

# Lepton Universality and $\tau$ Lepton Mass Measurement

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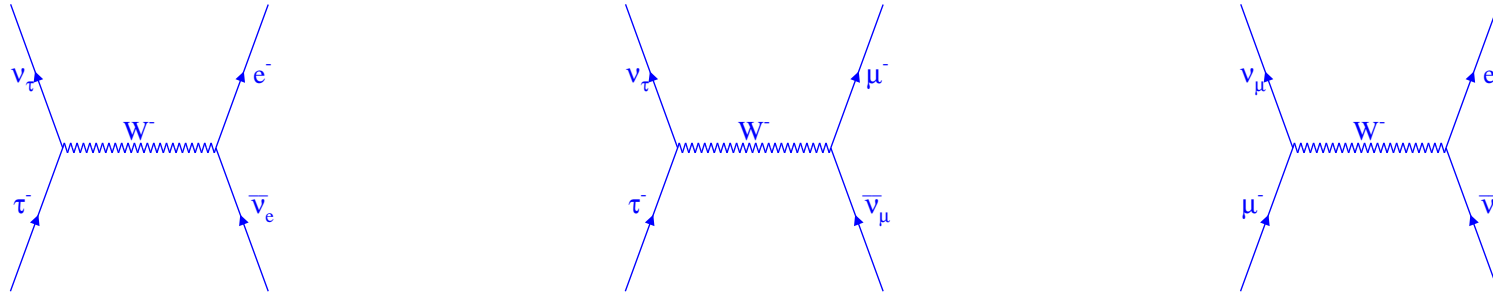
## Outline

1.  $\tau$  lepton and lepton universality
2.  $\tau$  mass at KEDR
3.  $\tau$  mass at Belle
4. Conclusions

## General

- During last two decades Standard Model (SM) successfully survived a lot of different tests
- First checked with electrons and muons, SM tests should also involve  $\tau$  leptons
- $\tau$  lepton may decay into both leptons and hadrons, we can study all interactions allowed in the SM and search for effects of New Physics
- One of the SM intrinsic features is flavor independence of the Fermi constant,  $G_F$
- B factories are a unique and extremely copious source of  $\tau^+\tau^-$  pairs providing about  $0.9 \times 10^6$  events per  $1 \text{ fb}^{-1}$

## Leptonic Universality in Leptonic Decays – I



$$\Gamma(L \rightarrow l\nu_L\bar{\nu}_l) = \frac{G_L^2 m_L^5}{192\pi^3} F_{\text{cor}}(m_L, m_l)$$

$$F_{\text{cor}}(m_L, m_l) = f(m_l^2/m_L^2) F_W F_{\text{rad}}$$

$$f(x) = 1 - 8x + 8x^3 - x^4 - 12x^2 \ln x$$

$$F_W = 1 + \frac{3}{5} \frac{m_l^2}{m_W^2}, \quad F_{\text{rad}} = 1 + \frac{\alpha(m_L)}{2\pi} \left( \frac{25}{4} - \pi^2 \right)$$

Lepton universality:  $G_e = G_\mu = G_\tau = G_F$

## Lepton Universality in Leptonic Decays – II

$$r = \left( \frac{G_\tau}{G_\mu} \right)^2 = \left( \frac{G(\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e)}{G(\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e)} \right)^2 = \left( \frac{m_\mu}{m_\tau} \right)^5 \left( \frac{t_\mu}{t_\tau} \right) \mathcal{B}(\tau \rightarrow e \nu_\tau \bar{\nu}_e) \frac{F_{\text{cor}}(m_\mu, m_e)}{F_{\text{cor}}(m_\tau, m_e)}$$

Correction	$\mu$	$\tau$
$f(m_e^2/m_L^2)$	0.9998	1.0000
$F_{\text{W}}(m_L)$	1.0000	1.0003
$F_{\text{rad}}(m_L)$	0.9958	0.9957
Total	0.99558	0.99597

Lepton universality  $\Rightarrow r = 1$

## Two Methods of $m_\tau$ Measurement

- Energy dependence of  $\sigma(e^+e^- \rightarrow \tau^+\tau^-)$  near threshold

$$\sigma_0 = \sigma(e^+e^- \rightarrow \tau^+\tau^-) = 86.85 \text{ (nb)}/s(\text{GeV}^2) \sqrt{1 - 4m_\tau^2/s} (1 + 2m_\tau^2/s).$$

First used by DELCO in 1978

- Pseudomass

Reconstruction of the invariant mass and energy of the hadronic system in hadronic  $\tau$  decays

Suggested and first used by ARGUS in 1992

## History of $m_\tau$ Measurements

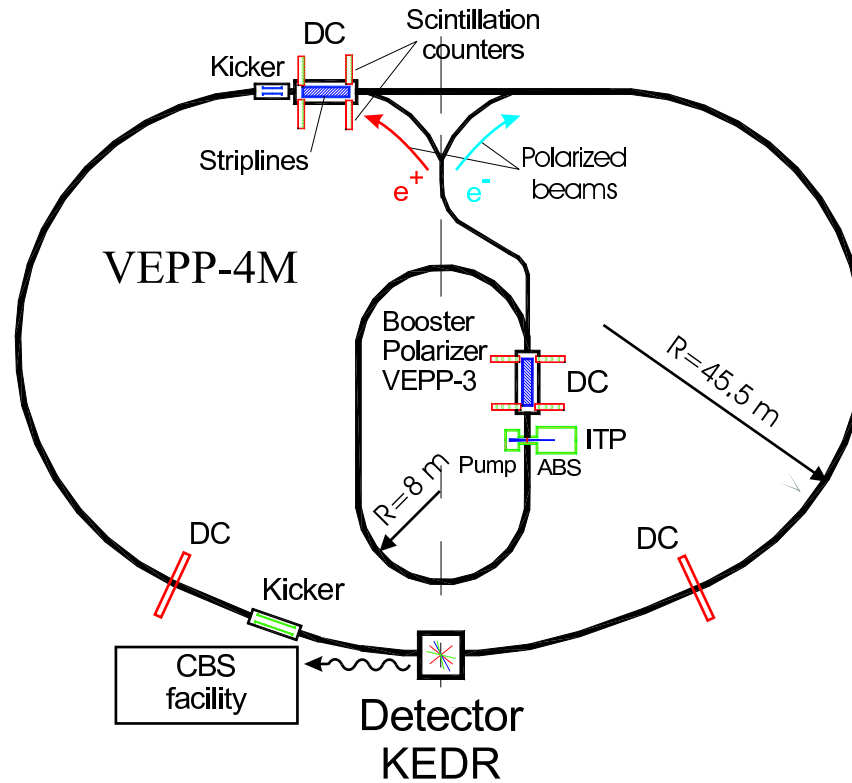
$m_\tau$ , MeV	$N_{ev}$	Group	$\sqrt{s}$ , GeV	Method
$1783_{-4}^{+3}$	692	DELCO, 1978	3.1 – 7.4	$\sigma$
$1776.3 \pm 2.4 \pm 1.4$	11 <i>k</i>	ARGUS, 1992	9.4 – 10.6	P/m
$1776.96_{-0.21-0.17}^{+0.18+0.25}$	65	BES, 1996	3.54 – 3.57	$\sigma$
$1778.2 \pm 0.8 \pm 1.2$	98.5 <i>k</i>	CLEO, 1997	10.6	P/m
$1775.1 \pm 1.6 \pm 1.0$	13.3 <i>k</i>	OPAL, 2000	$\sim 90$	P/m
$1776.99_{-0.26}^{+0.29}$		PDG, 2006		

## Test of Lepton Universality in Leptonic Decays

$$r = \left( \frac{G_\tau}{G_\mu} \right)^2$$

r	$t_\tau$ , fs	$\mathcal{B}(\tau \rightarrow e\nu_\tau\bar{\nu}_e)$ , %	$m_\tau$ , MeV	Comments
0.9405 $\pm 0.0249$	$305.6 \pm 6.0$ $\pm 0.0185$	$17.93 \pm 0.26$ $\pm 0.0136$	$1784.1^{+2.7}_{-3.6}$ $+0.0071$ $-0.0095$	PDG, 1992 $-2.4\sigma$
0.9999 $\pm 0.0069$	$291.0 \pm 1.5$ $\pm 0.0052$	$17.83 \pm 0.08$ $\pm 0.0045$	$1777.0^{+0.30}_{-0.27}$ $\pm 0.0008$	PDG, 1996 $-0.01\sigma$
1.0020 $\pm 0.0051$	$290.6 \pm 1.1$ $\pm 0.0038$	$17.84 \pm 0.06$ $\pm 0.0034$	$1776.99^{+0.29}_{-0.26}$ $\pm 0.0008$	PDG, 2004 $+0.4\sigma$

# VEPP-4M: General Layout





## Physics at VEPP-4M

- $\sqrt{s}$  from 2 to 11 GeV
- Originally designed for  $b$  quark physics  
is now running in the charmonium region
- $L_{\max} = 2 \times 10^{30} \text{ cm}^{-2}\text{s}^{-1}$  at 1.78 GeV
- Properties of  $\psi$  family states,  $2\gamma$  physics
- High-precision mass measurements ( $J/\psi$ ,  $\psi(2S)$ ,  $\tau$ ) based on two independent methods of energy determination:  
Resonant depolarization for absolute calibration (slow)  
Compton backscattering of laser 0.12 MeV photons (fast)

## Resonant Depolarization – I

Usual NMR based absolute energy determination –  $3 \cdot 10^{-4}$

Resonant depolarization suggested at BINP in 1975  
gives at least an order of magnitude better precision

In a storage ring with a flat orbit:

$$\Omega/\omega_0 = 1 + \gamma \cdot \mu'/\mu_0,$$

$\Omega$  – spin precession frequency,  $\omega_0$  – revolution frequency,  
 $\mu'/\mu_0$  – the ratio of the anomalous (normal) parts of emm known with an  
accuracy of  $10^{-9}$

The average  $\omega_0$  is determined by the RF frequency of the  
guiding field and can be set and determined with high accuracy

$\Omega$  is measured at the moment of depolarization  
by the external electromagnetic field with a frequency  $\omega_d$ :

$$\omega_d \pm \Omega = k\omega_0$$

## Resonant Depolarization – II

Since 1975 has been successfully used

to determine masses of various particles:

$K^\pm$ ,  $\omega$ ,  $\phi$ ,  $J/\psi$ ,  $\psi(2S)$ ,  $\Upsilon(3S)$  at BINP,

$\Upsilon(1S)$  at BINP and Cornell,  $\Upsilon(2S)$  at BINP and DESY,  $Z$  at CERN

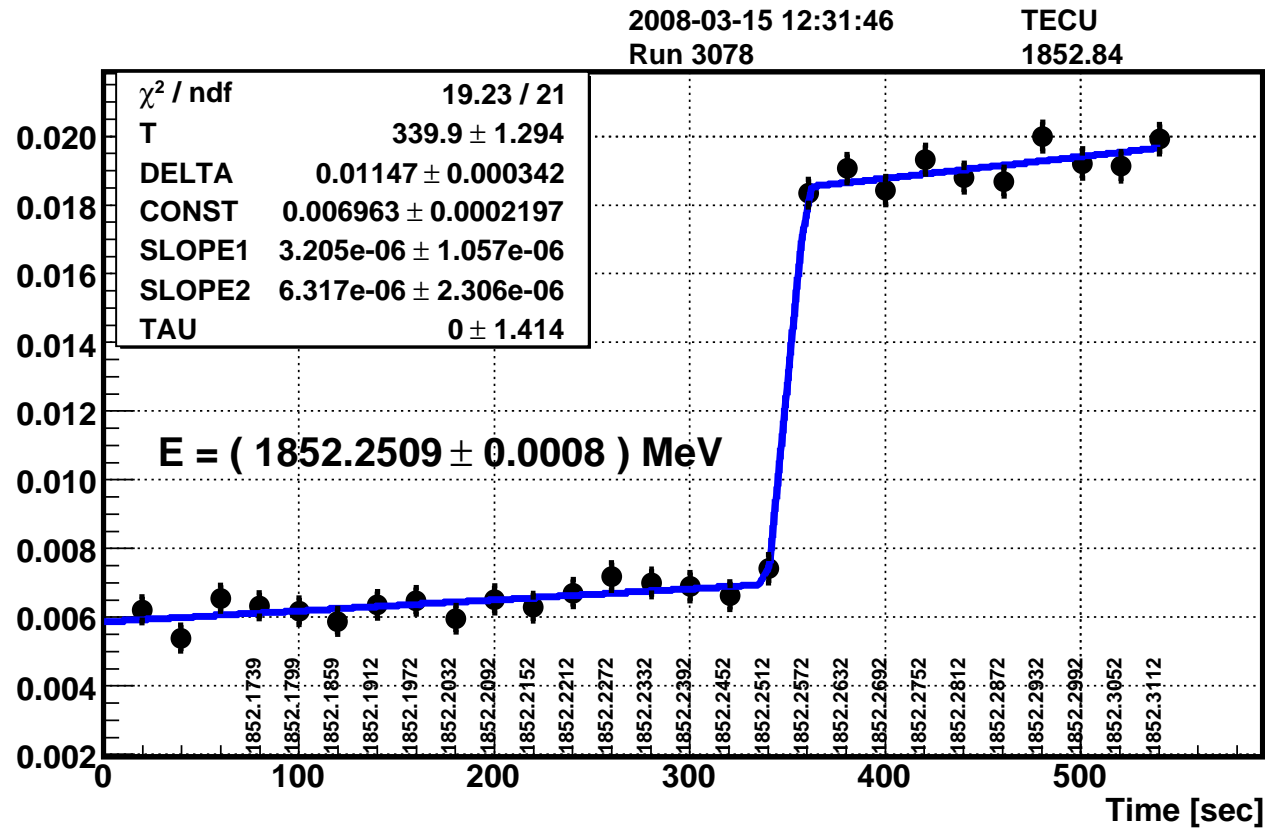
Also used at various SR facilities

State	Mass, MeV/ $c^2$	$\Delta m/m$	Factor
$\phi$	$1019.455 \pm 0.020$	$2.0 \cdot 10^{-5}$	25
$J/\psi$	$3096.916 \pm 0.011$	$3.6 \cdot 10^{-6}$	90
$\Upsilon(1S)$	$9460.30 \pm 0.26$	$2.7 \cdot 10^{-5}$	50
$Z$	$91187.6 \pm 2.1$	$2.3 \cdot 10^{-5}$	60

## Resonance Depolarization – III

- The beams get polarized at  $E_{\text{beam}} = 1772$  MeV, the polarization lifetime is  $\leq 1000$  s, the polarized beam is injected to VEPP-4M, 10 minutes later an unpolarized beam is added as a second bunch
- Touschek (intrabeam scattering) effect is used to detect the moment of depolarization; the cross section of polarized electrons is smaller than that for unpolarized particles
- The transverse wave with the magnetic field perpendicular to the polarization is used as a depolarizer, the depolarization time is about 2 s
- The counting rate of the polarimeter is 1 MHz at beam currents of 2-4 mA
- The process of RD energy calibration lasts about 2 hours and is performed once a day, more than 1500 calibrations were performed since 2002

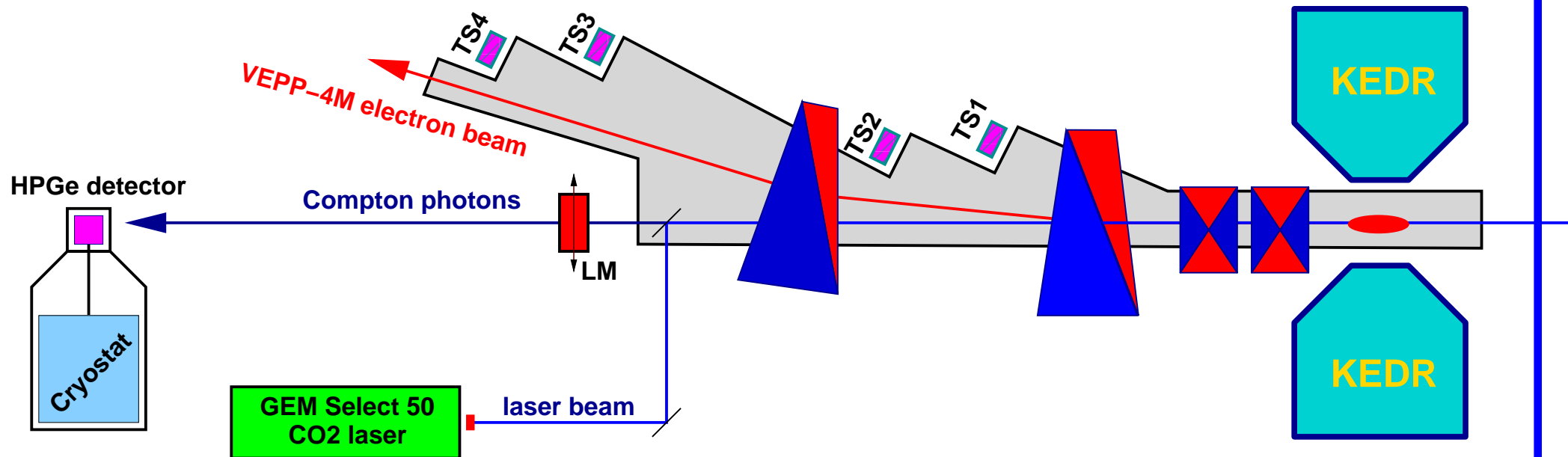
Typical RD Run at VEPP-4M



The resonant depolarization (RD) once a day with  $\sigma_E < 20 \text{ keV}$

## Compton Backscattering Monitor

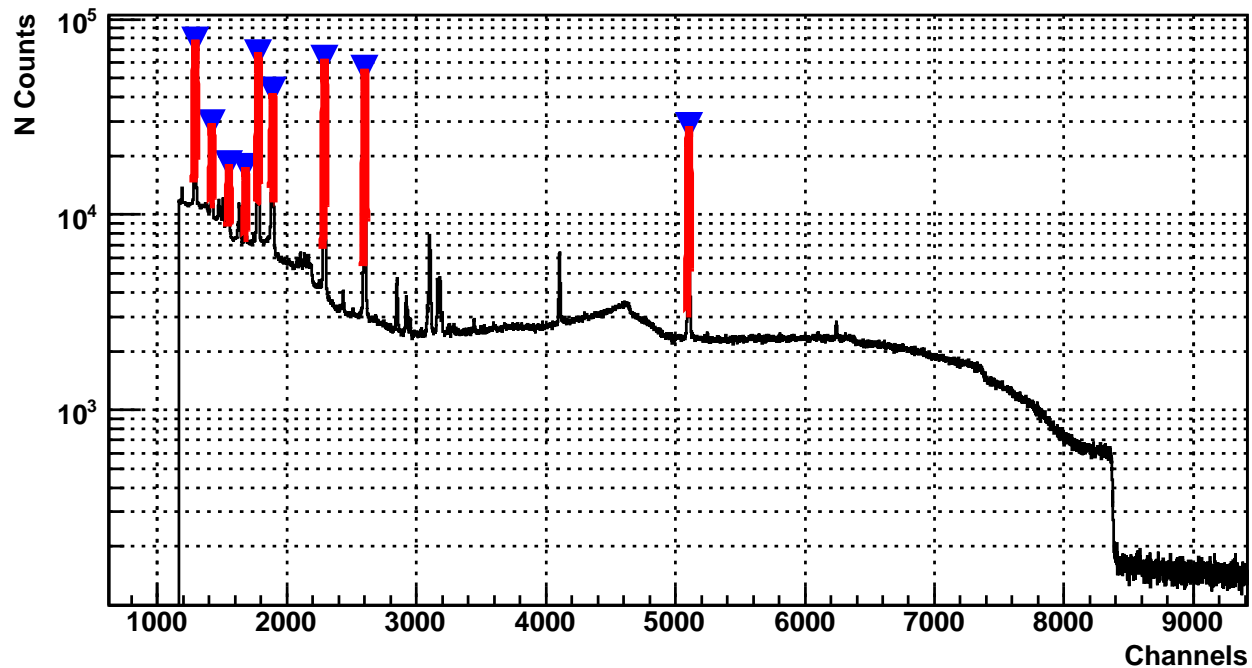
Realized at BESSY-I in 1987



A carbon dioxide laser is used,  $\lambda = 10.591 \mu\text{m}$  ( $\omega_0 = 0.117 \text{ eV}$ )

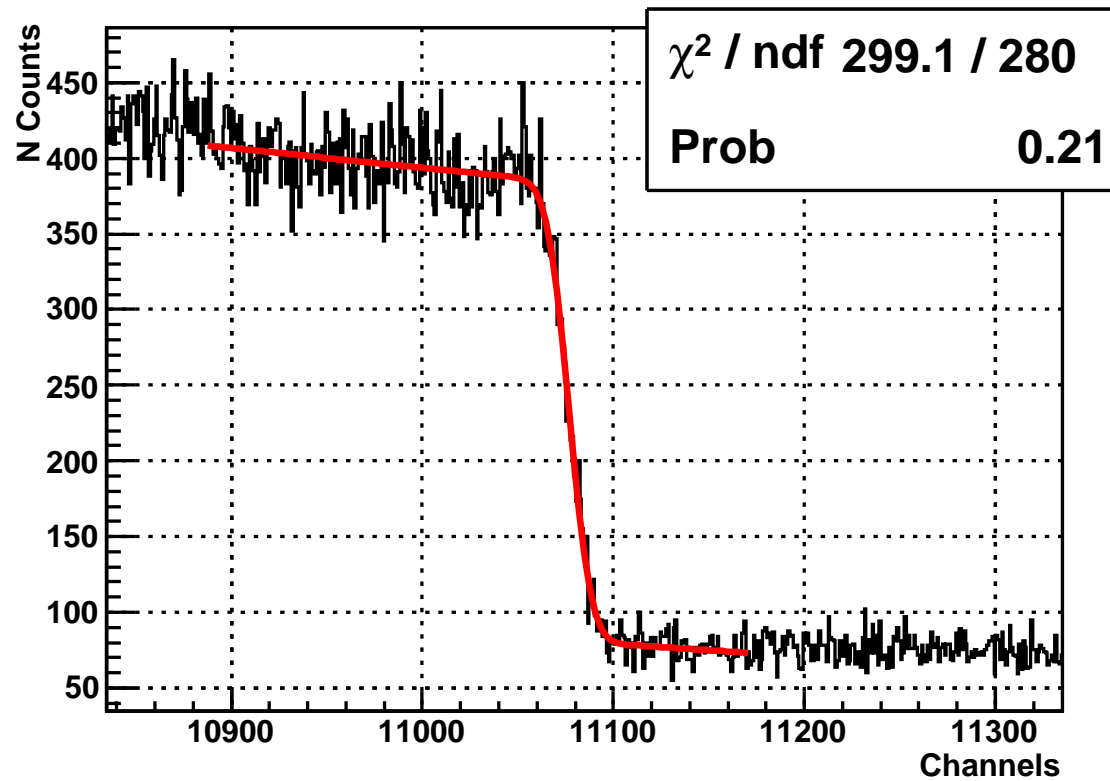
$\omega_{\text{max}} = 1\text{-}7 \text{ MeV}$ ,  $\Delta\omega_0/\omega_0 = 10^{-7}$ , cont. power of 30 W

## Spectrum of CBS Photons with Calibration Lines



A High Purity Germanium (HPG) detector,  $V_{\text{act}} = 120 \text{ cm}^3$ ,  $\epsilon = 5\%$  at 6 MeV,  
internal resolution  $(0.6 + 0.2\omega[\text{MeV}]) \text{ keV}$ , the pile-up noise is (1-3) keV  
HPG calibrated with  $\gamma$  sources in the 0.5-2.7 MeV range and extr. to  $\omega_{\text{max}}$

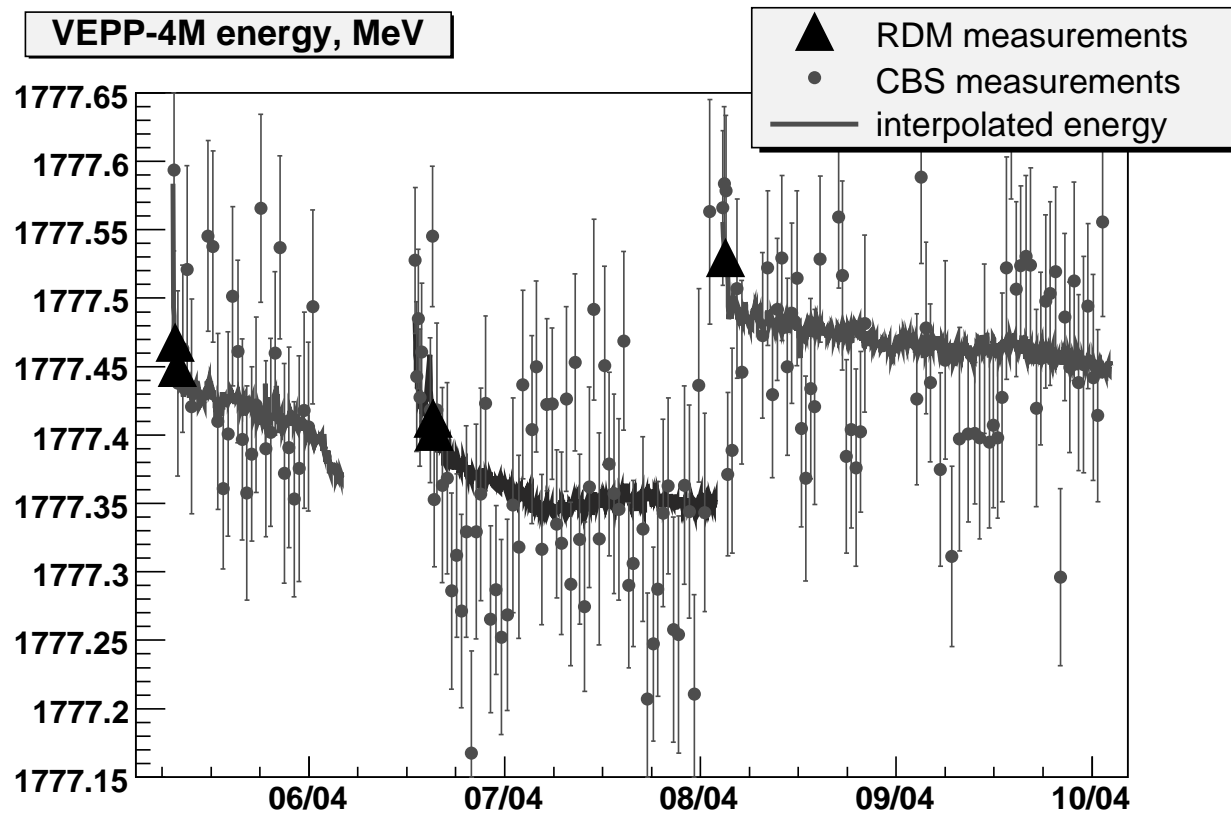
## Typical CBS Spectrum Edge at VEPP-4M



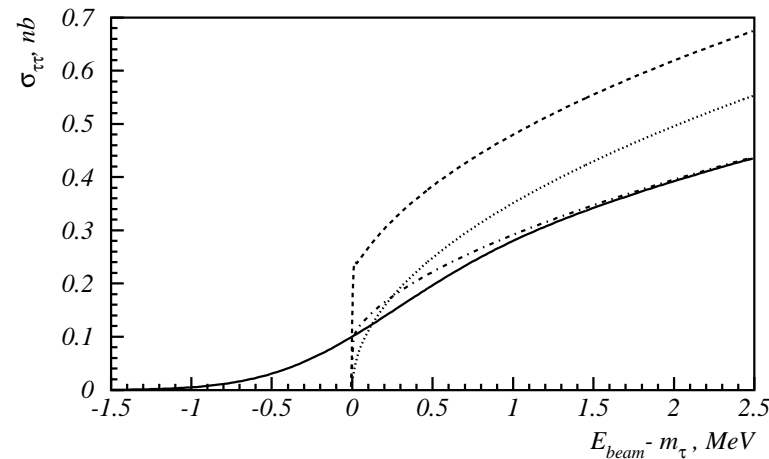
Between the RD, the Compton backscattering (CBS) with  $\sigma_E \approx 100$  keV



## VEPP-4M Energy Behaviour



During the run,  $E$  measured by CBS, then interpolation

$\sigma(e^+e^- \rightarrow \tau^+\tau^-)$  Near Threshold


$$\sigma(W) = \frac{1}{\sqrt{2\pi}\sigma_W} \int dW' \exp\left\{-\frac{(W-W')^2}{2\sigma_W^2}\right\} \int dx F(x, W') \sigma_{fs}(W' \sqrt{1-x}),$$

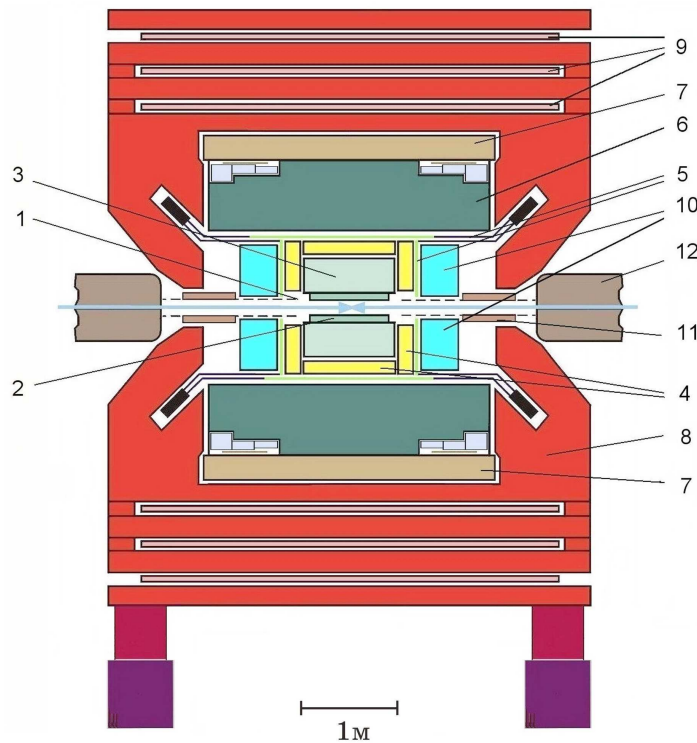
$$\sigma_{fs}(W) = \sigma_0(W) F_c(\beta) F_r(W) / |1 - \Pi(W)|^2$$

$$F_c(\beta) = (\pi\alpha/\beta) / (1 - \exp(-\pi\alpha/\beta)), \quad \beta = (1 - (2m_\tau/W)^2)^{1/2}$$

Dotted – Born, dashed – Coulomb, FSR and VP,

dash-dotted – ISR, solid – beam energy spread

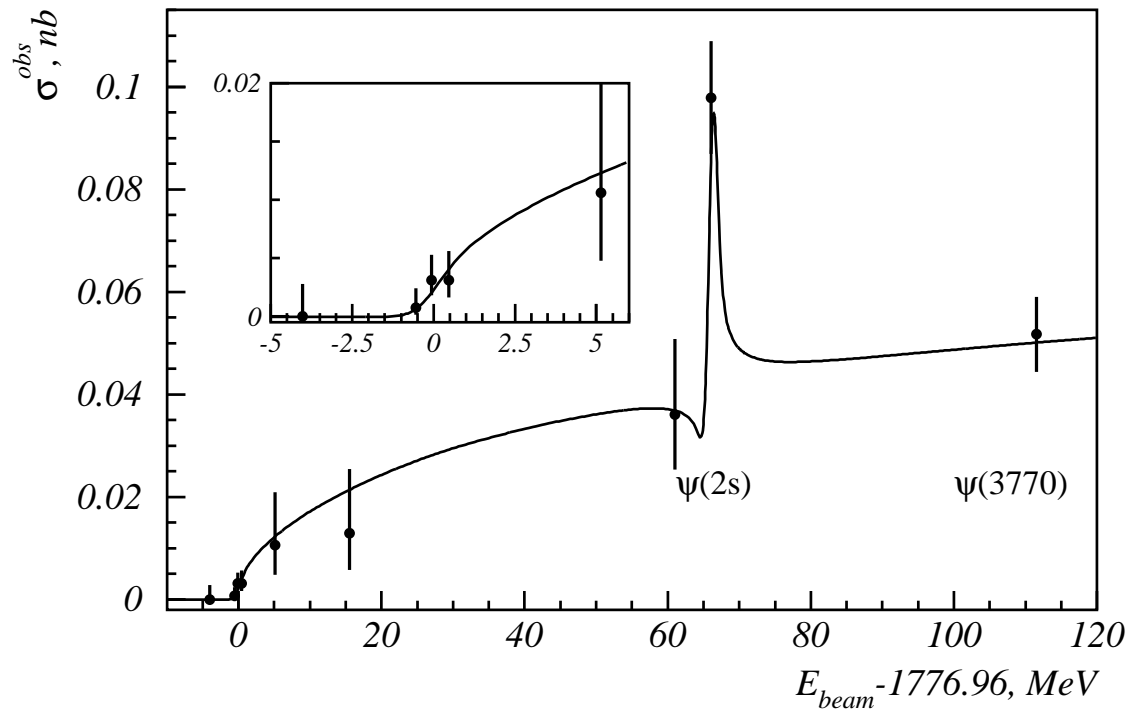
## KEDR Detector



- 1) Vacuum chamber, 2) Vertex detector,
- 3) Drift chamber, 4) Aerogel counters,
- 5) ToF-counters, 6) LKr calorimeter,
- 7) Superconducting coil, 8) Magnet yoke,
- 9) Muon tubes, 10) CsI calorimeter,
- 11) Compensation solenoid,
- 12) VEPP-4M quadrupole

$m_\tau$  at KEDR: Summary of the scan

Point	$\langle E \rangle$ , MeV	$\int Ldt$ , nb $^{-1}$	$N_{\tau\tau}$	$\sigma_{\tau\tau}^{\text{obs}}$ , pb
1	$1771.945 \pm 0.160$	668	0	$0.0_{-0.0}^{+2.8}$
2	$1776.408 \pm 0.086$	1382	1	$0.7_{-0.6}^{+1.7}$
3	$1776.896 \pm 0.045$	1605	6	$3.7_{-1.5}^{+2.2}$
4	$1777.419 \pm 0.061$	1288	4	$3.1_{-1.5}^{+2.5}$
5	$1782.103 \pm 0.060$	283	4	$14.1_{-6.8}^{+11.3}$
6	$1792.457 \pm 0.102$	233	3	$12.9_{-7.1}^{+12.5}$
7	$1837.994 \pm 0.092$	305	14	$45.8_{-12.2}^{+16.0}$
8	$1843.040 \pm 0.065$	807	79	$97.9 \pm 11.0$
9	$1888.521 \pm 0.228$	967	49	$50.7 \pm 7.2$
Total	Without $\psi(2S)$	6731	81	

$m_\tau$  at KEDR: Observed  $\sigma(e^+e^- \rightarrow \tau^+\tau^-)$ 


$\int L dt = 6.7 \text{ pb}^{-1}$ , 81 events selected

$m_\tau = 1776.81_{-0.23}^{+0.25} \text{ MeV}/c^2$ ,  $\epsilon = (2.25 \pm 0.28)\%$ ,  $\sigma_B = 0_{-0.00}^{+0.58} \text{ pb}$ .

$m_\tau$  at KEDR: Systematic Uncertainties – I

- Interpolation takes into account guiding field measurements, ring and tunnel temperature variations – 40 keV
- Detector efficiency variations (MC model, selection criteria, performance of subsystems) – 100 keV
- Beam energy spread (from  $\sigma_W(J/\psi)$  and  $\sigma_W(\psi(2S))$  and assuming linear growth  $\sigma_W(2m_\tau) = (1.07 \pm 0.02 \pm 0.04)$  MeV) – 25 keV
- Background (variation of shape, possible energy dependence) – 20 keV
- Instability of luminosity measurement (comparison of LKr and CsI) – 90 keV
- Calculation of  $\sigma(e^+e^- \rightarrow \tau^+\tau^-)$  (rad. corrections, interference) – 30 keV

$m_\tau$  at KEDR: Systematic Uncertainties – II

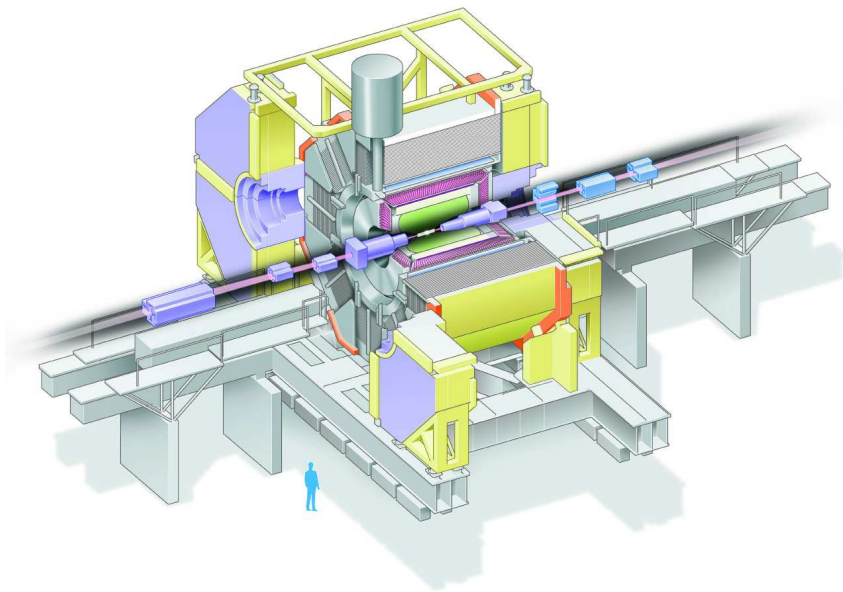
Source	$\sigma$ , keV/ $c^2$
Beam energy	40
Detection efficiency	100
Energy spread accuracy	25
BG energy dependence	20
Luminosity measurement	90
Energy spread variation	15
Cross section	30
Total	150

$$m_\tau = 1776.81_{-0.23}^{+0.25} \pm 0.15 \text{ MeV}/c^2$$

V.V. Anashin et al., JETP Letters 85, 347 (2007)

## KEKB and Belle Detector

- $3.5 \text{ GeV } e^+ \times 8.0 \text{ GeV } e^-$
- $\mathcal{L}_{\text{max}} = 1.71 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- Continuous injection  $\rightarrow 1.2 \text{ fb}^{-1}/\text{day}$
- $\int \mathcal{L} dt \approx 852 \text{ fb}^{-1}$

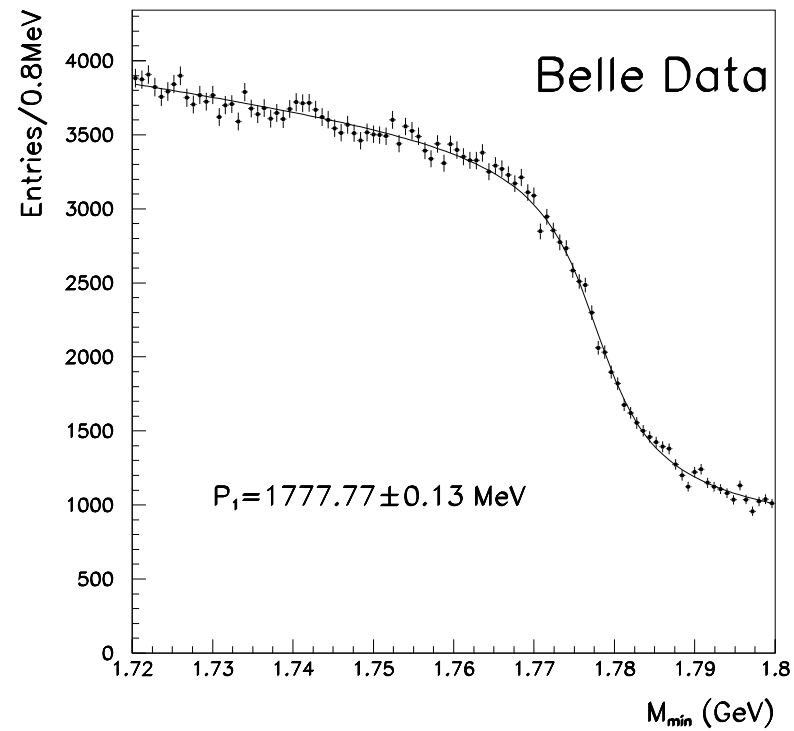


- Sil.VD: 3(4) layers DSSD
- CDC : small cells  $He + C_2H_6$
- TOF counters
- Aerogel CC:  $n = 1.015 \sim 1.030$
- CsI(Tl)  $16 X_0$
- SC solenoid 1.5 T
- $\mu K_L$  detection 14-15 layers RPC+Fe

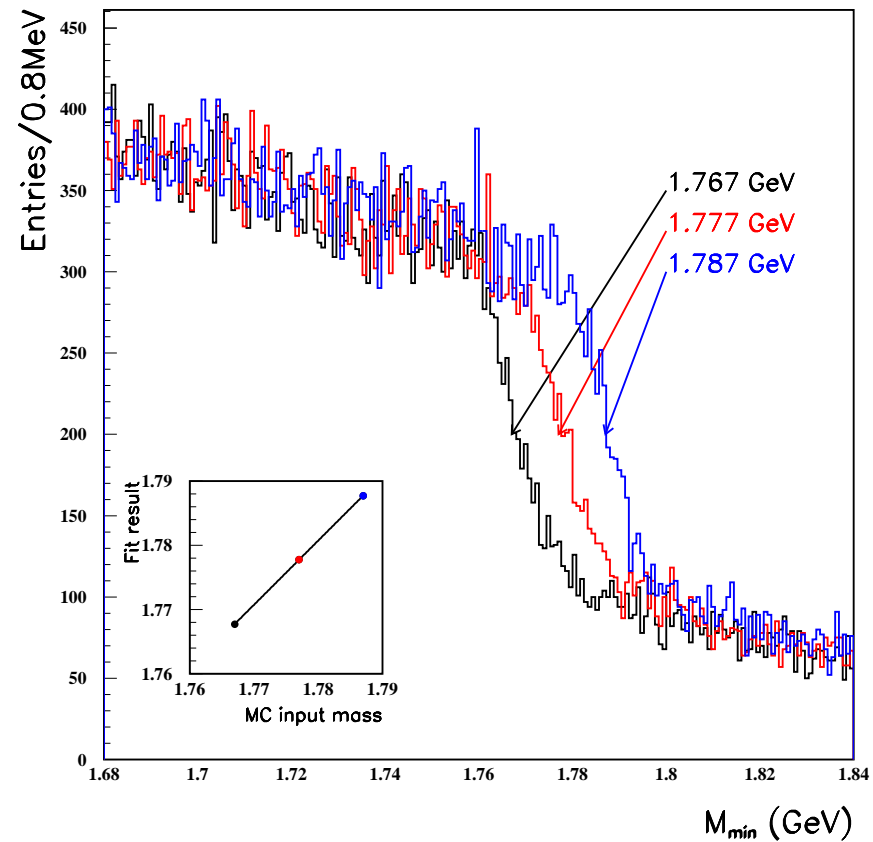


## $m_\tau$ at Belle: Pseudomass

- $414 \text{ fb}^{-1}$  or  $370 \times 10^6 \tau^+ \tau^-$  pairs
- $\sim 5.8 \cdot 10^6$  events  $\tau^- \rightarrow \pi^+ \pi^- \pi^- \nu_\tau$
- $p_\tau = p_X + p_\nu \Rightarrow m_X^2 + m_\nu^2 + 2(E_X E_\nu - |\vec{p}_X| |\vec{p}_\nu| \cos\theta)$
- $m_\nu = 0, |\vec{p}_\nu| = E_\nu = E_\tau - E_X$   
 $m_\tau^2 = m_X^2 + 2(E_\tau - E_X)(E_X - |\vec{p}_X| \cos\theta)$   
 $m_\tau^2 \geq m_{\min}^2 = m_X^2 + 2(E_{\text{beam}} - E_X)(E_X - |\vec{p}_X|).$
- The empirical edge function:  
 $f(m_{\min}) \sim (a_1 + a_2 m_{\min}) \tan^{-1} (m_{\min} - a_3) / a_4 + a_5 + a_6 m_{\min}$   
 $a_3$  is a  $\tau$  mass estimator

$m_\tau$  at Belle: Data

$$m_\tau = (1776.61 \pm 0.13) \text{ MeV}$$

$m_\tau$  at Belle: Monte Carlo

$$\Delta m_\tau = (1.16 \pm 0.14) \text{ MeV}$$

## $m_\tau$ at Belle: Systematic Uncertainties – I

- $E_{\text{beam}}$  is calibrated run by run using the beam-energy constrained mass of reconstructed  $B$  mesons. Its uncertainty of 1.5 MeV ( $\Delta m_B$ , tracking,  $\Gamma_{\Upsilon(4S)}$ ) gives  $\Delta m_\tau = 0.26$  MeV
- Momentum resolution (comparing MC and data on  $e^+e^- \rightarrow \mu^+\mu^-$ ) – 0.02 MeV
- Choice of the edge parameterization gives 0.18 MeV:
 
$$f_1(m_{\min}) = (a_1 + a_2 m_{\min}) \frac{m_{\min} - a_3}{\sqrt{a_2 + (m_{\min} - a_1)^2}} + a_5 + a_6 m_{\min},$$

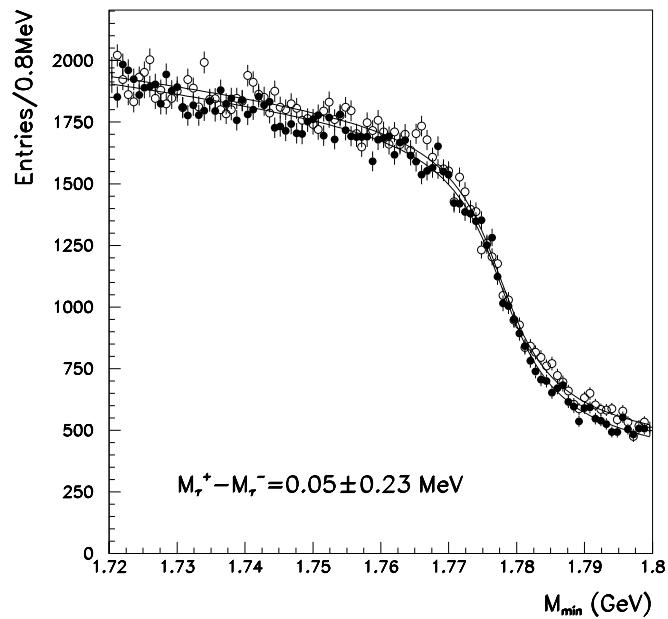
$$f_2(m_{\min}) = (a_1 + a_2 m_{\min}) \frac{-1}{1 + \exp[(m_{\min} - a_3)/a_4]} + a_5 + a_6 m_{\min}$$
- Variation of the fit range (1.72 – 1.80) GeV gives a shift of 0.04 MeV
- Variation of  $m_{a_1}$  and  $\Gamma_{a_1}$  in the  $\pm 300$  MeV range:  
model dependence of the  $3\pi$  spectrum yields a shift  $< 0.02$  MeV
- Backgrounds (misID  $\tau$  decay, non- $\tau^+\tau^-$ , ISR/FSR)  $\Rightarrow$  a shift  $< 0.01$  MeV
- A change of  $m_\nu$  from 0 to 10 MeV gives a shift by -0.1 MeV

$m_\tau$  at Belle: Systematic Uncertainties – II

Source	$\sigma$ , MeV/ $c^2$
Beam energy and tracking	0.26
Edge parameterization	0.18
MC statistics	0.14
Fit range	0.04
Momentum resolution	0.02
Model of $\tau \rightarrow 3\pi\nu_\tau$	0.02
Background	0.01
Total	0.35

$$m_\tau = (1776.61 \pm 0.13 \pm 0.35) \text{ MeV}$$

## $m_{\tau^+}$ and $m_{\tau^-}$ at Belle



CPT test by  $m_{\tau^+}$  vs.  $m_{\tau^-}$ :

$$\Delta m = m_{\tau^+} - m_{\tau^-} = 0.05 \pm 0.23 \pm 0.14 \text{ MeV}$$

Group	OPAL, 2000	Belle, 2006
$N_{\tau^+\tau^-}, 10^3$	160	370k
$ \Delta m /m_\tau$	$< 3.0 \times 10^{-3}$	$< 2.8 \times 10^{-4}$

K. Belous et al., Phys. Rev. Lett. 99, 011801 (2007)

Progress of  $m_\tau$ 

Group	$m_\tau$ , MeV
BES, 1996	$1776.96^{+0.18+0.25}_{-0.21-0.17}$
PDG, 2006	$1776.99^{+0.29}_{-0.26}$
KEDR, 2006	$1776.81^{+0.25}_{-0.23} \pm 0.15$
Belle, 2006	$1776.61 \pm 0.13 \pm 0.35$
PDG, 2008	$1776.84 \pm 0.17$

KEDR continues running to increase a data sample and decrease systematics

Belle has the best statistical error, but limited by systematic effects

$m_\tau$  at KEDR: 2008 preliminary

Year	2006	2008
$\int Ldt, \text{pb}^{-1}$	6.7	14.3
$N_{\text{ev}}$ at thr.	11	26
$m_\tau, \text{MeV}$	$1776.81^{+0.25}_{-0.23} \pm 0.15$	$1776.69^{+0.17}_{-0.19} \pm 0.15$

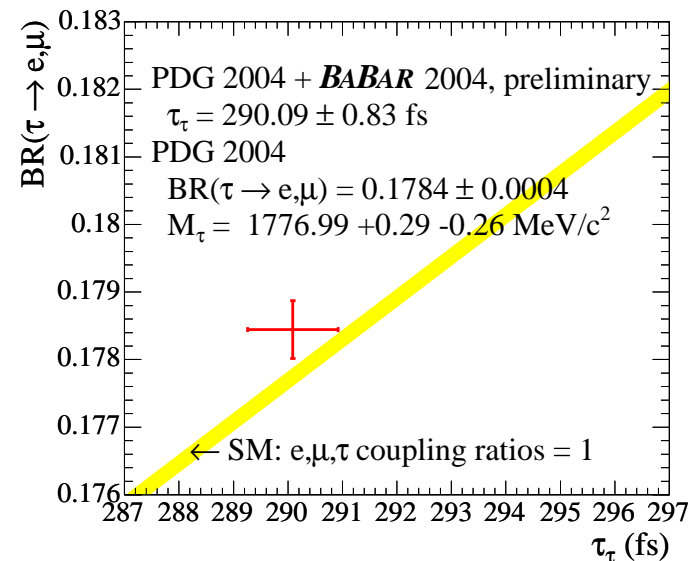
The goal is to reach a total error of 0.15 MeV



## τ Lepton Lifetime

Source	$N_{\tau\tau}, 10^3$	$\tau_\tau, \text{fs}$	$\delta\tau_{\tau\text{sys}}, \%$
DELPHI, 2004	150	$290.9 \pm 1.4 \pm 1.0$	0.34
PDG, 2008	–	$290.6 \pm 1.0$	0.28
BaBar, 2004	79000	$289.40 \pm 0.91 \pm 0.90$	0.31

- Measurement bias – 0.220%
- Background – 0.142%
- Alignment – 0.111%
- τ momentum – 0.100%
- Total – 0.310%



We can hopefully expect improvement in  $\tau_\tau$  from LHC

## τ Leptonic Branching

Measurements of  $B_e$ , %

Source	$N_{\tau\tau}, 10^3$	$B, \%$	$\delta B_{\text{sys}}, \%$
ALEPH, 2005	56	$17.837 \pm 0.072 \pm 0.036$	0.2
CLEO, 1997	3250	$17.76 \pm 0.06 \pm 0.17$	1.0
PDG, 2008	—	$17.85 \pm 0.05$	0.28

Systematic uncertainties in CLEO, %

$N_{\text{ev}}$	$N_{\tau\tau}$	$\epsilon$	Trig.	PID	BG	Total
0.36	0.71	0.48	0.28	0.19	0.16	1.00

## 2008 Test of Lepton Universality

- After 23 years the MuLan group at PSI recently improved the  $\mu^+$  lifetime by a factor of 3.5 (D.B. Chitwood et al., Phys. Rev. Lett. 99, 032001 (2007)).  
The improved PDG-08  $\tau_\mu = (2.197019 \pm 0.000021) \mu\text{s}$
- The unchanged PDG-08  $B_e = (17.85 \pm 0.05)\%$
- The unchanged PDG-08  $\tau_\tau = (290.6 \pm 1.0) \text{ fs}$
- The improved PDG-08  $m_\tau = (1776.84 \pm 0.17) \text{ MeV}$
- $r = 1.0030 \pm 0.0045 (0.67\sigma) \Rightarrow$  Leptonic universality is OK!

## Do We Need a Higher $m_\tau$ Precision?

- We should know masses of fundamental particles with high precision

Particle	Mass, MeV	$\sigma_m/m$
$e$	$0.510998910 \pm 0.000000013$	$2.5 \cdot 10^{-8}$
$\mu$	$105.6583668 \pm 0.0000038$	$3.6 \cdot 10^{-7}$
$\tau$	$1776.84 \pm 0.17$	$9.6 \cdot 10^{-5}$

- Is 1981 Koide formula pure numerology?

$$\frac{(\sqrt{m_e} + \sqrt{m_\mu} + \sqrt{m_\tau})^2}{(m_e + m_\mu + m_\tau)} = 1.4999973^{+0.0000395}_{-0.0000304}$$

## Lepton Universality in Hadronic Decays – I

$$\Gamma(\tau \rightarrow \pi \nu_\tau) = \frac{G_F^2 f_\pi^2 \cos^2 \theta_C}{16\pi} m_\tau^3 (1 - m_\pi^2/m_\tau^2)^2,$$

$$\Gamma(\pi \rightarrow \mu \nu_\mu) = \frac{G_F^2 f_\pi^2 \cos^2 \theta_C}{8\pi} m_\pi m_\mu^2 (1 - m_\mu^2/m_\pi^2)^2$$

$$\frac{\mathcal{B}(\tau \rightarrow \pi \nu_\tau)}{\mathcal{B}(\pi \rightarrow \mu \nu_\mu)} = \frac{m_\tau^3 (1 - m_\pi^2/m_\tau^2)^2}{2m_\pi m_\mu^2 (1 - m_\mu^2/m_\pi^2)^2} \frac{\tau_\tau}{\tau_\pi}$$

## Lepton Universality in Hadronic Decays – II

For  $\Gamma(\tau \rightarrow K\nu_\tau)$  similarly, but  $f_\pi \rightarrow f_K$  and  $\cos\theta_C \rightarrow \sin\theta_C$ :

$$\frac{\mathcal{B}(\tau \rightarrow K\nu_\tau)}{\mathcal{B}(K \rightarrow \mu\nu_\mu)} = \frac{m_\tau^3 (1 - m_K^2/m_\tau^2)^2}{2m_K m_\mu^2 (1 - m_\mu^2/m_K^2)^2} \frac{\tau_\tau}{\tau_K}$$

Mode	$\mathcal{B}^{(\text{th})}$	$\mathcal{B}^{(\text{exp})}$
$\tau \rightarrow \pi\nu_\tau$	$(10.87 \pm 0.05)\%$	$(11.08 \pm 0.13)\%$
$\tau \rightarrow K\nu_\tau$	$(7.08 \pm 0.04) \cdot 10^{-3}$	$(7.1 \pm 0.5) \cdot 10^{-3}$

## Charged Current Universality – I

A. Pich, April 2008:

$$|G_\mu/G_e|$$

$\mathcal{B}(\tau \rightarrow \mu)/\mathcal{B}(\tau \rightarrow e)$	$1.0000 \pm 0.0020$
$\mathcal{B}(\pi \rightarrow \mu)/\mathcal{B}(\pi \rightarrow e)$	$1.0021 \pm 0.0016$
$\mathcal{B}(K \rightarrow \mu)/\mathcal{B}(K \rightarrow e)$	$1.004 \pm 0.007$
$\mathcal{B}(K \rightarrow \pi\mu)/\mathcal{B}(K \rightarrow \pi e)$	$1.002 \pm 0.002$
$\mathcal{B}(W \rightarrow \mu)/\mathcal{B}(W \rightarrow e)$	$0.997 \pm 0.010$

## Charged Current Universality – II

$$|G_\tau/G_e|$$

$\mathcal{B}(\tau \rightarrow \mu)\tau_\mu/\tau_\tau$	$1.0005 \pm 0.0023$
$\mathcal{B}(W \rightarrow \tau)/\mathcal{B}(W \rightarrow e)$	$1.036 \pm 0.014$

$$|G_\tau/G_\mu|$$

$\mathcal{B}(\tau \rightarrow e)\tau_\mu/\tau_\tau$	$1.0006 \pm 0.0022$
$\Gamma(\tau \rightarrow \pi)/\Gamma(\pi \rightarrow \mu)$	$0.996 \pm 0.005$
$\Gamma(\tau \rightarrow K)/\Gamma(K \rightarrow \mu)$	$0.979 \pm 0.017$
$\mathcal{B}(W \rightarrow \tau)/\mathcal{B}(W \rightarrow \mu)$	$1.039 \pm 0.013$



## Conclusions

- Better accuracy of  $m_\tau$  after KEDR and Belle measurements
- $|G_\tau/G_\mu|$  improved
- Further progress impossible without improving  $\tau_\tau$  and  $\mathcal{B}(\tau^- \rightarrow e^- \nu_\tau \bar{\nu}_e)$
- Universality of charged current checked using  $\tau$ ,  $\pi$ ,  $K$  and  $W$  decays  
 $\Gamma(W \rightarrow \tau)$  too big?
- Tests with  $\tau$  are among the most precise,  $B$  factories help

Backup Slides

## τ Lepton Factories

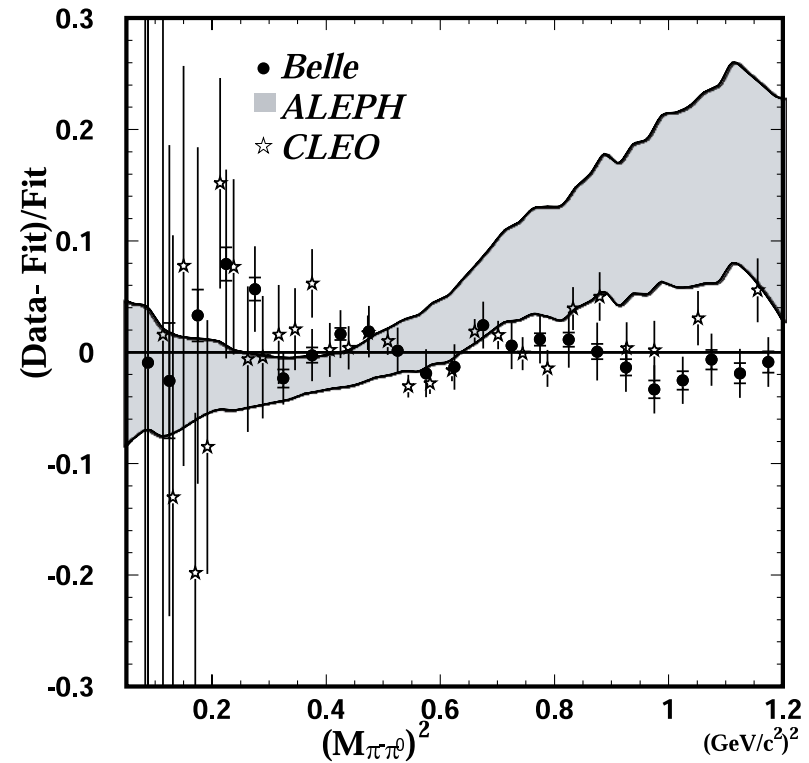
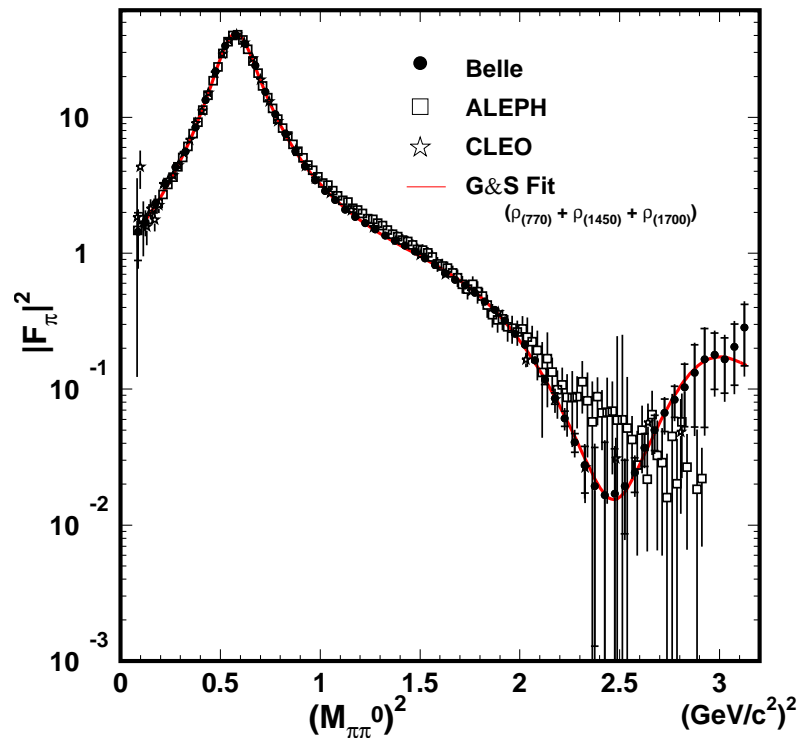
Group	$\int L dt, \text{fb}^{-1}$	$N_{\tau\tau}, 10^6$
LEP (Z-peak)	0.34	0.33
CLEO (10.6 GeV)	13.8	12.6
BaBar (10.6 GeV)	384	350
Belle (10.6 GeV)	543	490
τ-c (4.2 GeV)	10	32
SuperB	50k	45k

BaBar ( $\sim 530 \text{ fb}^{-1}$ ) and Belle ( $\sim 850 \text{ fb}^{-1}$ ) collected together about  $1.4 \text{ ab}^{-1}$

B-factory is also a τ factory producing  $0.9 \cdot 10^6 \tau^+\tau^-$  pairs per each  $\text{fb}^{-1}$ !!

## New data on $\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$ from Belle

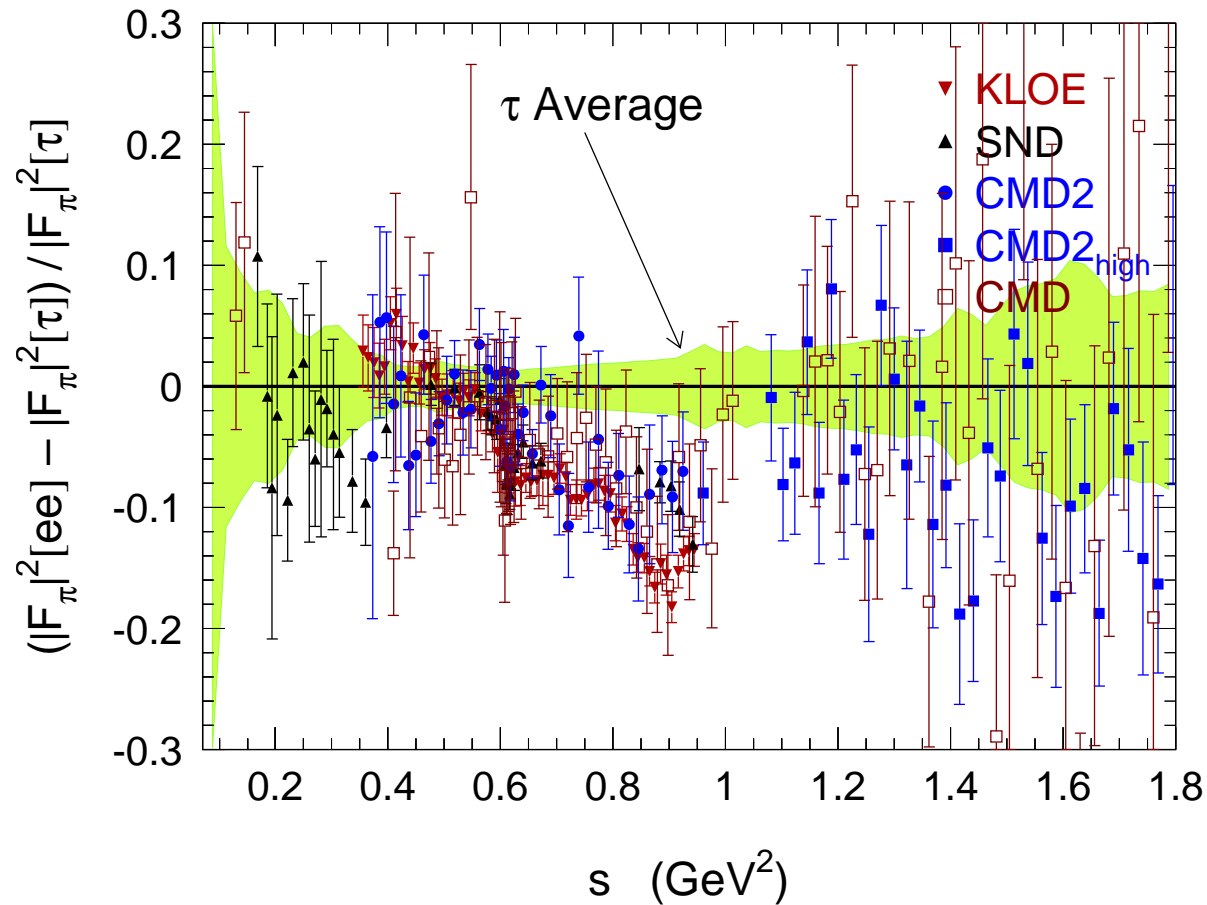
From 64M  $\tau^+ \tau^-$  pairs Belle selects 5.5M  $\tau^- \rightarrow h^- \pi^0 \nu_\tau$  events!



$$\mathcal{B}_{\text{Belle}} = (25.15 \pm 0.04 \pm 0.40)\%$$

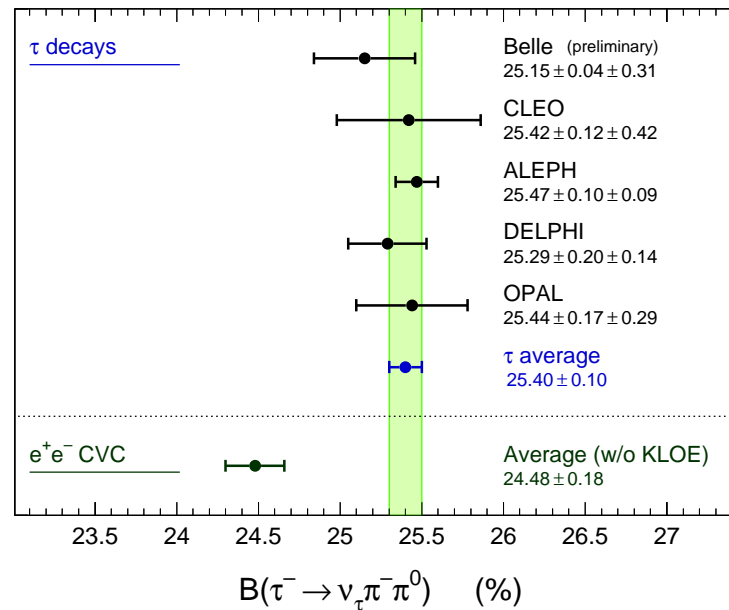
$$\mathcal{B}_{\text{ALEPH}} = (25.471 \pm 0.097 \pm 0.085)\%$$

The contributions to  $a_\mu^{\text{had}}$  are also compatible due to compensation at tails

CVC in the  $2\pi$  Channel.  $e^+e^-$  vs.  $\tau$  (Spectra)

Above the  $\rho$  meson  $e^+e^-$  spectral functions are lower than in  $\tau$  decays

## CVC in the $2\pi$ Channel. $e^+e^-$ vs. $\tau$ (Branchings)



The branching from all groups is systematically higher than the CVC prediction:  
 $\mathcal{B}_\tau - \mathcal{B}_{e^+e^-} = (0.92 \pm 0.21)\%$  or  $4.5\sigma$  from 0. The discrepancy is a 3.6% effect, about twice the SU(2) correction. The puzzle remains unsolved  $\Rightarrow$   $\tau$  data not used

M. Benayoun, arXiv:0711.4482: no conflict with consistent SU(2) breaking

## Theory vs Experiment – I

Contribution	$a_\mu, 10^{-10}$
Experiment	$11659208.0 \pm 6.3$
QED	$11658471.8 \pm 0.016$
Electroweak	$15.4 \pm 0.1 \pm 0.2$
Hadronic	$693.1 \pm 5.6$
Theory	$11659180.3 \pm 5.6$
Exp.–Theory	$27.7 \pm 8.4 (3.3\sigma)$

The difference between experiment and theory is  $3.3\sigma$ !  
(K.Hagiwara et al., PLB 649,173(2007)) claim even  $3.4\sigma$   
while F.Jegerlehner,2008 –  $2.8\sigma$ )

## Theory vs Experiment – II

