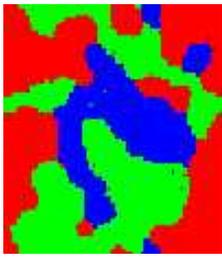


# Lattice Gauge Theory and Heavy Ion Collisions

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# Lattice Gauge Theory and Heavy Ion Collisions

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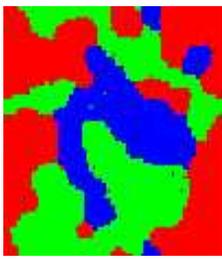
Exploring the properties of  
strongly interacting matter

theoretical background:

**Quantum Chromo Dynamics (QCD)**

experimental approach:

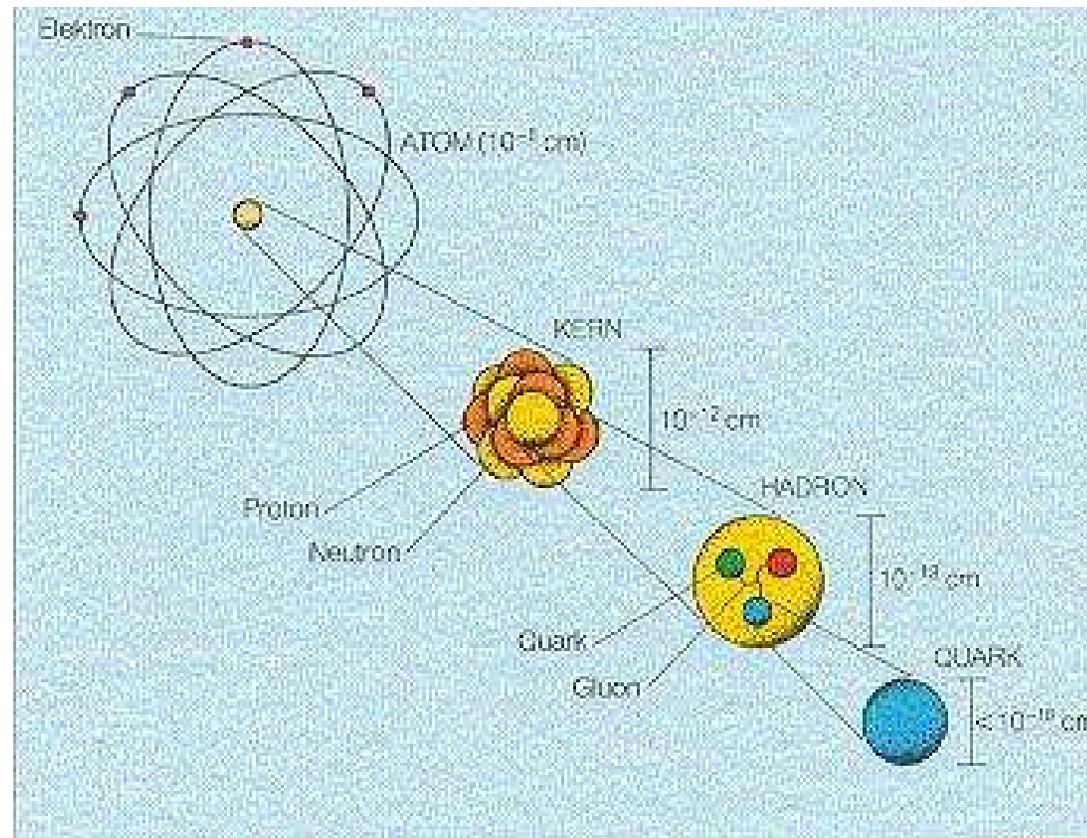
**collision of ultra-relativistic heavy ions**

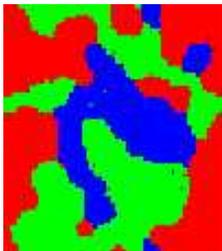


# From matter to elementary particles

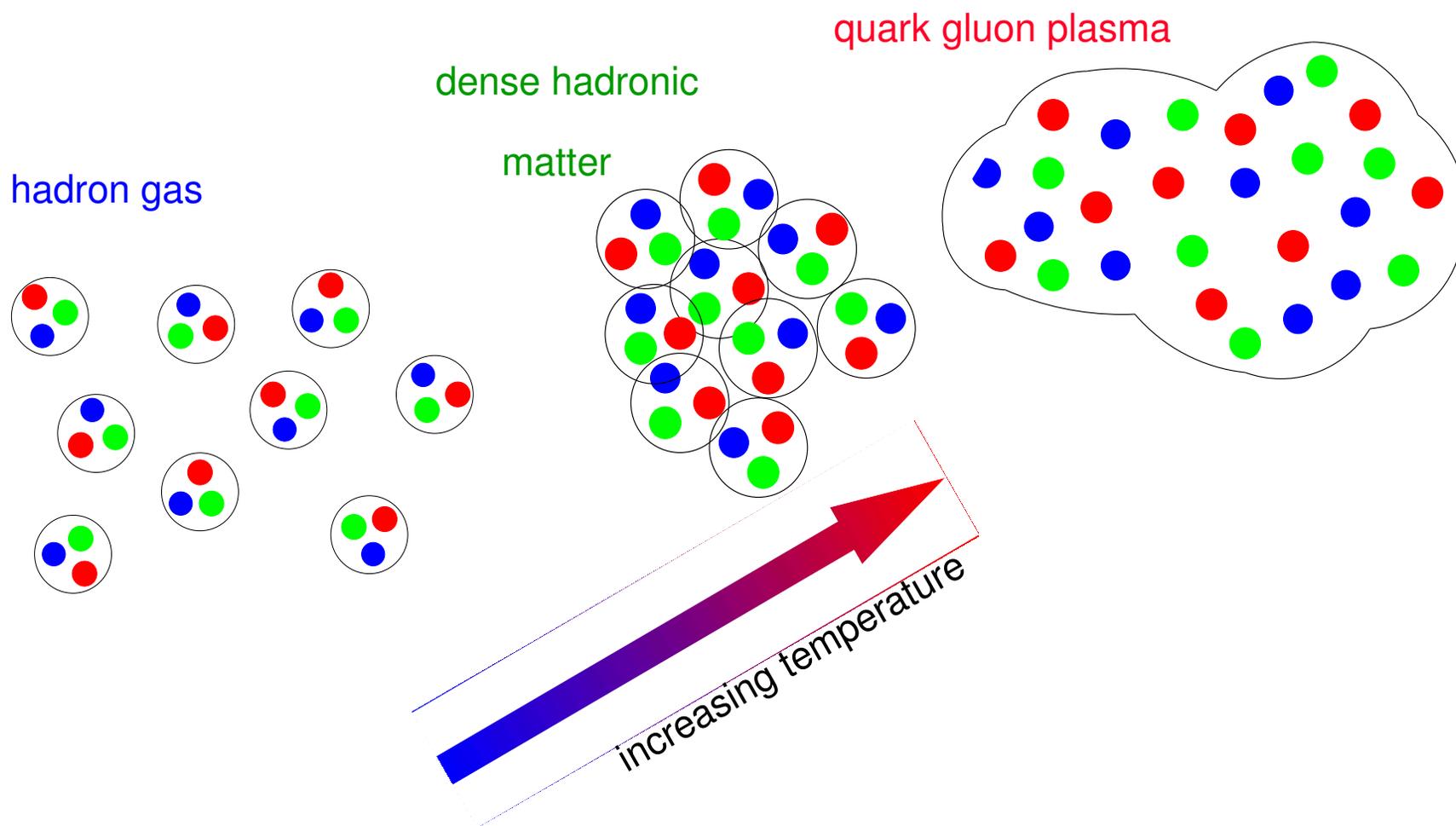
## Substructure of Matter

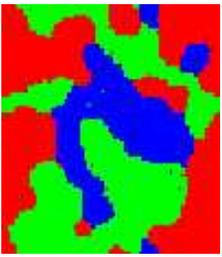
from atoms to nuclei to nucleons to quarks and gluons





# From matter to elementary particles ..to elementary particle matter

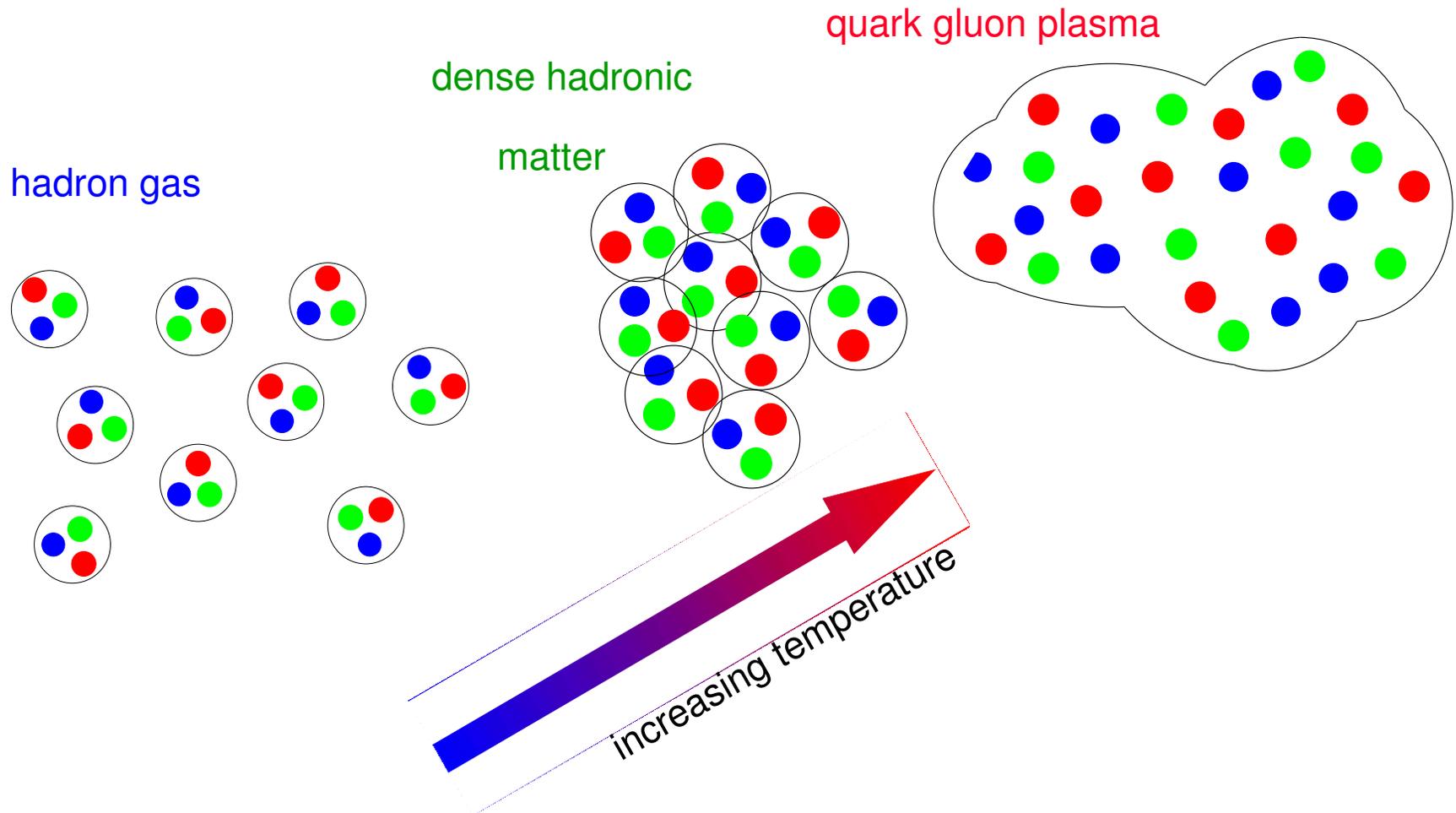


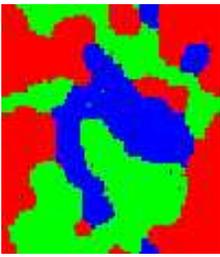


# Phase Transition from a Hadron Gas to the Quark-Gluon Plasma

temperatures in the early universe after  $10^{-6}$  sec:  $\sim 10^{12}$  K

density of neutron stars:  $\sim$  (3-10)-times nuclear matter density

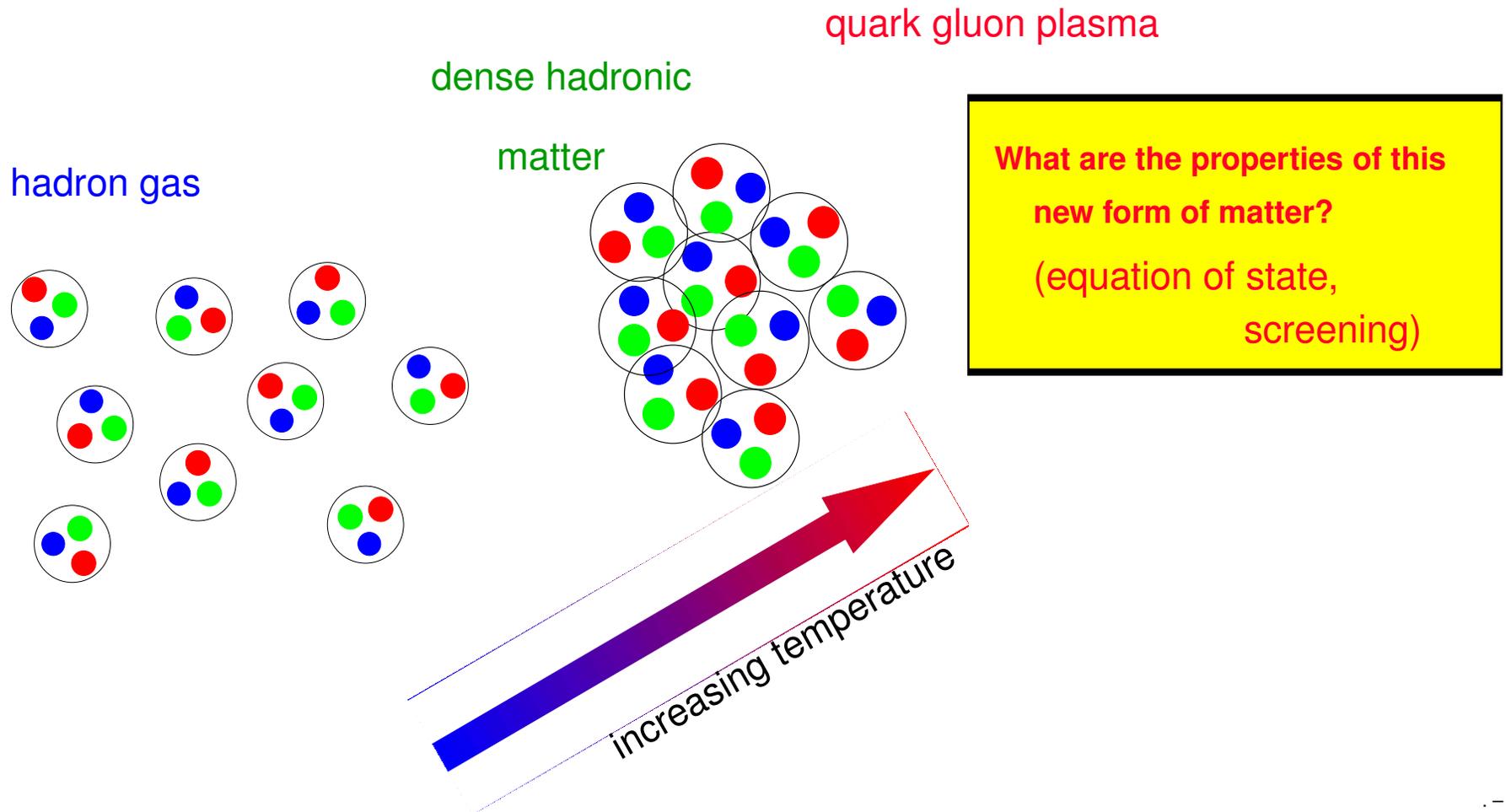


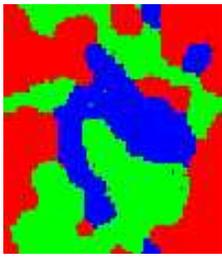


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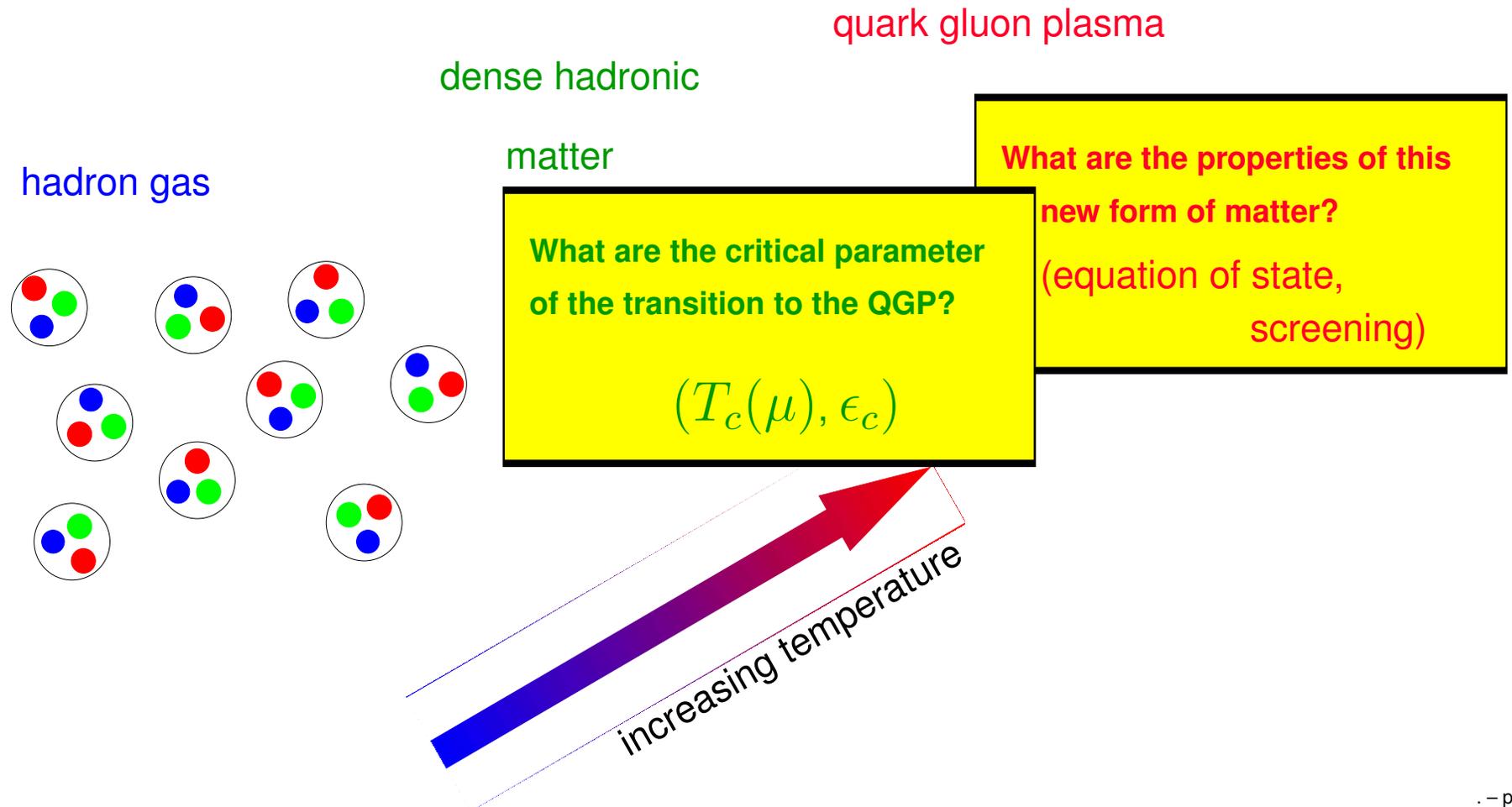


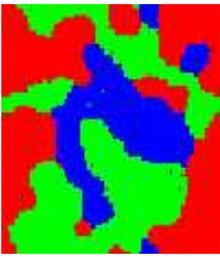


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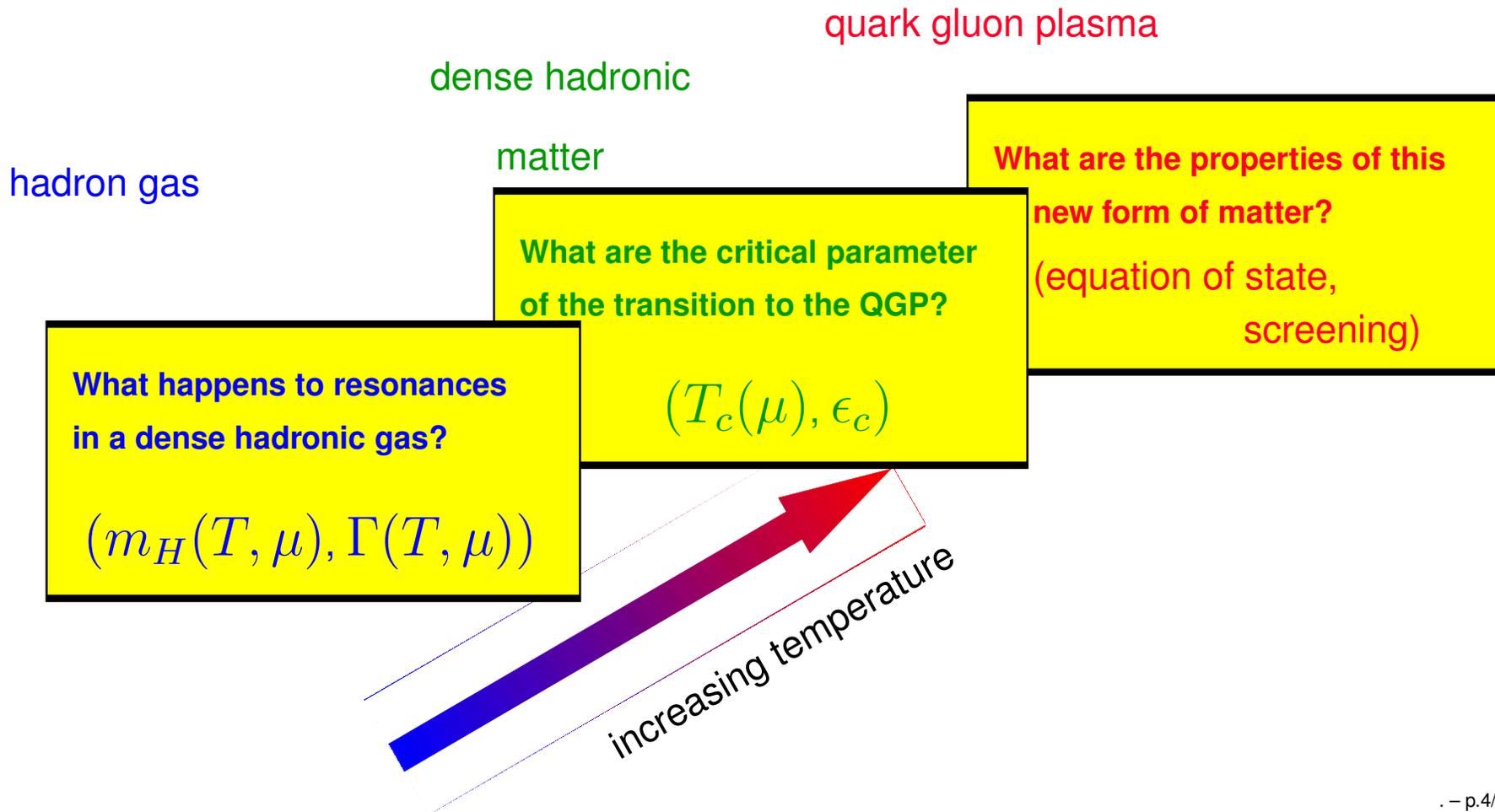


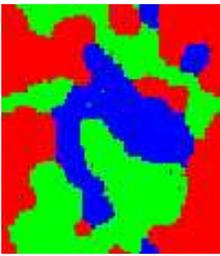


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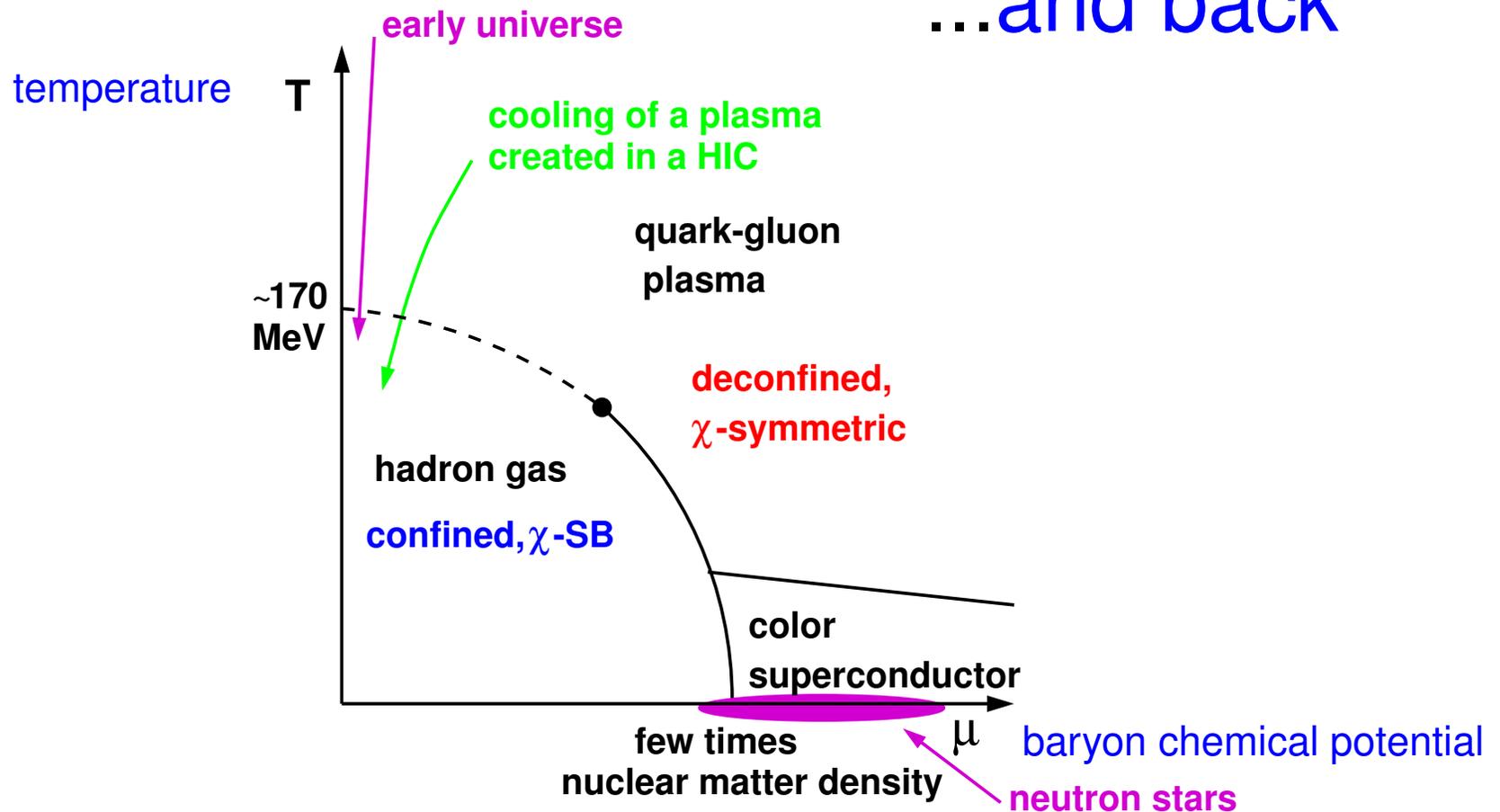




# Phase diagram of strongly interacting matter

## From Hadron Gas to Quark Gluon Plasma

...and back



## Highly Excited Nuclear Matter\*

G. F. Chapline, M. H. Johnson, E. Teller, and M. S. Weiss

*Lawrence Livermore Laboratory, University of California, Livermore, California 94550*

(Received 4 September 1973)

It is suggested that very hot and dense nuclear matter may be formed in a transient state in "head-on" collisions of very energetic heavy ions with medium and heavy nuclei. A study of the particles emitted in these collisions should give clues as to the nature of dense hot nuclear matter. Some simple models regarding the effects of meson and  $N^*$  production on the properties of dense hot nuclear matter are discussed.

What will be the effect of higher resonances? Models of the strong interactions based on the "bootstrap" idea lead to a density of states that increases exponentially with mass. This results from the fact that each new resonant state can combine with particles of lower or equal mass to make more resonant states.<sup>8</sup> In particular, the statistical bootstrap model leads to a density of states of the form<sup>9,10</sup>

$$N(m) = Cm^{-3}e^{m/\theta_0}, \quad (3)$$

where  $\theta_0$ , the "maximum temperature" of hadron matter, is about 174 MeV as determined from high-energy scattering experiments.<sup>5</sup> The param-

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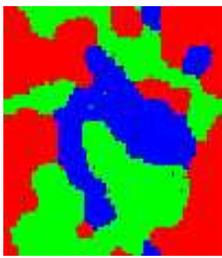
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resonance gas

$$T_c \simeq 174 \text{ MeV} \quad (!!!)$$

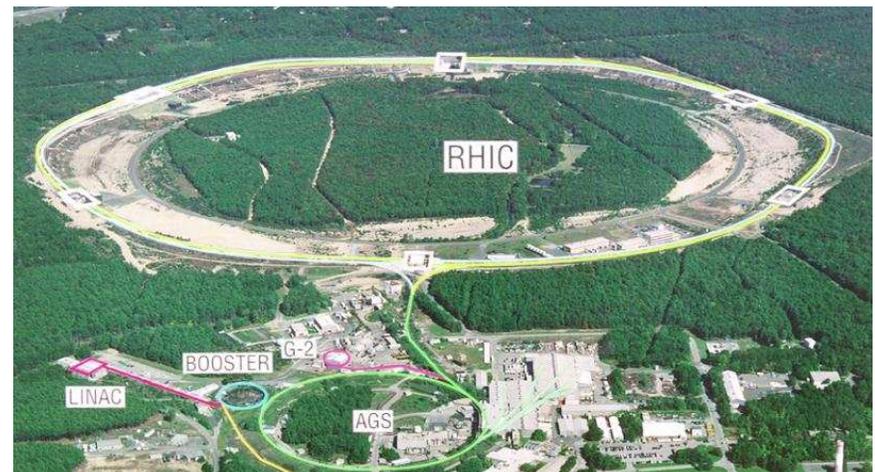


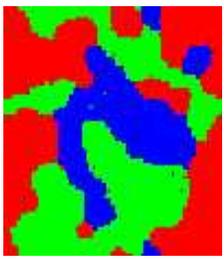
# Lattice Gauge Theory and Heavy Ion Collisions



Lattice Simulations of  
Finite Temperature QCD  
at Bielefeld University

Collision of Au-Au and other ions in the  
Relativistic Heavy Ion Collider (RHIC)  
at Brookhaven Nat. Lab. (BNL)





# Lattice Gauge Theory and Heavy Ion Collisions

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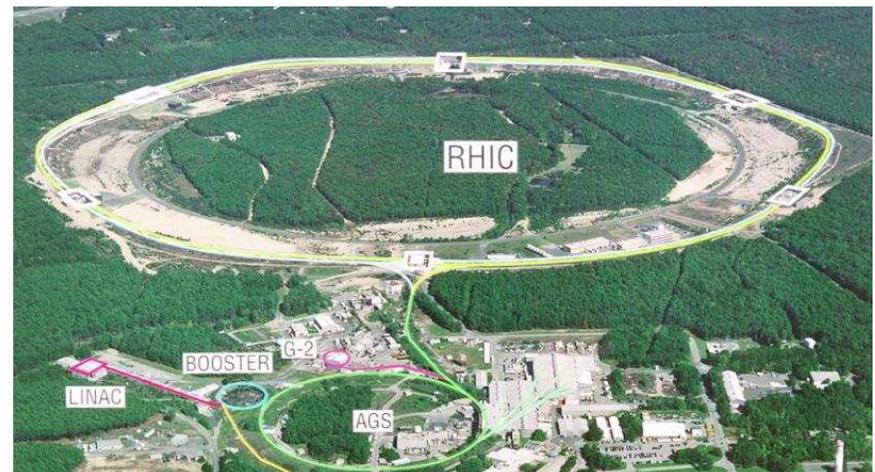
The machines

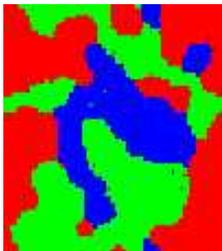
RHIC

circumference:  $\sim 4$  km

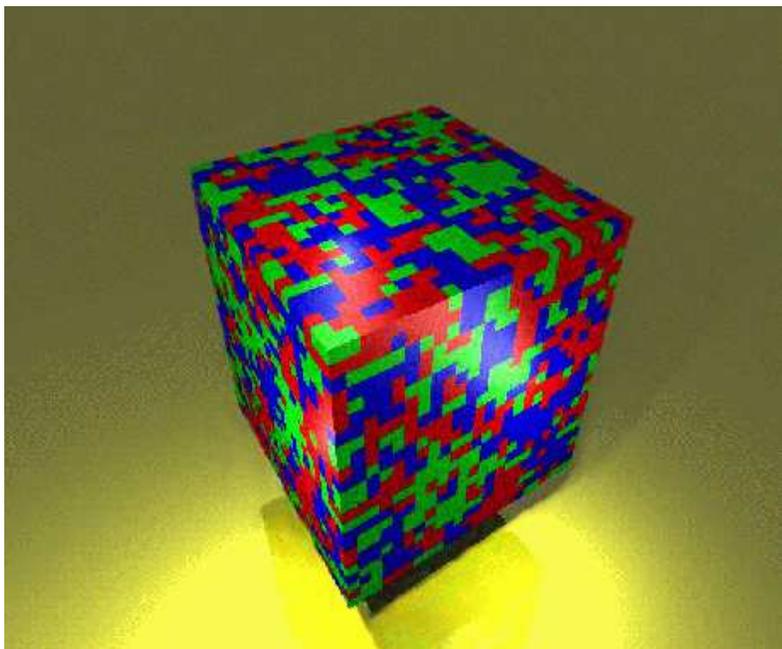
Au-Au collisions

beam energy: 200 GeV/A

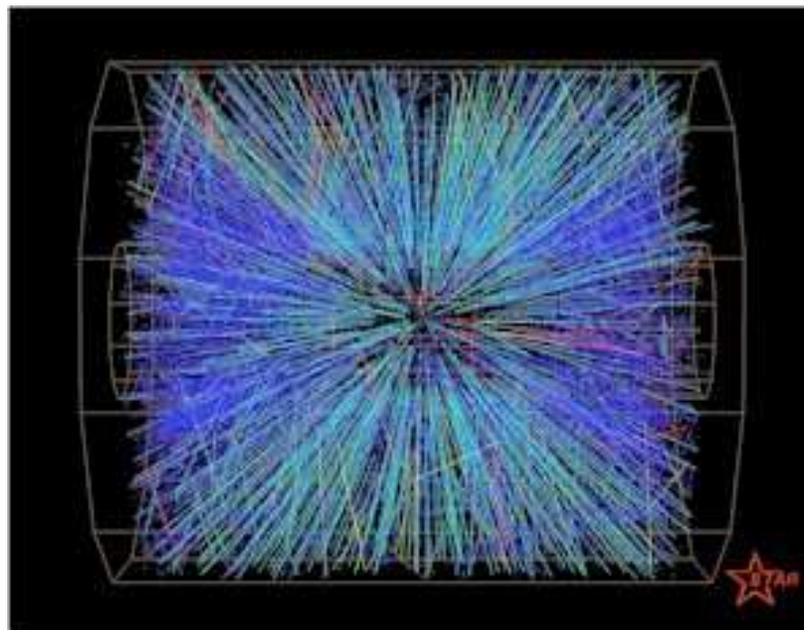


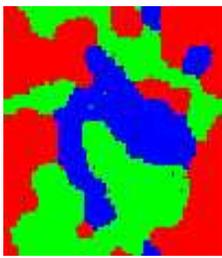


# Lattice Gauge Theory and Heavy Ion Collisions

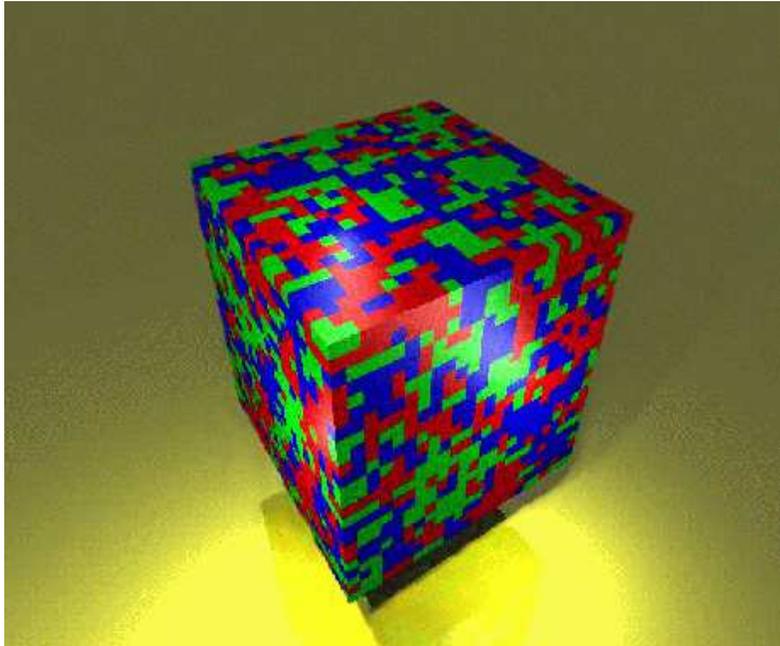


The events





# Lattice Gauge Theory and Heavy Ion Collisions

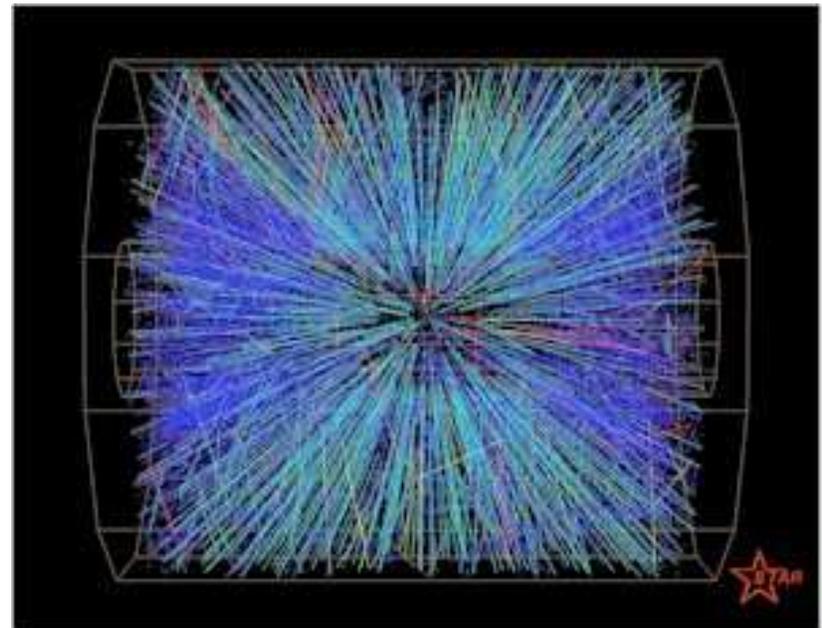


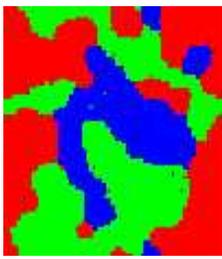
LGT:

- equilibrium thermodynamics of QCD;

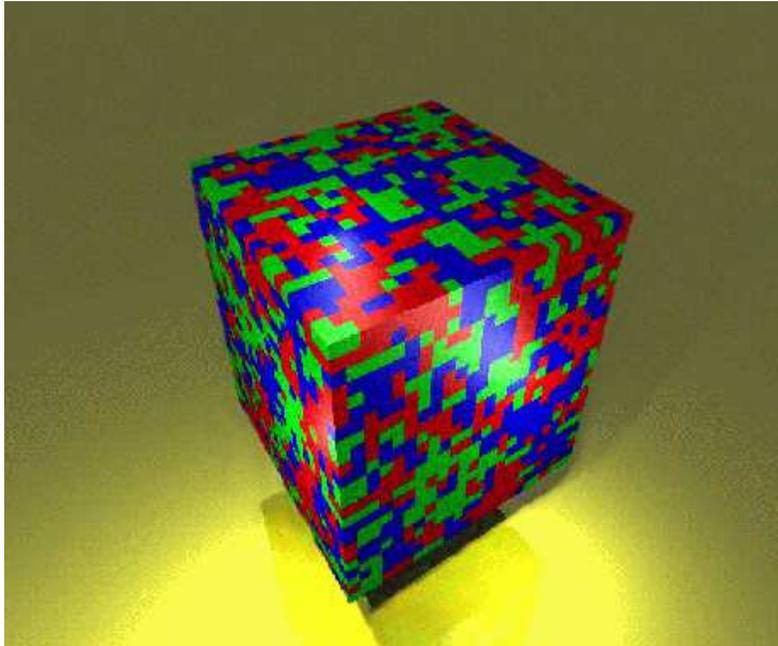
HIC:

- evolution of a dense interacting medium described by QCD;





# Lattice Gauge Theory and Heavy Ion Collisions

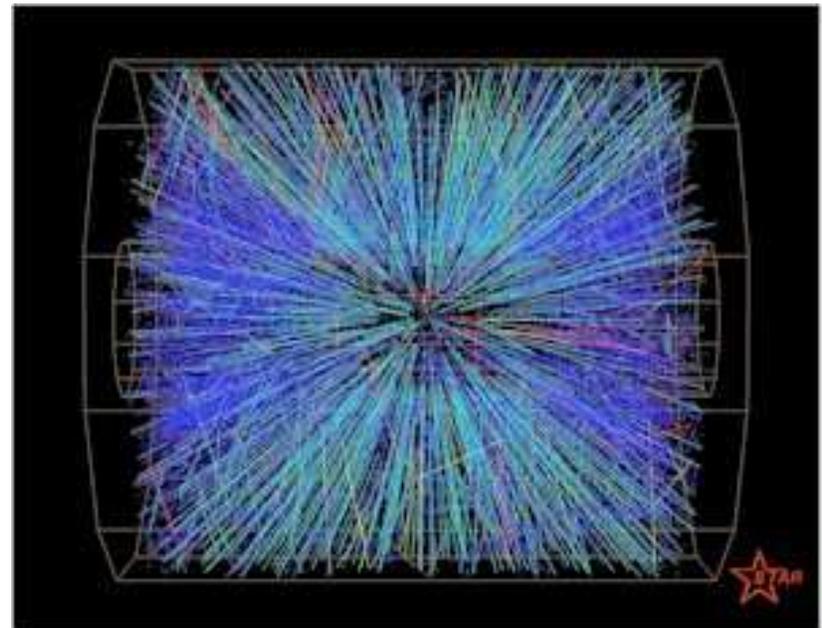


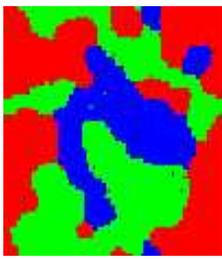
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- equilibrium thermodynamics of QCD;
- formulated in terms of basic degrees of freedom: quarks and gluons;

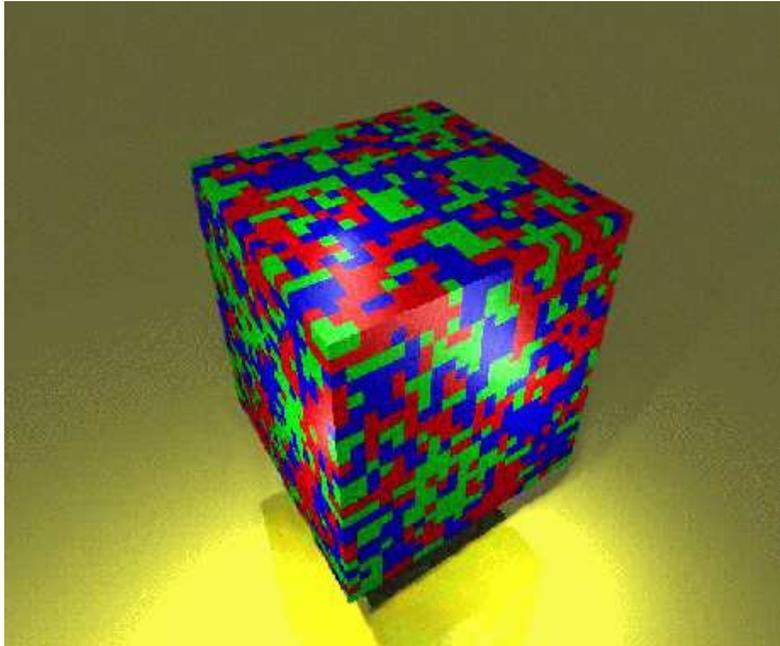
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# Lattice Gauge Theory and Heavy Ion Collisions

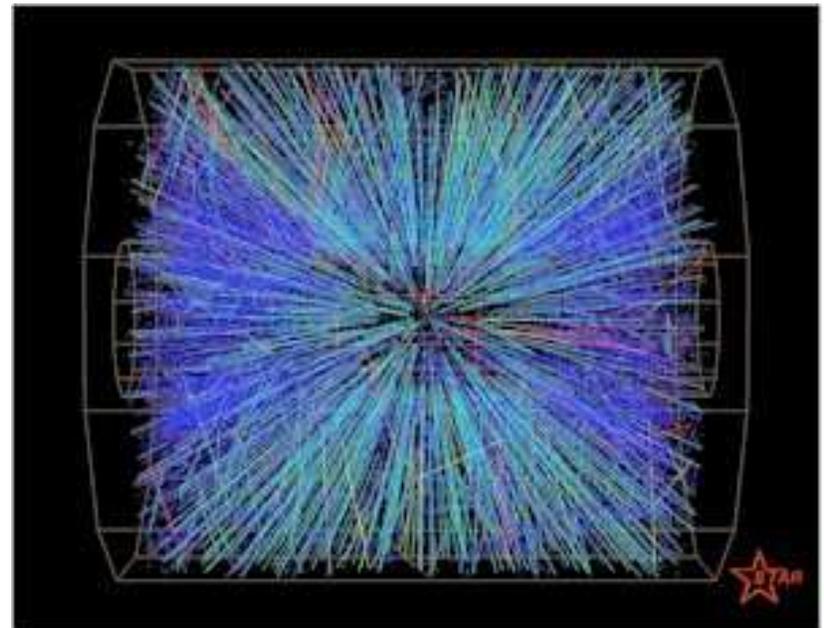


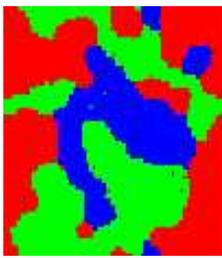
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- equilibrium thermodynamics of QCD;
- formulated in terms of basic degrees of freedom: quarks and gluons;
- observables expressed in terms of temperature and chemical potential

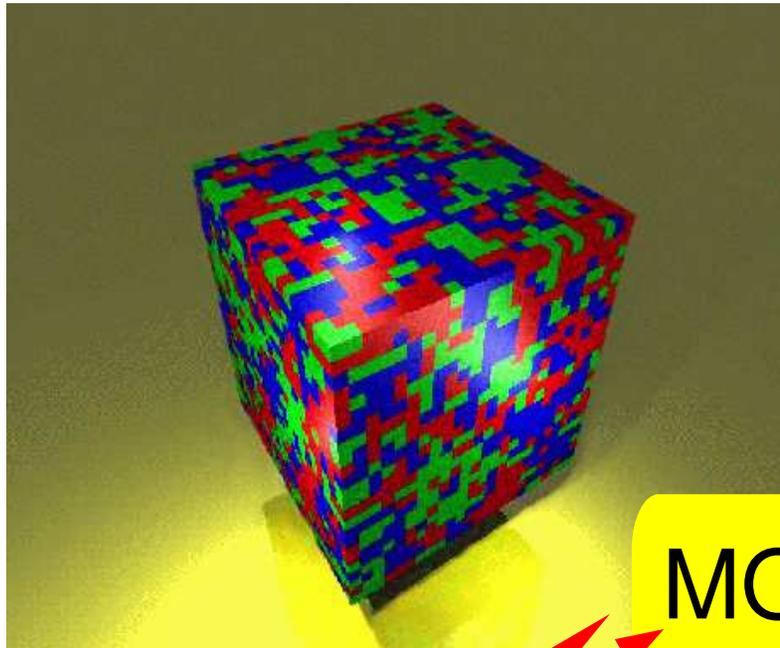
## HIC:

- evolution of a dense interacting medium described by QCD;
- observable properties in terms of hadrons, leptons and photons;
- observables parametrized in terms of energy and particle multiplicities





# Lattice Gauge Theory and Heavy Ion Collisions



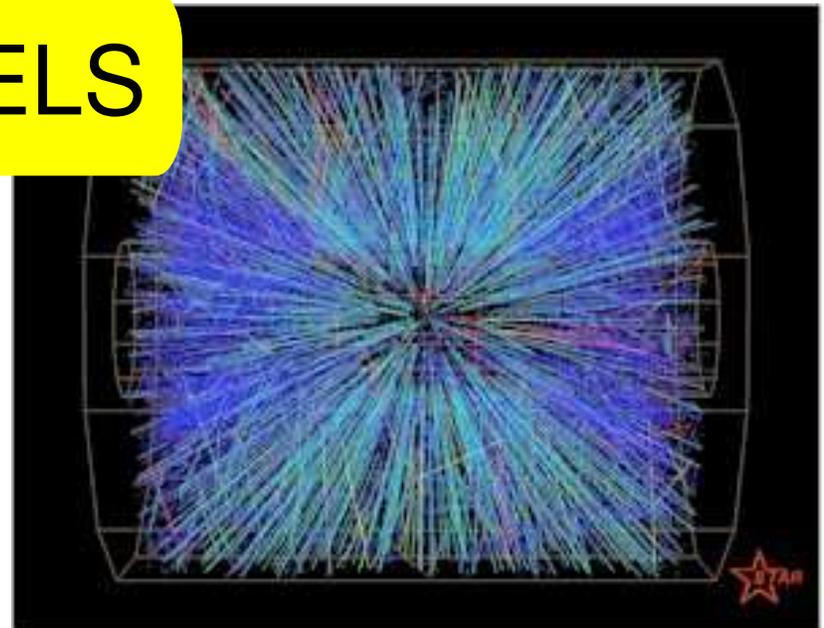
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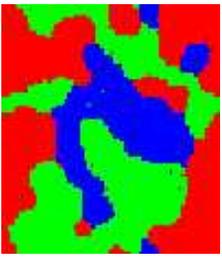
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MODELS

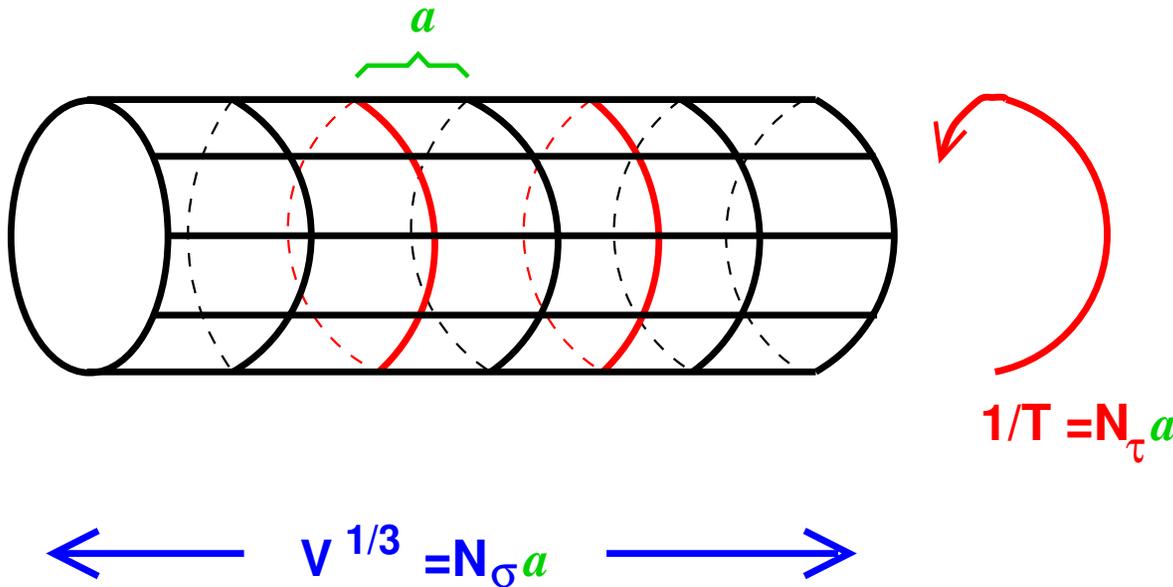
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# Analyzing hot and dense matter on the lattice: $N_\sigma^3 \times N_\tau$



APEmille

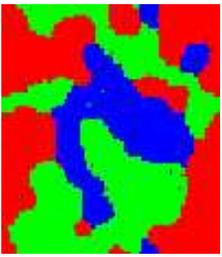


Quantum Chromo Dynamics

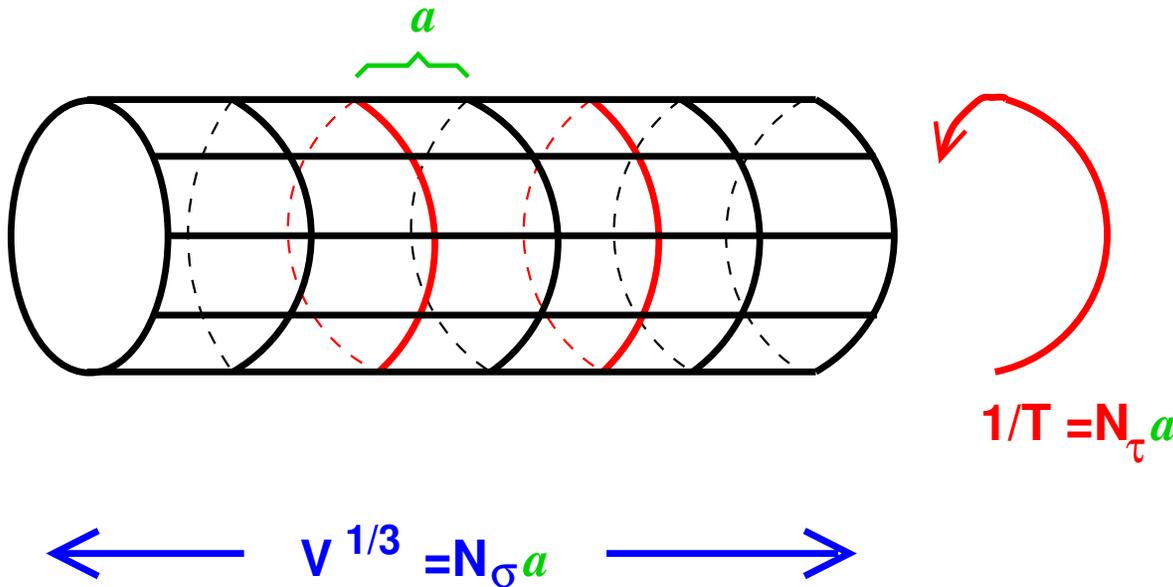
partition function:  $Z(V, T, \mu) = \int \mathcal{D}\mathcal{A} \mathcal{D}\psi \mathcal{D}\bar{\psi} e^{-S_E}$

$$S_E = \int_0^{1/T} dx_0 \int_V d^3x \mathcal{L}_E(\mathcal{A}, \psi, \bar{\psi}, \mu)$$

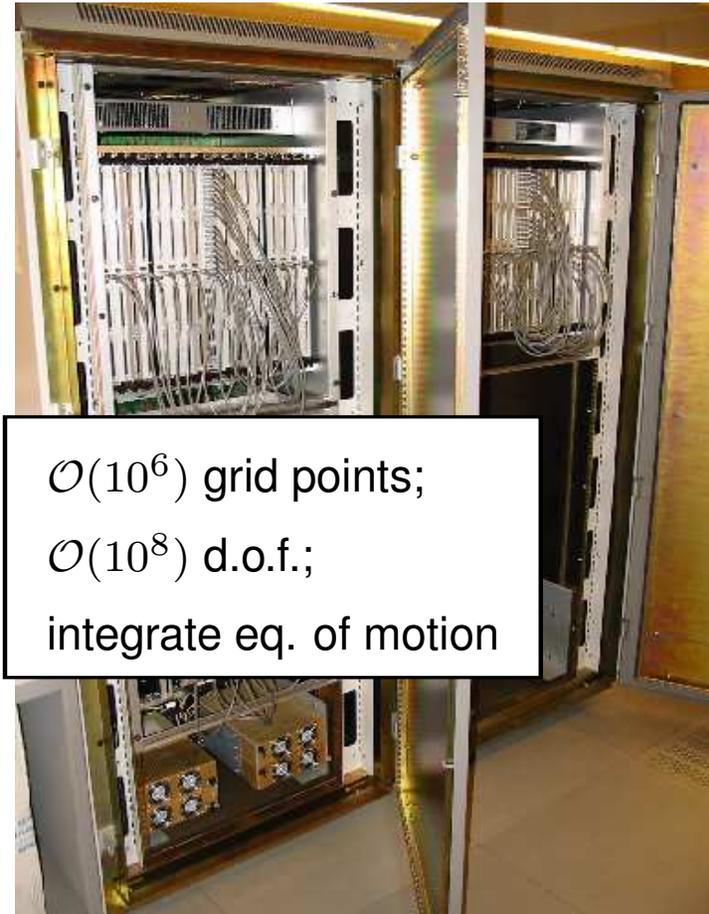
temperature
volume
chemical potential



# Analyzing hot and dense matter on the lattice: $N_\sigma^3 \times N_\tau$



**APEmille**



$\mathcal{O}(10^6)$  grid points;  
 $\mathcal{O}(10^8)$  d.o.f.;  
 integrate eq. of motion

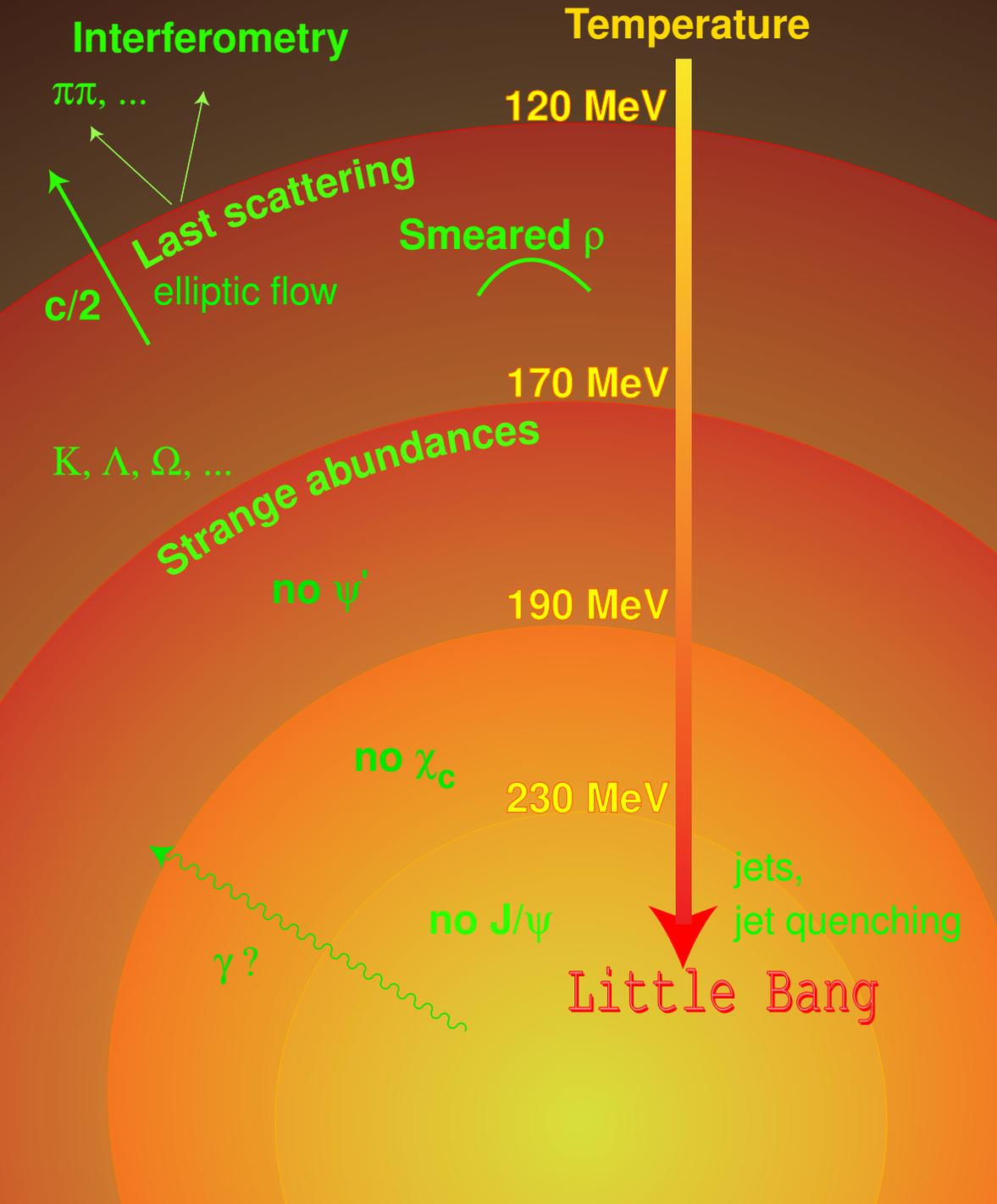
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temperature
volume
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# Towards A New State of Matter



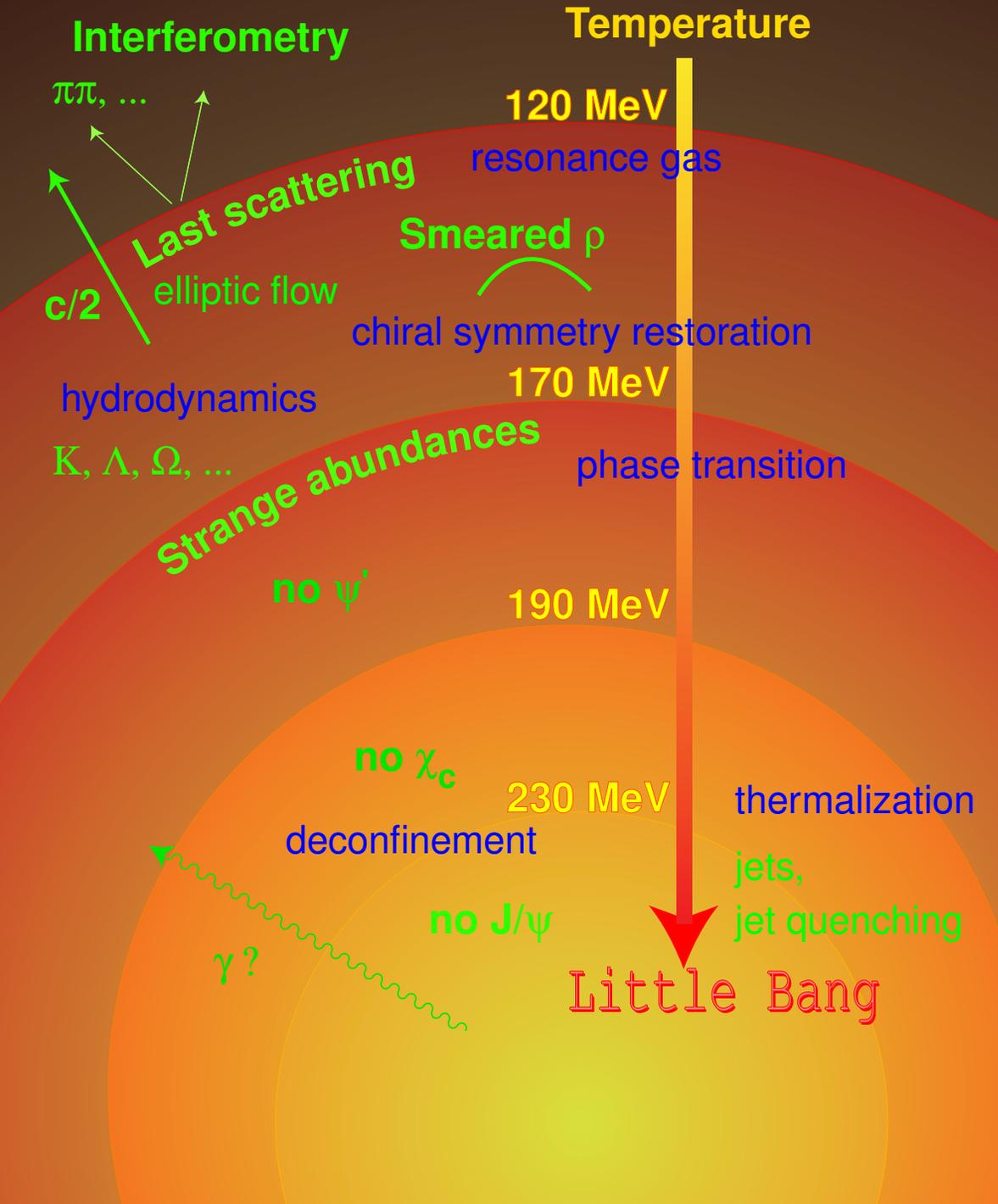
Where lattice calculations do/will contribute to the

development of theoretical concepts

and the

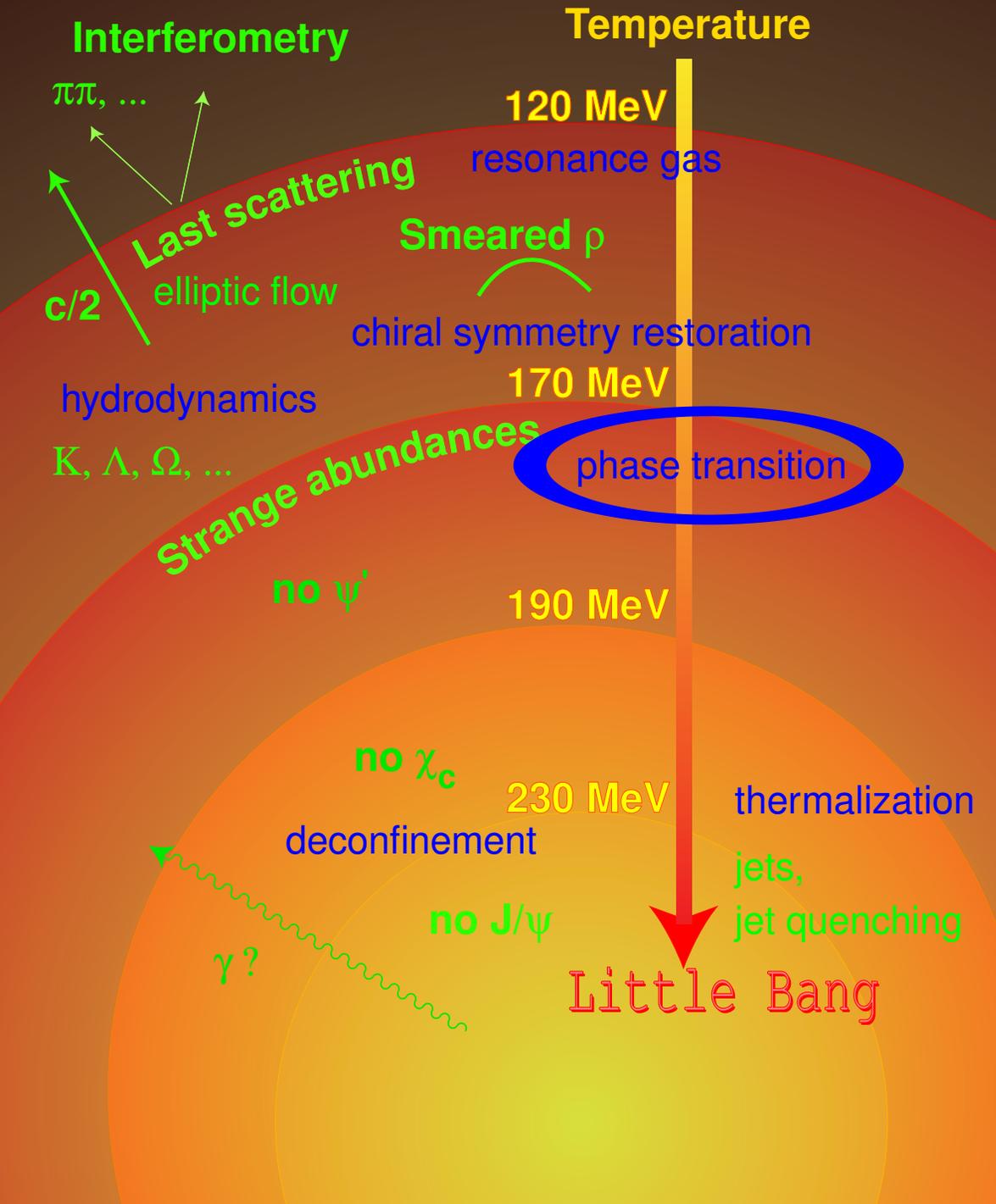
analysis of experimental observables

# Towards A New State of Matter



Where lattice calculations do/will contribute to the development of theoretical concepts and the analysis of experimental observables

# Towards A New State of Matter



Where lattice calculations do/will contribute to the

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and the

analysis of experimental observables

$$T_c, \epsilon_c$$

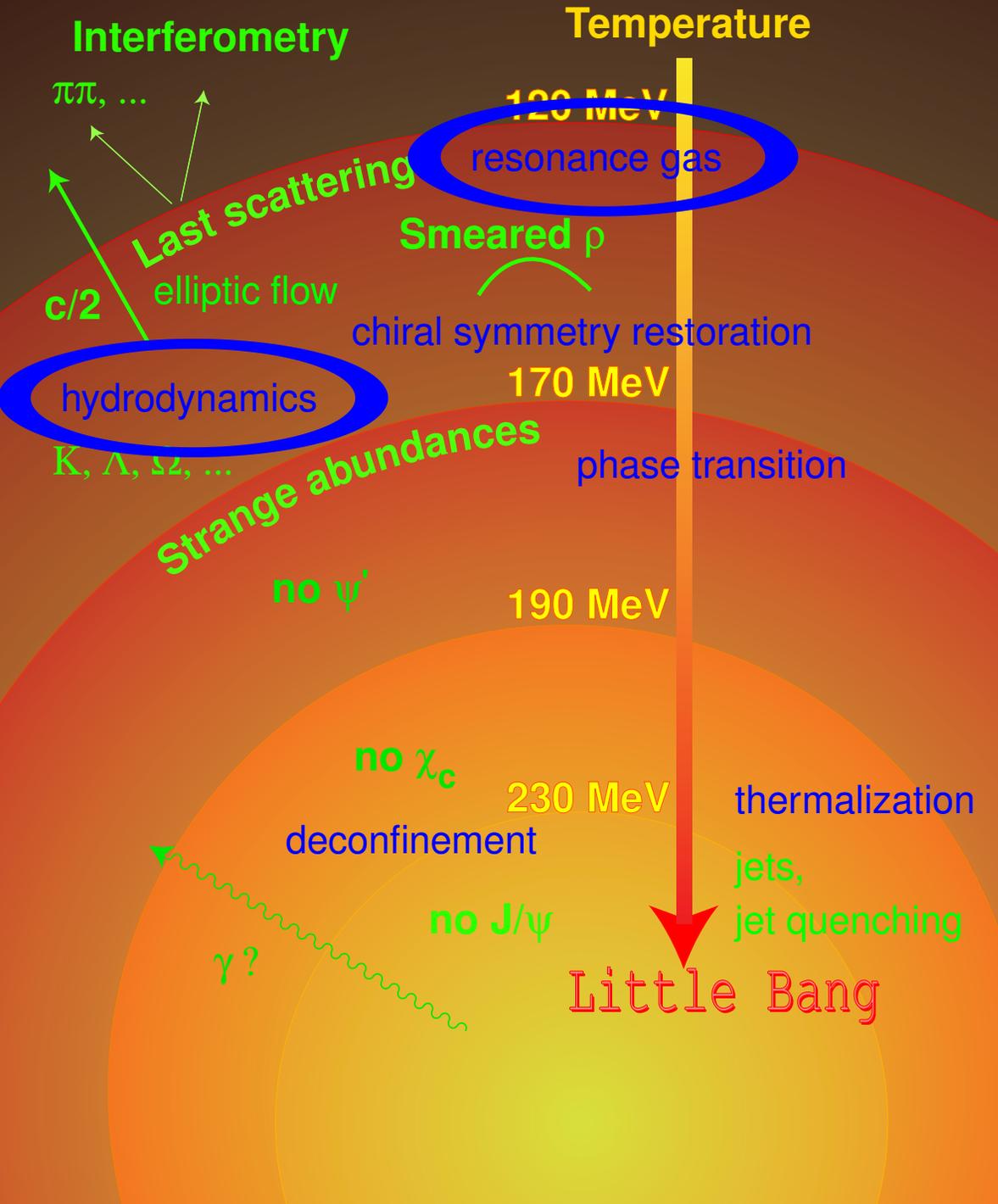
phase diagram in the  $(T, \mu_B)$ -plane;

$\mu \simeq 0$  : RHIC (LHC)

$\mu > 0$  : SPS (GSI future)

chiral critical point

# Towards A New State of Matter



Where lattice calculations do/will contribute to the

development of theoretical concepts

and the

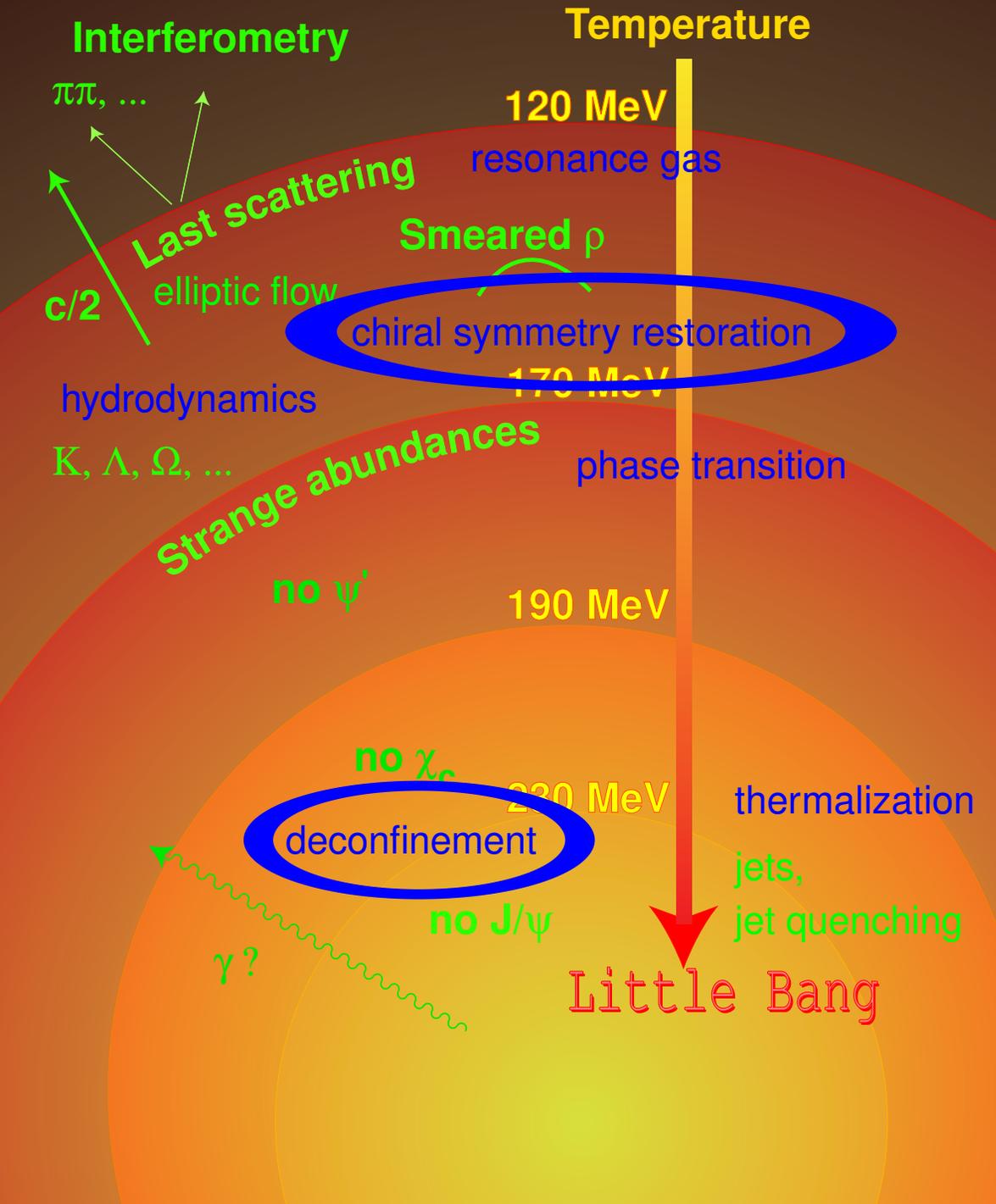
analysis of experimental observables

*EoS*

energy density, pressure, velocity of sound,...; susceptibilities (baryon number fluctuations);

strangeness contribution

# Towards A New State of Matter



Where lattice calculations do/will contribute to the

development of theoretical concepts

and the

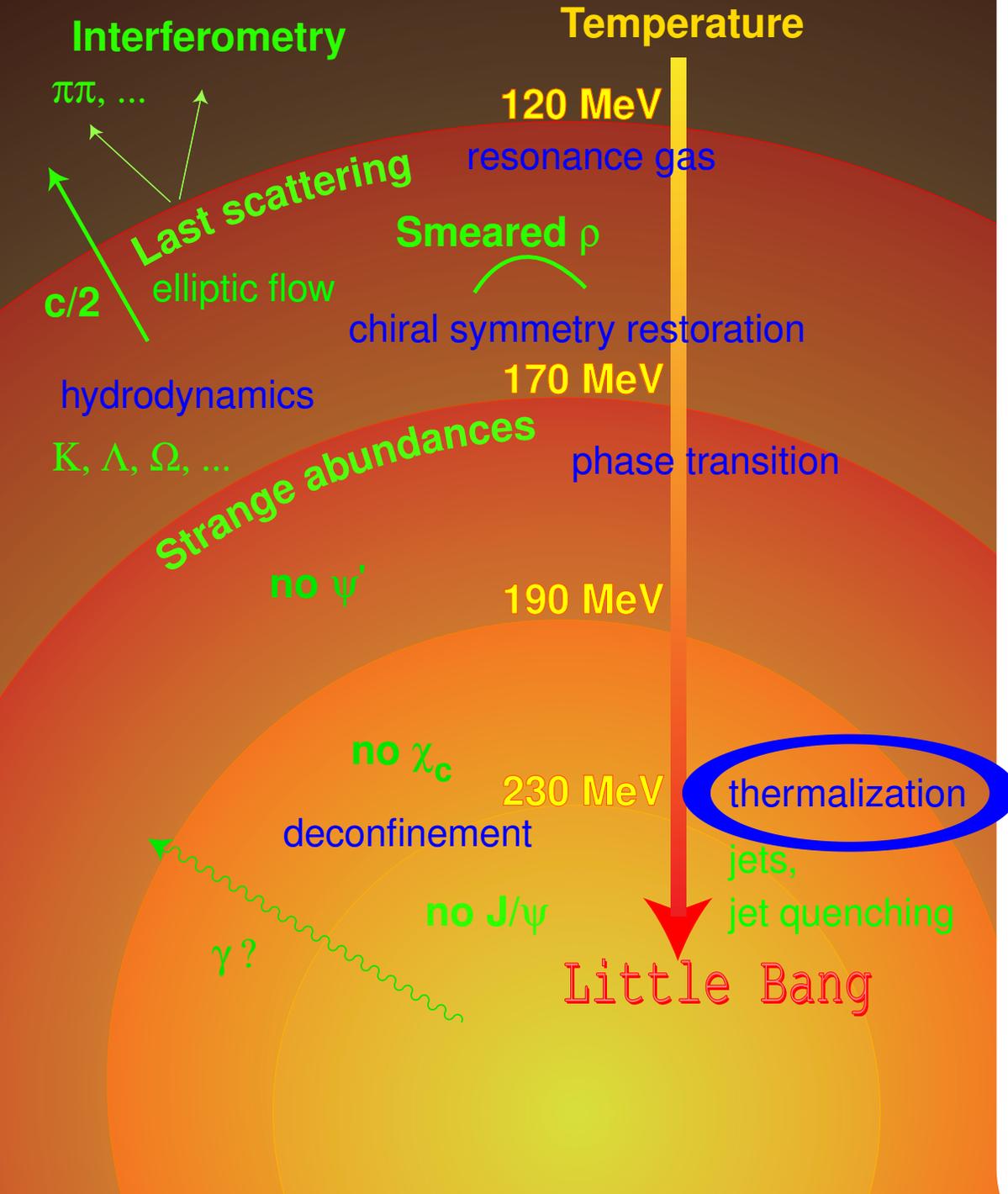
analysis of experimental observables

*In – medium hadron properties*

heavy quark potential, screening;  
charmonium spectroscopy;  
light quark bound states;

thermal dilepton rates

# Towards A New State of Matter



Where lattice calculations do/will contribute to the

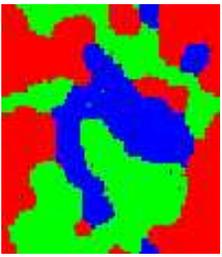
development of theoretical concepts

and the

analysis of experimental observables

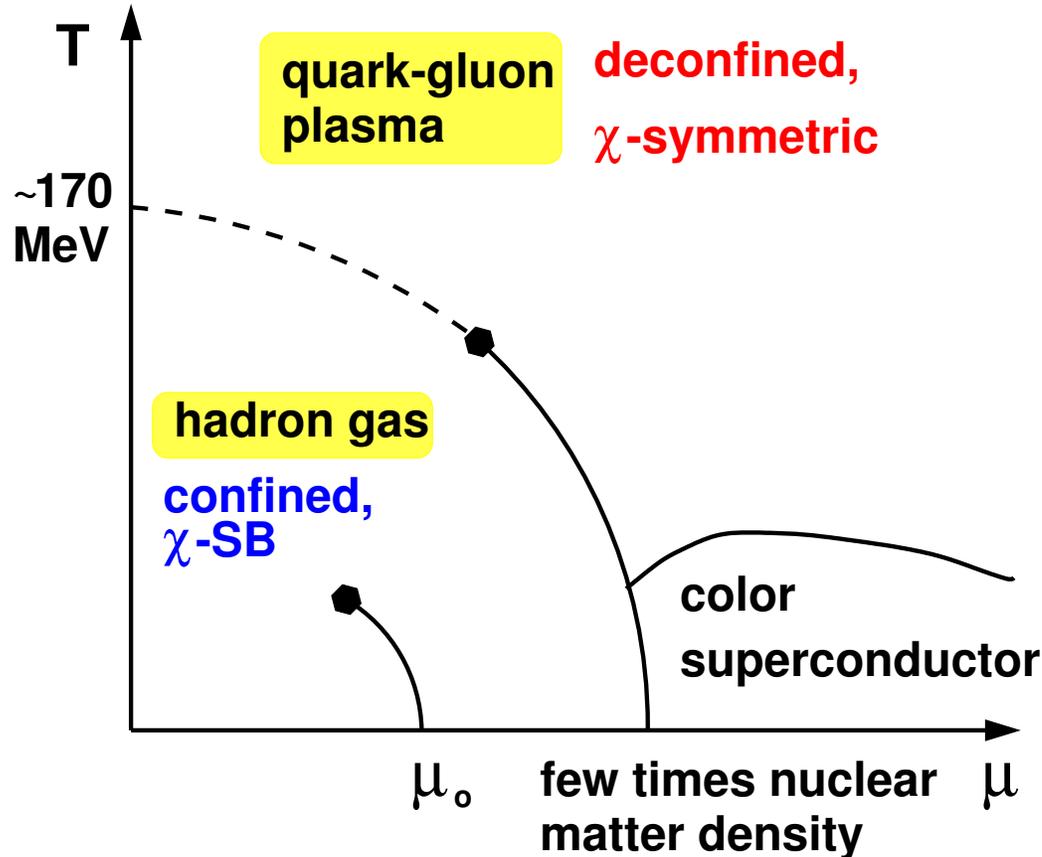
*short vs. long distance physics*

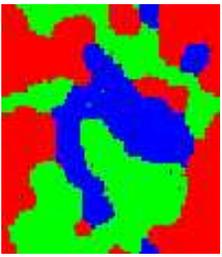
running coupling constant;  
transport coefficients



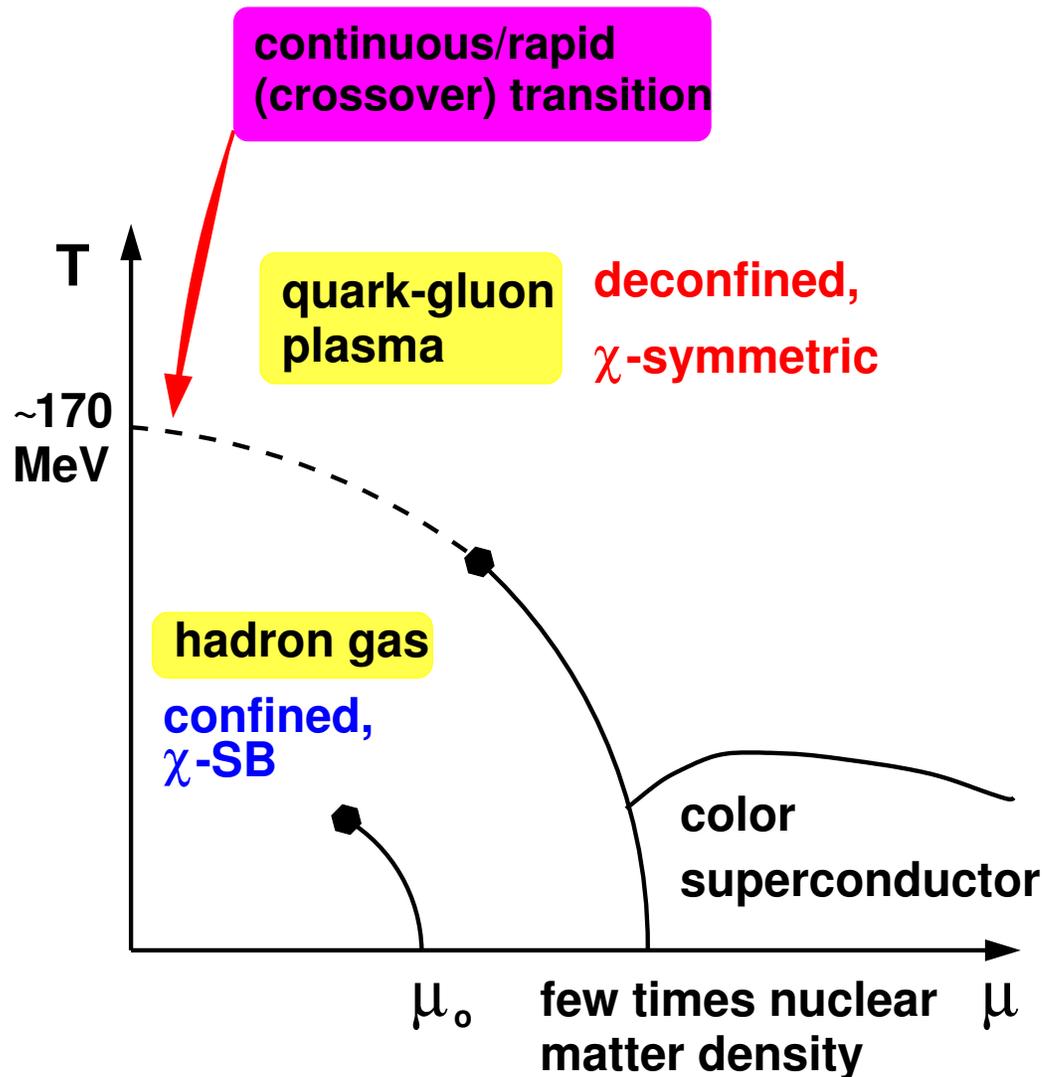
# Critical behavior in hot and dense matter: phase diagram

crossover vs.  
phase transition



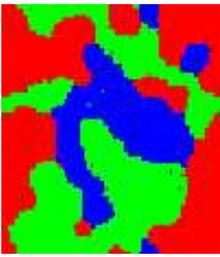


# Critical behavior in hot and dense matter: phase diagram

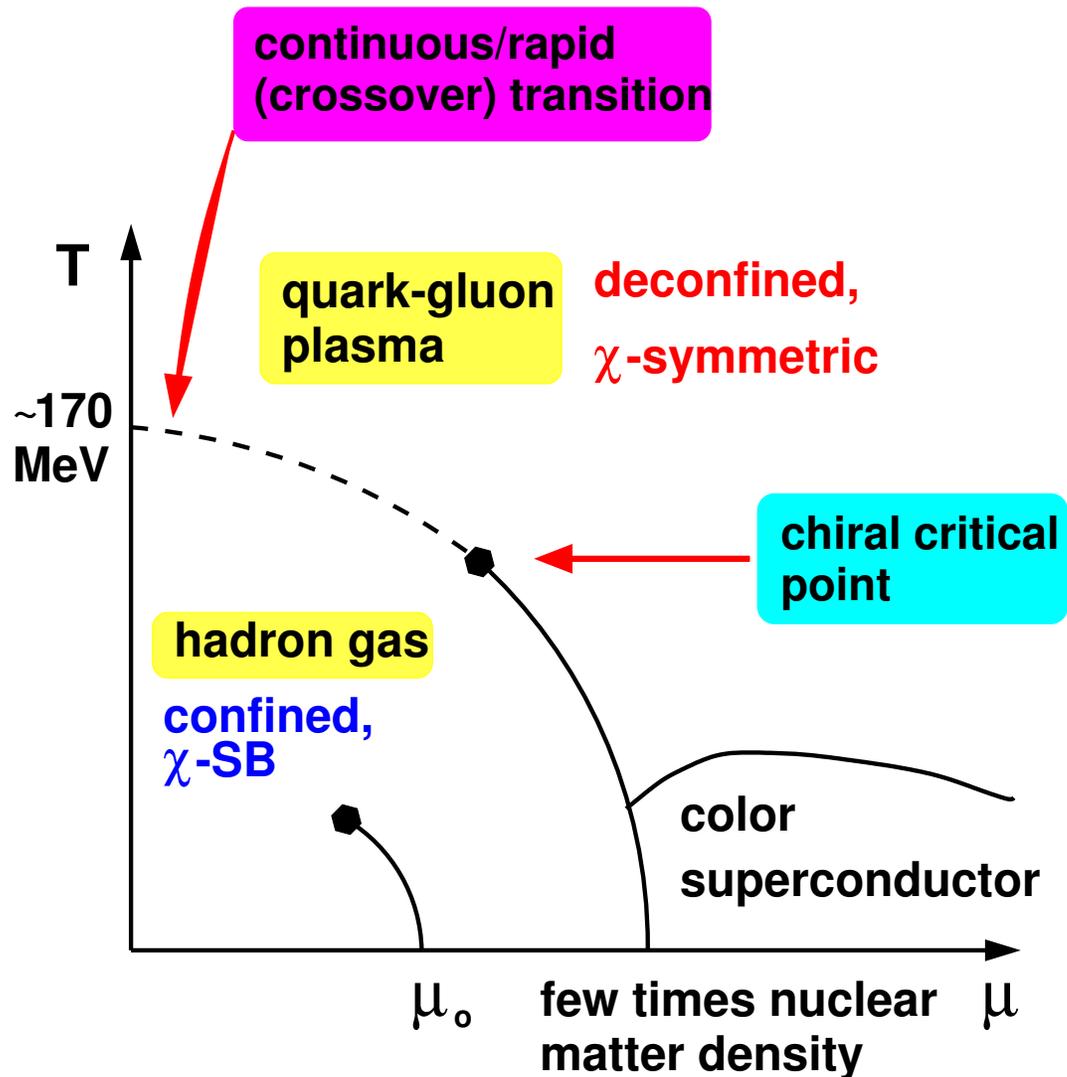


continuous transition for small chemical potential and small quark masses at

$$T_c \simeq 170 \text{ MeV}$$
$$\epsilon_c \simeq 0.7 \text{ GeV}/\text{fm}^3$$



# Critical behavior in hot and dense matter: phase diagram

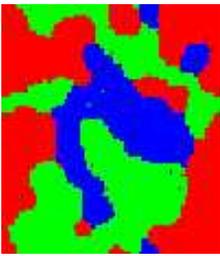


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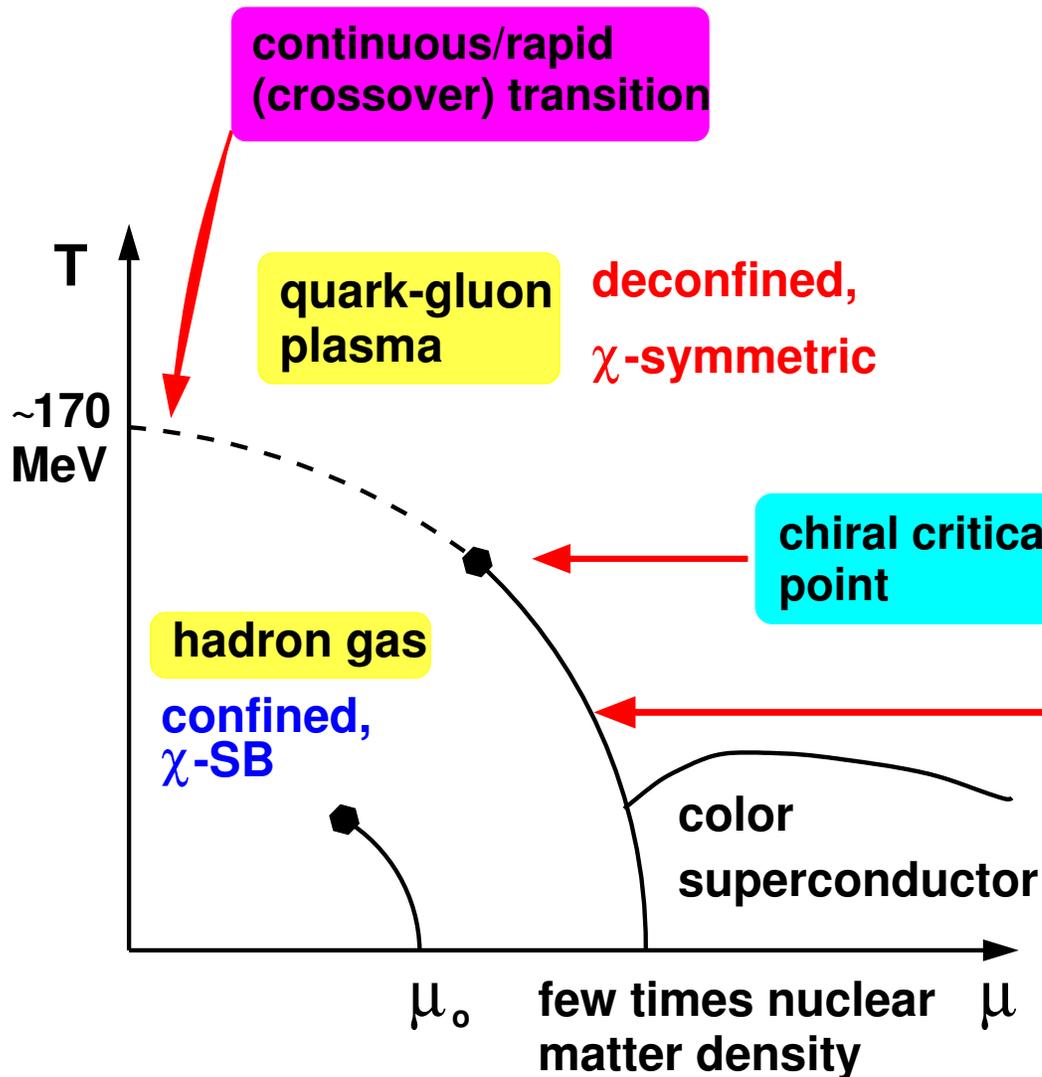
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2nd order phase transition; Ising universality class

$$T_c(\mu) \text{ under investigation}$$



# Critical behavior in hot and dense matter: phase diagram



continuous transition for small chemical potential and small quark masses at

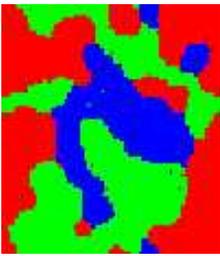
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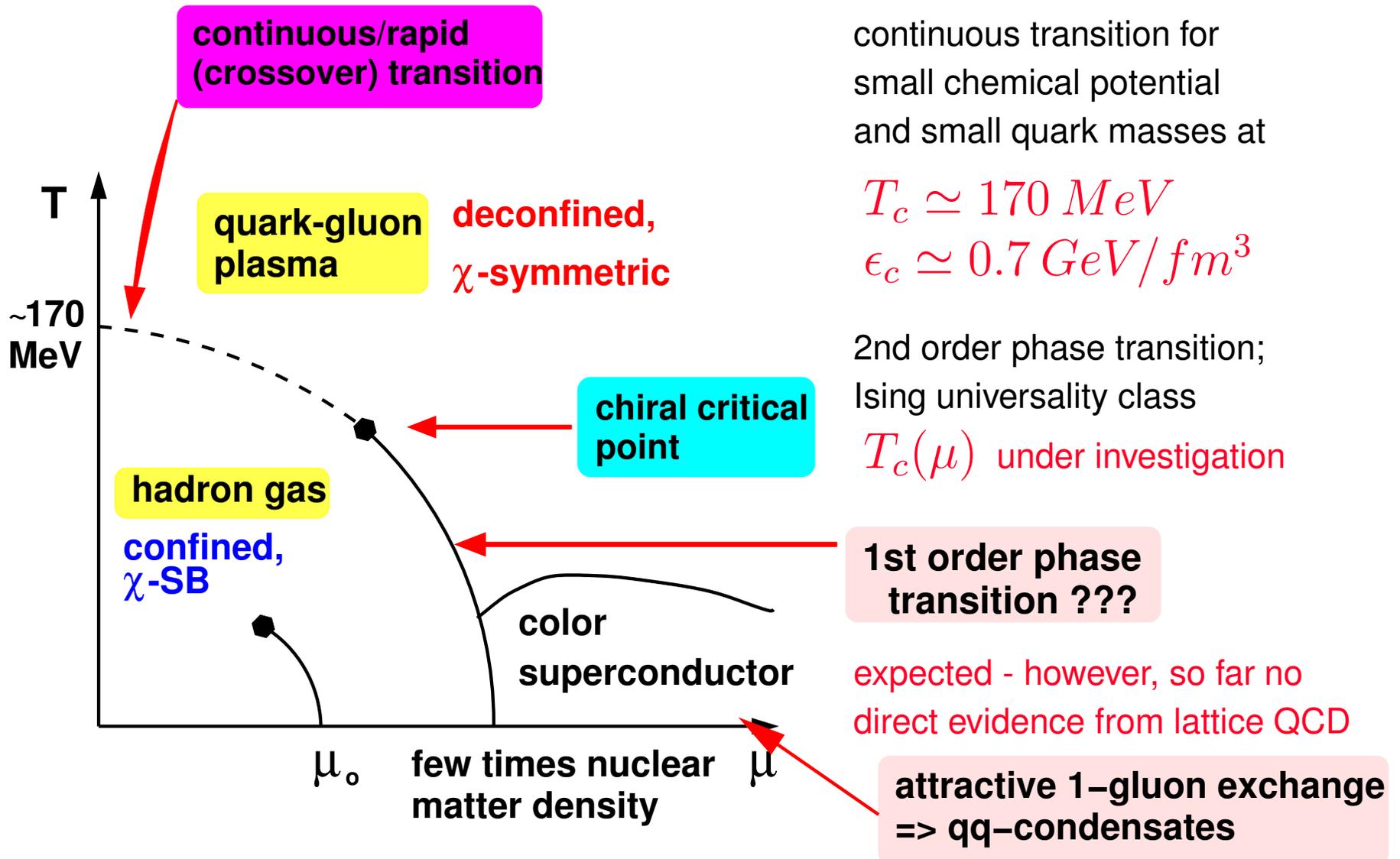
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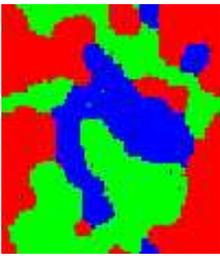
1st order phase transition ???

expected - however, so far no direct evidence from lattice QCD

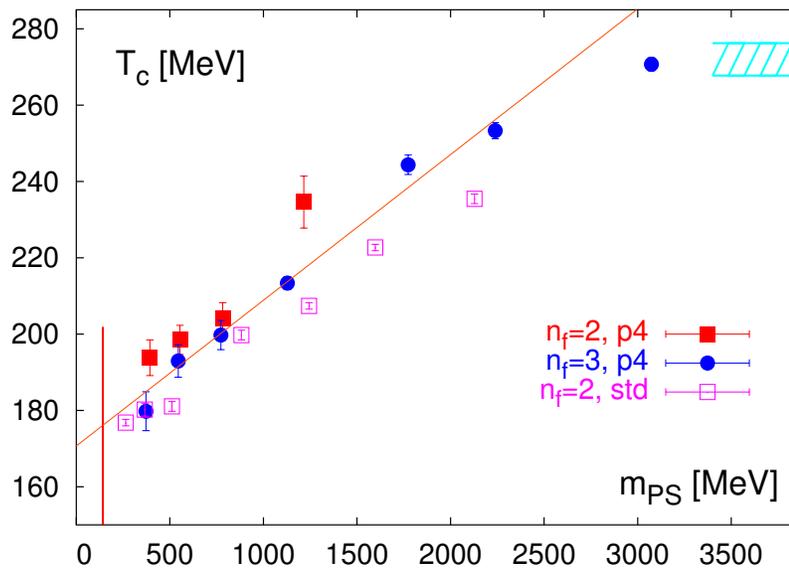


# Critical behavior in hot and dense matter: phase diagram





# Critical temperature, equation of state



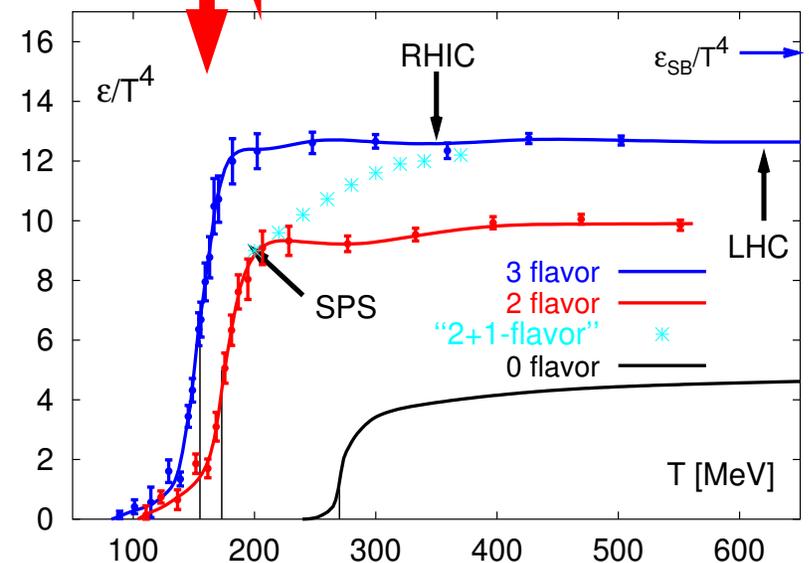
$$\epsilon_c \simeq (6 \pm 2) T_c^4$$

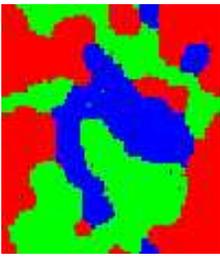
$$\simeq (0.3 - 1.3) \text{ GeV}/\text{fm}^3$$

$$T_c = (173 \pm 8 \pm \text{sys}) \text{ MeV}$$

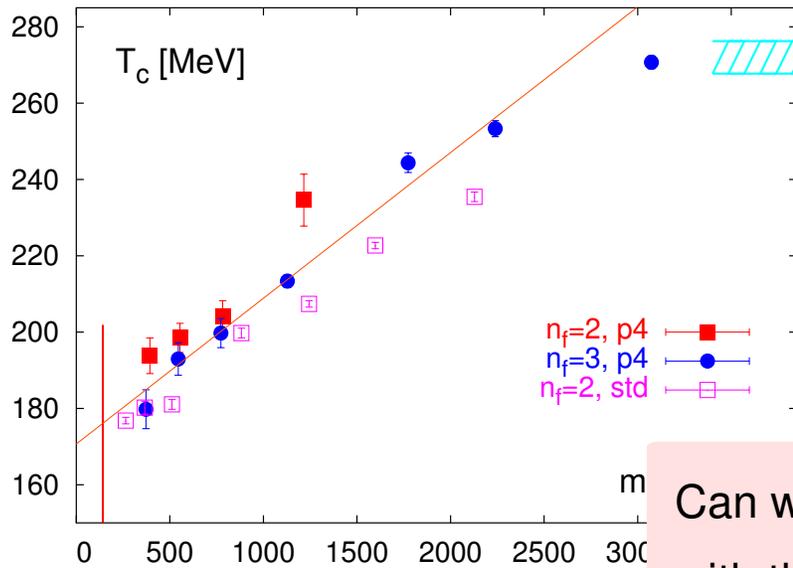
FK, E. Laermann, A. Peikert,  
Nucl. Phys. B605 (2001) 579

energy density for 0, 2 and 3-flavor QCD





# Critical temperature, equation of state

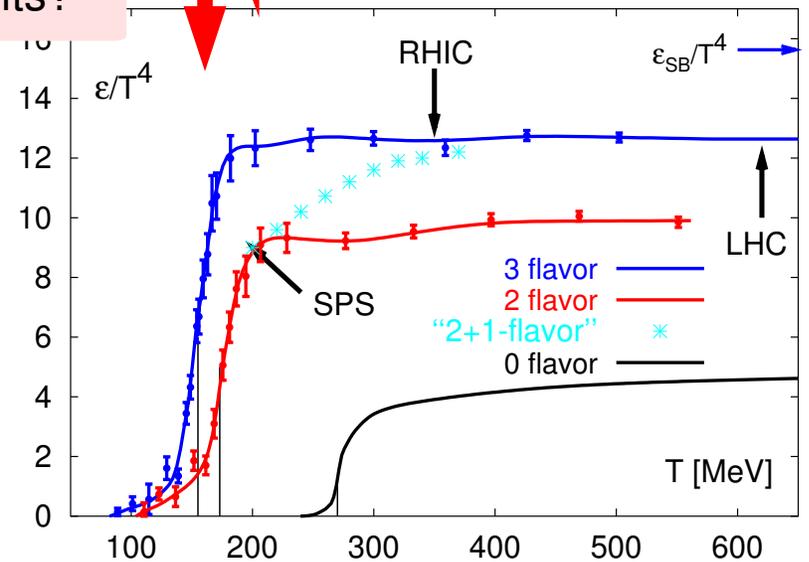


$$\epsilon_c \simeq (6 \pm 2) T_c^4$$

$$\simeq (0.3 - 1.3) \text{ GeV}/\text{fm}^3$$

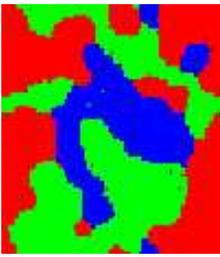
Can we be satisfied with these results?

energy density for 0, 2 and 3-flavor QCD

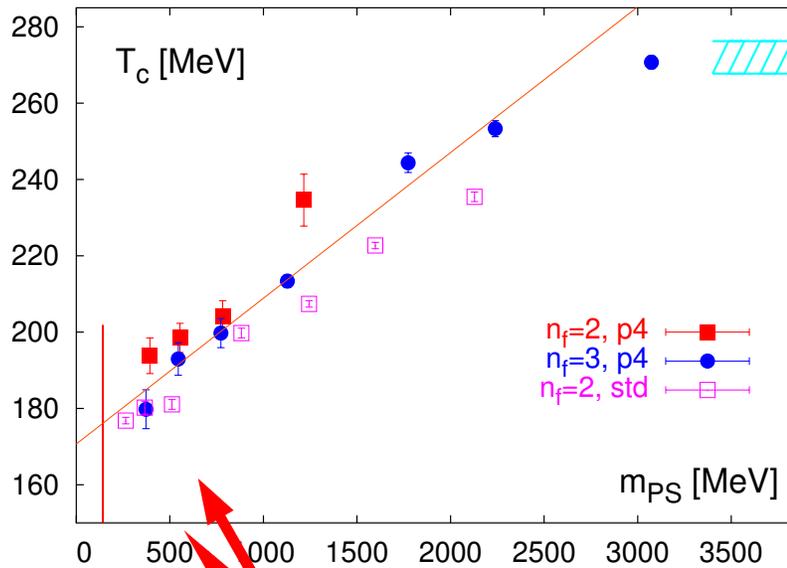


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FK, E. Laermann, A. Peikert,  
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# Critical temperature, equation of state



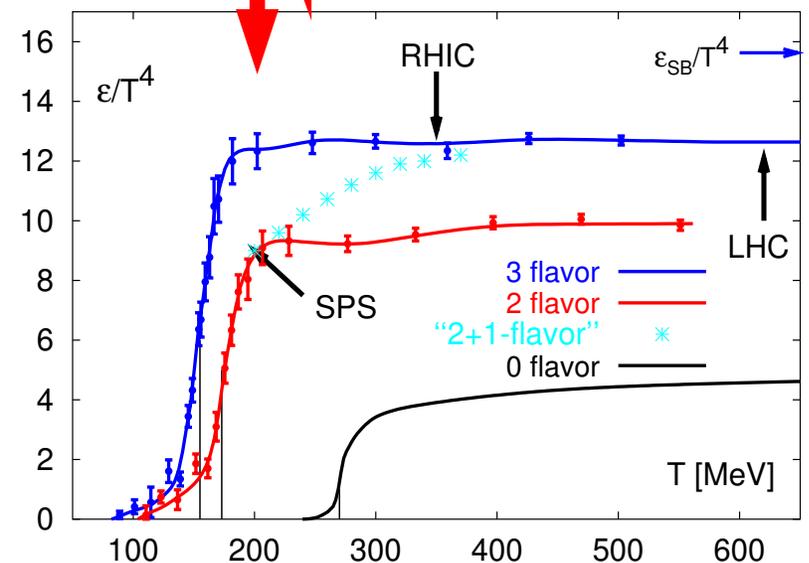
$T_c$

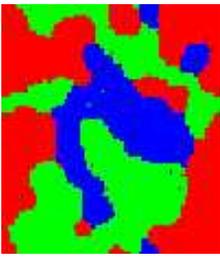
- $m_{PS} \gtrsim 300 \text{ MeV}$  (chiral limit??)
- $a \simeq 0.2 \text{ fm}$  (continuum limit??)
- improved staggered fermions,  
 $\Rightarrow$  flavor symmetry breaking  
 (need even better fermion actions)

$\epsilon_c$

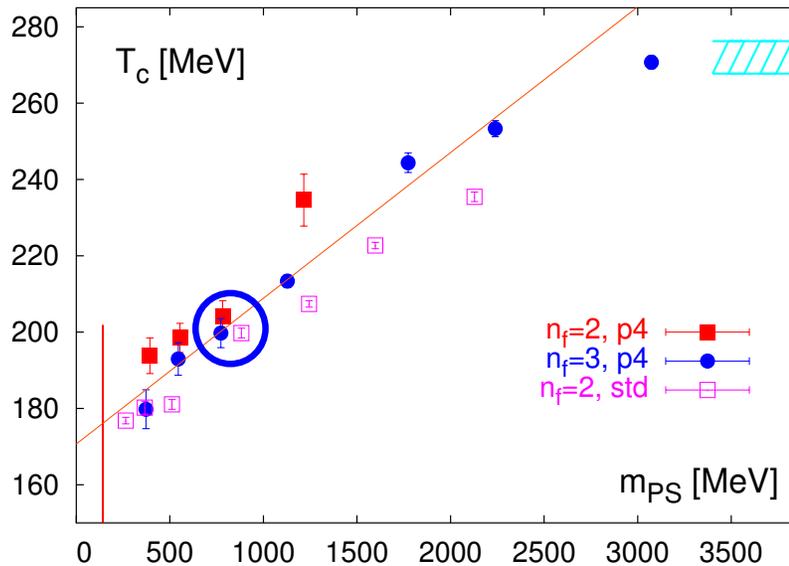
- $m_{PS} \simeq 770 \text{ MeV}$  (!!!)
- $V \simeq (4 \text{ fm})^3$  (thermodynamic limit)

energy density for 0, 2 and 3-flavor QCD

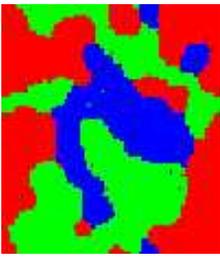




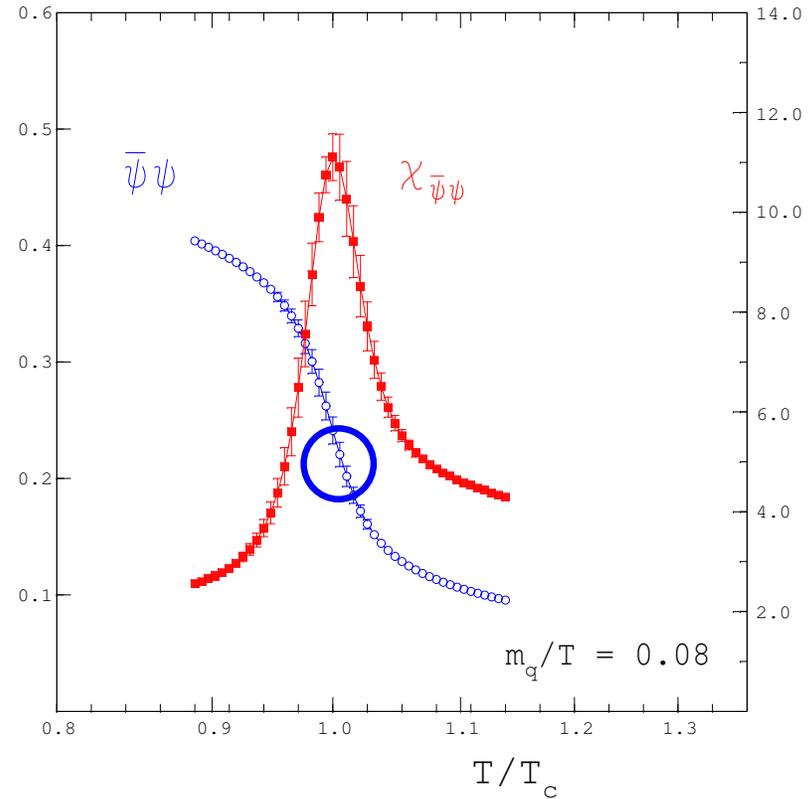
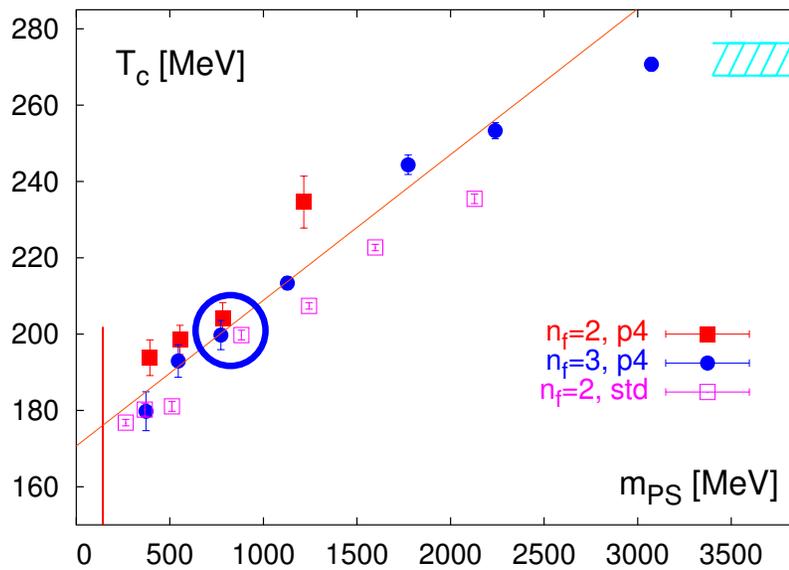
# What triggers the transition in strongly interacting matter?



QCD transition in a world with  
heavy pions:  $m_\pi \simeq 770 \text{ MeV}$   
not a "true phase transition"



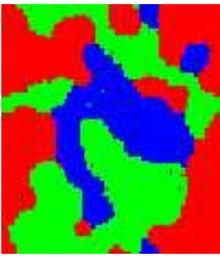
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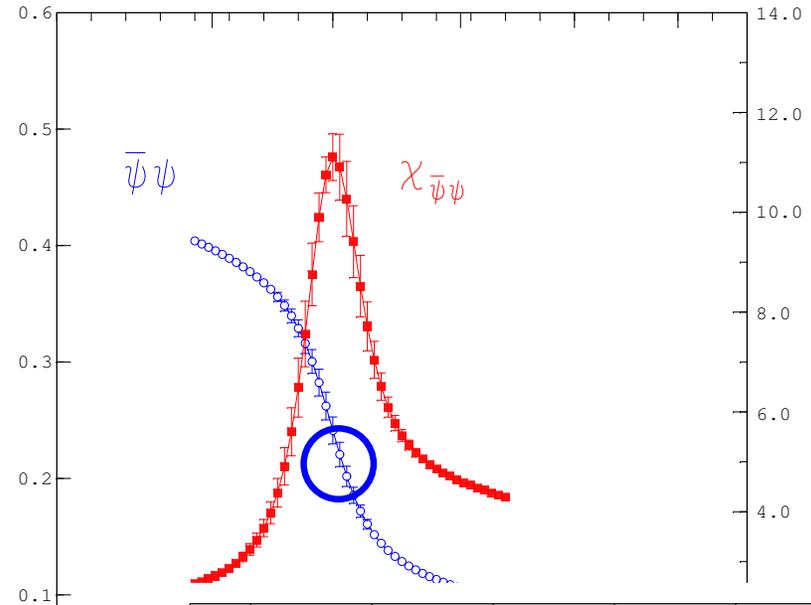
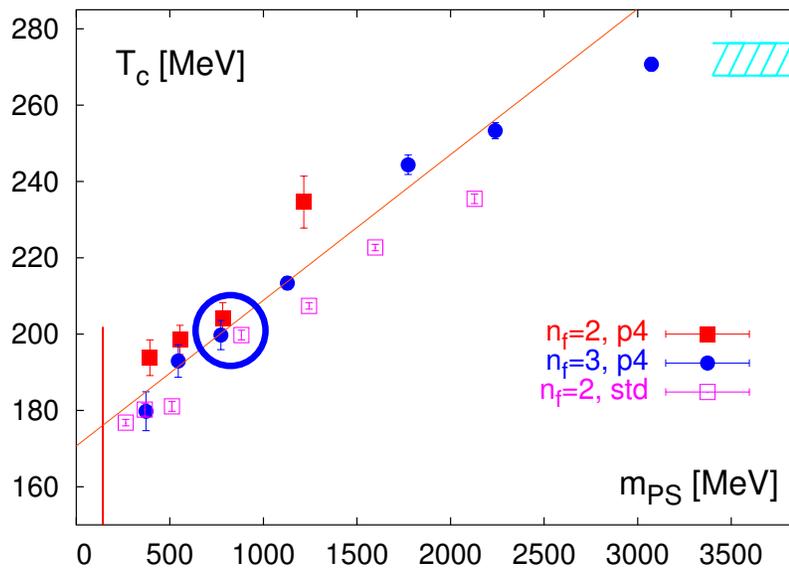
chiral symmetry restoration

– rapid drop of  $\langle \bar{\psi}\psi \rangle$

however:  $\langle \bar{\psi}\psi \rangle(T_c) > 0$



# What triggers the transition in strongly interacting matter?



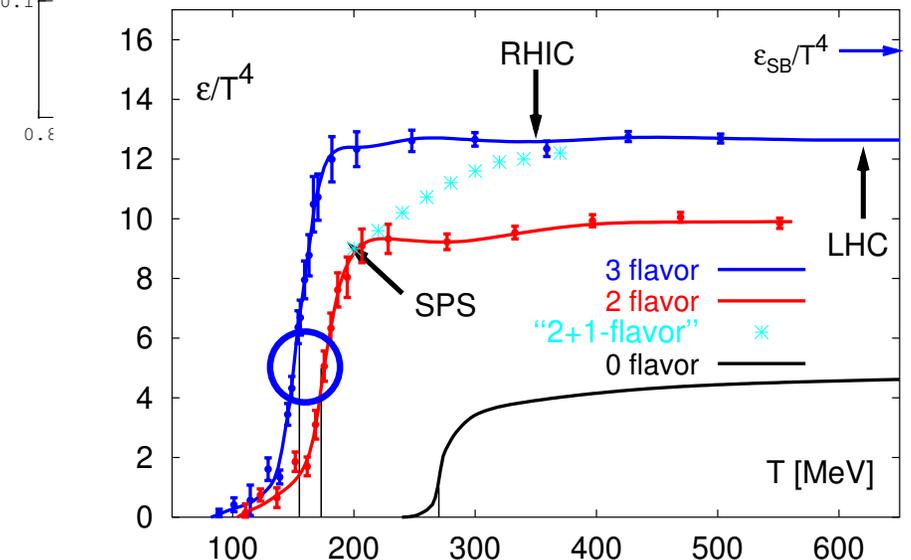
chiral symmetry restoration

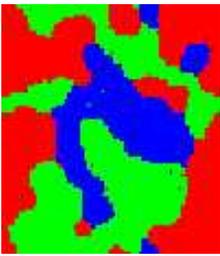
– rapid drop of  $\langle \bar{\psi}\psi \rangle$

however:  $\langle \bar{\psi}\psi \rangle(T_c) > 0$

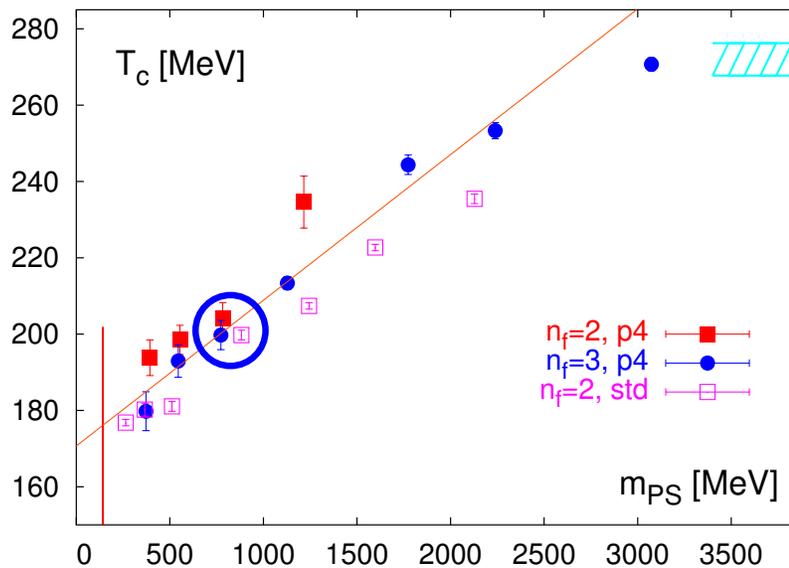
deconfinement

– rapid increase of d.o.f.





# What triggers the transition in strongly interacting matter?



chiral symmetry restoration

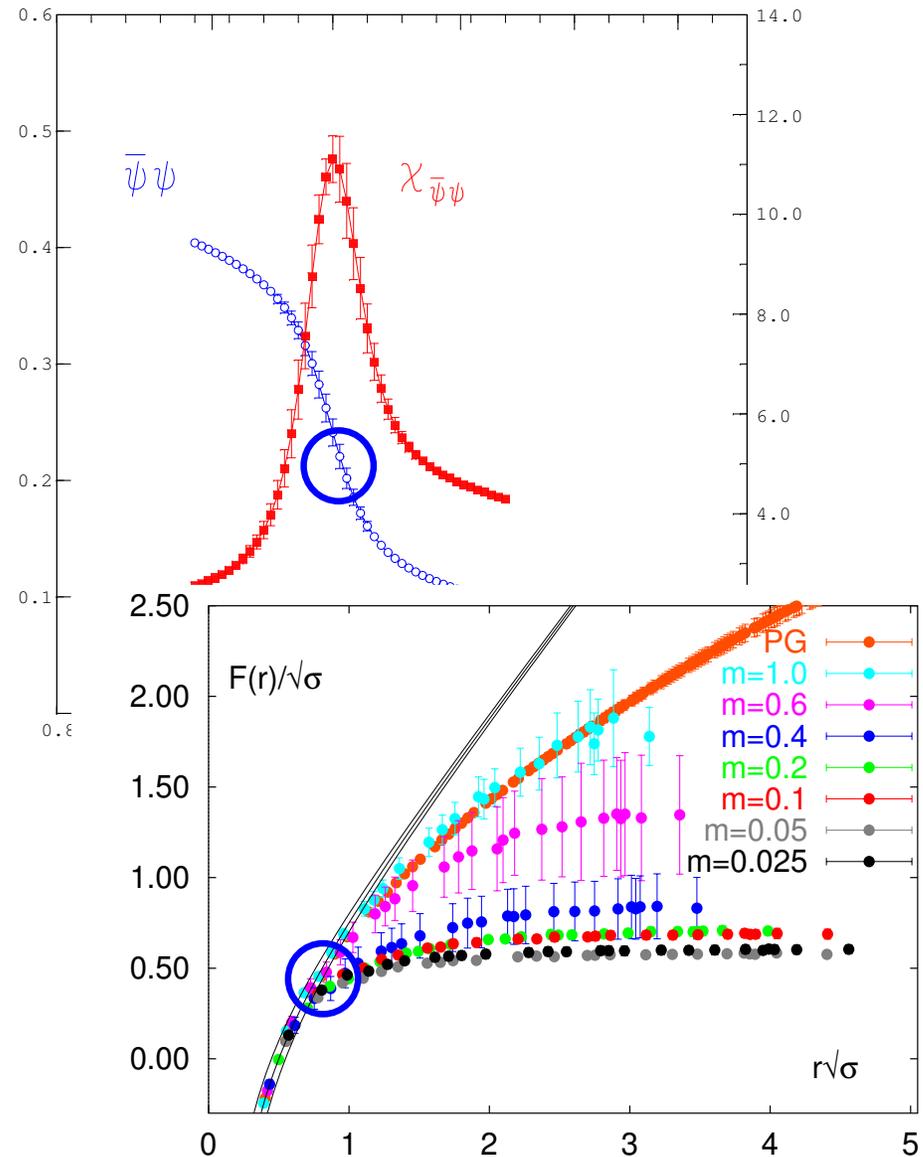
– rapid drop of  $\langle \bar{\psi}\psi \rangle$

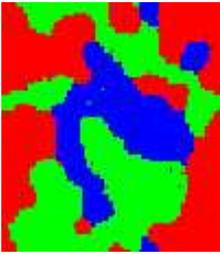
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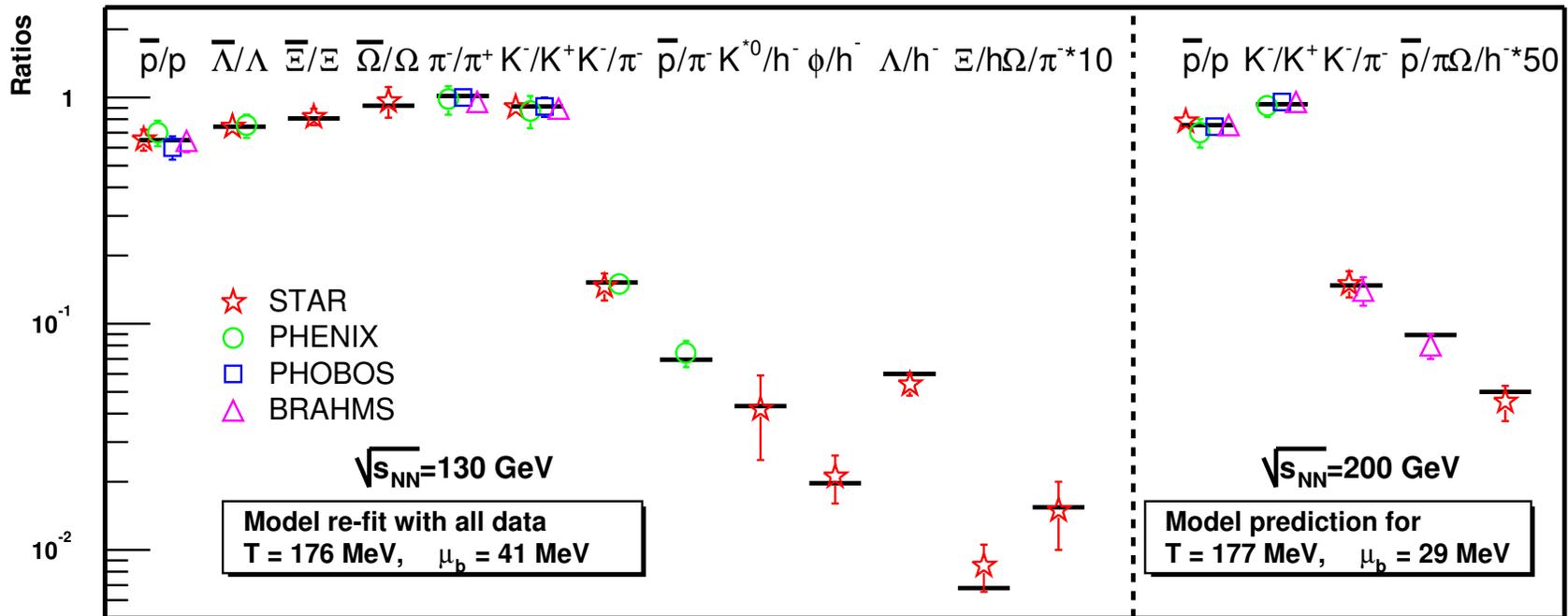
– rapid increase of d.o.f.

however: "no rigorous confinement"





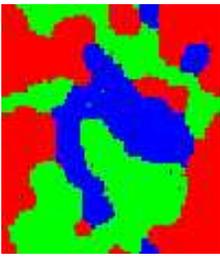
# Particle ratios and freeze out conditions



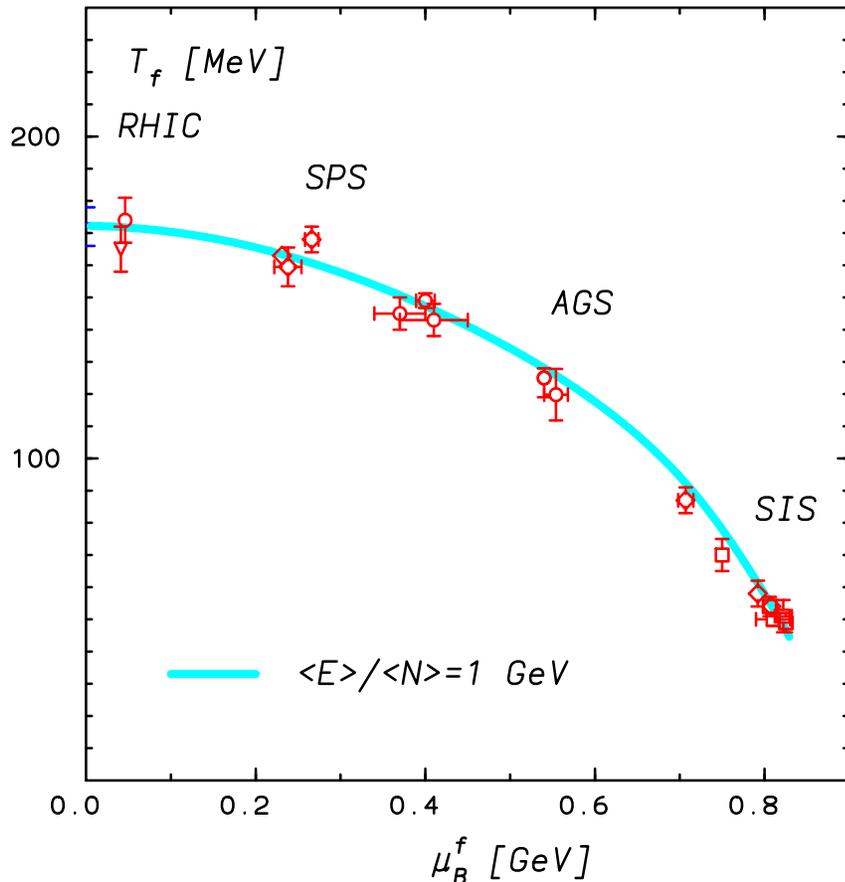
resonance gas:  $Z(T, V, \mu_i) = \text{Tr} e^{-\beta(H - \sum_i \mu_i Q_i)}$

describes observed particle ratios and freeze out conditions

P. Braun-Munzinger, D. Magestro, K. Redlich, J. Stachel, Phys. Lett. B518 (2001) 41



# Particle ratios and freeze out conditions

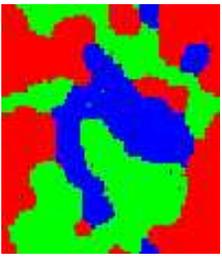


## resonance gas

describes observed particle ratios and freeze out conditions

- Is the freeze out temperature the critical temperature of the QCD transition?
- Which role do resonances play for the occurrence of the transition to the QGP?
- ... and what about deconfinement and chiral symmetry restoration?

$$\ln Z(T, V, \mu_B, \dots) = \sum_{m_i} \ln Z_i(T, V, \mu_B, \dots)$$



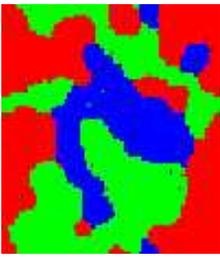
# Critical temperature, equation of state and the resonance gas

---

Hagedorn spectrum :  $\rho(m_H) \sim c m_H^a e^{m_H/T_H}$

$$\ln Z(T, \mu_B) = \int dm_H \rho(m_H) \ln Z_{m_H}(T, \mu_B)$$

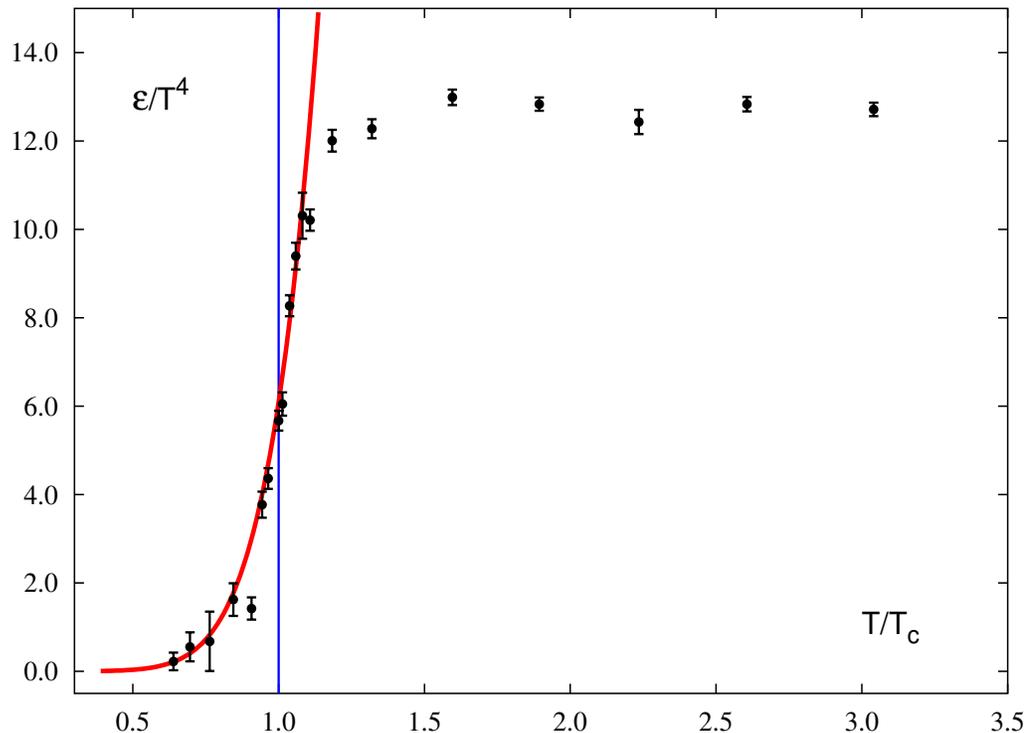
- $\int \Rightarrow \sum \sim$  experimentally known resonances



# Critical temperature, equation of state and the resonance gas

Hagedorn spectrum :  $\rho(m_H) \sim c m_H^a e^{m_H/T_H}$

$$\ln Z(T, \mu_B) = \int dm_H \rho(m_H) \ln Z_{m_H}(T, \mu_B)$$



resonance gas:

~ 1500 d.o.f. from

~ 300 exp. known resonances

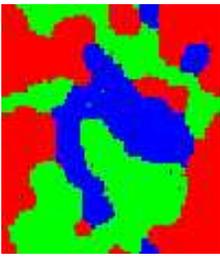
vs.

lattice calculation:

(2+1)-flavor QCD,  $m_q/T = 0.4$

resonances give large contribution at  $T_c$

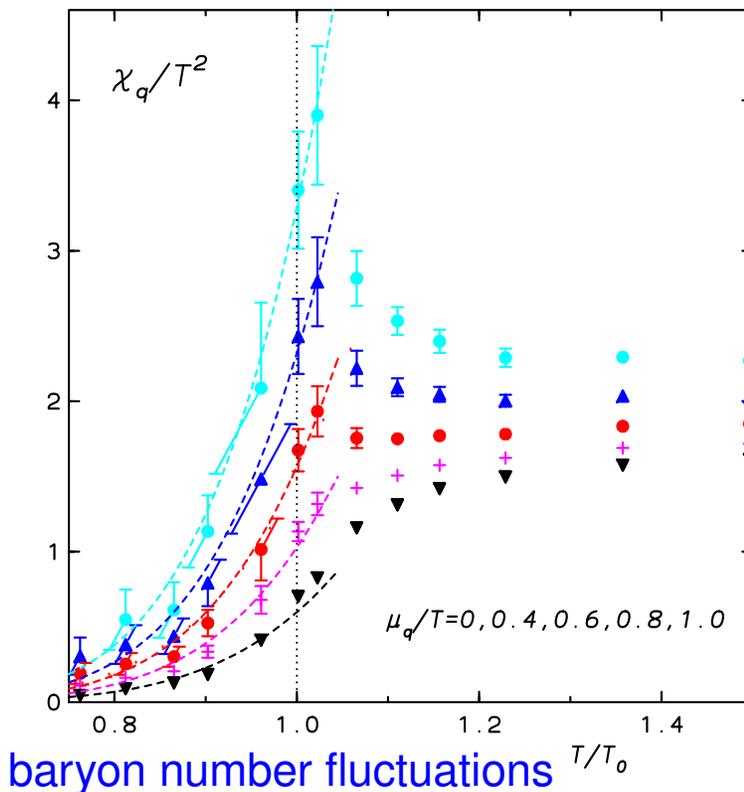
• explain eos for  $T \leq T_c$ ;



# Critical temperature, equation of state and the resonance gas

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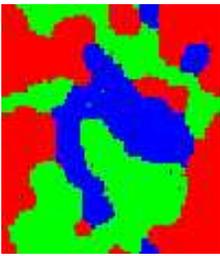
$$\ln Z(T, \mu_B) = \int dm_H \rho(m_H) \ln Z_{m_H}(T, \mu_B)$$



resonance gas:

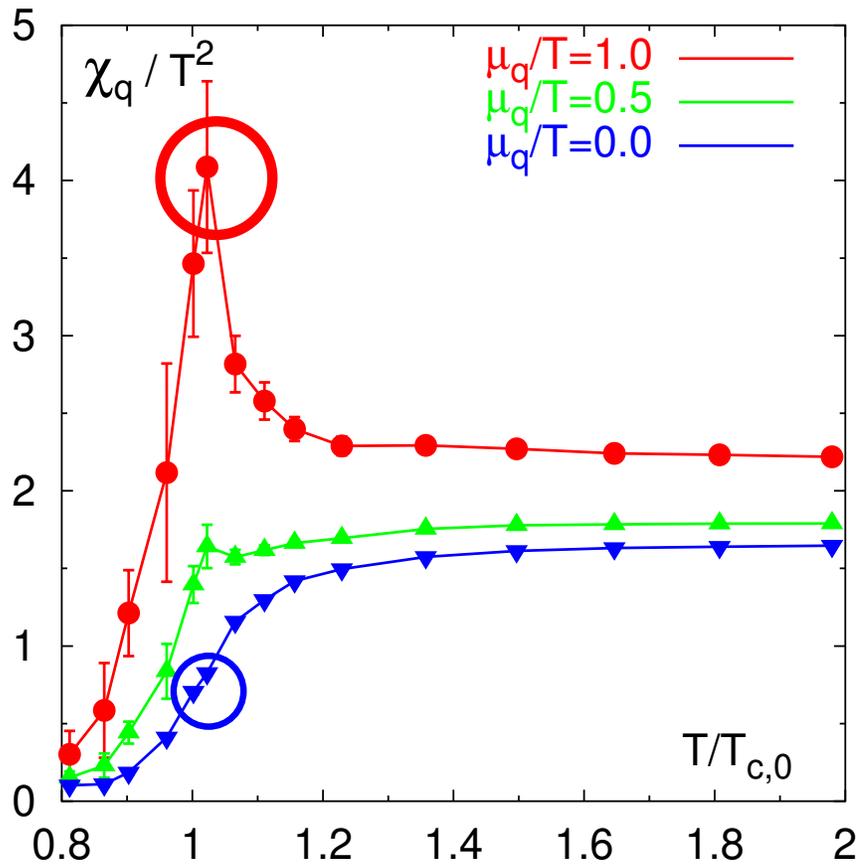
resonances give large contribution at  $T_c$

- explain eos for  $T \leq T_c$ ;
- explain eos for  $\mu_q > 0$  and  $T \leq T_c$ ;



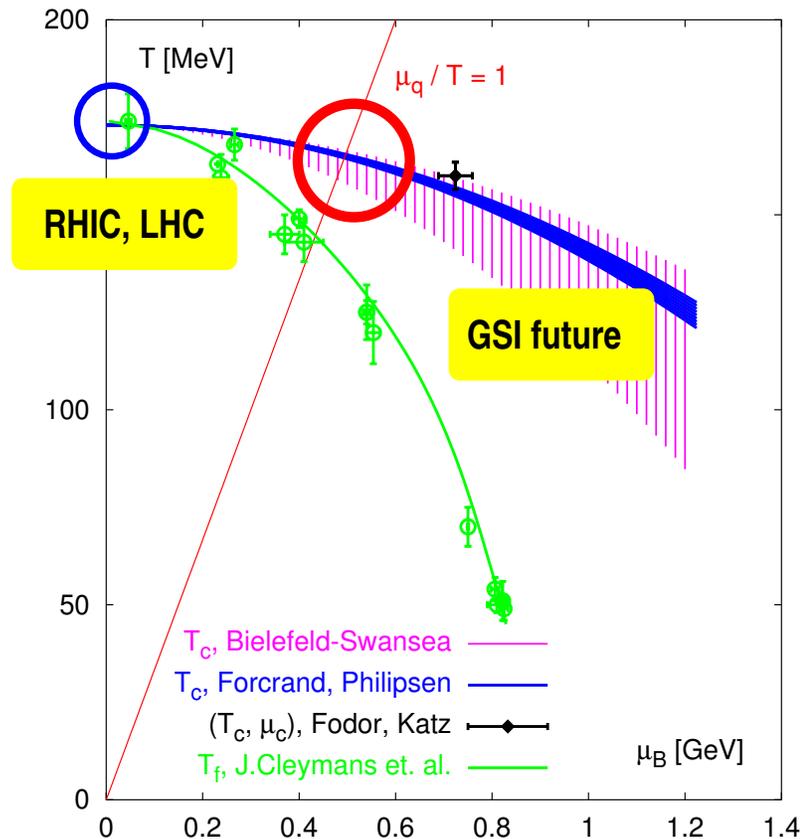
# Fluctuations of the baryon number density ( $\mu > 0$ )

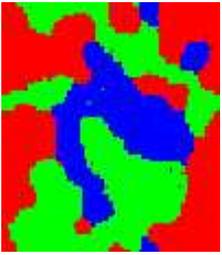
baryon number density fluctuations:  
(Bielefeld-Swansea, PRD68 (2003) 014507)



$$\frac{\chi_q}{T^3} = \left( \frac{d^2}{d(\mu/T)^2} \frac{p}{T^4} \right)_{T \text{ fixed}}$$

$$= \frac{9 T}{V} (\langle N_B^2 \rangle - \langle N_B \rangle^2)$$





# Extending the phase diagram to non-vanishing chemical potential

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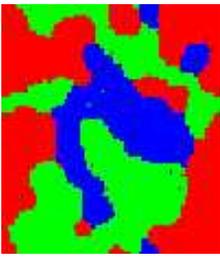
non-zero baryon number density:  $\mu > 0$

$$\begin{aligned} Z(V, T, \mu) &= \int \mathcal{D}A \mathcal{D}\psi \mathcal{D}\bar{\psi} e^{-S_E(V, T, \mu)} \\ &= \int \mathcal{D}A \mathcal{D} \det M(\mu) e^{-S_E(V, T)} \end{aligned}$$

↑↑ complex fermion determinant;

long standing problem

⇒ three (partial) solutions for large  $T$ , small  $\mu$



# Extending the phase diagram to non-vanishing chemical potential

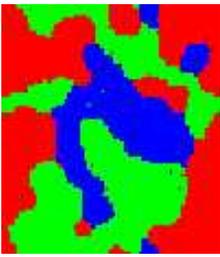
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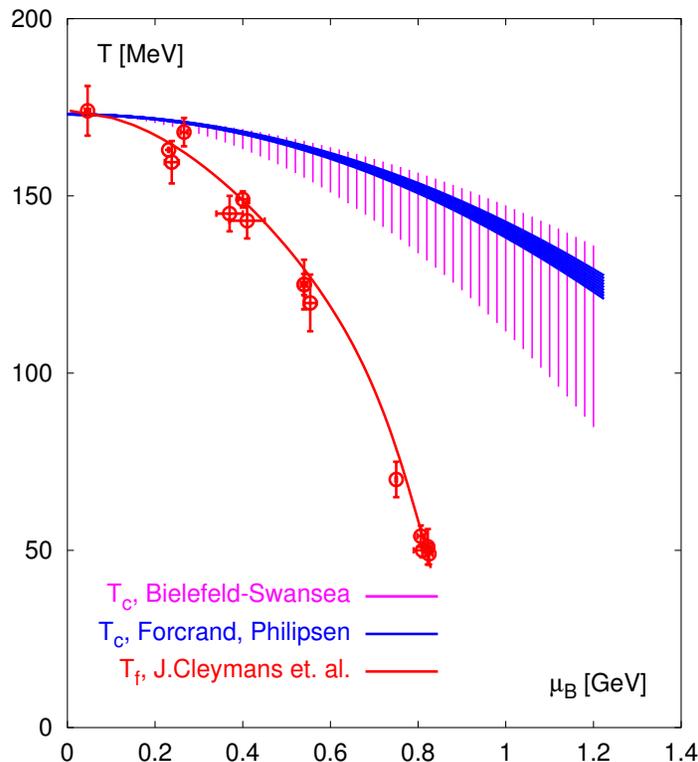
- exact evaluation of  $\det M$ : works well on small lattices; requires reweighting  
Z. Fodor, S.D. Katz, JHEP 0203 (2002) 014
- Taylor expansion around  $\mu = 0$ : works well for small  $\mu$ ; requires reweighting  
C. R. Allton et al. (Bielefeld-Swansea), Phys. Rev. D66 (2002) 074507
- imaginary chemical potential: works well for small  $\mu$ ; requires analytic continuation  
Ph. deForcrand, O. Philipsen, Nucl. Phys. B642 (2002) 290



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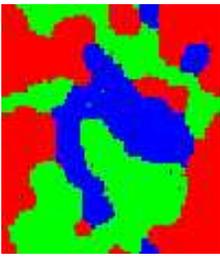


$$\frac{T_c(\mu)}{T_c(0)} : \quad 1 - 0.0056(4)(\mu_B/T)^2$$

deForcrand, Philipsen (imag.  $\mu$ )

$$1 - 0.0078(38)(\mu_B/T)^2$$

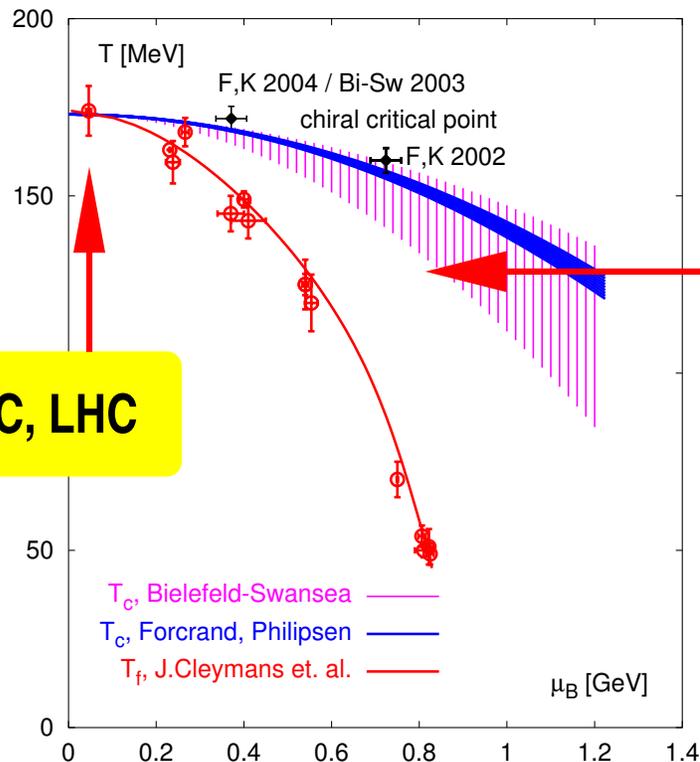
Bielefeld-Swansea  
( $\mathcal{O}(\mu^2)$  reweighting)



# Extending the phase diagram to non-vanishing chemical potential

non-zero baryon number density:  $\mu > 0$

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**GSI future**

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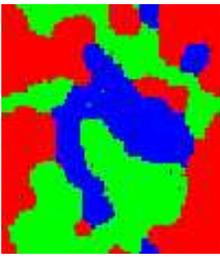
$$1 - 0.0078(38)(\mu_B/T)^2$$

Bielefeld-Swansea  
( $\mathcal{O}(\mu^2)$  reweighting)

chiral critical point

$\mu_c$  shifted from  $\simeq 700$  MeV to  $\simeq 400$  MeV

Fodor, Katz (exact determinants  $\Rightarrow$  small lattices)

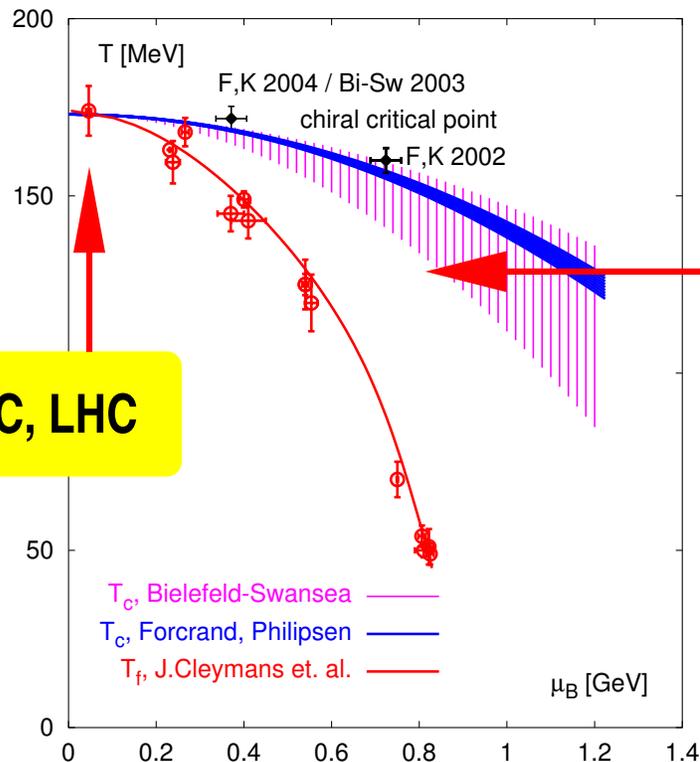


# Extending the phase diagram to non-vanishing chemical potential

non-zero baryon number density:  $\mu > 0$

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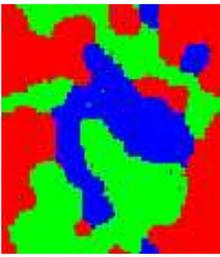
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( $\mathcal{O}(\mu^2)$  reweighting)

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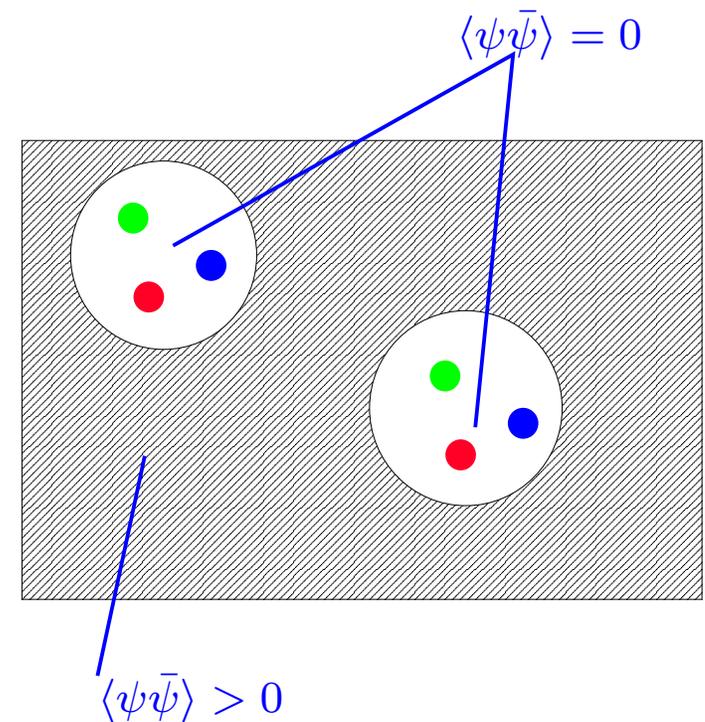
$\mu_c(m_q)$ : discrepancies between calculations with real and imaginary  $\mu$

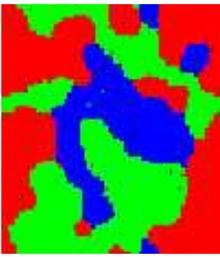


# In-medium properties of hadrons

- properties of light quark hadrons reflect chiral symmetry breaking: Goldstone pion, non-degenerate parity partners

chiral symmetry restoration

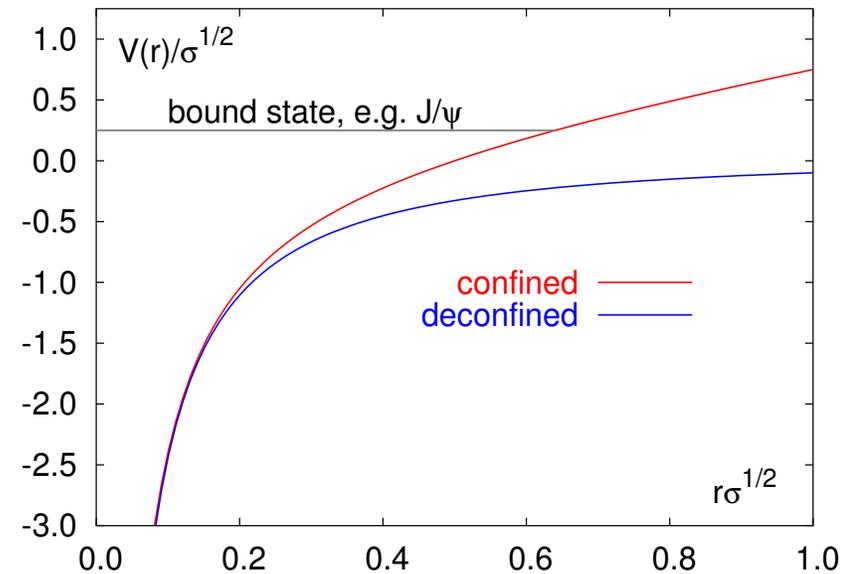


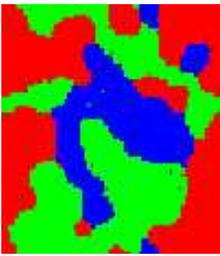


# In-medium properties of hadrons

- properties of light quark hadrons reflect chiral symmetry breaking: **Goldstone pion**, **non-degenerate parity partners**
- properties of heavy quark hadrons reflect structure of the heavy quark potential: **quarkonium spectra**

## Deconfinement



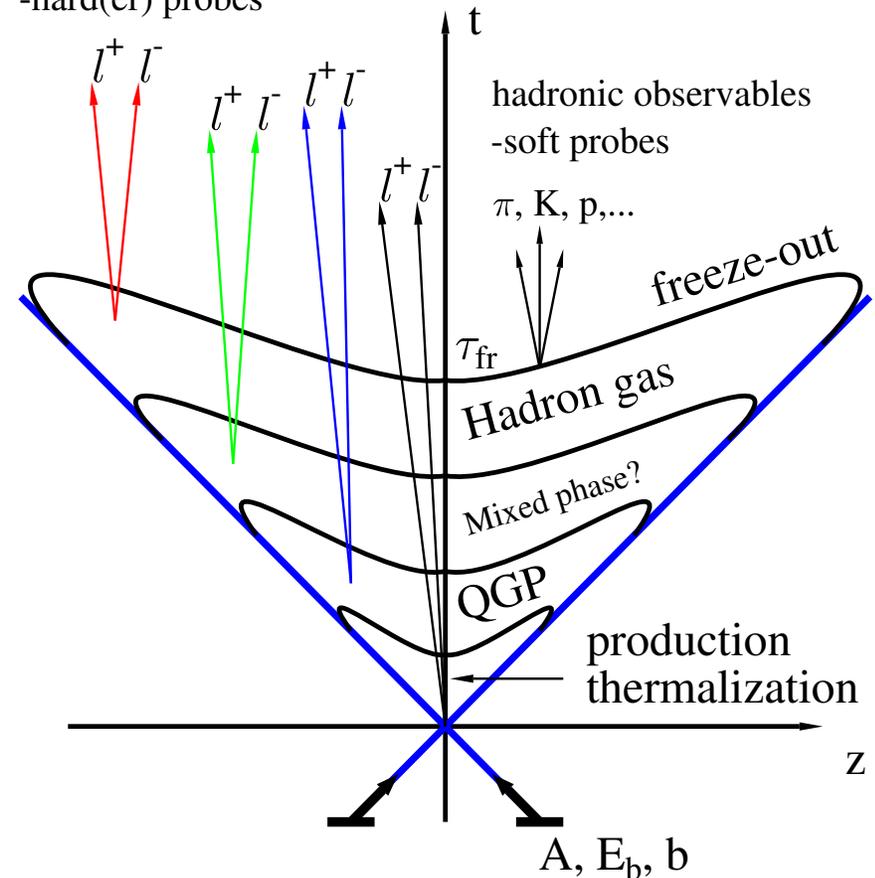


# In-medium properties of hadrons

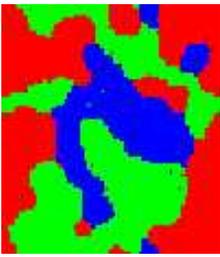
- properties of light quark hadrons reflect chiral symmetry breaking: **Goldstone pion, non-degenerate parity partners**
- properties of heavy quark hadrons reflect structure of the heavy quark potential: **quarkonium spectra**

thermal modifications of chiral condensate and heavy quark potential will influence the hadron spectrum

electromagnetic observables  
-hard(er) probes



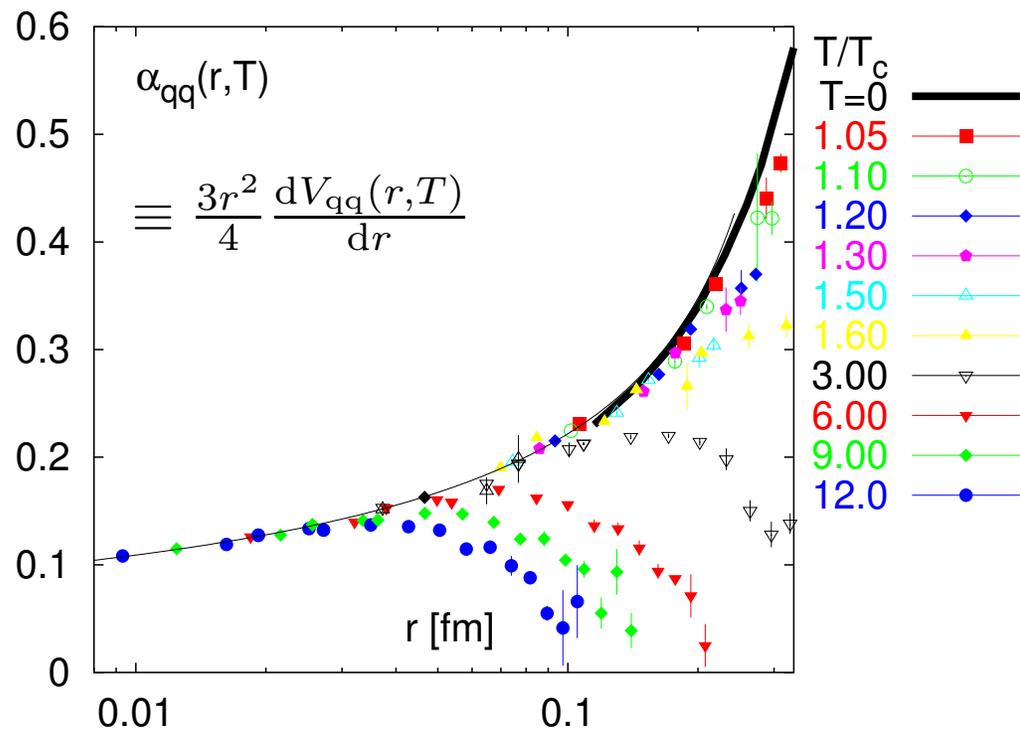
observable consequences in dilepton spectra



# Running coupling at finite $r$ and $T$ ... remnants of confinement in the QGP

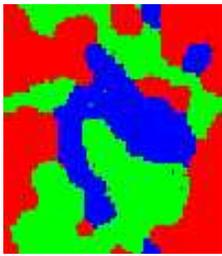
up to  $T \simeq 3T_c$ :  $\alpha_{\text{qq}}(r, T) \simeq \alpha_{\text{qq}}(r, 0)$  for  $r < 0.1$  fm

Do heavy quark bound states survive in the QGP?



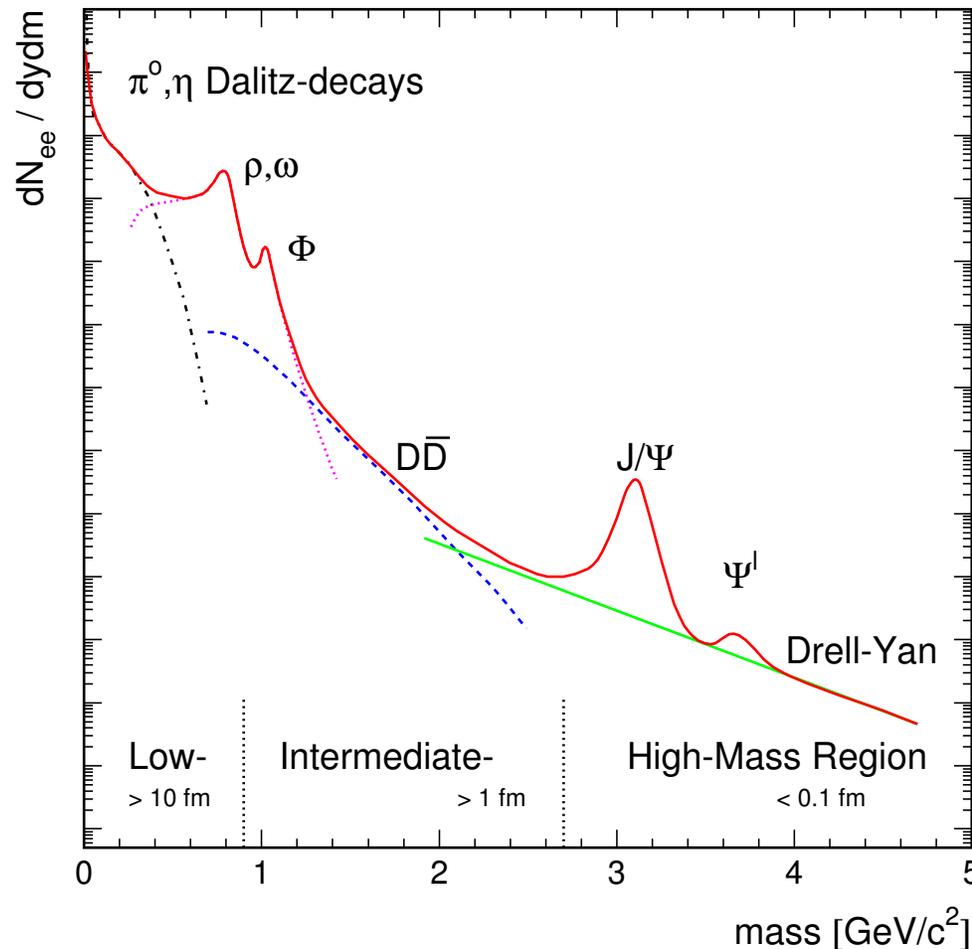
$T = 0$ : S. Necco, R. Sommer, NP B622 (2002) 328.

$T > 0$ : O. Kaczmarek, FK, P. Petreczky and F. Zantow, hep-lat/0406036

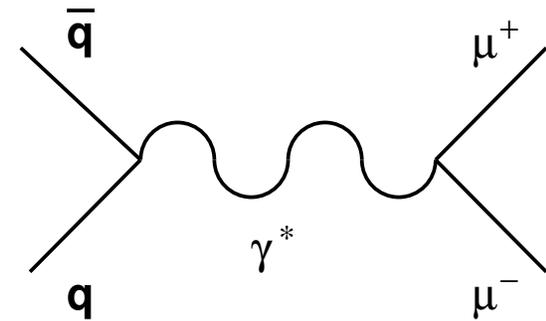


# Thermal vector meson properties from dilepton rates in heavy ion collisions

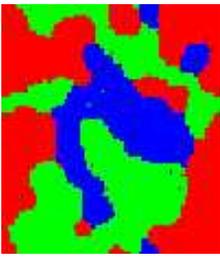
dilepton rate vs. invariant mass of  $l^+l^-$  pair



differential cross-section for  $\mu^+\mu^-$  pair production

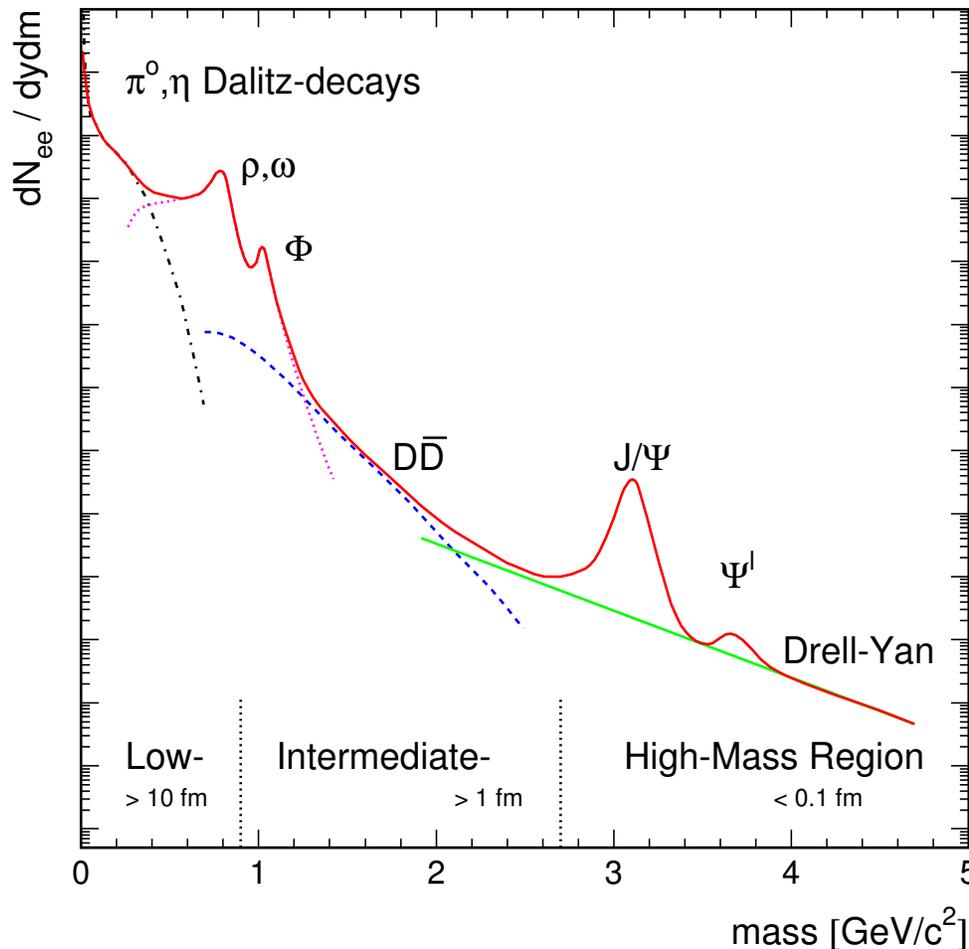


dilepton pair ( $e^+e^-$ ,  $\mu^+\mu^-$ ) production through annihilation of "thermal"  $\bar{q}q$ -pairs in hot and dense matter

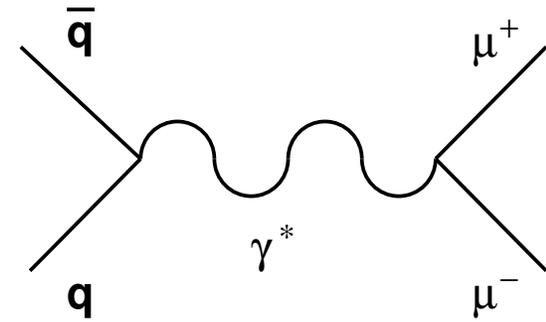


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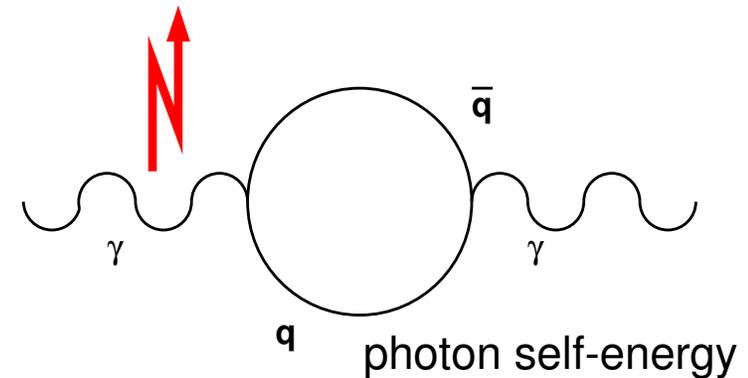


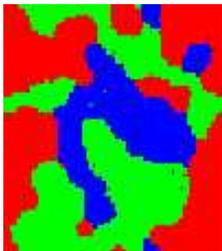
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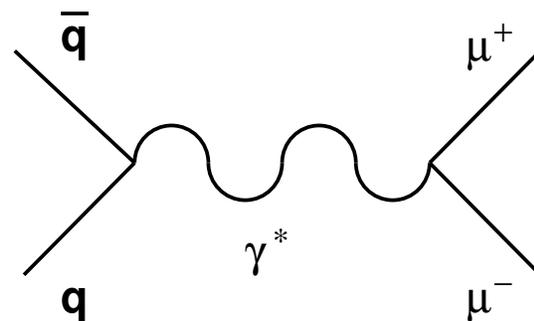
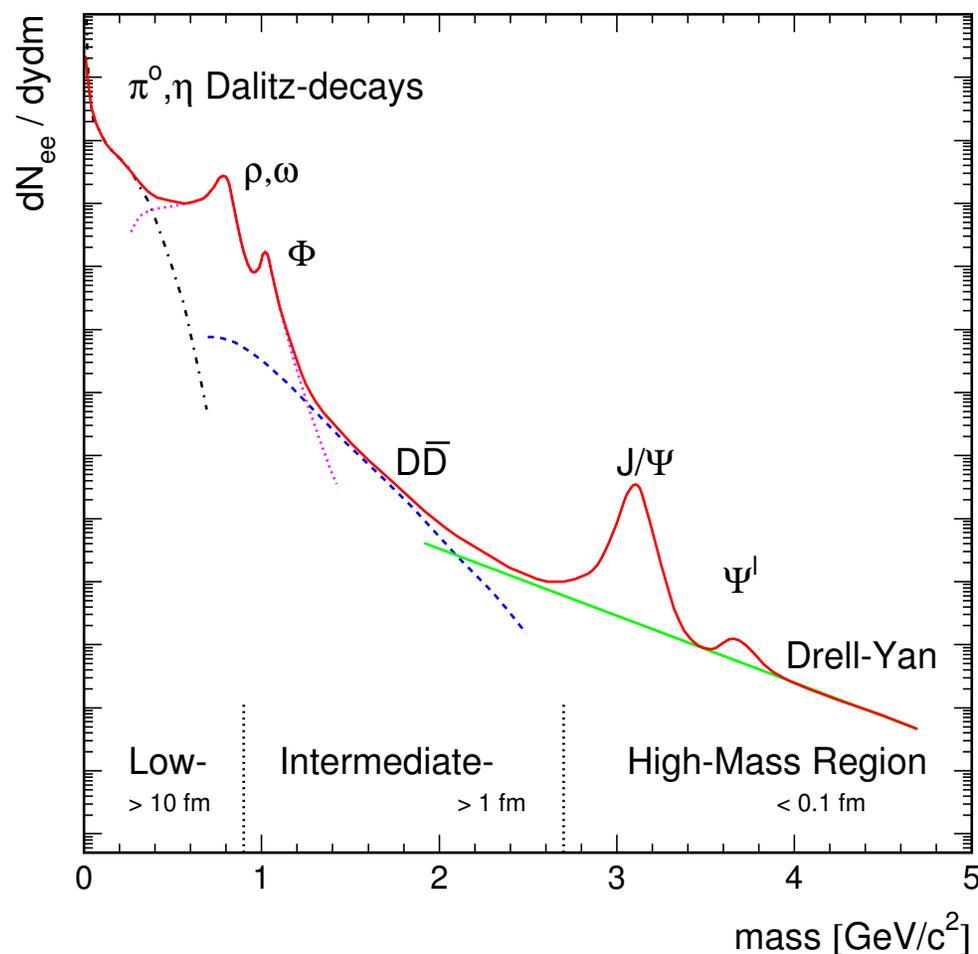
$$\text{rate} \sim |q\bar{q} \rightarrow \gamma^*|^2 \cdot |l^+l^- \rightarrow \gamma^*|^2$$





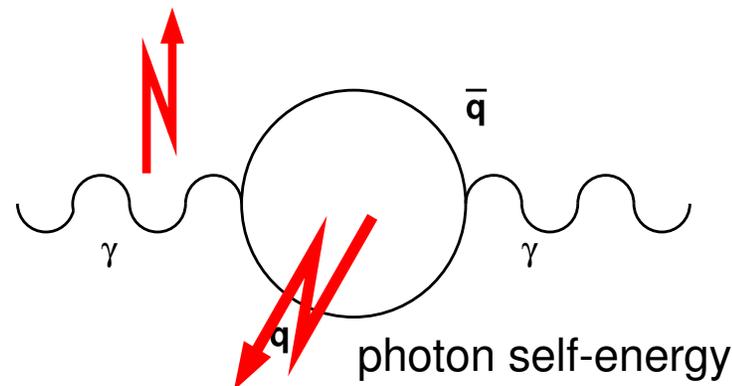
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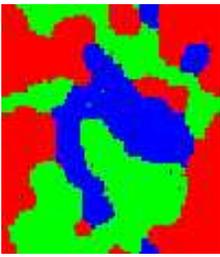


dilepton pair ( $e^+e^-$ ,  $\mu^+\mu^-$ ) production through annihilation of "thermal"  $\bar{q}q$ -pairs in hot and dense matter

$$\text{rate} \sim |q\bar{q} \rightarrow \gamma^*|^2 \cdot |l^+l^- \rightarrow \gamma^*|^2$$



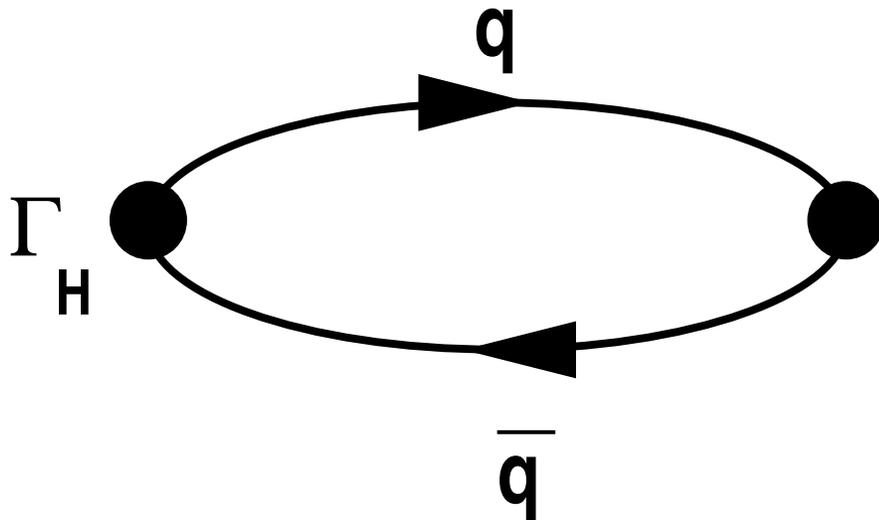
differential cross-section for  $\mu^+\mu^-$  pair production  $\Rightarrow$  thermal meson correlation function



# Thermal meson correlation functions and spectral functions

Thermal correlation functions: 2-point functions which describe propagation of a  $\bar{q}q$ -pair

spectral representation of correlator  $\Rightarrow$  dilepton and photon rates



spectral representation of  
Euclidean correlation functions

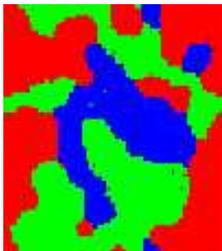
$$G_H^\beta(\tau, \vec{r}) = \int_0^\infty d\omega \int \frac{d^3\vec{p}}{(2\pi)^3} \sigma_H(\omega, \vec{p}, T) e^{i\vec{p}\vec{r}} \frac{\cosh(\omega(\tau - 1/2T))}{\sinh(\omega/2T)}$$

spectral representation of  
thermal photon rate:  $\omega = |\vec{p}|$

$$\omega \frac{d^3 R^\gamma}{d^3 p} = \frac{5\alpha}{6\pi^2} \frac{\sigma_V(\omega, \vec{p}, T)}{\omega^2 (e^{\omega/T} - 1)}$$

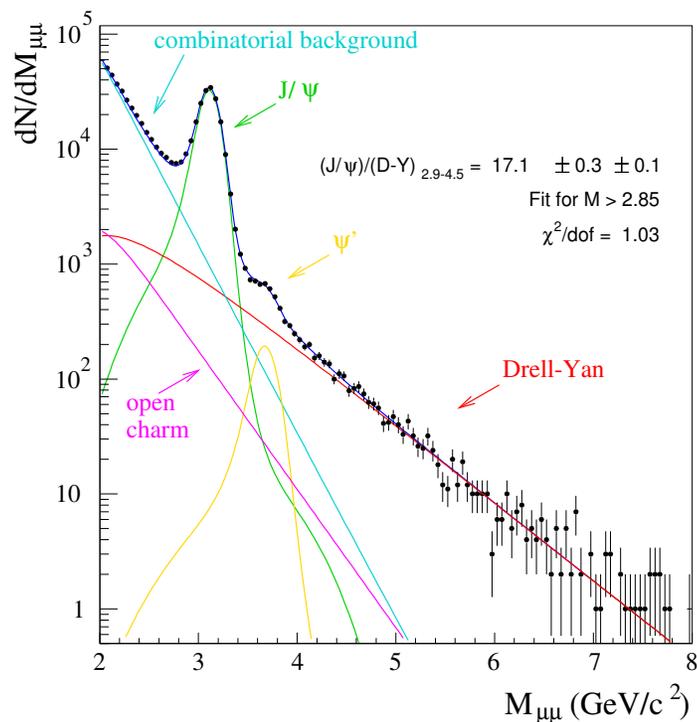
spectral representation of  
thermal dilepton rate

$$\frac{d^4 W}{d\omega d^3 p} = \frac{5\alpha^2}{27\pi^2} \frac{\sigma_V(\omega, \vec{p}, T)}{\omega^2 (e^{\omega/T} - 1)}$$



# Charmonium suppression in heavy ion collisions (SPS, CERN)

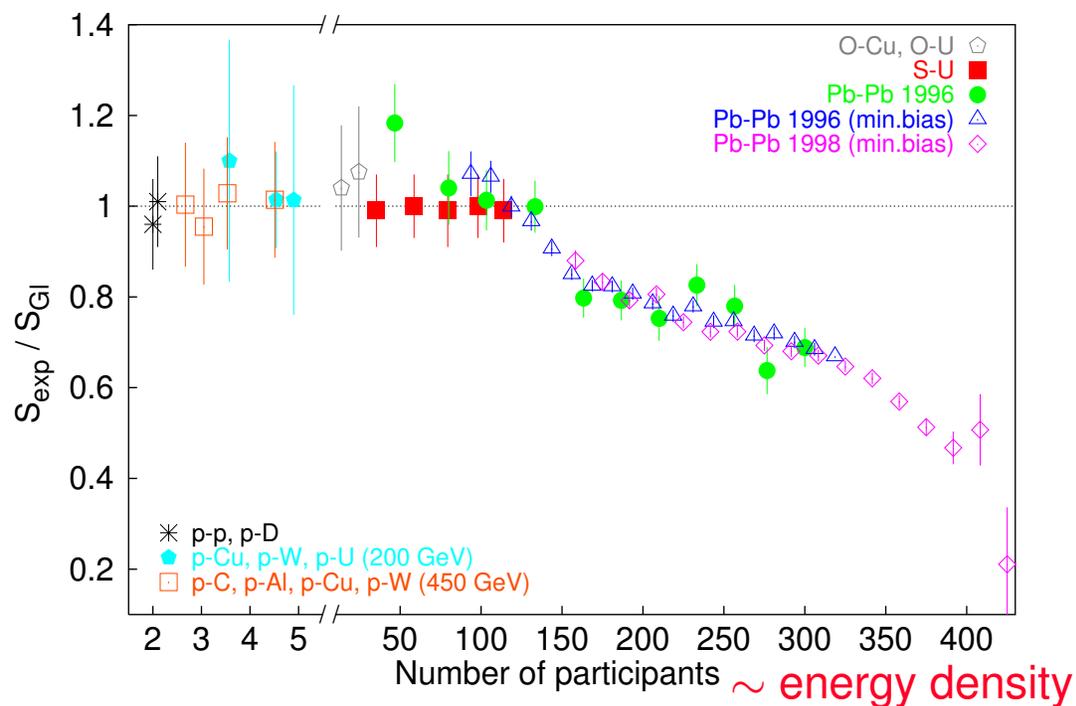
## Charmonium Production: dilepton rate



invariant mass of the pair

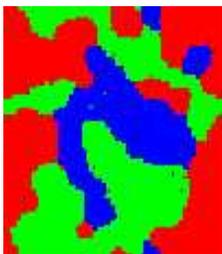
differential cross-section for  $\mu^+ \mu^-$  pair production

## Suppression Pattern



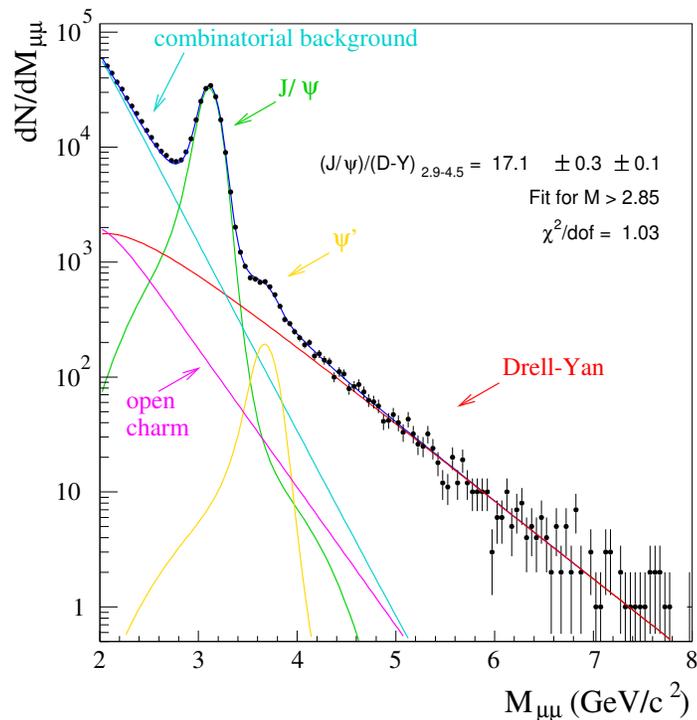
measured A-A rate normalized to rate expected from known p-A collisions

M.C.Abreu (NA50), Phys.Lett. B477 (2000) 28



# Charmonium suppression in heavy ion collisions (SPS, CERN)

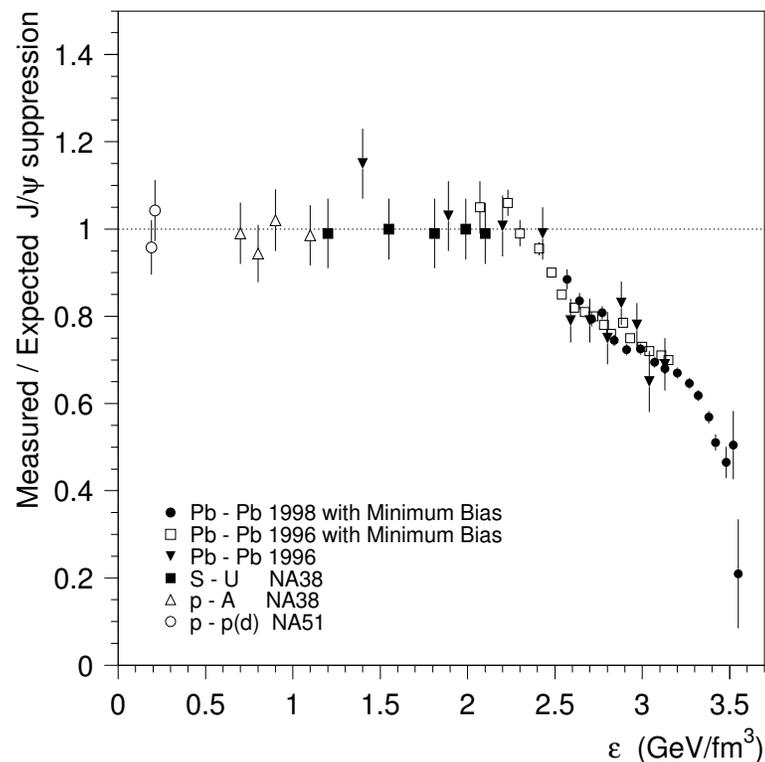
## Charmonium Production: dilepton rate



invariant mass of the pair

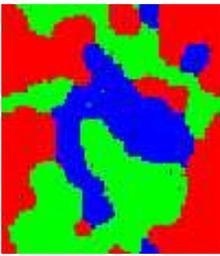
differential cross-section for  $\mu^+ \mu^-$  pair production

## Suppression Pattern



use Bjorken formula to convert participants to energy density

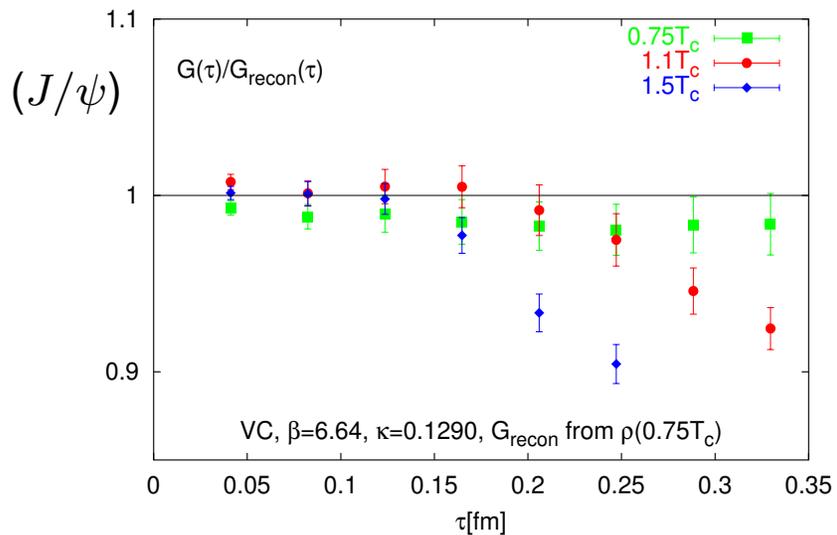
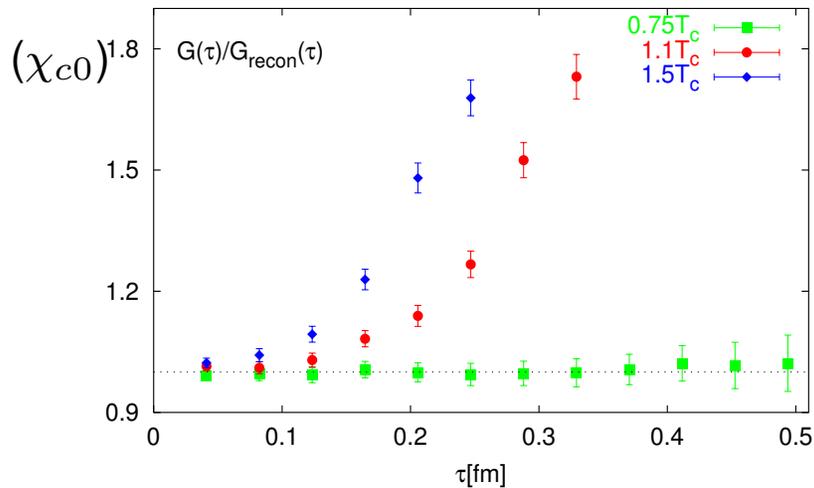
$$\epsilon \equiv \frac{1}{\tau_0 V_T} \left( \frac{dE_T}{dy} \right)_{y=0}$$



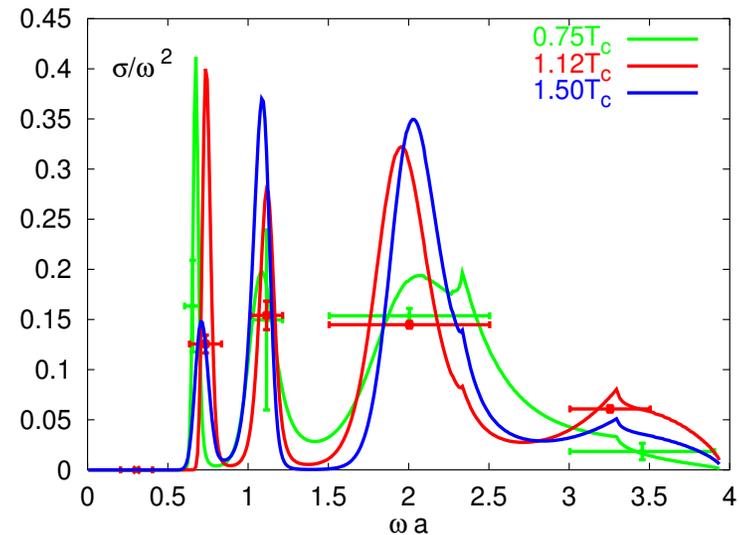
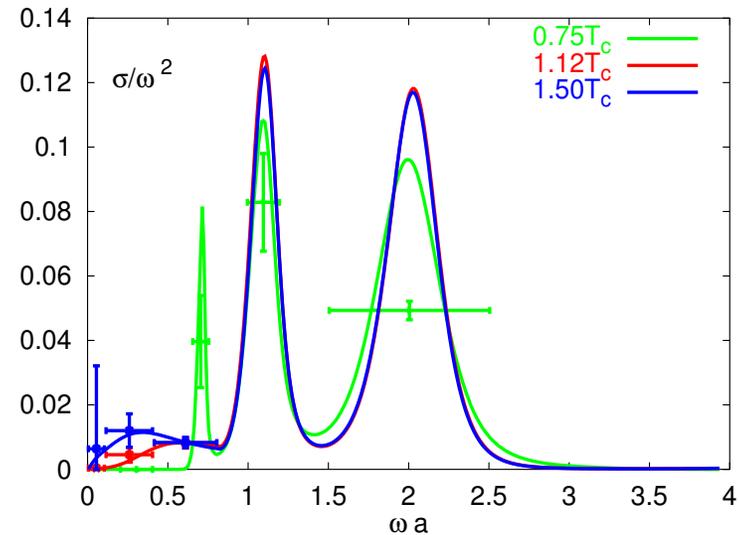
# Heavy quark spectral functions and correlation functions

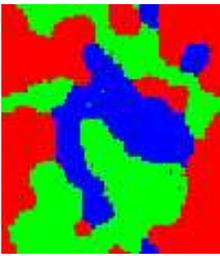
reconstructed correlation functions  
above  $T_c$  from data below  $T_c$

SC,  $\beta=6.64$ ,  $\kappa=0.1290$ ,  $G_{\text{recon}}$  from  $\rho(0.75T_c)$



reconstructed spectral functions  
using the Maximum Entropy Method

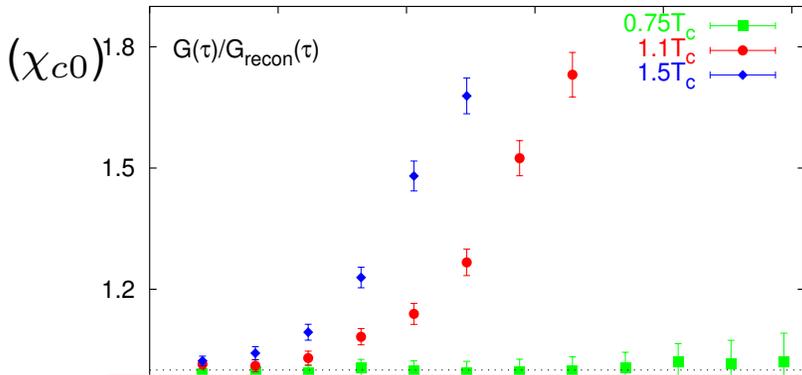




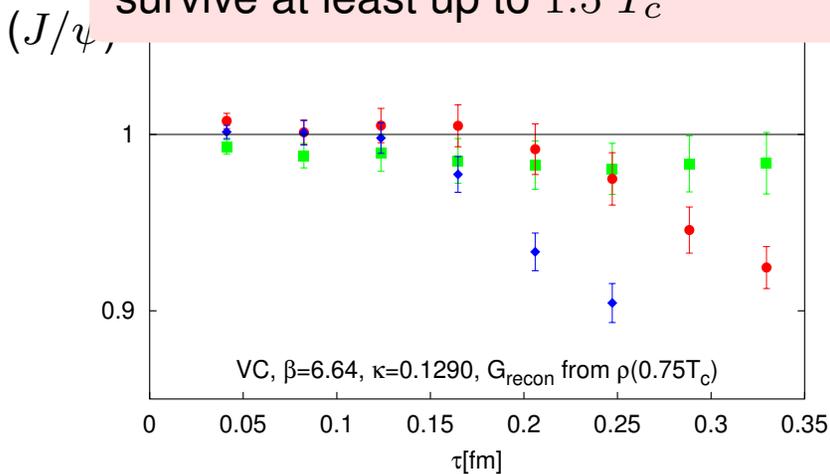
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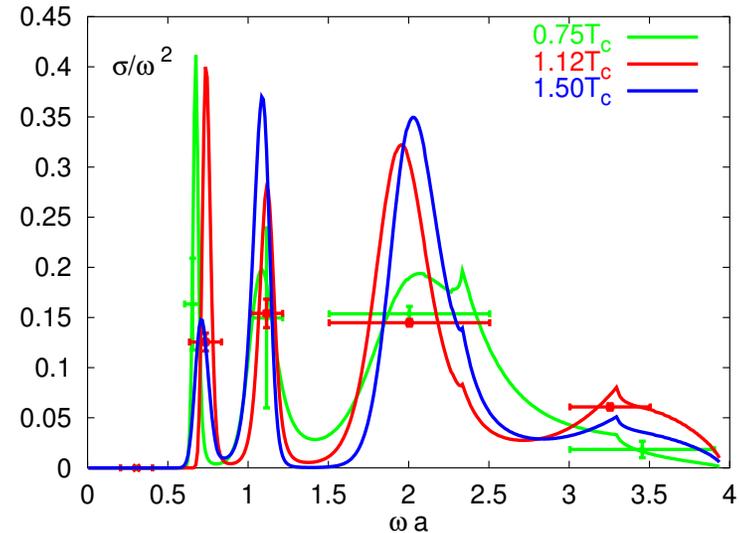
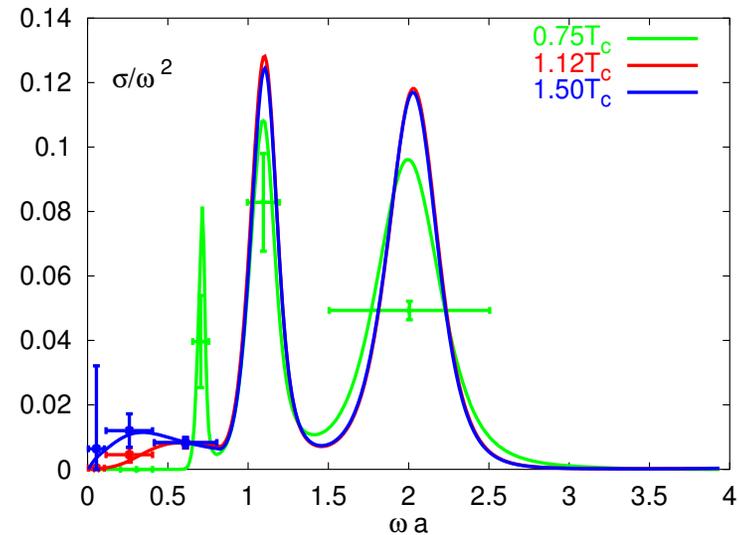
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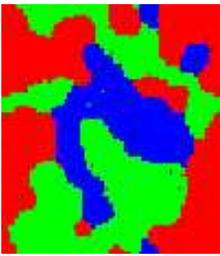


radial excitations ( $\chi_c$ ) disappear at  $T_c$ ;  
charmonium S-states ( $J/\psi$  and  $\eta_c$ )  
survive at least up to  $1.5 T_c$



reconstructed spectral functions  
using the Maximum Entropy Method

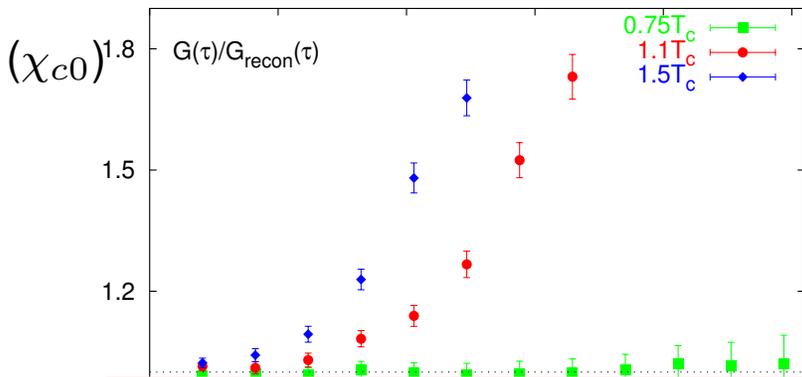




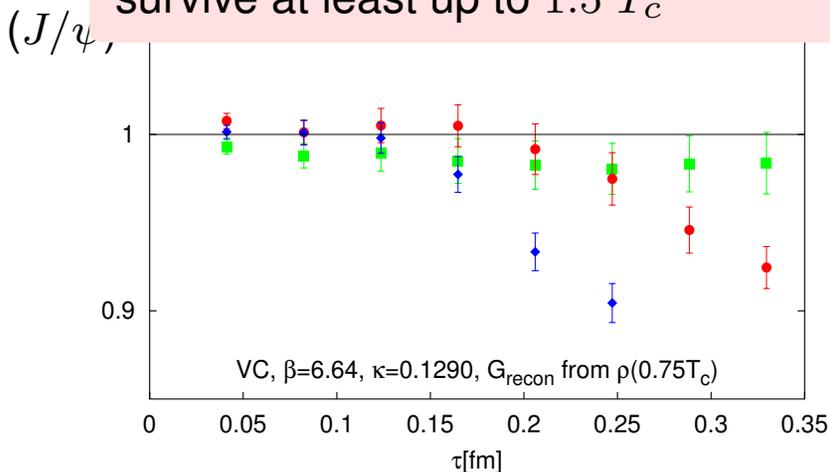
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above  $T_c$  from data below  $T_c$

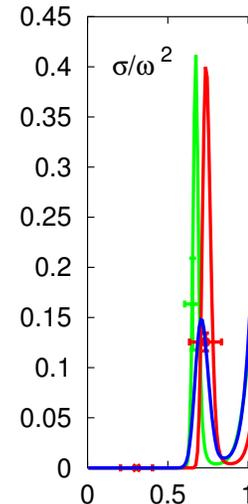
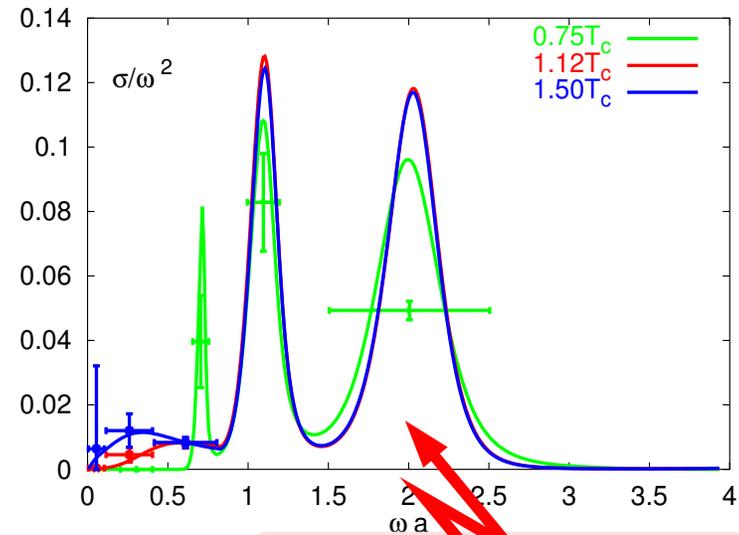
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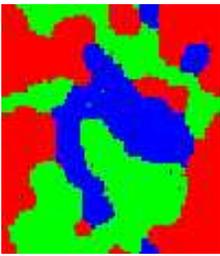
need to get better control over  
ultra-violet cut-off effects  
(Wilson-doublers)

use better fermion actions

- overlap fermions

- domain wall fermions

- (truncated) perfect actions...



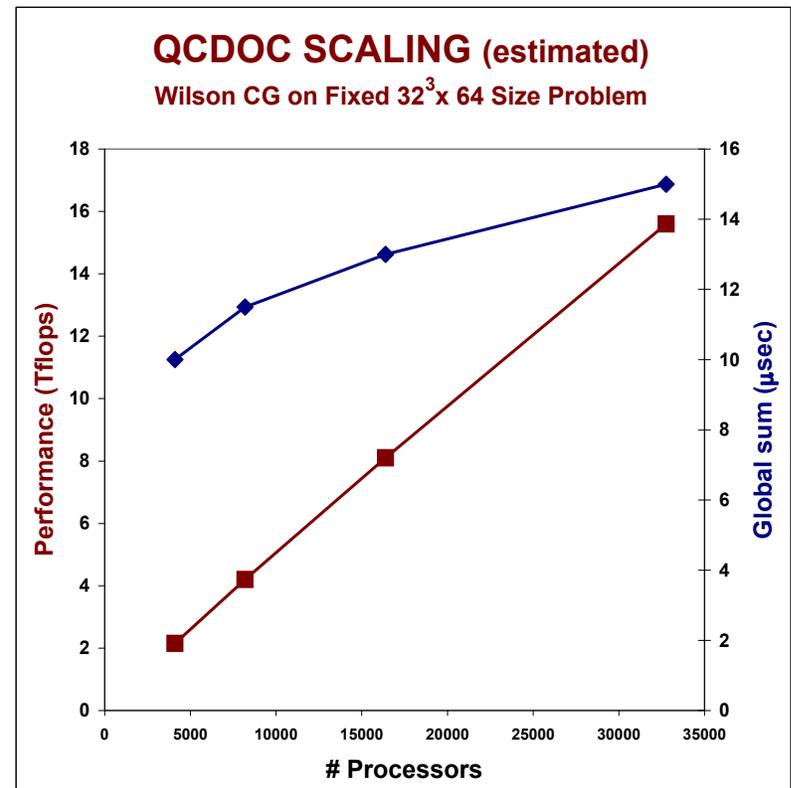
# Outlook: Next generation lattice calculations

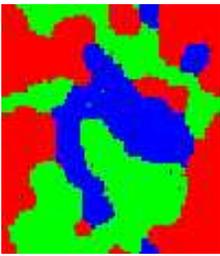
- Thermodynamics of pure gauge theory has been "solved" on (1-10)GFlops computers (1996)
- Thermodynamics of QCD with "still too heavy" quarks has been studied on (10-100) GFlops computers
- Analysis of "continuum and thermodynamic limit" of QCD thermodynamics with light quarks, requires computers with  $\sim 10$  TFlops peak speed. (LatFor, 2003)

## QCDOC and apeNEXT:

scaling to 10's of Teraflops

with \$1/MFlops Cost/performance





# Progress in lattice calculations... depends on...

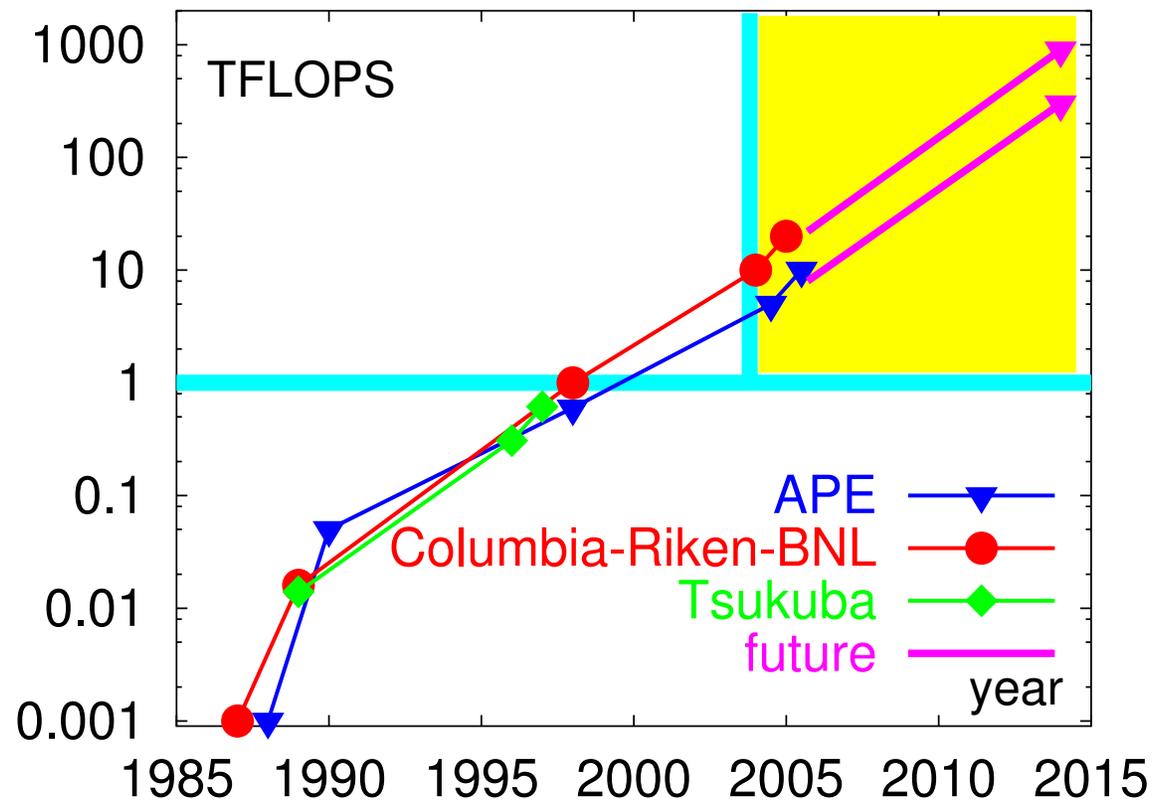
● development of (special purpose) computer hardware

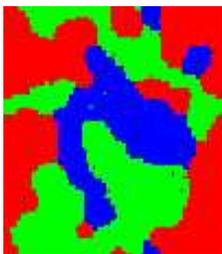


development of  
special purpose  
computer hardware



towards PETAFLUPS  
computing

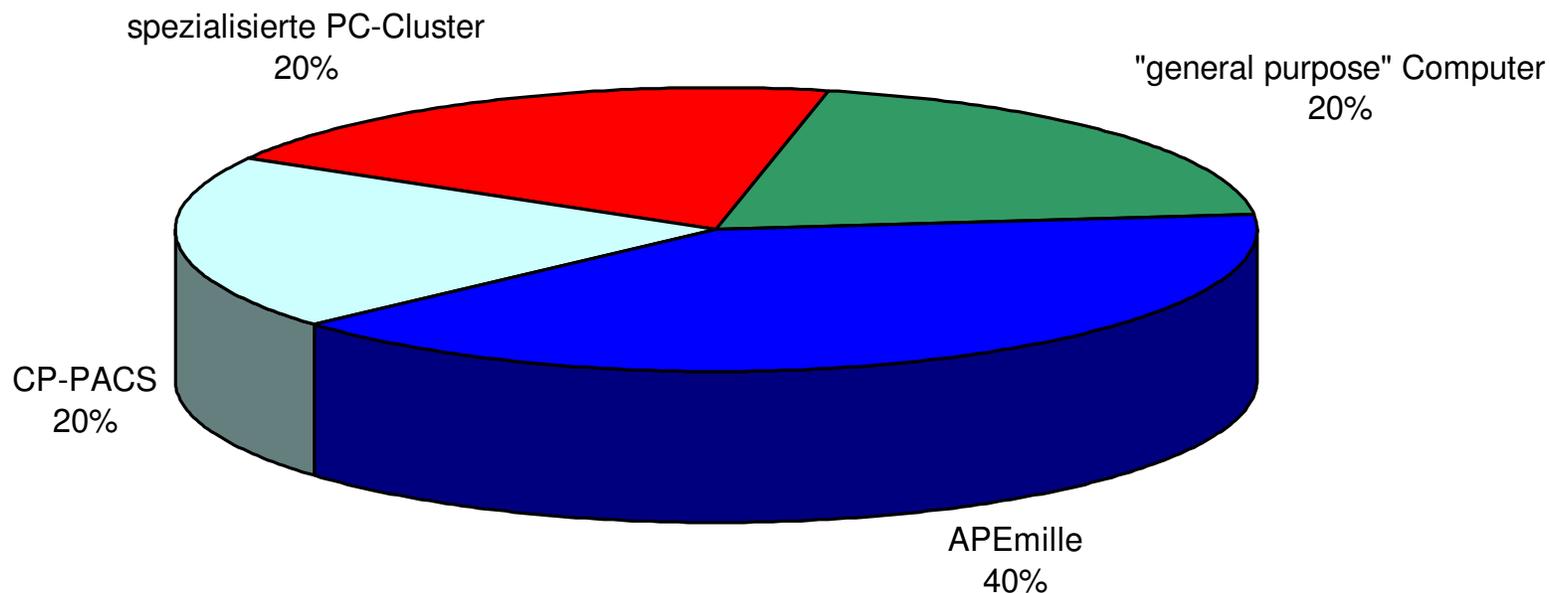


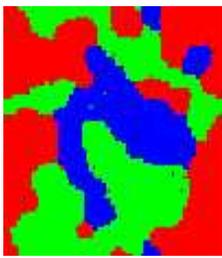


# Progress in lattice calculations... depends on...

## special purpose computer hardware

contribution of research done on special purpose computer  
to 10 top cited papers in LGT (1999-2004)





# Outlook: Next generation computers for lattice gauge theory

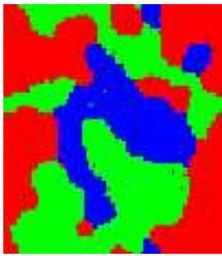
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today:

**APEmille**

so far the only dedicated  
large-scale computer installation used  
predominantly for QCD thermodynamics  
exists in Bielefeld: 120 GFlops



# Outlook: Next generation computers for lattice gauge theory

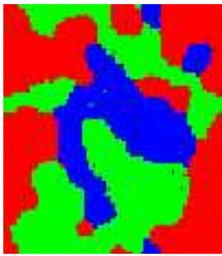
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## QCDOC and apeNEXT

2004:

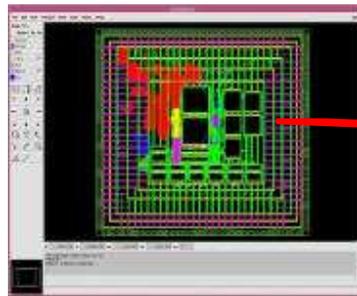
QCD thermodynamics on the next generation of special purpose  
dedicated QCD computers

installations with (10-20) TFlops peak speed are planned  
in the USA and Europe

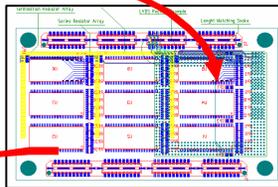


# apeNEXT: Next generation of APE computers

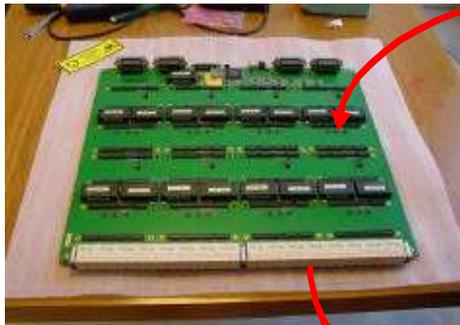
## Assembling apeNEXT...



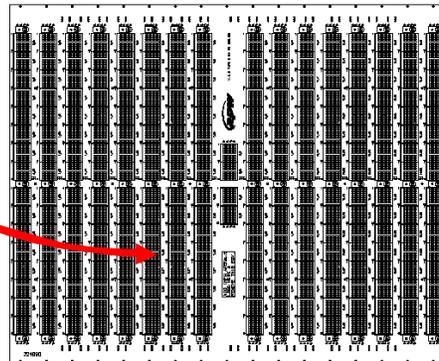
J&T Asic



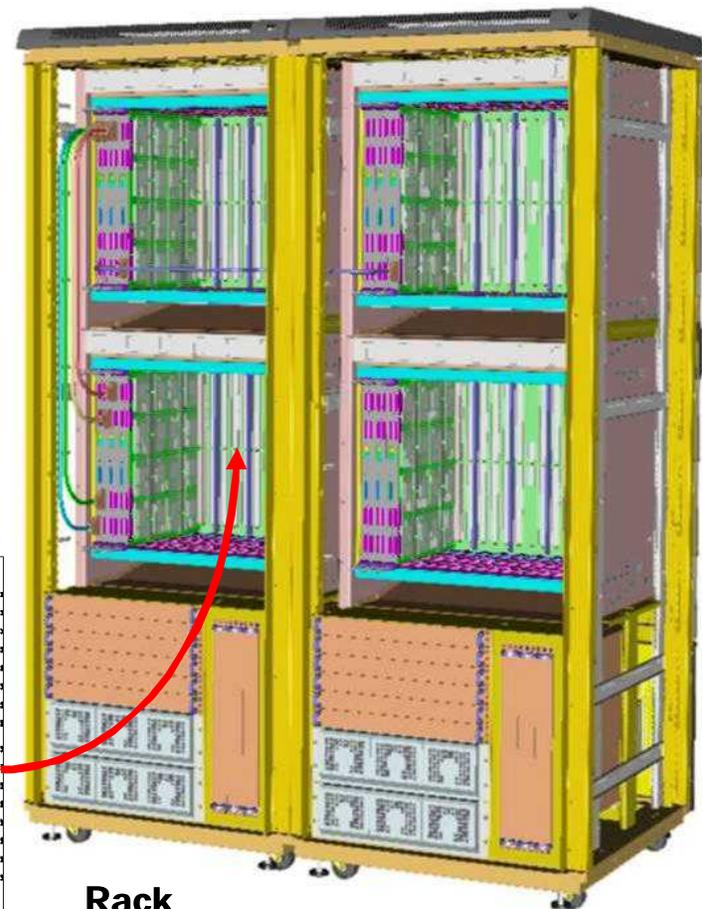
J&T module



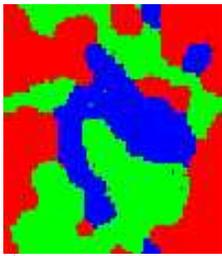
PB



BackPlane

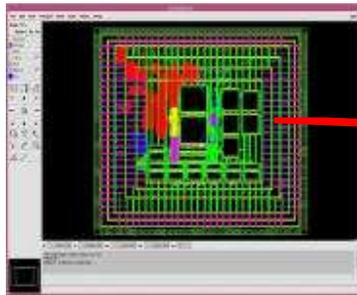


Rack

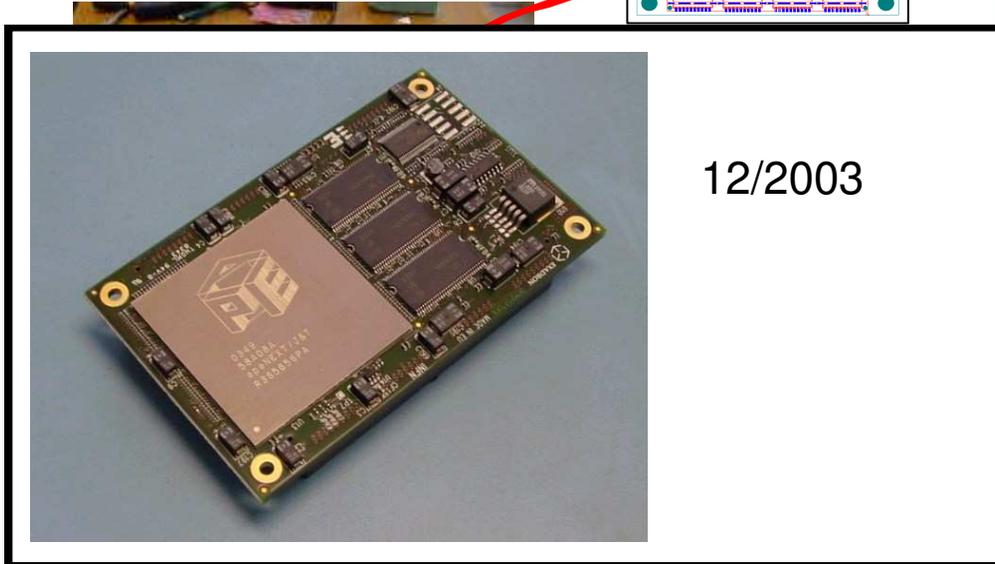


# apeNEXT: Next generation of APE computers

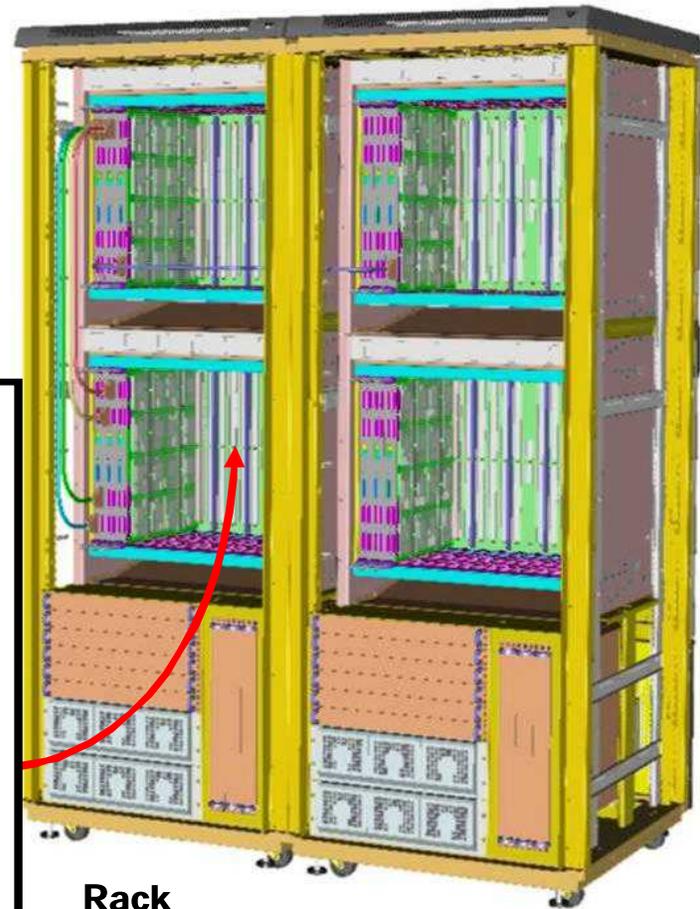
## Assembling apeNEXT...



J&T Asic

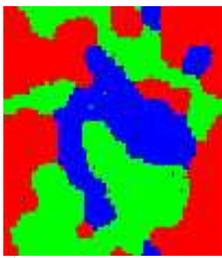


12/2003



Rack

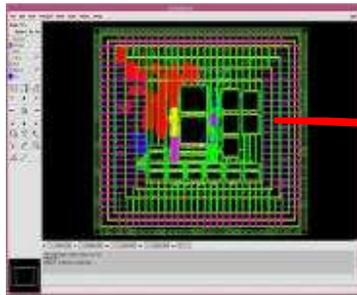
BackPlane



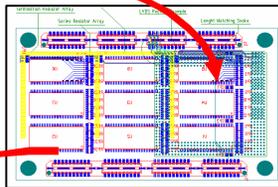
# apeNEXT: Next generation of APE computers



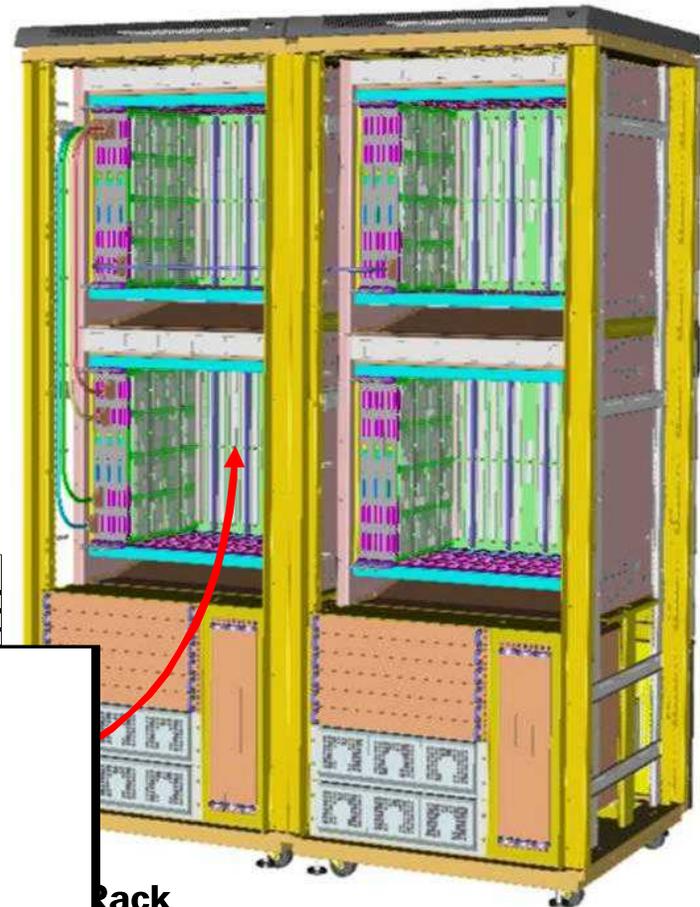
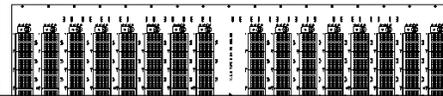
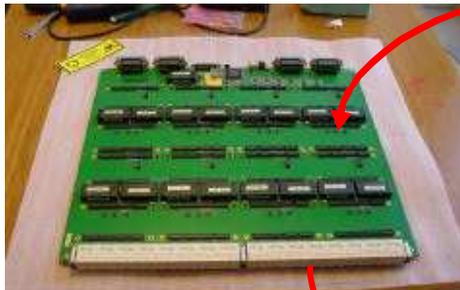
## Assembling apeNEXT...



J&T Asic



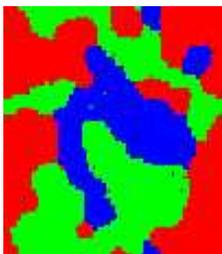
J&T module



Rack

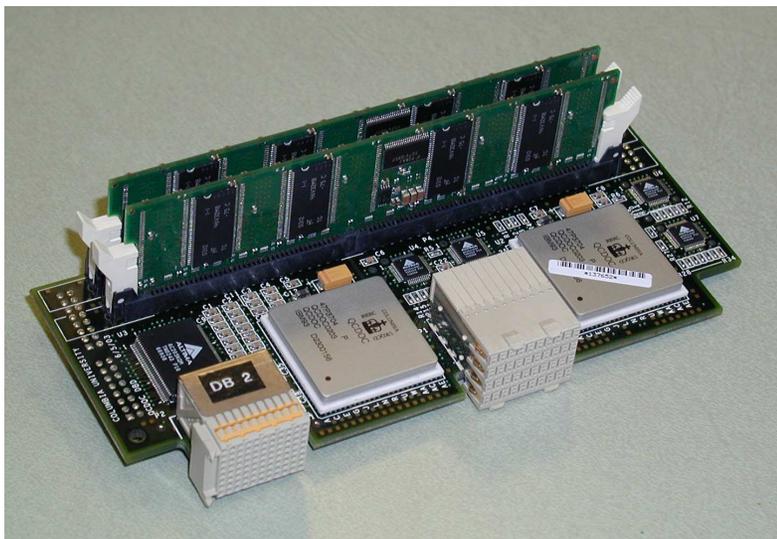
- first chips Dec. 2003
- two 0.8 TFlops prototypes ~ summer 2004
- first 3 TFlops installations in 2005

BackPlane



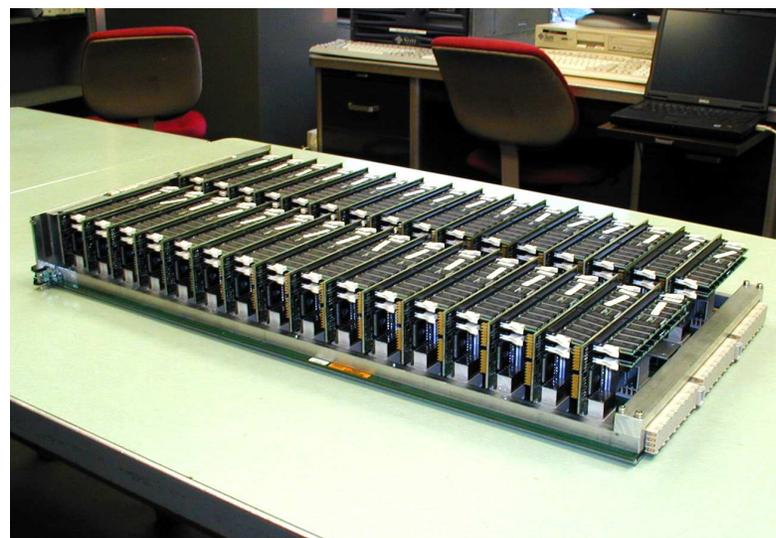
# QCDOC: Next generation of Columbia-RIKEN computer

Columbia – RIKEN – UKQCD Collaboration

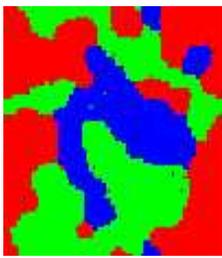


2 – node daughter card

- prototypes exist since 07/2003



64 – node mother board



# QCDOC: Next generation of Columbia-RIKEN computer

Columbia – RIKEN – UKQCD Collaboration

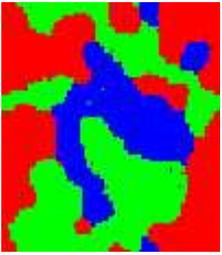


512 – node machine : (360 – 450) GFlops

- currently being debugged prototype (05/2004):  
0.25 Tbyte memory; 6 Gbit/sec Ethernet I/O bandwidth

*QCDOC computing center at BNL :*

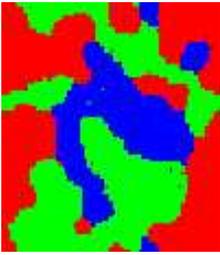
- 10 TFlops machine for RBRC: ~ autumn 2004
- 10 TFlops machine for american LGT community: ~ early 2005
- ... larger installations possible and needed!



# Conclusions

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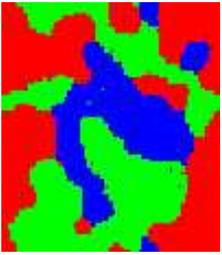
- **LGT** calculations contributed a lot to the understanding/interpretation of **HIC**



# Conclusions

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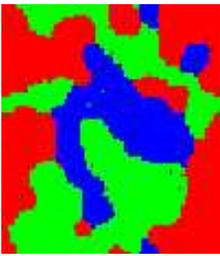
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# Conclusions

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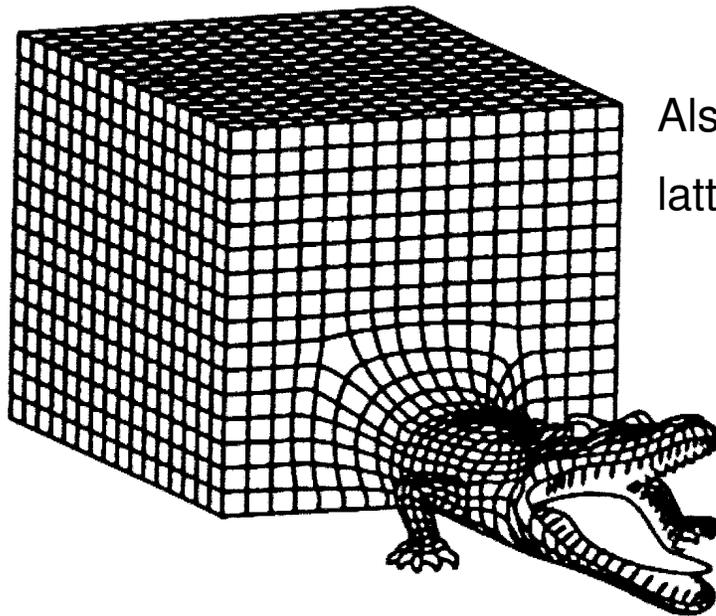
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- **Wish list for 2004/05 is ready: QCD thermodynamics on Teraflops computers**



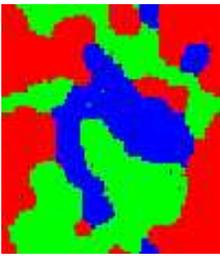
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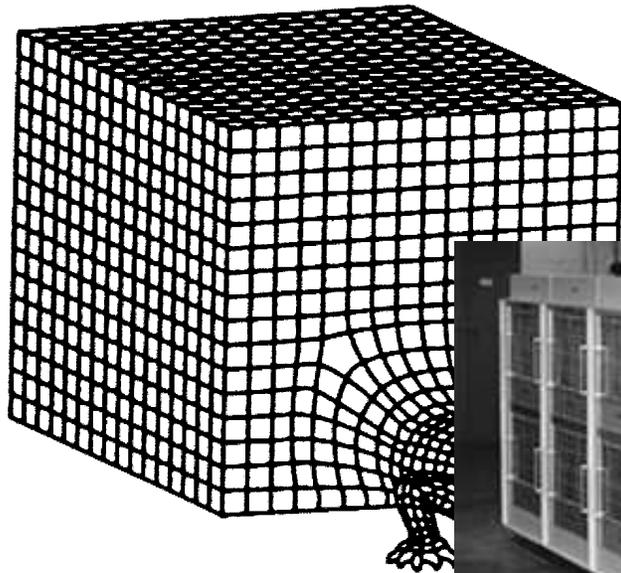


Also these calculations have to face the well-known lattice beasts: **ultra-violet** and **infra-red** problems



# Conclusions

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Also these calculations have to face the well-known lattice beasts: **ultra-violet** and **infra-red** problems



QCDOC and apeNEXT will take care of a large fraction of these problems