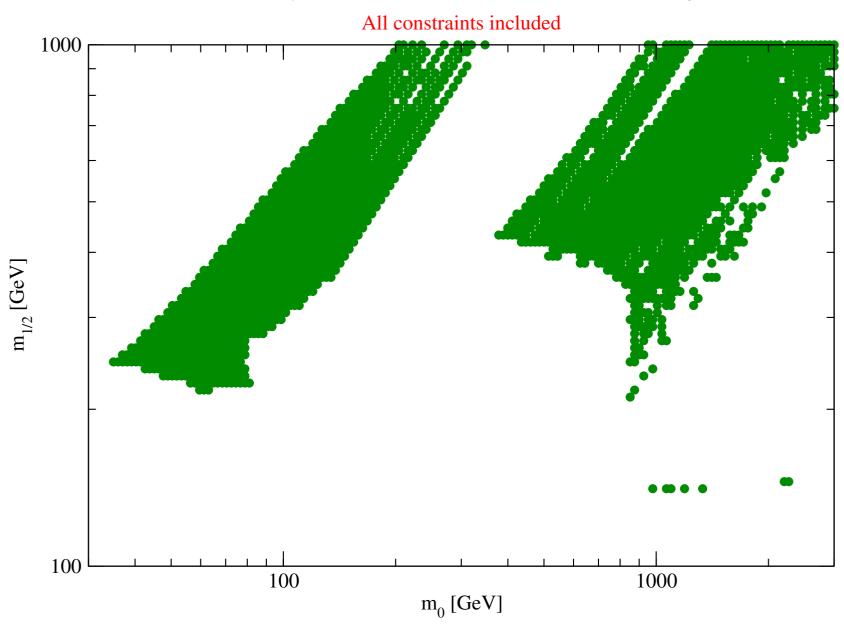
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QED parameter space

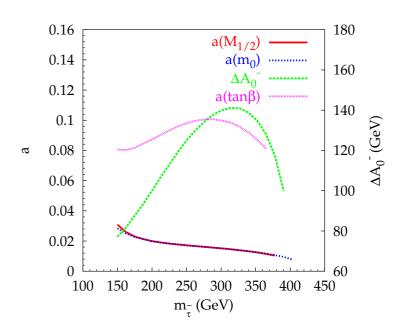


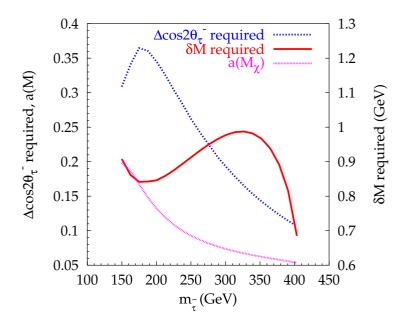
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Example: $\tilde{\tau}$ co–ann. region in mSUGRA Allanach et al. 2004

Precision with which one has to measure parameters in order to predict thermal $\tilde{\chi}_1^0$ relic density with WMAP accuracy:





Beyond mSUGRA

The predicted Dark Matter density can be altered by modifying the SUSY model and/or by modifying the cosmological model.

Reducing $\Omega_{\tilde{\chi}_1^0}$ by changing the SUSY model:

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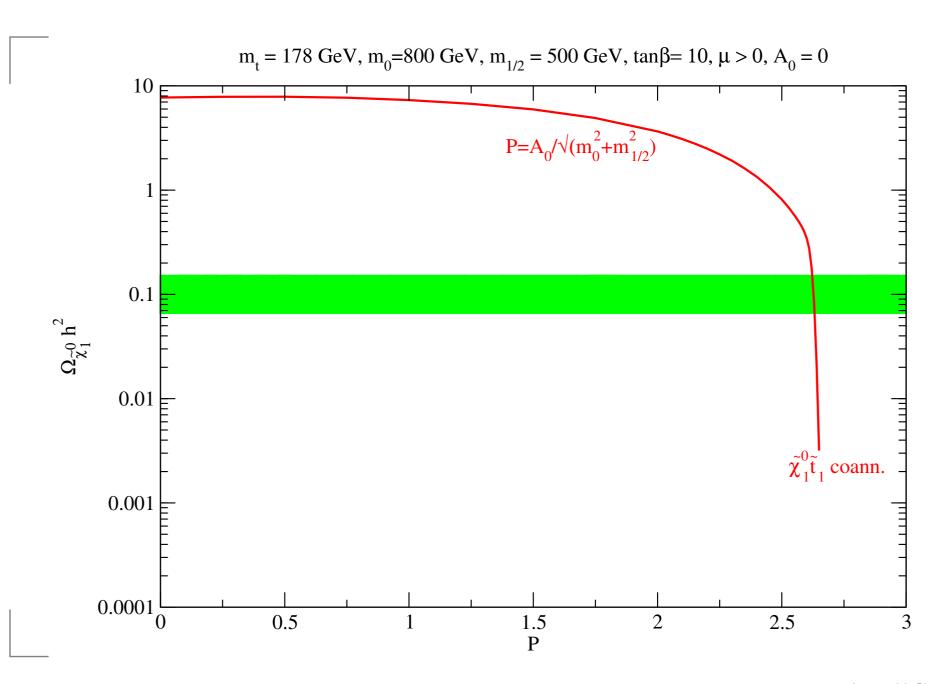
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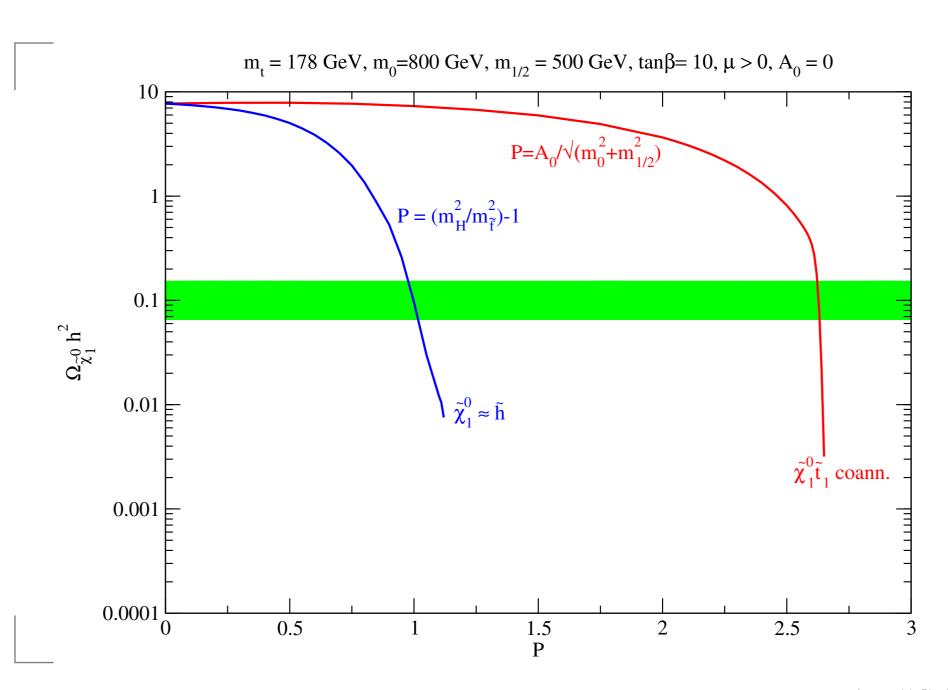
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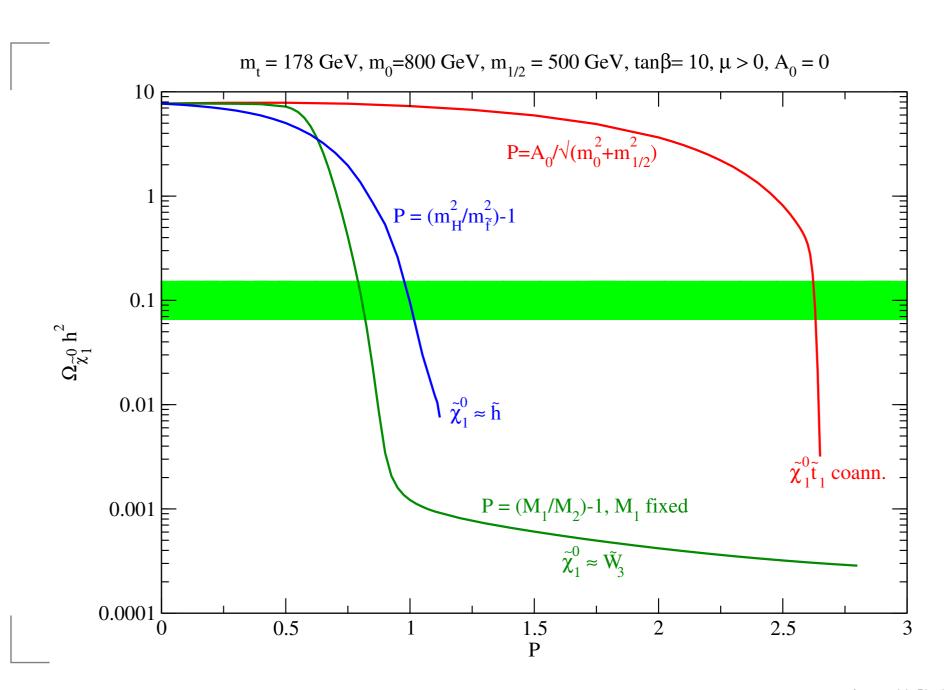
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These modifications lead to greatly altered collider phenomenology!







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- Detection of hidden sector DM seems impossible: Cross sections are way too small!

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If $\tilde{\chi}_1^0$ makes DM: Can use measurements at colliders to constrain cosmology!

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 - SUSY WIMPs: Relic density often depends very sensitively on parameters: need very accurate measurements in collider experiments!